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TREATISE

ON
COMMERCIAL ARITHMETLC .
TO WHICH ARE $\triangle D D E D$
PRAC'ICAL COURSES ON
MENSURATIION AND BOOK-KEEPING
LESIGNED FOR
HIGH SCHOOLS AND ACADEMISS
By The Christian Brothers.

Sanctioned by the Council of Public Instruction.

## QA 103 F7Is

Entered, according to Act of the Parliament of Canada, in the year one thousand eight hundred and seventy-two, by Ephrem Gifgnon, in the office of the Minister of Agriculture.

## 

 ply our High Schacks athl Academies in the Dowinion of Canada, with a moderate-sized book containing sufficiently developpeal and practical Treatises on Commercial Arithenote, Memsuration, and Book-keeping, saving, thereby, to formhes, the expense of several text-books, and phaching the study of these branches within the reach of dat laborng classes.
As decimals follow the same scale as whole numbers, we have chosen to theat them along with the latter; therefore, they will beffotind introduced in numeration.
Though we have system, yet, the ald method has not been neglected.
Amongst its variaher particular features, this work offers the importand advantage of proposing a far greater number of patatical questions than any other of the same size. We we also contident that students will find in it ath the indformations requisite to qualify them for the position of accountants or business men.
Some personf predey to have the answers pleced
merous examples of application, having for proncipal object to render the pupil familiar with figures.

Some desire the answers placed immediately after the examples, and others desire them omitted. Both methods have their advantages and their disad vantages. In order, therefore, that pupils may receive the advantages of both methods, the answers to nearly one third of the examples in this book are omitted. They will be found, together with elear solutions ol ail the examples, in a Key to this work, prepared for the use of teachers and private learners.

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Rule for Decimals. Applicati mera Addition.

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1. What ando or qu wabe abstrac

## COMMERCLAL ARITHMETIC

## DEFINITIONS.

1. Arichmetic is the science of numbers.
2. A Number is a unit, or a colleotion of unit
3. A Unit is one, or a aingle thing.
4. Magnitude, or Quantity, is any thing that will admit of increase or decrease.

4 bis. An Integral Number, or Integer, is a whole number; as three, eight dollars, tioenty horses.
5. Any quantity less than the unit, is a Fractional Number, or a Fraction ; as $\frac{1}{2}, \frac{2}{3}$ of a foot.
6. Numbers, in general, are either abstract or congrete.
7. Abstract Numbers are numbers used without roference
to any particular thing or quantity. Thus, five, seven, fifteen.

- They are divided into three clasoes:
lis. Those which are not accompanied with subdivisions, as four, eight, \&o. : they are called abstract integral numbers.
2nd. Those which are accompanied with decimal subdivisions as three units fifteen hundredths, -six units tuo hundred twenty-five thousandths: they are called abstract decimal numbers.
:irl. And lastly, those which contain cinly decimal subdivisions, an forty humdredths,-seventy-fice thousandiths: they are called ab. stract decimal fractions, or si:nply decimals.
\$. Concrete Numbers are numbers used with reference to some particular thing or quantity. Thus, seven dollars, sime
yards.

[^0]They are also subdivided into threv classes:
1st. Those which contain no subdivisions, as six yards, eleven pounds.
2nd. Those which are aecompanied with decinal subdivisions, as five dollars twenty-five cents.

3rd. And lastly, those which contain decimal sutulivi ions only, as twenty-five cents ( $\$ 0.25$ ).
©. A Simple Number is either an abstract or a concrete number of but one denomination; as, tioo, ten dollars, fifteen hats.
10. A Compound Number is a collection of concrete units whose subdivisions are not decimals, but represent several denominations, taken collectively; as, six pounds four shillings nine pence, three fect five inches, eto.
11. A Power is the product arising from multiplying a num. ber or quantity by itself, or repeating it any number of times as a factor.
v12. A Root is a factor repeated to produce a power.
13. A Demonstration is the process of reasoning by whiois r truth or principle is established.
14. An Operation is the process of finding, from given quandities, others that are required.
15. A Problem is a question requiring an operation.
16. A Rule is a direction for performing an operation.
17. Analysis, in Arithmetic, is the process of investigation principles, and solving problems, independently of set rules.
18. The Principal or Fiundamental Operations of Arith. metio are, Notation and Sumeration, Addition, Subtraction, Multiplication, and Division.

## S I G N 8.

18. A Sign is a symbol employed to indicate the relations of numbers, or quantities, or operations to be performed upon them.
$($.$) is the decimal sign indicating that the number after it is a$ decimal.
$\$$ means dollar.
[^1]+ , the sign of addition, is read plus. Thus, $\Omega+\mathbf{7}$ signifies that $\mathbf{7}$ is to be added to 8 .
- , the sign of subtraction, is read minus. 'Thus, $8-7$ signifies that 7 is to be subtracted from 8 .
$X$, the sign of multiplicution, is read multiplied by. Thus,
$9 \times 6$ signifies that 9 is to be multiplied by 6 . $0+$, the sign of division, is read divided by. Thus, $32+8$ signifios that 32 is to be divided by 3 .
$=$, the sign of equality, is read equal, or equal to. Thus, $8+6=14$, signifies that 8 plus 6 is equal to 14 .
(), a p renthesis, the sign of aggregation, indicates that all the uumbers, or quantities. included within it, are to be considered as a single one. Thus, $(\mathbf{7}+4) \times 3$, indicates that the sum of 7 and 4, or 11, is to be multiplied by 3. A vinouluı or bar, [], has the same signification. Thus, $9 \overline{\times 4}+3=12$.
[], brackets or arotehets, are used to indicate that the operations on the quantities contained within the parentheais have been performed, but before those indicated by the signs outaide the brackets. Thus, $[(8 \times 7)+14]+2$ eomes to $8 \times 7=56 ; 56+14$
$=70 ; 70+8=35$.
: is the sign of ratio. Thus, $6: 4$ means the ratio of 5 to 4 , and is read 5 is to 4.
$::$ indicates the sign of proportior, or the equality of ratios. Thus, $6: 9:: 8: 12$, is read, 6 is o 9 as 8 is to 12 .


## NOTATION AND NUMERATION.

20. Notation is the process ef expressing numbers by letters or figures; and,
21. Numeration is the process of reading numbers when expressed by figures.
2.2. Two methods of notation are in common use - the Roman and the Arabic.

## ROMAN NOTATION.

23. The Roman Notation, so called from its having originated with the Romans, employs seven capital letters to express numbers, viz.:

[^2]It will be seen from the following Table, that all numbers may be expressed by the use of these letters, either by repetitions or combinations.

1 s . Every repetition of a letter repents its value; thus, II, represents teoo; III, represents three; XX, liventy, etc.

2nd. When a letter of any value is placed after one of greater value, it adds its own value to the greater; but when placed before, its value is to be subtracted; thus, VII represents seven; XI represents eleven; while IX represents nine, or one less than ten ; XL, forty, eto.

3rd. A bar or dash ( - ) placed over a letter, increases its value a thousand-fold; thus $\overline{\mathrm{V}}$ denotes five thousand; $\overline{\mathrm{I}}$, four thousand; $\overline{\mathrm{X}}$, ten thousand, eto.

mbers may retitions or
thus, II, te.
of greater ien placed nts seven; less than
es its value four thou-

1. Six.
2. Fight.
3. Ten.
4. Thirteen.
5. Fifteen.
6. Seventeen.
7. Nineteen.
8. Twonty-five.

NOTATION.
EXERCISES IN ROMAN NOTATION.
Exprese the following numbers by letters:
Ane. V1.
-
10. Forty.
10. Forty-six.
11. Finty-four.
12. Sixty.
13. Sixty-eight.
14. Eighty-four.
15. Ninety-nine.
15. One hundred and six.
17. Four hundred and nineteen.
18. Eight hundred and seventy-five.
19. Nine hundred and sixty-five.
20. Four hundred and forty-one.
21. Four hundred and eighty-seven.
22. Six hundred and ninety-five.
23. One thousand six hindired and fifty.
24. Ore thousand eight hundred and forty.

## ARABIC NOTATION.

24. Arabic Notation employs ten characters, or figures, to express numbers, viz.:
 25. The first nin cipher because each has a one ofled significint fignres, digits, from the Lalue of its own. They are sometimes calle, cipher is called Latin word digitus, which signifies fing'r. Th
25. In order to reduce the numeral figures to value of itsown. we give each a second value nocording figures to a small number Thus, the first represents the acording to the place it occupies third, the hundreds. the fourthits; the second, the tens; th:each succeeding firure to the lh, units of thousands; and so on, the unit of which is tene left belonging to a distinct order, the right.
26. Sinee the value of a number expressed by any figure de pends upon the place the latter ocoupies, it follows that figures have two Values ; the one absolute or simple, that is, the value expressed by a figure stiading alone, or, when in a collectio. atanding in the right-hand place; the other relative or local, that

[^3]is, the vaine expressed by a figure used in combination with other figures and derending upon the place the figure occupies. The cipher beames significant when conneoted with other figures only, by filling a place whioh otherwise, would be vacant ( $\mathrm{N}_{\mathrm{o}} .28$ ).
Thus, in 8042 , the simple value of the first figure on the len hand is 8 , and ite local value 8 units of thousands, because it is a figure of the fourth order; the simple value of the third figure is 4 , and its local value 4 tens, because it is a figure of the 2nd order; the simple value of the first is 2 , and its local value 2 units; the cipher
fills the vacent place of the hundreds.

Period of Period of Period of Period of Period of Period of Poriod of Period of Sextill- Quiatill- Quadrill- Trillions. Billions. Millions.Thousands. Units.
ions.
ions.
ions.


## RULE FOR NOTATION.

28. To write in tigures any number without difficulty. Placc as muny dots or points as the number cortains figures; then begin at the left-hand, and write each figure in the place it must occupy, and if there are any vacant places, supply them with naughts or ciphers.

Example. Given the number four billions six millions twenty thousand five hundred units.
Write the 4 in the order of the units of billions, the 6 in the order of the units of inillions, the 2 in the order of tens of thousands, the 5 in the order of hundreds of unite, and put ciphers in the vacant
places. Thus
rith other es. The ures only, 28). n the left use it is a gure is 4, rder ; the be cipher

| 1. |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2. | X | 8. | VII | 13. | XXXV |  | CD |
| 3. | L | 8. 9. | VII | 14. | XL | 20. | CMIV |
| 4. | C | 10. | XI | 15. | XLIX | 21. | DCCXXX |
| 5. | D | 11. | $\underset{X V}{X I}$ | 16. | LXV | 22. | CMXLIX |
| 6. | M | 12. | XXIV | 17. | ECIR | 23. | $\overline{X I X}$ |
|  |  |  |  | 18. | CVI | 24. | $\frac{X I X}{M M}$ |

29. What is the rube for numeration?

## BULE FOR NUMERATION.

29. To read numbers represented by figures.

Begin at the right hand, and point off the figures into periods of three places each. The first period is called UnITs; the second, thousands; the third. millons; the fourth, blllions; the Ffth, trillions, \&c. The last may! 've but one or two figures.

Ex. The number 345678907654326 ie read in the following manner: three bundred and forty-five trillions, six hundred and and fify-four thouns, nine hundred and seven millions, six hundred EAR
EXERCISES IN NUMERATION OF SIMPLE NUMBERS. anad and white tere following numbers.

| 1. | 400 |  | -000 |  |
| :---: | :---: | :---: | :---: | :---: |
| 2. | 6004 8. | 800800003 | 13. | 28754105 |
| 3. | 80067 9. | 87974015 | 14. | 1000500 |
| 4. | 67000510. | 35000918 | 15. | 3008727 |
| 5. | 9006014 | 70150900 | 16. | 505054045 |
| 6. | 92100121 12. | $7080005.49$ | 17. | 78592835 |
|  |  | 4050300 | 18. | 106405021 |

## EXERCISES IN NOTATION AND NUMERATION OF SIMPLE NUMBERS.

EXPRESS BY FIGURES AND READ TEE FOLLOWING NUMBERS:

1. Twenty-seven, forty-eight, sixty-five.
2. Seventy-five, ninety-three, eight hundred.
3. One hundred and ten, one hundred and twenty-four.
4. Three hundred and fifty-one, six hundred and two.
5. Four hundred and ninety-one, nine hundred and nine.
6. One thousand and one, three hundred and three.
7. Nine humsand one hundred and twelve, thirty-six thousand.
8. Seven hundred and eigntionsand five hundred and two.
9. Two millions six hundred and thousand three hundred and ten.
10. Sevency-geven millions and twenty-five thousand.
11. Four hundred millions eight hundred thousand and fifteen.
three thousand four hundred.

## DECIMALS.

## DECIMALS.

30. By Decimals are meant parts ten times, : hundred times, a thousand times, ete., smaller that the unit, or which are suocessively ten times smaller than the other
31. The parts contained ten times in the unit are called tenths; the tenths of tenths, hundredths, because they are contained a hundred times in the unit; the tenths of hundredths, thousandths, because they are contained a thonsand times in the unit; the tenths of thousamdilis, ten-thous mulths, ifc.
32. A whole number and decimals, in a single expressim, constitute a Mixed Number.
Thus, 12.54 is a mixed number, and is real tweive, and decimal fify-four hundredths; 60.205 , real sixty, and decimal two hundred
and eight thousandthe

## NUMERATION TABLE

FOR WHOLE NUMBERS AND DECIMAI.S.

A8ORNDING pROGRESBION. $\underbrace{\text { Morind of Poriod of }}$
*As is easily seen, decimals, with regard to their order, follow inversely the system of numeration of whole numbers; the tenth. is ten times maller than the unit, whereas ten is the unit repeated ten times; the hundredth expresses the hundredth part of the unit, and a hundred, the unit repeated hundred times, \&o.

[^4]fol

## DROLMALM.

red times, are suotre culled are conndredthis, es in the
pression,
decimal hundred

## following exatuple: on decimal parts is made obvious

 Ifthe tenth purt at aided into ten equal parts, each piece will represent tenth into dea egniva thit or the whole apple. Dividing again each be the same for : $t^{2}$ citite, a dollar, we hundredths. The result would
334. Fcop ofte foregoing jilustrations, we deduce the following
I. Write first the whole nember, "ftor which place the decimal point; theul fiont the left to the right, vorite auccessively the tenths, the luundredthys, Mhe thonsindths, icc.

Thus, the $H$ hutest $\mathfrak{z}$ units 25 hundreathe is writen 3.25 .
II. If samue order of decimuls be wanting, fill the vacant places with ciphers.

Thus, the Hu4hswe lez units 5 hundredths is written 12.05 , in placing a cipher to repressit the tenths; and 4 unite 3
and 8 ten-thunsithflens is represented by 4.3808 tenths 8 handredths
'III. If theserefer vecima? the units, and the decimels folly, a cipher is put in the place of Thus, one tenuh iwients follow in their regular order. 5 thousandths, 0.0005 . There is always ${ }^{\circ}$ figitre less in decimals tha whole number, becathe the firme dects than in a corresponding whole number its arthtreluled in decimal unit which is included in the
35. Annexing cibhery to decimals. as long as the diginmif point is notils does not alter their value ten, a hundred tinos pomt is not displaced; the parts are made times smaller: whide ino numerous, but they are ten, a hundred Thus, 0.25 den compensation. by the addition cithere 1.200 by the additiva of one cipher, and 0.2500 valent to 25 humerestifici the value of the decimal is always equiEXERCISES WN HEPCHML NOTATIUN AND NUMLKATION. White per fiffiter tux rollowhic mixed xumeras.

1. Two hundred and sivieen, and three teaths.
2. Five hundred atid seven, and twenty-five Lundredthe.
3. Three huudrest atid four hindredthe.
4. Forty-fur,
5. Three huadred twity three bundredths.
6. Twenty, aud sintur forty-two ten-thollsandths.


[^5]@. Two humdred and twonts, and nine hundred-thousandths.
10. Une thousand and six, and five ten-thousandths
11. Four thousand and seven, and three hundred-thouzandtha.
12. Fint-nine, and twenty-two millionths.
3. Eighty-two, and thirty-six hundred-millionths.
14. Fight hundrel and fifteen, and sixteen thousandths.
15. Twenty-seven, and one hundred aud two billionths.
16. Twenty thousand and ten, and thirty millionths.

EXPREAS ORALLY AND WRITE IX WORDE THE FOLLOWING MIXED XUMBERS AKD INGLK DECIMALE.

Mixed numbers.

| 1. | 8.90 |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 2. | 9.908 | 6. | 354.0064 $\mathbf{3 5 2 . 0 6 0 4 6}$ | 10 | 41.004064 |
| 3. | 541.400 | 7. | 76.26007 | 11 | 452.010778 |
| 4. | 703.2004 | 8. | 375.500506 | 12 | $\begin{aligned} & 7657.008007 \\ & 189804 \end{aligned}$ |
| Single decimals. |  |  |  |  |  |
| 1. | 0.004 | 5. | 0.4072 | 9. |  |
| 2. | 0.000607 | 6. | 0.401950 | 10. | $0.736050210$ |
| 3. | 0.005 | 7. | 0.9540626 | 11. | 0.000500019 |
| 4. | 0.0007007 | 8. | 0.075003 | 12. | 0.00000501 |

.PPLICATION OF THE PKINCIPLES OF NUMERATION
as Laid down in nos. $27 \& 31$.
36i. According to the principles laid down in Nos. 27 \& 31, it follows:

1 st . That, to render a whole number, ten, a hundred, a thousand times greater, we must write at the right-hand side of the number, one, iwo, three naughts or ciphers (1).

Thue, the number 26 units, becomes 260 in adding a cipher ater the 6 , that is, ten times greater than the first, since the units become tens, and the tens, hundreds; or, in other words, the figure of the first order becomes a figure of the second order, and that of the second order, becomes a figure of the third order. If we add another cipher, we obtain 2600, which is a hundred times greater than the first number, since the 260 units have become 26 hundreds.

2nd. I'hat, when the whole number has a decimal annexed, it suffices to remove the decimal point to one, two, threc, Wo., figures towards the right, to ronder the number ton, a hundred, a thousand, \&c., timea grester.
Thus, 26.35 becomes ten times greator if written 263.5 , imoe the tenths become units, the units tens, \&c.

[^6]3ra. That, when the number of decimals is not sufficient 10 render the number as required, we must annex to its right-han! side as many ciphers as will answer the purpose.

Thus, to render the number 24.5 a thousand times greater, it would be necessary to remove the point three fivures towards the right ; but, as there is only one decimal, place two cipherss after the five, and the number becomes 24500, which number is evidently a thousand times greater than the first, since the units of the first order have been changed into units of thousands, or of the second order.
37. From the same principles, it follows also:

1st. That, to render a whole number ten, a hundred, a thousand times, \&c., smaller, it suffices to eut off from the right-hand side one, two, three, \&c., figures.
Thus, in the number 925 ; if we cut 'oft two figures by the decimal point we cbtain 9.25 , which is a hundred tinies smaller than the first, since the hundreds have become units, the tens, tenths, de. 2nd. That, if it be a mixed number, the decimal point must be removed one, two, three, \&c., figures towards the left.
Thus, to render 26.35 ten times smaller, remove the decimal point one figure towards the left, and it becomes 2.635 , that is, ten times omaller than the first, since the tens bec une units, the.

3rd. That, if the number, either whole or decimal only, doea not contain a sufficient number of figures at the left-hand side of the point, we must write as many ciphers as will answer the purpose of the question, taking care that one remain to take the ;lace of the units.

Thus, to render the numbers 8 and 2.635 a thousand times smaller, place three ciphers on the left-hand side of each of those numbers; the first of these ciphers will hold the place of the units, and the others will reduce the primitive number to the required value; thus, the numbers become 0.008 and 0.002635 , which are evidue; thus, the times smaller than the first, since the whits are evidently a thousand thousandths, dc.

## PRACTICAL EXERCISES

ON THE PROPERTIES OF DECIMAL NUMERATION.

1. Render the whole number 38
\(\left.\begin{array}{rrrrr}1^{\circ} \& 10 <br>
2^{\circ} \& 100 <br>
3^{\circ} \& 1000 <br>
4^{\circ} \& 10000 <br>
5^{\circ} \& 100000 <br>

6^{0} \& 1000000\end{array}\right\} \quad\) times greater. $\quad$|  |
| :---: | :---: | ---: |

[^7]
## 80

THE PROPERTIES OF NUMEHATION.
2. Render the mixed number 42.1064231

| 10 | 10 |  |
| :---: | :---: | :---: |
| $2{ }^{9}$ | 100 |  |
| $3{ }^{0}$ | 1000 |  |
| 40 | 10000 | times greater. |
| $5^{\circ}$ | 100000 |  |
|  | 1000000 |  |

3. Kender the mixed number 4.20
$\left.\begin{array}{rr}1^{\circ} & 10 \\ 2^{\circ} & 100 \\ 3^{\circ} & 1000 \\ 4^{\circ} & 10000 \\ 5^{\circ} & 100000 \\ 6^{\circ} & 1000000\end{array}\right\} \quad$ timea $\quad$ reater.
4. Render the decimal 0.05
$\left.\begin{array}{rr}1^{0} & 10 \\ 2^{0} & 100 \\ 3^{n} & 1000 \\ 4^{0} & 10000 \\ 50 & 100000 \\ 60 & 1000000\end{array}\right\} \quad$ times greater.
5. IRender the whole number 6705415
$\left.\begin{array}{rr}10 & 10 \\ 20 & 100 \\ 30 & 1000 \\ 40 & 10000 \\ 50 & 100000 \\ 6 & 1000000\end{array}\right\}$

Ans.
Ans.
Ans.
Ans.67054150000.
Ans.
Ans.
6. Render the mixed number 7610438.06
$\left.\begin{array}{rr}1^{\circ} & 10 \\ 2^{\circ} & 100 \\ 3^{0} & 1000 \\ 4^{\circ} & 10000 \\ 6^{\circ} & 100000 \\ 6^{\circ} & 1000000\end{array}\right\} \quad$ tinnea smaller.

Ans.
Ans. 76104.380
Ans.
Ans.
Ans.
76.1043806

Ans.
7. Render the mized number 5.45


Ans.
Ans.
Ans.
Ans.
Alls.
Ans.
146.2309
10. Hender the mixed mimber 1462.309.


| Ans. |  |
| :--- | :--- |
| Ans. |  |
| Ans. |  |
| Ans. |  |
| Ans. | 0.000005 |

Ans.
Ans.
Ans.
Alls.
Ans.
$\begin{array}{ll}\text { Ans. } & 0.00206007 \\ \text { Ans. }\end{array}$ Ans.

| $1{ }^{\circ}$ | 10) |  |
| :---: | :---: | :---: |
| $2{ }^{\circ}$ | 100 |  |
| $3{ }^{\circ}$ | 1070 |  |
|  | 100000 | limen amaller. |
|  | 1000001 |  |
|  | 10090001 |  |


$\begin{array}{llll}10 & \text { times greater. Ans. } & 1650 . \\ 100 & " & \text { smatler. Ans. } & 38.67\end{array}$
1000 " greater. Ans.
100 "
" Ans. 64040.
smaller. Ans. 0.074
greater. Ans.
smaller. Ans.
greater. Ans.
"Ans.
" Ans. 450.
emaller. Ans.
$" \quad$ Ans. 0.00005
greater. Ans.
smaller. Ans.
greater. Ans.
smaller. Ans.
" Ans.
greater. Ans.
". Alis.
smaller. Ans. 606才.0967
" Ans.
greater. Ans.
vualler. Ans.
enter. Ans.

## ADDITION.

38. Addition is the proces of uniting together several numbers of the same kind, so as to form a single number called the Sum or Amount.
39. Numbers are of the same kind when they have the same denomination.
For instance, dollars can be alded to doilars, pounds to pounds, and yarids to yards, \&c. ; but dollars could not be udded to yaris, nor shilhngs to feet.

## Example of an Addition with ohole numbers.

What is the sum of the three following numbers: 428, 635, and 874 ?

Anabipiss. - Having arranged the numbers, so that all the
operation.
428
635 874

1937 units of the same order shall stand in the eiame eoluman, we first add the oolumu of unis ; thus, 8 and five are 13, and 4 are 17 units, $=1$ ton and 7 units. Wo write the 7 unite under the column of units, and carry or add the 1 ten to the column of tens; thus, 1 added to 2 makeen 3 , and 3 are 6 , and 7 are 13 tens $=1$ hundred and 3 tons. Wo write the 3 cons under the column of tens, and earry the 1 hasdred to the column of bundreils; thus, 1 addod to 4 makes 5 , and 8 We write the 9 hundreds under the enfumn of hundreds; and and 9 humdrede. other columin to be added, we set down the 1 thongand in ithe thomerobing mo and find the ameunt of the three nambers to be 1937.

4(1). We begin the addition by the figures of the first column at the right-hind side, so that in whole numbers, we may carry the tens proceeding from the addition of the units to the colunin of the teus, the hundreds proceeding from the tens to the column of the hundreds, \&c.; and also in decimals, earry the tenths proceeding from the hundredths to the column of the tenths, and the units proceeding from the addition of the tenths to the column of the units, and so on.
41. From the preceding illustrations we deduce the following:

Rule.-1. Write the numbers to be added so that all the units of the same order shall stand in the same column; that is, units under units, tens uno $\rho_{T}$ iens, etc.
II. Beginning at un: •xdd downvard, or upioard, each column separately, and write sh. andernath, if it be less than ten.
III. If the sum of ws the unit figure only, asolisid the ten or teres to the next colume.
IV. Write the whole sum of the last column.

[^8]
## Ans.

which is ma ner dredtho.
43. ation to
44. and eac Then a the first

The

Ans. T which is $r$ Use on numbers :
penses are profit are
-We kno an additio ambunt of

[^9]
## apminem.

## ADDITION OF DECIMALS.

as for the uditition of unding decimals, we follow the sume process right, by a point, wis mule numbers; but we cut off from the which contains the most of ucimuls as there ure in the number Ex. Given the fill the numbers rudded. dredths, 4682 unit liowing numbers to be added: 3579 units 25 hun8856 naits 80 hundredthe.

OPERATIOX.
123.24
349.00
$56 . \% 5$
149.34
967.32

Ans. $\overline{1645.15}$
which is read 1645 units 15 hundredths.
Use or addition.-Addition serve
numbers: the whole cost whon serves to find the sum of several penses are given. The selling the buying price and other ex. profit are given, \&c. -We tnow that
an addition, when resalution or solving of a problem requires ambunt of seceral others. ind a number equal to the sum or

[^10]
## PRACTICE IN ADDITION.

1. $600+850+501+49+904+759+215+555$. Ans. 4433 unite.
2. $604+810+333+1226+3004+4004+5105$.
3. $19223+195974$ Ans. 15086 .
4. $15879+1523+18002.3+100610+3300$. Ans. 438135.
5. $1589+15957+100101+810799+975020+100110$.
6. $41+64+77+49+64+47+36+1012$. Ans. 1390 .
7. $110200+9104+4610+10110+95303+8888$.
8. $100989+100001454+77777707+10110000+100000090$.
9. $50319010+15015+132+20000020+109909+8888888$
$782704+189345 . \quad$ Ans. 80317134.
10. $49+97+68+45+54+68+38+97+75+63+49+$
$98+57+95+59+87+65+43+21+10$. . 118 . 1238.
11. $49+468+429+47+64+46+36+49+94+39+$
$93+29+92+87+78+57+86+39+47+74+98+57$.
12. $56+48+64+46+57+86+54+36+95+34+66$
$+44+33+99+65+67+66+77+59+96+69+49+95$
$+67+27+45+36+97$.
13. $52+34+42+29+423+695+987+429+678+542$
$+249+75+99+88+89+98+36+674+99+89+69+$ $429+98+103+138+274+391$.
14. $94+569+439+590+694+678+534+864+684+468$ $+94+95+649+946+495+789+647+963+769+956+$ $875+708+1075+3548+739$.
15. Express by figures and add up the following numbers: eighteen units, + ninety five, + one huudred and one, + one hundrel and twenty. three, + three hundred and ten, + six hundred.

ALs. 1247.
15. Required the sum of six hundred units, + eight hundred and fify, + five liundred and one, + forty-nine, + nine hundred and four, + seveu hundred and fifty-nine, + two hundred and fifteen, and five huadred and fifty-five.
16. Expresa by tigures one hundred and hiuety-five, + two hundred and eleven, + one hundrol and ten, + one hundred and ninety-nine, + eight hundred and one, + even hundred and reventy-geven, + nine hundred and one.

Ans. 319 .
17. Express by figures two thousand wine huudred and ninety. seven, + twenty-three thousand six hundred and fiftoen, + twelve thousand six hindred and ten, + one thousand and titteen, and make up the sum.
18. Required the sum of nineteen thonsand two hundred and twentythree unite, fone hundred and twenty-five thousand nine hundred and seventy-nine, + one hundred and eighty nine thousand and twenty-three. + one hundred thousand six handred and ten, + three thousand and three hundred.
19. Required the sum of fifteen thoūman eifath hundred and nevenis. nine units, + fifteen thousand nine hundred anll fifty-seven, + one hundred thousand one huudred and one, + eight hundred and ten thousand seven hundred and ninety-nine,' + nine hundred and seveaty. five thousand, + one bundred thousand and ten? Ans. 2017746.

> dred fo

> twenty. units ar 30. three $h$ thousan 31. R sandths, fifteen $n$ 32. R candths, ionthe, 33. A nine hun sand hur eight hut and nine 34. R thousand + twenty thousand thourand
35. Wl Eeven mil thousandt dredths:
thoueandt
20. Required the sam of fifty milhous three hundred and nineteen thousand and ten units, + fifteen thousand and fifteen, + one hundred and thirty-two, + twenty millions and twenty, + one hundred ani niue thousand nine hundred and nine, + eight millions eight hunared and eighty-eight thonsand eight hundred and eighty eight units, + cleven thousand, + eleven hundred and eleven?
$21.40 .05+104.8+1003.025+7.38+2.15$.
22. $0.4+0.20+0.0 .306+11.01+0.200+0.044+0.18$ Ans. 1157.405 vionsandtha
23. $0.0 .5+0.00012+1.110+0.0 .1 / n s .1 .0646$ ten thousandths.
24. $100 .+0.400+20.130+0.020+0.000015+0.014+0.0017$.
$2.6 .96+3.99+6.78+4.39+4.79+2.10012+0.0001005+0.1$.
$+6.81+7.59+0.76+4.36+7.95+2.75+2.98+4.67+7.69+4.42$ +7.889 . $+7.93+3.3 i+7.77+3.79+9.9^{\circ}$
26. $4.95+9.54+8.69+4.29+24$ Ans. 117.929 thuusandthe.
$+7.85+7.67+3.75+47.47+9.09+4.117+7.45+3.68+9.86$
27. $3.78+8.95+9.84+9.35+3.09+4.17+6.97$.
$+5.75+7.75+5.55+47+15+37.14+6.053+67+4.78+4.98$
28. $4.24+4.70+3.65+1.0+1.75+2.55+8.47$.
$9.80+1.40+3.75+7.40+4.65+1640+49.65+3.45+2.90+$
29. Lixpress by tiguren forty unit $+9.09+7.60+55.45+2.95$. dred four units and eight twenty-five thousanths, + seven,+ one thousand three units and units and fifteen hundredths, and udd tha thirty hundredihs, + two
30. Required the sim of for ar tenthan up. Ans. 1157.32.5. three hundred ten-thousandthe, + tenths, + twenty thousandths, + thousandths, + forty.four thousenthe hundredth, + two hundred
31. Required the sum of four hundred eighteen hundredths.
sandths, + one hundred ten-thousendths, + twelve hundred-thoufifteen millionths, + fourteen thousandthes, + eleven hundredths, +
32. Required the sum of three hundred.thousan Ans. 0.174135 . eandths, + eeven tenthe, + three hundred-thousandths, + four thowionths, + ninetcen thousandths. hundred-thousandths, + eight bill33. Add the following nus. nine hundred ten-th sand hundrelthe, + thirdths, + three hundred tenths, + one thoueight hundredthe, + eleven humbred thousar, twenty millionths, + and nineteen millionths. 34. Required the sum of one thousand Ars. 40.174529. thousandthe, + two thousand hundredths, tenths, + four hundred + twenty thousaud milhiontha, to ten thousadirtcen hundred tenths, thousandthe, + one thousand and fre thouand und twelve hundred. thousand millionths? 35. What is the seven millionths one of the following numbers: twenty-five, and thousandthe; one hundred and serventy ifix lundred and forty-three dredths: seventeen, and three seventy-flve, and eighty-nine hum. thouasndths? hundred and forty cight hundred Ans. 36:3.536487.

## 28

## ADDITION.

## PRACTICAL PROBLEMS OR QUESTIONS IN ADDITION,

1. I bought a honse for $\$ 25840$, I paid $\$ 1565$ for right of possession, and $\$ 238$ for repairs; what did it cost me?

OPERATION. ANALYSIS. -The whole cost of the house is equal to the $\$ 25840=\$ 27643$ Ans $=$ amount of the sumeded, that is $25840+1585+238$

1565
$\$ 27043$ Ans. 238 penses are paid.
$\longdiv { 2 7 6 4 3 }$ Ans.
2. I bought some merchandise for the sum of $\$ 245.65$; how much must I sell them to gain $\$ 25.20$ ?
operation.
$\$ 245.65$ 25.20

Analisis.-We must sell the merchandise at a price equal to what it cost, plus the sum we wish to guin; that is, $245.65+25.20=\$ 270.85$, selling price.
$\$ 270.85 \mathrm{Ans}$.
3. A family spends on Monday, $\$ 4.75$; on Tuesday, $\$ 1.15$ more than on Monday, and $\$ 2.05$ less than on Sunday : how much was spent during these three days?
Analysis.-First, find the expenditure of Tuesday and Sunday. On Tuesday, they spent $4.75+1.15=\$ 5.90$; on Sunday, $5.90+2.08=\$ 7.98$. Then, $4.75+5.90+7.98=\$ 18.63$, wholo exponse for the threc days.
4. A family owes the baker $\$ 27$; the butcher, $\$ 16$; the shoe-maker, $\$ 69$; the grocer, $\$ 108$; and for house-rent, 145 ; how much does the Ans. $\$ 395$.
5. Louis was born in 1847, in what year will he be 24 years old?
6. The population of Montreal is about 135000 sonls, that of Quebec, 64150 ; Three-Rivers, 8300 ; St. Hyacinth, 4102 ; PointLevis, 5300 ; Sorel, 5250 ; Sherbrooke, 4300 : what iq the whole population of those reven towns?
7. A wholesale merchant sold during the year 29023 Ans. 226402. $\$ 4500$ of yellow cotton ; $\$ 1592$ during the year $\$ 902.3$ worth of cloth; of merino. For how ; 1592 of Irish linen ; $\$ 1790$ of calico ; $\$ 856$
8. A man owed a much did he aell during the whole year? $\$ 240.50$; the 2 nd. $\$ 376.25$; certain of money; he paid the Ist. time owes $\$ 92$. How much did the 3 rd. $\$ 109.40$, after which he yet
9. A company of eoldiers have at first ? Ans. $\$ 818.15$. ment and they have still 13403 remaining cartridges in an engagebefore the engagement? How many had they
10. An army consiats of three grand divisions Ans. 43085. 8640 men, the $2 n d .7960$, there in the army? 11. The hind-quarters of an ox weigh 390 pounds. 25090 men. guartere 325 poundia each. the sixin 97 pound pounds each; the foreWhat is the whole weight of the ox? poundand the suet 95 pounds. 12. Andrew bought a horse and carriage for $\$ 310$; and pounds. ooth he gained $\$ 176$. How much did he sell thena for? Ans. $\$ 486$.
18. A man bought three fields for $\$ 7680$, he celle them at a proft of \$750. For how much did he sell them? Ans. $\$ 8430$. 14. John bought a new farm in a township; the 1 nt . year it yielded 736 bush. of oats; the 2nd. year, 3697 bush.; the 3rd. year, 9982 bush.; the 4th. year, 10065 bush.; the 5th. year, 12760 bush.: how many bushels did it yield in the five years? Ans. 37240 hush. 15. How many years elapsed from the taking of Troy, which oc. curred 1184 yeara before Chriat, till the year 1869 of the Christian ere? 16. A perton who was born in 1881 , died at the age of 37 . In what year did che die?
17. I have four bills to pay; the 1 Ans. 1868. the 3 rd., $\$ 96.15$; and the 4 th., $\$ 798$., of $\$ 1405$; the 2 nd., $\$ 875.40$; . What sum do I require to pay

$$
\text { 18. The at of the Dominion of Cansda is comnns. } \$ 3174.55 \text {. }
$$ the Province of Ontario, 180000 of Cansda is computed as follows: bec, 210000 square miles; the Provare miles; the Province af Quemiles; and the Province of New Bre of Nova Scotia, 19650 square What is the whole area? Brunswick, 27710 equare miles. 19. A tanner bought 25 hides for the Ans. 437360 square miles. prepared them, he sold them for the sum of $\$ 164.80$; after having How much did he sell them for? 12.60 more than he had paid. 20. A certan sum of money was divided amons. Ans. $\$ 277.40$. the 1 st., received $\$ 65$; the 2 nd., $\$ 26.30$ more among three persons: $\$ 32.10$ more than the eeeond. How more than the first ; the 3rd., was the sum divided? 21. A merchant in selling clord. $\$ 123.40$. Whole sum $\$ 279.70$. $\$ 143.40$ by the bargain ; how muth the amonnt of $\$ 6218.50$, lost 22. At the census of 1861 , the mid he pay for it? 1409430 inhabitants; that of Lhe population of Upper Canada was 300000; New Brunewick, 250wer Canada, ll30s0u; Nova Scotia, there in those four Provinces which How many inhabitants were of Canada ? 23. The battle of Marathon took Ans. 3090230 inhabitants. many years since that period to 1868 place 490 before Christ. How 24. Eighteen tanned horse-hides weigh 486 poins. 2358 years. 324 pouadis in being tanned. What was their pounds; they have lost 25. A number is euch that if diminished their raw weight 9 5976. What is the number? 26. Raw wool is worth $\$ 0.75$ per pound, when prepared it 12463 . \$2.45. What is the price of a pound of prepared wrepared it augments 27. The population of Europe consists of 2 i86001 9 Ans. \$3.20. that of North America, 43879348 ; that of South America inhabitants; that of Asia, 588700000 ; that of Africa, 64035000 America, 22007823 ; 20600000 ; that of Australia, 2025000 ; 64035000 ; that of Oceanica, What is the whole population of the globe that of Polynesia, 419000.

Ans. 1020360878 inhabitants.

## 8UBTRAOTION.

## SUBTRAOTION.

45. Subtraction is the process of finding the differenoe between two numbers of the saine kind.

The larger number, or that whish is to be diminished, is called the Minuesd; and the smaller, or that which is to be aubtracted, the Subtrahend.
46. The result of subtraction is called the remainder, excess, or difference.

Casm I.- To subtract when each figure in the subtrathend is less than the figure alove it in the minuend.

Ex. From 547 take 324.

OPERATION.
Minuend 547 Subtrahend 324
Remainder
223

A valiy:is.-We write the leas number under the grealor, so that units of the same order shall stand in the same column; then, we hogits at the right and procecil as follows: 4 units from 7 units leave 3 units, which wo write in units' place. Two tens from 4 tens leave two tens, which we write in tens' place. Three hundreds (rom 5 humdreds leave 2 hundreds, which
we write in hundreds' plate. Hence we have for the remainder, 2 hundreds, 2
tome, and 3 units, or 223 . tond, and 3 units, or 223.

Minu
Subt
Rem
4 fr m
! thou which on fron ten-the R ten-t under. hundre leave 4 or reins
Minuend
Subtrahend
(1.)

Remainder
457
325
132
(6.)

From
Take
EXAMPLES FOR PRAOTICR.


[^11]
## METHOD BY BORROWING.

OPERATION.

Minuend
Subtrahend
Remainder $\rightarrow$ Analysis.-Having placed the smaller namber under the greater, with nits under nnite, \&c., as in Case 1, we dravs a line underneath. Then, begimning at the right-hand we say : 5 units frum 9 units leave 4 units, Which is the difference of the units, and whioh is written in the units' plaee below. Wo than proceed to take the 7 tens from the 2 tons above ; but this cannot be dore, since the 7 if greator than the 2. We oanngt berrow from the next figure, as it is a cipher, we then borrow 1 frum the 3 thousands, whioh equala 10 hundreds, learings 9 abore the oipher, ant add the 1 hundrel equal to 10 tens, to the 2 tens, making 12 tens; 7 tens ifr m 9 leaves 5, which we write in humdreds' place helow. As we have taken
 Which wa write under. We cannot take 6 ten-thousands from 5 ten-thousands
oo fron the 8 hundred-thought on thousands, ind adding them to the 5 ten-thoured-thousand, which equands 10 a ten-thousands from 15 ton-thousade 5 ten-thousands, make 15 ton-thousands; under. Having talizen 1 hundred-thousave 9 ten-thousands, which we write hindrel-thousands are left; 3 hundred-thonandor tha 8 hundred tho: $:$ sinds, 7 leave 4 hundred-thousands, which we writo under; from 7 humdrod-thousands or remainder, to b:492554. Which we write under; and thus find the direrenoe,

| oreration. |
| :--- |
| 853029 |
| 3600475 |
| 492554 |

## METHOD HY ADDING 10 .

## Analitage-We first take the 5

 and find the difference to the 5 units from the 9 units, belu: As we can iot take $\bar{i}$ tens from, which we write tens to 2 tens, naking 12 tons; 7 tens froms, wa add 10 5 tens. But hnving idded 10 teng, 7 tens from 12 tens leave roinuend, ve shilli have a remainder I hundred, to the to compeneate, we add ia remainder 1 hundrod too large, the subtrahend, making 5 hundreds We Wenni to taiked to the 4 hundreds of we add 10 hundreds to 0, making 10 handreds; 5 hundreds from 10 from 0 ; so leave 5 bundreds, which we write below. Now, as we have from 1 l hundreds or 1 thousand, to the minuend, we shill have a remaindere ndded 10 hundreds, unless we add 1 thousand to the 0 of the thourands inder 1 thousond too largo, thusand; 1 thousand from 3 thouands leave e 1 to take the 6 ten-thousunds from the 5 ten-tho ? thousands. We then proceed ad 110 ten-thousands to the 5 ten-thousanda, thousands from 15 ton-thousands leave 9 ton-thaking 15 ten-thousands; 6 tenfor the 10 thus added to the 5 in the minuend, we adis. Then, to compensate hend, making 4 hundred-thousands, and subtract adce 1 to the 3 in the subtri4 hundred-thousands. Thus, we find the retract the 4 from the 8, which leave before.This operation depends on the prinoiple, that, if any two numbere are equilly moreased, their $u$ dif crence remaine the samp.
47. From the preceding illustrations we derive the folliowing

Rulk.-I. Write the less number under the greater, so thrit units of the same order nay stand under each other.
4. What io the rulo for subtraction?
II. Commeneing at the right-hand, take each figure of the sub*rahend from the figure above it, and write the result underneath.
III. If any figure in the subtrahend be greater than the correg. oonding figure above it, add 10 to that upper figure before subsacting, and then add one to the next left-hand figure of the subrahend.

## PROOF OF SUBTRACTION.

48. We make the Proof of Subtraction in addinis the reinainder to the subtrahend, their sum will be equal to the minuend, if the work is correct.

Ex. From 35678 take 27899.


This method of proof depends on the principle, that the greater of any two numbers is equal to the less added to the difference.

Use or subtraction.-Subtraction serves to find the gain or wss on goods; whut we still owe on a sum of money of which we have already paid a part; in general to find the surplus of a number over another; the difference between two numbers, dcc.

We know that the solution of a problem requires a subtraction, when we must find the difference between two numbers, or the excess of a number over another; and when it is required to find one of two numbers forming a total, that total or amount, und one of the numbers, being given.

EXAMPLES FOR PRAOTIOE.

|  | (1.) | (2.) | (3.) |  | (4) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Minuend | 76518 | 57813 | 13042 |  |  |
| Subtrahend | 49359 | 38675 | 13042 9176 |  | $250143$ |
| Remainder | 27159 | 19138 | 3866 |  | 73985 |
| Proof | 76518 | Proof 57813 | Proof 13042 |  |  |

48. How de yow prove oubtraotion ?
f the sub. derneath. The corres fore sub. $f$ the sub-
the reminuend,
a, we ada 27899. and minuend, le that the

## e greater

 rence.
## gain or

 $f$ which lus of $a$ \&c. raction, he excess done of one of (4.) 250143 17615873985
250143

SUBTRAOTION.
31


## SUBTRACTION OF IECIMALS.

E.r. From 86.7 take 69.354.
oberation.
86.700
69.354
17.346

Avalizeia. - Having faced the loss number under the grenter, sin that figures of the same decimal plave stind 7n the 8 ine cilama, wo write tue ciphers at the ri ht of finurifer that the mbuiend may have as many decimat numes as the oubtrahend; thou we rubtrate as in whole numbere, had finaliy flaco the decimal potat in the tomainder dircetly under that in tho given number.
32.
2. B which
(4.)
1.0062 0.43 0.57 C 2

Role.- I. Write the less number under the greater, so that the decimal points shall stand directly uniler prach other.
II. Sultruct as in whole numbers, and place the decimul point in the result dirictly wnder the poinis in the given numbers.

EXAMPLES fOR PHACTIOM.

|  |  | (1.) |  | (2.) | (3.) | (4.) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | From | - 12.067 |  | 8.11 |  |  |
|  |  | 9.71 |  | 6.7519 | $\begin{aligned} & 36.105 \\ & 7.11892 \end{aligned}$ | $1.0062$ |
|  | Ans. | 2.357 |  | 1.3581 |  |  |
| 5. |  |  |  |  | 28.98508 | 0.5762 |
| 6. | " | m $\begin{aligned} & 90.49 \\ & 109.191\end{aligned}$ | take | e 39.59 | Ans. | 50.90 |
| 7. | * | 5409.055 | / | 49.073 |  | 60.118 |
| 8. |  | 764907.05 | \% | 4045.997 | " | 363.0.38 |
| 9. |  | 89:450.07 |  | 98776.095 | " 676 | 977.255 |
| 10. |  | 46.5742 .5 |  | 98776.095 | ${ }^{6}$ |  |
| 11. |  | 870079.04 | ${ }^{6}$ | $\begin{array}{r}76908.075 \\ \hline 1987 \times 9.958\end{array}$ | " 348 | 834.425 |
| 12. |  | 410048.2136 | ، | $1987 \times 9.958$ | " 631 | 289.082 |
| 13. |  | 409004.9099 | ، | 9372.016 | ' 390 | 676.1976 |
| 14. |  | 570075.9004 | / | 100.137 | " 408 | 04.7729 |
| 15. | ' | 49.1019 | " | 4053.509 | " 5660 | 22.3914 |
| 16. |  | 610011.050 |  | ${ }^{35.708}$ |  |  |
| 17. |  | 71079.0013 | " | 31971.9999 | " 5780 | 33:4.0:01 |
| 18. | " | 79073.07 | " | $7 \$ 82.1736$ | " 633 | 596.8277 |
| 19. | " 1 | 126001.0001 |  | 98986.1204 | "710 | 24.9.496 |
| 20. | ${ }^{4} 1$ | 191279.9709 |  | 98996.9088 | " 27 | 04.0913 |
| 21. |  | 401645.1005 | ${ }^{6}$ | 50056.0093 | ${ }^{4} 1412$ | 23.9610 |
| 22. | " 70 | 700007.02:36 | " | 498.6709 | ${ }^{6} 4011$ | 46.4296 |
| 23. | " 41 | 411978.10359 |  | 79797.0098 | " |  |
| 24. |  | 960945.00005 |  | 36730.09671 | ' 3752 | 48.00688 |
| 25. | ${ }^{6}$ | 0.0707 | ${ }^{4}$ | 00979.00007 | c 3599 | 65.99998 |
| 6. | 14 | 0.0006 | $\mu$ | 0.000607 | " | 0.070093 |
| \%. | ${ }^{6}$ | 0.90019 | 4 | 0.0000075 | * | 0.00 |
| 9. | 4 | 0.0089 | \% | 0.7300007 | * | 0.170:893 |
| 9. | 4 | 0.0904 | 4 | 0.0070675 | ${ }^{6}$ | $0.001 \times 325$ |
| 0. | * | 0.7009 | 4 | 0.00289709 | ${ }^{6}$ | 0.08750291 |
| n. | * | 0.0901 | \% | 0.190007 | ${ }^{4}$ | 0.510893 |
|  |  |  |  | 0.004600008 | * | 0.094699992 |

atermagion.
ar aniler the plave stand the ri, ht of ay decimal is in whole in the reber.
o that the nul point ers.

| 32. | From | 0.0779 |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 33. | 4 | $0.900$ | ${ }_{6} 6$ | 0.01011001 | Ares. | 0.06778999 |
| 34. | " | 0.19100 | * |  |  | 0.8980096 |
| 35. | " | 0.4500 | ${ }_{6}$ | 0.09900035 | ${ }^{6}$ | 0.09199965 |
| 36. | " | 0.09839 | * | . 00050045 | * | 0.44449955 |
|  |  |  |  | -. 09500989 | $*$ | 0.00338041 | gain?

PRACTICAL PROBLEMS IN SUBTRACTION.
A field which had oost $\$ 2360$ was sold for $\$ 2628$. What is the

## oprration. <br> $\$ 268$ $\$ 2360$ $\$ 268$

2. How much does a merchant lose in selling for $\$ 4825.75$ gooda which cost him $\$ 5174.10$ ?

## operation.

\$5 174.10
$\$ 4825.75$
\% 348.35
3. A merchant bought floar for
\$685: how mach did he gain ?
4. Find the difference between 70401 and 6942 ?
5. What is the difference between 85450 and 54498 .
7. The greater of paid $\$ 971$; how much do 1 owe yet ?
what is the smaller ${ }^{\text {? }}$ two numbers is 1302, and their difference is 981 ;
8. A merchant sold in one day $\$ 2571.40$ worth of Alw. 321 . thereby cleared a profit of $\$ 630.95$. him? $\$ 03.95$. How much did the goods cost
9. To what number must we add 76 to increase it Ans. $\$ 1886.45$.
10. The city of Quebec was founded increase it to 740 ? many years from that period to 1870 . by Champlain in 1608 ; how
11. The area of the Province of Quebec is Ans. 262 years. that of the Province of Outario 180000 sqec is 210000 square miles; miles does the former exceed the latter ! sq. m. : by How many square 12. A father was 28 years old at the birth Ans. $30000 \mathrm{sq} . \mathrm{m}$. the age of the son when the father will berth of his son, what will be
13. What number mant be edded be 85 years old! Ans. 57 yr .
14. What will be the ae in to 357.75 to have 8000 ? 1792?
15. What number must be added to 4 Ans. 79 years. 10 units ? 16. In 1857, Canara exported to the Ans. 5 units 95 hundredths. $\$ 13206436.10$, and imported for to the United States for a value of importations exceed the exportations? 0.96 . How much did the 17. Napoleon I. died in 1821 at the age of 52 . Ans. $\$ 7018214.86$. be born ?

In what year wap tns. 1769.

## DUBTRAOTION.

 hundredthe? 12 20. The population of Paris is 1953262 Ans. 0.117 thousandths. London 2863141 ; how much does the populabitants and that of that of Paris?21. Alfred the Great died in 901 Ans. 909879 inhabitants. 24 years: in what year wha he born? 2\%. Charlemagne was born in 742 ; in 768, emperor of the West in 800 , and was crowned king of France he, 1st. at his coronation as king, and died in 814 . How old was age did he die; and thh. hang; 2nd. as emperor; 3rd. at what until 1869 ? 3 rd . at the Ans. 1 st. 26 an king, 2 nd . 68 as emperor, 23. Murillo of 72, and 4th. 1055 years. tioned, the firat bidding was $\$ 30000$, but it was finally at $\$ 117000$ and adjudged to the French wovernment knocked down in the museum of the Lourre. Required Government who placed it 1st. and the last bidding?
22. The population of Montreal, in $\mathbf{1 7 6 5}$, consisted Ans. $\$ 87000$. itants; in 1851, it was 57715 ; in 1856, 75000 ; insed of 7000 inhab. in 1868, about 135000 . What was the in 1851 to 1868 ? 25. A farmer reaped 1689 bushels of Ans. 77285 inhabitants. oats. He sold his neighbor John 890 wushat, and 965 bushels of bushels aats, and the remainder to J 890 bushels of wheat and 478 sort did he sell to Joseph ? Ans. 799 buph. How many bushels of each 26. Two merchants, in commencing. Wheat and 487 bush. oats. $\$ 18500$; the lat. invested $\$ 6590.40$. business, invested a capital of investment to equal that of the second? how much must he add to his
23. Had I $\$ 508.50$ more, I cond ? would have $\$ 75$ left; how much have p ? a debt of $\$ 1015.80$, and 28. A merchent sold $\$ 11630$ worth of Ans. $\$ 582.30$. than oost price; how much did it cost him? 29. A house which was ans. $\$ 10754$. profit of $\$ 840$ to its owner if he had $\$ 14350$, would have given a dit it cost ? 30. Gunpowder was invented in the year 1330 ; Ans. $\$ 13820$. before the invention of printing, which year 1330 ; how long was this

## PRACTICAI PROB <br> PRACTICAL PROBLEMS COMBINING ADDITION AND SUBTRACTION.

1. A retail merchant places $\$ 45.25$ in his drawer for change; on Monday he sells for 875.85 ; on Tueaday, for $\mathbf{7}$. 68.40 ; on Wednesday, Sor $\$ 80$; on Thursday, for $\$ 128.60$; on Friday, for $\$ 54.85$; and on Saturday, for $\$ 72.15$; a ter which he pays a Bill of $\$ 95.60$, another of $\$ 43.25$, and takes $\$ 240.75$ for his own expenses, and then there
campaigs $675 \%$ men. to have 12 usandthe. and that of idon exceed rabitants. $r$ a reign of 4ne. 849. $g$ of France wold was d. at what him death emperor,
being alloicked down placed it tween the $\$ 87000$. 100 inhab 1000; and ation from bitants. bushels of and 478 els of each h. oats. capital of add to him 319.20. 5.80, and 882.30.

876 more 10754. given a w much 13820. was this years.

AND
le ; on lnesiay, and on another o there at 9

Amatymom, - Mrus and out what sum be would have had if he had not patd angthing, and thon what he hae paid out.
Hn $\sin 9,45.25+76.86+88.40+86+128.80+54.85+72.16=\$ 530.10$. Ho hes thlann ont, $96.60-13.25-240.76=\$ 379.60$. There should be len Him. $\$ 150.60=150.50$; difforence $150.50-150-A n o . \$ 0.50$ rgainst
2. A market woman hering 152 eggs, sold to one person 14 of thens, wa mother 27, wanother 73, to another 24, and to another 5 : how tratiy romain?
8. A genticroan having $\$ 1128$, loat $\$ 328$, and Ans. 9. trich liml lir rernainin!?

1. The waters of the St. Lawrence cover an ares Ans. $\$ 318$. misem; two of itm tributarice, the Saguenay and St. Maurice equare the soe an area of 27000 square miles, and the other 21000 square milen. How rnuch does the area of the St. Lawrence exceed those of ins iwo tributsies? Ans. 517000 square miles.
2. A man bus bought four building lots for the suin of $\$ 16860$. For We lat. he praid $\$ 2070.30$; for the 2 nd., $\$ 3674.50$; for the 3 rd., 84175: how much has he paid for the 4th.? Ans. $\$ 6940.20$. 6. I depomited in a Savings Bank $\$ 8752.70$; the first time I drew from it sham of $\$ 4286$; the second, $\$ 1650.50$; the third, $\$ 972.75$. How mush have I left in the bank? Ans. \$1843.45.
3. Momen was born about 1571 years before Christ, lie left Egypt rith the fisbrewa the year 1491 before Christ, and died on Mount Neho, is the year 1451 before Christ. What age was he, 1 st. when he len Kgypt; 2nd. at his death; and 3rd. how long from the period of hin death to the Jear 1871 of the Christian ere?

Ans. 1st. 80 years; 2nd. 120 years; 3rd. 3222 years.
8. A speoulator gains $\$ 6570$, and then loses $\$ 3762.40$; at anothe $r$ time he gainy \$4545.72, and loses again \$5632.10. Tell how mucb his gains exceed hin losses?
9. A man deals in grains since 6 years; the lat. year he loat $\$ 356$; the 2 nd , he gained $\$ 780.20$; the 3rd., he gained $\$ 685.30$; the 4th., he lout $\$ 2800$; the 5th., he gained $\$ 4320.95$; and the 6 th., he loat agaia \$3000. Dilhe gain or lose, and how much? Ans. $\$ 169.55$ loss.
10. A uwish a sum of $\$ 690$, plıss $\$ 55.20$ for interes $t$. He reimbursed at different limen $\$ 87.50, \$ 210.00, \$ 318.45$; how much does he still awe?
11. A farnily owing its grocer \$508.75, takes agans. \$129.25. aronen of $\$ 240,32$ and then ines in payment $\$ 704.65$ effects to the the tralance of icu account? gives in payment $\$ 704.65$; what is yet
12. My brither owed \& cortain sum of money ; he Ano. \$44.42. \$284, $\$ 670.20, \$ 210.08$ and $\$ 346.30$. Finally, in settling; he gave a Bank note of $\$ 1000$, on which thay returned him $\$ 454$ change. What num did be owe? Ame. $\$ 1955.58$.
13. Poter hos 360 sheep, Maurice 145 more than Peter, and Churlem many waurice and Peter together !ecking 117. How uniny niseep han Charles?
14. A mierchant bought whole cargo of Port Ame. 748 abeep. $\$ 12347$; he puid $\$ 311.70$ for freight eago of Portu-Rico sugar worth mianion and muorege ; aftor which expenses, and $\$ 291.30$ for comRequired himerage; aftor which, he sold his sugar for $\$ 12511.30$. 9438.70 lose.
15. If I had sold $\$ 20$ more a piece of linen whioh oost me $\$ 360$, I would have gained $\$ 30$; how much did I sell it ? Ans. $\$ 360$.
16. A pecculator bought 217 cords of wood for $\$ 1085$. He gave in payment 1800 pounds of salmon valued at $\$ 144.00 ; 700$ bushels of potatoes worth $\$ 210$, and 1200 pounde augar equal to $\$ 72$. Hl,w much does he owe yet?
17. I have three oreditora ; I the 3rd. 8754 . On the ora; 1 owe the lat. $\$ 2500$, the 20.1 . $\$ 840$, and $\$ 1800$, and the other, other hand, I have 2 dobtora, the oue owen me what aum remains in has . Besides I have $\$ 3768$ in cash. Hequired 18. How many pounds of bread ing my dobte? Ans. $\$ 4018$. knowing that it takes 114 pounde of will 200 ponnds of flour give, 44 pounds evaporate in bating?
19. Three boxes oontaining Ans.
each box for drayage. the firut conteranges have cost $\$ 17.15$, and $\$ 3$ more; how many does the third oontain 40 oranges, the seoond 80 20. In adding $\$ 5.08$, the price Ans. 875. by a tanner for 4 calf and 6 hores an or hide, to the sum expended Required the price of the 6 horse hides, we oblain sum of $\$ 22.98$. have cost 34.40 ?
21. A cloth merchant bought 80 Ans. \$13.50. and, then sold 140 yards, angar 80 yards inore than he hat at Arst bis shop before hic last ; after whioh he has left inalf what he hed in
22. A dyer twought at purchase. How many yards had he at first? the simn of $\$ 3.84$. The three different times 109 pounds of dye for tity exceeded by 15 pounds hime he bought 47 pounds and this quan. did he buy in his second purchase purchase. How many pounds
23. A general starting for an expedition Ans. 30 pounds. of them to garrison g amall tom expedition with 18000 men, len 600 reinforcement of 800 more, 450 of at the amme time he received a hospitals. Having asked 3500 more whon he was obliged to leave in be lef 1750 at different poste. Required recived only 2730 ; of these on reaching his destination? Required the number of men he had Ase. 18730 man.

## MULTIPLIOATION.

49. Multiplication is the prooess of taking eae number as many times as there are units in another.
50. The terms in Multipliontion are:

1st. The Multiplicand, or number to be taken;
2nd. The Multiplier, or number by whioh we multiply, or which shows how many times the maltiplicand is to be taten ; 3rd. The Product, or the resalt obtained.
51. The multiplicand and maltiplier are aelled Factors, beoause they produce or make the produot.

[^12]
## mULTIPLIOATION.

## MULITIPLICATION TABLE.

| $1 \times 1=$ | $2 \times 1=2$ | $3 \times 1=3$ | $4 \times$ |
| :---: | :---: | :---: | :---: |
| $1 \times 2=2$ | $2 \times 2=4$ | $3 \times 2=6$ | $4 \times 2=8$ |
| $1 \times 3=3$ | $2 \times 3=6$ | $3 \times 3=9$ | $4 \times 3=12$ |
| $1 \times 1=4$ | $2 \times 4=8$ | $3 \times 4=12$ | $4 \times 4=16$ |
| $1 \times 6=6$ | $2 \times 6=10$ | $3 \times 5=15$ | $4 \times 5=20$ |
| $1 \times 6=6$ | $2 \times 6=12$ | $3 \times 6=18$ | $4 \times 6=24$ |
| $1 \times 7=7$ | $2 \times 7=14$ | $3 \times 7=21$ | $4 \times 7=28$ |
| $1 \times 8=8$ | $2 \times .8=16$ | $3 \times 8=34$ | $4 \times 8=32$ |
| $1 \times 9=9$ | $2 \times 9=18$ | $3 \times 9=27$ | $4 \times 9=36$ |
| $1 \times 10=10$ | $2 \times 10=20$ | $3 \times 10=30$ | $4 \times 10=40$ |
| $1 \times 11=11$ | $2 \times 11=42$ | $3 \times 11=33$ | $4 \times 11=44$ |
| $1 \times 12-12$ | $2 \times 12=24$ | $3 \times 12=36$ | $4 \times 12=48$ |
| $6 \times 1=5$ | $6 \times 1=6$ | $7 \times 1=7$ | $8 \times 1-8$ |
| $5 \times 2=10$ | $6 \times 2=12$ | $1 \times 2=14$ | $8 \times 2=16$ |
| $5 \times 3=15$ | $6 \times 3=18$ | $7 \times 3=21$ | $8 \times 3=24$ |
| $6 \times 4=20$ | $6 \times 4=24$ | $7 \times 4=28$ | $8 \times 4=32$ |
| $6 \times 5=25$ | $6 \times 5=30$ | $7 \times 6=35$ | $8 \times 6=40$ |
| $6 \times 6=30$ | $6 \times 6=36$ | $7 \times 6=42$ | $8 \times 6=48$ |
| $5 \times 7=35$ | $6 \times 7=42$ | $7 \times 7=49$ | $8 \times 7=56$ |
| $5 \times 8=40$ | $6 \times 8=48$ | $7 \times 8=56$ | $8 \times 8=64$ |
| $5 \times 9=45$ | $6 \times 9=84$ | $7 \times 9=63$ | $8 \times 9=72$ |
| $5 \times 10=50$ | $6 \times 10=60$ | $7 \times 10=70$ | $8 \times 10=80$ |
| $5 \times 11=55$ | $6 \times 11=66$ | $7 \times 11=77$ | $8 \times 11=88$ |
| $5 \times 12=60$ | $6 \times 12=72$ | $7 \times 12=84$ | $8 \times 12=96$ |
| $9 \times 1=9$ $92=18$ | $10 \times 1=10$ | $11 \times 1=11$ | $12 \times 1$ |
| $9 \times 2=18$ $9 \times 3=27$ | $10 \times 2=20$ | $11 \times 2=22$ | $12 \times 2=2$ |
| $9 \times 3=27$ $9 \times 4=36$ | $10 \times 3=30$ | $11 \times 3=33$ | $12 \times 3=36$ |
| $9 \times 4=36$ $9 \times 5=45$ | $10 \times 4=40$ | $11 \times 4=44$ | $12 \times 1=48$ |
| $9 \times 5=45$ | $10 \times 5=50$ | $11 \times 5=56$ | $12 \times 5$ |
| $9 \times 6=54$ | $10 \times 6=60$ | $11 \times 6=66$ | $18 \times 6=60$ $12 \times 6=72$ |
| $9 \times 7=63$ | $10 \times 7=70$ | $11 \times 7=77$ | 12 x |
| $9 \times 8=72$ $\times 8=81$ | $10 \times 8=80$ | $11 \times 8=88$ | $12 \times$ $12 \times 8=96$ |
| $\times 9=81$ $\times 10=90$ | $10 \times 9=90$ | $11 \times 9=99$ | $12 \times 8=96$ $12 \times 9=108$ |
| $9 \times 10=90$ | $10 \times 10=100$ | $11 \times 10=110$ | $12 \times 8=108$ $12 \times 10=120$ |
| $9 \times 11=99$ $9 \times 12=108$ | $10 \times 11=110$ | $11 \times 11=121$ | $12 \times 11=132$ |
| $9 \times 12=108$ | $10 \times 12=120$ | $11 \times 12=132$ | $12 \times 12=14$ |

Nork.-To ropent the TaWe by ming the coeond columbe monmptom Thas, 1 time 2 is 2, 2 times 2 aro 4, 3 timen 2 are 8,4 timen 2 are 8, an.

## MULTIPLICATION.

CaSE I.-To effect a multiplicution when the multiplier does
not exceed 12 .
E.x. Multiply 542 by 7.

## operation. <br> Multiplicand 542 Multiplier Product $\overline{3794}$

Analyais.- In this example, it is required to take 542 seren times. If wox take the anits of eaoh order 7 times, wo ahall take the ontire number 7 times. Therefore, Writing the multiplier under the unit figure of the multiplicand, we proceed thus: 7 times 2 units are 14 units $=1$ ten and 4 units; Wo write the 4 units next product. Seven times 4 tons are 28 tons, and the the 1 ten to add to the are 29 tens $=2$ bundreds and 9 tens; wo write the 9 ten in reserve, added, and reserve the 2 hundreds to add to the produot of ${ }^{9}$ tens in the tens' place, hundreds are 35 hundreds, and the 2 hundreds of hundreds. Seven times 5 added, are 37 hundrede, whioh the 2 hundreds reserved in the last produot
nXAMPLES FOR PRACTICE.
 Case II.-To effece multiplication when the multiplier exoceds 12.

## Ex. Multiply 478 by 64.

operation.
Multiplicand $\left.\begin{array}{lr}\text { Multiplicand } & 478 \\ \text { Multiplier } & 64 \\ \text { Partial } \\ \text { products. }\end{array}\right\} \begin{array}{r}1912 \\ \text { Entire product } \\ \hline\end{array}$

Analisis:- Wo write the multiplioand and multiplier as in Caee 1, and proceed thus. Four times 8 units are 32 units $=3$ tens and 2 units; wo write the 2 units in the place of units, and add the 3 tens to the product of thims. Four times 7 tens are 28 tens, +3 tens are 31 tens $=3$ hundreds and 1 ten; 3 write the 1 ton in the place of tens, and add tho 3 hundreds to the preduck of handrede. Four times 4 huodreds ase 18 hundredsandrode. Four timen

19 hundreds, which we write in its proper place. We thea, in like manner multiply by the 6 tons in the isultiplier, taking care t. Write the first agure siplier; and, addin the paren, in tens' plase direotly under the 6 of the mulwe find the wholo product of 478 producte obtained by the two multuplications,
Nort.-When there are oiphere betweon the signifioant gigures of the maltiplier, pass ovor them in the oporntion, and multiply by the vignligoant foratios only, remembering to net the arrt Agare of the prodinet andor the dgare of the
52. From the foregoing illustrations wo doduce the following

Rule.-I. Write the multiplier under the multiplicand, so. that units of the same order shall otand under one another, and dravo a line underneath.
II Multiply each figure of the multiplicand by oach figure of the multiplier successively, beginning with the wnit figure, and write the first figure of each partial product under the figure of the multiplier used, writing down and carrying as in addition.
III. If there are partial producte, add thom, and their sum will be the product required.

## PROOF OF MULTIPLICATION.

53. The Proof of multiplication is generally made by another multiplieation (1) in whieh one of the faotors equals the half, the third, or the fourth, ete., of one of the factors of the operation, and the other equals twice, three times, four times, eto., the other faotor of the operation. Or.

In multiplying the multiplicand by the multiplier diminished by 1 , and to the product adding the multiplioand; if tho sum be the same as the product by the whole of the multiplier, the work is correct.

DSE OF MULTIPLICATION.-Multiplication serves to render any number so many times greater; to take several parts of a number; to find the value of several units or parts of unita, when one of them is known; to bring a number expressing units of a certain "uture to another number expressing units which are subdivisions of the first, dec.

Generally we know that the solution of a problem requires a multiplicution, when the value of the unity is mentioned and that the value of several is required, or that of some parts of the unity.

[^13]
## MULTIPLIOATION.

EXAMPLES FOR PRACTIOR.

| (1.) |  | (2.) |
| :--- | ---: | ---: |
| Multiply | 8621 | 37215 |
| By | $\frac{47}{60347}$ | -185 |
|  | $\frac{34484}{186075}$ |  |
| Ans. | Ans. $\frac{223290}{2418975}$ |  |

4. 
5. 
6. 
7. 
8. 
9. 10. 
1. 
2. 
3. 
4. 
5. 
6. 
7. 
8. 
9. 
10. 
11. 
12. 
13. 
14. 
15. 
16. 
17. 
18. 
19. 
20. 
21. 
22. 
23. 
24. 
25. 
26. 
27. 
28. 
29. 
30. 
31. 
32. 
33. 
34. 

|  | 76 | $x$ | 27 | Ans |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 97 | $x$ | 34 | Ans. | 26358 |
| 74 | 49 | $x$ | 46 | ${ }^{6}$ | 23698 |
| 838 |  | $x$ | 57 | ${ }^{6}$ | 34454 |
| 75353 |  | $\times$ | 68 | \% | 478002 |
| 134679 |  | x | 79 | 6 | 51240516 |
| 824956 |  | X | 387 | " | 10639641 |
| 984765 |  | $\times$ | 756 | ${ }^{\prime}$ | 319257972 |
| 6654 |  | x | 789 | ${ }^{6}$ | $744482340$ |
| 97248 |  | $\times$ | 865 | ${ }^{6}$ | 5250006 |
| 689834 |  | - | 943 | \% | 84119520 |
| 867894 |  | $\stackrel{\times}{x}$ | 996 | 4 | 650513462 |
| 807497875 |  | - | 965 | ${ }_{6}$ | 864422424 |
| 84966 |  | x $\times$ $\times$ | 7649 | 16 | 779235449372 |
| 643956 |  | $x$ | 9475 | 6 | 649904934 |
| 96824 |  | $x$ | 4696 | ${ }^{6}$ | 5153983100 |
| 43208 |  | $x$ | 4962 | ${ }^{6}$ | 454685504 |
| 90480 |  | $x$ | 9007 | ${ }^{6}$ | 214398096 |
| 43 |  | x | 89006 | ${ }_{6}$ | 814953360 |
| 76496 |  | $x$ | 87969 | \% | 3827258 |
| 7674 |  | $x$ | 12478 | \% | 6729276624 |
| 3696 |  | $x$ | 819162 | 16 | 95756172 |
| 69421 | $\times$ | $\times$ | 21754 | ${ }^{6}$ | 3027622752 |
| 4321 | x |  | 987654 | ${ }^{6}$ | 1610184434 |
| 756849 | $\times$ |  | 74323 | ${ }_{6}$ | 4267652934 |
| 908708 | $\times$ |  | 70469 | 4 | 56251288227 |
| 4916 | $\times$ |  | 69678 | ${ }_{6}$ | 69109512052 |
| 7654208 | $\times$ |  | 20963 | ${ }_{6} 6$ | 342537048 |
| 80097 | $\times$ |  | 74269 | 10 | 160455162304 |
| 900007 | $\times$ |  | 700608 | ${ }^{6}$ | 5948724093 |
| 4300407 | x |  | 700608 | 4 | 630552104256 |
| 460004 | $x$ |  | 99804 | 4 | 3012899547456 |
| 960076 | $\times$ |  | 90708 | 4 | 45910239216 |
| 690800 | $\times$ |  | 456007 | ${ }^{6}$ | 87086573808 |
| 7006924 | $x$ |  | 540086 | ${ }^{6}$ | 315009635600 |
| 786530746 | $x$ |  | 357894 | ${ }^{6}$ | -3784341555464 |
| 416342605 | $\times$ |  | 987405 | 6 | 281494634809924 |
| 896302456 | x |  | 94376.5 | ، | 411098671149525 |
| 495307429 | $\times$ |  | 936704 | 6 | 845888887386840 |
| 757489007 | $\times$ |  | 900076 | 6 | 463956449974016 |
| 879407854 | $\times$ |  | 698765 | * | 681797675464532 |

(3.)

167034 304 668136 50111020 Ans. $\overline{50778336}$

26352
23698
34454
478002
51240516
10639641
319257972
744482340
5250006
84119520
650513462
864422424
649904934
515:3983100
454685504
214398096
814953360
3827258
95756172
3027622752
4267652934
56251288227 69109512052
342537048
160455162304
5948724093
$\$ 30552104256$
45910239216
87086573808
315009635600
3784341555464
281494634808924
845888887386840
463956449974016
614499429100310

| 45. | 954907089 | $\times$ | 600789 | Ane. | 673697675093221 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 46. | 457907842 | x | 796807 | ${ }_{6}$ | 364864173860494 |
| 47. | 856407809 | $x$ | 305407 | 1 | 261552939723263 |
| 48. | 674396856 | x | 285679 | ${ }^{6}$ | 192661019425224 |
| 49. | 1864321 | $\times$ | 609649 | ${ }^{6}$ | 1136581433329 |
| 50. | 2465783 | x | 3686407 | ${ }^{6}$ | 9089879711681 |
| 51. | 7240036 | $x$ | 4029008 | ${ }^{\prime}$ | 29170162964288 |
| 52. | 908007004 | $\times$ | 500123 | ${ }^{\prime}$ | 454115186861499 |

## MULTIPLICATION OF DECIMALS.

Ex. 1. Find the product of 4.35 by 8.26 .
ofrration. Analisis.-We multiply as in whole numbers, and point off 1.35 on the right-hand of the produot as many fignres for decimala
8.26 as there are dooimal placos in the multiplioand and maltiplier.
$\overline{2610} \quad$ that in multiplying 4.35 by 8.26 , or by 826 hundredths, which is
870 the same thing, wo take 826 times she hundredth part of 4.35 380 but we obtain the hundredth part in removing the point two fi$\overline{35.9310}$ Ans. gures towards the loft (No. 37, 2nd.) whioh will give 0.0435; 35.9310 Ans.there remains then but to ropeat 826 times thie hundredth part to obtain the product required. As the number repented oonmale of the same nature ; to separate the the product witl be oomposed of deci-ton-thousateth part, that is, cut oft 4 figures by the insertion of a point at the right side ( (io. 37). The same reasoning is applioable when thowe are throe, four, to. decimale in the multiplier.

If the factors are decimals only, we multiply as usual and cut off as many decimals in the product as there are in both factors; but if the product does not contain a sufficient number of figures, we fill up the vacant places by ciphers, placing one also for the unite.

## Ex. 2. Multiply 0.054 by 0.056 .

operation. Analysis.-Multiplying 54 by 56, we obtain 3024; but as there are 6 decimals in the two factore, wo place two oiphers at the left gide of tho produot and having put the decimal point, we place anothor oipher for the units, and thus wo find the number 0.003024, whioh is read 3 thousandthe 24 millionthe.
0.003024

## 54. Hence the following

Rule.-I. Multiply as in whole numbers, and point off as many figures for decimals, in the product, as there are decimals. in the multiplicand and multiplier.
II. If there are not as many figures in the product as there are decimal places in the multiplicand and multiplier, supply the do fciency by prefixing ciphers.

> Arern.-To multiply deolmals by 10, 100, 1000. 20., (Na. 80).

## MULTIPLICATION.

Proof.-The proof is the same as in multiplioation of whole numbers.

EXAMPLES FOR PRACTICE.

| 3. | 15.27 |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 4. | 6.55 | $\times$ | 9. | Ans. | 137.43 |
| 6. | 7.41 | $x$ | 98. |  | 622.3 |
| 6. | 197.19 | $x$ | 675. | ${ }^{6}$ | 5001.75 |
| 7. | 97.85 | $x$ | 56. | ${ }^{6}$ | 11042.64 |
| 8. | 69.78 | $\times$ | 975. | * | 95403.75 |
| 9. | 947. | $\times$ | 696. | ${ }^{6}$ | 41588.88 |
| 10. | 869. | $\times$ | 4.65 | " | 4403.55 |
| 11. | 345. | $x$ | 6.96 | " | 6048.24 |
| 12. | 57. | - | 3.95 | 4 | 1362.75 |
| 13. | 786. | $x$ | 9.475 | ${ }^{6}$ | 540.076 |
| 14. | 374. | $\stackrel{x}{x}$ | 7.789 | 6 | 6122.154 |
| 15. | 9.47 | $x$ | 2.967 | ${ }^{6}$ | 1109.658 |
| 16. | 39.47 | + | 6.694 | ${ }^{6}$ | 63.39218 |
| 17. | 676.49 | $\times$ | 28.9005 | \% | 1140.702735 |
| 18. | 401.04 | $\times$ | 60.705 | \% | 41066.32545 |
| 19. | 2617.09 | $\times$ | 13001.4 | " | 21913.456 |
| 20. | 6789.06 | $\times$ | 4281.45 | 41 | 75089.9805 |
| 21. | 3807.45 | $\times$ $\times$ $\times$ | 13808.927 | " 93 | 9640.72768 |
| 32. | 489.04 | $\times$ $\times$ $\times$ | 5321.807 | " 202 | 2510.2547 |
|  |  | $\times$ | 37.00845 | " | 8098.612388 |

## PRACTICAL PROBLEMS IN MULTIPLICATION.

1. If a workman eara $\$ 15$ per week: how much will he earn in

## 9 weeks?

Anaryary. - In ane woek he earns $\$ 15$; in 9 weeks he will earn nine times more, bucaure he works nine times longer; therefore in multiplying by 9 ge ob tsin the sum required $=15 \times 9=135$. Ans. In 9 woeks arns $\$ 13 \delta$.
2. How much will 125 yards of cloth cost at $\$ 3.25$ a yard? Austrysis.-If one yard cost $\$ 3.25,125$ gards will oost 125 timen move; in multipiying $\$ 3.25$ by 125 , the required sum $=3.25 \times 185=4 \mathrm{ne} .9406 .25$.
3. When a yard of cloth is worth $\$ 2.40$, how much will 75 hundredthe of a yard cost?

Analitase. - The yard being worth $\mathbf{\$ 2 . 4 0}$, the 75 -
worth 75 times the hundre 'h part of $\$ 2.40$. 75 hundredths of a gard will be 0.75 , we fad the sume required $=2.40 \times 0.75$; therefore, multiplying $\$ 2.40$ by
4. What will 1635 barrels of $\quad$ Ans. $\$ 1.80$.
5. What will 785 kegs of to sacco cost, at $\$ 25$ a piece ? A. $\$ 40875$.
6. What will 6679 bushels of wheat, at $\$ 36$ a keg ? A. $\$ 28260$.
7. How many pounds of flour are there in 387 cents a bushel 9 198 pounds in each barrel 9 are there in 387 barrels, there being
 containing 1639 letters ?
9. A' bouse has 296 windowe and each window contains letters. of glase, how many panes in the whole edifice? - panes in the whole edifice? Ans. 7080 panes.
10. Required how many trees in a nursery composed of 95 rows, if rach row contains 178 trees?

Ans. 16910 trees.
11. The circumference of the earth is divided into 360 degress and each degree into 69.5 English miles; required how many miles around the earth ?

Ans. 25020.
12. Required how many houra in a year of 365 daya? Ams. 8760 .
13. How many days in 1000 years?

Ams. 365000.
14. A man deposita $\$ 15$ every week in a Savinge Bank; how much does he deposit in one year or 52 weekn?

Ans. $\$ 780$.
15. A reanis of paper contains 20 quires; how many quires are there in 572 reame?
16. If a cask of wine contains 213 quarte; required how many quarts in 136 caske?
17. How many eggs are there in 37 dosen? 28968 quarts.
18. How many days has a person aged 84 years lived, reckoning 365 days to the year?
19. How many pens are there in 200 boxes each containing a gross or 144 pens?
20. How many deye elaped from the birt Ans. 28800 pene. Dec. 1869 inclusively ? ( N - , counting leap yearn.) Ame. 682186.
21. Europe produces yearly 3466 pounds of gold; what is the value in dollars knowing that a pound of this precious metal is estimated at $\$ 1718.50$ ?

Ans. $\$ 5956321$.
22. A library is composed of 75 shelves and each shelf contains 86 volumes; how many pages are there in all the voluines supposing asch volume to contain on an srerage 420 pages ? Ans. 2709000.
23. A speculator has purchased 268 horses and 274 times as many sheep: how many sheep has he purchesed? Ans. 73432.
24. There are 12 baga of wheat on a trick, each bag containing 3 bushels; how many pounds are there in the whole load, if the bushel weighs 50 pounde?

Ans. 1800 pounds.
25. A workman earn 88 a week: how much wil) he earm in 7 years?

Ans. $\$ 2912$.
26. How much will 240 pieces of cloth, each commining 44 jds. cosh, at $\$ 5.40$ per yard?

Ans. $\$ 57024$.
27. How many pair of shoes can be made in 265 days, in a factory in which 86 pair can be made in 1 day ?
28. If, at one load, a spen of horses can draw 2997 pounda; how many pounds can they draw in 327 loads?
29. A field of 7 acres of land yields 45 bushels oats per acre; what is the value of the crops of the 7 acres at $\$ 0.40$ abush.? Ans. $\$ 126$.
30. Supposing a sheep gives 6 pounds of wool a year; how many pounds will 28 sheep give in 3 years and what sum would it bring at 24 cents per pound?

31. What is the value of the crop of a field containing 4 acres, if an acre yields 62 bush. oats worth 45 cente per tursh. ? Ans. 11160 cts.
32. A laborer thrashes 45 sheaves of wheait per day, giving 15 pecks; how many sheaves could 14 laborers thrash in 9 daya, and what would be the quantity of ersin obtained ?

Ame. 5670 sheaves and 1890 pecks grain.

## CON'TRACTIONS IN MULTIPLICATION,

OR MULTIPLICATION BY FAOTORS.
55. In many instances, by the exercise of judgment, as it will be seen, the operation may be very much abridged.
56. Any number that may be produced by multiplying together two or more numbers, is called a Composite Number, Thus, $6,15,18$, are composite numbers; for $6=3 \times 2 ; 15=5 \times$ $3 ; 18=3 \times 3 \times 2$.
57. The Factors of a number are the several numbers which, or 2 and 3 and $4(2 \times 3 \times 4=24)$.
Nors.-The facorere muat not be oonfoundod with the parte of summbor. Thas, the fawore of which 10 ie composed, are 5 and $2,(5 \times 2=10)$; while the parto of while the parte are added, $\mathbf{6}$ produce ${ }^{6}+\mathrm{t}=10$ ). The factore are multiplied,

OAse I.-To effect multiplication when the multiplier is a composite number.

Es. 1. What will 45 acres of land cost, at $\$ 367$ an acre?

|  |
| :---: |
|  |  |
|  |  |

Aralyeis. - The factory of 15 are 5 and 9 . Now, if we mulHply the cost of 1 acre by 5, we obtain the oost of 5 acras; and, by multiplying the oost of 5 aoros by the faotor 9 , wo evidently obtain the cost of 9 times 5 acren, or 45 acres, the sum-
bor bought. Henoe the following \$16515 Ans.

## 58. Rule.-I. Separate the multiplier into two or more factors.

 II. Multiply the multiplicand by one of these factors, and that product by another; and so on, till all the factors have been used. The last product will be the one required.Noss.- The product of any number of fictors is the asme in whatover order thoy are multiplied. Thus, $4 \times 5=20$; and $5 \times 1=20$.

## EXAMFLEE FOR PRAOEEOE

2. Multiply 2745 by $28=4 \times 7$.
3. Multiply 65742 by $36=6 \times 7$.
4. Multiply 78036 by $72=3 \times 3 \times 8$.
5. Multiply 36783 by f1.
6. What will 56 horges cont at $\$ 178$ each?
7. What will 435 buehels of potatoes corit, at 32 cente Ans. $\$ 9968$.
8. What will 64 yards of merino cost 75 cente a buhbel?
9. In 1 mile there are 63360 inches ; , at 75 cente a yard? niles i-2nd. in 54 milea? 45

| 6. Whates i- 2nd. in 54 miles? |
| :--- |
| Ans. 1 st. 2851200 ; |

[^14]$$
\underline{y}
$$

Ans. 76860.
Anc. 5618592.
Asร. 2979423.
10. Thepe Ake xivit hours in one year: how many hours, lat. in

11. A hwo dsflonthes 12432 pounds of breas in one day; how many pounds wili ther entle consume, 1st. in 72 days ?-2nd. in 96 ?
12. An eare if Ans. 1st. 897804; 12. Ap ighe of lind oost $\$ 475$ : what will cost, lat. 15 acres? Cin Ans. lst. 7125 ;
Case H.-F ffect multiplication when the multiplier is 10 , 100,1009 , sic. ( $40.36,1$ st.).
59. Rylte.二Annex to the multiplicand as many ciphers as there are in the multiplier.

WEMPLES POR PRAOTIOE (p. 19).
Cabe HH:-Fl effect multiplication when there are ciphers at the righthunth of suif sw hinth of the factors.

Sx. 1. Multuly 1400 by 80.

1400
$\frac{80}{112000}$ (had 100 , sind tha multiplier into the factors 8 and 10 . Now, it in aridetit. (No. 5 ), that, if these soveral factors be multiplied to fither, thisy will produce che same product as the given numWhatis and ad an. Thua, $14 \times 8=112$, and $112 \times 100=$ 142000 , viry $1180 n \times 10=112000$, the same rosult as $\ln$ che sparattion
81. Fxam the oranading illustration we derive the following

RULE.- -Wrive the significant figures of the multiplier under those of the multiplicxed, and multiply them together. To their product, annege utiduany ciphers as there are on the right of both multiplicund and mittiplier.

HXAPLES FOR PRAOTIOE.
(d.)
Multiply
6860.
8592.
9423.
9968.
hel ?
in 45
200 ;
4. Kulkiply fillo4ji9 by 700500 .
6. Multiply 30i50for by 7007000 .
6. Mukiply $202093+7$ by 40302000 .
(3.)

1306950000 600800 1045560 784170 785215660000000
Ans. 427606215000. Ans. 21515743249000. Ans. 814249517400000.

8. Multiply feuthly millions seven thousand and six hundred, by cight milligns sitap fuhdred and sixty. Ans. 560114005776000 .

[^15]
## MULTHPLIOATION.

9. Multiply forty-nine milhons and forty-nine, by four hundred and ninety thousand.
10. Multiply one billion and twenty Ans. 24010024010000.
and one hundred. 11. Multiply ten billions nidety-six thousand Ans. 1100022000000 . by thirty thousand and seven hundred. 12. Multiply thirty millions, ninety-thousand Ans. 309971760000. six hundred thousand and eighty. Cabe IV.-To effect multiplication Ans. 18056887264000 . siplier is a factor of another part. Ex. 1. Multiply 7439 by 328.

| 7439 OPERATION. |  |
| :---: | :---: |
| 7399328 |  |
| $238048=$ Prod. by 8 unite. |  |
|  |  |
| $\underline{2439992}=$ I'rod. by 328 |  |

 $\overline{2439992}=$ i'rod. by 328. fector 8 of the other part of the multiplier, produet is the multiplier. Now, as the product of the multiplicene multiplier, we multiply it by 4 tens, that by the the parts, added together, give the trie produot or 32 tens. Thene product of of 4 tentaing 11. Ere give the trne produot by 328 ; and,

Ahalisara. - Wo oonsider the miltiplier as separatod into two parts, 32 tens and 8 unite, or $320+8$; of which the omaller part is evidently a faotor of the lerger, since the 32 tens, or 320 . is equal to 4 tene $\times 8$. We next multiply by the 8 mice, ohteinin next multiply by that part oftaining the product for 61. From this illustration we derive the following

Role.-Multiply first by the smaller ;-art of the multiplier; and then that partial product by a factor, or factors, of a lurger tial products will be the product required.

## EXAMPLES TOR PRAOTIOR.

2. Multiply 6526 by 568.
3. Multiply 3785 by 721 .
4. Multiply 85065 by 2432.

Anc. 3706768.
Ans. 2728985.
5. Multiply 236428 by 54918.
6. Multiply 397821 by 25125.
7. Multiply 1146084 by 24816 .
8. Multiply 5723605 by 4249784.

Are. 12984152904.
Ame. 2841220544.

OAse V.--To effect the multiplication of decimale when the multiplier is $10,100,1000$, etc. (No. 36, 2nd.)
62. Rule.-Remove the decimal point as many places to the right as there are oiphers in the multiplier, annexing ciphers if
required.
of that figure lected. figure

6
Rt
revers plica
II.
figure
euch from
the hi
than
of eac
III
result
Note than the oiphers.

> 2. To is gener figure al plication
3. W! produot If betwe
63. $W$ neeessar?

EXAMPLEA FOH PRACTICE (p. 20 and 21).
Case: VI.-Tr, fifect the multiplication of decimuls when it is not necessary tha all the decimai places of the prombat should be retainesl.

Ex. 1. Multiply 6.5628 by 5.786 , retaining only three decimal places in the product.
$\left.\begin{array}{rl}\text { OPEKLTLON. } \\ 6.5628 \\ 687.5\end{array}\right)$
of that immediately above the figure of figures in the multiplicand on the right figure being expresed in units of lected, except for the purpose of finding orders than thousandths, may be negfigure from their product.
63. From this illustration we deduce the following

Rule.-I. Write the multiplier, with the order of its figuree reversed, and witi, the units' place under that figure of the multiplicind which is the lowest decimul to be retained in the product.
II. Find the product of each figure of the multiplier by the figures ubove and to the left of it in the multiplicand increasing euch purtial product by as many units as would have been carried from the rejected part of the multiplicand, and one more when the highest figure in the rejected part of any product is 5 , or greater than 5 ; and write these partial products with the lowest figure of each in the same column.
III. Ald the partial products, and from the right-hand of the result point (ff the required number of decimal figures.
Notr.-l. Should the number of decimal places in the multiplicand be lene than the number requird in the product, supply the deficienoy by annexing diphers.
2. To obtain the number to be oarried to each oontracted partial product, it 18 generally necessary to multiply (mentally) only one figure at the right of the figure above the multiplying figure; but when the figures are large, the inultiplication should commence at least evo places to the right.
3. When the number of unitis in the highost order of the rejocted part of the produot is between 5 and 15 , we carry 1 ; if between 15 and 25 , we oarry 2 , if between 25 and 35 , we carry 3 ; and so on.
63. What io the rule for effecting tho meltiplication of decimab, when it is not necessary thit all the deoimal places of the product ohould be retainedt

## MULTipligation.

## EXAMPIEE FOR PRAOTIOE.

2. Multuply 472.35 by 64.3645 , and 3.657389 by 0.0536423 , retaining, in the first, 2 decimal places, and, in the second, 5 decimal
places.

| OPERATION. |  |
| :---: | :---: |
| 472.350 | OFER.ATLON. |
| 546.3 .46 | 3.657389 |
| $283+100$ | 3246350.0 |
| 188940 | 182869 |
| 14170 | 10972 |
| 2834 | 2194 |
| 189 | 146 |
| 23 | 7 |
| 3040.256 | 1 |
|  |  |
|  |  |

3. Multiply 751.2037 by 38.7136 , retaining 3 decimal places in the product.
4. Multiply 36.275 by 4.3678 , retain product.
5. Multiply 843.7527 by 8634.175 , retaining only the whole nurrbers in the product.
6. Me product. $\mathbf{4} 0.00564$, retaining only 3 decimal placia
7. Multiply 73.27593 by 0.075325 , carrying out the product wo the seventh decimal place.
8. Multiply 1.7323152 by 3962.57302 , retuining Ans. 5.5195095 . in the product.

## PRACTICAL PROBLEMS COMBINING ADDITION, SUBTRAC TION, AND MULTIPLICATION.

1. The hide of an ox costs $\$ 6.15$; it requires $\$ 2$ worth of bark, 9 quarts of oil'at $\$ 0.18$ a quart, and $\$ 0.60$ for labor to prepare it, Required the gain if it be sold afterwards for $\$ 12.75$ ?

2. A muolin manufaturer sold $10 . \$ 2.38$ gain. 170 pieces to Montreal merchants ; 8 one year, 540 pieces of it, viz. : to Toronto merchants; and the remaing to Quebec merchants; 130, what is that remainder? he remainder to Ottawa merchants:
3. A man lought 25 barrels of flour Ans. 155 pieces. rels of apples at $\$ 3$ a barrel; what four at $\$ 5.50$ a barrel, and 40 bar.
4. I paid for building ing house was the cost of all ? Ans. $\$ 257.50$. much less $\$ 892$, and for my furniture for my farm 3 times as buidding my houce; how muoh did I pey $\$ 140$ more than I paid for


21: for olothing, $\$ 120$ for books, and $\$ 165$ for other expenses: how much smn he save in 4 years? b. A merchant aull 7.5 yards of cloth at \$9 Ans. \$1250. ceivea in payment $1: i 2.25$ yards of linen at $\$ 0.47$ per yard: he re how minch will the merchant receive ? $\$ 0.92$, and a bill of $\$ 63.58$, 7. A frockeller male 'in invoice of book Ans. Nuhing. utrien it $\$ 1.20 ; 24 \mathrm{y}$ at $\$ \mathrm{~V} .90 ; 136$ at $\$ 0.67$; follows: 125 vol. What in the amount of his invoice? at $\$ 0.67$; and 275 at $\$ 0.50$; \%. Leen has $\$ 127$; 'eter, 3 times as much minus \&ns. $\$ 1601.82$. han an much on Leo and Peter toget!er: hows $\$ 205$; and John an! Joinn respectively, and how much how much have Peter y. Ans. Peter, $\$ 176$; John, $\$ 303$ all ?
9. A merchant bonght 15 pieces of blue olotho3; and all, $\$ 600$. yariln, and 12 pieces of black cloth of oloth, each containing 37 many yards of cloth did he buy of the each containing 34 yards ; bow
10. If $n$ cow cost $\$ 28$, a horee 6 the two kinds altogether?
an minch as the ocw and horse imes as much, and a farm 9 times more will the farm cowt than 5 borgether, minus $\$ 1 I 2$; how much
11. A wholesale urocer 5 horses and 12 cows, at the same rate? barrel; he fold st barreje of them at $\$ 12$ barrels of salmon at $\$ 10.50$ a at 新 a barre) ; how much did hem at $\$ 12$ a barrel, aut the remainder
12. If an ace of land proge gain or lose ? Ans. Gained $\$ 109.50$. bumielm of need; it is required how many bush. of seed will 7 know how many pounds of flax and the whole be worth, if the flax be sold produce, and how much will at \$2.5n per bush. ? Ans. 2534 pound at $\$ 0.18$ a pound and the seed

1:\%. In a dairy, there are 27 mich fiax ; 77 bish. seed; $\$ 648.62$. average, 108 prounds of butter; what cows which give each, on an in relling hin butter at $\$ 0.18$ a pound ? 14. $\Lambda$ firrner desire to manure a field Ans. $\$ 524.88$. masure worth $\$ 4$ the hundred weight, and pay 12 acres of land with buoured weight; how much will it cost pays $\$ 1.45$ for cartage per supposing he requires 2 hundred weight him to manure his tield,
1.. A cabinet-maker carns daily $\$ 1.55$; his ? Ans. $\$ 130.80$. three mone, 0.65 each ; how much can he his wife, $\$ 120$ : and his daily oxpenses of the whole family being he lay by every week, the
14. A lends B $\$ 19560$, B lets A being \$2.68 ? Ans. \$3.44. $\$ 3$ sy2, $m$ furm 4 times as much as the bank ntock to the amount of the remainder in cash ; how mush bank stuck - $\$ 1998$, and pays
17. A jewellor bought a certain cash did B pay A? Ans. $\$ 2098$. of $\$ 0.78$ pere pound; had hertain quantity of ivory, at the rate of Lave licen increased one eighth; bought 6 pounds more, the cost would
18. The repairs and superintendence of did be pay for his ivory? $\$ 943$ per mile; the expenses fordence of a railroad tract cost yearly besiden the company pays $\$ 626,40$ inprovements come to $\$ 4342.60$; other items; required the total yearls administration purposes and mileg long ? 19. A plumber furnishes three kinds of aine Ans. $\$ 136045$. of the firtt, in 2 inches at $\$ 0.32$ per yard zinc pipes : the diameter $\$ 0.64$; and the third, 8 incies at per yard; the second, 5 inches at

## DIVIBION.

99 yards long which is 20 yards more than the second and 34 more than the third; what sum must be paid to the plumber for hin 20. A handkerchief inanufacturer bought 78 Ans. $\$ 144.64$. of which 40 are warp, at $\$ 10.90$ per ponght 78 packages of thread, He paya $\$ 0.85$ per dozen for weaving and what will be his gain, knowing that he has for selling expenses; handkerchiefs, and sold them at the rate of $\$ 2.58$ mede 640 dozen of and sold them at the rate of $\$ 2.58$ per dozen?

Ans. $\$ 244$.

## DIVISION.

64. Division is the process of finding how many times one number is contained in another; or the process of finding one of 3, gives 12 for product io seek a number, which, being multiplied by plied, to obtain 12 in the product.

The product is called Dividend, the known factor, Divisor. and the factor sought, Quotient.

When the dividend does not contain the divisor an exact numbet of times, the part of the dividend left is called the Remalnder. and must be less than the divisor.

$$
\begin{aligned}
& \text { Case I.-Tt divide when the divisor does not exceed } 12 .
\end{aligned}
$$

Nurr,- When the prooess of dividing ie ocrried on in the mind, and the quotien only is net down, the operation is called Short Divition.
Ex. 1. Huw many times is 7 contained in 994?

## operation. <br> Divisor 7 ) 994 Dividend.

142 Quotient. dividend, for the hundreds' figure of the quotient. The 1.09 direotly under the 7 , its dividend, which is tens, we unite of the quotient. T. 9, the next figare of the tons, in which we fiad the divisor 7 to be contrined remaining, which equal 29 we write the 4 fur the ters' figure in the quotiont, 4 times, and 1 ten remaining; equals 10 unlts, which, united to 4, the last fiont, and the 1 ten remaining, units; in 14 units, 7 is contained 2 times; writigure of the dividead, make 14 the quotient, we bave 142 for the entire quotient.
65. Rule.-I. Write the divisor at the left-hand of the dividend, with a line between them, ant draw a horizontal line benputh the dividend.
64. What is division ? - What is the dividend ? - The divisor? - The quotient ? - Tive romaindar 8-65. What in the rulo for ohort division \%

Analybis, - We write the divisor on the left of the dividend with s line between them and another line bonesth the dividend; then, beginning at the let-hand, we ssy: 7 is con-

Id 34 more ber for his $\$ 144.64$. of thread, at $\$ 10.55$ ; expenses ; dozen of n? s. $\$ 244$.
imes one ng one of n. Thus, tiplied by be multi.

## Divisor.

## Drymion.

## PRACTICAL PROBLEMB.

## 1. Nine yards of silk velvet cost $\$ 72$; how much did it oost

Axalyas.-If the prioe of a yard wero known, in minltiplying it by 9 , wt moald obtain $\$ 72$; therefore, 72 is a produot baving for factore 9 and the price of a yard. Then. in dividing the product 72 by the faotor 9 , we obtain the price $\theta$ times $; 72 \div 1=$ Ans. \$8. Or again, an 9 yards cost $\$ 72$, 1 yard will cont ebtain the price of a yard. 9 timen lose yarde ; then, in dividing 72 by 9 , we
2. If 5 shilling make a dollar ; bow many dollare in 8890 shillings ?
3. A gentleman divided $\$ 89622$ equally among his. 9 children; how
uch did each receive? much did each receive?
4. How many barrels of flour, at $\$ 8$ ans. $\$ 3958$. $\$ 680$ ?
6. If 12 inches make one foot; how many feet ins. 85 barrels.
6. Eleven horses were sold for 52531 ; feet in 7501464 inches? received for each?
7. A boy spent in one month 260 Ans. $\$ 231$. for each; how many orases did he buy? for oragges, giving 4 cente 8. A carponter worined Il monthe for ? 3572 ; Ans. 65 . ceive a month ?
9. If maple is worth $\$ 6$ a cord ; Ans. $\$ 52$. \$1152?
10. A person wishes to distribute 168 apples equalls. 192 cords. and 3 girls; how many will each of them receive?

Cask IT.- To divide when the divisor exceets Nore. When the whole process of dive divisor exceeds 12. Long divioion.

Ex. Divide 4738 by 34.
operation.
Divisor. Divd'd. Quotient. 34) 4738 ( 43918 34
2nd. partial dividend $\overline{133}$
3rd. partial dividend $\frac{102}{318}$
306
12 Remainder.
nalysis. -Taking 47 hundreds for the first partial dividond, we say : 35 is oontained in 47, I time. The I we write in the quotient; $34 \times 1=34$ which we write under the 47 ; $47-34=13$, to whioh bringing down the next figure of the dividend; whioh is 3, we form 133 ; 34 in 133, 3 times. The 3 wo write in the quotient; $34 \times 3$ $=102$, whioh we write under the $133 ; 133-102$ write under Which bringing down the next figure of the dividend, weform $318 ; 34$ in $318,{ }_{9}$ thes. The 9 wo write in the quotient; $34 \times 9=306$, whioh wo write under vided, whioh we write in the arationder, or a pert of the dividend left andithe division.
66. Rule.-I. Write the divioor and dividend as in short division, and draw a curved line at the right-hand of the dividend.
II. Take for the frrst portial dividend, the least number of figures on the left that will consain the divisor, and place the quo. tient on the right.
III. Multiply the divisor by this quotient figure, place the prodwet under the partial dividend, subtract, and to the remuinder, annex the next term of the dividerid, for the second partial dividend.
annex the next term of the dividend, for the second partial divi dend.
IV. Divide as before, until all the figures of the dividend have beon brought down and divided.
V. If any partial dividend will not contain the divisor, place a cipher in the quotient, and bring down the next fugure of the dividend, and divide as before.
VI. If there be a remainder after dividing all the figures of the dividend, it must be written in the quotient, with the divisor underneath.

Norss.-1. If any remaindor be equal to, or greater than the divisor, responding figure in the quotient is too emal.
2. If the product of tho divisor by the quotient figure be greater partial dividend, the quoticnt figure is too large.

Proof.-It is the same as in short division.

## DIVIBION ACCORDING TO THE FRENOH METEOD.

Ex. Divide 11812 by 72.

OPERATION.
Dividend 11812 ( 72 Diviscr. $\frac{72}{461} \overline{164 / 2}$ Quotient. 432 292 288

Remainder.

Dageitation.-We see by tilu example in the margin, that the divisor is placed on the right of tho dividend, and the quotient below it. This mode gives the work a moro compact and noat appearance, and posesesser the edvantago of having tho tigares of the quotient near tho divisor, by which meane, the practical diffsulty of multiplying the divisor by a figure placed at a diatanoe from it, is removed.

## ABBREVIATION OF LONG DIVISION.

f\%. By the following method, we avoid writing the products in ion:; division, as in the example of Case II, above.

Ex. 1. Divide 8764 by 365 .

```
        opEibatiom.
36.5) 876.4 ( }2
        1464
        ...4 remainder.
```

Analrisis.-In this oporation, we say : 3 is oontained 2 times in $R$; wo write 2 at the quotient and multiply the divisor saying: 2 . times 5 are 10, which subtractod from 1 in (beonuse we inoroase the 6 by 10), leapee $f$. and onrry one ; 2 times 8 are 12 and 1 is 18

## Drviaion.

7, which, subtracted from 8, ieave 1; we bring down the 1 to form the sesond partial dividend. Then 3 in 14 ie oontained 4 times, whioh wo writo at the tial dividond in a similar ment; we subtract the product from the second parproof. Hence the foilowing

## Rule.-I. Obtain the first figure of the quotient in the usmal manner.

II. Multiply each fiqure of the divisor by this quotient figurs, subtract from the first partial dividend, and write underneath the remainder.
III. At the right of the first remainder, annex the next figure of the dividend, for a new partial dividend, and proceed as with the former, till the work is finished.
Obsirvition 1.- When, after having einployed all the figures of the dividend, there is still a remainder, we may reduce this remainder, firstly in tenths by adding a cipher at the right of it, and continue point at the quotient. When we oontinue the divieion, the second but place no more points at the qus by the addition of another cipher; the order they occupy. (Nos. 27 and 31.)
Ex. Divide 679 by 28.

## OPERATION.

28) $679(24.25$ $\overline{119}$ . 70 140

Axalyais.-Aftor the division, there romaime 7; We reduce this romainder to tonths by writing a oithe quotiont, and thend of it, and wo plase a point at romains yot 14 thon proosed as beforo. But an thoro hundredths by the winthe, we roduce this nambor to tiplying and aubtrioting an bef anothor oiphor. Kui-
 quotiont of 679 by 28 , as ehown by the proof.
Had there beon anothor remainder, wo woild have edded one more oipher. chay order of deoimal anity.
we first place a cipher When the dividend is amaller than the divisor, are no integers or whole a point at the quotient to signify that there tenths, hundredths, sce. numbers; then we reduce tho dividend to. (N. 36.), and proceed as before.

Ex. Given 6 to be divided by 25 ; what will be the operation ?

## OPRRATION.

25) 6.0 ( 0.24 100

0 in 6 ie nrsis,-Having disposed the terms, wo saj: 25 the quotient. Then we wedte a oipher and a point at by placing a cipher at the rishr-hend of it in tonthe 25 in 60 is oontained in rosi-hand of it, and say: reduce them into handredths by the addition of a ciO. 24 hundredtbs is the qustient of 6 divided by 25 anits.

USE or DIVISION.-Division serves to divide a number into equal parts; to render it a certain number of times smaller; to find hovo many times a number is contained into another ; to find by what number must a given number be multiplied to produce annther given number. Division serves also "I find the value of the unity when a certain given number of units or parts of units are howon, as for instance, the buying, the selling price of a yard, the gain or loss of a yard, dec. dec.; to find the number of units knowing their whole value and that of the unit, as for instance, the number of days that a laborer must work to earn a certain sum; and lastly, to find how many units there are in a number which expresses subdivisions of this unit, such as to find how many hours there are in any given number of minutes, \&c.

We know generally that the solwin of a problem requires a division when the value of sever :ins, or parts of units, are given, to find only one; Or, when t. caiue of the unit, and several units, or parts of units being given, we seek the number of units or parts of units.

## EXAMPLES FOR PRAOTIOE.

1. Find how many times is 72 contained in 23506 .
romaian 7; riting a oi00 a point at But ma thero - number to pher. MaiChat nothing
ors oiphor.
10 divisor, that there. vidend to.

## ation 9

We sag: 25 i a point at in tonthe and any: $1 a \mathrm{in}$. on of a citherefore,

PROOR by multiphication.
327 Quotient.
72 Divisor.
$\overline{654}$
$\frac{2289}{23544}$
52
23596
Remainden
Dividend.

| Quotients. | Rem. |
| :---: | ---: |
| 1746 | 3 |
| 2143 | 8 |
| 20284 | 3 |
| 31833 | 16 |
|  | 2 |
| 12442 | 21 |
|  | 19 |
| 13006 | 11 |
|  | 4 |
| 8652 | 15 |
|  | 5 |
| 14703 | 23 |
|  | 55 |
|  | 41 |

DIVigion.

| 16. | 4968 |  |  | Quotionts. | Resa |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 17. | 940025 | $\div$ | 64 | 77 | 40 |
| 18. 19. | 445124 | $\div$ | 70 |  | 61 |
| 20. | 4728 39006 | $\div$ | 75 | 6358 | 64 |
| 21. | +1679407 | $\div$ | 79 | 493 | 3 59 |
| 22. | 4306404 |  | 80 |  | 47 |
| 23. | $\begin{array}{r}167008 \\ \hline\end{array}$ | $\div$ | 85 87 | 50663 | 49 |
| 24. | 7456029 | $\div$ | 87 90 |  | 55 |
| 25. | 6717890 | $+$ |  | 82844 | 69 |

To calculate with two decimals in the quotient.


67. Wh

Den.

Hom.

DIVBGION.

## DIVISION OF DRCIMAIN.

E. 1. Divide 3.456 by 2.4 .

OPERATIOM.
24) 3.456 ( 1.44 Amp.

| $\frac{24}{105}$ |
| :--- |
| $\frac{86}{88}$ |
| 88 |

Es. 2. Divide 0.525 by 7.6.

OPERATION. $7600) 525.00$ ( 0.07 . 62500

> Axalysis. - We divide an in whele numbert; and, sinos the divioor and quotiont arn the two facturs, whioh, being multiplied together, produce the dividend, we point of two deoimal figures in the quotiont, thate the nomaber in the two feotors equal
67. From the preceding illustrations we deduce the following

RuL. I.-Divide as in whole numbers, and point off cs many decimals in the quotient as the decimals in the dividend exceed those of the divisor; but, if thers are not as many, supply the defioiency by prefixing ciphers.

Or,
Rule II.-lf the dividend and divisor have not the same number of decimals, annex ciphers at the right-side of the torm which has the least, so that it may have as many decimal figures as the other; then divide, without any regard to the point, as in whole numbers.

Kote 1.-To divide decimale by 10, 100, 1000, ato. (Ne. 3y).
Paoor.- The proof is the same as in division of whole num. bers.

HEAMPLES TOR PRAOTICE

| 3. | 79.1 | $+$ | 2.5 | Quotionts. $31.64$ | mom. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 4. | 67.8632 | $+$ | 16.4 | 31.64 $4.174$ | 95 |
| 5. | 2.3421 | $+$ | 42.2 | 0.055 | 911 |
| 6. | 0.338 | $+$ | 0.15 | 0.065 | 811 |
| 7. | 14. | $+$ | 0.7853 | 17. | 8 |
| 8. | 0.21318 | $+$ | 8.34 | 17. | 6516 |
| 9. | 10.85 | $+$ | 8.34 |  | 468 |

[^16]
## diviaton.

To calculate with five decimals in the quotient.

|  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 12. | 16.6 40.72 | $\div$ | 10.2 | Quotients. | Hom. |
| 13. | 46.634 | $\div$ | 16.12 |  | 34 |
| 14. | 79.685 | $\div$ | 39.122 | 1.19201 | 740 |
| 15. | 76.1234 | $\div$ | 14.244 | 1.19201 | 18478 |
| 16. | 59.2687 | $\div$ | 9.24 | 8.23846 | 6984 |
| 17. | 79.4 | $\div$ | 91.42 | 8.23846 | 296 |
| 18. | 70.8 | $\div$ | 9.04 |  | 1998 |
| . 9. | 29.40 | $\div$ | 10.08 | 8.78318 | 528 |
| 20. | 16.74 | $\div$ | 18.126 | 1.62197 | 960 |
| 21. | 0.7 | $+$ | 17.261 | 1.62197 | 17178 |
| 22. | 0.2 | $\div$ | 3.7 | 0.18918 |  |
| 23. | 0.42 | $\div$ | 3.2 | 0.18918 | 34 |
| 4. | 0.009 | $\div$ | 3.07 | 0.13680 |  |
|  |  | $\div$ | 0.000014 | 0.13680 | 240 |

analysis.- If the price of a $\$ 123.75$; how much will 1 yard cost ? would obtain $\$ 123.75$; therefore, $\$ 123.75$ is , n , in multiplying it by 45 , we the price of a yard. Dividing 123.75 by 45 , wo obtain thing for faotors 45 and $823.75 \div 45=\quad$ ard wo obtain the price of a yard $=$ 2. A laborer earns $\$ 2.65$ per day; in how Ane. $\$ 2.75$. 647.70?

Analysis. - As many times as $\$ 2.65$, the
in $\$ 47.70$, as many days will be required; price of a day's labor, aro contained
we obtain the number of days required $=\mathbf{4 7 . 7 0}$; ine in dividing 47.70 by 2.65 ,
3. The product of two numbers is $6610 \div 2.65=$ Ams. 18 days.

85 ; what is the other? 661045 ; one of the numbers is
4. What is the number that, being multiplied 72 Ans. 7777.
5. One of two factors is 4.75 and their produl by 72 will give 70344? other factor? 4.75 and their product 4222.18 . Find the
6. I paid $\$ 806$ for 196 reams of Ans. 888.88 hundredths. ream? reame of paper; how much is that per
7. What number is that which is 25 time Ans.
8. At $\$ 0.30$ per volume, how many times smaller than 3575 ?
9. If a cord of maple wood cost $\$ 4.60$;olumes can be got for $\$ 69$ ? bought for $\$ 989$ ?
10. How many sheets of paper in a volume in 80 Ans. 215. (The sheet in $8^{\circ}$ contains 16 pages.) volume in $-8^{\circ}$ of 1280 pages? 11. How many yards of carpet, at $\$ 4.60$ per yard Ans. 80 . for $\$ 676.20$ ? 12. If 63 gallone make a hogshead ; Ane. 147 yards? 2016 gallons make? 13. In how many days could 35 men accomplish as Ans. 32 . sa one man in 805 days ?
14. During a cruise of 64 days, $A$ Ans. 23. did the sail each day? Ans. 182 milee.
16. Haring multiplied 6.55 by $n$ certain number, we obtained 67.3125; What iff that number?
16. A tranp of the Grand Trunk Railway runs 62 miles an hour; at the same rate, libw long would it take to go round the world, the distance beipg affortt 2000 miles? Ans. 403 + hours. 17. The lagge whedls of a coach are 15 feet ins. circumference, the small onas 6 feqt; hew many turne will each make in a distance of 18. Find antiber Ars. Large, $9345+{ }^{7}$; sniall, $23363+4$.
19. I baught fo fer whose product by 0.005 would be 0.00025 . sollare did itt costoper dere? Containg 175 aares for $\$ 4.75$; how many 20. A batchar givere $\$ 66$ for sheep, at the rate of $\$ 3$ Ans. $\$ 25$. many sheep did wethy? 21. How futuy phir of slippera must be made bins. 20 sheep. eara 1.35 pardey, if he be paid $\$ 0.15$ for made by a shoemaker, to
22. The mpthel recelpts on a railroad 500 ery pair he makes? \$3600000. Rhequifed the average daily receipt miles long amount to oeived per milestandinly? Ane. A verage daily receipts how much is re-
23. The sir ortutifed in a puncheon do per mile $\$ 7200$.
23. The sir obtutived in a puncheon do per mile $\$ 7200$.
yard cost ? $t$ by 45, we otors 45 and f a yard $=$ lns. \$2.75.
ill he eapn 18 days.

- contained 70 by 2.65 , . 18 days.
umbers is 7777. re 70344? Find the redthe. that per watar it would contuif whould weigh 7507 . draohms ; how many; the is tie weight of the whtergreaticr than that draohms; how many times

24. A charcon maker places i 27 that of the air? A. 770 times. oost imm 5880 ; he cotrsumites 13 corcords of wood in a kiln which the value of the charcont obtained cords of fuel for the operation, and of $\$ 0.28$ par buhtat. Kequired homestimated at $\$ 231.14$, at the rate produced by a corrd off wood? how many bushels of coal have been 25. The papulatiof of the globe is sbout 1300. Ans. 6.5 bashels. supposed that it ifs refiewed every 33 in 1300860000 inhabitants; length is about io peargit. It is required (in Canada, the mean die yearly, daily, every hour sad equer minute? how many persons persons yearly; 100800 dajly; 1500 overy hour; Ans. 39420000 (or 5 every 4 \&ecgadfi.) ;

## GONTRACTIONS IN DIVISION,

 of bivibion by yaotora. Cabe I.- Th divide when the divisor is a composite number. Ex. 1. Divide 解抽 \&quilly among 28 peroone.-prramion.
4) 1696
7) 399 57 A4 4.
flitrist -The factorl of 28 are 4 and 7. We divide Fifop by 4; and the resulting quotiont by 7, and obtain gutatint'of 1596 divided by \& times be the sane as the
 then by 4 . Honee the following ciriding first by 7 , and
68. Ruws.- Wirinte dividend by one of the fuctors, und

## DTVIOION.

the quotient thus abtained, by a second factor, and so on, till evory factor of the divisor hus been used. The last quotient will be the

## EXAMPLES FOR PRAOTIOE.

2. Divide 4536 by $14=2 \times 7$.
3. Divide 9774 by $18=3 \times 6$.
4. Divide 14560 by $35=5 \times 7$.
5. Divide 126375 by $75=3 \times 5 \times 5$.
6. Divide 69384 by 42 , using its factors.
7. Divide 57456 by 72, vaing its factors.
8. Divide 246792 by 84 , usiog ite faetors.
9. Divide 2962875 by 125 , asing its factors.

Ann. 324.
Ans. 643.
Ans. 416.
Ans. 1685.
Ance. 1652.
Ane. 798.
To find the true remainder when the ation.
.
Exs. 1. Divide 10183 by 105, using the factors 3, 5, and 7, and And the true remaindes.

## oprantion.

3) 10183
4) 3394
5) $378 \ldots \ldots . . .$.
$\begin{aligned} & 96 \ldots 6 \times 5 \times 3=12 \\ & \times 30\end{aligned}$
$\overline{103}$ true rem.
 183 by 3, wo have a quotiont or 3394, and a romatinder of 1 undividod, which, bring a part of the given dividond, must also bo \& part of the truo remainder. The 3894 being a quotiont arlsing from dividing by 3 , its unite $a$ ano 3 times as great in valuo 20 multiplied by 3 to ohananoit of 4 . As thin 4 is 4 part of the 3384 , it muat bo trae potasinder of 12 aricing from stivide kind of units as the 1 . This makes io a quotiont of 96 and a remaindor of 6 . whioh are 5 timen an great in ralue as thaie 6 is a part of the 678, the units of fure, to ohange this leat romainder 6 , th unite of tha given di ridend, 10183; thereTo multiply it by 5 and 3 , and obtain a true rem te same value as the dividend, ing by 7. Adding the throe partial romaindern aindor of 90 , urisiug foom dividmaindor. Honew, the

$$
\cos
$$ divisors preceding the outiply each partial remainder by all the II Add the aeveral prod witl be: the true ramuinder.

## EXAMPLEE for practice.

2. Divide 3026 by 15 , uoing the factors 3 and 5 , and find the true
3. Divide 34709 by 48, using the fucture 6 and 7 , Ans. 11 . remainder. Ans. 17.

[^17] nt will be the

Ans. 324. Ans. 543. Ane. 416. Ans. 1686. 4ns. 1652 Ans. 798. ins. 2938. 24. 23703.

## the opan

and 7, and
-Dividlog 10 Te a quotiont emaiodor of ieh, bying a on dividond, part of the
The 3394 arlsing from - units are in valuo as 12vo 2 quoit must be s makes 7 , wo have 1e units of 83; thoredividond, oom divid-- true ro-
all the
the sume
he true - 11. he true 17.

DIVISIOM.
4. Divide 5858 by 84 , using the factors 3,4 , and 7 , and find the true remainder.
5. Divide 9078147 by 90 , using the factors 3 Ans. 62. the true remainder. 9, using the factors 3,5 , and 6 , and find
6. Divide 7360481 by 96 , using the factora 27. 27. the true remainder.
7. Divide 10165 by 120, asing the factors 2, 3, Ans. 65. the true remsinder. 8. Divide 63724 by 135, uaing the factore 3,5 , and ans. 85. true remainder.

Case II.-Tu divile a whole number by 10, 100, 1000, ste. (No.37, 1st)
70. Rule.-From the right-hand of the dividend, out off as many figures as there are ciphers in the divisor. Onder the figures so cut off, pluce the divisor, and the whole will form the quotient.

## RXAMPLES POR PRAOTICH.

1. Divide 87 by 10 .
2. Divide 5813 by 100.
3. Divide 7009 by 1000 .
4. Divide 510040 by 10000 .
5. Divide 200371 by 100 .

Case III.-To divide inhen the are of the divisor.

Exr. 1. Divide 85726 by 4500.

## OPERATION.

$45 \mid 00) ~ 857 \mid 26$ (197325. $\frac{\frac{45}{407}}{\frac{405}{226}}$ Remainder.

Analimig. - The factors of 4500 are 100 and 45. First, dividing by 100, (70), wo obtain for a quotient 857, and for a remaxinder 26. Dividing this quotient 1 y the remaining faotor, 45, wo obtain for 2 quotiont 19, and for a remainder 2, to Which annex $2 \beta$, tho first remainder, and underneath write the divisor, and wo have for the entire quotient 19 I98, and
71. Rule.-I. Cut of the ciphers from the divisor, and as many figures from the right of the dividend.
II. Divide the remaining figures of the dividend by the re. maining figures of the divisor.
III. Place the entire divisor under the true remainder, and annex it to the integral part of the quotient, for the entire quotient.

[^18]Drvinox.

## EXAMPLES FOR PRAOTIOR.

2. Divide ss 100 by 6000.
3. Divide 1047628 by 2400 .
4. Divide 72002 by 1200 .
5. Divide 96031425 by 92000 .
6. Divide 1247701 by 47000 .
7. Divide 1703945642 by 4160000 .
8. Divide 460352000 by 8100 .

Ans. $5 \frac{1}{6} 888$. Ans. $436 \frac{1}{2}$ 筑 Ans. . . . IT $^{2} \delta$. Ans. 263978$\}$. 37).

Case IV. -To divide a decimal by 10, 1v0, 1000, etc. (No. 72. Rode. - Remove the decimal point as many places 10 the enough in the number, prefix ciphers.

EXAMPLEB; TOR FraCtion (p. 20 and 21).
Cabs V. -To abridge the division of decimals, when the di visor contains a large number of them. Ex. 1. Divide 675.4563 by 23.54738 , three decimal places.
extending the quotient to

> CONTRACTED OPERATION.
23.54738 ) 675.4563 ( 28.684

$$
\begin{aligned}
\frac{47095}{20450} & =\text { product by } 2,+1 \\
\frac{18838}{1612} & =\text { product by } 8,+6 \\
\frac{1413}{199} & =\text { product by } 6,+3 \\
\frac{188}{11} & =\text { product by } 8,+4 \\
\frac{9}{2} & =\text { product by } 4,+1
\end{aligned}
$$

ANalysis. -In the contracted method we fret ace o
figures the above example will have in the quotienoertain how many places of of the divisor with the entire part of the quotient. Comparing the entire part quotient figure will be of the order of tens, dividend, it is evident that the first two places of whole numbers; and as there and therefore the quotient wii contain mri contain fine figures. Hence, wo divide are to be three places of decimals, it divisor, counting them from the loft toward thirst by five figures of the given and rejecting the figures 38, on the right. the right, thus, using the 23.547 , visor by its quotient figures, wo increase the produltiplying each contracted difigures, as in contracted multiplication of the product by haring regard to rejected By comparing the contracted with the demeans (Case VI, p. 57). the abbreviation, and the agreement of the oren method, we see the extent of Hence, the of the corresponding intermediate results.

[^19]the hows
23. $5 \frac{2}{2888}$.
 - • r ${ }^{2}$ 2639898. etc. (No. ces to the wot figures
the diotient to

ION. tirs part the first contain mals, it - given 23.547, ted di--jected tent of esults.
78. RuL, -I. Compare the significant figure on the left of the diniasir with those on the left of the dividend, and the left of howo muny figures will be required in the quitien, and detormine II. Fior the first contracted di . figures from the left of theted divisor, lake as many significant quirad in the quitient. asiven divisor as there "re places reore place from the right of, at each subsequent division reject
III the rejected figures of by the several quotient figures, aurry from Nomp-Annoz aptore to commoneing the work.

## EXAMPLES TOR PRAOTIOE.

2. Divise 487.24 by 1.003675 , extending the qeotient to 2 decimal placen.
3. Divide 2.3748 by 1.4736, extending the quo Ane. 485.46. decimal place. 4. Divide 3.2682 by 2.4736, and carry the quotient to Ane. 1.611. of decimain.
4. Divile 0.079085 by 0,8337 and to flaces decimal place 0.808 by 0.83497 , and carry the quotient to the fif 6. Divide 8972.436 by 756.3152 , extendivg Ans. 0.09471 . mal placer.
5. Divide 0.4879357 by 0.002963 , extending the Ans. 11.8629 . necond decimal place. 8. Dívide 12193263.1112635269 by 1234.56789 Ans. 164.69. tient to an many decimal places, by 1234.56789 , extending the quonumbern in it.

## DKCIMAL CURRENCY.

74. Decimal Currency is the currency whose denominations increase and decrease in a tenfold ratio.
75. Ourrency is coin, bank bills, treasury notes, etc., in virculation at a medium of trade.
76. Coln is money stamped, and has a given value established by lav.

Norns. - 1. The onrrenoy of the present Dominion of Cenade is dooimai currency; it hed bean effiteti bj cach of the Provinoes before their Federation. 2. Decimat eurrency is also the ourrency of the United States, and is sometimen called Peiforcal Money ; it was established by Congrest in 1792.
77. The prement Oolns of the Dominion of Onanada are of silver and copper.

The silver coins are the fifty-oent piece, the twenty-five-cent piece, the ten-cent pioce, and the five-cent piece.
Nurs.- The ebilling or twenty-oost piece, though still in ofroulation, is no
longer to be ooined.
The copper coins are the two-ent piece and the cent.
100 cents (cts.) make 1 dollar, marked $\$ 1$.
78. The Colins of the United States are of gold, silver, and nickel.
The gold coins are the doublosagle, eagle, half-eagle, quartereagle, three-dollars, and dollar.

The siluer coins are the dollar, half-dollar, quarter-dollar, dime, and half-dime.

The nickel coins are the 5 -cont, 3 -oent, 2 -cent, and 1 -cent pieces.
Nurnes.-1. The mill in not coinod; it in meed only in compntation.
2. To make the motal of coine morr corrioesblo, gold ooing contsin 9 parts by woight of gold and 1 part ex an alloy consiating of oilvor and coppor. Silver ooins oontain 9 parte of dilver mad 1 part of copper.

## table of the dnitid btatis ourzenot.


79. The Dollar is the unit of ourrenoy in the Dominion of Canada and the United States. Accounts are kept in dollars, cents, and milio.

Dimes, o.3nts, and mills, being fraotions of a dollar, are separated from the dollar by the deoimal point ; thus, four dollars two dimes three cents five mills, or fonr dollars two hundred thirty-five mills, are written $\%$. 235.

To exprets any number of cents less than 10, a oipher must be placed between the figure expressing that number and the decimal point; thus, 8 cents is written .08 , or 0.08 .
Niotes.-1. Business won frequemely writo onts as common fractions of $s$ doliar ; thus, $\$ 314$ is aloo writhon $\$ 8.2 f$, road 3 and fify dollara.
2. In bueiness transactions, when thefmal reanlt of eomputation eontains 5 mills or more, they are called ome cont, and when lew than 5 , they sre rejoeted.

## EXAMPLES FOR PRACXIOE.

1. Write fifteen dollarn twenty-three ceciser.
2. Write seven dollars sir cents.

Ans. \$16.23.
3. Write ten dollaras miare cenis.

Ans. \$7.06.
4. Write forty-two ceats.

Ans. \$0.42.

6. Write five dollars eight mills.
6. Write thirty cents.
7. Write one hundred cents.
8. Write one thonsand mills.
9. Write one cent five mills.
10. Write seventeen dollare four mills.
11. Write $\$ 6$ and 7 cents.
12. Write 3 eagles 4 dollars 3 dimes 3 mills.

## REDUCTION OF DECLMAL CURRENOV.

80. Reduction is the process of changing a Humiar of rao denomination to another number of a different denominais I which shall have the same valuc.

We see, $p .64$, that $\$ 1=100$ cents $=1000$ mills; hence the
81. Rule.-I. To change dollars to cents, multiply by 100 ; that is, unnex two ciphers.
II. To change dollars to mills, annex three cirhers.
III. To change cents to mills, anvex ome cipher.

Nore.-Dellars, cents, and mills, exprossed by a single number, are changed to mills by marely removing the decimal point to the right; and dollara and ents, by annexing one eipher and remuving the decitual point to the right.

Conversely,
Rute.-I. To change cents to dollars, divide by 100; that is, point off two figures from the right.
II. To change mills to dollars, point off three figures.
III. To change mills to cents, point off one figure.

## examples for pliadtioe.

1. In $\$ 7$ how many mills?

Analysis.-In $\$ 1$ there are 1000 mills, and in $\$ 7$ there are 7 times 1000 mills
$=7000$ mills.
2. In 356 cents how many dollars?

Analysis. - In $\$ 1$ there are 100 eents, therefore, 1 do of the number of cente -quals the number of dollars; $\frac{1}{100}$ of $356=\$ 3.56$.
3. Change $\$ 464$ to cents.
4. Change 612 cents to dollars.
5. Reduce $\$ 3.10$ to mills.
6. Reduce 35 cents to mills.
7. Reduce 7045 mills to dollars.
8. Change 10426 cents to dollars.
9. Reduce $\$ 4005$ to nills.
10. In 2064 mills how many ceute?

Nota.- We give no separate rules for Decimal currency, since it may be added. subtracted, multiplied and divided in the smine manner as decimals.

[^20]PRA' TTCAL PRORIEMS COMDINING THE FUNDAMENTAL
RULES.

1. A broker hought stucks for $\$ 3729.90$, and sold them for \$H168.135; how much did he gain? 2. If'l month's wages amount to $\$ 35.50$, what will 12 months warem amomat to? Ans. $\$ 426$.
2. It $\$ 7.40$ a barrel, how much flour can be bought for $\$ 111$ ? cost? quarts of strawberries cost $\$ 0.9375$, what will 1 quart 5. A farmer sold an equal number of chickens, Ans. $\$ 0.0625$. for $21: 30$ cents; the chickens at 14 , the ducks at ducks, and geese, 82 conts each; how many of each lind did he at 46 , and the geese at
3. Bonght 144 acres of land for $\$ 5040$, and soll ? 95 Ans. 15 . $\$ 48$ an acre, and the rmand for $\$ 5040$, and sold 95 acres of it at gain by the bargain?
4. A man solil 185 bushels of wheat at $\$ 0.62$ a bushel ans. $\$ 1235$. in payment 80 pounds of sugar at $\$ 0.09$ a pound, 25 peind received at $\$ 0.37 . \mathrm{i}$ a ponnd, and the remainder in cash ; how pounds of coffee he receive?
5. If a gentlenan's income be $\$ 3000$ a year and Ans. $\$ 66.585$.
a day, what will he save at the end of a year, and his expenses $\$ 4.20$
6. A man divided save at the end of a year, or 365 days?
$\$ 130$; and to the second, $\$ 20$ less than persons; to the first he gave the third receive?
7. A lumber merchent Ans. $\$ 120$. what is the price of each $\log$ ? 680 logs for the sum of $\$ 3644.80$; 11. With a Bank note of $\$ 1000$, I paid my taile, Ans. $\$ 5.36$. my shoemaker's of $\$ 75$ and my honserd my tailor's bill of $\$ 348$; lars have I left?
8. If a hat cost $\$ 4.25$, how much will give Ales. $\$ 202$. cost? 13. An army composed of 62100 men on the Ans. $\$ 255$. 13708 men less after the engagement; how the eve of a battle, has in the army?

> Ans. 48392 . 14. Hat is the price of a silver cover, if 15 cost $\$ 117$ ? A. $\$ 7.80$.


Ans. $\$ 380$. again for $\$ 52$; what is his profit? 17. A Danker is to receive $\$ 13950$ in three payments. $\$ 949$. amounting to $\$ 5800$, and the second, to $\$ 4320$ payments; the first amount of the third?
18. A silver cover costs $\$ 19.20$; how much will Ans. $\$ 3830$. ones cost?
19. I bought 150 apples for $\$ 105$ Ans. $\$ 160.80$. \$17.85? $\$ 1.05$; how many ean I buy for 20. A banker received during the first quarter, Ans. 2550. the second. s31940; during the third, $\$ 27674$; duri5t, $\$ 15936$; during $\$ 42769$. He paid out during the whole year $\$ 96843$; during the fourth, much he has left supposing be had $\$ 24375$ in his safe at the bed how of the year?
21. I sold at 65 cents a bushel, 58 bushels of barley tor which I had

## MENTAL

 them for 438.235.2 months' s. $\$ 426$. \$111?
111 quart $\$ 0.0625$. ind geese, le geese at Ins. 15. 3 of it at ch did I $\$ 1235$. 1 received 4 of coffee cash did 66.585. Ises $\$ 4.20$
paid 52 cts. per bushel ; how much did I gain? Ans.
22. Frank was born in 1857, in what year will he be 21 year. old?
23. A father was 34 years old at the birth of his son; Ans. 1878. the age of the son when the father will be 75 years old? Ans. 41.
24. An ommibus able to seat 18 pervons makes 12 trips per lay. how many travellers will it carry in one year of 365 days supposing that there are always 18 persons at each trip? Ans. 78840.
25. If we can buy a yard of tannel for $\$ 1.76$; how many yards of the same quality can be got for $\$ 626.56$ ? Ans. 356 .
26. A pedestrian sets out from Quebec to Montreal, the distance Lejigg 180 miles; he walks during 5 days at the rate of 27 miles per day; required what distance he has yet to go? Ans. 45 miles.
27. Of a certain sum, 82 persons have received each $\$ 24$ and there remains yet $\$ 36.40$; what is that sun? Ans. $\$ 2004.40$.
28. I bought 15 yards of linen at $\$ 0.25$ a yard, 37 gallot." oil at $\$ 1.30$ a gallon, 40 pounds of tea at $\$ 0.80$ a pound, and 108 pounds of coffee at $\$ 0.37$ a pound; required the amount of my Bill? A. \$1 23.81.
29. A bookbinder has 720 volumes to bind at the rate of $\$ 0.18$ a volunie; if it takes him 45 days to do the work: how much will he earn per day?
30. Having bought a barrel of oil contaming 28 gallons, $\$ 2.88$. $\$ 0.75$ a gallon, I lost 7 gallons by leakage and sold the remainder for $\$ 1.20$ per gallon; did I lose or gain and how much ? Ans. Gained \$4.20.
31. Having bought a house for $\$ 3740$ and making repairs for the sum of $\$ 1438$, I wish to sell it so as to gain $\$ 600$ : for how much aust I sell it?
32. What sum of money is required to pay A4 Ane. $\$ 5778$. whom has worked during 28 duys, at $\$ 0.80$ pay 34 wowknen each of 33. I bought 97 barrels of codfish at $\$ 5$ per day? Ans. $\$ 761.60$. 33. I bought 97 barrels of codfish at $\$ 5$ a barrel, I fave 17 barrels to the poor and sold the remainder at $\$ 8$ a barrel. Have I lost or gained and how much ?
34. Louis bought 500 acres of land for the sums. Gained $\$ 155$, $\$ 17876$. He afterwards sold it in lots as follows: 127 acres, at $\$ 47$; $21 \%$ acre at $\$ 96$; and the remainder, at $\$ 37$; how much did he gan br hir. bargain ?
35. Henry receives 45 cents to buy 6 pronds Ame. 814402. pound, and 2 copies at 3 centa a pirse ; what is his change? ceuts a 36. The overcoat of Wilfrid $\cos ^{2} 53$ times as muchange? Julius, which is worth $\$ 2.70$; what is the cost of Wilfrid's owerout of
37. A fruit dealer has received 15 dozen oranges in two broxes ont? of which contains 30 oranges more than the other ; how many ur, one are there in each box?
38. A milliner bought silk in a shop for 36 Ans. 105 and 75 . cents, needlen for 9 cente, un! onton for 18 cents ; afier puying her bull whe has 72 cents left; how much mousy had she? Ans. $\$ 1.55$.
39. What is the dividend when the divimor is 3061 and the quotient 1.055 ?
40. A bubcher sells a pound of meat for 9 eente Ans. 198.965 . spats; what proft does he make on 175 pounde? whioh oost bim 6 spnts; what proft does he make on 175 pounde? Ams. 15.25
41. A person having an income of $\$ 3285$, wishes to lay by $\$ 3$ a day. Requred how much that person can spend daily, the year buing of 365 days. Ans. $\$ 6.00$.
42. A merchant sold 75 yards of cloth at $\$ 2.70$ a yard, and has received in payment 132 yards of linen at 85 cents a yard and a note of $\$ 52.4 C$; how much has he yet to receive? Ans. $\$ 37.90$. 43. What is that number which, being augmented by 85 and divided by 9 , gives 25 for quotient?
14. A millionnaire owes a sum of $\$ 6540$ whin Ans. 140 . date in ten equal payments onu of $\$ 0540$ which he agrees to liquincome is $\$ 5925$; bow much can he apend ten years. His aunual tenth agreed upon?
45. What number must be divided by 37 Ans. $\$ 14.44$. be 13.25 and the remainder 0.35 ? 46. At 39 cents a pound, how much must be paid Ans. 490.60. wool, each bale containing 317 pounds? 47. If a pair of loots be sold for $\$ 3.16$; how much. $\$ 1112.67$. for 20 boxes, each containing 60 pairs? 48. How much will 3550 laths cost at 22 cents per Ans. $\$ 3792$ 49. How many barrels of apples containing 3 per hundred? cents a hushel can I buy for 8 to. 50 ? 50. A literary work consists of 6 volumes; Ans. 27 barrels. are 560 pages, in each page, 42 lines, and in in each volume there How ing, ters, and if 5 blers are there in the work, if it is divided into 60 ohsp, 1 if 5 blank lines are left between each chapter?
s136.50? How many cords of wood at $\$ 3.25 \overline{\mathrm{a}}$ cord did I buy for 52. Sold 20 pounde butter for $\$ 3.80$, how muc. Ans. 42. come to at the same price? 53. A cabinet-maker has earned $\$ 45$ in a certain Ans. \$11.21. ay working; had he worked 9 days more, he would have of days $\$ 67.50$; how much did he earn per day? 54. The sum of two numbers is 2458 , and their difference, 154 what are the two numbers?
55. When a son, who is now 30 years. 1306 and 1152. 35 and his mother 19 . what are years old, was born, his father was mother?
56. Having some money at my disput Ars. 65 and 49. the rate of $\$ 1750$ each, and 19 shares of Bank ing two farms at slare, and I have $\$ 113$ left; shares of Bank Stock at $\$ 103$ per mand $?$
57. In selling cloth for 8610 , a merchant gained as oloth cost him, less $\$^{\prime} 10$; what was the cost?
58. Although I wae robbed of $\$ 25$, yet atter having paid $\$ 5$ which I owed, I have $\$ 17$ left; how much money had I?
by $\$ 3$ a the year $\$ 6.00$. and has ad a note b37.90. id divided s. 140. to liqura aknual ying the 14.44.
ent may 90.60. bales of 12.67. be paid ;3792. d? h at 50 trrels.
ne there lettera. 50 ahap. buy for o. 42. pounds 1.21. of days earned 2.50 . 154, 152. cer was er and 149. rms at 3 per com570. us the 655. \$546

## BILLS AND ACCOUNTS.

82. A Bill, in business transactions, is a written statement of articles bought or sold, together with the prices of each, and the whole cost.

Nores,-1. The party who buys, or who receives money, goods, or services, etc., from another, is a Dettor ; sud the party who sells, or who parts with money, goods, etc., is a Creditor.
2. A bill of goods bought or sold, or of services received or rendered at a single transaction, and contsining only ons date, is often called a Bill of Pareela.
83. An Account is a registry of debts and credits.

Notes.-1. An account ehould always contain the names of both parties in the transaction, the price or value of each item or article, and the date of the traneaotion.
2. Acoounts may have only one side, which may be either debit or oredit; or it may have two sides, debit and oredit.
84. The Balance of an Account is the wifference between the amount of the debit and credit sides.
85. An Account Current is a full copy of an account, giving eaoh item of both debit and credit sides to date.

Nore.-An account onrrent hiving only one side is sometimes oalleci a Bill of Items.
86. An Invoice is a full statement in detail of goods sent to a purchaser or agent at the time the goods are forwarded, giving the marks and contents of each package, the charges paid, and how sent.
87. The Footing of a Bill is the total amount or cost of all the items.

Notrg. -1. When a oreditor receives the amount of a bill or an account ourrent, he acknowledges it to be paid by writing fit the bottom of the bill or asoount "Received Paynenc," and signing his name. If tho payment be made to a person authorized by the creditor to receive it, he should receipt the bill or account by writing the oreditor's name first and his own name under it, as in Form I.
2. Bills and sonounts are sometimes paid by the debtor giving to the creditor a promiseory note for the amount.

In the following bills and accounts the abbreviations are:

Dr. for debit or debtor. Cr. for credit or ereditor. yd. for yard. doz. for dozen.
bbl. for barrel.
bush. for bushel.
lb. for pound.
cwt. for hundred weight.
82. What is a Bill ?- What is meant by debtor and oreditor? - By a Bill of Paroels 9-83. What is an Acoount ?- 84. The Balance of an Account ?-85. An Aovoume curront 7- $A$ Bill of Itoms f- 88. An Invoien f-87. The Yooting
(Form 1.)
Mr. G. Murrat,
Kingston, Sept. 8, 1870.
Bought of E. P. Healet \& Co.


Received Paument,

> E. P. Healey \& $\mathrm{Co}_{\Perp}$ per N. Ryan.
(Form 2.)

Mr A. Seymour,
Montreal, Sept. 17, 1870.
Bought of T. McGreevy \& Co.


Mr. I
L. Jat
1870.

July
Aug.
1870.
(Form 3.)
Quebec, June 2, 1870.
Mr. D. Johnson,
Bought of Byrne, O'Brien \& Co.
: \& Co.

## $\int_{\$ 158 \mid 45}$

1870. 

July
Ang.
S-nt $\quad 4$


## Received Payment,

W. Peice \& Som.
D. S. R. TATLOR \& Co. in \% eurrent with O. Lyons \& Sox.


VIZ.: suger
2. 1 L. NO 8! 17 in lt
6. W. tobacco, 18 cts. 45 gallon balance

## On Form 1.

1. Soid ip fontreat, Fel: 2, 1870, by John Hogan, to Mr. A. Larue, viz. : 7 lbs . Qugerlet at at 25 cts ; 15 lbs . candles, at 22 cts ; 12 lbs . sugar, at 10 ata.; $18 \$ 1 \mathrm{dst}$. flour, at 24 cts . Footing of the bill, $\$ 11.17$.

## On Form 1.

2. Edinoyd the of Kingaton sold to T. Lee, Feb. 10, 1870, and I. Norris, his watht, collected the amount of the bill: 15 lbs . butter, as : 17 cts. ; 25 I (let.chleede, at 20 cts ; 750 lbs . maple sugar, at 9 cts ;


## On Form 2.

3. James (0)

 Footing of the bill, $\$ 160.69$.

## On Form 4.

4. Messre. B. Sharle d Co., Ottawa, sold to D. Hall; Feb. 12, 1870, 110 pair thine boots, at $\$ 3.75$; 28 pair buskins, at 86 cts.; Teb. 20, 40 pair Alpphetw, at 85 cts. ; March 2, 67 pair gaiters, at $\$ 1.15 ; 120$ pair boyje brogans, at $\$ 1.25$. On this are the following credits: Feb. 27, 16y adit, \$280; March 15, 110 boxes lemons, at \$3.20. What balatef wit due B. S. \& Co., March 23, when the account was sothtid?

Ans. \$65.63.

## On Form 5.

5. L. A. Conagy Co.; Ottawa, sold to G. Morin \& Bro., Jan. 2, 1870, 17 yds. brgatabth, at $\$ 5.2 \mathrm{j}$; Jan. 15, 29 yds. cassimere, at $\$ 1.62$; Feb. $\%, 60$ d 10 . bleached shirting at 17 cts. ; Feb. 7, 49 yds. ticking, at 27 cta... Fetb. 1 Lo $_{5}, 18 \mathrm{yds}$. blue cloth at $\$ 3.19$; June 17 , 27 yds. gray cloth, att 28.75 ; Aug. 3, 75 jds. flannel, at 61 cts. Remitted by G. Morp e Co. in part payment, as follows: Jan. 28, 1870, cash, 83 ; fhthe $\tilde{\nu}_{5}, 14$ bbls. Ontario Flour, at $\$ 7.20$; and
 What was the appritet of the note?

Ans. $\$ 153.28$.

## On Form 2.


 18 cts ; 54 lbe. shgar, at $12 \mathrm{cts}$. ; 20 lbs. soap, at 14 cts ; April 2,
 balance was due W.' B.; April 8 ?

Ans. \$36.65.

## On Form 3.

7. Sold, May 2, 1870 by L. T. Nolan, dealer in fruits, to R. 8 . Lemoine, Toronto: 32 bble. Montreal apples, marked 4, at $\$ 2.95$; 56 bbls. Greenings, marked 5, at $\$ 2.25$; 16 bbls. Harveys, marked 6 , at $\$ 1.80 ; 40$ bbls. Russete, marked 8, at $\$ 2.75$; paid $\$ 7.50$ for pack ing, and $\$ 13.40$ for transportation. Find the amount of bill. Forwarded by the "Western Line." Ans. $\$ 380.10$.

## On Form 1.

8. G. A. Parker of Quebec, sold to S. Montigny, May 6, 1870 : 20 lbs . Rio coffee, at 24 cts. : 50 lbs . W. I. sugar, at 7 cts.; 75 lbs. Pearl starch, at 13 cts.; 12 gallons syrup, at 65 cts. ; 90 lbs . butter crackers, at 9 cta. ; 54 lbs. picnic crackers, at 11 cta.-Footing of
the bill, $\$ 39.89$.

## On Form 5.

9. Philip Doyle, grocer, Toronto, sold to W. Morris \& Co. : June 11, 1870,473 gallons alcohol, at 95 cts.; 308 gal. old rum, at $\$ 1.90$; 610 gal . Holland gin, at $\$ 1.05$; Aug. 5, 207 gal. rum, at $\$ 1.75$; 119 gal. cognac, at $\$ 2.10$; Sept. 22, 401 gal. Scotch gin, at $\$ 1.15$. On this the following payments were made by W. Morris \& Co.: Oct. 4, 30 bbls. salnion, at $\$ 8.75$; Nov. 6, cash, $\$ 520$; Nov. 22, dratt on London, at 30 days, for the balance due P. D. What was the amount of the draft?

Ans. $\$ 1965.85$.

## On Form 4.

10. Mr. P. I. Gordon, Kingston, sold to J. Kelly: June 15, 1870 , 23 yds. silk, at 95 cts.; 15 yd. ribbon, at 45 cts.; 12 yds . muslin, at 18 cts. ; July 10, 4 yds. blue cloth, at $\$ 3.60 ; 3$ yds. broadcloth, at $\$ 4.50 ; 9$ yds. doeskin, at $\$ 1.25$; 1 cravat, $\$ 1.30$; Aug. 15,5 pair boots, at $\$ 6.50 ; 3$ doz. hose, at $\$ 2.40 ; 1$ doz. sleeve buttons, 50 cts. On this are the following credits : July 20 , by 3 bbls. green apples, at $\$ 3.20$; 15 bushels potatoes, at $22 \mathrm{cts}$. ; Aug. 20, by cash, $\$ 7.30$. What balance was due P. I. G., Aug. 24, when the account was settled ?

Ans. $\$ 91.21$.

## On Form 2.

11. O. J. Larxin tuaght of R. Hamilton \& Co., Montreal : May 12, 1870,18 plows, at $\$ 11 ; 23$ handsawe, at $\$ 3.50 ; 90$ spades, at 86 cts.; May, 30,86 shovels, at $50 \mathrm{cts} ; 46$ cwt. iron, at $\$ 12$; June 7.14 hammers, at 62 cts.; 12 mill-saws, at $\$ 12.12$. June 7 , credited by cash, $\$ 140$; June 15 , credited by cash, $\$ 375$. What balance was due R. H. \& Co., June 16 ?

Ans. $\$ 590.02$.

## On Form 3.

12. Invoiced by Lu Casey \& Son of Halifax, to A. C. Samson, May 4, 1870: 12 cratee Antwerp ware, marked 6, at 8175 ; 43 casks Roung
tllon
!llon wine, marked 9 , at $\$ 99$; 19 bbls. superfine flour, marked 10 , at $87 ; 23$ bhls. peas, marked 3, at $\$ 1.52$; 42 chests black tea, marked 5, at $\$ 17.50 ; 37$ chests gree 1 tea, marked 1, at $\$ 2.3 .75$; cooperage, $\$ 1: \%$; cartaye, $\$ 6.80$; Insurance, $\$ 32.50$. Forwarded by the "Maine Lixpress Line." Amount of Invoice, $\$ 3193.01$.

## On Form 4.

13. Measrs. Hall \& Brothers, St. Joinn, N. B., sold, June 1, 1870, to 1'. N. Walsh, 15260 lbs . pork, at $5 \frac{1}{2}$ cts.; 7215 j lhs. cheese, at $8 \frac{1}{2}$ ct.. ; July 3, 11521 bushels corn, at 50 cts. ; July 10,1560 bbls. Honr, at $\$ 6.12 \frac{1}{2}$. On the above are the following credits: June 25, by 1150 lbs . cotton, at $6 \frac{1}{4} \mathrm{cts}$; June 30, by cash, $\$ 750$; July 12 , 8256 llg . maple sugar, at 7 cts . $; 6450$ gallons molasses, at $37 \frac{1}{2}$ cts. What is the amount of cash requisite to balance the account on July 13 ?

Ans. $\$ 12953.78$.

## On Form 2.

14. B. C. Willis, bought of A. Murphy \& Co., publishers, Montreal : Aug. 4, 1870,75 Juneau's Mental Arithmetic, at 15 cts.; 50 Smith's Practical Arithmetic, at $37 \mathrm{cts} ;$.2 doz. Miller's Reader, at $\$ 4.50$; Aug. 12, 60 Ilenry's Grammar, at 7 cts. ; 36 Kerney's Compendium of History, at 72 cts. ; Sept. 1, 30 Walkingame's Primary Algebra, at 18 cts.; Sept. 1, credited by 50 Commercial Arithmetic of the Christian Brothers, at 40 cts. What balance was due A. M. \& Co., Sept. 2 ? Ans. \$54. 27.

## On Form 5.

15. S. N. Kelly bought of H. Hamel \& Co., Quebec, Feb. 3, 1870 , 18 yds. cambric, at 14 cts. ; 60 yds. calico, at 42 cts . 39 yds . cassimere, at $\$ 3.75$; March 10, 37 yds cotton, at 35 cts ; $6 \mathrm{yds}$. velvet, at s. 4.70 ; May 2, 30 yds . linen, at $\$ 2.65$; May 4, 24 yds. merino, at 75 cts . S. N. Kelly's credits are : April 1, 50 lbs. collee, at 25 cte.; April 9, 7 cords of maple, at $\$ 3.50$; May 20, dratt on Halifax, $\$ 78$; June 25, 1 gal, oil, $\$ 1.50$. What balance was due Hamel \& Co., June 26, 1870 ?

Ans. $\$ 196.12$.
Lee the pupils make out Bills or Accounts, as the case may be, in proper form, from the following.
16. Andrew Whelan of Three Rivers, sold to John Gussehn, July 5, 1870, and I. Kane, his clerk, collected the amount of the bill: 36 lbs . maple sugar, at 13 cts. ; 16 lbs . coffee, at 15 cts ; 13 lbs. tea, at 98 sts.; 13 lbs. chocolate, at 61 cts. 7 lbs. ginger, at 17 cts.; 47 lbs . cheese, at 9 cts.; 12 lbs pepper, iot $19 \mathrm{cts}. ; 20 \mathrm{lbs}$. butter, at $16 \mathrm{cts} ; 2$ gal. vinegar; at 68 cts. Footing of the bill, $\$ 40.01$.
17. Forwarded per the Eastern Line, June 3, 1870, by B. Ellis \& Co., Ottawa, to S. T. Garneau. Quebec : 18 pair worsted stockings, No. 6, at 90 cts.; 15 doz. napkins, No. 10, at 47 cco. : 24 pair men'e

## BILLS AND AOOOUNFS

kid gloves, No. 7, at 85 cts.; 20 doz. womer', 75 cts. ; 12 pair silk stockings, No. 16, at. $12.25 ;$ puir thread atockinge, No. 11, at $\$ 1.12 \mathrm{t}$. Paid for cantager, io cls. ; char es for packing, $\$ 1.60$. S. M. 0 'Reilly, Amount $\$ 101.95$. thier : 278 lbs . coffee, Reilly, Montreal, A pril 10, 1870 , to A. Gauham, at 11 cts.; 1540 lbs corned 1270 lbs . lard, at 13 cts. ; 800 lbs . 17 cts ; 217 lbs. maple sugar, at 7 ceef, at 8 cts ; 750 lbs . butter, at 150 bushels oats, at 65 cts ., at 7 cts. ; 126 doz. eggy, at 12 cts . 19. Sold in Toronto, A uril 20 1870 Footing of the bill, 87 si .6 s . Julia Meredith, and the bill paid: 3 doz. silvar Chainbers, to Mrs. 2 doz.; 2 doz. silver table spoons, at $\$ 35$ a doz ; able forks, at $\$ 43.75$ spoons, at $\$ 18.50$ a doz.; $1 \frac{1}{2}$ doz. ivory handlo; $2 \frac{3}{4}$ doz. silver teadoz.; 1 gold guard chain, at $\$ 136$. 20. P. Barry \& Son, at \$136. Footing of the bill, \$394.75. as follows: 2 loaves flour, at $\$ 7.80$; 91 white sugar, 52 lbs., at 15 cts.; 4 bble. extra $\because$ lbs. black pepper ${ }^{2}$. cheese, at 16 cts.; 15 lbs . raisiny, at 15 cts. peas, at 70 cts.; 5 bush. beaus, at $\$ 1.10$. 14 , at 23 cts; 3 bushels 1 gal molasses, 60 cts . 21. M. Peter Nelson owes D. I. Hooting of the till, $\$ 60.83$. 5, 1870, 3 gross shirt-studs, at 85 Hogan, Toronto, as follows: June stockings, at \$3.181; 3 doz. shirt fret. June 17, 15 doz. woolen ribbon, at 25 cts.; 30 pair silk gronts, at $\$ 5.05$; Aug. $2,12 \frac{1}{2}$ yds. at $\$ 2.85 ; 224$ yds. ticking, at 45 gloves, at $\$ 1.37 \frac{1}{3} ; 4$ doz. linen towels, 22. G. Turner \& Son, Quebec ${ }^{2}$. Footing of the bill, $\$ 131.37 \frac{1}{2}$. 17 pair boots, at $\$ 3.00 ;$ March, sold to A. I. Green, March 6, 1870 , 80 pair hose, at $\$ 1.20$; 23 pair 18, 19 pair shoes, at $\$ 1.08$; April 9 , A. 1. Green, the following pair gloves, at 75 cts. They received of 20 cts. ; 10 Third Readers, atedits: April 5, 27 Second Readers, at at \$4.75; 19 Golden Manuals $\$ 3.90$; May 11, 7 Brown's Dictionaries, cts. The balance due G. T. \& St $\$ 2.93 ; 20$ Christian Duties, at 37 amounted to $\$ 44.05$. 23. Sold by Sinith \& Watters, Kingston, July 24, 1870, to O. S. Peters: 275 bbls. Patapsco flour, at $\$ 7.16 ; 150$ bbls. Ontario flour, at $\$ 6.25 ; 170$ bbls. Chicago flour, at $\$ 5.87 \frac{1}{3} ; 214$ bushels corn, at 82 cts.; 326 bush. wheat, at $\$ 1.62 \frac{1}{2} ; 300$ bush. vais, at 91 ct 30 ; 24. Joseph R. Simon, $\quad$ Footing of the bill, $\$ 5413.48$. 1870, as follows: 5 yds. bought of C. T. Adams, Montreal, April 20, $\$ 5.50$; Trimings, $\$ 3.75 ; 3$ cloth, at $\$ 3.50 ; 1$ satin waistcont, gray fringe, at 68 cts.; 3 ; 3 yds. yellow linen, at $19 \mathrm{cts}. ; 11 \mathrm{yds}$. eassimere, at $\$ 2.25 ; 7$, yds. al of ribbon, at 31 cts.; 3 yd. blact 101 cts. $; 3$ skein silk thread, alpaca, at 55 cta.; 16 yds. cat: sc, 9 yds. white tlannel, at 90 cts. ; 2 cravats 4 yds. wadding, at cts., baize, at 58 cts.; 6 cotton chirte, at cravats, at $\$ 1.12 \frac{1}{2} ; 4$ yde green cts. ; 10 yds. muslin, ot $1+$ ctsts, at $65 \frac{1}{2}$ cts. ; 5 yds. merino, at 80 25. Sold by P. Mayrand \& Co., Hel Footing of the bill, $\$ 70.01$. follows: June 8, 1870, 4 pieces muslinaz, to Ed. O'Neil, grocer, an

pleces serge, 20 cm paid in the ace

To. 2, at thread ar es for 01.95. 1. Gau800 lbs. utter, at 2 cts . A.OS. o Mrs. $\$ 43.75$ er tea37.50 4.75. 1870, extra 5 cts. ushels 6 cts. ; roolen 1 yds. owels, $37 \frac{1}{2}$. 1870 ril 9 , ed of rs, at aries, at 37 1870,
). S. lour, , at ct ${ }^{\circ}$; 18.

120 , coci, yds. larl
precen Dutch linen, each 30 yils., at 70 cts. a yard; July 10,11 pieces werge, eweh 19 ydmo, at 56 cts. ; Aug. 6, 1750 gids. Low 11 cotton. at 20 ctm ; 371 yilm. Manchevter stuffe, at $25 \mathrm{cts}$. July 39, E. O'Neil, paid in parl 粠保. What balance was lue P. M. \& Co., Aug. 2, when the acesint wan male ont? Ans. $\$ 1284.16$.
26. Mexarn. F'raser, O'Dunnell \& Co., wholesale dealers, Montreal, mold u, Dhesil \& Lane: Aug. 4, 1870, 18 fine Iress coats, No. 52, at $\$ 27.810$; 46 cashm, men's Huck wool hats, No. 22, at $\$ 12.50$ per loz. ; $\frac{1}{3}$ doz. men's Pearl hate. No, 64 at $\$ 27$ per doz. ; 5 unlorellas 28 -in., at $\$ 1.75$; Oct. 12, bja\%. bieeris white cottun hose, No. 7, at \$2.60 per doz. ; 3 blackalcather valises, No. 72, at $\$!.50$. On this are the filluwing eredtu: Scpt. 10, by cash, $\$ 100$; Sept. 30, by cash, \$150; Oct. 7, by 50 lushelx esern, at $65 \mathrm{cts}$. . What halance was due F. O'D \& Co., Oct. 18, when the accomit was setcled? ans. 821.55.
27. Bromht of J. R. Williamo. Quebec, by H. S. Connolly : June 3, 1870, 7 : If, , maple sug ir, at $6 \frac{1}{4} \mathrm{cta} ;$.9 lbq. green tea, at bis cts. ; 21 gals. maple nyrup, at 70 cts ; July $1,12 \mathrm{lbs}$. pepper, at $25 \mathrm{cts}$. ; 10 lbs. иpices, at 20 ctu ; 12 lbs . ginger, at 18 cts ; 15 lbs . coffee, at
 peaches, at 124 cta. ; 2 bushela onions, at 80 cts.; Aug. 1, 13 lbs . mackrel, at $\mathcal{K}$ cto. ; 9 liba smoked herrings, at 20 cts. ; Ang. 10, 25 Ibw. zicu, at 5 cth.; 12 lb . Iried beef, at $12 \frac{1}{2}$ cts.; Sept. 4, 5 bush. corn mal, at so cts. ; 5 follks table salt, at 20 cts ; $17 \mathrm{lb} . \mathrm{l}$. sorla cracker, at 3 cts . Amount of the bill, son2.24, which was paid to L. R. Williarrom, Sept. 7.

2\%. Sulif by l. "! rulel, Montieal, to J. B. Poston, as follows: Oct. - 0 , 1670, 48 pair ungat, at 37 cts. ; 2: doz. pewter-polished bitw, at $85^{5} \mathrm{cts}$. per digz. $; 56$ doz. hinges, at i to. per doz.: Nov. 3,32 doz. curry-combe, at $45 \frac{1}{2}$ cts. a doz. 20 , ketw shoemakers' awls, at 68 cts, per packet; Nov. 12, 75 packet- $3 \frac{1}{2}$ in. sucrews, at 95 cts. per packet. L. 'Trisfel receivel of J. B. Puston on accuunt : Nov. 8, 2 caske Medoc wine, each 45 gal., at 50 cts. per gallon; iuc. 5, carth, 850. What balance was due L. T., Dec. 6? Ans. sise. 79
29. Invoiced hy D. Molson, Queljec, to V. R. Lewis, Ottawa, F'er 1, 1870 : \% canen calf boots, No. 3, each 67 pairs, at 33.75 ; 4 cases thick boov, No. 4, each 54 pairs, at 2.62 ; 2 cases gaiters, No. 7, earh 75 mairn, at \$1.12; 2 cases buskine, No. 10, each 27 pairs, at ©6 cts.; 2 camen plippers, No. 14, each 35 pairs, at 70 cts.; 2 cases rublorr, No. 18, each 50 pairs, at $\$ 1.04$; charged for packing, cartage, etc., $\$ 3.9 \%$.
30. N. P. Morrie \& Co., Halifax, sold Foting of the bill, si439.76. 1870, 60 yiln. print, at $12 \frac{1}{2}$ cta. ; 15 yds. ca U. S. l Brown, Sept. 7, cassinuere, at $\$ 1.60$ : Sept. $25,3.3$ vils, sheetince, at 9 cts. ; 6 yds. valvet, ut \$\%.011; 63 yds. broadclotin, at $\mathbb{S} 4.37 \frac{1}{2}$, Oct 29.30 yards
 the following credit": NOV. 1, by 22 lbs . butter at 20 cts : fill are cherry wud, at $\$ 3.100$; Dec. 4 , by cash, 816.00 ; i)ec. if, by cords lalor, at \$1.50. What balance wes due N. P. M. \& Co dey Whop the scentint wat metled? Ane, $821.76^{3}$

## PROPERTIES OF NUMBERS.

## EXACT IIVRSORS AND PRIME NUMBERA.

\$8. An Exact Divisor of a number is one that divides it without a remminder, or which gives an integer for the quotient.
89. All numbers are either even or odd.
90. In Even Number is a number of which 2 is an exact divisor ; as 2, 6, 8, 24.
91. An Odd Number is a number of which 2 is not an exact divisor ; as $1,3,7,15$.
Every number must be either prime or composite.
92. 1 Prime Number is one which can not be resolved or separated into two or more integral factors; as 1, 3, 5, 7.

Notss.-il. All prime numbers except 2 are odd numbers.
2. Numbers are prime to eaoh other, When they have no 00 m

7 and 13 are prime to each other, as are also 4, 11, and 15 .
D3. A Composite Number is one that has other exaet divisors besides 1 and itself; as 6,9,14.
94. The Prime eactors of a number are its exaots divisors; thus, 1,3 , and 7 , are factors of 21 .
95. The Power of a number is the product obtained by $t$ tiking tise number it certain number of times as a factor; thus, 16 is a power of 4 .

Note. - When the nu nber is taken onoe, it it oalled its first power; when taken twice, as a faotor, the produst is called its second power; and so on.
96. The Exponent of a power is a figure written at the right of a number, and a little above it, to show how many times it is taken as a factor; thus, in the expression $5^{2}$, the exponent is 2 , and the whole is read 5 second power.

From these principles,
1st. Any number which will exactly divide one of two numbers will divide their product.

2nd. Any number which will exactly divide each of two numbers will divide their sum.

3rd. Any number which will exactly divide each of two numbers will divide their difference.

[^21]
## FAOTORING

## We derive the following properties:

I. Tioo is an exact divisor of all evelt unmbers.
11. Three is an exact divisor of every number the sum of whose digits it will extetly divide.
III. Four is an exact divisor when it will exuotly divide the tens und units of a number.
JV. Five is an exact divisor of every number whose unit figure © 5.
V. Six is an exact divisor of every even number, the sum of whose digits it will exactly divide, or that 3 will exuctly divide.
VI. Eight is an exact divisor when it will exactly divide the hundreds, tens, and units of a number.
VII. Nine is an exact divisor when it will exnotly divide the sum of the digits of a number.
VIII. $T e n$ is an exaet divisor when 0 oceupies the units' place.
IX. Eleven is an exact divisor of every number whose sum of the digits, standing in the even places is equal to the sum of the digits standing in the odd places.

TABLE OT PRIME NUABELS FHOM 1 TO 1109.

| 1 | 59 | 139 | 233 | 337 | 439 | 557 | 653 | 769 | 883 | 1013 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 2 | 61 | 149 | 239 | 347 | 443 | 563 | 659 | 773 | 887 | 1049 |
| 3 | 67 | 151 | 241 | 349 | 449 | 569 | 661 | 737 | 907 | 1021 |
| 5 | 71 | 157 | 251 | 353 | 457 | 571 | 673 | 797 | 911 | 1031 |
| 7 | 73 | 163 | 257 | 359 | 461 | 577 | 677 | 809 | 913 | 1033 |
| 11 | 79 | 167 | 263 | 367 | 463 | 587 | 683 | 811 | 929 | 1039 |
| 13 | 83 | 173 | 269 | 373 | 467 | 593 | 691 | 821 | 937 | 1049 |
| 17 | 89 | 179 | 271 | 379 | 479 | 599 | 701 | 823 | 941 | 1051 |
| 19 | 97 | 181 | 277 | 383 | 487 | 601 | 709 | 827 | 947 | 1061 |
| 23 | 101 | 191 | 281 | 339 | 491 | 607 | 719 | 829 | 953 | 1063 |
| 29 | 103 | 193 | 283 | 397 | 199 | 613 | 727 | 839 | 967 | 1069 |
| 31 | 107 | 197 | 293 | 401 | 503 | 617 | 733 | 853 | 971 | 1087 |
| 37 | 109 | 199 | 307 | 409 | 509 | 619 | 739 | 857 | 977 | 1091 |
| 41 | 113 | 211 | 311 | 419 | 521 | 631 | 743 | 859 | 983 | 1093 |
| 43 | 127 | 223 | 313 | 421 | 523 | 641 | 751 | 863 | 991 | 1097 |
| 47 | 131 | 227 | 317 | 431 | 541 | 643 | 757 | 877 | 997 | 1103 |
| 53 | 137 | 229 | 331 | 433 | 547 | 647 | 761 | 881 | 1009 | 1109 |

## FAC'TORING.

₹i. Casw ..-To resolve n number into its prime factors.
Notr.-The process of factoring numbers depends upon the following prin. oiples:
I. Every prime faotor of a number is an exact divisor of that number.
II. The only exact divisors of a number are its prime factors, or some comblnations of its prime faotors.
E.c. What are the prime factors of 1596 ?


98 Rule.-Divide the given number by the smallest prime factor; divide the quotient in the same manner, and so continue the division until the quotient is a prime number. The several divisors and the last quotient will be the prime factors required. Proof. TI : product of all the prime factors will be the given number.

## examples for pradtioe.

Required the prime factors of

1. 28. 

$\begin{array}{ll}\text { 1. } 28 . & \text { Ans. 2, 2, } 7 . \\ \text { 3. } 36 . & \text { Ans. } \\ \text { 3. } 86 . & \text { Ans. } \\ \text { 4. } 144 . & \text { Ans. } \\ \text { 5. } 360 . & \text { Ans }\end{array}$

$|$| 6. 1140. | Ans. |  |
| :--- | :--- | :--- |
| 7. 3420. | Ans. |  |
| 8. | 2445. | Ans. |
| 9. | 2431. | Ans. |
| 10. 2205. | Ans. |  |

99). Cask II.-To find the prime factors common to two or more numbers.

Ex. What are the prime factors common to 84, 126, 2 id 210 ?

$$
\begin{aligned}
& \text { operation. } \\
& \begin{array}{l|lll}
2 & \frac{84,}{} & 126, & 210 . \\
7 & \frac{12,}{} 14, & 63, & 105 \\
\hline & 21, & 35 . \\
\hline 2, & 3, & \frac{35}{6 .}
\end{array}
\end{aligned}
$$

tors common to $84,1 \cdots$, and 210 . prime number which is an exact divisor numbers by the smallest II. Divide each set of motien divisor of each. become prime to each other. prime fuctors.

[^22]Notes thare is a

## examples for practiog.

Required the prime factors common to

1. 12 , and 24 .
2. 48,96 , and 120 .
3. 42,63 , and 105 .
4. 225, 435, and 540.
5. 48, 72, and 96.
6. 140, 210, and 280.
7. 252,336 , and 420 .
8. 960,1568 , and 5824 .
9. 330, 495, and 165.
10. 2340, 11934, 12987, and 14859.

## CANCELLATION.

101. Canceilation is the process of rejecting equal factors from numbers sustaining to each other the relation of dividend and divisor.
E.c. 1. Divide 112 by 56.

$$
\frac{112}{56}=\frac{8 \times \frac{\text { Operation. }}{8 \times 8 \times 2 \times 2}}{8 \times 2}=\frac{2}{1}=2
$$

Ans. 2, 2, and 3.
Ans. 3 and 7.

Ans. 2, 5, and 7.
102. Rule.-I. Write the dividend above and the divisor below a horizontal line.
II. Cancel all the factors common to inth dividend and diviont.
III. Divide the product of the remaining factors of the dividend by the product of the remaining factors of the divisor, and the result will be the quotient.

## EXAMPLES FOR PRACTIOE.

3. $16 \times 24 \times 48 \div 32 \times 36 \times 38=$
4. $12 \times 7 \times 5 \div 2 \times 4 \times 3$.
E. $16 \times 5 \times 10 \times 18 \div 8 \times 6 \times 2 \times 12$.
f. $84 \times 12 \times 18 \div 21 \times 24 \times 9$.
'. $72 \times 18 \times 16 \div 24 \times 16 \times 9$.
5. $22 \times 9 \times 12 \times 5 \div 3 \times 11 \times 6 \times 4$.
6. $76 \times 34 \times 96 \div 17 \times 51 \times 32$.
7. 10 ,
8. 15
9. 3 ,
10. 21 ,

Ans. ${ }^{8} 9^{\circ}$
Ans. $17 \frac{1}{2}$.
Ans. $12 \frac{1}{2}$.
Ans. 4.
Ans. 6.
Ans. 15.
10. $25 \times 7 \times 14 \times 36 \div 4 \times 10 \times$
1.1. $184 \times 145 \times 80 \div 23 \times 29 \times 80$.
12. $28 \times 27 \times 21 \times 15 \times 18 \div 7 \times 54 \times 7 \times 3 \times 4$.
13. $12 \times 5 \times 183 \times 18 \times 70 \div 3 \times 14 \times 9 \times 5 \times 20 \times 6$.
14. $213 \times 84 \times 190 \times 264 \div 30 \times 56 \times 36$.

## DIVISORS OF NUMBERS.

103. A Common Divisor or Measure of two or more numbers is any number that will exactly divide each of them.
104. The Greatest Common Divisor of two or more numters is the greatest exact divisor of each of them.
105. General principles.-1. One is a divisor of all integers.
II. Every number is a divisor of itself.
III. Every prime fuctor of a number is a divisor of that number.
IV. E'very product of any two or more prime factors of a number is a divisor of that number.
V. Every number equals the product of its prime fuctors.
VI. A number has no divisors except its prime factors and the product of every two or more of them. Hence, the product of all the prime factors common to two or more numbers is their greatest common divisor.

## COMMON DIVISOR.

106. To find a common divisor of two or more numbers.
E.x. Required a common divisor of 9,15 , and 21 .

OPERATION.
$9=3 \times 3$
$15=3 \times 5$
$21=3 \times 7$

Analysis. - We resolve each of the given numbers into two factors, one of which is cominon to all of thom. In the operation 3 is the cominon factor, and is therefore a common divisor of the numbors.
107. Rule.- Resolve the given numbers into their prime factors, then if any fuctor be common to all, it will be a common divisor.
103. What io a coman divisur ?-104. What is the greatest common divisor ?

Ex. Required the greatest common divisor of 117 and 1365.
operation.
117) 1365 (11 $\frac{117}{195}$
$11 \pi$

$$
\begin{aligned}
& 7 \overline{78}) 117(1 \\
& \left.\frac{78}{39}\right) 78(2 \\
& \frac{78}{0}
\end{aligned}
$$

common divisor of 117 and 1365 .

Analysis.- Since 117 is the greatest divisor of 117 , if it be a divisor of 1365 , it will be their greatest oommon divisor. By trial, 117 is found not to bo a divisor of 1365 , since there is a reinainder, 78 .

If 78 , the greatest divisor of itself, is a divisor of 117 , it is the greatest common divisor of 78 and 117, and also, of 117 and 1365. (111, IV.) By trial, 78 is found not to be a divisor of 117 , since there is a remainder; 39.
If 39 , the greatest divisor of itself, is a divisor of 78 , it is the greatest common divisor of 39 and 78 , also of 78 and 117 , and of 117 and 1365 . By trial, 39 is found to be a divisor of 78, and is, therefore, the greatest

Obs.-A knowledge of the Principles (111), will render the above analysis plain, since 32 is an exaot divisor of 78 , it is a divisor of $117=39+78$, and
112. Rule.-Divide the greater number by the less, and the divisor by the remainder, and so on, till there is no remainder. The last divisor will be the greatest common divisor sought.
Nork.-The greatest common divisor of three or more numbers oan be found by finding the greatest common divisor of two of the numbers, then the greatest rommon divisor of this greatest common divisor and a third number, and so on. The last common divisor will be the greatest common divisor of all the numbers.

## EXAMPLES FOR PRAOTICE.

Find the greatest common divisors of the following numbers :

1. 72 and 168.
2. 175 and 455 .
3. 169 and 866 .
4. 84,126 , and 210 .
5. 12, 18, 24, and 30 .
6. 385, 462, and 154 .
7. 12,15 , and 18.
8. 210, 350, and 770.
9. 70,105 , and 245 .

Ans. 24.
Ans. 35.
Ans. 1.
Ans. 42.
Ans. 6
10. 16, 20, and 24.
11. 78,234 , and 468.
12. 2041 and 8476.
13. 286, 429, and 715.
14. 1649 and 5423.
15. 92,116 , and 124 .
16. 252, 630, 1134 , and 1386.
17. 49373 and 14773 .
18. 3013, 2231, and 2047.

[^23]
## LEAST COMMON MULTIPLE.

## 118. A Multiple is a number exactly divisible by a given

 number ; thus, 15 is a multiple of 3 .114. A Common Multiple is a number exactly divisible by (wo or more giveñ numbers; thus, 24 is a common multiple of

Nors.-It is evident that the product of two or more numbers, or any number of times their product, must be a oommon multiple of the numbers. Henoe. A numbrrs together.

## 1RS. The Least Common IIultiple is the least number ex-

 actly divisible by two or more given numbers; thus, 30 is the least common multiple of 10 and 15.Note.-The least cominon multiple of two or more numbers contains all the prime factors of each of those numbors, and no other factors.
116. To find the least common multiple.

FIRST METHOD.
Ex. What is the least common multiple of $9,12,16$, and 20 ? analysis 78, and
nd the ainder.
ie found greatest so on. umbers.

$$
\begin{aligned}
& \text { OPERATION. } \\
& 9=3 \times 3 \\
& 12=2 \times 2 \times 3 \\
& 16=2 \times 2 \times 2 \times 2 \\
& 20=2 \times 2 \times 5 \\
& 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 5=720 \text { Ans. }
\end{aligned}
$$

 , it will be y trial, 117 365, since lf, is a dinon divisor and 1365. 10t to be a tinder; 39. If, is a dion divisor ad of 117 be a digreatest ainder.
in any of the given numbers is 3, and 5 , must be all the of given numberico; and the greatest number 16, and 20. Theral the prime factors necessary to produce in oome, 2, 2, 2, 2, 3, multiple requirod 720 , the product of these
of these lactors, is the least oommon

## 117. Rule.-I. Resolve the given numbers into their prime

II. Take all the prime factors of the largest number, and such prime factors of the other numbers as are not found in the largest number, and their product will be the least common multiple.

## SECOND METHOD.

Ex. What is the least common multiple of $10,16,24$, and 32 ? OPERATION.

| 2) | 10, | 16, | 24, | 32. |
| ---: | ---: | ---: | ---: | ---: |
| 2) | 5, | 8, | 12, | 16. |
| $2)$ | 5, | 4, | 6, | 8. |
|  | 5, | 2, | 3, | 4. |
| 5, | 1, | 3, | 2. |  |

[^24]115. What ie the least oommon multiple ? 11\% what in given numbers on a horizuntal line, then we divide by 2 , a prime num. ber that will divide all of the:n without arpishiciirs a nd write the quetients is a lire anderneath. Now, since sisa of the numibers in the secund 1 wo couln in the factor 2 ,

118. Rule.-I. Divide by the smallest prime number that is an excuct divisor of two or more of the numbers, and write the quotients and the undivided numbers underneuth.
II. Proceed with the resulting numbers in like manner, until there is no exact divisor of any two of them.
III. The product of the divisors and the resulting numbers will be the least common multiple sought.
Noras.-1. When numbers are prime to each other, their produot is their
last common multiple.
2. When any of the given numbers is a tactor of any of the othars it may be canoeled.

## EXAMPLES FOR PRAUTICE.

Required the least common multiples of the following numbers :

1. 24,36 , and 20 .
2. $7,14,21$, and 15 .
3. $14,19,38$, and 57 .
4. $8,12,16$, and 20.
5. 32, 34, and 36 .
6. $20,36,48$, and 50.
7. $9,18,27$, and 54 .
8. 12, 15, 42, and 60.
9. 10, 45, 75, and 90. Ans. 450.
10. 12, 15, 18, and 35. Ans. 1260.
11. $25,60,100$, and 125 .
12. $22,12,44$, and 11 .
13. 18, 27, 36, and 40.
14. 270, 189, 297, and 243.
15. 64, 84, 96, and 216.
16. $84,100,224$, and 300 .

## FRACTIONS.

119. A Fraction is one or more of the equal parts of a unit.
120. Two integers are required to write a fraction, one to express the number of parts into which the whole number is divided, and the other to express the number of these parts taken. Thus,
If an apple be divided into 2 equal parts, one of the parts is called one half; if divided into 3 equal parts, one of the parts is called one third, two of the parts two thirds; if divided into 4 equal parts, ont of the parts is called one fourth, etc. ; if divided into 5 equal parts, one of the parts is called one fifth, etc.

The parts are expressed by figures ; thus,

| One half is written | $\frac{1}{2}$ | Three fourths is written |  |
| :--- | :--- | :--- | :--- |
| One third | 6 |  |  |
| Two thirds | 6 | $\frac{3}{4}$ |  |
| Une fourth | 6 | $\frac{1}{2}$ | One fifth |

118. What is the rule for funding the lacot common multipie second method $p$ -119. What in a lisation? - 120. Hons many numbers are riewired to writs

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[^25]
## FRACTIONS.

that is orite the
ver, until
bers will
121. The twipinterers of a fraction are its Torms ; the one Lulow the the, the britominator; and the one above, the Numerator.
122. The forominator names the parts, and shows how many of them ine efful to a unit.
123. The Nuherator numbers the parts, and shows how many of them ate thikeii or expressed by the fraction.
124. Fxom the fifegoing definitions, it follows,
I. That the whlue of a fraction in units, is the quotient of the numerator divideql by the denominator.
II. That fratumber indicate division, the numerator being a dividend and the defiotinator a divisor.

1:25. To Aluqulye a fraction is to name the unit or quantity divided, the valhe of ofe of its equal parts and the number of
parts expressed?

In $\frac{5}{8}$ of a yard, the itflet of the fraction is 1 yard; the part or fractional unit, $\frac{1}{8}$ of a yard; aud the ifftiftber of fractional units expressed or numbered is 5 . Nis is the denominuthe, afted stions that the yard is considered as 6 equal parts. Five is the numerator, ithpi fith that 5 of those equal parts are enumerated. 5 is the dividend, And, $\phi$, thef lifisor. Hence, $\frac{5}{6}$ of $a$ yard expresses 5 equal parts of such value that, 6 oft theth' effital 1 yard, the unit of the fraction.
124. Frathighs are classitied as Simple, Compound, and Complex.
127. The simpole friscion is distinguished as Proper and Improper.
128. A Simple praction is one whose terms are integral; as $\frac{2}{8}, \frac{3}{4}, \frac{7}{6}$.
129. A poportraction is one whose numerator is leas than its denomimatry; as $\frac{1}{4}, \frac{5}{6},+\frac{2}{3}$.
130. An fmproper Fraction is one whose numerator equals or excceds its demphthtutor; as $\frac{3}{2}, \frac{3}{4}, \frac{7}{3}$.
131. A Comporind Rraction is a fraction of a fraction; as $\frac{2}{3}$ of $\frac{0}{4}$ of $\frac{7}{8}$. 8

13'. A Confales Fraction is one having a fraction or a mixed number in dither or both of its terms; as, $\frac{2}{\frac{3}{8}}, \frac{6}{7 \frac{3}{4}}, \frac{9 \frac{1}{2}}{13}, \frac{5 \frac{1}{8}}{9 \frac{2}{3}}$.
1333. A Ifixed 解mber is an integer and a fraction united in the same expresifyl; as 5 ?

[^26]134. Since fractions are expressions indieating the division of one number by another, it follows,
1st. That, if the numerator be multiplied, or the denominator be divided, by any number, the fraction is multiplied by the same number.
2nd. That, if the numerator be divided, or the denominator multiplied, by any number, the fraction is divided by the same number.
3rd. That, if the numerator and denominator be both multiplied, or both divided, by the same number, the fraction will not be changed in value.

## REDUCTION OF FRACTIONS.

135. The Reduction of a fraction is the process of changing its terms, or its form, without altering its value.
136. CASE I.-To riduce a whole or mixed number to an "quivalent iniproper fraction.
Ex. 1. Reduce 12 yards to fifths.

> OPERATION.
> $5 \times 12=\frac{60}{5}$, Ans.

Analysis.-In 1 yard there are 5 fifths, and in 12 yards there are 12 times 5 fifths $=\frac{60}{5}$.
137. Rolk.-Nultiply the whole number by the given denominator; take the product for a numerator, under which worite the given denominator.
E.x. 2. To reduce $15 \frac{8}{4}$ to fourths.

ORERATION. $15 \frac{3}{4}$
$\frac{4}{83}$, Ans.

Analisis.-In 1 there are 4 fourths; therefore, 4 times the number of whole ones equals the number of fourths; therefore, $15=60$, to which add $\frac{3}{4}$ and we have $15 \frac{3}{4}=\frac{60}{4}$.
138. Rule. - Multiply the whole number by the denominator of the fraction; to the product add the numerator, and under the sum write the denominator.

## eXAMPLES FOR practice.

1. Reduce 9 to thirds. Ans. $\frac{27}{3}$.
2. Reduce 12 to eighths. Ans. $\frac{3_{8}^{8}}{8}$.
3. Reduce 25 to fourths.
4. Reduce 36 to fifths.
5. Reduce 40 to thirteentine
6. Reduce 16 to ninths. Ans. 144.
7. Reduce 70 to tenths.
8. Reduce 52 to fifteenths.
9. Reduce 35 to sevenths.
10. Reduce 81 to elevenths.
[^27]Reduc
11. 373.
12. $45 \frac{5}{8}$.
13. 92.9
14. $233^{7}$
15. 132
16. 134
17. $96_{12}^{7}$
18. $44 \frac{5}{18}$

1:5!
aient wh
Ex. 1
$\mathfrak{y}$
140. the quoti

Reduce

1. 28. 
1. $\frac{27}{4}$.
2. $\frac{124}{24}$.
3. 20 E5.
4. $\frac{18}{15}$.
5. 
6. ${ }^{34}$.
. 1000.
7. 1738. 
1. $24 \frac{7}{8} \frac{3}{3}$
2. 

Note.-A are prime to

Ex. Re
2) $\frac{18}{4} \frac{8}{2}$
3) $\frac{\theta}{21}$
12) $\frac{38}{84}$

1. 18. 
1. ${ }^{27}$.
2. $1 \frac{4}{5}$.
3. 205 .
4. $\frac{89}{15} 8^{-}$
5. $150^{\circ}$.
6. 1000. 
1. 1738. 
1. $2 \frac{431}{3} \frac{1}{3}$

REDTITTION of FRACTIONS.
Reduce the following mixed mumbers to improper fracticas.

| 11. $37 \frac{3}{5}$. | Ans. 188. |  |  |
| :---: | :---: | :---: | :---: |
| 12. $45_{8}^{7}$. | Ans. 3 尔Z. | 19. $1255^{\frac{9}{13}}$ | Ans. 1834. |
| 13. 92. | Ans. | 20. $1722^{\frac{3}{3}}$. | Ans. ${ }^{\frac{3}{2} 8^{3} 3 .}$ |
| 14. 237 . |  | 22. $1711^{\frac{1}{4}}{ }^{\circ}$ |  |
| 15. 1324. |  | 23. $1677^{40}{ }^{\text {a }}$, | Ans. 4.9 . |
| 17. $96.8{ }^{7}$. | Ans. 1214. | 24. $209^{\frac{12}{12} \sigma^{2}}$. |  |
| 18. $44_{15}{ }^{5}$ |  | 25. $3311^{19}$. |  |
| 18. $44 \frac{5}{18}$. |  | 26. $116 \frac{1}{5}$. |  |

1:35. Case II.-To reduce an improper fraction to an equivrient whole or mixed number.

Ex. In $\frac{y}{8}$ of a yard, how many yarde?

> opEration.
> $\frac{17}{8}=37 \div 8=4 \%$ Ans.

Analissis. - Since 8 eighths make 1 yard, there will be as inany gards in 37 eighthe of a yard as 37 cuntains times 8 , or if yards.
140. Rule.-Divide the numerator by the denominator, and the quotient will be the number required.

## EXAMPLES FOR PRACTIOE.

Reduce the following improper fractions to whole or mixed numbers:

## 141 | Ans. 3. | 10. 163116. |
| ---: | :--- |
| Ans. $6 \frac{3}{4}$. | 11. |
| 478. |  | Ans. $24 \frac{4}{5}$. <br> 18. $\frac{2}{21 \frac{2}{2}} \frac{1}{5} 1$.

 <br> 18. $\frac{2}{21 \frac{2}{2}} \frac{1}{5} 1$.}> 12. 192 .
> 13. 20, 20.
> 14. ${ }^{2} 2^{5}$.
> 15. 4 487.
> 16. 3802.
> 17. 448.

Notr.-A fraction is in its lowest terms, when its numerator and denominator are prime to each other.
$\boldsymbol{E} \boldsymbol{x}$. Reduce $\frac{30}{87}$ to its lowest terms.

$$
\begin{aligned}
& \text { operation. } \\
& \text { 2) } \frac{38}{84}=\frac{18}{42} \\
& \text { 2) } \frac{18}{42}=\frac{9}{2 T} \\
& \text { 3) } \frac{\theta}{\partial I}=\frac{3}{7} \text { Ans. } \\
& \text { Or, } \\
& \text { 12) } \frac{38}{84}=\frac{8}{7} \\
& \text { Analysis. - Dividing both terms of the fras- } \\
& \text { tion by the same number does not alter the } \\
& \text { value of the fraction ( } 13 \pm, 3 \text { rd.); honco, we } \\
& \text { divide both terine of } \frac{36}{84} \text { by } 2 \text {, both terms of the } \\
& \text { result, } \frac{18}{4} \text {, by } 2 \text {, both terins of this result by } 3 \text {, } \\
& \text { and obtain } \frac{5}{7} \text { for the final result. } \Lambda_{8} 3 \text { and } 7 \\
& \text { are prime to each other, the lowest terms of } \\
& \frac{86}{8} \text { are } \frac{8}{7} \text {. } \\
& \text { Instead of dividing by the factors 2, 2, and }
\end{aligned}
$$

3, successively, we inay divide by the greatost common divisor of the given terms, and reduce the fraction to ita lowest terms in a single operation. Henee, the

11:*. RULe.-Cancel or reject all fuctors common to both numerator and denuminator. Or,

Divide both terms by their greatest common divisor.

## EXAMPLES FOR PRACTICE.

Reduce the following fractions to their lowest terms:

1. $\frac{5}{35}$.
2. $\frac{27}{3}$.
3. $\frac{14}{7}$.
4. $\frac{72}{72}$.

5. $\frac{1}{4} 4 \frac{1}{4}$.
6. $\frac{3}{38} 8$
7. $\frac{980}{1536}$.

Ans. 출.
Ans.
Ans.
Ans.
Ans. ${ }^{3}$.

| 9. ${ }^{\frac{1}{8}{ }^{\text {a }} \text {. }}$ | Ans. ${ }^{4}$. |  |
| :---: | :---: | :---: |
| 10. $\frac{1}{25} \frac{6}{8}$. | Ans. $\frac{1}{4}$. | $\begin{aligned} & \text { 18. } \frac{8187}{18 .} . \end{aligned}$ |
| 11. $\frac{128}{120}$ | Ans. |  |
| 12. ${ }^{14} 0^{4} 5^{\circ}$ | Ans. ${ }^{\frac{7}{4}}$. | 20. 851 |
| 13. ${ }^{\frac{1}{2} 07}{ }^{\text {a }}$ |  | 21. $\frac{5648}{589}{ }^{\text {a }}$ |
|  |  | 22. $\frac{31}{82} \frac{27}{3}$. |
|  |  | 24. ${ }^{\text {2 }}$, ${ }^{\text {a }}$ |

Ans. $\frac{1}{1}$. Ans. $1_{11}^{31}$.

Ans. $\frac{4}{8}$
143. Case IV.-To reduce a fraction to a decimal.
$\boldsymbol{E} \boldsymbol{x}$. Reduce ${ }_{\frac{7}{8}}$ to its equivalent decimal.
first operation.

$$
\frac{7}{8}=\frac{7000}{8000}=\frac{875}{1000}=0.875, \text { Ans. }
$$

second operation.

$$
\text { 8) } \frac{7.000}{0.875}
$$

we have the equivalent decimal 0.875 .
Analysis. -We first annex the same number of ciphers to both tatris of the fraction; this does not witer that value, ( 134,3 rd.) ; we then claidins toth resulling terms by 8 , inis shatifieant figure of the denomjanatry, to obtain the decimal deassureator, 1000. Umitting the denomicator, and prefixing the sign,
In the second operation, we omit the
practieally, by annexing the onit the intermediate steps, and obtain the result, result by the de?ominator, 8 .
144. Rule.-I. Annex ciphers to the numerator, and divide by the denominator.
II. Point off as many decimal places in the resuli as there are ciphers annexed.
Notr.-If the division is net oxact when a sufficiant number of decimal figures have been obtained, the sign, + , may be annexed to the decimal to indioate that there is still a remainder.

## EXAMPLES FOR PRACTICE.

Reduce the following fractions to equivalent decimals.

1. $\frac{1}{2}$. Ans. 0.5 .
2. $\frac{3}{4}$. Ans. 0.75 .
3. $\frac{4}{5}$ Ans. 0.8 .
4. $\frac{5}{8}$.
$\left\lvert\, \begin{array}{cc}6 . & \frac{1}{25} . \\ 7 . & \frac{15}{18} . \\ 8 . & \frac{7}{8} . \\ 9 . & \frac{17}{26} . \\ 10 . & \frac{3}{400} .\end{array}\right.$
Ans. 0.04. 11. $_{11} \frac{1}{8}$. Ans. 0.333 +
5. $\frac{13}{16}$.
6. $\frac{5}{84}$.

ס. $\frac{5}{7}$.
Ans. $0.714+$
Ans. 0.85.
14. $\frac{17}{250}$.
15. $\frac{19}{320}$.
142. What is the rule for reducing fractions to their lowest terms i- 144. Whas
is the rule for reducing a fraction to edecimal ?
145. Case V.-To reduce a decimul to a fraetion.

Ex. 1. Seduce 0.875 to an equivalent fraction.
() V に
$0.87 \%=8750=7$.

Analysis.-Writing the deaimal figuren, .875 , over the ouminon donominator, $100(1$, wo have 18.5007 . Hence, the
136. Rusk. Om: the decimal point, and supply the proper deruminualor.

Fix. 2, Healuce $0.5 \frac{1}{3}$ to a fraction.

$$
.5 \mathbf{z}=\frac{5 \mathbf{3}}{10}=\frac{16}{3}=\frac{16}{10}=\frac{8}{15} .
$$

147. Hus, - Omitting the decimul point, write the denomiwitor umber the decimal, and reduce the fraction to its lowest lerms (112).

EXIMPLES FOR PRACTICE.
Reduce the foslowing decimals to equivalent fractions:

1. 0.045
2. 0.75 .
3. 0.12
4. 0.125
5. 0.024 .
6. 0.655.
7. 0.0008 .
8. 0.68 .

Ans. ${ }^{3}{ }^{3}$.
Ans. $\frac{3}{4}$.

Ans. $\frac{201}{201}$.
Ans. $12^{1} 50^{\circ}$
9. 0.000125.
10. $0.3 \frac{3}{5}$.
11. 4.00075.
12. $0.66 \mathrm{i}_{\frac{2}{3}}$.
13. $0.57 \%$.
14. $0.10^{2}$.
15. $5.62 \frac{3}{6}$.

Ans. $\frac{3}{8}$,
Ans. $4 \frac{3}{00 n}$.
Ans.
Ans. $\frac{1}{7}$.

14\%. Case VI.-To reduce a compound fraction to a simplo one.

Ex. L. liedluce of $\frac{5}{7}$ to a simple fraction.



Ex, 2. Hellices of $\frac{4}{7}$ of $\frac{8}{8}$ of $\frac{9}{22}$ of $\frac{4}{6}$ of $3 \frac{2}{3}$ to a simple fraction.
OPERATION.

$$
\frac{8}{4} \times \frac{4}{7} \times \frac{5}{8} \times \frac{2}{28} \times \frac{2}{3} \times \frac{11}{8}=\frac{2}{7}, \text { Ans. }
$$

146, 147. What is the rule jor rednerng a decinub to a fradion?


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149. Rule.-I. Cancel the factors common to the numerators and denominators, if any.
II. Multiply the remaining numerators together for a new $n u$ merator, anil the remaining denominators for a niv denominator. Note.-All wisole and mixed numbers that occur in compound fractions mast be reduced to improper fractions, before the required reduction is performod.

## EXAMPLES FOR PRAOTICE.

1. What is $\frac{3}{3}$ of $\frac{3}{8}$ of $\frac{3}{4}$ ?
2. What is $\frac{1}{4}$ of $\frac{4}{8}$ of $\frac{5}{6}$ ?
3. What is $\frac{3}{8}$ of $\frac{9}{11}$ of 7 of $\frac{4}{7}$ ?
4. Required the value of $\frac{9}{7}$ of $\frac{1}{4}$ of $\frac{8}{12}$ ot 21 .
5. Reduce $\frac{3}{7}$ of $\frac{5}{8}$ of $\frac{1}{5}$ of $\frac{8}{8}$ of $\frac{1}{10}$ to a simple fraction.
6. What is the value of $\frac{5}{5}$ of $\frac{5}{8}$ of $\frac{8}{3}$ of $\frac{9}{12}$ of $\frac{24}{24}$ ?
7. What is the value of $\frac{3}{5}$ of $\frac{5}{8}$ of $\frac{8}{9}$ of $\frac{9}{12}$ of $\frac{24}{18}$ ?
8. Reduce $\frac{8}{14}$ of $\frac{7}{3}$ of $\frac{8}{12}$ to a simple fraction.
9. Reduce $\frac{24}{35}$ of $\frac{8}{175}$ of $\frac{15}{2 \frac{5}{2}}$ of $9 \frac{6}{8}$ to : 1 whole number.
10. What is the value of $\frac{1}{6}$ of $2 \frac{3}{4}$ of $1_{1}{ }^{3}$ ?
11. What is the value of $1_{5}^{3}$ of $\frac{5}{7}$ of $\frac{1}{15}$ of $\frac{2}{5}$ of $8 \frac{3}{4}$ ?
12. Reduce $\frac{9}{77}$ of $\frac{4}{5}$ of $\frac{17}{18}$ of $3 \frac{3}{5}$ to a simple fraction.
13. Required the value of $\frac{7}{\frac{7}{7}}$ of $7 \frac{1}{2}$ of $1 \frac{9}{13}$ of $\frac{8}{2 T}$ of $3 \frac{1}{3}$.
14. Case VII.-To reduce fructions to a common denomi. nator.

Ans. 2.
Ans. $\frac{7}{12}$.

## 151. A Common Denominator is a denominator commor to two or more fractions.

Ex. Reduce $\frac{2}{3}, \frac{3}{3}$, and $\frac{5}{5}$ to other fractions of equal value, having a a common denominator.

$$
\begin{aligned}
& \text { FIRST OPERATION. } \\
& 2 \times 4 \times 5=\frac{40}{60} \\
& \overline{3} \times 4 \times 5=\frac{45}{3 \times 3 \times 5} \\
& \overline{4} \times 3 \times 5=\frac{60}{4 \times 3 \times 4}=\frac{48}{60}
\end{aligned}
$$

Analysis.-The product of the denominators is evidently a common multiple of the denominators. Multiplying both terms of the fraction 3 by 4 and 5 , and of $\frac{3}{4}$ by 3 and 5 , and of $\frac{4}{5}$ by 3 and 4 , does not rhange the value of the fractions (134, 3rd.), and 10duces them to equivalent fractions having a common denominator. Honoe, the
second operation.
3, $\frac{3}{4}, \frac{4}{5},=\frac{40}{80}, \frac{, 5}{65}, \frac{48}{8}$.
153. Rule.-Multiply the terms of each fraction by all the denominators but its own (for new numerators and a common denominator).

Nore. - Mixed rumbers must first be reduood to improper fractions, and oome. pound fractions, to grmple onez.

[^28]156. denomino

## merator

new nuninator. ons must rmed.
s. $\frac{3}{10}$. ns. $\frac{1}{6}$.
$\frac{27}{176}$. 176
$2 \frac{6}{11}$
3. $\frac{3}{4} \frac{2}{5}$, and $\frac{2}{1}$.
4. $\frac{11}{1}, \frac{1}{2}, \frac{1}{2} \frac{9}{1}$, and $\frac{4}{7}$.
5. $\frac{7}{15}, \frac{5}{24}, \frac{37}{50}$, and $2 \frac{3}{5}$.
6. $\frac{2}{9}, \frac{8}{4}, 6$, and $\frac{1}{2} \mathrm{r}$.
7. $\frac{1}{2} \frac{5}{2}, \frac{3}{11}, \frac{4}{7}$, and $\frac{3}{4}$.
8. $\frac{3}{7}, \frac{9}{14}, \frac{11}{2}$, and $5 \frac{3}{7}$.
9. ${ }^{4} \mathrm{~T}, \frac{20}{3} \frac{2}{3}, 5$, and $7 \frac{1}{3}$.
10. $5 \frac{6}{15}, 7,7 \frac{3}{4}$, and 8 .
11. $\frac{7}{10}, \frac{2}{3}, 3 \frac{1}{5}$, and $1 \frac{4}{15}$.
12. $\frac{5}{4}, 9,7,5$, and 4 .
13. $\frac{7}{8}, \frac{7}{12}, \frac{7}{16}$, and $\frac{7}{20}$.
14. $\frac{32}{88}, \frac{5}{75}, 4 \frac{1}{3}$, and $\frac{4}{15}$.
15. $\frac{8}{15}, \frac{8}{11}, \frac{5}{24}$, and $\frac{1}{2} \frac{1}{2}$.

## ADDITION OF FRACTIONS.

Notes.-1. Fractions, to be added or' subtracted, inust be abstract or of iike denomination, and must have a commun denominator.
2. Only units of the same kind, whether fractional or iotegral oan be added ,together.

Ex. 1. What is the sum of $\frac{3}{8}, \frac{8}{6}$ : and $\frac{7}{12}$ ?

## operation.

$$
\frac{s}{6}+\frac{5}{6}+\frac{7}{12}=\frac{9+20+14}{24}=\frac{43}{24}=1 \frac{19}{2}, \text { Ans. }
$$

Analrsis. - We first reduce the given fractions to a common denominator. And as the resulting fractions, $\frac{9}{2} 4, \frac{20}{2}$, and $\frac{14}{2}$ have the same fractional wit. we add them by uniting their numerators into one sum, making $\frac{8}{2} \frac{3}{4}=!^{\text {a }}$
the answer.

Ex. 2. Add 73 $\frac{3}{4}$ 8 $\frac{5}{12}$, and 12.
operation.
$7+8+1=16$
$8+\frac{5}{12}+\frac{2}{8}=\frac{15}{17 \frac{5}{8}}$, Ans.

Analysis.- The sum of the integers, 7,8 , and 1 , is 16 ; the sum of the frac. tions, $\frac{3}{4}, \frac{5}{12}$, and $\frac{3}{3}$, is $1 \frac{5}{6}$. Hence, the sum of both fractions and integers is $18+1 \frac{5}{6}=17 \frac{5}{6}$. Hince the

15'7. Rule. I. To add fractions.- When necessary, reducr the fractions to their lerrst comewn denominator; then add the numerators and place the suri over the common denominator.
II. To add mixed numbers.-Add the integers and fractions separately, and then add their sums.

Nore- All fractional resulta should be reducod to their lowest terms, and if improper frations, to whole or mixed numbers.

15\%. What is the general rule for addin; fractione?

## EXAMPLES FOR PRACTICE.

1. What is the - $\quad$ m $1 t^{\prime} \frac{7}{8}, \frac{3}{6}$, and $\frac{2}{5}$ ?
2. What is the smm of : $5, \frac{7}{70}$ and $1 \frac{3}{15}$.
3. What is the sum of $\frac{7}{71}, \frac{9}{82}, \frac{5}{3}$, and $\frac{1}{6}$ ?
4. Add $\frac{4}{5}, 7^{7} 5, \frac{3}{5}$, and $\frac{1}{21}$.
5. Add $\frac{4}{5}, \frac{7}{10}$, and $\frac{13}{15}$.
6. Add $\frac{13}{15}, \frac{5}{12}$, and $\frac{7}{20}$.
$\therefore$ Find the snm of $\frac{2}{5}, \frac{3}{2}, \frac{5}{6}$, and $\frac{17}{18}$.
7. Find the sum of $\frac{1}{3}, \frac{3}{4}, \frac{13}{12}$, and $\frac{18}{12}$.
8. Add $14 \frac{4}{5}, 3 \frac{9}{10}, \frac{19}{2} 6$, and $1 \frac{2}{8}$.
9. Add $47^{7}, 8 \frac{5}{25}$, and $2 \frac{8}{35}$.
10. Add $4 \frac{1}{4}, 1 \frac{1}{8}$, and $47^{7}$.
11. What is the sum of $\frac{7}{8}, 1_{7}^{7}, 5$, and $10 \frac{5}{6}$.
12. Add $\frac{1}{2}$ of $\frac{2}{2}, \frac{4}{5}$ of $\frac{5}{7}$, and $\frac{3}{4}$.
13. Add $\frac{3}{5}$ of $\frac{2}{3}, \frac{1}{2}$ of $\frac{2}{7}$ of $\frac{3}{4}$, and $\frac{1}{2}$.
14. Add $41 \frac{1}{2}, 105 \frac{2}{9}, 350 \frac{3}{4}, 241 \frac{3}{5}$, and $472 \frac{1}{4}$.
15. Add $125 \frac{4}{5}, 327 \frac{5}{12}$, and $25 \frac{1}{4}$.
16. Add $\frac{1}{2}, \frac{2}{5}, \frac{3}{11}, \frac{1}{18}$, and $\frac{17}{33}$.
17. Find the sum of $17 \frac{8}{4}, 18 \frac{5}{12}$, and $11 \frac{2}{3}$.
18. Add $\frac{4}{4}$ of $18 \mathrm{I}^{3} \mathrm{~S}$, and $\frac{1}{12}$ of $\frac{4}{4}$ of $6{ }_{1}^{3}$.
19. Add $\frac{1}{3}$ of $\mathrm{x}^{3}$ of $\frac{1}{4}-$ to $\frac{1}{2}$ ot $\frac{2}{9}$.
20. Add $16 \frac{2}{3}, 4 \frac{7}{8}, 9 \frac{3}{5}, 3 \frac{1}{4}$, and $1 \frac{7}{8}$.
21. Add $3 \frac{1}{2}$ of $5 \frac{1}{4}, \frac{9}{22}$ of $7 \frac{1}{8}$, and $\frac{1}{8}$ of $\frac{4}{5}$.

Ans. $2 \frac{1}{2}$.
Ans. $2 \frac{12}{3}$.
Ans. $2 \frac{29}{3}{ }^{4}$.
Ans. $2_{\frac{9}{35}}{ }^{\circ}$

Ans. $3{ }^{7}{ }^{7}$.
Ans. $21 \frac{19}{60}$.
Ans. $10 \frac{29}{132}$.
Ans. ${ }^{\frac{5}{8}} 8$.
Ans. $1161 \frac{29}{98}$.
Ans. 189 $\frac{8}{98}$.

Ans. $40{ }^{\frac{4}{15}}$.

## SUBTRACTION OF FRACTIONS.

Ex. 1. From $\frac{3}{4}$ take $\frac{2}{3}$.

$$
\begin{gathered}
\text { OPERATION. } \\
\frac{3}{4}-\frac{2}{8}=\frac{9-8}{12}=\frac{1}{12}
\end{gathered}
$$

SECOND OPERATION.

$$
\begin{aligned}
& 243=171=\frac{855}{7}=\frac{35}{7} \\
& 16 \frac{4}{5}=\frac{84}{5}=\frac{58}{\frac{38}{287}}=7 \frac{92}{85}
\end{aligned}
$$

Analitis.-We reduce the given frastions to a common denominator, and have $\frac{9}{12}$ and $\frac{8}{12}$ which express fractional units of tho same valuc. ihen 9 twelfths less 8 twelfths equal 1 twalfth $=\frac{1}{12}$, the answer.
E. $\boldsymbol{x}$. 2. Frum $24 \frac{3}{7}$ take $16 \frac{4}{5}$.

FIRST operation.
$243=24 \frac{15}{35}$
$16 \frac{1}{5}=\frac{16 \frac{2}{35}}{7 \frac{22}{3} 5}$ Ans.

Analysis.-We first reduce tho frectional parts $\frac{3}{7}$ and $\frac{4}{5}$, to a commen denorrinatur, 35 . Since we cannot take $\frac{28}{3} 8$ from $\frac{1}{3} \frac{5}{5}$, we add $1=\frac{3}{3} 5$, to $\frac{1}{35}$, making $\frac{60}{3}$, and $\frac{28}{35}$ from $\frac{50}{3}$ leaves $\frac{2}{3}=\frac{3}{3}$. We noxt add 1 to the 6 in the subtrahend, and subtracting, we have $\frac{722}{35}$ for the entire remainder.
158. RoLs. I. To subtract fractions. - When necessary, re duce the fractions to their least common denominator. Subtract the numerator of the subtrahend from the numerator of the minuend, and place the difference of the new numerators over the common denominator.
II. To subtract mixed numbers.-Reduce the fractional purts to a common denominator, and thra subtract the fractional and integral parts separitely. Or,--Reduce the mixed numbers to improper fractions, then to a common denominator, and sultract the less fraction from the greater.

## EXAMPLES FOR PRACTICE.

| 3.4.4.5.6.7. |
| :---: |
|  |  |
|  |  |
|  |  |
|  |  |
|  |  |
|  |  |

11. $105-4 \frac{3}{3}$.
12. $14 \frac{1}{4}-3 \frac{3}{8}=$
13. $4 \frac{1}{4}-\frac{8}{8}$.
14. $9 \frac{1}{2}-37=$
15. $8 \frac{1}{5}-6 \frac{7}{2}$.
16. $19{ }^{1} \frac{1}{73}-338=$ Ans. $15 \frac{32}{3}$.
17. From $\frac{2}{3}$ of $\frac{5}{5}$ take $\frac{1}{5}$ of $\frac{2}{5}$.
18. From $\frac{1}{3}$ of $\frac{2}{2}$ take $\frac{1}{1}$ of $\frac{4}{4}$.
19. From $\frac{1}{4}$ of $\frac{9}{11}$ take $\frac{1}{4}$ of 2 .
20. From $\frac{3}{5}$ of $\frac{5}{7}$ of $3 \frac{1}{2}$ take $\frac{1}{5}$ of $1 \frac{1}{2}$.
21. What is the value of $\frac{1}{4}$ of $3-\frac{1}{1}$ of 2 .
22. From 72 lbs. there were taken at one time 175 Ans. $1_{12}^{12}$. another, $28 \frac{7}{12} \mathrm{lbs}$; what quantity remains?
23. From $\$ 15$, $\$ 3 \frac{1}{1}$ were given to $\mathrm{A}, \$ 4 \frac{1}{4}$ to $\mathrm{B}, \$ 2 \frac{1}{3}$ to C , and the remainder to D ; what did D receive?

## MULTIPLICATION OF FRACTIONS.

159. Case I.-To multiply a fraction by an integer.

Ex. Multiply $f$ by 3.

> FIRST OPERATION.
> $f \times 3=24=2 \frac{1}{2}$

ANALTBIS. -In the first operation, we tanltiply the numerator of the fraction by the integer, 3, and obtain 21 for the answer. It is evident that
cry, re ubtract e minecom al and bers to ubtract
$57 \frac{29}{60}$. . $12 \frac{7}{18}$. . $244 \frac{1}{8}$. . $87 \frac{7}{7}$. $.3 \frac{48}{375}$. s. 4 部忽. s. $5_{3}^{24}$.

## 2917.

$\frac{1}{3} \frac{37}{6}$.


2S. $\frac{1}{12}$. ind at lus. dd the
becond operation.
$\frac{7}{8} \times 3=\frac{7}{3}=2 \frac{1}{3}$
thimb operation.

$$
\frac{7}{9} \times \frac{8}{1}=\frac{7}{3}=21
$$

by dividing its den minator by
fraction is divided a before, while the as as large, as

fraction bing the numerator or dividing the denominator of a fach by any integer multiplies the fraction by that integer. Nots.- In the third operation, we express the multiplier in the form of a frartion, indicate the multiplication, and obtain tho rosult by can"ellation.

16id. Case II.-To multiply an int ger by a fraction, or in find a frectional part of an integer.
E.x. Multiply 24 by $\frac{5}{6}$.
first operation.
$24 \times \frac{8}{6}=\frac{120}{6}=20$.
second operation.

$$
24 \times \frac{5}{8}=4 \times 5=20
$$

thikid operation. $\frac{54}{1} \times \frac{5}{6}=20$.

Avalysis.-In the first operation, we first multiply the integer, 24, by the numerator of the fraction, then divide the product by the denminator, and obtain 20 for the answer.
In the second operation, we divide tho integer, 24, by tho denominator of the fraction, and obtain $\frac{1}{6}$ of $24=4$, which multiplied by 5 , the numerator of the fraction, gives $\frac{5}{6}$ of 24 $=20$. Henoo,

Mnltiplying by a firaction is taking the part of the multiplicand denoted by the mn/tiplier.

Note.-In the third operation, we express the integer, 24, in the form of a fraction, indicate the multiplication, and obtain the result by oancellation.
161. Case III.-To multiply a fraction by a fraction.

Note.-To multiply a fraotion by a fraction is to find a fractional part of a
Ex. Multiply $\frac{5}{12}$ by $\frac{4}{5}$.
first operation.
$\frac{5}{12} \times \frac{4}{5}=\frac{20}{60}=\frac{1}{8}$.
eecond operation.
$\frac{5}{12} \times \frac{4}{5}=\frac{1}{3}$.

Axalrass. -Tomultiply ${ }_{1}^{5}$ by $\frac{4}{5}$ is to take $\frac{A_{5}}{5}$ of the r ultiplioand, $5^{5}$. Now, to obtain $\frac{4}{5}$ of ${ }_{12}^{5}$, wo simply multip ${ }^{2} y^{2}$ tho mumerators togethor for a new numerator, and the denominators together for a now denominator (150).
Therefore,

Multiplying one fraction by another is the same as reducing compound fructions to simple ones.

From the foregoing we deduce the following general
162. Rule.-I. Reduce all integers and mixed umutirers to improper fructions.
II. Multiply together the numerators for a new mumerutor, and the denuminutors for a new denominator.
Notss.-1. Cancol all factors common to numeratory and denominatorys
2. 'The word of between fractions is equivalent to the sign of multiplication.

EXAMPLES FOR PRACTICE.


## PRACTICAL PROBLEMS.

Note. - In business transactions it is customary to add 1 oent when the fraotion is equal to or greater than a half of a cent, and to ounit it when it is less than the balf of a cent. The frnction is retained in the following answers.

Required the cost of

1. $6,7 \mathrm{lbs}$. of ham, at $12 \frac{1}{2} \mathrm{cts}$ per lb .
2. $7 \frac{1}{2}$ yds. of tape, at $6 \frac{3}{4}$ cts. per yard.
3. 9 ? quarts of plumes, at $7 \frac{2}{2}$ cts. per qt.
4. 56 lbs , of chalk, at $\frac{3}{4}$ of a cent per lb.
5. $7 \frac{3}{3}$ yards of muslin, at $9 \frac{3}{4}$ cts. per yard.
6. $7 \mathrm{~g}_{1} \mathrm{llbs}$. of beef, at 5 cts. per lb.
7. $6 \frac{1}{2}$ bush. of apples, at $74 \frac{1}{2} \mathrm{cts}$. per bush.
8. $12 \frac{1}{2}$ bush. of oats, at $62 \frac{1}{2}$ cts. per bush.

Ans. $\$ 0.8518$.
Ans. $\$ 0.75 \frac{17}{2}$.
Ans. $\$ 0.74$.
Ans. \$4.84\}.
109. What is the rule for the multiplication of fractions?
9.
10.
11.
12.
13.
14.
15.
16.
17.
18.
19.
20.
21.
22.
23.
24. 2
25. 7
26.
27.
28. 35
29. $7 \frac{3}{8}$
30. 75
31. 9
32. $6 \frac{3}{4}$
33. 23
34. 75
35. 21
36. $3 \frac{4}{5}$
37. 14
38. $6 \frac{3}{7}$
39. 18
40. 13
163.

Ex. Di
seor
$\frac{12}{8}$

Dividin fraction $b_{3}$
9. 79 bush. of salt, at $\frac{7}{8}$ of a dollar per bush.
10. $5 \frac{1}{2}$ quarts of nuts, at $9^{2}$ cts. per quart.
11. $2 \frac{3}{5}$ yards of cloth, at $\frac{7}{8}$ of a dullar per yd.
12. 9 barrels of vinegar, at $\$ 6_{8}^{3}$ per bbl.
13. 15 lls . of almonds, at $9 \frac{1}{2} \mathrm{cts}$. . per lb.
14. $8 \frac{3}{5}$ yds. of cloth, at 85 per yard.
15. 15 yds of ribion, at $26{ }_{5}^{3}$ cta. per yd.
16. $7 \frac{3}{2} \mathrm{lbs}$. of cotfee, at $\frac{3}{5}$ of a dullar per lb .
17. $8 \frac{5}{5}$ cords of wood, at $: 223$ per cord.
18. 12 cords of wood, at $\$ 6.37 \frac{1}{2}$ per cord.
19. 42 bus!. of apples, at 632 cts. per bush.
20. 11 cwt . of sugar, at $89_{8}^{3}$ per cwt.
21. $7 \frac{3}{5}$ doz. of eggs, at $12 \frac{1}{2}$ cts. per doz.
22. 112 bbls of salmon, at $\$ 545$ per bbl.
23. 122 bush. of putatues, at $37 \frac{1}{2}$ cts. per bush.
24. $22 \frac{3}{5}$ yds. of nelicia, at $87 \frac{3}{4}$ cts. per yard.
25. 73 cords of maple, at $\$ 5 \frac{3}{3}$ per cord.
26. 43 bush. of rye, ai $\$ 1.75$ per bush.
27. $10 \frac{8}{5}$ yde. of calico, at $15 \frac{3}{2}$ cts. per yd.
28. $35 \frac{1}{6}$ lbs. of raisins, at $18 \frac{3}{4}$ cts. per 1 b .
29. 73 $\frac{3}{8} \mathrm{yds}$. of cloth, at $\$: 3 \frac{1}{2}$ per yu.
30. 75 $\frac{3}{3}$ bush. of wheat, at $\$ 13$ per bush.
31. 9 doz. of adzes, at $\$ 10 \frac{5}{8}$ per doz.
32. $6 \frac{3}{3}$ bush. of turnips, at $37 \frac{1}{2}$ cts. per bush.
33. $234 \frac{4}{5}$ cords of wood, at $\$ 3 \frac{3}{8}$ per cord.
34. $75 \frac{1}{2}$ lbs. of sugar, at $7 \frac{8}{4} \mathrm{cts}$. per lb .
35. $212 \frac{2}{3} \mathrm{lbs}$. of beef, at $7 \frac{1}{2}$ cts. per lb .
36. 345 tons of hay, at $\$ 123$ per ton.
37. 144 buls of vinegar, at $\$ 102$ per bbl.
38. $6 \frac{3}{7}$ gal. of nolasses, at 233 cts. per gal.
39. 18 handkerchief's, at $\frac{8}{4}$ of a dollar each. 40. $13 \frac{1}{2} \mathrm{lbs}$ of fish, at $9 \frac{3}{4} \mathrm{cts}$. per lb .

Ans. $\$ 69$.
Ans $82.27 \frac{1}{2}$.
Ans. $\$ 1.42 \frac{1}{2}$.
Ans. $\$ 3.99$.
Ans. 52.217.
Ans. $\$ 26.58$.
Ans. $\$ 0.967$
Ans.
Ans. 841 事名.
Ans. $1.74 \frac{9}{10}$.
Ans. $\$ 25 \frac{13}{16}$.
Ans. $\$ 95_{8}^{5}$.

Ans. \$5.851.

## DIVISION OF FRACTIONS.

163. Case I.-I'o divide a fraction by an integer.

Ex. Divide $\frac{1}{1} \frac{2}{2}$ by 6.
first operation.

$$
\frac{12}{13} \div 6=\frac{2}{13}
$$

seoond eperation.
$\frac{12}{18} \div 6=\frac{12}{78}=\frac{12}{18}$.

Analysis. - In the first operation, we divide the numerator of the fraction by 6 , and write the quatient, 2 , over the denominator.

In the second oneration, we multiply the dencminator of the fraction by the divisor, 6, and writ the product under the numerator, 12. Henoe,

Dividing the numerator or multiplying the denominator of a fraction by any number divides the fraction by that number (134).
148. Case II.-Th divide an integer by a fraction.
fix. How many times will 24 contain $\frac{8}{7}$ ?

$$
\begin{gathered}
\text { MRAT operation. } \\
\mathbf{2 4} \div \frac{7}{7}=16 \mathrm{~s} \div 6=28 \\
\text { SGGOND opERATION. } \\
24 \div \frac{8}{7}=4 \times 7=28 .
\end{gathered}
$$

analysis.-'The integer 24 will comtain $\frac{2}{7}$ as many timos as there are sepenths in 24, equal 168 seveuthy. Now, if 24 contains I seventh 163 times, it will contain $\frac{8}{7}$ as many timos as 168 will contain 6 , or 28

In the second operation, wo divide bun in a .er by the numerator of the fraction, an. inultiply the quotient by the Heswift latur, which produces the snme result as in the first operation. Hence,

Diniding by, a fruction comsists in multiplying by the denomimulor, and dividing by the mumerator of the ilivisor.
1955. Cane III.-To divide a fraction by a fraction.

Ex, Divide ? by 3.
operation.

$$
\because \frac{3}{7}=\frac{3}{2}=\frac{91}{8} .
$$

ANALPBIS. -. We invert the terme of the divisur, and tien procsed aw in multiplioation of fractions (162). The reason of this process will be seen, if we cunsider that tho divisor, 1. in an expression denoting that 2 is to be diviled by 3 . Nuw, regarding 2 as *Winteger, we divide the fraction \& by it, by multiplying the donominator; thes, $\frac{1}{8} \times 2=\frac{7}{16}$. But the divisor, 2 , is 3 times as largo as it ought to bo, simen it was to be divided by 3 , as neen in the original fraction; therefore the quthente, ${ }_{7}^{7}$, is 3 as large as it should be, and must be multiplied by 3 ; thus, $\frac{7}{10} \times 2$ $1 *=\frac{21}{18}$, the answer By this operation we have inultiplied the denomiAntio if the divilend by the numerator of the divisor, and the numerator of the Chivilend by the denominator of the divisor.

Prom the foregoing we derive the following general
1845. Rulle.-I. Reduce integers and mixed numbers to improvier fractions.
11. Invert the terms of the divisor, and proceed as in multipliculiom of fractions (162).

Finks-1. The dividend and divisor may be reduoed to a oemmon denoniAler, and the numerator of the dividend bo divided by the numerator of the divent; this will give the came result as the rule.
2. Aphy cancellation where practicable.

## EXAMPLES bOR PRACTIOE.

|  | Ans. $\frac{3}{7}$ (4. $23 \div \frac{1}{4}$. |
| :---: | :---: |
| 2. ${ }^{2}+6$, | 5. $5 \div 1=$ |
| 名. $4 \div 3=$ | Ans. 6. 6.8 |

Ans. $3 \frac{1}{3}$.
1M\&, What is the ge oral rule for dividing fractions?
7. 1
8.
9. 2
10. 31
11. 7
12.
13.
14. 8
15. 63
16. 31
17.
18.
31.

The se by a sing
32. D
33. D
34. I)
35. D
36. D
37. D
38. D
39. Di
40. Di
41. W
$\frac{69}{8 \frac{9}{3}}=\frac{\frac{68}{88}}{\frac{8}{3}}$
fraction, an divide as $b$
42. Wh
43. Wh
44. Wh

4 will oonro are seethy. Now, 3 times, it 4as 168 will wo divide at by tho n. Hence, denomime of tho tipliaation his process ho divisor, ding 2 as omioator; ght to be, refore the 3 ; thus, - denomitor of the
$s$ to im-multi-
denonior of the ns. $3!$
7. $17 \div 7=$
8. $2^{5} \div \frac{5}{21} \div 8=$
10. $21 \div \frac{1}{31}=$
11. $75 \div 135=$
12. $\frac{10}{71} \div$ 号
13. $71 \div 3=$
14. $8 \div 167$.
15. $63 \div \frac{7}{7}=$
16. $3 \frac{1}{2} \div 71$.
17. $\frac{15}{25} \div 28=$
18. 暜 $\div 49$.

Ans. 3.
Ans. $\because: 19$.
Ans. 21
Ans. 117.
Ans. ${ }_{6}^{18}{ }^{18}$.
31. Divide $\mathbf{3}$ of $\mathbf{f}$ by of

$$
\begin{aligned}
& 0 \mathrm{r} \text {, } \\
& 3 \times 7 \times 7 \times \frac{9}{2}=18 \text {. }
\end{aligned}
$$

The seoond method of solution has the twofold id vantiges of giving the answer by a single operation, and of afferding greater faoility for oancellation.
32. Divide $7^{7}$ of 4 by $8^{8}$ of $\frac{8}{4}$.
33. Divide $\frac{1}{6}$ of $\frac{5}{15}$ by $\frac{8}{11}$ of $\frac{5}{18}$.
34. Divide $\frac{1}{5}$ of $\frac{1}{5}$ by $\frac{1}{2}$.
35. Divide $\frac{5}{5}$ of 6 by $1 \frac{1}{4}$ of 7 .
35. Divide $\frac{6}{8}$ of $7 \frac{3}{1 \mathrm{~T}}$ by ${ }^{4} \mathrm{~T}$ of $17 \frac{3}{9}$.
36. Divide $\frac{1}{2}$ of 4 by $\frac{5}{8}$ of $3 \frac{1}{4}$.
37. Divide $\frac{2}{3}$ of 14 of $\frac{8}{5_{2}}$ by 7 of 19 of 2.
39. Divide $\frac{8}{8}$ of $5 \frac{1}{2}$ of $7^{2}$ by ${ }^{5}$ of $3_{1}^{3}$.
40. Divide $\frac{3}{4}$ of $\frac{5}{7}$ of $\frac{4}{4}$ by $\frac{2}{3}$ of 8 of $\frac{2}{2}$.
40. Divide $\frac{1}{8}$ of 36 by 17 of $\frac{3}{5}$.
41. What is the value of $\frac{6 \frac{2}{9}}{8!}$ ?
operation.
$\frac{6 \frac{2}{8}}{8_{3}^{2}}=\frac{\frac{58}{98}}{\frac{80}{3}}=\frac{56}{9} \div \frac{26}{3}=\frac{28}{\frac{58}{2}} \times \frac{8}{3}=\frac{28}{36}$, Ans.
Ons.-Thisexample is only another form forexpressingdivision of fractions; it is called a complex fraction. We simply reduce the apper number or dividend to an iinproper fraction, and the lower number, or divisor, to an improper fraction, and ind then
divido as before.
42. What is the value of $\frac{43}{3}$ ?
43. What is the value of $\frac{\frac{5}{11}}{4 \frac{2}{8}}$ ?

Ans. $6 \frac{9}{14}$.
44. What is the value of $\frac{7 f^{f}}{8}$ ?

Analrals.-The dividend, reduced to a siuplo fraotion, is $\frac{7}{12}$; the divisor, reduced in like manner, is $7_{6}^{2}$; and 7 divided by ${ }^{2} \frac{1}{8}$ is 187 , the quotiont requirod. Of, wo may apply the genorill rule direatly by invorting both frotors

Ans. 2 \%.
Ans. 14.
22. $8 \frac{1}{4} \div 6 \frac{13}{5}$.

24. $15 \div 1 \frac{1}{15}$
25. $19 \div 19$
$26.14 \div 19$.$\quad$ Ans. $31 \frac{3}{14}$.
27. $92 \div 47=$
28. $4 \frac{3}{7} \div 17$.
29. $814 \div 95=$

Ans. 1.
Ans. $81 \frac{83}{61}$.

45．What is the value of $\frac{\text { of } \frac{3}{2}}{\frac{1}{2}}$ ？
Ane． 1.
46．What is the value of $\frac{4 \frac{1}{5} \text { of } 3 \frac{1}{2}}{}$ ？
47．What is the value of $\frac{8}{\frac{7}{8} \cdot f^{\frac{1}{7}}}$ ？
48．What is the value of $\frac{8}{4 \frac{8}{2} \text { of } \frac{19}{9}}$ ？
49．Leduce $\frac{\frac{5}{8} \text { of } \frac{8}{7}}{6 \frac{1}{5}-\frac{4}{15}}$ to its simplest form．
Ans． 1 音．
50．Reduce $\frac{51}{7!\times 1_{2}^{11} \times 3!} \times \frac{5}{18}$ 年 its simpleat form．

## PRACTICAL PROBLEMS．

1．If $\frac{3}{7}$ of an acre of land，sell for $\$ 63$ ，what will an acre sell for as the shine rate？

Ans． 8147.
2．At $\$ \frac{3}{3}$ per bushel，kow many bushels of onions can his longht for $\$ 12$ ？

Ans． 16.
3．How many times will $16 \frac{3}{4}$ gallons of vinegar fill a versel that holds 3 gallons？

4．At 番 of a cent each，how many apples can be bonght for $8 \frac{1}{4}$ cents？

Ans． 11.
5．If 15 pounds of raisins can be obtained for $\$ 3 \frac{3}{7}$ ，what will 1 pound cost？
6．A butcher expended $\$ 56 \frac{2}{5}$ for sheep，giving $\$ 1 \frac{1}{5}$ per head；how many sheep did he buy？

Ans． 47.
7．At $\$ 5$ per yard of broadcloth，what part of a yard can be bought for 景 of a dollar？

8．If I pay $5 \frac{2}{3}$ cents for riding 1 mile，how many miles can I ride for $113 \frac{1}{2}$ cents？

Ans． 20.
9．How many pounds of tea，at $\$ 11$ per pound，can be obtained for $\$ 13 \frac{1}{2}$ ？

Ans． 12.
10．It＇ 9 men consume $\frac{3}{4}$ of $9 \frac{3}{5}$ pounds of meat in a day，how much does each man consume？Ans．$\frac{4}{5}$ of a lb．

11．A man bought $37 \frac{2}{5}$ yards of calico for $\$ 5.61$ ，liow much did it cost per yard？

Ans．$\$ 0.15$ ．
12．How many tons of coal，at $\$ 5 \frac{3}{4}$ per ton，can be bought for $\$ 57$ ？
13．A horse eats $\frac{3}{8}$ of a bushel of oate in a day，in how many days will he eat $15 \frac{3}{4}$ bushels？

Ans． 42.
14．A merchant bought 97 sheep for $\$ 100 \frac{2}{2}$ ，how much did he give per head？

Ans．\＄1．04．
15．If a boy earn of a dollar a day，how many days will it take him to earn $\$ 9$ ？

Ans． 26.
16．1＇cter paid $\$ 543 \frac{3}{4}$ for a farm，giving $\$ 21 \frac{3}{4}$ per acre ；of how many acres did the farm cunsist？

Ans． 25.
17．If $\$ 2 \frac{8}{6}$ is paid tor $5 \frac{1}{6}$ pounds of grapes，how much is that pes poundi？

Ans．$\$ 0.50$ ．
18.
per ton 19. 20.
for $\${ }^{2} \mathrm{O}$ 21.
get for
would 8 25．
$\$ 31$ per
26．H
cover a 27.
each bot 28．If chased 29． H
if yards 30．A each，an did he ga

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167.
tions is t
them，gir

## 168. fractions．

## Ex．W

Greatest c Least com

Analysia． least cormmo tors 112，ho， fifthe，their fifths ；there $8^{8} \mathrm{f}$ as the an

167．Ther
18. How many tons of hay can be purehased for $\$ 119 \frac{1}{18}$, at $\$ 9 ?$ per ton? 19. At $\$ 12$ per day, huw many days murl a man Ans. $12 \frac{7}{0}$. 20. At $\frac{1}{2}$ of $\frac{3}{4}$ of a dollar per grallon, how nuch beer can be bonght for $\$_{10}^{8}$ ?
21. If $2 \frac{1}{2}$ apples are worth $3 \frac{1}{2}$ cents, what part of Ans. $2 \frac{2}{3}$ gal.
get for 1 cent? 2:. If 2 yards of merino cost sil, how much lese Ans. 9 yards cost? 23. If 3 turkeys cost $\$ 4 \frac{1}{2}$, how many can be bought Ans. 823.
24. If 3 horses eat $3 \frac{3}{5}$ bushels of oats in a day hht for $\$ 38$ ? ?
would 8 g bushels supply tor the vame time? day, how many borses 25. A young man, having slo, gave ? of his Ans. 7. \$31 per ream; how much did he buy? orhis money for paper at 26. How many feet of carpet 2? feet in .ins. 2 reams. cover a floor $14 \frac{1}{2}$ feet in length and 102 feet winth will be required to 27. How many bottles will be requir feet in width? Ans. each bottle will hold $h$ of ? of द fequired to hold $81^{*} 5$ gal. of' wine, if 28. If 5 barrels of flour cost $\$ 48 \frac{3}{4}$, how many barelans. Ans. chaved for $\$ 263 \frac{1}{4}$ ? 29. Huw much more than $8 \frac{8}{4}$ yards of tape, at 4 Ans. 27 . 1f yards of calico cost at 11 cts . a yard? 30. A farmer gave $\$ 46$ for some calves, 5 of which Ans. $\$ 0.11$ 妟. each, and traded the rest for $5 \frac{1}{2}$ bbls. of tlour, at $\$ 4$ a he sold for $\$ 5 \%$ did he gain? Ans. $\$ 4$.

## greatest common divisor of fracirions.

## 167. The Greatest Common Divisor of two or more fric.

 tions is the greatest number which will exictly divide each of them, giving a whole number for a quotient.168. To find the greatest common divisor of twoo or more

Ex. What is the greatest common divisor of $3 \frac{1}{3}, 1$, and $\frac{18}{5}$ ?

$$
\begin{gathered}
\text { OPERATION. } \\
3 \frac{1}{5}, 1 \frac{5}{7}, \frac{24}{3}=18,7, \frac{24}{36}=12, \frac{6}{8}, \frac{18}{8} .
\end{gathered}
$$

Greatest common divisor of the numerators $=4\}$ Greatestcommon Least common denominator of the fractions $=\overline{35}\}$ divisor required.

Analisis. - Having reduced the fractions to equivilent tractiong baving the least common denominator, we find the groatost oommon dirisor of the nizare. tors 112,60 , and 24 to be 4. Now, since the 112,60 , and 24 represont abirtyfifths, their greatost common divisor is not 4,2 whole number, bet thirty. fifths; thercfore w
it as the answer.

[^29]169. Rule.-Reduce the fractions, if necessary, to thair lenat common denominator. The greatest common divisor of the numur. ators, written over the least common denominator, will give the yreatest common divisor required.

## EXAMPLES FOR PRAOTIOE.

Required the greatest common divisor of

1. $\frac{2}{5}, \frac{1}{5}$, and 4 .
2. $\frac{5}{6} \cdot \frac{5}{4}$, and $18^{\circ}$.

Ans. $\frac{2}{45}$.
3. $\frac{14}{24}, \frac{7}{3}$, and $\frac{8 .}{45}$.
4. $\frac{5}{5}, \frac{8}{8}, \frac{10}{2}$, and $\frac{1}{6}$.
5. $34,57^{7}$, and $21^{8}$.
6. $2 \frac{1}{4} .4$, $\frac{1}{15}$, and $5 \frac{1}{8}$.
7. $8 \frac{1}{4}, 12 \frac{3}{5}$, and $9 \frac{3}{4}$.
8. $2 \frac{2}{9}, 4, \frac{4}{9}$, and $2 \frac{2}{5}$.

Ans. 䇆

## LEAST COMMON MULTIPLE OF FRACTIONS,

170. The Least Common Inultiple of two or more fractions is the least number which can be exactly divided by each of thew, giving a whole number for a quotient.
171. To find the least common mnltiple of two or more fructions, $\boldsymbol{E x}$. What is the least common multiple of $7 \frac{7}{\mathbf{7}}, 5 \mathbf{k}$, , and 315 ?

$$
\begin{gathered}
\text { operation. } \\
7 \frac{27}{5}, \frac{1}{4}, 3 \frac{1}{8}=\frac{88}{8}, \frac{21}{4}, \frac{6.3}{18} .
\end{gathered}
$$

Least common muit. of the numer. $=63,15$, Least common Greatest com. div. of the denom. $\left.=\overline{4} \doteq 15 \frac{3}{4}\right\}$ multip. required,

Analysis.-Having reduced the fractions to their simplest forta, we fixd the least common multiple of the numerators, 63,21 , and 63 , to be i3. N/w, sinere the 63,21 , and 63 are, from the nature of a fraction, dividends, of which thysif respective denominators, 8,4 , and 16, are the divisors (118), the least ernamman multiple of the fraotions is not 63, a whole number, but so many fractional parte of the greatest coamon divisor of the denominators. This common divioor we find to be 4, which, written as the denominator of the 63, gives $88=154$ we the least number that can be exactly divided by tho given fractions."
172. Rule.- Reluce the fractions, if necessary, to their lows ost terms. Then find the least common multiple of the numerulurs, which, written (ver the greatest common divisor of the denomb nators, will give the least common multiple required. Or,

Reduce the fractions, if necessary, to their least common dennminator. Then find the least common multiple of the numeritirs, and write it over the least common denominator.

[^30]50 cents
$33 \frac{1}{3}$ cents
25 cents
20 cents $16 \frac{2}{8}$ cents
171. price of a Ex. At

OPE
$A n$
175. as the pric

1. What pound?
2. What
3. At $6 \frac{1}{4}$
4. At $8 \frac{1}{0}$
b. What
5. At $\$ 3$.
6. What the ocot of any $a$ doblar i

## EXAMPLES FOR PRACTIOE.

Required the least common multipla of

1. $\frac{8}{16}, \frac{3}{4}$. and $2 \frac{1}{16}$.
2. $\frac{16}{7}, \frac{1}{3} \frac{5}{5}$, and $\frac{30}{28}$.
3. $\frac{8}{6}, \frac{6}{7}$, and $\frac{1}{5}$.
4. $\frac{7}{10}, \frac{14}{15}, \frac{8}{25}$, and $\frac{3}{5}$.

Ans. $8 \frac{1}{4}$.
Ans. 24.
5. $5 \frac{1}{4}, \frac{2}{12}$, and $1 \frac{1}{2}$.
6. $1 \frac{37}{75}, \frac{83}{100}$, and 222.
7. 15, $\frac{3}{4}$, and $\frac{5}{12}$.
8. $\frac{15}{15}, 5,6 \frac{3}{2}, \frac{12}{15}$, and $2 \frac{1}{2}$.

Ans. 3 .

## PRACTICE, OR ANALYSIS BY ALIQUOT PARTS.

173. An Aliquot Part of any number or quantity is such 2 4, and 6 are aliquot parts of 12 .
Nork.-An aliquot part may be a whole or a mixed number while a faetor must be a whole number.

## aliquot parts of one dollar.

50 cents $=\frac{1}{2}$ of 1 dollar.
$33 \frac{1}{3}$ cents $=\frac{1}{8}$ of 1 dollar.
25 cents $=\frac{1}{4}$ of 1 dollar.
20 cents $=\frac{1}{5}$ of 1 aollar.
$16 \frac{2}{2}$ cents $=\frac{1}{8}$ of 1 dollar.
$12 \frac{1}{2}$ cents $=\frac{1}{1}$ of 1 dollar.
10 cents $=\frac{1}{10}$ of 1 dollar. $8 \frac{1}{3}$ cents $=\frac{1}{12}$ of 1 dollar.
$6 \frac{1}{4}$ cents $=\frac{1}{16}$ of 1 dollar.
5 cents $=\frac{1}{20}$ of 1 dollar.
171. To find the cost of any number or quantity, when the price of a unit is an aliquot pirt of one dollur.
$\boldsymbol{E} \boldsymbol{x}$. At $12 \frac{1}{2}$ cents a yard, what will 416 yards of muslin cost?
operation.
8) 416

Ans. $\overline{\$ 52}$
Avaly sis.- If the price wore $\$ 1$ a yard, the cost would be as wany dollars as there are yards. But sinco the price is $t$ of a dellar a yard, the whole cost will bo $\downarrow$ as many dollars as there are yards; or, $t$
of $416=416 \div 8=\$ 52$. Hence, the of $416=416 \div 8=\$ 52$. Hence, the
175. Rule.-T'ulse such a fractioual part of the given number as the price is part of one dollir:

## examples for practice.

1. What will be the cost of 724 pounds of coffee at $33 \frac{1}{3}$ cts. a pound?
2. What cost 376 yards of calico, at 25 cts. per yd.? $\$ 241.331$.
3. At $6 \frac{1}{4}$ cts. a pound, what will 1056 cts. per yd.?
4. At $8 \frac{1}{2}$ cts. a dozen, what will 1050 los. of nails cost ? A. $\$ 66$.
5. What cost 384 yards of cost 387 dcz. of eggs ?
6. At $\$ 3.162$ each, what will 93 hats cost?
[^31]
## QUESTIONS

## INVOLVING THE RELATION OF PRICE, COBT, AND QUANTITY.

18(5. Case I.-The price and the quantity being given, to find the cost.

Analysis.-The cost of 5 units must be 5 times the price of 1 unit; of $\mathbf{b}$ units, if tiraes tho priee of 1 unit; of $\frac{5}{6}$ of a unit, $\frac{5}{6}$ times the price of 1 unit, etc. Henoe, the

18\%. Rule.-Multiply the price of one by the quantity.
178. Case II.-The cost and the quantity being given, to find the price.

Analyas.- By Case I, the cost is the product of the price multiplied by the quantity. Now, having the cost, which is a produet, and the quantity, which is one ol two factors, we have the product and one of two faetors given, to find the other factor. Hence, the
179. Rule. - Divide' the cost by the quantity.
180. Case III.-The price and the oost being given, to find the quantity.

Anslysis.- Reasoning as in Case II, we find that the oost is the produot of two factors, and the price is one of the factors. Hence, the
181. Rule.-Divide the cost by the price.
189. Case IV.-The quantity, and the price of 100 or 1000 , being given, to find the cost.

Analysis.-If the price of 100 units be multiplied by the number of units in a given quantity, the product will be 100 times the required rosult, heoause the multiplicr used is 100 times the true multiplier. For a similar reason, it will be the same if the given priee be 1000 units. The true value will be obtained oither by dividing the product by 100 or 1000 , as the case may be, or, by reducing the given quantity to hundreds and decimals of a hundred, or to thousands and decimils of a thousand. Hence, the
183. Rule.-I. Reduce the given quantity to hundreds and decimals of a hundred, or to thousands and decimals of a thousand.
II. Multiply the price by the quantity, and point off in the rosult as in multiplicrtion of decimals.
184. Case V.-To find the cost of artioles sold by the ton of 2000 pounds.

Analyas.- If the price of 1 ion or 2000 pounds be divided by 2 , the quotient will be the price of ton or 1000 pounds. We then have the quantity and the price of 1000 to find the cont. Hence, the

[^32]185. Rone.--Divide the price of 1 ton by 2 , and multiply the quotient by the number of pounils expressed as thousandths.

## hXAMPLES FOR PRACTICE IN THE PRECEDING OASER.

1. At $\$ 7.50$ per barrel, how many barrels of flour can be obtained for $\$ 217.50$ ?

Ans. 29 barrels.
2. If 1 gard of calico cost 23 cents, what will $31 \frac{1}{2}$ yards cost ?
3. What cost 15 tubs of butter, each containing $70 \frac{1}{2} \mathrm{lbs}$, at $\$ \frac{8}{1}$ a poumi?
4. What is the freight on $1244 \frac{1}{2}$ puunds from Montreal to Quebee, at $\$ 0.85$ per 100 lbs .?
5. If board for a family be $\$ 342.183$ Ans. $\$ 10.578+$. day?
6. How many dozen of eggs can be Ans. $\$ 0.93$. og can be bought for \$9.24, at lot ots.
7. What will 3921 feet of pine boards cost, at $\$ 17.25$ Ans. 88.
8. What is the value of 210 boards cost, at $\$ 17.25$ per 1000 ? at $\$ 17 \frac{3}{4}$ a ton ? 9. At $\$ 1 \frac{1}{2}$ a bushel, how many bushels of oats can be bought for $\$ 113.06 \frac{1}{4}$ ? Ans. $75 \frac{3}{8}$ bushels.
10. At 5 cents a pound, how many barrels of codfish, each containing 90 lbs ., can be purchased for $\$ 94.50$ ? Ans. 21 bbls.
11. What will be the cost of 1620 apple trees at $\$ 16 \frac{1}{2}$ per hundred ?
12. At $37 \frac{1}{2}$ cts. a bushel, what will $\frac{5}{8}$ of 456 bushels of potatues cost ?
13. How much must be paid for 486 feet of boards, at $\$ 20.25$ por $1000 ; 787 \frac{1}{2}$ feet of scantling, at $\$ 2.87 \frac{1}{2}$ per 100 ; and 4378 feet of lath, st $\$ 7.50$ per 1000 ?
14. What will be the cost of 4344 pounds of Paris plaster, at $\$ 3.87 \frac{1}{2}$ per ton?
15. If $32 \frac{1}{2}$ barrels of Montreal apples cost $\$ 9750$ Ans. $\$ 8.416 \frac{1}{2}$. per barrel?
16. How many acres of land can be bought for $\$ 2117$ Ans. $\$ 3$. an acre?
17. At $37 \frac{1}{2}$ cts. per bushel, how many barrels of pots. $376 \frac{7}{18}$. taining $2 \frac{1}{2}$ bushels, can be purchased for $\$ 50.62 \frac{1}{2}$ ? 18. If . 625 of a barrel of eels be worth $\$ 6.42$, Ans. 54.
19. What must be paid for 523 lbs . of meat, at $\$ 44^{5}$ ber wowh ? pounds?
20. What: cost 1080 lbs . of hay, at $\$ 12.75$ a Ans. $\$ 24.18 \mathrm{~J}$. mili feed at $\$ 15.50$ a ton? $\$ 12.75$ an, and $13 \$ 8 \mathrm{lbs}$ of
21. What will be the cost of 654 feet Ans. \$17.487. 1344 feet of siding, at $\$ 1.62 \frac{1}{2}$ per 100 ; and 2216 at $\$ 151$ per 1000 ; 1000 ?
22. A grocer bought 108 gallons of oil for $\$ 145.80$ Añ. $\$ 41.392_{2}$. of it by leakage. He mold the remainder at $\$ 1.70$, and loat 12 gal. much did he gain ?
23. A lumber dealer bought 106250 feet of lumber at $\$ 14.375$ per 1000 , and retailed it out at $\$ 1.75$ per 100 ; how much was his whole grain?

Ans. $\$ 332.03+$.
24. A load of plaster weighing 3360 pounds cost $\$ 5.71 \frac{1}{5}$, how unuch will a ton cost?
25. If $\$ 6.97 \frac{1}{2}$ be paid for 0.93 of a hundred pounds of beef, how much will one hundred pounds cost?
26. A farmer exchanged $42 \frac{3}{4}$ bushels of barleg worth $37{ }_{2}$ cts. per bushel, and $679 \frac{1}{2}$ lbs. of hay worth 75 cts. per hundred, for 18780 lbs. of plaster ; how much was the plaster worth per ton?
27. If 42 yards of cassimere cost $\$ 147$, what will be the oost of $34 \frac{4}{5}$ yards ?

Ans. $\$ 121.80$.
28. What is the value of 12 pieces of black cloth, each piece containing $27 \frac{2}{8}$ yards, worth $\$ 27$ a yard? Ans. $\$ 954.50$.
29. At $\frac{7}{8}$ per hushel, how many bushels of wheat may be bought for $\$ 18.90$ ? Ans. $21 \frac{3}{5}$.
30. A farmer sold to a merchant three loads of hay weighing res. pectively 2739,2217 , and $2881 \frac{1}{2}$ lbs., at $\$ 8 .^{\circ} 9$ per ton, and $421 \frac{1}{3}$ lbs, of pork, at $\$ 5.25$ per hundred. He received in exchange $46 \frac{1}{1}$ yards e muslin at $\$ 0.09,43$ yards of carpet at $\$ 4.50$, and the balanoe in m ney; how much money did he receive?

Let the pupils make out, in proper form, as the case may be, the following :

1. Sold by R. S. Gruham, Montreal, to E. Dudley, as follows: 1870, Jan. 3, $109 \frac{1}{2}$ yds. calico, at $18 \frac{1}{c}$ cts.; Feb 11, 430 yds. muslin, at $15 \frac{1}{2}$ cts. ; March 2, $37 \frac{1}{4}$ yds. sheeting, at $23 \frac{1}{4}$ cte.; May 16, $75 \frac{3}{5}$ yde. Irish linen, at 48 cts. ; $43 \frac{1}{8}$ yds. lace, at $78 \frac{3}{4}$ cts.

Footing of the bill, $\$ 161.007+$.
2. T. E. Clark bought of F. Larose \& Co., Quebec : 1870, June 10, $73 \frac{\mathrm{gal}}{} \mathbf{~ . ~ I r i s h ~ w h i s k y , ~ a t ~} 86 \mathrm{cts}$. ; $108 \frac{1}{4}$ gal. fine old rum, at $\$ 2.12 \frac{1}{2}$; 67 gal. Holland gin, at $\$ 1.45$; Aug. 14, $89 \frac{1}{3}$ gal. old cognac, at $\$ 2.67 \frac{1}{1} ; 107$ gal. brandy, at $\$ 1.37 \frac{1}{2}$; Sept. 7, $201 \frac{1}{8}$ gal. Scoteh gin, at $\$ 1.20$. T. E. Clark gave in part payment, Sept. 11,4 chests green ten, each $67 \frac{1}{2}$ lbs., at 56 cts. per lb. What balance was due F. L. \& Co., Sept. 12, when the bill was made out? Ans. $\$ 867.71 \frac{1}{4}$.
3. J. N. Webster, butcher, Kingston, sold to A. O'Regan, Oct. 6, 1870: A fillet of veal, weight $16 \frac{3}{3}$ lbs., at $10 \frac{1}{2}$ cts.; a loin of lamb, weight $7 \frac{1}{2}$ lbs., at $17 \frac{3}{4} \mathrm{cts}$; a leg of mutton, weight $13 \frac{3}{3} \mathrm{lbs}$., at $6 \frac{8}{4}$ cts. $;$ a leg of pork, weight $16 \frac{1}{4}$ lbs., at $9 \frac{1}{2}$ ets. ; a pig, weight $24 \frac{1}{2}$ lbs., at 121 cts ; a buttock of beet, weight $37 \frac{1}{4} \mathrm{lbs}$., at $7 \frac{1}{2} \mathrm{cts}$.

Footing of the bill, $\$ 11.31 \frac{1}{4}$.
4. If. Lemay \& Co. bought of Messre. A. Roche \& Son, Toronto, Sept. 3, 1870 : $1233_{5} \mathrm{lbs}$ g gum lac, at $\$ 1.15 ; 65{ }^{5}$ lbs. quinquina, at $\$ 14.10 ; 107 \frac{1}{2}$ lbs. rhubarb, at $\$ 2.10 ; 120 \frac{1}{3}$ lbs. sassafras, at $11 \frac{1}{4}$ cts.; $356 \frac{1}{2}$ lbe mastic, at $21 \frac{8}{4} \mathrm{cts}$.

Footing of the bill, $\$ 1415.918$.
5. Sold by B. H. Porter, Ottawa, to Miss D. Valcour, Aug. 20, 1870: 27矿 yds. Dresden lace, ${ }^{\text {at }} \$ 3.09$; $19 \frac{1}{4}$ yds. Flanders lace, at $\$ 1.62 \frac{1}{2} ; 83 \frac{1}{3}$ yds. gauze, at $45 \frac{1}{4}$ cts. ; $36 \frac{1}{2}$ yds. nuslin, at $18 \frac{1}{2}$ cto. $;$ 60 pair kid gloves, at 32 cts. ; $25 \frac{8}{6}$ dozen napkins, at $\$ 6.121$.

Footing of the bill, $\$ 335.36 \frac{1}{6}$
6. I

## : J.

bush., 87d per bt bush. ; Insura
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\& $\mathbf{O}^{\prime} \mathrm{N}$ crapes, 1751 y $\$ 1.80$; beville 10, by sight, f the acc
8. C.

6, 1870
391 yds drugget
$90 \frac{1}{2}$ cts.
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at $56 \frac{1}{2} \mathrm{c}$ paymen was the 10. T 1870, Ju chintz. e each 25 Aug. 2, ton, at 1

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6. At 2 bought for
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cts．per 780 lbs．
cost of 1.80
ce con－ 4.50
bought $21 \frac{8}{5}$ ． ing res－ 11 lbs， ards 0 in m

6．Invoiced，per Canadian Express，by S．Blanchard \＆Co．，Quebec， ：o J．Butler，Kingston，July 6， 1870 ：25 sacks tares，No．B，each $2 \frac{1}{2}$ bush．，at 34 cts．per bush．； 32 sacks pase，No．4，each 3 lunch．，at 871 cts．per bush．； 20 sacks data，No． 6 ，each 31 bush．，at $56 \frac{1}{2}$ cts． per bushy．； 8 racks malt，No．5，each $2 \frac{3}{4}$ bush．，at $\$ 1.37 \frac{1}{2}$ per bush．； 16 sacks beans，No．7，each $2 \frac{1}{2}$ bush．，al 85 cts．per bush． Insurance and cartage，$\$ 3.40$ ．Amount of Invoice，$\$ 221.56$.
7．T．McCullen \＆Co．，wholesale merchants，Halifax．sold to Lenoir \＆S＇Neil，Muntreal，as follows：May 19，1870， 85 pieces Norwich crapes，at $\$ 4.32$ ； 102 pieces Liverpool cottons，at si 7．63；June 5 ． $175 \frac{1}{8}$ gds．Antwerp sheeting，at $24 \frac{3}{3}$ cts．； $698 \frac{3}{5}$ yds．Amiens velvet，at $\$ 1.80$ ；Aus． $8,375 \frac{1}{3}$ gds．Yorkshire drab，at 65 cts ； $872 \frac{3}{4}$ gds．Ab－ beville merino，at $\$ 1.12 \frac{1}{3}$ ．On this are the following credits：July 10 ，by 18 bbls．Canadian flour，at $\$ 7.50$ ；Aug．12，by draft．at 3 day＇s sight，for $\$ 500$ ．What balance was due T．MacC．\＆Co．，Sept．3，when the account was settled？

8．C．N．Stonehouse of Montreal，sold to Mrs．F．Stephens，April 6，1870，and Ed．Noonan，his clerk，collected the amount of the bill： $39 \frac{1}{4}$ gds．camblet，at $31 \frac{1}{2}$ cts．； $47 \frac{3}{8}$ yds．shalloon，at 32 cts ； $27 \frac{8}{3}$ gds． drugget，at $46 \frac{1}{2} \mathrm{cts}$ ； $19 \frac{1}{8}$ gds．calico，at $11 \frac{1}{2}$ cts．； $41 \frac{1}{2}$ gds．chintz，at $90 \frac{1}{2}$ cts．； $34 \frac{1}{4} \mathrm{yds}$ ．calimanco，at $37 \frac{1}{3}$ cts．Amt．of the bill，$\$ 93.02 \frac{13}{13}$ ．

9．L．Rogers \＆Son，Quebec，sold to Mesars．O．Cooper \＆Co．，Cor－ el，as follows ：1870，April 5， $12 \frac{1}{3}$ doz．palm sack，at $\$ 9.42$ ；May 12 ， Port wine，red， 65 gal．，at $\$ 1.68$ ；421 gal．Claret，at $\$ 2.17 \frac{1}{4}$ ；June 10 ，Lisbon wine，white， $31 \frac{1}{4}$ gal．，at 45 cts．； $32 \frac{3}{3}$ gal．Rhenish wine， at $56 \frac{1}{2}$ cts．；July $8,25 \frac{1}{2}$ gal．Sherry wine，at $\$ 1.33$ ．Received in part payment，July 9,150 bush．oats，at $57 \frac{1}{2}$ cts．，and $\$ 60 \mathrm{inc}$ cash．What was the balance due to L．R．\＆Son，July 10 ？Ans．$\$ 240.63$.

10．T．J．Rinfret，bought of Testier \＆Gray，Montreal，as follows ： 1570，June 18， $4 \frac{1}{2}$ pieces muslin，each $37 \frac{1}{4}$ yd．，at $\$ 2.15$ ； $7 \frac{3}{3}$ pieces chintz．each $47 \frac{1}{2}$ gds．，at $92 \frac{1}{2}$ cts．；July 12， $4 \frac{1}{2}$ pieces Holland linen， each $25 \frac{1}{2}$ gds．，at $57 \frac{1}{4}$ cts ； $10 \frac{3}{3}$ pieces serge，each $19 \frac{1}{8} y d e$ ．，at 48 cts．； Aug．2， 17491 gds．，Randal cottons，at 17 cts ； $947 \frac{1}{4}$ yds．Lowell cot－ ton，at $18 \frac{1}{2}$ cts．What was the amount due，Aug．3，to T．\＆G ？

$$
\text { Ans. } \$ 1335.47
$$

## MISCELLANEOUS PROBLEMS．

1．What will be the cost of $15 \frac{1}{2}$ pound of honey，at $16 \frac{2}{3}$ cts．per pound ？

2．At $\$ 4 \frac{1}{2}$ per yard，how many yards may be bought for $\$ 11 \frac{1}{2}$ ？
3．Reduce $\frac{1763}{14}$ to a mixed number．
4．Reduce $\frac{1}{2}$ ，$\frac{2}{5}$ ，$\frac{8}{5}$ ，and $\frac{7}{8}$ to equivalent fractions having． $125 \frac{1}{1} \frac{13}{3}$ ． denominator．

5．The less of two numbers is $2378 \frac{2}{5}$ ，Ants．$\frac{n}{120}$ ，$\frac{80}{120}, \frac{75}{150}, \frac{105}{125}$ ． $w$ hat is the greater number？ $2378 \frac{9}{9}$ ，and their difference， $64 \frac{3}{3}$ ；

6．At 28 牟 cts．per bushel，how many bushels of Ans． $2442 \frac{33}{72}$ ． bought for $6 \frac{2}{2}$ cts．？

7．John has $6 \frac{1}{2}$ times $\$ 93$ ，James has 23 times Ans．$\frac{7}{12}$ bush． more has John than James？
8. What will $15 \frac{1}{3}$ cords of wood cost at $\frac{1}{2}$ of $\$ 9$ per cord
9. How many pounds in 4 bags, the first containing 360\%, the 000 nd $580 \frac{4}{5}$, the third $296 \frac{3}{4}$, and the fourth $375 \frac{9}{10}$ ? Ans. $1614 \frac{18}{8}$. 10. Andrew spent $\frac{2}{5}, \frac{1}{8}$, and $\frac{1}{1}$ of his money, and hail $\$ 54.50$ left; how much liad he at first? Ans. $\$ 384.7019$. 11. A servant had $f$ of his savings in one bank, $\{$ in another, and the remainder, which was 877 , in a third bank; how much money had he?

Ans. $\$ 140$.
12. Leo had $\frac{5}{5}$ of $\frac{5}{6}$ of $7 \frac{1}{2}$ times $\$ 7862$, and paid $\frac{1}{4}$ of $\frac{2}{5}$ of it for a Gr:m how much had he remaining? Ans. \$35379. 13. In 5 hogheads of sugar containing, respectively, $945 \frac{1}{2} \mathrm{lbs}$., $1054{ }^{10} 9$ lbs., $96.3 \frac{1}{7} \mathrm{lbs}$., $9012 \frac{23}{28}$, and 8995 , how many pounds?
14. Henry bought a bale of cloth for $\$ 96.37 \frac{1}{2}$; he disposes of it for of the cost, and by so doing, loses $\$ 2$ on a yard ; required the number of yards in the bale.
15. What is the value of $376 \frac{1}{2}$ acres of land, at $\$ 75 \frac{3}{3}$ Ans. 18 per acre? $\frac{9}{2}$.
16. If the transportation of $18 \frac{3}{4}$ tons of iron costs $\$ 48.15 \frac{3}{4}$, what is it per ton?
17. A man purchased 7 Ans. $\$ 2.624 .6$. yard; what did it 18. Charles has 634 shat ? 18. Charles has 634 sheep, which is 94 more than of $3 \mathbf{1}$ times David's number; how many has David? Ans. 243. 19. A man travels 4 miles in $\frac{3}{6}$ of an hour, how far will he travel in $1 \frac{1}{2}$ hours at the same rate?

Ans. 10 miles.
20. A merchant owned $\frac{3}{3}$ of a ship, and sold $\frac{1}{2}$ of $\frac{3}{3}$ of his share for $\$ 2400$. At that rate, what was the whole worth? Ans. $\$ 19200$. 21. What will $\frac{1}{2}$ of $10 \frac{7}{8}$ tons of coal cost, at $\frac{4}{25}$ of $\$ 42$ per ton?
22. If $\frac{1}{5}$ of $\frac{3}{4}$ of $3 \frac{1}{3}$ be multiplied by $\frac{1}{2}$ of itselif, and the product divided by $\frac{1}{3}$, what will be the result? ${ }^{2}$ Ans. $\frac{225}{1024}$.
23. B and C own 3144 sheep; how many has each, if $B$ has 18 times as many as C? Ans. B 1834, C 1310.
24. Edward has ${ }^{3}$ a dollar; he gives Louia $\frac{1}{2}$ of this amount, and then divides the remainder equally among three boys; what part does each of the 3 boys receive?
25. James obtains from two fields 344 bushels of oats; if the first yielded $\frac{3}{3}$ as much as the second, required the yield of each field ?
26. How long will it take a man to travel 553 miles, provided he trivels 31 miles per hour, and 97 hours per day ? Ans. 16 days.
27. I bought 15 loads of wood, each containing $11 \frac{2}{f}$ feet, cord neass ure, and divided it equally among 9 persons: what did each receive?
28. A tree, whose length was 136 feet, was broken into twe pieces hy falling; $\frac{3}{3}$ of the length of the longer piece equaled $\frac{3}{4}$ of the length of the shorter. What was the length of each piece? Ans. 72 and $6 \pm \mathrm{n}$. 29. How muny bushels of wheat worth 80 cts. a bushel, will pay for $\frac{5}{8}$ of a barrel of flour at $\$ 7 \frac{1}{5}$ a barrel? Ans. $7 \frac{1}{2}$ bush.
30. Dought $\frac{2}{2}$ of $\frac{5}{8}$ of $5 \frac{1}{2}$ yards of blue cloth at the rate of $\$ 3.50$ per yard; what is the cost?
31. If $\frac{6}{8}$ of $a$ barrel of eels costs $\$ 5$, how much will 2 tubs of eels vort, one containing $\frac{3}{2}$ of barrel, and the other $\frac{5}{8}$ of a barrel ?
32. If, $\frac{3}{5}$ of a gal. of porter is worth $\frac{3}{4}$ of a gal. of ale, and ale is worth \$3 per gal., how many gal. of porier will $\$ 20$ buy?

Ans. 24.
33. A oertain quantity of apples is to be divided anong 5 boys;

William is $t$ have $\frac{1}{4}$, John $\frac{2}{5}$, Peter $\frac{1}{10}$. Thomas $\frac{2 \pi}{5}$ and Paul the remainder, which is 24 ; what is the whole quantity ' be diviled? 34. What will be the cost of $7 \frac{1}{2}$ yds. of calico, at raj cts. per rd., and $12 \frac{1}{2}$ yds. of mmslin, at $18 \frac{3}{3}$ cts. per yard? Ans. s:3.esi. 35. Philip o; ns $\frac{3}{17}$ of a shipis curgo, valued at stamono: Daniel owns $\frac{15}{48}$ of the remainder; Joseph owns y $^{3}$ as much as Philip and Daniel; and Henry owns the remainder. How much dues each own? Ans. P, owns $\$ 87000:$ D, $\$ 210000$; J, $\$ 89100$; and H, $\$ 106900$. 36. I own $\frac{6}{8}$ of a steamboat, and sell $\frac{3}{4}$ of my share to $O$ wen for \$45000. What part of the steamboat have I left, and what is it worth at that rate?
37. If $4 \frac{3}{5}$ pounds of maple sugar cost 341 . $\frac{5}{3 / 2}$ left, worth 815000 . paid for $80 \frac{1}{4}$ pounds? 38. A grocer bough it in coffee at ${ }^{3}$ of a doll 2 tons of coal at $\$ 5 \frac{1}{4}$ per ton, and pad for so pay for the coal? 39. I have $\$ 800$ and wish to lay out $\$ 3108$ Ans. 133 lbs. a pound, and the remainder to lay out $\$ 346, \frac{8}{8}$ of it in sugar at 81 cts pounds of tea do I buy? 40. A merchant expended $\$ 840$ for dry goods Ans. $8591 \frac{1}{3} 59$ lbs. maining only $\frac{37}{7}$ as much money as he had goods, and then had rehad he at first?
41. A farmer has three fielda; the first contains $73{ }^{7}{ }^{7}$ gacres, the second $88{ }_{1}^{4}$ acres, the third 13910 acres. What is the largest-sized house-lots of the same extent intu which the three fields can be divided, and also the number of lots? Ans. Size of each lot, $71_{1}^{4}$ a.; 41 lots.
42. A man owning $135 \frac{3}{4}$ acres of land, sold $\frac{1}{1}$ of it, and gave $\frac{3}{8}$ of it to his son; what was the value of the remainder, at $\$ 57.80$ per
acre?
43. A merchant owns $\frac{7}{8}$ of a factory worth $\$ 4800$ ins. $_{2} \$ 2288.51 \frac{7}{3}$. his share to $A$, and the remaincory worth $\$ 48000$. He sells $\frac{B_{5}}{5}$ ceive from $A$ and $B$ respectively, and what How much does he reAns. From A, $\$ 25200$, what part has he remaining? 44. A drover bought 257 , 200 ; From B, $\$ 8400$; has left, $\frac{7}{10}$. bought 348 at $\$ 1.87$ per sheep, at $\$ 2.25$ per head; he afterward $\$ 1.75$ per head, and the remain then sold $\frac{2}{5}$ of the whole number at and how much?
45. A mother divided a basket of oranges Ans. Lost $\$ 35.87 \frac{1}{2}$ ters; to the first she gave 12 oranges among her three daugh. and to the third as mach as to the the third have? 46. What is the smallest sum of money with Ans. 48 oranges. purchase a number of sheep at $\$ 21$ eney with which a farmer could each, and a number of yearlings at $\$ 93$, a number of calves at $\$ 4 \frac{1}{2}$ could he buy with this money?

Ans. $\$ 112.50,50$ sheep, 25 calves, 12 yearlings. 47. In selling $46 \frac{1}{5}$ yards of merino for $\$ 50$ a I lost of the buying price. What was the cost of one yard? Ans. $81.318+$. 48. Bought 合 of a yard of cotton for $\frac{\mathrm{a}}{3}$ of 20 cents, and gave in pay. ment $1 \frac{1}{8}$ of a yard of cloth worth $\$ 32$ yd. Did I gain or lose by the
49. The $\frac{8}{11}$ of a fary are sown with corn; the $\frac{3}{14}$ with barley; and the remainder, containing 101 acres, planted with potatoes; how many acres dues the farm contain?
60. How many lushels of oats at $62 \frac{1}{1}$ cents per bus. $30{ }^{9} 97$ acres. are required to pay for 31 yards of cotton at $8 \frac{1}{4}$ cents a $y d$. , and $7!$ yards cloth, at $\$ 2.75$ per yard?

5l. If it required 34 days for a mason and Ans. $37 \frac{23}{2,30}$ bush. yds. of masonry, how long will it mason and his son to malie 22 cubic 52. If the $\frac{3}{5}$ of a hundred bottles of them to make a cubic yard? much will 3482 bottles come to ? much will 3482 bottles come to ?
5.3. What will he the price of 975 bushels of rye Ans. \$543.192. the same quality cost $\$ 5_{7}^{3}$ ?
54. A piece of silk velvet would bring $\$ 210$ were it $\frac{1}{6}$ longer ; know. ing the price of a yard to be $\$ 7.50$, required the length of the whole piece?
55. A market woman sold the 3 of a basket Ans. 24 yds. eggs to the remainder, the number she bad at of eggs, in adding 28 ed $\frac{1}{6}$ : how many had she?
56. A man has an income such, that if it wns. 35 eggs. price he paid for a mahogany writing desk, that is augmented by the $\$ 2.02 \frac{1}{2}$ per day. What is his income ? , that is $\$ 5.4$, he could spend 57. A weaver can weave a yard of linen in 17 Ans. $\$ 685.121$. it take him to weave: lat. 15 yds. ; 2nd. 20 yds hours; how long will $\frac{6}{17}$ of a yd.; 5th. $\frac{12}{12}$ of a yd.? Ans. $1^{\circ}{ }^{\circ} 8^{\frac{1}{2}}$ yds. ; 3rd. $4 \frac{5}{8}$ yds.; 4th.
 the $\frac{1}{4}$ and the $\frac{2}{8}$ of the sum paid for 93 lbs. be 60 cts ? 59 . In mixing 10 lbs . of bismuth with 6 lbs . of pevter and 4.2 lbs . of lead, we obtain an alloy which melts at the temperature of boiling water; required 1 st. what quantity of each metal enters into the mixt-
 6 th. $1 \mathrm{lb} . ; 7$ th. $1{ }^{1}{ }^{7} \mathrm{~J}$ lbs. ; 8th. 43 l lbs. ; 9th. $144 \frac{8}{7} \mathrm{lbs} . ; 10 \mathrm{th} .97 \frac{5}{2 \mathrm{~s}}$ lbs.? Ans. $1^{\circ} 1 \mathrm{lb}$. of bismuth, $\frac{5}{6} \mathrm{lb}$. of pewter, and $\frac{2}{5} \mathrm{lb}$. of lead ; $2^{\circ} \frac{8}{4} \mathrm{lb}$. of bismuth, $\frac{9}{20} \mathrm{lb}$. of pewter, and $\frac{3}{10} \mathrm{lb}$. of lead, etc. 60. A weaving machine makes $13^{7}$ yarde of cloth per ciay; how many yards will it make, lst. in 3 days; 2 nd . in $\mathrm{I}_{6}^{7}$ of a day ; 3rd. in 42 days; 4th. in 17 days; 5 th. in $32 \frac{1}{2}$ days; 6 th. in $47 \frac{12}{2}$ days; and 7 th. in $27+\frac{19}{27}$ days?
61. It would require 1800 Ans. $1^{\circ} 41 \frac{5}{8}$ yds.; $2^{\circ} 6^{6} \frac{9}{2} 8$ yds., etc. for a regiment ; but, on delivery, the cloth is found to be ton clothes and the purveyor is obliged to buy 2000 yards: what is the width of the cloth?
62. Paid $\$ 2235.45$ for 8 pieces of broadcloth of equal $1 \frac{7}{20} \mathrm{yds}$. remnant of $15 \frac{3}{10}$ yards: required the length of a piece knowing that one yard costs $\$ 10.50$ ?
63. The breadth of a painting is but the $\frac{7}{1 T}$ of its height. If the breadth equal the $\frac{4}{4}$ of $27_{13}^{705}$ yards, what is the height? $A .2, \frac{79}{195} \mathrm{yds}$. 64. A teacher of a select school has 60 pupils; 24 of them pay $\$ 1.25$ a month each, the $\frac{5}{g}$ of the remainder, $\$ 1.75$, and the rest $\$ 2.50$. How much does he receive from his pupils in 8 months? Ans. $\$ 840$. 165. The difference of time between two watches is $\frac{3}{4}$ of an hour ; one of them gains $4 \frac{3}{2}$ minutes per day, while the other loses 5 ? in the came time: in how many days will they again mark the same time?

## DINOMINATE NUMBERA.

66. How many herrings were there in a barrel of which 243 were sold at one time, then the ${ }^{3}$, and if there atill remain $\frac{2}{5}$. Required also the value of the whole barrel if the herrings were sold on an average Ans. 1080 herrings; $\$ 8.64$. 67. A dealer in porcelain bought a certain quantity of plates; he selle $\frac{1}{2}$ of them at 36 cents a doz., $\frac{1}{}$ at 38 cents a doz., and the remainder at 41 cents. How many dozen of plates did he buy, knowing that he paid 31 cents per doz n and gained \$1.05 by his bargain? 68. A man having bunght of bushels potatoes, forgets how much he pail per bushel; but remembers that there was a difference of $\$ 4$ between the $\frac{4}{7}$ and the $\frac{6}{6}$ of the sum laid out. How much did he pay per bushel?

$$
\text { 69. A dealer in furs sold a certain number of astrakhans. } \$ 0.37 \frac{1}{2}
$$

rate of $\$ 1.70$ a piece. Now, in adding to the ofrakhan skina at the $\frac{8}{13}$ of the same proceeds less $\$ 3.60$, he could pruceeds of his sales the \$19.20. How many atrakhan kins dit buy 25 fox skins at 70. A farmer sold t sheep and exp dit he -ell? chasing 5 lambs; the remapand expended the 8 of the sum in puritself less \$2.0\%. Requirel the of his money is equal to $\frac{1}{2}$ of the sum

Ans. $\$ 9$, the price price of a sheep and of a lamb?

## DENOMINATE NUMBERS.

186. A Simple Numbor 18 either an abstract or a denomi. nate number of but one denomination; as $18, \$ 12,40$ rods, 15 oranges (9).
187. A Compound Number is a collection of concrete units of different denominations (10): as. 3 feet 4 inches, 5 pounds 6 ounces, 2 days 8 hours 24 minutes.

Notr. - In sumple numbers and decimals the scale is uniform, and the law of increase and decrease is by 10. In compound numbers, the seale of increase and

## 188. A Denominate Number is any conerete number which

 expresses some particular kind or quantity; as 3 yards, 7 dollars 189. A Denominate Fraction is a concrete frotion whose integral unit is one of a denomination of some compound number. Thus, $\frac{8}{8}$ of a bushel is a denominate fraction, the integral unit feing one bushel; so are $\frac{2}{7}$ of a day, $\frac{3}{4}$ of a yard, etc., denominate fractions.190. Denominate Numbers express Currencies, Weights,
[^33]
## OURRENOI ${ }^{\text {G/ }}$.

1. Dominion of Canada Monet (77).
II. Old Oanadian Money, or Halifax Currenct.

TABLE.

| 4 larthinge make 1 penny, | d. |  |
| :--- | :--- | :--- |
| 12 pence | 4 shilling, | s. |
| 6 shillinge | 6 | 1 dollar, |
| 4 dcllars | \$ 1 pound, | . |



Meng-rivery 3d. of the old echage is equal to 6 eents of the new.
III. Einglat Money.

TABLE.
4 ferthingn (far. ar 4r.) make 1 nennv d.
12 perice
© 1 shilling
8.

20 shillings
" 1 pound or sovercign $£$ or sov.

Morme-1; Farthings are generally expressed as fractions of a peany; thus,

2. The ofd f , tho original abbreviation for shillinge, was formorly writton motime allilings and pence, and $d$, tho abbreviation for penoe, was omitted. Thwe 24, 68 , was written $3 f 6$. A straight line is now used in place of the $f$, and shilliegy wry writen on the left of it , and penoe on the right. Thus, $3_{2} 6,77_{3}$, eto.
\%. The prosent value of the sterling pound in the Dominion of Canade is \$4 Sex, whel hence the value of an English shilling is $24 \frac{1}{5}$ cents.
4. The outhe of Ragland in general ciroulation are: the sovereign ( $=\mathcal{E}_{1}$ ), adid lialfowervign ( $=100$. ), made of gold ; the orown $(=80$. ), the halforown ( $=20,6 d$. ), the forin $(=28$.$) , the shilling, the six-penoe, the four-penoe,$ 2 dhe thresoperee, made of oiver ; the penny, the half-penny, end the farbing, wite of coppow.
5. The atendard gold win of Yagland is 11 parts pure gold and 1 part zuoy.
 s75) comper, 24 penoo, in ooppor ooin, woigh a pound avoirdupois.

$$
\text { IV. Unifmp Staten Money } \mid \downarrow
$$

Horka.-
A carat woi
2. In apes

## V. French Monet.

191. French Ourreney is deeimal. The Franc is the unit of the currency, and is equal in value to $\$ 0.186$ Dominion of Canada money.

TABLE.
10 millimes make I centime.
10 centimes " 1 decime.
10 decimes " 1 franc.
Coins.- $\left\{\begin{array}{l}\text { Cold pieces of } 100,50,20,10, \text { and } 5 \text { francs. } \\ \text { Silver pieces of } 5,2,\end{array}\right.$ Coper pieces of 5, 2, and 1 france; 50 and 20 centimes. Copper or bronze pieces of $10,5,2$, and 1 centlines. dominion of oanada, enalise, and trench monets OOMPARED.
Evaline.


## WEIGHTS.

19)2. Weight is the measure of the quantity of matter a body coutains, determined according to some fixed standard. Three seales of weight are used in the Dominion of Canada, Great Britain, and the United States, viz. : Troy, Apotheoaries', and Avoir.
dupois.

## I. Troy Weiget.

183: Troy Weight is used in weighing gold, silver, ano jewele; in philosophical experiments, \&o.

TABLE.
24 grains (gr.) make 1 pennyweight, put. or dut.
20 pennyweights " 12 ounces 1 ounce, oz.
6 1 pound, oz.
prot. $\quad$ Er.

Porke.-1. Piamonds, eto., are woighed by carats, and fractione of a oarat.
4 ourat weighs 4 grains Troy woight.
2. In epeaking of the parity of gold
moaning $\frac{18}{2}$ pure gold and ${ }^{6}$ alloy.
2. 4 Troy pound is oqual to 372.085 Y jnoh gramamee.

## II. Apothecarige' Weight.

194. Apothecaries' Weight is used by pothecaries and physicians in mixing medioines; but medicines, in the quantity, are bought and sold by Avoirdupois weight.

TABLE.
20 grains (gr.) make 1 scruple, sc. or $\boldsymbol{2}$.
3 scruples " 1 dram, $d r$. or $\$$
8 drams " 1 ounce, oz. or 3 .
12 ounces " 1 pound, l6. or tb.

III. Avoirdupois Weight.
mo graium 100 n 16 lb Frone the Pr
2. T divide
3. T
roduce of the

| 16 drams (dr.) | make | 1 ounce, |  |
| :---: | :---: | :---: | :---: |
| 16 ounces | * | 1 pound, | lb. |
| 25 pounds | * | 1 quarter, | qr. |
| 4 quarters | \% | 1 hundred |  |
| 20 cwt., or 2000 lbe., | 1 | 1 ton, |  |

T.
poses of weighing.
TABLE.

$$
\begin{aligned}
& \text { Nots- The long or gross ton, hundred weight, and quirtor, were forinerly in } \\
& \text { common use ; but they have now fallen into disuuse among nerchants in Canada. } \\
& \text { The Custom- Douses oontinue to ure it. }
\end{aligned}
$$ The Custom-Louses onatinue to use it. Farmers and others weigh still some few articles by the long ton.

## LONG TON TABLE.



$$
\begin{aligned}
& \text { oz. dr. } \\
& \text { lb. } \quad 1=\quad \text { ar. } 16 \text {. } \\
& 256 .
\end{aligned}
$$

Morre. - I. Tceso graina Troy wate one pound mare welght, or add French wraight. This pound contalus 16 unncen; the ounoe, 8 drames and the dratio 7 th 100 nm , mare weight mat. It is also divided into two maros of $y$ ouncos eaeh. 16 lbe. maro weight make 108 lbs . Avoirdupois weight, or 131 fl lbe . Troy $;$ and, Froneh weighte and measures are yot It is proper to romark that the old the Provinoe of quebes.
2. To reduce or change the Jinglish pewad into Frenoh, muliply by 100 and divide by 108, and vice vorea.
3. To ohange a quatity from one waight to its oquivalent in another weight, of the weight required.

## MHASURES.

18(f). Heasure is that by which extent, dimension, capacity or amount is ascertained, determined according to some fixed standard. It may be properly divided into two classes.-Measures of Extension, and Measures of Capacity.

## MEASURES OF EXTENSION.

19\%\%. Extemsion has three dimensions - length, breadth and thickness.

A Line has only one dimension- length.
A Surface or Area has two dimensions - length and breadth. thickness. body has three dimensions - length, breadth, and

## I. Linear or Long Meabure.

 188. Linear or Long Measure, is used in measuring linesor distances.

1 inch (in.) =
12 inches
3 feet
$5 \frac{1}{2} \mathrm{yd}$., or 161 f . rods
furlongs, or 320 rode miles
691 miles (nearly)
360 degrees
table.
0.3363 French inch.
make 1 foot, ft.
$y d$.
$r d$.
fur.
mi.
lea.
deg. or ${ }^{\circ}$.

Norma.-1. For the purpose of moasuring oloth and othor geode eold by the yard, the gard in divided into halves, fourths, eighthe, and sixteenthy. The old table of oloth measure is practically obsolete.
2. In Mariners' Measure, 12 lines make 1 ; $20 \mathrm{~h} ; 4$ inches, 1 hana; ; faets 1 tathom; 120 fathoms, 1 cable-length; 7 f cable-lengths, 1 mile; of of 2 degre of the oircumference of the earth, 1 knot, or geographical mile, equal to $14 \frac{1}{2}$ itatute miles.
3. The length of a degree of latitude varies, being 68.72 miles at the equetor, 68.9 to 69.05 miles in middle latitudes, and 66.30 to 69.34 miles in the poler regions. The moan or average length is as stated in the table. A degree of longitude is greatest at the equator, where it is 69.16 miles, and it gradualiy deoreases toward the poles, where it is 0 .

## Table of the old Frence Linear Measures.



Notrs.-1. The French linear measures are in frequent use in the Provimes of Quebec.
2. The Engl. league $=15840$ Engl. feet, and the French league of Gamade $=15120$ French ft., or 16148.16 Engl. ft.; the difference betreen the twe $=$ 308.16 Engl. ft., or $288 \frac{4}{\frac{4}{8}}$ E French ft.

Surveyors' Linear or Long Measure. 199. A Gunter's Chain, used by land surveyors, is 4 rode or 66 feet long, and consists of 100 links.
table.

II. Square Meabure.
200. A Square is a figure bounded by four equal limes, perpendicular to each other. It is the Unit of Veroure for ons. paving, ete.
201. An Area or Surface is that which has length and breadth, without thickness.


The square in the margin in oalled three foot square, as it is three feet on each side. Elach of the small squares, within the large square, ropresents 1 square foot, or 1 foot equare. Since there are 3 square feet in enoh row, and 3 rows in the square, there are 3 times 3 aquare feet, equal to 9 equare feet in 3 feot square. Hence,

The area of a square or rectangle is found by multiplying it,
length by its width.
Nors.-From the above it will be observed thst the difference between 3 feet equare and 3 square feet is 6 square feet.

TABLE.
1 square inch (sq. in.) $=0.8767$ French inch.
144 square inches make 1 square foot, sq. ft.
$30 \frac{1}{4}$ square feet square yards $\quad$ " 1 square yard, sq. $y d$.
40 square rods os l square rod, sq. rd.
4 roods
" 1 rood, $\boldsymbol{R}$.
640 acres
" I square mile, sq. mi..


TABLE OF THE OLD FRENCH SQUARE MLASURES.
1 square inch (sq. in.) $=0.007921$ Engl. foot.
144 square inches make 1 square foot, sq. ft.
9 toises
100 perohes
7056 arpents
" I square toise,
4 I square perch,
" 1 square arpent.
" 1 square league,
sq. to.
sq. per.
sq. arp.
sq. $L$.
Notrs.-1. Artificers estimate their work as follows, vis. : glasing and stoneoutting, by the square yard; painting, plastering. paving, cerling, and paperhanging, by the square yards; flooring, partitioning, roofing, slating, tiliag, by by the square yerduare feet; briok-laying is estituated by the thoueand bricks, by the square yard, and by the square of 100 square feet

## MEABUARA.

2. In entimating the painting of monldinga, oeraleen, eto., the menanring-lino is earriod into all the inouldings and cornices.
3. In estimating brick-laying by either the aquare yard or the square of 100 feet, tho work is understood to loe 12 inches or 1, brick thick.
4. A thousand shingles are estimated to eover 1 square, being laid 5 inohes to the wosther.

SURVEYORS' SQUARE MEASURE.

202. This measure is used by surveyors in computing the

TABLE.


Notrs.-1. Canal and railroad engineers commonly use an ongineer's ohain, which consists of 100 links, each 1 foot long.
2. The contents of land are commonly estimated in square iniles, acres, and hundredths; the denomination, rood, is rapidly going into disuso. A squaso mile of land is also called a section.

## III. Cubic or Solid Measurx.

203. A Cube is a solid, or body, bounded by six equal square sides or faces. The sides of the squares are called its edges.
204. Cubic Measure is used in estimating the contents of solids, or bodies; as timber, wood, stone, etc.
205. The Contents, or Solidity, of a volume, is the number of times it contains a given unit of measure.

The measurements for computing solidity are always taken in the denominations of linear measure.

If each of the sides of a cube is 1 foot, it is called a cubic foot. If each of the sides of a cube is 3 feet $=1$ yard, it is called a oubic yard.


The annezed oube represents a oubic yard. Since each of the edges of a eubio yard is 3 feet, oach of its froes will contain 3 times 3 equal to 9 square feet. If, from one face of this oube, wo cut off a piece 1 foot in thicknoss, we evidently have 9 solid feet; and as the whole blook is 3 feet thiok, it must contain 3 times $9=27$ solid fect. Henoe,

To find the solid contents of a cube, multiply its length, breadth, and thicleness together.

TABIE．


## table of rrence measures．

1728 anbic inchzs
216 cubic feet
${ }_{\text {make }}^{1}{ }_{1}$ cubic foot，
cu．ft．
1000 French cubic feet
1000 cubic toises

$$
\begin{aligned}
& \text {. } \quad 1218.186432 \text { En. to. } \\
& . . \quad 9745.491456 \text { cubl. cub. feet. }
\end{aligned}
$$

the space it oocupies in cubie transportation companies ostimate light freight by
2．A pile of wood 8 fers and heavy freight，by weight．
and a cord foot is one foot in length of wide，and 4 feet high，contains one oord；
3．A perch of stone or $1 t^{\circ}$
4．Juiners，bricklayers and 1 foot high． sto．，of one half the openinge or rasons，make an allowance for windows，doors， mating their work by cubic menomal spacs．Bricklayers and masons，in esti－ walls of houses，cellarg，ato．，but eatimate no allowance for the corners of the entire length of the wall on the outsidg．
b．Engineers，in making estimato
dimensions with a line $\begin{gathered}\text { cstinatos for excavations and embankments，take the }\end{gathered}$ connputations are mado in feet ure divided into feet and decimals of a foot．The yards．In civil engineering，the decimals，and the results are reduced to cubio excavations and einc．unknents are finally reluced．

6．In scaling or monsuring timber for ship in
contents of round timber is deducted for that will make 36 fect of hewn or sawed waste in hewing or sawing．Thus，a log by neasurement ；but its tanrket value timber，actually contains 45 cubic fcet samed timber．Henee，the cubic contents of 36 equal to 36 oubic feet of hewn or timber，as estimated for market，are idontical．feec of round and 45 feet of hewn
7．Sawed timber，joists，planks，and soantlings are now generally bought and sold by what is callod board meaowre．
8 A cubio foot of distilled water at the maximurn density，at the level of the sea，and the barometer at 30 inches，is equal in weight to $62 \xi \mathrm{lbs}$ ．or 1000 os．

## MEASURES OF CAPACITY．

玉毛的．īfeasures of Capacity are all cubio measures，solid． ity and capacity being referred to different units．Capacity sig． nifies extent of space．
207．Measures of capacity may be properly subdivided inte two elseses，Measures of Liquids and Meusures of Dry Subsluntece．

## I. Liquid Measure.

:208. Liquid Measure, also called Wine Measure, is now used for measuring all kinds of liquids.

TABLE.
4 gills (gi.)
2 pints
4 quarts
$31 \frac{1}{2}$ gallons
2 barrels
2 hogsheads
2 pipes, or 4 hogsheads
$\begin{array}{cll}\text { make } 1 \text { pint, } & \text { pr. } \\ \text { " } & 1 \text { quart, } & \text { qt. } \\ \text { " } & 1 \text { gallon, } & \text { gal. } \\ \text { " } & 1 \text { barrel, } & \text { bbl. } \\ \text { " } & 1 \text { hogshead, } & \text { hhd. } \\ \text { " } & 1 \text { pipe, } & \text { pi. } \\ \text { " } & 1 \text { tun, } & \text { tun. }\end{array}$
pt. gi.
gal. $\quad$ gt. $1=\quad 2=\quad 4$.
bbl. $\quad$ gal. $1=1 \begin{aligned} & 1=8 \\ & 4= \\ & 8\end{aligned}$
pi. $\begin{aligned} \text { hhd. } 1=2=31 \frac{1}{2}=126=252=1003 . \\ 62=252=504=2016 .\end{aligned}$
tun. $1=2=4=126=504=1008=4016$. $1=2=4=8=252=1008=2016=1032$.
Norcs.-1. The Kaglish linperial gallon oontains 277.274 oubio incher or 10 lbs , A volrdupois of pure distilled water, weigiod at a temperature of $82^{\circ}$ Fahronheit, and under a barometer pressure of 30 inohos.
2. In the United stater the wine gallon contains 231 oubic inches, and the beer gallon 232 oubio inohes. Tho gallon of England is therefore abont equal to 1.2 gallons United States Wine Measure.
3. By an Aot of the Imperinl Parliament, 1826, the Imperial gallon of $\mathbf{2 7 7 . 2 7 4}$ oubic inches, was adopted as the only gallon, and is therefore the standard for both liquid and dry mensur
4. Becr is usaally sold by the gallon; sometimes, howover, in casks of $s, 10$, 20 gals. eto. The beer barrel oontains 36 gallons, ani the hogshead, 54 gallong.

## II. Dry Measure.

209. Dry Measure is used in measuring artioles not liquid, as grain, salt, fruit, roots, \&c.

TABLE.


Notes. sua's lear 805 d. 5 h .
ternal dismetar in 18 l inches, Winohester bushel is an upright eylinder whome in. inohos, or 77.627 lbs . Avoirdupoia of pepth 8 inches. It centaing $2[50.4$ oubic barometer. The bushel of Canais of pure distilled water, at $62^{\circ} \mathrm{Fahr}$. and 30 in. deep, and must oontain 2338.917 Engl 18 inches in diameter, and 8.701 inohos The atandard onit of Dry Measure ingl. oubio inches, or 1920 French oubio inchea. The standard unit of Dry Measure in the United States is the Winobester bushol. 6s 18.789 inohea in diameter, and 8 inchreat Britain is the Imperial bushol, whioh or 80 lbs . Avoirdupois of pure distilled deep. It oontsins 2218.192 eubic inches, 2. Grain is frequently bought and water at $62^{\circ}$ Fabr. and 30 ie. barometer. is, vis. : of wheat, 60 lbs . ; of ryo, $5 B \mathrm{lb}$ by weight. The atandard per bushel $\mathrm{lbs} . ;$ of oats, 34 lbs ; of peas, 60 lbs . ; of ; be Indian corn, 56 lbs ; of bariey, 48 of flax-seed, 56 lbs ; ; of Timothy-soed ; or reans, 50 lbs . ; of buokwheat, 40 lbs ;
3. The old Frenoh Weights and or red clover-seed, 30 lbs.
logal in the Province of Queboe.

## MEASURE OF TLIME.

214. Time is the measure of duration. The unit is the day. and the table is made up of its divisors and multiples.
or 10 lbs , brenheit, and the equal to 277.274 lard for
of 5,10 . gallons.
liquid,

TABLE.

| 60 seconds (sec.) <br> 60 minutes |  |  |  |
| :---: | :---: | :---: | :---: |
| 60 minutes <br> 24 hours | * | 1 hour, | $\underline{\min .}$ |
| 7 days | ! | 1 day, | do |
| 4 weeks | , | 1 week, | wh. |
| 365 days | " | 1 lunar month, | mo. |
| 366 days | 16 | 1 common year, | $y r$. |
| 12 calendar mo | " | 1 leap year, | $y r$. |
| 100 years | ${ }^{\prime}$ | 1 year, 1 century. | $y r .$ $\boldsymbol{C}$ |

The calendar year is divided as follows :-
No. of months. Seasons.

| of months. <br> 1 | Seasong. | Names (f montha. |  |  |
| :---: | :---: | :---: | :---: | :---: |
| $2$ | Winter, | $\left\{\begin{array}{l}\text { January, } \\ \text { February }\end{array}\right.$ | Jan. | 31. |
| 3 |  | S March, | Feb. | 28 or 29. |
| 4 | Spring, | $\left\{\begin{array}{l}\text { March, } \\ \text { April, }\end{array}\right.$ | Mar. | $31 .$ |
| 6 |  | May, | Apr. | 30. |
| 6 | Sum | \{ June, | Jun. | 30. |
| 8 | Summ | $\left\{\begin{array}{l}\text { culy, } \\ \text { August }\end{array}\right.$ | July. | 31. |
| 9 |  | August, | Aug. | 31. |
| 10 | Autumn, | $\left\{\begin{array}{l}\text { September, } \\ \text { October, }\end{array}\right.$ |  | 30. |
| 111 | Winter, | \{ November, | Oct. Nov. | 31. |
| 12 | Winter, | December, | $\begin{aligned} & \text { Nov. } \\ & \text { Dec. } \end{aligned}$ | 30. 31. | sur's leaving either equinox or solsticical Year is the time moasured from the 805 d .5 h .48 min .40 I's. $^{5}$ sec.

2. The Jutian Pear, eo called from the calendar instituted by Jnlina Cemar, contains $365 \frac{1}{4}$ days, as a medium; three years in saccersion contaising 365 daya, and the fourth year 366 days; which, as compared with the true solar year, produces a yearly error of $11 \mathrm{~m} .10 \frac{3}{10}$ soc., or of 1 whole day in about 120 years.
3. The Giregorian Year, or that instituted by Pope Gregory XIII, in the year 1582, and which is now the Civil or Legrl Year in use among the different natlons of the earth, cuntnins 365 days for three years in succession, and $360^{\circ}$ daye for the fourth, excepting centennial years whose number cannot bo exactly divided by 400. The Gregorian year gives an error of only 1 day in 3866 days.
4. The civil day begins and ends at 12 o'elock, midnight. The astronomical day, used hy astronomers in dating events, begins and ends at 12 o'clock, noon.
5. In most business transactions 30 days are called 1 month.

## TABLE:

GHOWING THE NUMBER OF DAYS FROM ANY DAY OF ONE MONTH TO THE SAME DAY OF ANY OTHER MONTH IN THE SAME YEAR.

| $\begin{aligned} & \text { PROM } \begin{array}{l} \text { DNY } \\ \text { DAY } \end{array} . \end{aligned}$ | to the samet day of |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Jan. | Feb. | Mar. | Apr. | 1185 | June\| | July | Aug. | Sept. | Oct. | Nov. | Deo. |
| January | 365 | 31 | 69 | 90 | 120 | 151 | 181 | 212 | 243 | 273 | 304 | 334 |
| February | 334 | 335 | 23 | 59 | 89 | 120 | 150 | 181 | 212 | 242 | 273 | 303 |
| March | 306 | 337 | 365 | 31 | 81 | 92 | 122 | 153 | 184 | 214 | 245 | 275 |
| Apri] | 275 | 306 | 334 | 365 | 30 | 61 | 91 | 122 | 153 | 183 | 214 | 244 |
| May | 245 | 270 | 304 | 335 | 365 | 31 | 61 | 92 | 123 | 153 | 184 | 214 |
| June | 214 | 245 | 273 | 304 | 334 | 365 | 30 | 61 | 92 | 122 | 153 | 183 |
| July | 184 | 215 | 243 | 274 | 304 | 335 | 365 | 31 | 62 | 92 | 123 | 153 |
| August | 153 | 184 | 212 | 243 | 273 | 304 | 334 | 365 | 31 | 01 | 92 | 122 |
| September | 122 | 153 | 181 | 212 | 242 | 273 | 303 | 334 | 3 35 | 30 | 61 | 91 |
| October November | 92 61 | 123 92 | 151 120 | 182 151 | 181 | 213 212 | 273 242 | 304 | 335 | 365 3 | ${ }_{31}{ }^{3}$ | 61 |
| Decermber | 31 | 62 | 90 | 121 | 11.1 | 182 | 212 212 | 243 | (3044 | 3334 | 365 <br> 335 | 30 365 |

For example, to find the number of daya from April 4th to Novomber 4th, we look for April in the left vertical column, and Novomber at the top, and, where the lines interseot, is 214 , the number sought. Again, to find the number of d $c y s$ from June 10th to September: 16 th, we ind the difference betwoen June 10th and September 10th to be 92 days, and add 6 days for the excess of the 16 th over the 10th of September, so we have 98 days as the exact difference.

If the end of February be included between the points of a time, a day must be added in leap year.

When the time exeeeds one year, there must be added 385 daya for each year.

## CIRCULAR MEASURE

211. Circular Measure, oalled also Angular Measure, is used principally in surveying, navigation, astronomy, and geography; for reckoning latitude and longitude, determining locations of places and vessels, and computing difference of time.

## An

Tho center is one which


Note. of $90^{\circ}$;

## 12 unit

12 doze

24 shee 20 quir
212. An Angle is the difference of direction of two lines which mett at a point; thus, A, $B, C$, is an angle. The lines are called the sid $s$ of the angle, and the point where they meet is called the !


21is. A Circle is a plane figure bounded by a curved line, all the parts of which are equally distant from a point within called the center.

A circumference is the curve line which bounds a circle, and alwaye contains 360 degrees.
An arc is any part of the circumference, as C D, D E.
The are within the sides of an angle whose vertex is on the
12 units make 1 dozen.
12 dozen

24 sheets make 1 gross.
20 quires
 center of a ciacle is the measure of the angle; thus, the arc C F , is one fourth of the circumference, and measures the angle $\mathbf{E} \mathbf{B C}$, which contains 90 degrees.

TABLE.

Note.-A qualrant, or right angle, is one-fourth of a ciroumference, or an are of $90^{\circ}$; as A B. $60^{\circ}$ is called a sextant, or $\frac{1}{6}$ of a circle.

MISCELLANEOUS TABLES.
COUNTING.

## THE METRIC SYSTEM OF WEIGHTS AND MEASURES.

The metric system of weights and measures-so oalled, because the metre is the unit from which the other units of the system, whether of length, area, solidity, capacity, or weight, are derived -originated in France in 1790. It was determined and established as follows: a very accurate survey of that portion of the terrestrial meridian, or north and south circle, between Dunkirk in the north of France, and Barelona in Spain, was made under the direction of Government, and from this measurement the exaot length of a quadrant of the entire meridian, or the distance from the equator to the north pole, was computed. The ten millionth part of this arc was denominated a metre, and from this all the standard units of measare and weight are derived and determined.

The metric system was finally made the only legal system throughout the whole of Franoe in 1841. Since that time, it has been adopted by Spain, Belgium, and Portugal, to the exolusion of other weights and measures. In Holland, other weights are used only in compounding medicines. In 1864 , the system was legalized in Great Britain; and its use, either as a whole or in some of its parts, has been authorized in Greece, Italy, Norway, Sweden, Mexico, Guatemala, Venezuala, Ecuador, United States of Columbia, Brazil, Chili, San Salvador, and Argentine Republic. In 1866, the use of the metric systen of weights and measures, was authorized by Congress for the whole of the United States.

## TABLES AUTHORIZED BY CONGRESS OF THE UNITED STATES.

measures of lengths.

| Metrio Donominations and Values. |  | Equivalents in Denominations in use. |
| :---: | :---: | :---: |
| Myriametre,... | 10,000 metres,....... | 6.2137 miles. |
| Kilowetre,...... | 1,000 metres,....... | 0.62137 miles, or 3280 feet, 10 inohes. |
| Hectometre,... | 100 metres,........ | 328 feet and 1 inch. |
| Decametre, .... | 10 metres, | 393.7 inches. |
| Metrre,......... | 1 metre,........ | 39.37 inches. |
| Decimetre, ..... | $\frac{1}{10}$ of a metie,... | 3.937 inches. |
| Centimetre,.... | $\frac{1}{100}$ of a metro,... | 0.3937 inch. |
| Millimetre, ..... | 1000 of a motro,... | 0.0394 inch. |

MEASURES GF GURTAOES.

RES.
because system, derived blished restrial in the ler the exact from llionth all the mined. system it has olusion ts are m was or in orway, States public. isures, ates.

| Motric Denominations and Values. |  | Equivalente in Denomination in |
| :---: | :---: | :---: |
| Heotare, ........ | 10,000 square metres, | 2.471 acres. |
| AnR,............ Centiaro,...... | 100 squaro metres, 1 square metre, | 1119.6 square yardm. |

mensures of solids.

| Metrio Donominations and Values. |  | Equivalents in Denominationg in nse. |
| :---: | :---: | :---: |
| Decastere,...... | 10 cubio metres, ...... | 13.079 oubic yards. |
|  | 1 cubic metre,...... | 0.2759 of a cord of wood. |
| Deoistore,...... | 100 cubic decimetres,. | 3.53144 cubic feet. |

MEASURES OF CAPacity.


WEIGHTS.

| Metric Denominations and Values. |  |  | Equivalents in De- |
| :---: | :---: | :---: | :---: |
| Names. | Number of grammes. | Weight of what quantity of water at maximum density | Avoirdupois weight. |
| Millier, or tonneau, Quintal, | 1,000,000 | 11 oubic metre, ............... | 2204.6 pounds. |
| Myriagramme,......... | 100,000 | 1 hectolitru, ................. | 220.46 pounds. |
| Kilngramme, or kilo, | 10,000 1,000 | 10 litres, ....................... | 22.046 pounds. |
| Heetogramme, ....... |  | 11 litre,......................... | 2,2046 pounds. |
| Decagramme, ....... |  | 10 cubio contimetres,....... | 3.5274 ounces. <br> 0.3527 ounce. |
| Gramer, .............. Decigramme, ....... |  | 1 cubic contimetre, ......... | 15.432 gr . Tr. W. |
| Contigramme, ......... |  | 17 ${ }^{1} 10$ of oubic eentimetre,... | 1.5432 grains. |
| Milligramme,......... | Too | 10 oubic millimetres,........ | 0.1643 of a grain. |

MEASURES OF ANGHAN.

| Matole trenominations and Values. |  | Equivalents in Denominati |
| :---: | :---: | :---: |
| Givelat....... | 400 grades, .............. |  |
| Quxilate... | 100 grades.................. | 1 aircle or $3600^{\circ}$. <br> 1 quadrant or 900 |
|  | 1 grado,...................... | 54 ininutes. ${ }^{\text {a }}$ ( $0^{0}$. |
| Steondi.u.o. | 100 of a $9 ., \ldots . . . . . . . . . . . .$. <br> to $\frac{1}{6}$ of | 32.4 seconds. |
|  |  | 0.324 of a aceond. |

## NOMENCLATURE AND TABLES

There are eight kinds of quantities for which tables are usually Comstructed; viz., Lengths, Surfuces, Volumes or Solids, Capacities, Weishts, Values, Times, and Angles or Ares. The table for Times is the same in the metric as in the ordinary system. The table for Angles is constructed upon a centesimal scaie. The table for the other six kinds of quantities are constructed upen $s$ deeimal seale. In each of the tables for Lengths, Surfaces, Volumow, Capacities, and Wuights, there are eight denominations of anity,-one principal and seven derivative. The principal units are the melre, which is the base of the system, and those derived dircetly from it. The two following tabular views present the fisctes ressatding the principal and derivative units, which should be fixed in the memory.

[^34]EMBRACING AS PRINCIPAL BOOKE,

# CASH BOOK. DOMESTIC ANJ FOREIGS INVOICE BOORS, SALES BOOK AND JOURNAL; 

ANI AS AUXILIARIES,<br>INVENTORY BOOE AND BULJ BOOK.

With a rol'tine taken fiom an extensive business hocse.

Remarks.-The particular feature of this set consists in the manner and form of original entries, which are made in separate books,-elvewhere used as ausiliaries,-from which they are either journ:lized, or passed directly to the Ledger at stated periods. This method has many advantages over consecutive entries in the Day Book, and, in one form or other, is adopted generally in all large establishments. The labors of the Book-keeper are thus divided up, and the separate departments of the business reeeivo such special record as to present all the facts in their clenrest light. Thus, if any particular information is desired respecting purchases, all the facts can be found at once in the Invoice Book; in the same manner, the facts and condition of the sales cim bo found in the Sales Book; the receipts and disbursements of eash, in the Cash Book, etc.

In thי previous sets, these books are represented; but they are used only as auxiliaries, the entries of the business being made in the other books without reference to them. This plan, it will be evident, although possessiug some merits, incolves a large amoun of unnecessary habor, which would prove a great objection in extensive house.. The special lanks themselves, however, are so essential in every well-regulated husiness, that they wonld receive favor, even at the expense of this alditional labor. If, t ! refore,

## JOBBIN ANJ IMPORTIXG BUSINRM.

they can be used without additional lubor, and even at a reduction of labor, it would seem that no farther argument wonld br yeedrid to secure their adoption.

The Invoice Books, and the Salos Book which follow, contan all purchases and sales of merchandise, with the condition thereof. AM sales and purchases not mude for cush pass from these books to the Ledger; all others, from the Cash Book.
$t$ consists in the nade in separate which they are ger at stated pcconsecutive enis adopted yenehe Book-keeper of the business facts in their on is desited resonce in the Inondition of the ts and disburse-
d ; but they are ss being made in ; plan, it will be ; a large amoun objection in exrowever, are so y would receive r. If, $\mathrm{t}^{1}$ refore

## ROUTINE FOR AUGUST 1871.

Nore.-To get the fuil advantage of this Sot, the student must pnystimet at. tention to the rontino of transactions as indioated bolow. Let hin mater atoorled withe different hooks precisely in the order given. Let him mako thie oxereises connectod wlth the Foreign Inroice extensions made by himself. The and roduction of curronoies, are highly essentiook, involving compound numbers, dian decimal ourreney, we bave taken essential. In reducins sterling to Canaladded to each foroign involece, tho duies, which the $£$ sterling. We have also tended with the invoice, but posted from the being paid in cash, are nor ex. lmporting houses, tho duties are not extended in tho Book. However, in many the Cash Book.

1. The broks are openel, as per first Journal entry. (Iuventurv Book copied-Cash Book commenced with balance on hand-Bill Book written up to show the notes, recejvable and payable, as ind cated in Journal entry.). . . . Bo't of S. B. Madlen for cash, Invoice of Prints, etc., $\$ 1303.76$ (Dom. I. B.-C. B.). . . Sold L. Reaudry, St. ... Sold Mdse this day, per., Inv. of Goods, $\$ 699.06$, íS. B.-13.13.) Rec'd cash on acct. of S. per Petty Cash Book, $\$ 97.50$ (C. B.).... for Blank Books \$5.25, (C. Boyce, \$600, (C. B.)-8. Pail A. Miller $\$ 800$, (C. B.).-5. Received of J. . Lent J. E. Lawrence, for one day, (C. B.). . . Paid cash for Postage St Lawrence, return loan, $\$ \$ 00$, Paid J. A. Hall, on private ostage Stamps, etc., $\$ 7.50$, (C. B.)... R. Boyce, in full of acct., $\$ 1440$, $\$ 80$, (C. B.)-6. Rec'll cash of S . in full of acct., $\$ 175$, (C. B.)- 8 . (C. B.)-7. Paid R. P. Davis cash, $\$ 120$, (C. B.)-16. Ro't of P. McHugh Mdse. per Petty Cash Book, Invoice of Cotton, $\$ 1006.144$. (Dom. I $A$ Co., on our note at 6 mos , steamer St. David, from J. Dutly \& C. B.-B. B.) ...Received per and Silk Goods, $\$ 221.11$; Paid \& Co., Liverpool, Invoice of Cotton C. B.)-11. Bo't of N. Casey \& Alties in cash, $\$ 32.09$, (For. I. B. vise of Bleached Shirtings \& Bro., on our note at 8 months, In. F. Peters \& Co., Three Rivers and Gloves, $\$ 273.52$, (S. B.-B. B.) note at 6 mos., Invice of Hose terage, etc., \$25, (C. B.)-14. Sold ...Paid cash for Drayage, Por note at 8 monthes. Invoice of Shin Hazel \& Foy, l'Islet, on their Rec'd cash in fill of J. N. Galt' Received per Steamer Nestorian, note, \$1264, (C. B.-B. B.)-15. Invoice of Goods, $\$ 246.36$; Paid dutic Chields \& Co., Manchester, C. B.). . . Suld Mdse. for cash, as in cash, $\$ 36.95$, (For. I. B. (C. B.)-18. S. I. Perron's as per Petty Cash Book, \$110.50, 18. S. I. Perron's note discounted, $\$ 800$ : Discount off,
$\$ 15.60$, (C. B.-B. B.)-20. Sold Stein \& Co., St. Mary, P. Q., on their note, at ( months, Invoice of Printe, $\$ 1425.48$, (S. B.-IB. B.) ....Paid T. J. Colston on private acot., $\$ 100$, (C. B.) - $\$ 1$. Sold Mise. for cash, per Petty Cash Book. $\$ 102.50$, (C. B.)-28. Paid cash in full of note, favor of G. H. Shills, $\$ 3800$, (C. B.-B. B.)-25. Sold Byrne \& Son, Kamouraska, for cash. Invoice of Goods, $\$ 400$, (S. B.-C. B.).... Stein \& Co.'s note discounted; Face of note, \$1425.48. Discount off, $\$ 50.44$, (C. B.-B. B. . . Rec'd per steamer Asia, from J. A. Knight, Dublin, Invoice of Goods, 840.14 ; Paid dnties in cash, $\$ 105.63$, (For. I. B.-C. B.).... Bo't of L. Power \& Co., for cash, Invoice of Printe, \$893.63, (D. I. B.-C. B.) ... Paid clerk hire in cash. \$50, (C. B.)-27. Sold Mdse. for cash, as per Petty Cash Book, $\$ 160$, (C. B.)-88. Sold C. E. Lawson, Sorel, on his note at 8 months, Invoice of Goods, \$171.04, (S. B.-B. B.)-29. Paid C. S. Mitchell, on pri ate acct., $\$ 130$, (C. B.)-30. Sold Mdse. as per Petty Cash Book, *2, (C. B.)-31. Rẹceived cash of W. E. Gray, in full of acct., \$14 30.20.

## ROUTLSE FOR SEPTEMBER 1871.

1. Sold A. M. Rooney \& Co., on their note at 6 months, Invoice of Gools, $\$ 1432.89$, (S. B.-B. B.) ...Paid cash for Drayage and Porterage, $\because 17.50$. (C. B.)-2. Lent L. Morgan, 8600, (C. B.)-8. Soll Mdse. as per Petty Cash Book, $\$ 70.20$, (C. B.)-5. Discounted our note, favor of A. G. Cook; face of note $\$ 1500$. Discount off: $\$ 29.75$, (C. B.-B. B.) . . . Sold S. D. Higgins, Quebec, on his note at 8 mos., Invoice of Goods, 8527 , (S. B.-B. B.)-6. R. M. Rooney \& Co.'s note disconnted; face of note $\$ 1432.89$. Discount off, $\$ 49.60$, (C. B.)-\%. Sold Mdse. as per Petty Cash Book, $\$ 150$, (C. B.)-8. Sold J. F. Nestor, St. Thomas, on his note at 8 months, Invoice ot Midse. $\$ 752.57$, (S. B.-B. B.)-10. Reo'd per steamer Africa, Glasgow, Invoice of Gooda, \$143.19. Duties paid in oash, $\$ 276.10$, (For. I. B.-C. B.)-12. Sold Mdse. as per Petty Cash Book, \$218.50, (C. B.).... Paid cash for Drayage, $\$ 75$, (C. B.)-15. Sold B. R. Woods, Ottawa, on his note at 8 months, Invoice of Goods, $\$ 908.29$, (S. B.-B. B.) ... Paid R. A. Hudon cash on private acct., $\$ 140$, (C. B.)-17. Sold Mdse. as per Petty Cash Book. $\$ 362.40$, (C. B.) -\$0. Ree'd per steamer St. Patrick, from J. Bailey \& Son. Liver pool, Invoice of Goods, $\$ 188.62$. Paid duties in cash, $\$ 2 \$ .29$, (For. I. B.-C. B.) .. . Bought of Bell \& Archer, on our note at 6 months,
 Levis, for cash, Mdse., 892.3.40, (S. B.-C. B.)-2B. Sold Mdse. as per Petty Cash Book, \$180, (C. B.)-25. Sold E. Curran, Richmond, for cash, Iuvoice of Gloves, $\$ 460.75$, (S. B.-C. B.) . . . . Paid Postage, Porterage, etc., in cash, \$12, (C. B.)-27. sold Lee \& Strang, To ronto, on their note at 8 mos., Iıvoice of Mixtures, $\$ 3303.71$, (S. B. -B. B.)-28. Sold T. Ross \& Co., Kingaton, on 8 months note, In voice of Goode, $\$ 578.52$, (S. B.-B. B.)--30. Sold A. R. Jacob, Batiscan, on note at $3^{\circ}$ months, Invoice of Goods, $\$ 100$, (S. B.--3. B.)
. Sold Mdse. per Petty Cash Book, $\$ 125$, (C. B.) ... Psid cash in full of Drayage acct., $\$ 20.75$, (C. D.)

## DOMESTIC INVOIOE BOOK.

Mary, P. Q., on (S. B.-B. B.) B.)-21. Sold B.)-23. Paid -B. B.)-25. of Goods. \$400, Face of note, ec'd per steamer 844.14; Paid of L. Power \& C. B.) ...Paid for cash, as per wson, Sorel. on - В. B.)-29. 30. Sold Mdse. d cash of W. E.
months, Invoice or Drayage and 00 (C. B.)-3. -5. Discounted Discount off, bec, on his note b. A. M. Rooney ount off, $\$ 49.60$, 50, (C. B.)-8. onths. Invoice of ter Africa, Glas1, $\$ 276.10$, (For. Book, \$218.50, -15. Sold 8. R. Goods, $\$ 908.29$, vate acct., \$140, \$362.40, (C. B.) ey \& Son. Liver h, $\$ 2 S .29$, (For. ote at 6 monthe, .Sold N. B. Roy, 3. Sold Mdse. as rran, Riohmond, . . Paid Postage, e \& Strang, To \$3303.71, (S. B. a 8 month note, old A. R. Jacob, 0 , (S. B.--B. B.) 3.) . . Psid casb

## DOMESTIC INVOICE BOOK,--SET IV.

This book contains copies of all invoices of merchandise parchased from importers and others in this country, with the eonditions of all such purchases. Each lot and package is distinguished by some peculiar mark, which is transferred to the invoice, thas serving an important purpose in checking the articles, adjusting
disputes, eto.
The purchases on time, for which notes are given, are passed to the Ledger from this book; those for cash, from the Cash
Book.

Quibec, August 1, 1871.


## DOIMESTIC INVOICE BOOK,-SET IV.

Quebec, Auaist 10, 1871.



Quibec, Septiamber 20, 1871.
DOMIESTIC INVOICE BOOK,-SET IV.

FOREIGN INVOICE BOOK,-SET IV. Quebec, A:jaust 10, 1871.


## Quebeg, August 15, 1871.



A mounts forward, Per Steamer "Nestorian," July 15, 1871.
$60 \frac{2}{4}$ Lavellas assorted, $3028^{2}$ (o) 37 d .
Makiug up. Casing. etc.
$\because$ Makine ud. Casin.. etc. 3
FOREIGN INVOICE BUOK，－SET IV． Quebec，August 25． 1871.
Camadian Curiency．

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| 48 | ¢r | $\mathrm{m}^{-1}$ | 「－ | ヶ～ | ¢－ |  |



## 8ALE BOOR.

## SALPS BOOK.

This book contains all the regular sales, either for cash or on time; the cash sales being extended in the inner column, are, of course, not included in the amount for which merchandise is oredited from the Sales Book. These sales, together with the peny sales not entered on the Sales Book, are posted from the Cash Book. The total credit of the merchandise account for the month will agree, in amount, with the monthly recapitulation in the Sales Book.

Quebec, August 1, 1871.


## SALES BOOK，－SET IV．

Quebec，August 14，167！．
or cash or on limn，are，of ndise is cred－ frith the perry om the Cash or the month n in the Sales


C．M． 389252 Prints， 9731858
E．A． 578852 ＂ 9651834
E．A． 620253 ＂ 9671895
D．C． 41875
E．N． 563049
E． $0.5685 / 49$

E．Latino

$$
\begin{array}{r}
119 \\
37
\end{array}
$$

＂
1924
＂ 9681954
＂ 971192925808 yd ．œ13 c． 755.04
Note at 6 months．
St．Mary，P．Q．

Burke \＆Son，
$\qquad$
Kamouraska．
4 Cases Bleached Shirting，
$7531745^{3}$
$75440 \quad 1741^{2} 6955 y d s$ ． $12 \frac{1}{2}$ cts． 20
Stein \＆Co．，
．
S．Mary，P．Q．

$$
\stackrel{9}{9}
$$



| 751 | 40 | 1736 |
| :--- | :--- | :--- | :--- |

869

$$
\begin{array}{rrrr}
1191 & 75 & \text { cts. } & \$ 89.44 \\
373 & 6 & 80 & 6 \\
610 & 30.20
\end{array}
$$

Note at 8 mos．from date．

Sales on time，
Sales for Cash，entered herein but posted
from C．B．
Petty sales，entered alone on C．B．，
Instal sales for the month，

## BALES BOOIK, -SET IV.

Quebec, September 1, 1871.


## SALES BOOK, - SET IV





This is the most convenient form for a Cash Book to be kept, in connection with a general merchandise business; the feature of special columns may be extended, if desirable. It will be seen that all cash entries, debit and credit, are taken to the Jedger, either through the Journal or directly, from this book, togethy with all accounts producing or costing eash. The amounts dis tinguished as "per petty Cash Book," are entered here from a

> Dr.

Cash.


## ASH BJOK,

Book to be kept ess ; the feature

It will be ween to the Ledger, is book, togetby he amounts dis ered here from a


## -SRTITV.

brok containing sales too insignitioant to be entered on the regular Sales Book. The column headed "Balances," will be found very convenient for the purposes for which it is used. The Checkmarks, in the column following dates, are made to indicate that the amounts opposite in the "Sundries" column have been jour. nalized. Were these amounts posted directly to the Ledger, the Ledger-page would be written instead of the Check-marks.

## Cash.

Cr.



The Bill Book çan never, with advantage, be made a principal book, from which to post. The form presented below is the best

## Bills

| No. | When <br> Keo'd. | Drawer or Endoreer. | Dramee or Maker. |
| :---: | :---: | :---: | :---: |
| 1 | Aug. 1 | W. H. Ellison. | J. N. Galt. |
| 2 | " | D. Atkinson. | S. I. Perron. |
| 3 | " 1 <br> 1 12 | H. M. \& Co. | L. Beaudry. |
| 4 | "12 <br> 12 | K. M. ${ }^{\text {a }}$ | ${ }_{\text {F. }}$ F. Peters \& ${ }^{\text {a }} \mathrm{Co}$. |
| 5 | " 14  <br> 1 20 | J. R. E.ast. | Hazel \& Foy. |
| 7 | " 28 | J. R. Last. | Stein \& Co. |
| 8 | Sept. 1 | H. M. «Co. | C. E. Lawson. |
| 9 | " 6 | " | A. M. Rooney \& Co. S. D. Higgins. |
| 10 | " 8 | " | J. F. Nestor. |
| 11 | " 15 | J. O. Moss. | S. R. Woods. |
| 12 | " 27 | H. M. \& Co. | Lee \& Strang. |
| 13 | " 28 | " ${ }^{\text {c }}$ | T. Rose \& Co. |
| 14 | " 30 | " | A. R. Ja job. |

Bills

| No. | When Issulud. | Drawer or Endosser. | Drawee or Maker. |
| :---: | :---: | :---: | :---: |
| 1 | Feb. 20 | G. H. Shills. |  |
| 2 | April 1 | S. A. Pugh. | IT. 3. ${ }_{\text {a }}$ |
| 3 | May 12 | A. G. Cook. | ، |
| 4 | Ang. 10 | P. McHugh \& Co. | ' |
| 6 | Sept. ${ }^{11}$ | N. Casey \& Bro. | " |

## 3ILL BOOK,

nade a principal below is the best
-SET IV.
for general purposes, although the arrangement in the former example is more comprehensive.

Receivable.

| Date. | Time. | When ${ }_{\text {Wuen }}$ | Amount. | When and How disposed of. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} \overline{1871} \\ \text { Feb. } 11 \end{gathered}$ |  | 1871 |  |  |  |  |
| April 12 | 8 mo . | Aug. 14 | 126.4 <br> 800 <br> 800 | Ang. | 14 | Paid. |
| Aug. ${ }_{12}$ | 3 mo 6 mo d |  | 699 <br> 690 <br> 06 |  | 18 | Discounted. |
| " 14 | 6 mo <br> 8 mo | ${ }^{\text {Feb. }}$ A pril 15 | 273 <br> 892 <br> 50 <br> 38 |  |  |  |
| " 20 | 6 mo . | Feb. 23 | $\begin{array}{r}369 \\ 1425 \\ \hline 88 \\ \hline 88\end{array}$ |  |  |  |
| " ${ }^{\prime 2} 2$ | 8 mo . | May 1 | 1714 |  |  | Discounted. |
| Sept ${ }^{\prime \prime}$ | 6 mo 8 mo 8 | $\mathrm{March}_{4}^{4}$ | 143289 |  | 6 | Discounted. |
| " 8 | 8 mo. | May ${ }^{\prime \prime}$ | 52700 |  |  |  |
| "15 | 8 mo. | " 18 | - 908 |  |  |  |
| 1 27 <br> 1  | 8 mo . | " 30 | 3303.71 |  |  |  |
| " 28 | 8 mo . | " 31 | 57852 |  |  |  |
| ${ }^{\prime} 30$ | 3 mo. | Jan. 2 | 10000 |  |  |  |

## Payable.



## INVENTORY BOOK.

This book is used to enumerate the different articles of unsold merchandise, at such times as may be deemed desirnble. It is, in this instance, purely an auxiliary, the amount of merchandise on hand being ineluded in the opening journal entry. Inventories are frequently copied into one of the Invoiee Books; but a separate book is preferable.

Mi'se. on hand, August 1, 1871.


## JOURNAL,-SET IV.

articles of unsold, desiruble. It is, th of merchandise try. Inventories ooks ; but a sep-
71.

| Price. | Amount. |
| :---: | :---: |
| . 11 | 61.98 |
| $.26^{3}$ | 21293 |
| . $06{ }^{1}$ | 12500 |
| 3.43 | 720.3 |
| . 25 | 34237 |
| . 60 | 34575 |
| . 522 | 246122 |
| 4.89 | 293440 |
| . 872 | 78750 |
| . 15 | 20880 |
| . 22 | 1760 |
| 1.50 | 16500 |
| . $222^{2}$ | 15463 |
| . 16 | 86400 |
| 4.50 | 67500 |
| . 90 | 13500 |
| . 17 | 328.35 |
| $.27^{2}$ | 25025 |
| $.37{ }^{2}$ | 28125 |
| 2.50 | 25000 |
| 4.46 | 62440 |
| 6.25 | 3125 |
| . $088^{2}$ | 70.46 |
| . 45 | 15188 |
| . 29 | $5 \% 00$ |
| . 14 | 3.35116 |
| . 50 | 26250 |
| . 091 | 20350 |
| $.17^{2}$ | 22164 |
| . 06 | 10351 |
| . 25 | 32500 |
| . 11 | 950.1 |
|  | $8299 / 46$ |

Quebec, August 1, 1871.


## JOURNAL,-SET IV.

Quebec. Avaust 31, 1871.


## JOURNAL,-SET IV.

Quebec, Septemben 30, 1871.



Dr.
Balanoes of their Losses


## ELL \& CO.'S

## eir Resources


their Losses

## and Gains.

BALANCE SHEET, SET IV.
and Liabilities.
Cr.


Cr.


BOOK-K EEPING

SINGIE FINTEY.

REMARKS.
Though we have introduced Double Entry Book-keepinge before Single Entry, yet, we admit that books may be kept by single entry by those unacquainted with the principles of double entry; but the mere kecping of accounts is not ali that is required. We gave the precedence to the method by double entry, as it is conceded to be greatly superior to that by single entry. In fact, the simplest settlement of Partnership accounts involves the principles of double entry; and, if the commonest English education includes a knowledge of Arithmetic, Mensuration, and even of Algebra and Geometry, iv ought surely to include a knowledge of accounts sufficient to make a partnership settlement between two mechanics.

The following set in Single Entry Book-keeping, though short, exhibits such a variety of transactions as is necessary to an illostration of it.

The principles of Single Entry are so easy of comprehension as scarcely to need explanation. Accounts are kept only for persons, who alone have accounts in a " Luedger," and become debtors and oreditors as they owe us or we owe bhem.

The principal books of entry are a "Day Book" and a "Ledger." Besides these, there are other books termed "Auxitiaries," varying, as in Double Entry, in na:aber and form according to the business.

All transactions requiring a debit or credit to any person with whom you have dealings, are entered in the Dity Book. The form of entry is very simple, thus: "Paul O'Neil Dr. To 5 yds. Linen (3) 25 cts.," or "Peter Howard Cr. By Cash on \%, $\$ 8.00$;" in every case specifying the details which constitute the debit or credit. This is the only book from which posts are made to the Ledger.

## DAY BOOK,-SINGLR ENTRY.

Remark. - The Day Book being derived from the " Auxiliary Books," might simpiy give the abridgement of the transactions. As the Cash Book is the only auxiliary one we open in this short single entry set, we write in the Day Book the details, that would otherwise be shown in the omitted auxiliaries.

Quebeo, July 5, 1871.
k-keeping before 3 kept by single f double entry; ; required. We try, as it is cony. In fact, the es the principles h education incven of Algebra dge of aceonints two mechanics. :, though short, sary to an illas-
mprehension as nly for persons, me debtors and

Book" and a ermed " Auxildd form accord-
ny person with rok. The form o 5 yds . Linen , $\$ 8.00$;" in the debit or re made to the


Qurbeo, Jtul 22, 1871.


## CASE BOOK,-SINGLE DNTRY.






## STATEMENT

## BHOWING THE OONDITION OF THE BUSINMES

On the 31st of July.


1. From Lodecr Accounto.-Balance due by
A. T. Hughes
2. From Coosk Book.-Balanoe of Cash on hand
B. From Bill Book.
S. J. Pieroe's Note, due September 1st 4. T. Hughes' Draft, due August 8
3. From Inventory. - Merchandise on hand.
$\qquad$ Liabilitice. $\qquad$
4. From Ledger Acciunte.-Balances duw to
C. I. Lane
J. N. Kirouac
J. Gleaso
5. From Bill Book.

Note favor R. J. Vincent, iue Aug. 12
" " S. Fraser \& Co., "Sept. 13
"" ". C. I. Lane " Aug. 15
" "S. Fraser \& Co., "Sept. 1st
Present worth or net capital
Yy capital at commencing business was
Net gain realized July 31at

## CHANGING SINGLA, TO DOUBLE ENTRY.

> Let the Books of the preceding Set in Single Entry, be changed to Doulle Entry.

## Preparatory Statement.



| Dr. | D. R. Marshall. |  |  |  |  | Cr. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | $\left\|\begin{array}{cc\|c}1871 \\ \text { July } & 1 \\ \text { " } \\ \\ 31\end{array}\right\|$ | (e) $\begin{aligned} & \text { By Capital } \\ & \text { c/ } \\ & \text { Net gain }\end{aligned}$ | $\sqrt{* 300000}$ |
| Dr. |  |  | Cash. |  |  | $C r$. |
| 1871   <br> July 31 $O_{n}$ hand |  |  | $\\|$ \$2995 $3^{3} \\| \mid$ |  |  |  |
| $\stackrel{D r}{ }$ |  |  | Bills Receivable. |  |  | $C r$. |
| $\stackrel{\rightharpoonup}{\infty} \underset{\substack{\text { Jaly } \\ \hline 1871 \\ \hline}}{ }$ | Notes on hand |  | - $\$ 205100$ | $\\|$ |  |  |
| Dr. |  | Merchandise. |  |  |  | Cr. |
| ${ }^{181811}\|31\|$ On hand $^{2}$ |  | \$ $81188{ }^{\text {93 }}$ |  | 1 |  |  |
| Dr. |  | Bills Payable. |  |  |  | Cr. |
|  |  |  |  | $\left\|\begin{array}{l}\text { 1571 } \\ \text { Jnly }\end{array}\right\|$ | Notes oultanding | \$ 81508 |

## PRACTICAL EXERCISTS

## MFMORANDUM I.

## Angust 1st, $1871, I, B$. N. Lindsay, commence businers wiwh

 a caprial, in Cash, of $\$ 500$ - - Paid in Catsh for Painte, Oils, Cilass, Brushes, etc., sí 05.32-Lettering Tin Sign for II. Young, \$1.75, and Gold hut I Light Stained Glask, s.5.-2. Paid in cash for 2 liooks Morin for Glazing 27 Lights 10 by 19 © Cu, $\$ 2 .-85$. Received of T. Bronzing of a Valve for L. S. Rogers, at 25 cents, in cash $\$ 6.75$.Blue Paint at 25 cents, $\$ 1.50 ; 18$ ins, 50 cents, and sold him 6 lhs. Paid in cash as follows : to W. White Paint at $12 \frac{1}{2}$ cents. -4 . Teakle, 2 days' Work at 75 cts . Rovid, 3 days' Work at $\$ 1.50$; to $\mathbf{H}$. me, viz. : for Lettering Sign 60 feet, at 20 trank R. R. Co. owes Border of Sign, 82 ; for Putting up Sign, \$5 cts. per foot ; for Gilding 4 days' Labor, at \$1.50. Paid Grand Trunk R. R. Co. owes me him on \%, in Cash s3.-6. The at 20 cents; for making Board an follows: for luttering Sign 15 ff . O'l'arrell for making Sign for and pitting up, \$4.25.-1 owe J. liec'd of John Ray for paiuting the Grani Trunk R. R. Co., s3.--7. Rec'd of H. Young in fill of as per agreement, in cash, $\$ 30$. Feigh \& Co., Paints, Oils, etc., of in cash, 86.75.-8. Bo't of 1 . Pail them in part in Cash, $\$ 25,-\mathrm{B}, \mathrm{t}$ Bill, amonating to $\$ 52.64$. Putty, amounting to $\$ 17.50$; Paints and ${ }^{\circ}$ W. G. McLean, Glass and Glazing of 1 light 11 by 18, 37 cts and Oils, amtg. to $\$ 122.50 .-$. Feigh \& Co. as follows: in cash cts., for L. S. Rogers.-11. Pail A. Lights 10 by 18, at 25 cts. -I owe Geo $\mathcal{V}$ Heconut, 811 ; and Glazing of 10 Sl.io. Paid him on 0 in owe Geo. N. Harper $5 \frac{1}{2}$ days' lalwor at days' Work at 75 cts.-18. The City Hall owes Teakle, in carh, 51 4 Lights 10 by 16 , at 25 cts. , $\$ 1$; for pain owes me, viz. : for Glazing per agreement, $\$ 15 .-15$. Gave A. Feigh \& 3 Rooms, 2 Coats, as Grand Trunk R. R. Co., for \$15.14.-17. Re, Co. an order on the Paint at 25 cts.-18. I owe Geo. N. Harper ${ }^{\text {. }}$. ${ }^{\text {d cash for } 37 \text { lbs. Ihue }}$ Paid him cash in full of a/e, $\$ 7.50$ Harper 31 days Labor at $\$ 1.50$. 20, Stained Glass, at \$4.50.-Paid.-Rec'd cash for 2 Lights 10 by at \$1.—R0. Rec'd cash or 'T. Bro. Teakle, in cash, 6 days' W ork cts. - Paid cash for Repairs of Shrown for 120 lbs . White Paint at 11 Frame, \$4.38.-22. Sold Horhop, \$2.12; for making Transparency, ency, Hame, \&c. for \$40.-\$4. R Galt Stained Glass for Tran-par. Glover, for Stained Glass, as Received cash as follows: of $F \cdot J$. painting Church, $\$ 210$. -25 . Her agreement, $\$ 25$; of C. Harris lir New Sash at Mimufactory, as per Young owes me, viz. : for Clazing 15, at 9 cts. ; $13 y$ Lights 10 by per agreement, to wit, 56 Lights 1 , by 3 cts. : for 20 Lighte, Old Glezing at 7 cts.; 1920 Lights 8 by 11), at 110 Window Frames, at 45 cts. ; forg 11 by 17 , at 35 ctso ; tor Panting -Paid cash as follows : to L. ; for Painting Reception Room, \$5.2i. Walter, $5 \frac{1}{2}$ days' Work, at $\$ 1.50$. Jones 6 days' Work, at $\$ 1.51$ : ti H. to P. Landry, 41 days' Work, at 75 . Teakle, 5 days' Work, at 81 : viz. : 1 Black Cloth Dreas Coat, 816 ; 1 pair. ${ }^{2}$. Bo't of L. S. lingers, *6.-Paid P. Gardner, Carpenter: for Pair Black Cassimere Pants,

## PRAOTICAL fexeroises in single entry.

onah \$22.50.-28. Paid cash for 10 zals. Linseel Oil, at \$1.624.29. Reo'd caeh for Tin Sign, \$10. Paid caah for Thin und Japanning, 84.25.-30. Harly \& 'G:ly owe tue for Painting cifice, as per agree ment, \$30.-Paid H. Tcakie, in cash, 6 days' Work, at \$1.-81. Paid for Rent of Shop one wemth, in cash, \$16.67.

Balances of the Resources and Liabilities.

| Resources. |  | Liabilities. |  |
| :---: | :---: | :---: | :---: |
| Caeh, balance on hand | \$540 08 | L. S. Rogers | 16 |
| Stock of tools, as per In. |  | J. O'Farrell | 300 |
| ventory-Book |  | W. G. MoLean | 14000 |
| Stook of paints, etc. |  |  |  |
| B. Young | 134124 |  | 15938 |
|  | 200 | Balance.-My net capital | 75193 |
| Grand Trunk R. R. Co. City Hall | 861 |  |  |
| Hardy \& Galt |  |  |  |
|  | 911 31 |  | 91131 |

Thus:
> "y net capital, on Sept. 1st, is
> $\$ 751.93$ at commencing husiness was only
> 575.00

My gains in buciness have been $\$ 176.93$

## MEMORANDUM II.

Sept. 1. 1871. I commence business with the following ro souroen: Cart, $\$ 801.34$; Merchandise, $\$ 5120$; Bille Receivable, $\$ 1385.60$; L. S. Burroughs owes me, on \%, $\$ 167.04 ;$ L. N. Volidon, $\$ 120.98$; T. A. Maguire, $\$ 96.40$; C. N. David, $\$ 50.64 .-$ I owe as follows: On Notes, $\$ 350$; to Poston \& Co., on \% , \$51.1? : 10 Garneau \& Roy, $\$ 180.88$. - Paid L. Davis, for repairs on the El , (4, \$3.74. -Sold C. N. David, on credit, 2 tbls. Flour, at \$5.25.-2. Sold L. N. Veldon, on $\%, 24$ gals. of Sperm Oil, at $\$ 1.50$; and 50 lbs . Pow. dered Sugar, at 10 cts. per pound. - 3. Bo't or Poston \& Co., on $\%$, 8 boxes Havana Sugar, 3284 lbs , net weight, at 7 h ots.-Paid in casil, fin a Set of Account Booka, \$20.50.-4. T. A. Maguire has paid me \& : 63 his nld account.-Sold D. S. Raymond, on account, 60 lbs. Cry it itugaz, at 10 eta.; and 100 lbs. Brown Havana Sugar, at $8 \frac{1}{8}$
 Had to 300 in cash -8. Bo't of W. C. Lord, for cash, Merchan-
 -6. C. A. David b-a tran painting in the atore dinve at $\$ 1.26$, for
which I am to give him credit. And I rell himn 2 lbs. Coffee at 2 s cts.; and 8 lha. Crushed Sugar, nt 12t cts.--9. Sold E. S. Rurpouphes, on account, 's bhls, of Flour at \&i, and 2 bhls. of Now Orleans Hu nar,
 Sold L. N. Veldon 2 bbls. of Fluur provions, for mp honse, 814.1f. Tea, at 45 cts . Bo't of him, 4 conr at $\$ 8_{7}^{7}$, und 4 Hm . of Ning Yung sis.-11. The amount of cash recils of Mapl. Womil for the Store, in -Soll 'T. A. Maguire 2 tulis of Butter. Sales to this dime is " 649.50.
 Burrongha has given me his vote foreee, at 13 cts- -18 . E. S. part payment of his accommt. - Pate for s.200. pryable in 3. lays, ia per bill, s53.-Sold I). S. Raymond 2 for Desk, Chaire, Stove, etc. 20 gallons of Sperm Oil, at $\$ 1.50$. He lis of Flour, at :87.25, and "bakey" for the past 6 months, amount has presented him bill for the balance of his account, $\$ 25.70$, in unting to $\$ 3.3 .05$, and hus paid on \%, in cash, :200.-Rec'd of S. in eash.-14. Paid Puaton \& Ca principal s700, with interest for three month the amount of his Not : Colton \& Son a bill of Mdse. amonnting ions, 810.50 .-Bought of $\mathrm{P}_{\mathrm{m}}$ my Note, at 2 monthe from date. - 15 io an Orider on Walter \& Letvia for Mde., to the Veldon hay piven me they have delivered me the roolo.- id. Sold amonnt of sol ; and Flour, at 57.50 ; 2 cwt. of Fish, at -16. Sold J. Grant 2 bitrrela of cts., and 2 lbs of Black Tea. at 45 cts. 25 ; 20 gals. Molaseses, at 35 in cawh, $\$ 20 .-17$. W. MeKay brougit Rec'd of C. N. Diavid on \%, roughs, requesting me to sell brought an Order from E. S. Hurand to charge the same to his (hurroughs) to the amb. of $\$ 36.92$, livered the goods. - Paid miy Note No. I account; and I have demonths and 15 days, $\$ 11.38$. - Sold No. 1 , for $\$ 350$, with interest, 6 112 Jbs . net, at 214 cts . -18 . Bo't M. S. Raymond 2 tubs of Butter, amounting to \$334.38. - Rec'd of 'T Mdse, of Poston \& Co., on acct., -Paid cash for 2 Corls of Mapie A. Maguire, on \%, in cash, 534. Cash Saley this week amount to S11. Wood, for the Store, \$13. -The bbls. of N. O. Sugar, 416 lbs , net, at 5 - 20 . Sold L. N. Vellon 2 taking his Note at 60 dave, for at 5 dets. -Lent L. Shea $\$ 1000$, $\$ 14.50$ on $\%$, in cash.-22. Delivered.-\$1. Rec'd of C. N. David guire's Order, goods amonnting to $\$ 21$ S. A. Buyd, on T. A. Mapaid me $\$ 50$, in cash, on $\%$.-\$4. J. Grant. E. S. Burronghs has Apples, at $82.12 \frac{1}{3}$, and paid the balance Grant has sold me 12 bbls. o? -Paid Garneau \& Roy $\$ 100$, on \%.- $\%$ his acct. in Cash, 85.90. for myself, $\$ 47.90$.-Sold L. N. Vellon 2 bis. Paid a bill for Clothing, ${ }^{60}$ gals., at 28 cts., and took his Note, on 1 , of Molasses, containing his account, $\$ 77.46$. -The Rutter wote, on demand, for the balance of the IIth inst., not proving as good which I sold to T. A. Maguire on him a deduction of 33 . - 3 as good as I thonght it was, I have male W-day, amounting to $\$ 685.60$. C. F. Joly's Note, No. 2, was paid in Note, dated ! 3th inzt. for 0200 -Gave Poston \& Co. E. S. Burrougha' this date, for 880 . - The Cash ; and also my Note, at 60 daye from -28. T. A. Naguire has passed a hast week amounted to $\$ 530.32$. viously received of U'. Ryan, for a Nute to me, which he hall preNote, on demand, for the balance -29. Gave Garneau \& Huy my

Pooton \& Co. $\$ 100$ on account, in cash. - Paid my Clerk's salary fór the inonth, in cash, 860 .-Cash Sales for the week, $\$ 338.96$.-Having taken an Inventory of the goods in the store. I find the amomet to be \$5086.41. I have Notes against various persons, amtg. to \$1127.46. I owe Notes amounting to $\$ 14.36$.

On September 30th, my Net Capital is $\$ 7528.73$, and my Net Gain, \$158.73.

## MEMORANDUM III.

October 1, 1871, W. S. Drum, Cabinet-Naker, associates with himself'T. A. Graham ;-Drum transferring to the firm such porlion of his resources and liabilities as is mutually agreed upon, and Gra ham investing their equivalent in cash. The parties are to share alike in gains and losses.
W. S. Druin invests in the business, as follows: Cash, 100 ; Sun dry Notes which he holds against others, per B. B., $\$ 700$; E. Miles ${ }^{\text { }}$ balance of account, his favor, 8111.50 ; J. R. Nesbitt's balance of accomnt, his favor, $\$ 74.80$; Materials and Unfinished Work, as per Inventory, $\$ 71: 3$ Stock of Furniture, as per Inventory, $\$ 420.86$; Stock of Tools, as per Inventory, $\$ 302.40$. W. S. Drum owes; viz., Sundry Notes, as per B.-B., amter. to $\$ 842$; I. McIntyre \& Co., bal. of acel., $\$ 134$; N. Percy \& Som, hal. of acct., \$150.40. T. A. Gra ham, invests in the business, in cash, \$1296.16.-2. Bo't tor cash of C. Vallee, Planks, as per Bill, $\$ 151.20$ - - \$B. Sold E. Ililes 2 Hair Cloth Malogany Sofas, at \$20. Rec'd from the same on account, in cash, $\$ 120 .-4$. Sold Mrs. C. Nelson, on acet. ; viz., 18 Mahogany Chairs, Cithe Seats, at $\$ 1.25$; 12 Mahogany Chairs, Hair-Cloth Seats, at $\$ 3$; 4 Cleery Dining.Tables, at $\$ 6$; 2 Maple French Berlsteads, at $\$ 4.25$; 2 Maple Low-Post Bedsteads, at \$2.75.-5. Sold P. AlcGee on acct., per wile, 2 doz. Windsor Chairs, at $\$ 12$; 1 doz. Windsor Chairs, for $\$ 15 ; 1$ loz. Windsor Chairs, for $\$ 10 ; 2$ Spring.Seat Black Walnut Sofas, at $\$ 21 .-6$. Paid for Wages, per Tme-Book, in cash, Sli.8. Suld for cash, 2 Bureanx, Mahogany Veneered, at $\$ 22$. Pail as follows: A. Patry, for repairs ot Shop, in cash, 8103 ; S. Jones, for Painting Shop, in cash, \$44; L. NeĨntyre \& Co., in full of aect., in cash, $\$ 134$; for Glazing 2 Lights of Glass, cash, 76 cts.- 9 . Rec'd cash for B. Motley's Note, Drun's favor, $\$ 250 .-$ Bo't of N. Percy \& Son, Lumber, for $\$ 270$. Gave in payment our Note at 30 days, in full of all acct.-Sold E. Miles, per daughter, on acct., 2 Black Walnut Footstools, at \$1.50.-Sold C. T. Renaud, on acct., f Patent Pivot Chairs for Office, at \$5.-11. Sold for cash, 2 Arm-Chairs for Otfice, \$10.-Sold E. Miles, per wife, on acct., 2 Black Walnut Extension Dining.Tables, at $\$ 40$ - -18 . Sold P. D. Flood, on acct., 4 Children's High Dining-Chairs, Mahogany, at \$2.-Sold Miss Anna Roy, on acct.; viz., 6 doz. Windsor Chairs, at $\$ 11$; 2 Rocking Chairs, Sec-ond-Hand, at \$9.—Paid cash for Wayes, \$75.-7E. Suld for cash Pints of Varnish, \$1.-E. Miles assumes P. McGee's account, trans ferred to him, for \$91.- \$ Bonght of L. McIntyre \& Co., Painte, Varnish, Brushes, etc., as per Bill, antg. to $\$ 350.52$. Pail to them cash, in part, $\$ 100 .-17$. Received fir Staining Cupboard, in cash,

## HIATS AS TO RESOUIOOES AND LIABILITIES.

\$1-50.-18. Sold P. D. Flood, on acct., ? Black Walnut Book-Cases, at $\$ 15$. -Sold for ca-h, 2 Reclining Chairs, at $\$ 25 .-19$. Sold for raslı 2 Ottomans, at \$7.-Sold E. Niles, per sen, on account, 2 Hat. $\therefore$ Sids, Mahogany Veneered, at slo.-20. P. D. Flood owes us for V'arnishing 1 Table, s1.-Sold for Cash 1 French Bedstead, Birds'. Eye Maple, \$9.-Paid cash for Wages, per Time-Book, \$76.24.-22. Sohl fur Steamboat Aurora; viz., 6 Mahogany Sofas, at $\$ 15$; 4 Tete a-Tetes, at $\$ 16 ; 2$ Rocking Chairs, at $\$ 12 ; 8$ Arm Chairs, at $\$ 8 ; 4$ dez. Chatis, at s30; 28 Cherry Wash-Stands, at $\$ 2 ; 28$ Looking. Glasses, at \$2. Rec'd cash in part payment, $\$ 300$. - Paid cash for Urum's Note, F. Walter's favor. Face of the Note, $\$ 400.6$. Discount from date, to Dec. 6th, amounts to $\$ 3 .-2: 3$. Pail W. S. Drum on acct., in cash, $\$ 20 .-B o ' t$ of J. King, ou account, I mmber, per Bill, 192.80-24. Paid cash as follows: Bill of Varnish, $\$ 27$; Gas Bill, \$28.50; Drayage of Furniture, \$1.-26. Solld E. Miles, per wife, on Wect., 2 Mahogany Bureaux, with Glass, at $\$ 25 .-27$. Paid cash for Wages, as per Time-Book, \$73.30-29. Sold lor cash; viz., 4 Ma hogany lhucking Chairs, Plush covered, at $\$ 12.50$; 2 Birds'.Eye Maple French Bedsteads, at $\$ 9$; 2 小oz. Cane-Seat Walnut Chairs, at $\$ 24$; 2 duz. Child's Hiph Chairs, al $\$ 1.25: 2$ doz. Child's Rocking Chairs, at $\$ 1.25$. -Paid cash as follows : for Bill of Veneering, $\$ 51.20$; to T. A. Graham, on acct., $\$ 50$; for Repairs of Lock, 50 cto.-Sold to Misa Anna Roy, on acct., 1 Mahogany Bureau, \$38.-iso. Sold Anas Roy has returued Black Walnut Centre Tables, at \$15. Mise instant, because it was too large for the room, auld her on tho $2 y$ th E. Milas as follows: his Note at 60 days for S ant. $\$ 33$. - Rec'd of acot., $\$ 125.50 .-31$. Hec'd cash for Repairin. -Paid wah for Rent of Shop, ©30; for Wagin Tableaand Chairs, \$3. $\$ 78.50$.

The Stock of furniture on hand am'ts, per Inv. Book., to $\$ 155: 3.50$
" " Materials and unfinished work, "
" $\begin{array}{lllll}\text { "tools, depreciated ly use } & \text { " } & \text { " } & 479.58 \\ \text { The amount of Bills Rec. in possession of the tiris. per } & & 283.90\end{array}$ " " "Bills Payable outstanding, ris, per 13. B. $\begin{aligned} & 600.00 \\ & 862.40\end{aligned}$

The Firm's net capital is $\$ 30 \mathrm{S3} .52$, and its net gidia, $\$ 561.20$ of which $\frac{1}{2}, \$ 28060$ for each partner.

## HINTS AS TO RESOURCES AND LIABILITIES.

The terms resources and liabilities are used extensively in this trea. tise, and their importance in properly defiuing the condition of the business has been forcibly set before the student. He has heen taught that certain Ledger Aocounts are nsed to show resources, and certain others to show liabilities, and that the correspondence between the

## GINTS AS TO REBOUROES AND LIABILITIB.

resources and liabilities this shown must agree in a certain sense, with the accounts showing gains and losses. Any careful observer, however, must be aware that all classes of resources are not equally valuable; and that, ' in the course of trade, persons may become indebted to us both on note and account who will never pay; the resource thus represented being absolutely valueless. In estimating the condition of a concern, therefore, it is well to know whether the books are truthful; that is whether the rocources exhibited on their pages are aisolute or fictitious. The liabilities are always presumed to be genuine.) The importance of this precaution will be apparent when we consider that all gains in business, as shown by representative accounts, are predicated upon the integrity of the resources. For instance, suppose we sell A, $\$ 300$ worth of Merchandise, and take his note for it. In recording the transaction, we credit Merchandise, and debit Bills Receivable. In estimating our gains and losses, we, of course include among the proceeds of Merchandise this amount, which adds $\$ 300$ to our gains. Our Merchandise acoount is closed, and the result finds its way into the T دoss and Gain account, thus having an impor. tant bearing upon the apparent prosperity of the business. But suppose this note should prove vorthless. It is now evident that the $\$ 300$ credited to Merohandise account was not a legitimate product, and that all gains predicated upon it are necessarily fictitious. But there are other resources represented in the Ledger, the exact value of which is uncertain,-they may be worth their face, or half of it, or nothing. How shall they be treated in a general exposition of affairs? Shouli, we consider them all valueless, and close them into Loss and Gain. the error may be as great as to permit them to remain and represent actual worth. The most approved method of disposing of this class of accounts, is to permit them to remain upon the Ledger, but to neutralize their effect by opening an aooount showing fictitious liabilities of the same account. An appropriate title for this account is "Suspense." When therefore doubtful resources exist on our Ledger, and we do not wish to represent anything more than actual gaino, the process should be to debit Loss and Gain, and credit "Suspense" with the amount of the doubtful resources. If any of these are after. wards paid, or their value becomes tangible, it is very easy to restore them by debiting Suspense and crediting Iross and Gain. This method is far preferable to the more usual one of closing up all doubtful account into Suspense. The Suspense accøunt in the latter case would represent either a loss or a resource. If a loss the amount may as well go at once so the Loss and Gain account; and if a resource, it had much better remain under its own more appropriate title. But the chief objection to this course would be the exhibitng of accounts as closed, which are yet owing and may be paid. If Mr. A, for instance, whom we thus consider doubtful, should desire to see hie account in our Ledger, that he may pay it, it might be awkward to inform him that, having considered his account worthless we had carried it into Loss and Gain. He might not desire to obange oup estimate of the value of his indehtedues.

ITISA.
a certain sense, careful observer 3 are not equally may become iner pay; the re. [n estimating the hether the booke ed on their pages 3 presumed to be 9 apparent when epresentative aces. For instance, take his note for undise, and debit es, we, of course unt, which adds d , and the result aving an inpor. iness. But supent that the $\$ 300$ ate product, and ious. Bat there at value of which of it, or nothing. affairs? Should Loss and Gain in and represent sing of this class iger, but to neutitious liabilities ccount is "Sus. our Ledger, and tual gains, the lit "Suspense" $f$ these are after. $y$ easy to restore n. This method all doubtful ac. atter case would amount may as if a resource, it riate title. But itng of accounte If Mr. A, for inre to see hie sobe awkward to rthless we had to change our



[^0]:    1. What is Arithmetic 9-2. What is a number? - 3. Definc unit? tade or quantity i- 5. Fraction ?- 6. How are numbers dunit 1- 4. Magniwe abstract nambers ?-8. What are comoreto numbers ? divided 1-7. What
[^1]:    9. What is a simple number 9 - 10. What is a compound number 9-11. What io e powar ?-12. What is e foct - 13. What it à demonstration $\ddagger$ - 14. Whas is an operation: - 15. What io a problon Y-16. 4 rule? - 17. What io Analycis? -18.
[^2]:    80. What is notation 1-21. What in numeration :- 22. How many meethode of sodation are now in comsmon wee $9-23$. Why is the Romam notation on exllod
[^3]:    24. Eow many ahnractere are enpologed in the Arabic Notation:-25. What are the firat nine choraters callad P- 26. How ean we repreent m!! yoseible nuw how with the tom forworl f-27. How many valwo have figures?
[^4]:    

[^5]:    33. Haplain ty an seoferto ill formation of decincal parto $1-$ of decimale alieved hy Hlysividy fiphars at their righs hand oidis?
[^6]:     groator i- 36. Do. 1 whole number wich a docimal annesedi
    (1) This moang that the number obtained, equals ten, a hundred traes, sen, the first; otherwise this reasoning would Lead us to condude that the unit in tell times groator thea the mit, whigh would to aberen.

[^7]:    

[^8]:    38. What is addition 7-39. What in moant by numbere of the oame bind f-4 Brow in addition to be oommencod 8-41. What io the growal rule for alidition if
[^9]:    42. How dr ioal proof?
[^10]:    12. Row do you add docimale t-43. What do you undercand by an arithmosloal prool8- 4. Bow is the proof of an addition yom underctand by an arithmet-
[^11]:    45. What is subtraetion?- Define minuend,-subtrahend.- 48. How iv the
    sulf called?
[^12]:    

    - 61. What are the maltiplioend ayd manimpon callat?

[^13]:    52. Whet ie the general rale for mulliplination 1-63. How is the proof of mel(1). In multiplying the multiplier by the meliplicased, the same produot mand
[^14]:    6. What in a composity namber ? 37 . What are the factors of any nember 9
[^15]:    
    

[^16]:    67. What is the rule for the divivion of dealmelef
[^17]:    C. 'What ie the rule for finding the true romalader?

[^18]:    70. What in the rule to divide by 10,100 , de. 8 - 71. What in thic rale for di--iding when there are oiphers on dhe righinhand of the divioor.
[^19]:    12. What is the rule to dinich a

    Perineal by 10, 100, 1000, eve ?

[^20]:    80. Whut is roduction ?- What is the rule for ehanging dollare to arn:e and mills i- Uente to nillo f-81. What in the rule for anatging cente to dollara fMfille to dollare i- Mille to osmet
[^21]:    88. What is an exact divisor i-89. What are all numbers? -90. Whit is an oven number ?-91. An odd number 9-12. A prime namber? - When ure numbers prime to enoh other 9-91. What is composito number 9-94. What are prime faotore 1-96. What is the power of a mumber f-96. What is am oxpe-
[^22]:    98. What is the rule to resolve a number into is arine fact the rute to find ihe prime factors common to two or wore fumberr:
[^23]:    123. Whes se a matiple \%-114. A ovavace multipiof
[^24]:    aer, 5 , in a line underneath as as before. Wo continue to divide by univided numhath divisor and remainders giver are all prime to enein other; the prime numWo again dim? hey 2 , und wrile the quotients, and the undivided num-

[^25]:    121. Wh The numer fraotion ? 131. $A$ cons tre?
[^26]:    121. What ase whe betpt dy d fraction?-122. Define the denominator?-123. The numerator" - 146. Hifye are finctione classified ? - 128. What is a simple fraotion ?-129. What it? te profer fraction?-1:0. An improper Iraction ?131. A compound friettent-132 A complex fraotion? 133 . $A$ mixed sum-
[^27]:    136. What is reduotion of a fraetion?-137. What is the sule for reducing a whole number to an oqwiealent improper fraction ?-138. Fer raducing number to an equivalent imgroger fraction?
[^28]:    119. What is the rule for reducing a compownd fradion to a vimple ona.163. Whut is the rule for jinding a cominom denominater $f$
[^29]:    167. What io the grentent common divisor of fresecioms!
[^30]:    169. What is the rule for finding the gre,test common divioor of fractionel170. What in the least common multiple of fraetione 1-172. What is the rute for findingt the heant emmon multiple of fractions?
[^31]:    173. What ie an aliquot part of a ntumber :-175. What io the rule for finding the ocat of any nomber or quantity, ohen the prive of a wnit is an aliguot part of
    a dodiar
[^32]:    177. What is the rule for finding the cost of articles, the price and the quandity baing given ?- 179. For finding the price of urticlet, the coat and the quantity being given ?-181. Por finding the quantity, the price and the coat boing given f103. For finding the een of ertioles, the quandity, or the priet of 100 er IU\$0, being given t
[^33]:    186. What it a simple number $9-187$. 4 oomponnd number $\%-$ :88. 4 donominate number \%-189. A donominate frootion ? -190 . What :88. A denumbers exprese? $?$
[^34]:    1. Principal unit of lengths.
    2. The base of the metric system, and near! one ten-millionth part of a quadrant of the earth's meridian.
    3. Equivalent, 39.3708 inches.
    
    ( 1. Twree orders of emall unite, or submultiples of each kind, are formed by dividing each of the principal units into tenthe, hundredths, and thonsandths.
    4. Four orders of larger units, or multiples of each kind, are formed by considering as a mait ten timen, one hundred times, one thousand times, and ten thousand times, each of the principal units.
     pal unit trom which they are derived, which
    indicates their relation to the principal unit.
    Millesimus, one thousandth, contracted
    Milli. Example, Millilitre $=$ Iobo of a litre,
    8 millilitres $=$ so so of a litre.
    5. Decimus, tenth, oontracted deci. EXx., Decimetre $=\frac{1}{10}$ metre; 3 decimetres $=\frac{3}{10}$ metre.
    6. Deca, ten. Example, Decametre, $=10$ metres; 5 decametres $=50$ metres.
    7. Hecaton, one hundred, contracted hecto. Ex., Hectolitre $=100$ litres; 7 bectolitres $=700$ litres.
    8. Kilioi, one thousand, contracted kilo. Ex Kilogramme $=1000$ grammes.
    9. Myria, ten thousand Ex., Myriastere $=$ 10,000 steres; 3 myr asteres $=30,000$ steres.
    10. The $a$ in deca and myria, and the $o$ in hecto and kilo, are dropped when prefixed to are.


    The tables being constructed upon a decimal scale, ten units of a lower order make one of the next higher, thus: 10 millimetres $=1$ centimetre; 10 centimetres $=1$ decimetre; 10 decimetres $=1$ metre; 10 metres $=1$ decametre, \&c.

    The facts in the preceding views being mastered, the tables can be constructed by the pupil at sight. For example: The names of the derivative units are formed by attaching the seven prefixes,
    in their order, to the principal units of the tablen. The order of pragression being ten, the table of capacitics will be written thus:10 Millilitres $=1$ Centilitro. 10 Litres $=1$ Decalitre. 10 Centilitres $=1$ Decilitre $\quad 10$ Decalitres $=1 \mathrm{H}$ ctolitre. 10 Decilitres =1 Litre. $\quad 10$ Hectolitres $=1$ Kilolitre. 10 Kilolitres = : Myrialitre

    All the tables peculiar to the Metrie System are presented together in a convenient form in the two following tables:-

    TABLE OF SUBMULTIPLES AND PRINCIPAL UNITS.

    | Nakes of Units. |  | Pronowoiltion. | Simbols. |
    | :---: | :---: | :---: | :---: |
    | PREPIX. | mask. |  |  |
    | 10 Milli Equal 1 Centi- | ¢ Metre | Mill'e.mee'ter | ${ }^{\text {M }}$ |
    |  | Are | Mill'-e-are | 4 |
    |  | Stere | Mill'e-ster | ${ }_{3}$ |
    |  | Litre | Mill'-eli'-ter | ${ }_{8} \mathrm{~L}$ |
    |  | Gramme | Mill'-egram | ${ }_{3}{ }^{\text {i }}$ |
    | 10 Centi. <br> Equal <br> 1 Deei- | Metre | Sent'e-mee'ter | ${ }_{2}{ }^{M}$ |
    |  | Ase | Sent'eere | ${ }^{\text {A }}$ |
    |  | Stere | Sent'-e-ster | ${ }_{2}$ |
    |  | Litre | Sent'e-li'ter | ${ }_{2} \mathrm{~L}$ |
    |  | Gramme | Sent'-egram | ${ }_{2} \mathrm{G}$ |
    | 10 Deci. Equal <br> 1 Principal Unit. | ( Metre | Des'e.mee'ter | ${ }_{2} \mathrm{M}$ |
    |  | Are | Des'-e-âre | ${ }_{2}{ }^{1}$ |
    |  | \{ Stere | Des'e-estêr | ${ }_{1} 8$ |
    |  | Litre | Des'-e-li'ter | ${ }_{1} \mathrm{~L}$ |
    |  | Gramme | Des'-e.gram | ${ }_{1} \mathrm{G}$ |
    | 10 Principal Units Equal <br> 1 Decar | Metre | Mee'ter | M |
    |  | Are | Are | $\Delta$ |
    |  | \{ Stere | Stêr | 8 |
    |  | Litre | Li'ter | $L$ |
    |  | Gramme | Gram | G |

    To se
    adoptio sary tha pronoun different they sho

    The 1 universa

    THE METRIO ETRTEM.
    TABLE OF MULTIPLES.
    

    ## ABBREVIATED NOMENCLATURE.

    To seeure the fullest advantage to business men by the universal adoption of the new system of weights and measures, it is neces sary that the names used should be short and easy to write and pronounce, that they should express clearly the relation of the different denominations of the same table to each other, and that they should be identical in all languages.
    The last two of these requirements would be secured by the universal use of the nomenclature adopted by the French. It is
    oosmopolitan in its oharacter: it belongs to their language no more than to any other. The former, however, is not scoured, It is evident to ill, that. for business purposes, the long names of the metric system are inconvenient, and that to shorten them would prove a great advantage. Fifforts have been made to introw duce short names; but these efforts have invariably sacrificed their universal and expressive character, which is of more importanee to the business world than their shortness.

    The only true course which seems to be open, is to abbrevite* the names already introduced, in such a way as to retain their peculiar characteristics.
    To secure this, the following plan of abbreviation is suggested:-
    First. Let the prefizes be abbreviated thus: Myr, kil, heet, dec, des, cent, mil.
    Second. Let the initial letter of the names of the five principal units be used, instead of the names themselves, thus: For metre, use a capital M ; for are, use a capital A ; for stere, a capital 8; for litre, a oapital L ; and, for gramme, a capital $G$.

    Third. For the names of multiples and sub-multiples, attach to these initial capital letters the abbreviated prefixes, thus: Kil M, pronounced kill-em' ; Kil S, pronounced kill-ess', \&e.

    By this method of abbreviation, the elements of the original terms are ret:ined in such a form that each part is clearly indi. cated. The capital letter used after the prefix will always point to the base-word of which it is the initial, although the pronur ciation is changed.

    ## TABLES WITH abBreviated nomenclatuble

    MEASURES OF LENGTES.

    Writton.

    | 10 Mil M, | Mill-em', | make | 1 Cent M |
    | :---: | :---: | :---: | :---: |
    | 10 Cent M, | Centrem', | " | 1 Des M. |
    | $\begin{aligned} & 10 \mathrm{De} \\ & 10 \mathrm{M}, \end{aligned}$ | Des-emi', | " | 1 M . |
    | 10 Dec M, | Dekem | " | 1 Dec M. |
    | 10 Heet M, | Hect-em, | " | 1 Kil M. |
    | 10 Kil M , | Kill-em, | " | ${ }_{1} \mathrm{Mgra}$. |

    guage no
    sceured, names of ten them 3 to intro Geed their aportance bbreviat tain their
    gested:- kil, heet, prineípal or metre, pital 8 ; 3, attech 1us: Kil origina! rly indiys point pronan.

    MEARURES OF SURFACES.

    Written.
    

    Pronounced.

    | Mill-a', | make | 1 Cent A |
    | :---: | :---: | :---: |
    | Centa', | " | 1 Des A. |
    | Des-a', | " | 1 A. |
    | A, | ${ }_{6}$ | 1 Dec |
    | Dek-a', | ${ }^{6}$ | 1 Hect A. |
    | Hect-a', | " | 1 Kil A. |
    | Kill-a,' | 6 | 1 Myr A. |

    MEASURES OF VOLUYEB, OR SOLIDS.

    | Written. | Prononnoed. |  |  |
    | :---: | :---: | :---: | :---: |
    | 10 Mil S , | Mill-ess' | make |  |
    | 10 Cent S, | Cent-ess, |  | 1 Cent S. <br> 1 Des 8 |
    | 10 Des S, | Des-ess', | 6 | $1 \text { Nes S. }$ |
    | 10 S , | Ess, | 6 | 1 Dec S. |
    | 10 Dec S, | Dek-ess', | 66 | 1 Dec $\$$. <br> 1 Hect S |
    | 10 Hect S, | Hect-ess', | 16 | 1 Kil S. |
    | $\begin{aligned} & 10 \text { Kil S, } \\ & \text { Myr S, } \end{aligned}$ | Kill-ess', | 18 | $1 \mathrm{Myr} \mathrm{S}_{\text {. }}$ |

    ## MEASURES OP CAPACITY.

    Writton,
    10 Mil L,
    10 Cent L,
    10 Des L,
    10 L,
    10 Dec L,
    10 Hect L,
    10 Kil L,
    Myr L,

    Pronounced.

    | Mill-ell', | make | 1 Cent L |
    | :---: | :---: | :---: |
    | Cent-ell', | 6 |  |
    | Dess-ell', | 6 | 1 L |
    | Ell, | 6 | 1 Dec I. |
    | Dek-ell', | 86 | 1 Hect 1 |
    | Hect.ell', | ${ }_{6}$ | 1 Kil L. |
    | $\begin{aligned} & \text { Kill-ell', } \\ & \text { Mir-ell', } \end{aligned}$ | 4 | 1 Myr L. |

    MEASURES OF WEIGETS.

    Written.
    10 Mill $G$, 10 Cent G, 10 Des $G$, 10 G 10 Dec G, 10 Hect $G$, $10 \mathrm{Kil} \mathrm{G}_{\mathrm{d}}$

    Pronousead.

    | Mill-gee, | make | , |
    | :---: | :---: | :---: |
    | Cent-gee', | ${ }_{6}$ |  |
    | Destgee', | 6 | 1 G. |
    | Gee, | 16. | 1 D |
    | Dek-gee', | " | 1 Hect $G$ |
    | Hect-gee', | ${ }^{6}$ | $1^{\prime} \mathrm{K}$ il C . |
    | Kill-gee,' | * | 1 Mrra. |

    ## REDUCTION OF COMPOUND DENOMINATE NUMBERS.

    214. Reduction is the proeess of changing numbers from one denomination to another, without altering their value.

    Reduction is of two kinds, Descending and Ascending.
    25. Reduction Doscending is changing numbers to lower denominations without altering their value ; as pounds to shillings, yards to feet, etc. It is performed by Multiplication.
    216. Reduction Ascending is changing numbers to higher denominations without altering their value; as farthings to pence, inches to feet, etc. It is performed by Division.

    ## REDUCTION DESCENDING.

    217. Case I.-To rediuce a compound number to lower do. nominations.
    Ex. Reduce $£ 45$ 7s. 8 d. to pence.

    | operation. | Analysis.-There are 20e. in $£ 1$; therefore |
    | :---: | :---: |
    | £45 78. 8d. | 20 times the number of $\mathcal{E}=$ the number of |
    | 20 | shillings. 20 times $45=9008$, to which we add |
    | 907 s. | therefore, 12 times the number are |
    | 12 | th3 number of pence. 12 times $907=10884 d^{\text {., }}$ |
    | 10892d. | to which we add $8 d$., and obtain 10892d. Hence the following |

    218. Rule.-I. Multiply the highest denomination of the given number by that number of the scale which will reduce it to the next lower denomination, and add to the product the given number, if any, of that lower denominution.
    II. Proceed in like manner with the results obtained in each Wwor denomination, until the reduction is brought to the denom. ination required.

    ## EXAMPLES FOR PRAOTICE.

    1. In $£ 3568.8$ d., how many pence?
    2. In $£ 28$ 12s. $8 \frac{3}{4}$ d., how many farthings?
    3. In 144b. 10oz. 18pwt. 22gr, how many grains? Ans. 85894.
    4. In 165T. 13cwt. 3qr. 19lb. 14oz., how many ounces?
    5. In 23 Hb 9 s 0 3 2 g 13 gr gr, how many grains?
    6. In $12 r d$. $8 y d$. $2 f t$., how many feet?
    7. How many inches in 2 mi . 4 fiter. 32 rd . 1 gd .?
    8. I: 60 arp . 7per. 1to. $5 f t$., how many feet?


    9. How many links in $7 m i$. 5fur. 6ch. 30l.?
    10. In $4 m i .49 \mathrm{ch}$. $72 l$., how many links?

    I1. 1 nches 12. In 10 A. $1 \boldsymbol{R}$. 25 sq. rd. 16 sq. Ans. 80937864 square inches. square inches?
    13. How many square links in 75 Ans. 65296108 square inches.
    14. How many poles in 3 townships of . ch. $8 P$. 118 sq. $l . ?$
    15. In 7sq. arp. 30 sq per. square inches?
    16. How many cubic feet in 67 Ans. 34080952 .
    17. In 30 oords of wood, how mards aubic inches ? feet of wood?
    18. In $4 \frac{3}{4} \mathrm{gal} .4 .25 q t .4 .75 \mathrm{gi}$., how many gills ?
    19. In $57 t u n s$ hhid. 50 gal . 3qt., how many pints?

    Ans. 190 .
    20. How many pints in 10 bu .3 .5 pk . $72 \mathrm{~F} q$. I pt.?
    21. How many quarts in 676 chaldrons, of 36 bushels each ?
    22. In 4da. 4h. 45 mi ., how many seconds? Ans. 362700.
    23. In $3 w /$. 2da. 1 h . 1 min., how many minutes?
    24. How many days from March 17th., 1870, to May 16th. 1871 ?
    25. In 44 S . $18^{\circ} 5$ ? ' $^{\prime} 23^{\prime \prime}$, how many secouds? Ans. 4820243'.
    26. How many minutes in $14 \frac{1}{2}$ C. IS. 10 1'?
    27. Reduce $38 \mathrm{lb}, 6 \mathrm{~s} 3 \mathrm{la}$, to grains.
    28. How many days from August 30th 1771, to June lat. 18729
    29. Louis has a lump of pure silver weighing 13lb. 90z. What is its value at $\$ 1.385 \frac{7}{10}$ per ounce?
    30. Change 13l6. 6oz. Avoirdupois weight to Trs. $\$ 228.6404$.
    31. Purchased 3A. IR 30rd. of land what did I pay for the land?
    32. Bought 2 hogsheads of sirup at 40 cts. Ans. $\$ 187171.871$. 12 cts. per quart; what did I gain by the bargain? gal., and sold it at
    215. Case II.-To reduce a denominate fraction to one of a lower denomination.
    $\boldsymbol{E x}$. Reduce ${ }_{8}$.
    gal.
    480.
    394.
    analyeis.-To reduce gallons to gills, we multiply successively by 4,2 , and 4 , the numbers in the scale. And, since the given number is a fraction, we indicate the process, ae in multiplication of fractions ; and, after oancolling, obtain $\frac{5}{28}$, the answer. Hence, the
    220. Ritle.-Multiply the fraction of the higher denomination by the numbers in the descending scale successsively, between the given and the required denominations.

    ## GXAMPLES POR PRACTICE.

    1. What part of a farthing is $\frac{1}{z^{2}}$ of a $£$ ? 2. Beduee rotos of a week to the fraction of a minute.
    2. What part of a square foot is $\frac{1}{5} \frac{1}{5 \sigma}$ of an acre? Ans. $\frac{4}{5} 8 q$. ft.
    
    3. Reduce $\frac{1}{6 \pm 0}$ of a $£$ to a fraction of a penny.

    Ans. ${ }_{8}^{3} d$.
    6. Reduce $\frac{3^{3}}{880}$ of a cowt. to the fraction of an ounce.
    7. What part of a pound is $\frac{3}{14000}$ of a ton?
    8. What part of a link is $\frac{1}{45}$ of a rod ?
    9. Reduce ${ }^{19} 88$ of a furlong to a fraction of a foot.
    10. What part of a pint is $\frac{5}{9} \sigma$ of a bushel ?
    11. Reduce $\frac{2}{6}$ of $\frac{2}{6}$ of, $2 l b$. to the fraction of an ounce Troy.
    12. What part of a square rod is $15^{3}$ of $4 \frac{1}{4}$ times $\frac{1}{18}_{2}^{6}$ of an acre?
    13. What fraction of a yard is of of $\frac{4}{7}$ of a rod ?
    
    15. Reduce 0.03125 of a mile to feet.
    221. Case III.-To reduce a denominate fraction to integers of lover denominations.
    E.c. What is the value of $\frac{3}{7}$ of a $£$ ?
    

    Analysis.- $\frac{3}{7}$ of $£ 1$ is the same as $\frac{1}{7}$ of $£ 3=8 \mathrm{e} .6 \mathrm{~d}$. $3 \frac{\mathrm{~s}}{7} \mathrm{far}$. Hence, the
    I
    

    \author{

    $f$ s. d. far. <br> | 3000 |
    | :--- |
    | $0863 \frac{3}{7}$, Ans. |

    }
    222. Rule.-Consider the numerator of the fraction as so many units of the given denomination, and divide them by the ienominator.

    ## EXAMPLES FOR PRAOTIOE.

    What it the value of
    > 2288. CASE IV.-To reduce a denominate decimal to integers
    of lower denominations

    1. $\frac{8}{1}$ of a $£$ ?
    2. $\frac{3}{5}$ of a bushel?
    3. $\frac{5}{-}$ - of a bhilling?
    4. $\frac{7}{8}$ of a cwt.?
    5. $\frac{5}{7}$ of a yard?
    6. \% of a lb. Avoirdupois?
    7. $\frac{9}{75}$ of a day ?
    8. $7^{5}$ of 15 cwt ?
    9. $\frac{6}{6}$ of 15 cwt. ? $\quad$ Ans. 12 cwt . 85lb. $11 o z .6 \frac{6}{7} d r$.
    
    10. ${ }^{2} \mathrm{~g}$ of a hhd. of wine?
    11. $\frac{1}{8}$ of $3 \frac{3}{8}$ cords of wood?
    12. $\frac{3}{7}$ of a sign?
     what part of the whole piece did I take?

    Ans. 5s. 5d. 19 ${ }^{\text {f }}$ far Ans. 1pt. 4qt. $1 \frac{3}{5} p t$.
    Ans. 3qr. 2lb. 12oz. $71 \mathrm{l} d \mathrm{dr}$.
    Ans. 7oz. 17 dr. Ans. 6gal. 2qt. 1pt. $0_{19}^{4} \mathrm{gi}$ i. part of the whole.plece did I take? 1
    int th
    and
    II
    manr at th
    1.
    2.
    3. 0
    4. 0
    5. 0
    6. 0
    7. 0
    8. 0
    9. 7.
    10. 0
    11. 0.
    12. 0.
    ${ }_{5}^{5} 8 q . f t$.
    $1 n s . \frac{3}{8} d$.

    Ans. $\frac{5}{8} l$.
    8. $\frac{5}{14} p t$.
    acre?
    ${ }_{649}^{640} d r$.

    0 integers
    $1028 \frac{1}{7}$ of
    $x$ as so by the
    $176 d r$.
    $6 \frac{6}{7} d r$.
    q. in.
    $1{ }_{1}^{4} 9$ gi.
    25"占. 2 gr. 1

    Ex. Reduce 0.628125 of a $£$ to shillings and pence.
    operation. £0.628125
    $\frac{20}{12.562500}$.
    12
    6.750000 d .

    4
    3.000000 far .
    

    Aralysis, - We first multiply the given decimal, 0.628125 of a $£$, by 20 to reduce it to shillings, and the result is 128 . and the decimal .5625 of a shilling. Wo then coultiply this decimal by 12 to reduce it to pence, and obtain $6 d$. 4, to reduce it to far. or docimal we multiply by 4, to reduce it to far. or qr., and the result is 3
    far. or $z$ of a $\alpha$. Hes, 6id.
    224. Rule.-I. Multiply the given decimal by that number ine the scale which will reduce it to the next lower denomination. and point off as in multiplication of decimuls.
    II. Proceed with the decimal part of the product in the same manner until reduced to the required denominations. The integers at the left vill be the answer required. . The integers

    ## EXA':PLES FOR PRAOTIOE.

    What in the value of

    1. 0.45 of a $£$ ?
    2. 0.748 of a bushel?
    3. 0.765 of a pound Troy?
    4. 1.7525 of a mile?
    5. 0.659 of a week ?
    6. $0.217^{\circ}$ ?
    7. 0.875 of a hhd. ?
    8. 0.865 of an acre?
    9. 7.88125 acres ?
    10. 0.625 of a fathom?
    11. 0.78875 of a long ton?
    12. 0.S.469 of a degree?

    Ans. 9e. 1d. $2 \frac{2}{5}$ far Ans. 2pk. 7qt. Ipt. 3.488 gi . Ams. 6 fur. Urd. 4yd. 1ft. Zgisin.

    Ame. 13' 1.2"'.
    Ans. 3R. 18\%og. rd.
    

    ## REDUOTION ABCRNDING.

    225. CASE I.-To reduce a denominute number to a compound
    number of higher denominations.
    Ex. In 78692gr., how many pounds Troy weight?
    oferation.
    24) 78692 gr .

    20 $\overline{3275 p} p t .20 \mathrm{gr}$.
    $1 2 \longdiv { 1 6 3 0 } . 1$ ४prot. 1316. 70\%.

    123b. 7es. 18 puct. 20 yr., Ame,

    ANalysis.-24gr. $=1$ 1piot.; thero.
    fore, $\frac{1}{24}$ of the namber of graina $=$ the number of ponny feighis. $\frac{1}{2}$ of 78692 - 3278 pwt., avd 20 gr . remain- ${ }^{24}$ ing. 20 put. $=10$ os.; therefore, $\frac{1}{\text { o }}$ of the number of penny woights $=0$ the number of ouncen. $\frac{1}{20}$ of $3278=$ 163on., and 18prot. romaining. 120 os. -16.1 therefors, $1 \frac{1}{5}$ of the number
    of onneess $=$ the number of pounds. $\frac{1}{12}$ of $163=13 l b$., and 7 ow. remalning, therefore, 78692gr. $=13 \mathrm{lb}$. 7os. 18 peot. 20 gr . Hence, the
    226. Rule.-I. Divide the given number by that number of the ascending scale which will reduce it to the next higher denomination.
    II. Divide in like manner the quotient thus obtained, and so proceed until it is brought to the denomination required. The last quotient, with the several remainders annexed in a reversed order; will be the answer.

    ## EXAMPLES FOR PRACTIOE.

    1. In $16452 f a r$., how many $£$ ?
    2. In 90720 pence, how many $£$ ?
    3. How many pounds in 4253?

    Ans. 117 2s. 9 d.
    4. In 78692 gr ., how many pounds Troy veight?
    5. A physician who a,verages daily 5 prescriptions of 20 grains each, how many pounds of medicine will he use in one year, or $\overline{\delta \delta} \dot{j}$ days?
    6. How many pounds of standard silver can be purchased for $\$ 1099.88$, at the rate of $\$ 0.062$ per pwt.?
    7. In $87320 l b$., how many tons?

    Ans. 43 T. 13cwt. $20 l b$.
    8. How much will $230 l b$. of hay cost, at $\$ 10$ per ton?
    9. In 1265 pints, how many bushels? Ans. $19 b u$. 3pk. lpt.
    10. At 6 cts. a pet, how much sirup can be bonght for $\$ 3.84$ ?
    11. How many francs in $\$ 176.70$ ?
    12. In 2468 pence. how many half crowns?
    13. In 90060 seconds, how many days ?

    Ans. 950.
    Ans. 1 d .1 h .1 mi . wide and $9 f$ hid be the cost of plastering a room $18 f$. long, 163 f . 15 and $9 f t$. high, at 22 cts. a sq. yd.:

    Ans. \$22.44.
    15. In a pond measuring $28 f$ f. 6 in ., how many fathoms deep is there?
    16. How many bushels of oats in $27072 q t . ?$ Ans. $846 b u s h$.
    17. How many days in 93960 seconds?
    18. The extent of a certain farm is found, by survey, to be 1377sq. ch. How many acres does it contain? Ans. 137A. 2 R. 32 per.
    19. $\Delta$ load of wood is 12 feet long and 3 feet wide, how high must it be to make a cord ?
    20. How many tons of round timber in 622080 Ans. $3 \frac{5}{7}$ ft. high.
    21. A cellar wall, $32 f$. by 410 is $6 f t$ higha cu. in.?
    much did it cost at $\$ 1.25$ ay $24 f$ f. is $6 f$. high and $1 \frac{1}{2} f$. thick. How
    Ans. $\$ 50.909+$.
    22. Reduce 16936 links to miles. Ans. 2mi. 9 ch. 3fi.
    23. In 161384 inches, how many miles ?
    24. How many beer gallons are them in lbd. 1 gal . 2qt., wine masure?
    25. In 5832000 square inches, how many roode?
    26. Reduce 20937 minates to signs.

    Ans. $27 \frac{3}{87}$.
    27. Change 16lb. jas. 1pie. The. $11 \mathrm{~S} .18{ }^{\circ} 57^{\prime}$.
    liugs. the nur
    28. A ship, during 3 days' storm at sea, changed her latitude 412 geographical miles; how many degrees and minutes did she change? 29. How many acres of land can be purchased in the city of Montreal for $\$ 147500$, at 65 cts a square fool! Ans. 5 A .33 per. $158 q . y \mathrm{~d}$. sq. ft. $119{ }_{157}^{24}$ s $3 q$. in.
    30. In 13360128 drams, how many tons?

    2d7. Case II. -To reduce a denominate fraction from a lower to a higher denomination.
    $\boldsymbol{E} \boldsymbol{x}$. Reduce $\frac{f}{5}$ of a farthing to the fraction of a $\boldsymbol{E}$.

    ## OPERATION.

    $\stackrel{\text { far. }}{\frac{1}{9}} \times \frac{1}{4} \times \frac{1}{12} \times \frac{1}{20}=\frac{1}{2160}$ Ans.
    lings. There are 20c. in $£ 1$, therefore $\frac{1}{20}$ of the number of $£$. Hence $\frac{4}{}$ far. $=4 \times \frac{10}{20}$ of the number of shillings equals 2.8. RULE.-Divide the fraction by the numbers in the scale, successively, between the given and the required denomination.

    ## examples for practice.

    ## What part of

    1. a pound Troy is $\frac{8}{5}$ of a grain?
    2. a pound is $\frac{5}{9}$ of a scruple ?
    
    3. a rod is $\frac{1}{4}$ of a foot?
    4. a mile is $\frac{8}{8}$ of a rod?
    5. a hundred-weight is $\frac{3}{2}$ of an ounce .
    6. an hour is $\frac{6}{8}$ of 20 seconds ?
    7. an acre is $\frac{5}{5}$ of a square foot?
    8. 3 hhd. is $\frac{4}{3}$ of a quart?
    9. 4 days is $\frac{8}{4}$ of a minute?
    10. a cord of wood is a pile $7 \frac{1}{2} f t$. long, $2 f t$. high, and Ans. $7 \frac{1}{688} \cdot$
    11. a rod is $2 \frac{3}{4}$ of $\frac{7}{12}$ of an ineli?
    12. an acre is $\frac{3}{19}$ of $\frac{4}{17}$ of $9 \frac{1}{2}$ square rods?
    13. Reduce 9.312 far. to the decimal of a $£$.
    14. Reduce 517.44 ft . to the decimal of a mile.
    15. Case III.-TTo reduce a compound number to a fraction of a higher denomination.
    Ex. Reduce se. Gd. 2 far. to the fraction of a $\boldsymbol{\varepsilon}$.

    OPERATION.
    $\begin{aligned} \text { Be. bd. } 2 \text { far. } & =410 \text { far } . \\ i £ & =\frac{41}{960} \mathrm{far} .\end{aligned}$

    ANAL PSia. - By reduction of demoningate numbers (217), we find se. bd. 2 far. $=410$ far., and that $£ 1=960$ far. One farthing is of o of a $£$, and $410 \mathrm{for}=410$ timon so $=44 \%=$
    230. Rule.-Reduce the given number to its lowest denomimution for the numerator, and a unit of the required denomination to the same denomination for the donominator of the re, uired fraction.

    EXAMPLES POR PRAOTIOE.
    What part of

    1. $2 f$ is $10 s$ s 10 d. ?
    2. a ton is 4 cwt. 3qr. 12l6.?
    3. an acre is $2 \boldsymbol{R}$. 20per.?
    4. a mile is 1 fur. $12 r d$. $4 y d$. $2 f t$.?
    5. a hogshead of wine is I8gal. 2qt.?
    6. a square rod is 144 ft . $19 \frac{1}{17} \mathrm{in}$.?
    7. 2cuvt. 3qr. is 1 cwt. $2 q r$. 20l6.?
    8. 30 days is $8 d a .17 h$. 20 min .?
    9. a bushel is $1 \frac{8}{5}$ pecks?

    Ans. $\frac{18}{4}$. Ans. ${ }^{\frac{4}{807} 7^{2}}$. Ans. $\frac{10}{6} 9$.

    Ans. $\frac{9}{17}$.
    An3. $\frac{15}{515}$
    10. a pound Troy is $100 z$. 13 put. 8 gr . ?
    231. Case IV.-To redice a compound number to a decimal of a higher denomination.
    Eix. Reduce 12s. 9d. 3far. to the decimal of a pound.

    | 3.00far. |  |
    | :---: | :---: |
    |  |  |
    | 12 | 9.7500 d . |
    | 20 | 12.812508. |
    |  | 0.640625£ |

    Ur; 12s. 9d. 3 far. $=615$ far.
    £1 $=960$ far.
    $\frac{1}{8} 1850{ }^{5}=£ 0.640625$, Ans.

    Aralymis.-Sinee there are 4 farthinge in $1 d$., $\ddagger$ of the number of farthings equals the number of pence. $\downarrow$ of $3=0.75 d$. whioh added to $9 d .=9.75 d$. There are $12 d$. in 18 ., therefore, $\frac{1}{12}$ of the number of pence equals the number of shillings. $\frac{1}{12}$ of $9.75 d,=0.8125$. which added to $: 28 .=$ 12.8125e. There are 20 e. in $£ 1$, therefore, $\frac{1}{20}$ of the number of shillings equals the number of pounds, $\frac{1}{20}$ of $12.8125=$ $\mathbf{£ 0 . 6 4 0 6 2 5}$. Hence, the
    232. Rule.-Divide the lowest denomination given by that number in the scale which will reduce it to the next higher denom.

    1. $£ 4$
    2. 27
    3. 27
    4. 69
    5. 0
    6. 77
    7. 17
    8. 18
    9. 

    $t$ denomi omination re, uired

    4ns. $\frac{13}{2}$. 8. $\frac{4^{487}}{2000}$.
    ns. 109.
    1ns. $\frac{9}{17} \cdot$
    23. $\frac{15}{5} \frac{15}{5}$
    decimal
    5. a pound Troy is $10 a z .12$ pot. 18 gr .?
    6. a fathom is 3 3 ${ }^{3} \mathrm{ft}$.?
    7. a ton is l6cut. sqr. 16.45lb.?
    8. $1 \frac{1}{4}$ bushels is 0.45 of a peck?
    9. Reduce 12T: 3cwot. 2qr. 20l6. to hundred-weights and the decimal of a hundred-weight.
    19. 112 Ans. 243.7. 17s. $5 \frac{1}{2} d$., and find their sum. Ans. $£ 2.710416$ +.

    ## REDUCTION OF THE OLD CANADIAN CURRBNCY TO THE NEW OR DECIMAL CURRENCY.

    Ex. Reduce $£ 7213$ 9룩 to cents.
    operation.
    and farthings by 5 , and divide the remainder by equal to $\frac{5}{12}$ of a cent.
    That each farthing is equal to $\frac{6}{12}$ of a cont, is evident from the fact that 48 farthings (or one shilling) are equal to 20 cents; or 12 farthings equal 5 cents, and one farthing equals $\frac{5}{12}$ of $a$ cent. Hence, the following
    233. Rule.-I. Multiply the pounds by 400, the shillings by 20, and take five-twelfths of the number expressing how many farthings there are in the given pence and farthings.
    II. Add the three results logether, and their sum will be the number of cents required.
    III. Consider the last two figures as cents, and the result will be dollars and cents.

    ## examples for praotice.

    How many dollars and cents in

    |  | 4311 ? | Ans | 11. |  |  |
    | :---: | :---: | :---: | :---: | :---: | :---: |
    |  | $2716{ }^{31}$ ? |  | 11. 97 | $311 \frac{1}{2}$ ? |  |
    |  | 2716 69 | Ans. \$111.383 ${ }^{\frac{3}{4} \text {. }}$ | 12. 4617 |  | Ans. \$187.52 |
    |  | 01481 ? | ins. \$2.94t. | 14. 12 |  |  |
    |  | 7719 41 ${ }^{\frac{1}{2}}$ ? |  | 15. 112 | 2 914? |  |
    |  | $1716{ }^{18} 8{ }^{5}$ ? | Ans. \$71.29 ${ }_{1}$ | 16. 17313 | 3 4? | Ans. \$694.66\% |
    |  | 9351 ? | An | $\begin{array}{ll} \text { 17. } 91 \\ \text { 18. } \end{array}$ | $8 \quad 8 ?$ |  |

    ## 142

    ## KKiltotion of the decimal currency To The

    OLD CANADIAN CURRENCY.H:C, Heduce $\$ 2.46 .88$ to the old Canadian currency.

    CHERATION.

    1) 216.88

    EKT. 72
    20
    14.408.

    12
    4.80 d .

    4
    3.20 far.

    Anw, sfyl $144 \frac{2}{4}+\frac{2}{10}=\frac{1}{5}$ far.

    Analysts.-We divide 246.88 by 4 , the number of dollars in $n$ pound, and the result is $\mathcal{E} 61$ and 72 hundredthe of a pound. We inultiply 72 by 20 (224). the number of shillings in a pound, and the result is 14 s . and 40 hundredths of a shilling. Agnin, we multiply 40 by 12, tho number of penoe in a shilling, and the result is $4 i l$. and 80 hundredths of a penny. Lastly, we multiply 80 by 4, the number of farthings in a penny, and the result is $3 f a_{i}$. and 20 hundredths or $\frac{1}{5}$ of a farthing. Hence, the

    2\%1. Rule. - Divide the given number by 4, and the quotient will be prounds and decimals of a pound. Then proceed as in No. 224.

    ## EXAMPLES FOR PRAOTIOE.

    Hednce to the old Canadian currency :-
    

    ## ADDITION OF COMPOUND NUMBERS.

    2th., Addition, Subtraction, Multiplication, and Division of Denomínate Numbers are performed by the same general methods, as are employed for like operations in Abstract Numbers. The only difierence arises from varying, instead of uniform scales.
     sul E4 13s, 9d.?

    |  |  |  |
    | :---: | :---: | :---: |
    | $\stackrel{1}{6}$ | ${ }^{8} 10$ | d. |
    | * | 18 | 10 |
    | 8 | 18 | 6 |
    | 4 | 18 | 9 |
    | 26 | 16 | 6 |


    ## О ТНЕ

    88 by 4, und, and edthe of a 0 (224). und, and redths of . y 40 by shilling, ndredths ly 80 by penny, ndredths

    Ex. 2. Add $\frac{7}{18}$ of a $£$ to $\frac{5}{7}$ of a shilling.
    operation.
    $\mathrm{T}_{\mathrm{t}}$ of a $£=9 \mathrm{~s} .4 d$.
    $\frac{8}{7}$ of a $s .=0$ s. $8 d .2 \frac{2}{7}$ far.
    Ans. 10s. 0d. $2 \frac{2}{7}$ fur. Or,
    $\frac{5}{7} \times \frac{1}{20}=1 \frac{5}{4} \mathbf{x}$.
    $\frac{7}{15}+\frac{1}{10} £=\frac{21}{2} 11 £ ;$ $\left.\frac{21}{13}\right)^{15}=10 s .0 d .2 \frac{2}{7}$ far.

    Analrsis.- We frat find the value of each frnotion in integers of less denominations (221), and then add the resulting or equivalent compound numbers.
    Or, we way reduoe the given fractions to fractions of the same denomination (219), then add them, and find tho valne of their sum in lower denominations. Henoe, the following
    236. RuLe.-I. If any of the numbers are denominate fractions, or if any of the denominations are mixed numbers, reduce the fractions to integers of lower denominations.
    II. Write the numbers so that units of the same denominations will stand in the same column.
    III. Beginning with the lowest denomination, add as in simple numbers, carrying to each succeeding denomination one for as many units as it takes of the denomination added, to make one of the next higher denomination.

    EXAMPLES FOR PRACTIOE.

    ## (1.)

    (2.)

    | $\boldsymbol{T}$. | $c w t$. | $q r$. | $l b$. | uz. | $d r$ |
    | ---: | ---: | ---: | ---: | ---: | ---: |
    | 71 | 19 | 3 | 27 | 14 | 13 |
    | 14 | 13 | 2 | 15 | 15 | 15 |
    | 14 | 13 | 1 | 11 | 13 | 12 |
    | 11 | 17 | 3 | 16 | 15 | 11 |
    | 13 | 18 | 2 | 13 | 11 | 13 |
    | 127 | 3 | 2 | 11 | 8 | 0 |

    (3.)

    | deg. | mi. fur. rd. | ft. | in. |  |  |
    | ---: | :---: | :---: | :---: | ---: | ---: |
    | 14 | 19 | 7 | 15 | 11 | 1 |
    | 61 | 47 | 6 | 39 | 10 | 11 |
    | 78 | 32 | 5 | 14 | 9 | 9 |
    | 17 | 59 | 7 | 36 | 16 | 10 |
    | 28 | 56 | 1 | 30 | 16 | 1 |
    | 205 | $8 \frac{1}{2}$ | 5 | 17 | $14 \frac{1}{2}$ | 8 |
    |  | $=4$ |  | $\frac{1}{2}$ | $=6$ |  |
    | 205 | 9 | 1 | 17 | 15 | 2 |

    (4.)

    | A. | R. | per. sq. | yd. sq. $\boldsymbol{f l}$. |  |
    | ---: | ---: | ---: | ---: | ---: |
    | 140 | 3 | 17 | 27 | 6 |
    | 320 | 1 | 30 | 14 | 2 |
    | 111 |  | 7 | 3 |  |
    | 214 | 2 | 15 | 22 | 7 |
    | 100 | 3 |  | 6 | 1 |
    | 25 | 1 | 36 |  | 8 |
    | 104 | 2 | 9 | 1 | 4 |

    5. What is the sum of 20lb. 9oz. 19pwt. 23gr., 10lb. 7oz. 15 puot. $13_{6}$ r., $110 z . \mathrm{g}_{\mathrm{gr}}$, and llb. 8oz. 1 7piot. 21 gr . ? Ans. 344b. loz. 13 prot.
    6. Find the aum of 81 th 11 s 6 s ls 19 gr ., 75 ft 10 s 7 s 2 s 13 gr .,
    
    7. Add 197sq. vd. 4sq. ft. 1041 sq . in. Ans. 272th 43.3318 gr . 5sq. yd. 8sq. fl. ¿"sq. in., and 217sq... 2 -sq. yd. 2sq. ft. 2794sq. in., Ans ig. yd. 7sq. ft. 12slisq. in.
    8. What is the sum of $17 \mathrm{Ans}, 563 \mathrm{sq} . \mathrm{yd}$. 4 sq . ft. 118.825 sq . in. $1 \mathrm{rd} .21 \mathrm{l}, \mathrm{}$,47 mi . 7 fur. 9 ch . 3rd. 19 mi . 8 ch .3 rd . $24 \mathrm{l} ., 16 \mathrm{mi}$. 3 fur. 7 ch . 31 mi .7 fur. 1ch. $20 \ell . ?$
    9. Add 3S. $22^{\circ} 50^{\prime}, 24^{\circ} 36^{\prime} 25.7^{\prime \prime}$ 17' Ans. $13 \mathrm{~B}^{\prime} \mathrm{mi}$. 7 fur. 4 ch . $12^{\circ} 36^{\prime} 17.8^{\prime \prime}$, and $57^{\prime} 3^{\prime \prime}$. $36^{\prime} 25.7^{\prime \prime}, 17^{\prime} 18.2^{\prime \prime}, 1 \mathrm{~S} .3^{\circ} 12^{\prime} 15.5^{\prime \prime}$,
    10. Find the suin of tit of mile, Ans. 6S. $3^{\circ} 33^{\prime} 14.5^{\prime \prime}$. ${ }^{7}{ }^{7}$ of a yard. Ir of a mile, of a mile, $\boldsymbol{y}^{3} T$ of $a$ furlong, and
    11. Add $\frac{4}{7}$ of a ton to 17 of a cwt. 6fur. 29rd. 3yd. lft. $01 \frac{1}{T} i n$.
    12. Add $\frac{\pi}{18}$ of a week to $\frac{17}{}$ of a duy.
    13. What is the snm of $\frac{5}{5}$ an and Ans. $2 d a .9 / h .18 \mathrm{~min}$.

    Ans. $3 B$ losq acre and of ot a rool?
    14. lind the sum of 4 of a cwt. ros. 8sq. yd. 5sq. ft. $113 \frac{1}{7} \mathrm{sq}$. in.
    15. A farmer received 60 cts . a buskel for 4 a 3 . a . by long tun table. taine! 42.4 bu . ; the second, 2866 b .; the for 4 loads of corn; the first con39bu. 291b. How much did he receive third, $363 \mathrm{bu} . ;$ and the fourth, 16. Add $\frac{2}{8}$ of a yard, $\frac{\text { e }}{8}$ of yareive for the whole? Ans. $\$ 101.90+$.

    ## SUB'TRACTION OF COMPOUND NUMBERS.

    Ex. 1. From $£ 35$ 6s. 10d. 1far. take $£ 14$ 15s. 8d. 3far.
    OPERATION.
     from 1 far, we write the remaindor, 3far. making $9 d$; ard making $9 d_{\text {. ; }}$; and $9 d$. from 10d. leaves $1 d$. ., which Next, as we oannot take 150. from 68., we add $£ 1$ we write in the remainder. taking 15s. from 26s., we write the renaind shillings. diding $£ 1$ to $£ 14$, we subtrainder, $1 / \begin{aligned} & \text { e., under the denomination of }\end{aligned}$ and writo the remainder, $£ 20$, we under tho column of $£ 35$, hs in simple numbers,
    E.c. 2. From $\frac{5}{8}$ of a mile subtract $\frac{4}{7}$ of a furlong.

    OPERATION.
    $\frac{8 i}{}$ mi. $=4$ fur. $17 \mathrm{rd} .4 \mathrm{yd} .0 f \mathrm{t} .10 \mathrm{in}$. ${ }_{1}^{4}$ fur. $=$
    Ans. $\overline{3}$

    Analyais,-W riting the subtrahend urador the minuend, placing units of the same denomination under each other, we bogin at the right-hand ; aince we oannot take 3 far. from 1 far., we add $1 d$. or 4 far. to 1 far., making 5 far. ; and takins 3 far. underneath tho column of farthinge. Ilav-

    ## SUBTRACTION OF COMPOUND NUMBERS.

    23.T. Ruce.-I. Write the swhtrohend under the minuend, hut units if the same denomination shall stand under each other. II. Beginning at the right-himil, subtract each rlenominution separately, as in simple numbers.
    III. If any term of the minuend is less than the corresponding term of the subtrahend, add to that term as many units us are required of that denomination to nuke one of the next higher, and from the sum tale the trim of the subtrahend, and add 1 to the next term of the subtrahend before silberacting.
    IV. Proceed in life manner with each denomination.

    ## EXAMPLES FOR PRACTICE.

    5. From £23 18s. 31 d. take £13 14s. $10 \frac{1}{4} d$.
    6. From 71 lb . 30z. 12 pwt . 15 gr . take 16 lh . Ans. £10 Bs. Sld.
    7. Subtract 3tb 85232318 gr . from 10 to 7 . 100 z . 17 pw i. 20 gr .
    8. From 171 T, 3 hhd .8 gal . l yt. 1 pt . 1 g 43 la 15 gr. 3qt. l pt. cgi.
    9. From 56A. $P$ Ans. 72T. 1 hhd 51 1. hhd. 19 gal . 113 in.
    deg. mi. fur. rd. yd. ft. in.

    | 95 | 3 | 7 | 31 | 1 | 1 | 3 |
    | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
    | 18 | 17 | 1 | 39 | 1 | 2 | 7 |
    | 76 | $55 \frac{1}{6}$ | 5 | 31 | $4 \frac{1}{2}$ | 1 | 8 |
    |  | $\frac{1}{6}$ | $=1$ | 13 | 1 | 2 | 6 |
    | 76 | 50 | 7 | 6 | 1 | 1 | 2 | Ans. take 17 A. 3 R. $13 p$. $127 f t$. Bin. 11. Prom $\frac{5}{5}$ of a bushel Ans. 6 mi. 9 mi. 7 fur. 19 rd . 16 ft

    12. From
    13. Subtract $\frac{8}{7}$ of 9 cunt $\frac{1}{}$ of a day. Ans. pk. $4 y t$. pt.
    14. From $5 \frac{1}{2} b \dot{b} l$. take from $\frac{1}{18}$ of 5 tons.
    15. Subtract 0.659 w of a hogshead.
    16. From a hogshead of sirum 2 weeks $3 \frac{5}{6}$ days. $4 b b l .11 \mathrm{gal}$. l gt. out, and 2 a for sale?

    ## (4.)

    | th | 3 | 3 | 2 | gr. |
    | :---: | :---: | :---: | :---: | :---: |
    | 15 | 7 | 3 | 1 | 14 |
    | 11 | 9 | 7 | 2 | 19 |
    | 3 | $y$ | 3 | 1 | 15 |

    $$
    \begin{array}{ccccc}
    \text { A. } & \text { K. } & \text { p. } & \text { ft. } & \text { is. } \\
    96 & 1 & 13 & 100 & 113 \\
    89 & 3 & 17 & 200 & 117 \\
    \hline 6 & 1 & 35 & 171 \frac{1}{4} & 140 \\
    \hline 6 & 1 & & 35 & 172
    \end{array} \frac{36}{32}=
    $$

    ## PRACTICAL PROBLEMS IN COMPOUND ADDITION AMD SUBTRACTION.

    1. I had 10A. 3R. 10 per. of land; and I have sold two houselotes, one containing lA. $1 \boldsymbol{R}$. 1:3per., the other $2 A$. $2 R$. 5 per. ; how mweh have I remaining?
    2. An excavation $58 f t$. long $37 f t$. wide, and $6 f$. deep is to be mede for a cellar; after $471 \mathrm{cu} . y d$. $16 \mathrm{cu} . \mathrm{fl} .972 \mathrm{cu}$. in. of earth have removed, how much atill remains to be taken out?
    3. Bought a hogshead of sugar weighing 9cuot. 3yr. 21ll,; sold John Icwt. 2qr. 15lb. ; to Bernard 2cwt. 3qr. 24lb. ; and to Thomag 3cwt. Iqr. 15lb. ; how much remains unsold? Ans. Icwot. 3qr. 17 lb .
    4. Joseph and Henry start from two places 120 miless apart, anl travel toward each other; after Joseph travels $\frac{3}{7}$, and Henry $\frac{8}{3}$, of the distance, how far are they apart? Ans. 41 mi . 7 fur. 9 rd .4 ft .75 sin .
    5. A man agrees to build 136 rd . and 15 ft . of stone feuce; at one time, he builds 36 rd . 2 ft . ; at another time, of 6 rd . 3 ft . ; and at one other time, 10 rd . 1 fl . How much still remains to be built ?
    6. A merchant sold goods to the amount of $£ 397$ 18s. 61 d .; and received in payment $£ 199$ 198. 10 盎d.; how much remains due?
    7. A hogshead of wine, lost by leakage, on an average, for 5 years, including two leap years, one gill of wine a day; how much ré mained?
    8. Suppose a person wes bor Ans. 5gal. 3qt. 1pt, lgi, anniversaries of his birthday will he February 29, 1792 : how many
    9. How long has a note to run, dated April 23, 1870, 1844 \% payable Dec. 9, 1874 ?
    10. From a mass of silver weighing 106 lb . Ans. 4 yr. 7 mo .15 da , spoons, weighing $5 l b$. 1 loz. 12 prot. $15 \mathrm{gr} . ;$ a tankard, 3 lb .0 oz .13 pa 14 gr ; a vase, 7tb. 11 oz. 14 pwt. 23 gr . ; how much unvirought silver, remains ?
    11. From a pile of wood containing Ans. 88 lb . $1108.18 p w t$. 20 gt . 56C. 112 cu . ft. ; at another time, 97 C .113 cu . ft. ; at at one ume, 126C. 97cu. ft. How many cords reniain unsold? ; at another time,
    12. Suppose a note given Sept. 10 , 185 unsold How long was the note on interest, if we 5 , to be paid Marcl: 5, 1868. How long, if the time is computed by days? 30 days to the month ? Ans. 1 st .11 yr. 5 mo . 25 da . ; 2nd. 4135 days.

    ## MULTIPLICATION OF COMPOUND NUMBEAS.

    Ex. 1. Multiply $£ 898$. 5d. by 6.

    | operation. |  |  |
    | :---: | :---: | :---: |
    |  | 8. | $d$. |
    |  | 9 | 5 |
    |  |  | 6 |
    |  |  |  |

    Analyane. -6 times $5 d$, are $30 d .=28,6 d$, We Write the $6 d$. ander the pence, and add the $2 t$, with the product of shillings. 6 times 90 . are 64 , and $2 a$. , are $568 .=£ 2168$. We write the 16 s . umder the shillings and add the $£ 2$ with the produet of
     wo write under pounds. Thorefore 6 times $48 \%$,

    Analy factors; arately: and obtair the value last produ 10 barrels barrel by anewer.
    240. ber, resol multiply -btained. ination of the multiplicand. II. Multinly as in simple numbers, and carry as in addition of compound numbers. risable to multiply by the componont farge, and is a composite number, it is ad-
    2. When the multipio it ponont factors. solved Into any convenient parts, and inultipla composite number, it may be re-
    on made by these several parts.
    Ex. 2. What will 45 yards of cloth cost, at $£ 2$ 3s. $6 d$. per yard ?
    

    > ANALYsis. - We find the number 45 equal to the product of 5 and 9 ; we therefore multiply the price of 1 yard by 5 , and then that product by $9 ;$ last and the the product is the answer. Hence $\boldsymbol{£} \overline{97 \quad 178 . \quad 6 d .}=$ price of $45 y \mathrm{ds}$. the
    285. Rule.- When the multiplier is a composite number, multiply by its fuctrors in succession. Ex. 3. What cost 643 barrels of flour, at $£ 258.7 d$. per bbl.? operation.

    $$
    \begin{aligned}
    & 10 \mathrm{bbl} .=\frac{221510}{10} \times 4=9134=\text { value of } 40 \mathrm{bbl} \text {. } \\
    & 100 \mathrm{bbl} .=22718 \quad 4, \times 6=1367 \quad 10 \quad 0=\text { value of } \mathbf{2} 00 \mathrm{bbl} . \\
    & \text { Ans. } \frac{146510 \mathrm{l}}{14 \mathrm{~L}}=\text { value of } \frac{200}{} \mathrm{bbl} .
    \end{aligned}
    $$

    Analyais.-Since 613 is not a composite number, we oannot resolve it into arately: thus, $643=600$ parat it into parts, and tind the value of each part sepand obtain the value of $10+40+3$ barrels, In the operation, we first multiply by 10 , the value of 100 barrels. Then, to and this pro luct we multiply by 10 , and obtain last product by 6 ; and to find the value of value of 600 bnrrels, we multiply the 10 barrels by 4 ; and to find the value of 3 barrels, we multiply the value of barrel by 3. Adding the several products, barrels, we multiply the value of 1 answer. Hence the
    240. Kule.-When the multiplier is not a composite num. ber, resolve it into auy convenient parts, as of units, tens, etc., multiply by these several parts, and add together the products thus obtained for the required result.

    ## EXAMPLES FOR PRACTIOE.

    ## (1.) <br> (2.)

    | cut. | qr. | lb. | oz. |
    | :---: | :---: | :---: | ---: |
    | 18 | 3 | 17 | 10 |
    |  |  |  | 6 |
    | 113 | 2 | 5 | 12 |

    (4.)
    mi. fur. rd. ft. $\begin{array}{llll}14 & 6 & 36 & 14\end{array}$
    
    (5.)
    7. How much cloth will it take for 8 suits of clothes, if each suit require $8 y d . \operatorname{lqr}$. $3 n a$. ?
    8. A man gives each of his 9 sons 23A. 3R. 1919p., what do they all receive?
    9. How long will it Ans. $214 A .3$ R. $12 p$. take him 8 h .45 min .50 sec ., to saw 1 cord?
    10. If 1 share in a certsin stock be valued at $£ 138 \mathrm{~s} .9 \frac{1}{2} d$., what is the value of 96 shares? Ans. $£ 1290$ 4s. Od.
    11. If a family consume 12 gat . $3 q \mathrm{t}$. lpt . of molasses in one week, what quantity will they consume in 1 year?
    12. If a man be $2 d a .5 h .17 \mathrm{~min}$. 19 sec . in walking 1 degree, how long would it take him to walk round the earth, allowing $365 \frac{1}{4}$ days to a year?
    13. What will be the value of 1 dozen gold cups, each cup weighing 9oz. $13 p w t$. 8 gr., at $\$ 212.38$ a pound?
    14. If a ship sails $3^{\circ} 24^{\prime} 10^{\prime \prime}$ per day, how far will she sail in 60 days?
    15. One ton of oopper ore will buy 17T. 14cuot. 3qr. 18lb. 140s. of iron ore; how much will 4.51 tons buy?
    16. If $\$ 80$ will buy $4 A$. 3R. 26 per. 20sq. yd. 3sq.ft. of land, how much will $\$ 4800$ buy?
    17. If l cask of oil contain 46 gal 2qt Ans. 295A. 10sq. yd. ars mill 100 casks of the same size contain?
    18. What is the cost of a board $18 f t$. 9in. long, and $2 f t .31 \mathrm{in}$. wide, at $\$ 0.053$ per foot?

    Ans. $\$ 2.277 \frac{1}{3} \frac{1}{2}$.
    19. Bought 17 bags of hops, each weighing 4cwt. 3yr. 7ib., at $\$ 5.8 \% \frac{1}{3}$ per cast. ; what was the cost?
    20. What cost 27T. l5cwt. lgr. $31 / b$. of hemp, at $\$ 183.62$ per ton?

    Ans. $\$ 5098.07+$.
    21. At $\$ 125.75$ per acre, what cost 37 A. 3 R. 35 rd . ?
    22. What cost the construction of 17 mi . 6 fur. 36 rd . of railroad, at $\$ 3765.60$ per mile? $\quad$ Ans. $\$ 67263.03+$.
    23. Bought a farm containing 144 A. $3 \boldsymbol{R}$. 30per., at $\$ 97.621$ per acre; what was the cost of the fawn?

    Ans. $\$ 14149.52+$.
    24. At $\$ 9.25$ per cwt , what cost 19 cut . 3 qr . 14 lb . of iron ?

    ## 3.)

    |  | 9 | $g r$. |
    | ---: | ---: | ---: |
    | 2 | 14 |  |
    |  | 11 |  |
    |  | 2 | 14 |
    | 5.) |  |  |
    |  |  |  |
    | fur. rd. |  |  |
    | 6 | 18 |  |
    |  | 8 |  | MULTIPLICATION OF COMPOUND NUMBERS

    solved by aliquot parts. table of aliqlot parts (173).
    
    the aliquot parts of $\$ 1$ (p. 105).
    241. Case I.- When the given price is: 10 furthings; $2^{\circ}$ pence, or pence and furthings; $3^{\circ}$ shillings, shillings and pence, or shillings, pance and farthings; $4^{\circ}$ pounds, shillings, pence and

    Ex. Find the price of 944 pens, at 3 . per pen.
    operation.
    

    Analyais. - In thisexample, the prioe being farthinge, we multiply the giren number by a peany; but. as $\frac{3}{} d$. is not an even part of a penny, we decompom it into $\frac{1}{2} d$. and $\ddagger d$.; $\ddagger d$. is the half of a penny, and $\ddagger d$., the fourth of a penny, or the half of $\frac{1}{} d$. We then take the of $£ 188$ for $\mid d$., giving for recult $£ 110$; then $\frac{1}{} d$., or $\frac{1}{}$ of $\ddagger d$., that $i 3$, one half of $£ 1194=190$. $8 d$., whioh wu add to £1 194 ; the aum then gir, $£ 2100$, for the answer.

    Ex. 2. What cost 1638 lb . of sugar, at 8 ld . per lb . $?$
    operation.
    16381b. at le $=1638 \mathrm{c}=£ 81180$
    
    Analysis.-The prioe being pence and furthinga, we multiply tho given number by a sbilling. Now, as $8 \frac{1}{2} d$. is net an aliquot part of a shilling, we deoompose it into 6d., $2 d$., and $1 d$. , und then proceed as in the forcgoing example.

    Ex. 3. Find the price of 252 yards of merino, at $3 \mathrm{~s} .9 \frac{1}{2} d$. per yd . operatioy.
    252 yards at $£ 1=£ 252$
    
    Anat.ysis. - Here, the price being shillinge, etc., we multiply the given number by a pound ; then, we docompose 3s. $9 \frac{1}{2} d$. into 3 e. $4 d$., $5 d$., and $0 \frac{1 d}{}$., and proseed as in the preceding examples.

    Ex. 4. What cost 694 cwt. of butter, at $£ 51161$ per cwt.? OPERATION.
    

    ## EXAMPLES FOR PRACTICE.

    
    9.

    Ex. Required the price of 1583 yards of cloth, at $£ 1211$ per yd.
    242. Case II. -When there is a fraction in the given quan. ON. $158 \frac{3}{4}$ yards, at 11211
    2s. $6 d .=£_{g}^{\prime}$
    $5 d .=\frac{1}{8}$ of $2 s .6 d$.
    1 of $x 1211$
    4 of $11 \mathrm{~s} .5 \frac{1}{2} d$.
    
    
     10. $5430 \times 0 \quad 3=67176$
    11. $2436 \times 0 \quad 61$
    12. $2147 \times 0 \quad 31=31623$
    1.. $7028 \times 0 \quad 8 \frac{8}{4}=241119$
    14. $2708 \times 0$
    $6 \frac{3}{4}$
    $\begin{aligned} & \text { 15. } 5491 \times 0 \\ & \text { 16. } 4936 \times 0 \\ & 168 \\ & 162\end{aligned}=17111101$
    17. $4967 \times 0101$
    18. $2522 \times 011=1151110$
    19. $2897 \times 0103=12915 \quad 23$
    20. $7509 \times 0 \quad 117$
    21. $1870 \times 0 \quad 93$
    22. $2244 \times 0 \quad 11_{4}^{1}=105 \quad 19 \quad 43$
    23. $392 \times 18$
    24. $576 \times 1 \quad 91=5100$
    $\begin{array}{lllll}\text { 25. } & 465 \times 3 \quad 7 \frac{1}{2}=84 \quad 5 & 71 \\ 26 . & 425 \times 411\end{array}$
    26. $425 \times 411 \frac{3}{4}$
    

    Analisis. - In this method, we first find the prioe of 158 yards, at $\boldsymbol{f 1}$ per sard. This is $£ 158150$; for the price of 158 yards is $£ 168$, and, the price of a quarter of a yard being evidently 5 s . 0d., that of 7 of a yard is 15 s . Then, the price at $£ 1$ per yard being $£ 15815$, the price at 2 \%. 6d. Fill be one eighth oi this, or $£ 1916101$; and the price at 5 d ., one sixth of the price at 2 e .6 d ., or $£_{3} 6 \mathrm{lq}$. The suin of these is $£ 181180 \ell$, the whole price, as before.

    ## EXAMPLES FOR PRACTICE.

    1. 187
    2. $328 \frac{3}{4}$
    3. 208
    4. 971
    5. 675
    6. 371
    7. 538
    8. 495
    ). 917
    9. 515
    10. 63
    11. 85
    12. $172 \frac{7}{10}$
    13. $176 \frac{8}{4}$
    14. 785
    15. $239 \frac{5}{4}$
    16. $375 \frac{5}{4}$
    17. 7591
    18. $774 \frac{8}{5}$
    19. $749 \frac{1}{12}$ both of several denominations. per cwt. ? 10s. 0d. $==£_{\frac{1}{2}}$. $2 \mathrm{~s} .6 \mathrm{~d} .=\frac{1}{4}$ of 10 s $2 q r .=\frac{1}{2}$ of 1 cutt. $10 l b .=\frac{1}{5}$ of $2 q r$. $5 l b .=1$ of 10 lb .
    $£ 5126 \times 94=\frac{£ 5126}{£ 528150}=$ cost of 1 cwt.
    $2 q r .=\frac{1}{2} c w t$.
    $2163=" 404$ cwt.
    $-q r .=\frac{1}{2} c w t$.
    $10 l b .=\frac{1}{5}$ of $2 q r$.
    $5 l b .=\frac{1}{2}$ of $10 l b$.
    Ane. . . .£533

    | £ s. <br> 1 17 |  |  |
    | :---: | :---: | :---: |
    |  |  |  |
    |  | 6 | 66 |
    |  | 13 | 310 |
    |  | 15 | 2 |
    |  | 7 |  |
    | 3 | 14 | 72 |
    | 0 | 4 | 8 |
    |  | 5 | 93 |
    |  | 18 | 104 |
    | 2 | 9 | 4 |
    |  | 18 | 9 |
    | 2 |  | 16 |
    |  | 15 | 10 |
    | 0 | 11 | 8 |
    | 7 |  | 33 |
    |  | 101 |  |
    |  | 191 | $11{ }^{\text {c }}$ |
    |  | 15 |  |
    |  |  |  |
    |  |  | $10 \frac{1}{2}=$ |

    243. Case III. _ When the given quantity and prive
    $\boldsymbol{E} x$. What is the cost of $94 \mathrm{c} w \mathrm{t} .2 q r .15 l b$. of tobacco, at $£ 5126$
    operation.
    

    $$
    \begin{aligned}
    & \text { Ans.....5532 } 81 \frac{1}{2}=\text { cost required } \\
    & \text { another method. }
    \end{aligned}
    $$

    470
    $11150=$ " " " " 2 "s. $6 d$.
    $2163="$ " $2 q r$. at $£ 5126$
    
    "
    $\qquad$

    $\square$

    |  | $\mathcal{E}$ | s. | $d$. |
    | :---: | :---: | :---: | :---: |
    | Ans. | 353 | 2 | 6 |
    | Ans. | 106 | 16 | 101 | Ans.

    Ans.
    Ans
    9650
    917
    11
    5 Ans. $\quad 125 \quad 14 \quad 2$ Ans. 1630139 Ans. $127114 \quad 0$ R Ans. $249 \quad 12 \quad 9{ }^{\circ}$

    Ans. $65416 \quad 5$
    Ans. 10321
    $\begin{array}{lrrr}\text { Ans. } & 5099 & 12 & 3! \\ \text { Ans. } & 1877 & 7 & 3 f\end{array}$
    Ans. $7416 \quad 15.104$ Ans. 6736 9 9\%
    1.

    1. 85cwt. 2qr. 7世t. at $£ 017$ + per cw:. Ans. £ 74 3 214.
    
    
    2. 129 cwot . lyr. 16 llb . at $£ 212$ 6. " 12 Ans. $£ 3: 391.400^{3}$.
    
    3. 28icwt. З3r. 7lb. at £1 1810 " 18 " Ans. $£ 55119$ 4+.
    
    4. 181cw'. 3qr. 53lh. at $£ 213$ " 4 "
    5. 175 tons $1 \times c w t$. lqr. at $£ 38130$ perton.
    6. $930 z$. 7 pqnt. ISgr. at $£ 0104$ per oz.
    7. $58 y d .3 q r$. Ince. at $£ 0128$ per yd.
    8. 8A. 3R. 19 per. at $£ 01810$ per acre.
    9. 58arp. 8per. 4 ft . at $£ 210 \mathrm{f}$ per arp.
    10. 11A. $1 \boldsymbol{R}$. 23per. at $£ 137 \frac{1}{2}$ per acre.

    Ans. $£ 6799004+$. Ans. $£ 48.411 \frac{1}{4}$.
    Ans. £ 8 7 $0 \frac{1}{3}+$ Ans. $£ 14810 \quad 6{ }_{15}^{4}$.

    ## DIVISION OF COMPOUND NUMBERS.

    Ex. 1. If 5 barrels of sugar weigh 9 cui. Iqr. 10lb., how much will
    1 barrel weigh ?
    operation.
    

    Analivaie. - One fifth of 9 ciot. is 1 coot. aud 4 ciot. n-16qr. remaining, to which we add the lqr., and haye $17 q r$. 1 fifth of $17 q r$. is $3 q r$. and $2 q r .=$ $50 l b$, remaining, to which we add the 10lb. and have 60lb. 1 fifth of $60 l 6$. is $12 l b$. Therefore, 1 fifth of 9 eot. 1 qr. $10 l b .=1000$. $3 q$ r. $12 l b$.
    244. Role.-I. Divide the highest denomination as in simple numbers, and each succeeding denomination in the same manner, if there be no remainder.
    II. If there be a remainder after dividing any denomination, reduce it to the next lower denomination, adding in the given num. ber of that denomination, if any, and divide as before.
    III. Proceed in like manner with all the denominations. The several partial quotients will be the quotient required.
    Notrs.-1. When the divisor is largo, and is a composite namber, we may ehorten the work hy dividing by the oomponent factors.
    2. When the divisor and dividond are both compound numbers, they must bs reduced to the same denominations, and the division then is the sane as in sim-
    ple numbers.
    $\boldsymbol{E} \boldsymbol{x}$. 2. When 24 -arde of silk velvet are sold for $£ 57100$, whal is the price of 1 yard

    ## operation.

    \& e.d.
    6) $5710 \quad 0=$ price of 24 yands.
    $4 \longdiv { 9 1 1 9 } =$ priee of 4 yarde.
    211 = price of 1 yand.
    Analyems.-24is equal to $\% \times 4$. We therefore divide the prioe by one of these faators, and the quotiont arising by the other. Honoe,
    245. Rule.-Divide by the factors of the composite number in succeession.

    Ex. 3. Divide £360 84 by 173.

    > operation.
    > $\ddagger$ 8. $d$.
    > 173) $\frac{360}{14}$ ४ 4 (£2
    > 173) $\frac{20}{288}$ ( le . 173
    > 115
    > 173) $\frac{12}{1384}(8 d$.
    > 173) $\frac{12}{1384}(8 d$.
    > 173) $\frac{12}{1384}(8 d$.

    Analysis, - We divide the pounds by 173, and obtain $£ 2$ for the quotient, and $£ 14$ remaining, which we reduee to shillings, and add the 8..; and again, divide by 173, and obtain 1e. for the quotient. The remainder. 115s., we reduse to pence, and add the 4d., and again divide by 173, and obtain $8 d$. for the quotient. Thus, the mothod is the same as by general rule (244). By uniting the several quotients, we obtair
    £2 18 , for the answer.

    Eac. 4. Divide $£ 2438$ by $£ 30 \frac{1}{5 \frac{1}{2}}$. operation. $\frac{\text { £24 3s. } 8 d .0 \text { far. }}{\text { £ } 3 \text { bs. } 5 d .2 \text { fur. }}=\frac{23216 \text { fur. }}{2902 \text { far. }}=8$.

    Analtsis. - Redacing both dividend and divisor to the lowest don nination mentinned in eithe, and then dividing as in simple numbers, we have 8 for the quotiont.

    EXAMPLES FOR PRACTIOE.

    | (1.) |  |
    | :---: | :---: |
    | T. | cwot. lb. |
    | 7) 45 | $15 \quad 25$ |
    | 6 | $10 \quad 75$ |

    (2.)

    9) | $l b$. | oz. | $d r$. |
    | ---: | ---: | ---: |
    | 143 | 5 | 5 |
    | 15 | 14 | 13 |

    (3.)
    hhd. gal. qt. pt. 12) $\frac{9 \quad 28 \quad 2}{4921}$
    4. A man in 1 month travels 746 mi . 5 fur., how far does he go in 1 day?
    5. If 21 yards of cloth cost $£ 1083$ whe. $24 m i$. ffur. 4 rd.
    6. If 35 loads of coal weigh 72 'T 3 , what is the price of 1 yard? load weigh?
    7. Divide $28^{\circ} 5 l^{\prime} 27.756^{\prime \prime}$ by 2.754 . Ans. 2T. 1cwot. 2qr. 6lb.
     persons. 32 9. When 96 shares of Ans. 39A. 3R. 18 per. 0yd. 6 ft. 64 in. what would be the cost of 1 share? 10. If a town 4 miles square be divided equally into 124 farms, how how much will each farm contain ? Ans. 82A. 2 R. $12 \frac{2}{3} \frac{1}{T}$ per.
    11. Divide 57T. 19crot. 42lb. $140 \%$. by 123.
    12. If a man walk round thíe earth in $2 y r .68 d a$. $19 h .54 \mathrm{mirr}$, how long would it take him to walk 1 degree, allowing $365 \frac{1}{4}$ days to a year?

    Ans. 2da. 5 h .17 min. 19 sec.
    13. Divide 916 mi . 3fur. 30rd. 10 ft. 6 in . by 47 .
    14. How many times are £5. 1010 contained in 25371010 ?

    Nores. whieh 001 is direotl reat of th noen.
    2. The and in on 1 minute honoe, in

    ## LONGITUDE AND TIME.

    246. Meridians of Longitude are direct lines on the globe, from the north pole to the south pole, crossing the equator at right angles.
    247. Longitude is distance on the globe, east or west of a determined meridian. In the British Isles and on this continent, also genorally on the ocean, the meridian of Greenwich Observatory, England is the determined meridian. All parts of the earth on this line are considered to have nó longitude.

    The highest longitude any place on the earth can have is $180^{\circ}$ east, or $180^{\circ}$ west from the determined meridian.
    248. The Tiquator and parallels of latitude being circles, are divided into $360^{\circ}$, called degrees of Longitude.

    Nores,-1. The earth revolves on its axis from west to eust onoe in 24 hours, which oonstitute a solar day. The middlo of this day is 12 noon. When tho sua is direotly over the meridian of a place, it is noon at that plaoe, and at places west of this moridian the time in before noon; at those east, the time is after
    2. The whole oirole of the earth $=360^{\circ}$ which pass nader the sun in 34 hours, and in one hour passes $\frac{1}{2}$ of $360^{\circ}=15^{\circ}$. One hour $=60$ minutes; hence, in 1 minute passes $\frac{1}{8^{\circ}}$ of $1^{\frac{1}{5}}=\frac{150}{\circ}=\frac{10}{\circ}=15^{\circ}$. One minute $=60$ seconds 1 COMPARISON OF LONGITUDE AND TIME,

    $$
    \begin{aligned}
    & 15^{\circ} \text { of longitude }=1 \text { hour of time. } \\
    & 15^{\prime} \text { of longitude }=1 \text { minute of time. } \\
    & 15^{\prime \prime} \text { of longitude }=1 \text { second of time. }
    \end{aligned}
    $$

    249. Rule.-I. The difference of longitude between two places, expressed in degrees, minutes, and seconds, divided by 15 will give their difference in time expressed in hours, minutes, and seconds.
    II. The difference of time in two places, expressed in hours, minutes, and scconds, mulliplied by 15 will give their difference in longitude expressed in degrees, minutes, and seconds.

    Notks.-1. If one place be in east, and the other in west lonyitude, the differonce of longitude is found by adding them; and, if the sum be greater than $180^{\circ}$,
    2. firese the ana appoars to muve from eact to west, when It is oxactly 12 Cotwesk at ons place, it will be pact 12 o'olook at all places east, and before 12 at all wisess wesh, Xence, if the difference of time betwoen two places, be subtracted frow the time at the easterly place, the result will be the time at the westerly leos; and, if the difference be added to the time at the vesterly place, the result What the time at the easterly place.

    ## EXAMPLES FOR PRACTIOE.

    1. Qneher is in longitude $71^{\circ} 16^{\prime}$ weat, and Toronto, $79^{\circ} 21^{\prime}$ west. When it is 12 o'olock at Toronto, what is the time at Quebec?

    $$
    \begin{aligned}
    & \text { OFRRATIO } . \\
    & 79^{\circ} 21^{\prime} \\
    & 71^{\circ} 16^{\prime} \\
    & \hline \mathrm{g}^{\circ} 5^{\prime} \\
    & \hline 0 \mathrm{ch} .32 \mathrm{mi} .20 \mathrm{sec} . \\
    & \frac{12}{12 \mathrm{~m} .32 \mathrm{mi} .20 \mathrm{sec}}
    \end{aligned}
    $$

    Axalysin.-The difference of longitude is $6^{6} 5^{\circ}$. Dividing by 15 and changing to time gives $32 \mathrm{min}$. . 20 seo. for the difference of time botwan the two places; and, as Quebeo is oant of Toronto, the time ls later, and we add the diference of time, which gives $12 h$. 32 mi . 20 cec . the time at $Q u$ uebeo.
    2. The longitude of Halifar is $63^{\circ} 35^{\prime} 30^{\prime \prime}$ west, and that of Ottawa 78 ${ }^{\circ}{ }^{\circ} 41^{\prime}$ west; when it is 10 o'clock 12 min . A. M. in Halifax, what lime in it at Ottawa?
    3. The longitude of Valparaiso is $71^{\circ} 37$ ' west, and the longitude of Rome is $20^{\circ} 30^{\prime}$ east; when it is $110^{\prime}$ clock 15 min . A. M. at Valpa. Fhiso, what is the time at Rome? Ans. 23 min . 28 sec . past 5 P. M.
    4. The longitude of New Orleans is $90^{\circ} 7^{\prime}$ west, of Philadelphia, $76^{\circ} 10^{\prime}$ west; what is the time at N. O. when it is 8 o 'cl. 20 min . 40rec, at Philadelphia?
    5. When it inc. An. 20 min .52 sec . it is at Bancor Benievt, Maine? 37 min .12 sec. P. M.; what is the longfude of B. The longitude of Jemalam in $35^{\circ} 32$, Ans. $68^{\circ} 47^{\prime}$ west.
     Mowtrew 730 $25^{\prime}$ west; when it is $10 o^{\prime} \mathrm{cl}$. A. M. at Jerusalem, what tine fow it at Montreal?
    7. The longizade of Boston is $71^{\circ}$ Ans. 2h. 44 min. 12 rec. A. M. delock 1. M. in Boston, it is 8 o'olock s3 west, and when it is 10 What is the longitude of Chicago? 8. The longitude of Constantinople is $28^{\circ} 48^{\prime}$ eans, and of Kingston, Cunals, $75^{\circ} 41^{\prime}$ west ; when it is $3 o^{\prime} \mathrm{cl}$. P. M. at the latter place, what time is it at the former?

    1. A captain at sea finils by his chronometer that it is 3 h . 40 min . 30ese. P, M., at Greenwich, when it is 1 h .10 min .45 sec . by solar time on bourd his veasel; in what longitude is the vessel?

    $$
    \text { Ans. } 37^{\circ} 26^{\prime} 15^{\prime \prime} \text { weat. }
    $$

    ## DUODECTMALS.

    250. Duodecimals are deneminate numbers, the denominations of which inorease according to the scale of 12 ; or denom-
    inate fractions, whose denominators are $1,12,144,1728$, ctc. In practice, duodecimals are applied to the measurement of extension, the foot being taken as the unit.

    ## TABLE.

     The marks ', ", "', "", are called indices.
    251. Duodecimals are added and subtrac cue in the same manner as compound numbers.

    ## MULTIPLICATION OF DUODECIMALS.

    Ex. How many square feet in a floor ' 9 ft. 7 ' long and $7 f t$. 9 ' wide ?
    Operation. Analisas,-Beginning at the right, $7^{\prime} \times 9^{\prime}=$ 9ft. 7'
    $\frac{7 f t .9^{\prime}}{7 f t .2^{\prime} 3^{\prime \prime}}$
    67 ft. 1'
    $74 f l .3^{\prime} 3^{\prime \prime}$ $63^{\prime \prime}=5^{\prime} 3^{\prime \prime}$; writing the $3^{\prime \prime}$ one place to the right, We reserve the $5^{\prime}$ ' to be addod to the noxt product. Then, $9 f t . \times 9^{\prime}+5^{\prime}=86^{\prime}=7 \mathrm{ft}$. $2^{\prime}$, which wo write in the places of feet and primes.' Next, multiplying by $7 f t$, , we have 7 ' $\times 7 f t .=49{ }^{\prime}$ are $4 f t$. 1 '; writing the ' 1 ' in the placo of primes, we rescive the $4 f t$. to be added to the next product. Then, $9 f t$. $\times 7 \mathrm{ft} .+4 f t .=67 \mathrm{ft}$., which we write in the place of feet. Adding the partial products, we have 74ft. $3^{\prime} 3^{\prime \prime}$ for the product required. Hence, the
    252. Rule.-I. Write the several terms of the multiplier under the corresponding terms of the multiplicand.
    II. Multiply each term of the multiplicand by each term of the multiplier separately, beginning with the lowest denomination in the multiplicand, and the highest in the multiplier, and worite the first figure of each partial product one place to the right of that of the preceding product, under its corresponding denomination, carrying 1 for every 12.
    III. Finally, add the several partial products; their sum will be the required answer.

    ## EXAMPLES FOR PRACTIOE.

    1. How many square feet in a piece of marble 12 ft . 7 ' long, and 4ft. 3 ' wide?
    2. What is the area of a floor, the length of which is $9 \mathrm{ft} .8^{\prime} \mathrm{li}^{\prime \prime}$, and width $3 f t$. 7 '?

    Ans. $34 f t$. $10^{\prime} 11^{\prime \prime} 5^{\prime \prime \prime}$.
    3. How many square feet in 10 boards, each $18 f t$. $10^{\prime}$ long and 1ff. $8^{\prime}$ wide?
    4. If a block of granite be 7ft. $6^{\prime}$ ' long, $3 f f .3^{\prime}$ wide, and $1 f t .10^{\circ}$ thick, what are the solid contents ? of land 80 ft . 10 in . long, and 60 ft . 8in. wide, with a inclose a piece 6in. high?
    6. What will the plastering of a room Ans. $2!22 f$ f. 6 '. yard, the length of which is $30 f$. 10 in cost, at 18 cents a squar of ceiling 8ft. $4^{\prime}$ ?

    ## DIVISION OF DUODEOIMALS.

    Ex. 'There are 8 ft. $5^{\prime} 3^{\prime \prime}$ in the surface of a marble slab, the lengt $h_{1}$ of which is $3 f t .9$; what is its width?

    ## OPERATION.

    3ft. 9' ) 8ft. 5' 3"' (2ft. 3', Ans.

    $$
    \begin{aligned}
    & \frac{7 \mathrm{ft} \cdot 6^{\prime}}{11^{\prime} 3^{\prime \prime}} \\
    & \frac{11^{\prime} 3^{\prime \prime}}{0}
    \end{aligned}
    $$

    ANALTELS, 3 fte is contained $i$ 。 $8 f t ., 2$ times. Multiplying the whole divisor by $2 f t$. gives $7 f t$. 6 ' for the produot, whioh we subtract from the corresponding denominations of the dividend, and obtain 11' for a remainder, to which wo annex the next denomination of the dividend, and have 11' 3 ". $3 f t$. is oontained in 11', 3 times. The divisor being maltiplied by this $3^{\prime}$ gives $11^{\prime} 3^{\prime \prime}$, which beiny subtrated fire divisor being multi-'
    leaves nothing. Therefore, tho marble slab was $2 f t$. $3^{\prime}$ in width.
    253. Rule.-I. Divide the highest term of the dividend, $1, /$ the highest term of the divisor; multiply the divisor by this term of the quotient, and subtract the product from the dividend.
    II. To the result bring down the next term of the dividend, and divide as before.

    ## EXAMPLES FOR PRACTIOE.

    1. Divide 184ft. 3' by 40ft. 11' 4'.
    2. Divide 41 ft. $8^{\prime} 7^{\prime \prime} 6^{\prime \prime \prime}$ by 7 ft. $4^{\prime}$.
    3. A table whose length is $6 f t .9^{\prime} 7^{\prime \prime}$, has ans. $5 f t .8^{\prime} 3^{\prime \prime} 2^{\prime \prime \prime}$ $11 " 2^{2 \prime \prime}$; what is its width ?
    4. What is the length of an alley whose ares is $792 f$ As. $4 f t$. 2 '. and width, $12 f$. $7^{\prime} 8^{\prime \prime}$ ?
    5. A block of marble containg $64 f$ t. $2^{\prime} 5^{\prime \prime}$; its Ans. $62 f t .8^{\prime} 6^{\prime \prime}$. its thickness 3 ff. $7^{\prime}$; what is its length? ${ }^{\prime}$; its width is $2 f .6^{\prime}$, and
    6. What is the width of a rectangular pond, whose leng. 7ft. $2^{\prime}$.
    
    7. A stick of timber is 3 ft .2 ' wide, 2 ft . 11 , Ans. $24 \mathrm{ft} .6^{\prime} 7^{\prime \prime}$ '. 135cu. ft. $10^{\prime} 2^{\prime \prime} l^{\prime \prime \prime}$. What is its length? 8. It required 8348q. $f t$. $3^{\prime}$ of board to cover building. The height was 17 board to cover the side of a certain building. The height was 17 ft . 9in.; what was the length of the
    aide Ane. 47 feet.
    t. 10 $3^{\prime \prime}$ - piece ce $7 f$. t. $6^{\prime}$ squar height 3.55.
    length،
    ned i , Whole for the om the of the a reenext , and in 11', multiinder,
    8. At ls. $6 \boldsymbol{6}$. sterling per yurd, how many yaris of linen may be bought for £5 66 ?
    9. Reduce 456575 grains to pounds, Apothecaries' Aus. 71 yd .
    10. If $22 \frac{3}{4}$ gallons of wine be bouth fir of each gallon?
    11. What is the value of 15 cut . Ans. £1 66.
    12. What wonld be the expense of making of tea, at 8950 per cwt.? 15rd., at $\$ 578.75$ per mile?
    13. What cost 7 hhd. 47 gal . of gin, at $\$ 87.25$ Ans. $\$ 50595.41_{64}^{14}$.
    14. Goliath was 63 cubits high ; what was her hogehead? cubit being lft. 7.168 in .? 8. Reduce 3cwt. lqr. 7lb. of hay to the deci Ans. IUf.. 4.592in.
    15. A farmer having 17 cut . $2 q \mathrm{r} .19 \mathrm{lb}$. of pori., , of a leng ton. of it, and the remainder he put into 6 barrels: barrel contain?
    16. Bought by A voirdupois weight $151 b$. $\therefore$ s. 'ccot. $1212 l b$. and sold the same by Apothecarght, at 25 ots. per dose; how much did I gain? (in doses of 10 gr . each, 11. How many solid feet in a stick of timbs. $\$ 2471.40$. 3in. wide, and lift. 6in. deep? stick of timber 34ft. 9in. long, ift.
    17. What is the value of a field 15 ch 75 l Ans. 65.1562 .5 ft . at $\$ 64$ per acre?
    18. What part of 4 gal . $3 q \mathrm{q}$. is $2 q t$. 1 pt . 2 gi .?

    Ans. $\$ 1260$. Ans. $\frac{1}{7}$.
    14. Thirty two men construct 28 mi . 4 fur . 32 rd . of road ; after com. pleting $\frac{1}{2}$ of it, $\frac{f}{}$ of the number of men left. What distance did each man construct before and after $\frac{1}{4}$ of the men left?

    Ans. 3 fur. $237 d$. before, and 4 fur. 302 rd . after. 15. If it require $3 h$. 20 min . for a man to cut 1 cord of wood, how many days of 8 hours each will be required to cut 746 cords, 96 feet?
    16. A housebreaker, having stolen property to the value . 10 min . was sentenced to pay at the rate of $£ 9129 \frac{3}{4}$ for every pound stolen. How much was the fine? Ans. $£ 921893 \frac{3}{4}+$. 17. Bought 4 barrels of cranberries, each containing $2 \frac{1}{2}$ bu. at $\$ 8$ per barrel, and retailed the same at $12 \frac{1}{2} \mathrm{cts}$. per quart, wine measure. How much was ny profit?
    18. Andrew received $\frac{1}{7}$ of a certann quantity or flour, Edward $\frac{1}{1} \mathrm{~T}$. of it, and Louis the remainder. Now it is found that Andrew ${ }^{2}$ of "6lb. and 8oz. more than Edward. How mich did each receiw has Ans. A received $210 \frac{3}{8} \mathrm{lb}$., E $133_{8}^{7} \mathrm{lb}$., and L $1128 \frac{3}{8} \mathrm{lb}$.
    19. A man having a hogshead of sirup, sold $I^{4}$, of it to F , $\frac{1}{8}$ of the remainder to $G$, and $\frac{1}{2}$ of the residue to J . How many gallons ro mained? Ans. 19 gal . 1 qt . 1 pt. $\mathrm{I}^{4} \mathrm{gi}$. weight.
    21. How much butter, at $18 \frac{3}{4}$ Ans. 16lb. 50z. 10pwot. 11.7 + gr. 22. The wall ofse, at a gallon ? and 14 feet in thickness; how many perches of masonry are there?
    23. The total yield of nine copper mines in 1868, was 39427,12 mat. lqr. llb.; in 1869, the same mines yielded 4101 T. 8ewt. 3 Zq , sblh, if copper was worth 20 cts . per lb ., of how much greater value was the amount produced in 1869, than 1868?

    Ans. $\$ 6.3530,1(1)$.
    24. Sold 15 cwt . 22l6. of rice at $\$ 3.75 \mathrm{a}$ cwt., and 7 crot . $36 / \mathrm{lh}$, of pearl barley, at $\$ 4.25$ a cwt. How much would be gained ly selling the whole at $4 \frac{1}{2}$ cts. a pound?
    25. Bought a lot 25 rods long and 20 rods wide for $\$ 10000$, and solk the same at 25 cts. per square foot. How much was my gain?
    26. Sold 72 yds. carpeting at $\$ 1.37 \frac{1}{2}$ a yd., and gained ${ }^{3} 18$, How much did it cost me per yaril?

    Ans, $\$ 1.124$
    27. How many square yards in the walls of a room 40 feet lowg, $31 \frac{1}{2}$ feet wide and 12 feet high ?
    28. How many tons of hay, at $\$ 0.75$ per cwt., must be given (or 35 cords of wood, at $\$ 0.60$ per cord foot?

    Ans. 11 toms.
    29. Purchased a farm, containing 176A. 3 R. 25 rd ., at $\$ 75.371 \% \times$ acre; what did it cost?

    Ans. \$13334.308 ${ }^{+}$.
    30. What will be the expense of plastering a room $40 f$. long, $38,8 f t$, wide, and $22 \frac{1}{4} f t$. high, at 18 cents a sq. yd., allowing 1375 sq . ft. for doors, windows, and base board? Ans. $\$ 69.784$
    31. When it is 11 A . M. at a place $30^{\circ}$ east of Greenwich, it is 3h. 44 min .20 sec . A. M. at Buffalo, United States; what is the low gitude of Buffalo ?
    32. Nineteen lots of equal size contain 159A. AR. $\mathbf{2 R}$. $77 \mathrm{sq}, \mathrm{rd}$, 2Geq, $y d .8 s q . f t$. $130 s q$. in. What is the value of one lot, the land being worth 50 cts. per square foot?
    33. Sold 4 building lots of ground; the first contained $\frac{1}{2}$ of 2 of 8 on acre; the second, $40 \frac{2}{3}$ rods; the third, $\frac{1}{7}$ of an acre ; and the fourthy s of 8 of an acre. How much land in the four lots? Ans. $3 \boldsymbol{R}$. 75per.
    34. How much beef, at 7d. per pound, ought I to receive tor $27 / 6$.

    12oz. of butter at ls. 9 d . per lb. ?
    Ans, 832 16.
    35. The difference in longitude between London and St. Cotion, Mo., is $90^{\circ} 20^{\prime}$; at a certain time each day it is as much noon in London as it lacks of noon in St. Louis. What is the time in St. Louis?
    36. Express in acres and the decimal of an acre the area of 49 square lots, each measuring 5 rd .8 ft . 3in. on a side.
    37. On an acre of ground there were erected 21 buildings occupying on an average $3 s q$. rd. $1128 q$. ft. ssq. in. How much of the sere remained unoccupied ?
    
    39.4 .
    39. A person lived in Montreal until he was l8yr. 8 mo . 24 da , old.
    in Toronto, $\frac{1}{8}$ as long; in Kingston, $\frac{2}{3}$ as long as in Toronto, and $\frac{1}{2}$ as low in Quebec as in Kingston. What was his age ? A. 31yr. 2mo. 20da.
    40. A farmer owning 195A. 3l. 38sq. rd. of land, divided of of it equally among his four sons. How much did each son receive, and how much had the father remaining?
    Ans. 36A. 2 R. $39 \frac{5}{8} s q . r d$. asch, and 48A. 3 R. $39 \frac{1}{2} s q$. rd. reinaining 41. A steamer, going firom Halifax to Liverpool, traversed 103 degreea of longitude daily. What length of time was it from one noon to the mext?

    Ame. 23 h .18 min .
    42. What cost 0.01975 of a ton of steel at 20 cents per pound ?
    43. A man having a feld 30 ro is square, sold 25 square rods to une of' inis neighbors, and 20 rods square to another. What is the value of the remainder at 8175 per acre? Ans. $5519.53 \frac{1}{3}$.
    44. A mar paid $\$ 16.50$ for a certain pile of wood. Measuring it he found that it contained $5 c d .6 c d . f t$. 12cu. ft. What did the wood cost him per sord?
    45. A grocer lost from $\frac{7}{8}$ of a hogshead of molases, $\$ 7.957+$ of a callon and $\frac{5}{6}$ of a quart. How much of the hogshead, expreseed decinn:ily, leaked out, and how much remained?

    Ans. $1.008 \frac{1}{3}$ gul. leaked out, and $54.11 \frac{2}{3}$ gal. remained. 46. From a piece or cioth containing 92 yards, scoats, eacin containing 3 y!. were taken; required the valne of the remainder at $\$ 5.32 \frac{1}{2}$ a yard? 47. If a gallon of distilled water weigh $8 i b$. $50 z, 6.74 d r$., what is the weight of 17 gal . 3qt. 1pt. 1gi.? Ans. 149lb. 5oz. 1.19dr.
    48. At $3 \frac{1}{2}$ cents per foot, what will be the cost of 12 planks, each ineasuring 56ft. 9'? Ans. \$23.83 $\frac{1}{2}$.
    49. If, when wheat is worth 6s. 3d. per bushel, a 5 -cent loaf welghs $240 z$., and allows the baker $1 \frac{1}{2}$ cts. a loaf for his labor, what shoula it weigh when wheat is $88.4 d$. per bushel, to aftord bim the same profit on a loaf?

    Ans. 1802.
    50. How much will it cost to carpet a roum 21 ft . long, 15 ft . wide, with carpeting $\frac{3}{4}$ of yd . wide, at $\$ 1.62 \frac{1}{2}$ per yd . ?
    51. What is the value of a pile of wood that is $10 r d$. long, $4 f$. wide, and $1 \frac{1}{2} y d$. high, at $\$ 5.75$ per cord ? Ans. $\$ 133.42-$
    52. My garden. which is 180 ft . long, and 150 ft . wide, is surrounded by a tight-board tence $5 \frac{1}{3} f t$. high. How much will it cost to paint the fence on buth sides at 12 cts. per sq. $y \mathrm{~d}$. ? Ans. \$93.862
    53. A merchant purchased in Manchester 34 bales of cloth for £8 19.5 per trale; he dicposed of the cloth at Porto-Rico for 212 czot . of sugar, at $£ 15$ per cwt. Did he lose or gain 9 and how much?
    ; 54. If a person spends in 6 monthis what be earns in $4 \frac{1}{2}$ months; how many dollars can he lay by in a year, supposing he earns $\$ 325$ in $2 \frac{1}{2}$ months?

    Ans. $\$ 390$.
    jos. A man has a piece of land $201 \frac{2}{2}$ rods long and $41 \frac{1}{4}$ rods wide, which he wishes to lay out into square lots of the greatest possible size. How many lote will there be ?

    Ans. 396.
    56. If a man can pay his creditors only 48 cents on a dollar, how much can he pay on a dett of $\$ 52.50$ ?
    57. How many bricks, 3in. long, 4in. wide, and 21 in. thick, are required to build the front of a house whose wall is $30 f t$. long, $24 f$. high, and $2 f$. thick, allowing the doors and windows to occupy 1 the aırfuce? 4.232 ?Q hmin'za 08. If I buy 145 gal. 2 gt. of molansem, at 20 ots. a gal., ead s5 gal. of it, how must I mell the remaunder per gal., so as to reoeive as much as the whole cost 1
    59. If I bny 120 gallons of rum for $\$ 75$, how much water must be added to it that I may sell it at 60 cents per gallon, and gain $\$ 15$ in the sale of it !
    60. Sold 125 equal loads of wood, measuring $115 \mathrm{Cd} .3 \mathrm{~cd} . f t$. 7cu.ft. for 8492.50. What is the quantity per load, and price per eord?

    Ans. $118 \frac{1}{5} \mathrm{cu}$. ft. each load, $\$ 4.26 \frac{2}{3}$ per cord.
    61. How many francs must a merchant in Paris send io Montreal in payment for a debt of $\$ 15989.862$ ?

    62 . If a man fill $\frac{1}{2}$ of a cask with brandy, $\frac{1}{4}$ with wine, and $\frac{1}{5}$ with water. and if it lack $21 \frac{2}{3}$ gallons of being full, how many gallons will that cask contain?

    Ans. 100 gal .
    63. If oy eelling cloth at $10 s .6 d$., $\frac{1}{8}$ of the price is gain, what part of the cost would be gained by eelling it at l3s.?
    64. A ship's chronometer, set at Greenwich, points to $5 h .45 \mathrm{~min}$. 24sec. P. M., when the sun is on the meridian. What is the ship's longitude?
    65. A grocer bought 15 barrels of salt, of 4 bushels each, at $\$ 1 \frac{2}{5}$ a barrel, and retailed it at a of a cent a pint. How much was his whole gain?

    Ans. \$4.60.
    66. James owns $\frac{8}{8}$ of a field, and Leo the remainder; $\frac{8}{4}$ of the difference between their shares is 5A. 3R. $16 \frac{1}{2} p e r$. What is Leo's share?
    67. A gentlenıan desirous of giving ls. 6d. apiece to some needy boys, found that he had not money enough in, his pocket by $5 d$. ; he therefore gave them 1s. $4 d$., and bad $9 d$. left. Required the number of boys.

    Ans. 7.
    68. A liquor agent has 50 gallons of wine of superior quality, worth $\$ 7.50$ a gallon; he wishes to reduce its quality by the addition of water, so that he may sell it at $\$ 5.25$ a gallon. How much water must he add ?
    69. A clothier has 960 soldiers' coats to make, each coat containing $2 \frac{1}{4} y d$. of cloth $1_{8}^{5} y d$. wide, and lined with drilling ${ }_{4}^{3} y d$. wide. How many yards of lining will be required?
    70. A ship captain, sailing from London to Portland, found, on taking an observation, that the sun at noon was $3 h$. 25 min . 40 sec . arlierthan the London time, as shown by his chronometer. How many degrees west had he sailed?
    71. My father's garden is $10 \frac{3}{4}$ rods long, and 82 rods wide, and surrounded by a fence $7 \frac{2}{5}$ feet high; he has laid out a walk around it, within the fence, $7 \frac{1}{2}$ feet wide on the two sides, and $5 \frac{1}{2}$ feet wide on the ends. How much remains for cultivation? Ans. 2l296sq. ft.
    72. A boy having been sent to a store with $5 \frac{1}{2}$ doz. of egge, was directed to purchase with them equal quantities of eugar, coffee, butter and tea; he disposed of his egigs at the rate of 2 for 5 cente, and paid for the articles purchased 17, 28, $37 \frac{1}{2}$ and $137 \frac{1}{2}$ cents per pound, respectively. What amount of each did he purchase?

    1. ft. 7cu.ft. reord ? per cord. to Montreal and $\frac{1}{5}$ with calions will P. 100 gal . , what part
    $5 h .45 \mathrm{~min}$. the ship's © $2 l^{\prime}$ E. :h, at $\$ 1 \frac{2}{5}$ a th his whole is. \$4.60. ; $\frac{3}{3}$ of the at is Leo's 2. 97per. ome needy by $5 d$. ; he e number Ans. 7. lity, worth addition of uch water $21 \frac{3}{7} \mathrm{gal}$. at containwide. How
    found, on in. 40 sec .
    ter. How e, and suraround it, ide on the $6 s q . f t$. eggs, was rr, coffee, 5 cents, cents per ?

    ## RATIO.

    254. Ratio is that relation between two numbers or quantities, which is expressed by the quotient arising from the division of the one by the other. Thus, the ratio of 12 to 4 is $12 \div 4=3$.
    255. The Terms of a ratio are the two numbers compared.
    256. A Couplet is the two terms of a ratio taken together.
    257. The Antecedent is the first term, or dividend.
    258. The Consequent is the second term, or divisor.
    259. A ratio may be expressed either by two dots (:) between the terms; or in the form of a fraction, by making the antecedent the numerator and the consequent the denominator. Thus, the ratio of 8 to 4 , may be expressed as $8: 4,0$ as ${ }^{3}$.
    260. A ratio is either direct or inverse.
    261. A Direct Ratio is the quotient of the antecedent by the consequent. Thus, 8 to 4 is $\frac{8}{4}$ or 2.
    262. An Inverse, or Reciprocal Ratio, is the quotient of . the consequent by the antecedent. Thus, 8 to 4 is $\frac{6}{8}$ or $\frac{1}{2}$.
    263. A Simple Ratio is that having but one cutrcedent and one consequent; it may be either direct or inverse. Thus, $6: 3$, or $\frac{1}{8}: \frac{1}{8}$.
    264. A Compound Ratio is the product of two or more ratios. Thus, the ratio compounded of $6: 3$ and $8: 4$ is $\frac{0}{3} \times \frac{8}{4}$ $=\frac{13}{2}=4$, or $6 \times 8: 3 \times 4=4$.
    265. From the foregoing we deduce the following principles of ratio.

    1st. Multiplying the consequent divides the ratio; diniding the consequent multiplies the ratio.
    2nd. Multiplying the antecedent multiplies the ratio; dividing the antecedent divides the ratio.

    3rd. Multiplying or dividing both antecedent aud coms quent by the same number does not ilter the ratio.

    GXAMPLEG HOR PRACTIOE.
    What is the direst ratio of

    1. 54 to 6 ?
    2. 108 to 18 ?
    Ans. 9.
    3. 13 to 52 ?
    4. 53 to 212?
    dns. $\frac{1}{3}$.
    5. 72yd. to $9 y d$. ?
    6. 7 to 21 ?
    7. 60 mi . to 4 fur. ?
    Ans. $\frac{1}{6}$.
    8. 17 to 68 ?
    9. 60 mi . to 4 fur.?
    10. 3 qt. to 20 grod.?
    Ans. 120.
    11. co to 12 ?

    Required the inverse ratio of

    | 11. 27 to 81. |  |
    | :--- | :--- | :--- |
    | 12. 72 to 8. |  |
    | $13 . ~$ | 16 to 48. |$\quad$ Ans. 3. | 14. 42 to 6. |
    | :--- |
    | 15. 02 to 2.503. |$\quad$ Ans. 1.

    17. Which is the greater, the ratio of 86 to 240 , or of 45 to 72 ?
    18. What is the ratio compounded of 35 to 40,60 to 75 , and 21 to 19 ? Ans. 148.
    19. If the consequent be 32 and the ratio $4 \frac{4}{7}$, what is the antecedent?
    20. If the antecedent be 71 and the ratio $\frac{5}{8}$, what is the consoquent?

    Ans. 12.

    ## PROPORTION.

    266. Proportion is the equality of ratios. It is indicated thus, $6: 3:: 8: 4$; or thus, $6: 3==8: 4$, and is read 6 is to 3 as 8 is to 4 ; or the rutio of 6 to $3=$ the ratio of 8 to 4 . Hence every proportion has two couplets and four terms.

    2fity. The Ext-omes are the first and fourth terms.
    268 . The Means are the second and third terms.
    265. Since in a proportion, the ratio of the first to the second term is equal to the ratio of the third to the fourth term, the proportion, $6: 3:: 8: 4$, becomes $\frac{8}{8}=\frac{8}{4}$, nultiplying each member by 3 and 4 , we have $6 \times 4=8 \times 3$. Hence,

    In every proportion, the product of the means is equal to the product of the exiremes.
    270. From the foregoing principles and illustrations, it follows that, any three terms of a proportion being given, the fourth may readily be found by the following
    281. Rule.-I. Divide the product of the extremes by one of the means, and the quotient will be the other mean. Or,
    II. Divide the product of the means by one of the extremes, and the quotient will be the other extreme.
    Notk.-We will denote the required term of a proportion by the letter $\boldsymbol{x}$.
    EXAMPLES FOR PRACTICE.

    1. Find the value of $x$ in the proportion,

    $$
    9: 16:: 36: x ; x=\frac{16 \times 36}{9}=64, \text { Ana. }
    $$

    What is the value of $x$ in each of the following proportions:

    1. $24 \quad 96:: 14: x$ ?
    Ans. 56.
    2. $x$ : $15:: 3: 9$ ?
    Ans. 5.
    3. $7: 42:: x: 96$ ?
    4. $16: x:: 10: 40$ ?
    5. $42: 70:: 3: x$ ?
    Ans. 16.
    6. $\$ 7 \frac{1}{2} \$ 10$ :: 36bu. : xbu.?
    7. $2 y d .: 8 y d .:: \$ 3 \frac{1}{2}: x$ ?
    8. 7.50 : $18::$ ox. : $7 \frac{1}{\text { h }}$ oz.?

    If 49 times 28 1372 da

    ## 278

    name 0 third teII. term, at third te:
    for the

    ## SIMPLE PROPOR'TION.

    272. Simple Proportion is an equality of two simple ratios, and consists of four terms.

    Notr.-Simplo Proportion is often called the Rule of Three, from the circumstance that threo torms being given to find a fourth.
    E.x. 1. If 12 yards of cloth cost $\$ 30$, what will 42 yards cost at the same rate?

    OPERATION.
    yd. Jd. \$ $\$$
    $12: 42:: 30: x$
    42
    60
    12) $\frac{120}{1260}$
    $s=\overline{\$ 105}$, Ans.

    Elucidation. - To arrange the given numbers in the order of a proportion, or state the question, we make $\$ 30$ the third term, beeause it is of the same kind as tho required fowrth term; and, as from the nature of the question the latter must be groater than the third term, we make the greater of the other two numbers the second term, and tho less the firat; and then, the product of the meo::3 divided by the fi: exen extreme, gives th: $\mathrm{K}_{4}$ uired extrome.

    ## THE SAME EXAMPLE BY ANALYGIS.

    If 12 yd . cost $\$ 30,1$ yard will cost $\frac{1}{12}$ of $\$ 30=\$ 2.50$; then, if 1 yd . cost $\$ 2.50$, $42 y$. will cost 42 times $\$ 2.50=\$ 105$, the answer, a before.
    E.x. 2. If 49 soldiers consume a certain quantity of flour in 28 days, how long will it take 70 soldiers to consume it?

    Boldiert OPERATIOM.
    

    ## THE SAME EXAMPLE ET ANALTEIG.

    If 49 soldiers consume the flour in 28 days, it will take 1 gol.iar 4. times 28 days $=1372$ days; then, if 1 soldier consume the flour in 1372 days, 70 soldiers will consume it in $\frac{1}{75}$ of 1372 days $=19 \frac{3}{5}$ days.


    #### Abstract

    278. Rule.-I. Frito the given number that is of the same name or kind as the required fourth tern, or anower, for the third term of the proportion: II. Of the other tioo numbers, write the larger for the seoond term, and the less for the first, when the unswer shonld exceed the third term; but write the less for the second term, and the larges for the first, whon the anowor showld be lose than the thind town.


    III. Multiply the second and third terms together, and divide their product by the first; or divide the third term by the ratio w/ the first term to the second.

    Nutes.-1. When the first and second terms are of different denominations, thoy must be reduced to the same donomination; and when the thirl term is compuond sumbor, it must be roduced to the lowest denominations mentioned in it. The answer will be of the same denomination as the third term.
    2. I'he pupil should perform these questions by analysis, ass well as by $\mathrm{z}^{\mathrm{nco}}$ portion, and introduee oancellation when it will rbbreviate cho uparation.

    ## EXAMPLES FOR PRACTIOE.

    1. Six laborers earn $\$ 7.68$; how much will 10 laborers earn? 35 labórers?
    2. If 23yd. of clots cost $£ 2533$; how much will $198 y$ d. cost?
    
    3. One-half a bushei of eris costs tol cts.; how much will 16 bushels cost ? 34 bushele? 72 buehels " $86 \frac{1}{2}$ bushels? $90 \frac{3}{4}$ bushels? $105 \frac{1}{6}$ bushels?

    Ane. $\$ 14.56 ; \$ 30.94 ; \$ 65.52$; ctc.
    4. 126lb. of butter cosi $\$ 16.38$; how many 1 lb . can be had for \$12.61? \$25.74? \$32.57? \$36.40? Ans. 97 lb ? ; 198lb.; etc.
    o. If a cwt. of tubacco is worth $\$ 39.25$; what is the value of [lb? $7 \frac{1}{2} \mathrm{cwt}$. ? 56 lb . ? 93 lb .4 zz.$\left.\right\} 107 \frac{3}{4} \mathrm{lb}$. ? Ans. $\$ 0.3925$; $\$ 294.37 \frac{1}{2}$; etc.
    6. The $\frac{3}{4}$ of 2 civt. of sirger cost $\$ 6.48$; what will be the cost of $\frac{7}{8}$ of a cwt. ? $\frac{5}{6}$ cwt. ? $\frac{5}{8} \mathrm{cwt}$. ? 番 cwt. ? Ans. $\$ 6.72 ; \$ 7.20$; etc. +
    7. If $40 \frac{1}{2}$ arpents of land are worth $\$ 215.50$; what is the value of ti arpents ? 70 nerchem ? 90 toises? $25 \frac{1}{2}$ arpents? 10 per. 4 to. it ft. ? $110 \frac{1}{2}$ arpents " Ans. $\$ 31.92 \frac{10}{2}$; $\$ 3.72 \frac{38}{8}$; $\$ 0.53 \frac{1}{87}$; etc.
    8. The $\mathrm{I}^{4}$ of an acre produce 18 cwt . 1 qr. $12{ }^{8} \mathrm{lb}$. of hay; what quantity will 1 acre produce? $8 \frac{1}{2}$ acres? $36 \frac{1}{2}$ per $?$
    9. At ls. 8d. per lb., what quantity of coffee can be had for $£ 36 \mathrm{~s}$.? £9 156 ? £ $4172 \frac{1}{2}$ ? £14 $010 \frac{3}{2}$ ? Ans. $39 \frac{3}{5} \mathrm{lb}$; $117 \frac{3}{1} \mathrm{lb}$; etc.
    10. If 19 gallone of oil cost $\$ 36.67$, how much will 37 gal . cost?
    
    11. I paid $\$ 78.80$ for 11 tons of coal; how much must I pay for 16 tons? 3 . tons? 184 tons? Ans. $\$ 107.45{ }^{5}{ }^{5} ; \$ 24.67+$; etc.
    12. If 3 glb. of coffee cost 72 cts., how much must be paid for $74 \frac{1}{2} \mathrm{lb} . ? 96 \frac{1}{2} \mathrm{lb}$ ? $109 \frac{1}{2 l b}$ ? 2 kcwt ? Ans. $\$ 14.62+$; $\$ 18.90$; etc.
    13. Six cwt. l qr. lib. of beef cost $£ 1376$, what quantity can be had torf8 123 ? £1 08 ? £17 126 ?
    14. For 172 days' work, $\$ 25.44$ were paid; how much will be paid for 1 day's ? 45 $\frac{1}{2}$ days' ? 891 days'? Ans. $\$ 1.44$; $\$ 65.52$; etc.
    15. The rent of a farm containing 12A. 2R. 30per. is $\$ 113.75$; what is the rent of another containing 5A. 1R. ? $16 \frac{1}{5}$ A.? 59 A . 2 R . 20per. ? 105 A . ?
    16. Seven bughels of rice cost $\begin{gathered}88.75 \\ \text {; }\end{gathered}$ how much will $12 \frac{1}{2}$ bustru. cost ? 18 IT bushels ? 263 bushel\%?
    17. In paying $\$ 11$ for 1428 of boarda, what quantity $\therefore$ whe
    
    18. I can get 336 pens for 3a. Gd. ; bow many can I get fir its 4 f £3 10 119 50 101? which the breadth is $2 \frac{1}{2}$ inches?
    31. A manufacture having failed owes $\$ 900$ Ans. $57 \frac{8}{5}$ inches. to D, and $\$ 1500$ to E. The value of hises $\$ 900$ to B. $\$ 1209$ to $\mathrm{C}, \$ 1400$ will each creditor receive? Anue of his property is $\$ 2800:$ how much
     M ft ? 450 ft . of split wood, at $£ 45 \mathrm{~s}$. per 33. If a bowl containing 2 cubic yd. is emptied in Ans. £1 18 3. : many hours will be required to empty a cistern 4 gd 12 minutes; how asd $2 \frac{1}{2} y$ d. deep? 34. One of two pieces of cloth costs 8335 , Ans. 3 hours. the length of each, knowing that the second is 11 yd. $\$ 390$; what is first?
    35. How long will it take to pump 54 barrels of 67 yd .; 2nd. 78 yd . can be pumped in 1 h .45 min . pump 54 barrels of water, if 24 barrels
    36. A workman received $\$ 26$
    he have received by working 14 days more? labor; how much would 7. What is the value of $3^{3}$, of $a$ boat, knowing Ans. $\$ 348$. f51?
    38. If the moon moves $13^{\circ} 10^{\prime} 35^{\prime \prime}$ in Ans. $£ 1018^{\prime 6} 6 \frac{9}{7}$.
    it perform its revolution? $13^{\circ} 10^{\prime} 35^{\prime \prime}$ in one day, in what time will 39. I bought 4950 copies on condition that $27 \mathrm{da} .7 \mathrm{~h} .43+\mathrm{min}$. cent more; how many shall I receive? 40. What is the value of 71b. lloz. of gold, knowing Ans. 5247 . worth $\$ 120$ ? 41. The $\hat{5}$ of a bushel of prunes cont $\$ 1$ ? what Ans. $\$ 1628.57$ \%. be bought for $\$ \frac{7}{25}$ :
    42. In retailing merchandiee for the sum of $\$ 5600$, I lost $\$ 4.50$ on every $\$ 100$; how muchi did I disturse?
    43. A pound of cinnamon costa $\$ 1.10$; for how much whonld I retail it to gain at the rate of $\$ 50$ on every $\$ 1000$ ? Ans. $\$ 1.15$ d.
    44. When metallic pens are $6 \frac{1}{4}$ cts. a dozen, how much will 10 gross cost? $16 \frac{1}{6}$ gross? $25 \frac{2}{2}$ gross? Ans. $88.06 \frac{1}{4}$; etc.
    45. When profits are $\$ 50$ on every 100 yards of cluth, how many yards must be sold to raise a profit of $\$ 850$ ? Ans. 1700 yd .
    46. What will be the price of 7 chests of tea, each containing $2 \frac{3}{4} \mathrm{cwt}$.,
    51 l . cost $£ 810 \mathrm{~s}$.
    47. One of two numbers is to the other as $5: 7 \frac{1}{2}$, and the smaller is 164.5; what is the greater?
    48. Two pieces of cloth are respectively 41 and 36 yards; the first piece costs $\$ 45$ more than the second; required the price of each.

    Ans. 18t. $\$ 369 ; 2$ nd. $\$ 324$.
    49. When wheat is sold at 7 s . 6 d . the bushel, a loaf of bread weighs 9 ounces; what should be the weight if wheat is but 6 s . the bushel?
    50. Every soldier in a regiment of 1000 men is to have a watchmat ; each coat will take 3 yyd. of cloth which is 17 yd . wide, and is 0 be lined with flannel, 1 lyd. wide; how many yards of flannel will se required to line the whole?
    51. To draw success on my business, I propose to give $\$ 5$ io the poor every time I gain $\$ 150$; how much will I have gained when my alma amount to $\$ 100$ ?
    62. John can plough a certain field in 5 days, and Mas. $\$ 3000$. 6 days; what time will both take, working together, to plough the field?
    53. A father earns 6s. 5d. per day, his son, 3s. $7 \frac{\text { Ans. }}{2}{ }^{2}{ }^{2} \frac{8}{11}$; in days. will they have economised £1 10 3, if they expend but 5s. per day?
    64. How much must I pay for paving a yard which Ans. 6 days. and 44 ft . wide, if 1425 sq . ft . cost $\$ 34 \frac{1}{5}$ ? ? yard which is 605 ft . long 55. Two gangs composed of 20 and 30 vards of a certain worls in 25 des and 30 men respectively, did 1500 had their number been aug nent how much would they have done 56. One hundred degreg nented by 15 ? Ans. 1950 yards. 56. One hundred degreet of Centigrade are equivalent to 80 degrees of Reaumur ; to how nany degrees of Reaumur will 232 degrees of Centigrade equal? Ans. $18 \frac{14^{\circ}}{}{ }^{\circ}$ of Reaumur.

    ## COMPOUND PROPORTION.

    284. Compound Proportion is an expression of equality vetween a compound and a simple ratio, or between two compound ration. Thus,

    $$
    \left.\begin{array}{r}
    12: 6 \\
    8: 4
    \end{array}\right\}:: 24: 6 \text {, is a compound proportion. }
    $$

    What in, $12 \times 8: 6 \times 4: 24: 6$; for, $12 \times 8 \times 6=6 \times 4 \times 24$

    Norn.-Componnd proportion ambrases that olane of questiens whone solution oriled Double Rule of rithe statementa in Simple proportion. It le sometimes

    E'x. If 6 men can earn $\$ 72$ in 10 days, by working 8 hours a day, how many dollars can 9 men earn in 5 days, by working 12 hours a day ?

    STATEMENT.

    |  |  |  |  |  |
    | :---: | :---: | :---: | :---: | :---: |
    | Mon. | $\$$. | Da. | Hr. |  |
    | 6 | 72 | 10 | 8 |  |
    | 9 | $x$ | 5 | 12 |  |

    Notw. -To aid in remembering the question and in forming the ratios, the pupil should write the conditions upon hir alate, or blackboard, as in the margin.

    ## MEXHOD BY PROPORTION.

    > OPERATION I.
    > operation in.

    If 6 men in 10 days of 8 hours each earn $\$ 72,1$ man in the same time will earn $\frac{1}{6}$ of $\$ 72=\$ 12$; and 9 men will earn $9 \times \$ 12=\$ 108$ If in 10 days of 8 hours each, 9 men earn $\$ 108$, in 1 day they will earn $\frac{1}{10}$ of $\$ 108=\$ 10.80$; and in 5 daye, $5 \times \$ 10.80=\$ 54$. If in 5 days by working 8 hours a day, 9 men earn $\$ 54$, by working 1 hour a day, they will earn it of $\$ 54=\$ 6.75$; and, by working 12 hours a day, they will earn $12 \times \$ 6.75=\$ 81$.
    275. RuLE-I. Make thut number which is of the same kind as the answer required, the third term of a proportion.
    II. Then take the other numbers in pairs, or two of a kind, and arrange them as in simple proportion.
    III. Finally, multiply the product of the second terms by the third, and divide the result by the product of the firat torme. The quotient will be the fourth term, or answer.
    NOTm-By reforonce to the shove atatoment, of the queation, cither mochod of celation is 80 plain as to mequirs no prole.

    ## MAMPLES FOR PRACTIOE

    1. Twelve hormes can plough 11 mares of land in 5 days; how many horses will it require to plough 33 acres in 18 days ? Ans. 10.
    2. If $\$ 900$ produce $\$ 50$ in 9 monthe, what sum will $\$ 450$ produce in 5 months?
     an average power of 2250 pouncis ; how murses, each drawing with proportion for 25 dayg work of 5 hores much should be received in 2430 pounds?
    3. By selling 75 otter sking ming. $\$ 27$. profit of $\$ 24$; how much would I heve me $\$ 3.60$ each, I made a Firginia silvered much wou I have gained in proportion on 45
    
    4. If 144 men, in 6 days, of 12 hours each, build a wall 200t. long, 3 high, and 2 n . thick ; in how men brild another wall 350 ff . Ien', 1rith and 3 ft . thick?
    5. If it require 45 tailors to makn SJJ ctats in 36 days, how many will be required to muke 200 in 27 days? Aus. 40 . 7. If 18 men in 24 days, by working 12 hours a day can make 240 olneks; how many men, in 9 days, by working 10 hours a day ean make 450 locks?

    $$
    \text { \%. If } 6 \text { horses eat } 70 \text { bushels of oats in } 9 \text { days, }
    $$

    fod with 280 bushels in 27 days?
    9. In ho many days will 6 p

    Ythe. 3 pk suffice for 9 persons duns consume in bush. of potatoes
    10. If 15000 lb of fersons (muring 22 days? Ans. 44 days.

    80 days in s citad four are sufficient to maintain 1500 men during
    that it may laet 2450 by how much should this quantity be increased
    11. Dofing 18 demen for 232 daya? Ans. 56050 lb .
    piece of aring 8 deya, of 8 hr . each, 14 laborers were employed at a
    pece or work $136 y$ y. long and $9 y d$. high ; how many yards will 36
    mborers do, working 7 hr . per day, during 14 days? Ans. 238 yd .
    12. How many planks 10 att. long and 13 inches thick, will be necmary wreplace 3000 planks, 12 ft . 8 in . long and $2 \frac{3}{3} \mathrm{jin}$. thick?
    18. The of a wall was constructed by 15 masons in 12 days, after which 7 lent; how long did it take the others to finish the work?
    14. To perform a piece of wurk, $46 \frac{1}{4} \mathrm{yd}$. long, 11 labarers were obliged to work 103 hours a day; how many men would it require to do $411_{8}^{8} \mathrm{yd}$. of the same labor, working $8 \frac{4}{5}$ hr. per day? Ans. 12 men.
    15. Paid \$12 for the painting of 5 doors, each measuring 8 ft . in weight by 3 ft . 6 in . in breadth; how much should be paid for the pairting of 7 windowe, each 9 ft . high by 4 ft . wide, reckoning 2 doors u* 8 windows?
    16. If 300 bushels of wheat at $6 \mathrm{~s}, 3 \mathrm{~d}$, Ans. 814.40 . ww many bushels at 4 a .6 d will io ., liquidate a certain debt, lawner $?$
    17. If the carriage of 5 cwt . 3qr. a ditan Aus. 1250 busisels. What mant we pay for the carriage istance of 150 mi es costs $\$ 24.58$, at the same rate?
    1\%, In a fort there are pronisi Aus. $\$ 14.135+$. showths. If the garrison be augns eaough for 1520 soldiers for 5 ean blowed them if tey remain $1_{h}^{\prime \prime}$ mo. longer? what daily ration 19. If 4 z. is inm, if they the bwashel: what ahould a 10, 2d loaf welsh whell wheat is 4s. 2 d . the bwhel?
     sallereld I place at interest to give me $\$ 200$ in
    2i. Juring how many ave A. $\$ 2500$. 2e much work how many uayo, of 8 . each, mu y m work, to do 22. A piece of cloth $30 y$ din 28 days, of 10 hr . c. h? Ans. 5 da. 25 the of three of cloth 30 yd . long, $8_{5}$ of a yard wide, was woven with 28 lbe of thres; what will be the length of a piece of a yard wide, dixs. $39_{1}^{7} \mathrm{~g}$ yards.

    200f. long, ch, will 30

    ## PFRCENTAGE.

    276. Per Cent., or Rato per Cent., also writuer io, atgnifies by the hundred. Thus, $6 \%$ means 6 of every hundred, and may signify 6 cents of every 100 cents, 6 dollars of every 100 dollars, etc.
    277. The Base is the number on which the pereentage is computed.
    27.4. Percentage is the required number of hundredths of the base. Thus, the percentage of $\$ 200$, at $5 \%$ is ros $^{8} \sigma$ of $\$ 200$ $=\$ 10$.
    278. The Amount or Difference is the sum or difference of the basc and percentage. Henee,

    The Amount $=$ the Buse + the Percentage.
    The Diffirence $=$ the Brse - the Percentuge.
    The Base = the Amount - the Percentage, or the Difference + the Percentage.

    The Percentage $=$ the Amount - the Base, or the Base the Difference.
    2SO. The rate per cent. may be expressed either by a decimal or a common fuction, as shown in the following
    ymbote.
    
    2.s I. Case I.-Given, the base and rate, to find the percer'age. Ex. What is $6 \%$ of 512 yards of cloth?

    TPERATION.
    R12
    $\overline{30.72} y d$. Ane.

    Analysis, $-6 \%=.06$. Therefore, $6 \%$ of 512 yd . is $.0 B$ of $512=30.72 \mathrm{yd}$. $\operatorname{sta}{ }^{3} \mathrm{~s}$ of 512 yards $=30.72 \mathrm{dd}$.

    $$
    \begin{aligned}
    \mathbf{0}_{\mathrm{R}}, 100 \% & =512 \mathrm{yd} . \\
    1 \% & =5.12 \mathrm{yd.} \\
    6 \% & =30.72 \mathrm{yd.} \text { Ans. }
    \end{aligned}
    $$

    282. Rule.-Multiply the base by the rate\% expressed decimally, and point off as in decimals. Or,

    Find that part of the base which the rate $\$$ is of 100.

    ## bxamples for phactice.

    1. What is $5 \%$ of $\$ 462 ? 4 \%$ of $1550 ? 8 \%$ of $\$ 630.25$ ? $7 \%$ of 8846 ?
    2. What is $9 \%$ of $\$ 75.37$ !? $7 \%$ Ans. $\$ 23.10 ; 62 ; \$ 50.42 ;$ etc. of $\$ 111$ ?
    3. What is $32 \%$ of $\$ 760.60$ ? $44 \%$ of Ans. $\$ 6.78$; 40.6 ; etc. $\ell 12512$ 6?
    4. What is $20 \%$ of 90 cwt ? 650 gal .
    5. What is $15 \%$ of 78 in. 18 cwt ; $\$ 4.25$; eto.
    6. A merchant having $\$ 3456$ in $\$ 23 \%$ of $8 \frac{3}{4} ?$ ? $3 \%$ of $£ 20158$ ? draw 18\%; how much will remain?
    7. A man having $\$ 3947$, gave $15 \%$ of it for flour; $25 \%$ for tea; 45\% for eloth and linen ; and the remaining 15\%, for sugar. How much did he spend for each?

    Ans. For F. $\$ 592.05$; T. $\$ 986.75$; C. $\$ 1776.15$; etc.
    8. A merchant bought 475 barrels of molasses for $\$ 7125$; and sold $40 \%$ of it at $\$ 21$ a barrel ; 30\% at $\$ 18$ a barrel ; and the remainder for what it cost. How much did he gain?

    Ans. $\$ 1567.50$.
    2.83. Case II.-Given, the base and percentage, to find the rate \%.
    Ex. What per cent. of $\$ 450$ is 27 ?
    ofgration.
    100
    $450) \frac{27}{2700}(6 \%$, Ans.
    000.

    Analrass.- $\$ 450$ is $100 \%$ of itself. $\$ 27$ is
     or $\frac{1}{50}$ of 27 times $100 \%=6 \%$ of $\$ 450$.
    $\begin{aligned} 0 \mathrm{r}, \$ 27 \text { is } \frac{23}{4} \sigma & =3 \text { of } \$ 450 \text {; therefors, } \\ \text { it is } \frac{3}{50} \text { of } 100 \% & =6 \% \text { of } \$ 450 \text {, }\end{aligned}$ it is $\frac{3}{50}$ of $100 \%=6 \%$ of $\$ 450$.
    Or, $\$ 450$ is $100 \%$ of iteelf; therefore, $\$ 1$ is $\frac{1}{5} \frac{1}{50}$ of $100 \%={ }_{2}^{2} \%$. and $\$ 27$ is 27 timen部 $\%=6 \%$ of $\$ 450$. Heuce the
    284. Rute -Maltiply 100\% by the percentage and divide by the base. Or, Find that part of 100 per cent. which the percentage is of the

    ## $o=\frac{1}{c} \frac{o f}{}$

    ing
    esced deci-

    ## 10.

    1597\% of 42 ; etc. 16.? $11 \%$ .6 ; etc. ? $68 \%$ of 92, etc. ? $9 \% \%$ of 15 ; eto. E20 158 ? es to with. for tea; tr. How

    5 ; eto. ; and sold emainder 57.50.
    find the
    elf. $\$ 27$ is , of 100 \%, of $\$ 450$.
    thorefors,
    sfore, $\$ 1$ is 27 times
    livide by
    of the

    ## EXAMPLES FOR PRAOTIOR.

    1. At what rate per cent. must we place $\$ 20$ to have $\$ 2$ ? $\$ 5$ to have $\$ 0.25$ ? $\$ 1440$ to have $\$ 21.60$ ? S160 5 to have $£ 121641$ ? $\$ 4$ to have $\$ 0.30$ ? Ans. 10\%; 5\% ; etc.
    2. What per cent. of 40 is 15 ? of 480 perches is 24 per.? of 31 is $\frac{1}{12}$ ? of is $\frac{1}{2}$ ? of 92 gal , is 11 gal . 2 yt .? Ans. $37 \frac{1}{2} \%$; $5 \%$; etc.
    3. What per cent. of 148 is $242^{2}$ ? of 301 b . Avoirdupois is 11 lb . 40 z ? of 720 lb . is 60 lb .? of 620 yd . is 46 yd . ? of 140 lb , is 77 lb .?

    Ans. $16 \%$; $372 \%$; etc.
    4. What per cent of $\$ 578$ is $\$ 26.01$ ? of $\$ 250$ is $\$ 80 ?$ of $\frac{2}{5}$ is $\frac{5}{\delta \delta}$ ? of $£ 315$ is 3 s .9 d . ?
    5. What per cent. of $\$ 300$ will give $25 \%$ of $\$ 72$ ? Ans. $6 \%$.
    6. Bought a horse for $\$ 840$, and sold him for $\$ 560$; how much did I loae per cent.? Ans. 331\%.
    7. A number increased by 2 equale 14 ; required the increase per cent.
    285. Case III.-Given, the rate per cent. and percentage, to find the base.

    Ex. I lost \$27, whioh is $6 \%$ of the money I had; how much had I at first?
    uperation.
    $\$ 27 \div .06=\$ 40$, Ans.
    Or, $\$ 27 \div \frac{3}{50}=\$ 450$. Ans.
    Or, $6 \%=\$ 27$.
    $1 \%=\frac{9}{2}$.
    $100 \%=\$ 450, A$

    Analysis.-If 6 g, or 06 of some nuinber is $\$ 27$, that number must be $\$ 27 \div .06$, or $\frac{3}{8},=\$ 450$.
    $0 \mathrm{r}, 6 \%$ of somo number is $\$ 27,1 \%$ of it is of $\$ 27=\frac{9}{6}$, and $1100 \%$, or the whole nuinber, is 100 times $\frac{9}{2}=\$ 450$. Hence the
    286. Rule.-Divide the percentage by the rate \% expressed decimally, or in the form of a common fraction. Or,

    Divide the percentage by the rate $\%$, and nultiply $b y 100$.

    ## EXAMPLES FOR PRAOTICE.

    1. 35 is $10 \%$ of what number? 84 is $7 \%$ of what number? $\$ 3.60$ is $15 \%$ of what number? $\$ 55.50$ is $41 \%$ of what number? 240 is 12$\} \%$ of what number?
    2. $\$ 66$ is $5 \frac{1}{2} \%$ of what sum? $5 \frac{1}{2}$ is $1 \frac{1}{2} \%$ of wisat 850 ; $?$ what sum?
    3. £32 83 is $71 \%$ of how much ? 207 is 60 ng Ans. $\$ 1200$; etc. is $12 \frac{2}{2} \%$ of how much?

    Ans. £432 34 ; etc.
    4. $\$ 2.81 \frac{1}{2}$ is $121 \%$ of how much? 3 mi . 1 fur. Iper. is $6 \frac{1}{6} \%$ of how much? $16 \frac{1}{2}$ is 23 of how much?

    Ans. $\$ 22.50$; etc.
    5. If the percentage be $\$ 37.50$, and the rate $2 \frac{1}{2} \%$; what is the base?

    Ans. $\$ 1500$.
    6. A farmer saved annually $\$ 145.50$, which was $331 \%$ of his annual income; required his ineome?
    287. Case IV.-Given, the rate per cent. and anow or
    difference, to find the brise.

    Ex. What number increased by $6 \%$ of itself is equal to $47 \%$ ?

    $$
    \begin{aligned}
    & \text { operation. } \\
    & 1+.06=1.06 \\
    & 477 \div 1.06=450, A: 78 . \\
    & \text { Or, } \quad \frac{53}{65}=477 \\
    & \begin{array}{l}
    10 \\
    50 \\
    50
    \end{array} \\
    & { }_{50}^{50}=450, \text { Ans. }
    \end{aligned}
    $$

    Analysis.-A number increasey by 8 it of itaelf, equal: $106 \%$, or 1.06 of itself, wition, by the condition of the questien, ik 477 ; hence, once the number equall $477+1.0 \%$ $=450$.

    Or, 6\% of $a$ number is $\frac{8}{18}=8$ of the number, whioh being increased by 50 , the number, equals $\frac{53}{5} \frac{3}{0}$ of the number, $=477$. If 53 of the number $=477$, 50 of the number $=\frac{50}{53}$ of $477=9$, and 50 , the number, equals 50 times 40
    288. Rule-Divide the amount by 1 plus the rate \% expreased decimally, or us a common fraction; and the difference by 1 minus the rate \%, expressed decimally, or as a common fraction.

    ## EXAMPLES FOR PRAOTIOE.

    1. What is that number, which, diminished by $5 \%$ of itself, yivee 429.40 ?
    2. What number increased by $5 \%$ Ans. 452,
    3. Whave $\$ 407.55$, $4 \%$ by $5 \%$ of itself, gives $\boldsymbol{\mathcal { L }} 1$ I $\%$ ?
    4. I have $\$ 407.55$, or $43 \%$ more than my neighbor : what sump thes
    my neighbor possess?
    5. The difference is $\$ 9.48 \frac{1}{2}$, and the rate, $12 \frac{2 \%}{}$. \$3. 20. base?
    6. Andrew has $£ 18998$, which is $7 \%$ lesg then what sum has the latter9 , whom
     $\$ 52.324$.
    7. A teacher spends $45 \%$ of his income, and saves $585 \mathrm{~s}^{\text {ans, }}$ 籼, his income?
    8. After taking $12 \%$ of a pile of wheat, there remain how many bushels were in the pile?
    9. Having increased my capital by $\$ 5682.60$; how much had I at first ?
    10. A shepherd lost, by disease $12 \%$ of his flock; how many whoe composed his primitive flock, knowing that there remain 1100 ?
    11. A clerk sponds $20 \%$ of $663_{3}^{2} \%$ more than $\frac{1}{}$ of bis income; what is his income, if he saves $\$ 533$ ?
    12. A gentleman sold two horses at $\$ 120$ each; for one he reenived 25\% more, and for the other $25 \%$ leess thar his value; what itwinemed
    13. A man, wishing to sell a horse, asked $25 \%$ more than in comp he finally sold it for $15 \%$ less than his asking price, and geiped 57.50 , How much did the horse cost him, and what was his eeling mies ? Ame. coot, 8120 ; anking mion, S109.

    ## MISCELLANEOUS EXAMPLES IN PERCENTAGE.

    1. Find $185^{\circ}$ of 70 cwt 1 qr .12 lb .
    2. $\$ 1 \frac{2}{5}$ is $\frac{8}{6}$ of what number?
    3. Find a mumber whieh, dimin
    4. A merchant owes $\$$ tion0; his prep by lo\% of itself, gives $£ 48$. rate per cent. can he pay?
    \%. A superior officer, having 1500 men under his Ans. 51 \% $9 \%$ of them in a battle, and $40 \%$ of the remainder his command, lost many remain?
    5. I sold cloth at £1 103 a yard, which Ans. 819 men. how much did it cost a yard?
    6. A man expends $\$ 18$, which is $33 \frac{1}{3} \%$ more than his weekl $664+$ what are his wages?
    Ans. silu.50. 8. After paying $42 \frac{1}{2 \%}$ of my debt, I find that $\$ 2650 \begin{gathered}\text { Ans. } \$ 13.50 \text { will settle the }\end{gathered}$ balance; how much did I owe?
    7. What per cent. of $£ 40$ will give 20 of $£ 7$ Ans. $154608.69+$.
    8. What per cent. of $£ 40$ will give $20 \%$ of $£ 7$ Ans. 15 ? Ans. $34 \%$ \% $\%$. sngar-plums, and has 12 cents of his money in play things, 3 . $\%$ in tain?
    9. What per cent. of a number ives 29 Ans. 48 cts. ber?
    10. A cargo of barley having been lamared, Ans. 183\%. to sell the whole for $\$ 1999.20$ which was at a the cwner was olliged did the cargo oost him? 13. A merchant having $\$ 2150$ deposited in a bank, Ans. $\$ 2940$. 15\% of it ; how much will remain? 14. There remains $25 \frac{1}{\mathrm{y}} \mathrm{d}$. of a piece of linen, after Ans. $\$ 1827.50$. of it; what was the length of the piece? 15. The number of deaths in a certain town, during Ans. 30 yards. 1950, which is $31 \%$ of the population; what is during the year, was habitants?
    11. A fishmonger had 720 bbl of fish, and soll Ans. 60000. cent. remained unsold?
    12. 181 l . 150 z . is $12 \frac{1}{2} \%$ of how many 1 b . ? Ans. $60 \%$.
    13. Gave to a Bencvolent Sucicty 29 hush. of Ans. 1511 b . $80 z$. of my entire crop; how many bushels had I remainine which was $14 \frac{2}{2} \%$ 19. What per cent. of $\frac{1}{2}$ of $\frac{6}{5}$ of $\frac{8}{8}$ gives $\frac{1}{4}$ ? remaining? Ans. 171 . 20. Joseph having received a legacy, deposited $75 \%$ Ans. $25 \%$. A short time after, be drew forth $30 \%$ of his depusit uf it in a bank. remained $£ 1280176$; what was the legacy? 21. In a certain coin there are 21 parts copp Ans. $\begin{aligned} & \text { and } 24: 391528 .\end{aligned}$ What per cent. is the copper and nickel? $A$. copper and 4 parts nickel;
    14. A gentleman has an ann ial income of 2070 . nickel $16 \%$. 20\% for pourishment, $8 \%$ for clothing. 3le of in 8270 : if he expends i4 ${ }^{\circ}$ in casual expenses, what are his annual expenses? 23. In an engegement, $5 \%$ of the army were killed A. 1363.50. battle, and 6\% of the remainder died of their wound on the field of The difference botween the number of the dead and the nurbespitals. wounded was 154 ; how many men compoesd the army? Ans. 22000 .

    ## PEBOENTAGA．

    24．Edward lives $3 \frac{1}{4}$ miles from the city，which distance is $9 \frac{1}{2} \%$ of
    Leu＇s residence uearer the city ；how far from the city does Leo hive？ 2．5．An army，having been twice decimated in batele，is reduced to 19.440 men ；what was the strength of the army before the combat？ 26 ．The eales of a mercantile establishment anount to \＄13lu00 yearly；the $\frac{2}{5}$ of these eales were made at a prufit of $28 \%$ ；the $\frac{4}{1} 5$ of the remainder，at a profit of $40 \%$ ；and the remainder，at a pruit of 17.1 \％；how much did the merchandise cost？：Ans．\＄10411：3．18＋ 27．＇ilie proprietor of the $\frac{5}{6}$ of a factory，sells $24 \%$ of his share to C．，and the remainder to D．，at the same rate，for $\$ 15800$ ；what is the value of the factory？
    28．After cutting a certain number of yard Ans．$\$ 24947.36 s+$ there remains $12 y \mathrm{~d} .2 \frac{1}{5} \mathrm{qr}$ ．，which is 70 年 less than a piece of cloth， what was the length of the prece？

    29．If £36 176 is $14 \frac{1}{4} \%$ of Panl＇s money，ans． 54 yd ．${ }^{1} \frac{8}{15}$ qr． money is $12 \%$ of Leo＇s，how much has Panl more if $53 \%$ of Paul＇e 30．My crop of potatoes this has Pan more than Leo？ year，and I have potatoes this year is $9 \%$ greater than that of last bushels did my last crop in the two years 6479 bushels；of how many 31．If the population consist ？Ans．3379bu． 4260000 inhatutants，what the Dominion of Canade，in 1869，was increase at the rate of $273 \%$ ？

    32．The net gains of a nursery in two years was Ans． 5431500 ． of the second year were $6 \%$ greater than years was $£ 2178$ ；the gains were the gains of each year？ Ans．£105＇ 5789

    ns． the remainder，and finally deposited $12 \%$ of what I had then， $34 \%$ of | much remains in the bank？ |
    | :--- |
    | had drawa；how |
    | 8595.36 ． | 34．A persón having a revenue of $\$ 560$ ，makes the following ex penses ：board，$\$ 130$ ；tailor，$\$ 145$ ；shoemaker，$\$ 28$ ；sundries，$\$ 36$ ； what per cent．of his revenue is each article，and what per cent． remains？Ans． $23{ }^{3} \frac{3}{4} \% ; 25 \frac{25}{8} \% ; 5 \% ; 63 \%$ ； $39 \frac{1}{\frac{1}{8} \%} \%$ ． $9 \%^{35}$ ．If a number be augmented by $11 \%$ of itself，and this amount by 92，it will become $\$ 7.75$ ；what is the number？Ans $\$ 6.40 \frac{6840}{1509}$ ． 36．A merchant expended the same sum in the purchase of wine， the whiskey anffee．In selling，he gained $8 \%$ on the wine and $5 \%$ on ontire sales ；but he lost $14 \%$ on the coffee；he received from his chandiee？

    37．Edmund and Charles have respectively Ans．£210 17 42货多． than Maurice，and the three have together $6 \%$ and $4 \%$ more money Maurice？

    38．A young man commences business on Ans．\＄7200． with a capital of $\$ 2700$ ．At the end of 10 monthe 1 st．of Fobruary， er as follows：Feb．，2\％gain；March， $31 \%$ gain；A rear in his Ledg． May， $11 \%$ gain；June， $2 \frac{3}{2} \%$ gain ；July，la $\frac{3}{2}$ loss；August， $1 \%$ loss； Sept． $1 \%$ loss；Oct． 2 亲 $\%$ gain ；Nov． $4 i \%$ gain；whagust，$\%$ gain； profits of his business during the 10 monthe？

    ## SIMPLE INTEREST.

    289. Interest is the compensation made by the borrower to the lender for the use of money.
    290. The Princiral is the sum lent.
    291. The Rate per cent, is the interest paid for the loan of $\$ 100$, $\& 100$, etc., during any time whatever, which is ordinarily a year.
    Nors.-The rate per oent. is commonly exprossed deoicaally as hundredthe.
    292. The Amount is the sum of the principal and interest.
    293. Simple Interest is the sum paid for the use of the principal only, during the time of the loan.
    294. Legal Interest is the rate per cent. established by law. It varies in different countries.
    Nore. - When no rate is mentioned, the rate established by the laws of the country in which the transantion takes plase, is always understood to be the one intended by the parties.
    295. Usury is a higher rate \% than is allowed by law.

    Notr.-The law prohibits uaury and makes it subjeot to a penalty.
    296. To find the interest on any sum, at any rute \%, for any number of years and months.
    E.x. What is the interest of $\$ 780$, for 5 years and 3 months ( 5 years), at $7 \%$ ? What is the amount?
    
    dnalysis. -The interest of $\$ 1$ for 1 year, at $7 \%$ is $\$ 0.07$, and of $\$ 780$ it is 780 times $\$ 0.07$ $=\$ 54.60$. If the interout of $\$ 780$ for 1 year, at $7 \%$ is 54.60 , for $5 \frac{1}{4}$ yeare it is $5 t$ times $\$ 54.60$ $=\$ 286.65$.

    Or, $\frac{7}{10}$ of the prineipal $=$ the interest for 1 year at 7 g . The amount is fonnd by adding the principal and interest together.
    297. Rule.-I. Multiply the principal by the rate $\%$ expressed decimally, and the product will give the interest for owe year.
    II. Multiply this prodict by the number of years, and the monthe as a fruction of a year, for the intereat required.

    The amount is found by adding the principal and interest together.


    ## BIMPLI INTREEBY.

    ## EXAMPLES FOR PRAOTIOR

    What is the interest of

    1. $\$ 450$ for 3 years, at $4 \%$ ?
    2. $\$ 16$ for 7 years, at $8 \%$ ?
    3. $\$ 656$ for 2 years, at $7 \%$ ?
    4. $\$ 1728$ for 1 year 6 months, at $6 \%$ ?
    5. $\$ 1740$ for 3 years, at $81 \%$ ?
    6. $\$ 878.25$ for 2 years, at $9 \frac{1}{2} \%$ ?
    7. $\$ 118.15$ for 2 years 6 months, at $6 \%$ ?
    8. $\$ 300$ for 3 years 10 months, at $7 \%$ ?
    9. $\$ 125.75$ for 4 years 6 months, at $8 \%$ ?
    10. $\$ 97.16$ for 1 year 5 months, at $6 \%$ ?
    11. $\$ 58.60$ for 2 years 9 months, at $\tau \%$ ?
    12. $\$ 76.50$ for 2 years 2 months, at $5 \%$ ?
    13. $\$ 444.44$ for 5 years, at $6 \frac{8}{5} \%$ ?
    14. $\$ 960.18$ for 1 year 2 months, at $7 \%$ ?
    15. $\$ 4501.80$ for 2 years 4 months, at $6 \frac{1}{4}$ क?
    16. $\$ 1671.32$ for 14 months, at $6 \%$ ?

    What is the amount of
    17. $\$ 53.68$ for 2 years 6 months, at $5 \%$ ?
    18. $\$ 978.18$ for 2 years 3 months, at $6 \%$ ?
    19. $\$ 3050$ for 4 years 8 months, at $5 \frac{1}{4} \%$ ?
    20. $\$ 81.81$ for 8 yeare 4 months, at $6 \%$ ?
    21. \$95 for 1 year and 6 monthe, at $5 \%$ ?
    22. $\$ 65256$ for $4 \frac{2}{2}$ months, at $7 \%$ ?
    23. $\$ 894$ for 20 months, at $6 \%$ ?
    24. $\$ 760$ for 5 geare 7 months, at $5 \frac{1}{2} \%$ ?

    Ans. $\$ 54$. Ans. $\$ 8.96$.

    Ane. $\$ 155.52$.
    Ans. $\$ 435$.
    Ans. $\$ 166.86$.

    Ans. \$45.27.
    Ans. \$8.258.
    Ans. $\$ 12.892$.
    Ans. $88.28+$.
    Ans. \$78.414. Ans. $\$ 656.5125$.

    Ans. $\$ 116.99$.

    Ans. $\$ 60.39$.
    Ans. $\$ 1110.234$.
    Ans. $\$ 3797.25$
    Ans. $\$ 122.715$.
    288. To find the interest on any sum, for any time, at any rate $\%$.

    ## SIX PER OENT. METHOD.

    To find the interest of $\$ 1$ for any time, at $6 \%$; slso, at any other rate \%.

    ANALTRIs.-At $6 \%$ per annum the interest on $\$ 1$.
    For 12 months
    " 62 months ( $\frac{3}{12}=\frac{1}{6}$ of 12 mo ) $\quad$ is $\$ .06$
    " 1 month, or 30 days ( $\frac{1}{12}$ of 12 mo )
    " 6 daye ( $\frac{1}{5}$ of 30 days)
    ( $\frac{1}{6}$ of $6 \mathrm{da}=\frac{1}{30}$ of 30 da.) ${ }^{6} .000 \frac{1}{6}$. Hence,
    lst. The interest on $\$ I$ is $\$ .005$ per month, or $\$ .01$ for every 2 months; 2nd. the interest on $\$ 1$ is $3.000 \frac{1}{5}$ per day, or $\$ 001$ for every
    6 days. Hence the

    E5y. Rule.-1. To find the rate:-Call every year $\$ .06$, every 2 monthe $\$ .01$, every 6 days $\$ .001$. rasd any lese number of days
    $A^{\prime}$
    II. To find the interest:-Multiply the procipal by the rate.

    Ex. 1. What is the interest of $\$ 660$, at $6 \mathbb{\%}$, for 3 years 7 months 27 days?
    oreration. Int. of $\$ 1$ for $3 y \mathrm{r}$. $=\$ 0.18$ the given principal is 660 time of

    | ". | " | " 7 mol. | $=\$ 0.18$ |
    | :--- | :--- | :--- | :--- |
    | " | " | " 27 days. | $=0.035$ |
    | " | " | $=$ | " | Exx. 2. Required the interest on $\$ 750$ for 8 years 8 months 9 days, at $7 \%$.

    ORERATION.

    $$
    \begin{aligned}
    & \begin{aligned}
    \mathbf{\$ 0 . 4 8} & =\text { Int. on } \$ 1 \text { for } 8 \mathrm{yr} .
    \end{aligned} \\
    & \begin{array}{lllll}
    0.04 & = & \text { " } & \text { " } & \text { " } \\
    8 \mathrm{mo} \\
    0.001 \frac{1}{2} & = & \text { " } & \text { " } & \text { " } 9 \text { days. }
    \end{array} \\
    & \frac{\$ 0.521 \frac{1}{2}}{\$ 0.086 \frac{1}{2}}=\text { " }=\text { " } 6 \text { " }
    \end{aligned}
    $$

    $$
    \begin{aligned}
    & \$ 750 \\
    & \frac{\$ .608{ }^{5} 5}{6000} \\
    & 45000 \\
    & 312 \frac{1}{2} \\
    & \$ \overline{456.312 \frac{1}{2}}=\text { Int. required. }
    \end{aligned}
    $$

    Aralpbig.-After finding the interest of $\$ 1$ for ihe given tima, $=0 \% \%$, by the method laid down in the precoding eicample. we divide the result by fo, and then find the interest at $1 \%$; wo then multiply be tis gen rece, 7, and obtain tha interest on $\$ 1$ for tho given time, at $7 \%$ Multaplyrgeg the principai, $\$ 750$, by the rate, $\$ .608{ }_{1}{ }^{5}$, we oblain $\mathbb{\$} 456.31$, whio to the inturest required. Hence the
    300. Ruse.-I. When the reto is greater or less than $6 \underline{6}$ : -Find the interest on Si, at fis, fur the given time, as in the preceding example.
    II. Then divide by s, and mulioply the guotient by the given the intereat regwimal

    ## GIMPLE INTYEETH.

    Nore. -The interast of the given principal, at $6 \%$, for the given time, could be obtained at Aret; then, this result divided by 6 and multiplied by the giver per cent. will give the same answor; or, add or subtract frome this intereat aneh $a$ fractional part of itelf as the given rate exceeds or falls short of $6 \%$ per annnn Thus, if the rate be $9 \%$, the interest at $6 \%$ should be increased $\frac{3}{4}$ or $\frac{1}{2}$ of iteolt. becanse 3 , the excess of 9 over 6 , in $\ddagger$ of 6 , and 00 on.

    When the time is short, business men use the following
    301. Rule.-Multiply the principal by the number of days, divide the product by 6, and remove the decimal pint thrpe places toward the left. (The result is the interest at 6\%.) Thin pro. ceed as in the ubove rule.

    ## METHOD BY ALIQUOT PARTE.

    Ex. What is the interest of $\$ 421.50$ for $3 y r .8 \mathrm{mo}$. and 15 da , at $9 \%$ ? OPERATION.

    Principal,
    Rate \%,
    Interest for 1 year,
    Int. for 3 yeare,
    Int. for $6 \mathrm{mo} .=\frac{1}{2}$ of 1 yr .
    $\$ 421.50$
    $\$ 37.9350$
    3
    $\$ 113.8050$
    Int. for $2 \mathrm{mo} .=\frac{1}{4}$ of 6 mo .
    18.9675

    Int. for $15 \mathrm{da} .=1$ of 2 mo
    6.3225

    Int. for 3 yr .8 mo . 15da. $\$ 1 \mathrm{~B} 0.6756 \frac{1}{4}, ~ A n s$.

    Aralymis,-Having found the interest for lyr. and then for 3 yr ., the ine. for smo. is obtained by first taking 1 of 1 jear's int., for timo., and thea $\&$ of this lnst int. for 2 mo . And since 15 days are $\frac{1}{}$ of 1 mo., or $t$ of 2 mo ., we take $t$ of "mo.'s int. for 15 dajs. The int. as found for the Eeveral parts of the whole time, added together, gives the interest required.

    Note. -Whenever the mamber wr mille is 5 and upwards, in business trapsactions, we add 1 oent and drop the unills. Hence, the interest in the above example is oelled $\$ 140.68$.
    319. Rule.-I. First find the interest for one year by multiplying the principal by the rate \%, decimally expressed, and this product by the number of years.
    II. Find the interest for the months and days by aliquot parts. The sum of the partial interests will be the interest required.

    METH(OD EY MONTHS.
    $E x$. What is the interest of $\$ 24.20$ fur $4 y r .7 \mathrm{mo}$. and 15 da ., at 6 \% ?

    OPERATION.
    6.05
    $\frac{21.29 .06 \times \$ 5.5}{8 \times 4}=\$ 6.7155$.
    
    2. The above is the product of the prinoipal, reto per cent., decimally oxpreseed in monthe and dimimals of a monte, div. lied by $12=8 \times 4$
    operation.
    $\$ 24.20$
    12) $\overline{1.4520}=$ Int. for 1 yr . $\overline{.1210}=$ Int. for 1 mo . 55.5

    6050
    6050
    6050
    303. RuLs.-I. Reduce the time to months and decimals os
    II. Find the interest for 1 year, and divide it by 12 ; the quotient will be 1 month's interest.
    III. Multiply this interest by the time expressed in months, and the product will be the interest required.

    ## METHOD BY PROPORTION.

    Ex. What is the interest of $\$ 52.50$, at $6 \%$, for 4 years 5 months
    Sol. $100: 6 \times 4 \mathrm{yr} .5 \mathrm{mo}$. 10 da . :: $\$ 52.50: x$; whence the 804 RULE. -100 is to the per cent. multiplied by the time, * the principal is to the interest.

    ## EXAMPLES FOR pridctice

    - Er solved by ayt of the chove methods.

    Norn.-If the principal be given in old currenc, reduce the shillings, pence and farthings, to the deoimal of a $\boldsymbol{£}$; then procem ns in deoimal ourronoy.

    What is the interest on

    1. $\$ 500$ for 1 yr . 10 mo . and 15 da ., at $69 ;$ ?
    2. $\$ 9862.12 \frac{1}{3}$ for $3 y$ r. 5 mo., at $4 \%$ ?
    3. £26 100 for 2 yr .4 mo., at $6 \%$ ?
    4. $\$ 972.40$ for $1 \mathbf{y r}$. 7 mo . 18 da . at 7 \% ?
    5. 2143 for $2 \mathrm{yr}_{\text {r }}$ and 9 mo ., at 8 \% ?
    6. $\$ 47.25$ for 1 yr . and 6 mo ., at $6 \%$ ?
    7. $£ 42180$ for $3 \mathbf{y r}$. 4 mo . 25da., at $6 \%$ ?
    8. $\$ 147.90$ for $5 m o .4$ da., at b\%?
    9. $\$ 145.50$ for 1 yr . 9 mo ., 24 da ., at $6 \%$ ?
    10. $\$ 579.75$ for 1 yr . 3mo. 2da., at $5 \%$ ?
    11. $£ 94126$ for $4 y r$. 6 mo . 7 da., at $\mathrm{y} \% \mathrm{z}$ ?
    12. $\$ 123.75$ for 2yr. 8 mo . 12 da., at $6 \%$ ?
    13. $\$ 50.40$ for $1 y r$. and 10 mo ., at $7 \%$ ?
    14. $\$ 475$ for $2 y r$. 7 mo . 20 da ., at 6 必?
    15. £6 11 . for $2 y r .4 m o .$, at $7 \%$ ?
    16. $\$ 336$ for 5 mo. lida., al $5 \%$ ?
    17. $\$ 1265.60$ for $5 y r$. 2mo. 9da., at $7 \%$ ?
    18. $\$ 72.12 \frac{1}{3}$ for 6 yr . and Smu., Et 4 4\%?
    19. $\$ 497.36$ for lyr. 6 mo. lda., at $5 \%$ ?
    20. £19154 for 2yr. 9 mo ., at 1\%?
    21. $\$ 7671.09$ for 3 yr . 8 mo . 5 da., at $\mathrm{F} \%$ ?
    22. \$49.80 for $2 y r$. and 11 mo., at 7\%?
    23. 350.80 for 15 mo . and 8da., at 10 g ?

    Ans. $\mathbf{\$ 5 6 . 2 5}$.
    Ans. $\$ 1347.82+$.
    Ans. \$14.84.
    Ans. $\$ 111.177+$.
    Ans. \$31.46.
    Ans. $\$ 4.25$ !
    Ans. f8 $152 \frac{1}{10}$
    dns. $\$ 5.01+$.
    Ans. $\$ 15.85+$.
    Ans. $\$ 36.395+$. Ans. $\$ 136.848+$.
    $A n s . \$ 20.04 \frac{3}{4}$.
    Ans. $\$ 6.468$.
    Ans. $\$ 75.208 \frac{1}{3}$. Ans. £1 $15 \frac{1}{4}$.

    Ans. $\$ 7.70$.
    Ans. $\$ 459.94+$. Ans. $\$ 18.51+$. Ans. $\$ 37.37+$ 。
    Ans. $\$ 21.039+$.
    Ans. $\$ 2258.70+$.
    Ans. $\$ 10.163^{\circ}$
    24. $\$ 1040$ for $6 y r .11$ mo. 29da., at $7 \%$ 个
    25. £24 188 for 10 mo . and 20da., at $7 \%$ ?
    26. $\$ .51 .17$ for 10 mo . and 29 da , at $4 \%$ ?
    27. $\$ 548.12$ for $6 y r .1$ mo. 3 da., at $7 \%$ ?
    28. $\$ 500$ for 2 yr . 5 mo . 12 da., at $6 \%$ ?
    29. \$909.50 for 5yr. 5mo. 4da., at 6 \% ?
    30. $£ 92120$ for 2 yr .10 mo ., at $6 \frac{1}{2} \%$ ?
    31. $\$ 680$ for 4 yr l mo . 15 da ., at $\mathrm{f} \%$ \%
    32. $\$ 2000$ for lyr. Bmo. l0da., at $!\%$ ?
    33. $\$ 471.11$ for 4 yr . and 8 mo ., at $i \frac{1}{2} \%$ ?
    34. $\$ 190.016$ for 3 mo .24 da ., at $4 \frac{1}{2} \%$ ?
    35. £427 88 for lyr. 5 mo ., at $5 \frac{3}{4} \%$ ?
    36. $\$ 708.20$ for 2 yr .2 mo . 12 da., at $4 \frac{3}{4} \%$ ?
    37. $\$ 640.70$ for 8 mo . and 26 da ., at $5 \frac{1}{2} \%$ ?
    38. $\$ 330.50$ for 18 mo . and 23 da ., at $6 \frac{1}{4} \%$ ?
    39. $\$ 950$ for 4 yr. 7 mo . 9 da., at $8 \frac{1}{4} \%$ ?
    40. £४1 100 for 2yr. and momo, at $4 \frac{3}{4} \%$ ?
    41. $\$ 150.80$ for 7 mo and 20 da ., at $7 \frac{1}{4} \%$ ?
    42. $\$ 1072.40$ for 5 yr. 10 mo . 5 da., at $6 \frac{1}{2} \%$ ?
    43. $\$ 601.20$ for 4 yr. 2 mo. 3 da., at $8 \frac{1}{2} \%$ "
    44. $\$ 1425.20$ for 1 yr . and 16 da ., at $4 \frac{1}{2} \%$ ?
    45. £319 109 for 1 yr .10 mo ., at $4 \frac{2}{8} \mathscr{L}_{0}$ ?
    46. $\$ 742.30$ for 4 yr .9 mo .19 da ., at $6 \frac{3}{4} \%$ ?
    47. $\$ 1370.40$ for $3 y r .4 \mathrm{mo} .27 \mathrm{da}$., at $7 \frac{1}{2} \%$ ?
    48. $\$ 160.75$ for 2 yr .11 mo .4 da ., at $5 \frac{3}{4} \%_{0}$ ?
    49. $\$ 1463.60$ for 7 yr .7 mo . 22da., at $6 \frac{1}{2} \%$ ?

    D0. $£ 184188$ for 1 lyr 9 mo .6 da ., at $3 \frac{1}{8} \%$ ?

    ## What is the amount of

    51. $\$ 0.145$ for 9 yr .9 mo . and 9da., at 6 ?
    52. $\$ 1051.50$ for 2 yr . 10 mo ., at $7 \%$ ?
    53. $\$ 168.13$ for 8 yr . 5 mo . 3da., at $6 \%$ ?
    54. $\$ 100.25$ for 2 mo . and 29 da ., at $4 \%$ ?
    $55 . \$ 1.011$ for 10 yr .10 mo . 10 da., at $6 \%$ ?
    56 . $\$ 1000$ for $3 y r .3 \mathrm{mo}$. 29 da ., at $5 \frac{1}{2} \%$ ?
    \%7. $\$ 168.50$ for 1 yr .5 mo and 10 da ., at $6 \frac{1}{3} \%$ ?
    55. $\$ 2000$ for 1 mo . 5 da ., at $6 \frac{3}{4} \%$ ?
    56. $\$ 0.05$ for 20 yr . 10 mo .15 da. , at $8 \%$ ?
    57. $\$ 325.25$ for 2 yr . 9 mo . 12 da., at $6 \frac{1}{2} \%$ ?
    58. $\$ 495.95$ for 5 yr .5 mo . 5da., at $6 \frac{3}{4} \%$ ?
    59. £109 39 for 7 yr .9 mo . 18 da ., at $345 \%$ ?
    60. $\$ 2560.75$ for 4 yr . 3 mo . 25 da ., at $6 \frac{1}{2} \%$ ?
    61. What is the interest of $\$ 1560$ from April 9 , to November 10 , at $5 \frac{1}{2} \%$ ?
    62. What is the amount of $\$ 175.08$ from May 7 180. $\$ 50.28$. ber 25,1863 , at $7 \frac{2}{\pi}$ ?
    63. What is the interet 9176.891 fom J. 22,1869 , at $6 \frac{1}{2} \%$ ?
    64. What is the amount of $\$ 1756.75$ from June 29, 1860, to February 12,1863 , at 7 os?

    Ans. $\$ 1183.18$.
    Ans. $\$ 2013.12 \frac{1}{3}$.
    Ans. $\$ 384.09+$.

    Ans. \$436.596. Ans. £1 $110 \frac{1}{4}+$ Ans. $\$ 233.72+$. Ans. $\$ 296.19$ +

    Ans. $\$ 168.30$.
    Ans. $\$ 164.888+$. Ans. £34 $164+$.

    Ans. $826.037+$. Ans. $8: 361.178+$

    Ans. $6.98+$.
    Ans. $\$ 213.35+$.
    Ans. $\$ 102.518+$.
    Ans. $\$ 350.30+$.
    Ans. $\$ 727.24+$.
    68. What is the interest of £43 26 fro.iv Yarch 17, to December 7, at 71 \% ? 69. What is the interest of $\$ 1530.50$ from February $10,182518+$, to January 25, 1869, at $\frac{1}{1} \%$ ?
    70. What is the amount of $\$ 158.30$ Ans. $\$ 7.33+$.

    December 30, 1871, at $7 \frac{1}{2} \%$ ?
    71. What is the interest of

    1869, at $+\%$ ? 72. What is the interest of $£ 3289$ Ans. $\$ 5.16+$. July 9, 1869, at $\frac{3}{1} \%$ ? 73. What is the am ber 9,1871 , at $8 \frac{1}{2} \%$ ? $\$ 89.96$ from June 19, 1870, to Decem 74. What is the interest of $\$ 990.75$ from October Ans. $\$ 100.886$. uary 15, 1869, at l $\frac{8}{4} \%$ ?
    75. What is the interest of $\$ 1030.10$ from November 8,1867 , to March 3, 1869, at $8 \frac{7}{8} \%$ ? 76. What is the interest of $£ 45104$ from December 10,1866 , to May 5, 1869, at ह\% \%

    ## EXAOT METHOD OF OOMPUTING INTEREST.

    305. In the preceding methods of computing interest, which are in general use, we have reckoned 30 days to the month, and 12 montins to the year, which allows to each year 360 instead of 365 days. Hence, the results obtained in these calculations are not strietly correct.

    The following exact method is used by business men in computing interest when the time is short.

    Notr.-The exect time, when it is less than a year, is found by the tablo on
    306. Kule.-Multiply the interest of the principal for 1 year by the exuct number of days it has been on interest, and divide the product by 365, the quotient will be the interest required.

    1. What is the interest of $\$ 345.60$, from February 5, 1869, to Aug. 20,1871 , at $7 \%$ ?
    2. What is the interest, at $5 \frac{1}{2} \%$, of $\$ 425.50$ from $\boldsymbol{A}$ ns. $\$ 61.374+$. November 20th.?
    3. What is the interest, at $6 \frac{1}{2} \%$, of $\$ 140.40$, from $\Delta u 8 . \$ 20.26+$. to Nov. 29th., 1871 ? ${ }^{\text {? }}$, $\$ 140.40$, from Aug. 29th., 1870,
    4. What is the intereet, at $8 \%$, of $\$ 4500$, from Mns. $\$ 11.426+$. Sept, 25th., 1971?
    5. What is the interest, at $7 \$ \%$, of $\$ 3790.45$, from July 20th., 1869, to Sept. 12th., 1871 ?
    6. What isthe interect, at $44 \%$ or 4816 3. Hrom Dopi ; 2th., 1868, to 4 ug . 20th., 1871?

    ## PARTIAL PAYMENTS.

    307. Partial Payments are payments of part of a noto, bond, or other mon yed obligation, made at different timiss.

    The payments are acknowledged by receipts written by the ereditor on the back of the note or obligation, which are called Indorsements.
    308. Role.-I. If the interest be paid by days:-Multiply The principal by the number of days which have elapsed bejore any payment was made. Subtract the first payment, und multiply the remainder by the number of days wohich passed between the first ond second payments. Subtract the second payment, and multiply this remainder by the number of duys which pussed between the secomel and third payments. Subtract the third payment, et:-
    11. Add all the products together, aud find the interest of 'heir sum for one day.
    111. If the interest is to be paid by the week or month :Substitute weeks or months for days, in the above rule.

    Ex. 1. How much principal snd interest have I to pay on the folkowing note, due Dec. 29, 1811 ?

    For value received, I prumine to pay James Carroll, or order, fou: Wtadred and twenty dollars, with interest, at $7 \%$ ? Thomas Brown.

    On this note were indorsed the following payments:-
    
    operation.
    From Sept. 8, 1868, to Oct. 1, 1869, there are 388 days.
    " Oct. 1, 1869, to Nov. 20, 1869, ‘" " 50 "
    " Nov. 20, 1869, to May 8, 1871, " " 534 "
    " May. 8, 1871, to Dec. 29, 1871, " " 235 "
    Whole principal $\$ 220.00$ for 388 days $=\$ 162960.00$ for 1 day

    First indorsement
    22.28
    $\begin{gathered}\$ 397.72 \\ 50.00 \\ \text { for } \\ 50 \text { days }\end{gathered}=\$ 19886.00$ for 1 day Scoond indorsement
    $\underset{\substack{\text { 24.87 } \\ \$ 347.72}}{ }$ for 534 days $=\$ 185682.48$ for 1 day.
    $\$ 99.85$ for 235 days $=\mathbf{\$ 2 3 4 6 4 . 7 5}$ for 1 day.

    Whole interest $=$ that of

    Hence, the int. for 1 day $=\$ 27439.5261+365=\$ 75.1767+$.

    | Then intereat due | $=\$ 75.1767+$ |
    | :--- | :--- |
    | Balance on note | $=99.8500$. |

    2. Nine months after date, I promise to pay Louis Merrill, or c i; four hundred and fifty dollars, with interest, at $6 \%$. for value received.
    A. N. Moreau.

    Indorsed as folluws: Oct. 7, 1869, $\$ 125.10$; Aug. 25, 1870, \$225.35. How muoh remained due Sept. 19, 1871 ?
    $A_{n 8}$. $\$ 142.8802+$.
    Kingaton, July 26, 1866.
    3. Four years after date, we promise to pay Lawrence Boyce, or order, three hundred twenty-five and $\frac{28}{100}$ dollars, with interest, at $7 \%$. Value received.
    L. R. Whelan \& Co.

    Indursed as follows: Jan. 20, 1867, \$121.18; March 14, 1858, $\$ 72.45$; July 26, 186y, \$133.85. How muoh remained duo Sept. 8, 18709 Ans. $\$ 41.01+$.

    ## $\$ 1737 \frac{50}{100}$.

    Toronto, March 6, 1868.
    4. On demand, we promise to pay Fisher \& Howe, or order, one thousand seven hundred thirty-seven and $\frac{50}{100}$ dollars, for value received, with interest, at $6 \not \%$ ? ${ }^{100}$ T. Johneon \& Bro.
    Indorsed as follows: June 1, 1808, \$623.80; Sept. 10, 1888, \$7u(0. How muoh was uue Jan. 31, 1869 ?
    $\$ 1240$.
    Ottawa, Aug. 18, 1869.
    5. For value received, I promise to pay R. N. Kelly, or order, twelve hundred and forty dollars, on demand, with interest, at $氏 \mathscr{\%}$.

    Joseph Rogers.
    Indorsta as follows: Sept. 25, 1869, \$05; Oct. 28, 1869, $\$ 217.86$; Deo. 12, 1869, \$432.36; April 6, 1570 , $\$ 120.20$; July 3, 1870, $\$ 366.50$. How much remained due Sept. 10, 1870 ?

    Ane. $\$ 43.768+$.
    $\boldsymbol{£} 30466$.
    Halifax, June 2, 1868.
    6. For vaiue received, I promise to pay N. J. Webster, or order, on demand, three hundred and four pounds six shillings and six pence, with interest, at $6 \%$.
    A. C. Murphy.

    Indorned as follows: July 17, 1868, £51 19 v ; Oct. 6, 1868, $£ 5280$; Dec.
     Ane. $£ 2413 \quad \frac{21}{125}$.
    

    ## IMAGE EVALUATION TEST TARGET (MT-3)

    
    
    

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    Corporation
    

    St. John, June 17, 1866.
    7. For value received, we jointly and severally promise to pay Edward Hammond, or order, on demand, fourteen thousand six hims dred and ninety-six $\frac{50}{100}$ dollars, with interest, at $8 \%$. J. P. Rooney.
    S. E. Hamilton.

    Indorsed as follows : Sept. 5, 1866, \$4927.60; Deo. 7, 1866, \$784.40; June 11, 867, $\$ 1964.40$; Feb. 7, 1868, $\$ 5685.80$; Dee. 19, 1868, $\$ 634.46$. How much emained due May 1,1869? Ane.\$2006. $266+$.
    8. A farmer gave a mortgage on his farm for $\$ 4875$, dated June 1, 1867, to be paid in 4 years, with $7 \frac{1}{2}$ \% interest. Six months from date ae paid $\$ 223.25$; Oct. 20, 1869 , §1250; July 3, 1870, $\$ 7.50$; Jan. 1, 1871, $\$ 250$; how much was due at the expiration of the given time? ins. $\$ 3595.31+$.

    ## PROBLEMS IN INTEREST.

    309. It will be observed that there are five parts or terms connected with each of the preceding questions in interest, viz: the Principal, the Ratc \% the Time, the Interest, and the Amount. The investigation of these involves five cases: I. To find the interest; II 'To find the amount; III. To find the principal; IV. To find the rate \%; V. To find the time.

    The Cases I. and II. have already been solved (296, 298).
    31D. Case III.-The interest, time, and rate \%, being given, to find the Prinoipal.
    Ex. What principal in 3 years, at $6 \%$, will gain $\$ 47.70$ interest?
    operation. .06 int. of $\$ 1$ for 1 yr . 3 . 18 ) $\$ 47.70$ ( $\$ 265$, Ans. By proportion.
    $\$ 100: x:: \$ 6 \times 3: \$ 47.70$.

    Analysis.-We fiad the interest of $\$ 1$ for 3 years. Siuce it requires 3 years from a principal of $\$ 1$ to gain 18 cents, it will require a principal of as many dollars to gain $\$ 47.70$ ss $\$ 0.18$ is contained times in $\$ 47.70$; dividing, we obtain $\$ 265$, the required principal. Henoe
    311. Rule. - Divide the given interest or amount by the interest or amount of $\$ 1$ for the given time and rate, and the quotient will be the principal.

    ## EXAMPLES FOR PRACTICE.

    What principal will is

    1. $6 y r .3$ mo., at $6 \%$, give $\$ 56.25$ ?
    2. lyr. 6 mo ., at $6 \%$, give $\$ 1.2924 \mathrm{int}$. ?
    3. 

    e to pay sir hinn oney. milton.
    ; June 11, low much 266+.
    June 1, :om date Jan. 1, n time?
    $1+$.
    ms coniz : the mount. the ind; IV.
    98). g given, rest ? ntereast $\alpha$ squiros 3 to gain inoipal of 47.70 ms $\$ 47.70$; requirod
    3. 4 mo . 18 da ., at $4 \%$, give $\$ 27.60$ int. ?
    4. 1 lyr . 4 mo ., at $8 \frac{1}{4} \%$, give $\$ 13.20$ int. ?
    5. 3 yr. 8 mo . 15 da ., at 6 \% $\%$, give $\$ 76.095$ int. ?
    6. 4 yr .9 mo .18 da ., at 9 \%. give $\$ 65.016$ interest?
    7. 8 yr . 8 mo . 12 da., at $5 \%$, yain $\$ 147.9435$ ?
    
    9. If the interest on a sum borrowed at $2 \%$ a month, is $\$ 24$ for 90 days, what is the sum? to produce \$619.15?
    312. CASE IV.-The principal, time and interest being given, to find the Rate \%.
    E.r. The intrrest of $\$ 750$ for 4 years is $\$ 180$, what is the rate $\%$ ?

    $$
    \begin{aligned}
    & \text { oparation. } \\
    & \text { \$750 } \\
    & \left.\frac{.04}{\$ 30.00}\right) \$ 180.00(6 \%, \text { Ans. } \\
    & \text { By proportion. } \\
    & \text { \$100: } \$ 750:: x \times 4: \$ 180 \text {. } \\
    & \text { Anslysis.-We fiad the intereat } \\
    & \text { on the principal for } 4 \text { years at } 1 \% \text {. } \\
    & \text { Since the interest of } \$ 1 \text { at } 1 \% \text { for } \\
    & 4 \text { years is } 4 \text { cts., the intereat of } \$ 750 \\
    & \text { will be } 750 \text { times as much, or } \$ 30 \text {. } \\
    & \text { Now, if } \$ 30 \text { is } 1 \%, \$ 180 \text { will be as } \\
    & \text { many } \% \text { as } \$ 30 \text { is contained times } \\
    & \text { in } \$ 180 \text {; dividing, we obtain } 6 \text {, the } \\
    & \text { required rate \%. Berce the }
    \end{aligned}
    $$

    313. Rule.-Divide the given interest by the iuterest of the. principal for the given time, at $1 \%$, and the quotient will be the rate \% required.

    ## EXAMPLES FOR FRACTICE.

    Required the rate per cent. if the intereat of

    1. $\$ 500$ for 1 yr. 3 mo. is $\$ 56.25$.
    2. $\$ 40$ for 2 yr . 9 mo . 12 da . is $\$ 13.36$.
    3. $\$ 540$ for 1 yr . 2 mo . 6 da . is $\$ 38.34$.
    4. $£ 37150$ for 1 yr .4 mo is $£ 31053$.
    5. $\$ 125$ for $3 y r$. 6 mo . is $\$ 32.37 \frac{1}{2}$.
    6. $\$ 1500$ for 3 yr . 3 mo . 29 da . is $\$ 274.77$.
    7. $\$ 124$ for 4 yr . 3 mo . 10 da . is $\$ 29.17 \mathrm{f}$.
    8. $\$ 36$ for $3 y \mathrm{r}$. 8 mo . 19 da . is $\$ 8.934$.
    9. At what rate $\%$ must $\$ 1$, or any other sum, be on interest, to double irself in $14 \frac{2}{7}$ years? Ens. $7 \%$.
    10. A man invested $\$ 4500$ in the Montreal Bank, and received a semi-annual dividend of $\$ 167.50$; what $\neq$ was the dividend?
    11. Cass V.-The principal, interest, and rate \% being given, to fisd the Time.
    
    12. Rute.-Divide the given interest by the interest on the principal for 1 year, and the quotient will be the time required in years and decimals.
    Nors.-The decimal part of the quotiont, if any, may be reducsd to momthe
    and days (by 210).

    In what time will

    1. $\$ 26$, at 6 \%. give $\$ 1.95$ interest?

    Ane. I7r. 3mo.
    2. $\$ 280$, at $6 \%$, give $\$ 84$ interest ?
    3. $\$ 45.25$, at $6 \%$, give $\$ 1.81$ interest : Ans. 5 years.
    4. $\$ 98$, at $8 \%$. gain $\$ 25.48$ ?
    5. $\$ 240$, at $(\mathbb{\%} \%$ amt. to $\$ 280$ ?
    6. $\$ 70.50$, a $\%$, give $\$ 31.72 \frac{1}{2}$ interest ?
    7. $\$ 408$, at $7 \%$ ant. to $\$ 434.18$ ?
    8. £120, at $4 \frac{1}{2} \%$, amt. to $£ 14080$ ?
    9. $\$ 1$, or any other sum, double itself, at $5 \%$ int.? Ans. ?
    10. $\$ 2365.24$ double itself, at $7 \%$ ?

    ## PROMISCUOUS EXAMPLES IN SIMPLE INTEREST.

    What principal will in

    1. 5yr. 4 mo., at $4 \%$, give $\$ 2048$ int. ?
    2. 5 mo . 6da., at $6 \%$, give $£ 13636 \mathrm{int}$. ?
    3. 1 yr .8 mo ., at $6 \frac{1}{2} \%$, give $\$ 97.50$ int. ?
    4. 9 mo . 2lda., at $5 \%$, give $£ 15150$ int.?
    5. 3yr. 5 mo. 18 da., at $5 \frac{1}{\lambda} \%$, give $\$ 288$ int.?
    6. 11 mo . 9 da., at $5 \frac{1}{2} \%$. give $\mathbf{£} 46626$ int. ?
    7. 4 yr . 5 mo . 14 da ., at 5 \% give $\$ 150.371$ int. ?
    8. 3 gr . 5 mo . 17 da., at $5 \frac{3}{4} \%$, give $\$ 1451.52$ int.?

    Ans. $\$ 9600$. Ans. £5237 10.

    Ans. $\$ 900$.

    In what time will
    9. $\$ 625$, at $6 \%$, give $\$ 262.50 \mathrm{int}$ ? 10. £67 100 , at $4 \%$, give $£ 2460$ int. ?
    ! $\$ 1779$, at $5 \%$, give \$296.5C int.?
    Ans.7yr.
    Ans. 9 yr .
    Ans. 3vr. 4 mp

    ## intarcent

    1 yoar. 1 year is $\theta$ will be Now, if ven primequire as $18 \$ 27$ is iding, we ed time.on the ired in
    12. $\$ 242$, at $4 \frac{8}{4} \alpha_{0}$ give $\$ 55 \mathrm{int}$ ?
    13. $£ 460$, at $5 \frac{1}{4} 9$, give $£ 50$ int.?
    14. $\$ 2178$, at $4 \frac{1}{1}$ 治, give $\$ 635.25 \mathrm{int}$. ?
    15. £405, at 6 \%. ive $\boldsymbol{x} 151176$ int. ?
    16. $\$ 481.25$, at $5 \%$, give $\$ 192.50$ int.?

    Required the rate \%, if the interest of
    17. $\$ 978.20$ for lyr. is $\$ 18.91$.
    18. $£ 110126$ for 50 da . is $£ 16101$.
    19. $\$ 1290$ for 124 da . is $\$ 19.991$.
    20. $\$ 4340$ for 3 yr . is $\$: 85.90$.
    21. $\$ 675$ for 44 mo . is $\$ 142.31 \frac{1}{4}$.
    22. $\$ 7500$ for 48 da. is $\$ 60$.
    23. $\$ 11004.75$ for 1 yr . is $\$ 550.23$ ?
    24. $£ 120$ for 6 mo . i 5 da is $£ 32100$.
    25. The annual sales of a starch manufacturer amount to $£ 273710$; supposing that his prufits are $5 \%$ per year, in how many years wilf they reach $£ 323189$ ?

    Ans. 2yr. 4 mo . 12 da .
    26. An individual disposed of the $\frac{5}{5}$ of his tund at $+\%$ and $\frac{1}{f}$ at 5 \% cricy year he draws as much as will pay the harneasing of a horse which baraess is worth $\$ 117.60$; what is the sumbt of his funds?
    27. What is the interest of $\$ 17.18$, from July $29 t h .$, isiti, to Sept. Ist., 1868 , at $6 \%$ ? Ans. $34.214+$.
    28. What will be the amount of $£ 19159$, at $7 \frac{1}{3}$ \& frou Feb. 17 th., 1864, to Dec. 30th., 1867 ?

    Ans. £25 $107+$.
    29. If $\$ 1756.75$ is placed on intereat, June 29th., 1866 , what will it mount to Feb. 12th., 1869, at $7 \%$ ?

    Ans. $\$ 2078.869+$.
    30. What principal, at $b \%$. during lyr. 8mo. 12da. will amount to £231 1211 령

    Ans. £213 100.
    31. On Aug. 15th., 1860 , I lent $\$ 5259$, at $6 \%$; what amount will be due me on May lst., 1868 ?

    Ans. $\$ 7492.164$.
    32. An individual buys $65 \frac{1}{8}$ ucres of land at the rate of $\$ 509.72$ per 100 acres; if he pays only at the end of 3 yr . 1 mo. 15 da. , the int. will equal to $\frac{1}{2}$ of the principal; what is the rate? Ans. $4 \%$.
    33. A person placed a certain sum on interest at $4 \%$, which produced $£ 427$ 10, in 3 years; what is the sum? Ans. $£ 356210$.
    34. What is the interest on a bill of $\$ 257.81$, dated March 1st., 1865, and payable July 16th., 1867, at $7 \%$ ? Ans. $\$ 42.86+$.
    35. Find the amount of $\$ 17041.20$, at $+\frac{3}{4} \%$, for 1 yr .7 mo .28 da .
    36. What sum is that which will give an interest of $\$ 900$, in 10 yr ., at $4!\%$ ?

    Ans. $\$ 2000$.
    37. A principal of $£ 11210$ was put on interest, and at the end of 8yr. amounted to $£ 144$; at what rate was the principal placed?
    38. A boy has accumulated a sum of money by his eavings, and wishes to obtain an annual revenue of $\$ 140$; if che rate is $5 \%$, wha principal must he have?

    Ans. $\$ 2800$.
    39. A merchant borrows the sum of $£ 938123$, which is owned by a minor aged 15 yr . 3mo. 20da. He keeps it until the owner is 21 years old; what sum will be then due, at $6 \%$ simple interest ?
    40. What will be the interest of \$325, from June 6th., 1866 , $w$ July 4 th., 1868, at 71 \% ? Ans. $\$ 49.02+$.
    41. A merchant says that his gain, during the nine years he carried on business, equals the price of 3659 yards of cloth at $\$ 2.08$ a yard; what was his annual revenue, supposing he placed his gain on interest at $5 \%$ ?
    42. From 1857 to 1867, the population of Syracuse augmented $24 \frac{3}{4} \%$; knowing the last year's number of inhabitants to be 102295 , tell ns what was the population in 1857 ?

    Ans. 82001 inhab.
    43. What sumimust be placed on interest, at $4 \%$, to amount to $\boldsymbol{£ 6 2 7} 186$ in $2 y r$. 10 no 16 da.?

    Ans. £563 $21 \frac{1}{2}$.
    44. A man assures me that if he places on interest a sum equivalent to 968 yd . of cloth at $\$ 3.18$ a yard, he will secure an annual revenue of $\$ 153.91 \frac{1}{5}$; what must be the rate? Ans. $5 \%$.
    45. From an investment of $\$ 35680$ in commercial concerns, I withdraw a gain of $\$ 223$ per month; what is the annual rate of the interest?

    Ans. $7 \frac{1}{2} \%$.
    46. A property was sold for $£ 2830$; the conditions were $£ 800$ in cash, $£ 875$ in 6 months, $£ 625$ in 10 months, and the remainder in 1 yr . 3 mo., with interest at $7 \%$; what was the amount paid ?
    47. A merchant having raised, during the 6 years of his business, a capital of $\$ 2965.10$, desires to know in what time he will receive $\$ 889.53$ as interest at $5 \%$ ?
    48. An individual borrowed $£ 3750$ at $7 \%$, and then lent it at $6 \%$; what will he lose in 146 days, if the year, for the first transaction, cousists of 360 days, and that of the second, 365 days?
    49. During what time must a certain sum be on interest at $4 \frac{1}{2} \%$ to produce $\frac{1}{6}$ of it?
    50. In selling merchandise at 12s. the yard, I make a profit of $6 \frac{1}{4} \%$; what is the price per yard?
    51. The $\frac{8}{8}$ of a sum of money is lent at $4 \%$, and the $\frac{2}{5}$, at $5 \%$; what is the sum, knowing that the annual interest is $\$ 28.52$ ? Ans. $\$ 655$.
    52. An apparatus for astroncmical purposes cost $£ 49$; but, as this sum could not be paid before 3yr. 9mo., the price was angmented $\frac{3}{20}$ of its primitive value; what was the rate? Ans. $4 \%$.
    53. A man placed on interest, at $4 \%$, a certain sum of money which produced in 5 years the frunds requisite for the purchase of 368 lbs . of preserved tamarinds, at $46 \frac{1}{2}$ cts. a 1 b . ; what was the sum?
    54. A merchant has invested in business a capital of $\$ 21840$ which produces him $12 \frac{1}{2} \%$ annually; but, for sanitary reasons, he retires from mercantile afliairs, and losns his monsy at $7 \frac{3}{4} \%$; how much will he lose in 2 yr . 5 mo . 10 da . by the change ? ${ }^{2}$ Ans. $\$ 2535.862$.
    55. What is that principal the $\frac{4}{5}$ of which at $6 \%$, and the remainder at $7 \%$ will give $\$ 4340$ interest? ${ }^{2}$ Ans. $\$ 70000.00$.
    56. A speculator desires to purchase a tract of land, containing 450 acres, at $£ 6176$ per acre, and, for this purpose, borrows money at $5 \frac{1}{2}$ of. At the expiration of 4 yr . 11 mo. 20da., he sells the of of the land at $\dot{f} \ell^{\prime} 10$ an acre, and the remainder, at $£ 829$ the acre; how much does he lose by the transaction?

    1866, $2+$. he car$\$ 2.08$ a is gain 0.536 . ed $24 \frac{3}{3} \%$; tell n inhab. nount to 212. n equiv. nual rev. . $5 \%$. cerns, I te of the $71 \%$. £800 in nder in usiness, receive . 6 yr . at 6 \% ; on, con-
    $41 \%$ to 10da. f $6 \%$; +d . ; what $\$ 655$. 28 this ted $\frac{3}{20}$ $4 \%$. which 88 lbs.
    which retires ch will $86 \frac{2}{2}$. ainder 100 ng 450 ney at eland much

    OOMPOUND INTEREBT.
    191

    ## COMPOUND INTEREST.

    isisis. Compound Interest is interest on both principal and miterest, when the latler is not paid when due.
    Nour. - The simple interest may be adsed to the principal annualiy, semi-annualily, (1narterly, or n onthly, necording to agreement. A ereditor may receive compunni interest withont being linble to the charge of usury, but cannot legally
    denan $i t$.
    E.x. What is the compound interent of $\$ 390$ for 3 years, at $5 \%$ ?

    $$
    \begin{aligned}
    & \text { opzration. } \\
    & \begin{array}{lll}
    \$ 390.00 \times .05=\begin{array}{l}
    \$ 390.00 \\
    19.50
    \end{array} & \begin{array}{l}
    \text { Principal for lst. year. } \\
    \text { Interest for lst. year. }
    \end{array} \\
    \$ 409.50 \times .05=\frac{20.50}{\$ 45} & \begin{array}{l}
    \text { Principal for 2nd. year. } \\
    \text { Interest for 2nd. y eur. }
    \end{array} \\
    \$ 429.975 \times .05-\$ 429.975 & \begin{array}{l}
    \text { Principal for 3rd. year. }
    \end{array}
    \end{array} \\
    & \$ 429.975 \times .05=\begin{array}{r}
    21.49875 \\
    \$ 451.4725
    \end{array} \text { Interest fur 3rd. year. } \\
    & \$ 451.47375 \text { Amount for } 3 \text { years. } \\
    & \frac{\$ 390.00000}{\$ 61.47375} \text { Compound interest. }
    \end{aligned}
    $$

    317. Rule.-I. Fint the amount of the given principal at the giv, $n$ rate for one year, and make it the principal for the second year.

    1I. Find the amount of this nevo principal, and make it the principal for the third year, and so continue to do for the given "1umber of years.
    III. Subtract the given principal from the last amount, and the remainder will be the compound interest.

    Notes.-1. When the time cuntains years, months, and days, find the amount for the jears, upon which compute the interest for the months and days, and add it to the last amount, before subtracting.
    2. When the interest is payable semi-annually or quarterly, find the amount of the given principal for the first interval, and make it the principal for the seeond interval, proceeding in all respects as when the interest is payable yearly.

    ## EXAMPLES FOR PRAOTICE.

    1. What is the compound interest of $\$ 970$ for 2 years 9 months and 24 days, at $6 \%$ ?
    2. What is the compound interest of $\$ 520$ for 3 Ans. $\$ 173.295$.
    3. What is the amount of sl28 for 3 y 5 years, at $5 \%$ ? at $6 \%$. compound interest?
    4. What is the $A n s$. $\$ 156.717$. payable semi-annually, at $6 \%$ ?
    5. What is the compound intoreat of $\$ 737.75$ for $\mathbf{2 1}$. $\$ 42.67+$. mami-annually, at $7 \$$ ?
    6. What will $\$ 900$ amount to in 1 year, at $7 \%$, compound interest, payatile quarterly?

    Ans. $\$ 964.67+$
    7. What is the amount of $\$ 500$ for lyr., interest payable every 3 months, compound interest, at $8 \%$ ?
    8. Find the comporind interest of $\$ 948$ for 3 years 4 months and 18 days, at $6 \%$ ?

    Ans. $\$ 207.051$.
    81\$. Compound interest may be computed more expeditiously by the use of the following

    TABLE
    Showing the amount of $\$ 1$, or $£ 1$, at $3,4,5,6,7$, and 8 per cent., compound interest, for uny number of years from 1 to 3.4 .

    | Years | 3 per cent. | 4 per cent. | 5 per oent. | 6 per cent. | 7 per cont. | 8 per oent. |
    | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
    | 1 | 1.030000 | 1.040000 | 1.050000 | 1.060000 | 1.070000 | 1.080000 |
    | 2 | 1.060900 | 1.081600 | 1.102500 | 1.12:3600 | 1.144900 | 1.166400 |
    | 3 | 1.092727 | 1.124864 | 1.157625 | 1.191016 | 1.225043 | 1.2:59712 |
    | 4 | 1.125509 | 1.169859 | 1.215506 | 1.262477 | 1.310796 | 1.360489 |
    | 5 | 1.159274 | 1.216653 | 1.276282 | 1.338226 | 1.402552 | 1.469328 |
    | 6 | 1.194052 | 1.265319 | 1.340096 | 1.418519 | 1.500730 | 1.586874 |
    | 7 | 1.229874 | 1.315932 | 1.407100 | 1.503630 | 1.605782 | 1.713824 |
    | 8 | 1.266770 | 1.368 .569 | 1.477455 | 1.593848 | 1.718186 | 1.850930 |
    | 9 | 1.304773 | 1.423312 | 1.551328 | 1.689479 | 1.838459 | 1.999005 |
    | 10 | 1.343916 | 1.480244 | 1.628895 | 1.790848 | 1.967151 | 2.158925 |
    | 11 | 1.35.4234 | 1.539454 | 1.710339 | 1.898299 | 2.104852 | 2.331639 |
    | 12 | 1.425761 | 1.601032 | 1.795856 | 2.012197 | 2.252192 | 2.518170 |
    | 13 | 1.468534 | 1.665074 | 1.885649 | 2.132928 | 2.409845 | 2.719624 |
    | 14 | 1.512590 | 1.731676 | 1.979932 | 2.260904 | 2.5785:34 | 2.937194 |
    | 15 | 1.557967 | 1.800914 | 2.07892 ४ | 2.396558 | 2.759032 | 3.172169 |
    | 16 | 1.604706 | 1.872981 | 2.182875 | 2.540352 | 2.952164 | 3.425943 |
    | 17 | 1.652848 | 1.947901 | 2.292018 | 2.692773 | 3.158815 | 3.700018 |
    | 18 | 1.702433 | 2.025817 | 2.406619 | 2.854339 | 3.379932 | 3.996020 |
    | 19 | 1.753506 | 2.106849 | 2.526950 | 3.025600 | 3.616528 | 4.315701 |
    | 20 | 1.806111 | 2.141123 | 2.653298 | 3.207136 | 3.869685 | 4.660957 |
    | 21 | 1.860295 | 2.278768 | 2.785963 | 3.399564 | 4.140562 | 5.033834 |
    | 22 | 1.916103 | 2.369919 | 2.925261 | 3.603537 | 4.430402 | 5.436540 |
    | 23 | 1.973587 | 2.464716 | 3.071524 | 3.819750 | 4.740530 | 5.871464 |
    | 24 | 2.032794 | 2.563304 | 3.225100 | 4.048935 | 5.072367 | 6.341181 |
    | 25 | 2.093778 | 2.665836 | 3.386355 | 4.291871 | 5.427433 | 6.848475 |
    | 26 | 2.156591 | 2.772470 | 3.555673 | 4.549383 | 5.807353 | 7.396353 |
    | 27 | 2.221289 | 2.883369 | 3.733456 | 4.822346 | 6.213863 | 7.988062 |
    | 28 | 2.287928 | 2.998703 | 3.920129 | 5.111687 | 6.648838 | 8.627106 |
    | 29 | 2.356566 | 3.118651 | 4.116136 | 5.418388 | 7.114257 | 9.317275 |
    | 30 | 2.427262 | 3.243398 | 4.321942 | -. 743491 | 7.612255 | 10.062657 |
    | 31 | 2.500080 | 3.373133 | 4.538040 | 6.088101 | 8.145113 | 10.867669 |
    | 32 | 2.575083 | 3.508059 | 4.764942 | 6.453387 | 8.715271 | 11.737083 |
    | 33 | 2.652335 | 3.648381 | 5.003189 | 6.840590 | 9.325340 | 12.676050 |
    | 34 | 2.731905 | 3.794316 | 6.253348 | 7.251025 | 9.978114 | 13.690134 |

    $964.67+$ every 3 hs and 18 07.0 s 1. editiously
    per cent., o 34.

    ## PROMISSORY NOTES.

    320. A Promissory Note is a written or printed engagement to pay, a certain sum either on demand or at a specified time.
    321. The Maker or Drawer of a note is the person who signs it and thus becomes responsible for its payment when due.
    322. The Payee of a note is the person to whom or to whose order it is made payable.
    323. The Indorser of a note is the person who signs his name on the back of it, and by so doing guarantees its payment, unless be writes "Without Recourse" over his name at the time.
    324. A Negotiable Note is a promissory note which is made payable to bearer or the order of some person ('ee Notes, Forms, 2, 3, 4).

    Nores.-1. If a note is payable to the bearer, it may be negocinted without indorselment.
    2. A note should contain the words " value received". and the sum for which it is given should be written ont in worls.
    365. A note may be male payable on demand, as in Form No. 1, or at the expiration of a certain time after its date, as in Forms Nor $_{6} 2,3$, and 4. A noto may he made payable to a particular person, as in Form No. 1 ; or to any person who is the bearer or holder of it, as in Furm. No. 2; or to the order of a person named in it, as in Form $N o .3$; and may be made payable at a particular place, as in Forme No. 4.

    The Note, Form No. 1, is due when the payee demands its pryment from the maker of it.

    Remark.-If no time ie fixed. in a note, it is payable on demnnd.
    The Note, Form No. 2, is payable to the holder of it at the expiration of six calendar months from its date.
    The Note, Form No. 3, is duc at the time specificd in it, to the saype who manter it. Jos. A. Walter may indur-w his mite in bhenk, that is to say, only write his name, and thus make any person law. fully holding the note, the payee; or, he may indorse it payable to the order of a particular person, in which case such person can make another person the payee, as Jos. A. Walter could, by indorsing the uote in blank or otherwise.

    The Note, Form No. 4, is payable only at the Bank named in it.
    326. The Face of a note is the sum named in it.
    327. Days of Grace are the three days usually allowed by law for the payment of a note after the expiration of the time specified in the note.

    3;38. The Maturity of a note is the expiration of the dayr of grace; a note is due at maturity.

    Rraark, -1. When a noto promises interest, as Forme 1, 2, and 3, the interest begins at the date of the note, and continues until the note is paid. If the time expressed in a note for its maturity bo stated in months, calendar monthe are understood; and if a note promises interest without stating the rate $\%$, it bears the legal interest of the country in whieh it is dited; also, a noto whigh does not promiso interest, if not paid when due, bears the same legal rate $\%$ of interest from the time it matures antil paid.
    2. If a note be not paid by its maker when it matures, it may on the same day be protested for mon-payment, and the indoisers may be required to pay it if they are at once notified of the proteot.
    3. If a note matures on Aumday or a logal holiday, it muat be paid en the day
    829. A Business Note is a note given for a valuable consideration. rt renders the maker liable for the amount to the payee, or to any subsequent bone fade bolder.
    330. An Accommodation Note is a note given for no vala able consideration. It does not render the maker liable to the payee, but makes him liable to any bonn file holder after it has been negotiated for value.

    Not. - Accommodation notes are usually given to enable the payee to borrow money on the credit of the makers of the notes.
    331. A Joint Note is a note signed by two or more persons, who are jointly liable for its payment. A Joint and Several Note is a note signed by two or more persons, who may be held, either jointly or singly, for its payment.
    332. A Produce Note is a written promise to deliver goods to a specified amount.
    333. A Due Bill is an acknowledgment of a debt due in money, or its equivalent in goods.
    334. A Bond is a written obligation, authenticated by a seal, to secure the payment of a sum of money for the performarice or non-performanoe of certain acts.
    335. A Mortgage or Mortgage Deed is a conveyance or' property given to secure the payment of a bond or debt, on condition that when payment is made, the conveyance is void and the mortgage is discharged.

    ## FORMS OF NORMS.

    ## Form No. 1. -Demand Note.

    3, the interest If the time $r$ inonthe are $\theta \%$, it bears which does not \% of interest
    the same day to pay it if
    allowed by of the time
    of the day
    $\$ 64 \frac{86}{80}$ Quebec, January 1.5 th., 1870 .
    On demand. of promise to pay OR. Eft Stasis, axcy:fous and $\frac{38}{100}$ dollies, with interest, at $5 \%$. Water Qincericed.

    Form No. 2.--Note Payable to Bearer (Negotiable.) $\$ 2$ 25.75. $\quad$ EAlontient, EFelvany 3, 1870. Ufir months after dute, Of promise to puy He of Cootion, of bearer, wo hundred sixtysfive and ing clotlass, with interast at $\sigma \%$. Oratuen received.
    (RTAMP.)
    e7. Ol. DPowet.
    Form No. 3.-Note Pafable to Order (Nequtiable).

    One yeat after date, $\odot$ promise to pray to the adet of ET, Ol. Slamson, ninety=nine and ${ }_{1070}$ dol: laws, with intesost, at 7\%. Olalue reocived.
    (oramp.)
    EO OF OByne.
    Form No. 4.-Note Payable at a Bank (Negotiable.)
    $\$ 87 \frac{80}{106}$.
    Earonta, Otpit 12, 1870.
    eforty days after dam, OF promise to pay to the ander of C. ©D. Etichots, at the Ontatio Obwne, oightyzeven and $\frac{90}{100}$ dothins. Qiutue received. crine.)

    Gohn EDouglas.

    Form of Produce Note. dotlass in goods, at out cone.
    (stamp.)
    OS. Michaut \& Ca

    ## Form of Due Bill.

    ## $\$ 103$.

    Ottarere, June Y, 1870.
    Quo Edward CY. Llushin, for values vecovivod. one hundred and three dollars, with insodow. (07akp.)
    

    ## PROFIT AND LOSS.

    336. Profit and Loss are commercial terms, used to express the gain or lows in business transactions.
    337. There are four terms or quantities to be considered is Profit and Loss, viz. :-
    1st. The Cost, or original number, which is the Base.
    2nd. The Rate \% of gain or loss, which is the Rate \%.
    3rd. The Gain, or Loss, which is the Percentage.
    th. The Selling Price, which is the Amount, or Difference.
    The questions follow the same rules as in Percentage.
    Selling Price $=$ Cost + Gain, or Cost - Loss.
    Cost $=$ Selling Price - Gain, or Selling Price + Loss.
    Gain $=$ Selling Price - Cost.
    $\boldsymbol{L}_{\text {oses }}=$ Cost - Dolling Prices.

    ## EXAMPLES FOR PRAOTICE.

    1. I bought cloth, at $\$ 2.50$ per yard, and sold it so as to gain $25 \%$; for how much did I sell it a yd.?

    Ans. \$3.121.
    To solve this Example, eee Case I., 282, Hole.
    2. A farm was bought for $\$ 4500$, and sold so as to gain $\$ 900$; how much was the gain \%?

    Ans. 20 \%.
    Te solve this Example, see Caso II., 284, Roli.
    3. By selling' a building lot, a man gained $\$ 175$, which was $12 \%$ of the cost; what was the cost ?

    Ans. \$1458.331.
    To colve this Example, see Case III., 286, Rute.
    4. A gentleman sold a horse for $\$ 180$, and thereby gained $20 \%$; what was the cost of the horse?

    Ans. $\$ 150$.
    2e colve this Examplo, ace Case IV., 288, Rule.
    6. A merchant lost $15 \%$ on his old stock of goods; how much did be lose on those that cost $12 \frac{1}{2}$ cts., $\$ 6 \frac{2}{3}, 38 \frac{1}{8}$ cts., $33 \frac{1}{3}$ cts., and $\$ 18 \frac{1}{3}$ ? Ans. 17 cts. $; \$ 1 ; 5 \overline{3} \mathrm{cts}$; eto.
    6. Bought sugar, at 12 cts . a pound, and sold it so as to gain 1 t the. a pound; required the gain $\%$.
    7. Sold butter at of a dollay a puund, which was at a gain of $25 \%$; required the cost per pound. Ans. $66{ }^{2}$ ets.
    8. A market woman sold oranges 80 as to gain of a cent on eaoh orange, which was at again of 334 ; what was the cost of an orange ?

    Ans. 2 cents.
    9. Suld a horse at $33 \frac{1}{3} \%$ gain, and with the money bought anothe: horse, which I sold for S. 20, and lost $25 \%$. Did I gain or lose by my trading? and how much?
    10. If I make a profit of $15 \frac{5}{1 \mathrm{I}} \%$ by selling paper for s" 0.85 ahove the cosst per ream, how much must be added to the selling price to realize a profit of 32 \% ?

    Ans. 93 ets.
    11. What phould I sell a barrel of flour for, that cost me £1 26 , to gain $16 \frac{2}{3} \%$ ?

    Ame \&1 63.
    12. A neighbor offers his house, which cost him $\$ 6910$, for $20 \%$ lees than coot ; what in his price?

    Ans. $\$ 5520$.
    13. A merchant selle cloth for $\$ 5$ a jard, which cost him $\$ 3.75$ a Jand; what is his gain per cent.?

    Ans. 33$\}$.
    14. I bought 640 yards calico at 15 ots. per yd., and sold it at a seduced price of $21 \%$; what did I lose ?

    Ans. $\$ 2.40$. -15. A grocer sells coffee at 7 J d . a lb . Which cost him 9 d .; what is his lose per cent.?
    16. A merchant buys at auction $\$ 9562.50$ worth of goods; it he sell them at an advance of $20 \%$ on the cost, what will be his net profita, deducting $\$ 600$ for expensee ?

    Ans. \$1312.50.
    17. How much should I sell differant qualities of sugar which cost 0 \&1 15, 2213 , and 22-12 6 the owt., to gain $12 \frac{1}{2}$ \% ? 5 weeks, and then sold him for paid $\$ 6$ for his nourishment during tine whole cost? was my gain per cent.? 21. A grocer sold tea which cost 3 s .1 dd . for 3s. 9d Ans. $16 \%$.
     was his gain per cent. on each article? Ans $20 \%$ for the 9 ; what 22. Bought 9 cwt . 72lb. of sugar for $\$ 65 \mathrm{~ns} .20 \%$ on the tea; etc. drayage; at how much per pound shoulp ; paid $\$ 5.15$ for freight and the buying price ? 23. A dealer in furs made uproft of $\$ 166$ in alling Ans. $\$ .08$. tity at $12 \%$ advance; what was the of mount sold? 24. A merchant bought a hogshead mount sold ? Ans. $\$ 1300$. been lost by leakage, he sold the read of wine for $\$ 189$; a part having found that his loss was $5 \%$ on the remainder at $\$ 3.99$ per gallon, and lose by leakage?
    25. Sold a cargo of corn for $\mathcal{E 4 0 0 0 , 4}$ at 25 Ans. 18 gallona. cargo cost ?
    26. Ia selling ts 40 I have gained had 1 sold it at $\$ 1$ a pound? $20 \%$; how much would 27. By selling cloth at $\$ 4$ the yard, I lose $20 \boldsymbol{\alpha}$; whe Ans. $32 \frac{1}{8} \%$. 28. What will I ga n per cent. by selling silks what was the cost? \$4.25?
    29. By selling lar $\mathcal{1}$ at fl 15 s . per owt. I gain Ans. $17 \frac{14}{4} \%$. would I gain or lose by selling it for 18 s. ? gain $75 \%$; how much $x$ 30. Sold wheat at $\$ 1.25$ the bushel thereby $\Delta n s$. Lose $10 \%$. per cent. would I have gained had I sold it a loeing $15 \%$; how much
    31. Lost $15 \%$, by selling a lot of paper at $\$ 1.647 \frac{1}{1}$ the bushel? should I have sold it to gain $12 \%$ ? paper for $\$ 480$; for how much 32. Sold a feld containing 106 A . 3R. 30nd Ans. $\$ 632.4705+$. making a profit of 18 \% on the coatt. 30rd., at $\$ 120$ an acre, thereby 33. Tea, sold at $25 \%$ loss, is $\$ 1.25 \mathrm{a}$ lh did the seld cost? or loss per cent. in selling it at $\$ 1.60 \mathrm{a} \mathrm{lb}$. ? what would be the gain 34. A lumber merohant sold 36840 feet of wood at Ane. $4 \%$ loss. and gained 28 \% ; how much would he have wood at $£ 5578$ per M., the wood at $£ 45$ per M. ? 35. The retail prices of my goods are $40 \%$ above the cost. I supply my customers wholesale at a reduction of $12 \%$ on the retail price; what is my profit on the goods sold by wholesale? ? the retail price; 36. An engineer sold an engine for $\$ 8812.50$ and lost 6 . $23 \frac{1}{5} \%$. cost; what should it have been sold for to gain 121 $\%$ ? $6 \%$ on the 37. I sold a horse at an advance of 30 gain $12 \frac{1}{2} \%$ ? bought another which $I$ sold for $£ 45 \quad 10$, losing and with this money horse cost me?
    38. A speculator sold Ane. lat. horse $£ 40 ; 2$ nd. what did each and realized a profit of the goode of a store at a reduction of 7 . tought?
    39. My retail price for grty unי" in \$4.75 per yd., by which I make a profit of $331 \%$. I sell 100 yd . by wholeoale at $30 \%$ reduction on the retail price. What is my gain or loss per cent., and how much do I receive a yard?

    Ans. $6 \frac{2}{2}$ lose ; $\$ 3.32 \frac{1}{2}$ a yd. a profit of $\delta \%$; what is the cost of a more than the cost and realizes 41. A grocer demanded for a cert.inard? Ans. $31 \frac{1}{4}$ cts. above the cost; but being a little musty, he sold them at $10 \%$ less than his first demand, and thus gained $\$ 98$ by the sale; what was his first demand?
    42. At what price should I sell codish which costs 16 s . $5 \frac{4}{5} \mathrm{~d}$. per cwt. to realize a profit of $12 \frac{1}{2} \%$ on the cost, after deducting $12 \frac{1}{2} \%$ of the price?

    Ans. £1 $12 \frac{1}{3} \frac{1}{5}$. weight to be 5 of tes. weight to be $5 \%$ less than that calculated, and $10 \%$ of the sales to be in baid debts, for how mueh must it be sold a puund to make a net profit of $14 \%$ on the cost?

    Ans. 16 cents a pound.
    44. J. Moran \& Co. bought dry goods for the amount of $\$ 6840$; they sold $\frac{1}{4}$ at $15 \%$ profit, at $18 \frac{\pi}{2} \%$, $\frac{1}{6}$ at $20 \%$, and the remainder at $331 \%$ profit ; what was their total profit?

    Ans. \$1482.00.

    ## COMMISSION AND BROKERAGE.

    335S. Commission and Brokerage are the percentages paid an agent, or broker, for the transaction of business, and is estimated at a certain rate per cent. on the amount of the sale, purchase, collection, eto., effected.
    3339. An Agent, Factor, Broker, Collector, or Commission Merchant, is a person who transacts business for another.

    Nores.-1. An agent may be a Special Agers, -that in, authorized to transact moly such busine: as is specified,--vr a Geweral Agent, who, ae such, osn craisact any buginess of the persod who employe him.
    2. Merchandise and Produce sunt to a person for esle or superintendence, are raid to bo consigned. The person sending them is termed a Consignor; the person to whom they are sent, is termed a Cousignee.
    3. A consigof o whose business office is remote from a consignor, is cometimes termed a Corregiondent, and usuaily acts as agent of the firm oonsigning him the goods.
    4. Brokers are classified aceording to the nature of the eales and contraots they effect. Thus, a Bill Broker is one who negotiates the uiscount on bilis of exchange, etc. : a Real-Listate Broker is ono who negotiates the saie of housos and lands; Lasurauce Broker, Ship Broker, Stock Broker, Pawit Broker, ete.
    j. A collector my have the business of settling accounts betweon individuals, or he may be an cfficer of the government, at a Collestor of the port, Whose businese is to aullect dutien ; a Collector of Traxes, ote.
    340. The Net Proceeds is the amount received from a sale or colleotion, less the commission and other charges.

    Questions on Cemmission and Brokerage follow the same rules as those in Percentage.

    EEAMPLES FOR PRAOTICK.

    1. A broker sold $\$ 15800$ worth of stosk for $C$; required his broker age at $\frac{1}{4} \%$ ?

    Ane. $\$ 39.50$.
    To solve this Rxample, $\infty$ Oeco I., 282, Rewn.
    2. An agent received $\$ 1600$ for selling a houm and lot for $\$ 25601$;
    what was his rate of commianion?
    
    3. A commission merchant reoeiven $\$ 84$ for selling wood, at $51 \%$; What is the smount sold ? To solve this Eliamples, ace Oco III., 285, Reser.
    4. An agent receivee 8105 to be invested in dry goods; after retaining his commiseion, 31 x , how mach was invected ? Ans. $\$ 3000$. To eolve this Exampto, en Ceso IV., 288, Rols.
    6. What 18 the commisaion on $\$ 874$, at 2 \& $\%$ on $\$ 71.50$, at
     Ame. $\$ 19.66 \frac{1}{2} ; \$ 2.501$; etc.
    6. What is the commicsion on $£ 15910$, at 3 \% on $£ 170106$,
    
     7. How much will I puy for the brokerage of $\$ 750$, at $\frac{1}{3} \%$ ? of $\$ 1540.40$, at ${ }^{2} \$$ ? of $\$ 3610.80$, at 1 द \%? of $\$ 823.50$, at $\%$ ? of \$1560.70, at $1 k \$$ ?
    8. Sold merchandise an followa. Ame $\$ 1.871$; $\$ 7.702$; etc. mission; 2nd. for $£ 16116$ ows ist. for $£ 942160$, at $4 \frac{1}{3} \%$ com. for £530 05 , at $34 \%$; what is the ; 3rd. for $£ 31057$, at $6 \%$; 4th. 9. What amount of brokerege the com.? Ans. £80 $751+$. becks, as follows: $\$ 590$, at 26 must I pay for exchanging green$30 \%$; $\$ 4532.09$, at $32 \%$; $\$ 87.30$; at $29 \%$, at $28 \%$; \$1615.72, at
    10. A farmer maid a boade; what the brokerage? $7 \%$ for investing $\$ 11730$, in Ontario
    11. $A$ moker rmaived \$iss for breying stooks Ans. $\$ 102.637+$. how mech monk did he bay? boying stoaks, at $\frac{5}{8} \%$ brokerage,
    12. A flour merchant remits the in ${ }^{\prime}$ Ans. $\$ 740 a$. the purchase of grain, after do his agent in Toronto $\$ 4740$ for much will the agent expend doducting the commission at $2 \mathrm{\$}$; how commission? (ise mend for his employer, and what will be his
    13. An agent sold. $\$ 4647.06-$, for grain ; $\$ 92.94$ + for commis. $\$ 10095.36$ to the orner estate on $4 \%$ commission, and remitted ell the property, and as the net proceeds; for what prioe did he
    14. An
    a head; after reserving his 4920 to expend in purchasing cows $\mathbf{*} \$ 32$ he purchase?
    15. A merchant havies on hand $470 c$, Ans. 150. rgent 34 \% for selling it ; what are thenet ancols of sugar, gawe an
    16. I purchesed 6000 busheie of wheat in Buthlo, at 81.37 , and shipped the same to iny agent in Kingston, who eold it at $\$ 1.62 \mathrm{z}$ How much did I make, after paying $\$ 543$ for expenses and a commir sion of $23 \%$ ?

    Ans. $\$ 723$.
    17. A broker charged to $54 \%$ for the exehange of $£ 681410$ in freenbacks; what was his brokerage? Ams. $£ 35153\}$.
    18. A commission merchant suld a consignment ot oats for $\$ 12686$. He charged $\$ 66$ for storage, and $6 \frac{1}{4} \%$ commission; what were the net proceeds?

    Ans. $\$ 11827.121$.
    19. An architect charges $\frac{2}{8} \%$ for his plan and survey of a building which cost $\$ 24000$, and $13 \%$ for superintending the work; how much did he receive?

    Ans. $\$ 450$.
    20. I sent to my correspondent in Bordeaux $£ 2097$ 10, with advice to invest in the purchase of wines, after deducting his commiseion of $3 \frac{1}{2} \%$; what was the sum invested and what was his commiseion? Ane. £2026 1144 , wines; $£ 70187 \frac{1}{5}$; commission.
    21. An agent having a debt of $\$ 157$, to collect, compromises for $90 \%$; what was his commission at 53 \%: Ans. \$77.71 1.
    22. Paid Folger Brothers $\$ 5.46$ for exchanging $\$ 364$ in United States' money; what was the rate of brokerage? Ans 11\%.
    23. A consignee in Glasgow informs his constituent of the purchase of Try Goods to the amount of $£ 395155$; what is his conmission at $21 \%$ ?

    Ans. $£ 8 \quad 181+$.
    24. Bought at Halifax a cargo of wheat, 9500 bashels, at $\$ 1.20$ per bushel, and sent it to my agent in Portland who sold it at $\$ 1.50$ per bushel; what did I realize on the whole after paying $\$ 320$ for expenses, and commission at $31 \%$ ?

    Ans. $\$ 2031.25$.
    25. My correspondent at Bordeaux charges $\$ 74.20$ for purchasing 264 owt . of honey at $\$ 10.50$ per cwt . ; what was the rate of commio sion?

    Ans. $287 \%$.
    26. A broker receives $£ 208576$ comprising the sum to be invested in Rasiroad stock at $£ 2015$ a share, and his brokerage at $\mathbf{1 \%}$; how many shares can he buy, and what is his brokerage?
    $2 \%$. A vertain piece of land was sold for $\$ 3925$, but the owner st ceived $\$ 3866.12 \frac{1}{2}$ as the net proceeds; what was the rate of commiseion ?

    Ans. $11 \%$
    28. I remitted $\$ 5500$ to my brokor with advice to invest in Bank stock, after deducting hie brokerage at $\%$ \% ; what was the investment 9
    29. The net proceeds of a sale were $£ 1408 \mathrm{l6}$, and the commission, f28 16 ; what was the rate of commiseion?

    Ans. $2 \%$.
    30. In charging $1 \frac{1}{2} \%$ for the investment of a certain sum, a broker realized $\$ 285$; what was the amount of the investment ? $\mathbf{A} . \$ 19000$.
    31. My agent in Cincinnati gives me information of the purchase of 4000 bushels of indian meal at 80 cts. per bushel, and desires me to remit a check ou New Yort تhich he can sell to a broker at $\frac{3}{4} \%$ preminm; what should the anount of the chects be, his commission being $3 \%$ ?

    Ans. $\$ 3271.464$.
    32. $\mathbf{A}$ factor received £6́ 12 for the ale of grain at $4 \%$ commis sion; what was the amount sold ? Ans. £140.
    38. Beceived from $\mathbf{A} \$ 700$ in specie; paid $3 \frac{1}{2} \%$ for changing it to
    gold; and, after deducting the commission at $2 \%$, employed the bal. ance in the purchase of fruit; what was paid for the fruit; and what was the commisuion? Ans. stifi.99, fruit; Sl3.il commission.
    34. Remitted to my correspondent at Rouen $£ 255$, for the purchase of calico at 9 d . per yard, after deductirg his commission at $2 \%$; how many yards will I receive?
    35. A speculator rec ${ }^{-}$ves $\$ 4113.50$ as the net proceeds of a sale, allowing $5 \%$ commission; what was the value of the property?
    36. A commission merehant who sharges 5 \% commission on sales and investments, receives 260 cwt . of cheese, at 6d. per lb ., and $£ 748$ 106 , in cash, with advice to purchese a cargo of cotton for the whole amount; what will be his total cou mission? Ans. £971:11.
    37. A Halifax agent buys 34 boxes of chocolate; he pays $\$ 7.50$ for freight and cartuge, and his commission is $1.2 \%$ on the amount of the purchase. He sends me a bill of $\$ 740.83 \frac{3}{4}$ for the whole; what war his commission; and, allowing 2501h. per box, how much did I pay per lb. for the chocolate? Ans. $\$ 10.83 \frac{3}{4}$ com. ; $\$ 0.08 \frac{1}{2}$ per 1 lb .
    38. A commission merchaut receives 125 barrels of flour from $A$, 150 bbl . from $\mathrm{B}, 225 \mathrm{bbl}$. from C ; he finds on inspection that $\mathrm{A}^{\prime} \mathrm{s}$ is $10 \%$ better than $B ' s$, and $\mathrm{C}^{\prime}$ в is $5 \frac{8}{11} \%$ better than $\mathrm{A}^{\prime}$; ; he sells the whole lot at $\$ 7$ per barrel, and charges $4 \%$ comnisaion. How much must be remit to each ? Ans. $\mathrm{A}, \$ 842.30 ; \mathrm{B}, \$ 918.87$; $\mathrm{C}, \$ 1598.83$.

    ## INSURANCE.

    341. Insurance is a contraot of indemnity, by which one party engiges, for a stipulated sum, to insure another against a risk or loss to which he is exposed.
    342. It is of two kinds: insurance on property, and insurance on life (1).
    343. The Insurer or Underwriter is the party taking the risk ; and the Insured or Assured, the party protected.
    344. The Policy is the written obligation or contract.
    345. Premium is the sum paid for insurance. It is alway reckoned at a certain per cent. on the value of the property in. sured, varying according to the degree or nature of the risk ar sumed.

    ## FIRE AND MARINE INSURANOE.

    346. Insurance on property is of two kinds: Fire Insurance, and Marine Insurance.
    347. Fire Insurance is an indemnification of damage and loss caused by fire or lightning.
    348. Marine Insurance is an indemnifiontion of damage and loss caused by the perils peculiar to navigation.
    349. In insurance, the calculations are based on the following principles:
    I. Premium is percentage. (278)
    II. The sum insured is the bane of preminm.
    [II. The sum covered by insurance is difference.

    ## EXAMPLES FOR PRAOTIOE

    1. What premiam must be paid for inouring goode to the amonat of $\$ 4500$, at $23 \%$ ?

    Ans. $\$ 112.50$.
    To solve this Example, eoe Case 1., 282, Ryne
    2. A man paid $\$ 64.80$ for the insuranoe of $\$ 8640$ on his house; what wae the rate of incurance?

    Ans. 1 \%
    To solve this Examplo, wo Cace II., 204, Dinn.
    3. The preminun iners insuring a tannery for of its value, at $12 \%$ was $\$ 145.60$; required the value of the tannery. Ans. $\$ 11648$.
    To colve this Hzample, ase CamiII. 288, Rote
    4. What must be paid for an insurance of $\$ 5728$ at $18 \$$ ?
    6. What premium must be paid for the inaurance of a reasel and cargo valued at £ 3649 8, at 3$\} \%$ ? Ans. £118 $121 \&+$.
    6. A schooner, insured for $\$ 5000$, at $24 \%$ was completely wrecked; how mach of the lose was covered by the insurance? A. $\$ 4887.50$.
    7. A hotel valued at $£ 3750$ is insured for $\%$ its value, at $\frac{3}{8} \%$. The policy and survey of the premises are charged 78. 6d.; what is the insurance?
    8. A store and its artock worth 56370 Ans. £9 150. sured, at 2 os, to eover both property and ; what sum must be in
    9. What is the premium property and premium? Ans. $\$ 6500$.
    10. I pay annually $\$ 4$ : insursace for $3 \%$ of the amonnt for ahich I am insured; ibrary, and this sum is
    11. What is the premium am insured; what is the amount? $\boldsymbol{£ 3}$ if $8 \%$ ?
    12. A business maw, hering 912000 Ans. £56 $199 \frac{1}{2}+$. cured for 毛 of their value, at $\frac{1}{6}$; if in orth goods, gete them in$\$ 2000$ of the stock, what real $\%$; if, in a conflagration, he saves but
    13. For what sum muat a house, valued at $\$ 8274$, Ans. $\$ 472$. \%, to cover the entire lose, in ease it is 14. My goods them to cover, in case of loss, both premium sum must I insure $56 \%$ ?

    $$
    \begin{aligned}
    & \text { 15. The premium of a achoothouse, insured at } 11 \text { Ant. £1600. }
    \end{aligned}
    $$ What sum was it insured ? $11 \%$, is $\$ 50$; for 16. An Insurance Company, atter having ingured a Ans. $\$ 4000$. ing for $\$ 35000$, at $21 \times$ roinsure the is at 8 insured a block of buildof prominn ?

    17. For what sum must goods wurth $£ 1938126$ be insured to cover both premium and goods in case of lose, the rate being 5 5 ?
    18. A brig estimated at $\$ 40000$ is incured for $\frac{8}{4}$ of its value at $13 \%$, and its cargo, worth $\$ 36000$, at $\frac{4}{5} \%$; what is the insurance?
    19. A merchant paid $\$ 1450$ for premium of insurance on a cargo of cotton coming from Havana, the rate of insurance being $2 \frac{1}{2} \%$; what was the value of the sargo?
    20. I paid sit for an insurance of $\$ 1200$; what is the rate of the premium?
    21. T'o $£ 5791610$, add $73 \%$ commission, and find Ans. $1 \frac{1}{2} \%$. of the sum, at $4 \%$ ?
    22. A merchant, $A$ Ans. £27 $54 \frac{3}{4}+$. $80 \%$ of its value at $31 \%$ and argo of 500 bbl . flour, has it insured for the price per bbl.?
    ; what was
    23. A ship-owner has two of hig vogola inoumd Ans. \$8.25.
    24. A ship-owner has two of his vessels insured for $\$ 30000$ in the Royal Insurance Co., at $\frac{8}{4} \%$, and for $\$ 45000$ in the Colonial Insurance Co., at $3 \%$; what is the rate of premium for the whole insurance?
    25. A house estimated at $£ 300$ was insured for ${ }_{3}$ of its value, during 3 years, at $1 \%$ per anmum. Towards the end of the third year, it was destroyed by fire; "wat is the actual loss of the proprietor without any allowance of interest? Ans £106.
    26. My house was insured for $\$ 45000$ during 5 years. The first year I paid $\$ 1.50$ for the policy and plans, and $\frac{6}{8} \%$ premium; every succeeding year, I paid $\frac{1}{2} \%$ premium. The house having been destroyed the fifth year, what was the loss of the insurance, no interest having been allowed?

    Ans. $\$ 43817.25$.
    26. I paid $\$ 46.75$ for insuring a store for the $\frac{1}{2}$ of its value. at 18\%; what is the store worth?

    27 . I took a policy of $£ 30115$ for the the value of both property and premium; what is the worth of the insured property, the rate being 3 ?
    28. A shipment of wheat was insured at $23 \mathscr{5}$, to cover $\frac{3}{4}$ of its value; the premium paid was $\$ 44.07$; the wheat being worth 80 cts. per bushel, how many bushels were shipped? Ans. 2825 bu.

    ## ASSHSSMENT OF TAXES.

    350. A Tax is a sum of money assessed on the person or property of an individual, for public purposes.
    351. When a tax is assessed on property, it is apportioned at a certain per cent. on the estimated value. When assessed oa the person, it is apportioned equally among the male citizens liable to assessment, and is called a poll tax.
    352. Property is of two kinds, viz. : real estate, and personal property.
    353. Real Astate is ficed or immovable property, suoh as lands, houses, otc.
    354. Personal Property is movable property, sueh as money, stooks, furniture, cattle, etc.
    355. An Inventory is a written list of articles of property. with their value.
    356. A Schedule is a list of taxible property with its owners' names and its value as estimated by assessors.

    357 . Assessors are officers appointed to make out a schedule of taxable property, and apportion taxes thereon.

    Ex. A tax of $\$ 840.75$ is to be raised in a cown containing 65 polls; the taxable property of the town amounts to $\$ 48000$, and each poll tax is 75 cts . ; what will be the tax on a dollar, and how much will be C's tax, whose property is valued at $\$ 5600$, and who pays for 2 polls?

    ## operation.

    $\$ 0.75 \times 65=\$ 48.75$, mount assensed on the polls.
    $\$ 840.75-\$ 48.75=\$ 792$, ant. to be assessed on the property.
    $\$ 792 \div \$ 48000=\$ 0.0165$, tax on $\$ 1$.
    $\$ 5600 \times \$ 0.0165=\$ 92.40, \mathrm{C}$ 's tax on property.
    $\$ 0.75 \times 2=\$ 1.50$, C'a tax on 2 poll. .
    $\$ 92.40+\$ 1.50=\$ 93.90$, amount of $C$ 's tax. Hence the
    358. Role:-I. Find the amount of poll tax, if any, and subtract it from the whole tox to be raised; the remainder will be the property tax.
    II. Divide the property tax by the whole amount of taxable property; the quotient will be the per cent., or the tax on $\$ 1$.
    III. Multiply each man's taxable property by the tax on \$1, mad to the product .uld his poll tax, if any; the result will be the shole amount of his tax.

    ## EXAMPLFS TOR PRACKICE

    1. The tax assessed on a certain town is $\$ 1485$; its property, both personal and real, is valued at $\$ 42000$, and it contains 300 polls, Which are assessed 75 cts a piece. What per cent. is the tax; that is, how much is the tax on a dollar; and how much is A's tax who pays for 3 polls, and whose property is valued at $\$ 2250$ ?

    $$
    \text { Ans. } 3 \text { cts. on } \$ 1 ; \$ 19.75, \mathrm{~A}^{\prime} \text { 's tax. }
    $$

    2. What is the tax of a non-resident, having pruperty in the same town, worth $\$ 7900$ ? Ans. \$
    3. How much will B's tax be, in the same town, who pays for 3 polls, and whose real estate is valued at $\$ 32000$, and his personal property, at $\$ 18880$ ?

    Ans. $\$ 1528.65$.
    4. What sum must be assessed in order to raise a net amount of \$1II23, and pay the commission for colleating at $21 \% \%$
    5. The expense for repairs of a public building was $\$ 2521.06$, which was defrayed by a tax upon the property of the town. The rate of taration was $3 \&$ mills on one dollar, and the oollector's 00 mmission was $31 \%$ : what was the valuation of the property f Ame. $\$ 803843.69+$
    deh as money, of property, 'h its owners' at a schedule ing 65 polls; id each poll v much will pays for 2
    property.
    the
    $f$ any, and nder will be
    of taxable on $\$ 1$.
    tax on \$1, twill be the
    perty, both 300 polls, e tax ; that 's tax who

    A's tax. the same \$
    pays for 3 is personal $\$ 1528.65$. amount of l.06, which ate of tazanission was $3843.69+$

    ## OUSTOM-HOUSE BUSINESS.

    359. Duties, or Customs, are taxes levied on imported goods, for the support of government and the protection of home industry.

    36©. All goods coning into the Dominion of Canada from Foreign countries are required by law to be landed at certain places or ports oalled Ports of Entry. Every Port of Entry has - Custom-House.
    361. A Custom.House is an office established by government for the transaction of business relating to duties. The officers attached to it are oilled Custom-House Officers. Their business is to inspeet the cargoes of all vessels entering at any of these ports; to inspeot the invoice of goods, collect the duties, etc.

    Notis.-1.-Benides the duties on merohandise, all vessels engaged in commerce are required to pay certain charges for the privilege of entering the port, eto. ; these oharges are called harbor dues.
    2. To carry on foreign eommeroe seoretly, without paying the duties imposed
    362. Duties are of two kinds - Ad Valorem and Specific.
    363. Ad Valorem Duty is a oertain per cent. on the cost of goods, as stated in the ingoioe.
    364. Specific Duty is a tax computed on the weight or measure of the goods, without regard to their cost ; hence, allowanoes are made before computing the duty.
    365. An Invoice is a statement of goods, from the seller to the buyer, or importer, showing the quantity and prioes of the articles.
    366. In the United States Custom-Houses, certain legal allowances are made for draft, tare, leakage, eto., before specifio duties are imposed. In Canada, however, these are not known, the tare being found by actually weighing one or more of the bozes, etc., containing the goods, and the leakage by gauging the calsk.

    Nors.-At present, the various kinds of spirits are the only artioles upon which specifio duties are eharged by the Canadian Tariff.
    367.-To compute ad valorem duties.

    Ex. What is the ad valorem duty, at $18 \%$, on an invoice of merino which cost \$256.60 ?

    ## operation.

    $\$ 266.50 \times .18=\$ 46.17$, Ans.
    368. Rilk. - Find the percentage on the invoiced value of the goods, at the given rate of tariff, and the result will be the ad valorem duty.
    3699. To coupute specific duties.

    Ex. What is the duty on 4 hogsheads of sugar, each weighing 1280 lb ., gross weight, at 2 cts. \& pound ; tare $14 \%$ ?
    $1280 \times 4=51201 \mathrm{~b} ., \mathrm{gr}$ grosn weight.
    $5120 \times .14=716.81 .$, tare.
    $5120 \times 716.8=4403.216$, net value.
    $4403.2 \times .02=\$ 121.018$, duty.

    Analysis. - We first find the Whole weight of the invoice which is 5120 lb . From this amount wo deduct the allowance for tare, 716.8Ib., and ocmputo the duty on the remainder. Hence the following

    87(1). Rule.-Deduct allowances, if necessary, and compute the duty, at the given rate, on the net value.

    ## EXAMPLES FOR PRACTIOR

    1. What is the ad valorem duty, at $19 \%$, on 15780 lb . of cordage, invoiced at 15 cts. per lb. ? Ans. \$449.73.
    2. At 7 cts. a pound, what is the specific duty on 346 kegs of tobacco, each weighing 130 lb ., allowing $6 \frac{\mathrm{lb}}{} \mathrm{l}$. per keg for tare ?
    3. At 30 cts. per gallon, what is the specific duty on 40 hhd . of wine, each gauging $58 \frac{1}{2}$ gallons?
    4. What is the duty at $33 \boldsymbol{q}$, on a bale of Holland linens which cost \$1593.50? Ans. $\$ 525.85 \frac{1}{2}$.
    5. What is the duty, at $20 \%$, on an invoice of broadeloth which ccst in Liver! , wl $£ 65710$, the pound sterling being valued at $\$ 4.86 \frac{2}{2}$ ?
    6. What is the specific duty, at 10 cts. per lb., on 25 chests of tea, each weighing 120 lb . ; tare $10 \%$ ?
    7. What was the rate $\&$ of duty on whose invoice value was $\$ 2250$, and for which $\$ 337.50$ duty was paid?

    Ans. 15 \%.
    8. A merchant imported 64 casks of wine, each containing 42 gal . net, the duty at $30 \%$ amounting to $\$ 1036.80$; at what price per gal. was the wine invoiced?
    9. A merchant in Montreal makes an importation of goods invoiced ut $\$ 16448$. On goods invoiced at $\$ 2400$, the dutien were at the rate of $4 \%$; on goods invoiced at $\$ 3360$, the duties were at the rate of $15 \%$; goods invoiced at $\$ 4800$, were free of duty; and on the remainder, the duties were at the rate of $30 \%$; what was the whole amount of the duties? Ans. $\$ 2366.40$.
    10. What is the duty at $18 \%$ on 60 kegs of prunes, each weighing 1 ēt., invoiced at 掊cts. per 1 b . ; tare at $3 \frac{1}{3} \%$ ?
    11. A. Hamel \& Bro., of Quebec, import from Manchester 15 pieces of Belgian caspeting, 40 yd. each, purchased at 58. per yd,, duty $24 \%$; 300 yd . of merine, at 4. per Jd., duty $19 \%$; 150 yd . Iriah linen, of

    ## DIBOOUNT AND PRESENT WORTH.

    208 2s. 6d., duty $15 \%$; and leather to the cont of 280 , duty 4 \%. What is the whole amount of duty, allowing the value of the ponid sterling to he $\$ 4.863$ ?
    12. S. R. Wilson \& Co., of Toronto impors. Ans. $\$ 261.88+$. 48 pipces of linen of 32 yd., of Toronto, imported from Athaterdam at $\$ 4$ Ob, $\$ 184.32$, and other each, on which they paid for the duties. tran the invoice value per yd charges to the amount of $⿻$ \$61.44. What charges were paid ?

    ## DISCOUNT AND PRESENT WORTR.

    371. Discount is an allowance or deduction made for the payment of a debt before it is due.
    372. The Present Worth of a note or debt, payable at a future time, without interest, is sach a sum as, being placed at legal interest, will amount to the given debt when it becomes due.
    Ex. What is the present worth and diecount of $\$ 25.44$, at $6 \%$,
    rayable in 1 year?

    OPERATION. \$ 1.06 , amount of $\$ 1$. $25.44 \div 1.06=\$ 24$. 25.44 , given sum. 24.00, present worth. \$1.44, discount.

    > ANalysif, Sinee $\$ 1$ in the present worth of $\$ 1.06$, it is evident that tho present worth of $\$ 25.44$ will be as many dollars as 1.0 is contained in 25.44 , or $\$ 24$. We find $\$ 24$ to be the present worth which, rubtraoted from the given sum, gives $\$ 1.44$ disoount. Henee the following
    373. Role.-I. Divide the given sum by the amount of $\$ 1$ worth.
    II. Subtract the present worth from the given swm, and the remainder will be the dISOOUNT.

    ## By proportion.

    I. To determine the present worth :-
    $100+(6 \times 1): 100:: 25.44: x=\mathbf{8 2 4}$; whenee the following formula: One hundred plus the rate multiplied by the time, is to one hundred as the given sum is to x , or the present worth of this sum. II. To determine the discount:$100+(6 \times 1): 6 \times 1:: 25.44: x=\$ 1.44$; whenee the
    following formula:

    One huldred plus the rale multiplied by the time, is to the rate multiplied by the time, as the given sumn is to $\mathbf{x}$, or the discount of inis aum.

    Notes.-1. The terms present woorth, dicoount, and tebt, are equivalent to principal, interest, and amowne. Hence, when the time, rate, \% and annount are given, the prinoipal mny be found by Case III., (311) ; and the interest by subtraoting the principnif from the amount,
    2. When payments are $t o$ he made at different times without interest, find the present worth of each payment separately. Their sum will be the present worth of the several nayinents, and this num subtraoted from the sum of the several paymente will leave the total discount.

    ## EXAMPLES TOR PRAOTIOE.

    What is the present worth of the following notes: $(1)$1. Dated Feb. 3rd., amounting to $\$ 104.60$, on 5 months' credit, diesounted June 6th., at 5 \% ?

    Ans. $\$ 104.20+$.
    2. Dated March 4th., mounting to $£ 58105$, on 7 months' credit, discounted Aug. 10 th., at $4 \%$ ?

    Ams. £58 35 +.
    3. Dated April 2nd., amounting to $\$ 206.15$, on 4 months' credit, disconnted May 30th., at ijos? Ans. \$204.564+.
    4. Dated May l5th., anuruting to $£ 13590$, on 8 months' credit, discounted Nor. 15 th., at $6 \%$ ? Ans. £134 $22+$.
    5. Dated Aug. 7th., amonuting to $\$ 8000.00$, on 6 months' credit, dascounted Dec. 5th., at $5 \%$ ? Ans. $\$ 7931.699+$.
    6. Dated Jan. 3rd. amounting to $£ 9036$, on 9 montha' credit, discounted Sept. 20th., at $7 \%$ ?
    7. Dated June 14th., ammming to $\$ 560.90$, on 3 months' credit, discounted Aug. 2nd., at $6 \%$ ? Ans. $\$ 1550.049+$.
    8. Dated Sept. 8th., amonnting to $\$ 795.10$, on 10 monthe' credit, diacounted Feb. 12th., at 5\%? Ans. $\$ 779.297+$.
    9. Dated Nov. 25 th., amounting to $\mathbf{5 8 7 5} 68$, on 7 months' credit, discounted May llth., at $6 \%$ ? Ans. $£ 868192 \mathrm{f}$ + 10. Dated Dec. 6th., amonuting to $\$ 630.50$, on 11 months' credit, discounted Sept. 18 th ., at $5 \%$ ? 11. Dated Oct. 9th., amunnting to $£ 9515$ o, on 9 mouths' credt disconnted June 7th., at $61 \%$ ? Ans. £ 9545 . 5 .
    12. Dated July l6th., amounting to $\$ 208.95$, un 5 months' credit, discounted Uct. 12th., at $4 \frac{3}{4} 4$ ? Ans. $\$ 207.20+$.
    13. Dated March 2nd., anncunting to $£ 140164$, on 8 mos.' credit, disernated Sypt. 28th., at $6 \frac{1}{2} \%$ ? 14. Dated n. 7th., mmonuting to $\$ 780.50$, on 11 months' credit, discuunted No
    15. Dated Alas. itc., ectuunting to $£ 7805$ Ans. $\$ 775.19+$ on 10 mos.' credit, disoounted Dec, ins or \& ? Ans. £773 1061 .
    16. Duled Fay : ${ }^{2}$, monounting $8 . \$ 436.75$, on 3 months' credit, discounted Juric \%zud, at $5 \frac{1}{2} \%$ ? $\quad$ Ans. $\$ 433.110$ +. 17. Dated March 14 th., amounting to $\$ 600.00$, on 7 months' aradit,
    iscouated Sept. 7th., at $7 \%$ ?

    Ans. \$595.714.
    the rate discount
    ivalent to mount are st by sub-
    t, find the sent worth 3e several
    edit, dis$20+$. ${ }^{\prime}$ crodit, $5+$. credit, $64+$. ' credit, $2+$. credit, $99+$. credit, 114. credit, $19+$. credit, $7+$ credit, $1 f+$ credit, $4+$ credis 5 credit, $0+$.
    credit, 1 옹․ credit, $9+$ credit, $6 \frac{1}{6}$. credit, $0+$. aradit, 714. 14. H
    38. I paid $\$ 320$ for a sum 1 owed; what was this sum, knowing that $5 \frac{1}{4} \%$ discount was allowed? Ans. 8336.80 .
    39. P'aid $£ 2315$ for 50 yd . of cloth ; having received 5 of discount, how much did it cost me per yard?
    40. Is it more advantageous to purchase flour at 25 yo on: 6 months' credit, or at $\$ 6.50$ on 9 months' credit, discount being 8 \% ?

    Ans. Flour at $\$ 6.25$ is the more advantageous.

    ## BANK DISCOUNT.

    374. A Bank is a corporation, legally established for the purpose of receiving and loaning money, and of furnishing a paper circulation.
    375. Bank Notes, or Bank Bills, are the notes made and issued by banks to circulate as moncy. They are payable in specie at the banks.


    876. The Capital of a bank is the money paid in by its stockholders, as the basis of business.
    377. The affairs of a bank are usually managed by a board of directors chosen by the stockholders, and the principal officers are a president, a cushier, and one or more teller..

    Obs.-The president and oashier sign the notes issued; the eashier superintends the bank accounts; and the tellers receive and pay out money. A brink check is an order, payable to bearer and drawn on the cashier for money.
    378. Bank Discount is the simple interest of a note, draft, or bill of exchange, deducted from it in advance, or before it becomes due. Thus, the bank discount on a note of $\$ 106$, puyable in 1 year, at $6 \%$, is $\$ 6.36$; while the true discount is but $\$ 6$.

    The interest is computed not only for the -pecified time, but for three days additional called days of grace.
    Ons.-1. The difference betwoen bank disconst and true discount is the sane as the difference between interest and true discount.
    2. The legal rate of disoount is ordinarily the same as the legal rate of interest.

    37\%. The Proceeds, Avails, or Cash Value of a note is its face or amount minus the discount.
    > 380. Case I.-The face of a note being given, to find the discount and procosde.

    Ex. What is the bank disconnt, and what are the proseeds of a note of $\$ 500$, payable in 30 days, at $6 \%$ ?

    ## OPBRATIOM.

    | Sum discounted, | \$500.00 |
    | :---: | :---: |
    | In ${ }_{6} 30$ days, or $\frac{1}{1} \frac{1}{4}$ of a year, | 2.50 |
    |  | . 25 |
    | Proceeds, or pre | 2.75 |

    ed for the ng a paper
    made and jayable in
    d a bank" takes charge perform two
    in by its
    y a board ral officers
    ior superiny. A brink ney.
    ote, draft, before it 106, pryis but $\$ 6$. time, but 8 the saine 3 of interest. note is its find the

    Analysis.- We find the interest on the sum discounted according to 297, and this int. is the bank diecount; we then subtract the disoount from the sum, and obtain the present worth, $\$ 497.25$. Hence the
    381. Rule.-I. Compute the interest on the face of the note for three days more than the specified time; the result will be the discount.
    II. Subtract the discount from the face of the note; the remainder woill be the proceeds.

    ## By propertion.

    100 : $500:: 6 \times \frac{33}{360}: x$, or the discount;
    or, $100: 500:: 100-\left(6 \times \frac{33}{360}\right): x$, or the proceeds.

    Note.-We take calendar months for the reokoning of titne on all the notes in bank disconnt, and compute interest as if the year contained only 360 days, instead of 365 , then the result is too large by $\frac{5}{365}$, or $\frac{1}{73}$ of itself. Hence, if greater acouracy is required, the interest for the days, when obtained by the rule, must be diminished by $\frac{1}{7}$ of itself; or, the method of computing interest, page 183, mast be followed.

    ## EXAMPLES FOR PRACTIOE.

    1. What is the discount and what are the proceeds of a note of $\$ 1000$, due in 60 days, at 6 \% Ans. Dis. $\$ 10.50$; pro. $\$ 989.50$.
    2. What is the present worth of a note of $£ 2000$, payable in 60 days and discounted at the Quebec Bank? Ans. £1979.
    3. Desiring to loan $£ 250$ of a Montreal Bank which discounts at 8 \%. I gave my note for £24.3 lis payable in 60 days; how much must I add to complete the amount I require? Ans. £9 $13 \%$. 4. A man sold his farm, containing 195 A . 2 R . 25 p ., at $\$ 27.50$ an acre, and received a note payable in 4 mo. 15 da., at $7 \%$ interest. Being in immediate need of money, he discounts the note at a bank; bow much did he receive? 5. Find the day of maturity, the time of discount, and present value of the following notes:-

    ## $£ 402$.

    Six monthe after date, for value received, I promise to pay Daniel Lee \& Co., or order, forty pounds and two shillings onrrency, at the Bank of Quebec.

    Discounted, April 3rd., 1869, at $6 \%$.
    Quehec, Dec. 3rd., 1868. A. T. Hermann. Ane Due June 3 | 61869 : terw of disc. 64da. ; pra., $239135 \frac{1}{4}+$.

    Ninety days after date, we promise to pay C. Simson, one thousand sixty-six and ${ }^{755}$ dollars, at the Union Bank, for value received.

    Rappe, Werber, \& Co.
    Discounted May 8th., at $7 \%$. Ans. Due July 18 | 21 ; term of disc., 74da. ; proceeds, $\$ 1051.40+$
    6. What is the difference between the true discount and bank dis. count of $\$ 950$, for 3 mo , at $7 \%$ ?
    7. What is the difference between the true discount and the bank discount of $£ 200009$, for 6 months, at $3 \%$ ?

    35:. Case II.-The proceeds of a note being given, to find the face.
    Ex. What is the amonnt of a bill, payable in 60 days, which dis. counted at a bank, at $6 \%$, gives $\$ 989.50$ for the proceeds?

    | operation. |  | Analysis. - Sinoe $\$ 0.9895$ is the prooeeds ci $\$ \mathrm{\$ l}$, the note of which $\$ 989.50$ is the proceeds, must be as many dollars as |
    | :---: | :---: | :---: |
    |  | \$1.0000 |  |
    | Int. of \$1 for 63 days | . 0105 |  |
    | Proceeds of \$1 | \$0.9895 | the |
    | $989.50 \div 0.9895$ | 1000, A |  |

    383. Rule.-Divide the proceeds of the note, by the proceeds of $\$ 1$, for the time and at the rate mentioned; the quotient will be the face of the note.

    By proportion.

    $$
    100-\left(6 \times \frac{983}{880}\right): 989.50:: 100: x=\text { the face. }
    $$

    ## EXAMPLES FOR PRACTICE.

    1. What sum, payable in 90 days, and discounted at $7 \%$, at a bank, will give $£ 170$ ?

    Ans. £173 $27 \frac{1}{5}$.
    2. A merchant desires to draw $\$ 5000$ from a bank, and for this purpose discounts his bill, payable in 90 days, at $6 \%$; what should be the amount of it?

    Ans. $\$ 5078.72+$.
    3. The proceeds of a note, due in 4 months, and discounted at the bank, at $6 \%$ are $£ 40718$; what is the face of the note?
    4. Bought goods at Toronto for the sum of $\$ 1486.90$, and. gave in payment my note at 4 months, at $7 \frac{1}{2} \%$ discount; what should be the amount of the note?
    5. A merchant wishes to borrow $\$ 750$ in a bank; what should be the face of his note, payable in 30da., allowing $1 \%$ discount per mo.?

    6 . I gave my note at 60 days for a debt of $£ 163 \mathrm{sin}$; if dieeount ie $11 \%$ monthly, what was the face of the mote?
    884. Oasm III.-The rate of bank discount being given, to find the corresponding rate of interest.
    Ex. What is the rate of interest of a note payable in 90 daya and discounted at 6 \$ ?
    operation.
     interest at 6 por oent., $\$ 0.9845$ in the $\quad$ as its prooeeds $\$ 0.9845$. Then, is as many per oent. an the given rate, same time will yield the same interest, at

    385 Rule.-Divide the given rate per cent., expressed dec imally, by the number denoting the proceeds of \$1 for the given time and rate. The qwotient will be the rate of interest required.

    ## By proportion.

    $$
    100-(6 \times \mu): 100:: 6: x=6 \text { H28t } \% \text {. }
    $$

    ## maxples for pradtion.

    1. What rate of intorest is pard when a note payable in 30 days is ciscounted at $6 \%$ ? Ame. $6 \frac{27}{68 \%} \%$
    2. A note payable in 2 monthe was discounted at $2 \%$ per month at what rate was the interest? Ans. $255_{4, \frac{25}{45} \%}^{5}$ annually.
    3. A note, payable in 1 year, wasdiscounted at $6 \%$, without regard to days of grace; to whal rate $\%$ of interest does the bank discount 4. When a note, payable in 90 daye, is diecounted Ans. $6 \frac{18}{7} \%$. at what rate was the interest paid $f$, is disoounted at $1 \frac{1}{2} \%$ per mo., 5. Whit was the rate per cent. oi a note payable Ans. $18 \frac{1087}{1807} \%$. discountsd at $\frac{1}{4}, 2,2 d, 3 \%$ monthly $?$ 6. What is the rate of intereat corresponding 8 多 $\%, 12 \frac{257}{7} \%$; otc. discount on a bill due in 10 montha, withonding to $5,6,7,10,12 \%$

    ## Ans. $5_{25}^{58}$ \% $6_{15}^{\circ} \%$, etc.

    386. Case IV.-The rate of intereat being given, to find the corresponding rate of lank discount.
    Ex. A man buys notes payable in 90 days, at a discount such that his money brings him $2 \%$ per month; what is the rate of dis.?

    $$
    \begin{aligned}
    & \text { ophratiox. } \\
    & \text { Beam, } \\
    & \text { Int. for } 93 \text { days, } \\
    & \text { Amt. " " } \\
    & \$ 6.20 \div 0.27 \times 775=\overline{\$ 106.20}
    \end{aligned}
    $$

    ANALTHis.-If We assume $\$ 100$ for the proceeds of a note, tho int. For 93 days, at $24 \%$, will be $\$ 6.20$, and the face of the note $\$ 106.20$, We have then, the face of the note, $\$ 106.20$, the interest, $\$ 6.20$, and the time, 93 days, to find the rate per cont., which is dom acoording
    ses7. Kule.-I. Find the interest and the amount of $\$ 1$ or $\$ 100$ for the time the note has to run.

    1I. Diside the interest by the interest of the amount at $1 \%$ for the sume time.

    By proportion.

    $$
    100+\left(24 \times \frac{8}{88}\right): 100:: 24: x=22189 \% \text {, } 100 .
    $$

    ## EXAMPLES FOR PRAOTIOE.

    1. At what rate of bank discount must a note, payable in 60 days, be discounted to obtain $6 \%$ interest?

    Ans. $5 \frac{1}{2} 8 \frac{80}{25} \%$.
    2. At what rate must a note, due in 30 days, be discounted to obtain 6 \% interest?
    3. Ai what rate must a note, payable in 120 dns. $5 \frac{195}{2}$ 告 $\%$. obtain $8 \%$ interest 9
    4. What rates of bank discount, of notes puyans. $7 \frac{808969}{1027^{333}} \%$. respond to $5,6,7,10$ \% interest?
     and 4 mo . hence, without grace, corresponding to $5 \%$ intereable 8 yr .
    6. At what cat
    6. At what rates must notes, payable at 60 days, be discounted, to pay a broker 1, 14, 2, $2 \frac{1}{2} \%$ per month? Ans. $11 \frac{86 \%}{102 \mathrm{I}} \%$, etc.

    ## PROMISCUOUS EXAMPLES IN DISCOUNT.

    What was the present worth, at true discount, of the following notae,
    when discounted :-

    1. Dated Feb. 3rd., discounted June 6th., amounting to $\$ 313.80$, payable in 5 months, at $5 \%$ ?
    2. Dated March 4(h.. discounted Aug. 10th., amt'g $10 £ 17511$ 3, payable in 7 mo., at $4 \%$ ? 3. Dated April 2nd., discounted May 30th., amominting to 8618.45 , payable in 4 mo., at $4 \frac{1}{2}$ g? ? Ans. S6 $13.55+$. 4. Dated May 15 th., discounted Nov. 15th., ant'g to $£ 4067^{\circ} 0$, pryable in 8 mo., at $6 \%$ ? Ans. £402 6 61 + .
    3. Dated Aug. 7 th., discounted Dec. 5th., amounting to $\$ 8000.00$, payable in 6 mo., at $5 \%$ ?

    Ans. $87931.69+$.
    6. Dated Jan. 3rd., discounted Sept. 20th., amt's to $\boldsymbol{£ 2 7 0} 10$ 6, payable in 9 mo., at $7 \%$ ?. Ans. £269 $1610 \frac{1}{4}+$
    7. Dated June 14th., discounted Aug. 2nd., amounting to $\$ 4682.70$, payable in 3 mo., at $6 \%$ ? Ans. $\$ 4650.14+$.
    8. Dated Sept. 8th., discounted Feb. 12 th, , amounting to $\$ 2385.30$, payable in 10 mo., at $5 \%$ ?
    9. Dated Nov. 25th., discounted May 11 th., ant' $g$ to $£ 26265^{\circ} 3$, payable in 7 mo., at $6 \%$ ? Ans. £2607 $2101+$.
    10. Dated Dec. 6 th., discounted Sept. 18th., amounting to \$189 . 50 , pryable in 11 mo., at $5 \%$ ?

    ## What were the $F$

    when discounted:-bank discount, of the following notes,
    11. Dated Oct. 9th., discounted June 7th., smonnting to £28750, payable in 9 ino., at $6 \frac{1}{4} \%$ ?
    12. Dated July 16 th., discounted Oct. l2th. Ans. £28: $101+$. payable in 5 mo., at $4 \frac{3}{4} \%$ ?
    13. Dated March 2nd.. d payable in $\alpha$ mo., at $6 \frac{1}{2} \%$ ?
    14. Dated Jan. 7th., 山心counted Nov, 3xd Ans. £419 $110 \frac{1}{\ddagger}+$.

    60 days, $\frac{18985}{2} \%$. ed to obtig 48 \% ounted to $\frac{969}{338}$ \% lays, cor\%, etc. able $8 y r$. st? unted, to etc.
    ag notee,
    30. For what sum must a noto, to run 4no. 16 da . that the bank proceeds may be \$1954 ?
    31. A person owes $£ 22500$ 4t, payable in 6 monus ifirs. $\$ 2000$. ready money at $2 \%$ diccount 45 , prejable in 6 months; if he pays pay?
    32. Had I bought goods for $£ 875$, I would havi. Ans. $£ 205044$. count ; but as I bough ther $£ 120$ disonly $£ 98$; did I obtaint them for $£ 620$, the discount amounted to and at what $\%$ does the more diminution in proportion to $m y$ purchases, 33. A merchant bought $\$ 461280$ Ans. $2^{2} 1^{2} \%$. and has the liberty of advancing 80 worth of oil, on 3 years credit, After 15 months he gave s2incing the payment, at a discount of $\frac{\%}{} \%$. remainder, knowing that $\$ 2291.60$; at what time did he settle the and knowing that he disbursed but $\$ 1703.52$ ?

    Ans. 22 mo . 20da. after the purchase.
    34. What sum discounted for 7 mo . 9dr., at $6 \frac{1}{4}$ \% per annum, oan produce a discount with which may be purohased the makings of 8 covered bencher, using $1 \frac{3}{4}$ yd. for each, at $\$ 1.80$ per yd. A. $8662.79+$
    35. Having bought two clocks for $\$ 505$, on $16 m 0$.'s credit, and having paid them before the term of maturity, I obtained $\$ 18.05$ discount, at $5 \%$ per annum ; at what epoch did I acquit the debt? A. 7no. 3la. aft.
    36. In a new building, two iron floors were laid, each floor being 15.36 yd . long and 8.25 yd . wide. The weight of the iron is 70 lb . per yard of superficie, and after being laid costs $\$ 5$ per 1001 b . I ask, lst. the total price of the two floors; 2nd. the discount that can be obtained by paying 68 days before the time, at $1 \%$ discount per month.

    ## STOOKB.

    388. Stocks is a general name given to government boads, and to money oapital invested in corporations.
    389. A Corporation is a body formed and authorized by iaw to act as a single person.
    39). The legal act of incorporation whioh defines the rights and powers of the corporation is called a Charter.
    390. The Capital Stock of a corporation is the money contributed and employed to carry on the business of the company.
    Notss.-1. When the oapital stook hes been all paid in, monoymay be raised, if necessary, by locus, secured by mortgage upon the property. The bonds izsued for these loans entitle the holders to a fixed rate of interest. Thus, bonds drawing $6 \%$ aunually are called 6 per cent. stook, or $6^{\prime} s$; do.
    391. To the bonds are attsohed what are oalled coupone, ench of which is a duo bill for the interest on the tond to which it is atteched, representing the amount of the poriodical dividend or interest, and the time of payment, which eoupons are severally cue off and presented for paymont as thoy beoomo due:
    392. Comols is a term abbreviated from the axpression "consolidated annuitios." Tho British govorament having at various times borrowed money at difforent
    rates of Interest and payable at different times, consolidated the stock or bonde thus isaued, by issuing new stock drawing interest at $3 \%$ per annum, payable semi-annually, and redeemable only at the option of tho government, becouring practioally perpetual unnuitiee. With the proeeods of this the old stock was redeemed. The quotations of those $3 \%$ perpetual annuities or consols, indioate pretty aocurately the state of the money market, as they form a staple oredit and beoome a standard for referenoe.

    39:. Stockholders are the owners of stook, either by original title or by subsequent purchase.
    3933. A Share is one of the equal parts into whioh oapital stock is divided. The value of a share in the original contribution of capital varies in different companies; in bank, insuranoe, and railroad companies of recent organization, it is usually $\$ 100$.
    394. Stooks are At Par when they sell for their original value.
    395. Above Par, at a premium or advanee, when they sell for more than their original value.
    396. Below Par, or at a dieeount, when they sell for less than their original value.
    397. An Installment is a portion of the capital stock required of the stockholders, as a payment on their subseription.
    398. An Assessment is a sum required of stockholders, to meet the losses or the business expenses of the company.
    399. A Dividend is a sum paid to the stockholders from the profits of the business.
    400. A person who buys and sells stocks, either for himself, or as the agent of another, is called a Stock Broker or Stock.

    ## EXAMPLES POR PRAOTIOE.

    Ex. 1. What is the cost of 27 shares of Grand Trunk Railroad stock at $4 \frac{1}{2} \%$ premium ?

    Notr.-In all these examples, $\$ 100$ will be considored as the value of ashare, unless otherwise mentioned.
    operation.
    $\$ 2700 \times .045=\$ 121.50$, premium. $\$ 2700+\$ 121.50=\$ 2821.50$, Ans.
    Or, $\$ 2700 \times \$ 1.045=\$ 2821: 50$, Ans.
    $\$ 1.045, \$ 2700$ will oost $\$ 2700 \times \$ 1 \cdot 045=\$ 2821.50$, Ane. $\$$
    By proportion. $100: 100+\mathbf{4 6}:: 27 \times 100: 8$.

    As. 2. 4 broker sold for me 64 shares of the Ocean Steamere Co. stock, at $15 \%$ discunnt, for which he charged $\$ \%$ brokerage; how much did I receive?

    OPERATION.
    $\$ 0.15+.0025=0.1525$. $\$ 1.00-\$ 0.1525=\$ 0.8475$ proceeds of $\$ 1$ of stock.
    $6400 \times \$ 0.8475=\$ 5424$, Ans.

    Inalysis.-Adding the rate of brokerage to the rate of disoount, we have 1525 ; hence $\$ 1$ will bring $\$ 1-\$ 0.1525=$ $\$ 0.8475$, and 64 shares or $\$ 6400$ will bring $6400 \times .8475=$ $\$ 8424$.

    By proportion. $100: 100-(15+0.25):: 64 \times 100: \infty$.
    Ex. 3. I put $\$ 17700$ into the hands of a broker to be invested in Ontario Province Bonds when their market value is 12 \% below par; how many shares will I receive if the broker oharges $\frac{1}{2} \%$ for his cervices?

    ## oftration.

    $81.00-\$ 0.12=\$ 0.88$, market value of $\$ 1$. $\$ 0.88+\$ 0.00 \frac{1}{2}=\$ 0.885$, cost of $\$ 1$. $\$ 17700 \div \$ 0.885=\$ 20000=200$ shares, Ans. stook will oost $\$ 0.885$. Hence, for $\$ 17700$, the broker $.885=\$ 20000$ or 200 shares.

    By proportion. $100-(12+.6): 100:: 17700: x \div 100$.
    Ex. 4. The Richelieu Company declares a dividend of $15 \frac{1}{\%}$; what will I receive for 24 shares?

    ANALYSIS.-Bince the stook is $12 \%$ bolow par, the market value of $\$ 1$ will be $\$ 0.88$; adding the rate of brokerage, we find that every dollar of the

    $$
    \begin{gathered}
    \text { OPERATION. }
    \end{gathered} \$ 2400 \times .15 \frac{1}{2}=\$ 372 . \quad \begin{aligned}
    & \text { ANALYBIs.-Aocording to } 282 \text {, we multiply the } \\
    & \text { base, } \$ 2400, \text { by the rate, } .15 \frac{1}{2}, \text { and obtain the } \\
    & \text { dividend, } \$ 372 .
    \end{aligned}
    $$

    $$
    \text { By proportion. } 100: 15 \frac{1}{2}:: 24 \times 100: x .
    $$

    Ext. 5. What income can we obtain by investing $\$ 10260$ in Quebec Province $6 \%$ bonds, purchased at $95 \%$ ?
    operation.
    $\$ 10260 \div .95=\$ 10800$, stock purchased. $\$ 10800 \times .06=\$ 648$, annual income.
    And since the stook beare $6 \%$ interest, we have $\$ 1$ nual income.

    Analyeis. - We divide the investment, $\$ 10280$, by the cost of $\$ 1$, and obtain $\$ 10800$, the stook which the invest ment will purchase, (288). $\$ 10800 \times .06=\$ 648$, the an-
    E.x. 6. A person desires to secure $\$ 450$ annual revenue; what capital must he invest in $5 \%$ bonde, when stock is purchased at $80 \%$ ?

    OPERATION.
    $\$ 450 \div .05=\$ 9000$, atock required. $\$ 9000 \times .80=\$ 7200$, cost, or investment.
    estment. value of the stock $b$ che market price of $\$ 1$, we have (Ex.5). Multiplylng the par cost of the required stock, or the sum to be invested. $\$ 9000 \times 80=\$ 7200$, the

    Ey proportion. $5: 100:: 450: x \times \mathbf{8 0}$.
    Ex. 7. What per cent. of my investment shall I secure, by pur chasing Montreal 7 per cents., at $105 \%$ ?
    OPERATION.
    $.07 \div 1.05=63 \%$.
    Analysis. - Since $\$ 1$ of stook will cost $\$ 1.05$,
    $\begin{aligned} & \text { and pay.07, the inoome is } \frac{3}{\text { ro }}=63 \% \text { of the in- } \\ & \text { vestment. }\end{aligned}$

    $$
    \text { By proportion. } 105: 100:: 7: 8 .
    $$

    Ex. 8. A man invested in a Steamboat Company, and received a dividend of 9 , which was $8 \frac{1}{\mathbf{3}} \%$ on his investment; at what price did he purchase?

    $$
    \$ 0.09 \div \$ 0.08 \frac{1}{5}=\$ 108, \text { Ane. }
    $$

    ANALT818.-Sinco $\$ 0.09$, the inoome of $\$ 1$ of the stock, is $8 f \%$ of the sum paid for it, we have, $\$ 0.09+\$ 0.081=$ \$108, the purohase prioe.
    By proportion. $8 \mathbf{z}$ : $100:: 9: x$.
    9. A person buys 25 shares of the Marine Bank, of $\$ 100$ each, at $12 \%$ discount ; how much nust he pay? Ans. $\$ 2200$. 10. What will I receive for 20 shares of the Central Railroad stock, at $135 \%$, brokerage being $1 \frac{8}{4} \%$ ? Ans. $\$ 2665$. 11. At $7 \frac{1}{2} \%$ premium, and $\frac{1}{4} \%$ brokerage, what will be the cost of 36 shares of the Bank of Commerce? Ans. $\$ 3879$. 12. A canal cost $£ 400000$; all expenses defrayed it brings in fl5000 annually. Suppose it to have been constructed by meane of shares of $£ 50$ each, and that an individual took 25 shares, what dividend will he receive annually? Ans. £46 176. 13. If 300 shares of the Ottawa Bank sell for $\$ 30112.50$, what is the premium, each share being $\$ 100$ ? Ans. $\frac{3}{8}$ \% preruium. 14. When the nominal value of stock is $£ 1210$, and the discoun $3 \frac{1}{2} \%$, how much must I pay for 30 shares? Ans. $£ 361176$.
    15. The steambuat company of the Saguenay declarea a dividend of $15 \%$ : what shall I receive for 65 shares the nominal value of which
    is $\$ 100$ per share?
    16. Bought stock at par, and sold is at $3 \%$ Ans. $\$ 975$. 6187100 ; how many chares did I parehaee? $\%$ premiant, gaining Ane. 624 shares.
    17. A n individual bonght, at the rate of $\$ 168.75$, a number of shares in the Pictou coal-mine company, the annual income of which is $\$ 10$ per share. With the income he purchases $\$ 260$ worth of goods; what was his investment, the brokerage being 1 \%? Ans. 84398.46 g.
    18. A merchant retires from business with a sum of $\$ 34520.50$, and buys with this capital government 6 's, at the rate of $\$ 70.45$; what will be his annual income?

    Ans. \$29.40.
    19. Ontario 41 's are sold at the rate of $£ 9417$; what income vill I obtain for $£ \mathbf{~ 3 7 9 4}$ ?

    Ans. £180.
    20. Sold $\$ 16400$ worth of North Bank Stook at 13 \% prenilum; what shall I receive?

    Ans. \$18532.
    21. A person, having $£ 2250$, invests thia sum in Ocean Telegraph Company Stock which eells at $17 \%$ discount; what amount of capital does he purchase?

    Ans. $\mathfrak{E} 271016101+$.
    22. Bought 36 shares of the Western Copper Mine Company, the par value of each being $\$ 500$, at $2 \%$ premium, and sold it at $28 \%$ discount; what is my loss?

    Ans. $\$ 5400$.
    23. I have an investment of $\$ 15000$ in a transatlantic steamship company; how many shares shall I own after a divitend of $8 \%$ is declared and payable in capital stock? Ans. 162 shares of $\$ 100$ each.
    24. What should be the rent of a farm, which cost $\$ 16992.10$, in order that the purchase capital may produce the same revenue as wonld be produced by the same sum, employed in the purchase of $61 \%$ bonds, at 91 \% ?

    Ans. \$1903.80.
    25 . A farmer invests $£ 36$, the price of three oxen, in the purchase of $5 \%$ bonds sold at the rate of $£ 7810$; at what real rate was his money placed?
    26. An exchange agent having $\$ 45000$ invested in bonds of the Canadian Transatlantic Steamship Company, exchanged them at $88 \%$, for capital stock in the same company valued at $62 \frac{1}{2} \underline{\alpha}$. The bonds brought 7 \% annually, while the shareholders received two dividends during the year, the first of $3 \%$, and the second of $3 \frac{1}{2} \%$; how much did the agent gain annually by the exchange ? Ans. \$968.40.
    27. An agent receives $\$ 25000$, with instructions to deduct his brokerage at 1 : $\%$, and then purchase bank stock for the balance; if the stock is selling at $3 \%$ discount, what will be the amount of his capital stock ?

    Ans. $\$ 25329.92+$
    28. An individual desires to invest $\$ 11158$ in $5 \%$ bonds. The market value being but $\$ 67.35$, he waits a few days, when it rises to $\$ 69.10$. Find, now, what income did he lose, and what incone he would have gained had the market value lowered to $\$ 66.25$, brokerage being $\frac{1}{3} \%$ ? Ans. Lost $\$ 20.90+$ income, would have gained $\$ 13.73+$
    29. I have $\$ 60500$ to invest in bonds. I can purchase $41 \%$ bonds at the rate of $\$ 95.30$, and $3 \%$ bonds at the rate of $\$ 69.25$; which would be the more profitable of the two? Ans. The $4 \frac{1}{2} \%$ bonds.
    30. How much more advantageous is it to iuvest $\$ 1128$ in $4 \frac{1}{4} \%$
     at 1 क ?
    31. A banker owns 150 shares in the Quebec Insurance Company.
    bir my agoen to buy them when they will rate at $\mathrm{S}\{\mathrm{\$}$ premiurn how ruach w!ll the 150 sharen cost me, knowing that the agent wi. charge me $7_{8}^{\%} \%$ brokerage? Ans. $\$ 15956.25$.
    32. A farmer sold corn for the amount of $\$ 413.4 .40$. With this sum he buys three $4 \frac{1}{2} \%$ bonds which produce an annual incone of $\$ 18$, at $90 \frac{9}{5} \%$ and une $3 \%$ bonds, producing annually $\$ 20$, at $642^{7} \% \%$. With the remainder diminiahed by $\$ 1.95$, he buys $3 \%$ honds at $68 \frac{1}{4}$; at What average rate should he purchase $4 \frac{1}{2} \%$ bonds, to have, for the price of the corn sold, the same quantity of revenue? Ans. $898.43+$
    33. In buying stock in the Labrador Company for the value of $\$ 10425$, at 500 per share, and producing $\$ 36$ for interest and dividend, a farmer secured a revenue of $\$ 540$. Required the market value of the stock per share, and at what rate he let out his money?
    34. In January 1848, the total Ans. 18t. \$695; 2nd. $\$ 5.185 \%$. ${ }^{25} \%$ $\mathbf{£ 3 7 8 0 1 9 8 5 5}$; what whe the amount of interest paid on them semiannually?
    35. A person desires to sell $\$ 3500$ of Montreal Ans. £567029733. being at 951 \%, he waits fe daya $95 \frac{1}{2}$ \% ; what profits did he realize? What loss would he have sustained had the market value lowered to $94 \frac{7}{10} \%$, brokerage, in both casers, being $\frac{1}{5} \%$ ?

    Ans. $\$ 22.75$ gain, and $\$ 17.50$ lose.
    36. A mason built 965 sq . yd. of a wall at $\$ 21.80$ per sq. yd. He desires to invest this suin in insurance company stock. In the Phoenix Insurance Co., the shares are $\$ 5000$ each ; they produce $\$ 200$ as interest and dividend, and are negotiated at $40 \%$ premium. In the Providence Co. the shares are $\$ 2500$ each; they produce $\$ 55$ as interest and dividend, and are negotiated at $45 \%$ premium. Which are the most advantageous, and by how much $\%$ ? How many shares can he purchase in taking the most advantageous, and what revenue could he secure? Ans. The first are the more advantageous by $1.478 \%$; 3 shares; and $\$ 600$ of revenue.

    ## PARTNERSHIP.

    401. A Partnership is an association of two, or more per sons in business, each of whom is catled a Partuer. Such an as sociation is called a Company, Firm, or House.

    > Nore.-The terme Capital or Stoek, Dividend, and Ascosement, have the same signification in Partnership as in Stooks.
    402. Case I.-To find euch partner's shafe of the profit or loss, when there is no regard to time.
    Ex. Three merchants, A, B, and C, associate together in business; $\Delta$ puts in $\$ 275, B \$ 475$, and $C \$ 500$. They gained $\$ 154$; what part of the profit muat be given to each?

    ## PARTERGHIP.

    


    #### Abstract

    Analyals.-Since the whole atock is $\$ 1250$, and the whole profit. $\$ 150$, the profit on evory $\$ 1$ of stuck will be as many dollars as 150 ountaine times 1250, or $\$ 0.12$ on every $\$ 1$ of stock. Then, ench iverchant's atock multiplied by .12 gives bie part of the whote prolit. The same rosult aiso may be obtained, as foliows :-


    By proportion.

    $$
    \left.\begin{array}{r}
    275 \\
    +475 \\
    +500
    \end{array}\right\}=1250: 150::\left\{\begin{array}{c}
    275 \\
    475 \\
    200
    \end{array}\right\}: x=\text { Ans. }\left\{\begin{array}{c}
    \$ 33, \text { A's profit. } \\
    57, \text { 13's protl. } \\
    60, \text { C's profit. }
    \end{array}\right.
    $$

    Proof, $\overline{\$ 150,}$ whole proft.
    4633. Rule.-The whole profit or loss, divided by the number denoting the whole stock, will give the profit or loss on each dollar of stock; and each partner's stock, multiplied by the number denoting the profit on 81, will give his share of the whole profit or loss.

    ## Or,

    As the whole stock is to each partner's stock, so is the whole profit or loss to each partner's profit or loss.

    ## EXAMPLEG FOR PRAOTIOE.

    1. With $£ 200$, two men gained $£ 50$; the firat man contribuca £ 25 , the second, £ 75 ; what part of the gain is each entitled to?

    $$
    \text { Ans. The first, } £ 315 ; \text { the second, } £ 1815 \text {. }
    $$

    2. Four merchants associated and raised a capital of $\$ 45000$, to which each man contributed equally. At the expiration of the partnerohip, the capital was found to be angmented by $\$ 26877$. What shall be the part of each man, knowing that the lst. ought to have 13 parts; the 2 nd., 11 ; the 3 rd., 8 : and the 4 th., 7 ?

    Ans. Ist., $\$ 23959$; 2ul., $\$ 20273$; 3rd., $\$ 14744$; 4th., $\$ 12901$.
    3. Three men associating together, gained $£ 28710$; the $1 \mathrm{st} .$, put in 400 yd . of velvet at $£ 1$ per yard; the 2 nd ., 350 yd . of cloth at $£ 2$; the 3 rd., 450 yd . of cassimere at 15 s . ; what part of the gain should each have?

    Ans. £80, £140, and £67 10.
    4. Four persons having joined in partnership agree that the int. put in $£ 1250$; the 2 nd., $\frac{1}{4}$ more than the first; the 3 rd., as much as the two others together; and the 4th., his industry during the year, which was estimated at $£ 2000$; what share of the profits, $£ 1525$, shall each receive?

    Ans. £250, £312d, £562 $\frac{1}{2}$, and $£ 400$.
    5. Four associates made a proft of $\$ 1500$. The first is to have 3 parts; the 2nd., 4 ; the $3 \mathrm{rd} ., 5$; and the 4 th. 6 . How mueh will
    
    6. The firat of five men, aboceiated in partnership, put in ssana; the znd., $\$ 100$ more than the firmt ; the 3rd., 100 more than the ree. ond ; and so on, with the others, always magmeating by \$10\%. If the gain is $\$ 1800$, whint ought to be the part of each?
    7. Three apeculaturs have together a capital of $\$ 4925$, which hrings them a profit of $\$ 616$; the 1st. received $\$ 150$ for his share of the gain ; the 2nl., $\$ 216$; and the 3 rd., $\$ 260$. What was pach one's investment?
    8. Two specuiators shipped 6000 Ane. $\$ 1200, \$ 1648, \$ 2080$. voyage 650 tonswere throwed 6000 tons of corn to Cubn. During the arose. If 250 tons were spoiled, how on account of a storm which ing that 3500 tons helonged to the frov?
    9. Three faimers bought 148 sheep at $\$ 4.1$ Ans. 525 and 375 tons. ment of which the lat. furnixhed $\$ 218.85$, the per head, for the pay. the 3rd, the remainder. They sold the she the 2 nd., 8236.323 , and them during 6 montha, at a proft of $\$ 1.60$ per head; haw murtured Ans $\$ 54.88$, $\$ 91.663^{2}$, 860 , did
    10. Three lumber merchants bons. $\$ 84.88, \$ 92.600_{2}, 860.243$. realized a profit of $£ 29689$. The first 76500 aaplings, on which they the second, $£ 5276104$. The tirst man contributed $£ 460$ tis 72 ; received, however, $£ 98$; the third man's part is not known, but he contrihution of the third as as his rhare of the profits. Tell us the the nrice of the saplings per humdred ? profits of the two others, and share $£ 49413$. The profts of Iat., $£ 9.3$ Ans. Thind merchant's £1 189 per hundred.
    11. Two dealers in furs made a joint pirchase of 268 adsorted fox and beaver skins, at $£ 11210$ per hundred; the first deater advanced E48 10 more than the second, and, together they realize a proft of 18 \% on the buying price. Required what is due to each, and at what price they sold the skins a piece i Ans. $£ 14954 \frac{5}{5}$ due to the "n : £200 io, to the first. The skins cost £1 $66 \frac{8}{5}$ a piece.
    12. Three students in Astrunomy join in raising $\$ 698.50$ for the purchase of a telescope. The seoond furnished $\frac{3}{3}$ of what the first gave, and the third furnished 手 of what the two others had alvanced; what was the contribution of each 9 tns. $\$ 277.81 \frac{1}{4}, \$ 166.68 \frac{3}{4}, \$ 254$.
    13. Four farmers associated in furmshing a quantity of हtraw which they sold at $\$ 7$ per hundred bundles; what did each receive, knowing that the 18t. furnished ${ }^{8} \mathrm{~K}$ of it ; that the 2 nd. furuished a quantity not mentioned, and that the 3rd. furnshed 600 bundlew, which quantity equalled the delivery of the 1st. and 4th., who furvished 240
    bundles?
    14. Two clockmakers joinci Ans $\$ 25.20, \$ 8.40, \$ 42.00$, $\$ 16.80$. the average price of $\$ 7.374$. in in the purchase of 120 clock worky at loss of the lst. surpssed $;$; in the speculation, they lost $\$ 135$. The lose and investment of each? of the 2nd. by $\$ 33.50$; what were the 2nd. Inv. \$332.69\%, lowe $\$ 50.76$. ${ }^{\text {Anc. }}$ 18t. Inv. 8552.30 g, loss $\$ 84.25$.
    15. Several persons agreed to conduct, during one year, a paper manufactory. The first put in $\frac{2}{8}$ of the stock ; the second, $\$ 4000$ less than the first; the third, $\$ 4000$ less than the second, and so on until the last. If the investments had been in sums equal to the highest, the capital stock would be augmented by \& . The merchandise sold produced a sum equal to the $\frac{8}{3}$ of what was put in, which wae employed in buying rags. In admitting that the $\frac{13}{13}$ of the sum proceeding from sales serve to cover the expenses of fabrication and investment, it is required to ascertain how many persons there were, how much each one put in, and what part of the gain each is entitled to?
    404. Case II.-To find each partner's share of the profit or loss, when the stock is employed for different periods of time.
    E.x. A and B entered into partnership; A furnished $\$ 240$ for 8 months, and B $\$ 560$ for 5 months. They lost $\$ 118$; what was each man's share of the loss?

    $$
    \begin{aligned}
    & \$ 240 \times 8=\$ 1920 . \\
    & 560 \times 5=\frac{2800}{\$ 4720} . \\
    & \$ 1920 \times 0.025=\$ 48, A ’ \text { loss. } \\
    & 2800 \times 0.025=70, \mathrm{~B} \text { 's loss. } \\
    & \text { Proof, } \overline{\$ 118} \text {, entire loss. } \\
    & \$ 118.00 \div 4720=\$ 0.025 \text {, lose on } \$ 1 .
    \end{aligned}
    $$

    operation.

    Aralysis.-It is evident that $\$ 240$ for 8 mo . is the same as $\$ 240 \times 8=\$ 1920$ for 1 mo., since $\$ 1920$ would lose as much in 1 mo. as $\$ 240$ in 8 mo . ; an: $\$ 560$ for 5 mo . is the same as $\$ 560 \times 5=\$ 2 \sim 00$ for 1 month. The question then is the same as if $A$ had furnished $\$ 1920$, and $B \$ 2500$, for equal timos. Then, if $\$ 1620+\$ 23011=\$ 4720$ lose $\$ 118, \$ 1$ will lose ${ }^{2} 7^{2} 20$ of $\$ 118=\$ 0.025$. and $\$ 1920 \times .025=\$ 18$, A's loss ; $\$ 2800 \times .025=\$ 70$, B's loss. The same results may be obtained as follows:-

    ## By proportion.

    $$
    \left.\begin{array}{c}
    \$ 240 \times 8=1920 \\
    560 \times 5=2800
    \end{array}\right\}=4720:\left\{\begin{array}{c}
    1920 \\
    2800
    \end{array}\right\}:: 118: x=A n s .\left\{\begin{array}{c}
    \$ 48, \text { A's loss. } \\
    70, B^{\prime} \text { 's loss. }
    \end{array}\right.
    $$

    405. Rule.-Multiply each partner's stock by the time it was in trade, and divide the whole profit or luss by the sum of the several products; by the quotient, multiply the product of each partner's stock and time, and the residt will be his share of the profit or loses.
    Or,

    Multiply each partner's stock by the time it was in trade; then, as the sum of these products is to each product, so is the whole proft or loss to each partner's profit or loss.
    for
    ear, a paper $\mathrm{d}, \$ 4000$ less d so on until the highest, handise sold ich was emsum proceed1 and investre were, how entitled to?
    the profit or of time.
    $1 \$ 240$ for 8 hat was each

    A's loss. B's loss. entire loss.

    ## examples for practiol

    1. Two persons contribute unequal sums towards a capital: the first puts in $\$ 2300$ for 2 years; the second, $\$ 1500$ for 18 months. What part of the gain, $\$ 1400$, should each person receive?

    Ans. \$940.15, \$459.85.
    2. Three individuals raised a capital sum with which they gained $£ 113710$ : the first contributed $£ 200$ for $2 \frac{1}{2}$ years; the second, $£ 125$ for 25 months; and the third, £248 15 for 35 months. What part of the gain should each have?

    Ans. 1st. £382 $15 \frac{1}{6}$; 2nd. £199 7 0 ${ }_{5}$; 3rd. £555 $710 \frac{1}{8}$.
    3. A porter associated with a pedler and raised a capital of $\$ 16000$. After two years they divided the gain, and the pedler, who had contributed $\$ 9000$, received $\$ 1800$; what did his companion receive, knowing that the latter left his share in the business but during 20 monthe?
    4. Four persons agree to form a partnership for 3 years. The first puts in at the beginuing $\$ 350$, and 5 months after $\$ 2400$ more; the second puts in $\$ 8000$ at first, and at the end of 20 months withdraws the half of his share, and 5 months after withdraws $\$ 2400$ more; the third puts in $\$ 1500$ in the beginning, and $\$ 5000$ at the end of 2 gears; the fourth puts in at first $\$ 600$, and every six months aug. ments his portion by a like amount; the gain being $\$ 80000$, what part did each receive?

    Ans. $\$ 14677.35+, \$ 33336.15-, \$ 19232.39+, \$ 12754.1 \mathrm{i}+$.
    5. Three merchants joined in business. The frst put in $£ 100112$ for 10 months; the second, $£ 1751126$ for 151 months; and the third, $£ 200039$ for 17 mo. and 20 days. Required each merchant's share of the proflts which amount to £350 3.9
    6. Two olothiers associate together; one of them contributed a sum with whioh could be bought 90 yd . of Broadcloth at $\$ 6$ per yard, the other put in a sum with which 60 yd. could be purchased at the same rate. In supposing the lst. to have had $\$ 6$ of the profits more than the 2nd., to how much did the profite amount? Ans. $\$ 30$.
    7. Four farmers rent a pasture for $\$ 975$. The first put 5 beeves on it during 54 days; the second, 7 cows during 63 days; the third, 8 heifers during 75 days; and the fourth, 6 horses during 50 days. It was caloulated that 1 beef consumed 11, times as much as a cow, or twice as much as a beifer, or $1 \frac{1}{4}$ times as much as a horse ; how much must each farmer pay?

    $$
    \begin{aligned}
    & \text { Ans. } \$ 238.45+; \$ 259.65-; \$ 264.94+; \$ 211.96-\text {. }
    \end{aligned}
    $$

    8. In the working of a mine during 6 years, three partners gain £21750. The tirst partner had put in £13437 10 in the beginuing, but after $2 \frac{1}{2}$ years, he withdrew £3275. The second put in his share, which was $£ 41000$, only $1 \frac{1}{8}$ years after the commencement of the work. Finally, the third made his contribution of $£ 53750$, but 3 yeare after the installinent of the first. What part of the profits should
    

    ## EXCHANGE.

    406. Exchange is the process of remitting money from one place to another by Drafts and Bills of Exchange.

    Notr,-For a full treatment of this and of the following subjects, see the Commercial Arithmetic.

    ## Form of a Draft.

    \$400. [stamp.] OUeliec, OP. Q., © March 1.1871.
    Shirty days after sight, pay to (ilenry Sims, at order, EFour Óluntied EDollaws, and charge tho came to my account. \% Janna OBentom. Sous Oercrik
    
    407. The Drawer, or Maker, is the person who signs the draft.
    408. The Drawer is the person on whom the draft is made.
    409. The Payee is the person to whom the draft is made payable.
    410. An Acceptance is the promise of the Drawee, to pay the draft at maturity, and is usually acknowledged by writing the word " Accepted" with his signature, across the face of the draft.
    411. An Indorsement of a draft, by the payee, is made in the same manner as the indorsement of a note.
    419. A Sight Draft is an order to pay at sight.
    418. A Time Draft is an order requiring payment at a specified time.
    414. A Draft or Bill of Exchange is at a Premium, when the price paid is greater than its face; and at a Discount. when the price paid is less than its face.
    415. Domestic, or Inland Exchange, is when both the drawer and drawee reside in the same country.

    Ex. 1. What must I pay in Ottawa for a draft of $\$ 640$ on Quebec, exchange being $1 \frac{1}{2} \%$ premium?

    Ex. 2. What must be paid in Montreal for a draft of $\$ 3500$ on Halifax, at 33 days, exchange $2 \frac{1}{6} \%$ premium.
    416. Casy I.-Given the face of a draft, the rate per cent. of exchange, and the time, to find its cost.
    chan

    $$
    \begin{aligned}
    & \text { OPERATION. } \\
    & \$ 640 \times 1.015=\$ 649.60, ~ A n s .
    \end{aligned} \quad \begin{aligned}
    & \text { ANALYSIS. } \\
    & \$ 1 \text { is The cost of exchange of } \\
    & \$ 10,640 \times \$ 0.015=\$ 1.015, \text { and of } \\
    & \$ 1.015=\$ 649.60 .
    \end{aligned}
    $$

    $\$ 1.000$
    $.006=$ disot. for 36 da at 6 \% .
    $\overline{\$ .994}=$ oost at par of $\$ 1$.
    $.022=$ rate of exohange.
    $\overline{\$ 1.016}=$ cost of $\$ 1$ of the draft
    $\$ 3500 \times 1.016=\$ 3556$, Ans.

    ANalysis.-The disoount of $\$ 1$ at $6 \%$ for 38 days is $\$ 0.046$, which being subtracted from $\$ 1$ leaves $\$ 0.994$, the cost of $\$ 1$ of the draft, if the exchange was at par. To this add the premium of $\$ 1$, $\$ 0.022$, and wo have $\$ 1.016$, the cost of $\$ 1$ of the draft. Hence the cost of $\$ 3500$, the draft, is $\$ 3500 \times 1.016=\$ 3556$.
    417. Rule.-I. For sight drafts.-Multiply the face of the draft by 1 plus the rate when exchange is at a premium, and by 1 minus the rate when exchange is at a discount.
    II. For drafts payable after sight.-Find the cost of $\$ 1$ at bank discount for the specified time, at the legal rate where the draft is purchased, then add the rate of exchrange when at a premium, or subtract it when at a discount, and multiply the face of the

    ## EXAMPLE FOR PRAOTIOE.

    1. A merchant in Toronto wishes to pay in Montreal $\$ 7930$, and exchange is $3 . \%$ premium; what will be the cont of the draft?
    2. A merchant in St. John, N. B., wishes to pay ins. $\$ 7989.47$ h. and exchange is $1 \frac{8}{4} \%$ discount ; required the cost of th Ottawa, $\$ 980$,
    3. What will be the cost, in Kins. 8962.85 . $\$ 800$, payable 60 days after Kingston, of a draft on Halifax for $2 \%$ ?
    4. A merohant in Kingston purchased a draft on Fredericton for \$340, payable 30 days after sight, at $6 \%$; what did it cost him, the rate of exchange being $1 \frac{1}{2} \%$ discount? $\quad$ Ans. $\$ 822.78$.
    5. What will be the cost of a draft of $\$ 4260$, for 60 days, at $6 \%$, axchange being $17 \%$ premian ?
    6. A merchant in Quebec receives from his agont 1200 bushels red wheat, purchased in Toronto at 65 cte. per bushel; in payment for which he remits a draft on Toronto, at $\frac{5}{8} \%$ discount. The transportation of his wheat cost $\$ 98$. What must he sell it for per bushel to gain \$225 ?

    Ans. $\$ 0.91 \frac{9}{8}$.
    418. Case II.-Given the cost of a draft, the rate per cent. of exchange, and the time, to fird its face.

    Eix. A merchant in Three Rivers paid $\$ 6856.10$ for a 60 days' draft on Toronto, exchange being $17 \%$ preminm, and interest $6 \%$; required the face of the draft.

    OPERATION.
    $\$ 1.0000$
    $.0105=$ the diseount for 63 days.
    $\overline{\$ .9895}=$ the cost of $\$ 1$ at par.
    $.01875=$ the rate of exchange.
    $\$ \overline{\$ 1.00825}=$ the cost of $\$ 1$ of the dratt.
    $\$ 6856.10 \div \$ 1.00825=\$ 6800$, Ans.

    Analysis.-By 416, Case I., Ex. 2, we find the cost of $\$ 1$ of the draft to be $\$ 1.00825$. Hence, $\$ 8858.11 \div \$ 1.00825 \mathrm{~cm}=\$ 800$, tis the face of the draf.
    415. Rule.-Divide the given cost by the cost of " draft for \$i, at the given rate of exchange; the quotient woill be the face of the required draft.

    ## ERAMPLES POB PRAOTIOR

    1. What draft may be purchased for $\$ 16416.10$, exchange being at $31 \%$ premium?

    Ans. $\$ 15860$.
    2. Required the face of a draft for $\$ 158.40$, exchange being at $1 \%$ discount?

    Ans. $\$ 160$.
    3. An agent in Kingston is directed to make the remittance by draft, of $\$ 565.32$, to his employer in Quebec, drawn at 60 days. What will be the face of the draft, exchange being at $1 \frac{3}{4} \%$ premium?
    4. That will be the face of a draft for $\$ 962.85$, exchange being at $8 \%$ discount?
    5. A man in Halifax, has $\$ 4800$ due him in Montreal; how much more will he realize by making a draft for this sum on Montreal and selling it at $\frac{1}{2} \%$ discount, than by having a draft on Halifax remitted to him, purchased in Montreal for this sum, at $\$ \%$ premium?

    Ans. 211.75 +

    ## FOREIGN EXCHANGE.

    420. A Foreign Bill of Exchange is a draft in whioh the drawer and drawee live in different countries. charge the same to my accounts.
     36. Welting tron Stree, SLoniom.

    Notk.-In foreign exchange, to prevent lose or delay, two or three drafts of the same tenor and date are drawn up and sent by different onveyances, or at dieferent times; on tl , payment of one, the other two are worthless. Each draft must have a starnp attached.
    421. Foreign exchange is computed 0.5 inland exchange, exsept that the currency of one country must be reduced to that of another.
    422. Rates of exchange between the Dominion of Canada and Great Britain are commonly reckoned, at a certain per cent. on the old par of exchange, instead of on the new par.

    Notr.-By an old act of Provincial Parliament it was enacted that $\boldsymbol{£ 1}$ sterling was $\$ 4.444$ Canadian money. But by a recent ant the value of the pound sterling was fixed at $\$ 4.866$. Now, the new par is equal to the old par plus $9 \frac{1}{2} \%$ of the par. par, that is, $\$ 4.444+9 \frac{1}{2} \%$ of $\$ 4.444$, which is .422 , equal to $\$ 4.866$, the new Great britain, must the rate of exchange la en tho Dominion of Canada and cording to the new standard.

    EXT. 1. A merchant in Quebec wishes to remit to London $£ 56036$ sterling; exchange being at 11 \% premium. How much must he pay for the bill of exchange?

    $$
    \begin{aligned}
    & \text { OPERATION. } \\
    & \$ 40 \times 1.11=\$ 4.931 \\
    & \dot{L} 6036=\text { E560.175 } \\
    & E 560.175 \times 4.93 \frac{1}{3}=\$ 2763.68, \text { Ane. }
    \end{aligned}
    $$

    rate; multiplying the froe of the bill, 566036 , deoimy, the cost of $\mathcal{E 1}$ at that - exchange of $£ 1$, wo obtain 39768.63 , the required cont of the bush.

    Ex. 2. What will be the face of a bill of exchange on Liverpool, purchased in Montreal for $\$ 5537.40$, exehange being at $10 \%$ premium?

    OPREATIOX. AKAETMIS.-We find, as in the $8481.10=\$ 4.88 \%$
    $86637.40 \div 4.88 \frac{8}{3}=81132130$. preseding example, the cost of $£ 1$, at the given rate of oxchange; then we divide $\$ 5537.40$, the given cest, by the cost of exehange for $s=1$, and obtain $£ 1132130$, the face.

    Ex. 3. What is the oot in Toronto of a bill on Paris, for 1780 aracs, oxhange being at $2 \frac{1}{2} \%$ discount ?
    operation.
    Commercial value of the frane, $=\$ 0.186$
    Deduet 21 \% disconnt, . . . . . . 0.00465
    Value of 1 tranc, . . . . . . . 8 \$.18136
    $\$ 0.18135 \times 1780=\$ 329.803$, Ane.
    423. From these illustrations we derive the following

    Rule.-I. To tind the cost of a bill, the face being given.Multiply the face by the cost of a unit of the currency in which the bill is expressed.
    II. To find the face of a bill, the cost being given. -Divide the givers coot by the cost of a unit of the currency in which the bill is so be expressed.

    Redoction of the Sterline Money to the Old of 90 ter New Oanadian Currenot, net par.

    Ar. Boduce $55603 \leq$ sterling, to Old Canadian Curreney:
    
    424. Role.-To reduee aterling money to Old Cauadian Curroncy, new par,-Add to the givon sum its fifth plus one welfith of the fifth.

    Liverpool, 6 premium? nd, 20 in the the cost of $£ 1$, rohange ; then the given cost, go for 81 , and the faos.
    is, for 1780
    ring
    given.o in which
    -Divide the h the bill is

    LD OR 5
    s.
    oney:

    - The pound 863, and the ponnd $-\$ 4$; Then fl ster.
    $=x_{1} 1 \frac{1}{6}$ old - $\frac{13}{88}$ of a numof $\frac{1}{6}$ of that ce the

    Causdian h plus one

    ## EXAMPLES FOR PRAOTIOE.

    1. What will be the commercial value in Ottawa, of a bill of exchange on London for $£ 39010$ ster., at $9 \%$ prem.? Ans. 81891.75 占.
    2. What will cost, in Amsterdam, a bill on Montreal for \$681.34, the course of exchange being ${ }^{\text {at }} \$ \$ 0.38$ per guilder? Ans. $\$ 717.20$.
    3. What must be paid in Kingston for a bill of exchange on Paris for 3000 francs, exchange being at $2 \%$ above par?
    4. What will be the cost in Montreal of a bill on Boat $n$, for $\$ 2000$, at $\frac{1}{2} \%$ premium?
    5. What will a bill of exchange on Hamburg for 500 Ans. $\$ 2010$. cost in Quebec, at 1 \% above par, the marg, for 5000 marce banco, 35 cts . $\quad$ par, the marc banco being equal to
    6. Bought in Toronto a bill of exchange on Glasgow tor £675 26 sterling; what did it cost me at $8 \frac{1}{2} \%$ premium? Ans. $\$ 3255.60+$.
    7. What will cost in Halifax a bill of exchange on Rouen for 56245 trancs, the course of exchange being 5 fr. 54 centimes per dollar?
    8. What will be the face of a bill on Ans. $\$ 10152.53+$.

    Montreal for $\$ 7125.50$, exchange being at 91 of that may be bought ia
    9. Paid in Quebec $£ 2170157$, old at $91 \%$ premium?
    on Lyons amounting to 49335 fro exahange below par?
    10. Received from L. Nelson \& $C$ Ame. $\$ 0.053$ + $£ 38150$, on J. Chalmers \& C Co., London, a bill of exchange for mal ourrency of Canada, at $9 \%$ premium? what is its value in deci-

    Ane. $\$ 1846.94+$.

    ## BQUATION OF PAYMEN'RS.

    425. Equation of Payments is the process of finding the mean or equitable time of payment of several sums, due at different times without interest.
    426. The Term of Credit is the time to elapse before a debt becomes due.
    427. The Average Term of Credit is the time to elapse before several debts, due at different times, may all be paid at once, without loss to debtor or creditor.
    428. The Equated Time is the date at whioh the several debts may be cancelled by one payment.

    ## 4ist. Cask I.-To find the average or equitable time of paying several debts due at different times.

    As. 1. On the first of March 1870, a man gave notes, as follows: the first for $\$ 250$ payable in 30 days; the seoond for $\$ 200$ payable in 60 days; the third for $\$ 300$ payable in 90 days. What wat the ar. erage term of eredit, and what the equated time of payment?

    > oprantion.
    > $45500 \div 750=62 \mathrm{da}$., average term of credit.

    March $1+62 d a$. $=$ May 2, Ans.
    amalyats. - The interest of $\$ 250$ for 30 days is the same as the interest of $\$ 1$ fer 7500 days; and of $\$ 200$ for 60 days, the saile ns of $\$ 1$ for 12000 days; and of $\$ 301$ for 90 day, the same of $\$ 1$ for 27000 days. Rence, the interest of all the aumas to the time of payment is the same as the interest of $\$ 1$ th: $7500 \mathrm{da} .+12000 \mathrm{da} .+27000 \mathrm{da} .=46500$ days. Now, if $\$ 1$ require 46500 days to gain a oertain sum, $\$ 250+\$ 200+\$ 300=\$ 750$ will require ${ }_{7}{ }^{1}$ of 46500 days; $46 j 00 \mathrm{da}$. $\div 750=62$ days, the average term of eredit ; and, Maroh 1, the date at whioh the orodits begin, $+62 \mathrm{da} .=$ May 2 , the equated time of payment.

    Ex. 2. Bought of D. I. Lyons several bills of goods, at different times, and on various terms of credit, as by the following statement. What is the equated time for the payment of the whole?
    

    ## ofiratiom.

    
    analyas. - We firat find the time when each of the bills will beoome due. Then, siace it will shorten the operation and not change the result, we take the first time when any bill becomes dwe, instead of its date, or the point from which to compute the average time. Now, since May 1 is the period from whioh the average time is oonputed, no time will be reckoned on the first bill, but the time for the payment of the second bill extends 67 days beyond May 1, and we multiply its acount by 67 . Proceeding in the same manner with the remaining bills, Fe find the average torm of oredit to be 71 days, and July 11, the equated time of payment.
    430. Rule.-Multiply eack payment by its own time of credit, and divide the sum of the products by the sum of the payments.

    Nors,-if the date of the average time of payment is requlrei, win Kx. 2, find the sime roken oach of the swma becomes dwe. Multiply each oum by the number of dayo intervening betwoen the date of its beooming dwe and the earliest date on which any swm becomee due. Then proceed as in the rule, and the quotient will bo the'average time reguired, in dayo forvourd from the dave of the cartiest sum boo maing dre.

    1. A merchant purchased $£ 4750$ worth of oloth, and agreed to pay $\frac{1}{5}$ of the sum every month until the cancellation of his debt; what will be the anrount of each payment? Ans. $£ 950$. 2. A man owes $\$ 15960$ payable as follows: $\frac{1}{4}$ in cash, $\frac{2}{5}$ in 6 mo ., and the remainder in I year; required tie amount of each payment?
    2. The sum of $\$ 1710$ is to be paid in two installments, viz. : $\frac{1}{2}$ in 6 mo., and the other $\frac{1}{1}$ in 10 mo . At what time should it be paid so as to make but one payinent ? follows: $\$ 525$ in 6 mo., and the balanoe in 9 mo. Wishing to make but one payment, how long shonld this payment he deferred?
    3. Un the la Jf January, 1868 , Ans. 7mo. 18da. frat for $\$ 500$ payol in 30 , 868 , a merchant gave three notes: the 60 days; the third tor 3600 days; the second for $\$ 400$ payable in time of payment? $\$ 000$ payable in 90 days. Required the equated
    4. A inerchant bought, on Ams. March 3, 1868. of merchandise and gat, on the 15th. of May, 1868, $\$ 8000$ worth and the remainder in 10 me pay $\frac{1}{3}$ of the price in 6 mo ., $\frac{1}{8}$ in 8 mog , single payment, how long But wishing to cancel his debt by a
    eferred?
    2me. 8mo. 24da.
    5. Case II.-To find the time of paying the balance of a debt, when partial payments have heem made before the debt is due.

    E'x. Bought $\$ 180$ worth of goods, at 8 nouthe' credit. At the end of 4 months, I paid $\$ 30$, and 2 monthe later, $\$ 40$; when, in equity, after the expiration of 8 months, shall I owe the balance?

    > OPLEATION.
    > $30 \times 4=120$
    > $40 \times 2=80$
    > $70-\$ 70=\$ 110 ;$ $\$ 180-\$ 70=\$ 110=1 \mathrm{mo} .25 \mathrm{da} .$, Ans.
    main unpaid, after the 8 monthe, rio of 20 , which we ind to bo $\$ 110$, should remonths, or 1 mo . 25 da .
    439. Rule.-Multiply each payment by the time it was made before it becomes due, and divide the sum of the products by the balance remaining unpaid; and the quotient will be the required time.

    ## EXAMPLES FOR PRAOTIOE.

    1. A vintner agreed to pay $\$ 1895.20$ for 2369 gal . of cognac brandy in 12 mo . ; but at the end of 10 mo he paid for 633 gal . Required the equated time of the balance*
    2. Bought of C. Lyons, at 6 mo. $£ 432$ worth of goods; at the end of 1 mo . I paid him £75, and 4 mo . after £200 more. How loug after the expiration of the 6 mo. should I pay the balance?

    Ans. 3 mo. 20 da.
    3. A grocer bought $\$ 2829.75$ worth of coftee which he desires to pay in three different payments: the urat is to the second as 4 is to 5 , and the third is equal to half the second. The first payment ghould be made in 4 mo . ; the second in 7 mo ; and the third in : year. But at the end of 6 mo. he paid $\$ 975$, how long can he keep the balance? Ans. 7 no. 18 da.
    4. An undertaker built a house for £f,035 payable in 15 mo.; but being in want of rome money, the proprietor pays him $£ 284710$ eight months before the time. How long, in equity, can the proprietor keep the balance to compensate the advance he made the undertaker?

    Ans. 22 mo. 4 da.
    6. Andrew having sold $\$ 8400$ worth of linen, at 12 mo. credit, reseived the $t$ of the price only 15 mo . after. Whien did he receive the ${ }^{2}$ ?
    6. I owed $\$ 600$ wt 13 monthe; I paid $\frac{2}{8}$ of this sum before it was due, so that I can keep the remainder 2 years withont injuring my ereditor. Required the time when the 2 were paid? A. 7 ino. $15 d a$.
    7. A trader owes $\$ 3000$ payable in 6 mo ; $\$ 4500$ payable in 8 mo ., and $\$ 9500$ payable in 10 mo. At the end of 5 mo. he pays $\$ 12000$. How long can be keep the balance?

    Ans. 17 mo. 24 da.

    ## ALLIGATION.

    488. Alligation treats of mixing or compounding articles or ingredients of different qualities or values. It is of two kindsAlligation Medial, and Alligation Alternate.

    ## ALLIGATION MEDIAL.

    434. Alligation Medial is the process of finding the mean or averaze rate of a mixture composed of articles of different qualities or values, the quantity and rate of each being given.
    435. To find the average value of several articles mixed, the quantity and rate of eisch being given.
    Exs. A grocer mixed 2cwt. of sugar worth $\$ 9$ per cwt. with 1 cwt. worth $\$ 7$ per cwt. and 2 cwt worth $\$ 10$ per cwt. ; what is 1 cwt . of the mixture worth?
    OPERATION.
    $9 \times 2=\$ 18$
    $7 \times 1=4$
    $10 \times \frac{2}{6}=\frac{20}{15}$

    Analysis.-Since 2owt. at $\$ 9$ per owt. is worth $\$ 18$, lewt. at $\$ 7$ ner ewt is worth $\$ 7$, and 2ewt. at $\$ 10$ per ewt. is worth $\$ 20 ; 2 \mathrm{cwt}+1 \mathrm{cwt}$. +2 cwt. $=5$ ewt. is worth $\$ 18+\$ 7+\$ 20 \Rightarrow$ $\$ 45$; and lcwt. is worth as many dollars as 45 oonking times 5, or \$9.
    486. Rule.- Find the valme of each of the articles, and divide the suin of their values by the uumber denoting the sum of the articles. The quotient will be the average value of the mixture.

    ## EXAMPLES FOR PRACTIOE.

    1. A farmer mixes together 10 bush. of oats at 40 cts. per bu., 15 bu. of corn at 50 cts. per bu., and 25 bu . of rye at 70 cts . per bu.; wingt is the "qlue of a busbel of the mixture? Ans. 58 cts.
    2. If I mix 20 pounds of tea at 70 cts . per pound with 15 pounds at 60 cts. per pound, and 80 pounds at 40 cts. per pound; what is the value of 1 lb . of this mixture?
    3. A dealer in liquors would mix 14 gal . of $4 \pi / 29 \mathrm{cts}$. wine at $\$ .75,24 \mathrm{gal}$, at $\$ .90$, and 16 gal . of water with 12 gal . of gallon of the mixture worth ? and 16 gal. at $\$ 1.10$; how much is a 4. A man bought 33 dith $\quad$ Ans. $\$ 0.73_{3}^{1} \frac{1}{5}$. $10 \frac{1}{2}$ cts. a dozen, 44 dozen at of eggs at 12 cts a dozen, 4 dozen at doz. He sells them so as to make $50 \%$ on and $5 \frac{1}{3}$ doz. at 10 cts . a he receive per dozen?
    4. A goldsmith wishes to compound 3 lb 6 Ans. 1615 cts . fine with 4 lb .8 oz .21 carats, $3 \mathrm{lb} .9 \mathrm{oz}, 20 \mathrm{carat}$. of gold 23 c carats alloy; what will be the fineness of thoz. 20 carats, and 2 lb .2 oz . of alloy; what will be the fineness of the composition? Ans. 18 carats.

    ## alligation alternate.

    437. Alligation Alternate is the proces:s of finding the proportional quantities to be taken of several articles or ingredients, whose prices or qualities are known to form a mixture of any given rate or quality.
    438. To find the proportional quantity to be used of euch ingredient, when the mean price or quality of the mixture is given.

    Ex. 1. What relative quantities of timothy seed worth $s 2$ a hushel, and clover seed worth $\$ 7$ a bushel, must be used to form a mixture worth $\$ 5$ a bushel ?

    > | OPERATION. |  |
    | :--- | :---: |
    | $6\left\{\begin{array}{l\|c\|c}2 & \frac{1}{8} & 2 \\ 7 & \frac{1}{2} & 3\end{array}\right\}$ Ans. |  |

    Analysis.- Since on every ingredient used whose price or quality is lese than the mean rate there will be a gain, and on avery ingredient whose price or quality be a lose, and since the gains and la grenter than the mean rate there will quantities used of each should and losses must be exactly equal, the relative one bushel of timothy seed worth such as reprosent the unit of value. By selling $\$ 1$ would require tof a bushorth $\$ 2$, for $\$ 5$, there is a gain of $\$ 3$; and to gain bushel of clover seed worth $\$ 7$, for $\$ 5$, we pizes opposite the 2 . By selling one require tof a bushel, whioh we place there is a loss of $\$ 2$; and to lese $\$ 1$ woald
    In every case, to find the we place opposite the 7 .
    per busbel or yound, \&ce. Honee if, valuo we must divide $\$ 1$ by tho gain or loss soed, we take $\ddagger$ of a bushel of olover seed, the we take $\ddagger$ of a bushel of timothy and wo shall have $\frac{1}{\frac{1}{2}}$ and $\frac{1}{1}$ for the proportional quantitics.

    ## alligation.

    E.x. 2. What proportions of coffees worth respectively 3, 4, 7 and 10 shillings a pound, must be taken to form a mixture worth 6 shillings a pound?

    OPERATION.
    

    Anal.ysis.-To preserve the equality of gaine and losses, wo must always compare two prices or simples one greater and one lean than the mean cute, and treat each pair or couplet, as a separate example. In the given example we form two couplois, and may compare either 3 and 10,4 and 7 , or 3 an 17,4 and 10 .

    We find that $\frac{1}{1}$ of a lb . at 3 s . must be taken to gain 1 shilling, and $t$ of a Ib . at 10s. to lose 1 shilling $;$ also $\frac{1}{}$ of a lb. at 4 s , to gain 1 shilling, and 1 lb . at 7 s . to lose 1 shilling. I'beso proportional nuinbsre, obtained by comparing the two couplets, are placed in columne 1 and 2 . If, now, we reduce the numbers in colmmes 1 and 2 to a common denominator, and use their numerators, we obtain tho integral numbers in columns 3 and 4, which, being arranged in oolumu 5, give the proportional quantities to be taken of each.

    It will bo seen that in comparing the simples of any pair or couplet, one of Which is greater, and the othgr less than the mean rate, the proportional number finally obtained for either term is the difference between the mean rare and the other term. Thus, in comparing 3 and 10 , the propertional number of the former is 4 , whi,h is the differenee between 10 and the moan rate 6 ; and the proportional number of the latter is 3 , which is the differonce between 3 and the mean rato. The same is true of every other couplet. Heace, when the simples and the mean rate are integers, tho intermediate steps taken to obtaio the final proportional numbers ins in columns 1, 2, 3 , anil 4 , may be omitted, and the same results readily found by taking the difference between each simple and the mean rate, and placing it opposite the one with which it is compared.

    From the foregoing examples and analyses we derive the following
    439. Rule.-I. Write the several prices or quatities in a column and the mean price or quality of the mixture at the left.
    II. Form couplets by comparing any price or quality less, with one that is greater than the mean rate, placing the part which must be used to gain 1 of the mean rate opposite the less simple, and the part that must be used to lose 1 opposite the greater simple, and do the same for cach simple in every couplet.
    III. If the proportional numbers are fractional, they may be reduced to integers, and if two or more stand in the same horizontal line, they must be added; the final results will be the proportional quantities required.

    Notes. 1. If the numbers in any couplet or column have a common feotor, it may be rejeoted.
    2. We may also multiply the numbers in any couplet or coluinn by any multiplier we chouse, without affecting the equality of che gains and losses, and thus obtain an indefinite number of resulte, any one of which boing taken will give a correat final result.

    3, 4, 7 and rorth 6 shil.
    the equality $t$ always eomjne greater rate, and treat parato examwe form two either 3 and ad 10.
    38. must be $d$ of alb. at 1 lb . at 7 s . mparing the the numbers merators, we yod in oolumu
    plet, one of ional number rate and the of tho former tho propornd the mean simples and the final prond the same and the mean
    re the fol-
    lities in a the left.
    less, with art which ss simple, eater sim-
    ey may be ame horibe the pro-
    non factor, it
    y any mulraz, and thus will givo a

    ## exampleg for practior.

    1. A grocer has nugars worth 10 cents, 11 cents, and 14 cents per pound; in what pr : rtions may he mix them to form a mixture worth 12 ct., per lb .? dns. 1 lb . at 10 cts., and 2 lb . at 11 and 14 cts .
    2. What proportions of water at no value, and wine worth $\$ 1.20$ a gallon, must be used to form a mixture worth 90 cents a gallon? Ans. 1 gal. of water to 3 gal . of wine.
    3. A farmer had sheep worth $\$ 2, \$ 2 \frac{1}{2}, \$ 3$, and $\$ 4$ per head ; what number could he sell of each, and realize an average price of $\$ 23$ per head? Ans. 5 of the 1st. kind, and 1 each of the 2nd. and 3rd., and 3 of the $4 t h$. kind.
    4. What relative quantities of alcohol $80,84,87,94$, and 96 per cent. strong must be used to form a mixture 90 per cent. strong?

    Ans. 6 of the first two kinds, four of the 3rd., 3 of the 4 th. and 16 of the 5th.
    440. To find the proportional quantity to be used of each ingredient, when the quantity of one of the simples is limited.

    Ex. A miller has oats worth 30 cents, corn worth 45 cents, and barley worth 84 cents per bushel; he desires to form a mixture worth 60 cents per bushel, and which shall contain 40 bushels of corn; how many bushels of oats and barley must he take?

    $$
    \begin{aligned}
    & \text { OPERATION. }
    \end{aligned}
    $$

    Analyais. By the same prooess as in Case I we find the proportional quantitiny of each to be 4 bushels. oats, 8 of eorn, and 10 of barley. But we wish to use 40 bushels of corn, whioh is 5 times the proportional number 8, and to proserve the equality of gain and loss we must take 5 times the proportional quantity of each of the other simples, or $5 \times 4=20$ bushels of oats, and $5 \times 10=50$ bushels of barley. Heuce the following
    441. RuLe.- Find the proportional quantitios as ill 438. Divide the given quantity b!y the proportional quantity of the same ingredient, and multiply each of the other proporlional quantities by the quotient thus obtained.

    ## eXAMPLES FOR PRACTICE.

    1. A merchant has teas worth $40,60,75$, and 90 cents per pound; how many pounds of each must he use with 20 pounds of that worth 75 cents, to form a mixture at 80 cents?

    Ans. 20 lbs . each of the first three kinde, and 130 lbs . of the fourth.
    2. A farmer bought 24 sheep at $\$ 2$ a head; how many must he buy at $\$ 3$ and $\$ 5$ a head, that he may sell the whole at an average price of $\$ 4$ a head, withoat loss? Ams. 24 at $\$ 3$, and 72 at $\$ 5$.
    3. How much alcohol worth 60 oents a gallon, and how much water, must he mixed with 180 gallons of rum worth $\$ 1.30$ a gallon, that the mixture may be worth 90 cents a gallon?

    Ans. 60 gallons each of aloohol and water.
    4. How many acres of land worth 35 dollars an acre must be added to a farin of $75^{\circ}$ acres, worth $\$ 50$ an acre, that the average value may be 540 an acre?
    5. A merchant mixed 80 pounds of sugar worth Ans. $6 \frac{1}{4}$ cents per pound with some worth $8 \frac{1}{3}$ cents and 10 cents per pound, so that the inixt. ure was worth $7 \frac{1}{2}$ cents per pound; how much of each kind did he use?
    442. To find the proportional quantity to be used of each ingredient, when the quantity of the whole compound is limited.
    Ex. A grocer has sugars worth 6 cents, 7 cents, 12 cents, and 13 cents per pound. He wishes to make a mixture of 120 pounds worth 10 cents a pound; how many pounds of each kind must he use?
    

    Analysis. By Case 1 we find the proportional quantities of eaoh to be 3 lbs. at 6 ets., 2 lbs. at 7 cts., 3 lbs. at 12 cts., and 4 lbs. at 13 ots. By adding the proportional quantities, we find that the mixture would be but 12 lbs. while the roquired mixture is 120 , or 10 times 12. Il' the wholo mixture is to be 10 times as much as the sum of tho proportional quantities, then the quantity of each simple used must be 10 times as much as its respeotive proportional, which would required 30 lbs . at $6 \mathrm{cts} ., 20$ lbs. at $7 \mathrm{cts} ., 30 \mathrm{lbs}$. at 12 ots., and 40 lbs, at 13 cts. Hence wo deduee the following
    4433. Rule. - Find the proportional numbers as in 438. Divide the given quantity by the sum of the proportional quantities, and multiply each of the proportional quantities by the quotient thus obtained.

    ## EXAMPLES FOR PRAOTICE.

    1. A furmer sold 170 sheep at an average price of 14 shillinge a head; for some he received 9 s., for some 128. , for some 188. , and for others 20 s . ; how many of each did he sell?

    Ans. 60 at $9 \mathrm{~s} ., 40$ at 12s., 20 at 18s., and 50 at 20 s .
    2. A jeweler melted together gold $16,18,21$, and 24 carats fine, so as to make a compound of 51 ounces 22 earate fine; how much of each sort did he take? Ans. 6 ounces each of the first three, and 33 ounces of the last.
    3. A man bonght 210 bushels of oats, corn, and wheat, and paid for the whole $\$ 178.50$; for the oats he paid $\$ \frac{1}{2}$, for the corm, $\$ 3$, and for the wheat $\$ 1 \frac{1}{2}$ per bushel; how many bushels of each kind did he ouy? Ans. 78 bu. each of oate and corn, and 54 bu . of wheat.
    4. A, B, and C are undor a joint contract to furnish 6000 bushels of corn, at 48 cts. a bushel; A's corn is worth $45 \mathrm{ets}$. , B's 51 ets ., and C's 54 ctss ; how many bushels must each put into the mixture that the contract may be fulfilled?
    5. One man and 3 boys received $\$ 8 t$ for 56 days labor; the man received $\$ 3$ per day, and the boys $\$ \frac{1}{2}, \$ \frac{3}{4}$, anci $\$ 1 \frac{1}{4}$ respectively; how many days did each labor? Ans. The man 16 days, and the boys 24,4 , and 12 days respectively.

    ## INVOLUTION.

    444. Involution is the prooess of raising a number to a given power.
    445. A Power is the produot arising from multiplying a number by itself, or repeating it several times as a factor,
    446. The Index or Exponent of a power is a small figure placed at the right and a little above the number, to show how many times it is used to produce the power :-
    Thus, $\left\{\begin{array}{l}3^{3}=\text { the first power of } 3, \text { or the root. } \\ 3^{2}=3 \times 3=9, \text { the second power, or square of } 3 . \\ 3^{3}=3 \times 3 \times 3=27, \text { the third power, or culve of } 3 . \\ 3^{4}=3 \times 3 \times 3 \times 3=81, \text { the fourth power of } 3 . \\ (3)^{4}=2 \times 3 \times 3 \times 3 \times 3=\frac{3}{243}, \text { the fifth power of } 3 .\end{array}\right.$
    Henoe, from these several powers of 3 , we derive the following
    447. Rule.-Multiply the given number by itself as many times, less 1, as there are units in the exponent of the required power.

    Nots. - A mixed number may be either reduced to an improper fraotion, or the frectional part reduced to a decimal, before involution.

    1. Square 25.
    2. Square 79.
    3. Cube 47 .
    4. Cube 39.
    5. $24^{4}=$ ?
    6. $(1.2)^{s}=$ ?

    Ans. 225.
    Ans. 6241. Ans. 103823.
    Ans. 59319.
    Ans. 331776.
    Ans. 2.48832.
    7. $(1.06)^{4}=$ ? Ans. 1.262476 .
    8. $\left(\frac{2}{8}\right)^{3}=$ ?
    9. $\left(\frac{7}{8}\right)^{3}=$ ?
    10. $\left(2_{8}^{2}\right)^{4}=$ ?
    11. $\left(1 \frac{3}{5}\right)^{6}=$ ?
    12. $(2)^{6}=$ ?

    Ans.
    Ans. $\frac{\rho^{2} 5^{5}}{5}$.
    Ans. $50 \frac{1}{81}$.
     Ans. $1577^{288} 8{ }^{8}$

    ## EVOLUTION.

    448. Evolution is the proeess of extracting the root of a number considered as a power; it is the reverse of Involution.
    449. The Root of a number is one of its equal faotorn.
    450. The First Root of a number is the number itrice.
    451. The Second Root, or Square Root, of a number, is one of its two equal factors. Thus, 4 is the square root of $16=$ $4 \times 4$.
    452. The Third Root, or Cube Root, of a number, is one of its three equal factors. Thus, 4 is the cube root of $64=4 \times$ $4 \times 4$.
    453. The Radical Sign is the character, $V$, which, placed before a number, indieates that its root is to be extracted.
    454. The Index of the root is the figure placed above the radical sign, to denote what root is to be taken. When no index is written, the index, 2 , is always understood.
    455. The names of roots are derived from the corresponding powers, and are denoted by the indices of the radical sign. Thus, $\sqrt{36}$ denotes the square root of $36 ; \sqrt[3]{36}$ denotes the cube root of $36 ; \sqrt[4]{36}$ denotes the fourth root of 36 ; etc.
    456. A Rational Root is a root which oan be exaetly obtained.
    457. A Surd is one which cannot be exactly obtained.

    ## SQUARE ROOT.

    The roots of the first ten integers and their squares are:

    $$
    \begin{array}{rrrrrrrrrr}
    1, & 2, & 3, & 4, & 5, & 6, & 7, & 8, & 9, & 10 . \\
    1, & 4, & 9, & 16, & 25, & 36, & 49, & 64, & 81, & 100 .
    \end{array}
    $$

    Norrs.-1. It will be observed that the seoond power or square of each of the numbers ountains twice as many figures as the root, or twice as many wanting one. Hence, to ascertain the number of figures in the squaro root of a given namber,-Begimning at the right, point it off into as many periods ats possible, of noo jigures each; and there will be as many figures in the root as there are periods.
    2. When the given number contains an odd number of figurea, the period ${ }^{\circ}$ the left can contain but one figure.

    Ex. What is the square root of 4096 ?
    
    umber, is of $16=$ ber, is one $4=4 \times$
    h, placed d. above the no inder
    esponding n. Thus, be rook of exactly
    458. Rurce.-I. Point off the given number into periods of tonn figures each, counting from units' place toward the left and right. II. Find the greatest prrfect square in the left-hand period and write its root on the right for the first figure in the root.
    III. Subtract the square of the mont figure from the left-hand period, and to the remainder annex the next perind for a dividend.
    IV. Double the part of the ront already found for a trial divisor, and see how many times it is contained in the dividend, exclusive of the right-hand figure, and write the quntient as the next divisor of the root, and also at the right of the trial divisor.
    V. Multiply the divisor thus formed by the figure of the root last found, and subtract the product from the dividend.
    VI. To this remainder annex the next period for a new dioidend, and divide the same by twice the root already found, and continue in this manner until all the periods are used.
    Norss.-1. When any dividend, exclusive of its right-hand igure, does not contain the divisor, a cipher must be plaoed in the root, and also at the right of the divisor; then, $f$ fto ringing down the nert period, this last divisor must be used as the diviso " ${ }^{-1}$. 3 new dividend.
    2. When there, binaler after all the periods have boen brought down periods of ciphers ring be annexed, and the figuros of the root thus obtained will be decimals.
    3. If the given number is a desimal, or a whole number and a decimal, tha root is extracted in tho same manner as in whole numbers, except, in pointing off the decimals, either alone or in connection with the whole nuaber, we place a point over every second figure toward the right, from the separatrix, filling the last period, if incomplete, with a oipher.
    4. The square root of a common fraction way be obtained by extracting the equare roots of the numerator and denominator soparately, provided the terme are perfect squares; otherwiso, the fraction may he reduced to a decimal.
    5. Mixed numbers may be reduced to the docinal form before oxtracting the root ; or, if the denominator of the fraction is a perfect square, to an improper
    fraction.

    ## EXAMPLES FOR PRACTIOK.

    1. What is the equare root of 1332259 of 62.8 ? OPERATION.
    
    2. What is the equare root of 169 ? of 576 ? of 1225 ? of 2401 ? of 3249 ? of $\mathbf{4 9 9 6}$ ? of 5329 ? of 6724 ? of 9801 ? of 10816 ?

    Ane. $13,24,35,49.57$. 64, ato
    3. What is the equare root of 41009 ? of 454176 ? of 505521 ? of 637821 ? of 648132 ? of 738417 ? of 809.15 ? of 927748 ? of 977137 ? of 999999 ? Ans. 247, 674, 711, 798, 805, 859, 899, etc.
    4. What is tl - square root of 234.09 ? of 5.4756 ? of 17.3056 ? of 256.6404 ? of $0 . . J 24$ ? of 0.120409 ? of 0.00008836 ? of 609151.76100 ? Ans. 15.3, 2.34, 4.16, 16.02, $0.32,0.347,0.0094,780.481$.
    5. What is the square root of $\frac{3}{4}$ ? of $69 \frac{974}{9} ?$ of $5^{49}$ ? of $60 \frac{1}{18}$ ? of $\frac{48}{147}$ ? of $\frac{8}{5}$ ? of 28574 of $\frac{12}{5}$ ? of $\frac{1008}{203}$ ? of $95 \frac{1}{16}$ ?

    Ans. $0.86602+, 2 \frac{7}{12}, \frac{7}{88}, 7, \frac{2}{5}, 0.7745+, 5 \frac{2}{2} .0 .858+, \frac{1}{4}, 9$.

    ## applications of the gquare root.

    1. What is the length of one side of a square farm containing 90 acres?

    Ans. 120 rods.
    2. A certain general has an army of 141376 men; how many must he place in rank and file to form them into a square? Ans. 376.
    3. A company of persons epent $\$ 75.69$; each spending as many cents as there were persons in the company. How much did each expend? Ans. \$0.87.
    4. Bought 200 yards of carpeting $1 \frac{1}{4}$ yards wide; what is the length of one side of the aquare room which this carpet will cover? A. 45 ft .
    5. A man owns three pieces of land ; the first is 125 rods long, and 53 wide; the sucond is 6,212 rods lung, and 34 wide; and the third contains 37 acres: what will be the length of the side of a square field whose area will be equal to the three pieces? Ans. $121.11+$ rods.
    6. Purchased 2 house-lots; the first is 242 feet square, and the second contsins 9 times the area of the firat; how many feet equare in the second?

    Ans. 726 feet.
    7. Required the sides of a rectangular court-yard having an area of 432 rods, and whose breadth is only the $\frac{8}{4}$ of the length?
    8. A cerwin field contains 48020 square rods; the length exceeds the breadth by 49 rods: what are the sides?

    Ans. 245 rode long; 196 rods wide.
    9. A school-master says that the number of his pupils multiplied by $\frac{1}{2}$ of itself is 2523 ; how many pupils has he?

    Ans. 8\%.
    10. How nuuch will it cost to roughcast the walls of a garden, having a surface of 8100 yards, at $87 \frac{1}{\mathrm{~h}}$ cte. per yard, the walls being $2{ }^{3} \frac{3}{0}$ yd. high ?

    Ans. $\$ 1449$.
    11. The greater of two numbers is 40 , and the eum of their squares 1625 ; what is the smaller number?

    Ans. 5.
    12. A clock-maker sold ihree watches whone prioes are as 5 is to 6 , and as 6 is to 9 ; the sum of the squares of the prices is 83550 . What is the price of each watch?

    Ane. $\$ 25, \$ 30, \$ 45$.
    13. What is the price of a raking machine, knowing that the price added to ite square gives $\$ 186$ for result ?

    - Ans. \$13.13 $\frac{1}{2}$.
    1.1. In dividing the square of the number of dollafy that I hafo by $\frac{1}{4}$ of the number iteelf I obtain $\$ 96$ for result. How many barrele of codfich, at \&t per barrel, ana I buy with the momoy I pomones


    ## CUBE ROOT.

    The roots of the first ten integers and their cubes are:-

    $$
    \begin{array}{rrrrrrrrrr}
    1, & 2, & 3, & 4, & 5, & 6, & 7, & 8, & 9, & 10 . \\
    1, & 8, & 27, & 64, & 125, & 216, & 343, & 512, & 729, & 1000 .
    \end{array}
    $$

    Note. - it will be observed that the cabe or third power of each of the uum bers contains three times as many figures as the root, or three times as many wanting ine, or tron at most. Hence, to determine the number of figures in the cube rout of a given number, - Beginning at the right, point it off into as many porit as tse poseible of three fiymres each, and there sill be as many figures in the
    root there are periods.

    ## A.r. What is the cube root of 157464 ?

    | opematiom. |  |
    | :---: | :---: |
    | (1) $6^{\mathbf{a}}=$ | $\begin{aligned} & 15746 \dot{4} \text { ( } 54 \\ & 125 \end{aligned}$ |
    | trial div., ${ }^{3} \times 50^{2}=7500$ | $\longdiv { 3 2 4 6 4 }$ |
    | $3 \times 50 \times 4=600$ | 32464 |
    | True divisor, $\quad \overline{8116} \times 4=$ | 32464 |
    | PROOF. |  |
    | $64 \times 54 \times 54=15746$ |  |

    plas thres times the tens intu the square of the units, plas the tensinto the units, Tho cube of tens is thousands, and muat the units, plas the oube of the units. the number. The groatest number of tens whose be found iu the thousands of eands is 5 , which we write an the tean figure of the root. Wot exceed 157 thou125 thousands, the oube of the 5 tene, from the 157 thous. We then subtract the 32 thnusands; and, annexing the next period, we have as the ant there remain 32484, equal three times the square of the tons into the as the entire remainder, the tens into the square of the units, plus the euto the onite, plus three times three times the square of the tens, plus three times or the units, or the product of the square of the units, multiplied by the units thes the tens into the units, plus three times the square of the tens of the root, we by dividing this rerasisder by somewhat ton large. Although it may be too large, it cannot bo tor a number the remainder 32464 contains not only three timos the square of the tens into the onits, but three times the tens into the equare of the units, plus the cube of the units. We therefore make three times the square of the tens of the ront, $=75$ hundreds, a trial divisor, with which we divide the 324 hundreds of the remainder, disuare of the tens by unite, since they cannot form any part of the produot of units figare of the root, or a nomits. The quotient figure obtained, 5 , must be the complete the divisor on the surpeeition that larger. But on undertaking to Fre find a divisor too iarge lor the remainder. Wo true unita syure of the root, one lesm, and to detormine whether it ander. We tharefore take 4, a number root, we add to the 75 hundreds of it oxpresses the real number of units in the root into the 4 units, plus the square of the 4 anite; and maltiplying the the divisor, 81116, thus formed, by the units, and aubtreotiog the ping the true from the rempinder, thano is nothing lofh, and eubtraoting the produet, 32484, 64 the arbe rook.

    Analysis,-Beginsoparate the given number into periods, by placing a point over the units' figure, then over thousande. Since the number of periods is two, the root will consist of two figures, tens and units. Then $157464=$ the oube of tens, plusthree times the square of

    ## 

    ## 246

    459. Role.-I. Point off the given number into periode of three figures each, counting from usits place toward the left and right.
    II. Find the greatest cube that does not exceed the left-hand period, and write its root for the first figure in the required root; subtract the cube from the left-hand period, and to the remainder bring down the next period for a dividend.
    III. At the left of the dividend write three times the square of the first figure of the root, and annex two ciphers, for a trial divisor ; divide the dividend b. the trial divisor, and vorite the quotient for a trial figure in the root.
    IV. Add to the trial divisor three times the product of the tens figure of the root by the units figure with a cipher annexed, and the square of the last figure, for a true divisor.
    V. Multiply the complete divisor by the trial figure; subtract the product from the dividend, and to the remainder bring down the next period for a new dividend.
    VI. Multiply the square of the root figures already found, by 3, and to the product annex two ciphers for a neto trial divioor; and proceed as before until all the periods are brought down.

    Notr.-The observations made in Notes 1, 2, 3, 4, and 5, nader the rule for the extraotion of the square root (458), are equally applicable to twe extraction of the cube root, except that two ciphers must be placed at the right of a true divisor when it is not oontained in its oorresponding dividend; and, in pointing of decimals, each period must contain three figures.

    EXAMPLES FOR PRACTIOR.

    1. What is the cube root of 12326391 ?
    opkration.

    | $2^{3}$ | ${ }_{8}^{1} 23239 i$ |
    | :---: | :---: |
    | Trial livisor, $3 \times 20^{2}=1200$ |  |
    | $3 \times 20 \times 3$  <br> $3^{2}$ $=$ | 4326 |
    | True divisor, $\quad \overline{1389} \times \mathbf{3}=$ | 4167 |
    | Trial divisor, $\begin{aligned} 3 \times 230^{2} & =158700 \\ 3 \times 230 \times 1 & =$ <br> 100\end{aligned} | 169391 |
    | $1:=1$ |  |
    | True divisor, $\overline{169391} \times 1=$ | 169391 |

    2. What is the cube root of 1331 f of 3375 ? of 121677 of 32768 ? of 110592 ?

    Ans. 11, 15, 23, 32, etc.
    5. What is the cube root of 185188 ? of 272144 ? of 456533 ? of 704969 \% of 970299 ?

    Ame. St, 64, 77, 89, etc.
    4. What is the oube root of 1367631 ? of 9938375 ? of 41781923 ? of 96071912 ? of 184220009 ? of 300763000 ? of 476379541 ? of 709 732288 ? of 736314327 ? of 997002999 ? Ans. 111, 215, 347, 458, 569, 670, 781, 892, 903, etc.
    5. What is the cabe root of 9.15 ? of 51662.1837824 ? of 11.03 ? of 0.518 ? of 0.12965 ? Ans. 2.091, 37.244, 2.22, 0.803, 0.2349.
    6. What is the cube root of $34 \frac{1}{4}$ ? of 1 ? of $39 \frac{38}{138}$ ? of 1358 ? of
    

    ## APPLICATIONB IN OUEE ROOT.

    1. A mason wishes to make a cubical cistern that shall oontain 2744 cubic feet of water; what must be the length of one of its sides ?
    2. A miller has a cubical box that $A n s$. 14 feet. what is the depth of the box?
    3. What quantity of paper which shall contain $\frac{27}{84}$ of a solid e required to make a cubical boz
    4. A carpenter has a plank 1 foot wide, 223 ? Ans. $\frac{3}{8}$ of a yd. inches thick; and wishes to make a box whose $\frac{3}{7}$ feet long, and $2 \frac{1}{2}$ its height, and whose length shall te twice whose width shall be twice contents of the box.
    5. How much must be pard for a Ans. 5719 cub. in. seed, bought at 55 cents per lb, ar certain number of pounds of lin. the number equal 26509168 ? ., knowing that the $\frac{?}{3}$ of the cube of
    6. A mattrese sum such that the 13 purchased 84 lb . of hair, for which he gave a vame cube equal $\$ 0.6591$. .
    7. Required the value of the articles contained Ans. $\$ 1 \$ 3.80$. containing as many articles, which cost contained in 25 boxes, each boxes?
    8. What is that number, whose 1 , and Ans. \$156.25. give 9 for product? $\}$ 9. Bought $\$ 164.64$ worth of oranges Ans. 6 . number of boxes, each containing oranges packed up in a certain there are boxes; and each orange cost times as many oranges as are boxes. Required the numge costs twice as many oents as there .
    9. In dividing the cube of a certain. Ane. 14 boxer, 588 oranges. of the same number, we obtain 131 number by the $?$ of the square ber? 11. A reaervoir, whose length is to its hreedth Ans. 9 . depth as 13 is to 3 , contains 99840 oubio dimencions of the reservoir?

    Ans. length 104 ft ., breadth 40 ft ., depth 24 f .
    12. Some merchants formed a partnership in which each partner vereted 1000 as many dollass as there wore amociates. Having made
    a profit of $\$ 2560$, they find that they have gained the half an muah per cent. as there are sisociates. How many partners were there is the company?
    13. An inlayer bous. Ans. \$1.35 per lb., and multiplying the quantity of pearl-shells; by paying the $\frac{5}{2}$ of itself, it gives a product of 59049 . Required the number of lbe. he bought?
    14. How much must $A n s .35 \frac{5}{27} 16$. certain number of mast a merchant pay, at 55 cents per 1 b. , for a certain number of bales of wool, each bale containing 145 lb ., che number of bales being such that in multiplying together its $\frac{3}{8} \frac{5}{6}$, and
    Ans. $\$ 3828$.

    Ans. $\$ 3828$.

    ## PROGRESSIONS.

    ## ARITEMETIOAL PROGRESBIOK.

    460. An Arithmetical Progression is a series of numbers increasing or decreasing by a constant difference.
    461. The Terms of a series are the numbers of which it is formed.
    462. The Extremes are the first and last terms,
    463. The Means are the intermediate terms.
    \$64. The Common Difference is the number added or subtracted. in order to form each successive tern.
    464. An Ascending Series is produced by adding the oommon difference to cach term suceessively ; as, $\mathbf{1}, \mathbf{3}, \mathbf{5}, \mathbf{7}, \mathbf{9}$, $11,13,15$, and 17.
    465. A Descending Series is produced by subtracting the common difference from each term sucoessively; as. $17,15,13$, $11,9,7,5,3$, and 1 .
    466. The sum of the extrem is equal to the sum of any two terms equally distant from them, or to double the middle term. Thus,

    $$
    \begin{array}{rrrrr}
    1 & 3 & 5 & 7 & 9 \\
    17 & 15 & 13 & 11 & 9 \\
    \hline 18 & \frac{9}{18} & \frac{9}{18} & \frac{18}{18} & \frac{18}{18}
    \end{array}
    $$

    468. The following are the five quantities considered, three of whioh being given, the other tioo may be found :-
    469. The first term,
    470. The last term,
    denoted by
    a.
    471. The oommon' difference,
    472. The number of terms,

    | " | " | 1. |
    | :--- | :--- | :--- |
    | " | " | c. |
    | " | " | n. |

    5. The sum of all the terms,
    " "
    s.

    ## 413. Case I.-Given the first term, the common differgnce, and the number of terms, to find the last term.

    Ex. The first term of an ascending series is 4 , the common difference 3 , and the number of terms 19 ; what is the last term?$$
    18=19-1
    $$

    Amalirsig. - The first torm is 4, the second torm $=$ 4 - once the common diffe ence, the third term $=$ inet twice the common differenee, ote. Therefore the Iact torm $=4+18$ times the common difference. Hence the Formala, $\mathbf{n}+(\mathbf{n}-1) \mathbf{c}=\mathbf{1}$, or the
    471. Rule. -To the first term add the product of the common difference and the number of terms less one.
    Here.-If the arios is dmoending, anbtriot the product from the first torm.

    ## Examples por pratotioe.

    1. The first term of an ascending series is 8 , the common difference

    5, and the number of terms 40 ; what is the last term? Ans. 203.
    2. I bought 16 acres of land, giving $\$ 1$ for the first acre, $\$ 9$ for the this rate? 3. The first term of a descending series is 75, Ans. $\$ 121$. ference 5 ; what is the 13 th. terin? series is 75 , and the common dif. 4. A board, 21 inches wide at the narrow end, and Ans. 15. increases in width $1 \frac{1}{2}$ inches for every foot in length. 10 feet long, width of the wide end?
    5. If the first term of an accending series be 3 , the Ans. $17 \frac{1}{1} \mathrm{in}$. l, and the number of terms 20, what is the last the common difference

    $$
    \text { Anac ravinglece } a+(n-1) c=1, c=\frac{1-a}{n-1} \text {. Hence, the }
    $$

    472. ROLs.- Divide the diference of the extremes by the number of terms less one.

    ## EXAMPLES FOR PRACTIGE.

    1. The first term is 3, the last term ie 15 , and the number of terms is 7; what is the common difference? the common difference? 3. A man has 10 sons; the youngeat is 8 , and thes. 3. old ; their ages increase in arithmetical p, and the eldest 44 years difference of their agoe?
    2. If the extremes are 0 and $2 \frac{1}{2}$, and the number of terms is 18 , what is the common difference?

    Ans. $\frac{5}{3!}$.
    473. Case [II.-Given the extremes, and the common difference, to find the number of terms.

    $$
    \text { Axalysis. }- \text { Since, } \mathbf{a}+(\mathbf{n}-1) \mathbf{c}=\mathbf{1}, \mathbf{n}=\frac{\mathbf{1}-\mathbf{a}}{\mathbf{c}}+1 \text {. Henoe, the }
    $$

    474. Rule.-Divide the difference of the extremes by the comnion difference, and increase the quotient by 1.

    ## EXAMPLES.

    1. The first term is 8 , the last term $\mathbf{2 0 3}$, and the common difference 5 ; what is the number of terms?

    Ans. 40.
    2. A man going a journey travelled the first day 7 miles, the last day 51 miles, and each day increased his journey by 4 miles; how many days did he travel?

    Ans. 12.
    3. The extremes are $2 \frac{1}{4}$ and 40 , and the common difference is $7 \frac{1}{2}$; what is the number of terms? Ans. 6.
    4. In what time can a debt be discharged, supposing the first week's payment to be $\$ 1$, and the payment of every succeeding week $t 0 \mathrm{in}$ crease by $\$ 2$, till the last payment shall be $\$ 103$ ? Ans. 52 weeks.
    475. Case IV.-Given the extremes, and the number of terms, tn find the sum of all the terms.
    ANALYSIS. - Since, the sum of the extremes of an arithmetical progression is equal to the sum of any two terms equally distant from them, it follows that the corms must average half the sum of the extremes. Henoe, $\mathrm{m}=\mathbf{1}(\mathbf{a}+\mathbf{1}) \mathrm{m}$.
    476. RuLe.-Multiply half of the sum of the extremes by the number of terms.

    ## EXAMPIEB.

    1. The extremes of an arithmetical series are 3 and 19 , and the number of terms 9 ; what is th: suin of the series? Ans. 99.
    2. A inan bought 16 acres of land, giving $\$ 1$ for the first acre, and $\$ 121$ for the last aere; the prices of the successive acres form an arithmetical progression. How much did the 16 acres cost? Ans. $\$ 976$.
    3. A gentleman wishes to discharge a deht in 11 annual payments such that the last payinent shall be $\$ 220$, and each payment greater than the preceding by $\$ 17$; what is the amonnt of the debt, and the first payment? Ans. 1st. payment, $\$ 50$.
    4. A merchant bought 20 pieces of cloth, giving for the first, $\$ 2$, and for the last $\$ 40$; the prices of the pieces form an arithmetical series; how much did the cloth cost? ins. $\$ 420$.
    5. If 100 oranges are placed in a line, exactly 2 yards from each other, and the first 2 yards from a basket; what distance must a boy travel, startine from the basket, to gather them up singly, and return

    19 is 18 , n8. $\frac{5}{34}$. non difHence, the s by the lns. 12. ce is $7 \frac{1}{2}$; Ans. 6. rst week's sek to in. weeks.
    of terms,
    gression is ws that the $\mathbf{t 1 )} \mathbf{n}$. remes by , and the Ans. 99. acre, and rm an ar1s. $\$ 976$. payments nt greater $t$, and the ent, $\$ 50$.
    : first, \$2, rithmetical 28. $\$ 420$. from each must a boy and return

    ## geombtrical progression.

    477. A Geometrical Progression is a series of numbers increasing or decreasing by a constant ratio.
    478. 'The Ratio is the constant multiplier or divisor.
    479. An Ascending Series is produced by any ratio greater than 1 , as 2, 4, 8, 16, 32, 64, etc.
    480. A Descending Series is produced when the ratio is less than 1 ; as $1, \frac{1}{2}, \frac{1}{4}, \frac{1}{8}, \frac{1}{18}, \frac{1}{32}, \frac{1}{85}$, ete.
    481. The following are the five quantities considered, three of which being given, the other two may be fuind:-
    482. The first term,
    483. The last term,

    | denoted by | a. |  |
    | :---: | :---: | :---: |
    | " | " | $\mathbf{1}$. |
    | " | " | $\mathbf{r}$. |
    | " | " | $\mathbf{n}$. |
    |  | " | $\mathbf{m}$. |

    Norm.-The Qeomatrical Mean between two numbers in the aquare root $\alpha$

    ## Chair produet

    182. Cass I.-Given the first term, the ratio, and the number of terms, to fint the last term.
    E.x. The first term of a geometrical series is 4, and the ratio is 3 ; what is the 9th. term?

    Analysis.-The first term $=4$, and from the nature of the series,

    > The second term $=4 \times 3^{1}$ The third term $=4 \times 3^{2}$
    > The formth opermation. and so on. Hence, the last term, $1=a \times \mathbf{r}^{n-1}=3^{8}=26244$, Ans.
    483. Rule.-Multiply the first term by that power of the ratio denoted by the number of terms, less one.
    Norn,-If the series is deoreasing, oonsider the first term as the last, and the last as the first, the ratio will then be greater than 1.

    ## EXAMPLLBS.

    1. The first term of a geometrical series is 2 , and the ratio 3 ; what is the 10 th. term?
    2. The first term of a series is 1458 , the number of terms 7 , and
    3. the ratio $\frac{1}{8}$; what is the last term? Ans. 2.
    4. A woman bought 9 egga, agreeing to pay 1 mill for the first egg, 2 mills for the second, and so on; what did the last egg cost her? Ame. $\mathbf{3} 0.256$.
    5. If the first term of a neriea in $\mathbf{3 0}$, the ratio 1.06 , and the number of terms 6 ; what is the last term?

    Ans. 40.146767328.
    5. A person traveling goes 2 miles the first, 4 miles the second 8 miles the third day, and so on, increasing in geometrical progression for 10 days. How fur did be travel the last day? Ans. $10 " 4$ miles
    6. Bought a lot of land containing 15 acres, agreeing to puy for the whole what the last acre would come to, reckoning 5 cts. for the first aare, 15 cts. for the second, and so on, in a threcfild ratio. What did the lot cost me?

    Ans.
    184. Case II.-Given the extremes and ratio, to find the sum of all the terms.

    Es. The first term is 2 , the last term is 128 , and the ratio $4 ;$ so quired the sum of all the terms.

    ## OFBRATION.

    $$
    \begin{array}{r}
    8+32+128+512=4 \times \text { sum of the series } \\
    2+8+32+128=1 \times \text { sum of the series } \\
    \begin{array}{r}
    512-2=3
    \end{array} \times \text { sum of the series. } \\
    \text { Hence } \frac{512{ }^{8}-2}{}=170, \text { the sum of the series. }
    \end{array}
    $$

    Aralysis.-Since $512=\mathbf{1 r}, 2=a$, and $3=\mathbf{r}-1,0=\frac{\mathbf{1 r}-\mathbf{a}}{\mathbf{r}-1}$.
    Hence, the
    485. Role.-Multiply the last term by the ratio, subtruct the first term from the product, and divide the remainder by the ratio less one.

    Norrs.-1. If the ratio is leme than 1, the product of the last torm, maltiplled by the ratio, must be snbtracted from the frit term; and, to obtain the divisor, the ratio must be subtrasted from the nnity, or 1 .
    2. When a desoending serios is continued to infinity, it becomes what is called an Ixpinits saming, whose leat torm must be regarded at 0, and its ratio as a fraction.
    To find the sum of an Infinite Sories, - Dreide the firwt lerm by a wait diminiohed by the fradion dencting the rutio.

    ## EXAMPLES.

    1. The frst term of a series is 4, the lant term is 62500, and the ratio 5 ; what is the sum of all the terms?
    2. If the first term of a series is 12 , the ratio 3 , and the number of terms 8; what is the sum of the series? Ans. 39360.
    3. The first term of a decreasing series is 102 , the last terin 4 , and the ratio $\frac{1}{2}$; what is the sum of the series?

    Ans. 151.
    4. If the firat term of a series is $\overline{5}$, the ratio $\frac{2}{3}$, and the number of terms 6 ; required the sum of the series. Ans. $13 \frac{106}{295}$.
    5. The first term of a decreasing series is 106 , the last term 10 , and the ratio $\frac{1}{2}$; raquined the sum of the termo.

    Ans. 130.
    6. In what time will a certain debt be diacharged by monthly pay. ments in geometrical progression, if the flrat and last payments are $\$ 1$ and $\$ 2048$, and the ratio 29 Ans. In 12 monthe. 7. A young man agreed to eerve in a store for 6 months. For the frat mouth he was to receive 83 , and each succeeding month's wages were to be increased by $\frac{2}{}$ of his wages for the month next preceding ; what sum did he receive for the 6 mouths'' Ans. $\$ 91.95+$. 8. A gentleman wishing to purchase a piece of ground, ineasuring 10 square rods, thought $\$ 1$ per sq. rod too high a price; he, nevertheless, agreed to give 1 cent for the first en. rod, 4 for the recond, 16 for the third, and so on, in a fourfold ratio ; how much did that ground
    cost him? Ans. \$3495. 25.

    ## MEASUREMENT OX LUMBER.

    486. Boards are usually measure by the square foot. The board is considered to be 1 inch in thickness.
    487 . Planks, Beams, Joists, etc., are usually measured by board measure.

    Round timber is sometimes measured by the ton, and sometimes by board measure.
    488. To find the contents of a board.

    Rule.-Multiply the length of the board, taken in feet, by ite width in feet, and the product will be the contents in sq. feet. Or, Multiply its length in feet by its width in inches, and the product divided by 12 will give the contents in square feet.
    Note.-If the board is tapering, take half the sum of the width of its ends for the width.
    E.x. 1. What are the contente of a board 36 feet long, and $1 \frac{1}{2}$ feet wide? What are the contenta of a bard 24 Ans. 54 sq. feet. wide ?
    3. What are the contents of a tapering board, 20 ins. 30 sq . feet. ends are, the one 24 inches, and the other 13 in, 20 feet long, whose
    489. To find the contents of planks, beams, joists, eto.

    Rule.-Mulliply the width, tuken in inches, by the thickness, in inches, and this product by the length, in feet; and the last product divided by 12 will give the oontents in feet, board meusure.
    Nots.-If the plank, beam, atc. is tapering in width, take hatf the sum of the width of the edds for the width; and if the taper be both of the width and the thickness, the common rule of obtaining the oontenta in cubic feet lis, to mulliply 14.

    Ex. 1. What are the contents of a plank 40 feet long, 2 feet wide, and 3 inches thick ?

    Ans. 240 sq . ft. inches How many feet are there in 9 joists, which are 15 feet long, 6 3. How many feet in 3 thick? Ans. $168 \frac{8}{4}$ feet. width tapers from 18 to 16 beams 24 feet long, 10 inches thick, whoss噱 16 inches?

    Ans. 858 feet.
    490. To find the contents of round timber.

    Rure.- Multiply the length, taken in feet, by the square of one fourth of the mean girth, talcen in inches; and, this product, dioided by 144 , will give the conients in cubric feet.
    Norms.-1. The girth of tapering timber is ausully taken about one thisd the distance from the larger to the amallor end.
    2. This rule is that in oommon use, though very far from giving the aotuan number of oubic feet in round lumber measured by it. 40 oubio feet, as given by the rale, are in fact equal to $50 \frac{92}{100}$ true oubis feet. The following rule gives results more nearly acourate, requiring to we diminishod by only one foot in 190, to give exact contents. Multi, ly the equare of one fifth of the mean givth, tabion in inches, by troice the lomgth, in foet; and divide by 144.

    Ex. 1. How many cubic feet in a atick of timber which is 50 feet long, and whose girth is 60 inches?
    2. What are the contents of a stick of timber Ans. $78 \frac{1}{8}$ cub. ft. feet, and girth 40 inches?
    3. How many cubic feet in a log 90 Ans. 205 feet. ference is 120 inches ? in a 90 feet long, and whose circum-Note.-Fur the culling and measur Ans. $562 \frac{1}{2}$ cub. feet. Staves, \&c., ac ording to the Consolidated Statutes of Canada, Ceals, See pugc 3 ij .

    ## MISCELLANEOUS EXAMPLES.

    1. A man sleeps $7 \frac{1}{2}$ hours each day. What per cent. of his time does he sizeep?
    2. What number is that to which, if you add 8 of 8 Ans. $31 \$ \%$. sum will be 61 ?
    3. A gentleman bought 95 yardo of cloth, of a yard wids. 55. and gave the same and $\$ 25$ for cloth of the same quality w, for $\$ 100$, How many yards did he buy?
    4. A father devised $\frac{7}{18}$ of his estate to one of his Ans. $899_{1 \frac{1}{6}} \mathrm{yd}$. the residue to the other $\frac{18}{8}$ and the remainder of his sons, and $\frac{7}{78}$ of ence of his sons' lar, and the res to be f257 3 wife. The differdid he leave for his widow?
    5. How many bricks 8 inches long, 4 inches wide, and 2 inct thick, will it take tu kuild a wall $40^{\circ}$ feet long, 20 feet high, inchee feet thick?
    6. If a man ean paint 4 muare yards in Ans. 43200 bricks. 6 min. 40 sec. in painting two sides of ard in one hour, and is 31 h . the wall?

    Ame. 80 8 .
    7. By selling wheat at 12 s .6 d . per bushel, I gain $£ 30$ on the quantity purchased; but if I sell it for $13 \mathrm{s}$.6 d . a bushel, I shall gain $£ 42$ on the same quantity. How many bushels were bought? Ans. 240.
    3. A grocer bought a hogshead of wine for $\$ 28.35$; how much water must be added to reduce the first to 35 cts. per gal. ? Ans. 18 gal.
    9. A futher, dying, left his son a legacy, $\frac{1}{4}$ of which he spent in 8 months; $\frac{8}{7}$ of the remainder lasted him 12 months longer, after him?
    10. A man had $\boldsymbol{z}$ of a yard of broadeloth, rate of $\$ 81$ per yard; he gave the broath, for which he paid at the of cassimere. What did the cassimere coth and 50 cents for 14 yards
    11. How many dollars. Canada currenct him per yd.? A. \$2.66 ? States currency?
    12. A grocer wishes to mix together brandy at 80 cts. a gal., wine at 70 cts., cider at 10 cts.. and water, $\frac{\text { m }}{}$ such proportions that the mixture may be worth 50 cte. a gal.; what quantity of each must be used ? Ans. 3 gal. of water, 2 of cider, 4 of wine, and 5 of brandy.
    13. If the longitude of Boston is $70^{\circ} 4^{\prime}$ west, what will be the time in that place when it is 3 h .35 min . A. M. in London $?$ Ans 10 h 54 min 44 sec. P . in London ?
    14. A merchant sold goods to 44 sec. P. M. of the previous day. of $4 \%$; and, having remitted the net proceeds to on a commission $\$$ \% for prompt payment, which amot proceeds to the owner, received commission? 15. I purchased railroad stock to the amount of Ans. $\$ 260$. found that the sum invested was $40 \%$ of amount of $\$ 2356.80$, and had I at first? 16. If $13 \frac{1}{2}$ bushels of wheat make $?$ barrels of Ane. $\$ 8248.80$. cis of wheat will be required to make 40 bars of four, how many bush.
    17. The capital of an inc to make 40 barrels of flour 9 Ans. 180. for one year are $\$ 58760$; rate of dividend can it declare? 18. By selling a lot of booke for $\$ 438$, bookseller Ans. $7 \frac{1}{3} \%$. much should the books have been sold for, bookseller loses $10 \%$; how
    19. What is the difference between the in to gain $12 \frac{1}{2} \%$ ?
    $\$ 540$ at $6 \%$, for 6 years 10 months? 20. I own 25 ehares of $\$ 50$ each which has declarec a sami-annual divi in the Gosford Railroad Co., I receive? $3 \frac{3}{\%}$. How much do 21. If 12 boarders eat $\$ 25$ worth of bresd in 2 Ans. $\$ 43.75$. $\$ 9.50$ per bbl. ; in how many months bread in 2 mo., when flour is of bread, when flour is $\$ 12$ per bbl.? 22. B hired a house for one year for $\$ 300$; at the Ans. $3 \frac{1}{25}$ mo. he takes in $C$ as a partuer, and at the end of 8 mone end of 4 months At the end of the year, what rent must each pay? Ans. $\mathrm{B} \$ 183 \mathrm{H} ; \mathrm{C} \$ 83 \mathbf{3}$; D $\$ 33 \mathrm{k}$. 23. A person mixed 12 cwt . of sugar at $\$ 10$, with 3 cwt . at $\$ 8$, and 8 cwt . at $\$ 7 \frac{1}{2}$; how mush was 1 owt . of the mixture worth ?
    24. A shipment of wheat was insured at $2 \% \%$ to cover of its value; the premium paid was $\$ 44.07$; the wheat being worth 80 cts. per bushel, how many bushels were shipped ? Ans. 2825 bush.
    25. A stack of hay will keep 24 cows or 18 horses one week. How many days will it keep 5 cows and 5 horses?

    Ans. $14 \frac{2}{5} \mathrm{da}$.
    26. C , of Montreal, remits to D , of Quebec, a bill of exchange on Liverpool, the avails of which he wishes to le invested in goods on his account. D, having disposed of the bill at $7 \frac{1}{2}$ \% advance, received $\$ 9675$; and, having reserved for himself $\frac{1}{4} 9^{\prime}$ on the sale of the bill, and 2 \% for commission, he invests the remainder. What is the amount invested, and for how much was the bill drawn?

    Ans. Investment, $\$ 9461.58 \frac{3}{3}$; the bill was $£ 2025$. 27. What per cent. is gained by buying oil at 80 cents a gallon, and selling it at 12 cents a pint? Anc. 20 \%.
    28. A merchant pays $\$ 10050$ for a stock of goods; he sells them at an advance of $331 \%$; the expenses connected with the business are 81750. How much does he gain?

    Ans. $\$ 1600$.
    29. What o'clock is it when the time from noon is $y^{\prime}$, of the time to midnight? Ans. 5 o'cl. 24 min . P. M.
    30. A merchant receives on commission three kinds of four ; from C he receives 20 bbl. , from D 25 bbl , and from E 40 bbl . He tinds that C's flour is $10 \%$ better than D's, and that D's is $20 \%$ better than E's. He sells the whole at $\$ 6$ per hbl. What in justice should each man receive? Ans. C receives $\$ 139 \frac{1}{21} \frac{1}{12} ; D, \$ 158 \frac{172}{2} \frac{2}{1} ; E, \$ 211 \frac{1}{2} \frac{4}{4}$.
    31. For what sum must a note be drawn at 4 mo., that the proceeds of it, when discounted at bank, at $7 \%$, shall be $\$ 875 . \therefore(1$ ?
    32. If $2 \frac{1}{3}$ yards of merino $1 \frac{2}{5}$ yards wide cost $\$ 3.37 \frac{2}{5}$. what will be the cost of $36 \frac{1}{2}$ yards $1 \frac{1}{2}$ yards wide? Ans. $\$ 52.779$.
    33. What must be the face of a note at 60 days, the proceeds of which, when discounted at Bank, at $6 \%$, are $\$ 100$ ? Ans. $\$ 101.06+$
    34. A merchant sold a piece of cloth for $\$ 24$, and thereby lost $25 \%$; what would he have gained had he sold it for $\$ 34$ ? Ans. $6 \frac{1}{4} \%$.
    35. A bankrupt compromises with his creditors for $37 \frac{1}{2} \%$; how much will he pay on a claim of $\$ 3656$ ? Ans. $\$ 1371$.
    36. A man, dying, left $\$ 3565$ to be placed at interest for his son, who was 16 yr. 5 mo .15 da . old; how much will he receive when he is 21 years old, allowing $7 \%$ interest?

    Ans. $84698.37+$.
    37. A garrison, consisting of 360 men, was provisioned for 6 months; but at the end of 5 months they dismissed so many of the meu that the remaining provision lasted 5 months longer; how many men were sent sway?

    Ans. 288.
    38. What sum must I invest in the New Brunswick $6 \%$ stock, selling at $2 \frac{1}{2} \%$ premium, to secure an annual income of $\$ 840$ ? Ans. $\$ 14350$.
    39. A grocer divided a barrel of flour into two parts, so that the smaller contained as much as the other ; how many pounds were there in each?
    40. A sportsman spends $i$ of his time in amoking, in gunning, 2 ho. per day in loafing, and 6 ho. in eating, drinking, and sleeping; how much remains for nseful purposes ? Ans. 2 ho.
    41. Exchanged 250 shares of $6 \%$ stock, est $70 \%$ for stock bearing $8 \%$, at $120 \%$; what is the difference in my income? Ama. \$333.33\%.
    42. Purchased 100 barmels herrings, at $\$ 5$ per bbl. and immediately sold them on a credit of six months. The note which I received for pay, I got discounted at the Union Bank; and, on examining my money, I found that I had gained $20 \%$ on my purchase. What did I receive per bbl. for the herrings? Ans. si6.18+.
    43. How many bricks are required to build the front of a honce 50 ft . 8 in . in length, 15 ft .8 in . in height, and 1 ft .6 in . in thickness, the dimensions of a brick being 84 and 2 inches? Ans. 32148 bricks.
    44. A woman buys apples at the rate of 5 for 2 cts ., and sells them at the rate of 4 for 3 cts . ; how many must she buy and sell to make a pront of $\$ 4.20$ ?
    45. Sent $\$ 12300$ to my agent in Toronto, Ans. 1200. flour at $\$ 10$ per bbl., atter deducting his comm which to purchase many barrels of flour did I receive? 46. Rorrowed of A $\$ 150$ tor six mens. 1200 . $\$ 100$; how long shall he keep it to conths; afterwards I lent him sum he lent me?
    17. A broker charges me $1 \frac{1}{3}$ \% for purchasing Ans. 9 mo. bills at $2.5 \%$ discount of theve or purchasing some uncurrent bank became worthless; I dispose of the remainder at par, and one of $\$ 50$ \$520. What was the amount of bills purchased ? par, and this make 48. 4 grocer mixed 5 lus. ot sugar, at $8 \frac{3}{4}$ cts. per Ib., with. $\$ 2500$. at $7 \frac{3}{4}$ cts. per lb., and 60 lha . at such a price that the mith 80 lhs., worth $9 \frac{3}{4}$ cts. per lb. Required the price per lb. of the mixtnre was sugar.
    49. A gencleman's garden is 234 rods loner and Ans. $12 \frac{1}{2}$ cts. is surrounded by a good fence 74 ft . high. Now, if $7 \frac{4}{7}$ rods wide, and walk around his garden within the ferce 75 , if he shall make a remain for coltivation? 50. A certain principal, at componnd Ans. 1 A. 3 R. 7 p. $85 \frac{1381}{6} \frac{\mathrm{ft}}{6}$. will amount to $\$ 669.113$; in what time interest for 5 years, at $6 \%$, to the same sum, at $6 \%$ simple interest ? Ans same principal amount
    51. I invested ? of my money in $\mathrm{K}_{\mathrm{o}} \mathrm{K}_{\mathrm{c}}$. 5 yr .7 mo .19 + da. $10 \frac{1}{4} \%$; the remainder I invested in reai estate, stock, which depreciated and thereby I gained $\$ 1500$. How much did, which alvanced $15 \%$, ments?
    52. What $\%$ in advance of the cost Ans. $\$ 250$. goods, so that, after allowing 5 of cost must a merchant mark his credit of 6 months, and $7 \%$ of the cost of the for bad cebts, an average he mav make a clear gain of $12 \frac{1}{2} \%$ on the first for his expenses, Ans. $29.56+\%$ g, 53. What is the greatest possibie number of hills of rye tliat can be planted on a square acre, the hills to occupy only a mathematical point, and no two hills to be nearer than $3 \frac{1}{2}$ feet? ? Ans. 4165.
    54. I wish to line the carpet of a room, $6 \frac{1}{3}$ yd. long and $5 \frac{1}{3} y d$, wide, with duct $\frac{7}{8}$ yd. wide. How many yards of lining must I purchase, if it will surinik $4 \%$ in length and $5 \%$ in width? Ans. $433_{3}^{5} y d$.
    65. A man bequeathed $\frac{1}{4}$ of his estate to his son, and $\frac{1}{5}$ of the remainder to his daughter, and the residue to his wife ; the difference between his son and daughter's portion was $\$ 100$; what did he give his wie?

    Ans. $\mathbf{5 6 0 0}$.

    ## MHOLLLANEOUS EXAMPLEg.

    66. Bight workmen; laboring 7 hours a day for 16 daye, were able to execute 1 of a job; in hov many days can they complete the residue, by working 9 hours a day, if 4 workmen be added to their number?
    67. Exchanged 50 Ontario bands $\$ 1000$ Ans. $15 \frac{5}{8}$ days. for Nova Scotia bonds of $\$ 200$ ear
    68. I lent a friend $\$ 700$, which he kept 20 months Ans. 310. after I borrowed of him $\$ 300$; how long should I keep it to yeare the favor?
    69. Bought merchandise as followe : July 3, Ans. 465.2 months. on 30 da. ; Aug. $17, \$ 6.48$; Sept. 12, $\$ 50$. What is due on the account Oct. 12, interest at $9 \%$ ?

    Ans. $\$ 142.60$.
    60. Lent a certain sum of money to $A$, and at the end or 3 yr. 7 mo. 20 da., I received for interest and principal $\$ 1000$; what sum did I lend?
    61. If 12 oz. of wool make 27 yd. of cloth, $1 t$ wide, how many pounde of wool are required to make 115 yd . of cloth 1 yd . wide? Ans. 24.
    62. Bought goods for $\$ 1500$, $\frac{1}{2}$ payable in 3 months, $\frac{1}{1}$ in 6 months, and the remainder in 9 monthe. How much ready cash ought I to pay for the gonde, money being worth $6 \%$ ? Ans. $\$ 1456.52$-.
    63. Purchased a quantity of oats, April 1.; May 1 its value had nereased 25 \%; June 1 its value was $30 \%$ more than May 1 ; July 1 I sold it for $i 5 \%$ less than its value June 1 , receiving in payment a 6 months' tote, which I got discounted at a bank, at 7 \%, receiving $\$ 12950$ on it. How much was my profit on the oats? Ans. $\$ 3238.52$.
    64. If 24.4 cubic inches of lead weigh 16 lb ., required the umber of feet of lead pipe that can be made from 80 lb . of lead, the caliber of the pipe $n o$ be 1 inch, and the thicknese of it $\frac{f}{f}$ on inch.

    Sive. $10.35+$ feet.
    65. Une-third of a quantity of goods was sold to gain a certaiu \%, -one-fourth to gain $1 \frac{1}{2}$ times as much of, and the remainder to gain $2 \frac{1}{2}$ times as muob \%. What is the gain $\%$ on each part, the gain upon the whole being $21 \%$ ? Ans. 1st., $12 \%$; 2nd., $18 \%$; 3rd., $30 \%$.
    66. A merchant in Kingston has 5000 franos due him on account in Paris. He can draw on Paris for this amount, and negotiate the bill at 192 cts. per franc ; or he can advise his correspondent in Paris to remit a draft on Canada, purchased with the sum due him, exchange on Canada being at the rate of 5 fr . 20 centimes per dollar. What sumu will the merehant receive oy each method? Ans. By draft on Paris, $\$ 970$; yy remittance from Paris, $\$ 961.5$.
    67. A mil is required to grind 160 bushels of provender; worth $\$ 1$ a bushel, from oats worth $\$ .40$, corn worth $\$ .80$, barley tic \$.90, and rye worth $\$ 1.10$. and wheat worth $\$ 1.30$ per bushei. nuw many buehols of each inind may he take?

    Ans. 20. 20, 20, 60, and 40, respectively. 68. How mneh coftee at $5.37 \frac{1}{\mathrm{~g}}$ a tio., must be given for 12 gal . 3 qt. of sirup, at $\$ .75$ a gallon ?
    69. A servant drawa off a gallon on each day, for Aass. 25 . $\mathbf{1 b}$. cask containing 10 gallons of wine, each time supplying the deficiency by the addition of a gallon of mator; and then, to esoape deteotion, bo of wine. Ho's much water still remains in the cask ?

    Ans. 1.0679577 gal., or more than a gallon and half a pint.
    70. A merchant has $\$ 216$ due him, to be paid in 7 months; but the debtor agrees to pay onehalf ready money, and $\frac{3}{4}$ of the remainder in 6 months. What time should be be allowed for paying
    71. A house that cont ع3931 50 , Ans. 3 yr. 2 mo. surance is $4 \%$, and the repairs 180 , rents for $£ 369109$; the indoes it pay? ne. owe a man the following notes: one of $\$ 500$ Ans. 8 \%. helder $\$ 50$, due July 15 ; and one of $\$ 1750$, due Sept Aprif 1 ; mant wishes to exohange them for two notes of $\$ 1500$. 10 . The wants one to fall due May 10; when should the of $\$ 1500$ each, and able?
    73. A trader bought merchandioe as follows: Ans. Cct. 20. May 23, $\$ 55.64$, on 30 da. ; $\bar{F}$ ne $2, \$ 82.60$, on: Ap 1 l , $\$ 150.22$; $\$ 90$. What was due on the account Sept. 262 mo., and July 14, $7 \%$ ? 74. By woriking 9 bours a day, for 154 daye 12 Ans. \$386.e7. oxecnte of a job, how many men may days, 12 men were able to idue be finished in 15 daye more, if the be withdrawn, and the res. 7 hours a day?
    75. At a certain time between 2 and 3 o'clock Ans. 4 men. was between 3 and 4. Within an hour atcock, the minutehand minute-hand had exactly changed places wither, the hour-hand and the precise time when the handsed places with each other. What was
    76. D and E traded together; D Ans. $2 \mathrm{hr} .15 \mathrm{~min} .56 \mathrm{H}^{9} \mathrm{fis} \mathrm{sec}$. received $\frac{1}{3}$ of the gain; the number ot in $£ 100$ for 512 days, and equal to the number of days it was employed in which E put in was oapital ?
    77. If stock bought at $8 \%$ discount will pay $7 \%$ Ans. $5 \% 20$. at what rate should it be bought to pay $10 \%$ ? 7 on the investment, 78. An importer sold cloth to a wholesale Ans. $35.6 \%$ lisct. the wholeaale dealer sold it to a clothier ate dealer at $10 \%$ advance; ier cold it at a farther advance of 25 s at $12 \frac{1}{2} \%$ advance; the clothmuch did it cost the importer? of 25 , and received $\$ 145 \%$. How 79. What is the difference between the incerest Ans. $\$ 93663$. $\$ 730$, for 5 yr .9 mo ., at $8 \%$ ? 80. A merohant sold 1 of his goods at an advance Ans. $\$ 105.80$. them at a loss of $8 \%$; $\frac{1}{20}$ of them at a profit of $30 \%$ of $25 \%$; yo of at a disoount of $20 \%$. For what $\%$ of the coest $30 \%$, and $\frac{1}{5}$ of them cold in order to lose $5 \%$ on the whole? 81. I received an $8 \%$ dividend un Montreal city rail Ans. $68 \frac{1}{4} \%$. invested the moneg in the same stuck at $80 \%$ city railroad stock, and creased to $\$ 13750$, what was the amount of $\$$. My stock having in82. A tailor bought 40 yards of broadeloth dividend ? A. $\$ 1000$. sponging it, it shrunk in length upon every 41 yd . wide ; tut on in width, one nail and a half upon every 4 yd. half a quarter., and he bought flannel 6 quarters wide, which ld yd. To line this cloth,
    width on every 20 yards in longth, and in width it shrunk hatf a nail. Required the number of yards of flannel used in lining the sloth.
    83. Stock purchased at $5 \%$ premium pays $6 \%$ on the invesiment, what \% will it pay if purchased at $15 \%$ discount? Ans. $7 \mathrm{I}^{7} \%$.
    84. A merchant failing in business can pay 76 cts. on a dollar. He offers, to pay his whole indebtedness without intereest in 5 years if his creditors will allow him to go on with his basiluess; his ofter being sesepted, how much will his creditors lose in the 5 years, money being worth $7 \%$ ?

    Ans. 尔 026 on a ciollar.
    85. Purchased $\varepsilon$ quantity of wine for $\$ 675.32 \frac{1}{6}$, at. 85 cents por gallion; but a part having leaked out, the remainder with sold st 40 sadvance, sund the oniginal cost was realized. What quantitg leaked out?
    86. A owes B $B 0$.nve in 4 moaths, and $\$ 840$ due in 6 months; B owes A $\$ 1600$ duc is. $\}$ mouth . If $A$ should make present paymen: of his debte, whenct, nu, B in justice to pay A? Ans. In 2 nn . $10 \frac{1}{2}$ da.
    87. How many Y, in ds of sugar at 8,13 , and 14 cts. per pound. may be mixed with 3 lb . at 9 f cts., 2 lb . at 8 l cts., and 4 lb . at 14 cts. a lb., so io gain 16 \% by selling the mixture at $\$ 4 \frac{1}{2}$ cts. per 1b.? Ans. 1 llb . at $8 ; 8 \mathrm{jlb}$. at $13 ; 81 \mathrm{lb}$. at 14 .
    88. What 18 the differcnce between the true and bank discount of $\$ 3000$, payable in 120 days, at $8 \frac{1}{2} \%$ ? Ans. $\$ 4.467$-.
    89. A general, forming his army into a square, had 284 men remaining; but increasing each side by one man, he wanted 25 men to complete the sqnare. How many men had he?

    Ans. 24000.
    90. C bought a house of D, and gave him lis boad for $\$ 6000$, dated April 1, 1866, payable in 5 equal annual installments of $\$ 1200$, the tirst to be paid April 1, 1867; C took up his bond April 1, 1869, seni-annual discount at the rate of $7 \%$ per annum on the payments due after April I, 1869, being deducted. What sum cancelled thי bond?

    Ans. $\$ 3365.94+$.
    91. I have a plauk $42 \frac{1}{4}$ feet in length, 24 inches wide, and 3 inches thick; required the side of a cubical box that can be made from it?
    92. If B owes $\$ 500$ due in 6 months, $\$ 400$ due in 4 months, and $\$ 300$ due in ? months, and pays $\frac{3}{3}$ of the whole in 3 months, when ought the remainder to be pail?

    Ans. In $10 \frac{3}{4}$ mo.
    93. A wholevale merchant sent a quantity of goods into the country to be sold at auction, on a commission of $4 \frac{1}{2} \%$. What amount of goods must be coll, that his agent may buy produce with the avails to the amount of $\$ 1910$, after retaining a commission of $2 \%$ ?

    $$
    \text { Ans. } 0 .
    $$

    94. If the annual rent of 23 A .1 R. 27 per. of land be $\$ 18 \%$ how much will be the rent of 71 A. 20 per. ? An $\% 69$.
    95. A Halifax merche hipped 1000 barrels of sait, hn as agent in New Orieans, directin, is moll it, and invest tin griseds in cotton; his agent sold the salmon at $\$ 14$ per bul., paiu, 74 charges, and bought cotton at $\$ .65$ per 1 l ., charging $3 \%$ commis 4 ve selling the ealnom and $5 \%$ for buying the cotton. How ma yo prids of sotton did he buy?

    Ans. 19495..: +ib.
    98. A man owes a debt to be paid in 4 equal installments at 4,9 , 12, and 20 months, respectively; discount being allowed at $5 \%$, he finds that $\$ 750$ ready money will pay the debt; how much did he owe?
    97. D's money was to E's as 2 to 3 ; Ans. $\$ 784.74+$. E had spent $40 \%$ mon $D$ had spent $\$ 40$, and money, plus $\$ 2$, ss 4 to 9 an D, D's money, minus $\$ 20$, was to E's 98. What is the cost of a 90 days' bill Ans. D, \$108; E, \$162. of $\$ 1000$, at $\%$ premium, and int $\%$ 99. Three men engaged in the orr at 6 ? ? Ans. \$990.75. and $\mathrm{B} \$ 6000$; they gained $\$ 1680$, of which C's ; A fure was $\$ 840$. quired $C$ 's stock and $A$ 's and $\mathrm{B}^{\prime}$ 's gain.

    Ans. C's stock, $\$ 10000$; A's gain, $\$ 336$; B's $\$ 504$.
    100. A man having lost $\frac{5}{8}$ of his money, found he had remaining only $\$ 672$; how much had he at first?
    101. A speculator invested at first? Ans. $\$ 1792$. selling these stocks at osed a certain amount in railroad stocks, by by investing the remainder he cated price he lost 爰 of his investment; money he had remaining, which leared $\$ 240$, and atterward lost $\frac{\%}{\%}$ of the much did he invest?
    102. Bought a certain number of horses for $\$ 2600$ Ans. $\$ 3600$. 8 more at $\$ 10$ less each, all would have coss for $\$ 2600$; had I bought did I bay?
    103. Louis can do a piece of Ans. 20. in how many days can both do it? 8 days, and John in 12 days; 104. A grocer bought 11 bushels of chestputs Ans. $4 \frac{4}{5}$ days. retailed them at 3 cents a half pint. Whatnuts at $\$ 3$ a bushel, and gain? 105. The head of a flsh is 12 inches Ans. $28 \%$. head $+\frac{1}{2}$ of the body, and the body is as long, the tail is as long as the together; what is the length of the fish? 106. A consignor sends ju0 barrels of flour to Ans. 96 inches. chant, with instructions to sell it and remit the net prommission merThe consignee pays $\$ 120.40$ for freight ant expenses, sells th by draft. $\$ 8.40$ per bbl., charges $2 \frac{1}{2} \%$ commission, and pays 3 sells the flour at draft ; how much does the consignor receive pays $\frac{3}{8}$ \% premium for 107. How many he consignor receive? Ans. $\$ 3959.75$. every 3 horses there is of the 25 be kept on 25 acres of land, if for every 2 horses, 1 acre of pasture? 108. Purchased 240 buabels Ans. 30 horses. $\$ 22.50$, and sold it at the rate of 221 at the rate of 18 bushels for gain on the whole? 109. I paid £93 150 , at the rate of $2 \frac{1}{2} \%$, for insurance $\begin{gathered}\text { Ans. } \$ 60 \text {. }\end{gathered}$ factory ; for what amount was the policy given? 110. Exchanged 75 railroad bonds of $\$ 500$ ? for bank stock at $5 \%$ premium, how many each, at 36 \% below par, I receive?
    111. Invested $£ 858$ in Government bonds at 100 Ans. 228志. brokerage, and afterward sold the stock at 12 at $106 \%$, paying $1 \frac{1}{4} \%$ 1\% What was my gain ? the stock at $12 \%$ preinium, brokerage Ane. £26.
    112. The longitude of Paris is $2^{\circ} 20^{\prime} 22^{\prime \prime}$ E., and of Constantinople, $8^{\circ} 59^{\prime} \mathrm{E}$. When it is I A. M. at the latter place, what time is it at the former? Ans. $33 \mathrm{~min} .25 \frac{7}{16} \mathrm{sec}$. past midnight.
    113. Having placed a bill of $\$ 775$ in the hands of a collector, who succeeded in obtaining $75 \%$ of it, and charged $8 \%$ commission, how much did I receive?
    114. Suppose that the earnings of the Grand Trunk R. R. for December 1870 were $\$ 472240$, which was an increase of $11 \frac{1}{8} \%$ over lie earnings for the same month in 1869. How much was the increase ?
    115. In a cask containing brandy and water, $\frac{?}{5}$ of the whole +3 gal. is brandy, and $\frac{1}{4}$ of the whole +2 gal. is water; required the number of gal. of each.

    Ans. 43 gal. brandy, 17 gal. water.
    116. Hamel, Perry, Lane, and Garneau are partners; Hamel takes \& of the gains or losses; Perry $\frac{1}{4}$, lane $\frac{1}{5}$, and (farneau the remainder. At the close of the year, the resources of the firm are : Casli $\$ 10312.50$, Merchandise $\$ 13447.50$; Bonds and Mortgages $\$ 11470$, Bank Stuck \$.4500; Hamel has drawn from the husiness $\$ 900$, Perry $\$ 525$, and Lane $\$ 280^{\circ}$; the liabilities are : Notes outstanding $\$ 5460$; Balance in favor of Ross \& Co., $\$ 1120$; Balance in favor of J. L. Murphy, $\$ 3967.50$; Hamel invested $\$ 9547.50$, Perry $\$ 7905$, Lane $\$ 6270$, and Garneau $\$ 3480$. What is each partner's interest in the business at the close of the year? Ans. Hamel, $\$ 9877.50$; Perry, $\$ 8302.50$; Lane, $\$ 6723$; Garneau, \$4279.50.
    117. What is the difference in cost between a draft on Toronto of $\$ 17302.80$, at $1 \frac{1}{4} \%$ premium, and one on St. John, N. B., for the same amount, at $\frac{1}{2} \%$ discount?

    Ans. $\$ 302.80$.
    118. A mechanic received $\$ 3.75$ a day for his labor, and paid $\$ 1.25$ a day for his board; at the expiration of 100 days behar ved $\$ 200$; how many days did he work ? Ans. $86 \frac{4}{3}$ dajs.
    119. For two successive years, a merchant annually contribated $\$ 100$ for charitable purposes, and added yearly to that part of his capital not thus expended, a simm equal to its half; at the end of the second year his capital was dqubled. Required his capital. Ans. $\$ 1500$.
    :20. A merchant in Halifax purchased 350 bales of cotton, each cuntaining 450 pounds, at $\$ .80 \mathrm{a} \mathrm{lb}$., and shipped them to Liverpool at a cost of $16 \%$ for freight and duties. How much in Canada currency did he gain by selling them at 2 s .10 d . sterling per lb., rate of exchange $171 \%$ ?

    Ans. $\$ 23415$.
    121. A piece of merino cust $\$ .80$ per yard; at what price shall it be marked, that the merchant may sell it at $10 \%$ less than the marked price, and still make $20 \%$ profit?

    Ans. $\$ 1.06 \frac{1}{8}$.
    122. A merchant in Quebec gave $\$ 2000$ for a bill of exchange of $\boldsymbol{£} 400$ to remit to London; what was the rate in favor of England?
    123. What yearly debt can be discharged by monthly payments, the first being $\$ 2$, the second $\$ 6$, and the third $\$ 18$, and so on, in geometrical progression?

    Ans. \$531440.
    124. A farmer sold one hog, weighing 250 lb. at 4 cts. per lb. ; a eecond, weighing 300 lb ., at $4 \frac{1}{2} \mathrm{cts}$. and a third, weighing 369 lb ., at cts. ; what was the average price per lb . for the whole ? A. $4 \frac{91}{\frac{1}{4}} \mathrm{cts}$.
    125. John's age is 4 times Mary's, but in 12 years John'月 age will be only $2 \frac{3}{2}$ times Mary's; required the age of each.

    Ans. Mary's age is 12 yr . ; John's is 48.
    126. A company of 50 men drank wine at 2 s . 6 d . per bottle, to the amount of $£ 10$. How many mell at the same rate will $£ 18$ worth of wine supply, when wine is worth 2 s . 3d. per bottle? Ans. 100 men.
    127. The sales of a clothing house amount to $\$ 100000$ a year; $\frac{1}{4}$ of the sales are made at a profit of $25 \%, \frac{9}{2 \%}$ at a profit of $20 \%$, and the remainder at a loss of $4 \%$. Required the cost of the goods.
    128. A merchant in Toronto purchased a Ans. $\$ 88750$. $\$ 2660$, drawn at 60 days, paying $\$ 257089$ a draft on Quebec for exchange?
    129. A man gave $\frac{1}{2}$ of his estate to his wife, Ans. $2 \frac{1}{2}$ ' disct. his oldest son, $\frac{1}{2}$ of the residue to his wife, $f$ of the remainder to what then remained, which was $\$ 1500$, was to daughter, and $\frac{1}{2}$ of among his other children, who received $\$ 150$ each equally distributed ber of his children, and the value of his estate
    130. A merchant by selling Ans. 12 children; $\$ 10000$. how much should the goods have been sold for to gain loses $10 \%$;
    131. An agent received $\$ 65$ for been sold for, to gain $123 \%$ ?
    was the rate of his commission?
    132. A merchant mariked a its season parche cost, but price, supposing he shetermined to sell it $20 \%$ below the marked
    133. A mang he should make $5 \%$. Did he make or lose? able in 2 years. If he accept the last $\$ 4000$ cash, or for $\$ 5000$, paypresent worth, at $10 \%$ discount ; how much received instead its than by the former? 134. A laborer worked 3 months, 25 daps each Ans. $\$ 166.66 \frac{2}{8}$. each day, for $\$ .08$ an hour, and received in each month, 10 hours each containing 15 bago of the grain per bushel? $\quad \frac{1}{2}$ bushels each. What was the price of
    135. Sold goods to the amount $\$ 348.25$, taking in Ans. $\$ 0.80$. 6, a promissory note for sixty days, which taking in payment, April counted at the bank, April 20 , at $7 \%$; how indorsed and had disceive?
    136. Suppose bank stock is purchased at 28 Ans. $\$ 344.93+$. bank declares a dividend of $9 \%$ per ashare and the price of the stock?
    137. A person, wishing to buy wheat with the Ans. $7 \frac{1}{32} \%$. sends to his agent 32 bales, each weat with the proceeds of cotton, the cotton at 26 cts . per lh ., for whighing 380 lb . The agent sells pays for freight and cheres which he charges $2 \frac{1}{4} \%$ commission; less his commissions fore $\$ 34.60$; and expende the remainder, bushel, for which he charges 13 and buying, in wheat at 85 cts . per obtained through this factor? $1 \frac{1}{2} \%$ commission; how much wheat is 138. A pole 63 feet long, in falling, was brit Ans. $3542+$ bu. the shorter piece being $\frac{2}{5}$ of the longer; what is into two pieces; piece?

    Ane. 18 and 45 ft .
    139. A farmer had a dairy of 43 cows, each furnishing 18 qt . of milk a day, from which liee nia. 040 tubs of butter of 60 lb . each in 30 days. He made a contract to deliver 100 tubs of 96 pounds each in 80 days. How many cown must he add to his dairy provided each additional cow firrnish 4 gallons of milk daily ?

    Ans. 27.
    140. In what time will $\$ 3045.20$ gain $\$ 190.32 \frac{1}{2}$ if the gain of 82494.75 for 1 yr .13 da., is $\$ 258.43$, and what io the rate per annum? Ane. 7 inc. 1 is cis. ; rate $10 \%$.
    141. Andrewr, Baker, and Childs entered into partnership. Andrewa put in $£ 3000$, liaker $£ 2000$, and Childs $£ 1750$. At the end of the Srst year Anilrews drew out £500, Baker £250, and Childs put in £750. At the close of the second year, Andrews and Baker each drew out .2250 , and Childs put in $£ 500$ more. At the end of the third year they dissolved partnership, and found that their joint property was $£ 7125$. What was each partner's share? Ans. Andrews', £2393 1044 ; Baker's, £1597 451 ; Childs', £3134 $52 \frac{2}{9}$.
    142. If I buy 50 shares Grand Trunk railroal stock at $141 \%$, and 50 shares Canada Central railroad stock at 139 \%, the former paying semi-annual dividend of $4 \frac{2}{10} \%$, the latter of $5 \%$; what rate of interest shall I realize on my investment?

    Ans. $6 \frac{1}{2} \%$.
    143. What is the cost of a bill on London for $£ 800176$ sterling, when the rate of exchange is $97 \%$ premium?
    144. J. Sheridan bought of L. H. Miles \& Co., the following bills of goods; Nov. 1, 1870 , bill of $\$ 750$, on 6 mo. credit; Dec. 15 , 1870, a bill of $\$ 300$, on 5 mo. ; Jan. 1, 1871 , a bill of $\$ 425$, on 4 mo .; Feb. 5, 1871, a bill of $\$ 275$, on 2 mo. What sum would settle the account, May 29, 1871, interest at 7 \% ?

    Ans. $\$ 1760.10$.
    145. When exchange on England is at $10 \%$ premiunı, and freight at ls. 3d. sterling per Winchester buskel, how much can be paid in Montreal for wheat per bushel, in answering an order from London limited to £3 10 per Imperial quarter?
    146. The duty on an invoice of $300 \mathrm{doz} n$ London porter, at $30 \%$, was $\$ 190.512$; breakag ${ }^{2}$, $2 \%$. Required the invoiced price per dozen. Ans. $\$ 2.16$.
    147. Three merchante have an interest in a steam vessel; A puts in $\$ 960$ for 6 months; $B$, a sum unknown, for 12 montla; $C, \$ 640$ for a time not known when the accounts were settled; A received $\$ 1200$ for his share, stock and profit; B, $\$ 2400$ for his, and C, 61040 for his. What was B's stock, and C's time?

    $$
    \text { Ans. B's stnc'z, } \$ 1000 \text {; C's time, } 15 \text { mo. }
    $$

    148. Merrill, Wells and Roche we:: irtn s in the giain bininess; Merrill had invested $\frac{1}{3}$, Wells $\frac{1}{5}$, and $\frac{3}{}$ ane of the capital. They were to share equally the gains or $h_{1}$ es. the business not being successful, the partuership was dissolved at the close of the vear, when the resources of the firm were found to be: Cash, $\$ 1780$; bar. iey on hand, 82500 ; corn, $\$ 1752$; rye, $\$ 350$; oats, $\$ 1650$; wheat \$5000. The liabilities were: Notes outstanding; $\$ 1562$; they owed \& Myler, $\$ 1200$, and P. Riley, $\$ 1875$. The net losses were $\$ 750$. What was the net capital of the firm at commencing, and what was each partner's net capital?

    18 qt. of lb. each in ounds each vided each Ans. 27. e gain of ate per anate $10 \%$. . Andrewn end of the ilds put in 3aker each end of the joint prop.ndrews', 23. $141 \%$, and uner paying rate of inne. $6 \frac{1}{2} \%$. 6 sterling, wing bills t; Dec. 15, , on 4 mo.; settle the 1760.10 . and freight be paid in m London
    r, at 30 \%, price per s. $\$ 2.16$.
    el; A puts ; C, 640 A received d C, 61040
    e, 15 mo.
    n blu ital. They not being f the vear, 178: ; bar. 50; wheat. they owed were $\$ 750$. d what whe

    ## ACCOUNTS OF STORAGE.

    491. Storage is the price charged for the sufe keeping of goods in a store or warehouse.
    There is no unifirm method of computing storage. The Chambers of Commerce of the different cities, adopt such rules and rates for storage as they deem equitable. The ch:rges for storage are usually, however, a certain rate per month for each box, bale, cask, etc.
    Norrs.-1. When goodes are withdrawu defore the olose of the month, no deduction is made, but storsge is charged for the $f$ " month. After the first month, ofties, all fractional parts of a one half, charg is made for a month. In some
    492. If, however, parts of a month ure considered full months. business, or aro received and delivered at sold on aocount, as in the eommission is k pt, showing the date and number of the place of the consignor, an aecount number sold or delivered. In compating the storage on such the diate and customary to average the time, and chargo tho storage on such an account it is If there is a fractional part of a barrel, eto., in the averate per month of 30 days. oase of parts of months above.
    E.c: What will be the cost for the storage of flour at 6 cents per barre.', which was received and delivered as follows: Received May 1 , 1871, 1000 barrels; May 26, 2000 barrels. Delivered May 16, 506 barrels; June I, 1000 barrels; June 12, 1100 bll. ; July 2,' 400 tibl.

    OPMRATION.

    $$
    1871 .
    $$

    May

    $$
    \text { " } 2
    $$

    "ay 1 , Rec. $100 \times 15=15000$
    16, Deliv. $\frac{500}{500}$
    Bal. $\overline{500} \times 10-5000$
    Rec. 2000
    Bai. $\overline{2500} \times 5=12500$
    June 1, Deliv. 1000
    Bal. $1500 \times 11=16500$ " 12, Deliv. 1100

    $$
    \text { Bal. } \quad 400 \times 20=8000
    $$

    July 2, Deliv. $400 \quad 310) \frac{570010}{}$ Chargeable for 1 month, $\frac{1900}{190}$ $1900 \mathrm{bbl} \times .06=\$ 114$, cost of storage. 492. Rule.-Commencing with the first date and ending with the last, multiply the number of bapye??, or other crticles in sioure, from each dute to the one NEXT following it, ly the number of days between these dates. Divide the sum of the several products ly 30, and the quotient will be the number of articles stored for one month, and this number multiplied ly the rate of storage for each article will give the amount of storuge charged.

    ## EXAMPIFA FOR PRACTICR.

    1. What will be the coat of storing salt at 2 cte. per barrel, recesved and delivered as follows: J ine 6, 1871, 120 bhl.; June 16, 140 bhl ; June 26, $600 \mathrm{bbl} . ;$ July .5, 300 bbl ; July $15,180 \mathrm{bbl}$; July 20, 160 b, Al. All delivered Agg. 1. Ans. $\$ 21.44$.
    2. What will be the storage of flour at 5 cents per bbl. per month, received and delivered as followa?

    Received July 1, 1871,400 bhl. ; July 15, 350 bbl. ; July 26, 450 bbl. Delivereil, July 12, 200 bbl.; July 20, 400 bbl.; Aug. I, 200 bbl. ; and Aug. 8,403 bbl.

    Ans. \$25.10.
    3. Received, and delivered, on account of James O'Neil, eandry bales of cotton, as follows: Received, May 1, 1871, 1848 bales; May 16, 96 bales; June 1, 240 tales. Delivered, June 12, 800 bales; July 1, 480 hales: Aug. 3. 320 hales; Aug. 10, 250 hales. Required the number of bales remaining in store on September 1, and the cost of storage up to that date, ut the rate of 5 cents a bale per month.

    Ans. In store, 334 ; cost, $\$ 240.75$.
    4. Receivel, July 3, 1871, 256 casks of wine, on storage, and on July 15, 381 more were added; July 15 , delivered 261, and July 26, 312 casks; July 30 , received 321 cavks, and Aug. 8, 163 casks; delivered, Aug. 16, 208 casks, Ang. 18, 103 casks, and Aug. 19, 115 casks; received, Sept. 1, 320 casks, Sept. 2, 106 casks, Sept. 7, 342 casks ; delivered, Sept. 12, 250 casks, Sept. 18,321 casks, Sept. 21, 133 casks, and the balance, Sept. 27. What was the cost fur the stor. age of the above, the charge being 6 cents per cask monthly?

    ## GENERAL AVERAGE.

    483. General Average is the process of computing the loss to be sustained by the owners of the ship, eargo, and freight, respectively, - when, owing to common peril at sea, any portion of the property has been danaged or destroyed for the common safety.
    484. Jetson is the portion of the cargo or of the equipment of the vessel thrown overboard.
    485. The Contributory Interests are the thrce kinds of property which are taxed to cover the loss. These are, 1st. the vessel, at its value before the loss; 2nd. the cargo, inoluding the part eacrificed; 3rd. the freight, less $\frac{1}{8}$ as an allowance for seamen's wages.
    486. The loss which is subject to general average includes, 1st. Etinon ; 2nd. Repairs to the vessel; 3rd. Expense of dotention to which the vessel is subject in port.

    Ncies.-1. The goods, whether saved, injured, or destroyed, are eatimaled at thoir value at the port of destination, except whed the adjustment of the generw sverage is mi. at the poot of leding.
    2. Only : of the cost of repairs to the versel is allowed, as it in assumed that the new work and material are worth $\frac{f}{}$ more than the nd.

    Ex. The ship "Armeila", on a voyage from Calcutta to Quebec with a cargo of silk, teas, etc., valued at S.i9215, sprnnin a leak in a gale, and the captain was compelled to throw overboard a portion of her cargo valued at sibi35 to save the vessel and the remainier of the cargo. The vessel was valued at $\$ 7.000$; the freight was $\$ 9600$ : and of the value of the cargo \$1750, belonged to P. N. Garnean, $\$ 11600$ to J. lienson \& Co., sy500 to Ross \& T:mms, and the remain. ing \$21555 to Murphy \& Field. Of the carro thrown overboard $\$ 2150$ belonged to P. N. Gurnean, slisio to j. Benson \& Co., \$s,05 to lioss and Timms, and $\$ 1770$ to Murphy and Field. The necessary repairs of the vessel were male at Goon Hope, costing $\$ 750$; and the expenses of the detention at that port were si55.75. How should the loss be distributed among the owners of the several contributory interents?

    OPERATION.

    LOSSES.
     $\$ 7030.75 \div \$ 140615=.05$, rate per cent. of loss.
    $\$ 75000 \times .05=\$ 3750.00$, amulint payable by vessel
    $59215 \times .05=2960.75, \quad$ "،
    
    Total contribution $\$ 7030.75$, to be distributed as fillows:
    $\$ 75000 \times .05=\$ 3750.00$, amount payable ly vencel.
    $6400 \times .05=320.10, \quad 66$ 6

    | $6400 \times .05=$ | 220.100 |  |  |  | sel. |
    | :---: | :---: | :---: | :---: | :---: | :---: |
    | $17560 \times .05=$ | 875.00 | 6 | " |  | felegh |
    | $11600 \times .05=$ | 580.00 , | 6 | 16 | ${ }^{6}$ | P. N. |
    | $8500 \times .05=$ | 425.00, | \% | /6 |  | J. Bens |
    | $21555 \times .05$ | 1077.75, | " | " 6 |  | $R_{u-s} \&$ |

    From the amount payable by the vesal Mhrphy \& lield. $\$ 155.75=\$ 655.75$, the cost of teessel must be dedncted $8500+$ detention. Hence, the net amount inaire, less $\frac{1}{8}$, and the expenses of the general loss is $\$ 3750$ - some that the vessel must contribute to other ownere of contributory inter $==\mathbf{8 3 0 9 4} .25$. So each of the from the amount of his payment \$3750 - ©c55.75 SuOn Hence,
    

    From the analysie of thic exampic we deduce the
    497. Rule.-1. Divide the entire loss by the sum of the contributory interests; the quotient will be the loss per cent.
    II. Multiply each contributory interest by the loss per cent.; the product will be :he amount of its contribution to the general loss.
    III. The difference between the loss of each contributory interest and the amount of its contribution will be the balunce to be paid. by it if its contribution exceeds its loss, and the amount to be roceived by it if its loss cxceeds its contribution.

    ## EXAMPLES FOR PRAOTICR.

    1. The ship Nestor, in her passage from Antwerp to Quebec, was crippled in a storm, in consequence of which the captáin had $\$ 4800$ worth of the cargo thrown overboard, and put into port for the necessary repairs, which cost $\$ 1260$. The charges for board of seamen, pilotage, and dockage, amounted to $\$ 170.46$. The contribntory interects were : vessel, $\$ 37800$; gross amount of freight $\$ 4992$; cargo shipped by S. Keller \& Co., $\$ 2574$; by Shiller \& Morse, $\$ 1752$; by Krauss \& Herr, $\$ 1152$; hy Lebrun \& Co., $\$ 804$; and by Ross \& Daller, $\$ 1200$. In adjusting the general average in Quebec, the deduction made from the gross amount of freight on account of seamen's wages was one third. Required the several elares of the general loss.
    2. A vessel valued at $\$ 35000$, having been disabled in a storm, entered port, and was refitted at an expense of $\$ 337.50$ for repairs, and $\$ 150$ for board of seamen, pilotage, and dockage. Of the cargo, var lued at $\$ 6250, \$ 3000$ belonged to $\mathrm{A} . \$ 2312.50$ to B , and $\$ 937.50$ to C ; and the amount sacrificed for the ship's safety was $\$ 1750$ of A's property, and $\$ 212.50$ of $B^{\prime}$; the gross charges for freight were $\$ 1878$ Required the balance, payable or receivable, by each of the parties, the loss being apportioned by general average.
    

    ## AVERAGINA OF ACCOUNTS.

    498. Averaging of Accounts (also oalled "Equation of Accounts," and "Compound Equation of Payments") is the process of finding the equated time for the payment of the balance of an accourt that contains both debits and credits.

    The dobit and credit sides of an account being respectively equivalent to the sum of their several items, due at the equated time, the first step in equating accounts is to find the time when each side of the account becomes due.

    This may be found by equating each side of the account, without any raference to the other, commencing either at the first or the last date of each, or by using the first or last date of the ac count as a common starling-point for both siden.

    The solution of the following example will sufficiently illustrate these two methods of equating the debit and credit sides of an account.

    In the following solution we have commenced at the first date and discounted.

    Dr. R. Seeley \& Co. in account with L. N. Thompson. $\dot{C r}$.
    

    Debits. FIRST METHOF.

    2uebec, was had \$4800 $r$ the necesof seamen, butory inte992; cargo \$1752; by by hoss \& bec, the deof seamen's eneral loss. atorm, enepairs, and cargo, va 37.50 to C ; of A's prowere $\$ 187$ the parties, able by $\underset{\text { a }}{\mathbf{A}}$; is the probalance of espectively he equated time when
    ount, withthe first or $\theta$ of the ac

    Due, 1871
    July $3, \$ 220 \times 00=$
    Oct. $1,125 \times 90=11250$
    Nov. 15, $200 \times 135=27000$
    1872
    Feb. $24, \quad 140 \times 236=33040$ April 1, $190 \times 272=51680$ \$87: )

    141 da.
    Debits are due 141 days from July 3, which is Nov. 21.

    Credits.
    

    Credits are due 101 days trom July 1, which is Oet. 10.

    The above account thus equated will stand as follows:

    Dr.
    Due, Nov. 21, 1871, $\$ 375$.
    Or thus:
    Debits.
    Due, 1871
    July 3, $\$ 220$ 入 $2=440$
    Oct. 1, $125 \times 92 \equiv 11500$
    Nov. 15, $200 \times 137=27400$
    1872
    Feb. 24, $140 \times 238=33320$
    April 1, $100 \times 274=52060$
    

    Debits due 143 days from July 1, which is Nov. 21.

    Cr.
    Due, Oct. 10, 1871, \$650.
    Credits. 1871

    Due,
    July $1, \$ 200 \times 00=$
    $\begin{array}{ll}\text { Oft. } & 3,150 \times 94=14100 \\ \text { Dec. } 20, & 300 \times 172=11600\end{array}$
    Dec. $20,300 \times 172=51600$
    \&650
    ) 65700
    101 da.

    Credits due 101 days trom July 1, which is Oct. 10 .

    The account thus eqiated stands as before:

    Dr.
    Due, Nov. 21, \$875.

    Cr.
    Dine, Oct. 10, $\$ 650$.

    Note. - In the above operation, we start from the earliest date upon which any item of either side of the aooount becomes due.

    The next step is to find when the balance of the acculunt, as thne equated, becomes due.

    > Debits,
    $\$ 875$
    Credits, 650

    $$
    (650 \times 42) \div 225=121 \text { days }
    $$

    Balance, $\$ 225$
    Difference in time 42 days.
    Or thus, by Discount :
    $\$ 6.50$
    
    $\$ 4.55 \div .0375$ (dis. of $\$ 225$ for 1 da.) $=121$ days.

    The balance is due I21 days from Nov. 21, 1871, which is March 22, 1872.
    misplanation.-Assume the account settled Nov. 21, the latest date. The oredit side of the account has been due from Oct. 10 to Nov. 21, or 44 days. Nov. 21, the credit side, is equal to $\$ 650$, and the interest of the same 42 days. That the debit side of the account may be increasod by an equal amount of interest, it is evident that the balanoe of the account must remain unpaid 121 dass, or the 121 days must bo counted forvard from Nov. 21. Or thus:
    The above account inay be stated as follows: Oct. 10, 1871, L. N. Thempson paid R. Seeley \& Co. $\$ 650$; Nov. 21, 1871 , K. Seeley \& Co. paid I. N. Thompson \$875. Now, sinco R. S. \& Co. had the uso of $\$ 650$ for 42 days L. N. T. is ontitled to the use of $\$ 225$ (the balanco) until its interest equals the interest of $\$ 650$ for 42 days, which is 121 days. 121 days from Nov. 21, 1871, is Maroh 21, 1872.

    PROOR.

    | Dr. |  | Cr. |  |
    | :---: | :---: | :---: | :---: |
    | Due, Nov. 21, | \$875.00 | Due, Oct. 10 | \$650.00 |
    | Int. to March 21, 1872 | 17.65 | Int. to March 21, 1872, | 17.65 |
    |  | \$892.65 | Balance, | 225.00 |
    |  |  |  | \$892.65 |

    Suppose the debit and credit aide of the above acconnt, when equated, to stand as follows:

    Mue, Nov, 21, 1871, $\$ 650$.

    Cr.
    1 Due Oct. 10, 1871, \$875.

    What is the equated time for the payment of the balance?
    Oredits, $\$ 875$ Debits, $\quad 650$

    Balance, $\$ 225$
    Difference in time, 42 days.
    Explanation.- Suppose the acoount settled Nov. 21. The credit side is equal
    to $\$ 375$, and its interest from Oct. ! 0 . to Nov. 21, or 42 days. That the debit tide of the aecount may be inoreased by an equal ainount of inicrest, the balanco of the account must be regarded as duo 163 days previous to Nor. 21, or June 11 . Or thus:

    Oct. 10, 1871, L. N. Thomrison paid R. Secley \& Co. \$875; N(v. 21, 1871, R.S. \& Co. paid l. N. T $\$ 650$. Since R. S. \& Co. had the use of $\$ 575$ for 42 days, L N. T. is entitled to the interest of $\$ 225$ (ho balance) tor 163 days. Hence, the balance must he regarded as due 163 days previous to Nov. 21. The $\$ 375$ question is: How long must $\$ 225$ be on interest to equal the interest of
    Notr.-If R. Seeley \& Co. should wish to give their note for the balance, it is evident the note must be dated June 11, 1871 .
    499. Rule.- First find the equated time for each sille of the account without any reference to the other. Then multiply the side of the account which falls due wiRst by the munber of dhys letween the dates of equated time, and aivide the prodnct by the balance of the acconat. The quotient will be the number if clays to be counted Forward from the Latest date when the smallea side of the account falls due First ; and backwari whe:s the
    laraer side falls due first.
    Notr.-Some authors give the following rois :-Multip!'y the smaller side of the occount by the number of days between the dates of equater time, and dioide the product by the lulance of the accosnt. The quartient will be the timee for consideration. From the equated date of the larger eide, counc yonwt ho when thit side becomoo dwe last, bul BAOSWA RD when it becomes due first.

    ## ANOTHER METHOD.

    500. The equated time for the payment of the balance of an account may be found directliy without first averaging the debit and credit items, by the following method:
    

    Explanation.-We assume July 1, 1871 (the earliest date upon which any item becomes due), as the time upon which all the items of the acoount become due. The interest of the debit items, from this assumed date of maturity to the time they respeetively buceme due, equals the interest of $\$ 1$ for 124720 days; the interest of the oredit items equals the interest of $\$ 1$ for 85700 days. Henee, the balance of interest in favor of the debit side equals the interest of $\$ 1$ for 59020 days, or $\$ 225$ for $\frac{1}{2} 5$ of 59020 days $=262$ days. Since the balanoe of items is also in favor of the debit side, it is evident it can remain unpaid 262 da. without interest, or will become due 262 days from July 1, 1871, whith is Maroh 21, 1872. If the balance of items had been on tho oredit side, it would have been due 262 days previous to July 1, 1871.

    501 . Rule.-I. Assume the earliest date upon which any item of the account becomes due to be the time of maturity for all the items.
    II. Mulliply each item by the number of days intervening between this assumed date, and the date upon which it brcomes due, un. 7 find the sum of these products on each side of the account. Then divide the Difference between the sums of the delit and credit products by the balance of the account; the quotient will be the time for considerertion.
    III. Whan the diffirence of products and the balance of the accomut full on the sive side, count FORWARD; when on opposite sides, comat backward.
    Notss. -1. Tho latest dato may be used as a startirg.point.
    ?. In finding the equated tiwe, when tice certs, if uny, are less than 50, reject om ; whot inore, ad $3 \$ 1$. The work will he elificierily acourate.

    ## FXAMPLES FOR PRACTICE.

    1. J. Murphy has witn C. Duval an account, which, when each side th equated, stands as foltors:

    $$
    D_{r} .
    $$

    Due, Sept. 5, \$1542.
    Due, Sept. 24, \$1296. What is the equated time of payment for the Lal.? Anz. May 28.
    2. L. N. Carroll has with Simms \& Norris an account, the debit and credil sides ot wrich, when equated, are ay follows:

    ## Dr.

    Due, Fel. 8, $\$ 650$.
    Cr. What mut ke the date of a note Due, Feb. 12, $\$ 2180$.
    3. What in the equated time for the payment of the thalance of an account, which, whon the two eites are equated, viands an ioliows

    Dr.
    Due, June 12, $\$ 540$.

    Cr.
    Due, Aug 1, *960. Ans. Oct. 4.

    ## AVEHAGING OF AOCOENES

    4. At what time will the balance of the following aosount commence drawing interest?

    Dr.
    Due, Oct. 20, \$2520.

    ## Cr.

    Due, Nov. 25, \$1800.
    Ans. July 22.

    - What is the balance of the following account, and when is it due? Dr.

    Jomy Woodery.
    Cr.

    | 1871 April 10 | T0 |  |  | 1871 |  |  |  |
    | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
    | May 20 | "6 Cash ${ }^{\text {chen }} 2 \mathrm{mo}$, | \$ 450 | 00 | April 25 | By Caslı | \$615 | 0 |
    | June 15 | " Mdse., | 300 | 00 | June 10 | ${ }^{6} 4$ | 180 | 00 |
    |  | Mdse., | 12.00 | 00 | July 20 | " Mdse. | 1840 | 0 |

    Ans. Balance, $\$ 615$; due June 20, 1871.
    6. At what time did the balance of the following account become due, allowing that each item drew interest from its date?

    Dr. C. Ryan in acot. witi N. Miller \& Co. Or.

    | 1871 |  |  |  |  |  |  |  |
    | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
    | $\begin{array}{cc}\text { Feb. } & 22 \\ \text { "6 } & 24\end{array}$ | To Mdse. | \$ 44 | 70 | 1871 Feb. ${ }^{\text {1 }} 4$ | By |  |  |
    | March 20 | " 6 | 38 | 00 | May 16 | $\mathrm{bl}_{6} \times 1$. | \$38 | 50 |
    | ${ }^{6} 23$ | " 6 | 12 | 50 | June 14 | " 6 | 20 | 00 |
    | May 4 | 4 6 | 105 | 00 |  |  | 76 | 60 |
    | June 21 | " 6 | 94 | 30 |  |  |  |  |
    | June 21 | 66 | 15 | 00 |  |  |  |  |

    Ans. 25 days back of April 1st. = March 7.
    7. Required the balanse of the following account, and when it is due.

    Dr. A. E. Roy in acot. wita T. Lroas \& Co. Or.
    

    Due 208 days prior to Nov. 20, 1871, or on April 26, 1871. 8. What is the equated tume for the payment of the tralance of the following account, the merchandise items having a credit of 4 mo. $?$

    Dr. S. Thomas \& Son in acct. with R. Hill. Cr.

    | 1871$M a y ~$11 | To Milse. |  | \$680 | 56 | 1872 | By Cash. | $\$ 400$ | 00 |
    | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
    |  |  |  | Jan. 11 |  |  |  |  |
    | June 16 | * | " |  | 272 | 60 |  |  | " 29 | 00 |
    | July 1:3 | " | " | 144 | 20 | Feb. 11 | 6 6 | 80 | 00 |
    | Alig. 23 | 6 | 16 | 400 | 00 | * 25 | 16 | 784 | 00 |
    | $\begin{array}{rrr}\text { ¢1 } & 30 \\ \text { Sept. } & 9\end{array}$ | ${ }^{6}$ | \% 6 | 273 | 32 00 |  |  |  |  |

    Ans. 808 days back of Feb. 7, 1872, or on Nov. 21, 1869.
    9. What is the balance of the following acct., and when is it due?
    Dr.
    L. Murphy in account with A. Kelly.
    Cr.

    | 1871 |  |  |  | 1871 |  |  |  |
    | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
    | May June 12 | To Mdse. | \$218 | 00 | May 25 | By draft, at 60 da . | \$200 | 0 |
    | June 12 | " Sundries | 274 | 01) | June 6 | " Cash | 325 | 00 |
    | Nov. 14 | " Mdse. | 268 | $00 \mid$ | Aug. ${ }^{\text {Act. }}$ |  | 100 42 |  |

    Ans. Bal., $\$ 249$, due Sept. 22, 1871.
    10. Suppose the following account was settled May 6, 1871, by draft on time, how many days' credit should be given?
    Dr. P. Robinson in acot. with 0'Neil \& Co. Or.

    | Feb. 1871 | Mdse. |  |  | Feb |  |  |  |
    | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
    | March | ${ }_{6} 6$ | 73 | 44 | Feb. Io | By Cash | \$197 | 44 |
    | April 17 | 16 | 96 | 50 | '6. 21 |  | 51 | 68 |
    | May 1 | \% 6 | 144 | 72 | April 23 | " Sundries | 30 | 34 |
    | $\underline{ }$ | , 6 | 196 | 96 | May 6 | " Mdse. | 17 | 92 |

    Ans. 19 days.
    11. When shall a draft for the settlement of the following account be made payable?

    Dr. S. T. Mitcerll in acot. with R. S. Lee.

    | 18\%1 | To Mdse. on 2 mo. | \$108 | 72 | 1871 |  | 0 |
    | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
    | July 14 | ${ }^{6} 6$ on 40 da. | 56 | 90 | Oct. 15 | By | \$100 |
    | Aug 16 | " ${ }^{6}$ | 191 | 50 | Nov. 10 | " 6 , at | 250 |
    | Nov. 25 | " Sundries | 52 | 44 | " 20 | "Cash | 300 |

    Ans. Feb. 10, 1872.
    12. When shall a note be made payable, to balance the following account?

    Cr.

    | 352 | 00 |
    | ---: | ---: |
    | 80 | 00 |
    | 784 | 00 |
    |  |  |

    1869. 

    is it due?
    Cr.
    3. $\$ 20000$

    32500
    100100
    42 00
    2, 1871.
    1871, by
    Cr.

    5168
    $30 \quad 34$
    17
    19 days.
    g account

    Cr.
    $\$ 100$ 60
    250
    300
    ), 1872.
    following

    Dr.
    C. R. Martel wi loct. with N. Scott \& Co.

    | April 12 | To Mdse. on 3 mo. |  |  |  | $\$ 265$ | 42 | $\left\lvert\, \begin{gathered}1871 \\ \text { July } 14\end{gathered}\right.$ |  |  |  |  |
    | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
    | " 20 |  |  |  |  |  |  |  |  |  |  |
    | "' 30 | " | ، | " | " |  | 118 | 24 | " 25 | " | ${ }^{\text {ch }}$ | +218 | 00 |
    | May 5 | " | ، | \% | " | 369 | 78 | Aug. 3 | ، | ${ }^{6}$ | 160 | 00 |
    | " 16 | " | '6 | ${ }^{6}$ | \% | 136 | 72 | " 17 | ${ }^{6}$ | ${ }^{6}$ | 185 | 00 |
    | 4 29 | " | ، | ${ }^{6}$ | ${ }^{\prime}$ | 96 | 39 | Sept. 16 | ${ }^{\prime}$ | 6 | 185 | 00 00 |
    |  |  |  |  | , | 268 | 21 | " 24 | " | ${ }^{6}$ | 280 | 00 00 |

    13. A merchant owes $\$ 1368$ Sept. 16. If he pays $\$ 1678$, July , pable July 14 , and $\$ 936$, payable for the payment of the balance? 2 , what will be the equated time 14. S. Jordan owes G. Peters, 1871, Ans. Nov. 19. $\$ 1000$; May 15, for coal, $\$ 800$. Peters. 1871, May 1, for merchandise, for timber, $\$ 200$. Peters owes Jordane 14, for horses, $\$ 600$; July 24, April 2, for sundries, $\$ 400$; May 6 , 1871 , March 7. for flour, $\$ 800$; carriages, $\$ 240$. Allowing all the for oats, si600; June 13, for two when will the balance of the acct. becouns to be on 6 months' credit,
    14. A farmer owes $\$ 750$, due June 10 ? Ans. April 27, 1872. and wishes to discharge the due June 10, and $\$ 1500$, due Nov. 18, at an interval of 40 days; when wation by two equal payments, made
    15. A merchant holds when must the two payments be made? the second for $\$ 960$, due June 10, the first for $\$ 600$, due March 10, He wishes to exchange them for and the third for $\$ 720$, due Ang. 10 . $\$ 1200$, payable April 10; what shall bers, one of which shall be for rity of the other? Ans. Fe sice face and when the matu-

    Ans. Face, \$1080; maturity Aug. 6 .

    ## CASH BALANCE.

    502. When an account current is settled by cash, it is not necessary to find the equated time. The true or cash balanee of an account at a particular date may be found directly as follows : Ex. 1. What will be the true balance of the following account June 1, 1871, the time of settlement, allowing that each item draws interest from its date, at $6 \%$ ?
    $D_{r}$.
    C. Johnson in acet. with Andrews \& Son. Cr.

    | 1871 |  |  |  |  |  |  |  |  |
    | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
    | $\text { March } 5$ | To Mdse. | \$160 | 00 | ${ }_{\text {March }}^{1871}$ |  |  |  |  |
    | April 11 | " | 440 | 00 | " |  | By Cash | \$270 | 0 |
    | " 19 | " | 100 | 00 | May | 2 | " | 200 | 00 |
    | May 1 | " | 330 | 00 | " | 20 | " | 720 | 0 |
    | " 4 | " | 370 | 00 |  |  |  |  |  |
    | " 21 | " | 220 |  |  |  |  |  |  |

    OPERATION.
    Debits.

    | Due, |  | Days. |
    | :---: | :---: | :---: |
    | March | 5, \$160 | $\times 88=14080$ |
    | " | 25, 440 | $\times 68=29920$ |
    | April | 11, 100 | $\times 51=5100$ |
    |  | 19, 110 | $\times 43=4730$ |
    | May | 1, 330 | $\times 31=10230$ |
    | " | 4, 370 | $\times 28=10360$ |
    | " | 21, 220 | $\times 11=2420$ |
    |  | \$1730 | 6) 76840 |
    |  |  | \$12.807 |

    

    | Sum of delitit items, "/ credit items, | $\begin{array}{r}\$ 1730 \\ 1630 \\ \hline\end{array}$ | Interest of debit items, | \$12.807 |
    | :---: | :---: | :---: | :---: |
    | edit items, |  | " credit |  |
    | Balance of items, | \$100 | Balance of interes; | \$3.130 |

    True balance June $1, \$ 100+\$ 3.13=\$ 103.13$.
    Explanation. Since each item of the debit side of the acoount was on interest from its date to the time of settlement, the total interest of the several debit items equals the interest of $\$ 1$ for 76840 days, which, at $6 \%$, gives $\$ 12.807$. (The int. of $\$ 1$ for 6 days is 1 miil; hence, the interest of $\$ 1$ for 76840 days is found by dividing 76840 by 6 , and pointing off three decimal places.) The total interest of the several credit items oquals the interest of $\$ 1$ for 58060 days. which is $\$ 9.677$. Now, instead of increasing each side of the account by its interest, and then finding the balance, this same result may be obtained by finding separately the balance of items and the balance of interests. If the two balances fall cn the same side of the account, it is evident the true balance will be their oum; if, an different sides, their difference.

    ## METHOD BY INTEREST.

     sither for finding the equated time for the paymeat of the balanot of accountu, or in finding the camel belanew.

    The above account, when balanced by interest, may be presented as follows:

    Dr. C. Johnson in acct. with Andrews \& Son. Cr.
    

    Frons excepted.
    Quebec, June 1, 1871.
    Andrews \& Son.
    ANOTHER METHOD BY INTEREST.
    Dr. Gibe \& Hughes in acct. ocrrent with J. Hunter. Cr.

    ## 1871

    
    

    Au. 10 " Craft |  | 12000 |
    | :--- | :--- | :--- |

    ## Inc.

    $\begin{array}{r}=\$ 3.870 \\ = \\ =2.167 \\ = \\ =1.440 \\ \hline\end{array}$
    $6 \%$.
    operation.
    

    ## OASH balanoe.

    503. Rule.-Multiply each itent of the account by the number of days intervening between the date on which it becomes due und the time of settlement. Divide the sums of the delit and credlit products a espuctively by 6 : the quotient will be the interest of the two sides of the account, at $6 \%$, expressed in mills. Find the balance of items and also the brtunce of interests.

    When the two balances fall on the same side of the account, the cash balance will be their sum ; when on opposite sides, their difference. Or,

    Find the interest of each item from the date on which it becomes duc, to the time of aettlencent. The rifference between the sums of interests on the delit and credit sides of the account will be the balanoe of interest.

    When the balance of interest falls on the same side as the Balance of items, the cash balance will be their SUM; when on "pposite sides, their difference. Or,

    Find the number of duys intervening between each muturity and the duy of settlement.

    Compute the interest on cach item for the corresponding interval of time; add the inferest to the item if the maturity is before the day of settlement, $;$, 7 blruct it fron the item if the maturity is after the duy of sillthent; the results will be the cash values of the several items.

    Add each coluns: of cash values, and the difference of the amounts will be the cash balance required.

    ## EXAMPLES FOR PRACTICE.

    1. The following account was settled Nov. 16, 1871. What was the cash balance, interest being computed on each item from date at 6 \% ?
    Dr. John Fraser in acct. with L. R. Barry. $\quad$ Ans. $\quad$ C $r$.

    ## 1871

    Feb| Feb. |  | To Merchandise |  |  |  |  |
    | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
    | April | 4 | ${ }_{6}{ }_{6}$ Merchandise | \$ 72200 | Feb. 16 | By Cash | \$10000 |
    | May | 22 | " 6 | 187 <br> 250 <br> 00 | March 24 | ${ }^{4} 4$ | 15000 |
    | July | 19 | " Cash |   <br> 250 00 <br> 50 00 | April 16 <br> 6 20 | " ${ }^{\text {a }}$ | 30000 |
    | " | 22 | " Merchandise |  | June 27 | " Mdse. | 9000 |
    | Oct. | 10 | " ${ }^{\text {a }}$ | 12500 | June $\begin{array}{cc}\text { Sept. } & 3 \\ \text { S }\end{array}$ |  | 35000 |
    | Nov. | 16 | " bal. new acc't. | 125 | Sept. 3 <br> Nov. 16 | " Cash ${ }^{\text {" }}$ bal. of int. | 20000 | Errors excepted.

    2. Quebec, Nov. 16, 1871
    L. R. Barry.
    3. D. A. Hamel is in account current with Lynch \& Co., as fullows: Deftor, March 17, 1871, to merchandise, on 3 months, $\$ 721.50$; A pril 9, to mise., on 3 months, $\$ 481.12$; May 16, to mdse, on 3 mo ., $\$ 1750.48$; July 14, to mdse, on 2 months, $\$ 470.50$. Creditor, March 21, 1871 , by aash on acot., $\$ 500$; May 10, by acceptance at 30 daya

    ## AOOOUNT OF SALEE.

    8600 ; July 2, by mundries, $\$ 750$; July 17, by cash on acct., $\$ 800$. Required the ea-h value, if eettled on July 21,1871 , interest at $6 \%$.
    3. N. L. ley is in account and ins. Ans.49 lows: Dettor, January 11, 1871 , interest with Stevens \& Co., as folFeb. 13, to cash, paid draft, $\$ 120$; midse., on 6 months, \$187.32; \$380.28; April 9, to mdse., on 4 mo., $\$ 194$, to mdse., on 4 mo., paid draft, $\$ 120$; Aug. 30. to mdse., $\$ 194.40$; May 25, to cash, Feb. 12, by cash, $\$ 144$; March 30 , by mdse., on 4255.60 cilior, May 11, hy milse., on 6 mo., 8360 ; July 12, on 4 montl u4.20; $\$ 60$; Sept. 20, by molse., on 4 mo., \$119 12, by midee., un 4 mo., ance, if settled on Dec. 10, 1871, int. at $6 \%$. Required the true bal. 4. Req' red the cash balance due on the foll Ans. $\$ 73.73+$. 1, 1871, materest being computed on each following account, on July James Fisher in account and muter on each item from date at $7 \%$. Jan 7, 1871, to bal. of acct., $\$ 120$; with Henry S. Lane: Debtor, 24 , to bills payable, $\$ 130.50 ; F 20$; Jan. 15 , to indse., $\$ 96.75$; Jan. to mdse., $\$ 80$; May 10 , to mdse., $\$ 300$, mose., $\$ 200.80$; March 7 , Creditor, A pril _, le71, by cash, $\$ 140$; June 9, to mdse., $\$ 340.75$. 20, hy order on C. R., $\$ 140$; May 31 ; A pril 30, by cash, $\$ 50$; May midee., $\$ 500$.
    ; June 11, by Ans. $\$ 23.52$.

    ## aCCOUNT OF SALES.

    504. An Account of Sales is a statement of the quantity and price of goods sold, the charges incurred in the sales, and the net procceds, which a cormmission merchant or consignee makes to his employer or consignor.

    The net proceetls is the sum to which the empioyer is entitled after all charges are deducted. The net proceeds are due as cash at the equited time of the different sales.

    Ex. 1. focount of Sales of grain for C. Morgan \& Co.

    ## What was

    m date at 215.54.Cr.
    

    3arry.
    fullows :
    $\$ 721.50$;
    m 3 mo., r, March 30 daya

    ## IMAGE EVALUATION TEST TARGET (MT-3)

    

    Photographic
    Sciences
    Corporation
    

    ## Charges.

    Commission on $\$ 5316.80$, at $2 \frac{1}{2} \%, \quad \$ 132.92$
    May 30, Freight on 764 bushels of wheat,
    38.20

    Drayage and sacks,
    40.90

    Advertising in "Mercury",
    6.25
    218.17

    Net proceeds to credit of C. Morgan \& Co.,
    $\$ 5093.63$
    Errors excepted.
    Quebec, June 1, 1871.
    John Latrd \& $0^{\prime}$ Neil.

    Ex. 2. Auconkt Sates of 1300 harrels of flour, sold for E. A. O'Dowi, Mostreal, P. Q.
    
    H. E.

    Quebec, March 30, 1871.
    L. Rcsselid Co.

    Per Lonis Bilodean.

    Accoest Sales for Steward \& Nolan.
    

    ## examples for practice.

    1. Sales of 544 harrels flour, for account of P. S. Renaud \& Co., Montreal, by L. J. McGreevy \& Son, Quebec, viz.: July 2, 1871, to Jos. White, 400 bll. Ohio extra, at $\$ 8.30,19 \mathrm{bbl}$. fine, at $\$ 5$; July 5 , to Sweeney \& Co., 125 bbl . Canada extra, at $\$ 7.50$. Charges as follows: June 15, freight per Steamboat "Quebec ", 544 bbl. at 16 cts.,
    $8 s \$ 10$ for damage on the same; storage, 3 cts. per bbl. ; insurance,
    10.88 ; commission on $\$ 4352.50$, at $2 \frac{1}{2} \%$. Required the net proceeds, and the date when they shall be accredited to the owner.

    Ans. Net proceeds, $\$ 4139.45$; due, July 10, 1871.
    2. L. R. Doyle \& Co. of Toronto, received into their store an Invoice of Fruit per Grand Trunk, from the United States, on acct. of 'T'. A. Kane, New Orleans, and sold it as followe: Aug. 3, 1871, 100 boxes raisins, at $\$ 3$, cash, 52 boxes lemons, at $\$ 3$, cash; Aug. 4, 25 boxes 2.54 ; commission on $\$ 434.27$, at $5 \$$. Required the net proceeds sad when due? Ans. Net proceeds, $\$ 3531.22$; due, Oct. 24, 1871.

    ## TABLE

    OF FOREIGN MONEYS OR CURRENCIES, vi. बL THE
    PAR VALUE OF THE UNIT, AS FIXED BY COMMERGIAL USAGE.

    | Cities and Countries. | Denominations and Metal. | Value. |
    | :---: | :---: | :---: |
    | Argentine Rep. | $\{100$ centesimos = 1 real; |  |
    |  | $\{8$ reals $=1$ dollar (silver) $=$ | \$1.016 |
    |  | $\left\{\begin{array}{c}60 \text { kreutzers }=1 \text { florin } "\end{array}\right.$ | 0.485 |
    | Austria. | $\{120$ " $=1$ rix-dollar " $=$ | 0.971 |
    | Azores. | ( 1000 reas $=1$ milrea (silver) | 2.278 |
    | Baden. | 60 kreutzers = 1 florin ${ }^{\text {a }}=$ | 0.8397 |
    | Batavia. | 48 stivers = 1 rix-dollar ${ }^{\text {/ }}$ | $0.78{ }^{\circ}$ |
    |  | $\{60$ kreutzers $=1 \mathrm{fl}$ rin (silver) $=$ | 0.395 |
    | Bevaria. | $\begin{cases}\text { crown, } \\ \text { ducat, }\end{cases}$ | 1.072 |
    | Bélgium. ${ }^{\text {E }}$ |  | 2.274 0.186 |

    nand \& Co., 2, 1871, to $\$ 5$; July 5 . arges as foll. at 16 cts., ; insurance, et proceeds, 10, 1871. e an Invoice ct. of T'. A. , 100 boxes 4, 25 buxes Id at 60 da . , at $\$ 3$, and 0,150 boxes , 220 jars 1 amounting deducted; l'be charges 08; cartage advertising, set proceeds 24, 1871.

    ## I'HE

    al dsage.

    Value.
    $\$ 1.016$
    0.485
    0.971
    2.278
    0.830
    0.397
    0.782
    0.395
    1.072
    2.274
    0.186

    Cities and Countries.

    Bolivia.
    Brazil.

    Bremen.
    Brunawiok. Thili.

    China.

    Columbia.
    Darmstedt.
    Denmark.

    Egypt.

    England.

    Franco.

    Frankfort.

    Genoa and
    Piedmont. (ltaly )
    
    
    

    | Cities and Countries. | Denominations and Metal. | Value. |
    | :---: | :---: | :---: |
    | Tripoli. | 120 paras = 1 utchlik (silver) $=$ | 0.149 |
    | Tunis. | 16 carobas $=1$ piaster ${ }^{\prime}=$ | 0.124 |
    | Turkey. | $\left\{100\right.$ aspers $=1$ piaster ${ }^{\prime} /=$ | 0.026 |
    |  | $\left\{\begin{array}{l}\text { 20 piasters }=1 \text { yormilik (gold) }=1 \\ \text { Exchange on London, } 104 \text { piaskers, more or lese }\end{array}\right.$ | 0.877 |
    |  | for $\pm 1 . \mathrm{l}$. |  |
    |  | Exob. on Paris, from 400 to 410 piasters for 100 fr. $\int 12$ soldi $=1$ forin (silver) $=$ |  |
    | Tuscany. | $\left\{1\right.$ crown or corona ${ }^{\text {a }}$ = | 0.262 $1.05^{n}$ |
    |  | 1 ruspone (gold) = | 6.925 |
    |  | (1 sequin ${ }^{\text {a }}$ = | 2.301 |
    |  | Nota. - For Exchange on Lonaon and Paris, (oce Italy.) |  |
    | United Stater. | $\left\{\begin{array}{l}10 \text { mills }=1 \text { cent; } 10 \text { cts. }=1 \text { dime; } 10 \\ \text { dimes }=1 \text { dollar (gold) }=1\end{array}\right.$ | 1.000 |
    | Wurtembure. | $\int 50$ kreutzers $=1$ guilder (silver) $=$ | 0.395 |
    |  | $\left\{\begin{array}{l}1 \text { crown } \\ \text { a }\end{array}\right.$ | 1.070 |
    |  | ( ${ }_{\text {l }}^{\text {duchange on }}$ London and (gold) $=$ | 2.236 |
    |  | Exchange on London and Paris, the cane as for Frankfort. |  |

    ## EXAMPLES FOR PRACTICE ON EXCHANGE (see 406).

    1. A draft on Toronto cost $£ 187$ 10s. in Liverpool, exchange being at $8 \%$ premium for sterling; required the face of the draft?
    2. What is the cost of a draft on St. Perersbourg for 6915 roubles 50 copecks, exchange being at 74 cts. a rouble? Ans. $\$ 511$ i.47.
    3. Received of J. Walter \& Son, Glasgow, a bill on Messre. S. Ross \& Co., of Montreal, for £1143 15s. What was its value in Canada currency, the premium being $9 \%$ in favor of sterling currency $?$
    4. What is the value in francs of a bill Ans. $\$ 5540.833+$. premium of $3 \%$, and $5 \frac{1}{3}$ fr. to the dollar? 5. A merchant in Halifax has 8250 pil Ans. 5359 fr .29 cen. Amsterdam and requats Amsterdam, and requests the remittance by draft; what sum will he receive, exchange on Canada being in Amsterdam at $2 \frac{1}{4}$ guilkere Ans. $\$ 3666.77+$.
    5. A broker paid in Ottaws $\$ 8030$ for $£ 1650$ draft on Dublin; at what per cent. of premium did he purchase it? Ans. 9 des.
    6. What is the value in Canade currency, of 2000 florins in the Wetherlands, at $2: \%$ premium? Ans. 8.320.
    7. Twenty days after the date of a drat drawn at Genoa, Dec. 3, 1871, at ninety days, for 1820 liras 15 soldi, C. Jenkins to whose order it was drawn, requests payment, and proposes for prepayment a fisoount of $3 \%$. What is the value of the eame in Canada curreacy, alldwing that the corona bears a premium of $5 \%$ ? Ame. \$1948.91.
    8. A trader in Liverponl wighes to invest $\mathbf{f 3 0 0 0}$ in merchandse in Venice; if he remits to his correspondent at Venice a bill purohased for this $811 m$, at the rate of 8 d. sterling per lira, what sum in the enrrency of Venice will the agent receive? Ans. 90000 liras
    9. i. O'lirien of Montreal, has consigned a cargo of oats, valned at £6:00, to Payue \& Moss, London. J. Wikon d Co., being about to import an invoice of ilry goods, have purchased of Brook \& Son, a bill of exchange, at $8 \pm \%$ premium, for the value of the said cargo. What should they pay for the hill? Ge Ans. $\$ 31344.44+$.
    10. To Messrs. Newman \& Walter, Hamburg.

    Gentlemen: Please pay to the order of P. Krauss, \$1301.50, and

    Toronto, Sept. 14, $1871 . \quad$ Yours, \&c.
    Requirel the value of the above in mark Mannina \& Lewis.解 12. To Messrs. Woodley \& Lyman Ans. 3792. m. b. 15 skill.
    T. Sharples \& Co., 2130 scudi, anter date, please pay to the order of

    > Naples, Jan. 3, 1871. Your ob't servants,

    What is the value of the above $A$ Almeras \& Oraini. a discount of $2 \%$ being allobere draft, if paid 30 days after date, at manding a premium of $5 \%$ ? for prepayment, and the scudi comAns. $\$ 2083_{6^{\frac{1}{8}}}$.

    ## ARBITRATION OF EXCHANGE.

    ## 505. Arbitration of Exchange is the process of com-

    juting exchange between two places by means of bills of exchange drawn on one or more intermediate places.Notrs.-1. Exchange thus made betwoen two places is called Indirect or Cireular Exchange. When there is but one intarmediate place on which a bill is dratn, the computation is called Simple Arbitration; but when there are two or more intervening places on which bills are drawn, the oomputation is called Composind Arbitration.
    2. The main object of arbitration of exehange is to ascertain the oheapent route for making drafts or remittances. E.r. 1. When exchange at Montreal on London is at $9 \frac{1}{2} \%$ premium, and that at London on Amsterdam is at the rate of 12.5 guilders to the f, what must a person in Montreal, remitting through London, pay for a bill of excharige on Amsterdam for 1200 guilders?

    $$
    \begin{aligned}
    & \text { OPERATION. } \\
    & \frac{1209}{\mathrm{~T} 2.5} \times \$ 400 \times 1.095=\$ 467.20 \\
    & \text { Or thus }:
    \end{aligned}
    $$

    | \$ $\% x$ |  |
    | :---: | :---: |
    | 12.5 g'ders | $1 £$ |
    |  | $\$ 40 \times 1.095$ |

    Analysis.-Since it takes $\boldsymbol{E !}$ in London to buy a bill of exchange for 12.5 guildors on Amsterduin, it will take $\frac{£ 1200}{12.5}$ to buy a bill for 1200 guilders; bat a bill on London for $£ 1$ costs io Montreal $\$ 40 \times 1.095$ (422).
    In the second form we draw a verMcal line, and plach equivalents with
    symbols of their units directly opposite each other, beginnirg with that of the required quantity, which, for convenience is denoted by $x$, and so arrange the terins that the second on the left shali bo of the same denomination as the first on the right; the third on the leit, the same as the socond on the right; und $\Delta 0$ on should thore be a greator number of terms.

    Ex. 2. A merchant in Toronto wishes to remit 8000 francs to Paria by circular exchange throurgh Lonton. If exchange at Toronto on Paris is at the rate of 5 frincs 30 centimes to the dollar, that at London on Paris at the rate of 26 francs 20 centimes to the 2, and that at Toronto on London at $9 \%$ premium, how much less than by direct exchange, will it cost him, knowing that he pays his agent in London $\frac{1}{2}$ \% commission?
    operation.
    ${ }^{8} 8.90=\$ 1509.43+$ the cost of direct exchange.

    | $\$ \boldsymbol{x}$ | 8000 fr. |
    | :--- | :--- |
    | 26.2 fr. | $1 £$ |
    | $9 £$ | $\$ 40<1.09$ |

    $\$ x=\$ 1486.61+$.
    $\$ 1509.43-\$ 1486.61=\$ 22.82$.
    $=$ difference in favor of indirect exchange.

    Avalysis.-The cost of the lirect oxchange would be as many doslars as soum contains $5.3=1509.43$.

    To find the eost of tho eircular exchance we proceed as in Exc. 1, ex:ept that in this case the fnotor $1+\frac{1}{1} /{ }^{\prime}$ $=1.005$, must bo insluded amoner the factors on the right of the vertical line to cover the commission paid to the agent in London.
    506. Ruse.-I. Draw a vertical line, and place the equivalent sums with the characters denoting their respective units directly opposite each other on the left and right of this line, representing the required sum by $x$, and writing it first and on the left, and arranging the other terms so that the second on the left shall be of the same demomination as the first on the right, the third on the left the same as that of the second on the right, and so nm .
    II. When a commission is allowed for remitting. put 1 plus the rate on the right ( Ex .2 ) if the cost, and on the left if the proceeds, of the exchange is required. When a commission is allowed for drawing, put 1 minus the rate on the left if the cost, and on the right if the proceeds, of the exchange is required.
    III. Divide the product of the terms on the right by the prodluct of the terms on the left, and the quotient will be the cinswer.

    Nute-Commission for remitting is a percentage on the price the agent who remits pays for a bill of exchange; and commission on drawing is a percentage an the value of the bill at the place where the agent besides.

    ## EXAMPLES FOR PRACTICE.

    1. When exchange at Quebec on Liverpool is at $9 \%$ premium, and at Liverpool on Brussels 25 francs per $£$ sterling; what will be the arbitrated price in Quebec for a bill of exchange on Brussels for 2000, france?
    2. If at Ottawa exchange on London is at 93.8 premium, and at London on Pitris 26 francs 86 centimes per $£ 1$; what is the arbitrated course of exchange between Ottawa and Paris, throngh Londou?
    3. Exchange between Paris and Ainsterdum ins. S0.181. france 20 centimes to the guilder, that terdim wine the the of 2 the rate of 25 framea 80 centimes, that between london mid Piris at Lon lon at $9 \frac{1}{2} \%$ preminm, what will he the cost of a renitumat on 900 guilders from Halifax to Amsterigu by bills of a remittance for London and Paris?
    4. A merchant in Kingraton owes a det $4 n s, 533.18+$. to pay which he purchases a bill a debt of 4880 thaiers in Bremen, and remits the same to his arent on London, at a prenium of $9 \%$, requested to draw. If the exchange between on whom his creditor is at the rate of 3 fll. sterling per thaler, and Lomion an! Bremen be $\frac{1}{2}$ \%, how much must have heen the cost of the charyes for brokerage 2.0, how much must have heen the cost of the bill in Kingston?
    5. When exchange in (uuebec on Toronto is at Ans. \$33ti.5.87+. on Halifax at $2 \%$ discomnt if the exchatige between pramm, and Toronto is at par, how much better is the circuitous route Halifax and between Quebec and Toronto than the direct?
    6. When exchange between Toronto and liverpool is at $872 \frac{1}{4} \%$. miun, and between Liverpoo! and Paris 25 franes 25 contimes per $£$ sterling, what sum in Toronto is equal to 6500 trances in Paris?
    7. A merchant in Montreal wishes to remit Ans. B. $211.36+$. $^{2}$ remit through Paris, what will his to remit to Dublin s2580. If he money, allowing $\$ 3$ to be equal to 16 france amount to in sterling pound sterling?
    8. A man in Kingston wishes to draw on Hamilts E.57:3 68. stock dividend of $\$ 1125$, and exchange direct oniton for a railroad discount; how much will he save hy drawing on hamilton is $1 \frac{1}{4} \%$ at $1 \frac{1}{2} \%$ premium, allowing his agent in draw on agent in Toronto discount, brokerage at $1 / \%$ ? agent us traw on Hamilton at $1 \%$
    9. A banker in Quebec rernits $\$ 150$ to Edimburg. $\$ 11.03+$. as follows: first to Lyons at 5 frails 30 ceuimes per by arbitration, Hamburg at 184.50 francs per 100 marks; thes per $\$ 1$; thence io 35 stivers per 2 marks; thence to Edimb; thence to Amsterdain at sterling. How much sterling to Edimburg at 220 stivers per $£$ burg, and what vill be hia gein taoney will he bave in bank at Edimburg, and what vill be his gain over direct exch. at $10.1 \%$ premimm? 10. Ans. $\left\{\begin{array}{l}\text { Proceeds in Edimburg, } \begin{array}{lll}\text { G } 916 & 5 & 91 . \\ \text { Gain by arbitration, } & 111 & 19\end{array} \\ \hline 1\end{array}\right.$ remits through London. Required to semit to Montreal 14320 francs, currency, allowing 25.80 francs to the $£$ value of the same in Carada 11. A merchant in Hamburg, wishing to cancel \& clain $\$ 4.82$. in Ottawa, and for that purpose buys a bill of excheo clain of $\$ 2340$ the rate of 2 francs per mark brokerage $\frac{1}{2} \%$. Allowing $\$ 35$ to 100 mark bancos, what to Ottawa, cost him? 12. $\Delta$ of Barceluan owes B of Liverpool, $\begin{gathered}\text { Ane. } 16884 \text { francs. } \\ \pm 1900 .\end{gathered}$
    draws on $\mathbf{C}$ of Amaterdam, $G$ of Ametenlam on D of Borfeaux, and D of Bonleaux on A of Barcelona. Allowing $£ 1$ exchanges for $1^{2}$ florins; 19 Horins for 40 francs; and 100 france for 19 Spanislt dollare, how many dollars will pay the bill? Ans. s912n.
    10. I wish to remit from Ghasgow to Quehec $£ 1275$ is. Wirat will he its value in Canada currency, remitting throngh Paris at the following rates: $£ 1$ equals 25 franos 80 centimes; and 5 frances 30 centimes, equal $\$ 1$ ? Ans. $\$ 6210.25+$.
    11. A merchant in Halifax wishes to remit to London $\$ 6250$, so as to receive the largest possible returns for the same. If he remits directly to London, the aterling currency will command a premium of $9 \%$; if through Paris, it must be at the rate of 5 francs 20 centimes to the dollar, and 25 franos 80 eentimes to the pound; but if through Hamburg, at the rate of 35 cents per mark banco, and 55 mark bancos per $£ 4$. Which is the most desirable course?
    $A \eta s$. The course through Hamburg is preferable by $£ 8113$, to the direct course, and by $£ 39023$, to that through France.

    ## ARBITRATION OF MERCHANDISE.

    507 . Arbitration in Merchandise ennsists in comparing the weights and measures of different countries; also, in finding from the value of any particular weight or measure of one country, the value of the corresponding weight or measure of another country.

    By tho operations herein involved, the merchant is enabled to determine in what way he can most advantageously export or import any species of merchandise. The operation obviously consists, not only in the comparison of the weights and ineasures of different countries, but alse is the exehange of currencies.

    ## TABLE

    OF THE PRINCIPAK WEIGETS AND MEASURES OF THE MOST IMPORTANT COMMEROIAL COUNTRIES IN THE WORLD REDUCED TO THEIR ENGLISH EQUIVALENTS.

    | AUSTRIA. <br> (Chief commercial cities, Vienna and Trieste.) | $i$ ell, woollen meas. $=26.6 \mathrm{in}$. <br> 1 ell, silk $=2$ i. 2 " <br> BADEN AND BAYARIA |
    | :---: | :---: |
    | 00 commercial $\mathrm{lb} .=123.6 \mathrm{Avdp}$. | (Principal commercial city, |
    | 1 staro $=2.34$ Winch. but | G.) |
    | 1 polonick $=0.861$ " " | if) gram. |
    | 1 simer $=15$ wine gal. | b. Avdp. |
    | 1 barile $=173$ " |  |

    mifeaux，and anges for 12 Spanial dol． s．s9120． iis．What Paris at the 5 francs 30 $210.25+$ ． 362.50 ，ко as e remits di－ premium of 20 centimes t if through lark bancos $3113 k$ ，to $\infty$.
    comparing in finding e country， of another
    enabled to export or iously con－ casures of es．
    iE Most
    LLD
    $=26.6 \mathrm{in}$ ． $=25.2$＂
    ARIA． al city，

    Trench $=$ gr．Troy．

    1 foot
    1 klafter $=6$ feet
    1 achetfel for corn
    1 eimer of wine 1 mass

    BELGIUM．
    （Principal commercial city， Antwerp．）
    Weights and Measures the same as in France．

    BRAZIL．
    （Principal commercial city， Rio de Janeiro．）
    Weights and Measures the same as in Portugal．

    BREMENS．
    （One of the four Free Cities of
    Germany．）
    1 pound
    1 centher $=1.09 \mathrm{l}$.
    1 viertel of wine $=116 \mathrm{lb}$ ．
    1 anker $=5$ viertels $=9.95 \mathrm{ral}$.
    1 oxhoft $=6$ ankers $=5 \times$ gal．
    1 scheffel of grain $=2$ bu．
    1 last $=40$ sheffels $=80.70$ hu．
    1 sione flax
    OHINA．
    （Principal commercial city， Canton．）
    1 catty
    1 pecul
    1 corid
    CUBA．
    （Principal commercial city， Havana．）
    quintal
    1 arroba of wine
    1 fanega of grain
    1 vara

    $$
    \begin{array}{r}
    =101.75 \mathrm{lb} \\
    =4.1 \mathrm{gal} \\
    =3 \mathrm{bu} .
    \end{array}
    $$

    DENMARK AND NORWAY．
    （Principal commercial cities，
    Copenhagen and Chrastina．）
    1 pound
    1 centuer $=100 \mathrm{lb}=110.20 \mathrm{l} \mathrm{h}$.
    $\begin{array}{ll}1 & \text { viertel of wine } \\ \mathrm{l} \text { anker of wine }\end{array}=2.04 \mathrm{gal}$.
    $\begin{array}{ll}1 \text { anker of wine } & =10 \mathrm{gal} .\end{array}$

    $$
    =1.33 \mathrm{lb}
    $$

    ## （Principal conmercial city，

    Alexamphia．）1 rotolo forioro
    1 rotolo zauro $=15 \mathrm{oz}$ ．
    1 rotolo zalino $=21.3135 \mathrm{oz}$ ．
    1 rotolo mina $=26.7140 \mathrm{oz}$.
    1 quintal coflee in Cairo $=10: 3,0 \mathrm{li}$ ．
    1 oka
    1 dragna
    1 pik of corn
    $\begin{aligned} &=0.23: 9 \mathrm{II} . \mathrm{Tr} \\ &=1.9375 \text { dwt．}\end{aligned}$
    1 rebebe of corn $=21.8 \mathrm{in}$ ．
    1 kisloz
    EペゥLIN1．
    （Principal commercial cities， Lonvon and Lavirnol．．）
    The English Weights and Jens．
    ures are the same us in：Canada．
    FRANCE．
    （Principal commerrial cities，
    Pabls，Lyove，and Marsealimes．）
    Weights and Selmures，see p． $12($ ）．
    FRANKF（）R＇on the Main，
    and the solthers palets of Germany．

    $$
    =133.33 \mathrm{lb}
    $$

    $$
    =14.62 \mathrm{in}
    $$

    1 1 l ．heavy $=17.625 \mathrm{oz}$ ．Avdp．
    1 IU．light $=15.05 \mathrm{oz}$ ．Ir．
    1 mark $=52502$ ．Tr
    1 ewt．of 100 heavy，or lus hight
    IU．$=111 \mathrm{lb}$ ．Avdp．
    1 carat of jewels $=1.321$ dwt．Tr．
    1 foot $=11.25 \mathrm{in}$ ．
    1 ell $=21.555 \mathrm{in}$ ．
    1 Frankf．Brabant ell＝27．666 in．
    1 malter of corn $=3.1 .56$ bush．
    1 simmer $\quad 4 \quad=6.312$ gal．
    1 maas of wine $=3.156$ pints．
    1 ohm
    1 fuder $=6$ ohms $=31.312$ gal．
    1 fuder $=6$ ohms $=187.87 \%$ gal．
    HAMBURG AND LUBECK．
    （Commercial cilies of（ikismany．）
    1 pound
    $=1.068 \mathrm{lb}$ ．

    $$
    \begin{aligned}
    & =11.6 \mathrm{in} . \mid 1 \mathrm{ahm}=4 \text { ankers }=40 \mathrm{gal} . \\
    & =5.75 \text { feet. } 1 \text { finder of wine }=237.16 \mathrm{gal} \text {. } \\
    & 1 \text { toence or bhl of grain= } 3.95 \mathrm{ha} \\
    & 1 \text { last }=12 \text { toende }=47.50 \mathrm{bn} \text {. } \\
    & \begin{aligned}
    1 \text { denish ell } & =24.06 \mathrm{bll} . \\
    & =2.06 \mathrm{in} .
    \end{aligned}
    \end{aligned}
    $$

    $\begin{aligned} & 100 \text { commercial } \mathrm{lb}=106.838 \mathrm{lb} . \\ & 1 \text { foot }=11.289 \mathrm{in} . \\ & 1 \text { ahmof wine }=38.25 \mathrm{gal} . \\ & 1 \text { Huder }=6 \text { ahnıs }=229.5 \text { gal. } \\ & 1 \text { last of grain }=89.64 \mathrm{bu} . \\ & 1 \text { stock }=11 \\ & 1 \text { Brabant elf }=134.4 \mathrm{bu} . \\ &=29.58 \mathrm{in} .\end{aligned}$ HINDOSTAN.
    (Principal commercial cilies, Bombay, Bengal, Calcutta, and Madras.)
    1 mannd $=74.625 \mathrm{lb}$. Avdp.
    1 seer $\quad=29.875 \mathrm{oz}$. Avdp.
    1 sicca $\quad=178.666 \mathrm{gr}$. Tr.
    1 cubit, or 1 covid $=18 \mathrm{in}$.
    $1 \mathrm{guz} \quad=36 \mathrm{in}$.
    1 coss $=4000$ cubits $=1.125 \mathrm{mi}$.
    1 pallie of corn $=9.5 \mathrm{lb}$. Avdp.
    1 candy $=500 \mathrm{lb}$. Avdp.
    1 garee of corn $=135 \mathrm{bu}$.
    1 candy of corn $=24.5 \mathrm{bu}$.
    HOLLAND.
    (Principal commercial cties, Amstelidam, Hablen, The
    Hagce, Rotterday, Leyden, etc.)
    1 foot
    1 ell
    1 last tor corn $=27.983 \mathrm{in}$.
    $=85.25 \mathrm{ba}$.
    1 vat $=100 \mathrm{kan}=1=41 \mathrm{gal}$. $=26.42$ gal.
    1 muddle $=100$ hop $=1$ bectol. $=2.84 \mathrm{bu}$.
    1 pound $\quad=1.08 \mathrm{lb}$
    1 Fr. kilogramme $=2.20 \mathrm{lb}$.
    1 last, marine $=4410 \mathrm{lb}$.

    ## LOMBARDY (Italy.) <br> (Principal commercial cities, Venice \& Muan.)

    1 libra $=1$ kilogramme $=2 \mathrm{lb}$. $3 \frac{1}{4}$ oz. Avdp.
    The Measures are equal to the French.

    NAPLES (Italy.)
    (Princip th conmercial city, Naples.)
    1 rottulu $\quad=1.96 \mathrm{lb}$.
    1 cantaro grosso $=100$ rottolo $=$ 196.60 Jb .

    | 1 cantaro piccolo | $=106 \mathrm{lb}$. |
    | :---: | :---: |
    | 1 salma of oil | $=42.75$ gal. |
    | 1 carro of wine | $=264$ gal. |
    | 1 carro of grain | 52.20 bu. |
    | 1 canna | $8{ }^{\text {c }}$ |

    PORTUGAL.

    ## (Principul commercial eity,

    Lisbon.)1 libra or arratel $=1.01 \mathrm{lb}$. 1 arroba $=22$ arratel ${ }_{8}=22.26 \mathrm{lb}$. 1 quintal $=4$ arrobas $=89.05 \mathrm{lb}$. 100 libras or arratelo $=101.19 \mathrm{lb}$. 1 almude of wine $=4.37 \mathrm{gal}$. 1 tonelado $\quad=227.25$ gal. 1 canada $=13.06$ pints. 1 moyo of corn $\quad=23.03 \mathrm{bu}$. 1 vara $=43.20 \mathrm{in}$.

    > PRUSSIA.
    (Principal commercial city, Beri,in.)
    1 pound $=1.03 \mathrm{lb}$. 100 pounds Dantzic $=103.3 \mathrm{lb}$. 1 quintal $=110 \mathrm{lb} .=113.42 \mathrm{lb}$. 1 eimer of wine $=18.14$ gal. 1 ahm
    1 scheffel of graia $\begin{aligned} & =18.66 \mathrm{ggi.} . \\ & =1.52 \mathrm{bu} .\end{aligned}$
    1 last of grain $=91 \mathrm{bu}$.
    1 Berlin ell $=25.5 \mathrm{in}$.
    1 Prussian ell $\quad=26.2 \mathrm{sin}$.

    ## RUSSIA.

    (Principal commercial cities,
    St. Petersackg and Warsaw.)
    1 pound (funt) $\quad=0.90 \mathrm{lb}$.
    1 pood $=40$ pounds $=36 \mathrm{lb}$.
    100 pounds $\quad=90.26 \mathrm{lb}$.
    1 wedro of wine $\quad=3.25$ gal.
    1 sorokovy $=40$ wedros $=130$ gal.
    1 chetwert of oorn $=5.95 \mathrm{blz}$.
    $l$ arsheen $\quad=28 \mathrm{in}$.
    1 sashen $\quad=7$ feet. SARDINIA (Italy.)
    (Principal commercial cities, Genon and Turin.)
    1 peso grosso $($ Genoa $)=12.166$ oz. Avdp.
    1 libra (Turin) $=13 \mathrm{oz}$. Avilp.
    1 palmo $($ Genoa) $=9.75 \mathrm{in}$.
    1 mina of corn " $=3.50$ bu.
    1 barile of wine " $=16.3$ gal.

    1 barile of oil $"=14.25 \mathrm{gal}$.
    1 piede liprando $\left(\right.$ Turi ${ }_{11}$ ) $=20.5 \mathrm{in}$.
    1 piede manelle $"=12.75 \mathrm{in}$.
    1 raso (ell)
    1 sacco fur wine
    1 brenta
    $"=23.5 \mathrm{in}$.
    $"=25.5$ gal.
    $"=10.80$ gal.
    SAXONY.
    (Principal commercial cities, Dresden and Leipsic.)
    1 pound $\quad=17.625 \mathrm{oz}$. Avdp.

    1 foot
    1 ell
    1 schaffel of corn
    1 wispel $\quad=22$ gal.
    1 kanne $=1$ litre $\quad=1.75$ pint.
    SMYRNA and the LEVANT.
    l oka
    1 cantaro
    1 rotolo
    1 drachm
    1 pik
    1 killow of corn $=11.625 \mathrm{gal}$.
    SPAIN.
    (Principal commercial city, Madrid.)
    1 pound
    1 arroba $=2 \mathrm{i}$ pounds $=25.38 \mathrm{lb}$.
    1 quintal $=4$ arrobas $=101.52 \mathrm{lb}$.
    1 cantaro or a roba of oil $=3.75$ gal.
    1 cantaro or arroba of wine $=$ 4.25 gal.

    1 moyo of wine $=16$ arrobas $=$ 68 gal.
    1 botta $=38$ arrohas of wine $=$
    $38 \frac{1}{2}$ arrobas of oil $=127.5$ gal.
    1 fanega of corn $\quad=1.57 \mathrm{bu}$.
    1 caliz $=12$ fanegas $=18.91 \mathrm{bu}$.
    1 vara or yard $\quad=33.37 \mathrm{in}$.

    ## SWEDEN.

    (Chiefcommer. city, Stocкнодм.) 1 pound
    pound of iron
    1 anker of wine

    1 eimer of wine $\quad=20.75 \mathrm{gal}$.
    ahn $=2$ eimers $=41.50 \mathrm{gal}$. pipe $=3$ alıns $=124.25$ gal.
    1 tun or barrel of corn $=4.16 \mathrm{bu}$.

    $$
    =23.36 \mathrm{in} .
    $$

    SWITZERLAND.
    (Principal commercial cities, Geneva, Bern, \& Basle.)
    $1 \mathrm{cwt} .=100 \mathrm{lb} .=50$ kilogr. $=$
    110.25 lb . Avdp.
    $1 \mathrm{lb} .=\frac{1}{2} \mathrm{kilog} .=17.625 \mathrm{oz}$. Avdp.
    1 foot $=0.3$ meter $=11.85 \mathrm{in}$.
    1 ell $=2$ feet.
    1 stab or staff $=4$ feet.
    1 malter of corn $=4.12 .5 \mathrm{bu}$.
    olum of wine $=3.5$ pints.

    - maas $6=33$ gal.

    TURKEY.
    (Principal commercial city, Constantinople.)
    1 pound, chequi, $=11.33 \mathrm{oz}$. Avd.
    1 oka $=14 \mathrm{oz}$. Avilp.
    1 pik, commercial $=27 \mathrm{in}$.
    1 killow of corn $=7.5$ gal.
    1 fortin $=4$ killows $=30$ gal.
    1 almud for liquids $=1.37 \mathrm{gal}$.
    TUSCANY.
    (Principal commercial cities, Florence and Legrors.)
    1 pound
    1 quintal
    1 braccio $\quad=74 \%$ lb. Avdp.
    1 mile $\quad=23$ in.
    100 eacchi of corn -1 mile 48 yd . 160 quartuzzi $=201 \mathrm{hu}$. 1 barile of oil

    $$
    =7 \frac{3}{8} \mathrm{gal} .
    $$

    UNITED STATES.

    ## (Principal commercial cities,

    Net York, Boston, Chicago, New Orleans, etc.)
    The Weights and Measures are the eame as in England.

    Republics of South Ats and measurcs of Mexieo, Central Aunerica, and of the the same as those of Portugare the same generally as those of Spain; of Brazil, United States, and of Hayti, the same, in gene North Amorican Proviuces, of the of Hayti are about $8 \%$ heavier, and ite measures the samgland; but the woighte $=9.75$ iu. $=3.6_{0} \mathrm{bu}$. $=16.3 \mathrm{gal}$.

    The inetric system has of late been adopted by Spain and Portugal, to the exclusion of other weights and measures. In lxb4, it was logalizod in Great Britain; and its use, cither as a whole or in some of its parts, has been authorized in I隹ece, Hollani, ituly, Norway, Swe len, Mexico, Guatemala, Venesuala, Kcualor, Columbia, Brazil, Chili, San Salvadur, Argentine Republic, and the United Stafer.
    'lle following examples will embrace oporations analogous to what we have alruady had, in addition to the exehango of weights and measures.

    Ex. 1. A Montreal merchant imports from Holland 2550 ells of linen, which he finds costs him 2 florins per yard. In payment of the same, he remits throurh London. The amount of the remittance is required, allowing $9 \frac{1}{2} \%$ premium in favor of sterling currency, that £l exchanges for 14 florins of Ainsterdam, the agent at London charging $\frac{1}{4} \%$ commission.

    | operation. |  |
    | :---: | :---: |
    | \$ $x$ | 25.50 ells |
    | 3 ft . | $2.3 \times 4 \mathrm{fl}$. |
    | 14 fl . | £1 |
    | ¢9 | \$40 $\times 1.095$ |
    |  | 1.0025 |
    | $\$ s=\$ 2725.176+$ Ans |  |

    Analysis. - Since 1 ell equals 2.3 ft., 2550 olis $\times 2.3 \div 3=$ the same in yards; the yards multiptied by 4 , equal the whole cost in florins, which, divided by 14, are reduced to sterling currency; and this in turn is exchanged to dollars by multiplying by 40 and dividing by 9 , and this value is increased $9 \frac{1}{2} \%$ by multiplying by 1.095 , anil fioally the brokerage is added by multiplying by 1.0025 .
    E.e. 2. A merchant of Toronto sends lard to Hamburg at $\$ 10$ per cwt., and orders remittance through Liverpool, expense of remittance to be paid by N . Ashley of Hambirg. Allowing $\$ 7$ exchange for 20 mank bancos, and $1: 35$ mark bancos exchange for $£ 1$; also, that the sterling $£$ bears a premium of 9 数 in Turonto, and that 105 lb . Hain. burg equals 112 lb . 'toronto. What is the cost of 1 lb . Hamburg charges for commission being 2 \%, insurance $1 \%$ ?
    OPERATRON.

    | 105 | 10 |
    | ---: | ---: |
    | 40 | 9 |
    | 109 | 100 |
    | 100 | 103 |
    | 7 | 96 |
    | $x$ | 16 |

    $x=4$ skilings $5+$ plennings per lb., Ans.

    Avalysis. $\$ 10 \div 105=$ price of 1 lb. Hamburg in Canala carreney, whioh $x \frac{9}{40}$ or $£ 1$, smil 109 makes the required deduction in favor of Sterling currenoy; then the remaining value $\times$ $\frac{1}{1} \frac{8}{6}$, is increased by the percentage of expense, and thet value so increased $x$ 135 or ${ }_{7}^{95}$ is exchanged to mark bansos; if $f 1=13{ }^{5}$ inarks, $f 7=96$ marks; and the marks $\times 16$ skill. $=4$ skilliogs $5+$ pfenniugs per lb., Ans.

    ## examples for practice.

    1. A merchant in Quebec ships 2000 ib. of butter to Bremen, and sells the aame at 12 grotes per Bremen lb. The total receipts are remitted to Paris, and the merchant of Quebec draws on his agent there. For how many francs at 5.25 to $\$ 1$ must he draw. allowing his agent in Paris charges $2 \%$ commission? Ans. 1290.44 + fr.
    2. 3. Enright of Halifax imports from Lisbon 18 quintals of raisins, for'which he paye 60 rees per arrated. He sells the same in the

    Halifax market at 7 cta, per lb. What is his total gain, allowing he pays $2 \%$ commirsion for remittance, etc.?
    3. R. N. Burke ot Montreal imports from Belgium 2500 kilogr. of flax, purelased at 60 centimes per kilogr. The expenses of importar tion, incholing commission, etc., amount to $10 \%$ on the first cost. How many dollars must R. N. B. remit through Liverpool, to pay for the same, allowing a preminm of $8 \%$ in tavor of Sterling currency, and 25 francs to $\pm 1$ ? Also, allowing 7 \% of the whole for waste, and that R. N. B. soll the flax for 8 cts. per net pound; what per cent. did he gain on the total cost?

    $$
    \begin{aligned}
    & \text { Ans. } \$ 316.80 \text { to be remitted, and } 29 \text { \% gained. }
    \end{aligned}
    $$

    4. Maple sugar is bought in Quebec at 8 cts, a ponnll, and exported to Naples, and sold at 3.5 carlini per rottolo, and remittance is ordered throngh Paris, the exchange between Naples and Paris being at the rate of 24 grani to 1 franc, and between Paris amd Quebec at the rate of 5.25 firancs to $\$ 1$. Allowing $1 \frac{2}{3} \%$ tare in Naples, and that freight, insuance, etc., amount to $5 \%$, what is the profit or lose of the trans. action?
    5. Wishing to import broadcloth, I find Ans. 65\% grined. will cost me at Liverpool 12s. 6d. sterling, and the quality I desire centimes. Allowing a premium of $9 \%$ in tavor of Sterling cuncs 12 and 5.25 francs to the dollar, at which market can I perchase most advantageously, the brokerage, etc., being the same in each place? 6. Having a quantity Ans. $4 \frac{1}{25}$ cts. per yd. in favor of Liverpool. market, I make inquiri of wheat, which I wish to export to the best most favorable places, and prond Lonlon and Amsterdam the two minurits. I find that in Amster proceed to investigite their comparative and remittance can be effesterdan it commands $127 \frac{1}{2}$ florins per last, to 80 francs, 5.20 francs being equal 1 is 39. 4d. sterling per bushelg equal to $8 l$; and at London the price $9 \%$ in the Canaila market, Sterling currency bearing a premium of through Paris, amount to $1 \frac{1}{2} \%$, that expense of remittance, etc., \%. To which market sliall while from London it amounts to only

    Ans. 18 cts. per bushel in favor of London.
    7. A merchant in Kingston imported 372 stone of flax from Bremen at 4 grotes per lb . Which is the better course of remittance : through Hainburg and Liverpool, at the rate of 4 thalers to 9 mark bancos, and 97 mark bancos to $£ 7$, the pound sterling bearing a premiunn of $9 \%$; or, throngh Paris and Naples, at the rate of 76 thalers to 63 scudi of Naples, and I sendo to 5 francs, and 5.25 francs to $\$ 1$; the expenves of transmiesion through the former course being $2 \frac{1}{2} \%$. and through the latter 31 \% ? Also, how much is gained by so remitting? Ans. Hamburg and Liverpool is $\$ 3.54$ less than Paris and Naples.
    8. Importel flax from Amsterdam; cost 8 centesimi per pound of Netherlands. To pay for the same, remittance was made through London and Bremen, with a premium of $8 \%$ in favor of Sterling cur. rency, $£ 21$ exchanging for 128 thalers, and 2 florins of Netherlands to 1 thaler of Bremen, expense of remittance being $5 \%$. What shall I gain per lb., and also at what rate $\%$, if I sell the sume at 4 ots. per pound of Canada?

    Ans. Gained 1 cent per lb., or $33 \%$.

    ## SUPPLEMENT TO PROGRESSIONS.

    ## arithmetical progression (460).

    508. Case V.-Given the common difference, the number of terms, and the sum of "ll the terms, to find the first term.

    Ex. The number of terms is 34 , the common difference 6 , and the sum of the terms, of a series of numbers in arithmetioal progression is 3536 ; what is the first term?
    Operation. $\mathbf{a}=\mathbf{n}-[(\mathbf{n}-1) \times 1 \mathbf{c}]=\frac{3536}{34}-[(34-1)$ $\times 3]=5$, the Arst term, Ans.
    509. Rule.-Divide the sum of the terms by the number of ternes; subtract from the quotient, if the series be ascending, otherwise add to $i t$, half the product of the common difficence into the number of terms less $\stackrel{\circ}{ } \cdot$.

    ## EXAMPLES POR PRACTIOE.

    1. If the number of terms be 22 , the common difference 5 , and the sum of the terms 1221 ; what is the first term? Ans. 3.
    2. A farmer is to receive $\$ 300$ in 12 payments, each succeeding payment to exceed the former by $\$ 4$; what will his first payment be?

    Ans. 3.
    510. Case VI.-Given the first term, the common difference, and the mumber of terms, to find the sum of all the terms.
    E.e. If the first term of a series of numbera in arithmetical progression be 5 , the number of terins 34 , and the common difference 6 ; what is the last term?

    Operation. $1=\mathbf{a}+[(\mathbf{n}-1) \times \mathbf{c}]=5+[(34-1) \times 6]$ 203, the last term, Ans.
    511. Role.-Add to twice the first term, if the series be ascending; otheruise sedtract from it the product of the common difference into the number of terms, less one; multiply the sum or difference by half the numler of terns.

    ## EXAMPLES FOR PRAOTICE

    1. If the first term be 3 , the number of terms 22 , and the common difterence 5 , what is the last term? Ans. 108.
    2. A man purciased 100 yards of cloth; the first yard cost him 40 cts., and each succeeding yard 20 cts . more to the last ; what did the last yard cost him?

    Ans. \$20.20.
    3. The frat term of an ascending series is $\frac{2}{3}$, the number of terme 18, and the common diff. $\%$, what is the last terme?

    Ans. 71.

    ## Geometrical proaression (477).

    512. Case III.-Given the first term, the common ratio, and the number of terms, to find the sum of the terms.

    Ex. If the first term of a series of numbers in geometrical progres. sion be 5 , the ratio 3 , and the number of terms 12 , what is the sum of the terms:

    Cperation. $\approx=\mathbf{a}\left(\frac{\mathbf{p}^{\mathrm{n}}-1}{\mathbf{r}-1}\right)=6 \times \frac{\mathbf{3 1}^{12}-1}{3-1}=1328600$, Ans.
    513. Rule.-From the power of the ratio ohose degree is the number of terms, subtract one; divide the remainder by the commos ratio, less one, and multiply the quotient by the first term.

    ## EXAMPLES FOR PRACTIOR.

    1. If the first term be 4 , the ratio 3 , and the number of terms 7 , what is the sum of the terms?
    2. The first term in a geometrical Ans. 4372. terms 7, and the common a
    so che sum of the terms?
    3. If a body be put in Aus. 5461 . the first portion por motion ty a force which mover it 8 miles in in the ratio of 7 fime, 7 miles in the secomd equal portion, and so, in the ratio of $\frac{7}{8}$, for ever, how many miles will it pass over? Ans. 64 miles.
    4. Case [V.-Given the first term, the last term, und the sum of the terms, to find the common ratio.
    E.x. The first term of a geometrical progression is 1, the last term is 177147 , and the sum of all the terms is 265720 ; what is the common ratio?

    Operation. $\mathbf{r}=\frac{\mathbf{s}-\mathrm{a}}{\mathrm{s}-1}=\frac{265720-1}{265720-177147}=3$, Ans.
    515. Rule.--Divide the difference betweers the first term and the sum ly the difference between the last term and the sum: the quotient will be the common rutio.

    ## EXAMPLES FOR PRACTICE.

    1. The first term is 4, the last term 1372, and the aum of the terme 1600 ; what is the ratio?
    2. The first teru of a geometrical Ans. 7. is 32, and the sum of the geometrical progression in the lant term
    3. A debt of $\$ 4095$ the terms is 637 ; what is the ratuo? Ans. 2. ments, in geometrical can be discharged in a year by monthly pay. and the last $\$ 2048$; what will b, of which the frat payment is $\$ 1$, and the last $\$ 2048$; what will be the ratio of the seriee?

    ## PROMISCOOUS FXAMPLES IN PROGREGSIONS.

    1. A hady gave to a poor person on the first day of the year $\$ .10$; on the second, $\$ .25$; and each succeeding day s. 15 more, than on the former: how much did this person receive on the lant day of the year?
    2. For 7 days a captain distributed some money to Ans. Soldiers; on the first day he gave them \$.40, and on the following days he muluplied that sum by a certain number: find that number, knowing that on the 7 th day, they received $\$ 290$.
    3. What sum must be paid for a thermometer, whoze price is equal to the 1 sl . term of an arithmetical progresslon, of which the lith. term is $\$ 7.50$ and the ratio $\$ .50$ ?
    4. How many loaves of 2 lb . each did a baker aell on the last day of a week, if, on the first day, he sold for $\$ 3.84$ at the rate of 1 ; cents per 16.; and, it the sale of each day was triple that of the preceding day?
    5. On the first year of his business, a confection Ans. 23328. on the 7th. year he cleared $\$ 473850$, required thoner oleared 5650 ; year.

    Ans. 3.

    ## LIFE INSURANCE.

    516. Life Insurance is a contract in which a company stipulates to pay a certam sum of money on the death of the person insured, in consideration of payments made by the insured as specified in the policy.


    517. Life Insurance Policies are of the following kinds: 1st. An Eudowment Insurance Policy, that is, a contract in which an Insurance Company agrees to pay to the party insured a specified sum at a eertain alge, or to his heirs, should his death occur before that age, on condition that he shall pay an annual premium until the policy matures; 2nd. A Non-forfeiting life, or Eud.w. ment Policy, is one in which, even though the party insured should fail to pay his annual premiuns after the first, the company agrees to pay an equitable amount of the sum insured on the maturity of the policy.

    The Expectation of Life is the avarage number of years that persons of the same age may be expeoted to live, as determined by tables of mortality.

    Notes. - 1. The annual premium mist be euoh a sum as will, when pnt at interest, amonnt to the sum insured, at the elose of the erepentation of life. This snan is easily foand upon the principlo of Life Annuities.
    2. Life Insurance Companies havo tables showing the peminun to be pald at sny age to securs ad annuity of $\$ 100$, during the romainiler of life.
    3. Since a payment is made at the issue of tho polioy, and another at the expiration of the first year, the number of payments on a poliey will always be 1 more than the number of years.
    4. There are two talles showing the Expeotation of life. One, called the Carlisio Trable, the other, the Wigglesworth Table. The Exspectation of Life, acoording to the two tables namod, is shown in the following
    

    LIFE TABLE.

    ## ANNUAL PREMIUM ON $\triangle$ policy of $\$ 100$.

    | $\underset{\substack{\text { Age at } \\ \text { issue. }}}{ }$ | Payments during life. | Payments To cease at 65 | Payments To cease at 60 . | Payments To ceaso at 50. | Ago at issue. |
    | :---: | :---: | :---: | :---: | :---: | :---: |
    | 14 | \$1.4707 | \$1.4999 | \$1.5238 |  |  |
    | 15 | 1.5105 | 1.5422 | 1.5683 | $\$ 1.6150$ 1.6681 | 14 15 |
    | 16 | 1.5516 | 1.5861 | 1.6145 | 1.68810 | 16 |
    | 17 | 1.5940 | 1.6316 | 1.6625 | 1.7826 | 17 |
    | 18 | 1.6377 | 1.6786 | 1.7124 | 1.8444 | 18 |
    | 20 | 1.6829 | 1.7275 | 1.7644 | 1.9096 | 19 |
    | 21 | 1.7296 1.7780 | 1.7782 | 1.8186 | 1.9785 | 20 |
    | 22 | 1.8280 | 1.8310 | 1.8753 | 2.0516 | 21 |
    | 23 | 1.8798 | 1.8859 1.9431 | 1.9344 1.9963 | 2.1292 | 22 |
    | 24 | 1.9335 | 2.0027 | 1.9963 | 2.2118 | 2.3 |
    | 25 | 1.9891 | 2.0648 | 2.0612 | 2.3000 | 24 |
    | 26 | 2.0470 | 2.1300 | 2.1291 | $2.39+4$ | 25 |
    | 27 | 2.1071 | 2.1981 | 2.2007 | 2.4959 | 26 |
    | 28 | 2.1696 | 2.2695 | 2.3555 | 2.6054 | 27 |
    | 29 | 2.2346 | 2.3444 | 2.4395 | 2.72 .38 | 28 |
    | 30 | 2.3023 | 2.4230 | 2.5284 | 2.8525 | 29 |
    | 31 | 2.3728 | 2.5058 | 2.6226 | 2.9928 | 311 |
    | 32 | 2.4464 | 2.5930 | 2.7228 | 3.1466 | 31 |
    | 33 | 2.5232 | 2.6851 | 2.8296 | 3.3163 | 32 |
    | 34 | 2.6034 | 2.7824 | 2.9436 | 3.6044 | 3.3 |
    | 35 | 2.6873 | 2.8856 | 3.0657 | 3.7142 3.9503 | 34 35 |
    | 36 | 2.7752 | 2.9951 | 3.1971 | 4.2182 | 36 |
    | 37 | 2.8674 | 3.1117 | 3.3387 | 4.5251 | 37 |
    | 38 | 2.9641 | 3.2361 | 3.4919 | 4.8807 | 38 |
    | 39 | 3.0658 | 3.3692 | 3.6584 | 5.2981 | 39 |
    | 40 | 3.1729 | 3.5120 | 3.8402 | 5.2981 5.7959 | 40 |
    | 41 | 3.2856 | 3.6654 | 4.0393 | 6.759 | 41 |
    | 42 | 3.4046 | 3.8311 | 4.2588 |  | 42 |
    | 4.3 | 3.5303 | 4.0106 | 4.5021 |  | 43 |
    | 44 | 3.6632 | 4.205 5 | 4.7735 |  | 44 |
    | 45 | 3.8038 | 4.4181 | 5.0782 |  | 45 |
    | 46 | 3.9530 | 4.6512 | 5.4235 |  | 46 |
    | 47 | 4.1111 | 4.9075 | 5.8180 |  | 47 |
    | 48 | 4.2782 | 5.1902 | 6.2726 |  | 48 |
    | 49 | 4.4549 | 5.5038 | 6.8032 |  | 49 |
    | 50 | 4.6417 | 5.8536 | 7.4317 |  | 50 |
    | 51 | 4.8393 | 6.2470 |  |  | 51 |
    | 52 | 5.0486 | 6.6935 |  |  | 52 |
    | 53 | 5.2708 | 7.2061 |  |  | 53 |
    | 64 | 6.5067 | 7.6017 |  |  | 54 |
    | 65 | 5.7577 | 8.5048 |  |  | 55 |

    ENDOWMENT ASSURANCE TABLE.
    
    

    ## life instranoz.

    ## NON-PORFEITING TABLER.

    Annual Premiums payable for five, ten, fifteen, or iwenty yearz, to secure $\mathbf{6 1 0 0}$, payable at the death of the insured. If tho insured be living, and should fail to make any paymant when due, the policy will not be torfeited (nll the other conditions of the poliev being e mplied wish), but will be geod fir a sum payable at death propoitioned to the number of preminms patd; that is, atter whe premium, on for each, suecesenth, one-fifteen, or one-twonticth of the sum assured, and so made during life on the ordinary annual Lifends of Return Fremiuns will be

    | Age. | Five Payı | $\begin{gathered} \text { Ten } \\ \text { Rown's } \end{gathered}$ | Fifteen Paym's | Twonty Paym's | Age. | Five Payin's | Ten Paym's | Fittecn <br> Payin's | l'wenty <br> Payn's |
    | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
    | 21 | 7.8181 |  |  | \$2.656 | 36 |  | 85 |  |  |
    | ? | 7.848 | 4.386 | ?.2.260 | 2.716 | 37 | 10.702 |  | 4.434 4.546 | \$3.726 |
    | 23 | 8.020 | 4.482 | 3.332 | 2.778 | 38 | 10.936 | 6.050 6.190 | 4.546 4.648 | 3.816 3.406 |
    | 24 | 8.192 | 4.582 | 3.412 | 2.844 | 39 | 11.178 | 6.190 6.336 | 4.648 4.758 | 3.906 4.002 |
    | 25 | 8.374 | 4.690 | 3.494 | 2.914 | 40 | 11.422 | 6.478 | 4.758 4.870 | 4.002 4.096 |
    | 26 | 8.556 | 4.798 | 3.574 | 2.986 | 41 | 11.664 | 6.612 | 4.870 4.972 | 4.096 4.136 |
    | 27 | 8.758 | 4.914 | 3.666 | 3.062 | $4{ }^{4}$ | 11.886 | 6.738 | 4.562 5.062 | 4.186 4.276 |
    | 28 | 8.962 | 5.030 | 3.750 | 3.138 | 43 | 12.110 | 6.862 | 5.062 | 4.276 4.366 |
    | 29 | 9.154 | 6.138 | 3.838 | 3.210 | 44 | 12.332 | 6.988 | -1.26 | 4.366 4.462 |
    | 30 | 9.316 | 5.234 | 3.908 | 3.274 | 45 | $12.56{ }^{1}$ | 6.988 7.122 | 5.266 5.366 | 4.462 4.364 |
    | 31 | 9.488 | 5.330 | 3.980 | 3.3381 | 46 | 12.808 | 7.262 | 5.361 5.48 | 4.364 4.676 |
    | 32 33 | 9.660 | 5.430 | 4.060 | 3.408 | 47 | 13.063 | 7.410 | 5.610 | 4.076 4.800 |
    | 33 | $\begin{array}{r}9.812 \\ \hline 10.5\end{array}$ | 5.540 | 4.152 | 3.480 | 48 | 13.336 | 7.574 | 5.752 | 4.936 |
    | 35 | $1 \begin{aligned} & 10.259 \\ & 14.400\end{aligned}$ | 5.6581 | $4.2+6$ | 3.558 | 49 | 13.648 | 7.715 | 5.914 | 5. 098 |
    | 35 | 14.400 | 5. 782 | 4.334 | 3.640 | 50 | 1:1.984 | 7.972 | 5.10 6.106 | 5.054 5.274 |

    ## EXAMPLES FOR PRACTICE.

    1. What cum must a person pay annually to an Insurance Com pany, for a life policy of $\$ 2750$, his age being 31 years at the issue of the policy?

    OPERATION. $\$ 2750 \times .023728=\$ 65.252, .4 n s$. mally, and obtain $\$ 65.252$, the annual premlum required. Tablo, expressed deciface face of the policy, $\$ 2750$, by the rate \% found opposite 31 years in \&85.252, the annual premlum required.
    2. A person at the age of 23 insures his life for $\$ 1500$; what is his annual preuium?
    3. What is the annurl payment Ans. \$2E.197. pavable a the age of payment onla andowment policy for sisbeu, 4. A man 32 yeare issned to a person at the age 0127 years? \$850, due at the age of 50 took an endowment gssurance policy for more would his heirs oame amount with papme realized if he had taken a life policy for the oame amount with payment to eeage at 50 ?

    Ano. \$265.40.
    6. A gentleman obtained an insurance on his life at the age of 26 , and died at the age of 45 , the policy taken required anmual payments ot premimm during life, and secnrel to hia heirs sis65y.2t more than the whole preminin paid. What is the face of the policy?
    6. Le, Perry, 50 years old, effects an insus. Ans. \$6195.80. for which he pay-an aunual, erects an insurance for life for s7000, If he shonld die at the age of preminn of $\$ 4.60$ on each $\$ 100$ insured. amount of insurance that of so years, how much less will te the without interest? Ans. $\$ 2660$.

    ## ANVIITIES.

    51\%. An Annuity is a fixed sum of money payable annually. or at the end of equal periods of time, to continue for a siven number of years, for life, or for ever.
    i15. A Certain Annuity is one whose period of oontinuance is for a definite number of years.

    5'20. A Contingent Annuity is one whose time of conmencement, or ending, or both, is uncertain.

    5:21. A Perpetual Annuity, or Perpetuity, is one which continues forever:
    522. An Annuity in Reversion (whether certain, contingent, or perpetual) is one which begins at a specified future time, or on the oocurrence of a specified future event.
    523. An Annuity in Arrears, or Forborne, is one whose payments were not made when due. Interest is to be reckoned on each payment of an annuity in arrears, from its maturity, the same as on any other debt.
    524. The Amount, or Final Value, of an annuity is the sum of all the payments, at compound interest, from the time each became due, to the end of the annuity.
    525. The Present Value of an amnuity, at compound in. terest, is the sum of the present values of all its payments; or the present worth of its final value. The present value, put out at compound interest, will amount, at the time of the expiration of the annuity, to its final value.

    Notes.-1. An annuity is said to be deferred, when it does not commence until after a certinin period; reversionary, when it does not commence untll after the occurrence of somo specified future evont, as the death of a certam until after the
     2. The subject of annuities is of life. Its principul applications are leases, life-estates importance in the affarrs reversluns, life-insurance, etc. The leases, life-estates, pensions, rents, duwers, tables which give the present and final values of $\$ 1$ fordily solved by means of ut the ordinay rates of interect.

    Shoving the amount of an cinntilly if $\$ 1$ per annum, at compound inferest for cony number of yeurs not exceeding fifty.
    

    ## al compound fifty.

    TA1B1, E
    Showing the present worth if an annuily $f * 1$ per annum, to comtimue for any number of years not race ding fifty.
    
     at compound interest,' in arrears, or forborne.
    E.x. An annuity of $\$ 400$ a year remaned unpaid 6 years; what is the amount due, at $6 \%$ compound interest?

    ## operation.

    $\$ 6.975319$, amount of $\$ 1$ for 6 years. (See Table).

    $$
    400
    $$

    \$2790.1276; " \$400 "
    Nots.-When the annuity draws simple interest, the amount is found as in anmaal interest.
    597. Rule.-Multiply the amount, or final value, of an annuity of $\$ 1$ for the given rate and time, fomml in the table, by the given annuity, and the product will be the required umount.
    528. To tind the present value of an annuity certain.
    $\boldsymbol{E} \boldsymbol{x}$. What is the present value of an annuity of $\$ 80$, to continue 20 years, at $5 \%$ ?

    OPERATION. $\$ 12.46221$, present value of $\$ 1$. 80
    $\$ 996.9768$; " $\quad \$ 50$.

    Notr.-Since the present value of an annuity is the present worth of its amount, or final value, the prisent value of an annuity may also be found by first finding the amount, and then the present worth of this amount.
    529. Rule.-Multiply the present value of an annuity of $\$ 1$, for the given rate and time, by the given annuity.
    530. To find the present value of an annuity in perpetuity.

    Ex. What is the present value of a perpetual leasehold, which yields an income of $\$ 840$ a year, at $6 \%$ ?

    $$
    \begin{gathered}
    \text { operation. } \\
    \$ 840 \div .06=\$ 14000, \text { present val. }
    \end{gathered}
    $$

    analysis.-The present value must evidently be a principal whioh yields an annual iuterest of $\$ 840$, at 6 per oent.
    581. Rule.-Divide the given annuity by the interest of $\$ 1$, for one year.

    Nore.-When an annuity is payable semi-annually, or quarterly, interest must be allowed on the half-yearly or quarterly payments to the close of the year.
    532. To find the present value of an annuity in reversion.

    Ex. What is the present value of an annuity of $\$ 500$, deferred 10 jears, and to continue 8 years, ailowing $6 \%$ compound interest ?
    dity certain, urs; what is (ble).
    is found as in
    e, of an anable, by the ount.
    in.
    to continue
    esent value of ent worth of its , the present may also be ; the amount, worth of this
    uity of $\$ 1$,
    rpetuity.
    hold, which
    orosent value a prinoipal ual interest of
    erest of \$1,
    interest must the year.
    version.
    deferred 10 terest ?
    

    Analysis - The present worth of an annuity of $\$ 1$ tor 18 years must be equal to its present worth for 10 years, plus it a prosent worth for the 8 succeeding years. Hence, the wresent worth of an annuity of \$1 for 8 years deferrod 10 years, must equal its present worth for 18 years minus its present worth for 10 yoars. The present wurth of $\$ 500$ is evidently 500 times the prosent worth of $\$ 1$.
    533. Rule.- Find from the table the present value of an anuity of $\$ 1$, commencing at once and continuing till the termrnation of the annuit!, and also, till the reversion commences. Multiply the dififronce of these present values, b!y the given annuity.

    Notr.-If the annaity is perpetual, the present worth of $\$ 1$, commenoing at onee, is found according to the rule ( 5 3fit.
    53. To find the rmmity, the present or final value, time and rate being given.
    E.x. An annuity running 8 years, at $6 \%$, compound interest, is worth $\$ 623.70$; what is the annuity?

    ## operation.

    $\$ 623.70 \div 86.209744=\$ 100.43+$.
    535. Divide the present or final value of the given annuity by the present or final value of an annuity of $\$ 1$, for the given rute and time.

    Note. - When the amount of an annuity, the time and rate, are given, the annuity may be found by dividing the given amount by the amount of $\$ 1$ for the

    ## EXAMPLES FOR PRAGTICE.

    1. What is the present value of an annuity of $\$ 1300$, to continue 12 years, at is \%
    2. A ground rent in the city of Ans. $\$ 11522.22+$. $\$ 1926$, at $6 \%$ int. What is the vatuec yields an annual income of
    3. Find the tinal value value of the estate? Ans. $\$ 32100$. $4 \%$ compound interest.
    4. The present value of an annuity, to te Ans. $\$ 7200.66+$. $6 \%$ : compouved interest, payable annually continued 14 years, at annuity.

    ANAl.ysis. - Since $\$ 6.209744$, at 6 of compound interest, for 8 years, yiolds an annuity of $\$ 1$, $\$ 623.70$ will yield an annuity equal to $\$ 623.70 \div 6.209744$. given iome und raie.
    $\$ 5520$; required the Ane. $8593.86+$.
    5. What is the present value of a leasehold of $\$ 900$, deferred 6 yr ., and to run 10 yr., at $5 \%$ compound interest? Ans. $\$ 2804.43+$.
    6. What is the amount of an anavity of $\$ 1000$, forborne for $15 \mathrm{yr}_{\text {- }}$ at $3 \frac{1}{2} \%$ compound interest?

    Ans. :19295.6 $\dot{8}$.
    7. A widuw is entitled to $\$ 420$ a year, payable semi-annually, for 18 years; what is the present value of lee interest, at $7 \%$, compound interest?
    8. A yearly pension, unpaid for 12 years, at $6 \%$, compound int., amounted to $\$ 9550.2762$; what was the pension ? Ans. $\$ 1139.12+$.
    9. What sum should be paid for a perpetual anunity of $\$ 1500$, pay. able semi-annually, interest being at $6 \%$ ? Ans. $\$ 25000$.
    10. A lease, whose rental is $\$ 600$ a year, is left to a son and a danghter. The son is to receive the rent for 8 years and the daughter for the 12 yr succeeding. What is the present value of the daughter's interest, allowing $5 \%$ compound interest?

    Ans. $\$ 3599.39+$.
    11. What will an aunuity of $\$ 40$, payable semi-annually, amount to, in arrears for 5 years, at $6 \%$ ?

    Ans. $\$ 458.55+$.
    12. I wiah to purchase an annuity which shall secure to my ward, at $5 \%$ compound interest, $\$ 300$ for 15 years. What must I deposit in the annuity office?
    13. A laborer agreed to work for 1 year and 6 months at the rate of $\$ 25$ payable monthly; he was paid only at the end of the 18 mo ; how much did he receive, being allowed $6 \%$ simple interest per an num?

    Ans. $\$ 469.12 \frac{1}{2}$.
    14. A merchant being desirous to secure a dowry for his son, deposits annually a sum which, placed at simple interest, commencing at his 12 th year to his 23rd., amounts to $\$ 630$, and that due for dowry, to $\$ 5580$; find the value of the yearly deposit, and the rate $\%$.

    $$
    \text { Aus. Deposit, } \$ 300 \text {; rate, } 30 \% \text {. }
    $$

    15. A founder wishes to economise $\$ 360$ in 5 years; what sum shall he have to deposit at the end of each year so as to have the required sum, at the end of the 5\%1. year, comprising both capital and compound interest, at $5 \%$ per annum?

    Ans. \$65.16.
    16. What is the amount of an annuity of $\$ 45$. payable semi-annualiy, for 3 years, at 7 \% compound interest? Ans. $\$ 294.75+$.
    17. A servant leaves his yearly salary of $\$ 2.50$ in the hands of his master, on condition that he will allow him $4 \frac{1}{2} \%$ interest, per annum, to be added to his capital ; find how much will be due the servant a the end of 15 years. Ans. \$5196.01.
    18. A marbler buys divers blocks of marble measuring altogether 4.850 cubic yards at $\$ 116$ a cu. yard; he pays $\$ 122.60$ in cash, and settles the remainder in 4 anuuities; what is the amount of each annuity at $4 \frac{1}{2} \%$ interest.

    Ans. \$445.99.
    19. Find the amount of an annuity of $\$ 223$ for $5 \frac{1}{2} \mathrm{yr}$. payable every three months, interest at $1 \frac{1}{2} \%$ also quarterly.

    Ans. $\$ 5729.62 \frac{1}{2}$.
    20. An oil merchant bought 32 bbl. of superfne olive oil, for which he paid yearly $\$ 190$ for 10 years. If money was worth $6 \%$ per annum compound int., what was the cost of a barrel ?

    Ans. \$43.70.
    21. A planter agrees to pay $\$ 598$ in 13 payments, in such a manner that each succeeding payment shall be greater than the preceding one by $\$ 6$; what will be his first and last payment? Ams. Last $\$ 82$.
    22. What mut be paid for a life annuity of $\$ 560$ a year, by a person aged 55 years, at $5 \%$, compound interest? Ans. $\$ 5794.32$
    23. An officer who is 54 years old, wishes to secber an annuity of £575. The company to which he applies charges $5 \%$ per aunum on the capital deposited: what capital must he deposit, if interest be calculated at $4 \frac{1}{2}$ \% yearly, and if the probable duration of his life be 18 years and 1 month? Ans. $£ 7341125 \frac{1}{2}$.
    24. A laborer, from the age of 16 to 60 years, spent yearly $\$ 5^{2}$. for tobacco ; at his death, he left $\$ 416.66 \frac{2}{8}$ to his children. How innch would he have left them, had he dispensed himself from that useleas habit, and placed every year that money at $6 \%$ compound inter.
    25. A mechanic bought tools for the sum of Ans. $\$ 1415.45 \frac{2}{3}$. pay yearly, so as to cancel his debt in 3 years, at 51120 : what did he pound interest?
    26. I have deposited $\$ 5000$ at 50 inter Ans. $\$ 411.27$. withdraw only $\$ 150$ yearly, and $5 \%$ interest, on condition that I will will be added to the capital; that the remainder of the intereat years?
    27. When dying, a father left a sum of Ans. \$659].71. a boy and a girl 10 years old. The sum noney to his twin children, deposited at $7 \%$, simple interest, and that appointed for the boy was interest, payable semi-annually; the amoun the girl, at $6 \%$ compound 21 years of age; what sum was appointed tor each was $\$ 2000$ when Ans. \$1129.94 + for the bod to each of them?
    28. A carpenter furnished and hung ; $\$ 1043.78+$, tor the girl. being $1 \frac{3}{5}$ yards wide and twice as high blinds to 35 windows each $\$ 3.37 \frac{1}{2}$ per square yard, buse as high. He was paid at the rate of must be added to make up for the that $\frac{3}{3}^{3}$ of the height of the window in 3 instalmente, the being at $5 \frac{1}{2} \%$; what wast in cash, and the others yearly ; interest
    29. A person wishes to sell payment? Ans. \$232.40; is to open 9 years hence sell an 11 years annuity of $\$ 700$, which money, if he is allowed a how tnuch will the purchaser pay in ready 30. A roof of 128 equare yards 6 discount? Ans. $\$ 3267.41$. minous cement of $\frac{1}{8}$ of an inch was ovelaid with a ecat of bitu. The contractor was paid inch mothickness, at 18 s . $1 \frac{1}{2} \mathrm{~d}$. a sq. yard. year, except the last which 6 instalments payable at the end of eaoh 5 of comp. int. ; what was each paid 5 mo. after the preceding one, at 31. 4 man who is 45 years payment? Ans. $£ 19$ 13 $8 \frac{3}{4}$. eecured a yearly income of $\$ 5340$, withdraws from businass, having his stock at the rate of $\$ 93.25$, and invock bearing $4 \frac{1}{2} \%$; he then se l What shall be his yearly income; 10 ift the amount in a life annuity. for selling his stock; $2^{\circ}$ if the company he has to pay $\frac{1}{8} \%$ brokerage charges 9 多 for management ; $3^{\circ}$ if thy where he secures the annuity man is supposed to live yet 24 yr. 11 mo. is caloulated at $4 \frac{1}{2} \%$ ? The
    32. A deltor owes $\$ 20000$ for whioh he pays in Ans. $\$ 6 \nmid 95.38$. could he yearly join to his capital so as pays in. at 7 \%s; what sum 20 5r., if $5 \%$ int. is allowed on his 80 as to cover both debt aind int. in 33. A clerk meceiwing a onlany yeash aoct.? Ams. $\$ 2004.8 \mathrm{~J}$.
    $\$ 8$ in a Savings Bank, at 312 ; and continues the same for 20 yeare, commencing at the age of 25 . What will be his capital at the end of the 20 th year, including an income of $\$ 40$ from stock bearing $41 \%$, which, ai his request, the bank purchased for him from his deposits every scond year. at the average rate of $93 \%$ ? Ans. $\$ 12852.94$.
    34. An cogineer who earns on an average $\$ 2.30$ a day, and works 25 days a month, spends yearty $\$ 17 \theta$ for houcesent, $\$ 85$ for family expenses, and $\$ 60$ for sundry expenses. We want to know; $1^{\circ}$ how muoll he may save yearly; $20^{\circ}$ what will be the total value of his yearly savings by depositing them at $6 \%$ compound interest, from his 30 th to his 47 th year; $3^{\circ}$ what yearly income he will enjoy at the age of 64 , if at 47 he converts the total value of his savings into an annuity bearing $4 \frac{1}{2} \%$ interest, supposing him to live to the age of 75 and 4 montls?

    Ans. $\mathbf{1}^{\circ} \$ 135 ; 2^{\circ} 3808.74 ; 3^{\circ} \$ 943.68+$.

    ## TEMPERATURE-THERMOMETERS.

    536. Temperature is a tenm employed to denote the condition of a body in respect to heat, or cold; it also expresses the greater or less capacity of a body to exoite in us the sensation of heat or cold.

    Note.-Heat and cold are correlative terms; that is, as the formor inopeares in a body, the latter decreasos, and the converse. Temperature generally refers to the amount of sensible heat in a body; eold being regardod as the absence of
    heat.
    > 537. A Thermometer is an instrument used to measure the temperature of bodies.

    Notes:-1. The construction of thermometers depends an the principie, whieh is universal, that bodies are expanded by increasing and contracted by deoreasing their tempepature. The thermometer commonly used for measuring remperatures neither oxtremely high nor extremely low consists ot a glass tube having a small bore of uniform diameter, and at its end a bulb within which is meroury. There wa also a scale which measures in degrees the length of the oolumn of merouny, whinh by its expansion or contraction within the tube indicetes the tempersture $t^{0}$ whieh the therinometer is exposed.
    2. Thermoneters are graduated by marking on the tubes, or attaohed platos, two points at which the meroury atands at Gixed and easily ascoriained temperatures, the hower boing that of frecring water callod the freening point, and the hisher theat of boiling water, when the baromoter stands at 29.92 fnohes ( 760 milumys.
    538. In the centigrade thermometer, or that of Celstins, the freering point is marked zero $\left(0^{\circ}\right)$, the boiling point, $100^{\circ}$; and the intemmediate space is divided into 100 equan parts called degrean
    533. In Fuhrenheit's thermometer the freezing point is marked $32^{\circ}$, and the boiling point, $212^{\circ}$, and the interval $\left(180^{\circ}\right)$ is dix ided into 180 equal parts.

    Notm-The $0^{\circ}$ of Fahrenheit's thermometer is the temperature of a mixture of snow and oommon salt.
    540. In Reaumur's thermometer the freezing point is inarked $0^{\circ}$, and the boiling point, $80^{\circ}$, the interval being divided into 80 equal parts or degrees.

    The graduations of these inetruments miay be extended upward from the boiling point, or downward from the freezing point of water, by repeating in these directions the equal divisions between these points (- $399^{\circ} \mathrm{C}$., - $39^{\circ} \mathrm{F}$., But below the freezing point for mercury mercury ( $3488^{\circ} \mathrm{C} . ; 660^{\circ} \mathrm{F} . ; 2791^{\circ}$ ), and above the boiling point of to indicate the temperature by the R.), the instruinents would cease fact, unreliable for temperatures scales. Their indications are, in ( $3133^{\circ}$ C.; $2502^{\circ} \mathrm{K}$.) $600^{\circ}$ by Fahrenheit's scale

    Norm.-For high tomperatures an instrument oalled a pyrometer is used Wedgwood's pyrometer $\mathbf{1 0 7 7 7 ^ { \circ }}$ on Fahrenheit's scale. For measuring tomperatures below - $30^{\circ} \mathrm{F}$., spirits of wine or alcohol instead of mercury is used for

    Since the interval between the freezing and boiling points of water is divided into 100 equal parts in the Centigrade, 180 equal parts in Fahrenheit's, and 80 equal parts in Reaumur's thermometers, it fol. freezing point of water is marked $32^{\circ}$ But in Fahrenheit's scale the Reaumur's scales, this point is $32^{\circ}$, whereas in the Centigrade and marked $0^{\circ}$. Hence,
    541. To change a temperature as given by Fahrenheit's scale into the same as given by the Centigrade scale.

    RUI.E.-i:xbtruct $32^{\circ}$ from Fahrenheit's degrees, and multiply the remainder by $\frac{5}{0}$. The product will be the temperature in Centigrade degrees.
    549. To change from Fahrenheit's to Reaumur's scale. Rule.:-Subtract $32^{\circ}$ from Fahrenheit's degrees, and multiply the remainder by s. The product will be the tenperature in Re. aumur's degrees.
    543. To change a temperaturo as given by the Centigrade seale into the same as given by Fahrenheit's.

    Rule.-Multiply the Centigrade degrees by $\frac{9}{5}$, and add $32^{\circ}$ to the product. The sum will be the temperature by Fahrenkeit's
    scale
    544. To ohange from Reaumur's to Fahrenheit's soale.

    Role.-Multiply the degrees on Reaumur's scale by $\frac{9}{\frac{9}{6} \text {, and add }}$ $32^{\circ}$ to the product. The sum will be the temperature by Fahrenheit's scale.

    Note. -The above rules are applicable to all temperatures, observing that on ohanginy degrees below 32 on Fahrenheit's scale to degrees on the Centigrade, or on Reaumur's seale, the minus aign inust be prefized to the result; and that when we change degrees below the zero on the Centigrade, or on Renumur's scale, to degrees on the Fahrenheit soale, we subtract the degrees on elther of the first scales after they are converted into degrees on Fahrenheit's scale from 32, if the degrees thus oonverte 1 be less than 32, and give the remainder the plus sign; but if the dogress on either of the first two scales ohanged into degrees on the Fahrenheit seale bs greator than 32, we subtract the 32 and prefix the minus -gn to ti.e result.
    545. The degrees on the Centigrade, Fohrenheit's, and Reaumur's scales, corresponding $t$ ) temperatures differing by $10^{\circ}$ Centigrade between the free $/$ ing and boiling points of water, are given in the following table:
    

    By means of the rules (541,542, 543, 544,) the student can readily extend this table above and below these limits.

    ## gXAMPLES FOR PRACTICE.

    1. What temperature by Fahrenheit's scale corresponds to $176^{\circ}$ Centigrade ?
    2. When the temperature of a body by Reaumur's Ans. $3484^{\circ}$. 78, what is it ly Fahrenheit's? Ans. $207 \frac{1}{2}^{\circ}$.
    3. What temperature by Reaumur's thermumeter answers to $83 \mathfrak{1}^{\circ}$ Oentigrade?
    4. What temperature by Centigrade's scale corresponds to $45^{\circ}$ Fairrenheit?
    5. When Fahrenheit's thermometer indicates - $13^{\circ}$, Ans. $7 \frac{20}{0}{ }^{\circ}$. the Centigradu and Reaumur's indicate?

    Ans, Centigrade, $\mathbf{- 2 5 ^ { \circ }}$; Begumur, $-20^{\circ}$.
    soale.
    量, and add by Fahren-
    erving that on Centigrade, or ult; and that numur's seale, her of the first from 32, if the the plus sign; tegrees on the fix the minus
    's, and Re. ng by $10^{\circ}$ f water, are
    umur.
    $0^{\circ}$ Zero.
    $8^{\circ}$
    $6^{\circ}$
    $4^{\circ}$
    $2^{\circ}$
    $0^{\circ}$
    $8^{\circ}$
    $6^{9}$
    $4^{\circ}$
    

    ## MENSURATION.

    ## DEFINITIONB.

    546. Mensuration treats of the measurement of lines, sur faces and solids.
    547. A Point is that which has place, or position, but not marnitude.
    548. A Line has length without breadth or thickness, and may be straight or ourved.
    549. A Surface is that which has length, or breadth, without height, or thickness. There are three kinds of surfaces; viz., plain, convex, or curved, and concave.
    550. A Plane Surface is one, every point of which is touched by a straight line, extended over and upon it.
    551. A Curved Surface is one that has length and breadth without thickness, and is constantly changing its direetion.
    552. A Concave Surface is the reverse of the ourved, and oonstitutes the interior surfaee of a hollow sphere.
    553. A Solid, Volume, or Body, is that whioh has length, breadth, and thickness. Length, breadth, and thiokness, are called dimensions. Hence, a solid has three dimensions, a surface two, and a line one.
    

    ## ANGLES.

    554. An Angle is the divergence of two straight lines from a cominon point ; as the angle A. Also read A B C. The two straight lines are called the sides of the angle, and the common point of interseotion, the vertax.
    555. A Right Angle is an angle formed by a straight line and a perpendicular to it, and contains $90^{\circ}$; as the angles ABE and EBC.
    556. An Acute Angle is one less than a right angle; as the angles EBD, DBC.

    557 . An Obtuse Angle is one greater than a right angle; as the an. gle A B D.

    ## TRLANGLEA,

    
    558. Parallel lines are those that lie in the same direction; they are everywhere equally distant from each other; as A B and C D.
    polygons.
    lines, sur n, but not kness, and , without wes; viz., which is d breadth on. rved, and as length, ness, are a surface
    
    559. A Polygon is a figure bounded by straight lines; as A B CDE.
    560 . A Diagonal of a figure is a line which joins two of its opposite angles; as A B and BD.
    561. The Perimeter of a polygon is the sum of all its sides; as A B C D E.
    562. The Base of a figure is the side on which it is supposed to stand; as B C.
    563. The Altitude is a line drawn from the opposite side, or angle, perpendicular to the base. its surface. .
    565. Polygons of three sides are called triangles; of 4, quadrilaterals; of 5 , pentagons; of 6 , hexingons: of 7 , heptagons; of 8 , octagons; of 9 , nonugons; of 10 , decagons; of 11 , undecagons; of 12, dodecagons, etc.

    ## TRIANGLES.

    566. There are several kinds of triangles, namely:
    567. An Equilateral Triangle, the three sides of which are equal.
    568. An Isosceles Triangle, two sides of which are equal.
    569. A Scalene Triangle, the three sides of which are unequal
    570. A Right-angled Triangle, which has one right unequal.

    In the right-angled triangle, the side opposite the righte. is called the hypothenuse.
    

    Equilateral.
    

    Inosceles. NOTI. -The dotted lines represoat the altitude of the triangle.
    

    Scalene:
    

    Kight-angled.

    ## QUAIIRILATERALS.

    587. There are three kinds of quadrilaterals, namely:
    588. The Parallelogram, which has its opposito sides parallel.
    589. The Trapezoid, which has only two of its sides parallel.
    590. The Trapezium, which has nene of its sides parallel.
    

    Parallelogram.
    

    Trapemoid.
    

    Trapexiuas.
    568. There are four kinds of parallelograms, namely :
    

    Squara.
    

    Bhombus.
    

    Khumboid.

    Rectangle.

    1. The Square, whose sides are equal, and whose angles are right angles.
    2. The Rectangle, which is any right-angled paraild iscram.
    3. The Rhombus, or Lozenge, whose sides are equal, and whose angles are not right angles.
    4. The Rhomboid, whose opposite sides are equal, but its angles are not right angles, and its length exceeds its breadth.
    OF THE CIRCLK.
    
    5. A Circle is a plane figure bounded by a line, every part of which is equally distant from a point within called the centre, as AGHBCED.

    The Circumference of a circle is the line that bounds it. It is divided into 360 parts oalled degrees.
    570. An Arc is any jortion of the circumference; as A D, A G.
    5\%i. A Radius is a line drawn from the centre to the circumference ; as OA, or O C.

    57 :. A Diameter is a line which passes through the centre, and is terminated by the circumference; as A B.
    573. A Chord is a straight line joining the extremitios of nn arc; us D U.
    574. A Secant is a line which neets the circumference in two points, and lies purtly within and partly without the circle; as $G \mathrm{H}$
    575. The Segment of': cirole is the portion inoluded by an are and its chord; as the space included by the are D) E C and the chord D C.

    575 . The Sector of a cirole is the portion included by two radii and the intercepted are; as the space 0 B CO.
    577. A Zone is the space between two parallel chords of a cirole; as the space AGHBA.

    Trapesiau.
    mely :
    uare, whose il, and whose rht angles.
    Rectangle, right-angled
    hombus, or ose sides are hose angles angles.
    Rhomboid, e sides are angles are les, and its its breadth.
    are bounded equally dise centre, as e is the line 360 parts
    ; as A D, to the cirthe centre,
    
    578. A Circular Ring is the space included between the circumference of two concentric oircles; as the sp.oe betwecu the rings A B and D E .
    579. A Lune, or Crescent, is the space contained between the aros of two intersecting circles.
    580. A Regular Polygon is one whose sides and angles are equal; as the pentagon A BCD E.
    581. An irr gular Polygon is one whose sides and myrles are unequme.
    589. An Insoribed Polygon is oue whose vertiges of all tho angles are in the ciroumference ; as A B CD E, and whose radins of the circle is $A 0$.
    5833. A Circumsoribed Polygon is one whose all sides are tangent to the circumference, and whose radius of the circle is 0 F.

    MENSURATICN OF SURFACES.
    Problem T.
    To find the area of any parallelogram.
    581. Rule.-Multiply the buse by the ultitude, and the product
     will be the aren.
    E.x. 1. What is the area of a square $A B C D$, whose side is 4 yards?
    Operation, $4 \times 4=16$ equare yards, Ans.
    2. Find the area of the squares whose sides are:

    1 st 26.30 yd ; 2nd 324.48 yd ; 3rd 638.7 yd .;
    4th 1476.004 yd.; 5 th 3684.0132 yd .
    Ans. 1 st 691.69 sq. yd.; 2nd 105287.2704 mq.
    

    Anatigis. -The ineight requirel should be suoh, as bein: anultiplied by the base, the product will equa! 112: hence, that hoight sho:id be equal to $112+$ $14=1$ yards, An9.
    5. Find the area of each of the following rectangles, whose bayes and altitudes are: 1st A $B=46.70 \mathrm{yd}$., $B C=15.15 \mathrm{yd} . ; 2$ nd $\mathrm{AB}=$ $146.24 \mathrm{yd} ., \mathrm{B} C=75.20 \mathrm{yd}$. ; 3rd A B $=206.75 \mathrm{yd} ., B C=147.24$ yd. $; 4$ th A $B=467.35 \mathrm{yd} ., \mathrm{B} . \mathrm{C}=250.75 \mathrm{yd}$.

    Ans. 1st 72l.511 $\frac{1}{2}$ g. yd. ; 2nd 10997.248 sq. yd., etc.
    
    6. What is the area of the rhombus $A$ C D of which the base A. B is 12 feet, and altitude E D, 4 feet?

    Operation. $12 \times 4=48$ sq. feet, Ans.
    7. Find the area of the rhombus whose bases and altitudes are as follows: lst A B $=40.22 \mathrm{yd}$., $\mathrm{E} D=32.75 \mathrm{yd} . ;$ 2nd $\mathrm{D} \mathrm{C}=105.75 \mathrm{yd} ., \mathrm{C} \mathrm{F}=$ 86.95 yd. ; 3rd A B $=145.20$ yd., $E D=127.54$ yd.; 4th D C $=$ $235.15 \mathrm{yd} ., \mathrm{C} \mathrm{F}=180.35 \mathrm{yd}$. ; 5th $\mathrm{A} B=375.75 \mathrm{yd} ., \mathrm{E} \mathrm{D}=295.85 \mathrm{yd}$. Ans. 1st li317.205 sq. yd.; 2nd 9194.9625 sq. yd.; 3rd 18518.8080 eq. yd., etc.
    8. Required the area of a room whose length is 15 feet 6 inches, and width, 7 ft .8 in .
    9. What is the differ. Ans. 118 sq . ft. 10 eq. in. and that of two diference between the area of a floor 50 feet square,
    10. Find the others, each 25 feet square? Ans. 1250 feet. heir altur bases of rectangles containing each 19208 sq. gd., their altitudes being respectively, 1st 100 yd., 2nd 224 yd., 3rd $352.80 \mathrm{yd} ., 4$ th $705.60 \mathrm{yd} .$, 5th 940.80 yd .

    Ans. 1st. 192.08 yd. ; 2nd. 85.75 yd., etc.
    11. How many boards will be required to floor a room 16 yards long by 8 yards wide, if each board is 3.90 yards long by .32 yard wide?

    Ans. 102.56 boards.
    12. A side-walk 35 ft .3 in . long by 2 ft .9 in . wide is to be overlaid with a mixture of bitume and sand. What will he the cost at $\$ 2.92 \frac{1}{2}$ a square foot?
    13. There is a square whose area is 3600 yd . Ans. what is the side of a square, and the breadth of a walk along each sicle and each end o! the equare, which shall take up just one half of the whole? sins. $42.42+y d$. , side of the square ; $8.78+y \mathrm{~d}$., breadth of the walk.
    14. A piece of land in the form of a parallelogram is 264 yd . long, and its width is $1^{5}$ of its length; how many bushels of wheat will be required to sow it, if it takes $1 \frac{1}{2}$ bu. per 1000 eq. yd. ? Ans. 43.56 bu.

    ## $T_{0}$

    gle A B C D, ards, and the
    yil., time.
    altitude of a ds, and arem

    Itiplied by the qual to $112+$
    ose bauses and
    2nd A B =
    $C=147.24$
    q. $\mathrm{yd} .$, etc. hombus A B 12 feet, and
    feet, Ans.
    mbua whose vs: lst A B yd., C F = 4th D C = $=295.85$ गd. d18518.8080
    eet 6 inches, 10 sq . in. ) feet square, 1250 feet. 108 sq. gd., 24 yd., 3rd

    5 yd., etc.
    oni 16 yards by . 32 yard 6 boards. , be overlaid rst at $\$ 2.92 \frac{1}{2}$ $283.54+$. s the side of each end o! ? of the walk. 64 yd. long, theat will be 43.56 bu.
    menduration of aurpacta.

    ## Panblem 11.

    To find the area of a triangle, when the base and altitude
     are known
    585. Rute. - Mrielifhly the base by the altitude, and hulf the product will be the aren. Or, Multiply the lase by half the allitude, and the prodnct witl bo the arect.
    E.x. I. What is tie area of the triangle A B C, whose lase $A C$ is 18 yards, and altitude B E, 10 yards? Ophatios. $18 \times 10 \div 2=90$ eq. yarde, Ans.
    2. Find the area of triangles whose bases and altitudes are as fol-
     $A C=245.67 \mathrm{yd} ., B \mathrm{Bd}=1 \mathrm{C}=109.21 \mathrm{yd},. \mathrm{~B} E=75.75 \mathrm{yd} . ; 4 \mathrm{th}$
    2nd 6491.2115 sq . yd., Ans. 40 yd. Ans. 1st $2457.34 \frac{2}{\mathrm{~g}} \mathrm{sq} . \mathrm{yd}_{\mathrm{d}}$;
    3. Find the area of Ans.
    92.2 feet.
    4. The triangular gable of a certain tuilding. 3526.65 sq . ft . and an altitude of 18 leet; how many building has a lase of 50 leet, it ?
    square feet of boards will cover altitude, 248,50 a riangular form whose base is Ans. 450 kq . ft . how much did yards, was sold at the rate of 530.40 yards, and
    6. Find the it cost ? uring as follows: of a piece of land divided into Ans. $\$ 18946.88 \frac{1}{4}$. the base of the : the base of the first is 15 ' toise triangles, measis $18 \frac{9}{20}$ to., altitude $8 \frac{25}{25}$ to. Ans. 0 arp. $39.26+$ sq. 1 ml .

    ## Problem III.

    ## To find the area of a triangle when the three sides are

    known.586. Role.-I. Aidd the three sides together and take half their sum.
    II. From this hulf sum take each side separately.
    III. Multiply together the half sum and each of the three remainders, and theif extract the square root of the product, which will be the required area. Nonk. - If a triangle be equilateral, its area equals the square of the sides mul-
    aplied by the decinnal 4330122 .
    Ex. 1. Find
    Ex. 1. Find the area of a triangle whose sides are 9, 15 , and 20 yd .
    Operation. $\quad(9+16+2 \theta) \div 2=22$, half sum; $22-9=13$,
    let rem.; $22-15=7$, 2nd rem. ; $22-20=2$, 3rd rem. Then, to obtain the prod ict, we have $22 \times 13 \times 7 \times 2=4004 ; \sqrt{4004}=$ $63 . \underline{i} 71$ sq. yards, the area, Ans.
    587. How many square yar:ls of plastering are there in a triangle, whose sides are 15,20 , and 25 feet ?
    588. The sides of a triangular field are 25.69 chains; what is its area? are 49 chains, 50.25 chains, and 4. What is the area of an isosceles triangl Ans. 61.4979 acres. each of the equal sides 22.5 ?
    589. How many square yards in a triangle whose Ans. 25l.55. 10 ft .4 in ., and 15 feet? 6. How many arpents are there in a triangular fis. $4.649 \mathrm{sq} \cdot \mathrm{yd}$. 15 to. 3 ft ., $24 \frac{\mathrm{l}}{\mathrm{g}}$ to., and 36 to. 5 ft .? triangular field whose sides are
    590. There is a triangle, the longest side. 0 arp. 15.063 sq . per. shortest side 9.2 feet, and the other side of which is 15.6 feet, the contents?
    591. How niany acres in a triangle whose Ans. $46.139+$ feet. and $1147 \frac{1}{2}$ yards?
    592. What is the area of a triangular Ans. 20 A. 3 R. 4.72 per. 35 perches?
    593. Find the area of each of the following equilas. $530.44+$ per.
    ides are : lst 15 ft .8 in the following equilateral triangles whose
    c.ns. Ist $106.28+$ eq. ft. ; 2nd $18 \mathrm{ft} .10^{\prime} 8^{\prime \prime} ; 3$ rd 81 yards? aquare yards.

    ## Problem IV.

    ## To find the hypothenuse of a right-angled triangle when the base and perpendicular are known.

    587. Rule.-I. Square each of the sides separately. II. Ald the squares together.
    III. Extract the square root of the sum, which will be the hy pothenuse of the triangle.
    Nurf. - Were it to find the base of a trianglo whose area and altitude are given. divide the area by the altitude, and double the quotient, the reault will $g$ ve
    the base.
    

    Ex. 1. In the right-angled triangle $A B C$, we have, $\mathrm{A} B=20$ feet, and $\mathrm{BC}=15$ feet, to find A C.
    Operation. $20^{2}=400 ; 15^{2}=225 ; 400+$

    $$
    225=625 ; \sqrt{625}=25 \mathrm{ft} \text {. A C. }
    $$

    2. The height of a mast planted on the brink of a pond, is 144 ft ., and the breadth of the pond 84 yards; what is the length of a line which would reach from the top of the mast to the Ans. $290.24+\mathrm{fl}$.
    3. The side roofs of a house of the street? Ans. 70 feet height, form a right angle at the which the eaves are of the same on one side is $12 \frac{1}{2}$ feet, and on the. Now, the length of the rafiers of the house?
    4. What would be the width of $A n s .21 \frac{1}{2}$ feet. the ratiers on each side were $12 \frac{1}{2}$ feet? 8 . What would be the widtb, if the rafters on $12 \frac{1}{2}$ fee? Ans. 17.67 ft .
    et? feet?

    Ans 24.78 ft .

    ## Problem V.

    ## When the hypothenuse and one side of a right-angled tri-

    ## angle are known, to find the other side.

    588. Rule.-Square the hypothenuse and also the other given side, and take their difference; extract the square root of this difference, and the result will be the riquired side.
    Ex. 1. In the right-angled triangle A B C, Prob. IV, there are given $A C=25$ feet, and $\overline{\bar{A}} B=20$ feet, find the side $B C$.
    Operation. $25^{2}=625 ; 202=400 ; 625-400=225 ; \sqrt{225}$
    15 feet, Ans.
    589. The hypothenuse of a triangle is 106 feet, and the perpendicular 90 feet; what is the base?
    590. The height of a wall on the brink of a river is 50 feet, and a line of 160 feet in length will just reach from the top of it to the opposite 4. The roof 'ot a house whose side walls are Ans. 151.98 feet. forms a right angle at the top; if one are each 36 teet hagh, long. and its opposite yoke fellow, if one of the rafters be 10 leet ing, the length of the prop set upri2, what is the breadth of the buildand the part of the floor at which it to suppurt the ridge of the roof, of the building 15.6204 ft , , which it must be placed? Ans. Breadth

    ## Probiem VI.

    ## To find the area of a trapezoid.

    585. Rule.-Multiply the sum of the parallel sides by the perpendicular distance between then, and then divide the product
    

    A E
    E.x. 1. What is the area of the trapezoin A B C D, having given A B = 34 yards, D C $=26$ yards, and $\mathrm{D} \mathrm{E}=20$ yards?

    Operation. $(34+26) \times 20=1200 ; 1206$ $\div 2=600 \mathrm{sq}$. yd., Ans.
    2. Required the area of trapezoids whose perpendicular heighte and bases are: $1 \mathrm{st} H=16 \mathrm{ft}$., $B=24 \mathrm{ft}$. and 36 ft .; 2nd $\mathrm{H}=20.15$ yd., $B=34.25 \mathrm{yd}$. and 62.49 yd ; 3 rd $\mathrm{H}=36 \frac{1}{\mathrm{f}} \mathrm{ft}, \mathrm{B}=75_{10}^{7} \mathrm{ft}$. and $85 \frac{1}{5} \mathrm{ft} \cdot ; 4 \mathrm{th} \mathrm{H}=55 \frac{1}{2} \mathrm{yd} ., \mathrm{B}=106 \mathrm{j} \mathrm{yd}$. and $134 \frac{4}{20} \mathrm{yd}$. : 5 th $\mathrm{H}=70 \frac{1}{4} \mathrm{ft}, \mathrm{B}=145 \frac{3}{3} \mathrm{ft}$. and $109 \frac{1}{4} \mathrm{f}$. Ans. 1 st 480 sq . ft.; 2nd $974.6555 \mathrm{sq} . \mathrm{yd}$. ; 3 rd 2923.15 sq . ft., etc.
    3. What is the area of a trapezoid, the parallel sides of which are 12.41 and 8.22 chanss, and the perpendicular distance hetween thent 5.15 chains?

    Ans. 5 A. 1 R. 9.956 per.
    4. The parallel sides of a piece of land having the form of a trapezoid, are 248' and 1644 links, and their perpendicular distance is 1030 links: find its area. Ans. 21 A. 0 R. 39.824 per.
    5. A field in the form of a trapezoid whose parallel sides are 75.28 and 60.72 yards, and the perpendicular distance 46 yards, was sold for $\$ 18768$; what shall be the cost of another field of the same kind having a rectangular form, whoee base is 115 yards, and altitude 75 yards?

    Ans. $\$ 51750$.

    ## Problem Vil.

    ## To find the area of a quadrilateral.

    550. Measure the four sides of the quadrilateral, and also one of the diagonals: the quadrilateral will thus be divided into two triangles, in both of which all the sides will be known. Then, find the areas of the triangles separately, and their sum will be the area of the quadrilateral.

    Or again,
    Let fall on the diagonal two perpendiculars drawn from the vertex of the opposite angles; multiply the sum of those perpendiculars by the diagonal, half of the product will be the area.
    

    Ex. 1. Suppose that in the quadrilateral A B C D, the diagonal A C $=88$, the perpendicular $\mathrm{D} \mathrm{E}=27$, and $B F=25$; what is the area?

    Operation. $\quad 27+25=52 ; 62 \times 88$ $\div 2=2288$, Ans.
    2. In the quadrilateral $A B C D$, the side $A B=12$ leet, the side $B C=$ 15 f ., the side $\mathrm{C} D=10 \mathrm{ft}$., the side
    $A D=18 \mathrm{f}$., and the diagonal $\mathrm{A} C=22 \mathrm{ft}$; what is the area?
    Ans. 174.02 sq. ft., 3. What is the area of a quadrilateral whose diagonal is 40.25 feet, and the 2 perpendiculars 12.25 , and $15.05 \mathrm{ft} . ? A .549 .4125 \mathrm{sq}$. ft.
    4. Required the area of a quadrilateral whose diagonal is 108 feet 6 inches, and the perpendiculars 56 feet 3 inches and 60 feet 9 inches.
    5. Find the area of each of the following quadrilaterals: lst diag. onal, 65, perpendiculars, 28 and $33 \frac{1}{2}$; 2nd perpendiculars, 18 and 16, diagonal, 42 ; 3rd diagonal, 100 , perpendiculars, 35 and 30 .

    Ans. let 1998.75 ; 2nd 714; etc.
    6. In the quadrilateral A B C D, A B $=40$ yards, D C $=36$ yd., $B F=34 y d ., D E=35.10 \mathrm{yd}$.; also, $\mathrm{F} E=8 \mathrm{yd}$. ; find the area of the quadrilateral.
    7. Suppose that in the quadrilateral A B CD D , on account of some obstacle, we conld measure only A B, D C, B F, D E, and F E, which measure respectively $25,22,20,21$, and 7 yards; what is the area of the quadrilateral?

    Ans. 585.275 sq. yards.

    ## Problem Viif.

    ## To find the area of a regular polygon.

    591. Multiply the perimeter of the figure by half the perpendicular let fall from the centre on one of the sides, and the product will be the area. Or,

    Square the side of the polygon, then multiply the square so found, by the tabular area set opposite the polygon of the same number of sides, and the product will be the area.

    The following Talle shows the areav of regular polygons of any number of sides, from three to twelve, the side of each being unity, or 1; It also shows the length of the radius of the inseribed circle.

    | Number of sides. | Names. | Areas. . | Radius of inscribed circle. |
    | :---: | :---: | :---: | :---: |
    | 3 | Triangle. | 0.4330127 | 0.28806751 |
    | 4 | Square . | 1.0000000 | 0.5000000 |
    | 5 | Pentagon. | 1.7204774 | 0.6881910 |
    | 6 | Hexagon | 2.5980762 | 0.86602 .54 |
    | 7 | Heptagron.. | :3.6339124 | 1.0382617 |
    | 8 9 | Octagon. Nunaron | 4.8284271 | 1.2071068 |
    | 9 10 | Nunagon | 6.1818242 | 1.3737387 |
    | 11 | Uecagon. | 7.6942088 9.3656404 | 1.5398418 |
    | 12 | Dodecagon. | $\begin{array}{r}9.3656404 \\ 11.1961524 \\ \hline\end{array}$ | $\begin{aligned} & 1.2028437 \\ & 1.0660254 \end{aligned}$ |

    

    A F B

    Ex. 1. Required the area of the regular pentagon A B CD E, each of whose sides A B, BC , etc., is 12 feet, and the perpendicular $0 \mathrm{~F}, 9$ feet.

    Operation. $12 \times 5 \times \frac{9}{2}=270 \mathrm{f}$., Ans.
    2. Find the area of each of the following regular hexagons: 1st side, $=20$, perpendic ular $=15 ; 2$ nd perpendicular $=12 \frac{1}{2}$, one of the sides $=18 ; 3$ rd side, $=36$, perpendicular $=27$.

    Ans. 1st 900, 2nd 675, 3rd 2916.
    3. Required the area of each of the following regular polygons. $1^{\circ}$ of a pentagon whose side is 30 , and the perpendicular, 24 feet; $2^{\circ}$ of a heptagon whose side is 16 , and the perpendicular, $12 \frac{1}{4}$ feet; 3 rd of an octagon whose perpendicular is 20 , and each side, 22 feet.
    4. What is the area of the following regnlar polygons: Ist of a hexagon whose side is 25.40 chains; 2nd of a nonagon whose side s 30.55 chains; 3rd of a dodecagon whose side is 28.30 chains?

    Ans. 1st 1676.174841 sq. ch. ; etc.
    5. How many pavements in the shape of a regular hexagon, the side of which is 3 inclies, are required to pave a room $6 \frac{1}{2}$ yards long by $4 \frac{3}{4}$ yards wide?

    Ans. $1.31+$ pavements.

    ## Problem IX.

    ## To find the area of an irregular polygon.

    599. Rule.-Divide the polygon into triangles and trapezoids; find the area of each separately according to the Prob. II and VI; the sum of these arcas will be the whole area of the polygon.
    

    Ex. 1. What is the area of the irregular polygon ABCDEFGH measuring as follows : $\mathrm{A} \ell=33 \mathrm{yd}$., $\ell n=84 \mathrm{yd} ., n p=28 \mathrm{yd}$., $p q=$ 31 yd., $q \mathrm{D}=13 \mathrm{yd}$. ; $\mathrm{Am}=41$ $\mathrm{yd} ., m o=96 \mathrm{yd} ., o \mathrm{D}=52 \mathrm{yd}$. ; $\mathrm{H} l=32 \mathrm{yd}$., $\mathrm{G} n=64 \mathrm{yd}$., $\mathrm{Fp}=$ $27 \mathrm{yd}$. . $\mathrm{Eq} q=70$ yd. ; mB $=32$ yil., $o \mathrm{C}=61 \mathrm{yd}$.?

    Operation. AlH $=33 \times 32 \div 2=528, \mathrm{H} \ln \mathrm{G}=84 \times(32$ $+64) \div 2=4032, \mathrm{G} n p \mathrm{~F}=28 \times(64+7) \div 2=1274, \mathrm{FpqE}$ $=31 \times(27+70) \div 2=1503.5, \mathrm{E} q \mathrm{D}=13 \because 70 \div 2=455$, $\mathrm{A} m \mathrm{~B}=41 \times 32 \div 2=656, \mathrm{BmoC}=96 \times(32+61) \div 2 \Rightarrow$ $4464, o \mathrm{CD}=52 \times 61 \div 2=1556$. Hence, the area of the polygon represented by A B CDEF G H $=528+4032+1274+1503.5$ $+455+656+4464+1586=14498.5$ sq. yd., or $2.995+$ acres, Arrs.
    2. Suppose the same irregular polygon $A . B C D E F G H$ to measure as tollows; $\mathrm{Am}=10 \mathrm{f}$. 3 in ., mo $=32 \mathrm{ft} .6 \mathrm{in} ., o \mathrm{D}=28 \mathrm{ft} ; \mathrm{Al}$ $=6 \mathrm{ft} .4 \mathrm{in} ., \ln =21 \mathrm{ft} .9 \mathrm{in}$., $n \mathrm{P}=12 \mathrm{ft} ., \mathrm{P} q=11 \mathrm{it} .6 \mathrm{in} ., q \mathrm{D}$ $=4 \mathrm{ft} .10 \mathrm{in} . ; \mathrm{B} m=10 \mathrm{ft} ., c o=15 \mathrm{ft} .2 \mathrm{in} . ; \mathrm{H} l=10 \mathrm{ft} .9 \mathrm{in} .$, $\mathrm{G} n=16 \mathrm{ft}$., $\mathrm{FP}=4 \mathrm{ft} .5 \mathrm{in.} \mathrm{E} q=,18 \mathrm{ft} .8 \mathrm{in} . ;$ what is its area? Ans. $1297.82+6 q . \mathrm{ft}$.

    ## promiscuous examples in rectilineal surfaces.

    1. A hall is 15 yards long, 7 yards wide, and 4 yards high; allowing 30 sq . yards for the windows, what must be paid for painting it, at the rate of 36 cts . per square yard for the walls, and 60 cts . for the ceiling ?
    2. Some paper 15 inches long and 12 inches Ans. $\$ 115.56$. quire; what will a quire of the same quaity 12 inches wide, costs 16 cts. a long and 13 inches wide? 3. The panelling of a room is 121 toises long and 3 s. $\$ .21 \frac{17}{4.5}$. what must be paid for it, knowing that the long and $\frac{3}{4}$ toises high : 18s. 4d. a sq. toise, and the painting 5 s . 3 d . carpenter's work costs 4. What is the width of the room, whose surface Ans. £11 $11 \frac{1}{3}$. ing that if it were square the same would be surface is 72 sq. yd. sd ., know-
    3. What is the area of a triangle, whose sides are Ans. 8 yd. 42 yar.is? 6. The hypothenuse of a triangle is 45 feet, and its. 276.66 yd . 25 ft . ; what is its base?
    4. How many sq. yd. in a quadrilateral figure Ans. 37.416 feet. 50 ft . and the two perpendiculars, 20 and figure, the diagonal being
    5. The walls of a room are 40 square toises in area. $122 \frac{\mathrm{sq}}{\mathrm{s}} \mathrm{s}$. yd. rolls of paper-hangings are required square toises in area; how many 32 ft . long and 18 inches wide ; and what must be paid the rolls being at $\$ 1.75$ a roll? 9. What is the surface of a sheet of Ans. 30 rolls; $\$ 52.50$. wide?
    6. The sides of three squares are 3 Ans. $\frac{1}{4} \mathrm{sq}$. yd., or $2 \frac{1}{4} \mathrm{sq}$. fu. of the side of a square which is equal to and 5 ft .; what is the length
    7. A court-yard is 15 J uis long and 6 yard Ans. $7.07+\mathrm{ft}$. paving-tiles are required to cover it, and 6 yards wide; how many long by 7 in . wide?
    8. A side-walk $6 \frac{1}{3}$ yards long and $1 \frac{1}{4}$ yards wide, is to be paved with stones, each stone has a surface of 70 square inches; what will be the cost of the whole pavement, at the rate of $\$ 18.50$ per hundred stones?
    9. What is the area of a garden in the shape of a Ans. $\$ 32.58$. length of which is 45 yd . and the breadth 2.5 yd .? 14. A square yard of a floor coste $\$ 2.80$, the .? the breadth is $5 \frac{1}{4}$ yeards; what is the leagth? 15. A ladder Íšy feet in learth stands upright Ans. $7 \frac{3}{4} 7$ yards. far must the bottom of it be drawn out from the against a wall, how the top 8 inches?
    10. What must be paid for the plastering of a wall 65.50 fi .11 in . and 5.25 yd . high, at the rate of $\$ 2.10$ tha.sq. yd.?

    ## MENSURATION OF EURFACES.

    17. What cost a piece of cloth $12 \frac{1}{2}$ yards long and $1 \frac{1}{2}$ yards wide, at the rate of $\$ 1.90$ a yard in length? Ans. $\$ 23.75$.
    18. What is the area of a trapezoid, whose diagonal is 45.10 yards long and the two perpendiculars, 15.80 and 20 yards?

    Ans. 807.29 sq. yards.
    19. A man plastered three ceilings each 7.35 yards long by 5.40 yards wide, and painted 6 doors each 2.05 yards high by 1.05 yards wide; what sum must be yet paid him, if he charges $\$ 1.22$ a sq. yard for the ceiling, and $\$ 0.36$ a sq. yard for the doors, having been paid already $\$ 22.40$ on account?
    20. Find the side of an equilateral triangle equal in area to a square whose side is 8 feet.
    21. Find the area of a piece of land comprising three trapezoids, and one triangle; the paraliel sides of the first trapezoid are 36 and 54 yards, altitude 19.50 yards; those of the second are 110 and 75 yards, altitude 126 yards; those of the third 186 and 141 yards, altitude 219 yards; the base of the triangle is 69 yards, altitude 36 yards.
    22. A field whose parallel sides are 630 and 436 yards, altitude 80 yd., is let for $\$ 200$ a yr. ; how much is it per acre? Ans. $\$ 22.70+$.
    23. A room 12 yards long by 7 yards broad was floored with boards 3 yards in length; the waste made on einploying those boards was $\frac{1}{8}$ of their gross surface, and they cost $\$ .25$ per sq. yard, gross surtace. The work was done in 12 days at $\$ 1.10$ a day, and the nails used amounted to $\$ 2.50$. Find the whole cost of the floor. Ans. $\$ 39.70$.
    24. A man wishes to plant 1815 treesatan equal distance from one another, so as to form a rectangle whose lengeh is to $i^{t s}$ breadth as 5 is to 3 ; how many trees should he plant on each line?

    Ans. 55 and 33.
    25. The $\frac{5}{8}$ of the cost of a barn gate being paid, there still remains釆 of that cost plus $\$ 23.40$ to be paid. Suppose the barn to have two gates each 3 yards in width and 5.40 yards in length; what cost the square yard?
    26. Some earth was brought and levelled upon a field whose area equals that of a regular heptagon, the side of which measures 42 yd .; what cost the work at $1 \frac{1}{2} d$. a sq. yd. ?

    Ans. £40 $1 \quad 3+$.
    27. What will be the cost of roofing a building with sheet-iron at $\$ 1.22$ a sq. yard, if the roof comprises two equal triangles whose bases are $9.40 \mathrm{yd} .$, and altitudes 6.32 yd ., and also two equal trapezoids whose parallel sides are 25.48 and 16.08 yd ., their altitudes being the same as those of the triangle?

    Ans. $\$ 392.92+$.
    28. The breadth of a field in the form of a parallelograin is to its length, as 5 is to 18 ; what are the dimensions of this field which, sowed in wheat, produced $28 \frac{2}{5}$ bushels per acre, and $345 \frac{13}{5}$ bushels in all ?
    29. An individual has a property forming a trapezoid whose parallel sides are 465 and 806 yards, altitude 550 yd . In the centre stands a square pond whose side is 45 yd . Find $1^{\circ}$ the whole area of the field; $2^{\circ}$ that of the pond; $3^{\circ}$ that of the cultivable part.

    Ans. $1^{\circ} 349525$ sq. yd. ; $2^{\circ} 2025 \mathrm{sq}$. yd.; $3^{\circ} 347500 \mathrm{sq}$. yd.
    yards wide, s. \$23.75.
    45.10 yards sq. yards. ong by 5.40 y 1.05 yarda 2 a sq. yard ig been paid
    to a square $2.15+\mathrm{ft}$. trapezoids, zoid are 36 nd are 110 36 and 141 rds, altitude $1+$ acres. altitude 80 $\$ 22.70+$. with boards hoards was $\frac{1}{8}$ oss surface. e nails used . $\$ 39.70$. ce from one oreadth as 5

    5 and 33. till remains to have two sat cost the Ans. $\$ 4$. whose area res 42 yd .; $013+$. heet-iron at whose bases trapezoids is being the $39.92+$ am is to its ield which, j13 bushels in width. ose parallel tre stands a of the field;

    10 sq. yd.
    30. The roof of a building comprises $1^{\circ}$ two equal trapezoids whose parallel sides are 22 and 8.70 yd ., ultitudes 9.25 yd ; $22^{\circ}$ two $\because q u a l$ triangles whose bases are 16.20 yd ., altitudes 7.20 yd ; also 4 hips each lieing $10.80 \mathrm{y}, 1$, long by 0.33 yd . broad, plus 1 row of slates 0.217 the gutters; the siates, which cost $\$ 9$ a thonsand, are 0.298 by $0.217 \mathrm{yd} .$, and are overlaid 0.198 yd . in their length. A slater can
    roof x sq . yd . a day roof 8 seq. yd. a day for $\$ 1.10$; each slate requires two nails at $\$ 0.15$ per lb., there being 285 nails in a pound; and 12 cents per 4 sq . yd. are paid for sundry expenses. Find the whole cost of that roof.

    Ans. $\$ 265.22 \frac{1}{2}$.

    ## Problem X.

    To find the circumference of a circle, the diameter being given. 593. Rule.-Multiply the diameter by 3.1416, and the product soill be the circumference.
    Nota.-3.1416 is the oircumference of a oircle whose diameter is 1 .
    

    Ex. 1. What is the circumference of a circle whose diameter is 18 yards?
    OpEr. $3.1416 \times 18=56.5504$ yd., Ans.
    2. Required the circumference of circles whose diameters are 1026 yd.; 2046.25 yd.; $3^{\circ} 59.75$ yd.; $4^{\circ} 67.75 \mathrm{yd}. ;{ }^{2} 46.25$
    
    3. What are the circumferences of circles ; whose radii are $10{ }^{\circ}{ }_{42.25}$ yd. $; 2^{\circ} 67.24$ yd. $; 3^{\circ} 117.70 \mathrm{yd}. ; 4^{\circ} 149.70$ yd. $; 5^{\circ} 160 \mathrm{ft} 9 \mathrm{in} .$. Ans. $1^{\circ} 265.4652 \mathrm{yd} . ; 2^{\circ}{ }^{\circ} 422.452368 \mathrm{yd} .$, etc.

    ## Problem XI.

    To find the diameter of a circle, the circumference being known.
    594. Rule.-Divide the circumference by 3.1416 , and the quotient will be the diameter.
    Ex. . What is the diameter of a circle whose circumference is
    Operation
    $25.1328 \div 3.1416=8$ yards, Ans.
    2. Required the diameters of circles whose circumferences are $1^{\circ}$ $37.70 \mathrm{yd} . ; 2^{20} 54.69 \mathrm{yd}$. $3^{\circ} 3^{\circ} 76.3 \pm \mathrm{yd} . ; 4^{4} 126.45 \mathrm{yd} . ; 5^{\circ} 206 \frac{1}{4} \mathrm{yd}$.; $3^{\circ} 24.2997+$ yd., ecc. Ans. $1^{\circ} 12.0002 \mathrm{yd} . ; 2^{\circ} 18.999 \mathrm{e}+\mathrm{yd}$. :
    3. What are thec.
     50 f. 6' $3^{\prime \prime}$ ?

    ## Prublem XII.

    To find the length of a circular arc, whe.s the number of degrees which it contains, and the radius of the circle are known.
    595. Rule.-Multiply the number of degrees by the decimal .01745 , and the product arising, by the radius of the circle.
    
    E.x. 1. Suppose the arc A B to contain 120 degrees, and the radius $A C$ be 10 teet; whas is the length of the arc?
    Oper. $01745 \times 120 \times 10=20.94$, Ans.
    2. What is the length of an arc containing $25^{\circ}$, the diameter of the circle being 15 ft . ? Ans. 3.2718 ft .
    3. Required the length of each of the following arcs: 1 -t $12^{\circ} 10^{\prime}$, diameter 20 ; 2nd $10^{\circ} 15^{\prime}$, diameter 68 ; 3rd $67^{\circ} 17^{\prime} 4+\frac{1}{2} \prime$ ", diameter 25 ; 4th $6\left(1^{\circ}\right.$. radius 14 .

    Ans. let $2.123+; 2 n d 6.0813+$, etc.
    Problem XIII.
    To find the length of the are of a circl :, the chord and radius being given.
    596. Rune.-I. Fiud the chord of half the arc.
    II. F'rom 8 times the chord of half the are, subtract the chord of the whole arc, divide the remuinder by 3, and the quotient will be the length of the arc, nearly.
    Ex. 1. If the chord A B, fig. of Prob. XII., equals 30 feet, and the radius $\mathrm{A} C$ be 20 feet ; what is the length of the arc $A D B$ ?

    Operation. First draw D C perpendicular to the chord A B ; it will bisect the chord at $P$, and the are of the chord at $D$. Then $A P$ $=15$ feet. Hence, ${\overline{\mathrm{AC}^{2}}}^{2}-{\overline{\mathrm{AP}^{2}}}^{2}=\overline{\mathrm{CP}^{2}}$, that is, $400-225=175$ and $\sqrt{175}=13.228=-\mathrm{CP}$.

    Then D C - CP $==20-13.228=6.772==$ D P.
    Again, $\mathrm{AD}=\sqrt{\mathrm{AP}^{2}+\mathrm{PD}^{2}}=\sqrt{225+45.859984 .}$
    Hence, $A D=16.457=$ chord of the half arc.
    $16.457 \times 8-30$
    Then, $-3=33.885==\operatorname{arc}$ A D B, Ans.
    2. If the chord A D of half the are A B D, fig. of Prob. XII, be 30 feet. and the chond A B of the whole arc, 50 feet; what is the length of the arc ?

    Ans. $63 \frac{1}{2}$ feet.
    3. The chord of an arc is 12 feet, and the chord of half the arc is 7 ; what is the length of the arc? Ans. 14 feet.
    4. The chord A B of the whole are, fig. of Prob. XII, equals 48.74 , and the chord A D of half the are equals 30.25 ; what is the length of the are?

    Ans. 64.42.

    ## Problem XIV.

    To find the area of a circle, the diameter, or the circumference, or both, being given.
    557. Rule.-Multiply the square of the dimmeter by .7854. Or,

    Multiply the square of the circumference by $\cdot 07958$. Or,
    Multiply the circumference by half the radius and the product will be the area.

    Ex. 1. What is the area of a circle whose diameter is 12 yards?
    Operation. $.7854 \times 12^{2}=.7854 \times 144=113.0976 \mathrm{sq} . \mathrm{yd}$., Ans.
    2. Find the area of a circle whose circumference is 12 yards.

    OPER. $.07958 \times 12^{2}=.07958 \times 144=11.459 \mathrm{l}$ sq. yd., Ans.
    3. Required the area of a circle whose circumference is 37.70 yd ., and the radius 6 yards.
    Operation. $37.70 \times \frac{6}{2}=113.10 \mathrm{sq} . \mathrm{yd}$. , Ans.
    4. Required the areas of the circles whose circumferences are $1^{0}$ 10.75 yd.; $2^{0} 5.4978$ yd.; $3^{0} 3 \frac{1}{2}$ miles; $4^{0} 35 \frac{1}{2}$ toises; $5^{\circ} 25 \frac{1}{4}$ yd.; $6^{0} 4 \frac{1}{6}$ miles. Ans. $1^{0} 91.9646$ sq. yd. ; $2^{0} 2.405+$ sq. yd.; $3^{0} .9748$ sq. mi. ; $4^{0} 100.2906+$ sq. to., etc.
    5. Find the areas of the circles whose dianeters are $1^{\circ} 7 \mathrm{yd}$.; $2^{0}$ 13.27 yd . ; $3^{0} 24 \mathrm{f} .7 \mathrm{in} . ; 4^{\circ} 40 \frac{1}{\mathrm{~d}} \mathrm{yd}$. ; $5^{\circ} 180.40 \mathrm{yd}$. Ans. $1^{0} 38.4846$ sq. yd.; $2^{0} 138.3033$ sq. yd. ; $3^{0} 474.6488$ sq. f., etc.
    6. What are the areas of the circles whose dimensions are as fol lowe: $1^{\circ}$ circumf. 21.9912 yd., radius 31 ; $2^{0}$ diameter 15 , circumf. $47.124 ; 3^{\circ}$ radius 25 , circumf. 157.08; $4^{0}$ circumf. 32.9868, diameter $10 \frac{1}{2} ; 5^{50}$ radius 16 , circunf. $105.55776 ; 6^{\circ}$ circumt. 6.2832, diammeter 2 ? Ans. $1^{9} 38.4846$ sq. $y \mathrm{yd} . ; 2^{\circ} 176.715 ; 3^{\circ} 1963.50$;
    $4^{\circ} 86.59035$, etc.

    Problem XV.
    Given a circle, to find a square which shall have an equal area.
    598. Rule.-I. The diameter $\times .8862=$ side of an equis. alent square.
    II. The circumference $\times .2821=$ side of an equivalent square
    E.x. 1. The diameter of a circular field is 650 yards, what would be the side of a equare field of an equal area?
    Operation. $650 \times .8862=576.03 \mathrm{sq} . \mathrm{yd}$., Ans.
    2. The circumference of a circular fishpond is 200: what is the side of $:$ square of an equal area?
    Operition. $200 \times .2821=56.42$, Ans.
    3. Finl the sides of squares of equal areas to circles whose circum. Rerences are $1^{10} 250 \mathrm{yd}$. ; $2^{0} 300 \mathrm{yd}$; ; $3^{30} 412.50 \mathrm{yd}$. ; $4^{0} 135.75 \mathrm{yd}$.; $5^{\wedge} 40 \mathrm{f}$. 10 in . $3^{0} 116.36625 \mathrm{yd}$., etc.
    4. What are the sides of squares of cqual areas to circles whose diameters are $1^{0} 25 \mathrm{yd} . ; 2^{\circ} 30 \mathrm{ft} . ; 3^{\circ} 75.10 \mathrm{yd} . ; 4^{0} 45 \mathrm{f} .8 \mathrm{in}$.; $5^{0} 20.65 \mathrm{yd}$.? $3^{\circ} 665.5536+y d$. , etc.

    ## Problem XVI.

    Given the diameter, or the circumference, of a circle, to find the side of the inscribed square.
    595. Rule. - I.-The diameter $\times . \% 071=$ side of the inscribed square.
    II. The circumference $\times . \mathbf{2 2 5 1}=$ side of the inscribed square.
    
    E.x. 1. The diameter A B of a circle is 300 ; what is the value of AC, the side of the inscribed square?

    Operation. $300 \times .7071=212.13$, Ans.
    2. What are the sides of the inscribed squares, if the diameters of the circle are $10312 ; 2^{0} 400 ; 3^{0} 150.20 ; 4^{\circ} 225.50 \mathrm{yd}$.; $5^{0} 170 \mathrm{fl} .8 \mathrm{in}$.
    Ans. $1^{0} 320.6152 .2^{\circ} 282.84 ; 3^{\circ} 106.206+$, etc.
    $\therefore$ Required the sides of the inscribed squares of which the circumle ences of the circle are $1^{0} 718 \mathrm{yd} ; 2^{0} 180.40 \mathrm{yd} . ; 3^{0} 368.10 ; 4^{0}$
    

    ## Problem XVII.

    To find the area of a sector of a circle.
    600. Rule.-I. Find the length of the arc by Problem XII. II Multiply the arc by one half the radius, and the product will be the area.
    what would
    what is the whose circum. $135.75 \mathrm{yd} . ;$ 84.63 yd .
    circles whose , 45 fl. 8 in.; $\mathbf{6 . 5 3 6 0} \mathrm{ft}$;

    ## circle, to

    side of the ibed square of a circle is , the side of 212.13, Ans. he inscribed e circle are 225.80 yd ;$06+$, etc. the circum. 368.10 ; $4^{0}$ $08+\mathrm{yd}$;

    Ex. 1. What is the area of the sector A D B C, Proh. XII, whose arc is 95 , and the radius of the circle 20 feet?

    Operation. $95 \times{ }_{2}^{20}=950$ feet, Ans.
    2. Required the area of a sector, of which the are is $26^{\circ}$, and the radius of the circle 24 feet.
    Operation. $01745 \times 26 \times 24=10.8888$, length of the are; $10.9888 \times \frac{2.4}{\frac{2}{2}}=130.6656 \mathrm{sq} . \mathrm{n}$. , Ans.
    3. What is the area of a sector, of which the are is 79 and the radius of the circle 47 inches?
    4. Find the area of a sector whose Ans. 1856.5 sq . in. $145^{\circ} 18^{\prime}$.
    5. What is the area of a senicircle in which Ans. 792.337.
    6. What is the area of a sector of Ans, 453.8745. and the rading of the circle $12 \frac{1}{2}$ ? , which , the arc is $73^{\circ} 44^{\prime} 30^{\prime \prime}$,

    ## Problem XVIIf.

    To find the area of the segment of a circle.
    601. Rule.-I. Find, by the last Prollem, the area of the sector which has the same arc with the segment.
    II. Find the area of the triangle formed by the chord of the segment and the tico radii draiwn to its extremities.
    III. If the segment is greater than the semicircle, add the tivo ureas together; but if it is less, subtract them, and the resull in either case, will be the area required.

    Or use the following
    Rule.-I. Multiply half the radius by the difference between the arc which is the lase of the segment, and the half of the chord that would subtend an arc doubled that of the given segment.
    II. If the segment is greater than a semicircle, multiply huly the radius by the sum of the arc and of the chord that would suly. tend an arc equal to double the given arc less $360^{\circ}$, the result woill be thie area required.

    Ex. 1. Let the chord A B, in the diagram of Prob. XII, be 24 , and the radius $C A$, be 20 ; what is the area of the segment $A \stackrel{24}{\mathrm{D}} \mathrm{B}$ ?
    Operation. $\sqrt{C_{A^{2}}-A P^{2}}=\sqrt{20^{2}-12^{2}}=16$, the measure of $C P$. Also $C D-C P=P D=20-16=4$, the measure of PD. Then, $\sqrt{A P^{2}+P^{1} D^{2}}=\sqrt{12^{2}+4^{2}}=\sqrt{160^{2}}=12.64911$
    $=A D$; and finally, $\frac{\left(A \frac{1}{D}: 8\right)-24}{3}=\frac{(12.64911 \times 8)-24}{3}-$ 26.7309, the measure of the arc A D B (Prob. XIII).
    $25.7309 \times 10$, half radius, $=257.309$, area of the sector A D B C; and $A P \times C P=12 \times 16=192$, area of triangle CAB ; and the area $A D B C-$ areat $C A B=$ nrea of segment $a D B$; that is, $257.309-192=65.309$, area required. It is also obvious, that the area of the sector A D B C sultracted from that of the whole circle A D B E, will leave the area of the sectot A E B C.
    2. Required the area of a segment whose arc is 220 degrees, the radius of the circle being 20 yards.
    Oprration. The double of $220^{\circ}$ less $360^{\circ}=440^{\circ}-360^{\circ}=$ $80^{\circ}$. The aro rectiffed of $220^{\circ}=3.1416 \times 40 \times \frac{22}{2} 2=76.79 \mathrm{yd}$.
    The chord of $80^{\circ}$ isee Table of chords) $=20 \times 1.2856=25.71$ yd. $\quad 20 \times\left(\frac{76.79+25.71}{2}\right)=1025$ sq. yd., area of the segt., Ans.
    3. What is the area of the segment of a circle whose radius is 10 , and the chord of the arc 16 yards?
    Operation. The chord in the table for the arc of the segment $=$ $\left.16 \div 10=1.6 ; 1.6=106^{\circ} 20\right)^{\circ}=106.333+;(3.1416 \times 20 \times$ $106.333) \div 360=18.5586$. The chord of an arc doubled, or $\left[360^{\circ}\right.$ $\left.-\left(106^{\circ} 20^{\circ} \times 2\right)\right]=147^{\circ} 20^{\prime}=1.9193 ; 1.9193 \times 10=19.193$; $\left.\frac{10}{2} \times[18.5586-19.193 \div 2)\right]=44.81+$ sq. yd., area of the seg.
    ment, ${ }^{2}$ Ans.
    4. Find the area of a segment; the radius of the circle being 10, and the chord of the arc 12 yards. Ans. 16.326 sq . yd.
    5. What is the area of the segment whose height is 27 and the diameter of the circle 75 ?
    6. Required the area of a segment whose are is $90^{\circ}$, and the radius of the circle 6 .
    7. In a circle whose radius is 50 feet, what are Ans. $28.27+$. segments whose chords are $1^{\circ} 17 \mathrm{ft}$; $2^{\circ} 24 \mathrm{ft}_{\mathrm{c}}$; $3^{0} 45.75 \mathrm{ft}$; 10 60.20 ft ; $5^{\circ} 70 \mathrm{ft}$.? ${ }_{20}^{0} 23.3125 \mathrm{sq}$. ft. ; $3^{\circ} 170.75 \mathrm{sq}$. ft., etc.

    ## Problem XIX.

    ## To find the area of an ellipse, the two axes being given.

    602. Rule.-Multiply the two axes together, and their prod. uct by the decimal .7854 , the result will be the required area.
    E
    
    , D
    E.x. 1. What is the area of a garden in the form of an ellipse whose transverse axis A B is 40 yards, and the conjugate axis D E is $2 \bar{u}$ yards?

    > Operation. $40 \times 25 \times .7854=785.40$ sq. yd., Ans.
    2. Required the areas of the ellipses whose axes are 105 and 4 yd .; 2012.14 and $1.25 \mathrm{yd} . ; 3^{\circ} 17.15$ and $7.29 \mathrm{yd}^{2} ; 4^{0} 45.2 \mathrm{a}$ and 34.18 yd. ; $5^{\circ} 70.40$ and 45.65 yd. $2^{\circ} 69.1269 \mathrm{sq}$. yd. ; $3^{\circ} 98.1934 \mathrm{sq}$. yd., etc.
    r A D B C $B$; and the B; that is, us, that the whole circle
    degrees, the $-360^{\circ}=$ $=76.79 \mathrm{yd}$. $36=25.71$ segt., Ans. adius is 10 , $6 \times 20 \times$ d, or $\left[360^{c}\right.$ $=19.193$; of the seg.
    being 10 , 3 sq. yd.
    7 and the $32.31+$. the radius $8.27+$. reas of the 75 ft . ; 10 sq. ft. ;
    given.
    eir prodarea. garden in verse axis axis D E
    $=785.40$

    ## Problem XX.

    Given the area of an ellipse and one of its axes, to find the other axis.
    603. Rule.-Divide the given area by $\mathbf{. 7 8 5 4}$, and that quo. tient b!/ the given axis, the result will be the required axis.

    Ex. 1. The area of an ellipse is 400 square feet, and one of its axes is 25 feet; what is the length of the other axis?

    Oper. $\quad 400 \div .7854 \div 25$, or $400 \div(.7854 \times 25)=20.37+\mathrm{ft}$. , Ans.
    2. The area of an elliptical plece of land is 6 acres, and one of its axes is 40 rods; what is the lengtl of the other axis?

    $$
    \text { Ans. } 30.55+\text { rods. }
    $$

    3. What are the conjugate axes of ellipses whose area is 72.24 sq. yd., and the transverse axes are $1^{0} 24 y d . ; 2^{0} 28 \mathrm{yd} . ; 3^{0} 36 \mathrm{yd} . ;$
    

    ## Problem XXI.

    Io find the circumfereace of an ellipse, the two ares being given.

    6(1). Rule - Multiply the sum of the two axes ly 1.5708, and the product will give the circumference, nearly.
    $\boldsymbol{E x}$. 1. What is the circumference of an ellipse, the longer axis of which is 20 and the shorter 16 ?

    Operation. $\quad(20+16) \times 1.5708=56.5488$, nearly, Ans.
    2. Required the circumferences, or perimeters, of ellipses whose axes are $1^{\circ} 12$ and $10 \mathrm{yd} . ; 2^{\circ} 18$ and $15 \mathrm{yd} .: 3^{\circ} 15$ and $12 \mathrm{yd} . ; 4^{\circ}$
     $2^{0} 51.83+y d . ; 3^{0} 42.41+y d .$, etc.

    ## Problem XXII.

    To find the area of a circular ring, or of the space included between two concentric circles.
    605. Rule.-Multiply the sum of the tuen diameters biy their difiference, and the product arising, by $\mathbf{. 7 8 5 4}$ for the area of the ring. Or,

    Square the diameter of each ring, subtract the square of the less from that of the greater, and multiply the difference of the squares by the decimal.7854, the product will be the area.
    

    Ex. 1. 'the diameter A B is 20, and DEE is 12; what is the ares of the ring?

    Operation. $20+12=32$, the sum; $20-12=8$, difference; $32 \times 8 \times$ $.7854=201.0624$, area of the ring, Ans.
    2. If the diameters are 16 and 10 , what will be the area included between the circumferences?
    3. What are the areas of Ans. 122.5224. 30 yards: $2^{\circ} 36$ areas of the rings whose diameters are $1^{\circ} 24$ and $151.40 \mathrm{yd} . ; 5^{\circ} 178.90$ ft. ; $3^{30} 60.30$ and $90.50 \mathrm{yd} . ; 4^{0} 114.36$ and $2^{\circ}$ il $105.845^{\circ} 178.90$ and 290.50 ? Ans. $1^{0} 254.4696 \mathrm{sq}$. yd.; $2^{0} 1105.8432$ sq. ft. ; $3^{0} 3576.8372$ sq. yd., etc.

    ## PROMISCUOUS EXAMPLES IN CIRCULAR SURFACES.

    1. What is the area of a circular pond whose radius is 12 yards?
    2. Required the area of a Ans. $452.3904 \mathrm{sq} . \mathrm{yd}$. yards.
    3. A circular basin occupies $\frac{1}{5}$ the area of ans. 447.1279 sq . yid. a square, the side of which is 45 area of a garden in the form of basin?
    4. What is the area of the semi-circular Ans. 11.354 yd . width is $2 \frac{3}{4}$ yards?
    5. The wheels of a carriage turn 2200 times ans. 2.9697 sq . yd. miles; what is their diameter? 2200 times over the space of 5
    6. What is the diameter of a ins. 3.8165 -- ft. fourth of the area of a rectangular circtar parterre which occupies the 16 yards?
    7. Find the area of a dial whose diameter is $4 \frac{1}{2}$ feet. 11.054 yd .
    8. The diameter of the large wheels Ans. $15.9043+\mathrm{sq}$. feet. yd.; what is the distance in wheels of a locomotive engine, is 1.66 engine, if each of its wheels revolved and leagues, run over by that , $f$ each of its wheels revolved 1695875 times?

    Ans. $5024.993+$ miles, or 1674.996 leagues.
    9. Required the area of an elliptical Hower-garden whose axes are 36 and 27 yards. $A n s .763 .4088$ sq. yd. 10. What is the length of an arc of $60^{\circ}$, in a circle whose radius is
    feet? 14 feet?
    11. Required, in arpents the radius equals the mi struction of rail-ways, that radius being the curves adopted for the coll-
    12. What is whose hase is 30 and height 20 yards?
    13. What are the areas $A n s .471 .24 \mathrm{sq} . \mathrm{yd}$. lateral triangle whose areas of the circles circumscribed to $1^{\circ}$ an equi$3^{\circ}$ a pentagon whose side is $9 \mathrm{yd}. ; 2^{2}$ a square whose side is 7 yd a $;$

    1 B is 20 , he area of
    :, the sum ; $32 \times 8 \times$ e ring, $A n s$.

    зa included 22.5224 . $1^{\circ} 24$ and 114.36 and sq. yd.;

    PACES.
    2 yards? 4 sq . yd. eter is 75 sq. yi. he firm of dius of the 354 yd. ow whose sq. yd.
    space of 5 65 -- t. cupies the und height 054 yd .
    sq. feet. re, is 1.66 - by that
    eagues.
    axes are sq. yd. radius is + feet. nd whose : the con$\frac{2}{75} \mathrm{arp}$. rectangle sq. $y \mathrm{~d}$. an equiis 7 yd . de is 10
    yd. ; $5^{\circ}$ an octagon whose side is 18 yd .? Ans. $1^{\circ} 37.6099 \mathrm{sq}$. yd .; $2^{\circ} 76.9770 \mathrm{eq} . \mathrm{yd} . ; 3^{\circ} 183 . \times 54286 \mathrm{sq}$. yd., etc.
    14. The chord of an arc is 30 and its height 7 feet; what is the length of the are?
    15. What are the radii of the circles equal in Ans. $34.13+\mathrm{fl}$. axes are $1^{\circ} 26$ and 12 yd. ; 20 circles equal in area to ellipses whose 52 and 42 yd ; $5^{\circ} 62.20$ and 46.40 yd ? $2^{\circ} 13.41$ yd.; $3^{\circ} 20.12$ yd., etc.

    Ans. $1^{\circ} 8.83 \mathrm{yd}$.;
    16. What weight will a solid cast iron column securely suppor whose diameter is .12 yd . in diameter and 3.80 yd . in height, if each hundredth sq. yd. of transversal section can support 666 pounds?
    17. Required the Ans. 75323 lb . to the $49^{\circ}$ of latitude north, knowing that the value of each degree of longitude, in that latitude, is 80018.43 yards.
    18. The diameters of two concentric circles the area of the ring formed by those circles? 45 and 30 ; what is

    $$
    \text { 19. How manv rinac o in hoo in rodiwer Ans. } 883.575 .
    $$

    19. How many rings 2 inches in radius, can be drawn from a tin sheet 22 inches long by 15 inches wide?

    Ans. $20 \frac{5}{8}$.
    20. The diameter of the bottom of a basket is .46 yd ., an 1 the circumference of its top is 2.262 yd .; what difference is there between the area of the lower base and that of the upper base?
    $A n s .0 .240977 \mathrm{sq} . \mathrm{yd}$.
    21. From a sinc sheet 28 inches long by 25 inches broad, how many ringe can be drawn whose diameters are $2 \frac{1}{2}$ and 31 in.? Ans. $57 \frac{1}{\%}$.
    22. The circumference of a circle is 314.16 yd .; what is the radius of a concentrio circle half the area?
    23. What is the area of the ring of a circular parterre, knowing that the exterior diameter of the parterre is 18.40 y 1. , and the breadth of the ring 80 yd . ?

    Ans. 44.233728 sq. yd.
    24. What in the side of a square equal in areat to a circle whose diameter is 4 ?

    Ans. $3.544+$.
    25. The exterior diameter of a circular pond is $15 \frac{1}{2}$ yards, the breadth of the ring ${ }^{\frac{9}{6}} \mathrm{yd}$.; required $1^{0}$ the area of the ring; $2^{\circ}$ what will be paid to have it paved in flag-stones, at the rate of $\$ 4.16$ a sq. yd.
    26. A circular garden whose diameter is 26.5 yd ., is enclosed by a grassy ring li.4 yd. broad; how many bundles of grass, euch weighing 36.64 lb ., can lie gathered from this ring, knowing that when the grass dries up, it luses 56 \% of its weight, and gives 2056 lb . of hay per acre?
    27. The radius of 2 oircular pond is 12 yd .; what must be the width of a grassy ring around the pond, that contains the same area?
    28. A triangular meadow whose sides are $5420, \begin{gathered}A n s .4 .97 \mathrm{yd} . \\ 6280, \\ 3400 \\ \mathrm{yd} .\end{gathered}$ encloses an elliptical pond whoe diameters are 195 and 348 yd . Find the worth of the hay produced lyy that meadow, if 5056 lb . are cut per acre, and sold at 4 cents per luudle of 10 lb . Ans. $\$ 38246.29+$.
    29. A man has a cistern whose diameter is 3 ft . $10 \frac{1}{5}$ in. ; its edge, whioh is $23 \frac{1}{g}$ in. broad, is to be covered with tin-plate at the cost of $\$ 2.10$ a sq. yd. Find the cost.
    30. The floor of a room cost $\$ 69.30$, at the rate of $\$ 4.50$ a sq. yd. Find the length of each of the diameters of an ellipse equal in area to that floor, if one of the diameters is $1 \frac{1}{2}$ of the other.
    31. A man gets a yard-gate made whose top is semicircular ; the square part of the gate is 4.5 yd . wile by 6.2 yd . high, and the diameter of the top part is equal to the breadth of the gate. He pays the carpenter at the rate of $\$ 9$ a sq. yd. ; the painter, 85 cts. a $\mathrm{sq} . y \mathrm{yd}$. for bronzing the outside, and 60 cts. a sq. yd. for the inside; the smith $\$ 25$ for irons. Find the whole cost.
    32. The flooring of a room cost $\$ 15$, which Ans. $\$ 399.65$. for the wood, and $\$ 0.65 \mathrm{a} \mathrm{eq}$. yd. for the work at $\$ 0.37 \mathrm{a}$ sq. yd. axes of an ellipse equal in area to that foor if the What must be the as 3 is to 5 ?
    33. How many bushels of Ans. 5.586 and 3.351 yd . can be gathered from a field of peas, reckoning $25_{7}^{4}$ bu. per arpent, of a circle whose radius is 326 area is equal to that of the segment 139.75 yd.?
    34. A inan, owning a circular piece of land Ans. $4.413+$ bu. sold the central portion of 25 perches of land containing 10 acres, he own still?
    35. The area of a field is equivalas. 6 acres 3 per. $26+\mathrm{sq}$. yd. whose radius is 380 yd . the chordent to that of the zone of a circle The field produces 3500 lb . of hay per zone are 284 and 328 yd . $11 \frac{3}{6} \mathrm{lb}$. eaoh can be gathered? 36. How many bundles of bean-stalk $A n s$. $185 \frac{4}{9}$ bundles. whose area is equal to that of a sermen were gathered from a fleld being part of a circle whose radius is 245 , he arc of which is $170^{\circ}$, $1760 \mathrm{lb}_{0}$, and the bundles weighed 131 lb yards; if each acre produced
    37. A field in the form of a sedtor 1 the radius of the circle 87.56 sector whose central angle is $86^{\circ}$, and was spent for sowing that field, knowing thated with oats. What sum oats per acre at the cost of 70 , knowing that it required 5 bushels of 38 The at the cost of 70 cts. a bushel?
    38. The area of a field is equal to that of a triangle, whose angle opposite its base, stands at the centre of a circle, the radius of which is 248 yd . This tield, being planted with vetch, produced 1840 lb . forage per acre; how many bundles, each weighing $7 \frac{1}{2} \mathrm{lb}$., were gath.
    ered $?$

    GOES.
    .50 a sq. yd. qual in area
    ircular; the d the diamHe pays the 3. a sq. yd. ; the smith $\$ 399.65$. 37 a sq. yd. must be the each other 3.351 yd . per arpent, he segment te segment $13+$ bu. g 10 acres, at part does $-\mathrm{sq} . \mathrm{yd}$. of a circle ad 328 yd. bundles of bundles. om a field ch is $170^{\circ}$, e produced bundles. s $86^{\circ}$, and What sum bushels of
    hose angle 3 of which d 1840 lb . were gath.

    ## MENSURATION OF SOLIDS.

    ## DEFINITIONS.

    606. The Mensuration of Solids is divided into two parts. 1st, The mensuration of the surfaces of solids; and 2nd, The mensuration of their solidities.
    607. A Solid is a magnitude whioh has length, breadth, and thickness.
    608. A Polyhedron is a body or solid contained by many sides or $\mathrm{p}^{\prime}$ mies.

    609 the edge of a polyhedron is the line formed by the common isursection of two adjacent faees.
    610. Polyhedrons are divided into regular and irregular polyhedrons.
    611. A Regular Polyhedron is a solid whose all faees are regular polygons equal to one an other, and whose solid angles are also equal to one an other.
    612. A solid angle is the space comprised between several planes which cut one an other at one point.
    613. An Irregular Polyhedron is a solid whose all faces are not regular polygons equal to one an other, and whose solids angles are unequal.
    

    Regular tetrahedron.
    

    Regular cotahedron.
    

    Regular ionsahedron. 614. Regular polyhedrons are five in number. Three are made of equilateral triangles; viz., the tetrahedron, the octahedron, the icosahedron; one of two squares, the hexakedron or cube; and one of pentagons, the dodecahedron.
    615. The regular Tetrahedron is a solid figure comprohended under four equilateral and equal triangles.
    616. The regular Octahedron is a solid contained by cight equilateral and equal triangles.
    617. The regular Ioceaheiros is a colid concisting of twenty
    equal and similar triangular pyramids, whose vertices meet in the eentre of a sphere supposed to circumscribe it.
    

    Regular hexahedron. Regular dodecahedron.
    618. The regular Hexahedron or cube, is a solid whose surface present 6 equal squares.
    619. The regular Dodecahedron is a solid contained under twelve equal and reg. ular permgons, or having twelve equal bases.
    690. The principaliirregular polyhedrons are the prism and the pyramid.
    691. A Prism is a figure whose bases, or ends, are any similar, equal, and parallel plane figures, and whose sides are parallelograms.
    622. A prism whose axis is perpendieular to the base, is called a right prisin.
    

    6\%8. An oblique prism is one whose axis is not perpendicular to the base.
    624. The height, or altitude of a prism, or solid, is a line drawn from its vertex, perpendicular to its base ; but in an oblique one, the altitude is the perpendicular of a rightangled triangle, whose hypothenuse is the axis.

    G®5. A triangular, quadrangular, pentagonal, hexagonal, etc., prism, is one whose base is a triangle, a quadrilateral, a pentagon, a hexagon, etc.
    626. A Parallelopipedon is a prism, whose base is a parallelogram.

    62\%. A Pyramid is a solid figure contanaed by several triangles, whose bases are all in the same plane, and which have one common vertex.
    
    Ambeva py ramid.
    
    Frustum of a pyramid cutting off the top by a plane parallel to the bise. 529. A Cylinder is a long, circular body, of uniform diam. etri, and its extremities forming equal parallel circles.
    630. A Cone is a solid body having a circle for its basc and tapering uniformly to a point called the vertex.
    
    631. The axis of the cune is the perpendicular drawn from its top to the centre of its base; as AS.

    6:3\%. The generant or side of the cone is the hypothenuse, which, by the revolution of the right-angled triangle, describes the lateral surface of the cone; as B S.
    6323. A right cone is one whose axis is perpendicular to the plane of its base, and its sides equal.
    634. An oblique or scalene cone, is one whose axis is inclined to the plane of its base, and its sides unequal.
    

    An oblique ${ }^{3}$ whose axis endicular to

    The height, of a prism, a line drawn tex, perpen$\varepsilon$ base; but of a right-
    agonal, etc., a pentagon,
    e is a parhave one
    
    
    642. A Spherical Sector is a solid generated by the revolution of a sector of a circle about one of its radii.
    643. A Spherical Segment is a portion of the sphere out of by any plane. The plane is the base of the segment; the perpendicular distance from the centre of the base to the conver surface, is the keight of the segment.
    644. A Spherical Wedge is the portion of a sphere comprehended between the halves of two great circles.
    645. A Spheroid, or Ellipsoid, is a figure produced by the revolution of a semi-ellipsis about one of its $\varepsilon$ xes, that axis remaining fixed. When it revolves about its tansverse axis, the figure is said to be prolate; and when about its conjugate axis, it is ealled oblate.

    ## Problem I.

    To find the surface or area of a prism.
    646. Rule.-Multiply the perimeter of the base by the altitude, and to the product add the area of the bases: the sum will be the surface.
    

    Ex. 1. What is the surface of a rectangular prism whove base is 3 by 4 yd., and altitude 5 yd .?

    Operation. The perimeter of the base is $(4 \times 2)+$ $(3 \times 2)=14 ; 14 \times 5=$ 70 yd., convex suriace; 70 $+(4 \times 3 \times 2)=94$ yd., Ans.
    E.x. 2. Required the entire surface of a pentagonal prism, when each side of the base is 10 feet and the height 30 .
    Operation. $10 \times 5 \times 30=1500$ so ft., convex surface; $10^{2} \times$ tabular number, or $100 \times 1.720477=172.0477$, area of one base.
    Then, convex surface $\begin{array}{lll}\text { lower base } & = & 1500 . \\ 172.0477 \\ \text { square feet. } \\ \text { " }\end{array}$
    

    ## MENGURATION OF SOLID8.

    3. What is the surface of a triangular prism, whose base is an equilateral triangle, each side of which neasures 20 inches, and its Ans. $127 \mathrm{sq} . \mathrm{ft} .58 \mathrm{sq}$. in.
    4. What is the wall-surface of a square room, whose sides are each 16 feet long and 10 feet high?
    5. A rectangular prism is 3 yd . long, 5 yd . broad, and 8 yd. high; what is $1^{\circ}$ the convex surface of the prisin: $2^{\circ}$ the whole surface of its two hases; $3^{\circ}$ the side $m_{1}$ a cube whose entire surface equals that of the prism? Ans. $10128 \mathrm{sq} . y d . ; 2^{\circ} 30 \mathrm{sq} . y d . ; 3^{\circ} 5.13 \mathrm{sq} . \mathrm{yd}$. 6. What extent of surface is an oblique prism, the ends of which are hexagonals, each side measuring 10 inches, the height of the 4, prism 20 feet, and the perimeter of a section perpendicular to the sides,
    6. Required the entire suriace ins. $93.60843+\mathrm{sq}$. ft . whose base is 15 and alticude 12 of an octagonal prism, the side of
    7. What must be paid for lining a rectans. 3612.7921 sq. ft . rate of 2 s .6 d . a yard, the inner dimenctangular box with tin, at the length, 4 tt .5 in. in breadth, and 31 ensions of the box being $5 \frac{1}{2}$ feet in ( $114 \frac{9}{4}$.

    ## Problem II.

    ## To find the solidity of a prism.

    ## 647. Rule.-Multiply the "res of the base by the perpendic. ular height, and the product will be the solidity.

    by the altihe sum will

    ## II. To find the slant height of a regular pyramid from its superficial area, and the side of its base.

    649. Rule.- From the whole area subtract the area of the base, and divide the remainder by one hulf the perimeter of the lase.

    ## III. To find the side of the base of a regular plramid from

    its superficial area and its slant height, the area of the base not being included.650. Rule.-Divide the given area by half the slant height, and that quotient again by the number of sides.
    

    Ex. 1. What is the entire area of a triangular pyramid, the slant height of which is 10 feet, and each side of the base 4 feet?

    Operation. $4 \times 3=12$, perimeter of the base; $12 \times \frac{10}{2}=60 \mathrm{sq}$. ft., area of convex surface; $4^{2} \times .4330127=6.9282$, the area of the bave; $60+6.9282=66.9282$ sq. ft., entire surface, Ans.
    E.r. 2. The area of a regular triangular pyramid is 31.732052 sq. ft., and the side of its bave 2 feet ; what is its height?

    Operation. $2^{2} \times .433013=1.732052$, area of base; and 31.732052 $-1.732052=30$, the upright area. Then $30 \div 3$, half the perimeter of the base $=10$.eet, Ans.
    $\boldsymbol{E x}$. 3. The superficial area of the sides of a regular triangular pyramid, is 30 square feet, and its height 10 feet; what is the linear measure of its sides?

    Operation. $30 \div 5=6$, and $6 \div 3=2$ feet, Ans.
    4. The slant height of a regular pentagonal pyramid is 40 feet, and each side of the base 15 feet; what is the convex surface, and also the entire surface? Ans. 1887.1074i5 sq. ft.
    5. What is the convex surface of a regular triangular pyramid, the slant height being 20 ft ., and each side of the base 5 ft . Ans. 150 ft .
    6. The area of the sides of a regular hexagonal pyramid is 360 square feet, and its slant height 36 feet ; what is the linear measure of its sides?
    7. What is the total area of a regular heptagonal Ans. 31 feet. slant height is 21 feet, and the measure of its sides 18 pyramid, whose

    Ams. 118.4263 eq. t
    8. The area of a regular heptagonal pyramid is 463.93 equare feet, and the side of its bsee 6 feet; what is ite slant height?

    ## Problem IV.

    ## To flind the surface of the frustum of a regalar pyramid.

    651. Rule.-Multiply half the sum of the perimeters of the twon lases by the slant height of the frustum. and to the product, add the area of the two ends, the result will be the entire surface.
    
    E.x. I. What is the superficial area of the frustum of a hexagonal pyramid, the slant height of which is 18 yards, the measure of the side of the larger base 6 yards, and of the smaller 4 yards?
    Operation. $6 \times 6=36$, perimeter of the base, and $4 \times 6=24$, upper perimeter. Then $(36+24) \div 2=30$, and $30 \times 18=540$ yd., 15.5884572, area of lower area of the sides. Again, $6 \times 2.5980762=$ area of upper base. Then, $540+15.5884+10.392=10.3923048$, square yards, Ans.
    652. The slant height of the frustum of a quadrangular pyramid is 16 feet, the measure of the side at the base 12 f ., and at the top 4 ft .; what is its whole surface? Ans. 672 sq. ft.
    653. What is the convex surface of the frustum of a heptagonal pyramid whose slant height is 50 feet, each side of the lower base 7 , and of the upper base 4 feet?

    Ans. 1925 sq. ft.
    Problem V.

    ## I. To find the solidity of a pyramid.

    652. Rule.-Multiply the areat of the base by one third of the height, the product will be the solidity.
    II. To find the side of a regular triangular, quadrangular, pentangular, etc., pyramid, from its solidity and height.
    653. Rule.-Divide the solidity by one third the perpendicular height and the result by the corresponding tabular number, and extract the square root of the quotient.
    III. To find the height of a regular pyramid from the side of the base, and its solidity.
    654. Rule.- Divide the solidity by the corresponding tabular number, and also by the square of the side of its buse, and multiply the result by 3 .

    Ex. 1. What is the solidity of a triangular pynamid, the beight of which is 20 feet, and each side of the bese 4 foet ?

    Operatmon. $4^{2} \times .4330127 \times{ }^{20}=46.188$ cub. ft., Ans.
    $\boldsymbol{E} \boldsymbol{x}$. 2. If the solidity of a reg. octagonad pyramid be 2133.5273088 solid feet, and its height 42 feet; what is the measure of one of its equad sides?

    Oferatron. $2433.5273088 \div{ }^{4}=173.8233792 ; 173.8233792 \div$ 4.8284272 (See Table) $=36$, and $\sqrt{36}=6 \mathrm{ft}$., side of the base required.
    E.c. 3. A regular octagonal pyramid contains 2433.5273088 solid feet, and one of its equal sides measures 6 feet ; what is its height?

    Operation. $\quad 2433.5273088 \div 4.8284272=504$, and $\left(504 \div 6{ }^{2}\right)$ $\times 3=42$ feet, Ans.
    4. Find the solidity of a regnlar pentagonal pyramid, its height being 15 feet, and each side of its base $2 \frac{1}{2}$ feet ? Ans. 53.7649 sq . ft.
    5. How many cubic yards in a criangular pyraniul, the height of which is 3.55 yards, and the three sides of its base $1.5,1.9$, and 2.6 yards?
    6. A regular pentagonal pyramid contains 45.879297 solid yarda and its sides measure 6 feet ; what is its height? Ans. 60 feet.
    7. How many solid yards are there in a pentagonal pyramid, the side of which, at the base, measures 6 feet. and its height 60 feet? dns. $45.8794+$ cu. yd.
    8. What is the measure ot one of the sides of a regular pentagonal pvramid, containing 4678.56 solid feet, and having a height of 54 feet? Ans. $12.29+$ feet.
    9. An octagonal stoue monument has a perpendicular height of 45 feet, and the linear measure of its side is 5 feet 10 inches. Also, each side of the inner cavity measures at the base 4 feet 11 inches, and its perpendicular height 41 feet. How many yaris of stone does the monument contain?

    Ans. $32.1973+$ cub. yd.

    ## Problem VI.

    ## To find the solidity of the frustum of a pyramid.

    655. Rule.-Multiply the areas of the two bases together, and extract the square root of the product. This root will be the urea of a base which is a mean between the other two. Take the sum of the areas of the three bases, and multiply it by one third of the alitude; the product will be the solidity.

    Ex. 1. If the length of a frustum of a square pyramid be 18 feet, the side of its greater base 27 inches, and that of its less 15 inches; what is the volume?

    Operation. $27 \mathrm{in} .=2.25 \mathrm{ft} .15 \mathrm{in} .=1.25 \mathrm{ft} ; 2.25^{2}=5.0625$, $1.25^{2}=1.5625 ; 5.0625 \times 1.5625=7.91015625 ; \sqrt{7.91015625}=$ $2.8125 ; 2.8125+5.9625+1.5625=9.4375 ; 9.4375 \times 18=56.625$ gub. fin 4 mis.
    2. What in the solidity of a regular pentagonal frustum, whose altitude is 8 feet, each side of the lower base 18 inches, and each side of the upper base 6 inches?
    3. What is the solidity of a frustum of pyraninia, whose height is 2 yd ., and the two ends are regular bexagons the sides of which are .70 and . 20 yd.?
    4. How many cuta Ans. $1.160484 \mathrm{cu} . y d$. the two bases being 504 and 11 a equare piece of timber, the areas of the two bases being 504 and 372 inches, and ite length $31 \frac{1}{2}$ feet? Ans. $95.44+$ cut. $\cap$.

    ## Problem Vif.

    ## I. To find the surface of a cylinder.

    656. Rule.-Multiply the circumference of the base by the altitude, and the product will be the convers surface; and to this, add the areas of the two lases, when the entire surfucce is required.

    ## II. To determine the area of surface in a cylindrical ing.

    657. Rule.-T'o the thickness of the ring add the inner diameter, and multiply the won by the thickness of the ring, and that jroduct by 9.8696 .
    

    ## id.

    together, ll be the ake the ne third
    $10^{2} \times .7854=78.54$, area of the base. $=911.064$ sq. ft., Ans.
    Ex. 2. The thickness of a cylindrical ring is 2 inches, and its inner diameter 6 inches; what is its area?
    Operation. $(2+6) \times 2=16$, and $16 \times 9.8696=157.9136$ square inches, Ans.
    3. Required the convex surface of a cylinder 13 feet long, the circumference of whose base is 57 inches. Ans. $61 \frac{3}{4} \mathrm{sq}$. ft .
    4. The radius of the base of a cylinder is .35 yd ., the height is twice the diameter of the base ; what is the whole surface of the cylinder ?
    5. Required the area of a ring 3 inches in Ans. 3.84846 sq . yd. diameter 8 inches.
    6. What is the concave surface of a semicirs. 325.6968 sq . in. eter is 15 feet, and length 60 foet? a semi-circular arch, whose diam. Ans. 1413.72 sq . $\mathrm{\Omega}$.
    7. How much nust be paid tor the painting of the wall and ceiling of a o ranlar room, whose diameter is 30 und height 15 feet, at $\$ 2.50$ a eq. $y d$.?

    Ans. \$589.05.

    ## Problem VIII.

    ## I. To find the solidity of a cylinder.

    658. Rulas.-Mnltiply the area of the base by the altitude, and the moduct will ber the solidity.

    ## II To find the solidity of a circular ring.

    65\%. Rule.-Add the inner diameter to the thicleness of the ring, and multiply the sum by the square of the thickness, and this product by 2.4674 , the result will be the required solidity.
    E.x. 1. If a cylinder measure 8 feet in diameter at its base, and 18 feet in length; how many solid feet does it contain?

    Operition. $8^{2} \times .7854=50.2656$, area of the base. Then, $50.2656 \times 18=904.7808$ cul. ft., Ans.

    Ex. 2. If the thickness of a cylindrical ring is 2 inches, and ita diameter 6 inches, what is its solidity?

    Oper. $(6+2) \times 2^{2}=32 ; 32 \times 2.4674=78.9568$ solid in., Ans.
    3. What is the capacity of a circular basin, the radius of whose base is 5 yards, and altitude 2 yards? Ans. 157.08 cub. yd.
    4. What is the solidity of a cylinder whose base equals 2.15 sq . yd., and altitude 1.46 yd ?
    5. What is the solidity of a circular ring, 4 inches in thickness and 18 inches in diameter? $\quad$ Ans. 868.5248 cub. in. 6. A cast-iron rod is $1 \frac{1}{2}$ inches in diameter, and 15 feet in length; what is its solidity in cubic inches? Ans. 318.087 cub. in.
    7. Required the solidity of a cylinder whose altitule is 1.50 yd. , and the circumference of whose base 2.08 yd . Ans. 1.132391 cub. yd. 8. The area of the base of a cylinder is 4 sq . yd., and the perpendicular distance between the two bases is 8 yards ; what is its solidity?

    ## Problem IX.

    ## I. To find the entire surface of a cone.

    660. Rule.-Mulliply the perimeter or the circumference of the base by half of the slunt height, und to the product add the areu of the buse.

    ## II. To find the height or diameter of a cone, one of them and its solidity being given.

    681. Rule. - Divide the solidity by .7854; then, if the diameter be required, by one third the iltitude also, and extract the square root of the quolieut; but if the Altitude be required, by the square of the diameter, and multiply the quotient by 3.
    
    E.x. 1. What is the entire surface of the cone whose virtex is C , the radius AB of its lifse being of feet, and the side CA, 40 feet?

    Oper "no. $3.1416 \times(5 \times 2)=31.416$, circumf. $i$ base. $31.416 \times 40=628.32$, convex surface; $10^{0^{2}} \times .7855^{2}=78.54$; $628.32+78.54=706.86 \mathrm{Nq} . \mathrm{ft} ., \bar{A} n \mathrm{n}$.

    E:c. $\mathbf{2}$. What is the diameter of the base of a cone, if its solidity be 24 feet, and its altitude 12 feet?

    Opkration. $\sqrt{\left(24 \div .7854 \div \frac{y^{2}}{3}\right)}=2.764$ feet, nearly, Ans.
    Ex. 3. If the solidity of a cone be 36 feet, and its diameter at the base 3 feet; what is its altitude?
    Oper. $\quad 36 \div .7854 \div 3^{2}=5.0929 ; 5.0929 \times 3=15.278$ f., Ans.
    4. Required the entire surface of a cone whose side is 36 and the diameter of its base 18 feet.
    5. If the solidity of a cone be 72 feet, and itas. 1272.348 eq . ft . is its diameter?
    6. The circumference of the base of a cone Ans. $3.027+$ feet. height is 20.75 ; what is the entire surface?
    7. What will it cost to tin a circular steeple, the Ans. $105.744+$ 16 feet in diameter, and the slant heirgt 48 fie, the base of which is yard?
    8. Find the convex surface of a cone, whose slans. $\$ 10053,+$. and the circumference at its base 12 feet. and the circumference at its hase 12 feet.
    9. If the solidity of a cone be 3684 feet, and its diameter 30 feet : what is its altitude?

    Ans. $15.635+$ feet.

    ## Problem X.

    ## To find the solidity of a cone.

    662. RuLe. - Multiply the area of the base by the altitucle; and divide the product by 3 , the quotient will be the solidity.
    $\boldsymbol{E x}$. I. What is the solidity of a cone, the diameter of whose base is 4 feet, and altitude 5 feet?

    Operation. $4^{2} \times .7854=12.5664$ square feet, area of the base; $(12.5664 \times 5) \div 3=20.944$ cub. ft., Ans.

    Ex. 2. What is the solidity of a cone whose side is 2.5 yards, and the radius of its base 1.5 yarids?

    Find first the altitude of the couc. The altitude, radius, and side of the eone, form a right-angled triangle whose hypothenuse is the side of the cone; let $k$ be tho altitude, we have
    $h^{2}=2.50^{2}-1.50^{2}=6.25-2.25=4 \mathrm{yd} . ;$ hence, $h=\sqrt{4}=$ $2 \mathrm{yd} . \quad 3.1416 \times 1.6^{2}=7.0686 \mathrm{sq}$. yd., area of the base; $7.0686 \times$ $2=4.7124$ cub. yd., Ans.
    3. The circumference of the base of a cone is 40 ft ., and the altitude 60 ft . ; what is its solidity?
    4. What is the solidity of a circularpyrans. 2546.56 cub . ft. at the base measures 4 ft ., and its height 18 fid, the diameter of which
    5. What is the solidity of area of the base 3.40 sq . yd .?
    6. Required the Ans. 1.530 cub. yd. the circumference of its base a cone whose altitude is 1.23 yd ., and 7. What is the solidity of a cone yd. Ans. 0.127913 cub . yd. alcitude 4 yards? Ans. 37.6992 cub. yd.

    ## Problem XI.

    ## To find the surface of the frustum of a cone.

    663. Rule - Add together the circumfernaces of the two bases; and multiply the sum by half the slunt height of the frustum; the product will be the convex suiface, to which add the areas of the bases, when the entire surface is required.
    
    $E x$. 1. What is the entire surface of the frustum of a cone, the slant height of which is 10 feet, and the circumferences of the bases 8 and 6 feet?

    Operation. $(8+6) \times \frac{10}{2}=70 \mathrm{sq}$. ft., convex surface ; $8^{2} \times .07958^{2}=5.09312$, lower base, $6^{2} \times .07958=2.86488$, upper base ; 70 $+5.09312+2.86488=77.958 \mathrm{sq}$. ft., entire surface, Ans.
    2. What is the convex susface of the frustum of a cone, the side being .7 yd ., and the radii of the bases .3 and .95 yd .?
    3. What is the concave surface of a tub whose diameter of the bottom is 2.10 yd ., that of the top 2.30 yd ., and slant height 3.84 yd .?

    Ans. $26.5402 \mathrm{sq} . \mathrm{y}$ d.
    4. There is a frustum of a cone, whose slant height is 12 feet, the circumference of the base 18 feet, and that of the upper end 9 feet; what is its whole surface? Ans. $1 y 4 . z 2+$ eq. ft .

    To find the solidity of the frustum of a cone.
    664. RuLe.-find the sum of the areas of the two ends, and
    of a geometrical mean betureen them; multiply the same by one third the altitude, and the product will be the solidity.
    $\boldsymbol{E x}$. 1. If the diameters of the two bases of the frustum of a cone be 24 and 20 feet, and the altitude 30 feet; what is its solidity?
    Operation. $24^{2} \times .7854=452.39$, area of the lower base; and $20^{2} \times .7854=314.16$, area of upper base ; and $\sqrt{15239 \times 314.16}$ $=376.99$, the geometrical mean; then, ( $452.39+314.16+376.99$ ) $\times \frac{30}{3}=11435.4$ cub. ft., Ans.
    2. What is the soii lity of the frustum of a cone, the altitude being .90 yd ,, the area of the lower base 2.25 sq. yd., and of the upper 1.21 sq. yd.?
    3. How many cubic feet in the fructum Ans. 1.533 cub yd. 28 feet, and the diameters of the bwes 22 a cone, whose altitinde is
    d Perird 18 feet?
    4. Required the solidity of the frustum of a cone, the altitude being 6.75 yd ., the circumference of the lower base 1.445 yd ., and of the upper .628 yd . Ans. .6106975 + cub. yd.
    5. What is the height of the frustum of a cone, the convex surface of which is 84 sq . ft., kuowing that the area of the upper base is 3 sq . ft., and of the lower base 12 sq . ft. ? Ans. 12 feet.

    ## Probaem XIII.

    ## I. To find the area of a wedge.

    665. Rule.- Find the area of the head, which is a parallelogram, of the two sides, which are parallelograms, and of the two ends, which are triangles; the sum of these several areas will be the required area.

    ## II. To find the area of a prismoid or frustum of a wedge.

    666. Rule.-Find the area of each of the sides und ends of the prismoid, separately; the amount of these several areas will be the area required.
    $\boldsymbol{E} x$. 1. The back of a wedge is 10 inches long and 2 broad, and each face 12 inshes long; what is its area?
    Oprration. $10 \times 2=20 \mathrm{sq}$. in., area of the head, and $12 \times 10$ $\times 2=240 \mathrm{sq}$. in., area of the two sides; $\sqrt{12^{2}-1^{2}}=11.96$, nearly, the perpendicular distance from the head of the wedge to the central point of its thickness or head: and $11.96 \times 2=23.92$, area of the two ends. Then $20+240+23.92=283.92 \mathrm{sq}$. in., Ans.
    $\boldsymbol{E} \boldsymbol{x}$. 2. The length and breadth of the tase of a prismoid are 10 and 2 inches, the length and breadth of the section cut off are 10 and 1 inches, and the length from the base to the upper section 10 in .; what is the area?

    > Oprramon. $10 \times 2=20 \mathrm{uq}$ in., area of the base; $10 \times 1=$

    10 sq . in., area of the section cut off; and $10 \times 10 \times 2=200 \mathrm{sq}$. in., area of both faces. Then $\frac{2-1}{2}=.5$ in., one half the differ. between the thickness of the base and the section cut off; and $\sqrt{10^{2}-.5^{2}}=$ 9.98 in ., the perpendicular distance between the base and upper section; and $(2+1) \times 9.98=29.94$ sq. in., area of the two ends. Then $20+10+200+29.94=259.94$ sq. in., Ans.
    3. The back of a wedge is 8 in . long and 4 in . broad, and each face 18 in . long; what is the area in sq. fl.? Ans. $2.7191+\mathrm{sq} . \mathrm{ft}$.
    4. The length and breadth of the back of a wedge are 10 and 4 in., the length and breadth of the upper section 5 and 2 in., and the length of each face 20 in .; what is the whole surf. ? Ans. $3.26+\mathrm{sq}$. ft.
    5. The perpendicular height of a wedge is 20 inches, the thickness of the head 3 inches, and its length 5 inches; what is its entire area?

    Ans. 274.85 sq. in.

    ## Problem XIV.

    ## I. To find the solidity of a wedge.

    657. Rule.-Multiply the sum of tuice the length of the base and the length of the edge by the breadth of the base, and that product by one sixth the height of the wedge, the result will be the solidity.

    ## II. To find the solidity of a prismoid or frustum of a wedge.

    668. Rule.-Multiply the sum of the areas of the two ends, and of four times the area of a section purallel to, and equally distant from, the two ends, by $\frac{1}{6}$ the height of a prismoid.
    $\boldsymbol{E} x$. 1. The length of the base of a wedge is 36 inches, its breadth 12 inches, the length of the edge 60 inches, and its height 18 inches; what is its solidity?

    Operation. $(36 \times 2+60) \times 12 \times 3=4752$ solid inches, or 2.75 solid feet, Ans.
    E.x. 2. The dimensions of a rectangular prismoid are as follows: length and breadth of the base 10 and 6 inches; of the face parallel to the base 6 and 4 inches; and the perpendicular height 40 inches. What is its solidity?

    Operation. $10 \times 6=60 \mathrm{sq}$. in., area of the base; $6 \times 4=24$ sq. in. of opposite section. Then $(10+6) \div 2=8$, the length of the central section, and $(6+4) \div 2=5$, the breadth of the central section. Then $(8 \times 5) \times 4=160 \mathrm{sq}$. in., or four times the area of the central section; $60+24+160=244$, and $244 \times \frac{40}{6}=1626+$ solid inches, Ans.
    3. What is the solidity of a stone pillar, the base measuring 3 tt . by 2 ft .6 in. ; the top 2 ft . by 1 foot 6 inches; and the perpendicular height being 8 feet?

    200 sq. in., r. between $-.5^{2}=$ upper secnds. Then
    each face + eq. ft. and 4 in., the length $+\varepsilon q$. ft. thickness tire area? ; sq. in.
    f the base and that sill be the
    l wedge. wo ends, lequally s breadth 3 inches; aches, or follows: parallel 0 inches.
    $4=24$ length of e central e area of $=1686+$
    g 3 fl. by ndicular 1b. in.
    4. If the length of the base of a wedge be 24 inches, its breadth $i$ inches, its edge 32 inches, and its height 33 inches; what is its solidity?

    Ans. 3080 cub. inches.

    ## Problem XV.

    ## I. To find the surface of a sphere or globe.

    669. Rule.-Find the arca of a circle of the same diameter as the sphere, and multiply the same by 4. Or,

    Multiply the diameter by the circumf creuce of the sphere, the product will l,e the surface.
    II. To find the diameter of a sphere from its surface.
    670. Rule.-Divide one fourth the area by .7854, and extract the square root of the quotient.
    III. To find the surface of a spheroid or ellipsoid.
    671. Rule.-Multiply lhe prodict of the two diameters by .7854 , and that product by 4 , the result will be the surface.
    IV. To find the convex surface of a segment or zone of a sphere.
    672. Rule.-Multiply the circumference of the sphere $c_{0}^{*}$ which the segment or zone forms a part, by the height of the segment or zone.
    
    $\boldsymbol{E x}$. 1. What is the surface of a globe 50 inches in diameter?

    Operation. The surface of a great circle is $.7854 \times 50^{2}=1963.50 \mathrm{sq} . \mathrm{in}$. Hence, the surface of the globe is $1963.5 \times 4=$ 7854 sq. inches, Ans. Or, $50 \times 3.1416=$ 157.08, the circumference of a great circle ; $157.08 \times 50=7854$ sq. in., surface of the globe, Ans.
    Ex. 2. If the area of the surface of a sphere be 24 square feet; what is its diameter?

    Operation. $(24 \div 4) \div .7854=7.6394$, and $\sqrt{7.6394}=2.76$ feet, Ans.

    Ex. 3. If the longer diameter of an ellipsoid be 6 feet, and the shorter 5 feet; what is its surface?

    Operation. $(6 \times 5) \times .7854=23.562 ; 23.562 \times 4=94.248$ eq. ft., Ans.

    Ex. 4. If the diameter of a sphere be 50 inches, what is the convex surface of a segment of the same 10 inches high?

    Operation. $50 \times 3.1416=157.08$, circumference of the circle, and $157.08 \times 10=1570.8 \mathrm{sq}$. in., area required, Ans.
    5. What is the surface of a sphere, the circumference of whose great circle is 4.84 yd . ?
    6. The diameter of a sphere is 21 inches; what is the surface of a zone whose height is $4 \frac{1}{2}$ inches? Ans. 296.8812 sq. in.
    7. If the surface of a sphere be 6.16 square yards, what is its diameter?
    8. The longer diameter of an ellipsoid is 18 feet, and the shorter 15 feet; what is its surface?
    9. Required the surface of the seginent of a sphere, comprised between two parallel plans at a distance of 1.25 yd . from each other, the radius of the sphere being 3.50 yd .

    Ans. $27.489 \mathrm{sq} . \mathrm{yd}$.
    10. The radius of a sphere is 3.08 yd . ; required $1^{\circ}$ the circumfer. ence of a great circle; $2^{\circ}$ the surface of that sphere.
    ${ }^{\prime}$ Ans. $1^{\circ} 19.352$ yd. ; $2^{\circ} 119.2098 \mathrm{sq}$. yd.
    11. The area of a zone is 2.85 sq . yd.; required the entire surface of the sphere, the height of the zone being .45 yd .?

    Ans. $12.742 \mathrm{sq} . \mathrm{yd}$.
    12. Required in miles the surface of the two frigid zones, allowing 327.15657 miles for the height of each of them, and 3955.82936 miles for the radius of the sphere.
    Nota.-To find the surfaces of irregular solids, or bodies, the following process is followed:-If the solids are composed of plane faces, find the area of ench face, and add them together for the tohole surface of the solid, if compoied of circular faces, divide these into a number of faces infinitely. great, so th"t sach might bn considered a plane. Then procsed as above to obtain the entirc surfuce.

    ## Problem XVI.

    ## I. To find the solidity of a sphere.

    673. Rule. - Multiply the surfuce by one third of the radius, anl the product will be the solidity. Or,

    Multiply the cube of the diameter by the decimal $\mathbf{5 2 3 6}$, and the product will be the solidity.

    ## II. To find the diameter of a sphere from its solidity.

    674 . Rule. - Divide the solidity by .5236, and m. 4 ...ce the cube root of the quotient.
    III. To find the solidity of a spheroid or ellipeoid.
    675. Rule.-Multiply the longer axis by the square of the shorter one, and the product by the decimal .5236. the result will be the required solidity.
    IV. To find the solidity of the segment of a sphere.
    

    6\%6. Rule.-1. From three times the di:meter of the sphere, deduct twoice the height of the segment ; multiply the remuin. der by the smure of the height, am that prorluct by .5236 ; the last product will be the
    solidity.

    6才7. Role.-2. To three times the square of the radius of the segment's brase, add the square of its heig't ; multiply this sum by the height, and the prodnct by .5236 ; the last result will be the solidity.

    ## V. To find the solidity of a por of a sphere.

    6\%8. Rule.-1. To the sum of the squares nf the radiio, the tron ends. add one third the square of the distince vetween them, (that is, of the height of the zone, multiply the result by the hifight of the zone, and again by 1.5708, and the lust result wül be ithr solicity.
    679. Rule.-2. For the middle zone of a sphere: From the squarr of the diameter of the sphere of which the zone is a part, suluiruct one third the square of its height, and multiply the remainuter by the height, a od also by .7854.

    ## VI. To find the solidity of a spherical sector.

    680. Rule.-Multiply the spherical surfuce by one third the radius of the sphere.

    Ex. 1. If the diameter of a globe be 12 inches, how many solid inclies does it contain?

    Operation. $\quad 3.1416 \times 12=37.6992$, circumfe nee of the giote; $37.6992 \times 12=452.3904 ; 452.3904 \times \frac{8}{3}=904 . .808$ cnb. m .: or $12^{8} \times .6236=904.7808$ cub. in., Ais.
    Ex. 2. What is the diametor of a sphere containing 6856 solid f. ? Operation. $\sqrt[8]{6856 \div .5236}=23.54+$ feet, Ans.
    Ex. 3. If the longer axis of an ellipocid be 3 leet, and the shorter one 2 fees; what is its solidity?
    Operation, $\left(2^{2} \times 3\right) \times .5236=6.2836 \mathrm{cub}$. f., Ans.
    Ex. 4. If the dianieter of a sphere be 30 feet, what is the soludity of a segment of the same, the height of which is 5 feet?

    Operation. By Rule 1; (20×3)-10=50; $50 \times 5^{2}=1250$; $1250 \times .5236=654.0$ cub. t., Ans.
    E.x. 5. What 18 the solidity of the temperate zone, the upper radtus being 1586.57232526 miles; the lower ratius 3648.56461068 miles; and the height 2062.2655 miles ?
    Oper. [(1586.57282526)2 $+(3648.867505: 38)^{2}+1(205 \pm .2656 ;)^{8}$ $\times 2062.2655 \times 1.5708=55877778668$ cubic miles, $A$ ins.
    Exe. 6. The diameter of a sphere is 15 feet. What in the solidity of a sector of the same, the circular bsse of which is 1 f feet distant from the central section?

    Opeiation. $15 \times 3.1416 \times 6=282.744 \times 1$.ft, the convex anirface of the sector. Then $15-2=7 \frac{1}{3}$, radius of the circle : 282.744 $\times\left(7 \frac{1}{2}-3=2 \frac{1}{2}\right)=706.86$ cub. ft., Ans.
    7 . Reterired the diameter of a cannon-ball weighing 80 lth . knuwing that atentis foct of cet-iron weighe $450 \frac{1}{2} \mathrm{lb}$.

    Ans. 0.6973 f .
    8. If hio diancter of the base of the segmentof a sphere be 30 feet, and the heght if the same 5 feet ; what is its solidity?

    Ans. 1832.6 cub. ft.
    9. Whas is itie solidity of a sector of a sphere $2 f$ leet in diameter, the eirenlar fase of which is 4 feet distant from the central section? Ans. 1804.5616 cub . ft.
    10. The surface of a sphere is 55.44 square yards: what is its solidity?
    11. What is the solid content of a spheroid, the longer axis of which is 16 feet, and the shorter 12 feet?
    12. What is the solidity of the torrid zone, the diameter of the earth being 7957.75 miles, and the height of the zone 8173.14565052 miles?

    Ans. 149455081137 cub. miles.
    13. The diameter of a sphere is 24 feet, what is its solid contents? Ans. 7238.2464 cub. ft.
    14. What is the solidity of a spherical segment whose height is 2 feet, and the diameter of the sphere 10 feet? Ans. 54.4544 cub. ft.
    15. Required the solidity of the middle zone of a sphere, the top and bottom diameters being each 4 feet, and its height 6 feet?

    Ans. 188.496 cub. $\boldsymbol{\Lambda}$.
    16. The height of a spherical segment is 8 inches, and the radius of its base 14 in . : what is its solulity? Ans. 2731.0976 cub. in.
    17. If the solidity of a sphere be 4.62 cub. yd,, what is 10 its diameter; $2^{\circ}$ the circumference of its great circle; $3^{\circ}$ ite whole surface?
    18. Required the volume of a epherical sector, the circular base of which is . 25 yd . distant from tise central section, and the diameter of the ephere 84 yd.

    Ans. 2.216712 cub. yd.
    19. The height of a spherical segment is .42 yd ., ite sarface 1.6632 sq. yd.; what is $1^{\circ}$ the redius of the sphere; $2^{\circ}{ }^{\circ}$ th s. lidity of the spherical sector?

    Ane. $1^{0} .63 \mathrm{yd} . ; 2^{\circ} .33^{\prime 2}$ cub. yd.
     the less 20 seet, n :us the height tetween them i.. fr...

    An $\quad \pi i$
    Problem XVII.
    To find the solidity of any regular foighendon. thive the radius of the inscribed sphere, and the product witl be the eolidity.

    This rule is evident from the fact, that any regular polyhedron might be divided into as many regular pyramids as it has bases, having their vertices in the centre of the inscribed sphere. Sote--To tind the solidity of any irregular body, suol: as a stone, a chom, to. immeree the tody in a vessel woith sulficieent water to cover ia, the oolveme of the wouter Or, weight the bondy and dinide ity oj the body immersed. the oame material; the quotient woill atholo the botid of a cubic foot or cubic inch of inahse.

    Ex. I. What is the solidity of a stone which, immersed in water, displaces 12 l lb . of it?

    Operation. The volume of one pound of water is $27.7274 \mathrm{cu} . \mathrm{in}$.; therefore the solidity of the stone is $27.7274 \times 12 \frac{1}{3}=346.5925$ cab. inches, Ans.

    Ex. 2. A vessel holding 5 gallous is filled with water; an objeot is immersed and then taken out ; the water remaining in the vessel is 3 gallons. What is the solidity of the object?
    Operation. $5-3.5=1.5$; a gallon contains 277.27 .4 cub. in.; hence $277.274 \times 1.5=415.911$ cil. in., Ans.
    Notr.-The aolidity of oertain bodies way be found by dividing them into pyramids or other solids whose wontents way easily be reckoned. The easiest didision eonsists in taking for the vortex of tho pyramid, the vertical angle of the
    solid, and for kinds of pyramids, is side opposite. An easy process to find the height of all of a tbin plane board, and a ruler the plane which is taken as the baso, by means that board ; the shurtest distanon between the the tup of the pyramid parallel to give the height of the pyramid.

    ## MISCELLANEOUS EXAMPLES IN SOLIDS.

    1. The solidity of a regular hexagonal prism is 71.1126 cub. yd ., and the side of the hexagon 2.34 yards; required $1^{\circ}$ the area of the base; $2^{\circ}$ the altitude of the prism
    2. What is the solid contents of a spherical segment, the diameter of whose base is 12 ft , and its altitude 5 ft ? Ans. $318.19+\mathrm{cll}$. ft .
    3. A room 9.25 yd . long, 4.85 yd . wide, and 4.80 yd . high, is to be papered; the rolls of paper are 12 yd . long by .5 yd . wide. Allow lug 12.25 sq . yd. for the apertures in the walls, how many rollo will be required, and what will be the cust the 7 cte. per roll?

    Ans. 20.515 rolls, and $\$ 15.38+$.
    4. Find the convex surface of an cylinder, "the radius of whose basie is 8.5 yd ., and ita altitude $\frac{8}{5}$ of the circumf. Ans. $185.707+\mathrm{sq}$. yd.
    5. A cable 3 feet loag and 9 inches in circunsference weighs 22 yd. what is the weight of another cable 6 feet in length and I fioot in cir. Ans. 96.1875 lb .
    6. What is the weight of a :quare briok pillar whose side is 0.75 yards, and height 4.75 yards, if 1 cubio yard of brick masonry weighs 36 civt. ?

    Ans. 96.1875 lb .
    7. The slant height of a regular hexagonal pyramid is 8 yd ., and the side of its base 6 yards; what is its whole surface?

    Ans. 237.5307 sq. yd.
    8. A man had a wall built for $\$ 136$, which was $\$ 3.20$ a cub. yd . What is the height of that wall, knowing that it is 14.5 yd . long and 70 thick?

    Ans. 4.18 yd.
    9. A rectangular basin is 12 to. long, 2.5 to. wide, and 1.5 to. deep; how many barrels of $31 \frac{1}{2}$ gal. each does it hold, there being 231 cu. in. in a gallon? Ans. $2811.9+$ bbl.
    10. The convex surface of regular triaugular pyramid is $45 \mathrm{sq} . y \mathrm{~d}$, the slant height is 6 yd. ; required the length of one of its side-edgee.

    Ans. 6.50 yd .
    11. The lower base of a pile of stone is 26 by 12 yd., the upper one 16 by 8 yd., and the pile is 3 yd . high ; find its cubic contents.

    Ans. 639.84 cub. yd.
    12. What is the convex surfacc of a right cone, the radius of whose base is 1.4 yd . and its side, the $\frac{3}{4}$ of the circumference of the base?

    Ans. $29.0167+\mathrm{sq} . \mathrm{yd}$.
    13. I desire to get a cylindrical tub made whose depth will be 3 st ; what must be its diameter that it may hold twice as much as a similar tuk whose depth is 5 ft ., and diameter $3 \frac{1}{2} \mathrm{ft}$.?

    Ans. 6.38 ft .
    14. What is the slant height of the frustum of a cone, whose convex surface is 12.26 square yards, and the radii of the two bases 1.71 and 2.2 yards?

    Ans. . 998 yd .
    15. How many cords in a pile of wood whose length, breadth, and height are respectively 15.5 , 4 , and 7.25 yd ? Ans. $94.81+$.
    16. What mu*t be the radius of a cylindrical basin holding 110045 gallons its depth being 5 yd.? Ans. 5.839+ yd
    17. How many solid feet in the frustum of a pyramid whose bases are regular octagons, the sides of which are respectively 21 and 9 in ., and the perpendicular distance of the basea 15 ft .?

    Ans. $119.20+$ cub. th.
    18. What is the surface of the base of a quadrangular prism, whose altitude is 1.15 yd ., and its solidity 4.25 cu . yd . ? Ans. 3.6956 sq , yd.
    19. Find the solidity of a beam whose length, breadth, and thickness, are respectively $12.75,0.35$, and 0.25 yd .

    Ans. $1.115625 \mathrm{cu} . \mathrm{yd}$.
    20. A niangets a cemented cistern made in the ground that will hold 3000 gal.; what will be its depth, the length and breadth being respectively 1.8 and 1.75 yd.?

    Ans. 4.715 yd.
    21. What is the solidity of a regular hexagonal pyramid whose altatude is 3.6 yd ., and the side of the base 3.6 yd . ${ }^{\text {a }}$

    Ans. 40.405651 cub. yd.
    22. What is the convex sufface of the trustum of a triangular pyramid whose bases are parallel, knowing that the sides of the lower bace are 2,3 , and 4 ft . ; the corresponding sides of the upper base 0.95. 1.20, and 2.10 ft ; and the height of the three trapmzoids 5,6 , and 6.45 feet?

    Ans. $40.4537 \mathrm{sq} . \mathrm{ft}$.
    23. What are the dimensions of a barn whose capacity is 810 cu .
    side is 0.75 sonry weighs 36.1875 lb . 3 yd ., and the $307 \mathrm{kq} . \mathrm{yd}$. 0 a cub. yd. yd. long and e. 4.18 yd .
    1.5 to. deep; ng 231 cu in. $11.9+b b l$. is 45 sq . yd ., is side-edgee. 8. 6.50 yd . the upper one ntents. 84 cub. yd. dius of whose the base? $7+$ sq. yd. will be 3 th ; h as a similar n8. 6.38 tt . whose convex ases 1.71 and 1s. . 998 yd . breadth, and s. $94.81+$. olding 110045 $5.839+\mathrm{yd}$ d whose bases 21 and 9 in.,
    $0+$ cub. fl. prism, whose 6956 sq, yd. and thickness, $5625 \mathrm{cu} . \mathrm{yd}$. und that will breadth being s. 4.71 j yd . mid whose al.

    351 cub. yd. riangular pyr3 of the lower ir upper base rapozoids 5, 6 , $.4537 \mathrm{sq} . \mathrm{f}$. city is 810 cu.
    yd. excluding the lon, if its breadth is $f$ of ite leugth, and its height up to the loft $\frac{3}{3}$ of its length?
    2.4. What is the altitude of a cone whose solidity is $3.077 \mathrm{ca} . \mathrm{yd}$. and the radius of its base $0.35 \mathrm{yd}$. ? $\quad$ Ans. 23.9 N 5 yd . 2.1 . What is the length of a great circle of a sphere which measures 12 tq. yards?
    26. A gentleman wishes to have a circular fish-pond mole in his garden that will cover an area of half an acre; what will be its diameter?
    27. What is the surface of a segment Aas. 55.50 yd . ical sector whose solidity is a segment serving as a base to a spher being 1.5 yd .?
    28. What is the surface of $A n s .5 .15 \mathrm{sq}$. yd. miles?
    20. Find the solidity of Ans. 196649433.55625464 sq . mi. ends being 1.5 and 0.55 yd . $\log 9.25 \mathrm{yd}$. long, the rircumference of its
    30. What must be the thickness of a Ans. 0.77338062 cub. yd. and external surfaces are 3 and 3.12 yards?
    31. A basin holds 1093.75 cubic yards of water; Ans. 0.1 yd. breadth as 7 to 5 , and to its depth as 5 to 3 water; its length is to its
    32. Required the convex surface as 5 to 3 ; find its dimensions. gonal pyramid whose baces are parallel, and uring respectively 1.64 and 1 vard, the slant one side of each meas.
    hejght being 2.25 yd .
    Ans.
    $20.79 \mathrm{sq} . \mathrm{yd}$. anil assumes a wand rests on a rectangular base of 4.25 by 2.15 yd., altitude is .8 yd., how many solid top whore length is $3.4 \mathrm{yd}$. ; if its
    
    34. A cubic foot of copper was drawn intons. 3.411333 cub. yd. eter; no netal being lost, how long was the wire? $\frac{1}{40}$ in. in diam-
    35. One pound of lead was drawn into a wire? fur 60 cts. ; allowing 1 cu . in. of lead to a wire 168 yd . long, and sold perfectly cylindrical, what was its diameter? 6.569 oz ., and the wire 36. A sphere, whose surface is 78.54 sq cutting the radius at its 2 from the 8.54 sq. $y d$. is divided by a plane of each part?
    37. What is the wns. 1st $23.5620 \mathrm{sq} . \mathrm{yd} . ; 2 \mathrm{nd} 54.973 \mathrm{sq} . \mathrm{yd}$. thickness, if the exeight of a copper spherical shell 0.985 inch in weight of a cubic footnal diameter of the sphere is 1.35 jd ., and the
    33. A gentleman wan copper $524 \frac{3}{4} \mathrm{lb}$.
    court-yard; the wants an elliptical fish-pond to be digged in his small axis 12.75 ydeat axis of that fish-pond is to measure 15 yd ., the ness of the wall which is the depth 4.50 yd., not including the thickdigging it, if the conh is . 45 yd. throughout. Required 10 the cost for of the masonry, at $\$ 15.45$ per cubes $\$ 1.75$ per cnbic yard; $2^{\circ}$ the cost the capacity of tio pond per cub. yd. ; $3^{\circ}$ the whole cost; and $4^{\circ}$ 39. A veses! is the shape of a frustum of a cune whose ralius of the lower base is $5 \frac{1}{2}$ inches, the diameter of the upper kise 13 inches, and its depth 16 incher, is filled with nitric acid. What is the value of that acid, if it be worth 16 cts. a quart? Ans. \$5.04.
    40. Supposing the ithon io be a perfect sphere, what is her surface, - her diameter being to liast of the Earth as 3 is to 11 , and the diameter of the Earth leing 7912 miles?

    Ans. $14626758 \mathrm{Ti}_{\mathrm{f}}^{\mathrm{kq}} \mathrm{mi}$.
    41. A founder wishes to cast a semi-spherical boiler whose internal diameter shall be $6 \frac{3}{4}$ feet, ita thiokness $2 \frac{7}{2} \mathrm{in}$. Required the weight of cast-iron it will take, if we allow $10 \%$ waste in melting, knowing that the specific weight of cast-iron is 7.206 Ans. $8608.36+\mathrm{lb}$.
    42. The interior space of a blast funasce consists of two conic frus. tume uniting at their larger base whose diameter is of the height of the furnace. The altitude of the upper frustum is $\frac{s}{}$ of the height of the furnace, its less diameter is $z^{3}$ of the greater. - The altitude of the lower frustum is ${ }_{2}{ }^{5}$ of the height of the furnace, its less diameter is $\frac{1}{8}$ of the greater. If the furnace is 15 yards high, what is its interior capucity?

    Ans. 41.921 cub. yd.
    43. A fountain in the form of the frustum of a cone is filled with vater. Required $1^{\circ}$ how many gallons it contains, if the circumferences of its bases are 16.95 and 15.86 yards, and its depth 5.35 yd ; $2^{\circ}$ in how many hours it will be emptied, if the water is let out by three pipes, of which the lat empties $1 \frac{1}{2}$ gal. in 1 minute; the 2nd, 11 gal . in 8 min . ; the 3 rd , 13 gal. in ${ }_{10}^{10}$ hr. ; $3^{9}$ what time would each pipe take to empty the whole fountan by itself?

    ## TABLE OF CHORDS.

    In the table of chords, the radius of any circle is represented by 1 ; and in decimal of the radius, is represented the length of chords that subtend ares of $1^{\prime}, 2^{\prime}, 3^{\prime}$, \&c., up to an arc of $180^{\circ}$, which is itself a scmi-circumference.

    Any chord which is not a diameter, subtends two aros, one of which is less, and the other greate than a semi-ciroumference; but their sum equls the circumfe ence.

    In all problems treating of ares, the smaller arc is almays implied, unless otherwise mentioned.

    1st Role.-To obtain the chord of any arc greater than a semicircumference, subtract the degrees of the given arc froi. $360^{\circ}$, and find in the table the chord that correspowis with the difference.
    $\boldsymbol{E} x$. What is the chord of a re of $310^{\circ}$ ?
    $360^{\circ}-310^{\circ}=50^{\circ}$. In $t$. . ble he chord of $50^{\circ}{ }_{18} 0.8452$.
    2nd Rule.-To find the lengi.. of any chord in any given circle, muitiply the radius of the given circle by the chord ind ited in the tuble.
    E.x.- How long is the ohord of an arc of $24^{\circ}$ in a circle whose radus is 25 yd . 9
    The chord of $24^{\circ}$ in the table is $0.4158 ; 25 \times 0.4158=10.39 b$ mards, Ame.

    3rd Retw:-To finl the radins of any circle, dinde the given chord by the corresponding chord in the tuble.
    $\boldsymbol{E} x$. What must he the radius of a circle in which a chord of 12 yards subtends an arc of $20^{\circ} 10^{\prime}$ ?

    The chord of $20^{\circ} 10^{\prime}$ in the table is $0.3502 ; 12+0.3502=34.204$ yards, Ans.

    4th Role.- To obtain the degrees of any arc. divide the chord by the radius of the circle, and flnd in the table the degrees correspond ing with the quotient.
    $\boldsymbol{E} \boldsymbol{x}$. - What are the degrees of an arc whose chorl in 4.24 yd ., if the radius of the circle is 20 yd .?
    $4.24 \div 20=0.2120 ; 0.21^{\prime} 2 v$ in the table indicates $12^{\circ} 10^{\prime}$, Ans.
    The following table gives the chords for every $10^{\prime}$ which is practically sufticient ; hut, hy a proper approxination, its use may lie extended to any number of degrees and minntes.

    TABLE OF CHORDS.

    | D. | 0 \% ${ }^{3}$ | $10^{\prime}$ | 20' | $30^{\prime}$ | $40^{\prime}$ | 50 |
    | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
    | uc | $0.0170^{0}$ | 1,0029 | 0,0058 | 0,0087 |  |  |
    | 1 | 0,0175 | 0,0204 | 0,0233 | 0,0087 0,0262 | 0,0116 0,0291 | 0,0145 0,0320 |
    | 2 | 1,0349 | 0,0378 | 0,0407 | 0,0436 | 0,0465 | 0,0320 |
    | 4 | 0523 | 0,0553 | 0,0582 | 0,0611 |  | 0,0494 |
    | 4 | , 0 ti98 | 0,0727 | 0,0756 | 0.0785 | 0,00t0 | 0,0669 |
    | 6 | 0,0872 | 0,0901 | 0,0931 | 0,0960 |  | 0,0843 |
    | 7 | 0,1047 | 0,1076 | 0,1105 | 0,1131 | 0,0939 | 0,1018 |
    | 7 | 0,1221 | 0,1250 | 0,127!) | 0,1134 | 0,1163 | 0,1192 |
    | 8 | 0,1395 | 0,1424 | 0,1453 | 0,1308 | 0,1337 | 0,1366 |
    | $!$ | 0,1569 | 0,1598 | 0,1453 0,1627 | 0,1482 | 0,1511 | 0,1540 |
    | 10 | 0,1743 | 0,1772 | 0,1 | 0,1656 | 0,1685 | $\therefore 1714$ |
    | 11 | 0,1917 | 0,1946 | 0,1975 | 0,1830 | 0,1859 | 1,1883 |
    | 12 | 0,2091 | 0,2120 | 0,1975 0,2148 | 0,2004 | 0,2033 | 0,206 |
    | 13 | 0,2264 | 0,2120 0,2293 | 0,2148 $0,23 \% 2$ | 0,2177 | 0,2206 | 0,2235 |
    | 14 | 0,2437 | 0,2436 | 0,2322 | 0,2351 | 0,2380 | 0,2409 |
    | 15 | 0,2611 | 0,2466 0,2639 | 0,2495 | 0,2524 | 0,255.3 | 0,2582 |
    | 16 | 0,2783 | 0,2639 0,2812 | 0,2668 | 0,2697 | 0,27:6 | 0.2755 |
    | 17 | 0,29.56 | 0,2812 | 0,2 211 | 0,2870 | 0,2899 | 0,2927 |
    | 18 | 0,3129 | 0,2985 0,3157 | 0,3014 0,3186 | 0,3042 | ,3071 | 0,3100 |
    | 19 | 0,3301 | 0,3157 0,3330 | 0,3186 | 0,3215 | 0,3244 | 0,3272 |
    | 20 | 0,3473 | 0,3330 0,3502 | 0,33.38 | 0,3:387 | 0,3416 | 0,3444 |
    | 21 | 0,3645 | 0,3502 0,3673 | 0,3530 | 0,3559 | 0,3587 | 0,3616 |
    | 22 | 0,3816 | 0,3673 0,3815 | 0,3702 0,327 | 0,3730 | 0,3759 | 0,3782 |
    | 23 | 0,3987 | 0,4016 | $0,3.373$ $0,40.14$ | 0,3902 | 0,3930 | 0,3959 |
    | 24 | 0,4158 | 0,4016 0,4187 | 0,4014 0,4215 | 0,4073 | 0,4101 | 0,4130 |
    | 2 | 0,4,158 | 0,4187 | 0,4215 | 0,4244 | 0,427\% | 0,4300 |


    | D. | , 0 | $10^{\prime}$ | - 20' | $30^{\prime}$ | $40^{\prime}$ | 50 ', |
    | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
    | 26 | 0,4499 | 0,4527 | 0,4356 | 0,4584 | 0,4612 | 0,4611 |
    | 28 | 0.4833 | 0,1467 | 0,4895 | 0,4923 | 0,4951 | 0,4979 |
    | 30 | 0,5176 | 0,5204 | 0,5233 | 0,5261 | 0,5289 | 0,5317 |
    | 32 | 0,5513 | 0,5511 | 0,5569 | 0,0598 | 0,5625 | 0,5652 |
    | 34 | 0,5,517 | 0,5875 | 0,5903 | 0,5931 | 0,5959 | 0,5986 |
    | 36 | 0,6180 | 0,6203 | 0,6236 | 0,6263 | 0,6:291 | 0,6319 |
    | 38 | 0,6511 | 0,6539 | 0,6566 | 0,6594 | 0,66: 1 | 0,6649 |
    | 40 | 0,6810 | 0,6468 | 0,6895 | 0,6922 | 0,6950 | 0,6977 |
    | 42 | 0,7167 | 0,7195 | 0,7222 | 0,7249 | 0,7276 | 0,7303 |
    | 44 | 0,7492 | 0,7519 | 0,7546 | 0,7573 | 0,7600 | 0,7627 |
    | 46 | 0,7815 | 0,7811 | 0,7868 | 0,7895 | 0,7922 | 0,7948 |
    | 50 | 0,8452 | 0,8.79 | 0,8505 | 0,8531 | 0,8558 | 0,8584 |
    | 54 | 0,9080 | 0,9106 | 0,91:2 | 0,9157 | 0,9183 | 0,9209 |
    | 58 | 0,9696 | 0,9722 | 0,9747 | 0,9772 | 0,9793 | 0,9823 |
    | 62 | 1,0301 | 1,n:326 | 1,0:351 | 1,0375 | 1,0400 | 1,0125 |
    | 66 | 1,0893 | 1,0917 | 1,09+1 | 1,0965 | 1,0990 | 1,1014 |
    | 70 | 1,1472 | 1,149.5 | 1,1519 | 1,1543 | 1,1567 | 1,1590 |
    | 74 | 1,2036 | 1,2460 | 1.2083 | 1,2106 | 1,2129 | 1,2152 |
    | 78 | 1,2586 | 1,260:) | 1,2632 | 1,2654 | 1,2677 | 1,2699 |
    | 82 | 1,3121 | 1,3143 | 1,316\% | 1,3187 | 1,3209 | 1,3231 |
    | 86 | 1,3640 | 1,3661 | 1,3682 | 1,3704 | 1,3725 | 1,3746 |
    | 90 | 1,4142 | 1,4163 | 1,4183 | 1,4204 | 1,4224 | 1,4245 |
    | 94 | 1,4627 | 1,46+7 | 1,4667 | 1,4686 | 1,4706 | 1,4726 |
    | 98 | 1,5094 | 1,5113 | 1,5132 | 1,5151 | 1,5170 | 1,5189 |
    | 100 | 1,5321 | 1,5340 | 1,5358 | 1,5377 | 1,5335 | 1,5414 |
    | 104 | 1,5760 | 1,5778 | 1,5796 | 1,5814 | 1,5832 | 1,5849 |
    | 108 | 1,6180 | 1,6197 | 1,6214 | 1,62:31 | 1,6248 | 1,6265 |
    | 112 | 1,6581 | 1,6597 | 1,6613 | 1,6629 | 1,6645 | 1,6662 |
    | 116 | 1,6961 | 1,6976 | 1,6991 | 1,7007 | 1,7022 | 1,7038 |
    | 120 | 1,7320 | 1,7335 | 1,7350 | 1,7364 | 1,7378 | 1,7393 |
    | 124 | 1,7659 | 1,7673 | 1,7686 | 1,7700 | 1,7713 | 1,7727 |
    | 128 | 1,7976 | 1,7989 | 1,8001 | 1,8013 | 1,8026 | 1,8039 |
    | 132 | 1,8271 | 1,8283 | 1,8294 | 1,8306 | 1,8318 | 1,8330 |
    | 136 | 1,8544 | 1,8554 | 1,8565 | 1,8576 | 1,8587 | 1,8593 |
    | 140 | 1,8794 | 1,8804 | 1,8814 | 1,8824 | 1,8833 | 1,8843 |
    | 144 | 1,9021 | 1,9030 | 1,9039 | 1,9048 | 1,9057 | 1,9065 |
    | 148 | 1,9225 | 1,9233 | 1,9241 | 1,9249 | 1,9257 | 1,9265 |
    | 152 | 1,9106 | 1,9113 | 1,9420 | 1,9427 | 1,9434 | 1,9441 |
    | 156 | 1,9563 | 1,9:369 | 1,9575 | 1,9581 | 1,9587 | 1,9593 |
    | 160 | 1,9696 | 1,9701 | 1,9706 | 1,9711 | 1,9716 | 1,9721 |
    | 164 | 1,9805 | 1,9809 | 1,9813 | 1,9817 | 1,9821 | 1,9825 |
    | 168 | 1,9899 | 1,9893 | 1,9896 | 1,9899 | 1,9902 | 1,9905 |
    | 170 | 1,9924 | 1,9926 | 1,9929 | 1,9931 | 1,9934 | 1,9936 |
    | 172 | 1,9951 | 1,9953 | 1,9955 | 1,9957 | 1,9959 | 1,9961 |
    | - 174 | 1,9973 | 1,9974 | 1,9975 | 1,997 ${ }^{\circ}$ | 1,9978 | 1,9980 |
    | 176 | 1,9988 | 1,9989 | 1,9990 | 1,9991 | 1,9992 | 1,9992 |
    | 179 | 1,9999 | 1,9999 | 1,9999 | 1,9999 | 1,9999 | 1,9999 |
    | 180 | 2,0000 |  |  |  |  |  |

    Culling and Measuring of Timbor, Masts, Spars, Deals, Staves and other artioles of a like nature.
    (From the Consolidated Statutes of Canada, Cap. 45.)

    0,4641
    0,4979
    0,5317
    0,5652
    0,5986
    0,6319
    0,6649
    0,6977
    0,7303
    0,7627
    0,7948
    0,8584
    0,9209
    0,9823
    1,0125
    1,1014
    1.1890

    1,2152
    1,2699
    1,3231
    1,3746
    1,4245
    1,4726
    1,5189
    1,5414
    1,5849
    1,6265
    1,6662
    1,7038
    1,7393
    1,7727
    1,80:39
    1,8330
    1,8598
    1,8843
    1,9065
    1,9265
    1,9441
    1,9593
    1,9721
    1,9825
    1,9905
    1,9936
    1,9961
    1,9930
    1,9992
    1,9999

    Doals.- A Qucbec Stnmard Deal is 12 feet long 11 inches broad and $2 \frac{1}{3}$ inches thick, and contains $2 . \mathrm{fr}$. 3 in. 6 pts. cubic. One Hundred Quebec Stundard contain 229 ft 2 in . cubie, or 4.29.50 loads, and are equivalent to 2750 fort superficial boaril meatsure of one inch thick.

    One Quebee Stantard is 100 piecess of 12 ft . by 11 in . by $2 \frac{1}{2}$ in., and is equal to $1 \mathrm{hd} .1 \mathrm{qr}$.16 pes. of St. Petersburg St:andurd ; anil 240 Quebec Standard Deals are equal to 11 loads.

    One Sh Petersburg Standard Hundred is equal to 120 pcs. of 12 ft . by 11 in . by $1 \frac{1}{2} \mathrm{in}$., and is equal to 72 Quebec Standard, and equal to $3^{3}$ loads of Timber.

    A Load of Deals is 600 square feet by one inch in thickness. equal to 50 cubic feet; or 300 square feet of 2 inches, or 400 of $1 \frac{1}{2}$ inch.

    A Load is equal to 21 deals 1 foot $10 \frac{1}{2}$ inches, $Q_{\text {uebee Stimn } 1 .}$ ard, and equal to $36 \frac{1}{3}$ St. Petersburg Standard deals.

    Rule.-To convert Quebec Standard Hundred into St. Petersburg Standard :-Add two-thirds of the quantity, mul divide the sum by 120. If there shostd be any remainder, divide if by 30. for quarters.

    Staves.-One Standard Stave is $5 \frac{1}{2}$ feet long, $1 \frac{1}{2}$ inch thick, and 5 inches broad.

    One Mille, or 1200 Standard Staves, is equal to 343 feet 9 inches, or $6 \frac{4}{8} 8$ loads.

    One hundred and seventy-five Standard Staves are equal to 50 feet 1 inch $6 \frac{3}{4}$ parts, or 1 load 1 inch $6 \frac{3}{4}$ parts.

    One Mille West India Staves, 1200 pieces, is equal to $87 \frac{1}{2}$ feet, or $1 \frac{37}{56}$ louds of timber.

    Owing to the variations in breadth and thickness of Staves, it is customary to allow one Milie, Quetrec Standard, to be equal to 13 loads

    Lathwood.-One oord of Lathwood is 8 feet long and 4 feet high, English measure,

    ## CUSTOMARY ALIOWANUE FOR FREIGHT AND BROKEN STOWAGE.

    Deals.-A Hundred St. Petersburg Standard, at twice the charged rate for timber per load.

    Staves.-A Mille Standard, at six times the rate chnrged for timber per load. A Mille West India, at twice the rate charged for timber per load.

    Lathwood.-A fathom of Lathwood, at the same rate as charged for timber per load.

    ## FREIGHT AND SHIPPING.

    To find Freight measurements, or cubical contents of packages.
    RuLe.-Multiply length, breadth and thicleness together ; for surfucos, length and breadth only.

    Fior Stowage. -97 quarters of Wheat, or 140 barrels of Flour, or 80 barrels of Ashes, are considered equal.

    For Grain. -42 culic feet equal 1 ton of shipping. One bushel is equal to $60 \mathrm{lbs} .2218 \frac{1}{2} \mathrm{cu}$. in. are equal to an Emperial bushel. 8 bushels are equal to one quarter $=17745 \mathrm{ca}$. in., or $10 \frac{27}{100} \mathrm{cu}$. ft. Therefore, 1 ton will take $4 \frac{1}{10}$ quarters, 1 bushel being $=60 \mathrm{lbs} . ; 1$ quarter $=480 \mathrm{lbs} . ; 1$ ton $=1968 \mathrm{bs} . ~ A$ ship of 200 tons measurement can, therefore, carry 820 quarters; but it can generally carry much more. - -

    ## CUBIC OR SOLID MEASURE.

    

    SQUARE MEASURE (see $p .118,119,120$ ).
    Engitish. " Frenor.
    

    The side of a square acre is $69 \frac{1}{2}$ yards in length, and is often ywited by French-Canadians as a unit of length for short diatances.

    1 French foot is equal to $121_{12}$ English Inches.
    104 " lbs. are " to 112 " Pounds.
    1 Camadian Minot is " to 1.054 Imperial Bushel.

    ## The following rules for Timber Calculations may be found useful by the trade.

    To Reduce Square Timber, of different sizes, to an Average Square.

    Rule.-Add the lengths (in feet) together; reduce the cubic contents of the whole to parts; divide the product by the total lineal feet; the square root of the quotient will be the average squire, in inches.

    To find the Cubic Contents of Round Timber.
    Rucs.- Square the diameter; multiply the product by 11 and divire by 14 ; multiply the result by the length of the log; then redlure the product to feet, inches, and parts, dividing by 12 and by 12 (or by 144).

    ## TABLE OF SPECIFIC GRAVI'TIES.

    In estimating the weights or specific gravities of bodies, rainWater is cenerally taken as the Standard. Experiment has shown, that a cubic foot of rain-water weighs $62 \frac{1}{2}$ pounds Avoirdupois, or 1000 ounces. It hence follows that a cubic inch weighs 003616898148 of a pound. If, therefore, the specific gravity of a body be muliiplied by the above decimal, the product will be the weight of a cubie inch of that body in pounds A:oirdupois, which maty be changed to 'Troy weight by being multiplied by 175 and the product divided by 144, since 144 lbs . Avoir. dapois $=175 \mathrm{lbs}$. Trog.

    The weight of a cubic foot of rain-water is taken as the unit.viz. 1000 ; und the weight of a cubic foot of any one of the following articles is in ounces Avoirdupois.

    ## SPECIFIC GRAVITY.

    Woons (Dry).
    Ash ..... 845
    Apple ..... 793
    Box-wood ..... 1031
    Beech ..... 852
    Birch ..... 567
    Butternat ..... 376
    Cedar ..... 561
    Cherry ..... 715
    Chesnut ..... 610
    Cocoa ..... 1040
    Cork ..... 240
    Cypress ..... 614
    Ebony (American) ..... 1331
    Elm570
    Fir, White ..... 512
    Haoknatack ..... 592
    Hazel ..... 860
    Hemlock ..... 368
    Holly ..... 760
    Uignum vitæ. ..... 1333
    Lime ..... 804
    logwood ..... 913
    Mahogany (Honduras). ..... 560
    Maple750
    Maple, bird's eyo ..... 576
    Oak (Canadian) ..... 872
    Oak (English) ..... 932
    Pear ..... 661
    Pine, White ..... 554
    Pine, Red ..... 590
    Pine, Yellow ..... 461
    Pine, Pitch ..... 660
    Plum ..... 785
    Poptar ..... 383
    Spruce ..... 500
    Tamarack ..... 38:3
    Walnut, Grey ..... 671
    Walnut, Black ..... 550
    Willow
    Aleohol, pure, $60^{\circ}$ ..... 794
    Beer. ..... 1034
    Brandy ..... 924
    Blood (human) ..... 10 54
    Bees-wax ..... 365
    Brass, cast ..... 8396
    Brick, fire ..... 2201
    Coal (Anthracite) ..... 1436
    Coal (Newcastle) ..... 1270
    Coke ..... 1000
    Copper, cast ..... 8788
    Earth, onminon ..... 2194
    Glass, window ..... 2642
    Gold, 22 carats. ..... 17486
    Granite (Scotch). ..... 2625
    Guttapereha ..... 980
    Honey ..... 1450
    Iron, cast ..... 7207
    Ivory ..... 1825
    Lead, east ..... 11352
    Lime, hydraulic ..... 2745
    Marble (Vermont) ..... 2650
    Mill ..... 1032
    Petroleum ..... 878
    Plaster of Paris. ..... 1176
    Platinum, native ..... 16000
    Quicksilver ..... 13568
    Salt ..... 2130
    Sand, common ..... 1650
    Silver, pure cast ..... 10474
    Soap, Castile. ..... 1071
    Starch ..... 950
    Steel Plates ..... 7806
    Tallow ..... 941
    Tin, pure ..... 7291
    Turpentine ..... 870
    Water, common ..... 1000
    Water, sea, ..... 1026
    585 Zinc, rolled ..... 102 ..... 102
    Zine, rolled ..... 7191

    ## BOOK-KERPING

    794 1034 $92+$ $10 \overline{4}$ 365 8396 2201 1436 1270 1000 8788 2194 2642 17486 2625 980 1450 7207 1825 11352 2745 2650 1032 878 1176 16000 13568 2130 1650 10474 1071 950 7806 941 7291
    870 1000 1026 7191

    ## DEFINITIONG.

    1. Book-Keeping is a systematie record of business traneactions, or the art of keeping accounts.
    Every perzon, engaged in business for himself, should keep a book of some kind m which to record all his business transactions. The mechanic, the farmer, the pro'essional man, etc., should keep an account with every person with whom they deal. For no one should trust transections of a pecuniary nature to his memery alone.
    2. All business transactions consist in an ezehange of values.
    3. There are two methods of Book-keeping in general use, distinguished as Single and Double entry.
    4. The Double Entry is conceded to be greatly superior to the Single Entry, particularly from its more excellent tests for determining the correctness of the work.
    5. Single Entry embraces only the aceounts of persons, and consists of but one debit, or one credit.
    6. Double Eatry is derived from the faet that every business transaction nust be entered to two or more Ledger accounts, as two or more persons or things are affected thereby.
    7. Two books appear iudispensable in Single Entry; viz., the Day Book and Ledger.
    8. The three main books used in Double Entry are the Day Book, Journal, and Ledger. The Day Book aud Journal are sometimes combiner in one.
    9. The number and chargnter of the auxiliary books depend somewhat on the nature and extent of the business, but more on the amount and kind of information desired. Those most in use are the Cash Book, Bill Book, Invoice Book, Sales Book, the Commission Sales Book, ete.
    10. The Day Book is that in which are entered the business transactions in the date and order of their occurrence.
    This book should bo plain, concise, and unequivocal in its statemente. As the records in it are supposed to be made when the transactions and all the circumstanser conneoted therewith are fresh in the mind, it is the only book allowed in court, iu cases of litigation.
    11. The Journal is a book in whieh the business transactions resorded in the Day Book are prepared to be entered in the Ledger, by ascertaining the proper debits and credits involved in each bransaction. This process is called journationg.
    12. The Leager is the book of results,-the tinal book of entry.

    ## BOOK-KEEPING.

    In this book, andar appropriate heade, colled nocounts, are arranged all the facts necessary for a furf and satisfintory statement of the bustness; Including not only an exhibition of the present resourees and liabilities, but a distinct reenrd of pirticular gaine and losses. The procees of transforring to the Ledger is called pooting.
    18. The Cash Book is that which shows all the sums of money which we reccive or pay, with a short explanation relating to each sum.

    The entrios, in this book, are made immediately on receiving or paying the sums. If properly kept, it will, at any time show the amount of eash on hand. It is customary, in most business houses, to olose up the Cash Book at the end of each business day, and bring the balance down as a basis for the next day's transactions.
    14. The Eill Book is that which shows a description of all the notes or acceptances in our favor or against us, with their dates, credits, when due, and amounts.
    The notes or acceptances in our favor are entered under the head of Receivable, and those against us under Payable.
    15. The Invoice Book is that in which are copied all bills of goods bought, and all invoices of goods reccived into our possession.

    From the Invoice Book the entries pass into the Day Book, either daily, weekly, or monthly. This book is sometimes made of coarse paper, and the original invuices pasted inta it.
    16. The Sales Book gives a full desoription of all goods sold or passed fron our hands, or out of our possession.
    From this book the amounts are tranferred to the Day Book, either daily, weokly, or monthly. At the time the purchaser selects his goods, they are deseribed in the Sales Book-quautity, quality, and price ; and from this book we make out his bill.
    17. The Commission Sales Book contains a minute desoriptinu of the merchandise sold by us for others.
    The entries in this book are drawn from the common Sales Book, and from it we mako the Accounts of Sales that. we may have to remit to those for whom we have sold.
    18. An Account is a statement of facts pertaining to some person, species of property or cause, which enters into the transaction, producing a debit or credit, and designated by a name, which appears upon the Ledger.
    19. Every account has two sides, a Debtor and a Cieditor; each containing the results of separate transactions.
    26. In overy transaction the sum of debits and eredits must be equal.
    facin Ledger mosoent, by the uee of these wrmes, in made to show an important realit of itsolf.

    ## BOOT-KEEPING.

    eranged all the ss, inoluding, distlnet reenrd edger ts oalled
    he sums of tion reluting
    or paying the eash on hand. $k$ at the end of the next day's
    iption of all their datee,

    1 of Receivable,
    ed all bills of , our posses-
    daily, weekly, the original in-
    ll goods sold
    c, either daily, le, they are den this book we
    nute desorip-
    ok, and from it e for whom we
    ing to some to the transby a name,
    a Creditor ; credits must
    21. A Resource is any kind of value belonging to the conoern.
    22. A Liability is any debt owing by the conoern.
    23. Cash is the title to designate money.

    The Cash account in the Ledger is debitel with all reoeipts of onsh, and creditel with all disbursementa. Th: differonee between tho two eides must, at any time, oxhibit a resource of the exact amount of eash on hand. The credit eide of Cash account oannot exceed the rlobit, as more cash cannot be paid out than has been roceived.
    24. Bills Receivable are written obligations of whatever form, in our possession, for which a certain specified amount is to be received.

    The Bills Reoeirable acoount is debited with notos received, and credited with ohose disposed of, or in any manner canceled. The oxcess, if any, must be on the debit side, and will indicate that portion of our rosources consisting in notes.
    25. Bills Payable are written obligations of the concern, for which a specified amount is to be prid.
    Under this head are placed, on the credit side, our notes and acceptances tasned, aud on the debit side, such of them as have been redeerned. The difference, if there be any, must exhibit our outstauding notes, or our liability in waredeemed рарет.
    26. Merchandise is a term which usually implies all property purchased or owned by the concern for purposes of traffic, and remaining in sture.

    Merchandise gonerally embraces all such property, unless the merohaut, being ourlous to know his gains or losses on a purticular kind, opens a separate ascount with that partioular kind, under its own special title. This aceount, or any of its correlative titlos, is debited with the cost of th eroperty represented, and oredited with its returng.
    27. Real Estaie relates to such property as houses and lands, and the account is similar in its objects and teachings to that of Merchandisc.
    28. Bank Stock, Railroad Stock, ete, are not accounts dissimilar to Merchandise and heal Eistate, inasmuch as stocks of all kinds are bought and sold at their market valuo, rather than the value written on their face.
    29. Shipment or Adventure is but another intme for Merchandice, and is used to distinguish hetween property in store and out of store.

    When property iase it mway to besold by an egent for uc, we should diainguish is from our mere nandice iu store by giving it a significant wame, such as "Shipment to Haifux, " "SLipment to A." our ageat, or "Alventure" to the
     with their proceeds, the cuitierence being a gain or lose.
    30. Peranial Accounts, that is, accounts representing persunal indebtedness, and desigmated by the proper names of such

    ## BOOK-KEEPING.

    persnus a: sustain relations of debtor and ereditor to the concern, are capable of showing either resources or habilities.

    Personal Acomints are debited with snch surns as, from time to time, the persona may beoome indebted to the concern, or the concern has paid them, and credted with what they have paid the concern, or the ooncern may have beoome indebted to thein.
    31. Stock, used as a Ledger title, means simply the proprietor of the business, or the stock-holder.
    There would bo no valid objeetlon to using the proprietor's name instead; but as no real goud would result from the change, authors, teachers, and praotioal acconntants, accept the term which custom has suggested.

    This nocount is usually the first opened in the Ledger, and is important to show the net investment. It is generally credited with the whole investment, and dobited with such liabilitics as the concern assumes to pay for the proprieter. The differcnee is the net investment, or what the coneern owes the proprietor.

    From the foregoing remarks, we derive the seven principles which follow, and we believe that every student who will thoroughly fimiliarize himself with them, will have no diffioulty in deciding upnn the proper debita and credits involvedin any business record which he may be called upon to make.

    ## PRINCIPLES.

    ## 1.-The Proprietor:

    The person or persons investing in the business should be credited, under some title, for all such investments, and also for his or their share of the gailin; on the other hand, he or they should be debited for all liabilities assumed by the coneern for him or them, for all sums withdrawn from the business by him or them, and for such loss as he or they are entitled to share.

    ## 2.-Cash.

    Cash account should be debited for all oash receipts, and credited for all cash disbursements.

    ## 3.--Merchandise.

    Merchandise, and all species of property, bought upon speculation, should be debited, under some appropriate head, for the cost of the property represented, and credited with its proceeds.

    > 4.-Bills Receivable.

    Biils Receivable account should bo debited with other peoph's notes, acceptances, and other written obligations when they become ours, and credited when they are paid, or otherwise disposed of.
    BOOE-KEEPING.

    ## 5.-Bills Payable.

    Bills Payavie account should be crealited with our notes, secept anoes, or written promises to pay, when they are iserued, and det. itecl when they are paid or redeemed.

    ## 6.-Persons.

    Personal accounts, such as the name of persons, banks, or other institutions, competent to sue or be sued, should be debiterl under their proper titles when they become indebted to us, or we get out of their debt, and credited when we beoome indebted to them, or they get out of our deht.

    > 7.-Expense, etc.

    All expenses, of whatever name, should be debited for the out. lay, and all causes, of whatever kind producing us value, should be credited under some name, for the amount thus produced.

    The foregoing principles are allembraced in the following simple

    ## FORMULA.

    Delit what costs the concern value; and Credit what produces
    uld be credso for his or y should be im or them, $r$ them, and
    s, and cred-
    on speculaad, for the proceeds.

    ## BOOK-KEEPING

    # DI <br> DOUBエ円 $\boldsymbol{H}$ NTEY. 

    ## SETI.

    ## (INITIATORY.)

    ## DAY BOOK, JOURNAL, AND LEDGER.

    REPRESENTING THE BUSINESS OF A SINGLE PROPRIETOR. WITA EXPLANATIONS FOR JOURNALIZING, STATEMENTS, BTO.

    ## INSTRUCTIONS FOR SET I.

    The following set comprises the most simple transactions in business; the main purpose being to illustrate the foregoing prinsiples, and to initiate the student more fully into the processes of Book keeping. The general instructions given in connection with this set, will apply with equal force to the succeeding ones. They should, therofore, be properly heeded.

    The transactions are first recorded historically in the Day Book, in the order of their occurrence; from thence transferred to the Journal, and from thence to the Ledger. In journalizing a transaction, the first thing to be sonsidered is, the person or thing affected; next, in what manner affeated; and laslay, the propar application of the principle. The check-mark $(\sqrt{ })$ is unde opposite the Day Book entry, immediately upon its being journalised.

    Transferring to the Leteser is called posting. If the transas. tions are properly journalized, the labor of posting is simply mechanical. It requires great care, however, and constant watchfulness, and nothing is more common with new begiuners than errors in posting.

    Commence with the first account in the Journal, and write it as a heading in the Ledger. See if the amount opposite, be in the debit or credit Journal column, and enter it on the corresponding side in the Ledger, using as an expression the opposite journal entry. Suppose, for esaniple, the journal entry to be "Merchandise Dr. To Cash." This expression implies, of course, that Merchandise is to be debited, and Cash credited. Under Merchandise account in the Ledger, on the debit side, we say, "To Cash," und carry the amount to the money column. Also, under Cash account on the credit side, we say, "By Merchandise," and carry the amount into the ceredit column. In posting from the Journal, be careful to enter in the column at the left of the account, the page of the Ledger to which the amount is posted, immediaiely apon its being entered in the Ledger.

    ## DAY BOOK,-SET I.

    Qogebec, January 2, 1871
    pactions in egoing prinprocesses of iection with ones. They

    Day Book, rred to the ing a transn or thing the propar ide opposite alized.

    ## DAY BOOK,-SET I.

    Quebec, Jandary 12, 1871.
    

    ## DAY BOOK, SHT 1.

    Quebeo, Pebruart 10, 1871.
    
    

    IMAGE EVALUATION TEST TARGET (MT-3)
    

    Quebrc, January 2, 1871.
    Dr.
    Cr.
    

    JOURNAL, -SET I
    Qubbeo, January 17, 1871. Dr
    Dr.
    Gr.
    
    R. Green is hers made Dr. because we
    here canceled our indobtedness to him by promising to pay tho amount to another person whom he has authorized to receive it, Prim th -Bills Payable is credited for our new li , bility thus assumed, Prim. 5.
    The only ohinge wrought in our affairs by this transaction is the transfer of a liability from a persona! focount to a note. We must now meet this obligation at its maturity, or be disgraced by having our paper
    protested.
    bills Receivable Dr., Prim. 4. Merchandie Cr., Pron. 3.

    $$
    \text { ——— } 81
    $$

    Express:
    Dr.
    To Cash.
    Eispesse Dr., Pron. 7.-Cash Cr., Prim. 2.
    $\qquad$ February 1

    Cain

    ## JOURNAL, SETT I.

    Quebec, February 2, 1871 . Dt. Cr.
    
    

    LBDGFR,-SET 1.
    (Liabilities assumed for the proprietor
    and account a dram out.) Dr.
    1871
    
    (Paid om. $) \quad$ Cr.
    
    
    LHDGER,-SWT 1.
    
    

    LEDG표R,-SETI.
    
    
    
    13：
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    $:=$
    88812
    
    ع189
    \｜
    T
    The object of the Balanoe Shet
     eorcantile operafions．Under there is occasion for new ones．－The Balance Sheen a cessation of basiness，dissolutlon of partnership， that wo poisess，and all that we owe or ang of＂Balances of owr Resources and Liabilitice＂，under two heads，the entire result of our
    
     goode are depreciated in value，but never at more than cost．
    Balances ofhis Resources and Liabilities．

    > balance on hand, 3al．on hand per
    balance on hand，
    balance in his favor，
    会
    W．S．Reid，
    －No CH
    ANOTHER FORM OF BALANCE SHEET.
    
    
    prooknis of olosing.

    ## PROOESS OF CLOSING.

    It is supposed that the student has gone through with the process of journalizing and posting the transnctions, and that his Ledger accounts present an equilibrium of debits and credits. 'lo test this lact, beforo proceeding farther, we will take a

    Dr.
    

    It will be seen, in the above form of the Trial Bulance, that the footings of the "Face of Ledger" columns exactly agree with the footings of the Day Book and Journal; which affords zonclusive evidence that all the transactions have found their way to the Ledger. The columms of "Differences," which must alse balance, will afford a convenient test of the results of cach account.
    Satisfied that the transactions have been properly posted, we now proceed to close the Ledger accounts. But let it not be forgotten that the object of closing the Ledger is to present, in a proper manner, both the present condition of our business and itg progress. Its present condition can be shown by a list of its resources and liabilities; and its progress, by a list of its gains and losses.

    By an eximination of the facts, it will be seen that $R$ rsources are shown by an excess of the Debit side of Real accounts, and Liabilities by an exces of the Ciedit side of Real accounts; and that Loss's are shown by an excess of the Debit side of Represeivtative accounts, and Guins by an excess of the Credit

    ## PROOESS OF CLOSINO.

    side of Representative accounts. This will suggest the propristy of openiag two accounts for these general results: one to contilin the resources and liabilities, and the other the gains and losses. We will now open these accounts under the titles of "Loss and Gain," and "Balance," the former to contain the results of the liepresextative, and the later of the Real accounts. Before proceediug to elose the accounts, we must ascertain if they are all in a condition to show the results desired. The Merelindise account, as it now stands, shows an excess of the debit side, and wonld therefore represent a loss, if the merchandise were ail sold. The account itself does not show whether the property is all sold; and the only means of ascertaining the facts in the case, is to take an actual inventory, or a valuation of that which romains unsold. This we now proceed to do, with the following result:

    ## INVENTORY.

    Merchandise remaining unsold, February 23, 1871.

    | 93 yards Euglish Black Sloth. | (1) \$5 | \$ 465 |  |
    | :---: | :---: | :---: | :---: |
    | 21 " Black Satin, | ${ }^{6} 4.10$ | 86 | 10 |
    | 432 " Irish Linen, | " 4.45 | 194 | 40 |
    | 86 " Silk Velvet, | ${ }^{6} 78.50$ | 645 |  |
    | 500 " French Merino, | \% 6.75 | 375 |  |
    | 3 Shawls, | " 60.00 | 180 |  |
    |  |  | \$1945 | 50 |

    Hence, we see that the unsold merohandise is worth \$1945 50, which amount we enter on the credit side of Merchandise account in red ink, * and transfer the same immediately to Balauce account. The accounts are now in a condition to close; and we will take them in their order. The first account (after Stock, which is the proprietor's own account) is Cash account. This account represents a resource consisting of cash on hand; the debit side showing the money received, and the credit side that disposed of. We close the account by entering the difference, in red ink, on the credit side, and footing up the sides, drawing double lines underneath. The red ink entry, or balance, is transferred immediately to the debit side of Balanee account. The nezt aceount, Merehandise, shows : $g^{\prime \prime 2}$, and the balance is truns-


    ## PROOASS OB CLOSINA.

    ferred to the credit side of Lass and Gain account. The next, Bills Reoeivable account, is olosed in the same manner as Cash account, the balance being transferred as a resource to Balance aocount. Bills Payable account shows a liability, and the balance is transferred to the credit sidle of Balance account. R. Green's account already bulanecs, and we close it by simply ruling the donble lines. Jos. Murray's account balances, and we close it in the same manner as the preceding account. Expense account shows a loss, and is transferred to the clebit side of Loss and Gain. Myler \& Lee's account shows a liability, and the balance is transferred to the credit side of Balanco aecount. D. Murphy's aocount balances, and we close it by simply ruling the double lines. C. Phelan's account shows a liability, and the balance is transferred to the credit side of Balance account. W. S. R $r^{\cdot}$ 's account shows a resource, and is transferred to the deoit of Bal. e e account.

    We have now the results of all the accounts exhibited under the heads of Loss and Gain and Balance, and if the balances have been properly transferred, these accounts, together with the (unclosed) Stock account, must be in equilibrium. To test this, we next take a Trial Balance of these three accounts, which we oall the

    ## seoond trial balance. Dr. Cr.

    | Stock, Loss and Gain, Balance, | $\$ 350$  <br> 166 85 <br> 5313 15 <br> $\$ 5830$  | $\begin{array}{r}\$ 4500 \\ 340 \\ 989 \\ \hline \mathbf{8 5 8 3 0} \\ \hline \mathbf{4 0}\end{array}$ |
    | :---: | :---: | :---: |

    The balances being properly transferred, we proceed to accom. plish the grand object of closing tbe Ledger, by carrying the net gain from the Loss and Gain to the credit side of Stock account, increasing the investment; but, bad it been a loss, to the debit side, decreasing the investment. The Stock account now contains the capital invested inoreased by the gain, which must, of course, equal the present worth, as shown by the Balance account. We now close Stock account into Balance, which must produce an equilibrium of the Balance account; and complete, in that account, the record of resources and liabilities.

    The object of closing the Ledger accounts is to restore the proprictor's account to the same relative position towards the business whioh it ocoupied at the commenoement ; viz., as showing the not investment, or net interest of the proprictor.

    ## ORDER OF OLOBING.

    ## ORDER UN CLOSING.

    The student will do well to observe particularly, and to follow out in prnetioc, the following oriler of closing the Ledger.

    First. -Open an account with "Loss and Gain," (if not already opened,) and another with "Balance"; the former to exhibit the losses and gains, and the latter the resources and liabalities.

    Second.-Ascertain from the inventory if any property remains unsold ; and, if so, credit each account for which such property was originally debited with the value of that unsold, making the entry in red ink. "By Balance," and transferrines the amount directly to the debit side of Balance account, making this entry in black ink, "To Merchandise," or "To Real Estate," or any other account from which the amount is transferred. The Ledger accounts will each show, now, one of the four following results; viz., a Resource, a Jiability, a Gain, or a Loss.
    ${ }_{9}$ Third. - Omitting Stoek account, (or Partner's accounts,) commence with the first account in the Ledger. First ascertain which of the above results it shows, and make the closing entry accordingly. If the difference represent a resource or a liability, enter upon the smaller side, in red inle, "To" or "By Balance," as the case may be, and trausfer the amount in black ink to the opposite side of Balance account. If the differcuce represent a gain or loss, enter on the smaller side in red ink, "To" or "By Loss and Gain," and transfer the amount, in the same manner, to Loss and Gain account. Close all the accounts (except Stock or Partners',) and transfer the balances as directed. The Loss and Gain account will now show, on the debit side, all the losses, and on the credit side, all the g:ilins, the differenoe being the net gain or net loss. The Balance account will show on the debit side all the resources, and on the credit side all the liabilities, (excepting the result of Stock or Partners' accounts,) the difference being the real interest or present investment of the proprietor or proprietors.

    Fourth.-'Take at "Second Trial Balance," or a Trial Balance. of the remaining open accounts, Stock or Partners', Loss and Gain, and Balance. If the balances have been properly transferred, the debits and credits of these acoounts, taken together. must be equal.

    Fifth-Close the Loss and Guin account into Stock, or, if it be a partncrship business, into the partners' accounts, dividing the gain or loss according to agreement. The Stock or Partners' aecounts will now show the original investment, increased by the gain, or decrcased by the loss; tho difference being the present

    ## practical exeroises.

    net investment. As the Balanoc account shows the same thing, they must, of course, arree.

    Sixth.-Close Stock acount (or Partners' accounts) into Bal. ance accomnt, which mast equalize that accomnt, it showing now, on one sile, the tot il resoures, and on the other, the total liabilities, and presenting, in the most condensed form, the oxaot present coudition of the business.

    ## PRACTICAL EXERCISES.

    The following memoranda will cumprise each a month's business, and the student is required to write up therefrom all the books represented in the preceding sories. The form and arrangenent of tho books he will of course gather from the exampes given; and he will find no point of dilliculty which has not beon fulty discussed in connection wilh set 1 . These exercises will require bim to study well the form of expression in the Day Book, and the prineiples which govern the Journal, and will affor 1 an excellent test of his proficiency in what he has passed over.

    ## MEMORANDUM I.

    January 2, 1891. I, L. N. Holmes, commenced the Dry good business with the following Resources: 350 yards Elbeuf Cloth, at £1 3; 600 yds. Belgian Linen, at 2s. $6 d . ; 310$ yds. American Cloth, at $10 \mathrm{~s} . ; 212$ yards Cassmere, at 6 s .3 d. ; and $£ 500$ in cash. $-\mathbf{3}$. Bonght of J. Brown, for cash. 100 yde. Indian cotton, at 9d.-4. Sold L. Harris, for cash, 18 yils. Elbent Cloth at $£ 176 ; 16 \frac{1}{2}$ yds. Belgian Linen, at 3s. 6d.-5. Sold L Newton on his note at 30 days. 150 yds. Elbeur Cloth, at $£ \backslash 15$ i.- $\mathbf{E}$. Bo't of H. Simon \& Co., on my nute due Feb. 15, 50 yds. gray cloth, at 12s.-7. Bo't of C. Dery, to be paid on the 18 th instant, 30 yd . Cotton Velvet, at 4s. 3d.-9. Sold E. G. Irvine, on $\%$, 3 j yds. Indian Cotton, at ls. $2 \frac{1}{2} \mathrm{~d}$.-10. Bo't of Bedard \& Jordan, 120 yils. Merino, at 5s. $7 \frac{1}{2} d$. paid them cash, £25; and the balance, at 60 days-11. Bo't of Morgan \& Co., on my note at 40 days, 28 yds. Silk velvet, at £2 $6: 3 \frac{1}{2}$. -12 . Sold D. St. Just. 30 yds. Cotton Velvet, at $6 \mathrm{~s} .9 \mathrm{~d} . ; 40$ yds. Merino, at $7 \mathrm{~s} .6 \frac{1}{2} \mathrm{~d}$. Received in payment, cash, $£ 154 \because$, and his note at 30 days for the balance. -13. Bo't of C. Harkin. on $\%$, 4 doz. Silk Handkerchiefs, at 3s. 6d. -14. Sold W. Dixon, 200 yds. American Cloth, at 12s. 9d.... Received in payment, cash, $£ 2710$, and the balance at 15 days.-16. Paid cash for Fuelyde 2 6.-1\%. Sold B. Morency, at 60 days, 150 yds. Cassimere, at 8s. $3 \frac{1}{2} d,-18$. Sold to Sunily persons, for cash, 5 yds. Cassimere, at 9s.; 6 Silk Handkerchiefs, at 48. 6d.; 80 yds. Belgian Linen, at 3 s .71 . ; on the same day, paid C. Dery, cash, for bal. of account now due, $£ 676 .-19$. Accepted C. Harkin's Draft on me at 8 days, in favor of A. Sykes, tor £8 8.-90. Received of E. G. Irvine, cash, on $\%, \ldots 15 .-{ }^{\circ} \mathrm{E}$. Bo't of S. McGill,
     F. Audibert 140 yds. Elbeut Cloth, at $£ 1185$. Rec'd in pay'm't his note at 15 da ., for $£ 150$, und cash for the bal.-24. Taken from the

    ## PRACTICAI EXERCISES.

    Store for my own use, ' 4 Silk bandkerchiefs, at 3s. 6d.-25. Sold D. N. Patton, 28 yds. Silk Velvet, at $£ 215$. Reoeived in payment. 100 yds. B'. e Cloth, at $15 \%$, and cash for the bal.-98. Received of B. Morency, a 0 yds. Yellow Cotton, at ls. 4d., on $\%$.- $9 \%$. Bo't of D. St. Jnst 30 yds. Scdan Cloth, at $£ 1263$. Gave in payment his note of the I2th instant, for $£ 10$; the balance on $\%$. - 28. Lent F. Audibert, cash, $£ 1210$, until l0th of February next.-80. Paid cash for acceptance favor of A. Sykes, $19 t h$ inst. ; on the same day, received cash of W. Dixon, in tull of $\%$.-31.-Paid cash for sundry oxpenses, £6 104.

    Take the detailed Inventory of the Merchandise unsold on Jannary 31st, and quoted at the cost price, the amount of which is £372 6 \&.
    Net Gain realized on Jannary 31st,
    My Net Capital

    ## MEMORANDUMII.

    February 1, I continue the same business with the followin resources and liabilities, shown in Balance account of last month' Ledger; viz., Resources: Merchandise, as per Inventory, \$1489.33, Cash, $\$ 2982.36$; Bills Receivalle, 1667.50 ; L. G. Irvine's account $\$ 3.70$; 13. Morency's do., $\$ 235.41$; F. Andibert's do., $\$ 50$; Liabib 1TIES: Notes outstanding, for $\$ 436.83$; Bedard and Jordan's acct, $\$ 35$; D. St. Just's do., $\$ 95.25 .-2$. Rec'd cash of F. Audibert, in ful, payment of the oan of last January 2Sth.-3. Gave D. St. Just, an order on 13. Morency for $\$ 60$, to he piil in cash.-4. Paid cash for Insurance in the Royal Insurance Co., on Merchandise amounting to $\$ 1400$, at $1 \frac{1}{4} \%$ premium. - 6 . Sold Kelly \& Shea, at 3 months, $20 \frac{1}{2}$ yds. Elbeut Cloth, at $\$ 5.60 ; 217$ yds. Belgian Linen, at $62 \frac{1}{2}$ cts.; 57 yds. Cassimere, at $\$ 1.70 ; 69 \mathrm{yd} \div$. Indian Cotton, at $22 \frac{1}{2} \mathrm{cts}$.-7. Rec'd cash of L. Newton, in full for his note of $\$ 1067.50$, due this day.-9. Sold H. T'. Perry, 65 yds. American Cloth, at $\$ 2.70 ; 2+\frac{1}{4}$ yds. Gray Cluth, at $S 2.75 ; 20 \frac{3}{4} \mathrm{yds}$. Merino, at $\$ 1.45 ; 31 \mathrm{yds}$. Yellow Cotton, at $32 \frac{1}{2}$ cts. Received in payment his note at 30 days, for $\$ 150$, his order on F. Audibert, for $\$ 30$, and cash for the balance. -10. Rec'd of F . Andibert, in payment for his note of January 23, last, amount'g to $\$ 600$, and due this day; viz., 32 yds Silk Velvet, at $\$ 9.30$, and cash for the balance.-11. Bought of A. Gibb, 218 yds. White Flanuel, at $87 \frac{1}{2}$ cts.; 195 yds. Red Flannel, at 92 cts. Gave in payment my Draft, at sight, on B. Morency, for $\$ 150$; the bal. at 1 month.-13. Sold G. S. Convey on $\%, 7 \frac{1}{2}$ yds. Silk Velvet, at $\$ 10.70$. --On the same day, sold to sundry persons, for cash, $8 \frac{3}{4}$ yds. White Flannel, at $\$ 1.12 ; 37 \frac{1}{2}$ yds. Bhe Cloth, at Sl.20.-14. Rec'd for my portion in my aunt's trequest, 560.75 , in cash, which I have deposited in the Únion Bank.-15. Paid in cash my note in favor of H . Simon \& Co., for \$120, due this day.-17. Sold C. R. McGrath, :ii 8 days, 8 Silk Handkerchiefs, a: 85 cts. $-\mathbf{- 1}$. Bo't of $A$. Lane $\&$ C... 210 yds. Black Watered Silk, at $\$ 1.35$. Gave in payment H. 'J. Pervy's note in my favor, for $\$ 150$; my note, at 40 days, fax $\$ 500$,

    ## PRACTICAL EXERCISEA.

    and cash tor the balance.-20. Accepted A. Gibb's Draft on me at 30 days, in fav. of G. Lafont, firs $\$ 20.15$, in full of his 0 . -21. Paid cash to Bedard \& Jordan, in fill of \%.-2Dis. Paid cash to my shoe maker, in full of his account, sl0.80.-24. Sold for cash $3 \frac{1}{2}$ yils. yds. Sack watered Silk, at $\$ 5.20 ; 18$ yds. Red Flannel, at $\$ 1.10 ; 20^{2}$ yds. Sedan Cloth, at 8i.30.-On the same day, Discnunted my acceptance of 20th inst., favor of G. Lafont, dne in 30 days from date. Paid for face of acceptance, less discuint fur 29 days at $6 \%$, in cash, sale at anction of theived $\$ 108.40$, in cash, as the net proceeds of the Store on the 24 th inst -28 . cash, $\$ 1400$, ant. for which. Rec'd from the Royal Insurance Co., in balance account.

    | Resources. |  |  | LIABILITIES. |  |  |
    | :---: | :---: | :---: | :---: | :---: | :---: |
    | Cash, <br> E. G. Irvine, <br> B. Morency, <br> F. Andibert, Kelly \& Shea, G. S. Convey, Union Bank, <br> C. R. McGrath, | 85657 |  | Bills Payable,D. St. Just,Stock, |  |  |
    |  |  | 70 |  | \$816 | $8: 3$ |
    |  | 25 | $4!$ |  | 35 |  |
    |  | 30 |  |  | 6875 |  |
    |  | 362 | 85 |  |  |  |
    |  |  | 25 |  |  |  |
    |  |  |  |  |  |  |
    |  | \$6727 |  |  |  |  |
    |  |  |  |  | \$6727 | 51 |

    ery, to my Dry, A. J. Hall, have this day joined Produce and Grofollows: Cash on hand, $£ 7553.3 ;$ Ny Resources and Liabilities are as as per Inventory, £48676; W. Notes on hand, £75; Merchandise, Notes outstanding amt'g to £137 10 . Reid owes me on $\%$, £11 15 . and C. Phelan, £61 5.-On the sai I owe Myler \& Lee, £48 12, 40 yds. Irish Linen, at $3 \mathrm{~s} . ; 18$ same day, Sold P. Lewis, for cash, yds. Silk Velvet, at £2 \& 6.-2 Yds. French Merino, at 4s. 6d.; $5 \frac{1}{2}$ Extra Superior Flour, at £1 Bought of F. Morin, fo: cash, 8 bbls. 7 bble. Superfine Flour (Cana 3 bbls. Extra Flour, at 2146 ; 1 ,awlor \& Son on my note dida wheat), at £1 3.-3. Bought of $\mathbf{H}$. £1 10 ; 80 bush. Peas, at 4 s . May 3rd next, 2 bbls. Oatmeal, at Butter, at $8 \frac{1}{2} d$. On the same day; 30 bush. Barley, at $58 . ; 108$ lbs. English Black Cloth, at $£ 1168$, Sold J. B. Davis, on $\%, 12$ yds. 25 yds. Irish Linen, at 2s. 9d.——3s yds. Black Satin, at £1 36 ; April 18, 40 bush. Peas, at 5 - Sold S. Reeve on his note due £1 18; 2 bbls. Superfine Flour, 6 d ; 1 bbl. Extra Superior Flour, at \& Co., at 15 days, 2 dozen Felt ${ }^{2} 16$ 2.-6. Bo't of L. Crawford Caps, at 7s. 3d. ; $130 \frac{1}{2}$ yds. Whit hats, at 4 s . $2 \frac{1}{2} \mathrm{~d}$. ; $1 \frac{1}{2}$ doz. Black

    ## practionl exerotses.

    Maurice for Cash. 1 bbl. Expa Superior Flour, 19.-Un the pame day, Accepted Myler \& Lee's Drafi on me at 10 days. in favor of T. Lebel, for £:37 10.-9. Reo'd of J. B. Davia, caali, on \%, $£ 1210$. -On the same day, Bo't for casio of Smith \& O'Neil. 30 lbs . coffee, at 1s. 2d.; 20 lbs . Tea, at 2 s . 6 d . ; Gions. Brown Sugar, at $5 \frac{1}{2} \mathrm{~d}$. ; 15 lbs . Chocolate, at 1s. 5d.; 24 lbs. Cheece. at 9d.-9. Sold W. Rolland, at one month, 15 yds. Irigh Linen. at 3s.; 30 yds. Red Flannel, at 4s. $4 \mathrm{~d} .-\mathbf{1 0}$. Bo't of A. Hamel \& Co. $54 \frac{1}{2}$ yds. Alpaca, at 28. 1d.; $113 \frac{1}{2}$ yds. Fsench Menino, at 5s. 3d.; 6 Carpet-bags, at 5 s .6 d. ; 3 doz. landkerchief, at 10s. 5 d . Gave in payment my note at 90 days, for $£ 2010$; the bal. on $\%$.-112. Rec'd of W. S. Reid, in cash, £il 15 , in full of \% .-13. Paid £:3 89 in cash for the purchase, oartage, etc., of $2 \frac{2}{2}$ cords of fire-wood.-14. Sold B. Jones on his note at 2 months, 70 yds. Red Flamel, at 4 s . 7d.; 15 yds. Englivh Black Cloth, at $£ 1169 \frac{13}{3} ; 28$ yds. White Flannel, at 4 s . $2 \frac{1}{2 d} .-15$. Sold for cash, 16 lhs. Butter, at $1 \mathrm{~s} . ; 5$ bu. Barley, at 6s. $7 \frac{1}{2}$ !.-16 . Rec'd of J. B. Davis a check on C. Howard, for $£ 171$, payable to the hearer, which was paill me this day, in cash, in full of $\%$. $\mathbf{1 7}$. Sold G. Lemay, 2 bbls. Superfine Flour, at $£ 17 ; 2$ hbls. Extra Superior Flour, at $\mathcal{1} 178$; 1 barrel Oatmeal, at $£ 111 ; 40 \mathrm{lbs}$. Butter, at $10 \frac{1}{2} \mathrm{~d}$. Rec'd in payment, cash, $£ 2106$; the balance on acct.-19. Paid L. Crawford \& Co. cash, in full of $\%$.-20. Paid cash for acseptance favor of T. Lebel, 7th inst--21. Paid cash for a horse and harness, £43 5.--22. Bought of F. R. Meredith, $61 \frac{1}{4}$ yds. Cassimere, at 9s. 3 d . Paid in cash, $£ 18$; the bal. at 20 days.一:3. Bo't of Myler \& Lee, 781 yds. Woolen Carpet, at $2 \mathrm{~s}, 7 \mathrm{~d}$. ; 85 yds . Printed Calico, at $10 \frac{1}{2} \mathrm{~d}$. ; 18 pair Cotton Gloves, at 1 s . 1 r d . ; 15 y yils. Welsh Flannel, at 28.6 d. ; 6 Silk Umi,rellaa, at 18s.91. Gave in payuent, cash, $£ 646$; an order on G. Lemay for $£ 5$; the bal. on $\%$.-24. Sold J. Bell, on $\%$, 1 bbl . Extra Flour, fl 7 ; 5 bush. peas, at (is. 2d.; 3 Felt Hate, at 5s. 6d.-On the same day, Sold to sundry persons for cash, 5 yds. French Merino, at 7s. $4 \frac{1}{2} \mathrm{~d} . ; 1$ carpet.bag, ©s. $4 \mathrm{~d} . ; 2$ Black Caps, at 9 s . 3d.-26. Sold B. Nolan 40 yds. French Merino, at 6 s . $8 \mathrm{~d} . *$ Kec'd in payment 5 bbls. Apples, at $£ 12$; and cash for the balance.- $\mathbf{2 7}$. Sold S. A. Hunt, 15 yils. Alpaca, at 3 . . 4d. ; 1 doz. Handkerchiefs, 12 s . $5 \mathrm{~d} . ; 25 \mathrm{lbs}$. Coffee, at $\mathrm{ls} .10 \mathrm{~d} . ; 10 \mathrm{lbs}$. 'Tea, at 3 s .5 d . Rec'd in payment his note at 40 days, for $£ 3112 \frac{1}{2}$; and cash for the bal. -On the same day, Paid cash, 3s. 6d., for cartage of the above sale. -28. Kecid of Gauthier \& Barry, Montreal, as per their Bill of Invoico of the 26 th inst.; viz., 5 bbls. Rye Meal, at $£ 17$; 50 bu=lhels Indian Corn, at 4s.; 60 bu. Oats, at 3s. 9d., which I paid, pursuant to their order, to J. Rogers, their agent, as follows: $\mathfrak{S}$. Reeve's note due April 17, for $£ 15104$; and sashlh for the balance.-On the same day, Paid cash for freight and ather expenses of the above Invoice, fl 3 7.-89. Paid cash for 1 pair of pants and 1 overcoat for my own use. 25 10.-39. Taken from the Store for Famly expenses during the month; viz.. \& lbs. Butter, at $8 \frac{1}{\frac{1}{2} d .}$; 5 Hes. Coffee, at 1 s . 2 d. ; 3 lbs . Tea, at 2 s .6 d .-On the same day, lont A Sraith, in cash, £10 126 , previous to babancing my accounts, and whose entry I had omitted-31. Paid cash tor sundry expeuses during the month vim., for Rent of Store, $£ 610$; for Family expenses, etc., fol 5 G
    -Un the pame in favor of T . ก $\%$, £12 10. . 30 lus. coffee, ingar, at $5 \frac{1}{d} d$; $-\boldsymbol{9}$. Sold W. yila, Red FlanAlpaca, at 28. oags, at 5s. 6d.; my note at 90 3. Reid, in cash, r the purchase, ones on his note English Black 21d.-15. Sold d. -16. Rec'd le to the bearer, 7. Sold G. LeSuperior Flour, 3utter, at $1012 d$. cet.-19. Paid I for acceptance se and harness, imere, at 9 s . 3 dJ . of Myler \& Lee, Jalico, at $10 \frac{1}{2} d$. nuel, at 2s. 6d. ; h, £6 46; an d J. Bell, on $\%$, 3 Felt Hats, at for cash, 5 yde. Black Caps, at it 6s. Sd. on Rec'd balance.-97. Handkerchiefs, 3s. 5d. Rec'd cash for the bal. the above sale. their Bill of In17 ; 50 bu-hels I paid, pursuant S. Reeve's note e.-On the same above Invoice, overcoat for my Famly expenses bs. Coffee, at ls. Sonith, in cash, hose entry I had ing the month etc. $\boldsymbol{R}$ : 5 -

    Take the detailed Inventory of the Merchandise unsold on March 31el, and quoted at the cost price, the anounl of which is £578 1611.

    Net Loss on March 31
    My net capital $6 / 1$

    $$
    \begin{array}{r}
    30521 \\
    1061604
    \end{array}
    $$

    ## MEMORANDUM IV.

    Aprii 1, I continue my business with the following Resources and Liablitiew taken from my Ledger of the preceding month, minus a few cents; viz., Cash on hand, $\$ 2525.17$; Merchandise as per Inventory, \$2:315.3s; Notes on hand, $\$ 512.30$; W. Rulland owes me $\$ 35$; G. Lemay do., $\$ 8.96$; J. Bell do., $\$ 14.86$; A. Smith do., $\$ 42.50$. Notes outstanding amtg. to $\$ 761.30$. I owe as followa: Myler \& Lee $\$ 88.90$; C. Phelan $\$ 25_{5} ;$ A. Hamel \& Co. $\$ 72.47$; F. R. Meredith $\$ 41.31$. 2. Bo't on my note, at 60 days, of J. Dawson, 5 bbls. Herrings, at $\$ 7$; 3 bbls. Codfish, at $\$ 7.40 ; 3$ bble. Mackerel, at $\$ 7.20$.-3. Bo't for cash $2 \theta$ Shares Montreal Bark Stock, at $\$ 104$. - 4. Rec'd cash in full of \% of G. Lemay, 88.96 .-5. Sold to sundry persons for cash, 5 lbs. Brown Sugar, at 12 cts. ; 10 lbs. Chocolate, at 44 cts.; 24 lbs. Cheese, at 19 cts.-6. Sold P. S. Roberts 30 yds. Irish Linen, at $68 \frac{1}{3}$ cts. ; 12 yds. Black Satin, at $\$ 4.85 ; 20$ yds. Cassimere, at $\$ 2.50$ Reo'd in payment, cash, $\$ 73$; and bal. at 15 days.--7. Sold E. Nolan, 391 yds. Woolen Carpet, at 76 cts.; 40 yds. Furseh Merino, at 831 cts. ; 373 yds. White Flannel, at 90 cts.; 2 doz. Bandkerchieft, at \$3.15. Rec'd in payment, his note at 40 drys, for $\$ 50$; his Order ou Myler \& Lee, for $\$ 26.45$; the balance on cet.-9. Lent G. S. Con vey on his note payable on the 2 2th inst., and without interest, 560 -On the same day, Sold P. Maguire, for cash, 6 Shares Montread Bank Stock, at $\$ 109$ - On the same day, Rec'l cash from W. Rollanit in full of acct.-10. Sold J. M. Lindsay, Richmond, 2 bbls. Extra Superior Flour, at $\$ 12.45$; 2 bbls. Extra Flour, at $\$ 11$; 1 bbl. Superfine Flour, $\$ 6.40$; 1 bbl . Oatmeal, $\$ 8.32$; 8 bm. Barley, at $\$ 1.4: 3 \frac{1}{2}$; 40 lbs . Brown Sugar, at $11 \frac{1}{4} \mathrm{cte}: 4 \mathrm{lhls}$. Apples. :1 7 , ini. Rec'd in payment, 100 bu . potatoes, at 41 sets., and his note at 60 days for the balance,-On the same day, Paid the Grand Trunk for freight of the alove Invoice, in cash, \$2.55.-11. Paid cash to F. R. Meredith, in full for his sale of March 2\%.-12. Sold for cash, $6 \frac{1}{4}$ yds. Engliah Black Cloth, at $\$ 7.72$; 3! yds. Black Satin, at $\$ 6.48$; 35 yds. Silt Velvel, at. 88.65 ; 5 Felt Hats, at \$1.20.-133. Deposited \$800, cash, in the Union Bank-14. Rec'd of P. S. Roberts his note at 90 days, dated the 6th inst., in full of $\%$. -16 . Sold H. Col'ins, at 3 months, 45 yds. Printed Calico, at 25 cts ; 9 pair Cottom Gloves, at $46 \frac{2}{2}$ cts. ; 12 yds. Welsh Clannel, at $72 \frac{1}{2}$ cts.; 5 Silk Umbreilas, at $\$ 4.55,-17$. Accppted byier\& Lee'a note un mo at susys in favorof C. Maynani in full cu' \%. - 18 . Sold N. Graham, 4 bbls. Rye Meal, at $\$ 8.80 ; 45$ bu. Indian Corn, at $\$ 1.10 ; 33$ bu. Oats, at 92 j cts. Rec'd in payment, cash for half of the sale, lams 2 of diec., $\$ 55.10$; the other half, that A, \$56.22, remains due-19 Gare my shoemplaer a ohook for

    ## pratotioal exeroises.

    $\$ 17.28$ on the Union Bank, in payment of his account.-20. Rec'd $\$ 3.4$ in cash for $6 \%$ dividend on 14 Shares Montreal Bank Stock. -81. Rec'd of J. Beaudry, Sorel, 150 bu. Oats, at 60 cts. ; 300 bu. Rye Meal, at 90 cts., which I sold immediately with $\$ 80$ profit, to E. Stephens. Rec'd in payment of the latter, a note at 2 ' days, for $\$ 200$; cash, $\$ 120$; the balance on $\%$. - 283. Bo't fur cash 10 blals. Extra Flour, at $\$ 4.80$; 15 bbls. Fancy Hlour, at $\$ 4.70$; 8 bbls. Superfine Flour, at $\$ 4.60 ; 3$ bbls. Oatıneal, at $\$ 5 .-94$. Lent cash to P. Fremont on his note at 40 days, and without interest, endorsed by A. Sauran, $\$ 65$.- $\mathbf{2 5}$. Rec'd cash of G. S. Convey in payment for his note of the 9th inst., due this day.-26. Sold C. A. Simpson, 8 Shares Montreal Bank Stock, at $\$ 112$. Rec'd in payment, 128 yda. Elbent Cloth, at $\$ 6$; and cash which I deposited in the Union Bank. - 97 . Sold N. O. Day on his note at 2 months, 35 bu. Peas, as 81.13 ; 17 bu. Barley, at $\$ 1.29$; 20 lbs. Coffee, at 30 ots.; 4 bbls. Herrings, at \$7.85.-28. Paid cash for Myler \& Lee's Drath, in favor of C. Maynard, \$62.45. - On the same day, Gave the carpenter an order on N. Grahain for $\$ 5.10$, for repairs of Store Fixturea- - $\mathbf{3 0}$. Sold J. S. O'Brien, 200 yds. Irish Linen, at 90 cts. ; 40 yds. Silk Velvet, at $\$ 9.20$; 12 Felt Hats, at $\$ 1.98 \frac{3}{4}$; 12 Black caps, at $\$ 1.90$. Rec'd in payment, Neil \& Roche's note, at 40 days, for $\$ 240$; cash, $\$ 203$; discount allowed tor the payment in cash, $\$ 3.80$; the bal. on \% $\%$.On the same day, Paid canh for sundry expenses; viz., Taxes and Gas, $\$ 5.63$, Family expense., $\$ 24.35$; Rent of Store, $\$ 26$.

    Take the detailed Inventorij of the Merchandise unsold April 30th, and quoted at the cost price.

    The Merchandise amounts to
    $\$ 2232.35$.
    The Shares of the Montreal Bank Stook, to 624.00 .
    BALANCE ACCOUNT.

    | REbovrces. |  |  | Liabilitige. |  |  |
    | :---: | :---: | :---: | :---: | :---: | :---: |
    | Cash, | \$ 835 | $\because 6$ | Bills Payable, | \$ 840 | 10 |
    | Merchandise, | 2232 | 95 | C. Phelan, | 245 | 00 |
    | Bills Receivable, | 1285 | 45 | A. Hamel'\& Co., | 72 | 47 |
    | J. Bell, | 14 | 86 | J. Beaudry, | 360 | 00 |
    | A. Smith, | 42 | 50 | Stock, | . 4821 | 02 |
    | Montreal Bank Stock, | 624 | 00 |  |  |  |
    | B. Nolan, | 26 | 98 |  |  |  |
    | Union Bank, | 910 | 72 |  |  |  |
    | H. Collins, | 46 | 90 |  |  |  |
    | N. Graham, | 51. | 13. |  |  |  |
    | E. Stephens, | 120 | 00 |  |  |  |
    | J. S. O'Brien, | 147 | 85 |  | 8 |  |
    |  | \$6338 | 59 |  | \$6338 | 59 | $0 ; 8$ blis. Su. - Lent cash to t , endorsed by ayment for lis pson, 8 Shares 28 yda. Elbent n Bank. - 77 . , at $31.13 ; 17$ s. Herrings, at or of C. May. ar an order on 30. Sold J. S. Silk Velvet, at 90. Rec'd in ; cash, \$203; bal. on \%.iz., Taxes and 26.

    unsold April
    232.95
    624.00
    

    # DAY BOOK, JOURNAL, CASH BOOK, BILL, BOOK, COMMISSION SALES BOOK, ACCOUN'I SALES. DAY BOOK, -SETII. 

    Quebec, April 1st, 1871.
    

    ## DAY BOOK,-SET II.

    Qumbic, Aphil 1st, 1871.
    

    ## DAY BOOK,-SET II.

    Quabec, Aphic 5, 1871.
    

    ## DAY BOOK,-SET II.

    Quebec, Aprif. 12, 1871.

    Reoeived infollignce that the Tow boat Levie annk yesterday ut them St. Lawrence river, near 4 "een Island, and han heen delivered over to the Umder. writers.

    The hoat being insured fur $\$ 21500$, we have received in Cash, (which we have tleposited in the National Bank, from the Queliec Ins. Co., nur 4 of same, $\$ 5375$, less Expenses $\$ 110,=\$ 5263$
    Lost the Bal. of our Share of the cost of said Boat, $(\$ 5400+\$ 90-\$ 5265)=225$

    Rec'd per Steamer Anna, from F. J. Ray, Halifax, N. S., to be sold on his $\%$ and risk, 400 blis. Codfish, invoiced $10 \$ 4.50$
    660 " Mackerel, " " 6.50 500 "Herrings, " " 5.00
    Paid Freight and Insurance, in cash,

    Bought of A. Stars \& Co., per Check on National Bank,
    30 Shares National Bank Steck, a $\$ 48$ per S.
    16
    Sold B.W. Hardy, for cash, from L. S. \& Co.'s Consigument, 4200 His. Butter, $10 \$ .16$ 800 buish. Corn, " 80 8672
    $\qquad$
    Closed L. Shaw \& Co.'s Consignment, and rendered then an Account Sales of the same.

    Our charges for Storage and Adver., $\$ 20.00$ Our Comisission on Sales, 64.13 L. Shaw \& "os.'s net proceeds, 2152.87

    Boughi, at Aucion, of steamboat Scel, for

    ## DAY BOOK,-SET II

    Qurbec, Apiti, 17, 1871.

    Gave our Note, @ 40 days, to the Quehec Ins. Co., for Ins. on our Share of the Steambont Sorel, for $\$ 6500, \infty 2 \%=8180$, and Pulicy 81 .

    Shipped per Steamboat Alfred, and consigned to Price \& Co., Kingston, Ontariu, tu be sold on unr \% and risk,
    50 bbls. Pearl Ashes, from Store, valued D $\$ 7$
    4 hhds. 4400 lbs Sugar, " $6 \$ 350$ (a) S.09

    600 bbls. Mackerel, (F. I. R's Consign. 396 ment) a $\$ 7.50$

    Paid cash for Ins.-Premium and Policy, | 4500 |
    | ---: | ---: |
    | 20 |

    The Steamboat St. Alban; on which we shipped guods to McLean \& Co., Montreal, got on fire at her arrival in purt, and our goods, which were resc: i? in a damaged condition, and upon which there was no insurance, were sold at auction tor
    casl.,
    "
    Shipped, per Steamboat Glory, to W. S. Kelly,
    Three Rivers, pursuant tu his order, and for his $\%_{c}$, 50 bbls. Superfine Flour, o $\$ 6.12 \quad 366$ 50 " Extra Mess Pork, " 11.00 550-916
    $\qquad$

    Quebeg, April 20, 1871.

    Sold E. G. Henry, for cash, 400 bbls. Codfish, (F. J. R's Con.) $\$ 52000$ 500 " Herrings " " " 63000 "

    Closed F. I. Ray's Consignment, and rendered him an Account Sales of the same.
    Our charges for Storage and Advertising, 50.00 Onr Commission on sales, 237.50 F. I. R. net proceeds, remitted in cash, 9062.50

    Sold to J. L. Fraser, 25 Shares National Bank Stock, at $@ \$ 52$
    Received payment as follows:
    Canceling for our indebteduess to him,
    $\$ 250.00$
    Interest on asme allowed by us,
    1.50

    Cash for the balance,
    1048.50-1300

    Received from G. Doyle \& Son, Ottawa, to be sold on their $\%$ and risk, 1000 bush. Wheat, 800 " Oats, 200 bbls. Tallow,
    Paid Freight in cash,

    Sold our Honse, No. 24 St. Louis street, to R. Fisher $\&$ Son, for
    Offeet, as part payment, the am't which we owe them on $\%$,
    $\$ 2562.60$
    Rec'd their Note at 18 months,
    secured by Mortgage on Property, for
    5000.00

    And Cash, for the balance, $\quad 437.40-8000$
    25
    Sold E. F. Andrews, at 40 days, on $\%$,
    200 bbls. Tallow, (G. D. \& Son's Cons.) $@ \$ 8$,

    ## DAY BOOK,-SET II.

    Quebec, April 26, 1871.
    Paid our Note, favor of Barclay \& Co., due April 14, by Check on National Bank, $\quad \begin{array}{r}\text { due April } \\ \$ 8750.00\end{array}$ Interest due on eame to date, $\begin{array}{r}\$ 8750.00 \\ 8.75 \\ \hline\end{array}$

    Paid cash for our Note of the 4 th inst., at 40 days, favor of L. R. O'Connor \& Co., Face of Note,

    Cash paid,
    Discount off to May 17,
    1993.34

    29
    Received advice from Price \& Co., Kingston, of the sale of 50 bbls. Pearl Ashes; 4400 lbs. Sugar; and 600 buls. Mackerel, shipped them on the 18th inst.
    Net proceeds remitted in cash,
    30
    Sold O. S. Dion, for cash,
    1000 bush. Wheat, (G. © \$1.40
    . D. \& Son's Consignment)
    "
    Closed G. Doyle \& Son's Consignment, and rendered
    them an Account Sales- 800 bush. Oats remaining unsold, Our charges for Storage and Adver., Our Commission on Sates,
    G. Doyle \& Son's net proceeds

    30
    F. O'Reilly has drawn cash for private use,

    Paid sundry expenses this month, in cash,

    Quebec, April 1st, 1871.
    Dr.
    Cr.
    
    *The term "Mortgage Payable" is but another name for Bills Payable: the adoounts may be kept separate or together. Ihere is a distinction between a promiserg note and a mortgage on real estate; and the majority of business en would profer to have that distinctiun preserved in their acoounts.

    Cr.
    

    Bills Payable: the istinction between a majority of business acocunts.

    | National, Bank <br> Dr. <br> To Tow-boat Nestor Stock. | \$4200 | $00 \\|$ \$ ${ }^{\text {¢200 }}$ |  |
    | :---: | :---: | :---: | :---: |
    | Merceandise Dr. To Sundries. <br> To Bhals Payable. <br> " National. Bank. <br> "L. R. o'Connor \& Co. | 13700 | $\left.\begin{array}{\|c\|\|} 00 \\ \\ 6000 \\ 3700 \\ 4000 \end{array} \right\rvert\,$ |  |
    | Cask <br> Dr. <br> To National. Bank. | 4000 | 400 | 00 |
    | Tow-boat Levis Stock Dr. <br> To Cash. | 9000 | ${ }^{\circ}$ | 00 |
    | Shipaent to Montreal. - Dr. <br> To Sundies. <br> " Merchandise. <br> " Cash. | 300400 | 3000 00 <br> 4 00 |  |
    | Real Estate Dr. To Sundries. <br> To Tow-boat Nestor Stock. <br> " National. Bang. <br> " Mortgage Payable. | 700000 | 2200 00 <br> 1500 00 <br> 3300 00 |  |

    * "Shipment to Montrea!" is a new aceount, opened to represent a particular enterprise, and although it relates to merchandise, it is distinct from the merchandise in Store, and is given this new name to mark that distinetiom the merthough we had sn!d our morchandise for $\$ 3000$, and immediately invested the same in this adventure. The shipment is debited with its cosh and merehandise
    and cash oredited.

    Quebed, april 9, 1871.

    Dr.
    Cr.
    

    * The account here opened-S. Shaw \& Co.'s Consignment-is preoisely the pame, in effeet, as would be an account with L. Shav \& Co., although it really represents the property of that firm, whioh we receive, as commission morchants, to sell. Instead, therefore, of debiting the Consignment account with the value a the property, we dobit it only with what it has eost us.


    ## JOURNAL,-SET II.

    Quebeg, April 16, 1871.
    Dr.
    Cr.
    Cash
    To L. Shaw \& Co.is Cons,
    . Shaw \& Co.'s Consion. Dr.
    To Sundries.
    " Storage \& Adpertisiso.
    " Сommission.
    "L. Suaw \& Co.
    
    owing to L . Shaw is made for the purpose of exhiniting an
    their Consignment aocount the renuit of our business mith books the aet amt. their property, we oan ascertan used washow the facts eon bera so far; and as as net proceeds, which ascertain from this asconnt how inuected with the sale of when its entire cost and be the difference between the sides fre entitled to, The effect of this entry will troeeds are properly shown; in thie case ancount, resulte to the account of L. Shaw \& Co.

    Quebeo, April 19, $1871 . \quad$ Dr. Cit.
    
    (1) Shipment to Montreal is treated precisely as any property or representativo account; baving beed debited with its costs, we now credit it with its proceeds. The difference will be, in this case, our loss.
    (i) Here the goods are not abipped for our account, but for the account of another party who ondered them. This is therefore a regular sale.

    5
    Cr.
    
    operty or representw credit it with its
    for the account of $r$ sale.

    ## JOURNAL,-SET 1 .

    Quebeg, April 23, 1871.
    Dr.
    Cr.
    G. Duyle \& Son's Consign. Dr. 24
    Sundries Dr. To Real Estate. R. Fisber \& Son Mortgage Receifable Casa

    | E. F. Andrews | 25 |  |
    | :---: | :---: | :---: |
    |  |  |  |
    | To G. Doyle \& Son's Cone. |  |  |

    
    (1) Notes, like cash, ought alwaya to be debited and credited with the value written upon them. If they are really worth more or less than this expressed the faco of the note is $\$ 8750$. but in some other account. in the presentcase, upon it, is $\$ 8758.75$; and this is the or:ount we the note, with the interest due cancel it. We therefore debit Bills Payable with are obliged to pay, in ordor to est with the amount we pay for Interest.
    (2) In this oase, the note is really worth less than ite expreased value, as we are obliged to pay for it only $\$ 1993.33$, which is $\$ 6.88$ less than its face. Wo
    here debit Bills Pyyub down, and credit Cash for the ane face of the note, aocording to principles laid that boing the amount produced by Interest, or by paying our note differenee, due.

    ## JOURNAL, --SET II.

    Quebed, Aphi. 29, 1871. Dr. Cr.
    

    We have omitted the Ledger in this Set, believing the student to be fully capable to post the accounts without assistance of this kind. We shall adhere to this plan hereafter, except in cases where some new principle or application may be otherwise more clearly shown

    The student will make his Ledger conform to the following Trial Balance, and close it in accordance with the Statement which follows

    TRIAL BALANCE.
    
    ving the student ussistance of this , except in cases otherwise more
    o the following the Statement
    

    INVENTORY OF UNSOLD PROPERTY.

    > Merchandise,
    > fot Tow. boat Nestor Stock,
    > Real Estate,
    > $t$ Steamboat Sorel Stock,
    > 5 Shares National Bank Stock, $a \$ 50$,

    ## STATEMENT,-SET II.

    ## LOSSES AND GAINS.

    |  |  |  |
    | :---: | :---: | :---: |
    |  |  |  |
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    ## ReSources and liabilities.

    

    From the forcyoing statement the student will be enabled to close up this Ledger with certainty and to produce the results in bis Balance account which are exhibited under the head of Rosources and Liabilitics there shown.

    ## CASH BOOK,

    ## Cash Receiven.

    

    ## BILL BOOK,

    Bidl.s

    | No. | $\begin{aligned} & \text { When } \\ & \text { recer, } \end{aligned}$ | Drawers. | In whose favor. | For what received. | Where pay. |
    | :---: | :---: | :---: | :---: | :---: | :---: |
    | 2 | $\left.\begin{array}{\|c\|c\|} \hline 187 \\ \lambda_{\text {pral }} & 1 \\ 1 \end{array} \right\rvert\,$ | L. Clint. <br> H. W. Cooper | F. O'Keilly. | Investment. | Our Office. |

    Bidis

    | No |  | Drawers. | In whone favor. | For what givell. | Where payable. |
    | :---: | :---: | :---: | :---: | :---: | :---: |
    | 1 | -18:11 | I, Biprue. | Biarolay fe Co. |  |  |
    | 2 | A! | Ourselves. | L. R. O'Connor \& Co. |  | Quebse. |
    | 3 <br> 4 |  |  | Quebee Ins. Co. |  | " |

    ## -SET II.

    ## Casil Disbursem.

    ## ital. $\$ 19600$ date. $\quad 1312$ ction. dale. 104850 <br> e. 43740 <br> us. date. <br> 1400

    

    ## Reqeivable.

    | I):Ite of Note. | 'finio to run. | When due. | Amomit. | Remarks. |
    | :---: | :---: | :---: | :---: | :---: |
    |  |  |  |  |  |
    | April 23 <br> Apre  | 60 days. <br> 60 days. | Nay $2 \frac{2}{5}$ June 18 18 | $* 4230$ 60 <br> 1020 00 | Paid April 17. |

    

    ## COMMISSION SALES

    Dr. L. Shaw \& Co.'s
    
    

    Dr.
    G. Doyle \& Son's
    

    The calculation for averaging this aocount, to asoertain when the uet proceeds

    Consignaent.

    | $\overline{1871} \Lambda_{\text {prill }}$ | Br Buals Receivabie, Sold H. W. Cooper on | 1 |  |
    | :---: | :---: | :---: | :---: |
    |  |  |  |  |
    | " 10 | " Casb, Sold B. W. Hardy. <br> 600 ku . Wheat, $\propto \$ 1.70$. 4200 lbe. Butter, $0 \$ .16 \quad \$ 672$ 800 bu. Corn, $\quad .80 \quad \underline{ }$ | \$1020 | 00 |
    |  |  | 1312 | 00 |
    |  |  | \$2332 | 00 |
    |  | Constanment. |  |  |

    
    
    are due, will be found in the Commeroial Arithmetio from p. 266 to 279.

    ## ACCOUNT SALES,-SET II.

    ## Account Sales of $\left\{\begin{array}{ccc}600 & \text { hi. Wheat, } \\ 801 & \ddots & \text { Chrn, } \\ 1200 & \text { lis. } & \text { Butter, }\end{array}\right\}$ on $\%$ and risk o? <br> L. Shaw \& Co.

    

    Sales of Goods by order and for $\%$ of F. I. Ray.

    | $\overline{\overline{1871} \mid} \begin{aligned} & \text { April\|l } \end{aligned}$ |  | Taken to our account, | 9500 | 00 |
    | :---: | :---: | :---: | :---: | :---: |
    |  |  |  |  |  |
    |  |  | Sot 600 bbls. Mackerel, $\bigcirc \$ 7.50$ \$4500.00 |  |  |
    | " 20 |  | Sold for Cash. <br> 400 bbls. Codfish, $a s 5 \quad 2000.00$ 3000.00 $\qquad$ Charges $\qquad$ $-$ |  |  |
    |  |  |  |  |  |
    |  |  |  |  |  |
    | $\begin{aligned} & \text { " } \\ & \text { "، } \end{aligned}$ | $\left\|\begin{array}{l} 13 \\ 20 \\ 61 \end{array}\right\|$ | Paid Freight \& Insurance, in cash, $\quad \$ 150.00$ Storage \& Advertising, |  |  |
    |  |  | Commission, $21 \%$ on $\$ 9500, \quad 237.50$ | 437 | 50 |
    |  |  | F. I. Ray's net proceeds remitted | \$9062 | 50 |
    |  |  | E. E. Byrne \& O'Reilly, Quebec, April 20, 1871. Per J. Maguire. |  |  |

    PRACTICAL EXERUISES, -SET 11.
    Sales of $\left\{\begin{array}{c}200 \mathrm{bbls.} \text { Tallow, } \\ 1000 \mathrm{bu} .\end{array}\right\}$ Wheat. $\%$ of $G$. Doylo \& Son.
    

    ## MEMORANDUM.

    May 1, 1871, A. J. Hall and R. S. Griffin have this day entered into coprtnership, under the style and firm of Hali \& Gmiprin; in the prosecution of a produce, grocery, domestic shipping business, and for buying and selling Bank. Stocks, etc. They art to furnish the Capital as agreed. A. J. Hall is to share one-third, and R. S. Griffin, two-thirds of the gains or losses. A. J. Hall's Resources and Liabilities are taken from the Balance Account of his Ledger of April, Memorandum IV, p. 30. R. S. Griffin's Resources and Lia bilities are as follows: Cash, $\$ 8755.41$; Merchandise, per Inventory, $\$ 3125$; Bills Payable, per B. B., \$2238.36.-2. Sold L. Parkins $68 \frac{1}{4}$ yds. Merino, at $\$ 1.32$; $5 \frac{1}{2}$ yds. Silk Velvet, at $\$ 8.50 ; 59 \%$ yds, Black Cloth, at $\$ 5.80$. Received in payment, cash, $\$ 200$; vhis yot at 40 days, for $\$ 150$; the balance at 3 months. On the same note Sold J. Morgan \& Co., 150 obls. Mess Pork, at $\$ 9.50 ; 100$ bble day, 20000 lbs., at $6 \frac{1}{4}$ cts. Rec'd in paymerk, at $\$ 9.50$; 100 bbls. I ard, at 6 cts. ; R. S. Griffin's note, their fent, 14 hhds. Sugar, 15400 lbs., commencing business, due 20th their favor, assumed by the Firm at sale and for discount on 29 th inst.. for $\$ 1500$; and cash for bal. of for 27 days is $\$ 6.75$.-8. Gave $\$ 7.75$. Disc't on R. S. Griffin's note Hall's note their favor, due the $H$. Lavlor \& Son, in payinent of $\Delta$. J. cash for the balance, fle this day, 30 bush. Oats, at 80 cts. ; and Gritia's nute, favor of Talbis On the same day, paid in Cash R. S. mencing businesm, dated Fobru Smith, assumed by the Firm at comAnut of Note, $\$ 738.36$. Thebrusry list, at 9 J days, with int. frow date. 44.-On the same day, Bo't of 0 or 93 days (includ. grace) an'ts to $\$ 11$. fine Flour, at $\$ 4.25$; 100 of C. Lawrence, 12.5 bbls. Extra SuperMese Beef at $\$ 11 ; 100$ bble Extra Mess Purk, at $\$ 9 ; 200$ bblig.

    ## PBACTICAL EXEROISE8,--SIET II.

    Hams, at :16; 50 bbls. Pearl Ashes, at $\$ 4.30$. Gave in payment, 3 bbls. Codfish. at $\$ 3.60 ; 100$ bushels Potatoes, at 48 as.: 14 hhds. Sugar, $15400 \mathrm{lbs} .$, at $7 \frac{1}{2}$ cts. ; and cash for the balanne.-4. Shipped per Stommer Prince Arthur, and consigned to Blanchard \& Kelly, Halitix, to be sold on our $\%$ and risk, 125 bbls. Extra Superfine Elour, at $\$ 4.25 ; 200$ bbls. Mess Beef, at $\$ 11 ; 15$ bbls. Fancy Flour at $\$ 4.70$. Paid drayage in cavh, $\$ 11.25$. Passed our note, at 30 days to the Quebec Insurance Co., for $\$ 2800$, at $1 \frac{1}{4} \%$.- 5 . Rec'd of S. A. Hunt, in payment of his note of March 27, amonnting to $\$ 14.2$. due on the Eth inst. ; viz., 2 bbls. Herrings, at $\$ 6$; and cash for the balance.-7. Paid cash for repairs of Sture, $\$ 25 .-0 n$ the same dar. Bought of J. S. O'Dowd \& Co. on $\%, 200 \mathrm{bbls}$. Mess Beef, at \$11.122.-On the same day, Shipped per Steamer Champlain, Capt. Bellean, and consigned to R. J. Wilson, St. John, N. B., to he sold un our $\%$ and risk, 50 hbls. Pearl Ashes, at $84.30 ; 200$ bbls. Mess Beef, ai $\$ 11.121$. Paid cash for drayage, etc., $\$ 7$; aleo to the Moutreal Insurance Co., for Ins. on $\$ 2430$, at $17 \%$ and Policy $\$ 1 .--$ 8. Thec'd of E . Stephens, in full of \%, his note at 30 days, fur $\$ 100$; and cash for the balance, $\$ 20$.- D. Discounted, at the Union Bank, Heil \& hirche"s note, favor of J. S. O'Brien, for $\$ 240$. Diset. for 35 dsys, $\$ 1.40$; exsh received, $\$ 238.60 .-10$. Paid C. Phelan cash in full cf $\boldsymbol{q}_{j}$-11. Rec'd peï Grand Trunk R. R. from Fisher \& Lee, Torontc, Mise., previously ordered by uE, viz., 3) hhds. Cuba Molasses, 3000 gals. at $25 \mathrm{cts}$. ; 30 hbds . CubaSugar, 30750 lbs at $4 \frac{1}{\mathrm{j}} \mathrm{cts}$. Pa:d in cash for freight, drayage, etc., $\$ 96$.-18. Bought for cash of R. Lyons \& Co., their Bill of Exchange on Hamel \& Norris, Torontu, and remitted the same this day to Fisher \& Lee, in payment of am't due them, $\$ 2133.75$. Paid $\frac{1}{4} \%$ premium for the bill.--14.' Bo't of C. L. Murray, on our note at 4 mos., 2500 bu. Red Wheat, delivered on board the Steamer Victoria, Capt. Barry, at $\$ 1.03$ per bush., and fhipped the same to N. C. Moreau, Picton, to be sold for our \% and risk. Issued our note, at 15 days, to the Quebee Insurance Cn., for Iuf, no $\$ 2 f(8.61$ at 11 \% and for Policy \&1.-15. E. Stepleme note for $\$ 20 n$ is due ard not paid.-16. Renpwed B Jonef' mote for \$198.06, now due. Rec'd his new note at 141 days, for $\$ 150$, and cash for the bal. and 144 days int. at $7 \%$.-17. Sold to Carroll \& Samson, 20 hids. Cuba Molasses, 2000 gals., at 27 cte.; 100 hbls. Prime Beef; at $\$ 9 ; 100$ bbls. Mess Beef, at $\$ 11.50$ Rec'd cash in part, $\$ 1295$; their note at 60 days, for balance, including disconnt, \$1308.74 The disc't on the note is for 63 days.-15. Accepted J. S. O'Dowd \& Co.'s draft on us, at 30 days' sight, favor of E. L. Tessier, for $\$ 1000$-19. B. Nolan lras this day renewed his note, favor of A. J. Hall. for $\$ 50$, assumed by the Firm, by another note for the came amt. and time, endorsed by J. Kerwin, and paid cash for 43 days' int. on the $n \in w$ note, 36 cts - $\mathbf{2 1}$. Bo't of H . Colline, 120 bols. Middlinge, at $\$ 4.20$; 60 lbls. Rye Flour, at $\$ 3.60$. Gave in payment, 35 bbls. Mess Pork, at $\$ 10$ : our check on the Union Bank, for $\$ 250$; hal. on \%:-2:3. Shipped per Steamer Laval, to S. Larue \& Co., Gaspe, for their $\%$, ant pursuluant to their order, 150 bbls . Mese Beef; at $\$ 11.50$. Paid cash for drayage, 84.75 .-24. Sold to ndry persous, for cash, 3 Larrels Herrings, at $\$ 7.50$ : 3 bble. Mackerel, at 88.40 ; 10 bbla.

    ## PRAOTLGAL RXEROISES,-8ET H.

    Middlings, at $\$ 5$; 1 piece, 32 yds ., Elbeuf Oloth, at \$7.-85. Rec'd intelligence that the Steamer Victoria, on which we made a Shipm't on the 14th inst., was wrecked in the Gulf of St. Lawrence on the 20th inst.,-Steamer and Cargo, total loss.--96. Discounted our ao ceptance of the 18 th inst., at 30 lays' sight, E. L. 'Tessier's favor, amt'g to $\$ 1000$. Discount for 25 days at $6 \%$, on $\$ 1000$, is $\$ 4.17$. Bal. paid in cash.-28. Paid R. S. Griffin cash for private use, $\$ 200$. -On the same day, sold as follows: to C. E. Panet, on $\%, 3 \pm 2$ yds. Red Flannel, at 80 cts., and $2 \frac{1}{4}$ yds. Black Satin, at 85 ; to N. Blake, on an order of J. B. Davis, 394 yds. Woolen Carpet, at 60 cts.; 8 4 bls. Superfine Flour, at $\$ 4.80$.-On the same day, Sold 'T. A. Bardy, 4 Shares of the Mantreal Bank Stock, at $\$ 106$. Rec'd in payment, 80 bbls. Gray Apples, at $\$ 5$; and cash for the bal.-29. The Quebec Insurance Co. has failed, and is able to pay but 10 cts. on the dollar 10 of indebtedness. Accordingly, we have received from the Assignees 10 \% on the am't of our Ins. on shipni't to Pictou of 14 th inst., per Sthe 20 ther Victoria, which was wrecked in the Gulf of St. Lawrence on which we inst. Amount insured $\$ 2608.6$ ] at $10 \%=\$ 260.86$, for cash for balancel our note of 14 th inst., at 15 days, $\$ 33.61$; and R. J. Wilson, St. John $N$ same day, reocived an Account Sales from the 7th inst. Net proceeds of Pearl Ashed and Beef sent him on by them, on Viger \& Roy, at sight (for Rec'd also a draft, remitted paid in cash $\$ 1500$.-30. Rec'd an A part proceeds) which has been \& Kelly, Halifax, of 200 bbls. Mess Beef beunt Sales from Blanchard of 4th inst. Net proceeds, $\$ 2380.86$. - On thonging to ship't to them dry persons for cash, 15 lbs . Brown Sugar the same day, sold to sun. at 30 cts ; 44 lbs . Butter, at 18 cts . 5 bur, at 10 cts ; 5 lbs . Chocolate, 3 bbls. Beef Hams, at $\$ 18 ; 2$ bbls. Extra Superior Forn, at 90 cts.; Laborers, $\$ 38$.

    ## INVENTORY OF UNSOLD PRUPERTY.

    Merchandise,
    Shipment to Halifax, balance of Mdse., Shares of the Montreal Bank Stock,

    The net losses, May 31, am't to Of which A. J. Hall's third is And K. S. Griffln's two thirda, A. J. Hall'4 capital is R. S. Gritlin's capital is
    
    \$1477.22
    492.41
    384.81
    4328.61
    8457.23

    ## SET III.

    ## JOURNAL DAY B00K,

    # INVOICE BOOK, SALES BOOK, COMMISSION SALES BOOK, ACCOUNT SALES, 

    FORMS OF NOTES, DRAFTS, LETTERS, ETC.

    ## PARTNERSHIP BUSINESB.

    Remank.-The Seta of books thus far shown in this work, have all been conducted upon the Ivalian method of hittorical Day Book, with separate Journal. We did 30 on account of its greater simpliciry, and not to distract the mind from more important considerations which it was neceseary to inforce. The student being now more thoroughly grounded in the science, we shall henceforth give a little attention to the more practical forms in use, and to a greater variety of entries than heretofore. We wish him particularly to note the peculiax form of the Journal Day Book introduced in this Set, that he may be able to express, in this manner, any conceivable transaction, combining all the essential points of the separate Day Book and Journal. Where mone severely practical forms-for the purposes of condensatiou-are not in use, the Journal Day Book meets with great favor, as being both plain and practical.
    In the transactions of this Set, we have introduced a new feature; vis., Mdse. Co. transactions. It will, of course, be understood that by "Merchandise Companies" is meant the temporary copartnerships existing between the consignor and consignee, having reference to the sale of particular consignments of merchandise. The nature of this species of copartnership differs from that of a general copartuership only in its duration, and the manner of conducting its sales. In Mdse. Co. business, one of the parners--the consignee-is the commission menchant, and, in that capacity, receives and disposes of the property
    whe would of a simple conssgnment; the only difference being that he is interested in the gaine and losses. The two methods given in this Set, and which are fully illustrated, differ only as regards the opening and closing entries. In the flrst method-exem, lified by of the property is respo"-the principle rengnized is, that the holder Lortie \& Bro. an inveice to for it. Thus, when we receive from C. A" with the invoice and expenses, and joint $\%$, we debit "Mdse. Co. cost of the invoice, thus mpenses, and credit the consignors with the as though it were all our own. Thrselves responsible for the property the same principle, will be to debite consignor's entry, if recognizing chandise. In the second med us for the entire cost of the meroroner of the property is rethod, the principle recognized is that the C. Lortie \& Bro., mise. to besponsible. Thus, when we receive from A" with our own share only sold on joint \%, we debit "Mdse. Co. or's entryy in this case, if made and credit the consignor. The consigndehit us for our share, and "Shit correspond with ours, would be to share.

    Where there are more than two parties interested, if the accounts are kept by the first method, the consignee should, as before, debit the Mdse. Co. account with ite entire cost-invoice and expenses-and credit the consignor with their (the consignee's and consignor's) joint share, and any other party or parties with his or their share. The consignor would, in such a case, debit the consignee with their joint share, and each of the other parties with his or their share. The other parties would, if making an entry to correspond, debit the consignee and credit the consignor each for his own share.
    Where there are more than two parties interested, and the accounts are kept by the second method, the consignee should dehit "Mdse. Co." account for his own share and all the oharges, and credit the consignor for his (the consignee's share). The consignor, on the other hand, should debit each of the parties for their respective shares, and "Ship't in Co." for his own share. Er their respective shares, and debit "Shipment in Co.," and credit Each of the other parties should ohare.

    ## JOURNAL DAY BOOK,-SET III.

    Quebec, Mat 3rd, 1871.
    understood that y copartnerships reference to the ne nature of this al copartnership sales. In Mdse. the commission of the property

    ## IMISSION

    LES,

    RS, ETC.

    work, have all Day Book, with rimplicicy, and rations whieh it dore thoroughly ille attention to ariety of entries e peculiar form he may be able tion, combining Journal. Where ndensatiou-are favor, as being I a new feature; popert

    ## 2 JOURNAL DAY BOOK,-SET III.

    Quebec, May 3rd, 1871.
    
    (1) Thero its aupposed to be two columan for dollaris and ceantr-ruded lines for the inpor colucan are not girom, in the preenat instanse, for ment of reom, ?

    Qdebeio, May 7, 1871.
    

    Queref, Mat 12, 1871.
    
    

    Quebeo, May 22, 1871.
    

    Quebec, May 26, 1871.
    

    8 JOURNAL DAY BOOK,-SET $I I I$.
    Quebec, May 29, 1871.
    
    III.
    

    JASH.

    ## TRIAL BALANCE.

    

    ## INVENTORY.

    The Mdse, remaining unsold, May 31, 1871, amounts to $\$ 3530.25$.
    
    Balances of their Resources and Liabilities.
    
    

    ## Quebec, May 3, 1871.

    Inventory of Merchandise advanced by R. A Hudon, as Capital :740 lbs. Lard, 1900 "Ham,

    | $@$ | $\$ .10$ | $\$ 74.00$ |
    | ---: | ---: | ---: |
    | $"$ | .13 | 247.00 |
    | $"$ | 3.72 | 186.00 |
    | $"$ | 5.50 | 330.00 |
    | $"$ | 4.50 | 207.00 |
    | " | .15 | 1050.00 |
    | $"$ | 50.00 | 400.00 |
    | $"$ | .80 | 96.00 |
    | $"$ | 5.00 | 110.00 | $\begin{array}{lll}60 & \text { " } & \text { Extra Superior Flour "" } \\ 46 & \text { " } & \text { Fancy Flour, } \\ 50 \text { bags, } 7000 \text { lbs. Coffee, } & " \\ 8 \text { casks Bordeanx Wine. } & " \\ 20 \text { lottles Champagne Wine, " } \\ 22 \text { gals. Cyprus Wine, } & \text { " }\end{array}$

    5.0 110.00

    Quebec, May 1, 1871.

    > Signed R. A. Hodon.
    M. H.

    Invoice of Flour sent per Grand Trunk R. K., and consigned to Mitchell \& Hudon, Quebec, to be sold on our $\%$ and risk:
    

    Ottawa, May 4, 1871.
    S. Waite \& Co.

    7

    Invoice of Merchandise shipped per Steamborat Champlain, Capt. Ricard, consigned to Mitchell \& Hudon, Quebec, pursuant to their order and for their \%, viz. : -

    |  |  | 1500 gal | Coal Oil, | ¢ $\$ .60$ | \$900.00 |
    | :---: | :---: | :---: | :---: | :---: | :---: |
    | 20 |  | 560 " | Linseed Oil, | " 1.00 | 560.00 |
    | 15 | " | Herringe, |  | 5.25 | 78.75 |
    |  |  |  |  |  | 1538.75 |


    | Insurance $@ 1 \%$ on $\$ 1650$, | $\$ 7.75$ |
    | :--- | :--- | ---: | ---: |
    | Drayage, | $\underline{3.10} \xrightarrow{10.85}$ |

    Montreal, May 6, 1871.
    D. C. Peachy \& Son.

    ## INVOICE BOOK, -SET III.

    Quebed, May 14, 1871.

    Quebec, May 14, 1871.
    Mebsre. Mitcreli. \& Hudon,
    

    ## SALES BOOK,-SET III.

    Quebec, May 4, 1871.
    

    ## SALES BOUK,-SET III.

    Qufbec, May 19, 1871.
    

    Involce of Merchandise per Brig St. Maurice, consigned to J. N. Carbray, Three Rivers, to be sold on our $\%$ and risk.
    

    Quebec, May 22, 1871.
    E. E.
    
    nsigned to J. N. and risk.
    
    
    
    

    # Account Sales of $\left\{\begin{array}{lll}80 & \text { bbls. Superfine Flour } \\ 45 & \text { " } & \text { Rye } \\ 70 & \text { " } & \text { Oatmeal }\end{array}\right\}$ for account of 

    S. White \& Co.
    

    Account Sales of Merchandise, on joint \% of C. Lortie \& Bro., and ourselves, each $\frac{1}{2}$.
    

    ## ACOOONT BALES.

    Sales of Merchandise on joint account of G. Quinn a Co.,
    E. Cary \& Son, and ourselves, each t
    Sales of Merchandise on joint account of G. Quinn \& Co.,
    E. Cary \& Son, and ourselves, each $\frac{1}{3}$.
    $\overline{1871}$
    May $\overline{18711}$ May 28 Sold D. C. Peachy \& Son, at 6 months,
    

    ## C. Lottie \&

    
    OHECK-BOOK,-SET III.
    

    ## RECEIPTS, NOTES, DRAFTS, to.

    RECEIPTS.
    (From tramaction of Jan, 31, p. 8.)
    Quebec, January 31, 1871.
    Recetved of Mr. A. J. Hall, Thirty Dollars, in full fur one month's rent of etore, up to date.
    E. R. Trucder.,
    
    (From transastion of Fob. 18, p. 9.)
    Quebec, Febwary 1; 1871.
    Received of Mr. A.J Hall, his note a eixty days, dated this day, for Two hundred \& fity Dollars.
    i Prean

    NOTES.
    (From transaction of May 3, p. 58.)
    $\$ 1500$. 100
    Queliec, April 25, 1871.
    Thirty days after date, I promise to pay to A. J. Hall, or order, Filteen hundred Dollars; value received. Due May 28, 1871.
    P. Racine.
    (From transaction of Feb. 18, p. 9.)
    Quebec, February 18, 1871.
    Sixty days from date, I promise to pay to the order of C. Phelan, at my office, Sixty-two pounds ten shillings, old Ca. nadian Currency; value received. Due April 22, 1871.
    A. J. Hall.

    DRAFTS.
    (From transaction of May 18, p. 61.)
    Outawa, May 15, 1871.
    At eight days sight, pay to the order of J. Raymond, Eleven hundred forty-nine $\frac{30}{00}$ Dolliars, value received, and charge the same to account of.
    S. Whate \& Co.

    ```
    LHTTER B'\K,-SET II.
    ```

    Nons-For the weceptation, Nitchell \& Huthon have writton goross the bllowing words: "Accepted May 18, 1871," under which they have signed.
    (From traneastion of May 20, p. B3.)

    ## $\$ 115$.

    Three Rivers, May 26, 1871.
    At sight, without grace, pay to the orier of Mitchell \& Hudon, One hundred and fifteen Dollars, value received, and charge to account of

    To F. T. Perron, Cashier,<br>J. N. Oarprat. National Bank, Quebec.

    ## BILL OF EXCHANGE.

    £36 56
    $\varepsilon$

    Fifteen days after sight of this our first of exchange (second and third of same tenor and date, unpaid), pay to the order of Mr. D. Saucier, Thirty-six pounds Five shillings Six pence, value received, and charge to account of

    Your obedient servant,

    > 7b Simms \& Devaux, Bankers, Wellington street,

    London.

    ## LETTER BOOK,-SET III.

    Remaris.-This book is used for taking copies of all business letters of importance, written to or reoeived from others. But letters received are ustally filed away.

    We give herewith letters in connection with the transactions of Set III. But we do not submit them as absolute models in their way. It would be as difficult to afford a model of a business letter, that is, one which it would be proper for evory one to copy, as it would for an artist to produce a cast of features that everybody would consider perfect.

    To be able to write a good business letter is no sinall aocomplishment, nor can it be acquired iy studying models, although much aid may be seoured in this way, pertaining to form, arrangement, and even style, if undertaken with no undue surmender of individuality; for a good businese letter shuah be neither more bor less than the transcript of a man's thoughts, or what he would say were he to speak with care and deliberation. As no two men ever think or talk exactlvike, so no two men conld be expected to write alike.

    There are, in business letters, certain qualifications which are equally essential to all, and with reference to which, general instructiona may be given. We will enumerate a few of these points : -1 st Like all other documents in manuscript, a business letter should be, chirographically, well written, so as to commend itself at once to the reader. Neatness and legibility are the chief requisites in a handwriting. 2nd The grammatical conatruction should be faultless; and, o.bove all, no document should be disfigured with misspelled words. 3rd The subject matter should be immediately apparent, stated without circumlocution, and in terms not to be misconstrued. A business document siould be written in brief terms, and yet explicitly.

    There is no qualification which will more surely commend young men to the favor of an employer than rroficiency in Business Correspondence.

    ## (Circblar.)

    G. S. Walls, Esq., Montreal.
    SIR:-
    We, the subecribers, respectfully announce to you that we have formed a copartnership under the firm of Mitcerli \& Eidon, for the prosecution of a wholesale Grocery, Wine Business, and General Commission. We take the liberty of assuring you that all tusiness intrusted to our care, shall receive from us, personally, prompt and faithful attention; in a word, that we will correspond to the confidence placed in us.

    ## Very respectfully, <br> Your obedient servants, <br> Mitceell \& Hudon.

    ## Messi з. Mitchell \& Hudon, Quebec.

    Gentiemen:-In reply to your circular of the lat inst., I heg leave to solicit the favor of your patronage for a general commission businese, and pledge myself for the strict observance of your commands, and faithful parformance of my duty.

    Respectiully yours,
    G. S. Walis.

    ## G. S. Walls, Esq., <br> Montreal.

    Qurbeo, May 4, 1871.

    Sir:-Enclosed we remit to you Bill of Lading and Invoice of Merchandise, amounting to 8575 , which we consign to ynu per Steamboat Quebec, to be sold for our \%. You will do us the favor to use all possible despatch in making sales and rendering account.

    ## Yours,

    Mitceell \& Hedon.

    Messrs. S. White \& Co.,
    Quebec. May 6, 1871.

    ## Ottana.

    Gentlemen:-We have the honor of informing you of the arrival, in good order, of your Consignment of Flour, pursuant to our order, and of which, your favor of,4th inst, gave us ailvice.

    We find it conformable to the Invoice, amounting to $\$ 1018.25$, which we have placed to the credit of your $\%$.

    We beg leave to assure you that we will pay all possitle attention to your orders. Offering you our sincerest thanks, we remain,

    Your obedient servante,
    Mitcrell \& Hudon.

    Messrs. D. C. Peachy \& Son,
    Qubbec, May 7, 1871.

    ## Montreal.

    Gents :-We are in receipt of the goods you consigned to ue, pursuant to our order of 3 rd inst., and of which you gave advice by your favor of 5 th inst. Save a few barrels of Herringe whose quality appears to us inferior, the rest is satisfactory.

    Your account is credited for the amount of Invoice, $\$ 1549.60$.
    Very respectfully yours,
    Mitchell \& Hudon.

    ## Messrs. L. Douglas \& Co.,

    Qubbec, May 10, 1871.
    Gents :-Enclosed, please find Invoice of Merchandise announting to $\$ 1272.68$, which we forward to you per Grand Trumk R. B., pursuant to your order of 4 th inst.

    Be 60 kind as to credit us for the same.
    Truly youra,
    Mitckeli. \& Etoon.

    May 4, 1871. and Invoice of gn to $y$ nil per do us the tavor ering account.

    ## \& Hedon.

    May 6, 1871.
    ing you of the pursuant to our lvice.
    ng to $\$ 1018.25$,
    ray all possitle est thanks, we

    ## nts,

    \& Hudon.

    May 7, 1871.
    :onsigned to us, gave advice by 8 whose quality
    ice, \$1549.60.
    urs,
    \& Hodon.
    y $10,1871$.
    handise amountd Truak R. R.

    ## Messrs. S. White \& Ca,

    Otrava.
    Qrabeg, May 12, 1971.
    Gents :- We acnd you, enelosed, Account Sales of Merehan dise forwaviled to us on 4 Gi inst. The net proceeds, due on June 4 ,
    is $\$ 114 \% .50$.

    Hoping tu be favored with new orders, and being gratefuibfor those already received, we remain, gendemen,

    - Respectfullay yours,

    Mitchell, \&udon.

    ## Messrs. Mitchell Hudon,

    > Quebec.

    Hatifax, May 7, 1871.
    Gentiemen :-In accordance with the agreement made between urs on the 3 rd inst., we ship you to day, per Brig Victoria, sunilry Merehandise amounting, as per enolosed Invoice, to $\$ 355($, to te sold on joint account.

    As these goods are said to be in great demand in your city, perhaps yeu might find it to our advantage to dispose of them at first opporsuning. However, knowing yeur abilities in business, we leave the whole to your somad judgment.

    > Very respectinlhy,
    > C. Lortie \& Bro.

    ## Messrs. Mitchell \& Hudon, Quebec.

    Montrial, May 15, 1871.
    Gravs :-Piease find enclosed, Account Sales of the Merchandise you shipped ne on the 4th inst. Your net proceeds, including Invoice and Gains on Sales, is $\$ 650$, which I bave entereci to your credit.

    > Your abedient servant,

    > G. S. Walis.

    Messrs. M. Blanchei \& Co., Pictou.

    Quebec, May 19, 1871.
    Gevts:-Herein enclosed, you wit find Invoice of Merchandise whieh we sdip you per Steamer Cartier, to he sold on joint \%. We have debited you for balf of the Invoiee, $\$ 644.60$.

    Hoping that you may have fair opportunities to sell advanta. geous!y, we memain, Genthemen,

    > Your humble servante,
    > Mvrcaell \& Hwon.

    ## GETGNR BOQK, - BET III.

    Messrs. Mitakelt \& Hudon.
    Montreal, May 14, 1871. Quebec.

    Gents:-We acoept with pleasure your proposition to join in a Company Speoulation. We, accordingly, ship you, per Schooner Vaudreuil, which is to sail to morrow, Merchandise, as per enclosed Invoice, to be sold in joint account with yourselves, E. Cary \& Son, and ourseives, eaeh one third.

    We have debited you fur $\frac{1}{2}$ of Invoice.
    Wishing you complete success in the sales of them, we beg to subscribe ourselves,

    Very truly yours, G. Quinn \& Co.

    J. N. Carioray. Esq.,<br>Three Rivers.

    Quebec, May 22. 1871.

    Sir :-Youse of the loth inst. is at hand. Your propositions are gratefully acceptec, In accordance therewith, we ship you per Schooner St. Maurice, 40 bags Red Wheat. and 90 bags Oats, as per enclosed Invoice, anomiting to $\$ 310.50$, which we consign to you to be sold on our $\%$ and risk.

    Hoping you wilh stady our best interests, we remain, sir,
    Youry respectfully,
    Mitchell \& Hudon.

    Messrs. C. Lortie \& Bro., Halifax.

    Quebec, May 23, 1871.
    Gentlemen:-We send you enclosed, Account Sales of the Merchandise forwarded on 7th inst. We have been quite successful in the pales of them, and we are of opinion, from actual appearances, that the good market thall contiuue for cometime. If you think advisable to risk a new concignment, we shall be happy to join you in it, or to sell for you on Commission.

    Very respectully,
    Matchell \& Hudor.

    Messrs. Mitcỉell \& Hudon, Quebec.

    Pweroc, May 23, 1871.
    Gents:-Enclosed, please find Account Sales of the Merchandise yeu shipped us on the 19th inst. Your ant proseeds is
    sition to join in ou, per Schooner as per enclosed E. Cary \& Son,
    theni, we beg to

    ## rs,

    ## dinn \& Co.

    May 22. 1871.
    our propositions we fhip you per nags Oate, as per e consign to you
    remain, sir, filly, 4 \& Hudon.

    May 23, 1871.
    unt Sales of the 1 quite successful chal appearances, e. If you think appy to join you

    145,
    \& Hudor.

    May 23, 1871.
    ales of the Mer. net proseeds is

    ## 

    8610.60. The sпавон seens favorable for the sale of the like goods.

    We whall ve happy to joi you again for any reasonable amount.
    Please advise us thereupon, and believe us,
    Truly yours,
    M. Blanchet \& Co.
    whessis. Mitchell \& Huton, Quebac.
    'Rhree Rivers, May 24, 1871.
    Gents :- Yon suall have heard through the newspapers before the receipt of this letter, of the stranding c © the Schooner St. Maurice, near 'Tlbree Rivers, on the 23 rd inst. The cargo was saved, but your Consigment on me heing rather damagen, I thought prudent to dispose of it at anction without delay. Enclosed you wils find Accomt Sales, and Check on Nationel Bank for \$115, as us proceeds.

    Waiting for a new Cousigmment which may prove more successful, I have the honor, Gentlemen, to he,

    Yours respectfully
    J. N. Carbray.

    ## J. N. Carbray. Esq.,

    ## Thrrg Rivers.

    Qtebec, May 26, 1871.
    Sir:-Your favor of the 24th inst. was reived, and the anclosed Check was honored by the National Bank.

    We approve of your proceedings concerning this sale. and beg of you to accept our sincere thanks.

    Believe us ever disposed to honor you with our confidence, Truly yours,

    Mitciela \& Heton.
    Messrs. G. Quinn \& Co., Montreal.

    Quebec, May 28, 1871.
    Gients:-We send your meiosel, Account Sales of your Invoice of Fruita of 21 st inst.

    Hoping you will fird the resalt satisfaetory, we beg to suth ${ }^{\text {scribe }}$ ourselves, Gentlemen,

    Very truly youns.
    bittereat \& Hudin.

    Messrs. L. Douglas \& Co.,
    Qeebec, May 30, 1371.
    Toronto.
    Gents:-We are in receipt of your favor of the 27 th inst., montaining a draft at sixty daye on A. Simus \& Devanx, London, for $\$ 1272.68$, which is placed to your credit.

    Please accept, Gentlemen, the sincere thanks of
    Your obedient servant:s,
    Mrchers \& fiedon.

    Messrs. D. C. Peachy \& Son,
    Quebec, May 31, 1871. Montrec!.

    Gents:-Enclosed, yon wit fud a Dreft at eight days' sight on N. Caron for 8260 , for which yut will ilease to credit us.

    We have the hooor, Ceaser non, to remain,
    Yoms gratefully,
    Mitchell \& Hudon..

    ## MEMOIRANDUM I.

    Sune 1, We, Mitchell \& Hudon, continue our business whe the Revorces and Liabilities taken from our Balance Sbeet p. 66.-2. Received advice from Douglas \& Co., Toronto, that they have purchased, as per agreement, 90 bbls. Extra Flour, to be sold on our joint \%, each $\frac{1}{2}$, and that they have debited us for $\frac{1}{2}$ the cost price which, as per bill, amounts to $\$ 585 .-3$. Shipped per Brig St. Hu bert, and consigned to S. McManus, St. Johns, Newfoundland, to be sold on our $\%$ and risk, produce, (S. B.) amtg. to $\$ 1864$. Qassed our note No. 3, at 6 mos., to the North Insurance Co., for ins. on $\$ 2010$, at $1 \frac{1}{4} \%$, and paid mn cash for Policy, \$1.25.-Rec'd per Grand Trink R. R., from L. Dion, Montreal, Bordeanx Wines (I. B.) amounting to $\$ 120$; and accepted his draft en us, favor Jones \& Co., at 20 days' sight, for the amt. of invoice-4. Gave Merchandise (S. B.) in payment of an order from P. Allard, for $\$ 369.20$. - Exehanged our note No. 5 with E. Cary \& Son's, for our inutual accommodation, each drawn at 30 days, for $\$ 320$; discomnted theirs at the National Bank, and rec'd in cash, \$318.24. Discount was taken for 33 days, at $6 \%$. -5. Bo't on joint acct. with G. S. Walls, each ${ }_{3}, 5000$ lbs. Chocolate, at 25 cts . We are to receive $5 \%$ cmmmission on the sale. Paid in cash for our half, \$625.-6. Rec'd of S. Lewis, in payment of his note No. 1 for $\$ 1000$, due this day, Merchamdise (I. B.) amtg. to $\$ 500$, and cash fom the bal,-7. Rec'd re: Erig Columbia, Capt. Rי"ssel, from C. A. Molson, Limenick, punent to our order and for on $\%$ Mdse. (1. R.) due in Limerick on suce lat next, amounting to $\ddagger$ Gave our bonds to the Custom-house for duties, at 3 and 6 mow., is?

    ## YRAOTICAI, EXERCISEN,—SFT NI.

    \$1440; raid Freight in cash, \$74. Rec'd at the same time by the same Jiry Columbia from C. A. Molson, 50 casks Sicily Wine (I. P.), ant. \$llot, to be sold on his \% and risk. Gave olir bonds to the Custor: house firs duties at 3 monthe, for \$1606.40; paid Freight in
     E. Lowehe, 5 casks Stcily Wine, of C. A. Molson's Consignment (C. S. E.), amtg. to $=60$ - 10. O. Martel's note, No. 2, for $\$ 2000$, is due and not paid. - Shipped per Brig Victoria, consigned to C. Iortie \& Bro., Halifax. Merchandise to he sold on \% of C. A. Mohson's Consignment (C. S. B.), antg. to $\$ 2481$. Paid cash for Freight, etc., 8??.76.-Shipped at the same time by the same Brig, and consignei to C. Lortie \& Bro. to be sold on our \% , Merchandise from our Store (S. B.) amig. to $\$ 258.75$, and an Invoice of Oats (C. S. B.) bo't of G. Morin, at 2 monthe, antg. to $\$ 180$. Paid cash for Freight, etc. 817.fi5.-11. Paid cash to the Quehec Insurance Co., for ins. on $\$ 9$ i00 of our stock, at $1 \frac{1}{2} \%$, policy included, $\$ 1+4$. -Gave in payment of C. A. Molson's draft on us, at sight, for \$3200, favor of Jos. S. Anbert; viz., Merchandise (S. B.) firs ©6013 ; 5 casks wine of C. A. M's Consigmment (C. S. B.), ant. $\$ 720$; and cash for the bal.- $\mathbf{1 2}$. U. Martel has paid in cash, his note No. 2, in our favor, which wen protested, 22000 - Rec'd cash for C. Lortie \& Bro., in payment of Uheir dralt on Lepage \& Garnean, fir $\$ 1600$. Our commisseion at $\frac{1}{2} \%$ is $\$ 8$. Net proceeds in cash, si592.-1:3. Bo't of J. B. Walls, for \% of N. S. Rulertson, and pursuant to his order, shipped per Steames Prussia, consigned to R. Murray. Portland, Mdee. (C. S. B.), anteg. to $\$ 5000$ for which we have given our acceptance, at 40 days, due July 26, for $\$ 5000$. Expenses for loading, etc., aint. to $\$ 156$. Our commission is $\$ 77.33$. - 1 . Bo't at anction, on joint account with $P$. Brady, each $\frac{1}{2}$, Mdse. (I. B.), amtg. to $\$ 9700$. Our $\frac{1}{2}$ purchase is \$4850, for which we gave our acceptance at :30 days, favor of King \& Co.-16. Paid cash for our note No. 1. favor of L. McCord, for $\$ 500$, due tha day.-17. Bo't of Healy \& Cameron, the Brig Masia, for $\$ 10000$, which we paid as follows: our draft at 30 days' sight, on M. Blanchet \& Co., for $\$ 1200$; E. Dunn's note, for $\$ 760$; and our check on National Bank for the bal.-18. Sent per Grand Trınk R. R., to S. White \& Co., Ottawa, pursuant to their order, Mdse. (C. S. B.), of C. A. I's Consignment, amtg. to $\$ 1360$. Rec'd in payment, our note No. 2, in their fivor, for $\$ 1149.30$, and their note at 40 days, for the bal.-19. Paid cash for repairing Brig Maria, 33.10.-20. Shipped per Brig Maria, and censigned to C. A. Molson, Limerick, to be sold on $\mathbf{j}$ nt $\%$ of himself, H. Brook, and ourselves, each $\frac{1}{3}, 10 \mathrm{~T}$. White Sugar from Mdse. Co. E., antg. to \$4850. Pad cash for louling, etc., $\$ 20.60$; gave our note at 2 mos., for ins. on $\$ 5000$, at $\frac{1}{2} \%$. Our commission on 84870.6 ), at $2 \frac{1}{2}$ \% is $\$ 121.764$; our commission for ins., at $\frac{1}{4} \%$ is $\$ 12.50$. We charged for the Freight ly our Brig Maria, s80. H. Arook's $\frac{1}{3}$ is $\$ 1703.28 \frac{5}{4}$; C. A. Molson's $\frac{1}{8}$, \$1703.285 ; and ours, $\$ 1703.28 \frac{5}{6}$. -21. Insured our Brig Maria in the Gult Insurance Co., for $\$ 10000$, at $\frac{1}{2} \%$. together with $\$ 1$ policy, which we have paid in cash. \$51.-28. Reced an Account Sales from I. Douglas \& Co., ot the Flour bought by them on the 2 midinst., on joint of ; the proceeds amonnting to $\$ 897.7 \%$. Our $\frac{1}{2}$ is $\$ 448,85$, and our net gain, $\$ 156.35$.

    ## PRACTICAI. EXERUISES,-8ET III.

    -24. Rec'd of S.,McManus, St. Johns, Newfoundland, Açant Sales of the Mdse. consignelt to lim by Brig St. Hubert. Net proceeds amtg. to $\$ 2120$. Res'd in payment an Invoice of Fish (I. B.) antg. to $\$ 2120$. Paid for f'reight, and other expense., in cash, \$61.34. Cloved our Invoice to St. Johns with a gain of \$229.25.-25. Paid cash for our acceptance of L. Dion's draft, favor of Jonea \& Co., for $\$ 120 .-26$. Sold J. Meranlt 4000 lb . Chocolate from Mdee. Co. D, at 35 cts . Rec'd eash, $\$ 800$; the bal. at 2 mos.-Sold R. Woods, on his note at 30 days, 1000 lbs . Chocolate from Mdse. Co. D., at 40 cts. -27. Closed Mise. Co. D., and rendered G. S. Walls an Account Sales of the same. Our charges for Storage, Advertising, etc., \$23.60; our Commission, is \% on \$1800. G. S. Walls' net gain, $\$ 218.20$. Our $\frac{1}{2}$ net gain, s. . . . . - 28. Rec'd from C. Lortie \& Bro., Halifax, Account Sales of the Mdse. shipped them from C. A. Molson's Coneignment. Net proceeds, $\$ 2962$ for which we rec'd their draft, at 60 days, on Hamel \& Bror., which was accepted.--Taken to our $\%$, at 2 mos., the remaining 10 casks, of C. A. Molson's Consignment, at \$128. Closed C. A. Molson's Consignment, and rendered him an Account Sales of the same. The expenses for Duty, etc., to this day, amt. to $\$ 1725.85$. Our Commission on Sales, at $5 \%$, is $\$ 354.10$; Storage and Advertising, $\$ 12$. Net proceeds due C. A. Moleon, on \$4990.00.-30, Rec'd from C. Lortie \& Bro. an Account Sales of our \&lipment of the 10 th inst. Ej Brig Victoria. Net proceeds, \$84:3. Rec'd also a draft from them. at 10 days' sight on Garneau \& Co. Paid cabh for clerk hire and other expenses, $\$ 104.75$.

    BALANCE ACCOUNT, JUNE 30.

    | Resources. |  | Liablicities. |  |  |
    | :---: | :---: | :---: | :---: | :---: |
    | Bills Receivable. | \$ 441570 | Bills Payable. | \$13266 |  |
    | Cash. | 1418558 | G. S. Walls. |  |  |
    | National Bank. | 1210100 | D. C. Peachy \& Son. |  | 10 |
    | Merchandise. | 12000\|00 | C. L.ortie \& Bro. | 5359 |  |
    | P. Allard. | $569{ }^{20}$ | E. Cary \& Son. |  |  |
    | A. Rinfret. | 30000 | G. Quinn \& Co. |  |  |
    | M. Blanchet \& Co. | $55{ }^{20}$ | C. A. Molson. | 4886 |  |
    | I. Douglas \& Co. | 15635 | G. Morin. |  |  |
    | N. S. Robertson. | 523333 | C. S. Mitchell. | 13500 |  |
    | H. Brook. | 17032285 | R. A. Hudon. | 13531 | 47 |
    | Brig Mariz. | 1000000 |  |  |  |
    | Sh'pt to Limerick. | $\begin{array}{r}1703 \\ 600 \\ \hline 235 \\ \hline 0\end{array}$ |  |  |  |
    |  | 1319 |  | \$52131 | 93 |

    ## MEMORANDUM II.

    Juhe ist, F. Belmont \& L. Moore, this day entered into co partnership, each investing $\$ 15000$. F. Be!mont's investment is on hand. L. Moore's investment is depositel in the Qt.ebec Bank.-S. Bo't of F. Belmont his store for $\$ 18750$. In payment, assumed mortgage on the property for $\$ 13500$, and Interest iue on mortgace to date $\$ 126$; paid cash for the bal. $\$ 5124 .-$ Bo't of Fremont \& Co. on \%, 10 hids. Sugar, 11250 lbs. at 8 cts. : 200 bbls . Thin Mess, at $\$ 13.50 ; 15000 \mathrm{lbs}$. Cheese, at $15 \mathrm{cts.-Paid}$ cash for carpenter's work and painting, $\$ 112.50$.-4. Received from Bennin:- \& Son, Toronto, to be sold on our joint $\%$, and risk, each $\frac{1}{2}, 600$ hbls, Extrit Flour, at $\$ 6 ; 150$ bbls. Prime Pork, at $\$ 14$; paid freight o same, in cash, 8150. -Rec'd from J. Arnold \& Bro., Kingston. to be sold on our joint $\%$ and risk, each $\frac{1}{2}, 5000$ bush. Western Wheat, at $\$ 1.20$ - 5. Sold for cash to H. Merrill, 300 bhls. Extra Flour, (Mdse. Co., A,) at \$7.-6. Sold. N. Harris, on his note at 30 days, 300 bbls. Extra Flour, (Mdse. Co. A.,) at $\$ 7.50$; 150 bbls. Prime Pork, (Mdse. Co. A.,) at \$18.-Closed company sales with Bennir, $\&$ Son, and rendered them an account of the same. Our charges for Storage \& Advertising, $\$ 15$; Commission $2 \frac{1}{2} \%$ on sales $\$ \ldots$; our $\frac{1}{2}$ net gain, $\$ 504.37$; Benning \& Son's do. $\$ 504.38$. -Sent to J'. Arnold \& Bro. to be sold on our joint $\%$, each $\frac{1}{2}$, the following merchandise, bo't on our note, at 90 days, of Jordan \& Sewell, 22500 lbs. Maple Sugar, at 8 cts.; 200 tubs Butter, 14000 lbs., at 15 cts.; 150 bbls. Green Apples, at $\$ 3$; paid insurance $\frac{1}{2} \%$ on $\$ 4500$, in cash. $\$ 22.50$ - 8 . Sold H. Gregory, at 30 days, 5000 bush.! Western Wheat, (Mdse. Co. B.,) at \$1.35.-Closed sales in company with J. Arnold \& Bro., Kingston, and rendered them an Account Sa'es. Our charges for Storage and Advertising. $\$ 30$; Commission on Sales, $2 \frac{1}{2}$ \%. J. Arnold \& Bro's. $\frac{1}{2}$ net gain, $\$ 275.62$; ours do., \$275.63.-9. Sold B. A. Chalmers, 15000 lbs. Cheese, ai 18 cts . Rec'd in payment his note at 30 days, for $\$ 1500$, and Cash, for the balance.-Accepted Benning \& Son's draft on us at 30 days sight, 'avor G. Ross \& Co., in full of their \%. -Rec'd per Stemboat Frontenac, Montreal, from J. D. Roe, to be sold on joint \% of himself, P. E. Unslow, Sorel, and ourselves, each $\frac{1}{8}$, as per contract, 850 bbls. Mess Pork, at $\$ 15$; paid freight, in cash, $\$ 300$. Our and J. D. Roe's $\frac{1}{8}$ invoice, $\$ 8500$; P. E. Onslow's $\frac{1}{3}$ do. $\$ 4250$.-N2. Bo't of Nelson \& Co., $\frac{1}{2}$ Steamboat Europa, for $\$ 15000$. Gave in payment, cash, $\$ 7500$, and onr note at 90 days for the bal.- $\mathbf{1 3}$. Sold L. J. Nolan, Quebec, 850 bbls. Mess Pork, (Mdse. Co. C., at \$17.65. Rec'd in payment his note at 40 days, for $\$ 10500$, and cash for the bal.-Closed Mdse. Co. C., and rendered J. D. Roe and P. E. Onslow each an account of the Salco. Our charges for Siorage and Advertising, $\$ 47.44$; our Commission $2 \frac{1}{2} .6$ on sales, $\$ 375.06$. J. D. Roe's $\frac{1}{3}$ net gain, $\$ 510$ : P. E. Oustur's $\frac{\frac{1}{3}}{3}$ net gain, $\$ 510$; our $\frac{1}{8}$ net gain $\$ 510$. - $\$ 5$. Sold W. J. Lyous, for cash, 10 hids. Sucar, 11250 lbs., at 12 cts.-16. Bo't of Jordan \& Sewell, 30 hhds. Brown Sugar, 30000 lbs., at 9 cte. paid in cash, $\$ 1200$; bal. on $\%,-18$. Paic

    ## PRAQTIOAL EXEROIBER,—8ET TR.

    cash as follows: for cleork hire to 15 th iont., $\$ 75$; to L. Moore, on $\%$., $\$ 225,-20$. B.'A. ('hakmers 1 , is dis. discounted his note ill our favor, du. July 12th; preculfs the note $\$ 1498.60$; discount uff, for 22 days. $\$ 6.40$.-Rec'd of J. Arnod \& Bro., an Account Sales of the Mise. sent them on the 7th inst, to be sold on our joint \%. Our $\frac{1}{2}$ net gain, 450 . -28. Shipped P. E. Onslow, Sorel, to be sold on joint \% of himeself, J. D. Roe, Montreal, and ourselves, each $\frac{1}{2}, 30$ hhids. Brown Sugar, 30000 !bs., ax $9 \frac{3}{4}$ cts. ; paid freight in cash, on same \$75.-25. F. Belmont has drawn on the Quelice Bank, ior personal expense, $\$ 300$. -Paid J. Astulú \&́ Dro's drat on us, favor of C. Russell, per check on Queliee Bank, for $\$ 1453.12$. :28. Rec'd cash fur rent of part of our Store \$2250. Per statement rendered this day, our share of earnings of last trip of Steambeat Eumpa, amts. to 5975 -29. Pard cash for sundry expenses to date,
    38.50.-30. Recd from P. E. Onslow, Acconut Sales of the Sugar shipped hins on the $\because 2$ nd inst. Our $\frac{1}{8}$ ret loss, $\$ 72.50$. F. Bemnont has this day invested in the firm, in cash, \$40.3.35. Duly ist. Recid from C. R. Kerney, Halifax to be sold on his and ur joini $\alpha$, each $\frac{1}{2}, 150$ bbls. Mackerel, invoiced at $\$ 7 ; 40$ bble. Heprings, involced at $\$ 4.50 ; 75$ bbls. Linseed Oil, invoiced at $\$ 40$; piad Freight per check on Quebec Bank, \$75. Deposited cash in the Quebes Bank, \$1-2750.-\$. Shipped P. Gilmour \& Co., St. John, N. B., to be aold on our joint $\%$, each $\frac{1}{2}, 200$ blils. Thin Mess, at $\$ 43.50$; paid Drayage, in cash, $\$ 27$.-3. Sold R. S. Venner, for cash, 150 bbla. Mackerel, (Mdse. Eo. D.,) at $\$ 7.50$. Nffected in- $^{\text {a }}$. -urance for $\$ 5500$, at $\frac{3}{4}$ gh on any property that may be in our warehouse, $\$ 56.25 .-4$. Shipped J. O'Regan \& Co., Montreal, as per their order, at 60 days, the following Merchandike; 75 bbls. Linseed Oil, (Mdse. Co. D.,) at $\$ 45$; 40 bble. Herrings, Mindee. Co. D.,) at $\$ 4.50 .-$ Closed Mdse. Co. D., and rendered C. R. Keracy an Account Sales of the same. Our charges for Storage, Advt rtising \& Insurance, $\$ 75$; our Commission, $2 \frac{1}{2}$ \% on Sales $\$ . . .$. .C. R. Kerney for his $\frac{1}{3}$ Invoice, $\$ 2115$, and net gain, $\$ 01.5!$. Our $\frac{1}{3}$ net gain, $\& .$. - $\boldsymbol{\sigma}$. Paid by check on Quelinc Bank, lvertising bills of Morning Chronicle, \$225.-6. Hee'd from Kane \& Joly, Hamilton, to be sold on joint $\%$ of themselves, A. C. MiHer, and ourselves, each $\frac{1}{8}, 150$ hhds. Brown Sugar, invoiced at $\$ 60$; paid Freight per check on Queliec Bank, \$750.- - Liec'd from Fi. Massoñ \& 40. , Sandwich, to be sold on theirs and our joint acct., eash 1, 500 bbls. Prime Popk, at $\$ 13.50$; 250 bbls. Lard, 50000 lbs., at $7 \frac{1}{2}$ cts.; paid Freight per check on Quebec Bank, \$750.--4. Sold J. N. Miles, Quebec, 150 hhds. Brown Sugar, (Mdie. Co. L., ) at siv5. Rec'd in payment, J. Mountain \& Co's. note, ad March 3, :871, due one day after date, for $\$ 7500$; due to date uss note $\$ 185.20$; and cash for balance.-Closel Mdse. Co. E., .nd ru dered Kane \& Joly and A. C. Miller, each an account of the sales. Our charges fur Storage, Advertising, etc., $\$ 75$; onr Commission $2 \frac{1}{2}$ \% on sales, \$. . . . Kanc \& Joly's net proceds $\$ 3381.25$; A. C. Miller's, $\$ 338.1 .25$; our net qain, \$381.25.- Rec'd cash for N. Harris' note, due this 'day, \$49:0.- 10. Deporited cash in the Quebec Bauk, \$0000.-12.

    ## PRAOTIOAL EXEROISES,-6ET III.

    to L. Moore, en ounted his note 98.60 ; discount o., an Ascount be sold on our Onslow, Sorel, and ourselves, ; paid freight inn the Quelice lí \& isco's dra"t for \$1453.12. Per statement ip of Steambcat xpenses to date, it Sales of the 3, 72.50 . F . h, \$403:3.35. sold on his and at \$7: 40 bbls. nvoiced at $\$ 40$; posited cash in $\& \mathrm{Co}$. , St. John, :Thin Mess, at S. Venner, for 0 . Effected in. may be in our ., Montreal, as ndike; 75 bbls. ngs, Mdee. Co. y. R. Kerhey an e, Advertising \& \& \$ . . . . . . . R. .51. Our $\frac{1}{2}$ net vertising bills of roly, Hamilton, and ourselves, aid Freight per Massoñ \& ijo., ach $\frac{1}{2}, 500$ bbls. bs., at $7 \frac{1}{2}$ cts. to. Sold J. N. o. Le, ) at *iv. urch 3, :871, note \$185.20; dered Kane \& Our charges n $21 \%$ on sales, ler's, §338.1.25; inote, due this 1k. \$6000.-12.

    Gave our check on Quebec Bank, in payment on mortgage, favor of
    T. S. Poston, for \$6986.25. The aint. applied on mortgage, is $\$ 6750$; the interest in full to date, $\$ 236.25 .-18$. Paid our acceptAccepted Fre Benning \& Son, due this day, in cash, $\$ 6204.38$. \$58i0.-14. Sold $H$. ${ }^{4}$ draft on 118 payable at 10 days sight, for (Mise. Co. F.., at $\$ 14.25$ arroll, for cash, 500 bbls. Prime Pork, Co., Montreal, of an errur in an Acc'd alvice from J. $\mathbf{O}^{\prime}$ Regan d in which we were credited ton Account Sales of last year's business, J. O'Regan \& Co., at 30 days little by $\$ 412.50$. Sold our draft on $\$: 3900.07$; disct. off $\$ 67.43$ - $-1 \%$ sight for which we received cash, bble. Lard, (Mdse. Co. F.,) at G. Sold J. B. Lewis, for cash, 250 rendered B. Masson \& Co., Sandwieh cts.-Closed Mdse. Co. F., and Our charges for Storage, Cooperaye an Account Sales of the same. $2 \frac{1}{2} \%$ on sales, $\$ \ldots$ B. Mayoperage, etc., $\$ 75$; our Commission
     \$9773.43. Rec'd cash for L Masson \& Co. cash in full of acct., \$10500,-285. Depositerl cash in. Nolan's note of the 13th June, from P. Gilmour \& Co. an A in Quethec Bank, \$15000.-2.5. Rec'd slupped then on the 2nd inst. Accont Sales of 200 bbls. Thin Mess, Accepted C. R. Kerney's note On net proceeds, \$1200.-26. MeGinn, for amt. due him, on us at 30 days sight, favor of $\mathbf{P}$. tavor of Frem it \& Co., due this $840 .-27$. Paid our acceptance cash of H. Gterory, in full of day, in cash, \$5850.-28. Rec'd Sewell, to bal. .....-31. Passed acct.-30. Paid Cash to Jordan \& amr. charged to his Private acet. to F. Belmont's Stock acct., the the stilt. charged to his Private acct Passed to Stock acct. of L. Moore, additional investme of June 30 . acct. Allowed 7 \% on F. Belmont's

    | INVE |  |  |
    | :---: | :---: | :---: |
    | Store, valued |  |  |
    | Steanmboat Europa Stock |  | \$22500.00 |
    | Interest due us on Notes |  | 15000.00 |
    | Less, interest due from us | $\left.\begin{array}{r}\$ 213.95 \\ 21.37\end{array}\right\}$ | 192.58 |

    ## BALANCE ACCOUNT, JULY 31.

    | Resources. <br> Real Estate. <br> Cash. <br> Quebec Bank. Billa Receivable. <br> Interest Receivable. <br> Steamb Europa Stocit. <br> Steamboat Europa. <br> P. Gikmour \& Co. |  | Liabilities. <br> Mortgage Payable <br> Bills Payable. <br> Interest Payable. <br> J. D. Roe. <br> P. E. Onslow. <br> Kave \& Joly. <br> A. C. Miller. <br> F. Belmont. <br> L. Moure. |  |
    | :---: | :---: | :---: | :---: |
    |  | \$22.500 00 |  |  |
    |  | 660 38210 |  | \$675000 |
    |  | 38210063 7500 |  | 16171515 2137 |
    |  | 21395 |  | $8010{ }^{21} 38$ |
    |  | 1506000 |  | 2932500 |
    |  | 37500 |  | 638125 |
    |  | 256350 |  | 3381 25 |
    |  |  |  | 236789 <br> 19697 <br> 98 |
    |  | $023 / 84$ |  |  |
    |  |  |  |  |

    ## SETIV. <br> <br> JOBBING AND IMPORTING BUSINESS,

    <br> <br> JOBBING AND IMPORTING BUSINESS,