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ADAMS'

NEW ARITHMETIC,

SUITED TO HALIFAX CURRENCY;

IN WHICH THE

PRINCIPLES OF OPERATING BY NUMBERS

ARE

ANALITICALLY EXPLAINED,

AND

SYNTHETICALLY APPLIED :

THUS COMBINING THE ADVANTAGES TO BE DERIVED BOTH FROM THE INDUCTIVE AND SYNTHETIC MODE OF INSTRUCTING :

THE WHOLE MADE FAMILIAR BY A GREAT VARIETY OF USEFUL AND INTERESTING EXAMPLES, CAUCULATED AT ONCE TO ENGAGE THE PUPIL IN THE STUDY, AND TO GIVE HIM A FULL KNOWLEDGE OF FIGURES IN THEIR APPLICATION TO ALL THE PRACTICAL PURPOSES OF LIFE.

DESIGNED FOR THE USE OF SCHOOLS & ACADEMIES IN THE BRITISH PROVINCES.

BY DANIEL, ADAMS, M. D.

SHERBROOKE, C. E. PUBLISHED BY WILLIAM BROOKS.

1849

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THERE are two mehods of teaching: the synthetic, and the analytic. In the synthetic method, the pupil is first presented with a general view of the science he is studying, and afterwards with the particulars of which it consists. The analytic method reverses this order : the pupil is first presented with the particulars, from which he is led, by certain natural and easy gradations, to those views which are more general and comprehensive.

The Scholar's Arithmetic published in 1801, is synthetic. If that is a fault of the work, it is a fault of the times in which it appeared. The analytic or inductive method of teaching, as now applied to elementary instruction, is among the improvements of later years. Its introduction is ascribed to PESTALOZ-ZI, a distinguished teacher in Switzerland. It has been applied to arithmetic, with great ingenuity, by Mr. ColBORN, in our own country.

The analytic is unquestionably the best method of acquiring knowledge; the synthetic is the best method of recapitulating or reviewing it. In a treatise designed for school education, both methods are useful. Such is the plan of the present undertaking which the author, occupied as he is with other objects and pursuits, would willingly have forborne, but that, the demand for the Scholar's Arithmetic still continuing; an obligation, incurred by long-continued and extended patronage, did not allow him to decline the labor of a revisal, which should adapt it to the present more enlightened views of teaching this science in our schools. In doing this, however, it has been necessary to make it a new work.

In the execution of this design, an analysis of each rule is first given, containing a familiar explanation of its various principles; after which follows a synthesis of these principles, with questions in form of a supplement. Nothing is taught dogmatically; no technical term is used till it has first been defined, nor any principle inculcated without a previous developement of its truth; and the pupil is made to understand the reason of each process as he proceeds.

The examples under each rule are mostly of a practical nature, beginning with those that are very easy, and gradually advancing to those more difficult, till one is introduced containing larger numbers, and which is not easily solved in the minds then in a plain, familiar manner, the pupil is shown how the solution may be facilitated by figures. In this way he is made to see at once their use and their application.

At the close of the fundamental rules, it has been thought advisable to collect into one clear view the distinguishing properties of those rules, and to give a number of examples involving one or more of them. These exercises will prepare the pupil more readily to understand the application of these to the succeeding rules; and besides, will serve to interest him in the science, since he will find himself able, by the application of a very few principles, to solve many curious questions.

The arrangement of the subjects is that, which to the author has appeared most natural. Fractions, have received all that consideration which their importance demands. The principles of a rule called Practice are exhibited, but its detail of cases omitted, as unnecessary, since the adoption and general use of federal money. The Rule of Three, or Proportion, is retained and the solution of questions involving the principles of proportion, by analysis, is distinctly shown.

The articles Alligation, Arithmetical and Geometrical Progression, Annuities and Permutation, were prepared by Mr. IRA Young, a member of Dattmouth College, from whose knowledge of the subject, and experience in teaching, I have derived important aid in other parts of the work.

The numerical paragraphs are chiefly for the purpose of reference; these references the pupil should not be allowed to neglect. His attention also ought to be particularly directed, by his instructor, to the illustration of each particular principle, from which general rules are deduced ; for this purpose, recitations by classes ought to be instituted in every school where arithmetic is taught.

The supplements to the rules, and the geometrical demonstrations of the extraction of the square and cube roots, are the only traits of the old work preserved in the new.

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DANIEL ADAMS.

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THE author of the following practical treatise upon Arithmetic, has made himself favourably known in the United States, and to a considerable extent in the Canadas, for a great number of years, by his works, designed for the use of Academies and primary schools. The "Scholars' Arithmetic," published in the year 1801, continued in almost universal use, until within a very short time past.-But juster views beginning to prevail, and sounder principles becoming established in the public mind, upon the subject of elementary education, a revision of the work seemed necessary. At this time, "Adams' New Arithmetic," was published. This seems evidently to have been prepared with much care. The author has recognised in it throughout, this important law in relation to the mind, that it must first be made acquainted with particular facts, or there will be no ability to arrive at correct general conclusions. Particular examples are therefore given upon each subject, and from them, in a manner obvious to the young mind, all the general rules are deduced. In other words, the author has carefully and prudently pursued, in his book, what is called the analytic method. The care used in defining necessary terms, which might not be quite clear, the practical character of the examples given under each rule, the methodical disposition of the different parts of each subject, and of the different subjects, the general perspicuity, simplicity and accuracy of the work, render it isvaluable to the pupil.

It is due the author to observe, that "Adams' New Arithmetic," for its adaptation to the capacities of young and ordinary minds, is justly considered the best practical reatise which has been offered to the public.

'In the present edition, the main purpose in view was to adapt Adams' work to the currency of the British Provinces. No separate article, as in the original, has been allotted to Federal Money; for this the pupil has been referred to Decimal Fractions, in which also almost all the examples will be found in the money of the United States. Adlitional examples in the compound rules have been given.

A 2

and the old ones retained, under the title of Halifax currency; and generally throughout the book, where denominitions of money occur, Halifax currency has been substituted for Federal money.

The rules and examples in Reduction of Currencies have been essentially changed i and in Reduction, after the Table of English Money, which is called the Table of Halifax Currency, a list of the Gold and Silver Coins current in the Province, has been inserted. This may be depended upon as entirely accurate. The tables of French, and Dry, Long, Square, and Solid Measure, have been given-and what are the weights and measures established by law in this Province is also stated.

The most novel feature in the book will be found in the rule of Interest. Certainly an innovation, but it is believed, an improvement, has been made. The pounds in any given sum upon which interest is to be cast, are left to stand as the units, and the shillings and pence are reduced to decimal parts of a pound. The interest is then obtained the same as in, Federal Money, and the decimal parts in the result feduced to shillings and pence. It is considered that this method is more simple and concise, and will be found in practice to be more convenient than any other .---But setting aside considerations of temporary convenience, if this change, and attempted amelioration, shall assist in some very slight degree in turning men's minds toward the Decimal Ratio, and inducing them to look forward to a period when all the denominations of money, weights, and measures, throughout the world, shall be expressed in DEC-IMALS, it cannot be affirmed that no benefit has been obtained.

The importance of the principal and essential alteration in the book, viz; the adaptation of it to the currency of the country, will not fail to be observed by every one. It is indeed singular, that hitherto, no *Canadian* Arithmetic in the English language, has been published. Mercantile, agricultural, and generally the business men of the country, will be aware of a benefit to be realized, and it is considered that something also bearing a relation to political advantage, may be in the result.

Sherbroake, L. C. June 6, 1849.

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<u>ARTTIMETO</u>

NUMERATION,

T 1. A SINGLE or individual thing is called a unit, unity or one; one and one more are called two; two and one more are called three, three and one more are called four; four and one more are called five; five and one more are called six; six and one more are called seven; seven and one more are called eight; eight and one more are called nine; nine and one more are called ten, &cc.

These terms, which are expressions for quantities, are called *numbers*. There are two methods of expressing numbers shorter than writing them out in words; one called the *Roman* method by letters,^{*} and the other the *Arabic* method by figures. The latter is that in general use.

In the Arabic method, the nine first numbers have each an appropriate character to represent them. Thus,

*In the Roman method by letters, I represents one, V five, X ten, L fifty, C one hundred, D five hundred, and M one thousand.

As often as any letter is repeated, so many times is its value repeated, unless it be a letter representing a less number, placed before one representing a greater, then, the less number is taken from the greater, thus IV represents four, IX nine, &c.gs will be seen in the followine TABLE :-

1	Ninety	LXXXX, or XC	
н	One hundred	C	
III	Two hundred	CC	
IIII, or IV	Three hundred	CCC	
V	Four hundred	CCCC	
VI	Five hundred	D, or In*	
VII	Six hundred	DC	
VIII	Seven hundred	DCC	
VIIII, or IX	Eight hundred	DCCC	
X	Nine hundred	DCCCC	
XX	One thousand	M, or Clot	
XXX	Five Thousand	100. or Vt_	
XXXX, or X	L Ten thousand	CCIDD, or X	
L	Fifty thousand	1000 -	
LX	Hundred thousand	CCCIDDD, or C	
LXX	One million	M	
LXXX	Two millions	MM	•
	I II III, or IV V VI VII VIII, or IX X X XXX XXX, or X L X LX LXX LXX	I Ninety II One hundred III Two hundred IIII, or IV Three hundred V Four hundred VI Five hundred VII Six hundred VII Six hundred VIII Seven hundred VIII Seven hundred VIII Seven hundred X Nine hundred X One thousand XXX Five Thousand XXX Five Thousand L Fifty thousand LX Hundred thousand LXX One million LXXX Two millions	I Ninety LXXXX, or XC II One hundred C III Two hundred CC IIII, or IV Three hundred CCC V Four hundred CCCC VI Five hundred DC VII Six hundred DC VIII Six hundred DCC VIII Seven hundred DCCC XX One thousand M, or Clot XXX Five Thousand Ioo, or V‡_ XXX Five Thousand CCloo, or X L Fifty thousand CCCloo, or X LX Hundred thousand CCCloo, or C LXX One million M

"I \mathcal{O} is used instead of D to represent five hundred, and for every additional \mathcal{O} annexed at the righ hand, the number is increased ten times. \mathcal{O} is used to represent one thousand, and for every C and \mathcal{O} put at each end; the number is increased ten times.

‡A line drawn over any number increases its value a thousand times.

88—107. 147—153.

154 151

166

203

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234 58

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87, 188. 201. 191—200.

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charact	er (1) as a	unit of the fi	rst or lower order	1. 185678
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nand, t	nat is, on the	ne lett hand	side of units; an	a
as, In t	nis case, ti	iere are no u	nits to be writte	n
with It	we write i	n the place of	units, a cipner, t	16
which	or itself sign	lines nothing	; thus, Len	10.
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Four "	1	Also the Par	Forty	40.
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Six "		86	Sixty	60.
Seven "		. 36	Seventy	70.
Eight "		CE SAL	Eightw	80.
Nine "	· · · · · · · · ·	19. 10 462 Will	Ninety	90.
l'en tens a	re called a	hundred, which	h forms a unit of	a still
higher orde	r. consisting	of hundreds.	represented by the	same
character (1) as a unit	of each of the	foregoing orders,	but is
written one	place furth	er toward the	left hand, that is	on the

left hand side of tens ; thus, ! - - one hundred 100.

Ten l

One hundred, one ten and one unit, are called that our One hundred and eleven 111.

In thi viz. u occup place numb exhibi der, o 3; bu ing fro thus, are six 6; but place q (sixty, by a si We ing dov then th then th tens, th three h three h

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figure th the first ond plac creased signifies is ten ti diately j a funda towards

order.

1, 2, 3,

¶ 2: There are three hundred sixty-five days in a year, In this number are contained all the orders now described. viz. units, tens, and hundreds. Let it be recollected, units. occupy the first place on the right hand; tens, the second place from the right hand ; hundreds, the third place. This number may pow be decomposed, that is, separated into parts, exhibiting each order by itself, as follows :--- The highest order, or hundreds, are three, represented by this character, 3; but, that it may be made to occupy the third place, counting from the right hand, it must be followed by two ciphers, thus, 300, (three hundred.) The next lower order, or tens, are six, (six tens are sixty,) represented by this character, 6; but, that it may occupy the second place, which is the place of tens, it must be followed by one cipher, thus 60, (sixty.) The lowest order, or units, are five, represented by a single character, thus, 5, (five.)

We may now combine all these parts together, first writing down the five units for the right hand figure, thus, 5; then the six tens (60) on the left hand of the units, thus 65; then the three hundreds (300) on the left hand of the six tens, thus, 365; which number, so written, may be read three hundred, six tens, and five units; or, as is more usual, three hundred and sixty-five.

¶ 3. Hence it appears, that figures have a different value according to the *place* they occupy, counting from the right hand towards the left.

Take for example the number 3 3 3, made by the same figure three times repeated. The 3 on the right hand, or in the first place, signifies 3 units; the same figure, in the secand place, signifies 3 tens, or thirty; its value is now increased tentimes. Again, the same figure in the third place, signifies neither 3 units, nor 3 tens, but 3 hundreds, which is ten times the value of the same figure in the place immediately preceding, that is, in the place of tens; and this is a fundamental law in notation, that a removal of one place towards the left increases the value of a figure TEN TIMES.

Ten hundred make a thousand, or a unit of the fourth order. Then follow tens and hundreds of thousands, in the

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NUMBERATION

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same manuer as tens and hundreds of units. To thousands succeed millions, billions, dec., to each of which, as to units and to thousands, are appropriated three places," as exhibited in the following examples : the standard an all the second

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To facilitate the reading of large numbers, it is frequently practised to point them off into periods of three figures each, as in the 2d example. The names and the order of the periods being known, this division enables us to read numbers consisting of many figures as easily as we can read three figures only. Thus, the above examples are read 3 (three) Quadrillions, 174 (one hundred seventy-four) Trillions, 592 (five hundred ninety-two) Billions, 837 (eight hundred thirty-seven) Millions, 463 (four hundred sixtythree) Thousands, 512 (five hundred and twelve.)

After the same manner are read the numbers contained in the following

"This is according to the French method of counting. The English, after hundreds of millions, instead of proceeding to billions, reckon thousands, tens and hundreds of thousands of millions, appropriating siz places, instead of three, to millions, billions, &c.

The table numbe perfec readily

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Note. followin them of 5 34 701 6539 The o is called in figure After foregoin lowing 1 1, S 2. E 3. I dred.) 4. E

NUMERATION.

NUMERATION TABLE.

Those words at the head of the table are applicable to any sum or number, and must be committed perfectly to memory, so as to be readily applied on any occasion.

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Of these characters, 1, 2, 3, 4, 5, 6, 7, 8, 9, 0, the nine first are sometimes called significant figures, or digits, in distinction from the last, which, of itself, is of no value, yet, placed at the right hand of another figure, it increases the value of that figure in the same ten fold proportion as if it had been followed by any one of the significant figures.

Note.	Should the	ne pupil	find a	ny difficult	ty in re	ading the
following	numbers,	let him	first (ranscribe	them,	and point.
them off	into perio	ds.				· -

5769	52831209	286297314013
34120	175264013	. 5203845761204
701602	3456720834	13478120673019
6539285	25037026531	341246801734526

The expressing of numbers, (as now shown,) by figures, is called Notation. The reading of any number set down in figures, is called Numeration.

After being able to read correctly all the numbers in the foregoing table, the pupil may proceed to express the following numbers by figures:

1. Seventy-six.

2. Eight hundred and seven.

3. Twelve hundred, (that is, one thousand and two hundred.)

4. Eighteen hundred.

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Hundreds of Millions. Tens of Millions. Millions. Hundreds of Thousands

Thousands

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¶ 3, 4.

5. Twenty-seven hundred and nineteen.

6. Forty-nine hundred and sixty.

7. Ninety-two thousand and forty-five.

- 8.- One hundred thousand.

9. Two millions, eighty thousands, and seven hundreds.

10. One hundred millions, one hundred thousand, one hundred and one.

11. Fifty-two millions, six thousand, and twenty.

12. Six billions, seven millions, eight thousand, and nine hundred.

13. Ninety-four billions, eighteen thousand, one hundred and seventeen.

14. One hundred thirty-two billions, two hundred millions, and nine.

15. Five trillions, sixty billions, twelve millions, and ten thousand.

16. Seven hundred trillions, eighty-six billions, and seven millions.

Addition of Simple Numbers.

¶ 4. 1. James had five peaches, his mother gave him 3 peaches more; how many peaches had he then?

2. John bought one book for 9 pence, and another for 6 pence; how many pence did he give for both?

3. Peter bought a wagon for 10 shillings, and sold it so as to gain 4 shillings; how many shillings did he get for it? 4. Frank gave 15 walnuts to one boy, 8 to another, and

had 7 left; how many walnuts had he at first?

5. A man bought a carriage for 54 pounds; he expended 8 pounds in repairs, and then sold it so as to gain 5 pounds; how many pounds did he get for the carriage?

6. A man bought 3 yoke of oxen; for the first he gave 16 pounds, for the second he gave 18 pounds, and for the third he gave 20 pounds; how many pounds did he give for the three?

7. Samuel bought an orange for four pence, and some walnuts for three pence; then he bought a knife for 1 shilling, and a book for 4 shilling; how many shillings did he spend, and how many pence?

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2+0 2-1 2+2 2-1-8 2+4 2+5 2+6 2+7 2-8 2+9

8. A man had 3 calves worth 10 shillings each, 4 calves worth 15 shillings each, and 7 calves worth 2 pounds each; how may calves had he?

9. A man sold a cow for 4 pounds, some corn for 5 pounds, wheat for 7 pounds, and butter for 2 pounds; how many pounds must he receive?

The putting together two or more numbers, (as in the foregoing examples,) so as to make one whole number, is called *Addition*, and the whole number is called the *sum*, or *amount*.

10. One man owes me 5 pounds, another 6 pounds, another 14 pounds, and another 3 pounds; what is the amount due to me?

11. What is the amount of 3, 7, 2, 4, 8, and 9 pounds? 12. In a certain school 9 study grammar, 15 study arithmetic, 20 attend to writing, and 12 study geography; what is the whole number of scholars?

SIGNS. A cross, +, one line horizontal and the other perpendicular, is the sign of addition. It shows that numbers, with this sign between them, are to be added together. It is sometimes read *plus*; which is a Latin word, signifying *more*.

Two parallell, horizontal lines, =, are the sign of equality. It signifies that the number *before* it is equal to the number *after* it. Thus, 5+3=8 is read 5 and 3 are 8; or, 5 plus (that is, more) 3 is equal to 8.

In this manner let the pupil be instructed to commit the following

ADDITION TABLE.

			r
2+0= 2	3+0=3	4+0=4	5+0= 5
2 + 1 = 3	3 + 1 = 4	4 + 1 = 5	5 + 1 = 6
2-2-4	3+2=5	4 + 2 = 6	5-2-7
2 - 3 = 5	3+3=6	4 + 3 = 7	5+3= 8
2-4= 6	3 + 4 = 7	4-4= 8	5-4= 9
2+5= 7	3+5=8	4+5=9	5+5=10
2+6=8	3+6=9	4 + 6 = 10	5 + 6 = 11
2+7=9	3+7=10	4 + 7 = 11	5+7=12
2+8=10	3 + 8 = 11	4 + 8 = 12	5 + 8 = 13
2+9=11	3 - 9 = 12	4 - 9 = 13	5-9-14
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5+9= how many? 8+7= how many? 4+3+2= how many? 6+4+5= how many? 2+0+4+6= how many? 7+8+0+8= how many? 9+3+3+4= how many? 8+2+8+3+5= how many? 5+7+6+1+8= how many? 3+9+7+0+5+6= how many? 4+1+0+4+4+5= how many? 2+5+2+3+7+3= how many?

¶ 5. When the numbers to be added are *small*, the addition is readily performed in the *mind*; but it will frequently be more convenient, and even necessary, to write the numbers down before adding them.

13. Harry had 43 books in his little library, his father gave him 25 volumes more; how many volumes had he then?

One of these numbers contains 4 tens and 3 units. The other number contains 2 tens and 5 units. To unite these two numbers together into one, write them down one under the other, placing the *units* of one number directly under *units* of the other, and the *tens* of one number directly under *tens* of the other, thus:

43 volumes. Having written the numbers in this 25 volumes. manner, draw a line underneath.

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Ans. 68 It nov 6 tens a 14. A horse for the whol Write units, ten

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Answer, After amples : 15. A basture, a he three 16. A nother 2 n the three 17. Bot o as to ga 25 + 150Hithert as not e ingle figu f a single res to exp 18. The

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43 volumes, We then begin at the right hand, and 25 volumes, add the 5 units of the lower number to the 3 units of the upper number, making 8 units, which we set down in unit's place. 111

We then proceed to the next column, 43 volumes, and add the 2 tens of the lower number 25 volumes, to the 4 tens of the upper number, making 6 tens, or 60, which we set down in

ten's place, and the work is done. Ans. 68 volumes. It now appears that Harry's whole number of volumes is 6 tens and 8 units, or 68 volumes; that is, 43+25=68.

14. A gentleman bought a carriage for 214 pounds, a horse for 30 pounds, and a saddle for 4 pounds; what was the whole amount?

Write the numbers as before directed, with units under units, tens under tens. &c.

OPERATION.

Carriage.	214 pounds,	Add as before. The units will
Horse,	30 pounds,	be 8, the tens 4, and the hundreds
Saddle,	4 pounds,	2, that is, 214+30+4=248.

Answer, 248 pounds.

After the same manner are performed the following examples:

15. A man had 15 sheep in one pasture, 20 in another pasture, and 143 in another; how many sheep had he in he three pastures? 15+20+143 = how many?

16. A man has three farms, one containing 500 acres, mother 213 acres, and another 76 acres; how many acres n the three farms? 500+213+76 how many?

17. Bought a farm for 625 pounds, and afterward sold it o as to gain 150 pounds; what did I sell the farm for ! 25 + 150 = how many?

Hitherto the amount of any one column, when added up, as not exceeded 9; consequently has been expressed by a ingle figure. But it will frequently happen that the amount f a single column will exceed 9, requiring two or more figres to express it.

18. There are three bags of money. The first contains B 2

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876 pounds, the second 653 pounds, the third 524 pounds; what is the amount contained in all the bags?

OPERATIO	DN.	
First bag,	876	
Second bag,	653	
Third bag,	524	
1		
Amount.	2053	

Writing down the numbers as already directed, we begin with the right hand, or unit column, and find the amount to be 13, that is, 3 units and 1 ten. Setting down the 3 units, or right hand figure, in unit's place, directly under the column,

we reserve the 1 ten, or left hand figure, to be added with the other tens, in the next column, saying, 1, which we reserved, to 2 makes 3, and 5 are 8, and 7 are 15, which is 5 units of its own order, and 1 unit of the next higher order, that is, 5 tens and 1 hundred. Setting down the 5 tens, or right hand figure, directly under the column of tens, we reserve the left hand figure, or 1 hundred, to be added in the column of hundreds, saying 1 to 5 is 6, and 6 are 12, and 8 are 20, which, being the last column, we set down the whole number, writing the 0, or right hand figure, directly under the column, and carrying forward the 2, or left hand figure, to the next place, or place of thousands. Wherefore we find the whole amount of money contained in the three bags to be 2053 pounds—the answer.

PROOF. We may reverse the order, and beginning at the top, add the figures downward. If the two results are alike the work is supposed to be right.

From the examples and illustrations now given, we de rive the following RULE.

I. Write the numbers to be added, one under another placing units under units, tens under tens, &c. and draw line underneath.

II. Begin at the right hand or unit column, and add to gether all the figures contained in that column; if th amount does not exceed 9, write it under the column; bu if the amount exceed 9, so that it shall require two or mor figures to express it, write down the unit figure only unde the column; the figure or figures to the left hand of unit being *tens*, are so many units of the next higher order which, being reserved, must be carried forward, and adde to the first figure in the next column.

III. Add each succeeding column in the same manne and set down the whole amount at the last column.

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EXAMPLES FOR PRACTICE.

19. A man bought four loads of hay; one load weighed 1817 pounds, another weighed 1950 pounds, another 2156 pounds, and another 2210 pounds; what was the amount of hay purchased?

20. A person owes A 100 pounds, B 522 pounds, C 785 pounds, D 92 pounds; what is the amount of his debts?

21. A farmer raised in one year 1200 bushels of wheat, 850 bushels of Indian corn, 1000 bushels of oats, 1086 bushels of barley, and 74 bushels of peas; what was the whole amount? Ans. 4210.

22. St. Paul's Cathedral, in London, cost 800,000 pounds sterling; the Royal Exchange 80,000 pounds; the Mansion-House 40,00 pounds; Black Friars Bridge 152,840 pounds; Westminster Bridge 389,000 pounds, and the Monument 13,000 pounds; what is the amount of these Ans. 1,474,840 pounds. sums?

23. If at the census in 1831, the population of the following counties was as follows :- Lower Canada: Gaspe, 4,171, Dorchester, 11,946; Nicolet, 12,504; Sherbrooke, 6,814; Stanstead, 8,272: Upper Canada: Gore, 23,552; Home, 32,871; Niagara, 21,974; London, 26180; Ottawa, 4,456; what was the whole number of inhabitants in these counties at that time? Ans. 152,740.

24. From the creation to the departure of the Israelites from Egypt was 2513 years; to the siege of Troy, 307 years more; to the building of Solomon's Temple, 180 years; to the building of Rome, 251 years; to the expulsion of the kings from Rome, 244 years; to the destruction of Carthage, 363 years; to the death of Julius Cesar, 102 years; to the Christian era 44 years; required the time from the creation to the Christian era. Ans. 4004 years. 25.

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SUPPLEMENT TO NUMERATION AND ADDITION. 15.

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29. What is the amount of 5674,3335, and 936 pounds? 30. A man has three orchards; in the first there are 140 trees that bear apples, and 64 trees that bear peaches; in the second, 234 trees bear apples, and 73 bear cherries; in the third, 47 trees bear plums, 36 bear pears, and 25 bear cherries; how many trees in all the orchards?

SUPPLEMENT

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TO NUMERATION AND ADDITION. QUESTIONS.

1. What is a single or indidividual thing called? 2. What is notation? 3. What are the methods of notation now in use? 4. How many are the Arabic characters or figures? 5. What is numerition? 6. What is a fundamental law in notation? 7. What is addition? 8. What is the rule for addition? 9. What is the result, or number sought, called? 10. What is the sign of addition? 11. ——of equality? 12. How is addition proved?

EXERCISES.

1. Washington was born in the year of our Lord 1732; he was 67 years old when he died; in what year of our Lord did he die?

2. The invasion of Greece by Xerxes, took place 481 years before Christ; how long ago is that this current year 1849? 3. There are two numbers, the less number is 8671, the difference between the numbers is 597; what is the greater number?

4. A man borrowed a sum of money, and paid in part 684 pounds; the sum left unpaid was 876 pounds, what was the sum borrowed?

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SUBTRACTION OF SIMPLE NUMBES.

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aid in part , what was 5. There are four numbers, the first 317, the second 812, the third 1350, and the fourth as much as the other three; what is the sum of them all?

6. A gentleman left his daughter 16 thousand, 16 hunired and 16 pounds; he left his son 1800 more than his laughter; what was his son's portion, and what was the mount of the whole estate? Ans. { Son's portion, 19,416. Whole estate.37,032.

7. A man, at his death, left his estate to his four chiliren, who, after paying debts to the amount of 1476 pounds, ecceived 4768 pounds each; how much was the whole esate? Ans. 20548.

8. A man bought four hogs, each weighing 375 pounds; now much did they all weigh? Ans. 1500.

9. The fore quarters of an ox weigh one hundred and ight pounds each, the hind quarters weigh one hundred ind twenty-four pounds each, the hide seventy-six pounds, ind the tallow sixty pounds; what is the whole weight of he ox? Ans. 600.

10. A man, being asked his age, said he was thirty-four tears old when his eldest son was born, who was then fifeen years of age; what was the age of the father?

11. A man sold two cows for five pounds each, twenty we ushels of corn for three pounds, and one hundred pounds f tallow for two pounds; what was his due?

Subtraction of Simple Numbers.

1 6. 1. Charles, having 11 pence, bought a book, for hich he gave 5 pence; how many pence had he left? **2.** John had 12 apples; he gave 5 of them to his brother; pw many had he left?

3. Peter played at marbles; he had 23 when he began, at when he had done he had only 12; how many did he se? 4. A man bought an article for 17 shillings and sold it again for 22 shillings; how many shillings did he gain?

5. Charles is 9 years old, and Andrew is 13; what is the difference in their ages?

6. A man borrowed 50 pounds, and paid all but 18; how many pounds did he pay? that is, take 18 from 50, and how many would there be left?

7. John bought several articles for 19 shillings; he gave for 4 books 6 shillings; what did the other articles cost him?

8. Peter bought a trunk for 17 shillings, and sold it for 22 shillings; how many shillings did he gain by the bargain?

9. Peter sold a wagon for 22 shillings, which was 5 shillings more than he gave for it; how many shillings did he give for the wagon?

10. A boy, being asked how old he was, said that he was 25 years younger than his father, whose age was 33 years; how old was the boy?

The taking of a less number from a greater (as in the foregoing examples) is called Subtraction. The greater number is called the *minuend*, the less number the subtrahend, and what is left after subtraction, is called the *difference* or *remainder*.

11. If the minuend be 8, and the subtrahend be 3, what is the remainder?

12. If the subtrahend be 4, and the minuend 16, what is the remainder?

13. Samuel bought a book for 11 pence; he paid down 4 pence; how many pence more must he pay?

SIGN. A short horizontal line, —, is the sign of subtraction. It is usually read minus, which is a Latin word signifying less. It shows that the number after it is to be taken from the number before it. Thus, 8—3—5, is read 8 minus or less 3 is equal to 5; or 3 from 8 leaves 5. The latter expression is to be used by the pupil in committing the following

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SUBTRACTION OF SIMPLE NUMBERS.

SUBTRACTION TABLE.



¶ 7. When the numbers are *small*, as in the foregoing examples, the taking of a less number from a greater, is readily done in the *mind*; but when the numbers are *large*, the operation is most easily performed part at a time, and therefore it is necessary to *write* the numbers down before performing the operation.

14. A farmer having a flock of 237 sheep, lost 114 of them by disease; how many had he left?

Here we have 4 units to be taken from 7 units, 1 ten to be taken from 3 tens, and 1 hundred to be taken from 2 hundreds. It will therefore be most convenient to write the less number under the greater, observing, as in addition, to place units under units, tens under tens, &cc., thus:

OPERATION. From 237, the minuend, Take 114, the subtrahend,

123

We now begin with the units, saying, 4(units) from 7 (units,) and there remain 3 (units,) which we set down directly under the column in unit's place.—

Then, proceeding to the next column we say 1 ten from 3 (tens,) and there remain 2 (tens,) which we set down in *ten's* place. Proceeding to the next column, we say, 1 (hundred) from 2 (hundreds,) and there remains 1, (hundred,) which we set down in *hundred's* place, and the work is done. It now appears, that the number of sheep left was 123: that is, 237-114=123.

After the same manner are performed the following examples:

15. There are two farms; one is valued at 973 pounds, and the other at 421 pounds; what is the difference in the value of the two farms?

16. A man's property is worth 2170 pounds, but he has debts to the amount of 1110 pounds; what will remain after paying his debts?

17. James having 15 shillings bought a book for which he gave 7 shillings ; how many shillings had he left?

OPERATION.

15 shillings.7 shillings.

A difficulty presents itself here; for we cannot take 7 from 5; but we can take 7 from 15, and there will remain 8.

8 shillings left.

18 A man bought several articles for 85 pounds, and other articles for 27 pounds; what did the former cost him more than the latter?

OPERATION. The same difficulty meets us here as in *First articles*, 85 the last example; we cannot take 7 from *Other articles*, 27 5; but in the last example the larger num

— ber consisted of 1 ten and 5 units, which **Difference**, 58 together make 15; we therefore took 7 from 15. Here we have 8 tens and 5 units. We can now in the mind, suppose 1 ten taken from the 8 tens, which would leave 7 tens, and this 1 ten we can suppose joined to the 5 units, making 15. We can now take 7 from 15, as before, and there will remain 8, which we set down. The taking of 1 ten out of 8 tens, and joining it with the 5 units is called *borrowing ten*. Proceeding to the next higher or der, or fens, we must consider the upper figure 8, from which we borrowed, 1 less, calling it seven; then, taking 2 (tens from 7 (tens) there will remain five (tens,) which we set down, making the difference 58. Or, instead of making the

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us here as in take 7 from e larger numunits, which refore took 7 We can now. tens, which ose joined to from 15, as The down. h the 5 units xt higher or 8, from which king 2 (tens which we se of making th

¶ 7,8. SUBTRACTION OF SIMPLE NUMBERS.

ing the upper figure, 1 less, calling it 7, we may make the *lower* figure 1 more, calling it 3, and the result will be the same; for 3 from 8 leaves 5, the same as 2 from 7.

19. A man borrowed 713 pounds, and paid 471 pounds; how many pounds did he then owe? 713 - 471 = how many? Ans. 242 pounds.

20. 1612-465=how many !

Ans. 1147. Ans. 36969.

21. 43751—6782—how many ?

 \P 8. The pupil will readily perceive, that subtraction is the reverse of addition.

22. A man bought 40 sheep, and sold 18 of them; how many had he left? 40-18=how many? Ans. 22 sheep.

23. A man sold 18 sheep, and had 22 left; how many had he at first? 18 + 22 = how many?

24. A man bought some articles for 75 pounds, and others for 16 pounds; what was the difference of costs?

75-16=how many? Reversed, 59+16=how many?

25. 114-103 == how many? Reversed, 11+103 == how many?

27. 143—76 = how many? Reversed, 67+76 = how many?

Hence, subtraction may be proved by addition, as in the foregoing examples, and addition by subtraction.

To prove subtraction, we may add the remainder to the subtrahend, and, if the work is correct, the amount will be equal to the minuend.

To prove addition, we may subtract, successively, from the amount, the several numbers which were added to produce it, and if the work is right, there will be no remainder. Thus 7+8+6=21; proof, 21-6=15, and 15-8=7, and 7-7=0.

From the remarks and illustrations now given, we deduce the following

RULE.

1. Write down the numbers, the less under the greater, placing units under units, tens under tens, &c., and draw a line under them.

II. Beginning with units, take successively each figure in the *lower* number from the figure *over* it, and write the remainder directly below.

III. When the figure in the lower number exceeds the figare over it, suppose 10 to be added to the upper figure; but in this case we must add 1 to the *lower* figure in the next column before subtracting. This is called borrowing 10.

EXAMPLES FOR PRACTICE.

27. If a farm and the buildings on it, be valued at 3000 pounds, and the buildings alone be valued at 1500 pounds, what is the value of the land?

28. The population of Lower Canada, at the last census, was 690782, at the census previous the census was 511917; what was the difference in the two enumerations?

29. What is the difference between 7,748,203 and 928,671?

30. Now much must you add to 358,642 to make 1,487,945?

31. A man bought an estate for 3798 pounds, and sold it for 4137 pounsd; did he gain or lose by it? and how much?

32. From 354,931,347,543 take 27,412,507,543.

33. From 824,264,213,909 take 631,245,653,356.

34. From 127,245,775,075,635 take 978,567,076,256.

SUPPLEMENT TO SUBTRACTION.

QUESTIONS.

1. What is subtraction? 1. What is the greater number called? 3. — the less number? 4. What is the result or answer called? 5. What is the sign of subtraction? 6. What is the rule? 7. What is understood by borrowing ten? 8. Of what is subtraction the reverse? 9. How is subtraction proved? 10. How is addition proved by subtraction?

FXERCISES.

1: How long from the discovery of America by Columbus, in 1492, to the period of the cession by France of all her possessions in North America to Great Britain in 1763?

2. Supposing a man to have been born in the year 1773, how old was he in 1848?

3. Supposing a man to have been 105 years old in the year id-23, in what year was he born?

4. There are two numbers, whose difference is \$764; the greater number is 15687; I demand the less?

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SUPPLEMENT TO SUBTRACTION.

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88:64; the

5. What number is that which taken from 3794, leaves 865?

6. What number is that to which if you add 789, it will become 6350?

7. In a certain city, there were 123707 inhabitants; in another 43,940; how many more inhabitants were there in one than in the other?

8. A man possessing an estate of twelve thousand pounds, gave two thousand five hundred pounds to each of his two daughters, and the remainder to his son; what was his son's share?

9. From seventeen million take fifty-six thousand, and what will remain?

10. What number, together with these three, viz. 1301, 2561, and 3120, will make ten thousand?

11. A man bought a horse for 35 pounds, and a chaise for 47 pounds; how much more did he give for the chaise than for the horse?

12. A man borrows 7 ten dollar bills, and three one dollar bills, and pays at one time 4 ten dollar bills and 5 one dollar bills; how many ten dollar bills and one dollar bills must he afterwards pay to cancel the debt?

Ans. 2 ten doll. bills and 8 one dol. 13. The greater of two numbers is 24, and the less is 16; what is the difference?

14. The greater of two numbers is 24, and their difference 8; what is the less number?

15. The sum of two numbers is 40, the less is 16; what is the greater?

16. A tree 68 feet high, was broken off by the wind; the top part which fell was 49 feet long; how high was the stump which was left?

17. Elizabeth became Queen of England in 1558; how many years since?

18. A man carried his produce to market; he sold his pork for 14 pounds, his cheese for 11 pounds, and his butter for 9 pounds; he received, in pay, salt to the value of \emptyset pounds, 3 pounds worth of sugar, two pounds worth of molasses, and the rest in money; how much money did he receive? Ans. 23 pounds.

19. A boy bought several sleds for 13 shillings, and gave 6 shillings to have them repaired; he sold them for 18 shill-

¶ 8.`

1 8.

ings; did he gain or lose by the bargain? and how much? 20. One man travels 67 miles in a day, another man follows at the "rate of 42 miles in a day; if they both start from the same place at the same time, how far will they be apart at the close of the first day? — of the second? of the third? — of the fourth?

21. One man starts from Toronto Monday morning, and travels at the rate of 40 miles a day; another starts from the same place Tuesday morning, and follows at the rate of 70 miles a day; how far are they apart Tuesday night? Ans. 10 miles.

22. A man owing 379 pounds, paid at one time 47 pounds, at another time, 84 pounds, at another time, 27 pounds, and at another 143 pounds; how much did he then owe?

Ans. 82 pounds.

23. A man has property to the amount of 34764 pounds, but there are demands against him to the amount of 14297 pounds; how many pounds will be left after the payment of his debts?

24. Four men bought a lot of land for 482 pounds; the first man paid 274 pound, the second man 194 pounds less than the first, and the third man 20 pounds less than the second; how much did the second, third, and the fourth man pay?

Ans. { Th

The third paid 60. The fourth paid 68.

35

25. A man, having 10,000 pounds, gave away 9 pounds; how many had he left? Ans. 9991.

Multiplication of Simple Numbers.

¶ 9. 1. If one orange cost 2 pence, how many pence must I give for 2 oranges? — how many pence for 3 oranges? — for 4 oranges?

2. One bushel of apples cost 3 shillings; how many shillings must I give for 2 bushels? —— for 3 bushels?

3. One gallon contains 4' quarts; how many quarts in 2 gallons? — in 3 gallons? — in 4 gallons?

4. Three men bought a horse; each man paid 6 pounds

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for his share; how many pounds did the horse cost them? 5. A man has 4 farms worth 95 pounds each; how many pounds are they all worth?

6. In one pound there are 20 shillings; how many shillings in 5 pounds?

7. How much will 4 pair of shoes cost at 9 shillings a pair?

8. How much will 3 pounds of tea cost at 5 shillings a pound?

9. There are 24 hours in 1 day; how many hours in 2 days? — in 3 days? — in 4 days? — in 7 days?

10. Six boys met a beggar and gave him 9 pence each; how many pence did the beggar receive?

When questions occur, (as in the above examples,) where the same number is to be added to itself several times, the operation may be facilitated by a rule, called *Multiplication*, in which the number to be repeated is called the *multiplicand*, and the number which shows how *many times* the multiplicand is to be repeated is called the *multiplier*. The multiplicand and multiplier, when spoken of *collectively* are called the *factors*, (producers,) and the answer is called the *product*.

11. There is an orchard in which there are 5 rows of trees and 27 trees in each row; how many trees in the orchard?

In the	first r	ow,	27 t	rees.
"	second	"	27	"
**	third	"	27	"
44	fourth	"	27	"
**	fifth	"	27	**

In this example, it is evident that the whole number of trees will be equal to the amount of *five* 27's added together. In adding, we find that 7 taken five times

In the orchard 135 trees. amounts to 35. We write down the five units, and reserve the 3 tens; the amount of 2 taken five times is 10, and the 3, which we reserved, makes 13, which, written to the left of units, makes the whole number of trees 135.

If we have learned that 7 taken 5 times amounts to 35, and that 2 taken 5 times amounts to 10, it is plain we need write the number 27 but once, and then, setting the multiplier under it, we may say, 5 times 7 are 35, writing down

MULTIPLICATION OF SIMPLE NUMBERS. ¶ 9, 10.

the 5, and reserving the 3 (tens) as in addition. Again 5 *Multiplicand*, 27 trees in each row. *Multiplier*, 5 rows. (tens,) which we reserved, make 13,

Product, 135 trees, Ans.

¶ 10. 12. There are on a board 3 rows of spots, and 4 spots in each row; how many spots on the board?

* * * * * * * * * * * *

30

A slight inspection of the figure will show that the number of spots may be found either by taking 4 three times, (3 times 4 are 12,) or by taking 3 four times, (4 times 3 are 12;) for we may say there

(tens,) as before.

are three rows of 4 spots each, or 4 rows of 3 spots each; therefore, we may use either of the given numbers for a multiplier, as best suits our convenience. We generally write the numbers as in subtraction, the larger number uppermost, with units under units, tens under tens, &c. Thus, *Multiplicand*, 4 spots. Note. 4 and 3 are the factors, *Multiplier*, 3 rows. which produce the product 12.

Product, 12 Ans.

Hence,—Multiplication is a short way of performing many additions; in other words—It is the method of repeating any number any given number of times.

SIGNS. Two short lines crossing each other in the form of the letter X, are the sign of multiplication. Thus, 3×4 =12, signifies that 3 times 4 are equal to 12, or 4 times 3 are 12.

Note. Before any progress can be made in this rule, the following table must be committed perfectly to memory.

¶ 10.

 $\begin{array}{c} 2 \times 0 \\ 2 \times 1 \\ 2 \times 2 \end{array}$

 2×3

 2×4 2×5

 2×6 2×7

 $\begin{array}{c} 2 \times 8 \\ 2 \times 9 \end{array}$

 2×10

 2×11

 2×12

 3×0

 3×1

 3×2

 3×3

 3×4

 3×5 3×6

 3×7 3×8

 3×9

 3×10

 3×11 3×12

 4×0

 4×1

 4×2 4×3

 4×4

MULTICATION TABLE.

Again 5 (tens) are s,) and 3, which we l, make 13, is before.

¶ 9, 10.

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bots, and 4 ? figure will ots may be be times, (3 four times, y say there pots each; abers for a e generally number up-&c. Thus, the factors, roduct 12.

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in the form Thus, 3×4 r 4 times 3

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2	X	0	=	0	4	X	10	=	40	7	×	7=	49	10	×	4=	4)
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2	X	3	=	6	5	X	0	=	0	7	Х	10 =	70	10	×	7 =	71)
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3	Х	0	=	0	5	Х	10	==	50	8	×	7=	56	11	Х	4=,	4	1
3	Х	1	=	3	5	Х	11	=	55	8	X	8==	64	11	X	5 =	5	5
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0	X	11 10	=	00 96	6	×	8	=	48	9	"	5=	45	12	"	2=	2	1
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4	Х	3	==	12	7	×	0	==	0	9		10 =	90	12	••	7=	2	1
4	×	4		16	7	×	1	_	7	9		11=	99	12		8=	104	0
4	Х	5	_	20	7	×	2	-	14	9		12=	108	12		y==	10	5
4	×	6	==	24	7	×	3	=	21	10)**	0=	0	12		10 = 11 = 11	124	0
11	X	7	=	28	7	"	4	=	28	10)''	1=	10	12		11 = 10 = 10 = 10	15	4
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9X2 how many?	4 X 3 X 2 -24.																	
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4 X 6 = how many?	3X2X5 how many !																	
8X9=how many?	$7 \times 1 \times 2 = how many?$																	
8 X 7'-how many?	8X3X2-how many?																	
X5=how many?	$3X_2X_4X_5$ = how many																	

13. What will 84 barrels of flour cost at 2 pounds a barrel? Ans. 168 pounds.

14. A merchant bought 12 dozen hats at the rate of 12 pounds per dozen; what did they cost? Ans. 144 pounds.

How many inches are there in 253 feet, every foot being 12 inches?

QPERATION. The product of 12, with each of the signifi-253cant figures or digits, having been committed

12 to memory from the multiplication table, it is just as easy to multiply by 12 as by a single

Ans. 3036 figure. Thus, 12 times 3 are 36, &c.

16. What will 476 barrels of fish cost at 3 pounds a barrel? Ans. 1428 pounds.

17. A piece of very valuable land, containing 33 acres. was sold for 246 pounds an acre; what did the whole come to ?

As 12 is the largest number, the product of which, with the nine digits, is found in the multiplication table, therefore, when the multiplier exceeds 12, we multiply by each figure in the multiplier separately. Thus:

OPERATION.

246 pounds, the price of one acre." **33** number of acres.

738 pounds, the price of three acres, 738 pounds, the price of thirty acres,

er consists of **3** tens and 3 units. First, multiplying by the **3** units gives us

Ans. 8118 pounds, the price of 33 acres. 738 pounds the price of 3 acres. We then multiply by the 3 tens, writing the first figure of the product (8) in ten's place, that is, directly under the figure by which we multiply. It now appears that the product by the 3 tens consists of the same figures as the product by the 3 units; but there is this differencethe figures in the product by the 3 tens are all removed one place further to the left hand, by which their value is increased tenfold, which is as it should be, because the price

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III. figure s remem duct d Having the mu sum of

18. 7 there in 19. 8 how m **20**. 1 chest? 21. 1 pounds 22. in an h rate? h year, or 23. 1 contain were th

> **24**. I 25. 26.

of 30 acres is evidently ten times as much as the price of 3 acres, that is, 70380 pounds; and it is plain that them two products, added together, give the price of 33 acres.

These examples will be sufficient to establish the following

RULE.

I. Write down the multiplicand, under which write the multiplier, placing units under units, tens under tens, &c., and draw a line underneath.

II. When the multiplier does not exceed 12, begin at the right hand of the multiplicand, and multiply each figure contained in it by the multiplier, setting down and carrying the same as in addition.

III. When the multiplier exceeds 12, multiply by each figure separately, first by the units, then by the tens, &c., remembering always to place the first figure of each product directly under the figure by which you multiply. Having gone through in this manner with each figure in the multiplier, add their several products together, and the sum of them will be the product required.

EXAMPLES FOR PRACTICE.

18. There are 320 rods in a mile; how many rods are there in 57 miles?

19. Suppose it to be 706 miles from Halifax to Quebec; how many rods is it?

20. What will 784 chests of tea cost, at 17 pounds a chest?

21. If 1851 men receive 758 pounds apiece; how many pounds will they all receive? Ans. 1403058 pounds.

22. There are 24 hours in a day; if a ship sail 7 miles in an hour, how many miles will she sail in 1 day, at that rate? how many miles in 36 days? how many miles in 1 year, or 365 days? Ans. 61329 miles in 1 year.

23. A merchant bought 13 pieces of cloth, each piece containing 28 yards, at 2 pounds a yard; how many yards were there, and what was the whole cost?

		An	s. The	whole cost was	728 pounds.
24 .	Multiply	37864 b	v 235.	Product.	8898040.
25.	"	29831 '	⁴ 952.	"	28399112.
26,	"	93956	* 8704.	16	817793024

inds a bar-68 pounds. rate of 12 44 pounds. foot being

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CONTRACTIONS IN MULTIPLICATION.

1. When the multiplier is a composite number.

¶ 11. Any number, which may be produced by the multiplication of two or more numbers, is called a *compos*-Thus, 15, which arises from the multiplicaite number. tion of 5 and 3, $(5 \times 3 = 15)$ is a composite number, and the numbers 5 and 3, which, multiplied together, produce it, are called component parts, or factors, of that number. So, also, 24 is a composite number; its component parts, or factors may be 2 and 12, $(2 \times 12 = 24;)$ or they may be 4 and 6, $(4 \times 6 = 24;)$ or they may be 2, 3, and 4. (2×3) $\times 4 = 24.)$

1. What will 15 pieces of cloth cost, at 4 pounds a piece? 15 pieces are equal to 5×3 pieces. The cost of 5 pieces would be $5 \times 4 = 20$ pounds; and be-4 5 cause 15 pieces contains 3 times 5 pieces, so the

cost of 15 pieces will evidently be 3 times the 20 cost of 5 pieces, that is, 20 pounds $\times 3 = 60$ pounds. 3 Ans. 60 pounds.

60

Wherefore, If the multiplier be a composite number, we may, if we please, multiply the multiplicand first by one of the component parts; that product by the other, and so on, if the component parts be more than two; and, having in this way multiplied by each of the component parts, the last product will be the product *required*.

2. What will 136 tons of potashes come to, at 24 pounds per ton?

 $6 \times 4 = 24$. It follows, therefore, that 6 and 4 are component parts or factors of 24. Hence,

136 tons.

6 one of the component parts, or factors.

816 pounds, the price of 6 tons.

4 the other component part, or factor.

Ans. 3264 pounds, the price of 136 tons.

3. Supposing **342** men to be employed in a certain piece of work, for which they are to receive 28 pounds, each, how much will they all receive?

 $7 \times 4 = 28$

Ans. 9576 pounds.

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24 pounds

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tain piece hds, each,

76 pounds.

12, 13. CONTRACTIONS IN MULTIPLICATION.

4.	Multiply	367	by 48.	Product,	17616.
5.	"	853	" 56.	**	47768.
6.,	· ···· / · · ·	1086	1 72.	1 4 44	78192

11. When the multiplier is 10, 100, 1000, &c...

¶ 12. It will be recollected, (¶ 3.) that any figure, on being removed one place towards the left hand, has its value increased tenfold; hence, to multiply any number by 10 it is only necessary to write a cipher on the right hand of it. Thus, 10 times 25 are 250; for the 5, which was units before, is now made tens, and the 2 which was tens before, is now made hundreds. So, also, if any figure be removed two places towards the left hand, its value is increased 100 times, &c. Hence,

When the multiplier is 10, 100, 1000, or 1 with any number of ciphers annexed, annex as many ciphers to the multiplicand as there are ciphers in the multiplier, and the multiplicand, so increased, will be the propuet required. Thus,

Multiply	46 by	10, t	he product	is	460
	83 by	100,		6-	8300
• 6	95 by	1000,	". –	1	95000

EXAMPLES FOR PRACTICE.

1. What will 76 loads of corn cost at 10 pounds a load?

2. If 100 men receive 32 pounds each, how many pounds will they all receive?

3. What will 1000 pieces of broadcloth cost, estimating each piece at 78 pounds?

4. Multiply 5682 by 10000.

5. "** 82134 ** 100000.

¶ 13. On the principle suggested in the last ¶, it follows,

When there are ciphers on the right hand of the multiplicand, multiplier, either or both, we may at first neglect these ciphers, multiplying by the significant figures only; after which we must annex as many ciphers to the product as there are ciphers on the right hand of the multiplicand and multiplier, counted together.

EXAMPLES FOR PRACTICE.

1. If 1300 men receive 460 pounds apiece, how many pounds will they all receive?

PERATION.	The ciphers in the multiplicand
460	and multiplier, counted together,
1300	are three. Disregarding these, we
×	write the significant figures of the
138	multiplier under the significant fig-
46	ures of the multiplicand, and mul-
、	tiply; after which we annex three
EDODOD - and	a sinhang to the night hand of the

Ans. 598000 pounds. ciphers to the right hand of the product, which gives the true answer.

2. The number of distinct buildings in New England, appropriated to the spinning, weaving, and printing of cotton goods, was estimated, in 1826, at 400, running, on an average, 700 spindles each; what was the whole number of spindles?

3.	Multiply	257	by	63000.
4.		8600	"	17.
5.	"	9340	"	460.
6.	"	5200	"	410.
7.	"	378	""	204.

OPERATION.

378
204
• .0

In the operation it will be seen, that multiplying by ciphers produces nothing. Therefore,

756 _____ 77112

III. When there are ciphers between the significant figeres of the multiplier, we may omit the ciphers, multiplying by the significant figures only, placing the first figure of each product directly under the figure by which we multiply.

EXAMPLES FOR PRACTICE.

8. Multiply 154326 by 3007.

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0 13. SUPPLEMENT TO MULTIPLICATION. 37 1 13 2 111 1 1. OPERATION. 11111 154326 how many I. 3007 111 in der ultiplicand 1080282 A 81.68 6 10 together, 462978 these, we ures of the 1111111 Product, 464058282 ificant fig-543 by 206. 9. Multiply , and mul-1 66 1620 . 2103. 10. nnex three 36243 " 32004. 11. 11. 1. nd of the

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nificant figs, multiplyfirst figure ich we mul-

SUPPLEMENT TO MULTIPLICATION.

QUESTIONS.

1. What is multiplication? 2. What is the number to be multiplied called? 3. — to multiply by called? 4. What is the result or answer called? 5. Taken collectively, what are the multiplicand and multiplier called? 7. What is the sign of multiplication? 7. What does it show? 8. In what order must the given numbers be placed for multiplication? 6. How do you proceed when the multiplier is less than 12? 10. When it exceeds 12, what is the method of procedure? 11. What is a composite number? 12. What is to be understood by the component parts, or factors, of any number? 13. How may you proceed, when the multiplier is a composite number? 14. To multiply by 10, 100, 1000, &c., what suffices? 15. Why? 16. When there are ciphers on the right hand of the multiplicand, multiplier, either or both, how may we proceed? 17. When there are ciphers between the significant figures of the multiplier, how are they to be treated?

EXERCISES.

1. An army of 10700 men having plundered a city, took so much money, that, when it was shared among them, each man received 46 pounds; what was the sum of money taken? 2. Supposing the number of houses in a certain town to

be 145, each house, on an average, containing two families, and each family 6 members, what would be the number of nhabitants in that town?

3. If 46 men. can do a piece of work in 60 days, how many men will it take to do it in one day?

4 Two men depart from the same place, and travel in opposite directions, one at the rate of 27 miles a day, the other 31 miles a day; how far apart will they be at the end of 6 days? Ans. 348 miles.

5 What number is that, the factors of which are 4, 7, 6, and 20? Ans. 3360.

6. If 18 men can do a piece of work in 90 days, how long will it take one man to do the same?

7. What sum of money must be divided between 27 men, so that each man may receive 115 pounds?

8. There is a certain number, the factors of which are 89 and 265; what is that number?

9. What is that number, of which 9, 12, and 14 are factors?

10. If a carriage wheel turn round 346 times in running 1 mile, how many times will it turn round in the distance from Quebec to Montreal it being 180 miles.

Ans. 62280.

1 13.

11. In one minute are 60 seconds; how many seconds, in 4 minutes? — in 5 minutes? — in 20 minutes? — in 40 minutes?

13. In one pound are 4 dollars; how many dollars in 3 pounds? —— in 300 pounds? —— in 467 pounds?

14. Two men, A and B, start from the same place at the same time, and travel the same way; A travels 52 miles a day, and B 44 miles a day; how far apart will they be at the end of 10 days?

15. If the interest of 100 pounds, for one year, be six pounds, how many pounds will be the interest for 2 years?

_____ for 4 years ? _____ for 10 years ? _____ for 35 years ? _____ for 84 years ?

16. If the interest of one hundred pounds, for one year, be six pounds, what is the interest for two hundred pounds the same time? —— 7 hundred pounds? —— 8 hundred pounds? ——95 hundred pounds?

17. A farmer sold 468 pounds of pork, at 3 pence a pound, and 48 pounds of cheese, at 4 pence a pound; how many pence must he receive in pay?

18. A boy bought 10 oranges; he kept 7 of them, and sold

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Ans. 62280. many seconds, 20 minutes!

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dollars in 3 oounds? ne place at the els 52 miles a will they be at

year, be six t for 2 years! for 35 years?

for one year, ndred pounds -8 hundred

t 3 pence a pound; how

hem, and sold

5 14. 15. READER MURIC READER NOTES IN DIVISION OF SIMPLE NUMBERS.

the others for 5 pence a piece; how many pence did he receive?

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19. The component parts of a certain number are 4, 5, 7, 6, 9, 8, and 3; what is the number?

20. In 1 hogshead are 63 gallons; how many gallons in 8 hogsheads? In 1 gallon are 4 quarts; how many quarts in 8 hogsheads? In 1 quart are 2 pints; how many pints in 8 hogsheads?

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Division of Simple Numbers. 22.415

and the strain of the wold and TA. 1. James divided 12 apples among four boys; how many did he give each boy? 2. James would divide 12 apples among three boys; how

many must he give each boy? A state state state and state who received 3 apples each; how many boys did he give them to !

4. If you had 20 pence, how many cakes could you buy at 2 pence a piece?

5. How many yards of cloth could you buy for 30 pounds. at 2 pounds a yard?

6. If you pay 250 shillings for 10 yards of cloth, what is one yard worth?

7. A man works 6 days for 42 shillings; how many shillings is that for one day?

8. How many quarts in 4 pints? ---- in 6 pints? ----in 10 pints?

9. How many times is 8 contained in 88?

10. If a man can travel 4 miles an hour, how many hours would it take him to travel 24 miles? + 1. Et ... , 14.

11. In an orchard there are 28 trees standing in rows, and there are 3 trees in a row; how many rows are there?

Remark. When any one thing is divided into two equal parts, one of those parts is called a half; if into 3 equal parts, one of those parts is called a third; if into four equal parts, one part is called a quarter or a fourth; if into five, one part is called a fifth, and so on.

12. A boy had two apples, and gave one half an apple to each of his companions; how many were his companions?

¶ 14, 15.

13. A boy divided four apples among his companions, by giving them one third of an apple each; among how many, did he divide his apples? 1 to 7199

14. H w many quarters in three oranges? 15. How many oranges would it take to give 12 boys one quarter of an orange each?

How much is one half, of 12 apples ? It is inclusion in .02 16. How much is one third of 12? Spiniston ?

18. How much is one fourth of 12? shiedenoid is th

19. A man had 30 sheep, and sold one fifth of them; how many of them did he sell?

20. A man purchased sheep for 13 shillings apiece, and paid for them all 117 shillings; what was their number?

21. How many oranges, at 3 pence each, may be bought for 12 bence gnound soliding 21 benerit solution. I

It is plain, that as many times as 3 pence can be taken from 12 pence, so many oranges may be bought, the object therefore, is to find how many times 3 is contained in 12

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rurstorange, 3.pence.	we see in this example, that
and her blienerater you	we may take 3 from 12 four
And may mino Bearnes (m	times, after which there is no
Second orange, 3 pence.	remainder; consequently, sub-
'spanod ne zor áng noá m	traction alone is sufficient for
6	the operation ; but we may come
Third orange, 3 pence.	to the same result by a process,
	-in most cases much shorter.
shillinge: now many shil-	called Division. TOTA PLAT A
Fourth orange, 3 pence.	mays is that for one day?
Saluiy inui	M. How many on use in 1 punts

¶ 15. It is plain, that the cost of one orange, (3 pence,) multiplied by the number of oranges, (4,) is equal to the cost of all the oranges, (12 pence;) 12 is, therefore, a pro-duct, and 3 one of its factors; and to find how many times 3 is contained in 12 is to find the other factor, which, multiplied into 3, will produce 12. "This factor we find by trial, to be 4, (4×3-12;) consequently, is contained in 12, 4 times? Solutine in the stole of string Ans. 4 oranges.

22.1 At man would divide 12 oranges equally among 3 children; how many oranges would each child have ? or the Here the object is to divide the 12 granges into 3 equal

parts, and to ascertain the number of oranges in each of companions; how many were ms companions?

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DIVISION OF SIMPLE NUMBERS.

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(3 pence,) jual to the fore, a prohany times which, mulind by trial, d m 12, 4 4 oranges. among 3 iave? to 3 equal in each of those parts. The operation is evidently as in the last example, and consists in finding a number, which, multiplied by 3, will produce 12. This number we have already found to be 4. Ans. 4 oranges apiece.

As, therefore, multiplication is a short way of performing many additions of the same number; so division is a short way of performing many subtractions of the same number; and may be defined, The method of finding how many times one number is contained in another; and also of dividing a number into any number of equal parts. In all cases, the process of division consists in finding one of the factors of a given product, when the other factor is known.

The number given to be divided, is called the dividend, and answers to the product in multiplication The number given to divide by is called the divisor, and answers to one of the factors in multiplication. The result, or answer sought, is called the quotient, (from the Latin word quoties, how many?) and answers to the other factor.

SIGN. The sign for division is a short horizontal line between two dots, \div . It shows that the number before it is to be divided by the number after it. Thus, $27 \div 9 = 3$, is read, 27 divided by 9 is equal to 3; or to shorten the expression, 27 by 9 is 3; or 9 in 27 3 times. In place of the dots, the dividend is often written over the line, and the divisor under it, to express division; thus, $\frac{2}{9} = 3$, read as before.

The reading used by the pupil in committing the following table may be 2 by 2 is 1, 4 by 2, &c., or 2 in 2 one time, 2 in 4 two times, &c.

DIVISION TABLE.

	$\frac{1}{2}$ $\frac{1}$	$\begin{array}{c} 1 \\ 1 \\ 2 \\ 1 \\ 1 \\ 2 \\ 1 \\ 1 \\ 1 \\ 1 \\$	1 2 3 4 5 6 7 8	$ \begin{array}{c} \underbrace{=}{} 1 \\ \underbrace{=}{2} \\ \underbrace{=}{2}$	$\begin{array}{c} \frac{7}{4} = 1\\ \frac{1}{4} = 2\\ \frac{3}{4} = 3\\ \frac{3}{4} = 4\\ \frac{3}{4} = 5\\ \frac{4}{4} = 5\\ \frac{4}{4} = 6\\ \frac{4}{4} = 6\\ \frac{4}{5} = 8\end{array}$
$\begin{array}{c} \frac{14}{2} = 7\\ \frac{16}{2} = 8\\ \frac{19}{2} = 9\end{array}$	$\begin{vmatrix} \frac{2}{3} = 7\\ \frac{2}{3} = 8\\ \frac{2}{3} = 9\\ \frac{2}{3} = 9 \end{vmatrix}$	$\begin{vmatrix} 28 \\ 4 \\ 3^2 \\ 3^6 \\ 4 \\ 3^6 \\ 9 \end{vmatrix}$	49 = 7 35 = 8 45 = 9	$4^{2}_{6} = 7$ $4^{3}_{6} = 8$ $5^{4}_{6} = 9$	$\frac{49}{5^6} = 7$ $\frac{56}{5^3} = 9$

DIVISION OF SIMPLE NUMBERS.

DIVISION TABLE-CONTINUED.

$\frac{2}{5} = 1$
₹=2
$\frac{1}{2} = 3$
§=4
$\frac{1}{2} = 5$
$\frac{1}{3} = 6$
₹=7
§ =8
§=9

28:-7, or $\frac{28}{12}$ = how many? 49:-7, or $\frac{49}{12}$ = how many? 42:-6, or $\frac{42}{6}$ = how many? 32:-4, or $\frac{32}{4}$ = how many? 54:-9, or $\frac{54}{8}$ = how many? 99:-11, or $\frac{99}{12}$ = how many? 32:-8, or $\frac{32}{8}$ = how many? 84:-12, or $\frac{81}{12}$ = how many? 33:-11, or $\frac{31}{12}$ = how many? 108:-12, or $\frac{108}{12}$ = how many?

¶ 16. 23. How many yards of cloth, at 4 shillings a yard, can be bought for 856 shillings?

Here the number to be divided is 856, which therefore is the *dividend*; 4 is the number to divide by, and therefore the *divisor*. It is not evident how many times 4 is contained in so large a number as 856. This difficulty will be readily overcome, if we decompose this number, thus:

856 = 800 + 40 + 16.

Beginning with the hundreds, we readily perceive that 4 is contained in 8 2 times; consequently, in 800 it is contain-200 times. Proceeding to the tens, 4 is contained in 4 1 time, and consequently in 40 it is contained 10 times. Lastly, in 16 it is contained 4 times. We now have 200+10+4=214 for the quotient, or the number of times 4 is contained in 856. Ans. 214 yards.

We may arrive to the same result without decomposing the dividend, except as it is done in the mind, taking it by parts, in the following manner:

Dividend.For the sake of convenience, weDivisor, 4) 856write down the dividend with the divisor on the left, and draw a line beQuotient, 214tween them; we also draw a line
underneath.the left hand, we seek how often the divisor (4) is contain

¶ 16. ed in times place 4 is or *ten's* p times we joi times, This Divisi ried on the div

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D. =1=2=3=4=5=6=7=8=9

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4 shillings a

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ed in 8, (hundreds,) the left hand figure; finding it to be 2 times we write 2 directly under the 8, which falling in the place of hundreds, is in reality 200. Proceeding to tens, 4 is contained in 5 (tens) 1 time, which we set down in ten's place, directly under the 5 (tens.) But after taking 4 times ten out of the 5 tens, there is 1 ten left. This 1 ten we join to the 6 units, making 16. Then, 4 into 16 goes 4 times, which we set down and the work is done.

This manner of performing the operation is called *Short Division*. The computation it may be perceived, is carried on *partly* in the mind, which is always easy to do when the divisor does not exceed 12.

RULE.

From the illustration of this example, we derive this general rule for dividing, when the divisor does not exceed 12:

1. Find how many times the divisor is contained in the first figure, or figures, of the dividend, and, setting it directly under the dividend, carry the remainder, if any, to the next figure as so many tens.

II. Find how many times the divisor is contained in *this* dividend, and set it down as before, continuing so to do till all the figures in the dividend are divided.

PROOF. We have seen, $(\P 15,)$ that the divisor and quotient are factors, whose product is the dividend, and we have also seen, that dividing the dividend by one factor is merely a process for finding the other.

Hence *division* and *multiplication* mutually prove each other.

To prove division, we may multiply the divisor by the quotient, and, if the work be right, the product will be the same as the dividend; or we may divide the dividend by the quotient, and, if the work is right, the result will be the same as the divisor.

To prove Multiplication, we may divide the product by one factor, and if the work be right, the quotient will be the other factor.

EXAMPLES FOR PRACTICE.

24. A man would divide 13,462,725 pounds among 5 men; how many pounds would each receive?

OPERATION. Dividend. Divisor, 5)13,462,725 Quotient, 2,692,545

PROOF.

Quotient. 2,692,545 5 divisor. In this example, as we cannot have 5 in the first figure, (1) we take two figures, and say 5 in 13 will go 2 times, and there are 3 over, which, joined to 4, the next figure, makes 34; and 5 in 34 will go 6 times, & c:

¶ 16, 17.

In proof of this example, we multiply the quotient by the divisor, and, as the product is the same as the dividend, we conclude that the work is right.— From a bare inspection of the

13,462,725 From a bare inspection of the above example and its proof, it is plain, as before stated, that division is the *reverse* of multiplication, and that the two rules mutually prove each other.

25: How many yards of cloth can be bought for 4,354,560 shillings, at 2 shillings a yard? — at 3 shillings? — at 4 shillings? — at 5 shillings? — at 6 shillings? — at 7? — at 8? — at 9? at 10?

Note. Let the pupil be required to prove the foregoing, and all of the following examples.

26. Divide 1005903360 by 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, and 12.

27. If 2 pints make a quart, how many quarts in 8 pints? — in 12 pints? — in 20 pints? — in 24 pints? — in 248 pints? — in 3674 pints? — in 47632 pints?

28. Four quarts make a gallon; how many gallons in 8 quarts? —— in 12 quarts? —— in 20 quarts? —— in 36 quarts? —— in 368 quarts? —— in 4896 quarts? —— in 5436144 quarts?

29. A man gave 86 apples to 5 boys; how many apples would each boy receive?

Dividend. Divisor, 5)86

Here, dividing the number of the apples (86) by the number of

Quotient, 17-1 Remainder. boys, (5,) we find, that each boy's share would be 17 apples; but there is 1 apple left.

¶ 17. 5)86

173

In order to divide *all* the apples equally among the boys, it is plain, we must divide this *one* remaining apple into 5 equal Then part of

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equal parts, and give one of these parts to each of the boys. 25 Then each, boy's share, would be 17 apples, and one fifth part of another, apple ; which is written thus, 174 apples ()

The 17, expressing whole apples, are called integers, o (that is, whole numbers) The t (one, fifth) of an apple, expressing part of a broken or divided apple, is called a fraction, (that is a broken number.)

Trees we may notice, that the eighth part 50 T 1? Fractions as we here see, are written with two, numbers, on one directly over the other, with a short line between them, showing that the upper number is to be divided by the lower. The upper number, or dividend, is, ing fractions, 1 called the numerator, and the lower number, or divisor is called the denominator. times 6, m k - 52, & c.

Note: A number like 17; composed of integers (17) and a fraction, (+,) is called a mixed number the blas 133

In the preceding example, the one apple, which was left after carrying the division as far as could be by whole numbers, is called the remainder, and is evidently a part of the divi lend yet undivided. In order to complete the division, this remain ler, as we before remarked, must be divided into 5 equal parts; but the divisor itself expresses the number of parts.' If, now, we examine the fraction, we shall see, that it consists of the remainder (1) for its numerator, and the divisor (5) for its denominator.

Therefore, if there be a remainder, set it down, at the right hand of the quotient for the numerator of a fraction, under which write the divisor for its denominator.

Proof of last example. In proving this example, we find it necessary to multiply our fraction by 5; but this is easily done, if we consider, that the fraction 1 express-

173 5

86

es one part of an apple divided into

With the start of

5 equal parts; hence, 5 times 1 is 3-1, that is, one whole apple, which we reserve to be added to the units, saying, 5

times 7 are 35, and one we reserved makes 36, &c. 30. Eight men drew a bounty of 453 pounds from government, how many pounds did each receive? VIEW MADELE

¶ 18, 19. DIVISION OF SIMPLE NUMBERS. A CONTRACT AND A STREET P 1815 191 1

Parallet to restore an allocation

Dividend. Here, after carrying the division as Divisor; 8)453 far as possible by whole numbers, we 1139.00 have a remainder of 5 pounds, which,

Quotient, 564 written as above directed, gives for the answer 56 pounds and § (five eighths) of another pound, to each man: 29 100 (. . A. B. L. M. M. . . .

¶ 18. Here we may notice, that the eighth part of 5 pounds is the same as 5 times the eighth part of 1 pound. that is, the eighth part of 5 pounds is a of a pound. Hence, a expresses the quotient of 5 divided by 8.

151.55 15

Proof. 4 is 5 parts, and 8 times 5 is 40, that is, 4°=5. 564 which, reserved and added to the product of 8

times 6, makes 53, &c. Hence, to multiply a 8 ----- fraction, we may multiply by the numerator.

and divide the product by the denominator, it is had 453

Or, in proving division, we may multiply the whole number in the quotient only, and to the product add the remainder; and this, till the pupil shall be more particularly taught in fractions, will be more easy in practice. Thus, 56×8= 448, and 448-5, the remainder, =453, as before.

31. There are 7 days in a week; how many weeks in 365 days? Ans. 524 weeks.

32. When flour is worth 2 pounds a barrel, how many barrels may be bought for 25 pounds? how many for 51 pounds? ---- for 487 pounds? ---- for 7631 pounds?

33. Divide 640 pounds among 4 men.

	640-4, or 640-160 po	unds, Ans.
34.	6786 or 67.8 = how many?	Ans. 113.
35.	⁵ ⁴ ⁰ = how many ?	1

36. 72,34 = how many?

37. 3464 == how many?

38. 2164 == how many?

39. 40 30 1 = how many?

40. 20 140 12 how many?

1 19. 41, Divide 4370 pounds equally among 21 men. When, as in this example, the divisor exceeds 12, it is evident that the computation cannot be readily carried on in the mind, as in the foregoing examples. Wherefore, it is more convenient to write down the computation at length in the following manner:

Ans. 3848.

A* 1

parts, findin of the 43 bei This, by ten divide be in t It is

to be t divisor making dividen bring d We

(tens;) quotien 170. and, fin multipl 168, un der to b of the c for the This

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56×8≓

weeks in 24 weeks. 10w many ny for 51 1ds?

nds, Ans. Ans. 113.

ns. 3844.

g 21 men. a 12, it is carried on erefore, it at length OPERATION. Divisor, Dividend, Quotient. and dividend as in short di-21)4370 (208₂₇. 42 42 170 168 We may write the divisor vision, but instead of writing the quotient under the dividend, it will be found more convenient to set it to the right hand.

2 Taking the dividend by parts, we seek how often we can have 21 in 43 (hundreds;) finding it to be 2 times, we set down 2 on the right hand of the dividend for the highest figure in the quotient. The 43 being hundreds, it follows, that the 2 must be hundreds. This, however, we need not regard, for it is to be followed by tens and units, obtained from the tens and units of the dividend, and will therefore, at the end of the operation, be in the place of hundreds, as it should be.

It is plain that 2 (hundred) times 21 pounds ought now to be taken out of the dividend; therefore, we multiply the divisor (21) by the quotient figure 2 (hundred) now found, making 42 (hundred,) which, written under the 43 in the dividend, we subtract, and to the remainder, 1, (hundred,) bring down the 7, (tens.) making 17 tens.

We then seek how often the divisor is contained in 17, (tens;) finding that it will not go, we write a cipher in the quotient, and bring down the next figure, making the whole 170. We then seek how often 21 can be contained in 170, and, finding it to be 8 times, we write 8 in the quotient, and multiplying the divisor by this number, we set the product, 168, under the 170; then subtracting, we find the remainder to be 2, which, written as a fraction on the right hand of the quotient, as already explained, gives 208_{21}^{21} pounds, for the answer.

This manner of performing the operation is called Long Division. It onsists in writing down the whole computation.

From the above example, we derive the following

RULE.

I. Place the divisor on the left of the dividend, separate them by a line, and draw another line on the right of the dividend to separate it from the quotient.

II. Take as many figures, on the left of the dividend, as

48

DIVISION OF SIMPLE NUMBERS. White the distant

· Il contain the divisor once or more; seek how many times they contain it, and place the answer on the right hand of the - dividend for the first figure in the quotient.

of of IHP Multiply the divisor by this quotient figure, and write the product under that part of the dividend taken.

IV. Subtract the product from the figures above, and to the remainder bring down the next figure in the dividend, and divide the number it makes up, as before. So continue to do, till all the figures in the dividend shall have been 1111 1 1111 brought down and divided."

Note 1. Having brought down a figure to the remainder, if the number it makes up be less than the divisor, write a cipher in the quotient, and bring down the next figure.

Note 2. If the product of the divisor, by any quotient figure, be greater than the part of the dividend taken, it is an evidence that the quotient figure is too large, and must whe diminished."If the remainder at any time be greater "than" then divisor, "or equal to it, the quotient figure is too . small, and must be increased.

odt in & out tol "EXAMPLES FOR PRACTICE." (.bonl: How many hogsherds of molasses, at 7 pounds a hogs-

head, may be bought for 6318 pounds?

TI in housing a bost of the MAns. 9024 hogsheads. 211 12. If a man's income be 1248 pounds a year, how much is that per week, there being 52 weeks in a year ?!

of i m boardman fol man is with "Ans. 24 pounds per week. tout 3. What will be the quotient of 153598, divided by 291, tout and the but, reductive and row of the but, reductive and the but and the Ans. 5296.14. -misi4. How many times is 68 contained in 30131?

hund Ans: 47817 times; that is, 478 times, and 17 of another .101113 time.

5. What will be the several quotients of 7652, divided by 16, 23, 34, 86, and 92?

192 6. If a farm, containing 256 acres, be worth 1850 pounds, what is that per acre?

7. What will be the quotient of 974932, divided by 365! Juscipe building of th Ans. 2671 365

8. Divide 3228242 pounds equally among 563 men; how many pounds must each man receive? Ans. 5734 pounds. 9. If 57624 be divided into 216, 586, and 976 equa parts, what will be the magnitude of one of each of these equal parts?

Ans. parts w 10.

11. said to there be 12. 13. 14. 9

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Ans. The magnitude of one of the last of these equal 1 2 2 growthe star at 21 des parts will be 59 40.

10. How many times does 1030603615 contain 3215? 11 1 1 Ans. 320561 times.

11. The earth in its annual revolution round the sun, is said to travel 596088000 miles; what is that per hour, there being 8766 hours in a year? , i i i i inter at "

12. 1234567890 == how many? 13. 40781220 == how many? 14. 987648031 = how many?

CONTRACTIONS IN DIVISION.

1. When the divisor is a composite number.

¶ 20. 1. Bought 15 yards of cloth for 30 pounds; how much was that per yard? . A sto la prof. east

15 yards are 3×5 yards. If there had been but 5 yards, the cost of one yard would be 30 = 6 pounds; but as there are 3 times 5 yards, the cost of one yard will evidently be but one third part of 6 pounds; that is, s=2 pounds, Ans.

Hence, when the divisor is a composite number, we may, if we please, divide the dividend by one of the component parts, and the quotient, arising from that division, by the other; the last quotient will be the answer.

2. If a man can travel 24 miles in a day, how many days will it take him to travel 264 miles?

It will evidently take him as many days as 264 contains 24. OPERATION.

24=	$=6 \times 4$. (6)264	· · · · ·	24)264(11 day	s, Ans.
of another		or,	24	
	4)44		· · · ·	· ·
2, divided by	-	~	24	,
950 hounds	11 da	iys.	24	

II. To divide by 10, 100, 1000, &c.

¶ 21. 1. A note of 2478 pounds is owned by 10 men

3. Divide 576 by $48 = (8 \times 6)$

4. Divide 1260 by $63 = (7 \times 9)$

5. Divide 2430 by 56.

what is each man's share?

850 pounds,

ded by 365? ns. 2671_{365} 3 men; how 734 pounds. 976 equal ch of these

1 0 - -----

1 3, 1, 1 . . .

Each man's share will be equal to the number of tens contained in the whole sum, and, if one of the figures be cut off at the right hand, all the figures to the left may be cons dered so many tens; therefore' each man's share will be 2i47 s pounds.

It is evident, also, that if 2 figures had been cut off from the right, all the remaining figures would have been so many hundreds; if 3 figures, so many thousands, &c. Hence, we derive this general RULE for dividing by 10, 100, 1000, &c.: Cut off from the right of the dividend so many figures as there are ciphers in the divisor, the figures to the left of the point will express the quotient, and those to the right, the remainder.

2. How many 100 in 42400? Ans. 424. Here the divisor is 100; we therefore cut off 2 424 00 figures on the right hand, and all the figures to the left (424) express the number of hundreds.

- Ans. 345-57. 3. How many 100 in 34567?
- 4. How many hundreds in 4567840 hundreds?
- 5. How many hundreds in 345600 hundreds?
- Ans, 426 145: 6. How many 100 in 42604 hundreds?
- 7. How many thousands in 4000? ----- in 25000?
 - 8. How many thousands in 6487 thousands ? Ans. 6487.

9. How many thousands in 42863 thousands? -368456 thousands ? ----- in 96842378 thousands ?

10. How many tens in 40? in 400? in 20? in 468? in 487? in 34640?

111. When there are CIPHERS on the right hand of the divisor. ¶ 22. 1. Divide 480 pounds among 40 men?

OPERATION.

40)480

In this example, our divisor, (40,) is a composite number, 12 pounds, Ans. $(10 \times 4 = 40;)$ we may therefore, divide by one component part, (10,) and that quotient by the other, (4;) but to divide by 10 we have seen, is but to cut off the right hand figure, leaving the figures to the left of the point for the quotient, which we divide by 4, and

the work is done. It is evident, that, if our divisor had been 400, we should have cut off 2 figures, and have divided in the same manner; if 4000, 3 figures, &c. Hence,

this general RULE: When there are ciphers at the right

4. I pounds 5. I 6. I 7. L 50, 600

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Ans. 424. re cut off 2 gures to the

ns. 345₁₀₀. ls?

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our divisor, ite number, may therethat quotient seen, is but igures to the ide by 4, and divisor had nd have divizc. Hence, at the right SUPPLEMENT TO DIVISION.

hand of the divisor, cut them off, and also as many places in the dividend; divide the remaining figures in the dividend, by the remaining figures in the divisor; then annex the figures cut off from the dividend, to the remainder.

2. Divide 748346 by 8000.

Dividend. Divisor, 8|000)748|346

Quotient, 93.-4346 Remainder. Ans. 93488 3. Divide 46720367 by 4200000.

Dividend.

42|00000)467|20367(11,520,867 Quotient.

10	
17	
41	
A9	

520367 Remainder.

4. How many pieces of cloth can be bought for 346508 pounds, at 20 pounds per piece ?

5. Divide 76428400 by 900000.

6. Divide 345006000 by 84000.

7. Divide 4680000 by 20, 200, 2000, 20000, 3000, 4000, 50, 600, 70000, and 80.

SUPPLEMENT TO DIVISION.

QUESTIONS.

1. What is division ? 2. In what does the process of division consist? 3. Division is the reverse of what? 4. What is the number to be divided called; and to what does it answer in multiplication? 5. What is the number to divide by called, and to what does it answer, &c.? 6. What is the result or answer called, &c. ? 7. What is the sign of division, and what does it show? 8. What is the other way of expressing division ? 9. What is short division, and how is it performed ? 10. How is division proved ? 11. How is multiplication proved ? 12. What are integers, ur whole numbers? 13. What are fractions, or broken numbers ? 14. What is a mixed number ? 15. When there is any thing left after division, what is it called, and how is it to be written ? 16. How are fractions written ? 17. What is the upper number called? 18. —— the lower number? 19. How do you multiply a fraction ? 20. To what do the numerator and the denominator of a fraction answer in division ? 21. What is long division? 22. Rule? 23. When the divisor is a composite number, how may we proceed? 24. When the divisor is 10, 100, or 1000, &c. how may the operation be contracted ? 25. When there are ciphers at the right hand of the divisor how may we proceed?

2. The bar of an an only EXERCISES on the transfer the transfer

1. An army of 1500 men, having plundered a city, took 2625000 pounds; what was each man's share?

2. A certain number of men were concerned in the payment of 18950 pounds; and each man paid 25 pounds; what was the number of men?

3. If 7412 eggs be packed in 34 baskets, how many in a basket?

4. What number must I multiply by 135 that the product may be 505710.

5. Light moves with such amazing rapidity, as to pass from the sun to the earth in about the space of 8 minutes.— Admitting the distance, as usually computed to be 95000000 miles, at what rate per minute does it travel ?

6. If the product of two numbers be 704, and the multiplier be 11, what is the multiplicand ? Ans. 64.

7. If the product be 704, and the multiplicand 64, what is the multiplier?

8. The divisor is 18, and the dividend 144; what is the quotient?

9. The quotient of two numbers is S, and the dividend 144; what is the divisor?

10. A man wishes to travel 585 miles in 13 days; how many miles must he travel each day?

11. If a man travels 45 miles a day, in how many days will he travel 585 miles?

12. A man sold 140 cows for 560 pounds; how much was that for each cow?

13. A man, selling his cows for 4 pounds each, received for all 560 pounds; how many cows did he sell?

14. If 12 inches make a foot, how many feet are there in 364812 inches?

15. If 364812 inches are 30401 feet, how many inches make 1 foot?

16. If you would divide 48750 pounds among 50 men, how many pounds would you give to each one?

17. If you distribute 48750 pounds among a number of men, in such a manner as to give to each one 975 pounds, how many men receive a share ?

18. A man has 17484 pounds of tea in 186 chests; how many pounds in each chest?

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19. A man would put up 17484 pounds of tea into chests containing 94 pounds each; how many chests must he have?

20. In a certain town there are 1740 inhabitants, and 12 persons in each house; how many houses are there? — in each house are 2 families, how many persons in each family?

21. If 2760 men can dig a certain canal in one day, how many days would it take 46 men to do the same? How many men would it take to do the work in 15 days? — in 5 days? — in 20 days? — 40 days? — in 120 days?

22. If a carriage wheel turns round 62280 times in running from Quebec to Montreal, a distance of 180 miles, how many times does it turn in running 1 mile? Ans. 346.

23. Sixty seconds make 1 minute; how many minutes in 3600 seconds? ——in 86400 seconds? ——in 604800 seconds? ——in 2419200 seconds?

24. Sixty minutes make one hour; how many hours in 1440 minutes? ______ in 10080 minutes? ______ in 40320 minutes? ______ in 525960 minutes?

25. Twenty-four hours make a day; how many days in 168 hours? ______ in 672 hours? ______ in 3766 hours? 26. How many times can I subtract forty-eight from four hundred and eighty?

27. How many times 3478 is equal to 47854?

28. A bushel of grain is 32 quarts; how many quarts must I dip out of a chest of grain to make one half $(\frac{1}{2})$ of a bushel? ________ for one fourth $(\frac{1}{4})$ of a bushel? ________ for one eighth $(\frac{1}{6})$ of a bushel? _______ Ans. to the last, 4 quarts. 29. How many is $\frac{1}{2}$ of 20? ________ $\frac{1}{2}$ of 48? _______ $\frac{1}{2}$ of 247? ________ $\frac{1}{2}$ of 847? _______ $\frac{1}{2}$ of 345878? _______ $\frac{1}{2}$ of 204030648? ________ Ans. to the last, 102015324. 30. How many walnuts are one third part $(\frac{1}{3})$ of 3 walnuts? _______ $\frac{1}{3}$ of 6 walnuts? _______ $\frac{1}{3}$ of 12 walnuts? ________ $\frac{1}{3}$ of 30? _______ $\frac{1}{2}$ of 3456320? Ans. to the last, 1152106 $\frac{2}{3}$. 31. What is $\frac{1}{2}$ of 4? _______ $\frac{1}{2}$ of 20? _______ $\frac{1}{5}$ of 320? ________ $\frac{1}{4}$ of 7843? _______ Ans. to the last, 1960 $\frac{2}{3}$.

MISCELLANEOUS QUESTIONS, Involving the principles of the preceding rules. Note. The preceding rules, viz. Numeration, Addition, E 2 Subtraction, Multiplication, and Division, are called the *Fundamental Rules of Arithmetic*, because they are the foundation of all other rules.

34 pounds; what did they both cost?

2. If a horse and chaise cost 91 pounds, and the chaise cost 57 pounds, what is the cost of the horse? If the horse cost 24 pounds, what is the cost of the chaise?

3. If the sum of 2 numbers be 487, and the greater number be 348, what is the less number? If the less number be 139, what is the greater number?

4. If the minuend be 7842, and the subtrahend 3481, what is the remainder? If the remainder be 4361, and the minuend be 7842, what is the subtrahend?

The When the minuend and remainder are given, how do you find the subtrahend?

When the subtrahend and the remainder are given, how do you find the minuend?

When you have the sum of two numbers, and one of them given, how do you find the other?

When you have the greater of two numbers, and their difference given, how do you find the less number?

When you have the less of two numbers, and their difference given, how do you find the greater number?

5. The sum of two numbers is 48, and one of the numbers is 19; what is the other?

6. The greater of two numbers is 29, and their difference 10; what is the less number?

7. The less of two numbers is 19, and their difference is 10; what is the greater?

8. A man bought 5 pieces of cloth at 44 pounds a piece; 974 dozen of shoes, at 3 pounds a dozen; 600 pieces of calico, at 6 pounds a piece; what is the amount?

9. A man sold six cows at 5 pounds each, and a yoke of oxen, for 19 pounds; in pay, he received a chaise, worth 31 pounds, and the rest in money; how much money did he receive?

10. What will be the cost of 15 pounds of butter, at 7 pence per pound?

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4. MISCELLANEOUS QUESTIONS.

shillings, at 8 shillings per bushel?

¶ 24. When the price of one pound, one bushel, &c. of any commodity is given, how do you find the cost of any number of pounds, or bushels, &c. of that commodity? If the price of the 1 pound, &c. be in shillings, in what will the whole cost be? If in pence, what?

When the cost of any given number of pounds, or bushels, &c. is given, how do you find the price of one pound or bushel, &c. In what kind of money will the answer be?

When the cost of a number of pounds, &c. is given, and also the price of one pound, &c. how do you find the number of pounds, &c.

12. When rye is 4 shillings per bushel, what will be the cost of 948 bushels?

13. If 648 pounds of tea cost 173 pounds, (that is 41520 pence) what is the price of one pound?

When the factors are given, how do you find the product? When the factor are given, how do you find the other factor?

When the divisor and quotient are given, how do you find the dividend?

When the dividend and quotient are given, how do you find the divisor ?

14. What is the product of 754 and 25?

15. What number, multiplied by 25, will produce 18850 ?

16. What number, multiplied by 754, will produce 18850?

17. If a man save 5 pence a day, how many pence would he save in a year, (365 days,)? —— how many in 45 years? How many cows could he buy with the money, at 742 pence each?

18. A boy bought a number of apples; he gave away ten of them to his companions, and afterwards bought thirty-four more, and divided half of what he then had among four companions, who received S apples each; how many apples did the boy first buy?

Let the pupil take the last number of apples, 8, and 'reverse the process. Ans. 40 apples.

19. There is a certain number, to which, if 4 be added, and 7 be substracted, and the difference be multiplied by 8, and the product divided by 3, the quotient will be 64; what is that number? Ans. 27. 20. A board has 8 rows of 8 squares, each; how many squares on the board?

¶ 25. 21. There is a spot of ground 5 rods long, and 3 rods wide; how many square rods does it contain?



Note. A square rod is a square (like one of those in in the annexed figure) measuring a rod on each side. By an inspection of the figure, it will be seen, that there are as many squares in a row as rods on one side, and that the number of rows is

equal to the number of rods, on the other side; therefore, $5 \times 3 = 15$, the number of squares. Ans. 15 square rods.

A figure, like A, B, C, D, having its opposite sides equal and parallel, is called a *parallelogram* or oblong.

22. There is an oblong field, 40 rods long, and 24 rods wide; how many square rods does it contain?

23. How many square inches in a board 12 inches long, and 12 inches broad? Ans. 144.

24. A certain township is six miles square; how many square miles does it contain? Ans. 36.

25. A man bought a lot of land for 2246 pounds; he sold one half of it for 1175 pounds at the rate of 3 pounds per acre; how many acres did he buy? and what did it cost him per acre?

26. A boy bought a sled for 56 pence, and sold it again for 8 quarts of walnuts; he sold one half of the nuts at 8 pence a quart, and gave the rest for a penknife, which he sold for 18 pence; how many pence did he lose by his bargains?

27. In a certain school-house, there are 5 rows of desks; on each row are six seats, and each seat will accommodate 2 pupils; there are also two rows, of 3 seats each, of the same size as the others, and one long seat where 8 pupils may sit; how many scholars will this house accommodate? Ans. 80.

28. How many square feet of boards will it take for the

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vs of desks; ccommodate each, of the ere 8 pupils commodate? Ans. 80. take for the floor of a room 16 feet long and 15 feet wide, if we allow 12 square feet for waste? All the stary Bring the

29. There is a room 6 yards long and 5 yards wide; how many yards of carpeting, a yard wide, will be sufficient to cover the floors, if the hearth and fireplace occupy 3 square yards? new above to un provision all bl B as in pli . 03

30. A board 14 feet long, contains 28 square feet; what is its breadth ?: Abata Istan a loddan . dr ar ad M . 31. How many pounds of pork, worth 4 pence a pound, can be bought for 144 pence ? The alman shill be and W . Ph

32. How many pounds of butter, at 9 pence per pound, must be paid for 25 pounds of tea, at 38 pence per pound?

33. 4+5+6+1+8= how many? ... 901 with

34. 4+3+10-2-4+6-7 = how many?

35. A man divides 30 bushels of potatoes among 3 poor men; how many bushels does each man receive? What is + of thirty? how many are ? (two-thirds) of 30?

36. How many are one-third $(\frac{1}{3})$ of 3? — of 6? of 9? _____ of 282 _____ of 45674312?

37. How many are two thirds $(\frac{2}{3})$ of 3?-of 6?

of 9! _____ of 282? _____ of 45674312? 38. How many are 1 of 40? _____ of 2 of 40? _____ 1 of 246876 ? 3 of 246876 ?

39. How many is t of 80? ---- t of 80? ---- t of 100? 40. An inch is one twelfth part $(-\frac{1}{2})$ of a foot how many feet in 12 inches? — in 24 inches ? — in 36 inches ? - in 12243648 inches?

41. If 4 pounds of tea cost 128 pence, what does 1 pound cost ? ---- 2 pounds ? ----- 3 pounds ? ----- 5 pounds ?. - 100 pounds ?

42. When oranges are worth 4 pence apiece, how many can be bought for 1464 pence?

43. The earth in moving round the sun, travels at the rate of 68000 miles an hour; how many miles does it travel in one day, (24 hours?) how many miles in one year, (365 days?) and how many days would it take a man to travel this last distance, at the rate of 40 miles a day? how many years? Ans. to the last, 40800.

44. How many pence can a man earn in 20 weeks, at 35 pence per day, Sundays excepted?

45. A man married at the age of 23; he lived with his

COMPOUND NUMBERS-REDUCTION. 126, 27.

wife 14 years; she then died, leaving him a daughter, 12 years of age; S years after the daughter was married to a man 5 years older than herself, who was 40 years of age when the father died; how old was the father at his death? Ans. 60.

46. There is a field 20 rods long, and 8 rods wide; how many square rods does it contain ? Ans. 160 rods.

47. What is the width of a field, which is 20 rods long, and contains 160 square rods.

48. What is the length of a field, 8 rods wide, and containing 160 square rods?

59. What is the width of a piece of land, 25 rods long, and containing 400 square rods?

COMPOUND NUMBERS.

¶ 26. A number expressing things of the same kind is called a *simple number*; thus, 100 men, 56 years, 75 cents, are each of them simple numbers; but when a number expresses things of different kinds, it is called a *compound number*; thus, 46 pounds 7 shillings and 6 pence, is a compound number; so 4 years 6 months and 3 days, 43 dollars 25 cents and 3 mills, are compound numbers.

Note. Different kinds, or names, are usually called different denominations.

Reduction.

¶ 27. In this Province as in England, money is reckoned in pounds, shillings pence and farthings. In the United States, money is reckoned in dollars, cents and mills. These are called denominations of money. Time is reckoned in years, months, weeks, days, hours, minutes, and seconds, called denomination of time. Distance is reckoned in miles, rods, feet, and is 'ves, called denominations of measure, &c.

The relative value of these denominations is exhibited in tables, which the pupil must commit to memory. The curren its ces Scotia denon pence

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HALIFAX CURRENCY.

HALIFAX CURRENCY.

The present currency of Lower Canada, is called Halifax currency, having been introduced into this Province, after its cession to Great Britain, by France, in 1763, from Nova Scotia. The denominations are the same in name as the denominations of English money, i. e. pounds, shillings, pence, and farthings; and the ratios of the different denominations to each other are the same as in English money. i. e. the shilling is one twentieth of the pound, the pentry one twelfth of the shilling, and the farthing one fourth of the penny. In value they are different, as will be seen in the ¶ upon reduction of currencies; where the ratio of each to the other, and of both to Federal Money is exhibited, with the method of ascertaining them in practice, for particular sums.

2	farthings (qrs.	.) make	1	half-penny,	marked	₽d.	
4	"	"	1	penny,	. "	d .	
12	pence	66 -	1	shilling,	"	s.	
20	shillings	**	1	pound, 1	"	£.	

Note. Farthings are often written as the fraction of a penny; thus, 1 farthing is written 1d., 2 farthings, 2d., 3 farthings, 2d.

It will be proper here to insert an abstract from the Provincial statute passed in 1842, fixing the value at which the gold and silver coins of other countries shall pass current in this Province.

The values assigned to the several coins by law in Canada, are not arbitrary, but are proportioned (except in the case of British silver) to the quantity of pure gold or silver in each. The \pounds currency was and is equal to 4 dollars of account; and a note for \$100 either in Upper or Lower Canada, is now, as it has always been payable by $\pounds 25$ cy., in any coins equivalent by law to that sum. By the currency Act the Provincial dollar of account is made equal in value to that of the United States. The coins, current by lav are :

British gold coins at the rate of £1 4s 4d cy. to £1 stg. American Eagles coined before 1st July 1834, at £2 13s 4d cy—Do. coined between 1st July, 1834, and 1st January, 1841, at £2 10s,—and at the same rates for half Eagles, &c.

The above ars a legal tender by tale if within two grains of full weight, deducting 1d cy. for each 1 of a grain wanting.

British gold and American gold coined before 1834, at 94s 10d cy. per oz. troy,— American gold coined between 1834 and 1841, at 93s cy. per oz. troy,— Coined Gold coin of France, at 98s 1d cy. per oz. troy. before Do of Laplate & Columbia at 89s 5d.

before Do. of Laplata & Columbia, at 898 5d " Apr. 26 Do. of Portugal & Brazil, at 948 6d " 1841. Sp. Mex. & Chilion Doubloons at 898 7d " —if offered respectively in sums of not less than \pounds " currency at one time.

British silver as above stated.

The dollars of Spain, United States, Peru, Chili, Central America, States of South America and of Mexico, coined before 1841, at 5s 1d currency, and half dollars at 2s 64d currency. Quarters at 1s 3d. Eights at 74d and sixteenths at 34d, if legal weight. The parts less than halves being a tender at the said rates by tale to the amount of £2 10s in one payment, until they have lost one twenty-fifth of their weight, and not aftewards.

French 5 franc silver pieces, coined before 26th April 1842, at 4s 8d each.

Gold and silver coins of the same nations of later dates, may be made current by proclamation to be issued as afore said the same ab normaping sur find by the association of the

Copper coins of the United Kingdom, (or any to be coined by Her Majesty of not less than five-sixths the weight of such coin) at their nominal rates.

The least legal weight of a Sovereign is, 5dwts. 2½ grs. —of an Eagle coined before 1834, 11 dwts. 6 grs., after 1834, 10 dwts. 18 grs.—of a Dollar, 17 dwts. 4 grs.—of a 5 franc piece 16 dwts. or of

1 27.

9 27

How penny in 3 pe in 8 pe

1 shilli lings ? How lings ?

in 4s.? 8s.? shilling in 2s. (——in

How pound ? in 3£? 4£ 6s. ? in 3£ 1

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to £1 stg. at £2 13s 1st Januaor half Ea-. 613-1. ··. .

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ore 1834, at 1. 1. 1. 1. 1. 1. 1. 1. 11, at 93s cy.

er oz. troy. d UE

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Chili, Central exico, coined ars at 2s 64d nd sixteenths alves being a of £2 10s in -fifth of their

th April 1842,

of later dates, sued as afore-

iny to be cointhe weight of

5dwts. $2\frac{1}{2}$ grs. s. 4 grs.—of a

REDUCTION.

The £ sterling, in any act or contract made after the passing of the Currency Act, [proclaimed 26 April, 1842] is to be understood as equivalent to £1 4s 1d cy., but in any act or contract made before that time, the word sterling is to be construed according to the intention of the Legislature or of the parties.

How many farthings in one | How many pence in 4 farpenny? —— in 2 pence ?—— things? —— in 8 farthings? in 3 pence ? ----- in 6 pence ? ----- in 12 farthings ? ----- in in 8 pence ?---- in 9 pence ? 24 farthings ? ---- in 32 far------ in 12 pence? ----- in things? ----- in 36 farthings? 1 shilling? — in 2 shil- in 48 qrs.? How many lings? shillings in 48 qrs? — in How many pence in 2 shil-96 qrs?

 lings ? _____ in 3 s. ? _____ How many shillings in 24

 in 4s. ? _____ in 6s. ? _____ in pence ? _____ in 36d. ? _____ in

 8s. ? _____ in 10s. ? _____ in 248d. ? _____ in 72d. ? _____ in

shillings and 2 pence ? ____96d. ? ____ in 120d. ? ____ in 2s. 3d. ? — in 2s. 4d. ? in 26d. ? — in 27d. ? — — in 4s. 3d. ? _ in 2s. 4d. ? in 26d. ? _ in 30d. ? _ _ _ in 30d. ? _ _ _ _ in 30d. ? _ _ _ _ _ in 51d. ? pound? — in $2 \pounds$ — How many pounds in 20 in $3\pounds$? ——in $4\pounds$ —— in shillings? ——in 40s.? —— $4\pounds$ 6s.? —— in $6\pounds$ 8s.? ——in 60s.? —— in 80s.? — in 3£ 10s.? ----- in 2£ 15s.? in 86s.? ----- in 128s.? ----staft - it and the think in 70s. ? ----- in 55s. ?

The changing of one kind, or denomination, into another kind, or denomination, without altering their value, is called *Reduction*. (¶ **27**.) Thus, when we change shillings into pounds, or pounds into shillings, we are said to reduce them. From the foregoing examples, it is evident, that, when we reduce a denomination of greater value into a denomination of less value, the reduction is performed by multiplication; and it is then called Reduction Descending.-But when we reduce a denomination of less value into one of greater value, the reduction is performed by divsion; it . 6 grs., after is then called Reduction Ascending. Thus, to reduce pounds

REDUCTION.

to shillings, it is plain we must multiply by 20. And again, to reduce shillings to pounds, we must divide by 20. It follows, therefore, that' reduction descending and ascending reciprocally prove each other. 1. In 172. 13s. 64d. how 2. In 16971 farthings, how many farthings?" () many pounds?' OPERATION. OPERATION. S. s. d. grs. Farthings in a penny 4)16971 3qr. at a 17 13 6 3. ... and f Pence in a shilling, 12)42426d. 20s. - 1.11 1111 Shillings in a pound 2035 313s 353s. in 17£. 13s. The I 12d. 17£. Ans. 17£ 135 634. - 4242d. e i in anti fille 4q. Farthings will be reduced to pence, if we divide them 16971grs. the Ans. by 4, because: every 4 far-In the above example, bethings make 1 penny. Therecause 20 shillings make 1 fore, 16971 farthings, divided pound, therefore we multiply by 4, the quotient is 4242 17£. by 20, increasing the pence, and a remainder of product by the addition of the 3, which is farthings, of the given shillings (13,) which, same name as the dividend. it is evident, must always be We then divide the pence done in like cases; then, be-(4242) by 12, reducing them cause 12 pence make 1 shilto shillings; and the shillings ling, we multiply the shillings (353) by 20, reducing them (353) by 12, adding in the to pounds. The last quotient given pence, (6.) Lastly, 17£., with the several rebecause 4 faithings make 1 mainders, 13s. 6d. 3qrs. conpenny, we multiply the pence stitute the answer. (4242) by 4, adding in the given farthings, (3.) We Note. In dividing 353s. by then find, that in 17£. 13s. 20, cut off the cipher, & c., 63d., are contained 16971 as taught ¶ 22. farthings. d. tox

[28. The process in the foregoing examples, if carefully examined, will will be found to be as follows, viz. To reduce high denominations To reduce low denominations to lower,—Multiply the high- to higher.—Divide the lowest est denomination by that num-denomination given by that succ til y deno In arc d and f obvio wher which

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ber which it takes of the next number which it takes of the less to make 1 of this higher, same to make 1, of the next (increasing the product by the higher. Proceed in the same number given if any of that manner with each succeeding less denomination.) Proceed denomination, until you have in the same manner with each brought it to the denominasucceeding denomination, un-tion required. til you have brought it to the N at a to an count in denomination required.

In the two examples, from which the above general rules arc deduced, the denominations are pounds, shillings, pence and farthings, considered as in Halifax Currency; but it is obvious that these rules can be applied to all currencies where the den minations are the same; or to currencies in which the denominations are different; and in general to all compound numbers. and the state of the state of the 11 N P or gran is

EXAMPLES FOR PRACTICE.

	an ISSEN a second	
3. Reduce	20£. 14s. 2d. to pence.	Ans. 4970.
4 "	24£. to farthings.	Ans. 23040.
5 "	66£. 6s. 6d. to pence.	Ans. 15912.
6. ""	158£. to farthings.	Ans. 151680.
7. "	1234£. 15s, 7d. to farthings.	Ans. 1185388.
· · · 8.	337587 farthings to pounds,	&c.
	Ans. 35	1£. 13s. Od. 3a.

9. " 1185388 farthings to pounds, &c.

Ans. 1234£. 15s. 7d.

as to the the

10. Reduce 32£. 15s. 8d.| 11. Reduce 31472 farthings, to farthings. - C 12 to pounds.

12. In 29 guineas, at 1£ 13. In 38976 farthings, how 3s. 4d. each, how many qrs. ? many guineas ?

15. Reduce 11736 pence to 14. Reduce \$163, at 6s. dollars. each, to pence?

16. In 15 guineas, how ma- 17. Reduce 21£. to guinny pounds?

Note. We cannot reduce guineas directly to pounds, but we may reduce the guineas to shillings, and then the shillings to pounds.

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y 20. - lt scending ings, how 16971 3qr. 2)4242 6'd. 0)35 3 135 17£. € 13s 63d. be reduced vide them ery_4 farny. Therengs, divided nt is 4242 mainderiof ings, of the e dividend. the pence ucing them the shillings ucing them ast quotient

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REDUCTION.

OLD CURRENCY.

12 deniers make 20 sous 1 livre, or franc.

The livres 10 d Halifax currency. In 32 livres 10 sous how many sous? In 97 livres 11 sous, how many sous?

In 650 sous, how many livres?

In 1951 sous, how many livres? In 10 livres 6 sous 9 deniers, how many deniers?

How many pounds currency in 96 livres?

GENERAL MONEY.

¶ 29. Federal money is the coin of the United States. The kinds or denominations, are eagles, dollars, dimes, cents, and mi¹¹s.

TABLE.

Sign. This character, \$, placed before a number, shows it to express federal money.

As 10 mills make a cent, 10 cents a dime, 10 dimes a dollar, &c. it is plain, that the relative value of mills, cents, dimes, dollars and eagles corresponds to the orders of units, tens, hundreds, &c. in simple numbers. Hence, they may be read either in the *lowest* denomination, or *partly* in a *kigher*, and partly in the lowest denomination. Thus:

34652 mills; or 3465 cents and 2 mills; or, reckoning the eagles tens of dollars, and the

The eagle is a gold coin, the dollar and dime are silver coins. the centis a copper coin. The mill is only *imaginary*, there being no coin of that denomination. There are half eagles, half dollars, half dimes, and half cents, *real* coins. Write and 2 m mills; 3 mill; 2 c cents and five cents

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dime inay Fo is pla figure figure Thus. dollar dullar_ quirin places point, but on with a 10 mill ceed 9. one pla place in the poir ident th cents.

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ited States.

ars, dimes,

1 cent.

=1 dime.

=1 dollar.

=1 eagle*

nber, shows

0 dimes a nills, cents, rs of units, e, they may partly in a Thus:

cents and 2

rs, and the

silver coins

there being

es, half dol-

dimes tens of cents, which is the usual practice, the whole may be read, 34 dollars 65 cents and 2 mills.

For ease in calculating, a point, (') called a scparatrix,* is placed between the dollars and cents, showing that all the figures at the left hand express dollars, while the two first figures at the right hand express cents, and the third, mills. Thus, the above example is written \$34'652; that is, 34 dollars 65 cents 2 mills, as above. As 100 cents make a dollar, the cents may be any number from 1 to 99, often requiring two figures to express them; for this reason, two places are appropriated to cents, at the right hand of the point, and if the number of cents be less than ten, requiring but one figure to express them, the ten's place must be filled with a cipher. Thus, 2 dollars and 6 cents are written 2'06. 10 mills make a cent, and consequently the mills never exceed 9, and are always expressed by a single figure. Only one place, therefore, is appropriated to mills, that is, the place immediately following cents, or the third place from the point. When there are no cents to be written, it is evident that we must write two ciphers to fill up the places of cents. Thus, 2 dollars and 7 mills are written 2007. Six cents are written, 06, and 7 mills are written '007.

Note. Sometimes 5 mills $=\frac{1}{2}$ a cent is expressed fractionally: thus, '125 (twelve cents and five mills) is expressed 121 (twelve and a half cents.)

17 dollars and 8 mills are writt	en, 17'008
4 dollars 5 cents,	- 4'05
75 cents,	- '75
24 dollars,	- 24'
9 cents,	- '09 '
4 mills,	- '004
6 dollars 1 cent and 3 mills,	- 6'013

Write down 470 dollars 2 cents; 342 dollars 40 cents and 2 mills; 100 dollars, 1 cent and 4 mills; 1 mill; 2 mills; 3 mills; 4 mills; $\frac{1}{2}$ cent, or 5 mills; 1 cent and 1 mill; 2 cents and 3 mills; six cents and one mill; sixty cents and one mill; four dollars and one cent; three cents; five cents; nine cents.

*The character used for the separatrix, in the "Scholars' Arithmetic," was the comma, the comma inverted is here adopted, to distinguish it from the comma used in punctuation.

REDUCTION OF FEDERAL MONEY.

¶ **30.** How many mills in one cent? — in 2 cents? — in 3 cents? — in 4 cents? — in 6 cents? — in 9 cents? — in 10 cents? — in 30 cents? — in 78 cents? — in 100 cents, (=1 dollar)? — in 2 dollars? — in 3 dollars? — in 4 dollars? — in 484 cents? — in 563 cents? — in 1 cent and 2 mills? — in 4 cents and 5 mills?

How many cents in 2 dollars? — in 4 dollars? — in 8 dollars? — in 3 dollars and 15 cents? — in 5 dollars and 20 cents? — in 8 dollars and 20 cents? — in 4 dollars and 6 cents?

How many dollars in 400 cents? — in 660 cents? in 380 cents? — in 40765 cents? How many cents in 1000 mills? How many dollars in 1000 mills? — in 3000 mills? — in 8000 mills? — in 4378 mills? — in 846732 mills?

As there are 10 mills in one cent, it is plain that cents are changed or reduced to mills by multiplying them by 10, that is, by merely annexing a cipher, (¶ 12.) 100 cents make a dollar; therefore dollars are changed to cents by annexing 2 ciphers, and to mills by annexing 3 ciphers. Thus, 16 dollars ==1600 cents ==16000 mills. Again, to change mills back to dollars, we have only to cut off the *three right hand* figures, (¶ 21;) and to change cents to dollars, cut off the *two right hand figures*, when all the figures to the *left* will be dollars, and the figures to the *right*, cents and mills.

Reduce 34 dollars to cents. Ans. 3400. Reduce 240 dollars and 14 cents to cents.

Reduce \$748'143 to mills. Reduce 748143 mills to dollars. Reduce 3467489 mills to dollars. Reduce 48742 cents to dollars. Reduce 1234678 mills to dollars. Reduce 3469876 cents to dollars. Reduce \$4867'467 to mills. Reduce 984 mills to dollars. Reduce 7 mills to dollars. Reduce \$'014 to mills. Reduce \$'014 to mills. Ans. 24014 cents. Ans, 748143 mills. Ans. \$748'143: Ans. 3467'489. Ans. \$487'42.

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Ans. \$ '984. Ans. \$ '007. 1 31:

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hat cents are n by 10, that ents make a y annexing 2 Thus, 16 dolchange mills e right hand cut off the the left will d mills.

Ans. 3400.

24014 cents. (48143 mills. s. \$748'143. s. 3467'489. us. \$487'42.

lns. \$ '984.

REDUCTION.

Reduce 984321 cents to mills.

Reduce $9617\frac{1}{2}$ cents to dollars.Ans. \$96'17 $\frac{1}{2}$.Reduce $2064\frac{1}{2}$ cents, 503 cents, 106 cents, $921\frac{1}{2}$ cents,500 cents, $726\frac{1}{2}$ cents to dollars.

Reduce 86753 mills, 96000 mills, 6042 mills, to dollars.

TROY WEIGHT.

¶**31.** It is established by law, that the pound Troy, with its parts, multiples, and proportions, shall be the standard weight for weighing gold^{*} and silver in coin or bullion, drugs, and precious stones. The denominations of Troy weight are pounds, ounces, pennyweights and grains.

TABLE.

24 grains (grs.) make 1 pennyweight, marked pwt. 20 pennyweights -- 1 cunce, -- - oz. 12 ounces -- - 1 pound, -- - lb.

1. How many grains in a 2. In 19680 grains how silver tankard weighing 3 lb. many pounds, &c. 5 oz.?

3. Reduce 210 lb. 8 oz. 12 4. In 50572 pwt. how mapwts. to pennyweights. ny pounds?

5. In 7 lb. 11 oz. 3 pwt. 6. Reduce 45681 grains to 9 grs. of silver, how many pounds. grains?

APOTHECARIES' WEIGHT.

Apothecaries' weight is used by apothecaries and physicians, in compounding medicines. The denominations are pounds, ounces, drams, scruples, and grains.

TABLE.

20 grains, (grs.) make	1 scruple, marked	E.
3 scruples	1 dram,	3.
8 drams	1 ounce,	3.
12 ounces	1 pound,	łb.

*The fineness of gold is tried by fire, and is reckoned in CARATS, by which is understood the 24th part of any quantity; if it lose nothing by the trial, it is said to be 24 carats fine. if it lose 2 carats, it is then 22 carats fine, which is the standard for gold.

Silver which abides the fire without loss is said to be 12 ounces fine. The standard for silver coin is 11 oz. 2 pwts. of fine silver, and 18 pwts. of copper melted together.

iThe pound and ounce apothecaries' weight and the pound and ounce Troy, are the same, only differently divivided, and subdivided.
7. In 9 lb. 83. 1 3. 2 D 8. Reduce 55799 grs. to 19 grs., how many grains. pounds.

AVOIRDUPOIS WEIGHT.*

It is established by law that the pound Avoirdupois with its parts &c. shall be considered as the standard for weighing every thing commonly sold by weight, except those articles, in weighing which, Troy weight is used. The denominations are tons, hundreds, quarters, pounds, ounces, and drams.

TABLE.

16 drams, (drs.) make 1	ounce, - marked - oz.
16 ounces 1	pound, 1b.
28 pounds 1	quarter, qr.
4 quarters 1	hundred weight cwt.
20 hundred weight - 1	ton T.

Note 1. In this kind of weight, the words gross and net are used. Gross is the weight of the goods, together with the box, bale, bag, cask, &c, which contains them. Net weight is the weight of the goods only, after deducting the weight of the box, bale, bag, or cask, &c., and all other allowances.

Note 2. A hundred weight, it will be perceived is 112 fb. Merchants at the present time, in the principal sea ports of the United States, buy and sell by the 100 pounds.

9. A merchant would put 109 cwt. 0 qrs. 12fb. of raisins into boxes, containing 26 many cwt. ? b. each; how many boxes

will it require?

11. In 12 tons, 15 cwt. 12. In 7323500 drams, how 1 qr. 19lb. 6 oz. 12 dr. how many tons? many drams?

13. In 28lb. avoirdupois, 14. In 34 lb. 0 oz. 6 pwt. how many pounds Troy? 16 grs. Troy, how many pounds avoiadupois?

*175 oz. Troy=192 oz. avoirdupois, and 1751b. troy=144lb avoirdupois, 11b. troy=5760 grains, and 1 lb. avoirdupois=7000 grains troy. 1

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¶ 31.

REDUCTION.

CLOTI: MEASURE.

Cloth measure is used in selling cloths and other goods sold by the yard, or ell. It is established by law that the English yard with its parts &c. shall be the standard for measuring all kinds of cloth or stuffs made of wool, flax &c. the English ell, when there is a special contract for it may be used with its parts. The denominations are ells, yards, quarters and nails.

TABLE.

Note. Consult ¶ 28 ex. 16.

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LONG MEASURE.

Long measure is used in measuring distances, or other things, where *length* is considered without regard to *breadth*. The denominations are degrees, leagues, miles, furlongs, rods, yards, feet, inches, and barley-corns.

TABLE.

¶ 31.

'99 grs. to

Avoirdupois standard for ght, except ht is used. ers, pounds,

d - oz. - lb. - qr. - cwt. - T. ross and net gether with them. Net educting the all other al-

ed is 112 lb. sea ports of ds. sof raisins,

each, how

drams, how

oz. 6 pwt. now many s?

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It is established by law, that the Paris foot with its parts, &c. shall be the standard measure of length, for measuring land, wood, timber, stone, masons', carpenters', and joiners' work. The English foot may be used when there is a special contract for it.

T	Δ.	R	T.	F.
	A	D.	_	 .

12 lines make 1 inch.	' 3 toises make 1 rod.
12 inches - 1 foot.	10 rods 1 arpent.
6 feet - 1 toise.	84 arpents - 1 leauge.
1 French foot == 1	17 English feet.

20. How many barley-corns, 21. In 4755801600 barleywill reach round the globe, it corns, how many degrees? being 360 degrees?

Note. To multiply by 2 is Note. The barley-corns beto take the multiplicand 2 ing divided by 3, and that times; to multiply by 1 is to quotient, by 12, we have take the multiplicand 1 time; 132106500 feet which are to to multiply by $\frac{1}{2}$ is to take be reduced to rods. We canthe multiplicand half a time, not easily divide by 161 on that is, the half of it. There-account of the fraction 1; but fore, to reduce 360 degrees to $16\frac{1}{2}$ feet = 33 half feet, in 1 statute miles, we multiply rod; and 132105600 feet = first by the whole number, 264211200 half feet, which 69, and to the product add divided by 33; gives 8006400 half the multiplicand. Thus : rods. AL . 57 3.1 271.2.1 **4)360** Hence, when the divisor is

69÷

3240

2160

25020 satute miles in 360°.

22. How many inches from Quebec to Three Rivers, sup-how many miles ? posing it to be 90 miles?

25. If a wheel 16 feet 6 in. 24. How many times will a wheel 16 feet and 6 inches in circumference, turn round in circumference, turn round 19200 times in going from in the distance from Quebec Quebec to St. Annes, what is to St. Annes, supposing it to the distance? be 60 miles?

b or 1, &c., we may reduce the divisor to halves or fourths &c., and reduce the dividend 180 half the multiplicand, to the same; then the guotient will be the true answer.

23. In^o 30539520 inches,

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26. In 28 leagues, 43 ar- 27. In 7000 feet how many pents, how many feet? how rods? how many arpents? many toises? how many rods?

LAND OR SQUARE MEASURE.

Square measure is used in measuring land, and any other thing, where length and breadth are considered. The de- ' nominations are miles, acres, roods, perches, yards, feet and inches.

1 32. 3 feet in length make a yard in long measure ; but it requires 3 feet in length, and 3 feet in breadth, to make a yard in square measure; 3 feet in length and 1 foot wide, make 3 square feet; 3 feet in length and 2 feet wide, make 2 times 3, that is, 6 square feet; 3 feet in length and 3 feet wide make 3 times 3, that is 9 square feet. This will clearly appear from the annexed figure.

3 feet =1 yard.



It is plain, also that a square foot. that is, a square 12 inches in length and 12 inches in breadth, must contain $12 \times 12 = 144$ square inches.

TABLE.

144 square inches= 12×12 ; that is, 12 inches in length and 12 inch- make 1 square foot. es in breadth, - '-- -

9 quare feet= 3×3 ; that is, 3 feet) I square yard. in length and 3 feet in breadth $30_{\frac{1}{2}}$ square yards $5_{\frac{1}{2}} \times 5_{\frac{1}{2}}$, or $272_{\frac{1}{2}}$ 1 square rod. square feet= $16\frac{1}{2} \times 16\frac{1}{2}$ perch or pole

520 inches,

16 feet 6 in. turn round going from nes, what is

1 rood. 40 square rods. - - - - - roods, or 160 square rods, - -1 acre. 4 - - 1 square mile.

Note. Gunter's chain, used in measuring land is 4 rods in length. It consists of 100 links, each link being 7,92 inches in length; 25 links make 1 rod long measure and 625 square links make 1 square rod.

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FRENCH SQUARE MEASURE.

144 square inches make 1 square foot.

36	-	feet	toise.
9	-	toises]	l rod.
100	-	rods 1	l arpent.
7056	-	arpents	l league.

62500 French feet =71289 English feet.

Reduce 16 leagues to feet, ----- to toises, ----- to rods. -to arpents, ------to leagues.

28. In 17 acres 3 roods 12 29. In 776457 square feet, rods, how many square feet ? how many acres?

Note. In reducing rods to Note. Here we have 776457 feet, the multiplier will be square feet to be divided by 2724. To multiply by 1, is to 2724. Reduce the divisor to take a fourth part of the mul-fourths, that is to the lowtiplicand. The principle is est denomination contained in the same as shown in ¶ 28, it; then reduce the dividend to *fourths*, that is, to the same ex. 20.

denomination, as shown ¶ 31, ex. 21.

feet, how many square miles?

30. Reduce 64 square miles 31. In 1,784,217,600 sq. to square feet.?

32. There is a town 6 miles 33. Reduce 23040 acres to square; how many square square miles. miles in that town? how many acres?

SOLID OR CUBIC MEASURE.

Solid or cubic measure is used in measuring things that have length, breadth, and *thickness*; such as timber, wood, stone, bales of goods, &c. The denominations are cords, tons, yards, feet and inches.

¶33. It has been shown, that a square yard contains $3 \times 3 = 9$ square feet. A cubic yard is 3 feet long, 3 feet wide, and 3 feet thick. Were it 3 feet long, 3 feet wide and one foot thick, it would contain 9 cubic feet; if 2 feet thick, it would contain $2 \times 9 = 18$ cubic feet; and, as it is

100 32. timber

34. how n **36**. wood 38. how r many a 40. inches

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3 fe

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yd=3 ft thick.

1728

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40

128 :

No

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1 foot

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square feet,

have 776457 be divided by the divisor to to the lowa contained in the dividend s, to the same s shown ¶ 31,

,**217**,600 sq. square miles? 3040 acres to

g things that imber, wood, ns are cords,

ard contains long, 3 feet 3 feet wide eet; if 2 feet and, as it is REDUCTION.

3 feet thick, it does contain 3×9=27 cubic feet. Thie will clearly appear from the an-

nexed figure.

lyd=3 ft long.



It is plain, also, that a cubic foot, that is, a solid 12 inches in length, 12 inches in breadth, and 12 inches in thickness, will contain $12 \times 12 \times 12 \pm 1728$ solid or cubic inches.

TABLE.

1728 solid inches, $=12 \times 12 \times 12$, that is, 12 inches in length, make one solid foot. 12 in breadth, 12 in thickness,

27 solid feet, $=3 \times 3 \times 3$

40 feet of round timber, or 50 feet of hewn timber.

128 solid feet, $=8 \times 4 \times 4$, that is, 8 feet in length, 4 feet in

1 cord of wood.

1 solid yard.

1 ton or load.

width, and 4 feet in height, What is called a cord foot, in measuring wood, is Note. 16 solid feet; that is, 4 feet in length, 4 feet in width, and 1 foot in height, and 8 such feet, that is 8 cord feet make 1 cord.

FRENCH SOLID MEASURE.

1728 solid inches make 1 solid foot.

216 - - feet make 1 toise.

1000 French feet =1218,186432 English feet.

32. Reduce 9 tons of round 33. In 622080 cubic incntimber to cubic inches. es how many tons of round timber?

34. In 37 cord feet of wood 35. In 592 solid feet of wood, how many cord feet? how many solid feet?

36. Reduce 64 cord feet of 37. In 8 cords of wood, wood to cords. how many cord feet?

39. In 2048 solid feet of 38. In 16 cords of wood, how many cord feet? how wood, how many cord feet; many solid feet? how many cords?

40. In 12 toises how many 41. In 834692773 inches how many feet; how many inches? G toises ?

WINE MEASURE, A State of the second se get in a were to be here

It is established by law that the wine gallon with its parts, &c. shall be the standard liquid measure, for measur-- ing wine, cider, beer, and all other liquids commonly sold by gauge, or measure of capacity. The denominations are tuns, pipes, hogsheads, barrels, gallons, quarts, pints, and gills.

: TABLE.

4 gills (gi.) - make - 1 pint, marked pt.	A
2 pints	deep,
4 quarts 1 gallon, - gal.	It
31 ¹ / ₂ gallons 1 barrel, bar.	parts,
63 gallons 1 hogshead, - hhd.	Dry I
2 hogsheads P.	1
2 pipes, or four hogsheads 1 tun, T.	20
Note. A gallon wine measure, contains 231 cubic inches.	
42. Reduce 12 pipes of wine 43. In 12096 pints of wine,	16
to pints. how many pipes?	3
44. In 9 P. 1 hhd. 22 gals. 45. Reduce 39032 gills to	2
3 qts. how many gills? pipes.	2
46. In a tun of cider, how 47. Reduce 252 gallons to	12
many gallons?	

ALE OR BEER MEASURE.

Ale or beer measure is used in measuring ale, beer, and - milk. The denominations are hogsheads, barrels, gallons quarts, and pints, in the second 1. . . . 3

TABLE.

2 pints (pts.)	make	1 quart,	marked	qt.	
4 quarts -	e ier	1 gallon,		gal.	
36 gallons -		1 barrel,	· · · · · ·	bar.	
54 gallons	1 1 1 1 1 1	1 hogshea	1d,	hhd.	
sover. A gallon	beer measu	ure, contain	ns 282 cubic	inches	
m. Reduce 47	bar. 18 gal	. 49. In	13680 pints	s of ale	la
of ale to pints.		how many	barrels?		
50, In 29 hhd	s. of beer	, 🖻 51. Re	duce 12528	pints t	:0
how many pints?	1 N	hogsheads	i.		20 20
					,0

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DRY MEASURE.

Dry measure is used in measuring all dry goods, such as grain, fruit, roots, salt, coal, &c. The denominations are chaldrons, bushels, pecks, quarts, and pints.

TABLE,

2	pints (pts	3.)	make	•	1	quart, -	marked	1	- qt.
8	quarts			-	1	peck, -	-	•	pk,
4	pecks	-	-	-	1	bushel, -		-	bu.
36	bushels	-	-	-	1	chaldron,	-	÷	ch.

Note. A gallon dry measure, contains 2684 cubic inches,

A Winchester bushel is 181 inches in diameter, 8 inches deep, and contains 2150²/₅ cubic inches,

It is established by law that the Canada Minot, with its parts, multiples, and proportions, shall be the standard in Dry Measure.

1 pot=116'94589 English cubic feet,

20 pots make one minot,

OLD MEASURE.

16 litrons		m	ake	-	1	-	-	-		-	boisseau.
3 boisseau	1X	-		-	1	-	•).=	-	-	٠	minot.
2 minots	-	-	-	-	1		-	-	٠	-	mine.
2 inines	-	.	í 🗭	-	1	-	-		-		setier.
12 setiers	-	-	-	-	1	-	-	-	•		muid.

40 French cubic inches=1 litron.

The standard measure for the sale and purchase of coal, for this Province, is the chaldron of 36 minots, each minot to be heaped up.

52. In 75 bushels of wheat how many pints? 53. In 4800 pints, how many pints?

54. Reduce 42 chaldrons of 55. In 6048 pecks, how many chaldrons?

11 11 13 1

TIME.

The denominations of time are years, months, weeks, days, hours, minutes, and seconds.

TABLE.

60 seconds (s.) - make - 1 minute, marked m. 60 minutes - - 1 hour, - - h.

¶ 33,

¶ 33. [*

allon with its re, for measurcommonly sold ominations are ts, pints, and

ked pt. gal. bar. hhd. P. T. 1 cubic inches. 6 pints of wine, wes ?

e 39032 gills to

252 gallons to

Ξ.

g ale, beer, and parrels, gallons

arked qt. gal bar hhd. 2 cubic inches 0 pints of ale.

12528 pints to

rels?

24	Jours	1.	-		1	day,	•	•	d.
7.	days	` -	-	•	1	week, -		-	w.
'4	weeks	-			1	month,	-	•	mo
13	months.	1 day	and 6	hours.	1	common	. or)		

or 365 days and 6 hours, J Julian year, J - yr.

¶ 34. The year is also divided into 12 calendar months, which in the order of their succession are numbered as follows, viz.

January, J	lst mon	th, has	31 days.
------------	---------	---------	----------

February, 2d,		- 28	
March, 3d,	4	- 31	10-
April, 4th,	-	- 30	
May, 5th,		- 31	
June, 6th,	-	- 30	Ca
July, 7th,		- 31	ou
August, Sth,	-	- 31	lec
September 9th,	•	- 30	Fe
October 10th		- 31	
November 11th		- 30	
December 12th.	`	- 31	

Note. When any year can be divided by 4 without a remainder, it is called leap year, in which February has 29 days.

The number of days in each month may be easily fixed in the mind by committing to memory the following lines:

> Thirty days hath September, April, June and November, February twenty-eight alone; All the rest have thirty-one.

The first seven letters of the alphabet, A, B, C, D, E, F, G, are used to mark the several days of the week, and they are disposed in such a manner, for every year, that the letter A shall stand for the 1st day of January, B for the 2d, &c. In pursuance of this order, the letter which shall stand for *Sunday*, in any year, is called the *Dominical* letter for that year. The Dominical letter being known, the day of the week on which each month comes in may be readily calculated from the following couplet:

> At Dover Dwells George Brown Esquire, Good Carlos Finch And David Fryer.

These words correspond to the 12 months of the year, and the *first letter* in each word marks the day of the week on Ci tude; other cles,

60 so 60 m 30 d 12 si 12 si into : 62. secon

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1 34.

1 34

d. W. mo. yr. dar months,

bered as fol-

en any year d by 4 withder, it is calr, in which s 29 days.

easily fixed owing lines:

D, **E**, **F**, **G**, and they are the letter A 2d, &c. In and for Sunor that year. the week on calculated

re,

e year, and he week on

REDUCTION.

which each corresponding month comes in; whence any other day may be easily found. For example, let it be required to find on what day of the week the 4th of July falls, in the year 1827, the Dominical letter for which year is G. Good answers to July; consequently, July comes in on a Sunday; wherefore the 4th of July falls on Wednesday.

Note. There are two Dominical letters in leap years, one for January and February, and another for the rest of the year.

56. Supposing your age to 57. Reduce 475047465 sebe 15y. 19d. J1h. 37m. 45s., conds to years.

how many seconds old are you, allowing 365 days 6 hours to the year?

58. How many minutes from the 1st day of January to the 59. Reduce 325440 minutes 14th day of August, inclu-to days. sively?

60. How many minutes from the commencement of the war between America and England, April 19th, 1775, to the how many years? settlement of a general peace,

which took place Jan. 20th, 17832

61. In 4079160 minutes,

CIRCULAR MEASURE, OR MOTION,

Circular measure is used in reckoning latitude and longitude; also in computing the revolution of the earth and other planets round the sun. The denominations are circles, signs, degrees, minutes and seconds.

TABLE.

60	seconds (") make		1	minute, m	arked `	1
60	minutes	-	1	degree, -	-	Ð
30	degrees	-	1	sign, -	-	s
12	signs, or 360 degrees,	-	1	circle of the zo	diac.	

Note. Every circle whether great or small, is divisible into 360 equal parts, called degrees.

62. Reduce 9s. 13º 25' to 63. In 1020300', how many seconds. degrees ? -

G 2

The following are denominations of things not included in the tables :---

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- 12 particular things make I dozen. 12 dozen
 - - 1 gross.
- 12 gross, or 144 dozen, - 1 great gross. -Also,

20 particular things make 1 score. 6 points make 1 line, (used in measuring the length of 12 lines 1 inch f the rods of clock pendulums. 1 hand } used in measuring the height of 4 inches horses.

1 fathom used in measuring depths at sea. 6 feet 112 pounds make 1 quintal of fish. • 24 sheets of paper make 1 quire. 20 quires 1 ream.

SUPPLEMENT TO REDUCTION.

QUESTIONS.

1. What is reduction ? 2. Of how many varieties is reduction ? 3. what is understood by different denominations, as of money, weight, measure, &c.? 4. How are high denominations brought into lower? 5. How are low denominations brought into higher? 6. What are the denomination's of Halifax currency ? 7. What name is given to the currency of this Province ? 8. And why? 9. Are the ratios of the different denominations to each other the same as in English momey? 10. Will the rule for reduction of one denomination to another in Halifax currrency; apply to all currencies in which the denominations are of the same name? 11. What is the use of Troy weight and, what are the denominations ? 12. ---- avoirdupois weight ? the denominations ? 13. What distinction do you make between gross and net weight ? 14. What distinction do you make between long, square, and cubic measure? 15. What are the denominations in long measure? 16. --- square messure? 17. --- in cubic measure? 18. How do you multiply by 1-2? 19. When the divisor contains a fraction how do you proceed? 20. How is the superficial contents of a square figure found? 21. How is the solid contents of any body found in cubic measure? 22. How many solid or cubic fect of wood make a cord ? 23. What is understood by a cord foot ? 24. How many such feet make a cord ? 25. What are the denominations of dry measure? 26. ---- of wine measure? 27. --- of time? 28. - of circular measure ? 29. For what is circular measure used ? 30. How many rods in length is Gunter's chain? of how, many links does it consist ? how many links make a rod ? 31. How many rods in a mile ? 32. How many square rods in an acre? 33. How many pounds make 1 cwt.?

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s reduction? 3. money, weight, ght into lower ? ? 6. What are me is given to re the ratios of in English moation to another h the denominaof Troy weight upois weight? n make between make between denominations ----- in cubic hen the divisor the superficial olid contents of id or cubic fect cord foot? 24. denominations -of time? 28. measure used ? ow, many links low many rods How many 5.

EXERCISES:

1. In 154 dollars, at 5s. each, how many pounds, &c. Ans. 38£. 10s.

2. In 36 guineas, at 1£. 3s. 4d each, how many crowns, at 5s. 6d.? Ans. 131 crowns and 2s. 10d. over.

3. How many rings, each weighing 5pwt. 7grs., may be made of 3lb. 5oz. 16pwt. 2grs. of gold? Ans. 158.

4. Suppose a bridge to be 212 rods in length, how many times will a chaise wheel, 18 feet 6 inches in circumference, turn round in passing over it? Ans 189_{222}^{18} times.

5. In 470 boxes sugar, each 26lb., how many cwt.?

6. In 10lb. of silver, how many spoons, each weighing toz. 10pwt.?

7. How many shingles, each covering a space 4 inches one way and 6 inches the other, would it take to cover 1 square foot? How many to cover a roof 40 feet long, and 24 wide? (See \P 25.) Ans. to the last, 5760 shingles. 8. How many cords of wood in a pile 26 feet long 4 feet

wide, and 6 feet high? Ans. 4 cords, and 7 cord feet. 9. There is a room 18 feet in length, 16 feet in width,

and 8 feet in height; how many rolls of paper, 2 feet wide, and containing 11 yards in each roll, will it take to cover the walls? $Ans. 8_{16}^{16}$.

10. How many cord feet in a load of wood $6\frac{1}{2}$ feet long, 2 feet wide, and 5 feet high? Ans. $4\frac{1}{16}$ cord feet.

11. If a ship sail 7 miles an hour, how far will she sail, at that rate, in 3w. 4d. 16h?

12. A merchant sold 12 hhds. of brandy, at \$3 a gallon; how much did each hogshead come to, and to how much in currency did the whole amount?

13. How much cloth, at 7s. a yard, may be bought for 29£. 1s?

14. A goldsmith sold a tankard for $10\pounds$ 8s. at the rate of 5s. 4d. per ounce; how much did it weigh?

15. An ingot of gold weighs 2lbs. Soz. 16pwt.; how much is it worth at 3d. per pwt.?

16. At 11 pence a pound, what will 1 T. 2cwt. 3qrs. 16lb. of lead come to ?

17. Reduce 14445 ells Flemish to ells English.

18. There is a house, the roof of which is $44\frac{1}{2}$ feet in length, and 20 feet in width, on each of the two sides; if 3 shingles in width cover one foot in length, how many

ADDITION OF COMPOUND NUMBERS.

shingles will it take to lay one course on this roof? if 3 courses make one foot, how many courses will there be on one side of the roof? how many shingles will it take to cover one side? — to cover both sides?

Ans. 16020 shingles.

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19. How many steps, of 30 inches each, must a man take in travelling 54½ miles?

20. How many seconds of time would a person redeem in 40 years, by rising each morning $\frac{1}{2}$ hour earlier than he now does?

21. If a man lay up $\frac{1}{2}$ a dollar each day Sundays excepted, how many pounds would he lay up in 45 years?

22. If 9 candles are made from 1 pound of tallow, how many dozen can be made from 24 pounds and 10 ounces?

23. If one pound of wool make 60 knots of yarn, how many skeins, of ten knots each, may be spun from 4 pounds 6 ounces of wool?

Addition of Compound Numbers.

¶ **35.** 1. A boy bought a knife for 9 pence, and a comb for 3 pence; how much did he give for both? Ans. 1 shilhing.

2. A boy gave 2s. 6d. for a slate, and 4s. 6d. for a book; how much did he give for both?

3. Bought one book for 1s. 6d., another for 2s. 3d., another for 7d.; how much did they all cost? Ans. 4s. 4d.

4. How many gallons are 2qts.+3qts.+1qt. ?

5. How many gallons are 3 qts. + 2 qts. + 1 qt. + 3 qts. + 2 qts.?

6. How many shillings are 2d + 3d + 5d + 6d + 7d?

7. How many pence are 1qr. + 2 qrs. + 3 qrs. + 2 qrs.+1qr. ?

8. How many pounds are 4s. + 10s. + 15s. + 1s.?

9. How many minutes are $30 \sec 45 \sec 20 \sec 2$

10. How many hours are 40 min. +25 min. +6 min.?

11. How many days are 4h + 8h + 10h + 20h?

12. How many yards in length are 1f. + 2f. + 1f.

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ays exceptirs? allow, how 10 ounces? yarn, how m 4 pounds

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and a comb Ans. 1 shil-

for a book;

2s. 3d., an-Ins. 4s. 4d.

-1 qt. +3

l.+7d ? rs.+2 grs.

1s. ? 20sec ? + 6 min. ? 20h. ? - 1f. ADDITION OF COMPOUND NUMBERS,

13. How many feeet are 4 in. +8 in. +10 in. +2in. +1 inch?

14. How much is the amount of 1yd 2ft. 6in + 2yds. 1 ft. 8 inches?

15. What is the amount of 2s. 6d. +4s. 3d. +7s. 8d.?

16. A man has 2 bottles, which he wishes to fill with wine; one will contain 2 gal. 3 qts. 1 pt. and the other 3 qts.; how much wine can be put in them?

17. A man bought a horse for $15\pounds$ 14s. 6d., a pair of oxen for $20\pounds$. 2s. 8d., and a cow for $5\pounds$. 6s. 4d.; what did he pay for all ?

When the numbers are large it will be most convenient to write them down, placing those of the same kind, or denomination, directly under each other, and, beginning with those of the least value, to add up each kind separately.

OPERATION.

¶ 35.

1 ns. 41	3	6
5	6	4
20	2	8
15	14	6
£.	s.	d.

In this example, adding up the column of pence, we find the amount to be 18 pence, which being == 1s. 6d., it is plain that we may write down the 6d. under the column of pence, and reserve the 1s. to be added in with the other shillings.

Next, adding up the column of shillings, together with the 1s. which we reserved we find the amount to be 23s. $=1\pounds$. 3s. Setting the 3s under its own column, we add the 1£. with the other pounds, and, finding the amount to be 41£. we write it down, and the work is done.

Ans. 41£. 3s. 6d.

Note. It will be recollected, that, to reduce a lower into a higher denomination, we divide by the number which it takes of the lower to make one of the higher denomination. In addition, this is usually called *carrying* for that number : thus, between pence and shillings, we carry for 12, and between shillings and pounds, for 20, &c.

The above process may be given in the form of a general RULE for the Addition of Compound Numbers.

I. Write the numbers to be added so that those of the same denomination may stand directly under each other.

II. Add together the numbers in the column of the lowest denomination, and carry for that number which it takes of

ADDITION OF COMOPUND NUMBERS.

the same to make 1 of the next higher denomination, Proceed in this manner with all the denominations, till you come to the last, whose amount is written as in simple numbers.

Proof. The same as in addition of simple numbers. EXAMPLES FOR PRACTICE.

.11 1.	HALIFAX CURRENCY.	

,							
£	S,	d, qr.	£	s: d.	1 ' es.	£ s.	`d,
46	11	3 2	72	9 61	18	3 19) 4
16	7	: 4 4	18	0 101		8 17	10
538	19	7 1	36	16 6		15	4
	0	·····		and the second	- ' - I		
£	·s.	d. '	£	s. d.	- : £	S.	d. 🕐
14	· 0	71	37	15 8	61	3	24
8	15	3	14	12 93	7	16	8
62	4	7	17	14.9	29	13 1	101
4	17	8	23	10 91	12	16	2
23	0	43.	× 8	60	0	7	59
6	6	7	14	0 5	24	13	0
91	0	10‡	54	$27\frac{1}{2}$	- 5	0 1	103]
			-		-		

No examples in Federal Money are here introduced, although the general rule for the addition of all compound numbers is precisely applicable to the addition of Federal Money, since that consists of different denominations. In Federal Money the denominations increase and decrease in a decimal ratio. The pupil is therefore referred to the rules for the Addition, Subtraction Multiplication and Division of Decimals, which are the same absolutely with the rules for the addition, subtraction, multiplication and division of Federal Money.

TROY WEIGHT.

lb.	oz.	pwt.	gr.	oz.	pwt.		02.	pwt.	gr.
36	7	10	11	6	14	9		-	ĭ 8
42	6	9	13	9	6	16		13	16
81	7	16	15.	3	11	10	3	7	4
							-		
	_								

TI viz., 3 na.

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2 p

23 c 19 c how

Bought a silver tankard, weighing 21b. 3 oz., a silver cup, weighing 3 oz. 10 pwt. and a silver thimble, weighing 2 pwts. 13 grs.; what was the weight of the whole?

AVOIRDUPOIS WEIGHT.

T. 14 25 7	cwt. 11 0 18 /	qr. 1 2 0	16 16 11 25	oz. 5 8 11	dr. 10 15 9	cwt. 16	qr. 3 3	lb. 18 16 22	oz. 6 8 11	dr. 14 12 10
		、 、								

A man bought 5 loads of hay, weighing as follows, viz. 23 cwt (= 1 T. 3 cwt.) 2 qrs. 17 lb.; 21 cwt. 1 qr. 19 lb.; 19 cwt. 0 qr. 24 lb.; 24 cwt. 3 qr.; 11 cwt. 0 qr. 1 lb.; how many tons in the whole?

CLOTH MEASURE.

yds.	qr.	n.	<i>E</i> . <i>F</i> .	qr.	na:	,	EE	qr.	na:
*36	ì	2	41	Î	2		75	-4	2
41	2	3	57	5	8		35	7	C
65	7	0	57.	0	3		28	3	1
				<u></u>					
		4							

There are four pieces of cloth, which measure as follows, viz., 37 yds. 2 qrs. 1 na.; 18 yds. 1 qr. 2 na.; 46 yds. 3 qrs. 3 na.; 12 yds. 0 qr. 3 na.; how many yards in the whole?

LONG MEASURE.

	deg. 59	mi. 46	fur. 6	r. 29	ft. 15	in. 10	bar. 2	mi. 3	fur. 7	pol.
	246 678	39 53	17	36 24	14 9	6 7	1	8 `	6	27
_										

¶ 35,

1 35.

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abers.

 $\begin{array}{c} d. \\ 2\frac{1}{2} \\ 8 \\ 10\frac{1}{4} \\ 2 \\ 5\frac{6}{4} \\ 0 \end{array}$

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duced, alcompound of Federal tions. In ecrease in to the rules Division of e rules for livision of

ADDITION OF COMPOUND NUMBERS.

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for 1s. 2. A how m 3. A

how m 4. Bo price of costs? 5. A how mu 6. A quarts; 7. Ho

4 gal.— 4 gal.—

1 gal, 3 8. Ho

inches, -10in? 9. Wł 10. Ha 3£ --15s 11. A for 5£ 14

	LA	ND OR	SQUARE	M	EAS	URE.	
Pol.	ft.	in.	A. r.	ood.	pol.	ft.	in.
36	179	137	56	3	37	245	228
19	248	119	29	1	28	93	25
12	96	75	416	2	31	128	119

There are 3 fields which measure as follows, viz. 17 A. 3r. 16p.: 28 A. 5r. 18p.; 11A. 0r. 25p.; how much land in the three fields?

SOLID OR CUBIC MEASURE.

To	n. ft.	in.	yds.	ft.	in.	cords.	ft.
29	Š6	1229	75	22	1412	37	119
12	-19	64	· '9	26	195	4	110
8	11	917	3	19	1091	48	127
				-			

WINE MEASURE.

hhds.	gal.	<i>qts</i> .	pts.	tun. 37	hhd.	gal.	q ts.	
27	39	3	Ó	19	1	50	1	
9	13	0	1	28	2	0	0	

A merchant bought two casks of brandy, containing as follows, viz. 70 gal. 3 qts.; 67 gal. 1qt.; how many hogsheads of 63 gal. each in the whole?

DRY MEASURE.

Bush.	р.	qt.	pt.			Ch.	bus.	p.	qt.
36 10	2 3	-5 7	1	~	١	48	27	-3 1	5
								-	.

¶ 35.

iz. 17 A. nuch land

cords. ft.

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1 36.

SUBTRACTION OF COMPOUND NUMBERS.

85

TIME.

Y.	mo.	w.	<i>d.</i>	h.	m.	s.	Y.	mo.	w.	d.
75	11	3	6	23	55	11	40	3	1	5
84	9	2	0	16	42	18	16	7	0	4
92	6	0	5	5	18	5	27	5	2	0
							·			,

Subtraction of Compound Numbers

36. 1. A boy bought a knife for 9 pence, and sold it for 1s. 4d.; how much did he gain by the bargain?

2. A boy bought a slate for 2s. 6d., and a book for 3s. 6d.; how much more was the cost of the book than of the slate? 3. A boy owed his playmate 2s.; he paid him 1s. 6d.;

how much did he then owe him?

4. Bought two books; the price of one was 4s. 6d., the price of the other 3s. 9d.; what was the difference of their costs ?

5. A boy lent 5s. 3d.; he received in payment 2s. 6d.; how much was then due?

6. A man has a bottle of wine containing 2 gallons and 3 quarts; after turning out 3 quarts how much remained?

7. How much is 4 gal, less 3 gal.? 4 gal.— (less) 2qt.? 4 gal.-1qt.? 4 gal. - 1 gal. 1qt.? 4 gal. - 1 gal. 2qts? 4 gal. - 1 gal. 3qts? 4 gal. - 2 gal. 3qts? 4 gal. 1 qt. -1 gal, 3 qts.?

8. How much is 1ft. — (less) 6in? 1ft. — 8 in? 6ft. 3 inches, -1 ft. 6 in. 7ft. Sin. - 4ft. 2in? 7ft. Sin. - 5ft. 10in?

9. What is the difference between $4\pounds$ 6s. and $1\pounds$ 8s. ?

10. How much is $3\pounds$ —(less) 1s,? $3\pounds$ —2s. $3\pounds$ —3s.? 3£ -15s? 3£ 4s.-2£ 6s? 10£ 4s. -5£ 8s?

11. A man bought a horse for 30£ 44. Sd., and a cow for $5\pounds$ 14s. 6d.; what is the difference of their costs?

qt. 5

OPERATION. £. s. d. Minuend, 30 4 8 Subtrahend, 5 14 6 As the two numbers are large, it will be convenient to write them down, the less under the greater, pence under pence, shillings under shillings, &c. We may now take 6d. from 8d., and

Ans. 24 10 2 $\$ may now take 6d. from 8d., and there will remain 2d. Proceeding to the shillings, we cannot take 14s from 4s., but we may borrow as in simple numbers, one from the pounds,=20s., which joined to the 4s. makes 24s. from which taking 14s. leaves 10s, which we set down. We must now carry 1 to the 5£ making 6£ which taken from 30£ leaves 24£ and the work is done.

Note. The most convenient way in borrowing is, to subtract the subtrahend from the figure borrowed, and add the difference to the minuend. Thus, in the above example, 14 from 20 leaves 6, and 4 is 10.

The process in the foregoing example may be presented in the form of a RULE for the Subtraction of Compound Numbers.

I. Write down the sums or quantities, the less under the greater, placing those numbers which are of the same denomifation directly under each other.

11. Beginning with the least denomination, take successively the lower number in each denomination from the upper, and write the remainder underneath, as in subtraction of simple numbers.

III. If the lower number of any denomination be greater than the upper, borrow as many units as make one of the next higher denomination, subtract the lower number therefrom, and to the remainder add the upper number, remembering always to add one to the next higher denomination for that which you borrowed.

Proof. Add the remainder and the subtrahend together, as in subtraction of simple numbers; if the work be right, the amount will be equal to the minuend.

EXAMPLES FOR PRACTICE.

HALIFAX CURRENCY.

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35	12	4	71	12	5

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520 109	11 17	 3 4		14 19	7	

SUBTRACTION OF COMPOUND NUMBERS.

MISCELLANEOUS EXAMPLES.

1. A merchant sold goods to the amount of $136 \pounds$ 7s. $6\frac{1}{2}d$, and received in payment 50£ 10s. 42d; how much remained due? Ans. $85 \pounds$ 17s. $1\frac{3}{4}$ d.

2. A man bought a farm for 1256£ 10s, and, in selling it, lost 87£ 10s. 6d; how much did he sell it for ?

Ans, 1168£ 198.6d.

3. A man bought a horse for $27\pounds$ and a pair of oxen for 19£ 12s. 81d; how much was the horse valued more than the oxen?

4. A merchant drew from a hogshead of molasses, at one time, 13 gal. 3qts; at another time, 5gal. 2qts 1pt; what quantity was there left? Ans. 43gal. 2qts. 1pt.

5. A pipe of brandy, containing 118 gal. sprang a leak, when it was found only 97gal. 3qts. 1pt. remained in the cask; how much was the leakage?

6. There was a silver tankard which weighed 3lb. 4ez.; the lid alone weighed 5oz. 7pwt. 13grs; how much did the tankard weigh without the lid?

7. From 15lb. 2oz. 5pwt. take 9oz. 9pwt. 10grs.

8. Bought a hogshead of sugar, weighing 9cwt. 2qrs. 17lb; sold at three several times as follows, viz. 2cwt. 1qr. 11ib. 5oz; 2qrs. 18b. 10oz; 25b. 6oz; what was the weight of sugar which remained unsold?

Ans. 6cwt. 1gr. 17lb. 11oz.

9. Bought a piece of black broadcleth, containing 36yds, 2qrs; two pieces of blue, one containing 10 yds. 3qrs. 2na. the other 18 yds. 3qrs. 3na; how much more was there of the black than of the blue?

10. From 28 miles, 5 fur. 16r. take 15m 6 fur. 26r 12ft 11, A farmer has two mowing fields; one containing 13

1 36, 37.

acres 6 roods; the other, 14 acres 3 roods: he has two pastures also; one containing 26 A. 2r. 27p; the other, 45 A. 5r. 33p: how much more has he of pasture than of mowing?

12. From 64A. 2r. 11p. 29ft. take 26A. 5r. 34p. 132ft.

13. From a pile of wood, containing 21 cords, was sold, at one time, 8 cords 76 cubic feet; at another time, 5 cords 7 cord feet; what was the quantity of wood left?

14. How many days, hours and minutes of any year will be future time on the 4th day of July, 20 minutes past 3 o'clock, P. M? Ans. 180 days, 8 hours, 40 minutes.

15. On the same day, hour and minute of July, given in the above example, what will be the difference between the past and future time of that month?

16. A note, bearing date Dec. 28th 1826, was paid Jan. 2d, 1827; how long was it at interest?

The distance of time from one date to that of another may be found by subtracting the first date from the last, observing to number the months according to their order. (¶34.)

OPERATION.

A. D.	{ 1827. 1826.	1st m. 2d day. 1228

Note. In casting interest, each month is reckoned 30 days.

Ans. 0 0 4 days.

17. A note, bearing date Oct. 20th, 1823, was paid April 25th, 1825; how long was the note at interest?

18. What is the difference of time from Sept. 29, 1816, to April 2d, 1819? Ans. 2y. 6m. 3d.

19. London is 51° 32', and Montreal 45° 30', N. latitude; what is the difference of latitude between the two places? Ans. 6° 2.'

20. Montreal is 73° 20', and the city of Washington is 77° 43' W. longitude; what is the difference of longitude between the two places? Ans. 4° 23'.

21. The island of Cuba lies between 74° and 85° W. longitude; how many degrees in longitude does it extend?

¶ 37. 1. When it is 12 o'clock at the most easterly extremity of the island of Cuba, what will be the hour at the most westerly extremity, the difference in longitude being 11°?

Note. The circumference of the earth being 360°, and the earth performing one entire revolution in 24 hours, it 2. M 77° 43' what is

3. Lo Islands 6 o'cloc hour in

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t. 29, 1816, 2y. 6m. 3d. 80', N. latieen the two Ans. 6° 2.' ashington is Clongitude Ans. 4° 23'. nd 85° W. it extend ? easterly exhe hour at ngitude be-

> 360°, and 4 hours, it

¶ 37, 38. MULTIPLICATION AND DIVISION, &C.

follows, that the motion of the earth on its surface, from west to east, is

15° of motion in 1 hour of time; consequently,

1º of motion in 4 minutes of time, and

1' of motion in 4 seconds of time.

From these premises it follows, that, when there is a difference in longitude between two places, there will be a corresponding difference in the hour, or time of the day, The difference in longitude being 15°, the difference in time will be one hour, the place *easterly* having the time of the day 1 hour *earlier* than the place *westerly*, which must be particularly regarded.

If the difference in longitude be 1°, the difference in time will be 4 minutes, &c.

Hence,—If the difference in longitude, in degrees and minutes, between two places, be multiplied by 4, the product will be the difference in time, in minutes and seconds, which may be reduced to hours.

We are now prepared to answer the above question.

11º 4

44 minutes.

Hence, when it is 12 o'clock at the most easterly extremity of the island, it will be 16 minutes past 11 o'clock at the most western extremity.

2. Montreal being 73° 20' W. longitude and Washington, 77° 43'; when it is 3 o'clock at the city of Washington, what is the hour at Montreal?

Ans. 17 minutes 32 seconds past 3 o'clock. 3. Lower Canada being about 73°, and the Sandwich Islands about 155° W. longitude, when it is 28 minutes past 6 o'clock, A. M. at the Sandwich Islands, what will be the hour in Lower Canada?

Ans. 12 o'clock at noon, lacking 4 minutes.

Multiplication & Division of Compound Numbers.

¶ 38. 1. A man bought 2 yards of cloth, at 1s. 6d. per yard; what was the cost? H 2 2. If 2 yards of cloth cost 3 shillings, what is that per yard?

3. A man has three pieces of cloth, each measuring 10 yds. 3qrs.; how many yards in the whole?

4. If 3 equal pieces of cloth contain 32yds. 1 qr., how much does each piece contain ?

5. A man has five bottles, each containing 2 gal. 1 qt. 1 pt.; how much wine do they all contain?

6. A man has 11 gal. 3qts. 1pt. of wine, which he would divide equally into 5 bottles; how much must he put into each bottle?

7. How many shillings are 3 times $Sd? = 3 \times 9d?$ = $3 \times 10d? = 4 \times 7d? = 7 \times 6d? = 10 \times 9d? = 2 \times 3qrs? = 5 \times 2qrs?$

8. How much is one third of 2 shillings ? — $\frac{1}{3}$ of 2s 3d? — $\frac{1}{3}$ of 2s. 6d? — $\frac{1}{3}$ of 2s. 4d? — $\frac{1}{3}$ of 3s. 6d? — $\frac{1}{10}$ of 7s. 6d? — $\frac{1}{2}$ of $\frac{1}{2}$ d? — $\frac{1}{2}$ of $\frac{2}{2}$ d?

9. At $1\pounds$ 5s. $8\frac{3}{4}$ d. per yard, 10. If 6 yards of cloth cost what will 6 yards of cloth $7\pounds$ 14s. $4\frac{1}{2}$ d, what is the price cost?

Here as the numbers are large, it will be most convenient to write them down before multiplying and dividing.

OPERATION. L s. d. yr.

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OPERATION. £ s. d. qr.

1 5 8 3 price of 1 yard 6)7 14 4 2 cost of 6 yards.

Ans. 7 14 4 2 cost of 6 yards

1. 5 8 3 price of 1 yard.

6 times 3 qrs. are 18qrs. = 4d. and 2qrs. over; we set tained in $7\pounds$ 1 time, and 1 \pounds down the two qrs; then, 6 times 8d. are 48d, and 4 to carry makes 52d. = 4s. and 4d. over; we write down the quotient, and reduce the remainder (1 \pounds) to shillings, (20s,) which, with the given again 6 times 5s. are 30s. and 4 to carry makes 34s. = 1 \pounds and 14s. over; 6 times 1 \pounds are 6 \pounds , and one to carry makes 7 \pounds , which we write down, and it is plain, that the united products arising over; 4d. = 16 qrs. which, ¶ 38.

gs, what is that per

each measuring 10 e?

32yds. 1 qr., how

ntaining 2 gal. 1 qt. aig?

ine, which he would ch must he put into

 $\frac{10 \times 9d}{2} = \frac{3 \times 9d}{2}$

ings ? — $\frac{1}{3}$ of 2s 3d? - $\frac{1}{3}$ of 3s. 6d? — $\frac{1}{10}$

6 yards of cloth cost 41d, what is the price

ll be most convenient g and dividing.

d. gr. 4 2 cost of 6 yards.

8 3 price of 1 yard.

eding after the manhort division, 6 is conhort division, 6 is conhort division, 6 is conhort, 1 time, and 1 \pounds e write down, the , and reduce the re-($1\pounds$) to shillings, hich, with the given , (14s,) make 34s; goes 5 times, and 4 4s. reduced to pence which with the give, (4d,) make 52d; 6 goes 8 times, and 4d hd = 16 qrs. which, from the several denomina-with the given qrs. (2) = 18tions is the real product arising from the whole compound number. (2) = 18and it is plain, that the united quotients arising from the several denominations, is the real quotient arising from the

whole compound number.

11. Multiply 3£ 4s. 6d. 12. Divide 22£ 11s. 6d. by 7.

13. What will be the cost 14. At 2£ 12s 6d. for 5 of 5 pairs of shoes at 10s. 6d. pairs of shoes, what is that a pair?

17. How many yards of cloth will be required for 9 yds. 3qrs. 3na, what does 1 coats, allowing 4 yards 1qr. coat contain? 3na. to each?

19. In 7 bottles of wine, 20. If 5 gal. 1 gill of wine each containing 2qts. 1pt. 3 be divided equally into 7 botgills, how many gallons? tles, how much will each con-

tain?

21. What will be the 22. If 8 silver cups weigh weight of 8 silver cups, each 3lb. 9oz. 1pwt. 16grs., what weighing 5oz. 12pwt 17grs? is the weight of each?

23. How much sugar in 12 hogsheads, each containing heads, how much will each 9c wt. 3qrs. 21lb?

25. In 15 loads of hay, each weighing 1T. 3cwt. 2qrs. with 17T. 12cwt. 2qrs. of hay, how many tons?

When the multiplier or divisor, exceeds 12, the operations of multiplying and dividing are not so easy, unless they be composite numbers; in that case, we may make use of the component parts, or factors, as was done in simple numbers.

Thus 15, in the example 15 being a composite numabove is a composite number, ber and 3 and 5 its compoproduced by the multiplica-nent parts, or factors, we may









tion of 3 and 5, $(3 \times 5 = 1)$	divide 17T. 12cwt. 2qrs. by
15.) We may therefore,	one of these component parts
multiply 1T. 3cwt. 2qrs. by	or factors, and the quotient
one of those component parts,	thence arising by the other,
or factors, and that product by	which will give the true an-
the other, which will give the	swer, as already taught,
true answer, as has been al-	(¶ 20.)
ready taught (¶11.)	

OPERATION.

T. cwt. 1 3	gr. 2 3 one of the factors.	One factor,	OPERATIO <i>T. cwt.</i> 3)17 12			on. T 2	
3	10 · 2	The other facto	r ,5	5)5	17	2	
17	12	2 the answer.	A	ńs,	ì	3	·2

27. What will 24 barrels 28. Bought 24 barrels of of flour cost, at 2£, 12s. 4d. flour for 62£ 16s; how much a barrel? || was that per barrel?

29. What will 112lb. of sugar cost at 71d. per lb.? Note. 8, 7, and 2, are fac-lb? 30. If 1cwt. of sugar cost 32, 7s. 8d., what is that per

tors of 112.

31. How much brandy in 84 pipes, each containing 112 brandy, containing 9468 gal. gal. 2qts. 1pt, 3g? 1qt. 1pt; how much in a pipe?

33. What will 139yds. of cloth cost, at 3£, 6s. 5d. per cloth for 461£ 11s. 11d; yard? what was that per yard?

139 is not a composite number. We may, however, decompose this number thus, by the multiplication of small 139-100+30+9. umbers, the better way is to

We may now multiply the divide after the manner of price of 1 yard by 10, which long division, setting down will give the price of 10 yards, the work of dividing and reand this product again by 10, ducing in manner as follows: which will give the price of 100 yards. Ti sente Ruli

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¶ 38.

OPERATION. T. cwt. gr 2 12 3)17 17 2 ,5)5 3 2 s, l

24 barrels of is; how much rel?

of sugar cost at is that per

84 pipes of ing 9468 gal. uch in a pipe? 139 yards of £ 11s. 11d; er yard? isor is such a t be produced tion of small tter way is to manner of setting down ding and rer as follows:

We may then multiply the price of 10 yards by 3, which - 13 will give the price of 30 yards and the price of 1 yard by 9, which will give the price of 9 yards, and these three products, added together, will evidently give the price of 139 yards; thus:

1 38.

τ.	S.	и.		-	
3	6	5 price	of	1	yard.
		10			-

4 2 price of 10 yards. 33 10

332 8 price of 100 yds. 1 99 12 29 17 9 price of

Note. In multiplying the lings, (11s,) making 891s, in price of 10 yards (33£ 4s which the divisor is contained 2d.) by 3, to get the price of 6 times, (6s,) and a remainder 30 yards, and in multiplying of 57s, which must be reducthe price of 1 yard (3± 6s. ed to pence, multiplying it by 5d.) by 9, to get the price of 12, and bringing in the given 9 yards, the multipliers, 3 pence, (11d,) together makand 9, need not be writtening 695d, in which the dividown, but may be carried in sor is contained 5 times, (5d,) the mind. and no remainder.

> The several quotients, 3£ 6s. 5d. evidently make the answer.

The processes in the foregoing examples may now be presented in the form of a

RULE for the Multiplication of RULE for the Division of Com-Compound Numbers. pound Numbers.

1. When the multiplier does 1. When the divisor does not exceed 12, multiply suc-not exceed 12, in the manner cessively the numbers of each of short division, find how denomination, beginning with many times it is contained in

£ 39)461 417	s. 11	d. 11(3£
si 44 20	 	
891 834	′6	
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695	(34.	

The divisor, 139, is contain-6 price of 30 yds. ed in 461 \pm 3 times (3 \pm ,) and 9 yds. a remainder of $44\pounds$, which must now be reduced to shil-461 11 11 price of 139 yds. lings, multiplying it by 20, and bringing in the given shil-

the least, as in multiplication the highest denomination, unof simple numbers, and carry der which write the quotient, as in addition of compound and if there be a remainder, numbers, setting down the whole product of the highest nomination, adding thereto the denomination.

denomination, and divide as before; so continue to do through all the denominations and the several quotients will be the answer

II. If the multiplier exceed be the answer. 12, and be a composite number, we may multiply first by one of the component parts, that product by another, and be more than two; the last product will be the product required. II. If the divisor exceed 12, and be a composite, we may divide first by one of the component parts, that quotient by another, and so on, if the comtwo, the last quotient will be the quotient required.

III. When the multiplier III. When the divisor exexceeds 12, and is not a composite, multiply first by 10, ite number, divide after the and this product by 10, which manner of long division, setwill give the product for 100; ting down the work of dividand if the hundreds in the muling and reducing.

tiplier be more than one, multiply the product of 100 by the number of hundreds; for the tens, multiply the product of 10 by the number of tens; for the units, multiply the multiplicand; and these several products will be the product required.

*EXAMPLES FOR PRACTICE,



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mination, une the quotient, a remainder, next less deling thereto the if any, of that and divide as ontinue to do denominations quotients will

visor exceed 12, site, we may dine of the comhat quotient by on, if the combe more than uotient will be quired.

the divisor exs not a composlivide after the g division, setwork of dividing.

> s. d. 4 11 48

Mult.ply by	£ s. d. 98 3 10 78	£ s. d. 64 11 2 93 93	
	986 11 4	892 5 3 145	
£	s. d.	£ s. d	
Divide 77	11 9 by 18.	143 2 3 by 2	1.
" 140	2 3 " 21.	1950 7 4 " 98	3
" 360	5 2 "133.	47 9 6 " 1	I.
" 7856	8 9 " 197.	562 8 3 " 2	D.

COMPOUND NUMBERS

MISCELLANEOUS EXAMPLES.

1. What will 359 yards of 2. Bought 359 yds. of cloth cloth cost, at 4s. 7½d. per for 83£ 0s 4½d; what was yard?

3 In 241 barrels of flour, 4. If 441cwt. 13lb. of flour each containing 1cwt 3qr. be contained in 241 barrels, 9lb; how many cwt? how much in a barrel?

5. How many bushels of wheat in 135 bags, each containing 2 bu. 3 pks ? $3 \times 9 \times 5 = 135$. 6. If 371bu. 1pk. of wheat be divided equally into 135 bags, how much will each bag contain ?

7. What will 35cwt. of tobacco cost, at 3s $10\frac{1}{2}$ d. per of tobacco, what is that per b?

9. If 14 men build 12 rods 6 feet of wall in one day, how many rods will they build in $7\frac{1}{2}$ days? 10. If 14 men build 92 rods 12 feet of stone wall in $7\frac{1}{2}$ days, how much is that per day?

¶ **39.** 1. At 10s. per yard, what will 17849 yards of cloth cost ?

Note. Operations in multiplication of pounds, shillings, pence, or of any compound numbers, may be facilitated by

taking aliquot parts of a higher denomination. Thus, in this last example, if the price had been 20s. i. e. $1\pounds$ per yard, it is clear, the price of the whole would have been equal to the whole number of yards in pounds, 17849; but the price is 10s. i. e. $\frac{1}{2}\pounds$ per yard, and so the price of the whole will be equal to $\frac{1}{2}$ the number of yards, $1^{7}\frac{8}{2}4^{9}$ in pounds; 8924 $\frac{1}{2}\pounds$, or 8924 \pounds 10s.

When one quantity is contained in another exactly 2, 3, 4, 5, &c. times, it is called an *aliquot* or *even* part of that quantity; thus 6d. is an aliquot part of a shilling, because $6d. \times 2=1$ shilling; so 3d. is an aliquot part of a shilling; $3d. \times 4=1s$. So 5s. is an aliquot part of a pound, for 5s. $\times 4=1\pounds$: and 3s. 4d. is an aliquot part of a pound, for 3s. $4d. \times 6=1\pounds$, &c.

From the illustration of the last example it appears, that, when the price per yard, pound, &c. is one of these aliquot parts of a shilling, or a pound, the cost may be found by dividing the given number of yards, pounds, &c. by that number which it takes of the price to make 1s. or $1\pounds$. If the price be 6d. we divide by 2; if 5s. we divide by 4; if 3s. 4d. by 6, &c. &c. This manner of calculating by aliquot parts, is called Practice.

2. What cost 34648 yards of cloth, at 10s. or $\frac{1}{2}\mathcal{L}$ per yard? — at 5s.= $\frac{1}{4}\mathcal{L}$ per yard? — at 4s.= $\frac{1}{5}\mathcal{L}$ per yard? — at 2s.= $\frac{1}{10}\mathcal{L}$ per yard? — at 2s.= $\frac{1}{10}\mathcal{L}$ per yard? — Ans. to last, 3464 \mathcal{L} 16s.

3. What cost 7430 pounds of sugar, at $6d = \frac{1}{2}s$. per lb? — at $4d = \frac{1}{3}s$. per lb? — at $3d = \frac{1}{4}s$ per lb? — at $2d = \frac{1}{6}s$. per lb? — at $1\frac{1}{2}d = \frac{1}{5}s$. per lb?

Ans. to the last, 74^{30} s.=928s. 9d.=46£ 8s. 9d. 4. At 3£ 16s. per cwt, what will $2qrs.=\frac{1}{2}cwt. cost$? — what will $1qr.=\frac{1}{4}cwt. cost$? — what will 16lb.= $\frac{1}{4}cwt. cost$? — what will 14lb.= $\frac{1}{5}cwt. cost$? — what will 8lb.= $\frac{1}{14}cwt. cost$? Ans. to the last, 5s. 54d.

5. What cost 340 yards of cloth, at 12s. 6d. per yard? 12s. 6d.=10s. $(=\pm x)$ and 2s. 6d. $(=\pm x)$; therefore, ± 1 ; $(=\pm x)$

 $\begin{array}{rl} 170\pounds & = \text{cost at 10s. per yard.} \\ 42\pounds & 10\text{s.} = \text{at 2s. 6d.} & \text{per yard.} \end{array}$

Ans. 212£ 10s.=at 12s. 6d. per yard.

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SUPPLEMENT TO COMPOUND NUMBERS.

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'hus, in this £ per yard, en equal to ut the price the whole in pounds;

exactly 2, 3, part of that ng, because f a shilling; und, for 5s. a pound, for

ppears, that, these aliquot be found by &c. by that s. or 1£. If vide by 4; if lating by ali-

)s. or $\frac{1}{2}\mathfrak{L}$ per $4s = \frac{1}{5} \pounds$ per at $2s = \frac{1}{10} \pounds$ t, 3464£ 16s. $=\frac{1}{2}$ s. per lb? 1b? b? =46£ 8s. 9d. $=\frac{1}{2}$ cwt. cost? will 16lb.= t? —— what last, 5s. 54d. 6d. per yard? herefore,

rd. rd.

ard.

2s. 6d=1 of 10s.)170£ at 10s. per yard. 42£ 10s. at 2s. 6d. per yard.

Ans. 212£, 10s. at 12s. 6d. per yard.

SUPPLEMENT TO COMPOUND NUMBERS. QUESTIONS.

1. What distinction do you make between simple and compound numbers? (P 26.) 2. What is the sule for addition of compound numbers ? 3. ---- for subtraction of, &c. 4. There are three conditions in the rule given for multiplication of compound humbers : what are they, and the methods of procedure under each? 5. The same questions in respect to the division of compound numbers? 6. When the multiplier or divisor is encumbered with a fraction, how do you proceed? 7. How is the distance of time from one date to another found? 8. How many degrees does the earth revolve from west to east in 1 hour? 9. In what time does it revolve 10? Where is the time or hour of the day earlier-at the place most easterly of most westerly? 10. The difference in longitude between two places being known, how is the difference in time calculated? 11. How may operations, in the multiplication of compound numbers be far cilitated ? 12. What are some of the aliquot parts of £1 ? ---- of 15. ? -- of lowt? 13. What is this manner of operating usually called ?

EXERCISES.

1. A gentleman is possessed of 11 dozen of silver spoons, each weighing 3oz. 5pwt; 2 doz. of tea spoons, each weighing 15pwt. 14gr; 3 silver cans, each 9oz. 7pwt.; 2 silver tankards, each 21oz. 15pwt; and 6 silver porringers, each 11oz. 18pwt; what is the weight of the whole?

Ans: 181b. 4oz. 3pwt.

Note. Let the pupil be required to reverse and prove the following examples :

2. An English guinea should weigh 5pwt. 6gr; a piece of gold weighs 3pwt. 17gr ; how much is that short of the weight of a guinea?

3. What is the weight of 6 chests of tes, each weighing. 3cwt. 2qrs. 91b?

4. In 35 pieces of cloth, each measuring 27 yards, how many yards?

¶ 39.

SUPPLEMENT TO COMPOUND NUMBERS. ¶ 39, 40.

5. How much brandy in 9 casks, each containing 45 gal. 3qts. 1pt?

6. If 31cwt. 2qrs. 201b. of sugar be distributed equally into 4 casks, how much will each contain?

Note. The pupil will recollect that 8, 7, and 2 are factors of 112, and may be used in place of that number.

8. If S00cwt. of cocoa cost $18\pounds$ 13s. 4d. what is that per cwt? what is it per lb.?

9. What will 9¹/₁cwt. of copper cost at 5s. 9d. per lb?

10. If $6\frac{1}{2}$ cwt. of chocolate cost 72£. 16s. what is that per lb?

11. What cost 456 bushels of potatoes, at 2s. 6d. per bushel ?

Note. 2s. 6d. is 1 of 1£ (See ¶ 39.)

12. What cost 86 yards of broadcloth, at 15s. per yard? Note. Consult ¶ 39, ex. 5.

13. What cost 7846 pounds of tea, at 7s. 6d. per lb.? ______at 14s. per lb?_____13s. 4d?

14. At \$94'25 per cwt. what will be the cost of 2qrs. of tea? — of 3 qrs? — of 14lbs? — of 21 lbs? — of 16lbs? — of 24lbs?

Note. Consult ¶ 39, ex. 4 and 5.

15. What will be the cost of 2 pks. and 4qts. of wheat, at 8s. 6d. per bushel?

16. Supposing a meteor to appear so high in the heavens as to be visible at Montreal, 73° 20', at the city of Washington, 77° 43', and at the Sandwich Islands, 155° W. longitude and that its appearance at the city of Washington be at 7 minutes past 9 o'clock in the evening; what will be the hour and minute of its appearance at Montreal and at the Sandwich Islands ?

Fractions.

 \P **40.** We have seen, (\P 17,) that numbers expressing whole things are called *integers* or whole numbers; but that in division, it is often necessary to divide or break a whole thing into parts, and that these parts are called fractions, or broken numbers.

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It will be recollected, (¶ 14, ex. 11,) that when a thing or unit is divided into 3 parts, the parts or fractions are called thirds; when into four parts, fourths; when into six parts, sixths; that is, the fraction takes its name or denomination from the number of parts into which the unit is divided. Thus if the unit be divided into 16 parts, the parts are called sixteenths, and 5 of these parts would be 5 sixteenths, expressed thus, $\frac{1}{16}$. The number below the short line, (16,) as before taught, (¶ 17,) is called the denominator, because it gives the name or denomination to the parts; the number above the line is called the numerator, because it numbers the parts.

The denominator shows how many parts it takes to make a unit or whole thing; the numerator shows how many of, these parts are expressed by the fraction.

1. If an orange be cut into 5 equal parts, by what fraction is 1 part expressed? — 2 parts? — 3 parts? — 4 parts? — 5 parts? how many parts make unity or a whole orange?

2. If a pie be cut into 8 equal pieces, and 2 of these pieces be given to Harry, what will be his fraction of the piel if 5 pieces be given to John, what will be his fraction? what fraction or part of the pie will be left?

It is important to bear in mind, that fractions arise from division, ($\P17$,) and that the numerator may be considered a dividend, and the denominator a divisor, and the value of the fraction is the quotient; thus, $\frac{1}{2}$ is the quotient of 1 (the numerator) divided by 2 (the denominator;) $\frac{1}{4}$ is the quotient arising from 1 divided by 4, and $\frac{3}{4}$ is 3 times as much, that is, 3 divided by 4; thus, one fourth part of 3 is the same as 3 fourths of 1.

Hence, in all cases a fraction is always expressed by the sign of division.

 $\frac{2}{3}$ expresses the quotient, $\int 3$ is the dividend, or numerator.

of which) 4 is the divisor or denominator.

3. If 4 oranges be equally divided among 6 boys, what part of an orange is each boy's share?

A sixth part of an orange is $\frac{1}{6}$, and a sixth part of 4 oranges is 4 such pieces,= $\frac{1}{6}$. Ans. $\frac{1}{6}$ of an orange.

4. If 3 apples be equally divided among 5 boys, what part of an apple is each boys share? if 4 apples, what? if 2 apples, what? if 5 apples, what?

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FRACTIONS.

5. What is the quotient of 1 divided by 3? of 2 by 3?of 1 by 4? of 2 by 4? of 3 by 4? of 5 by 7? of 6 by 8? of 4 by 5? of 2 by 14?6. What part of an orange is a third part of 2 oranges? one fourth of 2 oranges? 1 of 3 oranges? 1 of three oranges? 1 of 4? 1 of 2? 1 of 5?1 of 3? 1 of 2?

A proper fraction. Since the denominator shows the number of parts necessary to make a whole thing, or 1, it is plain that when the numerator is less than the denominator, the fraction is less than a unit, or whole thing; it is then called a proper fraction. Thus, $\frac{1}{2}$, $\frac{2}{3}$, &c. are proper fractions.

An improper fraction. When the numerator equals or exceeds the denominator, the fraction equals or exceeds unity, or 1, and is then called an improper fraction. Thus, $\frac{6}{5}$, $\frac{3}{4}$, $\frac{1}{2}$, are improper fractions.

A mized number, as already shown, is one composed of a whole number and a fraction. Thus, 141, 135, &c. are mixed numbers.

7. A father bought 4 oranges, and cut each orange into 6 equal parts; he gave to Samuel 3 pieces, to James 5 pieces, to Mary 7 pieces, and to Nancy 9 pieces; what was each one's fraction?

Was James' fraction proper or improper? Why?

Was Nancy's fraction proper, or improper? Why? To change an improper fraction to a whole or mixed number.

¶ 41. It is evident that every improper fraction must contain one or more whole ones, or integers.

1. How many whole apples are there in 4 halves $(\frac{4}{2})$ of an apple? — in $\frac{6}{2}$? — in $\frac{6}{2}$? — in $\frac{19}{2}$? — ? in $\frac{29}{2}$ — in $\frac{49}{2}$? — in $\frac{120}{2}$? in $\frac{94}{2}$?

2. How many yards in $\frac{2}{3}$ of a yard? — in $\frac{2}{3}$ of a yard? — in $\frac{2}{3}$? — in $\frac{2}{3}$? — in $\frac{1}{3}$? — in $\frac{1}{3}$? — in $\frac{1}{3}$? — in $\frac{1}{3}$?

3. How many bushels in 8 pecks? that is, in $\frac{9}{4}$ of a bushel? ______ in $\frac{19}{4}$? ______ in $\frac{19}{4}$?

This finding how many integers, or whole things, are contained in any improper fraction is called reducing an improper fraction to a whole or mixed number. or of

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4. If I give 27 children $\frac{1}{4}$ of an orange each, how many oranges will it take ? It will take $\frac{27}{3}$; and it is evident, operation. that dividing the numerator 27, (= the number of parts contained in the fraction,) by the denominator 4, (= the

Ans. $6\frac{3}{4}$ oranges.

number of parts in 1 orange,) will give the number of whole oranges.

Hence, To reduce an improper fraction to a whole or mixed number,—RULE: Divide the numerator by the demominator; the quotient will be the whole or mixed number.

EXAMPLES FOR PRACTICE.

5. A man, spending $\frac{1}{6}$ of a pound a day, in 83 days would spend $\frac{8}{6}$ of a pound; how many pounds would that be?

Ans. 135£.

6. In ¹⁴/₆₀⁷ of an hour, how many whole hours?

The 60th part of an hour is a minute; therefore the question is evidently the same as if it had been, in 1417 minutes, how many hours? Ans. 2337 hours.

7. In $\frac{9763}{12}$ of a shilling, how many units or shillings? Ans. 730_{12}^{+3} shillings.

8. Reduce 14ff 8 to a whole or mixed number.

9. Reduce $\frac{36}{26}$, $\frac{706}{40}$, $\frac{875}{106}$, $\frac{4786}{1006}$, $\frac{3465}{450}$, to whole or mixed numbers.

To reduce a whole or mixed number to an improper fraction.

¶ 42. We have seen, that an improper fraction may be changed to a whole or mixed number; and it is evident that by reversing the operation, a whole or mixed number may be changed to the form of an improper fraction.

1. In 2 whole apples, how many halves of an apple? Ans. 4 halves; that is §. In 3 apples how many halves? in 4 apples? in 6 apples? in 10 apples? in 24? in 60? in 170? in 492?

2. Reduce 2 yards to thirds. Ans. $\frac{6}{3}$. Reduce $2\frac{2}{3}$ yards to thirds. Ans. $\frac{8}{3}$. Reduce 3 yards to thirds $-3\frac{1}{3}$ yards. $-3\frac{2}{3}$ yards. $-5\frac{2}{3}$ yards. $-5\frac{2}{3}$ yards. $-6\frac{2}{3}$ yards.

 $3\frac{3}{4}$ yards. $-5\frac{5}{4}$ yards. $-5\frac{5}{4}$ yards. $-5\frac{5}{4}$ yards. $-5\frac{5}{4}$ yards. $-5\frac{5}{4}$ yards. $-5\frac{5}{4}$ bushels. $-5\frac{5}{4}$ bushels. $-5\frac{5}{4}$ bushels. $-5\frac{5}{4}$ bushels. $-5\frac{5}{4}$ bushels.

4. In 16⁵/₁₂ pounds, how many $\frac{1}{12}$ of a pound?

 $\frac{12}{1.2}$ make 1 pound : if therefore, we multiply 16 by 12, that is, multiply the whole number by the denominator, the

FRACTIONS.

product will be the number of 12ths in $16\pounds$: $16 \times 12 = 192$ and this, increased by the numerator of the fraction, (5,) evidently gives the whole number of 12ths; that is, 47 of a pound, Ans.

OPERATION.

16 The pounds

12

192=12ths in 16 pounds, or the whole number. 5=12ths contained in the *fraction*.

197= 197, the answer.

Hence,' To reduce a mied number to an improper fraction,--Rule: Multiply the whole number by the denominator of the fraction, to the product add the numerator, and write the result over the denominator.

EXAMPLES FOR PRACTICE.

5. What is the improper fraction equivalent to 23% hours? Ans. $1\%^{1}$ of an honr.

6. Reduce 730_{12}^3 shillings to 12ths.

As $\frac{1}{12}$ of a shilling is equal to 1 penny, the question is evidently the same as, in 730s. 3d., how many pence?

Ans. ⁸7^{§3} of a shilling ; that is 8763 pence.

7. Reduce 1_{16}^{16} , 17_{46}^{26} , 8_{100}^{75} , 4_{100}^{716} , and 7_{456}^{218} to improper fractions.

8. In 15617 days, how many 24ths of a day?

Ans. $\frac{376}{24}$ = 3761 hours.

9. In 342³/₄ gallons, how many 4ths of a gallon? Ans. ¹³/₄⁷¹ of a gallon=1371 quarts.

To reduce a fraction to its lowest or most simple terms.

¶ 43. The numerator and the denominator, taken together, are called the *terms of the fraction*.

If $\frac{1}{2}$ of an apple be divided into 2 equal parts, it becomes $\frac{2}{4}$. The effect on the fraction is evidently the same as if we had multiplied both of its terms by 2. In either case, the parts are made two times as MANY as they were before; but they are only HALF AS LARGE; for it will take 2 times as many fourths to make a whole one as it will take halves; and hence it is that $\frac{2}{4}$ is the same in value or quantity as $\frac{1}{2}$.

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multiplied by 2, it becomes $\frac{1}{2}$. Hence, $\frac{1}{2}=\frac{2}{2}=\frac{1}{2}$, and the reverse of this is evidently true, that $\frac{1}{2}=\frac{1}{2}$.

It follows therefore, by multiplying or dividing both terms of the fraction by the same number, we change its terms without altering its value.

Thus, if we reverse the above operation, and divide both terms of the fraction $\frac{1}{2}$ by 2, we obtain its equal, $\frac{2}{4}$; dividing again by 2, we obtain $\frac{1}{4}$, which is the most simple form of the fraction, because the terms are the *least* possible by which the fraction can be expressed.

The process of changing $\frac{1}{2}$ into its equal $\frac{1}{2}$, is called *reducing the fraction to its lowest terms*. It consists in dividing both terms of the fraction by any number which will divide them both without a remainder, and the quotient thence arising in the same manner, and so on, till it, appears that no number greater than 1 will again divide them.

A number which will divide two or more numbers without a remainder, is called a *common divisor*, or *common measure* of those numbers. The greatest number that will do this is called the *greatest common divisor*.

1. What part of an acre are 128 rods?

One rod is $_{160}^{160}$ of an acre and 128 rods are $_{165}^{160}$ of an acre. Let us reduce this fraction to its *lowest terms*. We find, by trial, that 4 will exactly measure both 128 and 160 and, dividing, we change the fraction to its equal $\frac{23}{43}$. Again we find that 8 is a divisor common to both terms, and, dividing, we reduce the fraction to its equal $\frac{4}{5}$, which is now in its lowest terms, for no greater number than 1 will again measure them. The operation may be presented thus:

4) $\frac{128}{160} = \frac{32}{40} = \frac{4}{5}$ of an acre, answer.

2. Reduce $\frac{45}{5}$, $\frac{99}{297}$, $\frac{14}{168}$, and $\frac{1644}{1644}$ to their lowest terms. Ans. $\frac{1}{2}$, $\frac{1}{3}$, $\frac{1}{4}$, and $\frac{2}{4}$.

Note. If any number ends with a cypher, it is evidently divisible by 10. If the two right hand figures are divisible by 4, the whole number is also. If it ends with an even number, it is divisible by 2; if with a 5 or 0, it is divisible by 5.

3. Reduce $\frac{499}{500}$, $\frac{45}{500}$, $\frac{195}{295}$, and $\frac{21}{51}$ to their lowest terms.

¶ 4.4. Any fraction may evidently be reduced to its lowest terms by a single division, if we use the greatest common divisor of the two terms. The greatest common measure of any two numbers may be found by a sort of trial easily made. Let the numbers be the two terms of the fraction $\frac{128}{128}$. The common divisor cannot exceed the less number, for it must measure it. We will try, therefore, if the less number, 128, which measures itself, will also measure or divide 160.

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32)128(4

128 in 160 goes 1 time, and 32 rémain; 128, therefore, is not a divisor of 160. We will now try whether this remainder be not the divisor sought; for if 32 be a divisor of 128, the former divi-

128 32 be a divisor of 128, the former divisor, it must also be a divisor of 160, which consists of 128 +32. 32 in 129 goes 4 times, without any remainder. Consequently, 32 is a divisor of 128 and 160. And it is evidently the greatest common divisor of these numbers; for it must be contained at least once more in 160 than in 128, and no number greater than their difference, that is, greater than 32, can do it.

Hence, the rule for finding the greatest common divisor of two numbers.—Divide the greater number by the less, and that divisor by the remainder, and so ou, always dividing the last divisor by the last remainder, till nothing remain. The last divisor will be the greatest common divisor required.

Note. It is evident, that, when we would find the greatest common divisor of more than two numbers, we may first find the greatest common divisor of two numbers, and then of that common divisor and one of the other numbers, and so on to the last number. Then will the greatest common divisor last found be the answer.

4. Find the greatest common divisor of the terms of the fraction $\frac{21}{5}$, and, by it, reduce the fraction to its lowest terms.



Greatest divis. 7)14(2.

Then, $7)_{35}^{21} = \frac{3}{5} Ans.$

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31=3 Ans.

5. Reduce 55 to its lowest terms.

Note. Let these examples be wrought by both methods; by several divisors, and also by finding the greatest common divisor.

6. Reduce 384 to its lowest terms.	Ans. 1.
7. Reduce 114 to its lowest terms.	Ans. 2
8. Reduce 468 to its lowest terms.	Ans. 117
9. Reduce 1478 to its lowest terms.	Ans. +

To divide a fraction by a whole number.

¶ 45. 1. If 2 yards of cloth cost 3 of a pound, what does 1 yard cost? how much is 3 divided by 2?

2. If a cow consume $\frac{2}{3}$ of a bushel of meal in 3 days, how much is that per day? $\frac{3}{4} \div 3$ how much?

3. If a boy divide $\frac{1}{2}$ of an orange among 2 boys, how much will he give each one ? $\frac{1}{2}$ how much ?

4. A boy hought 5 cakes for 12 of a shilling; what did 1 cake cost? 12.5=how much?

5. If 2 bushels of apples cost $\frac{2}{18}$ of a pound, what is that per bushel?

1 bushel is the half of 2 bushels; the half $\frac{2}{18}$ is $\frac{1}{18}$. Ans: $\frac{1}{18}$ pound.

6. If 3 horses consume $\frac{13}{13}$ of a ton of hay in a month, what will 1 horse consume in the same time ?

 $\frac{13}{13}$ are 12 parts; if 3 horses consume 12 such parts in a month, as many times as 3 are contained in 12, so many parts 1 horse will consume. Ans. $\frac{13}{13}$ of a ton.

7. If $\frac{2}{3}$ of a barrel of flour be divided equally among 5 families, how much will each family receive?

25 is 25 parts; 5 into 25 goes 5 times. Ans. 25 of a barrel

The process in the foregoing examples is evidently dividing a fraction by a whole number; and consists, as may be seen, in dividing the *numerator*, (when it can be done without a remainder,) and under the quotient writing the denominator. But it not unfrequently happens, that the numerator will not contain the whole number without a remainder.

8. A man divided $\frac{1}{2}$ of a pound equally among 2 persons; what part of a pound did he give to each?

1 of a pound divided into 2 equal parts will be 4th.

Ans. He gave 1 of a pound to each.

Ans. 3.

FRACTIONS.

¶ 45, 46.

9. A mother divided $\frac{1}{2}$ a pie among 4 children; what part of the pie did she give to each? $\frac{1}{2} \div 4$ = how much?

10. A boy divided $\frac{1}{3}$ of an orange equally among 3 of his companions; what was each one's share? $\frac{1}{3} \div 3 =$ how much?

11. A man divided $\frac{3}{4}$ of an apple equally between 2 children; what part did he give to each? $\frac{3}{4} \div$ by 2 = what part of a whole one?

 $\frac{3}{4}$ is 3 parts: if each of these parts be divided into 2 equal parts, they will make 6 parts. He may now give 3 parts to one, and 3 to the other: but 4ths divided into 2 equal parts become 8ths. The parts are now twice so many, but they are only half so large; consequently, $\frac{3}{4}$ is only half so much as $\frac{3}{4}$.

In these last examples, the fraction has been divided by multiplying the denominator, without changing the numerator. The reason is obvious; for, by multiplying the denominator by any number, the parts are made so many times smaller, since it will take so many more of them to make a whole one; and if no more of these smaller parts be taken than were before taken of the larger, that is, if the numerator be not changed, the value of the fraction is evidently made so many times less.

¶ 46. Hence, we have two ways to divide a fraction by a whole number.

I. **Divide the numerator** by the whole number, (if it will contain it without a remainder,) and under the quotient write the denominator. Otherwise,

II. Multiply the denominator by the whole number, and over the product write the numerator.

EXAMPLES FOR PRACTICE.

1. If 7 pounds of tobacco cost $\frac{21}{25}$ of a pound, what is that per pound? $\frac{21}{25}$ $\frac{21}{25}$ and $\frac{21}{25}$ of a lb.

2. If $\frac{18}{18}$ of an acre produce 24 bushels, what part of an acre will produce 1, bushel? $\frac{18}{18}$. $\frac{24}{24}$ how much?

3. If 12 yards of silk cost $\frac{19}{19}$ of a pound, what is that a yard? $\frac{19}{19}$ l2—how much?

4, Divide § by 16.

Note. When the divisor is a composite number, the intelligent pupil will perceive, that he can first divide by one component part, and the quotient thence arising by the other; thus last exam

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er; thus he may frequently shorten the operation. In the last example, $16=8\times2$ and $\frac{2}{5}\div8=\frac{1}{5}$, and $\frac{1}{5}\div2=\frac{1}{18}$.

Ans. Ts.

5. Divide $\frac{4}{10}$ by 12. Divide $\frac{1}{10}$ by 21. Divide $\frac{3}{49}$ by 24. 6. If 6 bushels of wheat cost £1§ what is it per bushel? *Note.* The mixed number may evidently be reduced to an improper fraction, and divided as before.

Ans. $\frac{1}{48} = \frac{7}{24}$ of a pound, expressing the fraction in its lowest terms. (¶ 43.)

7. Divide $\pounds 4_{11}^{+1}$ by 9.

the start want to

1 46, 47.

8. Divide 129 by 5.

9. Divide $14\frac{3}{4}$ by 8.

10. Divide 1841 by 7.

Quot. $\frac{7}{13}$ of a pound. Quot. $\frac{18}{7} = 24$.

Quot. $1\frac{27}{32}$. Quot. $26\frac{5}{14}$.

Note. When the mixed number is large, it will be most convenient, first to divide the whole number, and then reduce the remainder to an improper fraction; and, after dividing, annex the quotient of the fraction to the quotient of the whole number; thus, in the last example, dividing 1841 by 7, as in whole numbers, we obtain 26 integers, with $2\frac{1}{2}$ $=\frac{5}{2}$ remainder, which divided by 7, gives $\frac{1}{14}$ and $26 + \frac{1}{14}$ $=26\frac{1}{14}$, Ans.

11. Divide 27861 by 6.

Ans. 4643.

12. How many times is 24 contained in 764611?

Ans. 318347.

13. How many times is 3 contained in 462¹/₃? Ans. 154¹/₄.

To multiply a fraction by a whole number.

¶ 47. 1. If 1 yard of cloth cost $\frac{1}{3}$ of a pound, what will 2 yards cost? $\frac{1}{3} \times 2$ how much?

2. If a cow consume $\frac{1}{4}$ of a bushel of meal in 1 day, how much will she consume in 3 days? $\frac{1}{4}\times3$ =how much?

3. A boy bought 5 cakes, at $\frac{2}{3}$ of a shilling each; what did he give for the whole? $\frac{2}{3} \times 5$ how much?

4. How much is 2 times $\frac{1}{2}$? — 3 times $\frac{1}{2}$? — 2 times $\frac{2}{3}$?

5. Multiply 2 by 3. _____ 3 by 2. _____ 1 by 7.

6. If a man spend # of a shilling per day, how much will he spend in 7 days?

 $\frac{2}{3}$ is 3 parts. If he spend 3 such parts in 1 day, he will evidently spend 7 times 3, that is, $\frac{2}{3} = 2\frac{5}{3}$ in 7 days.

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Hence, we perceive, a fraction is multiplied by multiplying the numerator, without changing the denominator.

But it has been made evident, $(\P 46)$ that multiplying the denominator produces the same effect on the value of the fraction, as dividing the numerator: hence, also, dividing the denominator will produce the same effect on the value of the fraction, as multiplying the numerator. In all cases, therefore, where one of the terms of the fraction is to be multiplied the same result will be effected by dividing the other; and where one term is to be divided, the same result may be effected by multiplying the other.

This principle, borne distinctly in mind, will frequently enable the pupil to shorten the operations of fractions. Thus, in the following example:

At zer of a pound, for 1 pound of sugar, what will 11 pounds cost?

Multiplying the numerator by 11, we obtain for the product $\frac{2}{3} = \frac{1}{3}$ of a pound for the answer.

¶ 48. But by applying the above principle, and dividing the denominator, instead of multiplying the numerator we at once come to an answer, $\frac{2}{2}$ in much lower terms. Hence, there are two ways to multiply a fraction by a whole number:

I. Divide the denominator by the whole number, (when it can be done without a remainder,) and over the quotient write the numerator. Otherwise,

II. Multiply the numerator by the whole number, and under the product write the denominator. If then it be an improper fraction, it may be reduced to a whole or mixed number.

EXAMPLES FOR PRACTICE.

1. If one man consume $\frac{5}{36}$ of a barrel of flour in a month, how much will 18 men consume in the same time? ----6men? ---9 men? Ans. to the last, 11 barrels. 2. What is the product of $\frac{710}{120}$ multiplied by 40? $\frac{71}{120} \times$

40—equal how much ? Ans. 233.

3. Multiply 134 by 10. by ---- 20. ---- by 18. ---- by 36. ----- by 48. ----- by 60.

Note. When the multiplier is a composite number, the pupil will recollect (\P 11), that he may multiply first by one component part, and that product by the other. Thus,

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te number, the ultiply first by other. Thus, in the last example, the multiplier 60 is equal to 12×5 ; therefore, $\frac{13}{144} \times 12 = \frac{13}{12}$, and $\frac{13}{12} \times 5 = \frac{6}{12} = \frac{5}{12}$, Ans.

4. Multiply $5\frac{3}{4}$ by 7. Ans. $40\frac{1}{4}$. Note. It is evident that the mixed number may be reduced to an improper fraction, and multiplied, as in the preceding examples; but the operation will usually be shorter, to multiply the fraction and whole number separately, and add the results together. Thus, in the last example, 7 times 5 are 35; and 7 times $\frac{3}{4}$ are $\frac{2}{4}$ =5 $\frac{1}{4}$, which added to 35, make $40\frac{1}{4}$; Ans.

Or, we may multiply the fraction first, and, writing down the fraction, reserve the integers, to be carried to the product of the whole number.

5. What will 913 tons of hay come to at 3£ per ton? Ans. 28£ 19s.

6. If a man travel $2\frac{6}{40}$ miles in one hour, how far will he travel in 5 hours? — in 8 hours? — in 12 hours? — in 3 days, suppose he travel 12 hours each day?

Ans. to the last, 77² miles. Note. The fraction is here reduced to its lowest terms, the same will be done in all the following examples.

To multiply a whole number by a fraction.

¶ **49.** 1. If 36 pounds be paid for a piece of cloth, what $\cot \frac{3}{2}$ of it? $36 \times \frac{3}{2}$ —how much?

 $\frac{2}{4}$ of the quantity will cost $\frac{2}{4}$ of the price; $\frac{2}{4}$ of a time 36 pounds, that is, $\frac{3}{4}$ of 36 pounds, implies that 36 be first divided into 4 equal parts, and then that one of these parts be taken 3 times; 4 into 36 goes 9 times, and 3 times 9 is 27. Ans. 27 pounds.

From the above example it plainly appears that the object in multiplying by a fraction, whatever may be the multiplicand, is to take of the multiplicand a part, denoted by the multiplying fraction; and that this operation is composed of two others, viz. a division by the denominator of the multiplying fraction, and a multiplication of the quotient by the numerator. It is a matter of indifference, as it respects the result, which of these operations precedes the other, for 36 $\times 3 \div 4 = 27$, the same as $36 \div 4 \times 3 = 27$.

Hence,—Fo multiply by a fraction, whether the multiplicand be a whole number or a fraction,—RULE:

Divide the multiplicand by the denominator of the multi-

FRACTIONS.

plying fraction, and multiply the quotient by the numerator; or, (which will oftenbe found more convenient in practice,) first multiply by the numerator, and divide the product by the denominator.

Multiplication, therefore, when applied to fractions, does not always imply augmentation, or increase, as in whole numbers; for, when the multiplier is less than unity, it will always require the product to be less than the multiplicand, to which it would be only equal; if the multiplier were 1.

We have seen, ($\P10$,) that, when two numbers are multiplied together, either of them may be made the multiplier without affecting the result. In the last example, therefore, instead of multiplying 16 by $\frac{2}{3}$ we may multiply $\frac{2}{3}$ by 16, ($\P47$,) and the result will be the same.

EXAMPLES FOR PRACTICE.

2. What will 40 burnels of meal come to at 2 of a pound per barnel? 40×3=hpw much?

3. What will 24 yards of cloth cost at 3 of a pound per yard? 24×3= how much?

5. Multiply 45 by 70. Multiply 20 by 1.

To multiply one fraction by another.

¶ 50. 1. A man owning 4 of a farm, sold 3 of his share; what part of the whole farm did he sell ? 3 of 4 is how much?

We have just seen, ([[49,) that to multiply by a fraction, is to divide the multiplisand by the denominator, and to multiply the quotient by the numerator. $\frac{4}{5}$ divided by 3, the denominator of the multiplying fraction, ([[46,) is 1_5 , which, multiplied by 2, the numerator, ([[48,) is 1_5 , Ans.

The process, if carefully considered, will be found to consist in multiplying together the two numerators for a new numerator, and the two denominators for a new denominator.

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EXAMPLES FOR PRACTICE.

§ 8

A man, having ³/₄ of a pound, gave ¹/₁₀ of it for a dinner what did the dinner cost him?
 Ans. ³/₄₀ pound.
 Multiply ⁷/₅ by ²/₇.
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 Note. Fractions like the above, connected by the word

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FRACTIONS

of, are sometimes called compound fractions. The word or implies their continual multiplication into each other. Ans. 188 = 1.

Ans. $\frac{188}{100} = \frac{1}{20}$. When there are several fractions to be multiplied continually together, as the several numerators are factors of the new numerator, and the several denominators are factors of the new denominator, the operation may be shortened by dropping these factors which are the same in both terms, on the principle explained in $[] 4^{-1}$. Thus, in the last example, $\frac{1}{2}, \frac{2}{3}, \frac{2}{5}, \frac{2}{5$

6. What is the continual product of 7, 3, 4 of 3 and 34? Note. The integer 7 may be reduced to the form of an improper fraction, by writing a unit under it for a denominator, thus, 7. Ans. 843.

7. At 25 of a pound a yard, what will 3 of a yard of cloth cost?

8. At 13 pounds per barrel for floor, what will 75 of a barrel cost ?

1 = 1 then $\frac{1}{2} \times \frac{7}{16} = \frac{7}{128} \pm \frac{3}{16}$. Ans.

9. At i of a pound, per yard, what cost 7% yards?

Ans. 6116.

10. At \$21 per yard, what cost $6\frac{1}{2}$ yards? Ans. \$14 $\frac{1}{2}$? 11. What is the continued product of 3, $\frac{1}{2}$, $\frac{1}{2}$ of $\frac{3}{2}$, $\frac{2}{2}$, and $\frac{1}{2}$ of $\frac{3}{2}$ of $\frac{4}{2}$? Ans. $\frac{2}{2}\frac{1}{2}$?

may now be presented at one view :

1. To multiply a fraction by a whole number, or a whole number by a fraction.—Divide the denominator by the whole number, when it can be done without a remainder; otherwise, multiply the numerator by it, and under the product write the denominator, which may then be reduced to a whole or mixed number.

II. To multiply a mized number by a whole number;— Multiply the fraction and integers, separately, and add their products together.

III. To multiply one fraction by another,-Multiply to-

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Note. If either or both are mixed numbers, they may first be reduced to improper fractions.

EXAMPLES FOR PRACTICE.

1. At 22 per yard, what cost 4 yards of cloth ?-----5 yds? _____ 6 yds? _____ 8 yds? _____ 20 yds?

Ans. to the last, 15£. 2. Multiply 148 by $\frac{1}{2}$ ---- by $\frac{1}{4}$ ---- by $\frac{1}{70}$. Last product, 44 15.

3. If 2 4 tons of hay keep 1 horse through the winter, how much will it take to keep 3 horses the same time ?--7 horses? _____13 horses? Ans. to the last, 377 tons.

14. What will $8\frac{7}{12}$ barrels of order come to, at 7 shillings per barrel ? . . 1. 1. 2. 18

5. At 142.2 per cwt. what will be the cost of 147 cwt? 6. A owned $\frac{3}{2}$ of a note; B owned $\frac{6}{15}$ of the same; the note amounted to 1000 ; what was each one's share of the money ?

7. Multiply 1 of 2 by 2 of 4.	Product, 1.
8. Multiply 71 by 21.	Product, 151.
9. Multiply 7 by 22.	Product, 21.
10. Multiply 3 of 6 by 3.	Product, 1.
11. Multiply 7 of 2 by 1 of 4.	Product 3.

12. Multiply continually together 1 of 8, 3 of 7, 3 of 9. and 4 of 10. Product, 20.

13. Multiply 1000000 by §. Product, 5555558.

To divide a whole number by a fraction. ¶ 52. We have already shown (¶ 46,) how to divide a fraction by a whole number ; we now proceed to show how to divide a whole number by a fraction.

1. A man divided 9£ among some poor people, giving them 2 of a pound each; how many were the persons who received the money ? 9-3-how many?

1 pound is 4, and 9 pounds is 9 times as many, that is, 36; then 2 is contained in 36 as many times as 3 is contained in 36. Ans. 12 persons,

That is,-Multiply the dividend by the denominator of the dividing fraction, (thereby reducing the dividend to parts of the same magnitude as the divisor) and divide the product by the numerator.

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2. How many times is 3. contained in 8.7. 2 : 311 how many?

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5 Denominator.

Numerator, 3-),49

Quotient, 131 times the answer. To multiply by a fraction, we have seen, (¶ 49,) implies two operations—a division and a multiplication; so also, to divide by a fraction implies two operations—a multiplication

and a division.

¶ 53. Division is the reverse of multiplication.

To multiply by a fraction, To divide by a fraction, whether the multiplicand be whether the dividend be a a whole number or a fraction whole number or a fraction, as has already been shown, we multiply by the denomi-(\P 49,) we divide by the denominator of the multiplying and divide the product by the fraction, and multiply the quopumerator.

Note. In either case, it is matter of indifference, as it respects the result, which of these operations precedes the other; but in *practice* it will frequently be more convenient, that the multipliplication precede the division.

12 multiplied by 2, the product is 9.

In multiplication, the multiplier being less than unity, ing less than unity, or 1, will or 1, will require the product be contained a greater numto be less than the multipliber of times; consequently cand, (¶ 49,) to which it is only equal when the multiplier is 1, and greater when the multiplier is more than 1.

EXAMPLES FOR PRACTICE.

1. How many times is $\frac{1}{2}$ contained in 7? $7 \div \frac{1}{2}$ =How many?

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FRACTIONS.

1 53, 54.

2. How many times can I draw ‡ of a gallon of wine out of a cask containing 26 gallons?

3. Divide 3 by $\frac{3}{2}$. ---6 by $\frac{3}{2}$. ---10 by $\frac{3}{2}$.

4. If a man drink $\frac{1}{16}$ of a quart of rum a day, how long will 3 gallons last him 1

5. If 22 bushels of oats sow an acre, how many acres will 22 bushels sow ? 22-22=how many times ?

Note. Reduce the mixed number to an improper fraction, 23 = 1. Ans. 8 acres.

6. At 122 a yard, how many yards of cloth may be bought for 372 ? Ans. 267 yards.

7. How many times 103 contained in 84?

Ans. 903 times.

8. How many times is ²⁶ contained in 6? Ans. ⁴ of 1 time.

9 How many times is Sg contained in 53?

Ans. 644 times. 10. At $\frac{2}{5}$ of a pound for building 1 rod of stone wall, how many rods may be built for $87\pounds$? $87 \div \frac{2}{5}$ —how many times?

To divide one fraction by another.

¶ 54. 1. At $\frac{2}{3}$ of a pound per parrel, how much rye may be bought for $\frac{2}{3}$ of a pound ? $\frac{2}{3}$ is contained in $\frac{2}{3}$ how many times ?

Had the rye been 2 whole pounds per barrel, instead of $\frac{2}{3}$ of a pound, it is evident, that $\frac{3}{4}$ of a pound must have been $\frac{1}{20}$; but the divisor is 3ds, and 3ds will be contained 3 times where a like number of whole ones are contained 1 time; consequently the quotient $\frac{1}{10}$ is 3 times too *small*, and must therefore in order to give the true answer, be multiplied by 3, that is, by the denominator of the divisor; 3 times $\frac{1}{10}$ = $\frac{1}{10}$ barrel, answer.

The process is that already described, ¶ 52 and 53. If carefully considered, it will be perceived, that the numerator of the divisor is multiplied into the denominator of the dividend, and the denominator of the divisor into the numerator of the dividend; wherefore in practice, it will be more convenient to invert the divisor; thus, $\frac{2}{3}$ inverted becomes $\frac{3}{2}$; then multiply together the two upper terms for a numerator and the two lower terms for a denominator, as in the multipli**cati** exampl

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plication of one fraction by another. Thus, in the above example, 3×8^{119} 9 and beta fraction of the statement of the

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EXAMPLES FOR PRACTICE.

2. At $\frac{1}{4}$ of a pound per bushel for wheat, how many bushels may be bought for $\frac{1}{4}$ of a pound? How many times is $\frac{1}{4}$ contained in $\frac{1}{4}$? Ans. $\frac{3}{4}$ bushels.

3. If $\frac{1}{2}$ of a yard of cloth cost $\frac{3}{4}$ of a pound, what is that per yard? It will be recollected (¶ 24) that when the cost of any quantity is given to find the *price* of a unit, we *divide* the cost by the quantity. Thus, $\frac{3}{4}$ (the cost) divided by $\frac{1}{4}$ (the quantity) will give the price of 1 yard.

Ans. $\frac{24}{5}$ of a pound per yard. **PROOF.** If the work be right, (\P 16, "Proof,") the product of the quotient into the divisor will be equal to the dividend; thus, $\frac{24}{5} \times \frac{7}{5} = \frac{2}{5}$. This, it will be perceived, is multiplying the price of one yard ($\frac{24}{5}$) by the quantity ($\frac{7}{5}$) to find the cost ($\frac{2}{5}$;) and is, in fact, reversing the question; thus, if the price of one yard be $\frac{24}{5}$ of a pound, what will $\frac{7}{5}$ of a yard cost? Ans. $\frac{2}{5}$ of a pound.

Note. Let the pupil be required to reverse and prove the succeeding examples in the same manner.

4. How many bushels of wheat at $\frac{3}{16}$ of a pound per bushel, may be bought for $\frac{2}{5}$ of a pound? Ans. 42 bushels.

5. If 45 pounds of butter serve a family 1 week, how many weeks will 367 pounds serve them?

The mixed numbers, it will be recollected, may be reduced to improper fractions. Ans. S_{TBT} weeks.

6. Divide ½ by ½, Quot. 1 Divide ½ by ½ Quot. 2. 7. Divide ⅔ by ¼, Quot. 3 Divide ⅔ by ½ Quot. 3 8 Divide 2¼ by 1½, Quot. 1½. Divide 10⅔ by 2¼

Quot. 414.

'9. How many times is $\frac{1}{10}$ contained in $\frac{2}{5}$? Ans. 4 times. 10. How many times is $\frac{3}{5}$ contained in $\frac{4}{5}$?

> Ans. 113 times. Quot. 4.

¶ 55. The RULE for division of fractions may now be presented at one view :-

11 Divide $\frac{2}{3}$ of $\frac{2}{7}$ by $\frac{2}{4}$ of $\frac{1}{7}$.

I. To divide a fraction by a whole number, - Divide the

FRACTIONS.

numerator by the whole number, when it can be done without's remainder, and under the quotient write the denominator; otherwise, *multiply* the *denominator* by it, and over the product write the numerator.

II. To divide a whole number by a fraction,—Multiply the dividend by the denominator of the fraction, and divide the product by the numerator.

III. To divide one fraction by another,—Invert the divisor and multiply together the two upper terms for a numerator, and the two lower terms for a denominator.

Note. If either or both are mixed numbers, they may be reduced to improper fractions.

EXAMPLES FOR PRACTICE.

1. If 7 lb of tobacco cost $\frac{63}{100}$ of a pound, what is it per pound? $\frac{63}{100}$, 7 = 100 much? $\frac{1}{100}$ of $\frac{63}{100}$ is how much?

2. At 12 for 3 of a barrel of cider, what is that per barrel?

3. If 4 pounds of sugar cost $\frac{1}{3}$ of a pound, what does 1 pound cost?

4. If $\frac{7}{4}$ of a yard cost 13s. what is the price per yard?

5. If 143 yards cost 43£, what is the price per yard?

Ans. 2114.

6. At 41 pounds for 101 barrels of cider, what is that per barrel? Ans. 32.

7. How many times is 3 contained in 746? Ans. 1989.

8. Divide 1 of 3 by 3.

Divide 7 by 4 of 7.

A 46.06. 27.	Guve. UET.
Divide 1 of 1 by 8 of 2.	Quot. 18.
0. Divide $\frac{1}{10}$ of 4 by $\frac{4}{15}$.	Quot. 3.
11. Divide 48 by 8 of 4.	Quot. 22.
12. Divide # of 4 by 4#.	Quot. 20.

ADDITION AND SUBTRACTION OF FRACTIONS.

¶ 56. 1. A boy gave to one of his companions $\frac{2}{5}$ of an orange, to another $\frac{4}{5}$, to another $\frac{1}{5}$; what part of an orange did he give to all ? $\frac{2}{5+\frac{4}{5}+\frac{4}{5}}$ how much ? Ans. $\frac{2}{5}$.

2. A cow consumes in one month $\frac{1}{15}$ of a ton of hay; a horse, in the same time, consumes $\frac{1}{15}$ of a ton; and a pair of oxen $\frac{1}{15}$; how much do they all consume? how much more does the horse consume than the cow? — the oxen

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¶ 56, 57,

than the horse? 1 1 to how much? 15 how much?

3. 1+1+1=how much? 2-1=how much? 4. 20+20+20+10+20=how much? 11-10=how much?

5. A boy having 2 of an apple, gave 2 of it to his sister; what part of the apple had he left? 2 - 1- how much? When the denominators of two or more fractions are

When the denominators of two or more fractions are alike, (as in the foregoing examples) they are said to have a common denominator. The parts are then in the same denomination, and, consequently, of the same magnitude or value. It is evident, therefore, that they may be added or subtracted, by adding or subtracting their sumerators, that is, the number of their parts, care being taken to write under the result their proper denominator. Thus, $\frac{1}{17} + \frac{1}{17} =$ $\frac{1}{17}$; $\frac{1}{2} = \frac{1}{17}$.

6. A boy having an orange, gave 2 of it to his sister, and 1 to his brother; what part of the orange did he give away?

4ths and 8ths being parts of different magnitudes, or value, cannot be added together. We must therefore first reduce them to parts of the same magnitude, that is, to a common denominator. $\frac{3}{4}$ are three parts. If each of these parts be divided into 2 equal parts, that is, if we multiply both terms of the fraction $\frac{3}{4}$ by 2, (¶ 43) it will be changed to $\frac{6}{4}$; then $\frac{6}{4}$ and $\frac{1}{4}$ are $\frac{7}{4}$.

7. A man had 3 of a hogshead of molasses in one/ cask, and 3 of a hogshead in another; how much more in one cask than in the other?

Here, 3ds cannot be so divided as to become 5ths, nor can 5ths be so divided as to become 3ds; but if the 3ds be each divided into 5 equal parts, and the 5ths each into 3 equal parts, they will all become 15ths. The $\frac{2}{3}$ will become $\frac{19}{15}$, and the $\frac{3}{5}$ will become $\frac{1}{15}$; then $\frac{1}{15}$ taken from $\frac{19}{15}$ leaves $\frac{1}{15}$ Ans.

¶ 57. From the very process of dividing each of the parts, that is, of increasing the denominators by multiplying them, it follows that each denominator must be a factor of the common denominator; now, multiplying all the denomipators together will evidently produce such a number.

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Hence, — To reduce fractions of different denominators to equivalent fractions, having a common denominator, — RULE: Multiply together all the denominators for a common denominator; and as by this process each denominator is multiplied by all the others, so, to retain the value of each fraction, multiply each numerator by all the denominators, except its own, for a new numerator, and under it, write the common denominator.

EXAMPLES FOR PRACTICE.

1. Reduce 2, 2 and 5 to fractions of equal value, having a common denominator.

 $3 \times 4 \times 5 = 60$, the common denominator.

 $2 \times 4 \times 5 = 40$, the new numerator for the first fraction.

1 24

 $3 \times 3 \times 5 = 45$, the new numerator for the second fraction.

 $3 \times 4 \times 4 = 48$, the new numerator for the third fraction.

The new fractions, therefore, are $\frac{43}{54}$, $\frac{43}{54}$, and $\frac{43}{55}$. By an inspection of the operation, the pupil will perceive that the numerator and denominator of each fraction have been multiplied by the same numbers : consequently, (¶ 43) that their value has not been altered.

3. Reduce to equivalent fractions of a common denominator, and add together $\frac{1}{2}$, $\frac{3}{2}$ and $\frac{1}{2}$.

Ans. 83+38+18=78=148, amount.

4. Add together 3 and 4. Amount, 127.

5. What is the amount of $\frac{1}{2} + \frac{1}{3} + \frac{1}{4} + \frac{1}{4}$? Ans. $\frac{247}{210} = 1\frac{37}{210}$.

6. What are the fractions of a common denominator equivalent to $\frac{3}{4}$ and $\frac{5}{6}$? Ans. $\frac{19}{12}$ and $\frac{39}{12}$, or $\frac{9}{12}$ and $\frac{19}{12}$.

We have already seen (¶ 56, ex. 7,) that the common denominator may be any number, of which each given denominator is a factor, that is, any number which may be divided by cach of them without a remainder. Such a number is called a common multiple of all its common divisors, and the least number that will do this is called their least common multiple; therefore, the least common denominator of any fractions is the least common multiple of all their denominators. Though the rule already given will always find a common multiple of the given denominators, yet it will not always find their least common multiple. In the last example, 24 is evidently a common multiple of 4 and 6, for it

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will exactly measure both of them; but 12 will do the same, and as 12 is the *least* number that will do this, it is the *least* common multiple of 4 and 6. It will therefore be

1 57, 58.

convenient to have a *rule* for finding this least common multiple. Let the numbers be 4 and 6. It is evident that one number is a multiple of another, when the former contains all the factors of the latter. The

when the former contains an the factors of the factor. The factors of 4 are 2 and 2 $(2 \times 2 = 4)$. The factors of 6 are 2 and 3, $(2 \times 3 = 6)$ consequently, $2 \times 2 \times 3 = 12$ contains the factors of 4, that is, 2×3 and also contains the factors of 6, that is, 2×3 . 12 then, is a common multiple of 4 and 6, and it is the *least* common multiple, because it does not contain any factor, except those which make up the numbers 4 and 6; nor either of those repeated more than is necessary to produce 4 and 6. Hence it follows, that when any two numbers have a factor common to both, it may be once omitted; thus, 2 is a factor common both to 4 and 6, and is consequently once omitted.

[[58. On this principle is founded the RULE for finding the least common multiple of two or more numbers. Write down the numbers in a line, and divide them by any number that will measure two or more of them; and write the quotients and undivided numbers in a line beneath. Divide this line as before, and so on, until there are no two numbers that can be measured by the same divisor; then the continual product of all the divisors and numbers in the last line will be the least common multiple required.

Let us apply the rule to find the least common multiple of 4 and 6.

4 and 6 may both be measured by 2; the 2) 4 - 6 quotients are 2 and 3. There is no number greater than 1, which will measure 2 and 3. 2 - 3 Therefore, $2 \times 2 \times 3 = 12$ is the least common multiple of 4 and 6.

If the pupil examine the process, he will see that the divisor 2 is a factor common to 4 and 6, and that dividing 4 by this factor gives for a quotient its other factor, 2. In the same manner, dividing 6 gives its other factor, 3. Therefore the divisor and quotients make up all the factors of the two numbers, which, multiplied together, must give the common multiple.

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raction. nd fraction. fraction. 1 48. By an eive that the ve been mul-(¶ 43) that

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111, amount. Amount, 114. · 247=1210. denominator or $\frac{9}{12}$ and $\frac{19}{12}$. common den given denomay be diviich a number divisors, and eir least comninator of any their denomlways find a et it will not the last exand 6, for it

7. Reduce 7, 1,	and to equivalent fractions of the
least common denom	inator. wellen in hand bill be fit a from
OPERATION. 7 11	Then, 2×3×2=12, least common
2)4-2-8-6	denominator. It is evident we need
2 9 1 2 9	not multiply by the 1s. as this would
3 J. 2 - 1 - 0 - 0	not alter the number of survive
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To find the new numerators, that is, how many 12ths each fraction is, we may take 2, 1, 3, and 1 of 12, thus:

1 of 12=9)	New numerators, which,	12=
j of 12=6 (written over the common) <u>6</u>
1 of 12-8 (10)	denominators, give)
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8. Reduce 1, 1, and 5 to fractions having the least common denominator, and add them together.

9. Reduce $\frac{1}{2}$ and $\frac{1}{2}$ to fractions of the least common denominator, and subtract one from the other.

10. What is the least number that 3, 5, 8 and 10 will measure? that is the least of the first of the first is the first of the first is the first of the first is the first of the first of the first is the first of the first of

another 133 yards, and the other 157 yards; how many yards in the 3 pieces.

Before adding, reduce the fractional parts to their least common denominator; this being done, we shall have,

Adding together all the 24ths, viz. 18+20 $7\frac{3}{2}=7\frac{19}{22}$ +21, we obtain 59, that is, $\frac{32}{2}=2\frac{1}{22}$. We $13\frac{1}{2}=13\frac{29}{22}$ write down the fraction $\frac{11}{24}$ under the other $15\frac{7}{2}=15\frac{21}{24}$ fractions, and reserve the 2 integers to be carried to the amount of the other integers, Ans. $37\frac{1}{24}$ making in the whole $37\frac{1}{24}$ Ans.

12. There was a piece of cloth containing 343 yards, from which were taken 123 yards; how much was there left?

343-3424 124-1219

Ans. 2117 yds.

We cannot take 16 twenty-fourths $(\frac{19}{24})$ from 9 twenty-fourths, $(\frac{19}{24})$ we must therefore borrow 1 integer=24 twenty-fourths, $(\frac{29}{24})$ which, with $\frac{9}{24}$, makes $\frac{39}{24}$; we can now take $\frac{19}{24}$ from $\frac{39}{24}$, and there will remain $\frac{11}{24}$; but as

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viz. 18+20 2-231. We der the other ntegers to be ther integers,

ng 343 yards, was there left? wenty-fourths rths, $\left(\frac{9}{24}\right)$ we 1 integer = 24hich, with $\frac{9}{24}$, take 19 from ain $\frac{11}{1}$; but as

we borrowed, so also we must carry 1 to the 12, which makes it 13, and 13 from 34 heaves 21. Ans. 2147.

13. What is the amount of $\frac{1}{2}$ of $\frac{3}{4}$ of a yard, $\frac{2}{3}$ of a yard, and 1 of 2 yards?

Note. The compound fraction may be reduced to a simple fraction; thus, $\frac{1}{2}$ of $\frac{3}{4} = \frac{3}{4}$; and $\frac{1}{5}$ of $2 = \frac{2}{5}$; then, $\frac{3}{4} + \frac{3}{4}$ $+\frac{2}{5}=\frac{173}{120}=1\frac{53}{120}$ yds., answer.

¶ 59. From the foregoing examples we derive the following RULE :- To add or subtract fractions, add or subtract their numerators, when they have a common denominator; otherwise, they must first be reduced to a common denominator.

Note. Compound fractions must be reduced to simple fractions before adding or subtracting.

EXAMPLES FOR PRACTICE.

1. What is the amount of $\frac{6}{7}$, $4\frac{2}{3}$ and 12? Ans. 1734. 2. A man bought a farm, and sold $\frac{3}{4}$ of $\frac{1}{2}$ of it; what part of the farm had he left? **Ans.** §.

3. Add together $\frac{1}{2}$, $\frac{5}{8}$, $\frac{1}{4}$, $\frac{7}{10}$, $\frac{1}{5}$ and $\frac{14}{28}$? Amount. 238.

- 4. What is the difference between 14_{17}^{8} & 16_{37}^{7} ? Ans. 1_{35}^{16} .
- 5. From 13 take $\frac{3}{4}$.
- 6. From 3 take $\frac{1}{4}$.
- 7. From $147\frac{1}{3}$ take $48\frac{1}{5}$.
- 8. From $\frac{1}{4}$ of $\frac{4}{10}$ take $\frac{1}{2}$ of $\frac{2}{47}$.
- 9. Add together $112\frac{1}{2}$, $311\frac{2}{3}$, and $1000\frac{3}{4}$.
- 10. Add together 14, 11, $4\frac{2}{3}$, $\frac{1}{18}$ and $\frac{1}{2}$.
- 11. From $\frac{3}{4}$ take $\frac{1}{2}$. From $\frac{7}{8}$ take $\frac{3}{4}$.

12. What is the difference between $\frac{1}{2}$ and $\frac{1}{3}$? $\frac{2}{3}$ and $\frac{1}{3}$? \$ and 务? * and 꽃? 동 and *? 동 and ⅔?

13. How much is $1 - \frac{1}{4}? 1 - \frac{1}{2}? 1 - \frac{3}{8}? 1 - \frac{5}{8}? 2 - \frac{2}{3}?$ $2-\frac{4}{2}? 2_{\frac{1}{4}}-\frac{2}{3}? 3_{\frac{4}{5}}-\frac{1}{10}? 1000-\frac{1}{10}?$

REDUCTION OF FRACTIONS.

¶ 60. We have seen (¶27,) that integers of one denomination may be reduced to integers of another denomination. It is evident that fractions of one denomination, after the same manner, and by the same rules, may be reduced to *fractions* of another denomination; that is, *frac*tions, like integers, may be brought into lower denominations by multiplication, and into higher denominations by division.

 $Remainder, \frac{3}{4}$.

Rem. $\frac{37}{470}$.

- **R**emainder, $2\frac{1}{3}$.
- Rem. 988.

To reduce higher into LOWER To reduce lower into HIGHER denominations. _denominations. (RULE. See ¶ 28.) (RULE. See ¶ 28.) 1. Reduce $\frac{1}{280}$ of a pound 2. Reduce § of a penny to to pence, or the fraction of a the fraction of a pound. Note. 'Division is performpenny. Let it be recollect-led either by dividing the nu-Note. ed that a fraction is *multipli*-merator, or by *multiplying* the ed either by dividing its de-denominator. nominator, or by multiplying $\stackrel{\text{\tiny $}}{\neq}$ d. \div 12 = $\frac{1}{14}$ s. \div 20= its numerator. zto£. Ans. $_{7,80} \pounds \times 20 = _{14} s. \times 12 =$ Or thus: $\frac{6}{7}$ of $\frac{1}{12}$ of $\frac{1}{20} =$ 1680=280£. Ans. §d. Ans. Or thus: $\frac{1}{280}$ of $\frac{20}{1}$ of $\frac{12}{1}$ = $\frac{248}{5}$ of a penny, Ans. 3. Reduce $\frac{1}{1280}$ of a pound 4. Reduce $\frac{2}{3}$ of a farthing to the fraction of a farthing? to the fraction of a pound. $_{1280} \pounds \times 20 = _{1280} s. \times 12$ $\frac{3}{4}$ q. \div 4 $=_{16}^{3}$ d. \div 12 $=_{192}^{3}$ s. $=\frac{240}{1280}d\times 4=\frac{960}{1280}=\frac{3}{4}q.$ $\div 20 = 3340 = 1280 \pounds$ Or thus: Or thus: be requ Denom. 4 Num. 1 of a fr 20 s. in 1£. 4 q. in 1d. 20 16 12d. in 1s. 12 d. in 1 s. 240 192 20s. in £1. 4 q. in 1 d. 3840 960 Then $\frac{960}{1280}$, $=\frac{3}{4}$ q. Ans. Then $3340 = \pounds_{1280}$. Ans. 5. Reduce 2588 of a guin-6. Reduce § of a penny to ea to a fraction of a penny. the fraction of a guinea. 8. Reduce $\frac{4}{5}$ of a pound to 7. Reduce \$ of a guinea to the fraction of a pound. the fraction of a guinea.

Consult ¶ 28, ex. 12.

10. Reduce 23 of a guinea 9. Reduce 3 of a moidore, at 1£. 10s. to the fraction of to the fraction of a moidore. a guinea.

11. Reduce 27 of a pound, 12. Reduce 8 of an ounce Troy, to the fraction of an to the fraction of a pound Trov. ounce.

· ¶ 60.

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of a guinea a moidore.

of an ounce of a pound ¶ 60, 61.

REDUCTION OF FRACTIONS.

13. Reduce $\frac{1}{28}$ of a pound avoirdupois, to the fraction of an ounce.

15. A man has $\frac{1}{728}$ of a hogshead of wine; what part is that of a pint?

17. A cucumber grew to the length of $\frac{1}{3560}$ of a mile; what part is that of a foot?

19. Reduce $\frac{2}{5}$ of $\frac{1}{6}$ of a pound to the fraction of 1s.

21. Reduce $\frac{1}{5}$ of $\frac{2}{17}$ of 3 pounds to the fraction of a penny.

¶ 61. It will frequently be required to find the value of a fraction, that is to reduce a fraction to integers of less denominations.

1. What is the value of $\frac{2}{3}$ of a pound? In other words, reduce $\frac{2}{3}$ of a pound to shillings and pence.

 $\frac{3}{3}$ of a $\frac{2}{5}$ is $\frac{49}{5}$ =13 $\frac{1}{3}$ shillings; it is evident from $\frac{1}{3}$ of a shilling may be obtained some pence; $\frac{1}{3}$ of a shilling is $\frac{1}{3}$ =4d.—that is, multiply the numerator by that number which will reduce it to the next less denomination, and divide the product by the denominator; if there be a remainder, multiply and divide as before, and so on; the several quotients, placed one after another in their order, will be the answer.

14. Reduce \$ of an ounce to the fraction of a pound avoirdupois.

16, A man has $\frac{1}{100}$ of a pint of wine; what part is that of a hogshead?

18. A cucumber grew to the length of 1 foot 4 inches $=\frac{16}{2}=\frac{4}{3}$ of a foot; what part is that of a mile?

20. $\frac{29}{27}$ of a shilling is $\frac{2}{5}$ of what fraction of a pound?

22. ${}^{180}_{11}$ of a penny is $\frac{1}{5}$ of what fraction of 3 pounds? ${}^{180}_{11}$ of a penny, is ${}^{21}_{11}$ of what part of 3 pounds? ${}^{180}_{11}$ of a penny is $\frac{1}{5}$ of ${}^{21}_{11}$ of how many pounds?

It will frequently be required to reduce integers to the fraction of a greater denomination.

2. Reduce 13s. 4d. to the fraction of a pound.

13s. 4d. is 160 pence; there are 240 pence in a pound? therefore, 13s. 4d. is $\frac{16}{248} = \frac{2}{3}$ of a pound. That is, reduce the given sum or quantity to the least denomination mentioned in it, for a numerator; then reduce an integer of that greater denomination (to a fraction of which it is required to reduce the given sum or quantity) to the same denomination, for a denominator, and they will form the fraction required.

REDUCTION OF FRACTIONS.

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EXAMPLES F	OR PRACTICE.	
3. What is the value of $\frac{3}{2}$	4. Reduce 4d. 2q. to the	
of a shilling?	fraction of a shilling.	
OPERATION.	OPERATION.	
Numer. 3	4d. 2a. 1s.	
12	4 12	
Denom. 8)36(4d. 2a. Ans.	18 Numer. 12	
32	4	
4	48 Denom	
16(2a.	$+\frac{18}{3}=\frac{3}{2}$. Ans.	
16	48 8.	
5. What is the value of $\frac{3}{2}$	6. Reduce 7 oz. 4 pwt. to	
of a pound Troy ?	the fraction of a pound Troy.	
7. What is the value of $\frac{1}{2}$	8. Reduce S oz. 14 ² dr.	
of a pound avoirdupois?	to the fraction of a pound	
	avoirdupois.	
	Note.—Both the numerator	
	and the denominator must be	
	reduced to 9ths of a dr.	
9. 4 of a month is how ma-	10. 3 weeks 1d. 9h. 36m.	
ny days, hours and minutes?	is what fraction of a month?	
11. Reduce 4 of a mile to	12. Reduce 4 fur. 125 vds.	
its proper quantity.	2 ft. 1 in. 24 bar, to the frac-	
	tion of a mile.	
\cdot 13. Reduce $\frac{1}{2}$ of an acre	14. Reduce 1 rood 30 poles	
to its proper quantity.	to the fraction of an acre.	
15. What is the value of	16. Reduce 4s. 84d. to the	
15 of a dollar in shillings.	fraction of a dollar.	
pence. &c.?		
17. What is the value of	18. Reduce 2 ft. 8 in. 1+b.	

17. What is the value of ⁹₁₀ of a yard?

 r_3^3 of a ton.

to the fraction of a yard. 19. What is the value of 20. Reduce 4 cwt. 2 qr. 12 lb. 14 oz. $12\frac{4}{13}$ dr. to the fraction of a ton.

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Note. Let the pupil be required to reverse and prove the following examples :

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3. Ans.

z. 4 pwt. to bound Troy. oz. 14²/₂ dr. of a pound

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bood 30 poles an acre. s. $8\frac{1}{4}$ d. to the ar.

ft. 8 in. $1\frac{1}{5}$ b. a yard. cwt. 2 qr. $\frac{4}{3}$ dr. to the

nd prove the

21. What is the value of $\frac{9}{14}$ of a guinea?

22. Reduce 3 roods, $17\frac{1}{2}$ poles to the fraction of an acre.

23. A man bought 27 gal. 3 qts. 1 pt. of molasses; what part is that of a hogshead?

24. A man purchased $\frac{1}{13}$ of 7 cwt. of sugar; how much sugar did he purchase?

25. 13h. 42m. 51²/₄s. is what part or fraction of a day?

SUPPLEMENT TO FRACTIONS.

1. What are fractions? 2. Whence is it that the parts into which any thing or any number may be divided, take their name? 3. How are fractions represented by figures? 4. What is the number above the line called ?- Why is it so called ? 5. What is the number below the line called ?--Why is it so called ?--What does it show ? 6. What is 7. What is it which determines the magnitude of the parts ?- Why? a simple or proper fraction? ---- an improper fraction ---- a mixed number ? S. How is an improper fraction reduced to a whole or mixed number? 9. How is a mixed number reduced to an improper fraction ?-----a whole number ? 10. What is understood by the terms of the fraction? 11. How is a fraction reduced to its most simple or lowest terms ? 12. What is understood by a common diviso?? by the greatest common divisor ? 13. How is it found? 14. How many ways are there to multiply a fraction by a whole number? 15. How does it appear, that dividing the denominator multiplies the fraction? 16. How is a mixed number multiplied ? 17. What is implied in multiplying by a fraction? 18. Of how many operations does it consist? - What are they? 19. When the multiplier is less than a unit, what is the product compared with the multiplicand ? 20. How do you multiply a whole number by a fraction ? 21. How do you multiply one fraction by another? 22. How do you multiply a mixed number by a mixed number ? 23. How does it appear, that in multiplying both terms of the fraction by the same number the value of the fraction is not altered? 24. How many ways are there to divide a fraction by a whole number ? What are they ? 25. How does it appear that a fraction is divided by multiplying its denominator? 26. How does dividing by a fraction differ from multiplying by a fraction? 27. When the divisor is less than a unit, what is the quotient compared with the dividend? 28 What is understood by a common denominator? ---- the least common denominator? 29. How does it appear that each given denominator must be a factor of the common denominator ? 30. How is the common denominator to two or more fractions found? 31. What is understood by a multiple? ---- by a common multiple? _____ by the least common multiple ? What is the process of anding it ? 32. How are fractions added and subtracted? 33. How is a fraction of a greater denomination reduced to one of a less ? ----- of a less to a greater? 34. How are fractions of a greater deintegers of a less nomination reduced to integers of a less? denomination to the fraction of a greater?

EXERCISES.

1. of $12\frac{1}{2}$, $3\frac{2}{3}$ and $4\frac{2}{3}$? Ans. to the last, 2013.

2. To $\frac{7}{4}$ of a pound add $\frac{3}{4}$ of a shilling. Amount, 1848. Note. First reduce both to the same denomination.

3. § of a day added to $\frac{2}{3}$ of an hour, make how many hours ?----what part of a day ? Ans. to the last, \$3 d. 4. Add $\frac{1}{2}$ ib Troy to $\frac{7}{12}$ of an ounce.

Amount, 6 oz. 11 pwt. 16 gr. 5. How much is $\frac{1}{4}$ less $\frac{1}{8}$? $\frac{198}{-2}$ of $\frac{2}{3}$ of $\frac{2}{3}$? Ans. to the last, 193.

6. From $\frac{1}{2}$ shilling take $\frac{3}{4}$ of a penny.

7. From $\frac{3}{2}$ of an ounce take $\frac{7}{4}$ of a pwt.

Rem. 11 pwt. 3 gr.

8. From 4 days $7\frac{1}{2}$ hours, take 1 day $9\frac{3}{16}$ hours. Rem. 2 days, 22 hours, 20 min.

9. At $\pounds_{\frac{5}{2}}$ per yard, what costs $\frac{3}{4}$ of a yard of cloth?

The price of unity, or 1, being given to find the ¶ 62. cost of any quantity, either less or more than unity, multiply the price by the quantity. On the other hand, the cost of any quantity, either less or more than unity, being given, to find the price of unity, or 1, divide the cost by the quantity. Ans. £15.

1. If $\frac{1}{15}$ b of sugar cost $\frac{7}{15}$ of a shilling, what will $\frac{32}{45}$ of a pound cost?

This example will require two operations: first, as above, to find the price of 1 lb; secondly, having found the price of 1 lb, to find the cost of $\frac{32}{24}$ of a pound. $\frac{7}{15}$ s. $\div \frac{1}{13}$ ($\frac{1}{17}$ of $\frac{7}{15}$ s. ¶ 54)= $\frac{91}{165}$ s. the price of 1 lb. Then, $\frac{91}{165}$ s. $\times \frac{32}{43}$ ($\frac{32}{43}$ of $\frac{91}{165}$ s. 150 = $\frac{2912}{7095}$ s. = 4d. $3\frac{4971}{7095}$ q. the answer.

Or we may reason thus: first to find the price of 1 lb; $\frac{1}{13}$ lb costs $\frac{7}{15}$ s. If we knew what $\frac{1}{13}$ lb would cost, we might repeat this 13 times, and the result would be the price of I th. $\frac{11}{13}$ is 11 parts. If $\frac{11}{13}$ th costs $\frac{7}{15}$ s. it is evident $\frac{1}{13}$ lb will cost $\frac{1}{11}$ of $\frac{7}{15} = \frac{7}{165}$ s. and $\frac{13}{13}$ lb will cost 13 times as much, that is, $\frac{91}{165}$ s.= the price of 1 lb. Then, $\frac{32}{43}$ of $\frac{g_1}{165}$, $\frac{2912}{7095}$, the cost of $\frac{32}{43}$ of a pound. $\frac{2912}{7095}$, $\frac{32}{40}$, $\frac{32}{7095}$, $\frac{32}{705}$, $\frac{32}{7095}$, $\frac{32}{705}$, 349719, as before. This process is called solving the question by analysis.

After the same manner, let the pupil solve the following questions :

¶ 61, 62.

Rem. 51d.

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SUPPLEMENT TO FRACTIONS.

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pwt. 16 gr.

 $Rem. 5\frac{163}{220}.$

1 pwt. 3 gr. ars.

rs, 20 min. cloth?

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st, as above, at the price $\frac{113}{13}$ ($\frac{13}{13}$ of $\frac{13}{5}$ s. $\frac{23}{43}$ ($\frac{23}{43}$ r. ce of 1 fb; and cost, we build cost, we build be the $\frac{1}{5}$ s. it is eviwill cost 13 Then, $\frac{23}{43}$

281258.=4d. ag the ques-

e following

2. If 7 lb of tobacco cost $\frac{2}{3}$ of a pound, what is that a pound? $\frac{1}{3}$ of $\frac{3}{2}$ —how much? What is it for 4 lb? $\frac{4}{5}$ of $\frac{3}{4}$ —how much? What for 12 lb? $\frac{1}{5}$ of $\frac{3}{4}$ —how much? Ans. to the last, £13.

3. If 6½ yards of cloth cost £3, what cost 9¼ yards? Ans. £4. 5s. 4½d.

4. If 2 oz. of silver cost 11s. 3d. what costs $\frac{3}{4}$ of an oz? Ans. 4s. 2d. $2\frac{1}{2}q$.

5. If $\frac{1}{7}$ oz. costs 4s. 1d. what costs 1 oz? Ans. 5s. $\frac{8}{5}$ d. 6. If $\frac{1}{3}$ ib less by $\frac{1}{6}$ costs 13 $\frac{1}{5}$ d. what costs 14 ib less by $\frac{1}{5}$ of 2 ib ? Ans. £4. 9s. $9\frac{3}{55}$ d.

7. If $\frac{3}{5}$ yard costs \mathcal{L}_{8}^{7} , what will $40\frac{1}{2}$ yards cost.

Ans. $\pm 59.$ 1s. $2\frac{3}{2}$ d. 8. If $\frac{7}{15}$ of a ship costs ± 251 , what is $\frac{3}{52}$ of her worth? Ans. $\pm 53.$ 15s. 84d.

9. At £35 per cwt. what will 92 lb cost?

10. A merchant owning $\frac{4}{5}$ of a vessel, sold $\frac{2}{3}$ of his share for £39.5s. what was the vessel worth? Ans. £448 11s. 10 $\frac{1}{2}$ d. 11. If $\frac{4}{5}$ yards cost £4, what will $\frac{2}{15}$ of an ell Eng. cost.

Ans. 17s. 1d. 29q.

12. A merchant bought a number of bales of cloth, each containing 129_{27}^{17} yards, at the rate of $\pounds 7$ for 5 yards, and sold them out at the rate of $\pounds 11$ for 7 yards, and gained $\pounds 200$ by the bargain; how many bales were there?

First find for what he sold 5 yards; then what he gained on 5 yards—what he gained on 1 yard. Then, as many times as the sum gained on 1 yard is contained in £200, so many yards there must have been. Having found the number of yards, reduce them to bales. Ans. 9 bales.

13. If a staff 53 feet in length, cast a shadow of 6 feet, how high is that steeple whose shadow measures 153 feet? Ans. 1443 feet.

14. If 16 men finish a piece of work in $28\frac{1}{3}$ days, how long will it take 12 men to do the same work?

First find how long it would take 1 man to do it; then 12 men will do it in $\frac{1}{12}$ of that time. Ans. $37\frac{7}{4}$ days.

15. How many pieces of merchandise, at 20_{8}^{1} s. apiece, must be given for 240 pieces, at $12\frac{1}{2}$ s. apiece? Ans. $149\frac{11}{161}$.

16. How many yards of bocking that is $1\frac{1}{2}$ yd. wide will be sufficient to line 20 vds, of camlet that is $\frac{3}{2}$ of a yard wide ?

First find the contents of the camlet in square measure; then it will be easy to find how many yards in length of bocking that is 11 yd. wide it will take to make the same Ans. 12 yards of camlet. quantity.

17. If 14 yd. in breadth require 204 yds. in length to make a cloak, what in length that is $\frac{3}{4}$ yd wide will be required to make the same? Ans. 341 yds.

18. If 7 horses consume $2\frac{3}{4}$ tons of hay in 6 weeks, how many tons will 12 horses consume in 8 weeks?

If we knew how much 1 horse consumed in 1 week, it would be easy to find how much 12 horses would consume in 8 weeks.

 $2\frac{3}{4} = \frac{1}{4}$ tons. If 7 horses consume $\frac{1}{4}$ tons in 6 weeks; one horse will consume $\frac{1}{7}$ of $\frac{1}{4} = \frac{1}{28}$ of a ton in 6 weeks; and if a horse consume $\frac{1}{28}$ of a ton in 6 weeks, he will consume $\frac{1}{6}$ of $\frac{1}{24} = \frac{1}{168}$ of a ton in 1 week. 12 horses will consume 12 times $\frac{1}{168} = \frac{1}{168} \frac{2}{168}$ in 1 week, and in 8 weeks they will consume 8 times $\frac{132}{168} = \frac{132}{21} = 6\frac{2}{7}$ tons, answer.

19. A man with his family, which in all were 5 persons, did usually drink 7⁴/₅ gallons of cider in 1 week; how much will they drink in $22\frac{1}{2}$ weeks when 3 persons more are added to the family? Ans. 2804 gallons.

20. If 9 students spend £107 in 18 days, how much will 20 students spend in 30 days? Ans £39, 18s. 4310

Decimal Fractions.

¶ 63. We have seen, that an individual thing or number may be divided into any number of equal parts, and that these parts will be called halves, thirds, fourths, fifths, sixths, &c., according to the number of parts into which the thing or number may be divided; and that each of these parts may be again divided into any other number of equal parts, and so Such are called *common* or *vulgar* fractions. Their on. denominators are not uniform, but vary with every varying division of a unit. It is this circumstance which occasions the chief difficulty in the operations to be performed on them; for when numbers are divided into different kinds or parts, they cannot be so easily compared. This difficulty led to the invention of *decimal* fractions, in which an individual thing or number is supposed to be divided first into ten equal parts, which will be tenths, and each of these

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parts to be again divided into ten other equal parts, which will be *hundredths*; and each of these parts to be still further divided into ten other equal parts, which will be *thou*sandths; and so on. Such are called *decimal fractions*, (from the Latin word *decem*, which signifies *ten*,) because they increase and decrease in a *tenfold* proportion, in the same manner as whole numbers.

¶ 64. In this way of dividing a unit, it is evident, that the denominator to a decimal fraction will always be 10, 100, 1000, or 1 with a number of ciphers annexed; consequently, the denominator to a decimal fraction need not be expressed, for the numerator only, written with a point before it, (') called the separatrix, is sufficient of itself to express the true value. Thus,

The denominator to a decimal fraction, although not expressed, is always understood, and is 1 with as many ciphers annexed as there are places in the numerator. Thus, '3765 is a decimal consisting of four places; consequently, 1 with four ciphers annexed, (10000) is its proper denominator. Any decimal may be expressed in the form of a common fraction by writing under it its proper denominator. Thus, '3765 expressed in the form of a common fraction, is $\frac{3765}{10000}$.

When the whole numbers and decimals are expressed together, in the same number, it is called a *mixed number*. Thus, 25'63 is a mixed number, 25', or all the figures on the left hand of the decimal point, being whole numbers, and '63, or all the figures on the right hand of the decimal point, being decimals.

The names of the places to ten-millionths, and, generally, how to read or write decimal fractions, may be seen from the following

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25 and 63 Hundredths and 9 Millionths.

Hundredths. Thousandths. Ten-Thousandths. Hundred-Thousandths Millionths. Ten-Millionths.

6853 Ten-Thousandths. 86002 Hundred-Thousandths From the table it appears, that the first figure on the right hand of the decimal point signifies so many tenth parts of a unit; the second figure, so many hundredth parts of a unit; the third figure, so many thousandth parts of a unit, &c. It takes 10 thousandths to make 1 hundreth, 10 hundredths to make 1 tenth, and 10 tenths to make 1 unit, in the same manner as it takes 10 units to make 1 ten, 10 tens to make Consequently, we may regard unity as a 1 hundred, &c. starting point, from whence whole numbers proceed, continually *increasing* in a tenfold proportion towards the left

Tenths.

Thousandths. Hundredths.

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Numbers Whole

Decimal parts.

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4th place.

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hand, and decimals continually *decreasing* in the same proportion, towards the right hand. But as decimals decrease towards the right hand, it follows of course, that they increase towards the left hand, in the same manner as whole numbers.

¶ 65. The value of every figure is determined by its place from *units*. Consequently, ciphers placed at the *right* hand of decimals do not alter their value, since every significant figure continues to possess the same place from unity. Thus, '5, '50, '500, are all of the same value, each being equal to $r_{0}^{5}\sigma$ or $\frac{1}{2}$.

But every cipher placed at the *left* hand of decimal fractions *diminishes* them tenfold, by removing the significant figures further from unity, and consequently making each part ten times as small. Thus, '5, '05, '005, are of different value, '5 being equal to $_{T\sigma}$, or $\frac{1}{2}$, '05 being equal to $_{1} \frac{1}{2\sigma}$, or $\frac{1}{2\sigma}$, and '005 being equal to $_{T\sigma\sigma\sigma}$, or $\frac{1}{2\sigma}$.

Decimal fractions, having *different denominators*, are readily reduced to a *common denominator*, by annexing ciphers until they are equal in number of places. Thus, '5, '06, '234 may be reduced to '500, '060, '234, each of which has 1000 for a common denominator.

¶ **66.** Decimals are read in the same manner as whole numbers, giving the name of the lowest denomination, or right hand figure, to the whole. Thus, '6853 (the lowest denomination, or right hand figure, being ten-thousandths) is read 6853 ten-thousandths.

Any whole number may evidently be reduced to decimal parts, that is, to tenths, hundreths, thousandths, &c., by annexing ciphers. Thus, 25, is 250 tenths, 2500 hundredths, 25000 thousandths, &c Consequently, any mixed number may be read together giving it the name of the lowest denomination or right hand figure. Thus, 25'63 may be read 2563 hundredths, and the whole may be expressed in the form of a common fraction, thus, $\frac{256^3}{160^3}$.

The denominations in FEDERAL MONEY are made to correspond to the decimal divisions of a unit now described, dollars being units, or whole numbers, dimes tenths, cents hundredths, and mills thousandths of a dollar; consequently.

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¶ 66, 67.

the expression of any sum in dollars, cents and mills, is simply the expression of a mixed number in decimal fractions.

Forty-six and seven tenths= $46_{10}^{-}=46'7$. Write the following numbers in the same manner : Eighteen and thirty-four hundredths. Fifty-two and six hundreths. Nineteen and four hundred eighty-seven thousandths. Twenty and forty-two thousandths. One and five thousandths. 135 and 3784 ten thousandths. 9000 and 342 ter thousandths. 10000 and 15 ten-thousandths. 974 and 102 millionths. 320 and 3 tenths, 4 hundredths and 2 thousandths. 500 and 5 hundred thousandths. 47 millionths. Four hundred and twenty-three thousandths.

ADDITION AND SUBTRACTION OF DECIMAL FRACTIONS.

¶ 67. As the value of the parts in decimal fractions increases in the same proportion as units, tens, hundreds, &c., and may be read together, in the same manner as whole numbers, so, it is evident that all the operations on decimal fractions may be performed in the same manner as on whole numbers. The only difficulty, if any, that can arise, must be in finding where to place the decimal point, in the result.

This, in addition and subtraction, is determined by the same rule; consequently, they may be exhibited together.

1. A man bought a barrel of flour for \$8, a firkin of butter for $\$3^{+}50$, 7 pounds of sugar for $83\frac{1}{2}$ cents, an ounce of pepper for 6 cents; what did he give for the whole?

Note. See the table of Federal Money, ¶ 27. Let the pupil go back now and read carefully all that is said respecting Federal Money in Reduction. From what is there stated it is plain, that we may readily reduce any sums in federal money to the same denominations, as to cents or mills, and

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DECIMAL FRACTIONS.

and add or subtract them as simple numbers. Or, what is the same thing, we may set down the sums, taking care to write dollars under dollars, cents under cents, and mills under mills, in such order that the separating points of the several numbers shall fall directly under each other, and add them as simple numbers, placing the separatrix in the amount directly under the other points.

OPERATION.

\$8' = 8000 mills, or 1000ths of a dollar.
3'50 = 3500 mills, or 1000ths.
'835= 835 mills, or 1000ths.
'06 = , 60 mills, or 1000ths.

Ans. \$12'395=12395 mills, or 1000ths.

As the denominations of federal money correspond with the parts of decimal fractions, so the rules for adding and subtracting decimals are exactly the same as for the same operations in federal money.

2. A man owing \$375, paid \$175'75; how much did he then owe?

OPERATION.

\$375' = 37500 cents, or 100ths of a dollar. 175'75 = 17575 cents, or 100ths of a dollar.

\$199'25 = 19925 cents, or 100ths.

Wherefore,—In addition and subtraction of decimal fractions,—RULE: Write the numbers under each other, tenths under tenths, hundredths under hundredths, according to the value of their places, and point off in the result as many places for decimals as are equal to the greatest number of decimal places in any of the given numbers.

EXAMPLES FOR PRACTICE.

3. Bought 1 barrel of flour for 6 dollars and 75 cents, 10 1b. of coffee for 2 dollars 30 cents, 71b. of sugar for 92 cents, 1 lb. of raisins for 12½ cents, and 2 oranges for 6 cents; what was the whole amount? Ans. \$10'155.

4. A man is indebted to A, \$237'62; to B, \$350; to C, \$86'12¹₂; to D, \$9'62¹₂; and to E, \$0'834; what is the amount of his debts? Ans. \$684'204.

5. A man has three notes specifying the following suma, viz. three hundred dollars, fifty dollars sixty cents, and nine

133~

ADDITION AND SUBTRACTION OF DECIMALS. ¶ 67.

dollars eight cents; what is the amount of the three notes? Ans: \$359'68.

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6. A man gave 4 dollars 75 cents for a pair of boots, and 2 dollars 12½ cents for a pair of shoes; how much did the boots cost more than the shoes?

OPERATION.	F1	OPERATION.
4750 mills.	tert or,	\$4'75
2125 mills.		2425
· · · · · · · · · · · · · · · · ·		1

2625 mills= \$2'625 Ans. \$2'625 Ans.

7. A man bought a cow for eighteen dollars, and sold her again for twenty-one dollars thirty-seven and a half cents; how much did he gain? Ans. 3'375.

8. A man bought a horse for 82 dollars, and sold him again for seventy-nine dollars seventy-five cents; did he gain or lose ? and how much?"

9. A man sold wheat at several times as follows, viz. 13'25 bushels; 8'4 bushels; 23'051 bushels; 6 bushels, and '75 of a bushel; how much did he sell in the whole? Ans. 51'451 bushels.

10. What is the amount of $429, 21_{100}^{37}, 355, \frac{3}{1000}, 1_{100}^{7}, 300, 1$

11. What is the amount of 2 tenths, 80 hundredths, 89 thousandths, 6 thousandths, 9 tenths, and 5 thousandths? Ans. 2.

12. What is the amount of three hundred and twenty-nine and seven tenths; thirty-seven and one hundred sixty-two thousandths, and sixteen hundredths?

4316, paid \$376'865; how much did he then owe? Ans. \$3939'135.

14. From thirty-five thousand thake thirty-five thousandths. Ans. 34999'965.

15. From 5'83 take 4'2793.

263

 16. From 480 take 245'0075.
 Ans. 234'9925.

 17. What is the difference between 1793'13 and 817.

 05693 ?
 Ans. 976'07307.

18. From 4_{100}^{-8} take 2_{10}^{-1} . Remainder, 1_{100}^{-9} or 198. 19. What is the amount of 29_{10}^{-3} , 374_{100}^{-9} , 97_{100}^{-20} . 315 $_{1000}^{-4}$, 27, and 100_{10}^{-4} ? Ans. 942'957009. ^{•75} is ₁ Ans. sa 3. M

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follows, viz. ; 6 bushels, the whole? ;451 bushels. , $\frac{13}{100}$, $1\frac{15}{100}$, , or 808'143. indredths, 89 ousandths?

Ans. 2. d twenty-nine red sixty-two

; how much s. 33939'133. rty-five thous. 34999'965. Ans. 1'5507. 234'9925. 3'13' and 817. 1s. 976'07307. $1\frac{9}{105}$ or 1'98. $\frac{9}{5050}, 97\frac{2}{1}\frac{3}{2}\frac{3}{2}$. 942'957009.

MULTIPLICATION OF DECIMALS.

MULTIPLICATION OF DECIMAL FRACTIONS.

¶ 68. 1. How much hay in 7 loads; each containing 23,571 cwt?

23'571 cwt.= 23571 1000ths of a cwt.

Ans. 164'997 cwt.= 164997 1000ths of a cwt.

We may here, (¶ 66,) consider the multiplicand so many thousandths of a cwt., and then the product will evidently be thousandths, and will be reduced to a mixed or whole number by pointing off 3 figures, that is, the same number as are in the multiplicand; and as either factor may be made the multiplier, so, if the decimals had been in the multiplier, the same number of places must have been pointed off for decimals. Hence it follows, we must always point off in the product as many places for decimals as there are decimal places in both factors.

2. Multiply '75 by '25.

01	PERATION.
	'75
	25
	0.01
	375
	150

In this example, we have 4 decimal places, in both factors; we must therefore point off 4 places for decimals in the product. The reason of pointing off this number may appear still more plain, if we consider the two factors as common or vulgar fractions. Thus,

'1875 Product. common or vulgar fractions. Thus, '75 is $\frac{75}{100}$, and '25 is $\frac{25}{100}$: now, $\frac{75}{100} \times \frac{25}{100} = \frac{1875}{10000}$ '1875, Ans. same as before.

3. Multiply '125 by '03.

OPERATION.

'03

·125

Here, as the number of significant figures in the product is not equal to the number of decimals in both factors, the deficiency must be supplied

'00375 ' by prefixing ciphers, that is, placing them at the left hand. The correctness of the rule may appear from the following process: '125 is $\frac{125}{1000}$, and '03 is $\frac{13}{100}$: now, $\frac{125}{1000} \times \frac{375}{1000} = 00375$, the same as before.

These examples will be sufficient to establish the following
MULTIPLICATION OF DECIMALS.

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RULE.

In the multiplication of decimal fractions, multiply as in whole numbers, and from the product point off so many figures for decimals as there are decimal places in the multiplicand and multiplier counted together, and, if there are not so many figures in the product, supply the deficiency by prefixing ciphers.

As the denominations of federal money correspond with the parts of decimal fractions; the rules for the multiplication and division of both are the same.

EXAMPLES FOR PRACTICE.

4. At \$5'47 per yard, what cost 8'3 yards of cloth? Ans. 45'401.

5. At \$'07 per pound, what cost 26'5 pounds of rice? Ans. \$1:855 cwt.

6. If a barrel contain 1'75 cwt. of flour, what will be the weight of '63 of a barrel? Ans. 1'1025.

7. If a melon be worth \$0'9 what is '7 of a melon worth ! Ans. 6³₁₀ cents.

8. Multiply five hundredths by seven thousandths

	Product , '00035.
9. What is '3 of 116?	Ans. 34'8.
10. What is '85 of 3672?	Ans. 3121'2.
11. What is '37 of '0563?	Ans. '020831.
12. Multioly 572 by '58.	

13. Multiply eighty-six by four hundredths.

Product, 3'44.

14. Multiply '2062 by '0008.

15. Multiply forty-seven tenths by one thousand eightysix hundredths.

16. Multiply two hundredths by eleven thousandths.

17. What will be the cost of thirteen hundredths of a ton of hay, at \$11 a ton?

18. What will be the cost of three hundred seventy-five thousandths of a cord of wood at \$2 a cord?

19. If a man's wages be seventy-five hundreths of a dollar a day, how much will he earn in four weeks, Sundays excepted?

20. What will 250 bushels of rye come to at \$0'881 per bushel? Ans. \$221'25.

24. What is the value of 86 barrels of flour, at $637\frac{1}{2}a$ barrel?

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22. What will be the cost of a hogshead of molasses containing 63 gallons, at $28\frac{1}{2}$ cents a gallon? Ans. \$17'955. 23. If a man spend $12\frac{1}{2}$ cents a day, what will that amount to in a year of 365 days? what will it amount to in five years? Ans. \$228'12 $\frac{1}{2}$ in 5 years.

DIVISION OF DECIMAL FRACTIONS.

¶ 69. Multiplication is proved by division. We have seen, in multiplication, that the decimal places in the product must always be equal to the number of decimal places in the multiplicand and multiplier counted together. The multiplicand and multiplier, in proving multiplication, become the divisor and quotient in division. It follows of course, in division, that the number of decimal places in the divisor and quotient counted together, must always be equal to the number of decimal places in the dividend. This will still further appear from the examples and illustrations which follow:

1. If 6 barrels of flour cost \$44'718, what is that a barrel?

By taking away the decimal point, \$44'718=44718 mills, or 1000ths, which, divided by 6, the quotient is 7453 mills, =\$7'453, the answer.

Or, retaining the decimal point, divide as in whole numbers:

OPERATION. 6)44'718

As the decimal places in the divisor and quotient, counted together, must be equal to the number of

Ans. 7'453 decimal places in the dividend, there being no decimals in the divisor,—therefore point off three figures for decimals in the quotient, equal to the number of decimals in the dividend, which brings us to the same result as before.

2. At \$475 a barrel for eider, how many barrels may be bought for \$31?

In this example, there are decimals in the divisor, and none in the dividend. \$4'75=475 cents, and \$31, by annexing two ciphers =3100 cents; that is, reduce the dividend to parts of the same denomination as the divisor.— M \$2

¶ 68.

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cloth ? ns. 45'401. of rice ? 1!855 cwt.will be the ns. 1'1025. elon worth ? 6_{10}^{-1} cents. dths ect, '00035. Ans. 34'8. ns. 3121'2. is. '020831.

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\$0'88½ per s. **\$221'25**. at **\$6'37½** a DIVISION OF DECIMALS.

Then, it is plain, as many times 475 cents are contained in 3100 cents, so many barrels may be bought.

475)3100(6259 barrels, the answer; that is, 6 barrels and 249 of another barrel. 2850

But the remainder, 250, instead of be-250ing expressed in the form of a common fraction, may be reduced to 10ths by annexing a cipher. which, in effect, is multiplying it by 10, and the divisor continued, placing the decimal point after the 6, or whole ones already obtained, to distinguish it from the decimals The points may be withdrawn or not which are to follow. from the divisor and dividend.

OPERATION.

2500

2375

1250

950

3000

2850

150

4'75)31'00(6'526+barrels, the answer, that is 6 barrels and 526 thousandths of another bar-2850

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By annexing a cipher to the	ĥı
remainder, thereby reducing it	
10ths and continuing the division	

10ths, and continuing the division, we obtain from it '5, and a still further remainder of 125, which, by annexing another cipher, is reduced to 100ths, and so on.

The last remainder, 150, is 198 of a thousandth part of a barrel, which is of so trifling a value, as not to merit notice.

If now we count the decimals of the dividend, (for every cipher annexed to the remainder is evidently to be counted a decimal of the dividend,) we shall find them to be five, which corresponds with the number of decimal places in the divisor and quotient counted together.

3. Under ¶ 68, ex. 3, it was required to multiply '125 by '03; the product was '00375. Taking this product for a dividend, let it be required to divide '00375 by '125. One operation will prove the other. Knowing that the number of decimals in the quotient and divisor, counted together, will be equal to the decimal places in the dividend, we may divide as in whole numbers, being careful to retain the decimal points in their proper places. Thus:

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OPERATION. (125)(00375((03 375

The divisor, 125, in 375 goes 3 times and no remainder. We have only to place the decimal point in the quotient and the work is done.

000 the quotient and the work is done. There are five decimal places in the dividend; consequently there must be five in the divisor and quotient counted together; and, as there are *three* in the divisor, there must be two in the quotient; and since we have but one figure in the quotient, the *deficiency* must be supplied 'by prefixing a cypher.

¶ 79. The foregoing examples and remarks are sufficient to establish the following

RULE.

In the division of decimal fractions, divide as in whole numbers, and from the right hand of the quotient point off as many figures for decimals as the decimal figures in the dividend, exceed those in the divisor, and if there are not so many figures in the quotient, supply the defliciency by prefixing ciphers.

If at any time there is a remainder, or if the decimal figures in the divisor exceed those in the dividend cyphers may be annexed to the dividend or the remainder, and the quotient carried to any necessary degree of exactness; but the ciphers annexed must be counted so many decimals of the dividend.

EXAMPLES FOR PRACTICE,

4. If \$472,875 be divided equally between 13 men, how much will each one receive? Ans. \$36,375.

5. At \$'75 per bushel, how many bushels of rye can be bought for \$141? Ans. 188 bushels.

+ 6. At $6\frac{1}{4}$ cents apiece, how many oranges may be bought for \$8? Ans, 128 oranges,

7. If '6 of a barrel of flour cost \$5, what is that per barrel? Ans. 8'333+

Quot. '037+

Divide 2 by 53'1.

140 REDUCTION OF VULGAR FRACTIONS. &c. ¶ 70, 71;

9. Divide '012 by '005.

10. Divide three thousandths by four hundredths.

Quot. '075,

11. How many times is '17 contained in 8?

12. If I par \$468'75 for 75) pounds of wool, what is the value of 1 pound? Ans. \$8'625; or thus \$0'624

13. If a piece of cloth, measuring 125 yards, cost \$18125 what is that a yard?. Ans. \$1'45.

14. If 536 quintals of fish cost \$1913,52, how much is that a quintal? Ans. \$3'57.

15. Bought a farm, containing 84 acres, for \$3213; what did it cost me, per acre? Ans. \$38'25.

16. At \$954 for 3816, yards of flannel, what is that per Ans. \$0'25. vard?

REDUCTION OF COMMON OR VULGAR FRAC-TIONS TO DECIMALS.

¶ 71. 1. A man has 4 of a barrel of flour; what is that expressed in decimal parts?

As many times as the denominator of a fraction is contained in the numerator, so many whole ones are contained in the fraction. We can obtain no whole ones in $\frac{4}{5}$, because the denominator is not contained in the numerator. We may, however, reduce the numerator to tenths, (¶69, ex. 2,) by annexing a cipher to it, which, in effect, is multiplying it by 10, making 40 tenths, or 4'0. Then, as many times as the denominator, 5 is contained in 40, so many tenths, are contained in the fraction. 5 into 40 goes 8 times and no remainder. Ans. '8 of a bush.

2. Express $\frac{3}{4}$ of a dollar in decimal parts.

The numerator, 3, reduced to tenths, is 38, 30, which, divided by the denominator, 4, the quotient is 7 tenths, and a remainder of 2. This remainder must now be reduced to hundredths by annexing another cipher, making 20 hundredths. Then, as many times as the denominator 4, is contained in 20, so many hundredths also may be obtained. 4 into 20 goes 5 times, and no remainder. $\frac{3}{4}$ of a dollar, therefore, reduced to decimals, is 7 tenths and 5 hundredths, that is, '75 of a dollar.

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¶ 70, 71:

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hat is the 13 \$0'62<u>1</u> st \$181'25 ns. \$1'45. y much is ns. \$3'57. 213; what is. \$38'25. is that per ns. \$0'25.

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ion is concontained es in $\frac{4}{5}$, benumerator. *nths*, (¶69, ect, is mulien, as ma-40, so mab 40 goes 8 6 of a bush.

3'0, which, tenths, and reduced to ag 20 hunnator 4, is e obtained. of a dollar, hundredths, 171. REDUCTION OF VULGAR FRACTIONS, &C.

> Denom. 4)3'0('75 of a dollar, the answer. 28

> > 20 20

3. Reduce $\frac{4}{66}$ to a decimal fraction.

The numerator must be reduced to hundreths by annexing two ciphers, before the division can begin.

66)4'00('0606+, the answer. 396

> 400 396

As there can be no *tenths*, a cipher must be placed in the quotient, in tenths place.

Note. $\frac{4}{66}$ cannot be reduced exactly; for, however long the division be continued, there will still be a remainder.^{*} It is sufficiently exact for most purposes, if the decimal be extended to three or four places.

• Decimal figures which continually repeat, like '06, in this example, are called Repetends, or Circulating Decimals. If only one figure repeats, as '3333 or '7777, &c. it is called a single repetend: If two or more figures circulate alternately, as '060606, '234234234, &c. it is called a compound repetend. If other figures arise before those which circulate as '743933, '143010101, &c. the docimal is a mixed repetend.

A single repetend is denoted by writing only the circulating figure, with a point over it thus: '3, signifies that the 3 is to be continually repeated, forming an *infinite* or never ending series of 3's.

A compound repetend is denoted by a point over the first and last repeating figure: thus, 234 sign mes that 234 is to be continually repeated.

It may not be amiss, here to show how the value of any repetend may be found, or in other words, how it may be reduced to its equivalent vulgar fraction.

If we attempt to reduce $\frac{1}{2}$ to a *decimal*, we obtain a continual repetition of the figure 1: thus, '11111, that is, the *repetend* '1 The value of the repetend '1 then is $\frac{1}{2}$; the value of "222, &cc. the repetend '2 will be *twice* as much; that From the foregoing examples we may deduce the following general RULE: To reduce a common to a decimal fraction:—Annex one or more ciphers, as may be necessary, to the numerator, and divide it by the denominator. If then there be a remainder, annex another cipher, and divide as before, and so continue to do so long as there shall continue is, $\frac{2}{3}$. In the same manner, $(3-\frac{3}{3})$, and $(4-\frac{4}{3})$, and $(5-\frac{5}{3})$, and so on to (9), which $=\frac{9}{3}=1$.

1. What is the value of '8?

2. What is the value of $(\dot{6} \cdot Ans. \frac{6}{2} = \frac{2}{3}$. What is the value of $(\dot{3} - 0)$ of $(\dot{7} \cdot 2)$ of $(\dot{7} \cdot 2)$ of $(\dot{5} \cdot 2)$ of $(\dot{9} \cdot 2)$ of $(\dot{7} \cdot 2)$

If $\frac{1}{3}$ be reduced to a decimal, it produces '010101, or the repetend '01. The repetend '02, being 2 times as much, must be $\frac{2}{3}$ and ' $\dot{03}$ = $\frac{3}{3}$, and ' $\dot{48}$, being 48 times as much, must be $\frac{48}{3}$, and ' $\dot{74}$ = $\frac{3}{4}$, &c.

If $\frac{1}{989}$ be reduced to a decimal, it produces '001; consequently, ' $\dot{0}0\dot{2}_{=9}\dot{2}_{9}$, and ' $\dot{0}3\dot{7}_{=3}\dot{3}_{9}\dot{7}_{9}$, and $\dot{4}2\dot{5}_{=4}\dot{2}\dot{5}$, &c. As this principle will apply to any number of places, we have this general RULE for reducing a circulating decimal to a vulgar fraction.—Make the given repetend the numerator, and the denominotor will be as many 9s as there are repeating figures.

3. What is the vulgar fraction equvialent to '704?

Ans. 704

5. What is the value of '43?

El-river-

In this fraction, the repetend begins in the second place, or place of hundredths. The first figure, 4, is $\frac{4}{10}$, and the *repetend*, 3, is $\frac{3}{5}$ of $\frac{1}{10}$, that is, $\frac{3}{50}$; these two parts must be added together. $\frac{4}{10} + \frac{3}{50} = \frac{3}{50} = \frac{1}{50}$, ans. Hence, to find the value of a *mixed repetend*,—Find the value of the two parts *separately*, and add them together.

6. What is the value of '153? $\frac{15}{100} + \frac{3}{900} = \frac{138}{150} Ans.$

7. What is the value of '138 ? ____ '16 ?____'4123 ?

It is plain, that circulates may be added, subtracted, multiplied, and divided, by first reducing them to their equivalent vulgar fractions.

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¶ 71.

Ans. §.

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Ans. §. t is the val-· · 9 ?___· 1? '010101, or es as much, s as much,

001; conse = 423, orc. places, we ting decimal the numeras there are

704? Ans. 794. - '324?last, 3333333.

econd place, $\frac{4}{10}$, and the arts must be nce, to find e of the two

 $\frac{8}{0} = \frac{23}{150}$ Ans. -4123? subtracted, hem to their

¶ 71, 72. REDUCTION OF DECIMAL FRACTIONS.

to be a remainder, or until the fraction shall be reduced to any necessary degree of exactness. The quotient will be the decimal required, which must consist of as many decimal places as there are ciphers annexed to the numerator; and if there are not so many figures in the quotient, the deficiency must be supplied by prefixing ciphers

EXAMPLES FOR PRACTICE.

4. Reduce $\frac{1}{2}$, $\frac{1}{4}$, $\frac{12}{480}$, and $\frac{9}{1129}$ to decimals.

Ans. '5; '25; '025; '00797+

- 5. Reduce 33, 10000, 1785, and 60006 to decimals. Ans. '692+; '903; '0028+; '000183+
- 6. Reduce $\frac{478}{502}$, $\frac{10}{367}$, $\frac{16}{500}$ to decimals.
- 7. Reduce 4, 5, 5, 5, 1, 3, 3, 1, 1, 1, 5, 1, to decimals.
- 8. Reduce $\frac{1}{6}$, $\frac{3}{6}$, $\frac{5}{6}$, $\frac{1}{5}$, $\frac{2}{5}$, $\frac{3}{5}$, $\frac{4}{5}$, $\frac{1}{20}$, $\frac{1}{25}$, $\frac{3}{75}$ to decimals.

REDUCTION OF DECIMAL FRACTIONS.

¶ 72. Fractions, we have seen, (¶ 60) like integers, are reduced from low to higher denominations by division, and from high to lower denominations by *multiplication*.

To reduce a compound number to a decimal of the highest denomination.

1. Reduce 7s. 6d. to the decimal of a pound.

6d. reduced to the decimal of a shilling, that is, divided by 12, is '5s, which annexed to the 7s, making 7'5s, and divided by 20, is ' $375\pounds$, the answer.

The process may be presented in form of a *rule*, thus : Divide the *lowest* denomination given, annexing to it one or more ciphers, as may be necessary, by that number which it takes of the same to make onc of the next higher

To reduce the decimal of a higher denomination to integers of lower denominations. 2. Reduce '375£ to integers of lower denominations. * '375£ reduced to shillings, that is, multiplied by 20, is 7'50s.; then the fractional part, '50s, reduced to pence, that is, multiplied by 12, is 6d. Ans. 7s. 6d.

That is, multiply the given decimal by that number which it takes of the next lower denomination to make one of this higher, and from the right hand of the product point off. as many figures for decimals as there are figures in the denomination, and annex the given decimal, and so conquotient, as a decimal to that | tinue to do through all the dehigher denomination; so continue to do, until the whole shall be reduced to the decimal required.

EXAMPLES FOR PRACTICE. 3. Reduce 1 oz. 10 pwt. to the fraction of a pound.

> OPERATION. 20)10'0 pwt. 12)13 pz 45 th. Ans.

5. Reduce 4 cwt. 23 qrs. to the decimal of a ton.

Note. 23=2'6.

7. Reduce 38 gals 3'52 gts. of beer to the decimal of a hhd.

9. Reduce 1 qr. 2n. to the decimal of a yard.

11. Reduce 17h. 6m. 43s. to the decimal of a day.

13. Reduce 21s. 101d. to the decimal of a guinea.

15. Reduce 3cwt. Oqr. 7lb. Soz. to the decimal of a ton. | '15334821 of a ton ?

Let the pupil be required to reverse and prove the following examples:

17. Reduce 4 rods to the decimal of an acre.

18. What is the value of '7 of a lb of silver ?

19. Reduce 18 hours, 15m. 50'4 sec. to the decimal of a day.

20. What is the value of '67 of a league?

Reduce 10s. 91d. to the fraction of a pound.

¶ 73. There is a method of reducing shillings, pence

nominations; the several numbers at the left hand of the decimal points will be the value of the fraction in the proper denominations.

EXAMPLES FOR PRACTICE. 4. Reduce '125 lb Troy to integers of lower denominations.

: OPERATION. Њ. 125 12

oz. 1'500 20

pwt. 10'000, Ans loz. 10pwt. 6. What is the value of '2325 of a ton ?

8. What is the value of '72 hogshead of beer ?

10. What is the value of '375 of a yard?

12. What is the value of "713 of a day?

14. What is the value of '78125 of a guinea?

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¶ 73, 74, REDUCTION OF DECIMAL FRACTIONS.

and farthings to the decimal of a pound, by inspection, more simple and concise than the foregoing. The reasoning in relation to it is as follows:

Th of 20s. is 2s.; therefore every 2s. is 10, or '1.S. Every shilling is $z_{\sigma} = z_{\sigma}$, or '05£. Pence are readily reduced to farthings. Every farthing is stor &. Had it so happened, that 1000 farthings, instead of 960, had made a pound, then every farthing would have been Totor, or '001£. 960+40=1000; that is, $\frac{1}{24}$ of 960 added to 960 is 1000. Taking $\frac{1}{2^{4}}$ of a number, and adding to that number, is the same as multiplying the number by unity and the fraction $\frac{1}{24}$, 1_{24} . Suppose you have the fraction $\frac{24}{860}$. If you multiply both the numerator, and denominator by 1_{21} , you do not change the value of the fraction. Do this, and you obtain $\frac{25}{1000}$. $\frac{24}{1000}$ then is equal to $\frac{25}{1000}$. \pounds_{1000}^{24} is 24 farthings; of course it follows that 24 farthings is equal to Wherefore, if the number of farthings, in the £ - 250. given pence and farthings, be more than 12, 14 part will be more than $\frac{1}{2}$; therefore, add 1 to them; if they be more than 36, $\frac{1}{24}$ part will be more than $1\frac{1}{2}$; therefore add 2 to them; then call them so many thousandths, and the result will be correct within less than $\frac{1}{2}$ of $\frac{1}{1000}$ of a pound. Thus, 17s. 5²d is reduced to the decimal of a pound as follows : 16s== Then 5²d=23 farthings, which, in- $\pounds'8 \text{ and } 1s = \pounds'05.$ creased by 1, (the number being more than 12, but not exceeding 36) is $\pounds'024$, and the whole is $\pounds'874$, the answer. Wherefore, to reduce shillings, pence and farthings to the decimal of a pound by inspection,-Call every two shillings one tenth of a pound; every odd shilling, five hundredths;

and the number of farthings, in the given pence and farthings, so many thousandths, adding one, if the number be more than twelve and not exceeding thirty-six, and two," if the number be more than thirty-six.

¶ 71. Reasoning as above, the result, or the three first figures in any decimal of a pound, may readily be reduced back to shillings, pence and farthings, by inspection. Donble the first figure, or tenths, for shillings, and, if the second figure, or hundredths, be five or more than five, reckou another shilling ; then, after the five is deducted, call the figures in the second and third place so many farthings, abat-Ν

SUPPLEMENT TO DECIMAL FRACTIONS. 1 74.

ing one when they are above twelve, and two when above thirty-six, and the result will be the answer, sufficiently exact for all practical purposes. Thus, to find the value of '876£ by inspection :---

tenths of a pound = 16 shillings. **·8**. '05 hundredths of a pound 1 shilling. . -----. '026 thousandths, abating 1, =25 farthings = 0 s. 61 d. $= 17 \, s.$ 6į d. 876 of a pound Ans.

EXAMPLES FOR PRACTICE.

1. Find, by inspection, the decimal expressions of 9s. 7d. Ans. '479£, and '603£. and 12s. 07d.

2. Find, by inspection, the value of '523 £, and '694 £.

Ans. 10s. 51d., and 13s. 101d. 3. Reduce to decimals, by inspection, the following sums,

and find their amount, viz : 15s. 3d.; 8s. 111d.; 10s. 61d.; 1s. 81d.; 1d. and 21d. Amount, £1'833.

4. Find the value of '47£.

Note. When the decimal has but two figures, after taking out the shillings, the remainder, to be reduced to thousandths will require a cipher to be annexed to the right hand, or supposed to be so. Ans. 9s. 47d.

5. Value the following decimals, by inspection, and find their amount, viz. '785£.; '357£.; '916£.; '74£.; '5£.; '25£.; '09£.; and '008£. Ans. 3£. 128. 11d.

SUPPLEMENT TO DECIMAL FRACTIONS.

QUESTIONS.

1. What are decimal fractions? 2. Whence is the term derived? 3. How do decimals differ from common fractions? 4. How are decimal fractions written ? 5. How can the proper denominator to a decimal fraction be known, if it be not expressed ? 6. How is the value of every figure determined ? 7. What does the first figure on the right hand of the decimal point signify ? ---- the second figure ? ---- the third figure ? ---- fourth figure ? 8. How do ciphers, placed at the right hand of decimals affect their value ? 9. Placed at the left hand how do they affect their value ? 10. How are decimals read? 11. How are decimal fractions, having different denominators, reduced to a common denominator? 12. What is a mixed number? 13. How may any whole numle he reduced to decimal parts? 14. How can any mixed number be read together, and the whole expressed in the form of a common fraction? 15. What is observed respecting the denomina-

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2. sold, how . 3. barre of rie £63, were N it wi three 4.

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6 shillings. 1 shilling. 0 s. 61 d.

7 8. 61 d. Ans.

1s of 9s. 7d. and '603£. and '694 £. 1 13s. 104d. owing sums, 10s. 61d.; int, £1'833.

s, after takced to thouto the right Ins. 98, 47d. on, and find 74£.; '5£.; £. 12s. 11d.

TIONS.

term derived? How are deciator to a deciw is the value re on the right gure? ---- the placed at the t the left hand ead? 11. How uced to a com-How may any can any mixed the form of a the denomina¶ 74. SUPPLEMENT TO DECIMAL FRACTIONS.

tions in federal money ? 16. What is the rule for addition and subtraction of d scimals, particularly as respects placing the decimal point for reducing a compound number to a decimal of the highest denomination contained in it ? 19. What is the rule for finding the value of any given decimal of a higher denomination in terms of a lower ? .20. What is the rule for reducing shillings, pence and farthings to the deci-mal of a pound, by inspection? 21. What is the reasoning in rela-tion to this rule? 22. How may the three first figures of any decimal of a pound be reduced to shillings, pence and farthings, by inspection ?

EXERCISES.

1. A merchant had several remnants of cloth, measuring as follows :

7 3 yds.]	Hów many yards in the whole, and what would
6 4 "	the whole come to at \$3'67 per yard?
14 "	Note. Reduce the common fractions to deci
9 4 " (mals. Do the same wherever they occur in the
81 " I	examples which follow

1 9 8 31 "

Ans. 36'475 yards. \$133'863+,'cost.

2. From a piece of cloth containing 36# yds. a merchant, sold, at one time, 7_{10}^{3} yds. and at another time, 125 yards; how much of the cloth had he left? Ans. 16'7 yds.

. 3. A farmer bought 7 yards of broadcloth for $\pounds S_{T3}^{6}$, a barrel of flour for $\pounds 2_{15}^{4}$, a cask of lime for $\pounds 1_{\frac{8}{2}}$, and 7 lbs. of rice for \pounds_{2T} ; he paid 1 ton of hay at $\pounds 3_{T_{0}}$, 1 cow at $\pounds 6_3^2$, and the balance in pork at $\pounds_{I_0}^1$ per lb; how many were the pounds of pork?

Note. 'In reducing the common fractions in this example, it will be sufficiently exact if the decimal be extended to Ans. 1084 lb. three places.

4. At 121 cents per lb, what will 373 lbs of butter cost? Ans. \$4'7183.

5. At \$17'37 per ton for hay, what will 11g tons cost ? Ans. \$201'924.

6. The above example reversed. At \$201'925 for 115 tons of hay, what is that per ton ? Ans. \$17'37.

7. If '45 of a ton of hay cost \$9, what is that per ton? Consult ¶ 62. Ans. \$20.

8. At '4 of a dollar a gallon, what will '25 of a gallon of Ans. '1 of a dollar. molasses cost?

¶ 74.

9. At 9 dollars per cwt. what will 7 cwt. 3 qrs. 16 lbs. of sugar cost?

Note. Reduce the 3 qrs. 16 lbs. to the decimal of a cwt. extending the decimal in this, and the examples which follow to four places. Ans. 71'035+

10. At \$69'875 for 5 cwt. 1 qr. 14 lbs. of raisins, what is that per cwt. Ans. \$13.

11. What will 2300 lbs of hay come to at 7 mills per lb? Ans \$16'10.

12. What will 765½ lbs. of coffee come to at 18 cents per lb? Ans. \$137'79.

13. What will 12 gals. 3 qts. 1 pt. of gin cost, at 28 cents a quart?

Note. Reduce the whole quantity to quarts and the decimal of a quart. Ans. \$14'42.

14. Bought 16yds. 2qrs. 3na. of broadcloth for \$100'125. what was that per yard? Ans. \$6.

15. At \$1'92 per bushel, how much wheat may be purchased for \$'72? Ans. 1 peck 4 qts.

17. Bought a load of hay for \$9'17, paying at the rate of \$16 per ton; what was the weight of the hay?

Ans. 11 cwt. 1 qr. 23 lbs.

18. At \$302'4 per tun, what will 1 hhd. 15 gals. 3 qts. of wine cost? Ans. \$94'50.

19. The above reversed. At \$94'50 for 1 hhd. 15 gals. 3 qts. of wine, what is that per tun ? Ans. \$302'4.

Note. The following examples reciprocally prove each other, excepting when there are some fractional losses, as explained above, and even then the results will be sufficiently exact for all practical purposes. If, however, greater exactness be required, the decimals must be extended to a greater number of places.

20. At \$1'80 for 31 qts. of wine, what is that per gallon?

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22. If § of a ton of potash cost \$60'45, what is that per ton ? 21. At $$2^{215}$ per gallon, what cost $3\frac{1}{2}$ qts?

23. At \$96 72 per ton for potash, what will $\frac{5}{2}$ of a ton cost?

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Supposi the table course 4 of 20 shilling dollars, an given sum

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This can (see ¶ 73) is equal to The foll Halifax cur in pounds a lings, pence

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REDUCTION OF CURRENCIES.

Reduction of Currencies.

In the United States, since the act of Congress in 1786, establishing Federal money, calculations in money have generally been made in dollars, cents and mills. In England, the denominations, though the same in name as the currency of this Province, are different in value. In the United States, previous to the act of Congress, it was the custom to reckon in pounds, shillings &cc.; and now, though all accounts are kept in federal money, small sums are mentioned frequently in these denominations. There are different currencies of the same name in different parts of the United States. It may be necessary often in commercial dealings, and in the course of ordinary business, to change values in foreign currencies into the currency of the Procinces.

Supposing there is a sum in federal money—\$21'604' We find by the table of coins, π 27, that I dollar is equal to 5 shillings, and of course 4 dollars are equal to 1 pound, there being 4 times 5 shillings in 20 shillings. 'I'he value of pounds then, it is clear, is 4 times that of dollars, and cf course dollars are reduced to pounds by dividing the given sum by 4.

4) 24 dollars.

🐃 a) ls.

There remain, however, \$'604, $6 \le 2 \le 4$ and 4 mills to be changed to Halifax currency. By referring to Decimal Fractions, \P 66, we see that dollars are the units in federal money, and cents and mills decimal parts: cents hundredths, and mills thousandths. We have then simply to divide these decimals of a dollar by 4, and the quotient will be in decimal parts of a pound, thus:

4) '604 of a dollar.

'151 of a pound.

This can be reduced to shillings, pence and farthings by inspection, (see 173) as follows: £151 equal to 3s. 0d. 1qr. We find that \$24'604 is equal to £6 3s. 0d. 1qr. Ans,

The following then, is the general rule to reduce federal moncy to Halifax currency—divide the given sum by 4, and the quotient will be in pounds and decimal parts of a pound, which can be reduced to shillings, pence and farthings by inspection.

		EXA	MPLES	FOR PRACTI	CE.			,
Reduce	\$500 to	Halifax	currenc	y,	Ans £125			
do	27:304	· do	do	•••	· 6	11s	6d	lar.
do	118'25	do	do		29	lls	3d	+
do	236.50	do	do		59	23	6d	
Reduce	\$490 to	Halifax	curren	cy-\$56'03-		14	-\$8	5.63
	977'642	respective	ely to H	lalifax currency	y.			

To reduce Halifax currency to federal money, we must reverse the process in the above examples. The rule is as follows; Reduce the shillings, pence &c. if any, to the decimal of a pound, by inspection, N 2

REDUCTION OF CURRENCIES.

and multiply the given sum by 4, the product will be in the denominations of federal money.

EXAMPLES FOR PRACTICE.

Reduce £125 Helifex currency to federal money. Ans. \$500 59 2s 6d 236'50 do do do do

In order to change English sterling money, and the currencies in some degree in use in the different parts of the United States, into Halifax currency : since the denominations are the same in name, it will be necessary to take some other currency, the denominations of which are different, as a common object of comparison for these currencies, and for Halifax currency. By this means we shall be able to ascertain the values of the former relatively to those of the latter. We will take federal money as this common object of comparison, and will compare with a unit of one of its denominations, the dollar, one or more units of a denomination of Halifax currency, and the before mentioned currencies, the shilling.

- In Halifax currency -5s. = \$1.In English, or sterling money* (4s. 6d.)41s.=\$1.
- In New England currency - 6s. ==\$1.
- In Pennsylvania currency (7s. 6d.) - 74s.=\$1.

In Halifax currency 5s. are equal to \$1, and in English sterling money, 41s. are equal to \$1. Sterling money, then, is to Halifax currency as 5 to 41, or to avoid the fraction, as 10 to 9, since $2 \times 5 = 10$, and $2 \times 44 = 9$. Therefore, to change sterling money into Halifax currency, multiply by $\frac{19}{3}$, or, take once the given sum, and add $\frac{1}{3}$, thus—

9) £48 12s 9d sterling money.

5 8 1

54 0 10 Halifax currency.

Reduce £56 17s. 6d. sterling to Halifax currency. Ans. £63 3s. 10d. 92 4a. 6d. do do do do

In New England currency, 6s. are reckoned to the dollar. New England currency, then, is to Halifax currency as 5 to 6. Therefore, to reduce New England currency to Halifax currency, take five-sixths of the given sum, thus-

6) £14 5 4 New England currency.

£11 17 44 Halifax currency.

* Without Premium, which varies from 5 to 8 per cent.

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dollar. New . Therefore, ke five-sixths . . .

Reduce £60 4s. 10d. New England currency to Halifax currency. Ans. £50 4s 04d.

INTEREST.

To reduce Halifax currency to sterling money, or to reduce Halifax to New England, it is only necessary to reverse the process in the foregoing operations.

To reduce sterling to Halifax, we multiply by $\frac{10}{9}$, therefore, to reduce Halifax currency to sterling money, —divide the given sum by $\frac{10}{9}$, or, what is the same, multiply by $\frac{10}{10}$, that is, take $\frac{10}{10}$ of the given sum; e. g.

10) £54 0 10 Halifax currency.

5 8 1 9

£48 12 9 sterling money.

In the same manner, to reduce Halifax currency to New England,—take $\frac{6}{5}$ of the given sum, or, add $\frac{1}{5}$ to the given sum.

From the foregoing rules and illustrations the pupil himself will be able, by pursuing a similar course, to reduce, with facility, any currency, the denominations of which are pounds, shillings, &c. to any other in which the denominations are the same.

The following is the general rule for finding a multiplier to reduce any currency to the par of another: Make the number of shillings that are equal to a dollar in the currency to be reduced, the denominator of a fraction; and over this, for a numerator, write the number of shillings that are equal to a dollar in the currency to which the given sum is to be reduced.

Let the pupil find multipliers to reduce New York and Pennsylvania currencies to Halifax, and then Halifax currency to those.

INTEREST.

¶ 75. Interest is an allowance made by a debtor to a creditor for the use of money. It is computed at a certain number of pounds for the use of each hundred pounds, or so many dollars, for each hundred dollars, &cc. one year, and in the same proportion for a greater or less sum, or for a longer or shorter time.

The number of pounds so paid for the use of a hundred pounds, one year, is called the *rate per cent* or *per centum*; the words *per cent*, or *per centum* signifying by the hundred.

The highest rate allowed by law in the Canadas is 6 per cent,^{*} that is, 6 pounds for 100 pounds, 6 shillings for 100 shillings; in other words, $_{T_{57}}$ of the sum lent or due is paid for the use of it one year. This is called *legal* interest, and will here be understood when no other rate is mentioned.

Let us suppose the sum lent or due to be one pound. The hundredth part of one pound or $\frac{1}{100}$ of a pound is, decimally expressed, thus, '01, and $\frac{1}{100}$ of a pound, the legal interest, written as a decimal fraction, is '06. So of any rate per cent.

1 per cent expressed as a common fraction, is

 $\frac{1}{2}$ per cent is a half of one per cent, that is, - '005.

1 per cent is a fourth of one per cent, that is, - '0025.

² per cent is three times a quarter per cent, that is, '0075. Note. The rate per cent is a decimal carried to two places that is, th hundredths; all decimal expressions lower than hundredths are parts of one per cent. ²/₃ per cent, for instance, is '625 of 1 per cent, that is, '00625.

Write 24 per cent as a decimal fraction.

2 per cent is '02, and $\frac{1}{2}$ per cent is '005. Ans. '025. Write 4 per cent as a decimal fraction. $-4\frac{1}{2}$ per cent $-4\frac{3}{4}$ per cent. -5 per cent. $-7\frac{1}{4}$ per cent. $-9\frac{1}{2}$ per cent. $-8\frac{3}{4}$ per cent. (10 per cent is $\frac{10}{100}$; decimally '10) $-10\frac{1}{2}$ per cent. -11 per cent. $-12\frac{1}{2}$ per cent. 15 per cent.

1. If the interest of one pound for a year be '06 of a pound, what will be the interest on $\pounds 25$ for the same time?

It will be 25 times 6 or 6 times 25, which is the same thing :---

25 '06

1'50 answer; that is, £1 and 5 tenths. The 5 tenths must be reduced to shillings, pence and fart ... gs by the rule • In the New England States the legal ra' : is the same as in the Canadas. In England it is 5 per cent. for the re by *inspect* shillings. To find dent we n

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 $\pounds 1'4'$ be regarde auswer. 'J farthings b 8s; call the one 36 eq $\pounds'446$ —8s. year, at $4\frac{1}{2}$

Always, or either de to the deein by the rule. the tenths, and farthin reduction, i perfectly fa

3. What at 3 per cer at 7¹/₂ per ce

for the reduction of decimals; or with sufficient exactness by inspection. See \P 73. '50, or '5 of a pound equal 10 shillings. The interest of £25 for a year is then £1 10s.

To find the interest on any sum for one year, it is evident we need only multiply it by the *rate per cent* written as a *decimal* fraction. The product, observing to place the point as directed in multiplication of decimal fractions, will be the interest required.

Note. PRINCIPAL is the money due, for which interest is paid. AMOUNT is the principal and interest added together. 2. What will be the interest of £32 3s. for one year, at $4\frac{1}{2}$ per cent?

We are to multiply the principal by the rate per cent, $4\frac{1}{2}$, expressed in the form of a *decimal* '045; we must therefore reduce the 3s. in the principal, to decimal's by inspection. We find 3s. equal to '15. There being five decimal places

£32'15 principal. in the multiplicand and mul-'045 rate per cent., tiplier, 5 figures must be point-

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ed off for decimals/from the product, which gives the answer 1 pound and 44675 hundred thousandths. Anything less than thousandths need not

be regarded; hence, £1'446 is sufficiently exact for the answer. The '446 must be reduced to shillings, pence and farthings by inspection. Double the '4 for shillings, equals 8s; call the '046 so many farthings, deducting 2, because one 36 equals 44 farthings. In 44 qrs. there are 11d. $\pounds'446 = 8s. 11d$. The interest, then, of £32.3s. for one year, at 44 per cent, is £1.8s. 11d. *answer*.

Always, then, if there are shillings, pence and farthings, or either denomination, in the given principal, reduce them to the decimal of a pound by inspection, before multiplying by the rule. After obtaining the answer in decimals, reduce the tenths, hundredths and thousandths to shillings, pence and farthings, by inspection. The method of effecting each reduction, is exhibited in \P 73 and 74, and must be made perfectly familiar to the pupil's mind.

3. What will be the interest of £11 3s. 4d. for one year, at 3 per cent? ——at $5\frac{1}{2}$ per cent? ——at 6 per cent? at $7\frac{1}{4}$ per cent? —— at $8\frac{1}{2}$ per cent? —— at $9\frac{3}{4}$ per cent?

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--- at 10 per cent? --- at 10¹ per cent? at 11 per cent? --- at 11² per cent? --- at 12 per cent? --- at 12¹ per cent? --- at 12¹ per cent?

4. A tax on a certain town is £406 15s. 10²d. on which the collector is to receive $2\frac{1}{2}$ per cent for collecting; what will he receive for collecting the whole tax at the rate?

In this example, the shillings, &c. reduced to the decimal of a pound equal '795. Multiply therefore, £406'795 by the rate 21, that is '025. The answer, in decimals, is £10'169; the tenths, &c. reduced to shillings, &c. equal. 3s. 41d. The answer then, is £10 3s. 4d.

Note. In the same way are calculated commission, insurance, buying and selling stocks, loss and gain, or anything else rated at so much per cent without respect to time.

5. What must a man, paying 37¹/₂ per cent on his debts, pay on a debt of £132 5s.? Ans. £49 11s. 10¹/₂d.

6. A merchant having purchased goods to the amount of £580, sold them so as to gain 121 per cent, and in the same proportion for a greater or less sum; what was his whole gain, and what was the whole amount for which he sold the goods? Ans. His whole gain was £72 10s.; whole amount, £652 10s.

7. A merchant bought a quantity of goods for £173 15s. how much must he sell them for to gain 15 per cent? Ans. £199 16s. 3d.

¶ 76. COMMISSION is an allowance of so much per cent to a person called a *correspondent*, *fuctor*, or *broker*, for assisting merchants and others in purchasing and selling goods.

8. My correspondent sends me word that he has purchased goods to the amount of $\pounds 1286$ on my account; what will his commission come to at $2\frac{1}{2}$ per cent? Ans. $\pounds 32$ 3s.

9. What must I allow my correspondent for selling goods to the amount of $\pounds 2317$ 9s. $2\frac{3}{4}d$. at a commission of $3\frac{1}{4}$ per cent? Ans. $\pounds 75$ 6s. 4d.

INSURANCE is an exemption from hazard, obtained by the payment of a certain sum, which is generally so much per cent on the estimated value of the property insured.

PREMIUM is the sum paid by the insured for the insurance.

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obtained by ally so much insured. he insurance. POLICY is the name given to the instrument or writing, by which the contract of indemnity is effected between the insurer and insured.

10. What will be the premium for insuring a ship from Montreal to Liverpool, valued at 9450£, at 41 per cent? Ans. £425 5s.

11. What will be the annual premium for insurance on a house against loss by fire, valued at $875\pounds$ at $\frac{2}{3}$ per cent?

By removing the separatrix 2 figures towards the left, it is evident, the sum itself may be made to express the premium at 1 per cent, of which the given rate parts may be taken; thus, one per cent on $875\pounds$ is 8'75 and $\frac{2}{2}$ of $875\pounds$ is $6'562\pounds$. Ans. $6\pounds$ 11s. 3d.

12. What will be the premium for insurance on a ship and cargo valued at 6310£ at $\frac{1}{2}$ per cent? — at $\frac{2}{3}$ per cent? — at $\frac{3}{4}$ per cent? — at $\frac{4}{5}$ per cent? — at $\frac{3}{5}$ per cent? Ans. at $\frac{5}{5}$ per cent the premium is 39£ 7s. $8\frac{2}{5}$ d.

STOCK is a general name for the capital of any trading company or corporation, or of a fund established by government.

The value of stock is variable. When 100 pounds of stock sells for 100 pounds in *money*, the stock is said to be at *par*, which is a Latin word signifying *equal*; when for *more*, it is said to be above *par*; when for *less*, it is said to be *below* par.

13. What is the value of 756 \pounds of stock, at 12½ per cent? that is, when 1 pound of stock sells for 1 pound 12½ hundredths in *money*, which is 12½ per cent above par, or 12½ per cent *advance*, as it is sometimes called.

Ans. 850£ 11s.

14. What is the value of 3700£ of bank atock, at 95½ per cent? that is 4½ per cent below par? Ans. 3533£ 10s.

15. What is the value of $120\pounds$ of stock, at $92\frac{1}{2}$ per cent? — at 861 per cent? — at 673 per cent? — at 1041 per cent? — at 1081 per cent? — at 115 per cent? at 371 per cent advance?

Loss AND GAIN. 16. Bought a hogshead of molasses for 15 \pounds ; for how much must I sell it to gain 20 per cent? Ans. 18 \pounds .

17. Bought broadcloath at 12s. 6d. per yard; but, it be-

ing damaged, I am willing to sell it so as to lose 12 per cent; how much will it be per yard? Ans. 11s.

18. Bought calico at 1s. per yard; how must I sell it to gain 5 per cent? 10 per cent? 15 per cent? to lose 20 per cent? Ans. to the last, 9¹/₂.

¶ 77. We have seen how interest is cast on any sum of money when the time is one year; but it is frequently necessary to cast interest for months and days.

Now, the interest on $1\mathcal{L}$ for 1 year, at 6 per cent, being '06, is

'01, one hundredth for 2 months,

'005 five thousandth (or $\frac{1}{2}$ a hundredth) for 1 month of 30 days, (for so we reckon a month in casting interest.) and

'001 one thousandth for every 6 days; 6 being contained 5 times in 30.

Hence, it is very easy to cast in the mind, the interest on $1\pounds$, at 6 per cent for any given time. The hundredth, it is evident, will be equal to half the greatest even number of months; the thousandth will be 5 for the odd month, if there be one, and 1 for every time 6 is contained in the given number of the days.

Suppose the interest of $1\pounds$, at 6 per cent, be required for 9 months and 18 days. The greatest even number of the months is 8, half of which will be the hundredths '04; the thousandths, reckoning 5 for the odd month, and 3 for the 18 ($3\times 6=18$) days, will be '008, which, united with the hundredths ('048) give 4 hundredths and 8 thousandths; 4 hundredths, and 8 thousandths, or, '048£ reduced=11d.

Ans. 11d. 1. What will be the interest on $1\mathscr{L}$ for 5 months 6 days? 6 months 12 days? 7 months? 8 months 24 days? 10 months? 11 months 6 days? 12 months 18 days? 15 months 6 days? 16 months?

ODD DAYS.—2. What is the interest of $\pounds 1$ for 13 months 16 days?

The hundredths will be 6, and the thousandths 5, for the odd month, and 2 for 2 times 6 = 12 days, and there is a remainder of 4 days, the interest for which will be such

3. V months 17 day months Note be less a ciphe the last be '06,

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part of 1 thousandth as 4 days is part of 6 days, that is, # = 2 of a thousandth. Ans. '0672.

3. What will be the interest of £1 for 1 month 8 days? _____ 2 months 7 days? _____ 3 months 15 days? _____ 4 months 22 days? _____ 5 months 11 days? _____ 6 months 17 days? _____ 7 months 3 days? _____ 8 months 11 days? _____ 9 months 2 days? _____ 10 months 15 days? _____ 11 months 4 days? _____ 12 months 3 days?

Note. If there is no odd month, and the number of days be less than 6, so that there are no thousandths, it is evident, a cipher must be put in the place of thousandths; thus, in the last example,—12 months 3 days,—the hundreths will be '06, the thousandths 0, the 3 days $\frac{1}{2}$ a thousandth.

Ans. 1s. 22d.

4. What will be the interest of £1 for 2 months 1 day? 4 months 2 days? — 6 months 3 days? — 8 months 4 days? — 10 months 5 days? — for 3 days? for 1 day? — for 2 days? — for 4 days? — for 5 days? 5. What is the interest of £56 2s. 72 d. for 8 months 5 days? The interest of £1, for the given time, is '0402; therefore.

 $\frac{1}{2}$ and $\frac{1}{3}$ \pounds 56'13 principal.

'0404 interest of £1 for the given time.

224520 interest for 8 months. 2806 interest for 3 days. 1871 interest for 2 days.

 $\pounds 2'29197 = \pounds 258.9 \frac{3}{2} d.$

5 days=3 days+2 days. As the multiplicand is taken once for every six days, for 3 days take $\frac{1}{2}$, for 2 days take $\frac{1}{3}$, of the multiplicand. $\frac{1}{2} + \frac{1}{3} = \frac{5}{4}$. So also, if the odd days be 4 = 2 days + 2 days, take $\frac{1}{3}$ of the multiplicand *twice*; for 1 day, take $\frac{1}{4}$.

From the illustrations now given, it is evident,— To find the interest of any sum in Halifax currency, or any other currency of which the denominations are pounds, shillings, &c. at 6 per cent, it is only necessary to multiply the given principal, after having reduced the shillings and pence in it to the decimal of a pound by inspection, by the interest of $1 \pm$ for the given time, found as above directed and written as

a decimal fraction; after pointing off as many places for decimals in the product as there are decimal places in both the factors counted together, these can be reduced back again to shillings and pence by inspection:

EXAMPLES FOR PRACTICE.

6. What is the interest of £87 3s. 97d. for 1 year 3 Ans. £6 108. 94d. months? 1 1 1

7. Interest of £116 1s. 74. for 11 mo. 19 days?

		A	ns. £6 15s. 04d.
·Ir	itere	est of £200 for 8 mo. 4 days?	£8 2s. 74d.
9.	66	of 17s. for 19 mo. ?	1s. 71d.
10.	.66	of £8 10s. for 1 year 9 mo. 1	12 days?
		,	18s. 27d.
11.	66	of £675 for 1 mo. 21 days?	£5 14s. 8 ² d.
12.	"	of £8673 for 10 days?	£14 9s. 11d.
13.	"	of 14s. 71d. for 10 mo.?	
14.	"	of £96 for 3 days?) Note. The
15.	"	of £73 10s. for 2 days ?	interest of £1
16.	"	of £180 15s. f r 5 days?	for 6 days be-
17.	**	of £15000 for 1 day?	ing 1 thou-
sandth,	the	pounds themselves express the	interest in thou-
	-	· · · · · · · · · · · · · · · · · · ·	

sandths for six days, of which we may take parts Thus, 6)15000 thousandths,

2'500, that is, £2 10s. Ans. to the last. When the interest is required for a large number of years. it will be more convenient to find the interest for one year, and multiply it by the number of years; after which find the interest for the months and days, if any, as usual.

18. What is the interest of $\pounds 1000$ for 120 years?

Ans. £7200.

19. What is the interest of £520 0s. 9²/₄d. for 30 years Ans. £951 13s. 57d. and 6 months?

20. What is the interest on £400 for 10 years 3 months and 6 days? Ans. £246 8s.

21. What is the interest of £220 for 5 years? ---- for 12 years? — 50 years? Ans. to the last, £660.

22. What is the amount of $\pounds 86$, at interest 7 years? Ans. £122 2s. 43d.

23. What is the interest of \$48'30 for 1 year? It must be clear to the pupil's mind, that to obtain the

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¶ 78, 79.

INTEREST.

interest upon any sum in federal money, for any time, we proceed just as we do in Halifax currency; only we are not compelled to reduce any part of the given sum to decimals, since all the denominations of federal money are in a decimal ratio. The answer to the last example is \$2,899.

What is the interest of \$64 for 2 years? Ans. \$7'68. What is the interest of \$93'50 for 7 years, 6 months and 10 days? Ans. \$44'489.

¶ 78. 1. What is the interest of 36 pounds for 8 months, at 44 per cent?

Note. When the rate is any other than six per cent, first find the interest at six per cent, then divide the interest so found by such part as the interest, at the rate required, exceeds or falls short of the interest, at six per cent, and the quotient added to or subtracted from the interest at six per cent, as the case may be, will give the interest required.

£36

£1'08 £1 1s. 71d. answer.

2. Interest of £54 16s. 2²/₁d. for eighteen months, at five per cent ? Ans. £4 2s. 2¹/₂d.

3. Interest of £500 for nine months and nine days, at eight per cent? Ans. £31.

4. Interest of £62 2s. 4²/₄d. for one month and twenty days, at four per cent? Ans. 6s. 10²/₄d.

5. Interest of £85 for ten months and fifteen days, at 12} per cent? Ans. £9 5s. 10²/₂d.

6. What is the amount of £53 at ten per cent for seven months? Ans. £56 1s. $9\frac{3}{4}$ d.

The time, rate per cent and amount given, to find the principal.

¶ 79. 1. What sum of money, put at interest at 6 per cent, will amount to $\pounds 61$ Qs. $4\frac{2}{4}$ d. in 1 year 4 months ?

The amount of £1 at the given rate and time is £1'08; hence £61'02: £1'08=56'50, the principal required; that is, find the amount of £1 at the given rate and time, by which divide the given amount; the quotient will be the principal required. Ans. £56 10s.

2. What principal, at 8 per cent, in 1 year 6 months. will amount to £85 2s. 43d.? Ans. £76.

3. What principal, at 6 per cent, in 11 months 9 days, will amount to £99 6s. 23d.? Ans. £94.

4. A factor receives £988 to lay out after deducting his commission of 4 per cent; how much will remain to be laid out?

It is evident he ought not to receive commission on his This question, therefore, in principle, does own money. not differ from the preceding.

Note. In questions like this, where no respect is had to time, add the rate to $\pounds 1$. Ans. £950.

5. A factor receives £1008 to lay out after deducting his commission of 5 per cent; what does his commission amount to? Ans. £48.

DISCOUNT.—6. Suppose I owe a man $\pounds 397$ 10s. to be paid in 1 year, without interest, and I wish to pay him now, how much ought I to pay him when the usual rate is 6 per cent? I ought to pay him such a sum as, if put at interest, would, in one year, amount to £397 10s. The question, therefore, does not differ from the preceding. Ans. £375.

Note. An allowance made for the payment of any sum of money before it comes due, as in the last example, is called discount.

The sum which, put at interest, would, in the time and at the rate per cent for which discount is to be made, amount to the given sum, or debt, is called the present worth.

7. What is the present worth of $\pounds 834$ payable in 1 year, 7 months and 6 days, discounting at the rate of 7 per cent? Ans. £750.

8. What is the discount on £321 12s. 74d. due 4 years hence, discounting at the rate of 6 per cent?

Ans, £62 5s. 2²/₄d.

9. How much ready money must be paid for a note of £18, due fifteen months hence, discounting at the rate of 6 per cent? Ans. £16 14s. 104d.

10. Sold goods for $\pounds 650$, payable one half in 4 months, and the other half in 8 months; what must be discounted Ans. £18. for present payment?

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le in 1 year, 7 per cent? ns. £750. due 4 years

2 5s. $2\frac{2}{4}$ d. for a note of the rate of 6 14s. 10 $\frac{1}{2}$ d. in 4 months, discounted Ans, £18, ¶ 80, 81, 82.

INTEREST.

11. What is the present worth of £56 4s. payable in one year eight months, discounting at 6 per cent?——at 41 per cent?——at 5 per cent?——at 71 per cent?——at 9 per cent? Ans. to the last £48 17s. 42d.

The time, rate per cent, and interest being given to find the principal.

¶ **SO.** 1. What sum of money put at interest sixteen months, will gain \pounds 10 10s. at 6 per cent?

 $\pounds 1$ at the given rate and time, will gain '08; hence, $\pounds 10'50 \div \pounds'08 = \pounds 131'25$, the principal required; that isfind the interest of $\pounds 1$ at the given rate and time, by which divide the given gain or interest; the quotient will be the principal required. Ans. $\pounds 131 5s$.

2. A man paid \pounds 4 10s. 4²/₄d. interest at the rate of 6 per cent at the end of 1 year 4 months; what was the principal? Ans. \pounds 56 10s.

3. A man received for interest on a certain note at the end of one year $\pounds 20$; what was the principal, allowing the rate to have been 6 per cent? Ans. £333 6s. 8d.

The principal, interest and time being given, to find the rate per cent.

¶ S1. 1. If I pay \pounds 3 15s. 7¹/₄d. interest for the use of \pounds 36 for 1 year 6 months, what is that per cent?

The interest on £36 at one per cent, the given time, is $\pounds'54$; hence $\pounds 3'78 \div \pounds'54 = 07$, the rate required; that is, find the interest on the given sum, at one per cent, for the given time, by which divide the given interest; the quotient will be the rate at which interest was paid. Ans. 7 per ct.

2. At \pounds 2 6s. 9 $\frac{1}{2}$ d. for the use of \pounds 468 for a month, what is the rate per cent? Ans. 6 per cent.

3. At \pounds 46 16s. for the use of \pounds 520 for two years, what is that per cent? Ans. $4\frac{1}{2}$ per cent.

The prices at which goods are bought and sold, being given, to find the rate per cent of GAIN or LOSS.

¶ 82. 1. If I purchase cloth at £1 2s. a yard, and sell it at £1 7s. 6d. per yard; what do I gain per cent?

This question does not differ essentially from those in the foregoing paragraph. Subtracting the cost from the price O2

at sale, it is evident I gain \pounds 275 on a yard; that is $\frac{2}{140}$ of the first cost. $\frac{2}{140}$ 25 per cent, the answer. That is,—make a common fraction, writing the gain or loss for the numerator, and the price at which the article was bought for the denominator, then reduce it to a decimal.

2. A merchant purchases goods to the amount of £550; what per cent profit must he make to gain £66?

Ans. 12 per cent. 3. — What per cent profit must he make on the same purchase to gain £38 10s.? — to gain £24 15s.? to gain £2 15s.

Note. The last gain gives for a quotient '005, which is $\frac{1}{2}$ per cent. The rate per cent, it will be recollected, (¶ 75, note,) is a decimal carried to two places, or hundredths; all decimal expressions *lower* than hundredths are parts of one per cent.

4. Bought a hogshead of liquor, containing 114 gallons, at \pounds '96 per gallon, and sold it at \pounds 1 0s. 0d. $3\frac{1}{5}$ qrs. per gal. what was the whole gain, and what was the gain per cent?

Ans. £4 18s. $5\frac{3}{4}$ d. whole gain. $-4\frac{1}{2}$ gain per cent. 5. A merchant bought a quantity of tea for £365, which, proving to have been damaged, he sold for £332 3s.; what did he lose per cent? Ans. 9 per cent.

6. If I buy cloth at $\pounds 2$ per yard, and sell it for $\pounds 2$ 10s. per yard, what should I gain in laying out $\pounds 100$. Ans. $\pounds 25$.

7. Bought indigo at 6s. per lb. and sold the same at 4s, 6d. per lb.; what was the loss per cent? Ans. 25 per cent.

8. Bought 30 hogshead of liquors at £600; paid in duties £20 13s. $2\frac{3}{4}d$; for freight £40 15s. $7\frac{1}{4}d$; for porterage £6 1s.; and for insurance £30 16s. $9\frac{2}{4}d$; if I sell them at £26 per hogshead, how much shall I gain per cent?

Ans. 11'695 per cent.

The principal, rate per cent, and interest being given, to find the time.

¶ **S3.** 1. The interest on a note of £36, at 7 per cent, was £3 15s. $7\frac{3}{4}d$; what was the time ?

The interest on £36 for a year, at ? per ct, is £2 10s. $4\frac{3}{4}$ d. £3'78:£2'52=1'5 years, the time required ; that is—find the interest for one year on the principal given, at the given rate by which divide the given interest; the quotient will

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14 gallons, rs. per gal. 1 per cent? per cent. 3**65, wh**ich, 2 3s.; what per cent. for £2 10s. Ans. £25. same at 4s. 25 per cent. id in duties r porterage sell them at ent? per cent.

g given, to

7 per cent,

2 10s. 4⁴d. hat is—find it the given uotient will ¶ 83.

INTEREST.

be the time required in years and decimal parts of a year; the latter may then be reduced to months and days.

Ans. 1 year 6 months.

2. If £31 14s. $2\frac{2}{4}$ d. interest be paid on a note of £226 10s. what was the time, the rate being 6 per cent?

Ans. $2'33_{3}=2$ years 4 months.

3. A note of $\pounds 600$, paid interest $\pounds 20$, at 8 per cent; what was the time ?

Ans '416 \pm 5 months so nearly as to be called 5, and would be exactly 5, but for the fraction lost.

4. The interest on a note of $\pounds 217$ 5s. at 4 per cent was $\pounds 28$ 4s. 10d.; what was the time? Ans. 3 yrs. 3 mos.

Note. When the rate is 6 per cent, we may divide the interest by half the principal, removing the separatrix two places to the left, and the quotient will be the answer in months.

The method given above, of finding the interest upon any sum in Halifax currency, for any time, and at any rate, will be found sufficiently exact in practice, and as simple and concise, perhaps, as any that could be proposed.

The teacher will do well to see that the scholar understands perfectly the process by which the reciprocal reductions are effected by inspection, and the reason of this process.

If greater exactness be required, the reductions can be effected by the ordinary rules for the reduction of decimal fractions.

The following is a method of casting interest by *vulgar* fractions.

To obtain the interest upon any sum for any time, at any rate :---Multiply the lowest terms of a fraction, the numerator of which is the given rate, and the denominator 100, by the given number of years; multiply the lowest terms of a fraction, the numerator of which is the given rate, and the denominator 1200, by the given number of months; multiply the lowest terms of a fraction the numerator of which is the given rate, and the denominator 3600, by the given number of days; then reduce these several fractions to one common denominator; add them together, and by the resulting fraction multiply the given principal.

Find the interest of £100 for 2 yrs. 6 mo. 10 dy. at 6 per ct. $\frac{3}{5^{3}}$ (or $\frac{6}{160}$) \times 2 years $= \frac{6}{5^{3}}$

 $\frac{1}{200}$ (or $\frac{1}{1200}$) \times 6 months= $\frac{6}{200}$

80'00 (or 38800) × 10 days=880=880=880

 $\frac{5}{5\sigma}$, $\frac{2}{5\sigma}$, $\frac{1}{5\sigma}$, $\frac{1}{5\sigma}$ are to be reduced to one common denominator. Neglect the ciphers in the denominators—

 $5 \times 2 \times 6 = 60$; 1 + 2 + 2 = 5, the number of ciphers. The common denominator is then 60 and 5 ciphers.

 $6 \times 2 \times 6 = 72$; this with 4 ciphers is first numerator.

 $5 \times 6 \times 6 = 180$; this with 3 ciphers is 2d numerator.

 $5 \times 2 \times 1 = 10$; this with 3 ciphers is 3d numerator.

Each numerator has as many as 3 ciphers; cut off three from each, and three from the common denominator; ${}_{6700}^{720}$ +188 + ${}_{600}^{10}$ = ${}_{6000}^{91}$ = ${}_{600}^{91}$. Then £100, the given principal, multiplied by ${}_{600}^{91}$ = ${}_{600}^{91}$ = £15 3s. 4d.

The reasons of the different steps in the foregoing process will appear : when the rate, as in the above example, is 6 per cent, it is obvious that the interest of any given principal for one year is T_{00}^{6} or T_{00}^{3} of that principal. For any number of years, the interest must be as many times $\frac{3}{23}$ of the principal as there are units in the given number of years. In the example, 2 is the given number of years; multiply then $\frac{3}{50}$ by 2; or multiply the lowest terms of a fraction, the numerator of which is the given rate, and the denominator 100, by the given number of years. $\frac{6}{50}$ of the given principal then is the interest for 2 years. T200 of the given principal is the interest for 1 month; for there are 12 months in a year, and $_{16\sigma} \times _{12} = _{120\sigma} or _{20\sigma}$. 3800 Of the given principal is the interest for 1 day; for there are 30 days in 1 month, and $\frac{6}{1200} \times \frac{1}{30} = \frac{6}{3600} = \frac{1}{6000}$. We have then $\frac{3}{50}$ of given principal, as the interest for 1 year; $\frac{1}{2} \frac{1}{2} \frac{1}$ we have $\frac{3}{50} \times 2 = \frac{6}{50}$; for 6 months $\frac{1}{200} \times 6 = \frac{6}{200}$; for ten days, 5000 × 10=580=500. 50, 280 and 500 then of the given principal are the interest of $\pounds 100$ for 2 years, 6 months and 10 days. It is clear now, why we reduce these several fractions to one common denominator, add them together, and by the resulting fraction multiply the given principal.

Find the interest upon $\pounds 78$ 4s for 3 years, 9 months and 6 days, by this method, at 6 per cent and also at 5 per cent.

¶ 84. To find

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T S4 any par notes o method and also in merce RULE the note ment, w each en amounts amount

1. For or order, £100

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What wa The w which is 15s. for t for which £132-10 for which £10; the time of p which in 7 mo. 8 which, a 15s. 3d. endorsem of its dat this inter ¶ 84.

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onths and per cent. To find the interest due on Notes, &c. when partial payments have been made.

T 84. There is no statute in this Province, prescribing any particular form or method of casting interest upon notes or other obligations. It is believed the following method is generally allowed before the courts of the country, and also is that which has obtained to the greatest extent in mercantile transactions.

RULE.—Compute the interest upon the value for which the note or other instrument was given, to the time of payment, which add to the principal; find the amount also of each endorsement to the time of payment, which several amounts add together, and the sum subtract from the amount of the value upon the face of the note, or other instrument.

1. For value received, I promise to pay Louis Rousseau, or order, one hundred pounds fifteen shillings, with interest. £100 15s. Joun Burton.

May 1, 1822.

On this note were the following endorsements.

Dec.	25,	1822,	received	£10	
July	19,	1823,	66	· 1	4 s.
Sept.	<u>ا</u> ,	1824,	"	3	6s.
June	14,	1825,	"	21	15s.
April	115,	.1826	, "	54	9s.

What was due Aug. 3, 1827?

Ans. £31 3s. 1d.

The whole time is, from May 1st, 1822, to Aug. 3, 1827, which is 5 years, 3 months, 2 days. The interest of $\pounds 100$ 15s. for this time is £31 15s. $4\frac{2}{4}$ d. This added to the value for which the note u as given is £100 15s.+£31 15s. $4_{\rm f}^2$ d.= £132 10s. $4\frac{2}{4}$ d. which is equal to the amount of the value The first endorsement is for which the note was given. $\pounds 10$; the date of this endorsement is Dec. 25, 1822; the time of payment is Aug. 3, 1827. The time, therefore, for which interest is to be cast upon this endorsement, is 4 yrs. 7 mo. 8 ds. The interest for this time is $\pounds 2$ 15s. 3d. which, added to the endorsement, makes its amount $\pounds 12$ 15s. 3d. In the same way find the amount of each other endorsement, by casting the interest upon it from the day of its date to the day of the payment of the note, and add this interest to the principal, that is, the endorsement.

COMPOUND INTEREST. ¶ 84,85.

The	e 2d end	lorsement	is -	-	-	· -	3	6 1	4s.
	3d	66		•	•	-	-	3	6s.
	4th	"	-	-				21	158.
	5th	66		-				54	9s.
The	e time fo	or which	interest	is to	be d	cast u	pon t	he	
2d end	dorseme	nt is -	-	4 ve	ears,	0 m	onths,	23	days
3d	"	-		2	"	11	66 J	2	ű
4th	65		-	2	"	1	"	19	"
5th	"	-		1	"	3	"	18	"
							£	s.	d.
The	e interes	st upon th	e 2d e	ndor	seme	nt is	0	5	10
•	"	. . .	3d		""		0	11	6 <u>3</u>
	"	"	4th		"		2	15	81
3		, "	5th		"		4	.4	111
The	e amoun	t of the 2	d endo	rsem	ent i	s	1	'9	10
	**	13	d	"			3	17	63
	**	4	th	"			24	10	87
	66	5	th	**			58	13	117
The a	imount c	of 1st endo	orsemen	t we	foun	d to b	e 12	15	3
Fhe s	um of th	e amounts	of all t	he er	ndors	ement	ts 101	7	33
The v	alue up	on the fac	e of the	e not	e is	-	100	15	0
The a	mounto	f this valu	ie is	-	-	-	132	10	42
Subtr	act the s	um of am	ounts of	end	orsei	ments	101	7	33

Balance due Aug. 3d 1827, £ 31 3 1 2. For value received, I promise to pay Thomas Wilson, or order, two hundred thirty-eight pounds eighteen shillings, with interest.

h interest. £238–18s. Charles Stewart. _____ Jan. 6, 1820.

On this note were the following endorsements, viz :

	•		£ s.	d.
April 16, 1823, received	-	-	23 10	0
April 16, 1825, "	-		19 4	0
Jan. 1, 1826, "	-	-	87 19	0
Vhat was due July 11, 1827?				

COMPOUND INTEREST.

¶ 85. A. promises to pay B. $\pounds 256$ in three years, with interest annually; but at the end of one year, not finding it convenient to pay the interest, he consents to pay interest

2. At and wha amount for 6 yes

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¶ 84, 85.	¶ 85.2 COMPOUND INTEREST. 167	¢
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	on the interest from that time, the same as on the principal. Note.—Simple Interest is that which is allowed for the principal only; compound interest is that which is allowed for both principal and interest, when the latter is not paid at the time it becomes due. Compound Interest is calculated by adding the interest to the principal at the end of each year, and making the amount the principal for the next succeeding year. 1. What is the compound interest of £256 for three years, at 6 per cent?	,
0 5 10	$\pounds 256$ given sum or first principal.	
0 11 63	'06 '	
2 15 8		
4 4 11	15%6 interest, b to be added together.	
1 9 10	256'00 principal,) to 20 alloca togetheri	
$3 17 6_4^3$	971'36 amount or principal for second year	
58 13 11	'06	
12 15 3		
$01 7 3\frac{3}{4}$	16'2816 compound interest 2d year,) added	
00 15 0	271'36 principal, do stogether	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	287'6416 amount or principal for 3d year. '06	
31 3 1 nas Wilson, en shillings,	17"258496 compound interest 3d year, added 287'641 principal, do together	
TEWART.	304'899amount.256first principal subtracted.	
s, viz: s. d . 10 0 4 0 19 0	£48'899 compound interest for three years. Ans. £48 17s. 11 ³ d. 2. At 6 per cent, what will be the compound interest, and what the amount of £1 for two years? — what the amount for 3 years? — for 4 years? — for 5 years? for 6 years? — for 7 years? — for 8 years?	
years, with ot finding it pay interest	It is plain that the amount of £2, for any given time, will be two times as much as the amount of £1; the amount of £3 will be three times as much, &c.	

Hence, we may form the amounts of one pound, for several years, into a table of *multipliers* for finding the amount of any sum, for the same time.

TABLE,

Showing the amount of One Pound or One Dollar &c. for any number of years not exceeding 24, at the rates of 5 and 6 per cent Compound Interest.

lears	5 per cent	6 per cent	Years	5 per cent	6 per eent
1	1.05	1'06	13	1'88564-	2'13292+
2	1'1025	1.1236	14	1'97993-	2'26090+
3	1'15762+	1-19101-+	15	2'07892 +	2'39655+
4	1'21550+	1'26247+	16	$2^{\cdot}18287 +$	2'54035
5	1'27628+	1'33822+	17	2'29201+	2'69277+
6	1'34009-	1'41851-	18	2'40661+	2'85433
7	1'40710+	1'50363+	19	2'52695	3'02559+
8	1'47745+	1'59384-	20	2'65329+	3'20713+
9	1'55132+	1'68947+	21	2'78596+	3'39956+
10	1'62889+	1'79084+	22	2.92526+	3'60353+
11	1'71033+	1'89829-	23	3.07152+	3'81974+
12	1'79585+	2.01219+	24	3'22509+	4'04893

Note 1. Four decimals in the above numbers will be sufficiently accurate for most operations.

Note 2. When there are months and days, you may first find the amount for the years, and on that amount cast the interest for the months and days; this added to the amount, will give the answer.

3. What is the amount of £600 10s. for 20 years at 5 per cent, compound interest? — at 6 per cent?

£1 at 5 per cent by the table' is £2'65329; therefore, 2'65329×600'50=£1593'30+is £1593 6s. Ans. at 5 per cent; and 3'20713×600'50=£1925'881+is £1925 17s. 74d. ans. at 6 per cent.

4. What is the amount of £40 4s. at 6 per cent compound interest, for 4 years? — for 10 years? — for 18 years? — for 12 years? — for 3 years and 4 months? — for 24 years, 6 months and 18 days?

Ans. to the last £168 2s. 83d.

Note. Any sum at compound interest will double itself in 11 years, 10 months and 22 days. lowin

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COMPOUND INTEREST.

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4'04893-

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0 years at 5 nt? 9; therefore,

Ans. at 5 per £1925_17s.

er cent com-? —— for 18 nd 4 months?

68 2s. 8^3_4 d. double itself From what has now been advanced, we deduce the following general

RULE.

1. To find the interest when the time is one year, or, to find the rate per cent on any sum of money, without respect to time, as the premium for insurance, commission, &c.— Multiply the principal or given sum, after having reduced the shillings and pence in it to the decimal of a pound, by the rate per cent, written as a decimal fraction; after pointing off as many places for decimals in the product as there are decimals in both the factors, and reducing these decimals back to shillings and pence, we shall obtain the interest required.

II. When there are months and days in the given time, to find the interest on any sum of money at 6 per cent,— Multiply the principal, reducing the shillings and pence by inspection, by the interest on one pound for the given time found by inspection, and the product, as before, will be the interest required, taking care to reduce the decimal parts to shillings and pence by inspection.

III. To find the interest on one pound at 6 per cent, for any given time by inspection,—It is only to consider that half the greatest even number of months will denote *kundredths* of a pound, and that there will be five thousandths of a pound for the odd month, (if there be one) and one thousandth for every six days.

IV. If the sum given be in federal money,—The denominations being in a decimal ratio, we are saved from the necessity of effecting the reciprocal reductions, at the beginning and end of the process, otherwise proceed precisely as in Halifax currency.

V. If the interest required be at any other rate than six per cent, (if there be months, or months and days in the given time,)—First find the interest at six per cent; then divide the interest so found by such part or parts, as the interest, at the rate required, exceeds, or falls short of the interest at six per cent, and the quotient, or quotients, added to or subtracted from the interest at six per cent, as the case may require, will give the interest at the rate required.

Note. The interest on any number of pounds, for 6 days at 6 per cent, is readily found by cutting off the unit or

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right hand figure; those at the left hand will show the interest in hundredths for 6 days.

EXAMPLES FOR PRACTICE.

1 2 P

1. What is the interest of $\pounds 1600$ for 1 year 3 months? Ans. $\pounds 120$.

2. What is the interest of £5 16s. for 1 year 11 months? Ans. 13s. 4d.

3. What is the interest of £2 5s. 9½d. for 1 month 19 days, at 3 per cent? Ans. 2½d.

4. What is the interest of £18 for 2 years 14 days at 7 per cent? Ans. £2 11s. 44d.

5. What is the interest of £17 13s. 74d. for 11 months 28 days? Ans. £1 1s. 1d.

6. What is the interest of £200 for 1 day? ---- 2 days? 3 days? ----- 4 days? ----- 5 days?

Ans. for 5 days, 3s. 33d.

7. What is the interest of half \pounds '001 for 567 years ? Ans. 4d.

8. What is the interest of £81 for 2 years 14 days, at $\frac{1}{2}$ per cent? $\xrightarrow{2}$ per cent

9. What is the interest of £'09 for 45 years, 7 months, 11 days? Ans. 4s. 101d.

10. A.'s note of £175 was given Dec. 6, 1798, on which was endorsed a year's interest; what was due 1st Jan. 1803?

Note. Consult Ex. 16, Supplement to Subtraction of Compound Numbers. Ans. £207 4s. 4³/₂d.

11. B.'s note of £56 15s. was given June 6, 1801, on interest after 90 days; what was there due 9th Feb. 1802? Ans. £58 3s. 94d.

12. C.'s note of £365 was given Dec. 3, 1797; June 7, 1800, he paid £97 3s. $2\frac{1}{2}$ d.; what was there due 11th Sept. 1800? Ans. £327 0s. 74d.

13. Supposing a note of £422, dated July 5, 1797, on which were endorsed the following payments, viz. Sept. 13, 1799, £208 4s.; March 10, 1800, £96; what was there due 1st Jan. 1801 ?

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3 months? s. £120. [1 months? 13s. 4d. month 19 4ns. 2¹/₄d. 4 days at 7 11s. 4¹/₂d. 11 months 11 s. 1d. 2 days?

, 3s. 33d. years? Ans. 4d. 4 days, at ½ ----- 2 per -5 per cent? cent? 8 per — 12 per 2s. 10¹d. s, 7 months. 4s. 10¹d. 8, on which Jan. 1803? otraction of 7 4s. 43d. 6, 1801, on Feb. 1802? 8 3s. 9¹/₂d. 97; June 7, e 11th Sept. 7 Os. 71d. 5, 1797, on z. Sept. 13, as there due

SUPPLEMENT TO INTEREST.

Sapplement to Interest.

QUESTIONS.

1. What is interest? 2. How is it computed ? 3. What is under-stood by rate per cent? 4. — by principal? 5. — by amount? 6. — by legal interest? 7. — by commission ? 8. — insur-ance? 9. — premium ? 10. — policy? 11. — Stock ? 12. What is understood by stock being at par ? 13 .--- above par ? 14. -below par? 15. The rate per cent is a decimal carried to how many places ? 16. What are decimal expressions lower than hundredths ? 17. How is interest (when the time is one year) commission, insurance, or anything else rated at so much per cent without respect to time, found? 18: When the rate is one per cent, or less, how may the operation be contracted ? 19. How is the interest on one pound at 6 per cent, for any given time, found by inspection? 20. How is interest cast at 6 per cent, when there are months and days in the given time? 21. When the given time is less than 6 days, how is the interest most readily found ? 22. If the sum given be in federal money, how is interest cast ? 23. When the rate is any other than 6 per cent, if there be months and days in the given time, how is the interest found? 24. What is the rule for casting interest on notes, &c. when partial payments have been made ? 25. How may the principal be found, the time. rate per cent and amount being given ? 26. What is understood by discount? 27. ---- by present worth ? 28. How is the principal found, the time, rate per cent and interest being given? 29. How is the rate per cent of gain or loss found, the prices at which goods are bought and sold being given ? ,30. How is the rate per cent found, the principal, interest and time being given ? 31. How is the time found, the principal, rate per cent and interest being given 1: 32. How may interest be cust by vulgar fractions? 33. What is the ressoning in regard to this rule? 34. What is simple interest? 35.

EXERCISES.

1. What is the interest of £273 10s. $2\frac{1}{2}d$. for 1 year 10 days, at 7 per cent? Ans. £19 13s. $6\frac{1}{2}d$.

2. What is the interest of £486 for 1 year 3 months 19 days, at 8 per cent? Ans. £50 13s. 4²/₄d.

3. D.'s note of £203 was given Oct. 5, 1808, on interest after 3 months; Jan. 5, 1809, he paid £50; what was there due 2d May, 1811? Ans. £175 7s. 2d.

4. E.'s note of \pounds 870 was given Nov. 17, 1800, on interest after 90 days; Feb. 11, 1805, he paid \pounds 186; what was there due 23d Dec. 1807? Ans. \pounds 1009 11s. 63d.

5. What will be the annual insurance, at § per cent, on a house valued at £1600? Ans. £10.
SUPPLEMENT. TO INTEREST.

6. What will be the insurance of a ship and cargo, valued at £5643 at 1½ per cent? — at $\frac{4}{5}$ per cent? — at $\frac{1}{16}$ per cent? — at $\frac{1}{12}$ per cent?

Note. Consult ¶ 76, ex. 11. Ans. at # per cent £42 6s. 54d. 7. A man having compromised with his creditors at 624

per cent, what must he pay on a debt of £137 9s. $2\frac{1}{2}$ d. ? Ans. £85 18s. 3d.

8. What is the value of £800 Montreal Bank stock, at 1124 per cent? Ans. £900.

9. What is the value of £560 15s. of stock, at 93 per cent? Ans. £521 9s. 111d.

10. What principal, at 7 per cent, will, in 9 months 18 days, amount to £422 8s. ? Ans. £400.

11. What is the present worth of £426, payable in 4 years 12 days, discounting at the rate of 5 per cent?

In large sums, to bring out hundredths and thousandths correctly, it will sometimes be necessary to extend the decimal in the divisor to five places. Ans. £354 10s. 1.4d.

12. A merchant purchased goods for £250, ready money, and sold them again for £300, payable in 9 months; what did he gain, discounting at 6 per cent? Ans. £37 1s. $7\frac{1}{2}d$.

13. Sold goods for £3120, to be paid one half in three months, and the other half in six months; what must be discounted for present payment? Ans. £68 9s. 10d.

14. The interest on a certain note for 1 year 9 months was $\pounds 49$ 17s. 6d.; what was the principal? Ans. $\pounds 475$.

15. What principal, at 5 per cent, in 16 months 24 days, will gain £35? Ans. £500.

16. If I pay \pounds 15 10s. interest for the use of \pounds 500, nine months and nine days, what is the rate per cent?

17. If I buy candles at \$'167 per ib, and sell them at 20 cents, what shall I gain in laying out \$100?

Ans. \$19'76.

18: Bought hats at 4s. a-piece, and sold them again at 4s. 9d.; what is the profit in laying out $\pounds 100?$

Ans. £18 15s.

and sold it for \$40; what was gained or lost per cent?

20. At 4s: 6d. profit on one pound, how much is gained in laying out £100, that is, how much per cent?

Ans. £22 10s.

21. E to gain 22. E must it 23. E so good how mu 24. E but by s I sell th cost at t 25. A freight \$25; ho

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21. Bought cloth at \$4'48 per yard; how must I sell it to gain 121 per cent? Ans. 85'04. 1 .

22.' Bought a barrel of powder for £4; for how much must it be sold to lose 10 per cent ? Ans. £8 12s.

23. Bought cloth at 15s. per yard, which, not proving so good as I expected, I am content to lose '171 per cent ; how must I sell it per yard? Ans 128. 41d.

24. Bought 50 gallons of brandy at 92 cents per gallon, but by accident, ten gallons leaked out; at what rate must I sell the remainder per gallon, to gain upon the whole cost at the rate of ten per cent? Ans. \$1'265 per gal.

25. A merchant bought ten tons of iron for \$950; the freight and duties came to \$145, and his own charges to \$25; how must he sell it per lb, to gain twenty per cent by it? Ans. 6 cents per lb.

Equation of Payments.

¶ 86. Equation of Payments is the method of finding the mean time for the payment of several debts due at different times.

1. In how many months will one pound gain as much as five pounds will gain in six months?

2. In how many months will one pound gain as much as forty pounds will gain in fifteen months? Ans. 600.

3. In how many months will the use of five pounds be worth as much as the use of one pound for forty months?

4. Borrowed of a friend one pound for twenty months; afterwards lent my friend four pounds; how long ought he to keep it to become indemnified for the use of the one pound?

5. I have three notes against a man; one of $\pounds 12$, due in three months; one of £9, due in five months; and the other of $\pounds 6$, due in ten months; the man wishes to pay the whole at once; in what time ought he to pay it?

£12	for	3	months	is th	e same	as £1	for 36	months	5,
9		5	"		"	1	45	**	
6		10	"		**	1	60		ÿ
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27							141		
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He might therefore have one pound 141 (months, and he may keep twenty-seven pounds 27 part as long ? ithat is, 141 months 6 - days, Anso barred a name 1 55

Hence,—To find the mean time for several payments,— RULE Multiply each sum by its time of payment, and divide the sum of the *products* by the sum of the *payments*, and the quotient will be the answer.

Note. This rule is founded on the supposition that what is gained by keeping a debt a certain time after it is due, is the same as what is lost by paying it an equal time before it is due; but in the first case the gain is evidently equal to the interest on the debt for the given time, while in the second case the loss is only equal to the discount of the debt for that time, which is always less than the interest; therefore, the rule is not exactly true. The error, however, is so trifling, in most questions that occur in business, as - scarce to merit notice.

6. A merchant has owing to him £300, to be paid as follows: £50 in two months, £100 in five months, and the rest in eight months; and it is agreed to make one payment of the whole; in what time ought that payment to be?

7. A. owes B. £136, to be paid in ten months; £96 to be paid in seven months; and £260 to be paid in 4 months; what is the equated time for the payment of the whole?

Ans. 6 months 7 days+. S. A. owes B. \$600, of which 200 is to be paid at the present time, 200 in four months, and 200 in eight months; what is the equated time for the payment of the whole?

Ans. 4 months.

9. A. owes B. \$300, to be paid as follows: $\frac{1}{2}$ in three months, $\frac{1}{4}$ in four months, and the rest in six months; what is the equated time? Ans. $\frac{41}{4}$ months.

Ratio : or Relation of Numbers.

¶ 87. 1. What part of a gallon is three quarts? one gallon is four quarts, and three quarts is $\frac{3}{4}$ of four quarts. Ans. $\frac{3}{4}$ of a gallon. quarts, and $\frac{1}{3}$ 3. N

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187. RATIO; OR THE RELATION OF NUMBERS.

 $\frac{1}{2}$. What part of 3 quarts is one gallon? 1 gallon being 4 quarts, is $\frac{4}{3}$ of 3 quarts; that is, 4 quarts is 1 time 3 quarts and $\frac{1}{3}$ of another time. 11 to $Ans. \frac{4}{3} = 1\frac{1}{3}$.

3. What part of five bushels is twelve bushels?

Finding what part one number is of another, is the same as finding what is called the *ratio* or *relation* of one number to another; thus, the question, What part of five bushels is twelve bushels? is the same as What is the ratio of five bushels to twelve bushels? The *answer* is $\frac{1}{2}=2\frac{2}{5}$.

Ratio, therefore, may be defined the number of times one number is contained in another; or, the number of times one quantity is contained in another quantity of the same kind.

4. What part of eight yards is thirteen yards? or, What is the ratio of 8 yards to 13 yards?

13 vards is $\frac{1}{8}$ of 8 yards, expressing the division fractionally. If now we perform the division, we have for the ratio 13; that is, 13 yards is one time 8 yards, and 5 of another time.

We have seen (¶ 15, sign,) that division may be expressed fractionally. So also the ratio of one number to another, or the part one number is of another, may be expressed fractionally; to do which, make the number which is called the *part*, whether it be the larger or the smaller number, the *numerator* of a fraction, under which write the other number for a denominator. When the question is, What is the ratio, &c.? the number last named is the *part*; consequently it must be made the numerator of the fraction, and the number first named the denominator.

5. What part of 12 pounds is 11 pounds? or, 11 pounds is what part of 12 pounds? 11 is the number which expresses the part. To put this question in the other form, viz. What is the ratio, &c., let that number which expresses the part, be the number last named; thus, What is the ratio of 12 pounds to 11 pounds? Ans. $\frac{1}{14}$.

6. What part of $\pounds 1$ is 2s. 6d.? or, What is the ratio of $\pounds 1$ to 2s. 6d.?

 $\pounds 1 = 240$ pence, and 2s. 6d. = 30 pence; hence, $\frac{10}{240} = \frac{1}{6}$, is the answer.

7. What part of 13s. 6d. is \pounds 1 10s.? or, What is the ratio of 13s. 6d. to \pounds 1 10s.? Ans. $\frac{29}{29}$.

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8. What is the ratio of 3 to 5? — of 5 to 3? — of 7 to 19? — of 19 to 7? — of 15 to 90? — of 90 to 15? — of 84 to 160? — of 160 to 84? — of 615 to 1107? — of 1107 to 615? Ans. to the last $\frac{2}{3}$.

PROPORTION:

OR

THE SINGLE RULE OF THREE.

¶ SS. 1. If a piece of cloth 4 yards long, cost \pounds 12, what will be the cost of apiece of the same cloth seven yds. long ?

Had this piece contained twice the number of yards of the first piece, it is evident the price would have been twice as much; had it contained three times the number of yards, the price would have been three times as much; or had it contained only half the number of yards, the price would have been only half as much; that is, the cost of seven yds. will be such part of £12 as seven yards is part of four yards. Seven yards is $\frac{7}{4}$ of 4 yards; consequently, the price of 7 yards must be $\frac{7}{4}$ of the price of 4 yards, or $\frac{7}{4}$ of £12; $\frac{7}{4}$ of £12, that is, $12 \times \frac{7}{4} = \frac{64}{2} = £21$, answer.

2. If a horse travel 30 miles in 6 hours, how many miles will he travel in 11 hours at that rate?

11 hours is $\frac{1}{2}$ of 6 hours, that is, 11 hours is one time 6 hours, and $\frac{5}{2}$ of another time; consequently, he will travel, in 11 hours, L-time 30 miles, and $\frac{5}{2}$ of another time; that is, the ratio between the distances will be equal to the ratio between the times.

 $\frac{1}{6}$ of 30 miles, that is, $30 \times \frac{1}{6} = \frac{3}{6} = 55$ miles. If, then, no error has been committed, 55 miles must be $\frac{1}{6}$ of 30 miles. This is actually the case; for $\frac{5}{5} = \frac{1}{6}$.

Ans. 55 miles.

Quantities which have the same ratio between them are said to be *proportional*. Thus, these four quantities—

HOURS HOURS. MILES. MILES. 6, 11, 30, 55, written in this order, being such, that the second contains the first a is, the raratio betw proportio bination numbers To den bers 6, 11

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RULE OF THREE.

the first as many times as the fourth contains the third; that is, the ratio between the third and fourth being equal to the ratio between the first and second, form what is called a proportion. It follows, therefore, that proportion is a combination of two equal ratios. *Ratio* exists between *two* numbers; but proportion requires at least *three*.

To denote that there is a proportion between the numbers 6, 11, 30, 55, they are written thus—

6: 11:: 30: 35 which is read, 6 is to 11 as 30 is to 55; that is, 6 is the same part of 11 that 30 is of 55; or, 6 is contained in 11 as many times as 30 is contained in 55; or, lastly, the ratio or relation of 11 to 6 is the same as that of 55 to 30.

¶ **S9.** The first term of a ratio, or relation, is called the antecedent, and the second the consequent. In a proportion there are two antecedents, and two consequents, viz. the antecedent of the first ratio, and that of the second; the consequent of the first ratio and that of the second. In the proportion 6:11::30:55, the antecedents are 6,30; the consequents 11, 55.

The consequent, as we have already seen, is taken for the numerator, and the antecedent for the denominator of the fraction, which expresses the ratio or relation. Thus, the first ratio is $\frac{1}{6}$, the second $\frac{5}{3}\frac{5}{6}=\frac{1}{6}$; and that these two ratios are equal, we know, because the fractions are equal.

The two fractions ${}_{61}^{1}$ and ${}_{55}^{18}$ being equal, it follows that by reducing them to a common denominator; the numerator of the one will become equal to the numerator of the other, and, consequently, that 11 multiplied by 30 will give the same product as 55 multiplied by 6. This is actually the case, for $11 \times 30 = 330$, and $55 \times 6 = 330$. Hence it follows if four numbers be in proportion, the product of the first and last, or of the two extremes, is equal to the product of the second and third, or of the two means.

Hence it will be easy, having three terms in a proportion given, to find the fourth. Take the last example. Knowing that the distances travelled are in proportion to the times or hours occupied in travelling, we write the proportion thus—

HOURS.		HOURS,		MILES.		MILES.
6	:	11	::	30	:	

Now, since the product of the extremes is equal to the product of the means, we multiply together the two means, 11 and 30, which makes .330, and, dividing this product by the known extreme, 6, we obtain for the result 55, that is, 55 miles, which is the other extreme or term sought.

3. At \pounds 54 for 36 barrels of flour, how many barrels may be purchased for \pounds 186?

In this question, the unknown quantity is the number of barrels bought for £186, which ought to contain the 36 barrels as many times as £186 contains £54; we thus get the following proportion:

Pounds.		Pounds.			Barrels	·.	Barrels.
54	:	186	•	•	36	•	

: 186 :: 36 : .. 36

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54)6696(124 barrels, answer. 54

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The product 6696 of the two means, divided by 54, the known extreme, gives 124 barrels for the other extreme, which is the term sought, or answer.

Any three terms of a proportion being given, the operation by which we find the fourth, is called the *Rule of Three.* A just solution of the question will some times require that the order of the terms of proportion be changed. This may be done, provided the terms be so placed, that the product of the extremes shall be equal to that of the means.

4. If 3 men perform a certain piece of work in ten days, how long will it take 6 men to do the same?

The number of days in which six men will do the work, being the term sought, the known term of the same kind, viz. ten days, is made the third term. The two remaining terms are 3 men and 6 men, the ratio of which is §. But the more* men there are employed in the work, the less time will

• The rule of three has sometimes been divided into direct and innerse, a distinction which is totally useless. It may not however be sums to explain, in this place, in what this distinction consists.

The Rule of Three Direct is when more requires more, or less re-

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more, as in 14 he quantity 6, will re seven da Here les more tim be required to do it; consequently the days will be less in proportion as the number of men is greater. There is still a proportion in this case, but the order of the terms is inverted; for the number of men in the second set being two times that in the first, will require only one half the time. The first number of days, therefore, ought to contain the second as many times as the second number of men contains the first. This order of the terms being the reverse of that assigned to them in announcing the question, we say that the number of men is in the inverse ratio of the number of days. With a view, therefore, to a just solution of the question, we reverse the order of the two first terms, (in doing which, we invert the ratio,) and instead of writing the proportion 3 men : 6 men $(\frac{6}{3})$ we write it 6 men : 3 men, $(\frac{3}{3})$ that is, men. men. days. days. : : 3 10 ::

Note. We invert the ratio when we reverse the order of the terms in the proportion, because then the antecedent takes the place of the consequent, and the consequent that of the antecedent; consequently, the terms of the fraction which express the ratio are inverted; hence the ratio is inverted. Thus, the ratio expressed by $\frac{6}{3}$ =2, being inverted, is $\frac{3}{6}$ = $\frac{1}{2}$.

Having stated the proportion as above, we divide the product of the means, $(10 \times 3 = 30)$, by the known extreme 6, which gives 5, that is, 5 days, for the other extreme or term sought. Ans. 5 days.

From the examples and illustrations now given, we deduce the following general

The Rule of Three Inverse is when more requires less, or less requires more, as in this example: —If 6 men dig a certain quantity of trench in 14 hours, how many hours will it require 12 men to dig the same quantity? Here more requires less; that is, 12 men being more than 6, will require less time. Again—if 6 men perform a piece of work in seven days, how long will three men be in performing the same work? Here less requires more; for the number of men being less, will require more time.

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RULE.

Of the three given numbers, make that the third term which is of the same kind with the answer sought. Then consider, from the nature of the question, whether the answer will be greater or less than this term. If the answer is to be greater, place the greater of the two remaining numbers for the second term, and the less number for the first term; but if it is to be less, place the less of the two remaining numbers for the second term, and the greater for the first; and, in either case, multiply the second and third terms together, and divide the product by the first for the answer, which will always be of the same denomination as the third term.

Note 1. If the first and second terms contain different denominations, they must both be reduced to the same denomination.

If 8 yards of cloth cost £1 4s. what will 364 qrs. cost?

Reduce 8 yards and 364 quarters to the same denomination, by dividing the 364 quarters by 4, which will bring it into yards. $3\frac{6}{2}^4 = 91$.

> yds. yds. 8 : 91 :: £14s.

Note 2. If the third term be a compound number, it must either be reduced to integers of the lowest denomination, or the low denominations must be reduced to a fraction of the highest denomination contained in it.



Now multiply the 24s. by 91, and divide the product by 8; the answer will be shillings, which can be reduced to pounds; or, the 4s. can be reduced to the fraction of a pound, $4s. \div 20$, that is, $\frac{4}{20} = \frac{1}{5}$ of a pound; so $\pounds 1 4s. = \pounds 1\frac{1}{5}$. Or, we can reduce the 4s. to the decimal of a pound; 20)40 which, annexed to the $\pounds 1$, is equal to $\pounds 1^{\circ}2$.

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The first method is most usually practised.

Note 3, The same rule is applicable, whether the given quantities be integral, fractional, or decimal,

EXAMPLES FOR PRACTICE,

5. If 6 horses consume 21 bushels of oats in three weeks, how many bushels will serve 20 horses the same time?

Ans, 70 bushels.

6. The above question reversed. If 20 horses consume 70 bushels of oats in 3 weeks, how many bushels will serve 6 horses the same time? Ans. 21 bushels,

7. If 365 men consume 75 barrels of provisions in nine months, how much will 500 men consume in the same time? Ans, 10254 barrels,

8. If 500 men consume 10244 barrels of provisions in 9 months, how much will 365 men consume in the same time? Ans. 75 barrels,

9. A goldsmith sold a tankard for $\pounds 10$ 12s. at the rate of 5s, 4d, per ounce; I demand the weight of it.

Ans. 39 oz. 15 pwt, 10. If the moon move $13 \circ 10'$ 35'' in a day, in what time does it perform one revolution? Ans. 27d, 7h. 43m,

11. If a person whose rent is £33, pay £8 2s. parish taxes, how much should a person pay whose rent is £97?

Ans. ±9 2s. 214d, 12. If I buy 7 lbs, of sugar for 3s, 9d, how many pounds can I buy for £1 10s. ?

13. If 2 lbs. of sugar cost 1s, 3d., what will 100 lbs, of coffee cost, if 8 lbs of sugar are worth 5 lbs. of coffee ?

Ans, £5,

14. If I give $\pounds 6$ for the use of $\pounds 100$ for 12 months, what must I give for the use of $\pounds 983$ the same time?

Ans. £58,88

15. There is a cistern which has 4 pipes; the first will fill it in ten minutes, the second in twenty minutes, the 3d in forty minutes, the fourth in eighty minutes; in what time will all four, running together, fill it?

 $\frac{1}{10} + \frac{1}{20} + \frac{1}{40} + \frac{1}{80} = \frac{1}{80}$ cistern in 1 minute,

Ans, 53 minutes,

16. If a family of 10 persons spend 3 bushels of malt in a month, how many bushels will serve them when there are 30 in the family? Ans. 9 bushels, 182

Note. The rule of Proportion, although of frequent use, is not of indispensable necessity; for all questions under it may be solved on general principles, without the formality of a proportion; that is, by *analysis*, as already shown, ¶ 62 ex. 1. Thus, in the above example,—If 10 persons spend 3 bushels, 1 person, in the same time, would spend $\frac{1}{10}$ of 3 bushels, that is, $\frac{1}{10}$ of a bushel; and 30 persons would spend 30 times as much, that is $\frac{9}{10}$ —9 bushels, as before.

17. If a staff 5 feet 8 inches in length, cast a shadow of 6 feet, how high is that steeple whose shadow measures 153 feet?

18. The same by analysis. If 6 feet shadow require a staff of 5 feet 8 inches=68 inches, one foot shadow will require a staff of $\frac{1}{6}$ of 68 inches, or $\frac{68}{6}$ inch; then 153 feet shadow will require 153 times as much; that is, $\frac{68}{6} \times 153 = 10^{4}0^{4} = 1734$ inches=1441 feet as before.

19. If £3 sterling be equal to £ $3\frac{1}{3}$ Halifax, how much Halifax is equal to £1000 sterling? Ans. £1111 2s. $2\frac{2}{3}$ d.

20. If \pounds 1111 2s. $2\frac{2}{3}d$. Halifax be equal to \pounds 1000 sterling, how much sterling is equal to \pounds 3 $\frac{1}{3}$ Halifax? Ans. \pounds 3.

21. If £1000 sterling be equal to £1111 2s. $2\frac{2}{3}d$. Halifax, how much Halifax is equal to £3 sterling ? Ans. £ $3\frac{1}{3}$.

22. If £3 sterling be equal to £3¹/₃ Halifax, how much sterling is equal to £1111 2s. $2\frac{2}{3}$ d. Halifax? Ans. £1000.

23. Suppose 2000 soldiers had been supplied with bread sufficient to last them 12 weeks, allowing each man 14 oz. a day; but, on examination, they find 105 barrels, containing 200 lbs. each, wholly spoiled; what must the allowance be to each man, that the remainder may last them the same time? Ans. 12 ounces a day.

24. Suppose 2000 soldiers were put to an allowance of 12 oz. of bread per day for 12 weeks, having a seventh part of their bread spoiled, what was the whole weight of their bread, good and bad, and how much was spoiled?

Ans. { The whole weight, 147000 lbs. Spoiled, 21000 "

25. — 2000 soldiers, having lost 105 barrels of bread, weighing 200 lbs. each, were obliged to subsist on 12 oz. a day for 12 weeks; had none been lost, they might have had 26. their b

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14 oz. a day; what was the whole weight, including what was lost, and how much had they to subsist on ?

Ans. { Whole weight, 147000 lbs. Left to subsist on, 126000 "

26. — 2000 soldiers, after losing one seventh part of their bread, had each 12 oz. a day for 12 weeks; what was the whole weight of their bread, including that lost, and how much might they have had per day, each man, if none had been lost? Whole weight, 147000 lbs.

Ans. Loss, 21000 "

9 14 oz, per day, had none been lost. 27. There was a certain building raised in 8 months by 120 workmen; but, the same being demolished, it is required to be built in 2 months; I demand how many men must be employed about it. Ans. 480 men.

28. There is a cistern having a pipe which will empty it in ten hours; how many pipes of the same capacity will empty it in 24 minutes? Ans. 25 pipes.

29. A garrison of 1200 men has provisions for 9 months, at the rate of 14 oz. per day; how long will the provisions last, at the same allowance, if the garrison be reinforced by four hundred men ? Ans. $6\frac{3}{4}$ months.

30. If a piece of land, 40 rods in length and 4 in breadth, make an acre, how wide must it be when it is but 25 rods long? Ans. 67 rods.

31. If a man perform a journey in 15 days when the days are 12 hours long, in how many will he do it when the days are but 10 hours long? Ans. 18 days.

32. If a field will feed 6 cows 91 days, how long will it feed 21 cows? Ans. 26 days.

33. Lent a friend $\pounds 292$ for 6 months; some time after, he lent me $\pounds 806$; how long may I keep it to balance the favor? Ans. 2 months 5+days.

34. If 30 men can perform a piece of work in 11 days, how many men will accomplish another piece of work, four times as big, in a fifth part of the time? Ans. 600 men.

35. If $\frac{1}{13}$ lb. of sugar cost $\frac{7}{15}$ of a shilling, what will $\frac{32}{43}$ of a pound cost ?, Ans. 4d. $3\frac{3}{13}\frac{3}{15}\frac{1}{15}$ q.

Note. See ¶ 62, ex. 1, where the above question is solved by analysis. The eleven following are the next succeeding examples in the same paragraph.

RULE OF THREE,

36. If 7 lbs. of sugar cost 2 of 5s. what cost 12 lbs. Ans. 63s.

37. If 61 yards of cloth cost £3, what cost 91 yards? Ans. £4 5s. 41d.

38. If 2 oz. of silver cost 11s 2²/₅d, what cost ²/₂ oz.? Ans. 4s. 2²/₅d,

39. If $\frac{1}{7}$ oz. cost $4\frac{1}{72}$ s., what costs 1 oz. ? Ans. Gs. 5d. 40. If $\frac{1}{3}$ ib. less by $\frac{1}{6}$ ib cost 13 d., what cost 14 lbs. less by $\frac{1}{5}$ of 2 lbs. Ans. £4 9s. $9\frac{1}{2^{5}}$ d.

41. If $\frac{2}{5}$ of a yard cost \pounds , what will 40½ yards cost? Ans. £59 1s. 2²₄d.

42. If $\frac{1}{16}$ of a ship cost £251, what is $\frac{3}{32}$ of her worth? Ans. £53 15s. 84d.

43. At £35 per cwt., what will 93 lbs, cost?

Ans. 6s. 3_{56}^{56} d. 44. A merchant owning $\frac{4}{5}$ of a vessel, sold $\frac{2}{5}$ of his share for £957; what was the vessel worth ? Ans. £1794, 7s. 6d.

45. If $\frac{3}{2}$ of a yard cost $\mathcal{L}_{\frac{3}{2}}^{\frac{9}{2}}$, what will $\frac{9}{2}$ of an ell English cost? Ans. 17s. 1d. $2\frac{5}{2}q$.

46. A merchant bought a number of bales of velvet, each containing 129 $\frac{1}{2}$ yards, at the rate of $\pounds 7$ for 5 yards, and sold them out at the rate of $\pounds 11$ for 7 yards, and gained $\pounds 200$ by the bargain; how many bales were there?

Ans. 9 bales:

47. At \pounds 9 for 6 barrels of flour, what must be paid for 178 barrels ? Ans. \pounds 267.

48. At 9s. 6d. for 3 cwt. of hay, how much is that per ton? Ans. £3 3s. 4d.

49. If 2'5 lbs. of tobacco cost 75 cents, how much will 185 lbs. cost ? Ans. \$5'55.

50. What is the value of '15 of a hogshead of lime, at 11s. 111d. per hhd.? Ans. 1s. 91d.

51. If '15 of a hhd. of lime cost 1s. 9¹/₂d., what is it per hhd. ? Ans. 11s. 11¹/₄d.

COMPOUND PROPORTION.

(**90.** It frequently happens that the relation of the quantity required, to the given quantity of the same kind, depends upon several circumstances combined together; it is then called *Compound Proportion*, or *Double Rule of Three*.

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Ans. 6s. 35d. § of his share £1794 7s. 6d. an ell English , 17s. 1d. 2fq. of velvet, each r 5 yards, and ds, and gained there ?

Ans. 9 bales: st be paid for Ans. £267. ch is that per ns. £3 3s. 4d. w much will Ans. \$5'55. ad of lime, at Ans. 1s. 9½d. what is it per ns. 11s. 11¼d.

elation of the he same kind, d together; it ouble Rule of 1. If a man travel 273 miles in 13 days, travelling only seven hours in a day, how many miles will he travel in 12 days, if he travel 10 hours in a day?

This question may be solved several ways. First, by analysis—

If we knew how many miles the man travelled in one hour, it is plain we might take this number 10 times, which would be the number of miles he would travel in ten hours or in one of these long days; and this again taken 12 times, would be the number of miles he would travel in 12 days, travelling 10 hours each day.

If he travel 273 miles in 13 days, he will travel $\frac{1}{13}$ of 273 miles; that is, $\frac{27.3}{13}$ miles, in 1 day of 7 hours; and $\frac{1}{4}$ of $\frac{27.3}{13}$ miles is $\frac{27.3}{51}$ miles, the distance he travels in 1 hour; then, 10 times $\frac{27.3}{51} = \frac{27.3}{51}$ miles, the distance he travels in ten hours; and 12 times $\frac{27.3}{51} = \frac{32.75}{51} = 32.750 = 360$ miles, the distance he travels in 12 days, travelling ten hours each day.

Ans. 360 miles.

But the object is to show how the question may be solved by *proportion*—

First, it is to be regarded that the number of miles travelled over depends upon two circumstances, viz. the number of *days* the man travels, and the number of hours he travels each day.

We will not at first consider this latter circumstance, but suppose the number of hours to be the same in each case; the question then will be—If a man travel 273 miles in 13 days, how many miles will he travel in 12 days? This will furnish the following proportion :—

13 days : 12 days : : 273 miles : ---- miles, which gives for the fourth term or answer, 252 miles.

Now, taking into consideration the other circumstance, or that of the hours, we must say—If a man travelling seven hours a day for a certain number of days, travels 252 miles, how far will he travel in the same time, if he travel ten hours in a day? This will lead to the following proportion:

7 hours : 10 hours : : 252 miles : — miles. This gives for the fourth term or answer, 360 miles.

We see, then, that 273 miles has to the fourth term, or answer, the same proportion that 13 days has to 12 days,

 $\mathbf{Q2}$









and that seven hours has to ten hours. Stating this in the form of a proportion, we have

13 days : .12 days } :: 273 miles : ____ miles

by which it appears that 273 is to be multiplied by both 12 and 10; that is, 273 is to be multiplied by the product of 12×10 , and divided by the product of 13×7 , which, being done, gives 360 miles for the fourth term, or answer, as before.

In the same manner, any question relating to compound proportion, however complicated, may be stated and solved.

2. If 248 men, in 5 days of 11 hours each, can dig a trench 230 yards long, 3 wide, and 2 deep, in how many days of 9 hours each, will 24 men dig a trench 420 yards long, 5 wide and 3 deep?

Here the number of days, in which the proposed work can be done, depends on five circumstances, viz. the number of men employed, the number of hours they work each day, the length, breadth and depth of the trench. We will consider the question in relation to each of these circumstances, in the order in which they have been named—

1st. The number of men employed. Were all the circumstances in the two cases alike, except the number of men and the number of days, the question would consist only in finding in how many days 24 men would perform the work which 248 men had done in 5 days; we should then have

24 men : 248 men :: 5 days : ---- days.

2d. Hours in a day. But the first laborers worked 11 hours in a day, whereas the others worked only 9; less hours will require more days, which will give

9 hours : 11 hours : : 5 days : — days. 3d. Length of the ditches. The ditches being of unequal

length, as many more days will be necessary as the second is longer than the first; hence we shall have

230 length : 420 length : : 5 days : ---- days.

4th. Widths. Taking into consideration the widths, which are different, we have

3 wide : 5 wide : : 5 days — days.

5th. Depths. Lastly, the depths being different, we have 2 deep : 3 deep :: 5 days : ----- days. It we term, o that 2

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¶ 91. The continued product of all the second terms $248 \times 11 \times 420 \times 5 \times 3$, multiplied by the third term, 5 days, and this product divided by the continued product of the first terms, $24 \times 9 \times 230 \times 3 \times 2$, gives 288_{298080}^{84960} days for the fourth term, or answer. $288_{\pm 0.7}^{\pm 9}$.

But the first and second terms are the fractions $\frac{248}{74}$, $\frac{11}{9}$, $\frac{429}{5}$, $\frac{5}{5}$ and $\frac{3}{5}$, which express the ratios of the men and of the hours, of the lengths, widths and depths of the two Hence it follows, that the ratio of the number of ditches. days given to the number of days sought, is equal to the product of all the ratios, which result from a comparison of the terms relating to each circumstance of the question.

The product of all the ratios is found by multiplying together the fractions which express them, thus-

 $248 \times 11 \times 420 \times 5 \times 3$ 17186400 17186400

and this frac.

298080 .298080 $24 \times 9 \times 230 \times 3 \times 2$ represents the ratio of the quantity required to the given quantity of the same kind. A ratio resulting in this manner from the multiplication of several ratios, is called a compound ratio.

From the examples and illustrations now given, we deduce the following general

RULE

for solving questions in compound proportion, or Double Rule of Three, viz.—Make that number which is of the same kind with the required answer, the third term; and of the remaining numbers, take away two that are of the same kind, and arrange them according to the directions given in simple proportion: then any other two of the same kind, and so on till all are used.

Lastly, multiply the third term by the continued product of the second terms, and divide the result by the continued product of the first terms, and the quotient will be the 4th term, or answer required.

EXAMPLES FOR PRACTICE.

1. If 6 men build a wall 20 feet long, 6 feet high, and 4 feet thick in 16 days, in what time will 24 men build one 200 feet long, 8 feet high and 6 feet thick? Ans. 80 days.

2. If the freight of 9 hhds. of sugar, each weighing 12 cwt. 20 leagues, cost \pounds 16, what must be paid for the freight of 50 tierces, each weighing $2\frac{1}{2}$ cwt 100 leagues?

Ans. £92 11s. 102d.

3. If 56 lbs. of bread be sufficient for 7 men 14 days, how much bread will serve 21 men 3 days? Ans. 36 lbs.

The same by analysis. If 7 men consume 56 lbs. of bread, 1 man, in the same time, would consume $\frac{1}{7}$ of 56 lbs.= $\frac{5}{7}$ lbs.; and if he consume $\frac{5}{7}$ lbs. in 14 days, he would consume $\frac{1}{14}$ of $\frac{5}{7} = \frac{5}{9}$ lbs. in one day. 21 men would consume 21 times so much as 1 man; that is, 21 times $\frac{5}{9} = \frac{1}{9} \frac{1}{7} = \frac{1}{9}$ lbs. in 1 day, and in 3 days they would consume 3 times as much; that is, $\frac{3}{5} = \frac{3}{9} = 36$ lbs. as before.

Ans. 36 lbs.

Notc. Having wrought the following examples by the rule of proportion, let the pupil be required to do the same by *analysis*.

4. If 4 reapers receive $\pounds 2$ 15s. $2\frac{1}{2}d$. for 3 days' work, how many men may be hired 16 days for $\pounds 25$ 15s. $2\frac{1}{2}d$.? Ans. 7 men.

5. If 7 oz. 5 pwt. of bread be bought for $4\frac{3}{4}d$, when corn is 4s. 2d. per bushel, what weight of it may be bought for 1s. 2d. when the price per bushel is 5s. 6d.?

Ans. I lb. 4 oz. $3\frac{479}{27}$ pwts. 6. If £100 gain £6 in 1 year, what will £400 gain in 9 months?

Note. This and the three following examples reciprocally prove each other.

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¶91. SUPPLEMENT TO SINGLE RULE OF THREE. 189

7. If £100 gain £0 in 1 year, in what time will £400 gain £18?

8. If £400 gain £18 in 9 months, what is the rate per sent per annum?

9. What principal, at 6 per cent per annum will gain £18 in 9 months?

10. A usurer put out \$75 at interest, and at the end of 8 months, received, for principal and interest, \$79; I demand at what fate per cent he received interest.

Ans. 8 per cent.

11. If 3 men receive $\pounds 8_{10}^9$ for $19\frac{1}{2}$ days' work, how much must 20 men receive for $100\frac{1}{2}$ days?

Ans. £305 0s. 8d.

Supplement to Single Rule of Three.

QUESTIONS.

1. What is proportion? 2. How many numbers are required to form a ratio? 3. How many to form a proportion? 4. What is the first term of a ratio called? 3. — the second term? 6. Which is taken for the numerator, and which for the denominator of the fraction expressing the ratio? 7. How may it be known when 4 numbers are in proportion? 8. Having three terms in the proportion given, how may the fourth term be found? 9. What is the operation, by which the fourth term is found? 10. How does a ratio become interted? 11. What is the rule in proportion? 12. In what denomination will the 4th term or answer be found? 13. If the first and second terms contails different denominations, what is to be done? 14. What is compound proportion; or double rule of three? 15. Rate?

EXERCISES.

If I buy 76 yards of cloth for £25 5s. 10d: 50 (rs. what does it cost per ell English ? Ans. 9s. 31d.
Bought 4 pieces of Holland, each containing 24 ells

English for $\pounds 24$; how much was that per yard? Ans. 4s.

2. A garrison had provisions for 8 months, at the rate of 15 ounces to each person per day; how much must be allowed per day in order that the provisions may last $9\frac{1}{2}$ months? Ans. $12\frac{12}{12}$ oz.

4. How much land at 12s. 6d. per acre, must be given in exchange for 360 acres, at 18s. 9d. per acre?

Ans. 540 acres.

TELLOWSHIP.

¶ 91.92

5. Borrowed 185 quarters of corn when the price was 19s.; how much must I pay when the price is 17s. 4d.? Ans. 20243

6. A person owning $\frac{3}{2}$ of a coal mine, sells $\frac{3}{2}$ of his share for $\pounds 171$; what is the whole mine worth? Ans. $\pounds 380$.

7. If § of a gallon cost § of a pound, what cost § of a tun? Ans. £140.

8. At $\pounds l_2^1$ per cwt. what cost $3\frac{1}{3}$ lbs.? Ans. 10⁵d.

9. If $4\frac{1}{2}$ cwt. can be carried 36 miles for 35 shillings, how many pounds can be carried 20 miles for the same money? Ans. 907 $\frac{1}{2}$ lbs.

10. If the sun appears to move from east to west 360 degrees in 24 hours, how much is that in each hour ? — in each minute ? — in each second ?

Ans. to the last, 15'' of a deg.

11. If a family of 9 persons spend £112 10s. in 5 months, how much would be sufficient to maintain them 8 months if 5 persons more were added to the family? Ans. £280.

Note. Exercises 14th, 15th, 16th, 17th, 18th, 19th and 20th, "Supplement to Fractions," afford additional examples in single and double proportion, should more examples be thought necessary.

FELLOWSHIP.

¶ 92. 1. Two men own a farm; the first owns $\frac{1}{4}$, and the second owns $\frac{3}{4}$ of it; the farm is sold for £40; what is each man's share of the money?

2. Two men purchase a horse for 20 pounds, of which one pays 5 pounds, and the other 15 pounds; the horse is sold for 40 pounds; what is each man's share of the money?

3. A. and B. bought a quantity of cotton; A. paid 100 pounds, and B. 200 pounds; they sold it so as to gain 30 pounds; what were their respective shares of the gain?

The process of ascertaining the respective gains or losses of individuals engaged in joint trade, is called the rule of *Fellowship*.

The money, or value of the articles employed in trade, is called the *capital* or *stock*; the gain or 'loss to be shared is called the *dividend*.'

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It is plain that each man's gain or loss ought to have the same relation to the whole gain or loss, as his share of the stock does to the whole stock.

FELLOWSHIP.

Hence we have this RULE :-- As the whole stock : to each man's share of the stock : : the whole gain or loss : his share of the gain or loss.

4. Two persons have a joint stock in trade; A. put in £250, and B. £350; they gain £400; what is each man's share of the profit?

UPERATION.

A.'s stock, B.'s " $\begin{array}{c} \pounds 250\\ \hline 350\\ \hline \end{array}$ Then, $600:250:400:\pounds 166$ 13s. 4d. A.'s

Whole stock, £600 J 600: 350 :: 400 : 233 6s. 7d. B.'s The pupil will perceive that the process may be contracted by cutting off an equal number of ciphers from the first and second, or first and third terms; thus, 6 : 250 :: 4 : £166 13s. 4d. &c.

It is obvious, the correctness of the work may be ascertained by finding whether the sums of the shares of the gains are equal to the whole gain; thus, $\pounds 166\ 13s.\ 4d.+$ $\pounds 233\ 6s.\ 7d.=\pounds 400$, the whole gain.

5. A. B. and C. trade in company; A.'s capital was £175, B.'s £200, and C.'s £500; by misfortune they lose £250; what loss must each sustain? Ans. $\begin{cases} \pounds 50 & A.'s loss.\\ 57 2s. 10\frac{1}{4}d. & B.'s \\ 142 17s. 1\frac{1}{4}d. & C.'s \end{cases}$

6. Divide \$600 among 3 men, so that their shares may be to each other as 1, 2, 3, respectively.

Ans. \$100, \$200 and \$300.

7. Two merchants, A. and B. loaded a ship with 500 hhds. of rum; A. loaded 350 hhds. and B. the rest; in a storm, the seamen were obliged to throw overboard 100 hhds.; how much must each sustain of the loss?

Ans. A. 70, and B. 30 hhds. 8. A. and B. companied; A. put in \pounds 45, and took out $\frac{3}{2}$ of the gain; how much did B. put in? Ans. \pounds 30.

Note. They took out in the same proportion as they put in; if $\frac{3}{5}$ of the stock is £45, how much is $\frac{2}{5}$ of it?

9. A. and B. companied, and trade with a joint capital of

FELLOWSHIP.

1 92, 93,

£400; A, receives for his share of the gain, 1 as much as B; what was the stock of each?

£133 6s. 7d. A's stock, Ans.

£266. 13s. 4d. B's stock.

10. A bankrupt is indebted to B \$780, to C \$460, and to .D \$760; his estate is worth only \$600; how must it be divided?

The question evidently involves the principles of Note. fellowship, and may be wrought by it,

Ans. B \$234, C \$138, and D \$228, 11. B and C venture equal stocks in trade, and clear £164; by agreement, B was to have 5 per cent of the profits, because he managed the concerns; C was to have but 2 per cent, what was each one's gain? and how much did B receive for his trouble?

Ans. B.'s gain was £117 2s, 101d. and C.'s £46 17s, 11d, and B. received £70 5s. 81d, for his trouble,

12. A cotton factory, valued at £12000, is divided into 100 shares; if the profits amount to 15 per cent yearly, what will be the profit accruing to 1 share ?----- to 2 shares? Ans, to the last £450,

13. In the above-mentioned factory, repairs are to be made which will cost $\pounds 340$; what will be the tax on each share, necessary to raise the sum ?---- on 2 shares ?---on 3 shares? — on 10 shares? Ans, to the last, £34,

14. If a town raise a tax of £1850, and the whole town be valued at £37000, what will that be on £1? What will be the tax of a man whose property is valued at $\pounds 1780$?

Ans, 1s. on a pound, and $\pounds 89$ on $\pounds 1780$,

¶ 93. In assessing taxes, it is necessary to have an inventory of the property, both real and personal, of the whole town, and also of the whole number of the polls; and as the polls are rated at so much each, we must first take out from the whole tax what the polls amount to, and the remainder is to be assessed on the property, We may then find the tax upon one pound, and make a table containing the taxes on one, two, three, &c, to ten pounds , then on twenty, thirty, &c, to a hundred; then on 100, 200, &c, to 1000 pounds. Then knowing the inventory of any individual, it is easy to find the tax upon his property,

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FELLOWSHIP.

15. A certain town, valued at £64530, raises a tax of £2259 18s.; there are 540 polls, which are taxed 3s. each; what is the tax on a pound, and what will be B.'s tax, whose real estate is valued at £1340, his personal property at £874, and who pays for two polls.

It will be better in questions relating to the assessment of taxes to use decimals, as we have done in interest. The process will be shorter, and the result will be obtained with exactness. The shillings, therefore, in the given values, will be reduced to the decimal of a pound, and the table will be made out decimally, and the decimal parts in the final answer can be reduced to shillings and pence,

 $540 \times 60^{\circ}(3s.) = £324$, amount of the poll taxes, and 2259'90 (£2259 18s.) - £324 = 1935'90, to be assessed on property. £64530 : 1935'90 ;; £1'03; or $\frac{1825190}{64530} = 03$ tax on one pound, T A B L E.

	£	£	£	£		£	£
lax.on	1 is	· '03	Tax on 10 is	'30	Tax on	100 is	3.
	2	'06	20	'60		200	6 ⁴
	3	'09	30	'90		300	9
	4	'12	40	1/20	i .	400	12
	5	'15	50	1'50	ĺ	500	15
	6	'18	50	1'80	· ·	600	18
	7	'21	. 70	2'10		700	214
	8	'24	80	2'40	i	800	24'
	9	27	90	2'70		900	270
						1000	30

Now, to find B.'s tax, his real estate being $\pounds 1340$, I find by the table that

The tax on	_	-	£ 100) () i	z .		£ 30'	٠
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PELLOWSHIP.

16. What will C.'s tax amount to whose inventory is 874 dollars real, and 210 dollars personal property, and who pays for three polls? Ans. \$34'32.

17. What will be the tax of a man paying for one poll. whose property is valued at \$34'82? ---- at \$768 ? ---at \$940 ? ----- at \$4657 ? Ans. to last, \$140'31.

18. Two men paid \$10 for the use of a pasture 1 month; A. kept in 24 cows, and B. 16 cows; how much should each pay?

19. Two men hired a pasture for \$10; A. put in 8 cows 3 months, and B. put in 4 cows 4 months; how much should each pay?

¶94. The pasturage of 8 cows for 3 months is the same as 24 cows for 1 month; and the pasturage of 4 cows for 4 months is the same as of 16 cows for one month. The shares of A. and B. therefore, are 24 to 16, as in the former question. Hence, when time is regarded in fellowship,-Multiply each one's stock by the time he continues it in trade, and use the product for his share. This is called Double Fellowship. Ans. A. \$16, and B. \$4.

20. A. and B. enter into partnership; A. puts in £100 six months, and then puts in £50 more; B. puts in £200 four months, and then takes out £80; at the close of the year, they find that they have gained £95; what is the profit of Ans. { £43 14s. 21d. A.'s share. 51 5s. 9d. B.'s " each ?

21. A. with a capital of \$500, began trade Jan. 1, 1826, and meeting with success, took in B. as a partner, with a capital of \$600, on the 1st March following; four months after, they admit C. as a partner, who brought \$800 stock; at the close of the year, they find the gain to be \$700; how must it be divided among the partners?

> * \$250 A.'s share, Ans. 250 B.'s 200 C.'s ** "

QUESTIONS.

1. What is fellowship? 2. What is the rule for operating? 3. When time is regarded in fellowship, what is it called? 4. What is the method of operating in double fellowship? 5. How are taxes assessed? 6. How is fellowship proved?

¶ 94:

1 95, 90

simples, be of a n When to find th the proce 1. A f pence pe bushel, a what is a

It is p ber of bu 4 bush 3 66

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2. A lbs. wort mixture

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entory is 874 rty, and who Aws. \$34'32, for one poll, \$768 ? t, \$140'31. cure 1 month:

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nonths is the age of 4 cows e month. The in the former fellowship,ontinues it in This is called and B. \$4. ts in £100 six in £200 four e of the year, the profit of d. A.'s share. " B.'s Jan. 1, 1826, artner, with a ; four months

\$800 stock; be \$700; how

50 A.'s share, 50 B.'s " 00 C.'s "

operating? 3. d? 4. What is How are taxes

ALLIGATION.

ALLIGATION.

¶ 95. Alligation is the method of mixing two or more simples, of different qualities, so that the composition may be of a mean or middle quality.

When the quantities and prices of the simples are given to find the mean price of the mixture compounded of them, the process is called *Alligation Medial*.

1. A farmer mixed together 4 bushels of wheat, worth 66 pence per bushel, 3 bushels of rye, worth 32 pence per bushel, and 2 bushels of corn, worth 28 pence per bushel; what is a bushel of the mixture worth?

It is plain that the cost of the whole, divided by the number of bushels, will give the price of one bushel.

4 bushels, at 66 pence, cost 264 pence.

_					
3		32	46	. 96	
2	"	28	"	56	
		·		-	
91	oushels c	ost		416	pence.

416=462 pence, Ans.

2. A grocer mixed 5 lbs. of sugar, worth 10d. per lb. 8 lbs. worth 12d. 20 lbs. worth 14d.; what is a pound of the mixture worth? Ans. 1219d.

3. A goldsmith melted together 3 ounces of gold 20 carats fine, and 5 ounces 22 carats fine; what is the fineness of the mixture?

4. A grocer puts 6 gallons of water into a cask containing 40 gallons of rum, worth 2s. 7d. per gallon; what is a gallon of the mixture worth? Ans. 2s. 244d.

5. On a certain day the mercury was observed to stand in the thermometer as follows:--5 hours of the day it stood at 64 degrees; 4 hours at 70 degrees; 2 hours at 75 degrees, and 3 hours at 73 degrees; what was the mean temperature for that day?

It is plain this question does not differ, in the mode of its operation from the former. Ans. 69_{TT}^{2} degrees.

96. When the mean price or rate, and the prices or rates of the several simples are given, to find the proportions or quantities of each simple, the process is called allisgation alternate; alligation alternate is; therefore, the reverse of alligation medial, and may be proved by it.

1. A man has corn worth 40d. per bushel, which he wishes to mix with rye worth 50d. per bushel, so that the mixture may be worth 42d. per bushel; what proportions or quantities of each must he take?

Had the price of the mixture required exceeded the price of the corn, by just as much as it fell short of the price of the rye, it is plain he must have taken equal quantities of corn and rye; had the price of the mixture exceeded the price of the corn by only half as much as it fell short of the price of the rye, the compound would have required twice as much corn as rye; and in all cases the less the difference between the price of the mixture and that of one of the simples, the greater must be the quantity of that simple, in proportion to the other; that is, the quantities of the simples must be inversely as the differences of their prices from the price of the mixture; therefore, if these differences be mutually exchanged, they will directly express the relative quantities of each simple necessary to form the compound required. In the above example, the price of the mixture is 42d. and the price of the corn is 40d.; consequently the difference of their prices is 2d.; the price of the rye is 50d. which differs from the price of the mixture by 8d. Therefore, by exchanging these differences, we have 8 bushels of corn to 2 bushels of rye for the proportion required.

Ans. 8 bushels of corn to 2 bushels of rye, or in that pro-

The correctness of this result may now be ascertained by the last rule; thus, the cost of 8 bushels of corn at 40 pence is 320 pence; and 2 bushels of rye at 50 pence is 100 pence; then, 320+100=420, and 420 divided by the number of bushels, (8+2)=10, gives 42 pence for the price of the mixture.

2: A merchant has several kinds of tea; some at 8s. some at 9s. some at 11s. and some at 12s. per lb.; what proportions of each must he mix, that he may sell the compound at 10s. pet lb.

Here we have 4 simples; but it is plain that what has just been proved of *two* will apply to any number of *pairs*, if in each pair the price of *one* simple is greater, and that of the other less, than the price of the mixture required. Hence we have this 10s. }

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ALLIGATION.

RULE.

The mean rate and the several prices being reduced to the same denomination,—connect with a continued line each price that is less than the mean rate with one or more that is greater, and each price greater than the mean rate with one or more that is less.

Write the difference between the mean rate, or price, and the price of each simple opposite the price with which it is connected; (thus the difference of the two prices in each pair will be mutually exchanged) then the sum of the differences, standing against any price, will express the *relative quantity* to be taken of that price.

By attentively considering the rule, the pupil will perceive that there may be as many different ways of mixing the simples, and consequently as many different answers, as there are different ways of linking the several prices.

We will now apply the rule to solve the last question :----

$\begin{array}{c} \text{OPERATIONS.} \\ lbs. & Or, \\ 10s. \begin{cases} 8s. - 2 \\ 9s. - 1 \\ 11s. - 2 \\ 12s. - 2 \end{cases} \\ Ans. \begin{cases} 8s. - 2 \\ 9s. - 1 \\ 11s. - 1 \\ 12s. - 2 \\ 12s. -$

Here we set down the prices of the simples, one directly under another, in order, from least to greatest, as this is most convenient, and write the mean rate (10s.) at the left hand. In the first way of linking, we find that we may take in the proportion of 2 pounds of the teas at 8 and 12s. to 1 pound at 9 and 11s. In the second way, we find for the answer 3 pounds at 8 and 11s. to 1 pound at 9 and 12s.

3. What proportion of sugar, at Sd. 10d. and 14d. per lb. will compose a mixture worth 12d. per lb.

Ans. In the proportion of 2 lbs. at 8 and 10 pence to six pounds at 14 pence.

Note. As these quantities only express the proportions of each kind, it is plain that a compound of the same mean price will be formed by taking 3 times, 4 times, one half, or any proportion of each quantity. Hence,

When the quantity of one simple is given, after finding the proportional quantities by the above rule, we may say— As the proportional quantity : is to the given quantity :: so

ALLIGATION.

is each of the other proportional quantities : to the required quantities of each.

4. If a man wishes to mix a gallon of brandy worth 16s. with rum at 9s. per gallon, so that the mixture may be worth 11s. per gallon, how much rum must he use?

Taking the differences as above, we find the proportions to be 2 of brandy to 5 of rum; consequently, one gallon of brandy will require 21 gallons of rum. Ans. 24 gals,

5. A grocer has sugars worth 7d. 9d. and 12d. per pound, which he would mix so as to form a compound worth 10d. per lb.; what must be the proportions of each kind?

Ans. 2 lbs. of the 1st and 2nd to 4 lbs. of the 3rd kind. 6. If he use 1 lb. of the 1st kind, how much must he take of the others ?----- if 4 lbs. what ? ----- if 6 lbs. what ?--if 10 lbs. what ?-----if 20 lbs. what ?

Ans. to the last, 20 lbs. of the 2nd and 40 of the 3rd. 7. A merchant has spices at 16d. 20d. and 32d per lb.: he would mix 5 lbs. of the first sort with the others, so as to form a compound worth 24d. per lb; how much of each sort must he use?

Ans. 5 lbs. of the 2nd and 74 lbs. of the 3rd. 8. How many gallons of water of no value must be mixed with 60 gallons of rum, worth 48d. per gallon, to reduce its value to 42d. per gallon ? Ans. 84 gallons.

9. A man would mix 4 bushels of wheat at 90d. per bushel, rye at 70d. corn at 70d. and barley at 30d. so as to sell the mixture at 48d. per bushel; how much of each may he use?

10. A goldsmith would mix gold 17 carats fine with some 19, 21 and 24 carats fine, so that the compound may be 22 carats fine; what proportions of each must he use?

Ans. 2 of the 3 first sorts to 9 of the last.

11. If he use one ounce of the first kind, how much must he use of the others? What would be the quantity of the Ans. to the last, $7\frac{1}{2}$ ounces. compound?

12. If he would have the whole compound consist of 15 ounces, how much of each kind ? ----- if of 374 ounces how Ans. to last, 5 oz. of the 3 first, 221 oz. of the last. much ?

Hence, when the quantity of the compound is given, we may say-As the sum of the proportional quantities found by the above rule, is to the quantity required, so is each

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DUODECIMALS.

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os. of the 3rd. ust be mixed to reduce its s. 84 gallons. d. per bushel, as to sell the may he use? ne with some ad may be 22 use ?

proportional quantity, found by the rule, to the required quantity of each.

13. A man would mix a hundred pounds of sugar, some at 8d. some at 10d. and some at 14d. per lb., so that the compound may be worth 12d. per lb.; how much of each kind must he use?

We find the proportions to be 2, 2 and 6. Then 2+2+6=10, and (2:20 lbs. 8d.)

 $10:100:: \left\{ \begin{array}{l} 2:20 & \text{`` 10d.} \\ 6:60 & \text{`` 14d.} \end{array} \right\} Ans.$

14. How many gallons of water of no value, must be mixed with brandy at 120d. per gallon, so as to fill a vessel of 75 gallens, which may be worth 92d. per gallon?

Ans. $17\frac{1}{2}$ gallons of water to $57\frac{1}{2}$ of brandy. 15. A grocer has currants at 4d. 6d. 9d and 11d. per lb. and he would make a mixture of 240 lbs., so that the mixture may be sold at 8d. per lb.; how many pounds of each sort may he take?

Ans. 72, 24, 48 and 96 lbs.; or 48, 48, 72, 72, &c. Note. This question may have five different answers.

QUESTIONS.

1. What is alligation? 2. — medial? 3. — the rule for operating? 4. What is alligation alternate? 5. When the price of the mixture, and the price of the several simples are given, how do you find the proportional quantities of each simple? 6. When the quantity of one simple is given, how do you find the others? 7. When the quantity of the whole compound is given, how do you find the quantity of each simple?

DUODECIMALS.

¶ 97. Duodecimals are fractions of a foot. The word is derived from the Latin word *duodecim*, which signifies *twelve*. A foot, instead of being divided decimally into ten equal parts, is divided duodecimally into twelve equal parts, called inches, or *primes*, marked thus, ('). Again, each of these parts is conceived to be divided into twelve other equal parts called *seconds*, ("). In like manner, each second is conceived to be divided into twelve equal parts, called *thirds* (""); each third into twelve equal parts called *fourths*, ("") and so on to any extent.

MULTIPLICATION OF DUODECIMALS.

In this way of dividing a foot, it is obvious that 1' inch or prime is $-\frac{1}{12}$ of a foot, 1'' second is $\frac{1}{12}$ of $\frac{1}{12}$ $-\frac{1}{12}$ of a foot, 1''' third is $\frac{1}{12}$ of $\frac{1}{12}$ of $\frac{1}{12}$ $-\frac{1}{12}$ $\frac{1}{1728}$ " 1'''' fourth is $\frac{1}{12}$ of $\frac{1}{12}$ of $\frac{1}{12}$ of $\frac{1}{12}$ $-\frac{1}{28}$ 5 $\frac{1}{12}$ $\frac{1}{$

Duodecimals are added and subtracted in the same manner as compound numbers, 12 of a less denomination making one of a greater, as in the following TABLE

	I ADLL		
12''''	fourths make	1'''	' third,
12‴	thirds	1″	second,
12″	seconds >	l'	inch or prime,
12′	inches or primes	1	foot.

Note. The marks, ', ", "", "", &c. which distinguish the different parts, are called the indices of the parts or denominations.

MULTIPLICATION OF DUODECIMALS.

Duodecimals are chiefly used in measuring surfaces and solids.

1. How many square feet in a board 16 feet 7 inches long, and 1 foot 3 inches wide?

Note. Length×breadth=superficial contents, (¶ 25.) OPERATION.

Length Breadth	16 16 1	7′ 3′	
Dicuutii	_		

4	1′	9″
16	7'	

Ans. 20 8' 9"

7 inches or primes $=_{12}^{7}$ of a foot and 3 inches $=_{12}^{3}$ of a foot; consequently, the product of 7' $\times 3' =_{12}^{-2} 1_2'$ of a foot, that is, 21" = 1' and 9", wherefore, we set down the 9", and reserve the 1' to be carried forward to its proper place. To multiply 16

feet by 3' is to take $\frac{3}{12}$ of $\frac{16}{16} = \frac{48}{12}$, that is 48'; and the l' which we reserved makes 49',=4 feet l'; we therefore set down the l', and carry forward the four feet to its proper place. Then, multiplying the multiplicand by the one foot in the multiplier, and adding the two products together, we obtain the *answer*, 20 feet, 8', 9".

The only difficulty that can arise in the multiplication of duodecimals is, in finding of what denomination is the proIt is the mu the inc *ft.* 16 1 16 4

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Length, Breadth

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es = $\frac{7}{12}$ of a $\frac{3}{2}$ of a foot; oduct of 7' that is, 21" ore, we set reserve the ward to its multiply 16 ; and the 1' herefore set its proper the one foot ogether, we

plication of is the pro97. MULTIPLICATION OF DUODECTMALS.

duct of any two denominations. This may be ascertained as above, and in all cases it will be found to hold true that the product of any two denominations will always be of the denomination denoted by the sum of their indices. Thus, in the above example the sum of the indices of $7' \times 3'$ is "; consequently, the product is 21''; and thus primes multiplied by primes will produce seconds; primes multiplied by seconds produce thirds; fourths multiplied by 5ths produce ninths, &c.

ft.16 feet \times 1 foot = 16 feet; and 7' \times 116 7'foot = 7'. Then, 16 feet \times 3'=48'=1 3'4 feet, and 7' \times 3'=21"=1' 9". The two16 7'products added together, give for the
answer, 20 feet 8' 9", as before.

20 8' 9"

2. How many solid feet in a block 15 feet 8' long, 1 foot 5' wide, and 1 foot 4' thick?

f Length, 1 Breadth,	t. 15 1	8' 5'	14	
	15	8'		
1 ¹ -, '	6	6′	4″	•
	22	2'	4"	
Thickness	1	4'	1.1	, '
	22	. 21	4″	
[+ , , +	7	4	9″	À //
•				

The length multiplied by the breadth, and that product by the thickness, gives the solid contents. (1] 33.)

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MULTIPLICATION OF DUODECIMALS. 197, 98.

- EXAMPLES FOR PRACTICE.

3. How many square feet in a stock of 15 boards, 12 feet 8' in length, and 13' wide? Ans. 205 feet 10',

4. What is the product of 371 feet 2' 6" multiplied by 181 feet 1' 9"? Ans. 67242 feet 10' 1" 4" 6"".

Note. Painting, plastering, paving, and some other kinds of work, are done by the square yard. If the contents in square feet be divided by 9, the quotient, it is evident, will be square yards.

5. A man painted the walls of a room 8 feet 2' in height, and 72 feet 4' in compass; that is, the measure of all its sides; how many square yards did he paint?

Ans. 65 yards 5 feet 8' 8".

6. How many cord feet of wood in a load 8 feet long, 4 feet wide, and 3 feet 6 inches high ?

Note. It will be recollected that 16 solid feet make a word foot. Ans. 7 cord feet.

7. In a pile of wood 176 feet in length, 3 feet 9' wide, and 4 feet 3' high, how many cords ?

Ans. 21 cords, 775 cord feet.

8. How many cord feet of wood in a load 7 feet long, 3 feet wide, and 3 feet 4' high; and what will it come to at 2s. per cord foot?

Ans. 43 cord feet, and will come to Ss. 9d. 9. How much wood in a load 10 feet in length, 3 feet 9' in width, and 4 feet 8' in height ? and what will it cost at \$1'92 per cord ?

Ans. 1 cord and $2\frac{15}{16}$ cord feet, and it will come to $2^{\circ}62\frac{1}{2}$.

T 98. Remark.—By some surveyors of wood, dimensions are taken in feet and decimals of a foot. For this purpose, make a rule or scale 4 feet long, and divide it into feet and each foot into ten equal parts. On one end of the rule for 1 foot, let each of these parts be divided into ten other equal parts. The former division will be tenths, and the latter hundredths of a foot. Such a rule will be found very convenient for surveyors of wood and lumber, for painters, joiners, &c.; for the dimensions taken by it being in feet and decimal parts of a foot, the casts will be no other than so many operations in decimal fractions.

10. How many square feet in a hearth stone, which, by a

rule, as 2'6 feet square f 11. H 3'6 feet 12. H

1 98, 99

3'4 feet

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¶ 98, 99.

INVOLUTION.

rule, as above described, measures 4'5 feet in length, and 2'6 feet in width ? and what will be its cost, at 75 cents per square foot ? Ans. 11'7 feet; and it will cost \$8'775. 11. How many cords in a load of wood 7'5 feet in length, 3'6 feet in width, and 4'8 feet in height ? Ans. 1 cord 1 % ft.

12. How many cord feet in a load of wood 10 feet long, 3'4 feet wide, and 3'5 feet high? Ans. $7\frac{7}{76}$.

QUESTIONS.

1. What are duodecimals? 2. From what is the word derived? 3. Into how many parts is a foot usually divided, and what are the parts called? 4. What are the other denominations? 5. What is understood by the indices of the denominations? 6. In what are duodecimals chiefly used? 7. How are the contents of a surface bounded by straight lines found? 8. How are the contents of a solid found? 9. How is it known of what denomination is the product of any two denominations? 10. How may a scale or rule be formed for taking dimensions in feet and decimal parts of a foot?

INVOLUTION.

¶ 99. Involution, or the raising of powers, is the multiplying any given number into itself continually a certain number of times. The products thus produced are called the powers of the given number. The number itself is called the first power or root. If the first power be multiplied by itself, the product is called the second power or square : if the square be multiplied by the first power, the product is called the third power, or cube, &cc: thus :

5 is the root, or first power of 5,

$5 \times 5 = 25$ is th	e 2d p	ower,	or square	of 5, $=5^2$
5×5×5=125	3d -	66	cube, o	$f 5, =5^3$
$5 \times 5 \times 5 \times 5 = 625$	4th	**	biquadra	ate, of 5,=54
The number denotin	g the j	power	is called	the index, or
exponent; thus, 54 deno	tes tha	it 5 is :	raised or in	volved to the
4th power.				
1. What is the squar	e or 2d	power	r of 7?	Ans. 49.
9	of 30	1		Ang '900

2.	66.	• • • • • • • • • • • • • • • • • • •	Ans 900.
3.	**	" of 4000 ?	Ans. 16000000.
4.	"	cube or 3d power of 4?	Ans. 64.
5.	"	" of 800 ?	Ans. 512000000.
6.		4th power of 60 ?	Ans. 12960000.
EVOLUTION.

¶ 99, 100.

7. What is the square of 1? — of 2? — of 3? —

 f 4 ?
 Ans. 1, 4, 9, and 16.

 8. What is the cube of 1 ?----of 2 ?----of 3 ?---
 of 4 ? Ans. 1, 8, 27, and 64. of 4 ? 1 Ans. 4, 18, 49. 10. What is the cube of $\frac{2}{3}$? ---- of $\frac{4}{3}$? ---- of $\frac{4}{3}$? Ans. 87, 64, and 343. 11. What is the square of $\frac{1}{2}$? — the 5th power of $\frac{1}{2}$? Ans. 1, and 32. 12. What is the square of 1'5? —— the cube? Ans. 2'25, and 3'375. Ans, 2'985984, 13. What is the 6th power of 1'2? 14. Involve 21 to the 4th power: Note. A mixed number like the above may be reduced to an improper fraction before involving : thus, $2_{1}=\frac{9}{4}$; or it may be reduced to a decimal; thus, $2\frac{1}{4}=2^{\circ}25$. Ans. 6561=25161. 15. What is the value of 7⁴, that is, the 4th power of 7? Ans. 2401.

Ans. 729, 7776, 10000. 17 How much is 2^7 ? _____ 3^6 ? _____ 4^5 ? _____ 5^3 ? _____ $6^5? - 10^3?$ Ans. to the last, 100000000. The powers of the nine digits, from the first power to

the fifth, may be seen in the following

Roots	1	T	2	1	-3	4	T	õ	6	7	81	9
Squares	1	Ī	4	T	9	16	I	25	.36	49	64	81
Cubes ,	1	1	8	T	27	64	1	125	216	343	512	729
Biquadrat	s l	ī	16	T	81	256	1	625	1296	2401	4096	6561
Sursolids	1	Ī	32	T	243	1024	1	3125	7776	16807	32768	59049

TABLE.

EVOLUTION.

¶ 100. Evolution, or the extracting of roots, is the method of finding the root of any power or number.

The root, as we have seen, is that number which, by a continual multiplication into itself, produces the given power. . The square root is a number which, being squared, will

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EXTRACTION OF THE SQUARE ROOT.

produce the given number; and the cube, or third root, is a number which, being cubed or involved to the third power, , 9, and 16. will produce the given number; thus, the square root of 144 is 12, because $12^2 = 144$; and the cube root of 343 is 7, be-27, and 64. cause 7³, that is, $7 \times 7 \times 7 = 343$; and so of other numbers. 5. 4, 18, 49.

Although there is no number which will not produce a perfect power 'by involution, yet there are many numbers of which precise roots can never be obtained. But by the help of decimals, we can approximate, or approach towards the root to any assigned degree of exactness. Numbers, whose precise roots cannot be obtained, are called surd numbers, and those whose roots can be exactly obtained, are called *rational* numbers.

The square root is indicated by this character \checkmark placed before the number; the other roots by the same character with the index of the root placed over it. Thus, the square root of 16 is expressed $\sqrt{16}$; and the cube root of 27 is

expressed $\sqrt{27}$, and the 5th root of 7776, $\sqrt{7776}$.

When the power is expressed by several numbers, with the sign + or — between them, a line, or *vinculum*, is drawn from the top of the sign over all the parts of it; thus

the square root of 21-5 is $\sqrt{21-5}$, &c.

Fxtraction of the Square Root.

To extract the square root of any number is. **T 101.** to find a number, which, being multiplied into itself, shall produce the given number.

1. Supposing a man has 625 yards of carpeting, a yard wide, what is the length of one side of a square room, the foor of which the carpeting will cover ? that is, what is one side of a square, which contains 625 square yards?

We have seen (\P 32) that the contents of a square surface is found by multiplying the length of one side into itself, that is, by raising it to the second power; and hence, having the contents (625) given, we must extract its square rout to find one side of the room.

This we must do by a sort of trial, and

1st. We will endeavour to ascertain how many figures

512 1 729 4096 6561 32768 59049

9

81

81

64

roots, is the ber.

which, by a given power. squared, will ø

EXTRACTION OF THE SQUARE ROOT.

there will be in the root. This we can easily do, by pointing off the number, from units, into periods of two figures each; for the square of any root always contains just twice as many, or one figure *less* than twice as many figures, as are in the root; of which truth the pupil may easily satisfy himself by trial. Pointing off the number, we find that the

	OPERATION. 625(2 4 	5
d	Fig. 1.	
2	A	
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a	20	'ı

root will consist of *two* figures —a ten and a unit.

2d. We will now seek for the first figure, that is, for the tens of the root, and it is plain that we must extract it from the left hand period 6, (hunc dreds) The greatest square in 6 (hnndreds) we find, by trial, to be 4, (hundreds) the root of which is 2, (tens=20) therefore, we set 2 (tens) in the root. The root, it will be recollected, is one side of a square. Let us, then, form a square, (A. fig. 1,) each side of which shall be supposed 2 tens, = 20 yards, expressed by the root now obtained.

The contents of this square are 20×20 —400 yards, now disposed of, and which, consequently, are to be deducted from the whole number of yards, (625) leaving 225 yards. This deduction is most readily performed by subtracting the square number 4, (hundreds) or the square of 2, (the figure in the root already found) from the period 6, (hundreds) and bringing down the next period by the side of the remainder making 225, as before.

3d. The square A. is now to be enlarged by the addition of the 225 remaining yards; and in order that the figure may retain its square form, it is evident the addition must be made on *two* sides. Now, if the 225 yards be divided by the length of the *two* sides, (20+20=40) the quotient will be the *breadth* of this new addition of 225 yards to the sides c d and b c of the square A. of whic add this right ha divisor, tents of A, whic dividence Consequ 25 yard will exa

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1 101. EXTRACTION OF THE SQUARE ROOT.

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0 yards, now be deducted g 225 yards. subtracting re of 2, (the iod 6, (hune side of the

the addition at the figure ddition must e divided by quotient will s to the sides But our root already found, =2 tens, is the length of one side of the figure A; we therefore take *double* this root,=4 tens, for a divisor.



The divisor 4 (tens) is in reality 40, and we are to seek how many times 40 is contained in 225, or, which is the same thing, we may seek how many times 4 (tens) is contained in 22, (tens) rejecting the or right hand figure of the a dividend, because we have rejected the cipher in the divisor. We find our quotient, that is, the breadth of the s addition, to be 5 yards; but if we look at fig. 2, we shall perceive that this addition of 5 yards to the 2 sides does not complete the square; for there is still wanting in the corner D, a small square, each side

of which is equal to this last quotient, 5; we must therefore add this quotient 5, to the divisor 40, that is, place it at the right hand of the 4 (tens) making it 45; and then the whole divisor, 45, multiplied by the quotient, 5, will give the contents of the whole addition around the sides of the figure A, which, in this case, being 225 yards, the same as our dividend, we have no remainder, and the work is done. Consequently, fig. 2 represents the floor of a square room, 25 yards on a side, which 625 square yards of carpeting will exactly cover.

The proof may be seen by adding together the several parts of the figure, thus :---

EXTRACTION OF THE SQUARE ROOT.

e	square	A	contains	400	yards.	. still still state
	figure	B	"	100	·	Or we may prove in
	""	С	"	100	"	by involution, thus :-
	"	D	"	25	"	25×25=625, as be
	1		,			fore

Proof 625

From this example and illustration, we derive the following general

RULE

For the Extraction of the Square Root.

1. Point off the given number into periods of two figures each, by putting a dot over the units, another over the hundreds, and so on. These dots show the number of figures of which the root will consist.

II. Find the greatest square number in the left hand period, and write its root as a quotient in division. Subtract the square number from the left hand period, and to the remainder bring down the next period for a dividend.

III. Double the root already found for a divisor; seek liow many times the divisor is contained in the dividend, excepting the right hand figure, and place the result in the root, and also at the right hand of the divisor; multiply the divisor, thus augmented, by the last figure of the root, and subtract the product from the dividend; to the remainder bring down the next period for a new dividend.

IV. Double the root already found for a new divisor, and continue the operation as before, until all the periods are brought down, and the

Note 1. If we double the right hand figure of the last divisor, we shall have the double of the root.

Note 2. As the value of figures, whether integers or decimals, is determined by their distance from the place of units so we must always begin at unit's place to point off the given number, and, if it be a mixed number, we must point it off hoth ways from units, and if there be a deficiency in any period of decimals, it may be supplied by a cipher. It is plain the root must always consist of so many integers and decimals as there are periods belonging to each in the given number.

- EXAMPLES FOR PRACTICE.

2. What is the square root of 10342656?

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	38556
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3. What is the square root of 43264?



4.	What	is the	square	root	of 993001?	Ans. 999.
5.	**		• • •	"	234'09 ?	Ans. 15'3.
6.	"		"	"	964'5192360	241?
					Α	ns. 31'05671.
7.	"		**	"	'001296 ?	Ans. '036.
8.	"	·,	"	"	'2916 ?	Ans. '54.
9.			"	"	36372961 ?	Ans. 6031.
10.	"		""	"	164 ?	Ans. 12'8+

1102. In this last example, as there was a remainder after bringing down all the figures, we continued the operation to decimals, by annexing two ciphers for a new period, and thus we may continue the operation to any assigned degree of exactness; but the pupil will readily perceive that he can never in this manner obtain the *precise* root; for the last figure in each dividend will always be a cipher, and the last figure in each divisor is the same as the last quotient figure; but no one of the nine digits multiplied into itself,

S2

SUPPLEMENT TO THE SQUARE ROOT.

produces a number ending with a cipher; therefore, whatever be the quotient figure, there will still be a remainder.

11.	What is th	e square	root	of 3?	- Ans. 1'73+.
12.	66		66	107	Ans. 3'16
13.	"	"	"	184'2?	Ans. 13'57+.
14.	"	"	"	\$?	

Note.—We have seen (¶ 99, ex. 9,) that fractions are squared by squaring both the numerator and the denominator. Hence it follows, that the square root of a fraction is found by extracting the root of the numerator and of the denominator. The root of 4 is 2, and the root of 9 is 3.

•					Ans. 2.
15.	What is	the square	root	of 45?	Ans. Z.
16.	"	- • •	.4	16 ?	Ans. 4.
17.	46	**	66.	81 ?	Ans====================================
18.	66	"	"	2017	Ans. 44.
Whe	en the n	umerator	and	denominator	are not exact
square	s, the fra	ction may	be re	educed to a de	ecimal, and the
approx	imate roo	ot found. a	s dir	ected above.	

19.	What is	the square	root of	2='75?	Ans. '866+.
20.	"	•	""	35 ?	Ans. '912+.

SUPPLEMENT TO THE SQUARE ROOT.

QUESTIONS.

1. What is involution? 2. What is understood by a power? 3. - the first, the second, the third, the fourth power? 4. What is the index, or exponent? 5. How do you involve a number to any required power? 6. What is evolution? 7. What is a root? 8. Can the precise root of all numbers be found? 9. What is a surd number? 10. --- a rational ? 11. What is it to extract the square root of any number? 12. Why is the given sum pointed into periods of two figures each? 13. Why do we double the root for a divisor? 14. Why do we, in dividing, reject the right hand figure of the dividend ? 15. Why do we place the quotient figure to the right hand of the divisor? 16. How way we prove the work? 17. Why do we point off mixed numbers both ways from units? 18. When there is a remainder, how may we continue the operation ? 19, Why can we never obtain the precise root of suid numbers? 20. How do we extract the square root of vulgar fractions t

EXERCISES.

1. A general has 4095 men; how many must he place in rank and file, to form them into a square? Ans. 64.

2. If a rods doe 3. Ho taining 4 4. Th is 5184 of equal 5. A. other con field con how man

6. If a how much ing 4 tim 7. If t of one 4 times as large ? 8. It i

of a pare length a Note.

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SUPPLEMENT TO THE SQUARE ROOT.

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Ans. $\frac{2}{5}$. Ans. $\frac{1}{5}$. Ans. $\frac{1}{70}$. Ans. $\frac{1}{72}$ Ans. $\frac{1}{2}$. e not exact hal, and the

Ins. '866+. Ins. '912+.

ROOT.

power? 3. A. What is ber to any repot? 8. Can surd number? re root of any eriods of two divisor? 14. the dividend? nd of the diviwe point off is a remainwe never obve extract the

he place in Ans. 64. 2. If a square field contains 2025 square rods, how many rods does it measure on each side ? Ans. 45.

3. How many trees in each row of a square orchard containing 5625 trees? Ans. 75.

4. There is a circle whose area, or superficial contents, is 5184 feet; what will be the length of the side of a square of equal area? $\sqrt{5184}$ =72 feet, Ans.

5. A. has two fields, one containing 40 acres, and the other containing 50 acres, for which B. offers him a square field containing the same number of acres as both of these; how many rods must each side of this field measure?

Ans. 120 rods. 6. If a certain square field measure 20 rods on each side, how much will the side of a square field measure, containing 4 times as much? $\sqrt{20 \times 20} \times 4 = 40$ rods, Ans. 7. If the side of a square be 5 feet, what will be the side of one 4 times as large? 9 times as large? 16 times as large? 25 times as large? 36 times as large? Ans. 10ft. 15ft. 20ft. 25ft. and 30ft.

8. It is required to lay out 288 rods of land in the form of a parellelogram, which shall be twice as many rods in length as it is in width.

Note. If the field be divided in the middle, it will form two *equal* squares. Ans. 24 rods long and 12 rods wide.

9. I would set out, at equal distances, 784 apple trees, so that my orchard may be four times as long as it is broad; how many rows of trees must I have, and how many trees in each row? Ans. 14 rows, and 56 in each row.

10. There is an oblong piece of land, containing 192 square rods, of which the width is $\frac{3}{4}$ as much as the length; required, its dimensions. Ans. 16 by 12.

11. There is a circle whose diameter is 4 inches; what is the diameter of a circle 9 times as large?

Note. The areas, or contents of circles are in proportion to the squares of their diameters, or of their circumferences. Therefore, to find the diameter required, square the given diameter, multiply the square by the given ratio, and the square root of the product will be the diameter required.

 $\sqrt{4\times4\times9}=12$ inches, Ans. 12. There are two circular ponds in a gentleman's pleasure ground; the diameter of the less is 100 feet, and the greater is 3 times as large; what is its diameter?

Ans. 1732+ft.

13. If the diameter of a circle be 12 inches, what is the diameter of one 1 as large? Ans. 6 inches.

¶ 103. 14. A carpenter has a large wooden square; one part of it is 4 feet long, and the other 3 feet long; what is the length of a pole that will just reach from one end to the other (



Note.—A figure of three sides is called a triangle, and if one of the corners be a square corner, or right angle, like the angle at **B.** in the annexed figure, it is called a right-angled triangle, of which the square of the longest side A. C. (called the hypotenuse) is equal to the sum of the squares of the other 2 sides. A. B. and B. C.

 $4^2 = 16$, and $3^2 = 9$; then $\sqrt{9 + 16} = 5$ feet, Ans. 15. If, from the corner of a square room, 6 feet be measured off one way, and 8 feet the other way, along the sides of the room, what will be the length of a pole reaching from Ans. 10 feet. point to point?

16. A wall is 32 feet high, and a ditch before it is 24 feet wide; what is the length of a ladder that will reach from the top of the wall to the opposite side of the ditch?

Ans. 40 feet.

17. If the ladder be forty feet, and the wall 32 feet, what is the width of the ditch? Ans. 24 feet.

18. The ladder and ditch given, required the wall. Ans. 32 feet.

19. The distance between the lower ends of two equal rafters is 32 feet, and the height of the ridge above the beam on which they stand is 12 feet; required, the length of each Ans. 20 feet. rafter.

20. There is a building 30 feet in length and 22 feet in

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ns. 32 feet. f two equal ve the beam igth of each ns. 20 feet. 22 feet in

EXTRACTION OF THE CUBE ROOT.

width, and the gaves project beyond the wall a foot on every side; the roof terminates in a point at the centre of the building, and is there supported by a post, the top of which is ten feet above the beams on which the rafters rest; what is the distance from the foot of the post to the corners of the eaves? and what is the length of a rafter reaching to the middle of one *side*? —— a rafter reaching to the middle of one *end*? and a rafter reaching to the *corners* of the eaves? Ans. in order, 20ft.; 15'62 + ft; 18'86 + ft; and 22'36 + ft

21. There is a field 800 rods long and 600 rods wide; what is the distance between two opposite corners?

... Ans. 1000 rods.

22. There is a square field containing 90 acres; how many rods in length is each side of the field ? and how many rods apart are the opposite corners?

11.17

23. There is a square field containing 10 acres; what distance is the centre from each corner? Ans. $28^{\circ}28^{\circ}+$ rods.

EXTRACTION OF THE CUBE ROOT.

¶ 104. A solid body, having six equal sides, and each of the sides an *exact square*, is a *cube*, and the measure in length of one of its sides is the *root* of that cube; for the length, breadth, and thickness of such a body are all alike; consequently, the length of one side, raised to the third power, gives the solid contents. See ¶ 33.

Hence it follows, that extracting the cube root of any number of feet, is finding the length of one side, of a cubic body, of which the whole contents will be equal to the given number of feet.

1. What are the solid contents of a cubic block, of which each side measures 2 feet? Ans. $2^3=2\times2\times2=8$ feet.

2. How many solid feet in a cubic block, measuring 5ft. on each side? $Ans. 5^3 = 125$ feet.

3. How many feet in length is each side of a cubic block containing 125 solid feet? Mathematical solid feet? Mathematical solid feet?

Note. The root may be found by trial.

4. What is the side of a cubic block containing 64 solid feet? 27 solid feet? 216 solid feet? 512 solid feet? Ans. 4ft.; 3ft.; 6ft.; and 8ft.

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5. Supposing a man has 13824 feet of timber, in separate blocks of one cubic foot each; he wishes to pile them up in a cubic pile; what will be the length of each side of such a pile?

It is evident, the answer is found by extracting the cube root of 13824; but this number is so large, that we cannot so easily find the root by trial as in the former examples; We will endeavor, however, to do it by a sort of trial; and

1st. We will try to ascertain the number of figures, of which the root will consist. This we may do by pointing the number off into periods of 3 figures each (\P 101, ex. 1.)

Pointing off, we see, the root will consist of two figures, a ten and a unit. Let us then seek for the first figure, or tens of the root, which must be extracted from the left hand period, 13 (thousands.) The greatest cube in thirteen (thousands) we find by trial, or by the table of powers, to be 8 (thousands) the root of which is 2 (tens;) therefore, we place 2 (tens) in the root. The root, it will be recollected, is one side of a cube. Let us then form a cube, (fig. 1.) each side of which shall be supposed 20 feet, expressed by the root now obtained. The contents of this cube are $20 \times 20 \times 20 = 8000$ solid feet which are now disposed of,

and which, consequently, are to be deducted from the whole number of feet, 13824. 8000 taken from 13824, leave 5824 feet. This deduction is most readily performed by subtracting the cubic number, 8, or the cube of 2, (the figure of the root already found) from the period 13, (thousands) and bringing down the next period by the side of the remainder, making 5824, as before.

2d. The cubic pile A D is now to be enlarged by the

= 1200 made to already fore squ content: number effect, 2, (tens and 4× OPER

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EXTRACTION OF THE CUBE ROOT.

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ting the cube at we cannot er examples ; of trial; and of figures, of by pointing] 101, ex. 1.) we see, the of two figures, Let us then st figure, or which must a cube. Let w obtained. this cube are disposed of, 3824, leave erformed by d 13, (thou-

om the left (thousands.) e in thirteen find by trial, of powers, to the root of ;) therefore,) in the root. be recollectube, (fig. 1.) ich shall be t, expressed 00 solid feet om the whole e of 2, (the e side of the

rged by the

addition of 5824 solid feet, and, in order to preserve the cubic form of the pile, the addition must be made on one half of its sides, that is, on three sides, a, b, and c. Now, if the 5824 solid feet be divided by the square contents of these three equal sides, that is, by 3 times, $(20 \times 20 = 400)$ =1200, the quotient will be the thickness of the addition made to each of the sides a, b, c. But the root 2, (tens) already found, is the length of one of these sides; we therefore square the root 2, $(tens)=20\times 20=400$, for the square contents of one side, and multiply the product by three, the number of sides, $400 \times 3 = 1200$, or, which is the same in effect, and more convenient in practice, we may square the 2, (tens) and multiply the product by 300, thus, $2 \times 2 = 4$, and $4 \times 300 = 1200$, for the divisor, as before.

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Fig. II.

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The divisor, 1200, is con-**OPERATIONS** CONTINUED. tained in the dividend 4 times; 13824 (24 Root. consequently, 4 feet is the thickness of the addition made to each of the 3 sides a, b, c, Divis. 1200)5824 Dividend. and 4×1200=4800, is the solid feet contained in these additions; but if we look at fig. 2, we shall perceive that this addition to the 3 sides does not complete the cube; for there are deficiencies in the three corners n, n, n. Now the length of each of these deficiencies is the same as the length of each side, that is, 2 (tens)=20, and their width. and thickness are each equal to the last quotient figure (4); their contents, therefore, or 20 the number of feet required to fill these deficiencies, will be by multiplying the found square of the last quotient 20 figure $(4^2) = 16$, by the length of all the deficiencies, that is, by 3 times the length of each

side, which is expressed by the former quotient figure, 2 (tens.) 3 times 2 (tens) are 6 (tens)=60; or, what is the same in effect, and more convenient in practice, we may multiply the quotient figure 2 (tens) by 30, thus, 2×30 = 60, as before; then, 60×16 =960, contents of the three deficiencies, n, n, n.



Looking at fig. 3, we perceive there is still a deficiency in the corner where the last blocks meet. This deficiency is a cube, each side of which is equal to the last quotient 20 figure, 4. The cube of 4, therefore, $(4 \times 4 \times 4 = 64)$ will be the solid contents of this corner, which, in figure 4, is seen filled.

Now, the sum of these several additions, viz. 4800+960+64=5824, will make the subtrahend, which, subtracted from the dividend, leaves no remainder, and the work is done³

Figure 4 shows the pile which 13324 solid blocks of one foot cach would make, when laid together, and the root 24 shows the length of one side of the pile. The

correctness of the work may be ascertained by cubing the side now found, 24^3 , thus $24 \times 24 \times 24 = 13824$, the given number; or it may be proved by adding together the contents of all the several parts, thus—

Feet.—8009=contents of fig. 1.

4800=addition to the sides a, b, c, fig. 1.

13824 = contents of the whole pile, figure 4, -21 feet on each side.

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EXTRACTION OF THE CUBE ROOT.

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1. . *n*, *n*, fig. 2. fig. 4.

4,-21 feet

From the foregoing example and illustration, we derive the following

RULE

For Extracting the Cube Root.

I. Separate the given number into periods of three figures each, by putting a point over the unit figure, and every third figure beyond the place of units.

II. Find the greatest cube in the left hand period, and put its root in the quotient.

III. Subtract the cube thus found from the said period, and to the remainder bring down the next period, and call this the *dividend*.

IV. Multiply the square of the quotient by 300, calling it the *divisor*.

V. Seek how many times the divisor may be had in the dividend, and place the result in the root; then multiply the divisor by this quotient figure, and write the product under the dividend.

VI. Multiply the square of this quotient figure by the former figure or figures of the root, and this product by 30, and place the product under the last; under all, write the cube of this quotient figure, and call their amount the sub-trahend.

VII. Subtract the subtrahend from the dividend, and to the remainder bring down the next period for'a new dividend, with which proceed as before; and so on, till the whole is finished.

Note 1.—If it happens that the divisor is not contained in the dividend, a cipher must be put in the root, and the next period brought down for a dividend.

Note 2.—The same rule must be observed for continuing the operation, and pointing off for decimals, as in the square root.

Note 3.—The pupil will perceive that the number which we call the divisor, when multiplied by the last quotient figure, does not produce so large a number as the real subtrahend; hence, the figure in the root must frequently be smaller than the quotient figure.

EXAMPLES FOR PRACTICE.

6. What is the cube root of 1860867?

UPPLEMENT TO THE CUBE ROOT.

OPERATION.

1860867 (123 Ans. 4 1²×300=300) 860 first Dividend. vhat wou 600 $2^2 \times 1 \times 30 = 120$ 23 8 728 first Subtrahend. 12²×300=43200) 132867 second Dividend. - 64 129600 $3^{2} \times 12 \times 30 =$ 3240 27 132867 second Subtrahend, proportion 000000 What is the cube root of 373248? Ans. 72. " " 21024576? Ans. 276. " " 84'604519? Ans. 4'39. " " **'000343**? Ans. '07. " " 21 Ans. 1'25-

12.	"	33	"	87?	. Ans. 2.	what is th
Note	. See	¶ 99, ex.	10, a	nd ¶ 102, ex. 14	4.	
13.	"		66	125 ?	Ans. 5.	9. The
14.	"		"	343 ?	Ans. 17.	ter, and t
15.	""	**	çi	500?	Ans. 125+.	smaller gl
16.	"	"	"	125?	Ans. $\frac{1}{5}$.	10 10.

SUPPLEMENT TO THE CUBE ROOT. QUESTIONS.

1. What is a cube? 2. What is understood by the cube root? 3. What is it to extract the cube root? 4. Why is the square of the quo-tiont multiplied by 300 for a divisor? 5. Why, in finding the subtrahend, do we multiply the square of the last quotient figure by 30 times the former figure of the root ? 6. Why do we cube the quotient figure? 7. How do we prove the operation ?

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EXERCISES.

1. What is the side of a cubical mound, equal to one 288. feet long, 216 feet broad, and 48 feet high ? Ans. 144 ft. 2. There is a cubic box, one side of which is 2 feet; how 3. How many cubic, feet in one 8 times as large; and what would be the length of one side?

Ans. 64 solid feet, and one side is 4 feet 1 11 4. There is a cubical box, one side of which is 5 feet; what would be the side of one containing 27 times as much? - 64 times as much? —— 125 times as much?

Ans. 15, 20, and 25 feet. 5. There is a cubical box measuring 1 foot on each side; what is the side of a box 8 times as large? ----- 27 times? - 64 times? Ans. 2, 3, and 4 feet. ¶ 105. Hence, we see that the sides of cubes are as the cube roots of their solid contents, and consequently, their contents are as the cubes of their sides. The same d Subtrahend proportion is true of the similar sides, or of the diameters of all solid figures of similar forms. db

6. If a ball weighing 4 lbs. be 3 inches in diameter, what Ans. 72 will be the diameter of a ball of the same metal, weighing Ans. 276 2 lbs. ? 4:32 :: 33:63 . 1 Ans. 6 inches, Ans. 4'39. 7. If a ball, 6 inches in diameter, weigh 32 pounds, what Ans. '07. will be the weight of a ball 3 inches in diameter ? Ans. 4 lbs. 8. If a globe of silver, one inch in diameter, he worth \$6, what is the value of a globe one foot in diameter?

Ans. \$10368. 9. There are two globes; one of them is 1 foot in diame-Ans. $\frac{1}{12}$ ter, and the other 40 feet in diameter; how many of the 125+, smaller globes would it take to make one of the larger?

Ans: 64000. 1. 1. 1.

10. If the diameter of the sun is 112 times as much as the diameter of the earth, how many globes like the earth would it take to make one as large as the sun? Ans. 1404928.

11. If the planet Saturn is 1000 times as large as the cabe root? 3. earth, and the earth is 7900 miles in diameter, what is the hare of the quo- diameter of Saturn ? Ans. 79:00 miles.

12. There are two planets of equal density; the diameter The by 30 times of the less is to that of the larger as 2 to 9; what is the ratio puotient figure? of their solidities? Ans. $\frac{8}{725}$; or, as 8 to 729.

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Ans. 1'25+. Ans. 3.

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ARITHMETICAL PROGRESSION: ¶ 105, 106.

Note. The roots of most powers may be found by the square and cube root only: thus, the biquadrate or 4th root is the square root of the square root; the 6th root is the cube root of the square root; the 8th root is the square root of the 4th root; the 9th root is the cube root of the cube root, &c. Those roots, viz. the 5th, 7th, 11th, &c. which are not resolvable by the square and cube roots, seldom occur; and when they do, the work is most easily performed by logarithms; for if the logarithm of any number be divided by the index of the root, the quotient will be the logarithm of the root itself.

ARITHMETICAL PROGRESSION.

11 POG. Any rank or series of numbers more than two, increasing or decreasing by a constant difference, is called an Arithmetical Series, or Progression.

When the numbers are formed by a continual addition of the common difference, they form an ascending series; but when they are formed by a continual subtraction of the common difference, they form a descending series.

Thus, { 3, 5, 7, 9,11,13,15, &c. is an ascending series, 15,13,11, 9, 7, 5, 3, &c. is a descending "

The numbers which form the series are called the *terms* of the series. The first and last terms are the *extremes*, and the other terms are called the *means*.

There are five things in arithmetical progression, any three of which being given, the other two may be found :-

1st. The first term.

2d. The last term.

3d. The number of terms.

4th. The common difference.

5th. The sum of all the terms.

1. A man bought 100 yards of cloth, giving 4d. for the first yard, 7d. for the second, 10d. for the third, and so on with a common difference of 3d.; what was the cost of the last yard?

As the common difference, 3, is added to every yard except the last, it is plain the last yard must be 99×3 ; = 297 pence more than the first yard. Ans. 301 pence.

Hence the num tiply the ence, ar 2. If the num 3. The corn ; the cond co ence of

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ARITHMETICAL PROGRESSION.

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very yard ex- 9×3 ; = 297s. 301 pence. Hence, when the first term, the common difference, and the number of terms are given, to find the last term,—Multiply the number of terms, less one, by the common difference, and add the first term to the product for the last term.

2. If the first term be 4, the common différence 3, and the number of terms 100, what is the last term? Ans. 301.

3. There are 'in a certain triangular field, 41 rows of corn ; the first row, in one corner, is a single hill; the second contains three hills, and so on, with a common difference of 2; what is the number of hills in the last row?

Ans. 81 hills.

4. A man puts out $\pounds 1$ at 6 per cent simple interest, which in one year amounts to $\pounds 1_{50}^{-3}$, in two years to $\pounds 1_{50}^{-6}$, and so on, in arithmetical progression, with a common difference of \pounds_{50}^{-3} ; what would be the amount in 40 years?

Ans. ± 3228 . Hence we see, that the yearly amounts of any sum, at simple interest, form an arithmetical series, of which the *principal* is the first term, the *last* amount is the last term, the yearly interest is the *common difference*, and the number of years is one less than the number of terms.

5. A man bought 100 yards of cloth in arithmetical progression; for the first yard he gave 4d., and for the last 301 pence; what was the common increase of the price.on each succeeding yard?

This question is the reverse of example 1; therefore, 301 -4=297, and $297\div99=3$, common difference.

Hence, when the extremes and number of terms are given to find the common difference,—Divide the difference of the extremes by the number of terms, less 1, and the quotient will be the common difference.

6. If the extremes be 5 and 605,, and the number of terms 151, what is the common difference ? Ans. 4.

7. If a man puts out £1 at simple interest, for 40 years, and receives at the end of the time $\pounds 3\frac{29}{56}$, what is the rate ? If the extremes be 1 and $3\frac{2}{56}$, and the number of terms 41, what is the common difference ?

8. A man had 8 sons whose ages differed alike; the youngest was 10 years old, and the eldest 45; what was the common difference of their ages?
9. A man bought 100 yards of cloth in arithmetical series;

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he gave 4 pence for the first yard, and 301 pence for the last yard; what was the average price per yard, and what was the amount of the whole?

Since the price of each succeeding yard increases by a constant excess, it is plain the average price is as much *less* than the price of the last yard as it is *greater* than the price of the first yard; therefore, one half the sum of the first and last price is the average price.

One half of 4d. \pm 301d. \pm 1521d. \pm average price; and the price, 1521d. \times 100 \pm 15250d. \pm Ans. £63 10s. 10d., whole cost.

Hence, when the extremes and the number of terms are given, to find the sum of all the terms, —Multiply half the sum of the extremes by the number of terms, and the product will be the answer.

10. If the extremes be 5 and 605, and the num er of terms be 151, what is the sum of the series? Ans. 46055.

11. What is the sum of the first 100 numbers, in their natural order, that is, 1, 2, 3, 4, &c. Ans 5050.

12. How many times does a common clock strike in 12 hours? Ans. 78.

13. A man rents a house for £50 annually, to be paid at the close of each year; what will the rent amount to in 20 years, allowing 6 per cent simple interest for the use of the money?

The last year's rent will evidently be £50 without interest, the last but one will be the amount of £50 for 1 year, the last but two the amount of £50 for 2 years, and so on, in arithmetical series, to the first, which will be the amount of £50 for 19 years=£107.

If the first term be 50, the last term 107, and the number of terms 20, what is the sum of the series ? Ans. \pounds 1570.

14. What is the amount of an annual pension of $\pounds 100$, being in arrears, that is, remaining unpaid, for 40 years. allowing 5 per cent simple interest? Ans. $\pounds 7900$.

15. There are, in a certain triangular field, 41 rows of corn; the first row being in one corner, is a single hill, and the last row, on the side opposite, contains 81 hills; how many hills of corn in the field? Ans. 1681 hills.

16. If a triangular piece of land, 30 rods in length, be 20 rods wide at one end, and come to a point at the other, what number of square rods does it contain? Ans. 300.

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d the number Ans. £1570. sion of £100, for 40 years. Ans. £7900. d, 41 rows of ingle hill, and 1 hills; how is. 1681 hills. in length, be at the other, Ans. 300. 17. A debt is to be discharged at 11 several payments, in arithmetical series, the first to be $\pounds 5$, and the last $\pounds 75$; what is the whole debt? —— common difference between the several payments?

Ans. whole debt £440; common difference £7. 18. What is the sum of the series 1, 3, 5, 7, 9, &c. to 1001? Ans. 251001.

Note. By the reverse of the rule under ex. 5, the difference of the extremes 1000, divided by the common difference 2, gives a quotient, which, increased by 1, is the number of terms = 501.

19. What is the sum of the arithmetical series $2, 2_{1}, 3, 3_{1}, 4, 4_{2}, \&c.$ to the 50th term inclusive? Ans. 7121.

20. What is the sum of the decreasing series $30, 29_3^2$, $29_3^1, 29, 28_3^2$, &c. down to 0?

Note. $30 \div \frac{1}{3} + 1 = 91$, number of terms. Ans. 1365.

QUESTIONS.

1. What is an arithmetical progression? 2. When is the series called ascending? 3. — when descending? 4. What are the numbers forming the progression called? 5. What are the first and last terms called ? 6. What are the other terms called ? 7. When the first term, common difference, and number of terms are given, how do you find the last term? 8. How may arithmetical progression be applied to simple interest? 9. When the extremes and number of terms are given. how do you find the sum of all the terms ?

GEOMETRICAL PROGRESSION.

§ 107. Any series of numbers, continually increasing by a constant multiplier, or decreasing by a constant divisor, is called a *Geometrical Progression*. Thus, 1,2,4,8,16, &c. is an increasing geometrical series, and 8, 4, 2, 1, $\frac{1}{2}$, $\frac{1}{4}$, &c. is a decreasing geometrical series.

As in arithmetical, so also in geometrical progression, there are five things, any three of which being given, the other two may be found :---

1st. The first term; 2d. The last term; 3d. The number of terms; 4th. The ratio; 5th. The sum of all the terms. The ratio is the multiplier, or divisor, by which the series is formed.

1. A man bought a piece of silk, measuring 17 yards, and, by agreement, was to give what the last yard would come to, reckoning 3 pence for the first yard, 6 pence for the second, and so on, doubling the price to the last; what did the piece of silk cost him?

In examining the process by which the last term (196608)has been obtained, we see that it is a product of which the *ratio* (2) is sixteen times a factor, that is, *one time less* than the number of terms. The last term, then, is the sixteenth power of the ratio, (2) multiplied by the first term, (3.)

Now, to raise 2 to the 16th power, we need not produce all the intermediate powers; for $2^4=2\times2\times2\times2=16$, is a product of which the ratio 2 is 4 times a factor; how, if 16 be multiplied by 16, the product, 256, evidently contains the same factor (2) 4 times+4 times,=8 times; and 256× 256=65536, a product of which the ratio (2) is 8 times + 8 times,=16 times, factor; it is, therefore, the 16th power of 2, and, multiplied by 3, the first term, gives 196608, the last term, as before, Hence,

When the first term, ratio, and number of terms, are given, to find the last term,—

- I. Write down a few leading powers of the ratio with their indices, over them.

II. Add together the most convenient indices, to make an index less by one than the number of the term sought.

III. Multiply together the powers belonging to those indices, and their product, multiplied by the first term, will be the term sought.

2. If the first term be 5, and the ratio 3, what is the 8th term?

Powers of the ratio with 1, 2, 3, -4 = 7.

their indices over them $3, 9, 27, \times 81 = 2187 \times 5$, first term, = 10935, Ans.

3. A man plants 4 kernels of corn, which, at harvest, produce 32 kernels; these he plants the second year; now,

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GEOMETRICAL PROGRESSION.

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at harvest, year; now, supposing the annual increase to continue 8 fold, what would be the produce of the 16th year, allowing 1000 ker-Ans. 2199023255'552 bushels. pels to a pint?

4. Supposing a man had put out one penny at compound interest in 1620, what would have been the amount in 1824, allowing it to double once in 12 years? 1

 $2^{17} = 131072.$ Ans. £546 2s. 8d. 5. A man bought 4 yards of cloth, giving 2d. for the first yard, 6d. for the second, and so on in 3 fold ratio; what did the whole cost him?

2+6+18+54=:80 pence

Ans. 80 pence. In a long series, the process of adding in this manner would be tedious. Let us try, therefore, to devise some shorter method of coming to the same result. If all the terms, excepting the last, viz. 2+6+18, be multiplied by the ratio, 3, the product will be the series 0+18+54, subtracting the former series from the latter, we have for the remainder, 54-2, that is, the last term less the first term, which is evidently as many times the first series (2+6+18)as is expressed by the ratio, less one; hence, if we divide the difference of the extremes (54-2) by the ratio, less 1. (3-1) the quotient will be the sum of all the terms, except the last, and, adding the last term, we shall have the whole amount. Thus, 54-2=52, and 3-1=2; then 52-2= 26, and 54 added, makes 80. Ans. as before.

Hence, when the extremes and ratio are given to find the sum of the series,-Divide the difference of the extremes by the ratio less I, and the quotient, increased by the greater term, will be the answer.

6. If the extremes be 4 and 131072, and the ratio 8. what is the whole amount of the series?

131072 - 4

-+131072=149796. Ans. 8-1

7. What is the sum of the descending series 3, 1, $\frac{1}{3}$, $\frac{1}{4}$, 17, &c. extended to infinity?

It is evident the last term must become 0, or indefinitely near to nothing; therefore, the extremes are 3 and 0, and the ratio 3. Ans. 41.

8. What is the value of the infinite series $1+\frac{1}{2}+\frac{1}{2}+\frac{1}{5}+\frac{1}{5}$ Ans. 13. &c. ?

9. What is the value of the infinite series, $\frac{1}{10}$, $+\frac{1}{100}$ + $\frac{1}{1000}$, $\frac{1}{8}$ c.; or, what is the same, the decimal '11111, &c. continually repeated ? Ans. $\frac{1}{2}$.

11., A gentleman whose daughter was married on a new year's day, gave her $\pounds 1$, promising to tripple it on the first day of each month in the year; to how much did her portion amount?

Here, before finding the amount of the series, we must find the *last term*, as directed in the rule after ex. 1.

Ans. £265720.

The 2 processes of finding the last term, and the amount, may, however, be conveniently reduced to one, thus :---

When the first term, the ratio, and the number of terms, are given, to find the sum or amount of the series;—Raise the ratio to a power whose index is equal to the number of terms, from which subtract 1; divide the remainder by the ratio, less 1, and the quotient, multiplied by the first term, will be the *answer*.

Applying this rule to this last example, 3¹²=531441 and 531441-1

12. A man agrees to serve a farmer forty years, without any other reward than I kernel of corn for the first year, 10 for the second year, and so on, in 10 fold ratio, till the end of the term; what will be the amount of his wages, allowing 1000 kernels to a pint, and supposing he sells his corn for 30 pence per bushel?

13. A gentleman dying, left his estate to his 5 sons, to the youngest £1000, to the second £1500, and ordered that each son should exceed the younger by the ratio of $1\frac{1}{2}$; what was the amount of the estate?

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5 sons, to ordered that ratio of $1\frac{1}{2}$;

Note. Before finding the power of the ratio $1\frac{1}{2}$, it may be reduced to an improper fraction $\implies 3$, or to a decimal, 1'5.

 $\frac{\frac{3}{5}^{5}-1}{\frac{1}{5}^{5}-1} \times 1000 = 13187\frac{1}{2}; \text{ or, } \frac{1}{5}^{5}-1} \times 1000 =$ £13187'50 = £13187 10s, Ans. 1'5-1

Compound Interest by Progression.

¶ **108.** 1. What is the amount of $\pounds 4$ for 5 years, at 6 per cent compound interest ?

We have seen (¶ 86) that compound interest is that which arises from adding the interest to the principal at the close of each year, and, for the next year, casting the interest on that amount, and so on. The amount of $\pounds 1$ for one year is 1'06; if the principal, therefore, be multiplied by 1'06, the product will be its amount for one year; this amount multiplied by 1'06, will give the amount (compound interest) for two years; and this second amount multiplied by 1'06, will give the amount for three years; and so on.

Hence, the several amounts arising from any sum at compound interest, form a geometrical series, of which the principal is the first term; the amount of $\pounds 1$ or $\pounds 1$, &c. at the given rate per cent, is the ratio; the time, in years, is one less than the number of terms; and the last amount is the last term.

The last question may be resolved into this: If the first term be 4, the number of terms 6, and the ratio 1'06, what is the last term?

1'06⁵=1'338, and 1'338×4= \pounds 5'352+. Ans. \pounds 5 7s. 0¹/₂d. Note 1. The powers of the amounts of \pounds 1, at 5 and at 6 per cent, may be taken from the table under ¶ 85. Thus, opposite 5 years under 6 per cent, you find 1'838, &c.

Note 2. The several processes may be conveniently exhibited by the use of letters, thus :—

Let P represent the Principal.

R	"	Ratio or the amount of £1, &c. for 1 yr.
Т	"	Time in years.
A	"	Amount.

When two or more letters are joined together, like a word, they are to be multiplied together. Thus, PR. implies, that the principal is to be multiplied by the ratio. When one letter is placed *above* another, like the index of a power, the first is to be raised to a power, whose index is denoted by the second. Thus RT. implies that the ratio is to be raised to a power whose index shall be equal to the time, that is, the number of years.

2. What is the amount of £40 for 11 years, at 5 per cent compound interest?

RT. \times P=A ; therefore, 1'05¹¹ \times 40=68'4. Ans. £68 8s. 3. What is the amount of $\pounds 6$ for 4 years, at 10 per cent compound interest? Ans. £8 158. 8d.

4. If the amount of a certain sum for 5 years at 6 per cent compound interest, be £5 7s. 01d., what is that sum, or principal?

If the number of terms be 6, the ratio 1'06, and the last term 5'352, what is the first term ?

This question is the reverse of the last; therefore,

A	0.00%	
==	P; or - = 4	. Ans. £
RT.	1'338	

5. What principal, at 10 per cent compound interest, will amount, in 4 years, to $\pounds 8'7846$. Ans. £6.

6. What is the present worth of $\pounds 68$ 8s., due 11 years hence, discounting at the rate of 5 per cent compound in-Ans. £40. terest?

7. At what rate per cent will $\pounds 6$ amount to $\pounds 8'7846$ in 4 years?

If the first term be 6, the last term 8'7846, and the number of terms 5, what is the ratio?

8'7846

- = 1'4641 =the 4th power of $= \mathbf{R}\mathbf{T}$. that is.

the ratio; and then, by extracting the 4th root, we obtain 1'10 for the ratio. Ans. 10 per cent.

8. In what time will £6 amount to £8'7846, at 10 per cent compound interest?

8'7846 $-=\mathbf{R}\mathbf{r}\cdot$ that is, -- =1'4641=1'10^T ; therefore, if P

we divide 1'4641 by 1'10, and then divide the quotient thence arising by 1'10, and so on, till we obtain a quotient that will not contain 1'10, the number of these divisions will Ans. 4 years. be the number of years.

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GEOMETRICAL PROGRESSION.

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the quotient ain a quotient divisions will Ans. 4 years. 9. At 5 per cent compound interest, in what time will £40 amount to £68 Ss. ?

Having found the power of the ratio 1'05, as before, which is 1'71, you may look for this number in the *table* under the given rate, 5 per cent, and against it you will find the number of years. Ans. 11 years.

10. At 6 per cent compound interest, in what time will $\pounds 4$ amount to $\pounds 5$ 7s. $0\frac{1}{2}d$. Ans. 5 years.

Annuities at Compound Interest.

109. It may not be amiss, in this place, briefly to show the application of compound interest, in computing the amount and present worth of *annuities*.

An annuity is a sum payable at regular periods of one year each, either for a certain number of years, or during the life of the pensioner, or for ever.

When annuities, rents, &c. are not paid at the time they become due, they are said to be in arrears.

¹ The sum of all the annuities, rents, &c. remaining unpaid, together with the interest on each, for the time they have remained due, is called the amount.

1. What is the amount of an annual pension of $\pounds 100$, which has remained unpaid 4 years, allowing 6 per cent compound interest?

The last year's pension will be $\pounds 100$, without interest; the last but one will be the amount of $\pounds 100$ for one year; the last but two the amount (compound interest) of $\pounds 100$ for two years, and so on; and the sum of these several amounts will be the answer. We have then a series of amounts, that is, a geometrical series, (¶ 108) to find the sum of all the terms.

If the first term be 100, the number of terms 4, and the ratio 1'06; what is the sum of all the terms?

Consult the rule under \P 107, ex. 11.

Hence, when the annuity, the time, and rate per cent, are given, to find the amount—Raise the ratio (the amount of $\pounds 1$, &c. for one year) to a power denoted by the number of years; from this power subtract 1, then divide the

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GEOMETRICAL PROGRESSION.

remainder by the ratio less 1, and the quotient multiplied by the annuity, will be the amount.

Note. The powers of the amounts, at 5 and 6 per cent up to the 24th, may be taken from the table under ¶ 85.

2. What is the amount of an annuity of $\pounds 50$, it being in arrears 20 years, allowing 5 per cent compound interest? Ans. £1653 5s. 94d.

3: If the annual rent of a house, which is $\pounds 150$, be in arrears 4 years, what is the amount, allowing ten per cent compound interest? Ans. £696 3s.

4. To how much would a salary of $\pounds 500$ per annum amount in 14 years, the money being improved at six per cent compound interest ?----- in 10 years ?----- in 20 years ?

Ans. to the last, £25407 15s.

110. If the annuity is paid in advance, or if it be bought at the beginning of the first year, the sum which ought to be given for it is called the present worth.

5. What is the present worth of an annual pension of $\pounds 100$, to continue for four years, allowing 6 per cent compound interest?

The present worth is evidently a sum which, at six per cent, compound interest, would, in four years, produce an amount equal to the amount of the annuity in arrears the same time.

By the last rule we find the amount = £437'45, and by the directions under ¶ 108, ex. 4, we find the present worth $= \pounds 34651.$ Ans. £346 10s. 44d.

Hence, to find the present worth of any annuity,-First find its amount in arrears for the whole time; this amount, divided by that power of the ratio denoted by the number of years, will give the present worth.

6. What is the present worth of an annual salary of $\pounds 100$ to continue twenty years, allowing five per cent?

Ans. $\pounds 1246$ 4s. $4\frac{3}{4}$ d. The operations under this rule being somewhat tedious, we subjoin a

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GEOMETRICAL PROGRESSION.

TABLE

at multiplied

6 per cent der ¶ 85.), it being in d interest? 653 5s. 9½d. £150, be in ten per cent ns. £696 3s. per annum ed at six per in 20 years?

£25407 15s.

, or if it be sum which orth.

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h, at six per produce an arrears the

"45, and by resent worth 46 10s. 4½d.

uity,—First his amount, the number

ary of $\pounds 100$ 246 4s. $4\frac{3}{4}$ d. hat tedious,

Showing the present worth of £1 or \$1 annuity, at 5 and 6 per co	ent,
compound interest, for any number of years from 1 to 34.	

Years	5 per cent.	6 per cent.	Years	5 per cent.	6 per cent.
1	0'95238	0'94339	18	11'68958	10'8276'
2	1'85941	1'83339	19	12'08532	11415811
3	2'72325	2'67301	20	12'46221	11'46902
4	3'54595	3'4651	21	12'82115	11'76407
5	4'32948	4'21236	22	13'163	12'04158
6	5'07569	4'91732	23	13'48807	12.30338
7	5.78637	5'58238	24	13'79864	12'55035
8	6'46321	6'20979	25	14'09394	12.78335
9	7'10782	6'80169	26	14'37518	13'00316
10	7'72173	7'36008	27	14'64303	13'21053
11	8.30641	7'88687	28	14'89813	13'40616
12	8'86325	8.38384	29	15'14107	13'59072
13	9'39357	8'85268	30	15'37245	13.76483
14	9'89864	9.29498	31	15,59281	13'92908
15	10'37966	9'71225	32	15'80268	14.08398
16 _.	10.83777	10.10589	33	16'00255	14'22917
17	11'27407	10'47726	34	16'1929	14'36613

It is evident that the present worth of $\pounds 2$ annuity is two times as much as that of $\pounds 1$; the present worth of $\pounds 3$ will be three times as much, &c. Hence, to find the present worth of any annuity at 5 or 6 per cent,—Find in this table the present worth of $\pounds 1$ annuity, and multiply it by the given annuity, and the product will be the present worth.

7. What ready money will purchase an annuity of $\pounds 150$, to continue 30 years at 5 per cent compound interest?

The present worth of $\pounds 1$ annuity, by the table, for thirty years, is 15'37245; therefore, $15'37245 \times 150 = \pounds 2305'867 = \pounds 2305 \ 17s. \ 4d. \ Ans.$

8. What is the present worth of a yearly pension of $\pounds 40$, to continue ten years at 6 per cent compound interest? at 5 per cent ?—_____to continue fifteen years ?—____20 years ? ______25 years ?—____34 years ?

Ans. to the last, $\pounds 647$ 14s. $3\frac{3}{4}$ d. When annuities do not commence till a certain period of time has elapsed, or till some particular event has taken place, they are said to be in reversion. 9. What is the present worth of $\pounds 100$ annuity, to be continued four years, but not to commence till two years hence, allowing 6 per cent compound interest?

The present worth is evidently a sum which, at 6 per cent compound interest, would, in two years, produce an amount equal to the present worth of the annuity, were it to commence immediately. By the last rule, we find the present worth of the annuity, to commence immediately, to be £346'51, and by directions under \P 108, ex. 4, we find the present worth of £346'51 for two years to be £308'393. Ans. £308 7s. 104d.

Hence, to find the present worth of any annuity taken in reversion, at compound interest,—First, find the present worth, to commence immediately, and this sum, divided by the power of the ratio, denoted by the time in reversion, will give the answer.

10. What ready money will purchase the reversion of a lease of $\pounds 60$ per annum to continue 6 years, but not to commence till the end of three years, allowing 6 per cent compound interest to the purchaser?

The present worth to commence immediately, we find to 295'039

It is plain, the same result will be obtained by finding the present worth of the annuity, to commence immediately, and to continue to the end of the time, that is 3+6=9 years, and then subtracting from this sum the present worth of the annuity, continuing for the time of the reversion, 3 years. Or, we may find the present worth of $\pounds 1$ for the 2 times by the table, and multiply their difference by the given annuity. Thus, by the table,

The whole time, 9 years=6'80169 The time in reversion, 3 " =2'67301

> Difference, 4'12868 . 60

£247'72080. £247'72080=£247 14s. 4fd. Ans. 11. What is the present worth of a lease of £100, to con-

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247 14s. 43d.

y finding the mmediately, is 3+6=9 resent worth reversion, 3 £1 for the 2 by the given

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80 . 43d. Ans. 100, to continue 20 years, but not to commence till the end of 4 years, allowing 5 per cent?——what, if it be 6 years in reversion? ——8 years?——10 years?——14 years?

¶ **111.** 12. What is the worth of a freehold estate of which the yearly rent is $\pounds 60$, allowing to the purchaser 6 per cent?

In this case, the annuity continues for ever, and the estate is evidently worth a sum of which the yearly interest is equal to the yearly rent of the estate. The principal multiplied by the rate gives the interest; therefore, the interest divided by the rate will give the principal; $60 \div 06 = 1000$. Ans. £1000.

Hence, to find the present worth of an annuity, continuing for ever,—Divide the annuity by the rate per cent, and the quotient will be the present worth.

* Note. The worth will be the same, whether we reckon simple or compound interest; for since a year's interest of the price is the *annuity*, the profits arising from that price can neither be more nor less than the profits arising from the annuity, whether they be employed at simple or compound intere't.

13. What is the worth of £100 annuity, to continue for ever, allowing to the purchaser 4 per cent? — allowing 5 per cent? — 8 per cent? — 10 per cent? — 15 per cent? — 20 per cent? — Ans. to the last, £500.

14. Suppose a freehold estate of $\pounds 60$ per annum, to commence two years hence, be put on sale; what is its value, allowing the purchaser 6 per cent?

Its present worth is a sum which, at 6 per cent compound interest, would in two years produce an amount equal to the worth of the estate *if entered on immediately*.

 $\frac{60}{---} = \pounds 1000 = \text{the worth, if entered on immediately,}$

£1000

and $-----= \pounds 889'996 = \pounds 889$ 19s. 11d. the present worth, 1'06²

The same result may be obtained by subtracting from the worth of the estate, to commence immediately, the present worth of the annuity 60, for two years, the time of *reversion*. 'Thus, by the table, the present worth of $\pounds 1$ for two years is $1'83339 \times 60 = 110'0034 =$ present worth of £60 for two years, and £1000-110'0034 = £889'9966=£889 19s. 11d. Ans. as before.

15. What is the present worth of a perpetual annuity of £100, to commence 6 years hence, allowing the purchaser 5 per cent compound interest? — what, if 8 years in reversion? — 10 years? — 30 years?

Ans. to the last, $\pounds 462$ 15s. $1\frac{1}{4}d$. The foregoing examples in compound interest have been confined to *yearly* payments; if the payments are half-yearly, we take half the principal or annuity, half the rate per cent, and twice the number of years, and work as before, and so for any other part of a year.

QUESTIONS.

1. What is a geometrical progression or series ? 2. What is the ratio? 3. When the first term, the ratio and the number of terms, are given, how do you find the last term? 4. When the extremes and ratio are given, how do you find the sum of all the terms 4 5. When the first term, the ratio, and the number of terms are given, how do you find the amount of the series ? 6. When the ratio is a fraction, how do you proceed? 7. What is compound interest? 8. How does it appear that the amounts arising by compound interest, form a geometrical series ? 9. What is the ratio in compound interest? -- the number of terms ?----- the first term ? ----- the last term ? 10. When the rate, the time and the principal are given, how do you find the amount ?---I1. When A R and T are given, how do you find P? 12. When A P and T are given, how do you find R ? 13. When A P and R are given, how do you find T? 14. What is an annuity? 15. When are annuities said to be in arrears? 16. What is the amount? 17. In a geometrical series, to what is the amount of an annuity equivalent? 18. How do you find the amount of an annuity, at compound interest? 19. What is the present worth of an annuity? ---- how computed at compound interest ?----- how found by the table ? 20. What is understood by the term reversion ' 21. How do you find the present worth of an annuity, taken in reversion? ----- by the table? 22. How do you find the present worth of a freehold estate, or a perpetual annuity ?---- the same taken in reversion ?-----by the table ?

PERMUTATION.

112. Permutation is the method of finding how many different ways the order of any number of things may be varied or changed.

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: worth of £60 '9966—£889

al annuity of the purchaser Sycars in reears?

462 15s. 1⁴d. est have been e half-yearly, rate per cent, before, and so

2. What is the er of terms, are stremes and ra-5. When the n, how do you a fraction, how 8. How does it form a geomeerest ? ---- the m? 10. When lo you find the pu find P ? 12. When A P and annuity? 15. is the amount? n annuity equiy, at compound ty? --- how he table ? 20, do you find the - by the table? tate, or a pery the table ?

finding how f things may 1. Four gentlemen agreed to dine together, so long as they could sit every day in a different order or position; how many days did they dine together ?

Had there been but two of them, a and b, they could sit only in 2 times 1 (1×2=2) different positions, thus, a b, and b a. Had there been three, a b and c, they could sit in 1×2×3=6 different positions; for, beginning the order with a, there will be two positions, viz a b c, and a c b; next beginning with b, there will be two positions, b a c, and b c a; lastly, beginning with c, we have c a b, and c b a, that is, in all, 1×2×3=6 different positions. In the same manner if there be four, the different positions will be 1×2×3×4=24. Ans. 24.

Hence, to find the number of different changes or permutations, of which any number of different things are capable,—Multiply continually together all the terms of the natural series of numbers, from *one* up to the given number, and the last product will be the answer.

2. How many variations may there be in the position of the nine digits? Ans. 362880.

3. A man bought 25 cows, agreeing to pay for them one penny for every different order in which they could all be placed; how much did the cows cost him?

Ans. £64630041847212441600000. 4. A certain church has 8 bells; how many changes may be rung upon them ? Ans. 40320.

MISCELLANEOUS EXAMPLES.

¶ **113.** 1. $\overline{4+6} \times \overline{7-1} = 60$.

A line, or *vinculum*, drawn over several numbers, signifies that the numbers under it are to be taken jointly, or as one whole number

- 2. $9-8+4\times8+4-6$ how many? Ans. 30.
- 3. $7+4-2+3+40\times5$ how many? Ans. 230. $3+6-2\times4-2$
- 4. 2×2 =how many? Ans. $3_{\frac{1}{2}}$.

5. There are 2 numbers; the greater is 25 times 78, and their difference is 9 times 15; their sum and product are

Ans. 3765 is their sum, 3539250 their product. required. 6. What is the difference between thrice five and thirty, rallon, f

and thrice thirty-five? $35+3-5\times3+30=60$, Ans. 7. What is the difference between six dozen dozen, and

Ans. 792. It come t half a dozen dozen ?

8. What number divided by 7 will make 6488?

9. What number multiplied by 6 will make 2058?

10. A gentleman went to sea at 17 years of age; 8 years his pay i after, he had a son born, who died at the age of 35; after he recei whom the father lived twice 20 years; how old was the 25. A Ans. 100 years. bushel, father at his death?

11. What number is that which, being multiplied by 15, peived t e product will be $\frac{3}{4}$? 12. What decimal is that which, being multiplied by 15, 26. H the product will be $\frac{3}{4}$?

'75-15='05, Ans. must be the product will be '75?

13. What is the decimal equivalent to $\frac{1}{35}$? Ans. '0285714

14. What fraction is that, to which if you add ²/₅, the sum 27. H Ans. 18. In excha will be §?

15. What number is that, from which if you take $\frac{2}{5}$, the Note. remainder will be 4?

To what number is that, which being divided by $\frac{3}{4}$, the he same notient will be 21? Ans. $\frac{29}{4}$, the he same $\frac{16}{100}$, which being divided by $\frac{3}{4}$, the he same $\frac{16}{100}$, $\frac{153}{4}$, $\frac{153$ quotient will be 21?

17. What number is that, from which if you take $\frac{2}{5}$ of a exchange itself, the remainder will be 12? Ans. 20.

18. What number is that, to which if you add $\frac{2}{5}$ of $\frac{5}{3}$ of Ans. 12. itself, the whole will be 20?

elf, the whole will be 20? Ans. 12. Tave him 19. What number is that of which 9 is the $\frac{2}{3}$ part? Ans. $13\frac{1}{2}$, how man

20. A farmer carried a load of produce to market; he sold 30. A 780 lbs of pork, at 3d. per lb; 250 lbs of cheese, at 5d. per lb; bartering 154 lbs of butter, at 10d. per lb. In pay he received 60 lbs worth 18 of sugar, at 7d. per lb; 15 gallons of molasses, at 2s. 3d. per the broa gallon ; 1 barrel of mackerel, at 18s. 9d. ; 4 bushels of salt, 30d. : at 6s. 4d. per bushel; and the balance in money; how much Ans. £15 14s. 8d. Lectly ali monéy did he receive?

21. A farmer carried his grain to market, and sold 75 bushels of wheat at 7s. 3d. per bushel ; 64 bushels of rye at 4s. 9d. per bushel; 142 bushels of corn, at 2s. 6d. per bushel. In exchang exchange, he received sundry articles :---3 pieces cloth, each containing 31 yds. at 8s. 9d. per yd.; 2 quintals fish, 11s. 6d. per quintal; 8 hhds. salt, £1 1s. 6d. per hhd. and the balance pushel? in money; how much money did he receive? Ans. £9 14s

22. A will be t 23. B vill it ta 24. A

29. A ls. 10¹/₂d 31. I at 2s. 60 32. 1 32. If

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30, Ans.

88?

2058? ns. '0285714

Ans. 20.

fish, 11s. 6d. d the balance bushel?

their product. 22. A man exchanges 760 gallons of molasses, at 2s. per ve and thirty, gallon, for 661 cwt. of cheese at £1 per cwt.; how much will be the balance in his favor ? Ans. £9 10s. en dozen, and 23. Bought S4 yds. of cloth at 6s. 3d. per yd.; how much did Ans. 792. It come to ? how many bushels of wheat at 7s. 6d. per bushel, will it take to pay for it? Ans. to the last, 70 bushels.

24. A man sold 342lbs of beef at 4d. per lb, and received f age; 8 years his pay in molasses at 2s. per gallon; how many gallons did e of 35; after he receive? Ans. 57 gallons.

old was the 25. A man exchanged 70 bushels of rye at 4s. 6d. per ns. 100 years. pushel, for 40 bushels of wheat at 7s. per bushel, and retiplied by 15, reived the balance in oats at 2s. per bushel; how many $15 = \frac{1}{26}$, Ans. bushels of oats did he receive? Ans. $17\frac{1}{2}$. tiplied by 15, 26. How many bushels of potatoes at 1s. 6d. per bushel,

5='05, Ans. must be given for 32 bushels of barley at 2s. 6d. per bushel? Ans. 534 bushels.

dd 2, the sum 27. How much salt, at \$1'50 per bushel, must be given Ans. $\frac{13}{30}$ in exchange for 15 bushels of oats, at 2s. 3d. per bushel?

bu take 3/2, the Note. It will be recollected that when the price and cost Ans. 2/8.
ded by 3/2, the he same denomination before dividing. Ans. 4/2 bushels. Ans. 15/3.
you take 2/2 of a exchange for 40 yards of cloth at 7s. 6d. per yard?

Ans. $21\frac{9}{77}$ gallons.

add $\frac{2}{5}$ of $\frac{5}{3}$ of 29. A. had 41 cwt. of hops at 30s. per cwt. for which B. Ans. 12. rave him £20 in money, and the rest in prunes at 5d. per lb.; art? Ans. 13¹/₂. how many prunes did A. receive? Ans. 17cwt. 3qrs. 4¹/_b. arket; he sold 30. A. has linen cloth worth 2s. 6d. per yard; but in at 5d. per lb; partering he will have 2s. 9d. per yard; but in eccived 60 lbs worth 18s. 9d. per yard, ready money; at what price ought, at 2s. 3d. per the broadcloth to be rated, in bartering with A.?. ushels of salt, 30d.: 35d.:: 225d.: 262 d. ans. Or, $\frac{35}{36}$ of 225d....£1 y; how much 1s. 10 d. ans. The two operations will be seen to be ex-£15 14s. 8d. actly alike.

sold 75 bush 31. If cloth worth 2s. per yard, cash, be rated in barter rye at 4s.9d. at 2s. 6d., how should wheat, worth 8s. cash, be rated in bushel. In exchange for the cloth? Ans. 10s.

es cloth, each 32. If 4 bushels of corn cost \$2, what is it per bushel?" 32. If 9 bushels of wheat cost £3 7s. 6d. what is that per Ans. 7s. 6d.

Ans. £9 14s 34. If 40 sheep cost £25, what is that per head?

MISCELLANBOUS EXAMPLES.

233

35. If 3 bushels of oats cost 7s. 6d. how much are the

Ans. 2s. 6d for £42 per bushel? 36. If 22 yards of broadcloth cost £21 9s. what is the how mu price per yard? Ans. 198 6d

50. 87. At 2s. 6d. per bushel, how much corn can be bough £59 4s. for 10s. Ans. 4 bushels

38. A man haying $\pounds 25$, would lay it out in sheep, at 12s51. 6d. a-piece, how many can he buy? Ans. 40

39. If 20 cows cost $\pounds75$, what is the price of one cow **52**.

Ans. to the last. £56 5s

, 40. If 7 men consume 24 bs of meat in one week, how much would one man consume in the same time ?----2 men

-5 men ?-----10 men ? Ans. to the last, 347 lbs Note. Let the pupil, also perform these questions by th **5**6. rule of proportion.

days, at 41. If I pay £1 10s. for the use of £25, how much mus I pay for the use of £18 15s. ? Ans £1 2s. 6d and 3 d

42. What premium must I pay for the insurance of m house against loss by fire, at the rate of $\frac{1}{2}$ per cent, that is years an $\frac{1}{2}$ pound for 100 pounds, if my house be valued at £2475 Ans. £12 7s. 6d

43. What will be the insurance, per annum, of a stor and contents, valued at £9876 8s at $1\frac{1}{2}$ per centum ? Ans. £148 2s. 11d

44. What commission must I receive for selling $\pounds 47$ vears a worth of books at 8 per cent? Ans. £38 4s. 94

45. A merchant bought a quantity of goods for £734 for £5 and sold them so as to gain 21 per cent; how much did h gain, and for how much did he sell his goods ?-

Ans. to the last, £888 2s. 944

46. A merchant bought a quantity of goods at Montrea for £500, and paid £43 for their transportation; he sol them so as to gain 24 per cent on the whole cost; for how much did he sell them? Ans. £673 6s. 43d

47. Bought a quantity of books for $\pounds 64$, but for cash discount of 12 per cent was made; what did the books cost Ans. £56 6s. 434

48. Bought a book, the price of which was marked x2s. 6d., but for cash the bookseller will sell it at $33\frac{1}{3}$ pe Ans. 158 cent discount; what is the cash price? gain \pounds

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MISCELLANEOUS EXAMPLES.

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much are the Ans. 2s. 6d for £42; for how much must I sell it to gain 15 per cent? 9s. what is the how much per gallon? Ans. 19s 6d 50. Bought a cask of sugar, containing 740 pounds, for

n can be bough £59 4s.; how must I sell it per pound, to gain 25 per cent? Ans. 4 bushels in sheep, at 12s 51. What is the interest at 6 per cent of £71 0s 43d.

Ans. 40 for 17 months 12 days? Ce of one cow 50. What is the interest at 6 per cent, of £71 0s. 43d. Ans. 40 for 17 months 12 days? Ans. £6 2s. 63d. Ce of one cow 50. What is the interest of £487 0g. 03d for 18 months?

52. What is the interest of \pounds 487 0s. 0³/₄d. for 18 months? Ans. \pounds 43 16s. 7¹/₄d.

53. What is the interest of \$8'50 for 7 months? -Ans. \$'2971.

54. What is the interest of £1000 for 5 days? Ans. 16s. 8d.

55. What is the interest of 10s. for ten years? Ans. 6s.

56. What is the interest of \$84'25 for 15 months and 7 days, at 7 per cent ? Ans. \$7'486+

57. What is the interest of \$154'01 for 2 years, 4 months and 3 days, at 5 per cent? Ans. \$18'032.

58. What sum put to interest at 6 per cent, will in two years and 6 months, amount to \$150? Ans. \$130'434+ Note. See ¶ 79.

59. I owe a man £475 10s. to be paid in 16 months without interest; what is the present worth of that debt, the use of money being worth 6 per cent? Ans. £440 5s. 6 $\frac{1}{2}$ d.

60. What is the present worth of £1000 payable in four years and 2 months, discounting at the rate of 6 per cent? 61. Bought articles to the amount of £500, and sold them for £575, how much was gained ?

What per cent was gained? that is, how many pounds were gained on each $\pounds 100$ laid out? If $\pounds 500$ gain $\pounds 75$, what does $\pounds 100$ gain? Ans. 15 per cent.

62. Bought cloth at £3 10s. per piece, and sold it at £4 5s. per piece; how much was gained per centum ? Ans. 213.

63. A man bought a cask of liquor, containing 126 gallons for £283 10s. and sold it out at the rate of £2 15s. per gallon? how much was his whole gain? how much per gallon? how much per cent?

Ans. His whole gain $\pounds 63$; per gallon 10s. which is $22\frac{2}{3}$ per centum.

64. If £100 gain £6 in 12 months, in what time will it gain £4? \pounds 10? \pounds 14? Ans. to the last, 28 months.
65. In what time will £54 10s. at 6 per cent, gain £2 3s. 74d. Ans. 8 months.

66. Twenty men built a certain bridge in 60 days, but it being carried away in a freshet, it is required how many men can re-build it in 50 days?

days.

days.

50 : 60 : : 20 : 24 men. Ans 67. If a field will feed 7 horses 8 weeks, how long will it feed 28 horses ? Ans. 2 weeks.

men.

68. If a field 20 rods in length must be 8 rods in width to contain an acre, how much in width must be a field 16 rods in length, to contain the same? Ans. 10 rods.

69. If I purchase for a cloak twelve yards of plaid § of a yard wide, how much bocking 1½ yards wide must I buy to line it? Ans. 5 yards.

70. If a man earn £18 15s. in 5 months, how long must he work to earn £115? Ans. 30? months.

71. B. owes C. £540, but B. not being worth so much money, C. agrees to take 15s. on a pound; what sum must C. receive for the debt? Ans. £405.

72. A cistern whose capacity is 40° gallons, is supplied by a pipe which lets in 7 gallons in 5 minutes; but there is a leak in the bottom of the cistern which lets out 2 gallons in 6 minutes. Supposing the cistern empty, in what time would it be filled?

In one minute $\frac{7}{5}$ of a gallon is admitted, but in the same time $\frac{2}{5}$ of a gallon leaks out. Ans. 6 hours 15 minutes.

73. A ship has a leak which will fill it so as to make it sink in ten hours; it has also a pump which will clear it in 15 hours; now if they begin to pump when it begins to leak, in what time will it sink?

In one hour the ship would be $\frac{1}{15}$ filled by the leak, but in the same time it would be $\frac{1}{15}$ emptied by the pump.

Ans. 30 hours.

74. A cistern is supplied by a pipe which will fill it in 40 minutes; how many pipes of the same size will fill it in five minutes? Ans. 8.

75. Suppose I lend a friend \pounds 500 for four months, he promising to do me a like favour; some time afterward, I have need of \pounds 300; how long may I keep it to balance the former favour? Ans. 63 months.

76. S sions su part, tha 77. I be wort value of 78. I among than 3

> 79. 1 water m gallon? Note. £27 10 80. 4 way at after hin gain in thief?

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cent, gain £2 Ans. 8 months. 60 days, but it red how many

4 men. Ans ow long will it Ans. 2 weeks. rods in width t be a field 16 Ans. 10 rods. of plaid § of a must I buy to Ans. 5 yards. now long must . 30% months. orth so much hat sum must Ans. £405. is, is supplied ; but there is out 2 gallons in what time

t in the same s 15 minutes as to make it vill clear it in begins to leak,

the leak, but ne pump.

ns. 30 hours. will fill it in will fill it in Ans. 8.

w months, he afterward, I balance the s. $6\frac{2}{3}$ months.

76. Suppose 800 soldiers were in a garrison with provisions sufficient for 2 months; how many soldiers must depart, that the provisions may serve them 5 months? Ans, 480. 77. If my horse and saddle are worth £21, and my horse

be worth six times as much as my saddle, pray what is the value of my horse? Ans. £18.

78. Bought 45 barrels of beef at 17s. 6d. per barrel, among which are 16 barrels whereof 4 are worth no more than 3 of the others; how much must I pay?

Ans. £35 17s. 6d. 79. Bought 126 gallons of rum for £27 10s. how much water must be added to reduce the first cost to 3s. 9d. pergallon ?

Note. If 3s. 9d. buy one gallon, how many gallons will £27 10s. buy? • Ans. 203 gallons.

80. A thief having 24 miles start of the officer, holds his way at the rate of 6 miles an hour; the officer pressing on after him at the rate of 8 miles an hour, how much does he gain in one hour? how long before he will overtake the thief? Ans. 12 hours.

81. A hare starts 12 rods before a hound, but is not perceived by him till she has been up $1\frac{1}{4}$ minutes; she scuds away at the rate of 36 rods a minute, and the dog, on view, makes after at the rate of 40 rods a minute; how long will the course hold, and what distance will the dog run?

Ans. 141 minutes, and he will run 570 rods. 82. The hour and minute hands of a watch are exactly together at 12 o'clock; when are they next together?

In 1 hour the minute hand passes over 12 spaces, and the hour hand over one space; that is, the minute hand gains upon the hour hand eleven spaces in one hour; and it must gain twelve spaces to coincide with it. Ans. 1h. 5m. 27_{3}^{2} rs.

83. There is an island 20 miles in circumference, and 3 men start together to travel the same way about it; A. goes two miles per hour, B. four miles per hour, and C. six miles per hour; in what time will they come together again ?

Ans. 10 hours. 84. There is an island 20 miles in circumference, and two men start together to travel round it; A. travels two miles per hour, and B. six miles per hour; how long before they will again come together?

¶ 113 113.

B. gains 4 miles per hour, and must gain twenty miles thearn to overtake A.; A. and B. will therefore be together once in ach? Ans.

every five hours. 85. In a river, supposing two boats start at the same 2 learn time from places 300 miles apart; the one proceeding up 93. A stream is retarded by the current two miles per hour, while mother, that moving down stream is accelerated the same; if both geese;" be propelled by a steam engine which would move them addition miles per hour in still water, how far from each startin have, an place will the boats meet ? many ha

Ans. 1124 miles from the lower place, and 1874 mile from the upper place.

86. A man bought a pipe (126 gallons) of wine for $\pounds 275$ he wishes to fill 10 bottles, 4 of which contain two quarts 1 pears, and 6 of them 3 pints each, and to sell the remainder so a how ma to make 30 per cent on the first cost; at what rate per gal Ans. £5'936+ 1 red, a lon must he sell it?

87. Thomas sold 150 pine apples at 1s. 3d. apiece, and ed; how received as much money as Harry received for a certain number of water-melons at 9d. apiece; how much money the same did each receive, and how many melons had Harry?

Ans. £9 7s. 6d. and 250 melons.

88. The third part of an army was killed, the fourth part taken prisoners, and 1000 fled, how many were in this army!

This and the 18 following questions are usually wrough by a rule called *Position*, but they are more easily solved on general principles. Thus, $\frac{1}{3} + \frac{1}{4} = \frac{7}{12}$ of the army; there fore, 1000 is $\frac{5}{12}$ of the whole number of men; and if $\frac{5}{12}$ be 1000, how much is 12 twelfths, or the whole?

Ans. 24000 men

89. A farmer being asked how many sheep he had, and wered that he had them in 5 fields; in the first were $\frac{1}{4}$ of his flock, in the second $\frac{1}{6}$, in the third $\frac{1}{6}$ in the fourth $\frac{1}{16}$ and in the fifth 450; how many had he? Ans. 1200.

90. There is a pole, $\frac{1}{2}$ of which stands in the mud, $\frac{1}{2}$ in the water, and the rest of it out of the water; required the part out of the water. Ans. 12.

91. If a pole be $\frac{1}{3}$ in the mud, $\frac{3}{5}$ in the water, and 6 feet out of the water, what is the length of the pole? Ans. 90 feet.

92. The amount of a certain school is as follows: $\frac{1}{15}$ of the pupils study grammar, $\frac{2}{3}$ geography, $\frac{3}{10}$ arithmetic, $\frac{3}{24}$

97. W the sum 93. V the sum 84 =99. J and 3 o much? The 24 tin

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MISCELLANEOUS EXAMPLES.

twenty miles thearn to write, and 9 learn to read; what is the number of gether once in ach?

Ans. 5 in grammer, 30 in geography, 24 in arithmetic; rt at the same 12 learn to write, and 9 learn to read.

proceeding up 93. A man, driving his geese to market, was met by per hour, while nother, who said, "Good morrow, sit, with your hundred e same ; if both geese ;" says he, "I have not a hundred ; but if I had, in d move them addition to my present number, one half as many as I now each startinghave, and 22 geese more, I should have a hundred :" how

many had he?

and 1874 miles

100-2 $\frac{1}{2}$ is what part of his present number?

Harry ?

rd 250 melons. the fourth part e in this army! sually wrough e easily solved e army; there ; and if 5 be

3. 24000 men p he had, ans rst were 1 of the fourth $\frac{1}{12}$ Ans. 1200.

the mud, $\frac{1}{2}$ in ; required the Ans. 12.

er, and 6 feet Ans. 90 feet. ollows : 15 of rithmetic, 2

Ans. He had 65 geese.

wine for $\pounds 275$ 94. In an orchard of fruit trees, $\frac{1}{2}$ of them bear apples, ain two quarts 1 pears, 1 plums, 60 of them peaches, and 40, cherries; emainder so a how many trees does the orchard contain? Ans. 1200. at rate per gale 95. In a certain village, $\frac{1}{2}$ of the houses are painted white $1ns. \pounds 5'936+, \frac{1}{4}$ red, and $\frac{1}{4}$ yeld v, 3 are painted green, and 7 are unpaint-Bd. apiece, and ed; how many areas in the village? Ans. 120.

d for a certain 96. Seven eighths of a certain number exceed four fifths of v much money the same number by 6; required the number.

 $\frac{7}{4} - \frac{4}{5} = \frac{3}{10}$; consequently, 6 is $\frac{3}{40}$ of the required num-Ans. 80. ber.

97. What number is that, to which if $\frac{1}{2}$ of itself be added, Ans. 25. the sum will be 30?

93. What number is that to which if its 1 and 1 be added, the sum will be 84?

 $84 = 1 + \frac{1}{2} + \frac{1}{4} = \frac{1}{4}$ times the required number. Ans. 48. 99. What number is that, which, being increased by $\frac{2}{3}$ and $\frac{3}{2}$ of itself, and by 22 more, will be made 3 times as much?

The number, being taken 1, 3, and 5 times, will make 2_{15}^{4} times and 22 is evidently what that wants of 3 times, Ans. 30.

100. What number is that, which being increased by $\frac{2}{5}$, $\frac{3}{4}$ and $\frac{5}{4}$ of itself, the sum will be $234\frac{3}{4}$? Ans. 90.

101. B, C, and D; talking of their ages, C said his age was once and a half the age of B, and D said his age was twice and oné tenth the age of both, and that the sum of their ages was 93; what was the age of each?

Ans. B 12 years, C 18 years, D 63 years old. 102. A schoolmaster being asked how many scholars he 244

had, said, "If I had as many more as I now have, 2 as many, ½ as many, ¼ and ¼ as many, I should then have 435;" what was the number of his pupils? Ans. 120.

103. B and C commenced trade with equal sums of money; B gained a sum equal to $\frac{1}{5}$ of his whole stock, and C lost $\pounds 200$; then B.'s money was double that of C's; what was the stock of each?

By the condition of this question, one half of $\frac{6}{5}$, that is, $\frac{1}{2}$ of the stock, is equal to $\frac{1}{2}$ of the stock, less $\pounds 200$; consequently, $\pounds 200$ is $\frac{2}{3}$ of the stock. Ans. £500.

104. A man was hired 50 days on these conditions,--that for every day he worked, he should receive 3s. 9d., and for every day he was idle, he should forfeit 1s. 3d. : at the expiration of the time, he received $\pounds 2$ 17s. 6d., how many days did he work, and how many was he idle?

Had he worked every day, his wages would have been 3s. 9d. $\times 50 = \pounds 9$ 7s. 6d. that is $\pounds 2$ 10s. more than he received ; but every day he was idle lessened his wages 3s. 9d,+1s. 3d.=5s.; consequently he was idle 10 days.

Ans. He wrought 40, and was idle 10 days. 105. B and C have the same income; B saves $\frac{1}{2}$ of his; but C, by spending £30 per annum more than B, at the end of 8 years finds himself $\pounds 40$ in debt; what is their income, aud what does each spend per annum?

Ans. Their income, £200 per annum; B spends £175, and C £205 per annum.

106. A man, lying at the point of death, left his three sons his property; to $B \frac{1}{2}$ wanting £20, to $C \frac{1}{4}$; and to D the remainder, which was $\pounds 10$ less than the share of B; what was each one's share? Ans. £80, £50, and £70.

107. There is a fish, whose head is 4 feet long; his tail is as long as his head and half the length of his body, and his body is as long as his head and tail; what is the length of the fish?

The pupil will perceive that the length of the body is 1 the length of the fish. Ans. 32 feet.

108. B can do a certain piece of work in 4 days, and C can do the same work in 3 days; in what time would both working together, perform it? Ans. 14 days.

109. Three persons can perform a certain piece of work in the following manner: B and C can do it in 4 days, C

and D they all 110. do it in 111. his two proport per cen arrive a elder £ 112.

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he body is $\frac{1}{2}$ Ans. 32 feet. days, and C would both Ins. 14 days. ece of work n 4 days, C

MISCELLANEOUS EXAMPLES.

and **D** in 6 days, and **B** and **D** in 5 days: in what time can they all do it together? Ans. $3\frac{2}{37}$ days.

110. B and C can do a piece of work in 5 days; B can do it in 7 days; in how many days can C do it? Ans. 171.

111. A man died, leaving £1000 to be divided between his two sons, one 14 and the other 18 years of age, in such proportion that the share of each, being put to interest at 6 per cent, should amount to the same sum when they should arrive at the age of 21; what did each receive? Ans. The elder £546 3s. $0\frac{3}{4}d.+$; the younger £453 16s. 11d.

112. A house being let upon a lease of five years, at \pounds 15 per annum, and the rent being in arrear for the whole time, what is the sum due at the end of the term, simple interest being allowed at 6 per cent; Ans. \pounds 84.

113. If three dozen pair of gloves be equal in value to 40 yards of calico, and 100 yards of calico to three pieces of satinet of 30 yards each, and the satinet be worth 2s. 6d. per yard, how many pair of gloves can be bought for 20s. ? Ans. 8 pair.

114. B. C. and D., would divide $\pounds 100$ between them, so that C. may have $\pounds 3$ more than B. and D. $\pounds 4$ more than C; how much must each man have?

116. A man would draw off 30 gallons of wine into one pint and two pint bottles, of each an equal number; how many bottles of each kind will it take to contain the thirty gallons? Ans. 80 of each.

117. A merchant has canisters, some holding 5 pounds, some 7 pounds, and some 12 pounds; how many, of each an equal number, can be filled out of 12 cwt. 3 qrs. 12 lbs. of tea? Ans. 60.

118. If 18 grains of silver make a thimble, and 12 pwts. make a tea-spoon, how many, of each an equal number, can be made from 15 oz. 6 pwts. of silver ? Ans. 24 of each.

119. Let sixty pence be divided among three boys in such a manner that, as often as the first has three, the second shall have five, and the third seven pence; how many pence will each receive? Ans. 12, 20 and 23 pence.

120. A gentleman having fifty shillings to pay among his labourers for a day's work, would give to every boy 6d., to every woman 8d., and to every man 16d.; the number of boys, women and men was the same; I demand the number of each? $\mathcal{A}ns, 20.$

121. A gentleman had ± 7 17s. 6d. to pay among his laborers: to every boy he gave 6d., to every woman 8d., and to every man 16d.; and there were for every boy three women, for every woman two men; 1 demand the number of each? Ans. 15 boys, 45 women, and 90 men.

122. A farmer bought a sheep, a cow, and a yoke of oxen for £20 12s. 6d.; he gave for the cow 8 times as much as for the sheep, and for the oxen three times as much as for the cow; how much did he give for each? Ans. For the sheep, 12s. 6d. the cow £5, and the oxen £15.

123. There was a farm of which B. owned $\frac{2}{7}$, and C. $\frac{12}{27}$; the farm was sold for $\pounds 441$; what was each one's share of the money ? Ans. B.'s $\pounds 126$, and C.'s $\pounds 315$.

12.4. Four men traded together on a capital of £3000, of which B. put in $\frac{1}{2}$, C. $\frac{1}{2}$, D. $\frac{1}{6}$, and E. $\frac{1}{12}$; at the end of 3 years they had gained £2364; what was each one's share of the gain? Ans. B.'s £1182, C.'s £591, D.'s £394, E.'s £197.

125. Three merchants companied; B. furnished $\frac{2}{5}$ of the capital, C. $\frac{2}{5}$, and D. the rest; they gain $\pounds 1250$; what part of the capital did D furnish, and what is each one's share of the gain?

Ans. D. furnished $\frac{2}{30}$ of the capital; and B.'s share of the gain was £500, C.'s £468 15s., and D.'s £281 5s.

126. B, C. and D. traded in company; B. put in £125, C. £87 10s., and D. 120 yards of cloth; they gained £83 2s. 6d., of which D.'s share was £30; what was the value of D's cloth per yard, and what was B, and C.'s share of the gain? 600 1200 48

Note. D.'s gain being £30, is _______ 16624

whole gain; hence the gain of **B**, and \vec{C} , is readily found; also the price at w b D.'s cloth was valued per yard.

Ans. D.'s cloth pe ard, $\pounds 1$, B.'s share of the gain, $\pounds 31$ 5s., C.'s share, $\pounds 21$ 1. 6d.

127. Three gar eners, B. C. and D. having bought a giece of ground, f ad the profits of it amount to \pounds 120 per

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17, and C. $\frac{1}{2}$; one's share of ind C.'s £315. al of £3000, of at the end of 3 one's share of 394, E.'s £197. nished $\frac{2}{5}$ of the 50; what part th one's share

's share of the 81 5s.

the gain, £31

ing bought a to £120 per

annum. Now the sum of money which they laid down was in such proportion, that, as often as B paid $\pounds 5$, C. paid $\pounds 7$, and as often as C. paid $\pounds 4$, D. paid $\pounds 6$; I demand how much each man must have per annum of the gain?

Note. By the question, so often as B paid £5, D paid \$ of £7. Ans. B. £26 13s. 4d., C. £37 6s. 8d., D. £56.

128. A gentleman divided his fortune among his sons, giving B. $\pounds 9$ as often as C. $\pounds 5$, and D. $\pounds 3$ as $\pounds 7$ as C. $\pounds 7$; D.'s dividend was $1537\frac{1}{6}$; to what did the ...nole estate amount? Ans. $\pounds 11583$ 8s. 10d.

129. B. and C. undertake a piece of work for \pounds 13 10s., on which B. employed 3 hands 5 days, and C. employed 7 hands 3 days; what part of the work was done by B., and what part by C.? what was each one's share of the money?

Ans. B. $\frac{5}{12}$ and C $\frac{7}{12}$; B.'s money £5 12s. 6d, C.'s £7 17s. 6d.

130. B. and C. trade in company for one year only; on the 1st of January B. put in ± 300 , but C. could not put any money into the stock until the 1st of April; what did he then put in to have an equal share with B. at the end of the year? Ans. $\pounds 400$.

131. B. C. D. and E. spent 35s. at a reckoning, and being a little dipped, agreed that B. should pay $\frac{2}{3}$, C. $\frac{1}{2}$, D. $\frac{1}{3}$, and E. $\frac{1}{4}$; what did each pay in this proportion?

Ans. B. 13s. 4d., C. 10s., D. 6s. 8d. and E. 5s. 132. There are 3 horses belonging to 3 men, employed to draw a load of plaister from Montreal to Stanstead, for £6 12s. 2d. B. and C.'s horses together are supposed to do $\frac{3}{4}$ of the work, B. and D.'s $\frac{9}{10}$, C. and D.'s $\frac{13}{23}$; they are to be paid proportionally; what is each one's share of the money? Ans. $\begin{cases} B.'s \pm 2 \ 17s. 6d. (=\frac{12}{23}) \\ C.'s \ 1 \ 8s. 9d. (=\frac{5}{23}) \\ D.'s \ 2 \ 6s. 0d. (=\frac{2}{23}) \end{cases}$

Proof. £6 12s. 3d. 133. A person who was possessed of $\frac{2}{5}$ of a vessel, sold $\frac{5}{5}$ of his share for £375; what was the vessel worth ?

Ans. £1500.

134. A gay fellow soon got the better of $\frac{2}{7}$ of his fortune; he then gave £1500 for a commission, and his profusion continued till he had; but £450. left, which he found to be:

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just $\frac{3}{2}$ of his money after he : ad purchased his commission ; what was his fortune at first? Ans. £3780.

135. A younger brother received £1569, which was just T_2 of his elder brother's fortune, and 53 times the elder brother's fortune was § as much again as the father was worth; what was the value of his estate?

Ans. £19165 14s. 33d.

136. A gentleman left his son a fortune, $\frac{1}{16}$ of which he spent in three months; $\frac{3}{4}$ of $\frac{1}{6}$ of the remainder lasted him 9 months longer, when he had only £537 left; what was the sum bequeathed him by his father? Ans. £2082 18s. $2\tau^2_r$ d.

137. A cannon ball, at the first discharge, flies about a mile in 8 seconds; at this "rate, how long would a ball be in passing from the earth to the sun, it being 95173000 miles distant? Ans. 24 years, 46 days, 7⁵H. 33 min. 20 sec.

138. A general, disposing his army into a square battalion, found he had 231 over and above, but inc ing each side with one soldier, he wanted forty-four to fill up the square; of how many men did his army consist? Ans. 19000.

139. B. and C. cleared by an adventure at sea, 45 guiners, which was £35 per cent upon the money advanced, and with which they agreed to purchase a genteel horse and carriage, whereof they were to have the use in proportion to the sums adventured, which was found to be 11 to B. as often as 8 to C[•]; what money did each adventure?

Ans. B. £104 4s. $2\frac{1}{19}$ d., C £75 15s. $9\frac{1}{19}$ d. 140. Tubes may be made of gold, weighing not more than at the rate of $\frac{1}{1625}$ of a grain per foot; what would be the weight of such a tube which would extend across the Atlantic from Quebec to London, estimating the distance at 3000 miles? Ans. 1 lb 8 oz. 6 pwts. $3\frac{1}{19}$ grs.

141. A military officer drew up his soldiers in rank and file, having the number in rank and file equal; on being reinforced with three times his first number of men, he placed them all in the same form, and then the number in rank and file was just double what it was at first; he was again reinforced with three times his whole number of men, and after placing them all in the same form as at first, his number in rank and file was 40 men each; how many men had he at first? Ans. 100 men.

142. Supposing a man to stand 80 feet from a steeple,

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and tha 100 feet high ab of the s of the s

143. east, at south, a apart w 24 hour 144. rods; w

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would be cross the distance $3\frac{9}{1^3}$ grs. rank and being rene placed in rank vas again nen, and his nummen had 00 men. steeple, MISCELLANEOUS EXAMPLES.

and that a line reaching from the belfry to the man is just 100 feet in length, the top of the spire is three times as high above the ground as the steeple is; what is thé height of the spire ?/and the length of a line reaching from the top of the spire to the man? See \P 103.

Ans. to the last, 197 feet nearly. 143. Two ships sail from the same port; one sails directly east, at the rate of 10 miles an hour, and the other directly south, at the rate of $7\frac{1}{2}$ miles an hour; how many miles apart will they be at the end of 1 hour? —2 hours? 24 hours? —3 days? Ans. to last, 900 miles.

144. There is a square field, each side of which is 50 rods; what is the distance between opposite corners?

Ans. 76'71+rcds.

145. What is the area of a square field, of which the opposite corners are 70'71 rods apart? and what is the length of each side? Ans. to last, 50 rods nearly.

146. There is an oblong field, 20 rods wide, and the distance of the opposite corners is 33½ rods; what is the length of the field !-----its area !

Ans. Length $26\frac{2}{3}$ rods; area 3 acres, 1 rood, $13\frac{1}{3}$ rods. 147. There is a room 18 feet square; how many yards of carpeting, 1 yard wide, will be required to cover the floor of it? $18^2=324$ feet=36 yards. Ans.

148. If the floor of a square room contain 36 square yds. how many feet does it measure on each side ?

Ans. 18 feet.

When one side of a square is given, how do you find its area or superficial contents?

When the area or superficial contents of a square is given, how do you find *one side*?

149. If an oblong piece of ground be 80 rods long and 20 rods wide, what is its area ?

 $\begin{array}{c|c}
\mathbf{D} & \mathbf{C} \\
\vdots & \vdots & \vdots \\
\mathbf{E} & \mathbf{A} & \mathbf{F} & \mathbf{B}
\end{array}$

Note.—A parallelogram, or oblong, has its opposite sides equal and parallel, but the adjacent sides unequal. Thus, A. B. C. D. is a parallelogram, and also E. F. C. D. and it is easy to see that the contents of both are equal.

Ans. 1600 rods=10 acres.

150. What is the length of an oblong, or parallelogram, whose area is ten acres, and whose breadth is 20 rods?

Ans. 80 rods.

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151. If the area be ten acres, and the length 80 rods, what is the other side ?

When the length and breadth are given, how do you find the area of an oblong or parallelogram?

When the area and one side are given, how do you find the other side ?

152. If a board be 18 inches wide at one end, and ten inches wide at the other, what is the mean or average width of the board? Ans. 14 inches.

When the greatest and least width are given, how do you find the mean width?

153. How many square feet in a board 16 feet long, 1'8 feet wide at one end, and 1'3 at the other?

1'8+1'3

Mean width, ---=1'55; and $1'55 \times 16 = 24'8$ feet, Ans. 2

154. What is the number of square feet in a board 20 feet long, 2 feet wide at one end, and running to a point at the other?

How do you find the contents of a straight edged board, when one end is wider than the other ?

If the length be in feet, and the breadth in feet, in what denomination will the product be?

If the length be feet and the breadth inches, what parts of a foot will be the product?

155. There is an oblong field, 40 rods long and 20 rods wide; if a straight line be drawn from one corner to the opposite corner, it will be divided into two equal right-angled triangles; what is the area of each?

Ans. 400 square rods=2 acres 2 roods. 156. What is the area of a triangle, of which the base is 30 rods, and the perpendicular 10 rods? Ans. 150 rods.

157. If the area be 150 rods and the base 30 rods, what is the perpendicular ? Ans. 10 rods.

158. If the perpendicular be 10 rods, and the area 150 rods, what is the base? Ans. 30 rods.

When the *legs* (the base and perpendicular) of a rightangled triangle are given, how do you find its area? Wh

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s 2 roods. the base is 150 rods. ods, what s. 10 rods. area 150 s. 30 rods. of a righta? ¶ 113.

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MISCELLANEOUS EXAMPLES.

When the area and one of the legs are given, how do you find the other leg?

Note. Any triangle may be divided into two right-angled triangles, by drawing a perpendicular from one corner to the opposite side, as may be seen by the annexed figure :

Here, A.B.C. is a triangle, divided into two right-angled triangles, A. d C. and d B. C.; therefore, the whole base A. B. multiplied by one half the perpendicular, d C., will give the area A of the whole. If A. B.=60 feet, and d C=16 feet, what is the area ?

Ans. 480 feet.

159. There is a triangle, each side of which is 10 feet; what is the length of a perpendicular from one angle to its opposite side? and what is the area of the triangle?

Note. It is plain the perpendicular will divide the opposite side into two equal parts.

Ans. Perpendicular, S'66+feet; area, 43'3+feet. 160. What is the solid contents of a cube measuring six feet on each side? Ans. 216 feet.

When one side of a cube is given, how do you find its solid contents ?

When the solid contents of a cube are given, how do you find one side of it ?

161. How many cubic inches in a brick which is 8 inches long, 4 inches wide, and 2 inches thick? ——in 2 bricks?

163. How many bricks will it take to build a wall 40 ft. in length, 12 feet high and 2 feet thick ? Ans. 25920.

164. If a wall be 150 bricks,=100 feet in length, and 4 bricks,=16 inches in thickness, how many bricks will lay one course? -2 courses? -10 courses? If the wall be 48 courses,=8 feet high, how many bricks will build it? $150 \times 4 = 600$, and $600 \times 48 = 28800$, Ans.

165. The river Po is 1000 feet broad, and 10 feet deep, and it runs at the rate of 4 miles an hour; in what time will it discharge a cubic mile of water (reckoning 5000 feet to the mile) into the sea? Ans. 26 days, 1 hour.

166. If the country which supplies the river Po with water be 380 miles long, and 120 broad, and the whole land upon the surface of the earth be 62,700,000 square miles, and if the quantity of water discharged by the rivers into the sea be everywhere proportional to the extent of land by which the rivers are supplied, how many times greater than the Po will the whole amount of the rivers be?

Ans. 1375 times.

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167. Upon the same supposition, what quantity of water, altogether, will be discharged by all the rivers into the sea in a year, or 365 days? Ans. 19272 cubic miles.

168. If the proportion of the sea on the surface of the earth to that of land be as $10\frac{1}{2}$ to 5, and the mean depth of the sea be a quarter of a mile; how many years would it take, if the ocean were empty, to fill it by the rivers running at the present rate? Ans. 1708 years, 17 days, 12 hours.

Ans. 2109'375 lbs. weight on a square foot.

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10249980468750000000 " " of whole atmosphere. 170. If a circle be 14 feet in diameter, what is its circumference ?

- Note. It is found by calculation, that the circumference of a circle measures about 34 times as much as its diameter, or more accurately, in decimals, 3'14159 times.

Ans. 44 feet.

171. If a wheel measure 4 feet across from side to side, how many feet around it? Ans. 124,

172. If the diameter of a circular pond be 147 feet, what is its circumference ? Ans. 462 feet.

173. What is the diameter of a circle whose circumference is 462 feet? Ans. 147 feet. 174. side to

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ns. 44 feet. ide to side, Ans. 124, 7 feet, what s. 462 feet. circumfers. 147 feet. 174. If the distance through the centre of the earth, from side to side, be 7911 miles, how many miles around it?

7911×3'14159=24853 square miles, nearly. Ans.

175. What is the area or contents of a circle whose diameter is 7 feet, and its circumference 22 feet ?

Note. The area of a circle may be found by multiplying half the diameter into half the circumference.

Ans. 38½ square feet. 176. What is the area of a circle whose circumference is 176 rods? Ans. 2464 rods.

177. If a circle is drawn within a square, containing one square rod, what is the area of this circle?

Note. The diameter of the circle being one rod, the circumference will be 3'14159,

Ans. '7854 of a square rod, nearly. Hence, if we square the diameter of any circle, and multiply the square by '7854, the product will be the area of the circle.

178. What is the area of a circle whose diameter is ten rods? $10^2 \times '7854 = 78'54$. Ans. 78'54 rods.

179. How many square inches of leather will cover a ball 3½ inches in diameter?

Note. The area of a globe or ball is 4 times as much as the area of a circle of the same diameter, and may be found, therefore, by multiplying the whole circumference into the whole diameter. Ans. 38½ square inches.

180. What is the number of square miles on the surface of the earth, supposing its diameter 7911 miles?

7911×24853=196,612,083, Ans. 181. How many solid inches in a ball 7 inches in diameter?

Note. The solid contents of a globe are found by multiplying its area by $\frac{1}{2}$ part of its diameter.

Ans. 1793 solid inches.

182. What is the number of cubic miles in the earth, supposing its diameter as above?

Ans. 259,223,031,435 miles. 183. What is the capacity, in cubic inches, of a hollow globe 20 inches in diameter, and how much wine will it contain, one gallon being 231 cubic inches?

Ans. 4188'8-cubic inches, and 18'13+gallons.

184. There is a round log, all the way of a bigness ; the areas of the circular ends of it are each 3 square feet; how adding 2 many solid feet does one foot in length of this log contain? tenths, -2 feet in length ?-----3 feet ?-----10 feet ? A solid of ters, to this form is called a cykinder. to a cyl

How do you find the solid content of a cylinder, when the area of one end and the length are given?

185. What is the solid content of a round stick 20 feet and that long and 7 inches through, that is, the ends being 7 inches in diameter?

Find the area of one end, as before taught, and multiply it by the length. . . 1 Ans. 5'347+cubic feet.

If you multiply square inches by inches in length, what parts of a foot will the product be ?----- if square inches by feet in length, what part?

186. A Winchester bushel is 18'5 inches in diameter, and Sinches deep; how many cubic inches does it contain? Ans. 2150'4+.

It is plain, from the above, that the solid content of all bodies, which are of uniform bigness throughout, whatever may be the form of the ends, is found by multiplying the area of one end into its height or length.

Solids which decrease gradually from the base till they come to a point, are generally called Pyramids. If the base be a square, it is called a square pyramid; if a triangle, a priangular pyramid; if a circle, a circular pyramid or a conc. The point at the top of a pyramid is called the vertex, and a line, drawn from the *vertex* perpendicular to the *base*, is called the *perpendicular height* of the pyramid.

The solid content of any pyramid may be found by multiplying the area of the base by $\frac{1}{3}$ of the perpendicular height.

187. What is the solid content of a pyramid whose base is 4 feet square, and the perpendicular height 9 feet?

 $4^{2} \times = 48.$ Ans. 48 feet. 188: There is a cone, whose height is 27 feet, and whose base is 7 feet in diameter; what is its content?

Ans. 346 ½ feet.

189. There is a cask, whose head diameter is 25 inches, bung diameter 31 inches, and whose length is 36 inches; how many wine gallons does it contain? —— how many •*beer gallons?

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Multiply multiply and poin tent in , In the the head 25 in.+4

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346 J feet. 25 inches, 36 inches; how many

Note. The mean diameter of the cask may be found by re feet; how adding 2 thirds, or, if the staves be but a little curving, 6 log contain? tenths, of the difference between the head and bung diame-A' solid of ters, to the head diameter. The cask will then be reduced to a cylinder.

> Now, if the square of the mean diameter be multiplied by '7854, (ex. 177) the product will be the area of one end, and that, multiplied by the length, in inches, will give the solid content, in cubic inches, (ex. 185,) which, divided by

231, (note to table, wine meas.) will give the content in wine gallons, and, divided by 282, (note to table, beer meas.) will give the content in ale or beer measure.

In this process, we see that the square of the mean diameter will be multiplied by '7854, and divided, for wine gallons, by 231. Hence we may contract the operation by only multiplying by their quotient, $\frac{7854}{231} = 0034$) that is, by '0034 (or by 34, pointing off 4 figures from the product for decimals.)" For the same reason we may, for beer gallons, multiply by $(\frac{7.854}{282} \pm 0028)$, nearly) '0028, &c.

Hence this concise RULE for guaging or measuring casks: Multiply the square of the mean diameter by the length; multiply this product by 34, for wine, or by 28 for beer, and pointing off four decimals, the product will be the content in gallons and decimals of a gallon.

In the above example, the bung diameter, 31 in.—25 in. the head diameter=6 in. difference, and $\frac{2}{3}$ of 6=4 inches; 25 in. +4 in. =29 in. mean diameter.

Then $29^2 = 341$, and 841×36 in. = 30276.

(30276×34=1029384. Ans. 102'9384 wine gals. Then,) 30726×28=847728. Ans. 84'2728 beer gals.

190. How many wine gallons in a cask whose bung diameter is 36 inches, head diameter 27 inches, and length 45 inches? Ans. 166'617.

191. There is a lever 10 feet long, and the fulcrum, or prop, on which it turns is 2 feet from one end; how many pounds weight at the end, 2 feet from the prop, will be balanced by a power of 42 pounds at the other end, 8 feet from the prop.

Note. In turning around the prop, the end of the lever 8 feet from the prop will evidently pass over a space of eight inches, while the end 2 feet from the prop passes over a space of 2 inches. Now, it is a fundamental principle in mechanics, that the *weight* and *power* will exactly balance each other, when they are *inversely* as the spaces they pass over. Hence, in this example, 2 pounds, 8 feet from the prop, will balance 8 pounds 2 feet from the prop; therefore if we *divide* the distance of the *power* from the prop by the distance of the weight from the prop, the quotient will always express the *ratio* of the weight to the *power*; $\frac{9}{2}$ =4, that is, the weight will be four times as much as the power, 42×4 =168. Ans. 168 lbs.

192. Supposing the lever as above, what power would it require to raise 1000 pounds? Ans. ${}^{100}_{4}$ ==250 lbs.

193. If the weight to be raised be 5 times as much as the power to be applied, and the distance of the weight from the prop be 4 feet, how far from the prop must the power be applied? Ans. 20 feet.

194. If the greater distance be 40 feet, and the less half of a foot, and the power 175 fbs., what is the weight?

Ans. 14000 pounds.

195. Two men carry a kettle weighing 200 pounds; the kettle is suspended on a pole, the bale being 2 feet 6 inches from the hands of one, and 3 feet 4 inches from the hands of the other; how many pounds does each bear.

Ans. 1142 fbs. and 855 fbs. 196. There is a windlass, the wheel of which is 60 inches in diameter, and the axis, around which the rope coils, is 6 inches in diameter; how many pounds on the axle will be balanced by 240 pounds at the wheel ?

Note. The spaces passed over are evidently as the diameters or the circumferences; therefore, $\frac{6}{6} = 10$, ratio.

Ans. 2400 pounds.

197. If the diameter of the wheel be 60 inches, what must be the diameter of the axle, that the ratio of the weight to the power may be 10 to 1? Ans. 6 inches.

Note. This calculation is on the supposition that there is no friction, for which it is usual to add $\frac{1}{2}$ to the power which is to work the machine.

198. There is a screw whose threads are 1 inch asunder, which is turned by a lever 5 feet=60 inches long; what is the ratio of the weight to the power?

Note. The power applied at the end of the lever will de

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199. asunder will be 200. 10 feet, of that the pow 201. was 14 quarts of

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principle in ctly balance es they pass eet from the op; therefore prop by the tient will alpower; §=4, as the power, Ans. 168 lbs. wer would it °°==250 Њs. much as the weight from st the power Ans. 20 feet. the less half weight?

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2400 pounds. inches, what of the weight 1ns. 6 inches. that there is power which

inch asunder, long; what is

lever will de

scribe the circumference of a circle $60 \times 2 = 120$ inches in diameter, while the weight is raised 1 inch; therefore, the ratio will be found by dividing the circumference of a circle whose diameter is twice the length of the lever, by the distance between the threads of the screw. $120 \times 34 = 3774$ 3774

circumference, and-Ans.

199. There is a screw, whose threads are $\frac{1}{4}$ of an inch asunder; if it be turned by a lever 10 feet long, what weight will be balanced by 120 lbs. power? Ans. 30171 lbs.

200. There is a machine, in which the power moves over 10 feet, while the weight is raised 1 inch; what is the power of that machine, that is, what is the ratio of the weight to the power? Ans. 120.

201. A rough stone was put into a vessel, whose capacity was 14 wine quarts, which was afterwards filled with 21 quarts of water; what was the cubic content of the stone? Ans. 6644 inches.

FORMS OF NOTES AND RECEIPTS.

Forms of Notes, Receipts, Orders and Bills of Parcels.

NOTES.

No. 1.

Montreal, Oct. 22, 1849. For value received, I promise to pay to Oliver Bountiful, or order, two pounds, ten shillings and sixpence, on demand, with interest. WILLIAM TRUSTY.

Attest, TIMOTHY TESTIMONY.

C

No. IL.

Kingston, Oct. 10, 1849. For value received of A. B. in goods, wares, and merchandize, this day sold and delivered, I promise to pay him or bearer, — pounds, — shillings and — pence, in ten days from date, with interest. C — D —. No. III.

By two Persons.

Stanstead, Oct. 1, 1849. For value received of _____, in _____this day sold and delivered, we jointly and severally promise to pay him, or order, _____ pounds, _____ shillings and _____ pence in _____ days from date, with interest. B______ C____. D_____ E____.

RECEIPTS.

Montreal, Oct. 20, 1849. Received from Mr. Durance Adley, ten pounds, in full of all accounts. ORVAND CONSTANCY.

Receipt for Money received on a Note.

York, Nov. 1, 1849. Received of Mr. Simon Eastly (by the hand of Mr. Titus Trusty) sixteen pounds, ten shillings and sixpence, which is endorsed on his note of June 3, 1831.

SAMSON SNOW.

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ORDERS AND BILLS OF PARCELS.

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Receipt for Money received on Account. Stanstead, June 2, 1849. Received of Thomas Dubois, twenty pounds, on account. ORLANDO PROMPT.

Receipt for Money received for another Person.

Sherbrooke, June 4, 1849. Received from P. D. twenty-five pounds for account of J. T. ELI TRUEMAN.

Receipt for Interest due on a Note.

• Quebec Dec. 18, 1849.

Received of I. S. fifteen pounds, in full of one year's interest of £250, due to me on the — day of — last, on note from the said I. S. SOLOMON GRAY.

Receipt for Money paid before it becomes Due. Prescot, May 3, 1849.

Received of T. Z. fifteen pounds, advanced in full for one year's rent of my farm, leased to the sail T. Z. ending the first day of April next, 1850.

JOHN HONORUS.

ORDERS.

Belville, Nov 3, 1848.

Mr. Stephen Girard. For value received, pay to A. B., or order, five pounds and six shillings, and place the same to my account.

Montreal, Sept. 1, 1848.

Mr. Timothy Titus. Please to deliver to Mr. L. D. such goods as he may call for, to the amount of seven pounds, and place the same to the account of your obedient servant, NICANOR LINUS.

BILLS OF PARCELS.

It is usual, when goods are sold, for the seller to deliver to the buyer, with the goods, a bill of the articles, and their

22, 1849. r Bountiful, on demand, Trusty.

10, 1849. s, and mere to pay him - pence, in - D-----.

. 1, 1849. day sold and pay him, or ence in _____ C_____. E_____.

20, 1849. unds, in full NSTANCY.

e. . 1, 1849. of Mr. Titus ence, which

DN SNOW.

BILLS OF PARCELS.

prices, with the amount cast up. Such bills are sometimes called Bills of Parcels.

Montreal, 6th May, 1849.

Mr. Abel Atlas,

Bought of Benjamin Buck,

124 yards figured Satin, at 12s. 6d. per yard, 7 3 16 Sprigged Tabby, at 6s. 3d. 10 2 0

Received Payment,

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BENJ. BUCK.

Montreal, 14th May, 1849.

Mr. John Burton,

Bought of Geo. Williams,

3 hhds. new Rum, 118 gallons each, at 1s. 6d. per gallon. 2 pipes French Brandy, 126 & 132 gal. 5s. 7d. 1 hhd. brown Sugar, $9\frac{3}{4}$ cwt. at £2 11s. 9d. per cwt. 3 casks Rice, 269lb each, at 66 3d. Ϊħ. 5 bags Coffee, 75lb each, at 1s. 2d. " " 1 chest hyson Tea, S6lb, at " 4s. 8d. **Received** Payment,

For George Williams, THOMAS ROUSSEAU.

Wilderness, 8th Feb. 1849.

Mr. Simon Johnson, Bought of Asa Fullum,

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1500	"'	Lathing	, 1	0s.	Ød.	**	
650	"	Plank,	1	10s.	0d.	""	
879	"	Timber,	0	12s.	6d.	""	
236	"	"	0	13s.	9d.	""	

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