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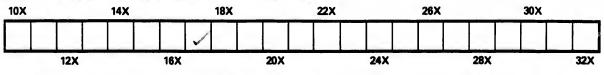
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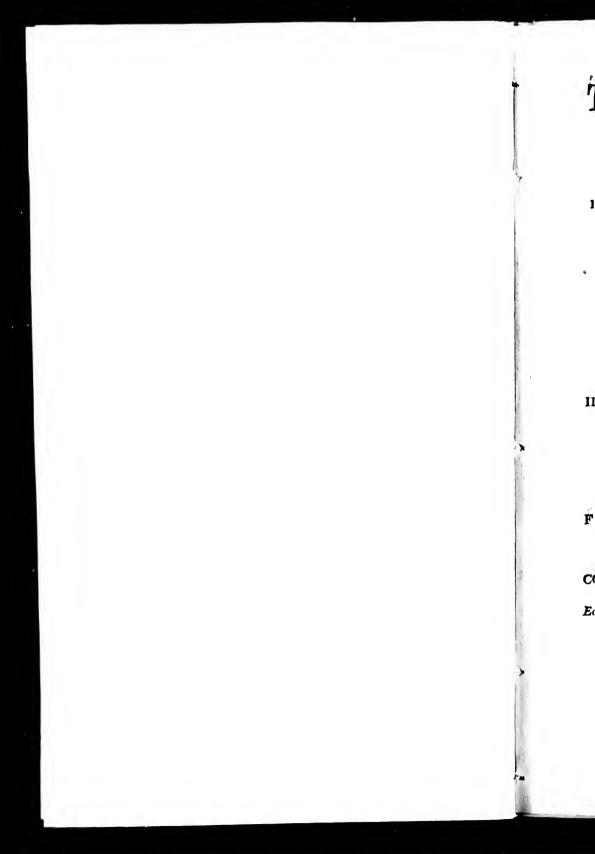
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THE

TUTOR'S ASSISTANT; BEING A COMPENDIUM OF PRACTICAL ARITHMETIC,

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Editor of the Improved Edition of Jones' Dictionary; Author of the Rational English Expositor, Sc.

> MONTREAL, R. & A. MILLER, No. 10, ST. FRANCOIS-XAVIER STREET 1952.

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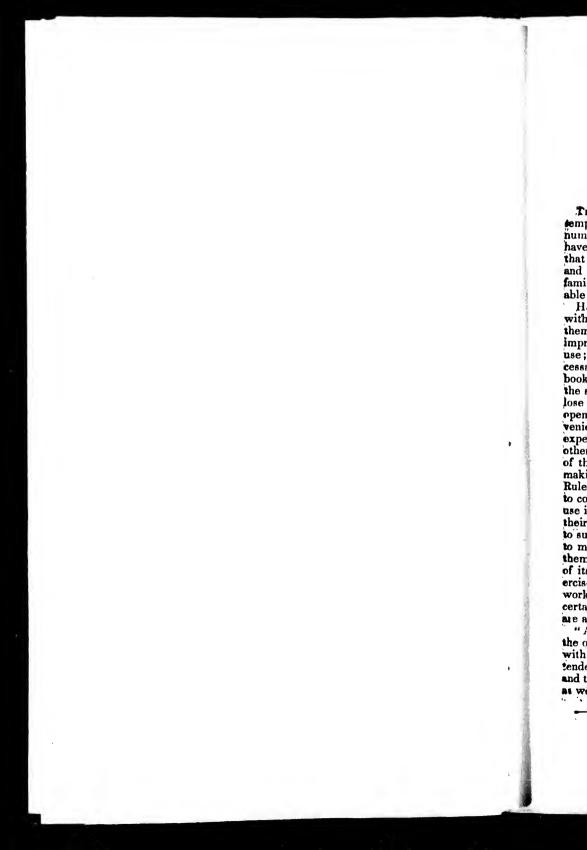
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THE AUTHOR'S PREFACE.

The public will, no doubt, be surprised to find there is the sempt made to publish a book of ARITHMETIC, when there is the same subject, and several of the same subject, and several of the same so lately made their appearance in the world; but I flatter myself that the following reasons, which induced me to compile it, the method and the conciseness of the Rules, which are laid down in so plain and familiar a manner, will have some weight towards its having a favour able reception.

Having some time ago drawn up a set of Rules and proper Questions, with their Answers annexed, for the use of my own school, and divided them into several books, as well for more ease to myself as the readier improvement of my scholars, I found them, by experience, of infinite use; for when a master takes upon him that laborious (though unnecessary) method of writing out the Rules and Questions in the children's books, he must either be toiling and slaving himself. after the fatigue of the school is over, to get ready the books for the next day, or else must lose that time which would be much better spent in instructing and opening the minds of his pupils. There was, however, still an inconvenience which prevented them from giving me the satisfaction I at first expected; that is, where there are several boys in a class. some one or other must wait till the boy who first has the book finishes the writing of those rules or questions he wants, which detains the others from making that progress they otherwise might, had they a proper book of Rules and Examples for each boy; to remedy which I was prompted to compile one, in order to have it printed, which might not only be of use in my own school, but in other school, where the instructers wish their scholars to make a quick progress. It will also be of great use to such persons as have acquired some knowledge of numbers at school, to make them the more perfect; likewise, to such as have completed themselves therein, it will prove, after an impartia perusai, on account of its great variety and brevity, a most agreeable and entertaining Exercise Book. I shall not presume to say anything more in favour of this work, but beg leave to refer the unprejudiced reader to the remark of a certain Author,* concerning compositions of this nature. His words are as follow :-

"And now, after all, it is possible that some, who like best to tread the old beaten path, and to toil at their business when they may do it with pleasure, may start an objection against the use of this well-intended Assistant because the course of Arithmetic s always the same; and therefore say that some boys, lazily inclined, when they see another as work upon the same question, will be apt to make his operation pass for their own. But these little forgeries are soon detected by the difference of the Tutor; therefore, as different questions to different boys do not in the least promote their improvement, so neither do the same questions impede it. Neither is it in the power of any master, (in the course of his business,) how full of spirits soever he may be, to frame new examples at pleasure in any Rule; but the same question will frequently occur in the same Rule, notwithstanding his greatest care and skill to the contrary.

" "It may also be farther objected, that to teach by a printed book is an argument of ignorance and incapacity, which is no less trifling than the former. He, indeed, (if such a one there be.) who is afraid his ischolars will improve too fast, will undoubtedly decry this method, but that master's ignorance can never be brought in question who can begin and end it readily; and, most certainly, that scholar's non-improvement can be as little questioned who makes a much greater progress by this than by the common method."

To enter into a long detail of every Rule would tire the reader, and swell the preface to an unusual length; I shall, therefore, only give a general idea of the method of proceeding, and leave the rest to speak for itself, which, I hope, the reader will find to answer the title, and the recommendation given it. As to the Rules, they follow in the same manner as the table of contents specifics, and in much the same order as they are generally taught in schools. I have gone through the four fundamental Rules in Integers first, before those of several denominations, in order that, they being well understood, the latter will be performed with much more ease and despatch, according to the rules shown, than by the customary method of dotting. In Multiplication I have shown both the beauty and use of that excellent Rule in resolving most Questions that occur in merchandising, and have prefixed to Reduction several Bills of Parcels, which are applicable to real business. In working Interest by Decimals 1 have added tables to the Rules, for the more ready calculating of Amnities, &c., and have not only shown the use, but the method of making them; likewise a Table calculated for finding the Interest of Money for any number of days, at any rate per cent., by Multiplication and Addition only, which may also be applied to the calculation of Incomes, Salaries, or Wages, for any number of days; and I may venture to say, I have gone through the whole with so much plainness and perspicuity, that there is none better extant.

I have nothing farther to add but a return of my sincere thanks to all those gentlemen, schoolmasters, and others, whose kind approbation and encouragement have now established the use of this book in almost every school of eminence throughout the kingdom, but I think my gratitude more especially due to those who have favoured me with their remarks; though I must still beg of every candid and judicious reader, that if he should, by chance, find a transposition of a letter, or a false figure, to excuse it; for, notwithstanding there has been great eare taken in correcting, yet errors of the press will inevitably creep in, and some may also have slipped my observation; in either of which cases the ad monition of a good-natured reader will be very acceptable to his

Much obliged and most obedient humble servant,

F. WALKINGAME

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CONTENTS.

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Page	Faga
NUMERATION and notation	Addition
INTEGERS.	Subtraction96
Simple Addition12	Multiplication
Subtraction	
Multiplication 16	Circulating Decimals
Division	netherion
Arithmetical and Commercial	
Tubles	L'adamaro IAT
Definitions	Conjoined Proportion 119
Reduction	Involution 110
Compound Addition	Production 110
Subtraction	Biquadrate Root
Multiplication	Roots of all Powers
Division	Single Position 190
Promiscuous Examples45 Rule of Three Direct49	
Inverse	Trogression Arithmetical
Double Rule of Three	Geometricat
Practice	sumple interest and Annumes150
Tare and Tret	spieloune
Invoices, &c	programon of a dymemis
Simple Interest, Commission, Bro-	compound interest and Annu-
kerage, Purchasing Stock, &c. 66	ties
Discount	DEODEGINATE 157
Compound Interest	
Equation of Payments	SUPERFICIAL MENSURATION.
Barter	Geometrical Definitions152
Profit and Loss	Mensuration of a Parallelogram,
Fellowship	&c
Alligation	Triangle165
Comparison of Weights and Measures	Trapezium. a. 109
Permutation	Figure an Irregular 166
	a Regular Poly.
VULGAR FRACTIONS.	166
Definitions, &c	Circle
Reduction	——. Area of
Addition	
SHOU'SCHON	
	Sector
Division	Segments
Double Rule of Three	Ellipse
Mouple Rule of Three	Collection of Questions
DECIMAL FRACTIONS.	Supplemental Questions
Definitions &c	Book-Keeping 131

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EXPLANATION OF

ARITIMETICAL SIGNS OR CHARACTERS.

× — into, and denotes MULTIPLICATION.

 \div — by, and denotes Division.

= is the sign of EQUALITY.

: :: are the signs of PROPORTION.

 \checkmark is the Radical Sign, or sign of Evolution.

o denotes the difference between two quantities when it is uncertain which is the greater.

ILLUSTRATIONS.

6+3=9 signifies 6 plus 3 equal 9: that is, 6 added to 3 equal 9.

- 7-4-3 signifies 7 minus 4 equal 3: that is, 4 taken from 7 leaves 3.
- $4 \times 3 = 12$ is read 4 into 3 equal 12: that is, 4 multiplied by 3 equal 12.
- 12÷4=3 is read 12 by 4 equal 3. But Division is more conveniently expressed in the form of a Fraction: thus,
 1² = 3; twelve divided by four equal three.

As 2:4::8:16; As 2 are to 4, so are 8 to 16.

 $\sqrt{16}=4$; the Square Root of 16 equal 4.

 $\sqrt{64-4}$; the Cube Root of 64 equal 4.

A vinculum connects two or more terms which are to be considered as forming one term or quantity. It is signified by a line drawn over them; or by parentheses including them.

A point is often used instead of the cross to denote Multiplication; and in Algebraical Theorems, &c., the multiplication of the quantities denoted by different letters is understood by placing the letters together without any sign between them. Thus 2.5+7, denotes that 5 and 7 are to be added, and the sum (12) to be multiplied by 2. Also, (ab+c). (n-1)denotes that a and b are to be multiplied, c added to the product, and the whole to be multiplied by one less than the number or quantity represented by n.

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Folio,	of which	2 leaves make a sheet,	ffo.
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ARIT cal c units Nu figure signi and t po va

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THE

TUTOR'S ASSISTANT,

BEING A COMPENDIUM OF

PRACTICAL ARITHMETIC.

Integers, or Whole Numbers.

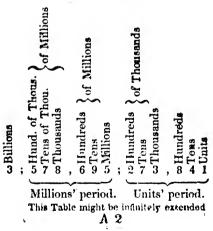
ARITHMETIC is the science of numbers; or the art of numerical computation. A whole number is a unit, or a collection of units.

Numbers are expressed by ten written characters called figures, or digits : viz. 1, 2, 3, 4, 5, 6, 7, 8, 9, which are significant figures, all declaring their own values by the names; and the cipher, or naught (0) an insignificant figure, indicating po value when it stands alone.

NUMERATION AND NOTATION.

A figure standing alone, or the first on the right of others, Jenotes only its simple value, as so many units, or ones; the second is so many tens; the third, so many hundreds, &c., increasing continually towards the left in a tenfold proportion.

Numeration is the art of reading numbers expressed in figures; and Notation, the art of expressing numbers by figures



d

THE TABLE.

Norg. To read any Number. Divide it into periods of six figures each, beginning at the right hand; and each period into semi-periods with a different mark, for the sake of distinction. The first on the right hand is the Units' period, the second the Millions' period, &c. Beginning at the left, observe that the three figures of every complete semiperiod must be reckoned as so must hundreds, tens, and units; joining the word thousands when you come to the middle of the period, and the proper name of the period at the end of it.

2. To express any given Number in Figures. Begin at the left, and write the figures which denote (as so many *bundreds. tens*, and *units.*) the number in that *semi-period*; and proceed thus with each successive semi-period, till the whole is completed; placing a separating comma in the middle of each period, or immediately after the thousands, and a semicolon between the periods. But observe, that though every semi-period but the first on the left must have its complete number of *three* figures, *that* may be incomplete, and consist of only one or two figures: also, where significant figures are not required in any part of a number, no semi-period must be omitted, but the places must be filled up with ciphers.

Example. Write in figures, seventy thousand four hundred billions, **two** hundred and ten thousand millions, and ninety-six.

First, write 70 (seventy) with a comma, these being thousands; ther, 400 (four hundred) with a semicolon, denoting the end of the period; pext, write 210 (two hundred and ten) and, because they are thousands, put a comma after them, and then 000 (three ciphers, there being no more millions) followed by a semicolon, to denote the completion of the period; again, put 000 (three more ciphers, denoting the absence of thousands) with a comma after them, and then 096, (ninety-six,) which will complete the number: thus, 70,400;210,000;000,096.

EXERCISES IN NUMERATION AND NOTATION.

Read, or write in words the following numbers

3 30 33 300 303 330 333 127 172 217 271	<pre>(13) 721 (14) 906 (15) 4294 (16) 94294 (17) 294294 (18) 3703 (19) 703703 (20) 311311 (21) 113113 (22) 131131131 (23) 708807780</pre>	 (25) 500050005 (26) 1010100 (27) 11110101 (28) 499994949 (29) 3584600987 (30) 584610070840 (31) 5846100708400 (32) 37613590200116 (33) 500800400000 (34) 60100800180070 (35) 3700000000075048
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* The figures in parentheses refer to the Editor's Key to this work.

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NUMERATION.

Express in figures the following numbers.

(1) Nine; ninety; ninety-nine; nine hundred; nine hundred and nine; nine hundred and ninety; nine hundred and ninety-nine.

(2) One hundred and eight; one hundred and eighty; eight hundred and one; eight hundred and ten; one hundred and sixteen; one hundred and sixty-one; six hundred and eleven.

(3) One hundred and twenty-three; one hundred and thirtytwo; two hundred and thirteen; two hundred and thirty-one. three hundred and twelve; three hundred and twenty-one.

(4) Two thousand five hundred and seventy-two.

(5) Seventy-two thousand five hundred and seventy-two.

(6) Five hundred and seventy-two thousand five hundred and seventy-two.

(7) Ten thousand nine hundred and ten.

(8) Nine hundred and ten thousand nine hundred and term

(9) One hundred and nine thousand nine hundred and one.

(10) One hundred and ninety thousand and ninety-one.

(11) Nine hundred and one thousand and nineteen.

(12) One hundred and fourteen millions, one hundred and forty-one thousand four hundred and eleven.

(13) Four hundred and six millions, six hundred and four thousand four hundred and sixty.

(14) Six hundred and forty millions, forty-six thousand and sixty-four.

(15) Seven millions, seventy thousand seven hundred.

(16) Seven hundred millions, seven thousand and seventy.

(17) Ten millions, one thousand one hundred.

(18) One hundred and one millions, eleven thousand cne hundred and ten.

(19) Twelve billions, seventeen thousand and nine millions and eighty-nine.

(20) Seven thousand five hundred and four trillions, sixty thousand millions, eight hundred thousand.

Roman Numere .

I	1	One.	1 VT	6	Six.	ΣI	11	Eleven.
II	2	Two.	¥11	7	Sever.	λΠ	12	Tweive.
ÌII	3	Three	' 11 I	8	Eight.	XIII	13	Thirteer's
ÌV	4	Four.	X	9	Nino	XIV	14	Four 😰 🕽
Ŵ.	5	Five	X	10	Ten	XV	15	Fifte A

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XVI	15	Sixteen.	1 CC	200	Two hundred.
XVII	17	Seventeen.	CCC	300	Three hundred.
XVIII	18	Eighteen.	CCCC	400	Four hundred.
XIX	19	Nineteen.	D	500	Five hundred.
XX	20	Twenty.	DC	600	Six hundred.
XXX	30	Thirty.	DCC	700	Seven hundred.
XL	40	Forty.	DCCC	800	Eight hundred.
L	50	Fifty.	DCCCC		
LX	60	Sixty.	M	1000	One thousand
LXX	70	Seventy.	MDCCO	CXXX	
LXXX	80	Eighty.			eight hundred and
XC	90	Ninety.			thirty.
C	100	One hundred.	ł		•

Notz. A less numerical letter standing before a greater, must be taken from it, as I before V or X, and X before L or C, &c., thus, IV. Four; IX. Nine; XL. Forty; XC. Ninety, &c. And a less numerical letter standing after a greater, is to be added to it, thus, VI. Six; XI. Eleven; LX. Sixty; CX. One Hundred and Ten.

All operations in Arithmetic are comprised under four elementary or fundamental Rules : viz., Addition, Subtraction, Multiplication, and Division.

ADDITION

TEACHES to find the sum of several numbers.

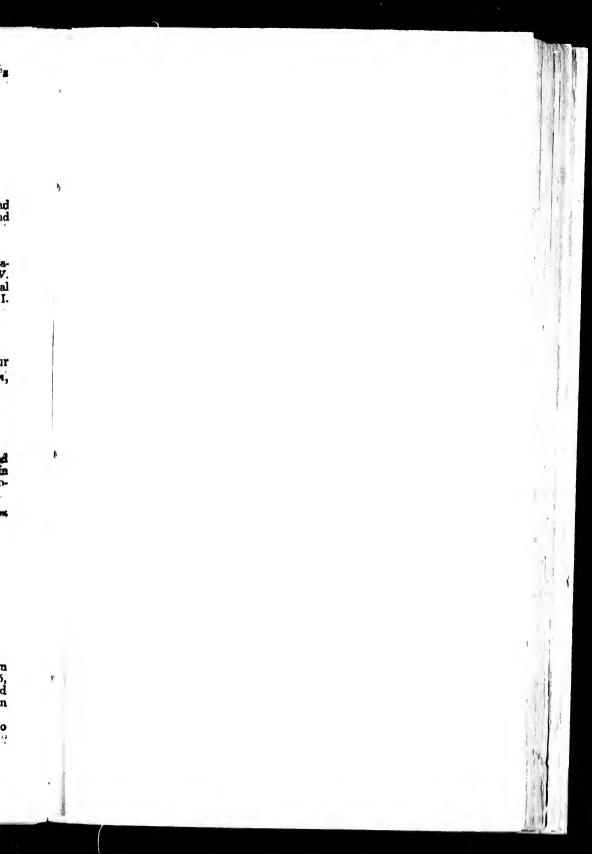
RULE. Place the numbers one under another, so that units may stand under units, tens under tens, &c.; add the units, set down the units in their sum, and carry the tens as so many ones to the next row; proceed thus to the last row, under which set down the whole amount.

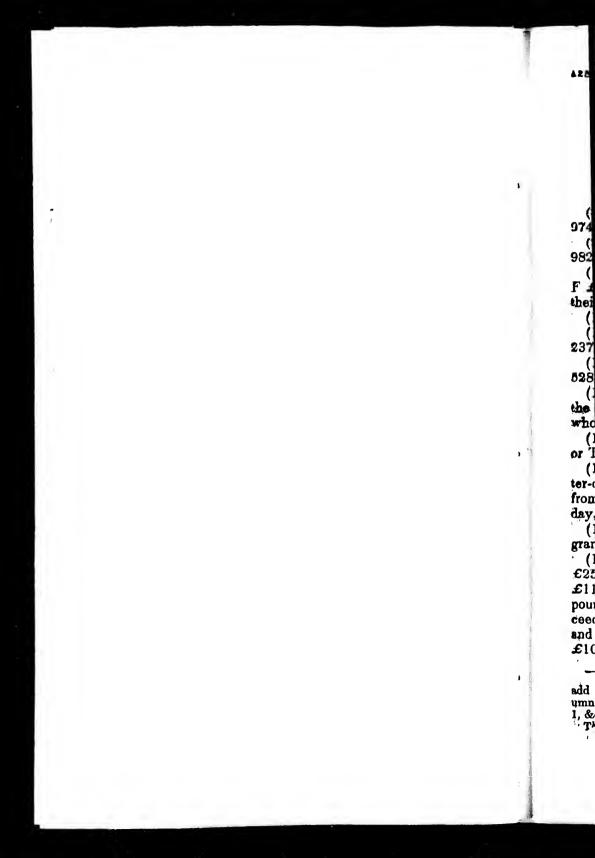
PROOF. Begin at the top and add the figures downwards: if the sum is found the same as before, it is presumed to be right.

*(1) 275	(2) 1234	(3) 75245	(4) 271048
110	7098	37502	325476
473	3314	91474	107584
354	6732	32145	625608
271	2546	47258	754087
352	6709	21476	27:736
			•

* Say 2 and 1 are 3, and 4 are 7, and 3 are 10, and 5 are 15, set down 5 and carry 1; 1 and 5 are 6, and 7 are 13, and 5 are 18, and 7 are 25, and one are 26, and 7 are 33, set down 3 and carry 3; 3 and 3 are 6, and 2 are 8, and 3 are 11, and 4 are 15, and 1 are 16, and 2 are 18, set down 18: so the sum is 1835.

After practising a few examples, it will be better for the learner to





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ADDITION OF INTEGERS.

(5) 590046	(6) 370416	(7)	781943	
73921	2890		56820	
400080	60872	1	1693748	
4987	998		300486	
19874	47523		92043750 0	
201486	9836		78632109	
9883	26627		9408175	

(8) What is the sum of 43, 401, 9747, 3464, 2263, 314, 974?

(9) Add 246034, 298765, 47321, 58653, 64218, 5376, 9821, and 640 together.

(10) If A has \pounds 56. B \pounds 104. C \pounds 274. D \pounds 1390. E \pounds 7003. F \pounds 1500. and G \pounds 998.; how much is the whole amount of their money?

(11) How many days are in the twelve calendar months?

(12) Add 87929, 135594, 7964, 3621, 27123, 8345, 35921; 2374, 64223, 42354, 3560, and 152165 together.

(13) Add 6228, 27305, 7856, 287, 7664, 100, 1423, 25258, 828, 3135, and 838.

(14) How many days are there in the first six months of the year; how many in the last six; and how many in the whole?

(15) In the year 1832, how many days from the Epiphany or Twelfth-day (Jan. 6th) to the last day of July?

(16) In the common year how many days from each Quarter-day to the next? That is, from Lady-day to Midsummer-day, from thence to Michaelmas-day, from thence to Christmasday, and from Christmas-day to the ensuing Lady-day ?

(17) When will the lease of a farm expire, which was granted in the year 1799, for ninety-nine years?

(18) A person deceased left his widow in possession of £2500. His eldest son inherited property of the value of £11340. To his two other sons he bequeathed a thousand pounds each more than to his daughter; whose portion exceeded the property left to her mother by £500. A nephew and a niece had legacies of £525. each; a public charity £105.; and his four servants the same sum to be divided

T' method will tend both to quickness and precision.

add the figures without naming them. Thus, in adding the first column of the above example, say 2, 3, 7, 10, 15; set down 5 and carry 1, &c.

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amongst them. What was the aggregate amount of his property?

(19) Tell the name and signification of the sign put between the following numbers: and find what they are equal to, as the sign requires.

1724 + 619 + 17 + 5400 + 12 + 999.

(20) Required the sum of forty-nine thousand and sixteen; four thousand eight hundred and forty; eight millions, seven hundred and seven thousand one hundred; nine hundred and ninety-nine; and eleven thousand one hundred and ten.

(21) When will a person, born in 1819, attain the age of 45?

(22) Henry came of age 13 years before the birth of his cousin James. How old will Henry be when James is of age?

(23) Homer, the celebrated Greek poet, is supposed to have flourished 907 years previous to the commencement of the Christian era. Admitting this to be fact, how many years was it from Homer's time to the close of the 18th century; and how long to A. D. 1827?

SUBTRACTION

TEACHES to take a less number from a greater, to find the remainder or Difference.

The number to be subtracted is the Subtrahend, and the other is called the Minuend.

RULE. Having placed the Subtrahend under the Minuend, (in the same order as in Addition.) begin at the units, and subtract each figure from that above it, setting down the remainder underneath. But when the lower figure is the greater, borrow ten; which add to the upper, and then subtract: set down the remainder, and carry one to the next figure of the Subtrahend for the ten that was borrowed.

PROOF. Add the Difference to the Subtrahend, and their sum will be the Minucud.

(1) F T	rom 2714754 ake 1542725	(4)	271508300 72811699	(7)	10000 00000 98 7 654321
(2)	42087296 34096187	(5)	375021599 278104609	(8)	2746981340 109568153 9
(3)	45270509 32761684	(6)	400087635 9184267	(9)	666740825 1093481 72

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ANT.] SUBTRACTION OF INTEGERS.

(10) From 123456789 subtract 98765432.

(11) From 31147680975 subtract 767380799.

(12) Subtract 641870035 from 1630054154.

(13) Required the *difference* between 240914 and 24091

(14) How much does twenty-five thousand and four exceed sixteen thousand three hundred and ninety ?

(15) If eighty-four thousand and forty-eight be deducted from half a million, what will remain?

(16) The annual income of Mr. Lemmington, senior, is twelve thousand five hundred and sixty pounds. Mr. Lemmington, junior, has an income of seven thousand eight hundred and eighteen pounds per annum. How much is the son's income less than his father's ?

(17) George the Fourth, at his accession to the throne, in 1820, was in the 58th year of his age. In what year was he born, and how long had he reigned on the 29th γ f January, 1829, the anniversary of his accession ?

(18) The sum of two numbers is 36570, and one of them, is twenty thousand and twelve: what is the other?

(19) Thomas has 115 marbles in two bags. In the green bag there are 68: how many are there in the other?

(20) Two brothers who were sailors in Admiral Lord Nelson's fleet, were born, the elder in 1767, and the younger in 1775. What was the difference of their ages, and how old was each when they fought in the battle of Trafalgar, in 1805?

(21) Henry Jenkins died in 1670, at the age of 169. How long prior to his death was the discovery of the continent of America by Columbus, in 1498 ?—Also, how many years have elapsed from his birth to 1827 ?

32906547 Minnend.Say 8 from 7 I cannot; borrow 10, and 7 arg**8210463** Subtrahend.17. 8 from 17, 9 remain; set down 9 and carry**24696079** Difference.1.—1 and 6 are 7, 7 from 4 I cannot; borrow**32906547** Proof.1.—1 and 4 are 14, 7 from 14, 7; set down 7 and
carry 1.—1 and 4 are 5, 5 from 5, nothing; set**down** (9) naught.—0 from 6, 6; set down 6.—1 from 0 I cannot; but1 from 10, 9; set down 9 and carry 1.

When the pupil is initiated in the practice by working an example or two, he may simplify the work by omitting to express some of the particulars. Thus, in the preceding example, it will be sufficient merely to say, 8 from 17, 9; set down 9 and entry 1; 1 and 6 are 7, 7 f 7; set down 7 and carry 1, &c.

EXAMPLE. From 32906547 subtract 8210468.

(22) Borrowed at various times, $\pounds 644.$, $\pounds 957.$, $\pounds 90.$, $\pounds 1378.$, and $\pounds 1293.$; and paid again the different sums of $\pounds 763.$, $\pounds 591.$, $\pounds 1161.$, $\pounds 1000.$, and $\pounds 847.$ —What remains unpaid?

(23) Explain the name and signification of the sign used; and work the two following examples.

10874 — 9999 51170 — 50049 (24) John is seventeen years younger than Thomas: how old will Thomas be when John is of age; and how old will John be when Thomas is 50?

MULTIPLICATION

TEACHES to repeat a given number as many times as there are units in another given number.

The number to be multiplied is called the Multiplicand; that by which we multiply is the Multiplier; and the number produced by multiplying is the Product.

RULE. When the multiplier is not more than 12 multiply the units' figure of the multiplicand, set down the units of the product, reserving the tens; multiply the next figure, to the product of which carry the tens reserved: proceed thus till the whole is multiplied, and set down the last product in full.*

MULTIPLICATION TABLE.

1	2	3	4	5	6	7	8	9	10	11	12
2	4	6	8	10	12	14	16	18	20	22	24
3	6	9	12	15	18	21	24	27	30	33	36
- 4	8	12	16	20	24	28	32	36	40	44	48
5	10	15	20	25	30	35	40	45	50	55	60
6	12	18	24	30	36	42	48	54	60	66	72
7	14	21	28	35	42	49	56	63	70	77	84
8	16	24	32	40	48	56	64	72	80	88	96
9	18	27	36	45	54	63	72	81	90	99	108
10	20	30	40	50	60	70	80	90	100	110	120
11	22	33	44	55	66	77	88	99	110	121	132
12	24	36	48	60	72	84	96	108	120	132	144

* EXAMPLE. Multiply 713097 by 4.

713097 4 2852388 Say 4 times 7 are 28, set down 8 and carry 2; 4 times 9 are 36 and 2 are 33, set down 8 and carry 3; 4 times 0 (naught) and 3 are 3, set down 3; 4 times 3 are 12, set down 2 and carry 1: 4 times 1 are 4 and 1 are 5, set down 5; 4 times 7 are 23, set down 28.

(1) M (2) M (3) M

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(4) M

(5) M (6) M

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(17) 1

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ASSISTANT.] MULTIPLICATION OF INTEGERS.

(1) Multiply 25104736 by 2.

(2) Multiply 52471021 by 3.

(4) Multiply 27104107 by 5.

(5) Multiply 23104759 by 6. (6) Multiply 7092516 by 7.

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(7) Multiply 3725104 by 8. (8) Multiply 4215466 by 9. (3) Multiply 7925437521 by 4. (9) Multiply 2701057 by 10. (10) Multiply 31040171 by 11.

(11) Multiply 73998063 by 12.

(12) Multiply 780149326 by 3, 4, 5, 6, 7, 8, 9, and 10.

(13) Multiply 123456789 by 4, 5, 6, 7, 8, and 9.

(14) Multiply 987654321 by 9, 10, 11, and 12.

When the multiplier is between 12 and 20, multiply by the units' figure in the multiplier, adding to each product the last figure multiplied.

(15) 5710592×13 . | (18) 2057165×16 . | (20) 9215324×18 . (16) 5107252×14 . (19) 6251721×17 . (21) 2571341×19 . (17) 7653210×15.

When the multiplier consists of several figures, multiply by each of them separately, observing to put the first figure of every product under that figure you multiply by. Add the several products together, and their sum will be the total product.[†]

PROOF. Make the former multiplicand the multiplier, and the multiplier the multiplicand; and if the work is right, the products of both operations will correspond. Otherwise. A presumptive or probable proof (not a positive one) may be obtained thus: Add together the figures in each factor, casting out or rejecting the nines in the sums as you proceed; set down the remainders on each side of a cross, multiply them together, and set down the excess above the nines in their product

* To multiply by 10, annex a cipher to the multiplicand, for the product. To multiply by 100, annex two ciphers, &c.

EXAMPLES.

* Multiply 96048 by 15.

1440720

96048 15 440720	Say 5 times 8 are 40, set down 0 and carry 4; 5 times 4 are 20 and 4 are 24, and 8 are 32, set down 2 and carry 3; 5 times 0 and 3 are 3, and 4 are 7, set down 7; 5 times 6 are 30, set down 0 and carry 3; 5 times 9 are 45 and 3 are 48, and 6 are 54, set down 4 and carry 5; 5 and 9 are
t Multiply	14, set down 14. 76047 by 249.

76047			-
~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~			Proof.
684423	Produc	t by 9.	0
304188		by 40.	0×6
152094	do.	by 200.	0
18935703	Total J	oroduct	

at the top of the cross. Then cast out the nines from the *product*, and place the *excess* below the cross. If these two correspond, the work is *probably* right: if not, it is *certainly* wrong.

(22) 271041071×5147 .	(21) 170925164×7419.
(23) 62310047×1668.	(25) 9500985742×61879.
(26) 17014958	68567×4768756.

When ciphers are intermixed with the significant figures in the multiplier, they may be omitted; but great care must be taken to place the first figure of the next product under the figure you multiply by.*

Ciphers on the right of the multiplier or multiplicand (if omitted in the work) must be placed in the total product.

(27)	$571204 \times 27009.$	(30)	$1379500 \times 3400.$
(28)	$7561240325 \times 57002.$	(31)	7271000×52600.
(29)	$562710934 \times 590030.$	(32)	74837000×975000.

A number produced from multiplying two numbers together is called a *compósite number*; and the two numbers producing it are called the *factors*, or *component parts*. When the multiplier is a *compósite number*, you may multiply by one of the *factors*; and that product multiplied by the *other* will give the total product.[‡]

(33)	771	$039 \times 35.$
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(34) 921563 \times 32.

(35) 715241 \times 56.

(36) 679998×132.

(37) 7984956 \times 144.

(38) 8760472×999.§ (39) 7039654×99999.

(40) A boy can point 16000 pins in an hour. How many can five boys do in six days, supposing them to work 10 cleap hours in a day?

Exa	AMPLES.
 Multiply 31864 by 7008. 31864 7008 Proof. 254912 6 223048 4×6 223302912 6 	t Multiply 63175 by 45. 63175 $5 \times 9 = 45$ 315875 9 2842875
t Multiply 63350 by 5200. 63350 5200 Proof. 12770 1 31925 4×7 332020000 1	§ For an abridged method of multiplying by a series of ninss, see the Key.

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(41) If a person walks upon an average 7 miles a day, how many miles will he travel in 42 years, reckoning 365 days to a year?

(42) Multiply the sum of 365, 9081, and 22048, by the difference between 9081 and 22018.

(43) Required the continued product of 112, 45, 17, and 99.

Note. Multiply all the numbers one into another.

DIVISION

TEACHES to find how often one number is contained in another: or to divide a number into any equal parts required.

The number to be divided is called the *Dividend*; that by which we divide is the *Divisor*; and the number obtained by dividing is the *Quotient*; which shows how many times the divisor is contained in the dividend. When it is not contained an exact number of times, there is a part of the dividend left, which is called the *Remainder*.

RULE. When the divisor is not more than 12, find how often it is contained in the first figure (or two figures) of the dividend; set down the quotient underneath, and carry the overplus (if any) to the next in the dividend, as so many tens; find how often the divisor is contained therein, set it down, and continue in the same manner to the end.

When the divisor exceeds 12, find the number of times if is contained in a sufficient part of the dividend, which may be called a *dividual*; place the quotient figure on the right, multiply the divisor by it, subtract the product from the dividual, and to the remainder bring down the next figure of the dividend, which will form a new dividual: proceed with this as before, and so on, till all the figures are brought down.

FROOF. Multiply the divisor and quotient together, adding the remainder (if any) and the product will be the same as the dividend.

(1) Divide 725107 by 2.* (2) Divide 7210472 by 3.

* EXAMPLE. Divide 7323105 by 4.

Divisor 4)7328105 Dividend. Quotient 1832026-1 Rem.

> 4 7328105 Proof.

Say the fours in 7, once and 3 over; the fours in 33, 8 times 4 are 32 and 1 over; the fours in 12, 3 times; the fours in 8, twice; the fours in 1, 0 and 1 over; the fours in 10, twice 4 are 8, fours are 24 and 1 over.

and 2 over; the fours in 25, six fours are 24 and 1 over.

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DIVISION OF INTEGERS.

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(3) Divide 7210416 by 4.	$(14)7210473$ $\div 37.$
	(15) 42749467 \div 347.
(5) Divide 5231037 by 6.	$(16)734097143 \div 5743.$
(6) Divide 2532701 by 7.	(17) 1610478407 \div 54716.
(7) Divide 2547325 by 8.	$(18) 4973401891 \div 510834.$
(8) Divide 25047306 by 9.	$(19) 51704567874 \div 4765043.$
(9) Divide 70312645 by 10.	$(20) 17453798946123741 \div$
(10) Divide 12804763 by 11.	31479461.
(11) Divide 79043260 by 12.	$(21)25473221$ $\div 27100.\ddagger$
(12) Divide 37000421 by 3,	$(22)725347216 \div 572100.$
5, 7, and 9.	$(23)752473729 \div 373000.$
(13) Divide 111111111 by 6,	$(24) 6325104997 \div 215000.$
9, 11, and 12.	

When the divisor is a *composite number*, you may divide the dividend by one of the *component parts*, and that quotient by the *other*; which will give the quotient required. But the *true remainder* must be found by the following

RULE. Multiply the second remainder by the first divisor: to that product add the first remainder, which will give the true one.

(25)	3210473÷27.§
	7210473÷35.

(27) $6251043 \div 42$. (28) $5761034 \div 54$,

• EXAMPLE. Divide 40855 by 29. Dividend. Divisor 29)40855(1403 Quotient. $\begin{array}{r}
29 \\
29 \\
118 \\
255 \\
255 \\
23 \\
232 \\
40855 \\
106 \\
255 \\
23 \\
23 \\
\end{array}$ Remainder.

* When the divisor is large, the quotient figures are most easily found by trials of the first figure (or two) in the leading figures of the dividend.

‡ Ciphers at the right of the divisor may be cut off, and as many figures from the right of the dividend; but these must be annoxed to the remainder at last.

§ EXAMPLE. Divide 314659 by 21. 21=7×3)314659

$$\frac{7)104886-1}{14983-5} \bigg\} = 5 \times 3 + 1 = 16 \text{ rem}.$$

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DIVISION OF INTEGERS.

A number may be divided by 10, 100, 1000, &c., by merely outting off one, two, three, &c., figures on the right: the other figures are the quotient, those cut off are the remainder.

Thus $76390 \div 10 = 7639$; $238457 \div 10 = 23845$ and 7 rem. And $4598653 \div 1000 = 4598$ and 653 rem.

(29) $65941089 \div 10.$ (31) $18043329 \div 10000.$

(30) $7208465 \div 100.$ (32) $7406572 \div 1200.$

(33) What is the difference between the 12th part of 107724, and the 23d part of 346610?

(34) If a ship bound to Jamaica set sail from Liverpool on the 25th of January, 1828, and arrived at that island on the 8th of March, what was the velocity of her sailing per day and per hour; the distance being 4558 miles?

Note. This is the *direct* distance. The circuitous course of the ship would be considerably more.

(35) The period of Jupiter's revolution in his orbit round the sun, which is the year of that planet, is 4330 of our days. How many of our years, reckoning 365 days to the year, are equal to five years of Jupiter?

(36) I would plant 2072 clms in 14 rows, the trees in each row 17 feet asunder: what length will the grove be?

(37) If a chest of oranges, 1292 in number, be distributed, one moiety among 19 boys, the other among 17 girls: how many will fall to the share of each?

(38) The circumference of the earth's orbit, or annual path round the sun, is about 596440000 miles. Supposing the year to be exactly $365\frac{1}{4}$ days, or 8766 hours, how many miles in an hour, and how many in a minute, are we carried by this motion?

(39) Required the sum, the difference, the product, and the quotient, of 3679 and 283: and also the quotient of the product divided by the sum.

(40) The sum of two numbers is 4290; the less number is 143: what is their difference, product, and quotient; and the quotient of the product divided by the difference?

(41) The product of a certain number multiplied by 694, when 320 are added, is equal to 5000000: what is that number?

(42) Allowing the earth to revolve on its axis in exactly 24 hours, and the circumference at the equator to be 24864 miles; at what rate per hour and per minute are the inhabitants of that part carried round by the revolution? Also, at what rate are the inhabitants of London carried round, the circumference m that latitude being 15480 miles?

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ARITHMETICAL AND COMMERCIAL TABLES.

STERLING MONEY.

4 farthings (qrs.) make 1 penny, d.

12 pence 1 shilling, s. 5 shillings 1 crown, cr.

20 shillings 1 pound, or sovereign, \mathcal{L} .

 $\frac{1}{d}$. denotes a farthing, $\frac{1}{d}d$. a halfpenny, and $\frac{3}{d}d$. three farthings.

> Qrs. 4 == 1 penny. 48 = 12 = 1 shilling. 240 = 60 = 5 = 1 crown. 960 = 240 = 20 = 4 = 1 pound.

OBSOLETE COINS.

A guinea (weight 5 dwts. 91 grs.) value 21s. A moidore, 27s. A, pistole, 17s. A mark, 13s. 4d. An angel, 10s. A noble, 6s. 8d. A tester, 6d. A groat, 4d.

Notes. Gold is considered the standard metal; and there is no alteration in the new coin, either in fineness or weight, from that of former, ation in the *new work*, either in findences of weight, from that of lefther, coinages; 21 sovereigns being equal in weight to 20 guineas. 1869 sovereigns weigh exactly 40 hs troy. A sovereign is therefore a little more than 5 dwts. $3\frac{1}{4}$ grs. (5 dwts. 3274 grs.) and a half sovereign rath-er exceeds 2 dwts. $13\frac{1}{2}$ grs. (2 dwts. 13.637 grs.) The new silver coin is of the same fineness as that of former coinages; but 1 h. of silver is now coined into 66s. instead of 62s., as it was formerly, so that one shilling now weighs 3 dwts. $15\frac{3}{11}$ grs., and other silver pieces in proportion.

The mint value of gold is £3..17..10¹/₂. per ounce, and of silver 5s. 6d.: The standard for gold coin is 22 parts (commonly called *carats*) of fine gold, and 2 parts (or *carats*) of copper, melted together. For silver coin, 11 oz. 2 dwts. of fine silver, alloyed with 13 dwts. of copper.

Farthings.	Farthings.	Pence.	Pence.	Pence.	Shillings.
grs. d.	qrs. d.	d. s .	d. s.d.	d. s. d .	s. £. s.
4 are 1	32 are 8	36 are 3	20 are 1 8	160are13 4	80 are 4 0
6 11	34 35	48 4	30 2 6	17014 2	90 4 10
82	36 9	60 5	403 4	18015 0	100 5 0
10 21	$339\frac{1}{2}$	72 6	50 4 2	19015 10	110 5 10
12 3	4010	84 7	60 5 0	20016 8	120 6 0
$14 \dots 3\frac{1}{3}$	4210	96 8	70 510		130 6 10
16 4				Shillings.	
18 4 4	46115	12010	907 6	s. £. s.	150 7 10
$20 \dots 5^{-1}$	481 <i>s</i> .	13211	1008 4	20 are 1 0	160 8 O
22 53		14412	1109 2	30 110	170 8 10
				40 2 0	
26 64	d. s.	16814	13010 10	50210	190 9 10
.28 7	12 are 1	18015	14011 8	60 3 0	20010 0
30 74	24 2	19216	15012 6	70 310	21010 10

MONEY TABLE.

No lings £12. gives

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Nore. When the units' figure is cut off from any number of shillings, half the remaining figures will be the pounds. Thus, 256s.= £12. 16s. because half of 25=12; and the one over prefixed to the 6, gives 16s.

WEIGHTS AND MEASURES.

TROY WEIGHT.

24 grains (gr.) make 1 pennyweight, dwt. 20 pennyweights 1 ounce 0Z. 12 ounces łb. 1 pound, Grains. 24 = 1 pennyweight. 480 = 20 = 1 ounce. 5760 = 240 = 12 = 1 pound. Gold, silver, and gems, are weighed by this weight APOTHECARIES' WEIGHT. 20 grains (gr.) make 1 scruple, . Э 3 scruples . . 1 dram, . 3 8 drams . . . 1 ounce, 3 12 ounces . . . 1 pound, . . В. **Grains.** 20 = 1 scruple. 60 =3 = 1 dram. 480 = 24 = 8 = 1 ounce.

5760 = 283 = 96 = 12 = 1 pound.

This is used only in the mixing of medicines.

These are the same grain, ounce, and pound, as those in Troy Weight.

AVOIRDUPOIS WEIGHT.

	6 drams (dr.) make					1 ounce,.	•	02.
	6 ounces							
	4 pounds				•	1 stone, .	•	st.
2	8 pounds, or 2 stone	s.		•		1 quarter,	•	qr.
	4 quarters, or 8 st. o	r 1	12 H	•		1 hundred,	•	cwt.
2	0 hundreds	•			•	1 ton,		ť.

Drams. 16 = 1 ounce.

256 = 16 = 1 pound.

3584 = 224 = 14 = 1 stone.

7168 = 448 = 28 = 2 = 1 quarter.

28672 = 1792 = 112 = 8 = 4 = 1 cwt.

573440 = 35340 = 2240 = 160 = 80 = 20 = 1 ton.

By this weight nearly all the common necessaries of life are weighed. A truss of hay=56 b. and one of straw=36 b. A load is 36 trusses. A peck loaf weighs 17 b. 6 oz. 1 dr. In the metropolis, 8 b. are a stone of meat. A fother of lead is 19½ cwt. In some districts, goods of various descriptions (as cheese, coal, &c., are sold by the long cwt. or 120 b.

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5s. 6d. ats) of for sil-

 $\begin{array}{c} ngs. \\ \textbf{f}. s. \\ \textbf{f}. s.$

WEIGHTS AND MEASURES

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WOOL.

When wool is purchased from the grower, the legal stone of 14 Hb. and the tod of 28 Hb. are used. But in the dealings between woolstaplers and manufacturers,

15 pounds are	•	•	1	stone.
2 stones or 30 Hz.				tod.
8 tods, or 240 lb.	,	•	1	pack or sack.

COMPARISON OF WEIGHTS.

A grain is the elementary or standard weight 1 ounce avoirdupois is . $437\frac{1}{2}$ grains. 1 ounce troy . . . 4801 pound troy . . . 57601 pound avoirdupois . . 7000

175 pounds troy=144 pounds avoirdupois.

175 ounces troy=192 ounces avoirdupois.

We may, therefore, reduce lbs. Troy into Avoirdupois by multiplying them by 144, and dividing by 175, &c.

LINEAL, OR LONG MEASURE.

12 inches (<i>in.</i>) make	1 foot, ft
3 feet, or 36 inches	1 yard, yd.
2 yards, or 6 feet	1 fathom, fa.
51 yards, or $16\frac{1}{2}$ feet	1 pole, rod, or perch, p.
4 poles, or 22 yards	1 land chain,* . ch.
40 poles, or 10 ch., or 220 yds.	1 furlong, fur.
8 furlongs, or 1760 yards .	1 mile, m.
3 miles	1 league, l.

Barley-corns.

3 = 1 inch.

36 = 12 = 1 foot. 108 = 36 = 3 = 1 yard 594 = 198 = 161 = 51 = 1 pole. 23760 = 7920 = 660 = 220 = 40 = 1 furlong. 190080 = 63360 = 5280 = 1760 = 320 = 8 = 1 mile.

Norr. It is commonly supposed that the English inch was original by taken from three grains of barley, selected from the middle of the ear and well dried.

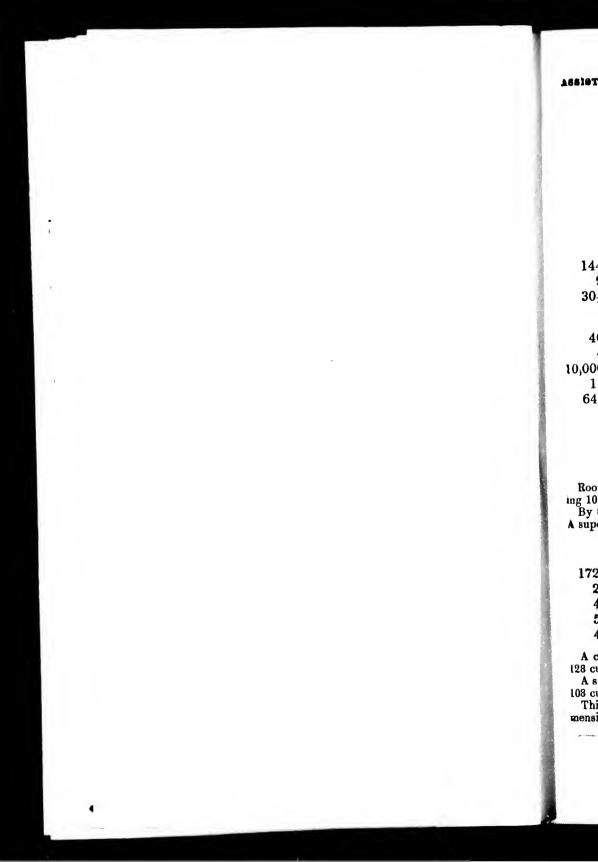
A twelfth part of an inch is called a *line*.

4 inches are a hand, used in measuring the height of horses. 5 feet are a pace. A cubit $= 1\frac{1}{2}$ feet nearly.

This measure determines the length of lines. A line has the dimention of length only, without breadth or thickness.

* The chan consists of 100 links, each link being - 7.92 inches.

OR'S ston**e** dealplying d. a. p. h. ur. riginal of the 5 feet dimen 1.1 1 J



TABLES OF MEASURES.

CLOTH MEASURE.

21 inches (in.) make .	
4 nails, or 9 inches .	. 1 quarter, . qr.
4 quarters	
5 quarters	
A Flemish ell is 3 qrs.	A French ell 6 qrs.

Used for all drapery goods.

SUPERFICIAL, OR SQUARE MEASURE.

144 square inches (sq. in.) ma	ke 1 square foot, sq. ft.
9 square feet	. 1 square yard, sq. yd.
$30_{\frac{1}{4}}$ sq. yards, or $272_{\frac{1}{4}}$ sq. fee	t 1 sq. rod, pole, or perch

Also, in the measure of land,

40 perches make	. 1 rood,	• •	r .
4 roods, or 4840 yards .			
10,000 square links			
10 sq. chains, or 100,000 linl			
640 acres	. 1 square r	nile,	sq. m.
Inches. $144 = 1$ foot. 1296 = 9 = 1 y	vard.		
$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	= 1 pole.	3	
$1508150 \equiv 10850 \equiv 1210$ 6272640 = 43560 = 4840			

Roofing, flooring, &c., are commonly charged by the Square, contain ing 100 square feet.

By this measure is expressed the area of any superficies, or surface. A superficies has measurable length and breadth.

CUBIC, OR SOLID MEASURE.

1728 cubic inches (in.) make .	1 cubic foot.
27 cubic feet	1 cubic yard.*
40 feet of round timber, or 50 feet of hewn timber	1 ton, or load.
42 feet	1 ton of shipping.

A cord of wood is 4 feet broad, 4 feet deep, and 8 feet long, being 128 cubic feet.

A stack of wood is 3 feet broad, 3 feet deep, and 12 feet long, being 108 cubic feet.

This determines the solid contents of bodies. A solid has three dimensions, length, breadth, and thickness.

* A solid yard of earth is called a load.

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TABLES OF MEASURES.

26

IMPERIAL MEASURE.

This is the standard now established by Act of Parliament, as a general measure of capacity for liquid and dry articles.

> 2 pints (*pt.*) make . . . 1 quart, *qt*. 4 quarts 1 gallon, *gal*.

The imperial or standard gallon must contain 10 ibs. Avoirdupois weight of pure water, at the temperature of 62° of Fahrenheit's thermometer. This quantity measures 2771* cubic inches; being about one-fifth greater than the old wine measure, one-thirty-second greater than the old dry measure, and one-sixtieth less than the old ale measure.

IN DRY MEASURE,

2	gallons	(ga	<i>l.</i>)	ma	ke		1	peck,	pk.
4	pecks	•	•	•	•		1	bushel,	Ъ.
8	bushels				•		1	quarter,	q r .

Corn to be stricken off the measure with a round stick, or roller. *Obsolete.* A coom = 4 bushels; a chaldron = 4 quarters; a wey = 5 quarters; a last = 2 weys.

Solid inches. $277\frac{1}{4} = 1$ gallon.

 $554\frac{1}{2} = 2 = 1$ peck. 2218 = 8 = 4 = 1 bushel.

17744 = 64 = 32 = 8 = 1 quarter.

OF COALS,

3 bushels make	1 sack.
12 sacks, or 36 bushels	1 chaldron.
21 chaldrons	1 score.

All the measures used for heaped goods are to be of cylindrical form; the diameter being at least double the depth. The height of the raised cone to be equal to three-fourths of the depth of the measure.

The old dry gallon contained 2684 cubic inches.

NOTE. The bushel, for measuring heaped goods, must be 17.81 inches in diameter, and 8.904 inches deep; or if made 18 inches in diameter, the depth will be 8.717 inches. The cone to be raised 6.6 inches in height.

In WINE AND SPIRIT MEASURE, the old gallon contained 231 cubic inches.

63 gallons were a hogshead, hhd.

2 hogsheads, or 126 gallons a pipe or butt.

4 hogsheads, or 252 gallons a tun.

More accurately, 277.274 cubic inches.

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TABLES OF MEASURES.

Some other denominations have been long obsolete; as, an anker (10 gallons;) a runlet (18 gallons;) a tierce (42 gallons;) a puncheon (84 gallons.) But casks of most descriptions are generally charged according to the number of gallons contained.

Solid inches.					
	$69\frac{5}{16} =$				
				1 gallon.	
1	$.7466\frac{3}{4} =$	504 =	252 =	63 = 1 hog	shead.
				$126 = 2 = \tilde{1}$	
e	59867 = 3	2016 =	1008 = 2	252 = 4 = 2	== 1 tun.

In ALE, BEER, OF PORTER MEASURE, the old gallon contain ed 282 cubic inches; and measures of the following denomi nations have been in use :---

A firkin, conta	inin	g.		9 gallons.	
A kilderkin	• •	•		18 gallons.	
A barrel .					
A hogshead					
A butt					
Cubic inches $34\frac{21}{32} = 1$				0	
$69\frac{5}{16} = 5$	2=	1 qu	art.		
$277\frac{1}{5} = 8$					
$2495\frac{1}{4} = 75$					
$4990\frac{1}{2} = 144$	1 =	72 =	18 =	2 = 1 kilderkin.	
$9981^{-} = 288$	3 = 1	44 ==	36 =	4=2=1 barrel.	
$14971\frac{1}{2} = 433$	2 = 2	16 =	54 =	$6=3=1\frac{1}{2}=1$ hog	rsh'd.
				12 = 6 = 3 = 2 = 1	

*RULES FOR CHANGING OLD MEASURES TO IMPERIAL.

ALE Multiply by 60, and divide by 59; or add $\frac{1}{56}$ part. (True' within $\frac{1}{10000}$ part of the whole.)

Or, multiply by 179, and divide by 176. (True, within $\frac{1}{1000000}$ part.): DRY. Multiply by 32, and divide by 33; or deduct $\frac{1}{33}$ part (Error, less than $\frac{1}{3700}$ part.)

WINE. Multiply by 5, and divide by 6, or deduct $\frac{1}{6}$ part. (Error, less than $\frac{1}{1000}$ part.)

Or, multiply by 624, and divide by 749. (Error, less than $\frac{1}{6000000}$ part.)

*RULES FOR CHANGING IMPERIAL TO OLD MEASURES.

ALE. Multiply by 59, and divide by 60, or deduct $\frac{1}{50}$ part. Or, multiply by 176, and divide by 179.

DRV. Multiply by 33, and divide by 32, or add $\frac{1}{32}$ part.—That is, add one peck in every quarter, one quart in every bushel, or half a pint in every peck.

WINE. Multiply by 6, and divide by 5, or add $\frac{1}{3}$ part. Otherwise, multiply by 749, and divide by 624.

* Examples applying to these Rules will be found in the Miscella neous Questions in the latter part of the book.

TIME.

60	seconds	(sec.)	ma	ke		•	•			1 minute, . min	
60	minutes		•	•		•	•	•		1 hour, hr.	
24	hours .		•	3	•		•	•	•	1 day,* <i>d</i> .	
										1 week, wk.	
52	weeks,	1 day	, 6 ł	lour	s, (or 👌				1 Julian year, yr.	
365	days, 6	hours				- 5	•	•	•	i Julian year, yr.	
365	days, 5	hours	, 48	min	ı.,	51 <u>1</u>	se	con	ıds	The Solar year.†	
										1 century.	
	•									•	

Seconds. 60 = 1 minute.

3600 = 60 = 1 hour.

86400 = 1440 = 24 = 1 day.

604800 = 10080 = 168 = 7 = 1 week. 31557600 = 525960 = 8766 = 365 d. 6h. = 52 w. 1 d. 6h. = 1 Julian year.

 $31556931 = 525948 = 8765 = 365 d. 5 h. 48 m. 51\frac{1}{2}'' = 1$ Solar year.

The year is divided into 12 Calendar months; January, February, March, April, May, June, July, August, September, October, November, December.

The days are thirty in September, In April, June, and in November; Twenty-eight in February alone, To February twenty-nine.

The *lcap-ycars* are those which can be *exactly* divided by 4; as, 1824, 1828, &c. Hence it appears that the year is accounted 365 days, for *three years together*; and 366 days in the *fourth*: the average being $365\frac{1}{4}$ days. (*The Julian Year.*)

Four weeks are frequently called a *month*; but in this sense it is better to avoid the term.

NOTE. In all questions in this book, where the proposed or required time consists of years, months, weeks, &c., allow 4 weeks to a month, and 13 months to a year.

GEOMETRY.

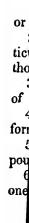
60 seconds	(″)	mal	ce		1 minute, '
60 minutes	•			•	1 degree, °
360 degrees					1 circle.

Many highly important calculations in the mathematical sciences are founded on this division of the circle.

In Astronomy, the great circle of the *ecliptic* (or of the zodiac) is divided into 12 signs, each 30°.

t The Solar, or true year, is that portion of time in which the earth makes one entire revolution round the sun.

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^{*} A day is the time in which the earth revolves once upon its axis. by law and custom it is reckoned from midnight to midnight; but the astronomical day begins at noon.

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REDUCTION.

In Geography, a degree of latitude, or of longitude on the equator, measures nearly $69_{\overline{10}}$ British miles. But a minuto of a degree is called a geographical mile.

ARTICLES SOLD BY TALE.

12 articles o								24	sheets	of	pa	per	1 quire.
12 dozen .	•	•		•	•	1	gross.	20	quires	•	•	•	1 ream.
							great gross.	2	reams	•	•		1 bundle.
20 articles	•	•	•	•	•	1	score.						

DEFINITIONS.

1. A NUMBER is called *abstract*, when it is considered *simply* or without reference to any subject; as seven, a thousand, &c.

2. When a number is applied to denote so many of a particular subject, it is a *concréte* number; as seven pounds, a thousand yards, &c.

3. A denomination is a name of any particular distinctive part of money, weight, or measure; as penny, pound, yard, &c.

4. The association of a concrete number with its subject, forms a quantity.

5. A simple quantity has only one denomination; as seven pounds.

6. A compound quantity consists of more denominations than one; as seven pounds five shillings.

REDUCTION

Is the method of changing quantities of one denomination into another denomination, retaining the same value.

RULE. Consider how many of the less name make one of the greater; and multiply by that number to reduce the greater name to the less, or divide by it to reduce the less name to the greater.

£. S			EXAMPLES.
20		0J	Reduce £386½. into farthings.
168 12			The $\pounds 8$. being multiplied by 20, and the 8s. add- ed make 168s : these being multiplied by 12 and
2022 4	d.		ed, make 168s.; these being multiplied by 12, and the $6d$. added, make $2022d$.; which being multi- plied by 4 and the 2 farthings added, make in the
8090	qr s	. Ans.	whole 8090 farthings.

[TUTOR'S

REDUCTION.

(1) In $\pounds 12$, how many shillings, pence, and farthings? Ans. 240s. 2880d. 11520 grs. (2) In 311520 farthings, how many pounds? Ans. £324..10. (3) Change 21 guineas into farthings. Ans. 21168 grs. (4) In £17..5..31. how many farthings? Ans. 16573 grs. (5) In $\pounds 25..14..1$. how many pence? Ans. 6169d. (6) Reduce 17940 pence to crowns. Ans. 299 crowns. (7) In 15 crowns, how many shillings and sixpences? Ans. 75s. 150 sixpences. (8) Change 57 half-crowns into threepences, pence, and Ans. 570 threepences, 1710d. 6840 farthings. farthings. (9) How many half-crowns, and how many sixpences, are equivalent to $\pounds 25..17..6$? Ans. 207 half-cr. 1035 sixpences. (10) Convert $\pounds 17..11..9$. into threepences. Ans 1407 threep. (11) Change £10..13..10 $\frac{1}{4}$. into halfpence. Ans. 5133. (12) In 52 crowns, as many half-crowns, shillings, and pence, how many farthings? Ans. 21424 far. (13) Convert 17380 farthings into \pounds . Ans. \pounds 18.2.1. (14) In 21424 farthings, how many crowns, half-crowns shillings, and pence, of each an equal number? Ans. 52. (15) Reduce 60 guineas to shillings, crowns, and pounds. Ans. 1260s. 252 crowns, £63. (16) Reduce 76 moidores* into pounds. Ans. £102..12. (17) How many shillings, half-crowns, and crowns, an equal number of each, are there in $\pounds 556$.? Ans. 1308 of each, and 2s. over. (18) In 1308 crowns, as many half-crowns, and as many shillings, how many pounds? Ans. £555..18. (19) Seven men brought £15..10. each into the mint, to be exchanged for guineas; how many would they have? Ans. 103 guineas and 7s. over. (20) In 525 American dollars, at 4s. 6d. each, how many **pounds** sterling? Ans. £118..2..6. Cónverse to the preceding EXAMPLE. In 8090 farthings, how many pounds? Dividing the farthings by 4, we obtain 2022d.

and 2 over, which are *farthings*, because the re-

mainder is a part of the dividend. Divide 2022

by 12, and we obtain 163s. and 6d. over: these

shillings divided by 20, give £8 8s., so that the

answer is £8..8..64. • 27 shillings. The moidore is current in Portugal, but not in Eng

land.

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hgs, and 24 far. 2.2..1. 2-crowns as. 52. pounds. , £63. 02..12. owns, an

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ASSISTANT.]

REDUCTION. WEIGHTS AND MEASURES.

TROY WEIGHT.

(21) In 27 ounces of gold, how many grains? Ans. 12960.

(22) Reduce 3 lb. 10 oz. 7 dwt. 5 gr. to grains ? Ans. 22253. (23) In 8 ingots of silver, each ingot weighing 7 lb. 4 oz.

17 dwts. 15 gr. how many grains? Ans. 341304 gr.

(24) How many ingots weighing 7 lb. 4 oz. 17 dwts. 15 gr. each are there in 341304 grains? Ans. 8 ingots.

APOTHECARIES' WEIGHT.

(25) In 27^{tb}. 73. 23. 1 3. 2 gr. how many grains? Ans. 159022 grains.

(26) In a compound of 93. 43. 13. how many pills of 5 grains each? Ans. 916 pills.

AVOIRDUPOIS WEIGHT.

(27) In 14769 ounces, how many cwt.?

Ans. 8 cwt. 0 qr. 27 lb. 1 oz.

(28) In 34 tons, 17 cwt. 1 qr. 19 lb. how many pounds? Ans. 78111 lb.

(29) In 9 cwt. 2 qrs. 14 lb. of indigo, how many half stones, and how many pounds? Ans. 154 half stones, 1078 lb.

(30) How many stones and pounds are there in 27 hogsheads of tobacco, each weighing neat $8\frac{3}{4}$ cwt.?

Ans. 1890 stones, 26460 lb.

(31) Bought 32 bags of hops, each bag 2 cwt. 1 qr. 14 lb., and another of 150 lb., how many cwt. are there in the whole? Ans. 77 cwt. 1 qr. 10 lb.

(32) In 27 cwt. of raisins, how many parcels of 18 lb. each? Ans. 168.

CLOTH MEASURE.

(33) In 27 yards, how many nails? Ans. 432.
(34) In 75 English ells, how many yards?

Ans. 93 yards, 3 grs

(35) In 24 pieces, each containing 32 Flemish ells, how many English ells? Ans. 460 English ells, 4 qrs.

(36) In 17 pieces of cloth, each 27 Flemish ells, how many yards? Ans. 344 yards, 1 qr.

(37) In 9111 yards, how many English ells? Ans. 729.

(38) In 12 bales of cloth, each containing 25 pieces, of 15 English ells, how many yards? Ans. 5625.

LONG MEASURE.

(39) In 57¹/₂ miles, how many furlongs and poles? Ans 460 furlongs, 18400 poles.

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(40) In 7 miles, how many feet and inches?

Ans. 36960 feet, 443520 inches.

(41) In 72 leagues, how many yards? Ans. 380160 yards.

(42) If the distance from London to Bawtry be accounted 150 miles, what is the number of leagues, and also the number of yards, feet, and inches?

Ans. 50 leagues, 264000 yards, 792000 feet, 9504000 inches.

(43) How often will the wheel of a coach, that is 17 feet in circumference, turn in 100 miles? Ans. $31058\frac{14}{14}$ times round.

(44) How many barley-corns will reach round the globe, the circumference being 360 degrees, supposing that each degree were 69 miles and a half? Ans. 4755801600

See Table of Geometry, page 28.

LAND MEASURE.

(45) In 27 a. 3 r. 19 p. how many perches? Ans. 4459.

(46) A person having a piece of ground, containing 37 acres, 1 perch, intends to dispose of 15 acres: how many perches will he have left? Ans. 3521 perches.

(47) There are 4 fields to be divided into shares of 75 perches each; the first field contains 5 acres; the second 4 acres, 2 perches; the third 7 acres, 3 roods; and the fourth 2 acres, 1 rood: how many shares will there be?

Ans. 40 shares, 42 perches rem.

(48) In a field of 9 acres and a half, how many gardens may be made, each containing 500 square yards?

Ans. 91, and 480 yards rem.

IMPERIAL MEASURE.

(49) In 10080 pints of port wine, how many tuns? Ans. 5 tuns.

(50) In 35 pipes of Madeira, how many gallons and pints? Ans. 4410 gals. 35280 pints.

(51) A gentleman ordered his butler to bottle off $\frac{2}{3}$ of a pipe of French wine into quarts, and the rest into pints. How many dozen of each had he? Ans. 28 dozen of each.

(52) In 46 barrels of beer, how many pints? Ans. 13248

(53) In 10 barrels of ale, how many gallons and quarts?

Ans. 360 gals. 1440 qts.

(54) In 12480 pints of porter, how many kilderkins? Ans. 86 kil. 1 fir. 3 gals.

(55) In 108 barrels of ale, how many hogsheads? Ans. 72.

(56) In 120 quarters of corn, how many bushels, pecks, gal-

lons, and quarts? Ans. 960 bu. 3840 pks. 7680 gal. 30720 qts.

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s? 5 tuns. nd pints? 0 pints. off 2 of a nto pints. en of each. 13248 quarts? 140 gts. cins? 3 gols. Ans. 72.

becks, gal-30720 *qts*. ASSISTANT.]

COMPOUND ADDITION.

(57) How many bushels are there in 970 pints?

Ans. 15 bu. 1 gal. 2 pts.

(58) In 1 score, 16 chaldrons of coals, how many sacks and bushels? Ans. 444 sacks, 1332 bushels.

TIME.

(59) In 72015 hours, how many weeks?

Ans. 428 weeks, 4 days, 15 hours.

(60) How many days were there from the birth of Christ, to Christmas, 1794, estimating $365\frac{1}{4}$ days to the year? Ans. $655258\frac{1}{2}$ days.

(61) Stowe writes, that London was built 1108 years before our Saviour's birth. Find the number of hours to Christmas, 1794. Ans. 25438932 hours.

(62) From July 18th, 1799, to April 18th, 1826, how many days? Ans. $9770\frac{1}{2}$ days, reckoning $365\frac{1}{4}$ days to a year.

(63) In a lunar month, containing 29 days, 12 hours, 44 minutes, 2 seconds and eight-tenths, how many tenth parts of seconds? Ans. 25514428.

(64) How many seconds are there in 18 centuries, estimating the solar year at 365 days, 5 hours, 48 minutes, $51\frac{1}{2}$ seconds? Ans. 56802476700 seconds.

COMPOUND ADDITION

TEACHES to find the sum of Compound Quantities.

RULE. Add the numbers of the *least denomination*: divide the sum by as many as make one of the next greater; set down the remainder (if any) and carry the quotient to those of the next greater: proceed thus to the greatest denomination, which add as in Simple Addition. **PROOF.** As in simple Addition.

Ex	AMPL	E.
£.	8.	d.
	7	
	18	
	19	
	10	
4	0	9 4
45	17	43

Say 1, 2, 5, 7 farthings are 1 penny 3 farthings; set down $\frac{3}{4}$ and carry 'd.-1, 10, 11, 16, 20, 30, 40*d*. are 3s. 4*d*.; set down 4*d*. and carry 3s.-3, 12, 20, 27, 37, 47, 57*s*. are £2. 17*s*.; set down 17*s*. and carry £2. The rest as in Simple Addition.

In Addition of Money, the reduction of one denomination to the next greater is generally done without the trouble of dividing, by the knowledge previously acquired of the Money Tables.

COMPOUND ADDITION.

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MONEY.

	MON	EY.	
(1) £ s. d. 2 13 $5\frac{1}{2}$ 7 3 $4\frac{1}{4}$ 5 15 $4\frac{1}{2}$ 9 17 $6\frac{1}{4}$ 7 16 3 5 14 $7\frac{3}{4}$	$\begin{array}{c} (4) \\ \textbf{f.} & s. & d. \\ \textbf{75} & \textbf{3} & \textbf{0} \\ 54 & 17 & 1 \\ 91 & 15 & 11\frac{1}{4} \\ 35 & 16 & 1\frac{3}{4} \\ 29 & 19 & 11\frac{1}{4} \\ 91 & 17 & 3\frac{1}{4} \end{array}$	$\begin{array}{c} (7) \\ \pounds. \ s. \ d. \\ 21 \ 14 \ 7\frac{1}{4} \\ 75 \ 16 \ 0 \\ 79 \ 2 \ 4\frac{1}{4} \\ 57 \ 16 \ 5\frac{1}{2} \\ 26 \ 13 \ 8\frac{3}{4} \\ 54 \ 2 \ 7 \end{array}$	$\begin{array}{c} (10) \\ \pounds & s. & d. \\ 261 & 17 & 14 \\ 379 & 13 & 5 \\ 257 & 16 & 73 \\ 184 & 13 & 5 \\ 725 & 2 & 34 \\ 359 & 6 & 5 \end{array}$
$\begin{array}{c} (2) \\ \textbf{\pounds} & \textbf{s.} & \textbf{d.} \\ 27 & 7 & 0 \\ 34 & 14 & 101 \\ 57 & 19 & 21 \\ 91 & 16 & 0 \\ 75 & 18 & 7\frac{3}{4} \\ 97 & 13 & 5 \end{array}$	$\begin{array}{c} (5) \\ \pounds & s. & d. \\ 257 & 1 & 5\frac{1}{4} \\ 734 & 3 & 7\frac{3}{4} \\ 595 & 5 & 3 \\ 159 & 14 & 7\frac{1}{2} \\ 207 & 5 & 4 \\ 798 & 16 & 7\frac{1}{4} \end{array}$	$\begin{array}{c} (8)\\ \textbf{\pounds}. & s. & d.\\ 73 & 2 & 1\frac{1}{2}\\ 25 & 12 & 7\\ 96 & 13 & 5\frac{1}{2}\\ 76 & 17 & 3\frac{1}{4}\\ 97 & 14 & 1\frac{1}{2}\\ 54 & 11 & 7\frac{1}{4} \end{array}$	$\begin{array}{c} (11)\\ \pounds. & s. & d.\\ 31 & 1 & 1\frac{1}{2}\\ 75 & 13 & 1\\ 39 & 19 & 7\frac{1}{4}\\ 97 & 17 & 3\frac{1}{4}\\ 36 & 13 & 5\\ 24 & 16 & 3\frac{1}{4} \end{array}$
$\begin{array}{c} (3) \\ \textbf{f.} & s. & d. \\ 35 & 17 & 0 \\ 59 & 14 & 10\frac{1}{2} \\ 97 & 13 & 10\frac{1}{4} \\ 37 & 16 & 8\frac{1}{4} \\ 97 & 15 & 7 \\ \textbf{59} & 16 & 0\frac{1}{2} \end{array}$	$\begin{array}{c} (6) \\ \pounds & s. \ d. \\ 525 \ 2 \ 4\frac{1}{4} \\ 179 \ 3 \ 5 \\ 250 \ 4 \ 7\frac{1}{4} \\ 975 \ 3 \ 5\frac{1}{4} \\ 254 \ 5 \ 7 \\ 379 \ 4 \ 5\frac{3}{4} \\ \end{array}$	$\begin{array}{c} (9)\\ \pounds, & s. \ d.\\ 127 & 4 \ 7\frac{1}{2}\\ 525 & 3 \ 10\\ 271 & 0 \ 0\\ 524 & 9 \ 1\\ 379 & 4 \ 0\frac{1}{2}\\ 215 & 5 \ 11\frac{3}{4}\\ \end{array}$	(12) £. s. d. 27 13 51 16 12 101 9 13 01 15 2 101 37 19 0 56 19 13 (12)

WEIGHTS AND MEASURES.

TROY WEIGHT.	APOTHECARIES' WEIGHT.						
(13) (14)	(15) (16)						
oz. dwt. gr. lh. oz. dwt. gr.	1b. 3. 3. D. 3. 3. D. gr.						
5 11 4 5 2 15 22	17 10 7 1 2 1 0 12						
7 19 21 3 11 17 14	9 5 2 2 1 7 1 17						
3 15 14 3 7 15 19	27 11 1 2 10 2 0 14						
7 19 22 9 1 13 21	9 5 6 1 5 7 1 15						
9 18 15 3 9 7 23	37 10 5 2 9 5 2 13						
8 13 12 5 2 15 17	49 0 7 0 1 4 1 18						

34

(17

ASSI

(20)

26 279

ASSISTANT.	COMPOUN	D ADDITION.	35
	AVOIRDU	POIS WEIGHT.	
152 272 303 255 173	15 15 14 10 15 11 10 4 6 2	$\begin{array}{cccc} cwt. \ qrs. lb. \\ 25 \ 1 \ 17 \\ 72 \ 3 \ 26 \\ 54 \ 1 \ 16 \\ 24 \ 1 \ 16 \\ 17 \ 0 \ 19 \\ 55 \ 2 \ 16 \end{array} \tag{1}$	9) t. cwt. qrs. lb. 7 17 2 12 5 5 3 14 2 4 1 17 3 18 2 19 7 9 3 20 8 5 1 24
	LONG	MEASURE.	
(20) yds. 225 171 52 397 154 137	$ \begin{array}{c ccccc} ft. in. & (21) lea \\ 1 & 9 & 72 \\ 0 & 3 & 27 \\ 2 & 6 & 35 \\ 0 & 10 & 79 \\ 2 & 7 & 51 \\ 1 & 4 & 72 \\ \hline \end{array} $	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
E.	1		ASURE. (26)
yds. qrs. n. 135 3 3 70 2 2 95 3 0 176 1 3 26 0 1 279 2 1	$\begin{array}{c} E. e. qrs. n. \\ 272 & 2 & 1 \\ 152 & 1 & 2 \\ 79 & 0 & 1 \\ 156 & 2 & 0 \\ 79 & 3 & 1 \\ 154 & 2 & 1 \\ \hline \end{array}$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
	IMPERIA	L MEASURE.	
(27) WI		(29)	ID BEER
thds.gals.qts. 31 57 1 97 18 2 76 13 1 55 46 2 87 38 3 55 17 1	t. hhd.gal.qts. 14 3 27 2 19 2 56 3 17 0 39 2 75 2 16 1 54 1 19 2 97 3 54 3	bar. fir gal 25 2 7 17 3 5 96 2 6 75 1 8 96 3 7 75 0 5	hhd. gai. gas. 76 51 2 57 3 3 97 27 3 22 17 2 32 19 3 55 18 3
	(17) $b.$ 152 272 303 255 173 635 (20) $yds.$ 225 171 52 397 154 137 CLOTH (23) yds. $qrs. n.$ 135 3 3 70 2 2 95 3 0 176 1 3 26 0 1 279 2 1 Mds.gals.qts. 31 57 1 97 18 2 76 13 1 55 46 2 87 38 3 55 17 1	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	AVOIR DUPOIS WEIGHT. (17) $b.$ oz. dr. 152 15 15 272 14 10 72 3 26 303 15 11 272 14 10 72 3 26 303 15 11 54 1 16 255 10 4 24 1 16 173 6 2 17 0 19 635 13 13 55 2 16 17 0 19 635 13 13 55 2 16 17 0 19 635 13 13 55 2 16 17 0 3 27 1 7 22 52 2 6 397 0 10 79 0 6 12 154 2 7 51 1 6 17 137 1 4 72 0 5 21 154 2 7 135 3 3 272 2 1 726 1 31 70 2 2 152 1 2 219 2 17 95 3 0 79 0 1 155 2 16 156 2 0 879 1 21 26 0 1 79 3 1 156 2 0 879 1 21 26 0 1 79 3 1 154 2 7 95 3 0 79 0 1 155 2 1 154 2 1 757 0 0 155 17 1 14 3 27 2 97 18 2 19 2 56 17 3 5 76 13 1 17 0 39 2 96 3 7 55 17 1 97 3 54 3 75 0 5 Land ME (29) bar, fir gal 25 2 7 75 0 5

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COMPOUND ADDITION.

DRY. LIME. (31)(32)(33)(34) p. gal. qts. qrs. h. a. h. m. b. *b*. 10. *d*. 11. p. 8. 1 2 $\mathbf{2}$ 713 11 57 2 15 42 41 300 2 16 1 167 211 3 $\mathbf{2}$ - 9 95 3 21 27 51 0 1 0 517 3 0 0 0 21 760 15 37 28 369 0 7 76 $\mathbf{2}$ 3 21 53 2 21 42 27 50 3 2 15 1 1 9574 6 3 3 $\mathbf{2}$ 0 1 79 1 15 982 18 47 38

(35) A, B, C, and D, were partners in the purchase of a quantity of goods : A laid out $\pounds 7$. half-a-guinea, and a crown; B, 49s. C, 54s. 6d. and D, 87d. What was the purchase? Ans. $\pounds 13..6..3$.

(36) A man lent his friend at different times these several sums, viz. $\pounds 63.-\pounds 25..15.-\pounds 32..7.-\pounds 15..14..10$. and four score and nineteen pounds, half-a-guinea, and a shilling. How much was the whole loan? Ans. $\pounds 236..8..4$.

(37) Bought goods, for which I paid $\pounds 54..17$; for packing 13s. 8d.; carriage $\pounds 1..5..4$; and expenses over making the bargain 14s. 3d. What was the whole cost? Ans. $\pounds 57..10..3$

(38) A nobleman, previous to quitting town, wished to discharge his tradesmen's bills. On inquiry he found that he owed 82 guineas for rent;—to his wine-merchant, $\pounds 72..5$; to his confectioner, $\pounds 12..13..4$;—to his draper, $\pounds 47..13..2$; to his tailor, $\pounds 110..15..6$;—to his coach-maker, $\pounds 157..8$;—to his tallow-chandler, $\pounds 8..17..9$;—to his corn-factor, $\pounds 170..6..8$; —to his brewer, $\pounds 52..17..0$;—to his butcher, $\pounds 122..11..5$; to his baker, $\pounds 37..9..5$;—and to his servants for wages, $\pounds 53..18$. What money must he draw from his banker, ineluding $\pounds 100$. that he wished to take with him?

Ans. £1032..17..3.

(39) A father was 24 years of age (allowing 13 months to a year, and 28 days to a month) at the birth of his first child • between the eldest and next born was 1 year, 11 months, and 14 days; between the second and third were 2 years, 1 month, and 15 days; between the third and fourth, 2 years, 10 months, and 25 days. When the fourth was 27 years, 9 months, and 12 days old, what age was the father ?

Ans. 58 years, 7 months, 10 days.

4

(40) A clerk having been out collecting debts, presented an account that A paid him $\pounds 7..5..2$;—B $\pounds 15..18..6\frac{1}{2}$;— C $\pounds 150..13..2\frac{1}{2}$;—D $\pounds 17..6..8$;—F 5 guineas, 2 crown pieces. 4 ha

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* Ex £. 89..1 54..1 34..1

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use of a crown; hase? ..6..3. several nd four shilling. ...8...4. packing the bar-7..10..3 d to disthat he 2..5;-3..2;---..8 ;—to 70..6..8; 1..5;--wages, ker, in-

17..3. onths to st child · ths, and month, months, ths, and

days. resented 3..6½; a pieces.

COMPOUND SUBTRACTION.

4 half-crowns and 4s. 2d.;—F paid him only twenty groats ;— G £76..15..9¹/₂;—and H £121..12..4. How much was the whole amount? Ans. £396..7..6¹/₄.

(41) A nobleman had a service of plate, which consisted of twenty dishes, weighing 203 oz. 8 dwts.; 36 plates, 408 oz. 9 dwts.; 5 dozen spoons, 112 oz. 8 dwts.; 6 salts, and 6 pepper-boxes, 71 oz. 7 dwts.; knives and forks, 73 oz. 5 dwts.; two large cups, a tankard, and a mug, 121 oz. 4 dwts.; a teaurn and lamp, 131 oz. 7 dwts.; with sundry other small articles, weighing 105 oz. 5 dwts. The weight of the whole is required. Ans. 102 lb. 2 oz. 13 dwts.

(42) A hop-merchant buys 5 bags of hops, of which the first weighed 2 cwt. 3 qrs. 13 lb.; the second, 2 cwt. 2 qrs. 11 lb.; the third, 2 cwt. 3 qrs. 5 lb.; the fourth, 2 cwt. 3 qrs. 12 lb.; the fifth, 2 cwt. 3 qrs. 15 lb. He purchased also two pockets, each pocket weighing 84 lb. I desire to know the weight of the whole. Ans. 15 cwt. 2 qrs.

COMPOUND SUBTRACTION

TEACHES to find the difference of Compound Quantities.

RULE. Subtract as in integers: but borrow (when there is occasion) as many as are equal to one of the next greater denomination: observing to carry one to the next for that which was borrowed.*

PROOF. As in Simple Subtraction.

MONEY.

(1) £. From 715 Take 476	s. 2 3	d. 71 81 81	(2) 3 2	£. 816 218	s. 3 2	d. 5 ¹ / ₂ 1 ² / ₄	(3) £. 87 79	$\begin{array}{c} s. & d. \\ 2 & 10 \\ 3 & 7\frac{1}{3} \end{array}$
			I _				I	

* EXAMPLE. Subtract £54..17..91. from £89..12..71.

5. s. d. Because 3 farthings cannot be taken from 2, say 3 **89..12..7**, from 4, 1, and 2 are 3; set down 3 and carry 1.—1 and **54..17..9**, 9 are 10, 10 from 12, 2, and 7 are 9; set down 9 and **carry 1.**—1 and 17 are 18, 18 from 20, 2, and 12 are **14**; set down 14 and cary 1 to the pounds.

38	COMPOUND SU	JBTRACTION.	['TUTOR'S	ASSIST
$\begin{array}{c} (4) \\ \pounds \ s. \ d. \\ 3 \ 15 \ 1\frac{1}{2} \\ 1 \ 14 \ 7 \end{array}$	$\begin{array}{c} (7) \\ \pounds. & s. & d. \\ 321 & 17 & 1\frac{1}{2} \\ 257 & 14 & 7 \end{array}$	$ \begin{array}{c} (10) \\ \pounds & s. \ d. \\ 527 & 3 \ 5\frac{1}{4} \\ 139 & 5 \ 7\frac{1}{2} \end{array} $	$ \begin{array}{c} (13) \\ \pounds & s. \ d. \\ 10 & 7 & 6 \\ 9 & 19 & 7 \\ \hline \end{array} $	(2 yds. 107 78
$ \begin{array}{c} (5) \\ \mathbf{\pounds}. & s. & d. \\ 25 & 2 & 5\frac{1}{4} \\ 17 & 9 & 8\frac{1}{2} \end{array} $	$\begin{array}{c} (8) \\ \pounds. s. d. \\ 59 15 3\frac{1}{4} \\ 36 17 2 \end{array}$	$\begin{array}{c} (11) \\ \pounds. s. d. \\ 300 15 0 \\ 296 15 10 \end{array}$	$\begin{array}{c} (14) \\ \pounds. & s. & d. \\ 500 & 0 & 0 \\ 499 & 19 & 11\frac{3}{4} \end{array}$	yds. 9
$\begin{array}{c} (6) \\ \pounds. \ s. \ d. \\ 37 \ 3 \ 4\frac{1}{4} \\ 25 \ 5 \ 2\frac{1}{4} \end{array}$	$\begin{array}{c} (9) \\ \pounds & s. & d. \\ 71 & 2 & 4 \\ 19 & 13 & 7\frac{3}{4} \end{array}$	$ \begin{array}{c} (12)\\ \pounds s. d.\\ 68 13 9\\ 44 19 10\frac{1}{2} \end{array} $	$\begin{array}{c} (15) \\ \pounds & s. & d. \\ 779 & 12 & 0 \\ 689 & 13 & 6 \end{array}$	3 (2) a.
Paid at	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	(17) Lent Received	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	175 59
different { times Paid in all Remains to pay	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	at several { times	$\begin{array}{rrrrr} 74 & 15 & 9 \\ 23 & 17 & 4\frac{1}{2} \\ \hline \end{array}$	*(37) <i>y</i> 7 2 -
	VEIGHTS ANI	- D MEASURES.		, (40 Davme
TROY W (18) 13. oz. dwt. gr. 52 1 7 2 39 0 15 7	$\begin{array}{c} \text{(19)}\\ \text{(b. oz. dwt. gr.}\\ 7 & 2 & 2 & 7\\ 5 & 7 & 1 & 5\\ \hline \\ \text{AVOIR DUPOI} \end{array}$		(21)	payme (41 it, 14 ceed t (42 in cas he cle he the
(22) lb. oz. da 35 10 5 29 12 7	$\begin{array}{c c} r. & (23) & cwt. \\ 5 & & 35 \end{array}$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	t. cwt. qrs. lb. 1 1 2 7 9 11 3 15	(43) • In year. † In

(41 it, 14 ceed t (42 in cas he cle he the (43

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13)

19 7

(14)

(15)

13 6

s. d. 0 0

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CIGHT.

3. 9. gr

2 1 13

qrs. lb. 2 7 3 15

21)

B 1 18

s. d. 7 6

s. d. 0 0 19 113

s. d. 12 0

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COMPOUND SUBTRACTION.

LONG 1	MEASURE.	IMPERIAL MEASUREWINE.								
(25)	(26)	(31)	(32)							
	lea. mi. fur. po.	hhd. gal. qls. pls.	tun hhd. gal.qts.							
107 2 10	147 2 6 29	47 47 2 1	42 2 37 2							
78 2 11	58 2 7 33	28 59 3 0	17 3 49 3							
CLOTH	MEASURE.	ALE AND	D BEER.							
(27)	(28)	(33)	(34)							
	E. c. qrs. n.	ar. fir. gal. hhd. gal. qts.								
71 1 2	35 2 1	37 2 1	27 27 1							
3 2 1	14 3 2	25 1 7	12 50 2							
LAND	MEASURE.	CORN AN	D COAL.							
(29)	(30)	(35)	(36)							
a. r. p.	a. r. p.	qr. b. p.	sc. ch. sa. b.							
175 1 27	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	65 2 1	3 16 1 0							
59 0 37	279 3 5	57 2 3	2 12 2 1							

TIME.

*(37) <i>yrs</i> . 79 23	ю. 2 3	<i>d</i> . 4 5	(38)	24	42	scc. 45 47	† (39)	yrs. 10 5	m. 7 8	d. 20 29
]							

(40) When an estate of £300. per annum is reduced by the payment of taxes to 12 score and £14..6. what are the taxes ? Ans. £45..14.

(41) A horse with his furniture is worth £37..5; without it, 14 guineas; how much does the price of the furniture exceed that of the horse? Ans. £7..17.

(42) A merchant commencing trade, owed \pounds 750; he had in cash, commodities, the stocks, and good debts, \pounds 12510..7; he cleared the first year by commerce \pounds 452..3..6. What was he then worth? Ans. \pounds 12212..10..6.

(43) A gentleman left $\pounds 45247$. to his two daughters, of

* In this example allow 4 weeks to a month, and 13 months to the year.

* In this, reckon 30 days to a month, and 12 months to the year.

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which the younger was to have 15 thousand, 15 hundred, and twice $\pounds 15$. What was the elder sister's fortune?

£.

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per 2

(44) A tradesman being insolvent, called all his creditors together, and found he owed to A £53.7..6;—to B £105..10, —to C £34..5..2;—to D £28..16..5;—to E £14..15..8;—to F £112..9;—and to G £143..12..9. The value of his stock was £212..6; and the amount of good book-debts was £112..8..3; besides £21..10..5. money in hand. How much would his creditors lose by taking the whole of his effects? Ans. The creditors lost £146..11..10.

(45) My agent at Seville, in Spain, renders me the following account of money received for the sale of goods sent him on commission, viz. for bees' wax £37..15..4; stockings £37..6..7; tobacco £125..11..6; linen cloth £112..14..8; tin £115..10..5. He informs me at the same time, that he has shipped, agreeably to my order, wines, value £250..15; fruit £51..12..6; figs £19..17..6; oil £19..12..4; and Spanish wool, value £115..15..6. How stands the balance of the account between us? Ans. Due to the agent £28..14..4.

(46) The great bell at Oxford, the heaviest in England, is stated to weigh 7 tons, 11 cwt. 3 qrs. 4 lbs., that of St. Paul's, in London, 5 tons, 2 cwt. 1 qr. 22 lbs., and that of Lincoln, called the *Great Tom*, 4 tons, 16 cwt. 3 qrs. 16 lbs. How much is the aggregate weight of these three bells inferior to that of the great bell at Moscow, which is 198 tons?

Ans. 180 tons, 8 cwt. 3 grs. 14 lbs.

COMPOUND MULTIPLICATION

Is the method of multiplying Compound Quantities.

RULE. Multiply the *least denomination*; reduce the product and carry to the next, as directed in Compound Addition; and the same with the rest.

When the multiplier is a composite number above 12, multiply (as before directed) by its component parts. For other numbers, multiply by the factors of the nearest composite; adding to the last product, so many times the top line as will supply the deficiency; or subtracting so many times, if there is an excess.

Ans. £28717.

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COMPOUND MULTIPLICATION.

ndred, and

£28717. creditors c105..10, 5..8;-to his stock lebts was low much effects ? .11..10. he followoods sent stockings .14..8; tin at he has ..15; íruit nish wool, le account 8..14..4. ngland, is St. Paul's, f Lincoln, bs. How inferior to s? 14 lbs.

e product tion; and

12, mul-For other *ompósite*; e as will , if there

	MON	IEY.	
• (1)	(2)	(3)	(4)
£. s. d.	£ . s. d.	£ d.	£. s. d.
$35\ 12\ 7\frac{3}{4}$	75 13 $1\frac{1}{2}$	$62 \ 5 \ 4\frac{1}{4}$	$57 \ 2 \ 4\frac{3}{4}$
2	3	4	5
$153\frac{1}{2}$			
£. s.	<i>d</i> .	£.	s. d.
(5) 57 18	$7\frac{1}{4} \times 6.$	(9) 135	13 $6\frac{3}{4} \times 10$.
(6) 81 9	$11\frac{1}{2} \times 7.$	(10) 79	16 $7\frac{1}{2} \times 11$
(7) 64 10	5 × 8.	(11) 247	$14 \ 11\frac{1}{2} \times 12.$
(8) 118 6	$4\frac{1}{4} \times 9.$		7 $5\frac{3}{4} \times 12$.
£ s. d.		<i>d</i> .	£. s. d.
(13) 0 9 6	×18.; (16) 1;	5 $3\frac{1}{2} \times 35.$	(19) 1 5 3×97.
(14) 1 2 6	$\times 26.1$ (17)		(20) 0 6 4×43.
		9 7 × 37.	· ·

(21) What is the value of 127 tb. of souchong tea, at 12s. 3d. per tb.? Ans. £77..15..9.

(22) 135 stones of soap, at 7s. 5d. per stone? Ans. \pm 50..1..3.

(23) 74 ells of diaper, at 1s. $4\frac{1}{2}d$. per ell? Ans. £5..1..9.

(24) 6 doz. pairs of gloves, at 1s. 10d. per pair? Ans. $\pounds 6..12$.

Note. When the fraction $\frac{1}{4}$, $\frac{1}{2}$, or $\frac{3}{4}$ is connected with the multiplier, take half the given price (or the price of one) for $\frac{1}{4}$, half of that for $\frac{1}{4}$, and for $\frac{3}{4}$, add them both together.§

* In this example, say twice 3 are 6, 6 farthings are $1\frac{1}{2}d$. set down $\frac{1}{2}d$. and carry 1; twice 7 are 14 and 1 are 15, 15*d*. are 1*s*. 3*d*. set down 3*d*. and carry 1; twice 12 are 24 and 1 are 25, 25*s*. are £1...5. set down 5*s*. and carry 1; twice 5 are 10 and 1 are 11, set down 1 and carry 1; twice 3 are 6 and 1 are 7, set down 7.

twice 5 are 0 and 1 are 7, se	
s. d.	\pounds . s. d.
† 9 6	‡ 1 2 6
2×9=18	8×3+2=2€
<u>19. 0</u>	9 0 0
Э	y 3
£811 0 Ans.	27 0 0
	Multiplicand×2=2 5 0
§ Example.	£29 5 0 Ans
What is the value of	s. d.
113 lbs. of tea, at 10s. 9d.	½ ×10 9
per 16.7	11
	$\mathbf{\pounds}_{5183}^{-1}$ = the value of 11.
	$\frac{1}{2} \times 5 4\frac{1}{2} = do \frac{1}{2}.$
	2 8 = do 1
	£6 6 33 Ans.
	and the off series

COMPOUND MULTIPI ICATION

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14	COMPOUND ROLLING TORING	frozon a
er ell ?		at 3s. 4 <u>1</u> d 2460 <u>3</u> .
(26) 1	$75\frac{1}{2}$ b. of hemp, at 1s. 3d. per b.?	
	Ans. £	4144] .
(27)	$19\frac{1}{2}$ yds. of muslin, at 4s. 3d. per yd. ? Ans.	£42101.
	$35\frac{1}{2}$ cwt. of raw sugar, at £4156. per c	
· · ·	Ans. £10	
(29)	1541 cwt. of raisins, at $\pounds 41710$. per cw	vt. ?
• • •	Ans. £7	
(30)	$117\frac{1}{4}$ gallons of gin, at 12s. 6d. per gallon	
()		73571.
(31)	$85\frac{3}{4}$ cwt. of logwood, at £178. per cwt.	
(/	Ans. $\pounds 1$	
(32)	17 ³ / ₄ yards of superfine scarlet cloth, at £	
yard ?	$Ans. \pm 20$	
	$37\frac{1}{2}$ lb. of hyson tea, at 12s. 4d. per lb.? Ans	
	$56\frac{3}{2}$ cwt. of molasses, at £2187. per cw	
(04) (L_{4} cwit. of molasses, at $\Sigma\Sigma$. for the L_{1}	
(35)	873 b. of Turkey coffee, at 4s. 3d. per b.	
(55)		
(26)	Ans. £18.	.1.4114.
(30).	$120\frac{3}{4}$ cwt. of hops, at £476. per cwt.?	

Ans. £528..5..71.

When the multiplier is large, multiply the given quantity (or price) by a series of *tens*, to find 10, 100, 1000 times, &c., as far as to the value of the *highest place* of the multiplier; multiply the last product by the figure in that place, and each preceding product by the figure of corresponding value; that is, the product for 100 by the *number of hundreds*, the product for 10 by the *number of tens*, and the *original quantity* by the *units' figure*, c_{yc} . The *sum* of the products thus obtained will be the *total product*.*

• EXAMPLE. Multiply £7..14..94. by 3645.

	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c} \pounds. \ s. \ d. \\ = \ 381311\frac{1}{2} = \end{array} $	times. 5
The product for 10	77 711 ×4=	= 30911 8 =	40
The product for 100	77319 2 ×6=	= 464315 0 =	60 0
The product for 1000	to the second seco	= 23218150 = $28210157 =$	and the second se

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] COMPOUND MULTIPLICATION.

at 3s. 4<u>1</u>d 4..6..0<u>3</u>.

 $\begin{array}{c} ...14..4\frac{1}{2}.\\ \pounds 4..2..10\frac{1}{2}.\\ \forall t. ?\\ 59..10. 3.\\ t. ?\\ 55..15..3.\\ ?\\ 73..5..7\frac{1}{2}.\\ ?\\ 8..12..5.\\ 1..3..6. \text{ per}\\ ...17..1\frac{1}{2}.\\ \pounds 23..2..6\\ t. ?\end{array}$

6..4..71. ? .12..111.

28..5..74.

en quantity times, &c., plier; mul-, and each value; that the product tity by the otained will

times. 5 40 600 <u>3000</u> <u>3645</u> (37) 407 ^{lb}. of gall-nuts, at 3s. $9\frac{1}{2}d$. per ^{lb}.? Ans. £77..3..2 $\frac{1}{2}$.

(38) 729 stones of beef, at 7s. $7\frac{1}{4}d$. per stone? Ans. £277..3..5 $\frac{1}{4}$.

(39) 2068 yards of lace, at 9s. $5\frac{1}{2}d$. per yard? Ans. £977..19.10.

(40) What is the produce of a toll-gate in the course of the year if the tolls amount, on an average, to 11s. $7\frac{1}{2}d$. per day? Ans. $\mathcal{L}212..3.1\frac{1}{2}$.

(41) How much money must be equally divided among 18 men, to give each $\pounds 14..6..8\frac{1}{2}$? Ans. $\pounds 258..0..9$.

(42) A privateer manued with 250 sailors captured a prize of which each man shared £125..15..6. What was the value of the prize? Ans. £31443..15.

(43) What sum did a gentleman receive as a dower with his wife, whose fortune was a cabinet with two divisions, in each division 87 drawers, and each drawer containing 21 guineas? Ans. $\pounds 3836..14$.

(44) A merchant began trade with £19118; for 5 years together he cleared £1086. a year; and the next 4 years £2715..10..6. a year; but the last 3 years he was in trade he had the misfortune to lose, upon an average, £475..4..6. a year. What was his real fortune at the end of the 12 years? Ans. £33984..8..6.

(45) In many parts of the kingdom coals are weighed in the wagon or eart upon a machine, constructed for the purpose.
If 3 of these draughts amounted together to 137 cwt. 2 qrs.
10 lb.; and the tare, or weight of the wagon, was 13 cwt.
1 qr.; how many coals had the customer in 12 such draughts? Ans. 391 cwt. 1 qr. 12 lb.

(46) A certain gentleman lays up every year $\pounds 294..12..6$. and spends daily $\pounds 1..12..6$. What is his annual income ? Ans. $\pounds 887..15$.

WEIGHTS AND MEASURES.

(47) Multiply 9 lb. 10 oz. 15 dwts. 19 gr. by 9, 11, and 12

(48) Multiply 23 tons, 9 cwt. 3 qrs. 18 lb. by 7, 8, and 9.

(49) Multiply 107 yards, 3 qrs. 2 nails, by 10, 17, and 29.

(50) Multiply 33 bar. 2 fir. 3 gal. by 11, and 12.

(51) Multiply 110 miles, 6 fur. 26 poles, by 12, 13, and 39.

(52) A lunar month contains 29 days, 12 hours, 44 min. 3 seconds nearly. What time is contained in 13 lunar months?

COMPOUND DIVISION.

TUTOR'S

COMPOUND DIVISION

TEACHES to find any required *part* of a *Compound Quantity*

RULE. Divide the greatest denomination; reduce the remainder to the next less, to which add the next; divide that, and proceed as be fore to the end.

When the divisor is above 12, the work must be done at length: an less it is a composite number, for which observe the directions in Simple Division.

PROOF by Multiplication.

MONEY.

$\begin{array}{c} \mathbf{\hat{L}} & \mathbf{\hat{s}} & \mathbf{\hat{d}} \\ \mathbf{\hat{2}} & \mathbf{\hat{2}} & \mathbf{\hat{2}} & \mathbf{\hat{2}} \\ \mathbf{\hat{2}} & \mathbf{\hat{2}} & \mathbf{\hat{2}} & \mathbf{\hat{4}} \\ \end{array}$	$\begin{array}{c} \mathbf{\pounds}. & (2) \\ \mathbf{\pounds}. & s. & d. \\ 3)37 & 7 & 7 \end{array}$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	a) s. d. 7 0
£. s. (5) 78 10 (6) 25 19 (7) 16 14 (8) 124 15	$\begin{array}{c} d. \\ 9\frac{1}{2} \div 6. \\ 7\frac{3}{4} \div 7. \\ 1\frac{1}{2} \div 8. \\ 2\frac{1}{2} \div 9. \end{array}$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	y 10. y 11.
$\begin{array}{cccccc} (13) & 66 & 6 \\ (14) & 596 & 12 \\ (15) & 564 & 4 \end{array}$	$6\frac{3}{4} \div 25.$ $7\frac{1}{4} \div 36.$ $6 \div 63.$	(17) 928 12 8 b	y 99. y 110 y 144.

(19) Divide £1407..17..7. by 243.

(20) Divide £700791 .14..4. by 1794.

(21) Divide £490981..3..74. by 31715.

(22) Divide £19743052..5..71/2. by 214723.

(23) If a man spend $\pounds 257..2..5$. in 12 months, what is that Ans. $\pounds 21..8..6\frac{1}{4} \frac{3}{12}$. per month?

(24) The clothing of 35 charity boys came to $\pm 57..3..7$. what was the expense of each boy? Ans. £1..12..812.

(25) If I gave $\pounds 37..6..4\frac{3}{4}$ for nine pieces of cloth, what was that per piece? Ans. £4..2..117.

* EXAMPLE. Divide £27..14..111. by 5.

	Say the fives in 27, 5
£. s. d.	£2. are 40s. and 14 are
$5)271411\frac{1}{2}$	5 are 50 and 4 over;
$51011\frac{3}{5}$	the fives in 59, 11 fives
	16 qrs. and 2 are 18, 1

5 times 5 are 25 and 2 over; e 54, the fives in 54, 10 times 4s. are 48d. and 11 are 59,s are 55 and 4 over; 4d. are the fives in 18, 3 times five are 15, and 3 over, or $\frac{3}{4}$.

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minutes

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TUTOR'S

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PROMISCUOUS EXAMPLES.

(26) If 20 cwt. of tobacco cost $\pounds 27..5..4\frac{1}{2}$; at what rate did 1 buy it per cwt.? Ans. $\pounds 1..7..3\frac{1}{2}$.

(27) What is the value of one hogshead of beer, when 120 nogsheads are sold for £154..17..10? Ans. £1..5..9 $\frac{3}{4}$ $\frac{16}{120}$.

(28) Bought 72 yards of cloth for £85..6. What was the price per yard? Ans. £1..3..8 $\frac{1}{4}$ $\frac{2}{4}$.

(29) Gave £275..3..4. for 18 bales of cloth. What is the price of one bale? Ans. £15..5..8 $\frac{3}{4}$ $\frac{19}{8}$.

(30) A prize of £7257..3..6. is to be equally divided among 500 sailors. What is each man's share ? Ans. £14..10..31 388

(31) A club of 25 persons joined to purchase a lottery ticket of £10. value, which was drawn a prize of £4000. What was each man's contribution, and his share of the prizemoney? Ans. Each contribution 8s. and share of prize £160.

(32) A tradesman cleared £2805. in $7\frac{1}{2}$ years. What was his yearly profit? Ans. £374.

(33) What was the weekly salary of a clerk who received $\pounds 266..18..1\frac{1}{2}$. for 90 weeks? Ans. $\pounds 2..19..3\frac{3}{4}$.

(34) If 100000 quills cost me £187..17..1. what is the price per thousand? Ans. £1..17.. $6\frac{3}{4}$ $\frac{40}{100}$.

WEIGHTS AND MEASURES.

(35) Divide 83 lb. 5 oz. 10 dwts. 17 gr. by 8, 10, and 12.

(36) Divide 29 tons, 17 cwt. 0 grs. 18 lb. by 9, 15, and 19.

(37) Divide 114 yards, 3 qrs. 2 nails, by 10, and 16.

(38) Divide 1017 miles, 6 fur. 38 poles, by 11, and 49.

(39) Divide 2019 acres, 3 roods, 29 perches, by 26.

(40) Divide 117 years, 7 months, 26 days, 11 hours, 27 minutes, by 37.

PROMISCUOUS EXAMPLES.

(1) Of three numbers, the first is 215, the second 519, and the third is equal to the other two. What is the sum of them all? Ans. 1468.

(2) The less of two sums of money is $\pounds 40$. and their difference $\pounds 14$. What is the greater sum, and the amount of both? Ans. $\pounds 54$. the greater, $\pounds 94$. the sum.

(3) What number added to ten thousand and eighty-nine,
will make the sum fifteen thousand and forty? Ans. 4951.
(4) What is the difference between six dozen dozen, and

half a dozen dozen; and what is their sum and product? Ans. Diff. 792, sum 936, product 62208.

. what is that $8..6\frac{1}{4}$ $\frac{8}{12}$. 2.57..3..7. $.12..8\frac{1}{3}\frac{2}{3}$. cloth, what $4..2..11\frac{7}{4}$.

and 2 over; 54, 10 times d 11 are 59, over; 4d. are 3 times five 45

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PROMISCUOUS EXAMPLES.

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(5) What difference is there between twice eight and fifty and twice fifty-eight, and what is their product?

Ans. 50 diff. 7656 product.

(6) The greater of two numbers is 37 times 45, and their difference is 19 times 4 : required their sum and product. Ans. 3254 sum, 264:685 product.

(7) A gentleman left his elder daughter £1:00. more than the younger, whose fortune was 11 thousand, 11 hundred, Find the portion of the elder, and the amount of and £11. Ans. Elder's portion £13611. amount £25722. both.

(8) The sum of two numbers is 360, the less is 144. What is their difference and their product?

Ans. 72 difference, 31104 product.

(9) There are 2545 bullocks to be divided among 509 men. Required the number and the value of each man's share, supposing every bullock worth $\pounds 9..14..6$.

Ans. Each man had 5 bullocks, and £48..12..6. for his share. (10) How many cubic feet are contained in a room, the length of which is 24 feet, the breadth 14 feet, and the height 11 feet ?* Ans. 3696.

(11) A gentleman's garden, containing 9625 square yards, is 35 yards broad : what is the length? Ans. 275 yards.

(12) What sum added to the 43d part of \pounds 4429. will make the total amount = £240? Ans. £137.

(13) Divide 20s. among A, B, and C, so that A may have 2s. less than B, and C 2s. more than B.

Ans. A 4s. 8d. B 6s. 8d. and C 8s. 8d. (14) In an army consisting of 187 squadrons of horse, each 157 men, and 207 battalions of foot, each 560 men, how many effective soldiers are there, supposing that in 7 hospitals there are 473 sick? Ans. 144806.

(15) A tradesman gave his daughter, as a marriage portion, a scrutoire, containing 12 drawers; in each drawer were six divisions, and in each division there were $\pounds 50$. four crown pieces, and eight half-crown pieces. How much had she to her fortune ? Ans. £3744.

(16) There are 1000 men in a regiment, of whom 50 are officers : how many privates are there to one officer? Ans. 19.

(17) What number must 7847 be multiplied by, to produce 3013248? Ans. 384.

* Multiply the three dimensions continually together.

(18) \$ quarter's apartiner

(19) remainde (20) A sum of . riotous a four ham each: h (21) *I* $\pm 12,000$ equally c (22) A public ch —to four keepers, What wa (23) I 12s. 8d.purse: v (24) \$ the quoti is the di (25) A ed 12 cu weight w quired th A

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PROMISCUOUS EXAMPLES.

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8s. 8d. orse, each how many pitals there 144806. ge portion, r were six our crown had she to $\pounds 3744.$ om 50 are ? Ans. 19. to produce ns. 384.

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(18) Suppose I pay eight guineas and half-a-crown for a quarter's rent, but am allowed 15s. for repairs; what does my apartment cost me annually, and how much in seven years?

Ans. In one year, £31..2. In seven, £217..14. (19) The quotient is 1083; the divisor 28604; and the remainder 1788; what is the dividend ? Ans. 30979920.

(20) An assessment was made on a certain hundred, for the sum of $\pounds 386...15..6$. the amount of the damage done by a riotous assemblage. Four parishes paid $\pounds 37..14..2$. each; four hamlets $\pounds 31..4..2$. each; and four townships $\pounds 18..12..6$. each: how much was deficient? Ans $\pounds 36..12..2$.

(21) An army, consisting of 20,000 men, got a booty of \pounds 12,000; what was each man's share, if the whole were equally divided among them? Ans. 12s.

(22) A gentleman left, by will, to his wife, $\pounds 4560$;—to a public charity, $\pounds 572..10$;—to four nephews, $\pounds 750..10$. each; —to four nieces, $\pounds 375..12..6$. each;—to thirty poor house-keepers, 10 guineas each;—and to his executors, 150 guineas. What was the amount of his property? Ans. $\pounds 10109..10$.

(23) My purse and money, said Dick to Harry, are worth 12s. 8d. but the money is worth seven times the value of the purse : what did the purse contain ? Ans. 11s. 1d.

(24) Supposing 20 to be the remainder of a division, 423 the quotient, and the divisor the sum of both, plus 19; what is the dividend? Ans. 195446.

(25) A merchant bought two lots of tobacco, which weighed 12 cwt. 3 qrs. 15 lb. for £114..15..6.; their difference in weight was 1 cwt. 2 qrs. 13 lb. and in price £7..15..6. Required their respective weights and value.*

Ans. Greater weight 7 cwt. 1 qr. value £61..5..6.

Less weight 5 cwt. 2 qrs. 15 lb. value £53..10.

(26) Divide 1000 crowns in such a manner among A, B.
and C, that A may receive 129 crowns more than B, and B,
178 less than C. Ans. A 360 crowns, B 231, C 409.
(27) If 103 guineas and 7s. be divided among 7 men, how

many pounds sterling is the share of each? Ans. £15..10. (28) A certain person had 25 purses, each purse containing 12 guineas, a crown, and a moidoire, how many pounds sterling had he in all? Ans. £355.

* Add the difference to the sum, and divide by 2 for the greater; abtract the difference from the sum, and divide by 2 for the less

PROPORTION.

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(29) A gentleman, in his will, left £50. to the poor, and ordered that $\frac{1}{3}$ should be given to old men, each man to have $5s.-\frac{1}{4}$ to old women, each woman to have $2s. 6d.-\frac{1}{5}$ to poor boys, each boy to have $1s.-\frac{1}{5}$ to poor girls, each girl to have 9d. and the remainder to the person who distributed it: how many of each sort were there, and what remained for the person who distributed the money?

Ans. 66 men, 100 women, 200 boys, 222 girls, £2..13..6. for the distributor.

(30) A gentleman sent a tankard to his goldsmith, that weighed 50 oz. 8 dwts. to be made into spoons, each weighing 2 oz. 16 dwts. how many would he have? Ans. 18.

(31) A gentleman has sent to a silversmith 137 oz. 6 dwts 9 gr. of silver to be made into tankards of 17 oz. 15 dwts. 10 gr each; spoons, of 21 oz. 11 dwts. 13 gr. per dozen; salts, of 3 oz. 10 dwts. each; and forks, of 21 oz. 11 dwts. 13 gr. per dozen; and for every tankard to have one salt, a dozen spoons and a dozen forks: what number of each will he have?

Ans. Two of each sort, 8 oz. 9 dwts. 9 gr. over.

(32) How many parcels of sugar of 16 lb. 2 oz. each are there in 16 cwt. 1 qr. 15 lb.?

Ans. 113 parcels, and 12 lb. 14 oz. over.

(33) In an arc of 7 signs, 14° 3' 53", how many seconds ? Ans. 806633".

(34) How many *lbs.* of *lead* would counterpoise a mass of *bullion* weighing 100 *lbs.* Troy ?* Ans. 82 *lb.* 4 oz. $9\frac{25}{175}$ dr.

(35) If an apothecary mixes together 1 *lb*. avoirdupois of white wax, 4 *lbs*. of spermaceti, and 12 *lbs*. of olive oil, how many ounces, apothecaries' weight, will the mass of ointment weigh, and how many masses of 3 drams each will it contain?

Ans. The whole 247 oz. $7_{\frac{64}{192}}$ dr. and 661 of 3 dr. each.

PROPORTION.

PROPORTION is either DIRECT, OF INVERSE. It is commonly called the RULE OF THREE; there being always three numbers or terms given, two of which are terms of supposition; and the other is the term of demand : because it requires a fourth

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^{*} Bullion is the term denoting gold or silver in the mass. Lead is weighed by Avoirdupois weight. See the Table of COMPARISON OF WEIGHTS.

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poor, and n to have $\frac{1}{2}$ to poor cl to have l it: how d for the

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term to be found, in the same proportion to itself, as that which is between the other two.

GENERAL RULE FOR STATING THE QUESTION. Put the term of demand in the third place: that term of supposition which is of the same kind as the demand, the first; and the other, which is of the same kind as the required term, the second.*

Also, the terms being thus arranged, reduce the first and third (if necessary) into one name, and the second into the lowest denomination mentioned.

THE RULE OF THREE DIRECT

REQUIRES the fourth term to be greater than the second, when the third is greater than the first; or the fourth to be less than the second, when the third is less than the first.

RULE. Multiply the second and third together, and divide their product by the first: the quotient will be the answer, in the same denomination as the second.[†]

The following methods of contracting the operations in the RULE OF THREE are highly important, and should never be lost sight of:—

1. Let the first and third terms be reduced no lower than is necessary to make them of the same denomination.

2. Let the *dividing term* and *either* (but not *both*) of *the other* terms be divided by any number that will divide them *exactly*; and use the quotients instead of the original numbers.

3. When it is conveniently practicable, work by Compound Multiplication and Division, instead of reducing the terms.

* Some modern authors prefer placing the *term of demand* the *second*, and that *similar* to the *required term* the *third*. This arrangement will answer the purpose equally well, observing that those of *like kind* must be reduced (if necessary) to the *same name*.

† The following GENERAL RULE comprehends both the cases of DIRECT and INVERSE PROPORTION under one head; which is considered by many scientific men of the present day as a more systematic arrangement.

RULE. The question being stated, and the terms prepared, consider, from the nature of the case, whether the required term is to be greater or less than the second, or term of similar kind: if greater, multiply that similar to the answer by the greater of the other two, and divide the product by the less; if less, multiply it by the less and divide the product by the greater. In either case the quotient will be the term required, in the same denomination as the similar term.

NOTE. It is evident that the above Rule will answer generally, whether the term of demand is put in the second or third place.

ER DIRECT. [TUTOR'S

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(1) If one lb. of sugar cost 4¹/₂d. what will 54 lb. cost ?*
(2) If a gallon of beer cost 10d. what is that per barrel? Ans. £1..10.

(3) If a pair of shoes cost 4s. 6d. what is the value of 12 dozen pairs?[†]

(4) If one yard of cloth cost 15s. 6d. what will 32 yards cost at the same rate? Ans. $\pounds 24..16$.

(5) If 32 yards of cloth cost $\pounds 24..16$. what is the value of one yard? Ans. 15s. 6d.

(6) If I gave $\pounds 4..18$. for 1 cwt. of sugar, at what rate did I buy it per lb? Ans. $10\frac{1}{2}d$.

(7) Bought 20 pieces of cloth, each piece 20 ells, for 12s 6d. per ell, what is the value of the whole ? Ans. £250.

(8) What will 25 cwt. 3 qrs. 14 lb. of tobacco come to, at $15\frac{1}{2}d$. per lb.? Ans. £187..3..3.

(9) Bought 27¹/₄ yards of muslin, at 6s. $9\frac{1}{2}d$. per yard, what is the amount of the whole? Ans. £9..5..0³/₄.

(10) Bought 17 cwt. 1 qr. 14 lb. of iron, at $3\frac{1}{4}d$. per lb what was the price of the whole? Ans. £26..7..0 $\frac{1}{2}$.

(11) If coffee is sold for $5\frac{1}{2}d$. per ounce, what will be the price of 2 cwt.? Ans. £82..2..8.

(12) How many yards of cloth may be bought for $\pounds 21$. 11..1 $\frac{1}{2}$. when $3\frac{1}{2}$ yards cost $\pounds 2..14..3$.?

Ans. 27 yards, 3 qrs. 1,1 nail.

(13) If 1 cwt. of Cheshire cheese cost £1..14..8. what must I give for $3\frac{1}{2}$ lb.? Ans. 1s. 1d.

(14) Bought 1 cwt. 24 lb. 8 oz. of old lead, at 9s. per cwt. what did the lead cost? Ans. 10s. $11\frac{1}{2}\frac{1}{224}d$.

(15) If a gentleman's income be $\pounds 500$. a year, and he spend 19s. 4d. per day, what is his annual saving? Ans. $\pounds 147..3..4$.

(16) If 14 yards of cloth cost 10 guineas, how many Flemish ells can I buy for £283..17..6.? Ans. 504 Fl. ells, 2 grs.

(17) If 504 Flemish ells, 2 quarters, cost $\pounds 283..17..6$. what is the cost of 14 yards? Ans. $\pounds 10..10$.

1b. d. 1b.	pr. s. d. grs.
As 1:41::54	pr. s. d. prs. • As 1 : 46 : : 144
4 18	12
18 4)972 grs.	2140
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32 yards 24..16. e value of 5s. 6d. t rate did $10\frac{1}{2}d.$ s, for 12*s* £250. ome to, at 37..3..3. yard, what $5..0\frac{3}{4}\frac{1}{2}$. d. per lb 5..7..01. vill be the 32..2..8. for $\pounds 21$.

 $\frac{1}{31}$ nail. what must 1s. 1d. s. per cwt. $\frac{1}{2}$ $\frac{1}{22}$ $\frac{2}{4}$ d. d he spend 2147..3..4.any Flemells, 2 qrs. 7..6. what 210..10.

d. prs. .6 : : 144 .2 .0 .2 .0 .0 .0 .0 .0 .0 ASSISTANT.

RULE OF THREE DIRECT.

(18) At the rate of $\pounds 1..1..8$. for 3 *lb*. of gum acacia, what must be given for 29 *lb*. 4 oz.? Ans. 10..11..3.

(19) If 1 English ell, 2 quarters, cost 4s. 7d. what will $39\frac{1}{2}$ yards cost at the same rate? Ans. $\pounds 5.. \pounds .. 5\frac{1}{4} \frac{5}{4}$.

(20) If 27 yards of Holland cost $\pounds 5..12..6$. how many E. glisl clls can I buy for $\pounds 100.$? Ans. 384 ells.

(21) If 7 yards of cloth cost 17s. 8d. what is the value of 5 pieces, each containing $27\frac{1}{2}$ yards? Ans. 17.7.01 1.

(22) A draper bought 420 yards of broadcloth, at the rate of 14s. $10\frac{3}{4}d$. per ell English: what was the amount of the purchase money? Ans. £250..5.

(23) A grocer bought 4 hogsheads of sugar, each hogshead weighing neat 6 cwt. 2 qrs. 14 lb. at $\pounds 2..8..6$. per cwt. what is the value ? Ans. $\pounds 64..5..3$.

(24) A draper bought 8 packs of cloth, each pack containing 4 parcels, each parcel 10 pieces, and each piece 26 yards; at the rate of $\pounds 4..16$. for 6 yards: what was the purchase money? Ans. $\pounds 6656$.

(25) If 24 *lb*. of raisins cost 6s. 6d. what will 18 frails cost, and frail weighing neat 3 qrs. 18 *lb*.? Ans. \pounds 24..17..3.

(26) When the price of silver is 5s. per ounce, what is the value of 14 ingots, each ingot weighing 7 lb. 5 oz. 10 dwts.? Ans. £313..5.

(27) What is the value of a pack of wool, weighing 2 cwt. 1 qr. 19 lb. at 17s. per tod of 28 lb.?

Ans. $\pounds 8..4..6\frac{1}{4}$

(28) Bought 171 tons of lead, at $\pounds 14$. per ton; paid carriage and other incidental charges, $\pounds 4..10$. Required the whole cost, and the cost per lb.

Ans. £2398..10. the whole cost, and the cost per lb. $1\frac{1}{2}d$. $\frac{4}{3}\frac{3}{8}\frac{3}{3}\frac{7}{07}$. (29) If a pair of stockings cost 10 groats, how many dozen pairs can I buy for £43..5.? Ans. 21 doz. $7\frac{1}{2}$ pairs.

(30) Bought 27 doz. 5 lb. of candles, at the rate of 5s. 9d a dozen: what did they cost? Ans. $\pounds 7..17..7$?

(31) A factor bought 86 pieces of stuff, which cost him $\pounds 517..17..10$. at 4s. 10d. per yard. How many yards were there in the whole, and how many English ells in a piece?

Ans. 2143 yards; and 19 ells. 4 qrs. $2\frac{6}{8}\frac{6}{6}$ nails, in a piece.

(32) A gentleman has an annuity of £896..17. What may he spend daily, that at the year's end he may lay up 200 guineas, after giving to the poor quarterly 10 moidores?

Ans. £1..14..8 44.

RULE OF THREE INVERSE.

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THE RULE OF THREE INVERSE

REQUIRES the *fourth* term to be *less* than the *second*, when the *third* is *greater* than the *first*; or the *fourth* to be *greater* than the *second*, when the *third* is *less* than the *first*.

RULE. Multiply the first and second together, and divide their product by the third: the quotient will be the answer, as before.

(1) If 8 men can do a piece of work in 12 days, in how many days can 16 men do the same?*

(2) If 54 men can build a house in 90 days, how many men can do the same in 50 days? Ans. $97\frac{1}{5}$ men.

(3) If, when a peck of wheat is sold for 2s, the penny loaf weighs 8 oz.; how much must it weigh when the peck is worth but 1s. 6d? Ans. $10\frac{2}{3}$ oz.

(4) How many sovereigns, of 20s. each, are equivalent to 240 pieces, value 12s. each? Ans. 144.

(5) How many yards of stuff three quarters wide, are equal in measure to 30 yards of 5 quarters wide? Ans. 50 yds.

(6) If I lend a friend $\pounds 200$. for 12 months, how long ought he to lend me $\pounds 150$.? Ans. 16 months.

(7) If for 24s. I have 1200 *lb*. carried 36 miles, what weight can I have carried 24 miles for the same money ?

Ans. 1800 lb.

(8) If I have a right to keep 45 sheep on a common 20 weeks, how long may I keep 50 upon it? Ans. 18 weeks.

(9) A besieged town has a garrison of 1000 soldiers, with provisions for only 3 months. How many must be sent away, that the provisions may last 5 months? Ans. 400.

(10) If £20. worth of wine be sufficient to serve an ordinary of 100 men, when the price is £30. per tun; how many will £20. worth suffice, when the price is only £24. per tun? Ans. 125 men.

(11) A courier makes a journey in 24 days, by travelling 12 hours a day: how many days will he be in going the same journey, travelling 16 hours a day? Ans. 18 days.

(12) How much will line a cloak, which is made of 4 yards of plush, 7 quarters wide, the stuff for the lining being but 3 quarters wide? Ans. $9\frac{1}{3}$ yards.

* As 8: 12:: 16: $\frac{m}{16}$ = 6 days. Ans.

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DIRECT AND INVERSE PROPORTION PROMISCUOUSLY ARRANGED.

(1) If 14 yards of broadcloth cost $\pounds 9..12$. what is the purchase of 75 yards? Ans. $\pounds 51..8..6\frac{3}{4}$.

(2) If 14 pioneers make a trench in 18 days, in how many days would 34 men make a similar trench; working, in both cases, 12 hours a day? Ans. 7 days, 4 hours, $56\frac{9}{17}$ minutes.

(3) How much must I lend to a friend for 12 months, to requite his kindness in having lent me $\pounds 64$. for 8 months? Ans. $\pounds 42..13..4$.

(4) Bought 59 cwt. 2 qrs. 21 lb. of tobacco, at $\pounds 2...17..4$ per cwt. what does it come to? Ans. $\pounds 171..2..1$.

(5) A woollen draper purchased 147 yards of broadcloth, at 14s. 6d. per yard. Suppose that he sold it in pieces for coats, each $1\frac{3}{4}$ yard, how much must he charge for each, so as to gain £16..10..9. by the whole? Ans. £1..9..3 $\frac{3}{4}$.

(6) If $\pounds 100$. gain $\pounds 4..10$. interest in 12 months, what sum will gain the same in 18 months? Ans. $\pounds 66..13..4$.

(7) A draper having sold 147 yards of cloth, at the rate of $\pounds 1..9..3\frac{3}{4}$. for $1\frac{3}{4}$ yard, found that he had gained $\pounds 16..10..9$. What did the whole cost him, and how much per yard?

Ans. The whole £106..11..6. and 14s. 6d. per yard.

(8) If £100. in 12 months gain £4..10. interest, in what time will £66..13..4 gain the same interest? Ans. 18 months (9) If a draper bought 147 yards of cloth, at 14s. 6d. per yard, and sold it in pieces for coats, each $1\frac{3}{4}$ yard, for £1..9..3 $\frac{3}{4}$.; how much would he gain per yard, and by the whole? Ans. 2s. 3d. per yard, £16..10..9. by the whole.

(10) If 1 cwt. cost £12..12..6. what must be given for 14 cwt. 1 qr. 19 lb.? Ans. £182..0..11 $\frac{1}{2}$ $\frac{8}{112}$.

(11) If £100. gain £4.10. in 12 months, what interest will £375. gain in the same time? Ans. £16..17..6.

(12) A regiment of soldiers, consisting of 1000 men, are to have new coats, each to be made of $2\frac{1}{2}$ yards of cloth, 5 quarters wide, and to be lined with shalloon of 3 quarters wide. How many yards of shalloon will line them?

Ans. 4166 yards, 2 qrs. $2\frac{2}{3}$ nails.

THE DOUBLE RULE OF THREE

HAS five terms given, three of supposition and two of demand, to find a *sixth*, in the same proportion with the terms of demand, as that of the terms of supposition. It comprises two

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operations of the SING E RULE.—But it may comprise 'hree four, or more operations of the Single Rule; as there may be seven terms given to find an *eighth*, or *nine* to find a *tenth*, &c. In this respect it is unlimited; and is therefore more properly called COMPOUND PROPORTION.

SRULE 1. Put the terms of demand one under another in the third place; the terms of supposition in the same order in the first place; except that which is of the same nature as the required term, which must be in the second place.

Examine the statings separately, using the middle term in each, to know if the proportion is *direct* or *inverse*. When direct, mark the *first* term with an asterisk: when inverse, mark the *third* term.

Find the product of the marked terms for a Divisor, and the product of all the rest for a Dividend: divide, and the quotient will be the answer.*

RULE 2. (1) Of the conditional terms, put the principal cause of action, gain or loss, &c., in the *first* place. (2) Put that which denotes time or distance, &c., in the *second*, and the other in the *third*. (3) Put the terms of demand under the *like* terms of supposition. (4) If the blank falls in the *third* place, multiply the first and second terms for a divisor, and the other three for a dividend. (5) But if the blank is in the *first* or *second* place, divide the product of the rest by the product of the third and fourth terms, for the answer.

Note. It will save much labour to write the terms of the Dividend over, and those of the Divisor under a line, like those of a compound fraction, and to cancel them accordingly. See Reduction of Vulgar Fractions, Case 6.

PROOF. By two operations of the Single Rule of Three. (1) If 14 horses eat 56 bushels of oats in 16 days, how many bushels will serve 20 horses 24 days?

* See also Supplemental Que	
$ \begin{array}{c} \dagger \text{ By Rule 1.} \\ h. \\ \mathbf{As} \ast 14 \\ d. \\ \ast 16 \end{array} \begin{array}{c} b. \\ 56 \\ \vdots \\ 56 \\ \vdots \end{array} \begin{array}{c} h. \\ 20 \\ d. \\ 24 \end{array} \begin{array}{c} \vdots \\ 56 \\ \vdots \\ 4 \end{array} $	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
By Rule 2. 7 h. d. b. 8 10 12 14:16:56 $\neq, 20 \times 24 = 120$ 20:24: $-20 \times 24 = 120$ $22 \times 24 = 22$	By two single statings h. b. h. b. (1) As 14:56:20:80 d. b. d. b. (2) As 16:80:24:120

(2)many (3)will £ (4) will g (5) will £ (6)150 n 7 cut. (7)many (8)pay 3 (9) sume soldie (10 days, days (1)what same (1)many

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PRACTICE.

(2) If 8 men in 14 days can mow 112 acres of grass, how many men can mow 2000 acres in ten days? Ans. 200 men

(3) If $\pounds 100$. in 12 months gain $\pounds 6$. interest, how much will $\pounds 75$. gain in 9 months? (4) If $\pounds 100$ is 10 months? (5) $\pounds 100$ is 10 months?

(4) If $\pounds 100$. in 12 months gain $\pounds 6$. interest, what principal will gain $\pounds 3..7..6$. in 9 months? Ans. $\pounds 75$.

(5) If $\pounds 100$. gain $\pounds 6$. interest in 12 months, in what time will $\pounds 75$. gain $\pounds 3..7..6$. interest ? Ans. 9 months.

(6) If a carrier charges $\pounds 2..2$, for the carriage of 3 *cwt*. 150 miles, ? 7. a ought he to charge for the carriage of 7 *cwt*. 3 *qrs*. 14 *lb*. 3 miles ? Ans. $\pounds 1..16..9$.

(7) If 40 acres of grass be mown by 8 men in 7 days, how many acres can be mown by 24 men in 28 days? Ans. 480.

(8) If $\pounds 2$. will pay 8 men for 5 days' work, how much will pay 32 men for 24 days' work? Ans. $\pounds 38..8$.

(9) If a regiment of soldiers, consisting of 1360 men, consume 351 quarters of wheat in 108 days, how much will 11232 soldiers consume in 56 days? Ans. $1503_{\frac{9}{55}}$, qrs.

(10) If 939 horses consume 351 quarters of oats in 168 days, how many horses will consume 1404 quarters in 56 days? Ans. 11268.

(11) If I pay £14..10. for the carriage of 60 cwt. 20 miles, what weight can I have carried 30 miles for £5..8..9. at the same rate? Ans. 15 cwt.

(12) If 144 threepenny loaves serve 18 men for 6 days, how many fourpenny loaves will serve 21 men for 9 days?

Ans. 189.

1.4

PRACTICE

Is so called from its general use among merchants and tradesmen.

It is a concise method of computing the value of articles, &c., by taking *aliquot parts*.

The GENERAL RULE is to suppose the price one pound, one shilling, or one penny each. Then will the given number of articles, considered accordingly as pounds, or shillings, or pence, be the supposed value of the whole; out of which the aliquot part or parts are to be taken for the real price

NOTE. An aliquot part of a number is such a part as being taken a certain number of times will produce the number exactly: thus, 4 is an aliquot part of 12; because 3 fours are 12.

PRACTICE.

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	ALIQUO'	r Parts.	
Of a pound. s. d. £. 10 0 are $\frac{1}{2}$ 6 8 $\frac{1}{3}$ 5 0 $\frac{1}{4}$ 4 0 $\frac{1}{5}$ 3 4 $\frac{1}{6}$ 2 6 $\frac{1}{3}$ 2 6 $\frac{1}{12}$ 1 8 $\frac{1}{12}$ 1 8 $\frac{1}{12}$ 1 8 $\frac{1}{12}$ 1 8 $\frac{1}{12}$ 1 9 $\frac{1}{16}$ 1 0 $\frac{1}{20}$ 0 8 $\frac{3}{10}$ 0 6 $\frac{1}{40}$ 0 6 $\frac{1}{40}$ 0 6 $\frac{1}{40}$ 3 $\frac{1}{40}$ $\frac{1}{3}$ 1 $\frac{1}{2}$ $\frac{1}{6}$ 1 $\frac{1}{12}$ $\frac{1}{12}$	Of a penny. 2 qrs. are $\frac{1}{2}d$. 1 qr. is $\frac{1}{4}d$. 1 qr. is $\frac{1}{4}d$. Of a ton. cwt. ton. 10 are $\frac{1}{2}$ 5 $\frac{1}{4}$ 4 $\frac{1}{3}$ 2 3 qr 12 lb $\frac{1}{1}$ 2 $\frac{1}{2}$ 1 is $\frac{10}{20}$ Of a cwt. qr. lb. cwt. qr. cwt. $\frac{1}{4}$ 1, or 28 $\frac{1}{4}$ 16 $\frac{1}{14}$ 14 $\frac{1}{8}$ 8 $\frac{1}{14}$ 7 $\frac{1}{16}$	Of a quarter. $0f$ <	Of an oz. Troy. The same as the parts of a £. changing the names from shillings to dwts. Of a dwt. gr. dwt. 12 are $\frac{1}{2}$ 6 $\frac{1}{2}$ 4 $\frac{1}{2}$ 1 $\frac{1}{2}$ $\frac{1}{12}$ 1 $\frac{1}{2}$ $\frac{1}{12}$ 1 $\frac{1}{2}$ $\frac{1}{12}$

RULE 1. When the price is less than a penny, call the given num ber *pence*, and take the *aliquot parts* that are in a penny; then divido by 12 and 20, to reduce the answer to pounds.

(1) $\frac{1}{4}$ is $\frac{1}{4}$ 5704 <i>lb</i> . at $\frac{1}{4}$	(2) 7695 at $\frac{1}{2}d$.	(4) 6547 at $\frac{3}{4}d$.
12)1426	Ans. £1607 $\frac{1}{2}$.	Ans. £2092 $\frac{1}{4}$.
$\frac{2 \overline{0})11 810}{Ans. \pm 51810}$	(3) 5470 at $\frac{1}{2}d$. Ans. £11711.	(5) 4573 at $\frac{3}{4}d$. Ans. £1459 $\frac{3}{4}$.

RULE 2. When the price is less than a shilling, call the given number shillings, take the aliquot part or parts that are in a shilling, add the quotients together, and divide by 20, as in the preceding rule.

$\begin{array}{c c} \textbf{(1) 7547 at 1d.} \\ \textbf{Ans. £31811.} \\ \hline \textbf{Ans. £} \end{array}$	at $1\frac{1}{4}d$. [(3) 54325 at $1\frac{1}{4}d$. 19108 $\frac{3}{4}$.] Ans. £339107 $\frac{1}{4}$
• 1d. = $\frac{1}{12}$ 7547s. 2[0]62[811] Ans. £31811.	$ \begin{array}{c} \dagger \ 1d. = \frac{1}{12} \ \frac{3751s.}{3127} \\ \frac{1}{4} = \frac{1}{4} \ \frac{3127}{781\frac{3}{4}} \\ 2 \overline{0)39 08\frac{3}{4}} \\ \underline{\pounds 19108\frac{3}{4}} \\ \end{array} $

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(4) 6254 at $1\frac{3}{4}d$.	(18) 2715 at $5\frac{1}{4}d$.	(32) 9872 at 8 ³ 4.
Ans. £45120 $\frac{1}{2}$.	Ans. £5979 $\frac{3}{4}$.	Ans. £359184
(5) 2351 at 2d.	(19) 3120 at $5\frac{1}{2}d$.	(33) 5272 at 9d.
Ans. £191110.	Ans. £7110.	Ans. £19714
(6) 7210 at $2\frac{1}{4}d$.	(20) 7521 at $5\frac{3}{4}d$.	$(34) 6325$ at $9\frac{1}{4}d$.
Àns. £671110 $\frac{1}{2}$.	Ans. £18039 $\frac{3}{4}$.	Ans. £2431561.
(7) 2.710 at $2\frac{1}{2}d$.	(21) 3271 at 6d.	(35) 7924 at $9\frac{1}{2}d$.
Ans. £2847.	Ans. £81156.	Áns. £313132.
(8) 3250 at $2\frac{3}{4}d$.	(22) 7914 at $6\frac{1}{4}d$.	(36) 2150 at $9\frac{3}{4}d$.
Ans. $\pm 3749\frac{1}{2}$.	Ans. $\pounds 206110\frac{1}{2}$.	Ans. £87610 $\frac{1}{2}$
(9) 2715 at 3d.	(23) 3250 at $6\frac{1}{2}d$.	(37) 6325 at 10d.
Ans. £33189.	Ans. £8805.	Ans. £2631010
(10) 7062 at $3\frac{1}{4}d$.	(24) 2708 at $6\frac{3}{4}d$.	(38) 5724 at $10\frac{1}{4}d$.
Ans. $\pm 95127\frac{1}{2}$.	Ans. £7633.	Ans. £24493
(11) 2147 at $3\frac{1}{2}d$.	(25) 3271 at 7d.	(39) 6327 at $10\frac{1}{4}d$.
Ans. $\pounds 3162\frac{1}{2}$.	Ans. £9581.	Ans. $\pounds 27043\frac{3}{4}$.
(12) 7000 at $3\frac{3}{4}d$.	(26) 3254 at $7\frac{1}{4}d$.	(40) 3254 at $10\frac{1}{2}d$.
Ans. £10976.	Ans. £98511 $\frac{1}{2}$.	Ans. £14273.
(13) 3257 at 4d.	(27) 2701 at $7\frac{1}{2}d$.	(41) 7291 at $10\frac{3}{4}d$.
Ans. £5458.	Ans. $\pounds 8481\frac{1}{2}$.	Ans. $\pounds 326116\frac{1}{4}$.
(14) 2056 at $4\frac{1}{4}d$.	(28) 3714 at $7\frac{3}{4}d$.	(42) 3256 at 11d.
Ans. £3682.	Ans. £119187 $\frac{1}{2}$.	Ans. £14948.
(15) 3752 at $4\frac{1}{2}d$.	(29) 2710 at 8d.	(43) 7254 at $11\frac{1}{4}d$.
Ans. £7070.	Ans. £9068.	Ans. £34007 $\frac{1}{2}$.
(16) 2107 at $4\frac{3}{4}d$.	(30) 3514 at $8\frac{1}{4}d$.	(44) 3754 at $11\frac{1}{2}d$.
Ans. $\pounds 41140\frac{1}{4}$.	Ans. $\pounds 1201510\frac{1}{2}$.	Ans. £179177.
(17) 3210 at 5d.	(31) 2759 at $8\frac{1}{2}d$.	(45) 7972 at $11\frac{3}{4}d$.
Ans. £66176.	Ans. $\pm 97143\frac{1}{2}$.	Ans. £390511.

RULE 3. When the price is more than one shilling, and less than two, take the part or parts for the excess above a shilling, add the quotients is the given quantity, and reduce the whole to pounds as before. Or, when convenient, take the aliquot part of a pound.

*(1) 2106 at $12\frac{1}{4}d$. (2) 3715 at $12\frac{1}{2}d$. (3) 2712 at $12\frac{3}{4}d$. Ans. £107..9..10 $\frac{1}{2}$. Ans. £193..9..9 $\frac{1}{2}$. (3) Ans. £144..1..6

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• d. $\frac{1}{4} = \begin{cases} \frac{1}{12} & \frac{2106s.}{(175..6)} \\ \frac{1}{4} & \frac{1}{(175..6)} \\ \frac{1}{2} & \frac{210}{214|9..10\frac{1}{2}} \\ 2|0) & \frac{214|9..10\frac{1}{2}}{214|9..10\frac{1}{2}} \end{cases}$ Ans. £107..9..10¹/₂.

This example is worked by taking $\frac{1}{12}$, and then $\frac{1}{4}$ of that; because a farthing is $\frac{1}{18}$ of a shilling; which is $=\frac{1}{12}$ of $\frac{1}{4}$, or $\frac{1}{4}$ of $\frac{1}{12}$, because 4 *twelves* are 48.

PRACTICE.

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(4) 2107 at 1s. 1d.	(19) 2750 at 1s. $4\frac{3}{4}d$.	$(34) 7104 \text{ at } 1s. 8\frac{1}{2}d.$ Ans. £60616.
Ans. £11427.	Ans. £19118 $6\frac{1}{2}$.	Ans. £60616.
(5) 3215 at $1s$. $1\frac{1}{4}d$.	(20) 3725 at 1s. 5d.	(35) 1004 at 1s. $8\frac{3}{4}d$.
$Ans. \pm 177910_4^3$.	Áns. £263171.	Ans. £86161.
		(36) 2104 at 1s. 9d.
	Ans. $\pounds 521110\frac{1}{2}$.	
(7) 7904 at 1s. $1\frac{3}{4}d$.	(22) 2597 at 1s. $5\frac{1}{2}d$.	(37) 2571 at 1s $9\frac{1}{4}d$.
		Ans. $\pounds 227129\frac{3}{4}$.
(8) 3750 at 1s. 2d.	(23) 7210 at 1s. $5\frac{3}{4}d$.	(38) 2104 at 1s. $9\frac{1}{2}d$.
Ans. £21815.	Ans. $\pounds 53349\frac{1}{2}$.	Ans. £18898.
(9) 3291 at 1s. $2\frac{1}{4}d$.	(24) 7524 at 1s. 6d.	(39) 7506 at 1s. $9\frac{3}{4}d$.
Ans. £1958 $0\frac{3}{4}$.	Ans. £5646.	Ans. £68047 $\frac{1}{2}$.
(10) 9254 at 1s. $2\frac{1}{2}d$.	(25) 7103 at 1s. $6\frac{1}{4}d$.	(40) 1071 at 1s. 10d
Ans. £559111.	Ans. $\pounds 54025\frac{3}{4}$.	Ans. £9836.
(11) 7250 at 1s. $2\frac{3}{4}d$.	(26) 3254 at 1s. $6\frac{1}{2}d$.	(41) 5200 at $1s. 10\frac{1}{4}d$.
Ans. £445115 $\frac{1}{2}$.	Ans. £250167.	Ans. £48218.
(12) 7591 at 1s. 3d.	(27) 7925 at 1s. $6\frac{3}{4}d$.	$(42)2117$ at 1s. $10\frac{1}{2}d$
Ans. £47489.	Ans. $\pounds 61929\frac{3}{4}$.	Ans. £19894 $\frac{1}{2}$
	(28) 9271 at 1s. 7d.	
	Ans. £733191.	
(14) 5271 at 1s. $3\frac{1}{2}d$.	(29) 7210 at 1s. $7\frac{1}{4}d$.	(44) 5000 at 1s. 11d
Ans. £34084 $\frac{1}{2}$	Ans. £57860 $\frac{1}{2}$.	Ans. £47934
(15) 3254 at 1s. $3\frac{3}{4}d$.	(30) 2310 at 1s. $7\frac{1}{2}d$.	$(45)2105$ at $1s. 11\frac{1}{4}d$
Ans. $\pounds 2131010\frac{1}{2}$.	Ans. £187139.	Ans. £2031851
(16) 2915 at 1s. 4d.	(31) 2504 at 1s. $7\frac{3}{4}d$.	$(46)1006$ at $1s.11\frac{1}{2}d$
Ans. £19468.	Ans. £20612.	Ans. £98101
(17) 3270 at 1s. $4\frac{1}{4}d$.	(32) 7152 at 1s. 8d.	$(47)2705$ at 1s. $11\frac{3}{4}d$
Ans. $\pounds 22181\frac{1}{2}$.	Ans. £596.	Ans. £267137 $\frac{3}{4}$
(18) 7059 at 1s. $4\frac{1}{2}d$.	(33) 2905 at 1s. $8\frac{1}{4}d$.	$(48)5000$ at $1s.11\frac{1}{2}d$
Ans. £48561 $\frac{1}{2}$.	$\begin{array}{c} \textbf{(33) 2905 at 1s. 8\frac{1}{4}d.} \\ Ans. \ \pounds 24522\frac{1}{4}. \end{array}$	Ans. £489118

RULE 4. When the price is an *even* number of shillings, the given quantity may be multiplied by *half* that number, doubles the units figure of the product for shillings, and the rest of the product will be pounds. Or take the aliquot part of a pound.

(1) 2750 at 2s.	(4) 1572 at 8s.	(7) 5271 at $14s$.
	Ans £62816.	
(2) 3254 at 4s.	(5) 2102 at 10s.	(8) 3123 at 16s.
Ans. £65016.	Ans. £1051.	Ans. £24988
(3) 2710 at 6s.	(6) 2101 at 12s.	(9) 1075 at 16s.
Ans. £813.	(6) 2101 at 12s. Ans. \pounds 26012.	Ans. £860

UTOR'S

1s. 8¹/₃d. 606..16. 1s. 83d. **5..16..1.** 1s. 9d. £184..2 $1s. 9 \frac{1}{2}d.$..12...93. $1s. 9\frac{1}{3}d.$ 88..9..8. 1s. 93d. $0..4..7\frac{1}{2}$. 1s. 10d 98..3..6. $s. 10\frac{1}{4}d.$ 82..1..8. $18.10\frac{1}{6}d$ $8..9..4\frac{1}{2}$ $s.10\frac{3}{4}d$ 5..9..11s. 11d79..3..4 $|s.11\frac{1}{4}d$ $..18..5\frac{1}{4}$ s. 113d 8..10..1 $s. 11\frac{3}{4}d$ $..13..7\frac{3}{4}$ $s.11\frac{1}{2}d$ 9..11..8

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14*s*. 689..14. 16*s*. 2498..8 16*s*. . £860 ASSISTANT.]

PRACTICE.

(10) 1621 at 18s. Ans. £1458.18. NOTE. At 2s. take the *tenth*, and at 10s. take the *half* of so many £.

RULE. 5. When the price is an *odd* number of shillings, work by Rule 4th for the *greatest even* number, and add $\frac{1}{20}$ of the given quantity for the odd shilling.—Or, take such parts of a pound as will make the given price.

*(1) 3270 at 3s.	(4) 3214 at 9s.	(7) 2150 at 15s
Ans. £49010.	Ans. £14466.	Ans. £161210.
(2) 3271 at 5s.	(5) 2710 at 11s.	(8) 3142 at 17s.
Ans. £81715.	Ans. £149010.	Ans. £267014.
(3) 2715 at 7s.	(6) 3179 at 13s.	(9) 2150 at 19s.
Ans. £9505.	Ans. £20667.	Ans. £204210.

RULE 6. When the price consists of shillings and pence, suppose the given number to be *pounds*, and take such *aliquot part*, or the *sum* of such *aliquot parts*, as will make the given price.—Or, work for the shillings as in the preceding Rules, and take parts for the residue.

	‡(7) 2710 at 3s. 2d.	
Ans. £90368.	Ans. £42918.	Ans. £62807.
(2) 3150 at 3s. 4d.	(8) 7514 at 4s. 7d.	(14) 2510 at 14s. $7\frac{1}{4}d$.
Ans. £525.	Ans. 1721192.	Ans. £1832165 $\frac{1}{2}$.
(3) 2715 at 2s. 6d.	(9) 2517 at 5s. 3d.	(15) 3715 at 9s. 41d.
Ans. £33976.	Ans. £660143.	Ans. £17418112.
(4) 7150 at 1s. 8d.	(10) 2547 at 7s. $3\frac{1}{2}d$.	$(16)2572 ext{ at } 13s. 7\frac{1}{2}d.$
Ans. £595168.	Ans. $\pounds 92811.10\frac{1}{2}$.	Ans. £17523 6.
(5) 3215 at 1s. 4d.	(11) 3271 at 5s. $9\frac{1}{4}d$.	$(17)7251$ at $14s.8\frac{1}{4}d$.
Ans. £21468.	Ans. $\pounds 943164\frac{3}{4}$.	Ans. £53241903.
(6) 7211 at 1s. 3d.	$(12)2103 \text{ at } 15s. 4\frac{1}{2}d.$	(18) 3210 at 15s. 73 d
Ans. £450139.	Ans. £1616137 $\frac{1}{2}$.	Ans. $\pounds 251131\frac{1}{2}d$

RULE 7. When the price consists of pounds, shillings, and pence multiply the given quantity by the *number* of pounds, and take *aliquot parts* for the residue.—Or, work for the shillings as in the preceding Rules, &c.—Or, when the given number of articles is not large, work by Compound Multiplication.

$\begin{array}{c} s. & s. \\ * & 2 = \frac{1}{16} & 3270 \end{array}$	s. d. £. $\dagger 68 = \frac{1}{3} 2710$	s. d. ‡ 26=	
$1 = \frac{1}{2} \frac{327}{16310}$ Ans. £49010	Ans. £903	8. 8.	33835 9((424

TUTOR'S

PRACTICE.

*(1) 7215 at £74.	(7) 2107 nt £113.	(13) 3210 at £11863.
Ans. £51948.	Ans. £347611.	Ans. £618957
(2) 2104 at £53. Ans. £1083512.	Ans. £13931134.	(14) 2157 at £2744. Ans. £51097104.
	Ans. £15212126.	(15) 142 at £11524. Ans. £250264.
(4) 7156 at £56.	(10) 2701 at £234.	(16) 95 at £151474.
Ans. £3792616.	Ans. £585234.	Ans. £149474
	(11) 27 15 at £11724. Aus_£5051074.	(17) 37 at £11951. Ans. £73081.
(6) 3215 at £117.	(12) 2157 at £31524.	(18) 2175 at £21544.
Ans. £594715.	Ans. £31031954.	Ans. £6022074

RULE 8. When the given quantity consists of several denominations multiply the price by the number of the highest, and take aliquot parts for the inferior denominations.

(1) At $\pounds_{3..17..6}$. per *cwt*. what is the value of 25 *cwt*. 2 grs. 14 *lb*. of soap ?†

(2) At $\pounds 1..4..9$. per *cwt*. what is the value of 17 cwt. 1 qr 17 *lb*.? *Ans.* $\pounds 21..10..8$.

(3) Sold 85 cwt. 1 qr. 10 lb. of iron, at $\pm 1..7..8$. per cwt. what is the value of the whole? Ans. $\pm 118..1..01$.

(4) If hops are sold at $\pounds 4...5..8$. per *cwt*. what must be given for 72 *cwt*. 1 *qr*. 18 *lb*.? Ans. $\pounds 310...3..2$.

(5) What is the value of 27 cwt. 2 qrs. 15 lb. of logwood at \pounds 1..1..4. per cwt.? Ans. \pounds 29..9..6 $\frac{1}{4}$.

(6) Bought 78 cwt. 3 qrs. 12 lb. of molasses, at $\pounds 2..17..9$ per cwt. what must I give for the whole? Ans. $\pounds 227..14$.

(7) Sold 56 cwt. 1 qr. 17 lb. of sugar, at $\pounds 2..15..9$. per cwt how much is the whole charge? Ans. $\pounds 157..4..41$.

(8) What is the value of 97 cwt. 15 lb. of currants, a £3..17..10. per cwt. ? Ans. £378..0..3

(9) At £4..14..6. the *cwt*. what is the value of 37 *cwt*. 2 *or*. 13 *lb*. of raw sugar ? *Ans.* £177..14..8

8.	t 2 qrs.=; £3176
* 4=+ 7215	5×5=2-
•	19 76
50505	5
1443	<i>lb.</i> 96176
£51948 Ans	14= 1189
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TUTOR'S

E1..18..61. **189..5..74 E2..7..44**. **09..7..104**. **1..15..22**. **250..2..64**. **5..14..74**. **494..7..42 ..19..53**.

C73..0..81. C2..15..41. 022..0..71

minations quot parts

25 cw:

wt. 1 gr .10..8. per cwt. 3..1..**0**]. must be)..3..2. logwood .9..61. 2..17..9 7..14. per cwt 4..41. rants, a ..0..3 ot. 2 or 4..81

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ABSISTANT.]

TARE AND TRET.

(10) Bought sugar at \pounds 3..14..6. the cwt. what did I give for 15 cwt. 1 qr. 10 lb.? Ans. \pounds 57..2..9.

(11) Required the value of 17 oz. 8 dwts. 18 grs. of gold, at $\pounds 3..17..10\frac{1}{2}$. per ounce. Ans. $\pounds 67..17..11$.

(13) Required the value of 13 hhds. 42 gals. of Champagne wine, at $\pounds 25..13..6$. per hhd. Ans. $\pounds 350..17..10$.

(14) A gentleman purchased at an auction an estate of 149 a. 3 r. 20 p. at £54..10. per acre. What was the whole purchase money, including the auction duty of 7d. in the \pounds . the attorney's bill for the deeds of conveyance, £33..6..8. and his surveyor's charge for measuring it, at 1s. per acre?

Ans. £8447..5..01.

BULE 9. To find the price of 1 lb. at a given number of shillings per ewt.

Multiply the shillings by 3 and divide the product by 7; the quotient will be the price of 1 *lb*. in farthings.*

(1) What is the price of 1 lb. at 44s. 4d. per cwt. ?*

(2) What are the respective prices per *ib.* at 86s. 4d.; $\Im s$.; and 116s. 8d. per *cwt*.? Ans. $9\frac{1}{4}d.$, $3\frac{3}{4}d.$, and 1s. $0\frac{1}{2}d.$

RULE 10 It is sometimes expedient to change the price of the quantity for each other. Thus 48 yards at 2s. 9d. will be equivalent to 33 yards at 4s.; because 2s. 9d. = 33d. and 4s. = 48d.

(1) What is the value of 72 yds. at 3s. 5d. and at 14s. 7d. per yard? Ans. $\pounds 12..6.$, and $\pounds 52..10$.

(2) 80 yds. at 15s. 3d. and at 16s. 8d. per yard?

Ans. £61., and £66..13..4.

(3) 42 lbs. at $11\frac{1}{2}d$. and at 1s. $3\frac{1}{4}d$. per lb. ? Ans. £2..0..3., and £2..13..4 $\frac{1}{4}$.

TARE AND TRET.

Gross weight is the weight of any goods, together with that of the package which contains them.

• Multiplying by 3 reduces the shillings to fourpences, and 7 fourpences (or 2s. 4d.) are the value of 1 cwt. at 1 farthing per U.

> + 44s. 4d. $\frac{3}{7)133}$ 19 farthings = 43d. per lb. Ans.

6)

Neat weight is that of the *articles alone*, or what remains after the deduction of all allowances.

Tare is an allowance for the weight of the package. It is either so much in the whole, or at so much per bag, box, barrel, &c., or at so much in the cwt.

Tret is an allowance of 4 lb. in 104 lb. (or $\frac{1}{2\delta}$ part) for waste.

Cloff is an allowance of 2 lb, in 3 cuct, on some goods: but both these are nearly obsolete.

Suttle is the remainder when any particular allowance has been deducted.

RULE. When the Tare is at so much for each bag, &c., the whole Tare may be found by multiplying by the number of them. When it is at so much per each take the aligned parts of the Gross for the Tare. Subtract the Tare from the Grossi the remainder is the Neat: unless there is Tret allowed.

If Tree is allowed, it is $\frac{1}{2}$ of the Tare sature, which being subtracted from it, the remainder is the Near. But if Cloff also is to be allowed, the case. There each, multiplied by 2, and divided by 3, will be the lbs. Cloff, which subtract to find the Near.

(1) In 7 frails of raisins, each weighing 5 cut. 2 grs. 5 lb. gross, tare at 23 lb. por frail, how much near weight '*

(2) What is the heat weight of 25 hogsheals of tobacco, weighing gross 163 cars 2 provided in tare 160 % per hogshead?

(3) In 16 bags of popper, each weighing 55 %. 40x gross, tare per bag, 3 %. 5 min how many pounds near ' Ang 1310 %.

(4) What is the year weight bit 5 hogsheads of tooscoo, weighing gross 75 per 1 pr 14 5 tube in the whole 752 5 ? And de nut 2 rrs 18 5.

(5) lu 75 barrels of first each 2 gra 17 5 grosst mare in the whole 397 5 how much meat weight? And 50 mot. 1 gr.
(6) What is the beat weight of 15 outsi of numerical each S out 2 ors 5 15 grosst mare it 14 5 her mot. "



(7) cwt. 1 (8)

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(9) gross, weigh (10) to cus (11) as usu (12) weigh and cl (13)

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ASSISTANT.]

INVOICES.

(7) In 25 barrels of figs, each 2 cwt. 1 qr gross, tare per cwt. 16 lb. how much neat weight? Ans. 48 cwt. 0 qr. 24 lb.

(8) What is the neat weight of 9 hogsheads of sugar, each weighing gross 8 cwt. 3 qrs. 14 lb. tare 16 lb per cwt.?

Ans. 68 cwt. 1 qr. 24 lb.

(9) In 1 butt of currents, weighing 12 cwt. 2 qrs. 24 lb. gross, tare 14 lb. per cwt. tret 4 lb. per 104 lb. what is the neat weight ?*

(10) In 7 cwt. 3 qrs. 27 lb. gross, tare 36 lb. tret according to custom, how many pounds neat? Ans. 826 lb.

(11) In 152 cwt. 1 qr. 3 lb. gross, tare 10 lb. per cwt. tret as usual, how much neat weight? Ans. 133 cwt. 1 qr. 12 lb.

(12) What is the neat weight of 3 hogsheads of tobacco, weighing $15 \ cwt$. $3 \ qrs$. 20 *lb*. gross, tare 7 *lb*. per. *cwt*. tret and cloff as usual ?†

(13) In 7 hogsheads of tobacco, each weighing gross 5 cwt. 2 qrs. 7 lb.; tare 8 lb. per cwt. tret and cloff as usual, how much neat weight? Ans. 34 cwt. 2 qrs. 8 lb.

INVOICES, OR BILLS OF PARCELS.

(1) Mrs. Bland,

London, Sept. 1, 1830.

Bought of Jane Harris.

	<i>s</i> .	d.	£.	<i>d</i> .
15 pairs worsted stockings at	4	6 per pr.	•	
1 doz. thread ditto at	3	2		
$\frac{1}{2}$ doz. black silk ditto . at	8	3		
$1\frac{1}{2}$ doz. milled hose at			•	
2 doz. cotton ditto at				
17 pairs kid gloves at				
	_			21184
lb. cwt.qrs.lb.		<i>lb.</i> съ	vt. qrs. l	<i>Ъ.</i>
• $14 = \frac{1}{8}$ 12224 gross		$7 = \frac{1}{10}$	5 3 2	0 gross.
<i>lb.</i> <u>1210</u> tare.			3 2	$7\frac{1}{2}$ tare.
$4 = \frac{1}{36}$ 11 0 14 suttle.		26)1	4 3 2	$0\frac{1}{2}$ suttle.
1 19 tret.			2	8 [°] tret.
Ans. 10.2.23 neat.		1	4 1 1	$2\frac{1}{3}$ suttle.
		$14 \times 2 \div 3 =$		$9\frac{1}{2}$ cloff.
		Ans. 1	4 1	3 neat.

UTOR'S	•	es.	INVOICE	64
, 1830	, June :	De tby	Pearson,	(2) Mr. Isaac
		-	ht of John Sims a	Bou
s. d.	£.	<i>d</i> .	<i>s</i> .	
		6 per yard	a t 9	5 yds. satir
	•	4	red silk . at 17	181 yds. flow
	•	8	brocade. at 19	2 yds. rich
	•	2	net at 3 a velvet . at 27	61 yds. sarc
	•	6	a velvet. at 27	31 yds. Gen
	•	3	ng at 6	3 yds. lustr
.119	$\pounds \overline{62}$			
, 1830.	June 4	Nottingham,	ld,	3) Miss Enfi
		10mpson.	ught of Joseph Th	В
s. d.	£.	<i>d</i> .	<i>s</i> .	
		6 per yard	ric at 12	41 yds. cam
	•	3	nat 8 ed calico.at 5 nsat 2	21 yds. mus
	•	4	d calico. at 5	5 yds. prin
	•	3 each	nsat 2	2 doz. napl
	•	7 per ell	at 1	4 ells diape
	•	$1\frac{1}{2}$	sat 1	5 ells dowl
.1411	£17			

Received the above,

Joseph Thompson.

(4) Mrs. Mary Bright sold to the Right Honourable Lady Anna Maria Lamb 18 yards of French lace at 12s. 3d. per yd 5 pairs of fine kid gloves at 2s. 2d. per pair, 1 dozen French fans at 3s. 6d. each, two superb silk shawls at three guineas each, 4 dozen Irish lamb at 1s. 3d. per pair, and 6 sets of knots at 2s. 6d. per set .--- Please to make the Invoice for her. Total amount £23..14..4.

(5) Mr. Thomas Ward sold to James Russell Vernon, Esc. 171 yards of fine serge at 3s. 9d. per yd. 18 yds. of drugget at 9s. per yd. 151 yds. of superfine scarlet at 22s. per yd. 164 yds. of Yorkshire black at 18s. per yd. 25 yds. of shalloon at 1s. 9d. per yd. and 17 yds. of drab at 17s. 6d. per yd.-Make an Invoice of these articles. Total amount $\pm 60..10..5$.

(6) Mr. Samuel Green, of Wolverhampton, sent to Messes. Wright and Johnson, agreeably to order, 27 calf skins u 3s. 6d. each, 75 sheep skins at 1s. 7d. 39 coloured ditto u (9)

, 829. 4)ct. .830 Feb.

Feb.

TUTOR'S	ASSISTANT.]
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INVOICES.

*s. 8d. 15 buck skins at 11s. 6d. 17 Russia hides at 10s. 7d. and 125 lamb skins at 1s. $2\frac{1}{2}d$.—Draw up the Invoice. Total amount £39..1..8 $\frac{1}{2}$.

(7) Mr. Richard Groves sent the following articles to the Rev. Samuel Walsingham: viz. 2 stones of raw sugar at $6\frac{1}{2}d$. per tb. 2 loaves of sugar, $15\frac{1}{2}$ tb. at $11\frac{1}{2}d$. per tb. a stone of East India rice at $3\frac{1}{2}d$. per tb. 2 stones Carolina rice at 5d. per tb. 15 oz. nutmegs at $5\frac{1}{2}d$. per oz. and half a stone of Dutch coffee at 1s 10d. per tb.—Make a copy of the Invoice.

Total amount $\pounds 3..5..5\frac{3}{4}$.

61 per 18.

d.

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at 0

BILLS OF BOOK-DEBTS.

To Samuel Grant and Co., Dr

(8) Mr Charles Cross,

April 14. Belfast butter, 1 cwt.

1830.

Chester.

£. s. d.

c. s. d.

62..11..9

e 4, 1830.

e 3, 1830

s. d.

17..14..11

pson.

able Lady 3d. per yd en French ee guineas 6 sets of ce for her. 3..14..4. non, Esa, drugget at er yd. 163 shalloon at ∕d.—Ma⊧e ..10..51to Messes. skins u ed ditto u

Cheese, 7 cwt. 3 qrs. 12 lb. at 56 0 long cwt. May 8. Butter, ½ firkin, 28lb.at 0 54 per #. July 17. 5 Chesh. cheeses, 127 lb. at 0 " 61 66 Sept. 4. 2 Stilton ditto, 15 lb. at 0 $10\frac{1}{2}$ " Cream cheese, 13lb.at 0 8î £30..1..6¥ Dec. 28. Received the contents. Samuel Grant. (9) Mr. Charles Septimus Twigg, Newark. To Isaac Jones, Dr. , 829. s. d. £. s. d Oct. 22. Tares, 39 bushels at 1 10 per bush .830 4 per qr. Pease, 18 bushels at 30 Feb. 18. Malt, 7 qrs. at 63 6 per qr. 2 cwt. 1 qr at 1 Hops, 5 per lb. 41 per bush. Feb. 20. Oats, 6 qrs. at 2 . Beans, 17 grs. at 37 4 per qr. .

£84..9..11

1830. July 1. Received the above for Isaac Jones Thomas West.

SIMPLE INTEREST.

SIMPLE INTEREST

Is the premium allowed for the loan of any sum of money during a given space of time.

The *Prin.inal* is the money lent, for which *Interest* is to be received.

The Rate per cent. per annum is the quantity of Interes. (agreed on between the Borrower and the Lender) to be paid for the use of every $\pounds 100$. of the Principal, for one year.

The Amount is the Principal and Interest added together.

I. To find the Interest of any Sum of Money for a Year.

RULE. Multiply the *Principal* by the *Rate per cent*. and that Product divided by 100 will give the *Interest* required.

NOTE. When the *Rate* is an aliquot part of 100, the *Interest* may be calculated more expeditiously by taking such part of the *Principal*. Thus, for 5 per cent. take $\frac{1}{20}$; for 4 per cent. $\frac{1}{25}$, or $\frac{1}{5}$ of $\frac{1}{5}$; for 2 per cent. $\frac{1}{36}$; for $2\frac{1}{2}$ per cent. $\frac{1}{40}$; for 3 per cent. $\frac{1}{36}$, *plus* $\frac{1}{2}$ of that; &c.

This Rule is applied to the calculation of Commission, Brokerag^a, Purchasing Stocks, Insurance, Discounting of Bills, &c.*

II. For several Years. Multiply the Interest of one year by the number of years, and the product will be the answer.

For parts of a year, as months and days, &c., the Interest may be found by taking the aliquot parts of a year; or by the Rule of Three: and it is customary to allow 12 months to the year, and 30 days to a month.[†]

* To discount a Bill of Exchange is to advance the cash for it before it becomes due; deducting the *Interest* for the time it has to run Bankers always charge *Discount* as the *Interest* of the sum.

† At the rate of 5 per cent the interest of \pounds 1. for a year is 1s., or one penny for a month. Therefore, the principal \times the number of months, gives the interest in pence.

Or. take the parts of a year for the *months*, out of as many shillings as there are *pounds* in the *principal*.

Thus, to find the interest of $\pounds 10.10$, for 2 months, say $40\frac{1}{2}d. \times 2 =$ 81d. = 6s. 9d.; or, 2 months being $\frac{1}{6}$ of a year, 40s. 6d. $\div 6 = 6s$. 9d. Ans.

For days, take the aliquot parts of a month. The interest for days at 5 per cent. may also be found by multiplying the principal by the number of days; and the product divided by 365 will give the answer in *shillings*; or divided by 7300 (-365×20) will give the answer in pounds.

(1) V

cent. per (2) W cent. pe (3) V annum, (4) W per cent (5) V

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> (11) 1**7**..10.

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ny shillings

 $\begin{array}{c} 0\frac{1}{2}d. \times 2 = \\ 6 = 6s. \ 9a. \end{array}$

est for days ipal by the the answer answer in (1) What is the interest of ± 375 . for a year, at ± 5 . per cent. per annum ?*

(2) What is the interest of £945..10. for a year, at £4. per cent. per annum? $Ans. £37..16..4\frac{3}{4}$.

(3) What is the interest of $\pounds 547..15$. at $\pounds 5$. per cent. per annum, for 3 years? Ans. $\pounds 82..3..3$.

(4) What is the interest of $\pounds 254..17..6$. for 5 years, at $\pounds 4$. per cent. per annum? Ans. $\pounds 50..19..6$.

(5) What is the amount of $\pounds 556..13..4$. at $\pounds 5$. per cent per annum, in 5 years? Ans. $\pounds 695..16..8$.

NOTE. Commission and Brokerage (commonly called Brokage) are allowances of so much per cent. to an agent or broker, for buying or selling goods, or transacting business for another.

(6) My correspondent informs me that he has bought goods to the amount of $\pounds 754..16$. on my account, what is his commission at $\pounds 2\frac{1}{2}$. per cent.? Ans. $\pounds 18..17..4\frac{3}{4}$.

(7) If 1 allow my factor $\pounds 3_{\frac{3}{4}}$. per cent. for commission, what will he require on $\pounds 876..5..10$? Ans. $\pounds 32..17..2_{\frac{1}{2}}$.

NOTE. Stock is a general term to designate the Capitals of our Trading Companies; or to denote *Property* in the *Public Funds*; which means the Money paid by Government for the interest of the *National Debt.* The quantity of Stock is a *nominal* sum, for which the owner receives a certain rate of interest while he holds the same.

(8) At $\pounds 110\frac{1}{4}$. per cent. what is the purchase of $\pounds 2054..16$. South Sea stock? Ans. $\pounds 2265..8..4$.

(9) At $\pounds 104_{\frac{3}{8}}$. per cent. South Sea annuities, what is the purchase of $\pounds 1797..14$.? Ans. $\pounds 1876..6..11_{\frac{3}{4}}$.

(10) At $\pounds 96\frac{3}{4}$. per cent. what is the purchase of $\pounds 577..19$. Bank annuities? Ans. $\pounds 559..3..3\frac{3}{4}$.

(11) At $\pounds 124\frac{5}{8}$. per cent. what is the purchase of $\pounds 758.$. 17.10. India stock? Ans. $\pounds 945..15..4\frac{1}{4}$.

(12) What sum will purchase £1284. of the 3 per cent. Consols, at $\pounds \Im \Im_3^7$. per cent.; including the broker's charge of **1**, or 2s. 6d. per cent. on the amount of stock ?

Ans. £770..7..11 $\frac{3}{4}$.

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* £. 375	
5	Better thus :
£. 18 75 20	$\pounds. \pounds. \\ 5 = \frac{1}{20} 375$
s. 15 00	Ans. £1815.
Ans. £1815.	

Cutting the two figures in the above divides the number by 100: see Division, p. 21

SIMPLE INTEREST.

(13) If I employ a broker to buy goods for me, to the amount of $\pounds 2575..17..6$. what is the brokerage at 4s. per cent.?*

(14) What is the broker's charge on a sale amounting to \pounds 7105..5..10. at 5s. 6d. per cent.? Ans. \pounds 19..10..94.

(15) What is the brokage on goods sold for $\pounds 975..6..4$. at 6s. 6d. per cent.? Ans. $\pounds 3..3..4\frac{1}{2}$.

(16) What is the interest of £257..5..1. at £4. per cent. per annum, for a year and three quarters? Ans. £18..0..1 $\frac{1}{2}$.

(17) What is the interest of $\pounds 479..5$. for $5\frac{1}{4}$ years, at $\pounds 5$. per cent. per annum? Ans. $\pounds 125..16..0\frac{3}{4}$.

(18) What is the amount of £576..2..7. in $7\frac{1}{4}$ years, at £4 $\frac{1}{2}$. per cent. per annum? Ans. £764..1..8 $\frac{1}{2}$.

(19) What is the interest of £259..13..5. for 20 weeks, at £5. per cent. per annum? Ans. £4..19..10 $\frac{1}{4}$.

(20) What is the interest of $\pounds 2726..1.4$. at $\pounds 4\frac{1}{2}$. per cent per annum, for 3 years, 154 days? Ans. $\pounds 419..15..6\frac{1}{4}$.

(21) Compute the interest of $\pounds 155$. for 49 days, and for 146 days, at $\pounds 5$. per cent. per annum.

Ans. $\pounds 1..0..9\frac{1}{2}$ and $\pounds 3..2..0$.

(22) What will a banker charge for the discount of a bill of £76..10. and another of £54. negotiated on the 18th of May; the former becoming due June 30, and the latter July 13; discounting at £5. per cent.? Ans. 8s. 11d. and 8s. 3d.

When the Amount, Time, and Rate per cent. are given, to find the Principal.

RULE. As the amount of $\pounds 100$, at the rate and for the time given is to $\pounds 100$, so is the amount given to the principal required.

(23) What principal being put to interest will amount to $\pounds 402..10$. in 5 years, at $\pounds 3$. per cent. per annum ?†

(24) What principal being put to interest for 9 years will amount to $\pounds 734..8$. at $\pounds 4$. per cent. per annum?

Ans. £540.

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s. £. s. d. * $4=\frac{1}{5}$ 257517 6	03
£. 5 15 3 6	12
20	42
s. 3 03	4
Ans. £5303.	1 68
£. †£3×5+100=£115. As 115 :	£. £. s. £ 100 : : 40310 : 350 Ang.

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DISCOUNT.

(25) What principal, being put to interest for 7 years at $\pounds 5$. per cent. per annum, will amount to $\pounds 334..16$.?

Ans. £248.

When the Principal, Rate per cent. and Amount are given, to find the Time.

RULE. As the interest for 1 year is to 1 year, so is the whole interest to the number of years.

(26) In what time will £350. amount to £402.10. at £3. per cent. per annum ?*

(27) In what time will £540. amount to £734..8. at £4. per cent. per annum? Ans. 9 years.

(28) In what time will £248. amount to £334..16. at £5. per cent. per annum? Ans. 7 years.

When the Principal, Amount, and Time are given, to find the Rate per cent.

RULE. As the principal is to the whole interest, so is £100. to its interest for the given time. Divide that interest by the number of years, and the quotient will be the rate per cent.

(29) At what rate per cent. will \pounds 350. amount to \pounds 402..10. in 5 years ?†

(30) At what rate per cent. will £248. amount to £334..16. in 7 years? Ans. £5. per cent.

(31) At what rate per cent. will £540. amount to £734..8. in 9 years? Ans. £4. per cent.

DISCOUNT

Is the abatement of so much money, on any sum received before it is due, as the money received, if put to interest, would gain at the rate, and in the time given. Thus $\pounds 100$. present money would discharge a debt of $\pounds 105$. to be paid a year hence, *Discount* being made at $\pounds 5$. per cent.

£. * $\frac{350 \times 3}{100} = \pounds 10..10$. the interest for 1 year. $\pounds 402..10. - \pounds 350. = \pounds 52..10$. the whole interest. As $\pounds 10..10: 1$ year :: $\pounds 52..10: 5$ years. Ans. † As $\pounds 350: \pounds 52..10: \pounds 100: \pounds 15 =$ the interest of $\pounds 100$. for 5 years. Then $15 \div 5 = \pounds 3$ the rate per cent.

DISCOUNT.

70

RULE. As £100. with its interest for the time given is to that interest, so is the sum given to the *Discount* required.

Also, As that Amount of £100. is to £100., so is the given sum to the **Present** worth.

But if either the *Discount* or the *Present worth* be found by the proportion the other may be found by subtracting that from the given sum.

(1) What are the discount and present worth of $\pounds 386..5$. for 6 months, at $\pounds 6$. per cent. per annum ?*

(2) How much shall I receive in present payment for a debt of £357..10. due 9 months hence, allowing discount at £5. per cent. per annum? Ans. £344..11..6 $\frac{3}{2}$ $\frac{15}{2}$.

(3) What is the discount of £275..10. for 7 months, at £5. per cent. per annum? Ans. £7..16..1 $\frac{3}{4}$ $\frac{95}{247}$.

(4) What is the present worth of £527 .9..1. payable in 7 months, at $\pounds 4\frac{1}{4}$. per cent. per annum?

Ans. £514..13..101 2 6930.

(5) Required the present worth of £875..5..6. due in 5 months, at £4 $\frac{1}{2}$. per cent. per annum. Ans. £859..3..3 $\frac{3}{4}$ $\frac{75}{4073}$.

(6) What is the present worth of $\pounds 500$. payable in 10 months, at $\pounds 5$. per cent. per annum? Ans. $\pounds 480$.

(7) How much ready money ought I to receive for a note of £75. due in 15 months, at £5. per cent. per annum? Ans. £70..11..9 $\frac{3}{2\pi}$.

(8) What will be the present worth of £150. payable at 3 instalments of four months; *i. e.* one-third at 4 months, one-third at 8 months, and one-third at 12 months, discounting at £5. per cent. per annum? Ans. £145..3..8 $\frac{1}{2}$.

(9) Of a debt of £575..10. one moiety is to be paid in 3 months, and the other in 6 months. What discount must be allowed for present payment, at £5. per cent. per annum? Ans. £10..11..43.

 $6 \text{ m.} = \frac{1}{2} \underbrace{\pounds_{0}}_{100} \underbrace{\pounds_{0}}_{3} = 103 = \text{amount of } \pounds_{100} \text{ in 6 months}$ $\underbrace{\pounds_{0}}_{4} \underbrace{\pounds_{0}}_{3} \underbrace{\pounds_{0}}_{3} \underbrace{\pounds_{0}}_{3} \underbrace{\pounds_{0}}_{3} \underbrace{\pounds_{0}}_{3} \underbrace{\pounds_{0}}_{3} \underbrace{103}_{1158.15} \underbrace{11..5}_{11..5} \text{ discount.}$ $\underbrace{\frac{1133}{25}}_{20} \underbrace{\frac{20}{103515} = 5s.}$

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(10) What is the present worth of $\pounds 500$. at $\pounds 4$. per cent. per annum, $\pounds 100$. being to be paid down, and the rest at two 6 months? Ans. $\pounds 488..7..8\frac{1}{2}$.

(11) Bought goods amounting to £109..16. at 6 months' credit, or $\pounds 3\frac{1}{2}$, per cent. discount for prompt payment. How much ready money will discharge the account ?*

Ans. $\pounds 105..13..4\frac{1}{2}$.

NOTE. The Rule to find the present worth of any sum of money is precisely identical with that case in Simple Interest in which the Amount, Time, and Rate per cent. are given to find the Principal. See page 68.

COMPOUND INTEREST

Is that which arises from both the Principal and Interest: that is, when the interest of money, having become due, and not being paid, is added to the Principal, and the subsequent Interest is computed on the *Amount*.

RULE. Compute the first year's interest, which add to the principal: then find the interest of that amount, which add as before, and so on for the number of years. Subtract the given sum from the *last Amount*, and the remainder will be the *Compound Interest*.

(1) What is the compound interest of $\pounds 500$. forborne 3 years, at $\pounds 5$. per cent. per annum ?

(2) What is the amount of £400. in $3\frac{1}{2}$ years, at £5. per cent. per annum, compound interest? Ans. £474..12.. $6\frac{1}{4}$.

(3) What will £650. amount to in 5 years, at £5. per cent. per annum, compound interest? Ans. £829..11..7 $\frac{1}{2}$.

(4) What is the amount of $\pounds 550..10$. for $3\frac{1}{2}$ years, at $\pounds 6$ per cent. per annum, compound interest? Ans. $\pounds 675..6..5$.

(5) What is the compound interest of \pounds 764. for 4 years and 9 months, at \pounds 6. per cent. per annum?

Ans. £243..18..8.

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* The discount in cases of this sort is so much per cent. on the sum, without regard to time. It is, therefore, computed as a year's interest.

1 30	£500		-1 	E551 5	
	25		20	2711 :	3
1 20	525	amount in	1 yr.	57816 :	B amount in 3 years.
-		5		500.: 0 () principal subtract.
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EQUATION OF PAYMENTS.

(6) What is the compound interest of $\pm 57..10..6$. for 5 years, 7 months, and 15 days, at £5. per cent. per annum? Ans. £18..3..81.

(7) What is the compound interest of $\pm 259..10$. for 3 years, 9 months, and 10 days, at $\pounds 4\frac{1}{2}$. per cent. per annum ? Ans. £46..19..101.

EQUATION OF PAYMENTS

Is when several sums are due at different times, to find a mean time for paying the whole debt; to do which, this is the common

RULE. Multiply each term by its time, and divide the sum of the products by the whole debt, the quotient is accounted the mean time

£.

Ans. 71 months.

(1) A owes B £200. whereof	$40 \times 3 = 120$
$\pounds 40$, is to be paid at 3 months,	$60 \times 5 = 300$
\pounds 60. at 5 months, and \pounds 100. at 10	$100 \times 10 = 1000$
months: at what time may the whole	$2 00)1\overline{4} \overline{20}$
debt be paid together without pre-	Ans. $7\frac{1}{10}n$
judice to either?	21/13. 1 10

(2) B owes C £800. whereof £200. is to be paid at 3 months, $\pounds 100$. at 4 months, $\pounds 300$. at 5 months, and $\pounds 200$. at 6 months; but they agree that the whole shall be paid at once; what is the equated time? Ans. 4 months, 18[§] days.

(3) A debt of ± 360 , was to have been paid as follows: viz.: £120. at 2 months, £200. at 4 months, and the rest at 5 months; but the parties have agreed to have it paid at one mean time : what is that time ? Ans. 3 months, $13\frac{1}{4}$ days.

(4) A merchant bought goods to the value of ± 500 . to pay £100. at the end of 3 months, £150. at the end of 6 months, and $\pounds 250$. at the end of 12 months; but it was afterwards agreed to discharge the debt at one payment: required the time. Ans. 8 months, 12 days.

(5) H is indebted to L a certain sum, which is to be paid at 6 different payments, that is $\frac{1}{4}$ at 2 months, $\frac{1}{4}$ at 3 months, $\frac{1}{8}$ at 4 months, $\frac{1}{4}$ at 5 months, $\frac{1}{8}$ at 6 months, and the rest at 7 months; but they mutually agree that the whole shall be paid at one equated time : what is that time ? Ans. 41 months.

(6) A is indebted to B £120. whereof $\frac{1}{2}$ is to be paid at 3 months, $\frac{1}{4}$ at 6 months, and the rest at 9 months : what is the equated time of the whole payment? Ans. 51 months.

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BARTER.

BARTER

Is the exchanging of commodities.

Rons. Compute, by the most expeditious method, fac value of the article whose quantity is given: then find what quantity of the other at the rate proposed, may be had for the same money.

NOTE. Sometimes one tradesman, in bartering, advances his goods above the ready money price. In this case, it will be necessary to proportionate the other's bartering price to his ready money price, by tho Rule of Three.

(1) What quantity of chocolate at 4s. per lb. must be exchanged for 2 cwt. of tea, at 9s. per lb.?*

(2) A and B. barter: A has 20 cwt. of prunes, at 4d. per b. roady money, but in barter will have 5d. per lb, and B has hops worth 32s. per owt. ready money: what ought B to charge his hops, and what quantity must he give for the 20 cwt. of prunes ?

(3) How much tea at 9s. per lb. can I have in barier for 4 cwt. 2 grs. of chocolate, at 4s. per lb.? Ans. 2 cwt.

(4) A exchanges with B $23\frac{1}{2}$ cwt. of cheese, worth 52s 6d. per cwt., for 8 pieces of cloth containing 248 yards, at 4s. 4d. per yard; the difference to be paid in money. Who receives the balance, and how much?... Ans. A. receives £7..19..1.

(5) How much ginger at $15\frac{1}{4}d$. per *lb*. must be exchanged for $3\frac{1}{2}$ *lb*. of pepper, at $13\frac{1}{2}d$. per *lb*? Ans. 3 *lb*. $1\frac{35}{61}$ oz.

(6) How many dozen of candles, at 5s. 2d. per dozen, must be bartered for 3 cwt. 2 qrs. 16 lb. of tallow, at 37s. 4d. per cwt.? Ans. 26 dozen, $3\frac{5}{6}\frac{4}{2}$ lb.

(7) A exchanges with B 608 yards of cloth, worth 14s. per

* $224 \times 9 = 2016s$. the value of the tea. As 4s. : 1 lb. :: 2016s. : 504 lb. of chocolate. Ans. As 4d. : 5d. :: 32s. : 40s. the price per cwt. to be charged for the hops. 20 cwt. = 2240 lb. 5 11200d. the value of the prunes. As 40s. : 1 cwt. :: 11200d. : $\frac{11200}{480} = 23 \text{ cwt. } 1 \text{ qr. } 9\frac{16}{18} \text{ lb. Asw}$.

PROFIT AND LOSS.

yard, for 85 cut. 2 grs. 24 lb. of bees' wax, and £125..12. in cash. What was the wax charged per cwt.? Ans. £3..10.

(8) A barters with B 320 dozen of candles at 4s. 6d. per dozen, for cotton at 8d. per lb. and ± 30 . in sh. What was Ans. 11 cwt. 1 qr. the quantity of cotton?

(9) How much cotton, at 1s. 2d. per lb. must be given for 114 lb. of tebacco, at 6d. per lb.? Ans. 48# lb.

PROFIT AND LOSS

is a Rule by which we discover the gain or loss in the buy. ing and selling of goods; and which enables us to adjust the prices of articles, so as to gain or lose so much per cent., &c.

The questions are solved by the Rule of Three, or Practice

The prime cost means the purchase money: therefore

The prime cost $\begin{cases} plus \text{ the gain, or} \\ minus \text{ the loss,} \end{cases}$ equal the selling price.

The selling price minus { the prime cost equal the gain. the gain equal the prime cost.

The selling price plus the loss equal the prime cost.

Gain or loss per cent. means so much on £100. purchase money, or prime cost: therefore, when £20. per cent. are gained, £120. is the selling price per cent.; when £20. per cent. are lost, £80. is the sell ing price.

Case 1. Given, the prime cost and the selling price of an integer or quantity, to find the gain or loss per cent.

As the prime cost given: the gain or loss :: £100. : the gain or lon per cent.

Case 2. Given, the prime cost as before, with a proposed gain or loss per cent. to find the selling price.

As £100. : { £100. plus the gain } : : the prime cost : the selling price.

Case 3. Given, the selling price of an integer or quantity, and the gain or loss per cent. to find the prime cost

or, £100. minus the loss }: £100. :: the selling price : the prime cost.

Case 4. Given, the selling price of an integer, and the gain per cent. to find the gain per cent. at some other proposed price.

As the selling price : £100. plus the gain :: the proposed price : the selling price per cent. from which deduct £100. for the gain per cent. required.

Secondly, To find another selling price, at a different gain per cent. As £100. plus the gain : the selling price :: £100. plus the proposed gain : the selling price required.

A much greater variety of cases may occur; but it is presumed that the student was arrains a due knowledge of these will easily compre hond the rest.

74

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PROFIT AND LOSS.

(1) If 1 yard of cloth cost 11s. and is sold for 12s. 6d. what is the gain per cent. ?*

(2) If 60 ells of Holland cost £18. what must 1 ell be sold * for to gain £8. per cent. ?†

(3) If 1 *lb*. of tobacco cost 16*d*. and be sold for 20*d*. what is the gain per cent. ? Ans. $\pounds 25$.

(4) If a parcel of cloth be sold for £560. gaining £12. per cent. what is the prime cost? Ans. £500.

(5) If a yard of cloth be bought for 13s. 4d. and sold again for 16s. what is the gain per cent.? Ans. $\pounds 20$.

(6) If 112 *lb*. of iron cost 27s. 6d. what must 1 *cwt*. be sold for to gain £15. per cent.? Ans. £1..11..7 $\frac{1}{2}$.

(7) If 375 yards of cloth be sold for £490. at £20. per cent. profit, what did it cost per yard? Ans. £1..1..9 $\frac{1}{4}$ $\frac{125}{375}$.

(8) Sold 1 cwt. of hops for £6..15. at the rate of £25. per cent. profit. What would have been the gain per cent. if they had been sold for £8. per cwt.? Ans. £48..2..11 $\frac{1}{2}$?

(9) If 90 ells of cambric cost £60, how must I sell it per yard to gain £18, per cent.? Ans. 12s. $7\frac{18}{450}d$.

(10) A plumber sold 10 fothers of lead for $\pounds 204..15$. and gained after the rate of $\pounds 12..10$. per cent. What did it cost him per cwt.? Ans. 18s. 8d.

(11) What was the profit on 436 yards of cloth, bought at 88. 6d. and sold at 10s. 4d. per yard? Ans. £39..19..4.

(12) Bought 14 tons of steel at $\pounds 69$. per ton, which was retailed at 6d. per lb. What was the loss sustained?

Ans. £182.

(13) Bought 124 yards of linen for £32. How should the same be retailed per yard to gain £15. per cent.?

Ans. 5s. $11\frac{28}{124}d$.

(14) Bought 249 yards of cloth at 3s. 4d. per yard, and retailed the same at 4s. 2d. per yard. What was the whole gain, and how much per cent. ?‡

Ans. £10..7..6. profit, and £25. per cent.

* As $11s. : 1s. 6d. : : \pounds 100 : \frac{100 \times 3}{22} = \pounds 13..12..8\frac{1}{2} \frac{10}{11}$. Ans. * As $11s. : 1s. 6d. : : \pounds 100 : \frac{100 \times 3}{22} = \pounds 13..12..8\frac{1}{2} \frac{10}{11}$. Ans. * $\frac{2}{sixp. \frac{23}{23}} = \frac{3}{3} sixp.$ * As $\pounds 100 : \pounds 108 : : \pounds 18 : \frac{108 \times 18}{100} = \pounds 19..8..9\frac{1}{2} \frac{4}{15}$ the celling price. And $\pounds 19..8..9\frac{1}{2} \div 60 = 6s. 5\frac{3}{4}d.$ the price per ell. * For the solving of this question, see Cases 1 and Sh

FELLOWSHIP.

76

FELLOWSHIP, OR PARTNERSHIP

Is a rule by which any number or quantity may be divided into certain proportionate parts. It is applied to determine the respective shares of gain or loss of the several partners in a company; in proportion to their respective shares of the capital employed as a joint stock : also in the division of common lands, and other cases of a similar kind.

FELLOWSHIP WITHOUT TIME.

RULE. As the whole stock is to the whole gain or loss; so is each individual share to the correspondent gain or loss.

PROOF. The sum of the shares will be equal to the whole gain or loss.

(1) A and B join in trade. A puts into stock £20. and B £40; they gain £50. What is the share of each ?*

(2) A, B, and C joined in trade; A put in £20; B £30 and C £40; and they gained £180. What is each man's part of the gain? Ans. A £40. B £60. C £80.

(3) Four persons, B, C, D, and E formed a joint stock; B put in £227; C £349; D £115; and E £439; they gainet £428. Required each person's share of the gain.

Ans. B £85..19.. $6\frac{3}{4}$ $\frac{69}{113}$. C £132..3..9 $\frac{12}{113}$.

 $D \pounds 43..11..1_{\frac{3}{4}} \frac{25}{113}$. $E \pounds 166..5..6_{\frac{1}{4}} \frac{7}{113}$

(4) D, E, and F entered into partnership. D's stock was $\pounds750$; E's $\pounds460$; and F's $\pounds500$; and at the end of 12 months they had gained $\pounds684$. What is each man's particular share of the gain? Ans. $D \pounds300$, $E \pounds184$. and $F \pounds200$.

(5) A tradesman is indebted to B £275..14; to C £304..7; to D £152; and to E £104..6; but upon his decease his estate is found to be worth but £675..15. How must it be divided among his creditors ?

Ans. B's share £222..15..2—6584. C's £245..18..1 $\frac{1}{2}$ —15750.

D's £122..16..2 $\frac{3}{4}$ -12227. and E's £84..5..5-15620. (6) Four persons trade together with a joint capital; of which A has $\frac{1}{3}$, B $\frac{1}{4}$, C $\frac{1}{5}$, and D $\frac{1}{6}$, and at the end of 6

> * 20+40=60As 60 : 50 : : $\begin{cases} 20 : \pounds 16..13.. 4=A's share. \\ 40 : 33.. 6.. 8=B's share. \\ 50.. 0.. 0 Proof. \end{cases}$

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FELLOWSHIP.

souths they gain £100. What is each person's share of the gain? Ans. A £35..1..9-12. B £26..6.. $3\frac{3}{4}$ -9.

C $\pounds 21..1..0\frac{1}{2}$ —30. and D $\pounds 17..10..10\frac{1}{2}$ —6. (7) Two persons joined in the purchase of an estate yielding £1700. per annum, for £27200. whereof D paid £15000. and E the rest: some time after, they sold it for 24 years purchase. What was each person's share ?*

Ans. D £22500. E £18300.

(8) D, E, and F, form a joint capital of $\pounds 047$. Their respective shares are in proportion to each other as 4, 6, and 8 and the gain is equal to D's stock. Required each person's stock and gain.

Ans. D's stock £143..15..6 $\frac{6}{9}$ gain, £31..19..0 $\frac{4}{27}$.

 $E'_{s} \ldots 215..13..4' \ldots 47..18..6_{\frac{6}{27}}$

 $F's \ldots 287..11..1\frac{3}{9} \ldots 63..18..0\frac{3}{27}$

(9) D, E, and F, joined in partnership; the amount of their stock was $\pounds 100$; D's gain was $\pounds 3$; E's $\pounds 5$; and F's $\pounds 8$; what was each man's stock?

Ans. D's stock £18..15. E's £31..5. and F's £50.

FELLOWSHIP WITH TIME.

RULE. As the sum of the products of each person's money and time is to the whole gain or loss; so is each individual product to the corresponding gain or loss.

(1) D and E enter into partnership; D puts in £40. for three months, and E £75. for four months, and they gain £70. What is each man's share of the gain ?†

(2) Three tradesmen joined in company; D put into the joint stock £195..14. for three months; E £169..18..3. for 5 months; and F £59..14..10. for 11 months: they gained £364..18. What is each man's share of the gain?

Ans. D's £102..6..4—5008. E's £148..1..1 $\frac{1}{2}$ —482802. and F's £114..10..6 $\frac{1}{4}$ —14707.

(3) Three merchants join in company for 18 months: D, puts in \pounds 500, and at 5 months' end takes out \pounds 200, at 10

* The sale of a property for so many years purchase, is understood to be, for so much present money as the annual rent or value \times that number of years.

 $t 40 \times 3 = 120$ $75 \times 4 = 300$ 420 As 42|0:7|0:; $\begin{cases} 120: \pounds 20=D' \text{ share.} \\ 300: 50=E' \text{ s share.} \\ 70 \text{ Proof.} \end{cases}$

ALLIGATION,

78

months' end puts in £300. and at the end of 14 months takes out £130; E puts in £400. and at the end of 3 months £270 more, at 9 months he takes out £140. but puts in £100. at the end of 12 months, and withdraws £99. at the end of 15 months; F puts in £900. and at 6 months takes out £200, at the end of 11 months puts in £500. but takes out £200, at the end of 11 months puts in £500. but takes out that and £100. more at the end of 13 months. They gain £200. Required each man's share of the gain.

> Ans. D $\pounds 50..7..6-21720$. E $\pounds 62..12..5\frac{1}{4}-29859$, and F $\pounds 87..0..0\frac{1}{4}-14167$.

(4) D, E, and F, hold a piece of ground in common, for which they are to pay £36.10.6: D puts in 23 oxen 27 days; E 21 oxen 35 days; and F 16 oxen 23 days. What is each man to pay of the said rent?

> Ans. D £13..3.. $1\frac{1}{2}$ -624. E £15..11..5-1688. and F £7..15..11-1136.

ALLIGATION

Is a rule by which we ascertain the *mean price* of any compound formed by mixing ingredients of *various prices*; or the quantities of the various articles which will form a mixture of a certain *mean* or *average value*. It comprises four distinct cases.

CASE 1. ALLIGATION MEDIAL. The various quantities and prices being given, to find the *mean price* of the mixture.

Rule. Multiply each quantity by its price, and divide the sum of the products by the sum of the quantities.*

(1) A grocer mixed 4 cwt. of sugar, at 56s. per cwt, with 7 cwt. at 43s. per cwt. and 5 cwt. at 37s. per cwt. What is the value of 1 cwt. of this mixture? Ans. $\pounds 2..4..4\frac{1}{2}$.

(2) A vintner mixes 15 gallons of canary, at 8s. per gallon, with 20 gallons, at 7s. 4d. per gallon; 10 gallons of sherry,

EXAMPLE.

* A farmer mixed 20 bushels of wheat, at 5s. per bushel, and 36 bushels of rye, at 3s. per bushel, with 40 bushels of barley, at 2s. per bushel. What is the worth of bushel of this mixture?

$\begin{array}{c} s. & s. \\ 20 \times 5 = 100 \\ 36 \times 3 = 108 \\ 40 \times 2 = 50 \\ \overline{96} & 96)\overline{208}(7 \ s. \ Ans \end{array}$

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ALLIGATION.

at 6s. 8d. per gallon; and 24 gallons of white wine, at 4s per gallon. What is the worth of a gallon of this mixture? Ans. 6s. $2\frac{1}{2}\frac{4}{4}\frac{6}{6}d$.

(3) A malster mixes 30 quarters of brown malt, at 28s. per quarter, with 46 quarters of pale, at 30s. per quarter, and 24 quarters of high dried ditto, at 25s. per quarter. What is one quarter of the mixture worth? Ans. $\pounds 1..8..2\frac{1}{4} \frac{6}{16}d$.

(4) A vintner mixes 20 quarts of port, at 5s. 4d. per quart, with 12 quarts of white wine, at 5s. per quart, 30 quarts of Lisbon, at 6s. per quart, and 20 quarts of mountain, at 4s. 6d. per quart. What is a quart of this mixture worth?

Ans. 5s. $3\frac{3}{4} = \frac{5}{2} d$.

(5) A refiner melts 12 *lb*. of silver bullion, of 6 oz. fine, with 8 *lb*. of 7 oz. fine, and 10 *lb*. of 8 oz. fine; required the fineness of 1 *lb*. of that mixture.

Ans. 6 oz. 18 dwt. 16 gr.

CASE 2. ALLIGATION ALTERNATE. The various prices being given, to find the quantities which may be mixed, to bear a certain average price.

RULE. Arrange the given prices in one column, with the proposed average price on the left.

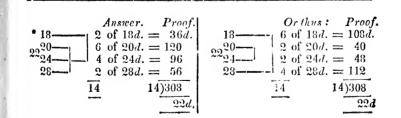
Link each less than the average with one greater.

Place against each term the difference between that with which it is linked and the mean: and the respective differences will be the quantities required.

Note. Questions in this rule admit of a great variety of answers, according to the manner of linking them also by taking other numbers proportional to the answers found

(1) A vintner would mix four sorts of wine together, of 18d. 20d. 24d. and 28d. per quart, what quantity of each sort must be take to sell the mixture at 22d. per quart ?*

(2) A grocer would mix sugar at 4d. 6d. and 10d. per lb



ALLIGATION.

80

so as to sell the compound for 8*d*. per *lb*. What quantity of each kind must he take?

Ans. 2 lb. at 4d. 2 lb. at 6d. and 6 lb. at 10d. (3) How much tea at 16s. 14s. 9s. and 8s. per lb. will compose a mixture worth 10s. per lb.?

Ans. 1 lb. at 16s. 2 lb. at 14s. 6 lb. at 9s. and 4 lb. at 8s.

(4) A farmer would mix as much barley, at 3s. 6d. per bushel, ryc at 4s. per bushel, and oats at 2s. per bushel, as will make a mixture worth 2s. 6d. per bushel. How much of each sort? Ans. 6b. of barley, 6 of rye, and 30 of oats.

(5) A tobacconist would mix tobacco at 2s., 1s. 6d., and 1s. 3d. per lb. so that the compound may be worth 1s. 8d. per lb. What quantity of each sort must he take?

Ans. 7 lb. at 2s. 4 lb. at 1s. 6d. and 4 lb. at 1s. 3d.

CASE 3. ALLIGATION PARTIAL. This is similar to Case 2. except that one of the quantities is limited.

RULE. Link the prices, and place the differences as before.

Then, as the difference opposite to that whose quantity is given, is to each other difference; so is the given quantity to each required quantity.

(1) A tobacconist intends to mix 20 *lb*. of tobacco at 15*d*. per *lb*. with others at 16*d*. 18*d*. and 22*d*. per *lb*. How many pounds of each sort must he take to make one pound of the mixture worth 17d.?*

(2) How much coffee, at 3s. at 2s. and at 1s. 6d. per lb. with 20 lb. at 5s. will make a mixture worth 2s. 8d. per lb.?

Ans. 35 lb. at 3s. 70 lb. at 2s. and 10 lb. at 1s. 6d.

(3) A distiller would mix 10 gallons of French brandy, at 48s. per gallon, with British at 28s. and spirits at 16s. per gallon. What quantity of each sort must he take to afford it for 32s. per gallon? Ans. 8 British, and 8 spirits.
(4) What quantity of teas at 12s. 10s. and 6s. must be

mixed with 20 1b. at 4s. per 1b. that the mixture may be wort's 8s. per 1b.? Ans. 10 lb. at 6s. 10 lb. at 10s. 20 lb. at 12s

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CASE 4. ALLIGATION TOTAL. This is also similar to Case 2, except that the whole quantity of the compound is limited.

RULE. Link the prices, and place the differences as before.

Then, As the sum of the differences is to each particular difference; so is the quantity given to each required quantity.

(1) A grocer has four sorts of sugar at 12d. 10d. 6d. and 4d. per lb. and would make a composition of 144 lb. worth 8d. per lb. What quantity of each sort must he take?*

(2) A grocer having 4 sorts of tea at 5s. 6s. 8s. and 9s. per *lb*. would have a composition of 87 *lb*. worth 7s. per *lb*. What quantity must there be of each sort?

Ans. 14½ lb. of 5s. 29 lb. of 6s. 29 lb. of 8s. and 14½ lb. of 9s.
(3) A vintner having 4 sorts of wine, viz. white wine at 16s. per gallon, Flemish at 24s. per gallon, Malaga at 32s. per gallon, and Canary at 40s. per gallon; would make a mixture of 60 gallons worth 20s. per gallon. What quantity of each sort must he take ?

Ans. 45 gallons of white wine, 5 of Flemish, 5 of Malaga, and 5 of Canary.

(4) A jeweller would melt together four sorts of gold, of 24, 22, 20, and 15 carats fine, so as to produce a compound of 42 oz. of 17 carats fine. How much must he take of each sort? Ans. 4 oz. of 24, 4 oz. of 22, 4 oz. of 20, and 30 oz. of 15 carats fine.

COMPARISON OF WEIGHTS AND MEASURES.

This is merely an application of the Rule of Proportion.

(1) If 50 Dutch pence be worth 65 French pence, how many Dutch pence arc equal to 350 French pence ?†

(2) If 12 yards at London make 8 clis at Paris, how many, ells at Paris will make 64 yards at London ? Ans. $42\frac{2}{3}$

	Answer.Proof.448 at $12d. = 576$ As224 at $10d. = 240$ As224 at $6d. = 144$ 448 at $4d. = 192$	1b. 1b.
• 12	4 48 at $12d. = 576$ As	12:4::144:48
°10	2 24 at $10d. = 240$ As	12:2::144:24
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VULGAR FRACTIONS.

82

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(3) If 30 *lb* at London make 28 *lb*. at Amsterdam, how many *lb*. at London will be equal to 350 *lb*. at Amsterdam? Ans. 375.

(4) If 95 *lb*. Flemish make 100 *lb*. English, how many *lb*. English are equal to 275 *lb*. Flemish? Ans. 289_{19}

PERMUTATION

Is the changing or varying of the order of things.

To find the number of changes that may be made in the position of any given number of things.

RULE. Multiply the numbers 1, 2, 3, 4, &c., continually together, to the given number of terms, and the last product will be the answer.

(1) How many changes may be rung upon 12 bells, and n what time would they be rung, at the rate of 10 changes in a minute, and reckoning the year to contain 365 days, 6 hours?

 $1 \times 2 \times 3 \times 4 \times 5 \times 6 \times 7 \times 8 \times 9 \times 10 \times 11 \times 12 = 479001600$ changes, which $\div 10 = 47900160$ minutes = 91 years, 26 days, 6 hours.

(2) A young scholar, coming to town for the convenience of a good library, made a bargain with the person with whom he lodged, to give him $\pounds 40$. for his board and lodging during so long a time as he could place the family (consisting of 6 persons besides himself) in different positions, every day at dinner. How long might he stay for his $\pounds 40$.?

Ans. 5040 days.

VULGAR FRACTIONS.

DEFINITIONS.

1. A Fraction is a part or parts of a unit, or of any whole number or quantity; and is expressed by two numbers, called the *terms*, with a line between them.

2. The upper term is called the Numerator, and the lower term, the Denominator. The Denominator shows into how

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VULGAR FRACTIONS.

many equal parts unity is divided and the Numerator is the number of those equal parts signified by the Fraction.*

8. Every Fraction may be understood to represent Division; the Numerator being the dividend, and the Denominator the divisor.

Fractions are distinguished as follows:

4. A SIMPLE FRACTION consists of one numerator and one denominator: as $\frac{3}{4}$, $\frac{1}{12}$, &c.

5. A COMPOUND FRACTION, or fraction of a fraction, consists of two or more fractions connected by the word of: as $\frac{1}{2}$ of $\frac{3}{5}$ of $\frac{7}{12}$, &c. This properly denotes the *product* of the several fractions.

6. A PROPER FRACTION is one which has the numerator less than the denominator: as $\frac{1}{4}$, $\frac{2}{4}$, $\frac{3}{4}$, $\frac{11}{12}$, &c.[‡]

7. An IMPROPER FRACTION is one which has the numerator either equal to, or greater than the denominator: as $\frac{4}{4}$, $\frac{5}{4}$, $\frac{5}{12}$, $\frac{15}{2}$, &c.‡

8. A MIXED NUMBER is composed of a whole number and a fraction, as $1\frac{2}{3}$, $17\frac{1}{2}$, $8\frac{7}{94}$, &c.

9. A COMPLEX FRACTION has a fractional numerator or denominator: but this denotes Division of Fractions. Thus, $\frac{2}{3}$, two-thirds divided by five-sixths, $\frac{8}{1\frac{2}{3}}$, eight divided by one and two-thirds.

* In the fraction five-twelfths $(\frac{5}{12})$ the Denominator 12 shows that the unit or whole quantity is supposed to be divided into 12 equal parts : so that if it be one shilling, each part will be one-twelfth of 1s, or one penny. The Numerator shows that 5 is the number of those twelfth parts intended to be taken : so $\frac{5}{12}$ of a shilling are the same as 5 pence ; $\frac{5}{12}$ of a foot, the same as 5 inches.

[†] The fraction $\frac{5}{12}$ signifies not only $\frac{5}{12}$ of a unit, but 5 units divided into 12 parts, or a twelfth part of five : and it is obvious that *five* twelfth parts of one shilling (or five pence) is the same as one. twelfth part of five shillings. This mode of considering Fractions temoves many of the student's difficulties.

[†] A proper fraction is always less than unity: thus ³/₄ wants one fourth, and $\frac{11}{12}$ wants one-twelfth of being equal to 1. But an improper fraction is equal to unity when the terms are equal, and greater than unity when the numerator is we greater.

Thus 4, or $\frac{11}{12}$, or $\frac{13}{33}$, is each =1; and $\frac{1}{123}$ $\frac{1}{23} = 3\frac{2}{30}$.

VULGAR FRACTIONS.

84

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TUTOR'S

10. A COMMON MEASURE (or DIVISOR) is a number that will exactly divide both the terms. When it is the greatest number by which they are both divisible, it is called the GREATEST COMMON MEASURE.

Note. A prime number has no factor, except itself and unity.

A multiple signifies any product of a number; and is therefore divisiblo by the number of which it is a multiple: thus 14, 21, 28, &c., are multiples of seven. Also 14 is a common multiple of 2 and 7; 21, of 3 and 7, &c.

REDUCTION

Is the method of changing the form of fractional numbers or quantities, without altering the value.

Case 1. To reduce a fraction to its lowest terms.

RULE. Divide both the terms by any common measure that can be discovered by inspection; which will produce an equivalent fraction in lower terms. Treat the new fraction in a similar manner; repeating the operation till the lowest terms are obtained."

When the object cannot be accomplished by this process, divide the greater term by the less, and that divisor by the remainder, and so on till nothing remains. The last divisor will be the greatest common measure; by which divide both terms of the fraction, and the quotients will be the lowest terms.

	Reduce $\frac{3.0}{1.25}$ to its lowest terms.	Ans. 1.
(2)	Reduce $\frac{2}{6} \frac{0}{8} \frac{1}{4}$ to its lowest terms.	Ans. Ary.
(3)	Reduce $\frac{192}{576}$ to the least terms.	Ans. 1.
(4)	Reduce $\frac{325}{6}$ to the least terms.	Ans. \$.
(5)	Abbreviate $\frac{5}{6}\frac{1}{2}\frac{5}{2}$ as much as possible.	Ans. $\frac{3}{4}$.
(6)	Reduce $\frac{12549}{21045}$ to its lowest terms.	Ans. 4.

* This first method of *abbreviating* fractions is, when practicable, always to be preferred: and in the application of it, the following obaervations will be found exceedingly useful.

An even number is divisible by 2.

A number is divisible by 4, when the *tens* and *units* are so; and by 3, when the *hundreds*, *tens*, and *units* are divisible by 8.

A number is a multiple of 3, or of 9, when the sum of its digits is a multiple of 3, or of 9.

A 5 or a 0 in the units' place, admits of division by 5; one cipher ad mits of division by 10, two, by 100, Sec. (7 (8)

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REDUCTION.

(7) Reduce $\frac{p \cdot p \cdot 7 \cdot 1 \cdot 5}{1 \cdot 1 \cdot 3 \cdot 9 \cdot 6 \cdot 5}$ to the lowest terms. Ans. 7 (8) What are the lowest terms of $\frac{3 \cdot 1 \cdot 9 \cdot 9}{3 \cdot 5 \cdot 5 \cdot 2}$? Ans. 7.

Case 2. To reduce an improper fraction to its equivalent number.

RULE. Divide the upper term by the lower.

This is evident from Definition 3.

(1)	Reduce	12° to a mixed number. 12°	=183. Ans.
(2)	Reduce	$\frac{69}{3}$ to its equivalent number.	Ans. 13 _‡ .
		² ⁴ / ₅ to its equivalent number.	Ans. 274.
(4)	Reduce	$1\frac{2}{2}\frac{4}{3}5$ to its equivalent number.	Ans. 5613.
(5)	Reduce	$3\frac{9}{24}$ to its equivalent number.	Ans. 1837.
(6)	Reduce	$1\frac{1}{18}$ to its equivalent number.	Ans. 711.

Case 3. To reduce a mixed number to an improper fraction.*

Ruiz. Multiply the whole number by the denominator of the fraction, and to the product add the numerator for the numerator required, which place over the denominator.

Note. Any whole number may be expressed in a fractional form by putting 1 for the denominator : thus $11 = \frac{1}{4}$.

(1) Reduce 183 to the form of a fraction.

A number is a multiple of 11, when the sum of the 1st, 3d, 5th, &c., digits = that of the 2d, 4th, 6th, &c., digits, after retrenching the elevens contained in each.

A multiple of both 2 and 3 is, of course, a multiple of 6; and a multiple of 3 and 4 may be divided by 12.

All prime numbers, except 2 and 5, have 1, 3, 7, or 9, in the units' place: all others are composite.

EXAMPLES.

(1) Reduce $\frac{1820}{1820}$ to the least terms possible. $\div 10 \div 9 \div 2$	Now, because we cannot easily discover a common measure pro- ceed thus :
$\frac{1200}{1626} = \frac{120}{162} = \frac{14}{18} = \frac{7}{6}.$ Ans. (2) Reduce $\frac{12540}{21045}$ to the lowest terms.	76)133(1 then 19)76 76 19)133 = 4 . Ans.
$\begin{array}{c} 5 \\ \frac{1}{2540} \\ \frac{12540}{11048} \\ = \\ \frac{2508}{1380} \\ = \\ \frac{336}{1483} \\ = \\ \frac{76}{133}. \end{array}$	57)76(1 <u>57</u>
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 $18\frac{3}{7} = \frac{18 \times 7 + 3}{7} = 1\frac{29}{7}$. Ans.

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VULGAR FRACTIONS.

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(2) Reduce $56\frac{13}{22}$ to an improper fraction.	Ans. 1245.
(3) Reduce $183\frac{5}{21}$ to an improper fraction.	Ans. 3 8 4 8.
(4) Reduce $13\frac{4}{5}$ to its equivalent fraction.	Ans. 9.
(5) Reduce 27 ² / ₆ to its equivalent fraction.	Ans. 245.
(6) Reduce 514.5 to a fractional form.	Ans. 8229.

To reduce a fraction to another of the same value, Case 4. having a certain proposed numerator or denominator.

Rule. As the present numerator is to the denominator, so is the proposed numerator to its denominator. Or, as the present denominator is to the numerator, so is the proposed denominator to its numerator.

(1) Reduce 2 to a fraction of the same value, whose numerator shall be 12. As 2:3::12:18. Ans. $\frac{12}{14}$.

(2) Reduce 5 to a fraction of the same value, whose nu merator shall be 25. Ans. 25.

(3) Reduce $\frac{5}{7}$ to a fraction of the same value, whose nu merator shall be 47. Ans. $\frac{1}{65\frac{4}{5}}$.

(4) Reduce 2 to a fraction of the same value, whose denominator shall be 18. Ans. $\frac{12}{18}$.

(5) Reduce 5 to a fraction of the same value, whose denominator shall be 35. Ans. 25.

(6) Reduce $\frac{3}{9}$ to a fraction of the same value, whose de-Ans. $\frac{16\frac{3}{9}}{19}$. nominator shall be 19.

Case 5. To reduce complex and compound fractions to a simple form.

RULE. For a complex fraction, reduce both terms to simple fractions: then by inverting the lower fraction, they may be considered as the terms of a compound fraction. And to reduce a compound fraction, arrange all the numerators above a line, and the denominators below, with the signs of multiplication interserted; divide all the upper and lower terms that are *commensurable*,* cancelling them with a dash, and placing their quotients above and below them respectively. Do the same with the quotients: then the products of the uncancelled numbers will give the single fraction in its lowest terms.

† This rule is of the highest importance as tending to expedite the **t**

^{*} That is, having a common divisor.

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iose nu- $15. \frac{12}{18}$ nose nu IS. 25. hose nu 47 $\cdot \overline{65\frac{4}{5}}$ hose de $is. \frac{12}{18}.$ hose de $vs. \frac{25}{35}.$ hose de- $\frac{16\frac{3}{9}}{19}$.

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fractions: ed as the raction, ar. ors below, upper and dash, and . Do the d numbers

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(1)	Reduce	$\frac{36\frac{2}{3}}{48}$	to a	simple	fraction.	Ans. 55.
(2)	Reduce	$\frac{23\frac{5}{4}}{38}$	to a	simple	fraction.	Ans. 133.
(3)	Reduce	$\frac{47}{65\frac{4}{5}}$	to a	simple	fraction.	Ans. §.
(4)	Reduce	$\frac{19}{44\frac{1}{3}}$	to a	simple	fraction.	Ans. 3.
(5) (6)	Reduce Reduce	23 of 55 of	3 01 4 01		a simple fraction.	Ans. 1 . Ans. 55 .

siness of computation, by a reviating to the utmost all fractional expressions, as we proceed.

EXAMPLES.

(1) Reduce the *complex* fraction $\frac{7\frac{1}{3}}{8\frac{5}{6}}$ to a simple form.

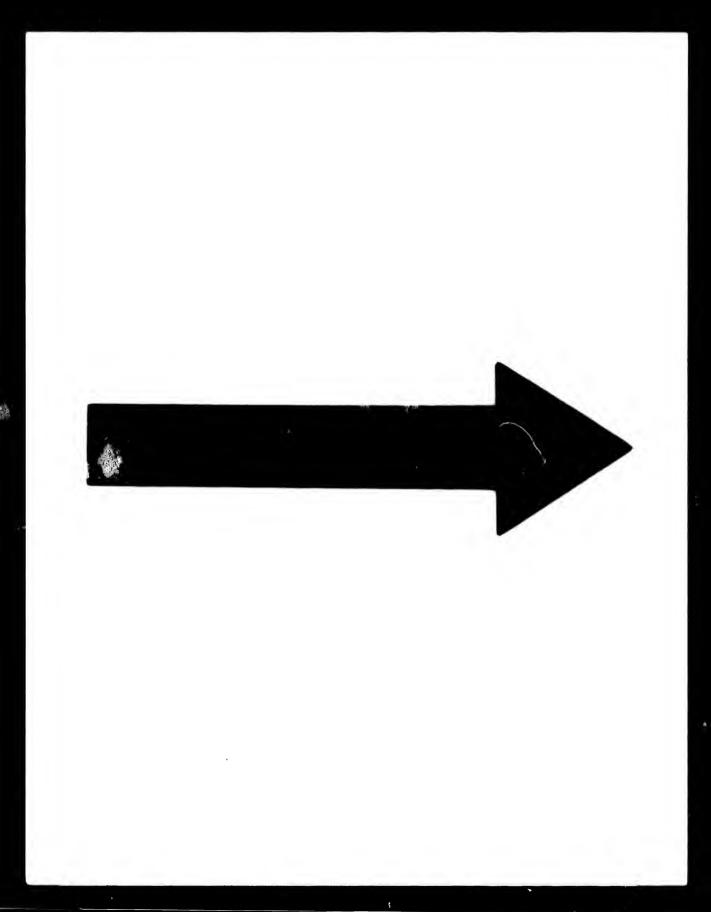
$$\frac{\frac{7_{\frac{1}{3}}}{8_{\frac{5}{9}}}}{\frac{7_{\frac{1}{3}}}{9}} = \frac{\frac{2}{2} \frac{3}{2}}{\frac{2}{2} \times \frac{9}{9}}{\frac{3 \times \pi}{1}} = \frac{6}{7} Ans.$$

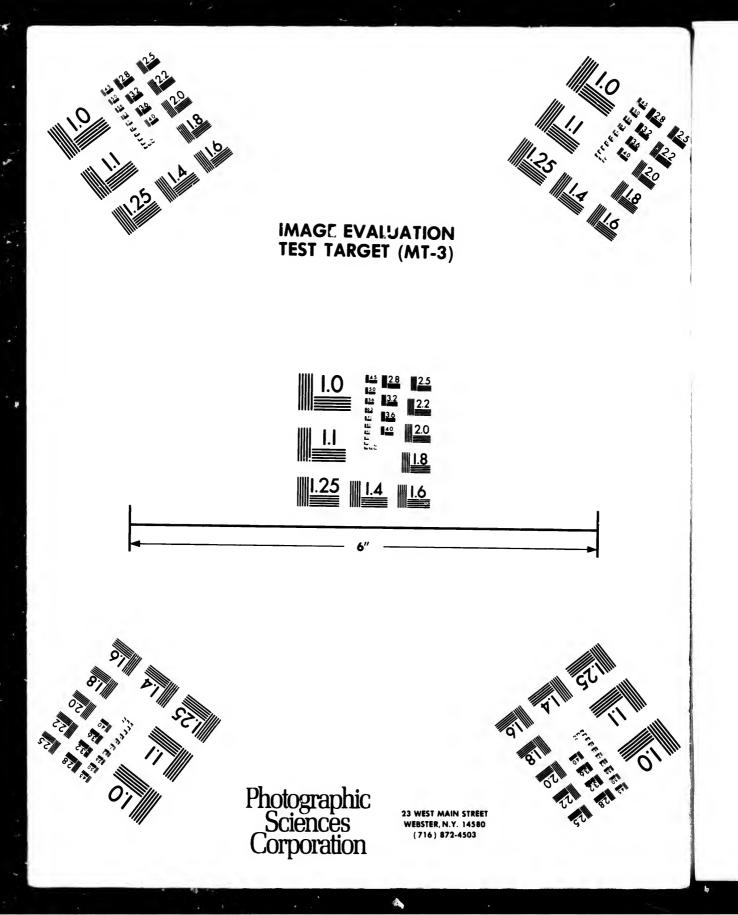
(2) Reduce $\frac{9}{10}$ of $\frac{2}{3}$ of $\frac{7}{8}$ of $\frac{5}{14}$ to a simple fraction.

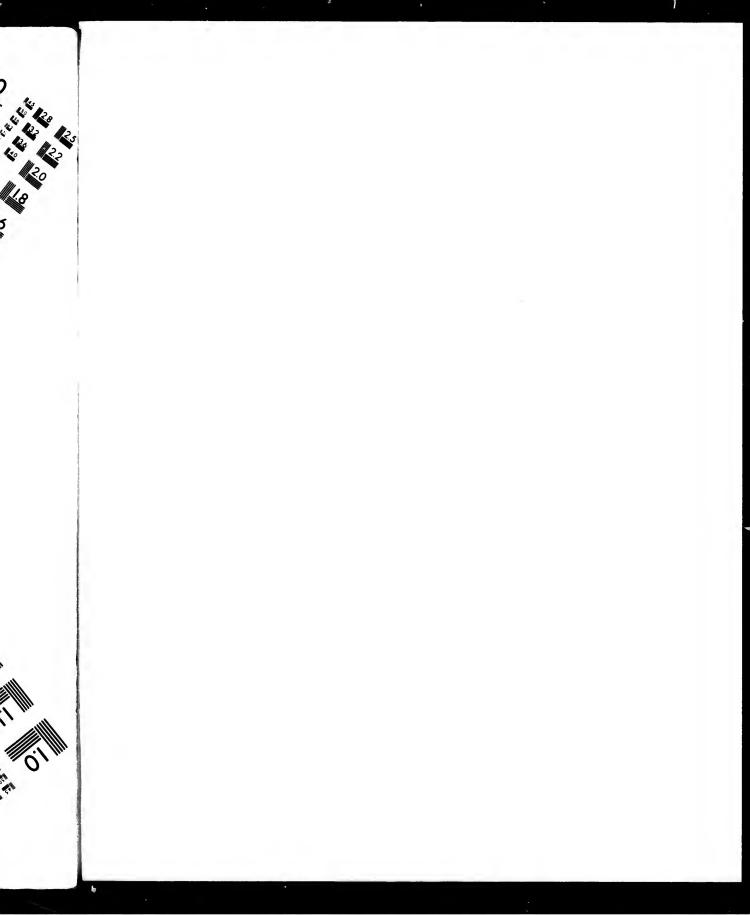
$$\frac{3}{10}$$
 of $\frac{2}{3}$ of $\frac{7}{8}$ of $\frac{5}{14} = \frac{\frac{3}{9} \times \frac{1}{2} \times \frac{1}{7} \times \frac{1}{5}}{\frac{1}{4} \times \frac{3}{2} \times \frac{3}{16} \times \frac{3}{16} \times \frac{3}{16}} = \frac{3}{16}$. Ans.

(3) Reduce the annexed fractional expression to its proper quanpiny.

$$\frac{16}{11} \text{ of } \frac{111\frac{9}{13}}{108} \text{ of } \frac{\frac{72}{147}}{\frac{18}{25}} \text{ of } \frac{6\frac{8}{15}}{24\frac{8}{13}} \text{ of } \frac{\pounds}{8\frac{5}{64}} = \frac{16}{11} \times \frac{1452}{13} \times \frac{72}{147} \times \frac{98}{15} \times \frac{567}{64} \\
= \frac{1}{11} \frac{1}{125} \times \frac{1}{25} \times \frac{98}{13} \times \frac{567}{64} = \frac{1}{11} \times \frac{1}{10} \times \frac{1}{10} \times \frac{1}{10} \times \frac{1}{10} \times \frac{98}{13} \times \frac{567}{64} \\
= \frac{1}{14} \frac{1}{124} \times \frac{9}{15} \times \frac{5}{14} \times \frac{9}{15} \times \frac{98}{13} \times \frac{567}{64} = \frac{1}{11} \times \frac{1}{10} \times \frac{1}{10} \times \frac{1}{10} \times \frac{98}{13} \times \frac{567}{64} \\
= \frac{1}{14} \frac{1}{124} \times \frac{9}{15} \times \frac{5}{13} \times \frac{98}{15} \times \frac{1}{125} \times \frac{98}{13} \times \frac{5}{13} \times \frac{567}{64} = \frac{1}{13} \times \frac{1$$







VULGAR FRACTIONS.

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- (7) Reduce $\frac{1}{14}$ of $\frac{13\frac{2}{5}}{14\frac{4}{5}}$ of $\frac{28}{38\frac{2}{5}}$ to a simple fraction. Ans. 117. (8) Reduce $\frac{3}{4}$ of $\frac{6}{9T}$ of $11\frac{3}{8}$ to a single fraction. Ans. $\frac{6}{18}$. (9) Reduce $\frac{77}{128}$ of $37\frac{1}{3}$ of 5 to its equivalent number.
- Ans. 1127. (10) Reduce $\frac{1}{14}$ of $2\frac{3}{3}$ of $\frac{1}{4}$ to its equivalent number. Ans. 74,

Case 6. To reduce a fractional quantity of a given denomina tion to an equivalent fraction of another denomination.

RULE. Consider what numbers would reduce the greater denomins tion to the less; then to reduce to a greater name, multiply the denom inator by those numbers, and to reduce to a less name, multiply the *mimerator*: the compound thus produced, when reduced to a simple form, will be the fraction required.

- (1) Reduce 7 of a penny to the fraction of a pound.*
- (2) Reduce $\frac{3}{4}d$. to the fraction of a crown. Ans. $\frac{1}{56}$ cr.

(3) Reduce 4 divis. to the fraction of a lb. troy. Ans. $\frac{1}{24\pi}$ lb

(4) Reduce 4 lb. avoirdupois to the fraction of a cwt. Ans. $\frac{1}{190}$ cwt.

(5) Reduce $15^{\frac{7}{20}}$ of a pound to the fraction of a penny.

(6) Reduce $\pounds_{3\frac{1}{2}\overline{0}}$, to the fraction of a penny. Ans. $\frac{3}{4}d$.

(7) Reduce $\frac{1}{3b}$ of a pound troy to the fraction of a penny-weight. Ans. 4 dwt.

(8) Reduce $\frac{1}{160}$ cwt. to the fraction of a lb. Ans. 4 lb.

Case 7. To find the proper value of a fractional quantity.

RULE. Reduce the numerator to such lower denomination as may be necessary, and divide by the denominator; abbreviating as much as possible in valuing the remainders.

Note. It is evident, from Definition 3, that this Case is precisely that of Compound Division.

(1) Reduce 3 of a pound sterling to its proper value.

•
$$\frac{7}{16} = \frac{7}{8 \times 12 \times 20} = \mathcal{L}_{1\overline{10}20}^{7}$$
. Ans.
+ $\mathcal{L}_{1\overline{10}20}^{7} = \frac{7 \times 20 \times 12}{1920} = \frac{7 \times 12}{96} = \frac{7}{8}d$. Ans.
+ $\mathcal{L}_{1\overline{1}}^{7} = \frac{3 \times 20}{4} = 3 \times 5 = 15s$. Ans.

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REDUCTION.

(2) Reduce §s. to its proper value. Ans. 4d. 3§ qrs.
(3) Reduce 4 of a lb. avoirdupois to its proper value.

Ans. 9 oz. 24 dr

(4) Reduce $\frac{1}{2}$ cwt. to its proper value. Ans. 3 qrs. $3\frac{1}{2}$ lb (5) Reduce $\frac{3}{2}$ of a lb. troy to its proper value.

Ans. 7 oz. 4 dwt.

(5) Reduce $\frac{14}{25}$ of an ell English to its proper value. Ans. 2 grs. $3\frac{1}{5}$ naise.

(7) What is the value of $\pm \frac{5}{2} \frac{7}{18}$ Ans. 19s. 101 1

(8) Reduce $\frac{235}{352}$ of a mile to its proper value. Ans. 6 fur. 105 yds.

(9) Reduce $\frac{73}{48}$ of an acre to its proper value.

Ans. 1 a. 2 r. 31 per.

(10) Find the value of $\frac{15487}{15487}$ cwt. Ans. 1 qr. 22 lb. $\frac{2377}{1387}$.

Case 8. To reduce any given quantity to the fraction of a greater denomination.

BULE. Reduce the given quantity (if compound) to the lowest denomination mentioned, that it may assume a simple form: then multiply the denominator, as in Case 6.

(1) Reduce 15s. to the fraction of a pound sterling. $15s = \mathcal{L}_{\frac{1}{2}} = \mathcal{L}_{\frac{3}{4}}^{2}$. Ans.

(2) Reduce 4d. 31 qrs. to the fraction of a shilling. Ans. 3

(3) Reduce 9 oz. 24 dr. to the fraction of a lb. avoirdupois Ans. 4 lb.

(4) Reduce 3 qrs. 31 lb. to the fraction of a cwt.

(5) Reduce 7 oz. 4 dwts. to the fraction of a lb. troy.

Ans. 3 lb. (6) Reduce 2 qrs. 31 nails to the fraction of an English all. Ans. 3 ell.

(7) Reduce 14s. $6\frac{1}{2}d$. $\frac{2}{11}$ to the fraction of a £.

Ans. £ B.

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(8) Reduce 4d. $1\frac{1}{15}$ qrs. to the fraction of a crown. Ans. $\frac{29}{305}$ cr.

(9) What fraction of an acre are 3 roods, 32 perches?

Ans. 18 a.

(10) What part of a shilling are $\frac{2}{3}$ of 2d. Ans. $\frac{1}{3}s$

Case 9. To find the least common multiple of two or more numbers.

RULE. Arrange the given numbers in a line, (omitting any one that is a factor of one of the others,) and divide any two or more of them by semmon divisor, placing the quotients and undivided numbers below;

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proceed with these in the same manner, and repeat the process till there remain not any two numbers *commensurable*: the continued product of the divisors, quotients, and undivided numbers, will be the least common multiple.

(1) Required the least common multiple of 2, 3, 4, 5, 6, 7, 9, and 10.*

(2) Find the least number divisible by 3, 4, 5, 6, 7, and 8. Ans. 840.

(3) What is the least common multiple of 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, and 12? Ans. 27720.

Case 10. To reduce fractions to a common denominator.

RULE 1. Multiply each numerator into all the denominators, except its own, for a numerator; and all the denominators for a common denominator. Or,

RULE 2. Find the *least common multiple* of the denominators, which will be the *least common denominator*. Divide this by each denominator, and multiply the several quotients by the respective numerators for the required numerators.

- (1) Reduce $\frac{2}{4}$ and $\frac{4}{4}$ to a common denominator.
- (2) Reduce $\frac{1}{2}$, $\frac{3}{4}$, and $\frac{5}{8}$, to a common denominator.

Ans. $\frac{32}{64}$, $\frac{48}{64}$, and $\frac{49}{64}$; or $\frac{4}{8}$, $\frac{9}{8}$, and $\frac{5}{8}$.

(3) Reduce $\frac{7}{6}$, $\frac{4}{6}$, $\frac{6}{16}$, and $\frac{6}{7}$, to a common denominator. Ans. $\frac{7}{840}$, $\frac{5}{840}$, $\frac{5}{840}$, and $\frac{72}{720}$.

- (4) Reduce $\frac{3}{5}$, $\frac{1}{2}$, and $\frac{1}{7}$, to a common denominator.
- (5) Reduce $\frac{3}{17}$, $\frac{4}{7}$, and $\frac{3\frac{1}{2}}{15}$ of 2, to a common denominator. Ans. $\frac{315}{155}$, $\frac{660}{1555}$, and $\frac{39}{1555}$.

(6) Reduce $1\frac{1}{4}$, $2\frac{1}{5}$, and $\frac{1}{3}$ of $1\frac{1}{4}$, to a common denominator. Ans. $\frac{75}{60}$, $\frac{139}{60}$, and $\frac{25}{60}$.

* 2 and 4, being factors of 8, 3 a factor of 9, and 5 a factor of 10, may be omitted. Thus,

2)6,	7,	8,	9,	10
3)3,	7,	4,	9,	5
1,	7,	4,	3,	5

Then $2 \times 3 \times 7 \times 4 \times 3 \times 5 = 42 \times 60 = 2520$, the least number divisible by all the given numbers.

 $\begin{array}{c} 1 & 2 \times 7 = 14 \\ 4 \times 4 = 16 \\ 4 \times 7 = 28 \end{array}$ numerators. Ans. $\frac{14}{28}$ and $\frac{16}{38}$

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SUBTRACTION.

ADDITION.

RULE. Reduce the given fractions to a common denominaton over which place the sum of the numerators.

(1) Add $\frac{3}{3}$ and $\frac{9}{4}$ together. $\frac{3}{3}$ +	$\frac{1}{2} = \frac{1}{2} + \frac{1}{2} + \frac{1}{2} = \frac{2}{2} + \frac{1}{2} = \frac{3}{2} + \frac{3}$
(2) Add $\frac{3}{4}$, $\frac{2}{7}$, and $\frac{5}{6}$.	(6) Add $5\frac{2}{3}$, $6\frac{7}{8}$, and $4\frac{1}{3}$.
	(7) Add $1\frac{4}{9}$, $3\frac{1}{7}$, and $\frac{1}{2}$ of 7.
(4) Add 73 and 3 together.	(8) Add $\frac{9}{10}$ of $6\frac{7}{8}$, and $\frac{4}{4}$ of $7\frac{1}{4}$.
(5) Add 4, and 3 of 3.	(9) Add $\frac{1}{5}$ of $9\frac{3}{8}$, and $\frac{2}{3}$ of $4\frac{5}{8}$.
Fractional quantities may be	reduced to their proper values.

their proper values, and the sum found by Compound Addition.

(10) Add $\frac{a}{b}$ of a pound to $\frac{5}{6}$ of a shilling. Ans. Ss. 4d. (11) Add $\frac{1}{2}d$. $\frac{5}{8}s$. and $\pounds_{\frac{2}{3}}^2$. Ans. 14s.

(12) Add $\frac{3}{5}$ lb. troy, $\frac{1}{6}$ oz. and $\frac{5}{4}$ oz.

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Ans. 7 oz. 19 dwts. 20 gr.

(13) Add 4 of a ton to $\frac{5}{6}$ of a cwt.

Ans. 12 cwt. 1 $qr. 1\frac{1}{4}$ lb.

(14) What is the sum of $\frac{2}{3}$ of £17..7..6d., $\frac{4}{5}$ of £1 $\frac{2}{3}$. and ? of a crown? Ans. $\pounds 13..0..2\frac{1}{2}$.

(15) Add $\frac{4}{5}$ of 3 a. 1 r. 20 p., $\frac{3}{5}$ of an acre, and $\frac{3}{4}$ of 3 roods, 15 perches. Ans. 3 a. 2 r. $33\frac{1}{2}$ p.

SUBTRACTION.

RULE. Reduce the given fractions to a common denominator, over which place the *difference* of the numerators.

When the numerator of the fractional part in the subtrahend is greator than the other numerator, borrow a fraction equal to unity, having the common denominator; then subtract, and carry one to the integer of the subtrahend.

(1) From $\frac{3}{4}$ take $\frac{5}{4}$. $\frac{3}{4} - \frac{5}{2} = \frac{2}{21} - \frac{2}{218} = \frac{1}{218}$. Ans.

- (2) From $\frac{5}{6}$ take $\frac{3}{5}$. (3) From $5\frac{2}{3}$ take $\frac{9}{10}$ of $\frac{5}{8}$. (6) From $64\frac{1}{4}$ take $\frac{2}{3}$ of $\frac{2}{3}$. (7) From $15\frac{1}{8}$ take $12\frac{7}{40}$.

- (4) From $\frac{38}{45}$ take $\frac{3}{5}$ of $\frac{1}{3}$. (8) Subtract $\frac{23}{55}$ from $\frac{13}{5}$. (5) From $\frac{19}{26}$ take $\frac{1}{7}$ of $\frac{9}{3}$. (9) Subtract $\frac{17}{21}$ from $\frac{1}{8}$ of 9.

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Fractional quantities may be reduced to their proper values, as directed in Addition

* When there are integers among the given numbers, first find the sum of the fractions, to which add the integers.

Thus in Ex. 3, $\frac{1}{5} + \frac{2}{5} = \frac{3}{5}$; then $\frac{3}{5} + \frac{1}{5} = \frac{9}{5} + \frac{5}{5} - \frac{14}{15}$; and $4 + \frac{14}{15} = \frac{9}{5} + \frac{5}{5} - \frac{14}{15}$; 414. Ans.

VULGAR FRACTIONS.

TUTOR'S

(10) From 3 of a pound take 3 of a shilling. Ans. 7s. 11d

(11) From 13.5. take $\frac{2}{3}$ of $7\frac{1}{2}d$. Ans. 1s. 3d.

(12) What is the difference between $\frac{3}{4}$ of $\pounds 1_{\frac{5}{4}}$; and $Ans. 2d. 3\frac{1}{4} qrs.$

(13) Subtract $\frac{5}{5}$ cwt. from $\frac{4}{5}$ ton. Ans. 10 cwt. 2 qrs. $10\frac{2}{3}$ lb. (14) From $\frac{2}{5}$ of 5 lb. troy subtract $\frac{5}{5}$ of $3\frac{1}{2}$ oz.

Ans. 3 lb. 2 oz. 1 dwt. 23 gr.

(15) Subtract $7\frac{1}{230}$ furlongs from $1\frac{5}{11}$ mile.

Ans. 4 fur. 9 yds.

MULTIPLICATION.

RULE. Prepare the given numbers (if they require it) by the rules of Reduction: then multiply all the numerators together for the numerator of the *product*, and all the denominators for the denominator.

(1) Multiply $\frac{3}{4}$ by $\frac{3}{3}$. $\frac{3}{4} \times \frac{3}{2} = \frac{9}{26}$. Ans. (2) Multiply $\frac{7}{4}$ by $\frac{3}{3}$. $\frac{3}{4} \times \frac{3}{2} = \frac{9}{26}$. Ans. (3) Multiply $\frac{1}{4}$ by $\frac{3}{2}$. (6) Multiply $\frac{1}{4}$ of $\frac{3}{4}$ by $\frac{5}{4}$. (4) Multiply $430\frac{3}{5}$ by $13\frac{5}{6}$. (7) Multiply $5\frac{4}{7}$ by $\frac{5}{6}$. (4) Multiply $430\frac{3}{5}$ by $18\frac{3}{4}$. (8) Multiply 24 by $\frac{3}{2}$. (5) Multiply $\frac{1}{24}$ by $\frac{3}{4}$ of $\frac{5}{7}$. (9) Multiply $\frac{3}{4}$ of 9 by $\frac{7}{6}$. (10) Multiply $\pounds 3..15..9\frac{1}{4}\frac{1}{5}$ by $\frac{9}{71}$ of 5. Ans. $\pounds 15..9..11\frac{3}{4}\frac{9}{11}$. (11) Multiply $3\frac{14}{4}$ miles by $\frac{4}{7}$ of $4\frac{3}{2}\frac{7}{6}$. Ans. 8 m. 2 f. 1884 yds. (12) Required the product, in square feet, of 14 ft. 7 in. by 8 ft. 9 in. Ans. $127\frac{2}{49}$ sq. ft.

DIVISION.

RULL. Frepare the given numbers (if they require it) by the rules of Reduction; then *invert the divisor*, and proceed as in Multiplication.

(1) Divide $\frac{9}{26}$ by $\frac{3}{5}$.† (2) Divide $\frac{14}{14}$ by $\frac{5}{6}$. (3) Divide $7935\frac{2}{36}$ by $13\frac{5}{6}$. (4) Divide $7935\frac{2}{46}$ by $18\frac{3}{5}$. (5) Divide 16 by 24. (6) Divide $\frac{16}{16}$ by $\frac{4}{12}$. (7) Divide $\frac{441}{936}$ by $\frac{3}{10}$ of $\frac{10\frac{1}{2}}{\frac{7}{5}}$. (8) Divide $9\frac{1}{6}$ by $\frac{1}{2}$ of 7. (9) Divide $\frac{3}{6}$ by $\frac{2}{3}$ of $\frac{3}{4}$ of $\frac{5}{6}$. (10) Divide $\frac{2}{3}$ of 16 by $\frac{2}{7}$ of $\frac{3}{4}$.

• A number inverted becomes the reciprocal of that number: which is the quotient arising from dividing unity by the given num ber: thus $1\div 7=\frac{1}{2}$, the reciprocal of 7; $1+\frac{3}{3}=\frac{5}{2}$, the reciprocal of $\frac{3}{3}$.

 $\frac{1}{2}\frac{9}{20} + \frac{3}{4} = \frac{9}{20} \times \frac{5}{3} = \frac{3}{4}$ Ans.

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RULE OF THREE.

(11) Divide £112462 by 32 of 12. Ans. £3.17.101 2.

(12) Divide 1s. $4\frac{1}{3}d.\frac{5}{6}$ by $\frac{2}{3}$ of $\frac{18}{5}$. Ans. 6d. $3\frac{6}{12}qrs.$

(13) Divide 3 qrs. $24\frac{15}{15}$ lb. by $\frac{7}{15}$ of $1\frac{1}{2}$, in the fraction of **a** *cwt.*; and value the quotient. Ans. 1 *cwt.* 1 *qr.* 155 *lb.* (14) What must £7..14..6. be multiplied by, to produce £21..17..9? Ans. $2\frac{1}{2}$.

THE RULE OF THREE.

Rule. Prepare the terms, previous to stating, so that no subsequent Reduction will be necessary: then, having stated the question, as previously directed, *invert the dividing term*, and the continued product of the three will be the answer.

(1) If $\frac{3}{4}$ of a yard cost $\mathcal{L}_{\frac{5}{8}}^{5}$, what will $\frac{9}{10}$ of a yard cost?

(2) If $\frac{5}{6}$ yd. cost $\pounds_{\frac{2}{3}}^2$ what will $\frac{1}{1\frac{1}{2}}$ yd. cost ? Ans. 14s. 8d (3) If $\frac{3}{4}$ of a yard of lawn cost 7s. 3d. what will $10\frac{1}{4}$ yards

Ans. $\pounds 4..19..10\frac{1}{2}\frac{2}{3}$,

(4) If $\frac{7}{8}$ lb. cost $\frac{3}{4}s$. how much will $\frac{3}{8}s$. buy? Ans. $1\frac{1}{27}$ lb. (5) If 48 men can build a wall in 241 days, how many

men can do the same in 192 days? Ans. $6\frac{1}{16}$ men.

(6) If $\frac{3}{4}$ of a yard of Holland cost $\pounds_{\frac{1}{3}}$. what will $12\frac{2}{3}$ ells cost at the same rate? Aus. $\pounds 7.0.8\frac{3}{4}\frac{5}{9}$.

(7) If $3\frac{1}{4}$ yards of cloth, that is $1\frac{1}{5}$ yard wide, be sufficient to make a cloak, how much that is $\frac{4}{5}$ of a yard wide will make another of the same size? Ans. $4\frac{7}{5}$ yards.

(8) If $12\frac{1}{2}$ yards of cloth cost 15s. 9d. what will $48\frac{1}{4}$ yards cost at the same rate? Ans. $\pounds 3.0..9\frac{1}{2}\frac{4}{43}$.

(9) If $25\frac{2}{7}s$, will pay for the carriage of 1 cwt. 145 $\frac{1}{4}$ miles; how far may $6\frac{1}{2}$ cwt. be carried for the same money?

Ans. $22\frac{9}{26}$ miles.

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(10) If $\frac{9}{10}$ of a cwt. cost £14. 4s. what is the value of 74 cwt.? Ans. £118.6.8.

(11) If $\frac{3}{4}$ lb. of cochineal cost £1..5. what will $36\frac{7}{16}$, lb come to?

(12) How much in length that is 7_{16}^{3} inches broad will make a foot square ? Ans. 20_{145}^{4} inches.

(13) What is the value of 4 pieces of broadcloth, each 27 yards, at 15 s. per yard? Ans. £85..14..31 4.

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DECIMAL FRACTIONS.

(14) If a penny white loaf weigh 7 oz. where a bushel of wheat costs 5s. 6d. what is the bushel worth when a penny white loaf weighs but $2\frac{1}{2}$ oz.? Ans. 15s. 4d. $3\frac{1}{5}$ qrs.

(15) What quantity of shalloon that is $\frac{3}{4}$ of a yard wide will line $7\frac{1}{4}$ yards of cloth that is $1\frac{1}{4}$ yard wide? Ans. 15 yards.

(16) Bought $3\frac{1}{2}$ pieces of silk, each containing $24\frac{3}{4}$ ells, at 6s. $0\frac{3}{4}d$. per ell. How must I sell it per yard to gain £5. by the bargain? Ans. 5s. $9\frac{1}{4}d$. $\frac{3}{4}\frac{6}{5}\frac{6}{5}$.

THE DOUBLE RULE OF THREE.

(1) If a carrier receive $\pounds 2_{10}^{1}$, for the carriage of 3 *ewt*. 150 miles, how much ought he to receive for the carriage of 7 *cwt*. $3\frac{1}{2}$ qrs., 50 miles? Ans. £1..16..9.

(2) If £100. in 12 months gain £5¹/₄. interest, what principal will gain £3³/₈. in 9 months? Ans. £85..14..3¹/₄ 4.

(3) If 9 students spend $\pounds 10\frac{7}{9}$. in 18 days, how much will 20 students spend in 30 days? Ans. $\pounds 39..18..4\frac{2}{9}\frac{9}{1}$.

(4) Two persons carned $4\frac{5}{8}s$. for one day's labour: how much would 5 persons earn in $10\frac{1}{2}$ days, at the same rate? Ans. $\pounds 6..1..4\frac{3}{2}\frac{1}{4}$.

(5) If £50. in 5 months gain $\pounds 2_{\overline{144}}^{37}$, what time will $\pounds \overline{134}^{1}_{\overline{4}}$. require to gain $\pounds 1_{\overline{17}}^{1}$? Ans. 9 months.

(6) If the carriage of 60 cwt., 20 miles, cost $\pounds 14\frac{1}{2}$., what weight can I have carried 30 miles for $\pounds 5\frac{7}{16}$.? Ans. 15 cwt.

DECIMAL FRACTIONS.

IN Decimal Fractions the unit is supposed to be divided into tenths, hundredths, thousandth parts, &c., consequently the denominator is always 10, or 100, or 1000, &c.

In our system of Notation, the figures of a whole number follow each other in a decimal (or tenfold) proportion. Hence, the numerator of a decimal Fraction is written as a whole number, only distinguished by a separating point prefixed to it. Thus 5 for $\frac{1}{10}$, 25 for $\frac{1}{100}$, 123 for $\frac{1}{1000}$.

The denominator is, therefore, not expressed; being always understood to be 1, with as many ciphers affixed as there are places in the numerator.

The different values of figures will be evident in the an-

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DECIMALS

Integers of thous. 7 Millions.	Decimal parts. 5 5 7, Willionth parts. 5 Ten thous. parts. 2 Tenthous and th parts. 2 Tenth parts of unity.
s. ls. hous. s of thous.	t parts. nous. parts. 18. parts. 111 parts. 111 parts. 11 parts. uts of <i>unity</i> .

From this it plainly appears that the figures of the *dccimal* fraction decrease successively from left to right in a tenfold proportion, precisely as those of the *whole number*.*

Ciphers on the right of other decimals do not alter their value: for $2 = \frac{2}{100}$, $20 = \frac{200}{1000}$, $200 = \frac{200}{1000}$, are all equal. But one cipher on the left diminishes the value ten times, two ciphers, one hundred times, &c., for $02 = \frac{2}{1000}$, $002 = \frac{2}{1000}$, &c.

A vulgar fraction having a denominator compounded of 2, or 5, or of both, when converted into its equivalent decimal fraction, will be finite: that is, will terminate at some certain number of places. All others are *infinite*; and because they have one or more figures continually repeated without end, they are called *Circulating Decimals*. The repeating figures are called *repetends*.

One repeating figure is called a single repetend; as 222, &c.; generally written thus, 2'; or thus 2. But when more than one repeat, the decimal is a compound repetend; as 36, 36, &c., or 142857 142857, &c. These may be written 36', and 142857'; or 36, and 142857.

Pure repetends consist of the repeating figures alone; but mixed repetends have other figures before the circulating decimal begins : as .045', .96`354'.

Finite decimals may be considered as infinite, by making ciphers to recur, which do not alter the value.

Circulating decimals having the same number of repeating figures are called similar repetends, and those which have an unequal number are dissimilar. Similar and conterminous repetends begin and terminate at the same places.

^{*} The first, second, third, fourth, &c., places of decimals are called primes, seconds, thirds, fourths, &c., respectively; and decimals are read th '9: 57.57 fifty-seven, and five, seven, of a decimal; that is, fifty seven, and fifty-seven hundred ths. 206.043 two hundred and six, and nawy, four, three; that is, 206, and forty-three thousand the

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DECIMALS.

ADDITION.

RULE, Place the numbers so that the decimal points may stand to ... perpendicular line: then will units be under units, &c., according to their respective values. Then add as in integers.

- (1) Add $72 \cdot 5 + 32 \cdot 071 + 2 \cdot 1574 + 371 \cdot 4 + 2 \cdot 75$.
- (2) Add 30.07 + 2.0071 + 59.432 + 7.1.
- (3) Add $3\cdot 5 + 47\cdot 25 + 927\cdot 01 + 2\cdot 0073 + 1\cdot 5$.
- (4) Add 52.75+47.21+724+31.452+.3075.
- (5) Add $3275+27\cdot514+1\cdot005+725+7\cdot32$.
- (6) Add $27 \cdot 5 + 52 + 3 \cdot 2675 + \cdot 5741 + 2720$.

SUBTRACTION.

RULE. Place the subtrahend under the minuend with the decimal points as in Addition; and subtract as in integers.

(1) From 2754 take 2371.	(5) From 571 take 54.72.
	(6) From 625 take 76.91.
(3) From 271 take 215 7.	(7) From 23.415 take 3742
(4) From 270.2 take 75.4075.	(8) From 107 take 0007.

MULTIPLICATION.

RULE. Place the factors, and multiply them as in whole numbers, and in the product point off as many decimal places as there are in both factors together. When there are not so many figures in the product, supply the defect with ciphers on the left.

(1) Multiply 2.071 by 2.27.	(7) 27·35 × 7·70011	•
(2) Multiply 27.15 by 24.3.*	(8) 57.21 × .0075.	
(3) Multiply 2365 by 2435.		
(4) Multiply 72347 by 23.15.	(10) 20.15 × .2705,	
(5) Multiply 17105 by 3257.	(11)	
(6) Multiply 17105 by 0327.	$(12)^{\circ} \cdot 3409803 \times \cdot 001621$	8.

When the multiplier is 10, 100, 1000, &c., it is only removing the separating point in the multiplicand so many places towards the right as there are ciphers in the multiplier: thus, $578 \times 10 = 578$, $578 \times 100 = 578$, $578 \times 100 = 578$, and $578 \times 10000 = 5780$

CONTRACTED MULTIPLICATION.

RULZ. Write the multiplier under the multiplicand in an invested order, the units' figure under that place which is intended to be retained in the product.

• The 2nd example may be multiplied in two products, first by 3, and that product by 8 for 24. The 3rd, 6th, 7th, and 12th may be contracted in a similar way. etar and row hi arise rate incl N siree

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DIVISION.

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take 54.72. 5 take 76.91. 415 take 3742 7 take 0007.

whole numbers, there are in both is in the product,

× 7.70011. × .0075. × .007. × .2705.

× .0025.

× ·0016218.

nly removing the newards the right 10 = 5.78, $.578 \times 780$

nd in an inverted aded to be retain-

ducts, first by 3, 12th may be con In multiplying, begin with that figure of the multiplicand which stands over the multiplying figure, rejecting all on the right of that; and set down the first figures of all the products in a perpendicular row.

Increase the first figure of each product by carrying to it what would arise from multiplying the two next rejected figures on the right, at the rate of one from 5 to 14 inclusive, two from 15 to 24, three from 25 to 34 inclusive, &c.

Note. If perfect occuracy as far as the last decimal figure be desired, it will be eligible to find one figure more in the product than is actually wanted.

(13) Multiply 384.672158 by 3.683, and let there be only four places of decimals in the product.*

(14) Multiply 3.141592 by 52.7438, retaining only four places of decimals in the product. Ans. 165.6995.

(15) Multiply 238.645 by 8217.5, retaining only the integers in the product. Ans. 1961064.

place of decimals; and again, reserving three places.

Ans. 6276.9, and 6276.951.

(17) Multiply 395.3756 by .75642, retaining only four laces of decimals. Ans. 299.0700.

DIVISION.

DIVIDE as in integers, and the first figure of the quotient will be of the same value as that figure of the dividend which stands over the units in the first product of the divisor, so that the point must be placed accordingly; ciphers being prefixed, when necessary.

Note 1. After proceeding through the dividend, to ascertain if the quotient is correctly *pointed*, observe that the decimal places in the divisor and quotient together must equal in number those of the dividend. 2. When there are *fewer* decimal places in the dividend than in the divisor, *equalize* them by *affiring ciphers*; and the quotient, to *that extent*, will be a *whole* number.

Contracted method.	Common method
384-672158 386-3	384.672158 3.683
11540165	11540 16474
2308033	307737 7264
307738	2308032 948
11540	1154016474
1416 7476	1416 7475 57914

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3. Ciphers may be subjoined to the decimal part of the dividend, or brought down as if they were subjoined, in order to continue the operation to any degree of exactness desired.

(1) Divide 217.75 by 65.	$(7) 7382 \cdot 54 \div 6 \cdot 4252.$
(2) Divide 709 by 2.574.	$(8) \cdot 0851648 \div 423.$
(3) Divide 125 by 1045.	(9) $267 \cdot 15975 \div 13 \cdot 25$.
(4) Divide 48 by 144.	(10) 72.1564 \div .1347.
(5) Divide 5.714 by 8275.	(11) 85643·825 ÷ 6·321.
(6) Divide 715 by 3075.	$ (12)$ $1 \div 3.1416.$

To divide by 10, 100, 1000, &c., remove the separating point in the dividend so many places towards the left as there are ciphers in the divisor, and the thing is accomplished.

Thus $5784 \div 10 = 5784$, $5784 \div 100 = 5784$, $5784 \div 1000 = 5784$, $5784 \div 1000 = 5784$, $5784 \div 10000 = 5784$.

(13)	$3719 \div 10.$	(15) 130.7 ÷ 10	000.
(14)	$3719 \div 10.$ $3.74 \div 100.$	$(16) 34.012 \div 100$	000.

CONTRACTED DIVISION.

Ascertain the value of the first quotient figure, from which it will be known what number of figures in the quotient will serve the purpose required. Use that number of the figures in the divisor, (rejecting the others on the right,) and a sufficient number of the dividend, to find the first figure of the quotient; make each remainder a new dividual, and for each succeeding figure reject another from the divisor: but observe to earry to each product from the rejected figures, as in Contracted Multiplication.

Note. When there are *fewer* figures in the divisor than the number wanted in the quotient, proceed by the common rule till those in the divisor are just as many as remain to be found in the quotient, and then use the contraction.

(17) Divide 70.23 by 7.9863, to three places of decimals.

(18) Divide $721 \cdot 17562$ by $2 \cdot 257432$, to the extent of only three places of decimals in the quotient.

(19) Divide 25.1367 by 217.35, to the fourth decimal.

Common Method.
7.9853)70.2300(8.793
638904
6339 60
5590 41
7 19 190
718 767
30 4230
23'9589
6.4641
Brend & Aller and Brend

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e dividend, or tinue the op-

÷ 6.4252.

÷ 423.

÷ 13.25.

÷ ·1347.

 $\div 6.321.$

÷ 3·1416.

g point in the ciphers in the

1000 = 5.784

1000.

hich it will be ve the purpose (rejecting the end, to find the v dividual, and r: but observe in Contracted

an the number Il those in the tient, and then

of decimals.* stent of only

decimal.

(20) Divide 51.47542 by .123415, to the second decimal.
(21) Divide 27104 by .3712, the integral quotient only.

CIRCULATING DECIMALS.

To reduce a circulate to a vulgar fraction.

RULE. 1. For a pure repetend, make the circulating figures the numerator, to as many nines for the denominator.

2. For a mixed repetend, subtract the finite part from the whole, and make the difference the numerator; the denominator to which will consist of as many nines as there are repetends, with as many ciphers subjoined as there are finite figures.

EXAMPLES.

(1) Reduce $\cdot 1'$, $\cdot 3'$, $\cdot 9'$, $\cdot \cdot 01'$, and $\cdot 142857'$ to their equivalent vulgar fractions.

 $\begin{array}{c} 1' = \frac{1}{6}; \ 3' = \frac{3}{6} = \frac{1}{3}; \ 9' = \frac{9}{6} = 1; \ 01' = \frac{1}{69}; \ \text{and} \ 142857' \\ = \frac{1}{6} \frac{4}{6} \frac{2}{6x_1} \frac{57}{6} = \frac{1}{16} \frac{57}{11} \frac{7}{11} \frac{3}{12} = \frac{52}{376} \frac{9}{376} \frac{1}{376} = \frac{4}{3367} \frac{8}{367} = \frac{1}{7}. \end{array}$

(2) Reduce .03`45' and 3.5`126' to equivalent vulgar fractions.

$$\begin{array}{l} \cdot 03^{\circ}45^{\prime} = \frac{345-3}{9900} = \frac{342}{9900} = \frac{342}{1100} = \frac{19}{550}, \\ 3 \cdot 5^{\circ}126^{\prime} = \frac{35126-35}{9990} = \frac{35091}{9990} = \frac{35091}{1110} = \frac{3890}{1110} = 3\frac{509}{1110}. \end{array}$$
 Or thus i

$$3 \cdot 5^{\circ}126^{\prime} = 3 + \frac{5126-5}{9990} = 3\frac{5121}{9990} = 3\frac{509}{1110}.$$

In ADDITION and SUBTRACTION of Circulating Decimals, make them similar and conterminous, and carry to the figures on the right whatever would arise from the repetends being continued.

Note In all cases, when the repetend is 9, make it a cipher, and add 1 to the next figure: for 999, &c. = 1.

In MULTIPLICATION, carry to the product of the right hand figure what would arise from the product of the *rcpetends continued*; and in finding the sum of the products, observe what is directed in ADDITION.

In DIVISION, it is only necessary to observe that the operation may be carried on with the *rcpeating* figures of the dividend_i to any extent required.

NOTE. When the *Multiplier* or the *Divisor* is a circulate, the most convenient method is, to change it into a common fraction.

DECIMALS.

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EXAMPLES.

(3) What is the sum of 25. 142857', 10 3'90', 12.035', and 4.02 567'?

		Similar.		ar and conterminous.
25.142857/	=	$25^{\circ}142857'$		25·14`285714'
10.3`90′	_	10·3`909090'		10·39`090909⁄
12.035	_	12.03`555555'		12.03`5555555
4.02`567'		4.02\567567		4·02`567567 ′
			Sum	51 59 499746'

(4) What is the difference between $567 \cdot 367'$ and $55 \cdot 0^{\circ} 9729'$? Also, between 57, and $49 \cdot 8^{\circ} 53'$? $567 \cdot 367' = 567 \cdot 3^{\circ} 673 673 673 673'$ $55 \cdot 0^{\circ} 9729' = 55 \cdot 0^{\circ} 9729 9729 9729'$ difference $512 \cdot 2^{\circ} 700 67 637 39 43'$ diff. $7 \cdot 1^{\circ} 46'$

	2 ¹
Multiply 65.316' by .753.	(6) Multiply 13. 45 by 3. 36.
65.316	$3.30 = 3\frac{3}{6} = 3\frac{1}{11} = \frac{3}{11}$
.753	13. 45/
195950	37
3265833/	94`18´
457216661	403`63 ′
product 49.183450	1i)497.`SI'
	product 45.256198, &c.

(7) Divide 150.9.045' by 33.	(8) Divide 17.8054' by 3.6'.
3)150.9\045'	$3 \cdot 6' = 3\frac{6}{5} = 3\frac{2}{3} = 1\frac{1}{3}$
11)50.3'015'	$17.8054' \times \frac{3}{11} = \frac{53.4163'}{11}$
4.5'728637' quotient.	4.856.03' quotient. 11

(9) What are the equivalents to $\cdot 004^{+3}54'$ and $65^{-}00063^{+}648'$? Ans. $\frac{1}{10}\frac{29}{660}$, and $65_{7}\frac{47}{7000}$.

(10) What is the sum of $57\cdot575 + 3\cdot59\cdot163' + 210\cdot16' + 06\cdot3759'$? Ans. $271\cdot397\cdot057674235892'$.

(11) Required the difference between 36.30.45207 and 47.280.43'. Ans. 10.975.9135982268'.

(12) Multiply 4.1428571' by 347; and 17.0154' by 6.148': Ans. 15361714285'; and 104.851387205'.

(13) Divide 1536. 714285' by 347; and 104.85 387205' by 6. 148'. Ans 4. 428571'; and 1720.54'.

(5)

2.035', and

us.

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5 0`9729']

 $\frac{9853'}{146'}$ $\frac{1}{9}$ $\frac{1}{9}$ $\frac{1}{3}$ $\frac{1}{1}$ $\frac{1}{3}$ $\frac{1}{4}$ $\frac{1}{3}$ $\frac{1}{4}$ $\frac{1}{3}$

13`63' 7·`81'

6198, &ë. by 3.6'.

 $= \frac{1}{3}$ 3.4163'11

 $\begin{array}{c} 0.63 \cdot 648' \\ 4 & 7 & 7 \\ 210 \cdot 16' \\ 35892' \\ 35892' \\ 207 \quad \text{and} \\ 82268' \\ 37206' \\ 87206' \\ 87205' \\ 197 \\ 2954' \\ \end{array}$

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REDUCTION.

REDUC'TION.

To reduce a Vulgar Fraction to a Decimal.

RULE. Add ciphers to the numerator, and divide by the denominator; the quotient will be the decimal fraction required.

- (1) Reduce $\frac{1}{4}$, $\frac{1}{2}$, $\frac{3}{4}$, and $\frac{3}{8}$, to decimals.
- Ans. $\cdot 25$, $\cdot 5$, $\cdot 75$, and $\cdot 375$.(2) Reduce $\frac{1}{3}$, $\frac{1}{5}$, $\frac{1}{7}$, and $\frac{1}{9}$, to decimals.Ans. $\cdot 3'$, $\cdot 2$, $\cdot 142857'$, and $\cdot 1'$.(3) Reduce $\frac{5}{26}$ to a decimal.Ans. $\cdot 1'923076'$.
- (4) Reduce $\frac{1}{14}$ of $\frac{10}{19}$ to a decimal. Ans. \cdot 6`043956'.

To reduce a given quantity to the Decimal of any denomination required.

RULE. Reduce those of the lowest denomination to decimal parts of the next superior, on the left of which place the given quantity of that denomination; reduce this to the next, and proceed as before, till it is of the denomination required.

(5) Reduce $5s.^*$ 9s. and 16s. to the decimals of a pound. Ans. \pounds 25, \pounds 45, and \pounds :8.

- (6) Reduce 8s. 4d. to the decimal of a \mathcal{L} . Ans. \mathcal{L} 416'.
- (7) Reduce 16s. $7\frac{3}{4}d$ to the decimal of a \pounds .
- (8) Reduce 19s. $5\frac{1}{2}d$. to the decimal of a \pounds .

Ans. £.972916'.

(mg

(9) Reduce 12 grains to the decimal of a *lb.* troy. Ans. *lb.* '002083'.

(10) Reduce $12_{\frac{1}{6}\frac{3}{4}}$ drams to the decimal of a *lb*. avoirdupois. Ans. *lb*. 047668+.

(11) Reduce 2 qrs. $14\frac{1}{4}$ lb. to the decimal of a cwt. Ans. cwt. 62723+.

(12) Reduce 2 furlongs, 161¹/₂ yards to the decimal of a mile. Ans. ·341761`36' mile.

(13) Reduce $5\frac{14}{15}$ pints to the decimal of a gallon. Ans. '7416' gal.

(14) Reduce $4\frac{1}{2}$ gallons of wine to the decimal of a hogshead. Ans. \cdot 0'714285'.

* 20)5.00s. £ 25 Ans.

DECIMALS.

TUTOR'S

(15) Required the mixed decimal number equivalent to $\pounds 3..9..1 \frac{1.63}{1.2.50} d$. Ans. $\pounds 3.45471$.

(16) Express 7 weeks, 3 days, in the decimal of a year. Ans. yr. 142465+.

To find the proper value of a Decimal Fraction of any Integer.

RULE. Multiply the given decimal by the proper number to reduce it to the next inferior denomination, pointing off the given number of decimals in the product; reduce these to the next, and so on to the lowest; and the whole numbers on the left (being collected together) will be the value required.

A decimal of a \pounds may be thus valued by inspection. Double the *tenths* for *shillings*, and call the number in the *second* and *third*, farthings, abating one above 12, and two above 37. But if the *second* is 5, or upwards, call the 5 one *shilling*, and reckon only the excess above five with the third.

By reversing these directions, any given sum in shillings, &c., may be expressed in the decimal of a \pounds .—Thus, half the shillings are tenths. and an odd shilling, 5 hundredths; the rest (in farthings) add into the second and third places, increasing one above 11 farthings, and two above 36.

(17) What is the value of $\cdot 8322916$ of a £.*

(18) Reduce \pounds .740596 to its proper value.

Ans. 14s. 9d. 2 97216 grs.

(19) What is the value of $\cdot 082084$ of a *lb*. troy? Ans. 19 dwts. 16.80384 grains.

(20) What is the value of $\cdot 4909375$ lb. avoirdupois?

- Ans. 7 oz. 13.68 drams.
- (21) What is the value of \pounds 19895?

(22) What is the value of $\cdot 625$ of a cwt. ? Ans. 2 grs. 14 lb.

(23) What is the value of 0.071428 of a hogshead of wine !

- Ans. 4 gal. 1.999856 gts
- (24) What is the value of 0625 of a barrel of beer? Ans. 2 gallons, 1 quart

(25) What is the value of .142465 of a year? Ans. 51.999725 days

* £8322916		
20	By	inspection.
s. 16.6458320	£.	s. d.
12	•8	= 160
d. 7.749984	·032	= 0.73
A	d832	= 1673
	573 very nearly.	

quivalent to 23·45471. of a year. 42465+.

any Integer.

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Double the ad third, fare second is 5, excess above

gs, &c., may gs aro tenths. add into the ags, and *two*

216 qrs. ? 4 grains. bois ? 8 drams.

992 qrs. 9 qrs. 14 lå. d of wine ! 856 qts Deer ? 1 quart

5 days

d. .0 73 .73

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DECIMALS.

		Decin	nai Ta	bles of Col	in, Weight, a	nd Measur	
	TAB	LE I.				Grains.	Decimals.
Q		G Mo		3 qrs.	$\cdot 0625$	12	·025
				2	011666	11	·022916
£1	. the	e Inte	ger.	1	·020833	10	·020833
<i>s</i> .	dec	. s.	dec.	TAB	LE III.	9	.01875
19	.95		•45		WEIGHT.	8	·016666
18	.9	8	•4			7	$\cdot 014583$
17	.85		·35		e Integer.	6	.0125
16	.8	6	•3		s the same		·010416
15	.75		·25	as Pence	in Table 11.	4	· 0 08333
14	.7	4	·2			3	.00625
13	.65		·15	dwts.	Decimals.	2	$\cdot 004166$
12	.6	2	·1	10	·041666	1	$\cdot 002083$
11	.55		·05	9	·0375		TE IV
10	.5	1		8	·033333		LE IV.
	·			7	·029166	AVOIR.	Weight.
6	d.	·025		6	.025	1 cut. th	ie Integer.
5			,)833	5	$\cdot 020833$		
4			6666	4	·016666	Qrs.	Decimals. •75
3		·012		3	.0125		•75
2			3333	2	·008333	1	·5 ·25
1			166	1 .004166		1	.20
						1 4 7 7	
_ _		.003	125	12 gr.	·002083	14 <i>lbs</i> ,	.125
	qrs.		20833	11	·001910	13	·116071
2			.0416	10	.001736	12	·107143
	l	1001	0410	9	$\cdot 001562$		·098214
	TAB	LE II	•	8	·001389	10	·089286
E	NG.	COIN.	18	7	001305	9	·080357
-			Foot		·001042	8	·071428
		ntege		5	·000868	7	·0625
		nege	••	4	·000694	6	·053571
Penc				3	$\cdot 000521$	5	·044643
Inch	ies.	Deci	mals,	2	$\cdot 000321$	4	·035714
6		·5		ĩ	·000173	3	$\cdot 026786$
5		•416	6666			2	·017857
4			333	1 <i>oz</i> . th	e Integer.	1	·008928
3		$\cdot 25$		Penny-w	eights the		
2		·166	6666	same a	as Shillings		·004464
1		·083	333	in the	first Table.	7	· 0 03906

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1.4.

DECIMALS.

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	Decimal Ta	bles of Coi	n, Weight, a	nd Measu	re.	
6 <i>oz</i> . 5 4 3	·003348 ·002790 ·002232 001674	80 g. 70 60 50	·317460 ·277777 ·238095 ·198412	3 pt. 2 1	00)5 952)3968)1984
2 2 1 34 12 4	001116 ·000558 ·000418 ·000279 ·000139	$ \begin{array}{c} 40 \\ 30 \\ 20 \\ 10 \\ 9 \\ 8 \end{array} $	158730 ·119047 ·079365 ·039682 ·035714 ·031746	TABLE VII. MEASURES. Liquid. Dry. 1 Gal. 1 Qr.		es. Dry. Qr.
Avoir. 1 <i>lb</i> . th	BLE V. WEIGHT. e Integer.	7 6 5 4 3	·027777 ·023809 ·019841 ·015873 ·011904	Pts. 4 3	Integ Dec. 5 375	Bush. 4 3
Ounces. 8 7 6 5	Decimals. •5 •4375 •375 •3125	$\frac{2}{1}$ $\frac{4 pts.}{3}$	·007936 ·003968 ·001984 ·001488	$ \begin{array}{c c} 1 \\ \frac{3}{4} \\ \frac{1}{2} \\ 0 \end{array} $	25 125 9375 625 3125	2
4 3 2 1	·25 ·1875 ·125 ·0625	2 1	·000992 ·000496	Decima 02343 01562	ls. Q 375 25	r. Pks. 3 2
8dr. 7 6 5	·03125 ·027343 ·023437 ·019531	Ú Ú	shead the teger.	·00781 ·00585 ·00390 ·00195	59 26	1 3 pts 2 1
4 3 2 1	·015625 ·011718 ·007812 ·003906	30 20 10 9 8	·476190 ·317460 ·158730 ·142857 ·126984			SURE.
LIQUID	BLE VI. MEASURE. he Integer. Decimals. ·396825 ·357142	7 6 5 4 3 2	·111111 ·095238 ·079365 ·063492 ·047619 ·031746 ·015873	Yards 1000 900 800 700 600	·50 ·51 ·45 ·39	cimals. 58182 11364 54545 97727 40909

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		• •
·00	5952 3968 1984	
	es. Dry. Qr.	-
c. 75 75 75 25 25	Busi 4 3 2 1 3 4 3 2 1 3 2 1 3 2 1 3 2 1 3 4 3 2 1 1 1 1 1 1 1 1 1 1 1 1 1	h.
	3 pt 2 1	s.
	ur E . teger	
568 51 454 397	<i>imals</i> 3182 1364 1545 7727 9909	

	Decimal Tables of Coin, Weight, and Measure.						
500 yd.	500 ml + 284001 + 80 d + 210178						
400	$\cdot 227272$	70	$\cdot 191781$	TABLE X.			
300	·170454	60	$\cdot 164383$	CLOTH MEASUR			
200	·113636	50	·136986		he Integer.		
100	.056818	40	$\cdot 109589$		e same as		
90	·051136	30	$\cdot 082192$		ole iv.		
80	$\cdot 045454$	20	$\cdot 054794$	Nails.	Decimals.		
70	$\cdot 039773$	10	·027397	3	·1875		
60	$\cdot 034091$	9	$\cdot 024657$	2Car	.125		
50	·028409	8	.021918	1	·0625		
40	$\cdot 022727$	7	$\cdot 019178$		LE XI.		
30	·017045	6	.016438		-		
20	·011364	5	·013698		WEIGHT.		
10	·005682	4	·010959	A Foth.	the Integer.		
9	·005114	3	.008219	Hund.	Decimals.		
8	·004545	2	·005479	10	·512820		
7	·003977	1	·002739	9	·461538		
6	·003409	1 Day t	ie Integer.	8	·410256		
5	·002841	12hrs.	•5	7	·358974		
4	$\cdot 002273$	11	$\cdot 458333$	6	·307692		
3	·001704	10	·416666	5	256410		
2	·001136	9	·375	4	·205128		
1	·000568	8	·333333	3	·153846		
2 ft.	0003787	7	$\cdot 291666$	2	$\cdot 102564$		
1	0001894	6	·25	1	051282		
6 in.	.0000947	5	·208333	3qrs	038461		
3	.0000474	4	·166666	2	025641		
2	·0000315	3	$\cdot 125$	1	·012820		
1	·0000158	2	·083333	14 lbs.	0064102		
		1	·041665	13	·0059523		
TAB	LE IX.	30 m.	020833	12	0054945		
	IME.	20	·013888	11	0050366		
		10	.006944	10	.0045787		
1 Year t	he Integer.	9	$\cdot 00625$	9	.0041208		
Months t	the same as	8	·005555	8	·0036630		
Pence i	n Table 11.	7	·004861	7	·0032051		
		6	•004166	6	0027472		
Days.	Decimals.	5	$\cdot 003472$	5	0022893		
300	$\cdot 821918$	4	·002777	4	0018315		
200	·547945	3	·002083	3	·0013736		
[100	$\cdot 273973$	2	·001388	2	0009157		
90	. •246575	1	000694	1	0004578		
F 2							

DECIMALS

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THE RULE OF THREE.

(1) If $26\frac{1}{2}$ yards cost £3..16..3. what will $32\frac{1}{4}$ yds. cost ?*

(2) If $7\frac{3}{4}$ yards of cloth cost £2..12..9. what will $140\frac{1}{2}$ yards of the same cost ? Ans. £47..16..3 $\frac{1}{2}$.

(3) If a chest of sugar, weighing 7 cwt. 2 qrs. 14 lb. cost \pounds 36..12..9. what will 2 cwt. 1 qr. 21 lb. of the same cost? Ans. \pounds 11..14..23.

(4) What will $326\frac{1}{4}$ lb. of coffee be worth when $1\frac{1}{2}$ lb. is sold for 3s. 6d.? Ans. £38.1..3.

(5) What is the value of 19 oz 3 dwts. 5 grs. of gold, at $\pounds 2..19$. per oz.? Ans. $\pounds 56..10..5..2\cdot 3$ grs.

(6) What is the charge for $827\frac{3}{4}$ yards of painting, at $10\frac{1}{2}d$. per yard? Ans. £36..4..3..1.5 grs.

(7) If I lent my friend £34. for $\frac{5}{8}$ of a year, how much ought he to lend me for $\frac{5}{12}$ of a year? Ans. £51.

(8) If $\frac{3}{4}$ of a yard of cloth, that is $2\frac{1}{4}$ yards broad, niake a garment, how much of $\frac{4}{5}$ of a yard wide will make a similar one? Ans. 2 yds. 1.75 nail.

(9) If 1 oz. of silver is worth 5s. 6d. what is the price of a tankard that weighs 1 lb. 10 oz. 10 dwts. 4 grs.?

Ans. £6..3..9..2.2 qrs.

(10) What is the value of 15 cwt. 1 qr. 19 lb. of cotton, at 15d. per lb? Ans. £107..18..9.

(11) If 1 cwt. of currants cost £2..9..6. what will 45 cwt. 3 grs. 14 lb. cost at the same rate? Ans. £113..10..9 $\frac{3}{4}$.

(12) Bought 6 chests of sugar, each 6 cwt. 3 qrs. at $\pounds 2.,16$. per cwt. What do they come to? Ans. $\pounds 113..8$.

(13) Bought a tankard for $\pounds 10..12$. at the rate of 5s. 4d. per oz. What was the weight? Ans. 39 oz. 15 dwts.

(14) Gave £187..3..3. for 25 cwt. 3 qrs. 14 lb. of coffee: at what rate did I buy it per lb.? Ans. 1s. $3\frac{1}{2}d$

(15) Bought 29 lb. 4 oz. of snuff for $\pounds 10..11..3$. What is the value of 3 lb.? Ans. $\pounds 1..1..8$.

(16) If I give 1s. 1d. for $3\frac{1}{2}$ lb. of rags, what will be the value of 1 cwt.? Ans. £1..14..8.

yds. £. yds. £. * As $26\cdot5$: $3\cdot8125$: : $32\cdot25$: $4\cdot63974$ $32\cdot25$ $26\cdot5)\overline{122\cdot953125}(4\cdot63974 - \pounds 4 \ 12...91$. Ang.

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EXCHANGE

EXCHANGE

is the act of bartering the money of one place for that of another, by means of a written instrument called a *Bill of Exchange*.

The operations in this Rulo consist in finding the quantity of one sort of money that will be equal to a given sum of the other, according to the existing Course of Exchange.

Par of Exchange signifies the equality in the intrinsic value of two sums of money of different countries, and shows how much of the one is worth a constant sum (or piece of coin) of the other.

Course of Exchange is the comparative value between the money of two different countries at any particular time, which often fluctuates above or below the *Par*.

Agio is a difference of so much per cent. in the value of the Bank-money and the Current-money of some foreign countries, the former being of superior value.

To change Foreign Money into British Sterling Money, or Sterling into Foreign, according to a given Course of Exchange.

RULE. As the quantity of Foreign mentioned in the given course of exchange is to the quantity of Sterling, so is any other sum of the Foreign to its corresponding value in Sterling money.

eign to its corresponding value in Sterling money. And by mutually changing the words Foreign and Sterling, the Rule will serve for changing Sterling into Foreign money.

I. FRANCE.

Accounts are kept at Paris, Lyons, and Rouen, in livres, sols, and deniers, and exchange is made by the écu, or crown = 4s. 6d. at par.

TABLE.12 deniers make 1 sol.20 sols ..3 livres ..1 écu, or crown.

(1) How many crowns must be paid at Paris to receive \mathbf{r} London £180. exchange at 4s. 6d. per crown ?*

> s. d. cr. £. * As 4..6 : 1 :: 130 2 40 9 sixp. 9)7290 sixp. E00 crowns. Ang

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ds. cost ?* will 140* ..16..3ţ. 14 lb. costne cost? ..14..23. n 11 lb. is 38.1..3. of gold, at .2.3 grs. g, at 101d. 1.5 grs. how much ıs. £51. oad, niake e a similar 75 nail. e price of 2.2 qrs.

2.2 qrs. cotton, at 7..18..9.ill 45 cwt. $.10..9\frac{3}{4}.$ at £2..16. 2113..8. of 5s. 4d. $.5 \ dwts.$ of coffee: $1s. 3\frac{1}{2}d$ What is 21..1..8.cill be the ...14..8.

EXCHANGE.

(2) How mucr. scering must be paid in London, to receive in Paris 758 crowns, exchange at 4s. 8d. per crown?

Ans. £176..17. 4.

[TUTOR'S

(3) A merchant in London remits $\pounds 176..17..4$. to his correspondent at Paris: what is the value in French crowns, at 4s. 8d. per crown? Ans. 758 crowns.

(4) Change 725 crowns, 17 sols, 7 deniers, at 4s. $6\frac{1}{2}$, per crown, into sterling money. Ans. £164:.14..0 $\frac{1}{2}$. $\frac{3}{2}\frac{1}{2}\frac{1}{2}$.

(5) Change $\pounds 164..14..0\frac{1}{2}$. sterling into French crowns, exchange at 4s. $6\frac{1}{2}d$. per crown.

Ans. 725 crowns, 17 sols, 741 deniers.

II. SPAIN.

Accounts are kept at Madrid, Cadiz, and Seville, in dollars, rials, and maravedies, and exchange is made by the piece of eight=4s. 6d. at par.

TABLE. 34 maravedies make 1 rial.

8 rials . . . 1 piastre, or piece of eight. 10 rials . . . 1 dollar.

(6) A merchant at Cadiz remits to London 2547 pieces of eight, at 4s. 8d. per piece : how much sterling is the sum? Ans. £594..6.

(7) How many pieces of eight, at 4s. 8d. each, will answer a bill of £594..6. sterling? Ans. 2547.

(8) If I pay here a bill of £2500., for what Spanish money may I draw my bill at Madrid, exchange at 4s. $9\frac{1}{2}d$. per piece of eight? Ans. 10434 pieces of eight, 6 rials, $8\frac{2}{2}\frac{9}{3}$ mar.

HI. ITALY.

Accounts are kept at Genoa and Leghorn in livres, sols, and deniers, and exchange is made by the piece of eight or dollar=4s. 6d. at par.

TABLE. 12 deniers make 1 sol.

20 sols . . . 1 livre.

5 livres . . 1 piece of eight at Genoa.

6 livres . . 1 piece of eight at Leghorn.

N. B. The exchange at Florence is by ducatoons; at Venice by ducats.

TABLE. 6 solidi make 1 gross. 24 gross . . 1 ducat.

(9) How much sterling money may a person receive in London, if he pay in Genoa 976 dollars at 4s. 5d. per dollar? Ans. £215..10. 8.

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to receive n? 5..17.4.to his corcrowns, at crowns. s. $6\frac{1}{2}d.$ per $0\frac{1}{4}.\frac{3}{2}\frac{1}{8}g.$ rowns, ex-

deniers.

in dollars, e piece of

e of eight.

pieces of ne sum? 594..6. vill answer s. 2547. ish money per piece 23 mar.

vres, sols, f eight or

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eceive in er dollar? ..10.8

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EXCHANCE.

(10) A factor has sold goods at Florence for 250 ducatoons, at 4s. 6d. each: what is the value in pounds sterling? Ans. $\pounds 56..5$.

(11) If 275 ducats, at 4s. 5d. each, be remitted from Venice to London, what is the value in pounds sterling?

Ans. £60..14..7.

(12) A traveller would exchange $\pounds 60..14..7$. sterling for Venice ducats, at 4s. 5d. each; how many must he receive? Ans. 275.

IV. PORTUGAL.

Accounts are kept at Oporto and Lisbon, in reas, and exchange is made by the milrea = 6s. $8\frac{1}{2}d$. at par.

TABLE. 1000 reas make 1 milrea.

(13) A gentleman being desirous to remit to his correspondent in London 2750 milreas, exchange at 6s. 5d. per. milrea, for how much sterling will he be creditor in London? Ans. £882..5..10.

(14) A merchant at Oporto remits to London 4366 milreas, 183 reas, at 5s. $5\frac{5}{8}d$. exchange per milrea : how much sterling must be paid in London for this remittance?

Ans. £1193..17..6..3.0375 grs.

(15) If I pay a bill in London of £1193..17..6..3.0375 qrs what must I draw for on my correspondent in Lisbon, exchange at 5s. $5\frac{5}{6}d$. per milrea? Ans. 4366 milreas, 183 reas

V. HOLLAND, FLANDERS, AND GERMANY.

At Antwerp, Amsterdam, Brussels, Rotterdam, and Hamburgh, some accounts are kept in pounds, shillings, and pence, as in England; others in guilders, stivers, and pennings: exchange with London, at from 33s. to 36s. or 38s. Flemish per pound sterling.

TABLE. 8 pennings make 1 groat.

2 groats, or 16 pennings 1 stiver.

20 stivers 1 guilder, or florin.

ALSO, 12 groats, or six stivers, make 1 schelling.

20 schellings, or 6 guilders 1 pound.

(16) Remitted from London to Amsterdam a bill of $\pounds754.10$. sterling: how many pounds Flemish is the sum, the exchange at 33s. 6d. Flemish per pound sterling?

Ans. £1263..15..9. Flemish.

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(17) A merchant in Rotterdam remits $\pounds 1263..15..9$. Flemish to be paid in London; how much sterling money must he

CONJOINED PROPORTION.

draw for, the exchange being at 33s. 6d. Flemish per pound sterling? Ans. £754..10.

(18) If I pay in London $\pounds 852..12..6$. sterling, how many guilders must I draw for at Amsterdam, exchange at 34 schellings, $4\frac{1}{2}$ groats Flemish per pound sterling?

Ans. 8792 guild. 13 stiv. 1 gr. 61 pennings.

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(19) What must I draw for in London, if I pay in Amsterdam 8792 guild. 13 stiv. 14¹/₂ pennings, exchange at 34 schellings, 4¹/₂ groats per pound sterling? Ans. £852..12..6.

To convert Bank Money into Currency; and the contrary.

As 100 : 100 plus the cgio : : the Bank-money : the Currency.

As 100 plus the agio : 100 : : the Currency : the Bankmoney.

(20) Change 794 guilders, 15 stivers, Current money, into Bank florins, agio $4\frac{3}{8}$ per cent.

Ans. 761 guilders, 8 stivers, 11735 pennings.

(21) Change 761 guilders, 9 stivers Bank, into Current money, agio $4\frac{3}{8}$ per cent.

Ans. 794 guilders, 15 stivers, $4\frac{3}{10}$ pennings.

VI. IRELAND,

The par of exchange, long established with Ireland, was $\pounds 108..6..8$. Irish = $\pounds 100$. English. That is, $\pounds 1..1..8$. Irish = $\pounds 1$. English; or 13d. Irish = 1s. English.

But the English and Irish currency are now assimilated.

(22) A gentleman remitted to Ireland £575..15. sterling: what would he receive there, the exchange being at £10. per cent.? Ans. £633..6..6.

(23) What would be paid in London for a remittance of $\pounds 633..6..6$. Irish, exchange at $\pounds 10$. per cent.? Ans. $\pounds 575..15$.

CONJOINED PROPORTION; OR COMPOUND ARBI-TRATION OF EXCHANGE

Is the method of comparing the coins, weights, or measures of one country with those of another, when the comparison is to be made *through the medium* of those of other countries.

Case 1. When it is required to find how many of the first sort mentioned are equal to a given quantity of the last

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per pound 754..10. how many t 34 schel-

in Amstert 34 schel-2..12..6.

contrary.

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imilated. 5. sterling : at $\pounds 10$. per 633..6..6. nittance of $\pounds \pounds 575..15$.

D ARBI-

r measures comparison r countries. of the first last RULE. Place the terms alternately, antecedents and consequents, in two columns, left and right. The last term, being an antecedent, will stand on the left.

Divide the product of the antecedents by the product of the consequents for the answer.

PROOF. By as many single statements as the question requires.

(1) If 20 *lb*. at London make 23 *lb*. at Antworp, and 155 *lb* at Antworp make 180 *lb*. at Leghorn, how many *lb*. at London are equal to 72 *lb*. at Leghorn ?*

(2) If 12 *lb*. at London make 10 *lb*. at Amsterdam, and 100 *lb*. at Amsterdam 120 *lb*. at Toulouse, how many *lb*. at London are equal to 40 *lb*. at Toulouse? Ans. 40 *lb*.

(3) If 140 braces at Venice be equal to 156 braces at Leghorn, and 7 braces at Leghorn equal to 4 ells English, how many braces at Venice are equal to 16 ells English?

Ans. 25-5.

(4) If 40 *lb*. at London make 36 *lb*. at Amsterdam, and 90 *lb*. at Amsterdam make 116 *lb*. at Dantzic, how many *lb*. at London are equal to 130 *lb*. at Dantzic? Ans. $112\frac{2}{20}$.

Case 2. When it is required to find how many of the last sort mentioned are equal to a given quantity of the first.

RULE. Place the *antecedent* and *consequent* terms as before; but the last term, being a *consequent*, will stand on the right. Divide the product of the consequents by that of the antecedents.

(5) If 12 *lb*. at London make 10 *lb*. at Amsterdam, and 100 *lb*. at Amsterdam 120 *lb*. at Toulouse, how many *lb*. at Toulouse are equal to 40 *lb*. at London? Ans. 40 *lb*.

(6) If 40 lb. at London make 36 lb. at Amsterdam, and 90 lb. at Amsterdam 116 lb. at Dantzic, how many lb. at Dantzio are equal to 122 lb. at London? Ans. $141\frac{1}{23}$

* Antecedents. Consequents. 20 *lb*. London = 23 *lb*. Antwerp. 155 *lb*. Antwerp = 180 *lb*. Leghorn. 72 *lb*. Leghorn = how many London? 1 8 $\frac{20 \times 155 \times 72}{23 \times 1 \% 0} = \frac{1240}{23} = 53\frac{21}{23}$ *lb*. Ans. 9 1

EVOLUTION.

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INVOLUTION

Is the method of finding the powers of numbers.

Any number is the first power of itself, and the root of all its powers : and when the root is multiplied by itself the product is the second power; the second multiplied by the first produces the third, &c.

The second power is commonly called the square, and the third power the cube.

Numbers called *indices*, or *exponents*, are placed on the right, a little above the line, to denote the respective powers. Thus, 3² signifies the square, or second power of 3; the small figure ² being the *index*, or *exponent*.

To involve a number to any power.

RULE. Multiply the given number (or root) by itself continually one time less than the index of the power: that is, once for the second, twice for the third power, &c.

Observe, that any two or more powers multiplied together will produce a power whose index is the sum of their indices. Thus, the seventh power is the product of the fourth and the third, because the sum of the indices 4+3=7.

ILLUSTRATIONS.

 3^{1} , or 3.

The first power of

3 is $5^2 = 5 \times 5 = 25.$ The second power of 5 is

4 is The third power of $4^{3} = 4 \times 4 \times 4 = 64$.

The fourth power of $\cdot 05$ is $\cdot 05^4 = \cdot 05 \times \cdot 05 \times \cdot 05 \times \cdot 05 =$ ·00000625.

 $\frac{2}{3}$ is $\frac{2}{3}$ $\left| {}^{5} = \frac{2}{3} \times \frac{2}{3} \times \frac{2}{3} \times \frac{2}{3} \times \frac{2}{3} \times \frac{2}{3} = \frac{32}{243}$. The fifth power of

(1) Required the squares of 43, 2174, $4\cdot 3$, and $\cdot 2174$.

Ans. 1849, 4726276, 18.49, and .04726276 (2) Cube 111, 1.11, $\frac{3}{4}$, and $2\frac{5}{8}$.

Ans. 1367631, 1.367631, 27/64, and 1845

(3) Involve 9 to the ninth power. Ans. 387420489

(4) Find the third, fifth, and eighth powers (without finaling the fourth, sixth, and seventh) of 17.

Ans. 4.913, 14.19857, and 69.75757441 (5) What are the third and sixth powers of $\cdot 05$?

Ans. 000125, and 000000015625

EVOLUTION

Is the method of extracting the roots of powers. It is therefore the reverse of Involution; by referring to which it will

root of all elf the proby the first

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 $\frac{1}{3} = \frac{3}{2} \frac{3}{4} \frac{3}{3}$. $\cdot 2174$. 726276

l 18<u>45</u> 420489 thout finel-

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SQUARE ROOT.

be obvious, that the Square Root of a number, multiplied by itself, will produce that number; and that the Cube Root, multiplied twice by itself, will produce the number (or power) of which it is the root.

Note. The roots of complete powers are called *rational*; and those which cannot be completely extracted, are called *surds*, or *irrational* roots: thus $\sqrt{4} = 2$, is *rational*; but $\sqrt{5}$ is a *surd*. The surd roots may, however, be found to any extent proposed.

SQUARE ROOT.

RULE 1. Place points over the units, hundreds, &c., so as to form seriods of two figures each.

2. From the first period on the left, subtract the greatest square contained in it; put the root on the right as a quotient; annex the succeeding period to the remainder, and call that number the *Résolvend*.

3. Divide the resolvend, exclusive of the units, by double the root; annex the quotient to the root, and also to the right of the divisor to complete it: then multiply the divisor by that quotient figure, and subtract the product from the resolvend.

4. The remainder, with the next period joined, will form a new resolvend; and double the root, a new divisor; with which proceed as before.

Note 1. When the number of figures in the *Integer* is uneven, the first period will consist of but one figure. When there is an odd number of *decimals*, a cipher must be added to complete the periods.

2. When the figures of the whole number are exhausted, periods of ciphers may be used at pleasure, to continue the extraction in decimals. In all cases, the root will consist of as many figures as there are periods, whether integral or decimal.

Roots.	1.	2.	3.	4.	5.	6.	7.	8.	9.	
SQUARES.	1.	4.	9.	16.	25.	36.	49.	64.	81.	
 1) What is 2) What is 3) What is 	the	square	ŗ	o to	f 10	6929	9?			327. 1698.

* 119025(345 the root.	345
9	345
64)290 256	1725
256	1380
685)3425	1035
3425	Proof 119025.

EVOLUTION.

(4) What is the square root of 2268741? Ans. 1506.23+.

- (5) What is the square root of 7596796? Ans. 2756.228+.
- (6) What is the square root of 4.372594? Ans. 2.091+.
- (7) What is the square root of 2.2710957? Ans. 1.50701+.
- (8) What is the square root of 00082754? Ans. 01809+.
- (9) What is the square root of 1.270059? Ans. 1.1269+.

To find the Roots of fractional Numbers.

RULE. When the terms of a Fraction are complete powers, extract their roots for the corresponding terms of the root.

When they are surds, find an equivalent fraction, by multiplying both terms by the denominator; or by the least number that will make the denominator a square. Then divide the root of the numerator by the root of the denominator for the answer.—Or, reduce the fraction to a decimal, and extract its root.

Mixed numbers may either be reduced to their equivalent fractions; or into a decimal form.

(10)	What is	the	square	root	of	2384 ?	Ans. 2.
(11)	What is	the	square	root	of	9216?	Ans. 4.
(12)	What is	the	square	root	of	$51\frac{21}{25}$?	Ans. 71.
(13)	What is	the	square	root	of	$27\frac{9}{16}$?	Ans. $5\frac{1}{4}$.
(14)	What is	the	square	root	of	$9_{\frac{1}{4}\frac{3}{9}}$?	Ans. 34.
(15)	What is	the	square	root	oſ	275?	Ans. 89802+
(16)	What is	the	square	root	of	$\frac{478}{549}$?	Ans. •93309+-
(17)	What is	the	square	root	oſ	$85\frac{14}{15}$?	Ans. 9.27+.
(18)	What is	the	square	root	of	857?	Ans. 2.9519+,

To find a mean proportional between any two given numbers.

RULE. Extract the square root of their product.

(19) What is the mean proportional between 3 and 12? $\sqrt{3 \times 12} = \sqrt{36} = 6$ the mean proportional. Ans.

(20) What is the mean proportional between 4276 and 842? Ans. 1897.4+.

To find the side of a square equal in area to any given surface.

RULE. Extract the square root of the given area for the side of the square sought.

(21) If the content of a given circle be 160, what is the side of the square equal? Ans. 12.64911.

(22) If the area of a circle is 750, what is the side of the square equal? Ans. 2738612.

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 $\begin{array}{c|c} Ans. \frac{2}{3}.\\ Ans. \frac{2}{5}.\\ Ans. 7\frac{1}{5}.\\ Ans. 5\frac{1}{4}.\\ Ans. 3\frac{1}{4}.\\ 39802+\\ 93309+\\ 9\cdot27+\\ 9\cdot27+\\ 9519+. \end{array}$

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SQUARE ROOT.

The area of a circle given, to find the diameter.

RULE. As 355: 452, or, as 1: 1.273239:: the area : the square of the diameter; or, multiply the square root of the area by 1.12837, and the product will be the diameter.

(23) What length of cord must be tied to a cow's tail, the other end fixed in the ground, to enable her to cat just an acre of grass, and no more; supposing the cow and tail to measure $5\frac{1}{2}$ yards? Ans. 33.75 yards.

The area of a circle given, to find the circumference.

RULE. As 113 : 1420, or, as 1 : 12.56637 :: the area : the square of the circumference; or, multiply the square root of the area by 3.5449, and the product will be the circumference.

(24) When the area is 12, what is the circumference? Ans. 12.279.

(25) When the area is 160, what is the circumference?

Two sides of a right-angled triangle being given, to find the third side.

Case 1. The base and perpendicular being given, to find the hypotenuse.

RULE. The square root of the sum of the squares of the base and perpendicular is the length of the hypotenuse.

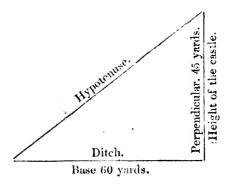
Case 2. The hypotenuse and perpendicular being given, to find the base.

RULE. The square root of the difference of the squares of the hypotenuse and perpendicular is the length of the base.

Case 3. The base and hypotenuse being given, to find the perpendicular.

RULE. The square root of the difference of the squares of the hypotenuse and base is the height of the perpendicular.

(26) The top of a castle from the ground is 45 yards high, and it is surrounded with a ditch 60 yards broad : what length must a ladder be to reach from the outside of the ditch to the top of the castle ? Ans. 75 yards



(27) The wall of a town is 25 feet high, and is surrounded by a moat of 30 feet in breadth: required the length of a ladder that will reach from the outside of the moat to the top of the wall? Ans. 39.05 feet.

N. B. These two questions may be varied for examples to the second and third cases.

(28) In an army consisting of 331776 men, how many must be in rank and file to form a solid square ? Ans. 576.

(29) A certain square pavement contains 48841 equal square stones. How many are contained in one of the sides ? Ans. 221.

CUBE ROOT.

RULE 1. Point every third figure of the given number, beginning at the units' place; find the greatest cube in the first period, and subtract it therefrom; put the root in the quotient, and bring down the figures in the next period to the remainder for a *Resolvend*.

2. Multiply the square of the root found by 300 for a *Divisor*, and annex to the root the number of times which that is contained in the *Resolvend*.

3. Add 30 times the preceding figure (or figures) multiplied by the last and the square of the last, to the divisor, and multiply the snm by the last for a *Subtrahend*; subtract it from the *Resolvend*, and repeat the process as far as necessary.*

* The subjoined Theorems (deduced from Problem 91, page 266, Emergen's Algebra) are very convenient approximations for the Cube Root.

$$r + \frac{1}{2}\sqrt{\left(\frac{4n-r^3}{3r}\right)} = \frac{1}{2}r + \sqrt{\left(\frac{n}{3r} - \frac{1}{12}r^2\right)} =$$

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CUBE ROOT.

Note. As the units must always be pointed, there will be sometimes only one or two figures in the first period.—The decimals must always consist of so many figures as will constitute *complete periods*, as in the Square Root.—Also, what is observed in Note 2, Square Root, will hold good in this Rule.

Roots	. 1.	2: 3	. 4.	5.	6.	7.	8.	9.
CUBES	: 1.	8. 27	. 64. 1	125.	216. 3	343.	512. 7	729.
(1) Wha	t is the	e cube	root of	· 992	52847	?*		
(2) What	t is th	e cube	root of	f 389	017?		Ar	is. 73.
(3) Wha	t is the	e cube	root of	573	5339?	1		. 179.
(4) Wha	t is th	e cube	root of	f 324	61759	?	Ans	. 319.
(5) Wha	t is th	e cube	root of	846	04519	?	Ans	. 439.
(6) Wha	t is the	e cube	root of	f 270	54036	008?	Ans.	3002.
(7) Wha							? Ans.	8765.
(8) What	t is th	e cube	root of	12.9	07787	5?	Ans.	2.35.
(9) What	it is th	e cube	root o	f •00	19066	24?	Ans	·124.

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 \mathbf{R} , the required root, nearly. In which n denotes the given number, and r an assumed root found by trial.

The second formula, which is more convenient than the other, because it contains no higher power than the square of r, may be thus expressed.

Divide the given number by three times the assumed root, and from the quotient subtract $\frac{1}{12}$ of the square of the assumed root: the square root of the remainder, added to half the assumed root, will give the root required. See also the method of extracting ANY ROOT by approximation.

> * 99252847(463 the root. $4^{3} = 64$ $4^{2} \times 300 = 4800)35252$ resolvend. $720 = 4 \times 30 \times 6$ $36 = 6^{2}$ 4800 divisor. 5556 6 33336 subtrahend. $46^{3} \times 300 = 634800)1916847$ resolvend. $4140 = 46 \times 30 \times 3$ $9 = 3^{2}$ 634800 634800 638949 31916847 subtrahend.

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(10) What is the cube root of 36155.02756? Ans. 33.06+.

(11) What is the cube root of 33.230979937? Ans. 3.215+.

(12) What is the cube root of 15926.972504? Ans. 25.16+.

To find the Roots of Fractional Numbers.

Rule. When the terms of a fraction are complete powers, extract their roots for the corresponding terms of the root.

When they are surds, if both terms be multiplied by the square of the denominator, an equal fraction will be produced, the denominator of which will be a cube. Then divide the root of the numerator by the root of the denominator for the answer.—Or, the fraction hay be reduced to a decimal, and its root extracted.

Mixed numbers may be reduced as in the Square Root.

(13)	What is the	cube root	of 250?	Ans. \$.
	What is the			
	What is the			
	What is the			
	What is the			
(18)	What is the	cube root	of 4?	Ans. 8298265+.
(19)	What is the	cube root	of \$?	Ans. 8220707+.
(20)	What is the	cube root	of $\frac{5}{1}$?	Ans. 1.930978+.
(21)	What is the	cube root	of 9 <u>‡</u> ?	Ans. 2.092845+.
(22)	What is the	soube root	of $8\frac{5}{7}$?	Ans. 2.0578352+.

(23) A water cistern in the form of a cube contains 60 cubic feet, 143 inches; what is the length of the side?

Ans. 47 inches.

(24) There is an excavation made for a cellar equal in length, breadth, and depth; which required 4913 cubic feet of earth to be dug out. What is the length of the side ?

Ans. 17 fect.

(25) There is a building of cubic form, which contains 389017 solid feet: what is the superfician content of one of its sides? Ans. 5329 sq. feet.

Between two numbers given, to find two mean proportionals.

RULE. Divide the greater extreme by the less, and the cube root of the quotient multiplied by the less extreme gives the *less mean*; multiply the said cube root by the less mean, and the product will be the greater mean proportional.

(26) What are the two mean proportionals between 6 and 162? Ans. 18 and 54.

(27) What are the two mean proportionals between 4 and 108? Ans. 12 and 36.

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Ans. $\frac{3}{8}$. Ans. $2\frac{1}{3}$. Ans. $3\frac{1}{4}$. Ans. $7\frac{2}{5}$. 98265+. 20707+. 30978+. 92845+. 78352+. ns 60 cubis

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ween 6 and 3 and 54. ween 4 and 3 and 36. ROOTS OF ALL POWERS.

To find the side of a cube equal in solidity to any given solid as a globe, cylinder, prism, cone, &c.

RULE. The cube root of the solid content given is the side of a cube of equal solidity.

(28) If the solid content of a globe is 10648, what is the side of a cube of equal solidity? Ans. 22.

The side of a cube being given, to find the side of a cube that shall be double, treble, &c., in quantity to the cube given.

RULE. Cube the side given, and multiply it by 2, 3, &c., the cube root of the product will be the side sought.

(29) There is a cubical vessel whose side is 12 inches, and it is required to find the side of another vessel that will contain three times as much. Ans. $17\cdot30699$ inches.

BIQUADRATE ROOT.

RULE. Extract the square root of the given number, and then the equare root of that square root, which will be the biquadrate root rc-quired.

(1) What is the biquadrate root of 531441? Ans. 27.

(2) What is the biquadrate root of 33362176? Ans. 76.

(3) What is the biquadrate root of 5719140625? Ans. 275.

A GENERAL RULE FOR EXTRACTING THE ROOTS OF ALL POWERS.

1. PREPARE the given number by pointing it into periods of two figures each for the square root, three for the cube root, &c.

2. Find the first figure of the root, and subtract its power from the first period.

3. Bring down the first figure in the next period to the remainder, and call that the *dividend*.

4. Involve the root to the next inferior power to the given one, and multiply it by the index of the given power for a *divisor*.

5. Find a quotient figure by common division, and annex it to the root; then involve the whole root to the given power for a subtrahend, which subtract from the first two periods.

6. To the remainder bring down the first figure of the next period for a new *dividend*; find a new *divisor* and a new *subtrahend*, as before; subtract from *three periods*, and proceed thus to the end.

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POSITION.

Otherwise. To find ANY ROOT by approximation.

RULE. Let g denote the given number or power, n the index of the power, a an assumed power nearly equal to g, r its root, and R the required root.

Then, as $\frac{(n+1)a+(n-1)g}{2}$: $a \oslash g$:: r: $R \oslash r$; * which dif-

ference or correctional number, being added or subtracted, (as required,) will give R, and by repeating the process, any degree of accuracy may be obtained.

- (1) What is the square root of 141376?
- (2) What is the cube root of 53157376? Ans. 376.
- (3) What is the fourth root of 19987173376? Ans. 376.

(4) Required the fifth root of 2508.474615614240625.

Ans. 4.785.

(5) Required the sixth root of 3.1416. Ans. 1.210201+

SINGLE POSITION

Is the method of using one supposed number, and working with it as the true one, to find the real number required.[‡]

RULE. As the result from the supposition is to the true result, so is the supposed number to the true one required.

Phoor. Add the several parts together, according to the conditions of the question.

(1) A schoolmaster being asked how many scholars he had, said, "If I had as many, half as many, and one quarter as many more, I should have 88." How many had he ?§

* This for the Cube Root will be, As $2a + g : a \circ g :: r : R \circ r$.

+ 141376(376 the root. 9 $3 \times 2 = 6)51$ dividend. $37^2 = 1369$ subtrahend. $37 \times 2 = 74)447$ dividend. $276^2 = 141376$ subtrahend.

t Questions belonging to this Rule have the results proportional to their suppositions; the conditions requiring the number sought to be increased by the addition of itself, or of some known multiple or part thereof, or to be diminished by the subtraction of such part.

§ Suppose he had 40. Then 40 + 40 + 20 + 10 = 110. And, as $110:89:40:\frac{38 \times 40}{110} = \frac{352}{11} - 32$ Ans.

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;* which dif-(as required,) accuracy may

Ans. 376. Ans. 376. 240625. Ans. 4785. 1.210201+

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POSITION.

(2) A person who had a certain number of antique coins, said, if the third, fourth, and sixth parts of the number were added together, they would make 54. How many had he?

Ans. 72.

(3) A chaise, a horse, and harness, cost $\pounds 60$; the horse being double the price of the harness, and the chaise double the price of the horse and harness. What was given for each?

Ans. Horse £13..6..8. harness £6..13..4. chaise £40.

(4) What sum of money will amount to \pounds 300. in ten years, at \pounds 6. per cent. per annum, simple interest?

Ans. £187..10.

(5) A, B, and C, dividing a quantity of goods, which cost \pounds 120. mutually agreed that B should have a third part more than A, and C a fourth part more than B. What must each man pay? Ans. A \pounds 30. B \pounds 40. C \pounds 50.

(6) A gentleman bought a house, with a garden, and a horse in the stable for \pounds 500. He paid four times the price of the horse for the garden, and 5 times the price of the garden for the house. What were their respective prices?

Ans. Horse $\pounds 20$. garden $\pounds 80$. house $\pounds 400$.

DOUBLE POSITION

REQUIRES the use of two supposed numbers to find the true one required.*

RULE. Work with the two supposed numbers, and mark the crears in the results with + or -, according as they exceed or fall short of the true result; then place the errors against their respective positions, and multiply them crosswise.

If the errors be of *like* kinds, i. e. *both greater*, or *both less* than the given number, take their difference for a divisor, and the difference of the products for a dividend. But if *unlike*, take their sum for a divisor, and the sum of their products for a dividend: the quotient will be the answer.

* Questions belong to this Rule which require the addition or subtraction of a number, &c., which is not any known part of the number required. The results are, therefore, not proportional to their suppositions.

The following Rule will, in some cases, be found more eligible: Multiply the *difference* of the supposed numbers by the *less error*; and divide the product by the *difference* of the errors when they are of

(1) A, B, and C, would divide $\pounds 200$. among them, so that B may have $\pounds 6$. more than A, and C $\pounds 8$. more than B. How much must each have ?*

(2) A man had two silver cups of unequal weight, having one cover to both of 5 onnces. Now if the cover is put on the less cup, it will double the weight of the greater; and put on the greater cup, it will be thrice as heavy as the less. What is the weight of each?

Ans. 3 ounces the less, and 4 the greater.

(3) Three persons conversing about their ages; says K, "My age is equal to that of H, and $\frac{1}{4}$ of L's;" and L says, "I am as old as both of you together." Required the ages of K and L; H's being 30. Ans. K 50, and L 80.

(4) D, E, and F, playing at cards, staked 324 crowns; but disputing about the tricks, each man seized as many as he could: E got 15 more than D; and F got a fifth part of both their sums added together. How many did each person get? Ans. $D \ 127\frac{1}{2}$, $E \ 142\frac{1}{2}$, and F 54.

(5) A gentleman meeting with some ladies, said to them, "Good morning to you, ten fair maids." "Sir, you mistake,"

like kinds, or by their sum, when unlike; the quotient will be a correctional number; which being added to the nearest supposition when defective, or subtracted from it when excessive, will give the number required.

* 1st. Suppose A's share $=$ 40 then B's $=$ 46 and C's $=$ 54 Sum 140	2nd. Suppose A's share = $\begin{array}{c} \pounds \\ 70 \\ \text{then B's} = \\ \text{and C's} = \\ 84 \\ \hline \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ &$
Therefore the error is	Here the error is $+$ 30, or 30 too
- 60, or 60 too little.	much.
sup. err.	£.
40 60	A 60
$_{70} \times _{30}$	B 66
4200 1200	C 74
divisor. 1200	200 Proof.
60+30=9 0)540 0 dividend.	
$\mathbf{\pounds}\mathbf{\widehat{60}} = \mathbf{A's}$ share.	
Or, by the Rule in the Note	9.
$\frac{70 - 40 \times 30}{60 + 30} = \frac{30 \times 30}{90}$	10, the correctional numbers

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thare = 701 B's = 761 C's = 84Sum 230 + 30, or 30 ten ϵ .

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PROGRESSION.

answered one of them, "we are not tee but if we were three times as many as we are, we should be as many above ten as we are now under." How many were they? Ans. 5.

ARITHMETICAL PROGRESSION.

An Aruhmetical Progression is a series of numbers increasing or decreasing uniformly by a continued equal difference. Thus,

1, 2, 3, 4, 5, &c. 2, 5, 8, 11, 14, &c. 9 8 7 6 5 &c. 1 nus, are increasing Arithmetical Series.

9, 8, 7, 6, 5, &c. are decreasing Arithmetical Series.

Observe, that the *terms* of the first series are formed by adding successively the common difference 1, and the second by the common difference 3. The terms of the third and the fourth diminish continually by the subtraction of 1 and 4 respectively.

In an odd number of terms, the double of the mean (or middle term) is equal to the sum of the extremes, or of any two terms equidistant from the mean. Thus, in 1, 2, 3, 4, 5, the double of 3=1+5=2+4=6.

In an even number of terms, the sum of the two means is equal to the sum of the extremes, or of any two equidistant terms. Thus, in 2, 4, 6, 8, 10, 12, 6+8=2+12=4+10=14.

To give *Theorems or Rules* for the solution of the various cases, the terms are represented by symbols, or letters.

Thus let a denote the less extreme, or least term,

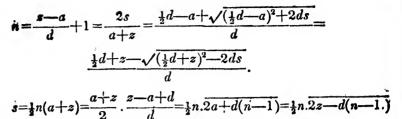
- z the greater extreme, or greatest term,
- d the common difference,
- *n* the *number* of terms, and
 - the sum of all the terms.

Any three being given, the others may be found.

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NOTE. The twenty cases in this Rule may be resolved by the following Theorems:---

 $a = z - (n-1)d = \frac{2s}{n} - z = \frac{s}{n} - \frac{1}{2}d(n-1) = \frac{1}{2}d + \sqrt{(\frac{1}{2}d+z)^2 - 2ds};$ $s = a + (n-1)d = \frac{2s}{n} - a = \frac{1}{n} + \frac{1}{2}d(n-1) = \sqrt{(\frac{1}{2}d-a)^2 + 2ds} - \frac{1}{2}ds;$ $d = \frac{z-a}{n-1} = \frac{s-an}{n-1} \cdot \frac{2}{n} = \frac{nz-s}{n-1} \cdot \frac{2}{n} - \frac{(z+a)\cdot(z-a)}{2s-a-z};$



Moreover, when the least term a = nothing, the Theorem's become z=d(n-1), and $s=\frac{1}{2}nz$.

Case 1. The two extremes and the number of terms being given; to find the sum.

RULE. Multiply the sum of the extremes by the number of terms; and half the product will be the answer.*

(1) How many strokes does the hammer of a clock strike in 12 hours ?†

(2) A man bought 17 yards of cloth, and gave for the first yard 2s. and for the last 10s. What was the price of the 17 yards? Ans. £5..2.

(3) If 100 eggs be placed in a right line, exactly a yard from each other, and the first a yard from a basket, how far must a person travel to gather them all up singly, and return with every egg to put it into the basket?

Ans. 5 miles, 1300 yards:

Case 2. The same three terms given, to find the common difference.

. RULE. Divide the difference of the extremes by the number of terms less 1, and the quotient will be the answer.

(4) A man had eight sons, whose ages were in arithmetical progression; the youngest being 4 years old, and the eldest 32. What was the common difference of their ages ?

(5) A man travelling from London to a certain place, went 3 miles the first day, and increased every day by an equal excess, making the twelfth day's journey 58 miles:

124

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^{*} The learner should find each of these cases among the preceding *Theorems*. Thus, the present Rule will be found designated by $b = \frac{1}{2}n(a+z_{*})$ &c.

 $^{+12+1 \}times 6 = 13 \times 6 = 78$. Ans.

^{: 32-4-8-1=28-7=4} years. Ane.

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PROGRESSION.

What was the daily increase, and how far did he tra 4 in 12 days?

Ans. 5 miles daily increase, the whole distance 366 miles.

Case 3. The two extremes and the common difference being given, to find the number of terms.

RULE. Divide the difference of the extremes by the common difference, and the quotient increased by *unity* is the number sought.

(6) A person travelling into the country, went 3 miles the first day, and increased every day 5 miles, till at last he went 58 miles in one day. How many days did he travel ? Ans. 12.

(7) A man being asked how many sons he had, said, that the youngest was 4 years old, and the eldest $32 \cdot$ and that his family had increased one in every 4 years. How many had up? Ans. 8.

Case 4. The greater extreme, the number of terms, and the common difference being given, to find the less extreme.

RULE. Multiply the common difference by the number of terms less 1; subtract the product from the greater extreme, and the difference will be the less extreme.

(8) A man went from London to a certain town in the country in 10 days; every day's journey exceeding the former by 4 miles, and the last being 46 miles: what was the first? Ans. 10 miles.

(9) A man took out of his pocket, at 8 several times, so many different numbers of shillings, every one exceeding the former by 6, the last being 46: what was the first? Ans. 4.

Case 5. The common difference, the number of terms, and the sum being given, to find the less extreme.

RULE. Divide the sum by the number of terms: from the c_1 otient subtract half the product of the common difference into the number of terms less 1; and the remainder will be the less extreme.

(10) A man is to receive £360. at 12 several payments, each payment to exceed the former by £4. and is willing to bestow the first payment on any one that can tell him what . is. What will that person have for his pains? Ans. £8.

Case 6. The less extreme, the common difference, and the num ber of terms being given, to find the greater extreme

RULE Multiply the number of terms less 1 by the common differ

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Theorems

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ence; to this product add the less extreme, and the sum will be the greater extreme.

(11) What is the last number of an arithmetical progression, beginning at 6, and continuing by the increase of 8 to 20 places ? Ans. 158.

GEOMETRICAL PROGRESSION.

A Geometrical Progression is a series of numbers increasing or decreasing uniformly by a common ratio; that is, by the continual multiplication or division of some particular number. Thus,

1, 2, 4, 8, 16, 32, &c., is an *increasing Geometrical Series*, in which the terms are formed by multiplying successively by the ratio 2.

81, 27, 9, 3, 1, $\frac{1}{3}$, &c., is a decreasing Geometrical Series, in which the terms are formed by dividing successively by the ratio 3. It is evident that either of these may be continued without end.

In an odd number of terms, the square of the mean is equal to the product of the extremes, or of any two terms equidistant from the mean. Thus, in 3, 6, 12, 24, 48; $12 \times 12 = 3 \times 48$ = $6 \times 24 = 144$.

In an even number of terms, the product of the two means is equal to the product of the extremes, or of any two equidistant terms. Thus, in 32, 16, 8, 4, 2, 1; $8 \times 4 = 32 \times 1 =$ $16 \times 2 = 32$.

To give *Theorems*, or Rules expressed in symbols, for the solution of the various cases, as in Arithmetical Progression, let a denote the *less extreme*,

- *z* the greater extreme,
- r the ratio,

n the *number* of terms, and

s the sum of all the terms.

Any three being given, the others may be found.

Note. The twenty *Theorems* following solve all the possible cases in Geometrical Progression.

Theor. I. $r^{n-1} = \frac{z}{a};$ or, $\frac{\log z - \log a}{\log r} + 1 = n.$

* In this case, if the quotient of $\frac{z}{a}$ be divided continually by r, tilt mothing remains; the number of divisions ± 1 will give n.

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ASSISTANT.]

PROGRESSION.

II.
$$\frac{rz-a}{r-1} = s$$
; or, $z + \frac{z-a}{r-1} = s$.
III. $\left(\frac{z}{a}\right)^{\frac{1}{n-1}} = r$; or, $\overline{\text{Log. } z - \log . a \div n - 1} = \text{Log. } r$
IV. $z + \frac{z-a}{\left(\frac{z}{a}\right)^{\frac{1}{n-1}} - 1} = s$.
V. $\frac{s-a}{s-z} = r$.
VI. $\left(\frac{s-a}{s-z}\right)^{n-1} = \frac{z}{a}$; from which *n* may be found, as in
or, $\frac{\text{Log. } z - \log . a}{\text{Log. } (s-a) - \log . (s-z)} + 1 = n$. VII. $ar^{n-1} = z$.
VIII. $\frac{a(r^n-1)}{r-1} = s$. IX. $\frac{(r-1)s+a}{r} = s - \frac{s-a}{r} = z$
X. $r^n = \frac{(r-1)s}{a} + 1$; or, $\frac{\text{Log. } (r-1)s+a - \log . a}{r} = s$.
XI. $z \times \overline{s-z} = 1 = a \times \overline{s-a} = 1$; whence *z* may be found by
Double Position. XII. $\frac{sr}{a} - r^n = \frac{s-a}{a}$; whence *r* may be
found in the same manner.
XIII. $\frac{z}{r^{n-1}} = a$. XIV. $\frac{z(r^n-1)}{r^n - r^{n-1}} = s$.
XV. $rz - (r-1)s = a$. XVI. $r^{n-1} = \frac{z}{rz - (r-1)s}$; or,
 $\frac{1 \log . z - \log . \overline{rz - (r-1)s}}{1 \log . r} + 1 = n$.

XVII. $a \times \overline{s-a}|^{n-1} = z \times \overline{s-z}|^{n-1}$. XVIII. $\frac{r^{n-1}s}{s-z} r^n = \frac{z}{s-z}$

From the two preceding, a and r are to be found by Double Position.

XIX.
$$\frac{(r-1)s}{r^n-1} = a$$
. XX. $\frac{r^n-r^{n-1}}{r^n-1} \times s = z$.

In a Geometrical series decreasing ad infinitum. a becomes =0, and n is infinite, or greater than any assignable number.

Hence the three following will exhibit all the various cases of such a scries.

I.
$$s = \frac{rz}{r-1} = z + \frac{z}{r-1} = \frac{z^3}{z - \frac{z}{r}}$$
. II. $z = \frac{s(r-1)}{r}$. III. $r = \frac{s}{s-z}$.

Note. In these cases, when the ratio is a proper fraction, r must be taken == the reciprocal of the fraction. Thus, when the ratio is $\frac{2}{3}$, $r = \frac{4}{3}$.

Case 1. The less extreme, the ratio, and the number of terms being given, to find the greater extreme (or any remote term) without producing all the intermediate terms.

RULE 1. When the least term is equal to the ratio. Write down a few of the leading terms of the series, and over them the arithmetical series, 1, 2, 3, 4, &c., as *indices* or *exponents*. Find which of the *indices*, added together, will give the *index* of the term sought, and the continual product of the terms standing under those indices will be the term sought.

2. When the least term is not equal to the ratio. Write down the leading terms as before, and over them the *indices*, 0, 1, 2, 3, 4, &co. Examine which of *these*, added together, will give an *index one less* than the *number* of the *term sought*; multiply the terms under such indices into each other, dividing the product of every two by the first term, and the last quotient will be the term required."

Otherwise. By Theorem VII.

(1) A man agrees, for 12 peaches, to pay only the price of the last; reckoning a farthing for the first, and a halfpenny for the second, &c., doubling the price to the last. What must he give for them ?[†]

(2) A farmer, who went to a fair to buy some oxen, met with a drover who had 23, for which he asked him $\pounds 16$. a piece. After a great deal of dodging between the parties, it was finally agreed that the farmer should pay the price of the last ox only, reckoning a farthing for the first, and doubling it to the last. How much would they cost him?

Ans. £1369..1..4.

* If the least term is unity, there will (of course) be no division.

t Here a = 1, r = 2, and n = 12, a and r being unequal.

Indices, 0, 1, 2, 3, 4. Geom. series, 1, 2, 4, 8, 16. Then 4+4+3=11=n-1. Hence $16 \times 16 \times 8 = 2048$ grs. = z, and 2048 grs. = $\mathfrak{D}_{2..2..8}$ Aug.

128

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ABRISTANT.]

PROGRESSION.

(3) A sum of money is to be divided among 8 persons, the first to have £20, the second £60, and so on in triple proportion. What will the last have ?* Ans. £43740.

(4) A gentleman dying left nine sons, to whom and to his executors he bequeathed his estate in the manner following: To his executors £50., to his youngest son twice as much as to the executors, to the next, double that sum, and so on to the eldest. What was his fortune? Ans. £25600.

Case 2. The less extreme, the ratio, and the number of terms being given, to find the sum of all the terms.

RULE. Find the greater extreme as before, and divide the difference between the extremes by the ratio less 1; to the quotient add the greater extreme for the sum required. This is Theorem II. Or, by Theorem VIII; without finding z.

(5) A young man conversant with numbers, agreed with a gentleman to serve him twelve months, provided he would give him a farthing for his first month's service, a penny for the second, and 4d. for the third, &c. What did his wages amount to ?† Ans. £5825..8..51.

(6) A man bought a horse, and by agreement was to give a farthing for the first nail, three for the second, &c. Now supposing there were 8 nails in each of his four shoes, what was the price of the horse? Ans. £965114681693..13..4.

(7) A person whose daughter was married on new-year's day, gave her husband 1s. towards her portion; promising to double the sum on the first day of every month during the year. What was her portion? Ans. £204..15.

(8) A laceman, well versed in numbers, agreed with a gentleman to sell him 22 yards of rich brocaded gold lace. for 2 pins the first yard, 6 pins the second, &c., in triple proportion. What was the price of the lace, valuing the pins

* Indices 0, 1, 2, 3. Geom. series 20, 60, 180, 540. Then 3+3+1=7=n-1. Hence $\frac{540 \times 540 \times 60}{20 \times 20} = 540 \times 27 \times 3 = 43740 = z.$ 20×20 Otherwise $ar^{n-1}=20\times 3^{7}=43740=z$. t Here a=1, r=4, and z=12. Therefore $s = \frac{4^{12}-1}{4-1} = \frac{16777215}{3}$

= 5592405 grs.

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at 100 for a farthing? Also, what did the laceman gain supposing the lace to have cost him \pounds 7. per yard?

Ans. The lace sold for £326886..0..9. Gain £326732..0..9.

Case 3. The first term, and the ratio, being given, to find the sum of an infinite decreasing series.

RULE. Divide the square of the first term by the difference between the first and second.*

(9) What is the sum of the circulating decimal '9', or the series $\frac{9}{10} + \frac{9}{1000} + \frac{9}{1000}$, &c., continued *ad infinitum? Ans.* 1.

(10) Required the sum of the infinite series $\frac{1}{2} + \frac{1}{4} + \frac{1}{8}$, &c.; also of the series $\frac{1}{3} + \frac{1}{9} + \frac{1}{27}$, &c. Ans. 1, and $\frac{1}{2}$.

(11) Suppose a body to be put in motion by a force which gives it a velocity of 10 miles the first minute, (or any given space of time,) 9 miles in the second equal space, and so on in the ratio of $\frac{9}{10}$; how many miles would it pass over, if gontinued in motion for ever? Ans. 100 miles.

SIMPLE INTEREST, BY DECIMALS.

To give Theorems for the solution of the different cases in Simple Interest, let p denote the principal, r the ratio, t the time, (in years,) i the interest, and a the amount.

Note. The Ratio is the interest of \pounds 1. for one year, at the rate per cent. proposed, and may be found by Proportion: thus, at \pounds 5. per cent. per annum, say,

As $\pounds 100 : \pounds 5 :: 1\pounds : \pounds 05$, the ratio.

Therefore the ratio at

3 per 34	r ce	ent.	is	•	•	·03 ·035 ·04	$\begin{vmatrix} 4\frac{1}{2} \\ 5 \end{vmatrix}$	per	.ce	nt.	is	•	•	•	·045 ·05	
						•04										

Case 1. When the principal, rate per cent. and time are given, to find the interest.

RULE. Multiply the principal, ratio, and time together, and the product will be the interest required.

That is, prt = i.

(1) What is the interest of $\pounds 945..10$. for 3 years, at $\pounds 5$. per cent. per annum ?†

* See the third formula, Theorem I. for infinite series, page 128. $pri = \pounds 945 \cdot 5 \times \cdot 05 \times 3 = \pounds 141 \cdot \ell^2 \cdot 5 = \pounds 141 \cdot 16 \cdot .6$. Ans.

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ASSISTANT.]

(2) What is the interest of $\pounds 547..14$, at $\pounds 4$. per cent. per annum, for 6 years? Ans. $\pounds 131..8..11..2.08$ qrs.

(3) What is the interest of $\pounds 796..15$., at $\pounds 4\frac{1}{2}$. per cent. per sannum, for 5 years? Ans. $\pounds 179..5..4\frac{1}{2}$.

(4) What is the interest of $\pounds 397..9..5$. for $2\frac{1}{2}$ years, at $\pounds 3\frac{1}{2}$. per cent. per annum? Ans. $\pounds 34..15..6..3\cdot 55$ qrs.

(5) What is the interest of £554..17..6. for 3 years, 8 months, at £4½. per cent. per annum? Ans. £91..11..1.05d.
(6) What is the interest of £236..18..8. for 3 years, 8 months, at £5½. per cent. per annum?

Ans. £47..15..7..2 293 grs.

When the interest is for any number of days only.

RULE. Multiply the interest of $\mathcal{L}1$. for a day, at the given rate, by the principal and the number of days, and the product will be the answer.

The Interest of $\pounds 1$. for one day.

At £2 per ce	ent.—.£	C·00005479452*	at $\pounds 4 = \cdot 00010958904$	
2]	2000	·00006849315	$4\frac{1}{2}$ - 00012328767	
3	*** ,	$\cdot 00008219178$	5 = 00013698630	
313	 ,	$\cdot 00009589041$	$5\frac{1}{2} = 00015068493, \&c$	3.

(7) What is the interest of $\pounds 240$. for 120 days, at $\pounds 4$. per cent. per annum ?[†]

(8) What is the interest of £364..18. for 154 days, at £5. per cent. per annum? Ans. £7..13..11 $\frac{1}{4}$.

(9) What is the interest of $\pounds 725..15$. for 74 days, at $\pounds 4$. per cent. per annum? Ans. $\pounds 5..17..8\frac{1}{2}$.

(10) What is the interest of \pounds 100. from the 1st of June, 1826, to the 9th of March following, at \pounds 5. per cent. per annum? Ans. \pounds 3..16..113.

Case 2. When p, r, and t are given, to find a.

RULE. prt + p = a.

(11) What will $\pounds 279..12$. amount to in 7 years, at $\pounds 4\frac{1}{2}$ per cent. per annum ?

(12) What will $\pounds 320..17$ amount to in 5 years, at $\pounds 3\frac{1}{2}$ per cent. per annum ? Ans. $\pounds 376..19..11..2.8$ qrs.

* The table is formed thus :---

As 365 days : £02 :: 1 day : £00005479452, &c.

* $\cdot 00010953904 \times 240 \times 120 = \pounds 3 \cdot 156164352 = \pounds 3 \cdot .14$. Ans. $\downarrow 279 \cdot 6 \times \cdot 045 \times 7 + 279 \cdot 6 = \pounds 367 \cdot 674 = \pounds 367 \cdot .13 \cdot .5 \cdot .3 \cdot 04$ grs.

SIMPLE INTEREST.

(13) What will $\pounds 926..12$. amount to in 5½ years, at $\pounds 4$. per cent. per annum? Ans. $\pounds 1130..9..0..192$ grs.

(14) What will £273..18. amount to in 4 years, 175 days, at £3. per cent. per annum? Ans. £310..14..1..3 \cdot 3512 qrs

Case 3. When a, r, and t are given, to find p.

RULE. $\frac{a}{rt+1}=p$

(15) What principal, being put to interest, will amount to $\pounds 367..13..5..304 \ qrs.$ in 7 years, at $\pounds 4\frac{1}{2}$. per cent. per annum?

(16) What principal will amount to £376..19..11..2.8 qrs. in 5 years, at $\pounds 3\frac{1}{2}$. per cent. per annum? Ans. £320..17:

(17) What principal will amount to £1130..9..0..1.92 qrs. in $5\frac{1}{2}$ years, at £4. per cent. per annum? Ans. £926..12

(18) What principal will amount to £310..14..1..3 3512 grs. in 4 years, 175 days, at £3. per cent. per annum? Ans. £273..18.

Case 4. When a, p, and t are given, to find r.

RULE. $\frac{a-p}{pt}=r.$

(19) At what rate per cent. per annum will $\pounds 279..12$. amount to $\pounds 367..13..5..3.04$ grs. in 7 years ?

(20) At what rate per cent. per annum will $\pounds 320..17$, amount to $\pounds 376..19..11..28$ grs. in 5 years?

Ans. £31. per cent.

TUTOR'S

(21) At what rate per cent. per annum will £926..12, amount to £1130..9..0.1 92 qrs. in 51 years?

Ans. £4. per cent.

(22) At what rate per cent. per annum will £273..18 amount to £310..14..1..3 3512 qrs. in 4 years, 175 days? Ans. £3. per cent

Case 5. When a, p, and r are given, to find t.

EULE.
$$\frac{a-p}{pr} = t$$
.

* $045 \times 7 + 1 = 1.315$; then $367.674 \div 1.315 = \pounds 279.6 = \pounds 279.12$ Ans.

 $\frac{1}{1} \frac{367 \cdot 674 - 279 \cdot 6}{279 \cdot 6 \times 7} = \frac{88 \cdot 074}{1957 \cdot 2} = \cdot 045, \text{ or } \pounds 4\frac{1}{2}. \text{ per cent. } Ans.$

rs, at £4. 92 qrs. 175 days, 3512 qrs

p.

amount to r annum ? 1..2.8 qrs. 320..17: ..1.92 qrs. £926..12 .1..3.3512 um ?

273..18.

7.

£279..12.

£320..17.

per cent. £926..12.

per cent. £273..18 days ? 3. per cent

Ιţ.

=£279..12

Ans.

(23) In what time will £279..12 amount to £367..13..5.. 3.04 qrs at £4 $\frac{1}{2}$ per cent per annum ?*

(24) In what time will £320..17. amount to £376..19..11.. 2.8 qrs. at £3 $\frac{1}{2}$. per cent per annum? Ans. 5 years.

(25) In what time will £926..12. amount to £1130..9..0,. 1.92 qrs. at £4. per cent. per annum? Ans. $5\frac{1}{2}$ years.

(26) In what time will £273..18. amount to £310..14..1.. 3.3512 grs. at £3. per cent. per annum?

Ans. 4 years, 175 days.

ANNUITIES.

An annuity is a yearly income or rent. Perpetual Annuities are those which are to continue for ever; Terminable Annuities are to cease within a limited time; and Life Annuities are to continue during the term of life of one or more persons.

The Amount of Annuities in Arrears.

Let u denote the annuity, r, t, and a, as before.

Case 1. Given, u, r, and t, to find a.

RULE. $\left(\frac{t-1,r}{2}+1\right) \times tu = a$.

ABBISTANT.]

(27) If a salary of £150, be forborne 5 years, at £5, per cent. per annum, what will be the amount? \dagger

(28) If £250. yearly pension be forborne 7 years, what will it amount to at £4. per cent. per annum? Ans. £1960.

(29) There is a house let upon lease for $5\frac{1}{2}$ years, at £60. per annum, what will be the accumulated rent, allowing interest at £4 $\frac{1}{2}$. per cent. per annum? Ans. £363..8..3

(30) Suppose an annual pension of $\pounds 28$. remain unpaid for 8 years, what would it amount to at $\pounds 5$. per cent. per annum 1 Ans. $\pounds 263..4$.

Norz. When the annuity is payable half-yearly, or quarterly. \cdot will denote a single payment, r, the interest of £1. for that interval ω time,

and t, the number of payments. (31) If a salary of $\pounds 150$., payable every half-year, remain

unpaid for 5 years, what will it amount to in that time, allowing interest at $\pounds 5$. per cent. per annum? Ans. $\pounds 834..7..6$.

* $367 \cdot 674 - 279 \cdot 6 = 88 \cdot 074$, and $279 \cdot 6 \times \cdot 045 = 12 \cdot 582$; then $88 \cdot 074 \div 12 \cdot 582 = 7$ years, Ans.

 $\frac{1}{2} \left(\frac{4 \times \cdot 05}{2} + 1 \right) \times 5 \times 150 = (2 \times \cdot 05 + 1) \times 5 \times 150 = 1.1 \times 10^{-1}$

SIMPLE INTEREST.

TUTOR'S

(32) If a salary of £150., payable every quarter, were left unpaid for 5 years, what would it amount to in that time at £5. per cent. per annum? Ans. £839. 1..3.

NOTE. It may be observed by comparing the results of the 27th, **31st**, and 32nd examples, that half-yearly payments are more advantageous than yearly, and quarterly more than half-yearly.

Case 2. When a, r, and t, are given, to find u.

RULE. $\frac{2a}{(r.(t-1)+2)\times t} = u.$

. (33) If a salary amounted to \pounds 825. in 5 years, at \pounds 5, per cent. per annum, what was the salary ?*

(34) If a house has been let upon lease for $5\frac{1}{2}$ years, and the amount in that time is £363..8..3. at £4 $\frac{1}{2}$. per cent. per annum, what is the yearly rent? Ans. £60.

(35) If a pension amounted to $\pounds 1960$. in 7 years, at $\pounds 4$. per cent. per annum, what was the pension? Ans. $\pounds 250$.

(36) Suppose the amount of z pension was £263..4. in 8 years, at £5. per cent. per annum, what was the pension? Ans. £28.

(37) If the amount of a salary, payable half-yearly, be $\pounds 834..7..6$. in 5 years, at $\pounds 5$. per cent. per annum; what is the salary per year? \uparrow Ans. $\pounds 150$.

(38) If the amount of an annuity, payable quarterly, was \pounds 839.1.3. in 5 years, at \pounds 5. per cent. per annum; what was the annuity? Ans. \pounds 150.

Case 3. When u, a, and t are given, to find r.

RULE. $\frac{(a-ut)\times 2}{(t-1)\times ut}=r.$

(39) If a salary of £150, per annum amounts to £825, in 5 years, what is the rate per cent. ?

(40) If a house has been let upon lease for $5\frac{1}{2}$ years, at £60. per annum, at what rate per cent. would it amount to £363..8..3? Ans. £4 $\frac{1}{2}$. per cent.

• 825 × 2	1650	1650	£150 A	tne.	
$(.)5 \times 4 + 25) \times 5$	2·2×5	11	-100. A		
† See note, p. 133.					
$(825 - \overline{150 \times 5})$		-750 .	75	$r = \frac{1}{20} = 0$	15
$4 \times 150 \times 5$	2 × 150	$\overline{5\times5} = \overline{1}$	50×10	20	Γ.
• r: therefore the rate i	is £5. per cent	t.			

SIMPLE INTEREST.

(41) If a pension of $\pounds 250$. per annum amounts to $\pounds 1960$. in 7 years, what is the rate per cent.? Ans. $\pounds 4$. per cent.

(42) Suppose the amount of a yearly pension of £28. be £263..4. in 8 years, what is the rate per cent. per annum? Ans. £5. per cent.

(43) If a salary of £150. per annum, payable half-yearly, amount to £834..7..6. in 5 years, what is the rate per cent. ?* Ans. £5. per cent.

(44) If an annuity of £150. per annum, payable quarterly, amount to £839..1..3. in 5 years, what is the rate per cent.? Ans. £5. per cent.

Case 4. When u, a, and r are given, to find t.

ROLE.
$$\frac{\sqrt{8r}\frac{a}{u} + (2-r)^2 - (2-r)}{2r} = t.$$

Or, put $\frac{1}{r} - \frac{1}{2} = m$; then $\sqrt{\left(\frac{2a}{ur} + m^2\right)} - m = t.$

(45) In what time will a salary of \pounds 150. per annum amount to \pounds 825. at \pounds 5. per cent. ?†

(46) If a house is let upon lease at \pounds 60, per annum till it amount to \pounds 363..8..3, at \pounds 4¹/₂, per cent. per annum, for what term of years was it let? Ans. 5¹/₂ years.

(47) If a pension of £250, per annum, having been forborne a certain time, amount to £1960, at £4, per cent., how long has been the time of forbearance? Ans. 7 years.

(48) In what time will a yearly pension of £28. amount to £263..4. at £5. per cent. per annum? Ans. 8 years.

(49) If an annuity of £150. per annum, payable halfyearly, amounted to £834..7..6. at £5. per cent, what time was the payment forborne?* Ans. 5 years.

(50) If a yearly pension of $\pounds 150$, payable quarterly, amounts to $\pounds 839..1..3$. at $\pounds 5$. per cent. per annum, what has been the time of forbearance? Ans. 5 years.

• See Note, p. 133
•
$$\sqrt{8 \times \cdot 05 \times \frac{825}{150} + (2 - \cdot 05)^2 - (2 - \cdot 05)}}_{2 \times \cdot 05}$$

• $\sqrt{\frac{\cdot 40 \times 5 \cdot 5 + 3 \cdot 6025 - 1 \cdot 95}{\cdot 1}}_{2 \times \cdot 05} = 2 \cdot 45 - 1 \cdot 95}_{2 \times \cdot 1} = 5 \div \cdot 1 = 5 \text{ ycars. A*s.}$

were left at time at 9.1..3.

[TUTOR'S

ASSISTANT.

of the 27th, pre advanta-

at £5. per

years, and r cent. per $is. \pm 60.$ ars, at $\pm 4.$ s. $\pm 250.$ 63..4. in 8 ension ? $ns. \pm 28.$ yearly, be n; what is s. $\pm 150.$ rterly, was ; what was s. $\pm 150.$ d r.

to £825. in

¹/₂ years, at amount to per cent.

5.



SIMPLE INTEREST.

[TUTOR'S

No.	£. s. d	. qrs.	No.	8. 0	l. qrs.	No.	qrs.
30000	82 3 1	0 0.11	200	10 1	1 2.03	1	2.63
20000	54 15 1	0 2.74	100	5	5 3.01	0.9	2.37
10000	27 7 1	1 1.37	90	41	1 0.71	0.8	2.10
9000		1 3.23	80	4	4 2.41	0.7	1.84
8000		4 1.10	70	-	0 0.11	0.6	1.58
7000		6 2.96	60		3 1.81		1.32
6000		9 0.82	50	2	8 3.51	0·5 0·4	1.05
5000		1 2.68	40		2 1.21	0.3	0.79
4000		2 0.55	30	ĩ	7 2.90	0.2	0.23 J
3000		4 2.41	20	î	1 0.60	0.1	0.26
2000		7 0.27	ĩo	Ō	6 2.30	0.09	0.24
1000		9 2:14	9	ŏ	5 3.67	0.08	0.21
900		3 3.14		ŏ	5 1.04	0.00	0.18
			87	Ő	4 2.41	0.06	0.16
800				-			
700	1 18	4 1.10	6	0	3 3.78	0.05	0.13
600		0 2.08	5	0	3 1.15	0.04	0.11
500	17	4 3 07	4	0	2 2.52	0.03	0.08
400		1 0.02	3	0	1 3.89	0.05	0.02
300	0 16	5 1.04	2	0	1 1.26	0.01	0.03
the second s							

A Table by which the Interest of any sum from £1. to £30000. may be easily computed for any number of days, at any rate per cent.

The above Table is thus constructed: as 365 days : £1. :: 1 day : 2.63 grs., &c. Hence it appears that the several tabular sums are those which answer to the respective numbers of days, at the rate of £1. per year.

In a similar Table in Rees's Cyclopædia, there are no fewer than 16 errors. In Dr. Hutton's Table, (Arithmetic, page 84, 12th edition,) there is one error. The above may be depended on as accurate.

RULE. Multiply the principal by the rate, both in pounds, and the product by the number of days: divide the last product by 100, collect from the Table the several sums answering to the several parts of the quotient, and the aggregate amount will be the Interest required.

Example 1. What	t is the interest of .	£3	7()10). fo	r 220	days
at £41. per cent. p	er annum ?		£	. s.	<i>d</i> .	qrs.	• 3
370.5	Against 3000 stand	ls	8	4	4	2.41	
4.5	600						
18525	60		0	3	3	1.81	
14820	7	•	0	Q	4	2.41	
1667.25	0.9		0	0	0	2.37	
1007 20	0.05 .		0	0	0	0.13	

decimal.

3.21 Ans

z. per cent.	per annum s				æ,	. S.	<i>u</i> .
370.5	Against 3000	sta	ind	ls	8	4	4
4.5	600		•		1	12	10
18525	60		•	•	0	3	3
14820	7			•	0	Ò	-4
1667.25	01	·9.	•	•	0	0	0
220	01	05	•		0	0	0
3334500	3667	95]	10	0	11
333450		'Tr	ue	t	o t	he l	ast

3667 95.00

000. may be er cent.

	qrs.	
	2.63	
ł	2.37	
	2.10	
l	1.84	
	1.58	
ł	1.32	
	1.05	
	0.79	
ļ	0·53 0·26	
	0.26	
	0.54	
	0.21	
ŀ	0.18	
l	0.16	
1	0.13	
	0.11	
l	0.08	
l	0.05	
1	0.03	

. :: 1 day 1 ms are those te of £1. per

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nds, and the y 100, collect parts of the quired.

r 220 days

qrs.	
2.41	
2.08	
1.81	
2.41	
2.37	

0.13

3.21 Ans

decimal.

SSISTANT.]	SIMPLE INTEREST.			13	Ý
	Taking Ex. 8, page 131, we	ha ha	Ve		
364 ⁻ 9 5	£		d.		
1824.5	Against 2000 stands 5			qrs. 0·27	
154	800 2			0.11	
72980	9 0	0	5	3 67	
273675	0.7 0	0	0	1.84	
2809 73.0	0.03 0	0	0	0·08	
2009/13.0	2809.73 7	13	11	1.97 An	5

Example 3. What is the interest of $\pounds 17..10$. for 117 days at $\pounds 43$. per cent. per annum? 17.5

11.0	
4.75	£. s. d. grs.
875	Against 90 stands 0 4 11 0.71
1225	7 0 0 4 2.41
700	0.2 0 0 0 0.53
83.125	$0.05 \dots 0 0 0.13$
117	97.25 0 5 3 3.78 Ans.
581875	
914375	
97 25.625	

To find the amount of a yearly income or salary, &c, for a number of days.

Multiply the number of pounds per year by the number of lays; collect the Tabular sums answering to the product, as before, and their aggregate will be the answer.

Example. What will a person receive for 45 days, at the rate of $\pounds 105$. per annum ?

105 45	Against 4000 stands			d. 2	
525	700	1	18	4	1.10
420	20	Ó	1		0.60
4705	5	Ó	0	3	1.12
4140	4725	12	18	10	3.40 Ans.

Norr. Any of the preceding examples of interest for days, in page 131, or examples 20 and 21, page 68, may be worked by this method.

DISCOUNT.

June Aug. Sept. Dec. Feb. Mar. May July Nov. Apr Oct. Jan To 90120151181212243273304334365 31 59 Jan. |334|365|||28|||59|||89|120|150|181|212|242|273|303|Feb. Mar. |306|337|365||31||61||92|122|153|184|214|245|275Apr. 245 276 304 335 365 31 61 May 92 123 153 184 214 From 214 245 273 304 334 365 30 61 92 122 153 183Jime 184 215 243 274 304 335 365 31 July 62 92 123 153 Aug. |153|184|212|243|273|304|334|365|||31|61 92.22Sept. |122|153|181|212|242|273|303|334|365|30 61 91 92|123|151|182|212|243|273|304|335|365||31|Oct. 61 Nov. 61 92 120 151 181 212 242 273 304 334 365 30 62 90 121 151 182 212 243 274 304 335 365 Dec. 31

A Table showing the number of days from any day in the month to the same day in any other month through the year

DISCOUNT.

LET s represent the sum to be discounted, r the ratio, t the time, (in years,) and p the present worth.

Case 1. Given s, r, and t, to find p.

RULE.
$$\frac{s}{rt+1} = p$$
.

(1) What is the present worth of $\pounds 357..10$. to be paid 9 months hence, at $\pounds 5$. per cent. per annum ?*

(2) What is the present worth of £275..10 due 7 months hence, at £5. per cent per annum? Ans. £267..13..10.152d.

(3) What is the present worth of £875..5. 6. due 5 months hence, at $\pounds 4\frac{1}{2}$. per cent. per annum?

Ans. £859..3..3.01824 qrs.

(4) How much ready money can I receive for a note of $\pounds 75$ due 15 months hence, at $\pounds 5$. per cent. per approximate $Ans. \pounds 70..11..9.1764d.$

 $357 \cdot 5 - 05 \times 75 + 1 = 344 \cdot 5783 = £344 \cdot 11 \cdot 6 \cdot 3 \cdot 168 \ qrs. \ Ans.$

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month to the

Uct. Nov. Dec.	
$\begin{array}{c} 73 \\ 204 \\ 334 \\ 42 \\ 273 \\ 303 \\ 14 \\ 245 \\ 275 \\ 83 \\ 214 \\ 244 \\ 53 \\ 184 \\ 214 \\ 22 \\ 153 \\ 183 \\ 92 \\ 123 \\ 153 \\ 61 \\ 92 \\ 22 \\ 30 \\ 61 \\ 91 \\ 365 \\ 31 \\ 61 \\ 34 \\ 365 \\ 30 \\ 304 \\ 335 \\ 365 \end{array}$	

e ratio, t the

to be paid 9

ue 7 months $.13..10 \cdot 152d$. lue 5 months

01824 qrs. for a note of annum? ...9.1764d.

68 grs. Ans.

A SISTANT.]

DISCOUNT.

Case 2. When p, r, and t are given, to find s.

RULE prt + p = s.

(5) If the present worth of a sum of money due 9 months hence, allowing $\pounds 5$. per cent. per annum, be $\pounds 344..11..6$. 3.168 qrs., what was the sum due ?*

(6) A person owing a certain sum, payable 7 months hence agrees with the creditor to pay him down £267..13..10.152d., allowing £5. per cent. per annum for present payment : what is the debt? Ans. £275..10.

(7) A person receives £859..3..3..3.01824 qrs. for a sum of money due 5 months hence, allowing the debtor £4 $\frac{1}{2}$. per cent. per annum for present payment: what was the sum due?

Ans. £875..5..6.

(8) A person paid $\pounds 70..11..9.1764d$. for a debt due 15 months hence, being allowed $\pounds 5$. per cent. per annum for the discount. How much was the debt? Ans. $\pounds 75$.

Case 3. When s, p, and t are given, to find r.

RULE. $\frac{s-p}{pt} = r.$

(9) At what rate per cent. per annum will £357..10., payable 9 months hence, produce £344..11..6..3.168 qrs. for present payment ?†

(10) At what rate per cent. per annum will $\pounds 275..10.$, payable 7 months hence, be worth $\pounds 267..13..10.152d$. for present payment? Ans. $\pounds 5.$ per cent.

(11) At what rate per cent. per annum will $\pounds 875..5..6.$, payable 5 months hence, produce the present payment of $\pounds 859..3..3..3 \cdot 01824$ qrs.? Ans. $\pounds 4\frac{1}{2}$, per cent.

(12) At what rate per cent. per annum will $\pounds 75.$, payable 15 months hence, produce the present payment of $\pounds 70..11..9.1764d.$ Ans. $\pounds 5.$ per cent.

Case 4. When s, p, and r are given, to find t.

RULE.
$$\frac{s-p}{pr} = t$$

* $344.5783 \times .05 \times .75 + 344.5783 = £357..10$. Ana

 $\frac{1}{357 \cdot 5 - 344 \cdot 5783} = 05 \text{ or } \pounds 5. \text{ per cent. Ang.}$

(13) The present worth of £357..10., due at a certain time to come, is £344..11..6..3.168 qrs. at £5. per cent. per annum: in what time should the sum have been paid without any discount?

(14) The present worth of £275..10., due at a certain time to come, is £267..13..10.152d. at £5. per cent. per annum: in what time should the sum have been paid without discount? Ans. 7 months.

(15) A person receives £859..3..3.01824 qrs. for £875.. 5.6., due at a certain time to come, allowing £ $4\frac{1}{2}$. per cent. per annum discount: in what time should the debt have been discharged without any discount? Ans. 5 months.

(16) I have received £70..11..9 1764d. for a debt of £75., allowing the person £5. per cent. per annum for prompt payment: when would the debt have been payable without discount? Ans. 15 months.

EQUATION OF PAYMENTS.

To find the equated time for the payment of a sum of money due at several times.

RULE. Find the present worth of each payment for its respective time by Case 1, Discount, page 138, thus :--

Add all the present worths together, call their sum p', and the sum of all the payments s'; then by Case 4, Discount, p. 139.† $\frac{1}{p'r+1} = p.$ $\frac{p'-p'}{p'r} = e, \quad the$ equated time.

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$\frac{357 \cdot 5 - 344 \cdot 5783}{344 \cdot 5783 \times \cdot 05} = \cdot 75 = 9 \text{ months. Ans.}$

† The above is Kersey's Rule. It produces a result something less than the precise truth, but sufficiently accurate for any purpose of real utility. The only Rule that is strictly true for the equation of two payments at Simple Interest is that given by Malcolm, which is founded on the principle, that the interest of the money withheld after it becomes due, ought to be equal to the discount of that which is paid before it is due. But Malcolm's Rule, though it has Leen simplified in expression by Bonnycastle and others, and is capable of further simplification than I have yet seen in print, is at best very operose, and may be regarded, Mr. Keith justly observes, as a useless curiosity.—EDITOR.

ertain time per annum : vithout any

certain time per annum: without dis-7 months. s. for £875.. $\frac{1}{2}$. per cent. b have been 5 months. ebt of £75., for prompt able without

5 months.

of money dus

 $\overline{1} = p$ $\frac{p'}{r} = e$, the equated time.

something less purpose of real ton of two payis founded on fter it becomes aid before it is in expression plification than y be regarded, ntor.

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(1) D owes E \pounds 200., whereof \pounds 40. is to be paid at three months, \pounds 60. at 6 months, and \pounds 100. at 9 months: at what time may the whole debt be paid together, discount being allowed at \pounds 5. per cent. per annum?*

(2) D owes E £800, whereof £200. is to be paid in 3 months, £200. at 4 months, and £400. at 6 months; but they agree to have the whole paid at once, allowing discount at the rate of £5. per cent. per annum. The equated time is required. Ans. 4 months, 22 days.

(3) E owes F \pounds 1200., which is to be paid as follows: \pounds 200. down, \pounds 500, at the end of ten months, and the rest at the end of 20 months; but they agree to have only one payment of the whole, discounting at \pounds 3. per cent. per annum. The equated time is required. Ans. 1 year, 11 days.

COMPOUND INTEREST.

THE same symbols are adopted in this as in Simple Interest, and denote the same things; except that the ratio (r,) which in Simple Interest denotes the *interest* of $\pounds 1$., signifies in this Rule the *amount* of $\pounds 1$. for a year. It may be thus found by Proportion.

As $\pounds 100 : \pounds 105 : : \pounds 1 : \pounds 1 \cdot 05$, the ratio at $\pounds 5$ per cent. per annum. The ratios are, therefore,

at	3 per	cent.	:		•	1.03 at	4 <u>1</u> pe	er cent.		1.045
	31	"			•	1.035	5	"		I.02
	4	66	•	•	•	1.04	51	"	•	1.055, &c.

 $\frac{40}{1\cdot 0125} = 39\cdot 5061; \quad \frac{60}{1\cdot 025} = 58\cdot 5365; \quad \frac{100}{1\cdot 0375} = 96\cdot 3855;$ then $200 - \overline{39.5061 + 58.5365 + 96.3855} = 5.5719$; 5.5719 and $\frac{5.6715}{194\cdot4281\times05} = \cdot57315 = 6$ months, 26 days. Ans.

t The law of England does not allow the lender to receive Compoun Interest for his money when the receipt of the Interest has been fo borne. But in the granting or purchasing of Annuities, Leases, & either immediate or in reversion, it is customary, and indeed necessary to compute them on the principles of Compound Interest, for otherwise the calculation would involve most egregious injustice and absurdity.

COMPOUND INTEREST.

Yr.e	3 ner Cent	31 ner Cent	4 per Cent.	41 mer Cent.	5 ner Cent
$\frac{1}{1}$	$\frac{1.0300000}{1.0300000}$	1.0350000	1.0.100000	1.0450000	1.0500000
	1.0609000	1.0330000 1.0712250	1.0316000	1.0920250	1.1025000
ŝ	1.0927270	$1 \cdot 1087179$	$1 \cdot 1248640$	$1 \cdot 1411661$	1.1576250
	1.1255088	1.1475230	1.1698586	1.1925186	1.2155062
5	$1 \cdot 1200000$ $1 \cdot 1592741$	1.1876863	1.2166529	1.2461819	1.2762816
$\frac{3}{6}$					
	1.1940523	1.2292553	1.2653190	1.3022601	1.3400956
7	1.2298739	1.2722793	1.3159318	1.3608618	1.4071004
$\frac{8}{9}$	1.2667701	1.3168090	1.3685690	$1 \cdot 4221006$ $1 \cdot 4860951$	1.4774554
10	1.3047732 1.3439164	1.3628974 1.4105988	$1 \cdot 4233113$ $1 \cdot 4802443$	1.48609.91 1.5529694	1.5513282 1.6288946
11	1.3842339	1.4599697	1.5394541	1.6228530	1.7103394
12	1.4257609	1.5110687	1.6010322	1.6958814	1.7958563
13	1.4685337	1.5639561	1.6650735	1.7721961	1.8856491
14	1.5125897	1.6186945	1.7316764	1.8519449	1.9799316
15	1.5579674	1.6753488	1.8009435	1.9352824	2.0789282
16	1.6047064	1.7339860	1.8729812	2.0223702	2.1828746
17	1.6528476	1.7946756	1.9479005	2.1133768	2.2920183
18	1 702 4331	1.8574892	2.0258165	2.2084788	2.4066192
19	1.7535060	1.9225013	$2 \cdot 1068492$	2.3078603	2.5269502
20	1.8061112	1.9897889	2.1911231	2.4117140	2.6532977
21	1.8602946	2.0594315	2.2787681	$2 \cdot 5202412$	2.7859626
22	1.9161034	2.1315116	2.3699133	2.6336520	2.9252607
23	1.9735865	2.2061145	2.4647155	2.7521663	3.0715237
24	2.0327941	2.2833285	2.5633042	2.8760138	3.2250999
25	2.0937779	2.3632450	2.6658363	3.0054345	3.3863549
26	$2 \cdot 1565913$	2.4459586	2.7724693	3.1406790	3.5556727
27	2.2212890	2.5315671	2.8833686	3.2820096	3.7334563
28	2.2879277	2.6201720	2.9987033	3.4297000	3.9201291
29	2.3565655	2.7118780	$3 \cdot 1186514$	$3 \cdot 5840365$	4.1161356
30	2.4272625	2.8067937	3.2433975	3.7453181	4.3219424
16	2.5000303	2.9050315	3.3731334	3.9138574	4.5380395
32	2.5750827	3.0067076	3.2080287	4.0399810	4.7649414
33	2.6523352	3.1119123	3.6483811	4.2740302	5.0031885
34	2.7319053	3.2208603	3.7913163	4.4663615	5.2533479
35	$2 \cdot 8138624$	3.3335904	3.9460390	4.6673473	5.5160153
36	2.8982783	3.4502661	4.1039325	4.8773785	5.7918161
37	2.9852266	3.5710254	4.2680898	5.0968605	6.0814069
33	3.0747834	3.6960113	4.4338134	5.3262192	6.3854773
39	3.1670269	3.8253717	4.6163660	5.5658991	6.7047511
40	3 2620378	3.9592597	4.8010206	5.8163645	7.0399887
-10	0 ~0~0010	9 0002001	1 2 00 10 200	0.0100040	1 0.000001

A Table of the Amount of £1. for years.

These tabular numbers are the successive powers of r; thus, $1.05^2 = 1.1025$, &c.*

* The amount of $\pounds 1$. in t years is the last term of an increasing geometrical series, of which the first term = the ratio, and the number of terms = t, because the first year's amount is identical with the ratio; and as $1:r::r:r^2 =$ the amount in 2 years, as $1:r::r^2::r^3 =$ the amount in 3 years, &c. The successive amounts r, r^2, r^3 , &c., are evidently in geometrical progression, and the amount in t years is

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per Cent.

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·1025000

1576250 2155062

2762816

·3400956

·4071004

·4774554

 $\cdot 5513282$

·6288946

 $\cdot 7103394$ 7958563

·8856491

 $\cdot 9799316$ 0789282

 $\cdot 1828746$ 2920183

4066192

.5269502

·6532977

·7859626

·9252607

071523722509993.3863549 -5556727

 $\cdot 7334563$

 $\cdot 9201291$

 $\cdot 1161356$

 $\cdot 3219424$

 $\cdot 5380395$

.7649414

0031885

·2533479

·5160153

 $\cdot 7918161$

0814069

·3854773

·7047511

·0399887

thus, 1 052=

creasing geo

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Case 1. When p, r, and t are given, to find a.

RULE. $pr^{t} == a$. Or, log. $r \times t + \log_{10} p = \log_{10} a$.

Or by the Table. Multiply the tabular amount of £1. by the principal, and the product will be the amount required.

(1) What will £225. amount to in 3 years, at £5. per cent. per annum ?*

(2) What will $\pounds 200$, amount to in 4 years, at $\pounds 5$, per cent per annum? Ans. £243..2..0..1.2 grs

(3) What will £450, amount to in 5 years, at £4, per cent. per annum ? Ans. £547..9..10..2.0538368 grs.

(4) What will £500. amount to in 4 years, at £4 $\frac{1}{2}$. per Ans. £596.5..2.232075d. cent. per annum?

Case 2. When a, r, and t are given, to find p.

RULE. $\frac{a}{t} = p$. Or, $\overline{\log a - \log r} \times t = \log p$.

(5) What principal, being put to interest, will amount to £260..9..3³. in 3 years, at £5. per cent. per annum ?†

(6) What principal, being put to interest, will amount to $\pounds 243..2..0..1 \cdot 2$ grs. in 4 years, at $\pounds 5$. per cent. per annum? Ans. £200.

(7) What principal will amount to $\pounds 547..9..10..2.0538368$ qrs. in 5 years, at £4. per cent. per annum? Ans. £450.

 $= 1^{4}$, because the *index* always corresponds with the time. By referring to Theorem VII, Geometrical Progression, it will also be seen that such last term $= r \times r^{t-1} = r^t$, when a = r.

The immense increase of money accumulating at Compound Interest for a long period is sufficient to astonish the human mind, and to stagger the credibility of persons who are not in some degree conversant with the properties of Geometrical Progression. The amount of a farthing, placed out at Compound Interest at the commencement of the Christian era, and continued to the conclusion of the eighteenth century, would be 144035 quintillions of pounds. But of the magnitude of this sum, spoken of in the abstract, no just conception can be formed When, however, by a further calculation, we have ascertained that to coin such a quantity of money (were it possible) in sovereigns of the present weight and fineness, would require 60,308170 solid globes of gold, each as large as the earth, we are enabled to entertain a more adequate idea of the sum whose vastness, without having recourse to this adscititious assistance, placed it almost beyond the reach of our livited understandings.

The amount at Simple Interest, for the same period, would be only 1s. 103d .-- EDITOR.

* 1.05³ × 225 = 1.57625 × 225 = 260.465625 = £260..9..3 Ans

 $+ \frac{260 \cdot 465625}{1 \cdot 05^3} = \frac{260 \cdot 465625}{1 \cdot 157625} = \pounds 225.$ Ans.

th the ratio; $2::r^3 = the$ 13, &c., are

in t years is

COMPOUND INTEREST

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(8) What principal will amount to $\pounds 596..5..2 \cdot 232075d$. in 4 years, at $\pounds 4\frac{1}{4}$ per cent. per annum? Ans. $\pounds 500$.

Case 3. When p, a, and t are given, to find r.

RELE. $\frac{a}{p} = r^{t}$, the root of which, being extracted, will give r.

Or, $\log a - \log p - t = \log r$.

(9) At what rate per cent. per annum will £225. amount to £260..9..33. in 3 years ?*

(10) At what rate per cent. per annum will £200. amount to £243..2..0..1.2 grs. in 4 years? Ans. £5. per cent.

(11) At what rate per cent. per annum will £450. amount

o £547..9..10..2 0538368 qrs. in 5 years? Ans. £4. per cent.
 (12) At what rate per cent. per annum will £500. amount

to £596.2593003125 in 4 years ? Ans. £41. per cent.

Case 4. When p, a, and r are given, to find t.

RULE. $\frac{a}{p} = r^{i}$, which being continually divided by r till here r^{i} remains, the number of the divisions will be c_{i} at to t.

Or, $\log a - \log p + \log r = t.t$

(13) In what time will £225. amount to £260..9..3 $\frac{3}{4}$. at £5. per cent. per annum $\frac{1}{2}$

(14) In what time will £200. amount to £243..2025. a £5. per cent. per annum? Ans. 4 years.

(15) In what time will £450. amount to £547..9..10 2.0538368 qrs. at £4. per cent. per annum? Ans. 5 years.

(16) In what time will £500. amount to £596.2593003125 at £44. per cent. per annum? Ans. 4 years.

THE AMOUNT OF ANNUITIES IN ARREARS.

Norz. u represents the annuity, pension, or yearly rent; a, r, and t as before.

• 260.465625 = 1.157625, and ⁸ 1.157625 = 1.05, or .55. per cent. And

† In all cases of this nature t cannot be found without Logarithms, unless it be a whole number.

 $\frac{1260 \cdot 465625}{225} = 1 \cdot 157625; \frac{1 \cdot 157625}{1 \cdot 05} = 1 \cdot 1025; \frac{1 \cdot 1025}{1 \cdot 05} = 1 \cdot 05; \frac{1 \cdot 05}{1$

.2.232075d. in Ans. £500.

d, will give r.

£225. amount

£200. amount £5. per cent. £450. amount is. £4. per cent. £500. amount $\pounds_{\frac{1}{2}}$, per cent.

find r.

find t.

ions will be a

£260..9..33. at

243..2.025.. a Ans. 4 years. 5547..9..10 Ans. 5 years. 96.2593003125 Ans. 4 years.

y rent; a, r, and !

25. per cent. And thout Logarithms,

CARS.

ABSISTANT.

COMPOUND INTEREST.

A Table of the amount of £1. annuity for years.

Yrs.	3 per Cent.	3½ per Cent.	4 per Cent.	44 per Cent.	5 per Cent.
ľ	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000
2	2.0300000	2.0320000			1 [•] 2·0500000
3	3.0909000	3.106552	3.1510000	3.1370250	3.1525000
4	4-1836270	4.2149429	4.2464640	4.52281811	4.3101250
5	5.3091358	5.3624659	5.4163226	5-1767097	5.5256312
6	6.4684099	6.5501522	6.63297.55	6.7.163916	6.8019128
7	7:6624622	7.7.7.94075	7.8932945	8.0191517	8.1420034
8	8-8923361	9.0516868	9.2142263	9.3000135	9.5491038
9	10.1201065				11.0265642
10	11 4633794	11.7313932	12.0061071	12.5885095	12.5778924
11	12:8077958	13.1419920	13.4863514	13.8111786	14-2067870
12	14.1920297	14:6019617	15.0258055	$15 \cdot 4640316$	15.917126-
13	15.6177906		16.6268377		17.7129827
14	17.0863243		$18 \cdot 2919112$		$19 \cdot 5986318$
15	18:5989140	19.2956810	20.0235376	20.7840540	21.578563
16	20.1568814	20.9710293	21.8245311	22.7193364	23.6574910
17	21.7615878	22.7050158	-23.6975153	24.7417066	25.840366
18	23:4144354		25.6454158	26.8526334	28+1323843
19	2 5·1168685		27.6712293		30.2390037
20	26.8703745	28,2796819	29.7780785	31.3714225	33.0659539
21	28:6764857		31.9692016		25.7 192510
22	30.5367803		$34 \cdot 2479697$		$38 \cdot 505214$:
23	32. 528837		36 .61788835	38.9370297	41.4304749
24	34.4264702		39.0826040		44.5019936
25	36.4592643	$38 \cdot 9493 \cdot 569$	41.6459032	44.5652093	47.727093.
26	38.5530422	41-3131019	44.3117445	47.5706443	51.113453
27	40.7096335		47.0842143		54.669126
. 58	42.9309225		+49.9675829		
. 29	45.2188502		25.9665865	57.4230329	62.322711
: 30	47;5754157	51.6226776	56.0349376	61.0076694	66-438847
31	50.0026782		59:3283351	64.7523875	70.760789.
32	52-5027535		62.7014685		75-298829
33	55.0778412		66-2095272		80.063770
34	57.7301764		69-8579033		85.066958
. 35	60.4620817	66.6740130	73.6522246	$81 \cdot 4966178$	90.320306
36	63.2759441		77.5983135		95.836322
37	66.1742224			01.0413439	101.623138
83				96.1332044	107.709545
39				$-101 \cdot 4644236$	114.095022
40	75.4012593	84.5502779	95.6235153	,107.0303227	120.799773

 $5 = 1.05; \frac{1.05}{1.05} = 1.05$ time sought = 3

Note. The preceding Table is formed thus: the first year's amount is $\pounds 1$, and $1 \times 1.05 + 1 = 2.05$, the second year's amount; $2.05 \times 1.05 + 1 = 3.1525$, the third year's amount, &c.

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COMPOUND INTEREST

Case 1. When u, t, and r are given to find a.

RULE. $\frac{r^{4}-1}{r-1} \times u = a.$

Or, by the Table. Multiply the tabular amount of $\pounds 1$. annuity by the given annuity, and the product will be the amount required.

(17) What will an annuity of £50. per annum amount to in 4 years, at £5. per cent. per annum $?^*$

(18) What will a pension of $\pounds 45$. per annum, payable yearly, amount to in 5 years, at $\pounds 5$. per cent. per annum? Ans. $\pounds 248..13s..3$ 27 grs.

(19) If an annual salary of $\pounds 40$, be forborne 6 years, at $\pounds 4$, per cent. per annum, what is the amount?

Ans. £265..6..4..2.25775616 qrs.

(20) If an annuity of £75:, payable yearly, be omitted to be paid for 10 years, what is the amount at £5. per cent. per annum? $Ans. \pm 943..6..10.0656d.+$

Case 2. When a_i r, and t are given, to find u.

RULE. $\frac{r-1}{r^4-1} \times a = u$.

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(21) What annuity, being forborne 4 years, will amount to $\pounds 215..10..1$, at $\pounds 5.$ per cent. per annum ?

(22) What pension, forborne 5 years, will amount to \pounds 248. 13s. 3·27 grs. at \pounds 5. per cent. per annum? Ans. \pounds 45.

(23) What salary, being omitted to be paid 6 years, will amount to $\pounds 265..6..4..2 \cdot 25775616$ grs. at $\pounds 4$. per cent. per annum? Ans. $\pounds 40$.

(24) If the payment of an annuity, being forborne 10 years, amount to $\pounds 943..6..10.0656d$. at $\pounds 5$. per cent. per annuit, what is the annuity? Ans. $\pounds 75$.

Case 3. When u, a, and r are given, to find t.

* $\frac{1.05^4-1}{.05} \times 50 = (1.21550625-1) \times 1000 = 215.50625 = £215$. 10.13. Ans.

Or, by the Table, thus: 4-310125 × 50° = 5215.50625, as before.

+ $\frac{-05 \times 215 \cdot 50625}{1 \cdot 05^4 - 1}$ = $\frac{-05 \times 215 \cdot 50625}{-215 \cdot 50625}$ = $05 \times 1000 = 250$. And.

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£1. annuity by equired.

im amount to

rum, payable er annum? s..3.27 grs. e 6 years, at

75616 grs. be omitted to per cent. per 0.0656d.+

find u.

will amount to

ount to £248. Ans. £45. 6 years, will per cent. per Ans. £40. orne 10 years, t. per annum, Ans. £75.

find t.

50625 = £219.

125. as before.

1) := £30. And.

COMPOUND INTEREST.

ASSISTANT.

BULE. $\frac{(r-1)a}{u} + 1 = r^t$, which being commuting under of divisions nothing remains, the number of divisions will be equal to t.

(25) In what time will £50, per annum amount to £215.. 10.11. at £5. per cent. per annum, for non-payment?*

(26) In what time will £45, per annum amount to £248. 13s..3·27 grs. allowing £5. per cent. per annum for forbearalice of payment? Ans: 5 years.

(27) In what time will £40. per annum amount to £265. 6..4..2.25775616 ors. at £4. per cent. per annum?

Ans. 6 years.

(23) In what time will £75, per annum amount to £943.. 6.10.0656d. allowing £5. per cent. per annum for forbedrance of payment? Ans. 10 years.

NOTE. The examples relating to the Present Worth of Annuities at Simple Interest are now expunged from this work, because, being entirely useless, except as a mere arithmetical exercise, it is presumed that the judicious teacher will prefer the substitution of other matter of more real utility which is introduced to supply their place. The Theorems are, however; retained in a note, page 148, in order that the ingenious student, who may wish to calculate any example both ways, may have an opportunity of indulging his curiosity, and of comparing the true and the false results. That the principle of computing their value by Simple Interest is erroncous and absurd; will be manifested by the following observations :-

The present worth of an annuity of £150., to continue only 40 years; calculated at £5. per cent. per annum, Simple Interest, (by Theorem 1; Note, page 148,) would be £3950. But this sum, put out at the same rate, will produce £197..10. annual interest (or £47..10. a year more than the proposed annuity) for ever. If computed on the true principle; (by the Theorem, Case 1, page 149,) the present value is £2573..17..3,

The present value of any perpetual annuity (great or small) computed at Simple Interest, is an unlimited or infinite sum; but by using Com-pound Interest, we shall obtain a rational result. For instance, an annuity of £150., to continue for ever, will, (by Case 1, Perpetual Annuities, page 152,) at £5. per cent., be worth £3000. purchase; which, it is evident, is the sum that will yield £150. annual interest.-EDITOR.

* $\frac{0.5 \times 215 \cdot 50625}{50} + 1 = \cdot 001 \times 215 \cdot 50625 + 1 = 1 \cdot 21550625$; which

being continually divided by 1.05, the number of divisions will be 4, the years required. Ans.

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COMPOUND INTEREST.

THE PRESENT WORTH OF ANNUITIES.*

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A Table of the present worth of £1. annuity for years.

Yrs.	3 ner Cent.	34 per Cent.	4 per Cent.	41 per Cent.	5 ner Cent.
1	0.9708738	0.9661336	$\frac{1}{0.9615385}$	0.9569378	0.9523810
2	1.9134697	1.8996943	1.8860947	1.8726677	1.8594105
$\tilde{3}$	2.8286114	2.8016370	2.7750910	2.7489643	2.7232481
4	3.7170984	3 ⋅6730792	3.6298952	3.5875256	3.5459506
5	4.5797072	4.5150524	4.4518223	4.3899766	
-					
6 7	5.4171915	5.3285530	5·2421368	5.1578723	5 0756922
8	6.2302830	$6 \cdot 1145440 \\ 6 \cdot 8739556$	6.0020546 6.7327448	5.8927.008	
89	7.0196922			6.5958859	
9 10	7:7861089 8:5302028	7:6076866 8:3166054	7:4353315 8:1108956	7.2687903 7.9127180	7·1078218 7·7217351
11	9.2526241	9.0015511	8.760.1765	8.5289167	8.3064144
12	9.9540040	9.6633344		9.1135806	
13	10.6349553	10.3027385	9.9856476	9.6328522	
14	11:2960731	10.9205203	16.5631227	10.2228251	
15	11.9379350	11.5174109	$11 \cdot 1183872$	10.7395455	10.3796583
16	12.5611019	12.0941163	11.6522954	11:2340148	10.8377698
17	13.1661183	12.6513206	12.1656686	11.7071912	11 27 40665
18	13.7535129	13.1896817	12.6592967	$12 \cdot 1599916$	11.6895872
19	14.3237989	13.7098374	$13 \cdot 1539391$	$12 \cdot 5932934$	12.0853210
20_	14.8774747	$14 \cdot 2124033$	$13 \cdot 5903260$	13.0079363	12:4622105
21	15.4150240	14.6979742	14.0291596	13.4047237	12.8211529
22	15.9369165	$15 \cdot 167 1248$			13.1630028
23	16.4436083	15.6204104			13.4885741
24	16.9355420	16.0583675	$15 \cdot 2469628$		13.7986420
25	17.4131476	$16 \cdot 4315145$	15.6220796	14.8282088	14.0939448
26	17.8768423	16.8903522	15.9827688	15.1466113	14.3751855
27	18.3270314		16.3295854	15.4513027	14 6430338
$\tilde{28}$	18.7641082	17.6670187	16.6630629	15.7428734	
29	19.1384546	18.0357669	16.9837143		15.1410737
30	19.6004414	18.3920453	17.2920330		15.3724511
31	20.0004286	18.7362757	17.5834933	16.5443903	15.5928106
$\frac{31}{32}$	20.0004236 20.3887656	13.7362757 19.0688654	17.5834953 17.8735512	16.5443903	15.8026768
33	20.3857030 20.7657919	19.00000004	17.8755512 18.1476454		
34	20 7057919 21 ·1318368	19.5902031	$13 \cdot 147 \cdot 0454 \\ 18 \cdot 41 \cdot 1197 \cdot 5$	17.0228019	16.1929041
35	$21^{13}100000000000000000000000000000000000$	20.0006611	$18^{6}6646130$	$17 \cdot 2407 \cdot 57.0$ $17 \cdot 4610122$	
	21.3322526	20.2904933	18.9032817	17.6660404	16.5468518
3.	22.1672355	20.5705254	19.1425785	17.8622396	
. I	22.4924617		19.3678639	18.0499900	
-	22·8082153	21·1024998	19.5844345	18.2296555	
10	93·11477 21	21.3550723	19.7927735	18.4015842	$17 \cdot 1590865$

* Present Worth of Annuities at Simple Interest.

Theor. I. $\frac{r(t-1)+2}{2tr+2} \times tu = p$. If $\frac{tr+1}{(r.(t-1)+2).t} \times 2p = t$.

TIES.*

or years.

t. 5 per Cent. 8 0.9523810 7 1.85941053 2.72324816 3.5459506 i6 4·3294768 23 5 0756922 $08 5 \cdot 78637.35$ 59 6.4632129 03 7.1078218 80 7.7217351 67 8.3064144 06 8.8632518 .2.2 $9 \cdot 3935732$ 51 9.8986412 155 10.3796583 148 10.3377698 $912\,11 \cdot 27\,40665$ 016 11.6895872 934 12.0853210 363 12.4622105 237 12 8211529 246 13.1630028 747 13.4885741 782 13.7986420 038 14.0939448 113 14.3751855 027 14:6430338 734 14.8981274 884 15.1410737 884 15.3724511 903 15.5928106 907 15.8026768 619 16 00 25493 578 16.1929041 122 16.37 41944 404 16.5468518 396 16.7112874 900]16.8678928555 17.0170408

Interest.

$$\frac{1}{1+2} \times 2p = 1$$

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Note. The above table is thus formed: $\pounds 1 \div 1.05 = .9523810$, the present worth of the first year; this $\div 1.05 = .9070295$, which, added to the first year's present worth, gives 1.8594105, the present worth of 2 years; then $.9070295 \div 1.05$, and the quotient added to 1.8594105 = 2.7232481, the present worth of 3 years, &c.

(lase 1. When u, t, and r are given, to find p, the present worth.

RULE.
$$(u - \frac{u}{r^{t}}) \div (r - 1) = p$$
.

Qr, h. the '- ble. Multiply the tabular present worth for the time given the en annuity, and the product will be the present worth required.

(29) What is the present worth of an annuity of \pounds 30., to continue 7 years, at \pounds 5. per cent. per annum ?*

(30) What is the present worth of a pension of $\pounds 40$. per annum, to continue 8 years, at $\pounds 5$. per cent. per annum?

(31) What is the present worth of an annual salary of $\pounds 35$,

to continue 7 years, at £4. per cent. per annum? Ans. £210..1..5.04d.

(32) What is the yearly rent of $\pounds 50.$, to continue 5 years, worth in ready money, at $\pounds 5.$ per cent. per annum?

Ans. £216..9..5..2.08 grs.

Case 2. When p, t, and r are given, to find u.

RULE.
$$\frac{pr^{t}(r-1)}{r^{t}-1}=u.$$

(33) If an annuity be purchased for £173..11..10.08d., to

III.
$$\frac{(tu-p) \times 2}{(2p-(t-1)u).t} = r.$$

IV. Put $\frac{1}{r} - (\frac{p}{u} + \frac{1}{2}) = m;$ then $\sqrt{(\frac{2p}{ru} + m^2)} - m = t.$

For Annuities in Reversion, it is only necessary to observe the Rules for Reversionary Annuities at Compound Interest, and to calculate (according to the directions therein given) by the Theorems for Simple Interest.

* $30 - \frac{30}{1 \cdot 05^7} = 30 - \frac{30}{1 \cdot 4071} = 30 - 21 \cdot 3204 = 8 \cdot 6796$ and $8 \cdot 6796$

 $\div 05 = \pounds 173.592 = \pounds 173..11..10.08d$. Ans.

Qr, by the Table, 5.7863735 \times 30 = £173.591205. Ane.

COMPOUND INTEREST.

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be continued 7 years, at $\pounds 5$. per cent. per annum, what is the annuity ?*

(34) If $\pm 258..10..6..3264$ qrs. be paid down for a salary 8 years to come, at £5. per cent. per annum, what is the salary? Ans £40.

(35) If the present payment of $\pounds 210..1..5$ 04*d*. be required for a pension for 7 years to come, at $\pounds 4$. per cent. per annum, what is the pension? Ans. $\pounds 35$.

(36) If the present worth of an annuity, 5 years to come, be $\pounds 216..9..5..2.08$ qrs. at $\pounds 5.$ per cent. per annum, what is the annuity? Ans. $\pounds 50.$

Case 3. When u, p, and r are given, to find t.

RULE. $\frac{u}{p+u-pr} = r$, which being continually divided by r till nothing remains, the number of divisions will be equal to t.

(37) How long may a lease of £30. yearly rent be had for £173..11..10.08*d*., allowing £5. per cent. per annum to the purchaser ?†

(38) If £258..10..6..3 264 qrs. is paid down for a lease of £40. per an r im, at £5. per cent. per annum, how long is the lease purch rd for? Ans. 8 years.

(39) If a house is let upon lease for £35. per annum, and the lessor disposes of the lease for £210..1..5.04*d*., allowing after the rate of £4. per cent. per annum, what term of the lease remains unexpired? Ans. 7 years.

(40) For what time is a lease of £50. per annum purchased, when present payment is made of £216..9..5..2:08 qrs., at £5. per cent. per annum? Ans. 5 years.

ANNUITIES, ETC., IN REVERSION.

To find the present worth of annuities in reversion.

RULE 1. Find the present worth of the annuity, for the time of ite continuance, as if it were to commence immediately, by Case 1. page 149. Then find what principal will amount to that sum in the given

[•] $173 \cdot 592 \times 1 \cdot 4071 \times \cdot 05 \div \cdot 4071 = 12 \cdot 213 \div \cdot 4071 = £30$. Ans. Or, by the Table, $173 \cdot 592 \div 5 \cdot 7863735 = £30$. Ans.

 $^{173 \}cdot 592 + 30 - (173 \cdot 592 \times 1 \cdot 05) = 203 \cdot 592 - 132 \cdot 2716 = 21 \cdot 3204;$ and $30 - 21 \cdot 3204 = 1 \cdot 4071$; which being continually divided by 1 \cdot 05, the number of divisions will be 7: therefore t = 7 years. Ans. Or, by the Table, $173 \cdot 592 \div 30 = 5 \cdot 7864$; and referring to the column of 5 per pert, we find the number $5 \cdot 7863735$ against 7 years.

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m, what is the

h for a salary b, what is the Ans £40. d. be required ht. per annum, Ans. £35. Tears to come, num, what is Ans. £50.

find t.

livided by r till ber of divisions

ent be had for annum to the

for a lease of bw long is the ns. 8 years. er annum, and 04d., allowing it term of the ns. 7 years, num purchas-1.5..2:08 qrs., ns. 5 years.

version.

the time of ite y Case 1, page in in the given

=£30. Ans.

716=21.3204; ivided by 1.05, . Ans. Or, by column of 5 per COMPOUND INTEREST.

time before the annuity commences, (by Case 2, Compound Interest, page 143,) which will be the present worth.

RULE 2. Find the present worth of a similar annuity supposed to commence immediately, and continue during the whole period; and also the present worth of the same till the time when the reversionary annuity actually commences, and the difference of these two will be the present value required.

Note When calculating by the Table, this is the most eligible method.

RULE 3. Find the amount of the anunity at the time of its cessation. (by Case 1, page 146,) and the present worth of that amount (being found by Case 2, Compound Interest, page 143) will be the value required.

(41) What is the present worth of a reversion of a lease of \pounds 40. per annum, to continue for 6 years, but not to commence till the end of 2 years, allowing £5. per cent. per annum to the purchaser?*

(42) What is the present worth of a reversion of a lease o. £60. per annum, to continue 7 years, but not to commence till the end of 3 years, allowing £5. per cent. per annum to the purchaser? Ans. £299..18..216d.

(43) A house is let at \pounds 30. per annum on a lease, of which 4 years are yet unexpired, and which the lessee is desirous of renewing at the same rental, to continue 7 years beyond the term of the present lease. What will the lessor expect as a bonus for such a renewal of the lease, considering the house to be worth double the present rent, and allowing interest for the money now advanced at \pounds 5. per cent. per annum?

Ar.s. £142..16..3..1.152 grs.

To find the annuity in reversion which a given sum will purchase.

RULE. Find the amount of the given sum for the time before the annuity commences, by Case 1, Compound Interest, page 143, which will be the value of the annuity at its commencement.

Call this value p, and then find the annuity as in Case 2, page 149.

(44) What annuity, to be entered upon 2 years hence, and

• $40 - \frac{40}{1.05^6} = 40 - \frac{40}{1.3400956} = 40 - 29.84361 = 10.15139$; and 10.15139 $\div .05 = 203.0278$; then $203.0278 \div 1.05^2 = \pounds 184.1522 = \ddagger$ £184..3..0..2.112 grs. Ans. then to continue 6 years, may be purchased for £184..3..0.. 2.112 grs. at £5. per cent. per annum?*

(45) The present worth of a lease, taken in reversion for 7 years, but not to commence till the end of three years, is $\pounds 299..18..2\cdot 16d.$, allowing $\pounds 5.$ per cent. per annum to the purchaser: what is the yearly rent? Ans. $\pounds 60.$

(46) There is a lease that has yet 4 years to run, and the lessee has purchased the reversion of a renewed lease, at the same rental of £30, per annum, for the term of 7 years, commencing at the expiration of the present lease, for which he has paid down £142.16.3.1152 qrs. What increase of rent is reckoned on the property according to this contract, allowing £5, per cent. per annum for present payment? Ans. £30.

PERPETUAL ANNUITIES, OR FREEHOLD ESTATES

Case 1. When u and r are given, to find p, the present worth, or purchase money.

RULE.
$$\frac{u}{r-1} = p.\dagger$$

(47) What is the worth of a freehold estate of £50. yearly rent, allowing £5. per cent. per annum to the buyer ? \ddagger

(48) What is a real estate of \pounds 140. per annum worth in present money, allowing \pounds 4. per cent. per annum to the purchaser? Ans. \pounds 3500.

(49) What must the purchaser give for a freehold estate of $\pounds 437..10$. yearly rent, so as to make $\pounds 3\frac{1}{2}$. per cent. per annum by the investment of his capital? Ans. $\pounds 12500$.

Case 2. When p and r are given, to find u.

RULE. $p \times \overline{r-1} = u$.

(50) If a freehold estate is bought for $\pounds 1000.$, what must

* $184 \cdot 1522 \times 1 \cdot 1025 = 203 \cdot 0278$; then $203 \cdot 0278 \times 1 \cdot 3400956 \times \cdot 05$	•
$\frac{3400956}{203\cdot0278\times1+(203\cdot0278\times3400956)}\times 05 = \frac{203\cdot0278}{3400956}$	
$3400956 + 203.0278 \times .05 = 800.0005 \times .05 = £40. Ans.$	

Or, by the Table, $184 \cdot 1522 \div (6 \cdot 4632129 - 1 \cdot 3594105) = 184 \cdot 1522 \div 4 \cdot 6038024 = \pounds 40$. Ans.

t This rule is deduced from the *formula* in page 149; for, in Annuities continuing for ever, t is *infinite*, and the subtractive quantity r = r = o; therefore the theorem assumes the above form. $t = 50 - .05 = \pounds 1000$. Ans.

152

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£184..3..0..

reversion for ree years, is nnum to the Ans. £60. Tun, and the lease, at the years, comfor which he prease of rent ntract, allow-? Ans. £30.

TATES

present worth,

f £50. yearly ayer ?‡ aum worth in im to the purns. £3500. hold estate of cent. per ans. £12500.

ıd **u**.

0., what must

203.0278

 $) = 184 \cdot 1522 \div$

; for, in Annai ive quantity w n. ASSISTANT.]

COMPOUND INTEREST.

be the yearly rent, to pay the purchaser £5. per cent. per annum interest for his money ?*

(51) If an estate be sold for \pounds 3500, what is the yearly rent allowing to the purchaser \pounds 4. per cent. per annum? Ans. \pounds 140.

(52) If a freehold estate is bought for £12500., and will yield the purchaser $\pounds 3\frac{1}{2}$. per cent. per annum, what is the yearly rent? Ans. £437..10.

Case 3. When p and u are given, to find r.

RULE. $\frac{u}{n} + 1 = r$.

(53) If an estate of £50. per annum is bought for £1000., what is the rate per cent. per annum $?^{\dagger}$

(54) If a freehold estate of $\pounds 140$. per annum is sold for $\pounds 3500$, what interest will it pay to the purchaser?

Ans. £4. per cent.

(55) If an estate in perpetuity of $\pounds 437..10$. per annum is sold for $\pounds 12500$, what interest will it pay to the purchaser $\frac{1}{2}$ Ans. $\pounds 3\frac{1}{2}$. per cent.

FREEHOLD ESTATES IN REVERSION.

To find the present worth of a freehold estate in reversion.

RULE. Find the value of the estate, supposing it were to come into (mmediate possession, as in Case 1, page 152. Then suppose that value (p) to be a, and find what principal will amount to a in the time to come, previous to possession, by Case 2, Compound Interest, page 143. Such principal will be the present value.

(56) What must be paid down for the purchase of a freehold of £50. per annum, to be entered upon 4 years hence, allowing the purchaser at the rate of £5. per cent. per annum for his purchase money ?‡

(57) What must be paid down for the reversion of a real estate of $\pounds 200$. per annum, so as to pay the purchaser $\pounds 4$. per cent. per annum for his capital, supposing 2 years to elapse before the estate comes into possession?

Ans. £4622..15..7..1.76 qrs.

• $1000 \times \cdot 05 = \pounds 50$. Ans.

 $+\frac{50}{1000}+1=1.05=$ £5. per cent. Ans.

 $\pm 50 \div .05 = 1000$; then $1000 \div 1.2155 = \pounds 822.7067 = \pounds 822..14..1.$ 9.432 grs. Ans

G 2

COMPCUND INTEREST.

(58) A freehold, producing £280. annual rent, is to be disposed of, with a reserve of the next 3 years' rent to the present proprietor. What is it worth in ready money, allowing £31. per cent. per annum to the purchaser?

Ans. £7215..10..9..3.36 qrs.

TUTOR &

To find the yearly rent of an estate in reversion, having its present value given.

RULE. Find the amount of the given present value in the *time before* possession: thus, pr = a. Then consider that amount to be the present value (p) of the perpetual annuity, and find the annuity thus: $p \times (r-1) = u$.

(59) What must be the rent of a freehold property, to come into possession 4 years hence, for which £822..14..1..2.432 grs. is paid down, allowing the purchaser £5. per cent. per annum ?*

(60) A freehold estate is sold for $\pounds 4622..15..7..1$ 76 grs., the vender reserving to himself the first two years' rent. Reguired the annual value to pay the purchaser $\pounds 4$. per cent. per annum for his capital. Ans. $\pounds 200$.

(61) A freehold estate has been purchased for £7215..10.. 9..3 36 qrs., the possession of which is not to be given up till after the expiration of 3 years. What must be the annual rent to pay the purchaser at the rate of $\pm 3\frac{1}{3}$. per cent. per annum?

DISCOUNT, ON THE PRINCIPLES OF COMPOUND INTEREST.

Norr. The following Table is constructed by the continual division of 1 by the ratio (r): thus $1 \div 1.05 \pm .9523810$, the first year's present worth; then $.9523810 \div 1.05 \pm .9070295$, the second year's present worth; and $.9070295 \div 1.05 \pm .8638376$, the third, &c.

* $822.70625 \times 1.2155 = 1000$; then $1000 \times .05 = \pounds 50$. Ans.

t This is merely a repetition of the various cases in Compound Inscreest. For instance, to find the present worth of any debt due some time hence, is precisely the same operation as finding what principal will amount to that sum in the given time; and this observation will equally apply to the identity of the other cases. The entire omission, therefore, of *Discount*, (at *Compound Interest*,) arranged under that specific head, would be no detriment to the learner. It is, however, retained here, for the sake of those who may think some repetition of the subject desirable.—EDITOR.

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COMPOUND INTEREST.

[TUTOR .

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1.1.76 grs., rent. Reper cent. s. ± 200 . $\pm 7215..10$.. given up till the annual er cent. per s. ± 280 .

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Ans.

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Yr.	3 per Cent.	31 ner Cent	A ner Cent	45 per Cent.	5 ner Cout
1	·9708738	·9661836	·9615385	·9569378	·9523810
2	•9425959	·9335107	·9245562	·9157299	-9070295
ŝ	•9151417	·9019427	•8839963	•8762966	*8633376
4	•8884870	·8714422	*8548042	·8335613	.8227025
5	•8626088	•8419732	•8219271	*8024510	.7835262
6	·8374843	·8135006	•7903145	•7678957	7462154
7	·8130915	·7859910	·7599173	•7348235	.7106813
8	•7894092	•7594116	·7306902	· 7 031851	·6763394
9	•7664167	·7337310	·7025867	·6729044	·6446089
10	•7 440939	•7039183	·67 55641	•6439277	·6139133
11	•7224213	·6849457	·6495809	·6161987	·5846793
12	·7013799	·6617833	·6245970	·5896639	·5568374
13	·6809513	·6394041	·6005741	•564?~16	·5303214
14	·6611178	·6177818	·5774751	•53(° ¹ 729	·5050680
15	•6418619	·5968906	·5552645	-5317204	·4810171
16	•6231669	•5767059	:5339032	•4ə44693	•4581115
17	·6050164	•3572038	• 5133 ⊺30	•4731764	+1362967
18	·5873946	·5383611	·4936.281	·4528004	·4155207
19	•5702860	•5201557	•4746424	•4333018	·3957340
20	•5536758	•5025659	•4563869	·4146429	·3763895
21	•5375493	·4855709	·4388336	$\cdot 3967874$	·3589424
22	•5218925	·4691506	•4219554	·3797009	· 3 418499
23	•5066918	•4532856	•4057263	•3633501	-3255713
24	•4919337	•4379571	•3901215	•3477035	•3100679
25	•4776056	•4231470	·3751168	·3327306	·2953028
26	•4636947	4088377	·3606892	·3184025	·2812407
27	·4501891	:3950122	·3468166	•3046914	2678483
28 29	·4370768 ·4243464	·3316543 ·3627482	+3334775 +3206514	+2915707 +2790150	-2550936 -2429463
29 30	·4243464 ·4119868	·308 · 482	·3033187	·2670000	2313774
31	-3999872	·3442304	2964603	2555024	2203595
32	·3883370	3325897	·2850579	2444999	·2098562
33	·3770263	3213427	·2740942	2339712	·1998725
34	·3660449	·3104761	$\cdot 2635521$	-2238959	·1903548
35	• 3553 834	•2999769	2534155	$\cdot 2142544$	$\cdot 1812903$
36	·3450324	·2898327	·2436687	·2050282	·1726574
37	·3349829	·2800316	$\cdot 2342968$	·1961992	$\cdot 1644356$
38	·3252262	·2705619	$\cdot 2252854$	·1877504	$\cdot 1566054$
39	·3157536	·2614125	$\cdot 2166206$	1796455	·1491480
40	·3065568	·2525725	2082890	17 19 27	$\cdot 1420457$

A Table of the present worth of L1. due any number of years hence from 1 to 40.

Case 1. To find the present worth of any sum due after a cer tain period.

RULE. The same as in Case 2, Compound Interest, considering a method the debt whose present value is required.

(1) If $\pounds 344...14...9...1.92$ qrs. be payable in 7 years' time, that is the present worth, discount being made at $\pounds 5$. per ont. per annum?*

(2) A debt of £409..9 00992s., payable 4 years hence, is agreed to be paid in present money: what sum must the creditor receive, discounting at £4. per cent. per annum?

Ans. £350.

Case 2. To find the debt whose present worth is given.

RULE. See Case 1, Compound Interest.

(3) If $\pounds 245$, be received for a debt payable 7 years hence, allowing $\pounds 5$, per cent, per annum to the debtor for present payment, what is the debt?

(4) There is a sum of money due at the expiration of 4 years, but the creditor agrees to take £350 in ready money, allowing £4. per cent. per annum discount. What was the debt? Ans. £409..900992s.

Case 3. When the rest are given, to find the time.

RULE. See Case 4, Compound Interest.

(5) A person receives £245. now for a debt of £344.14.9. 1.92 qrs., discounting at £5. per cent. per annum: in what time was the debt payable ?[‡]

(6) There is a debt of $\pounds 409..9 \cdot 00992s$. due a certain time hence, but $\pounds 4$. per cent. per annum being allowed to the debtor for the present payment of $\pounds 350.$, it is required to find in what time the sum was to be paid. Ans. 4 years.

Case 4. When the rest are given, to find the rate per cent. RULE. As in Case 3, Compound Interest.

(7) The present worth of $\pounds 344..14..9..192$ qrs., payable

in

 $344.7395 \div 245 = 1.4071$; the continual divisions of which by 1.05, will be 7 = the number of years. Ans.

156

A

TUTOR'S.

^{*} $344.7395 \div 1.4071 = \pounds 245$. Ans.

Or, by the Table, '7106813 × 344'7395 = £245. Ans.

 $^{+ 245 \}times 1.4071 = \pounds 344.7395 = \pounds 344..14..9..1.92$ qrs. Ans.

TUTOR'S.

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Ans. which by 1.05, A\$\$ISTANT.]

DUODECIMALS.

7 years hence, is $\pounds 245$, at what rate per cent. per annum is discount allowed ?*

(8) There is a debt of $\pounds 409..9\ 00992s$. payable in 4 years, but it is agreed to take $\pounds 350$. present payment. Required the rate of discount. Ans. $\pounds 4$. per cent.

EQUATION OF PAYMENTS AT COMPOUND INTEREST.

RULE 1. Find the present worth of each payment respectively; and add them together for the *whole present worth*: then the time in which that present worth will amount to the sum of the debts will be the *true* equated time required.

2. Find the amount of each debt from the time of its becoming due till the time of the last payment, and add the respective amounts and the last payment into one sum. Then find *the time* in which the sum of the debts would amount to that sum of the amounts: subtract *this* from the time of the last payment, and the difference will be the *true*equated time.

(1) Required the true equated time for the payment of a debt of $\pounds 400$. of which $\pounds 320$. is now due, and the rest at the end of 5 years; reckoning compound interest at the rate of $\pounds 5$. per cent per annum. Ans. 90714 years.

(2) If $\pounds 100$, will become due one year hence, and $\pounds 104$. three years hence, what is the true equated time for payment of the whole, allowing compound interest at $\pounds 4$. per cent. per annum?

(3) If a person will have to receive £200. at the end of 3 years, and £80. more at the end of 5 years, in what time ought he to receive the whole at one payment, allowing £5 per cent. per annum, compound interest?

Ans. 3.5518 years.

DUODECIMALS

Are so named from the integer of each denomination containing twelve of the next inferior. They are in general use among artificers for computing the quantities of their materials and labour, both in Superficial and Solid Measure.[†]

* $344.7395 \div 245 = 1.4071$; and $\sqrt[7]{1.4071} = 1.05$; which gives £5. per cent. Ans.

[†] † For a clear and intelligible explanation of the different Measures see the Tables, page 24, &c.

12 inches (') make 1 foot.

12 seconds (") 1 inch, or prime.

12 thirds ("") 1 second, &c.

To multiply duodecimally.

RULE 1 Under the multiplicand write the corresponding terms of the multiplier.

2. Multiply by the feet in the multiplier, observing to carry one for every twelve, from each lower denomination to the next superior.

3. In the same manner multiply by the inches in the multiplier, setting the result from each term one place farther to the right.

4. Proceed in like manner with the remaining denominations, and the sum of the products will be the total product.

Norr 1. Length and breadth multiplied together produce the area of a superficies; and this multiplied by the thickness, produces the solid content of a body.

2. It is generally more eligible to take aliquot parts out of the multi plicand for the inches, &c., in the multiplier.

-		ft	. ,		,	ft	. ,	,,		ft.	ļ	ų,		11
(1)	Mult.	7			by	3	6	•		.				•
(2)	Mult,	8	5		by		7		A	28. 38	6	11		
(3)	Mult.		8		by	7	6		а.	72	6	0		
(4)	Mult.	9 8 7	1		by	3	5		a.	27	7	5		•
(5)	Mult.	7	6		by	5	9		а.	43	1	5 6		
(6)	Mult.	4	7		by	3	10		а.	17	6	1Ŏ		
(7)	Mult.	7	5	9	by		5	3	а.	25	8	6	2	3.
(8)	Mult.	10	4	5	by	7	8	6	а.	79	11	Q	6	6.
(9)	Mult.	75	7		by	9	8		a.	730	7	8		
(Ì0)	Mult.	97	8		by	8	9		ą.	854	7	0		
(11)	Mult.	57	9		by	9	5		<i>a</i> .	543	9	9		
(12)	Mult.	75	9		by	17	7		а.	1331	11	3		
(13)	Mult.	87	5		by	35	8		а.	3117	10	- 4		
(14)	Mult.	179	3		by	38	10		a.	6960	10	6		
(15)	Mult.	259	2		by	48	11		α.	12677	6	10		
(16)	Mult.	257	9		by	39	11		<i>a</i> .	10288	6	3		
(17)	Mult.	311	4	7	by	36	7	5	<i>a</i> .	11402	2	4	11	11.
(18)	Mult.	321	7	3	by	9	3	6	<i>a</i> .	2988	2	10	4	6
ft.	i14-		in	. (Other	wise		P	roof	by Decin	als.			
* 7	9 6		6	Ŧ	17	9				•75				
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DUODECIMALS.

Glazing, Masons' flat work, and some parts of Joiners' work, are computed at so much per square foot.

Painters', Plasterers', Pavers', and some descriptions of Joiners' work, are estimated by the square yard.

Roofs, Floors, Partitions, &c., by the square of 100 feet. Bricklayers' work by the square rod, containing 2721 feet

(19) A certain house has 3 tiers of windows, 3 in a tier the height of the first tier being 7 feet 10 inches, the second 6 feet 8 inches, and the third 5 feet 4 inches, and the breadth of each window is 3 feet 11 inches. What will the glazing cost at 14d. per square foot ?*

(20) What is the price of 8 squares of glass, each measuring 4 feet 10 inches long, and 2 feet 11 inches broad, at $4\frac{1}{4}d$. per square foot? Ans. £1..18..9.

(21) What is the value of 8 squares, each measuring 3 feet by 1 foot 6 inches, at $7\frac{3}{4}d$. per square foot ? Ans. £1..3..3.

(22) What is the price of a marble slab 5 feet 7 inches long and 1 foot 10 inches broad, at 6s. per square foot?

Ans. £3..1..5.

(23) What will be the expense of ceiling a room the length of which is 74 feet 9 inches, and the width 11 feet 6 inches, at 3s. $10\frac{1}{2}d$. per square yard? Ans. £18..10..1.

(24) What will the paving of a court-yard cost at $4\frac{2}{4}d$. per square yard, the length being 58 feet 6 inches, and the breadth 54 feet 9 inches? Ans. £7..0.10.

(25) The circuit of a room is 97 feet 8 inches, and the height 9 feet 10 inches: what is the charge for painting it, at 2s. $8\frac{3}{4}d$. per square yard? Ans. £14..11..2.

(26) What is the expense of a piece of wainscot 8 feet 3 inches long and 6 feet 6 inches broad, at 6s. $7\frac{1}{2}d$. per square yard? Ans. £1..19..5.

ft. in. * 7 10	$in. ft. in. 6 = \frac{1}{2}$ 19 10
* 7 10 6 8 5 4	0 = 3 19 10 11
	in. 218 2
19 10 the whole height. 3 11	$3 = \frac{1}{3}$ 9 11 4 11 6"
3	$1 = \frac{1}{20} \frac{1}{233} \frac{1}{0} \frac{1}{6} \text{ at } 14d.$
11 9 the whole breadth.	$d.$ $2 = \frac{1}{6} \pounds 11 \ 13 \ 0 \ \text{the value at 1a.}$
	1 18 10 the value at 2d.
valu	$1e \text{ of } 6'' = 0 0 0 \frac{1}{2}$
	£13 11 101 Ans.

(27) What will the paving of a court-yard cost at 3s. 2d. per square yard, the length being 27 feet 10 inches, and the breadth 14 feet 9 inches? Ans. £7..4..5.

(28) A certain court-yard is 42 feet 9 inches in front, and 68 feet 6 inches long; a causeway the whole length, and 5 feet 6 inches broad, is laid with Purbeck stone, at 3s. 6d. per square yard, and the rest is paved with pebbles, at 3s. per square yard. What is the expense? Ans. £49..17..0 $\frac{1}{2}$.

(29) What will the plastering of a ceiling cost at 10*d*. per square yard, supposing the length 21 feet 8 inches, and the breadth 14 feet 10 inches? Ans. $\pounds 1..9..9$.

(30) What will the wainscoting of a room cost at 6s. per square yard, supposing the height of the room (including the cornice and moulding) is 12 feet 6 inches, and the compass 83 feet 8 inches; the three window shutters each 7 feet 8 inches by 3 feet 6 inches, and the door 7 feet by 3 feet 6 inches? The shutters and door being worked on both sides, are reckoned work and half-work. Ans. £36..12..2 $\frac{1}{2}$.

(31) In a piece of partitioning 173 feet 10 inches long, and 10 feet 7 inches in height, how many squares?

Ans. 18 squares, 39 feet, 8' 10".

(32) A house of three stories, besides the ground floor, measuring 20 feet 8 inches by 16 feet 9 inches, is to be floored at $\pounds 6..10$. per square: there are 7 fire-places, two of which measure 6 feet by 4 feet 6 inches each, two others 6 feet by 5 feet 4 inches each, two others 5 feet 8 inches by 4 feet 8 inches each, and the seventh 5 feet 2 inches by 4 feet, and the well-hole for the stairs is 10 feet 6 inches by 8 feet 9 inches. What will the whole amount to ?

Ans. £53..13..34.

[TUTOR'S

(33) If a house measures within the walls 52 feet 8 inches in length, and 30 feet 6 inches in breadth, the root being of a true pitch, what will it cost roofing at 10s. 6d. per square ? Ans. £12..12..113.

Note. A roof is said to be of a true pitch when the rafters are $\frac{1}{2}$ of the breadth of the building. In this case, therefore, the breadth must be accounted equal to the breadth and half-breadth of the building.

(34) What will the tiling of a barn cost at 25s. 6d. per square, the length being 43 feet 10 inches, and the breadth 27 feet 5 inches on the flat, the eave-boards projecting 16 inches on each side? Ans. $\pounds 24...9...5\frac{3}{4}$.

Note. Bricklayers compute their work at the says of a brick and

ASSISTANT.]

st at 3s. 2d. hes, and the £7..4..5.

in front, and ngth, and 5 it 3s. 6d. per s, at 3s. per $49..17..0\frac{1}{2}$. t at 10d. per

hes, and the $\pounds 1..9..9$.

st at 6s. per ncluding the compass 83 feet 8 inches et 6 inches? es, are reck-36..12..2¹/₂. hes long, and

eet, 8' 10". ground floor, to be floored wo of which ers 6 feet by s by 4 feet 8 y 4 feet, and s by 8 feet 9

53..13..3<u>1</u>. feet 8 inches on being of a er square ? 2..12..11<u>3</u>.

rafters are $\frac{2}{3}$ of e breadth must he building.

25s. 6d. per 1 the breadth projecting 16 $\pounds 24..9..5\frac{3}{4}$.

of a brick and

a half thick; therefore, if the thickness of a wall is more or less, it inust be reduced to the standard thickness by multiplying the area of the wall by the number of half bricks in the thickness, and dividing the product by 3.

*(35) If the area of a wall is 4085 feet, and the thickness two bricks and a half, how many rods does it contain of the standard thickness? Ans. 25 rods, 8 feet.

(36) If a gar in wall is 254 feet in compass, 12 feet 7 inches high, and 3 bricks thick, how many rods does it contain? Ans. 23 rods, 136 feet.

(37) How many rods are there in a wall $62\frac{1}{2}$ feet long, 14 feet 8 inches high, and $2\frac{1}{2}$ bricks thick ?

Ans. 5 rods, 167 feet.

(38) The end wall of a house is 28 feet 10 inches in length; the height of the roof from the ground is 55 feet 8 inches; and the gable (or triangular part at the top) rises 42 courses of bricks, reckoning 4 courses to a foot. The wall to the height of 20 feet is $2\frac{1}{2}$ bricks thick, 20 feet more, 2 bricks thick, and the remaining part a brick and a half thick; and the gable is 1 brick thick. What is the charge for the whole wall, at £5..16. per rod? Ans. £48..13..5 $\frac{1}{2}$.

To multiply several figures by several, and obtain the product in one line only.

RULE. Multiply the units of the multiplicand by the units of the multiplier, set down the units of the product, and carry the tens; next multiply the tens in the multiplicand by the units of the multiplier, to which add the product of the units of the multiplicand multiplied by the tens in the multiplicand by the tens carried; then multiply the hundreds in the multiplicand by the units of the multiplier, adding the product of the tens in the multiplicand multiplied by the tens in the multiplier, and the units of the multiplied by the tens in the multiplier, and the units of the multiplied by the tens in the multiplier, and so proceed till you have multiplied the multiplicand all through, by every figure in the multiplier.

> Multiply . 35234 by . 52424 Product 1847107216

EXPLANATION. .

First, $4 \times 4 = 16$, that is 6 and carry 1. Secondly, $(3 \times 4) + (4 \times 2)$ and 1 that is carried = 21, set down 1 and carry 2. Thirdly, $(2 \times 4) + (3 \times 2) + (4 \times 4) + 2$ carried = 32; that is, 2 and carry 3. Fourthly, $(5 \times 4) + (2 \times 2) + (3 \times 4) + (4 \times 2) + 3$ carried = 47; set down 7 nd carry 4. Fifthly, $(3 \times 4) + (5 \times 2) + (2 \times 4) + (3 \times 2) + (4 \times 5) + 4$ carried = 60; set down 0 and carry 6. Sixthly, $(3 \times 2) + (5 \times 4) + (2 \times 2) + (3 \times 5) + 6$ carried = 51; set down 1 and carry 5. Sev

" In this and the three following examples the rod is considered = 272 feet.

enthly, $(3 \times 4) + (5 \times 2) + (2 \times 5) + 5$ carried = 37; set down 7 and carry 3. Eighthly, $(3 \times 2) + (5 \times 5) + 3$ carried = 34; set down 4 and carry 3. Lastly, $3 \times 5 + 3$ carried = 18; set down 18, and the work is finished.

MENSURATION OF SUPERFICIES.

GEOMETRICAL DEFINITIONS.

GEOMETRY is the science which investigates the nature and properties of lines, angles, surfaces, and solid bodies.

A point has no parts or magnitude.

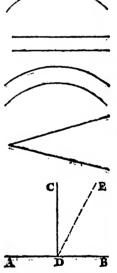
A line has length only, without breadth or thickness.

A line drawn wholly in the same direction, or the shortest distance between two points, is a *right* or *straight line*. That which continually changes its direction is a curve.

Parallel lines preserve the same distance from each other throughout; and therefore would never meet, though infinitely produced.

An angle is the degree of inclination of two lines, or the opening between them when they meet in a point; which is called the angular point.

When a line meeting nother inclines not either way, but makes equal angles on each side, those are called right angles; and the lines are perpendicular to each other. Thus the angle ADC == the angle BDC.*



An oblique angle is either acute or obtuse. An acute angle is less than a right angle, as BDE; and an obtuse angle, greater than a right angle, as ADE.

"When more than two lines meet, forming several angles at the same point, it is necessary to designate each angle by three letters, placing that which is at the angular point in the middle. Thus, the angle BDC is that formed by the lines BD and CD.

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ASSISTANT.] MENSURATION OF SUPERFICIES.

A superficies or surface is a space contained within ines and has two dimensions, length and breadth.

A solid is a space or body bounded by surfaces, and has three dimensions, length, breadth, and thickness.

A triangle is a superficies bounded by three lines. A quadrangle, or quadrilateral, is bounded by four lines.

A right-angled triangle has one right angle, (Fig. page 116,) an obtuse-angled triangle has one obtuse angle, and an acuteangled triangle has all its angles acute.

An equilateral triangle has the three sides (and consequently the three angles) all equal to each other.

An isosceles triangle has two equal sides.

A scalene triangle has all the three sides unequal.

A parallelogram is a quadrangle having the opposite sides equal and parallel.^a When the angles are right ones, it is called a *rectangle*.^b And a rectangle having all its sides equal is a square.^e

A rhombus has all its sides equal, but oblique angles.⁴

A rhomboid has oblique angles, and only its opposite sides equal.

All other quadrilaterals are *trapeziums*; but a trapezium that has two sides parallel is called a *trapezoid*.

The base^f of a figure is the side on which it is supposed to stand; and a line drawn from the vertex, or opposite angle, perpendicular to the base, is the *altitude*,^f or perpendicular height.

Right-lined plane figures of more than four sides are called *polygons*. A 1 lygon of five sides (or angles) is a *pentagon*, one of six a *hex..gon*, &c. Vide Table, page 166.

A circle^g is a plane figure, contained under one curve line, called the circumference, which is in every part equidistant from the centre, or middle point within it. The circle contains more space than any other plane figure of equal compass.

A straight line passing through the centre, and meeting the circumference in two opposite points, is called the diameter;^h and half the diameter, or the distance from the centre to the circumference, is the radius.¹

An arc of a circle is any portion of the circumference.*

- ¹ The line AB, Figs. 3 and 4, is the base, and CD the altitude.
- Fig. 7. b The line AB Fig. 7. AC or BC. AD or ADB, Fig. 8.

[•] Figs. 1, 2, and 3. • Fig. 2. • Fig. 1. • Fig. 3. • Fig. 5.

A chord is a right line joining the extremes of an arc.¹ The versed sine is part of the diameter cut off by the chord.^m

A segment is a space contained between an arc and its chord.ⁿ A semicircle is a segment, the chord of which is the diameter.

A sector is bounded by an arc and two radii.^o When the two radii are at right angles it is a quadrant, or fourth part of the circle.

The circumference of every circle is supposed to be divided into 360 equal parts, called degrees; and each degree into 60 equal parts, called minutes, &c.

The measure of an angle is determined by the number of degrees in the arc of a circle contained between the two lines forming the angle, described round the angular point as a centre Thus the angle ACB (Fig. 8.) is an angle of so many degrees as are contained in the arc AB. Hence, a right angle contains 90 degrees.

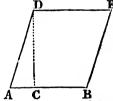
An ellipse (or regular oval) is a plane figure bounded by a curve called the circumference, returning into itself, and described from two points, called the foci or focuses, in the transverse (or longest) diameter. The shortest diameter, which intersects the transverse at right angles, is called the conjugate. The diameters are also called axes.^p

MENSURATION.

To find the area of a Parallelogram, whether it be Problem 1. a Square, an oblong Rectangle, a Rhombus, or a Rhomboid.

RULE. Multiply the length by the altitude or Fig. 1. Fig. 2. perpendicular breadth; the product will be the area. B A (1) The base of the largest Egyptian pyramid is a square, whose side is 693 feet. Upon how many acres of ground does it stand?

(2) Required the area of a rectangular board, whose length is $12\frac{1}{2}$ feet, and breadth 9 inches.



(3) What quantity of land does a m DE. ⁿ AEBDA. ° Fig. 9. P Fig. 10. **JAB or AD, Fig. 8**.

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ASSISTANT.] MENSURATION OF SUPERMOTES.

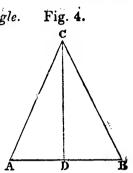
thombus contain, the base of which is 1490, and the perpendicular breadth 1280 links?

Problem 2. To find the area of a Triangle. Fi

Ruiz. Multiply the base by the altitude. and half the product will be the area.

(1) Required the number of square yards in a triangle, whose base is 49 feet, and height $25\frac{1}{4}$ feet.

(2) What is the area of the gable of a house, the base or distance between the eaves being 22 feet 5 inches, and the perpendicular from the ridge to the middle of the base, 9 feet 4 inches?

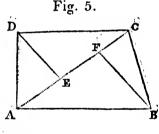


RULE 2: When the three sides only are given.—From half the sum of the sides subtract each side severally: multiply the half sum and the three remainders continually together; and the square root of their product will be the area.

(3) The three sides of a triangular fish-poind are 140, 336, and 415 yards respectively. What is the value of the land which it occupies, at $\pounds 225$. per acre?

Problem 3. To find the area of *a* Trapezium, or a Trapezoid.

Runz. Divide the trapezium into two triangles by a diagonal: multiply the diagonal by the sum of the two perpendiculars falling upon it; and half the product will be the area.



That is,
$$\frac{DE + BF \times AC}{2}$$
 = the area

For a trapezoid. Multiply the sum of the two parallel sides by the perpendicular distance between them; and half the product will be the area.

(1) How many square yards of paving are in the trapezium, whose diagonal is 65 feet, and the perpendiculars 28 and 33½ feet?

(2) Find the area of a trapezium whose south side is 2740 links; east side 3575, west side 4105, and north side 3755 links; and the diagonal from the south-west to the north-east angle 4835 links.

(3) Required the area of a trapezoid whose parallel sides are $20\frac{1}{2}$ feet and $12\frac{1}{4}$ feet respectively; the perpendicular distance being $10\frac{3}{4}$ feet?

(4) How many square feet are in a board, whose length is 12} feet, and the breadths of the two ends 15 inches and 11 inches respectively?

Problem 4. To find the area of an Irregular Figure.

RULE: Divide it by drawing diagonals into trapeziums and triangles Find the area of each, and their sum will be the area of the whole:

1. Required the content of the irregular figure ABCDEFGA, in which are given the following diagonals and perpendiculars: namely, AC = 5.5

 $\begin{array}{c} \text{Ac} = 5 \cdot 5 \\ \text{FD} = 5 \cdot 2 \\ \text{Gc} = 4 \cdot 4 \\ \text{Gm} = 1 \cdot 3 \\ \text{Bn} = 1 \cdot 8 \\ \text{Go} = 1 \cdot 2 \\ \text{Ep} = 0 \cdot 8 \\ \text{Dq} = 2 \cdot 3 \end{array}$

Fig. 6.

B

Problem 5. To find the area of a Regular Polygon.

RULE 1. Multiply the perimeter (or sum of the sides) by the perpendicular drawn from the centre to one of the sides; and half the product will be the area.

RULE 2. Multiply the square of the side by the corresponding tabtular area, or multiplier opposite to the name in the following table; and the product will be the area.

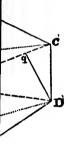
No. of sides.	Names of Polygons.	Areas, or Multipliers.
3	Trigon, or Equilateral Triangle	0.4330127
4	Tetragon, or square	1.0000000
5	Pentagon	1.7204774
6	Hexagon	2.5980762
7	Heptagon	3.6339124
8	Octagon	4.8284271
9	Nonagon	6 1818242
10	Decagon	7.6942088
11	Undecagon	9.3656399
12	Duodecagon	11.1961524

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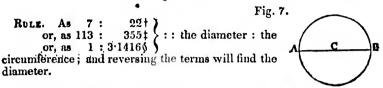
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39124	
84271	
18242	
42088	
56399	
61524	
and the second s	

ASSISTANT.] MENSURATION OF SUPERFICIES

(1) Required the area of a regular pentagon whose side is 25 feet.

(2) Required the area of an octagon whose side is 20 feet.

Problem 6 To find the diameter or circumference of a Circle, the one from the other.*



(1) Required the circumference of a circle whose diameter is 12.

* To find the proportion which the circumference bears to the diameter, and thence to find the area of a circle, is a problem that has engaged the anxious attention of mathematicians of all ages. It is now general ly considered impossible to determine it exactly; but various approximations have been found, some of which have been carried to so great a degree of accuracy, that in a circle as immense in magnitude as the orbit of the planet Saturn, the diameter of which is about 158 millions of miles, we are enabled to express the circumference (the diameter being given) so nearly approximating to the truth, as not to deviate from it so much as the breadth of a single hair. The three approximations in the Rule are those in general use.

† This is the ratio assigned by Archimedes, a celebrated philosopher of Syracuse, who flourished about two centuries before the Christian era. It answers the purpose sufficiently well when particular accuracy is not required.

t This was discovered by Metius, a Dutchman, about two centuries since. It is a very good approximation, agreeing with the truth to the sixth figure.

§ This is an abridgment of the celebrated Van Ceulen's proportion, who was nearly contemporary with Metius. By a patient and most laborious investigation, he determined it truly to 36 places of figures, (3 141598, &c.) But it has been since extended to considerably more than 100 places. This proportion is extremely convenient, from the circumstance of the first term being unity; which saves the labour of division, in finding the circumference of any other circle whose diametor is given. It is not quite so accurate as the preceding.

As 7 : 22 :: 12 : $\frac{22 \times 12}{7} = \frac{264}{7} = 37.714285$	
wr, as 113 : 355 :: 12 : $\frac{355 \times 12}{113} = 37.699115$	ence.
er, es 1 : 3 1416 : : 12 : 3 1416 \times 12 = 37 6992	

MENSURATION OF ELEARFICIES.

(2) What is the circumference when the diameter is 45? (3) What is the diameter of a column whose circumference

is 9 feet 6 inches?

(4) If the circumference of a great circle of the earth (as the equator) were exactly 25000 miles, what would be the diameter?

Problem 7. To find the area of a Circle.

RULE 1. The area is equal to a fourth part of the product of the circumference into the diameter, or the product of half the circumference into half the diameter.

Therefore, when the diameter is 1, the area $=\frac{1 \times 3 \cdot 1416}{4} = 7354$; whence we have

RULE 2. Multiply the square of the diameter by 7854, and the pro duct will be the area.

RULE 3. Multiply the square of the circumference by 07958 for the area.

(1) Required the area of the circle proposed in Example 1. Problem 6.*

(2) Find the area of the circle proposed in Example 2. Problem 6.

(3) What is the area of the end of a roller whose diameter is 2 feet 3 inches?

(4) Required the area when the circumference is 81 feet.

Problem 8. To find the side of a square inscribed in a circle. **RULE.** Multiply the radius by 1.4142, (that is, by $\sqrt{2}$,) or multiply the diameter by 7071.†

(1). Find the side of the square inscribed in the circle whose diameter is 12.

(2) What is the side of the square inscribed in a circle whose diameter is 6 feet 5 inches?

 $\frac{37 \cdot 6992 \times 12}{4} = 37 \cdot 6992 \times 3 = 113 \cdot 0976$ or, $12^2 \times .7854 = 12 \times 12 \times .7854 = 113 \cdot 0976$ the area.

+ The following Rules exhibit the principal relations between the circle and its equal square, or inscribed square.

1. The diameter $\times 8862269$ = the side of an equal square. 2. The circumfer. $\times 2820948$ =

- 3. The diameter × 7071068 4. The circumfer. × 2250791 = the side of the inscribed square 5. The area × 6366197

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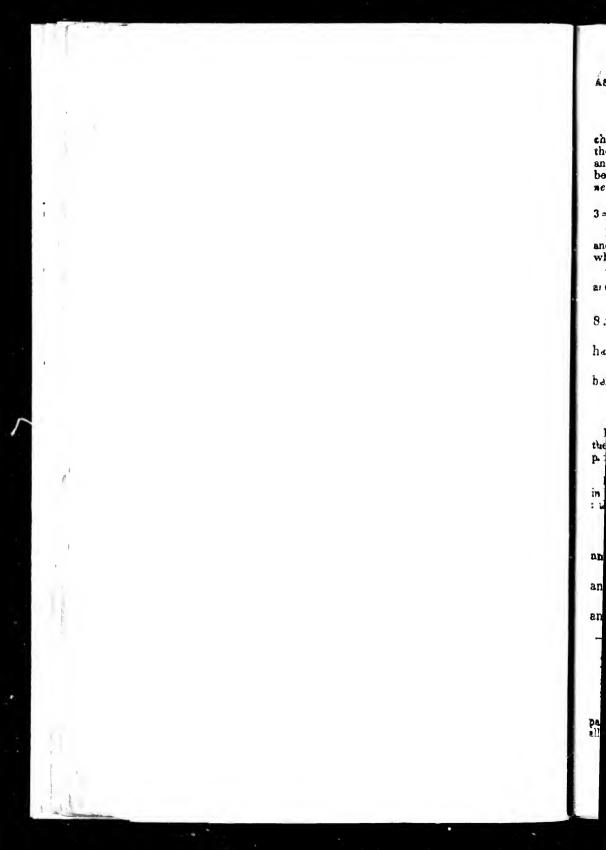
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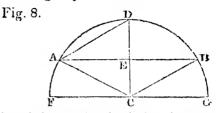
nscribed square



Problem 9. To find the length of a Circular Arc.

RULE 1. From 8 times the chord of half the arc subtract the chord of the whole arc, and f of the difference will be the length of the arc, nearly.

That is AD \times 8 – AB \div $3 = \operatorname{arc} ADB.$



Note. Half the chord of the whole arc, the chord of half the arc, and the versed sine, are sides of a right angled triangle; any two of which being given, the third may be found as directed in page 115.

RULE 2. Multiply the number of degrees in the arc by the radius. a d the product by 01745, for the length of the arc.

(1) The chord of the whole arc is 20, and the versed sine 8. what is the length of the arc?

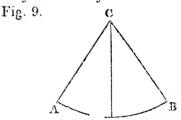
(2) What is the length of the arc when the chord of the half arc is 10.625, and its versed sine 5^{2}

(3) Required the length of an arc of 12° 10', the radius being 10 feet.

Problem 10. To find the area of a Sector of a circle.

RULE 1. Multiply the length of the arc by the radius, and half the p. pduct will be the area.

RULE 2. As 360° : the degrees in the arc : : the area of the circle : the area of the Sector.



(1) Required the area of the sector, when the radius is 15, and the chord of the whole arc 18 feet.

(2) What is the area of a sector whose arc is $147^{\circ} 29'$. and the radius 25?

(3) Required the area of a sector, whose radius is 20 feet, and the versed sine 1 foot 9 inches.*

6. The side of a square $\times 1.414214 =$ the diameter } of its circum-7. The side of a square $\times 4.442363 =$ the circumf. Scribing circle.

- 8. The side of a square $\times 1.128379 =$ the diameter (of an equal cir-
- 9. The side of a square $\times 3.544908 =$ the circumf. cle.

• By the properties of the circle, the versed sine X the remaining. part of the diameter = the square of half the chord of the arc; whence all the requisites may be found.

(4) What is the area of the sector, when the chord of half its arc is 14 feet 2 inches, and the versed sine 6 feet 8 inches?*

Problem 11. To find the area of a Circular Segment.

RULE 1. Find the area of the sector; and also the area of the triangle formed by the chord and the two radii of the sector: their difference, when the segment is less than a semicircle, or their sum, when it is greater, will be the area of the segment.

RULE 2. Divide the height of the segment by the diameter, and find the quotient in the column of heights in the following table. Multiply the corresponding area by the square of the diameter, for the area of the segment.

Height.	Area of Segment.	Height.	Area of Segment.	Height.	Area of Segment.	Height.	Area of Segment.
·01	+00133	.14	$\cdot 06683$	·26	$\cdot 16226$	·39	$\cdot 28359$
$\cdot 02$	$\cdot 00375$.15	$\cdot 07387$	·27	$\cdot 17109$	•40	·29337
·03	$\cdot 00687$	·16	.08111	·28	$\cdot 18002$	•41	·30319
·04	$\cdot 01054$.17	·08854	$\cdot 29$	18905	•42	·31304
$\cdot 05$	·01468	·18	.09613	·30	$\cdot 19817$	•43	$\cdot 32293$
•06	·01924	$\cdot 19$	$\cdot 10390$	•31	$\cdot 20738$	•44	·33284
•07	$\cdot 02417$	$\cdot 30$	$\cdot 11132$	$\cdot 32$	$\cdot 21667$	•45	·34278
$\cdot 08$	$\cdot 02944$	$\cdot 21$	$\cdot 11990$	•33	$\cdot 22603$	•46	·35274
•09	$\cdot 03501$	22	$\cdot 12811$	$\cdot 34$	·23547	•47	·36272
•10	·04088	23	·13647	•35	$\cdot 24498$	•48	·37270
•11	$\cdot 04701$	·24	$\cdot 14494$	•36	$\cdot 25455$	•49	$\cdot 38270$
$\cdot 12$	$\cdot 05339$	$\cdot 25$	$\cdot 15355$	•37	$\cdot 26418$	•50	·39270
·13	·06000			$\cdot 38$	$\cdot 27386$		

Table of the Areas of Circular Segments.

(1) What is the area of a segment, when the chord of the whole arc is 60, and the chord of half the arc $37\frac{1}{2}$?

* When the half chord (see AE, Fig. 7) of the arc is found by the properties of a right angled triangle, then $AE^2 =$ the versed sine (DE) \times the remaining part of the diameter; whence the diameter (and consequently the radius) will be known.

t When there is a remainder (or fraction) after the second quotient figure, in dividing the height by the diameter; having taken ont the area answering to the two figures, add to it such fractional part of the difference between that and the next succeeding area, for the sake of greater accuracy.

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· Segment.

e area of the trictor: their differtheir sum, when

iameter, and find table. Multiply r, for the area of

nents.

Height.	Area of Segment.	
·39	·28359	
·40	·29337	
·41	·30319	
$\cdot 42$	·31304	
·43	·32293	
·44	·33284	
·45	$\cdot 34278$	
•46	$\cdot 35274$	
·47	·36272	
$\cdot 48$	·37270	
·49	·38270	
·50	·39270	
	1	

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rc is found by the e versed sine (DE) ameter (and conse-

ne second quotient ving taken out the sectional part of the en, for the sake of (2) What is the area of a segment whose height is 18, and the diameter of the circle 48?

(3) Required the area of a circular segment whose height is 2 and chord 20.

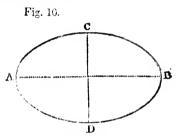
(4) What is the area of the segment of a circle whose radius is 24, the chord of the whole arc 20, and the chord of half the arc 10.2?

(5) If the radius of a circle is 10 feet, what is the area of the segment whose chord is 12 feet?

Problem 12. To find the circumference of an Ellipse, the transverse and conjugate diameters being given.

RULE. Multiply the square root of half the sum of the squares of the two diameters by 3.1416, and the product will be the circumference hearly.*

(1) What is the circumference of an ellipse whose transverse diameter is 24, and conjugate 18?



(2) The two axes of an ellipse are 60 and 45 yards respectively: what is the circumference?

Problem 13. To find the area of an Ellipse.

RULE. Multiply the product of the axes by 7354 for the area.

(1) Required the area of an ellipse whose axes are 35 and 25.

(2) What will be the expense of trenching an elliptic garden, whose axes are 70 and 50 feet, at $3\frac{3}{4}d$. per square yard?

(3) Required the area of the ellipse in Grosvenor Square, London, the transverse diameter being 8.40 chains, and the conjugate 6.12 chains.

Problem 14. To find the area of an Elliptic Segment, the base being parallel to either axis.

RULE. Divide the height of the segment by that are of which it is a part, and find, in the *Table of Circular Segments*, a versed sine equal to the quotient.

* If the half sum of the two diameters be multiplied by 3.1416, the product will give the circumference sufficiently near for most practicel purposes.

Multiply the corresponding *tabular area* and the two **axes continu**. ally together, and the product will be the area required.

(1) What is the area of an elliptic segment cut off by a line (called a double ordinate) parallel to the conjugate diameter at the distance of 36 yards from the centre, the axes being 120 and 40 yards respectively?

(2) Required the number of sonare yards in the segment of an ellipse, cut off by an ordina e paratiel to the transverse diameter; the height being 5 feet, and the two axes 35 and 25 feet respectively.

A COLLECTION OF QUESTIONS.

(1) WHAT is the value of 14 barrels of soap, at $4\frac{1}{2}d$. per *lb*., each barrel containing 254 *lb*.? Ans. £66..13..6.

(2) A and B joined in partnership; A put into the joint stock £320. for 5 months, and B £460. for 3 months: they gained £100. What is each man's share of the gain?

Ans. A's £53..13..9 $\frac{27}{298}$, and B's £46..6..2 $\frac{28}{298}$.

(3) How many yards of cloth, at 17s. 6d. per yard, can **I** have for 13 cwt. 2 qrs. of wool, at 14d. per lb.?

Ans. 100 yards, 31 grs.

(4) If I buy 1000 clls of Flemish linen for $\pounds 90.$, at what price must I sell it per English ell to gain $\pounds 10.$ by the whole? Ans. 3s. 4d. per ell.

(5) A has 648 yards of cloth at 14s. per yard, ready money, but in barter will have 16s. B has wine at \pounds 42. per tun, ready money: what must he charge it per tun in barter; and what quantity must be given in exchange for the cloth?

Ans. £48. per tun, and the quantity, 10 tuns, 3 hhds., $12\frac{3}{5}$ gals.

(6) A jeweller sold jewels to the value of £1200., for which he has received in part 876 French pistoles, at 16s. 6d. each. How much more is due to him? Ans. £477..6.

(7) An oilman bought 417 cwt. 1 qr. 15 lb. gross weight of train oil, tare 20 lb. per cwt. : how many neat gallons were there, allowing $7\frac{1}{2}$ lb. to a gallon? Ans. 5120 gallons.

(8) If I buy cloth at 14s. 6d. per yard, and sell it at 16s 9d., what is the gain per cent.? Ans. £15..10..4 $\frac{4}{26}$.

(9) Bought 27 bags of ginger, each weighing gross $84\frac{3}{4}$ lb.; tare $1\frac{3}{4}$ lb. per bag, tret as usual: what is the value at $8\frac{1}{4}$ d. per lb.? Ans. £76..13..2 $\frac{1}{4}$.

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at $4\frac{1}{2}d$. per 66..13..6. to the joint onths: they gain? $5..6..2\frac{28}{298}$. yard, can I

ds, 3½ qrs. 290., at what ± 10 . by the 4d. per ell. yard, ready e at £42. per tun in barter; r the cloth? hds., 12³/₅ gals. 00., for which 16s. 6d. each. s. £477..6. oss weight of gallons were 20 gallons. sell it at 16s $15..10..4\frac{4}{29}$. gross 843 1b.; value at 81d: 676.13.24

ASSISTANT.] A COLLECTION OF QUESTIONS.

(10) If $\frac{2}{3}$ oz. cost $\frac{7}{6}s$. what will $\frac{5}{6}$ lb. cost? Ans. 17s. 6d. (11) If $\frac{5}{6}$ of a gallon cost $\frac{5}{3}$ of a \mathcal{L} . what will $\frac{5}{9}$ of a tun cost? Ans. $\mathcal{L}105$.

(12) A gentleman who spends one day with another $\pounds 1..7..10\frac{1}{2}$. lays up at the year's end $\pounds 340$. What is his annual income? Ans. $\pounds 848..14..4\frac{1}{2}$.

(13) What is the difference in ounces, between 13 fothers of lead, and 39 boxes of tin, each box weighing 388 *lb*.?

Ans. 212160 ounces.

(14) A captain, commanding a crew of 160 mariners, captured a prize worth £1360. The captain was allowed onetifth, and the rest was equally divided among the sailors. What was each man's share?

Ans. The captain had £272, and each sailor £6..16.

(15) At what rate per cent. will $\pounds 956$. amount to $\pounds 1314$.. 10. in $7\frac{1}{2}$ years, at simple interest ? Ans. $\pounds 5$. per cent.

(16) A has 24 cows worth $\pounds 3.12$. each, and \hat{B} 7 horses worth $\pounds 13$. each. How much will make good the difference, in case they interchange their droves of cattle? Ans. $\pounds 4..12$.

(17) A man left £120. to be given to three persons, A, B, and C; B to have twice as much as A, and C as much as A and B; what was the share of each?

Ans. A £20. B £40. and C £60.

(18) \pounds 1000. is to be divided among three men, in such a manner, that if A has \pounds 3. B shall have \pounds 5. and C \pounds 8. How much will each man have ?

Ans. A £187..10. B £312..10. and C £500. (19) A piece of wainscot is S feet $6\frac{1}{2}$ inches long, and 2 feet $9\frac{3}{4}$ inches broad: what is the superficial content?

Ans. 24 feet 0' 3" 4" 6"".

(20) A garrison of 360 men, who had originally six months' provisions, having endured a siege of 5 months, without obtaining any relief or fresh supply, wish to know how many men must depart, that the provisions may suffice for the residue 5 months longer ? Ans. 288 men.

(21) The less of two numbers is 187; the difference 34. The square of their product is required. Ans. 1707920329

(22) A butcher sent his man with \pounds 216. to a fair to bur cattle; he bought oven at \pounds 11. cows at 40s. colts at \pounds and hogs at \pounds 1..15. each, and of each a like number. wna, was the number of each? Ans. 13 of each sort, and \pounds 8. over

(23) What number added to $11\frac{3}{2}$ will produce $36\frac{3}{2}\frac{7}{6}$ Ans. $24\frac{3}{6}\frac{1}{16}$

A COLLECTION OF QUESTIONS.

(24) What number multiplied by $\frac{3}{7}$ will produce $11_{\frac{1}{7}\frac{7}{7}}$? Ans. $26\frac{4}{7}$.

(25) What is the value of 179 hogsheads of tobacco, each weighing 13 cwt. at $\pounds 2..7..1$. per cwt.? Ans. $\pounds 5478..2..11$.

(26) My factor informs me that he has bought goods on my account, of the value of $\mathcal{L}500..13..6$ What will his commission come to at $\mathcal{L}3\frac{1}{2}$, per cent.? Ans. $\mathcal{L}17..10..5..2\frac{1}{2}\frac{1}{3}$ grs

(27) If $\frac{1}{3}$ of 6 were three, what would $\frac{1}{4}$ of 20 be ? Ans. 7 $\frac{1}{4}$

(28) Reduce 3 qrs. 14 lb. to the decimal of a cwt.

Ans. .875 cwt.

(29) How many lb. of sugar, at $4\frac{1}{2}d$. per lb. must be given in barter for 60 gross of inkle, at 8s. 8d. per gross?

Ans. 1386²/₄ lb.

(30) If I buy yarn for 9d. per lb. and sell it again for $13\frac{1}{2}d$ per lb. what is the gain per cent.? Ans. £50.

(31) A tobacconist mixes 20 lb. of tobacco at 9d. per lb. with 60 lb. at 12d. per lb. 40 lb. at 18d. per lb. and 12 lb. at 2s. per lb. what is a pound of the mixture worth?

Ans. 1s. $2\frac{1}{4}d$.

(32) What is the difference between twice eight and twenty, and twice twenty-eight; also between twice five and fifty and twice fifty-five? Ans. 20, and 50.

(33) Whereas a noble and a mark just 15 yards did buy; How many ells of the same cloth for £50. had 1?

Ans. 600 ells.

(34) A broker bought for his principal, in the year 1720 \pounds 400. South Sea stock, at \pounds 650. per cent. and sold it again when it was worth but \pounds 130. per cent. What was the whole loss? Ans. \pounds 2080.

(35) C has candles at 6s. per dozen ready money, but in barter will have 6s. 6d. per dozen; D has cotton at 9d. per lb. ready money: what price must the cotton be charged in barter; and how much must be exchanged for 100 dozen o' candles ! Ans. The cotton at $9\frac{3}{4}d$. per lb. and the quantity. 7 cwt. 0 grs. 16 lb.

(36) If a clerk's salary is $\pounds 73$. a year, what is that pe day? Ans. 4s.

(37) B has an estate of £53. per annum, and pays 5s. 104 to the subsidy: what must C pay, whose estate is worth £100. per annum? Ans. 11s. $0\frac{4}{5\pi}d$.

(38) If I buy 100 yards of riband, at 3 yards for a shilling and 100 yards more at 2 yards for a shilling, and sell the

TUTOR'S

[TUTOR'S

 $11_{77}?$ s. 2649. acco, eacb 78..2..11. bods on my is commis $5..2\frac{1}{2}\frac{7}{5} qrs$? Ans. 71 wt.875 cwt. st be given $1386_{\frac{2}{3}}$ lb. in for $13\frac{1}{3}d$ ns. £50. 9d. per lb. nd 12 *lb*. at $2\frac{1}{4}d. \frac{9}{17}$ and twenty,

e and fifty , and 50.

s did buy;). had I ? . 600 *ells*.

year 1720 sold it again as the whole s. £2080. oney, but in n at 9d. per charged in 00 dozen o the quantity.

t is that pe Ans. 4s. oays 5s. 104 the is work $11s. 0\frac{4}{5\pi}d$. or a shilling and sell the

ASSISTANT.] A COLLECTION OF QUESTIONS.

whole at the rate of 5 yards for 2 shillings; whether do I gain or lose, and how much? Ans. Lose 3s. 4d.

(39) From what number must $\frac{3}{5}$ be deducted, that the remainder may be $\frac{1}{5}$?

(40) A farmer wishes to mix rye at 4s. a bushel, barley at 3s., and oats at 2s. How much must he take of each to sell the mixture at 2s. 6d. per bushel?

Ans. 6 of rye, 6 of barley, and 24 of oats. (41) If $\frac{3}{6}$ of a ship is worth £3740., what is the value of the whole? Ans. £9973..6.8.

(42) Bought a cask of wine for $\pounds 62..8$, at 5s. 4d. per gallon. How many gallons were there? Ans. 234.

(43) A dissipated young fellow in a short time got through $\frac{1}{4}$ of his fortune; he then gave £2200. for a commission in the army: his profusion continued till he had no more than 880 guineas left, which was $\frac{3}{2\sigma}$ of his money after the commission was bought. What was his fortune at first?

Ans. £10450.

(44) A sum of money is to be divided amongst four men. so that the first shall have $\frac{1}{3}$, the second $\frac{1}{4}$, the third $\frac{1}{6}$, and the fourth the remainder, which is $\pounds 28$. What is the sum? Ans. $\pounds 112$.

(45) What is the amount of £1000. in $5\frac{1}{2}$ years at £1 $\frac{3}{4}$. per cent. per annum, simple interest? Ans. £1261..5.

(46) Sold goods, amounting to the value of £700., at two 4 months. What is the present worth at £5. per cent. per annum, simple interest? Ans. £682..19..5 $\frac{1}{4}$, $\frac{17.7}{1.861}$.

(47) A room 30 feet long and 18 feet wide is to be covered with painted cloth. How many yards of three-quarters wide will cover it? Ans. 80 yards.

(48) Betty told her brother George that, though her marriage portion took £19312. out of her family, it was but $\frac{3}{5}$ of two years' rent. What was his annual income?

Ans. £16093..6..8,

(49) A gentleman having 50s. to pay among his labources for a day's work, gave to every boy 6d., to every woman 8d., and to every man 16d. There was an equal number of each description. What was that number ? Ans. 20 of each.

(50) What is the solid content of a stone that measures 4 feet 6 inches long, 2 feet 9 incnes broad, and 3 feet 4 inches deep? $Ans. 41\frac{1}{4}$ soud feet.

(51) What does the pay of a ship's crew, consisting of 64C sailors, amount to for 32 mondus' service, each man's pay being 22s 6d. per mondul? Anc. $\pounds 23040$.

TUTOR'S

SUPPLEMENTAL QUESTIONS.

(52) A traveller would change 500 French crowns, at 4s. Bd. per crown, into sterling money, but he must pay a halfpenny per crown for change. How much sterling money will he receive? Ans. £111..9.2.

(53) B and C traded together, and gained $\pounds 100$; B put in $\pounds 640$, C put in so much that he was entitled to $\pounds 60$. of the gain. What was C's stock? Ans. $\pounds 960$.

(54) From what principal sum did £20, interest arise in one year, at the rate of £5, per cent. per annum? Ans. £400.

(55) How many French pistoles, at 17s. 6d. each, are equal to 672 Spanish guilders, at 2s. each? Ans. 764.

(56) Out of 7 choeses, each weighing 1 cwt. 2 qrs. 5 lb., how many allowances for seamen may be cut, each weighing 5 or . 7 drams? Ans. 356335.

(57) If 48 taken from 120 leaves 72, and 72 taken from 9! leaves 19, and 7 taken from thence leaves 12, what numler is that, out of which, when you have taken 48, 72, 19, and 7, leaves 12? Ans. 158.

(58) A farmer, unskilled in numbers, ordered £500. to be divided among his 5 sons, thus: "Give A, says he, $\frac{1}{3}$, B $\frac{1}{3}$, D $\frac{1}{6}$, and E $\frac{1}{7}$ part." Divide this equitably among them according to the futher's intention.

Ans. A £152..10..1 $\frac{1}{4}$ $\frac{1}{4}$ $\frac{6}{5}$ $\frac{5}{6}$. B £114..7..6 $\frac{3}{4}$ $\frac{42}{5}$ $\frac{3}{4}$. C £91..10..0 $\frac{3}{4}$ $\frac{63}{4}$. D £76..5..0 $\frac{1}{2}$ $\frac{2}{4}$ $\frac{5}{5}$. E £65..7..2 $\frac{1}{4}$ $\frac{45}{485}$. (59) When first the marriage knot was tied

Between my wife and me,

My age did hers as far exceed,

As three times three does three;

But when ten years, and half ten years,

We man and wife had been,

Her age came then as near to mine

As eight is to sixteen.

Quest. What was each of our ages when we married? Ans. 45 years the man, 15 the woman.

SUPPLEMENTAL QUESTIONS.

(1) How many gallons of the imperial standard measure are respectively equal to a hogshead of wine and a hogshead of ale, old measure; and what was the difference between the two hogsheads in cubic inches?

(2) What quantity of the old ale measure would correspond to 54 gallons of the imperial standard?

176

TUTOR'S

wns, at 4.s. bay a halimoney will 11..9..2. ; B put in 260. of the s. £960. arise in one s. £400. h, are equal ns. 764. 2 grs. 5 lb., h weighing 356334. taken from what num-72, 19, and 1ns. 158. 6500. to be he, 1, B 1 mong them

..7..63 433.

narried ? he woman.

ard measure a hogshead ace between

ould cerres.

(3) How many gallons of the old wine measure are equal in quantity to 63 gallons, imporial measure?

(4) Reduce 15 quarters, 3 bushels, 1 peck, old measure, to its equivalent in the imperial standard measure.

(5) A lady who was asked the time of the day, said that it was between *three* and *four*: but being desired to name the *exact* time, she replied, "The minute hand is advanced half an hour precisely before the hour hand." Required the exact time.

(6) If 7 men can build a wall 40 yards long, 4 feet high, and 2 feet thick, in 32 days; how many men will build a wall 240 yards long, 6 feet high, and 3 feet thick, in 8 days ?*

(7) The weight of a certain bar of iron 2 feet long, 3 inches es broad, and 1 inch thick, is 20 *lbs.* What is the weight of a bar of similar quality which is $7\frac{1}{4}$ feet long, $4\frac{1}{2}$ inches broad, and $3\frac{1}{2}$ inches thick?

(8) A person who had five-ninths of a mine, made his younger brother a present of half his share, and sold half the remainder to his cousin John, who soon after purchased $\frac{1}{3}$ of the younger brother's share; but now offers to dispose of half his interest in the mine for $\mathcal{L}150$. Estimating at the same rate, what is the value of the whole mine, and of each brother's share?

(9) A, travelling from London to Manchester, and B from Manchester to London, set out at the same time. They meet at the end of six days, A having travelled 3 miles a day

RULE. Arrange the terms of the first cause and effect in one line, and the corresponding terms of the second cause in dieffect exactly under them; supplying the place of the term englat with an asterisk, and connecting the contrary causes and effects by cross lines. Multiply continually the terms of each cause and the other effect: divide the product arising from the full number of terms by the product of those with which the blank term is connected, and the quotient will be the answer.

Solution of the above example.

$ \begin{array}{c} \text{mon} & \frac{days}{32} & \frac{build}{2} y, \ bag \ fi, \ h, \ fi, \ h, \\ \textbf{If} \ \textbf{7} & \frac{32}{32} & \frac{40}{2}; \ 4:2 \\ \textbf{*} & \vdots & 8 \\ & \frac{2}{3} uvoll. \end{array} $	$\begin{cases} 1 & 6 & 3 \\ \hline & 6 & 3 \\ \hline & 7 \times 32 \times 249 \times 6 \times 3 \\ \hline & 8 & 49 \times 4 \times 2 \\ \hline & 1 & 1 & 1 \\ \hline & 1 & 1 & 1 \\ \end{cases} = 378 \text{ men.}$
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H C

^{*} Questions of *Compound Proportion* in which the terms are numerous may be solved by Rule 1, for the Double Rule of Three; but the following method is more convenient.

more than B. At what rate did each go, the distance being 186 miles?

(10) A coach, which runs the whole distance in 31 hours, starts from London at the same time that another, which does it in 21 hours, starts from Manchester. Required the number of hours elapsed, and the distance travelled by each when they meet.

(11) A load of corn was sold for .C15. at a loss of 15 per cent. What should it have been sold for to gain as much per cent. as the corn cost?

(12) Two men purchased a grinding stone 42 inches in diameter for a guinea; of which the first paid twelve shillings. They agree that the first shall use it till his share is worn down. What will be the diameter when the second receives it?

(13) If A and B together do a piece of work in $7\frac{3}{4}$ days, which A alone would accomplish in $12\frac{1}{2}$ days; in what time would B do it himself?

(14) A person lent \pounds 400, and agreed to receive in return a yearly payment of \pounds 50, for 13 years. Whether would he gain or lose thereby, reckoning Compound Interest at \pounds 5, per cent. per annum?

(15) By selling a horse for .C50. I gained one-fourth of what he cost me; but the whole cost (including the expense of his keep) was one-fourth more than the original purchase. How much did I give for him, what did I expend in keeping him and what did I gain per cent.?

(16) It has been found by experiment, that sound is conveyed through the air at the rate of 1112 feet in a second. How far distant is the cloud, when $7\frac{3}{4}$ seconds elapse between seeing the flash of lightning and hearing the thunder?

(17) What is the height of a tower that projects a shadow75.75 yards long, at the same time that a perpendicular staff,3 feet high, gives a shade of 4.55 feet in length?

(18) A bankrupt owes $\pounds 2580$, and the value of his effects is $\pounds 846$, and the amount of recoverable debts $\pounds 358..12$, besides which he has an unexpired lease that has 13 years to run, valued at $\pounds 12$, a year more than the stipulated rent. If the lease be disposed of for present money, allowing Compound Interest at $\pounds 5$, per cent, per annum; and if the working of the commission and other expenses amount to $\pounds 172$; wha will his creditors have in the pound, provided they allow him $\pounds 150$, to recommence business?

(19) A youth aged 12 years, having had bequeathed to him

178

TUTOR'S

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f his effects 358..12. be-13 years to ed rent. If owing Comthe working \pounds 172; wha by allow him

athed to him

an annuity of .250. for 12 years, to commence when he comes of age, the executors think it will be more advantageous to exchange this for an annuity to commence immediately, and continue till he is 21, to enable them to give him some education and a trade. What will be such annuity, $\pounds 100$, being reserved at the conclusion to set him up in business?

(20) There is an island 73 miles in circumference, to travel round which three pedestrians all start at the same time: A travels 5 miles a day, B travels 8, and C 10 miles a day. In how many days will they all come together again, and how many circuits will each have made ?

(21) What will a banker charge for discounting a bill of £52.10. on the 7th of April, the bill being dae on the 19th of Mav?

(22) My agent in I is n having advised the that he has purchased goods on my account to the amount of $\pounds756.10$, at six months' credit, or $\pounds7\frac{1}{2}$, per cent. discount for prompt payment, if I send a remittance of $\pounds400$, to be paid down on account, after deducting out of it his charge for commission at $\pounds2\frac{1}{4}$, per cent., what will remain to be discharged at the end of six months !*

(23) If I insure a house for £250, at the annual charge of 1s. 6d. per cent., and the furniture, &c., for £150, at the rate of 4s. 6d. per cent., what shall I have to pay yearly to the Insurance office, including the duty paid to Government of $\frac{1}{2}$, or 2s. 6d. per cent.?

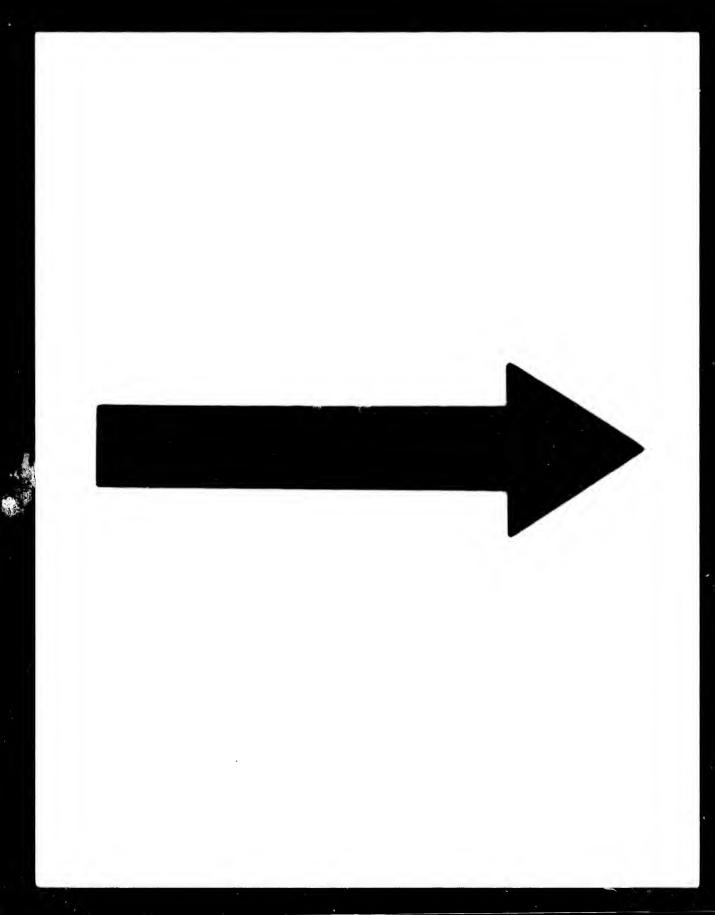
(24) If 12 oxen will eat 31 acres of grass in 4 weeks, and 21 oxen will eat 10 acres in 9 weeks, how many exen will eat 24 acres in 18 weeks, allowing the grass to grow uniformly.?

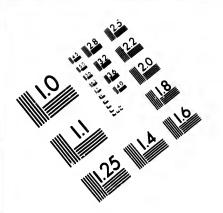
(25) A bath is supplied with water by two cocks, from one of which it may be filled in 40 minutes, and from the other in 50 minutes: a discharging cock will so not how her clied) in 25 minutes. If all the three be opened and costate time, in what time will the back be filled, supposing the indix and efflux to be uniform?

(26) A person who had spont two-thirds of his money at one place, and half the remainder at another, found that he had $\pounds 32..12$. left. How much had he at $\hbar 2..12$.

(27) The length, breadth, and height of a room are ! 6

* See Note to Example 11, Discount, page 71.





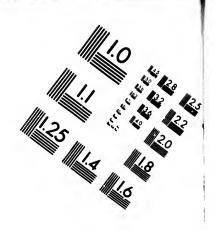
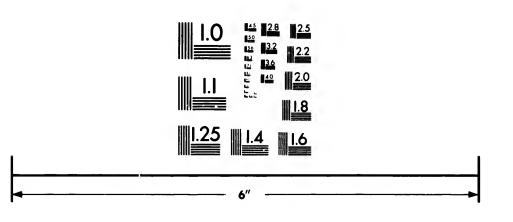
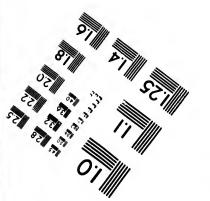
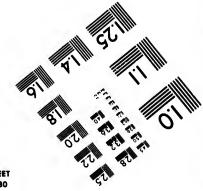


IMAGE EVALUATION TEST TARGET (MT-3)

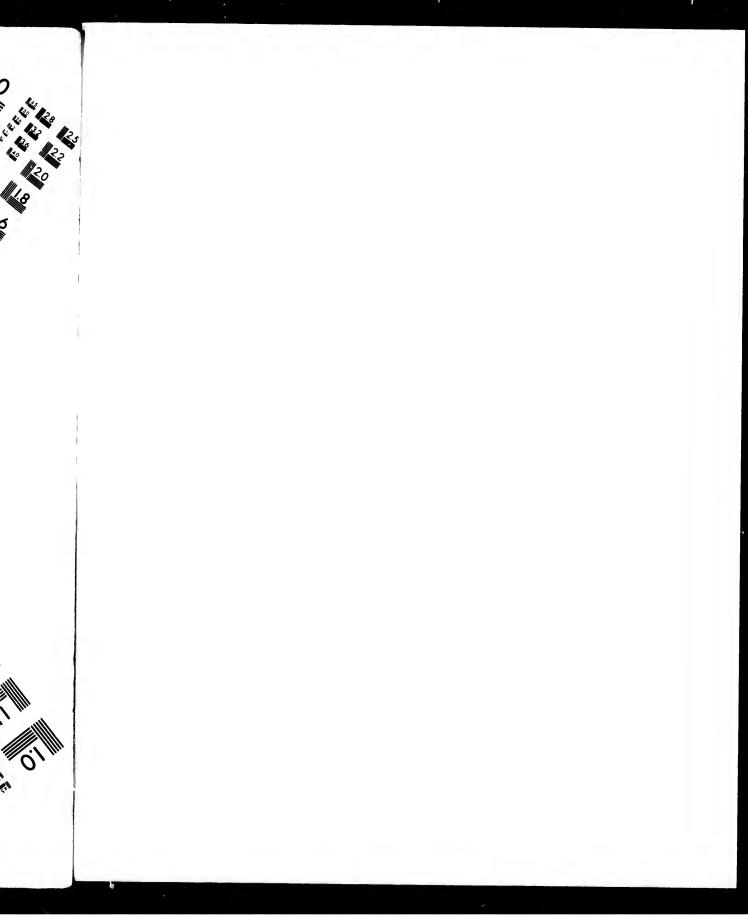




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and 4 yards respectively. What is the longest right line that can be taken within that room?

TUTOR'S

(28) What must be the length of a cord with which a horse may be tethered to a certain point in a straight fence, so as to allow him the liberty of grazing to the extent of 1 rood, supposing that he can reach 2 yards beyond the tether?

(29) A person playing at cards, lost three nights successively. The first night he lost half his sovereigns and half a sovereign besides; the second night he lost half the remainder and half a sovereign more; and the third night half the remainder and half a sovereign more, which reduced his stock to twenty. How many sovereigns had he at first?

(30) The month of July, 1828, was remarkable, both in England and several parts of the Continent, for excessive rains. At Darby, the quantity collected in the pluviameter (or rain-guage) between the hours of nine, A. M., of the 9th of that month and six the following morning (an interval of 21 hours) was 3:59 inches; to the evening of the 15th it amounted to $7\frac{1}{2}$ inches; and by the conclusion of the 29th, an interval of 21 days, of which 10 only were very rainy, the total depth of water collected was $11\frac{1}{3}$ inches. How many hogsheads, of 54 and 63 imperial gallons respectively, fall on an acre of ground to amount to the depth of one inch; and how many hogsheads of each kind fell on the surface of an acre during each of the three coveral intervals above mentioned ?

(31) A person who occupies a piece of ground for which he pays a rent of $\pounds 10$, per annum, wishes to take it upon a lease for forty years, with the obligation of laying out upon it during the present year $\pounds 600$, in the erection of a building, which is to be left in good tenantable condition at the termination of the lease. The question is, how much will be a fair annual rent for the lease to pay during the term of continuance of such tenure, admitting the ground rent paid at present to be a fair one, and supposing the customary interest of money to be at the rate of $\pounds 5$, per cent, per annum? Also, supposing interest to be at $\pounds 4$, per cent, per annum?

(32) What will be the expense of covoring and guttering a roof with lead at 18s, *per cart.*, the length of the roof being 40 feet, and the breadth or gut over it 52 feet; the guttering 57 feet long and 0 feet wide: the lead for the former being 9834 D_{c} and for the latter 7873 D_{c} to the square foot !

[TUTOR'S

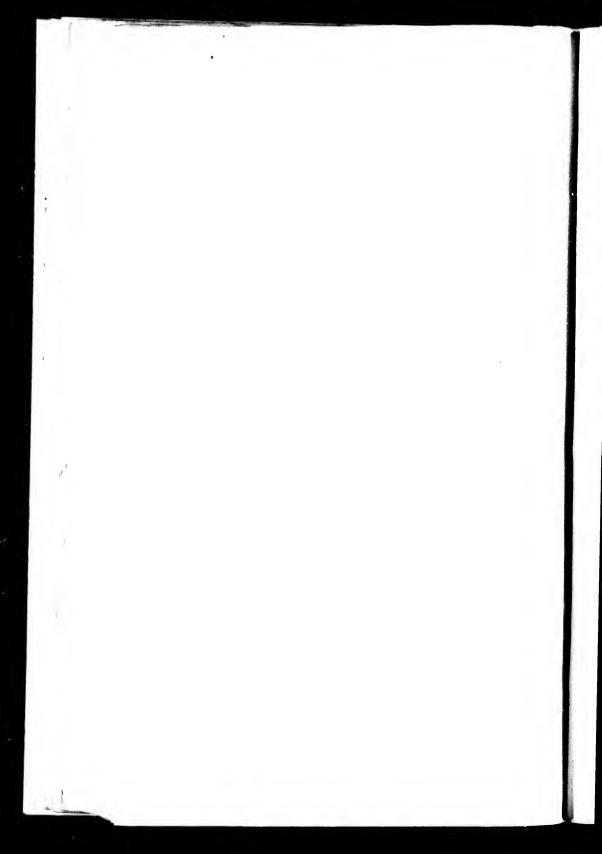
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for which it upon a g out upon a building, the termiill be a fair of continuat present interest of m ? Also, n ? l guttering roof being guttering mer being foot ?



(181)

A COMPENDIUM OF

BOOK-KEEPING,

BY SINGLE ENTRY;

Intended for the purpose of initiating Youth in the LEADING PRINCIPLES of that important Branch of Science.

BOOK-KEEPING is the art of recording pecuniary or commercial transactions in a regular and systematic manner.

The science of Book-keeping admits of innumerable varieties of method: but its general principles are invariable. These being well understood, the knowledge of any particular system, adapted to the peculiar concerns of any counting-house, will be easily acquired.

Single Entry, being the most simple and concise, is the method usually adopted in retail business.

The General Rule to be observed in every system of Book-keeping, is,

To make any person Debtor (Dr.) for money or goods which he receives from me, and to make him Creditor (Cr.) for whatever I receives from him.

The books usually kept in *Single Entry*, are the Day-Book, the Cash-Book, the Ledger, and the Bill-Book.

The Day-Book, when a person commences business, begins with an inventory of the existing state of his affairs: after which are entered, in the regular order of time, the daily transactions of Goods bought and sold.

The Cash-Book contains the particulars of all Money transactions. It is ruled in a folio form: on the left hand page, Cash is debited to all sums received, and on the right, Cash is credited by all sums paid. The Balance (or quantity which the Dr. side exceeds the Cr.) shows the amount of Cash in hand. This should be ascertained weekly, and in some concerns daily, in order to prove if it corresponds with the real Cash in hand.

In the Ledger are collected the dispersed accounts of each person from the Day-Book and Cush-Book, and entered in a concise manner in one folio; the sums in which he is Dr, being arranged on the left-hand, and those in which he is Cr. on the right-hand page of the folio: so that the Balance of his account (the difference between the Dr, and Cr, sides) may always be easily ascertained by inspection. The transferring of accounts from the Day-Book and Cash-Book to the Ledger, is called posting.

In many trades it is found convenient to keep the accounts of Goods Sold at the former end, and those of Goods Bought at the latter end of the Ledger. But in concerns of magnitude, two Ledgers are more convenient; one for Goods Sold, and the other, called the "Bought Ledger," for Goods Bought.

In the BILL-BOOK are copied the periodics of all Bills of Exchange, whether Receivable or Payable. The former are those which come into the Tradesman's per session, and are drawn upon some other person; the latter are those which are drawn upon and accepted by him.—Printed Bill-Books may be had of any Bookseller.

NOTE. In the following transactions, Bills Receivable are considered as Cash: but many Accountants do not enter them as such, till Cash has been actually receiv el for them

(182)

MEMORANDUMS

OF THE TRANSACTIONS STATED IN THE FOLLOWING BOOKS.

- ⁵28. 5. Received from Allen, Wild, and Co. of Leeds, on credit, 9 pieces of super blue cloth, each 36 yds. at 25s. 6d. per yard — and 2 pieces of narrow brown, 84 yds. at 4s. 9d.
- Sold Bernard Mason 2 st. raw sugar, at 9¹/₂d. pcr 10.-3¹/₂ 10. green tea, at 8s. 6d.—and 3¹/₃ yds. blue cloth, at 28s.
- Bought of Samuel Fletcher, 1 cwt. 1 qr. 5 lb. Kent hops, at £5..7. per cwt.—and 1½ cwt. of Worcester, at £5..11..6;—six months' credit, or 5 per cent. discount for cash.—Paid him Bill, No. 1, £24..3..9. and received from him a cheque on Smith and Co. Bankers, for the difference, including discount.
- 3. Bought of Simmonds and Co. Liverpool, 2 cws. yellow soap, at 76s.-12 doz. dip candles, at 8s. 6d.-and 4 doz. mould do. at 11s. 3d.
- 24. Sold William Tomlinson 7 yds. narrow cloth, at 5s. 3d.—and 15 yds. calico, at 84d.
- 19. Sold Hazard and Jones 11 st. yellow soap. at 9d. per lb.-1 st. mottled, at 91d.-9 lb. candles, at 9d.-and 3 lb. mould do. at 121d. Paid Cash for Bill, No. 1, W. Holmes, £45..10.
- 23. Received from J. Sanderson, goods as per invoice £7..3..6.
- 52. Sold Hazard and Jones 17 1/2 1/2. lonf sugar, at 1s. 1d.-12 1/2. raw do. at 10d.-11 1/2. Congou tea, at 7s. 6d.-and 1/2 1/2. Hyson, at 12s.
- 21. Paid the balance due to J. Herdson, cash £37..5..6. abatement
 4d.—Sold him on credit 10 lb. hops, at 13d.—and half a ream of cap-paper, at 7d. per guire.
- cap-paper, at 7*d. per quire.* Feb. 1. Sold W. Tomlinson 2 st. yellow soap, at 9*d. per lb.*—6 *lb.* mould candles, at 1s. 1*d.*—and 16 *lb.* lump sugar, at 12½*d.* Received of him cash for account due, including the present goods, £4..13. abatement 3½*d.*

Paid Bernard Mason the balance due, cash £832; abatement 5s. 21d.

- 4. Received of James Taylor $\frac{1}{2}$ yr's. interest on £70. due this day, £1..15.
- 3 Sold W. Tomlinson 1 piece super blue cloth, 36 yds. at 27s. 6d.—for Bill at one month.
- 3. W. Tomlinson paid me a *Bill* on Jones and Co. London, due May 10, £60. which should have been at one month.—Charged him discount, 10s.—Paid, agreeably to his order, the difference to J. Sims, in cash, £10.
- 3. Bought of J. Sanderson, cheese 25 cwt. 3 qrs. 17 lb. at £3..2..6. per cwt.—Paid his whole account in cash, £33. abatement 1s. 834. Accepted Allen, Wild, and Co.'s Bill at two months, drawn Jan 3, £80.
- 12. Received of Hazard and Jones's assignee, cash £2..7..24. for composition on £3..15..6. at 12s. 6d. in the £.

(183)

DAY-BOOK, (page 1.)

-				-
Folio of Ledger.	Inventory, January 1st, 1830.	£.	8.	đ.
Le	I have in Ready Money	1500	0	Q
	Bills Receivable, No. 1, on S. Johnson, due 29th instaut	24	3	9
	cwt. qr. lb.			
	Tea, 3 chests gross <i>ut.</i> 3 1 17 tare 0 2 7			
	Duty included on 2 3 10 at 6s. 2d. per lb.	98	ł	0
·	cwt. qr lb.			
	Raw Sugar, 2 hhds. weighing 27 3 18 neat, at £3148. per cwt.	104	4	Ð
	James Taylor owes me on bond, dated August 4th, 1826, with interest at £5. per cent. per			
1	annum -	70	0	0
1	I owe as follows :	1796	8	9
1	John Herdson, a balance of accounts	37	5	10
	Bernard Mason, for purchase of my house by auc- tion, to be paid 1st February next - £200 {	840	0	0
1	Duty on do. at $\pounds 5$. per cent. 40 § Bills payable, viz.: No. 1, W. Holmes's bill, to			ý
•	H. Williams or order, accepted by me, due 19th	45	10	0
2	instant			
1	5	932	15	10
	Allen, Wild, and Co., Leeds Cr.			
	†By 3 pieces superfine blue cloth, each 36 yds. at 25s. 6d. per yd.	137	14	0
	2 pieces narrow brown, 84 yds. at 4s. 9d. Wrappers	19 0	19	0 6
	Wrappers	[
2		157	18	6
•	Lernard Mason Dr.	1	2	2
	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	1	7	71
	3 3 yds blue cloth, at 28s	5	5	0
1		7	14	91

This column contains the figures of reference to the follo of the Ledger in which any account is posted. They should be antiten in red int.
† The preposition By is always parbefore any article for which a person is credited.
‡ The preposition To is generally placed before articles for which a person is debe, ed; but some Bookkoopers cruit 3.

R.C.

t, 9 pieces d 2 pieces Ib. green

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at £5,.7. ths' credit, £24..3..9. rs, for the

v soap, at ld do. at

ind 15 yds.

1b.--- st. . at 12 d.

6.

16. 1aw do. 123. abatement a ream of

b....6 lb. Received la, £4..13.

itement 5s.

e this day,

7s. 6d.-for

i, duo May d him die-J. Sims, in

at £3..2..6. nt 1s. 834

lrawn Jan

1. for com

	DAI-DOOK' (hage a.)			
	1830, Jan. 9.	£.		d .
	Samuel Fletcher Cr			
	cwt. qr. lb. £. s. d.			
	By Kent hops, 1 1 5 at 5 7 0 -	6	18	6
	Worcester do. 1 2 0 at 5 11 6	8	7	3
	Six months' credit, or £5. per cent. discount for			
2	present payment	15	5	9
• • • • • • •				
	Simmonds and Co., Liverpool Cr.		10	•
	By Yellow sonp, 2 cwt. at 76s	75	$\frac{12}{2}$	0
	4 doz, candies, at $8s$, $6d$ 4 doz , mould do. at $11s$, $3d$	0	$\frac{2}{5}$	0
	4 aoz. mound do. at 118. 5a			
2		14	19	0
	William Tomlinson Dr.			
	To narrow cloth, 7 yds. at 5s. 6d	1	18	· 6
	calico, $15 yds$. at $0s$. $8\frac{1}{2}d$.	Ō	10	73
•	canco, 10 gas. at 05. 034.			
2	19	2	9	15
•	Hazard and Jones Dr.			
	To 14 st. yellow soap, at 9d. per lb	0	15	9
	A st. mottled do. at 91d.	Ŏ	5	64
	9 lb. candles, at 9d	Ő	6	9
	3 12. moulds, at 1s. 01d	Ŏ	3	11
3		1	11	2
•	James Sanderson Cr.			
3	By goods as per Invoice*	7	3	6
	28			
	Hazard and Jones Dr.			
	To 171 lb. loaf sugar, at 1s. 1d	0	18	114
	12 <i>lb</i> . raw do. at 10 <i>d</i>	0	10	0
	14 lb. Congou tea, at 7s. 6d	0	9	43
	4 lb. Hyson, at 12s	0	6	0
3		2	4	4
•	John Herdson Dr.			
	To Hops, 10 lb. at 1s. 1d.	0	1.	10
	$\frac{1}{2}$ ream cap paper, at $7d$. per quire	0	5	10
	3 ream cap paper, at via per quite	i		
1	Feb. 1	5	16	8
-	William Tomlinson Dr.			
	To 2 st. yellow soap, at 9d. per lb	1	1	0
	6 <i>lb</i> . mould candles, at 1s. 1d	Ô	6	6
	16 lb. lump sugar, at 1s. 04d	Ö	16	8
2	ý l			2
		1 2	4	<u> </u>

DAY-BOOK, (page 2.)

* Many tradesmen keep an *Invoice Book*, into which all invoices of goods purchased are regularly transcribed. Some paste the invoices themselves within a blank book The account of Allen, Wild, and Co. (D. B., p. 1,) is supposed to be a copy from their invoice. Some make the *Invoice Book* serve also for the "Bought Ledger." This last method, when the nature of the trade will admit, is well worth adopting

184

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DAY-BOOK, (page 3.)

	1830, Feb. 4	£.	a. }	a.
1	James Taylor Dr. To half a year's interest on £70. at £5. per cent. per annum	1	15	0
3	William Tomlinson Dr. To 1 piece superfine blue cloth, 36 yds. at 27s. 6d. For bill at one month.	49	10	0
3	James Sanderson Cr. cwt. qr. b. £. s. d. By cheese* 25 3 17 at 3 2 6 per cwt. 10	80	18	2
2	Allen, Wild, and Co., Leeds Dr. To my acceptance of their Bill at 2 months, drawn 3rd Jan. B. P. Book. No. 2.	80	0	0
•	Oats' Purveyance, in Partnership with J. Herdson.† Dr. To Cash, for Oats purchased by me‡ Do. do by J. Herdson Do. for warehouse room, &c.	26 449 1	11 0 13	0 3 8
3	Cr.	477	4	11
	By Cash received for Oats sold by J. H.	507 55	9 2	2 8
3		562	11	10
3	L. s. d. Dr. To Profit, ½ (42135½) being my share J. H. ½ (42135½) being his share 12	85	6	11
	John Herdson Dr. To Cash advanced to him on Oats' concern Oats sold and received for by him	433 55	17 2	0 8
1	Cr.	488	19	8
	By Oats purchased by him - his share of profit	449 4 2	0 13	3 51
1		491	13	81
			•	• • •

* This is supposed to be bought by the long cwt. (120 lb.) agreeably to the general practice.

† Vide Example of a Partnership Concern, p. 187.

: In this concern, the entries of Cash are not made in the Cash-Book ; this being only a general statement of transactions supposed to have taken place before the opening of these books

ods purchased a blank book ppy from their r." This last ıg

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CASH-BOOK.

186

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INDEX TO THE LEDGER .

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composition on £3..15..6. at 12s. 6d. in the £. Loss £1..8..3§.

A Allen, Wild, and Co. 2	Ν
B Bills payable 2	O Oats' purveyanco - 3
С	Р
D	Q
Е	R
F' Fletcher Samuel - 2	S Stock 1 Simmonds and Co 2
G	Sanderson James - 3
Herdson John 1 Hazard and Jones - 3	T Taylor James 1 Tomlinson Wm 2
Į J	UV
K	W
L	ХҰ
M Mason Bernard - 1	Z

* The Ledger has an Alphabetical Index, showing, at one view, in what folio any person's account may be found.

EXAMPLE OF A PARTNERSHIP CONCERN.

John Herdson and I have been engaged in a joint concern as purveyors of oxis for the army. I have purchased oats for the joint stock to the amount of 220.11. H has paid, for oats purchased by him, $\pounds449..0.3$. I have received, for oats that have been disposed of, $\pounds507..9.2$; and my partner has received, from the same source, $\pounds55..2.8$. I have advanced to him, at different times, $\pounds433..17$; and have paid, for warehouse room and other sundry expenses, $\pounds1..13..8$. From these general heads, collected from the particulars recorded in the Granary Book, it is required to state the transactions.

It may, perhaps, be interesting to the learner to be informed that the above was a real occurrence; for an accurate statement of which the writer was some time since supplied to by the parties concerned.

88	LEDGE	n, (I	ollo 1	.)			
Int on	00	0	10	1 8	Til	0	
÷	15 0	15		13		0	
9 1621	1 70	71	37	491		840	
-	c. b. 1 ff0. 3		-	*m		н	
 LEDGER d. 1830 Contra By sundrie amount of property 13 10 14 property 18 0³/₂ 18 0³/₂ 18 0³/₂ 18 0³/₂ 19 property 10 property 11 property 12 property 13 property 14 property 14 property 15 property 16 property 17 property 18 property 18 property 19 property 18 property 18 property 18 property 10 property 11 property 11 property 12 property 13 property 14 property 14 property 14 property 14 property 15 property 16 property 16 property 17 property 18 property 18 property 19 property 10 property 10 property 11 property 11 property 12 property 13 property 14 property 15 property 16 property 16 property 18 property	1830 Contra Feb. 4 By Cash for interest - Balance -		1830 Contra an. 1 By 4 balance of accounts	Feb.12 By sundries, on Oats' con- ceru		1830 Contra Jan. 1 By purchase of house, and duty, due Feb. 1	
1830 Jan. 1	1330 Feb. 4		1830 Jan. 1	Feb.12		1830 Jan. 1	
	00	0	10	42	84	94 24	0
	0 15	15	IJ	16 17 17	13	14 5	0
4 60	70 1	11	37	483 1	491	7 832	640
1 ff0.3	- 0		c. b. 1	£0.3 ₩0.3		1 . b. 1	
Pr. Brudrice, amount of my ehts idance accound the Book. This account shore the Book. This account shore the Book. This account shore the heat a central bulance in taken, the heat to discover the value of bis at that this, and the gain or low at	1830 James Taylor Dr. au. 1 To money on bond - eb. 4 half a year's interest		1630 John Herdson Dr. an. 31 To cash £3756. abat. 4d. c. b. 1	To sundries Do. on Oats' concern Balance	_	1830 Bernard Mason Dr 1 an. 8 To sundries - 1 eb. 1 Cash £332. abat. 5s. 24d. c. b. 1	
(1) 1830 Stock 1830 Stock Feb. 12 D Mote 1 Note 1 1 cust in 1 cust in 1 cust in 1 cust in 1 cust in 1 cust	1830 . Jan. 1 Feb. 4		1830 . Jan. 31	Feb.12		1830 Jan. 8 Feb. 1	

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LEDGER (folio 2.)

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(2)- 1830 Jan. 19	Bills Payable Dr. To Cash	c.b.1 45	£.	s. 10	LEI d. 0	LEDGER: d. 1830 0 Jan. 1	GER: 1830 <i>Contra</i> Jan. 1 By Holmes's bill, No. 1	L. No. 1	1	\$\$:01	20	~
Feb.12	Ralance	ffo. 3	80	0	0	Feb.10	Feb.10 Allen, Wild, and Co.'s bill No. 2	Co.'s bill	h.b.1	03	0	0	
1830 Feb.10	Allen, Wild, & Co. Leeds, Dr. To Bills payable - Balance	3 ffo. 3		0 18	0	1830 Jan. 5	1830 <i>Contra</i> Jan. 5 By Cloth	. cr.	1	157	18	e	
			157	18	9								
1830 Jan. 9	1830 Samuel Fletcher Dr. an. 9 To Bill, and disc. on hops c. b. 1	c. b. 1	54	19	0	13:30 Jan. 9	Contra By Hops - Cr. Cheque on Smith & Co. c. b. 1	Cr. _ nith & Co.	c. b. 1	15 9	5 13	o. m	
										54	19	0	
Feb. 12	Simonds & Co. Liverpool, Dr. To Balance	ffo. 3	14	19	0	1830 Jan. 10	1830 <i>Contra</i> an. 10 By goods -	స ,	c:	14	19	0	
1830 Jan. 14 Feb. 1	William Tomlinson Dr. To goods	50 50	63 63	64	52	1830 Feb. 1	1830 Contra Feb. 1 By Cash Abatement	ి .	c '.']	40	13 0	0 34	• •
19 62	To Cloth Cash £10. Discount 10a. c. b. 1	c. b. 1	<u> </u>	E 5 1 2	178100	<u></u>	By 1621 -		ن. 1	•	0 13	10	
			99	c	•		-					T	

• When an account is palanced, a double line is drawn through the men ev columns, both ou the Dr. and Cr. sides of the Ledger : as in ¹ Here agreeum: above 0 0 640

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LEDSER, (folio 3.)

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GER. 1330 <i>Contra</i> feb.12 By cash for composition, c. b. 1 remainder lost c. b. 1		Contra Cr. By goods		Contra Cr. By sundries			BALANCE.	1830 Contra Cr. 1830 Contra Cr. By J. Herdson, I owe Bills Payable Allen, Wild and Co Simmonds and Co.
LEDGER. d. 1830 2 Feb.12 4		83 Jan. 23 Feb.10		1830 Feb.22				114 Feb.12 0
EE.	9	8		11	11	10		114 0
=	15	I		4	9	=		13 0
4-0	3	\$ 8		477	85	562		565 70
6 6		c. b. 1		~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~	ń			c. b. 1 565 ff0. 1 70
1830 Hazard and Jones Dr. 1830 Hazard and Jones Dr. 1910 - Sugar and tea	·	1830 James Sanderson Dr. feb.10 To cash £88. abat. 1s. 8§d. c. b.1		1830 Oats' Purveyance, in Co. with J. Herdson Dr. eb.12 To Sundries	Profit, 4 to self £421354 }		GENERAL	Balance Dr. To cash in hand • • James Taylor, owes me
1830 Jan. 19		1830 Feb.10		1830 Feb.12				1830 Feb.12

