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## 

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The only Idaition propired as an Introductiony. Teet Boon to Kason's Grammar.
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To the President and Members of the County of EIgin Toach-s Ansioviation:
In accordance with a motion passed at the inat regular meoting ci the Association, appointing the undersigned a Committee to comsider the respective merits of different linglish Grammary, witho fiew to suggent the mont suitable one for Publio schoole, wit the leave to report, that, after fully compare that "Millary Emintong Language Irescons! " is best adapted to the wantis of funfor pap"' and would urge its authorization on the Governments and its fantoduotion into our Public Schools.
St Thomas, NOV. SOth, 1878.

> A. F. RUTLER O. Ingpector.
> J. MaHisAN, TOWa Inopeotor.

It was moved and seconded that the ropent be rocolved and adopted,-Oarried umanimovaly.

# Prioo, Oloth Hixtra, <br> <br> W. J. GAGE \& OOMPANY. 

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of the sum paid for 240 gallons of wine $J$ ambits together wite iN duly to 96.00 and true duty on each gallo rue $\frac{1}{5}$ of the Joreqiial cost what Fo is the duty ken palm. for home work

$$
\begin{aligned}
& \text { - } \frac{1}{5} 1 a_{y}-196 \\
& \text { 24. } \frac{240}{5}=48 \quad \frac{16}{249460} 68.85 \\
& \begin{array}{l}
\frac{6}{5}=96 \\
16
\end{array} \\
& \frac{1450}{\left.\frac{14}{44}\right)^{2} \frac{9}{8} \frac{1}{3}}
\end{aligned}
$$



The importance of Arithmetic as a branch of in. struction is universally admitted; but, until a comparatively recent period, the results of teaching it were very unsatisfactory, and not at all commensurate with the time usually devoted to it in our schools. This was not owing to any inherent difficulty in the subject itself, but to the method of teaching it. The rule was stated first, an example illustrating the rule followed, and the reason of it came last. Now exactly the reverse of this is adopted by all good teachers. The examples and illustrations precede and lead up to the enunciation of the rule, whenever a rule is considered necessary. But while the method of teaching Arithmetic has undergone a complete change. no corresponding change has taken place in our ellmentary textbooks. To remedy this defect the following pages have been written.

We would call attention to the general features of the work:

1. The Unitary System- - In all our best schools this system has already superseded the cumbrous and illogical methods of our ordinary textbooks. Its advantages are so great that it must soon become universal. It has been defined as a method of solving arithmetical problems independently of rules by reasoning out each step of the solution from some previous one, until by a series of deductions, the result sought is obtained. This system trains the pupils to habits of neatness, exactness, and to logical habits of thought ; but its chief advantage is its extreme simplicity, dispensing with set rules, and enabling the pupil to solve problems in Simple and Compound Proportion, Simple and Compound Interest, Percent-
ages, Profit and Loss, Partnership, \&c., by one uniform, elegant, and simple process.
2. Arrangrment.-The different subjects have been arranged with reference to their importance and their simplicity ; the less difficult and more practioal first, and the more intricate and less important afterwards. Thus, problems in Canadian Money, Bills, \&e., have been introduced immediately after Division, as being of greater importance than any other subject, within the range of the pupils' ability, at that stage of their progress. Each chapter is divided into sections with the same idea running through the section. This will oblige the pupil to confine his attention to one thing at a time, and thus, enable him the more easily to master it.
3. Oral Exercises.-Each subject has been elucidated $b_{j}$ Oral Exercises leading up to written work. This arrangement will assist the pupil in arriving at the reasons for the methods employed, and, to a certain extent, make him the author of his own definitions and rules. It has other advantages. Quickness in calculation is in itself an important object to attain. This can never be attained by mere slate-work in which the pupil is allowed to think at leisure at every step.
4. Roles.-The Rule is given as a convenient summary of the methods employed in the solutions of the examples which precede it. The aim has been to lead the pupil to derive his own methods of operation.
5. Exercisms.-Special pains has been taken in framing and selecting the exercises for the different sections in order to obtain such as will not only evolve thought on the part of the pupil, but more especially prepare him for the business relations of life.

The authors will be pleased if these pages assist their fellow-teachers in bringing this important subject before their pupils in a manner more interesting and instructive than it-has been hitherto.

Toronto, May, 1878.

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## ELEMENTARY ARITHMETIC

 ON THE
## UNITARY SYSTEM.

OHAPTEK $I$.

## Section 1.-Definitions and Notation and Numeration.

1. Arithmetic is the science of numbers and the art of computing by them.
2. A Unit is a single thing; as a man, a dog, a ball, \&c.
3. A Number is a unit or collection of units; ons dollar is a unit ; five dollars is a collection of units.
4. In common arithmetic, all numbers are expressed by means of the significant figures,
$\begin{array}{lllllllll}1 & 9 & 3 & 4 & 5 & 6 & 7 & 8 & 9\end{array}$ called one, two, three, fö̀r, five, six, seven, eight, nine, and the figure 0 , which is called a cipher or zero, and which has no value in itself.
5. Numbers are considered as being either Ab stract or Concrete.

A Concrete Number is one applied to a partioular unit; as 5 men, 6 horses, 9 dollars.

An Abstract Number is one not applied to any particular unit; as 3, 6, 8 .
f. Similar Numbers are such as have the same anit; as 6 boys, 8 boys, 10 boys.

## Exercise $\mathrm{i}_{\mathbf{2}}$

1. How many units in 5 ? In 5 books? In 9 pencils?
2. What is the unit of 5 ? Of 5 books? Of 3 balls?
3. State which are sbstract and which concrete of the following numbers:

6, 7,8 books, 9 men, 3, 4, 5 apples, 2,1 cent.
4. What is the unit of 8 miles? 9 miles? 7 ? 6 cents $?$
5. Which are the similar numbers in the following:8 apples, 7 apples, 4 boys, 7, 6 apples, 9 boys, 2 cents, 4 girls, 5 cents, $9,8,5$ girls?

## NOTATION AND NUMERATION. <br> The Arabic System.

7. Notation is the art of writing down in figures any number expressed in words.
8. Numeration is the art of reading in words any number expressed in figures.
9. All Numbers are expressed in figures by means of the nine significant figures and zero, as follows:
10. All whole numbers under ten are expressed by means of the nine sigaif. cant figures.
11. The value of any figure is increased ten-fold by writing a figure on the right of it.
It follows that
12. Ten may be expressed by writing 1 and 0 on its right, thus, 10 ; for the value of the 1 is in. creased ten-fold by the zero which follows it. Similarly,
Twenty, Thirty, Forty, Fifty, Sixty, Seventy, Eighty, Ninety, may be expressed thus:
$20,30,40,50,60,70,80,90$ respectively.
13. Numbers between ten and twenty, between twenty and thirty, ice., way be expressed by an application of the preceding statements, thus:

Ex. Express in figures the number seventy-eight.
We have first to express the number seventy, and as seventy is ten times seven, we write down 7 and then make it seventy by writing some other fignre after it. Now, we might use a cipher for this purpose, but since we have to express eight besides seventy, we write an 8 after the 7 , and then read the figures 78 as seventy-eight.

## Exercise ii.

Write down in figures:

1. Seven ; nine; four ; two.
2. Thirty-six ; eighty-four; twenty ; sixty-nine.
3. Forty-four; seventy; ninety-six; sixteen.
4. Fourteen; twelve; thirty-nine; fifty-six.
5. Write as one numuer
four tens and eight units; nine tens and seven units; three tens and six units; six tens.
6. Write in words the numbers expressed by the following figures:

| 6. | 7, | 11, | 15, | 19, | 59, | 84, | 96, | 98. |
| ---: | ---: | ---: | :--- | :--- | :--- | :--- | :--- | :--- |
| 7. | 71, | 12, | 28, | 91, | 44, | 17, | 22, | 34. |
| 8. | 20, | 37, | 48, | 76, | 99, | 69, | 70, | 87. |
| 9. | 14, | 35, | 89, | 78, | 54, | 49, | 50, | 18. |
| 10. | 90, | 80, | 39, | 28, | 11, | 19, | 27, | 31. |

10. A Hun red may be expressed by writing ten, 10, and then placing a 0 after it, thus, 100 : for the value of the number 10 is increased ten-fold by writing a figure after it.

Similarly,
Two Hundred, Three Hundred, Four Hundred, \&c., may be expressed thus:

$$
200, \quad 300, \quad 400, \quad \text { \&c. }
$$

Numbers between one hundred and two hundred, between two hundred and three hundred, \&c., may be expressed by an application of the statements in art. $\theta$, thus:

Ex. Let it be required to write Eight Hundred and Seventy-eight.

Since Eight Hundred may bs expressed by 800, and

Seventy-eight by 78, we are able to express Hight Hundred and Seventy-Eight by 878 , i.e., by substituting the figures 7,8 , in place of the two ciphers in 800.

## Exercise iii.

Write in figures the following numbers:

1. One hundred and forty-nine; three hundred and eight ; nine hundred and seventy-four.
2. Two hundred ; four hundred and twenty; six hun. dred and ninety-four.
3. Five hundred and sixty; nine hundred and eight; four hundred and forty-four.
4. 7 hundreds, 3 tens and 5 units; 9 hundreds and 6 tens; 4 hundreds and 6 units.
5. 3 hundreds and nine units; 8 tens, 6 hundreds and 7 units; 2 units, 7 tens and 5 hundreds.

Write in words the numbers expressed by the following figures:

| 6. | 207, | 371, | 185, | 190, | 368. |
| ---: | :--- | :--- | :--- | :--- | :--- |
| 7. | 570, | 472, | 807, | 909, | 990. |
| 8. | 368, | 584, | 760, | 321, | 999. |
| 9. | 394, | 786, | 475, | 782, | 700. |
| 10. | 506, | 300, | 407, | 740, | 397. |

11. Numbers which consist of more than three figures are divided into periods, or groups of three figures, counting always from the right hand side.
12. The names of the periods commencing at the right are Units, Thousands, Millions, Billions, Trillions, \&c.
13. The places in any period have the same aame as in the units period, and all the places must be filled, if not occupied by a significant figure, with a cipher.

Ex. 1. Write in figures seventy-eight thousand and sixty-four.

> | Thousauds | Units. |
| :---: | :---: |
| 78 | 064. |

Ex. 2. Write in figures twenty millions, six hun= dred thousand and seven.

| Millions | Thousands | $\begin{array}{c}\text { Units. } \\ 20\end{array}$ |
| :---: | :---: | :---: |
| 600 | 007. |  |

## 표ercise iv.

Express in figures the following numbers:

1. Six thousand and six; four thousand three hundred ; nine thousand and eighty.
2. Three thousand seven hundred; seven thousand nine hundred and six ; three thousand and eighty-four.
3. Sixty-four thousand and nine; eight hundred and seven thousand and sixty-eight; sevenhundred thousand, three hundred and sixteen.
4. Four millions, thirty thousand and ninety-seven; eight hundred and nine millions, seven thousand and thirty-nine; five hundred and eighty-six millions and seven.
5. Eight billions; sixty-four billions, seven millions and twenty-four; four billions, four millions and four.
6. Four hundred and eight millions, three thousand and nine; seventy-four billions, seventy-four thousand and four; five hundred billions and five hundred.
7. Eighty billions and seventy millions; eight hundred millions and eight ; three hundred billions, three hundred thousand and ninety.
8. Fifty-seven billions, seven hundred millions and eighty; eleven millions and eleven'; nineteen billions and fourteen thousand.
9. Seven trillions and seventy; four hundred millions and one; six hundred trillions, six hundred billions and six hundred.
10. Ninety-nine trillions and eight; seven hundred billions, seventy millions and seven thousand; sixteen trillions, sixteen billions and sixteen.

Write in words the numbers expressed by the following figures :
11. 7077, 85079, 56950, 473628.
12. 56418, 784006, 400507, 360004.
13. 300071, $901007,720009,182010$
14. $3140006,50000600,8600010070$.
15. $51636207640,70000000100,920070070070$.

## THE ROMAN NOTATION.

14 The system of Notation described above is the one in general use at the present time, and is called the "Aribic Notation" because it was introduced into Europe by the Arabs, who had obtained it from
the Hindoos. Another method was in nse among the Romans, of which the following is a brief description :

1st. Instead of figures being used to express numbers the following ietters were employed, viz.:

I, V, X, L, C, D, M, of which the simple values were respectively :
$1,5,10,50,100,500,1000$.
2nd. If two characters of the same value were placed side by side, or if a character was followed by one of less value than itself, the number denoted by the expression was the sum of their simple values, thus, XX represented 20; XI denoted 11.

3rd. If a character was followed by one of greater value than itself, the number denoted by the expression was the difference of their simple values, thus, IX represented 9 ; XL represented 40 .

Note.-To write any number in Roman Numerals resolve the number into its different parts and always write down one part before proceeding to another, beginning at the left hand side.

Ex. Express 1877 in Roman numorals. $1877=1000,800,70$ and 7. $1080=\mathbf{M}$ $800=$ DCCC $70=\mathrm{LXX}$ $7=$ VII.
Hence $1877=$ MDCCCLXXVII.

## Exercise $v$.

Write in Roman numerals-

1. $19,24,49,84,99$.
2. 187, 208, 781, 962, 999.
3. 1301, 1390, 1684, 1815, 1878.

Write in figures-
4. XLIV, IXPY YOIV, LXXI.
5. XCEX, CXXIX, CLXXVII.
6. DLV, MDCIV, MDCCOXIX MXC.

## Review Fxercise.

1. Define unit and number, and distinguish between abstract and concrete numbers.
2. Whence was the ordinary system of notation derived? What methods did the Romans adopt to represent numbers?
3. Express in figures the first hundred numbers with their respective names.
4. Write the smallest and largest number possible with the following five characters: $0,1,2,3,4$, and express them in words.
5. Write down the different ways in which each of the nine digits can be made up of two less numbers.
6. The number 27 is composed of 16 and 11. Write down all the other two numbers which can make up the number 27.
7. How many tens, how many hundreds, how many thousands, and how many ten thousands are there in a million of units?

## Section II.-Addition.

1. James had 3 marbles and John gave him 2 more ; how many has James now ?
2. How many are 5 apples and 4 apples?
3. How many are 2 books and 3 books and 4 books?
4. John has 8 cents, his father gives him 5 cents more; how much money has he now?

厄. How many are 2 balls and 7 balls and 5 balls?
6. Mary is 5 years cld ; how old will she be seven years hence?
7. James bought 2 books; for one he gave 9 cents and for the other 8 cents; how much did he give for both books?
8. Jane spent 5 centō on candy, 9 cents on a slaté, and thon had 6 cents left; how much had she at first?

## ADDITION TABLE.

| 1 | $\left\{\begin{array}{l}0 \\ 1\end{array}\right.$ | 1 | 2 1 | 8 <br> 1 | 4 1 | 5 1 | 6 1 | 7 1 | 8 | 9 1 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
|  | $\left\{\begin{array}{l}0 \\ 2\end{array}\right.$ | 1 2 | 2 2 | 3 2 | 4 2 | 5 2 | 6 2 | 7 2 | 8 | 9 2 |
|  | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 |
| 3 | 0 <br> 8 | 1 | 2 3 | 3 | 3 | 5 3 | 6 3 | 7 3 | 8 3 | 9 8 |
|  | 8 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| 4 | 0 4 | 1 4 | 2 4 | 3 4 | 4 | 5 4 | 6 4 | 7 4 | 4 | 4 |
|  | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 |
| 5 | 0 5 | 1 | 2 5 | 3 5 | 5 | $\begin{aligned} & 5 \\ & 5 \end{aligned}$ | $\begin{aligned} & 6 \\ & 5 \end{aligned}$ | $\begin{aligned} & 7 \\ & 5 \end{aligned}$ | $\begin{aligned} & 8 \\ & 5 \end{aligned}$ | 9 5 |
|  | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
| 6 | $\begin{aligned} & 0 \\ & 6 \end{aligned}$ | 1 | 2 | 8 | 4 | $\begin{aligned} & 5 \\ & 6 \end{aligned}$ | 6 6 | $\begin{aligned} & 7 \\ & 6 \end{aligned}$ | 8 | 9 6 |
|  | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| 7 | $\begin{aligned} & 0 \\ & 7 \end{aligned}$ | $\begin{aligned} & 1 \\ & 7 \end{aligned}$ | 2 7 | $\begin{aligned} & 3 \\ & 7 \end{aligned}$ | $\begin{aligned} & 4 \\ & 7 \\ & \hline \end{aligned}$ | $\begin{aligned} & 5 \\ & 7 \\ & \hline \end{aligned}$ | $\begin{aligned} & 6 \\ & 7 \end{aligned}$ | $\begin{aligned} & 7 \\ & 7 \end{aligned}$ | $\begin{aligned} & 8 \\ & 7 \end{aligned}$ | 9 7 |
|  | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 |
| 8 | $\begin{aligned} & 0 \\ & 8 \end{aligned}$ | $\begin{aligned} & 1 \\ & 8 \end{aligned}$ | $\begin{aligned} & 2 \\ & 8 \end{aligned}$ | $\begin{aligned} & 8 \\ & 8 \end{aligned}$ | $\begin{aligned} & 4 \\ & 8 \end{aligned}$ | $\begin{aligned} & 5 \\ & 8 \end{aligned}$ | $\begin{aligned} & 6 \\ & 8 \end{aligned}$ | $\begin{aligned} & 7 \\ & 8 \end{aligned}$ | $\begin{aligned} & 8 \\ & 8 \end{aligned}$ | 9 <br> 8 |
|  | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 |
| 9 | 0 9 | 1 | 2 9 | 3 9 | 4 | $\begin{aligned} & 5 \\ & 9 \end{aligned}$ | $\begin{aligned} & 6 \\ & 9 \end{aligned}$ | $\begin{aligned} & 7 \\ & 9 \end{aligned}$ | $\begin{aligned} & 8 \\ & 9 \end{aligned}$ | 9 |
|  | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 |
| 10 | ${ }_{0}$ | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|  | 10 | 10 | 10 | 10 | 10 | 10 | 10 | 10 | 10 | 10 |
|  | 10 | 11 | 12 | 18 | 14 | 15 | 16 | 17 | 18 | 19 |

## ADDITION.

## Oral Exercises.

1. How many are 5 and 9 ? 15 and 9 ?
2. How many are 6 and 7 ? 16 and 7 ? 46 and 71
3. How many are 4 and 8? 24 and 8 ? 84 and 8 ?
4. Count by 2 's as far as 30.
5. Count by 4 's from 3 to 51 .
6. Count by 6 's from 4 to 76 .
7. Count by 7's from 4 to 95 .
8. How many are 17 and 7 ? 27 and 7 ? 57 and 7 ?
9. How many are 2 and 3 and 4 and 5 and 6 and 7 and 8 and 9 ?
10. How many are 6 and 8 and 9 and 4 and 6 and 7 and 8 ?
11. A farmer sold some oats for 7 dollars, and a ton of hay for 9 dollars; how many dollars did he receive for both?
12. Paid 8 cents for raisins, and 9 cents for cloves; how many cents did both cost?
13. There are 9 boys in one class, and 7 in another ; how many in both classes?
14. If you work 8 examples in arithmetic to-day, and 7 to-morrow, how many will you work in both days?
15. There are 9 birds on one tree, and 10 on another; how many birds on both trees?
16. A lady sold 10 pounds of butter at one time, 12 pounds at another, and 3 pounds at another; how many pounde did she sell in all?
17. James has 9 cents, John has 10 cents, and William has 12 cents; how many cents have the three boys?
18. A hat cost 7 dollars, a vest 4 dollars, a coat 12 dollars, and a pair of boots 10 dollars; how much did they all cost?
19. Uniting two or more numbers of the same kind, so as to find how much they all equal, is called Addition.
20. The number found by adding two or more numbers together is called the Sum.
21. The numbers which are added together are called Addends.
22. The sign of Addition, + , is called Plus, and when placed between two numbers shows that they are to be addod.
23. The sign, $=$, is called the Sign of Equality, and when placed between two numbers shows that they are equal. Thus, $2+3=5$, and is read, 2 plus 3 equals 5.
24. Principle.-Only similar numbers can be added. Thus 3 boys and 2 boys; 4 cents and 7 cents, can be added together.
25. Addition may be divided into two cases:
26. Addition of numbers in which the sum of any column is less than ton.
27. Addition of numbers in which the sum of any or all of the columns exceeds nine units of that place.

## Case I.

22. To add any column of Figures whose sum does not exceed nine.

Ex. I. How many are 21 cents, 15 cents, and 12 cents?
21 cents
15
12
$\overline{48}$ cents.

Write the numbers, as above, placing units under units, and tens under tens, and begin at the right to add. Thus, 2 and 5 are 7, and 1 are 8, which we write in the place of units; adding the tens. wé have 1 and 1 are 2 , and 2 are 4, which we write in the tens' place. Hence the entire sum is 48 cents.

After a little practice the pupil should proceed as follows: 2, 7, 8; set the 8 in the units' column. Next, 1, 2,4 ; set the 4 in the tens' column.

## Exercise vi.

| $\begin{aligned} & 11) \\ & 10 \\ & 21 \\ & 10 \end{aligned}$ |
| :---: |
|  |  |
|  |  |
|  |  |

(2)

18 boya.

$$
20
$$

60
(3)


ADDITION.


1. A boy spent 23 conts for a melon, 32 cents for peaches, and 24 cents for pears; how many cents did he spend?
2. Of the trees in an orchard, 23 are peach trees, 10 are plum trees, 12 are pear trees, and-48 are apple trees; how many trees are there in the orchard?
3. A farmer hag 2929 anus in cotton. 421 socros in corn, 10 aores in wheat, and 101 in oats; how many acres has ho cultivation?
4. A gentleman paid 225 doliars for a buggy, 231 dollara for a horse, 300 dollars for a carriage, and 40 dollars for harness; what did he pay for all?
5. A man travellad on the cars for four days, as follows: the first day he went 313 miles, the second day 242 miles, the third day 220 miles, and the fourth day 214 miles; how many miles did he travei in the four days?
6. A merchant bought four bales of cloth; the first bale measured 805 yards, the second 213 yards, the third 240 yards, the fourth 211 yards; how many yards dia he buy?
7. Four merchants loaded a freight train with cotton; the first put on 213 bales, the second 232 bales, the third 312 bales, and the fourth 121 bales; how many bales were put on?
8. A merchant went to Montreal and invested 5213 dollars in dry goods, 2431 dollars in groceries, 1000 dollars in hardware, and 345 dollars in confectionery; how much did he invest?
9. Four men built a factory; the first furnished 13214 dollars, the second 31423 dollars, the third 43230 dollars, and the fourth 10122 dollars; what was the cost of the factory?
10. The population of 4 cities is as follows: the first contains 321213 persons, the second 213310 persons, the third 145245 persons, and the fourth 220180 persons; what is the total population?

Case. II.
23. To add when the Sum of any column exceeds Nine Units of that place.

Ex. 2. Find the sum of $\mathbf{3 5 8}$ dollars, 369 dollars, 4008 dollars, 328 dollars, and 9 dollars.
$\left.\begin{array}{r}358 \\ 369 \\ 4008 \\ 40 \text { dars } \\ 828\end{array}\right)$

## 5072 dollars.

For convenience in adaing, write the numbera, placing units under units, tens under tens, \&c. Begin at the column of the lowest order; thus, $9,17,25,34,42$ : 48
nuits $=4$ tens and 2 units. Write the 2 under the units' column and add the 4 tens with the column of tens; thus, 6, 12, 17: 17 tens $=1$ hundred and 7 tens. Write 7 under the column of tens and add 1 with the column of hundreds: thus, 4, 7, 10: 10 hundreds $=1$ thousand and 0 hundreds. Write 0 ?nder the column of hundreds and add 1 with the thousania' column ; thus 5 . Write the 5 under the thousands' colums:, making the sum 5072.
24. PROOF.-Begin at the top of the units' column and add the several columns downwards ; if the two results agree the work may be presumed to be correct.

Exercise viii.
(1

| 42 |
| :--- |
| 28 |
| 43 |
| 4 |

(2)

(8)
(4)

48 girls. 25 « 72
(10)

| $(5)$ | $(6)$ | $(7)$ | $(8)$ | $(9)$ | $(10)$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| 45 | 84 | 16 | 46 | 84 | 95 |
| 69 | 72 | 61 | 64 | 46 | 50 |
| 82 | 91 | 85 | 51 | 87 | 68 |
| - | - | - | - | - | - |
| $(11)$ | $(12)$ | $(13)$ | $(14)$ | $(15)$ | $(16)$ |
| 642 | 272 | 615 | 465 | 956 | 925 |
| 847 | 447 | 421 | 641 | 508 | 575 |
| 872 | 638 | 879 | 848 | 467 | 259 |
| - | - | - | - | - | - |
| $(17)$ | $(18)$ | $(19)$ | $(20)$ | $(21)$ | $(22)$ |
| 752 | 842 | 253 | 897 | 156 | 851 |
| 423 | 426 | 541 | 111 | 481 | 818 |
| 709 | 151 | 422 | 843 | 423 | 805 |
| 820 | 737 | 735 | 625 | 782 | 167 |
|  | - | - | - | - | - |
| $(23)$ | $(24)$ | $(25)$ | $(26)$ | $(27)$ | $\mathbf{( 2 8 )}$ |
| 4818 | 1122 | 2291 | 8574 | 4449 | 1857 |
| 5914 | 7914 | 5723 | 8333 | 2575 | 2468 |
| 6115 | 1284 | 2102 | 4680 | 4404 | 5555 |
| 7086 | 8024 | 6838 | 3391 | 3685 | 6666 |


rind the sum-
41. Of $6472+8735+4633+4854$.
42. Of $2762+8756+9783+4578$.
43. Of $1617+8743+7284+9621$.
44. Of $2650+4062+8705+9030$.
45. Of $5005+6007+7583+4783$.
46. Of $27845+67832+74281+68432$.
47. Of $47823+68421+70070+60504$.
48. Of $127+6434+7805+66782$.
49. Of $10+8756+405+66782$.
50. Of $7560+804+7854+87400$.
51. Of $1525+960+820+10+378000^{1}$

Exercise ix.

## Practical Problems.

1. A gave 27 dollars for a cow, 45 dollars for an ox, and 150 dollars for a horse ; what did they all cost?
2. A has 120 acres of land, $B$ has 310 acres, $C$ has 516 acres, and D has 715 acres; how many acres have they together?
3. There are 31 days in January, 28 in February, 31 in March, and 30 in April ; how many days are there in these four months?
4. A man travelled 215 miles one weer, 195 the next week, 273 the next, and 878 the next; how far did he travel?
5. A weighs 127 pounds, B weighs 215 pounds, $O 176$ pounds, D 184 pounds, and E 284 pounds; what is the sum of their weights?
6. A farmer raised 576 bushels of corn, 915 bushels of oats, 8149 bushels of wheat, and 2785 bushels of rye; how many bushels did he raise in all?
7. A owns 214 acres of land, B owns 719 acres, C owns 2186 acres, and Downs 372 rcres; how many acres do they together own?
8. A bought a horse for 168 dollars, and a carriage for 876 dollars, and sold them so as to gain 89 dollars ; How much did he receive for them?
9. In one book there are 725 pages, in another book there are 827 pages, and in another book there are as many as in both the formor; how many pages in all?
10. A merchant bought cloth for 756 dollars, silk for 859 dollars, muslin for 867 dollars, and calico for 255 dollars; how much did they all cost?
11. A paid 825 dollars for a span of horses, and 248 dollars more than this for a carriage; for how much must he sell them both to gain 275 dollars?
12. A gains in one year 465 dollars, B gains 186 dollars y core than A , and C gains as much as A and B toggther; how much did $B$ gain? how much did $C$ gain ? how much did they all gain?

## Section III.-Subtraction

1. John had 5 cents, and bought an orange for 2 cents; how many cents had he left?
2. Mary had 6 cups, but broke 3 ; how many had she remaining?
3. A man, earning 10 dollars a week, spent 6 dollars for provisions; how many dollars has he left?
4. If a merchant has 12 barrels of flour, and he sells 7 of them, how many barrels has he left?
5. If you have 27 dollars, and spend 12 dollars, how much wi!! you have remaining?
6. How many are 6 apples less 3 apples.
7. How many are 6 less 8 ? 6 less 4 ?

SUBTRACTION TABLE.

| 1 | 1 | 2 1 | 3 1 | 4 1 | 5 1 | 6 1 | 7 | 8 1 | 9 1 | 10 1 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 2 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 |
|  | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 |
|  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 3 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
|  | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 8 |
|  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 4 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 |
|  | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 |
|  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 5 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
|  | 5 | 5 | 5 | 5 | 5 | 5 | 5 | 5 | 5 | 5 |
|  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 6 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
|  | 6 | 6 | 6 | 6 | 6 | 6 | 6 | 6 | 6 | 6 |
|  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 7 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 |
|  | 7 | 7 | 7 | 7 | 7 | 7 | 7 | 7 | 7 | 7 |
|  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| 8 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 |
|  | 8 | 8 | 8 | 8 | 8 | 8 | 8 | 8 | 8 | 8 |
|  | 0 | 1 | 2 | 3 | 4 | 4 | 6 | 7 | 8 | 9 |
| 9 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 |
|  | 9 | 9 | 9 | 9 | 9 | 9 | 9 | 9 | 9 | 9 |
|  | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |

## Oral Exercises.

1. Subtract by 2 's from 100 to 2 ; thus, 2 from 100 leaven 88, 2 from 98 leaves 96 , and so on.
2. Subtract by 3 's from 100 to 1 ; by 4 's from 100 to 0 .
3. Subtract by 4 's from 95 to 3 ; by 5 's from 100 to 0.
4. Subtract by 6 's from 100 to 4 ; by 7's from 100 to 2.
5. Suhtract by 7 's from 99 to 1 ; by 8 's from 100 to 4 .
6. Subtract by 9 's from 100 to 1 ; by 9 's from 99 to 0 .
7. Count by 4 's from 3 to 89 , and back again to 19.
8. Count by 5 's from 6 to 66 , and back again to 26 .
9. Count by 7 's from 18 to 58 , and back again to 11. 10. Count by 8 's from 25 to 65 , and back again to 1 .
10. Jane is 11 years old, and Mary is 7 years younger; what is Mary's age?
11. A grocer sold tea for 10 dollars, and thus gainod 8 dollars; what did the tea cost him?
12. If I buy cloth for 7 dollars, at what price must I sell in order to lose 4 dollars?
13. John has 11 dollars; he pays 2 dollars for books, and 3 dollars for a hat; how much money has he left?
14. Mary has 9 dollars; she pays 7 dollars for a dress, and then earns 3 dollars more; how mnch has she now?
15. A boy having 12 apples, bought 6 more, and then sold 8 ; how many had he left?
16. Jrmes had 5 dollars, he earned 5 dollars more, and then spent 6 dollars; how much did he then have?
17. A merchant geve 8 dollars for a certain article, and paid 4 dollars for carriage ; at what prioe must he sell to gain 3 dollars ?
18. Finding the difference between two numbers is called Subtraction.
19. The number found by taking one number from another is called the Difference or Remainder.

2\%. The uumber from which the other is taken is called the Minuend.
28. That which is taken from the Minuend is called the Subtrahend.

²9. The sign of subtraction, - , is called Minus, and when placed between two numbers shows that the one on the right of the sign is to be taken from the one on the left of it. Thus, 6-2 is read 6 minus 2, and means that 2 is to be taken from 6.

30 Principle.-Only similar numbers can be subtracted; thus, 4 boys from 7 boys; 6 cents from 8 cents, \&c.
31. Subtraction may be divided into two cases:

1. When no figure of the subtrahemi is greater trana its correspondiug figure of the minuend.
2. When a figure of the subtrahend is greater than its corresponding figure of the minuend.

## Case I.

32. To subtract when no figure of the subtrahend is greater than its corresponding figure of the minuend.

Ex. I. A grocer bought 678 oranges, and sold 835 of them; how many had he left?


Here we are required to find the diffirence batween 678 and 535 . We write the less number under the greater, placing units under units and tens under tens. Beginning with the units we say: 5 units from 8 units leave 3 units, and we set the 3 in the units' column below. Then 3 tens from 7 tens leave 4 tens, and we set the 4 in the tens' column. Lastly, 3 hundreds from 6 hundreds leave 3 hundreds, and we set the three in the hundreds' colnmn. Hence we have as the whole remainder 3 hundreds 4 tens and 3 units, or 343.

Exercise x.

| (1) | (2) | (3) | (4) | (5) | (6) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 625 | 456 | 763 | 617 | 767 | 896 |
| 312 | 215 | 512 | 215 | 123 | 432 |
| (7) | (8) | (9) | (10) | (11) | (12) |
| 279 | 807 | 796 | 736 | 967 | 875 |
| 136 | 502 | 452 | 432 | 234 | 345 |
| (13) | (14) | (15) | (16) | (17) | (18) |
| 8763 | 9076 | 8769 | 5076 | 4872 | 7659 |
| 4321 | 4054 | 1546 | 3075 | 2342 | 3237 |
| (19) | (20) | (21) | (22) | (28) | (24) |
| 8769 | 4876 | 8275 | 8799 | 8591 | 5857 |
| 8257 | 2142 | 3251 | 2542 | 7230 | 1234 |
| (25) | (26) | (27) | (28) | (29) | (30) |
| 784 | 82345 | 57596 | 72578 | 27397 | 67385 |
| 361 | 22121 | 21321 | 41362 | 22315 | 24123 |


| (81) | (32) | (33) | (84) | (85) |
| :---: | :---: | :---: | :---: | :---: |
| 57897 | 67858 | 87578 | 96754 | 81296 |
| 21472 | 32721 | 21335 | $: 1423$ | 20135 |
| (36) | (37) | (38) | (89) | (40) |
| 253786 | 472589 | 87695 | 56728 | 98785 |
| 213123 | 212324 | 23542 | 21306 | 21842 |
| (41) | (42) | (48) | (44) | (45) |
| 873967 | 873972 | 72587 | 95837 | 89976 |
| 212851 | 132421 | 51234 | 51321 | 32742 |
| 314 from 678. 51. 1235 |  |  |  |  |
| 425 from | 658. | 52. | 3726 from | 4963. |
| 561 from | 789. | 53. | 2532 from | 8748. |
| 254 from | 576. | 54. | 4720 from | 7856. |
| 437 from | 869. | 55. | 12345 fr | 68799. |

Exercise xi .

## Practical Problems.

1. In a school of 74 pupils, 31 are boys; how many girls are there?
\%. A girl had 75 cents and paid 81 cents cor a slate ; how many cents had she left ?
2. A man bought a horse for 98 dollars, and sold it for 82 dollars; what did he lose?
3. Two parties played a game of base ball and made 87 runs. One party made 53 runs; how many did the other party make?
4. Jane and Susan together answered 87 questions in geography. Jane answered 43 of them; how many did Susan answer?
5. A gentleman bought a buggy for 225 dollara, and sold it for 268 dollars; what was his pro ?
6. A man bought a horse for 265 dollars, und sold it for 232 dollars; how much did he lose?
7. A man deposited 5237 dollars in the bank; he afterwards drew out 3125 dollars; how much remained?
8. A man dying leit 27894 dollars to his son and his daughter. The share of the son was 13452 dollars; what was the daughter's share?

## Case II.


#### Abstract

33. To subtract when a figure in the Subtrahend is greater than its corresponding figure in the Minuend.


Ex. 2. From 522 dollars subtract 285 dollars.
522 dollars.
285 "
237 "
We begin at the right, but as we cannot take 5 units from 2 units, we borrow 1 ten from the 2 tens, and adding the 1 ten, $=10$ units, to the 2 units, we have 12 units. Then 5 units from 12 units leave 7 units, which we write under the units' column. Now, as we borrowed 1 ten from the 2 teus, we left only 1 ten. As we cannot take 8 tens from 1 ten, we borrow 1 hundred from the 5 hundreds, and considering the 1 hundred borrowed as 10 tens, we add it to the 1 ten, making it 11 tens; then 8 tens from 11 tens leave 3 tens, which we write in the tens' column. Now, as we borrowed 1 hundred from 5 hundreds, we left only 4 hundreds : hence we say, 2 hundreds from 4 hundreds leave 2 hundreds, which we write in the hundreds' column, making the remainder 2 hundreds 3 tens and 7 units, or 237.

There is another method of performing subtraction, which depends on the following principle:

The difference between two numbers remains the same when each of them is increased by the same number.

For example, $5-2=3$. Now, if we add 10 to each, we have $15-12=3$, as before.

In Ex. 2, if we ad $\$ 0$ units to 2 units we have 12 units. Then 5 units from 12 units leave 7 units, which we write in the place of units. Now, as we added 10 units to the minuend, if we add an equal number to the subtrahend the difference will remain the same. But 10 units $=1$ ten. Adding 1 ten to 8 tens we have 9 tens; and as we cannot take 9 tens from 2 tens, we add 10 tens, thereby making 12 tens; then 9 tens from 12 tens leave 3 tens, which we write in the place of tens. Since we added 10
tens to the minuend, we must add an equal number to the subtrahend, in order that the difference may remain the same. But 10 tens $=1$ hundred. Adding 1 hundred to 2 hundreds we get 3 hundreds; and taking 3 hundreds from 5 hundrede we get 2 hundreds, which we write in the hundreds' place. This is the method usually employed.
34. $P R O O F$.-Add the remainder to the subtrahend; the sum will equal the minuend if the work is correct.

| Exercise xii. |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| (1) | (2) | (3) | (4) | (5) | (6) |
| 573 | 748 | 835 | 968 | 839 | 538 |
| 248 | 375 | 573 | 675 | 584 | 394 |
| (7) | (8) | (9) | (10) | (11) | (12) |
| 659 | 839 | 547 | 658 | 735 | 848 |
| 475 | 583 | 284 | 372 | 373 | 539 |
| (13) | (14) | (15) | (16) | - (17) | (18) |
| 524 | 752 | 845 | 307 | 456 | 450 |
| 356 | 387 | 579 | 138 | 387 | 382 |
| (19) | (20) | (21) | (22) | (23) | (24) |
| 854 | 943 | 607 | 500 | 704 | 403 |
| 396 | 765 | 309 | 325 | 507 | 285 |
| (25) | (26) | (27) | (28) | (29) | (30) |
| 726 | 857 | 785 | 792 | 807 | 650 |
| 387 | 389 | 558 | 295 | 328 | 357 |
| (31) | (32) | (33) | (34) | (35) | (36) |
| 3876 | 6385 | 6735 | 407 | 4070 | 4135 |
| 2379 | 3527 | 2547 | 3128 | 2137 | 1216 |
| (37) | (38) | (39) | (40) | (41) | (42) |
| 8672 | 5283 | 8175 | 2534 | 6735 | 7219 |
| 3728 | $24 \% 6$ | 2836 | 1235 | 5376 | 1978 |


| $(48)$ | $(44)$ | $(45)$ | $(46)$ | $(47)$ | $(48)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 8522 | 7135 | 6347 | 8185 | 7345 | 4372 |
| 6243 | 1872 | 2563 | 2453 | 2876 | 2585 |
| - | - | - | - | - | - |
| $(49)$ | $(50)$ | $(51)$ | $(52)$ | $(58)$ | $(54)$ |
| 85672 | 43763 | 87253 | 73875 | $C 3527$ | 53413 |
| 23828 | 24235 | 34365 | 38376 | 14238 | 28401 |
|  | - | - | - |  |  |
| Exercise xiii |  |  |  |  |  |
| Practical Problems. |  |  |  |  |  |

1. A horse was bought for 125 dollars, and sold for 117 dollars; how much was lost by the sale?
2. A roll of carpet contained 156 yards, but 79 yards were sold from it; how much remains?
3. A house cost 5440 dollars, and was sold for 6000 dollars; how much was the gain?
4. A man died in 1878 at the age of 75 years; when was he born?
5. A town which ten years ago kad a population of 3745 , has now a population of 6996 ; what is the gain?
6. I went to a store and bought a knife for 56 cents, and gave the storekeeper a four dollar bill ( 400 cents) to pay for it; how much change did he give me back?
7. Two little girls picked 74 quarts of blackberries one summer; if one picked 37 quarts, how many quarts did the other pick?
8. Mr. Robinson's horse and carriage cost four hundred dollars; what did the horse cost, if the carriage cost two hundred and twenty-five dollars?
9. Suppose a man's income is 2453 dollars a year, and his expenses are 1947. dollars, how much can he save in a year?
10. Smith bought of Brown 875 acres of land for 23400 dollars. For 500 acres of the tract he paid 11379 dollars; how many acres wervin the remainder of the tract? And for what sum was it purchased?

## Addition and Subtraction.

## Exercise xiv.

Find the result of

1. $768+276-369+284-782$.
2. $369+784+468-266-368-248$.
B. $1764-839+786+724-368-256$.
3. $136-769-284+968+268+372$.
4. $269-1846+368-274+2976+769$.
5. $769+785+368-784-369-249$.
6. $1869-2846+362-489+3007+249$.
7. $2845+3624-78695+784+93768$.
8. $7369-245-12456+85769-2572$.
9. $3004+2006-5008-3604+7200$.

## Exercise. xv.

## Practical Problems.

1. A man owing 1369 dollars, paid at one time 264 dollars, and at another 748 dollars; how much did he still owe?
2. A man bought a farm for 6780 dollars; he spent 1875 dollars for improvements and 977 dollars for stock. He then sold the whole for 9000 dollars; did he gain or lose, and how much?
3. The sum of four numbers is 986287 ; the first is 23789, the second is 11892 less than the first, the third is 85416 more than the second; what is the fourth?
4. What number increased by the difference between 1458 and 2362 will make the sum of 8641,789 and 70081
5. A collector received 1200 dollars from four men; from the first he got 352 dollars, from the second 67 dollars more than this, and from the third 94 dollars less; how much did he receive from the fourth?
6. At an election, in which there were two candidates, the whole number of votes was 3694 ; the defeated oandidate received 1369 votes; what was the majority?
7. A boy shot an arrow up the road 173 feet and another down the road 234 feet; bis little brother brought them to him; how far did he walk to get them?
8. John and James play marbles, John has 24 at the beginning and James 36. The first game John wins 4, the next he wins 6 , the next he loses 5 , the next he loses 3, the next he wins 2 ; how many marbles has each now?
9. Find the final remainder in subtracting 54368 as many times as possible from 476209.
10. From the difference between 576 and 7852, take the difference between 19101 and 18453.
11. The sum of two numbers is 8764 ; the difference of the same two numbers is 1658 ;' what are the numbers?

## Section IV.-Multiplication.

1. There are 5 oranges in each of three dishes; how many are there altogether? 5 and 5 and 5 are how many? Three 5's or three times 5 are how many?
2. If there are 3 berries in one cluster, how many berries are there in 5 clusters? $3+3+3+3+3$ are how many?
3. There are 3 feet in one yard, how many feet are there in 2 yards? In 4 yards? In 6 yards?
4. There are 6 working days in 1 week, how many working days are there in 2 weeks? In 5 weeks? $6+6+6+6+6$ are how many?
5. What will 3 hats cost at 2 dollars each ?

Since 1 hat costs 2 dollars, 3 hats will cost $2+2+2$ dollars or 3 times 2 dollars, or 6 dollars. Hence 3 hats will costs 6 dollars.
6. If John walks 3 miles an hour, how far will he go in 4 hours?
7. If a First Book costs 3 cents, what will 5 First Books cost?
8. What will 4 buns cost at 2 cents each
9. If little James takes 2 steps in a yard, how many steps will he take in going 5 yards ?
10. John bought 4 tops at 3 cents a piece, how much money did he spend?

3,5. When any number is to be added to itself two or more times the work may be shortened by a process called Mriltiplication.
36. The number resulting from the Multiplication is called the Product.

3\%. The number to be added several times to itself is called the MuItiplicand.
38. The number denoting how many times the Multiplicand is to be taken is called the Multiplier.
39. The Sign of Multiplication is formed by two short lines crossing each other slantingly; thus, $x$.

It shows that the second of the two numbers between which it is placed is to be multiplied by the first, thus 4 times 8 is written $4 \times 8$.

## 40. Principles.-

Milltiplication table.

| rice | Three | Four |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| :s 2 | 1 is. 3 | 1 is 4 | ${ }^{\text {timos. }}$ is. 5 |  |  |
| ci... $4^{\text {a }}$ | $2 \ldots 6$ | $2 . .8$ | 2 .. 10 | 2 ... 12 |  |
| \% ... 6 | 3 ... 9 | 3 ... 12 | 3 ... 15 | 3 ... 18 |  |
| $4 . .8$ | 4 ... 12 | $4 . . .16$ | 4 ... 20 | 4 ... 24 | 4 ... 28 |
| $5 . . .10$ | 5 ... 15 | 5 ... 20 | $5 . .25$ | 5 ... 30 |  |
| 6 ... 12 | 6 ... 18 | 6 ... 24 | 6 ... 30 | 6 ... 36 | 6 ... 42 |
| $7 . . .14$ | 7 ... 21 | 7 ... 28 | 7 ... 35 | 7 ... 42 |  |
| 8 ... 16 | $8 . . .24$ | 8 ... 32 | 8 ... 40 | $8 . . .48$ |  |
| 9... 18 | 9 ... 27 | 9 ... 36 | $9 . . .45$ | 9 ... 54 |  |
| $10 . . .20$ | 10 .. 30 | $10 . . .40$ | $10 . . .50$ | $10 . . .60$ | $10 . . .70$ |
| 1.1 ... 22 | $11 . .33$ | $11 . . .44$ | $11 . . .55$ | $11 . . .66$ | $11 . . .77$ |
| $12 . . .24$ | $12 . .36$ |  | $12 . . .60$ | 12 ... 72 | $12 \ldots 84$ |


|  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |
| is 8 | 1 is 9 | 1 is 10 | 1 is 11 | 12 |
| ... 16 | $2 \ldots 18$ | $2 \ldots 20$ | 2 ... 22 | 2 ... 24 |
| 24 | 3 ... 27 | 3 ... 30 |  | 3 |
| 32 | 36 | 40 |  | 48 |
| 40 | 5 ... 45 | 5 ... 50 |  | 60 |
| ... 48 | 6 ... 54 | 6 ... 60 | 66 | 72 |
| . 56 | 7 ... 63 | 7 ... 70 | 77 | 7 ... 84 |
| 64 | 8 ... 72 | 80 | 8 ... 88 |  |
|  | 81 | 90 | 99 | 9 ... 108 |
| $10 . . .80$ | 10 ... 90 | $10 . . .100$ | 10 ... 110 | $10 . . .120$ |
| $11 . . .88$ | $11 . . .99$ | $11 . . .110$ | 11... 121 | $11 \ldots 132$ |
| 12. | 12 |  |  |  |

Oral Exercise.

1. Multiply by 2 from 1 to 12 ; by 3 from 1 to 6.
2. Multiply by 4 from 3 to 9 ; by 5 from 12 to 4.
3. Multiply by 6 from 3 to 10 ; by 7 from 12 to 5 .
4. Multiply 8 from 12 to 2 ; by 9 from 1 to 11 .
5. What will 5 hats cost at 7 dollars each?

If 1 hat costs 7 dollars, 5 bets will cost 5 timo $g$ dollars, or 35 dollars.
6. What will 4 pairs of boots cost at 6 dollars a pair?
7. A sheep costs 7 dollars; how much will 6 shcep cost at the same rate?
8. How much will 12 tone of coal cost at 6 dollars a ton?
9. A man can earn 4 dollars a day; how much can ho earn in 9 days?
10. At the rate of 8 marbles for a cent, how many can be bought for 12 cents?
11. What will 7 lead pencils cost at 7 cents apiece?
12. If a man cuts 3 cords of wood in a day, how many cords can he out in 12 days?
13. If 8 men can do a piece of work in 7 days, how many days will it take one man to do it?
14. How many dollars will buy 9 tons of hay at 12 dollars a ton?
15. In an orchard there are 12 rows of treen, and 11 trees in each row; how many trees are there in the orchard?
16. If a quantity of provisions will last 8 men 7 days, how many days will the same provisions last one man?
17. If 12 bushels of apples are picked from each of 8 trees, how many bushels are picked from all?
41. Multiplication may be divided into two case:

1. When the Multiplier does not exceed twelve.
2. When the Multiplier exceeds twelve.

Gase I.
42. When the Multiplier does not exceed twelve.

Ex. r.-How many are 4 times 87 boys?

Ist Operation. 87 boys. 87 6 87 87 "

2nd Operation. 87 boys. 4

348 boys.

Snm 348 boja.
In the first operation we find the result by Addition.
In the second operation, which is much shorter, we
write down 87 once, and we put 4 , the number of timen it is to be taken, under the units' figure of the Multiplioand. We then begin at the right hand side to multiply by 4 ; 4 times 7 units are 28 units, or 2 tens and 8 units. Wo write tho 8 units under tho units and add the 2 tons to the product of the tons. Wo next take 4 times 8 tens. 4 timos 8 tens are 32 tens and 2 tens make 84 tens, or 8 hundrods and 4 tens. Then we write down 4 in the tens' placo and 8 in the hundreds place.

刃xercise xvi.

| Multiply | (1) |
| :--- | ---: |
| By | 7482 |
|  | 2 |

6. There are 56 sheep in one fluck ; how many sheep are there in 6 such flocks? What in the value of each flock at 7 dollars a hoad?
7. A man bought 384 pounds of cugar; he sold 290 pounds; how much had ho left? How much did he receive for what he sold, at 9 conts a pound? What is the remainder worth at 8 conts a pound? At 7 cents a pound ?
8. A merchant sold 378 kegs of nails at 9 dollars a keg ; 32 hundred weight of iron at 7 dollars a bundred weight; what did each of the articles come to? What did both come to? Ho paid away 1389 dollars; how much money had ho left?
9. I have a book with 220 pages, there are 6 paragraphs on each page; there are 9 lines in each paragraph; thare are 8 words in each line ; there are, on an average, 5 lotters in each word; how many paragraphs are there in the book? How many lines? How meny words? How many letters?
10. A grocer sold 37 pounds of rice at 8 cents a pound; 46 pounds of sugar at 9 cents a pound; what did the rico come to? What did the sugar come to? What did both come to? What did one cost more than the other?
11. A man bought 137 pints of chestnuts at 8 cents a pint; 246 pints of peanuts at 9 cents a pint; what did each cost? What did both cost? How much did one cost more then the other?
12. To multiply by the factors of a number.
13. The Factors of a number are those numbers which multiplied together will produce it. Thus, 8 and 5 are the factora of 15 .

Ex. 2. Multiply 742 by 36.

| $36=6 \times 6$, or $9 \times 4$, or $12 \times 3$. |  |  |  |
| :---: | :---: | ---: | ---: |
| 742 | 742 | 742 | 742 |
| 36 | 6 | 9 | 12 |
| 4452 | 4452 | 6678 | 8904 |
| 2226 | 6 | 4 | 3 |
| 26712 | 26712 | 26712 | 26712 |

It is thus seen that the Mritiplicand multiplied by tue Multiplier, or by any set of factors into which it can be suparated, gives the same product.

Multiply

## Exercise xviii.

1. 478 by 25.
2. 976 by 42 .
3. 1879 by 63.
4. 1862 by 49 .
5. 8936 by 54 .
6. 4729 by 72 .
7. 2345 by 81.
8. 3764 by 64.
9. 2978 by 45.
10. 3475 by 18 .
11. 7649 by 24.
12. 9365 by 144.
13. In one mile there are 1760 yards, how many yarda are there in 56 miles?
14. If sound travels 1142 feet in one second how far will it move in one minute or 60 seconds.
15. What will 72 bushels of wheat cost at 118 cents for one bushel?
16. If 27 men can do a piece of work in 17 days, how long will it take one man to do the same work?
17. What is the cost of 24 horses at the rate of 125 dollars each ?
18. If a yoke of oxen costs 135 dollars, what will 63 yoke cost?
19. If a man spends 945 dollars in a year, how much will he spend at the same rate in 21 years?
20. There are 1440 minutes in a day; how many min utes are there in 28 days?

## Case II.

45. When the Multiplier exceeds twelve.

Ex. 3. Multiply 479 by 57.

$$
479
$$

57
1st"partial product $3953=7$ times the Multiplicand.
2nd "، $\quad 2395=50 \cdot " \quad$ "
Entire " $27303=57$
Since 57 is composed of 7 units and 5 tens or 50,57 times the number must be equal to 7 times the number, plus 50 times thie number. 7 times 479 is 3353 , the first partial product. We get 50 tirres 479 by frst fuadiug 5 times 479 and then multiplying this result by 10 . 5 times 479 is 2395 and 10 times 2395 is 23950 , the second partial product. We write this under the tirst product so that
units may come under units, tens under tens, \&o., and then we add the two partial products together.

In actual practice we always omit the 0 and write the second partial product as above.

## 46. PROOF.-Multiply the Multiplier by the Multiplicand. If the product is the same as before the work is likely to be correct.

## Exercise xix.

## Multiply

1. 744 by 635 .
2. 895 by 386 .
3. 972 by 243.
4. 825 by 682 .
5. 973 by 745 .
6. 8462 by 781 .
7. 9643 by 683.
8. 8532 by 763.
9. 8984 by 133.
10. 4659 by 886.
11. 28352 by 345 .
12. 41678 by 287.
13. 34073 by 435.
14. 40735 by 628.
15. 29304 by 789.
16. 90705 by 897.
17. 43445 by 678.
18. 37436 by 835 .
19. 88888 by 789.
20. 23567 by 597 .
21. 6484 by 6372
22. 7856 by 3375.
23. 6748 by 6334.
24. 4878 by 3437.
25. 8547 by 7733.
26. 85474 by 2547.
27. 46887 by 3489.
28. 56184 by 5474.
29. 56664 by 4871.
30. 25473 by 4487.
31. 73519 by 4735.
32. 81897 bV 8456,
33. 21346 by 31452.
34. 47309 by 45233.
35. 25737 by 63252.
36. 43629 by 28516.
37. 10786 by 31672.
38. 47396 by 73462.
39. 76448 by 54173.
40. 28354 by 31867.

## 4\%. To multiply when the Multiplicand, the Multiplier, or both, contain ciphers.

Ex. 4. Multiply 2479 by 4006.

4006
$148 \overline{7} \overline{4}$ 9916 9980874
$2479 \quad 4006$ times 2479 equals 4000 times 2479 plus 6 times 2479. 6 timos 2479 is $14874 ; 4000$ times 2479 is 9916000. These partial products are writton one under the other as before, the 0's being omitted.

Exercise Xx.

## Multiply

1. 41. by 307.
1. 7004 by 902.
b. 1:64 by 5004.
2. 2769 by 708.
3. 9006 by 7036.
4. 1684 by 4008 .
5. 2002 by 4103.
6. 3678 by 7068.
7. 9999 by 8008 .
8. 3674 by 200901.

Ex 5. Multiply 614000 by 700 .
This result is the same as that ob.

614000
700
429800000 tained by multiplying 614 by 7, and then annexing to the right five noughts, which is the sum of the number of noughts to the right of both the multiplicand, 614, and the multiplier, 7.

## Exercise xxi

Find the value

1. $0{ }^{\prime} 743 \times 600$.
2. Or $847 \times 700$.
3. Of $9642 \times 6300$.
4. Of $1875 \times 6340$.
5. Of $27 \times 9000$.
6. Of $6000 \times 13$.
7. Of $18000 \times 623$.
8. Of $6400 \times 640$.
9. Of $650 \times 650$.
10. Of $83600 \times 7500$.
11. Of $9230 \times 7000$.
12. Of $8000 \times 61000$.

## Exercise xxii. Prectical Probiems.

1. In 1 ream oi paper there are 480 sheets. How many Whosth are there in 947 reaus ?
2. If $s$ vottou mill manufactures 637 yards oi cloth in - day, how many yards will it make in 307 days?
3. At 125 dollars each what will 49 horses cost?
4. A merchaut bought 29 piecos of cloth; in each piece there were 57 yards; how many yards were there in the whole ?
5. If 19008 pounds of hay are required for the horses of a cavalry regiment for one day, how many pounds will be needed for 206 days?
6. What would be the cost of constructing 809 miles of plank road, at 3975 dollars a mile?
7. How many apples will an orchard containing 208 trees produce, if the average yiold is 1269 applea for each tree $?$
8. In 8 editions of 750 books each, how many pager are there, if each book contains 407 pages?
9. How many yards of sheeting are thero in 57 bales, each bale containing 25 pieces and each picce 43 yards?
11). In a cotton mill thore are 29 looms; each loom can weave 42 yards daily. At this rate, how many yards can be woven in 159 days?
10. A lot cost 420 dollars ; how much will 105 lots cost at the same rate?
11. A drover has 406 cows worth 30 dollars oach : how much are they all worth?
| 13. How much will it cost to build 307 miles of railroad at 4060 dollars a mile ?
12. A contractor built 604 miles of railroad at 6500 dollars a mile; how mnch did he get for :t?
13. If it requires 720 barrels of provisions to eupply an army for one day, how many barrels will bo required for 365 days?
14. If one acre of land costs 9620 dollars, how much will 736 acres cost?
15. If it costs 98650 dollara to build one mile of railroad, how much will it cost to build 2809 miles?
16. There are 15 fiells of ecen; in each field there are 97 rows, and 250 hills in cach row; how many hills are there in the 15 ficldn?
17. How many yard, of sloth are there in 43 bales, each bale containing 73 nicces, and each piece 29 yards?
18. If a railway train 18 miles an hour, how far will it go in 17 day: of 24 hour: each?

## Exercise sxiii.

Practical Problems involving the trevious Rules.

1. B bomint a house for 2990 dollars, and gavo for it 98 cows at 24 dollars oach, and tino rest in money; how much money did he pay?
2. One army contains 4575 mon , and snother 36 times as many, lacking 1986 inen; how many men dre thore in the second army?
3. Mr. Peter's has 2461 gallons of coal oil, Mr. Martin hoss 1146 gallons, and Mr. Bousm has 147 times as much as both; how much has Mr. Deuson?
4. A farmor sold 129 cows at 87 dollars each, and re-

## of $8=$ dudurieucamiov. $62=380$

5. B sold 76 hens at 78 cents each, 96 turkeys at 324 cents each, and received in payment 24000 cents; how much remains due?
6. A's barn cost 2485 dollars, his house cost 3 times as much, and his farm cost as much as both; what was the oost of the house? what was the cost of the farm?
7. A drover bought 36 horses at 145 dollars a heed, and 96 cows at 28 dothars $n$ head; which cost the most, and how much?
8. A's book contains 243 pages, with 2850 lotters on a page, and B's contains 325 pages, with 3465 letters on a page; how many letters in A's book? how many in B's?
9. A man has 75 bags of apples, each bag containing 2 bushels; how much will hereceive for them, at 125 cents a bushel?
10. A farmer sold 25 firkins of butter, each firkin containing 126 pounds, and received for each pound 37 cents; how much did he receive for it all?
11. Find the product of the sum and difference of $\mathbf{7 8 4}$ and 397.
12. It 474 men cut 800 cords of wood in two days, how. long would it take one man to do it?
13. A farmer sold 129 cows at 29 dollars each, and received in payment 2300 dollars; how much yet remains due?
14. A's barn cost 175 dollars; his house cost 16 times as much, and his farm cost as much as both; what was the cost of the house? what was the cost of the farm?
15. A man bought 56 acres of land at 45 dollars an acre, and 78 acres at 62 dollars an acre, and sold the whole at 53 dollars an acre. Did he gain or lose, and how much ?
16. A merchant bought 1600 barrels of flour at 7 dollars a barrel ; he sold 900 barrels at 12 dollars a barrel; and the remainder at 5 dollars a barrel. Did he gain or lose, and how much?
17. If a house is worth 3250 dollars, and the farm on which it stands 3 times as much and 450 dollars more, and the stock on the farm trice as much as the house lacking 2368 dollars; what is the value of the whole?
18. A has 4278 dollars more than $B$, and 1225 dollars less than C, who has 7864 dollars; and $D$ has as much as $A$ and $B$ together. How much has D ?
19. A man invests in trade 450 dollars at one time, at another 840 dollars, at another 1125 dollars, and at another 1640 dollars; hnw much must be added to these sums that the amount invested by him shall be increased three fold?
20. A man sold his house for 4500 dollars, and 250 acres of land at 75 dollars an acre; he got in payment 5000 dollars in cash, 239 cattle at 25 dollars each, and 317 streep at 5 dollars each; how much was still due him?

## Section IV.-Division.

1. John has 9 apoles which he wishes to divide equally among his 3 brothers; how many apples can he give to each?

Hore we are required to divide 99 apples. apples into 3 equal parts. If John 3 gives each brother one apple, it will require 3 apples, and 6 apples would 6 1st remainder. be left. If, now, he gives each of thom 3 anothor apple, it will require 3 more -
apples, and 3 apples would be left. If 3 2nd remainder. he gives then one apioce a third time 3 there would be none left. Henco, it is plain that he can give each of his 0 3rd remainder. brothers 3 apples.

In this example we sec that 9 contains 3 three times, for if we subtract 3 from 9 three times, nothing is left. A number, therefore, may be divided into equal parts by sub. traction. Hence, we see that division is simply a short method of performing several successive subtractions of the samo number.

We might have obtained the result in a shorter way, as follows: Sinco 3 times 3 is 9 , wo see that 3 is contained in 9 three times. Hence, to find how many times one number is contained in a second, we have merely to find what number multiplied by the first will produce the second.
2. How many times 2 horses are 6 horses?
3. How many times 3 cents are 12 cents ?
4. How many times is 5 containd in 15 ?

Since 3 times 5 is 15,5 is contained 3 times in 15.
5. How many timos is 6 contain d in 30 ?
6. If a boy earns 24 dollars, how many times 4 dollars does he earn?
7. How many times 6 boys are 30 boys?
8. Three dogs have 12 feet; how many feet has 1 $\operatorname{dog}$ ?
9. How many times 4 feet are 12 feet ?
10. A. bush has 8 roses; how meny times 2 roses has it? How many times 4 roses?
11. How many times 9 boys are 27 boys?
12. A house has 12 doors; how many times 3 doors has it?
13. How many times 7 horses are 21 horses?
14. How many times is 7 contained in 28 ?
15. How many times is 4 contained in 20 ?
16. How many times is 5 contained in 30 ?
48. When it is required to find how many times one number contains another the process is called Division.
49. The number to be divided is called the Dividend.
54. The number by which we divido is called the Divisor.
51. The number of times the Divisor is contained in the Dividend is called the Quotient.

5\%. When the Divisor does not go an exact number of times into the Dividend, the excess is called the Remainder.

5\%. The remainder, being part of the Dividend, will always be of the same kind or denomination as the Dividend.
54. The Sign of Division is a short horizontal line, with a dot above it and another below it: thus, $\div$. It shows that the number before it is to be divided by the number after it. Thus $8 \div 2=4$ is read, 8 divided by 2 is equal to 4 .
55. Division is frequently indicated by a line. with the dividend above it and the divisor below it thus, $\frac{9}{3}$ signifies that 9 is to be divided by 9 .
56. Division may be divided into two cases:

1. When the divisor dioes not exceed twelve.
2. When the divisor excmeds tivelve.

DIVISION TABLE.


## Oral Exercise.

1. 36 is how many times 4 ? How many times 12 ?
2. How many times 7 is 28 ? Is 42 ? İs 84 ? Is 35 ?
3. How many times 9 in 27? In 45 ? In 63 ? In 99 ?
4. A farmer recoived 8 dollars for 2 sheep; what was the price of each?

Since he received 8 dollars for 2 sheep, for 1 shee $\dot{x}^{\prime}$ he must get as many dollars as the number of times 2 is contained in 8.2 is contained 4 times in 8 , because 4 times 2 is 8 ; hence 4 dollars was the price of each sheep.
5. If a man walks 24 miles in 6 hours, how far will he walk in 1 hour?
6. If 1 man can do a piece of work in 32 days, how long will it take 8 men to do it?
7. If 7 yards of silk can be got for 21 dollars, how much will 1 yard cost?
8. If 27 yards of cloth car bo bought for 3 dollars, how many yards can be got for 1 dollar.
9. If 3 hats cost 9 dollars, how much will 1 hat cost? How much will 7 cost? How much will 12 cost?
10. How many times 5 oranges are 50 oranges? Is tho result a concrete number, or au abstract number?
11. If you can buy a lead pencil for 3 cents, how many can you buy for 24 cents?
12. How many barrels of apples, at 2 dollars a barrel, can be bought for 24 dollars?
13. If a man walks 3 miles an hour, dow many houre will it take him to walk 18 miles?
14. A farmer divides 84 bushels of apples equally among 12 men ; how many bushels does each receive?
15. 72 cents are paid for 12 eggs; how much will 1 cost at the same rate?
16. How long will it take 12 men to perform a piece of work that 1 man can do in 60 days?
17. A man planted an orchavd of 120 trees and put 10 in cach row ; how many rows are there in the orchard i
18. How many wou at 9 dollars a month can be hired 1 month for 81 dollars?
20. If 6 barrels of flour cost 54 dollars, how much will 1 barrol cost?

## Case 1.

## 5'. When the divisor does not exceed Twelve.

Ex. I. How many times is 7 contained in 952 ? Divisor. Dividend. Quotient.
7) $\underset{7}{952} \underset{ }{7} \mathbf{( 1 3 6}$

7
25
21
42
42

> We write the divisor at the left, and the Quotient at the right of the Dividend, and begin -at the left to divide. 7 is con. tained in 9 hundreds 1
hundred times and a remainder. We write the 1 hundred in the Quotient, and multiply the Divisor 7 by the 1 hundred. This gives us 7 hundreds, which we write under the hundreds of the Dividend. We then subtract the 7 hundreds from the 9 hundreds and the remainder is 2 hundreds, or 20 tens. We add the 5 tens of the dividend to these 20 tens and set down the 25 tens. 7 is contained in 25 tens 3 tens times, and a remainder. We write the 3 tens in the Quotient and multiply the Divisor by the 8 tens of the Quotient. This gives 21 tens, which we write under the partial Dividend, 25 tens. We subtract, and the remainder is 4 tens or 40 units. We add the 2 units of the Dividend to these 40 units and set down the 42 units. 7 is contained in 42 units 6 units times. We write the 6 units in the Quotient and multiply the Divisor by the 6 units. This gives us 42 units, which we subtract as before, and nothing remains.

The working of the preceding example may be shortened as follows :-

Divisor 7) 952 Dividend. We write the Divisor to the $\overline{1} 36$ Quotient. left of the Dividend and proceed as follows:-
7 is contained in 9, 1 time and 2 over. We place the 2 before the 5 and thus make 25.7 is contained in 25,3 times and 4 over. We place this 4 before 2 and thus make 42. 7 is contained in 42, 6 times.

When the Divisor does not exceed 12 the multiplication and subtraction are performed mentally the quotient only. boing written down, the work being thus greatly shorteneci. This is called Short Division.

When all the different steps of the solution are written, the process is called Long Division.

## Exercise xxiv.

| $(1 ;$ | $(2)$ | $(3)$ | $(4)$ | $(5)$ |
| :---: | :---: | :---: | :---: | :---: |
| $2) 36($ | $2) 58($ | $2) 54($ | $2(92($ | $2) 96($ |
| $(6)$ | $(7)$ | $(8)$ | $(9)$ | $(10)$ |
| $3) 576($ | $3) 465($ | $6) 723($ | $3) 873($ | $3) 975($ |
| $(11)$ | $(12)$ | $(13)$ | $(14)$ | $(15)$ |
| $4) 852($ | $4) 764($ | $4) 932($ | $4) 576($ | $4) 748($ |
| $(16)$ | $(17)$ | $(18)$ | $(19)$ | $(20)$ |
| $5) 735($ | $5) 850($ | $5)!75($ | $5) 745($ | $5) 835($ |
| $(21)$ | $(22)$ | $(23)$ | $(24)$ | $(25)$ |
| $6) 732($ | $6) 846($ | $6) 924($ | $6) 972($ | $6) 834($ |
| $(26)$ | $(27)$ | $(28)$ | $(29)$ | $(30)$ |
| $7) 784($ | $7) 798($ | $7) 833($ | $7) 9660^{\prime}$ | $7) 959($ |
| $(31)$ | $(32)$ | $(333)$ | $(34)$ | $(35)$ |
| $8) 896($ | $8) 936$ | $8) 944($ | $8) 976($ | $8) 992($ |
| $(36)$ | $(37)$ | $(38)$ | $(39)$ | $(40)$ |
| $9) 468($ | $9) 576($ | $9) 864($ | $9) 738($ | $9) 666($ |

## Exercise xxv.

| (1) | (2) | (3) | (4) | (5) |
| :---: | :---: | :---: | :---: | :---: |
| 2)456 | 2)786 | 2)548 | 2)374 | 2)538 |
| (6) | (7) | (8) | (9) | (10) |
| 3)735 | 3)816 | 3)522 | 3)414 | 3)738 |
| (11) | (12) | (13) | (14) | (15) |
| 3)669 | 3)513 | 3)546 | 3)765 | 3)825 |
| (16) | (17) | (18) | (19) | (20) |
| 1)512 | 4)624 | 4)732 | 4)576 | $8_{4}$ ) 824 |
| (21) | (22) | (23) | (24) | (25) |
| 4)736 | 4)816 | 4)972 | 4)608 | 4)436 |
| (26) | (27) | (28) | (29) | (30) |
| 5)615 | 5)735 | 5) 645 | 6) 785 | 6) 840 |

The pupil is expeoted to work Exercise Xxiv., first by Long Div: wion. and 38It hy Short Division.
$\times \begin{gathered}\text { 5) } 815 \\ \times\end{gathered}$
(36)
6)834
(41)
6)1476
(46)
7) 2569
(51)
8)7256
-
(56)
9) 8892
$5{ }_{5}^{(32)}$
厄) 935
(37)
6) 648
(42)
6) 3336
(47)
7) 4732
(52)
8):3656
(57)
9) 3978
$5 \begin{array}{r}(83) \\ 58 \\ 7\end{array}$
(38)
6)654
(43)
6) 2514
(48)
7) 9456
(53)
8)7576
(58)
9) 2565
5) ${ }^{184)}$
(35)
5)880
(40)
(89)
6) 864
(45)
(44)
6)7338
(49)
(50)
7)9859
7)9870
(54)
8) 29352
8) 111032
(59)
?) 68288
(60;
9)67356

## Exercise xxvi. Practical Problems.

1. At 6 cents each, how many oranges can be bought fo: 354 cents?
2. At 2 dollars a day how many days' work can I hire for 346 dollars?
3. How many pounds of rice at 4 cents a pound can I buy for 3672 cents?
4. In 3 feet there is 1 yard ; how many yards are there in 693 feet?
5. If 8 men can dig 768 rods of ditch in 3 weeks, how many rods can 1 man dig in the same time?
6. If 7 yards of cloth cost 637 cents, what will 1 yard cost?
7. If 9 men can dig 135 bushels of potatoes in 1 day, how many bushels can 1 man dig in 1 day?
8. When 7 is multiplied by a certain number the pro duct is 861 , what is the number?
9. If 6 bins of equal size are exactly filled by 36312 bushels of grain, how much doos each bin hold?
10. If 7 men can cut 56 cords of wood in 4 days, how much can 1 man out in the same time?

Ex. 2. Divide 70268 by 7.
Divisor 7 ) 70268 Dividend.
10038 Quotient, 2 Remainder.
In this example we say 7 is contained in 7 ten thousands, 1 ten thousand times and no remainder. We put down this 1 in the ten thousands' place. 7 is not contained in 0 thousands. We put a 0 in the thousands' place. 7 is not contained in 2 hundreds. We again write a 0 in the hundreds' place. 7 is contained in 26 tens, 3 tens times and 5 over. We write the 3 in the tens' place. 7 is contained 8 times in 58 units and 2 over. We write $S$ in the units' place and indicate the division of the 2 , thus, $\frac{3}{2}$; this is annexed to 10038 , thus, $10038{ }_{2}^{2}$.
58. PROOFF-Multiply the Quotient by the Divisor. and to the Product add the Remainder, if any, and if the result is the same as the Dividend the work is likely to be correct.

## Exercise xxvii.

Divide

1. 6532 by 3.
2. 11236 by 9 .
3. 57636 by 6.
4. 11485 by 7 .
5. 98537 by 8 .
6. 345246 by 5 .
7. 1684245 by 4.
8. 3432126 by 6 .
9. 6216563 by 8 .
10. 7295849 lyỳ 10.
11. 16779120 by 12.
12. 37000305 by 5 .
13. 5767692 by 7 .
14. 56464237 by 9.
15. 46626289 by 11.
16. 2523360 by 6 .
17. 160590736 by 8.
18. 370370480 by 10.
19. 101650247 by 12.
20. 51088982 by 7 .
21. 67320837 by 9 .
22. 30040526 by 11.
23. 106131923 by 12.
24. 740048200 by 8.
25. 45603875 by 10.
26. 836384072 by 9.

Exercise xxviii.

## Practical Problems.

1. When flour is worth 8 dollars a barrel, how many barreis could be bougit for 3456 dollars?
2. If 7 casks of sugar weigh 8792 pounds, what is the avorage weight of cach eask ?
3. A father dying left an estate of 37356 dollars to be divided equally among his wife, his two sons and his three daughters; what was the share of each?
4. Five men bought a horse for 160 dollars; they hire him out at 4 dollars a day for 24 days, and sell him for 120 dollars; how much will each one gain?
5. A grocer bought 15 barrels of flour for 100 dollars; he sold it so as to gain 20 dollars; how much did he receive per barrel?
6. How long will it take two boys, starting at the same place, and travelling in opposite directions, to be 29076 rods apart, if one goes 5 and the other 7 rods in a minute 1
7. If 66 apples are divided equally among 5 boys, how many does each boy receive?

In performing this division we
see that each boy receives $\quad$ 5) 66 Dividond. 13 whole apples, and that

13! Quotient. there is one apple left. This apple, boing part of the dividend, is also to be divided among the 5 boys, but when anything is divided into five equal parts one of the parts is called one-fifth and is written $\frac{1}{3}$. Each boy will, therefore, rective 181 apples.
8. If 4 sacks of coffee weigh 523 pounds; what is the weight of each?
9. If 626 dollars be divided equally among 5 men, what would be the sl are of each?
10. In one week there are 7 days; how many weekn are there in 365 days?
11. John, James and William have altogether 756 marbles, which they wish to divide equally; what will be the share of each?
12. A man has 4 equal lots of land, containing in all 2759 acres; how many acres are there in each lot?
13. If 9 car-loads of freight weigh 141712 pounds, what is the weight in each car-load ?
14. If 8 wagons carry 4384 bricks, how many bricks can be carried on one wagon?

## Case II.

ef. When the Divisor is greater than Twelve.

```
Ex. 3. Divide 4839 by 17. Divisor. Dividend Quotient. 17) 4839 ( 284 34 148 186
79
68
11 Remainder.
```

Since 17 is not contained in 4 thousands any thousand times, we unite the 4 thousands to the 8 hundreds, making 48 hundreds; 17 is contained in 48 hundreds 2 hundred times. We set down 2 as the first figure in the quotient, then multiply 17 by 2 , and subtract the product, 34 from 48. The remainder is 14 . To this remainder we annex the 3 tens of the dividend, making 143 tens; 17 is contained in 143 tens 8 tens times. We set down 8 as the next figure of the quotient, then multiply 17 by 8 , and subtract the product, 136 from 143. The remainder is 7 ; to this remainder annex the next figure of tie dividend. and continue as before.

Ex. 4. Divide 74198 by 37
37) 74198 (2005

74
198
185
18
In this example we find there is no remainder on subtracting 74 from 74 and on bringing down 1, the third figure of the dividend 37 is not contained in it; we therefore write 0 as the second figure of the quotient. When we bring down 9, the next figure of the dividend, 37 is not sontained in 19 ; we therefore write another 0 as the third figure of the quotient. When we bring down 8 the last figure of the dividend, 87 is contained in 1985 times, and we go on as before.
Note.-For every fiure of the dividend brought down one figure must be written in the quotiont.

The proof is the same as in Short Division. 2005 Quotient.

37 Divisor.
14035
6015
74185 Product.
13 Remainder.
74198 Dividend.

## Divide

1. 764 by 31 .
2. 367 by 41.
3. 987 by 53.
4. 4567 by 61.
5. 2936 by 74.
6. 38271 by 65.
7. 29781 by 56.
8. 71847 by 76.
9. 67654 by 122.
10. 39298 by 801.
11. 80157 by 346.
12. 466281 by 936.
13. 159750 by 425.
14. 539902 by 239.
15. 999999 by 198.

## Exercise xxix.

16. 2802690 by 990.
17. 8991207 by 1449.
18. 9672160 by 1560 .
19. 6192138 by 1653.
20. 3515772 by 1736.
21. 9876480 by 1976.
22. 24197460 by 2492 .
23. 8231505 by 1905 .
24. 13896225 by 2975.
25. 16084440 by 5058.
26. 23103465 by 6391.
27. 18356508 by 16074.
28. 572105376 by 78617 .
29. 344943192 by 134376.
30. 1806147420 by 35805.

## Exercise xxx. <br> Practical Problems.

1. There are 24 hours in a day; how many days are there in 1032 hours?
2. If a man walks 25 miles in a day, how long will it take him to walk 950 miles?
3. Sound moves 37060 feet in 34 seconds; how far will it move in 1 second?
4. A drover bought 23 head of cattle for 786 dollars; what was the price per head?
5. In 1 year there are 52 we iss; how many years are there in 9708 weaks.
6. If 75 shares of bank stook sell for 9225 dollars, what is the price per share?
7. A mon bought a farm of 524 acres for 24104 dollars; what was the average price per acre?
8. How many bales could be made out of 281765 pounds of cotton, allowing 517 pounds to the bale?
9. If a steamship sails 5836 miles in 17 days, what would be the average daily distance?
10. A flour barrel holds 196 pounds of flour; how many barrels will it take to hold 406700 pounds?

ABBREVIATED PROCESSES IN LONG DIVISION.
Case I.
60. To divide by a composite number.
61. A Composite Number is one which may be produced by multiplying together two or more numbeis, neither of which is 1 . Since $16=8 \times 2,16$ is a composite number.

Ex. 5. Divide 8769 by 42.
7) 8769
6)1252 and 5 units over $=5$.

208 " 4 sevens over $=28$.
Remainder $=33$.
Since the factors of 42 are 7 and 6 we divide by these factors in succession. First, dividing by 7 we obtain 1252 for quotient and 5 ror remainder. This is 5 units. We then divide the quotient by 6 and obtain 208 for quotient and 4 for remainder. This is 4 groups of 7 units each or 28 units. The remainder is, therefore, 28 units +5 units $=33$ units. Hence the true remainder is found by multiplying the last remainder by the first divisor and widing to the product the first remainder.

Exercise $x \times x i$

## Divide

1. 46827 by 27 .
2. 87468 by 64 .
3. 97648 by 69.
4. 13853 by 45 .
5. 8042396 by 85 .
6. 7808216 by 49 .
7. 8742 by 25 .
8. 76842 by 96.
9. $87 c 48$ by 81.
10. 419421 by 99.
11. 339240 by 132.
12. 806345 by 144.

## Case II.

## 62. To Divide when there are ciphers at the right of the Divisor.

## Ex. 6. Divide 8593 by 700.

The divisor, 700, may be resolved into the factors 7 and 100. We first divide by the factor 100 by cutting off two fis 85 for the quotient and tho figures at the right, and get divide the quotient and 93 for the remainder. We then divide the quotient, 85, by the other factor, 7, and obtain 12 for the quotient and 1 for a remainder. The last remainder, 1, being multiplied by the divisor, 100, and 93, the first remainder, added, we obtain 193 for the true remainder.

Hence, to divide, when there are ciphors at the right of the divisor we cut off the ciphers from the divisor, and the same number of figures from the right of the dividend; we then divine the remaining figures of the dividend by the remaining figures of the divisor and prefix the remainder to the figures cut off, and the result will be the true remainder.

## Exercise xxxii.

## Divide

1. 725 by 30.
2. 7642 by 60 .
3. 8642 by 700 .
4. 97861 by 300 .
5. 72369 by 90 .
6. 94678 by 80 ,

7,00)85,93
12 and 193 rem.
6. A farmer sol 24 horses for 5640 dollars; how much did he receive apiece for them?
7. There are 25 pounds in a quarter; how many quar. ters are there in 34450 oounds?
8. How many bushels of oats at 56 cents a bushel cau be bought for 13272 centis?
9. If 48 acres of land produce 2064 bushels of corn, how much will be produced from one acre?
10. If a man travels 2052 miles in 54 days, what is the average travel per day?
63. If any three of the four numbers, that form the Divisor, Dividend, Qnotient and Remainder be given, we can find the fourth.

1. Let Divisor, Dividend, and Quotient be given. Multiply the Divisor by the Quotient, subtract the result from the Dividend, and we have the Remainder.
2. Let Divisor, Quotient, and Remainder be given. Multiply the Divisor by the Quotient, add the Remainder to the result, and we have the Dividend.
3. Let Divisor, Dividend, and Remainder be given. Subtract the Remainder from the Dividend, divide the result by the Divisor, and we have the Quotient.
4. Let Quotient, Dividend, and Remainder be given. Subtract the Remainder from the Dividend, divide the result by the Quotient, and we have the Divisor.

## Exercise xxxiv.

1. What number divided by 75 will give a quotient of 117 and remainder of 39 ?
2. What number must be taken from 9765 so that it may be exactly divisible by 132 ?
3. Of what number is 483 both divisor and quotient?
4. What number larger than 216 will divide 75168 with. out a remainder?
5. What number must be added to $\mathbf{3 8 4 7 2}$ so that it may be exactly divisible by 879 ?
6. The answer to a question in Mnltiplication is 1404836 and the multiplicand is 5163 ; what is the multiplier?
7. If the quationt be 5000 when the divisor is 2001 and the remainder 100, what is the dividend?
8. What number divided by 528 will give 86 for quotient and leave 44 as a romainder?
9. If the dividend be 784622 and the quotient be 4044, what is the divisor and the remainder?
10. If the quotient be 194; the divisor 4044, and the remainder 87, what is the dividend?

## Exercise xxxv. Practical Problems Involving the Previous Rules.

Ex 1. A carpenter can earn 45 dollars a month; his expenses are at the rate of 24 dollars a month. He wishes to purchase a lot of ground which contains 19 acres, and is held at 42 dollars per acre; in what time may he save enough to make the purchase?

He saves $45-24=21$ dollars a month.
The lot will cost $19 \times 42=798$ dollars ; then the number of months in which he can savo enough to purchase the lot is $798 \div 21=38$ months.
21. A farmer bought land from $A$ at 60 dollars an acre, and the same quantity from, $B$ at 85 dollars an acre. The whole amounted to 53215 dollars; how many acres did he buy from each?
2. A merchant sold a piece of cloth containing 45 yards, another piece containing 57 yards, and another containing 63 yards, at 14 dbllars a yard; what did the whole amount to?
3. A man left 2535 dollars each to his four children, but one of them dying the three remaining children divided the money equally among them; how much did each receive?
4. A man earns 25 dollars a week, and spends 12 dollars a week; he saves 195 dollars; how many weeks does he work?
5. A farmer has 24 cows and 93 sheep, worth 1521 dollars; if the sheep are worth 5 dollars each, how much is each cow worth?
6. If 29 men earn 7946 cents in a day, and 25 boys earn 5450 cents in a day, how much more does one man earn in a day than one boy?
7. How many barrels of flour at 6 dollars a barrel are equal in value to 1100 tons of coal at 9 dollars $a$ ton?
8. If a mechanic earus 52 dollars month, and his expenses are 34 dollars a month, how long will it. take him to pay for s farm of 36 acres. worth 12 dollars an acm?
9. A clerk's salary is 1200 dollars a year; he pays 5 dollars a week for board, 2 dollars a month for car fare, and his other expenses amount to about 1 dollar a day; how much can he save in a year?
10. Mr. Jones bought a farm of 110 acres at 75 dollars an acre, 2200 dollars to be paid down, and the remainder in five equal yearly instalments; what must he pay each year?
11. A man has 18 piles of wood, each containing 25 cords, and each cord 128 cubic feet; how many cubic feet of wood has he?
12. A man exchanged 159 cords of wood at 5 dollars a cord, for a horse valued at 144 dollars, and the balance in sheep at 3 dollars each; how many sheep did he receive?
13. A merchant balancing bis accounts found that he had on hand merchandize worth 475 dollars, and cash amounting to 2570 dollars; he had lóst by bad debts dollars, and owed 525 dollars; if his original capital was 2000 dollars, what had he gained?
14. A cistern containing 13500 gallons is filled by two pipes, one discharging 250 gallons an hour, and the other 300 gallons, but, by a leak in one of the pipes, 100 gallons are lost in an hour ; if the cistern is empty, how long will it take to fill it?

Ex. 2. If 3 pounds of coffee cost 30 cents, what will 8 pounds cost ?
The cost of 3 pounds of coffee $=30$ cents ;

15. What will 15 slates cost, if 5 slates cost 80 cents?
16. If 4 trees cost 72 cents, what will 3 trees cost?
17. If 6 barrels of flour cost 48 dollars, what will 7 barrels cost?
18. What will be the cost of 16 cords of wood, if 4 cords cost 24 dollars?
19. If 15 yards of cloth cost 75 dollars, what will 20 yards cost?
20. If 7 pounds of beef cost 56 cents, what will 5 pounde oost?
 can 4 men earn in the same time?
22. If 28 acres of land cost 4480 dollars, how much will 48 acres cost at the same rate?
23. In 52 years there are 18980 days, how many day: are there in 65 years?
24. Twenty-five barrels of flour weigh 4900 pounds; what is the weight of 36 barrels?
25. If you can buy 765 yards of oloth for 51 dollars, how many yards can you get for 376 dollars?
26. If 38 acres of land cost 11172 dollars, how many acres can be bought for 107310 dollars?
28. If 13 houses cost 16250 dollars, what will 25 houses cost ?
29. If 17 horses cost 1802 dollars, how 'much will 8 horses cost ?
30. Fifteen men can hnsk 1095 bushels of corn in a day; how many bushels can 27 husk ?

Ex. 3. If 7 men do a piece of work in 86 days, in how many days can 28 men do it ?

$$
\begin{aligned}
& \text { Time for } 7 \text { men to do the work }=36 \text { days; } \\
& \begin{array}{rlr}
\text { " } 1 \text { man " } & =7 \times 36 \text { days; } \\
\text { " } 28 \mathrm{men} " \quad ~ " ~ & =\frac{7 \times 36}{28}=9 \text { days. }
\end{array}
\end{aligned}
$$

81. If 15 workmen can do a piece of work in 25 days, in what time can 25 men do the same?
82. A field can be mowed by 40 men in 9 days, in how many days would it be finished by 30 men?
83. If 16 men can build a house in 20 days, how long would it take 10 men to build it?
84. If 19 men can finish a work in 437 days, how long will it take 23 men to do the same work?
85. If 18 horses can cart away the earth from a cellar in 75 days, in how many days would 27 horses do this work ? 36. Ten men engage to build a house in 63 days, but 3 of them being taken sick, how long will it take the rest to build the house?
86. If 6 carpenters can build a house in 72 days, how long would it occupy 9 carpenters to build the same?
87. How long will it take 40 men to build a wall, if 12 men can do it in 20 days?
88. How long will it take 9 men to do the same amount of work that 6 men can do in 15 days?
89. How long will 19 men take to do a piece of work which requires 17 men 133 days to do ?

Ex. 4. If 30 men build a wall in 18 days, how many men will be required to do it in 12 days?

Men required to build the wall in 18 days $=30$ men;

$$
\text { " " " " " } 12 \text { days }=\frac{18 \times 30}{12}=45 \mathrm{men} \text {. }
$$

41. If 4 men can dig a garden in 7 days, how many men would be required to dig it in 1 day?
42. If 28 men can mow a field of grass in 12 dayn, how many men will be required to mow it in 4 days?
43. If 7 men can reap a field of wheat in 18 days, how many men would be required to do the same worlz in 6 days?
44. A piece of work was to have been performed by 144 men in 36 days, but a number of them having been dissharged, the work was performed in 48 days; how many men worked?
45. If 20 men can perform a piece of work in 15 days, now many men will it take to do it in 12 days?
46. How many men in 26 days can perform the same. amount of work that 39 men can do in 76 days?
47. A drain is aug by 49 men in 96 days; how many men would have been required to dig it in 84 days?
48. If 8 workmon can build a wall in 27 days, how many workmen would be required to build it in $\mathbf{3}$ days?
49. If 100 workmen can perform a piece of work in 12 days, how many men are sufficient to perform the work in 8 days?
50. A gentleman met a number of beggars, and relieved 9 of them by giving 25 cents to each one; how many would he have relieved for the same sum had he given them only 15 cents apiece?

## EXAMINATION PAPERS.

I.

1. Define the following terms: Unit, Number, Notation, and Numeration.
2. Add together four millions twenty thousand and sev-enty-nine, twelve millions two thousand and seven, a:ad one million and five thousand, and subtract 16538107 from the sum.
3. Find the remainder after anbtracting the numbers 44444, 9999, 666, 77, 1, in succession from 1000000.
4. Add together the sum, difference, product, and quotient of the two numbers 825 and 9818375.
5. I bought a farm of 186 acres for 8568 dollars, and sold 33 acres of it at 75 dollars an acre, and the remainder for what it cost ; how much did I gain by the bargain?
II.
6. Explain the meaning of the following terms, and give an example of each : Subtrahend, Multiplicand, Product, Divisor, Quotient, Remainder.
7. Find the sum of the following numbers, and express. the result in words: 1234567, 8765433, 6894703, 8105297, 5712848 , and 4187157.
8. What is the difference between the aggregate of 1050, 325, 1769, 150801, and a million. Show that the same difference is obtained by taking one of the numbers from a million, another from the remainder, and so on for the rest of the numbers.
9. Express MMDCXCIX. and CCCXXIX. in the ordinary numerical characters ; find their product, and express the result in Roman characters.
10. How many bushels of wheat, ati 125 cents per bushel, should be exchanged for 250 pounds of sugar, at 8 cents per pound?

## III.

1. From 7503 take 871, and explain the process of "borrowing and carrying" in the common rule of subtraction.
2. How may the process of subtraction be verified? Give an example.
3. By how much does the sum of the numbers 27182818284 and 31415926535 exceed their difference?
4. What arithmetical operation bears the same relation to subtraction that multiplioation bears to addition?
5. Bought a farm for 35380 dollars, and having made improvements valued at 3420 dollars, I sold one-half of it for 21750 dollars, at 75 dollars an acre; how many acres did I purchase, and at what price per acre ?
IV.
6. What is the object of division? Show that it may be considered a shortened subtraction.
7. What are the factors of a number?
8. If division by a composite number be performed by successively dividing by its factora, show how the complete remainder may be found. Ex. 1437281 divided by 105.
9. How much can a man earn in 114 days, if he can oarn 48 dollars in 24 days?
10. A man bought a number of sheep at the rate of 8 for 18 dollars; how many did he buy for 8648 dollars?

## V.

1. What is multiplication? Show by an example thatit is a short method of performing addition?
2. Show by an example that two or more factors will give the same product in whatever order they are multiplied.
.. IIow many times must 1874 be added to itself to make $a$ total of 163038 ?
3. The product of 75 by 43 is 3225 ; how much must be added to it to obtain the product of 77 by 43 ?
4. A drover bought 79 oxen at 42 dollars each; be sold 25 at 40 dollars each; for how much per head must he sell the rest so as to gain 544 dollars on the whole tranaaction $?$

## VI.

1. Given the divisor, quotient and remainder, how is the dividend found?
2. I bought a farm of 150 acres for 12000 dollars; I sold 29 acres at 95 dollars an acre, 75 at 112 dollars an acre, and the rest at 96 dollars an acre; what did I gain by this transaction?
3. What number is that, which being multiplied by $\mathbf{1 5}$, the product divided by 16, the quotient multiplied by 7 , 85 subtracted from the product, the remainder divided by ten, and 52 subtracted from the quotient, the remainder is 18 ?
4. I bought a farm for 6480 dollars, and after spending 890 dollars on improvements on it, I sold one half of it for 4050 dollars at 45 iollars an acre; how many acres did I buy, and at what price per acre?
5. If 16 men can perform a piece of work in 36 days, in how many days can they do it with the aid of 8 more men?

## VII.

1. Explain why in addition of numbers the operation is began at the units' place. Is this necossary? Illustrate by an example.
2. A person willed hin property to hia three elinatam. To the youngest he gave 2149 dollars; to the second 3 times as much; and to the eldest 5 times as much as to the second; find the value of the property.
3. Two ships 8120 miles apart approach each other, the one sailing at the rate of 146 miles a day, and the other at 127 miles; how far will they be apart at the end of 9 days?
4. John found a bagful of coins. On counting them he found there were 5 cent pieces, 10 cent pieces, and 20 cent pieces in it, and the same number of each; how many of each were there, if the whole amounted to 8645 cents ?
5. A gentleman dying disposed of his property worth 53175 dollars, as follows: he left 1500 dollars to a church; 4 times this sum to a college; and he divided the remainder equally among his 5 sons and 2 daughters; what was
the share of each child?

## VIII.

1. If a man has a salary of 2400 dollars a year, and spends 4 dollars a day, how much will he save in 5 yeara, allowing 865 days in a year?
2. What number must be taken 708 times from exeoss so as to leave 69 for remainder?
3. A drover bought 12 head of cattle at 22 doll on mode ; 9 head at 25 dollars each; and 4 head at 32 dc rare eack; at how much per head must he sell them sc to gain 158 dollars?
4. Three boys go picking berries and agre: "o divide the proceeds equally; the first picks 15 quarts and sells them at 13 cents a quart; the second picks 16 quarts and sells them at 12 cents a quart; and the third picks 12 quarts and sells them at 18 cents a quart; find what each one gets.
j. Two iravellers, $A$ and $B$, meeting on a journey, found that the whole distance botib had travelled was 2145 miles, and that $B$ had gone 217 s.and farther than $A$; how

## OHAPTER II.

## Canadian Money.

64. Canadian Money is the legal currency of the Dominion of Canada. It is composed of dollars, cents and mills. The dollar is the unit, and is denoted by the symbol \$.
65. 

> yo mills $=$ y cent. roo cents $=\$ \mathrm{r}$.
66. Dollars are separated from cents, in writing, by a point. Thus $\$ 6.75$ is read six dollars and seventy-five cents. Any number of cents less than ten, when written with dollars, occupies the second place to the right of the point, and the first place is occupied by a cipher ; thus, $\$ 4.05$ is read four dollars and five cents. The mill is one-tenth of a cent and is written one place to the right of the cents; thus, $\$ 3.755$ is read 3 dollars, 75 cents and 5 mills.

6\%. The present silver coins of the Dominion are the fifty-cent piece, the twenty-five-cent piece the ten-cent piece, and the five-cent piece. The only copper coin is the one-cent piece.
Note.-The mill is not coined; it is used only in computation. When the final result of a business computation contains mills, if $\delta$, or more, they are reckoned 1 cent, and if less than 5 they are rejected.
68. Since numbers expressing mills, cents and dollars increase from right to left in the same manner as the numbers with which we have been dealing, they may bo added, subtracted, multiplied, and divided in the same manner.

## Exercise xxxvi.

Read the following :

| $\$ 1.15$. | $\$ 14.25$. | $\$ 21.50$. | $\$ .243$. |
| :--- | ---: | ---: | ---: |
| $\$ 3.24$. | $\$ 6.00$. | $\$ 107.16$. | $\$ .803$. |
| $\$ 1.17$. | $\$ 18.05$. | $\$ 107.60$. | $\$ 8.03$. |
| $\$ 19.30$. | $\$ 25.07$. | $\$ 100.70$. | $\$ 6.003$. |

Write in figures :

1. Five dollars and twonty-five oents; eighty-seven dollars and forty cents.
2. Seventy dollars and sixty-seven cents; two dollars and four cents.
3. Ninety dollars and nine cents; one hundred and one dollars and ten cents.
4. One hundred and twenty-nine dollars and one cent; nine hundred dollars and ninety cents.
5. One thousand dollars; one thousand and seven dollars and three cents.
6. Five thousand three hundred dollars and forty-three cents.
7. Twenty-three thousand and five dollars; forty thousand dollars, forty cents and five mills.
8. Five thousand dollars and five cents; five hundred thousand and nine dollars and thirty-seven cents.
9. Four hundred and eighty thousand dollars; five hundred thousand five hundred dollars, fifty cents and seven mills.
10. One million dollars; one million, one thousand and one dollars, one cent and one mill.

## Reduction.

## Oral Exercise.

1. How many cents are there in $\$ 3$ ?
2. How many cents are there in $\$ 2$ ?
3. How many cents are there in $\$ 3.16$ ?
4. How many cents are equal to a five-dollar bill?
5. How many cents are equal to a dollar bill and 25 cents?
6. How miny cants are there in a half-dollar and a quarter-dollar 3
7. How many conts are there in one dollar and a half!
8. How many ten-cent pieces are there in \$4?
9. How many cents are equal to 2 five-dollar bills ?
10. Huw many five-cent pieces are there in $\$ 2$ ?
11. Reduction is the procoss of changing the denomination or name of a number without changing its value.

Ex. r. How many cents are there in $\$ 9.29$ ?
Since $\$ 1=100$ cents ;
$\$ 3=8 \times 100$ cents or 800 cents;
300 cents and 29 cents make 329 cents;
therefore $\$ 3.29=829$ cents.
Hence in reducing a number of dollars and conts to cents, we simply remove the point.

Ex. 2. How many dollars are there in 6904 cents ?
Since 100 conts $=\$ 1$;

$$
\begin{aligned}
1 \text { cont } & =\$ \frac{1}{100} ; \\
6904 \text { cents } & =\$ \frac{6904}{100}=\$ 69.04 .
\end{aligned}
$$

For when 6904 cents is divided by 100 the quotient is 69, and the remaindor 4 cents.

Hence, in reducing cents to dollars the point must be placeil two places from tho right.

## Exercise xxxvii.

How many cents are there in

1. $\$ 5$;
2. \$29.18;
3. $\$ 361.07$;
4. $\$ 1875.63$;
-. $\$ 20063.07$;
5. 368 cents;

700 cents;
7. 3641 cents ; 7008 cents ;
8. 54168 cents ; - 500700 contio ;
9. 300041 conts; 280014 cents;
10. 2000009 cents ; 7010018 cents ;

1236 cents. 910998 cents. 084007 centis. 340001 cents. 10000091 cents.

## Addition. Oral Exercises.

1. A book cost $\$ 1.25$, and a slate 50 cents; how much did they both cost?
2. A pound of toa cost $\$ 1$, a pound of coffee 25 cents, and a ham 75 cents, what was the total cost?
3. If I pay $\$ 1.20$ for a turkey, $\$ 1.15$ for a goose and 60) cents for butter, how much do I pay for all?
4. Bought a lot for $\$ 6$, a bag of flur for $\$ 4$, and a cord of wood for $\$ 7.50$; how much did $I$ pay for all?
5. Paid 90 conts for paper, 10 cents for pins. and $\$ 1.25$ for a book; how much did I pay for all?
6. A book costs 90 cents, a pen-holder 10 conts, and $u$ slate 35 cents; how much do they all cost?

Ex. 3. Add together $\$ 7.37, \$ 29.78, \$ 0.29 \$ 187.04$ and $\$ 500$.
\$ 7.37 29.78
0.29
187.14
500.00
and write the point in tho cum two places
\$i24.48 from the right to reduce the cents to dollars.

## Exercise xxsviii.

| $(1)$ | $(2)$ | $(3)$ | $(4)$ |
| :---: | :---: | :---: | :---: |
| $\$ 1.36$ | $\$ 184.36$ | $\$ 1843.21$ | $\$ 105.20$ |
| 169.08 | 769.28 | 978.89 | 110.00 |
| 208.72 | 41.07 | 36.07 | 409.00 |
| 714.89 | 869.36 | 862.48 | 1001.65 |

5. A farmer receives $\$ 15.87$ for a cow, $\$ 75$ for a horse, $\$ 3.13$ for some potatoes, and $\$ 5.55$ for some poultry; how much does he receive in all?
6. Sold some velvet for $\$ 3.33$, broadcloth for $\$ 18.75$, silk for $\$ 12.50$, muslin for $\$ 5.40$, carpeting for $\$ 50.05$, a shuwl for $\$ 12.25$; what is the annount of the bill?
7. If a house cost $\$ 3487.75$; repairs, $\$ 53.37$; painting, $\$ 119.23$; furniture, $\$ 1563.39$; moving, $\$ 0$; what was the whole cost?
8. A lady gives $2 \overline{\text { conts }}$ cer needles, $\$ 17.50$ for a dress, $\$ 2.63$ for trimmings, $\$ 1.50$ for a cap, and 12 cents for thread; how muoh does she lay out?

## Subtraction.

## Oral Exercises

1. John bought a book for $\$ 1.50$ and sold it for $\$ 1.75$; how much did he gain?
2. A merchant bought goods for $\$ 4.75$ and sold them for $\$ 6$; how much did he gain?
3. John had $\$ 10$; he paid $\$ 2.50$ for some books, and $\$ 1.50$ for a satchel; how much money has he left?
4. Mary had $\$ 1.25$; she paid 75 cents for some ribbons, and 25 cents for car tickets; how much has she loft?
5. Bought some rice for 60 cents, some sugar for 45 conte and some tea for $\$ 1$; how much change should I get from a five dollar bill?
6. Bought a horse for $\$ 120$, a saddle for $\$ 15$, and sold Both for $\$ 150$; what was my gain?
$X$ 7. I bought a pound of rice for 8 cents, crackers for 15 cents, raisins for 18 cents, candy for 10 cents; how much change should I get back if I gave the clerk $\$ 1.00$.

Ex. 4. John owes $\$ 137.35$ and pays $\$ 29.17$; how much does he still owe?
\$137.35 Placing dollars under dollars and 29.17 cents under cents, we regard the dollars
$\$ 108.18$ and cents as so many cents and subtract as in simple numbers. We then write the point two places from the right of the remainder to reduce the cents to dollars.

Exercise Xxxix.

| $(1)$ | $(2)$ | $(3)$ | $(4)$ |
| :---: | :---: | :---: | :---: |
| $\$ 104.36$ | $\$ 76.14$ | $\$ 200.00$ | $\$ 182.36$ |
| 9.78 | 17.39 | 156.81 |  |

5. A man has $\$ 10000$; he buys a house worth $\$ 4829.36$; how much money has he remaining?
6. John has $\$ 17.21$, James has $\$ 41.00$; how much has James more than John?
7. My salary is $\$ 1000$ a year; I pay for rent $\$ 150$, for groceries $\$ 325.40$, tor putter $\$ 60.30$, for dry goods $\$ 127.6 仑$, and for other expenses $\$ 75.60$; how much do I sone?
8. A man worth $\$ 10000$ gave away $\$ 956.38$, and lost $X$ \$1127.82; what was he then worth?
9. If a lady gives 12 cents for ink, 63 cents for pens,
$\$ 13.30$ for books, and $\$ 1.87$ for paper ; how much change must she get for a twenty dollar bill?
10. Bought $\$ 75$ worth of hay, and $\$ 25.25$ worth of corn; paid $\$ 49.88$; how much is still due:
11. I paid $\$ 4637.25$ for a iarm, $\$ 3675.25$ for build$\chi$ ing a house, and $\$ 2896.87$ for building a burn; I soll my property for $\$ 13000$; how much did I gain?
12. I paid $\$ 246.75$ for a horse, $\$ 325.45$ for \& mulb, $\$ 42.25$ for an ox, $\$ 37.50$ for a cow; I sold them all for $\$ 603.50$; what was the loss?

## Multiplication. <br> Oral Exercises.

1. What will 10 pounds of fish cost at 12 oents $A$ pound?
2. That will 3 pairs of boots cost at $\$ 5.25$ a pair?
3. If I earn $\$ 10.50$ in 1 week, how much ean I earn in 2 weeks?
4. Bought 2 hats at $\$ 1.25$ each, and 3 collars at 25 conts each; how much did I pay for them?
5. Thomas earns 75 cents a day; his oxpenses are 52 cents a day; how much does he save in 7 days?
6. A man bought 4 bushels of wheat al $\$ 1.12$, and sold the flour for $\$ 5$; how much did he gain?
7. Bought 5 barrels of fiour at $\$ 8.50$ a barrel, and 6 bushels of wheat at $\$ 1.25$ a bushel ; what was the cost of both?
8. What is the cost of 2 pairs of chickens at 75 cents a pair, and 5 pairs of ducks at 60 centa a pair?
9. Bought 5 pounds of coffee ar 85 cents a pound, and 12 pounds of ham at 22 cente a pound how much change did I get from a five-dollar bill:

Ex. 5. Multiply $\$ 78.89$ by 8.
$\$ 78.39$
We resard tho dollars and sents as 8 so many cenis, and multiply as in
$\$ 627.12$ Simple Muliphition, and von wo right of the product, to reduce the cents to dollars.

> Exercise xl.

|  |
| :---: |
|  |  |
|  |  |

(3)
(4)
\$247.10
$\$ 48.75$
19
125
6. A farmer sold 175 acres of land at $\$ 37.50$ an aore; how much did he get for the land?
6. A miller sold 525 barrels of flour at $\$ 6.71$ a barrel ; how much did he receive for all of it?
7. What will 42 calves cost at $\$ 3.75$ apiece ?
8. At 37 cents apiece, what will 75 geese cost 9
9. What will 890 cords of wood cost at $\$ 3.78$ a cord ?
10. What will be the cost of 14 yards of black silk at $\$ 1.20$ a yard?
11. If a boy's wages are $\$ 4.75$ a week, how much will he earn in a year, or 52 weeks ?

- 12. If a clerk earbs $\$ 8$ a week, and spends $\$ 4.75$ a week, how much will ho lay by in a year?

13. What will it cost six persons to board for a year at the rate of $\$ 5.75$ apiece each week?
14. What is the value of 17 chests of tea, each weighing 59 pounds, at $\$ 0.72$ a pound ?
15. A merchant sold 15 barrels of pork, each weighing 200 pounds at 12 cents a pound; what did he receive?
16. A lady goes to market with 10 dollars; she buys 6 dozen eggs at 27 cents, 7 pounds of meat at 16 cents, and 3 bushels of potatoes at $\$ 1.25$; how much money has she remaining?
17. A drover bought 95 cows at $\$ 37.25$ each, and sold them at $\$ 40$ each; how much did he make?
18. Mr. Good bought 15 hogsheads of molasses, containing 63 gallons each, at 65 cents a gallon, and sold it at $\$ 1.10$ a gallon; what was his gain ?

## Division. Oral Exercises.

1. If 7 hens cost $\$ 3.57$, what will 1 cost $?$
2. At 5 cenis each, how many oranges can $I$ buy for $\$ 1$ ?
3. I paid $\$ 18.24$ for 6 wicks' board; how much did I pay a week?
4. At 6 cents each, how many lemons can $I$ buy for \$3.72?
5. If 4 hats cost $\$ 5$, what will 7 such hats cost?
6. A yard of calico is worth 12 cents; if I buy 15 yards and give a two-dollar bill in payment, how much change should I get?
7. If a barrel of flour costs $\$ 6.25$, how many barrele can De bought for $\$ 50$ ?
8. At the rate of 15 cents a dozen, how many dozen buttons can be bought for $\$ 3$ ?
9. If I bny 17 pounds of sugar at 10 cents a pound, how many oranges at 5 cents each can I get for the change due me from a five-dollar bill?
10. A yard of calico is worth 9 cents; how many yards can I get for 10 dozen of eggs, worth 18 conts adozen?
11. If I trede 6 pounds of buttor at 20 cents a pound, and 10 pounds of lard at 12 cents a pound, for sugar at 12 cents a pound, how many pounds of sugar do I get?

Ex. 6. Divide $\$ 639.75$ by 5 .
5)639.75
$\$ 127.95$

We regard the dollars and cents as so many cents, and divido as in simple division. Then we place the point in the quotient to separate the dollars from the cents.
Ex. 7. When potatoes are worth $\$ 1.25$ a bag, how many bagfuls can be bought for $\$ 46.25$ ?

125(4625(37
375
875
875
(1)

We are required to find how often $\$ 1.25$ is contained in $\$ 46.25$. We regard $\$ 1.25$ as 125 centa and $\$ 46.25$ ag 4625 cents and then wo divide in the usual way.

## Exercise xli.

## 6) $\$ 76.32$

(2)
(3)
7) $\$ 149.59$
8) $\$ 145.36$
(4)
9) $\$ 237.06$
5. If a person spends $\$ 410.28$ in a year, how much is that a week, allowing 52 weeks to a year?
6. Divide $\$ 2117.71$ equally among 35 fanilies, and find the share of each.
7. A man pays for some land $\$ 400$ cash and $\$ 192.80$ in prodnce. If there were 57 acres, how much does the land cost him per acre?
8. How many sheep can be bought for $\$ 3 n 2.95$ at $\$ 4.15$ each.
9. If 93 oranges cost $\$ 5.58$, what will 37 cost ?
10. I bought a house for $\$ 3453$, and paid for it in instalments of $\$ 575.50$ each ; how many payments did I have to make?
11. William earned $\$ 3.25$ a day, and paid 75 cents for board; in how many days would he save $\$ 019.50$ ?
12. A merchant received $\$ 853.25$ for a case of silk, including $\$ 1.25$ cost of box. How many pieces of silk were in the case, if he recoived $\$ 53.25$ apiece ?
how 1ango fards n? und, at 12

## BILLS.

7(1. A Bill of goods is a written statement of the goods sold, giving the quantity and price of each article and total cost, also the date of the sale, with the names of the buyer and seller.
71. The party who owes is called a Debtor, and the party to whom a debi is owed is called a Creditor.

## SPECIMEN OF A BILL.

Toronto, February 23, 1878.
James Brown, Esq.,
Bought of C. Meredith.

| 1878. \| |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Jan. | 19 | 15 lb . Coffee at 32c. | 4 | 80 |
|  | 23 | 16 " Lard at 15c. | 2 | 40 |
| Feb. | 2 | 25 "Sugar at 13c | 3 | 25 |
|  | 20 | 16 " Ham at 16c | 2 | 56 |
|  |  |  | $\$ 18$ | 01 |

speomen of a receipted blll.
Toronto, March 1, 1878.
John Smith, Dr.
To George Brown.

| 1878. |  |  |  |  | \$ | c. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Jan. | 1 | To 75 lbs. of sugar at \$0.12, | \$9 | 00 |  | c. |
| Feb. | 2 | " 47 yds . of cloth " 3.25 , | 152 | 75 |  |  |
|  |  | Cr. |  |  | 161 | 75 |
| Jan. | 7 | By 75 bu. of corn, at $\$ 0.78$, | \$58 | 50 |  |  |
| Feb. | 2 | " 43 bu . of apples " 1.25 . | 53 | 75 |  |  |
|  |  |  |  |  | 112 | 25 |
|  |  | Balance due, |  |  | \$49 | 50 |

## 1070, 解arch isth.

Received Payment, George Brown.

## Exercise xlif.

Make out bills for the following accounts, supplying dates:

1. Mr. J. Jones bought of R. Walker 10 yards silk, at $\$ 2.50$; 12 yards of flannel, at 40 cents; 16 yards calico, at 15 cents.
2. Mr. Brown bought of McClung \& Bros. 10 pounds tea, at 75 cents ; 8 lbs . raisins, at 18 cents; 5 pounds rice, at 10 cents; 12 lbs. butter, at 21 cents.
3. James Taylor boucht of Thomas Yellowlees 5 quires foolscap, at 25 cents; 1 Hamblin Smith's Arithmetic, at 75 cents; 3 rolls wall paper, at 45 cents; 4 dolls, at 25 cents.
4. David Montgomery bought of F. F. McArthur 20 yards cotton, at 11 cents; 15 yards print, at 16 cents; 12 yards braid, at 6 cents; 3 pairs gloves, at 27 cents; 26 yards dress goods, at 63 cents; 1 hat, at $\$ 5.25$.
5. Robert Davey bought of Murdoch Bros. 18 bags salt, at 75 cents; 4 barrels plaster, at 98 cents; 10 pounds coffee, at 35 cents; 1 chest tea, 18 pounds, at 65 cents; 48 grain bags, at $\$ 3.60$ a doz.
6. Levi Van Camp sold Wm. Burns \& Co. 257 bushels wheat, at $\$ 1.12 ; 475$ bushels oats, at 36 cents; 45 bushels corn, at 76 cents; 175 bushels pease, at 82 cents; 867 bushels barley, at 69 cents.
7. A. Thompson bought of A. Harrison 32 pounds sugar, at 12 cents; 11 pounds coffee, at 35 cents; 26 pounds soap, at 8 cents; 14 pounds rice, at 9 cents; 7 pounds fish at 15 cents; 18 pounds crackers, at 12 cents.
8. W. West bought of T. Brown 27 pairs calfskin boots, at $\$ 4.50 ; 96$ pairs gaiters, at $\$ 2.25 ; 126$ pairs overshoes, at 91 cents; 18 pairs slippers, at 95 cents; 75 pairs heavy boots, at $\$ 2.75$.
9. Mrs. Jones bought of R. Walker \& Co. 25 yards calico, at 12 cents; 12 spools cotton, at 5 cents; 16 yards lipaca, at 75 cents; 17 yards muslin, at 18 cents; 6 ikeins tape, at 2 cents.
10. Murdoch Bros. sold to A. Preston the following: 27 yards calico at 13 cents; 45 yards muslin at 18 cents ; 10 yards linen at 45 cents; 17 yards cambric at 15 cents; and 9 handkerchiefs at 45 ceats; and took in exchange 12 bushels potatoes at 65 cente: 3 barrels apples at $\$ 3.25$, 13 lbs. butter at 35 cents. and the remainder in cash. How much eash was paid? Make out a receipted bill.

## 巴XAMINATION PAPERS.

tilk, at calico, ounds Is rice, quires tic, at at 25

1 A farmer gave $\$ 43.50$ for sheep, at the rate of $\$ 7.25$ for 3 sheop; how many did he buy?

No. of sheep bought for $\$ 7.25=3$ sheep;

8. If 18 chickens cost $\$ 4.20$, how much will 3 chickens cost?
8. A merchant bought 9 pieces of cloth, each containing 50 yards, for which he paid $\$ 2317.50$; what was the ccst of a single yard?
4. $\Lambda$ bauker has $\$ 20000$ in cash; he pays for 50 shares or stock, at $\$ 97.50$ a sbare; and 100 shares, at $\$ 110$ a share ; how many shares, at $\$ 41.25$ each, can he bay with the remainder of his money?
5. I owed $\$ 276$ and paid $\$ 17.25$ on it; how many times must I pay such a sum to cancel the debt?

## II.

1. I retail envelopes at 12 conts a pack, gaining 3 cents on each pack of 24 ; what did they cost me per 1000.

Cost of 24 envelopes $=9$ cents.
2. A grocer sold 9760 pounds of flour, at $\$ 4.25$ per 100 lbs.; what was the amount of the sale?
3. Messrs. Smith \& Co., burn in their store, in a year, 62560 cubic feet of gas, at $\$ 4.50$ per 1000 feet; what is their gas bill for a year?
4. A man bought a quantity of coal for $\$ 250$, and by retailing it at $\$ 5.75$ a ton, he gained $\$ 37.50$; how many tons did he buy?
5. The charge of sending a telegram to a certain place is 40 cents tor ten words, and 5 cents for each additional word; what would a despatch of 24 words cost me?
III.

1. A horse worth $\$ 150$, and 7 cows at $\$ 25$ each, were exchanged for 57 sheep and $\$ 25.75$ in money ; what were the sheep valued at por head?

Value of horse and cows $=\$ 150+7 \times \$ 25=\$ 825$.
Value of sheep $=\$ 325-\$ 25.75=\$ 299.25$.
Hence " 57 sheep $=\$ 299.25$;
Therefore " 1 sheep $=\frac{\$ 299.25}{57}$
$=\$ 5.25$.
2. A merchant bought 5 pieces of cloth of equal lengths, at $\$ 3.25$ a yard; he gained $\$ 18.75$ on the whole cost by selling 4 of the pieces for $\$ 750$; how many yards were there in each piece?
3. At an election there were three candidates $A, B$, and C; the total number of votes polled was 7734. The successful candidate, A, got 203 votes more than C, who got 107 votes less than one-third of the total vote polled ; what was A's majority over B ?
4. A father divided his property worth $\$ 4767$ among his three sons A, B, and C, in such a way that A got as much as $B$ and $C$ together, and $B$ and $C$ shared alike; what was C's share?
5. If the continued product of $275,376,484$ and 196 be divided by $77 \times 28 \times 47 \times 55$, what will be the quotient?

## IV.

1. A merchant expended $\$ 547.40$ for cloth. He sold a certain number of yards for $\$ 522$, at $\$ 1.45$ per yard, and gained on what he sold $\$ 108$. How many yards did he buy and how much did he gain per yard on the cloth he sold?
2. A farmer exchanged 390 bushels of wheat worth $\$ 1.20$ a bushel, for an equal number of bushels of barley at 75 cents a bushel, an? oats at 42 cents a bushel; how many bushels each did he receive?
3. John Turner has manufactured in 4 years 7740 pairs of shoes, making each successive year 250 pairs more than the year before; how many pairs did he manufacture the first year?
4. If 80 men have sufficient provisions for 75 days, and 20 men go away, how long will they last the rest?
5. The product of 275 and 86 is 23650 ; how much must be taken from the product to give the product of 275 and 82 ; and to give the product of 270 and 86 ?

## OHAPTER III.

## MæASURES AND MULTIPLES.

Section 1.-Prime Numbers, Prime Factors, \&c.
192. In the series of numbers $1,2,3,4$, \&c., a distinction may be observed of odd and even numbers.

An Odd number is one which cannot be divided into two equal whole numbers, as $1,3,5, \& c$. An Even number is one which can be divided into two equal whole numbers, as $2,4,6$, \&c.
ry3. There is another, and a more important division of numbers into two classes, one class consisting of numbers, each of which is divisible only by 1 and a number equal to itself, as $2,3,5, \& c$. ; and the other class consisting of numbers which admit of other divisors, as $4,6,8$, \&c. The numbers in the former class are called prime numbers; and those in the latter class composite numbers. (Art. 61).
74. A Prime Number is one which can be exactly divided only by unity and a number equal to itself.
195. The Prime Factors of a number are the prime numbers, which when multiplied together will produce it; thus, 2, 2 and 3 are the prime factors of 12 .

## Oral Exercises.

1. What are the prime factors of $\mathbf{3 0}$ ?

The prime factors of 30 are 3,2 and $\bar{\sigma}$, since these are the only prime numbers which multipłied together will produce 30.
2. Name the prime numbers from 16 to 53 ? from 53 to 101 ?
3. What are the prime factors of 12 ? 16 ? 15 ? 18 ?
4. What are the prime factors of 21 ? 25? 27? 32? 38? 34 ?
5. What prime factor is found in both 6 and 9 ?
6. What prime factor is found in both 20 and 26 ?
7. What prime factor is common to 12 and $30 ? 21$ and 28 ?
8. What prime factor is common to 85 and $50 ? 14$ and 70? is and 99? 42 and 48? 26 and 39 ?
ga. To resolve a number into its Prime Factors.

Ex. x. Find the prime factors of 105.
3) 105
5) $\frac{35}{7}$

Dividing 105 by 8 , a prime factor, we have 35 ; dividing 35 by 5 , a prime factor, we have 7, a prime number, therefore the prime factors of 105 are $3,5,7$.

Exercise xliii.
Find the prime factors of

| 1. | 48. | 5. | 175. | 9. | 429. | 18. | 818. |
| :--- | :--- | :--- | :--- | ---: | :--- | :--- | :--- |
| 2. | 72. | 6. | 270. | 10. | 276. | $1 .$. | 836. |
| 8. | 81. | 7. | 160. | 11. | 800. | 15. | 855. |
| 4. | 108. | 8. | 325. | 12. | 180. | 16. | 1155. |

What prime factors are common to

| 17. | 50 and $70 ?$ | 19. |
| :--- | :--- | :--- |
| 18. | 68 and 147 ? |  |
| and $96 ?$ | 20. | 120 and $600 ?$ |

## Section II.-Cancellation.

ry. Cancellation is the process of shorvening operations in division by rejecting or cancelling equal factors common to both dividend and divisor.

Ex. r. Divide 28 by 8.

$$
\frac{28}{8}=\frac{4 \times 7}{4 \times 2}=\frac{7}{2}=3 \frac{1}{2} .
$$

Write the divisor 8, under the dividend 28. Resolve 28 into $4 \times 7$, and 8 into $4 \times 2$. Cancel the common factor 4 in dividend and divisor, and we have 7 divided by 2 or $8 \frac{1}{2}$.

The same result will be obtained by dividing both dividend and divisor by 4.

Hence cancelling a common factor from both dividend and divisor does not chenge the quotient.

Exercise xliv.

1. Divide $16 \times 4 \times 5$ by $8 \times 2 \times 10$.
2. Divide $7 \times 16 \times 6$ by $14 \times 3 \times 8$.
3. Divide $9 \times 7 \times 16 \times 16$ by $21 \times 32 \times 2$.
4. Divide $27 \times 12 \times 14$ by $9 \times 4 \times 7$.
5. Divide $72 \times 45 \times 140$ by $18 \times 24 \times 35$.
6. Divide $24 \times 82 \times 86 \times 144$ by $64 \times 108 \times 8$.
7. How many yards of muslin, worth 12 cents a yard, may be bought for 16 pounds of butter, worth 15 cents a pound?
8. How many bushels of potatoes at 75 cente a bushel must a farmer give for 36 yards of carpet worth $\$ 1.50$ a yard?
9. A tailor bought 12 pieces of cloth, each containing 22 yards, worth $\$ 2.25$ a yard; he mado 27 suits of clothes; how much must he get per suit so as not to lose?
10. If a farmer exchange 25 bushels of wheat at $\$ 1.20$ a bushel for cloth at 40 cents a yard, how many yards does he get?
11. Three pieces of cloth containing 80 yards each, worth $\$ 5$ a yard, wereaxchanged for 5 pieces of cloth containing 45 yards each; what was the second kind worth per yard?
12. Divide the continued product of $16,18,24,25,30$ and 45 by the continued product of 27,72 and 100.

## Section III.-The Highest Common Factor. Oral Exercises.

Name a common factor

1. Of 6 and 9.
2. Of 12 and 10.
3. Of 27 and 24.
4. Of 16 and 20 .
5. Of 12 and 18.
6. Of 16 and 40 .

What is the highest common factor
7. Of 12 and 10 ? 10. Of 24 and 72 ?
8. Of 20 and 15 ?
11. Of 24 and 12 ?
9. Of 25 and 50 ?
12. Of 72 and 144 ?
98. A Common Factor of two or more numbers is a number that will exactly divide each of the given numbers.
79. The Highest Common Factor, called slso the Greatest Common Measure, of two or more numbers is the largest number that will exactly divide eaoh of the given numbers.

Ex. 1. Find the highest common factor of 18,36 and 72.
6) $18,36,72$ We place the numbers as in the margin.
3) 3, 6, 12 By dividing each number by 6 , we take $1,2,4$. out the common factor 6 ; by dividing each of the quotients by 3 we take out the common factor 3 ; since the quotients $1,2,4$ have no factor common to all of them 6 and 3 are all the common factors of the given numbers, hence $6 \times 3$, or 18 is their H. C. F.

Hence to find the H. C. IF of two or nore numbers, ws divide by any common factor of all the mumbers; we then divide the quotients in'the same manner, and thus continus until the quotients have no common factor; the product of all the divisors will be the highest common,iactor.

## Exercise xlv.

Find the H. C. F.

1. Of $15,20,30$.
2. Of $16,20,24$.
3. Of $24,96,80$.
4. Of $28,56,42$.
5. Of $30,50,60$.
6. Of $84,126,210$.
7. Of 120, 240, 72.
8. Of $44,110,77$.
9. Of $75,300,450$.
10. Oi 144, 576, 720.
11. A man has two logs which he wishes to cut into boards of equal length; one is 24 feet, and the other 16 feet long; what is the greatest length into which the boards can be cut?
12. What is the greatest equal lengths into which two trees can be cut, one being 105 feet in length and the other 84 feet?
13. Three pigces of carpet, of 48,64 and 80 yards, it cut into the longest possible equal lengths, will exactly cover a parlor floor, each piece being the length os the parlor; how long is the parlor?
14. A grocer has 136 quaits of strawberries, and 15\% quarts of plums, which he wishes to put into boxes, each box to hold the same number of quarts, and the largest number possible ; how many quarts may he put into each box?
15. What is the greatest number of pears you could buy with 180 cents, or 225 cents, or 315 cents, so as to get the same number each time?
16. A certain school consists of 182 pupils in the lower echool, and 99 in the upper school; how might each of
those be divided so that the whole school should be dis. tributed into equal sections?
17. To find the H. C. F. when the num. hel's are large.

Ex. 2. Find the H. C. F. of 91 and 143.
21) 143 ( 1

91
62) 91 ( 1

52
89) 52 (1

89
13) 39 ( 8

39 .

That which we are sceking to find is the largest number that will divide both numbers. Now any mumber that will divide two other unubers will also divide their difference or their sum, and as we can soe the factors of a small number more easily than of a large one, we divide the greater of the two numbers by the less; then we divide the less number by the remainder, and each former rerasinder by the new remainder, till we find a number that will divide the last remainder exactly. This will be the H. C. F. of the two numbers.

To find the H. C. F. of more than two numbers, first find the H. C. F. of two of them; then find the H. O. F. of the common factor thus found and a third number ; and so on through all the numbers. The last common factor found will be the H. C. F. of all the numbers.

## Exercise xlvi.

Find the H. C. F. of

1. 115 and 161.
2. 333 and 592.
3. 697 and 820 .
4. 392 and 672 .
5. 405 and 900 .
6. 1220 and 2013.
7. A 12. 14385, 20391 and 49287.
8. A grocer has two hogsheads of sugar, one containing 1104 pounds, and the other 1288 pounds. He wishes to put this sugar into barrels, each barrel to contain the same number of pounds, and this the greatest number possible ; of how many pounds must each barrel consist?
9. A and $B$ purchased horses at the same rate per head; the value of $A$ 's horses was $\$ 623$; and of $B$ 's $\$ 1068$; what was the number purchased by each?

## Sention IV.-Least Common Multiple.

## Oral Exercises.

1. What number is three times 5 ? four times 7 ?

A number which is one or more times anotre number is called a multiple of that number.
2. W? 1 at number is a multiple of 3 ? of 5 ? of 9 ?
8. Name two multiples of 8 ; three multiples of 7.
4. Wbat number is a multiple oi boih 4 and 6? 3 and 5 ?
5. What multiple is common to both 3 and 4 ? 4 and 7 ?
6. Name all the multiples of 4 from 3 to 30 .
7. What is the least number of which 3 and 5 are factors.
8. What is the least number exactly divisible by 8,4 , and 8.
9. What is the least number exactly divisible by 10 and $12 ?$ by 8 and $12 ?$ by 6 and $10 ?$ by 12 and 18 ?
10. James has just enough money to buy oranges at 5 cents each, pears at 4 cents each, or tops at 6 cents each; how much money has he?
81. A Multiple of a numbor is a number that is exactly divisible by that number.
82. A Common Multiple of twe or more numbers is a number that is exactly divisible by each of the given numbers. Thus, 24 is a common multiple of 4 and 6 , because it is exactly divisible by each of them.
83. The Least Common Multiple (I. C. M.), of two or more numbers is the least number that is exactly divisible by each of them.

Ex. 1. Find the least common multiple of 24,20 , and 83.

$$
\begin{aligned}
& 24=2 \times 2 \times 2 \times 8 \\
& 20=2 \times 2 \times 5 \\
& 33=3 \times 11 \\
& \text { L.C.M. }=2 \times 2 \times 2 \times 3 \times 5 \times 11=1820 .
\end{aligned}
$$

The I. C. M. of the given numbers nust contain the factors $2,2,2$ and 3 to be divisible by 24 ; it must contain the factors 2,2 and 5 , to be divisible by 20 ; it must contain the facturs 3 and 11 to be divisible by 88 . Since the number 1320 contains all these factors and no others, it is the least common multiple of 24,20 , and 83 .

Bence to find the I. C. M. of two or more umbers we find the prime factors of the numbers, and take the product of these factors, using each the greatest number of times it occurs in any of the given numbers.
84. When the eeveral numbers are not large, the process may be shortened by successive divisions of the given sumbers, by prime factors which are common to two or more of the given numbers. By this means, all the divisors will consist of the prime factors common to two or more of the numbers, and the numbers left after the divisions will be the factors which are not common to any iwo of the numbers. Then the product of these common prime factors, and the factors which are not common, will be the least common multiple of the given numbers.

Ex. 2. Find the L. C. M. of $15,24,36$, and 42.
2) $15,24,36,42$ Here 2, 2, 3 are the prime factors
2) $15,12,18,21$ common to two or more of the
3) $15,6,9,21$ numbers, and $5,2,3,7$ are the factors not common.

$$
\begin{aligned}
\text { L. C. M. }= & 2 \times 2 \times 3 \times 5 \times 2 \times 3 \times 7=2520 . \\
& \text { Exercise xlvii. }
\end{aligned}
$$

Find the L. C. M. of

1. 15,10 and 5.
2. 20, 10 and 30.
3. 9, 12 and 18.
4. 10, 25 and 30.
5. 24, 30 and 36.
6. 5, 9, 12 and 15 .
7. 12, 15, 18 and 24.
8. $22,55,77$ and 110.
9. $15,30,42$ and 72.
10. $21,54,56$ and 84.
11. $5,7,16,28,48$ and 21.
12. 16, 12, 14, 32, 50 and 75.
13. $15,18,24,40,50,60$ and 90.
14. The even numbers from 14 to 28 inclusivo.
15. The odd numbers from 13 to 25 inclnsive.
16. What is the least number which divided by 8 , by 18 , and br 14 gives in each case the remainder 5 ?
17. What is the least sum of money for which I can purchase citler sheep at $\$ 6$, cows at $\$ 28$, or horses at $\$ 150$ a head?
18. What is the least number of bushels of wheat that would ma'e an exact number of full loads for three drays hauling respectively 24,30 or 36 bushels a load?
19. What is the least number of cents with which you could buy an exact number of lemons at 6 cents apiece ; or oranges at 8 cents; or bananas at 10 cents; or pinn apples at 16 cents?
20. How many bushels would fill a number of barrels, each containing 3 bushols, or a number of sacks, each oontaining 4 bushels, or a number of casks, each containing 14 bushels, the quantity to be the same in each case, and the smallest possible?
21. $A, B, C$, and $D$ start together, and travel the same way around an island which is 600 miles in circuit. A goes 20 miles per day, $E, 30, C, 25$, and $D, 40$. How long must their journeyings contiaue, in order that they may all come together again?

## 巴XAMINATION PAPERS.

## I.

1. How do you determine whether a given number is prime or composite? Which of the following numbers are prime and which composite:-611, 643, 707, 757, 991 1089 ?
2. Divide the continued product of $0,15,16,24,12,21$, and 17 by the continued product of $2,10,9,8,36,7$, and 51.
3. What is the least number of dollars that will purchase an exact number of cows at $\$ 24$ each, sheep at $\$ 6$, ox horses at $\$ 127$ each?
4. What is the least number which, divided by 18,21 , and 30 gives 13 for remainder in each case ?
5. A man owns 3 tracts of land, containing 525, 725, and 875 acres respectively. He wishes to divide each tract into lots that will contain the same number of acres, and this the largest number possible; of how many acres must his lots consist?

## II.

1. Define Highest Common Factor and Prime Factor, and explain when a number is Odd and when Even.
2. Find the largest number which will divide 941 and and 1484 , leaving as remainder respectively 16 and 9.
3. What is the quotient of $1.44 \times 75 \times 15 \times 32 \times 23$ divided by $432 \times 25 \times 8 \times 30$ ?
4. What is the least number of marbles that can be dividod equally among 16, 21, 24 or 30 boys?
5. A can dig 24 post ?1oles in a day; B can dig 25 , and C 30 in the same time. What is the smallest number which will furnizh eanct daýs laiuor eition for each working slone or for all working together?

## III.

1. The product of four conseoutive numbers is 73440 ; find the numbers.
2. What is the least number of acres in a farm that can be exactly divided into lots oi 12 acres, 15 acres, 18 acres or 25 acres each ?
3. A farmer sold 4 loads of apples, each containing 15 barrels, and each barrel 3 bushels at 60 cents a bushel. He received as payment 6 barrels of pork, each weighing 200 pounds ; what was the pork worth a pound?
4. The product of two numbers is 152368 , and 7 times one of them is 2996 ; what is the other one?
5. How many rails will onclose a field 7163 foet long by 3815 feet wide, provided the fence is straight, 6 rails high, the rails of equal length, and the longest that can be used?
IV.
6. A farmer exchanged 9 tubs of butter, each containing 56 pounds, worth 25 cents per pound, for 4 chests of tea, each containing 42 pounds: what was the toa worth per pound?
7. What is the smallest sum of money with which I can buy sheep at $\$ 5$ each, cows at $\$ 24$ each, oxen at $\$ 54$ each, or horses at $\$ 135$ each ?
8. Divide the continued product $151,72,144,972$, and 750 by the continued product of $9,17,18,24,36$ and 45.
9. Find the least number which dividod by 1595, 2530, and 3168 , will leave the same remainder, 719
10. The following are the prime factors of a number : 2 , $2,3,5,5,7,11,11,13,19,89$, and 227 ; find the number.

## V.

1. State and prove the rule for finding the H. C. F. of treo numbers, and find the H.C. F. of 1287000 and 504504.
2. Find the L. C. M. of 16, 24 , and $3 n_{\text {, nd explain the }}$ method.
3. A schoc! was found to contain such a number of boys, that when arranged in sixes, 3erans, nines of twelves, there wero always tive over ; how many children, $x t$ leust, did the school contain?
4. The fore and hind whoels of a carriage are 12 and 15 feet in circumferense; find the least mamber of revolutions of each that will give the same lenoth.
5. Explain the terms mensure ont common mexsurs; and prove, by means of an example, that every common measure of the dividend and divisor is a meadure of the resuainder.

## GHAPTER IV.

## FRACTIONS.

## Section I. Definitions.

## Oral Exercises.

1. If an apple is divided into two equal yrarts, what is one of these equal parts called?
2. How many halves are there in anything? Wrive down one-half. (See example 7, page 42).
3. When I divide an orange into three equal parts, what is one of these equal parts called? What are two of thom called?
4. How many thirds are there in anything? How many fourths are there in anything?
5. How would you get fourths? fifths? sixths?
6. How many thirds make a whole? How many fourths? sevenths ? tenths?
7. Into how many equal parts must a thing be divided to get halves? fifths? serenths? eighths?
8. Two halves of an apple are equal to how many whole apples?
9. What are four fourths of a pear equal to?
10. Which are the smuller, halves or thirds? Halves or fourths? thirds or fourths?

The value of the part varies according to the number of equal parts into which the whole is divided. The more parts it is divided into, the smaller they must be.

| Hale | Third | Half |
| :---: | :---: | :---: | :---: | :---: |
| Tourth $\quad$ Fourth | Fourth | Fhird |

One half of a thing is greater then one third; one third is greater than one fourth.
85. A Fraction is an expression representing one or more of the equal parts of a unit.
86. Fractions are divided into two classes, Com mon, or Vulgar Fractions, and Decimal Fractions.
87. A Common Fraction is one which is expressed by two numbers one placed above the other with a line between them; thus four-fifths is written $\frac{4}{5}$; nine-elevenths, $\frac{9}{1 T}$; ten thirty-fifths, $\frac{10}{36}$.
88. One of these equal parts is called the Fractional Unit and instead of the name of this unit being written after the number of such units as in whole numbers, it is placed under it. Thus, three apples is written 3 apples and 3 fourths, $\frac{3}{4}$.
89. The number written below the line is called the Denominator or "name-giver" because it indicates the name of the fractional unit, i. e. it shows into how many equal parts the whole is divided.
90. The number written above the line is called the Numerator, i.e. the "numberer" or "counter," because it indicates how many of the parts named by the denominator are to be taken.
91. The Terms of a fraction are the numerator and denominator. Thus, $\frac{5}{8}$ is a fraction--5 and 8 are its terms.
92. A Proper Fraction is one whose numerator is less than its denominator. Thus, $\frac{1}{2}, \frac{2}{3}, \frac{7}{8}$ are proper fractions.
93. If we cut an apple into two equal parts, one-half will be represented by $\frac{1}{2}$.
If we cut an apple into four equal parts, one-half will be represented by $\frac{2}{4}$.
If we cut an apple ints oight equal parts, one-half will be represented by $\frac{4}{8}$.

Similarly,

$$
\therefore \frac{1}{2}=\frac{3}{4}=\frac{4}{8} .
$$

If we cut an apple into three equal parts, one-third will be represented by $\frac{1}{3}$.
If we cut an apple into nine equal parts, one-third will be represented by $\frac{\stackrel{5}{y} \text {. }}{}$

[^0]If we cut an apple into eighteen equal parts, one-third will be represented by ${ }_{18}$.

$$
\therefore \frac{1}{3}=\frac{3}{9}=\frac{6}{18} .
$$

Hence, we conclude the value of a fraction is not altered by multiplying or dividing both its numerator and its denominator by the same number.

The following is another proof of this important proposition :

$\mathrm{CD}=\frac{{ }_{15}^{\circ}}{}$ of EF,
and $\mathrm{AB}=\frac{2}{5}$ of EF ;
but $A B=C D$;

$$
\therefore \frac{2}{5}={ }_{15}^{6}
$$

94. By the help of the following proposition, which is best explained by an example, we shall be able to obtain another dofinition of a fraction.

Ex. 1. Prove that $\frac{2}{5}$ of $1=\frac{1}{6}$ of 2 .
Since $1=f i v c$-fifths of a unit,
$2=t e n$-fifths of a unit;
$\therefore \frac{1}{5}$ of $2=\frac{1}{6}$ of $x e n$-fifths of a unit
$=t w o$-fifths of a unit
$=\frac{2}{5}$ of 1 ;
$\therefore \frac{1}{5}$ of $2=\frac{2}{5}$ of 1 .
Hence, we may define a fraction as a simple manner of indicating that its numerator is to be divided by its denominator.
95. Since 3 apples multiplied by $2=6$ apples,
so 3 eighths ( $\frac{3}{8}$ ) " $2=6$ eighths $\left(\frac{6}{8}\right)$;

$$
\therefore 2 \times \frac{3}{8}=\frac{6}{8} .
$$

iaence to multiply a fraction by a whole number, ws simpiy muilipiy the numerator b̄y tīte whole number, and retais tive denominator.

Sinee 8 marbler divided by $2=4$ marbles, so 8 ninths ( $\frac{8}{9}$ ) " $2=4$ ninths ( $\left(\frac{4}{9}\right)$;

$$
\therefore \frac{8}{9} \div 2=\frac{4}{5} \text {. }
$$

Hence a fraction is divided by any number by dividing the numerator by the number and retaining the denominator.
96. From the preceding article it appears that fractions may, in general, be treated as whole numbers. They are in all respects exactly like other dinominations, such as a cent, which is $\frac{1}{100}$ of a dollar, a shilling, which is $\frac{1}{20}$ of a pound, or a penny, which is $\frac{1}{12}$ of a shilling, only it is impossible to find 2 name for every kind of fractional unit which we can employ. It is enough to indicate the unit, as ${ }_{1}^{1} 7,5$ of them being $\frac{5}{17}$.

## Section II-Reduction of Fractions.

## Case I.

9\%. To reduce whole or mixed numbers tc improper Fractions.
99. A mixed Number consists of a whole numbar and a fraction; as $3 \frac{1}{5}, 4 \frac{3}{7}$, \&c.
99. An Improper Fraction is one whose numerator is not less than its denominator.

## Oral Exercises.

1. How many halves in 5 apples?

In 1 apple there are 2 halves, and in 5 apples there are 5 times 2 halves, or 10 halves.
2. How many halves in 6? In 10 ? In 13? In 40 ?
3. How many fourths in 4 ? In 6? In 9? In 12?
4. How many fifths in $4 \frac{3}{6}$ ?

In 1 there are 5 fifths, and in 4 there are 4 times 5 fifths or 20 fifths, winich added to $\mathbf{3}$ fifthe, make 28 fiftius; therefor $\frac{4}{6}=\frac{23}{5}$.
6. How many fourths in $7 \frac{3}{4}$ ? In $5 \frac{3}{4}$ ? In $9 \frac{1}{4} ?$ In $12 \frac{3}{4}$ ?


Ex. I. Reduce $27 \frac{3}{4}$ to fourths.

$$
\begin{gathered}
27 \frac{3}{4}=27+4 ; \\
\text { Now, } \quad 1=\frac{4}{4} ; \\
\therefore \quad 27=\frac{27 \times 4}{4}=\frac{108}{4} ; \\
\therefore \quad 27+\frac{3}{4}=\frac{108}{4}+\frac{3}{4}=\frac{111}{4}=\frac{27 \times 4+3 .}{4} .
\end{gathered}
$$

Hence, to reduce improper fractions to mixed numbers, $\boldsymbol{v a}_{1}$ multiply the whole number by the denominator of the frao tion, add the numerator to the product, and write the denominator under the sum.

Exercise xlviii.
Reduce to improper fractions

1. $3 \frac{4}{7}$.
2. $35 \frac{11}{2}$.
3. $82 \frac{15}{17}$.
4. $51 \frac{17}{23}$.
5. $86_{15}^{5}$.
6. $99 \frac{\mathrm{I}}{\mathrm{I}}$.
7. $78 \frac{19}{9}$.
8. $2377^{1 \frac{3}{3}}$.
9. $304{ }_{2}^{756}$.
10. $1306 \frac{9}{178}$.
11. $2500 \frac{1}{9} \frac{8}{7} \frac{4}{3}$.
12. $10011_{10}^{11} \mathrm{r}$.
13. $2897 \frac{7}{9} 9 \frac{1}{8}$.

## Case II.

100. To reduce improper fractions to whole or mixed numbers.

Ex. 2. Reduce $\frac{87}{17}$ to 3 mixed number.
Since dividing both terms of a fraction by the same number does not change its value (Art. 93),

$$
\frac{87}{11}=\frac{87 \div 11}{11 \div 11}=\frac{710}{11}=7 \frac{10}{11} .
$$

Hence to reduce an improper fraction to a whole or mixea number we simply divide the numerator by the denominator.

## Exercise xlix.

Reduce the following fractions to whole or mixed numbers:

1. $\frac{19}{5}$.
2. $\frac{81}{6}$.
3. $\frac{45}{7}$.
4. $\frac{78}{18}$.
5. $\frac{9}{3}$.
6. $\frac{102}{2}$.
7. $\frac{196}{16}$.
8. ${ }^{982} 16$.
9. $\frac{195}{46}$.
10. $\frac{325}{25}$.
11. ${ }^{\frac{178}{17} \text {. }}$
12. $\frac{582}{19}$.
13. $\frac{4407}{136}$.
14. $\frac{5919}{50}$.
15. $\frac{17007}{33}$.
16. $\frac{32460}{48}$.
17. 95650 .
18. $\frac{73648}{138}$.

## Case III.

101. To reduce a fraction to its lowest terms.
102. A fraction is in its Lowest Terms when the numerator and denominator have no common factor.

Ex. 3. Reduce $\frac{48}{108}$ to its lowest terms.

$$
\frac{48}{108}=\frac{12}{27}=\frac{4}{5} .
$$

Dividing both terms of $\frac{48}{108}$ by the common factor 4, reduces it to $\frac{12}{27}$; dividing both terms of this fraction by 3 , reduces it to $\frac{4}{9}$. Since $\frac{4}{8}$ has its numerator and denominator prime to each other it is in its lowest terms.

We might have found the H. C. F. of the numerator and denominator and divided both terms by it at once.

Hence to reduce a fraction to its lowest terms we divids both terms by a common factor, and the result again by a common factor, and so on till the terms have no comnion factor.

Or we may divide both terms of the fraction by their Highest Common Factor.

Exercise 1.
Reduce the following fractions to their lowest terms.

| 1. $\frac{1}{20}$. | 9. $\frac{2888}{864}$. | 17. $\frac{304}{1072}$. |
| :---: | :---: | :---: |
| 2. $\frac{1}{2} \frac{8}{7}$. | 10. $\frac{792}{864}$. | 18. ${ }^{660}{ }^{\text {T }} 15{ }^{\text {a }}$ |
| 3. $\frac{1}{35}$. | 11. $\frac{840}{4312}$. | 19. $\frac{672}{1088}$. |
| 4. $\frac{24}{36}$. | 12. $\frac{1176{ }^{1} 16 .}{}$ | 20. $\frac{18884}{6940}$. |
| ¢. $\frac{75}{96}$. | 13. $\frac{6161}{717} 1$. | 21. $\frac{42435}{315}$. |
| 6. $\frac{80}{112}$ | 14. $\frac{64}{7} \frac{400}{00}$. | 22. $\frac{3}{42186}{ }^{\text {a }}$ |
| 7. $\frac{210}{294}$ | 15. $\frac{1}{2} \frac{296}{884}$. | 23. $\frac{1109}{2863}$ |
| 8. $\frac{68}{7 \frac{8}{6} \text {. }}$ | 16. $\frac{18}{26989}$. | 24. $\frac{2418}{2887}$. |

Case IV.
19\%. To reảuce a Compound fraction to a Simple one.
104. A Compound Fraction is a fraction of a fraction; as $\frac{1}{2}$ of $\frac{3}{4} ; \frac{3}{7}$ of $\frac{4}{6}$, \&c.
105. A Simple Fraction is one in which both numerator and denominator are whole numbers; as $\frac{8}{4}, \frac{8}{6}, \& c$.

## Oral Exercises.

1. What is $\frac{1}{2}$ or 6 apples? Of 10 boys? Oi 16 oents ?
2. What is $\frac{1}{2}$ of 6 ninths? Of 10 elevenths? Of 10 twentieths?
3. What is $\frac{1}{2}$ of $\frac{6}{9}$ ?

$$
\begin{aligned}
& \text { Since } \frac{1}{3} \text { of } 6 \text { apples }=3 \text { apples, } \\
& \frac{1}{2} \text { of } 6 \text { ninths }\left(\frac{8}{9}\right)=8 \text { ninths }\left(\frac{3}{9}\right) .
\end{aligned}
$$

4. What is $\frac{1}{3}$ of $\frac{12}{17}$ ? of $\frac{18}{2} \frac{8}{2}$ ? of $\frac{1}{2} \frac{8}{5}$ ? of $\frac{9}{22}$ ?
5. What is $\frac{1}{5}$ ol $\frac{6}{7} ? \frac{2}{6}$ of $\frac{5}{7}$ ? $\frac{3}{6}$ of $\frac{15}{18} ? \frac{4}{6}$ of $\frac{2}{2} \frac{1}{5}$ ?
6. What is $\frac{1}{3}$ of $\frac{1}{4}$ ?

$$
\begin{gathered}
\frac{1}{4}=\frac{3}{1^{2}}, \\
\frac{1}{3} \text { of } \frac{1}{4}=\frac{1}{3} \text { of } \frac{3}{12}=\frac{1}{12}
\end{gathered}
$$

7. What is $\frac{1}{2}$ of $\frac{1}{3}$ ? $\frac{1}{5}$ ot $\frac{1}{2}$ ? $\frac{1}{4}$ of $\frac{1}{3}$ ? $\frac{1}{4}$ of $\frac{1}{6}$ ?
8. A boy had $\frac{1}{5}$ of a dollar, and lost $\frac{1}{i}$ of it what part of a dollar did he lose?
9. A man owned $\frac{1}{7}$ of a farm, and sold $\frac{1}{6}$ of his share ; how much did he sell?
10. I had $\frac{1}{2}$ a ton ot coal, and gave my neighbour $\frac{1}{6}$ of it ; he gave his brother $\frac{f}{3}$ ot his share; how much did his brother get?

Ex. 4. Reduce $\frac{3}{6}$ of $\frac{7}{8}$ to a simple fraction.

$$
\begin{aligned}
& \quad \frac{7}{8}=\frac{3.5}{40}, \\
& \frac{1}{5} \text { of } \frac{7}{8}=\frac{1}{6} \text { of } \frac{35}{40}=\frac{7}{40} ; \\
& \therefore \frac{3}{6} \text { of } \frac{7}{8}=3 \times \frac{7}{8}=\frac{21}{4}=\frac{3 \times 7}{8 \times 8} \\
& \quad=\frac{\text { the product of the namerators }}{\text { the product of the denominators }} .
\end{aligned}
$$

Hence to reduce a compound fraction to a simple one, multiply the numerators together for a new numerator, and the denominators together for a new denominator.
'Nots.-Before performing the multiplication, mixed numbers should be reduced to improper fractions wa any factor common to a numerator and denominator casceiled

## 玉xercise $\mathbf{1 i}$.

Simplify the following fractions:

- $\frac{4}{7}$ of $\frac{5}{15}$.

2. $\frac{2}{3}$ of $\frac{9}{2}$.
3. $\frac{3}{4}$ of 4 .
4. $2^{3}$ of $\frac{5}{9}$.
5. $\frac{5}{7}$ of $\frac{4}{8}$ of $\frac{2}{3}$.
6. $\frac{4}{9}$ of $\frac{3}{1}$ of $\frac{6}{8}$.
7. ${ }^{3}$ of $\frac{5}{7}$ of $2 \frac{4}{9}$.
8. $\frac{5}{6}$ of $\frac{6}{7}$ of $\frac{7}{8}$ of $\frac{8}{8}$.
9. $\frac{4}{7}$ of $\frac{3}{4}$ ol $\frac{9}{10}$ of $\frac{7}{16}$.
10. $\frac{5}{8}$ of $\frac{6}{7}$ of $\frac{7}{8}$ of $\frac{8}{17}$.
11. $\frac{8}{4}$ of $\frac{2}{5}$ of $\frac{9}{12}$ of $\frac{2}{3}$.
12. $\frac{1}{2}$ of $\frac{3}{4}$ of $\frac{1}{28}$ of 7 .
13. $\frac{3}{6}$ of $T^{4}$ of $\frac{17}{23}$ of $5 \frac{3}{4}$.
14. $\frac{22}{3}$ of $\frac{8}{7 I}$ of $\frac{1}{2} \frac{5}{2}$ of $9 \frac{8}{8}$.
15. $\frac{5}{7}$ of $8 \frac{3}{4}$ of $\frac{1}{8}$ of $2 \frac{1}{7}$.
16. $\frac{5}{16}$ of $\frac{9}{8}$ of $\frac{1}{8}$ of $4 \frac{1}{4}$.
17. $\frac{2}{9}$ of $\frac{5}{3}$ of $\frac{3}{8}$ of 9 .
18. $\frac{1}{9}$ of $\frac{8}{18}$ of $3 \frac{18}{18}$ of 6 .

Exercise lii.

1. Some boys owned $\frac{2}{3}$ of a boat ; they sold $\frac{3}{4}$ of their share; what part of the boat did they sell?
2. Having $\frac{3}{4}$ of a bushel of potatoes, I gave away $\frac{5}{8}$ of what I had ; what part of a bushel did I give away?
3. A boy had $\frac{9}{10}$ of a dollar, and spent $\frac{9}{6}$ of it; how much did he spend?
4. A gentleman owning $\frac{3}{5}$ of a factory gave $\frac{2}{9}$ of what he owned to his son; what part of the whole factory was the son's share.
5. $A$ has $\frac{4}{7}$ of a ton of hay, which is $\frac{3}{4}$ as much as $B$ has; how much has $B$ ?

$$
\begin{aligned}
& \frac{3}{4} \text { of what } B \text { has }=\frac{4}{7} \text { of a ton; } \\
& \begin{array}{lll}
\therefore \frac{1}{4} & \text { " } & =\frac{1}{3} \text { of } \frac{4}{7} \text { of } a \text { ton }=\frac{4}{2 T} \text { of a ton; } \\
\therefore \frac{4}{4} & \text { " } & =4 \times \frac{4}{2 T} \text { of } a \text { ton }=\frac{1}{2} \frac{6}{2} \text { of } a \text { ton; }
\end{array} \\
& \text {. } \therefore \quad B \text { has } \frac{1}{2} \frac{8}{1} \text { of a ton. }
\end{aligned}
$$

6. A owns $\frac{4}{7}$ of a railroad, and $\frac{3}{4}$ of this is $3 \frac{3}{7}$ times what $B$ owns; how much does $B$ own?
7. How many acres of land has $B$, if $\frac{3}{15}$ of 18 is $\frac{6}{25}$ of his number?
8. $A$ 's money equals ${ }^{\frac{8}{15}}$ of $\$ 8750$, and $A$ 's is $\frac{32}{8}$ of $B$ 's money; how much money has $B$ ?

## Case V.

106. To reduce Fractions to equivalent ones having the least common denominator.
107. Lat 諰 denominutorts be prime to each otiter and the frastions in their simplest form.



Ex. 6. Reduce $\frac{9}{3}$, $\frac{3}{4}$, and $\frac{4}{5}$ to their least common demominator.

Since multiplying the terms of a fraction by the same number does not change its value, we have,

$$
\begin{aligned}
& \frac{2}{3}=\frac{4 \times 5 \times 2}{4 \times 5 \times 3}=\frac{40}{60}, \\
& \frac{3}{4}=\frac{3 \times 5 \times 3}{3 \times 8 \times 4}=\frac{45}{80},
\end{aligned}
$$

And

$$
\frac{4}{5}=\frac{3 \times 4 \times 4}{3 \times 4 \times 5}=\frac{48}{80}:
$$

Hence to reduce fractions to equivalent ones having a common denominator, we multiply both terms of each fraction by all the denominators except its own.

Exercise liii.
Reduce to equivalent fractions having a common donominator

| 1. $\frac{3}{6}, \frac{7}{9}$. | 4. $\frac{2}{3}, \frac{3}{5}, \frac{5}{7}$. | 7. $\frac{3}{5}, \frac{1}{3}, \frac{2}{7}, \frac{1}{4}$. |
| :--- | :--- | :--- | :--- | :--- |
| 2. $\frac{6}{7}, \frac{9}{10}$. | 5. $\frac{5}{7}, \frac{2}{3}, \frac{4}{5}$. | 8. $\frac{5}{7}, \frac{3}{8}, \frac{4}{9}, \frac{11}{13}$. |
| 3. $\frac{8}{9}, \frac{7}{15}$ | 6. $\frac{3}{8}, \frac{2}{3}, \frac{3}{4}$. | 9. $\frac{3}{5}, \frac{6}{8}, \frac{4}{9}, \frac{8}{11}$. |

2. Let the denominators be not prime to each other.

Ex. 6. Reduce $\frac{2}{3}, \frac{3}{4}, \frac{6}{6}$, and $\frac{7}{8}$ to their least com. mon denominator.
L. C. M. of $3,4,6,8=24$.
$\frac{2}{3}=\frac{8 \times 2}{8 \times 3}=\frac{16}{24}$. Wo find the J. C. M. of the denomi$\frac{3}{4}=\frac{6 \times 3}{6 \times 4}=\frac{13}{24}$. nators to he 24 , hence 24 is the least $\frac{5}{6}=\frac{4 \times 5}{4 \times 6}=\frac{20}{24}$. common denominator. Dividing $\frac{7}{8}=\frac{8 \times 7}{3 \times 8}=\frac{21}{24} . \quad 24$ by 3 , the denominator of $\frac{2}{3}$, we find we must multiply 3 by 8 to produce 24 , similarly with the other fractions.

Luto reduce fractions to a common donominator, Wegina the least common multiple of the denominutors, divide this by each denominator, and multiply both terms of the fraction by the quioient.

## Fxercise liv.

Reduce the following fructions to their least oommon denominator.

1. $\frac{2}{3}, \frac{5}{8}, \frac{3}{5}$.
2. $\frac{1}{2}, \frac{3}{4}, \frac{7}{8}$.
3. $\frac{7}{8}, \frac{9}{10}, 2^{7} \pi$.
4. $\frac{5}{9}, \frac{7}{12}, \frac{11}{18}$.
5. $\frac{5}{6}, \frac{4}{8}, \frac{7}{12}$.
6. $\frac{3}{4}, \frac{7}{10}, \frac{5}{6}$.
7. $\frac{1}{2}, \frac{7}{12}, \frac{1}{2} \frac{1}{0}$.
8. $\frac{5}{6}, \frac{4}{5}, \frac{2}{3}$.
9. $\frac{7}{8}, \frac{3}{4}, \frac{4}{6}$.
10. $2, \frac{8}{10}, \frac{4}{8}$.
11. $2 \frac{1}{2}, 3 \frac{1}{3}, \frac{5}{6}$.
12. $\frac{7}{3}, 4 \frac{1}{3}, 5$.
13. $3,4 \frac{1}{3}, \frac{1}{16}$.

ㄷ. $\frac{7}{8}, \frac{5}{14}, \frac{5}{12}, \frac{19}{42}$.
15. $\frac{4}{7}, \frac{5}{1 T}, \frac{9}{77}, 6$.
16. $\frac{4}{15}, 4 \frac{1}{3}, \frac{4}{7}, 2$.
17. $\frac{7}{12}, \frac{17}{2}, \frac{1}{3} \frac{1}{6}, \frac{55}{64}$.
18. $2 \frac{1}{4}, 7 \frac{1}{6}, 3 \frac{3}{9}, 4 \frac{7}{12}$.

10\%. Comparison of Fractions with respect to Magnitude.

To compare fractions we must express them in terms of the same fractional unit, that is we must bring them to a common denominator. When they are so expressed they are compared as other numbers are.

Ex. 7. Arrange the fractions $\frac{5}{8}, \frac{4}{9}, \frac{7}{12}$, in order of magnitude.

Reducing, to equivalent fractions having a common denominator we have $\frac{30}{36} ; \frac{16}{36}, \frac{21}{36}$; hence the order 0 : magnitude is $\frac{4}{9}, \frac{7}{12}, \frac{5}{6}$.

If two fractious happen to have the same numerator, that which has the smaller denominator is the greater; for its units are greater, and there are the same number of them in each.

Fixercise lv.
Find which is the greater,

1. $\frac{4}{7}$ or $\frac{5}{9}$.
2. $\frac{8}{9}$ or $\frac{25}{27}$.
3. $\frac{7}{\frac{7}{6}}$ or $\frac{11}{18}$.
4. $\frac{17}{27}$ or $\frac{2}{25} \frac{1}{2}$.
5. $\frac{15}{18}$ or $\frac{1}{27} \frac{7}{2}$.
6. $\frac{5}{34}$ or $\frac{7}{5^{7}}$.
7. $\frac{7}{40}$ or $\frac{1}{15}$.
8. $\frac{9}{11}$ or $\frac{13}{13}$.
9. $\frac{7}{18}$ or $\frac{10}{21}$.

Which is the greatest and which the least of the following:
10. $\frac{7}{15}, \frac{10}{20}, \frac{16}{3} \frac{1}{3}$ ?
11. $\frac{5}{11}, \frac{9}{22}, \frac{16}{3}$ ?
12. $\frac{3}{16}, \frac{2}{9}, \frac{7}{22}$ ?
13. $\frac{4}{10}, \frac{17}{20}, \frac{21}{25}$ ?
14. $\frac{9}{11}, \frac{13}{15}, \frac{17}{4}$ ?
15. $\frac{5}{6}, \frac{8}{7}, \frac{8}{8}$ ?

Arrange in ascending order of magnitude 16. $\frac{17}{81}, \frac{4}{18}, \frac{5}{47}, \frac{4}{84}, \frac{2}{9} . \quad \left\lvert\, \quad 17 . \frac{1}{2}\right., \frac{3}{3}, \frac{3}{4}, \frac{4}{6}, \frac{1}{2} \frac{4}{8}$.

Section III. Addition.
Case I.
108. To add proper fractions.

## Oral Exercises.

1. What is the sum of 2 apples, 8 apples and 5 apples?
2. What is the sum of 2 elevenths, 3 elevenths and 5 elevenths?
3. How many ninths are $\frac{2}{9}, \frac{4}{9}, \frac{1}{9}$, and $\frac{7}{9}$ ?
4. James paid $\$ \frac{1}{5}$ for a slate, $\$ \frac{2}{5}$ for a reader, and $\$ \frac{4}{5}$ for an arithmetic; how much did he pay fur all?
5. Mary paid $\$ \frac{4}{6}$ for some ribbon and $\$ \frac{5}{6}$ for a pair of gloves; how much did she pay for both?
6. Jane bought $\frac{3}{4}$ of a yard of ribbon at one time and $\frac{7}{8}$ of a yard at another time; how much did she buy at both times?
$\frac{3}{4}=\frac{6}{8}$, and $\frac{6}{8}+\frac{7}{8}=\frac{13}{8}=1 \frac{5}{8}$. She, therefore, bought $1 \frac{8}{8}$ yards.
7. A farmer sold $\frac{1}{6}$ of his grain to one man, and $\frac{1}{6}$ of it to another; how much did he sell altogether ?
$\frac{1}{5}=\frac{6}{30}$, and $\frac{1}{8}=\frac{5}{30} ; \therefore \frac{1}{6}+\frac{1}{6}=\frac{6}{30}+\frac{5}{30}=\frac{11}{30}$.
8. If I pay $\frac{1}{4}$ of a dollar for butter, $\frac{3}{6}$ of a dollar for eggs, and $\frac{1}{2}$ a dollar for cheese ; how much do I pay for all ?
9. What is the sum of $\frac{1}{4}$ and $\frac{1}{6}$ ? of $\frac{1}{6}$ and $\frac{1}{4}$ ? of $\frac{1}{4}$ and $\frac{3}{8}$ ?
10. What is the sum of $\frac{1}{2}$ and $\frac{1}{3} ?$ of $\frac{1}{2}$ and $\frac{2}{6} ?$ of $\frac{2}{3}$ and $\frac{3}{4}$ ?

Ex. I. Find the sum of $\frac{2}{6}, \frac{5}{6}$, and $\frac{3}{10}$.
$\frac{2}{5}+\frac{8}{8}+\frac{3}{10}=\frac{12}{30}+\frac{25}{30}+\frac{9}{30}=\frac{46}{30}=\frac{23}{15}=1 \frac{8}{15}$.
In this example we are required to add fifths, sixths, and tenths together. As the addends have not the same name, we cannot add them till they are changed into others having the same fractional unit. We, therefore, change the fractions into others having a
common denominator, we then add the numerators together for a new numerator, and call the sum 30ths. We reduce the improper fraction to its lowest terms, and then to the mixed number, $1_{18}^{8}$.

Hence, to add fractions, we reduce them to others having a common denominator; we then add the numerators together for a new numerator and place the sum over the common denominator.

## Exercise lvi.

Add together the following fractions :

1. $\frac{2}{3}$ and $\frac{3}{4}$.
2. $\frac{4}{8}$ and $\frac{7}{8}$.
3. $\frac{5}{12}$ and $\frac{7}{18}$ -
4. $\frac{1}{2}, \frac{1}{3}$ and $\frac{3}{4}$.
5. $\frac{1}{2}, \frac{3}{6}$ and $\frac{7}{8}$.
6. $\frac{4}{25}, \frac{9}{40}$ and $\frac{3}{20}$
7. $\frac{5}{6}, \frac{2}{7}, \frac{3}{4}$ and $\frac{8}{13}$.
8. $\frac{3}{4}, \frac{7}{16}, \frac{6}{6}$ and $\frac{5}{12}$.
9. $\frac{3}{5}, \frac{4}{7}, \frac{1}{2} \frac{3}{1}$ and $\frac{7}{16}$.
10. $\frac{1}{4}, \frac{1}{6}, \frac{5}{6}$ and $\frac{2}{9}$.
11. $\frac{2}{3}, \frac{4}{4}, \frac{11}{12}$ and $\frac{29}{42}$.
12. $\frac{1}{3}, \frac{1}{\frac{1}{2}}, \frac{1}{12}$ and $\frac{1}{17}$.

## Case II.

109. To add mixed numbers.

Ex. 2. Add together $2 \frac{1}{4}, 3 \frac{4}{5}, 7 \frac{5}{12}$ and $\frac{9}{10}$.

$$
\begin{aligned}
& 2 \frac{1}{4}+3 \frac{4}{5}+7 \frac{5}{12}+\frac{7}{10} \\
= & 2+3+7+\frac{7}{4}+\frac{6}{5}+\frac{5}{12}+{ }^{7} 0 \\
= & 12+\frac{15}{6}+\frac{48}{80}+\frac{25}{60}+\frac{42}{60} \\
= & 12+\frac{130}{60}=12+2 \frac{1}{6}=14 \frac{1}{6} .
\end{aligned}
$$

Note. - When there are mixed numbers in the example we add the sum of the whole numbers to the sum of the fractions.

## झxercise lvi.

Find the sum of the following fractions:

1. $2 \frac{1}{2}, 8_{3}^{2}$ and $4 \frac{1}{6}$.
2. $2 \frac{1}{3},{ }_{12}^{5}$ and $7 \frac{1}{1}$.
3. $2 \frac{5}{7}, 8 \frac{1}{3}$ and $4 \frac{9}{14}$.
4. $3 \frac{2}{3}, 1 \frac{3}{4}$ and $1^{1} 5$.
5. $1 \frac{5}{19}, \frac{11}{38}$ and $2 \frac{6}{7}$.
6. $80 \frac{4}{6}, 4 \frac{9}{10}$ and $10 \frac{5}{6}$.
7. $2 \frac{1}{3}, 4 \frac{4}{5}, 7 \frac{1}{1_{2}^{2}}$ and $8_{\mathrm{T}_{\frac{5}{8}}}$.
8. $7 \frac{5}{5}, 10 \frac{4}{13}, 4 \frac{1}{3}$ and $7 \frac{7}{30}$
9. $1 \frac{1}{8}, 8 \frac{1}{3}, 2 \frac{3}{4}$ and $5 \frac{5}{12}$.
10. $4 \frac{1}{3}, 5 \frac{1}{4}, 3 \frac{1}{5}$ and $9 \frac{1}{16}$.
11. $4 \frac{2}{5}, 3 \frac{1}{3}, 4 \frac{5}{9}$ and ${ }^{4}{ }^{4}$.
12. $5 \frac{1}{3}, 6 \frac{3}{4}, 3 \frac{2}{5}$ and $\frac{11}{12}$.

## Section IV. Subtraction.

Case I.

## 110. Tosubtract one fraction from another.

## Oral Exercisos.

1. John has 7 marbles, James has 4 ; how many marbles has John more than Jrmes?
2. John has $\frac{7}{12}$ of an apple, James has $\frac{4}{T^{2}}$ of an apple ; how much has John more than James,?
3. How much less is $\frac{3}{8}$ than $\frac{7}{8}$ ? $\frac{8}{8}$ than $\frac{5}{8}$ ? $\frac{3}{8}$ than $\frac{8}{8}$ ?
4. John has $\frac{1}{3}$ of an apple, James has $\frac{1}{4}$ of an apple; how much has John more than James?

$$
\frac{1}{3}=\frac{4}{12}, \text { and } \frac{1}{4}=\frac{3}{12} ; \therefore \frac{1}{3}-\frac{1}{4}=\frac{4}{12}-\frac{3}{12}=\frac{1}{12} .
$$

5. A boy spent $\frac{1}{2}$ of his money for a coat and $\frac{1}{4}$ of it for a hat; how much had hè left?
6. What is the difference between $\frac{1}{3}$ and $\frac{1}{2}$ ? $\frac{2}{3}$ and $\frac{3}{4}$ ?
7. What is the difference between $\frac{3}{3}$ and $\frac{5}{12}$ ? between $\frac{1}{4}$ and $\frac{1}{8}$ ?

Ex. r. From $\frac{7^{-}}{12}$ take $\frac{7}{20}$.

$$
\frac{7}{12}-\frac{7}{20}=\frac{35}{60}-\frac{21}{60}=\frac{14}{60}=\frac{7}{30} .
$$

In this example we are required to take twentieths from twelfths. As we can only subtract numbers that have the same name, we must change the fractions into equivalent ones, having a common denominator. $\frac{7}{12}$ becomes $\frac{3}{6} \frac{5}{0}$, and $\frac{7}{20}$ becomes $\frac{21}{67}$. We now find the difference between $\frac{35}{60}$ and $\frac{2 i}{60}+$ be $\frac{14}{6}$ which reduced to its lowest terms is $\frac{7}{30}$.

Hence to subtract one fraction from another we reduce the fractions to others laving a common denominator; we then subtract the numerator of the subtrahend from the numerator of the minuend; and place tho difference over the common denominutor.

## Exercise lviii

Find the differenco between

1. $\frac{5}{7}$ and $\frac{3}{5}$.
2. $\frac{23}{2}$ and $\frac{43}{4}$.
3. $\frac{7}{2}$ and $\frac{2}{5}$.
4. $\frac{2}{7}$ and $\frac{4}{13}$.
5. $\frac{2}{19}$ and $\frac{6}{9}$.
6. $\frac{5}{9}$ and $\frac{1}{1}$.
7. $\frac{5}{6}$ and $\frac{19}{20}$.
8. $\frac{17}{8}$ and $\frac{4}{5}$.
9. $\frac{5}{7}$ and $\frac{13}{100}$.
10. $\frac{9}{12}$ and $\frac{16}{63}$.
11. $\frac{14}{39}$ and $\frac{15}{65}$.
12. $\frac{9}{36}$ and $\frac{7}{30}$.

## Case II.

111. To subtract when one or both the fractions are mixed numbers.
Ex. 2. From $16 \frac{1}{\frac{1}{3}}$ take $9 \frac{3}{4}$.

We first reduce the fractional parts of the given numbers to their least common denominator, 12. Then, since $\frac{9}{12}$ cannot be taken from $\frac{4}{1^{2}}$, we add 1 or $\frac{19}{12}$ to both minuend and subtrahend, (Art. 38). This gives $16 \frac{16}{2}$ for minuend and $10 \frac{9}{12}$ for subtrahend. Then subtracting the fractions and integers separately we have $16 \frac{1}{2}-10 \frac{9}{12}=6 \frac{7}{12}$, the required result.

Note.-The fractional part of the result can be obtained much more readily by subtracting the numerator of the fraction in the subtrahend from the common denominator and adding the remainder to the numerator of the fraction in the minuend. Thus $12-9=3 ; 3+4=7$. This is the numerator of the fractional part of the result. The integral part is obtained as above.

Exercise lix.
Find the value of

1. $3 \frac{3}{7}-1 \frac{4}{5}$.
2. $2 \frac{1}{8}-1 \frac{1}{10}$.
3. $6 \frac{1}{2}-2 \frac{1}{12}$.
4. $8 \frac{3}{7}-5 \frac{4}{9}$.
5. $3 \frac{5}{12}-1 \frac{5}{6}$.
6. 9-43 .
7. $2 \frac{5}{6}-1 \frac{7}{12}$.
8. $18 \frac{2}{9}-5 \frac{5}{6}$.
9. $5 \frac{3}{14}-2 \frac{2}{2} 0$.
10. $28 \frac{16}{63}-3 \frac{9}{14}$.
11. $4 \frac{7}{8}-1 \frac{1}{4} \frac{3}{4}$.
12. $25 \frac{7}{10}-14 \frac{1}{16}$.

Exercise lx.

## Practical Problems.

1. The sum of two numbers is $26 \frac{1}{4}$ and the less is $7 \frac{5}{7}$; what is the greater ?
2. From a barrel of vinegar containing $31 \frac{1}{2}$ gallons, $14 \frac{1}{16}$ gallons were drawn; how much was there left?
3. To what fraction must the sum of $\frac{1}{3}$ and $\frac{1}{18}$ be added. that the sum may be $\frac{14}{15}$ ?
4. From a piece of silk containing $35 \frac{2}{6}$ yards, $14 \frac{3}{3}$ yards were sold; how much remained in the piece ?
b. From $\$ 10$, $2 \frac{1}{\text { t }}$ were given to James, $\$ 8 \frac{1}{4}$ to Jane, S1 $\frac{1}{2}$ to Emily, and the remainder to Mary ; what did the receive?
5. A has two farms, one of $70 \frac{3}{7}$ acres and the other of $118 \frac{1}{35}$ acres ; if he sells $87 \frac{1}{2}$ acres, how much land has he left?
6. How much paper has a printer left if he had on hand $30{ }^{7} \frac{7}{2}$ reams, and has used 7 7 年 reams for one job, and 83 reams for another?
7. A grocer, having mixed $15 \frac{3}{7}$ pounds of tea with $1 h^{2}$ pounds of a different kind, sold all the mixture but $18 \frac{1}{3}$ poands ; how much did be sell?
y. B started on a journey of 100 miles; the first day he travelled $30 \frac{5}{12}$ miles, the second day $86 \frac{6}{9}$ miles; how far has he yet to go?
8. Henry had $\$ 47 \frac{1}{3}$, and James as much lacking $\$ 9{ }^{\frac{4}{\delta}}$; how many dollars had James?
9. The selling price of a horse was $\$ 125 \frac{3}{7}$; the gain was $\$ 26 \frac{3}{5}$; what was the cost price?
10. Hind the sum of the greatest and least of the fractinns $\frac{3}{8}, \frac{5}{21}, \frac{4}{9}, \frac{7}{20}$, the sum of the other two, and the difference of these sums.

## Exercise lxi. Practical Problems.

1. $\$ 249 \frac{1}{4}$ is $\$ 134 \frac{1}{3}$ less than the value of $m y$ horse and carriage ; what are they worth?
2. A boy paid $\$ \frac{1}{5}$ for a ball, $\$ \frac{1}{6}$ for a slate, $\$ \frac{7}{8}$ for a knife and $\$ \frac{7}{13}$ for a book; how much did he spend?
3. What is the entire weighi of 4 crocks of butter weighing as follows: the first $10 \frac{1}{4}$ pounds; the second, 11尔 pounds; the third, $18 \frac{{ }^{5}}{16}$ pounds, and the fourth $14 \frac{1}{2}$ pounds ?
4. Three men bought a horse; the first paid $\$ 41 \frac{5}{8}$, the second paid $\$ 53 \frac{11}{2}$, and the third as much as the other two ; what was the cost of the horse?
5. A grocer has 3 barrels of molasses; the first contains 278 gallons, the second, $42 \frac{7}{18}$, and the third, $36 \frac{5}{6}$ gallons; how many gallons are there in the three barrels?
6. What number is that from which if $5 \frac{1}{1} \frac{1}{2}$ is taken the remainder will be $2 \frac{17}{17}$ ?
7. A merohant sold $84 \frac{5}{6}$ yards of cloth for $\$ 94{ }^{5}{ }^{6}$, $39 \frac{25}{27}$
yards for $\$ 124 \frac{5}{6}$, and $70 \frac{5}{6}$ yards for $\$ 184 \frac{2}{3}$; how many yards of oloth did he sell and how much did he receive for the whole?
8. Four geese weigh respectively $9 \frac{5}{3}, 10 \frac{2}{3}, 12 \frac{7}{18}$ and $11 \frac{6}{6}$ pounds; what is their entire weight?
9. A lady hired a gardener at 15 cents an hour for 8 days; how much did she pay him if he worked $6 \frac{6}{12}$ hours the first day, $7 \frac{8}{6}$ the second, and $5 \frac{3}{4}$ the third?
10. If $5 \frac{6}{7}$ gallons of brandy are mixed with $1 \frac{9}{12}$ gallons of water and $3 \frac{{ }^{5}}{5}$ gallons of whiskey, how many gallons ure there in the mixture?
11. A paid $\$ 46 \frac{1}{2}$ for an ox, and $\$ 57 \frac{5}{1^{2}}$ more than this for a horse ; for how much must he sell them to gain $\$ 26 \frac{7}{9}$ ?
12. A owns $71 \frac{5}{8}$ acres of land, $B$ owns $112 \frac{5}{18}$ acres; C owns $217 \frac{17}{2}$ acres, and $D$ owns $372 \frac{17}{2}$ acres; how many acres do they together own?

## Section V. Multiplication of Fractions.

## Case x .

- 112. To multiply a fraction by a whole number.

Ex. I. Multiply $\frac{3}{10}$ by 5.
Since 3 apples multiplied by $5=15$ apples,
so 8 tenths ( $\frac{3}{10}$ ) multiplied by $5=15$ tenths ( $1 \frac{5}{10}$ );

$$
\therefore 5 \times \frac{3}{10}=\frac{18}{10}=\frac{6 \times 8}{10}
$$

But $\frac{5 \times 8}{10}=\frac{3}{2}(\operatorname{Art.77})=\frac{3}{10 \div 5}$.
Hence, to multiply a fraction by any number we oither. multiply the numerator or divide the denominator by it.

## Oral Exercises.

1. What is the cost of 6 yards of oloth at $\frac{3}{4}$ of a dollar a yard?

Cost of 1 yard $=\$$ ? ;
" 6 yards $=6 \times \$ \frac{3}{4}=\$ \frac{1}{8}=\$ 4 \frac{1}{2}$.
2. If a man earns $\frac{3}{4}$ of a dollar in 1 day, how much can be carn at the same rate in 12 days?
3. If a yard of cloth costs $\frac{3}{6}$ of a dollar, how much will 9 yards cost?
4. If a bushel of potatoes costs $\frac{7}{8}$ of a dollar, what will 5 bushels cost ?

5 If a yard of ribbon costs $\frac{3}{7}$ of a dollar, how much will 10 yards cost ?
6. If a basket holds $\frac{8}{8}$ of a bushel of apples, how many bushels will 9 baskets hold?
7. If a barrel of flour costs $\$ 8 \frac{3}{4}$, what will 5 barrela cost?

Multiply the fractional and integral parts separately and add the products.
8. If a yard of cloth costs $\$ 2 \frac{5}{8}$, what will 7 yards cost?
9. How much is 6 times $\frac{7}{8} ? \frac{9}{10}$ ? $\frac{1}{1 \frac{1}{2}} ? \frac{3}{6}$ ?
10. How much ic 8 times $\frac{10}{12}$ ? $\frac{9}{12}$ ? $\frac{6}{8}$ ? $\frac{6}{6}$ ?
11. How much is 10 times $1 \frac{3}{20}$ ? $2 \frac{3}{24}$ ? $6 \frac{1}{8}$ ? $8 \frac{6}{12}$ ?

## Exercise lxii.

Multiply

1. $\frac{1}{1} \frac{6}{8}$ by 9. $\quad$ 4. $\frac{14}{14}$ by $10 . \mid$ 7. $\frac{1}{1}_{18}^{8}$ by 21.
2. $\frac{12}{15}$ by 8 .
3. $\frac{9}{28}$ by 7 .
4. $\frac{1}{21}$ by 49 .
5. $\frac{11}{14}$ by 91 .
6. $\frac{8}{18}$ by 24 .
7. $\frac{15}{182}$ by 36 .
8. At $\$ 1 \frac{1}{4}$ a day, how much does a man earn in 4 weeks, of 6 days each?
9. What is the cost of $\mathbf{3 6}$ dozen eggs, at $86 \frac{1}{2}$ cents a dozen?
10. At $\$ 16 \frac{3}{4}$ a month, what will a buy earn in 12 months?
11. What is the cost of 12 pounds of beef at $14 \frac{3}{4}$ cents a pound?
12. What is the cost of 14 bushels of oats at $62 \frac{1}{2}$ cents a bushel ?

## Case ri.

113. To multiply a whole number or a fraction by a fraction.

The definition of multiplication given in Art.- 35, has no meaning when applied to fractions. Since the multiplier must always be an abstract number (Art. 40) we can no more multiply by $\frac{2}{3}$ than by 2 apples. We must, therefore, extend the meaning of the sign, $x$, whon we apply it to fractions.

It is found convenient to agree that $\frac{2}{8} \times \frac{4}{6}$ shall mean 5 of $\frac{4}{5}$.

## Exercise lxiii.

Note.-Cancel the factors common to the numerators and the denominators.

Find the value of

1. $\frac{5}{6} \times 18$.
2. $\frac{8}{9} \times 45$. 8. $\frac{6}{6} \times 43$.
3. $\frac{7}{16} \times 124$.
4. $1 \frac{12}{2} \times \frac{2}{10}$.
5. $\frac{9}{10} \times{ }_{2}^{5} \mathrm{~T} \times \frac{7}{25}$.
6. $\frac{6}{7} \times \frac{9}{12} \times \frac{14}{12}$.
1.3. What should be paid for $\frac{1}{2}$ of $\frac{7}{8}$ ot a pound of tea, at the rate of $\frac{13}{16}$ of a dollar per pound?
7. What should be paid for $\frac{2}{3}$ of a barrel of apples, if the whole barrel is worth $\frac{18}{16}$ of a dollar?
8. $A$ has $\frac{3}{4}$ of $\$ 375, B$ has $\frac{4}{5}$ as much, and $C \frac{8}{5}$ as much as both ; how many dollars haseach, and how many have they all?

Ex. 3. Multiply $6 \frac{2}{5}$ by $7 \frac{4}{5}$.

$$
\begin{aligned}
7 \frac{4}{5} & =\frac{39}{5}, \text { and } 6 \frac{2}{3}= \\
\therefore 7 \frac{20}{8} & \times \frac{2}{3}
\end{aligned}=\frac{39}{5} \times \frac{20}{3}=\frac{13}{13} \times \frac{4}{2}=52 .
$$

Exercise lxif.
Find the value oi

1. $34 \times 5 \frac{2}{7}$.
2. $89 \frac{3}{6} \times 83$ ㅎ.
3. $6 \frac{2}{3} \times 7 \frac{2}{5}$.
4. $17 \frac{2}{5} \times 16 \frac{3}{3}$.

-     - 

7. If a cord of wood costs $\$ 44$, what will $3 \frac{1}{3}$ cords cost?

$$
\begin{aligned}
\text { Dovt of } 1 \text { cord } & =\$ 4 \frac{1}{4} ; \\
\quad 8 \frac{1}{2} \text { cords } & =8 \frac{1}{2} \times \$ 4 \frac{1}{2} \times \$ \frac{17}{4}=\$ \frac{119}{8}=\$ 14 \frac{7}{8} .
\end{aligned}
$$

8. Tf pound of sugar is worth $9 \frac{1}{2}$ cents, what will $4 \frac{1}{2}$ pounds cost?
9. If a man reaps $3 \frac{3}{4}$ acres of wheat in a day, how many acres could he reap in $2 \frac{2}{3}$ days?
10. What would be the cost of $18 \frac{3}{4}$ acres of land at $\$ 18 \frac{3}{4}$ per acre?
11. If $a$ ton of coal costs $6 \frac{7}{8}$ dollars, what will be the cost of $9 \frac{4}{6}$ tons at the same rate?
12. Mr. Jones rented a house at $\$ 42 \frac{3}{3}$ a month, taking t, lease for 5 years; but disposed of the lease at the end of 8i years: how much rent did he pay?
13. A vill of books at retail amounts to $\$ 375 \frac{5}{8}$, but $I$ got a reduction of $\frac{1}{3}$ for wholesale and $z^{3}$ 万 for cash; what was the exact amount of the bill?

## Section VI.-Division of Fractions

## Case 1.

114. To divide a fraction by an integer. Oral Exercises.
115. If 8 apples are divided by 4 , what is the quotient ?
116. If 8 ninths are divided by 4, what is the quotient?
117. Divide $\frac{9}{9}$ by $2 ; \mathrm{T}^{6}$ by $3 ; \frac{18}{17}$ by 8 .
118. If 3 ducks cost $\frac{6}{10}$ of a dollar, how much will 1 duck cost?

Cost of 3 ducks $=\${ }^{\frac{6}{6}}$;
" 1 duck $=\frac{1}{3}$ of $\$ \frac{\beta}{10}=\$ \frac{2}{10}=\$ \frac{1}{6}=20$ cents.
6. If 8 caps cost $\frac{9}{10}$ of a dollar, how much will 1 cap cost?
6. William had $\frac{9}{12}$ of an crange, and divided it eqnally among 3 of his schoolmates; what part of an orange did he give to each?
7. A man shares $\frac{8}{9}$ of a ton of coal among 6 persons, how much does each get?

Share of 5 persons $=\frac{8}{8}$ of a ton;

$$
\begin{aligned}
\text { "1 person } & =\frac{1}{5} \text { of } \frac{8}{8} \text { of a ton; } \\
& =\frac{8}{46} \text { of a ton. }
\end{aligned}
$$

8. If 8 men can do $\frac{3}{5}$ of a piece of work, how much can 1 man do in the same time ?
9. If 3 men together own $\frac{2}{3}$ of a vessel, what part of the vessel does 1 man own, if their shares are equal?
10. A lady gave $\frac{3}{6}$ of a pound of candy to her 4 sons and 2 daughters; what was the share of each?

Ex, x. Divide $\frac{8}{8}$ by 4.
Since 8 apples divided by $4=2$ apples, so 8 ninths ( $\frac{8}{9}$ ) " $\quad$ = 2 rinths ( $\left(\frac{2}{9}\right)$;

$$
\therefore \frac{8}{9} \div 4=\frac{2}{9}=\frac{8 \div 4}{9}
$$

We may obtain the same result by multiplying the denominator of $\frac{8}{9}$ by 4 , and reducing the resulting fraction to its lowest terms; thus

$$
\frac{8}{9} \div 4=\frac{8}{4 \times 9}=\frac{2}{9}
$$

Hence to divide a fraction by any number we eitner divide the numerator by the number or multiply the do nominator by it.

## Exercise lxv.

Note. Reduce mixed numbers to inaproper fractions. Divide

1. $\frac{15}{17}$ by 5
2. $\frac{35}{40}$ by 7 .
3. $\frac{63}{64}$ by 9 .
4. $\frac{7}{8}$ by 17 .
5. $7 \frac{1}{5}$ by 6.
6. $4 \frac{2}{3}$ by 7 .
7. $4 \frac{5}{7}$ by 10.
8. 1293 by 16 .
9. $287 \frac{5}{8}$ by 12.
10. If a man can reap $22 \frac{3}{4}$ acros of wheat in 7 days, how much could he reap in 1 day?
11. If a man can cut $15 \frac{3}{4}$ cords of wood in 7 days, how many cords could he cut in 1 day? ${ }^{\circ}$
12. If a man can walk $38 \frac{1}{3}$ miles in 10 hours, how far could he walk in 1 hour?
13. If 7 tons of coal cost $\$ 60 \frac{2}{3}$, what is the price per ton 1

## Case II.

115: To divide a whole number or a trac. tion by a fraction.

Ex. 2. Divide $\frac{2}{3}$ by $\frac{5}{5}$.

$$
\frac{2}{3}=\frac{10}{15} \text {, and } \frac{3}{5}=\frac{9}{15} .
$$

Since 10 apples divided by 9 apples $=\frac{10}{9}$,
so 10 fifteenths $\left(\frac{10}{15}\right)$ divided by 9 fifteenths $\left(\frac{9}{15}\right)=\frac{10}{9}$;

$$
\begin{aligned}
\therefore \frac{2}{3} \div \frac{3}{5} & =\frac{10}{15} \div \frac{9}{15}=\frac{10}{9} \\
& =\frac{6 \times 2}{3 \times 3}=\frac{5}{3} \times \frac{2}{3}
\end{aligned}
$$

- dividend multipliei by divienr inverted.

Ex. 3. Divide 10 by $\frac{3}{4}$.

$$
\begin{gathered}
10=\frac{10}{1}=\frac{40}{4} . \\
10 \div \frac{3}{4}=-\frac{40}{4} \div \frac{3}{4}=\frac{40}{3}=\frac{4 \times 10}{3 \times 1}=\frac{4}{3} \times \frac{10}{1} . \\
=\text { dividend molteplied by d:visor inverted. }
\end{gathered}
$$

Hence to divide one fraction by another, invert the divisor and multiply the dividend by the fraction thus formed.

## Oral Exercises.

1 At $\$ \frac{3}{8}$ a yard, how many yards of cloth can be bought ใ01 $\$ 0$ ?

Yards bought for $\$ \frac{3}{\delta}=1$ yard;

$$
\begin{array}{ll}
\text { " } & \text { " } \$ 1=1 \div \frac{5}{6}=\frac{5}{3} \text { yards ; } \\
\text { " } & \text { " } \$ 6=6 \times \frac{5}{3} \text { yards }=10 \text { yards. }
\end{array}
$$

2. If a yard of cloth costs $\$ \frac{5}{6}$, how many yards can be bought for $\$ 10$ ?
3. If a bottle holds $\frac{1}{6}$ of a gallon, how many bottles will be required to hold 5 gallons?
4. If a bushel of apples costs $\frac{3}{4}$ of a dollar, how many bushels can be bought for $\$ 12$ ?
5. How many times is $\frac{1}{3}$ contained in $10 ?$ in $15 ?$ in $20 ?$
6. How often is $\frac{3}{4}$ contained in $9 ?$ in $6 ?$ in 12 ?
7. How many baskets holding $\frac{3}{4}$ of a bushel each will be required to hold 15 bushels of peaches?
8. If a quire of puper costs $\$ \frac{3}{10}$, hew many quires can I get for $\$ \frac{4}{5}$ ?
9. When apples are worth $\$ \frac{3}{4}$ per bushel, how many bushels can be lought for $\$ \frac{3}{5}$ ?
10. At $\$ \frac{7}{8}$ per yard, how many yards of silk can be be bought for $\$ 4 \frac{1}{2}$ ?

## Exercise lxvi.

Divide

1. 10 by $\frac{8}{7}$.
2. 18 by $\frac{6}{7}$.
3. 30 by $\frac{7}{8}$.
4. 40 by 3 t.

5. $9 \frac{3}{4}$ by $\frac{2}{10}$.
6. $7 \frac{5}{24}$ by $12 \frac{8}{15}$.
7. $21 \frac{3}{7}$ by $12 \frac{8}{25}$.

Exercise lxvii.

## Practical Problems.

1. If $\frac{3}{4}$ of a yard of cloth cost 24 cents, what would a whole yard cost?

" $\frac{4}{4}$ or 1 yard $=4 \times 8$ cents $=32$ cents.
2. At $\$ 1 \frac{7}{9}$ per bushel, how many bushels of wheat can be bought for $\$ 42 \frac{2}{3}$ ?
3. If a ton of coal is worth $\$ 6 \frac{3}{5}$, how many tons can be bought for $\$ 89 \frac{6}{10}$ ?
4. If a busuel of apples onsts $\$ 2$, how many bushels could be bought for $\$ 60 \frac{3}{4}$ ?
5. If a man earns $\$ 7 \frac{7}{8}$ in a week, how long will it require him to errn $\$ 20 \frac{3}{4}$ ?
6. A man divided $80 \frac{4}{3}$ pounds of flour among the poor, giving to each $2 \frac{4}{5}$ pounds; how many persons were therin?
7. If $21 \frac{3}{4}$ pounds of tea cost $\$ 18 \frac{3}{8} \frac{9}{0}$, what will 1 pound oost?
8. If an errand boy earns. $\$ 7 \frac{1}{8}$ in a week, how long will it require him to earn $\$ 201$ ?
9. A man raised $93 \frac{3}{4}$ bushels of wheat on $8 \frac{1}{3}$ acres of land; how many bushels per acre was that?
10. In how many days will a horse eat $329 \frac{1}{3}$ pecks of oats, if he eats $1{ }_{11}^{8}$ pecks daily?
11. If $\frac{4}{9}$ of an acre of land sell for $\$ 30$, what will an acre sell for at the same rate?
12. The product of two numbers is 27 , and one of them is $2 \frac{5}{9}$; what is the other?

## Section VII. Complex Fractions.

116. To reduce a Complex Fraction to a Simple One.
117. A Complex Fraction is one in whicb either the numerator or denominator, or both, are fractions ; as $\frac{\frac{3}{7}}{7}, \frac{4}{2 \frac{1}{2}}, \frac{34}{\frac{1}{8}}$.
Ex. I. Reduce $\frac{\frac{1}{3}}{\frac{3}{6}}$ to a simple fraction.
Since the numerator of a fraction is the dividend and the denominator, the divisor (art. 94) we have simply to divide the numerator, $\frac{7}{y}$, by the denominator, $\frac{3}{5}$, as in division of fractions;
hence, $\frac{\frac{1}{2}}{\frac{3}{6}}=\frac{1}{8} \div \frac{3}{8}=\frac{1}{9} \times \frac{8}{3}=\frac{6}{27}$.
Ex. 2. Reduce $\frac{8}{4 \frac{1}{6}}$ to $a$ simple fraction.

$$
\frac{8}{1} \div 4 \frac{4}{6}=\frac{8}{1} \times \frac{5}{21}=\frac{40}{21}=1 \frac{1}{29} .
$$

In many cases it is simpler to multiply the numertor and denominator of the complex fraction by the L. O. M. of the denominators ; thus,

$$
\frac{8}{4 \frac{1}{6}}=\frac{5 \times 8}{5 \times 4 \frac{1}{6}}=\frac{40}{21}-1 \frac{1}{2} \frac{2}{2} .
$$

Ex. 3. Simplify $\frac{1+\frac{1}{1}}{1-\frac{1}{3}}+\frac{1}{1}+\frac{\frac{3}{3}}{\frac{3}{6}}$.
Mnltiplying the numerntor and denominator of the the dividend by 3 , and the numerator and denominator of the divisor by 5 , we have

$$
\frac{3+1}{3-1} \div \frac{5+8}{5-\frac{3}{3}}=\frac{4}{2} \div \frac{8}{2}=\frac{4}{8}=\frac{1}{2}
$$

Fxercise lxviii.

1. $\frac{52}{3 \frac{1}{4}}$. 6. $\frac{9 \frac{7}{9}}{2 \frac{1}{27}}$
2. $\frac{33}{5}$.
3. $\frac{\frac{14}{45}}{1 \frac{1}{2} \frac{17}{25}}$.
4. $\frac{11}{7 \frac{11}{17}}$.
5. $\frac{4 \frac{2}{9}}{2 \frac{3}{8}}$.
6. $\frac{5 \frac{3}{1 I}}{\frac{2}{71}}$.
7. $\frac{8 \frac{3}{4}}{5 \frac{5}{8}}$.
8. $\frac{15 \frac{3}{6}}{7 \frac{4}{6}}$.
9. $\frac{9}{3 \frac{3}{1 T}}$.
10. $\frac{23}{2 \frac{2}{3}+\frac{2}{6}}$.
11. $\frac{2 \frac{1}{2}+\frac{12}{3}}{3 \frac{2}{3}-\frac{1}{2}}$.
12. $\frac{14 \frac{1}{4}-6 \frac{1}{2}}{3 \frac{1}{3}}+7 \frac{1}{6}$.
13. $\frac{4 \frac{1}{12}+6 \frac{1}{8}}{9 \frac{1}{5}-3 \frac{1}{4}}$.
14. $\frac{2 \frac{1}{3}+1 \frac{35}{4}}{9 \frac{2}{8}-\frac{39}{112}}$.
15. $\frac{3 \frac{1}{3} \text { of } 1 \frac{1}{6}}{1 \frac{1}{3} \text { of } 1 \frac{1}{4}}$
16. $\frac{3 \frac{3}{7} \text { of } 2 \frac{1}{1} \text {. }}{\frac{1}{2} \text { of } 8 \frac{9}{14}}$.
17. $\frac{4 \frac{4}{15} \text { of } 2 \frac{5}{5 \frac{1}{6}}-4 \frac{1}{2}}{}$.
18. $\frac{2 \frac{1}{4}+3 \frac{1}{6}}{5 \frac{1}{2} \times \frac{1 \frac{1}{2}}{3}}$
19. $\frac{2 \frac{1}{3}-1 \frac{1}{6}}{1 \frac{3}{6} \text { of } 1 \frac{7}{8}}$.
20. Brackets, which are of scveral kinds-e. g., (), \{\}, []-are used to denote that all numbers included within any pair of them are to be considered as forming but one number, and are therefore to be equally affected by any number not included within the same pair of brackets, thus

$$
\begin{aligned}
& (6+3) \times 8=9 \times 8=72 . \\
\text { Also, } & {[8+2 \times\{9+3 \times(4+3)+17\}+21] \times 9 } \\
= & {[8+2 \times\{9+21+17\}+21] \times 9 } \\
= & {[8+94+211 \times 9} \\
= & 123 \times 9 \\
= & 1107 .
\end{aligned}
$$

119. A Vinculum is a sign sometimes used instead of brackets. It consists of a line drawn over the numbers to bs considered as forming one numberthus, $2 \times \overline{8}+\overline{8}=2 \times 11=22$.

In removing brackeis from an expression, it is bast to commence with the innermost and to remove the brackets one by one, the outermost last of all.
120. If a nv nber is ylaced before a bracket, with no sign after it, it is implied that the contents of the bracket is to be multiplied by the number. In like manner, if two brackets stand side by side, with no sign between them, it is implied that the contents of one bracket are to be multiplied by the contents of the other.
Ex. 4. Simplify $\frac{2 \frac{1}{2}-\frac{2}{3} \text { of } 1 \frac{5}{6} \text {. }}{\frac{1}{6} \text { of } 8 \frac{1}{3}+\frac{13}{3}}$.

$$
\begin{aligned}
& \frac{2 \frac{1}{2}-\frac{2}{3} \frac{1}{6}}{\frac{1}{6} \text { of } 3 \frac{1}{6}+\frac{13}{36}}=\frac{24-\frac{2}{3} \text { of } \frac{11}{6}}{\frac{1}{6} \text { of } \frac{10}{3}+\frac{13}{36}}=\frac{2 \frac{1}{3}-\frac{11}{9}}{\frac{2}{3}+\frac{18}{36}}=\frac{36\left(2 \frac{1}{8}-\frac{11}{9}\right)}{36\left(\frac{2}{3}+\frac{13}{36}\right)} \\
& =\frac{81-44}{24+13}=\frac{37}{37}=1 \text {. }
\end{aligned}
$$

Note 1.-In multiplying $2 \Varangle$ by 36 , multiply the fraotional and integral parts separately, and add the results.
2. In multiplying $\frac{x_{1}}{9}$ by 36 , divide the denominator, 9 , into 36 , and multiply the numerator, 11, by the quotient, 4 .
Ex. 5. Simplify $8+\frac{1}{2+\frac{5}{7+\frac{1}{2}}}$.
Beginning at the lowest fraction, considering 5 as its numerator and $7+\frac{1}{2}$ as its denominator, and mu: tiplying each of these terms by 2 , we have

$$
8+\frac{1}{2+\frac{5}{7+\frac{1}{2}}}=8+\frac{1}{2+\frac{10}{14+1}}=8+\frac{15}{30+10}=8 \frac{8}{8}
$$

Fxercise Ixix.
Simplify the following expressions:

1. $\frac{3 \frac{2}{3}}{4 \frac{1}{7}} \times\left(8 \frac{3}{6} \times 5 \frac{4}{7}\right)-17 \frac{3}{4}$.
2. $\left(\frac{2}{3}\right.$ of $\frac{8}{6}$ of $\left.3 \frac{3}{4}+8 \frac{2}{3}\right) \div\left(10 \frac{1}{2}-7 \frac{3}{12}\right)$.
3. $\frac{9 \frac{5}{8} \text { of } \frac{2}{1 I}}{6 \frac{3}{10} \text { of } \frac{6}{9}}+\frac{6 \frac{2}{3} \text { of } \frac{9}{10}}{4 \frac{1}{8} \text { of } 2 \frac{10}{10}}$.
4. $\left(19 \frac{4}{5}-3 \frac{3}{4}\right) \times\left(3 \frac{4}{5}-2 \frac{3}{7}\right)$.
5. $19 \frac{4}{3}-8 \frac{3}{4} \times 3 \frac{4}{5}-2 \frac{3}{7}$.
6. $19 \frac{4}{6}-3 \frac{3}{4} \times\left(3 \frac{4}{6}-2 \frac{3}{7}\right)$.
7. $\left(\frac{4 \frac{1}{2}+5 \frac{3}{4}}{5 \frac{7}{8}-2 \frac{1}{4}}\right) \times\left(2-\frac{3}{5 \frac{1}{8}}\right)$.
8. $\frac{\frac{4}{7} \text { of } \frac{3}{8}}{\frac{1}{14}-\frac{{ }^{\frac{5}{8}}}{4 \frac{5}{6} \frac{1}{6}}}$ of $\frac{7 \frac{3}{5}}{7 \frac{1}{2} \frac{5}{2}}-6 \frac{1}{2}$.
9. $\left(\frac{1}{2}+\frac{1}{3}\right) \times\left(\frac{1}{4}+\frac{1}{5}\right)=\left(\frac{1}{2}-\frac{1}{3}\right) \times\left(\frac{1}{4}-\frac{1}{8}\right)$
10. $\left(\frac{1}{2}+\frac{1}{3}\right) \times\left(\frac{1}{4}-\frac{1}{5}\right) \div\left(\frac{1}{6}-\frac{1}{7}\right)$.
11. $\left(\frac{2}{19}+\frac{1}{3}\right) \div\left(3-\frac{1}{3}\right) \times\left(\frac{1}{3}+2 \frac{1}{6}\right)$.
12. $\left(2 \frac{1}{3}+1 \frac{1}{6}+3 \frac{1}{2}\right) \div \frac{1}{4}$ of $\frac{6}{3}$ of $1 \frac{6}{9}$.
13. $\frac{1 \frac{1}{4}-\frac{5}{12}}{1 \frac{1}{4}+\frac{5}{12}}+\frac{6}{7}$ of $\frac{9 \times 5}{14 \times 3}-\frac{11 \frac{2}{4}}{15}$.
14. $\frac{3 \frac{1}{2}-2 \frac{1}{6}}{\frac{1}{4} \text { of }\left(\frac{1}{6}+\frac{1}{7}\right)} \div 15 \frac{5}{9}$.
15. $2 \frac{1}{2}+\frac{3 \frac{1}{2}-\frac{1}{4}}{3 \frac{1}{2}+\frac{1}{4}}-2 \frac{3}{6}$ of $\frac{12}{13}-\frac{6}{7}$.
16. $2 \frac{1}{2}+\frac{8 \frac{1}{2}-\frac{1}{4}}{3 \frac{1}{2}+\frac{1}{4}}-2 \frac{3}{6}$ of $\left(\frac{12}{13}-\frac{6}{7}\right)$.

## ㅍXAMINATION PAPHRS.

## I.

1. What is a fraction? Define a Simple, a Compound, a Proper Fraction.
2. What rule of fractions is anticipated in reducing a mised number to an improper fraction?

3 If the numerator and denominator of 2 fraction be multiplied by the same number, the fraction thus ob tained is equivalent to the former fraction. Prove the truth of this statement by taking the fractions $\frac{3}{3}$ and $\frac{10}{10}$ and sinowing that they are equivalent.
4. What name is given to a fractional expression of the form of $\frac{3}{2}$ of $\frac{7}{4}$ ?

## ELEMENTARY ABITEMESTO.

State and illustrate the rule for multiplying one fraction by another, and show that the product of two proper fractions must always be numerically less than either of them?
5. What is meant by a vulgar fraction? When is a vulgar fraction greater than unity? What is it then called and whv?

## II.

1. A vulgar fraction may be considered as expressing the division of the numerator by the denominator. Explain this.
2. Explain the principle upon which vulgar fractions are reduced to their equivalents having a common denominator. When may the common denominator be less than the product of all the denominators; and how is it then determined? Ex. $\frac{3}{4}, \frac{5}{6}, \frac{7}{8}, \frac{5}{9}, \frac{11}{12}$.
3. By what fraction must $\frac{2}{3}$ be divided to give a quotient 11 ? Can more than one such fraction be found?
4. State and prove the rule for the division of one valgar fraction by another. Divide $\frac{3}{2}$ by $\frac{4}{5}$; show that a proper fraction will always be increased by dividing it by another proper fraction. By what fraction must $\frac{11}{12}$ be divided to give a quotient 3 ?
5. A man's wages are $\$ 3 \frac{4}{5}$ a day, and his daily exponses are $\$ 1 \frac{7}{8}$; how many days must he labour to enable him to buy a suit of clothes worth $\$ 46 \frac{1}{5}$ ?

## III.

1. Define Numerator and Denominator and show why they are properly applied to the terms of a fraction.
2. John had $\frac{3}{4}$ of a melon and gave away $\frac{8}{9}$ of what he had; what part of the melon had he left?
3. A miller wishes to put 39 bushels of wheat into bags, each bag to hold $2 \frac{1}{6}$ bushels; how many bags would it require?
4. A man owned $\frac{3}{3}$ of a ship and sold $\frac{3}{8}$ of his share for $\$ 5475$; what was the whole ship worth?

5 If $7 \frac{1}{2}$ pounds of coffee cost $187 \frac{1}{2}$ cents; what will 8 bag containing $63 \frac{2}{6}$ pounds cost ?

## IV.

1. Before subtracting fractions, why is it necessary to change them to others having a common denominator?
2. Arrange the fractions $\frac{3}{7}, \frac{2}{5}, \frac{7}{15}, \frac{1}{2} \frac{2}{3}$, $\frac{2}{3}$ of $\frac{9}{18}$ in order of magnitude.
3. If $\$ 2 \frac{3}{8}$ will pay a woman's wages for $2 \frac{1}{2}$ days, how much will pay for $5 \frac{1}{3}$ days' work ?
4. James by mistake subtracted $\frac{7}{8}$ instead of $\frac{8}{7}$; was his answer too large, or too small, and how much ?
5. A man owning $\frac{3}{3}$ of a factory, sold $\frac{6}{7}$ of what he owned for $\$ 15750$; what was the factory worth ?

## V.

1. State the principle involved when fractions are changed to others having a common denominator.
2. I bought $7 \frac{6}{13}$ thousand feet of bcards for $\$ 135.80$; at the same rate, what would $19 \frac{3}{4}$ thousand feet cost?
3. I paid $\$ 7888.30$ for $83^{9}{ }^{9}$ acres of wild land; what would 7 acres cost at the same rate?
4. What is the least number that must be taken from 60 so that it may be exactly divisible by $7 \frac{5}{12}$ ?
5. On $\frac{2}{3}$ of my field I planted corn ; on $\frac{2}{3}$ of the remainder I sowed wheat; on $\frac{2}{3}$ of the remainder I planted potatoes ; the rest, consisting of $\frac{1}{3}$ of an acre, was planted in beans; how large was my field?

## VI.

1. Explain the different steps to be taken so that one fraction can be compared with another.
2. The sum of $\frac{\frac{2}{2} \text { of } \frac{3}{4}}{\frac{1}{2}}$ end $\frac{\frac{2}{6} \text { of } \frac{5}{6}}{\frac{2}{9} \text { of } 4 \frac{1}{2}}$ is equal to how many times their difference ?
3. A merchant lost $\frac{2}{6}$ of his capital ; afterwards he gained $\$ 740$, and was then worth $\$ 3500$; how much did ho lose?
4. A father divided a piece of land among his three sons; the first got $12 \frac{1}{4}$ acres, the second $\frac{3}{8}$ of the whole, and the third as much as the other two ; how much did the third get?
5. A daughter receives as a bequest from her father $\$ 553 \frac{1}{3}$, which is $\frac{2}{3}$ of $\frac{3}{6}$ of the legacy left to her brother; but the brother's share was $\frac{8}{26}$ of the whole property; what was the father worth?

## OHAPTER $\nabla$.

## DECIMALS.

## Section I. Definitions.

## Oral Exercises.

$\times$

1. If an apple is divided into ten equal parts, what is ne of the equal parts called? What are 7 of these oalled ? 3 of them?
2. If a unit is divided into 10 equal parts, what are the * parts called? What is the fractionab unit?
3. If 1 tenth oì an apple is divided into ten equal parts what part of the whole appie 181 part 13 parts 19 parts?
4. How are hundredths got ? How are they got from tenths?
5. What part of 1 tenth is 1 hundredth? How many 1 hundredths in 1 unit ? in 1 tenth ?
6. If 1 hundredth of an apple is divided into ten equal parts, what is the fractional unit called:
7. How many thousandths are equal to 1 hundredth: To 1 tenth? To 1 unit?
8. What is $\frac{1}{10}$ of $\frac{1}{10}$ ? $\frac{1}{10}$ of $\frac{1}{10}$ of $\frac{1}{10}$ ? $\frac{1}{10}$ of $\frac{1}{100}$ ?
9. A Decimal Fraction is one which has for its denominator 10, 100, 1000, or some power of ten.
10. The Power of a number is the product obtained by multiplying the number by itself one, or more times.

Thus 9 is the second power of 3 , for $9=3 \times 3$.
27 "third " 3, for $27=3 \times 3 \times 3$.
81 " fourth " 3, for $81=3 \times 3 \times 3 \times 8$.
123. The Denominator of a decimal fraction is never expressed, but is always understood. For brevity decimal fractions are usually called Decimals. A decimal fraction is expressed by writing the IVumerator with a point (.) before it.

Thus, $\frac{1}{10}$ is written $\cdot 1$.
124. The Point placed before decimals is called the decimal point. It separates the fractional part from whole numbers.
125. The first place to the right of the decimal point is that of tenths; the second place is that of hundredths ; the third, that of thousandths; the fourlh, that of ten-thousandths; the fifth, that of hundred-thousandths; \&c.
Thus, $23 \cdot 045=2 \times 10+3+\frac{0}{10}+\frac{4}{100}+\frac{5}{1000}$.
Hence it appears that decimals are simply an extension of the ordinary system of notation and numeration.
126. Zeros afixed to a decimal have no effect on its value ; that is $\cdot 9, \cdot 90, \cdot 900$ are all equal ;

$$
\begin{aligned}
\text { for } \quad 0 & =\frac{9}{10} \\
\cdot 90 & =\frac{900}{100}=\frac{9}{10} . \\
\cdot 900 & =\frac{900}{1000}=\frac{9}{10} .
\end{aligned}
$$

12\%. To convert a decimal to a vulgar fraction.

Since 878 means 8 tenths, 7 hundredths, and 8 thousandths;

$$
\begin{aligned}
\therefore 878 & =\frac{3}{10}+\frac{7}{100}+\frac{8}{1000} \\
& =\frac{300+70+8}{1000} \\
& =\frac{378}{1000 .}
\end{aligned}
$$

Similarly -00807 means 3 thousandths and 7 hundredthousandths;

$$
\begin{aligned}
\therefore 00307 & =\frac{3}{1000}+100000 \\
& =\frac{300+7}{100000} \\
& =\frac{307}{100000}
\end{aligned}
$$

Honce to expross a decimal ${ }_{3}$ a vulgar fraction write the given deoimal a whole number for the numerator of
the vulgar fraction, and for the denominator write 1 followed by as many ciphors as there are decimal places in the given decimal.

Conversely a frection having $10,100,1000$, \&c., for denominator may be expressed as a decimal by writing the numerator and counting off from the right as many figures as there are ciphers in the denominator.

Thus $3 \frac{175}{1000}=3 \cdot 175$, and $\mathrm{T}^{\frac{7}{0} \frac{5}{00}}=\cdot 075$.

## Exercise lxz.

Express the, following decimals as common fraotions:

| 1. 7. | 6. $\cdot 4123$. | 11. 00427. |
| :---: | :---: | :---: |
| 2. 36. | 7. 0614. | 12. $\cdot 00036$. |
| 3. 08. | 8. 0078. | 13. $\cdot 02007$. |
| 4. . 784. | 9. 7614. | 14. 712465. |
| 5. -709. | 10. -3005. | 15. $\cdot 000006$ |

Express the following fractions as decimals :

| 16. | $\frac{8}{10}$ | 20. | ${ }^{6}$ \% | 24 | 12 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 17. | $\frac{71}{100}$ | 21. | $2 \frac{7}{100}$. | 25 | ${ }^{18496}{ }^{18000}$ |
| 18. | $\frac{27}{10}$ | 22. | $4 \frac{16}{100}$. |  | $8^{10 \%}$ |
| 19. | $\frac{7}{100}$ | 28. | $16 \frac{128}{1000}$. |  | $16 \frac{188}{10000}$ |

Exercise lxxi.
Write the following decimals in words :

| 1. | .9. | 5. | $4 \cdot 81$. | 9. | $21 \cdot 3601$. |
| :--- | :--- | :--- | :--- | ---: | :--- |
| 2. | $\cdot 27$. | 6. | $7 \cdot 216$. | 10. | $17 \cdot 0064$. |
| 8. | $\cdot 368$. | 7. | $8 \cdot 314$. | 11. | 18.0008. |
| 4. | $\cdot 064$. | 8. | $5 \cdot 8167$. | 12. | $20 \cdot 01458$. |

Express in figures the following:
13. Eight tenths; two, and seven hundredths; nine thousandths.
14. Eight hundred and seven, and ninety-four thousandths; three thousand and seventeen, and seven hundred and nine ten-thousandths; three, and one thousand and eight millionthe.
15. Six, and four ten-thousandths ; eighty, and six hundred and nine ten-millionths; one hundred and one, and one thousand and one hundred-thoumandths.

## Section II. Addition.

128. To add Decimals.

Ex. 1. What is the sum of $9.7,14.085,81.64$ and -7165?

| $8 \cdot 7000$ |
| ---: |
| $14 \cdot 0850$ |
| $81 \cdot 6400$ |
| $\cdot 7165$ |
| $100 \cdot 0915$ |


| $8 \cdot 7$ |
| :---: |
| $14 \cdot 085$ |
| or $81 \cdot 64$ |
| $\cdot 7165$ |
| $100 \cdot 0915$ |

Since we can add figures of the same name only we write the addends so that units will be under units, tenths under tenths, \&c. This is always the case when the points range in the same straight line. Then beginning at the lowest order we add as if the figures were integers and place the decimal point in the sum before the tenths.

Fxercise lxxii.

| $(1)$ | $(2)$ | $(8)$ | $(4)$ |
| :---: | :---: | :---: | :---: |
| $42 \cdot 3$ | $12 \cdot 326$ | $4031 \cdot 06$ | .608242 |
| $13 \cdot 06$ | $204 \cdot 00$ | $108 \cdot 304$ | .0315044 |
| $8 \cdot 049$ | $8 \cdot 8024$ | $9 \cdot .001345$ | .8084 |
| $1 \cdot 6$ | $52 \cdot 007$ | $76 \cdot 739$ | .086 |
| .037 | $824 \cdot 1$ | $250 \cdot 0007$ | .9106 |

Find the sum of
5. $4 \cdot 5+70 \cdot 63+1 \cdot 079+25$.
b. $\cdot 126+8 \cdot 05+\cdot 07+: 528+7 \cdot 093$.
7. $111 \cdot 306+\cdot 0317+2 \cdot 793+\cdot 007$.
8. $470 \cdot 05+72 \cdot 701+3 \cdot 0315+413 \cdot 2658$.
9. $12 \cdot 3987+4 \cdot 1462+\cdot 02063+13+10 \cdot 962$.
10. $210 \cdot 7+14563 \cdot 21+\cdot 0173+382 \cdot 74156$.
11. $9 \cdot 127+17 \cdot 72+\cdot 004]+2 \cdot 31+170 \cdot 96$.
12. $\cdot 101285+17 \cdot 061+3 \cdot 2001+5 \cdot 38706$.
13. $2 \cdot 325+\cdot 0012+5 \cdot 086+219 \cdot 6832+\cdot 407$.
14. A merchant has 4 pieces of calico measuring resspuctively, $25 \cdot 5$ yards, $29 \cdot 125$ yards, $34 \cdot 25$ yards and $38 \cdot 75$ yards ; how many yards are there in the 4 pieces ? 15. Four fields contain ag followe: $15 \cdot 875$ arres, 12.6125 acres, 14.006 acres, 16.5 acres; how many aores do the four fields contain ?

## Section III. Subtraction.

129. To subtract decimals.

Ex. x. From 17.018 take 1.90764.

| 17.01800 |  | 17.01 |
| :---: | :---: | :---: |
| 1.90764 | or | $1 \cdot 90764$ |
| 15;10530 |  | 15.10586 |

We write the subtrahend under the minuond, placing tenths undor tenths, hundredtho under hundredths, to. Then, as there are more figures in the subtrahend than in the minuend, we may annex as many ciphers as will render the number of decimal places in eaoh the same. This will not affect the value of the minuend (1.1rt. 126). We then subtract as in whole numbers and place the decimal point in the remainder immediately to the left of the tenths.

## Nxercise lxxiil.

|  | (1) | $(2)$ | $(8)$ | $(4)$ |
| :--- | :--- | :--- | :--- | :--- |
| From | 18.5 | $2 \cdot 8706$ | .50876 | -86 |
| Take | $2 \cdot 8476$ | $\cdot 49$ | .065 | -12704 |
|  |  |  |  |  |

From

| 5. 1.869 | take | -0374. | 9. $204 \cdot 1$ | take | 36.002. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 6. $\cdot 0061$ | " | -00089. | 10. 1000 | ' | 999.99. |
| 7. $6 \cdot 723$ | " | $2 \cdot 7981$ | 11. 2 | * | 1-3678. |
| 8. $9 \cdot 30$ 5 | " | $7 \cdot 9$ | 12. 17-36 | c | $9 \cdot 0184$ |

Find the value of
18. (7.2-2.75) - (1.9-.0027).
14. $36+7 \cdot 07-24 \cdot 896-(3 \cdot 164-789)$.
15. $(273 \cdot 29-41 \cdot 802)-(7 \cdot 162+51 \cdot 386-(99858)$
16. The length of a' seconds pendulum is $39 \cdot 1392$ inches, and that of a French metre $39 \cdot 371$ inches. Find the difference in length between them.
17. A sovereign weighs 123.274 grains, and a shilling $87 \cdot 272$ grains ; find their difference in weight.
18. Thise eleven thousandths from eleven hundredths.
19. Adu together the sum and difference of seventythitco the
20. From a piece of muslin containing 27.5 yards, marchant soid $18 \cdot 75$ yards ; how much was left?

## Section IV. Mruitiplication.

130. To multiply decimals.

Ex. x. Multiply 7 by 9.
Since $7=\frac{7}{10}$ and $9=\frac{9}{10}$;

$$
\therefore .9 \times \cdot 7=\frac{9}{10} \times \frac{7}{10}=\frac{63}{100}=\cdot 63 .
$$

2x. 2. Multiply $\cdot 781$ by $\cdot 06$.
Since $781=\frac{731}{1000}$ and $\cdot 00=106$;
$\therefore \cdot 06 \times 781=\frac{8}{100} \times \frac{731}{1000}=\frac{43980}{000} 00=\cdot 04386$.
Ex. 3. Multiply 8.76 by $2 \cdot$. .
Since $\mathbf{8 . 7 6}=\frac{376}{16}$ and $2 \cdot 4=\frac{24}{10}$;
$\therefore 2.4 \times 3.76=\frac{24}{10} \times \frac{396}{1070}=\frac{9024}{1000}=9.024$.
Hence to multiply decimals, multiply as in the case of integers and mark off from the right of the product as many decimal places as there are decimals in the factors.

Exercise lxxiv.

|  | (1) | (2) | (3) | (4) |
| :---: | :---: | :---: | :---: | :---: |
| Wultiply | $4 \cdot 64$ | 53.062 | -1346 | $675 \cdot 1$ |
| Ey | $8 \cdot 85$ | $4 \cdot 53$ | $\cdot 203$ | -008 |

Mrultiply
e. 718 by 8.47 .
6. 3.96 by 068 .
7. $9 \cdot 07$ by $1 \cdot 06$.
8. $\cdot 008$ by ${ }^{-009}$.
9. $13 \cdot 14$ by 0236.
10. $714 \cdot 6$ by $1 \cdot 124$.
11. $9 \cdot 006$ by $\cdot 0045$.
12. $1 \cdot 001$ by $1 \cdot 009$.
28. A square link contains 62.726 square inchus; what In the area in incles of 5327 square links?
i4 A pint of water weighs 1.25 pounds avoirdupois; what is the weight of 7.8 pints? 8

- 15. Gold is 19.26 times heavier than water; what vieight of gold is of the same bulk as 17.342 pounds of water?

15. The circumference of a circle measures $3 \cdot 14159$ times its diameter; what will be the length of the circumference of a circle whose diameter measuros $\mathbf{6 7} \cdot 258$ miles?
16. Find the produet of the sinn and difference of 27 and 27.
17. What is the weight of five cubic feet of water, if a pubic foot weighs $62 \cdot 455$ pounds avoirdupois?
18. To multiply by 1 followed by ciphers.

Ex. 4. Multiply $71 \cdot 134$ by 10 ; by 100 ; by 100000 . $71 \cdot 184$

10
$711 \cdot 340$
From these examples, it will be seen that the decimal point has been moved to the right in the product as many places as there are ciphers in the multiplier.

Hence to multiply by 1 followed by ciphers, move the decimal point as many places to the right in the multiplicand as there are cipher's in the multiplier, and the result will be the product.

## Section V.-Division.

13\%. To divide one decimal hy another.
Ex. r. Divide 9 by 3 .

$$
\frac{9}{3}=\frac{10 \times 9}{10 \times \cdot 3}=\frac{90}{3}=30
$$

In this example we muiltiply both divisor and dividend by 10 . This makes the divisor a whole number. We then proceed as in ordiuary division.

Ex. 2. Divide 97.92 by 9 .
9) 97.92 As the divisor is already a whole number $10 \cdot 88$ we proceed to divide as usual.
Ex. 3. Divide $3 \cdot 24$ by 00081.
Multiplying both divisor and dividend by 100000 we get $324000 \div 81$, which can easily be worked by ordinary division.

Ex. 4. Divide 736644 by $234 \cdot 6$.
We multiply the divisor and dividond by 10 ; the divisor is now a whole number. The operation will then stand as follows:

2346 ) 7•36644 ( 00314 . We first bring down 3 tentins 7038

3284
2346
9384
9384 and put the decimal point in the quotient. The divisor is not contained in 73 tenths; we therefore put a 0 in the quotiont aud bring down 6 hunaredths. Since the divisor is not contained in 736 hum. dredths, we put another 0 in
the quotient and bring down 6 thousandths. The divisor is now contained in 7366 thousandths. The rest of the work proceeds as in ordinary division.

Hence, if the divisor is a decinal, we multiply both divisor and dividend by such a power of 10 as will make the divisor a whole number, and then we divide as in simple division placing the decimal point in the quotient as soon as the tenths figure of the dividend is brought doun.

## Exercise lxxv.

Divide

1. 16.578 by 5.4 .
2. 48.591 by 96 .
3. 2.56 by 0032 .
4. $4 \cdot 126$ by 640 .
5. ${ }^{2} 1$ by 0025 .
6. $\cdot 0012$ by $1 \cdot 6$.
7. 0774 by 480 .
8. $21 \cdot 3$ by $37 \cdot 5$.
9. 202 by 01.
10. $406 \cdot 8$ by 018.
11. $1 \cdot 066$ by 13 .
12. $15 \cdot 77$ by $\cdot 19$.
13. To divide by 1 followed by ciphers.

Ex. 4. Divide $136 \cdot 15$ by 10 ; by 100 ; by 10000 .
$10 \frac{\mid 136 \cdot 15}{13 \cdot 615} \quad 100 \frac{\mid 136 \cdot 15}{1 \cdot 3615} \quad 10000 \frac{136 \cdot 15}{\cdot 013615}$

From these examples, it will be seen that the decimal point has been moved to the left in the quotient as many places as there are ciphers in the divisor. Hence to divide by 1 followed by ciphers, move the decimal point as many places to the left in the dividend as there are ciphers in the divisor, and the result will be th.. quotient.

Section VI-Reduction of Decimals.
134. To reduce a Vulgar Fraction to a Decimal.

Ex. I. Reduce $\frac{3}{40}$ to a decimal.
40) $300\left(\cdot 075 \quad \frac{3}{40}\right.$ equals $\frac{1}{40}$ of 3 (Art. 94): 8 equals 200 tenthe 30 tenths equals 300 hun200 dreatis, and $\frac{10}{40} 0$ bundredths re7 hundredths, and 20 hundredths remaining. 20 hundredths equals 200 thousandths, end $\frac{1}{4}$ of 200 thousandths is 5 thousandiths; Lence $\frac{3}{40}=075$.

Hence to reduce a vulgar fraction to a decimal, annes ciphers to the numerator and divide by the denominator of the fraction, and place the decimal point in the quotiont as soon as the first cipher is annexed.

## Exercise lxxvi.

Reduce the following to decimals:

1. $\frac{3}{16}$.
2. $\frac{3}{4}$.
3. $\frac{6}{8}$.
4. $\frac{9}{40}$.
5. $\frac{5}{32}$.
6. $\frac{7}{125}$. 12. $6 \frac{3}{6}$.
7. $24{ }^{\frac{1}{2}}{ }^{\circ}$
8. $3 \frac{21}{40}$.
9. $46 \frac{5}{16}$.

## Section VII.-Circulating Decimals.

135. To reduce a circulating decimal to a vulgar fraction.

In reducing vulgar fractions to decimals we find that sometimes the division will not terminate, but the same figure or figures will be repeated over again continually.

Ex. I. Reduce $\frac{1}{3}$ to a decimal.

$$
\frac{1}{3}=\cdot 3333, \& c .
$$

Ex. 2. Reduce $\frac{5}{1 T}$ to a decimal.

$$
\frac{5}{1 T}=4545, \& c
$$

136. Decimals of this kind are called Repeating or Circulating Decimals. The part repeated is called the Period or Repetend.

13\%. It is usual to express the repetend by writing it down and placing a dot over the first and last figures of the part repeated. When there is only one figure repeated the dot is placed over it.

Thus, $\cdot 333 B, \& c$., is indicated $\cdot \dot{3}$.

$$
\begin{array}{lll}
-4545, \text { \&c., } & \text { " } \dot{4} \dot{5} . \\
-2353, ~ \& c ., & " & \cdot 2 \dot{3} .
\end{array}
$$

Ex. 3. Reduce $\frac{3}{22}$ to a decimal.

$$
\frac{3}{3 \cdot 2}=1863636, \& c .,=\cdot 1 \dot{8} \dot{6}
$$

138. A pure circulating decimal is one in which the figures that repeat begin immediately after the decimal point.
139. A mixed circulating decimal is one in which the figures that repeat do not begin immeriately after the decimal point.
140. Since
$\frac{f}{6}=\cdot 11111 \ldots$
Also $\frac{1}{98}=\frac{1}{9} \div 11=\cdot \sigma 10101 .$.
$\frac{2}{5}=-22222 \ldots$
$\frac{5}{9}=.55555 \ldots$ $\begin{array}{ll}{ }_{9}^{89} & =\cdot 050505 \ldots \\ \frac{8}{98} & =-171717 \ldots\end{array}$

Similarly, $\frac{1}{998}=\frac{1}{9} \div 111=\cdot 001001 \ldots$ $\frac{125}{999} \quad=125125 \ldots$
From the preceding examples it is evident that a Pure Circulating Decimal may be expressed as a fraction by writing the figures that repeat as numerator, and as muny nines as there arb figures in the repetend for Senominator of the fraction.

$$
\begin{aligned}
& . \dot{378}=\frac{378}{999} \\
& 5 \cdot \dot{4} \dot{3}=543 \\
& .037 \dot{8}=378
\end{aligned}
$$

1 14. Mixed Circulating Decimals may be reduced to vulgar fractions in the following manner :

Ex. 4. $\cdot 03 \dot{4}={ }^{0} 03 \frac{4}{9}=\frac{34}{100}=\frac{31}{900}=\frac{34-3}{900}$.
Ex_5. $\cdot 05 \dot{4} \dot{B}=: 05 \frac{43}{9 \theta}=\frac{5 \frac{43}{99}}{100}=\frac{558}{9900}=\frac{6 \pm 3-5}{9900}$.
Ex. 6. $\cdot 013 \dot{6}=\cdot 013 \frac{6}{9}=\frac{13 \frac{6}{9}}{1000}=\frac{123}{9000}=\frac{136-1 \frac{13}{900} 0}{9}$.
From these examples it is evident that a Mixed Circulating Decimal may be expressed as a fraction by subtracting the part of the decimal which does not repeat from the whole decimat and placing the romaindor: as numerator, and as many nines as there are figures in the repetend, followed by as many ciphers as there are figures in the part which does not repeai, as ubtiominatior of the fraction.

## झxercise lxxvil.

Reduce to vulgar fractions:

| 1. $\cdot \dot{8}$. | 5. $\cdot 0 \dot{2} \dot{4}$. | 9. $4 \cdot 0 \dot{5} 8 \dot{1}$. |
| :--- | :--- | :--- |
| 2. $\cdot \dot{5} \dot{4}$. | 6. $\cdot 31 \dot{4}$. | 10. $11 \cdot 2 \dot{8} \dot{7}$. |
| 3. $\cdot \dot{7} \dot{9} \dot{9}$. | 7. $\cdot 00 \dot{6} \overline{7} \dot{5}$. | 11. $3 \cdot 4 \dot{1} \dot{8}$. |
| 4. $\cdot \dot{\operatorname{sig} \dot{9}}$ | 8. $\cdot 044 \dot{3}$. | $12.2 \cdot 3 \dot{4} \dot{5}$. |

142. The Addition and Subtraction of Circulating Decimals is generally performed by ropeating the period as many times as seems sufficient to insure the required degree of accuracy, and then adding or subtracting.
143. Multiplication and Division of Circulating Decimals may also be performed by carrying out the repetend, but these operations are more usually performed by reducing the decimals to vulgar fractions, then multiplying or dividing these fractions, and reducing the results onco more to decimals.

Ex. 7. Multiply $2 \dot{3}$ by $\cdot \dot{3} \dot{6}$.

$$
\cdot \dot{3} \dot{6} \times \cdot \dot{2} \dot{3}=\frac{36}{3} \times \frac{21}{90}=\frac{14}{165}=\cdot 0 \dot{8} \dot{1}
$$

Ex. 8. Divide $1 \dot{6}$ by $\cdot 00 \dot{2} \overline{7}$.

$$
\cdot 1 \dot{6} \div 00 \dot{2} \dot{7}=\frac{15}{90} \div 9 \frac{27}{900}=\frac{350}{9}=61 \cdot \dot{1}
$$

## Exercise lxxviii.

Find the value of

1. $\cdot 3 \dot{1} 00 \dot{7}+21 \cdot 008+41 \cdot 607 \dot{3} 4 \dot{2}$.
2. $\cdot \dot{3}-\cdot \dot{0} \dot{9}$ and $\cdot 0 \dot{4}-\cdot 0076923 \dot{8}$.
3. $\quad 37 \cdot 2 \dot{3} \times \cdot 2 \dot{6}$ and $7 . \dot{7} \dot{2} \times \cdot \cdot \dot{2} 9 \dot{7}$.
4. $\cdot \dot{3} \div \dot{0} \dot{9}$ and $\cdot 042 \div \cdot 03 \dot{6}$.

## EXAMINATION PAPERS.

1. What are decimal fractions? How does the use of them facilitate calculation?
2. Represent as vulgar fractions $1 \cdot 25, \cdot 0004$. How does it affect the value of a decimal to place ciphers (1)
after the decinal places, (2) between the decimal places and the decimal point. Decimals may be multiplied and divided by $10,100,1000, \& c$., merely by shifting the decimal point ; show this. Divide 000121 by 11.
3. What are the advantages of decimal fractions? Express as a decimal, 17359 divided by one million. Divide 00125 by $2 \cdot 5$. If the number of decimal places in the divisor exceed the number in the dividend, how do you - proseed ? Explain this, by making 2.5 the dividend and -00125 the divisor.
4. Multiply $2 \cdot 564$ by $\cdot 047$, and divide $\cdot 00169$ by $\cdot 013$. Vorify the result by putting the decimals in the form of vulgar fractions.

ס. What aro zecurring decimals? Find the recurring decimal equivalent to $\frac{5}{7}$, and find the vulgar fraction equivalent to the recurring decimal 81246246 ......

## II.

1. Explain the notation of decimal fractions, and show how the value of a decimal is affected by moving the decimal point two places to the right or left. Write $\frac{375}{1000}$ as a decimal, and express the one-millionth part of the name fraction as a decimal. Multiply $85 \cdot 345$ by $4 \cdot 175$. Divide $25 \cdot 6$ by 00016 .
2. Divide 365 by 20. If in obtaining the quotient you out off the cipher from the divisor and actually divide by 2, what corresponding change should be made in the dividend?
3. Prove that $333 \dot{3} \times 2121 \dot{2} i=\cdot 070707$.
4. Prove the rule for fixing the position of the decimal point, when one decimal fraction is multiplied by another.

Express as vulgar fractions in their lowest terms:
(1) $0625 \times 0032$;
(2) $\cdot 016 \div \cdot 64$;
(3) $\cdot \mathbf{4} \dot{5}-\stackrel{-45}{ }$.
5. Simplify $\frac{1.18}{.152} \times \frac{3.04}{2.95}$, and divide the result by $\cdot 00125$.

> III.

1. Prove the rule for dividing one decimal fraction by another, and find the value of $\frac{05 \times 05 \times 05+1}{1.05}$.
2. Stato and explain the rule for reducing ovolgor fraction to a decimal fraction.

Find the value of $t \div \cdot 01001$ and of $10.01 \div \frac{1}{80}$.
3. Reduce 064 and $15 \cdot 625$ to vulgar fractions ; multiply them together in that form, and then reduce the rosult to decimals. Prove by multiplying the decinals as they stand.
4. Which is the greater, $1 \frac{3}{3} \times 2 \frac{5}{6}$, or $\cdot 018 \times 216$ ?
5. Suppose unity represents 0012 , what number represents 0001 ?

## IV.

1. Whether is $\mathbf{1 - 1 2 1 4 7 2 6 5 3}$ more accurately representedby $1 \cdot 1214726$ or $1 \cdot 1214727$, and why?
2. Express in decimal notation the value of $8.0625-6 \frac{1}{26}$ $-\cdot 00375+1 \cdot 09236-\frac{25679}{10000}$.
3. A bought a house with 25 of his money; he spent 575 of it in buying a farm and had $\$ 2100$ left; find the cost of the house and farm respectively.
4. What is the smallest number that can be exactly divided by the nine significant figures? Simplify $\frac{5}{8}$ of $\frac{4}{10}-\frac{7}{9}$ of $\frac{4}{21}$.
5. What number is that, from which if there be taken $\frac{2}{7}$ of $\cdot 375$, and to the remainder $\cdot 5 \dot{3}$ of $\cdot 3125$ be added, the sum is 10 ?

## V.

1. Find the value of $\frac{3}{15}$ of $\left(\frac{7}{9}+1 \frac{2}{3}\right)$, and prove it equal to $\frac{1}{3}$ of $20 \frac{3}{4} \div 10 \frac{3}{8}$.
2. Prove the rule for finding the valne of a oirculating decimal ; and reduce $1 \div 99999$ and $1 \div 10001$ to oirculating decimals.
3. Prove that $46.2 \div 92.4=75 \times \cdot \dot{6}$.
4. Prove that $02 \times \cdot 02 \times \cdot 005 \times \cdot 005=\cdot 0001 \times \cdot 0001$.
5. Divide $\frac{1}{4}+\frac{1}{8}+\frac{1}{12}+\frac{1}{16}+\frac{1}{20}$ by $\frac{1}{6}+\frac{1}{10}+\frac{1}{18}+\frac{1}{30}$, and reduce the result to a decimal.

## CHAPTER VI.

## COMMERCIAL ARITHMETIC.

## Section 1.-Tables and Reduction.

144. ENGLISH OR STERLING MONEY.
4 farthings (far.) $=1$ penny, or $1 d$. 12 pence $=1$ shilling, " $1 s$. 20 shillings $=1$ pound, " $£ 1$.
Note 1.-Farthings are usually written as a fraction of 1d. Thus 1 far. is written $\frac{1}{4} d$.; 2 far., $\frac{1}{2} d . ; 3$ far., $\frac{3}{4} d$.

Note $2 .-£ 1$ sterling $=\$ 4.86 \frac{2}{3}$, and 1s. $=24 \frac{1}{3}$ conts.

## Oral Exercises.

Repeat the table of English money.
How many far. in $2 \mathrm{~d} . ?$ in 3 d . ? in 6d.? in 8d.?
How many pence in 12 far. $?$ in 16 far. ? in 20 far. $!$
How many pence in 2 s .? in 3 s . ? in 5 s . ? in 6 s .?
How many far. in 1s. ? in 2 s . ? in 3s. ? in 5 s . ?
How zany shillings in $£ 1$ 12s.? in $£ 2$ 15s.?
145. There are two kinds of Reduction, Reduction Descending and Reduction Ascending.
146. Reduction Descending is the process of changing a number from a higher to a lower denomination.

14\%. Reduction Ascending is the process of changing a number from a lower to a higher denomination.

Ex. 1. Reduce $£ 65 \mathrm{~s} .3$ d. to farthings.

| $\begin{array}{ccc} £ 6 & 5 \mathrm{~s} . & 34 \mathrm{~d} . \\ 20 & \end{array}$ | In 1 pound there are 20 shillings, and in fó thore are $C$ timos 20 s ., or 120 s .; 120s. plus 5 s . aro |
| :---: | :---: |
| 125s. | 125 s .; in 1 shilling there are 12 |
| 12 | pence, and in 125s. there are 125 |
|  | times 12d., or 1500d.; 1500d. plus |
| 1503d | 3 d . are 150 dd. in 1d. there aro 4 |
| 4 | farthings, and in 1503d. there are |
|  | 1503 timos 4 far., or 6012 far.; |
| 6013 far. | 6012 far. plus 1 far. are 6018 far. |
| Ex 2. How far. <br> 4\|3679 | $£$ s. d. in 3679 farthings ? <br> There are 4 far. in 1d., hence |
| 12\|919 3 far. | in 3679 far. thore are as many |
| $20 \mid 767 \mathrm{~d}$. | pence as the numbor of times 4 |
| $£ 316 \mathrm{~s}$. | is contained in $3679 ; 3679 \div 4$ |
| s. £3 16s. $7 \frac{3}{4} \mathrm{~d}$. | $=919$ and 8 over. This 3 is 3 |
| There are 12 | 1s., hence in 919d. there are as |
| ing | mber of times 12 is contained |
| $19 \div 12=$ | nd 7 over. This 7 is 7d. There |
| s. in $£ 1$, | 76s. there are as many younds as |
|  | 0 is contained in $76 ; 76 \div 20=3$ |
|  | 16 shillings. |

Exercise lxxix.
Reduce

1. 7 s .8 d . to pence.
2. $£ 13 \mathrm{~s}$. to farthings.
3. 7145d. to £, \&c.
4. 6185 s . to $£$, © c .
5. $£ 100 \mathrm{~s} .6 \mathrm{~d}$. to pence.
6. $£ 26 \mathrm{~s} .8 \mathrm{~d}$. to pence.
7. 3910 far. to $£$, be.
8. 7168d. to £, \&c.
9. £191 9s. 113 $\frac{3}{4} \mathrm{~d}$. to fur.
10. £3 Gs. $10 \frac{1}{4}$. to far. 11. 78916 d . to $£, \& \mathrm{c}$.
11. $£ 1007 \mathrm{~d}$. to far.
12. 

## UNITED STATES MONEY.


149. AVOIRDUPOIS WEIGHT.

| 16 drams (dr.) | $=1$ ounce, | or | 1 oz. |
| ---: | :--- | :--- | :--- |
| 16 ounces $\cdot$. | $=1$ pound, | ". | 1 lb. |
| 25 pounds. | $=1$ quarter, | 1 qr |  |
| 4 quarters. | $=1$ hundred-weight, | 1 owt |  |
| 20 hundred-weight | $=1$ ton. | or | 1 l. |

Nots 1. $-\Lambda$ voirdnpois Weight is used for welghing. evorything except jewels, procious metals, and medicines, when disponsed.

Note 2.-28 pounds equal 1 quarter in Greal Britain. Oral Exercises.
Repeat the table of Avoirdupois Weight.
How many ouncos in 2 lb .; in 3 lb .4 oz .; in 4 lb .? How many quarters in 28 lb . ; in 49 lb . : in 100 lb .?
How many drams in 2 oz .6 dr ; in 3 oz .4 dr ?
How many tons in 58 cwt. 3 in 112 cwt. $?$ in 200 cwt.?
Ex 3. Reduce 2 cwt. Ex. 4. Reduce 147658 $\$ \mathrm{oz} .11 \mathrm{dr}$. to drams. |lbs. to tons, etc.


## Exercise lxxx.

Reduce

1. 2 t .3 qr .6 lb . to drams. |2. 76385 qrs. to tons, \&c.
2. 5 tb .6 oz .14 dr . to drams. 4.3 cwt .8 lb .5 oz . to ounces.
3. 21645 oz . to owt., \&c. G. 51649 lb . to tons, \&c.

## 130.

TROY WEIGHT.
24 grains (gr.) . $\cdot=1$ pennyweight, $\cdot \because 1$ dwt.
20 pennyweights . . $=1$ ounce, . . . 1 oz.
12 ounces . . . . $=1$ pound, . . . . 1 lb .
Note 1.-This is chiefly used for weighing gold, silver and jowels.

Note 2. -1 lb . avcirdupois $=7000$ grains, 1 lb . troy $\cdot=5750$ grainsoejuf Oral Exercises:
How many oz. in 2 lb ? in. $3 \mathrm{lk} . ?$ in 5 lb .9 .

How many lb. in 86 oz .8 in $48 \mathrm{oz} . ?$ in $60 \mathrm{oz} . ?$ in 44 oz. $?$ in 78 oz. ?

How many dwt. in 2 oz . ? in $8 \mathrm{oz} ?$ in 4 oz . $?$ in 48 gr ? 151.

APOTHECARIES' WEIGHT.
20 grains (gr.) . . $=1$ scruple, . . or 1 sc. or 1 Э.
3 scruples, . . $=1$ dram, . . or 1 dr . or 13 .
8 drams, . . $=1$ ounce, . . . or 1 oz . or 13 . 12 ounces, . . . $=1$ pound, . . or 1 lb . or 1 lb .

Note 1.-The ounce and pound of Apothecaries' Weight are the same as in Troy Weight.

Note 2.-Apothecaries' Weight is used in mixing medicines. These are bought and sold by Avoirdupois Weight.

How many

1. Grains in $7 Э$ ? $11 Э$ ?
2. Drams in 53 ? 73?
3. Scruples in 93? 163?
4. Ounces in 883 ? 963 ?
5. Drams in 24 Э? 96 Э ?
6. Pounds in 108 ? 1683?

Exercise lxxxi.
Reduce

1. $1 \mathrm{lb}, 4 \mathrm{oz}$. to ounces.
2. 7163 sc. to lb. \&c.
3. 7685 dwt . to lb. \&c.
4. 11 oz .8 drs. to grains.
5. 3 oz .6 dwt . to grains.
6. 73564 grains tolb. (Troy) \&o.

| es (in.) |  | 1 foot, or |
| :---: | :---: | :---: |
| 3 feet | - . . | 1 yard, "1 yd. |
| $5 \frac{1}{2}$ yards | -••• | 1 rod, "1 rd. |
| 40 rods | . . . . $=$ | 1 furlong, " 1 fur. |
| 8 furlongs |  | mile, " 1 mi. |
| 3 miles. |  | 1 lea |

Note 1.-Cloth Measure is not now used. Cloth is bought by the yard, half-yard, quarter-yard, etc.

Note 2.-Gunter's Chain is used in measuring land. It is 22 yards long and is divided into 100 links.

Note 3.-Mariners use the following:
6 feet . . . . . . . . . $=1$ fathom.
120 fathoms . . . . . . $=1$ cable length.
880 fathoms . . . . . . $=1$ mile.

Repeat the table of Lineal Measure.
How many feet in 4 yd. $?$ in $6 \mathrm{yd} .1 \mathrm{ft} . ?$

How many miles in 17 fur. $?$ in 320 rods 9 in 69 fur. $?$ How many teet in 9 fath. $?$ in $2 \mathrm{rd} . ?$ in 12 yd .1
Ex. 5. How many feet Ex. 6. How many rods in 12 rd .8 yd .2 ft .? in 209 ft ?

| rd. | yd. | ft. |
| :---: | :---: | :---: |
| 12 | 3 | 2 |
| $5 \frac{1}{2}$ |  |  |
| $\overline{63}$ |  |  |
| $\bar{B}$ |  |  |
| $\overline{69}$ | yd. |  |

209 ft. Ans.
Ans. 12 rd .3 yd .2 ft .
Note.-To divide by $5 \frac{1}{3}$,
Note.-We multiply by we reduce both to halves, 6 , and add to the product then the remainder is halves. the 3 yds., and then multi- which we reduce to whules. plying by $\frac{1}{2}$, we have 69 yd . by dividing by 2 .

Fxercise lxxxii.
Reduce

1. 1 mi .1 fur. 1 rd . to inches.
2. 76452 in. to mi., etc. B. 7568 feet to mi ., etc.
3. 2 rd .1 yd to feet.
4. 7 chains to bet.
5. 16752 in . to fathoms.
6. SURFACE OR SQUARE MEASURE.
. 144 square inches $=1$ square foot, or 1 sq. ft.
9 square feet $=1$ square yard, " 1 sq. yd.
$30 \frac{1}{4}$ square yards $=1$ square rod, " 1 sq. rd.
40 square rods = 1 rood, " 1 r.
4 roods $=1$ acre, " 1 a.
640 acres $=1$ square mile, " 1 sq. m.
Note 1.-A surface is that which has length and breacth without thickness.

1 in.
Note 2.-A square is a plane surface which has four equal sides and four equal angles. $\square$ 1 in.

Note 3.-A square inch is a square each of whose sides is an inch long.

Note 4:-10,000 square links $=1$ square chain. 10 square chains $=1$ acre.

## 154. CUBIC OR SOLID MEASURE.

1728 cubic inches (cu. in.) $=1$ cubic foot, or 1 cu . ft. $\begin{array}{lll}27 \text { cubic feet } & =1 \text { cubic yard, "1 cu. yd. } \\ 128 \text { cubic feet } & =1 \text { cord, } & 1 \mathrm{~cd} \text {. }\end{array}$
Note 1.-A cube is a solid bound by 6 equal squares.
Note 2.-A cord is a pile of wood 4 ft . wide, 4 ft . high, and 8 ft . long.


## Oral Exercises.

Repeat the table of square mensure.
How many inches in 2 sq . ft .?
How many acres in 16 roods? in 320 sq. rods 1
How many feet in $3 \mathrm{~cm} . \mathrm{yd}$. ? in $4 \mathrm{cu} . \mathrm{yd} .20 \mathrm{cu} . \mathrm{ft}$.? What is thediffercnce between 3 sq .in. and 3 in . square 1 8 in. are is a square each side of which is $\mathbf{B i n}$. long, and hence $=9 \mathrm{sq}$. in.

## Exercise lxxxiii.

## Reduce

1. $\mathbf{1 9 9 7}$ sq. rd. to acres, \&c. $4.7689 \mathrm{cu} . \mathrm{ft}$. to cords.
2. 3 sq. rds. 2 ft . to inches. 5. 12 a. 6 rd . to inches.
3. 8469 cu in to feet

## 155. <br> DRY MEASURE.

2 pints (pt.) . . . . $=1$ quart, . . . or 1 qt. 4 quarts . . . . $=1$ gallon, . . or 1 gal. 2 gallons . . . . . = 1 peck, . . or 1 pk . 4 pecks . . . . . . $=1$ bushel, . . or 1 bu. Note 1.-Dry Measure is used in measuring grain, fruit, \&c.

Note 2.-By the "Weights and Measures" Act of 1873, the "Imperial Bushel," containing eight "Imperial Gallons̀," of $277 \cdot 274$ cubic inches in each, is the standarả hushel in Canada.

Note 8.-By the samd Aot, the following articles trê to be restimated by the Cental of 100 lbs : Barley, beans, charcoal, corn, oats, peas, potatoes, rye, salt, seeds, and wheat.

1. Noxeri4.- 8 bushels $=1$ quarter in Great Britain, 1 is:

Note 5.-The following table shows the weight of a bushel of the article nained, ha determined by the same Ast:

Whodt! ! ! 60 mb
Ryo Corn ....... 56 lb . "Burley......4815.
156.
\& gills (gi.) $\quad . \quad 1$ pint, $\quad . \quad 1$ pt.
8 pints $1 \% 10$ quart, 0 and or 1 qt. 4 quatts $=1$ gallon, 0 or or 1 gal .
1.1 Norter 1.-A barrel of beer contains 36 gals.

$$
\text { A hogshead of boer us } 54 \text { gals. }
$$

A hogshesd of wine ". 68 gals.
N6te' 2. - The "wine gallon contains 281 cubic inches ; the beer gallon ogntains 282 cubic inches, and the Imperial or standard gallon, 277 274 etble inohes.

H5Vminco as" MEASURE OF TIMEEOTN Ni! d 60 weondé (ceo.) $4 . \quad$.

$$
60 \text { minutes, }
$$

Note 1.- The number of days in each month may be remembered by means of the following lines:

> Thirty days has Soptember,
> is April, Juno, and November;
> FAbruary has twenty-eight alone-
> Aht the reat have thirty-one
> But loap year coning onne in foar,
> February then has one day more.

Note 2.-The leap years are those that can be divided by 4 without a remainder: as, 1864, 1868. 1872, oto. Put of the oven hundrode, only thase that oan be divided by 400 arelogp yairs The year 1000 will, not he follof yeasil bat 2000 will be.

## 158. MISOELLANEOUS TABLE.

12 units $=1$ dozen. $\mid 24$ sheets . $=1$ quire.
12 dozen $=1$ gross.
12 gross $=1$ great gross.
20 units $=1$ score.

20 quires . . $=1$ ream. 196 lb . flour . = 1 barrel. 200 lb . pork . = 1 barrel. Oral Exercises.
Repeat Time Measure.
How many days in 3 weeks? in 5 weeks and 8 days? How many dozen in $84 ?$ in 182 ? in $150 ?$
Was 1600 a Leap year? 1876 ? 1854 ?
How many hours in $360 \mathrm{~min} . ?$ in $788 \mathrm{~min} . ? 600 \mathrm{~min}$ ?

## 思xercise lxxxiv.

Reduce

1. 7 da .16 hr . to seconds.
2. 7684 pints to bushels, etc.
3. 84 gal. 8 gills to gills.
$4.86 \mathrm{bu} .8 \mathrm{qt}$.1 pt . to pints.
4. 2685 gills to gallons.
5. 17 qr . 8 bu. to pecks.
6. 3685 lb . of wheat to bu.
7. 785693 sec. to weeks, etc.
8. 3586 lbs. Timothy seed to bu., etc.
9. 78 da. 9 min . to seconds.
10. $1576 \mathrm{cu} . \mathrm{ft}$. to cords.

## Section II.-Compound Addition.

 159. To add compound numbers.160. A compound number is one composed of 2 or more numbers of different denominations which can be reduced to the same denomination.

The sum of $£ 6$ and $£ 4$ is tound by simple addition.
The sum of $£ 612 \mathrm{~s}$. and $£ 49 \mathrm{~s}$. is found by compound addition.

Ex. 1. Find the sum of $£ 76 \mathrm{~s} .8$ d., $\boldsymbol{5 5} 9 \mathrm{~s} .8 \mathrm{~d}$., $£ 89 \mathrm{~s} .7 \mathrm{~d}$., and $£ 97 \mathrm{~s} .9 \mathrm{~d}$.

| - and |  |
| :---: | :---: |
| $\begin{array}{lll} 8 & 8 . & d . \\ 7 & 6 & 8 \end{array}$ | $\begin{array}{ccc} f & \text { s. } & \text { d. } \\ 7 & 6 & 8 \end{array}$ |
| 598 | 69 |
| 897 | 89 |
| $\begin{array}{llll}9 & 7 & 9\end{array}$ | 979 |
| 293127 | 8013 |

We write the numbers so that units of the same name will be in the same column. Then we add the pence column as. in simple addition and find the sum to be 27. Similarly with the other columns. Hence the correct
sum is $\mathbf{L 2 9}$ 818. $_{6} 27$. But it is usual in writing denominate numbers not to have more units of any denomination than 1 less than the number required to make 1 of the next higher denomination ; thus, a rod 12 in . long is said to be 1 ft . in length. We do not say 20 cwt . of hay, but 1 ton, \&c. We therefore change the 27 d . to 2 s . 3 d . We set down the 3d. under the pence' column and add the 2 s. to $31 \mathrm{~s} . ; 31 \mathrm{~s} .+2 \mathrm{~s} .=38 \mathrm{~s} . ; 33 \mathrm{~s} .=£ 113 \mathrm{~s}$. We set down the 18s. under the shillings' column and add the $£ 1$ tx £ $29 ; £ 29+£ 1=£ 30$.

Exercise lxxyv.
(1) (2)

| lb. | oz. | dwt. |
| :--- | ---: | ---: |
| 17 | 9 | 16 |
| 25 | 6 | 12 |
| 72 | 11 | 18 |
| 57 | 10 | 19 |

(4)
(5)

| cwt. | qr. | lb. | oz. |
| :---: | :---: | :---: | :---: |
| L0 | 3 | 12 | 11 |
| 16 | 2 | 16 | 12 |
| 17 | 0 | 22 | 15 |
| 19 | 1 | 18 | 13 |

$\begin{array}{rcrr}\text { ba. } & \text { pk. } & \text { qt. } & \text { pt. } \\ 10 & 1 & 1 & 1 \\ 2 & 3 & 6 & 0 \\ 5 & 2 & 3 & 1 \\ 8 & 3 & 1 & 1 \\ 15 & 2 & 4 & 0\end{array}$
(8)

| rả. | yd. | ft. |  |
| :---: | :---: | :---: | :---: |
| 17 | in. |  |  |
| 1 | 2 | 6 |  |
| 21 | 2 | 1 | 7 |
| 23 | 3 | 0 | 8 |
| 25 | 5 | 2 | 9 |

(6)

| rd. | yd. | ft. | in. |
| ---: | ---: | ---: | ---: |
| 37 | 4 | 1 | 9 |
| 30 | 5 | 2 | 2 |
|  | 3 | 2 | 7 |
| 1 | 0 | 2 | 10 |
| 25 | 1 | 1 | 11 |

7. Find the sum of 1 wk .2 da. 13 h .4 .0 min .30 sec .; 2 wk. 6 da. 10 h .8 min .3 sec . 5 da. 22 h .55 min. $45 \mathrm{sec} . ; 4 \mathrm{~h} .1 \mathrm{~min} .15 \mathrm{sec}$.; and 1 wk .2 da. 4 h .5 min.
8. Add together 10 rd .4 yd. $2 \mathrm{ft} .8 \mathrm{in} ; 1 \mathrm{rd} .8 \mathrm{yd}$. 8 rd. 2 yd. 1 ft .6 in . ; 1 rd. 4 in .; and 2 yd. 1 ft .9 in.

Section III. Compound Subtraction. 161. To subtract Compound Numbers.

Ex. I. From 16 lb .8 oz. 6 dwt. take 7 lb .4 oz. 12 dwt.
lb. oz. dwt.
16. 86

We write the subtrahend innder the
$7 \quad 4 \quad 12$
$\begin{array}{lll}9 & 8 & 14\end{array}$ minuend, so that units of the same name will be in the same column, and begin at the right to subtract.

Since we cannot take 12 dwt. from 6 dwt., we take 1 oz . or 20 dwt. from the 8 oz . 'and add it to the 6 dwi., making 20 dwt. 26 dwt. $-12 \mathrm{dwt}=14$ dwt.
Singe we took 1 oz. from 8 oz ., we left only 7 om .7 om. $-4 \mathrm{oz} .=8 \mathrm{oz} .16 \mathrm{lb} .-7 \mathrm{lb} .=9 \mathrm{lb}$.

## Exercise lxxxvi.

(2)

| mi. | fur. | rd. |
| :---: | :---: | :---: |
| 60 | 0 | 0 |
| 40 | 7 | 89 |

(5)
(1)

| Ib | 3 | 3 | $Э$ | gr. |
| ---: | ---: | ---: | ---: | ---: |
| 24 | 7 | 2 | 1 | 16 |
| 16 | 10 | 3 | 2 | 17 |

(4)

| fur. | rd. | yd. | ft. | in. |  |  | s. | d. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 7 | 31 | 1 | 1 | 8 |  | 43 | 11 | 10 |
| 1 | 39 | 1 | 2 | 7 |  | 15 | 14 | 6 |

(8)
a. r. sq.rd. $69 \quad 8 \quad 25$ 100 88
7. A farmer had 200 bu . of wheat, and sold 28 bu .2 pk . 5 qt. 1 pt. to one man, and as much to another; how much remained?
8. A miner having 112 lb . of gold sent his mother 17 lb . 10 oz .15 dwt .20 gr ., and 3 lb .16 dwt . less to his father; how much did he retain?
9. From a barrel of beer containing 54 gallons, a person drew 12 gal. 3 qt. one day, and 9 gal. 2 qt. 1 pt. another; how much was left ?
10. From 89 sq. rd. 29 sq. yd. 128 sq. in., subtract 17 sq. rd. 16 sq. yd. 5 sq. ft.
11. A grocer has 1 cwt. 18 lb . of sugar in one barrel, 3 qr. 21 lb . in another, and 1 cwt .2 qr .11 lb . in a third. After selling 1 cwt .3 qr .15 lb ., how much will he have left?

## Section IV. Compound Multiplication.

162. To multiply a Compound Number.

Ex. 工. Multiply 3 da. 19 hrs . 59 min . by 97.

| da. <br> 8 | hrs. <br> 19 | min. <br> 59 <br> 97 |  | da. <br> 8 | hrs. <br> 19 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 291 | 1843 | 5723 |  | min. <br> 69 <br> 97 |  |

We multiply each denomination separately, as in simple multiplication, and obtain as product 291 da. 1843 hrs . 5723 min . But as 5723 min . $=95 \mathrm{hrs} .23 \mathrm{~min}$., we write down 23 min., and add the 95 hrs . to 1848 hrs . 1848 hrs. $+95 \mathrm{hrs} .=1938 \mathrm{hrs} .=80$ da. 18 irrs . \&c.

Nore.-The usual method of working this example is to multiply first by 10 , this product by 9 , then to multiply the 3 da. 19 hrs .59 min . by 7, and add the result to the
last product. We reoommend the method in the example as being on the whole easier and more convenient.

We write the divisor at the left of the dividend. 17 is contained 4 times in 80 da. and 12 da . over; $12 \mathrm{da} .=288$ h. ; $288 \mathrm{~h} .+6 \mathrm{~h} .=294 \mathrm{~h} . \quad 17$ is contained 17 times in 294 h . and 5 h. over; $5 \mathrm{~h} .=800 \mathrm{~min}$. ; 800 min . $+40 \mathrm{~min} .=840 \mathrm{~min} . \quad 17$ is contained 20 times in 840 min .

Ex. 2. Divide $£ 12$ 1s. 6 d. by $£ 16 \mathrm{~s} .10 \mathrm{~d}$.

$$
\frac{£ 12 \text { 1s. 6d. }}{£ 16 \mathrm{~s} .10 \mathrm{~d} .}-\frac{2898 \mathrm{~d} .}{322 \mathrm{~d} .}=9 .
$$

Ex. 3. A divided a field of 11a. into lots of 1 r . 4 per. each; how many lots were there?

$$
\frac{11 \mathrm{a} .}{1 \mathrm{r.} .4 \text { per. }}=\frac{1760 \text { per. }}{44 \text { per. }}=40
$$

When we divide one compound number by another, we reduce each to the lowest denomination named in either, and divide as in simple division.

Exercise lxxzviii.
(1)

## E. s. d. <br> t) 61184

(2)
6) $76 \quad 10 \quad 14 \quad 12$
(3)
4. Divide 4 gal. 2 qt. by 144.
5. Divide 40 cu. yd. 10 cu . ft. by 18.
6. Divide $£ 487 \mathrm{~s} .4 \mathrm{~d}$. by $£ 611 \mathrm{~d}$.
7. Divide 69 bu .3 pk .6 qt. by 6 bu .3 pk .6 qt.
8. Divide 697 lb .7 oz .5 dr. by 60 lb .10 oz .6 dr.
9. Divide 80 bu. 2 pk. 4 qt . by 13 bu .3 pk .5 qt .
10. A farmer put up 1000 bushels of apples in 350 barrels of uniform size; how many bushels, \&c., did each barrel contain?
11. How many demijohns, each containing 2 gal. 3 qt. ! pt., can be filled from a tank holding 71 gal. 3 qt. 1 pt. of wine?
12. A drove of cattle ate 6 T .19 cwt .87 lb . of hay in a week; how long will 34 T. 19 cwt .85 lb . last them ?

## Section VI.-Denominate Fractions.

164. To find the value of a Fraction of a Denuminate Number.

Ex. 1. How many shillings, \&c., are there in $\frac{3}{8}$ of a pound?

Since $2 \frac{2}{2}=\frac{1}{8}$ of $£ 3$ (Art. 94), we divide $£ 8$ by 8 as in compound division.

Ex. 2. Find the value of $3 \ddagger$ of $\frac{3}{13}$ of 2 t. 8 cwt .
$8 \frac{1}{4}$ of $1^{3}$ of $2 \mathrm{t} .8 \mathrm{cwt}=\frac{\mathrm{r}}{4}$ of $\frac{3}{13}$ of 2 t .3 cwt .
$=4$ of 2 t .3 cwt .
$=\frac{0 \mathrm{t} .9 \mathrm{cmt}}{4}=1 \mathrm{t} .12 \mathrm{owt} .1 \mathrm{qr}$.

## Exercise lxxxix.

What is the valuo

1. Of $\frac{4}{5}$ of a bushel ?
2. Of $\frac{2}{3}$ of a mile ?
3. Of $\frac{7}{8}$ of a rod ?
4. Of $\frac{3}{7}$ of $£ 316 \mathrm{~s} .8 \frac{3}{4} \mathrm{~d}$. ; of $£ 1816 \mathrm{~s} .7 \frac{1}{2} \mathrm{~d} . \div 3 \frac{2}{3}$ ?
5. Of $\frac{3}{5}$ of a week $+\frac{3}{3}$ of a day $+\frac{2}{3}$ of an hour?
6. Of $\frac{33}{1100}$ owt. - $\frac{8}{15}$ of 2 lbs .8 oz .10 drs .?
7. To Express one number as the fraction of another.

Ex 3. Express 4 rd. 2 yd. 1 ft .4 in . as the fraction of 1 mile.
$4 \mathrm{rd} .2 \mathrm{yd} .1 \mathrm{ft} .4 \mathrm{in} .=880 \mathrm{in}$. and $1 \mathrm{~m} .=63360 \mathrm{in}$.

$\therefore 880 \mathrm{in}$. $=\frac{88}{83} \frac{80}{360}$ of 63360 in .
Hence the fraction required is $\frac{880}{83} \frac{0}{80}=\frac{1}{72}$.
Noxt.-The example, Express 4 lbs. as the fraction of 8 lbs. may be written in any of the following ways:

1. Reduce 4 lb . to the fraction of 8 lb .
2. What fraction of 8 lb . is 4 lb .?
3. What part of 8 lb . is 4 lb .?
4. If 8 lb . is the unit, what is the measure of 4 lb. ?

## Fxercime xc.

1. What part of an ounce is $\frac{8}{10}$ of a soruple $?$
2. What part of a ton is $\frac{t}{8}$ of an ounce?
3. What part of a mile is $\frac{8}{y}$ of a rod?
4. What part of an acre is $\frac{1}{2}$ of a square foot?
5. Reduce $\frac{8}{g}$ of a gill to the fraction of a gallon.
6. Reduce $\frac{5}{7}$ of an inch to the fraction of a rod.
7. Reduce $\frac{t}{5}$ of $a \mathrm{lb}$. to the fraction of a ton.
8. What fraction of $£ 82 \mathrm{~s} .6 \frac{3}{4} \mathrm{~d}$. is 14 s . $10 \frac{1}{4} \mathrm{~d}$. ?
9. Express 18s. $10 \frac{1}{1} \mathrm{~d}$. as a fraction of $\boldsymbol{x} 2 \mathrm{9s}$. 7d.
10. Express 2 a. 31 per. as a fraction of 4 a. 2 r .17 per.
11. Reduce $2 \boldsymbol{2}$
12. Reduce $\frac{1 \theta^{\frac{1}{72}} 0}{}$ of a mile to the fraction of an inch.
13. To find the value of a Decimal of $n$ Denominate Number.
Ex. 4. What is the value of $\mathbf{7 8 7 5}$ of $£ 1$ ?
£.7875
20
s. 15.7500

Ex. 5. Find the value of $2 \cdot 16$ of 1 yd .
$2 \cdot 16$ of $1 \mathrm{yd} .=2 \frac{18}{90}$ of $1 \mathrm{yd} .=\frac{18}{6}$ of $1 \mathrm{yd} .=2 \mathrm{yd} .6 \mathrm{in}$. Exercise xci.
Find the value of

1. 94375 of 1 acre.
2. 815625 of 1 lb . Troy.
3. 875 of 1 s .
4. 785 of 1 hr .
5. 497 of 1 day.
6. $\cdot \mathbf{4 8 7 5}$ of $£ 1$.
7. 965625 of 1 mile.
8. 778125 of 1 ton.
9. $\mathbf{6} 28125$ of $£ 1$.
10. $3 \cdot 4588$ of 1 s .
11. $2 \cdot 5884375$ of 1 day.
12. 002083 of $\$ 1$.
d.9.0000 Hence 7875 of $£:=15 \mathrm{~s}$. 9d.
$\cdot 7875$ of $£ 1=\cdot 7875$ of 20 s .
$=15.75 \mathrm{~s}$.
$\cdot 75$ of $18 .=-75$ of 12 d .
$=9 \mathrm{~d}$.
13. To Express a Compound Number as a Decimal of a Higher Denomination.
Ex. 6. Reduce 8 r. 16 per. to the decimal of 1 a. ; and express 5 a. 8 r . 16 per. in acres only.
$40) 16$ per.
16 per. $=\frac{16}{40} \mathrm{r} .=4 \mathrm{r}$.
4) $3 \cdot 4 \mathrm{r}$.

85 a.
7. Express 17 owt. 3 qrs. 14 lbs. 8 oz. in owt. onty.
8. Express 7 bu. 3 pk .1 gal. in busheln only.
9. Express $8 \frac{3}{4} \mathrm{ft}$. as the decimal of 1 fathom.
10. What decimal of 4 oz. is $2 \mathrm{oz} .16 \mathrm{dwt} .19 \cdot 2 \mathrm{gr}$.
11. Express 5 da. 9 hr .46 min .48 sec . in hours only.
12. Express $\frac{8}{<}$ of $\frac{1}{2}$ of 224 lb . as the decimal of 1 ton.

Section VII. Practice.
168. Practice is a convenient method of solving many examples in Multiplication of Compound Numbers.

Ex. r. Find the cost of 864 articles at $88 \frac{1}{3}$ cents esoh.

$$
88 \frac{1}{3} c=\$ \frac{1}{\frac{\$ 364}{\$ 121 \cdot 83 \frac{1}{3}}=\quad=\text { cost at } \$ 1 \text { each. }}
$$

Ex. 2. Find the price of 2 a. 3 r. 14 per. of land at $\$ 160$ per acre.

$$
40 \left\lvert\, \begin{aligned}
& \frac{2 \times \$ 160}{3 \times \$ 40}=\$ 320=120=\text { price of } 2 \mathrm{a} \\
& \frac{14 \times \$ 1}{14 \times 14}=\quad \text { r r. } \\
& \$ 354=\text { entire cost. }
\end{aligned}\right.
$$

Ex. 3. Find the cost of 7 t .6 cwt .3 qr .5 lb . of iron at $\$ 60$ per ton.


Exeroise xciij.
Find the price of

1. 768 articles ${ }^{2}$ 2K 2 。
K. 185 artioles at
2. 297 " 60 c .
3. 364 " 81.20.
4. $291 \ll 1.83 \frac{1}{3}$.
5. 828
6. 147
7. 264

8. 15 a. 8 r. 25 per. of land at $\$ 24$ per acre. 10. 9 gal. 3 qt . 1 pt. of wine at $\$ 3.60$ per gallon
9. 84 bu .3 pk .1 gal . of wheat at $\$ 1.20$ per bushel.
10. 7 oz .15 dwt .6 gr . of gold at $\$ 16$ per ounce.
11. 29 a. 3 r .17 per, of land at $\$ 80$ per acre.
12. 8 t .13 cwt .1 qr .15 lb . of hay at $\$ 12$ per ton.
13. What is the cost of constructing a road 17 mi .8 fur. 15 rd. long at $\$ 1880$ per mile.

## Exercise xciv.

## Problems' Involving the Previous Rules.

1. What is the value of a silver pitcher weighing 2 lb . 10 oz. avoirdupois, at $\$ 2.24$ per ounce Troy?

$$
1 \mathrm{oz} . \text { Troy. }=480 \mathrm{gr} .
$$

1 lb . Avoird. $=7000 \mathrm{gr}$.
2 lb .10 oz . " $=2 \frac{8}{8} \times 7000 \mathrm{gr} .=\frac{21}{8} \times \frac{7000}{480} \mathrm{oz}$. Troy.
Price 1 oz. Troy $=\$ 2.24$.
Price of $\frac{21}{8} \times \frac{7000}{480} \mathrm{oz}$. Troy $=\frac{21}{8} \times \frac{7000}{480} \times \$ 2.24=\$ 85.75$.
2. How many pounds of gold are actually as heavy as 10 lb . of iron?
8. If a druggist buys 25 lb . avoirdupois of drugs at $\$ 8 \frac{1}{3}$ a pound, and sells them in prescriptions at 75 cents an ounce apothecaries' weight, what is the gain ?
4. How many sovereigns will weigh one ounce avoirdupois, if 1869 weigh 40 pounds troy?
5. If $\frac{1}{3}$ of an inch on a map corresponds to seven milea of a country, what distance on the map represents 20 miles?
6. The value of 1 lb . troy of standard gold is $£ 4614 \mathrm{~s}$ 6d.; calculate the value of a vase of the same material whose weight is 39 oz .18 dwt .

$$
\begin{array}{r}
1 \mathrm{lb} .=240 \mathrm{dwt} . ; \quad \begin{array}{r}
39 \mathrm{oz} .18 \mathrm{dwt.}=798 \mathrm{dwt} . \\
£ 46 \\
14 \mathrm{~s} .6 \mathrm{~d} .
\end{array}=11214 \mathrm{~d} .
\end{array}
$$

Cost of $240 \mathrm{dwt}=11214 \mathrm{~d} . ;$
$\cdots \quad 1 \mathrm{dwt} .=\frac{11214 \mathrm{~d}}{240}=\frac{8607}{120} \mathrm{~d} . ;$
$\therefore \quad 798 \mathrm{dwt}=\frac{798 \times 5807}{120} \mathrm{~d} .=\frac{133 \times 5607}{20} \mathrm{~d}$.

$$
=87286 \frac{11}{2} \mathrm{~d},=£ 1557 \mathrm{~s}, 2 \frac{11}{2} \mathrm{~d}
$$

7. If 81 owt. of cheese cost $£ 694 \mathrm{~s} .8 \mathrm{~d}$., what will 15 cwt. 2 qr. cost ?
8. Bought 2 oz . of tea for $7 \frac{3}{1} \mathrm{~d}$., what is that per lb . P
9. If 8 qr .24 lh . cost $£ 416 \mathrm{~s} .8 \mathrm{~d}$., how much is that per lb.
10. If when flour is $\$ 5$ a barrel the five-cent loaf of bread weighs 10 oz., what ought to be its weight when tour is $\$ 8$ a barrel?
11. If $1 \nmid$ acres of land sell for $\$ 34.50$, what will 20 a. 2 r. 10 per. cost, at the same rate ?
12. If 18 a. 3 r. 20 per. cost $\$ 900$, what will 150 aores cost at the same rate?
13. If $1 \frac{1}{2}$ bushels of wheat cost $\$ 1.68 \frac{3}{4}$, what will 154 ba 1 pk. 6 qt. cost ?
14. If a train travels 800 miles in 9 hr .40 min., how long will it be in travelling 223 miles !

15 . If 7 gal .1 qt . of wine cost $\$ 17.40$, what will 8 qt . 1 pt . cost at the same rate ?
16. If 15 yards, $\frac{3}{4}$ yard wide, will make a dreas, how many yards, f of a yard wide, will make another dress of the same size?

Yards required $\frac{3}{4}$ or $\frac{6}{8}$ yd. wide $=15$ yards.
" $\frac{1}{\text { t yd. } " ~}=6 \times 15$ ydm.
$\omega$
Pyd. " $=\frac{6 \times 15}{6}$
$=18 \mathrm{yds}$.
17. How many yards of cloth, $\frac{5}{8}$. wide, will be required to line 35 yards, $1 \frac{3}{4}$ yards wide?
18. If it requires 36 yards of carpeting, $\frac{3}{4} \mathrm{yd}$. wide, to cover a floor, how meny yards, $\frac{7}{8}$ yd. wide, will be required to cover the same floor?
19. A regiment of 1000 men are to have new coats; each coat is to contain $2 \frac{1}{2}$ yards of oloth, $1 \frac{1}{}$ yards wide, and to be lined with shalloon 3 yd . wide ; how many yards of shalloon will be required i
20. A bankrupt owes $\$ 4000$, and his assets-that is, his whole property-amounts to no more than $\$ 840$; what dividend will his creditors receive in the dollar ?

Assets paid on $\$ 4000=\$ 840$;

$$
\text { " } \quad \$ 1=\$ \frac{840}{4000}=\$ \frac{81}{100}=21 \text { conts. }
$$

21. A merchant became insolvent, owing $\$ 6850$, and had only $\$ 4952$ with which to pay his creditors; how much should a creditor, whose olaim is $\$ 1540$, receive ?
22. What does a bankrupt pay in the pound if his ereditors receive $£ 3765 \mathrm{~s}$. out of $£ 2076$ ?
23. How much will a creditor lose on a debt of $\$ 5812.25$ if he receives only $67 \frac{1}{2}$ cents in the dollar 9
24. A creditor loses $87 \frac{1}{4}$ oents in the dollar of what was due to him, and thereby loses 8880 ; what was the sum due?
25. The people of a school section wish to build a new school-house, which will cost $\$ 2850$. The taxable property of the section is valued at $\$ 190000$; what will be the tax on the dollar, and what will be a man's tax whome property is valued at $\$ 7500$ ?

$$
\begin{aligned}
& \text { Tax on } \$ 190000=\$ 2850 \text {; }
\end{aligned}
$$

26. In a sohool section a tax of $\$ 800$ is to be raised. If the amount of taxable property is $\$ 250000$, what will be the tax on the dollar, and what is $A$ 's tax, whose property is valued at $\$ 1800$ ?
27. What is the assessed value of property tared $\$ 87.80$ at the rate of $4 \frac{1}{2}$ mills on the dollar?
28. A person after paying an income tax of 22 mills on the dollar has \$2984 left; what is his income?
29. A merchant buys a chest of tea containing 2 qr . 10 lb . at 60 cents per lb., and two chests containing 8 qr . 15 lb . at 70 cents per lb .; what will he gain by selling the misture at 80 cents per lb. ?

$$
\begin{aligned}
& 2 \mathrm{gr} .10 \mathrm{lb} .=60 \mathrm{lb} . ; 8 \mathrm{qr} .16 \mathrm{lb} .=90 \mathrm{lb} \text {. } \\
& \begin{array}{l}
60 \mathrm{lb} \text {. at } \quad 60 \text { cents per lb. }=\$ 36 \text {; } \\
90 \quad \text { " } \\
70
\end{array} \\
& \therefore \text { Cost of } 150 \text { u } 80 \text { " }=\$ 99 \text {. } \\
& \text { Cost of } 150 \text { " } 80 \text { " } \quad=\$ 120 \text {; } \\
& \text { Gain }=\$ 21 \text {. }
\end{aligned}
$$

30. A groeer buys coffee at $\$ 34$ per cwt., and chicory at $\$ 10$ per owt., and mixes them in the proportion of 5 parts of chicory to 7 of coffee; he sells the mixtare at 80 cents per lb. ; what does he gain on each pound ?
31. If I mix 20 lb . of tea at 70 cents per lb. with 15 lb . at 60 cents per lb . and 40 lb . at $62 \frac{t}{5}$ cents per lb , what is 1 lb . of the mixture worth ?

## OHAPTEK VII.

## AVERAGES AND PERCENTAGFE.

## Section I. Averages.

169. The Average of several numbers is that number which when put in place of each of the given numbers makes their sum the same.

Ex. I. Find the average of $80,35,42,80$ and 100. $30+35+42+80+100=287$.
There are 5 numbers; therefore $\frac{1}{5}$ of 287 will be the number which substituted for each of the given numbers will produce the sum 287 ; $\frac{287}{5}=57 \cdot 4$.

## Ezercise xcv.

Find the average of

1. $16,18,26,80,36,42,50$ and 56.
2. 17, 0. 20, 30, 70, 100, 27, 9 and 17.
3. 120, $840,560,780,320$ and 840.
4. Five pupils obtained the following marks at an examination, $60,36,75,21$, and 80 , respectively; what was their avorage mark ?
5. There were 45 papils at school on Monday, 48 on Tuesday, 47 on Wednesday, 45 on Tharsday, and 40 on Friday. What was the average attend unce for the week?
6. The average temperature of the different months during the past 87 years at Toronto was, of Jan. 29094, Feb. $22^{\circ} \cdot 58$, March $29^{\circ} .05$, April $40^{\circ} .68$, May $61^{\circ} .68$, June 61 .84 , July $67^{\circ} .48$, Aug. $66^{\circ} .351$, Sopt. $58^{\circ} .10$, Oot. $45^{\circ} .74$, Nov. $86^{\circ} .03$, Dec. $25^{\circ} .56$. What was the average yearly temperature during that period?

## Section II. Percentage.

17(1. The term, por cont. means by or on a kundred; thus, 3 per cent. on raything means 8 on every hundred of it. Hence 1 per cent. of a namber is rof of it; 2 per cent, is $\frac{2}{100}$ of it ; 7 per cent. is $\frac{7}{100}$ of it, \&c,
171. The sign, $\%$, is generally used to represent the words per cent. Thus, $3 \%$ is read 3 per cent.

Ex. 1. Find 5 per cent of $\$ 360$. Since $\$ 100$ yields $\$ 5$;

$$
\begin{aligned}
& \$ 1 \\
& \$ 360 \\
& \$ 1
\end{aligned} \frac{\$ 18}{100} ; \frac{360 \times 8}{100} \text { or } \$ 18 .
$$

Find
Exercise xcti.

1. 16 per cent. of $450 . \quad$ 4. $5 \nmid$ per cent. of $\$ 200$.
2. 20 " of $\$ 75$. 5. $2 \frac{1}{3}$ " of 600 men .
3. $83 \frac{1}{3}$ " of 69 sheep.
4. $7 \frac{1}{7}$ " of 630 .

Ex. 2. A merchant sold 80 yd . of oloth from a web containing 250 yd .; what per cent of the web did he sell ?

From 250 yd. he sold 80 yd ;
1 yd . " $\frac{80}{250} \mathrm{yd}$; 100 yd . " $\frac{100 \times 80}{250} \mathrm{yd}$. or 82 yd .
$\therefore$ he sold $32 \%$.
7. A farmer who had 800 bu. of wheat sold 820 bu.; what per cent. of his wheat did he sell?
8. $\mathbf{A}$ fourth of a field has been ploughed; what per cent. of the field remains to be ploughed?
9. 780 is what per cent. of 1300 ? of 2145 ?

Ex. 3. Of what number is $60,8 \%$ ?
Sinoe $8=8 \%$ of 100 ;

$$
\begin{aligned}
1 & =8 \% \text { of } \frac{100}{8} ; \\
60 & =8 \% \text { of } \frac{60 \times 100}{8}=750 .
\end{aligned}
$$

10. Find the number of which 275 is $25 \%$.
11. How much must be a clerk's salary in order that 17 $\%$ of it may be $\$ 204$ ?

## Section III.-Insurance.

172. Insurance is security gaaranteed by one party on being paid a certain sum, to another against any loss.

1\%\%. The Premium is the sum paid for the insurance. It is always a certain per cent. of the sum insured.
174. The Policy is the written contract of insurance.

Ex. 1. What is the premium for insuring a house valued at $\$ 5000$ at $1 \downarrow$ per cent.

Preminm on $\$ 100=\$ 1$;

$$
\begin{array}{ll}
\because \quad \$ 1 & =\$ \frac{11}{100} ; \\
& \$ \quad \$ 5000 \\
& =\$ \frac{5000 \times 1\}}{100}=\$ 62.60 .
\end{array}
$$

## Exercise xevii.

Find the premium on

1. $\$ 600$ at $8 \%$.
2. $\$ 8000$ at $1 \$ \%$.
3. $\$ 840$ at $1 \frac{1}{3} \%$.
4. $\$ 7360$ at $1 \frac{1}{2} \%$.
5. $\$ 760$ at $2 \%$.
6. $\$ 375$ at $8 \%$.
7. $\$ 9500$ at $1 \frac{3}{4} \%$.
8. $\$ 4890$ at $1 \frac{1}{3} \%$.

Ex. 2. For what sum should goods worth $\$ 4,900$ be insured at $2 \%$ so that, in case of loss, the owner may recover both the value of the goods and premium paid $?$
Premium on $\$ 100$ at $2 \%$ is $\$ 2$.
Insurance on goods worth $\$ 98=\$ 100$;

9. For what sum must a house worth $\$ 2400$ be insured at $4 \%$ so that, in case it is burned, the owner may recover both its value and the premium paid?
10. What sum should be insured at $3 \%$, on goods worth $\$ 6790$, that the owner may receive both their value and the premium, in case of loss?
11. The premium at $2 \frac{1}{2} \%$ on a cargo of goods amounted to $\$ 1750$; what was the value of the cargo ?
12. The premium for insuring a house at $\frac{1}{4} \%$ is $\$ 24$; what is the value of the house?
13. The premium for insuring a house and furniture at


## Section IV. Commission and Brokerage.

1ys. Commission is the charge made by an agent for buying or selling goods, and is generally $a$ percentage on the money omployed in the transaction.

17\%. Brokerage is the charge made by a broker for buying or selling stocks, bills of exchange, etc.

Ex. 1. My agent has bought tea, on my account, to the amount of $\$ 750$. What is his commission at $2 \%$ ?

$$
\begin{aligned}
\text { The commission on } \$ 100 & =\$ 2 ; \\
& \$ 1=\$ 100 ; \\
& \$ 750
\end{aligned}=\$ \frac{700 \times 9}{}=\$ 15 .
$$

Exercise xctiii.
Find the commission on
$1 . \$ 230$ at $4 \%$.
2. $\$ 790$ at $2 \%$.
${ }^{\text {i11 }}$ g. $\$ 800$ at $1+\%$.
4. $\$ 1200$ at $2 t$ \% :
5. $\$ 7600$ at $81 \%$
6. $\$ 4800$ at $2 \frac{1}{2} \%$.

Ex. 2. I send my agent $\$ 1470$ with instructions to deduct his commission at $5 \%$ and invest the " ba ' ance in wheat. How much does hé invest'?

Commission on $\$ 100$ at $5 \%$ is $\$ 5$.
Sum invested out of $\$ 105=\$ 100$;

110以19.8

1 - 1 (2)
$\$ 1=\$ 100 ;$
$81470=\frac{8140 \times 100}{13105}$
$=\$ 1400$.
7. Sernt $\$ 2600$ to my agent to invest after doducting his commission at $4 \%$ What sum did he invest?
8. I sent my agent $\$ 9180$ with instructions to deduct his 60 minission at $2 \%$ and invest the balance in wheat. How much wheat aid he purchase at $\$ 1.20$ per bushef $8^{\prime}$
9. An agent receives 81.55 as his compensation for purchasing goods at $4 \%$ commission." What is the valtie of goods purchasea'?
 What is his brokerage at $\frac{1}{}$ per cent ?
11. If a commission of $\$ 106.47$ is paid for selling $\$ 3276$ worth of goods, what is the rate per cent?

## Section V.-Interest.

1. If I lend you $\$ 500$ and you have to pay $m e \$ 1$ for the use of each $\$ 100$ per year, how much will I receive for 1 year?
2. How much must you pay for the use of $\$ 800$ for 1 year, if you have to pay $\$ 2$ for the use of each $\$ 100$ per year, or 2 cents for each dollar? If you have to pay $\$ 3$ ? \$4? \$8?

1\%'. The sum paid for the use of money is called Interest.
178. The money on which the interest is paid is called the Principal.
179. The number of dollars paid for the use of $\$ 100$ for one year is called the Rate per cent.

Note 1.-When the rate per cent. is stated without the mention of any length of time, the time is understood to be one year.

Ex. 1. What is the interest on $\$ 2750$ for 1 year at 8 per cent. ?

Interest on $\$ 100$ for 1 year $=8$;

$$
\begin{aligned}
& \because \quad \begin{array}{lll}
\because & \$ 1 & \prime \\
& \$ 2750 & =\$ 100:
\end{array} \\
& \text { • } \$ 2750 ، \quad=\frac{\$ 2750 \times 8}{100} \\
& =8220 \text {. }
\end{aligned}
$$

1. What is the interest on $\$ 600$ for 1 year at $8 \%$ ?
2. What is the interest on $\$ 550$ for 1 year at $7 \%$ ?
3. What is the interest on $\$ 3152.16$ for 1 year at $7 \frac{1}{2} \%$ ?
4. A man borrowed $\$ 7200$ for 1 year, viz., $\$ 1250$ at $7 \%$; $\$ 1340$ at $7 \frac{1}{2} \%$; $\$ 2360$ at $8 \%$; and the remainder at $8 \frac{1}{2} \%$. How much interest has he to pay at the end of the year?
5. Four brothers have to divide equally the interest of $\$ 25800$ at $7 \%$. How much does each receive each year?

Ex. 2. What is the interest on $\$ 575$ for 5 years at $7 \%$ ?

Interest on $\$ 100$ for 1 year $=87$;

7. What is the interest on $\$ 986$ for 4 years at $6 \%$ ?
8. What is the interest on $\$ 1573$ for 4 years at $8 \%$ ?
9. What is the interest on $\$ 500$ for 2 years att $8 \frac{1}{2} \%$ ?
10. What is the interest on $\$ 2245.85$ for 5 years at $7 \frac{1}{2} \% 1$

Ex. 3. What is the interest on $\$ 672$ for 4 yr .8 mo. at $9 \%$ ?
$4 \mathrm{yr} .8 \mathrm{mo} .=4 \mathrm{r}_{2}^{8}$ yr. $=4{ }^{3}$ years.
Interest on $\$ 100$ for 1 year $=\$ 9$;

11. What is the interest on $\$ 924$ for 3 yr .7 mo . at $6 \%$ ?
12. What is the interest on $\$ 954$ for 4 yr .8 mo . at $7 \%$ ?
18. What is the interest on $\$ 504.72$ for 3 yr .10 mo . at $8 \%$ ?
14. What is the interest on $\$ 640.75$ for 8 yr .4 mo . at $9 \%$ ?
180. From the preceding examples wo have the following rule for finding the interest on a given sum of money at a given rate per cent. for any number of years.

Multiply the Principal by the Rate per cent., the product by the number of years, and divide this result by 100.
181. The Amount is the name given to the prin. cipal and interest together.

Ex. 4. If a man borrows $\$ 480$ for 8 months at $8 \%$, what amount should he return at the end of that period?

Interest on $\$ 480$ for 12 months $=\$ \frac{4 \mathrm{~B} 0 \times \mathrm{y}}{100}$;


$$
\begin{aligned}
& \text { Interest }=\$ 25.60 \\
& \text { Principai }=\$ 480.00 \\
& \text { Amount }=\$ 505.60
\end{aligned}
$$

18. Find the interest on $\$ 500$ for 156 days at $7 \%$.
19. Find the interest on $\$ 7500$ from May 5 to Oct. 27 , at $8 \%$.
20. Find the interest on $\$ 8000$ from Jan. 26, 1876, to March 81, 1878, at $7 \frac{1}{2} \%$.

Ex. 6. At what rate per cent. must $\$ 756$ be put at interest for 4 years to yield $\$ 241.92$ ?

Interest on $\$ 756$ for 1 year $=\$ \frac{241.02}{4}=\$ 60.48$;

$$
\begin{array}{rll}
4 & \quad \$ 1 \quad & =\$ \frac{60.48}{756} ; \\
" \quad \$ 100 \quad " \quad & =\$ \frac{100 \times 60.48}{756} \\
& =\$ 8, \text { or } 8 \text { per cent. }
\end{array}
$$

21. A man pays ${ }^{\frac{5}{7} 72}$ for the use of $\$ 900$ for 1 year, what is the rate per cent?
22. A man lent $\$ 484$ for 5 years, and received $\$ 181.50$ for the interest; what was the rate per cent.?
23. If $\$ 108.68$ interest is received on a principal of $\$ 432$ for 4 vears, what is the rate per cent. ?

Ex. 7. What principal will bring $\$ 200$ interest in 146 days at 5 per cent. ?

Principal to give $\$ 5$ in $\mathbf{3 6 5}$ days $=\$ 100$;

24. A man borrowed money at 7 per cent, and paid $\$ 245$ interest a year ; how much money did he borrow?
25. A man bequeathes his wife $\$ 875$ a year, his daughter $\$ 770$ a year, and his son $\$ 630$ a year; what sum must be invested at 7 per cent. to produce these amounts ?
26. Suppose a gentleman's interest on money, at 6 per cent., is $\$ 45$ per month. How much is he worth ?

Ex. 8. In what time will $\$ 800$ amount to $\$ 880$ at 8 per cent.

Interest $=\$ 880-\$ 800=\$ 80$.
The interest of $\$ 800$ for 1 year at 8 per cent. is $\$ 64$.
Time to produce $\$ 64=1$ year ;

$$
\begin{aligned}
\$ 1 & =\frac{1}{64} \text { year } ; \\
\$ 80 & =\frac{80}{64}=1 \frac{1}{4} \text { years } \\
& =1 \text { jr. } 3 \text { mo. } .
\end{aligned}
$$

27. How long a time would be required for $\$ 525$ to gain $\$ 110.25$ at 7 per cent. ?
28. How long a time would it require for $\$ 625$ to amount to $\$ 756.25$ at 7 per cent. ?
29. A principal of $\$ 600$ was loaned May 20th, 1878 , at $7 \frac{1}{2}$ per cent. At what date did it amount to $\$ 796.87 \frac{1}{2}$ ?
30. A note given for $\$ 273.25$ at 7 per cent, remained unpaid until the interest equalled the principal? How long did it run ?

## Section VI.-Present Worth and Discount.

John Smith owes me a debt of $\$ 108$ to be paid at the end of a year, without interest; how much is the debt worth ot present, and how much ahould be allowed for the immediate payment of the debt, money being worth 8 per cent.?

If I receive $\$ 100$, and put it ont to interest at $8 \%$ for one year, it will amount to $\$ 108$; hence, the present worth of the debt is $\$ 100$. Evidently $\$ 8$ should be allowed for immediate payment.
182. The Present Worth of a note or debt, payable at some future time, without interest, is such a sum as, being put out to interest, will amount to the given debt when it becomes due.
183. The allowance or deduction made for the payment of the debt before it becomes due is called Discount.

Ex. 1. What is the present worth of $\$ 585$, payable in 1 year, the rate of interest being 7 per cent ?
Amount of $\$ 100$ in 1 yr. at $7 \%=\$ 107$.

## Exercise c .

1. What is the present worth of $\$ 1250.509$, payable in 1 year, the rate of interest being $7 \%$ ?
2. What is the present worth of $\$ 512.40$, payable in 1 year, when money is worth $12 \%$ ?

Ex. 2. What is the present worth of $\$ 787.75$ due in 2 yr. 6 mo., when money is worth $6 \%$ ?

Amount of $\$ 100$ for 2 yr .6 mo . at $6 \%=\$ 115$.
Present worth of $\$ 115$

$$
\begin{aligned}
& \text { " " } \$ 1=\$ \frac{100}{15} \text {; } \\
& \text { " } \quad 8787.75=\$ \frac{787.75 \times 100}{115} \\
& =\$ 685 .
\end{aligned}
$$

3. What must be paid now to cancel a debt of $\$ 994.50$ due 1 yr. 9 mos. hence, at $6 \%$ ?
4. Which is the more profitable, to buy lumber at $\$ 25$ a thousand on 9 months' credit, or at $\$ 24.50$, on 6 months' credit, money being worth $6 \%$ ?
5. Bought two lots for $\$ 2541$, on 3 years' time, without interest ; what is the cash value, monev heing woth $7 \%$ ?
6. I buy goods for $\$ 1150$ cash and sell them for $\$ 1224$ on a credit of 4 months; do I gain or lose, and how much, interest being $6 \%$ ?

Ex. 3. A note for $\$ 1880.06$ becomes due in 15 months; what deduction should be made for the immediate nayment of the money, supposing money to be worth $8 \%$ ?

The interest on $\$ 100$
Discount on $\$ 110$
" \$1

$$
\begin{aligned}
\text { for } 15 \text { months } & =\$ 10 . \\
" \quad & =\$ 10 ; \\
" \quad & =\$ 110 ; \\
& =\$ \frac{1380.06 \times 10}{110} \\
& =\$ 125.46 .
\end{aligned}
$$

7. What is the discount on $\$ 897.82$ payable in 3 years, when money is worth $7 \%$ ?
8. What is the discount on a note for $\$ 1174.32$ due in 3 jr .8 mo., money being worth $8 \%$ ?
9. What is the difference between the interest and the discount on $\$ 525$ due 10 mos. hence, at $6 \%$ ?
10. The discount found in Ex. 3 is called True Discount. There is another kind of discount called Bankers' Discount, or Bank Discount.

The difference between the two kinds of discount is this-the true discount is the interest of the present value of the bill for the time, while the bankers' discount is the interest of the amount of the bill itself, not only for the specified time but for three days additional called days of grace. The bankers' discount is thus always in excess of the true discount.

Ex. 4. What is the discount and present worth of a note of $\$ 584$, drawn Jan. 8 at 11 months, discounted at the Bank May 10, at 5 per cent.

11 mo. from Jan. $8=$ Dec. 8,
which with 3 days of grace $=$ Dec 11 . From May 10 to Dec. 11 is 215 days. Discount or Interest of $\$ 584$ for 215 days at $5 \%$ $\begin{aligned} \text { Principal } & =\$ 17.20 \\ \text { Present Worth } & =\$ 566.80\end{aligned}$
10. What is the bank discount on a note for $\$ 730$ for 30 days at $6 \%$.
11. Suppose a bill for $\$ 1200$ is drawn on the 12 th of Angnst at $\hat{6}$ montins, and paid by a bauker on the ist of January, find the money he takes off at 7\%.

## OHAPTER VIII.

## SQUARE ROOT.

1. What is the second power of $\overline{5}$ ? of 9 ? of 12 ?
2. What number multíplied by itself will produce 86 ? -49\% 121? 81 ?
3. Find the number whose second power is $9 ?$ is $25 ?$ is $64 ?$ is 144 ?
4. Resolve each of the following numbers into two equal factors: $16,25,81,49,100$.
5. The Second Power of a number is called its Square.

Nots.-The square of a number is indicated by writing 2 to the right and above the given number; thus, $5^{2}$ is read 5 squared.
186. The Square Root of a number is one of its two equal factors.

18\%. Principle. The square of a number of two digits is equal to the square of the tens, plus twice the tens multiplied by the units, plus the square of the units. Thus,

$$
35^{2}=30^{2}+2 \times 30 \times 5+5^{2}=900+300+25=1225
$$

Ex. I. Find the square root of 2025.
$20 \mid 25$ ( 45 We separate the number into periods of
16 425 ing from the decimal point. We then 425 4 as the does not exceed 20. This is 4. We write 4 as the first figure of the square root and place its square, 16, under 20 and subtract, and to the remainder, 4 , we annex the next period, 25 , to make a dividend. We double the figure 4, placed in the root to form the first figure of a divisor. As we have to annex another figure to 8 , we call the 8,8 tens or 80 . 80 is contained in 425 5 times. We write 5 as the second figure of the root and annex it to the 8 . We next multinly 85 by 5 and mitite the product under 425 and subtract. As there is no romainder the square root is 45 .

## Exercise ci.

Find the square root; of

| 1. | 289. | 5. | 1296. | 9. | 4096. |
| :--- | :--- | :--- | :--- | ---: | :--- |
| 2. | 361. | 6. | 5625. | 10. | 1869. |
| 3. | 576. | 7. | 9025. | 11. | 2209. |
| 4. | 626. | 8. | 2401. | 12. | 3136. |

Ex. 2. Find the square root of 4124961. then double the parting down the next period. We as a divisor. Wart of the root already found and write 40 12493 times call it 400, and find that it goes into the 40. Wenow we put 3 in the root and annex it to 1209, under the multiply 403 by 3 and write the product Find the square root of
13. 890625.
14. 262144.
15. 117649.
16. 5764801.
17. 40005625.
18. 25080064.

Ex. 3. Extract the square root of 7 to four places of decimals. 70100100100 ( 8866. 64

168 \begin{tabular}{l|l}

1666 \& | 600 |
| :--- |
| 489 | <br>

$\frac{11100}{9996}$ <br>
\hline
\end{tabular}

10044
In finding the square root of a decimal fraction care must be taken to make the decimal consist of an even number of figures. This is done so that the denominator of the equivalent vulgar fraction may be a complete square, Which is the case in $\frac{70}{100}, \frac{7000}{1000}$, $\frac{700000}{100000}$, \&c., but not in $\frac{7}{10}$ $\frac{700}{1000}, \frac{70000}{100000}$, \&c.
Find the square root of
19. 2209.
20. 0729.
91. - 1024.
22. 714.
28. 895.
24. $\cdot 9$.
25. 71.
26. 6.4.
27. 14.4.

## CHAPTER IX.

## MEASUREMENT OF SURFACES AND SObIDS.

## Section I.-Area of a Rectangle.

188. A Rectangle is a plane surface having four sides and four equal angles. A slate, a door, \&c., are examples of a rectangle.

Ex. I. A room is 18 feet long and 15 feet wide; what is its area?

Area of surface 1 ft . long by 1 ft . wide $=1 \mathrm{sq}$. ft. 18 ft . long by 1 ft . wide $=18 \mathrm{sq}$. ft. 18 ft . long by 15 ft. wide $=15 \times 18 \mathrm{sq} . \mathrm{ft}$. $=270 \mathrm{sq}$. ft.
Hence, to find the area of a rectangle, we multiply its longth by its width.

## Exercise cil.

Find the area of the rectangles having the following dimensions:

1. 8 ft . by 12 ft .
2. $6 \frac{1}{2} \mathrm{ft}$. by 14 ft .
3. 21 ft . by 25 ft .
4. 2 yd .2 ft . by 7 yd .
5. 17 yd . by 20 yd . 2 ft .
6. 19 ft .7 in . by 24 ft .

## Section II.-Carpeting Rooms.

189. Oarpets are sold in strips, and when the width of a strip is known, we can ascertain what length of carpet will be required to cover a given surface.

Ex. I. How many yards of carpet 2 ft .3 in . wide will be required for a room 21 ft . by 18 ft ?
Area of surface to be covered $=18 \times 21 \mathrm{sq} . \mathrm{ft}_{\mathrm{t}}$ Length of carpet, 1 ft . wide, required to cover given area

$$
=18 \times 21 \text { feet; }
$$

Length of carpet, $2 \ddagger \mathrm{ft}$. wide, required
to cover given area $\quad=\frac{18 \times 21}{2 t} \mathrm{ft}$. $=56$ yards.
Exercise cili.
How many yards of carpet 27 in . wide will be required for rooms whose dimensions are

1. $27 \mathrm{ft} . \mathrm{by} .21 \mathrm{ft}$.?
2. 15 ft . by 12 ft .?
3. 18 ft . by 24 ft . ?
4. 26 ft . by 86 ft .?

Find the cost of carpeting rooms whose dimensiuns are:
5. 18 ft . by 20 ft . with carpet 3 ft . wide, at $\$ 1.20$ a yd .
6. 20 ft . by 24 ft ., with carpet 30 in . wide, at 90 cts. a yd.
7. 15 ft . by $17 \frac{1}{2} \mathrm{ft}$., with carpet 3 ft . wide, at $\$ 1$ à yd .
8. The cost of carpeting a room 18 ft . long by 16 ft . wide, with carpet worth $\$ 1.20$ a yd., is $\$ 51.20$; how wide is the carpet?

## Section III.-Papering a Room.

190. Room papers, like carpets, are sold in strips and we ascertain the quantity that will cover a wall in the same manner as we ascertained the quantity of carpet required to cover a floor.

Ex. r. How many yards of paper 16 in . wide will be required for a room 18 ft . long, 14 ft . wide, and 8 ft . high, which contains 1 door 7 ft . high by $8 \frac{1}{2} \mathrm{ft}$. wide and 8 windows each 5 ft . high by $2 \frac{1}{2} \mathrm{ft}$. wide. Length of surface to be cov-

$$
\text { ered }=(18+14+18+14) \mathrm{ft} .=64 \mathrm{ft} .
$$

Area of entire wallis $=(8 \times 64) \mathrm{sq} \cdot \mathrm{ft} .=512 \mathrm{sq} . \mathrm{ft}$.
Area of door $=(33 \times 7) \mathrm{sq} . \mathrm{ft} .=24 \frac{1}{2} \mathrm{sq} . \mathrm{ft}$.
Area of 8 windows $=\left(3 \times 2 \frac{1}{2} \times 5\right) \mathrm{sq} . \mathrm{ft} .=37 \frac{1}{2} \mathrm{sq} . \mathrm{ft}$. Area of door and windows $=\left(24 \frac{1}{2}+37 \frac{1}{2}\right) \mathrm{sq} . \mathrm{ft} .=62 \mathrm{sq} . \mathrm{ft}$.

Area to be papered $=(512-62) \mathrm{sq} . \mathrm{ft} .=450 \mathrm{sq}$. ft.

$$
450 \mathrm{sq} . \mathrm{ft} .=450 \times 144 \mathrm{sq} . \mathrm{in}
$$

$\therefore$ length of paper required $=\frac{450 \times 144}{18}=4050 \mathrm{in}$.

$$
=112 \frac{1}{2} \text { yards. }
$$

## Exercise civ.

1. How meny yards of paper 20 in . wide will be required for a room 20 ft . long, 15 ft . wide, apd 9 ft . high ?
2. How many sq. ft, of paper will be required for a room 18 ft .9 in . long, 15 ft .3 in . wide and $8 \frac{1}{2} \mathrm{ft}$. high ?
3. A room 24 ft . long, 20 ft . wide and 10 ft . high contains 2 doors each 7 ft . by 4 ft . and 6 windows each $5 \frac{1}{4} \mathrm{ft}$. by 4 ft . ; find how many yards of paper 2 ft . wide will be required to paper it 9
4. How many yards of paper 30 in . wide will it require to cover the walls of a room 15 ft . long, 12 ft . wide and 8 ft. high ?
5. William Benson has agreed to plaster the walls and ceiling of the room in the last example, at 10 cents per sq. yd.; what will his bill amount to?

## Section IV.-Measurement of Solidity.

Ex. r. Find the number of cubic feet in a rectangular piece of timber 24 ft . long, 3 ft . wide, and 2 ft. thick.

If this piece of timber be cut into blocks 1 ft . long there will be 24 such blocks.
Number of cu. ft. in 1 block $=6 \mathrm{cu}$. ft.
24 blocks $=24 \times 6 \mathrm{cu} . \mathrm{ft} .=144 \mathrm{cu} . \mathrm{ft}$.
Hence to find the cubic content of a rectangular solid, we take the product of its length, breadth, and thickness.

## Exercise CV.

Find the cubic content of the rectangular solids whose dimensians are

1. $8 \mathrm{ft} ., 6 \mathrm{ft} ., 5 \mathrm{ft}$.
2. $2 \frac{1}{2} \mathrm{ft}$., $5 \frac{1}{3} \mathrm{ft}$., $7 \frac{1}{8} \mathrm{ft}$.
3. 3 ft ., $7 \frac{1}{2} \mathrm{ft}$., $8 \frac{1}{\frac{1}{\mathrm{f}} \mathrm{ft}}$.
4. 2.6 ft ., 8.5 ft ., 5 ft .

Ex. 2. How many bricks will be required to build a wall 20 ft . long, 15 ft . high, and 18 in . thick, each brick being 8 in. long, 4 in. wiae, and 3 in. thick?

Cubic content of wall $=(20 \times 12 \times 15 \times 12 \times 18)$ cu.in.

$$
\text { " brick }=(8 \times 4 \times 3) \text { cu. in. }
$$

$\therefore$ Number of bricks required $=\frac{20 \times 12 \times 15 \times 12 \times 18}{8 \times 4 \times 3}$

$$
=8100
$$

5. How many bricks will be required to build a wall 45 ft. long, 20 ft . high, and 15 in . thick, each brick being 9 in. long, $4 \frac{1}{2}$ in. wide, and 3 in. thick ?
6. What will it cost to put a stone foundation under a barn 36 ft . long by 24 fit. wido at 25 cents a cubic jazd, the wall being 7 feet high and 2 ft . thick ?

## Miscellaneous Problems.

1. A garrison of 800 men had provisions to last for 60 days, but 15 days afterwards 80 men were killed ; how long will they last the remainder?

They would last 800 men 45 days.

2. 28 shanty men have provisions for 20 days, but 7 men more arrived; how long will the provisions now last?
8. A garrison of 1000 men was victualled for 28 days; after 11 days it was reinforced by 2400 men; how long will the provisions last?
4. A garrison of 450 men had provisions for 5 months, but 200 men were sent away; how long will the provisions last the remainder?
6. A garrison of 1000 men was victualled for $\mathbf{3 0}$ days; after 10 days it was reinforced by 8000 men; in what time would the provisions be exhausted?
6. $A$ can do a piece of work in 8 days, and $B$ can do it in 9 days; how long will it require $\boldsymbol{A}$ and $\boldsymbol{B}$ working together to do it ?
$\begin{aligned} & \text { The part } A \text { dees daily }=\frac{1}{8} \\ & \text { " } B \\ & \text { " } A \& B \text { do." }=\frac{1}{8} \\ &=\frac{1}{8}+\frac{1}{8}=\frac{1}{7} \frac{7}{2} ;\end{aligned}$
$\therefore$ thiey do $\frac{1}{79}$ in $\frac{1}{1}^{\frac{3}{y}}$ day;
$\therefore$ they do the whole work in $\frac{18}{17}$ days, or $4 \frac{4}{1} \frac{1}{7}$ days.
7. $A$ can do a piece of work in 12 hours, and $B$ can do it in 15 hours; in what tirne can both working together do the work?
8. $A$ can do a piece of work in 20 days ; $B$ can do it in 24 days, and $O$ can do it in 80 days; in wiat time will they all do it working together P
9. 1 oan build a wall in 8 days, $B$ in 12 day and $O$ in 15 days; in what time can they all build it working togother?
10. A anantity of flour lasta a man and wife 9 daya, and the wife alone 27 days; how long would it last the mas alome?
11. 4 oan do a piece of work in 20 days; after working at it for 8 days $B$ comes to help him and they finish the work in 5 days; how long would it take $B$ by himself to do the work?
12. $A$ can do $\frac{?}{z}$ of a piece of work in 8 days; $B$ can do 7 of the same work in 12 days; in what time could both working together do 2 such pieces of work ?
18. $A$ and $B$ can mow a field in 12 days; $A$ and $C$ in 15 days; $B$ and $C$ in 20 days ; in what time could $A$ mow it by himself ?

$\therefore 2 A^{\prime} s$ and $2 B^{\prime} s$ and $2 C^{\prime \prime} s " \quad \frac{1}{18}+\frac{1}{15}+\frac{1}{20}{ }^{\prime \prime}=\frac{1}{5}$;

$\therefore A$ can do the work in 20 days.
14. $A$ and $B$ can do a piece of work in 8 days; $A$ and $C$ can do it in 9 days, and $B$ and $O$ in 10 days; in what time can all three working together do it?
15. $A$ and $C$ can dig a gardon in 10 days; $B$ and $O$ can dig $\frac{1}{3}$ of the same garden in 4 days, and $B$ alone can dig it in 20 days; in what time can $A$ do it by himself?
16. A piece of work has been half done by $A, B$, and $C$ working together, in 8 days; if $A$ and $B$ together can finish it in 12 days, in what time could $C$ have finished it?
17. A can do a piece of work in 6 days of 10 hours each, and $B$ can do it in 8 days of 9 hours each; for how many hours a day should $A$ and $B$ be ongaged together, that the work may be done in 4 days?
18. If 6 men or 9 women can do a piece of work in 12 days, in what time will 4 men and 7 women do it?

6 men do the work in 12 days $\therefore 1$ man does $\frac{1}{12}$ of it in 1 day.
9 women do the work in 12 days.$\therefore 1$ woman does $\frac{1}{108}$ of it in 1 day.
$\therefore 4$ men and 7 women do $\frac{4}{12}+\frac{7}{108}$ or $\frac{13}{108}$ of it in 1 day.
$\therefore \quad$ " " $\frac{1}{108}$ of it in $\frac{1}{13}$ day.
$\therefore \quad$ " do it in $\frac{108}{13}$ day, or $8 \frac{4}{13}$ days.
19. If 7 boys or 4 men can do a piece of work in 9 digys in whot time con 4 boyg and 7 men do it?
20. If 3 men or 5 women do a piece of work in 12 dayn, in what time can 2 men and 1 woman do it?
21. If 1 man aud 2 women can do a piece of work in 8 days, and 8 men and 4 women can do it in 3 days, in what time can 1 man or 1 woman do it ?

Since 1 man and 2 women do $\frac{1}{8}$ of it in 1 day
$\therefore \quad 2$ men and 4 women do $\frac{1}{4}$ "
But 3 men and 4 women do
$\therefore 1$ man does $\frac{1}{3}-\frac{1}{4}$, or $\frac{1}{12}$
$\therefore 1$ man will do it in 12 days.
Now 1 man and 2 women do $\frac{1}{8}$ of it in 1 day
$\therefore 2$ women do $\frac{1}{8}-\frac{1}{12}$, or $\frac{1}{2 \pi}$
$\therefore 1$ woman will do it in 48 days.
22. If 3 men and 2 boys do a piece of work in 8 days, and 3 men and 7 boys can do it in 6 days, in what time can 1 man or 1 boy do it?
23. If 2 men and 5 boys can do a piece of work in 20 days, and 1 man and 8 boys can do it in 18 days, in what time can 1 man or 1 boy do it?
24. If 7 men and $\xi$ women can do a piece of work in 23 days, and 3 men and 8 women can do it in $3 \frac{11}{43}$ days; in what time can 1 man or 1 woman do the work?
25. 8 women and 2 boys can do a work in $6 \frac{2}{3}$ dayss, and 2 women and three boys can do it in $7_{1} \frac{1}{7}$ days; in what time can 1 woman or 1 boy do it?
26. A cistern is filled by 2 pipes in 8 and 10 hours respectively; in what time will they fill it when they both run at the same time?

They fill $\frac{1}{8}+\frac{1}{10}$ of the vessel in 1 hr .
$\therefore \quad$ " $\frac{5+4}{40}$, or $\frac{9}{40}$
$\therefore \quad$ " $\frac{1}{40}$ in $\frac{1}{8} \mathrm{hr}$.
$\therefore$ they fill the vessel in $\frac{40}{8}$ or $4 \frac{4}{9} \mathrm{hr}$.
27. A vessel is filled by 3 taps, running separately, in 60,75 , and 90 minutes respectively; in what time will they fill it when they all run at the same time?
28. Two pipes running together can empty a cistern in 8 hours, and one by itself can do it in 12 hours; in what time can the other empty it?
29. Two pipes running together can empty a vessel in 50 minutes; one of them can empty $\frac{2}{8}$ of the vessel in 40 minn $r$; in what time can the other empty $\frac{1}{3}$ of it
80. A cistern is flled by two pipes, $A$ and $\bar{B}$, in 20 and 24 minutes respectively, and is emptied by a tap, $C$, in 30 minutes; in what time will it be filled by all running together?
31. A bath is filled by a pipe in 60 minutes; it is emptied by a waste pipe in 40 minutes; in what time will the bath be emptied if both pipes are opened at once?

One pipe empties $\frac{1}{40}$ of vessel in 1 minute.
The other fills $\frac{1}{80}$ of vessel in 1 minute.
$\therefore$ when both are running ( $\frac{1}{40}-\frac{1}{80}$ ), or $\frac{1}{120}$ of the vessel is emptied in 1 minute.
$\therefore$ the vessel is emptied in 120 minutes.
82. A vessel can be filled by 2 taps running separately in 80 and 36 minutes respectively, and emptied by a third in 15 min . ; if the vessel is full and all 3 taps running at once, in what time will it be emptied ?
33. A bath can be anlled by two taps running separately in 20 and 30 minutes respectively, and emptied by two others in 24 and 18 min . respectively; if the bath is full and all four taps opened, in what time will the bath be emptied?
84. A gave to James $\frac{1}{3}$ of his money and to John ${ }^{5}$ of it, and had $\$ 2.10$ left. How much had he at first? He gave away $\frac{1}{3}+\frac{5}{18}$ or $\frac{11}{1}$ of his money. He had left $\frac{18}{18}-\frac{1}{18}$, or $\frac{7}{18}$
$\therefore \frac{7}{18}$ of his money, $=\$ 2.10$;

$$
\frac{1}{18} \quad 6 \quad=\$ \frac{210}{7} ;
$$

$$
\frac{18}{18}, \text { or his money }=\frac{18 \times 2.10}{7}
$$

$$
=\$ 5.40
$$

85. A father willed to his eldest son $\frac{2}{6}$ of his property; to his second son $\frac{2}{7}$ of it, and to his youngest son the rest amounting to $\$ 7238$. What was the property worth?
86. A post is $\frac{1}{8}$ in the earth, $\frac{3}{7}$ in the water, and 13 feet above the water. Whatis the length of the post?
87. A man devotes $\cdot 12$ of his income to charity, 25 for educating his children, 45 for household expences, and saves the remainder, which is $\$ 284.76$. What is his income?
88. A ship whose cargo was worth $\$ 25000$ being disabled, $45 \frac{1}{2}$ of the whole cargo was thrown overhoard. What would a merchant lose who owned -25 of the cargo ?
89. A laborer in one week dug 5 rods more than $\frac{1}{2}$ the length of a ditch, and the next week he dug the remain. ing 20 rods; how long was the ditch ?

Length of ditoh dug first week $=\frac{1}{2}$ ditch +5 rods;
$\therefore$ Length remaining $=\frac{1}{2}$ ditch less 5 rods;
$\therefore \frac{1}{2}$ length of ditch less 5 rods $=20$ rods;

$$
\begin{aligned}
\therefore \frac{1}{2} \text { length of ditch } & =20 \mathrm{rods}+5 \text { rods } \\
& =25 \text { rods } ;
\end{aligned}
$$

$\therefore$ length of ditch $=\mathbf{5 0}$ rods.
40. A man invested $\$ 300$ more than $\frac{2}{8}$ of his money in a house and $\$ 500$ more than $\frac{4}{3}$ of the remainder in a lot and had now $\$ 900$ left. How much was he worth ?
41. If 10 men can chop 90 cords of wood in 8 days, how many cords can be chopped by 20 men in 4 days? Cords ohopped by 10 men in 8 days $=90$ cords ;

| $\omega$ | 1 man " 8 days $=\frac{90}{10}=9$ cords $;$ |
| :--- | :--- |
| $\omega$ | 1 man 1 day $=\frac{9}{8} \mathrm{crds} ;$ |
| $\omega$ | 20 men " 1 day $=\frac{20 \times 9}{8}=\frac{45}{2}$ cords ; |
| $\omega$ | 20 men " 4 days $=\frac{4 \times 45}{2}=90$ cords. |

Nore.-When the pupil has become familiar with the unitary system, and thoroughly understands the reason of each step, the process may be abridged by leaving out the steps in italios.
42. If 8 men build 33 ft . of wall in 11 days, in how many days will 12 men build 36 feet?
43. If 36 men earn $\$ 324$ in 18 days, how much will 42 men earn in 87 days ?
44. How many days will it take 15 men to cut 810 cords of wood, working 9 hours a day, if 18 men can cut 364 cords in 14 days, working 12 hours a day ?
45. It costs a family of 5 persons $\$ 135$ for 6 weeks' board, how much will it cost a family of 7 persons at the same rate for 3 weeks?
46. If 12 men can dig a ditch 16 rods long in 8 days, in how many days can 24 men dig a ditch of the same depth and width, 32 rods in length 1
Time in which 12 men will dig 16 rods $=8$ days;

$$
\begin{aligned}
& \text { 4 } 1 \text { man " } 1 \text { rod }=\frac{12 \times 8}{16} \text { days ; } \\
& \text { の } 24 \text { men ". } 32 \mathrm{rods}=\frac{82 \times 12 \times 8}{24 \times 18} \text { days } \\
& =8 \text { day. }
\end{aligned}
$$

61. A grocer bought a quantity of stgar for $\$ 115$; for what must he sell it to gain 18 per cent. ?
62. A grocer sells a quantity of sugar for $\$ 324$, and thereby loses 10 per cent.; what did the sugar cost?

That which sold for $\$ 90$ cost $\$ 100$;

| " | $\$ 1$ | $" \$ \frac{100}{90}$ |
| :--- | :--- | :--- |
| c | $\$ 324$ | " $\$ \frac{324 \times 100}{90}$ |
|  | $=\$ 360$. |  |

68. A man sells a piece of cloth for $\$ 52.67$ and thereby gains 15 per cent.; what was the cost of the cloth?
69. Sold salt at $\$ 1.37 \frac{3}{4}$ per bushel, which was 5 per cent. less than cost; what was the cost?
70. Divide $\$ 200$ between $A$ and $B$, so that for every $\$ 3$ that A. gets, $B$ shall get $\$ 2$.

Sum of shares $=\$ 3+\$ 2=\$ 5$.
A's share of $\$ 5=\$ 3$;

$$
\begin{array}{ll}
* & \$ 1=\$ 8 \\
& \$ 200=\$ \$^{200 \times 3}=\$ 120 .
\end{array}
$$

B's share may be found in a similar manner, or by simply subtracting $A$ 's share from the whole sum to be divided.

Note.-In the above case the shares of $A$ and $B$ are said to be in the ratio of 3 to 2 , or in the proportion of 3 to 2 .
66. The sum of two numbers is 1260 ; and they are to each other as 57 and 48 ; what are the numbers?
67. Divide $\$ 500$ among three persons, $A, B$, and $C$, so that the three portions may be to each other as the numbers 5,9 and 6 , respectively.
68. A bankrupt has three creditors, to whom the sums due are as the numbers $8,4,5$; if his assets are valued at $\$ 600$, find the sums they will respectively receive.
69. At an election the number of rotes cast was 510 , and $\frac{2}{3}$ of the votes for one candidate equalled $\frac{3}{4}$ of the votes for another ; how many votes were cast for each?

Let $\boldsymbol{A}$ and $B$ be the candidates.
, of $A^{\prime} \mathrm{s}$ votes $=\frac{3}{3}$ of $B$ 's votes;
$\frac{1}{3}{ }^{\frac{1}{3}} \quad=\frac{1}{4}$ of $\frac{3}{4}$ of $B$ 's votes $=\frac{3}{8}$ of $B$ 's votes:
$A ' s$ votes $=\frac{3 \times 3}{8}=\frac{9}{8}$ of $B ' s$ votes.
$t$ of $B^{\prime} s$ voter $+\frac{8}{8}$ of $B^{\prime}$ s votes $=510$.

$$
\begin{aligned}
& B^{\prime} \text { s votes }=\frac{8 \times 8 s^{\prime} 10}{1^{7}}=240 ; \\
& A^{\prime} s " s=510-240=270 .
\end{aligned}
$$

70. $A$ and $B$ have 210 acres of land, and $\frac{3}{4}$ of $A$ 's share equals $\frac{6}{7}$ of $B$ 's ; how many acres has each ?
71. Two neighbours raised 3800 bushels of wheat, and $\frac{5}{3}$ of what one raised equalled $\frac{5}{5}$ of what the other raised; how much did each raise?
72. $A$ and $B$ engage in trade; $A$ furnishes $\$ 6000$ and $B$ $\$ 4000$; they gain $\$ 1200$; what is each one's share of the gain?

The total sum in trade is $\$ 6000+\$ 4000=\$ 10000$; with which they gain $\$ 1200$.
Gain on $\$ 10000=\$ 1200$;

$$
\begin{aligned}
& " \quad \$ 1=\$ \frac{1200}{10000}=\$ \frac{12}{100} ; \\
& " \quad \$ 6000=\$ \frac{6000 \times 12}{100}=\$ 720=A^{\prime} \text { s share. } \\
& " \quad \$ 4000=\$ \frac{4000 \times 12}{100}=\$ 480 B^{\prime} \text { s share. }
\end{aligned}
$$

73. $A, B$ and $C$ buy a house for $\$ 2500 ; A$ pays $\$ 500$; $B \$ 1200 ; C \$ 800$; they rent it for $\$ 300$; what is each one's share of the rent ?
74. A man dying, willed to his son $\$ 6500$, to his widow $\$ 8000$, and to his daughter $\$ 5500$; but his estate amounted to only $\$ 12000$; how much did each get?
75. $A$ and $B$ jointly rented a pasture for $\$ 24 ; A$ put in 36 cows and $B 24$ cows; how much of the rent ought each to pay?
76. $A, B$ and $C$ hired a carriage for $\$ 15.75$, each agreeing to pay in proportion to the number of miles he rode. $A$ rode 90 miles, $B 75$, and $C 60$ miles; what part of the hire ought each to pay?
77. $A$ and $B$ engaged in trade; $A$ put in $\$ 560$ for 6 months, and $B \$ 450$ for 8 months; they gained $\$ 513$; what was each man's share of the gain?
$\$ 540$ for 6 menths $=6 \times \$ 540$ for 1 month.
$\$ 450$ for 8 months $=8 \times \$ 450$
Total sum in trade for 1 month $=\$ 3240+\$ 3600=\$ 6840$
Gain on $\$ 6840=\$ 513$
" $\$ 1=\$ \frac{813}{}=\${ }^{3}{ }^{3}$;
" $\$ 3240=\$ \frac{3240 \times 3}{40}=\$ 243=A^{\prime}$ 's gain.
" $\$ 3600=\$ \frac{3600 \times 8}{40}=\$ 270=B$ 's gain.
78. Three men, $A, B$ and $C$, rented a pasture for \$70.56; $A$ put in 36 cows for 5 months; $B 48$ cows for 4 months; and $O 72$ cows for 3 months. What part of the rent ought each to pay?
79. Bowman, Johnston, and Reed agreed to do a piece of work for $\$ 1600$; Bowman furnished 7 men for 30 days; Johnston, 5 men for 40 days; and Reed 6 men for 32 days. How much should each receive if they paid $\$ 95$ clerk hire?
80. Two persons are in partnership 2 years; $A$ at first put in $\$ 2500$ and $B \$ 3000$; at the end of 9 months $A$ took out $\$ 800$ and $B$ put in $\$ 500$; they lost in 2 years $\$ 3825$; what was each one's share of the loss?
81. What is the Compound Interest of $\$ 400$ for 3 years at 6 per cent.?

Nort.-Compound Interest is interest, not only for the use of the sum borrowed, but also for the use of the interest if it be not paid when it falls due.
Amt. of $\$ 100$ for $1 \mathrm{yr} .=\$ 106$;
" $\$ 1 \quad$ " $=\$ \frac{106}{00}=\$ 1.06$.
" $\$ 1$ for $2 \mathrm{yr} .=\$ 1.06+$ int. of $\$ 1.06$

$$
=\$ 1.06+\frac{6}{100} \times \$ 1.06=\$(1.06)^{2} ;
$$

" $\$ 1$ for $8 \mathrm{yr} .=\$(1.06)^{2}+$ int. of $\$(1.06)^{2}$

$$
=\$(1.06)^{2}+{ }^{6} \times \$(1.06)^{2}=\$(1.06)^{2}
$$

$$
\text { ، } \$ 400 \quad \text { " }=400 \times \$(1.06)^{3}=\$ 476.4064
$$

Amount $=\$ 476.406$
Principal $=400.00$
Compound Interest $=\widetilde{\$ 76.406}$
82. What is the compound interest of $\$ 650$ for 8 years at 6 per cent.
83. Find the amount of $\$ 1000$ for 4 years at 5 per cent.
84. Find the difference between the simple and compound interest of $\$ 350$ for 3 years at 8 per cent.
85. A sum of money put out at simple interest for 2 years at 8 per cent. amounted to $\$ 464$; to what sum would it have amounted had it been lent at compound interest?
86. The true discount on a sum of money for 3 years at 8 per cent. is $\$ 120$; what is the compound interest of the same for the same time.
87. A man deposits in the Savings Bank $\$ 500$, on which the interest at $6 \%$ is to be added to the principal every 6 months; how much money has the man in the bank at the end of two years?

## ANSWERS. <br> Exercise I.-Page 2.

1. $5 ; 5 ; 9$.
2. 1; 1 book; 1 ball.
3. $6,7,3,4,2$ are abstract ; 8 books, 9 men, 5 apples, 1 ceut are concrete. $\quad 4.1$ mile: $1 ; 1$ cent.
4. 3 apples, 7 apples, and 6 apples; 4 boys and 9 boys; 7 , 9 and 8 ; 2 cents and 5 cents; 4 girls and 5 girls.

## Exercise II.-Page 3.

1. 7; 9; 4; 2. $\quad$ 2. $30 ; 84 ; 20 ; 69$.
2. $44 ; 70 ; 96 ; 16.4 .14 ; 12 ; 39 ; 56.5 .48 ; 97 ; 36 ; 60$.
3. Seven; eleven; fifteen; nineteen; fifty-nine; eightyfour ; ninety-six ; ninety-eight.
4. Seventy-one; twelve; twenty-eight; ninety-one; fortyfour ; seventeen; twenty two ; thirty-four.
5. Twenty ; thirty-seven; forty-eight; seventy-six ; ninetynine; sixty-nine; seventy; eighty seven.
6. Fourteen ; thirty-five'; eighty-nine; seventy-eight ; fiftyfour; forty-nine; fifty; thirteen.
7. Ninety; eighty; thirty-nine; twenty-eight; eleven; nineteen; twenty-seven; thirty-one.

## Exercise III.-Page 4.

1. 149 ; 308; 974. 2. 200 ; 420 ; 694.
2. $560 ; 908 ; 444.4 .735 ; 960 ; 406$.
3. 309 ; 687; 572.
4. Two hundred and seven; three huudred and seventy-one: one handred and eighty-five; one handred and ninety; threc hundred and sixty-eight.
5. Five hundred and seventy ; four hundred and seventy-two; eight hundred and seven; nine hundred and nine; nine handred and ninety.
6. Three hundred and sixty-eight ; five hundred and eightyfour; 'seven hundred and sisty; three hundred and twentyone; nine hundred and ninety-nine.
7. Three hundred and ninety-four; seven hundred and eighty-six; four hundred and seventy-five; seven hundred and eighty-two ; seven hundred.
8. Five hundred and six; three hundred; four hundred and seven; seven handred and forty; three handred and ninety-peven.

## Exercise IV.-Page 5.

1. $6006 ; 4300 ; 9080$.
2. 3700 ; 7906 ; 3084.
3. $64009 ; 807068$; 700316.
4. 4030097 ; $809007039 ; 586000007$ :
5. 8000000000 ; 64007000024 ; 4004000004.
6. 408003009 ; $74000074004 ; 500000000500$.
7. $80070000000 ; 800000008 ; 300000300090$.
8. $57700000080 ; 11000011 ; 19000014000$.
9. 7000000000070; 400000001 ; 600600000000600 .
10. 99000000000008 ; 700070007000 ; 16016000000016.
11. Seven thousand and seventy-seven; eighty-five thousand and seventy-nine; fifty-six thousand nine hundred and fifty; four hundred and seventy-three thousand, six hundred and twenty-eight.
12. Fifty-six thousand four hundred and eighteen; seven hundred and eighty-four thousand and six ; four handred thousand five haudred and seven; three hundred and sixty thousand and four.
13. Three hundred thousaud and seventy-one; nine handred and one thousand and seven: seven hundred and twenty thousand and nine; one hundred and eighty-two thousand and ten.
14. Three millions one hundred and forty thousand and six; fifty millions and six hundred; three billions six hundred millions ten thousand and seventy.
15. Fifty-one billions six hundred and thirty-six millions two hundred and seven thousand six hundred and forty; serenty billions and one hundred; nine hundred and twenty billions seventy milllons seventy thousand and seventy.

## Exercise $\nabla$. -Page 6.

1. XIX ; XXIV ; XLIX; LXXXIV ; XCIX.
2. CLXXXVII; CCVIII; DCCLX XXI; CMLXII ; CMXCIX;
3. MCCCI; MCCCXC; MDCLXXXIV; MDCCCXV.

MDCCCLXXVII1.
4. $44 ; 69 ; 94 ; 71$.
6. $99 ; 129 ; 177$.
6. 555 ; 1604 ; 1819 ; 1030.

Exercise VI.-Page 10.

1. 46 horses.
2. 98 boys.
3. 39 girls.
4. 978. 
1. 956 .
2. 898. 
1. 956. 

g. 979.
13. 898.
17. 9879.
10. 697.
14. 879.
21. 87988.
25. 768989.
18. 8989.
22. 88998.
7. 889.
8. 879.
26. 789689.
11. 798.
12. 998.
15.889.
16. 8589.
19. 9989.
20. 98878.
23. 79988.
24. 797898.

## Exercise VII.-Page 11.

1. 79 cents.
2. 796 dollars.
3. 878 bales.
4. 899898 persons.
5. 88 trees.
6. 968 acros.
7. 989 miles.
8. 969 yards.
9. 8989 dollars.
10. 97989 dollars.
11. 113 dollars.
12. 78 cents.
13. 152 boys.
14. 145 girls.
15. 146. 
1. 247. 
1. 213. 
1. 1954. 
1. 
2. 161. 
1. 217. 
1. 1931. 
1. 1357. 
1. 1915. 
1. 2704. 
1. 1656. 
1. 1951. 
1. 1759. 
1. 1842. 
1. 2141. 
1. 23878. 
1. 1976. 
1. 16954. 
1. 14978. 
1. 15113. 24. 18294. 
1. 24459. 
1. 31405. 
1. 29377
2. 16046. 
1. 22825. 
1. 29165. 
1. 256648. 
1. 21232. 
1. 166581. 
1. 338306. 
1. 2033781. 
1. 226871. 
1. 25879. 
1. 27265. 
1. 199859286
2. 24692. 
1. 238390. 
1. 246818. 
1. 24447. 
1. 23378. 
1. 103618. 51. 41121. 

Exercise IX.-Page 14.

1. 222 dollars.
2. 1661 acres.
3. 120 days.
4. 1061 miles.
5. 936 pounds.
6. 7428 bushelb
7. 3441 acres.
8. 633 dollars.
9. 2104 pages.
10. 2237 dollars.
11. 1173 dollars.
12. B, 601 dollars; C, 1066 dollars; 2132 dollars.

Exercise X.-Page 18.

| 1. 813. | 2. 241. | 3. 251. | 4. 402. |
| :---: | :---: | :---: | :---: |
| 5. 644. | 6. 464. | 7. 143. | 8. 305. |
| 9. 344. | 10. 304. | 11. 733. | 12. 530. |
| 13. 4442. | 14. 5022. | 15. 2223. | 16. 2001. |
| 17. 2530. | 18. 4422. | 19. 5512. | 20. 2734. |
| 21. 5024. | 22. 6257. | 23. 1361. | 24. 4623. |
| 25. 423. | 26. 60224. | 27. 36275. | 28. 31216. |
| 29. 5082. | 30. 43262. | 31. 36425. | 32. 35137. |
| 33. 66243. | 34. 75331. | 35. 61161. | 36. 40663. |
| 37. 260265. | 38. 64153. | 39. 35422. | 40. 77443. |
| 41. 161116. | 42. 741551. | 43. 21353. | 44. 44516. |
| 45. 57234. | 46. 364. | 47. 233. | 48. 228. |
| 49.322. | 50. 432. | 51. 2533. | 52. 1243. |
| 53. 6216. | 54. 83136. | 55. 56454. |  |

Exercise XI.-Page 19.

1. 43 girls.
2. 44 cents.
3. 16 doilars.
4. 34 runs.
5. 44 questions.
6. 43 dollars.
7. 33 dollars.
8. 2112 dollars.
9. 14442 dollars.

## Exercise XII.—Page 21.

| 1. 325. | 2, 373. | 3. 262. | 4. 293. |
| :---: | :---: | :---: | :---: |
| E. 255. | 6. 144. | 7. 184. | 8. 256. |
| 9. 263. | 10. 286. | 11. 362. | 12. 309. |
| 13. 168. | 14. 365. | 15. 266. | 16. 169. |
| 17. 69. | 18. C8. | 19. 458. | 20. 178. |
| 21. 298. | 22. 175. | 23. 197. | 24. 118. |
| 25. 339. | 26. 468. | 27. 177. | 28. 497. |
| 29. 479. | 30. 293. | 31. 1497. | 32. 2858. |
| 33. 4188. | 34. 948. | 35. 1933. | 36. 2919. |
| 37. 4944. | 38. 2857. | 32. 5339. | 40. 1299. |
| 41. 1359. | 42. 5247. | 43. 2279. | 44. 5263. |
| 45. 3784. | 46. 5682. | 47. 4469. | 48. 1789. |
| 49. 11844. | 50. 19528. | 61. 52888. | 52. 35499 |
| 53. 49289. | 54. 25012. |  |  |

Exercise XIII.-Page 22.

1. 8 dollars.
2. 77 yards.
3. 560 dollars.
4. 1803. 
1. 3251. 
1. 344 cents.
2. 37 quarts.
3. 175 dollars. 9. 506 dollars. 10. 375 acres; 12021 dollars.

Exercise XIV.-Page 22.

1. 177. 
1. 739. 
1. 1811. 
1. 691. 
1. 2262. 
1. 520. 
1. 2152. 
1. 22326. 
1. 77865. 
1. 3598. 

Exercise XV.-Page 23.

1. 357 dollars.
2. Lost 632 dollars.
3. 853288. 
1. 10534. 
1. 171 dollars.
2. 956. 
1. 814 feet.
2. 6628. 
1. John 28, James 32.
2. 41265. 
1. 5211 and 3553.

Exercise XVI.—Page 27.
$\begin{array}{llll}\text { 1. } 14864 . & \text { 2. } 16864 . & \text { 3. } 216936 & \text { 4. } 368492 .\end{array}$
5. 195 boys.
2. 16864 .
3. 216936
9. 2106 girls.
6. 282 cents.
7. 959 cows.
8. 1488 apples.
13. 23526.
10. 1890.
11. 3360 .
12. 3070.
17. 53838.
1..
15. 43710.
16. 78112.
21. 153132.
18.
19. 72028.
20. 661672 .
25. 53936.
29. 428215.
2. 630855.
23. 352794.
24. 646857.
26. 54360.
27. 432481.
28. 364704.
33. 6283784.
30. 1023024.
31. 3417355.
32. 6044346.
37. 10860916. 38. 9091656.
35. 7865490.
36. 9162527.

Exercise XVII.--Page 27.

1. 16280 cents.
2. 185430 cents.
3. 2709 dollara
4. 15215 dollars.
5. 336 sheep ; 392 dollars.
6. 94 pounds; 2610 cents ; 752 cents; 658 eents.
7. 3402 dollars ; 224 dollars; 3626 dollars ; 2237 dollars.
8. 1320 paragraphs; 11880 lines; 95040 words; 475200 letters.
9. 296 cents; 414 cents; 710 cents; 118 cents.
10. 1096 cents ; 2214 cents ; 3310 cents; 1118 cents.

Exercise XVIII.-Page 29.

1. 11950. 
1. 66738. 
1. 40992. 
1. 118377. 
1. 189945. 
1. 482544. 
1. 340488. 
1. 62550. 
1. 240896. 
1. 134010. 
1. 98560 yards.
2. 183576. 
1. 1348560 .
2. 459 days.
3. 68520 feet.
4. 8496 cents.
5. 19845 dollars.
6. 3000 dollars.
7. 8505 dollars.

Exercise XIX.-Page 30.

| 1. 472440. | 2. 300720. | 3. 236196. |
| :---: | :---: | :---: |
| 4. 562650. | 5. 724885. | 6. 6608822. |
| 7. 6586169. | 8. 6509916. | 9. 1194872. |
| 10. 4127874. | 11. 9781440 . | 12. 11961586. |
| 13. 14821755. | 14. 25581580. | 15. 23120856. |
| 16. 81362385. | 17. 29455710. | 18. 31259060. |
| 19. 70132632. | 20. 14069499. | 21. 41316048. |
| 22. 26514000. | 23. 42741832. | 24. 16765686. |
| 25. 66093951. | 26. 217702278. | 27. 163588743. |
| 28. 307551216. | 29. 276010344. | 30. 114297351. |
| 31. 348112465. | 32. 283036132. | 33. 671374392. |
| 84. 2139927997. | 35. 1627916724. | 36. 1244124564 |
| 87. 341614192. | 38. 3481804952. | 39. 4141417504 |

Exercise XX.-Page 31.

1. 127405. 
1. 6317608. 
1. 6825456. 
1. 1960452. 
1. 63366216. 
1. 6749472 .
2. 8214206. 
1. 25996104. 
1. 80071992 . 10. 738110274.

Exercise XXI.-Page 31.

1. 445300 .
2. 592900 .
3. 60744600. 
1. 11887500. 
1. 243000 .
2. 258000 .
3. 627000000 .
4. 11214000. 
1. 4096000 .
2. 422500 .

Exercise XXI.-Page 31.

1. 454560 sheets.
2. 1653 yards.
3. 263952 apples.
4. 103662 yaitds.
5. 1246420 dollars,
6. 7080320 dollara
7. 89784 yards.
8. 195559 yards.
9. 3915648 pounds.
10. 915750 pages.
11. 44100 dollaז̃.
12. 6125 dollars.
13. 1228275 dollars.
14. 12. 12180 ucllate.
1. 3926000 dollars. 15. 262800 barrels.
2. 277107850 dollars 18. 372480 hills. 20. 7344 miles.

Exercise. XXIII-Page 32.

1. 608 dollars.
2. 162764 men.
3. 530229 gal.
4. 2773 dollars.
5. 12652 cents.
6. 7455 dollars ; 9940 dollars. 7. The horses ; 2532 dollars.
7. A's 706800 ; B's 1126125 letters.
8. 18750 cents.
9. 116550 cents.
10. 457047. 
1. 944 days.
2. 1441 dollars. 14. House, 2800 dollars; Farm, 2975 dollars. 15. Loss 254 dollars.
3. Gain 3100 dollars 17. 17582 dollars. 18. 9000 dollars.
4. 8110 dollars 20. 10690 dollars.

Exercise XXIV.-Page 39.

| 1. 18. | 2. 29. | 3. 27. | 4. 46. | 5. 48. | 6. 192. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 7. 105. | 8. 241. | 9. 291. | 10. 325. | 11. 213. | 12. 191. |
| 13. 233. | 14. 144. | 15. 187. | 16. 147. | 17. 170. | 18. 195. |
| 19. 149. | 20. 167. | 21. 122. | 22.141. | 23. 154. | 24. 162. |
| 25. 139. | 26. 112. | 27. 114. | 28. 119. | 29. 138. | 30. 137. |
| 31. 112. | 32. 117. | 33. 118. | 34. 122. | 35. 124. | 36. 52. |
| 37. 64. | 38. 96. | 39. 82. | 40. 74. |  |  |

## Exercise XXV.-Page 39.

| 1. 228. | 2. 368. | 3. 274. | 4. 187. | 5. 269. |
| :---: | :---: | :---: | :---: | :---: |
| 6. 245. | 7. 272. | 8. 174. | 9. 138. | 10. 246. |
| 11. 223. | 12. 171. | 13. 182. | 14. 255. | 15. 275. |
| 16. 128. | 17. 156. | 18. 183. | 19. 144. | 20. 206. |
| 21. 184. | 22. 204. | 23. 243. | 24152. | 25. 109. |
| 26. 123. | 27. 147. | 28. 129. | 29. 157. | 30. 168. |
| 31. 163. | 32. 187. | 33. 156. | 34.153. | 35. 176. |
| 36. 139. | 37. 108. | 38. 109. | 39. 129. | 40. 144. |
| 41. 246. | 42. 556. | 43. 419. | 44. 609. | 45. 1223. |
| 46. 367. | 47. 676. | 48. 1208. | 49. 1337. | 50. 1410. |
| 51. 907. | 52. 457. | 53. 947. | 54. 3669. | 55. 13879. |
| 56. 988. | 57. 442. | 58. 285. | 59. 7032. | - 60. 7484. |

Fxercise XXVI.-Page 40.

1. 59 oranges.
2. 173 days' work.
3. 918 pounds.
4. 231 yards.
5. 96 rods.
6. 91 cents.
7. 15 busheis.
8. 123. 
1. 6052 bushels.
2. 8 cords.

Exercise XXVII.-Page 41.

| 1. $2177 \frac{1}{3}$. | 2. 1248\%. | 3. 9606. |
| :---: | :---: | :---: |
| 4. 1640 年. | 5. 12317 1. | 6. 690491. |
| 7. 420061 ¢ | 8. 572004 웅. | 9. 777070 ㄹ. |
| 10.729584 ${ }^{\text {¹0 }}$ - | 11. 1398260. | 12. 7400061. |
| 13. 823956. | 14. 6273804\%. | 15. 4238753 T . |
| 16. 420560. | 17. 20073842. | 18. 37037048. |
| 19.8470853 ${ }^{\text {? }}$ - | 20. 7298426. | 21. 7480093. |
| 22. 2730956 ti. | 23. $88443261 \frac{1}{2}$. | 24. 92506025. |
| 25.4560387 ${ }^{\text {18, }}$ | 26. 37376008. |  |

## Hxercise XXVII．－－Page 41.

1． 432 barrels．
4．11 dollars．
8．130 pounds．
11． 252.
14． 548 brioks．

2． 1256 pounds．
3． 6226 dollars．
5． 8 dollars．
9． 125 d dollars．
12． $689 \frac{3}{\text { a }}$ acres．
6． 2423 minuter．
10． 52$\}$ weeks．
13． 157457 pounds．

I7 ercise XXIX．－Page 44.

1． $24 \frac{3}{3} 9$ ．
4． $74 \frac{18}{\frac{1}{1}}$ ．
7． 53114 ．
10． 49 ．${ }^{\circ}{ }^{\circ} \mathrm{T}$ ．
13． $375 \frac{17}{175}$ ．
16． 2831.
19． 3746.
22．9710 ${ }^{2140}{ }^{\circ}$ ．
25． 3180.
28． 7277 P＊＊ํㅜㄱ．

2． $8 \frac{1}{19}$ ．
3． $18 \frac{1}{6}$ ．
5． 39 it？
8． $945 \frac{2}{7}$ ？ 6.
11． $231 \frac{3}{23}$ ．
14． 2259 룡․

20．2025 ${ }^{\text {P7 }}$ T．
23． 4321.
26． 3615.
29．${ }^{5} 567$.

6． $588 \frac{1}{6}$ ．
9． 554 ini
12． $498 \frac{1}{6}$ h．
15． 5050 \％
18． $620010^{15}$

24． 4671.
27． 1142.
30． 50444.

Exercise XXX．－Page 44.
1． 43 days．
2． 38 days．
3． 1090 ieet．
4． 32 dollars．
5． 129 years．
6． 123 dohars．
7． 46 dollars．
9． 343 y miles．

10． 2075 barrels．
Fxercise XXXI．－Page 45.
1． $17344^{\circ}$ ．
2． 1366 年年．
3．1549\％t．
4．307혼ㅇ․
5． 24692523 ．
6． 149147 2 $_{8}^{8}$ ．
7．34931．
11． 2570.
8． 800 \％．
10．42365\％．

Exercise XXXII．－Page 46.
1． $24{ }_{8}^{8} 0$ ．
2． $127 \frac{2}{8}$ ？
3． 12 数等．
4． 326 \％$\%$－
5． $804{ }^{\circ} \%$ ．
6． $1183 \frac{8}{8}$ ．

8．$E \frac{3}{8} \frac{8}{8} 8 \frac{8}{8}$ ．

10． 153 8ํㅜำ
11． $673_{1 \frac{1}{3} \frac{7}{7} 75}^{8}$ ．

Exercise XXXIII．－Page 46.

1． 108 yards．
2． 65 hours．
3． 123 pounds．
4． 30 pounds．
5． 42 bushels．
6． 235 dollars．
7． 1378 quarters．
8． 237 bushels．
9． 43 bushels．
10． 38 miles．
Exercise XXXIV．－Page 47.
1． 8814.
2． 129
3． 233289.
4． 348.
5． 186.
6． 272.
7． 10005100 ．
8． 19052.
9． 194 and 86．10． 784623.

Exercise XXXV．－Page 48.
1． 367 acres．
2． 2310 dollars．
3． 845 dollars．
4． 15 weeks．
5． 44 dollars．
6． 56 cents．
7． 1650 barrels．
8． 24 months．
9． 551 dollars．

| 10. 1210 dollars. | 11. 41600 o. ft. | 12. 217 sheep, |
| :---: | :---: | :---: |
| 13. 520 dollars. | 14. 30 hours. | 15. 240 cents. |
| 16. 54 cents. | 17. 56 dollars | 18. 96 dollars. |
| 19. 100 dollars. | 20. 40 certs. | 21. 12 dollars. |
| 22. 6880 dollars. | 23. 23725 days. | 24. 7056 pounds. |
| 25. 5640 yards. | 26. 365 acres. | 28. 31250 dollars |
| 29. 954 dollars. | 30. 1971 bushels. | 31. 15 days. |
| 32. 12 days. | 33. 32 days. | 34. 361 days. |
| 35. 50 days. | 36. 90 days. | 37. 48 days. |
| 38. 6 days. | 39. 10 days. | 40. 119 days. |
| 41. 28 men . | 42. 84 men . | 43. 21 men . |
| 44. 108 men . | 45. 25 men . | 46. 114 men. |
| 47. 56 men . | 48. 72 men . | 49. 150 men . |

## Examination Papers:-Page 51. <br> I. <br> 2. 488979 . <br> 3. 944813 . <br> 4. 7706307420 . <br> 5. 1116 dollars. II.

2. 29900000 . Twenty-nine millions, nine hundred thousand.
3. 846055 .
4. 2699,329 ; $\overline{\text { DCCCLXXXVIIICMLXXI. }}$
5. 16 bushels.

## III.

3. 64365636568 .
4. 580 acres ; 61 dollars.

> IV.
4. 228 dollars.
6. 608 sheep.
V.
3. 86.
4. 86 .
5. 53 dollars. VI.
a. 3571 dollars.
3. 112.
4. $\mathbf{1 8 0}$ acres ; $\mathbf{3 6}$ dollars.
5. 24 days.
VII.
2. 40831 dollars. 3. 663 miles. 4. 247. 5. 6525 dollars. VIII.

1. 4700 dollars.
2. 973. 
1. 31 dollars.
2. 201 cents.
3. 964 miles; 1181 miles.

## Exercise XXXVIU.-Page 58 ,

1. $\$ 1163.55$
2. \$1864.07.
3. $\$ 3220.65$.
4. $\$ 1624.90$.
5. $\$ 99.05$
6. $\$ 82.28$.
7. $\$ 5232.74$
8. $\$ 22$.

Exercise EXXIX .-Page 59.

1. $\mathbf{5 9 4 . 5 ̄}$.
2. $\overline{\text { § }} \overline{5} 8.75$.
3. $\begin{gathered}\text { 4 } \\ 3\end{gathered} \mathbf{1 9}$.
4. ${ }^{\text {T }} 592.61$.
5. $\$ 5170.64$.
6. \$4.08.
7. $\$ 23.79$.
8. $\$ 261.07$.
9. $\$ 7915.80$.
10. 850.37.
11. $\$ 1790.68$.
12. \%48.45.

Fxercise XL.-Page 60.

1. $\$ 391.85$.
2. \$1482.96.
3. $\$ 926.25$.
4. 897670 .
5. $\$ 6562.50$.
6. $\$ 3522.75$
7. $\$ 157.50$.
8. $\$ 27.75$.
9. 83364.20 .
10. $\$ 16.80$.
11. $\$ 247$.
12. $\$ 169$.
13. $\$ 1794$.
14. $\$ 722.16$.
15. $\$ 360$.
16. \$3.51.
17. \$261.25.
18. $\$ 425.25$.

Exercise XLI.-Page 62.

1. $\$ 1272$.
2. \$21.37.
3. $\$ 18.17$.
4. $\$ 26.34$.
5. \$7.89.
6. $\$ 60.50 \frac{2}{2} \frac{1}{5}$.
7. $\$ 10.40$.
8. 73 sheep.
9. \$2.22.
10. 6. 
1. 365 days.
2. 16 pieces.

## Exercise XLII.-Page 64.

1. $\$ 32.20$.
2. $\$ 1196$.
3. $\$ 4.35$.
4. \$27.76.
5. \$47.02.
6. $\$ 889.77$.
7. \$14.24.
8. $\$ 771.51$
9. \$18.78. 10. \$3.31.

## Examination Papers.-Page 65.

I.
2. 70 cents.
3. $\$ 5.15$.
4. 100 .
5. 15 times more.
II.
2. $\$ 414.80$
3. $\$ 281.52$.
4. 50 tong.
5. $\$ 1.10$.
2. 45 yards.
8. 85 votes.
4. $\$ 1191.75$.
5. 1760 . IV.

1. 476 yards ; 30 cents.
2. 400 bushels.
3. 1560 pairs.
4. 100 days.
5. $1100 ; 430$.

Exercise XLIII.-Page 68.

| 1. $2,2,2,2,3$. | 2. $2,2,2,3,3$. | 3. 3, |
| :---: | :---: | :---: |
| 4. $2,2,3,3,3$. | 5. 5, 5, 7. | 6. $2,3,3,3,5$. |
| 7. 2, 2, 2, 2, 2, 5 . | 8. $5,5,13$. | 9. 3, 11, 13. |
| 10. 2, 2, 3, 23. |  | 11. $2,2,2,2,2,5,5$. |
| 12. 2, 2, 3, 3, 5. | 13. No prime factors. | 14. 2, 2, 2, 2, 3, 7 . |
| 15. 3, 3, 5, 19. | 16. $3,5,7,11$. | 17. 2 and 5 . |
| 18.3. | 19. 7 and 3. | 20. 2, 2, 2, 3 and 5. |

Exercise XLIV.-Page 68.

1. 2. 
1. 2. 
1. 12. 
1. 18. 
1. 30 .
2. 72. 
1. 20 yards.
2. 72 bushels.
3. \$22.
4. 75 yards.
5. \$2.
6. 1440. 

Ezercise XLV.-Page 70.

1. 5. 
1. 4. 
1. 8 .
2. 14. 
1. 10 .
2. 42. 
1. 24. 
1. 11. 
1. 75. 
1. 144. 
1. 8 feet. 12. 21 feet. 13. 16 feet. 14. 8 quarts. 15. 45 pearm. 16. 3,11 , or 33 pupils in each section.

## Exercise XLVI.-Page 71.

1. 23. 
1. 37. 
1. 41. 
1. 56. 
1. 45. 
1. 61 .
2. 42. 
1. 11. 
1. 813. 
1. 630. 
1. Prime.
2. 21. 
1. 184 lbs.
2. 7 and 12.

Exercise XLVII.-Page 73.

1. 30. 
1. 60. 
1. 36. 
1. 150 .
2. 360 .
3. 180. 
1. 360 .
2. 770 .
3. 2520. 
1. 1512. 
1. 1680. 
1. 16800. 
1. 1800 .
2. 720720. 
1. 50702925. 
1. 173. 
1. $\$ 2100$.
2. 360 bushels.
3. 240 cents.
4. 84 bushels.
5. 120 days.

Examination Papers.-Page 74.
I.

1. 611, 707, and 1089 are comp.; 643, 757, and 991 are prime. 2. 8. 3. $\$ 3048$. 4. 643 . 5. 25 acres.
II.
2. 25. 
1. 46. 
1. 1680 marbles.
2. 47400 holes. III.
3. 15, 16, 17, and 18.
4. 900 acres.
5. 9672 rails.
IV.
6. 75 cents.
7. $\$ 1080$.
8. 3600 .
9. 10565999 .
10. 1267994828100 .
$\nabla$.
11. 10206. 
1. 240. 
1. 257. 
1. 5 and 4.

Exercise XLVIII.-Page 80.

| 1. \% | 2. ${ }^{2}{ }^{1}$. | 3. ${ }_{7}$ | 4. 9 |
| :---: | :---: | :---: | :---: |
| 5. ${ }^{1912} 12$. | 6. ${ }^{\circ}$ | 7. ${ }^{13} 1{ }^{\text {a }}$. | 8. $\frac{1400}{17}$. |
| 9. $\frac{1190}{23}$. | 10. $\frac{108}{19}{ }^{\circ}$. | 11. $\frac{1000}{12}$. | 12. $\frac{7741}{98}$. |
| 13. $\frac{36039}{}{ }^{\text {a }}$, | 14. $\frac{71819}{280}$. | 15. $\frac{888477}{178}$. |  |
| 17. $\frac{101715}{101}$ |  |  |  |
|  | Exercise | IX.--Page 80 |  |
| 1. 3 ! | ' 2. 5t. | 3. $6 \frac{9}{}$. | 4. $7{ }^{\text {c }}$ \% |
| 5. 33. | 6. 17. | 7. 12 T ¢ | 8. $65_{17}{ }^{7}$. |
| 9. $16{ }^{8}{ }^{8}{ }^{\text {a }}$ | 10. 13. | 11. 29. | 12. $51 \frac{1}{3}$. |
| 13. 3249 | 14. 1003:. | 15. 5154. | 16.6764 |
| 17. 369it. | 18. 522 ¢ำ |  | 16. |

Ezercise L．－Page 81.
1．
2．$\frac{2}{3}$ ．
3．$\frac{z}{8}$ ．
4． 2.
5．$\frac{8}{8}$ ．
6．$\%$ ．
7．
13． 11.
8．io
9．$\frac{1}{8}$ ．
14．$\frac{3}{4}$ ．
15．$\frac{1}{8} \frac{2}{2} \frac{2}{8}$ ．
10．$\frac{1}{1} \frac{1}{2}$ ．
11．各务．
12．${ }^{5}$
19． $\mathrm{T}^{7}$ ．
20． $\mathrm{I}^{4}$ ．
21． $1 \frac{1}{1}$ ．
16．$\frac{8}{4} \frac{1}{2}$ f．
17．$\frac{8}{7}$－
18．$\frac{4}{4}$
22．$\frac{2}{3}$ ．
23．1f．
24．$\frac{14}{8 \frac{1}{7} \frac{1}{7} \text { ．}}$
Exercise LI．－Page 83.
1． 17.
2． $\mathrm{I}^{2}$－
3． $3^{\frac{1}{18}}$ ．
4． $1 \frac{1}{8} \frac{9}{8}$ ．
5． $2^{n}$ ．
6．$)^{5}$ ．
7．$\frac{1}{2} \frac{0}{1}$ ．
8．．
9．8\％
10．$\frac{1}{8} \frac{9}{8}$ ．
11． 1.
13．$\frac{3}{3}$ ．
14． 3.
15． $2 \frac{1}{8} \frac{9}{8}$ ．
16． $4 \frac{7}{2}$ ．
17． 14.
12．$\frac{8}{82}$ ．

Exercise LII．－Page 83.
1．$\frac{1}{2}$ ．
3.
3．\％
4．Is．
6．$\frac{1}{8}$ ．
1． $12 \frac{1}{2}$ acres．
8．$\$ 8750$ ．

Exercise LIII．－Page 84.


2． $98, \frac{98}{78}$ ．
3．$\frac{85}{95}$ ，$\frac{83}{87}$ ．

6．$\frac{35}{8} \frac{4}{6}, \frac{40}{80}, \frac{78}{8} \%$ ．


Exercise LIV．－Page 85.

1．$\frac{2}{88}, \frac{2}{8} 8, \frac{1}{8} \frac{8}{6}$ ．
2．$\frac{4}{8}$ ，$\frac{2}{8}$ ．$\frac{7}{8}$ ．
5．$\frac{28}{8} \frac{1}{8}, \frac{1}{8} \frac{7}{8}, \frac{27}{3}$ ．
3．$\frac{3}{4} \frac{5}{8}, \frac{38}{8}$ ， 18.
4．$\frac{27}{87}, \frac{21}{81}, \frac{3}{3}$ ．

11． $8^{3}, \frac{20}{8}, \frac{5}{8}$ ．
6．$\frac{48}{8} \frac{4}{8}, \frac{48}{8}$ ，$\frac{8}{8} \frac{5}{8}$ ．
7．$\frac{15}{8}, \frac{8}{8} \frac{5}{8}$ ，홍․․

10．$\frac{30}{10}, \frac{3}{10}, \frac{8}{10}$ ．

13．$\frac{48}{18}, 7 \frac{7}{8}, 1^{2} 8$.

17．$\frac{8}{5} \frac{138}{8}, \frac{1}{5} \frac{18}{78}, \frac{1779}{7} \frac{1}{8}, \frac{1}{x} \frac{98}{7}$ ．
Exercise LV．－Page 85.
1． 5.
2． 34.
3．논ㅇ․
4． 14.
5．$\frac{18}{6}$ ．
6．$\frac{17}{17}$ ．
7．${ }^{8} \frac{8}{4}$ ．
8． $\boldsymbol{x}^{7}$ ．
9．$\frac{18}{\frac{8}{8}}$ ．
10．$\frac{18}{28}$ ；$\frac{1}{8} \frac{1}{8}-$

12．$\frac{8}{8}$ ；${ }^{8}$ ．

15．$\frac{8}{8}$ ；$\frac{5}{8}$ ．

17．$\frac{1}{3}, \frac{1}{2} \frac{8}{6}, \frac{2}{3}$ ，量，$\frac{4}{8}$ ．

3xercise LVI．－Page 87.
1． 3.15.
2． $1 \frac{17}{4} \frac{1}{6}$ ．
3．28．
4． $1 \frac{1}{4}$ ．
b．1星曻
6．$\frac{18}{2} \frac{8}{7}$ ．
7． 2 ？
8．${ }^{\frac{5}{5}}$ ．
9． 2 e＇s
10． 1 Tํㅜㅇ．
11． $3 \frac{8}{8}^{\frac{8}{2}}$ ．
1．2． 17.

Exercise．LVII．－Page 87.
1． $1012 \frac{2}{6}$
2． $10{ }^{7}{ }^{7}$ ．
3． 10 等．

6． $46{ }_{6}^{9}{ }^{8}$ ．
16． $21 \frac{1}{4}$ ．
$\therefore 22$ rigo $^{\circ}$
11． 128 ．
4． 5 多 8.
9． $12 \frac{5}{8}$ ．




Exercise LVIII．－Page 88.
1．हैร•
2．$\frac{17}{8}$ ．
3．$\frac{17}{8}$ 年，
4．$\frac{8}{2}$ ．


7．${ }^{7}$ ．
8．$\frac{78}{8} \frac{8}{8}$ ．
9． $1^{77} \mathrm{~T}$ ．
10．${ }^{7}$ ． Exercise LIX．－Page 89.
1． $1_{3}^{3}$ ？.
2． $1_{10}^{10}$ ．
3． $3_{12}^{2}$ ．
4． $2 \frac{29}{8}$ ？ ．
5． $1_{17}^{7}$ ．
6． 14.
7． $2 \frac{12}{2}$ ．
8． $2 \frac{5}{5}$ 웅．
9． 44.
10． 12 T．
11． $24 \frac{1}{2} \frac{1}{8}$ ．
12． $10 \frac{5}{8}$ ．

Exercise LX．－－Page 89.
1． $18 \frac{1}{2} \frac{5}{6}$ ．
2． $16 \frac{9}{\mathrm{To}}$ gallons．
3．${ }^{5}$ 名．
4． $20 \frac{1}{1}$ yards．
5．$\$ 3 \frac{1}{8}$ ．
6． $101_{\left.1^{2}\right\}}$ acres．
7． $14 \frac{1}{8} \frac{8}{8}$ reams．
8． $34 \frac{1}{2} \frac{7}{\frac{1}{2}}$ pounds．
10．$\$ 38_{1^{1}}{ }^{1}$
11．$\$ 98 \frac{2}{2}$ s．
9． $33{ }_{3}^{1} \frac{1}{6}$ miles．

Exercise LXI．－Page 90.
1．$\$ 383_{1} \frac{1}{2}$ ．
2．$\$ 1$ 亲灵．
3． $49 \mathrm{r}^{7}$ pounds．
4．$\$ 1911^{\frac{1}{3}}$－
5． $106 \frac{3}{4} \frac{1}{4}$ gallons．
6． $8 \frac{8}{\frac{1}{6}}$ ．
7． $145 \frac{1}{17}$ y yards ；$\$ 403 \frac{1}{1 \frac{2}{2}}$ ．
8． $44_{\mathrm{Y} \frac{9}{6}}$ pounds．
9．\＄3．
10． $10 \frac{7}{1} \frac{1}{4}$ gallons．
11．$\$ 177^{\frac{7}{8} 8}$ ．
12． 774 조 acres．
 Exercise LXII．－Page 92.
1． $7 \frac{1}{2}$ ．
2． $6 \frac{1}{5}$ ．
3． 24.
4． $9 \frac{1}{3}$ ．
5． $37 \frac{1}{8}$ ．
6． $71 \frac{1}{2}$ ．
7． 26 ．
8． $10{ }^{2}$ ．
9． 4 롤．
10．$\$ 30$ ．
11．$\$ 13.14$ ．
12．\＄201．
18．$\$ 1.77$.
14．\＄8．75．

Exercise LXIII．－Page 03.
1． 15.
2． 40 ．
3． $35 \frac{5}{8}$ ．
4． 543.
5． 18.
6．${ }^{8} 8$.
7．$\frac{3}{8}$ ．
8．${ }^{\frac{7}{4}}$ ．

14．${ }^{\text {W．}}$ ．
10．$\frac{7}{8}$ ．
11． $1_{1}^{7}$ ．
15．A，\＄2814； B，\＄225；C，\＄303 ${ }^{\frac{3}{4}}$ ；$\$ 810$ ．

Exercise LXIV．－Page 94.
1． 17 \％
2． $49 \frac{1}{3}$ ．
3． 290.
4． 1320.
5． 8789.
6． $61 \frac{1}{2}$ ．
8． $42 \frac{2}{4}$ ceuts． 9.10 acres．10．$\$ 351_{17}^{9}$ ．11．$\$ 67$ 8． 12．$\$ 1667$ 4．13．$\$ 227 \frac{2}{2} \frac{1}{6}$ ．

Exercise LXV．－Page 96.
1．$\frac{1}{2} \cdot$
2．$\frac{1}{8}$ ．
3．${ }^{7} \frac{7}{7}$ ．
4．1t？
5．1\}.
6．$\frac{2}{2}$ 7．${ }^{2}$ ．
8． $8{ }_{1}^{1{ }^{1}}$
9． 23 童
10． 31 acrea．
11．21 cords．12． $3 \frac{1}{6}$ miles． 13 ． $8_{3}^{2}$ ．

Exercise LXVI．－Pago 97.
1． 14 ，
2． 21 ．
3． 34 ？
4． 11 ．
5． 3.
6．$\frac{8}{8}$ ㅇ．
7．1998．
8． 1 ！．
9． $10 \%$ ．
10．${ }^{1845}$
11． 14 ．


Fxercise LXVII．－Page 97.
2． 24 bushels．
3． 14 tons．
4． 27 bushels
5． $24 \%$ weeks．
6． 11 persons．
7． 8 \％
8． 24 weeks．
9． $11 \frac{1}{4}$ bushels．
10．i90 days．
11．$\$ 67 \frac{1}{2}$ ．
12． $10 \frac{1}{2}$ 亲．

Exercise LXV11I．－Page 99.
1． 16.
2 3．
3．$\frac{8}{8} \cdot$
4．$\frac{8}{28}$－
5．1f
6． $4 \frac{1}{5}$ ．
7． 2.
8． 1 g．
9． 2.
10． $2 \frac{3}{4}$ ．
11． $7 \frac{1}{2}$ ．
12． $3 \frac{1}{4}$ ．
13．$\frac{1}{8} \frac{1}{3} \frac{1}{2}$ ．
14． $1_{1}^{73}{ }^{73}$ ．
15． $\mathrm{I}_{1}^{\mathrm{h}}$ ．
16． 2 ？
17． $38 \mathrm{I}^{2} \mathrm{I}$ ．
1816.
19．11．
20． 4$\}$

Exercise LXIX．－－Page 100.
1．$\frac{1}{8}$ ．
2． $3 \frac{1}{8} \frac{8}{9}$ ．
3． 1.
4． 22 个！
6． $3^{\frac{1}{4} 4^{7}}$ ．
6． $14 \frac{2}{3} \frac{8}{8}$ ．
7． 4.
8． 1.
9．$\frac{1}{8} \frac{1}{8}$ ．
10． 1 昜．
11 in．
12． 15.
13． 1818.
14． 1.
15． $2^{2} 1^{3} \delta$ ．
16． 3 每的

Examination Papers．－－Page 101.
11.
3．It
4． 11 ； 就．
5． 24 days，
III．
2．$\frac{1}{3}$ ．
3． 18 bags．
4．$\$ 21000$ ．
6．\＄15．85． IV．

3．$\$ 5.60$ ．
4．Toc large by 1 ．
5．$\$ 33075$ ．
V．
2．$\$ 359.45$ ．
3． 660.80 ．
4． 3.
5． 9 acres．

2． 2.
3．$\$ 1840$ ．
4． 49 acres．
6．$\$ 5187.50$ ， Fxercise LXX．－Page 106.

| 1．${ }^{7}$ | 2． $\mathrm{I}^{8}{ }^{\text {fo}}$ ． | 3．İ\％ | 4． 19880 |
| :---: | :---: | :---: | :---: |
| 5．${ }^{\text {700 }}$ | 6．${ }^{4} 10888$. | 7． 18850 | 8．บ ${ }^{9}{ }^{\circ}{ }^{\circ} 0{ }^{\circ}$ |
|  | 10．${ }^{80005}$ | 11． $10^{4} 0^{2} 700^{7}$ | 12． $10 \frac{8}{88} 0{ }^{\text {d }}$ |
| 13． 1288870. | 14．${ }^{2} 11^{2} 0^{4} 0^{6} / 6$ |  | 16． 8. |
| 17． 71. | 18． 27. | 19． 07. | 20．136． |
| 21． 2.07. | 22． $4 \cdot 16$. | 23．16．126． | 24．126．36\％． |
| 25． 18496. | 26． $3 \cdot 00007$. | 27．16．001．63． |  |

## Exercise LXXI．－Page 106.

1．Nine－teuths．2．Twenty－seven hundredths．8．Three hundred and sixty－eight thousandths．4．Sixty－four thon－ sandths．6．Four，and．thirty one hundredths．6．Seven，and two hundred and sixteen thousandths．7．Three，and thren hundred and fourteen thousandths．8．Five，and eight thou．
sand one hundred und oncty-вeven teu-thousandths. 9. Twenty. one, and three thousand six hundred and one ten-thousandths. 10. Seventeen, and sixty-four ten-thousandths. 11. Eighteen, and eighty-one hundred-thousandths. 12. Twenty, and one thousand four hundred and fifty.eight hundred thousandths. 13. $\cdot 8$; $2 \cdot 07$; $\cdot 009$. 14. $807 \cdot 094$; 3017•0709; 3•001008. 15. 6.0004; $80 \cdot 0000609$; $101 \cdot 01001$.

Exercise LXXII.-Prge 107.

|  | 1. $65 \cdot 046$. | 2. $600 \cdot 7354$. |
| :--- | :--- | :--- |
| 4. $2 \cdot 4397464$. | 5. $101 \cdot 209$. | 3. $4475 \cdot 105045$ |
| 7. $114 \cdot 1377$. | 8. $959 \cdot 0483$. | 6. $10 \cdot 876$. |
| 10. $15156 \cdot 66886$. | 11. $200 \cdot 1211$. | 9. $40 \cdot 52753$. |
| 13. $227 \cdot 5024$ | $14.122 \cdot 625$ yds. | $12.25 \cdot 749445$. |
|  |  |  |

Ezercise LXXIII.--Page 108.

1. $16 \cdot 1524$.
2. $2 \cdot 3806$.
3. $\cdot 43876$.
4.     - 23296. 
1. $1 \cdot 8316$
2. $\cdot 00521$.
3. $2 \cdot 9249$.
4. $\cdot \mathrm{Cl}$.
5. $2 \cdot 5527$.
6. -2318 inches.
7.     - 146 .

Exercise TıXXIV.-Page 109.

1. $15 \cdot 544$.
2. $5 \cdot 4008$.
3. $240 \cdot 37086$.
4. 0273238
5. $9 \cdot 6142$.
6. $803 \cdot 2104$.
7. $2474 \cdot 11$.
8. 000072 .
9. $\cdot 040527$.
10. $334141 \cdot 402$ sq. in. 14.9 .75 pounds.
11. $117 \cdot 04936022 \mathrm{mi} .17$. 728-9271.
12. $168 \cdot 098$.
13. 6322. 
1. $8 \cdot 3416$.
2. 15.799.
3. $173 \cdot 03863$.
4. $36 \cdot 002$ grains.
5. 99. 

$$
-x-0-2
$$

Exercise LXXV.-Page 111.

|  | Exercise |  |  |
| :---: | :---: | :---: | :---: |
| 1. 3-07. | 2. $50 \cdot 615625$. | 3. 800 . |  |
| 5. 1240. | 6. 00075 |  |  |
| 9. 20200. | 10. 22600. | 11. $\cdot 082$. |  |
|  | Ezercise LXXYI.-Page 112. |  |  |
| 1. $\cdot 1875$. | 2. 75. | 3. 625. | 4. 2225. |
| 5. 15625. | 6. 025. | 7. 0375. | 8. 876 |
| 9. 06875. | 10. 078125. | 11. 056. | . $6 \cdot 6$. |
| 3. $24 \cdot 008$. | 14. 3.52E. | 15. 46.3125. |  |

Exercise LXXVII.-Page 114.

1. $\frac{1}{8}$
2. IT-
3. $\frac{2}{8} 7$.
4. $88 \%$.
5. $1 \frac{1}{4} 5$.
6. ${ }^{2} \frac{1}{8} \frac{1}{6}$.

7. $2^{188} 00^{8}$

8. $3 \frac{2}{2} \frac{5}{3}$.
9. $2 \frac{1}{8}$.

Hxercise LIXXVIII.-Page 1.14.

1. $62 \cdot 920413349443052$ î
2. $\dot{2} \dot{4} ;-03 \dot{2} 7116 \dot{3}$.
3. $9.92 \dot{8}: 2 \dot{2} 9 \dot{7}$.
4. $3 \cdot \dot{6} ; 1 \cdot 1 \times \dot{4} \dot{6}$.
enty. dthe. teen, 1 one diths. 1008.
5. 92 d .
6. £309 5s.
7. $£ 4$ 1s. $5 \frac{1}{2} \mathrm{~d}$.
8. 3209 far.
9. $24 \cdot 97502 \dot{4} ; 500 \cdot 5$.
10. 18 ; $15 \frac{5}{8} ; 1$,
11. 9525. 
1. 2. 
1. $12 \times 2 \frac{5}{8}$.
IV.
2. $1 \cdot 1214727$.
3. $\cdot 54321$.
4. 2520 ; 3 옥.
5. $97 \frac{17}{6}$.
$\nabla$.
6. $\frac{2}{3}$.
7. $\cdot 00001$; $\cdot 00009999$.
8. 1.60546875.

Exercise LXXLX.-Page 118.
Exercise LXXX.-Page 119.

1. 1044736 dr .
(xercise 1 XXX Page 119
2. 1390 dr . 3. 13 cwt .2 qr .2 lb .13 oz.
3. 954 t. 16 cwt. 1 qr.
4. 4933 oz .
5. 25 t .16 cwt .1 qr .24 lb .
6. 1104 far.
7. $£ 2915 \mathrm{~s} .5 \mathrm{~d}$.
8. 11 ; $2^{\frac{1}{8} 00} ; \cdot 000011$.
9. $\cdot 017359 ;-0005$.
10. $120508 ; \cdot 13$.

II.
11. $\cdot 375 ; \cdot 000000375 ; 356 \cdot 315375 ; 160000$. 2. $\cdot 01825$.
 III.
12. 2406 d .
13. 560 d .
14. $£ 29$ 16s. 11 d .
15. 183839 far.

Exercise LXXXI.-Page 120.

1. 16 oz .
2. 24 lb .10
3. 32 lb .5 dwt .
4. 5460 gr .

Exercise LXXXII.-Page 121.

1. 71478 in.
2. 1 mi .3 fur. 18 per. 3 yd .2 ft.
3. 1 mi. 1 fur. 26 per. 2 ft.
4. 36 ft .
5. 232 fath. 4 ft.

Exercise LXXXIII.—Page 122.

1. 12 a .1 r .37 rd .
2. 117900 in .
3. 4 cu. ft. 1557 in .
4. 60 c .9 ft .
5. 75506904 clu . in.
6. 135424 cu . in.

Exercise LXXXIV.-Page 124.

| 662400 seo. | 2. 120 bu .2 qt . | 3. 2691 gi . |
| :---: | :---: | :---: |
| 4. 2311 pt . | 5. $83 \mathrm{gal} .3 \mathrm{qt} .1 \mathrm{pt}$.1 gi . | 6. 556 p |
| 7. 61 bu .25 lb | 8. 1 wk .2 da. 2 hr .14 min | sec. |
| 9. 74 hm 24 lb | 10. 6739740 seo. | 11. 12 c .4 |

## Exercise LXXXV．－Page 125.

1． 174 lb .3 oz ．
3． 88 rd .5 yds .1 ft .6 in ．
5． 43 bu .1 pk .1 pt ．
7． 6 wk .3 da． 6 h． 50 min .33 sec.

2． 74 ewt． 21 lb .3 os．
4．$£ 3414 \mathrm{~s} .8 \mathrm{~d}$ ．
6． 95 rd． 5 yd． 2 ft .3 in
8． 22 rd． 2 yd． 8 in．

Exercise LXXXVI．－Page 126.
1． 7 lb .8 oz .6 dr .1 scr． 19 gr ．
2． 19 mi .1 rd ．
3． 59 a .2 r .27 rd ．
5．$£ 27 \mathrm{l7s} .4 \mathrm{~d}$ ．
7． 142 bu .2 pk． 5 qt ．
9． 31 gal． 2 qt． 1 pt．
4． 5 fur． $31 \mathrm{rd}$.5 yd .2 in ．
6． 38 per． 18 yd .2 ft .36 in ．
8． 79 lb .3 oz .5 dwt .4 gr ．
10． $22 \mathrm{sq} . \mathrm{rd} .12 \mathrm{yd} .4 \mathrm{ft} .128 \mathrm{in}$ ．
11． $1 \mathrm{cwt}, 3$ qr． 10 lb ．

## Exercise LXXXVII．－Page 127.

1． 90 cwt .3 qr .7 lb .13 oz.
3． 75 da． 23 h .34 min .40 sec ．
5． 4985 cwt． 1 qr．
7． 15 （）a． 2 r． 35 sq．rd．
9． 88 mi ． 3 fur． 2 rd． 3 yd ．
11．$£ 2805 \mathrm{~s}$ ． $9 \frac{1}{2} \mathrm{~d}$ ．
12． 662 mi ． 4 fur． 28 rd .3 yd .2 ft .2 in．13． 2739 bu .1 pk .5 qt ．

## Exercise LXXXVIII．－Page 128.

1．$£ 159 \mathrm{~s} .7 \mathrm{~d}$ ．
3． 16 t .2 cwt .1 qr .13 lb ．
5． $2 \mathrm{cu} . \mathrm{yd} .6 \mathrm{ft} .960 \mathrm{in}$ ．
7． $103_{3^{3}}$ ．
9． $5 \frac{7}{\frac{1}{9}}$ ．
11． 25 dimijohns．

2． 50 lb .2 oz .7 dwt .3 gr ．
4．$£ 6009 \mathrm{~s} .6 \frac{3}{4} \mathrm{~d}$ ．
6． 1 lb .1 oz ． 12 dwt ．
8． 23332 gal． 2 qt ．
10． $5 \mathrm{oz} \cdot 19 \mathrm{dwt}$ ．

## Exercise LXXXIX．－Page 129.

1． $3 \mathrm{pk} .1 \mathrm{qt}. 1_{\mathrm{l}}^{\mathrm{p}} \mathrm{pt}$ ．
3． 4 yd． $2 \mathrm{ft} .5 \frac{1}{4} \mathrm{in}$.
517 cwt 2 qr ．

9． 1 lb .9 oz ．
Exercise XC．－－Page 129.
1．$\frac{1}{8}$ ．
2．रо⿱⿱亠䒑日\zh20。
5．$\frac{1}{8 .}$
9 （46015．
6． $18^{\frac{5}{8}}{ }^{\circ}$
10．$\frac{8}{5} \frac{5}{8} \frac{1}{4}$ ．
Fxercise XCL．－Page 130.

1． 3 r .31 rd ．
4． 47 min .6 sec．
7． 7 fur． 29 per．
10． $3 \mathrm{~s} .5 \frac{1}{2} \mathrm{~d}$ ．

2． 12 lb .9 oz .15 dwt .18 gr ，
4． 1 gi．
6． 8.
8． $11 \frac{21}{5} \frac{1}{8} 97$.
10． 2 bu． 3 pk .3 qt．
12． 5 weeks．

2． 5 fur． 13 rd .1 yd． 2 ft .6 in ．
4． 2 fur． 16 rd ．
6． 2 r． 8 rd .26 yd .8 ft ．
8． 4 da． 23 h． 28 min ．

Fxercise XOII．－Page 130.
1． $2 \cdot 525$.
2． 282 t ．
8． 78125 oz.
4． 775 mi ．
5． 3185 pk ．
6．$£ 9 \cdot 26875$.
7． 17.895 owt．
8． 7.875 ba ．
）． 625 fath．
10．$\cdot 71$.
11． $129 \cdot 78 \mathrm{hr}$ ．
12． 001625 t ．
Exercise XCIII．－Page 131.
2．$\$ 192$.
2．$\$ 148.50$ ．
3．$\$ 436.80$ ．
4．$\$ 388$.
5．$\$ 2667.50$ ．
6．$\$ .615$ ．
7．$\$ 496.12 \frac{1}{2}$ ．
8．\＄308．
9．$\$ 381.75$ ．
10．\＄35．55．
11．$\$ 101.85$ ．
12．$\$ 124.20$ ．
13．$\$ 2388.50$ ．14．$\$ 44.04$ ．15．$\$ 32753.12 \frac{1}{2}$ ．
Exercise XCIV．－Page 132.
2． 124 lb ．
5． $1 \frac{1}{2}$ in．
9．11䒜d．
12．$\$ 7152.31 \frac{1}{\mathrm{t}} \mathrm{tf}$ ．
15．\＄2．10．
19． $4166 \frac{3}{3} \mathrm{yd}$ ．
23．$\$ 1736.231$ ．
27．$\$ 8400$ ．
3．$\$ 65.10_{1 / 5}^{\text {f }}$ ．
4． 3 青程．
7．£34 12s． 4 d ．
8．5s． 2 d ．
10． 64 oz ．
11．$\$ 567.525$ ．
13．$\$ 173.744^{\text {¹ }}$ ．
14． 7 hr .11 min .8 sec ．
17． 98 yd ．
18． $30 \% \mathrm{yd}$ ．
21．\＄1108．80．
22．3s． $7 \mathrm{I}^{2}$ 多d．
24．$\$ 880$ ．
26．is ct．；$\$ 5.76$ ．
28．$\$ 3000$ ．
30． 6 cents．

31． 64 centr．
Exercise XCV．－Page 135.
1．34．25．
2． 32.22 ．
6． $43^{9} .99$ ．
Exercise XOVI．－Page 136.
1． 72.
2．$\$ 15$ ．
3． 23 sheep．
4．$\$ 10.50$ ．
5． 14 men．
6． 45.
7． $40 \%$ ．
8． $75 \%$ ．
9． $60 \%$ ； $36{ }_{\mathrm{I}}^{4} \%$ ． 10.1100.
11．$\$ 1200$ ．

Exerciso XCVII．－Page 137.
1．$\$ 18$.
2．\＄11．20．
3．$\$ 15.20$ ．
4．$\$ 11.25$ ．
5．$\$ 100$ ．
6．$\$ 110.40$ ．
7．$\$ 166.25$ ．
8． 865.20 ．
9．$\$ 2500$ ．
10．$\$ 7000$ ．
11．$\$ 70000$ ．
12．$\$ 9600$ ．

13．$\$ 5276$ ．
Exercise XCVIII．－Page 138.
1．$\$ 14.40$ ．
2．$\$ 15.80$ ．
3．$\$ 10$ ．
4．$\$ 30$.
5．$\$ 247$.
6．$\$ 112$.
7．$\$ 2500$ ．
8． 7500 ba ．
9．\＄788．75．
10．$\$ 1.75$ ．
11． 34 per cent．

Exercise XCIX．－Page 139.
1．\＄48．
2．$£ .8 .50$ ．
4．$\$ 568.05$ ．
5．$\$ 451.50$ ．
8．$\$ 503.36$ ．
11．$\$ 198.66$ ．
9．$\$ 85$ ．
14．$\$ 192 \cdot 225$.
12．\＄311．64．
15．$\$ 882$.
17．$\$ 934.92$ ．
20．eㅡㅁ $1208 \cdot 89$
18．$\$ 14 \cdot 358 .$.
21．8 pas ent．
3．$\$ 236 \cdot 412$ ．
7．$\$ 236.64$.
10．$\$ 842.19 \mathrm{~g}$ ．
13．$\$ 154.78$ ．
16．$\$ 2076.36$ ．
19．\＄287．67．．．
2． $7 \frac{1}{7}$ near

23． 6 per cent
26．$\$ 9000$ ． 29．Oct．4， 1877.

24．$\$ 3500$ ．
27． 3 yr ．
30．147 yr．

25．\＄3250c．
28． 8 yr ．

Exercise C．－Page 143.

| 1．$\$ 1168.70$. | 2．$\$ 457.50$ | 3．$\$ 900$. | 4．The latter． |
| :--- | :--- | :--- | :--- |
| 5．$\$ 2100$. | 6．Gain $\$ 50$. | 7．$\$ 155.82$. | 8．$\$ 242.32$. |
| 9．$\$ 1.25$. | 10．$\$ 3.60$. | 11．$\$ 10.35 .$. |  |

Exercise CI．－Page 146.


Exercise CII．－Page 147.
1． 96 sq ．ft．
4． $18 \frac{\mathrm{~g}}{\mathrm{~g}} \mathrm{sq}$ ．yd．
2． 91 sq ．ft．
5． $351 \frac{1}{3} \mathrm{sq}$ ．vd．
3． 525 sq．ft．
6． 470 sq．ft．

Fxercise OIII．－Page 148.
1． 84 Jd ．
2． $26 \frac{3}{3}$ yd．
3． 64 yd ．
4． $138 \frac{1}{3} \mathrm{yd}$ ．
5．\＄48．
6．\＄57．60．
7．\＄29．162．
8． $2 \frac{1}{\mathrm{ft}}$ ．

Exercise CIV．－Page 148.
1． 126 yd．2． 578 sq ．ft．3． $115 \frac{1}{3} \mathrm{yd}$ ．4． $57 \frac{3}{3}$ yd．5．$\$ 6.80$ ． Exercise CV．－Page 149.
1． $240 \mathrm{cu} . \mathrm{ft}$ ．
3． $187 \frac{1}{2} \mathrm{cu} . \mathrm{ft}$ ．
4． $45 \frac{1}{\mathrm{c}} \mathrm{cu} . \mathrm{ft}$ ．
2． 95 cu ．ft．
5． 16000 ．
6．$\$ 14.51$ 掌多。

## Misceilaneous Problems．－Page 150.


59. $\$ 1.50$ 60. $\$ 7225$. 61. $\$ 135.70$.
63. $\$ 45.80$.
64. $\$ 1.45$.
67. $\$ 125$; $\$ 225$; $\$ 150$.
70. 112 a.; 98 a.
73. $\$ 60$; $\$ 144$; \$96.
75. 814.40 ; $\$ 9.60$.
78. \$21.60; \$23.04; \$25.92.
80. $\$ 1440$; $\$ 2385$.
84. \$6.8992.
82. $\$ 124.16$...
85. 466.56.
87. 3562.75 .2.
66. 576,684.
68. $\$ 150$; $\$ 200$; $\$ 250$.
71. 1520 bu. ; 2280 bu.
74. $\$ 3900$; $\$ 4800$; $\$ 3300$.
76. $\$ 6.30$; $\$ 5.25$; $\$ 4.20$.
79. $\$ 525$; $\$ 500 ; \$ 480$.
83. $\$ 1215.50 . .$.
86. \$161.02....
sq. ft.
sq. ft.
$38 \frac{1}{3} \mathrm{yd}$. ft .
$\$ 6.80$.
cu. ft.
51等.

120 da.
a 40 da .


IMAGE EVALUATION TEST TARGET (MT-3)





Photographic Sciences
Corporation


## EXAMINATION PAPERS.

JULI EXAMINATIONS, 1877.

## ADMISSION TO HIGH SCHOOLS.

## TLME-TWE HOURE.

Examiner,-J. A. MoLellan, LL.D.

1. What is the least number that must be added to five millions to make the sum exactly divisible by seven thousand and nineteen?
2. Simplify $\frac{20}{21}-\left(\frac{48 \frac{1}{2}+7 \frac{1}{\frac{1}{2}}-16 \frac{3}{2}}{16 \frac{1}{2} \times 14 \frac{1}{\frac{1}{3}} \times 12 \frac{5}{4}} \div \frac{5 \frac{3}{2}}{7 \frac{2}{3}}\right)$.
3. Simplify $\frac{£ 1412 \mathrm{~s} .11 \mathrm{~d}}{10 \mathrm{~s}-3 \frac{\mathrm{~s}}{\mathrm{~g}}} \times \frac{£ 1010 \mathrm{~s} .10 \mathrm{~d}}{10 \mathrm{~s} .9 \frac{1}{2} \mathrm{~d}}$
4. A man bought a quantity of hay at $\$ 15$ for 20 cwts. He sold it at 85 cents per cwt ., gaiuing $\$ 22.25$. How many cwt. did he buy?
5. 3t yards of oloth cost $\$ 12.50$; what will 23 1\% yards cost ?
C. A person having an annual income of $\$ 1400$, spends a sum equal to $\$ 625.50$ more than he saves. Find his daily expenditure (year $=365$ days).
6. A lady had in her purse just money enough to buy a cortain quantity of silk; but she spent for the money in flannel, of the remainder in calico, and had then only enough money left to buy $10 \frac{1}{2}$ yards of silk. How many yards of silk could she have bought at first?
7. A room 15 feet wide and 18 feet long is covered with matting at a cost of $\$ 25$; what would be the expense of covering, with the same quality of matting, a room a yard longer and a yard wider?
8. The average of four quantities is $183^{30}{ }^{\frac{5}{7} 9}$; the first is 26.207, the second $3.59 \dot{2}$, and the third is 38.06 . Find the fourth.
9. A bankrupt owes to A $\$ 1039.84$, and to $\mathrm{B} \$ 612.80$; if A receivgs $\$ 357.44 \frac{1}{2}$, what will B receive?

Note. -10 marke to each question.

# ADMISSION TO HIGH SCHOOLS. 

1. How often is 6 yds .2 ft . contained in 25 fumiongs ?
2. If I buy 3 bushels, paying 5 cents for avery 3 quarts, and sell at a profit of 10 cents per gallon, find the selling price of the whole.

3. Reduce 2 hrs .20 min . to the Cecimal of 3$\}$ weeks.
4. A sum of money was divided ainong $A, B$, snd $C$. A received of the sam ; B, $\$ 20$ less than of what was left; and the remainder, which was of of share, was given to C. Find the scm divided.
5. Trees are planted 12 feet apart around the sides of a rectangular field 40 rods long, containing two acres. Find the number of trees.
6. I buy a farm containing 80 acres, and sell $f$ of it for $\frac{8}{8}$ of the cost of the farm; ${ }^{\top}$ then sell ths remaiader at $\$ 60$ per acre, and neither gain nor loose by the whole transaction. Find the cost of the ferm.
7. Find the amount of the following bill of goods:183 cords of wood, at $\$ 8.50$ per cord. 16 yards of oloth, at $\$ 1.12 \frac{1}{2}$ per yard. 12 bus. 25 lbs . of wheat, at $\$ 120$ per bus. 1,400 feet of lumber, at $\$ 12.50$ per thousamad. 65 tons 12 owt. of coal, at $\$ 0.30$ per owt.

JULY EXAMINATIONS, 1878.

## ADMISSION TO HIGH SCHOOLS.

$\frac{\text { Values. }}{12}$
3. I sell $12 \frac{1}{2}$ tons of coal for $\$ 80$, which is one. seventh more than the cost. Find the gain per owt.
4. $.001 \times .001 \div .0001$.
5. A cistern is two-thirds full ; one pipe rans out and two run in. The first pipe can empty it in eight hours, the second can fill it in twelve hours, and the third can fill it in sixteen hours. There is also a leak half as large as the second pipe, in how many hours will the cistern be half full?
6. Ten men can do a piece of work in twelve days. Aftel they have worked four days, three boys join them in the work, by which means the whole is done in ten days. What part of the work is done by one boy in one day?
7. I buy a number of boxes of oranges for $\$ 600$, of which twelve boxes are unsaleable. I sell two-thirds of the remainder for $\$ 400$, and gain on them $\$ 40$. How many boxes did I buy?
8. Find the total cost of the following:-Catting a pile of wood 80 ft . long, 6 ft . high, and 4 ft . wide, at 60 c. per cord.-Digging a cellar 44 ft . long, 30 ft . wide, and 8 ft . deep, at 18c. per cubic yard.-Plastering a room 24 ft . long, 16 ft . wide and 10 ft . high, at 15 c . per square Jd.-Sawing 68c0 shingles at $40 c$ per 1000 .

## PROVINCIAL MODEL SCHOOL.

## SECOND DIVISION.

1. Among how many persons can you divide $£ 9625 \mathrm{~s}$. $0 \frac{1}{2}$ d., giving each of them £137 9s. $3 \frac{1}{2} d$.
2. Divide $\$ 6640$ among $A, B$, and $C$, so that $A$ may have one-quarter of $i t$, and $B$, four times as mach as $C$.
3. If 5 men do as much work as 8 boys in a day, how many days will it take 32 boys to finish a piece of work of which 15 men did one-fourth in 16 days?
4. If the dividend be 6050034, the quotient 550003, and the remainder 1, what is the divisor?
5. Divide 478673 by 105 by using its component fastors, and explain how the true remainder is obtained.
6. The price of 2 turkeys and 9 chickens is $\$ 14.40$, and the price of 5 inireys and 3 chickens is $\$ 20.40$. Find the price of a íurkey and of a chicken.
7. Reduce to a decimal, correct to 6 places, $1+\frac{1}{1}+\frac{1}{1 \times 2}+$ $\frac{1}{1 \times 2 \times 3}+\frac{1}{1 \times 2 \times 3 \times 4}+$ etc.
8. Find the value of $2 \frac{1}{2} \times \frac{1}{3 \frac{1}{2}+\frac{1}{43}}$ of 13 aores.
9. A drover invested $\$ 30,450$ in the purchase of horses at a certain average price. He sold a part of them for $\$ 12,000$, at $\$ 400$ each, and lost $\$ 35$ per head.. At what pice must he sell the remainder so as to gain $\$ 750$ on the whole?
10. If 14 men can do a piece of work in 14 days, working 10 hours per day, how long ought the work to ocoupy 12 men working 7 hours a day?

11 Two watches are set together; one loses 7 sec. and the other gains 8 sec. a day. When will one be a quarter of an hour before the other?

## CITY OF TORONTO.

## COMPINED EXAMINATION.

1. Divide 540 tons, 10 owt., 3 qrs., 15 lbs., by 375.
2. How many seconds are there from $90^{\prime}$ olock a.m., on 13th January, 1876, to 16 minutes past 10 o'clock p.m., on 27 th June, 1877 ?
3. Reduce 3s. 6 d . to the decimal of $£ 710 \mathrm{~s}$.

$$
\text { 4. Simplify } \frac{2}{3+\frac{1}{4+\frac{1}{5+\frac{1}{6}}}}
$$

5. Reduce 1 ton, to lbs., oz., \&c., Apothecaries' weight.
6. Simplify $\frac{\frac{1}{4}+\frac{1}{4}+\frac{1}{6}}{\frac{1}{3 \frac{1}{4}}+\frac{1}{4 \frac{1}{4}}+\frac{1}{5 \frac{1}{2}}}$
7. If 6 men will dig so trench 30 yds . long and 8 yds . broad in six days of 16 hours each, in how many days of 12 hours each will 8 men dig a trench 40 yds. long and 16 yds. broad ?
8. Divide the difference of $19 C$ and fo by their sum; and also their sam by their difference, and $\rho$ t the sum of the quotients.
9. What is the interest on $\$ 757.60$ for four years and four months, at $6 \frac{1}{2}$ per cent ?
10. Find the difference in the expense of carpeting a room 24 ft .9 in . lung and 15 ft .6 in . broad, with carpet $\frac{3}{3}$ of a yard wide, at $\$ 1.50$ per yard, and with v ypet $\frac{7}{8}$ of a yard wide, at 70 cents per yard.
11. A man sells a house for $\$ 437.50$, and loses $12 \frac{1}{2}$ per cent. on the original cost. What was the original cost ?
12. How many flag stones, each 2.88 ft . wide and 8.30 ft . long, are required to pave a walk round a grass plot $137 \cdot 31 \mathrm{ft}$. long and $125 \cdot 79 \mathrm{ft}$. wide, the walk being 4.15 yds . wide ?

# -OUNTY OF WATERLOO. <br> COMPETITIVE EXAMINATION. 

Promotion from 5th to 6th Form.

1. Divide 480 into two parts, one of which shall be threeGifths of the other.
2. The figures in the units and millions places are 8 and 5 respectively; what will they become when 999,999 is added to the number.
3. Find the price of 9 tons, 19 cwt ., 3 qrs., $12 \mathrm{lbs} ., 8 \mathrm{oz}$., at $\$ 86.24$ a top? Peduce the answer to $£$ s. d., taking the value of the $\boldsymbol{E}$ to be $\$ 4.867$.
4. A car is exactly filled by barrows that hold each 9 cwt., and emptiè $\dot{\alpha}$ by sacks that hold each 5 cwt . given that it holds between 8 and 10 tons, find the exact amount.
5. Simplify $\frac{.004 \div \cdot 0005}{2.4 \dot{2} \dot{3}+3 . \dot{5} 7 \dot{6}+2.000191 \dot{i}}$
6. A man borrowed $\$ 500$ on the 21st January, 1874, at 8 per cent. interest, payable half yearly; every half-year he pays $\$ 80$. How much will he owe on the 21st July 1876, whatever he pays each half year over and above the interest due being deducted from the principal?
7. A, who owes B $\$ 1000$, sends him 725 M ft. of lumber, which $B$ sells at $\$ 16$ per $M$, charging 3 per cent. commission, and paying out of the proceeds expenses amounting to $\$ 161.50$. How much is coming to $A$ ?
8. If $B$ buys for $A$, with the sum you found due him from No. 7, flour at $\$ 4.50$ a barrel, charging $3 \frac{1}{2}$ per cent. commission, how many barrels will A. receive ?
9. If I buy broadcloth at $\$ 3.60$ a yard; what must $I$ ask for it a yard that I may be able to throw off 10 per cent. from my price and yet make 25 per cent. profit?
10. How much Dominion 6 per cents at 108 can I buy for $\$ 16,200$, and what yearly income shall I have therefrom?
11. The population of a town has increased 5 per cent. eince last year. It has now 3780 inhobitants; haw many kad is then?
12. I borrowed $\$ 250$ on the 1st October, 1875, and paid buck $\$ 268$ on the 24th February, 1876; what rate of interest per annum had I been charged?

## COUNTY OF DURHAM.

COMPETITIVE EXAMINATION.
Senior.
Values.

1. A can do $\frac{1}{2}$ of a piece of work in one hour, B can do $\frac{8}{4}$ of the remainder in 1 hour, and $C$ can finish it in 20 minutes. How long will it take $\mathrm{A}, \mathrm{R}$ and C together to do the work?
2. If it costs $\$ 70.40$ to carpet a room 24 feet long with carpet 24 feet wide, at $\$ 1.10$ per yard, find the width of the room.
3. By selling tea at 96 cts. per lb., a merchant gains $\ddagger$ of the cost; he then raises the price to $\$ 1.05$ per 1 lb .; what does he clear on every $\$ 8.40$ of his outlay by the latter price?
4. John McCromb rents a house, the cash value of which is $\$ 2400$, and which is kept in repair by the owner at an annual outlay of $\$ 20$ paid at the end of the year. He pays in advance an annual rent of $\$ 200$. How mach a year would he save by buying the house and paying for it in aash, money being worth 7 per cent. per annum ?
18
5. Simplify (a)

(b) ( $\frac{3}{\frac{1}{2}}-\frac{1}{2}$ of $\frac{3}{3}$ ) of $£ 411 \mathrm{~s}$. 4d. is what fraction of ( $\frac{1}{2}$ of $\left.\frac{8}{4}-\frac{1}{8}\right)$ of $\$ 164.40$, £1 being worth $\$ 44$.
120 marks \& full papor.

## answers T0 EXAMINATION PAPERS.

1. 4547. 
1. $222 \frac{1}{2}$ cwt.
2. $37 \frac{1}{2} \mathrm{yds}$.
3. $\$ 210.65$.

## ADMISSION TO HIGH SCHOOLS.

July, $187 \%$.
2. 14.
5. \$93.75.
-8. * $^{2} 5$.
3. $£ 41 \mathrm{1s} .5$ 거․
6. $\$ 2.77$ 多
9. $4 \frac{8}{8} \frac{1}{6}$.

December, $187 \%$.

1. 825 times.
2. \$4.00.
3. $312 \frac{1}{8}$.
4. $0041 \dot{6}$.
5. $\$ 3000$.
6. $\$ 200$.
7. 509.625 .
8. 132 trees.

July, 1878.

1. $2,2,3,3,5,7$.
2. 31116. 
1. 4 cents.
2. 01 .
3. 120 boxes.
4. 8 hrs .
5. $\$ 101.8$ : $\frac{1}{z}$.
6. rt.

PROVINCIAL MODEL S SHOOL.

1. 7 persons.
2. 36 days.
3. Turkey, $\$ 3.60$; Chicken, 80 cents.
4. $\mathrm{A}, \$ 1660 ; \mathrm{B}, \$ 3984 ; \mathrm{C}, \$ 996$.
5. $8_{1^{R} 7^{\circ} \text { a. }}$
6. 60 days.
7. $\$ 480$.
8. $45588^{88}{ }^{8}{ }^{2}$.
9. $2 \cdot 718281$.

$$
\text { 10. } 23 \frac{1}{2} \text { days. }
$$

## CITY OF TORONTO.

1. 1 ton 8 cwt. 3 qr. 7 lbs. 14 oz. $8 \mathrm{f}_{\mathrm{s}} \mathrm{dr}$.
2. 45926160 sec.
3. 623. 
1. $\frac{8}{4} \frac{\pi}{2} \frac{1}{2}$.
2. 2430 lb .6 oz .5 dr. 1 scr .
3. 16 days.

4. $1^{7}{ }^{787}{ }^{87}$.
5. $\$ 51.15$.
6. $\$ 500$.
7. $\$ 218.39_{\mathrm{T}^{1} s}$.
8. 300. 

COUNTY of waterloo.

1. 390 , and 180.
2. 9 tons:
3. 7 and 6.
4. $£ 177$ Is. $7 \frac{3}{4} d$.
5. \$10090.50.
6. 7. 
1. $\$ 175.02$.
2. $\$ 15000 ; \$ 900$
3. $2166 \frac{8}{8} \frac{1}{2} \mathfrak{i}$ bul. $^{2}$
4. $\$ 5$.
5. 3600. 

COUNTY OF DURHAM.

1. 48 min .
2. 18 ft .
3. $\$ 2.10$.

4. $\$ 4.95$.
5. 32 lb . tea; 21 lb . coffee.
6. $1 \frac{5}{6}$; $\frac{4}{9}$ ?


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[^0]:    $\therefore$ stands for the word tharefore.

