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An Investigation into the Elastic Constants of Rocks, More Especially with Reference to Cubic Compressibility

BY

FRANK D. ADAMS AND ERNEST G. COKER

WASHINGTON, D. C.
Published by the Carnegie Institution of Washington
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AN INVESTIGATION INTO THE ELASTIC CONSTANTS OF ROCKS, MORE ESPECIALLY WITH REFERENCE TO CUBIC COMPRESSIBILITY.

INTRODUCTION.

The question as to the amount of cubic compression which rocks may undergo under the stresses to which they are subjected in the earth's crust is one which has a direct bearing on many very important problems in geophysics. It is, however, a subject which has been but little investigated as the experimental difficulties connected with it are very considerable. The importance of a series of determinations of the cubic compressibility of a few typical plutonic igneous rocks was some time since impressed upon the authors by Mr. G. K. Gilbert, with a request that if possible they should make such determinations in connection with the researches on rock deformation which are now being carried out at McGill University under the auspices of the Carnegie Institution of Washington. An examination of all the direct methods proposed or adopted for the measurement of the cubic compressibility of solids showed that none of these could be satisfactorily applied to such materials as rocks, but the indirect methods based on Hook's law and which have been applied to metals and other compact isotropic bodies having an approximately perfect elasticity promised to give satisfactory results if applied to certain rocks, more especially to the class of rocks referred to above, viz, the acid and basic plutonic rocks, which form the greater part at least of the outer portions of the earth's crust. The present paper sets forth the methods adopted and the results obtained.

The work which was carried out in the laboratories of McGill University was commenced by the authors whose names appear on the title page, and was carried well towards completion when Dr Coker was called to take the professorship of mechanical engineering in the Finsbury Technical Institute of London, England. He was accordingly obliged to give up the work of the research and his place was taken by Mr. Charles McKergow, lecturer in mechanical engineering in McGill University, but who immediately on the completion of the work was appointed to the professorship in mechanical engineering in the University of Virginia. A large number of the very careful measurements of elastic constants which are given in the paper were made by the latter gentleman.

METHODS WHICH MAY BE USED IN THE DETERMINATION OF THE ELASTIC CONSTANTS OF MATERIALS.

The determination of the cubic compressibility of solid substances is, as above mentioned, beset with serious difficulties. On the one hand, every direct method which has been suggested presents experimental difficulties which tend to impair its accuracy, while on the other hand the indirect methods are based on assumptions as to the isotropy of the materials, which are not warranted in the case of certain rocks. The indirect methods depending on the theory of elasticity are capable of considerable variation, and it is of interest to examine them in some detail in order to see whether certain of them at least may not be depended upon to give reliable and satisfactory results.

The determination of the elastic constants of metals has engaged the attention of many physicists and at the present time a large amount of information exists as to the values of these constants for various metals.

It is well known that in homogeneous elastic substances a simple compression stress causes a lateral strain, which bears a fixed ratio to the compression strain for any particular substance within the limit of elasticity. If, then,* we call p_x the stress on a plane perpendicular to x in the direction x, and e_x the corresponding strain, then for a direct compression stress p_x there will be a strain in the direction of this stress of amount p_x/E, where E is Young's modulus, and lateral strain of magnitude p_x/mE, where m is the ratio of the longitudinal compression to the lateral extension per unit of length.

If we suppose further that a body is subjected to cubical stress of intensity p_x, we easily see that for small and therefore superposable strains the cubical strain e_c is

$$e_c = 3p_x \frac{m-2}{mE}$$

and since the modulus of cubical compressibility D is the ratio of the stress per unit of area to the cubical strain produced, we have

$$D = \frac{p_x}{e_c} = \frac{1}{3}\frac{m}{m-2}E.$$

Hence if we know E and m we can calculate the value of

Further, it is shown in treatises on elasticity that if C is the modulus of shear, then

$$C = \frac{1}{2}\frac{m}{m+1}E$$

*See Ewing's Strength of Materials, Chapters I & II.

and since C and E are quantities which can be ascertained by experiment, we can from them calculate m and D.

In an important paper by Nagaoka* this latter method has been used to determine the elastic constants of a series of rocks. The value of E was determined by supporting a bar at the ends and measuring the angular change at the support due to a given load applied at the center; the value of E is then obtained by the formula $E = 3wl^2/4bd^3\theta$, where l is the length of the bar between the supports, b is the breadth of the bar, d the depth, and θ the angular change at the ends for a load, W. In order to determine the value of m, a specimen of rectangular section was twisted by a given torque, T, and the amount of the strain measured. It has been shown by St Venant that for such a case the value of C is given by the formula

$$T = C\theta b^3 h\left[\frac{16}{3} - \frac{32^2 b}{\pi^5}\sum_{0}^{\infty}\frac{\tanh\,(2n+1)\frac{\pi h}{2b}}{(2n+1)^5}\right]$$

where θ is the angular change, and from this formula values of C were calculated from the observations.

This method appears to us to be open to some minor objections in that the formula for determining E is based upon a theory of flexure, which although sufficient for many purposes is nevertheless only approximate, and it is well known that values of E obtained by flexure experiments in this manner often differ from the values of E obtained by direct compression experiments by not inconsiderable amounts

Further, in experiments upon the deflection of beams cut from rocks, it is difficult to obtain consistent readings, because of the time effect of the loading, and this difficulty is noticed in the paper cited.

As an example of the results obtained in this way, we may quote the results of certain experiments made by us with a pure white marble from Vermont.

Lath-shaped pieces of the marble were carefully prepared and were suspended on two wedge-shaped supports and then loaded in the middle. The weights were placed in a light brass pan, hanging from a thick wire which passed over the middle of the lath and lay flat upon it.

Each experiment occupied about half an hour, and the deflection was measured by attaching a scale to the marble and reading it with reference to a thin wire stretched in front of the specimen, a properly mounted telescope being employed for this purpose. The marble was in all cases placed so that its broader surface rested on the terminal supports.

*Elastic Constants of Rocks and the Velocity of Seismic Waves. H. Nagaoka. Phil. Mag., Vol. L, 1900, p. 53.

Of the several experiments made two may be selected. The pan and wire in each case weighed 3 ounces

In the first experiment the marble had the following dimensions: Length, 12 inches; length between supports, 11 inches; breadth, 1.259 inches; thickness, 0.284 to 0.298 inch.

The figures obtained are as follows:

	Inch.
Load with pan only (taken as zero point)	0.486
with pan plus 4 ounces	.487
8 ounces	.488
12 ounces	.489
16 ounces	.490
20 ounces	.491
24 ounces	.491
28 ounces	.492
32 ounces	.493
36 ounces	.494
40 ounces	.497
44 ounces	.498
48 ounces	.500
52 ounces	.501
56 ounces	.503
60 ounces	.505
60 ounces (after 2 minutes)	.506
64 ounces	.515
64 ounces (after 1½ minutes)	.516
66 ounces	.517
68 ounces	.518
68 ounces (after 1½ minutes)	.520
70 ounces	.521
72 ounces	.522
72 ounces (after 1 minute)	.522
74 ounces	.526
76 ounces	.528
76 ounces (after 1½ minutes)	.531
78 ounces	.533
80 ounces	.534
80 ounces (after 2 minutes, moving fast	.540
82 ounces	.541
82 ounces (after 1½ minutes)	.543
72 ounces (weight reduced, large permanent set)	.542
84 ounces	.547
86 ounces	.549
86 ounces (after ½ minute; broke)	.554
Total deflection before breaking	.064

In the second experiment the marble lath was longer and at the same time somewhat thicker. Its dimensions were as follows: Length, 16 inches; length between supports, 15 inches; breadth, 1.229 to 1.284 inches; thickness, .347 to .356 inch.

	Inch.
Load with pan only	.343
with pan plus 8 ounces	.349
16 ounces	.368
24 ounces	.389
24 ounces (after 1½ minutes)	.392
28 ounces	.401
32 ounces	.416
32 ounces (after 1½ minutes)	.423
36 ounces	.438
40 ounces	.460
Load with pan only (weight removed, large permanent set)	.412
with pan plus 40 ounces (after 2 minutes)	.471
44 ounces	.492
44 ounces (after a few seconds)	.500
44 ounces (after 1 minute; broke)	.520
Total deflection	.177

Here it will be noticed that when a certain load is reached a distinct movement sets in and is maintained without any further increase of load, the movement growing in amount as the limit of the strength of the rock is approached and producing a permanent set.

Experiments on the determination of the elastic constants of rocks when subjected to twist were also found to be frequently unsatisfactory, owing to the low ultimate shearing values of many rocks.

While a glance at the list of rocks whose elastic constants have been measured by Nagaoka will at once show that most of them are rocks whose elasticity must be of a very imperfect kind, *e. g.*, weathered clay slate, Schalstein, tuff, etc.; the method which he has employed for the determination of Young's modulus gives very low results, even in the case of rocks such as marble and granite, where the elasticity might be supposed to be of a high order, and comparable to that which these rocks have been shown to possess in the case of the types selected for investigation in the present paper. This is shown by the following figures comprising the values obtained by him for each of the marbles and granites contained in his list.

Paleozoic marble.	E (Young's modulus).	Granite:	E (Young's modulus)
No. 11A	10,120,000	No. 69 (Sho[illegible]a)	6,140,000
11B	7,950,000	68 (Hita[illegible]	2,853,000
12A	5,440,000	71 (Hitachi)	2,175,000
12B	4,770,000	56 (Hitachi)	1,588,000
		52 (Hitachi)	3,265,000

Of these marbles No. 11, if a mean of the two readings be taken, has about the same modulus as the average of those on our list, while No. 12 is very much lower. The highest value given for any granite in Nagaoka's list, viz. No. 69, is somewhat higher than that of the lowest of the granites in our series, that from Stanstead. The other granites examined by Nagaoka have values for E assigned to them which are so low that they are comparable only to that of the sandstone in our series. Of the three sandstones included in Nagaoka's list the Izumi sandstone of the Mesozoic has modulus of 1,322,000, while the other two, which belong to the Diluvium, have values for E of 587,500 and 583,000, respectively.

And so when an attempt is made to calculate the cubic compression D from the values given in Nagaoka's list and obtained by his method, it is found that a negative value is actually obtained in about one-third of the rocks which he has examined. His figures, however, were intended chiefly for the purpose of calculating the velocity of the propagation of earthquake shocks.

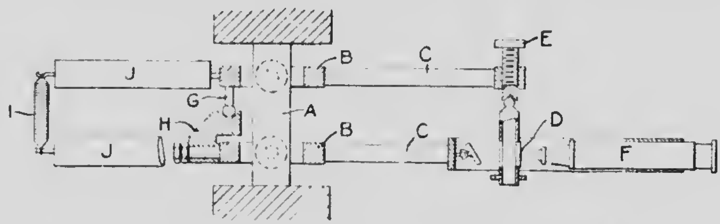


Fig. 1.—Instrument for determining the modulus of a simple strain.

In consequence of the somewhat unsatisfactory results obtained in our preliminary experiments with this method, as well as the facts with regard to Nagaoka's figures just mentioned, it was decided to adopt a somewhat different method and one which avoided both torsion and flexure and depended simply on strain produced by simple compressive stress. This will be termed the "method of simple compression."

Among the possible indirect methods, this seems to be the most satisfactory, as the assumptions necessary in the calculation of compressibility are reduced to a minimum, and the range of stress for which the ratio of stress to strain is practically constant is great. We were able to measure the strains obtained very accurately, by means of an apparatus forming part of the equipment of the testing laboratory of McGill University, for the use of which we are indebted to Dean Bovey.

This is an instrument designed by Professor Ewing, and of which a diagrammatic representation is given in figure 1, in which A is a specimen of the rock gripped by screws passing through a pair of collars, B, which are 1.25 inch apart, to which latter metal rods, C, are attached. The upper rod carries a glass plate, D, with a fine line scratched upon it, the position of which can be adjusted by a screw, E, while the lower rod carries a micrometer microscope, F. The upper and lower collars, B, are connected by a stud, G, the upper one engaging with the conical hole of the swivel piece H in the lower, and contact is maintained by a spring, I, while the weights of the microscope and projecting arms are balanced by lead cylinders, J. A buzzer was attached to the upper lead cylinder which, when operated, caused a slight vibration in the instrument, producing a perfect adjustment as the pressure was applied.

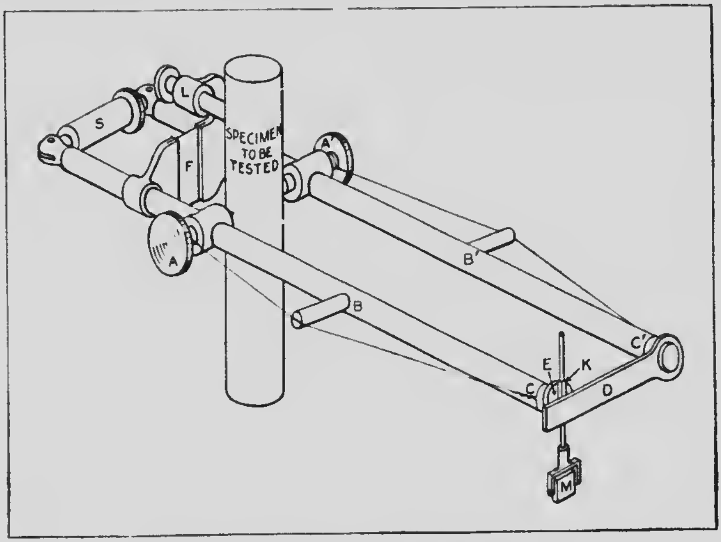


FIG. 2.—Perspective view of lateral extensometer.

The proportions of this instrument were so adjusted that one division on the micrometer scale corresponded to $\frac{1}{250,000}$ of an inch, and before using it the instrument was calibrated by aid of a Whitworth measuring machine and was found to be in correct adjustment. This instrument enabled us to determine the modulus of simple compression with great accuracy.

The linear strain perpendicular to the length of the specimen was measured by an instrument which had been designed by E. G. Coker some time previously for experiments on the lateral strains developed in metals.* Figure 2 is

*See Proceedings Royal Soc., Edinburgh, Session 1904-5. Vol. XXV, pt. VI.

a diagrammatic view of the apparatus, which consists of a pair of brass tubes, *B*, *B'*, provided with set screws, *A*, *A'*, for attachment to the specimen, and connected together by a flexible steel plate, *F*, forming the fulcrum. The ends of the tubes near the fulcrum plate are pressed apart by an adjustable spring *S*, to insure a uniform pressure on the screw points gripping the specimen. On the opposite end of the tubes is a spring finger, *D*, of ebony, pressing against a double knife edge, *K*, seated in a shallow V notch cut in the end of the other arm. The knife-edge carries an adjustable mirror, *M*, so that if any change in the diameter of the specimen occurs the two tubes move relatively to one another in a horizontal plane and thereby cause the knife-edge mirror to rotate; the rotation of this latter is observed and measured by a telescope and scale placed at a suitable distance.

For convenience in adjustment there is a screw, *L*, for tilting the apparatus about the axis of the gripping screws, and the tubes *B*, *B'* are trussed to prevent vibration. This instrument was calibrated by aid of a Whitworth measuring machine and the scale adjusted so that one division corresponded to one-millionth of an inch.

APPLICATION OF THE METHOD OF SIMPLE COMPRESSION TO THE DETERMINATION OF THE CUBIC COMPRESSIBILITY OF METALS.

The behavior of such metals as wrought iron and steel over a wide range of stress shows that these metals may be considered as almost perfectly elastic. The results of the theory of elastic bodies may therefore be applied in their cases with great confidence.

As a typical example of the behavior of such materials we may consider the deportment of a specimen of wrought iron when subjected to a cycle of compression stresses, commencing at 1,000 pounds and rising to 9,000 pounds, afterwards returning to the original load.

The readings obtained for the longitudinal and lateral strains will show in such a case that equal increments or decrements of load produce strains which are very exactly proportional thereto. This is clearly shown in a plot of these readings, where the ordinates represent the total load and the abscissæ represent strains. In both cases the relation of stress to strain is represented by a straight line returning upon itself. Traces which vary but little from the ideal straight line are given by black Belgian marble, as will be seen on page 25.

Such results afford an arbitrary standard by which can be judged the degree of approximation to perfect elasticity exhibited by other metals and by rocks under similar conditions.

If we now calculate the value of the modulus E for simple compression, since this is the relation of the compression stress p to the strain e, we have

$$p = Ee$$

If we call A the cross-sectional area of the specimen when stressed by a load, P, and x the decrease of length over a measured length, L, gripped between the screw points of the measuring apparatus, we obtain

$$E=\frac{PL}{xA}$$

which, in case of a specimen of wrought iron examined for a range of 8,000 pounds, gave a value of 28,100,000, the units being pounds and inches.

The ratio m of the longitudinal strain to the lateral strain in the same case was 3.65, and using the formula

$$D=\frac{1}{3}\frac{m}{m-2}E$$

we obtain for the modulus of cubical compression (or bulk modulus) D, the value 21,300,000, a constant for the material, the reciprocal of which gives the decrease in volume of 1 cubic inch for 1 pound of pressure.

While certain rocks, such as many of the marbles, have a structure identical with that of wrought iron, most of the rocks constituting the earth's crust are composed of several minerals, and thus resemble cast iron in character, the gray variety of this substance being an aggregate of crystals or individuals of the metal iron (wrought iron), graphite, etc.

It will therefore be of interest to ascertain how a specimen of cast iron behaves under compression stress, and how far its elasticity falls short of that which would be exhibited by a perfectly elastic body.

For this purpose a fine-grained specimen of somewhat hard cast iron was faced and tested. The results of this test are given in the following table, and the stress-strain curves are plotted in figure 3. I represents longitudinal compression and II lateral extension.

The behavior of cast iron, as exhibited by these experimental results, shows a falling away from the theoretical standard of perfect elasticity, but even in the most perfectly elastic bodies there is probably a slight hysteresis effect, so that we are justified in using the results obtained to calculate the modulus of compressibility, if the error introduced thereby is negligible or very small.

It may be pointed out that this method and others of the indirect type have been freely used to obtain values of the bulk modulus for cast iron and metals of like character, and it will be shown that the composite crystalline rocks are very similar to cast iron in their behavior under stress, although generally more perfectly elastic.

Cast Iron

Size	1.034 × 1.006		1.034	1.006
Area	1.041	1.041	....	..
E	15,000,000	18,000,000	....	...
σ	.25	.25	....	....
D	10,000,000	10,000,000	....	...
C	6,000,000	6,000,000	....	....
Longitudinal compression (multiply readings by 4 for millionths).			Lateral extension—(millionths).	
Load (in pounds).	Side *P.*	Side *U.*	Side *P.*	Side *U.*
1,000............	0	0	0	0
2,000............	19	20	12	11
3,000............	40	37	26	21
4,000............	60	58	41	32
5,000............	80	78	56	48
6,000............	100	100	72	65
7,000............	120	120	86	83
8,000............	140	143	102	99
9,000............	160	160	119	116
8,000............	145	143	106	108
7,000............	123	125	90	85
6,000............	104	110	76	70
5,000............	85	90	60	60
4,000............	63	63	44	50
3,000............	44	40	30	39
2,000............	20	21	13	21
1,000............	0	0	6	9

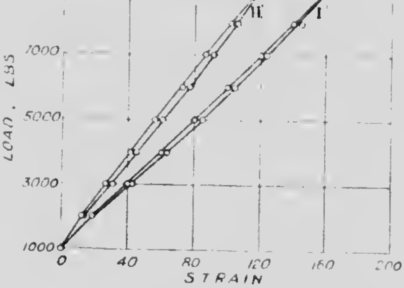


FIG. 3.—Cast iron Stress-strain curves.

APPLICATION OF THE METHOD OF SIMPLE COMPRESSION TO THE DETERMINATION OF THE COMPRESSIBILITY OF ROCKS.

It has been noted in the case of marble when subjected to bending stress that the strain as exhibited by the deflection of a point of the bar increases with the time, and the strength under shear produced by a torque was also found to be so small that a determination of the strain was very difficult to measure.

These difficulties have been noted by Nagaoka,* who states that:

> Preliminary experiments on granite show that Hooke's law does not hold even for very small flexure and tension, and that the after effect is very considerable from the pressure, when the prism is sufficiently loaded or twisted, the deviation from the direct proportionality between strain and stress was incomparably greater as compared with that observed in metal. This must be chiefly due to the low limit of elasticity, so that it is necessary to experiment only within very narrow limits of loading and twisting. These limits are widely different for different specimens of rocks, and the modulus of elasticity, as well as that of rigidity, was always determined with such stresses as will approximately produce strains proportional to them. The deviation from Hooke's law was prominent in certain specimens of sandstone, and it was more marked in tension than in flexure experiments; in certain rocks it is indeed doubtful if anything like a proportionality between stress and strain can be found, even for extremely small change of shape. On releasing these rocks from stress the return toward the former state is extremely small, showing that the elasticity of the rock is of a very inferior order.

These observations of Nagaoka for bending and twisting have been confirmed by our own deflection experiments, as above mentioned.

If, however, the rock be subjected to direct compression, strains in which the time effect is small and the lag of the strain is also small are almost invariably obtained. This is especially the case if before the actual experiment is carried out the material be several times subjected to a range of stresses at least as great as those employed in the experiment itself. This preliminary stressing brings the material to "a state of ease," and is also commonly adopted when the elastic constants of metals are determined.

It is evident, therefore, that this direct compression method may with confidence be applied to the measurement of the cubic compression of rocks, although as mentioned below the accuracy of the result so obtained will differ with different classes of rocks.

If the rock be massive, compact, and crystalline (or glassy) the method can be safely employed and good results will be obtained. If, on the other hand, the rock is schistose, porous, or loosely coherent, the method will from the nature of the case be very much less satisfactory.

The plutonic igneous rocks as a class most nearly resemble the metals in structure, being holocrystalline and massive, and therefore present the

*Elastic Constants of Rocks and the Velocity of Seismic Waves. H. Nagaoka. Phil. Mag., vol. L, 1900, p. 58.

nearest approach among rocks to perfect elasticity; they are therefore a class of rocks to which this method is especially applicable. It fortunately happens that they are also a class of rocks a knowledge of whose compressibility is of special importance for the elucidation of many geological problems, constituting as they do the greater part of the earth's crust.

A second class of rocks which are comparable with them in their approach to perfect elasticity comprises the marbles and certain limestones.

A series of sixteen typical rocks representative of these two classes were accordingly selected for measurement. Under the first class a number of granites were chosen as representing the acid plutonic rocks and a number of types of the gabbro essexite series were selected as representing the basic plutonic rocks. In all these cases great care was taken to choose the most homogeneous and massive rocks of each series and to secure test pieces free from all flaws and cracks. As representing the second class a number of typical marbles and limestones, also perfectly massive in character, were selected. For purposes of comparison, or contrast, a sandstone was added to the list as being a rock which, on account of its more or less porous nature could hardly be expected to yield satisfactory results by this method.

An examination of the stress strain curves of these 16 rocks, omitting the sandstone, shows that on the average they possess a rather more perfect elasticity and exhibit less hysteresis than cast iron. Some of them, as for instance the Baveno granite, the nepheline syenite, the diabase, and the black Belgian marble, show much better curves, approximating in fact to the straight lines given by wrought iron, which may be considered for our present purpose as expressing perfect elasticity.

The close approximation to perfect elasticity is shown by the return of the curve to its initial or starting point, and the amount of the hysteresis is shown by the width of the loop.

The width of this hysteresis (or lag) curve or loop, indicates the amount of the divergence from Hook's law which the material exhibits, this law being that the stress and strain are *directly* proportional. When the curve is narrow, as it is in all cases except the Stanstead granite and the sandstone, the divergence from Hook's law is not great enough to seriously affect the result.

The rocks, therefore, with these exceptions, fulfil the conditions of elasticity necessary to the successful application of the method. In these two cases the results are less certain, owing to the greater hysteresis of the rock.

It might at first sight appear that while the method employed is theoretically perfect as applied to the measurement of the compressibility of vitreous rocks and of very fine grained crystalline rocks, a considerable error might be introduced when the rocks are coarser in grain. In the case of all the common crystalline rocks, the individual grains of which the rock is composed are anisotropic, that is, they have different moduli of elasticity in different directions. In massive rocks such as those investigated, however, these grains occur in the rock with an absolutely irregular orientation and would in the case of a fine grained rock mutually compensate for one another in any transverse line along which the expansion of the rock under compression might be measured. If, however, the rock were coarser in grain, fewer individual crystals would be found in any transverse line of section, and there might possibly in this way be a lack of compensation, as the rock in one section might be composed of grains whose axis of greater elasticity approximated on an average more nearly to the direction of measurement than in other sections. If such were really the case, there should be in these coarser-grained rocks an exceptionally great variation in the readings obtained from different specimens of the same rock, as well as from the different sections in the same specimen.

But such is not the case, as will be seen by an examination of the figure accompanying table. They represent the results obtained from ten measurements of the compressibility of Baveno granite, which is coarse in grain, and ten of Sudbury diabase, which is very fine in grain, together with eight measurements on Tennessee limestone, which is rather coarse grain, and seven on plate glass. They were made in each case on two or more specimens cut from the same mass and the measurements of the expansion were made on several different planes through each, so that in every case the measurement was effected in a different line through the rock, all of these, however, of course being at right angles to the direction of the compressive stress and lying in the medial plane of the column.

Full details concerning each measurement will be found in the tables which set forth the results obtained, under the sections dealing with the several rocks in question. The size of grain and the texture of the rock can also be seen by examining the photomicrographs and color prints of the polished surfaces of the respective rocks.

	Max.	Min	Diff.
Baveno granite (coarse) 10 trials	4,880,000	4,380,000	500,000
Sudbury diabase (very fine) 10 trials	11,170,000	9,655,000	1,515,000
Plate glass, 13 trials	6,930,000	6,020,000	910,000
Tennessee marble (rather coarse) 7 trials	6,130,000	5,770,000	360,000

It will thus be seen that there is no correspondence between the coarseness of grain and the magnitude of the variations in the readings obtained. The differences in glass, which is an isotropic material in which the elasticity is equal in all directions, are greater than in the Tennessee marble, which is rather coarse in grain, and in Baveno granite, which is the coarsest . . . .

the set. The greatest differences obtained are those found in the finest grained rock in the series, viz, the Sudbury diabase.

It is evident, therefore, that the different moduli of elasticity of the constituent grains of a rock do not introduce any perceptible error in measurements made by this method, when a column an inch in diameter is employed, and when the rocks are not coarser in grain than the Baveno granite. In fact, while surrounded on all sides by other grains, no individual grain can expand freely, as it would if subjected to compression unhampered by any surrounding medium, and thus the anisotropic character of the individual grains produces but little effect on the elasticity of the rock as a whole.

These experiments also show that in the case of rocks composed of several minerals it makes no perceptible difference whether the points of attachment of the instrument are embedded in the grains of one mineral or of another.

The chief source of error and the one to which the variations observed are for the most part to be attributed seems to be a mechanical one, viz, the difficulty of getting an ideal contact between these points of attachment and the specimen to be measured, especially in view of the extremely small dimensions of the movement to be measured.

The question of the influence of temperature on the elasticity and compressibility of rocks is of course one which has an important bearing on certain problems of geophysics. The only investigation of this subject, so far as can be ascertained, consists of a few preliminary experiments by Nagaoka and Kasakabe.* In these the torsion method was employed, and the experiments were carried out on a single rock, viz, sandstone. This rock, as has already been mentioned, being porous and stratified in character, is a material whose elastic properties are far from ideal. The results are summed up by the authors in the following words:

> Preliminary experiments with sandstone show that the modulus of elasticity is much affected by the variation of temperature, *i. e.*, about 0.5 per cent per degree. It does not, however, necessarily diminish with the increase of temperature where the temperature is low, *i. e.*, it is maximum about 0° C.

As has been shown however, the values for the elastic constants obtained by this torsion and bending method have yielded results which can not in all cases be correct and which differ very considerably from those obtained by the more direct and simple method which has been employed in the present paper. These results bearing on the variation of elasticity induced by changes of temperature, especially in view of the fact that they are stated by the

*Modulus of Elasticity of Rocks and Velocities of Seismic Waves. Publications of the Earthquake Investigation Committee. No. 17. Tokyo, 1904, p. 43.

investigators to be "preliminary," can as yet hardly be taken as of general application to all rocks, even if correct for the specimen of sandstone examined

In our own investigations the laboratory was maintained at a temperature of from 63° to 68° F (17.2° to 20° C), and a thorough investigation into the effect of temperature was not undertaken, as this would be very difficult to carry out when employing the method of direct compression used, the difficulty consisting in heating the specimen itself without in any way affecting the measuring apparatus attached to it.

It seemed, however, possible to ascertain whether any serious change in the elastic constants of the massive crystalline rocks employed in the present investigation would result from a moderate change of temperature For purpose of trial the rock selected was the Sudbury diabase, a typical fine grained plutonic rock A column of it was placed by Mr McKergow in a small testing machine having a capacity of 50 tons, and the temperature of the room in which the machine was set up having been lowered to + 10° F, a cycle of compression readings were taken in the usual way adopted when Young's modulus is to be determined The temperature of the room was then raised by about 10° and another cycle of readings were taken It was then raised another 10° and a third series of readings were obtained, and so through successive stages of 10° until the normal temperature of the room (about 65° F) was reached The initial reading of the instrument before the application of pressure was of course different in each case, owing to the expansion of the rock which followed from heating These initial points were plotted on a line, and the results obtained when the specimen was subjected to a certain maximum load, together with the increase of temperature at each stage, were plotted on a second line If the compression was greater at 65° than at 10° for the same load these two lines should have diverged, but as a matter of fact they were practically parallel The differences between the readings given by the same load at different temperatures were no greater than those obtained by different measurements under the same load at the same temperature The conclusion therefore seems to be indicated that a change of temperature made no perceptible difference within the range of temperatures employed, although a difference of 0.5 per cent for each degree centigrade, which was Nagaoka's result, would mean a difference of about 25 per cent in range of temperature employed by Mr McKergow

While, therefore, this experiment can not be considered as supplying accurate information concerning the effect produced by a rise in temperature on the elastic constants of rocks, for the instruments themselves are in some measure affected by the same changes of temperature, they serve to show that in the case of the massive crystalline rocks the influence of temperature is probably not very great The subject is one which requires further investigation

THE METHOD OF MEASUREMENT.

In carrying out the measurements, prisms of the rock approximately 1 inch square and 3 inches long were usually employed (see fig 4). These were cut and ground with smooth faces, but were not polished. In these two small round holes were drilled in the medial line of each vertical face for the purpose of attaching the instrument, when Young's modulus was to be measured. These holes were made by means of a small diamond drill and were perfectly round and smooth. They were each 0.05 to 0.08 inch in diameter and 0.125 inch deep and 1.25 inches apart, lying at equal distances above and below the center of the prisms. These holes were champfered at the outer end, as shown in figure 4, and were found to afford the most perfect attachment which could be secured for the points of the instrument. By means of these prisms two sets of measurements of the vertical compression could be made with each prism, by attaching the instrument first to one pair of opposite faces and then to the other.

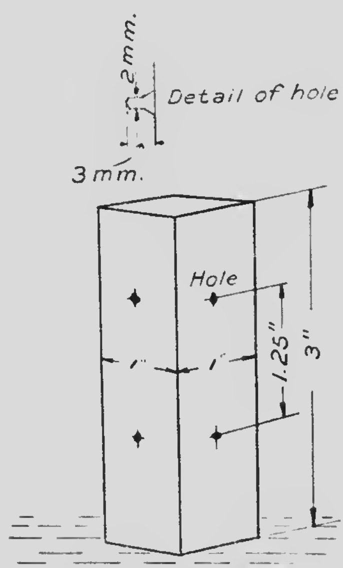


FIG. 4. Square test specimen of rock.

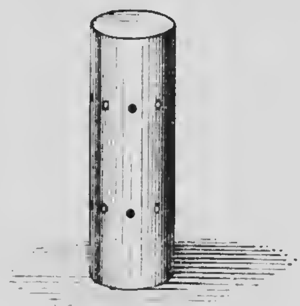


FIG. 5. Round test specimen, showing position of holes.

In some cases round columns were used (see fig. 5). These were approximately 1 inch in diameter and 3 inches in length. With these it was possible to make four sets of measurements in compression with each column, by drilling eight pairs of holes, as above described, whose planes intersected at angles of 45° instead of 90° as in the square prisms.

It was of course necessary in every case, whether prisms or columns were employed, to exercise great care to have the ends of the test pieces very carefully faced and absolutely parallel to one another. Before the actual measurements were made, the rock in every case was brought to a "state of ease" in the manner already described.

The pressure was applied in most cases by a 100-ton Wickstead testing machine, which was so carefully adjusted that it was sensitive to a load of 4 pounds.

The specimen, having been placed in the press and reduced to a state of ease, was then after careful adjustment submitted to loads increasing in successive stages of 1,000 pounds until the limit of safety had been reached, when the load was reduced successively by the same amounts, accurate readings being taken at each increment and decrement of load. The maximum load employed in the case of most rocks was 9,000 pounds, equivalent to from 9,000 pounds to about 11,500 pounds per square inch, according to whether a square or round prism was employed. In the case, however, of some of the stronger rocks a load of as much as 15,000 pounds per square inch was employed.

In the determination of the lateral strain, which was made upon the same set of columns as those used for measuring the vertical compression, care was taken that the theoretical conditions were realized, and that the material was free to expand laterally, as otherwise the values obtained for the lateral extension would be inaccurate. In all cases, therefore, the measuring apparatus was set as nearly as possible upon the central section of the test piece, and the ends of the specimen, after being ground smooth, were coated with a thin film of oil, so that the polished pressure plates of the machine would have as little tendency as possible to prevent freedom of lateral expansion.

In a number of cases accurate measurements were taken during the successive cycles of loading and unloading to which the specimen was subjected in order to bring it to a state of rest. These are recorded in the case of the Baveno granite and the Stanstead granite and served to show how the hysteresis of the rock may be reduced to a minimum by subjecting the test piece to this process. The measurements of each cycle usually occupied from 10 to 15 minutes.

It was at first conjectured that in the case of rocks composed of several minerals differences of reading might result from the attachment of the extensometer to different portions of the rock, the points of the instrument being fixed in some cases in grains of one mineral and in other cases in grains of another. It was found, however, as has already been mentioned, that the measurements on two sets of prism faces made in the manner above described, or on the four planes intersecting the vertical columns, where these had been provided with eight pairs of holes, showed that in the case of the rocks examined the differences between the several measurements on the same prism seem to be unaffected by the circumstance above referred to. The differences between the measurements thus made on rocks composed of several minerals were no greater than those found in the case of the limestones, which were composed of the single mineral calcite, or on glass.

In the case of the majority of the rocks investigated, a number of prisms or columns cut from the same block of rock were measured in order to ascertain whether different test pieces would give identical readings. It was found as a result of these investigations that the differences between the different specimens were no greater than those which were obtained by measuring the same specimens with the instrument attached at different places. In the case, however, of the Quincy granite, test pieces from two different blocks of the rock were prepared, and it was found that while the several measurements made on each test piece agreed among themselves, there was a distinct divergence in the elastic constants of the two specimens of the rock. This was probably due to a difference in composition, as the two rocks differed somewhat in appearance.

In the case of the green gabbro from New Glasgow, the results obtained by measurements made upon different parts of the same prism were discordant, for reasons which will be pointed out and which were dependent upon the structure of the rock.

Fifty five specimens of rock, nineteen of glass, and two of iron were employed in this investigation and every conceivable precaution was taken to insure the attainment of accurate results. The rocks in all cases were air dry, having been allowed to remain in the laboratory for several weeks after they had been cut, before the measurements were made.

In the accompanying tables the following elastic constants are given:

- E. Young's modulus, *i.e.*, the quotient of the longitudinal stress by the longitudinal compression.
- σ. Poisson's Ratio; this is the reciprocal of m.
- D. Modulus of Cubic Compression $= \frac{1}{3}\left(\frac{m}{m-2}\right)E$. The reciprocal of this gives the decrease in volume of a cubic inch of the material for a pressure of 1 pound per square inch applied on every side.
- C. Modulus of Shear $= \frac{1}{2}\left(\frac{m}{m+1}\right)E$, which is the quotient of torsional stress to torsional strain.
- m. The ratio of longitudinal compression to lateral extension per unit of length.

E and m are measured directly; the other values are calculated from them.

These values in the case of each rock are given in the respective tables, expressed in inch and pound units, and the results are summarized in a general table on page 69.

The measurements were made in these units on account of the fact of the testing machine employed was graduated to read pounds.

For purposes of comparison, however, this latter table has been recalculated in C. G. S. units, and the results are set forth in the second table to be found on page 69.

In the case of metal, Poisson's ratio is generally arrived at by stretching the bar and determining the value of the longitudinal extension divided by the lateral contraction. In case of rocks the tensile strength being low and the materials being brittle, it is more convenient and more accurate to make the determination by compressing a short bar or column, and determining the value of the longitudinal compression divided by the lateral expansion. This gives the value designated as m, of which Poisson's ratio is the reciprocal. Theoretically one method is as accurate as the other. In actual practice it might be supposed that the short compression columns in question would not expand quite so much at the ends as in the middle because of the friction against the compression plates. In order, however, to cause these to slip as easily as possible over the ends of the column, the surface of the rock in contact with them was always made very smooth and also was slightly oiled. It was found that, these precautions being observed, the expansion at the ends of the column was practically as great as at the center, where the measurement was taken, the differences being so small that no serious discrepancy was introduced.

In the tables the first transverse line designates the specimen employed as *a*, *b*, *c*, or *d*. The second line gives the diameter of the specimen, which is often slightly different in the two directions. The length of the column in all cases was about 3 inches, but this is not stated in the table, as the compression is not measured on the total length of the column, but on the length of that portion of it which lies between the points of attachment of the instrument.

The third line gives the area, which is approximately 1 square inch in the case of a square prism and three-quarters of a square inch in the case of a round column.

In the four succeeding lines the four elastic constants E, σ, D, and C, are given, as determined by each measurement.

Another transverse line contains the letters U or P, which designate the two diameters of the column when two measurements were made on the same square prism, these two directions being always at right angles to one another. In the case of round columns, on which measurements were frequently made in several planes, these are designated as "first holes," "second holes," etc.

In each table there follows the values obtained for successive loadings of 1,000 pounds in the case of each specimen, first for compression, when the figures multiplied by four give millionths of an inch, and then for lateral expansion, given directly in millionths of an inch. These afford the data for calculating the constants and for plotting the curves which accompany every table.

In the figures for the constants of iron and of one or two of the rocks, which are the result of measurements which were made at the beginning of the investigation, a slight correction has been made, owing to the inaccurate calibration of the extensometer, which will explain a certain discrepancy which will appear if the figures are recalculated.

THE ELASTIC CONSTANTS OF ROCKS COMPOSED OF A SINGLE MINERAL.

MARBLES AND LIMESTONES

BLACK BELGIAN MARBLE, BELGIUM

This rock is known in trade by the name of "Belgian black" or "Noir fin." It is an extremely fine grained black marble which takes a very high polish and is used very extensively in interior decoration. It has a splintery fracture, breaking almost like glass.

When thin sections are examined under the microscope the rock is found to be so fine in grain that a high power is necessary to resolve it. It is composed of minute calcite grains from 0.02 mm. to 0.002 mm. in diameter and of irregular shape, between and around which are occasional minute films and spots of a black color.

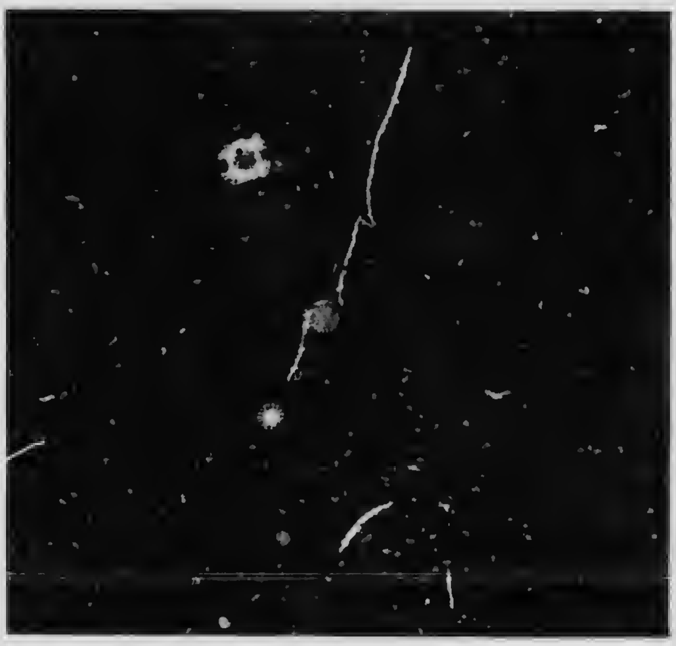
In this very fine grained and even groundmass are embedded a very few larger forms of clear white calcite, some of them rodlike, others circular in shape, and others possessing more complicated outlines. These are evidently of organic origin, representing small fragments of fossils. They are very sparsely scattered through the rock. The rock also contains occasional minute grains or crystals of iron pyrites.

Fragments of this rock dissolve readily in cold dilute hydrochloric acid, giving off a fetid odor and leaving a considerable amount of a light flocculent residue, black in color and apparently consisting of some form of bituminous matter. In the residue there are also a few minute grains of pyrite.

Plate I A is a color process photograph of a polished surface of this marble and Plate I B is a photomicrograph of a thin section of the rock, taken in ordinary light and magnified 27 diameters.

A square prism of the rock of the usual dimensions was employed to measure the elastic constants, and the results are set forth in the table found on page 25.

A. PHOTOGRAPH OF POLISHED SURFACE, (NATURAL SIZE)



B. PHOTOMICROGRAPH OF THIN SECTION, (X 27 DIAM.-ORDINARY LIGHT)

BLACK BELGIAN MARBLE, ("NOIR FIN").

Black Belgian Marble.

Size	.96 × .96	.96
Area	922	...
F	11,070,000	....
σ	.278	...
D	8,303,000	
C	4,330,000	
Load (in pounds).	Longitudinal compression (multiply readings by 4 for millionths).	Lateral extension (millionths).
1,000	0	0
2,000	25	24
3,000	53	51
4,000	84	76
5,000	116	103
6,000	147	129
7,000	178	155
8,000	210	182
9,000	240	209
8,000	211	183
7,000	180	157
6,000	148	131
5,000	118	104
4,000	88	78
3,000	57	51
2,000	30	23
1,000	1	4

The elastic constants were found to be as follows:

$E = 10{,}070{,}000$; $\sigma = 0.278$; $D = 8{,}303{,}000$; $C = 4{,}330{,}000$

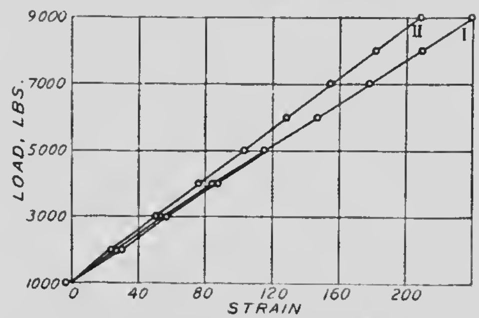


FIG. 6.—Black Belgian Marble. Stress-strain curves.

A plot of the readings is given in figure 6, from which it is clearly seen that the rock is practically free from hysteresis, and that within the range of pressures employed its elasticity is almost perfect I represents longitudinal compression and II lateral extension.

WHITE MARBLE, CARRARA, ITALY

A white, very fine grained saccharoidal marble. Under the microscope it is seen to consist of a mosaic of calcite grains. In this mosaic some grains are larger than others, but there is no great difference in their relative sizes and the average grain of the rock is uniform throughout. The average diameter of calcite crystals closely approximates 0.2 mm. The grains come against one another along sharp and usually straight lines. There is no trace of foliation in the rock, nor is there any trace of flattening or elongation of the grains in any one direction. The rock is perfectly massive. Between crossed nicols the calcite individuals extinguish uniformly and show no signs of pressure. Some of them show a few twin lamellæ.

A color process photograph of a polished surface of the rock employed is shown in Plate II A and a photomicrograph of a thin section of the rock, taken in ordinary light and magnified 27 diameters, is shown in Plate II B.

Three specimens of the rock were used in measuring the elastic constants, two square prisms (*a* and *b*) and a round column (*c*). Two sets of measurements were made on both *b* and *c*, the instrument being as usual affixed to the specimen in two positions at right angles to one another in each specimen. In this way five complete sets of measurements were made. The results are set forth in the table on page 27.

The means of the results obtained for the respective elastic constants are as follows:

$E = 8,046,000$; $\sigma = 0.2744$; $D = 5,046,000$; $C = 3,154,000$

The difference between the highest and lowest determinations of D is 420,000 pounds.

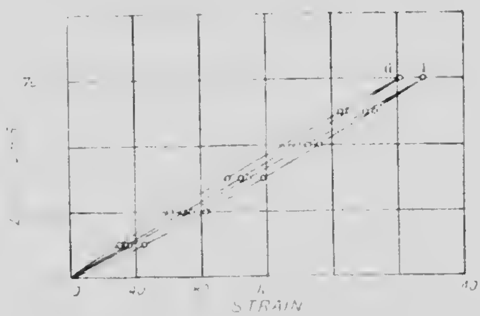
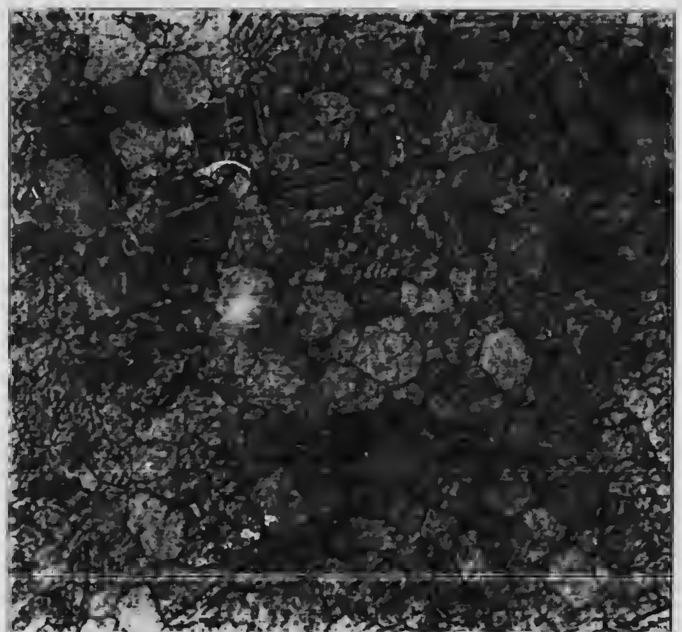


Fig. 7. Carrara marble, specimen *a*. Stress-strain curves.

Figure 7 shows the results obtained from specimen *a* in graphic form. I represents longitudinal compression and II lateral extension. The hysteresis is greater than in the case of Belgian black or Tennessee marble, but is about the same in amount as that shown by the Vermont marble and the Trenton limestone from Montreal.

A. PHOTOGRAPH OF POLISHED SURFACE. (NATURAL SIZE)



B. PHOTOMICROGRAPH OF THIN SECTION. (× 27 DIAM.; ORDINARY LIGHT)

CARRARA MARBLE.

Carrara Marble.

No	*a*	*b*	*b*	*c*	*c*
Size	1.032 1.035	1.017 1.016		.985	.985
Area	1.07	1.033	1.033	.62	.762
p	8,120,000	7,800,000	8,055,000	8,210,000	8,045,000
σ	281	274	273	275	269
D	6,140,000	5,750,000	5,920,000	6,100,000	5,790,000
C	3,170,000	3,060,000	3,160,000	3,210,000	3,170,000

LONGITUDINAL COMPRESSION. MULTIPLY READINGS BY 4 FOR MILLIONTHS

Load (10 pounds)	Side *U*	Side *P*	Side *U*	Side *P*	Side *U*
1,000	0	0	0	0	0
2,000	35	40	35	50	50
3,000	75	80	80	100	100
4,000	110	120	120	150	155
5,000	145	160	160	200	205
6,000	180	205	200	250	255
7,000	216	240	235		
8,000		275	270		
9,000		310	300		
8,000		290	295		
7,000	216	247	260		
6,000	185	210	215	250	255
5,000	152	171	170	210	210
4,000	118	125	130	160	165
3,000	82	85	90	105	110
2,000	44	45	30	53	55
1,000	0	5	5	0	0

LATERAL EXTENSION.—MILLIONTHS

No.	*a*	*b*	*b*	*c*
Size.	1.032	1.016	1.017	.985
Load (10 pounds).		Side *P*.	Side *U*.	
1,000	0	0	0	0
2,000	30	35	37	45
3,000	62	75	73	95
4,000	95	110	108	130
5,000	130	145	141	175
6,000	165	183	177	217
7,000	200	.	..	...
8,000			..	...
9,000	..		.	....
8,000	..	.	....	....
7,000	200		..	....
6,000	170	183	177	217
5,000	154	150	180	180
4,000	105	120	112	137
3,000	70	83	75	100
2,000	35	40	35	52
1,000	3	4	2	4

WHITE MARBLE, VERMONT, UNITED STATES

This is a pure white marble indistinguishable from the Carrara marble in a hand specimen. Under the microscope also it resembles this rock very closely. The grains show, however, a somewhat greater variation in relative size and there is a tendency to a flattening in one direction, giving a very faint foliation to the rock. On this account only a single specimen was used, since the foliation in question, although barely perceptible, might affect the elasticity of rock, and it was therefore considered safer to rely upon the Carrara marble in measuring the elastic constants of this class of rocks. In the prism of Vermont marble employed, the foliation lay in the direction of the longer axis of the prism. It is probable that this foliation would not be found in all Vermont marbles, but happened to be present in the specimen procured for examination.

A photomicrograph of a thin section of the rock, in this case taken between crossed nicols and magnified 31 diameters, is shown in Plate III. A color-process photograph was not prepared, since the rock in such a photograph would be identical in appearance with the Carrara marble, of which such a photograph has already been given.

Vermont Marble.

Size	1.017 1.012	
Area	1.029	
E	7,592,000	
σ	.263	
D	5,341,000	
C	3,000,000	
Load (in pounds)	Longitudinal compression (multiply readings by 4 for millionths)	Lateral extension (millionths)
1,000	0	0
2,000	40	30
3,000	80	64
4,000	120	100
5,000	157	135
6,000	200	172
7,000	. .	
8,000		
9,000	.	.
8,000	. .	.
7,000	. . . .	. . .
6,000	200	172
5,000	165	140
4,000	125	108
3,000	90	75
2,000	51	39
1,000	5	1

[illegible]

[illegible]

A square prism of the marble was employed in measuring the elastic constants, and the detailed results are given in the accompanying table, and are represented in graphic form in figure 8. I represents longitudinal compression and II lateral extension.

The following are the values obtained:

$E = 7,592,000$; $\sigma = 0.263$; $D = 5,341,000$; $C = 3,000,000$

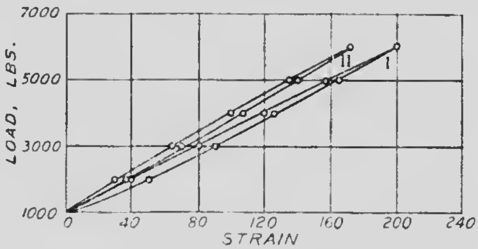


FIG. 8. Vermont marble. Stress-strain curves.

MARBLE, TENNESSEE, UNITED STATES.

This is a marble known in trade as "Pink Tennessee," and is largely used for decorative work. It has a brownish pink color and when polished shows a somewhat mottled surface.

Under the microscope it is seen to consist of rather large irregular-shaped and often distinctly rounded individuals of calcite, which are fitted closely together along sharp and in some cases crenulated lines. These individuals are almost invariably traversed by narrow lamellæ, due to polysynthetic twinning, and are occasionally twisted so that they show an undulatory extinction. Between these large calcite individuals there are frequently present masses of what is apparently a tabulate coral, showing sheaves of tubes which in cross section are approximately circular in outline. The calcite individuals are often embedded in this coralline material, as if they had been developed by its recrystallization; in other cases, however, their appearance suggests a derivation from crinoidal fragments. All the tubes of the coral, as well as the interspaces of the tubes, if any existed, are now filled with calcite, so that the substance of the rock is continuous, resulting in a compact marble. Fragments of the rock dissolve readily in cold dilute hydrochloric acid, leaving only a very trifling residue, which has the color of the rock itself.

A color-process photograph of a polished surface of the rock is shown in Plate IV A, and a photomicrograph of a thin section of the rock, taken in ordinary light and magnified 27 diameters, is shown in Plate IV B. In this photomicrograph a fragment of the coralline material is seen in the center of the field, while the border is formed chiefly of individual calcite grains.

Tennessee Marble.

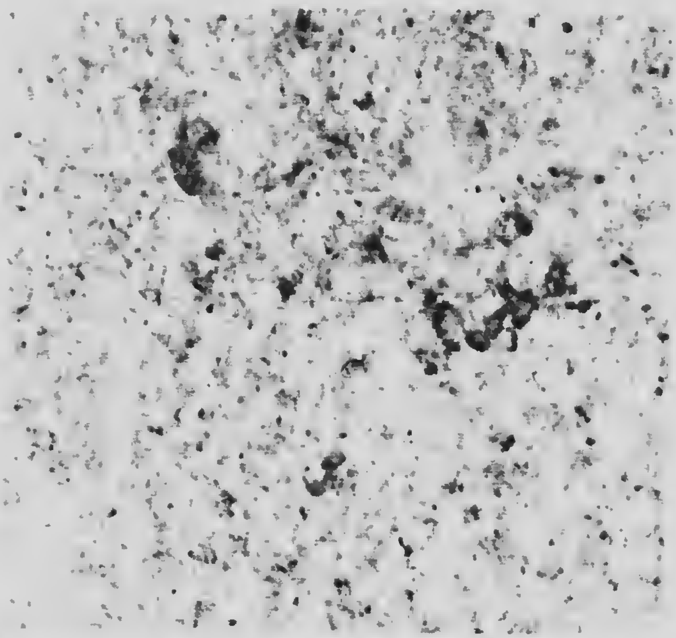
No.	*a*	*a*	*b*	*b*	*c*	*c*	*c*
Size	1.037 × .996		1.004 × .911		1 × .97		
Area	1.033	1.033	.915	.915	.97	.97	.97
E	9,140,000	8,960,000		9,260,000	8,760,000	8,900,000	8,900,000
σ	281	267		248	247	248	258
D	6,080,000	5,970,000	6,070,000	5,970,000	5,780,000	5,770,000	6,130,000
C	3,688,000	3,595,000	3,650,000	3,725,000	3,510,000	3,575,000	3,540,000

LONGITUDINAL COMPRESSION. MULTIPLY READINGS BY 4 FOR MILLIONTHS.

Load in pounds	Side *C.*	Side *P*	Side *P*	Side *C.*	Side *C*	Side *P*	Side *P.*
1,000	0	0	0	0	0	0	0
2,000	20	35	40	30	35	30	25
3,000	65	70	75	60	75	70	60
4,000	100	100	110	100	110	105	95
5,000	130	130	150	140	145	140	130
6,000	165	170	190	185	184	180	170
7,000	200	205	230	220		215	210
8,000	230	230	270	270		250	250
9,000	265	270	300	295		290	290
8,000	230		275			275	
7,000	200		250			255	
6,000	170		220		184	190	
5,000	135		180		170	165	
4,000	100		130		140	120	
3,000	65		110		100	90	
2,000	30		45		60	60	
1,000	5	4	10	5	5	5	4

LATERAL EXTENSION—MILLIONTHS.

No.	*a*	*a*	*b*	*b*	*c*	*c*
Size	1.037	.996	.911	1.004	.970	1.000
Load in pounds	Side *C*	Side *P*	Side *C*	Side *P.*	Side *C*	Side *P*
1,000	0	0	0	0	0	0
2,000	20					
3,000	50					
4,000	80					
5,000	105					
6,000	130	125	130	153	141	140
7,000	160					
8,000	200					
9,000	220					
8,000	180					
7,000	160					
6,000	130	125	130	153	141	140
5,000	100					
4,000	75					
3,000	50					
2,000	20					
1,000	−15	−7	2	5	8	8



A. PHOTOGRAPH OF POLISHED SURFACE, (NATURAL SIZE)

B. PHOTOMICROGRAPH OF THIN SECTION, (x 27 DIAM.-ORDINARY LIGHT)

MARBLE, TENNESSEE, ("PINK TENNESSEE")

Three square prisms of the rock were employed in measuring the elastic constants, and on these seven sets of measurements of vertical compression and six of lateral extension were made, as shown in the table on page 30.

The averages of the results obtained are as follows:

$E = 9,006,000$; $\sigma = 0.2513$; $D = 5,967,000$; $C = 3,607,000$

The difference between the highest and lowest values obtained for D is 360,000. As will be seen by consulting figure 9 the rock is almost free from hysteresis. In this figure I represents the longitudinal compression and II lateral extension.

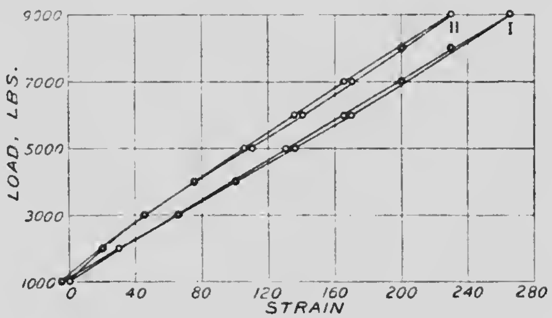


FIG. 9.—Tennessee Marble. Stress-strain curves.

FOSSILIFEROUS LIMESTONE (TRENTON FORMATION), MILE END QUARRY, MONTREAL, CANADA.

This is a typical fossiliferous limestone of the Trenton formation (Ordovician). It was taken from a massive bed 2 feet in thickness known as the "Lower Bed" at the quarry from which the greater part of the building stone for the city of Montreal is obtained. The rock is dark gray in color, and is compact and solid in character.

Under the microscope it is seen to be composed of fragments of fossils which are in some cases angular and in others more or less rounded. They are chiefly bits of Monticulipora and of Crinoids and show the structure of these organisms perfectly. These fragments lie embedded in clear transparent calcite, occurring as large individuals which form a continuous mosaic, giving rise in this way to a perfectly compact rock.

A color-process photograph of a polished surface of this rock is given in Plate V A. A photomicrograph of a thin section of the rock, taken in ordinary light and magnified 27 diameters, is shown in Plate V B. In the photomicrograph a fragment of a Monticuliporid is seen in the center of the field, while the darker areas about the periphery of the field are Crinoid fragments, each with a secondary enlargement, consisting of pure calcite, surrounding it.

Trenton Limestone, Montreal, Canada.

No.	*a*	*a*	*b*	*b*	*a*	*b*
Size	97		984		97	984
Area	749	749	762	.762	. . .	. . .
E.	9,280,000	9,490,000	9,120,000	8,930,000	. .	. .
σ	25	2562	2545	2482	.	. . .
D	6,180,000	6,480,000	6,190,000	5,820,000	.	
C	3,710,000	3,775,000	3,645,000	3,415,000	.	. . .
Longitudinal compression.—Multiply readings by 4 for millionths.					Lateral extension (millionths).	
Load (in pounds).	Side *U.*	Side *P.*	Side *V.*	Side *P.*		
1,000	0	0	0	0	0	0
2,000	50	50	50	50	30	34
3,000	90	90	85	90	60	70
4,000	140	135	135	130	95	100
5,000	180	175	180	170	135	140
6,000	225	220	225	230	175	180
7,000	. . .	. . . .	. . . .	. . . .	. . .	. . . .
8,000	. .	. . .	. . . .	. . . .	. . . .	. . . .
9,000		. . . .	. . . .	. . . .	. . .	. . . .
8,000		.	. . .	. . . .	. . . .	. . . .
7,000			. .	. . .		. . . .
6,000	225	220	225	230	175	180
5,000	185	180	100	185	140	147
4,000	140	143	140	140	100	106
3,000	95	95	90	95	65	73
2,000	55	54	54	55	32	35
1,000	4	0	4	5	2	2

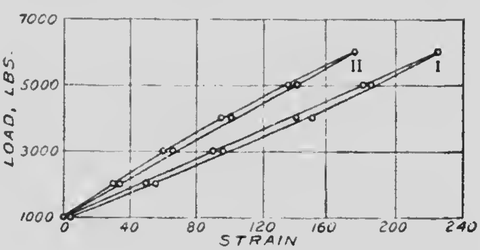
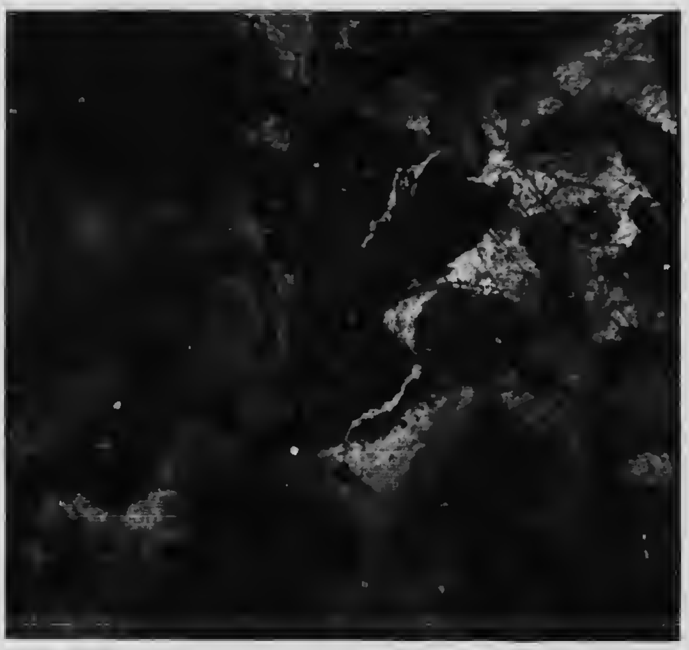


FIG. 10.—Trenton limestone. Stress-strain curves.

A. PHOTOGRAPH OF POLISHED SURFACE, (NATURAL SIZE)



B. PHOTOMICROGRAPH OF THIN SECTION, (× 27 DIAM.-ORDINARY LIGHT)

TRENTON LIMESTONE, MONTREAL, CANADA.

The elastic constants of the rock were measured on two round columns, four measurements of vertical compression and two of lateral extension being made. The results are given in the table on page 32.

The averages of the results obtained are as follows:

$$E = 9,205,000; \quad \sigma = 0.2522; \quad D = 6,167,500; \quad C = 3,636,000.$$

The difference between the highest and lowest readings for D is 660,000. The results of the measurement of specimen *a* are shown in graphic form in figure 10. I represents longitudinal compression and II lateral extension.

THE ELASTIC CONSTANTS OF ROCKS COMPOSED OF MORE THAN ONE MINERAL.

ACID PLUTONIC ROCKS.

GRANITE, BAVENO, ITALY.

This well known granite is pale pink in color, and although coarser in grain than the rocks just described, is a granite of medium grain and is very uniform in character. It resembles the Lily Lake granite closely in appearance, although it is a little finer in grain.

It is composed essentially of quartz and orthoclase, with very small proportion of biotite; the biotite is in places somewhat altered to chlorite, and the orthoclase is in places somewhat turbid from the presence of kaolin, but the rock may nevertheless be characterized as a very fresh one.

It has a typical hypidiomorphic granular structure. The orthoclase often shows faint microperthitic intergrowths, and some plagioclase is present as an accessory constituent. The quartz usually shows a very faint undulatory extinction, although this is in some cases quite distinct.

A color-process photograph of a polished surface of the rock is shown in Plate VI A, and a photomicrograph of a thin section of the rock is shown in Plate VI B. The latter was taken between crossed nicols in polarized light and is magnified 30 diameters. The crack seen crossing the rock in the photomicrograph was developed during the grinding of the thin section and does not indicate any shattering or lack of continuity in the substance of the rock itself.

Four round columns, *b*, *c*, *d* and *e*, were employed in the measurement of the elastic constants of this granite. On specimen *b* a double set of measurements was made in each of the planes *U* and *P*, which planes were at right angles to one another. In the case of column *c* two sets of measurements were made in two planes, also at right angles to one another (referred to as "first holes" and "second holes"). In column *d* four sets of holes were drilled, so as to carry out measurements on four diametral planes, making angles of 45° with one another. The first set of holes, however, were defective, so measurements were made on the second, third, and fourth sets only. On column *e* a single set of measurements was completed when the column broke.

In this way ten measurements of vertical compression and six of lateral extension were obtained. The results are presented in the table on page 35.

The averages of the results obtained are as follows:

$$E = 6,833,000; \quad \sigma = 0.2528; \quad D = 4,604,000, \quad C = 2,724,800$$

The difference between the highest and lowest results obtained for *D* amounts to 500,000.

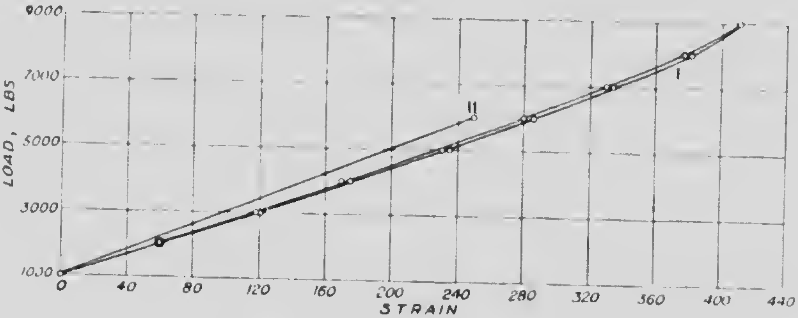
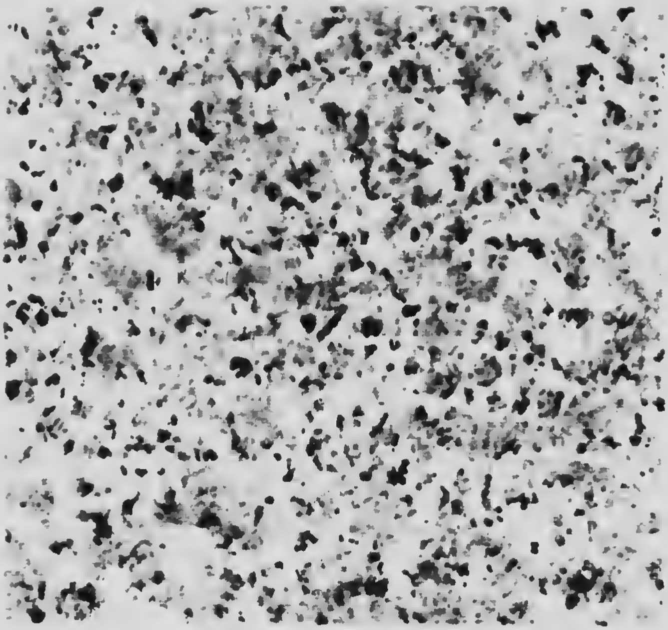


FIG. 11.—Baveno Granite. Stress strain curves.

As mentioned in the chapter on the "Application of the Method of Simple Compression to the Case of Rocks," in order to obtain consistent and reliable results, the specimen of the rock (and for that matter the same is true of the specimen of any metal if its elastic constants are to be determined) must first be bought to "state of ease" by loading and unloading it several times in succession, employing each time a pressure equal to the maximum load to which the specimen is to be subjected, when the measurements are subsequently made.

As a matter of interest in the case of the Baveno granite (as well as in that of the Stanstead granite referred to later), readings were taken during the first four cycles of compression, when this state of ease was being induced, and the results are presented graphically in figure 12.



[illegible]OGRAPH [illegible] (NA[illegible]RA[illegible]

B. PHOTOMICROGRAPH OF [illegible]N SECTION, (X 30 DIAM. NICOLS CROSSED)

GRANITE, BAVENO, ITALY

Granite, Baveno, Italy.

No.	*b*	*b*	*b*	*b*	*c*	*c*	*d*	*d*	*d*	*e*
Size	.978	.			978	..	.978	..	...	978
Area	.75			...	.75	...	.75	.	....	.75
Side	*U.*	*U.*	P_1	P_2	1st holes	2d holes	2d holes	3d holes	4th holes	....
E.	6,620,000	6,730,000	7,430,000	6,950,000	6,950,000	6,840,000	6,840,000	6,620,000	6,730,000	6,620,000
σ	.2483	.2525	.2465	.2505	.2505	.247	.265	.257	.261	.2495
D.	4,380,000	4,530,000	4,880,000	4,645,000	4,645,000	4,470,000	4,850,000	4,540,000	4,680,000	4,420,000
C.	2,650,000	2,682,000	2,980,000	2,780,000	2,780,000	2,730,000	2,700,000	2,631,000	2,670,000	2,645,000

LONGITUDINAL COMPRESSION—MULTIPLY READINGS BY 4 FOR MILLIONTHS.

Load (in pounds).										
1,000	0	0	0	0	0	0	0	0	0	0
2,000	.		60	70	.	.	.	..	....	80
3,000	...	.	118	130	...				....	145
4,000	...	.	175	180	....	.			.	210
5,000	....		230	240	...				...	260
6,000	315	310	280	300	300	305	305	315	310	315
7,000	....		330	342	.			..		368
8,000	....	....	380	400			.		.	419
9,000	....	..	410	450				.		465
8,000	....		385	410			.	...	..	420
7,000	...	..	335	390	.	.	.	.	.	375
6,000	315	310	285	312	300	305	305	315	310	325
5,000			235	254				.	..	280
4,000	...	.	170	204			.	..		225
3,000	....	.	120	145					..	160
2,000	....	.	60	85					..	90
1,000	2	5	3	18	2	4	4	10	8	10

LATERAL EXTENSION—MILLIONTHS.

No.	*b*		*b*	*c*	*d*	*e*
Size	.978		978	978	978	.978
Area	....		.....	....	....	....
Side	P_1 and P_2		*U*	....	......	....
1,000	0	0	0	0	0	0
2,000	...	....	...	....	....	....
3,000	....	....	....	....	....	....
4,000	...	....	....	....	....	....
5,000	....	....	....	....	....	....
6,000	216	235	245	235	253	246
7,000	....	....	...	....	....	....
8,000	....	....	....	....	....	....
9,000	....	....	....	....	....	....
8,000	....	...	....	....	....	....
7,000	....	....	....	....	....	....
6,000	216	235	245	235	253	246
5,000	....	....	....	....	....	....
4,000	....	....	....	....	....	....
3,000	....	....	....	....	....	....
2,000	....	....	....	....	....	....
1,000	1	4	5	7	5	10

The curves represent the readings for longitudinal compression, and, as will be seen, after the first cycle of compression the rock did not return quite to its original position, but this imperfection in elasticity becomes progressively smaller in the subsequent loadings till in the fourth compression cycle the return is almost perfect and the hysteresis very small

Figure 11 shows the curves obtained by plotting the values secured from the measurement of the elastic constants of specimen *b* after the state of ease had been induced, and if the curve for longitudinal compression in this be compared with that shown in figure 12 the great improvement in the elasticity of the rock will at once be seen In figure 11, I represents longitudinal compression and II lateral extension

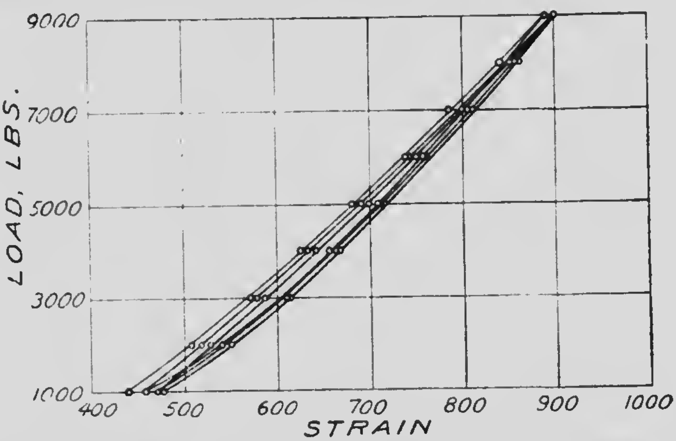


FIG. 12 Stress-strain curves obtained in the first four cycles of compression from a column of Baveno granite, showing the progress toward a state of ease.

GRANITE, PETERHEAD, SCOTLAND.

A pink granite which is almost indistinguishable from the Lily Lake granite in hand specimens or polished blocks In the thin sections also the resembl[illegible] is very close The description given of the Lily Lake granite wo[illegible] apply to this rock, except that the Peterhead granite contains ra[illegible] plagioclase and less biotite The microperthite also is more turbid, i[illegible] greater alteration The quartz and microperthite which make up the [illegible] part of the rock have evidently crystallized out at about the same time, since they have equally good crystalline outlines and impress their form upon each other with about equal frequency The quartz usually shows pronounced undulatory extinction

Owing to its practical identity with the Lily Lake granite, in appearance and composition, it has been considered unnecessary to give either a photograph of the polished surface of the rock or a photomicrograph of a thin section

Those given for the Lily Lake granite may be considered as representing this rock also Two square prisms of the rock were prepared and on these five sets of measurements of vertical compression and two of lateral expansion were made These are given in the accompanying table, and the curves

Granite, Peterhead, Scotland.

No.	*b*	*b*	*b*	*a*	*a*	*b*	*a*
Size.	1 006 1			998 1 056		1,000	.998
Area	1 006	1 006	1 006	1 052	1 052	. .	. . .
E.	8,020,000	8,280,000	8,375,000	8,400,000	8,400,000	. .	. . . .
σ	204	212	215	214	213	. .	. . . .
D	4,520,000	4,790,000	4,860,000	4,900,000	4,890,000	. .	. . .
C	3,330,000	3,415,000	3,450,000	3,400,000	3,400,000	. .	. . .
	Longitudinal compression (multiply readings by 4 for millionths).					Lateral extension (millionths).	
Load (in pounds).	Side. *U.*	Side. *U.*	Side. *P.*	Side. *P.*	Side. *P.*		
1,000	0	0	0	0	0	0	0
2,000	40	40	40	40	. . . .	25	25
3,000	85	80	85	80	. . . .	50	49
4,000	125	120	125	120	. . . .	75	74
5,000	165	160	160	160	. . . .	100	101
6,000	200	195	195	200	. . . .	125	125
7,000	240	230	225	230	. . . .	150	149
8,000	270	260	260	270	. . . .	178	175
9,000	310	300	296	310	309	203	200
8,000	270	. . . .	. . . .	. . . .	. . .	180	170
7,000	245	. . . .	. . . .	. . . .	. . . .	155	150
6,000	205	. . . .	. . . .	. . . .	. . . .	130	125
5,000	170	. . . .	. . . .	. . . .	. . . .	105	100
4,000	135	. . . .	. . . .	. . . .	. . . .	78	75
3,000	95	. . . .	. . . .	. . . .	. . . .	54	49
2,000	50	. . . .	. . . .	. . . .	. . . .	26	20
1,000	5	4	−4	5	4	−5	−2

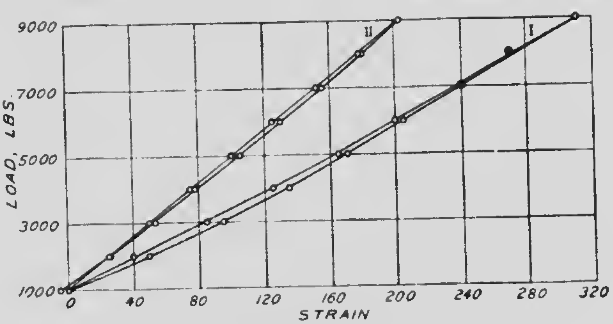


FIG. 13.—Peterhead granite. Stress-strain curves.

given by *b* are shown in figure 13. Of these curves, I represents longitudinal compression and II lateral extension.

The averages of the results obtained are as follows:

$$E = 8,295,000; \quad \sigma = 0.2112; \quad D = 4,792,000; \quad C = 3,399,000$$

The difference beween the highest and lowest values obtained for D amounts to 380,000, or if one abnormally low determination be omitted the difference is 110,000

GRANITE, LILY LAKE, PROVINCE OF NEW BRUNSWICK, CANADA.

A typical rather coarse-grained pink granite. Under the microscope it is seen to present the usual hypidiomorphic structure of this rock, and to be composed of biotite, microperthite, and quartz as essential constituents. A small amount of plagioclase occurs as an accessory constituent. There are also a few minute crystals of a highly doubly refracting mineral which has also a high index of refraction, and apparently crystallizes in square prisms. This is probably zircon or possibly monazite.

The feldspars and quartz preponderate largely. The microperthite, which is the most abundant constituent in the rock, is composed of a minute intergrowth of two feldspars, in neither of which can twinning be detected. One is, in all probability, orthoclase and the other albite. The former is more or less turbid from the presence of alteration products, such as are commonly found in this mineral species, while the latter is clear and fresh. The quartz shows marked undulatory extinction as in the case of the Westerly granite. The biotite is fresh and deep brown in color.

This rock is, as stated above, a typical granite, rather coarse in grain, and which has undergone but very little alteration.

A color process photograph of a polished surface of the rock is seen in Plate VII A and a photomicrograph of a thin section magnified 30 diameters and taken between crossed nicols in polarized light, is shown in Plate VII B.

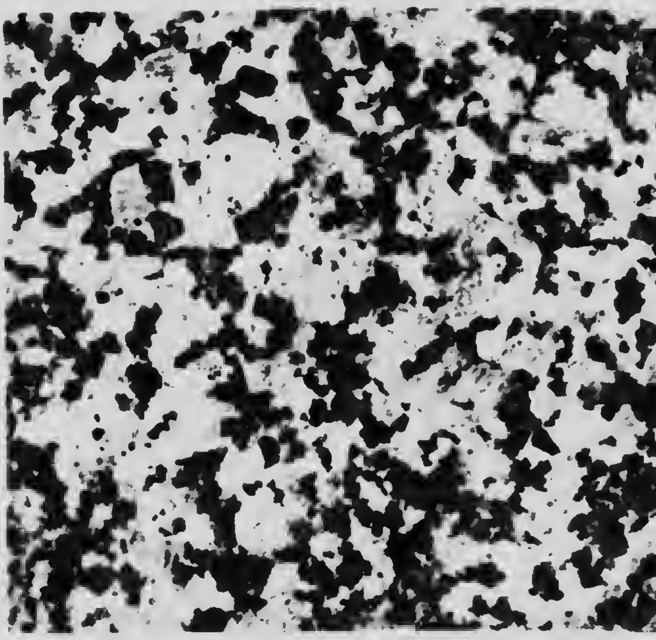
Two square prisms of the rock were prepared and their elastic constants determined. The results are given in the table on page 39.

The stress-strain curves given by specimen *c* are shown in figure 14. In this figure I represents longitudinal compression and II lateral extension.

The means of the results obtained are as follows:

$$E = 8,165,000; \quad \sigma = 0.1982; \quad D = 4,517,500; \quad C = 3,380,000.$$

The difference between the two determinations of D is only 105,000.



A. PHOTOGRAPH OF POLISHED SURFACE, (NATURAL SIZE)

B. PHOTOMICROGRAPH OF THIN SECTION (x 30 DIAM.-NICOLS CROSSED)

GRANITE, LILY LAKE, CANADA.

Granite, Lily Lake, Province of New Brunswick, Canada.

No.	*a*	*c*	*a*	*c*
Size	.965 .955	.995 1.05		....
Area	.922	1.045		....
E	8,230,000	8,100,000		....
σ	.2	.1965		....
D	4,570,000	4,465,000		....
C	3,370,000	3,390,000	....	....

Load (in pounds).	Longitudinal compression (multiply readings by 4 for millionths).		Lateral extension (millionths).	
1,000	0	0	0	0
2,000	43	40	21	15
3,000	84	80	39	41
4,000	125	120	59	62
5,000	161	155	81	84
6,000	201	190	100	106
7,000	238	225	119	130
8,000	274	260	141	152
9,000	308	295	159	185
8,000	277	268	140	155
7,000	245	234	118	135
6,000	208	200	99	110
5,000	170	170	80	90
4,000	133	132	60	70
3,000	93	92	39	50
2,000	50	50	20	25
1,000	0	−4	0	0

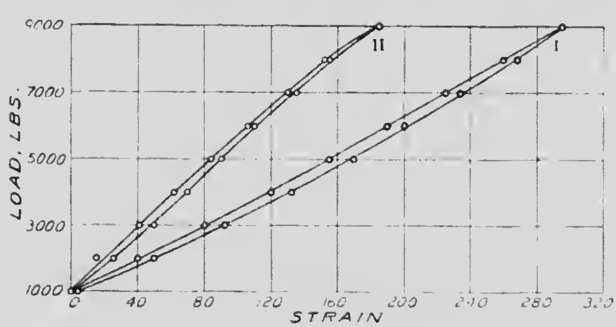


FIG. 14.—Lily Lake Granite. Stress-strain curves

GRANITE, WESTERLY, RHODE ISLAND, UNITED STATES

This rock is a fresh, very fine grained, massive, pale pink granite, being much finer in grain than the other granites referred to in this paper.

Under the microscope it is seen to be composed essentially of biotite, microcline, orthoclase, and quartz. In addition to these constituents a small percentage of plagioclase and a few grains of magnetite are present as accessory constituents, together with a little chlorite and muscovite as alteration products.

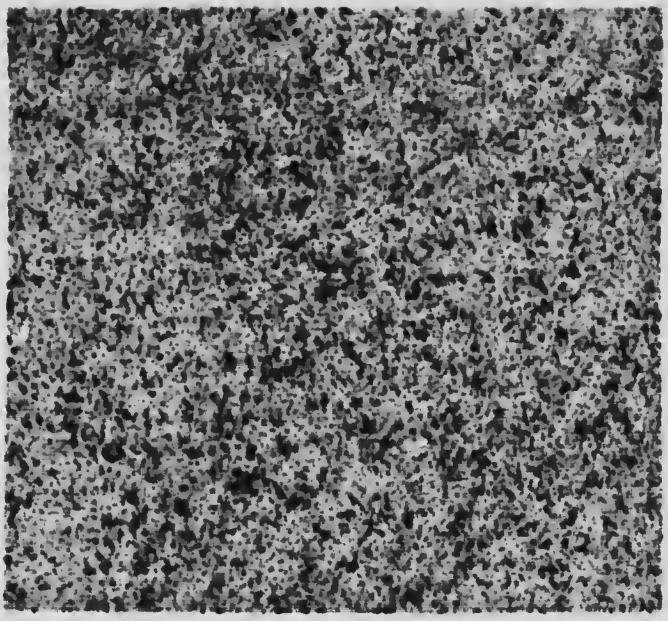
The feldspars form the greater part of the rock, microcline being by far the most abundant of these. It shows in a striking manner the characteristic cross hatched twinning of this species, and is usually quite fresh. The orthoclase in untwinned individuals is frequently distinctly turbid from the development of kaolin, and in a few places muscovite in larger individuals can be seen inclosed in it, apparently developing as a secondary product at its expense.

The quartz, which is next in abundance, usually shows marked undulatory extinction, and some grains have been so strained that they fall into areas with distinctly different optical orientations. The quartz, instead of occupying corners between the feldspar individuals, usually occurs as subangular or more or less rounded grains associated with the feldspar, and apparently more nearly contemporaneous with this mineral in its crystallization than is usually the case. The rock often shows a tendency to granophyric structure, small rounded grains or vermiform inclusions of quartz being sometimes seen in the microcline. The structure otherwise is of the normal granite type. The biotite is very subordinate in amount and is more or less changed into chlorite.

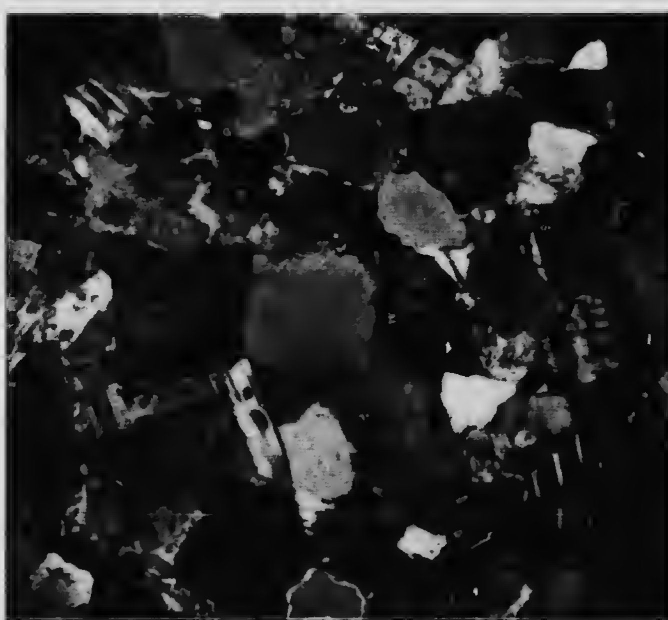
Although these decomposition products are present, the rock can not be considered as one which has undergone much alteration. It has, as a matter of fact, undergone very little, and is to be classed as a distinctly fresh rock—much fresher than granites usually are.

A color process photograph of the rock is seen in Plate VIII A and a photomicrograph of a thin section taken between crossed nicols in polarized light and magnified 30 diameters is shown in Plate VIII B.

Four test pieces were used in measuring the elastic constants, viz, two square prisms, *a* and *b*, and two round columns, *c* and *d*. Two sets of determinations were made on each of the first three specimens, the instruments being attached to different pairs of sides in each case, and four sets of determinations were made on specimen *d* in planes making angles at 45° with one another. Ten determinations of vertical compression and three of lateral extension were thus made the results of which are given in the following table:



A. PHOTOGRAPH OF POLISHED SURFACE, (NATURAL SIZE)



B. PHOTOMICROGRAPH OF THIN SECTION, (X 30 DIAMETERS NICOLS CROSSED)

GRANITE, WESTERLY, RHODE ISLAND.

Granite, Westerly, Rhode Island, U. S. A.

No.	*a*	*a*	*b*	*b*	*c*	*c*	*d*	*d*	*d*	*d*
Size	1.008 1.002		.981 .929		.975		.975			
Area	1.01		.91		.75		.75			
Side	*P'*	*P*	*P*	*P'*	1st holes	2d holes	1st hole	2d holes	3d holes	4th holes
E	7,180,000	7,090,000	7,628,000	7,715,000	7,670,000	7,335,000	7,575,000	7,335,000	7,170,000	7,250,000
σ	.21	.1985	.241	.211			.225	.223	.2225	.222
D	4,110,000	3,980,000	3,938,000	3,848,000			4,600,000	4,420,000	4,320,000	4,340,000
C	2,970,000	2,960,000	3,070,000	3,185,000			3,090,000	2,980,000	2,940,000	2,961,000

LONGITUDINAL COMPRESSION. MULTIPLY READINGS BY 4 FOR MILLIONTHS.

Load (in pounds)	Side *P*	Side *P*	Side *P'*	Side *P'*	1st holes	2d holes	1st holes	2d holes	3d holes	4th holes
1,000	0	0	0	0	0	0	0	0	0	0
2,000	50	40	50		..					
3,000	95	80	100	155			143	145	145	144
4,000	145	120	150							.
5,000	180	160	190							
6,000	225	210	235	310			298	301	302	303
7,000	265	260	275					.	.	. . .
8,000	305	310	315						.	. . .
9,000	345	319	361	355	435	455	440	455	465	460
8,000	310		320					. . .	. . . .	. . . .
7,000	270		280		.	.	. .	. . .	. . .	. . .
6,000	235		240	312			300	305	305	305
5,000	200		195					.	. .	. .
4,000	160								.	. . . .
3,000	110			157			115	149	150	149
2,000	60							.	.	. . . .
1,000	5			3			3	10	15	12

LATERAL EXTENSION—MILLIONTHS.

No.	*a*	*b*	*d*
Size	1.002	.929	.975
Load (in pounds).			
1,000	0	0	0
2,000	25	30	30
3,000	50	50	80
4,000	75	85	120
5,000	100	125	175
6,000	130	177	209
7,000	160		. .
8,000	190		. . .
9,000	220	. .	. . .
8,000	195	. . .	. . . .
7,000	165	. . . .	. . . .
6,000	140	177	209
5,000	115	135	160
4,000	90	100	130
3,000	60	70	90
2,000	30	30	45
1,000	0	0	5

The stress-strain curves obtained from specimen *a* are given in [illegible] re 15 In this figure, I represents longitudinal compression and II lateral [illegible] nsion

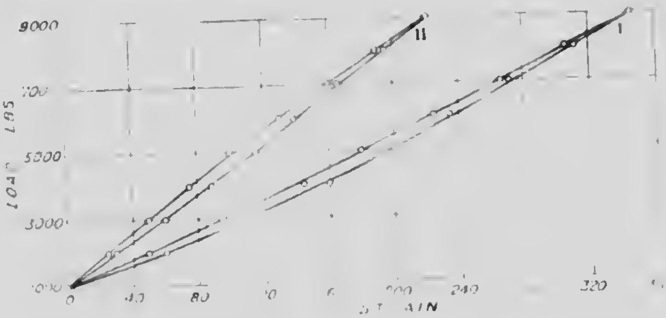


FIG. 15.—Westerly Granite. Stress-strain curve

[illegible] averages of the value[illegible] obtained are as follows:

E [illegible] 7,[illegible] 4,500; [illegible] 195, *D* = 4,397,500;

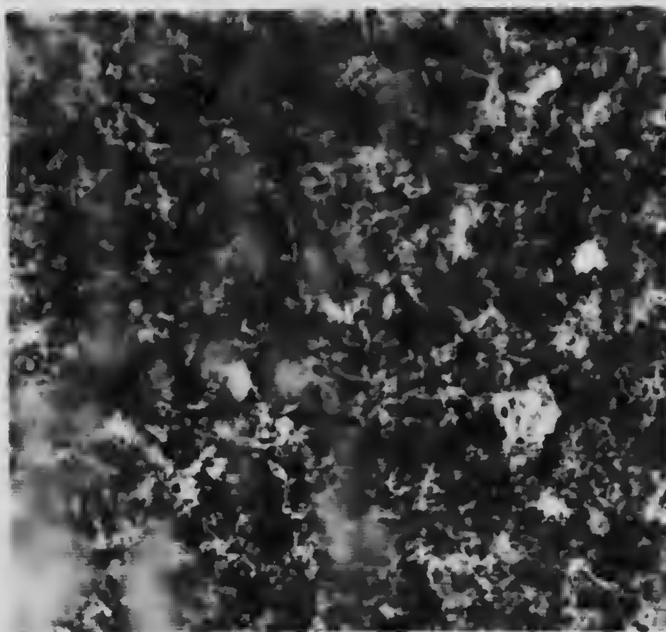
The difference[illegible] between the highest and lowest values [illegible] our de[illegible]nations of *D* on specimen *d* was only 280,000 [illegible] Of the other [illegible] mus [illegible] on an average somewhat lower, and *b* [illegible] mewha[illegible] igh[illegible] results

GRAN[illegible] OF QUINCY, MASSACHUSETTS, UNITE[illegible] ATES

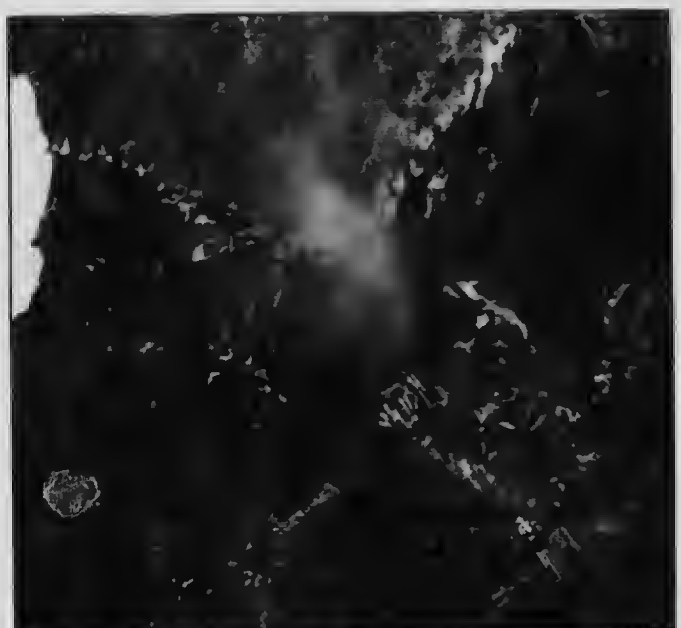
[illegible] rock is a [illegible] ather co[illegible] rse grained g[illegible] granite comp[illegible] sed [illegible] largely of microp[illegible] rthite and quartz. The iron magnesia constituent[illegible] are [illegible] represente[illegible] by a very deep [illegible] n, almost black, hornblende associated with [illegible] ch [illegible] appears to be a s[illegible] ller amount of a ver[illegible] dark colored p[illegible] roxene. These constituents belong to the alkali rich varieti[illegible] their respective familie[illegible] [illegible] so opaque that it is difficul[illegible] to determi[illegible] heir pr[illegible] ise character [illegible] [illegible] ery irregular in shape, [illegible] n th[illegible] spar g[illegible] and [illegible] penetrated by cryst[illegible] [illegible] show[illegible] that the separated [illegible] t later than the feldsp[illegible] Th[illegible] s stron[illegible] dulate[illegible] extinction. The rock is fresh an[illegible] nalter[illegible]

A color process photograph of [illegible] lis[illegible] [illegible] [illegible] ranite is shown in Plate IX A, and a pho[illegible] ograph[illegible] [illegible] take[illegible] between crossed nicols in polarized light a[illegible] agnified [illegible] repro[illegible] ed in Plate IX B.

Two large specimens of the rock, [illegible] hich differed sli[illegible] from one [illegible] appearance were secured and exam[illegible] d. Three sq[illegible] are prisms, *a*, *c* [illegible] were prep[illegible] from one specimen a[illegible] one square prism, *b*, from the [illegible] ther



[illegible] SURFACE [illegible]



B. PHOTOMICROGRAPH [illegible] SECTION, [illegible] NICOLS CR[illegible]
[illegible] MASSA[illegible]

Granite, Quincy, Massachusetts, United States.

	First specimen.						Second specimen.	
No.	*a*	*a*	*c*	*c*	*d*	*d*	*b*	*b*
Size	.989 1.071		1.063 .955		1.011 .954		.945 .892	
Area	1.06	1.06	1.01	1.01	.965	.965	.843	.843
E.....	6,560,000	6,840,000	6,630,000	6,630,000	6,820,000	7,000,000	8,135,000	8,360,000
σ.....	.185	.1925	.21	.21	.244	.25	.1915	.204
D....	3,470,000	3,710,000	3,810,000	3,810,000	4,440,000	4,666,000	4,390,000	4,720,000
C.....	2,765,000	2,865,000	2,760,000	2,760,000	2,740,000	2,800,000	3,410,000	3,480,000

LONGITUDINAL COMPRESSION—MULTIPLY READINGS BY 4 FOR MILLIONTHS.

Load (in pounds).	Side *U.*	Side *P.*	Side *U.*	Side *P.*	Side *U.*	Side *P.*	Side *U.*	Side *P.*
1,000	0	0	0	0	0	0	0	0
2,000	60	50	56	....	45	....	....	50
3,000	110	95	109	....	100	....	....	100
4,000	160	145	161	....	150	....	....	142
5,000	200	185	206	....	198	....	....	193
6,000	240	230	259	....	246	....	....	225
7,000	280	270	291	....	290	....	....	260
8,000	320	310	334	....	330	....	....	310
9,000	360	345	374	374	380	370	365	355
8,000	321	315	325	....	340	....	....	314
7,000	282	280	290	....	298	....	....	274
6,000	245	235	260	....	250	....	....	235
5,000	203	195	210	....	210	....	....	190
4,000	162	140	165	....	165	....	....	145
3,000	112	90	110	....	115	....	....	100
2,000	63	40	60	....	60	....	....	50
1,000	4	5	5	0	5	5	3	5

LATERAL EXTENSION—MILLIONTHS.

	First specimen.			Second specimen.	
No.	*a*	*c*	*d*	*b*	*b*
Size	.989	.955	1.011	.892	.945
1,000	0	0	0	0	0
2,000	....	25	35	24	20
3,000	....	55	70	51	45
4,000	....	90	110	76	70
5,000	....	115	150	101	100
6,000	....	145	190	125	125
7,000	....	175	230	157	155
8,000	....	200	270	174	186
9,000	210	240	300	206	219
8,000	....	205	275	175	192
7,000	....	180	240	153	164
6,000	....	155	195	127	134
5,000	....	120	155	103	105
4,000	....	95	120	77	88
3,000	....	60	75	50	50
2,000	....	30	40	25	25
1,000	5	5	10	2	3

specimen, which was rather darker in color Two series of compression determinations were made on each of these prisms. Eight series of measurements were thus made of vertical compression and five of lateral extension

In the second specimen of the rock, D was found to have a rather higher value than in the case of the first specimen, although prism d, cut from the first specimen, approaches this value closely The duplicate determinations made on each of the prisms agree very closely with one another. The results of the measurements are given in the table on page 44

The average of the values obtained in the case of the first specimen are as follows:

$E = 6,747,000$; $\sigma = 0.2152$; $D = 3,984,000$; $C = 2,781,600$.

The average of those obtained from the second specimen are as follows:

$E = 8,247,500$; $\sigma = 0.1977$; $D = 4,555,000$; $C = 3,445,000$.

In this case, as has been mentioned, the two specimens represent different varieties of the Quincy granite. The stress strain curve given by specimen b is shown in figure 16 In this figure, I represents longitudinal compression and II lateral extension.

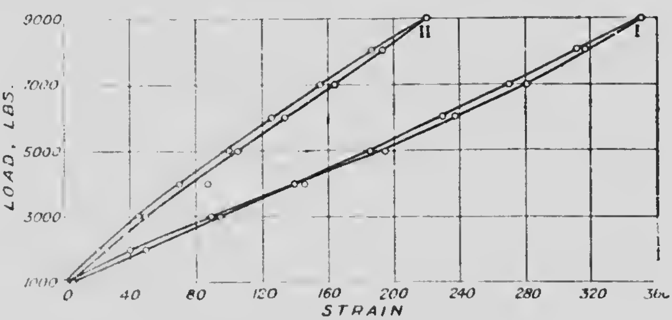


FIG. 16 Quincy Granite. Stress strain curves.

GRANITE, STANSTEAD, PROVINCE OF QUEBEC, CANADA

This is a fine grained gray granite, which occurs as a large intrusive mass cutting strata of lower Paleozoic age. It is extensively quarried and is largely used as building material and for paving sets in the city of Montreal

It is biotite muscovite granite, having as its essential constituents orthoclase, quartz, and biotite, but containing also a rather small amount of muscovite and epidote, both of which occur as skeleton crystals of considerable dimensions, for the most part growing in the feldspar and apparently of secondary origin The rock is very fresh, being almost entirely free from the usual decomposition products In addition to orthoclase, the rock con tains a considerable percentage of microcline and of a plagioclase of the soda lime series The mica is relatively more abundant than in the other granites described in the present paper The quartz shows marked undulatory extinction and in some cases even an incipient granulation. The size of the grain of this rock is intermediate between that of the Westerly and the other granites, which latter are themselves about equally coarse.

The elastic constants were measured on three square prisms, four sets of measurements of vertical compression and three of lateral extension being made. The results are given in the following table:

Granite, Stanstead, Province of Quebec, Canada.

No.	*a*	*b*	*b*	*d*	*a*	*b*	*d*
Size	.954 .95	1.015 1.0009	1.015 1.00098	1.0083 .957	.954	1.015	.957
Area	.906	1.016	1.016	.965	....	....	....
Side	..	*U.*	*P.*	..			....
E	6,000,000	5,030,000	5,540,000	6,170,000	.	....	....
σ	.253	.251	.282	.248		....	....
D.	4,040,000	3,360,000	4,250,000	4,110,000	....	....	....
C.	2,395,000	2,015,000	2,155,000	2,470,000	.	....	....
Load (in pounds).	Longitudinal compression (multiply readings by 4 for millionths).				Lateral extension (millionths).		
1,000	0	0	0	0	0	0	0
2,000	70	58	75	60	29	30	40
3,000	135	122	145	125	61	70	80
4,000	200	190	200	180	105	125	119
5,000	250	250	245	230	149	180	155
6,000	310	310	305	280	200	230	195
7,000	360	370	350	325	246	280	235
8,000	415	430	395	375	295	335	275
9,000	460	490	445	420	355	400	320
8,000	430	440	....	385	320	340	295
7,000	385	380	....	340	275	290	265
6,000	330	315	....	295	230	250	230
5,000	280	255	....	250	189	190	200
4,000	220	195	....	200	140	130	160
3,000	160	125	...	140	90	70	110
2,000	90	60	...	80	45	20	50
1,000	10	10	5	2	−5	−6	15

The averages of the results obtained are as follows:

$E = 5,685,000$; $\sigma = 0.2585$; $L = 3,940,000$; $C = 2,258,700$.

This rock, as will be seen, has a low modulus of elasticity, and like other rocks of which this is true, the lateral extension varies considerably in different specimens and the rock does not come readily to a state of ease. This is seen from figure 17, which shows the results obtained in the first three cycles of compression made upon a column of the rock. The hysteresis shown is much greater than in the case of any of the other crystalline rocks examined, and even after repeated stressing this hysteresis, although reduced, does not disappear, as is seen from the curve of the results obtained from column *a* given in figure 18. In this figure I represents longitudinal compression and II lateral extension. The variation in the results obtained for *D* accordingly is high, amounting to 800,000.

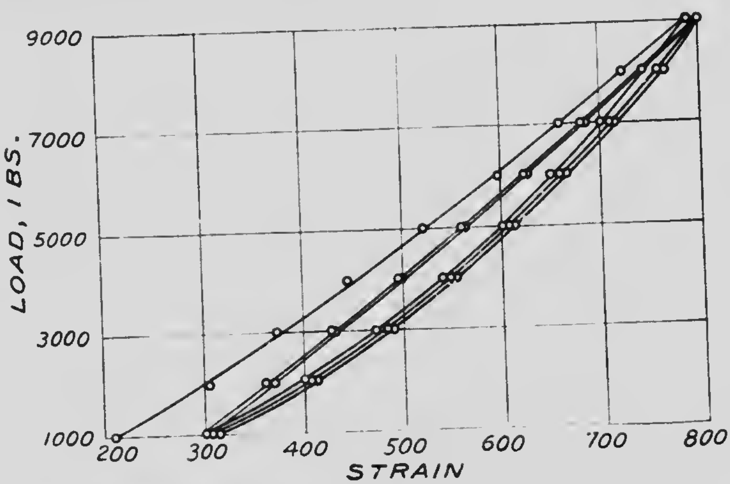
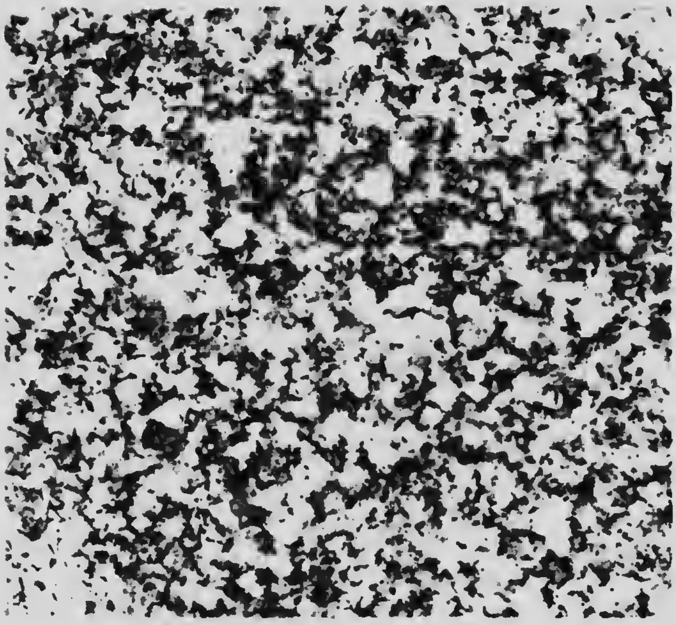


FIG. 17. Stress-strain curves obtained in the first three cycles of compression, from a column of Stanstead Granite, showing its imperfect elasticity.

On account of its defective elasticity the result of the measurement of the compressibility of this rock is less satisfactory than that of the other granites, from which it differs considerably in the value obtained for *D*, although the values obtained in the case of the other granites agree pretty closely among themselves. The cause of this defective elasticity in the Stanstead granite is not clear, although it may be connected with a lack of strength in the rock, which in its turn may be connected with the presence in the rock of so large an amount of mica.

It is a weak rock compared with other granites or with the essexite from Mount Johnson, as shown by the results of a series of tests carried out in the Testing Laboratory of McGill University, and given in the table on page 47.

A color process photograph of a polished surface of the rock is shown in Plate X A, and the photomicrograph of a thin section of it in Plate X B. This



A. PHOTOGRAPH OF POLISHED SURFACE, (NATURAL SIZE)

B. PHOTOMICROGRAPH OF THIN SECTION (× 27 DIAM.—ORDINARY LIGHT)

GRANITE, STANSTEAD, CANADA.

Table showing comparative strength of Stanstead Granite.

Specimen.	Dimensions.	Area.	Weight	Actual load at initial failure	Load per sq. in. at initial failure.	Max. load.	Max. load per sq. inch.
	Inches.	*Sq. In*	*Lbs*	*Lbs*	*Lbs.*	*Lbs*	*Lbs.*
Granite,	A 2.56 by 2.55 by 2.66	6.528	[illegible]5	113,000	17,310	124,300	18,040
St. Philip, Quebec	B 2.47 by 2.46 by 2.52	6.[illegible]		115,000	18,026	142,800	23,500
Essexite,	A 2.47 by 2.68 by 2.54	6.[illegible]		138,000	20,[illegible]40	148,700	22,465
Mt. Johnson, Quebec	B 2.48 by 2.56 by 2.56	6.[illegible]		141,000	22,[illegible]	167,700	26,334
Granite,	A 2.61 by 2.50 by 2.52	6.525	1.565	92,700		92,700	14,206
Stanstead, Quebec	B 2.56 by 2.55 by 2.47	6.528	1.511	88,300		89,300	13,526

latter is taken in ordinary light and magnified 27 diameters The fact that this photomicrograph is taken in ordinary light, while those of other granites just described are taken between crossed nicols, gives this rock an appearance of being coarser in grain than it really is, owing to the boundaries of the colorless constituents being ill defined. The size of the grain may be seen, however, by comparing the dimensions of the iron-magnesia constituents of the rocks or still better by comparing the grain of the several rocks as shown in the photographs of the polished surfaces.

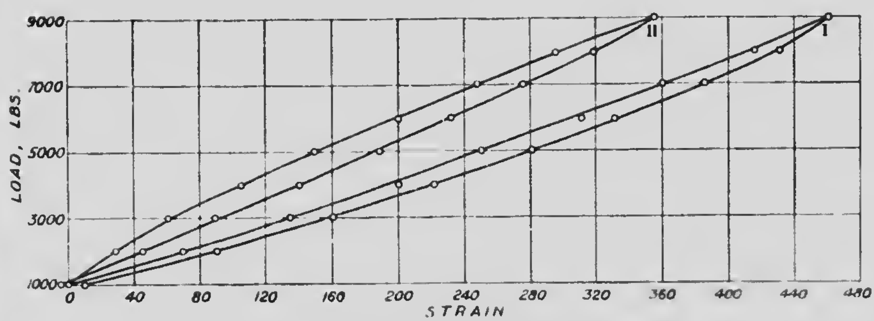


FIG. 18.—Stanstead Granite. Stress-strain curves

NEPHELINE SYENITE.

NEPHELINE SYENITE, CORPORATION QUARRY, MONTREAL, CANADA.

This is a typical nepheline syenite which forms a portion of Mount Royal, one of the Monteregian Hills and which cuts an earlier intrusion of essexite like that to be described later from Mount Johnson

It is a hard and tough rock used as road metal on the streets of the city of Montreal. It is rather light gray in color and often shows locally a more or less distinct parallelism of the constituent minerals, owing to movements during the final stages of the consolidation of the rock, representing in fact a sort of fluidal structure. Traces of this are seen in the specimen from which the colored photograph accompanying this description was taken, but the prism of the rock on which the elastic constants were measured, while otherwise identical with the specimen photographed, showed no traces whatsoever of the fluidal structure in question, but was absolutely massive.

Under the microscope the rock is seen to be composed chiefly of light colored "salic" constituents of which feldspar is by far the most abundant. This is chiefly orthoclase, but this mineral is much intergrown with plagioclase, which is also present in not inconsiderable amount. These feldspars have for the most part a lath shaped development, and it is on account of the more or less parallel arrangement of these laths and of the hornblende crystals that the

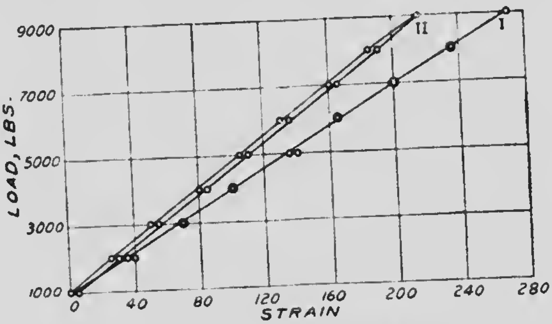
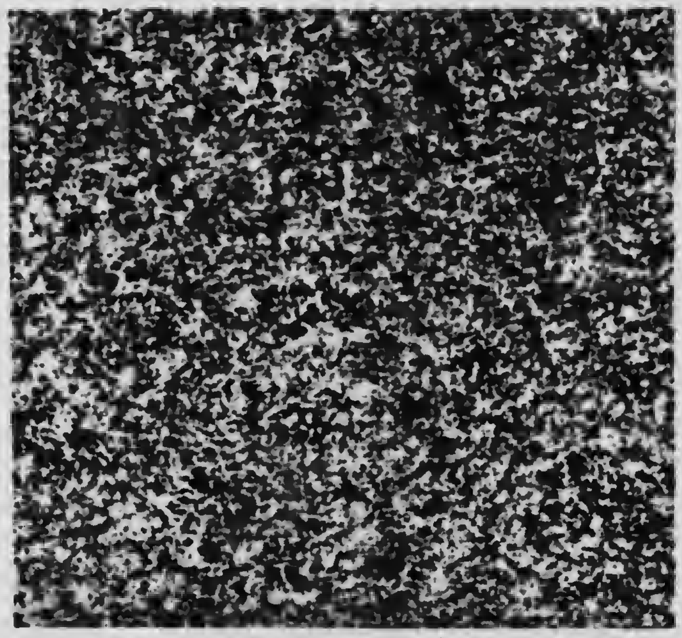


FIG. 19.—Nepheline Syenite. Stress-strain curves.

fluidal structure above mentioned results. Associated with the feldspar is nepheline in rather small amount, and also nosean often in well-defined individuals. These occur in some cases as inclusions in the feldspar. In other cases they lie in the corners between the latter. The dark ("femic") constituents are represented chiefly by a greenish-brown alkali hornblende, with which biotite is associated in much smaller amount. This hornblende has a tendency to an acicular development. There are also present in small amounts, as accessory constituents, sphene magnetite and pyrite.

The rock is fresh, there being no signs of decomposition. Although the nepheline and the nosean are in most cases somewhat altered, the changes which have overtaken them are quite independent of surface decay.

A color-process photograph of a polished surface is seen in Plate XI A, and a photomicrograph taken between crossed nicols and magnified 30 diameters is shown in Plate XI B.



A. PHOTOGRAPH OF POLISHED SURFACE, (NATURAL SIZE)

B. PHOTOMICROGRAPH OF THIN SECTION, (X 30 DIAM.-NICOLS CROSSED)

NEPHELINE SYENITE, MONTREAL, CANADA

Two sets of measurements for the elastic constants were made on a single square prism of the rock, using first one set of faces and then the other The results are set forth in the following table:

Nepheline Syenite Montreal, Canada

No	a	a	a	a
Size	1 × 1.003		1	1.003
Area	1.003	1.003		
E	9,230,000	9,045,000		
σ	.249	.263		
D	6,125,000	6,350,000		
C	3,695,000	3,575,000		

Load (in pounds)	Longitudinal compression (multiply readings by 1 for millionths). Side C.	Side P	Lateral extension (millionths). Side C	Side P.
1,000	0	0	0	0
2,000	35	35	25	25
3,000	70	65	50	51
4,000	100	105	80	80
5,000	135	135	105	110
6,000	165	170	130	145
7,000	200	205	160	175
8,000	235	245	185	200
9,000	270	275	216	230
8,000	234	240	190	200
7,000	200	210	165	180
6,000	165	170	135	155
5,000	140	140	110	125
4,000	100	105	85	95
3,000	70	70	55	65
2,000	35	35	30	35
1,000	5	2	5	5

The stress-strain curves obtained in the first set of measurements are seen in fig. 10 (p. 48), in which I represents longitudinal compression and II shows lateral extension An examination of these will show that the rock exhibits very little hysteresis, the values for longitudinal compression giving a straight line, as in the case of wrought iron and other metals

The averages of the results obtained are as follows:

$E = 9{,}137{,}500$; $\sigma = 0.256$, $D = 6{,}237{,}500$; $C = 3{,}635{,}000$

The differences between the two determinations for the value of D amounted to only 225,000 pounds As will be observed, the value of D for this rock is much higher than that for any of the granites.

BASIC PLUTONIC ROCKS

ANORTHOSITE, NEW GLASGOW, PROVINCE OF QUEBEC, CANADA

This rock is from the great Morin anorthosite intrusion which occupies an area of 990 square miles on the border of the Laurentian protaxis, some 30 miles north of the city of Montreal.* The specimen is from the margin of the intrusion, where the mass has undergone extensive movement of the nature of rockflow, which movement has been brought about by pressure exerted upon the earth's crust in this district. The flow has taken place through a granulation of the larger individuals of the original rock, combined with a movement of this granulated material under the influence of the pressure, giving rise to a rude banding in the rock. This granulation has not, however, been accompanied by any loss of strength, for the rock is a hard and exceedingly tough one, being used as paving sets in some of the streets in the city of Montreal, where there is an especially heavy traffic.

Most of the Morin intrusion consists almost exclusively of plagioclase feldspar, which has the composition of labradorite, with only a very small portion of iron magnesia constituents, and hence the rock is properly termed "anorthosite."

The specimen used for the determination of the elastic constants of the rock was cut from a paving set which was richer than usual in the iron-magnesia constituents and which consequently might be more properly referred to as gabbro, although it is merely a part of the anorthosite locally richer in these darker constituents. It has a rudely streaked structure, as seen in the accompanying color process photograph of a polished specimen (Plate XII A). This structure crossed the vertical face of the test piece diagonally, so that if there be a variation in the values of the elastic constants dependent on the direction of the streaking, the readings attained will represent a mean, or at any rate an intermediate value.

Under the microscope the rock is seen to be composed chiefly of plagioclase, associated with which is a pale green augite, a deep green hornblende, with a few grains of ilmenite, and an occasional individual of hypersthene, now altered to serpentine, and of pyrite.

The plagioclase forms a mosaic of well-twinned grains, through which are distributed the other constituents in little irregular-shaped grains of rounded or subrounded outline. Of these the augite in the most abundant. With the exception of the alteration which has overtaken the few hypersthene grains

*Adams, F. D. Report on the Geology of a Portion of the Laurentian Area lying to the North of the Island of Montreal. Annual Report of the Geological Survey of Canada, Part J, vol. VIII, 1896, p. 111.

A. PHOTOGRAPH OF POLISHED SURFACE, (NATURAL SIZE)

B. PHOTOMICROGRAPH OF THIN SECTION, (X 30 DIAM.-NICOLS CROSSED)

ANORTHOSITE, NEW GLASGOW, CANADA

the rock is absolutely fresh. The structure is allotriomorphic, and there is a tendency to a parallel arrangement among the grains of the darker constituents.

A photomicrograph of a thin section of the rock taken between crossed nicols in polarized light and magnified 30 diameters is shown in Plate XII B.

The elastic constants were determined on a square prism of the rock, and as the rock is very strong, the loading was carried up to 15,000 pounds instead of 9,000 pounds, as in the other rocks.

The figures obtained are set forth as in the following table:

Anorthosite, New Glasgow, Province of Quebec, Canada.

Size	.99 × .99	
Area	.981	
E	11,960,000	
σ	.262	
D	8,368,000	
C	4,750,000	
Load (in pounds).	Longitudinal compression (multiply readings by 4 for millionths).	Lateral extension (millionths).
1,000	0	0
3,000	51	41
5,000	101	81
7,000	157	124
9,000	212	168
11,000	264	214
13,000	318	260
15,000	373	309
13,000	328	266
11,000	278	222
9,000	227	179
7,000	173	135
5,000	116	90
3,000	58	44
1,000	3	0

The averages of the values found are as follows:

$E = 11,960,000$; $\sigma = 0.262$; $D = 8,368,000$; $C = 4,750,000$.

The stress-strain curves of the rock are shown in figure 20, in which I represents longitudinal compression and II lateral extension.

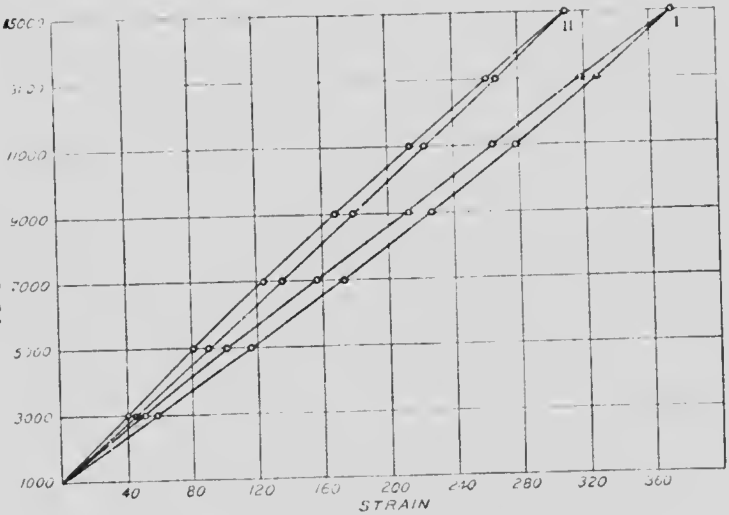


FIG. 20. New Glasgow Anorthosite. Stress-strain curves.

ESSEXITE, MOUNT JOHNSON, PROVINCE OF QUEBEC, CANADA.

This is a rather coarse grained essexite from a quarry on the slope of Mount Johnson, which is a typical butte arising from the Paleozoic plain to the south of the city of Montreal and forming one of the Monteregian Hills.* The rock is massive and uniform in character and dark gray in color, and is extensively used as a building stone and also for monuments.

The iron magnesia constituents are represented by a violet augite, a deep brown hornblende, and a biotite also very deep brown in color, the first mentioned being the most abundant and all three being frequently intimately intergrown. The light colored constituents are plagioclase and nepheline, the former being more abundant than the latter, which often occurs as inclusions in the feldspar. Although polysynthetic twinning is frequently seen in the feldspar, a considerable proportion of it is untwinned. A separation by Thoulet's solution, however, shows that the feldspar is all plagioclase, there being no orthoclase in the rock. Magnetite in the form of small grains and apatite in rather large, well defined crystals are present in considerable amount as accessory constituents. The rock is perfectly fresh. The constituents of the rock, and more especially the feldspar, have a tendency

*Adams, F. D. The Monteregian Hills, a Canadian Petrographical Province. Journal of Geology, April May, 1903.

Essexite, Mount Johnson, Province of Quebec, Canada

No.	a	a	a	b	c
Size	975 · 992	.975 · .992	.975 · .992	.9025 · .9825	971 · 1 007
Alea	.966	.966	966	886	978
E	9,580,000	9,580,000	9,580,000	9,565,000	10,430,000
σ	2663	.2663	2663	2363	2563
D	6,840,000	6,840,000	6,840,000	6,060,000	7,170,000
C	3,781,000	3,781,000	3 781,000	3,860,000	4,160,000

LONGITUDINAL COMPRESSION—MULTIPLY READINGS BY 4 FOR MILLIONTHS.

Load (in pounds).					
1,000	0	−1	−4	0	0
2,000	26	30	30	30	28
3,000	60	68	63	60	50
4,000	95	100	100	100	90
5,000	131	135	133	140	115
6,000	168	169	165	180	150
7,000	200	200	196	215	180
8,000	238	240	236	260	210
9,000	270	270	266	295	245
8,000	236	235	235	260	210
7,000	200	200	200	220	180
6,000	169	170	165	185	150
5,000	135	135	132	140	115
4,000	100	100	100	110	90
3,000	68	65	66	70	50
2,000	30	30	31	25	28
1,000	−1	−4	−5	−5	0

LATERAL EXTENSION—MILLIONTHS.

No.	a	b	c
Size	975	.9825	.971
Load (in pounds).			
1,000	0	0	0
2,000	27	25	
3,000	35	45	
4,000	82	70	
5,000	110	95	
6,000	136	130	
7,000	161	150	. .
8,000	188	180	
9,000	225	220	195
8,000	195	180	.
7,000	172	155	. . .
6,000	146	135	. . . .
5,000	118	100	. . . .
4,000	00	75	. . . .
3,000	49	45	. . . .
2,000	30	20	. . . .
1,000	0	5	3

to assume a more lath-shaped development than in the case of the granites. The laths running as they do in all directions through the rock, probably have a tendency to bind the rock more firmly together than when the feldspar has a more equi-dimensional development, as in the granites. The rock has a hypidiomorphic structure, and, like the granites described in this paper, is perfectly massive

A color process photograph of a polished surface of this rock is shown in Plate XIII A, and a photomicrograph of a thin section taken between crossed nicols in polarized light and magnified 30 diameters is to be seen in Plate XIII B.

Three square prisms of the rock were used, and five determinations of vertical compression with three of lateral extension were made. The results are given in the table on page 53

The averages of the results obtained are as follows:

$E = 9,746,00$; $\sigma = 0.2583$; $D = 6,750,000$; $C = 3,872,600$.

The results obtained for the three measurements on prism *a* were practically identical The figures obtained for the compressibility of *c* are little higher and those for *b* are considerably lower The difference between the highest and the lowest values obtained for *D* amounts to 1,110,000 pounds, but the difference, if the results of the single measurement on *b* be omitted from consideration, amounts to only 330,000 pounds

The stress-strain curves plotted from the measurements obtained from the prism *a* are given in figure 21, and show that the elasticity of the rock is of a very high order In this figure I represents vertical compression and II lateral extension

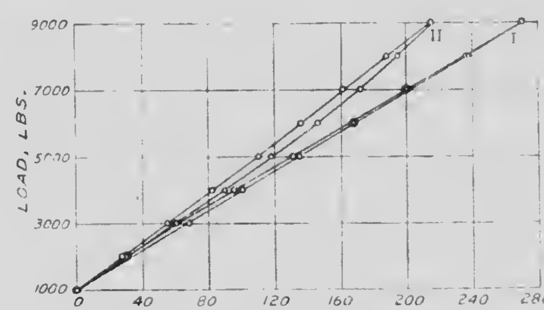
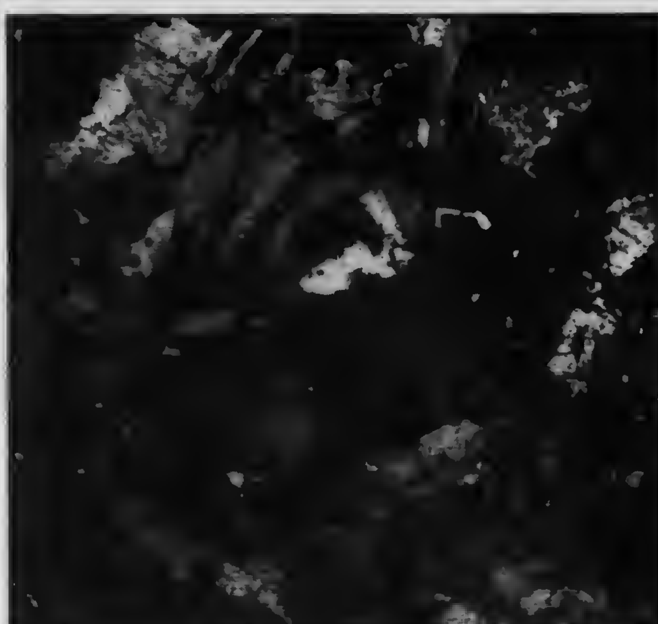


FIG. 21 —Mount Johnson Essexite. Stress-strain curves

A. PHOTOGRAPH OF POLISHED SURFACE, (NATURAL SIZE)



B. PHOTOMICROGRAPH OF [illegible] SECTION, (X 30 [illegible] NICOLS CROSSED)

ESSEXITE, MOUNT JOHNSON, CANADA.

GREEN GABBRO, NEW GLASGOW, PROVINCE OF QUEBEC, CANADA

This rock forms a large dyke* cutting the anorthosite from the locality described above. It is a rock which is darker in color than the anorthosite, owing to a much higher content of iron-magnesia constituents, but which, like that rock, is quarried and used for paving sets.

Under the microscope this rock is seen to differ entirely in structure from the other igneous rocks examined. It is composed of a very pale green augite, a rhombic pyroxene of the same color, and plagioclase, the two former minerals being present in about equal amount, and the plagioclase not forming more than about one-quarter of the rock; there is also present a small amount of a pale green spinel.

The rock is seen to have been crushed in a most extraordinary manner and to present a most striking cataclastic structure. The plagioclase occurs in groups of individuals which are well twinned, and are frequently very much bent and twisted—one individual being bent through an angle of 65°. The mineral is also filled with very minute rounded inclusions, which give to it a green color. These plagioclase grains, quite irregular in form, lie embedded in a mass of little irregular-shaped grains of augite and rhombic pyroxene. These vary somewhat in size. The two pyroxenes are sometimes intimately intermixed and at other times separated into groups of grains of their respective species, which are distinguished from one another by the different values of their double refraction and by the fact that one has parallel and the other inclined extinction. The spinel is associated with this minutely granulated pyroxene.

The original structure of the rock has been entirely broken down, and it now presents an assemblage of grains of the minerals varying in size and differing in arrangement from place to place in the slide. The pyroxenes are granulated, the plagioclase twisted, and the whole presents a perfect cataclastic appearance, differing entirely in this respect from that of the anorthosite just described. This cataclastic structure is combined in some specimens of the rock with a more or less distinct parallel arrangement of the constituent minerals, although this is not very distinct in the specimen shown in the color-process photograph of a polished surface (Plate XIV A).

To this irregularity in structure may be attributed the irregularities in the elastic deportment of the rock.

A photomicrograph of a thin section of the rock taken between crossed nicols in polarized light and magnified 30 diameters is given in Plate XIV B.

It is found that satisfactory measurements of the elastic constants could not be made in the case of this rock, the same specimen giving a great variation

*Adams F. D. Op. cit., p. 121.

in values for Poisson's ratio, when measured in different directions. A similar variation is also obtained with different specimens of the rock. The rock in fact, is not uniform and isotropic, so that, as has been mentioned, it is not one which is suitable for the application of the method employed in this paper, if accurate results are required.

The figures obtained from the measurement of two specimens are given in the following table:

Green Gabbro, New Glasgow, Province of Quebec, Canada.

	b	*c*	*b*	*c*
No.	956 .968	1 · 1 022	968	1
Size	.925	1.022		
Area	12,300,000	19,000,000		
E	1985	24		
σ	6,810,000	12,300,000		
D	5,130,000	7,600,000		
C				

Load (in pounds)	Longitudinal compression (multiply readings by 4 for millionths)		Lateral extension (millionths).	
	0	0	0	0
1,000	25	14	17	11
2,000	50	29	33	21
3,000	75	47	50	32
4,000	105	59	67	40
5,000	135	79	83	61
6,000	160	94		
7,000	190	100		
8,000	220	129		
9,000	190	105		
8,000	165	95	83	61
7,000	140	83	65	45
6,000	110	65	55	35
5,000	85	50	35	25
4,000	60	[illegible]	20	15
3,000	35	15	5	2
2,000	9	0		
1,000				

As will be seen, *D* in one case is 6,810,000 and in the other 12,300,000. In figure 22 the stress-strain curves obtained by plotting the results of the measurement of prism *b* are given, and show a considerable permanent set, but comparatively little hysteresis. In this figure I represents longitudinal compression and II lateral extension. Prism *c* gives an equally good curve. It is quite probable that both are correct for their respective specimens

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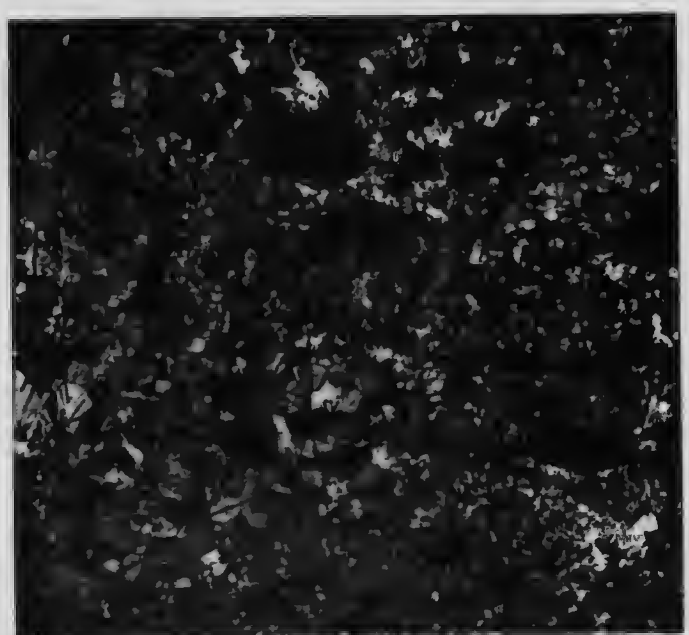
A. PHOTOGRAPH OF POLISHED SURFACE, (NATURAL SIZE)



B. PH... OM... R... APH OF ... N SECTION (× 30 D AM... ... S CROSSED)

... ARP... W GLAS... W, CANADA

In the table giving a summary of results (see page 69), the values given for this rock represent the mean of these highly divergent readings and should be used only in the light of the explanation given above.

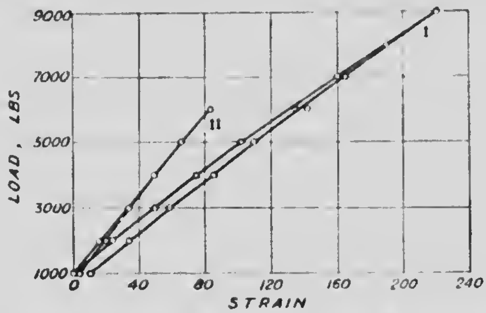


FIG. 22 Green Gabbro, New Glasgow. Stress-strain curves.

OLIVINE DIABASE, NEAR SUDBURY, PROVINCE OF ONTARIO, CANADA.

This is a very typical fresh olivine diabase, which occurs in the form of a large dyke, cutting rocks of Huronian age just northwest of the Murray Mine near Sudbury. It is one of a number of similar diabase dykes, which occur in this district of great nickel-bearing gabbro intrusions. It is rather coarse in grain for a diabase, but nevertheless much finer in grain than any of the granites described in this paper, except that from Westerly, Rhode Island, these two rocks being approximately equal in coarseness of grain, although differing entirely in structure. The rock is composed of violet-brown augite, pale green olivine, colorless plagioclase, and opaque black iron ore. There is also a very small amount of accessory biotite, a few minute acicular crystals of apatite, and an occasional minute grain of pyrite. The augite presents the usual microscopical characters of this species, and is very fresh, scarcely a trace of decomposition being anywhere discernible in it. The olivine, which crystallized before the augite, and therefore often occurs as inclusions in it, while for the most part fresh, is in many places partially altered to a deep green serpentine. It is much less abundant than the augite. The plagioclase occurs in the usual sharp, well-defined, lath-like form, always showing polysynthetic twinning according to the albite law, which in the same individual is often combined with twinning according to the pericline or Carlsbad law. It is fresh and brilliantly polarizing. The iron ore, which is black and opaque, is abundant, occurring in well-defined more or less angular grains.

The rock is perfectly massive and possesses a typical "ophitic" or "diabase" structure, the plagioclase having the form of well-defined laths

penetrating the augite and even the iron ore, but not the olivine so far as can be observed. Many little seams apparently of the nature of joints traverse the rock, and care had to be exercised to secure prisms of the rock free from these, on which to determine the elastic constants.

A color-process photograph of a polished surface of the rock is shown in Plate XV A, and a photomicrograph of a thin section of the rock taken in ordinary light and magnified 27 diameters is seen in Plate XV B.

Four test pieces were used in determining the elastic constants of the rock, viz, three round columns and one nearly square prism. They are designated as *a*, *b*, *c*, and *d*. The three round columns were cut out of a block of the diabase by means of an annular diamond drill. For these we are indebted to Dr. Logan Waller Page, of the Agricultural Department at Washington. Two measurements were made on each of these in planes at right angles to one another, in each case, while four measurements were made on the prism *d*, using two pairs of faces. In this way ten sets of measurements were made for the elastic constants of this diabase.

The values obtained are given in the following tables:

Olivine Diabase, Sudbury, Ontario, Canada.

No.	*d*	*d*	*d*	*d*	*d*	*d*	*d*
Size	1.000 864		....	....	1.00	1.00	1.00
Area	864	.864	864	.864	....	....	....
E	13,150,000	13,330,000	13,450,000	12,860,000	....	....	....
σ	276	.285	287	.279	....	....	....
D	9,810,000	10,340,000	10,500,000	9,655,000	....	....	....
C	5,170,000	5,200,000	5,230,000	5,020,000	....	....	....
	Longitudinal compression (multiply readings by 4 for millionths).				Lateral extension (millionths).		
Load (in pounds).	Side U.	Side U_1	Side U_2	Side U_3	Side U_3	Side U_1	Side U.
1,000	0	0	0	0	0	0	0
2,000	25	25	25	26	25	25	25
3,000	50	51	52	58	50	50	49
4,000	75	76	80	85	75	75	74
5,000	102	103	105	110	100	100	98
6,000	127	130	135	140	124	125	124
7,000	155	155	152	169	148	150	146
8,000	185	187	182	205	173	170	168
9,000	220	217	215	225	200	198	194
8,000	190	190	185	200	175	.	168
7,000	157	157	155	175	152		147
6,000	130	134	134	145	128	.	125
5,000	105	105	105	110	103	. .	99
4,000	79	80	80	80	78	.	75
3,000	50	54	50	51	52	.	50
2,000	25	27	25	25	28	....	25
1,000	0	3	0	0	0	0	0

A. PHOTOGRAPH OF POLISHED SURFACE. (NATURAL SIZE)

B. PHOTOMICROGRAPH OF THIN SECTION. (X 27 DIAM.-ORDINARY LIGHT)

OLIVINE DIABASE, SUDBURY, CANADA.

Olivine Diabase, Sudbury, Province of Ontario, Canada—Continued.

No.	*a*	*a*	*b*	*b*	*c*	*c*
Size	.981	.981	.983	.983	.983	.983
Area	.756	.756	.758	.758	.758	.758
E	13,250,000	13,780,000	14,020,000	14,320,000	14,020,000	14,320,000
σ	2865	281	.291	.277	291	283
D	10,340,000	10,460,000	11,170,000	10,720,000	11,170,000	11,000,000
C	5,160,000	5,380,000	5,430,000	5,620,000	5,430,000	5,580,000

Longitudinal Compression.—Multiply Readings by 4 for Millionths.

Load (in pounds).	Side *U.*	Side *P.*	Side *U.*	Side *P.*	Side *U.*	Side *P.*
1,000	0	0	0	0	0	0
2,000	30	30	30	25	30	30
3,000	60	60	60	55	60	60
4,000	90	90	90	95	90	85
5,000	125	120	115	110	120	115
6,000	155	150	145	140	150	145
7,000	185	180	175	170	180	175
8,000	225	215	210	200	210	205
9,000	250	240	235	230	235	230
8,000	220	210	210	200	210	205
7,000	190	185	170	175	180	175
6,000	165	155	145	140	150	145
5,000	130	125	115	115	120	115
4,000	105	100	85	95	90	85
3,000	75	60	55	55	60	60
2,000	45	25	30	25	30	30
1,000	15	0	0	0	0	0

Lateral Extension.—Millionths.

No.	*a*	*a*	*b*	*b*	*c*	*c*
Size	.981	.981	983	.983	.983	.983
Load (in pounds).	Side *U.*	Side *P.*	Side *U.*	Side *P.*	Side *U.*	Side *P.*
1,000	0	0	0	0	0	0
2,000	28	28	28	25	21	27
3,000	54	51	54	49	49	53
4,000	83	78	82	73	78	79
5,000	111	103	110	100	105	107
6,000	140	130	138	122	131	130
7,000	169	156	164	149	160	154
8,000	198	183	191	172	185	183
9,000	225	210	215	200	215	205
8,000	200	185	192	171	195	180
7,000	172	155	170	150	170	166
6,000	144	135	140	125	145	130
5,000	115	110	118	100	115	110
4,000	85	78	88	75	85	80
3,000	52	54	56	50	55	55
2,000	22	26	30	25	25	26
1,000	0	0	0	0	0	0

As will be seen, the values obtained for *D* in this rock are considerably higher than those yielded by any other rock of the series examined. In the six independent measurements carried out on the first three specimens, the difference between the highest and lowest values for *D* amounted to 830,000 pounds, while on the four measurements made on specimen *d* there is a rather greater difference amounting to [illegible]5,000 pounds.

The averages of the determinations made on each of these columns are as follows:

	E	*D*	*σ*	*C*
a	13,515,000	10,400,000	0.2838	5,270,000
b	14,170,000	10,045,000	0.2840	5,525,000
c	1[illegible] 170,000	11,085,000	0.2870	5,505,000
d	[illegible] 107,750	10,076,000	0.2812	5,155,000
Average	13,763,187	10,626,500	0.2840	5,363,750

The stress-strain curves given by a specimen this rock are shown in figure 23. As will be seen from these curves, in its approach to perfect elasticity the rock is comparable to plate glass.

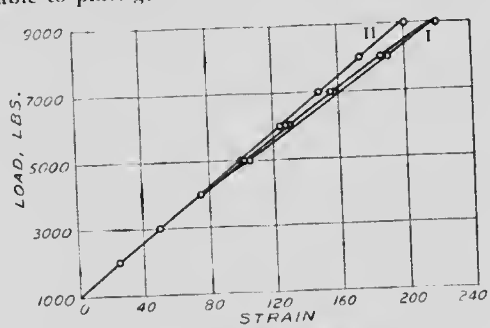
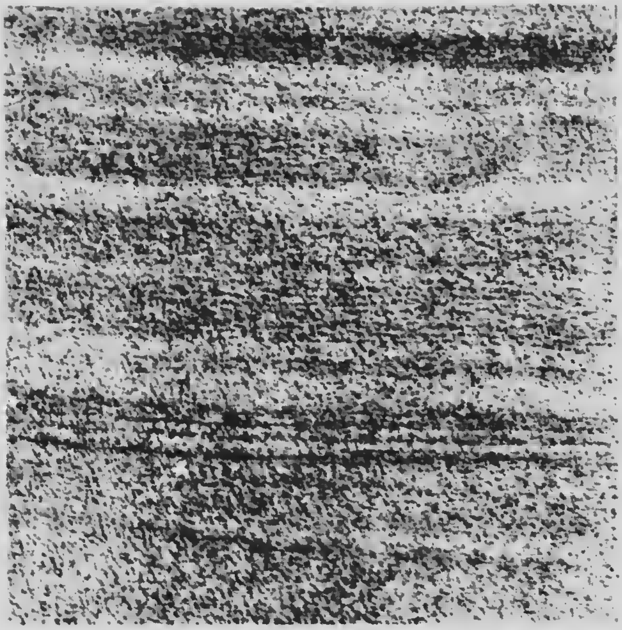


FIG. 23.—Sudbury Diabase. Stress-strain curves.

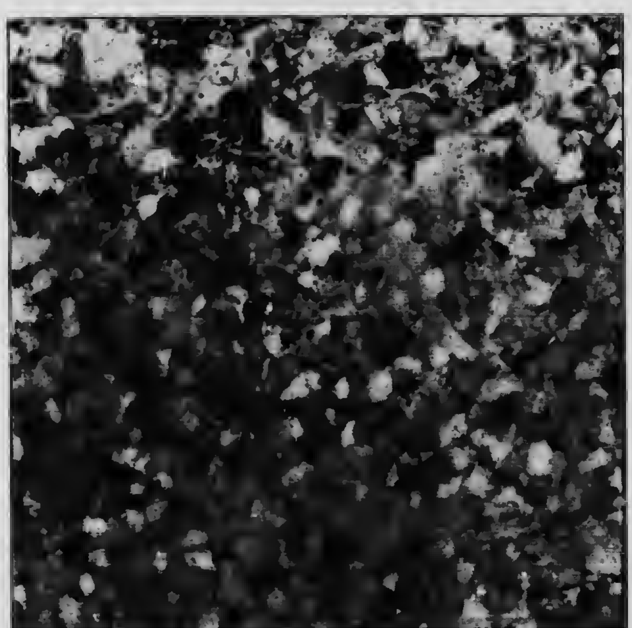
SANDSTONE, CLEVELAND, OHIO, UNITED STATES.

This is a fine and even grained yellowish sandstone used very extensively for building purposes. The bedding is marked by a slight variation in color in different beds. The prism of the rock used in determining its elastic constants was cut from a single bed of uniform character and color, and was taken in the plane of the bedding. A color-process photograph of a smooth surface of the rock is shown in Plate XVI A.

Under the microscope it is seen to be a typical highly feldspathic sandstone. The constituent minerals are present in grains which are approximately



A. PHOTOGRAPH OF FLAT SURFACE, (NATURAL SIZE)



B. PHOTOMICROGRAPH OF THIN SECTION, (X 27 DIAM.—ORDINARY LIGHT)

SANDSTONE, CLEVELAND, OHIO

uniform in size and of rudely rounded or subangular outline. The quartz grains are clear and fresh; the feldspar individuals, which are abundant, on the other hand, are for the most part in an advanced stage of alteration, being always turbid and in most cases quite opaque, from the presence of alteration products. Some few grains of comparatively unaltered plagioclase are, however, present, and scattered through the rock there is a considerable amount of hydrated oxide of iron, which often lies between the grains, forming a cement. The rock, however, also contains a not inconsiderable amount of calcite, which causes it to effervesce slightly when treated with dilute hydrochloric acid, and which is also seen to lie between the clastic grains also forming a cement, often in the form of individuals of a size comparable to those of the other minerals.

The rock, however, is not a crystalline rock, but a typical clastic one. There is not a continuous crystalline web or mosaic, but a mass of rounded or subangular grains which are in part cemented together as above described, but in part are separated by minute open spaces. It is to be expected, therefore, that the rock will show serious defects in elasticity, as proves to be the case when attempt is made to determine its elastic constants. A photomicrograph of the rock taken in ordinary light and multiplied 27 diameters is shown in Plate XVI B.

A square prism of the rock was employed, and it was found to be dangerous to submit it to a load of over 4,000 pounds, the crushing weight of the rock being much lower than that of the other rocks, which are crystalline in texture.

The figures obtained are given in the following table:

Sandstone, Cleveland, Ohio, United States.

Size	1.000 × 1.025	1.000
Area	1.025	..
E	2,290,000	
σ	.29	
D	1,816,000	
C	888,000	
Load (in pounds).	Longitudinal compression (multiply readings by 4 for millionths).	Lateral extension (millionths).
1,000	0	0
2,000	152	110
3,000	288	241
4,000	426	306
3,000	309	305
2,000	175	178
1,000	?	0

The stress-strain curves are shown in figure 24.

As will be seen, the rock displays a marked hysteresis and is not therefore an ideal material for the application of this method of determining compressibility.

The results obtained are as follows:

$$E = 2,290,000; \quad \sigma = 0.29; \quad D = 1,816,000; \quad C = 888,000.$$

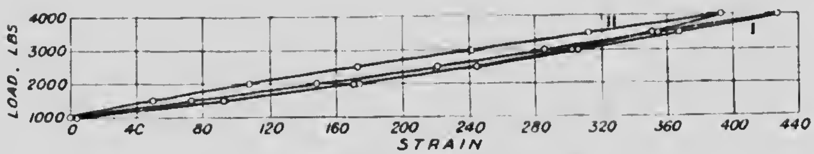


Fig. 24.—Sandstone. Stress-strain curves.

THE ELASTIC CONSTANTS OF GLASS.

As in geophysical speculations, the earth in respect to its rigidity and compressibility is often compared to a globe of glass, it seemed advisable to determine as accurately as possible the elastic constants of glass, for the purpose of comparing them with the results obtained in the case of the various rocks considered in this paper, employing the same methods and carrying out the work under exactly the same conditions. This material lends itself excellently to this method of measuring these constants, provided the glass is free from all irregularities in its substance and is isotropic in character. The first difficulty experienced was that of obtaining such a glass. At the outset it was thought that thick glass rods such as are used for various purposes in the chemical and physical laboratory might be employed, but although several lots of the purest variety of this material were procured, the glass constituting it was found in all cases to contain minute air bubbles, and when examined between crossed nicols in polarized light, showed brilliant colors—red, yellow, and blue. This indicated a state of marked tension in the glass, evidently due to the rod having been drawn when the glass was in a viscous state, which was also shown by the circular arrangement of the little bubbles in the rod, following the direction of its surface. Short lengths of this rod, moreover, when tested in compression, so soon as the maximum load had been exceeded, instead of splitting from top to bottom, broke as if composed of a series of rudely concentric shells. All attempts on the part of the various glass makers to whom this glass was submitted for a thorough annealing, failed to remove or in fact to reduce to any considerable extent this anisotropic condition.

The figures obtained from one of these glass rods approximately an inch in diameter are given in the following table:

Glass Rod.

Size	985	.97
Area	774	
E	8,075,000	
σ	2	. . .
D	4,485,000	. .
C	3,361,000	. . . .
Load (in pounds).	Longitudinal compression (multiply readings by 4 for millionths).	Lateral extension (millionths).
1,000	0	0
2,000	55	32
3,000	95	61
4,000	145	95
5,000	200	123
6,000	250	155
7,000	300	. .
8,000	350	. . .
9,000		. . . .
8,000	350	. . . .
7,000	305	.
6,000	250	155
5,000	205	125
4,000	160	100
3,000	115	65
2,000	65	35
1,000	5	2

That the tension in this glass seriously affected the results obtained—as might be expected—is clearly seen in the value for *D* being much too low, as will be shown later.

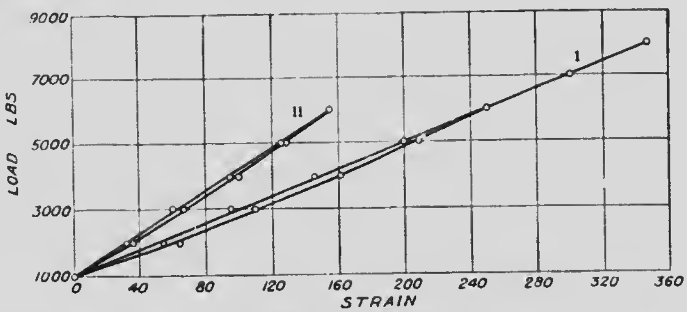


FIG. 25. Glass Rod. Stress-strain curves.

The stress-strain curves plotted from these values are shown in figure 25. As will be seen, the material exhibits a distinct hysteresis.

After a prolonged search for isotropic glass in masses of sufficient size to measure the elastic constants, it was found that plate glass answered the requirements. A piece of one inch plate glass made in Great Britain was accordingly secured and was cut into strips an inch wide, and these again into three inch lengths. The square prisms thus produced were then properly faced and polished. The glass was found to be absolutely free from all flaws and impurities and when examined between crossed nicols the prisms, although an inch thick, showed in one direction at right angles to vertical axis absolute blackness throughout a complete revolution, while in the other direction at right angles to this there was during a revolution an alternation of blackness with a pale grayish illumination. This change was so slight that, considering the thickness of the glass and the sensitiveness of the test, the material may

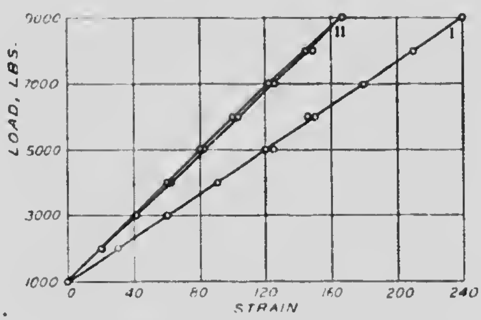


FIG. 26.—Plate Glass. Stress-strain curves.

be considered to be practically free from internal tension and to be isotropic in character.

In order to get a good average and to eliminate chance errors as far as possible, seven of these prisms were taken, and two complete sets of determinations were made on each of them, using in every case different pairs of faces. Fourteen determinations were thus made of each of the elastic constants. The figures obtained are set forth in the table on page 65.

In this table a complete series of values obtained from each specimen are given in double rows. When the average of all these results is taken, the values obtained for the several constants of plate glass are as follows:

$$E = 10,500,000; \quad \sigma = 0.2273; \quad D = 6,448,000; \quad C = 4,290,000.$$

The stress-strain curves given by one of the prisms is shown in figure 26. In this figure I represents longitudinal compression and II lateral extension.

Plate Glass.

No.	*a*	*b*	*c*	*d*	*e*	*f*	*g*
Size	9855 × 1.0[illegible]	9865 × 1.0055	981 × 1.0135	1.016 × 1.008	1.021 × .9955	1.02[illegible] × 1.0025	1.025 × .994
Area	1.0057	.992	.991	1.024	1.017	1.021	1.016
E	10,350,000 10,590,000	10,950,000 10,500,000	10,480,000 10,350,000	10,390,000 10,380,000	10,[illegible]50,000 10,940,000	10,180,000 10,600,000	10,150,000 10,230,000
σ	.2281 .228	.236 .2311	.226 .235	.233 .227	[illegible]	.229 .225	.216 .215
D	6,370,000 6,480,000	6,930,000 6,580,000	6,460,000 6,520,000	6,180,000 6,350,000	[illegible]0,000 6[illegible]00	6,370,000 6,440,000	6,140,000 6,020,000
C	4,220,000 4,410,000	4,140,000 4,250,000	4,280,000 4,190,000	4,210,000 4,230,000	[illegible]30,000 [illegible]140,000	4,220,000 4,310,000	4,300,000 4,360,000

Longitudional Compression—Multiply Readings by 4 for Millionths.

Load (in pounds)	Side U	Side P	Side U	Side P	Side U	Side P	Side U	Side P	Side U	Side P	Side U	Side P	Side U	Side P
1,000	0	0	0	0	0	0	0	0	0	0	0	0	0	0
2,000	30	30	25	30	30	30	30	30	30	30	28	25	30	30
3,000	60	55	55	60	60	60	60	60	60	55	55	55	60	60
4,000	90	85	85	90	90	90	90	90	90	85	85	85	85	90
5,000	120	115	115	120	120	120	120	115	115	110	[illegible]	110	115	125
6,000	145	145	145	145	150	150	150	145	145	135	145	140	145	145
7,000	175	175	175	175	180	180	180	175	175	170	175	170	180	175
8,000	210	205	205	210	210	210	205	205	205	195	200	195	205	210
9,000	240	235	230	240	240	243	235	235	235	225	235	230	235	240
8,000	210	205	205	210	210	210	205	205	205	195	205	105	205	210
7,000	180	180	175	180	180	180	180	175	175	170	175	170	175	180
6,000	150	145	145	150	150	155	150	145	145	135	145	140	145	150
5,000	120	115	115	120	120	120	120	115	115	110	115	115	115	120
4,000	90	85	85	90	90	90	90	90	85	85	85	85	85	90
3,000	60	55	55	60	60	60	60	55	55	60	60	60	60	60
2,000	30	30	25	30	30	30	30	30	30	30	30	30	30	30
1,000	0	0	0	0	0	0	0	0	0	0	0	0	0	0

Lateral Extension—Millionths.

1,000	0	0	0	0	0	0	0	0	0	0	0	0	0	0
2,000	22	22	21	22	19	22	20	19	[illegible]	19	20	19	21	20
3,000	44	45	42	45	38	46	[illegible]	39	[illegible]	40	41	39	42	42
4,000	68	68	66	68	60	69	63	60	[illegible]	59	65	60	60	62
5,000	89	89	88	89	81	92	[illegible]	81	[illegible]	80	89	79	80	83
6,000	111	111	109	111	103	115	[illegible]	105	[illegible]	100	109	100	100	103
7,000	132	133	129	133	124	138	[illegible]	126	124	122	130	122	122	122
8,000	153	156	151	156	149	160	157	148	145	143	155	145	144	144
9,000	173	175	172	179	170	180	178	169	169	165	176	165	167	165
8,000	155	155	152	157	149	163	159	149	149	145	155	147	149	147
7,000	135	133	130	135	125	140	135	129	126	125	130	125	125	125
6,000	115	112	110	115	103	115	100	106	105	105	112	105	103	106
5,000	93	90	90	90	80	90	89	85	88	88	90	85	82	89
4,000	70	71	70	70	60	65	64	62	62	62	69	65	62	69
3,000	49	45	45	50	40	42	40	42	41	41	45	43	42	49
2,000	22	23	22	25	21	20	20	21	21	21	22	22	22	28
1,000	0	0	0	0	0	0	0	0	0	0	0	0	0	0

Determinations of the cubic compressibility of glass, D, have been made by other observers using various methods. The results go to show that different varieties of glass vary considerably in their compressibility. These determinations may be tabulated as follows:*

Everett	..	5,074,600 to 6,379,400 (C. G. S = 3.5 to 4.4 × 10^{11}).
Amagat—Common glass	.	6,745,000 (.000002181 per atmosphere).
Amagat—Crystal glass		6,112,300 (.000002405 per atmosphere).
Tait	. ..	5,657,700 (.0000026 per atmosphere).

As will be seen, the figures obtained for plate glass in the present investigation lie a little above the average of the various values here given, and are nearly those of the highest value obtained by Everett.

SUMMARY OF RESULTS.

The table on page 69 gives a summary of the average values obtained for E, σ, C and D in the case of all rocks examined in this investigation. With these are placed, for purposes of comparison, the results obtained for these constants in the case of wrought iron, cast iron and glass. In the second table on page 69 these values are again presented, recalculated into C. G. S. units.

The rocks fall naturally into three groups, differing from one another in compressibility, but the several members of each group agreeing fairly closely among themselves.

These three groups show a corresponding difference in composition.

The first group consists of the marbles and limestones. These have an average value for D of 6,345,000. One of these, however, the Black Belgian marble which is very much finer in grain than the others and breaks almost like a piece of glass, has a very much higher value for D than that possessed by the other rocks which among themselves are nearly identical. If we omit this Belgian marble, the average of D for the other limestones and marbles, is 5,855,000.

The second group comprises the granites. These again show a close agreement of values among themselves, except in the case of the Stanstead granite, which rock, as already mentioned, shows a defective elasticity. The average value of D for the granites is 4,309,000.

The third group embraces the basic intrusives (gabbro, anorthosite, essexite, and diabase). These show greater differences, but have an average value for D of 8,825,000. The nepheline syenite, although higher in silica and therefore properly speaking an acid rock: in its freedom from quartz, and its richness in feldspar (although the feldspar is largely orthoclase instead of plagioclase), in mineralogical composition belongs with these basic rocks rather than with the granites. It also approaches the essexite most nearly in its compressibility.

*See Everett, Illustrations of the C. G. S. System of Units with tables of Physical Constants. MacMillan & Co., 1902, pp. 60 to 64. The figures there expressed in various units have been here recalculated into inch-pound values.

If the nepheline syenite be included with the basic rocks, an average value of *D* is obtained of 8,308,000.

This omits from consideration the sandstone, it being a rock of an entirely different class from the others, and furthermore one which shows so much hysteresis that the application of this method to it is less satisfactory than in the case of the other rocks of the series.

These results may be presented as follows:

	Average of *D*.
Marbles and limestone	6,345,000
Granites	4,399,000
Basic intrusives	8,308,000

The cause of the much greater compressibility of granite as compared with the marbles and basic intrusives is not clear, but would seem to be connected with the presence of quartz. The only determination of the cubic compressibility of quartz, so far as can be ascertained, is one by Voigt,* the value obtained being 5,504,190 pounds (387×10^6 grams per sq. cm.). This compressibility, as will be seen, is much greater than that found in the case of either the limestones or the basic intrusives, and while not in itself sufficiently great to account for the high compressibility of the granites, goes to show that in the quartz we have a mineral which is more compressible than the ordinary rock making minerals which form the chief constituents in the rocks of the series examined.

The marbles and the limestones of the earth's crust are confined to its most superficial portion, resulting as they do from the process of sedimentation. There is every reason to believe, however, that what we may term the substructure of the earth's crust is composed of acid and basic plutonic igneous rocks. These make up the lowest part of the crust to which we have access and are found coming up from the still greater depths.

The cubic compressibility *D* of the earth's crust must lie between the values given above for the granites and the basic intrusives, approaching one or other of these values according to the relative proportion in it of one or other of these classes of rocks.

If we take the average of the values obtained from these two classes of rocks as represented by the seven granites and the five basic intrusives (including the nepheline syenite) the values obtained for *D* of 6,353,500.

This, as will be seen, differs but little from the value of *D* obtained for plate glass which is 6,448,000.

If, therefore, the earth's crust be composed of granite and basic igneous rocks in approximately equal proportions, its compressibility will be that of glass. If it be composed almost exclusively of granite, the earth's crust will be more

*Quoted in Becker: Experiments on Schistosity and Slaty Cleavage, Bulletin 241, U. S. Geol. Survey, p. 32.

compressible than glass, and if the basic rocks preponderate very largely it will be less compressible than this substance.

It is, however, in any case much more compressible than steel, which has a value for D of from 26,098,000 to 27,547,000 (18 to 19 $\times$ 10^{11}, C. G. S.).*

The compression to which the rocks were subjected in this investigation ranged from 6,000 to 17,340 pounds to the square inch. Most of the rocks, however, were subjected to a load of from 9,000 to 15,000 pounds per square inch, and their bulk compression was determined for these loads as maxima. Higher pressures could not be employed without running the risk of breaking the specimen and at the same time of destroying the measuring apparatus. One apparatus was in fact so destroyed.

The question arises as to whether under still higher pressures, if rupture could be avoided, the ratio of load to compression would be maintained. Judging from the deportment of much stronger substances such as steel, when similarly tested, it is inferred that this ratio of bulk compression will remain constant for very much higher pressures, or until deformation sets in and the rock begins to flow.

With regard to the accuracy of the results obtained by this method as compared with those obtainable by any method in which cubic compression is actually produced and measured, it may be observed that by far the best method of this kind hitherto suggested seems to be that proposed by Richards and Stull.† We have endeavored to make use of this method in order to obtain results for purposes of comparison with those given in the present paper but have not hitherto succeeded in overcoming certain experimental difficulties. The experimental errors in this method, though apparently small, still exist, and in applying it to rocks, which are much less compressible than the substances examined by Richards and Stull, these errors become proportionately more serious. Moreover, higher pressures than those used in the method employed in the present paper could scarcely be employed in this direct method, while difficulties dependent on the possible lack of absolute continuity in the substance of the rock and the danger of minute air-filled spaces would probably present themselves in the case of most rocks. It seems that, all things being considered, the indirect method here employed is probably as accurate as any direct method which can be used. The attempt to apply Richards and Stull's method to rocks is still being continued, however, and it is hoped that satisfactory results may be eventually obtained by its use.

*Illustrations of the C. G. S. System of Units, with Tables of Physical Constants. MacMillan & Co., 1902, p. 60.

†New Method of Determining Compressibility. Published by the Carnegie Institution of Washington, December, 1903.

Elastic Constants of Rocks.

SUMMARY OF RESULTS (AVERAGE) EXPRESSED IN INCH-POUND UNITS.

Specimen.	E	σ	C	$D=\frac{1}{3}\left(\frac{m}{m-2}\right)E$
Wrought iron	28,100,000	0.2800	11,000,000	21,300,000
Cast iron	15,000,000	0.2500	6,000,000	10,000,000
Black Belgian marble	11,070,000	0.2780	4,330,000	8,303,000
Carrara marble	8,046,000	0.2744	3,154,000	5,946,000
Vermont marble	7,592,000	0.2630	3,000,000	5,341,000
Tennessee marble	9,006,000	0.2513	3,607,000	5,967,000
Montreal limestone	9,205,000	0.2522	3,636,000	6,167,500
Baveno granite	6,833,000	0.2528	2,724,800	4,604,000
Peterhead granite	8,295,000	0.2112	3,399,000	4,792,000
Lily Lake granite	8,165,000	0.1982	3,380,000	4,517,500
Westerly granite	7,394,500	0.2195	3,019,700	4,397,500
Quincy granite (1)	6,747,000	0.2152	2,781,600	3,984,000
Quincy granite (2)	8,247,500	0.1977	3,445,000	4,555,000
Stanstead granite	5,685,000	0.2585	2,258,700	3,940,000
Nepheline syenite	9,137,500	0.2560	3,635,000	6,237,500
New Glasgow anorthosite	11,960,000	0.2620	4,750,000	8,368,000
Mount Johnson essexite	9,746,000	0.2583	3,872,600	6,750,000
New Glasgow gabbro*	15,650,000	0.2192	6,365,000	9,555,000
Sudbury diabase	13,763,000	0.2840	5,364,000	10,626,500
Ohio sandstone	2,290,000	0.2900	888,000	1,816,000
Plate glass	10,500,000	0.2273	4,290,000	6,448,000

SUMMARY OF RESULTS (AVERAGE) EXPRESSED IN C. G. S. UNITS.

Specimen.	E	σ	C	D
Wrought iron	19.37×10^{11}	0.2800	7.590×10^{11}	14.680×10^{11}
Cast iron	10.34×10^{11}	0.2500	4.132×10^{11}	6.897×10^{11}
Black Belgian marble	7.24×10^{11}	0.2780	2.982×10^{11}	5.736×10^{11}
Carrara marble	5.54×10^{11}	0.2744	2.171×10^{11}	4.090×10^{11}
Vermont marble	5.24×10^{11}	0.2630	2.069×10^{11}	3.680×10^{11}
Tennessee marble	6.21×10^{11}	0.2513	2.482×10^{11}	4.115×10^{11}
Montreal limestone	6.35×10^{11}	0.2522	2.504×10^{11}	4.250×10^{11}
Baveno granite	4.71×10^{11}	0.2528	1.875×10^{11}	3.179×10^{11}
Peterhead granite	5.71×10^{11}	0.2112	2.340×10^{11}	3.300×10^{11}
Lily Lake granite	5.63×10^{11}	0.1982	2.330×10^{11}	3.103×10^{11}
Westerly granite	5.09×10^{11}	0.2195	2.080×10^{11}	3.029×10^{11}
Quincy granite (1)	4.64×10^{11}	0.2152	1.916×10^{11}	2.750×10^{11}
Quincy granite (2)	5.68×10^{11}	0.1977	2.373×10^{11}	3.140×10^{11}
Stanstead granite	3.92×10^{11}	0.2585	1.556×10^{11}	2.718×10^{11}
Nepheline syenite	6.29×10^{11}	0.2560	2.505×10^{11}	4.290×10^{11}
New Glasgow anorthosite	8.25×10^{11}	0.2620	3.275×10^{11}	5.760×10^{11}
Mount Johnson essexite	6.71×10^{11}	0.2583	2.670×10^{11}	4.650×10^{11}
New Glasgow gabbro*	10.80×10^{11}	0.2192	4.380×10^{11}	6.589×10^{11}
Sudbury diabase	9.49×10^{11}	0.2840	3.700×10^{11}	7.329×10^{11}
Ohio sandstone	1.58×10^{11}	0.2900	$.612 \times 10^{11}$	1.250×10^{11}
Plate glass	7.24×10^{11}	0.2273	2.960×10^{11}	4.439×10^{11}

*See page 57