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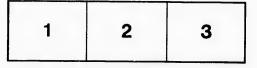
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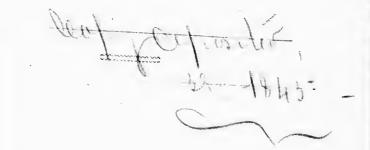


ROYAL CANADIAN SERIES.

ARITHMETIC

FOR

PUBLIC SCHOOLS.



TORONTO: CANADA PUBLISHING COMPANY (LIMITED) 1882. Entered according to Act of the Parliament of Canada in the Year One Thousand Eight Hundred and Eighty-two, by the CANADA PUBLISHING COMPANY (LIMITED), in the Office of the Minister of Agriculture.

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PREFACE

The distinctive purpose of this work has been to furnish a simple, lucid, and systematic exposition of the theory and practice of Arithmetic, covering the ground which is usually traversed by the pupil before entering the High School.

Arithmetic, it may be said, is above everything else a practical study. The art of computation is undoubtedly of much value in the practical concerns of every day life; but the habit of investigating the principles on which this art is based is not of inferior importance. The former gives to the student a mastery of figures, which will be serviceable in commercial and scientific pursuits: the latter tends to concentrate his attention; to induce habits of patient abstraction and accurate thought; to familiarize him with the laws of reasoning, and to lead him to examine carefully the grounds of every inference he draws.

The difficulty hitherto met with in text-books on Arithmetic is that the theoretical has been made subordinate to the practical. But if the theory is imperfectly understood, and the principles are not comprehended, then questions can only be solved mechanically. Hence the necessity of first making the rules intelligible, and then impressing them on the mind by copious and practical illustration. With this object in view, two important principles have been kept in mind: (1) That the exercises shall be so constructed as to require the pupil to think; and (2) That they shall consist largely of examples selected with especial reference to the pursuits of an agricultural and commercial people.

A comparison of the present work with those which are specially valued on account of the character and number of the problems they contain will, it is believed, show that it comprehends everything that is usually regarded as of practical importance in Arithmetic. The prominent features of the work may be enumerated as follows:

lanada in the y-two, by the n the Office of (1) The investigation of the principle on which a rule in Arithmetic depends always precedes the statement of the rule itself.

(2) Every process employed in the solution of a question is referred to some general law or axiom in the theory of numbers.

(3) These general truths, as they may be called, are distinctly enunciated and are printed in italics. If self-evident, they are illustrated by simple numerical examples; if otherwise, more extended demonstrations are given: in every case, the truth itself is stated in a clear, concise form.

(4) The solution of money problems, and the application of reduction to concrete quantities in their simplest form, leading the pupil gradually up from the abstract to the **c**oncrete, are placed earlier in the course than is usual, and are thus made available in subsequent exercises.

(5) The logical relations of the several parts of Arithmetic are lucidly marked by their arrangement. For example: Reduction is not treated as a separate rule, but so much of it as belongs to Multiplication falls under that head, while the rest takes its proper place as one of the practical applications of Division.

As will be apparent, considerable space has been taken up with exercises for rapid mental work, the importance of which, if the principles which underlie them are fully brought out by the teacher and grasped by the pupil, can hardly be over-estimated. It is confidently believed that the exercises will be found sufficiently numerous and varied, and that the examples solved in Ex. 26, 42, 43, 51, 57, 58 and 59, and in the Examination Papers 1 to 6, will aid in the illustration of the general principles which form the key to all problems in Arithmetic. The work, as a whole, it is hoped, will prove of the highest service to both teacher and student, and merit a permanent place among our Canadian educational textbooks.

TORONTO, June, 1882.

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		179	NOTATION AND NUMERATION.
		180	
		182	1. A Unit is one, or a single thing.
			Ex.—One: one boy; one dollar.
			2. A Number is a unit, or a collection of units, and answers
	•••	185	the question How many?
•••		186	Ex.—Three, Five, Twelve, Sixty.
	•••	187 187	3. The unit of any number is one of the collection of units which form the number.
	•••	187	Ex.—The unit of eight is one; the unit of six horses
		192	is one horse; the unit of twenty dollars is one dollar
			4. A Unit may be either abstract or concrete.
			5. An Abstract Unit is one that does not refer to any nor
	•••	194	ticular object of thing.
•••		195	Ex.—One.
es ar	- 1		6. A Concrete Unit is one that is applied to some particular object or thing.
		108	ExOne cent, one quart.
	•••	198	7. A number is Abstract or Concrete, according as its unit
3.			is abstract or concrete.
		2 01	ExThree, Seven, Twelve Forty One Hundred
		203	and Abstract Numbers.
		-	Three Dollars, Seven Gallons, Twelve Men, Forty
•••	1 t o	xxv	Books, One Hundred Cents, are Concrete Numbers.

2	8. All numbers in ordinary use are formed from the charac- ters 1, 2, 3, 4, 5, 6, 7, 8, 9, 0.
f	<i>Ex.</i> —384, 9072, 165.
	9. The Figures 1, 2, 3, 4, 5, 6, 7, 8, 9, are read one, two, three, four, five, six, seven, eight, nine, and are called Digits, or Significant figures.
17. Th a b	10. The Figure 0, called nought, zero, or cipher, has no value, and is termed the Insignificant figure.
18. The	11. The Art of Expressing Numbers by means of these or other characters is called Notation.
Forty Fifty, Sixty,	12. Notation is of two kinds, Arabic Notation and Roman Notation.
The	ARABIC NOTATION.
ea to	ARABIC NOTATION.
	13. Arabic Notation is the art of expressing numbers by means of the characters 1, 2, 3, 4, 5, 6, 7, 8, 9, 0. (It is so called because it was introduced by the Arabs.)
1. Wr 2. Wri	14. The next number above nine is ten, which is expressed by the figure one placed to the left of the figure nought, meaning one ten and no units; in the same way eleven, or ten units and one unit, may be ex- pressed by the figure one (meaning one ten) placed to the left of the figure one (meaning one unit), and so on for the rest of this order.
	15. The complete order will then be:
3. Writ	Ten, represented by 10 Eleven, " " 11Fifteen, represented by 15 Sixteen, " " 16Twelve, " " 12 Thirteen, " " 13 Fourteen, " " 14Sixteen, " " 16 Sixteen, " " 17 Eighteen, " " 18 Niuetcen, " " 19The pupil will notice that the first part of each word agrees with the right-hand figure in the number expressing its value.
	16. In like manner, all numbers in the next group are expressed by using the figure two, followed by the
	3

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e read one, two, , and are called

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ng numbers by , 7, 8, 9, 0. oduced by the

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ented by 15 '' 16 ''. 17 '' 18 '' 19

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ext group are blowed by the

ARABIC NOTATION.

original digits in order, the number twenty (written 20) meaning two tens and no units, the rest being formed by proceeding as before, thus:

Twenty-one,	represented	by	21
Twenty-two,	6 6	ü	22
Twenty-three,	,	"	23, etc., etc.

17. The next group will express three tens, called thirty, and a certain number of units, the successive numbers being formed in the same manner as before.

18. The remaining groups will commence with the following key words:-

Fifty, Sixty,	66 66		50 60	Seventy, re Eighty, Ninety,	66 66	 80
The pupi each w to it.	l will ag ord bea	ain r irs to	noti o th	ce the liken le digit in th	ess the first ne number o	J -

19. We now come to the greatest number that can be expressed by two figures, viz., 99, meaning, of course, nine tens and nine units.

EXERCISE 1.

- 1. Write down the following numbers in figures :--Four, Eleven, Twenty-six, Thirty-seven, Forty-five, Sixtyeight, Seventy-seven, Fifty-nine, Eighty, Ninety-two.
- 2. Write down the smallest and also the greatest number expressed
 - by one figure.
 - by two figures.
 - by the figures two and three.
 - by the figures three and nine.
 - by the figures nine and one.
 - by the figures one and seven.
 - by the figures seven and eight.
 - by the figures eight and two.
- 3. Write down in order all the numbers

From twenty-five to forty-seven.

- " sixty-three to seventy-eight.
- " seventeen to eleven.
- forty-seven to thirty-three.

- 4. Write down the number of words, and also the numbe of letters, in this sentence.
- 5. Count the numbers between fifty and seventy-five.
- 6. Write down any numbers you can make

by using both the figures 6, 8. by using both the figures 7, 6. by using both the figures 8, 7.

20. We left off at the number 99, and must now show how to represent a number having one more unit than 9ç The required number is called one hundred, and 1 written 100,—the figure 1 meaning one hundred units the next figure 0 meaning no ten units, and the last meaning no units.

21. We thus arrive at one hundred, two hundred, etc., and by combining the hundreds group, and the preceding group of tens, and the simple group of units, w complete all numbers that can be formed with thre figures.

Ex.—One hundred and sixty-four is written 164 meaning one hundred units, six tens of units (or sixt units), and four units.

Four hundred and four would be written 404, the zero meaning that there are no units in the tens group

Eight hundred and sixty is written 860, the zero in plying that there are no units in the units group.

- 22. We now see the importance of the figure 0 as a meat of keeping other figures in their places, for without i 404 would be 44, four tens and four units; 860 woulbe 86, or eight tens and six units.
- 23. The hundreds group or order brings us up to the number 999, the largest that can be written with three figures

Ex.—Write down the number Three Hundred an Seventy-nine.

The three, standing for hundreds, must be place on the left of the required number, in the hundred 1. W1 se au fi fo ho

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2. Wr di

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ARABIC NOTATION.

place; the seventy or, seven tens, we must put in the next place, to the right of the three—that is, in the tens' place; and the nine, which means just nine units, must be in the next or units' place. The number then stands thus:—

Hundreds.	Tens.	Units.
3	7	9
	or, 379.	

If the number had been three hundred and nine, then, there being no tens, the tens' place would be filled by zero, as 309. If the number had been three hundred and seventy, then, there being no units, the units' place would be filled by the zero, as 370.

The number o83, meaning no hundreds and eight tens and three units, should be written 83, for it can be of no use to express hundreds when there are none,

EXERCISE 2.

- I. Write down the following numbers :--One hundred and seventeen; three hundred and eleven; five hundred and eleven; five hundred and seventy-five; eight hundred and ninety-nine; four hundred; sixty-nine; five hundred and seven; eight hundred and sixty; four hundred and ten; nine hundred and nine; seven hundred and eighty-seven.
- 2. Write down, in order, the numbers between one hundred and five and one hundred and twenty.
- 3. Write down all the numbers of three figures in which the two left hand figures are seven and nine; in which the two right hand figures are eight and nought; in which the outside figures are six and seven; in which the outside figures are seven and nought.
- 4 Write down the greatest and least number composed of three figures.
- 5. Write down all the numbers formed from the figures six, eight and nine.

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st now show how nore unit than 96 hundred, and 1 one hundred units hits, and the laste

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written 404, then the **tens** group a 860, the zero in: units group.

ure 0 as a mean ces, for without i units : 860 woul

up to the numbe with three figures ree Hundred an

, must be place in the hundred

6

6. Write down, in order, all the numbers made up of the 27. As figures three, nought, nine, commencing with the smallest number. 7. How many numbers are there between one hundred and one hundred and ninety-nine; between ninety seven and one hundred and nine. 28. Pr 8. Write down, in order, all the different numbers formed by using (1) the three figures 7, 0, 0 (2) " 8, 0, 6 ** (3) 9, 9, 8 **2**9. Af .. " 7, 7, 7 **30.** Af 24. We next proceed to numbers of four figures, the first 1 one after 999 being written 1000, and called one thousand. The remaining numbers of four figures are formed by writing thousands in the fourth Ċ place, hundreds in the third place, tens in the second place, and units in the first place from the 31. Th right. Thus 7809 represents nine units of the first t order, no units of the second order or tens, eight ι units of the third order or hundreds, and seven ¢ units of the fourth order or thousands. r whole number is read seven thousand eight hundred The and nine. f 25. The pupil will by this time see that one unit of any of ¢ these orders has the same value as ten units of the f next lower order, that is to say :- One thousand is The the same in value as ten hundreds; one hundred " is the same as ten tens; and one ten the same "

26. We should therefore naturally expect to meet after the order of thousands a fifth order representing ten thousands, and this is the case; but instead of giving it a new name it is known as the order of tens of thousands. Thus 86079 represents eight tens of thousands, six thousands, no hundreds, seven tens, and nine units: or eighty-six thousand and seventy-nine.

as ten units.

" And we

..

"

" "

"

... "

en one hundred ; between ninety.

numbers formed

6 3

figures, the first and called one s of four figures in the fourth e, tens in the t place from the nits of the first or tens, eight eds, and seven ousands. The l eight hundred

unit of any of en units of the ne thousand is ; one hundred ten the same

meet after the presenting ten instead of givorder of tens nts eight tens ndreds, seven thousand and

ARABIC NOTATION.

- rs made up of the 27. As the order hundreds followed in value the order tens (Art. 20), so now we have hundreds of thousands following in value tens of thousands, and forming the sixth order from the right.
 - 28. Proceeding as before, we obtain (after one hundred thousand), two hundred thousand, three hundred thousand, and so on until we reach ten hundred thousand. This is expressed by a new name, and called a million.
 - 29. After counting to a million, we proceed to count one million, two millions, three millions, and so on as far as ten millions, which forms the seventh place from the right, or the seventh order.
 - 30. After this hundreds of millions will follow tens of millions, just as hundreds of thousands followed tens of thousands (Art. 27); and hundreds followed tens (Art. 20). We then come to ten hundreds of millions, which is called a billion.
 - 31. The figures 1, 2, 3, 4, etc., when they stand alone, or when they occupy the first place, denote simply so many units or ones, and are called units of the first order. When they occupy the second place, they represent tens, and are called units of the second order. When found in the third place, they stand for hundreds, and are called units of the third order, and so on. This may be illustrated by the following table:-

The 1st order of units is called units.

	2nd	"	* 6	**	tens.
" "	3rd	**	66	**	hundreds.
	4th	66	**	66	thousands.
* *	5th	**	66	* *	ten-thousands.
**	6th	**	66	• •	hundred-thousands.
**	7th	"	4 6	• 6	millions.
" "	8th	* *	4.6	* *	ten-millions.
"	9th	""	**	• •	hundred-millions.
56	Ioth	"	64	••	billions.
4 14	11th	44	· •	• •	ten-billions.
"	12th	**	**	••	hundred-billions.

And we may extend this table to trillions, quadrillions, etc.

32. The pupil must now practice writing down on the slate any number that may be read.

Ex.—Express in figures the number nine hundred and seventy thousand six hundred and eight.

Here the highest order of units is hundreds of thousands, and there are nine of them; the next order is tens of thousands; of which there are seven; the next order is thousands, of which there are none; the next hundreds, of which we have six; the next tens, of which there are none; the next units, of which we have eight. To write the number we first set down the units of the highest order, and this is hundreds of thousands; then the tens of thousands, thousands, hundreds, tens, units, one after the other, always putting in a cipher or zero for the order of which there are no units. The number must then be written

970608.

Too much attention cannot be paid to the placing of the zero.

EXERCISE 8.

1. Write the following numbers in figures:

Nine thousand and forty-eight.

Five thousand and seven.

Forty-three thousand six hundred and fifty-nine.

Five hundred and thirty-six thousand three hundred and two.

Four hundred and five thousand three hundred and thirteen.

Five million forty-three thousand and thirty-seven. Sixty-four thousand seven hundred and ninety-two. Three hundred and fifty-six thousand and ninety-seven. Nine million three hundred and forty-five thousand and

twenty-seven. Eighty thousand and fifty-six. Nine million ninety thousand nine hundred.

Eighty-three thousand and seven.

Nine thousand and ninety.

Write Th

Ele Six 2. Wr

3. Wri 1 4. Wri 5. Wri f

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33. In R expr

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Note to T requires a m pupil has yes have been les

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nundreds of n; the next e are seven; re are none; x; the next xt units, of aber we first and this is s of thouis, one after zero for the umber must

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nine. e hundred

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ROMAN NOTATION.

Write he following numbers in figures:

Three hundred and seventy-five million eight hundred and sixty-seven thousand seven hundred and ninetynine.

Eleven thousand and seventy-one.

Six million eight thousand seven hundred and four.

 Write down the greatest and least numbers that can be formed

> by using 4 figures. " " 5 " " " 6 " " " 7 "

- 3. Write down, in order, all the numbers of four figures having 3 for the left hand figure and 72 for the two right hand figures.
- 4. Write down the greatest and least numbers that can be formed by using all the figures 7, 3, 0, 5.
- 5. Write down all the different numbers that can be formed by using all the figures 7, 0, 0, 8, and name the greatest and the least.

ROMAN NOTATION.

33. In Roman Notation seven Capital letters were used to express numbers. The letters were

Ī	standing	for the	number	т
V	"	"	44	-
Х	" "	"	**	5 10
L	**	66	**	50
С	66	4.6	"	100
D	**	•1	**	
Μ	66	66	"	500

All other numbers being expressed by combining these letters in different ways. Hence Roman Notation is the expression of numbers by letters.

NOTE TO TEACHER.—As the writing of numbers by Roman Notation requires a more extended idea of Addition and Subtraction than the pupil has yet obtained, it may be omitted until after these operations have been learned.

34. They are combined with the following results:

1. When any letter is repeated its value is repeated. Thus, X stands for 10, and XXX stands for 30; C stands for 100, CC stands for 200. XX

XXI

XL

L

LX

 \mathbf{XC}

XXV

CXX

CLXIV

Write th

1. Thir

2. Seve

3. Nine

4. Twe

5. Thir

6. Fort; 7. Nine

8. One

9. Two

10. Seve

11. Eight

12. Twel

13. Eight

14. Six tl

15. Fiftee

16. Eleve

17. Eight

ty

foi

cig

С

XXX

2. When a letter of less value follows one of greater value, its own value must be added to that of the greater.

Thus, V = 5. VIII = 8, C = 100, CIII = 103, LX = 60.

3. When a letter of less value comes before one of greater value it takes away its value from that of the greater.

Thus, X = 10, IX = 9, L = 50, XL = 40.

4. When a letter of less value stands between two of greater value the less must be taken from the one that follows it, and the remainder must be added to the one that precedes it.

$$1 \text{ mus XIX} = 19, \text{CXL} = 140, \text{CXC} = 100.$$

5. A bar over a letter or letters makes it as many thousands as there are units in the letter or letters.

Thus $\overline{V} = 5000$, $\overline{L} = 50,000$, $\overline{C} = 100,000$, $\overline{IX} = 9,000$.

A letter is not usually repeated more than three times. Thus 400 would be written CD rather than CCCC.

35. These methods will be found quite sufficient to form all ordinary numbers, and although this Notation could be used in business and other calculations, the process would be very tedious, and for this reason is not used. The characters are chiefly employed to mark the hours on clocks and watches, to number volumes and chapters of books, to indicate the values of coins, bank-bills, etc.

TABLE OF ROMAN NOTATION

-								****	1Un					~ '
1	•					One.	t X					Ten.	18.	Sever
II						Two.	NT .	•	•	•	•	len.		dre
III						Three.	VIV.	•	•	•	•	Eleven.	19.	Four
IV				÷	•	Four.						Hourtoon		1
V	·	•	•	•	•	Five.						Hittoon	100 a a .	T3 . C.
VI	•	•	•	•	•	Five.						Sivtoon	10 A A A	m .
iv	•	•	•	•	•	Six.	[/ II]					1.10htoon	100	The set of
IV	•	•	•	•	•	Nine.	XIX				•	Ninotoon	42.	гопу
		•		÷		Six. Nine.	[/ II]					Eighteen. Nineteen	100	T

ROMAN NOTATION.

	ROMAN	NOTATION. 11
results: ulue is repeated. tands for 30; C s one of greater to that of the co, CIII = 103,	$\begin{array}{rcccccccccccccccccccccccccccccccccccc$	CD Four hundred. D Five hundred. DC Six hundred. DCC Seven hundred. DCCC Eight hundred. DCCC Nine hundred. M One thousand. MM Two thousand.
before one of the from that of	$\begin{array}{c} \overline{CXX} & \cdot & 120000 \\ \overline{CLXIV} & \cdot & 164000 \end{array} \overline{\mathbf{M}} .$	· · 5000 DLCXL · 550140 · 1000000 MDXC · 1000590
, $XL = 40$. between two of a from the one ast be added to XC = 190. tes it as many tter or letters. = 100,000, IX hore than three D rather than cient to form Notation could ns, the process on is not used. to mark the r volumes and hues of coins,	 Write the following in Arabia Thirteen. Seventeen. Nineteen. Twenty-six. Thirty-eight. Forty-four. Ninety-seven. One hundred and fifty. Two hundred and eighty. Seven hundred and forty-four. Eight hundred and forty-four. Twelve hundred, Eighty-seven. Six thousand. Fifteen hundred. Eleven thousand. Eight hundred and eighty-eight. 	 RCISE 4. c and also in Roman Notation : 23. Sixty-seven. 24. Ninety-one. 25. One thousand eight hundred and eighty-one. 26. Twenty-seven. 27. Forty-nine. 28. Seventy-three. 29. Sixty-eight. 30. Eighty-four. 31. Ninety-seven. 32. One hundred and ten. 33. Five hundred and fifty. 34. Seven hundred and forty. 35. Nine hundred and forty. 36. Sixteen hundred. 37. Fifty thousand and five. 38. Three hundred and eighteen. 39. Seven hundred and ninety.
Eleven. Fourteen. Sixteen.	 Seven thousand five hundred and ninety-two. Four thousand seven hundred and eleven. Fifty-two. Thirty-nine. Forty-three. 	 Cone thousand and ninety- six. Twenty-five thousand. Fifty-nine thousand three hundred. Eighty-seven thousand and forty.

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NUMERATION.

- 36. Numeration is the art of expressing in words those numbers that may be given in figures or letters.
- 37. If the pupil clearly understands the method of expressing numbers in Notation, there will not be much trouble in reading any number that may be set down in figures. To read large numbers more easily, the figures are separated by commas into periods or groups, commencing from the right hand; and the method that is nearly always adopted is that in which each period or group consists of **three** figures.
- 38. The first or right hand period contains units, tens, and hundreds, and is called the period of units; the second period contains thousands, ten-thousands, and hundred-thousands, and is called the period of thousands; the third period contains millions, ten-millions, and hundred-millions, and is called the period of millions; and so on for the others. This can be more clearly seen from the following table :--

39, Hei be

> Point at fig

First w

Point

Hundred-Thousands. Hundred-Trillions, Hundred-Billions. Hundred-Millions Ten-Thousands. Ten-Trillions. Ten-Billions. Ten-Millions. Thousands. Hundreds. Trillions. Millions. Billions. Units. Tens. 8 9 6 5 4 3 2 7 5 6 5 4 1 4 Š 5th Period. 4th Period. 3rd Period. 2nd Period. 1st Portod TRILLIONS. BILLIONS. MILLIONS. THOUSANDS. UNITS. The value of the figures in the above table, expressed in

words, is eight hundred and ninety-six trillion, five hundred and forty-three billion, two hundred and oventy-five million, four hundred and fifty-six thoustatic, one hundred and forty-five. This table may be extended to any number of orders. The periods after trillic as are, in their order, quadrillions, quintillions, sextillions, septillions, octillions, and nonillions. (a) Point

- 1. 1: 2. (3. 2 4. 5 5. 6. 4 7. ((b) Write 1. N
 - 2. T
 - 3. Si
 - 4. Se

NUMERATION.

39. Hence we have the following rule for reading large num bers easily:

RULE FOR NUMERATION.

Point off the number into periods of three figures each, beginning at the right hand; then begin at the left hand, and read the figures of each period separately, adding the name of each period except the units' period.

Ex. 1.-Read 261034.

First point off by commas, thus: 261,034. The number will then read

261 thousand, and 34.

Ex. 2.- Read 4604792816.

Point off thus ; 4,604,792,816, and read :

4 billion, 604 million, 792 thousand, 816.

EXERCISE 5.

(a) Point off, read and write:

Ι.	116234.	8. 141120. 15	. 7640.
2.	65231.	9. 101207. 16	
3.	20703.	10. 68978. 17	
4.	71005.	11. 72020. 18	1008003.
5.		12. 80001. 19	. 212375647.
6.	48000.	13. 857000. 20	. 609003588.
7.	60029.	14. 91029. 21	. 897856846.

- (b) Write in figures and read:
 - 1. Nine in the 1st period.
 - 2. Two hundred in the 1st period.
 - 3. Sixi; in the 2nd period, two in the 1st.
 - 4. Seven hundred in the 3rd period.

words those letters.

od of expressnot be much y be set down re easily, the to periods or and; and the that in which ures.

its, tens, and f units; the iousands, and iod of thou-, ten-millions, e period of This can be le:---

Hundreds. Units. Tens.

I 4 5 Ist Pariod UNITS.

expressed in trillion, five hundred and fty-six thoutable may be periods after 1s, quintills, and non-

 (b) Write in figures and read : 5. Two hundred and thirty in the 3rd period, sixty in the 1st. 	
5. Two hundred and thirty in the ard period sind	
the ist.	(đ) W
	10
6. Eighty-one in the 4th period, five hundred and one in the ard, seven in the and truck	II
in the 3rd, seven in the 2nd, twelve in the 1st. 7. Thirty in the 5th period, six hundred and three in the 1st.	
	12
8. Seven hundred in the 5th period, eighty in the 4th.	
9. Eight in the 4th period, seven in the 3rd, fourte 1 in the 2nd, and ten in the 1st.	13
10. Fifteen in the 6th period, eighteen in the 4th, two	14
hundred and seven in the 3rd, and eighty-one in the	
	15
(c) Point off, read and write:	
1. 60701892. 7. 163194568.	16.
8. 3050050183.	
9. 500204.	
10. 594900.	(e) Ex
5. 593000070500. 6. 190190001900. 12. 2007980134.	
(d) Write in figures:	
1. Eighteen in the 2nd period.	
2. Two in the 3rd period, sixty in the 2nd, one hundred and fifty-three in the 1st.	
3. Sixty in each of the 4th, 3rd, 2nd and 1st periods.	
4. 60 million, 200 thousand, 500.	
5. 402 billion, 348 million, 213 thousand, 20.	
6. 78 trillion, 640 billion, o million, 6 thousand, 16.	
7. 6 billion, 542 million, 25.	
8. Six billion, five hundred and forty-two million, twenty- five.	
9. Four hundred and two billion, three hundred and forty-eight million, two hundred and thirteen thou- sand and twenty.	

14

6.94 ·

NUMERATION.

(d) Write in figures:

- 10. Five million, eight thousand, nine hundred and fortynine.
- 11. Two hundred million, three hundred thousand, eight hundred.
- 12. Twenty-nine billion, five hundred and ninety-nine million, six hundred and one.
- 13. Four trillion, five hundred and fifty-eight million, two hundred and forty-thousand and seventy.

14. Thirty-two billion, one million, three hundred and forty-three thousand, four hundred and four.

- 15. Five hundred and fifty-five million, seven hundred and seventy-seven thousand, six hundred and sixtynine.
- 16. Eight hundred and six billion, seventy million, five thousand, two hundred and six.

(e) Express in Arabic Notation, and also in words:

 XIX. XXI. XXI. X. XLV. LXV. LXV. LXV. LXXIX. LXXXV. CX. CXIX. CXIV. CXXV. CLX. CLX. CLX. CCLX. CCXC. CCXC. DCXXIX. 	 22. MDCCCLXIX. 23. VCXCIII. 24. XVIJ. 25. MM CXXII 26. MM MD. 27. CDL. 28. XLVIII. 29. DXXXVI. 30. MDCCXCIV. 31. XCXVI. 32. CCCLXXXI. 33. LCMXCIX. 34. MMDCXII. 35. VCDLXX. 36. CCLXV. 37. MMMDCXXVII
15. CCLX. 16. CCXC.	35. VCDLXX.

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(e) Express in Arabic Notation, and also in words:

43. Th tl b

> I a I a 2 4 3 4 5 4

> 6 '

7 '

5 ar

1 ar 2 " 3 "

4 "

7 "

9 "

10 "

9 and

2 "

3 " 4 "

5 "

9 ". 10 "

5 " 6 "

8 "

I are

6 " 7 "

8 "

8 · 9 ·

42. IXXXV.	52. VDLIX.
43. xviii.	53. DLX.
44. lxxvii.	54. XXXID.
45. LXVII. 46. CLXIV.	55. LIXCCCXLIV.
40. CLATV. 47. CXXXV.	56. XVDCCXLIX.
48. CXLIX.	57. MMMMXC.
49. MXIX.	58. VMDCCXLIX.
50. DCLIII.	59. MDXXVCDLXXIX.
51. CXCIX.	60. MDCCCLXXXII.
-	WDCCCLXXXII.

(If more examples are required for practice, those found in the subsequent Exercises will answer the purpose.)

ADDITION.

40. The Addition of two or more numbers is the method of finding how many units are in all the numbers if taken together.

The number of units found is called the sum of the given numbers.

Thus the sum of 4 and 5 is 9, for in 4 there are four units and in 5 there are five units, and if we count five more units after we get four we obtain 9 units.

- 41. This is often written 4 + 5 = 9, the sign + meaning that the numbers on each side of it are to be added together. It is called **Plus**.
- 42. The sign = means that the expressions on each side of it are equal, or of the same value. It is read Equal to.

Ex. 3 + 6 = 9 would be read three plus six equal to nine, and it means that the sum of 3 and 6 is nine.

ADDITION.

so in words:

X.

). CXLIV. CXLIX. MXC. CXLIX. VCDLXXIX. CLXXXII.

tice, those found inswer the pur-

s the method of imbers if taken

the sum of the

there are four we count five y units.

meaning that be added to-

reach side of sread Equal

lus six equal and 6 is nine. 43. The following table should be committed to memory by the pupil, who should at the same time be quite sure, by counting, that the sums are correct:

[
I and	2 and	3 and	4 and	
I are 2	I are 3	I are 4	I are 5	
- 3	2 " 4	2 " 5	2 " 6	
5 4	3 " 5	3 " 6	3 " 7	
1 4 5	4 " 6	4 " 7	4 " 8	
5 0	5 " 7	5 " 8	5 " 9	
	6 " 8	6 ' 9	6 " IO	
1	7 " 9	7 " 10	7 " 11	
9	8 " 10	8 " 11	8 " 12	
9 10	9 11	9 " 12	9 " I3	
	10 " 12	10 " 13	10 " 14	
5 and	6 and	7 and	8 and	
1 are 6	I are 7	I are 8	I are g	
1 - 7	2 " 8	2 " 9	2 " 10	
5 0	3 " 9	3 " 10	3 " 11	
1 7 9	4 " 10	4 " 11	4 " 12	
5 10	5 " 11	5 " 12	5 " 13	
	6 " 12	6 "13	6 " 14	
/ 14	7 " 13 8 " 1	7 "14	7 " 15	
	0 14	8 " 15	8 " 16	
9 14	9 15	9 '' 16	9 " 17	
10 " 15	10 " 16	10 " 17	10 " 18	
9 and	10 and	II and	12 and	
I are IO	I are II	I are 12	1 are 13	
2 " 11	2 " 12	2 " 13	2 " 14	
3 " 12	3 " 13	3 " 14	3 " 15	
4 " 13	4 " 14	4 " 15	4 " 16	
5 " 14	5 12	5 " 16	5 " 17	
15	6 16	6 " 17	6 " 18	
1 10	7 17	7 " 18	7 " 19	
-/ 1	8 " 18	8 " 19	8 " 20	
9 10	9 " 19	9 " 20	9 " 21	
10 " 19	10 " 20	10 " 21	10 " 22	

ADDITION TABLE.

17

44. The following method will make the pupil quick at adding numbers, and should be practised by recitation as well as on the slate or paper:

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B

B

4 · 8 -6 -

9-

7-8-

Ac

Ad

1

1

I

2

3

2

Ad

Ex. 1.—Add by 2's from 1 to 19.

Resuli.-1, 3, 5, 7, 9, 11, 13, 15, 17, 19.

Reason.—1 and 2 make 3, and 2 make 5, and 2 make 7, and so on.

Ex. 2.—Add by 2's and 3's alternately, or one after the other, from 1 to 31.

Result.----1, 3, 6, 8, 11, 13, 16, 18, 21, 23, 26, 28, 31.

Reason.—1 and 2 make 3, and 3 make 6, and 2 make 8, and 3 make 11, and so on.

EXERCISE 6.

These questions should be solved mentally. Add:

By 2's from 4 to 50.	By 5's from 1 to 61.
By 3's from 1 to 43.	By 5's from 7 to 82.
By 3's from 6 to 51.	By 6's from 0 to 72.
By 4's from 1 to 53.	By 6's from 2 to 80.
By 4's from 5 to 45.	By 6's from 10 to 88.
By 2's and 4's alternately	from I to 40.

By 3's and 4's alternately from 0 to 56.

By 2's and 5's alternately from 4 to 60.

By 3's and 5's alternately from 7 to 63.

Begin with 1 and add 2 successively till the sum equals 101.

Begin with 2 and add 2 successively till the sum equals 100.

Begin with 2 and add 3 successively till the sum equals 101.

Begin with 3 and add 3 successively till the sum equals 102.

e pupil quick at ised by recitation

19. ke 5, and 2 make

ely, or one after

3, 26, 28, 31. e 6, and 2 make

ientally.

m 1 to 61. m 7 to 82. m 0 to 72. m 2 to 80. m 10 to 88.

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ie sum equals

Begin with 3 and add 4 successively till the sum equals 103. Begin with 4 and add 5 successively till the sum equals 104. Begin with 5 and add 7 successively till the sum equals 103. Begin with 6 and add 8 successively till the sum equals 102. Begin with 9 and add 9 successively till the sum equals 108. 4+2+3+7+1+5+9+6+3 =what? 8+3+5+9+2+0+4+7+8 = what? 6+5+2+1+9+7+6+8+4 = what? 9+8+6+7+4+1+5+3+8 =what? 7+8+9+0+7+8+9+0+7 = what? 8+9+5+8+9+7+0+9+8+2+6+1+4+3 = what? Add: By 7's from 1 to 71. By 10's from o to 120. By 7's from 3 to 87. By 10's from 13 to 153. By 8's from o to 96. By 11's from 1 to 100. By 8's from 6 to 102. By 11's from 4 to 92. By 9's from 2 to 92. By 12's from o to 144. By 9's from 10 to 109. By 12's from 3 to 135. Add rapidly the following : 4, 6, 5, 3, and 7. 13, 5, 6, 10, and 3. 6, 4, 8, 2, and 5. 12, 10, 2, 0, and 9. 10, 9, 5, 3, and 6. 27, 10, 3, 8, and 7. 10, 3, 7, 9, and 8. 36, 12, 7, 4, and 10. 14, 5, 3, 6, and 10. 11, 12, 10, 9, and 8. Add the numbers, 2 , 3, 4, 2, 3, 4, 2, 3, 4, etc., till the sum = 63. 3, 4, 5, 3, 4, 5, 3, 4, 5, etc., till the sum = 84. 2, 4, 6, 2, 4, 6, 2, 4, 6, etc., till the sum = q6.

Add alternately,

5, 6, 5, 6, 5, 6, 5, 6, 5, 6, etc., till the sum = 88. 6, 4, 6, 4, 6, 4, 6, 4, 6, 4, 6, 4, etc., till the sum = 100. 7, 5, 7, 5, 7, 5, 7, 5, 7, 5, etc., till the sum = 120. 8, 9, 8, 9, 8, 9, 8, 9, 8, 9, etc., till the sum = 119.

- 45. All numbers may be added together by means of the preceding table, and we will first add numbers when the sum of each order in them is less than 10.
- 46. To add numbers together, they must be of the same kind.

Ex.—5 peaches and 4 apples, if added together, make neither 9 peaches nor 9 apples. In the same way, 5 tens and 4 units make neither 9 tens nor 9 units.

47. Hence, when we add, we should always place figures of the same kind in the same column, that is, units under units, tens under tens, hundreds under hundreds, etc.

48. We thus have the following

RULE FOR ADDITION.

- 1. Write the numbers to be added, placing figures of the same kind in the same column, that is, units under units, tens under tens, etc., and draw a line beneath.
- 2. Begin at the right, and add the figures in each column from bottom to top.
- 3. Place under each column the result obtained by adding its figures.
- 49. To test the result, proceed in the same way, adding from top to bottom. The two sums should be the same, if the work be correct.

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ADDITION.

Ex. 1.—Find the sum of 422, 342, and 134.

um = 88. um = 100. um = 120.um = 119.

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place figures that is, units ls under hun-

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column from

by adding its

adding from the same, if

		~	4
r C 4 bundreds	stens 43	4 o o units	
8	9	8	

Ve write the numbers, placing units under units, tens under tens, hundreds under hundreds. We begin at the units' column and say: 4 units and 2 units are 6 units, and 2 units are 8 units, and we write the 8 under the units' column. Next, 3 tens and 4 tens are 7 tens, and 2 tens are 9 tens, and we write the 9 under the tens' column. Next, 1 hundred and 3 hundreds are 4 hundreds, and 4 hundreds are 8 hundreds, and we write the 8 under the hundreds' column. Hence, the entire sum is 8 hundreds 9 tens and 8 units, or 898.

In practice we shorten the work in this way: 4 and 2 are 6, and 2 are 8; 3 and 4 are 7, and 2 are 9; 1 and 3 are 4, and 4 are 8; making 898.

Ex. 2.-Add 3214, 2312, and 3453.

Here 3 and 2 are 5, and 4 are 9, which we place under units' column. Next, 5 and 1 are 6, and 1 are 7,
3214 which we place under tens' column. Next, 4
2312 and 3 are 7, and 2 are 9, which we write under
3453 hundreds' column. Lastly 3 and 2 are 5, and 3 are 8, which we set under thousands' column,
8979 making the sum 8979.

EXERCISE 7.

K The first thirty of the following quetions should be worked mentally.

(a) 1. A farmer harvested five loads of hay one day and six loads another day; how many loads did he harvest in the two days?

21

2. Henry's father gave him seven cents, and his brother gave him five: how many cents did a	20. Ho
e and here how many cents did he get in all?	dol
3. John worked six days one week and six days the next week: how many days did he work in the two weeks?	21. Da pea
4. I have six cherries in one hand and eight cherries in the other: how many have I in both hands?	did 22. Ho
5. Thomas has seven apples in one basket and nine in another: how many has he in both ?	23. A b five
6. There are seven sheep in one pen and seven in another: how many sheep are in the two pens?	24. Ho bird
7. How many are seven dollars, four dollars, and two dollars?	25. Wi plu
8. I had nine trees in the garden, and I set out five more: how many trees have I now in the garden?	26. In oth
9. Cora bought some paper for eight cents and some pens for eight cents: how much did she spend?	27. Ho 28. Sus
to. James had eight plums, Joseph had nine, and John had four: how many had they in all?	20. Ous her 29. Ho
11. There were ten wild ducks flying, when four more joined them: how many ducks were then in the flock?	30. Jan
12. How many are eight cents, six cents, and five cents?	how
13. There are seven books on one desk and six on another: how many books are on the two desks?	31. A 1 the
14. Joseph had three cents, his aunt gave him five, and his brother gave him eight : how many had he then ?	fou: (b) Add t
15. One hen had four chickens, and another had nine : how many chickens were there altogether?	(1 2
16. Herbert had four apples, his brother gave him three, and his sister two: how many did he then have?	6:
17. One word contains ten letters, and another seven: how many letters are there in the two words?	(7) 18 71:
18. Mary had nine books, and her mother gave her three more: how many had she then?	(13)
19. A man gave nine dollars for a plough, eight dollars for a rake, and six for a harrow : how much did he give for all?	7840 210 33

ADDITION.

nd his brother get in all?

: days the next he two weeks?

tht cherries in ands?

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en in another:

lars, and two

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n five, and his he then ?

er had nine :

ve him three, n have ?

seven: how

ve her three

it dollars for did he give

- 20. How many are nine dollars, three dollars, and four dollars?
- 21. David gave seven cents for apples, eleven cents for pears, and eight cents for peaches; how many cents did he spend?
- 22. How many are six and three and five?
- 23. A boy bought a pencil for ten cents and some peus for five; what did both cost?
- 24. How many are eight birds, seven birds, and two birds?
- 25. William spent nine cents for pears and eight for plums; how many cents did he spend altogether?
- 26. In one window there are nine panes of glass, in another six; how many are there in the two?
- 27. How many are eight and five and three?
- 28. Susan had eleven pears; her father gave her five, and her mother three; how many had she then?
- 29. How many are seven and five and six?
- 30. Jane paid six cents for silk, seven cents for a spool of thread, nine cents for pins, and four cents for tape; how much did she pay for all?
- 31. A man owns 4 farms; the first contains 1143 acres, the second 2320 acres, the third 3425 acres, and the fourth 2010. How many acres does he own?
- (b) Add together

(1)	(2)	(3)	(4)	(5)	(6)
23	43	27	36	72	123
62	36	31	22	17	241
(7)	(8)	(9)	(10)	(11)	(12)
181	5431	7654	5346	6135	4523
712	2364	1235	2453	3 ⁸ 44	2236
(13)	(14)	(15)	(16)	(17)	(18)
7840	2253	1122	1216	3701	21020
2105	4314	2203	2701	1293	34917
33	2432	3322	1082	2005	22032

(b) Add together :

(21)	(22)	(23)	24)	
3093124	202020	9334567	1212021	
2101003	333222	40101	2301304	
3003251	262626	623311	33330	
2020	102101	2020	201000	
	3093124 2101003 3003251	3093124 202020 2101003 333222 3003251 262626	3093124 202020 9334567 2101003 333222 40101 3003251 262626 623311	$\begin{array}{cccccccccccccccccccccccccccccccccccc$

50. We now come to the case, in which the sum in any column is equal to 10, or more than 10.

Ex.—Add together 378, 691, and 421.

Writing units under units, tens under tens, etc., as before, we say: 1 unit and 1 unit are 2 units, and 8 units are 10 units, which are equal to 1 ten and 0 units. Set down the 0 units under the units' column and take the 1 ten to the next, or tens' column. Then, 1 ten (which we carry) and 2 tens are 3 tens, and 9 tens are 12 tens, and 7 tens are 19 tens, which are equal to I hundred and 9 tens. Set the 9 tens under the tens' column and carry the I hundred to the next or the hundreds' column. Then, I hundred (which we carry) and 4 hundreds are 5 hundreds, and 6 hundreds are 11 hundreds, and 3 hundreds are 14 hundreds, which are equal to 1 thousand and 4 hundreds. Set down the 4 hundreds under its own column, and as there is no thousands' column, we must simply place the I thousand under the place where the thousands' column would be. Thus we have the answer, 1490.

In short:

I and I are 2, and 8 are 10. Set down the 0 and carry the I. Then, I and 2 are 3, and 9 are 12, and 7 are 19. Set down the 9 and carry the I. Again, I and 4 are 5, and 6 are II, and 3 are 14. Set down the 4 and carry the I to the next place to the left, or, in other words, set down the 14. 1. Writ

52. We

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Now IOL

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in t 2. Begin the colu righ carr

3. Procee the t

- 53. As in rect dow
- 54. In ad to a figu

24 -

ADDITION.

51. The work might be written thus:

(23)	24)
4567	1212021
1010	2301304
3311	33330
2020	201000

e sum in any

421.

r tens, etc., units, and 8 r ten and 0 nits' column imn. Then, tens, and q , which are tens under to the next d (which we 6 hundreds hundreds, Ireds. Set nn, and as mply place thousands' ver, 1490.

the 0 and re 12, and Again, 1 Set down he left, or,

 $\frac{3}{6}$ hundreds + 7 tens + 8 units 9 66 66 I 4 66 +2 66 + I 13 hundreds + 18 tens + 10 units Now 10 units = 1 ten +0 units 18 tens -1 hundred +8 tens+0 units 13 hundreds = 1 thousand + 3 hundreds + 0 tens + 0 units 1 thousand +4 hundreds +9 tens +0 units

This is exactly the same result as we had before.

52. We thus obtain the following complete

RULE FOR ADDITION.

- 1. Write the numbers to be added, placing figures of the same kind in the same column.
- 2. Begin at the right hand and add each column separately. If the amount of any column be less than 10, place it under the column added; but if the amount be 10 or more, place the right-hand figure of the amount under the column added, and carry the left-hand figure or figures to the next column.
- 3. Proceed in the same way through all the columns, and set down the whole amount of the last column.
- 53. As in the former case, the best way of proving the correctness of the result is by adding from the top line downwards.
- 54. In adding numbers, the pupil should be always taught to add without repeating the sum each time a new figure is added.

Ex.—Add together 869, 4931, 2687, 1072.

	869	
	4931	
	2687 1072	
Ans.	9559	

Beginning at the right, we say 2 and 7 are 9, and 1 are 10, and 9 are 19, instead of saying, 2 and 7 are 9. 9 and 1 are 10, 10 and 9 are 19.

4. Fi

5. Fi

6. Fi

7. Fir 845 8. WI

9. WI 10. Ada II. Wh 12. Fin 13. If 8 and wha 14. Add 15. Add (1 3480 2724 5306 1098 6930 7645 2336 4284 3897 2100. 76080 63621 25373 25160 57545 80772

93004 17417

62624 34273

68.

After placing down the 9 units we carry the x ten, and begin to add the second column in the same way, saying, 1 and 7 are 8, and 8 are 16, and 3 are 19, and 6 are 25, and so on for all the columns.

EXERCISE 8.

I. Add t	ogether:			
(1)	(2)	(3)	(4)	(5)
756	425	127	106	6204
895	143	341	341	2413
7 ⁸ 4	231	210	121	1231
(6)	(7)	(8)	(9)	(10)
7856	276	748	4681	36487
8943	483	249	7362	10462
6789	874	838	8428	38420
4584	965	749	1697	79549
(11)	(12)	(13)	(14)	(15)
417	251	4376	5438	59763
819	432	8231	7846	47
234	846	2343	829	8623
846	735	5678	9731	437
721	897	658	96	24675
(16) 749831 8632 54317 432613 48 460 Find the	(17) 12734 63741 32347 87698 37 794	(18) 3786 97643 278 89784 3264 1640	(19) 8763 48694 7687 24 89643 159	(20) 1379463 207839 999 7638 72109 367294

2. Find the sum of 79 + 863 + 900832 + 8632 + 473423 + 7

3. Find the sum of 12+36701+10+9+8764+99910.

250 0 - 1		ADDII	ION.	27	
are 9, and 1 are 5, 2 and 7 are 9,	4. Find the	sum of agona	1 . 1 6 . 1 0.		
, ~ and 7 are 9,	5. Find the	sum of 789632	++++07+879002	+876+970.	
arry AL	J. Turd ture	50111 01 98032 + 71	308-1822-1 07 1	10000 1 . 0	
arry the r ten,	a a a a a a a a a a a a a a a a a a a	sum of 1324-	-4354653+12+	876+07842-1	
n the samo way, nd 3 are 19, and					
s.	7. Find the	sum of 98673 +	- 10370634 + 0	+ 061700 1	
	8. What is t	he sum of 824780	5+70+876245	2701016	
	9. What is t	he sum of 34688	2 6 6 7 9 7 0 7 0 3 4 5 +	37341+0327	
	10. Add 181.4	01 1 8	+037+423+98	³ 976+ <u>3</u> 8?	
	101 Had 1014	-24+897156+88	31 + 71512.		
(5) 6204	II. what is th	e sum of $82 + 87$	3+93+9+82468	3+10002012	
2413		$\frac{111}{3247} + 86$	$1302 \pm 81 \pm 0.070$		
1231					
	and this s	um be added to be the total sur	the sum of 8	in to 389727,	
(10)	what will	be the total sur	?	and 932016,	
36487	14. Add togetl	ier the answers	in question		
10462	15. Add togetl	Art	in questions 3,	7, 9, 10, 12.	
38420	(1)				
79549	348037	(2) 460375	(3)	(4)	
	272465	841681	963172	849652	
(15)	530634	239724	300725 463248	361728	
59763	109871	763256	721003	412381	
47 8623	693036	437891	387356	635403	
437	764543	825432	241653	872545 406223	
24675	233638 428432	285678	603280	294867	,
	389763	310720	532176	811236	ł.
(20)	210045	403521. 687489	278321	576037	
379463	760806	324061	829248	213744	
07839	636215	530724	171320	764368	
999	² 53734	623452	206782 461027	305216	
7638	251600	487638	589203	436720	
72109	575453	290731	248639	823284	
67294	807720	803256	730461	217436	
	930045 174173	731463	672398	592301 243762	
473423+7	626245	379574	246175	739445	
	342734	823156	928340	429374	
-99910.	51-754	928348	731629	684569	
					·

ADDITION.

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 17. In one year, a farmer made by his horses \$364, by h for the cows \$785, by his slicep \$1064, by his pigs \$184, 1 at his corn \$304, by his hay \$97, and by his oats \$40 ag. An what did he make in all? 18. One shepherd has 327 sheep, another has 25 more that he: how many have both? 19. By selling a farm for \$6478 the owner lost \$2734 as years old? 20. James was born in 1856: in what year will he be years old? 21. The first of three numbers is 398, the second is 67 more than the first, and the third \$25 more than the second find the sum of the three. 22. A grocer lost \$957, and had left \$5635: how much having lost that sum? 23. Commencing with 324, what is the sum of all the num bers below 335? 24. The population of a village was 1527, the next year it gained 421, the second year 923, the third year \$45 the fourth 1760, the fifth 1099: what was the populat \$34. A m \$642 to an the end of the fifth year? 25. A man left his estate to his wife, two sons, and three and each daughter \$3784: what was the value of the end of the fifth year? 26. A. owns a farm worth \$8920, three horses worth \$15 as for the each, a pair of oxen worth \$98, five cows worth \$22 to an the property? 27. Washington word \$25 the property? 	E CONVATERS.
 18. One shepherd has 327 sheep, another has 25 more that he: how many have both? 19. By selling a farm for \$6478 the owner lost \$2734 20. James was born in 1856: in what year will he be years old? 21. The first of three numbers is 398, the second is 67 more than the first, and the third \$25 more than the second find the sum of the three. 22. A grocer lost \$957, and had left \$5635: how much having lost that sum? 23. Commencing with 324, what is the sum of all the num bers below 335? 24. The population of a village was 1527, the next year it gained 421, the second year 923, the third year 845 the fourth 1760, the fifth 1099: what was the population at the end of the fifth year? 25. A man left his estate to his wife, two sons, and three daughters. His wife received \$9527, each son \$5726 and each daughter \$3784: what was the value of the how hele estate? 26. A. owns a farm worth \$8920, three horses worth \$15; so first each, a pair of oxen worth \$1832: what is the total \$25. Washington worth \$15. \$25. Five apiece, and sheep worth \$1832: what is the total \$27. Washington word in the second \$16. \$16. \$25. \$16. \$25. \$16. \$25. \$25. \$25. \$25. \$25. \$25. \$25. \$25	17. In one year, a farmer made by his horses \$364, by h cows \$785, by his sheep \$1064, by his pigs \$184, b his corn \$304, by his hay \$97, and by his oats \$46 29. An what did he make in all?
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 20. James was born in 1856: in what year will he be years old? 21. The first of three numbers is 398, the second is 67 more than the first, and the third 825 more than the second find the sum of the three. 22. A grocer lost \$957. and had left \$5635: how much having lost that sum? 23. Commencing with 324, what is the sum of all the num bers below 335? 24. The population of a village was 1527, the next yea it gained 421, the second year 923, the third year 845 tion at the end of the fifth year? 25. A man left his estate to his wife, two sons, and three daughters. His wife received \$957, each son \$5726 and each daughter \$3784: what was the value of the forth whole estate? 26. A. owns a farm worth \$8920, three horses worth \$15 as for the value of his property? 27. Washington was the sum of his property? 	19. By selling a farm for \$6478 the owner lost \$2734 what did it cost at first?
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 24. The population of a village was 1527, the next yea it gained 421, the second year 923, the third year 845 the fourth 1760, the fifth 1099: what was the popula 34. A m function at the end of the fifth year? 25. A man left his estate to his wife, two sons, and three daughters. His wife received \$9527, each son \$5726 and each daughter \$3784: what was the value of the whole estate? 26. A. owns a farm worth \$8920, three horses worth \$15 as for the how each, a pair of oxen worth \$1832: what is the total value of his property? 27. Washington was interpreted and the second second	23. Commencing with 324, what is the sum of all the num 33. Three
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 26. A. owns a farm worth \$8920, three horses worth \$15 apiece, and sheep worth \$98, five cows worth \$25 first value of his property? 27. Washington wash 	25. A man left his estate to his wife, two sons, and three daughters. His wife received \$9527, each son \$5726 as for whole estate?
27. Washington many the f	 26. A. owns a farm worth \$8920, three horses worth \$15 35. Five p apiece, and sheep worth \$98, five cows worth \$2 35. Five p first of state of his property?
did he die?	7. Washington was born in 1732, and Napoleon 36 years the fin later; Napoleon died at the age of ranking 36 years
than	than t

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ADDITION.

- and 247 pear tree
- horses \$364, by h y his pigs \$184, b

sons, and three

each son \$5726

he value of the

ses worth \$15

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t is the total

ash, 639 beech, 1828. The population of a certain city was 23000 in the year 1845; in the next five years it gained 5630; in the next five, 8763; in the next 16420; in the next, 22109: how many inhabitants had it at the end of the latter time?

29

- d by his oats \$46 29. An army consists of 6450 cavalry, 27846 artillery, and 270874 more infantry than both cavalry and artillery : er has 25 more tha how many men were there in the army?
- 30. A. has \$5786; B., \$6724; C., \$10536; D. as much as owner lost \$2734 A. and C.; E. as much as A., B., and D.; F. as much as all the rest : how much have they in all?
- year will he be 4 31. A. has \$84; B. has \$23 more than A.; C. has as much as A. and B.; and D. as much as A., B., and C. together: how many dollars have they in all? second is 67 mor
- than the second 32. A. deposits his money in five banks; in the first he has \$897, in the second \$673, in the third as much as in the first and second, in the fourth as much as in 5635: how muc the second and third, and in the fifth as much as in \$957 instead c all the others: how much money has he deposited in all P
- n of all the num 33. Three men enter into partnership; the first man puts \$3845, the second \$2375, and the third puts in \$585 more than the sums put in by the other two: what 7, the next yea sum did they all put in? third year 845
- vas the popula 34. A man builds seven houses; for the first he receives \$647, for the second \$799, for the third \$949, for the fourth \$1467, for the fifth \$1986, for the sixth as much as for the first and fourth, and for the seventh as much as for the third and fifth : how much does he receive for building the sixth and seventh respectively, and how much for building them all?
 - 35. Five persons deposited money in the same bank; the first deposited \$5987, the second \$12980, the third \$65973, the fourth \$37345, and the fifth as much as the first and second together: how many dollars did they all deposit?
- in what yea 36. The first of four numbers is 3125, the second is greater than the first by 5108, the third is equal to the sum of

TRS.

the first and second, and the fourth is equal to sum of the third and first : what is the sum of the f numbers?

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- 37. The ship Orient sailed from Marseilles to Buenos Ay distant 6375 miles, thence to Valparaiso 2764 mi thence to San Francisco 6346 miles, thence to Sandwich Islands 2152 miles, thence to Melbou 5588 miles, thence to Yokohama 5434 miles, the to Calcutta 5115 miles, thence to Bombay 2257 mil thence to Suez 2006 miles, and thence back to M seilles 1314 miles: what was the entire distar sailed?
- 38. Find the sum of four hundred and three; 5025; si thousand and seventy; eighty-seven thousand; 20 one hundred and three.
- 39. Find the sum of 2050; three hundred and seventy th sand and two hundred; four million and five; two r lion, ninety thousand, seven hundred and eighty; hundred thousand and seventy; 98002; seven milli nine thousand and one; 70070.
- 40. Find the sum of two hundred thousand, two hundred three hundred million, six thousand and thirt seventy million, seventy thousand and seventy; n 55. By Ac hundred and four million, nine thousand and for 55. By Ac eighty thousand; ninety million, nine thousand; hundred thousand and sixty; five thousand, sev hundred; four million, twenty thousand, eight hu dred and twenty.
- 41. Find the sum of all the different numbers you c make by using all the figures :

(1) (2) (3)	3.			ο.	
(2)	3,	8,	9.		
(3)	7,	9,	о,	о.	

- 42. Add together all the different numbers of five figur each number beginning with 375, and ending with 57. The g
- 43. Lily has 17 roses; Laura has 11 more than Li Charles has 18 dahlias more than Laura has ros and Jennie has 14 dahlias more than Charles: h many dahlias has Jennie?

44. He: 43 1 cen Sar

45. Ma Ma tha Tan pen

- 46. Hei to ' had
- 47. A r how of 5

48. Joh 40 3 ther

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nore than Li aura has ros n Charles ; h

SUBTRACTION.

- 44. Henry's purse contains 329 cents; Edward's contains 43 more than Henry's, and Henry's contains as many cents as Sarah's, less 94 cents : how many cents does Sarah's purse contain?
- 45. Mary bought a pencil for which she gave 95 cents; Maude bought one for which she gave 13 cents more than Mary; and Maude's pencil cost as much as Jane's, less 23 cents : what was the cost of Jane's pencil?
- 46. Henry lends \$913 to Thomas, \$473 to Samuel, \$576 to Theodore, and has \$576 left : how many dollars had he at first?
- 47. A man was 37 years old when his son was born: how old will he be, when his son has reached the age of 59?
- 48. John throws a ball 30 yards up the road, and another 40 yards down the road : how far must he walk to bring them both back again?

SUBTRACTION.

- nd seventy; n 55. By Addition we find that 7 units and 4 units make 11 units. We will now find what 11 units become when 4 units are taken away. If I of the 4 units be taken from 11, the result will be 10; if 1 of the remaining 3 units be taken from 10, there will be 9 units left. Again, take 1 of the remaining 2 units from the 9 and 8 will remain; and, finally, take the 1 remaining unit from 8 and we have 7 units left. Thus we see, that if 4 be taken from 11 there will be 7 left.
 - 56. This process of finding the number of units left after taking a certain number from a greater number is called Subtraction.
- a ending with 57. The greater number, as the 11 in the above example, is called the Minuend, and the lesser, as the 4 above, is called the Subtrahend. That which is left, as the 7 above, is called the Difference, Remainder, or Excess.

- 58. This operation is expressed by placing a sign between 60. The the two numbers. The sign - is called Minus. Thus, 10 - 3 = 7.

This is read :- Ten minus three equal to 7, and means that if 3 units be taken from 10 units 7 units will be left. Here to is the Minuend, 3 is the Subtrahend, and 7 is the Remainder.

59. The following cable should be perfectly understood and remembered by the pupil:

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1	4	"	8	.	14	"	7 8	I	-	"	7	I	5	"	7	1	7	"	7	
	5	"	9		-5 :6	"	-	10	-	"	8	ľ	7	"	8	I	8	**	8	
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4				1	7		10	18		"	10	Ig)	"	10	20	-	"	10	
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SUBTRACTION TABLE.

TFACHER -- Drill the pupils thoroughly in this table by asking questions in every possible form.

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- 4. Ho
- 5. Ho
- 6. Fiv
- 7. Six
- 8. Ho
- q. Ho
- 10 WI
- 11. WI
- 12. Sut

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nderstood and

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		"	1	1.1
1 7	,	"	2	
8	, ·		3	
9		"	4	1.1
10	•	•	5	
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is t	able	b	y	() La la

sign - between 60. The following method will teach pupils to be quick at subtracting numbers, and should be practised aloud as well as on the slate or paper:

Ex. 1.-Subtract by 2's from 19 to 1.

Result.-- 19, 17, 15, 13, 11, 9, 7, 5, 3, 1.

Reason.-2 from 19 leaves 17; 2 from 17 leaves 15, etc.

Ex. 2.—Subtract by 3's and 2's, one after the other. from 31 to 1.

Result.-31, 28, 26, 23, 21, 18, 16, 13, 11, 8, 6, 3, 1.

Reason.-3 from 31 leaves 28; 2 from 28 leaves 26; 3 from 26 leaves 23; 2 from 23 leaves 21, etc.

Compare these results with Art. 44, and notice that Subtraction is exactly the converse or opposite of Addition.

EXERCISE 9.

These questions should be solved mentally.

- 1. If John is 15 years old and George is 6, what is the difference in their ages?
- 2. How many are 16 cents 7 cents?
- 3. How many are 18 dollars 5 dollars?
- 4. How many are 14 6? 16 4? 12 5?
- 5. How many are 18 8? 20 6? 21 4?
- 6. Five balls taken from 11 balls leave how many?
- 7. Six cents from 20 cents leave how many?
- 8. How many are 7 5? 17 5? 27 5?
- 9. How many are 9 6? 19 6? 29 6?
- 10. What number added to 8 will make 12?
- 11. What number and 9 make 13? 14? 15? 10?
- 12. Subtract by 2's from 24 to 0.

In the same manner, subtract

in the same manner, subtract	
13. By 2's from 25 to 1. 14. By 2's from 31 to 2. 19. By 4's from 41 to 1.	• 40. Geo spe
15. By 3's from 30 to 0. 20. By 4's from 51 to 3. 16. By 3's from 37 to 1. 21. By 5's from 60 to 0. 17. By 3's from 40 to 4. 22. By 5's from 63 to 3. 23. By 6's from 66 to 0.	41. The and the:
25. Count by 4's from 2 to 58, and back from 58 to 2.	42. Tal man
20. Count by 5's from 1 to 61, and back to 1.	43. Mar olde
27. Count by 6's from 3 to 69, and back to 3.	44. A n it a
28. Count by 4's from 5 to 53, and back to 5.29. Count by 6's from 7 to 67, and back to 7.	moi
30. What is the difference between nine dollars and fifteer dollars?	45. Jam gav had
31. A man earned fifteen dollars one week, and spen seven dollars: how much had he left?	46. A b afte
32. A man has two sons, one fourteen years old, the other eight: what is the difference between their ages ?	47. Joh mot
33. Take nine yards from thirteen yards: how many yards remain?	mai 48. A
34. A man had sixteen dollars: he spent eleven dollars of it for a dictionary, and the remainder for paper: what did the paper cost?	doll he 49. A 1
35. A woman carried eighteen dozen eggs to market; she broke seven dozen, and sold the rest: how many did she sell?	son dol hov
36. William bought sixteen marbles, and he gave his brother seven of them: how many did he keep?	61. To su
37. Mary had fifteen examples to work out: after finishing nine, how many had she then to do?	the
38. Take seven books from thirteen books: and how many will remain?	nor san
39. A. merchant had nineteen barrels of flour; he sold twelve barrels, and kept the rest: how many did he keep?	62. Henc ber uni tho

- s from 41 to 1. s from 51 to 3.
- s from 60 to 0. s from 63 to 3.
- s from 66 to 0.
- s from 65 to 5.
- om 58 to 2.
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- lars and fifteer
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- w many yards
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- market; she ow many did
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- d how many
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- 40. George had seventeen cents; he lost nine cents, and spent the rest for ink: what did the ink cost?
- 41. There were fourteen books on one shelf of a book-case, and eight on another: how many more books were there on one shelf than on the other?
- 42. Take eight cherries from fifteen cherries: and how many will remain?
- 43. Mary is sixteen years old, and Jane seven: how much older is Mary than Jane?
- 44. A man sold a cart for eighteen dollars; he received for it a barrel of flour worth nine dollars, and the rest in money: how much money did he receive?
- 45. James's father gave him ten cents, and his mother gave him nine: after spending eight cents, how much had he left?
- 46. A boy had thirteen marbles; he bought five more, and afterwards lost ten: how many had he then?
- 47. John had eight books, his father gave him five, his mother two; he then gave four to his brother; how many had he left?
- 48. A man had sixteen dollars; he gave away seven dollars and afterwards earned nine: how much had he then?
- 49. A merchant bought some cloth for nine dollars, and some silk for five dollars; he sold both for sixteen dollars: did he gain or lose by the bargain: if so, how much?
- 61. To subtract one number from another they must be of the same kind.

"Im-5 dollars from 8 apples leaves neither 3 dollars nor 3 apples. In the same way, 3 units from 7 thoucands leaves neither 4 units nor 4 thousands.

62. Hence when we subtract, we should always write numbers of the same kind in the same column, that is, units under units, tens under tens, thousands under thousands, etc.

63. We thus have the following

RULE FOR SUBTRACTION.

- 1. Write the numbers to be subtracted, the less under the greater, placing units under units, tens under tens, etc., and draw a line underneath.
- 2. Begin at the right, and subtract each figure from the one above, placing the result under the figure subtracted.
- 64. To test the result, add the Subtrahend, or middle number, to the Difference, or lower number, and if the work be correct the sum should be the same as the Minuend, or upper number; or, subtract the lower number from the upper, and the result should be the same as the middle number.

Ex. 1.-Subtract 238 from 749.



Difference 5 I I

- We place the numbers, units under units, tens under tens, and hundreds under hundreds. Then begin at the units' column and say: 8 units from 9 units leaves 1 unit, and we write the 1 under the units' column. Then 3 tens from 4 tens leaves 1 ten, and we put the 1 under the ten's column. Then 2 hundreds from 7 hundreds leaves 5 hundreds, and we place the 5 under the hundreds' column. The answer being 511.
- In practice we shorten the work thus: 8 from 9 leaves 1; 3 from 4 leaves 1; 2 from 7 leaves 5; leaving altogether 511.
- To prove the correctness of the work, we add 238 to 511 and obtain 749; or we may subtract 511 from 749 and obtain 238.

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The reason for this is as follows: 4 from 9 leaves 5; and if we add the 4 back again to the 5, we must obtain the 9 we had at first.

Again, if 4 taken from 9 leaves 5, the pupil will easily see that 5 taken from 9 must leave 4.

Hence the proof of the work.

Ex. 2.—Find the difference between 3065 and 78195.

78195	
3065	

75130

Here 5 from 5 leaves 0, which is placed under the units' column; 6 from 9 leaves 3 under the tens' column; o from 1 leaves 1 under the hundreds' column: 3 from 8 leaves 5 under the thousands' column; o from 7 leaves 7 in the ten-thousands' column.

EXERCISE 10.

(1)	(2)	(3)	(4)	(5)	(6)
469	5642	9874	8072.	2741	5462
327	4130	3623	3051	1301	1350
(7) 6408 3207	8420 87	0) (10) 742 783 331 542	9 1243		(13) 86493 34272
(14) 972897 120341	(15) 985094 382040	(16) 9876578 1234569	899 997		(18) 9892976 4730834
(19)	(20)	(21)	(22)	(23)	(24)
75853	89487	75659	87392	75 ²⁸ 5	88456
45213	32315	32417	43181	43151	32142
(25)	(26)	(27)	(28)	(29)	(30)
546875	347985	973856	825944	756345	914756
513213	323415	951231	812512	713125	902314

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(31)	(32)	(33)	(34)	(35)	(36)	54. Two
41876	38789	64187	918764	187137	59123	nish
31023	13321	33123	312311	123013	32122	55. The
(37) 418764 213321	(38) 13912 13311	(39) 67134 32132	(40) 67183 21033	(41) 91276 21230	(42 41876 31232	55. The and pro- 56. The and

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- 43. A boy had 36 marbles and gave 24 of them to his playmate: how many had he remaining ?
- 44. Joseph caught 295 quail, and John caught 184: how many more did Joseph catch than John?
- 45. Wilson had \$6847, and Joseph \$2437 : how much more had Wilson than Joseph ?
- 46. Thomas having 447 bushels of potatoes, sold 234 bushels of them to Perry: how many bushels had Thomas remaining?
- 47. A farmer bought a span of horses for \$346, and a yoke of oxen for \$135: how much more did he give for the horses than for the oxen?
- 48. A drover having 1465 sheep, sold 1235 of them: how many had he remaining?
- 49. A gentleman owns a store worth \$4695, and a gristmill worth \$2135: how much more is the store worth than the grist-mill?
- 50. A gentleman gave for a house and lot \$9399, and for a cotton factory \$8495: how much more did he give for the one than for the other?
- 51. A speculator bought some land for \$12897, and a tannery for \$10444: how much more did the land cost than the tannery?
- 52. A merchant, having 9847 yards of cloth, sold 5844 yards of it: how many yards had he remaining?
- 53. A drover bought cattle to the amount of 9647 dollars, and sheep to the amount of 5434 dollars: how much more did he give for the cattle than for the sheep?

(35)	(36)
87137	59123
23013	32122
(41)	(42
)1276	4187t
1230	31232

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647 dollars, how much sheep?

- 54. Two men jointly built a mill for 7856 dollars; one furnished 4520 dollars: what did the other furnish?
- 55. The earnings of a factory for a year were 45689 dollars, and the expenses were 21352 dollars: what were the profits?
- 56. The gross receipts of a railroad were 357845 dollars, and the running expenses for the same time were 213423 dollars: what were the net earnings?
- 57. A. has a grist-mill worth 1875 dollars, and a saw-mill worth 1032 dollars: how much more is the one worth than the other?
- 58. A farmer had 3672 sheep and 2312 lambs: how many more sheep had he than lambs?
- 59. A man was driving 534 geese to market, and on the way had 21 stolen from him : how many had he remaining?
- 60. A farmer had 327 bushels of oats, and sold 125 bushels of them: how many bushels had he remaining?
- 61. A merchant in one year sold 18972 barrels of flour and 7370 barrels of sugar: how many more barrels of flour did he sell than sugar?
- 62. A ship is valued at 54789 dollars, and its cargo at 40357 dollars: how much more is the ship valued at than the cargo?
- 63. A gentleman having 577897 dollars, gave to his eldest son 16805 dollars: how much had he remaining?

65. In all the former examples, the figures of the larger number were either greater or equal to the corresponding figure in the lesser number. We will now consider those cases in which the figures of the larger number may be less than the corresponding figures of the other.

Ex.-Subtract 695 from 932.

 $93^{2} = 900 + 30 + 2$ hundreds. tens. units. = 9 + 3 + 2

In the same way,

695	hu ==	udra 6	oris.	tons.		units
71		~		9	+	5
The numbers	then	st-	and .			

Now, we cannot take 5 from 2 units, hence we increase the latter by 1 ten or 10 units, thus making it 12 units; then 5 units from 12 units leaves 7 units, which we place as usual. Again, since we took 1 of the 3 tens to add to the 2 units we must have only 2 tens left from which to take the 9 tens, and here, since we cannot take 9 from 2, we must take 1 of the 9 hundreds or 10 tens and add it to the 2 tens, making 12 tens. Then 9 tens from 12 tens leaves 3 tens, which we place as usual. Again having taken 1 hundred from the 9 hundreds, we can have only 8 hundreds left, and since we can take the 6 hundreds from the 8 hundreds we do so, and place the 2 hundreds as usual.

The work may be shown thus :

695 =	т. + 3 +	v. = 9 + 2 = 9 + 3	T. U.			
$^{237} =$	•	•		= 2 +	2 1	

- 66. By another method, it is usual to add one, when necessary, to the figures of the Subtrahend, instead of taking one away from the figures of the Minuend.
 - In the previous example, instead of saying 9 tens from 12 tens leaves 3 tens, we say 10 tens from 13 tens leaves 3 tens, which gives the same result; and instead of saying 6 hundreds from 8 hundreds, we say 7 hundreds from 9 hundreds, so that we only change the figures of the Subtrahend.
- 67. This system, known as carrying one, is done mentally while working a question in Subtraction, and depends

on the of the 68. We the

> 1. Writ units,

2. Subtr one a

3. If an add 1 by 1 as bej

PROOF.

a)

(26 7322 2413

4324

on the fact that r unit of any order is equal to ro units of the next order to the right of it.

68. We thus have the following

RULE FOR SUBTRACTION.

- 1. Write the less number under the greater, placing units under units, tens under tens, etc., and begin at the right to subtract.
- 2. Subtract, if possible, each figure in the lower line from the one above it, and set the remainder below.
- 3. If any figure in the lower line is greater than the one above it, add 10 to the upper figure before subtracting, and diminish by 1 the next left-hand figure in the upper line, and proceed as before.
- **PROOF.**—Add the remainder to the subtrahend; the sum should be equal to the minuend.

(2) 976 53 I	(3) 704 483	(4) 1806 7-0	(5) 57 ² 259
(7)	(8)	(9)	(10)
		400500	4236 3089
445	20371	213327	
(12)	(13)	(14)	(15)
4360	5491	6180	4192
3451	4542	2435	1435
(17)	(18)	(19)	(20)
927381	917183	618190	519080
345432	421354	234221	324121
(22)	(23)	(24)	(25)
			423453
443544	232154	135212	141514
(27)	(28)	(29)	(30)
734271	826041	46095	555555
241342	434425	28736	123456
	976 531 (7) 7580 4245 (12) 4360 3451 (17) 927381 345432 (22) 705180 443544 (27) 734271	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$

EXERCISE 11.

hence we inus making it aves 7 units, we took 1 of have only 2 of here, since e 1 of the 9 tens, making saves 3 tens, taken 1 hunonly 8 hunndreds from hundreds as

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one, when instead of inuend. og 9 tens s from 13 esult; and ds, we say ly change

mentally depends

	42 ARITHMETIC FOR BEGINNERS.	
	(b) I From Sand A	18
	(b) 1. From 854 take 578.	
1	2. From 1799 take 1732.	(7) 1. From
	3. From 5496 subtract 1492.	2. From
diff. for	4. From 1584 subtract 920.	3. From
1	5. From 5672 subtract 2356.	dred
j	6. From 74760 subtract 39817.	4. From
and the second	7. From 8416 subtract 2918.	5. Fror
ł	8. From 30811 subtract 13240.	6, Fror
	9. From 27880 subtract 9226.	
and the second s	10. From 35846 subtract 12829.	7. From
, majo	11. From 75901 subtract 17980.	8. From
	12. From 37229 subtract 17991.	9. Fron
	13. From 100304 subtract 62818.	Io. Fron
	14. From 1000302 subtract 888772.	11. Fron
and the second se	$-J_{1} + 10441 002201 \text{ subtract}$	12. Wha
1	16. From 1000000 subtract 300998.	12
1.	(c) Find the value of	13. How
	1.758901 - 349806. 23 802460	14. How
	2.329500 - 54650	15. How
	4. $10000 - 200$	16. How
	5. $189501 - 188607$ 20. $7405676 - 567456$	17. From
1	0.75035 - 24310	18. The l
	7. 786. $9000 - 17664509$ $20. 780023 - 320412.$	what
	3/0420010 - 820710077 - 433/4	
	9. $97001 - 50077$. 10. $76734 - 977$. 30. $700 - 2$. 31. $8004 - 7008$. 32. 81040	
	11.56100 $32.830240 - 270128$	
	12.700000 - 00. $33.03001 - 38994$	
	13.5700 - 500, $34.733124 - 291431$.	
	14.9777 - 89. $35.70800 - 8004.$	
	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	1. Mr. 4
	17,230400 - 87040 - 300,11247003 - 4612278	sheer
1	18.349130 - 04131 $39.70001 - 7.$	2. How
	19,400500 - 80072	Amer
1	20.739745 - 76275 $42.40321 - 198372$	3. A. bo
1	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	remai
	$44.\ 100010110 - 999991.$	4 A. pu
	99 991	\$4790
	·	

(r) 1. From 65 million take 650 thousand 980.

2. From nine hundred thousand take five hundred and 50.

- 3. From 12 million 12 hundred take 400 thousand 4 hundred.
- 4. From 280 million and 11 take 24 million 650 thousand.
- 5. From twelve hundred and ninety take seventy-five.
- 6. From 6 hundred million take 500 million 5 hundred.
- 7. From six hundred and 48 take one hundred and 70.
- 8. From 460 million and 10 take 920 thousand 750.
- 9. From 1 million and 20 take 960 thousand.
- 10. From 756 million 3 thousand take 657 million and 8.
- 11. From six hundred and 90 take seventy-five.
- 12. What is the difference between 900000 and 123454?
- 13. How much larger is 38607 than 3867?
- 14. How much smaller is 34730 than 38607?
- 15. How much must be taken from 2483 to leave 391?
- 16. How much must be added to 2032 to make 2483?
- 17. From 7630005 take 3270006.
- 18. The larger of two numbers is 10640 and the less 9535 : what is their difference?

EXERCISE 12.

- 1. Mr. A. had 350 sheep in two lots; in one lot were 175 sheep: how many were in the other?
- 2. How many years have elapsed since the discovery of America in 1492?
- 3. A, borrowed from B. \$9780, and paid \$2176: how much remained due?
- 4 A. purchased a farm for \$10000, and paid thereon \$4790 how much remained due?

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30012. 98372. 23679.

- 990991.

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 5. B. bought merchandise which he sold for \$11275, a made thereby \$2114: what was the cost price? 6. In 1870 the population 	1	
6. In 1870 the population of	21.	If I boof it:
7. The sum of two numbers is 9427, and the greater 5825: what is the less number 2.	22.	A man part i much
8. The minuend is 57, the subtrahend is 27: what is the remainder?	23.	The 95000
9. The minuend is 67, the remainder is 20: what is t		24000 moon
10. The subtrahend is 12, the remainder is 18: what the minuend ?	24.	If I b what
11. A gentleman gave to his son \$3862, and to his daug ter \$5324: how much more did he give to his daug ter than to his son?		A gen the ho of the
12. In an orchard there are 425 apple-trees, and 297 plus- trees: how many more apple-trees are there the plum-trees?	26.	A lum feet o
13. A man travelled 14637 miles during one year and 98. miles the next year: how much farther did he trav the one year than the other?	27.	The b the P what
14. A merchant had area and a	28.	A man had h
15. A speculator hought	29.	A mer and c
16. A man owning 45761 acres of land, sold 23927 acres it : how many acres had he remains and 23927 acres	30.	If two 73462 how r
of them : how many had be remaining a sold 492t	31.	One p 50914
more than it had the more h	32.	the or Moun
19. A merchant sold a quantit		and 2 how 1
they cost him?	3 3·	Bonaj when
20. A man having 21695 feet of umber, cold 7962 feet a it : how many feet had he remaining ?	24	born i Sir Is
in comanning (SIE 18

part is cultivated; the former part is 125 acres: how

9500000 miles; the distance to the moon is about 240000: how much farther is it to the sun than to the

23. The distance from the earth to the sun is about

of it: how much remains unpaid?

much is the latter?

moon?

old for \$11275,a he cost price? 1. If I borrow of my neighbour \$9673, and pay him \$999

egain in 10 year 22. A man has a farm of 400 acres; part is woodland, and nd the greater

- s 20: what is t
- er is 18: what
- 24. If I bought a ship for \$42650, and sold it for \$49000: what did I gain?
 - 25. A gentleman gave \$12462 for a house and some land ; the house alone was worth \$9375: what was the value of the land?
 - 26. A lumberman having 650000 feet of boards, sold 162372 feet of them : how many feet then remained?
 - 27. The battle of Inkermann was fought in the year 1854; the Peninsular War was begun 46 years before this : in what year did the latter war begin?
 - 28. A man having \$100000, gave away \$365: how much had he left?
 - 29. A merchant owns property to the amount of \$45563, and owes \$21209: how much is he really worth?
 - 30. If two candidates for office received in the aggregate 73462 votes, and the successful one had 45309 votes: how many did the other have?
 - 31. One province contains 55405 square miles, and another 50914 square miles : how many more square miles does the one contain than the other?
 - 32. Mount Sorata, in South America, is 24812 feet high, and 21241 feet higher than Mount Snowdon, in Wales ' how high is Mount Snowdon?
 - 33. Bonaparte was declared emperor in the year 1804, when he was 35 years of age: in what year was he born?
 - 34 Sir Isaac Newton was born in the year 1642, and died in 1727: how old was he when he died?

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FOR BEGINNERS.	
 35. Glass windows began to be used in private houses England in the year 1180, which was 516 years a what year was the discovery of glass made? 36. Gunpowder man 	f
 37. Find a number to which, if thirty-four thousand thr hundred and twenty-six be added, the result will 	9. The in cor tha
feet high : how much higher is it than Mount Etna Sicily, which is 10050 foot higher is it than Mount Etna	In th giv
39. Sorata, the highest land in America, is 24812 feet high how many feet higher is it than Mount Ararat who is 17000 feet high?	by by Agair
40. The highest land in North America is Mount St. Elia which is 15000 feet high, and this mountain is 8711 feet higher than Mount Washington in New Haus shire: how high is Mount W	as s 70. This nar
41. St. Peter's Church at Rome, which is 450 feet high, i 157 feet higher than St. James' Cathedral, Toroute what is the height of the Games' Cathedral, Toroute	I 2 3 4
more than he willed to his sons \$17496, which was \$3820 he will to his daughters : how much di	4 5 6 7 8
 43. A man owning 25721 acres of land, sold 19395 acres of it: how many acres had he remaining? 44. A merchant having 78004 barrels of flour, sold 49726 45. Is the many barrels had he remaining? 	9 10
and the latter To and the latt	12 Again
James has won 17 marbles from John?	I 2 In the
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MULTIPLICATION.

59. The numbers that were added together in the examples in Addition were nearly always different. We now come to a short method of adding together numbers that are the same.

Ex. 3+3+3+3=12.

In this example we have the number 3 taken 4 times, giving 12 as the sum; but instead of finding this sum by the usual process of addition, we obtain the same by saying 4 times 3 are 12.

Again, 5+5+5+5+5+5=30, which result is the same as saying 5 taken 6 times gives 30, or 6 times 5 are 30.

70. This produces a Table, which may be obtained by ordinary Addition, for

	I	+	I	=	2			or	twice	I	are	2
	2	+	2	=	4				"	2	64	4
	3	+	3	-	4 6					3	""	4 6
		+	4	=	8				66	4	"	8
	4 5 6	+	5 6	=	10				**	56	"	10
	6	+	6	=	12				**	Ğ	"	[2
	7 8	+	7	=	14				**	7	"	14
	8	+	8	=	16				**	7 8	"	١Ġ
	9	+	· 9		18				**	9	"	18
1	10	+	10	=	20				**	10	""	20
	11	+	II	=	22				**	II	" "	22
	12	+	12		24				"	12	"	24
Λg	ain	,										
	1	÷	I	+	I	=	3	or three	times	I	are	3

In the same way four times 6 will be found to be 24; five times 7 will be 35, etc.

71. These results will now be placed in the form of a Table, called the Multiplication Table, which must be accurately memorized by the pupil.

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MULTIPLICATION TABLE.

Once 1 is 1 2 " 2 3 " 3 4 " 4 5 " 5 6 " 6 7 " 7 8 " 8 9 " 9 10 " 10 11 " 11 12 " 12 5 times	Twice I are 2 "" 3 "" 6 4 "" 8 5 "" 10 6 " 12 7 "" 14 8 "" 16 9 "" 18 10 "" 20 11 "" 22 12 "" 24 6 times	3 " 4 " 5 " 6 " 7 " 8 " 9 " 10 " 11 " 30 12	3 1 are 4 4 2 " 8 9 3 " 12 2 4 " 16 5 ' 20 6 " 24 7 ' 28 8 " 32 9 ' 36 10 " 30 10 ' 40 11 ' 44 12 '' 48 '' 10 ''
I are 5 2 '' 10 3 '' 15 4 '' 20 5 '' 25 6 '' 30 7 '' 35 8 '' 40 9 '' 45 10 '' 50 11 '' 55 12 '' 60	1 are 6 2 " 3 " 4 " 5 " 6 " 7 " 48 " 9 " 54 " 10 " 60 11 12 " 72	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{c} 8 \text{ times} \\ 1 \text{ are } 8 \\ 2 \text{ `` 16} \\ 3 \text{ `` 24} \\ 4 \text{ `` 32} \\ 5 \text{ `` 40} \\ 6 \text{ `` 48} \\ 7 \text{ `` 56} \\ 8 \text{ `` 64} \\ 9 \text{ `` 72} \\ 10 \text{ `` 80} \\ 11 \text{ `` 88} \\ 12 \text{ `` 96} \end{array}$
9 times 1 are 9 2 " 18 3 " 27 4 " 36 5 " 45 6 " 54 7 " 63 8 " 72 9 " 81 10 " 90 11 " 99 12 " 708	Io times I are IO 2 " 20 3 " 30 4 " 40 5 " 50 6 " 60 7 " 70 8 " 80 9 " 90 10 " 100 II " 110 I2 " 120	II times I are II 2 " 22 3 " 33 4 " 44 5 " 55 6 " 66 7 " 77 8 " 88 9 " 99 10 " 110 II " 121 12 " 132.	12 times 1 are 12 2 " 24 3 " 36 4 " 48 5 " 60 6 " 72 7 " 84 8 " 96 9 " 108 10 " 120 11 " 132 12 times 12 times

72. Mult the the:

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73. The s by by is t is t

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74. The f ł

> Since rep cen 2 9 b Since 7 d

MULTIPLICATION.

- 72. Multiplication is, then, a short method of Addition, or the art of repeating one number as many times as there are units in another.
 - The number which is to be added or repeated is called the Multiplicand.
 - The number which shows the number of times the Multiplicand is to be repeated is called the Multiplier.

The final result is called the Product.

- 73. The sign of this operation is \times , and is read multiplied by. Thus, $11 \times 6 = 66$, would be read 11 multiplied by 6 equals 66. Here 11 is the multiplicand, for it is the number which is to be repeated six times. 6 is the multiplier, for it shews the number of times the multiplicand 11 is to be repeated. 66 is the product, for it shows the result of repeating 11 six times.
 - The pupil must clearly understand that while the result, 66, is supposed to be remembered from the Table, it may be obtained by adding, in the same way, six 11's together, that is,

11	
II	
II	
II	
II	
11	
-	

66 Ans.

74. The following Mental Questions will test the pupil's knowledge of the Multiplication Table:

Ex.—What will 8 peaches cost at 6 cents apiece? Ans. 48 cents.

Since 1 peach costs 6 cents, 8 peaches must cost 6 cents repeated 8 times, or 8 times 6 cents, which will be 48 cents.

Ex. 2.—If a barrel of flour costs 7 dollars, what will 9 barrels cost? *Ans.* 63 dollars.

Since 1 barrel costs 7 dollars, 9 barrels must cost 9 times 7 dollars, that is, 63 dollars.

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4 times

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2 3 4 5 6 7 8 9	**	4	0 8 6 4	1
7		.5	6	1
5	••	6	4	
)		73	2	
		80	2	
		88		
		90)	
z t	im	~~~	-	
	re	12		
	"	24	1	
	"	26	1	
	6	18	1	
	4	60		
6	•	36 48 60 72	1	
	•	84	1	
61		56	1	

08 20

The product must always be of the same kind a the multiplicand, for it is only the multiplican repeated a certain number of times.

The best practice is to take the different products in th Multiplication Table, and give the numbers that ar multiplied together to produce these products.

Ex.—What numbers give 42? Ans. 6 and 7. What numbers give 108? Ans. 12 and 9.

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7. Re

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12. In 1 the 13. At :

15. If a in 5

COST 14. The the

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44, 63, (b) 1. A (8 q

EXERCISE 18.

(a) I. Copy on your slates and fill out the following:

$7 \times 5 = 3 \times 2 =$	-one wing	:
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	mes 6, and back fro	
Repeat from once 8 to 10 tim	ies 8, and back.	12.
	= 7 minut Later	1000

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2.

3.

5.

MULTIPLICATION.

he same kind i ne multiplican

products in thumbers that ar roducts.

. 6 and 7. . 12 and 9.

wing:

9× 4 = 9× 0 = 10× 5= 12X I = = 01 X 01 IX 9 = 8× 5 = $I \times 3 =$ 2X 2 = 2× 3 = 5× 4 = × 4 = X 5 = X I = × 7 = × 4 = × 5 = X IO =nce 5 to 10

10, 3 times

ck from 10

ck. ck. 6. Repeat from once 9 to 10 times 9, and back.

- 7. Repeat from once 10 to 10 times 10, and back.
- What two numbers produce by multiplication the following numbers: 2, 8, 12, 40, 60, 72, 12, 11, 22, 36, 24, 44, 54, 77, 81, 96, 55, 84, 108, 88, 132, 120, 64, 49, 56, 63, etc.
- (b) 1. A quart of berries makes 2 pints: how many pints in 8 quarts?
 - 2. There are 12 inches in one foot length of rope: how many inches in 9 such lengths?
 - 3. If 1 lemon costs 7 cents, how many cents must you pay for 4 lemons?
 - 4. One gallon contains 4 quarts: how many quarts are there in 11 gallons?
 - 5. One peck contains 8 quarts: how many quarts are there in 7 pecks?
 - 6. What would 12 pears cost at 7 cents apiece?
 - 7. How much would 5 bags of meal cost at 9 dollars a bag?
 - 8. At 10 cents a pint, how much would 8 pints of cherries cost?
 - 9. At 11 cents a pound, how much would 7 pounds of sugar cost?
 - 10. In one week there are 7 days: how many days are there in 11 weeks?
 - 11. At 8 cents a quart, what would be the cost of 7 quarts of berries?
 - 12. In 1 florin there are 45 cents: how many cents would there be in 7 florins?
 - 13. At 3 dollars a bushel, what would 12 bushels of grapes cost?
 - 14. There are 4 gills in one pint: how many gills would there be in 12 pints?
 - 15. If a horse runs 12 miles an hour, how far would he run in 5 hours?

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FOR BEGINNERS.	
16. In one yard there are a first	
pounds of oatmeal?	
10. In one foot there are 12 inches: how many inches in 11 feet?	36. A s lea ma
19. How much would 8 pounds of metal cost at 6 cents a	37. W
20. At 8 cents apiece, how much would you pay for a	38. Th
would 10 boxes hold?	39. Ho
22. If a ton of coal cost o doll	40. If eig
worth? what would 9 ounces of blue he	41. If sev
24. Six feet make a fathom: how many feet would there	42. W
25. If a bunch of grapes costs 7 cents, what would a	43. If
would there he in 12 miles how many furlouse	44. W
27. At 10 cents a gill, how much would 11 gills of wine	45. I b wh
20. In one bushel there are 4 pecks: how many necks are	46. W
29. At 3 cents a box, how many cents must you pay for 7	the
30. There is a mant	75. The
in a row: how many tulips are there in the garden?	rea the

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- how many inches will you ascend in eleven steps? of stairs is eleven inches high:
- 32. If you work eleven examples each day, how many will

33. How many are seven times seven pounds?

34. There are seven days in one week : how many days are

52

MULTIPLICATION.

feet in 8 yards) you pay for c

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lls of wine

pecks are

pay for 7

six tulips arden ? hes high :

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days are

- 35. What will be the cost of seven pounds of raisins at nine cents a pound?
- 36. A sheet of paper can be folded so as to make four leaves: how many leaves will eleven such sheets make?
- 37. What is the cost of eight pounds of soap at seven cents a pound?
- 38. There are twelve inches in a foot : how many inches are there in twelve feet?
- 39. How many inches in eight feet?
- 40. If one barrel of flour costs nine dollars, how much will eight barrels cost?
- 41. If one shot weighs six pounds, what is the weight of seven such shot?
- 42. What is the weight of eight packages of coffee, if each weighs five pounds?
- 43. If one pound of rice costs twelve cents, what is the cost of seven packages of a pound each?
- 44. What is the cost of twelve pair of boots at six dollars a pair?
- 45. I bought eleven pounds of glue at eight cents a pound what was the cost?
- 46. William had six cents; his sister gave him three more, aud his mother gave him seven times as many as he then had: how many did his mother give him?
- 75. The pupil is now supposed to be quite familiar and ready with the Multiplication Table, and we will therefore go on with the different cases that occur in multiplication.
 - First we will multiply any number by a number of one figure, or by any number from 1 to 12.

Ex.-Multiply 3781 by 7.

Multiplicand. 3781 Multiplier..... 7 Product....... 26467

Place the multiplier 7 under the multiplicand 3781, and beg n to multiply from the right, or units' place. 7 times 1 unit are 7 units, which we place in the usual place. 7 times 8 tens are 56 tens, that is 5 hundreds and 6 tens; place the 6 tens in its proper place, and carry the 5 hundreds. 7 times 7 hundreds are 49 hundreds, which, with the 5 hundreds we carried, make 54 hundred, or 5 thousands and 4 hundreds; place the 4 hundreds in its own place, and carry the 5 thousands. 7 times 3 thousands are 21 thousands, and the 5 thousands we carried make 26 thousands, which is placed on the left.

(a) I. M

2. M 3. M

4. M

5. M

6. M 7. M

8. M

9. M

10. M 11. M

12. M

13. M

14. M

15. M

16. M 17. M

18. M 19. M 20. M 21. M 22. M 23. M 24. M 25. M 26. M

27. M

28. M 29. M 30. M 31. M

76. This may be done more easily by neglecting for the time the words units, tens, etc.

Thus: 7 times 1 are 7, put down the 7; 7 times 8 are 56, put down the 6 and carry 5; 7 times 7 are 49, and 5 (carried) make 54, put down the 4 and carry the 5: 7 times 3 are 21, and the 5 (carried) make 26.

The pupil should be satisfied that the same result could have been obtained by Addition, thus:

3781
3781
3781
3781
3781
3781
3781

26467

77. Thus, when the multiplier does not exceed 12, we have

RULE FOR MULTIPLICATION.

Place the Multiplier under the Multiplicand; begin at the units' place, and multiply each figure in the Multiplicand by the Multiplier. Set down the right-hand figure of the product, and carry the left-hand figure or figures, if any, to the next product-just as in Addition,

NULTIPLICATION.

EXERCISE 14.

id 3781, and ts' place. 7 in the usual 5 hundreds place, and are 49 hun. rried, make ; place the the 5 thouds, and the s, which is

(a)

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mes 8 are re 49, and rry the 5;

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a) 1.	Multiply	123 by 2.	32. Multiply 45613 by 4.
2.	Multiply	134 by 2.	33. Multiply 34520 by 3.
3.	Multiply	223 by 2.	34. Multiply 56042 by 5.
4.	Multiply	246 by 2.	35. Multiply 21264 by 2.
5.	Multiply	278 by 2.	36. Multiply 60153 by 6.
6.	Multiply	495 by 2.	37. Multiply 32305 by 5.
7.	Multiply	1312 by 2,	38. Multiply 57802 by
8.	Multiply	2172 by 2.	39. Multiply Cor35 by 5.
9.	Multiply	3629 by 2.	40. Multiply 91216 by 6.
10.	Multiply	3785 by 2.	41. Multiply 12357 by 7.
11.	Multiply	4006 by 2.	42. Multiply 23460 by 6.
12.	Multiply	4308 by 2.	43. Multiply 68913 by 3.
13.	Multiply	142034 by 2.	44. Multiply 57802 by 2.
14.	Multiply	1706324 by 2.	45. Multiply 62819 by 5.
15.	Multiply	3614503 by 2.	46. Multiply 93856 by 6.
16.	Multiply	462178 by 2.	47. Multiply 28475 by 4.
17.	Multiply	1203062 by 3.	48. Multiply 39586 by 5.
18.	Multiply	21607835 by 3.	49. Multiply 40697 by 6.
19.		93420 by 3.	50. Multiply 17364 by 3.
20.	Multiply		51. Multiply 51708 by 4.
21.	Multiply	1039246 by 4.	52. Multiply 5876 by 4.
22.	Multiply	217906 by 4.	53. Multiply 8546 by 7.
23.	Multiply	509367 by 4.	54. Multiply 502 by 9.
24.	Multiply	567239 by 5.	55. Multiply 246025 by 5.
25.	Multiply	6146802 by 6.	56. Multiply 512604 by 8.
26.	Multiply	4601792 by 5.	57. Multiply 648 by 7.
27.	Multiply		58. Multiply 1082 by 9.
28.			59. Multiply 5050 by 4.
29.		4286072 by 7.	60. Multiply 73046 by 3.
30.	Multiply	237000 by 7.	61. Multiply 10708 by 2.
31.	Multiply	23416 by 2.	62. Multiply 980789 by 8.
	(63)	(64)	(65) (66) (67)
	2413	3142	3546 5354 81897
	II	12	II I2 II
	(68)	(69)	(70) (71) (72)
	900867	8602968	716914 765439 8419829
	11	12	12 11 11

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(<i>a</i>)	(73) 8270802 12	(74) 3443 1 I	(75) 1345 12	(76) 77777 11	(77) 888888 12	10. I di
	(78) 666666	(79) 99999999	(80) 4040404	(81)	(82)	11. A do
	10	12	11	575757 12	484848 11	12. A ho 13. W
83.	82386× 7.	06. 1	8889 × 12.			MR
84. 85.	$357 \times 5.$ $8645 \times 8.$	97. 18	8476×11. 958× 7.	109. 960 110. 593	514 X 8	14. If sh
86. 87. 88. 89.	²⁰⁷⁹ × 9. 8842 × 4. 3749 × 7. 13146 × 9.	99. 760 100. 194 101. 426	$281 \times 11.$ $514 \times 8.$ $847 \times 12.$	111. 9268 112. 7602 113. 1047 114. 3270	281 X 9. 748 X 7.	15. T To th
90. 91.	876×10. 2345×12.	102. 859 103. 482 104. 715	403 × 7. 736 × 11.	115. 6503 116. 3826 117. 6169	04 × 8.	16. In th
92. 93. 94.	998 × 11. 8134 × 12. 7312 × 11.	105. 5480	$269 \times 8.$	118. 4380	82 × 7.	17. If
95.	8183×12.	107. 2040 108. 5379	158× 7.	120. 7638	57 × 12.	18. If re
	a man sold are receive for					19. If co
2. V 3. V	Vhat is the c Vhat is the c	ost of 184 b	arrels of me	al, at \$6a b	arrel ?	20. W mi
	Vhat is the c cre?					21. Ni
4. V 5. II	Vhat is the c	ost of 4786 b	arrels of flor	ur, at \$9 a.b	arrel?	wl 22. İf
tł	n 1 mile the here in 5 mile	es?	o ieet: ho	w many fe	et are	co
6. Ir	1 mile there here in 5 mile	are 1760 m				23. Tł ar
7. If	9 men can s in one man c	ow a farm i				24. Ho th cu
8. If	6 men can ys can one r	build a me				25. W en
q. If	460 hushels	of grain and	ic same wa.	u r	1	26. If To
for	w many bus the same ti	me?	enecessary	to feed 8 h	orses	27. W of
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MULTIPLICATION.

- 10. I bought 245 cords of maple, at \$7 a cord: how much did the whole cost me?
- 11. A dealer sold 8 animals, at \$253 apiece: how many dollars did he receive for them?
- 12. A girl bought 189 yards of ribbon at 6 cents per yard : how much did it cost her ?
- 13. What is the cost of 2988 boxes of figs, at \$3 a box?
- 14. If a steamer can go 395 miles in one day, how far can she go in 9 days at the same rate?
- 15. There are 10 companies in the Queen's Own Rifles, Toronto, each having 42 men : how many men are there in the regiment?
- 16. In one mile there are 5280 feet: how many feet are there in 4 miles?
- 17. If a mill turns out 9757 yards of carpet in one week, how many yards could it produce in 5 weeks?
- 18. If a ship can carry 7856 barrels of ore, how many barrels could be carried in 6 ships?
- 19. If a waggon can carry 5837 shingles, how many shingles could be carried in 7 waggons?
- 20. What would 8 miles of pavement cost, at \$3489 per mile?
- 21. Nine men built a vessel, each one putting in \$8457: what was the cost of the vessel?
- 22. If a barge can carry 19857 pounds, how many pounds could 4 such vessels carry?
- 23. There are 63360 inches in a mile: how many inches are there in 5 miles?
- 24. How many miles would a yacht sail in going around the earth 6 times, the earth being 24855 miles in circumference?
- 25. What would be the cost of constructing 7 miles of embankment, at \$35248 per mile?
- 26. If 11 clergymen are paid \$2212 dollars apiece in Toronto, what do they receive in all?
- 27. What is paid to 12 teachers in Hamilton, at the rate of \$862 each?

 $7071 \times 11.$ $7071 \times 11.$ $70304 \times 8.$ $2637 \times 12.$ $960 \times 9.$ $8082 \times 7.$ $406 \times 11.$ $867 \times 12.$

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(82)

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4748× 7.

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- 28. In 1 mile there are 5280 feet: how many feet are there in 7 miles?
- 29. In 1 mile there are 1760 yards: how many yards are there in 8 miles?
- 30. If in one barrel there are 196 pounds of meal, how many pounds are there in 5 barrels?
- 31. A. sold 4 horses, at \$175 apiece: how many dollars did he receive for them?
- 32. A lady bought 89 yards of silk twist, at 5 cents a yard : how much did the twist cost her?
- 33. What is the cost of 1786 boxes of grapes, at \$2 a box?
- 34. If a vessel can go 387 miles in 1 day, how far can she go in 9 days at the same rate?
- 35. A merchant bought 1789 coats, at \$4 apiece: how much did he pay for them all?
- 36. A farmer sold 7 fat cattle for \$97 apiece: how much did he receive for them all ?
- 37. In 1 gallon there are 4 quarts: how many quarts will there be in 8451 gallons?
- 38. There are 160 square rods in 1 acre of land: how many square rods are there in 11 acres?
- 39. How many pence are there in 32916 shillings, at 12 pence to the shilling?
- 40. In 1 year there are 365 days: how many days are there in 11 years?
 - In the question, "Bought 149 square yards of land at \$7 a yard," although we have to find what \$7 become when repeated 149 times, yet we may, for the sake of convenience, look upon 7 as the multiplier, the product being dollars.
- 78 The next case of multiplication is that in which the multiplier is greater than 12.

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MULTIPLICATION.

Ex. 1.—Multiply 1396 by 364, that is, find what 1396 becomes when repeated 364 times.

		1396
		364
$1396 \times 4 = 5584$	-	5584
$1396 \times 60 = 83760$	Or,	8376
1396 × 300 = 418800		4188
508144		508144

- The number 364 = 3 hundreds + 6 tens + 4 units, hence the multiplicand is to be repeated 300 times, and 60 times, and 4 times. If we then take 4 times the multiplicand, and 60 times the multiplicand, and 300 times the multiplicand, these results added together must give 364 times the multiplicand.
- By the previous case, 4 times 1396 gives 5584. This we put down as usual.
- Again, 1396 multiplied by 6 tens is the same as 6 tens by 1396 (Art. 77), and this we find to be 8376 tens, which result in the addition must (since it is tens) be put one place to the left of the last result, 5584.
- Again, 1396 multiplied by 3 hundreds is the same as 3 hundreds by 1396, and this is 4188 hundreds, which must therefore in the addition be put one place to the left of the tens' result, 8376.
- Having placed these three results ready for addition, nothing remains but to add them together in the usual way.

We thus find that $1396 \times 364 = 508144$.

In the same way we proceed with any number of figures in the multiplier.

Ex. 2.-Multiply 872 by 307.

$872 \times 7 = 6104$		307
$872 \times 0 = 00$ $872 \times 300 = 261600$	Or,	6104 26160
267704		267704

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Here 7 times 872 gives 5104. There are no tens in the multiplier, hence we might have filled the usual line with noughts, but one nought is enough to keep the next result in its proper place. 3 times 872 gives 2616, and this being hundreds, it must be put one place to the left of the nought, which makes the tens' place.

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A ld as before, and we find $872 \times 307 = 267704$.

Ex. 3.—Multiply 371 by 2100.



779100

- In this example there are no units or tens in the multiplier, therefore the first result, 371, must be placed to represent hundreds, that is, three places to the left of the units' place. The next result, being thousands, viz., 742 thousands, it will be put one place to the left of the last result. Add together as usual.
- 79. We see from this that any number may be multiplied by 10, 100, 1000, etc., by adding 1, 2, 3, etc., noughts to the right of the number to be multiplied.

Thus, $389 \times 100 = 38900$. $40 \times 1000 = 40000$.

80. As there are 100 cents in a dollar, this principle is very useful in expressing any number of dollars as cents.

Ex. 1.—How many cents are there in \$84?

There will be 84 times as many cents in 84 dollars as there are cents in 1 dollar, that is, $84 \times 100 = 8400$ cents. *Ex.* 2.—How many cents are there in \$64.52; that is, 64 dollars and 52 cents?

> \$64 = 6400 cents.6400 cents + 52 cents = 6452 cents.

81. Hence, to express any number of dollars and cents as cents, we have only to remove the point which separates the dollars from the cents, and the result will be the required number of cents.

Ex. 3. - \$106.97 = 10697 cents.

MULTIPLICATION.

82. Suppose we have to multiply any number by 16. We know that $8 \times 2 = 16$, and therefore to repeat the number 16 times would amount to the same as repeating it 8 times and then repeating this result 2 times; or, since $2 \times 8 = 16$, it would be the same to repeat the number 2 times and then repeat that result 8 times.

Again, $4 \times 4 = 16$. We may therefore repeat the number 4 times, and this r sult again 4 times; each of these methods would give the same product.

Ex.—Multiply 362 by 44.

	36	2	
	398	-	
•		_	

15928

- Since $44=11 \times 4$, we multiply 362 by 11, which gives 3982, and then multiply 3982 by 4, giving 15928 as the final product.
- 83. The numbers 8 and 2, or 4 and 4, are called the factors of 16. (See Art. 74.)

•	The fact	ors of
12	are	2, 6.
48	are	12, 4.
120	are	12, 10.

84. A result in Multiplication may be proved to be correct by using the multiplicand as the multiplier, which should give the same product, if worked correctly.

EXERCISE 15.

As many as possible of the following questions should be worked by factors as well as by the ordinary method.

(a)	(1) 462 4		(2) 3846	(3) 8462	(4) 7846
	35	;	39	47	147

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62	ARITHMETIC FO	R BBGINNERS.	•	
$(a) \begin{array}{c} (5) \\ 3976 \\ 183 \\ \end{array}$	(6) 2243 144	763521 438	(8) 1283 144	(a) (4)
(9) 2526 136	(10) 52365 543	(11) 3678543 4567	(12) 76785316 7615	(45 467 \$
(13) 67854 10234	(14) 6503455 234	(15) 98610275 357 ⁸ 9	(16) 568 287	(5: 3764 5
(17) 3985 733	(18) 987 891	(19) 7415 3 ⁸ 7	(20) 8097 869	(b) Mult 1. 2. I
(21) 57423 159	(22) 194 57	(23) 3678543 4567	(24) 437 35 ⁶	3. 4. 10 5. 630 6. 4.
(25) 274 167	(26) 433 26 96	(27) 999 999	(28) 841 841	7. 36 8. 7 9. 88 10. 68.
(29) 3759 3757	(30) 8643 923	.(31) 3976 948	(32) 907 740	11.753 12.1 13.4 14.68
(33) 657 408	(34) 6258 346	(35) 5679 507	(36) 7856 658	15. 76 16. 78 17. 708 18. 4: 19. 70
(37) 9008 784	(38) 3207 2345	(39) 6579 3506	(40) 8579 4078	20. 1 21. 10 22. 23. 7
(41) 7058 6 007	(42) 35768 3456	(43) 726 27	(44) 4628 554	24. 6 25. 7 26. 38 27. 67 28. 74

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10 - 20 B

(45) (46) (7) 3648 4275 30 54 (49) (50) 4620 8726 3'34 463 (53) (54) 37642 3794257 $386(b) Multiply1. 74 by 10.2. 10000 by 869.3. 4698 by 1000.4. 100000 by 76984.5. 6307918 by 20790.6. 44670 by 145.7. 367950 by 756.8. 78609 by 406.9. 887002 by 903.10. 684207 by 7006.11. 7532100 by 4861.12. 17565 by 1800.13. 43450 by 1700.14. 685900 by 190.$	(47) 8463 3759 (51) 7692 356 (55) 27403 584 29. 2572 by 30. 40306 by 31. 86072 by 32. 48746 by	127.
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	7692 356 (55) 27403 584 29. 2572 by 30. 40306 by 31. 86072 by 32. 48746 by	2146 179 (56) 81650 789 94. 127.
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I. 74 byIO.2.10000 by $869.$ 3. 4698 by1000.4.100000 by $76984.$ 5. 6307918 by $20790.$ 6. 44670 by $145.$ 7. 367950 by $756.$ 8. 78609 by $406.$ 9. 887002 by $903.$ 10. 684207 by $7006.$ 11. 7532100 by $4861.$ 12. 17565 by $1800.$ 13. 43450 by $1700.$	30. 40306 by 31. 86072 by 32. 48746 by	127.
2. 10000 by 869. 3. 4698 by 1000. 4. 100000 by 76984. 5. 6307918 by 20790. 6. 44670 by 145. 7. 367950 by 756. 8. 78609 by 406. 9. 887002 by 903. 10. 684207 by 7006. 11. 7532100 by 4861. 12. 17565 by 1800. 13. 43450 by 1700.	30. 40306 by 31. 86072 by 32. 48746 by	127.
15. 76980 by 1600. 16. 78600 by 1400. 17. 708060 by 38506. 19. 70800 by 69870. 20. 1011 by 754. 21. 10009 by 869. 22. 386 by 99. 23. 7815 by 98 24. 6188 by 97. 25. 7289 by 999. 26. 38751 by 998. 27. 67583 by 996.	 33. 30975 by 34. 6408 by 35. 703475 by 36. 370607 by 37. 600326 by 38. 730096 by 39. 2407068 by 40. 408091 by 41. 73069 by 42. 4372 by 43. 3065 by 44. 36204 by 45. 4008 by 46. 47672 by 47. 302076 by 48. 73008 by 49. 430605 by 50. 290361 by 51. 2784 by 52. 68470 by 53. 3060724 by 54. 130065 by 	316.

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(c) t. Multiply seven thousand six hundred and one by seven.	19. Th sa
2. Multiply thirteen hundred and eighty-four by eleven and twelve in succession.	20, W sai
3. Multiply together two, three, four, five, six, seven, eight, nine, and ten.	21. On is 1
4. Find the product of three hundred and forty-seven and five hundred and eighty three.	22. Mu hu
5. Find the product of twelve thousand and three and three thousand and twelve.	23. Mi eig
6. How much is twelve times four times three thousand four hundred and seven?	24. Ho \$42 25. Ho
7. Multiply together three thousand three hundred, three thousand and thirty, and three thousand and three.	26. A. ma
 8. Find the square of six hundred and seventy-nine. K² (The square of a number is that number multiplied by itself.) 	27. A ma 28. Ho
9. Find the square of two thousand seven hundred and forty-seven.	29. Ho in 4
10. Find the square of seventeen hundred.	20. A o
11. Multiply three millions seventeen thousand and ninety by four thousand and eighty-four.	stoc
12. Multiply the square of two hundred and thirty-nine by eleven.	(d) 1. If a app
13. Find the product of one thousand three hundred and fifty-six, five hundred and seventy-eight, and two hundred and fifty.	orcl 2. Hoy eac
14. Multiply the square of seventeen by the square of nineteen.	3. How the
15. Multiply six thousand and ninety-seven by nine hun- dred and eight.	4. Wh a ba
16. Multiply fifty-four thousand and forty-nine by six	5. If a

- thousand and seventy-five. 17. The two factors of a certain number are 656 and 907:
- what is the number?
- 18. Multiply thirty-seven thousand and twenty-eight by 508.

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- 6. Wh acro
 - 7. A g ave will

MULTIPLICATION.

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- 19. The multiplier being 987, the multiplicand six thousand four hundred and sixteen : required the product.
- 20. What is the product of 908060 multiplied by five thousand four hundred ?
- 21. One factor is 718151, the other seven hundred: what is the product?
- 22. Multiply six hundred and seventy-four thousand two hundred by two thousand one hundred and four.
- 23. Multiply ninety-three thousand one hundred and eighty-six by four thousand four hundred and fifty-five.
- 24. How many cents are there in \$5? in \$60? in \$18? in \$47? in \$22.05? in \$872.06? in \$540.10? in \$80.80?
- 25. How many more cents are there in \$20 than in \$12.75?
- 26. A. earns \$1.75 in a day, and B. earns \$1.60: how many more cents does A. earn in 6 days than B.?
- 27. A man has \$860.75, and lends another \$851: how many cents has he left?
- 28. How many cents are there in 10 times \$60?
- 29. How many more cents are there in 3 times \$17 than in 4 times \$3.25?
- 20. A owns \$570.60 in stock, and buys 3 times as much more: how many cents will he then have invested in stock?
- (d) 1. If an orchard containing 313 trees yields 15 bushels of apples to a tree, how many bushels does the whole orchard produce?
 - 2. How many panes of glass are there in 18 windows, if each window contains 24 panes?
 - 3. How many bushels of wheat will 160 acres produce, at the average rate of 45 bushels to the acre?
 - 4. What is the cost of 2463 barrels of flour, at 19 dollars a barrel?
 - 5. If a man can earn 83 dollars in one month, how many dollars can he earn in 18 months?
 - 6. What will be the cost of an estate containing 684 acres, at 57 dollars per acre?
 - 7. A garden has 625 hills of potatoes, and each hill will average 13 potatoes: how many potatoes at that rate will there be in the garden?

ARITHMETIC FOR BLUINNEPS.

8. If 17 men do a piece of work in 91 days, how long will it take one man alone to do it?	26. A
9. What will be the cost of building a line of telegraph 274 miles long, at \$967 a mile?	27. In fur
10. If 1049 pounds of tobacco can be raised from an acre of land, how many pounds will 386 acres produce?	28. He
many yards can it make in 207 days?	29. W
12. What will be the cost of building 279 miles of railroad. at \$27384 a mile?	30. Ho
13. A crop of cotton was put up in 340 bales, each bale containing 596 pounds: what was the weight of the entire crop?	394 31. A s she
14. What is the value of 108 buildings, at \$1896 each?	32. If a
15. What is the cost of 257 yoke of oxen, at \$175 a yoke?	wo
10. What is the cost of 428 lots, at \$284 each?	33. WI a b
17. In 1 ream of paper there are 480 sheets: how many sheets are there in 217 reams?	34. Wł dol
18. How much will it cost to build a line of telegraph from Toronto to Lake Nipissing, the distance being 236 miles, at \$1270 a mile?	35. Wł dol
19. If a cotton mill manufacture 658 yards of cloth in a day, how many yards can it make in 309 days?	36. W1 23
20. How many yards of cloth are in 265 pieces, each piece containing 32 yards?	37. Wł a b
21. Sound travels 1142 feet in 1 second : how far will it travel in 60 seconds?	38. Ho tob
22. Light travels 192000 miles in 1 second: how far will it travel in 494 seconds?	39. At of 1
23. A drover bought 685 oxen, at \$104 apr 3 what was the cost of all of them?	40. If 7 it ta
24. A merchant bought 25 pieces of broadcloth, each piece containing 48 yards, at \$9 a yard: how much did he pay for the whole ?	41. Wh eac 12. Wha
25. If the <i>Thunderer</i> can steam 18 miles in 1 hour, how far can she steam in 34 days of 24 hours each?	43. Wh doll

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MULTIPLICATION.

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- 26. A man bought 8969 acres of land, at \$196 an acre: how much did the whole cost him ?
- 27. In 1 furlong there are 660 feet : how many feet are in 8 furlongs (1 mile)?
- 28. How many pounds of pork are there in 395 barrels, there being 200 pounds in each barrel?
- 29. What is the value of 346 shares of bank stock, at \$125 a share?
- 30. How many pages are there in 5896 books, the being 394 pages in each book?
- 31. A speculator bought 302 cattle, and 293 times as many sheep : how many sheep did he buy?
- 32. If a body move at the rate of 378 miles a day, how far would it move in 365 days?
- 33. What is the cost of 1787 barrels of sugar, at 18 dollars a barrel?
- 34. What is the value of 1982 barrels of molasses, at 15 dollars a barrel?
- 35. What is the cost of 3784 pieces of broadcloth, at 143 dollars apiece?
- 36. What will I be charged for 21423 barrels of pork, at 23 dollars a barrel?
- 37. What must I pay for 47879 bushels of corn, at 65 cents a bushel?
- 38. How many dollars would purchase 3785 kegs of tobacco, at 34 dollars a keg?
- 39. At 19 dollars a firkin, what is the cost of 91072 firkins of butter?
- 40. If 7842 men build a fort in 137 days, how long would it take 1 man to build it?
- 41. What will be the value of 237 cows, at 23 dollars each?
- 42. What will be the cost of 397 loads or metal, at 37 dollars a load?
- 43. What is the cost of 2473 tons of wrought iron, at 297 dollars a ton?

- 44. If a regiment consists of 1128 men, how many men are there in an army of 203 regiments?
- 45. In a factory there are 873 yards of cloth made in 1 day: how many yards, at this rate, can be made in 313 days?
- 46. In one load a span of horses can draw 2997 pounds how many pounds would they draw in 327 loads?
- 47. There are 15 fields of plants; in each field there are 97 rows, and 256 plants in each row: how many plants are there in all?
- 48. How many letters are there in a book containing 672 pages, each page containing 43 lines, and each line 47 letters?
- 49. A freight train consists of 21 cars; each car contains 85 barrels, and each barrel weighs 196 pounds: how many pounds are in the entire cargo?
- 50. The distance from Toronto to Thornhill is 12 miles; each mile contains 1760 yards, and each yard 3 feet: how many feet are there from one place to the other?
- 51. In an orchard there are 14 rows of plum trees; each row contains 27 trees, and each tree bears 108 plums, how many plums are in the orchard?
- 52. It requires 1716 rails to fence one side of a square garden: how many rails will be required to fence 13 lots of the same size and shape?
- 53. An army lost in battle 315 killed and 417 wounded; the enemy lost altogether 13 times as many: how many soldiers were killed and wounded in the battle?
- 54. If two steamers should leave Collingwood at the same time, and should sail in the same direction, the first at the rate of 18 miles an hour, the second at the rate of 15 miles an hour, how far apart would they be in 36 hours?
- 55. An army consists of 6 divisions, each division of 4 battalions, and each battalion of 613 men: find the number of men in the army.
- 56. If a planing-mill run 4360 feet of boards a day how many will it run out in 106 days?

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- 57. Supposing the earth to move around the sun at the rate of 68000 miles an hour, how far will it move in 365 days of 24 hours each?
- 58. Bought from Davison, Scott & Co. 427 cheeses, weighing, with the cases, 67 pounds each; each case weighs 5 pounds: find the cost of the cheese at 11 cents a pound.
- 59. On a holiday in the City of Toronto, the Street Railway Company placed on the road 76 cars; the fare is 5 cents: supposing each to carry, on an average, 18 persons, and to make 10 trips, how much money was taken by the Company on that day?
- 85. The following mental exercises will be found useful in accustoming the pupils to rapid thought.
 - The questions should be read out slowly at first, but gradually faster, and each pupil should write upon a slate or paper on the desk in front the result obtained.
 - As this is the most valuable work that can be done by the beginner, the teacher should add largely to the number of problems here set.

Ex. 1.—Add 15 to 4, subtract 9, add 11, subtract 5: what is the result?

15+4=19; 19-9=10; 10+11=21; 21-5=16. Ans. 16.

While the teacher dictates the example, "to 15 add 4, subtract 9," etc., the pupils think 19, 10, etc.

Ex. 2.—Take 19, subtract 9, multiply by 7, subtract 11, subtract 9.

The pupil would think : 19, 10, 70, 59, 50. Ans. 50.

EXERCISE 16.

- 1. To 12 add 7, subtract 5, add 4, add 8: result?
- 2. From 25 take 10, add 7, add 8, take 9: result?
- 3. To 17 add 18, subtract 7, add 9, subtract 5: result?

- 4. To 26 add 18, subtract 5, add 6, subtract 9, add 5, take 8: result?
- 5. From 27 take 9, add 7, subtract 10, subtract 6, add 11: result?
- 6. Add 9 to 15, subtract 11, add 10, subtract 9, subtract 14: result?
- 7. Take 4 from 23, add 1, add 25, subtract 5, subtract 20, add 6: result?
- 8. Add 7 to 8, subtract 3, add 8, add 12, subtract 7, subtract 5, add 6, add 4, subtract 10: result?
- 9. Take 7 from 15, add 6, take 5, add 10, take 3, add 4, add 6, take 7, add 8, take 9: result?
- 10. To 13 add 7, subtract 5, multiply by 2, subtract 15, subtract 10, multiply by 3, subtract 5: result?
- 11. From 15 subtract 9, multiply by 3, subtract 8, add 5, multiply by 2, subtract 20, add 8, multiply by 2, subtract 9, add 9: result?
- 12. Multiply 12 by 5, subtract 40, add 5, multiply by 2, subtract 25, add 5, multiply by 3, add 7 : result ?
- 13. Take 12 from 48, add 6, take 7, add 8, take 3, add 7, take 9, add 11, take 4, add 3, take 5, add 9, take 10, add 7, take 8, add 9, add 3, take 5: result?
- 14. From 16 subtract 9, multiply by 3, subtract 7, add 4, multiply by 6, subtract 7, add 9, subtract 8 : result ?
- 15. Add 6 to 18, subtract 9, multiply by 4, subtract 25, multiply by 2, subtract 40, multiply by 7: result?
- 16. From 19 subtract 8, multiply by 6, subtract 11, add 7, subtract 20, add 8, multiply by 3, add 9: result?
- 17. Multiply 7 by 6, subtract 12, add 4, subtract 14, multiply by 6, subtract 20, multiply by 3, subtract 12, add 12: result?
- 18. Add 11 to 29, multiply by 2, subtract 16, add 6, multiply by 10: result?
- 19. Take 19 from 39, multiply by 5, subtract 50, add 10, multiply by 3. subtract 100: result?
- 20. To 23 add 7, multiply by 3, add 10, subtract 50, multiply by 2, subtract 100, multiply by 6 : result?

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- , subtract 9, add 5,
- , subtract 6, add 11:
- subtract 9, subtract
- tract 5, subtract 20,
- 12, subtract 7, subresult ?
- 1 10, take 3, add 4,
- by 2, subtract 15, t 5: result?
- subtract 8, add 5, nultiply by 2, sub-
- d 5, multiply by 2, dd 7 : result ?
- d 8, take 3, add 7, 5, add 9, take 10, result?
- subtract 7, add 4, btract 8 : result ?
- by 4, subtract 25, by 7: result?
- subtract 11, add 7, dd 9: result?
- subtract 14, mul-3, subtract 12, add
- t 16, add 6, multi-
- ibtract 50, add 10,
- subtract 50, mul-6 : result?

MULTIPLICATION.

- 21. Add 7 to 9, subtract 6, multiply by 4, subtract 20, add 7, subtract 5, multiply by 2, subtract 8, add 5: result?
- 22. Subtract 8 from 17, multiply by 5, subtract 15, multiply by 20, subtract 30, add 9, subtract 9: result?
- 23. To the product of 8 and 8 add 6, subtract 30, add 2, subtract 12, multiply by 3, subtract 4, add 6: result?
- 24. To 19 add 11, subtract 15, multiply by 4, subtract 12, multiply by 2, add 9, subtract 5, multiply by 11: result?
- 25. Subtract 9 from 21, add 8, subtract 6, add 11, multiply by 4, subtract 7, add 9, subtract 8: result?
- 26. To the product of 9 and 6 add 6, subtract 12, subtract 18, multiply by 2, subtract 20, add 5, multiply by 2, add 10, multiply by 3, add 15, subtract 7, add 6: result?
- 27. From 23 subtract 8, multiply by 2, multiply by 4, subtract 20, subtract 21, add 6, multiply by 2, subtract 20, multiply by 3, add 8, subtract 7, add 9 : result?
- 28. To 31 add 12, subtract 10, add 6, subtract 7, subtract 8, subtract 4, add 9, subtract 3, add 6, add 8, add 10, subtract 5, add 8, subtract 2, add 6, subtract 7, add 4, subtract 6: result?
- 29. From 63 subtract 7, add 3, add 6, add 12, subtract 4, add 10, subtract 5, add 6, subtract 7, add 3, subtract 6, add 9, subtract 8, add 6, subtract 4, add 3, subtract 2, add 7: result?
- 30. Add 7 to 9, subtract 8, add 20, add 14, add 30, subtract 4, add 5, subtract 6, add 7, subtract 8, add 9, subtract 10, add 4, add 5, add 8, subtract 7, add 4, subtract 5: result?

DIVISION.

86. We have seen that 3 dollars repeated 5 times are 15 dollars. Now let us see how often we can take 3 dollars from 15 dollars.

15 3	dollars			
12 3	dollars	= 1 st	rema	ainder.
9 3	"	=2nd	I	"
6 3	"	= 3rd		ce
3	44	=4th		"
0	44	= 5th		"

Thus, 3 dollars may be taken 5 times away from 15 dollars, that is, just as many times as it was before repeated in order to produce 15 dollars.

This fact is expressed by saying that 3 is contained in 15, 5 times. In the same manner it may be shewn that 4 is contained in 12, 3 times; and 8 contained in 56, 7 times.

87. Again, since 3 dollars can be taken 5 times from 15 dollars, this is but another way of saying that \$15 can be divided into 5 parts, each part being 3 dollars. In the same way, if 20 units be divided into 4 parts of the same size, each will be 5 units, and since, in repeating the parts in the multiplication, they were, of necessity, the same size, so in this process we will always suppose the parts to be the same size, or of the same value. WH tl tl 88. Th: fc n

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When we wish to divide 32 into 4 parts, it is understood that they shall be of the same size, viz: 8 units in this case.

88. This operation, then, is called **Division**, which is therefore the method of finding the number of times one number is contained in another.

- The number which contains, or is divided by the other is known as the Dividend.
- The number which is to be divided into the Dividend is called the Divisor.

The number which shows now often the Divisor is contained in the Dividend is termed the Quotient.

89. The sign for this operation is +, placed between the two numbers, and shews that the number coming before it, viz., the Dividen⁴, is to be divided by the one coming after it, viz. : the Divisor, thus:

45 + 9 = 5,

Reads, 45 divided by 9 equals 5, and means that 9 may be taken from 45, 5 times; or, that 9 is contained in 45, 5 times; or, that if 45 be divided into 9 equal parts, each part is 5.

The pupil should remember that it is the Divisor which always follows the sign of Division.

- 90. Division will easily be seen to be the converse of Multiplication, for from 7 and 4 we obtained 28 by the latter process, while from 7 and 28 we obtain 4 by the former process.
 - Every result, then, in the Multiplication Table (Art. 71) will also furnish us with a corresponding result in the Division Table. This is, in fact, the very work done by the pupil in Ex. 13(a).

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91. The following Table can be seen at once to agree with the Table in Art. 71.

DIVISION TABLE.

1. H in 2. H in 3. H fre 4. D

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I + I = I	2 + 2 = 1	3 + 3 = 1 + 4 + 4 = 1	2. H in
$2 \div 1 = 2$	4 + 2 = 2	$6 \div 3 = 2$ $8 \div 4 = 2$	2
3 + 1 = 3	6 + 2 = 3	$9 \div 3 = 3$ $12 \div 4 = 3$	3. H fr
4 + 1 = 4	$8 \div 2 = 4$	$12 \div 3 = 4$ $16 \div 4 = 4$	
5 + 1 = 5	10 + 2 = 5	$15 \div 3 = 5$ $20 \div 4 = 5$	4. D
$6 \div 1 = 6$	$12 \div 2 = 6$	$18 \div 3 = 6$ $24 \div 4 = 6$	
7 + 1 = 7	$14 \div 2 = 7$	$21 \div 3 = 7$ $28 \div 4 = 7$	
8 + 1 = 8	$16 \div 2 = 8$	$24 \div 3 = 8$ $32 \div 4 = 8$	5
9 + 1 = 9	$18 \div 2 = 9$	27 + 3 = 9 $36 + 4 = 9$	
$5 \div 5 = \mathbf{I}$	$6 \div 6 = 1$	$7 + 7 = 1$ $8 \div 8 = 1$	
10 + 5 = 2	$12 \div 6 = 2$	14 + 7 = 2 $16 + 8 = 2$	5. W
15 + 5 = 3	18 + 6 = 3	21 + 7 = 3 $24 + 8 = 3$	45
20 + 5 = 4	$24 \div 6 = 4$	$28 \div 7 = 4$ $32 \div 8 = 4$	81 16
$25 \div 5 = 5$	30 + 6 = 5	35 + 7 = 5 $40 + 8 = 5$	16
$30 \div 5 = 6$	36 + 6 = 6	$42 \div 7 = 6$ $48 \div 8 = 6$	6. If
35 + 5 = 7	$42 \div 6 = 7$	49 + 7 = 7 $56 + 8 = 7$	bo
$40 \div 5 = 8$	48 + 6 = 8	$56 \div 7 = 8$ $64 \div 8 = 8$	16
$45 \div 5 = 9$	54 + 6 = 9	$63 \div 7 = 9 + 72 \div 8 = 9$	7. 36
9 + 9 = 1	10 + 10 = 1	11 + 11 = 1 $12 + 12 = 1$	8. 32
18 + 9 = 2	20 + 10 = 2	$22 \div 11 = 2$ $24 \div 12 = 2$	
27 + 9 = 3	30 + 10 = 3	$33 \div 11 = 3 36 \div 12 = 3$	9. 24
36 + 9 = 4	$40 \div 10 = 4$	$44 \div 11 = 4 \ 48 \div 12 = 4$	10. 48
45 + 9 = 5	50 + 10 = 5	55 + 11 = 5 60 + 12 = 5	11. Fr
$54 \div 9 = 6$	10 + 10 = 6	$66 \div 11 = 6$ $72 \div 12 = 6$	ma
63 + 9 = 7	$70 \div 10 = 7$	$77 \div 11 = 7$ 84 $\div 12 = 7$	12. If
72 + 9 = 8	80 + 10 = 8	88 + 11 = 8 96 + 12 = 8	do
81 + 9 = 9	90 + 10 = 9	$99 + 11 = 9 \cdot 108 + 12 = 9$	13. W
			for

Mental Exercises in Division,

1. How many 4's are in 12? in 16? in 48? in 24? in 36? in 28? 2. How many loads of 5 tons each are there in 40 tons ? in 60 tons? in 35 tons? in 15 tons? 3. How many times can 7 be taken from 14? from 42? from 63? from 84? 4. Divide by 3, from 3 into 3 to 3 into 27. by 5, from 5 into 15 to 5 into 45. by 7, from 7 into 42 to 7 into 84. y 8, from 8 into 24 to 8 into 88. by 9, from 9 into 108 to 9 into 27. by 10, from 10 into 10 to 10 into 70. by 12, from 12 into 132 to 12 into 36. 5. What is the quotient in, $36 \div 4, 72 \div 8, 56 \div 7, 108 \div 12,$ 45--9, 77÷7, $8i \div 9$, $72 \div 6$, $54 \div 6$, $132 \div 11$, $64 \div 8$, $30 \div 3$, $42 \div 6, 80 \div 10, 27 \div 9,$ $16 \div 8$, 35÷ 7, 28÷4, 16÷2, $14 \div 2, 60 \div 5,$ $35 \div 5, 84 \div 12, 63 \div 7.$ 6. If a box holds 4 pounds of sugar, how many such boxes will be required to hold 36 pounds ? 28 pounds ? 16 pounds? 44 pounds? 7. 36 is how many times 9? 4? 6? 12? 8. 32 is how many times 4? 82 9. 24 is how many times 2? 3? 4? 6? 8? 12? 10. 48 is how many times 4? 6? 8? 12? 11. From a pile of 60 bricks, how many loads of 12 bricks may be taken away? 12. If \$56 be equally distributed among 7 men, how many dollars does each man receive? 13. When apples are 3 cents each, how many can I buy for 24 cents?

(In other words, how many times must three cents be repeated to give 24 cents,; the answer will be 8.

4 = 1

4 = 2

4 = 3

4 = 4

4 = 5

4 = 6

1 = 7

4 = 8

4 = 9

8 = 1

8 = 2

8 = 3

8 = 1

8 = 5

8 = 6

8 = 7

8 = 8

8 = 0

12 = 1

12 = 2

12 = 3

12 = 4

12 = 5

12 = 6

12 = 7

12 = 8

12 = 9

I could thus buy 8 apples. This must be correct, for each apple costing 3 cents, 8 apples must cost 8 times 3 cents, that is, 24 cents.)

32. W

33. W

34. \\

35. A in

36. If

37. If

39. A

40. A

41. A 1

42. A 1

43. If .

44. A r

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- 14. If a man travel 6 miles an hour, how long will it take him to travel 54 miles?
- 15. How many tubs containing 9 gallons each can be filied from a hogshead containing 63 gallons?
- 16. If a man drive 8 miles an hour, in what time will he drive 56 miles?
- 17. A farmer bought some lambs for \$60, paying \$5 a head: how many lambs did he buy?
- 18. At \$9 a week, in what time will a man earn \$36? \$54? \$72? \$81? \$108?
- 19. If 7 barrels of sugar cost \$63, what will 1 barrel cost?
- 20. If 6 kegs of powder cost \$72, what will 1 keg cost ?
- 21. If a man travel 48 miles in 4 days, how far does he travel in 1 day?
- 22. What will be the cost of 1 ton of coal, if 8 tons cost \$64?
- 23. If you divide \$84 among 7 children, how many dollars will each child have?
- 24. If a man build 72 feet of fencing 11 8 days, how many feet can he build in 1 day?
- 25. If 9 dozens of fish cost 108 cents, what is the cost of 1 dozen?
- 26. How many articles at \$12 each can be bought for \$84? For \$108? For \$120?
- 27. How many lots of 5 acres each are in 20 acres?
- 28. How many barrels, each holding 3 bushels, will be required for 18 bushels of onions? For 21 bushels?
- 29. How many times can 6 yards of canvas be cut off from a piece containing 30 yards?
- 30. How many times can 6 cents be taken from 24 cents?
- 31. Distribute \$28 equally among 7 people : how many dollars will each receive?

DIVISION.

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cents? v many 32. What is one of 4 equal parts of 40? Of 36? Of 48?

33. What is one of 6 equal parts of 30? Of 42? Of 48?

- 34. What is one of 7 equal parts of 56 pounds?
- 35. A teacher having 66 maps, distributed them equally in a class of 11 pupils: how many did each get?
- 36. If 96 pounds of bread are divided equally among 12 persons, how many pounds will each receive?
- 37. If 88 dollars are divided equally among 8 persons, how many dollars will each have?
- 38. If 120 barrels of flour are divided equally among 12 families, how much flour will each receive?
- 39. A master having 108 pupils, divided them into 9 equal classes: how many were in each class?
- 40. A picnic party of 11 persons spent \$132: how much was that apiece?
- 41. A party of 10 persons found a purse containing \$100, which they shared equally: how much did each receive?
- 42. A lad having \$96, wishes to divide it equally among 8 friends: how much can he give to each?
- 43. If you pay 84 cents for a horse and waggon to go 7 miles, how much is that a mile?
- ++. A man having 120 feet of land, divided it into 6 equal lots; how many feet were there in each lot?
- 92. In all the previous examples of Division, the pupil must have noticed that the divisor was contained an exact number of times in the dividend. This is not always the case, for example:
 - I have 22 pears, and give 4 pears to each boy in the class: how many boys were there?
 - If there had been 5 boys, I would require only 20 pears; but if there had been 6 boys I must have 24 pears: so the only thing I can do is to give the 5 boys in the class 4 pears each, and keep the ther 2 that remain for myself.

- **93.** This number, 2 (in the case before us), is called the **Remainder**, and may be said to be that which is left after the divisor has been taken as many times as possible from the dividend.
 - If the remainder be first taken from the dividend, the result must contain the divisor exactly. Thus: 4 may be subtracted from, or contained in, 30, 7 times, but there will be 2 left, and we see that if the 2 be taken from the 30, the result, 28, will contain 4 exactly.

Ex. 1.—Divide 77 by 8.

Since 8 times 9 are 72, the quotient must be 9; and since 72 is less than 77 by 5, then 5 must be the remainder.

Ex. 2.—What must be taken from 49 that it may contain 9 five times?

The number that contains 9 five times we know to be 45, and since this number is 4 less than 49, 4 must be the required result.

EXERCISE 18.

Mental Examples on the Remainder.

1. Give the quotient and remainder, if any, in-

18+ 4,	21+ 5,	62÷ 7,	41+11,	39 + 6	71 + 8,
90+12,	80÷ 7,	23+12,	62+ 9,	73+ 8.	45÷ 0.
83+10,	31 + 3,	42÷ 6,	70÷ 8,	75+ 9.	120+11.
140+12,	93÷10.	48+12,	79÷ 7,	80+12,	100+11.

- 2. What number must be divided by 6 to give a remain der 3 and quotient 5?
- If 6 times 5, or 30, be divided by 6, the quotient will be 5 exactly, with no remainder. Hence, if there is to be a remainder of 3, the number must be 33.
- PROOF.—6 is contained in 33, 5 times, and 3 over for a remainder.
- 3. What number must be divided by 5 to give-

Quotient 7, remainder 2? Quotient 8, remainder 4? Quotient 11, remainder 3?

- 4. To giv must b by 12?
- 5. A man much l
 - 6. From allowed
 - 7. A. recei men, ai among
- 8. If I had each : I
- 9 Countin and 4 o
- 10. How m same nu
- 11. From T ride 7 n be at the
- 12. How ma they be
- 13. There ar 3 boys 1 each row
- 14. John has and kee brothers
- 15. Four qua many ga 31 quarts gallon me
- 16. If lamp p in front o A.'s door far will th
- 17. Find the
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 - 66

DIVISION

4. To give a quotient 7 and remainder 6, what number

5. A man had \$100, and gave \$9 apiece to 8 boys : how

6. From 93 bushels of oats, how many horses can be

7. A. receives what is left after dividing \$100 among 8 men, and B. receives what is left after dividing \$120 among 11 men : how much more does B. get than A.? 8. If I had 7 more apples, I could give 8 boys 11 apples

9 Counting his marbles by sevens, Joseph had 11 lots

10. How many could be put in each lot, to have the

11. From Toronto to Hamilton is 40 miles; a man can ride 7 miles an hour : how far from Hamilton will he

12. How many will be left over from 93 bank notes if they be tied in packages of 8? of 10? of 11? of 12? 13. There are 75 boys in the class, and 6 rows of seats: if 3 boys have to stand, how many seats are there in

14. John has 47 plums, and gives 5 to each of his brothers

15. Four quarts of milk will fill a gallon measure : how many gallons would there be in a pail which holds

16. If lamp posts be placed 11 feet apart, and one placed

brothers had John ? what was his own share?

and keeps the smallest share himself: how many

31 quarts? and how many quarts will be left alter the

in front of A.'s door, how many will there be between

allowed to bushels each, and what would be left?

must be divided by 7? by 8? by 9? by 10? by 11?

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- A.'s door and B.'s door, a distance of 139 feet? how far will the end one be from B.'s door? 17. Find the dividends, having-

gallon measures are filled?

each row?

by 12?

much had he left?

each: how many have 1?

be at the end of 5 hours?

and 4 over : how many had he?

same number of marbles in each?

Divisor 8, Quotient 11, and Remainder 3. 10, \$5 4, 61 2. " 6.6 12, 9. 61 7. ** 9, 1.6 8, .. 7.

- 18. Frank having 68 cents, bought 7 tops, and had 5 cents left: what were the tops apiece?
- 19. How many 3-cent postage stamps can you obtain for 35 cents?
- 20. How many 5-cent pieces can you obtain for 39 cents?
- 21. How many 8-dollar law stamps can be obtained for \$67?
- 2. How many 8-cent loaves of bread can be made out of 75 cents' worth of flour?

23. How many times 7 in 8 times 8, and how many over?

- 24. How many times 9 in 7 times 8, and how many over?
- 25. In 7 times 9, how many times 6, and how many over?
- 26. In 8 times 11, how many times 9, and how many over?
- 27. In 9 times 12, how many times 11, and how many over?
- 94 All the previous examples have depended on a thorough knowledge of the Multiplication and Division Tables. No dividend has been larger than 144, and no divisor greater than 12.

The next case is that in which we have any dividend, but the divisor not greater than 12.

Ex. 1.—Divide 9639 by 3.

3)9639

3213

The dividend is 9 thousands, 6 hundreds, 3 tens, and 9 units.

First, divide the 9 thousands by 3. The result or quotient is 3 thousands, which is written in its proper place under the dividend.

Then, 3 is divided into 6 hundreds, and gives 2 hundreds, which is placed, as usual, after the thousands.

Next, 3 tens divided by 3 gives 1 ten, and this is placed after the hundreds.

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DIVISION

Finally, 9 units divided by 3 gives 3 units, which is written in the units' place.

The whole quotient is, therefore, 3 thousand 2 hundred and 13.

PROOF. $-3213 \times 3 = 9639$.

Ex. 2.—Divide 3955 by 4. 4)3955

3933

988-3

The dividend is 3 thousands, 9 hundreds, 5 tens, and 5 units.

Since the first figure 3 does not contain 4, we say 3 thousands=30 hundreds, making, with the 9 hundreds, 39 hundreds. Then 4 is contained in 39, 9 times and 3 over. That is, 9 hundreds, and 3 hundreds over. Place the 9 as usual, and carry the 3 hundreds on to the 5 tens, making 35 tens. Then 4 is contained in 35, 8 times and 3 over. That is, 8 tens and 3 tens over. Place the 8 tens after the 9 hundreds, and carry on the 3 tens, which with the 5 units make 35 units. Then, finally, 4 is contained in 35, 8 times and 3 over: that is, 8 units and 3 units over.

The quotient is 988, and the remainder 3.

The same method is used for all numbers, however large, in the dividend.

95. From this we have the following

RULE FOR DIVISION.

Write the divisor to the left of the dividend, drawing a line between them, also a line beneath the awidend.

If the divisor will exactly divide each figure in the dividend, place the quotients thus obtained in the proper order under the line. This will be the required quotient.

If the divisor will not exactly divide each figure in the dividend, proceed as follows :

Divide the divisor into the first figure, if possible; if not, into the first two figures; or, if not then, into the first three. Write this quotient in its own place under the dividend. If

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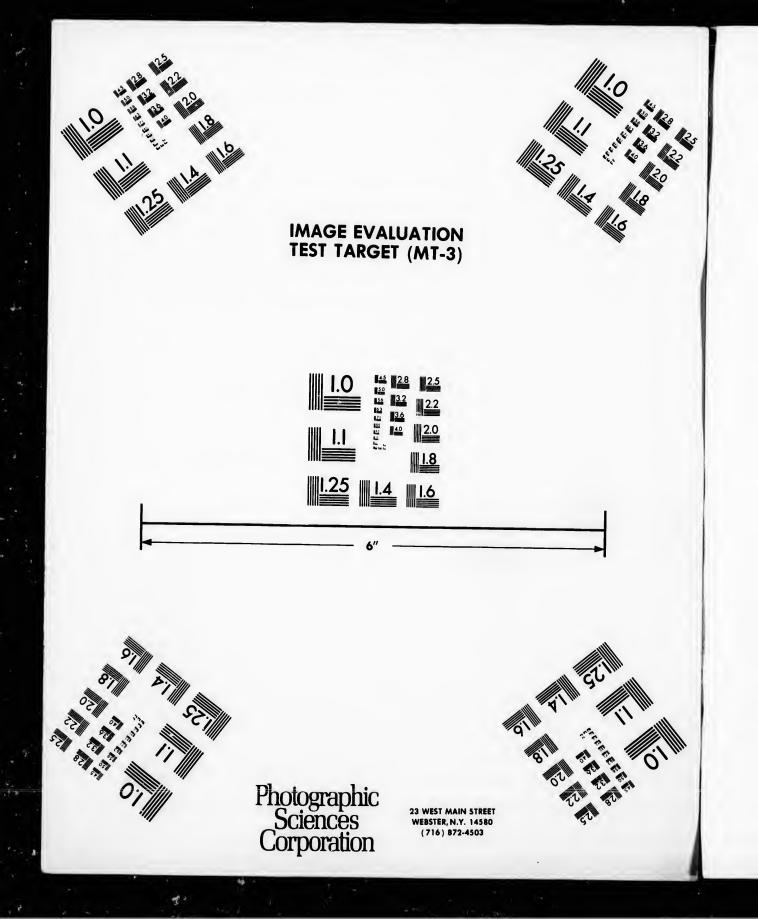
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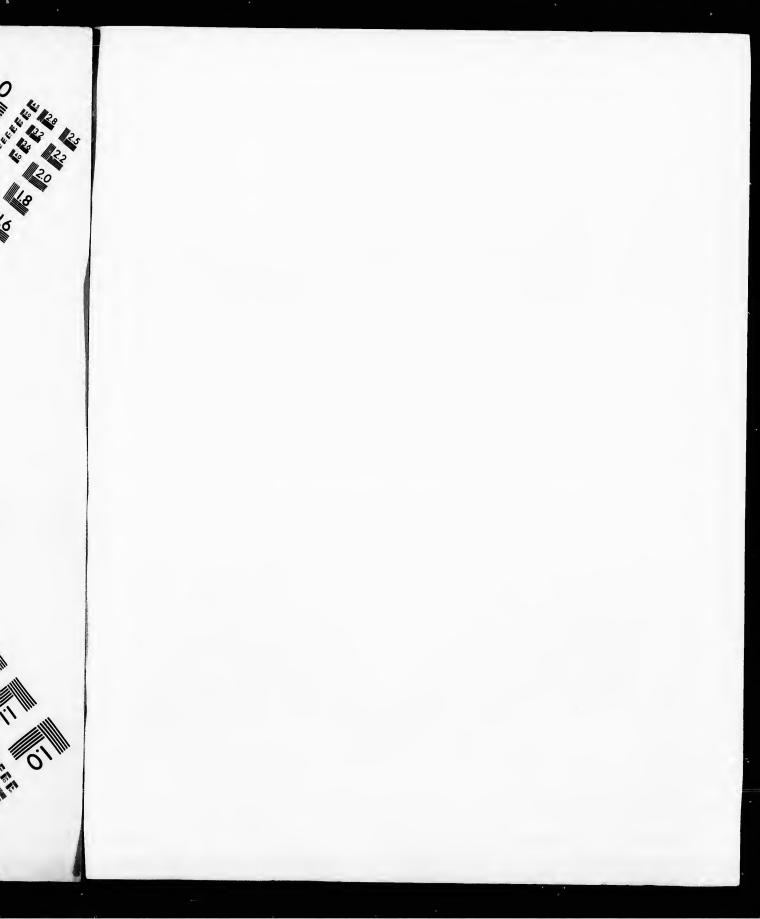
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there be a remainder, place it before the next figure in the divider d. Proceed as before, and carry the remainder to the next jure in the dividend, but if the divisor will not divide, write a nought below in the quotient, and carry the figure or figures to the next one in the dividend. Divide these as before, and so on till all the figures in the dividend are taken in. Place the remainder, if any, to the right of the quotient.

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Ex.-Divide 116501 by 12.

12)116501

9708-5

Here 12 will not divide the first figure 1 or the two first figures 11, therefore we say 12 is contained in 116, 9 times and 8 over; put the 8 with the 5, and say 12 is contained in 85, 7 times and 1 over; take the 1 with the 0; but 12 is not contained in 10; therefore, put down a nought in the quotient, and take in the next figure 1 with the 10, and then say 12 is contained in 101, 8 times and 5 over. This 5 is the remainder, and it must be always less than the divisor.

$\frac{\text{Proof.}-9708 \times 12 = 116496}{116496 + 5 = 116501}$

- That 15, multiply the quotient by the divisor, and to the result add the remainder, if any. This will give the dividend, if the work be correct.
- 96. Where the process is thus carried on mentally, and the quotient only set down, it is called Short Division.

EXERCISE 19.

Divide:

-		
1. 624 by 2.	12. 9306 by 3.	23. 176 by 4.
2 862 by 2.	13. 746 by 2.	24. 215 by 5.
3. 684 by 2.	14. 368 by 2.	
		25. 252 by 6.
4. 396 by 3.	15. 459 by 3.	26. 364 by 7.
5. 693 by 3. 6 848 by 4.	16. 756 by 3.	27. 434 by 7.
6 848 by 4.	7501	
	17. 928 by 4.	28. 336 by 8
7. 484 by 4.	18. 568 by 4.	29. 568 by 8.
8. 884 by 4.	19. 655 by 5.	
		30. 736 by 8.
9. 555 by 3.	20. 605 by 5.	31. 378 by 9.
10. 8642 by 2.		
	21. 9246 by 2.	32. 459 by 9.
11. 3693 by 3.	22. 136 by 4.	22. 8128 by 4

figure in the inder to the not divide, the figure or de these as ad are taken the quotient.

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, and the Division.

 176 by 4.

 215 by 5.

 252 by 6.

 364 by 7.

 36 by 8.

 366 by 8.

 366 by 8.

 366 by 8.

 366 by 9.

 378 by 9.

 59 by 9.

9.

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11.

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28 by 4.

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DIVISION.

Divide :

34. 6126 by 3.	41. 972 by 3.	48. 7535 by 5.
35. 5255 by 5.	42. 896 by 4.	49. 9372 by 2.
36. 6312 by 6.	43. 675 by 5.	50. 6185 by 5.
37. 8432 by 8.	44. 775 by 5.	51. 8491 by 7.
38 756 by 3.	45. 735 by 7.	52 9656 by 8.
39 978 by 2.	46. 8208 by 4.	53. 9981 by 9.
40. 872 by 4.	47. 6075 by 3.	54. 32568 by 3.
Turner to		JT 34300 DV 3.

- 55. Twenty-seven thousand five hundred and twelve by eight.
- 56. Thirty-two thousand four hundred and ninety-six by six,
- 57. Fourteen million eight hundred and sixty-five thousand nine hundred and thirty-two by two.
- 58. Thirty-six thousand nine hundred and forty-five by nine.
- 59. Seventy-two thousand three hundred and forty-five by five.
- 60. Forty-five million eight hundred and twenty-eight thousand nine hundred and twenty-seven by nine.
 - The pupil should prove the answers to each of the preceding questions, instead of referring to the answers in the book.

EXERCISE 20.

Find the quotient and remainder, if any, in each of the following questions, proving each result :

	-	0	• •
(1)	(2)	(3)	(4)
4) <u>3654</u>	5)72584	3)86471	7)40505
(5)	(6)	(7)	⁽⁸⁾
9)476589	12)987654	11)334523	8)639724
$\begin{array}{r} 2718065+8,\\ 7893201+9,\\ 5013487+6,\\ 3920384+7,\\ 8372146+8,\\ 4365984+9,\\ 453678+11,\\ 1496583+12,\\ 5703214+7,\\ 6183420+8,\\ \end{array}$	19. 37068 20. 61758 21. 81609 22. 51172 23. 44650 24. 76003 25. 397843 26. 430176 27. 740086 28. 423056	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{c} 7814873+11.\\ 7076217+12.\\ 1275923+11.\\ 11330434+12.\\ 41241154+11.\\ 2314205+12.\\ 3^274604+11.\\ 4677021+12.\\ 8570198+11.\\ 5891270+12.\\ \end{array}$

- 39. How many times may 3 be taken from 27021?
- 40. How often is 4 contained in 28032?
- 41. The divisor is 5, the dividend is 33515 : find the quotient.
- 42. How many 7's in 44268?

84

- 43. How many times must 6 be taken from 49392 to leave no remainder?
- 44. How many 8's in 44248?
- 45. How many times 9 is 37845?
- 46. How many times 7 is 42924 ?

97. To divide by 10, 100, 1000, etc.

- The number 3766 may be read 376 tens and 6 units. Thus we see that if one figure be cut off the right of a number, the remaining figures shew the number of tens there are in it : as 376 in the case above.
- In the same manner, 3766 may be read 37 hundreds and 66. Thus, if two figures be cut off the right of a number, the remaining figures shew the number in dreds in it: 37 in this case.
- 98. Therefore we see that to divide by 10, 100, 10000, 10000, etc., we need only cut off one, two, three, four, etc., figures from the right of the dividend, the quotient will be the remaining figures, and the figures cut off will be the remainder.
 - (Compare Art. 79.)

Ex.-Divide 87631 by 1000.

- Cut off three figures from the right. The remaining figures, 87, will be the quotient, and the figures 631, that were cut off, will be the remainder.
- 99. This principle is very useful in the matter of dollars and cents, for, as there are 100 cents in every dollar, to bring any number of cents to dollars we need only cut off the last two figures as above, and the remaining number will be the required dollars, and the figures cut off will be the number of cents left over.

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DIVISION.

Ex.—86342 cents will be the same as 863 dollars and 42 cents; or,

86342 cents = \$863.42,

The dot . being placed to separate the dollars from the cents.

(Compare Art. 81.)

EXERCISE 21.

Divide :

	7316 by		8. 712934 by 100000.
	83174 by		9. 392 by 100.
3.			10. 37214 by 1000.
	73001 by		11. 74321 by 1000.
	97312 by		12. 30600 by 100.
	83916 by		13. 3000000 by 100.
7.	513712 by	100.	14. 6060600 by 100000.

- 15. Express 10862 cents in dollars, etc.
- 16. Express 312 cents in dollars, etc.
- 17. How many dollars will be the same sum as 461000 cents?
- 18. How many cents will be left if 861070 cents be exchanged for one-dollar bills?
- 19. How many dollar bills will be obtained?
- 20. How many dollars would buy as much land as 7310700 cents?

EXERCISE 22.

- 1. If 2 waggons of equal size carry 4896 bricks, how many bricks will one waggon carry?
- 2. If 2 houses are bought for 47054 dollars, how much is one of them worth?
- 3. If 3 mines cost 156378 dollars, how much does one mine cost?
- 4. If 3 times a certain price is \$47901612, what is the price?

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5. A grant of 60148 acres is to be divided among 4 per- sons: what is each one's share?	21.
6. Divide \$10632475 among 5 colleges : what will be the share of each ?	22.
 7. Eight men have an equal interest in 268112 acres of land: how much has each ? 8. If 9 square feet make one square yard, how many 	23.
square yards are in 26002197 square feet? 9. In a market garden containing 8 acres there are 42336 hills of potatoes: how many hills are there in one	24.
acre?	25.
10. Add the quotient of 36140292 divided by 9 to the quotient of 31623424 divided by 8	26.
11. Divide 163207431 by 3 times 3.	
12. A man died having an estate of 146329 dollars; his widow received 23193 dollars, and the remainder was divided equally among four hospitals: how much did each hospital receive?	27.
13. I have 327 lemons, and sell 311: how many remain? how much shall I receive at 8 cents each for those I have sold?	28. 29.
 14. At 2 cents each, how many apples can I buy for \$43.44? The same money will buy how many toys. at 3 cents each? How many tarts, at 4 cents each? 	30.
15. At 2 dollars a day, how many men can I hire for 346 dollars? For 496 dollars? For 3176 dollars?	31.
16. At 3 cents a spool, how many spools of thread can I buy for \$3.84? For \$5.73? For \$49.62?	32.
17. There are 4 pecks in a bushel: how many pecks are	33.
there in 3844 bushels? In 7688 bushels? In 15376 bushels?	34.
18. There are 4 quarts in a gallon : how many gallons are there in 132 quarts? In 396 quarts? In 792 quarts?	35.
19. How many pounds of sugar, at 9 cents a pound can I buy for \$36.90? For \$73.44?	36.
20. At 4 dollars each, how many tickets can be bought for 64 dollars? For 192 dollars? For 1152 dollars?	37.

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- 21. There are 3 feet in 1 yard: how many feet are there in 27 yards? In 16 yards? In 29 yards?
- 22. Three feet make r yard: how many yards are there in 69 feet? In 276 feet? In 828 feet?
- 23. If 4 pumpkins weigh 108 pounds, how much will 1 of them weigh? If 3 weigh 108 pounds, what will 1 weigh?
- 24. If 4 iron rods of equal length measure 44 feet, what is the length of each? If they measure 132 feet, what is the length of each?
- 25. If 3 bushels of turnips will fill one barrel, how many barrels will 255 bushels fill?
- 26. A man bought a lot for 3792 dollars, which was 3 times as much as his house cost him : how much did his house cost him?
- 27. Four asylums are to share equally 7248 dollars: now much does each receive?
- 28. How many barrels of meal, at 5 dollars a barrel, can be bought for 3575 dollars?
- 29. At 4 dollars each, how many hats can be bought for 796 dollars?
- 30. At 11 dollars a barrel, how many barrels of vinegar can be bought for 1749 dollars?
- 31. There are 7 days in one week, how many weeks are in 365 days (one year)?
- 32. If 9 acres of land cost 1125 dollars, what will 1 acre cost?
- 33. If 6 cows cost 1272 dollars, what will 1 cow cost?
- 34. If a horse travels 693 miles in 7 days how far does he travel in 1 day?
- 35. 1704 acres of land are to be divided equally among 8 charities: how many acres will each receive?
- 36. If 9 mules sell for 1359 dollars, what will be the sum received for each ?
- 37. A man bought 12 tons of hay for 180 dollars; how much did he pay a ton?

- 38. A boy sold 11 rabbits for \$2.75: how much did he receive apiece?
- 39. A girl spent \$3.54 for buttons, giving 3 cents apiece for them : how many did she buy?
- 40. X. is worth 15795 dollars, which is 5 times as much as Y. is worth, and Y. is worth 3 times as much as Z.: how much are Y. and Z. each worth?
- 41. A.'s land cost 2358 dollars, which is 3 times as much as the building of the house cost: what was the cost of the building?
- 42. A butcher bought 12 oxen for 1764 dollars : what was the average cost of each ?
- 43. A cooper worked 12 months for 216 dollars: how much did he receive a month?
- 44. If 4 yards of tweed will make a coat, how many coats could be made out of 1876 yards?
- 45. A grocer spent 3661 dollars in sugar at 7 dollars per barrel: how many barrels did he buy?
- 46. How many barrels of cider at 5 dollars a barrel could be bought for 2235 dollars?
- 47. There are 4 weeks in 1 month: how many months are there in 5764 weeks?
- 48. A grocer spent \$12.75 for baskets at 5 cents apiece : how many did he buy ?
- 49. A school-house was built jointly by 7 gentlemen at an expense of 2625 dollars: what sum did each subscribe?
- 50. In 1 bushel there are 4 pecks : how many bushels are in 1176 pecks?
- 51. A mill worth 43652 dollars was owned by 7 men in equal shares: what was the value of a share?
- 52. If a train in 8 days runs 2896 miles, what would be the average run in 1 day?
- 53. A patent valued at 38125 dollars was owned in equal shares by 5 men : how much did each man own?
- 54. At 6 dollars a gallon, how many gallons of wine could be bought for 2274 dollars?
- 55. From the sun to the earth is about 92000000 miles; light travels this distance in about 8 mir.utes: how many miles does light travel in a minute?

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Ex. 1.—Divide 18763 by 16.

16000	
16)2700(100 1600	
16)1160(70 1120	
$16) \frac{1}{43}(2) \frac{1}{32}$	

11 1172----11

The dividend is 18 thousand, 7 hundred, 6 tens, and 3 units.

- 16 is contained in 18 thousand 1 thousand times, leaving a remainder of 2 thousand, which with the 7 hundred make 27 hundred.
- 16 is contained in 27 hundred 1 hundred times, leaving a remainder of 11 hundred, which with the 6 tens make 116 tens.
- 16 is contained in 116 tens 7 times, leaving a remainder of 4 tens, which with the 3 units make 43 units.
- 16 is contained in 43 units 2 times, leaving a final remainder of 11 units.
- The whole quotient is therefore 1 thousand, 1 hundred, 7 tens, and 2 units, or 1172, and the remainder 11.

The noughts to the right, expressing the thousands, hundreds, etc., are omitted in practice, because the place of the figures shews their value.

Ex. 2.—Divide 588491 by 83. 83) 588491 (7090—-2t581 749 747

- The least number of figures on the left of the dividend that will contain 8_3 is 5,8,8, that is, 588 thousand, and this contains 8_3 ,7 times. $8_3 \times 7$ gives 58_1 ; or, in full, $8_3 \times 7000$ gives 581000. Subtracting the 581 from 588, we find the remainder to be 7. Bring down the next figure, 4, in the dividend, and we see that 74 will not contain 8_3 ; or, in other words, 74 hundreds will contain 8_3 no hundred times, and this no hundreds must be expressed in the quotient by the nought.
- Since 74 will not contain 83, we bring down another figure, 9. 749 contains 83, 9 times, with a remainder 2.
- Bring down the next figure, 1, and then, since 21 will contain 83 no times, we place a nought in the quotient and call the 21 our final remainder.

The following proof shews the correctness of the result :

$\begin{array}{rll} 8_3 \times 7 \ \text{thousands} = 581000\\ 8_3 \times 0 \ \text{hundreds} = & 0\\ 8_3 \times 9 \ \text{tens} & = & 7470\\ 8_3 \times 0 \ \text{units} & = & 0 \end{array}$	
Remainder 588470 21	
Dividend 588491	

- 01. When the divisor is greater than 12, and the different products are expressed, the process is called Long Division.
- 102. We then have the following

RULE FOR LONG DIVISION.

- Write the divisor and dividend as before, leaving a place on the right for the quotient.
- Find how many times the divisor is contained in the fewest number of figures on the left of the dividend. Place this as the first figure of the quotient.
- Multiply the divisor by it, and subtract the product from these figures at the left of the dividend.
- Attach, or bring down, to the difference. the next figure to the right in the dividend.

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DIVISION.

If the number thus formed will contain the divisor, place the number of times as the next figure in the quotient, and proceed as before; but if it does not contain the divisor, place a nought in the quotient, then bring down the next figure from the dividend.

91

Proceed in the same manner until all the figures in the dividend are brought down.

The number that is then left is the final remainder. PROOF—The same as in Short Division.

- In finding the quotient figure, the pupil will be assisted by seeing how many times the first figure of the divisor is contained in the first figure, or, if necessary, the first two figures of the dividend; an allowance being made for the carrying figure.
- If any of the remainders (before bringing down a new figure) be equal to or greater than the divisor, it shows that the previous quotient figure is too small, and must be increased.
- If any of the products of the divisor by a quotient figure be greater than the number above it, it shows that the quotient figure is too great, and must be diminished.
- After the first quotient figure is obtained, there must be as many figures written in the quotient as there are figures brought down from the dividend.

EXERCISE 23.

Divide :

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I.	J J	14.	8995 by	35	27.	475524 by 612	
2.	133 43 33	15.	9576 by		28.		
3.		16.	9315 by	45	29.		
	882 by 42		27715 hy		30.	3156584 by 722	
5.	2996 by 14	18.	43692 by	33	31.	5173302 by 834	
0.	3042 by 13	19.	82242 by	54	32.	5926431 by 643	
<u>7</u> .	3995 by 17	20.	88641 by	63	33.	3214664 by 566	
	5832 by 18		76875 by	75	34.	6923471 by 555	
	5103 by 21		35784 by		35.	14293624 by 675	
	7524 by 22		30618 by	126	36.	56243121 by 686	
1.	5448 by 24	24.	38232 by	236	37.	692348726 by 807	
	5668 by 26		146448 by	324	38.	496839715 by 1017	
3.	7099 by 31	26,	199864 by	301	39.	786935846 by 3118	

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40	. How m	any times	s can \$86 be taken from \$17354?
41.	\$52 fro:	m \$7012	?
42.	\$17 fro	m \$13354	?
43.	\$62 fro	m \$3406	?
		m \$45078	
		1 \$60702	
		n \$13415	
47.	How m	any 73's i	n 1731195?
48.		" 46's i	n 76131702 ?
49.	**	" 381's in	n 13261467 ?
50.		" 937's in	n 13189212?
51.		" 754's in	n 762294 ?
52.	"	" 112's in	n 51867?
53.	**		7281711?
54.		" 85's ii	1 33490 ?
55.	**	" 556's ii	3931476?
56.	•• •	' 2624's in	73484248?
57.	•• •	" 736's in	863256 ?
F	ind the o	uotients :	and also the remainders if any
	sulting f	rom the fo	blowing divisors and dividends :
58.	3076	and	11214887.
59.	269181	and	1246038849.
60.	6739549	and	2331883954.
61.		and	8659110.
6 .		1	

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1172481547818.

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DIVISION.

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- 73. Divide forty thousand two hundred and seventy-eight by seventy-five.
- 74. Divide seven hundred and sixty-five thonsand four hundred and thirty-one by ninety-six.
- 75. Divide three hundred thousand four hundred and twenty-eight by three hundred and twenty-four.
- 76. Divide forty-three million two hundred and ten thousand and forty by one thousand two hundred and thirty-six.
- 77. Divide fifty-six million thirty thousand one hundred and sixty-nine by two thousand and four.
- 78. Divide one hundred and nine million four hundred and twenty-six thousand and fifty-one by seven thousand three hundred and fifteen.
- 79. Divide four billion two hundred and eighty milnon nine hundred and sixty thousand three hundred and forty-two by fifteen thousand and three.
- 80. Divide thirty-one billion eighty-two million six hundred thousand five hundred and seventy-eight by four hundred and seven thousand and fifty-three.

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103. It was shewn in Art. 83 that instead of multiplying by 16, for example, we could use its factors, 4 and 4 The same principle holds true in Division.

Ex. 1.-Divide 8413 by 24.

$$3) \frac{8413}{2804 - 1}$$

350 - 4

The factors of 24 are 3 and 8, those being the numbers which, when multiplied together, produce or make up 24. We therefore divide by 3, which gives 2804 and 1 over, and then divide the quotient by 8, which gives 350 and 4 over

Now, the 2804 represents that number of 3's; hence the 4 that was left on dividing it by 8 must mean four 3's, or 12.

This 12 with the 1 left over at first makes in all 13, which is the exact remainder.

7354 ?

PROOF: $350 \times 8 = 2800$ $2800 \times 3 = 8400$ 8400 + 13 = 8413 *Ex.* 2.—Divide 42711 by 99. 9) 42711 11) 4745-6 431-4 $4 \times 9 = 36, 36 + 6 = 42$ Remainder.

The factors of 99 are 9 and 11. The final quotient is

43¹. The final quotient is

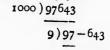
The last remainder 4 means four 9's, or 36, and this with the first remainder 6 gives us the true remainder, 42.

104. We thus have the following

RULE FOR DIVIDING BY FACTORS.

- Find the factors of the divisor. Divide the dividend, as usual, by one of them, and then this quotient by the other. This result will be the true quotient.
- To find the true remainder, multiply the last remainder, if any, by the first divisor, and to the product add the first remainder, if any. The result will be the required remainder.
- 105. This principle enables us to divide more easily by any number ending in noughts: for example, 800. The factors of this number are 8 and 100, so we divide by the 100 first and then by the 8, and find the true remainder in the usual way.

Ex. 1.-Divide 97643 by 9000.



 $7 \times 1000 + 643 = 7643$ Remainder. 106. This might have been done more rapidly thus 9)97.643

10-7643

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Div 1. 43

2. 30 3. 830 4. 43 5. 403 6. 84 7.739 8. 73 9. 631 10. 508 11. 508 12. 623 13. 400 14. 572 15. \$1 16. 17. 1 18. \$9 19.

DIVISION.

For we can divide by the 1000 by merely cutting off the three figures to the right (Art. 79), then divide the remaining figures by the 9, and to the remainder, 7, attach the figures cut off, making in all 7643.

Ex.	2	Divide	976341	by	3700.	
-----	---	--------	--------	----	-------	--

37)9763′41 (263	
74	
236	
222	
143	
111	
32	3241 Remainder.

First cut off the 41 to the right or the dividend, then to the remainder 32 attach the two figures 41, and we have the full remainder, 3241.

EXERCISE 24.

Divide :

Billide,			
1. 436899 by 14.	20.	8349 by	100.
2. 300527 by 18.	21.	7630 by	100.
3. 8307611 by 16.	22.	7491 by	1000.
4. 439205 by 21.	23.	\$860000 by	100.
5. 4031729 by 24.	24.	312946 by	10000.
6. 843043 by 25.	25.	36972 by	10.
7. 7390478 by 28.	26.	131111 by	400.
8. 736255 by 42.	27.	23218 by	60.
9. 6310972 by 49.	28.	\$22120 by	70.
10. 5084263 by 35.	29.	40220 by	1900.
11. 5083753 by 48.	30.	131127 by	
12. 6230749 by 56.	31.	89952 by	500.
13. 4003767 by 36.	32.	7306597 by	30.
14. 5726009 by 44.	33.	4590000 hy	306000.
15. \$19866 by 77.	34.	\$13834500 by	
16. 8514 by 99.	35.	11579112 by	890000.
17. 15336 by 72.	36.		
18. \$93312 by 108.	37.	796532 by	230.
19. 4361 by 10.	38.	46512 by	8000.
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EXERCISE 25.

1. A man bought 15 horses for \$1455 : how much did he pay apiece ?	20.
2. A man paid \$1400 for oxen : at the rate of \$56 each, how many did he buy?	21.
3. What will 1 barrel of oatmeal cost, if 37 barrels cost \$296?	
4. There are 28035 pages in 89 volumes: how many pages will be in each book ?	22.
5. A horse can travel 45 miles in a day : how long will he take to go 3330 miles ?	23.
6. The wages of Jones for 17 months come to \$595 : how much was he paid a month?	24. 25.
 7. The cost of 97 sheep was \$388: what did each cost? 8. If 95 lots of land cost \$22515, what is that for one lot? 	26.
9. My agent sends me from Montreal 4368 hams, being 13 times too many : how many did I require?	27. 28.
10. If 15 boys work 5475 questions in 15 weeks, how many did each boy do?	29.
11. There are 24 hours in the day: express 66360 hours in days.	
12. In the workhouse there are 72 men whose ages amount to 5976 years : what is the average age of each ?	30. 31.
13. I can employ 15 carpenters for \$3555 for the season: what do I pay each man?	32.
14. There is a new moon every 28 days: how many new moons will there be in 108192 days?	

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DIVISION.

- 15. How many battalions can be formed out of 32340 soldiers, giving 420 men to each battalion?
- 16. How many 10-cent pieces would make up \$64.60?
- 17. How many 25-cent pieces would pay a debt of \$468?
- 18. A wealthy merchant distributed to 980 poor people, in an equal proportion, 876432 pounds of flour: what would each receive, and how much would be left?
- 19. If 63 gallons make a hogshead, how many hogsheads will there be in 1449 gallons?
- 20. How much would be left from \$2449 after 116 men had been paid 21 dollars each?
- 21. An excursion boat can carry 105 people : how many trips must it run to take 2486 people, and how many go on the last trip ?
- 22. The total outfit of a regiment of cavalry 1200 strong cost \$236400 : what was the cost of each man's outfit ?
- 23. How many miles of road, at \$26000 a mile, can be built for \$11050000?
- 24. To give 236979, by what must I multiply 1809?
- 25. In an engagement, 4376 soldiers use 205672 cartridges : how many is that for each man ?
- 26. How many feet are there in a mile, if 42 miles contain 221760 feet?
- 27. Of what number is 158 both divisor and quotient?
- 28. How many bales of cotton, each weighing 427 pounds, are there in a crop of 468419 pounds?
- 29. A moulder has 17385 pounds of metal : find the least number of pounds he must buy in order to cast cannonballs each weighing 68 pounds?
- 30. How many could he then cast?
- 31. Divide one billion by 256.
- 32. The quotient is 345, the dividend is 273240: find the divisor.

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EXAMPLES ON ALL PREVIOUS PRINCIPLES.

Ex. 1.—If 5 apples cost 10 cents, what must I pay for 8 apples ?

If 5 apples cost 10 cents, 1 apple must cost 2 cents, and 8 apples would cost 8 times 2 cents, or 16 cents.

Ans. 16 cents.

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Ex. 2.—How many pears at 3 cents apiece ought 1 to receive in exchange for 12 apples at 2 cents apiece? In order to make the bargain even, the value of all the pears must be the same as the value of all the apples, which is 24 cents. How many pears, then, must there be to amount to 24 cents, at 3 cents apiece?

Ans. 8 pears.

Con account of the pears being worth more apiece than the apples, there must be a less number of pears than apples.

Ex. 3.—If 3 men can build a house in 21 days, how long must 7 men be employed to do the same work?

If 3 men take 21 days, one man would require 3 times as long as 3 men, that is, 63 days. One man doing the work in 63 days, 7 men would need only 9 days.

Ans. 9 days.

The pupil must be taught very carefully to distinguish between Ex. 1 and Ex. 3. It is quite natural to reason thus: If 3 men take 21 days, 1 man would take 7 days; in fact, this is the very mistake the pupil will be apt to make.

Ex. 4.—A boy bought the same number of oranges as lemons, paying 5 cents each for oranges and 7 cents each for lemons: how many would he get for 84 cents?

If the boy had only 5 cents and 7 cents, that is 12 cents. he could only buy 1 orange and 1 lemon. Hence, for every 12 cents he owns he could buy one of each, and as he owns 84 cents, or 7 times 12 cents, he could buy 7 oranges and 7 iemons. Ans. 7 of each.

Ex. 5 - I gave 11 peaches to each of 8 boys, and kept 5 myself: how many had I at first?

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For the boys alone I would need 8 times 11 peaches, or 88 peaches; but as I want 5 myself I must have 88+5, or 93, to begin with. Ans. 93 peaches.

In this problem the 93 is the dividend, the 8 is the divisor, 11 the quotient, and 5 the remainder. Hence we see that to find the dividend, 93, we multiply the divisor and quotient together, and add in the remainder.

Ex. 6. A man buys a farm of 150 acres at 80 dollars an acre; he pays \$5000 down, and the rest in 8 equal yearly payments: what does he pay each year?

The cost of the farm is $80 \times 150 = 12000$. After paying 5000 down, there will be left 12000 - 5000 =7000 to be paid in 8 equal payments. Each payment must therefore be 7000 + 8 = 875. Ans. 8875.

EXERCISE 26.

- I. A merchant left \$4538 to his wife, \$3289 to his daughter, and \$2567 to his nephew : what was the amount of his property ?
- 2. I bought a buggy for \$475, and a pair of horses at \$175 each : find the whole cost.
- 3. Which is worth more, 27 houses at \$1125 each, or 205 oxen at \$140 each: and how much?
- 4. Divide the product of 204 and 238, by their difference.
- 5. Seven hundred and eight men are formed in two rows: how many will be in each row? How many in each row if they were drawn up in four rows? How many if in six rows?
- 6. From what number must 72 be taken to leave a remainder equal to 3 times 45?
- 7. Find a number to which if 347 be added the sum will be 347 less than 1000.
- 8. How many times does a clock, if it sounds the hours, strike in a day?

9.	A man bought 47 feet of land : for 25 feet he paid $$41$ a foot, for the rest $$45$ a foot : how much did all cost?	23
10.	Add three hundred and sixty-two thousand four hun- dred and nine to eight hundred and seven thousand nine hundred and eighty-four, and divide their sum by eight.	24
11.	A man left \$14389 to be divided thus : to his widow \$5000, to his son \$4000, to each of four servants \$100, and the rest to be equally divided among his three daughters : what will each of the daughters receive?	26.
12.	There are 24 sheets of paper in a quire : how many sheets in 3 dozen packets, each containing 5 quires?	27.
13.	A farmer bought 3 horses and 4 mules for \$1122; the mules cost \$144 each: what did each of the horses cost?	28.
14.	A merchant bought 13 bales of cloth, each bale con- taining 27 pieces, and each piece measuring 34 yards: what would be the value of the whole at 17 cents per yard?	20. 30.
15.	If 36 men can cut a road in 77 days, how many men can do the same in 21 days?	
16.	How many yards of velvet at 7 dollars a yard, 8 dol- lars a yard, and 9 dollars a yard, the same quantity of each, cau a dealer buy for 1800 dollars?	31. 32.
17.	What number added to the product of 327 and 8; will give 30000?	33.
18.	When a man's property was divided, his son received \$5148, and the rest was divided among 11 churches. giving each \$936: what was the property worth?	34.
19.	Divide the sum of 5168 and 5206 by three times their difference.	35.
20.	How many weeks will it take a man to build 17 wall: of 154 feet each, if he build 22 feet a week?	36.
21.	What must be multiplied by 327 to give 236421 gallons?	. Jo.
22.	A. had 75 cows, B. 90 oxen; each sold his cattle for \$2250: how much per head did A. receive more than B.?	37.

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- 23. I bought 16 pieces of print of 33 yards each at 10 cents a yard, and paid for them with tea at 80 cents a pound: how much tea was given?
- 24 The quotient is 345, the dividend 273240: what is the divisor?
- 25. The divisor is 213, the quotient 437, and the remainder 196: what is the dividend?
- 26. A. has 2280 dollars to lay out for horses and oxen, and wishes to purchase the same number of each: if he pays \$65 a head for horses and \$30 for oxen, how many of each can he buy?
- 27. I bought some books for \$3.57, and sold them at 20 cents apiece, losing 17 cents: how many books were there?
- 28. A vessel saus 5712 miles in 48 days : how many miles does she go in a day ? how many in 5 days ?
- 20. A man's salary is \$3150 a year; his expenses are \$2817 a year: how much can he save in 6 years?
- 30. A.'s income is 5 times B.'s, B.'s income is 3 times C.'s, and C.'s income is \$1325: find the incomes of all together.
- 31. How many cases, each containing 6 dozen books, can be filled from 18 parcels, each containing 3124?
- 32. If 27 clerks receive \$3888 for 16 days' work, how much a day was that for each man?
- 33. What number is that to which if 17 be added the result is five times 384?
- 34. A man's income is 398 dollars a year: if he spend each year 256 dollars, how much will he save in 12 years?
- 35. A man had an income of \$3742 a year (52 weeks); he spent \$1500, gave to the hospital \$370, and saved the rest: how much did he save per week?
- 36. If 563 be multiplied by a certain number, and 1043 be added, the result is 23000: find the number.
- 37. For 21 pigs and 43 calves a farmer received \$401; the calves were sold at \$2 each: what was the price of each pig?

38. Find a number, such that if the sum of 89 and 256 be subtracted from it, the remainder is 12 times 399.	55.
39. A man bought wheat at 47 cents a bushel, and sold it for 55 cents a bushel; he gained \$3276.45: how many bushels did he buy?	56.
40. What number must be multiplied by 37 to make the product equal to the sum of 1998 and 2006?	57.
41. Eight pounds of tea cost \$4.80: what was the price of 6 pounds?	
42. If 11 men can sod an acre of ground in 12 days, how many days will 4 men take to do the same amount of sodding?	58.
43. If 144 dollars would pay for 24 yards of cloth, what will be the price of 56 yards of the same kind?	59 . 60,
44. Seven sheep can be bought for \$24.50: how much will a flock of 133 cost?	
 45. If 4 bushels of apples can be bought for \$3, how many, at the same rate, can be bought for \$51? 	б1.
56 cents pay for ?	
47. In how many hours can 2 boys do as much work as 6 boys in 3 hours?	62.
48. In how many days can 4 boys earn as much as 8 boys in 6 days ?	63.
49. In how many weeks can 15 men earn as much as 3 men in 25 weeks?	64.
50. In how many days will o norses eat as much as 18 horses in 5 days?	0. .
51. Divide the sum of 1692 and 1786 by their difference.	1 65. 1
52. A man exchanged 159 coats at \$5 each for a horse valued at \$144, and the balance in hats at \$3 apiece: how many hats did he receive?	t l
53. A. traded with B., giving 305 paintings at \$45 each, and receiving 77 reapers at \$181 each : which owes the other, and how much ?	66. I ł
 54. \$89648 is 8 times as much as I paid for a house; but I paid \$126 more than the house was worth : what was it worth? 	67. A a s
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- 55. I bought 312 barrels of oatmeal at \$5 a barrel, and sold them for \$2496: how much was gained on each barrel?
- 56. By selling 31 lots for \$3100 I lose \$155: for what should I sell 16 lots to gain \$597?
- 57. A man's yearly salary was \$9237; he spent \$136 on house repairs; for hired men he paid 4 times as much, lacking \$95; and for other expenses, \$1902: what has he left to put by yearly?
- 58. I bought 25 sacks of flour for \$125: what must I sell them for per sack to gain \$75?
- 59. What will be the gain on each sack in the last question?
- 60. Jones sold the same number of plover, snipe, and quail for \$17.70—the plover at 12 cents, the snipe at 37 cents, and the quail at 69 cents each: how many of each did he sell?
- 61. Ten thousand railway checks are to be marked by 3 men; the first marks 200 an hour; the second and third each mark 150 an hour: how long will they take to mark the whole, all working together?
- 62. If 59 articles cost me \$43.07, how much must I sell 23 of them for to gain \$1.83 on those sold?
- 63. A man earns \$50 a month, but it costs him \$30 a month to live: how many months will he take to save enough to purchase 48 acres of land at \$10 an acre?
- 64. I sold 28 horses at \$122 each; then bought 224 sheep at \$12 each, 8 cows at \$60 each, and spent the remainder in calves at \$8 each: how many calves did I buy?
- 65. If it costs \$56 for bricks to build a cistern, when bricks are worth \$8 a thousand, what will it cost for bricks to build it, when they are worth \$10 a thousand?
- 66. If 5 barrels of cider are worth \$20, how many tons of hay, at \$12 a ton, will 9 barrels of cider buy ?
- 67. A merchant bought 3 pieces of cloth of equal lengths at \$5 a yard; he gained \$35 on the whole cost by selling 2 pieces for \$350. How many yards in each piece?

107. The following examples will be found somewhat similar to those in Exercise 16, and although rather more difficult, the pupil should now be able to solve them mentally with a fair degree of rapidity.

The note in Art. 85 applies equally well to this case.

EXERCISE 27.

- 1. To 5 add 7, multiply by 3, subtract 6, divide by 5, multiply by 8, divide by 4, add 8: what is the result?
- 2. From 15 take 8, multiply by 6, divide by 7, add 10, divide by 8, add 20, subtract 4, divide by 3, multiply by 7: what is the result?
- 3. Multiply 7 by 8, subtract 2, divide by 6, add 7, divide by 4, add 26, divide by 5, multiply by 7, add 6, divide by 8, multiply by 4: result?
- 4. Divide 45 by 5, multiply by 3, add 8, divide by 7, add 31, subtract 4, divide by 8, multiply by 9, add 6, divide by 7, add 15, subtract 9, multiply by 8: result?
- 5. Add 9 to 19, divide by 7, multiply by 8, take 7, divide by 5, multiply by 12, subtract 4, divide by 8, add 27: result?
- 6. Subtract 7 from 25, divide by 6, multiply by 9, add 8, divide by 7, multiply by 20, subtract 4, divide by 12, multiply by 3: result?
- 7. To the product of 7 and 5, add 9, divide by 11, multiply by 12, subtract 3, divide by 9, multiply by 10, add 6, divide by 7, add 8, divide by 2, add 19, divide^bby 9, multiply by 12: result?
- 8. To the quotient of 63 divided by 7, add 6, multiply by 4, divide by 12, add 30, divide by 7, add 16, divide by 7, multiply by 11, add 9, divide by 7, add 15, subtract 7, divide by 7, add 16 : result?
- 9. To the difference between 7 and 15, add 10 divide by 6, multiply by 11, add 9, divide by 7, multiply by 9, subtract 6, divide by 8, multiply by 7, add 9: result?

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de by [·] by 9, esult ?

- 10. To 23 add 9, divide by 8, add 35, divide by 3, add 8, divide by 7, multiply by 20, divide by 10, add 27, subtract 9, divide by 8, multiply by 15, add 19: result ?
- 11. From 41 take 5, divide by 9, multiply by 11, add 12, divide by 8, multiply by 7, subtract 5, divide by 4, multiply by 7, subtract 5, divide by 9, add 34, divide by 2: result?
- 12. Add 35 to 9, divide by 11, multiply by 25, subtract 16, divide by 12, add 43, divide by 5, add 53, subtract 13, divide by 5 : result ?
- 13. Multiply 7 by 8, add 10, divide by 11, add 21, divide by 9, multiply by 12, add 12, divide by 8, multiply by 11, divide by 22: result?
- 14. Divide 72 by 9, multiply by 7, subtract 8, divide by 6, multiply by 12, add 12, divide by 9, add 52, divide by 8, multiply by 10, divide by 20 : result?
- 15. To 61 add 11 divide by 6, subtract 11, add 55 divide by 7, multiply by 6, subtract 18, divide by 6, multiply by 30, take 50, divide by 5 : result?
- 16. From 85 take 15, divide by 7, multiply by 8, add 16, divide by 8, add 30, divide by 7, multiply by 12, add 8, divide by 8: result?
- 17. Multiply 30 by 4, divide by 12, add 25, divide by 7, multiply by 11, add 9, divide by 8, multiply by 5, subtract 7, add 3, divide by 9: result?
- 18. Add 17 to 20, subtract 9, divide by 7, multiply by 25, subtract 4, divide by 8, add 8, multiply by 4, subtract 20, add 30, divide by 10, multiply by 8, add 12, divide by 12, add 10: result ?
- 19. Divide 56 by 8, multiply by 9, divide by 7, multiply by 8, add 5, divide by 11, multiply by 6, add 21, divide by 9, add 20, divide by 3, multiply by 5, add 15, divide by 10, multiply by 8, divide by 6: result?
- 20. From 63 take 9, add 16, divide by 10, add 41, subtract 20, divide by 4, add 93, subtract 17, add 2, divide by 5, multiply by 3, subtract 8, add 27, divide by 7, subtract 10, multiply by 13: result?

CHAPTER II.

FACTORING.

- 108. There are two ways of making up the number 6, either by adding 4 and 2, or by multiplying 3 and 2.
 - As in Art. 83, where the number 6, is made up by multiplying 3 and 2, each of these numbers is called a Factor of 6. Each of them is also an Exact Divisor of 6.
- 109. A Factor of a number may therefore be said to be an **Exact Divisor** of the number.
 - It is very desirable that the pupil should be able to tell the different Divisors of any number.
 - Ex. 1.—Find all the Divisors of 18.

 $18 = 9 \times 2$, or 3×6 ,

Hence the Divisors are 9, 6, 3, 2.

- 110. The numbers 2, 3, 5, 7, 11, etc., have no exact Divisors or Factors, and all such numbers are called **Prime Numbers**.
 - Since the number 3 divides both 6 and 9, 3 is said to be a Common Divisor of 6 and 9. So 5 is a Common Divisor of 15 and 20; 4 is a Common Divisor of 3, 12, and 16.
- 111. A Common Divisor is any number that will exactly divide two or more numbers.

Ex.—Find a Common Divisor of 16, 20, 24.

 $16=2 \times 8.$ $20=2 \times 10.$ $34=2 \times 12,$ Therefore 2 is a Common Divisor. (106) Th We J

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Again, .

 $16=4\times4, \\ 20=4\times5, \\ 24=4\times6,$

Therefore 4 is also a Common Divisor.

We thus see that there may be more than one Common Divisor to two or more numbers; and, since 4 is the greater of the two Divisors, it is called the **Greatest Common**-**Divisor** of 16, 20, and 24.

112. The Greatest Common Divisor (G.C.D.) is the greatest number that will exactly divide two or more numbers.

Ex.—Find the Greatest Com. Div. of 18, 24, 30. We see, by inspection, that 2. 3, and 6 are the only Common Divisors of 18, 24, and 30, therefore the G. C. D. is 6.

- The Divisors, Common Divisors, and Greatest Common Divisors should, if possible, be found by inspection.
- 113. The following will be found a simple method of finding the G. C. D. of any numbers:

Take 16, 24, and 50.

- The G. C. D. cannot be greater than 16, and must be some divisor of 16. The greatest divisor of 16 is 8, but this will not divide 50. The next divisor of 16 is 4, but this will not divide 50. The next divisor is 2, and since this also divides 24 and 50, it must be the G. C. D.
- 111. This gives us the following

RULE FOR FINDING THE GREATEST COMMON DIVISOR.

Take the least of the given numbers and try its divisors in order, beginning with the greatest.

The first one that will divide each of the other numbers will be the required Greatest Common Divisor.

Ex.-20, 24, and 28.

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24.

The divisors of 20 are 10, 5, 4, and 2. The first one that divides both 24 and 28 is 4. Hence 4 is their G.C.D.

EXERCISE 28.

These questions should be solved mentally.

- 1. What numbers will exactly divide 12? 48? 56? 81?
- 2. Find the exact divisors of 21; 32; 49; 42; 36.
- 3. What numbers under 50 are exactly divisible by 2? 3? 4? 5? 6? 7? 8? 9? 10? 11? 12?
- 4. What numbers between 50 and 121 have for a factor 5? 7? 9? 12? Write down the other factor in each case.
- 5. Write down the simplest or prime factors of 64, 54, 78, 120, 145, 152, 99, 117, 189.
- 6. What numbers less than 150 are divisible by both 3 and 4? 4 and 5? 5 and 6? 3 and 8?
- 7. Name the three least numbers that exactly contain both 3 and 5; 2 and 5; 2 and 3; 3 and 4; 4 and 5.
- 8. Write down in order the prime numbers less than 50; between 50 and 100.
- 9. What three prime numbers will divide 42? 30? 105?
- 10. Find the common divisors of 24 and 30; of 27 and 36; of 15 and 45; of 36 and 64; of 72 and 80; of 90 and 120.
- 11. Name all the common divisors of 12, 18 and 20; of 24, 40 and 60; of 36, 48 and 72; of 24, 36, 60, 72.
- 12. Write down the G. C. D. in each part of questions 10 and 11.
- 13. What is the G. C. D. of 16, 24, and 36? of 9, 27, and 33? of 15, 35, and 50? of 18, 32, and 60?

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FACTORING.

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115. When the given numbers are large, the G. C. D. can not always be found by inspection.

The following method is then adopted :

Ex.-Find the G. C. D. of 697 and 820.

697)	820(1 697
	123)697(5 615
	41)82(2 82
	02

Divide the less into the greater number—the remainder is 123, which we divide into the first divisor 697. This leaves a remainder 82, which we divide into the previous divisor 123, leaving a remainder 41. The number 41 is divided into the previous divisor 82, and since it is contained exactly, 41 is the **G. C. D.**

In finding the G. C D., if the last divisor is 1, the given numbers are r = d to be prime to one another.

116. From the above we have the following

RULE FOR FINDING THE GREATEST COMMON DIVISOR.

Divide the less into the greater of the given numbers, then divide the remainder then obtained into the previous divisor, and so on, until an exact divisor is obtained. This exact divisor will be the G. C. D. required.

If there be three or more numbers, find the G. C. D. of any two of them. Then find the G. C. D. of this result and a third number and so on. The final result will be the G. C. D. required.

Ex.-Find the G. C. D. of 585, 765, and 285.

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8? 56? 81? 42; 36.

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tly contain 4; 4 and 5. rs less than

? 30? 105? ; of 27 and and 80; of

and 20; of 6, 60, 72. questions

f 9, 27, and

The G. C. D. of 585 and 765 is 45. The G. C. D. of 45 and the third number 285 is 15. Hence 15 is the G. C. D. of the given numbers.	118. 4
The pupil should prove the truth of the result, in other words, see that the G. C. D. obtained will exactly divide each of the given numbers.	A
Thus: $585+15=39$.	
765+15=51. 285+15=19.	119. A
EXERCISE 29.	
1. Find the greatest common divisor of 161 and 115.	
2. Find the greatest common divisor of 592 and 332.	N
 Find the greatest common divisor of 2013 and 1220. Find the greatest common divisor of 576 and 960. 	
5. Find the greatest common divisor of 592 and 1225.	
6. Find the greatest common divisor of 1369 and 703.	120. T
7. Find the greatest common divisor of 1866 and 1492.	120. 1
8. Find the greatest common divisor of 1029 and 1197.	
9. Find the greatest common divisor of 992, 352 and 672.	
10. Find the greatest common divisor of 867, 1088 and	
714. 11. Find the greatest common divisor of 1134, 1386 and 630.	R
12. What is the length of the longest pole that will	
measure 84 feet, 56 feet and 70 feet?	121. TH
117. Wherever we have a Divisor we must have a Dividend. The object of the previous exercise was to	Ta
find the Divisor . We shall now proceed to find the	Tł
Dividend, of which certain numbers are given as Divisors. When we speak of a Divisor or a Divi-	
dend, we always refer to an Exact Divisor and an Exact Dividend.	
Since $3 \times 4 = 12$, 12 contains both 3 and 4, and is there-	
fore an Exact Dividend of 3, and also of 4.	

G. C. D. of nce 15 is the

the result, in btained will rs.

- 51 and 115. 92 and 332. 13 and 1220. 76 and 960. 92 and 1225.
- ig and 703.
- 6 and 1492.
- 2, 352 and
- 7, 1088 and
- 4, 1386 and
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ve a Divircise was to l to find the re given as or a Divisor and an

nd is thereof 4. 118. An **Exact Dividend** of a given number is therefore a number which will contain the given number without any remainder.

An Exact Dividend is also called a Multiple.

- Since 15 contains 3 and also 5 exactly, 15 is a dividend of 3 and also of 5, and is called a **Common Dividend** of 3 and 5.
- 119. A Common Dividend is a number that contains two or more numbers exactly.

Ex.—24 is a Common Dividend of 2 and 4. 18 is a Common Dividend of 2, 3. and 5.

- Now, 36 is a Common Dividend of 2, 3, and 4; and so likewise is 24, and also 12. And since of the common dividends 36, 24, and 12, 12 is the least, it is called the Least Common Dividend of 2, 3, and 4.
- 120. The Least Common Dividend (L. C. D.) of two or more numbers is the least dividend that will contain each of the numbers exactly.

Ex.—The L. C. D. of 2, 3, and 8 is 24, because 24 is the least dividend that will contain 2, 3, or 8. The L. C. D. of 4, 5, 12 is 60.

- All Dividends, Common Dividends, and Least Common Dividends should be found, if possible, by inspection.
- 121. The following will be found a good method of finding the L. C. D. mentally:

Take 5, 8, and 12.

The L. C. D. cannot be 12, because 12 does not contain either 5 or 8. The next number that contains 12 is 24, but this does not contain 5, although it contains 8. Then we try 3 times 12, 4 times 12, etc., until we come to 9 times 12, or 108. None of these will answer, but the next one, 10 times 12, or 120, contains both 5, 8, and 12, and must be the L. C. D.

122. Hence we have the following

RULE FOR FINDING THE LEAST COMMON DIVIDEND.

Take the greatest of the given numbers, and try its dividends in order, beginning with the least. The first one that will contain each of the other numbers will be the required Least Common Dividend.

Ex.—Find the L. C. D. of 10, 24, and 30.

The successive dividends of 30 are 60, 90, and 120; and since 120 is the first one that will contain 10 and 24, the L. C. D. must be 120.

EXERCISE 30.

F These questions should be solved mentally.

- 1. What numbers below 50 are dividends of 2? of 3? of 4? of 5? of 6? of 7? of 8? of 9? of 10? of 11? of 12?
- 3. What numbers between 50 and 145 exactly contain 7? 9? 11? 12?
- 4. Of what two prime numbers is 12 a common dividend?
- 5. Of what numbers is 12 a common dividend? 18? 24? 30?
- 6. Write in order each number below 100 that 1s a common dividend of 2 and 3; of 3 and 7; of 2, 3. and 4; of 4, 5, and 6; of 2, 5, and 7; of 2, 3, 4, and 5; of 3 and 8; of 8 and 10.
- 7. Write down the L. C. D. in each part of question 6.
- 8. Find the L. C. D. of 8 and 12; of 9 and 12; of 2, 4. 5, and 6; of 2, 3, and 10; of 3, 4, and 8; of 4, 5, and 8; of 6, 3, and 8; of 2, 5, 8, and 10; of 3, 12, and 4; of 6, 18, and 9; of 4, 12, and 16; of 8, 10, and 12.

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FACTORING.

- 123. In finding a common dividend of 3, 4, 12, 15, we need not consider 3 or 4, because any number that is a dividend of 15 must be a dividend of 3; and any number that is a dividend of 12 must be a dividend of 4.
 - Hence in finding the L. C. D. of any numbers we may always strike out any one of them that is a divisor of any other.

124. We thus have the following

RULE FOR FINDING THE LEAST COM-MON DIVIDEND OF SEVERAL NUM-BERS.

- Place the given numbers in a line, and first strike out any one of them that is a divisor of any other.
- Then begin with the lowest divisor, 2, and divide by it as often as it is contained in any two of the numbers, bringing down any numbers that are not divisible.
- Proceed thus with 3, 5, 7, etc., always striking out in any line any number that is a divisor of any other number in that line.
- Finally, multiply together the different divisors and all the numbers in the last line.

The product thus obtained will be the required L. C. D.

Ex.—Find the Least Common Dividend of 4, 6, 10, 12, 30, 45, 75, 100.

2) <u>4</u> ,	6,	XØ,	Ι2,	30,	45,	75,	100
2)			6,	ĽŞ,	45,	75,	50
3)			3,		45,	75,	25
5 _)					15,	25,	
						2.	5	

L.C.D. $-2 \times 2 \times 3 \times 5 \times 3 \times 5 = 9^{\circ 0}$. Ans.

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question 6.

12; of 2, 4, of 4, 5, and 12, and 4; o, and 12.

- Writing the numbers in a line, we first strike out 4 and 6, since each is a divisor of 12. Then strike out 10, since it is a divisor of 30. (Art. 123.)
- Now divide by 2, and we obtain the quotients as above, of which we strike out 15, because it is contained in 45.
- Again divide by 2, and then strike out 3 and 25, for each is contained in 75.
- Now, since 2 will no longer divide any two numbers in the line, we try 3, and then 5.
- Finally, multiply together the four divisors and the last quotients, and we obtain the L. C. D. as above.
- 125. To find the L. C. D. of two large numbers, we first find the Greatest Common Divisor.
 - Then divide this G. C.[•]D. into either of the numbers, and multiply the quotient by the other number.
 - The product will be the required least common dividend.

Ex.—Find the L. C. D. of 970 and 1261. Their greatest common divisor will be found to be 97.

Then 970 + 97 = 10.

 $1261 \times 10 = 12510$, which is the required L.C.D.

Proof:

12610 + 970 = 13.12610 + 1261 = 10.

126. If there be several large numbers, find the L. C. D. of any two, then find the L. C. D. of this result and a third number, and so on.

The final result will be the required L. C. D.

As in the case of the Greatest Common Divisor, the pupil should prove the truth of the result by finding, as in Art. 125, if the L. C. D. will contain each of the given numbers exactly.

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EXERCISE 31. Find the Least Common Dividend: 1. Of 5, 15, 9, 6 and 3. 2. Of 4, 5, 10, 8, 18 and 15. 3. Of 12, 36, 25, 60, 35 and 72. 4. Of 63, 81, 14, 54, 27 and 9. 5. Of 7, 72, 84, 42, 12 and 6. 6. Of 72, 36, 180, 24, 18, 9 and 120. 7. Of 90, 10, 64, 70, 45, 8 and 32. 8. Of 40. 24, 8, 32, 20, 16 and 10. 9. Of 29, 144, 216, 180, 90 and 252. 10. Of 60, 78, 42, 96, 56, 48 and 39. 11. Of 2041 and 8476. 12. Of 812 and 336. 13. Of 7056 and 7392. 14. Of 7212, 9015 and 24040. 15. Of 7218, 6015, and 5213. 16. Of 2712, 816, 54, and 15. 17. Of 250, 360, 49, and 700. 18. Of 32, 44, 52, 13, 65, and 48. 19. Of 76, 748, 448, 152, and 38. 20. What is the smallest quantity of barley that can be carted away in either 20, 25, 30, 35, or 40 bushel carts, and how many loads would there be of each?

21. Find the least amount of money that can be paid by either 2, 3, 4, 5, 10, 20, 50, or 100 dollar bills and how many of each kind would be required?

CHAPTER III.

FRACTIONS.

- 127. We have spoken of one dollar, one pound, one pint, one foot, etc., but have not mentioned any smaller part than one of each. We must now see how we can express any part of a dollar, a pound, a pint, or a foot.
 - If we divide a foot, for instance, into two equal parts, each part is called a half, and written 1—the figure showing that the unit (in this case a foot) is divided into two equal parts, and the figure 1 showing that we have taken one of these parts.
 - In the same way, if a foot be divided into 3, 4, 5, 6, etc., equal parts, each part will be called a third, fourth, fifth, sixth, etc., respectively, and be represented by $\frac{1}{3}$, $\frac{1}{4}$, $\frac{1}{5}$, $\frac{1}{6}$, etc.
 - It will also be seen that to make up the whole, or the unit, we must take

Two-halves, or Three-thirds, or Four-fourths, or Five-fifths.

etc., etc.

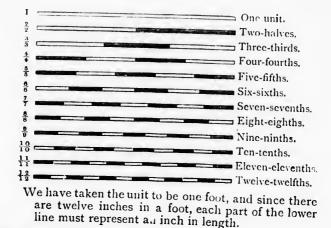
This will be easily seen from the following figure, where the unit is taken as a foot in length.

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129.

FRACTIONS.



128. The following result will then be seen by using a straight-edge or measure :

The whole One-half One-third One-fourth	equals "	12 inches. 6 inches. 4 inches.
One-fourth One-sixth	**	3 inches. 2 inches.
		~ mones.

Thus we see that we find one-half of any number by dividing it by 2, one-third by dividing it by 3, onefourth by 4, etc.

Hence, $\frac{1}{2}$ of 40 cents = 10 cents. $\frac{1}{9}$ of 81 apples = 9 apples. $\frac{1}{16}$ of 30 days = 2 days.

129. Again, referring to our figure, we see that two-thirds of 12 inches are 8 inches, that is, twice as long as one-third; three-sixths are 6 inches, or three times as much as one-sixth; seven-twelfths are 7 inches. or 7 times as much as one-twelfth.

In the same manner, $\frac{1}{11}$ of \$44 must be 5 times $\frac{1}{11}$ of \$44, that is 5 times \$4, which is equal to \$20.

So, $\frac{4}{9}$ of 63 = 4 times $\frac{1}{9}$ of 63 = 28. $\frac{1}{18}$ of 26 = 10 times $\frac{1}{18}$ of 26 = 2.

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- 130. The symbols 1/2, 1/3, 3/6, etc., are called Fractions, and represent one or more of the equal parts of the whole or unit.
- 131. The lower number is called the **Denominator**, because it points out or shows the number of equal parts into which the unit is divided, or, in other words, it shows the size of the parts.
- 132. The upper number is called the Numerator, for it tells the number of parts taken.
 - Thus $\frac{0}{1T}$ is a Fraction, and represents nine of the equal parts of the unit. It is the Denominator, and shows the size of the parts to be elevenths. 9 is the Numerator, for it tells that the number of parts taken is nine.

EXERCISE 32.

These questions should be solved mentally.

- **1.** Read the following fractions, naming the denomina tor and numerator to each: $\frac{2}{3}$, $\frac{1}{7}$, $\frac{1}{5}$, $\frac{5}{71}$, $\frac{7}{75}$, $\frac{6}{5}$, $\frac{1}{15}$, $\frac{5}{71}$, $\frac{7}{75}$, $\frac{6}{5}$, $\frac{1}{15}$, $\frac{5}{71}$, $\frac{7}{75}$, $\frac{6}{71}$, $\frac{1}{75}$, $\frac{1}{75}$.
- 2. Write the following fractions in figures : Five-ninths. Five-elevenths. Three-sevenths. Nine-fourteenths. Two-fifths. Eleven-t welfths. Four-sevenths. Eight-fifteenths. Five-sixths. Seven-twentieths. Three-eighths. Eight-thirteenths. Four-ninths. Four-twentieths. Seven-ninths. Eleven-nineteenths. Seven-tenths. Sixteen-twenty-thirds. Five-sevenths. Three-fourteenths. Eight-nir.ths. Four-fortieths. Nine-tenths. One-seventieth. One-twelfth. Seventy-ninetieths.
- 3. When anything is divided into seven equal parts, what is one part called? Three parts? Five parts?

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4. What is one of the eleven equal parts of anything called? Seven of the twelve equal parts? Nine of the ten equal parts? Fourteen of the fifteen equal parts? Eighteen of the twenty equal parts?

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- 5. What is meant by one-ninth of a quantity of apples? Seven-elevenths of a heap of oats? Ten-twelfths of a distance? Four-twentieths of the value of a vessel? Five-sevenths of a man's property?
- 6. How many sixths in the whole of an estate? Tenths in one-half of an apple? Quarters in one-half of a yard? Sixths in one-third of a pound? Eighths in one-quarter? Sixteenths in one-eighth?
- 7. What is $\frac{1}{4}$ of 8? $\frac{1}{3}$ of 12? $\frac{1}{6}$ of 25? $\frac{1}{7}$ of 63? $\frac{1}{6}$ of 18? $\frac{1}{11}$ of 55? $\frac{1}{12}$ of 48? $\frac{1}{10}$ of 120? $\frac{3}{5}$ of 24? $\frac{3}{7}$ of 45? $\frac{1}{17}$ of 88? $\frac{3}{7}$ of 21? $\frac{1}{15}$ of 39? $\frac{3}{5}$ of 27 pounds? $\frac{3}{5}$ of 48 ounces? $\frac{5}{5}$ of 1 ounce, or 20 pennyweights? $\frac{5}{5}$ of 42 inches? $\frac{5}{11}$ of 77 acres? $\frac{19}{11}$ of 66 yards? $\frac{5}{7}$ of \$84?
- 8. How much of anything will be left if $\frac{1}{7}$ be taken away? If $\frac{1}{10}$ be taken away? If $\frac{3}{71}$ be taken away? If $\frac{3}{10}$ be taken away? If $\frac{3}{10}$ of it be lost? If $\frac{4}{10}$ of it be given away? If $\frac{9}{10}$ of it be sold? If $\frac{10}{17}$ of it be lost?
- 9. How much of anything must be taken from it to leave $\frac{6}{6}$ of it? $\frac{7}{10}$ of it? $\frac{7}{12}$ of it? $\frac{9}{75}$ of it? $\frac{4}{7}$ of it? $\frac{13}{17}$ of it? $\frac{4}{15}$ of it? $\frac{11}{12}$ of it?
- 10. What part of my farm may I sell to have $\frac{4}{5}$ of it left? $\frac{3}{7}$ of it? $\frac{5}{11}$ of it? $\frac{12}{19}$ of it? $\frac{5}{11}$ of it? $\frac{5}{12}$ of it? $\frac{3}{16}$ of it? $\frac{1}{8}$ of it?
- 11. A farm contains 260 acres: how many acres in $\frac{4}{5}$ of it? in $\frac{3}{10}$ of it? in $\frac{3}{13}$ of it? $\frac{1}{10}$ of it?
- 12. If a of a vessel be worth \$60, what will the worth?
- 13. If $\frac{1}{6}$ of my property be 100 acres, find the number of acres in $\frac{1}{6}$ of it.
- 14. If $\frac{2}{3}$ of a number be 16, what will $\frac{1}{3}$ of it be?
- 15. If $\frac{a}{1}$ of a bushel of oats be worth 72 cents, what would $\frac{1}{4}$ be worth? What would a bushel be worth? What would $\frac{1}{13}$ of a bushel be worth? $\frac{a}{12}$ of a bushel? $\frac{7}{13}$ of a bushel?
- 16. How old is a boy $\frac{3}{7}$ of whose age is just 6 years?
- 17. If $\frac{1}{2}$ of a pound of tea be worth 72 cents, find the price of a pound.

- 18. What is coffee worth a pound when 40 cents pays for ³/₃ of a pound ?
- 19. I bought a keg of nails : having but \$8 I could only pay for \$ of it. What must I yet pay ?

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133. We have seen that $\frac{1}{2}, \frac{4}{2}, \frac{3}{2}, \frac{4}{3}, \frac{6}{3}, \frac{6}{12}$ of the unit, in Art. 127, was the same in each case, namely, 6 of the 12 equal parts or inches. This shows that a fraction may be expressed in many different forms, and still be the same in value. In other words, if we decrease the size of the parts we must take more of them, and if we increase the size of the parts we must take fewer of them. Again, if we increase the number of parts taken we must decrease their size, and if we decrease the number of parts taken we must increase their size.

The Numerator and Denominator are called the Terms of a Fraction.

Since $\frac{1}{2} = \frac{2}{4}$, $\frac{4}{3} = \frac{6}{12}$, etc., we deduce the following important Principle:

134. If the iwo terms of any fraction be multiplied by the same number, the value of the fraction is not changed.

 $Ex. -\frac{3}{5} = \frac{1}{2}\frac{5}{5}; \frac{2}{3} = \frac{1}{2}\frac{6}{3}.$

Again, since $\frac{6}{12} = \frac{2}{3}$, $\frac{4}{3} = \frac{1}{2}$, etc., we deduce the following important Principle:

135. If the two terms of any fraction be divided by the same number, the value of the fraction is not changed.

 $Ex. -\frac{10}{22} = \frac{5}{11}; \frac{12}{16} = \frac{3}{4}.$

Ex. 1.—Express \ddagger as a fraction, having 15 for its denominator, or change \ddagger to fifteenths.

To obtain 15 from 5, we must multiply 5 by 3, and since both terms of a fraction must be multiplied by the same number to have no effect on its value, we must multiply the numerator 4 by 3. This gives us the fraction $\frac{12}{12}$.

Thus $\frac{1}{2} = \frac{1}{14}$.

FRACTIONS,

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nd since d by the we must us the Ex. 2.—Change $\{\frac{1}{6}$ to eighths, that is, express $\{\frac{1}{6}$ as a fraction having its denominator 8.

To obtain 8 from 16 we divide 16 by 2, hence we must also divide 10 by 2, to give a new numerator.

Ans. A.

- 136. When the fraction $\frac{10}{16}$ is changed to $\frac{4}{5}$, the fraction $\frac{10}{16}$ is said to be brought to its lowest terms.
 - Instead of speaking of $\frac{1}{16}$ of a pound of sugar, we would express the same amount of sugar more easily by saying $\frac{5}{8}$ of a pound.

All fractions should be expressed in their lowest terms.

- 137. A fraction is in its lowest terms when its numerator and denominator cannot both be divided exactly by any number greater than 1.
 - Reduce $\frac{1}{2}$ to its lowest terms. By dividing both terms by 2 we obtain $\frac{4}{3}$; again divide both terms of $\frac{4}{3}$ by 2 we have $\frac{2}{3}$, which we see is the required fraction.

In other words, r_3 of anything is the same as $\frac{2}{3}$ of it.

Instead of having two operations, we might have divided both terms of $\frac{\theta}{12}$ by 4. and thus find the lowest terms at once.

This number 4 we know is the G.C.D. of 8 and 12.

138. Hence to reduce a fraction to its lowest terms we have the following

RULE.

Divide both numerator and aenominator of the fraction by their Greatest Common Divisor.

EXERCISE, 33.

- (a) I. Change ^A/₄ to a fraction having its denominator 8;
 12, 20; 40; 32; 60.
 - 2. Express $\frac{a}{6}$ of a yard as twelfths; as sixteenths; as thirtieths.

3. How many twentieths of a dollar must I exchange for a half? for a quarter? for four-fifths? for seventenths?

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5. 6.

7. 8.

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- 4. Change
 - ? to thirty-fifths.
 - a to fortieths.
 - a to thirty-sixths.
 - 4 to forty-fifths.

(b) Reduce the following fractions to their lowest terms:

	30,	20,	\$.	6.	39	900 ,	27	
2.	14,	18,	510.	7.	28		27.36.	
3.	25,	728,	45	8.	320	232,	102	
	84,	$\frac{33}{110}$,	65	Q.	$\frac{63}{135}$	297,		
	26,32,		1000.			96 144	119 <u>30</u> 44	
0	32'	121	1000		198,	144,	44	

- 11. What fraction with lowest terms will express the same as $\frac{8}{120}$? $\frac{42}{54}$? $\frac{60}{70}$?
- 12. Shew that the fractions $\frac{3}{60}$, $\frac{2}{5}$, and $\frac{2}{5}$ are the same in value.
- 139. Hitherto we have spoken of such parts of the unit or whole as $\frac{3}{5}$, $\frac{5}{7}$, $\frac{5}{70}$, etc., that is, a part less than a whole in each case.
 - We now come to notice such fractions as $\frac{e}{5}$, $\frac{10}{7}$, $\frac{21}{5}$, $\frac{12}{10}$. etc.
 - Now $\frac{5}{5}$ means five-fifths and one-fifth, that is the whole and one-fifth besides, which is written $1\frac{1}{3}$ and read one and one-fifth. So $\frac{10}{7}$ means seven-sevenths and three-sevenths, or $1\frac{3}{7}$. $\frac{3}{8}^{1} = 16$ eighths and 5 eighths = $2\frac{5}{8}$.
- 140. Such fractions as $\frac{3}{6}$, $\frac{5}{6}$, $\frac{6}{11}$, etc., in which the numerator is less than the denominator, are called **Proper Fractions**.
- 141. Such fractions as $\frac{5}{6}$, $\frac{10}{29}$, $\frac{2}{3}$, etc., in which the numerator is equal to orgreater than the denominator are called Improper Fractions.
- 142. The expressions $2\frac{5}{6}$, $6\frac{1}{4}$, $8\frac{3}{5}$, etc., are called Mixed Fractions, being made up of a whole number and a fraction.

st I exchange s? for seven-

owest terms:

 $\begin{array}{c} 1 \\ 0, & \frac{27}{307} \\ 0, & \frac{27}{30} \\ 0, & \frac{27}{30} \\ \frac{5}{2}, & \frac{102}{144} \\ \frac{7}{7}, & \frac{91}{119} \\ \frac{89}{4}, & \frac{89}{44} \end{array}$

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 $\frac{1}{7}, \frac{1}{7}, \frac{2}{8}, \frac{12}{10}$

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FRACTIONS.

143. We see by Art. 139 that every improper fraction may be brought to a mixed fraction by means of the following

RULE.

Divide the numerator of the improper fraction by the denominator, and the quotient will be the whole number.

Place the remainder, if any, over the denominator, to form the other part of the mixed fraction.

Ex.—Reduce $\frac{23}{6}$ to a mixed fraction.

Dividing 23 by 6 we obtain 3 for the quotient and 5 for the remainder. Hence $3\frac{5}{6}$ will be the required mixed fraction.

In the mixed fraction 3^a/₄ the 3 is the same as 18 sixths, which with the other 5 sixths make 23 sixths, ¹⁰/₄.

144. Hence, to reduce a mixed fraction to an improper fraction we have the following

RULE.

Multiply the whole number by the denominator, to the product add the numerator, and under the sum write the denominator.

Ex.—Reduce $7\frac{3}{5}$ to an improper fraction.

Multiplying 7 by 5, we have 35; adding 3 to this product gives 38; therefore the required fraction is §.

EXERCISE 34.

(a) Express the following improper fractions as mixed fractions, or whole numbers :

1. 149. 2. 213. 3. 244. 5. 244. 5. 244. 5. 244. 7. 8. 258. 7. 8. 259. 7. 8. 259. 7. 8. 259. 10. 577.	$12. \begin{array}{c} 0.5\\ -5\\ 13. \begin{array}{c} 9.3\\ 7\\ -7\\ -7\\ -7\\ -7\\ -7\\ -7\\ -7\\ -7\\ -7\\$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
2. $\frac{2}{3}$. 3. $\frac{2}{4}$. 5. $\frac{19}{5}$. 6. $\frac{3}{4}$. 7. $\frac{3}{5}$. 8. $\frac{39}{5}$. 9. $\frac{45}{5}$. 10. $\frac{57}{7}$.	14. $\frac{10^2}{5}$.	25. 49.	36. 30.
4. 51.	$15. \frac{1-2}{3}$.	26. ⁷³ .	$37 \cdot \frac{32}{8}$.
5. 5.	10. $\frac{14}{6}$.	$27. \frac{8}{12}$	38. 115.
0. 4.	17. 4.	$28. \frac{108}{67}.$	$39. \frac{129}{9}.$
7. 6.	$10. \frac{17}{3}$	29. ⁶⁴ / ₉ .	40. $1\frac{4}{8}$
0. 8.	$19. \frac{1}{4}.$	$30. \frac{59}{8}$.	4^{I} $\frac{200}{12}$.
9. 7 .	21, 35	31. 5.	42. 15.
11. $\frac{7}{10}$.	22. $\frac{41}{10}$	32. 20.	43. 63.
10.	44. 10.	53. 5.	44. 478.

and the brothing has.	
(b) Change the following mixed fractions to improper fractions:	145. If
I. $6\frac{2}{3}$.12. $9\frac{5}{6}$.23. $7\frac{5}{6}$.34. $16\frac{3}{8}$.2. $9\frac{1}{4}$.13. $10\frac{3}{4}$.24. $9\frac{5}{8}$.35. $17\frac{5}{12}$.3. $6\frac{1}{4}$.14. $8\frac{5}{7}$.25. $10\frac{3}{6}$.36. $57\frac{1}{12}$.4. $10\frac{5}{8}$.15. $7\frac{5}{8}$.26. $12\frac{9}{7}$.37. $81\frac{5}{6}$.5. $9\frac{1}{2}$.16. $5\frac{1}{17}$.27. $14\frac{3}{4}$.38. $124\frac{1}{2}$.6. $3\frac{2}{5}$.17. $10\frac{6}{7}$.28. $16\frac{9}{8}$.39. $342\frac{9}{3}$.7. $4\frac{1}{1}$. $18.$ $12\frac{1}{8}$.29. $22\frac{6}{7}$.40. $200\frac{3}{9}$.8. $3\frac{5}{12}$.19. $11\frac{1}{9}$.30. $32\frac{3}{7}$.41. $1256\frac{2}{7}$.9. $5\frac{3}{3}$.20. $9\frac{6}{9}$.31. $45\frac{3}{3}$. $42.$ $4091\frac{7}{17}$.10. $7\frac{3}{4}$.21. $7\frac{5}{12}$.32. $23\frac{3}{4}$. $42.$ $4091\frac{7}{17}$.11. $8\frac{2}{8}$.22. $8\frac{7}{7}$. $33.$ $5\frac{7}{7}$.	W Al N
(c) I. How many whole days are there in $\frac{1}{6}$ of a day? In $\frac{4}{7}$ of a day?	Tł
2. How many whole ounces are there in $\mathfrak{S}^{\mathfrak{o}}$ of an ounce? In $\mathfrak{L}^{\mathfrak{o}}$ ounces? In $\mathfrak{L}^{\mathfrak{o}}$ of an ounce?	146. In

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- ounce? In 11 ounces? In 105 of an ounce? of an 3. Take away as many dollars as you can from $\frac{6}{2}$ of a dollar, and what will be left? From 100 of a
- 4. How many boys could receive a dollar ap ece out of $\frac{489}{12}$ of a dollar? What part of a dollar would be left?
- 5. Change 51 to fourths.
- 6. Change 15 to fifths.

dollar?

- 7. Reduce 13th to sixths.
- 8. Reduce 8 $\frac{3}{11}$ to elevenths.
- 9. Change 31 to sevenths. To fourteenths.
- 10. Change 51 to ninths. To eighteenths.
- 11. Change $6_{\frac{5}{12}}$ to twelfths. To twenty-fourths.
- 12. Change 8_{14}^3 to fourteenths. To forty-seconds.
- 13. Reduce $9\frac{5}{20}$ to twentieths. To sixtieths.
- 14. How many eighths of a pound are there in 25% pounds? In 301 pounds? In 1001 pounds?
- 15. How many more quarters of a yard are there in 85^3_4 yards than in 324 yards?

FRACTIONS

to improper

- 34. 16<u>3</u>. 35. 173. 36. 57-3-37. 815. 38. 1241. 39. 342을. 40. 2005 41. 1256².
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here in 25 rids? here in 853 145. If we take the two fractions $\frac{7}{12}$ and $\frac{5}{8}$, and wish to know the greater of the two, it might not be known from a glance at the fractions. We will therefore find a method of comparing fractions, that is, finding out the order in which they stand according to their value.

We know that $\frac{7}{12} = \frac{14}{24}$. Also, $\frac{5}{4} = \frac{15}{24}$

- Now we have the two fractions $\frac{14}{24}$ and $\frac{15}{24}$, in each of which the size of the parts of the unit is the same, that is, twenty-fourths; but in the first there are 14 and in the second 15 of these twenty-fourths taken. Hence we see at a glance that $\frac{1.5}{24}$ is greater than $\frac{1.4}{24}$ by $\frac{1}{24}$, that is, $\frac{5}{8}$ is greater than $\frac{7}{12}$ by $\frac{1}{24}$.
- Thus, a boy who received # of a lot of apples would have more than a boy who obtained $\frac{7}{12}$ of the lot.
- 146. In order to compare the two fractions, they were brought to other fractions, having the same denominator, 24. This is the method we were seeking, and applies to any number of fractions.
 - This same denominator, it will be easily noticed, is the L. C. D. of the given denominators.
- 147. We thus have the following

RULE FOR COMPARING FRACTIONS.

Find the L. C. D. of all the given denominators.

Bring each fraction to another having the L. C. D. for a new denominator.

The value of the fractions will then depend entirely on the value of the new numerators.

Mixed fractions must be first brought to improper fractions.

Ex.-Find the greatest and least of the following: 1 of a pound, 1 of a pound, 2 of a pound.

The L.C.D. of the denominators 3, 12 and 9 is 36.

 $\frac{1}{4}$ of a pound = $\frac{24}{34}$ of a pound. $\frac{1}{13}$ of a pound = $\frac{15}{36}$ of a pound.

 $\frac{1}{4}$ of a pound = $\frac{28}{24}$ of a pound.

Hence we have 24 parts, 15 parts, and 28 parts of a pound. Therefore $\frac{28}{36}$ or $\frac{7}{9}$ of a pound is the greatest, $\frac{2}{3}$ or $\frac{2}{3}$ of a pound is the next, and $\frac{1}{3}$ or $\frac{5}{12}$ of a pound is the least.

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EXERCISE 35.

(a) Arrange the following fractions in their order of value: $I. \frac{1}{2}.$ 울. 충. 2. 4. 3. 3. 4. 4. (b) 1. A. owns $\frac{1}{2}$ a ton, B. $\frac{2}{3}$ of a ton, C. $\frac{7}{4}$ of a ton, and D. § of a ton : who has the most, and who the least? 2. A. does § of a day's work, B. 8, C. 9, and D. 4. which should draw the most pay? Which the least? 3. John has \$3\$, James \$3\$, Henry \$5\$, Charles \$912: 150. T arrange their names in the order of their wealth. 4. A man rides 19 quarters of a mile, drives 311 miles, walks of a mile, and sails # of a mile : which was the longest, and which the shortest? 5. A pole is $\frac{31}{7}$ feet high, another $8\frac{5}{14}$, another $\frac{9}{7}$, and another 9%: arrange them in order of height. 6. Which is the greatest and which the least of the following amounts : \$95, \$315, \$45, \$4? Arrange them in order of value. ADDITION OF FRACTIONS. 148. We now proceed to add fractions when the fractions have denominators that are alike. In this case, since the parts of the unit or whole are the same in each fraction, the sum of the numerators will show the number of parts there are altogether. If we add \$ of a pound to \$ of a pound, or 2 and 3 of the same size parts (sevenths), we must obtain 5 of these sevenths, that is \$ of a pound.

ADDITION OF FRACTIONS.

28 parts of is the great- $\frac{15}{5}$ or $\frac{5}{12}$ of a

ler of value:

2.	23.
$\frac{1}{12}$.	$\frac{19}{20}$.
10.	18.
6.	8.

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2 and 3 of obtain 5 of 149. Hence we have the following

RULE.

Add together the several numerators, and under the sum place the given denominator.

Ex.—Add together $\frac{1}{12}$, $\frac{5}{12}$, and $\frac{7}{12}$.

The sum of the numerators is 13, so the required fraction must be $\frac{13}{12}$.

To add fractions when the fractions have denominators that are unlike.

In this case, since the size of the parts of the unit or whole is not the same in each fraction, the fractions must be brought to other fractions having the same denominator. Then we proceed as in the former case.

150. This gives the following

RULE.

Reduce all the fractions to others having the same denominator.

Add the new numerators, and under their sum place the new denominator.

Ex. 1.—Find the sum of $\frac{3}{10}$ and $\frac{3}{13}$.

$$\frac{3}{10} + \frac{5}{12} = \frac{18 + 25}{60} = \frac{43}{60}$$

Here $\frac{3}{10} = \frac{18}{60}$, $\frac{5}{12} = \frac{26}{60}$, and the sum is $\frac{43}{60}$.

If there be any mixed fractions, the whole numbers are added separately, and then the sum of the fractions is added to that sum.

 $Ex. 2. - Add \$_{5\frac{1}{10}}, \$_{7\frac{1}{8}}, \$_{10\frac{1}{4}}.$ 5 + 7 + 10 = 22. $\frac{1}{10} + \frac{1}{8} + \frac{1}{4} = \frac{4 + 5 + 10}{40} = \frac{19}{40}$ $\$_{22} + \$_{\frac{1}{40}}^{\frac{1}{2}} = \$_{22\frac{1}{40}}.$

SUBTRACTION OF FRACTIONS.

151. In subtracting one fraction from another, the same remarks apply as in the addition of fractions, except that instead of adding the numerators we subtract them.

 $Ex. \ 1. -\frac{5}{6} - \frac{4}{6} = \frac{3}{6}.$ $\frac{5}{12} - \frac{3}{10} = \frac{25 - 18}{60} = \frac{7}{60}$

Ex. 2—From $23\frac{5}{12}$ subtract $17\frac{3}{4}$.

 $\begin{array}{c} 23\frac{9}{12} \\ 17\frac{3}{2} \\ \hline 17\frac{3}{2} \\ \hline 5\frac{8}{12} \\ \hline 5\frac{8}{12} \\ \hline 17\frac{3}{2} \\ \hline 5\frac{8}{12} \\ \hline 17\frac{3}{2} \\ \hline 5\frac{1}{12}

The work might be written in the following form :

$23\frac{5}{12} = 22 + 1\frac{5}{12}$	$=22+\frac{17}{2}$
$17\frac{3}{4} = 17 + \frac{3}{4}$	$= 17 + \frac{9}{32}$
Difference	$= 5 + \frac{8}{12} = 5^{\frac{2}{5}}$

In giving a result or answer, improper fractions should (unless otherwise stated) be brought to mixed fractions, and all fractions reduced to their lowest terms.

EXERCISE 36.

These questions should be solved mentally.

- 1. Add together and find the difference between: $\frac{1}{2}$ and $\frac{1}{2}$; $\frac{3}{4}$ and $\frac{6}{4}$; $\frac{3}{7}$ and $\frac{3}{7}$; $\frac{5}{6}$ and $\frac{1}{2}$; $\frac{1}{3}$ and $\frac{1}{4}$; $\frac{8}{2}$ and $\frac{8}{3}$, $\frac{1}{3}$, $\frac{3}{6}$ and $\frac{1}{2}$; $\frac{6}{7}$ of a foot and $\frac{7}{4}$ of a foot; $\frac{3}{7}$ of a farm and $\frac{1}{4}$ of a farm; $\frac{5}{12}$ and $\frac{1}{9}$; $\frac{3}{16}$ and $\frac{1}{6}$; $\frac{1}{5}$ of a share and $\frac{1}{6}$ of a share; $\frac{7}{12}$ and $\frac{1}{8}$.
- Add together ²/₃ and ¹/₁₂; ¹/₄, ¹/₂, ³/₄; ³/₄ of a yard, ¹/₃ of a yard; ¹/₃, ¹/₁₀, ³/₂₀.
- 3. John had 5 of an apple, and gave away 1 of the apple: what had he left?

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SUBTRACTION OF FRACTIONS.

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- 4. Bought goods for a dollar, and sold them for 14 dollars: what did I gain?
- 5. A boy paid 1 of a dollar for a book, 1 a dollar for a bag, 1 of a dollar for paints: how much did he spend?
- 6. Find the difference between, and also the sum of $\frac{4}{5}$ and $\frac{2}{5}$; $\frac{1}{6}$ and $\frac{3}{5}$; $\frac{3}{7}$ and $\frac{3}{5}$; $\frac{3}{7}$ and $\frac{2}{3}$; $\frac{3}{4}$ and $\frac{2}{5}$; $\frac{3}{4}$ and $\frac{4}{5}$; $\frac{3}{7}$ and $1\frac{2}{7}$; $2\frac{1}{5}$ inches and $1\frac{1}{3}$ inches; $5\frac{1}{3}$ and $3\frac{3}{5}$; $7\frac{1}{10}$ and $3\frac{3}{5}$; $5\frac{1}{2}$ yards and $2\frac{3}{7}$ yards; $6\frac{1}{4}$ ounces and $4\frac{3}{7}$ ounces; $17\frac{1}{6}$ cents and $12\frac{7}{6}$ cents; 20 $\frac{1}{71}$ oranges and $15\frac{10}{17}$ oranges; $7\frac{3}{10}$ dollars and $5\frac{3}{7}$
- 7. What must I add to $\$1\frac{3}{4}$ to make $\$3\frac{1}{4}$?
- 8. What must I take from $7\frac{1}{2}$ to make $3\frac{3}{2}$?
- 9. From what must $3\frac{1}{2}$ be taken to leave $2\frac{1}{2}$?
- 10. What would be left if $3\frac{5}{8}$ yards were taken from $6\frac{1}{4}$ yards?
- II. From what must we cut off 5³/₅ yards to leave 3²/₅ yards?
- 12. To what must 5¹/₈ cents be added to produce 10¹/₂ cents?
- 13. What part of a farm must be sold to leave $\frac{1}{10}$ of it?
- 14. What must be taken from a square rod of land (30¹/₂ yards) to leave 15¹/₂ yards?

152. The pupil will have noticed that in adding such fractions as $\frac{1}{2}$ and $\frac{1}{6}$ the result, $\frac{1}{56}$, is just the sum of the denominators placed over their product. The difference of the fractions would be the difference of their denominators placed over their product. For example $\frac{1}{11} - \frac{1}{12} = \frac{1}{152}$.

This may be stated as follows :

The sum or difference of two fractions, having 1 for a numerator, is the sum or difference of their denominators, placed over their product.

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EXERCISE, 37.

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1. $4\frac{1}{3} + 3\frac{1}{7}$. 10. $48\frac{7}{8} - 26\frac{1}{16}$. 2. $19\frac{1}{1} + 13\frac{1}{18}$. 11. $75\frac{16}{16} - 36\frac{1}{21}$. 3. $8\frac{1}{2} + 6\frac{1}{3}$. 12. $1\frac{1}{10} + 6\frac{1}{6} + 18\frac{1}{2}\frac{6}{9} + 2\frac{7}{80}$. 10. $48\frac{7}{8} - 26\frac{1}{16}$. 11. $75\frac{16}{16} - 36\frac{1}{21}$. 11. $75\frac{16}{16} - 36\frac{1}{21}$. 12. $1\frac{1}{10} + 6\frac{1}{2} + 18\frac{1}{2}\frac{6}{9} + 2\frac{7}{80}$.	
4. $25\frac{3}{8} + 14\frac{1}{2}$. 13 $46\frac{5}{8} - 15\frac{1}{6}$. 5. $20\frac{3}{8} - 16\frac{1}{2}$. 14. $13\frac{1}{7} + 99\frac{3}{8} + 512\frac{5}{16}$. 6. $18\frac{1}{4} - 12\frac{1}{7}$. 15. $3\frac{1}{7} - 1\frac{3}{6}$.	3
6. $18\frac{1}{4} - 12\frac{1}{7}$. 15. $3\frac{1}{45} - 1\frac{3}{9}$. 7. $22\frac{1}{7}\frac{1}{2} + 18\frac{1}{5}$. 16. $\frac{7}{25} - \frac{7}{35}$. 8. $21\frac{1}{2} + 15\frac{1}{7}$. 17. $4\frac{2}{7} + \frac{7}{186} + 3\frac{1}{9}$. 9. $33\frac{1}{3} + 24\frac{1}{4}$. 18. $\frac{2}{50} - \frac{5}{24}$.	31
19. A boy had 4 acres; his brother gave him # of an- other, his sister # of another, and his father # of another: how many had he then?	33
20. A merchant had a piece of calico containing $3+\frac{3}{4}$ yards, and sold off it $2+\frac{3}{6}$ yards : how much was left?	33 34
21. A man paid \$11 for a coat, \$# for a knife, \$# for a brush, and \$# for a comb : how much did they all cost?	35
22. A man bought 17 ⁶ pounds of butter, from which he sold 12 ¹ / ₂ pounds : how much remained ?	36.
23. From a cask containing 42 ¹ / ₄ gallons of molasses, a grocer drew off 17 ¹ / ₂ gallons : how many gallons remained?	37.
24. A man bought a horse for \$73 ^δ / ₀ , a carriage for \$97 ^δ / ₀ , a set of harness for \$37 ^δ / ₁₂ : what was the cost of the whole ?	38.
25. A man gave away at different times \$ ⁴ / ₇ , \$ ³ / ₂ , \$ ⁴ / ₃ , and \$ ³ / ₄ : how much did he give away in all?	39.
26. A man started on a journey of $45\frac{2}{3}$ miles, and travelled $28\frac{7}{3}$ miles : how far had he still to travel?	40. 41.
27. A merchant bought 2723 yards of muslin from one man, 1173 yards from another, and 3215 yards from a third: how many yards did he buy in all?	42.
28. James has 3 fishing lines; the first measures $12\frac{1}{2}$ feet, the second $14\frac{1}{4}$ feet, and the third $15\frac{3}{9}$ feet: how many feet in the 3 lines?	

SUBTRACTION OF FRACTIONS.

- 29. A merchant bought 3 pieces of calico, the first containing 251 yards, the second 221 yards, and the third 341 yards: how many yards are there in the 3 pieces?
- 30. If I have \$4373, and pay out \$3413, how much have I left?
- 31. A lady having \$100, paid \$8‡ for a pocket handkerchief, \$15½ for a dress hat, \$46§ for a cloak : how much had she left?
- 32. A clerk earned \$501 per month. He paid \$202 for board, \$53 for washing, and \$48 for other expenses: how much did he save per month?
- 33. What number added to 147[‡] will make 216[‡]?
- 34. What number added to $307\frac{1}{7} + 210\frac{3}{4}$ will make $700\frac{3}{6}$?
- 35. What number must be added to the difference of 1865 and 2143 to make 104213?
- 36. What fraction added to the sum of $\frac{1}{8}$, $\frac{3}{12}$, and $\frac{5}{18}$, $\frac{3}{18}$,
- 37. Bought a quantity of barrel staves for \$160³/₅, and lumber for \$1136⁴/₅: I sold the staves for \$205¹/₂, and the lumber for \$1240⁹/₁₆: what was my whole gain?
- 38. A man bought a ton of hay for \$15³/₈, a barrel of flour for \$9⁴/₁₃, and a barrel of apples for \$3⁷/₉: what change should be given to him for 3 ten-dollar bills?
- 39. What must be taken from $35\frac{1}{2}$ to leave $22\frac{2}{5}$?
- 40. From what must $24\frac{4}{7}$ be taken to leave $63\frac{22}{35}$?
- 41. Bought of Davison, Scott & Co. four cheeses weighing 46⁵/₈, 48²/₈, 49⁷/₆, and 57¹/₄ pounds respectively: what was their whole weight?
- 42. A pole has three-eighths of its length painted red, two-fifths of it white, and the rest of it blue: what part of its length is blue?

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MULTIPLICATION OF FRACTIONS.

- 153. To multiply a fraction by a whole number when the denominator does not contain the whole number exactly.
 - Multiply $\frac{3}{2}$ by 7. Here we have simply to find what 3 parts become when repeated 7 times, the parts being fifths. The result will be 21 parts or fifths, which is written $\frac{3}{2}$.

Therefore $\frac{1}{6} \times 7 = \frac{1}{6}$.

- When the denominator does contain the whole number exactly.
- Multiply $\frac{1}{10}$ by 5. Here, instead of repeating the number of parts, we will increase their size 5 times, that is, make the tenths become halves, since fivetenths make one-half, and the result will be $\frac{1}{2}$, taking the same number of parts we had before.

Therefore $\frac{3}{10} \times 5 = \frac{3}{4}$.

154. From the preceding examples we deduce the following

RULE.

To multiply a fraction by a whole number, divide the denominator by the whole number, if possible, and keep the same numerator; or multiply the numerator by the whole number, and keep the same denominator.

 $Ex. 1. - \frac{5}{13} \times 3 = \frac{5}{4}.$ $Ex. 2. - \frac{5}{5} \times 3 = \frac{5}{4}.$

155. To multiply a mixed fraction by a whole number.

What will 12 pounds of sugar cost at 11³/₈ cents a pound? Or, multiply 11³/₈ cents by 12.

The 11³/₅ cents may be broken into two parts— 11 cents and ³/₅ cents. We first multiply the ¹¹/₅ ³/₅ by 12. This gives ³/₅, which is equal to $7\frac{1}{5}$ cents. We write down the ¹/₅ and carry the 7 cents to the next order to the left as usual. 139¹/₅ Then 11×12=132; 132 added to the 7 cents makes 139 cents. The result will thus be \$1.39¹/₅.

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MULTIPLICATION OF FRACTIONS.

156. From this we have the following

RULE.

To multiply a mixed fraction by a whole number, multiply the fractional part by the multiplier, and reduce this, if possible, to a mixed fraction.

Then multiply the other part of the mixed fraction by the multiplier, and add to the product the part carried, if any.

EXERCISE 88.

These questions should be solved mentally.

- 1. Multiply $\frac{3}{12}$ of a dollar by 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12.
- 2. Multiply ⁶/₁₆ of 2 pound by 2, 6, 8, 12, 10.
- 3. If a basket holds $\frac{8}{10}$ of a bushel of apples, how much can be put into 3 baskets? 5 baskets? 7 baskets? 10 baskets?
- 4. If each man receive \$23, how much will 3 men receive? 6 men? 8 men?
- 5. At 23 cents a yard, find the cost of 3 yards; 6 yards; 4 yards.
- 6. What will $\frac{1}{8}$ of a ton of hay cost at \$24 a ton?
- 7. How many units in 6 times 1/8? In 8 times 1/8? In 11 times 4?
- 8. At 61 cents each, what will 12 pencils cost?
- 9. Find the cost of 7 dozen pens at $10\frac{1}{4}$ cents a dozen?
- 10. A man earns \$53 a week: what will he earn in a month (4 weeks)?
- 11. Find the cost of 10 citrons at $15\frac{1}{2}$ cents each.
- 12. What will 8 cords of wood cost at $5\frac{1}{16}$ a cord?
- 13. How far can I travel in 10 hours at the rate of 63 mile an hour?
- 14. A horse eats $2\frac{1}{2}$ bushels of oats in one week : how much will he eat in two months?

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DIVISION OF FRACTIONS.

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- 157. To divide a fraction by a whole number when the numerator can be exactly divided by the whole number.
 - If 4 men earn $\frac{2}{3}$ of a dollar, how much is that each? This may be written: If 4 men earn 8 parts, how much will 1 man earn? The fourth part of 8 parts, that is, 2 parts, or ninths.

Therefore $\$_{3}^{*} \div 4 = \$_{3}^{*}$.

- When the numerator does not exactly contain the whole number.
- Divide $\frac{3}{4}$ of an apple into 5 equal parts, that is, divide $\frac{3}{4}$ by 5. Here, since we cannot divide the 3 parts exactly by 5, we must decrease the size of the parts, making each part five times smaller, that is, twentieths.

Therefore $\frac{3}{4} \div 5 = \frac{3}{20}$.

158. This gives us the following

RULE.

To divide a fraction by a whole number, divide the numerator. if possible, by the whole number, keeping the same denominator; or multiply the denominator by the whole number, keeping the same numerator.

 $Ex. 1. - \frac{n}{7} \div 2 = \frac{3}{7}.$ $Ex. 2. - \frac{3}{5} \div 2 = \frac{3}{10}.$

- 159. To divide a mixed fraction by a whole number.
 - 5) $13\frac{9}{2\frac{3}{4}}$ Divide \$13\frac{9}{4} equally among 5 men. 5 is contained in 13, 2 times and 3 over. This 3 with the $\frac{3}{4}$ makes $\frac{15}{4}$, and by the preceding principle the fifth part of $\frac{15}{4}$ is $\frac{5}{4}$. Hence the result must be \$2\frac{3}{4}.

 $5) 12\frac{3}{6} E_{\pi}. 2.-Divide 12\frac{3}{6} by 5. 12÷5=2, with 2$ $remaining. <math>2\frac{3}{5}=\frac{1}{3}$. $1\frac{3}{5}\div5=\frac{1}{2}\frac{3}{5}$. There-

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160. From this we deduce the following

RULE.

To divide a mixed fraction by a whole number, divide the whole number of the mixed fraction by the divisor, if possuble, reduce the remaining part, if any, to an improper fraction, then divide as usual.

Ex.-Divide 15% by 5.

15+5=3. $\frac{3}{2}+5=\frac{3}{20}.$ Therefore $15\frac{3}{4}+5=3\frac{3}{20}.$ Ans.

EXERCISE 39.

IS These questions should be solved mentally.

- 1. Divide # of a dollar by 2, 3, 4, 5, 6, 7, 8.
- Find the third part of ¹/₁ of a pound; the fifth part; the eighth part.
- 3. What does each man get if ⁹/₁₀ of an acre of land be divided among 3 mcn? Among 4 men? Among 6 men? Among 9 men?
- 4. Four men can earn \$121 a day : what will one man earn? Three men? Six men?
- 5. At the rate of $\Im_{\overline{z}}^{\overline{z}}$ for 3 bushels, what will one bushel of oats cost? Seven bushels?
- 6. A man had 10 gallons of cream, and sold ½ of it for \$13: how much a gallon did he get? How much a quart?
- 7. I sold 3 barrels of meal for $20\frac{1}{2}$: what did I get a barrel?
- 8. A man pays \$12½ for 5 sheep: how much was it apiece? What would be the cost of 2? Of 3? Of 4?
- 9. How often is 6 contained in 1312? In 1513? In 124? In 1117?
- 10. There are $5\frac{1}{2}$ yards in a rod of fencing : how many yards in a quarter of a rod? In six rods?
- 11. I bought 5 barrels of flour for \$15³/₅, in selling I gain \$5¹/₅: what did I sell it at per barrel? If I lost \$5¹/₅, how much did I sell each barrel for?

- 12. What are apples worth each at 15³/₇ cents a dozen? At 20⁴/₁₀ cents a dozen?
- 13. A gallon contains 32 gills: how many gills are there in $\frac{7}{5}$ of a gallon? In $\frac{5}{4}$ of a gallon? In $\frac{5}{10}$ of a
- 14. A rod being 5¹/₂ yards in length, how many yards in 3 rods? In 10 rods?

161. To multiply a fraction by a fraction. Ex.—Multiply $\frac{3}{4}$ by $\frac{5}{2}$.

- $\frac{1}{7}$ of $\frac{3}{7}$, or a quarter of $\frac{3}{7}$, is $\frac{5}{25}$, and $\frac{3}{2}$ of $\frac{3}{7}$, or threequarters of $\frac{5}{7}$, will be 3 times $\frac{5}{25}$, or $\frac{1}{25}$, which equals
 - $\frac{3\times5}{4\times7}$ that is, equal to the product of the numera
 - tors placed over the product of the denominators of the given fractions.

The expression $\frac{3}{4}$ of $\frac{5}{7}$ is called a Compound Fraction.

162. A Compound Fraction may thus be called a fraction of a fraction.

163. From the above we have the following

RULE.

To multiply fractions together, or to simplify compound fractions, first reduce each mixed fraction, if any, to an improper fraction. Then multiply the numerators together for a new numerator, and the denominators together for a new denominator, always reducing the resulting fraction to its lowest terms.

Ex. 1.—Find the product of $\frac{5}{12}$ and $\frac{9}{20}$.

 $\frac{5}{12} \times \frac{9}{20} = \frac{5 \times 9}{12 \times 20} = \frac{45}{240} = \frac{3}{16}$

The product of the numerators is 45, and the product of the denominators is 240, and the fraction $\frac{4}{2}$, when reduced to its lowest terms, is $\frac{3}{16}$, which is therefore the required result. If

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product on 340, hich is 164. In the above example, instead of finding the fraction $\frac{45}{240}$ and then reducing it to its lowest terms, we may reduce the fraction $\frac{5 \times 9}{12 \times 20}$ to its lowest terms at once by dividing both terms of the fraction by the same number, thus:

5 is contained in itself once, and in 20 four times. Again 3 will divide 9 three times, and 12 four times. Now multiply as before and we obtain $\frac{1 \times 3}{4 \times 4} = \frac{3}{16}$

165. This method is always used when possible, and the operation is known by the name of **Cancelling**.

Ex. 2.—Simplify $\frac{5}{6} \oplus_{i} \frac{7}{8} \times \frac{4}{9}$ of $\frac{1}{2} \frac{9}{1} \times 2\frac{8}{6}$.

This expression may be written:

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Ex. 3.—If a pound of sugar costs $6\frac{3}{7}$ cents, what must I pay for $3\frac{3}{11}$ pounds?

If one pound cost $6\frac{3}{7}$ cents, the cost of $3\frac{9}{11}$ will be $3\frac{9}{11}$ times $6\frac{3}{7}$ cents.

$$6\frac{3}{7} \times 3\frac{a}{11} = \frac{4}{7} \times \frac{5}{11} = 20$$
 cents.

EXERCISE 40.

- 1. Find the product of $\frac{4}{5}$ and $\frac{1}{4}$.
- 2. Multiply of by 9
- 3. Multiply together 20, 5, 27
- 4. Find the value of $I_{\frac{1}{19}} \circ f_{\frac{1}{18}} \circ f_{\frac{1}{18}}$
- 5. Simplify $10\frac{1}{2} \times 2\frac{2}{3}$.
- 6. Simplify $\frac{9}{14}$ of $6\frac{1}{2}$ of $1\frac{1}{3} \times \frac{1}{10} \times \frac{7}{13}$ of $1\frac{1}{4}$.
- 7. Multiply $\frac{9}{16}$ of $2\frac{1}{2}$ of $3\frac{1}{9}$ by $6\frac{1}{2}$ of $7\frac{1}{8}$.

- 8. Simplify $_{1_{\overline{6}}}^{\prime}$ of $_{\overline{1_{5}}}^{3}$ of $_{7_{\overline{5}}}^{1} \times 3_{8}^{1}$ of $_{\overline{1_{87}}}^{20}$ of $_{\frac{3}{5}}^{3}$.
- 9. What will $3\frac{3}{5}$ pounds of rice cost at $4\frac{1}{2}$ cents a pound?
- 1). Find the value of $4\frac{4}{5}$ pounds of butter at $27\frac{1}{4}$ cents per pound.
- 11. Find the cost of 26¹/₄ ounces of candy at 5¹/₅ cents an ounce.
- What must I pay for 4¹/₂ bushels of clover seed at \$7⁶/₆ a bushel?
- How far can a man, walking 2^s/₂ miles an hour, go in 17¹/₂ hours?
- 14. What number divided by $4\frac{2}{3}$ will give $8\frac{5}{8}$ as a result
- 15. What does A. earn in 9³/₅ weeks at the rate of \$23¹/₃ per week?
- 16. What is \$ of \$171?
- 17. With a machine, a man cuts 8½ cord of maple a day: what quantity can he cut in 4½ days at the same rate?
- 18. What will 33¹/₃ pounds of tea cost at 93³/₄ cents a pound?
- 19. What will $212\frac{2}{3}$ pounds of meat cost at $7\frac{1}{2}$ cents a pound?
- 20. How many cords of wood will 45 men chop in $15\frac{1}{2}$ days, if each chop $2\frac{1}{5}$ cords a day?
- 21. Find the amount of the following account: 7¹/₂ lbs. of rice @ 5³/₃cts. a pound; 9^T/₈ quarts of beans @ 7²/₃cts. a quart; 12¹/₃ yards of ribbon @ 6^T/₅cts. a yard; 9³/₄ yards of linen @ 7³/₈cts. a yard; 12¹/₂ yards of lace @ 62¹/₂cts. a yard.
- 22. A trunk cost $\frac{1}{4}$ of $\$16\frac{3}{4}$, and a valise $\frac{3}{4}$ as much as the trunk; what did I pay for the valise?
- 23. Multiply 18 times $\frac{7}{6}$ of $5\frac{1}{4}$ by $\frac{1}{6}$ of 4 times $\frac{5}{6}$ of 3.
- 24. Find the cost of $\frac{1}{3}$ of 5 yards of lace at $\frac{3}{4}$ of $\frac{5}{18\frac{1}{2}}$ a yard.
- 25. What must be paid for $\frac{5}{6}$ of $156\frac{3}{5}$ acres of land at $\frac{4}{5}$ of $54\frac{9}{10}$ an acre?
- 26. The yacht "Oriole" can make $10\frac{4}{11}$ knots an hour : how many knots would she sail in $4\frac{1}{11}$ hours?

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DIVISION OF FRACTIONS.

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In $\frac{5}{7}$, r unit is contained five-sevenths of a time. Then one-eighth of 1 unit must be contained eight times as often, that is, $\frac{49}{7}$ times. Now, three-eighths of r unit will be contained one-third as many times as one-eighth, that is, $\frac{49}{7}$ of a time.

And $\frac{4^\circ}{2i} = \frac{5 \times 8}{7 \times 3}$

This result will be seen to be the same as that obtained by multiplying the first fraction by the latter inverted, that is, with the places of its two terms changed.

167. This gives us the following

RULE.

To divide a fraction by a fraction, reduce mixed and compound fractions, if any, to simple fractions. Then invert the divisor and multiply the numerators together for a new numerator, and the denominators together for a new denominator.

Ex. 1.—Divide $\frac{1}{2}$ of $\frac{3}{2}$ of $\frac{3}{2}$ by $\frac{1}{2}$ of $\frac{3}{2}$.

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$\frac{1}{7}$ of $\frac{3}{4} = \frac{3}{28}$	
$\frac{1}{4} \div \frac{3}{28} = \frac{1}{4} \times \frac{\frac{7}{28}}{3} = \frac{7}{3} = 2\frac{1}{8}$	

The dividend becomes $\frac{1}{2}$, the divisor $\frac{3}{28}$, which being inverted is $\frac{2}{38}$. Then $\frac{1}{4}$ multiplied by $\frac{2}{39}$ gives $\frac{7}{4}$, or $2\frac{1}{4}$, the required result.

interim x. 2.—How many pieces of cloth $\frac{1}{16}$ of a yard long can be cut from $\frac{1}{2}$ of $\frac{9}{10}$ of a yard?

There must be as many pieces of cloth as the number of times that $\frac{2}{15}$ is contained in $\frac{1}{2}$ of $\frac{2}{10}$.

$$\frac{1}{2} \text{ of } \frac{9}{10} \div \frac{2}{15} = \frac{9}{20} \times \frac{15}{2} = \frac{27}{8} = 3\frac{3}{8} \text{ pieces.}$$

EXERCISE 41.

1. Divide 3 to by 3.

2. Divide 18 by 8.

3. Divide 38 by 9.

4. Find the quotient of #2 + 13.

5. How often is $2\frac{1}{2}$ contained in $6\frac{1}{4}$?

6. How many times $2\frac{1}{3}$ is $18\frac{3}{3}$?

7. What number must be multiplied by $1\frac{1}{4}$ to give $7\frac{1}{2}$?

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8. The dividend is $12\frac{1}{4}$; quotient, $3\frac{1}{2}$; find the divisor.

9. Divide 3 of \$ of 16 by 3 of 5 of 51.

10. How many times $\frac{7}{4}$ of $\frac{3}{4}$ of $\frac{3}{7}$ is $\frac{1}{7}$ of $\frac{3}{4}$?

- 11. Find the quotient of $\frac{3}{16}$ of $3\frac{2}{3} \times 6$ divided by $1\frac{3}{7}$ of 6 times $\frac{7}{9}$.
- How many yards of silk can be bought for \$317²/₃ at \$3²/₃ a yard?
- 13. A man earns § of a dollar an hour: in how many hours will he earn \$174?
- 14. How many times $\frac{11}{23}$ of a dollar is \$175?
- 15. Divide $\frac{45}{28}$ of $\frac{21}{16}$ of $\frac{9}{12}$ of $\frac{10}{13}$ by $\frac{3}{28}$ of $\frac{30}{36}$ of $\frac{3}{4}$ of 5.
- 16. How much tea at $1\frac{2}{8}$ a pound can I buy with $57\frac{3}{4}$?
- 17. At the rate of $3\frac{3}{10}$ miles an hour, how long will I take to walk $45\frac{3}{10}$ miles?
- 18. A scarf requires \$ of a yard of silk: how many scarfs can be made from 31¼ yards of silk?

DIVISION OF FRACTIONS.

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- 19. How many bottles, each holding $1\frac{3}{8}$ pints, can be filled from a barrel of cider containing $61\frac{3}{2}$ pints, and how much will be left?
- 20. A man can run ¹/₂₀ of a mile in 5¹/₂ minutes, how far can he run per minute ?
- 21. There are $2\frac{1}{4}$ inches in a piece of cloth : how many pieces would be the same length as $123\frac{3}{4}$ inches?
- 22. If I pay \$11/1 per pound for tea, how much tea can I buy for \$9? For \$24? For \$64?
- 23. If a man spend $\$_{4\frac{3}{6}}$ a month on tobacco, in what time will he waste one week's wages, $\$_{27\frac{1}{6}}$?
- 24. How long will ¹³/₁₃ of a cord of wood last a family using ³/₂₆ of ¹/₂ a cord a day?
- 25. How long will a boy take to save \$700, if he carns \$7¹/₂ and spends \$5³/₄ of it every week?
- 26. The "Chicora" steamed 156 miles in 105 hours: what is her speed per minute (60 minutes to the hour)?
- 168. Fractions are often written in this form

$$\frac{5\frac{1}{4}}{2\frac{5}{8}}; \ \frac{5}{6\frac{1}{4}}; \ \frac{1}{3} \ of \ \frac{3}{4}; \ \frac{3}{8} \ of \ 9; \ \frac{3}{1\frac{1}{2}} \times \frac{9}{10} \ of \ \frac{3}{4}.$$

These fractions are called Complex Fractions.

- 169. A Complex Fraction is therefore a fraction which has a fraction in either its numerator or denominator, or in both.
- 170. Since we have seen that a fraction means the division of the numerator by the denominator, it follows that the above fractions can be simplified by ordinary division of fractions.

Thus:

$$Ex. 1. - \frac{5\frac{1}{4}}{2\frac{3}{8}} = \frac{21}{4} \cdot \frac{21}{8} = \frac{21}{4} \times \frac{8}{21} = 2.$$

$$Ex. 2. - \text{Simplify } \frac{\frac{3}{5} \times \frac{19}{5}}{4\frac{1}{3} \text{ of } \frac{3}{5}}.$$

$$\frac{\frac{8}{5} \times \frac{19}{5}}{4\frac{1}{5} \text{ of } \frac{3}{5}} = \frac{\frac{1}{3}}{\frac{3}{57}} = \frac{1}{3} + \frac{26}{27} = \frac{1}{3} \times \frac{\frac{27}{7}}{26} = \frac{9}{26}.$$

Ex. 3.—Simplify $(8\frac{1}{4} + 3\frac{1}{2}) \div 7\frac{3}{5}$.

Since the expression $8\frac{1}{4} + 3\frac{1}{2}$ is enclosed in the Bracket (), it must be simplified first, and the result divided by $7\frac{3}{5}$. If the bracket were omitted, we should first divide $3\frac{1}{2}$ by $7\frac{3}{5}$, and then add the quotient to $8\frac{1}{4}$, which would give a result quite different from the one required.

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 $\begin{aligned} & 8\frac{1}{4} + 3\frac{1}{2} = 11\frac{3}{4} = \frac{47}{7} \\ & 4\frac{7}{7} + 7\frac{3}{6} = \frac{47}{7} \\ & Ex. 4. - \text{Simplify } 2\frac{1}{6} + 5\frac{1}{4} \times \frac{6}{21} - 6\frac{2}{5} \text{ of } \frac{1}{2} + \frac{3}{11} + \frac{6}{44} \\ & 5\frac{1}{2} \times \frac{6}{31} = \frac{21}{2} \times \frac{6}{51} = 2 \end{aligned}$

 $6^{\frac{3}{2}} \text{ of } \frac{1}{2} = \frac{3}{5} \times \frac{1}{2} = \frac{1}{5} \\ \frac{3}{11} \div \frac{5}{44} = \frac{3}{11} \times \frac{4}{5} = \frac{1}{5}$

- $2\frac{1}{5} + 2 \frac{16}{5} + \frac{12}{5} = 4\frac{1}{5} 3\frac{1}{5} + 2\frac{3}{5} = 1 + 2\frac{3}{5} = 3\frac{3}{5}$
- The pupil will carefully notice that unless a bracket interferes, the operations shown by the signs \times , of, and \div , are carried out before any of the others.
- Thus: In Ex. 4, instead of adding $2\frac{1}{6}$ and $5\frac{1}{4}$, we multiply $5\frac{1}{4}$ by $\frac{8}{21}$, and instead of adding $\frac{1}{4}$ to $\frac{5}{11}$, we simplify $6\frac{2}{6}$ of $\frac{1}{4}$, and $\frac{5}{11} \div \frac{5}{44}$.

A bracket should always be used in any case of doubt.

171. A Bar or Vinculum has the same effect as a bracket.

The expression $\frac{3}{4} - \frac{5}{7}$ of $\frac{3}{4}\frac{5}{6}$ has the same meaning as $(\frac{3}{4} - \frac{5}{7})$ of $\frac{3}{6}\frac{5}{6}$. The value of the expression as it now stands is $\frac{1}{46}$. If the vinculum or bracket had not been given, the result would be $\frac{67}{166}$, as the pupil may find.

EXERCISE 42.

Simplify the following expressions :

 I. $\frac{3}{I_{\frac{1}{3}}}$ 4. $\frac{I}{I_{\frac{1}{3}} \times I_{\frac{1}{2}}}$ 7. $\frac{3I}{9J_{\frac{1}{3}}}$

 2. $\frac{5}{I_{\frac{3}{4}}}$ 5. $\frac{7}{I_{\frac{3}{3}}}$ 8. $\frac{3\frac{1}{2} \div 2\frac{1}{4}}{6 \div 4\frac{1}{2}}$

 3. $\frac{6}{I_{\frac{3}{4}}}$ 6. $\frac{I}{I_{\frac{4}{3}}$ of $I_{\frac{1}{2}}$ 9. $\frac{7}{6}$ of $60\frac{n}{10} \times \frac{n}{83}$

DIVISION OF FRACTIONS.

Simplify the following expressions :

$10, \ \frac{\frac{1}{8} \text{ of } \frac{5}{3} \text{ of } \frac{9}{11}}{5 \times \frac{3}{8} \text{ of } \frac{5}{7}}.$	18. $(3 \div \frac{3}{4}) - 2\frac{1}{2}$.
$5 \times \frac{3}{8}$ of $\frac{5}{7}$	19. ³ / ₈ of ¹ / ₇ of 3 ⁸ / ₈
11. $\frac{8\frac{1}{4} \times \frac{1}{3} \text{ of } 7}{2}$	47+8
$\frac{3}{4} \text{ of } \frac{3}{5} \text{ of } 5$	20. $(1^{j} - \frac{3}{5} - 2\frac{1}{7} \times 5) \times 3\frac{1}{7}$.
12. $26 \times \frac{5}{7} + 2\frac{1}{2}$.	21. $(\overline{1\frac{3}{4}+\frac{2}{4}}) \div (3\frac{1}{7}-1\frac{3}{14}) \times 2.$
13. $(4\frac{3}{7}-2\frac{1}{7})\times 3\frac{9}{7}$.	$22 \cdot \left(\frac{\frac{1}{2} - \frac{1}{3}}{\frac{1}{2} + \frac{1}{3}} + \frac{\frac{1}{3} - \frac{1}{4}}{\frac{1}{3} + \frac{1}{4}}\right) - \left(\frac{\frac{1}{4} - \frac{1}{6}}{\frac{1}{4} + \frac{1}{6}} - \frac{\frac{1}{6} - \frac{1}{6}}{\frac{1}{6} + \frac{1}{6}}\right).$
14. $2+6\frac{3}{7}\div\frac{5}{9}$.	
15. $3\frac{1}{4} + (4\frac{3}{4} \div \frac{2}{3}).$	23. $\frac{\frac{3}{6} \text{ of } \frac{2}{9} - \frac{4}{7} \text{ of } \frac{1}{8}}{\frac{1}{7} \text{ of } \frac{1}{1} + \frac{3}{7} \frac{1}{7} \frac$
16. $4\frac{3}{4} \div (3\frac{1}{7} + \frac{2}{3}).$	$ \begin{array}{c} \frac{4}{15} \text{ of } \frac{1}{28} + \frac{3}{10} \text{ of } \frac{7}{9} \\ \frac{3^{\frac{5}{4}} \times 3^{\frac{1}{3}}}{3} \cdot \frac{6^{\frac{3}{3}} \times 8^{\frac{5}{9}}}{9} \\ \end{array} \right) \left(\begin{array}{c} 14^{\frac{2}{5}} \cdot \cdot \cdot \cdot \cdot \cdot \cdot \\ 14^{\frac{2}{5}} \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \\ 14^{\frac{2}{5}} \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \\ 14^{\frac{2}{5}} \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \\ 14^{\frac{2}{5}} \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \\ 14^{\frac{2}{5}} \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot $
17. $(14-8) \div \frac{3}{4}$.	$24 \cdot \left(\frac{3\frac{3}{4} \times 3\frac{1}{3}}{2\frac{1}{2} + \frac{5}{16}} \div \frac{6\frac{2}{3} \times 8\frac{8}{9}}{8\frac{8}{9} - 6\frac{2}{3}}\right) + \left(\frac{14\frac{2}{5}}{6\frac{9}{7}} \times \frac{5\frac{5}{9}}{7\frac{7}{11}}\right)$
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 $\frac{5}{10} \times \frac{8}{83}$

GENERAL EXAMPLES ON FRACTIONS.

Ex. 1.—What part of 7 times 4 is one-ninth of 72? $7 \times 4 = 28$; $\frac{1}{9}$ of 72 = 8.

Now, what part of 28 is 8? Since I is $\frac{1}{28}$ of 28, 8 must be $\frac{8}{28}$ of it, that is $\frac{2}{7}$.

This question can be written in many ways. Instead of saying, "What part of 28 is 8?" we may say, "8 is what fraction of 28?" or "Express 8 as a part of 28," or, "What fraction is 8 of 28?"

Now the answer to each question is $\frac{\alpha}{48}$. We thus see that we always place in the numerator the quantity which is to be the part or fraction of the other.

Ex. 2. $-4\frac{3}{5}$ is what part of $18\frac{2}{5}$?

Here we write $4\frac{3}{5}$ in the numerator and $18\frac{3}{5}$ in the denominator, and reduce the fraction thus formed to its lowest terms.

$$\frac{4\frac{3}{5}}{18\frac{2}{5}} = \frac{23}{5} \div \frac{92}{5} = \frac{\cancel{1}{23}}{\cancel{1}{3}} \times \frac{\cancel{1}{3}}{\cancel{1}{3}} = \frac{\cancel{1}{4}}{\cancel{1}{3}}$$

ARITHMETIC FOR BEGINNERS.	
The pupil should always prove that the result is correct. Thus:	
Show that $\frac{1}{4}$ of $18\frac{2}{6}$ is $4\frac{3}{6}$.	
$\frac{1}{4}$ of $18\frac{2}{6} = \frac{1}{4}$ of $\frac{23}{5} = \frac{23}{5} = 4\frac{3}{5}$	1.
$\begin{array}{c} A & 5 & 5 \\ Hence the answer \frac{1}{4} is correct. \end{array}$	14
<i>Ex.</i> 3.— $\frac{4}{5}$ of 60 is $\frac{3}{5}$ of what?	15
Since $\frac{1}{3}$ of $60 = 48$, the question now stands: "48 is $\frac{3}{8}$ of what?"	16
If 48 is $\frac{4}{8}$, then $\frac{1}{3}$ of 48, that is 16, must be $\frac{1}{4}$, and $\frac{4}{8}$, or the required number, must be $16 \times 8 = 128$.	17. 18.
PROOF: $\frac{3}{8}$ of $128 = 48$	19.
Ex. 4.— $\frac{3}{3}$ of 27 is $\frac{5}{7}$ of how many times 3? Since $\frac{3}{5}$ of 27 = 18, the question then stands: "18 is $\frac{5}{7}$ of what?"	20.
This we know by Ex. 3 to be 21.	21.
Now we must find how many times 3 this 21 is. We know it is 7 times, which is the required result	22,
$PROOF: 7 \times 3 = 21.$	
\$ of 21 = 18.	
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EXERCISE 48.

1. What must be divided by $11\frac{1}{20}$ to produce $7\frac{4}{5}$? 2. To what must $\frac{8}{4\frac{1}{4}} + \frac{4\frac{1}{2}}{4}$ be added to give $\frac{3\frac{5}{7}}{4\frac{5}{1}} + \frac{6}{4}$? 3. What part of \$5% is \$11? 4. What part of a day (24 hours) is 51 hours? 5. 84 minutes is what fraction of an hour (60 minutes)? 6. What part of $\frac{1}{2}$ of a peck is $\frac{1}{2}$ a peck? 7. What part of \$11 is \$ of \$16? 8. \$ of a peck is \$ of what? 9. 1 of 132 pounds is 2 of what? 10. 12 is \$ of \$ of what ?

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the result is

- ls: "48 is }
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- 21 is. We i result.

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- ? minutes)?

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GENERAL EXAMPLES ON FRACTIONS.

- 11. If \$120 was # of what I paid for a horse, what was the price paid?
- 12. What is the cost of $2\frac{2}{11}$ loads at \$220 for 16 loads?
- 13. $\frac{1}{10}$ of 39 ounces is $\frac{9}{10}$ of the weight of a parcel : find its weight?
- 14. $\frac{3}{17}$ of $\frac{3}{5}$ of $\frac{5}{47}$ is $\frac{5}{7}$ of $\frac{3}{13}$ of a man's rent: find the
- 15. A. had \$260, and spent $\frac{7}{13}$ of it, which was just I of what B. earned : how much did B. earn?
- 16. Of how many times 9 is $\frac{3}{4}$ of 20 the five-ninths?
- 17. What number is $\frac{3}{6}$ of $4\frac{4}{5}$ times $\frac{3}{4}$ of 12?
- 18. What part of 42 is 3 times \$ of 30?
- 19. I paid \$50 for a waggon, and \$ of the cost of it was just 3 of 3 times the cost of the harness: what was the harness worth ?
- 20. If \$200 is 4 dollars more than 3 of 4 times my money,
- 21. Of how many times \$ of \$10 is \$ of \$25 the three-
- 22. If \$ of 18 years is just \$ of 4 times \$ of a boy's age, what is his age?

Ex. 5.—A man owned $\frac{5}{12}$ of a vessel, and sold $\frac{1}{15}$ of his share: what part had he left?

If he sold $\frac{1}{13}$ of his share, he must have $\frac{12}{13}$ of his share

$$\frac{12}{13}$$
 of $\frac{5}{12} = \frac{5}{13}$

The pupil will likely proceed to find what part he sold, that is, $\frac{1}{13}$ of $\frac{1}{13}$, and then subtract the result from $\frac{\delta}{13}$, which, although correct, causes a waste of time, for we want to know, not the part sold, but the part left.

Ex. 6.—After giving $\frac{2}{7}$ of his estate to a college, a gentleman had \$55000 left : what had he at first ?

If he gave away $\frac{2}{7}$ of the estate he must have $\frac{2}{7}$ of it left; and since $\frac{1}{2} =$ \$55000, then $\frac{1}{2} =$ \$11000, hence the whole or $\frac{7}{7} =$ \$77000.

23. A man gave away $\frac{2}{5}$ of $\frac{2}{5}$ of $\frac{4}{15}$ of his money: what part had he left?	29
24. I owned § of 76 of 50 of a business, and sold f of my share: what part of the business do I now own?	30
25. A mine is worth \$2200; a man owns for of # of it, and lost for of his share: what part of the mine has he left, and what is he now worth ?	31.
26. A man owns \$ of \$ of \$ of \$ of an investment; on selling \$ of his share he finds himself worth \$100 less than before: what is the value of the whole investment?	32. 33.
27. B. owned $(\frac{1}{14} - \frac{5}{2})$ of an estate, and sold $\frac{1}{3}$ of the estate: what part of the estate, and what part of his former share does he now own?	34.
28. A man sold $\frac{1}{2}$ his load to the first one he met, $\frac{1}{3}$ of the remainder to the next one, $\frac{1}{4}$ of the remainder to the next one, and so on: what part of the load had he left after 10 bargains?	35. 36.
Ex. 7.—A field could be ploughed by A. in 4 days, and by B. in 5 days: in what time could both together do the work?	37.
A. does the whole work in 4 days, therefore he does $\frac{1}{4}$ of the work in 1 day; also B. does $\frac{1}{2}$ of the work in 1 day. Both working together would thus do $\frac{1}{4} + \frac{1}{6}$ = $\frac{9}{20}$ of the work in 1 day.	38. 4 t 39. A
A. and B. do $\frac{9}{20}$ in 1 day. " " $\frac{1}{20}$ in $\frac{1}{9}$ day. " " $\frac{9}{20}$ or the whole work in $\frac{9}{20} = 2\frac{9}{9}$ days.	t t 40. A
Ex. 8.—Two pipes running together can fill a tank in 20 minutes: one of them could alone fill it in 35 minutes: how long would the other take to fill it?	tl 41. A an w
Both pipes fill $\frac{1}{30}$ of the tank in 1 minute. One pipe fills $\frac{1}{30}$ """""""" The other must fill $\frac{1}{20} - \frac{1}{35} = \frac{3}{140}$ in 1 minute. It fills $\frac{3}{140}$ of the tank in 1 minute. " $\frac{1}{140}$ """ $\frac{1}{3}$ minute.	42. A ac or
" $\frac{140}{140}$ " " $\frac{1}{3}^{\circ} = 46^{\circ}_{3}$ minutes.	:

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GENERAL EXAMPLES IN FRACTIONS.

- 29. A. can do his work in 5¹/₄ hours: how much can he do in an hour?
- 30. A. and B. can together do a of a job in 6 days: how much can they do in a day?
- 31. A. can do the work in 8 days, B. in 3 days, and C. in 9 days: how long would the three together take?
- 32. A man can do to if a journey in 1 day: how long will he take to finish it?
- 33. A pipe can fill ⁴/₁₇ of a vat in 3 hours: how long will it take to fill the whole?
- 34. A., B. and C. dig a ditch in 5 days; B. and C. can do it in 8 days: how long would A. take to do it?
- 35. A. can do a work in ¹/₃ of a day, B. in ¹/₃ of a day, and C. in I day: how long will the three men take?
- 36. A. mows 2 acres in 3 days, B. 5 acres in 6 days: in what time can they together mow 9 acres?
- 37. A., B. and C. can do a piece of work in a week; A. and B. do § of it, B. and C. do § of it; how much of it can B. do?
- 38. Three taps can fill a tank in 30 minutes, 40 minutes, and 60 minutes respectively: how long will they take, all being opened at the same time?
- 39. A pipe can fill a vat with water in 11 minutes; another can empty it in 20 minutes: in what time will the vat be filled if both are opened at the same time?
- 40. A man paid 1 of his debts, then 1 of the remainder : there was then due \$850: what did he owe at first?
- 41. A telegraph pole is § of its length in air, 1 in water, and the remainder, which is 8 feet, in the ground : what is the length of the pole?
- 42. A boy in flying his kite lost ³/₅ of the string, then added 65 feet, and found that it was just ³/₅ of the original length : what was the length at first?

CHAPTER IV.

CANADIAN MONEY.

- 172. The Government of every country makes or coins money, which is used by its people in buying and selling.
- 173. The Canadian Government coins and issues the following pieces of money: The one cent piece, made of copper; the five cent piece, ten cent piece, twenty-five cent piece, and the fifty cent piece, all of which are silver coins.

174.	The five cent piece	=	5 cents.
	The ten cent piece	-	10 cents.
	The twenty-five cent piece		25 cents.
	The fifty cent piece	=	50 cents.

- 175. The Dollar, which is equal to 100 cents, is paper money, issued either by the Government or by the Banks of the country, and may be changed into coin at any time by presenting it at the Banks.
 - There are also Two-Dollar Bills, Four-Dollar Bills, Five-Dollar Bills, Ten-Dollar Bills, Twenty-Dollar Bills, Fifty-Dollar Bills, One Hundred-Dollar Bills. as the Banks or the Government may be pleased to issue.
- 176. As stated before, the Dollar is represented by the character \$. Thus, \$45 is read: Forty-five dollars.
 - The cents are often represented by the letter c, thus, 27c. is read: Twenty-seven cents.
 - If dollars and cents be taken together, they are written thus: \$84.52 is read: Eighty-four dollars and fifty-two cents. \$7.08 is read: Seven dollars and eight cents.

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CANADIAN MONFE.

Since $25 \text{ cents} = 50 \text{ cents} $	tofa S.		same as	\$30.25
75 cents =	2	P1/2	6.6	\$17.50.
/3 cents =	4	\$503	54	\$50 7F

177. We have seen in Arts. 81 and 91 how we change dollars into cents or cents into dollars.

178. The most necessary requirement in any business is the correct addition of suns of money expressed as dollars and cents.

> Ex.—Add together \$30.0: \$150.75, \$80.73. \$712.40, \$212.04.

\$30.65 The amounts are written as in Simple Addition. The sum of the cents is 257 cents, sor 200 cents and 57 cents, that is, two dollars and fifty-seven cents. We write the 57 cents under the cents column, and carry the 2 dollars, and proceed to add as

- 179. We see, then, that the Addition and Subtraction of Canadian money is the same as Simple Addition. Care, however, must be taken that the separating dot . be written in its proper place in the sum or difference.
- 180. We have now to multiply and divide sums of money by any number.

Ex.-Multiply \$241.35 by 8.

\$241.35Writing the numbers as usual, we first and8tiply the number of cents by 8, which gives280 cents, or 2 dollars and 80 cents.

\$1930.80 Place the 80 cents in the usual place. Again,

multiplying the number of dollars by 8, gives 1928 dollars, which with the two dollars carried from the cents, makes 1930 dollars. The final sum is therefore \$1930.80.

This is the product that would have been obtained if the numbers had been multiplied as in Simple Multiplication.

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181. To divide a sum of money by any number.

Ex.—Divide \$197.35 by 5; or, in other words, divide \$197.35 into 5 equal parts.

5)\$197.35 Writing the numbers as usual, we first \$39.47 divide the number of dollars. This gives 39 dollars and a remainder of 2 dollars, or 200 cents. The 200 cents taken with the 35 cents make up 235 cents, which being divided by 5 gives 47 cents.

Hence the quotient is \$39.47.

This is the quotient that would have been found if the numbers had been divided as in Simple D₁.

41) 5412 (132Ex.—How often will 41 cents be contained in \$54.12?41tained in \$54.12?131This is the same as finding how often12341 cents is contained in 5412 cents.82We therefore simply divide 5412 by8241, and obtain 132 times.

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- 182. We thus see that Addition, Subtraction, Multiplication, and Division of Canadian Money is the same as in whole numbers.
 - The statement in the last Article applies equally as well to United States money.

EXERCISE 44.

- 1. Add-together \$34.12, \$43.24, \$21.34, \$20.41, \$34.12 and \$21.32.
- 2. I gave to A. \$41.23, to B. \$42.23, to C. \$14.43, to D. \$3.43, to E. \$24.02, to F. \$24.01: what did I give in all?
- 3. A man owes A. \$27.18, B. \$56.43, C. \$8.94, D. \$45.73, E. \$108.99, F. \$62.86, and G. \$5.09: how much does he owe in all?

CANADIAN MONEY.

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- 4. Bought of Jas. Foster & Sons: Knives, \$41.23; Nails, \$40.32; Tools, \$34.23; Fire-arms, \$24.32; Gunpowder, \$42.43; Sundries, \$32.43: find the total cost.
- 5. I made the following deposits in the Dominion Bank: Cheques, \$412.13; Notes, \$401.21; Silver, \$124.10; Gold, \$132; Drafts, \$301.24: find the total deposit.
- 6. Find the amount of the following accounts: \$40.19, \$78.51, \$90.84, \$112.79, \$29.08, \$5.18, \$929.03, \$33.33.
- 7. I spent \$800.50 in Toronto, \$75.40 more in Hamilton, but \$101.05 less in London: what did I spend altogether?
- 8. Bought a farm for \$3273.08, a house for \$1503.91, horses for \$429.17, cows for \$273.54, sheep for \$290.09, hogs for \$447.26, and furniture for \$298.98: what was the total amount?
- 9. Bought of Rice Lewis & Son the following bill: Tackle, \$88.88; Rope, \$99.99; Pulleys, \$90.09; Wire, \$7.70; Flags, \$17.90; Steel, \$183.84; and Cutlery, \$611.12: find the amount of the bill.
- After lending A. 60 dollars, B. 139 dollars 44 cents, C. 56 dollars 73 cents, D. 78 dollars 17 cents, E. \$93.39, F. \$45.09, I had left \$357.28: what sum had I at first ?
- 11. Add together 26 dollars 3 cents, 50 dollars 90 cents, 49 dollars 1 cent, 108 dollars 14 cents, 77 dollars 25 cents, 83 dollars 68 cents, and 40 dollars 8 cents.
- 12. From \$593.15 take \$208.28.
- 13. I owe a firm \$503.01, and pay \$267.08: what do I still owe?
- 14. What change do I receive from a hundred dollar bill if I pay for goods worth \$67 43?
- Find the difference between nine hundred and three dollars and twenty cents, and \$705.82.
- 16. A. is worth \$19327.30, and B. \$29120.91: what is the one worth more than the other?
- "17. What is the cost of 327 oxen at twenty-seven dollars and three cents each?

- 18. Find the cost of 13 barrels of apples, each containing three bushels, at 73 cts. a bushel.
- 19. What will 50 boys receive for 2 days' work of 9 hours each, at the rate of 15 cts. an hour for each?
- 20. What will be the cost of 2192 pounds of lard at 9 cts.
- 21. Bought of the Virginia Tobacco Company, Toronto, 5 hogsheads of tobacco, each weighing 560 pounds, at 28 cts. a pound : what was the whole cost ?
- 22. Find the value of the uniforms for 14 companies of 90 men each, at \$414 per uniform?
- 23. A merchant sold 3725 barrels of flour, gaining 42 cts. on each barrel : find the total gain.
- 24. What will the paving of 880 square yards of road cost at \$2.05 a square yard?
- 25. At 32 cts. a foot, what will 391 feet of rope cost?
- 26. Messrs. W: A. Murray & Co. received from Europe to bales of silk, each containing 27 pieces of 33 yards each: what was the value of the whole at \$2.90 a yard?
- 27. How often will \$85.14 contain 99 cents?
- 28. I buy books at \$1.08 each, and pay \$933.12 : how many books do I buy?
- 29. Divide \$18321 by \$2.40.
- 30. If \$221.20 be equally divided among 70 men, what does each get?
- 31. If \$402.20 be equally divided among 19 men, how much will remain?
- 32. A bank pays off a debt of \$147085.96 at the rate of \$253.16 a month: how long will it take to pay it all off?

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- 33. Bought from Eby, Blain & Co. 20 boxes of raisins, 22 pounds in each, and paid \$66: how much is that a pound?
- 34. A dealer sells 15 bags of coffee for \$378, worth 24 cts. a pound: how many pounds did he put in each bag?
- 35. Jones is worth \$19381.37, and Brown \$2917.39 less than Jones : what are both together worth?

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STERLING MONEY.

- 36. A man having \$379, bought 97 lambs at \$2.95 each: h w much had he left?
- 35. Sold J. Cleghorn & Son 37 boxes of figs at \$2.75 a box, losing \$27.30: what did they cost me at first?
- 38. Received from A. \$19.89, from B. \$33.24, from C. \$25.47 more than from A.: how much less was received from B. than from C.?
- 39. Bought 359 shares at \$1.20 a share, and had left \$99.80: what sum had I at first?
- 40. Bought 324 pounds of t a for \$243: if I sold it for 15c. a pound more than I gave for it, what was my whole gain and se ing price per pound?
- 41. A man sold his house for \$1567.30 and his land for \$3121.30, and bought building lots at \$23.80 each : how many could he buy?
- 42. While I was making \$80 a week, I saved \$98.35 in five weeks: what d I spend a week?
- Borrowed from A. \$93.86, \$46.31, and \$101.88; from B. \$9.08; and then paid off my debt to C., which was \$197.58: what had I left?
- 44. How many 25-cent pieces would pay for 80 horses at \$1021 each ?
- 45. A man sold 53 bags of flour at \$1.04 a bag; his neighbor sold 13 bags less, but at 15 cts. more a bag: how much more did one get than the other;

BRITISH OR STERLING MONEY.

- 183. After understanding the coinage of our country, it is necessary to enquire into that of Great Britain, on account of the very close relation between the two countries.
- 184. The smallest coin of Great Britain is the Farthing, which is made of copper.
 - Four of these pieces make up in value one Penny, also a copper coin.
 - There are twelve pence in a Shilling (a silver coin). which passes in Canada for 24 cents.

Twenty shillings make the Found, or gold Sovereign.

185. We thus have the following

TABLE OF STERLING MONEY.

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4 farthings	make	I	penny.	d.	
-2 pence	"	I	shilling.	e.	
20 shillings	" "	I		£.	
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The farthing being a quarter of a penny, is written $\frac{1}{2}$; two farthings, being the half of a penny, is written $\frac{1}{2}$; three farthings is written $\frac{3}{2}$.

Thus £7 8s. 7³/₄d. is read: 7 pounds, 8 shillings, 7 pence, 3 farthings.

186. We see that any number of pounds are brought to shillings by multiplying the number of pounds by 20; shillings to pence by multiplying by 12; pence to farthings by multiplying by 4.

Ex. 1.-Express £8 as pence.

i and as pence.
£There are 20 shillings in £1, hence8there must be 8 times 20 shillings in20£8, that is 160 shillings.
160 shillings. There are 12 pence in 1 shilling, hence 12 there will be 160 times 12 pence in 160 shillings, that is 1920 pence.
1920 pence. Therefore $\pounds 8 = 1920$ pence.
<i>Ex.</i> 2.—Express £2 105. 11 $\frac{1}{2}$ d. as farthings. £ s. d. In £2 there are 40 shillings, as before, 2 10 11 $\frac{1}{2}$ but we must add to these the 10 shil- lings, which makes 50 shillings.
50 Again, in 50 shillings there are 600 pence, 12 which when added to the 11 pence gives 611 pence.
$\begin{array}{ccc} 611 \\ 4 \\ \hline 4 \\ \hline 6446 \end{array} \qquad \begin{array}{c} \text{Finally, in } 611 \text{ pence there are } 2444 \\ farthings, which with the \frac{1}{2}d., or 2 farthings, makes 2446 farthings. \end{array}$
Therefore £2 10s. $11\frac{1}{2}d. = 2446$ farthings.
n the same way, any number of a higher 1

187. In the same way, any number of a higher denomination may be brought to an equal value in a lower denomination,

STERLING MONEY.

188. We will now express any number of a lower denomination in units of a higher denomination.

Ex. 1.—Change 1200 farthings to pounds.

4)1200
12)300
2'0)2'5
1'5

Since 4 farthings make 1 penny, 1200 farthings will make just one-quarter of 1200 pence, that is 300 pence. In the same manner, 300 pence will make onetwelfth of 300 shillings, that is 25 shil-

lings. Lastly, we divide the number of shillings by 20, to bring them to pounds, which gives 1 pound and 5 shillings remaining. Hence 1200 farthings=£1 5s.

Ex. 2. - Express 3477 farthings in the higher orders.

,	Dimiti di condetta.
4) <u>34</u> 77	Dividing the farthings by 4. we obtain
12)8691	and period diff. I farthing moment
2'0)7'2 51	
the second secon	/~ Summers and E Dence and
$3 12 5\frac{1}{4}$	
Thornford	we have 3 pounds and 12 shillings over.

Therefore 3477 farthings = £3 12s. 5 d.

189. In the same way, any number of units of a lower order may be brought to the same value in units of a higher order.

EXERCISE 45.

- 1. How many farthings in 141d.? In 273d.?
- 2. How many pence in 468s.? In £55 19s. 7d.?
- 3. Express £754 17s. 9^a/₄d. in farthings.
- 4. How many pounds in 7660s.? In 114720d.?
- 5. Reduce £15 8s. 71d. to farthings
- 6. Change 21368 farthings to pounds, etc.
- 7. Reduce 854d. to pounds, etc.
- 8. Bring £3 19s. 7d. to farthings.
- 9. Express 4s. 23d. in farthings.
- 10. Reduce £21 os. o3d. to farthings.
- 11. Express in £ s. d.:
 - (I) 5317 pence.
 - (3) 38003 farthings.

(2) 16629 farthings. (4) 720370 pence.

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- 22. How many six-penny pieces in £528 6s. 6d.?
- 13. How many pounds, etc., in 3729 three-penny pieces?
- 14. In an English school, half the boys wrote in copy books, and paid 3d. each week; 99 boys paid 21 a a week; and 59 paid 1d.: how many in the school, and what was paid in all?

190. To add together any sums of money.

Ex. 1.--Add together £4 8s. 61d., £1 9s. 112d., 105. $4\frac{1}{2}$ d., £3 19s. 112d.

- s. d. We first place the quantities so that 8 61 the same kind are in the same column. 9 113 Adding the farthings' column, we get 9 10 42 farthings, that is 2 pence and 1 farth.
 - farthings, that is 2 pence and t farthing. We write the 1 farthing in its proper place, and carry the 2 pence to the pence column.

The pence column gives when added 32 pence, which with the 2 pence carried is 34 pence, or 2 shillings and 10 pence.

Write the 10 pence under the proper column, and carry the 2 shillings to the sum of the shillings' column.

This makes in all 48 shillings, which is equal to 2 pounds and 8 shillings. Place the 8 shillings under the proper column, and carry the 2 pounds.

This, when added to the pounds' column, gives 10 pounds.

Hence the total sum is £10 8s. 10¹d.

As in Art. 51 of Simple Addition, we might have placed each total under its column, as £2 456 34^o/₂d., but, as in that case, we always change the units of the lower order into units of a higher, and write down the remaining units under their own column. 191.

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STERLING MONEY.

EXERCISE 46.

Add together the following sums of money:

- 1. £15 105. 9d., £8 9s. 7d., £1 12s. 10d., £1 18s. 4d.
- 2. £8 95. 7³/₄d., £7 125. 4¹/₄d., £1 195. 11¹/₂d., 155. 8³/₄d.
- 3. £9 8s. 10d., £8 16s. 11d., £7 8s. 3d., £8 16s. 2d., £7 3s. 4d., £8 17s. 2d., £3 8s. 11d., £6 9s. 2d., £3 7s. 5d.
- 4. £8 17s. 5d., £5 8s. 61d., £7 4s. 41d., 19s. 43d., £18 10s. 11d., £3 7s. 4d., £5 12s. 72d., £8 19s. 2d., £7 2s. 4d.
- 5. £94 15s. 5³/₄d., £87 16s. 6¹/₄d., £91 17s. 7¹/₂d., £67 18s. 8³/₄d., £84 19s. 9¹/₂d., £98 0s. 0³/₄d., £56 17s. 11d., £133 38. 10¹/₄d., £212 18s. 9d.
- 6. £816 175. 8¹/₄d., £389 185 10¹/₄d., £31 175. 11d., £346 185. 6¹/₄d., £407 135. 8³/₄d., £748 115. 11d., £567 145. 4³/₄d., £687 155. 10¹/₄d., £827 165. 10³/₄d.
- 7. $\pounds7148$ 115. $8\frac{1}{2}d. + \pounds3596$ 185. $11\frac{1}{2}d. + \pounds71416$ 135. $8\frac{1}{2}d. + \pounds81$ 115. $4d. + \pounds7186$ 135. $4\frac{3}{2}d. + \pounds714$ 135. $8\frac{3}{2}d. + \pounds8196$ 185. $10\frac{1}{2}d + \pounds811$ 85. 6d.
- 8. \pounds_{17846} 178. 8d. $+\pounds_{3479}$ 138. 11d. +6783 148. 5d. $+\pounds_{687}$ 158. 10d. $+\pounds_{8412}$ 118. 4d. $+\pounds_{6791}$ 158. 7d. $+\pounds_{6149}$ 178. 8d. $+\pounds_{8416}$ 118. 3d. $+\pounds_{879}$ 188. 4d. $+\pounds_{7358}$ 138. Ed.
- 9. £4738 17s. 2d. +£3947 19s. 8d. +£7135 13s. od. + £914 os. 8d. +£4783 15s. 11d. +£7198 17s. od. + £8359 11s. 8d. +£8746 os. od. +£879 8s. 7d. +£9157 16s. 8d.
- 10. \pounds_{3109} os. 11d. $+\pounds_{798}$ 13s. $4\frac{1}{2}d + \pounds_{9146}$ 13s. 7d. + \pounds_{874} os. 8d. $+\pounds_{9146}$ 3s. 4d. $+\pounds_{8749}$ 13s. 5d. $+\pounds_{8735}$ 19s. 9d. $+\pounds_{9146}$ 17s. 8d. $+\pounds_{874}$ 13s. $4\frac{1}{2}d. +\pounds_{68}$ 10s. $4\frac{3}{4}d.$

191. To subtract one sum of money from another.

Ex. 2.-Take £3 55. 82d. from £5 45. 62d.

5	s. 4 5	d. 6 1 8 <u>3</u>	say, 3 farthings from 2 farthings we cannot. Add one of the next higher
£1	18	91	or a forthing a

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farthings. Again, having taken one of the 6 pence, we have to take 8 pence from 5 pence, which we cannot. Add 1 shilling or 12 pence. Then 8 pence from 17 pence leaves 9 pence.

Again, having used one of the 4 shillings, we have to take 5 shillings from 3 shillings, which we cannot. Add I pound or 20 shillings.

Then 5 shillings from 23 shillings leaves 18 shillings.

Lastly, having used one of the 5 pounds, we have to take 3 from 4 pounds, which leaves one pound. Hence the difference is £1 18s. 9³/₄d.

The only difference between this and simple subtraction is that, in simple subtraction, we always add 10, because 10 units of any order make 1 of the next higher, while in the present case the number of units in the orders above differs in each, that is, 4 in the first, 12 in the second, and 20 in the third. In every other respect the operations are exactly alike.

EXERCISE 47.

- 1. From £58 19s. 91d. take £50 2s. 41d.
- 2. How much greater is £60 8s. 9d. than £50 19s. 11d? 3. I owned £715 10s., and lost £620 14s. 61d. : what
- 4. Subtract £92004 18s. 53d. from £99153 10s. 21d.
- 5. A man had £8 6s. $9\frac{3}{4}d$; he gave away £2 4s. $5\frac{1}{4}d$. and then spent \pounds_3 os. 4d. : what had he left?
- 6. Bought goods for £9 6s. $10\frac{1}{4}$ d., and paid £2 17s, $2\frac{3}{4}$ d., what do I still owe?

7. What must be put with £47541 5s. 63d. to make up £50650 6s. 53d.?

8. A man has in cash £3443 15s., a house worth £474 8s. 9d., goods worth £713 11s., a farm worth £574, debts due to him £315, a vessel valued at £957 18s. 1112d; but he owes A. £115 7s. 8d., B. £74 13s. 4d., and C. £327 18s. $4\frac{3}{4}$ d : find what he is really worth.

9. From six hundred and seventy-one pounds eleven shillings and eight pence, take the sum of £600 15s. and twenty-five pounds and five pence.

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STERLING MONEY.

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192. To multiply any sum of money by a whole

Ex. 3.-What will £12 10s. 84d. produce when repeated 11 times?

s.

d. Set down the numbers as usual. We 12 10 81 will, in the first place, leave each product unchanged under its own II. column or order, as in Art. 190, thus: £132 110 8811 Eleven times 1 farthing is 11 farth-

ings; 11 times 8 pence is 88 pence; 11 times 10 shillings is 110 shillings; 11 times 12 pounds is 132 pounds.

The result is £132 1105. 8811d. Now 11 farthings are 2 pence and 3 farthings. We set down the 3 farthings and carry the 2 pence to the 88 pence, making it 90 pence. Again, 90 pence make 7 shillings and 6 pence. Place the 6 pence under its own column, and carry the 7 shillings to the 110 shillings, making it 117 shillings. But 117 shillings are 5 pounds and 17 shillings. Place the 17 shillings as usual, and carry the 5 pounds to the 132 pounds, making 137 pounds. The work would then appear thus :

£	s.	d.
12	10	8 1
		11

£137 17 63

193. This will be seen to agree perfectly with simple multiplication of numbers, and every remark made in regard to simple multiplication will apply to the present case.

194. We may, therefore, use the factors of any multiplier, instead of taking the multiplier at once.

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Ex. 4.—If 24 men earn £3 155. $10\frac{1}{2}$ d. each, what is earned in all ?- that is, find 24 times £3 15s.

23 15 101 The factors of 24 are 3 and 8. First multiply by 3, which gives 11 pounds 7 shillings and 7 pence half-penny, or 2 farthings. Next multiply by 8, 71 7 8 as follows: 8 times 2 farthings = 16farthings = 4d. 8 times 7 pence = I O 56 pence. This with the 4d. carried

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gives 60 pence, which = 5 shillings and no pence remaining. 8 times 7 shillings = 56 shillings. This, with the 5s. carried, makes 61s., or £3 and 1s. 8 times £11 = £88, which, with the £3 carried, gives £91.

Hence the amount earned is £91 1s.

EXERCISE 48.

- 1. What is the value of three articles at £4 6s. 7¹/₂d.
- 2. One man can earn £9 8s. 4¹/₄d.; what will 4 men earn?

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- 3. At 175. 32d. each, what must I pay for 7 articles ?
- 4. What does £74 18s. 11¹/₂d. produce when repeated 6
- 5. Find 8 times £18 os. 11d.
- 6. One-ninth of a vessel is worth £17 155. 01d. : what is the whole worth?
- 7. What will 10 persons spend at the rate of £13 5s. 7¹/₄d.
- 8. Find the value of 11 sewing-machines at £18 os. 4¹/₄d.
- 9. Multiply £70 os. 112d. by 12.
- 10. If 18 men each subscribe sixty-three pounds and eight pence three farthings, what will the whole subscription amount to?
- 11. At 1d. each, articles cost £13 178. 01d., what will they cost at 38. each?
- 12. 29 men are employed on a road : what will be required to pay them at arate of £5 7s. 6½d. each?
- 13. What amount must be five 1 among 35 men that each may receive £132 os. 3td.?
- 14. A drover makes a profit of £2 95. 21d. on every animal he takes to market: what will he gain in a day when he takes 31 to market?

15. Of what amount is £81 os. 81d. the 187th part?

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- 16. The "Dominion" carried to Liverpool from Quebec 132 head of cattle; on arrival they sold for £8 75. 91d. per head : what did the owner receive for them ?
- 17. Brick is worth in England £2 5s. 7d. a thousand : what will be the cost of brick to build a bake-house requiring 10 thousand?
- 18. What must be paid for 12 dozen Christmas geese at

195. To divide any sum of money by a whole num-

When the divisor is 12 or under, the work is carried on mentally, as in Simple Division.

Ex. 5.-If £812 155. 01d. be divided among 11 women, what will each receive? or, divide £812 15s. old. by 11.

 \pounds s. d. Set down the numbers as usual. As 11)812 1 in simple division, 11 is contained in 812, 73 times and 9 pounds over, 73 17 03 that is, the eleventh part of £812 is \pounds_{73} and \pounds_{9} remaining. Write the \pounds_{73} in its proper place, and carry the £9.

Now the £9 must be brought to shillings, and then added to the other 15 shillings, that is, 180+15=195. Again, 11 is contained in 195, 17 times and 8 shillings over. Write the 175. in its proper place, and carry the 8 shillings.

These 8 shillings are equal to 96 pence, and as there are no pence to be added, 11 is contained in 96, 8 times and 8d. over. Write the 8d. as usual, and carry the 8d. left over.

These 8 pence, with the 1 farthing, make 33 farthings, and 11 is contained in 33, 3 times. Write down the 3 farthings in its place.

Each woman, therefore, would receive $\pounds73$ 17s. $8\frac{3}{4}d$.

196. When the divisor is greater than 12.

Ex. 6 .- Divide £93 16s. 101d. into 99 equal parts.

- £ s. d. s. d.
- 99)93 16 101 (18 111

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Here, £93 will not contain 99, hence it 1800 16 (added) is reduced to shillings (1860), and the 16s. added, making 1876 shil-) 1876 (18 This contains 99, 18 times. lings. 99 Place this 18s. in the quotient, and 886 bring the remaining 94s. to pence 792 (1128), add in the 10d., and divide the result, 1138 pence, by 99. This 94 gives 11 pence, and 49 pence over. 12 Write the 11d. in the quotient. Bring 1128 the 49 pence to farthings (196), and 10 (added) add the 1d., or 2 farthings, making)1138 (11 198 farthings. Finally, divide by 99, 1089 and we have 2 tarthings, or 1d., to place in the quotient. 49 Thus the quotient is 18s. 111d.

196The above agrees exactly with the
work performed in Art. 100, the mul-
tipliers there, however, being 10 in
each case, instead of 20, 12, and 4, as
in the present case.

197. To divide one sum of money by another.

Ex. 7.—If each person earn 175. 11⁸/₄d., how many persons will £50 6s. 10d. pay? In other words, how many times does £50 6s. 10d. contain 175. 11³/₄d.?

Before we can divide one number by another, we have shown that they must be of the same kind. Hence we must bring each of the given amounts to units of the same order, that is farthings.

£50 6s. 10d. =48328 farthings 17s. 11 $\frac{3}{4}$ d. = 863 "

The question now is: How often are 863 farthings

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contained in 48328 farthings. This will be found by division.

803) 48328 4315	(56	
	5178 5178			

Hence there will be 56 persons.

198. From the above we obtain the following

RULE.

To divide one amount by another, reduce each to the towest order mentioned in either. Then divide as in simple division.

In the preceding examples we have made use of Sterling Money to explain the addition, subtraction, multiplication and division of compound quantities. The same principles apply to all other compound quantities.

EXERCISE 49.

- 1. Find the fourth part of £57 18s. 9d.
- 2. How much more in the fifth part of £798 13s. 4d. than in the sixth part of £33 17s. 6d.?
- 3. What is the value of a sixth share in a vessel that cost £899 7s. 6d.?
- 4. Divide £812 155. 04d. into 11 equal parts.
- 5. If 23 men earn £91 118. $4\frac{1}{2}$ d., what is that apiece?
- 6. I paid £92961 115. 11d. for 111 lots of land: how much was that for each?
- 7. The cost of carrying 149 cattle to Liverpool by the "Allan Line" was £589 9s. 7¹/₂d.: how much was that a head?
- 8. What sum of money must be multiplied by 9027 to produce £7175571 14s. 03d.?

equal parts.

99, hence it (1860), and 1876 shil-, 18 times, otient, and to pence and divide 99. This bence over, ent. Bring (196), and (5, making vide by 99, or $\frac{1}{2}$ d., to

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vide £6917	7s.	11d. by 129.
_£4747	5s.	3 ³ d. by 375.
£17303	I 2S.	11d. by 250.
£7957	4s.	61d. by 100.

- 10. If 14 hundred-weight of sugar cost in Bristol £35 8s. 9d., how much is that per hundred-weight ?
- 11. If 99 bags of figs cost in Glasgow £413 18s. 101d., what will a bag cost in Edinburgh, the carriage being 6s. 41d. per bag?

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12. Divide £3 75. $4\frac{1}{2}$ d. by 95. $7\frac{1}{2}$ d.

£803 7s. 4d. by £73 os. 8d. £255 3s. od. by £15 18s. 111d.

- £907 4s. od. by £8 8s. od.
- 13. To how many men will £37 3s. allow £4 12s. 10¹/₂d.
- 14. A lady spent £75 os. 9d. in lace shawls at £6 5s. o_4^3 d. each : how many shawls did she buy?
- 15. What part of £670 7s. is £83 15s. 101d.?
- 16. How often is £280 155, 01d. contained in £33971 os.
- 17. How many purses of £12 75. 10¹d. each can be made up of £14871 55.?
- 18. How many times can £13 os. ofd. be taken from \pounds_{175} 3s. $6\frac{3}{4}$ d., and how much will be left?
- 199. After the Table of Money, the most necessary, perhaps, is the Table of Weight, as nearly all the articles of merchandise are bought and sold by weight.
- 200. The smallest weight used for this purpose, in practice, is the ounce, sixteen of which make up a pound.
- 201. The Table in full is as follows :

AVOIRDUPOIS WEIGHT.

- 16 ounces (oz.) make 1 pound, 1b. 100 pounds
- " I hundredweight, cwt. 20 cwt. " 1 ton, T.
- It is used in weighing all heavy merchandise, such as iron, groceries, etc.

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TABLE OF WEIGHT.

The pupil should be taught to express every order in units of every lower order; for example

 $T_{.} = 20 \text{ cwt.} = 2000 \text{ lbs.} = 32000 \text{ oz.}$

1 cwt. = 100 lbs. = 1600 oz.

I lb. =16 oz.

A similar table may be made for every other weight or measure.

202. A different table is used when dispensing drugs, medicines etc., and is called

APOTHECARIES' WEIGHT.

20 grains	(gr.)) make	: 1	scruple, sc.	
-----------	-------	--------	-----	--------------	--

3 scruples	66	1 dram, dr.
8 drams	" (I ounce, oz.
12 ounces	66	I pound lb

203. The following is the table used by jewellers in weighing precious stones, gold, silver, etc., and is called

TROY WEIGHT.

24 grains (gr.) make 1 pennyweight, dwt.

20 pennyweights " 1 ounce, oz.

12 ounces " I pound, lb.

The "grain," "ounce" and "pound" are the same in the two latter tables, that is, a grain of gold dust would balance a grain of quinine.

204. All examples in the preceding tables are worked just as in the case of sterling money.

Ex. 1.-In 2 lbs. 5 dwt. of gold, how many grains?

lbs. dwt.

5 Since there are 12 oz. in 1 lb., there must 2 12 be 12 times 2 or 24 oz. in 2 lbs.

24 OZ. As there were no ounces given, we have none to add to the 24 ounces. 20

485 dwt. Again; since there are 20 dwt. in 1 oz., there must be 24 times 20, or 480 dwt. 24 in 24 ozs. This, with the 5 dwt. given, 1940 makes a total of 485 dwt. In the same manner, 485 dwt. equals 485 times 24, 970 or 11640 grains.

11640 grs.

Bristol £35 eight? 18s. 101d., e carriage

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Ex. 2.—A quantity of sugar weighing 11 T. 6 cwt. 10 lbs., just fills 5 vats; what will each vat hold? Here we must find the fifth part of the given weight.

cwt. lbs. oz. Dividing 11 tons by 5, we get 5)11 2 tons and 1 ton over.

I T. 20 cwt., which, with the 2 5 22 given 6 cwt., makes 26 cwt. 98 $26 \text{ cwt.} \div 5 = 5 \text{ cwt. and } 1 \text{ cwt., or 100 lbs. over.}$ This, with the 13 lbs., makes 113 lbs. 113 lbs. $\div 5 = 22$ lbs. and 3 lbs., or 48 ounces over.

 $48 \text{ oz.} \div 5 = 9\frac{3}{5} \text{ ounces.}$ Each vat will thus hold 2 T. 5 cwt. 22 lbs. 98 oz.

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EXERCISE 50.

The first eleven examples to be solved mentally.

(a) 1. What part of a pound of tea is 4 oz.? 8 oz.? 12 oz.? 2. What part of a ton is 5 cwt.? 12 cwt.? 8 cwt.?

3. What part of a cwt. is 25 lbs.? 50 lbs.? 4. What is the difference between 1 grain and 1 pennyweight? Between I ton and I cwt.? Between I dram and 2 scruples? Between 2 oz. and 12 drams? Between 1 hundredweight and 60 pounds?

5. How many grains of silver in 1 of a lb.? In 1 of a lb.? In f of a lb.? In f of a lb.?

6. How many grains in 1 pound of old silver? 7. How many ounces in 3 pounds of ginger? In 2 lbs. of quinine? In a of a lb. of sago? In 1 lb. 5 oz. of

8. How many ounces in $\frac{1}{4}$ lb. of tea, $\frac{1}{2}$ lb. of sugar, and

9. What is the cost of $\frac{1}{2}$ lb. of nutmegs at 8 cents an ounce? Of a of a scruple of quinine at 3 cents a

grain? Of $\frac{2}{3}$ of a lb. of gold coin at \$20 an ounce? 10. How many ounces in $\frac{1}{2}$ a cwt.? II. Which is the cheaper of the following prices:

T. 6 cwt. each vat

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TABLE OF WEIGHT.

- (a) $\frac{1}{2}$ d. a grain or 1s. a dwt. ?
- (b) \$5 a cwt. or \$100 a ton?
- (c) 20c. an oz. or \$2.50 a lb. of opium?
- (d) 48c. a lb. or 4c. an oz. of spice?
- (e) 50c. a lb. or \$60 a cwt. ?
- (f) \$2 a dwt. or \$50 an oz.?
- (b) 1. Write out a Table for Troy and Apothecaries' Weight like the Table in Art. 201.
 - 2. In 1746 grains Troy, how many oz., etc.?
 - 3. In 5 lbs. 7 dwt. how many grains?
 - 4. How many pounds, etc., in one million grains Troy?
 - 5. Find the number of grains in 10 lbs. 1 oz. 10 dwt. 1 gr.
 - 6. How many grains of calomel in 7 oz. 3 sc.?
 - 7. Find the number of lbs. in 691 sc.
 - 8. How many powders of morphine of 1 grain each can be made from 3 lbs. 2 oz. 3 dr. 2 sc. 5 grs.?
 - 9. In 5 cwt. 84 lbs. of sugar, how many one pound packages?
 - 10. How many ounces of 80-cent tea can be put up from 3 cwt. 55 lbs. 4 oz.?
 - 11. How many cwts., etc., make 5767 oz.?
 - 12. Change 7359 pounds of coal to tons, etc.
 - 13. A dealer sold to one customer 3 tons 5 cwt. 17 lbs. 13 oz. of sugar; to another, 4 tons 7 cwt. 35 lbs. 12 oz.; to another 1 ton 15 cwt. 63 lbs. 7 oz.: how much sugar did he sell in all?
 - 14. What is the sum of 15 tons 6 cwt. 45 lbs. 5 oz.; 3 tons, 17 cwt. 80lbs. 6 oz.; and 26 tons 31 lbs. 7 oz.?
 - 15. What is the sum of 21 lbs. 7 oz. 12 dwts. 10 grs.;
 28 lbs. 5 oz. 8 dwts. 7 grs.; 7 lbs. 6 dwts. 15 grs.;
 41 lbs. 6 oz. 20 grs.; and 9 lbs. 7 grs.?
 - 16. From 16 cwt. 90 lbs., take 8 cwt. 58 lbs. 6 oz.

ARITHMETIC FOR BEGINNERS. 17. From 85 tons 16 cwt. 39 lbs., take 61 tons 14 cwt. 18. A man sold 15 loads of grain, each weighing 1 T. $270\frac{1}{3}$ lbs; what did the whole weigh? 19. If 25 men each buy 16 T. 3 cwt. 101 lbs. of goods, what do they buy in all? 20. Each of 56 goblets weighs 12 lbs. 3 oz. 16 dwt.; find the weight of the whole. 21. If a Mexican dollar weigh 17 dwt. $4\frac{1}{4}$ grs., what 22. A grocer buys 13 hogsheads of sugar weighing 6 T. 8 cwt. 57 lbs., what did each weigh? 23. If 31 cwt. 18 lbs. of rice be put up in parcels of 3 lbs. 8 oz. each, how many parcels will there be? 24. How many ounces will be left over ? 25. How many bags of salt, each containing 2 cwt. 35 lbs., are there in 3 T. 3 cwt. 45 lbs? 26. How many forks, each weighing 2 oz. 10 dwt. can be made from 13 lbs. 7 oz. 15 dwt. of silver, and what will be left over? 27. A grocer having 17 cwt. 69 lbs. of soda, sold 4 cwt. 96 lbs. of it, and the remainder he put into six boxes; how much did each box contain? 28. Divide 7 lbs. 6 oz. 13 dwt. by 3 oz. 15 dwt. 13 grs. 29. Divide 131 lbs. 2 oz. 15 dwt. 20 grs. by 2 lbs. 7 oz. 30. Divide 3 T. 2 cwt. 40 lbs. by 12 cwt. 48 lbs. 31. If one-thirteenth of a certain gold coinage be alloy, what is the quantity of pure gold in 274 pieces weighing 54 grs. each? 32. What is the total weight of silver in half a dozen dishes, each weighing 49 oz. 3 dwt. 4 grs.; a dozen plates, each weighing 16 oz. 17 dwt.; and a salver, weighing 126 oz. 15 dwt. 18 grs, ? 33. Add together 2 of 5 cwt. 40 lbs. ; 2 of 3 tons 6 cwt.

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207.

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13 grs. bs. 7 oz.

e alloy, pieces

dozen dozen salver,

5 cwt.

TABLE OF WEIGHT.

- 34. What is the difference between $\frac{1}{3}$ of $4\frac{1}{2}$ of 2 lbs. 5 oz. 6 dwt.; and $\frac{3}{7}$ of $2\frac{1}{3}$ of 6 oz. 10 dwt. 10 grs.?
- 35. How often is 3 of 5 scr. of quinine contained in a package containing 6 lbs. 7 oz.?
- 36. What weight is that of which 17 lbs. 2 oz. is $\frac{11}{11}$? of which $5\frac{1}{2}$ cwt. is $\frac{0}{11}$?
- 37. Of what weight is 2 oz. 3 dwt. three-seventeenths?
- 38. What part of 3 cwt. 6 lbs. would just balance 2 lbs. $6\frac{1}{2}$ oz.?
- 39. Add together $\frac{1}{3}$ of 2 lb., $\frac{3}{7}$ of 5 oz., $6\frac{7}{8}$ dwt., and $3\frac{1}{3}$ grs.
- 40. By how much does the $\frac{1}{4}$ of $6\frac{1}{2}$ tons exceed the $\frac{1}{3}$ of 13 cwt. 17 lbs. $5\frac{1}{4}$ oz. ?
- 41. How much weight must be added to $3\frac{4}{11}$ cwt. to make 1 ton 2 cwt. 12 lbs.? and what weight taken from $23\frac{5}{10}$ tons will leave $\frac{5}{2}$ of $9\frac{1}{4}$ lbs.?
- 42. Take from 5 tons of potatoes its third, its fourth, and its fifth part; what part of 17¹/₄ tons is the remainder?
- 205. All distances, lengths, breadths or widths, and heights, are expressed in miles, yards, feet, inches, &c.
 - Thus: Toronto is distant from Montreal 333 miles; a room is 20 feet long; a piece of cloth is 22 inches wide; a flag pole is 80 feet in height.
- **206.** These are included in a table called

LINEAR, or LONG MEASURE.

12 inches (in.)	make	I	foot, ft.
3 feet	66	I	yard, yd.
5½ yards	66	1	rod, rd.
40 rods	66	I	furlong, fur.
8 furlongs	66	I	mile, mi.

207. A yard measure might be shown thus :

				-	-		ADD DOG TO THE OWNER.	Contraction of the local division of the loc	Colored Western	COLUMN ADDRESS	of the local division in	 -	-	-			_			
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The three larger divisions would represent one foot each.

The thirty-six smaller divisions would each represent one inch.

208. Cloth, ribbons, etc., are usually sold by this measure, the following parts of the yard being the most 212 Half of a yard, =18 inches. Quarter of a yard, = 9Eighth of a yard, $= 4\frac{1}{2}$ Sixteenth of a yard, = $2\frac{1}{4}$ " " The sixteenth of a yard was formerly known as The Flemish Ell was $\frac{3}{4}$ of a yard, or 27 inches. " English Ell " 213. т " " French Ell or 45 inches. " " or 54 inches. These Cloth Measures are now seldom used. The following measures are used for special I. I Hand =4 in., for measuring the height of horses. 30 I Fathom = 6 ft., for measuring the depth of water. 16 I Chain = 100 links=66 ft., for measuring roads and 64 K 80 chains =1 mile. 209. By Long Measure we would find the length and breadth of a room to be a certain number of feet, yards, etc. We now wish to measure the surface of the floor. а 210. If a piece of paper were 1 inch long Fr and 1 inch broad, it would represent what is called I Square Inch of Area or Surface. 214. We 211. A Square Inch is, therefore, a SOUARE INCH r square, one inch in length and one inch in breadth. Ex. S

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SQUARE MEASURE.

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- In the same way, a Square Foot is a square, each side of which is one foot, or 12 inches in length, and from the figure we see it must contain 144 square inches.
- A Square Yard will thus contain 9 square feet, as seen from the figure where each of the small squares represents a sq. foot.

SQUARE

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lowing table, called SQUARE MEASURE.

213. These are all included in the fol-

144 square inches (sq. in.) make	I square foot on ft
9 square feet	**	1 square yard, sq. yd.
301 square yards	**	i square rod, sq. rd.
160 square rods	**	I acre, ac.
640 acres		I square mile.

Arts. 211 and 212 were found by multiplying their length by their breadth, thus:

I square foot = 12 × 12 = 144 sq. in. I square yard = $3 \times 3 = 9$ sq. ft. also, I square rod = $5\frac{1}{2} \times 5\frac{1}{2} = 30\frac{1}{4}$ sq. yds.

- From this we see that part of the above table is derived from the table of Long Measure, the 12 in., 3 ft. and $5\frac{1}{2}$ yds occurring there first.
- 214. We see then that to find the area of a floor, etc., we multiply its length by its width.
 - Ex. A table 10 feet long and 5 feet wide contains 50 square feet; for if it were only 1 foot wide, it would contain 10 square feet, but, being 5 feet wide, it must contain 5 times 10 sq. feet, or 50 sq. ft.

215. The only other measurement required is that of a solid block of marble, wood, etc., knowing its length, breadth and thickness.

216. If a block of wood were 1 inch 1 long, I inch wide and I inch thick, it would represent what is called a Cubic Inch.

217. If the square foot of surface in Fig. 2, Art. 212 had been 1 in. thick, it would contain 144 cubic inches, and, therefore, if it had been 1 foot, or 12 inches thick, it would contain



12 × 144, or 1728 cubic inches, and be what is known as a Cubic Foot.



In the same manner, if the square yard of surface in Fig. 2, Art. 212 had been one yard or three feet thick, it would contain 3×9, or 27 cubic feet, and represent a Cubic Yard.

218. We thus make up the table of

CUBIC or SOLID MEASURE.

1728 cubic inches (cu. in.) make 1 cubic foot, cu. ft. 27 cubic feet 66 1 cubic yard, cu. yd. This table, like the last, may be derived from that

of Long Measure, thus :

 $12 \times 12 \times 12 = 1728$ cubic inches in 1 cu. ft.

 $3 \times 3 \times 3 = 27$ cubic feet in 1 cu. yd.

219. We see, then, that to find the contents of a solid, we multiply its length, breadth and thickness together.

Ex. Find the contents of a block of stone, 2 yds. long, 4 feet wide, and 3 feet deep.

2 yards long = 6 feet long.

 $6 \times 4 = 24$ sq. ft. = its top surface.

24 CI Therefo 24 Cu E A feet w Ex. Ex 5월)75-2 11)1508 4'0)137 8)3written wit Sq. rds. 12 301 366 3 369 y 9 6'0)332'8 ft. 55 *** = viding the

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SQUARE MEASURE.

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we ner. ds. Now, a slab from the top, 1 foot thick, would contain 24 cubic feet.

Therefore, being 3 feet deep, there would be 3 times 24 cubic feet=72 cubic feet=2 cu. yds., 18 cu. ft.

For A cord of wood is 8 feet long, 4 feet high, and 4 feet wide; or 128 cubic feet.

Ex. Express 7544 yards as miles, etc.

$5\frac{1}{2}$)7544 2 2	First, we reduce the yards to rods by dividing $5\frac{1}{2}$, thus:
	Bring the 51 yards to half-yards, that is
11)15088	II; then bring the 7544 yards to half.

88 II; then bring the 7544 yards to halfyards, that is 15088; then 11 half-yards

4'0)137'1-7 are contained in 15088 half-yards, 1371 times and 7 half-yards. or 3¹/₃ 9)34-11 yards remaining.

- Proceeding, as usual, we obtain 4 mi. 2 4-2 fur. 11 rds. $3\frac{1}{2}$ yds., which may be written with the $3\frac{1}{2}$ yds. expressed as 3 yds. 1 ft. 6 in.

Sq. rds.	Sq. yds.	Sq.ft.	
12	6	-	

area. One side is 60 ft. in	
other.	
	 Ex. A garden is 12 rds. 6 yds. 7 ft. in area. One side is 60 ft. in length; find the length of the other.

9 6'0)332'8 ft.

 $55\frac{28}{60} = \frac{7}{15}$

 $30\frac{1}{4}$ 366 3 369 y

Since the area is found by multiplying the length and breadth together, we shall find the breadth to be $55\frac{1}{15}$ ft., by di-

viding the area 3328 sq. ft. by the length, which is 60 ft.

EXERCISE 51.

The first 11 examples to be solved mentally.

- 1. What part of a foot in length is 8 in. ? 6 in. ? 4 in. ? 3 un. ? 2 in. ?
- 2. What part of a yard of rope is 18 in.? 2 ft.? 12 in.? 9 in.? 4 in.? 3 in.? 2 in.?
- 3. What part of a square foot is 72 in.? 48 in.? 36 in.? 24 in.? 12 in.? 6 in.? 3 in.?

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DEGINNERS.	
4. What part of a sq. yard of sheet-iron is 3 ft.? 6 ft.? 1 ft.? 2 ft. 36 in.? 4 ft. 72 in.? 6 ft. 108 in.?	Ig
5. An acre of farm land is worth \$320; what must I pay for 80 rods? 40 rods? 32 rods? 20 rods? 16	20
6. If a wire fence cost 30c. per yard, what is the price of a foot? and what will be the cost of 2 rods? I furlong? I mile?	K
7. A cubic foot of matal :	21.
is the value of I solid inch? the ninth part of a cubic yard?	
	22.
8. A hall-way is 72 inches wide, and takes sixty square yards of matting to cover it; what is its length?	
many yards in length of carpet 1 yard wide; how required for it? Find its cost at pard wide will be	23.
10. What is the area of a room al and 1	24.
	25.
11. Which is the cheaper of the following prices ?	-3.
 (a) 5c. an inch, or 5oc. a foot, for lead pipe? (b) soc. an inch, or \$4 a yard, for cloth? (c) \$6 a yard, or 5oc. an inch, for lace ? (d) \$1 a yard, or \$6 a rod, for fencing? (e) 6oc. a sq. foot, or \$6.50 a sq. yd., of carpet? (f) 24c. for 8 in., or \$1 a yard, of ribbon ? 	26. 27. 28.
12. Write out tables for Long and Square Measures, as in Art. 201.	
13. Express 213 inches in length as yards, etc.	29.] t
14. How many yards, etc., in 1649 inches of wire?	c
15. How many inches in 6 rds. 4 yds. 2 ft. 9 in. of distance?	30. H
	12
16. What part of a mile is 2 fur. 36 rds. 2 yds.?	31. E
4/ How many cords of wood one the	0
	32. I
18. How many fathoms are there in a depth of $\frac{7}{5}$ of a mile?	ro 60 fi

SQUARE MEASURE.

3 ft.? 6 ft.? B in.?

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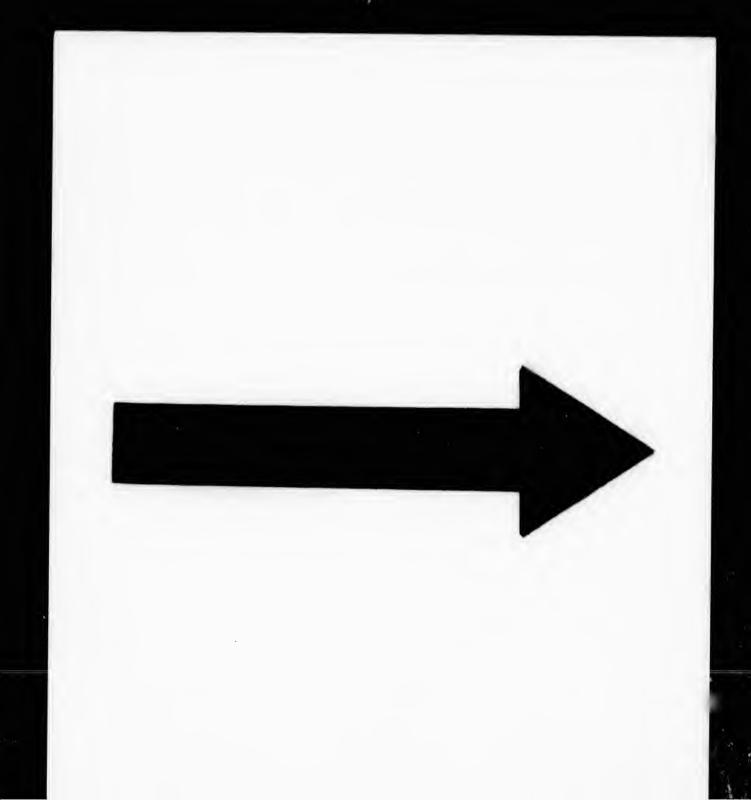
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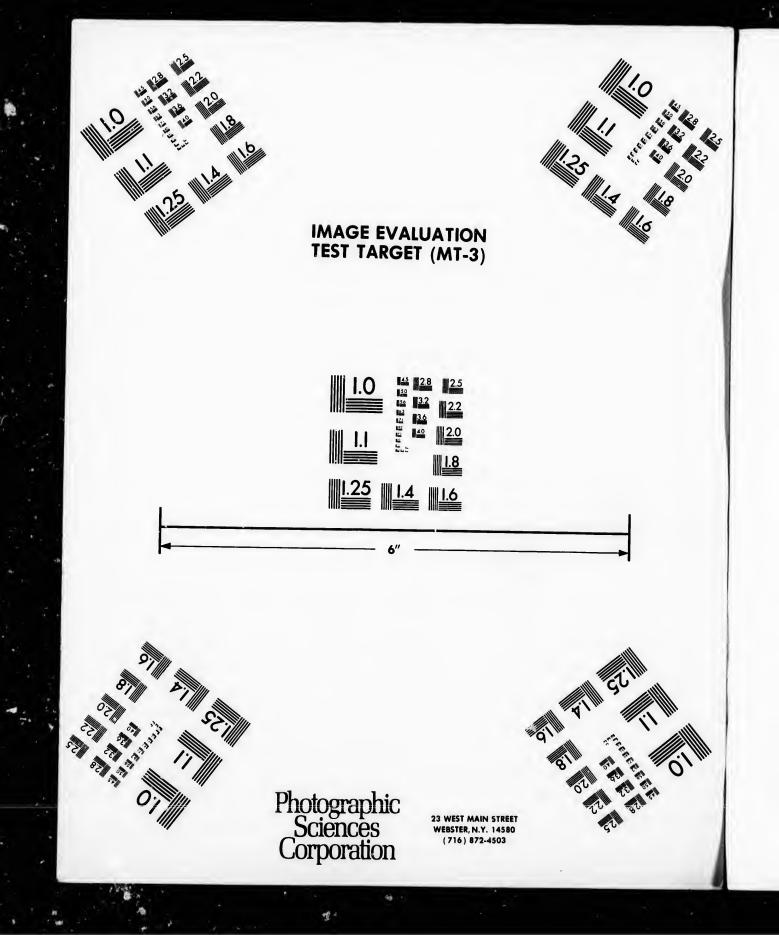
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- 19. Find the cost of digging a drain 20 feet long. 2 yds. wide, and 14 feet deep, at 90 cents per cubic yard.
- 20. Find the sum of 12 yds. 4 rds. 3 ft. 25 in.; 33 yds. 2 ft. 10 in.; 7 ft. 132 in.; 10 yds. 7 ft.; 31 yds. 100 in.; 76 yds. 89 in.

In dividing by 30¹/₄, bring both divisor and dividend ourths.

- 21. The area of a board is 21 feet; its length 15 18 in., what is its breadth?
- 22. What is the area of the four walls of a room, 13 ft. 9 in. wide, 16 ft. 3 in. long, and 14 feet high? and what is the cost of papering it at 2c. a sq. ft.?
- 23. How many suits of clothes can be made from 13 pieces of cloth, each containing 21½ yds., if it takes 7¹/₀ yards to make a suit?
- 24. In 987,654,321 inches how many miles, etc.?
- 25. If I have to measure a distance of 3 furlongs with a line three rods and a half long; how many times will the line measure the distance?
- 26. In 169,500,087,647 sq. inches, how many square miles, etc.?
- 27. If a plank be $6\frac{3}{4}$ inches wide, what length of it will give a surface of 2 square feet?
- 28. A block of marble contains 1296 cu. feet, its breadth and depth are each 9 feet; what will be its length?
- 29. If 17 men reap 19 ac. 97 sq. rods in a day, and 8 of them reap one-third of an acre each; how much ought each of the others to reap?
- 30. How many sq. yards of block pavement in a street $\frac{1}{2}$ mile long and I chain wide.
- 31. By how much does a road 18 miles long exceed one of 12 mi. 3 fur. 17 rods?
- 32. I have five farms; the first contains 29 ac. 133 sq. rods, the second 100 ac. 81 sq. rods, the third 85 ac. 69 sq. rods, the fourth 71 ac. 137 sq. rods, and the fifth 112 ac. 98 sq. rods; how much land do I own?







- 33. If a mountain be $4\frac{7}{8}$ miles high, express its altitude as a fraction of the earth's diameter, which is 7926 miles.
- 34. What length is that of which 25 yards is $\frac{15}{27}$? of which 7 feet is $\frac{21}{100}$?
- 35. What length in seet would require to be added to a telegraph wire, which reaches only $\frac{7}{24}$ of the distance between Toronto and Thornhill to complete the whole distance, 12 miles?
- 36. What part of 2 miles would just measure $\frac{3}{4}$ of 10 rods?
- 37. A block of land is r_1^4 miles square, how many acres would there be in $\frac{1}{r_0}$ of it?

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38. Divide 10¹/₄ square miles of land among 33 persons and give each an equal share; what would each receive?

220. Time is measured by seconds, minutes, hours, days, weeks, months and years, as shown by the following

TABLE OF TIME.

60 seconds (sec.) make 1 minute, min.

60 minutes	4.6	I hour, hr.
24 hours	"	I day, da.
7 days	"	I week, wk.
65 days	" "	I vear. vr.

221. The months of the year are January, February, March, April, May, June, July, August, September, October, November and December.

April, June, September and November have each 30 days, and all the others have 31 days, except February, which has 28 and sometimes 29 days.

Leap Year, and thus has 366 days.

Leap Years are exactly divisible by 4, such as 1860, 1880, 1888.

Ex. How many hours from 12 o'clock, noon, on the 15th of December, to 12 o'clock, midnight, on the 10th of January next?

TABLE OF TIME.

Since December has 31 days, there will be 16 days up to noon, and 12 hours more on the last day of December up to midnight. From this time to January 10th gives 10 days more; in all 16+10, or 26 days. and 12 hours.

 $26 \text{ days} = 26 \times 24 \text{ hours} = 624 \text{ hours}.$ 624 + 12 = 636 hours.

EXERCISE, 52.

The first seven questions to be solved mentally.

- 1. How many minutes in $\frac{1}{2}$ an hour? in $\frac{3}{4}$ of an hour? in 1 of an hour ? in 11 hours? in 4 hours?
- 2. What part of an hour is 30 minutes ? 45 minutes ? 20 minutes? 10 minutes? 15 minutes?
- 3. How many days in 2 wks? in 3² wks? in the two first months of the year? in 2 years? in $\frac{1}{2}$ of a leap
- 4. What part of a week is 3 days? 24 hrs. ? 12 hrs. ? 31 days? 48 hrs.?
- 5. A man can earn \$3 an hour, how much can he earn in a day? in 10 days? in 15 min.? in 1 min.?
- 6. How long from 6 o'clock in the morning to 8 o'clock at night? from midnight to mid-day?
- 7. Which is the cheaper of the following rates:
 - (a) 10c. an hour, or 2 a day, for a cab?
 - (b) \$2 a day or \$14.50 a week?
 - (c) IC. a min. or 50C. an hour?
 - (d) 10c. for 20 min. or 40c. an hour?
 - (e) \$24 for 3 mos. or \$100 a year?
 - (f) \$2 a day or \$62 for the month of April?
- 8. How many seconds in a year? in a leap year? in the month of June? in the month of August? in the month of February, 1880? in a week? in a day? in
- 9. How many minutes in the year 1882? in the year 1884? in the month of July? in September? in the longest month in the year? in the shortest month of

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the year? in the first three months of 1888? in the last three months of the year?

- 10. How many seconds in 5 hrs. 15 min. 12 sec.?
- 11. How many hours, etc., in 38497 sec.?
- 12. How many days from April 1st to Oct. 19th?
- 13. Reduce 27789 min. to weeks, etc.
- 14. What part of a week is 6 days, 12 hrs. and 30 min.?
- 15. Find the difference between $\frac{9}{16}$ of a day and $\frac{4}{5}$ of
- 16. How many days from August 24th, 1883, to August 12th, 1884?
- 17. How many minutes from 18 min. past 9 to 32 min. to 10 in the morning?
- 18. What part of a week is wasted by a boy who is idle for 2 days 10 hours?
- 19. Find the third part of 3 wks. 6 da. 14 hrs. 17 min. 57 sec.
- 20. What part of a day is 1 hr. 52 min. 30 sec. ?
- 21. What must be taken from $\frac{2}{5}$ of 14 da. 9 hrs. to leave half an hour and 8 min.?
- 22. Find the value of $\frac{9}{10}$ of a day $+\frac{7}{2}$ of 1 hr. $-\frac{1}{3}$ of 13 hrs. 2 min. 6 sec.
- 23. From half-past 5 p.m., on the 30th of June, to 20 min. to 11 a.m., on the 5th of September, how much time elapses?
- 24. The true year contains 365 days, 5 hrs., 48 min., $49\frac{7}{10}$ sec.; how many days, etc., in 12 years?
- 25. Express $\frac{8}{13}$ of an hour in terms of a minute, of a day, and of a week.
- 26, What is the period of which 3 hrs. 20 min. is 5 ? of which three days is ??

27. Of what time is 3 min. 10 sec. the seven-fifths?

28. What time would you have to add to 3 hrs. 5 min. 20 sec. so that it would become § of a day? 222

223. 224. 1888? in the

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- 29. How long would it take a man to complete a journey of 20 miles at the rate of 3½ miles an hour? And if he started at 10 a.m., at what time by the clock would he finish it?
- 30. Two men start to walk, the one from Toronto, the other from Newmarket, a distance of 32 miles, at 9 a.m., the one walks at the rate of 3 miles an hour, the other 31 miles an hour; at what time by the clock will they meet?
- 31. A boy studies on Monday 5 hrs. 30 sec., $\frac{3}{4}$ of $\frac{11}{12}$ of a day on Tuesday, $\frac{5}{7}$ of 12 hours on Wednesday, $\frac{2}{3}$ of 10 hrs. 20 min. on Thursday, and $\frac{5}{7}$ of 8 hrs. 10 min. 40 sec. on Friday; how many hours would he study during a school week?
- 32. A girl commenced to read a book of 320 pages on Monday at 9 a.m.; if she read every day for 4 hours at the rate of 5 pages in 20 min.; at what time would she finish it?
- 222. Goods are bought and sold, not only by weight, but are often measured: as, a pint of beans, a gallon of milk, a bushel of potatoes, a hogshead of wine.
- 223. Liquids, such as wine, ale, etc., are measured in a different way from fruits, grain, etc.
- 224. The latter, and such commodities as are taken up in the hand, are measured by the following

TABLE OF DRY MEASURE.

2 pints (pt.)	make	I	quart. ot.
4 quarts	4.4	I	gallon, gal.
2 gallons	* 6	I	peck, pk.
4 pecks	**	I	bushel, bush.

The standard measure in Canada is the "Imperial Gallon," containing 277²⁷/₁₀₀₀ cubic inches.

The law determines the weight of a bushel of different kinds of produce, as follows:

Oats, - · · 34 lbs.	Corn, 56 lbs
Barley, $\cdot \cdot \cdot \cdot \cdot 48$ lbs.	
48 lbs.	Wheat, - 60 lbs.
Duckwheat	D
Timothy Seed, 48 lbs.	Beans, 60 lbs.
Thinking Seed, 48 lbs.	Peas, 60 lbs.
Flax Seed, - 50 lbs.	Ch. 6 00 105.
Ruo	Clover Seed, 60 lbs.
Rye, - 56 lbs.	Polatoes, 60 lbs
5	\bullet oranges, \bullet on the

225. Wine, ale, etc., are measured by the following

TABLE OF LIQUID MEASURE.

4 gills (gi.) make 1 pint, pt.

2 pints " I quart, qt.

4 quarts " I gallon, gal.

A hogshead (hhd.) of wine contains 63 gals. A hogshead of beer or ale "54 gals.

A	Darrel of beer or ale	66	36 gais.
	5		J. 6413.

EXERCISE 53.

The first 8 questions to be solved mentally.

- 1. In a quart of water how many gills? how many half pints?
- 2. If hickory nuts are 20c. a quart, what is the price of a pint? a half-pint? a peck? a quarter of a peck? a half-bushel? three-quarters of a bushel?
- 3 I paid 80c. for a gallon of Fulton & Michie's best vinegar: how much was that a quart? a halfpint? for 6 gills? for half a gallon?
- 4. Bought a bushel of Spanish chestnuts from Cleghorn & Son for \$4; what was the price for half a gallon? for a quart? for 3 bushels? for 4 quarts?
- 5. Bought from Farmer Jones, potatoes at 60c. a bush el; in order to gain 10c. on every peck I sell, what must I charge for a bushel? for $\frac{1}{5}$ of a peck? for a bushel and a quarter? for half a peck?
- 6. What part of a bushel of corn is 3 pks? $\frac{1}{2}$ a gal. lon? 4 gals.? 8 qts.? 8 pints?

2

7. Which is the cheaper of the following prices:

5 lbs. 5 lbs. 5 lbs. 6 lbs. 6 lbs. 1 lbs. 1 lbs.

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 $\frac{1}{2}$ a gal.

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LIQUID MEASURE.

- (a) \$1 a bushel, or 25c. a peck?
- (b) 20c. a qt., or 10c. a pint?
- (c) 5c. a gallon, or 6oc. a bushel?
- (d) \$2 a quart, or 30c. a gill?
- (c) Soc. a peck, or 12c. a gallon?
- 8. At 30c. a gallon, what is the cost of a hogshead of ale? a quart of nuts?
- 9. How many dozen of pint bottles could be filled from 20 barrels of ale ?
- 10. By how much does the number of gals. in 10000 pts. of wine exceed the number of hogsheads in 10000 gallons?
- 11. How many pints of water in 6 gals. 3 qts. 1 pt.?
- 12. How many bushels, etc., of nuts in 1387 qts.?
- 13. How many hogsheads of wine in 6324 gills?
- 14. I bought 4 barrels of spirits, each holding $15\frac{3}{4}$ gallons, at $3\frac{1}{2}$ c. a gill; what can I sell it for, so as to gain \$20?
- 15. How many gallons of cider at 12½c. a gallon can I obtain in exchange for 130 bushels of apples, at 35c. a bushel?
- 16. What is the value of 325 bags of beans, each containing 2 bush. 1 pk., at 70c. a bushel?
- 17. How many loads of apples each containing 27³/₄ bush. at 45c. a bush., can be bought for \$49.95.
- 18. What part of 1 gallon is 2 qts. $1\frac{1}{4}$ pt.?
- 19. If 376 gals. 3 qts. 1 pt. of milk be divided equally among 9 charities, how much will each receive?
- 20. A man bought ⁵⁷/₆ of a bushel of nuts and sold them at ioc. a quart, but only gave 1½ pts. to a quart; how much did he receive?
- 21. A man bought 14 bags of beans, each holding 2 bush. 2 pks., for \$21, and sold them in boxes of 1 bush. 3 pks. each; find the price per box.
- 22. What part of 62 gals. 2 qts. 1 pt. must be taken from a hogshead of wine to leave 42 gals. 1 pt.?

182

- 23. If a vessel is $\frac{2}{8}$ full, and after 70 pints are drawn off, is found to be $\frac{2}{8}$ full, how much did it contain?
- 24. If a barrel of ale is $\frac{9}{10}$ empty, how many quarts are still left in it?
- 25. How many barrels of ale could be filled from a vat containing 1296 gallons? and how many dozen quart bottles would this quantity fill?
- 26. How many bushels of clover seed in 5 loads, each weighing 1 ton 36 lbs.?
- 27. How many bushels of oats would weigh as much as 560 bushels of corn ?
- 28. How many bushels of oats would a horse eat in 1 year, if fed three times a day, and given 5 quarts at each meal?
- 29. What part of a bushel of potatoes would weigh as much as $\frac{2}{3}$ of a bushel of buckwheat ?
- 30. How many barrels of flour of 196 lbs. could be made from 1000 bushels of wheat, if it takes 3 lbs. of wheat to make 2 lbs. of flour?

226. Many articles of merchandise are bought and sold by special names, the most important of which compose the following

GENERAL TABLE.

1 dozen (doz.) 1 score	= 12 articles. = 20 "
I quire	
I ream	= 24 sheets.
I gross	= 20 quires.
I great gross	= 12 dozen.
I stone	= 12 gross.
I brl. of flour	= 14 pounds.
I " port out	=196 "
I "pork or bee	t = 200 "

EXERCISE 54.

The following questions should be solved mentally: 6

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11.

12.

re drawn off, ontain ?

y quarts are

d from a vat nany dozen

loads, each

as much as

eat in 1 5 quarts

weigh as

d be made s 3 lbs. of

d sold by compose

I men-

GENERAL TABLE.

1. How many articles in 3 dozen? in $5\frac{1}{2}$ dozen? in 2 score? in I score and 3 dozen? in 3 score and ten? in $6\frac{3}{4}$ dozen? in one-half a score? in $\frac{1}{3}$ of a dozen $+\frac{1}{5}$ of a score? in 5 more than $1\frac{1}{4}$ dozen?

- 2. At 6oc. a dozen, what is the cost of half a dozen oranges? of 2 score apples? of 5 peaches? of half a score of lemons? of a gross of pens at 5c. a doz.?
- 3. What part of a score is a dozen?
- 4. If foolscap paper costs ic. a sheet, what must I pay for a quire? for 21 dozen sheets? for a ream? for 8 sheets more than half a quire? for 2 quires less 11 sheets? for $\frac{1}{4}$ of a ream?

5. Which is the cheaper of the following prices :----

12c. a dozen, or 20c. a score ? 3c. a piece, or 3oc. a dozen? 50c. a quire, or 2c. a sheet ? a dozen for 30c., or 80c. a score? $1\frac{1}{2}$ c. each, or 20c. a dozen? 2 score for a shilling, or $\frac{1}{2}$ shilling a score?

- 6. A bought eggs for 30c. a dozen, how much per dozen must he sell them for to gain 1c. apiece? to gain 15c. a dozen? to lose 1c. each? to gain 20c. a score? to lose 10c. a score?
- 7. How many score of sheep in 5 flocks, each contain-
- 8. How many boxes, each containing 1 gross, are there in nine million pens?
- 9. What would 120 gross of spools cost at 50c. a
- 10. How many barrels in 1120 stones of flour; and what would the whole cost at \$3 per cwt.?
- 11. From 60 reams of paper, how many books of 400 pages each could be made, if one sheet is folded
- 12. How many stones of flour will weigh as much as 21 barrels of pork?

- 13. How many barrels of beef can be packed from 20 carcases, each weighing 1150 pounds, and what would the whole cost at \$16.50 per barrel?
- 14. What part of a stone would weigh as much as $\frac{1}{38}$ of
- 15. If 10 eggs weigh a pound, how many dozen would weigh as much as a hog, that would make 21 barrels
- 16. Three-fourths of a ream is what part of 10 quires?
- of a book containing 800 pages? of 450 sheets? 17. A grocer in packing 6 dozen dozen eggs, broke half a dozen dozen, and sold the remainder at 20 cents
- a dozen. How much did he receive for the eggs? 18. How many reams of paper will print an edition of 2500 copies of the Royal Canadian Reader No. 4. each copy containing 384 pages, if one sheet make
- 19. What is the cost of a great gross of steel pens, at 61
- 20. At \$22.86 per ream, what will 9 reams, 6 quires, 12
- 21. How large an edition of an Elementary Arithmetic
 - can be printed from 99 reams of paper, allowing
- 22. How many dozen cabbages can be planted 2 feet apart, in a garden containing 132 rows two feet wide, and 20 rods long, and what would they be worth, when brought to market at 40 cents per dozen ? How many acres are there in the garden?

230

229

2

 $\mathbf{2}$

acked from 20 nds, and what parrel?

much as 1 of

dozen would ake 21 barrels

of 10 quires? o sheets ?

s, broke half r at 20 cents r the eggs?

in edition of eader No. 4. sheet make

l pens, at 61

6 quires, 12

Arithmetic r, allowing

ted 2 feet two feet I they be cents per garden?

CHAPTER V.

DECIMALS.

227. In the previous system of notation, we have seen that the figures increase ten fold from right to left. That is, decrease tenfold from left to right. This can be carried out in the same manner to the right of the

228. In the number 843'5'267, if we call the 5 units, the values to its left increase, and those to its right decrease tenfold for each place.

Thus, 5 means 5 units.

13 means 3 tens of units.

2 means 2 tenths of a unit.

14 means 4 hundreds of units.

6 means 6 hundredths of a unit.

8 means 8 thousands of units.

7 means 7 thousandths of a unit.

And so on for any number.

229. The part 267 is called a decimal, and we shall see that it may be expressed as a fraction, for

$$^{207} = \frac{2}{10} + \frac{2}{100} + \frac{2}{1000} = \frac{200 + 60 + 7}{1000} = \frac{267}{1000}$$

230. The expression 8435.267 will be read :- 8 thousand 4 hundred and thirty-five, decimal two six seven, (not decimal two hundred and sixty-seven.)

It may also be read :--- 8 thousand, four hundred and thirty-five, and two hundred and sixty-seven thousandths. The pupil should be well exercised in writing decimals rapidly, when they are read in the latter

231. The dot (:) on the right of the units' figure in Art. 228 is called the Decimal Point, and marks the beginning of the decimal part, and the dot on the left is not written in practice.

232. Hence any decimal can be written in a fractional form by using the figures of the decimal for the numerator, and writing for the denominator, 1, followed by as many ciphers as there are places in the decimal.

Ex. 1. $\cdot 02605 = \frac{3605}{1000000}$ $E_{x. 2. 12.006} = 12\frac{6}{1000}$

233. For the same reason, we can express the fractional form in a decimal form, by using the numerator for the decimal part and counting off from the right as many places as there are ciphers in the denominator, supplying ciphers to the left, if

$$Ex. 3. - \frac{509}{10000} = 0502.$$

$$Ex. 4. - \frac{7.013}{1003} = 7502.$$

234. All examples given in the decimal form may, therefore, be worked by Vulgar Fractions, but Addition and Subtraction may also be performed just like whole numbers, care being taken, as before, that only like orders are added together, or subtracted from one another.

235

Ex. 5. Find the sum of 4.02, 0075, 16.31, and 41.032. $4.02 = 4\frac{1}{100}; 0075 = \frac{75}{10000}$ $16.31 = 16\frac{31}{100}; 41.032 = 41\frac{33}{1000}$ 4+16+41=61 $\frac{1}{100} + \frac{1}{10000} + \frac{3}{100} + \frac{3}{1000} =$ 200+75+3100+320 ____3695 10000 ='3695. 10000

Hence the sum is 61.3695. This may also be worked thus :----

4'02 .0075 16.31 41.032 61.3695

e in Art. 228 the beginthe left is

onal form by merator, and many ciphers

al form in a lecimal part as there are to the left, if

therefore, tion and ke whole only like rom one

41'032.

DECIMALS.

Ex. 6.—Find the difference between $2\tau \frac{1}{1000}$ and 40'935.

 $21\frac{1}{1000} = 21.007$

40.935 21.007 19.928

This may also be worked thus :---

 $40.935 - 21\frac{7}{1000} = 40\frac{9.3}{1000} - 21\frac{7}{1000} = 19\frac{9.38}{1000}.$ Ex. 7.—Multiply .037 by .042.

 $\begin{array}{c} `037 = \frac{1}{1000} ; : 042 = \frac{1}{1000} ; \\ \hline 1000 \times \frac{1}{1000} \times \frac{1}{1000} = \frac{1}{1000000} = 001554. \end{array}$ This may also be worked thus :--



°001554

235. From this we see that we multiply as if they were whole numbers, and then mark off from the right of the product as many decimal places as there are in the multiplier and multiplicand together, supplying ciphers to the left, when necessary.

Ex. 8.-Multiply 31.25 by .0196.

3 1.25
18750 28125
3125
612500

decimal have no value, and may be struck off, leaving .6125.

Ex. 9.-Divide .0296 by .08.

 $\begin{array}{c} \cdot 0296 = \frac{3}{100} \frac{3}{000}; \ \cdot 08 = \frac{8}{100}, \\ \frac{3}{100} \frac{9}{000} \frac{3}{100} + \frac{3}{100} \frac{9}{100} + \frac{3}{100} \frac{9}{100} \times \frac{3}{100} = \frac{3}{100} = \cdot37, \\ \mathbf{K} \qquad \mathbf{P}_{\text{ROOF}}: \ \cdot 08 \times \cdot 37 = \frac{8}{100} \times \frac{3}{100} = \frac{3}{1000} = \frac{3}{10000} = \cdot0296. \end{array}$

This Example may also be worked thus:



Now, since there are four places of decimals in the dividend, two in the divisor and two in the quotient, we see that the number of places in the quotient can always be found by taking the number of places in the divisor from the number of places in the dividend and marking off this difference as the number of places in the quotient.

We also notice that 37 is obtained by dividing 8 into 296, just as if they were whole numbers.

236. From this we obtain the following

RULE FOR DIVISION OF DECIMALS.

Divide the numbers as if they were whole numbers, and mark off from the right of the quotient, the number of places there are in the dividend more than in the divisor, prefixing ciphers to the left, if necessary.

Since a decimal is not affected in value by adding ciphers to the right, we can thus always make the dividend have more places than the divisor. Ex. 10.—Divide 52.3 by 125. The dividend may be written 52.3000.

$ \begin{array}{r} 125)523000(4184) \\ \underline{500} \\ 230 \\ \underline{125} \\ 1050 \end{array} $	In the divisor, 125, we have 3 places; in the dividend 52'3000, we have 4 places; hence in the quotient we must have
1000	must have I place, which gives 418.4.
500 500	$P_{\text{ROOF}} := 418.4 \times .125 = 52.30000 = 52.30000 = 52.3000 = 52.3000 = 52.3000 = 52.3000 = 52.3000 = 52.3000 = 52.3000 = 52.3000 = 52.3000 = 52.3000 = 52.3000 = 52.3000 = 52.3000 = 52.3000 = 52.30000 = 52.30000 = 52.30000 = 52.300000 = 52.30000 = 52.30000 = 52.30000 = 52.30000 = 52.30000 = 52.30000 = 52.30000000 = 52.3000000 = 52.3000000000000000000000000000000000000$

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237. In many cases the division will be very long, and very often will not terminate, and it is then required to find

DIVISION OF DECIMALS.

Ex. 11.—Find the quotient to four places of decimals when 2.51 is divided by '109.

109)25100000(230275	
218	Now, there are 3 places of deci-
330	mais in the divisor and since
327	we are to have a places of
300	accinate in the motient there
218	must be 7 places in the dim
820	
763	operation will be performed
570	as one will dill the duotiont
545	will be 23.0275.
3+5	

EXERCISE 55.

The pupil should prove the results in each question.

(a.) Express as ordinary fractions in their simplest form :--

 1. '495; '0075; 12'8; 68'1875.

 2. '375; '225; '0068; '3125.

 3. '95; '875; '4375; 8'275.

(b.) 1. The distance from A to B is 42.3 chains, from B to C is 13.06 ch., from C to D is 8.049 ch., from C to D is 1.6 ch., from D to E is .037 ch. How far from A to E?

2. A man had 1000 acres of land, and sold 450.625 acres; how many acres has he left?

- 3. From '00038 take 36 ten-millionths.
- 4. What must be taken from 34.634 acres to leave
- 5. To how many pounds of chicory must 23.859 pounds of coffee be added to produce a mixture of 29.796 pounds?
- 7. What is the sum of 18 thousandths, 15 millionths, 81 hundredths, 146 ten-thousandths, 834 hundredthousandths?

nals in the e quotient, uotient can f places in n the divithe number

ling 8 into

LS.

and mark blaces there prefixing

y adding lake the

have 3 ividend places; ent we which

125 =

d very to find s:—

- 8. What is the cost of 34.5 yds of cloth, at \$3.15 per
- 9. Since 16.5 feet make a rod, how many feet are
- 10. The product of two numbers is 0048; one is 06:

11. Divide

.04905 by 327. 135.05 by .037. 71.142 by '0071.

150.75 by 30.25. 300.402 by 12.1. 4.00334 by 6.31.

13. Find the quotients each to five places of decimals.

·3412 + 8·4736. ·004134 + ·3243. ·00079085 + ·83497.

238. We have seen that any decimal may be expressed as a vulgar fraction; we will now reduce a vulgar fraction to its equivalent decimal.

- The fraction $\frac{3}{6}$ is equal to $\frac{6}{10}$, which may be written $\cdot 6$.
- The former might have been obtained by dividing 30

6)<u>3</u>.0

and the latter by dividing 1.00 by 25, thus:-

239. Hence we see that, while such fractions as $\frac{1}{2}$, $\frac{1}{$ etc., may be known by inspection to be .5, .25, .2, etc., any fraction may be reduced to a decimal by simply dividing the numerator by the denominator.

240

DIVISION OF DECIMALS. **Ex. 1.**—Express $\frac{5}{16}$ as a decimal.

at \$3.15 per any feet are

one is of:

decimals.

pressed as ulgar frac-

written ·6.

viding 3.0

 $\frac{1}{2}, \frac{1}{2}, \frac{1}{3}, \frac$ inator.

	- Dxpress	Te as a decimal.
	16)5.0000(.315	
	48	filler, the value of the number
	20	ator is not altered by adding ciphers to the right of the de- cimal point
	16	cimal point.
	. 40	
	32	It will then be seen that the po- sition of the decimal point is
	80 80	found as in ordinary division
	Ex. 2. What dec	cimal of a pound is the same as $\frac{3}{32}$ of
	a pound ?	
	4) <u>3.0000</u> 8) <u>7500</u>	Here the division is carried on by means of the factors of an it by
	8) 7500	means of the factors of 32, that is:
	* 09375	4 and 8. Therefore, $\frac{3}{32}$ of a pound is the same as $\frac{1}{322}$ of a pound is
	The previous result	the same as 09375 of a pound is lts may be proved thus;—
	1210	- she
	·U937	$5 = \frac{5 \cdot 1 \cdot 2 \cdot 5}{1 \cdot 0 \cdot 0 \cdot 0} = \frac{5}{1 \cdot 6}.$ $5 = \frac{9 \cdot 3 \cdot 1 \cdot 5}{1 \cdot 0 \cdot 0 \cdot 0 \cdot 0} = \frac{3}{3 \cdot 2}.$
240.	The nave seen in A	rt opp that t
	sion will not terr	rt. 237 that, in many cases, the divi- minate, in other words, there will no matter how for words.
	be a remainder, i	no matter how for words, there will
	J. Hounde 49	to a decimal
	43/20 000/022	a dominar.
	0.00	Here the remaindance
		Iere the remainder, 10, is contin- ually repeated; then we see that the figure 2 in the area of the figure 2 in the second secon
	90	
	100	
	90	being written .62.
	IO Fr d Francisco	
	Ex. 4.—Express $\frac{103}{168}$	as a decimal.
1	65)103.000(.624	

	being written .62.
10	
Ex. 4Express	103 1 .
1	tes as a decimal.
165)103.000(.624	
990 400 330 700 660 400	The remainder, 40, repeats, and therefore the figures in the quotient from the 2 will re- peat, and the quotient is written in the form .624.

- 241. Such expressions are called Circulating Decimals, or Repeating Decimals, from the fact that one or more figures in them circulate or repeat.
 - The result of Ex. 1 would, if carried out, be written .62222, etc., and in Ex. 2 the quotient would be written .6242424, etc.
 - The dots are placed over the figure or figures that repeat. Thus:

244

1:

(1

I,

б.

2.

3.

4. 5. 6.

(i) 1.

·0572 means ·057205720572, etc.

•62947 means •62947947947, etc.

242. Decimals like 0572, where all the figures after the point repeat. are called Pure Circulating Decimals.

Decimals, like .62947, where some of the figures after the point do not repeat, are called Mixed Circulating Decimals.

243. These decimals are reduced to vulgar fractions by the following

RULE.

If the decimal is a Pure Circulating Decimal, place the repeating part of the decimal for the numerator, and for the denominator as many nines as there are figures in the repeating part.

If a Mixed Circulating Decimal, subtract the part that does not repeat from the whole decimal, place the difference for the numerator, and for the denominator as many nines as there are figures in the repeating part, followed by as many ciphers as there are figures that do not repect in the decimal.

Ex. 1.--- $037 = \frac{37}{9000}$.

Ex. 2.—'037= $\frac{34}{900}$.

Subtracting 3 from 37 leaves 34, which is placed as numerator.

Ex. 3. -5.892.5892 - 58 = 5834.

ecimals, or one or more

ut, be writt would be

res that re-

after the ng Deci-

ures after d Circu-

tions by

ce the red for the n the re-

that does rence for nines as as many decimal.

ced as

DIVISION OF DECIMALS.

Thus, the required fraction will be

6434 Or 5884.

These results may be proved by dividing the numerator by the denominator

244. All examples on Circulating Decimals are worked by reducing the decimals to fractions. The operations are then performed as in fractions, and the result thus obtained expressed as a decimal.

Ex. 1.-2.740 × 243 = $\frac{2736}{600} \times \frac{243}{5000} = \frac{2}{3} = 6$. $Ex. 2. - 22 + 13 = \frac{29}{66} \times \frac{90}{18} = \frac{10}{6} = 1.6$

EXERCISE 56.

(a) Express the following fractions as decimals :----

7. 197. 85-	$3 \cdot \frac{1}{20}$.	4. 12.	51.4	5		
128	9. 24 -	10 31				
	J. 333.	10. 5	17. 103	.0		
lowest terms	tollowing :	decimals	as fraction	s in their		
1. 7205. 2. 6. 0160 7 10	•72. 3.	·i35. 4.	*	lon-ć'		
60169. 72	045. 8.	1045. 0	-93. 3.	23503.		
) DV '3.			. '00006.		
2. Find the prod	uct of star	162 and .				
3. Divide 082 by	· ·Ġ.					
4. Find the quotient of 31.791 divided by 3.973.						
5. Divide hart the the standard by 3.973.						

5. Divide 297 into 2.297.

r. B.

(*i*)

6. The product of two decimals is $1\frac{4}{6}$; one of them is 245, find the other,

CHAPTER VI.

PERCENTAGE.

- 245. The word Percentage occurs so often in ordinary business affairs, that everyone should know its meaning.
 - If a man has 100 gallons of vinegar, and loses 20 gallons, he is said to have lost 20 per cent. If a man has 100 dollars, and by trading, increases it to 140 dollars, he is said to have gained 40 per cent.

24

246. The term **Per Cent**. thus means per hundred, and is only a short way of writing **per centum** (per hundred.)

We see that 20 per cent. means 20 on every hundred; therefore, 20 per cent of anything, is the same as $\frac{20}{100}$, or $\frac{1}{5}$ of it.

Thus:--80 per cent. of 150 pounds of sugar is the same as $\frac{80}{100}$ of 150, or $\frac{4}{5}$ of 150, which equals 120 pounds.

The expression % stands for per cent.; thus, 5% means 5 per cent., or $\frac{1}{20}$.

Ex. 1. What is 8% of 150 pounds?

$$8\% = \frac{8}{100} = \frac{2}{25}$$

 $\frac{2}{25}$ of 150 lbs. = 12 pounds.

Ex. 2. What is 120% of 80 yards?

$$120\% = \frac{1200}{100} = \frac{6}{5}$$
.
 $\frac{6}{5}$ of 80 yards = 96 yards.

Ex. 3. A man lost 8 horses out of a purchase of 400; what did he lose %?

Here we are to find what he lost on 100 horses, if he lost 8 on 400.

[191]

PERCENTAGE.

400 gave a loss of 8, therefore 100 gave a loss of 2. That is, he lost 2 per cent.

PROOF: $2\% = \frac{2}{100} = \frac{1}{50}$, and $\frac{1}{50}$ of 400 = 8.

That is 8 horses lost.

Ex. 4. A man had a flock of 800 sheep, and lost 60%of them by disease; how many sheep were left?

Since he lost 60%, he must have (100% - 60%) or 40%

$$40\% = \frac{40}{100} = \frac{8}{5}$$
.
 $\frac{8}{5}$ of $800 = 320$ sheep.

Compare this with Ex. 5, page 145.

247. The expressions on and off occur in a peculiar sense in percentage.

A merchant selling his goods (bought in England) at 60% on would sell them for 60% or $\frac{3}{2}$ more than their total cost price. Thus 60% on cost, means $\frac{3}{2}$ more than cost, or § of the cost.

Hence 20% on 60c. a yard is \$ of 60c., or 72c. a yard. 40% on 10d. a pound is \$ of 10d., or 14d. a pound.

Again, a farmer selling a plough at 20% off the cost would just receive 80%, or ‡ of the cost.

Hence 15% off \$40, would leave 85% or $\frac{1}{25}$ of \$40, that is \$34, making a loss of \$6.

30 % off 80 bushels would be 70% or $\frac{1}{10}$ of 80 bushels, which is 56 bushels.

EXERCISE 57.

The first 12 questions should be solved mentally.

1. Express the following percentages in their simplest

	1%. 17½%. 45%.	2%. 20%. 150%.	4%. 25%. 90%.	5%. 3°%. 75%.	10%. 33 $\frac{1}{3}$ %. 66 $\frac{2}{3}$ %.	12 <u>1</u> %. 35%	15%. 40%.
2.	What [•]	% of a	mania		is <u>3</u> of 7 7?		180%.

dinary busi. ts meaning. oses 20 gal-If a man s it to 140 cent.

red, and is (per hun-

every hunng, is the

gar is the equals 120

thus, 5%

e of 400;

ses, if he

- 3. What is the difference between 30% of my farm and 3 of it? 3% of a lot and 60% of it? 50% of \$800 and 40% of \$800? 3 of 80 pks. and 80% of 80 pks? 15% of 200 acres and 1 of 200 acres?
- 4. A man owned 60% of a farm of 640 acres and sold $\frac{1}{2}$ of it; how many acres had he left?
- 5. A merchant makes \$60 on \$200; what is his gain %?
- 6. A had \$600; at the end of the year he has \$900; what did he gain %?
- 7. What is gained per cent., if ³/₄ of a farm is sold for what ²/₄ of it cost?
- 8. What is the gain %, when goods are sold so that of what they all cost is received for half the goods?
- 9. Sold ⁴/₅ of a hhd. of molasses for what the whole cost me; what was my gain per cent.?
- 10. What per cent. is gained by buying oil at 30 cents a gallon, and selling it at 12 cents a pint?
- 11. A's money is 50% more than B's; how much per cent less is B's than A's?
- 12. If I sell $\frac{3}{8}$ of an acre of land for what $\frac{3}{8}$ of it cost, what per cent. do I lose?
- 13. What is 65% on \$145? 40% off \$560?
- 14. What is $12\frac{1}{2}$ % on $\frac{7}{4}$ of a shilling? 25% of $\frac{1}{16}$ of a gallon? 20% off $\frac{1}{16}$ of a yard? 180% on $\frac{3}{47}$ of a dollar?
- 15. What % on \$9 is \$12? \$18? \$13.50?
- 16. A merchant gains 25%; what is the gain in a sale of £250 10s. 5d., and what is the cost price ?
- 17. A merchant loses 12½%; what is the loss in a sale of \$721.70, and what was the cost price?
- 18. What per cent. more than $\frac{5}{9}$ is $\frac{5}{6}$?
- 19. What per cent. less than $\frac{20}{27}$ is $\frac{8}{15}$?
- 20. One-fifth is what per cent. of three-fourths?

PENCENTAGE.

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sale of

- 21. Having used my wagon three years, I sold it for \$66, which was 40% less than the cost; what was the cost?
- 22. If 331% of what is received for goods is gain, what is the gain per cent.?
- 23. Sold 1 of a section of land in Manitoba for what 1 of 5 sections cost; what per cent. was gained on the part sold?
- 24. A man bought $\frac{3}{5}$ of a coal mine, and sold $\frac{4}{5}$ of his share for \$11,700, which was 30% above the cost; what was the cost of the mine?
- 25. The population of a town of 18000 inhabitants increases 5% every year; what will be the number of inhabitants at the end of 2 years?
- 26. A man gains 17¹/₂ per cent. on tea; if he sold 400 lbs. and gained \$42, what did it cost him a pound?
- 27. A and B each sold 240 acres of land, A gaining $7\frac{1}{2}$ % and B losing $12\frac{1}{2}$ %; if A received \$960 more than B, what did they pay an acre for the land?
- 28. A man bought a farm of 160 acres at \$32 per acre; he paid \$200 for fencing, \$150 for repairing buildings, and \$18 for improving the grounds; at what price per acre must it be sold to gain 25% on the entire cost?
- 29. A farmer raised 20% more wool this year than last; the amount raised during the two years was 1320 lbs.; what amount of wool was raised each year?
- 30. A man dying, left 33[±]/₈% of his property to his wife, 50% of the remainder to his son, 75% of the residue to his daughter, and the balance, \$120, to his servant; how much did each receive?

CHAPTER VII.

PRACTICAL PROBLEMS IN MEASUREMENTS.

248. The pupil should now be able to work the more difficult of those problems requiring a knowledge of Long, Square, and Cubic Measures.

249. The following suggestions, together with those given in Arts. 214, 215, 219, will be found useful in working

1. When measures are given in different denominations, they should be expressed in the the highest, instead of being reduced to the lowest, thus :

5 yds. 2. ft. 3 in. $= 5\frac{3}{4}$ yds. $8 \text{ sq. ft. } 72 \text{ sq. in.} = 8\frac{1}{2} \text{ sq. ft.}$

 $5 \operatorname{cu. yds.} 9 \operatorname{cu. ft.} = 5\frac{1}{3} \operatorname{cu. yds.}$ 2. Two measures of length when multiplied together give square measure, hence any square measure divided by a long measure must produce a long meas-

Since 8 ft. \times 5 ft. = 40 sq. ft. then 40 sq. ft. \div 5 ft. = 8 ft. or 40 sq. ft. $\div 8$ ft. = 5 ft.

3. Three measures of length when multiplied together, or a square measure multiplied by a long measure give a cubic measure. Hence a cubic measure when divided by a long measure gives a square measure, or a cubic measure divided by a square measure gives a long measure, thus:

Since $12 \text{ in.} \times 5 \text{ in.} \times 3 \text{ in.} = 130 \text{ cu. in.}$ or 60 sq. in. \times 3 in. = 180 cu. in. Then 180 cu. in. \div 3 in. = 60 sq. in. or 180 cu. in. \div 60 sq. in. = 3 in.

4. In papering a room the area of the paper must be the same as that of the four walls, and its length can be found by dividing this area by the width of the paper, or its width can be found by dividing this area by the length of the paper.

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- 5. The area of the four walls can be easily found by multiplying the length round the room by its height.
- 6. In painting a surface, if the part not requiring paint be \$, the part to be painted must be the remaining \$.
- 250. A few examples will show these more clearly.
 - S The numbers in brackets refer to the previous suggestions.
 - Ex. 1.—A room is 14 ft. 11 in. long, 10 ft. 7 in. wide, and 9 ft. 4 in. high: how many square feet are there in the walls?
 - 14 ft. 11 in. + 10 ft. 7 in. = 25 ft. 6 in. = $25\frac{1}{2}$ ft. = length of the two adjacent walls; $25\frac{1}{2} \times 2 = 51$ ft. = length of the four walls;
 - 51 ft. \times 9 ft. 4 in. = 51 $\times \frac{28}{3}$ = 476 sq. ft. (5).

Ex. 2.—Find the cost of painting the walls in the preceding example at 42%. a square yard.

 $\begin{array}{l} 476 \div 9 = \frac{47}{9} = \mathrm{sq. yds. in the walls}; \ 42\% \mathrm{c.} = \$^3_7; \\ \frac{47}{9} \times \$^3_7 = \$^6 \frac{3}{3} = \$22\frac{3}{3}. \end{array}$

- Ex. 3.—Find the cost of papering a room 40 ft. 7 in. long, 20 ft. 8 in. wide, and 121 feet high, with paper $\frac{7}{5}$ yd. wide, and 18c. a yard, if the windows, doors, etc., take up $\frac{1}{5}$ of the walls?
 - 40 ft. 7 in. + 20 ft. 8 in. = $61\frac{1}{4}$ ft. (1);
 - $61\frac{1}{4} \times 2 = \frac{245}{2} = \text{length round the room};$
 - $\frac{24n}{2} \times 12\frac{1}{7} = \frac{24n}{2} \times \frac{65}{7} = \text{number of sq. ft. in the walls (5).}$

⁶ Since $\frac{1}{5}$ of the surface does not require papering, we take $\frac{4}{5}$ of it (6);

- Then $\frac{245}{2} \times \frac{85}{7} \times \frac{4}{5} =$ sq. ft. to be papered, and $\frac{245}{2} \times \frac{85}{7} \times \frac{4}{5} \times \frac{1}{9} =$ sq. yds. of paper required.
- Now to find the length of the paper we divide its area by its width (4).
- Thus $\frac{254}{2} \times \frac{85}{7} \times \frac{4}{5} \times \frac{1}{9} \times \frac{8}{7} = \text{length of paper re-quired.}$

To find its value, multiply its length by the price per yard.

 $\frac{245}{2} \times \frac{85}{7} \times \frac{4}{5} \times \frac{1}{9} \times \frac{8}{7} \times 18c. = \$27.20.$

ARITUMETIC FOR BEGINN ERS.

It will be noticed that the different steps are kept in a fractional form until the end, and then simplifiel, far by this means we can by cancelling save

Ex. 4.—A piece of timber with its end 18 inches square contains 5 cu. yds. : find its value when sold at 40c. per foot in length.

18 in. $=\frac{1}{2}$ yd.; $\frac{1}{2} \times \frac{1}{2} = \frac{1}{4}$ yd. = area of the end. Therefore the length must be $5 \div \frac{1}{2} = 20$ yards (3); and 20 yds. = 60 ft., hence 40c. \times 60 = \$24.

EXERCISE 58.

- 1. Find the length of a table 6 ft. 11 in. wide, and containing 62 sq. ft. 36 sq. in.
- 2. Find the length of a room 13 ft. broad, the carpeting of which at 4s. 6d. per sq. yard costs £4 19s. 8d.
- 3. A block of ice is 45 in. long, 52 in. broad, and contains 161 cubic feet : find its thickness.
- 4. The papering of a room with paper 30 in. wide at 15c. a yard costs \$10.80: how many square yards in the walls, and if the length be 16 ft. and the breadth
- 5. The cost of painting the walls of a room at 12c. a sq. foot is \$110.17: the height is 11 ft. 6 in., and the breadth 15 ft. 8 in., find the length.
- 6. A path 4 yds. wide around the outside of a garden 85 yds, long and 168 feet broad, is to be paved at 14c. a sq. yd. : find the cost.
- 7. It takes 136° yds. of paper for a room 9 yds. 5 in. long, 14 ft. 7 in. broad, and 4 yds. 10 in. high: how many inches wide is the paper ?
- 8. Find the height of a room 20 ft. by 15 ft., the papering of which at 15c. a sq. yd. costs \$14.00.
- 9. A roof is 50 f long by 10 ft, wide, find the cost of covering it w. is slate 10 in. by 45 in., if the slates are worth \$6 por bousand.

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CHAPTER VIII.

BILLS OR ACCOUNTS.

251. When goods, etc., are sold by one person to another, a Bill or Account is made out by the seller, and sent with the goods to the buyer, to enable him to see the exact cost of the goods bought.

252. If a firm in England sells a quantity of carpetings to a firm in Toronto, the Bill would be sent as follows:

KIDDERMINSTER, Oct. 20, 1881.

Messes. JNO. MACDONALD & CO., Toronto,

1881.

Bo't of Edward Hughes & Sons.

		1									. 50	NS.
Sept.	5	420 600	yds	. Aubusso	n A	xmins	ster @	5/6		£ 115	s. 10	<i>d</i> .
Sept.		1		Brussels, "	5 1	Fram "		1 1		105	0	0
Oct.	1			Tapestry,			B. "			130	ο	0
				1				2/1		22	18	4
DED	T								1	2373	8	4

253. In practice, many short methods are used for calculating the amount of a Bill, and should be carefully remembered and applied as often as possible by the pupil. For example :

Since $\frac{3}{4}$ of a lb. costs as much as 1 lb. all but $\frac{1}{4}$, therefore $\frac{3}{4}$ of a lb. @ 80c. = 80c. - 20c. = 60c.

Also, $\frac{7}{8}$ of a yd. @ \$1.60 = \$1.60 - 20c. = \$1.40.

Again, since $33\frac{1}{3}c. = \frac{1}{3}$ of $\$_1$,

24 yds. @ $33\frac{1}{3}$ c. would be $\frac{1}{3}$ of the cost of 24 yds. @ \$1, that is \$8.

Since 8oc. = $\frac{4}{5}$ of $\frac{5}{7}$,

75 lbs. @ 8oc. would cost # of \$75, that is \$75-\$15 = \$60.

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A UPIMSPIC FOR BESINNERS.

The mental exercises in Ex. 50, 51, 52, 53 and 54, will be of great assistance in working this class of problems with rapidity.

EXERCISE 59.

Make out, date, and find the amount of each of the

1. Rice Lewis & Sons, Toronto, sold to Adam & Co., Hamilton: 47 bales Wire @ \$1.99; 220 kegs Nails @ \$2.95; 270 boxes Glass @ \$1.663; 40 kegs Spikes @ \$5.871; 315 boxes Tin Plates @ \$4.20.

- 2. Virginia Tobacco Company, Toronto, sells Simpson, Stuart & Co., Hamilton : 50 caddies " Twin Navy," 191 lbs. each, @ 30c. per lb.; 25 butts "Dark Sweet," 52 fbs. each, @ $16\frac{1}{2}c.$; 20 boxes "Dark Sweet," 105 fbs. each, at 16c.
- 3. T. H. Barraclough, Ingersoll, bought of J. D. King & Co., Toronto : 12 pairs French Kid Boots @ \$4.25; 24 pairs Misses' Tie Shoes at \$1.75; 24 pairs Boys' Shoes @ \$1.75 ; 12 pairs Men's Knee Boots @ \$4.50.
- 4. J. S. Robertson & Bros., Whitby, buy of Canada Publishing Co., Toronto : 12000 Envelopes @ \$2.871 per M; 375 Pass-Books @ 6c.; 29 doz. Slates @ \$2.40; 64 doz. Lead Pencils @ 371c.; 18 doz. Maps (assorted) @ \$27.75.

5. Geo. Lewis sold to Capt. McMaster: 25 lbs. Sugar @ 9c.; 40 lbs. Maple Sugar @ 183c.; 6 lbs. Cheese @ 121c.; 8 lbs. Butter @ 23c.; 4 lbs. Raisins at 15c.; 2 lbs. Cream Tartar @ 45c.

6. Chas. Pollock, Toronto, sells to W. Brown, Barrie: 281 yds. Silk @ \$2.60 per yd.; 473 yds. Lace @ \$14 per yd.; 287 yds. Velvet @ \$2.80 per yd.; 161 doz. Silk Spools @ 6oc. per doz.

7. P. B. Ball & Co., Toronto, sell to Clinton E. Brush & Bro., Toronto: 500 doz. Knitted Squares @ \$9.35 per doz.; 2053 doz. Kid Gloves @ \$11.60 per doz.; 406 doz. Child's Hose @ \$2.25 per doz.; 100 Men's

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2, 53 and 54, this class of

EXAMINATION PAPERS.

The following papers are similar to those given at the examination for entrance to High Schools and Collegiate

PAPER I.

Ex. 1.—Divide \$80 between A and B, so as to give A

Suppose A to receive his extra \$30 first, then the remainder \$50, must be twice the amount each receives after this, that is \$25 apiece. Thus B receives \$25.

A "

\$25+\$30=\$55.

- 1. Define Greatest Common Divisor, Improper Fraction,
- 2. Express $\frac{7}{11}$ of $\frac{1.9}{14}$ of $\frac{9.9}{30}$ as a fraction having 75 for its
- 3. A house is worth \$576, which is just \$156 more than \$ of 21 times the value of a barn : find the value of the barn.
- 4. A man sells 105 lbs. of sugar at the rate of 8 lbs. for \$1, and gains 17c. : find the cost of .ie sugar per lb.
- 5. What is the greatest number that will exactly divide each of the numbers 1190, 408, 4012, and 1445?
- 6. I sold a farm for 25 % more than it cost me to A, who sold it to B for \$1000, which was 333 % less than it cost him: what did it cost me?
- 7. Reduce the fraction $\frac{321771}{860420}$ to its lowest terms. 8. The sixth part of a farm exceeds its eighth part by 20 acres less than its ninth part : how many acres in the
- 9. Two men had \$7583 divided between them; the difference between their shares was \$461 : what did each get?
- 10. A room is 67 ft. long, 11 ft. 2 in. high, 38% ft. wide; the doors and windows take up $\frac{1}{10}$ of the area of the walls and ceiling: find the cost of painting the remainder at 18c. per sq. yd.

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lam & Co., 220 kegs 3; 40 kegs \$4.20.

Simpson, in Navy," ts "Dark es "Dark

D. King @ \$4.25; irs Boys' @ \$4.50. Canada 3 \$2.871

lates @ z. Maps

. Sugar Cheese at 15c.;

Barrie: @\$14 doz.

Brush \$9.35 doz.; Men's

EXAMINATION PAPERS

PAPER II.

Ex. 2.—If 7 lbs of coffee are worth as much as 2 lbs. of tea. 3 lbs. of tea worth 11 lbs of sugar, and 41 lbs. of coffee cest 48c , what will 191 lbs. of sugar cost?

1 lb. of coffee = $\frac{48}{4\frac{1}{2}}$ c. = $\frac{96}{9}$ c.

1 lb. of tea $=\frac{7}{4}$ lbs. coffee $=\frac{7}{2}$ of $\frac{9}{4}$ c.

I lb. of sugar $=\frac{3}{11}$ lbs. tea $=\frac{3}{11}$ or $\frac{7}{2}$ of $\frac{9}{9}$ c. Hence $19\frac{1}{4}$ lbs. of sugar = $19\frac{1}{4} \times \frac{9}{11} \times \frac{7}{2} \times \frac{9}{6}$ c. = \$1.96.

- 1. Find the smallest number to be taken from 101443929 that the remainder may exactly contain 25203. 2. Divide 213×84×190 times 264 by 30 times 56 multiplied
- 3. Express in Roman numerals 114; 11983.
- 4. What is the least number of which each of the numbers 144, 240, 480. and 960 is a factor? 5. If $\frac{1}{2}$ of a lb. be worth $66\frac{2}{3}$ c., and $\frac{3}{2}$ of a lb. be worth as much
- as $\frac{1}{1+}$ of a bushel, find the value of 100 bushels. 6. If I sell my flour at \$2 a bag I lose \$30, but if I charge \$3 a bag I gain \$30: how many bags were there, and what did they cost me per bag?
- 7. How much water must I put into a hhd. of wine worth
- \$336 to make the mixture worth \$1.20 per quart? 8. A and B earn \$840 between them, but 2 of A's equals

 $\frac{9}{16}$ of B's earnings: what did each earn? 9. If the difference between 75 and $\frac{9}{7}$ of $121\frac{4}{3}+\frac{3}{4}$ of $48\frac{3}{3}$ be taken from $150\frac{1}{2}$, by how many times $\frac{4}{6}$ of $1\frac{1}{6}$ of $4-2\frac{1}{4}$

should the result be multiplied to produce $342\frac{63}{100}$? 10. The furniture of a house is worth \$10000, and $\frac{1}{10}$ of $\frac{1}{2}$ of $\frac{1}{2}$ of the furniture costs as much as $\frac{1}{2}$ of $\frac{1}{2}$ of the

house: find the cost of both together. 11. A farmer gave his eldest son $\frac{1}{1+1}$ of his farm, and $\frac{9}{0.5}$ of the remainder to the younger, who thus received 10 acres

7

8.

less than his brother : how many acres in the farm? 12. A and B traded with equal sums of money; A increased his money 20%; B lost \$220, and then had $\frac{1}{2}$ as much as

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EXAMINATION PAPERS,

PAPER III.

Ex. 3.—After spending \$60 more than $\frac{1}{2}$ of his money, a man had \$120 left: what had he at first?

If he had spent only $\frac{5}{8}$ of his money he would have had $\frac{560}{100}$ more left, or $\frac{5180}{180}$.

Then, having spent § of his money, he must have § of it left.

Therefore, $\frac{3}{8}$ of the money = \$180. $\frac{1}{8}$ "" = \$60. $\frac{5}{8}$ "" = \$480. Pk(0)F: $\frac{5}{8}$ of 480 = 300. 300 + 60 = \$360, amount spent. \$480 - \$360 = \$120, " left.

I. What is a pure Circulating Decimal? How do you reduce it to its equivalent fraction ? Express as a decimal:

$$\frac{3\frac{1}{8}}{8}$$
 + 625 + $\frac{1}{8}$ of $\frac{7\frac{3}{6}}{105}$ of 4 - 1.05.

- 2. One-half the sum of two numbers is 500, and one-half their difference is 300: what are the numbers?
- 3. If $\frac{1}{6}$ of 56 and also $\frac{3}{2}$ of it be added to itself, the sum is just 26 less than double the number: find the number.
- 4. How high is a pile of wood 12 yds. long, 12 ft. wide, which contains 18 cords?
- 5. A can do ⁴/₂ of a job in 2³/₅ hrs., and B can do ⁴/₂ of it in 4¹/₂ hrs.: how long would they take, working together?
- 6. I gain 10% by selling vinegar at 22c. a qt.: how many barrels of 63 gals. each did I buy for \$1058.40?
- 7. If $\frac{1}{3}$ of $1\frac{3}{4}$ be multiplied by $\frac{1}{13}$ of the square of $8\frac{4}{7}$, and $\frac{2\frac{1}{3}}{3\frac{1}{7}}$ be added to the product, from what should the result be taken to produce $\frac{11\frac{3}{32}}{81}$?
- 8. A man worked 6³/₄ weeks, and, having spent \$15 more than \$ of his earnings, had \$45 left: what did he earn a week?

as 2 lbs. of $14\frac{1}{2}$ lbs. of cost ?

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EXAMINATION PAPERS.

PAPER IV.

Ex. 4.—A man can row 5 miles an hour in still water : how long will he take to go 21 miles up a stream and back, the stream running 2 miles an hour? Going up, the stream retards him 2 miles an hour, making

21÷3=7 hrs., time to go 21 miles up.

Going down, the stream helps him 2 miles an hour, making

21--7=3 lirs, time to go 21 miles down. Hence, $7+3 \times 10$ hrs., whole time.

1. Divide (to four places of decimals) the sum of .075 and

 $\frac{75}{10000}$ by the difference between 7.5 and $\frac{75}{700}$. 2. A can do a piece of work in $12\frac{1}{4}$ days of 9 hrs. each, but

with B helping him he can do it in 2⁴ days : how many hours would B alone require to finish it?

3. I gave away \$351, and then had \$20.20 more than I gave

4. A man paves his garden 49 ft. long and 10 yds. wide at 45c. a sq. yd., except two grass plots each 7 ft. square :

5. A stream runs hah a mile in 15 min., and a man can row a mile in 10 min. : how much longer will he be in going

up, than in coming down, a distance of 32 miles? 6. What decimal part of a grain would balance .000075 lbs.

7. I paid \$39 to the Queen City Insurance Co. for insurance

at $1\frac{1}{6}$, what part of my factory, worth \$4550, would I

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8. Divide 570 acres of land among A, B and C, giving B and C equal shares, but A 60 acres more than B and C

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EXALINATION PAPERS.

PAPER V.

Ex. 5.- A, going 12 miles an hour, gives B, who goes 8 miles an hour, a start of 40 miles : how long before B

Argoes 4 miles an hour more than B, that is, Λ approaches or overtakes B at the rate of 4 miles an hour, and since he must overtake 40 miles, it will take $\lim_{t \to -4} 4 = 10$

This applies to the large hand (A) and the small hand

A goes 60 min. spaces in 60 min. 5 " " " 60 "

Therefore, Λ approaches B at the rate of 55 min. spaces in

1. What must be multiplied by '08008 to give 48536'488

2. From the sum of $\frac{4}{5}$ lb. $4\frac{5}{5}$ oz. and $31\frac{1}{5}$ dwt. take the difference between $\frac{3}{5}$ oz. and $\frac{7}{5}$ dwt.

- 3. Simplify $\frac{9}{38\frac{1}{4}} \times \frac{174\frac{4}{9}}{196\frac{1}{4}} \times \frac{44\frac{5}{8}}{16\frac{1}{3}} \cdot \frac{36\frac{4}{7}}{40\frac{5}{11}}$
- 4. Two men jointly owned a farm in Manitoba; one had 470 acres more than 3, and the other 790 acres more than of the farm: find the share of each.
- 5. If $\frac{5}{7}$ of a sum of money be decreased by $\frac{3}{7}$ of the sum, the remainder will be \$62 more than 20 of the remainder:
- 6. A train going 25 miles an hour starts at 1 o'clock P.M. on a trip of 230 miles; another going 37 miles an hour starts from the same place at 12 min. past 4 o'clock P.M.: when and where will the former be overtaken?
- 7. Divide \$540 between George, Henry, and Fred, giving George 30% more than Fred's share, and Henry \$80 more than the other two together.
- 8. By selling my cloth at \$1.26 a yard, I gain 11 cents more than I lose by selling it at \$1.05 a yard : what would I gain by selling 800 yards at \$1.40 a yard?

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EXAMINATION PAPERS.

PAPER VI.

Ex. 6.—If 27 men build 32 yards of fencing in 64 hours,

how long will it take 36 men to build 108 yards of the First, looking at the amount of work done, 108 yards will

require $\frac{10.8}{84}$ of the time required for 32 yards. That is : 108 of 64 hrs. Again, considering the number of men, 36 men will require

37 of the time required by 27 men. That is: $\frac{27}{36}$ of $\frac{103}{32}$ of 64 hrs. = 162 hrs.

Is In all problems such as the preceding, every corresponding pair of terms is formed into a proper or an improper fraction, and the different fractions thus formed

- 1. How many square yards in an acre? What part of a
- sq. yd. must be added to $\frac{1}{13}$ sq. ft. $+\frac{7}{13}$ sq. in. to produce 2. Multiply 40 and 15625 millionths by 1632 ten-thou-
- 3. If $\frac{3}{7}$ of the sum of a certain number and its seventh part,

be added to the original number, the result will be 292: what is the number?

4. Divide \$6000 between C and D, giving D \$1800 more

than 3 times the amount C receives. 5. A train leaves Toronto for Collingwood, 95 miles, at 13

miles an hour; another leaves Collingwood for Toronto at the same time, but goes 23 miles an hour: when will they be just 5 miles apart?

6. A room is 4 yds. 2 ft. wide, 5¹/₃ yds. long, and 8 ft. high: find the cost of papering the walls with paper 24 in. wide

7. A and B receive the same salary; A saves ? of his, but B spends \$36 a month more than A, and is \$30 in debt at

- the end of 5 months: what does each spend a month? 8. If 12 men in 24 days of 9 hrs. each build 192 cu. ft. of wall, how many men will be required to build 320 cu. ft.
- of wall in 27 days of 10 hrs. each? 9. A grocer drew off '45 of a cask of syrup, then 20 gallons, and it was found to want 65 of being full : how many gallons would it contain?

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ANSWERS.

EXERCISE 1.-Page 3.

- I. 4; II; 26; 37; 45; 68; 77; 59; 80; 92.
- 2. 1, 9; 10, 99; 23, 32; 39, 93; 19, 91; 17, 71; 78, 87;
- 3. 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47.
- 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 78; 17, 16, 15, 14, 13, 12, 11;
- 47, 46, 45, 44, 43, 42, 41, 40, 39, 38, 37, 36, 35, 34, 33. 4. 15; 64.
- 5. 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64. 65, 66, 67, 68, 69, 70, 71, 72, 73, 74. 6. 68, 86; 67, 76; 78, 87.

EXERCISE 2.-Page 5.

- 1. 117; 311; 511; 575; 899; 400; 69; 507; 860; 410;
- 2. 106, 107, 108, 109, 110, 111, 112, 113, 114, 115, 116, 117,
- 3. 790, 791, 792, 793, 794, 795, 796, 797, 798, 799; 180, 280, 380, 480, 580, 680, 780, 880, 980; 607, 617, 627, 637, 647, 657, 667, 677, 687, 697;
- 700, 710, 720, 730, 740, 750, 760, 770, 780, 790. 4. 999; 100.
- 5. 689, 698, 869, 896, 968, 986.
- 6. 39 (which is the same as 039), 93, 309, 390, 903, 930.
- 8. (1) 7, 70, 700. (2) 68, 86, 608, 680, 806, 860. (3) 899, 989,998. (4) 777.

EXERCISE 3.-Page 8.

I. 9048; 5007; 43659; 536302; 405313; 5043037; 64792; 356097; 9345027; 80056; 9090900; 83007; 9090; 375867799; 11071; 6008704.

- 2. 9999, 1000; 99999, 10000; 999999, 100000; 9999999,
- 3. 3072, 3172, 3272, 3372, 3472, 3572, 3672, 3772, 3872, 4. 7530; 3057.
- 5. 8700, 7800, 8070, 7080, 7008, 8007; 8700 greatest; 7008

EXERCISE 4.-Page 11.

1. 13, XIII. 2. 17, XVII. 3. 19, XIX. 4. 25, XXVI. 5. 38, XXXVIII. 6. 44, XLIV. 7. 97, XCVII. 8. 150, CL. 9. 280, CCLXXX. 10. 738, DCCXXXVIII. II. 844, DCCCXLIV. 12. 1200, MCC. 13. 87, LXXXVII. 14. 6000, VM. 15. 1500, MD. 16. 11000, XM. 17. 888, DCCCLXXXVIII. 18. 7592, VMMDXCII. 19. 4711, MVDCCXI. 20. 52, LII. 21. 39, XXXIX.

22. 43, XLIII.

23. 67, LXVII. 24. 91, XCI. 25. 1881, MDCCCLXXXI. 26. 27, XXVII. 27. 49, XLIX. 28. 73, LXXIII. 29. 68, LXVIII. 30. 84, LXXXIV. 31. 97, XCVII. 32. 110, CX. 33. 530, DL. 34. 740, DCCXL. 35. 990, CMXC. 36. 1600, MDC. 37. 50005, LV. 38. 318, CCCXVIII. 39. 796, DCCXCVI. 40. 1096, MXCVI. 41. 25000, XXV. 42. 59300, MLXCCC.

43. 87040, LXXXVMMXL.

(c)

EXERCISE 5.-Page 13.

- (a) 1. 116,234. One hundred and sixteen thousand, two hundred and thirty-four.
 - 2. 65,231. Sixty-five thousand, two hundred and thirtyone.
 - 3. 20,703. Twenty thousand, seven hundred and three.
 - 4. 71,005. Seventy-one thousand and five. 5. 3,104.
 - Three thousand, one hundred and four. 6. 48,000. Forty-eight thousand.

ii

; \$9999999,

3772, 3572,

test; 7008

LXXXI.

C. MMXL.

vo hunthirty-

three.

ANSWERS,

- 7. 60,029. Sixty thousand and twenty-nine.
- 8. 141,120. One hundred and forty-one thousand, one hundred and twenty.
- 9. 101,207. One hundred and one thousand. two hundred and seven.
- 10. 68,978. Sixty-eight thousand, nine hundred and seven. ty-eight.
- 11. 72,020. Seventy-two thousand and twenty.
- 12. 80,001. Eighty thousand and one.
- 13. 857,000. Eight hundred and fifty-seven thousand.
- 14. 91,029. Ninety-one thousand and twenty-nine.
- 15. 7,640. Seven thousand, six hundred and forty.
- 16. 800,900. Eight hundred thousand, nine hundred.
- 17. 2,568,242. Two million, five hundred and sixty-eight thousand, two hundred and forty-two.
- 18. 1,008,003. One million, eight thousand and three.
- 19. 212,375.647. Two hundred and twelve million, three hundred and seventy-five thousand, six hundred and forty-seven.
- 20. 609,003,588. Six hundred and nine million, three thousand, five hundred and eighty-eight.
- 21. 897,856,846. Eight hundred and ninety-seven million, eight hundred and fifty-six thousand, eight hundred and forty-six,
- (b) 1. 9. Nine.
 - 2. 200. Two hundred.
 - 3. 60,002. Sixty thousand and two.
 - 4. 700,000,000. Seven hundred million,
 - 5. 230,000,060. Two hundred and thirty million, and sixty.
 - 6. 81,501,007,012. Eighty-one billion, five hundred and one million, seven thousand and twelve.
 - 7. 30,000,000,000,603. Thirty trillion, six hundred and three.
 - 8. 700,080,000,000,000. Seven hundred trillion and eighty billion.
 - 9. 8,007,014,010. Eight billion, seven million, fourteen thousand and ten.
- 10. 15,000,018,207,000,081. Fifteen quadrillion, eighteen billion, two hundred and seven million and eighty-one.
- (c) 1. 60,701,892. Sixty million, seven hundred and one thousand, eight hundred and ninety-two.

- 2. 50,607,801. Fifty million, six hundred and seven thousand, eight hundred and one. 3. 600,000. Six hundred thousand.
- 4. 49,000,000. Forty-nine million.
- 5. 593,006,070,500. Five hundred and ninety-three bil-
- lion, six million, seventy thousand, five hundred. 6. 190, 190,001,900. One hundred and ninety billion, one hundred and ninety million, one thousand, nine hun-
- 7. 163,194,568. One hundred and sixty-three million, one hundred and ninety-four thousand, five hundred and sixty-eight.
- 8. 3,050,050,183. Three billion, fifty million, fifty thousand, one hundred and eighty-three.
- 9. 5,000,204. Five million, two hundred and four. 10. 594,900. Five hundred and ninety-four thousand, nine 11. 12,000,012.
- Twelve million and twelve. 12. 2,007,980,134. Two billion, seven million, nine hundred and eighty thousand, one hundred and thirty-four.
- (d) 1. 18,000.
 - 2. 2,060,153.
 - 3. 60,060,060,060.
 - 4. 60,200,500.
 - 5. 402,348,213,020.
 - 6. 78,640,000,006,016.
 - 7. 6,542,000,025.
 - 8. 6,542,000,025.
- (e) 1. 19. Nineteen.
 - 2. 21. Twenty-one.
 - 3. 10. Ten.
 - 4. 45. Forty-five.
 - 5. 65. Sixty-five.
 - 6. 64. Sixty-four.
 - 7. 79. Seventy-nine.
 - 8. 85. Eighty-five.
- 9. 110. One hundred and ten.
- 10. 119. One hundred and nineteen. 11. 100. One hundred.
- 12. 114. One hundred and fourteen. 13. 160. One hundred and sixty.

- 9. 402,348,213,020.
- 10. 5,008,949.
- 11. 200,300,800.
- 12. 29,599,000,601.
- 13. 4,000,558,240,070.
- 14. 32,001,343,404.
- 15. 555,777,669.
- 16. 806,070,005,206.

iv

and seven

y-three bilidred. billion, one nine hun-

nillion, one ndred and

fifty thou-

mr. sand, nine

hundred -four.

0.

70.

14. 190. One hundred and ninety. 15. 260. Two hundred and sixty. 16. 290. Two hundred and ninety. 17. 629. Six hundred and twenty-nine. 18. 811. Eight hundred and eleven. 19. 950. Nine hundred and fifty. 20. 1,259. One thousand, two hundred and fifty-nine. 21. 76. Seventy-six. 22. 1,869. One thousand, eight hundred and sixty-nine. 23. 5.193. Five thousand, one hundred and ninety-three. 24. 17. Seventeen. 25. 2,222. Two thousand, two hundred and twenty-two. 26. 3,500. Three thousand, five hundred. 27. 450. Four hundred and fifty. 28. 48. Forty-eight. 29. 536. Five hundred and thirty-six. 30. 1,794. One thousand, seven hundred and ninety-four. 31. 10,116. Ten thousand, one hundred and sixteen. 32. 381. Three hundred and eighty-one. 33. 50,999. Fifty thousand, nine hundred and ninety-nine. 34. 1,001,612. One million, one thousand, six hundred and 35. 5,470. Five thousand, four hundred and seventy. 36. 265. Two hundred and sixty-five. 37. 3,627. Three thousand, six hundred and twenty-seven. 38. 19. Nineteen. 39. 54. Fifty-four. 40. 402. Four hundred and two. 41. 536. Five hundred and thirty-six. 42. 85. Eighty-five. 43. 18. Eighteen. 44. 77. Seventy-seven. 45. 67. Sixty-seven. 46. 164. One hundred and sixty-four. 47. 135. One hundred and thirty-five. 48. 149. One hundred and forty-nine. 49. 1.org. One thousand and nineteen. 50. 653. Six hundred and fifty-three. 51. 100,099. One hundred thousand and ninety-nine. 52. 5,559. Five thousand, five hundred and fifty-nine. 53. 560,000. Five-hundred and sixty thousand. 54. 31,500. Thirty-one thousand, five hundred.

ANSWERS.

55. 59.344. Fifty-nine thousand, three hundred and forty-

- 56. 15,749. Fiftcen thousand, seven hundred and forty-57. 1,003,090. One million, three thousand and ninety.
- 58. 6,749. Six thousand, seven hundred and forty-nine.
- 59. 1,525,479. One million, five hundred and twenty-five thousand, four hundred and seventy-nine. 60. 1,882. One thousand, eight hundred and eighty-two.

late in a	EXERCISE 7Page	91
(a) 1. 11 loads. 2. 12 cents. 3. 12 days. 4. 14 cherries. 5. 16 apples. 6. 14 sheep. 7. 13 dollars. 8. 14 trees. 9. 16 cents. 10. 21 plums. 11. 14 ducks.	12. 19 cents. 13. 13 books. 14. 16 cents. 15. 13 chickens. 16. 9 apples. 17. 17 letters. 18. 12 books. 19. 23 dollars. 20. 16 dollars. 21. 26 cents.	22. 14. 23. 15 cents. 24. 17 birds. 25. 17 cents. 26. 15 panes. 27. 16. 28. 19 pears. 29. 18. 30. 26 cents. 31. 8898 acres.
(<i>b</i>) 1. 85. 2. 79. 3. 58. 4. 58. 5. 89. 6. 364. 7. 893. 8. 7795.	9. 8889. 10. 7799. 11. 9979. 12. 6759. 13. 9978. 14. 8999. 15. 6647. 16. 4999.	176999. 18.77969. 19.848699. 20.148798. 21.8199398. 22.899969. 23.9999999. 24.3747655.
EN	XERCISE 8.—Page 26.	
1. 2435. 2. 799. 3. 678. 4. 568. 5. 9848. 6. 28172. 7. 2598. 4. 2598.	9. 22168. 10. 164918. 11. 3037. 12. 3161. 13. 21286. 14. 23940. 15. 93545. 16. 1245901. 17. 197351.	 18. 196395. 19. 154970. 20. 2035342. 2. 1384473. 3. 145406. 4. 1670551. 5. 193372. 6. 4523181. 7. 96379092.

EXERCISE 7.-Page 21.

* vi

and forty-	1	ANSWERS.	v:
	8. 1739183.	1 21 21-2	
ud forty-	9. 134762.	21, 2153. 22. \$7549	36. 37199.
5	10. 969754.	22. 47549	37. 39351 miles.
inety.	11. 1825941.	23. 3619.	38. 154691.
-nine.	12. 10965339.	24. 6575.	39. 13740178.
enty-five	13. 1564442.	25 \$32331.	40. 1369000923.
any-nye	11 108 20 10 20	26. \$11425	41.
y-two.	14. 108594353.	27. 1821.	1. 16665.
y.two.	15.	28. 75922.	9. 4112
	1. 9339190.	29. 339466 men.	• 53328.
	a. 11178170.	30. \$13610	
	3. 10306156.	31. \$764.	42. 375540.
its.	+. 10670291.	32. \$10766.	43. 60 dahlias.
ls.	16. 4289 trees.	33. \$13025.	44. 466 cents.
ts.	17. \$2844.	34. \$2114,\$2935	45. 131 cents.
es.	18. 679 sheep.	\$10897.	
	19. \$9212.	35. \$141252.	47. 96 years.
rs.	2.19.4.	55. 4141252.	48. 140 yards.
s.	T.	VERGIER 10 D	1
res.		XERCISE 10 Fage	37.
ies.			
	1. 142.	22. 44211.	43. 12 marbles.
	2. 1512.	23. 32134.	44. III quail.
	3. 6251.	24. 56314.	45. \$4410.
	4. 5021.	25. 33662,	46 ara hugh al
	5. 1440.	26. 24570.	46. 213 bushels.
	6. 4112.	27. 22625.	47. \$211.
	7. 3201.	28. 13432.	48. 230 sheep.
	8. 5310.	29. 43220.	49. \$2560.
	9. 2411.	30. 12442.	50. \$1404.
	1 . 2412.	31. 10853.	51. \$2453.
	II. II20.	31. 10053.	52. 4003 yards.
- Charles	12. 3732.	32. 25468.	53. 4213 dollars.
	13. 52221.	33. 31064.	54 3336 dollars.
	14. 852556.	34. 6.6453.	55. 24337 dollars.
	14. 032550.	35. 64124.	56. 144422 dollars
	15. 603054.	36. 37001.	57. 843 dollars.
	16. 864201110.	37. 205443.	58. 1360 sheep.
	17. 10035174.	38. 601.	59. 513 geese.
1. The second second second second second second second second second second second second second second second	18. 5162142.	39. 35002.	60. 202 bushels.
	19. 30640.	40. 46150.	61 II foot
14	2 . 57172.	41. 70046,	61. 11602 harrels.
	21. 43242.		62. 14432 dollars.
11		1	63. 561092 dollars

Control of

ANSWERS,

EXERCISE 11.-Page 41. (a) 1. 83. 11. 618. 2. 445. 21. 491978. 12. 909. 3. 221. 22. 261636. 13. 949. 4. 1086. 23. 294928. 14. 3745. 5. 313. 24. 680929. 15. 2757. 6. 2384. 25. 281939. 16. 41830. 7. 3335. 26. 490909. 17. 581949. 8. 24465. 27. 492929. 18. 495829. 9. 185173. 28. 391616. 19. 383969. 10. 1147. 29. 17359. 20. 194959. 30. 432099. (6) 1. 276. 7. 5498. 2. 67. 12. 19238. 8, 17571. 3. 4004. 13. 37486. 9. 18654. 4. 664. 14. 111530. 10. 23017. 5. 3316. 15. 591203. 11. 57921. 6. 34943. 16. 666667. (c) 1. 409095. 16. 90014. 2. 274850. 31. 996. 17. 145129. 3. 707970092. 32. 459812. 18. 254999. 4. 9610. 33. 44007. 19. 319527. 5. 896. 20. 663367. 34. 491693. 6. 51306. 35. 62796. 21. 427165. 7. 60964492. 36. 4989050. 22. 587979. 8. 549913964. 37. 1700261. 23. 758451. 9. 46924. 38. 6634585. 24. 823011. 10. 75757. 39. 69994. 25. 900829. 11. 56300. 40. 8974088. 26. 6898220. 12. 699901. 41. 287949. 27. 19542. 13. 5200. 42. 852642. 28. 459611. 14. 9688. 43. 899999. 29. 31229. 30. 698. 15. 75999. 44. 90100199. (1) 1. 64349020. 7. 478. 8. 459079260. 2. 899450. 13. 34740. 3. 11600800, 14. 3877. 9. 40020. 4. 255350011. 15. 2092. 10. 99002992. 5. 1215. 16. 401. 11. 615. 6. 99999500. 17. 4359999. 12. 776546. 18. 1105.

viii

EXERCISE 12.—Page 43.

 175 sheep. 7604. \$7604. \$5210. \$9161. 285866. 3602. 30. 47. 30. \$1462. 12. 128. 4794 miles. \$221708. \$221708. 21834 acres. 	 48805 barrels. 19. \$38094. 19. \$38094. 20. 13733 feet. 21. \$8674. 22. 275 acres. 23. 94760000 miles 24. \$6350. 25. \$3087. 26. 487628 feet. 27. 1808. 28. \$99635. 29. \$24354. 20. 28153 votes. 31. 4491 sq. miles. 	 32. 3571 feet. 33. 1769. 34. 85 years. 35. 664. 36. 110 years. 37. 2984679. 38. 7925 feet. 39. 7812 feet. 40. 8712 feet. 41. 293 feet. 42. \$13667. 43. 6326 acres. 44. 28278 bar.els. 45. John 32; James 90.
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EXERCISE 14.-Page 55.

2. $268.$ 24. $2836195.$ 45. $314095.$ 3. $446.$ 25. $36880812.$ 46. $563136.$ 4. $492.$ 26. $23008960.$ 48. $197930.$ 5. $556.$ 27. $5772463.$ 49. $244182.$ 6. $990.$ 28. $5105520.$ 50. $52092.$ 7. $2624.$ 29. $30002504.$ 51. $206832.$ 9. $7258.$ 31. $46832.$ 53. $59822.$ 10. $7570.$ 32. $182452.$ 54. $4518.$ 12. $8616.$ 34. $280210.$ 56. $4100832.$ 13. $284068.$ 35. $42528.$ 57. $4536.$ 15. $7229066.$ 37. $161525.$ 59. $20200.$ 16. $924356.$ 39. $400675.$ 61. $21416.$ 19. $280260.$ 41. $86499.$ 63. $26543.$ 20. $2115258.$ 42. $140760.$ 64. $37704.$ 21. $4156984.$ 43. $220739.$ 65. $39006.$	(a) 1. 246.	1	
2.203.24. $2836195.$ 10. $57595.$ 3.446.25. $36880812.$ 47. $113900.$ 4.492.26. $23008960.$ 48. $197930.$ 5.556.27. $5772463.$ 49. $244182.$ 7. $2624.$ 29. $30002504.$ $50.$ $52092.$ 8. $4344.$ 20. $1659000.$ $52.$ $23504.$ 9. $7258.$ 31. $46832.$ $53.$ $59822.$ 10. $7570.$ $32.$ $182452.$ $54.$ $4518.$ 12. $8616.$ $34.$ $280210.$ $56.$ $4100832.$ 13. $284068.$ $35.$ $42528.$ $57.$ $4536.$ 14. $3412648.$ $36.$ $360918.$ $58.$ $9738.$ 15. $7229006.$ $37.$ $161525.$ $59.$ $20200.$ 17. $3609186.$ $39.$ $400675.$ $61.$ $21416.$ 19. $280260.$ $41.$ $86499.$ $63.$ $26543.$ 20. $2115258.$ $42.$ $140760.$ $64.$ $37704.$ 22. $871624.$ $43.$ $206739.$ $65.$ $39006.$		23. 2037468.	1 45 211005
3.440. $25.36880812.$ $47.113900.$ $4.492.$ $26.23008960.$ $48.197930.$ $5.556.$ $27.5772463.$ $49.244182.$ $6.990.$ $28.5105520.$ $50.52092.$ $7.2624.$ $29.30002504.$ $51.206832.$ $9.7258.$ $31.46832.$ $53.59822.$ $10.7570.$ $32.182452.$ $54.4518.$ $11.8012.$ $33.103560.$ $55.1230125.$ $13.284068.$ $35.42528.$ $57.4536.$ $14.3412648.$ $36.360918.$ $58.9738.$ $15.7229006.$ $37.161525.$ $59.20200.$ $17.3609186.$ $39.400675.$ $61.21416.$ $19.280260.$ $41.86499.$ $63.26543.$ $21.4156984.$ $43.206739.$ $65.39006.$	2. 268.	24. 2826 Tor	43. 314095.
4. $492.$ 25. $30600812.$ 47. $113900.$ 5. $556.$ 26. $23008960.$ 48. $197930.$ 6. $990.$ 28. $5105520.$ 50. $52092.$ 7. $2624.$ 29. $30002504.$ 51. $206832.$ 8. $4344.$ 30. $1659000.$ 52. $23504.$ 9. $7258.$ 31. $46832.$ 53. $59822.$ 10. $7570.$ 32. $182452.$ 54. $4518.$ 11. $8012.$ 33. $103560.$ 55. $1230125.$ 13. $284068.$ 35. $42528.$ 57. $4536.$ 14. $3412648.$ 36. $360918.$ 58. $9738.$ 15. $7229006.$ 37. $161525.$ 59. $20200.$ 16. $924356.$ 39. $400675.$ 61. $21416.$ 19. $280260.$ 41. $86499.$ 63. $26543.$ 20. $2115258.$ 42. $140760.$ 64. $37704.$ 21. $4156984.$ 43. $220739.$ 65. $39006.$	3. 416.		40. 503136.
5.556. $27.5772463.$ $48.197930.$ $6.990.$ $27.5772463.$ $49.244182.$ $7.2624.$ $29.3002504.$ $50.52092.$ $8.4344.$ $29.3002504.$ $51.206832.$ $9.7258.$ $31.46832.$ $52.23504.$ $10.7570.$ $32.182452.$ $54.4518.$ $11.8012.$ $33.103560.$ $55.1230125.$ $13.284068.$ $35.42528.$ $57.4536.$ $14.412648.$ $36.360918.$ $58.9738.$ $15.7229006.$ $37.161525.$ $59.20200.$ $17.3609186.$ $39.400675.$ $61.219138.$ $18.64823505.$ $40.547476.$ $62.7846312.$ $19.280260.$ $41.86499.$ $63.26543.$ $21.4156984.$ $43.206739.$ $65.39006.$		25. 30880812.	47. 113000
3.550. $27.5772463.$ $49.244182.$ $6.990.$ $28.5105520.$ $50.52092.$ $7.2624.$ $29.30002504.$ $51.206832.$ $8.4344.$ $30.1659000.$ $52.23504.$ $9.7258.$ $31.46832.$ $53.59822.$ $10.7570.$ $32.182452.$ $54.4518.$ $12.8616.$ $34.280210.$ $55.1230125.$ $13.284068.$ $35.42528.$ $57.4536.$ $14.3412648.$ $36.360918.$ $59.2020.$ $15.7229066.$ $37.161525.$ $59.20200.$ $16.924356.$ $39.400675.$ $61.21416.$ $19.280260.$ $41.86499.$ $63.26543.$ $20.2115258.$ $42.140760.$ $64.37704.$ $21.4156984.$ $43.206739.$ $65.39006.$		26. 23008060.	18 100000
6. 990.28. $5105520.$ 49. $244182.$ 7. $2624.$ 29. $30002504.$ 50. $52092.$ 8. $4344.$ 30. $1659000.$ 52. $23504.$ 9. $7258.$ 31. $46832.$ 53. $59822.$ 10. $7570.$ 32. $182452.$ 54. $4518.$ 11. $8012.$ 33. $103560.$ 55. $1230125.$ 13. $284068.$ 35. $42528.$ 57. $4536.$ 14. $3412648.$ 36. $360918.$ 58. $9738.$ 15. $7229006.$ 37. $161525.$ 59. $20200.$ 16. $924356.$ 38. $115604.$ 60. $219138.$ 17. $3609186.$ 39. $400675.$ 61. $21416.$ 19. $280260.$ 41. $86499.$ 63. $26543.$ 20. $2115258.$ 42. $140760.$ 64. $37704.$ 21. $4156984.$ 43. $206739.$ 65. $39006.$	5. 556.	27. 5772463	40. 19/930.
7. $2024.$ 20. $5105520.$ $50.$ $52092.$ 8. $4344.$ 29. $30002504.$ $51.$ $206832.$ 9. $7258.$ $31.$ $46832.$ $52.$ $23504.$ 10. $7570.$ $32.$ $182452.$ $53.$ $59822.$ 11. $8012.$ $33.$ $103560.$ $55.$ $1230125.$ 12. $8616.$ $34.$ $280210.$ $56.$ $4100832.$ 13. $284068.$ $35.$ $42528.$ $57.$ $4536.$ 14. $3412648.$ $36.$ $360918.$ $58.$ $9738.$ 15. $7229006.$ $37.$ $161525.$ $59.$ $20200.$ 17. $3609186.$ $39.$ $400675.$ $61.$ $21416.$ 19. $280260.$ $41.$ $86499.$ $63.$ $26543.$ 20. $2115258.$ $42.$ $140760.$ $64.$ $37704.$ 21. $4156984.$ $43.$ $206739.$ $65.$ $39006.$	6. 990.	-7. 3772403.	49. 244182.
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	7 260.	20. 5105520.	
0. $1344.$ $30.$ $1659000.$ $52.$ $23504.$ $9.$ $7258.$ $31.$ $46832.$ $53.$ $59822.$ $10.$ $7570.$ $32.$ $182452.$ $54.$ $4518.$ $11.$ $8012.$ $33.$ $103560.$ $55.$ $1230125.$ $13.$ $284068.$ $34.$ $280210.$ $56.$ $4100832.$ $14.$ $3412648.$ $35.$ $42528.$ $57.$ $4536.$ $15.$ $7229006.$ $37.$ $161525.$ $59.$ $20200.$ $16.$ $924356.$ $38.$ $115604.$ $60.$ $219138.$ $17.$ $3609186.$ $39.$ $400675.$ $61.$ $21416.$ $19.$ $280260.$ $41.$ $86499.$ $63.$ $26543.$ $20.$ $2115258.$ $42.$ $140760.$ $64.$ $37704.$ $21.$ $4156984.$ $43.$ $206739.$ $65.$ $39006.$	7. 2024.	29. 3000250.1.	57 006921
9. $7258.$ 31. $46832.$ $52. 23504.$ 10. $7570.$ 32. $182452.$ $53. 59822.$ 11. $8012.$ 33. $103560.$ $55. 1230125.$ 12. $8616.$ 34. $280210.$ $56. 4100832.$ 13. $284068.$ $35. 42528.$ $57. 4536.$ 14. $3412648.$ $36. 360918.$ $58. 9738.$ 15. $7229006.$ $37. 161525.$ $59. 20200.$ 17. $3609186.$ $39. 400675.$ $61. 21416.$ 19. $280260.$ $41. 86499.$ $63. 26543.$ 20. $2115258.$ $42. 140760.$ $64. 37704.$ 21. $4156984.$ $43. 206739.$ $65. 39006.$	8. 4344.	30. 1650000	
10.7570.32. $182452.$ 53. $59822.$ 11. $8012.$ 33. $103560.$ 54. $4518.$ 12. $8616.$ 34. $280210.$ 56. $4100832.$ 13. $284068.$ $35.$ $42528.$ 57. $4536.$ 14. $3412648.$ $36.$ $360918.$ 57. $4536.$ 15. $7229006.$ $37.$ $161525.$ 59. $20200.$ 16. $924356.$ $39.$ $400675.$ $61.$ $21416.$ 19. $280260.$ $41.$ $86499.$ $63.$ $26543.$ 20. $2115258.$ $42.$ $140760.$ $64.$ $37704.$ 21. $4156984.$ $43.$ $206739.$ $65.$ $39006.$	9. 7258.	Je. 1039000.	52. 23504.
11. $8012.$ $32.$ $102452.$ $54.$ $4518.$ 12. $8616.$ $34.$ $280210.$ $55.$ $1230125.$ 13. $284068.$ $35.$ $42528.$ $57.$ $4536.$ 14. $3412648.$ $35.$ $42528.$ $57.$ $4536.$ 15. $7229006.$ $37.$ $161525.$ $59.$ $20200.$ 16. $924356.$ $39.$ $400675.$ $61.$ $21416.$ 17. $3609186.$ $39.$ $400675.$ $61.$ $21416.$ 19. $280260.$ $41.$ $86499.$ $63.$ $26543.$ 20. $2115258.$ $42.$ $140760.$ $64.$ $37704.$ 21. $4156984.$ $43.$ $206739.$ $65.$ $39006.$	10 7570	. 31. 40832.	53. 50822.
11. $3012.$ 33. $103560.$ $547.476.$ 12. $8616.$ $34.280210.$ $55.1230125.$ 13. $284068.$ $35.42528.$ $56.4100832.$ 14. $3412648.$ $36.360918.$ $58.9738.$ 15. $7229006.$ $37.161525.$ $59.20200.$ 17. $3609186.$ $39.400675.$ $61.21416.$ 19. $280260.$ $41.86499.$ $63.26543.$ 20. $2115258.$ $42.140760.$ $64.37704.$ 21. $4156984.$ $43.206739.$ $65.39006.$	10. 7570.	32. 182452.	
12. 8016. $34. 280210.$ $50. 1430832.$ 13. 284068. $35. 42528.$ $57. 4536.$ 14. 3412648. $36. 360918.$ $58. 9738.$ 15. 7229006. $37. 161525.$ $59. 20200.$ 17. 3609186. $39. 400675.$ $61. 21416.$ 19. 280260. $41. 86499.$ $63. 26543.$ 20. 2115258. $42. 140760.$ $64. 37704.$ 21. 4156984. $43. 206739.$ $65. 39006.$	11. 8012.	33. 102560	
13. 28_{4068} .34. 220210 .56. 4100832 .14. 3412648 .35. 42528 .57. 4536 .15. 7229006 .36. 360918 .58. 9738 .15. 722906 .37. 161525 .59. 20200 .16. 924356 .38. 115604 .60. 219138 .17. 3609186 .39. 400675 .61. 21416 .19. 280260 .41. 86499 .63. 26543 .20. 2115258 .42. 140760 .64. 37704 .21. 4156984 .43. 206739 .65. 39006 .	12. 8616.		55. 1230125.
14. $3412648.$ $35.$ $42528.$ $57.$ $4536.$ $15.$ $7229006.$ $36.$ $360918.$ $58.$ $9738.$ $16.$ $924356.$ $37.$ $161525.$ $59.$ $20200.$ $17.$ $3609186.$ $39.$ $400675.$ $61.$ $219138.$ $18.$ $64823505.$ $40.$ $547476.$ $62.$ $7846312.$ $19.$ $280260.$ $41.$ $86499.$ $63.$ $26543.$ $21.$ $4156984.$ $43.$ $206739.$ $65.$ $39006.$			56. 4100832.
14. $3412048.$ 36. $360918.$ 57. $4530.$ 15. $7229006.$ 37. $161525.$ 59. $20200.$ 16. $924356.$ 38. $115604.$ 60. $219138.$ 17. $3609186.$ 39. $400675.$ 61. $21416.$ 18. $64823505.$ 40. $547476.$ 62. $7846312.$ 19. $280260.$ 41. $86499.$ 63. $26543.$ 20. $2115258.$ 42. $140760.$ 64. $37704.$ 21. $4156984.$ 43. $206739.$ 65. $39006.$		35. 42528.	
15.7229006. $37.161525.$ $59.20200.$ $16.924356.$ $38.115604.$ $50.219138.$ $17.3609186.$ $39.400675.$ $61.21416.$ $18.64823505.$ $40.547476.$ $62.7846312.$ $19.280260.$ $41.86499.$ $63.26543.$ $20.2115258.$ $42.140760.$ $64.37704.$ $21.4156984.$ $43.206739.$ $65.39006.$		36. 360018	57. 4530.
16. 924356. $37. 101525.$ $59. 20200.$ $17. 3609186.$ $38. 115604.$ $60. 219138.$ $18. 64823505.$ $40.6675.$ $61. 21416.$ $19. 280260.$ $41. 86499.$ $63. 26543.$ $20. 2115258.$ $42. 140760.$ $64. 37704.$ $21. 4156984.$ $43. 206739.$ $65. 39006.$	15. 7229006.	37 16:00	50. 9738.
17. 3609186. $39. 115004.$ $60. 219138.$ $18. 64823505.$ $39. 400675.$ $61. 21416.$ $19. 280260.$ $41. 86499.$ $63. 26543.$ $20. 2115258.$ $42. 140760.$ $64. 37704.$ $21. 4156984.$ $43. 206739.$ $65. 39006.$	16. 024256	57. 101525.	59. 20200.
$18. 6_{4}8_{2}3_{5}0_{5}$. $39. 40007_{5}$. $61. 21416$. $19. 280260$. $40. 547476$. $62. 7846312$. $20. 2115258$. $41. 86499$. $63. 26543$. $21. 4156984$. $43. 206739$. $64. 37704$. $22. 871624$ $65. 39006$.	17 0600-06	33. 115604.	60. 210128
15. 04623505. $40. 547476.$ $62. 7846312.$ $19. 280260.$ $41. 86499.$ $63. 26543.$ $20. 2115258.$ $42. 140760.$ $64. 37704.$ $21. 4156984.$ $43. 206739.$ $65. 39006.$	17. 3009180.	39. 400675.	6. 0
19. $280260.$ 41. $86499.$ 02. $7840312.$ 20. $2115258.$ 41. $86499.$ 63. $26543.$ 21. $4156984.$ 43. $206739.$ 64. $37704.$ 22. $871624.$ 65. $39006.$	18. 64823505.	40 547476	01. 21410.
20. $2115258.$ 41. $50439.$ 63. $26543.$ 21. $4156984.$ 42. $140760.$ 64. $37704.$ 22. $871624.$ 43. $206739.$ 65. $39006.$	19, 280260.	+0. 5+/4/0.	62. 7846312.
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	20 2115258	41. 00499.	63. 26543.
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	-0. 4115250.	42. 140760.	64 27704
42. 071021	21. 4150984.	43. 206720	6- 3//04.
44. 115004. 66. 64248.	22. 871624.	11 11 160	05. 39006.
	, -+.	44. 115004.	66. 64248.

91978. 61636. 94928. 30929. 31939. 2929. 1616. 359. 2099. 238. 86.

530. 203. 667.

93. 6. 550. 261. 885.

9. 2.). 19**9.**

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ix

67. 900.867. 85. 69160. 68. 9909537. 103. 3376821. 86. 18711. 69. 103235616. 104. 7873096. 87. 35368. 70. 8602968. 105. 4384552. 88. 26243. 71. 8419829. 106. 10456714. 89. 118314. 72. 92618119. 107. 1841625. 9 . 8760. 73. 99249624. 108. 37657.6. 91. 28140. 74. 37873. 109. 10563091. 92. 10978. 75. 16140. 110. 4748112. 93. 97608. 76. 855547. 111. 11122164. 94. 8 432. 77. 10666596. 112. 6842529. 95. 98196. 78. 6666660. 113. 733236. 96. 226668. 79. 119999988. 114. 3597781. 97. 203236. 80. 44444444. 115. 5202432. 98. 30.65706. 81. 6909084. 116. 4591644. 99. 8363091. 82. 5333328. 117. 5552640. 100. 1556112. 83. 576702. 118. 3066574. 101. 5122164. 84. 1785. 119. 9585466. 102. 7732530. 120. 9166404. (6) 1. \$585. 15. 420 men. 2. \$1104. 28. 36960 feet. 16. 21120 feet. 3. \$17883. 29. 14080 yds. 17. 48785 yds. 4. \$43074. 30. 980 pounds. 18. 47136 brls. 5. 26400 feet. 31. \$700. 19. 40859 shingles. 6. 8800 yards. 20. \$27912. 32. 445 cts. 7. 162 days. 33. \$3572. 21. \$76113. 8. 894 days. 34. 3483 miles. 35. \$7156. 22. 79428 pounds, 9. 3680 bushels. 23. 316800 inches. 10. \$1715. 36. \$679. 24. 149136 miles, 11. \$2024. 37. 33804 quarts. 25. \$246736. 12. 1134 cts. 38. 1760 sq. rods. 26. \$24332. 13. \$8964. 39. 394992 pence 27. \$10344. 14. 3555 miles. 40. 4015 days.

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EXERCISE 15.-Page 61.

| (a) 1. 101840. 2. 149994. 3. 397714. 4. 1153362. 5. 727668. 6. 322992. 7. 334422198. | 13. 694417836. | 20. 7036203 |
|--|----------------|-------------|
| | 1 1521008/04. | 21. 9130257 |

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(a) .

3376821. 7873096. 4384552. 10456704. 1841625. 1025. 3765766. 10563691. 1748112. 1122164. 842529. 33236. 53230. 597781. 202432: 591644. 52640. 66574. 85466. 66404. 60 feet. 80 yds. pounds. cts. 2. miles. 6. quarts. sq.rods. 2pence lays.

31975.

ANSWERS

| 22. 11058.
23. 16799905881
24. 155572.
25. 45758.
26. 4159296.
27. 998001.
28. 707281.
29. 14130081.
3 ⁰ . 7977489.
31. 3769248.
32. 671180.
33. 268056.
(b) 1. 740. | $\begin{array}{c} 36. 5169248. \\ 37. 7062272. \\ 38. 7520415. \\ 39. 23065974. \\ 40. 34985162. \\ 41. 42397406. \\ 42. 123614208. \\ 43. 19602. \\ 44. 2563912. \\ 45. 131328. \end{array}$ | 46. 230850 .
47. 31812417 .
48. 3379446 .
49. 2420880 .
50. 4040138 .
51. 2738352 .
52. 384134 .
53. 2145594 .
54. 14645612 .
55. 16003352 .
56. 64421850 . |
|--|---|---|
| 2. 8690000. 3. 4698000. 4. 76984000000. 5. 131141615220. 6. 6477150. 7. 278170200. 8. 31915254. 9. 800962806. 10. 4793554242. 11. 36613538100. 12. 31617000. 13. 73865000. 14. 130321000. 15. 1231680000. 16. 110040000. 17. 346949400. 13. 1636562800. 10. 4946796000. | 20. 762294.
21. 8697821.
22. 38214.
23. 765870.
24. 600236.
25. 7281711.
26. 38673498.
27. 67312668.
28. 73818055.
29. 241768.
30. 5118862.
31. 17902976.
32. 15403736.
33. 15704325.
34. 2082600.
35. 271541350.
36. 1508741097.
37. 1587862270.
38. 3654860576. | $\begin{array}{c} 39. \ 8199473608. \\ 40. \ 982275037. \\ 41. \ 3363731415. \\ 42. \ 559616. \\ 43. \ 257460. \\ 43. \ 257460. \\ 44. \ 14988456. \\ 45. \ 14925792. \\ 46. \ 11155248. \\ 47. \ 182151828. \\ 48. \ 148644288. \\ 49. \ 1724573025. \\ 50. \ 8828716566. \\ 51. \ 601344. \\ 52. \ 29784450. \\ 53. \ 7364101944. \\ 54. \ 104598273 \\ 55. \ 118605858c. \\ 56. \ 15920205. \end{array}$ |
| (c) 1. 53207.
2. 182688.
3. 3628800.
4. 202301.
5. 36153036.
6. 163536.
7. 30026997000.
8. 461041.
9. 7546009.
10. 2890000.
11. 12321795560. | 12. 628331.
13. 195942000.
14. 104329.
15. 5536076.
16. 328347675.
17. 594992.
18. 18810224.
19. 6332592.
20. 4903524000.
21. 502705700.
22. 1418516800. | 23. 415143630. 24. 500; 6.0.;
1800; 4700;
2205; 872c6;
54010; 8080. 25. 725 cents. 26. 90 cents. 27. 975 cents. 28. 60000 cents. 29. 3800 cents. 30. 228240 cents. |

xi

(a) 1. 4695 bush. 21. 68520 feet. 2. 432 panes. 41. 5451 dollars. 22. 94848000 miles. 3. 7200 bush. 42. 14689 dollars. 23. \$71240. 4. +5797 dollars. 43. 734481 dollars. 24. \$10800. 5. 1494 dollars. 44. 228984 men. 25. 14688 miles. 6. 38988 dollars. 45. 273249 yards. 26. \$1757924. 7. 8125 potatoes. 27. 5280 feet. 46. 980019 pounds. 8. 1547 days. 28. 79000 pounds. 47. 372480 plants. 9. \$264958. 48. 1358112 letters. 29. \$43250. 10. 404914 lbs. 49. 349860 pounds. 30. 2323024 pages. 11. 186516 yards. 50. 63360 feet. 31. 88486 sheep. 12. \$7640136. 51. 40824 plums. 32. 137970 miles. 13. 202640 lbs. 52. 89232 rails. 33. 32166 dollars. 14. \$204763. 53. 10248 soldiers. 34. 29730 dollars. 15. \$44975. 54. 108 miles. 35. 541112 dollars. 16. \$121552. 55. 14712 men. 36. 492729 dollars. 17. 104160 sheets. 37. 3112135 cents. 56. 462160 feet. rS. \$299720. 57. 595680000 miles 58. 291214 cents. 38. 128690 dollars. 19. 203322 yards. 39. 1730368 dollars. 59. 68400 cents. 40. 1074354 days. EXERCISE 16.—Page 69. I. 26. 11. 36. 2. 21. 21. 41. 12. 97. 3. 32. 22. 570. 13. 48. 4. 33. 23. 92. 14. 102. 5. 20. 24. 1100. 15. 210. 6. o. 25. 94. 16. 159. 7. 26. 26. 314. 8. 17. 300. 20. 18. 700. 27. 460. 9. 18. 28. 48. IO. IO. 19. 80. 29. 85. 20. 0.

EXERCISE 19.—Page 82.

30. 74.

| 1. 312. | 8. 221. | 15. 153. |
|---------|-----------|-----------|
| 2. 431. | 9. 185. | 16. 252. |
| 3. 342. | 10. 4321. | 17. 232. |
| 4. 132. | 11. 1231. | 18. 142. |
| 5. 231. | 12. 3102. | 19. 131. |
| 6. 212. | 13. 373. | 20. 121. |
| 7. 121. | 14. 184. | 21. 4623. |

ANSWERS.

5451 dollars. 14689 dollars. 734481 dollars. 228984 men. 273249 yards. 980019 pounds. 372480 plants. 1358112 letters. 349860 pounds. 53360 feet. .0824 plums. 9232 rails. 0248 soldiers. o8 miles. 1712 men. 52160 feet. 5680000 miles 1214 cents. 400 cents, 4I. ' 570. 12. 100. 4.

14.

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3. 2.

2.

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3.

45. 105. 33. 2032. 49. 2052. 31. 2042. 47. 2025. EXERCISE 20.—Page 83. 1. 913-2. 17. 814744-6. 2. 14516-4. 18. 772927-4. 3. 28823-2. 19. 411869-2. 4. 5786-3. 20. 561436-6. 5. 52954-3. 21. 680078-1. 6. 82304-6. 22. 731040-4. 7. 30411-2. 23. 5;8129-5. 8. 79965-4. 24. 841484. 9. 339758-1. 25. 568345-5. 10. 877022-3. 26. 537720—5. 27. 822311—5. 11. 835581-1. 12. 560054--6. 28. 384597-2. 13. 1046518-2. 29. 710443. 14. 485109-3. 30. 589684-9. 15. 41243-5. 31. 115993. 16. 124715-3. EXERCISE 21.—Page 85. 1. 731-6. 8. 7-12934. 2. 8317-4.

22. 34.

23. 44.

24. 43.

25. 42.

25. 52.

27. 62.

28. 42.

29. 71.

30. 92.

31. 42.

32. 51.

7. 5137-12.

32. 944202-10. 33. 3749195-9. 34. 192850-5. 35. 297691-3. 36. 389751-9. 37. 779108-10. 38. 490939-2. 39. 9007 times. 40. 7008 times. 41. 6703. 42. 6324. 43. 8232 times. 44. 5531. 45. 4205 times. 46. 6132 times. 15. \$108.62. 9.3-92. 16. \$3.12. 3. 61-92. 10. 37-214. 17. \$4610. 4. 73-1. 11. 74-321. 18. 70 cents. 5. 9-7312. 12. 306. 6. 839-16.

13. 30000.

14. 60-60600.

ANSWERS.

35. 1051.

36. 1052.

37. 1054.

38. 252.

39. 489.

40. 218.

41. 324.

42. 224.

43. 135.

44. 155.

- - 19. 8610 bills.
 - 20. 73107 dollars.

xiii

48. 1507.

49. 4686.

50. 1237.

51. 1213.

52. 1207.

53. 1109.

55. 3439.

55. 5416.

58. 4105.

57. 7432966.

5). 14469. 6). 5092103.

54. 10856.

ANOWERS.

| EXERCISE | 22Paro | 05 |
|----------|--------|----|
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| 1. 2448 bricks.19. 410; 816 lbs.38. 25 cents.2. 23527 dollars. 23527 dollars. $20. 16; 48; 288$ kts. $39. 118$ buttons.3. 52126 dollars. $22. 23; 92; 276$ yds. $1053 Z's.$ $4. 15937 acres. $23; 27; 36$ pounds. $40. 3159$ Y's; $5. 15037$ acres. $23; 27; 36$ pounds. $41. 786$ dollars. $6. $2126495.$ $24. 11; 33$ feet. $22. 147$ dollars. $7. 33514$ acres. $26. 1264$ dollars. $44. 469$ coats. $9. 5292$ hills. $27. 1812$ dollars. $44. 469$ coats. $10. 7968516.$ $27. 1812$ dollars. $46. 447$ barrels. $11. 78134159.$ $29. 199$ hats. $46. 447$ barrels. $12. 30784$ dollars. $30. 159$ barrels. $46. 447$ barrels. $14. 2172; 1448;$ $32. 125$ dollars. $49. 375$ dollars. $15. 173; 248; 1588.$ $34. 99$ miles. $51. 6236$ dollars. $16. 128; 191; 1654.$ $35. 213$ acres. $51. 6236$ dollars. $17. 961; 1922; 3844.$ $37. 15$ dollars. $54. 379$ gallons. $18. 33; 99; 198$ gals. $37. 15$ dollars. $55. 11500000$ miles. |
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|--|

EXERCISE 23.-Page 91.

| 1. 21. | 1 | |
|-----------|-----------------|------------------|
| | 20. 1407. | 1 |
| 2. 23. | 21 1007 | 39. 252384-2534. |
| 3. 24. | 21. 1025. | 40. 201. |
| | 22. 426. | -70. 201. |
| 4. 21. | 22 242 | 41. 134. |
| 5. 214. | 23. 243. | 42. 785 |
| 5. 2.4. | 24. 162. | + 105 |
| 6. 234. | 25. 452. | 43. 54. |
| 7. 235. | -2. 45 | 44. 617. |
| | 26. 664. | 14. 017. |
| 8. 324. | 27. 777. | 45. 1190. |
| 9. 243. | | 46. 243. |
| 10 212 | 28. 1802. | 47 -43 |
| 10. 342. | 29. 1945. | 47. 2371. |
| 11. 227. | -3943. | 48. 1655037. |
| 12. 218. | 30. 4372. | 10 219-5 |
| | 31. 6203. | 49. 34807. |
| 13. 229. | 22 0016 | 50. 14076. |
| 14. 257. | 32. 9216-543. | 51. 1011. |
| | 33. 5679-350. | 5-1 1011. |
| 15. 228. | 34. 12474-401. | 52. 463. |
| 16. 207. | 57. 124/4-401. | 53. 7289. |
| 17. 1205. | 35. 21175-499. | 55 7 = 6 g t |
| 17. 1205. | 36. 81987-39. | 54. 394. |
| 13. 1324. | 27 5729. | 55. 7071. |
| 19. 1523. | 37. 771849-173. | 56. 28co4. |
| - 54 5+ 1 | 38. 474536-523. | 5 |
| | | 57. 1172. |

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xiv

5 cents. 18 buttons. 159 Y's; 053 Z's. 36 dollars. 17 dollars. dollars. g coats. 3 barrels. 7 barrels. 41 months. 5 baskets. dollars. bushels. 6 dollars. miles. 5 dollars. gallons. boooo miles,

384-2534.

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037. 7. 6.

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ANSWERS.

58. 3645-2867. 66. 9830291-7000. 74. 7973-23. 59. 4629. 67. 5006284. 60. 346. 75. 927---80. 63. 4000059. 61. 19214-542. 76. 34959-716. 69. 5748362. 77. 27959-333. 62. 34045-1098. 70. 2779458-5888. 78. 14959-966. 63. 1343-1652. 71. 6438192-73401. 79. 285340-4322. 64. 12207-445. 72. 13786926. 80. 76360-33498. 65. 529-2228. 73. 537-3.

· EXERCISE 24.-Page 95.

| 1. $31207-1$.
2. $16695-17$.
3. $519225-11$.
4. $20914-11$.
5. $167988-17$.
6. $33721-18$.
7. $263945-18$.
8. $17529-37$.
9. $128795-17$.
10. $145264-23$.
11. $105911-25$.
12. $111263-21$.
13. $111215-27$.
14. $130136-25$.
15. $$258$.
16. 86 . | 17. 213.
18. $\$864.$
19. $436-1.$
20. $83-49.$
21. 76-30.
22. 7-491.
23. $\$8600.$
24. $31-2946.$
25. $3697-2.$
26. $327-311.$
27. $386-58.$
28. $\$316.$
29. $21-320.$
30. $10-11227.$
31. $179-452.$ | $\begin{array}{cccccccccccccccccccccccccccccccccccc$ |
|---|---|--|
|---|---|--|

EXERCISE 25.—Page 96.

1. \$97. 12. 83 years. 2. \$25. 22. \$197. 13. \$237. 3. \$8. 23. 425 miles. 14. 3864. 4. 315 pages. 5. 74 ('-ys. 24. 131. 15. 77 battalions. 25. 47 cartridges. 16. 646. 6. \$35. 26. 5280 feet. 17. 1872. 7. \$4. 27. 24964. 18. 894 pounds; 8. \$237. 28. 1097 bales. 312 pounds. 9. 336 hams. 29. 23 pounds. 19. 23 hhds. 1.). 365 questions. 30. 256 balls. 20. \$13. 11. 2765 days. 31. 3906250. 21. 24 trips; 71. 32. 792.

xv

| 1. $\$10394$.24. 792 .46.8 oranges.2. $\$825$.25. 93277 .46.8 oranges.3.Houses; $\$1675$.26.24.48.12 days.4.1428.27.17 books.49.5 weeks.5.354,177,118.28.119 miles;50.15 days.6.207.799. $\$1998$.51.37.52.217 hats.7.306.29. $\$1998$.52.217 hats.53.A owes B;9. $\$2015$.31.781 cases.54. $\$1080$.\$212.10.146299—1.32.\$9.33.1903.55.\$3.12.4320 sheets.34. $\$1704$.56. $\$2277$.13. $\$182$.35. $\$36$.57. $\$6750$.14. $\$2028.78$.36.39.58. $\$8.$ 16.75 yards.38. $$133$. $60.$ $15.$ 19.91.41. $\$3.60.$ $63.$ $24.$ $$162.$ 19.91.41. $\$3.60.$ $63.$ $24.$ $$162.$ 19.91.41. $\$3.60.$ $63.$ $24.$ $$16.62.$ 20.119 weeks.42. 33 days. $64.$ 31 calves.21. 723 gallons.43. $\$336.$ $67.$ 21 yards.22. $\$5.$ $64.$ $80.$ $67.$ 21 yards. | | Ų | |
|---|--|--|---|
| | 3. Houses; \$1675.
4. 1428.
5. 354, 177, 118.
6. 207.
7. 306.
8. 156 times.
9. \$2015.
10. 146299-1.
11. \$1663.
12. 4320 sheets.
13. \$182.
14. \$2028.78.
15. 132 men.
16. 75 yards.
17. 897.
18. \$15444.
19. 91.
20. 119 weeks.
21. 723 gallons.
22. \$5. | 25. 93277. 26. 24. 27. 17 books, 28. 119 miles; 595 miles. 29. \$1998. 30. \$25175. 31. 781 cases. 32. \$9. 33. 1903. 34. \$1704. 35. \$36. 36. 39. 37. \$15. 38. 5133. 39. 36405 bush. 40. 162. 41. \$3.60. 42. 33 days. 43. \$336. 44. \$465.50. | 47. 9 hours.
48. 12 days.
49. 5 weeks.
50. 15 days.
51. 37.
52. 217 hats.
53. A owes B;
\$212.
54. \$11080.
55. \$3.
56. \$2277.
57. \$6750.
58. \$8.
59. \$3.
60. 15.
61. 20 hours.
62. \$18.62.
63. 24 months.
64. 31 calves.
65. \$70.
66. 3 tons. |

EXERCISE 26.—Page 99.

EXERCISE 27.—Page 104.

| 1. 20.
2. 42.
3. 24.
4. 96.
5. 34.
6. 24.
7. 36. | 8. 18.
9. 51.
10. 64.
11. 21.
12. 10.
13. 3.
14. 4. | 15. 20.
16. 10.
17. 4.
18. 17.
19. 8.
20. 0. |
|--|---|---|
|--|---|---|

EXERCISE 20.—Page 110.

(b

| 2.
3. | 23.
4.
61.
192. | 5. I.
6. 37.
7. 2.
8. 21. | 9. 32.
10. 17.
11. 126. |
|----------|--------------------------|------------------------------------|-------------------------------|
| | | 1 | 12. 14 feet. |

xvi

| | ANSWERS. | xvii |
|--|--|---|
| | EXERCISE 31.—Page 1 | 15, |
| 1. 90.
2. 360.
3. 12600.
4. 1134.
5. 504.
6. 360.
7. 20160.
8. 480.
9. 438480 | 10. 43680.
11. 1330732.
12. 9744.
13. 155232.
14. 72120.
15. 469170.
16. 4149360.
17. 441000. | 18. 68640.
19. 1591744.
20. 4200, 210,
168, 140,
120, 105.
21. 300, 150, 100,
75, 60, 30,
15, 6, 3. |
| | EXERCISE 33.—Page 12 | 1. |
| (a) 1. $\frac{6}{8}; \frac{9}{12}; \frac{1}{12}; \frac{1}{16}; \frac{13\frac{1}{3}}{16}$ | $\frac{1}{2}\frac{5}{0}; \frac{3}{40}; \frac{24}{32}; \frac{45}{60}, 3. \frac{10}{20};$ | $\begin{array}{c} \frac{5}{2}5; \ \frac{1}{2}6; \ \frac{1}{2}6; \\ \frac{2}{2}5; \ \frac{5}{3}0; \ \frac{5}{2}6; \\ \frac{4}{2}5; \ \frac{5}{3}0; \ \frac{5}{4}5. \end{array}$ |
| $ \begin{pmatrix} j \\ j \end{pmatrix} \mathbf{I}. \frac{3}{5}, \frac{2}{5}, \frac{3}{5}, \frac{3}{4}, \\ 2. \frac{7}{5}, \frac{5}{6}, \frac{1}{3}, \\ 3. \frac{5}{7}, \frac{9}{11}, \frac{7}{7}, \\ 4. \frac{7}{8}, \frac{3}{10}, \frac{1}{12} \end{pmatrix} $ | 5. $\frac{1}{1}\frac{3}{6}$, $\frac{1}{6}$, $\frac{1}{100}$.
6. $\frac{1}{10}$, $\frac{9}{100}$, $\frac{3}{23}$.
7. 1. 7. 8. | 9. $\frac{7}{1_3}$, $\frac{1}{3}$, $\frac{1}{1_7}$,
10. $\frac{1}{3_3}$, $\frac{1}{3}$, $\frac{1}{3_7}$,
11. $\frac{2}{3}$, $\frac{1}{2}$, $\frac{2}{3}$, $\frac{4}{4}$. |
| | EXERCISE 34.—Page 123 | |
| $ \begin{array}{c} (a) \ \mathbf{I}. & \frac{1}{1-\frac{3}{4}}. \\ 2. & 7. \\ 3. & 7. \\ 4. & 6\frac{1}{5}. \\ 5. & 3\frac{4}{5}. \\ 6. & 5\frac{3}{4}. \\ 7. & 5\frac{1}{6}. \\ 8. & 4\frac{7}{5}. \\ 9. & 6\frac{3}{7}. \\ 10. & 7\frac{1}{8}. \\ 11. & 7\frac{1}{2}. \\ (b) \ \mathbf{I}. & \frac{20}{5}. \\ 2. & \frac{37}{4}. \\ 3. & \frac{27}{4}. \\ 4. & \frac{5}{5}. \\ 5. & \frac{10}{2}. \\ \end{array} $ | $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$ | $\begin{array}{c} 34. \ 6\frac{1}{6}, \\ 35. \ 4\frac{1}{7}, \\ 36. \ 6, \\ 37. \ 4, \\ 38. \ 14\frac{8}{3}, \\ 39. \ 14\frac{1}{3}, \\ 40. \ 17\frac{1}{9}, \\ 41. \ 16\frac{3}{3}, \\ 42. \ 28\frac{1}{13}, \\ 42. \ 28\frac{1}{13}, \\ 43. \ 31\frac{1}{12}, \\ 44. \ 6\frac{12}{9}, \\ 44. \ 6\frac{12}{9}, \\ 16. \ \frac{58}{9}, \\ 16. \ \frac{58}{9}, \\ 19. \ \frac{109}{9}, \\ 20. \ \frac{59}{9}, \end{array}$ |

oranges. nours. days. veeks. days.

hats. wesB; 2. 080.

77. 50.

ours. 52. onths. lves.

s. rds.

et.

| xv. i | AN | SWERS. | |
|--|---|--|---|
| $\begin{array}{c} 24. & \frac{7}{9}.\\ 25. & \frac{8}{3}.\\ 26. & \frac{8}{7}. \end{array}$ | 27. $\frac{5}{4}$.
28. $\frac{5}{8}$.
29. $\frac{1}{2}\frac{3}{4}$.
30. $\frac{2}{7}\frac{7}{2}$.
31. $\frac{2}{5}\frac{8}{5}$.
32. $\frac{9}{4}^{5}$. | $\begin{array}{c} 33 \cdot \frac{37}{7}, \\ 34 \cdot \frac{1}{8} \frac{1}{3} \frac{1}{8}, \\ 35 \cdot \frac{969}{19}, \\ 36 \cdot \frac{6379}{19}, \\ 37 \cdot \frac{734}{9}, \end{array}$ | 38. $\frac{2 \pm n}{2}$.
39. $\frac{10 \times 28}{3}$.
40. $\frac{18 \times 5}{3}$.
41. $\frac{8 \times 5}{7}$.
42. $\frac{4 \times 60 \times 8}{11}$. |
| (c) 1. 12 days;
5 days. 2. 6 ounces;
11 ounces;
9 ounces. 3. \$²/₈; \$¹/₁. | $\begin{array}{c} 5 & \frac{4}{3} \\ 6 & \frac{7}{5} \\ 7 & \frac{7}{9} \\ 8 & \frac{9}{1} \frac{1}{1} \\ 9 & \frac{2}{7} \\ \end{array}$ | | IO. $\frac{4}{9}$; $\frac{9}{2}$;
II. $\frac{71}{12}$; $\frac{10.4}{934}$,
I2. $\frac{11.5}{15}$; $\frac{34.5}{932}$,
I3. $\frac{16.5}{95}$; $\frac{65.5}{950}$,
I4. $\frac{20.3}{93}$; $\frac{24.5}{94}$; $\frac{80.9}{95}$,
I5. \mathcal{R}_{14}^{14} , |
| E | XERCISE 32 | 5.—Pago 126. | |

| $\begin{array}{c ccccccccccccccccccccccccccccccccccc$ | $\begin{array}{c} \frac{49}{2}, \frac{49}{2}, \frac{49}{2}, \frac{49}{2}, \frac{49}{2}, \frac{49}{2}, \frac{49}{2}, \frac{59}{2}, |
|---|--|
|---|--|

EXERCISE 37.-Page 130.

| I. $7\frac{1}{3}\frac{2}{5}$. |) 77 | |
|---|------------------------------|--------------------------|
| 2. $32\frac{1}{36}$. | $15.2\frac{2}{45}$. | 29. 821 yards. |
| 3. $14\frac{5}{6}$. | $16. \frac{2}{25}.$ | $3^{-1} - \$96_{1}^{-1}$ |
| 4. 404. | 17. 8 135. | 31. \$293. |
| 5 27 | 18. 240. | 32. \$192. |
| 5. $3\frac{7}{8}$.
6. $6\frac{3}{2\frac{3}{8}}$. | 19. 523 acres. | 32. 4195. |
| 0. 028. | 20. 13 3 vards. | 33. $69\frac{90}{63}$. |
| 7. 4047. | 21. $\$14\frac{61}{72}$. | 34. $182\frac{41}{66}$. |
| 8. $36\frac{9}{14}$. | 22. $5\frac{1}{3}$ pounds. | 35. 101444. |
| $5 \cdot 57 \frac{1}{12}$ | 23. 243 gallons. | 36. 28. |
| IO. $22\frac{7}{16}$. | 24. $$208\frac{1}{36}$. | 37. \$140-1 |
| 11. 30.4 | 24. \$20035. | 38. \$137. |
| 12. $28\frac{41}{60}$. | 25. \$1 4 . | 39. $13\frac{1}{10}$. |
| 13. $31\frac{1}{2}\frac{1}{4}$. | 26. $16\frac{19}{24}$ miles. | 40. 881. |
| 14. $6_{24\frac{7}{8}}$. | $27.712\frac{1}{4}$ vards. | 41. 20147 lbs. |
| 4. 0243. | 28. 423 fect. | 42. $\frac{9}{40}$. |
| | • | 14. 40. |

٢ ANSWERS. 38. 240. EXERCISE 40.-Page 137. 39. Lozs. 10. 1803. I. 10. 10. \$1.30%. 19. \$15.95. II. 8704. 2. 121. 11. \$1.361. 2. 10008. 3. 18. 20. 1953 cords. 12. \$351. 21. \$10.60 17. 4. 137. 13. 40 miles. 22. \$313. 5. 28. 14. 401. ?; P: 6. 38. 23. 147. 15. \$224. 16. \$10⁷/₂₀. 7; 154. 24. \$231. 7. 2381. 5; 345. 8. I⁴₁₁. 25. \$5734. 17. 381 cords. 5; 655. 9. 161 cts. 18. \$31.25. 26. 42 knots. 3; 244; 802. 4, EXERCISE 41.-Page 140, I. 3. 11. 11. 2. 37. 20. 10 mile. 12. 933 yards. 21. 55 pieces. 10. 3. 4. 13. 46 hours. 22. 9^p/₁₁; 4. 3. 5, 120. 14. 368 times. 5. 21 times. 262; 5, 800. 15. 38%. 6. 8 times. 69⁹ pounds. 16. 30⁴/₅ pounds. 23. 61 months. 7. 6. 17. 12₁₃ hours. t; Walk-8. 312. 24. 8 days. 18. 50 scarfs. 25. 400 weeks. 9. 1-9. 19. 44 bottles; feet. 26. 25 mile. 10. \$ times. ⁺[♀] pint. \$ \$ 0, \$ 120. EXERCISE 42.-Page 142. $\begin{array}{c} I \cdot \frac{9}{20} \\ 2 \cdot \frac{1}{35} \end{array}$ 7. $\frac{1}{3}$. 8. $1\frac{1}{6}$. 13. 824. 19. 17. 14. 137. yards. 20. II143. 3. 25. 9. 8 - 1 - . 15. 103. 1. 4. 15. 21. 581. IO. 7. 16. 1-7.9 5. $\frac{91}{39}$. 6. $\frac{10}{37}$. • 22. 3. II. 710. 17. 8. 23. 13. 12. 13-9 18. 11. 24. 124. EXERCISE 43.—Page 144. 4. I. I.5. 9. 80 lbs. 2. 67 17. 24. 10. 191. 1.8. 18. 4. 3. 7. 11. \$140. 19. \$15. 4. 8. 12. \$30. 20. \$35. 5. 1. 6. 1. 13. 32 ounces. 14. $5_{1\frac{1}{1}\frac{8}{9}}$. 21. 5 times. lbs. 7. 11. 8. 24 pk. 22. 12 years. 15. \$308. 23. 21. 16. 3 times. 24. 10.

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| 25. 317, \$100.
26. \$1000. | 31. 1 <u>31</u> days.
32. 5 days. | 37. 8. |
|--|--------------------------------------|--------------------------------|
| $\begin{array}{c} 27. \ \frac{1}{36}, \ \frac{1}{13}.\\ 28. \ \frac{1}{11}. \end{array}$ | 33. 124 hours.
34. 134 days. | 38. 131 min.
39. 241 min. |
| $\begin{array}{c} 29. \frac{4}{21}. \\ 30. \frac{1}{8}. \end{array}$ | 35. # day.
36. 6 days. | 40. \$1912.50.
41. 60 feet. |
| | Joi o days. | 42. 150 feet |

EXERCISE 44.—Page 150.

| 1. $$174.55$.
2. $$149.35$.
3. $$315.22$.
4. $$214.96$.
5. $$1370.68$.
6. $$1318.95$.
7. $$2375.85$.
8. $$6516.03$.
9. $$1099.52$.
10. $$830.10$.
11. $$435.09$.
12. $$384.87$.
13. $$235.93$.
14. $$32.57$.
15. $$197.38$. | \$9793.61. \$8838.81. \$28.47. \$135. \$197.28. \$784. \$51975. \$1564.50. \$125.12. \$25839. \$864 books. \$7630 times. \$3.16. | 31. 16 cts.
32. 581 months.
33. 15 cts.
34. 105 pounds.
35. \$35845.35.
36. \$92.85.
37. \$129.05.
38. \$12.12.
39. \$530.60.
40. \$48.60; goc.
41. 197 lots.
42. \$60.33.
43. \$53.55.
44. 32800 pieces.
45. \$7.52. |
|--|--|---|
|--|--|---|

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EXERCISE 45.—Page 155.

| 58; 1092 far. 5616d.; 13435d. 724695 far. £383; £478. 14814 far. £22 5s. 2d. | 9. 203 far.
10. 20163 far. | \$. £39 115. 8⁴/₄d. 4. £3001 105. 10d. 12. 21133 sixpences. 13. £46 125. 3d. 14. 316 boys; £4 05. 11d. |
|---|-------------------------------|---|
|---|-------------------------------|---|

EXERCISE 46.—Page 157.

| 1. $\pounds 27$ 115. 6d. | 6. $\pounds _{4825}$ 5s. $g_{4}^{\alpha}d$. |
|---|---|
| 2. $\pounds 18$ 175. 8 $\frac{1}{4}$ d. | 7. $\pounds _{99153}$ 10s. $z_{4}^{\alpha}d$. |
| 3. $\pounds 63$ 165. 2d. | 8. $\pounds _{66807}$ 9s. 8d. |
| 4. $\pounds 66$ 25. 1 $\frac{1}{4}$ d. | 9. $\pounds _{55862}$ 6s. |
| 5. £928 8s. 91. | 9. $\pounds 55862$ os. 4d.
10. $\pounds 50650$ 6s. $5\frac{3}{4}$ d. |

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EXERCISE 47.-Page 158.

| 1. £8 175. 5d. | 4. £7148 118. 81d. | 7. £3100 05. 11d. |
|------------------|--------------------|--|
| 2. £9 85. rod. | 5. £3 28. 01d. | 8. £5960 148. 3 ³ / ₄ d. |
| 3. £94 15s. 5≩d. | 6. £6 9s. 71d. | 9. £45 16s. 3d. |

EXERCISE 48.-Page 160.

| 1. £12 198. 101d. | 7. £132 16s. 01d. | 13. £4630 195. 5¾d. |
|-------------------|---------------------|----------------------------------|
| 2. £37 138. 5d | 8. £198 3s. 104d. | 14. £76 4s. 9¾d. |
| 3. £6 15. 2‡d. | 9. £840 115. 6d. | 15. £15153 12s. 51d. |
| 4. £449 135. 9d. | 10. £1134 135. 11d. | 16. £1107 8s. 6d. |
| 5. ±144 75. 4d. | 11. £498 135. 6d. | 17. £22 155. 10d.
18. £52 15. |

EXERCISE 49.—Page 163.

| t. £14 9s. 8 ¹ d. | 8. £794 18s. ofd. | 12. 7; 11; 16; 108. |
|-------------------------------------|---|------------------------|
| 2. £154 15. 9d. | 9. \$53 12S. 51d.; | 13. 8 men. |
| 3. £149 175. 11d. | | 14. 12 shawls. |
| 4. £73 175. 83d. | £69 4s. 3 ¹ / ₂ d.; | I 5. 1. |
| 5. £3 198. 71d. | £73 os. 01d. | 121 times. |
| 6. £83 155. 04d.
7. £3 195. 14d. | 10. £2 105. 71d. | 17. 1200 purses. |
| 1. 23 195. 180. 1 | 11. £4 10s. | 18. 13 times; £635.31d |

EXERCISE 50.-Page 166.

| (b) 2. 3 oz. 12 dwt. 18 grs. | 16. 8 cwt. 31 lbs. 10 oz. |
|--------------------------------|---|
| 3. 28968 grs. | 17. 24 T. I cwt. 71 lbs. |
| 4. 173 lbs. 7 oz. 6 dwt. 16 | 18. 17 T. 55 lbs. |
| grs. | 19. 403 T. 17 cwt. 55 lbs. |
| 5. 58321 grs. | 20. 689 lbs. 8 oz. 16 dwt. |
| 6. 3420 grs. | 21. 6 lbs. 10 oz. 10 dwt. |
| 7. 2 lbs. 4 oz. 6 drs. 1 scr. | 22. 9 cwt. 89 lbs. |
| 8. 13465 powders. | 23. 890 parcels. |
| 9. 504 packages. | 24. 48 ounces. |
| 10. 5684 oz. | 25. 27 bags. |
| 11. 3 CWt. 60 Ibs. 7 oz. | 26. 65 forks; 1 oz. 5 dwt. |
| **• 3 1. 13 UWL. 59 IDS. | 27. 2 cwt. 125 lbs. |
| 13.91.0CWL 17 IDS. | 28. 24. |
| 14. 45 1. 4 Cwt. 57 lbs. 2 oz. | 29. 50. |
| If IOM IDA MUSE OIL | 30. 5. |
| | 31. 2 lbs. 4 oz. 9 dwt. $1\frac{11}{13}$ grs. |

3: min.
13: min.
24: min.
\$1912.50.
60 feet.
150 feet.

cts. 1 months. cts. 5 pounds. 5845.35. 2.85. 29.05. 2.12. 30.60. 3.60; goc. lots. -33. -55. 00 pieces. 2.

. 8³4. os. 10d. (pences. 3d. ; 1d. izzí

| 32. 51 lbs. 11 oz. 18 d | wt i an tr |
|---|--|
| -0 gis. | |
| 33. 3 T. 56 lbs 1 - 9 - | 55000 |
| 34. 3 lbs. 1 oz. 8 dwt. 14g | 39. IO 07 0 dust |
| 35. 884 [‡] times. | rs. 40. IT. 8 Cwt 10 11 grs. |
| 36. 21 lbs. 61 oz.; | rs. 40. 1 T. 8 cwt. 10 lb. $14\frac{1}{2}$ oz. 41. 18 cwt. 75-7 lb. $14\frac{1}{2}$ oz. |
| 6 Swt 702 1 | 41. 18 cwt. $75\frac{7}{11}$ lbs.;
23 T. 5 cwt |
| 6 cwt. 723 lbs. | $\begin{array}{c ccccccccccccccccccccccccccccccccccc$ |
| EXEDUIG | 7- 207. |
| 13. 5 yds. 2 ft. 9 in. | E 51.—Page 173. |
| 14. 45 vds of | 26. 42 sa mi |
| 14. 45 yds. 2 ft. 5 in. | 26. 42 sq. mi. 142 ac. 20 sq.
rds. 20 sq. vda 6 |
| 15. 1365 inches. | |
| 16. $\frac{1}{17}$ of a mile. | |
| 17. 221 cords. | 27. 3 ft. 63 in. |
| 18. 770 fathoms. | 28. 16 feet. |
| 19. \$56. | 29. 1 ac. 141 sq. rds. 4 sq.
yds. 4 sq. ft |
| 20, 9 sq. rd , 13 sq. rda | |
| sq. ft. 3. sq in. | |
| 21. 14 inches. | J. S III. A fur an ada |
| 22. 933 sq. yds.; | 32. 400 ac. 38 sq. rds. |
| \$16.80. | 33. 13 136. |
| ² 3. 39 suits. | 34. 45 yds.; 333 ft. |
| 24. 15587 mi - 5 | 35. 44880 ft. |
| 24. 15587 mi. 7 fur. 33 rds. | $36. \frac{1}{256}$. |
| ~ 100 3 111. | 37. 100 acres. |
| 25. 34 ² / ₇ times. | 38 108 ap - C |
| EVEDOLOD | 38. 198 ac. 1263 sq rds. |
| 8. 315260001 astis | ² .—Page 177. |
| | 19. 1 wk. 2 da. 4 hrs. 45 min.
59 sec. |
| 2592000; 2678400; | 50 see |
| 2505600; 604800; | 59 sec.
20. 54. |
| 86400; 3600 sec. | |
| 9. 525600; 527040; | 21. 5 da. 17 hrs. 22 min. |
| 44040; 43200: | |
| 44040; 40320; | 23. 66 da. 17 hrs. 10 min.
24. 4382 da. 21 hrs. |
| 131040; 132480 min | |
| 10912 seconds | $56\frac{2}{5}$ sec. |
| II. IO hrs. AT min an and | 25. $\frac{460}{13}$; $\frac{1}{38}$; $\frac{2}{273}$.
26. 6 hrs. $\frac{1}{38}$; $\frac{2}{273}$. |
| 12. 201 days. | |
| 13. 2 wks. 5 da. 7 hrs. 9 min. | 27. 2 min. 15 ⁵ / ₇ sec. |
| 14. 313 6. | |
| 15. 5 da. 54 min. | 28. 11 hrs. 54 min. 40 sec.
29. 5 hrs. 42 ^e min.; |
| 16. 354 days. | |
| 17 to minut | 177 min. to 4 P.M. |
| 17. 10 minutes. | |
| 18. ²⁹ / ₈₄ . | |
| • | 32. Saturday, at 10.20 A.M. |
| | |

(a

(6

(*a*)

XXII

16 grs.

. 20^{4 p}/₂₁ grs. o lb. 14⁴/₂ oz. · lbs. ; 19³⁷⁷/₅₃₂ lbs.

••

2 ac. 20 sq. ls. 6 sq. ft.

rds. 4 sq. 18 sq. in. rds. rds.

•

q rds.

•45 min.

min. S sec. min. 45 min.

hrs.

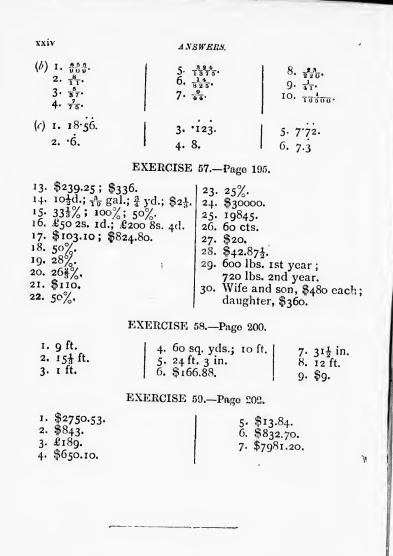
o sec.

Μ. 1. A.M_

| ANSWERS. | | XXII | |
|--|---|---|-------------|
| ز ` | EXERCISE 5 | 3.—Page 180. | |
| 9. 480 dozen.
10. $1091\frac{7}{73}$.
(11. 55 pints.
12. 43 bush. 1 pl
13. 3 hhds. 8 gal.
14. \$90.56.
15. 364 gals.
16. \$511.87 $\frac{1}{2}$.
17. 4 loads.
18. $\frac{21}{84}$.
19. 41 gals. 3 qts | «. 3 qts.
2 qts. 1 pt. | 20. \$3.80.
21. \$1.05.
22. $\frac{1}{3}$.
23. 30 gals.
24. 14 $\frac{3}{4}$ qts.
25. 36 barrels; 42
26. 169 $\frac{3}{4}$ bush.
27. 922 $\frac{1}{7}$ bush.
28. 171 bush. 3 qt
29. $\frac{1}{75}$.
30. 204 $\frac{1}{75}$ barrels. | |
| E | XERCISE 54 | | |
| 7. 2450 score.
8. 62500 boxes.
9. \$720.
10. 80 brls.; \$47
11. 1152 books.
12. 300 stones.
13. 115 brls.; \$18
14. $\frac{1}{2}$. | 0.40. | 15. 416 $\frac{3}{4}$ doz.
16. $\frac{3}{4}$; $\frac{9}{10}$; $\frac{4}{5}$.
17. \$13.20.
18. $83\frac{1}{4}$ reams.
19. \$12.
20. \$213.16 $\frac{1}{2}\frac{9}{6}$.
21. 2970 volumes. | 26: 2 ar |
| 14. $\frac{1}{2}$. 22. 18.5 doz.; \$726; 2 ac.
EXERCISE 55.—Page 189. | | | |
| (a) I. $\frac{p}{200}$; $\frac{q}{100}$; 12 | $\frac{1}{5}$; $68\frac{3}{16}$,
3. $\frac{19}{20}$; $\frac{7}{8}$; $\frac{7}{1}$ | 2. $\frac{3}{2}$; $\frac{9}{2}$; $\frac{17}{2}$. | <u>1</u> 6. |
| (δ) 1. 65.046 ch.
2. 549.375 ac.
3. '0003764.
4. 5.6857 ac.
5. 5.937 lbs.
6. 99.96154 miles
7. '850955. | | 8. \$108.675.
9. 391.05 ft.
10. 08.
11. 15; 3650; 10020
12. 4'9834; 24.8266
13. '04026; '01274; | : .6244 |
| EX | ERCISE 56 | -Page 193. | |
| $(a) 1. \cdot 625.$ 2. $\cdot 0625.$ 3. $\cdot 85.$ 4. $\cdot 52.$ 5. $\cdot 35.$ 6. $2 \cdot 625.$ | 7. '024, 8. '03906; 9. 24'6, 10. '484375 11. '11584, 12. 1'5008, | 5. 15. 123.
16. 23809
17. 624. | 5. |

ANSWERS

iii



l

 7.72. 7.3

car; year. , \$480 cach; 50.

7. 31½ in. 8. 12 ft. 9. \$9.

3

. o.

ANSWERS.

EXAMINATION PAPERS .- Page 203.

PAPER I.

| | 17.
\$1200.
2813 . | 8. 288 ac.
9. \$3561;\$4022.
10. \$89.11. |
|---|---|---|
| | PAPER II. | |
| 1. 1854.
2. 14839.
3. CXIV;
XMCMLXXXIII.
4. 2880. | 5. \$2000.
6. 60;
\$2.50.
7. 7 gals. | 8. A \$360; B \$480.
9. 3 times.
10. \$18333 ¹ / ₃ .
11. 282 ac.
12. \$550. |

PAPER III.

| 1. 197'325. | 3. 70.
4. $5\frac{1}{3}$ ft.
5. $3\frac{1}{8}$ hrs. | 6. 21 brls. |
|-------------|---|------------------------------------|
| 2. 800; | 4 4 | 0. 21 0115. |
| • | 4. 5 § II. | 7. 7-4-8 |
| 200. | 5. 21 hrs | 7. $7\frac{48}{140}$.
8. \$16. |
| | J. 38 113. | 0. 210. |

PAPER IV.

| 1. •0122. | 5. 4 hrs. | 8. A 315 ac. |
|-------------|-------------------|------------------------|
| 2. 323 hrs. | 6. •432. | B $127\frac{1}{2}$ ac. |
| 3. \$90.70. | 7• 7 . | C $127\frac{1}{2}$ ac. |
| 4. \$68.60. | | 0 12/1 ac. |

PAPER V.

| bo5100 gals. I lb. 3 oz. 8 dwt. 21 grs. ⁷T. | 6. 8 min. to 11 P.M.; | | Henry \$31';
George \$130;
Fred \$100.
\$240. |
|---|-----------------------|--|--|
|---|-----------------------|--|--|

PAPER VI.

| 1. 4840 sq. yds.; | 4. C \$1050; | 7. A \$75: |
|------------------------|------------------------|------------------------|
| 7 5. | D \$4950. | 7. A \$75;
B \$111. |
| 2. 6·53055.
3. 196. | 5. $2\frac{1}{2}$ hrs. | 8. 16 men. |
| J. 1901 | 6. \$4.80. | 9. 100 gals. |

XXV

