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## LOAN TABLES

BY

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The following Tables are an extension of a set published in the Canadian Almanac for 1870, which gavo the values from 1 to 12 years for rates of interest per cent. per annum 10, 101 $, 11,11 \frac{1}{2}, 12$ payable half-yearly. In the present set, the time runs up to 20 years, and the rates are $8,9,10,11,12,13$; with some additional 'Cables which seemed likely to be of use.

## EXPLANATION AND USE OF THE TABLES.

When a loan is contracted to be repaid (principal and interest) by equal instalments extending over a term of years, the following tables will give the amount of the instalment, monthly, quarterly, half-yearly, or yearly, for various rates of interest, and will also give the present worth or surrender value of the instalments for any unexpired portion of the term.

As interest is in this comntry generally payable half-yearly, the half-yearly rate has been taken as the basis, and the calculations are made ou the true yearly rate corresponding and not the nominal rate. Thus 10 per cent. per anmum, payable half-y early, is understood to mean 5 per cent. per half-year, the true yearly rate in this case being 101; for, $\$ 100$ being put out for one year at 5 per cent. per half-year, would amount at the end of the year to $\$ 110.25$. Both the true and the nominal rates for the various periods are given in a foot note to each table.
(1.) Table I. gives the instalment payable at the end of each month, quarter, half-year, or year, to repay a loan of $\$ 1,000$ in any period from 1 to 20 years.
These instuments are given exact to the nearest cent above the true value when the difference exceeds one-tenth of a cent.
(2.) Table II. gives the present value of an instalment of $\$ 1$ payable at the end of each month, quarter, half-year, or year, during any number of years from 1 to 20.
By aid of this table, the present value c. an instalment for an exact number of years is at once found by multiplying the instal. ment by the corresponding number in the table.

Exampre.-Interest at 10 per cent. per annum, payable halfyearly. An instalment of $\$ 20$ is payable at the end of each month for 7 years: required, the present value.
No, corresponding in Table II. ..... 60.6174
Instalinent ..... 20
Present value ..... $\$ 1212.35$
(3.) Table III. gives the present value of $\$ 1$ due at the end of any number of months from 1 to 12.

By aid of this Table and Table II., the present value of an instalment for a broken period of a number of years and some months can be found-as follows:

From Table II. take the present value of an instalment of $\$ 1$ for the named number of years, and discount it for the number of months by multiplying it by the factor corresponding to that number of months in Table III.; then add to it the present values taken from Table III. of the several instalments of \$1, payable during the broken period of months, and multiply the final sum by the given instalment.

Example 1.-Interest at 10 per cent. per annum, payable halfyearly A yearly instalment of $\$ 500$ has 3 years and 9 months to run: required, its present value.
From Table II., present value of $\$ 1$ for 3 years 2.47595

Multiply this by the factor for 9 monthis from Table III. 0.9294284

$$
\text { giving } \overline{2.301218}
$$

Add the present value of an instalment $\$ 1$ duc at the end of 9 months, from Table III. .
0.9 .9125
3.230646

Multiply the instalment $\$ 500$ by this number, giving Present value $\$ 1615.32$
Example 2.-Same rate.
A half-yearly instalment of 8250 has 6 years and 11 months to run: required, its present value.
From Table II., present value of half-yearly instalment $\$ 1$ for 6 years. 8.8632

Multiply this by the factor for 11 months from Table III. 0.9144350

$$
\text { giving } 8.10482
$$

| Brought forward | 8.10482 |
| :---: | :---: |
| Add the present value of an instalment $\$ 1$ due at the end of 5 months, from Table III. | 0.96016 |
| And the present value of an instalment $\$ 1$ due at the end of 11 months | 0.91443 |
|  | 0.97941 |

Multiply the instalment $\$ 250$ by this number, giving Present value. . . $\$ 2494.85$
Example 3.-Required the present value of a quarterly instalment of $\$ 100$, unexpired period being 7 yenrs and 5 months, interest at 11 per cent. per anoum, payable half-yearly. From Table II., present value of instalment of $\$ 1$ for 7 years, is
19.4395

Multiply this by the factor for 5 mos., from Table III. 0.9563633

|  | giving | 18.5912 |
| ---: | ---: | ---: |
| Add the present value of $\$ 1$ due at end of 2 months.. | 0.9823 |  |
| And the present value of $\$ 1$ due at end of 5 months.. | 0.9564 |  |
|  | giving | 20.5299 |

Multiply the instalment $\$ 100$ by this number, giving..
Present value.... \$2052.99
In the same way by aid of these two Tables, the present value of a monthly instalment for a broken period may be found, but this will be more conveniently effected by Table IV.
(4.) Table IV. gives the present values of a monthly instalment for any number of months not exceeding a year.

By aid of this and the previous tables, the present value of a monthly instalment for a broken period of a number of years and some months ean be found, as follows:
From Table II. take the present value of an instalment of $\$ 1$ for the named number of years, and discount it for the number of months by multiplying it by the factor corresponding to that number of months in Table III ; then add the present value of an instalment of $\$ 1$ from Table 1V. for the number of months, and multiply the final sum by the given instalment.

Example.-Interest 10 per cent. per annum, payable half-yearly.
An instalment of $\$ 12.50$ per month has 4 years and 8 months to run: required, its present value.
Present value of monthly instalment $\$ 1$ for 4 years, fromTable II.89.6795
Multiply this by the factor for 8 months, from Table III. 0.93701 it , giving 37.0866
Add present value of monthly instulment of \&1 for 8 months, from Table IV.7.7139
44.8005
Multiply tho instalment $\$ 12.50$ by this number, giving Present value. ... §560.01
(5.) Table V. gives the mmount with interest of $\$ 1$ after any number of montis from 1 to 12.
liy aid of this and Table IS., the present value of an instalment for a broken period of a number of yeurs and some months can s.lso be found, as follows:

From Table II. take the present value of an instalment of sl for the number of years next ereater than the broken period, and find the amount of it for the difference between the given number of months and one year, by multiplying it by the factor corresponding to that difierence in 'Table $V$. Then subtract from it the amounts (with interest, of the several instalments of 81 (if any) paid during that difference as given in Table V., and multiply the resuli by the given instalment.

Example 1.-Interest 10 per cent. per annum, payable halfyenrly. A yearly instalment of $\$ 000$ has 3 years and 9 montlas to run: required, its present value.

From Table If., present value of yearly instalment of
$\$ 1$ for 4 years
3.15279

Multiply this by the factor for 3 montlis, from Table V.,
1.024695, giving
3.23065

No instalment has been paid during the 3 months. Therefore, multiply the instalment $\$ 500$ by the above, giving ............................. Present value \$1615.32

Esampliz 2.-A halfyearly iustalment of $\$ 250$ has 6 years and 11 months to run: required, its present value. (Same rate.)
From Tuble II., present value of half-yearly instalment of $\$ 1$ for 7 years, is
9.8986

Multiply this by the factor for 1 month, from Table V., 1.008165, giving.
9.9794

No instalment has been paid during the 1 month.
Therefore, multiply the instalment $\$ 2.50$ by the above, giving Present value
$\$ 2494.85$
Example 3.-Required the present value of a quarterly instal. ment of $\$ 100$, unexpired period being 7 years and 5 months. (Same rate.)
From Table II., present value of quarterly instalment of $\$ 1$ for 8 years, is.
21.2082

Multiply this by tho factor for 7 months, from Table V. 1.064456
giving 22.5751
Subtract the amount of the instalment of $\$ 1$ paid 4 months before
1.0363

And the amount of the instalment of $\$ 1$ paic! 1 month before.
$\frac{1.0089}{\text { giving }}-\frac{2.0452}{2.05299}$

Multiply the instalment $\$ 100$ by this number, giving Present value.
$\$ 2052.99$
In the same way by the aid of these two Tables the present value of a monthly instalinent for a broken period can be found; but this can be more couveniently effected by Table VI.
(6). Table VI. gives the amount at the end of any number of months, not exceeding a year, of a mouthly instalment of $\$ 1$ paid at the end of each month during that period.
By aid of this, and Tables II. and V., the present value of a monthly instalment for a broken period of a number of years and some months can be found as follows: From Table II, take the present value of a monthly instalment of $\$ 1$ for the number of years next greater than the broken period, and find the amount of
it for the difference between the given number of months and one year by multiplying it by the faetor corresponding to that difference in Table V.; then subtract from it the amount of an instalment of $\$ 1$ fur that difference given in Table VI., and multiply the result by the given instalment.

(7). Table VIII. gives the present value of $\$ 1$ dine at the end of any number of years, froun 1 to 20 .

With the aid of Table III. this also gives the present value of a sum due after a broken period of a number of yeurs and some months, as follows;
Multiply the sum by the factor corresponding to the number of years in Table VIII., and then multiply this product by the factor corresponding to the number of months in Table III.

Example. - Required the present value of 84,000 , due 17 years and 8 months hence, interest 10 per cent. payable half-yearly. Multiply $\$ 4,000$ by the faetor for 17 years, from Tablo VIII., 0.1903548, giving
761.4192 Multiply this by the factor for 8 months from Table III. 0.9370174
Present value..
(8) By the aid of this and previous Tables, the value of an ordinary mortgage, where the principal is paid at the end of the poriod, can be caloulated for any of the given rates of interest.

Consiler the interest payable on the mortgage as an instalment and calculate its present value by the preceding rules; then add
to it the present value of the principal payable at the end of the period, which will be found as in the last example.

Ex. 1.-A mortgage of $\$ 5,000$, interest at 6 per cent. per annum, has 7 years and 10 months to run: find its present value, interest at 10 per cent. per annum, payable half-yearly.

The interest, $\$ 300$, may be considered a yearly instalment.
The present value of yearly instalment of $\$ 1$ for 7 years, from Table II, is 4.82860

Multiply this by the factor for 10 months from Table III. 0.9219014
giving 4.451491
Add the present value of the instalment of $\$ 1$ due at the end of 10 mouths 0.921901
giving 5.373392
Multiply the instalment $\$ 300$ by this number, giving Present value.... \$1,612 02

Again: multiply the principal, $\$ 5,000$, by the factor for 7 years from Table V11I, 0.5050679 , giving..... 2525.34 Multiply this by the factor for 10 mos. from Table III. 0.9219014
giving $\$ 2,32811$
Adding these results, the present value required is. ... $\$ 3,940 \quad 13$
Ex. 2.-A mortgage of $\$ 4,000$, interest at 5 per cent. per annum, payable half-yearly, has 17 years and 8 months to run: finu its present value, interest 10 per cent. per annum, payable half-yearly.

The interest, $\$ 100$, will be considered a half-yearly instalment.
The present value of a half-yearly instalment of $\$ 1$ for
17 years, from Table II, is
16.1929

Multiply this by the factor for 8 months, from Table III. 0.937 Cl 74
giving 15.17303
Add the present value of instalment of $\$ 1$ due at end of 2 months, from Table III.
0.98387

And the present value of the same, due at end of $8 \mathrm{mos} . \quad 0.93702$
Multiply the interest, $\$ 100$, by this number, giving... $\$ 1,70039$
The present value of the principal, $\$ 4,000$, due 17 years
and 8 months hence, is found, in the last example
but one, to be
$\$ 71346$
Adding these two results, we find the present value.
required to bo $\ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots .{ }^{2} \ldots 2,42285$
(9). Sometimes the borrower may wish to pay off part of his debt by a lump sum at some time during the running of his payments. In this case, having calculated the present value of his future payments, deduct from it the sum he pays down, and consider the remainder as a new lonn. If the borrower wishes to continue his payments at a reduced rate for the same period, the new rate of instalment can be obtained at once from Table I, when the period is an exact number of years; but if he wishes to continue to pay the same amount of instalment, reducing the period during which the payments are to continue, obtain from Tables II. and III. the period which will give for that instalment a present value next less than the above-mentioned remainder; take the difference between this present value and such remainder; this difference improved for the period at the given rate of interest will be an additional sum, which he must pay along with the final instalment to clear the account. To obtain this difference so improved, if for a broken period of a number of years and some months, divide the difference by the factor corresponding to the number of years in Table VIII, and then divide this quotient by the factor corresponding to the number of months in Table III.
Example 1. - Interest at 10 per cent. per annum, payable halfyearly. A monthly instalment of $\$ 20$ as a lon has 5 years to run, and the borrower wishes to pay down $\$ 500$ along with his instalment: to find the reduced instalment for the remaining period.
The present value of the instalments from Table II. .... $\$ 94573$

| Deduct. | 500 |
| :---: | :---: |
| Remainder | 44573 |

Multiply this by the number for 5 years from Table I, 21.15, and dividing by 1000, we obtain $\$ 943$ for the reduced instalment,

Example 2.-Interest as abovo.
A monthly instalment of $\$ 10$ has 7 years and 3 months to run, and the borrower wishes to pay down along with his instalment $\$ 200$ : to find the reduction in the period.
Present value of instalments, found as in (3) ............ . $\$ 62108$
Deduct............... 20000
Remainder
42108
The present value of a monthly instalment, $\$ 10$, is now to be found, which is next below $\$ 42108$ in the Tables.

From Table II, it is seen that the presen value of a monthly instalment of $\$ 10$ for 4 years is $\$ 39580$, and on trial with Table III. it is found that the present value of an instalment of $\$ 10$ for a period of 4 years and 3 months is $\$ 41578$, and is the next below the given remainder $\$ 22108$. Hence the period required is 4 years and 3 months, and the remaining difference $\$ 50$, amounting in this period to $\$ 803$, leaves this additional sum to be paid along with the final instalment.
(10). Given the loan, the instalment, and the number of years for repayment: it is required to determine the rate of interest.

When the instalment for $\$ 1,000$ lies between two values in the Tables, an approximate value of the rate of interest can at once bo obtained by interpolation, and this will in general be near enough for practical purposes; or from this approximate value, closer and closer values may be obtained by the method of "trial and error," or "double position."

When the instalment for $\$ 1,000$ is beyond the Tables, the method of proceeding will be found in the Appendix.

Interest 8 per Cent. per Annum, Payable Half-yearly.

TABLE I.
Instalments to repay a Loan of $\$ 1000$ in the named number of years, payable

| Years. | Yearly. | Half-yearly. | Quarterly. | Montlly. | Years. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 1081.60 | 530.20 | 262.00 | 86.93 | 1 |
| 2 | 562.00 | 275.49 | 136.40 | 45.17 | 2 |
| 3 | 389.16 | 190.77 | 94.45 | 3128 | 3 |
| 4 | 303.00 | 148.53 | 73.54 | 24.36 | 4 |
| 5 | 251.52 | 123.29 | 61.04 | 20.22 | 5 |
| 6 | 217.37 | 106.56 | 52.76 | 17.47 | 6 |
| 7 | 193.13 | 91.67 | 46.87 | 15.53 | 7 |
| 8 | 175.08 | 85.82 | 42.49 | 14.77 | 8 |
| 9 | 161.15 | 79.00 | 89.11 | 12.96 | 9 |
| 10 | 150.11 | 73.59 | 3643 | 12.07 | 10 |
| 11 | 141.17 | 69.20 | 34.26 | 11.35 | 11 |
| 12 | 133.80 | 65.59 | 32.48 | 10.76 | 12 |
| 13 | 127.64 | 62.57 | 30.98 | 10.26 | 13 |
| 14 | 122.43 | 60.02 | 29.72 | 9.84 | 14 |
| 15 | 117.98 | 57.83 | 28.64 | 9.49 | 15 |
| 16 | 114.14 | 55.95 | 27.70 | 9.18 | 16 |
| 17 | 110.81 | 54.32 | 26.90 | 8.91 | 17 |
| 18 | 107.89 | 52.89 | 26.19 | 8.68 | 18 |
| 19 | 105.33 | 51.64 | 25.51 | 8.47 | 19 |
| 20 | 103.07 | 50.53 | 25.02 | 8.29 | 20 |

Nominal Rates of Interest : S per eent. per annum payable half-yearly; 7.9216 per cent. per annum payable quarterly; 7.8708 per eent. per ancum payable monthly.

Actual llates : 8.16 per cent. per annum ; 4 per eent. per half-year ; 1.0804 per cent. per quarter; 0.6559 per cent. per month ${ }_{4}$

Interest 8 per Cent. per Anndy, Papabje Half-qrarly.

TABLE II.
Present Value of Instalment of $\$ 1$ payable

| Years. | Yearly. | Half-Yearly. | Quarterly. | Monthly. | Years. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.92456 | 1.8861 | 3.8095 | 11.5037 | 1 |
| 2 | 1.77936 | 3.6299 | 7.3317 | 22.1396 | 2 |
| 3 | 2.66968 | 5.2421 | 10.5881 | 31.9730 | 3 |
| 4 | 3.30037 | 6.7327 | 13.5988 | 41.0646 | 4 |
| 5 | 397593 | 8.1109 | 16.3824 | 49.4703 | 5 |
| 6 | 4.60053 | 9.8851 | 18.9560 | 57.2418 | 6 |
| 7 | 5.17800 | 10.5631 | 21.3354 | 64.4270 | 7 |
| 8 | 5.71191 | 11.6523 | 23.5353 | 71.0701 | 8 |
| 9 | 6.20554 | 12.6593 | 25.5693 | 77.2121 | 9 |
| 10 | 6.66192 | 13.5903 | 27.4498 | 82.8906 | 10 |
| 11 | 7.08388 | 14.4511 | 29.1884 | 88.1408 | 11 |
| 12 | 7.47400 | 15.2470 | 30.7969 | 92.9948 | 12 |
| 13 | 7.33469 | 15.9828 | 32.2821 | 97.4827 | 13 |
| 14 | 8.10817 | 166631 | 83.6561 | 101.6320 | 14 |
| 15 | 8.47649 | 17.2920 | 34.9265 | 105.4682 | 15 |
| 16 | 8.76154 | 17.8735 | 36.1011 | 109.0150 | 16 |
| 17 | 9.02510 | 18.4112 | 37.1870 | 112.2943 | 17 |
| 18 | 9.26876 | 18.9083 | 33.1910 | 115.3261 | 18 |
| 19 | 9.49405 | 19.3679 | 39.1193 | 118.1292 | 19 |
| 20 | 9.70234 | 19.7928 | 39.9775 | 120.7208 | 20 |

Interest 8 per Cent. per Annum, Payable Haly-yearlif.

## TABLE III.

Present value of $\$ 1$ due after any number of months, from 1 to 12.

| Months. | Present Value. |
| :---: | :---: |
| 1 | 0.9934845 |
| 2 | 0.9870115 |
| 3 | 0.9805808 |
| 4 | 0.9741915 |
| 5 | 0.9678443 |
| 6 | 0.9615386 |
| 7 | 0.9552736 |
| 8 | 0.9490496 |
| 9 | 0.9428060 |
| 10 | 0.9367229 |
| 11 | 0.9306197 |
| 12 | 0.9245563 |

TABLE IV.
The present value of an Instal--ment of \$1, payable at the end of each month during the named numbtr of months.

| Months. | Present Valuc. |
| :---: | :---: |
| 1 | 0.993485 |
| 2 | 1.950496 |
| 8 | 2.961077 |
| 4 | 3.935268 |
| 5 | 4.903113 |
| 6 | 5.864651 |
| 7 | 8 |
| 8 | 7.768974 |
| 9 | 8.711840 |
| 10 | 9.648563 |
| 11 | 10.579183 |
| 12 | 11.503739 |

## Interest 8 per Cent. fer Annuy, Parabli Halffearlt.

## Table vi.

TABLE V.
Amount of \$1 in any number of months, from 1 to 12.

| Mouths. | Anouuts. |
| :---: | :---: |
| 1 | 1.006559 |
| 2 | 1.018160 |
| 3 | 1.019804 |
| 4 | 1.026492 |
| 5 | 1.033225 |
| 6 | 1.040000 |
| 7 | 1.046820 |
| 8 | 1.053685 |
| 9 | 1.060596 |
| 10 | 1.067552 |
| 11 | 1.074552 |
| 12 | 1.081600 |

Amount at the conl of amy mumber of months. from 1 to 12 , of a Momehly lustalment of 今\% paid at the end of cach mondh cluring that period.

| Months. | Amounts. |
| :---: | :---: |
| 1 | 1.000000 |
| 2 | 2.066559 |
| 3 | 3.019719 |
| 4 | 4.039523 |
| 5 | 6.066015 |
| 6 | 6.099240 |
| 7 | 7.139240 |
| 8 | 8.186060 |
| 9 | 9.239745 |
| 10 | 10.300341 |
| 11 | 11.367893 |
| 12 | 12.442445 |

TABLE VIII.
Present Value of $\$ 1$ due at the end of any number of years, from 1 to 20 .

| Yrs. | Present Values. | Yrs. | Present Values. |
| :---: | :---: | :---: | :---: |
| 1 | 0.924556 | 11 | 0.421955 |
| 2 | 0.854804 | 12 | 0.390121 |
| 3 | 0.790815 | 13 | 0.360689 |
| 4 | 0.730690 | 14 | 0.333477 |
| 5 | 0.675564 | 15 | 0.308319 |
| 6 | 0.624597 | 16 | 0.285058 |
| 7 | 0.577475 | 17 | 0.263552 |
| 8 | $0.5 \% 3908$ | 18 | 0.243669 |
| 9 | 0.498628 | 19 | 0.225285 |
| 10 | 0.456397 | 20 | 0.208289 |

Interest 9 per Cent. per Annum, Payable Half-yearly.

TABLE I.
Instalments to repay a Loan of $\$ 1000$ in the named inumber of years, payable

| Years. | Yearly. | Half-yearly. | Quarterly. | Monthly. | Years. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 1092.03 | 534.00 | 264.06 | 87.38 | 1 |
| 2 | 570.04 | 278.75 | 137.84 | 45.61 | 2 |
| 3 | 396.48 | 19388 | 95.88 | 31.73 | 3 |
| 4 | 310.05 | 151.61 | 74.97 | 24.81 | 4 |
| 5 | 258.45 | 126.38 | 62.50 | 20.68 | 5 |
| 6 | 224.27 | 109.67 | 54.23 | 17.95 | 6 |
| 7 | 200.05 | 97.82 | 48.88 | 16.01 | 7 |
| 8 | 182.04 | 89.02 | 44.02 | 14.57 | 8 |
| 9 | 168.18 | 82.24 | 40.67 | 13.46 | 9 |
| 10 | 157.22 | 76.88 | 38.02 | 12.58 | 10 |
| 11 | 148.36 | 72.55 | 35.85 | 11.87 | 11 |
| 12 | 141.08 | 68.99 | 54.12 | 11.29 | 12 |
| 13 | 135.02 | 66.03 | 32.65 | 10.81 | 13 |
| 14 | 129.90 | 63.52 | 31.41 | 10.40 | 14 |
| 15 | 125.55 | 61.40 | 20.36 | 10.05 | 15 |
| 16 | 121.81 | 59.57 | 29.46 | 9.75 | 16 |
| 17 | 118.58 | 57.99 | 28.68 | 9.49 | 17 |
| 18 | 115.76 | 56.61 | 28.00 | 9.27 | 18 |
| 19 | 112.30 | 55.41 | 27.40 | 9.07 | 19 |
| 20 | 111.14 | 54.35 | 26.88 | 8.90 | 20 |

Nominal Rate of Interest : 9 per cent. per anumm payable half-yearly; 8.9008 per cent. per annum payable quarterly $; 8.8350$ per cent. per amum payable monthly.

Actual Rate : 9.2025 per cent. per annum ; $4 \frac{1}{2}$ per cent. per half-year; 2.2252 per cont. per quarter ; 0.7363 per cent. ver month.

Interest 9 fer Cent. per Annuy, Pafabie Half-yearly.

TABLE II.
Present Value of Instalmont of $\$ 1$ payable

| Years | Yearly. | Half-Yearly. | Quarterly | Monthly: | Years. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.91573 | 1.8797 | 3.7870 | 11.4449 | 1 |
| 2 | 1.75429 | 3.5875 | 7.2549 | 21.9253 | 2 |
| 3 | 2.52219 | 5.1579 | 10.4805 | 81.5225 | 3 |
| 4 | 3.22537 | 6. 5959 | 13.8385 | 40.8110 | 4 |
| 5 | 3.86930 | 7.9127 | 16.0015 | 48.3589 | 5 |
| 6 | 4.45896 | 9.1186 | 18.4401 | 55.7285 | 6 |
| 7 | 4.99894 | 10.2228 | 20.6781 | 62.4772 | 7 |
| 8 | 5.49341 | 11.2840 | 22.7180 | 68.6071 | 8 |
| 9 | 5.94621 | 12.164 | 24.5006 | 71.3162 | 9 |
| 10 | 6.36085 | 13.0079 | $26.305: 3$ | 79.4985 | 10 |
| 11 | 6.74055 | 13.7844 | 27.8756 | S4.2440 | 11 |
| 12 | 7.08825 | 14.4955 | 29.3135 | 88.5896 | 12 |
| 13 | 7.40566 | 15.1466 | 30.630\% | 92.5690 | 13 |
| 14 | 7.69823 | 15.7429 | 31.8361 | 96.2131 | 14 |
| 15 | 7.96523 | 16.2889 | 529102 | 99.5501 | 15 |
| 16 | 8.20073 | 16.7889 | 83.9514 | 102.6459 | 16 |
| 17 | 8.43362 | 17.2468 | 34.875: | 105.4042 | 17 |
| 18 | 8.63865 | 17.6660 | 35.7252 | 107.9666 | 18 |
| 19 | 8.82640 | 18.0500 | 36.5016 | 110.3131 | 19 |
| 20 | 8.99833 | 18.4016 | 37.2126 | 112.4619 | 20 |

## Interrat 9 per Cent, per Annum, Payable Halfryearly.

TABLE III.
Present value of $\$ 1$ due after. any number of months, from 1 to 12.

| Months. | Present Values. |
| :---: | :---: |
| 1 | 0.9926908 |
| 2 | 0.9854349 |
| 3 | 0.9782321 |
| 4 | 0.9710818 |
| 5 | 0.9639839 |
| 6 | 09569378 |
| 7 | 0.9499433 |
| 8 | 0.9429998 |
| 9 | 0.9361072 |
| 10 | 0.9292650 |
| 11 | 0.9224722 |
| 12 | 0.9157301 |

TABLE IV.
The present value of an Instal. ment of \$1, payable at the end of each month during the named number of months.

| Months. | Present Values. |
| :---: | :---: |
| 1 | 0.992691 |
| 2 | 1.978126 |
| 3 | 2.956358 |
| 4 | 3.927440 |
| 5 | 4.891423 |
| 6 | 6.848361 |
| 7 | 6.798305 |
| 8 | 7.741304 |
| 9 | 8.677412 |
| 10 | 9.606677 |
| 11 | 10.529149 |
| 12 | 11.444879 |

## Interest 9 per Cent. per Annum, Payable Half- fearly.

TABLE VI.

TABLE V.
Amount of \$1 in any number of months from 1 to 12.

| Months. | Amounts. |
| :---: | :---: |
| 1 | 1.007363 |
| 2 | 1.014780 |
| 3 | 1.022252 |
| 4 | 1.029779 |
| 5 | 1.037362 |
| 6 | 1.045000 |
| 7 | 1.052695 |
| 8 | 1.060446 |
| 9 | 1.068254 |
| 10 | 1.076119 |
| 11 | 1.084044 |
| 12 | 1.092025 |

Amount at the end of any number of months, from 1 to 12, of a monthly Instalment of \$1, paid at the end of each month during that period.

| Months. | Amounts. |
| :---: | :---: |
| 1 | 1.000000 |
| 2 | 2.007363 |
| 3 | 3.022143 |
| 4 | 4.044395 |
| 5 | 5.074174 |
| 6 | 6.111536 |
| 7 | 7.156536 |
| 8 | 8.209231 |
| 9 | 9.269677 |
| 10 | 10.337931 |
| 11 | 11.414050 |
| 12 | 12.498094 |

Intrrest 9 per Cent. per Annum, Payable Half-fearly.

TABLE VIII.
Present value of $\$ 1$ due at the end of any number of years from 1 to 20.

## TABLE VII.

Amount at the end of any number of guarters, from 1 to 4, of a quarterly Instalment of \$1, paid at the end of each quarter during that period.


| Yrs. | Present Values. | Yrs. | Present Values. |
| :---: | :---: | :---: | :---: |
| 1 | 0.9157300 | 11 | 0.3797009 |
| 2 | 0.8385613 | 12 | 0.3477035 |
| 3 | 0.7678957 | 13 | 0.3184025 |
| 4 | 0.7031851 | 14 | 0.2915707 |
| 5 | 0.6439277 | 15 | 0.2670000 |
| 6 | 0.5896639 | 16 | 0.2444999 |
| 7 | 0.5399729 | 17 | 0.2238959 |
| 8 | 0.4944693 | 18 | 0.2050282 |
| 9 | 0.4528004 | 19 | 0.1877504 |
| 10 | 0.4146429 | 20 | 0.1719287 |

Interest 10 per Oent. per Annum, Payable Malf-yearly.

## TABLE I.

Instalments to repay a Loan of $\$ 1000$, in the named number of years, payable

| Years. | Yearly. | IIalf-yearly. | Quarterly. | Monthly. | Years. |
| :---: | ---: | :---: | :---: | :---: | :---: |
| 1 | 1102.50 | 537.81 | 265.63 | 87.83 | 1 |
| 2 | 578.13 | 282.02 | 139.29 | 46.06 | 2 |
| 3 | 403.89 | 197.02 | 97.31 | 32.18 | 3 |
| 4 | 317.18 | 154.73 | 76.42 | 25.27 | 4 |
| 5 | 265.49 | 129.51 | 63.97 | 21.15 | 5 |
| 6 | 231.30 | 112.83 | 55.73 | 18.43 | 6 |
| 7 | 207.10 | 101.03 | 49.90 | 16.50 | 7 |
| 8 | 189.16 | 92.27 | 45.58 | 15.07 | 8 |
| 9 | 175.37 | 85.55 | 42.26 | 13.97 | 9 |
| 10 | 164.50 | 80.25 | 39.64 | 13.11 | 10 |
| 11 | 155.74 | 75.98 | 37.53 | 12.41 | 11 |
| 12 | 148.57 | 72.48 | 35.80 | 11.84 | 12 |
| 13 | 142.61 | 69.57 | 34.36 | 11.36 | 13 |
| 14 | 137.61 | 67.13 | 33.16 | 10.96 | 14 |
| 15 | 133.36 | 65.06 | 32.13 | 10.63 | 15 |
| 16 | 129.73 | 63.28 | 31.26 | 10.34 | 16 |
| 17 | 126.60 | 61.76 | 30.51 | 10.09 | 17 |
| 18 | 123.89 | 60.44 | 29.85 | 9.87 | 18 |
| 19 | 191.54 | 59.29 | 29.28 | 9.68 | 19 |
| 20 | 119.47 | 58.28 | 28.79 | 9.52 | 20 |

Nominal Rates of Interest : 10 per cent. per annum, payable half-yearly; 9.86304 per cent. per annum, payable quarterly ; 9.71788 per cent. per annum, payable monthly.

Actual Rates: 10.25 per cent. per annum; 5 per cent. per half-year 2.46591 per cent. per quarter ; 0.81649 per cent. per month.

Interest 10 fer Cent. per Annud, Payable Half-Yearly

TABLE II.
Present Value of Instalment of $\$ 1$ payable

| Years. | Yearly. | Half-Yearly. | Quarterly. | Monthly. | Years. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.90703 | 1.8594 | 3.7647 | 11.3867 | 1 |
| 2 | 1.72973 | 3.5460 | 7.1795 | 21.7147 | 2 |
| 3 | 2.47595 | 5.0757 | 10.2767 | 31.0826 | 3 |
| 4 | 3.15279 | 6.4632 | 13.0860 | 39.5795 | 4 |
| 5 | 3.76670 | 7.7217 | 15.6342 | 47.2865 | 5 |
| 6 | 4.32354 | 8.8632 | 17.9454 | 54.2769 | 6 |
| 7 | 4.82860 | 9.8986 | 200417 | 60.6174 | 7 |
| 8 | 5.28672 | 10.8378 | 21.9432 | 66.3685 | 8 |
| 9 | 5.70224 | 11.6896 | 2R.6679 | 71.5548 | 9 |
| 10 | 6.07913 | 12.4622 | 25.28:2 | 76.3163 | 10 |
| 11 | 6.42098 | 12.1630 | 26.6511 | 80.6078 | 11 |
| 12 | 6.78104 | 13.7986 | 279881 | 84.5003 | 12 |
| 13 | 7.01229 | 14.3752 | 29.1054 | 88.0310 | 13 |
| 14 | 7.26738 | 14.8981 | 30.1642 | 91.2334 | 14 |
| 15 | 7.49876 | $15 \quad 3795$ | 31.1245 | 94.1380 | 15 |
| 16 | 7.70862 | 15.8027 | 31.9956 | 96.7726 | 16 |
| 17 | 7.89898 | 16.1929 | 32.7857 | 99.1623 | 17 |
| 18 | 8.07163 | 16.5469 | 33.5023 | 101.3298 | 18 |
| 19 | 8.22824 | 16.8679 | 34.1523 | 103.2958 | 19 |
| 20 | 837029 | 17.1591 | 34.7419 | 105.0790 | 20 |

Table III.
Present value of $\$ 1$ due after any number of months from
1 to 12.


## TABLE IV.

The present value of an Instalmene of $\$ 1$, payable at the end of each month during the named number of months.

| Months. | Present Values. |
| :---: | :---: |
| 1 | 0.991901 |
| 2 | 1.975769 |
| 3 | 2.951669 |
| 4 | 3.919666 |
| 5 | 4.879823 |
| 6 | 5.832203 |
| 7 | 6.776871 |
| 8 | 7.713899 |
| 9 | 8.643317 |
| 10 | 9.565219 |
| 11 | 10.479654 |
| 12 | 11.386683 |

Interest 10 per Cent. per Annum, Payable Half-yearly.

TABLE $V$.
Amount of $\$ 1$ in any number of monthe from 1 to 12.

| Months. | Amounts. | monthly instalment of :1 1 ut the end of cach month dur that perioil. |  |
| :---: | :---: | :---: | :---: |
| 1 | 1.008165 | Months. | Amounts. |
| 2 | 1016397 | 1 | 1.006000 |
| 3 | 1.024695 | 2 | 2.008165 |
| 4 | 1.038062 | 3 | 3.024562 |
| 5 | 1.041496 | 4 | 4.049257 |
| 6 | 1.050006 | 5 | 5.082319 |
| 7 | 1.058573 | $\bullet 6$ | 6.123815 |
| 8 | 1.067216 | 7 | 7.173815 |
| 9 | 1.075930 | 8 | 8.232388 |
| 10 | 1.0847 .4 | 9 | 9299604 |
| 11 | 1.093571 | 10 | 10.875534 |
| 12 | 1.102500 | 11 | 11.460248 |
|  |  | 12 | 12.553819 |

## Interest 10 per Cent. per Annuy, Payable Halffyearly.

## TABLE VIII.

Present value of $\$ 1$ due at the end of any

TABLE VII.
Amount at the end of any number of quarters from 1 to 4 of a quarterly instalment of $\$ 1$, paid at the end of each quarter during that period.

| Qrs. | Amounts. |
| :---: | :---: |
| 1 | 1.000000 |
| 2 | 2.024695 |
| 3 | 3.074695 |
| 4 | 4.150624 |

number of years, from 1 to 20.

| Yrs. | Present Values. | Yrs. | Present Values. |
| :---: | :---: | :---: | :---: |
| 1 | 0.9070295 | 11 | 0.3418409 |
| 2 | 0.8227025 | 12 | 0.3100679 |
| 3 | 0.7462154 | 15 | 0.2812407 |
| 4 | 0.6768394 | 14 | 0.2550936 |
| 5 | 0.6139132 | 15 | 0.2318774 |
| 6 | 0.5568374 | 16 | 0.2098662 |
| 7 | 0.5050679 | 17 | 0.1903548 |
| 8 | 0.4581115 | 18 | 0.1726574 |
| 9 | 0.4155206 | 19 | 0.1566054 |
| 10 | 0.3768895 | 20 | 0.1420457 |

Interest 11 per Cent. per Annum, Payaple Malf-yearly.

> TABLE I.
> Instalments to repay a Loan of $\leqslant 1000$ in the named number of years, payable

| Years. | Yearly. | Half-yearly. | Quarterly. | Monthly. | Years. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 1113.03 | 541.62 | 267.19 | 88.27 | 1 |
| 2 | 586.29 | 285.30 | 140.74 | 46.50 | 2 |
| 3 | 411.37 | 20018 | 98.75 | 32.63 | 3 |
| 4 | 324.42 | 157.87 | 77.88 | 25.73 | 4 |
| 5 | 272.64 | 132.67 | 65.45 | 21.63 | 5 |
| 6 | 238.44 | 116.03 | 57.24 | 18.91 | 6 |
| 7 | 214.30 | 104.28 | 51.45 | 17.00 | 7 |
| 8 | 196.43 | 95.59 | 47.16 | 15.58 | 8 |
| 9 | 182.74 | 88.92 | 43.87 | 14.50 | 9 |
| 10 | 171.97 | 83.68 | 41.28 | 13.64 | 10 |
| 11 | 163.32 | 79.48 | 39.21 | 12.96 | 11 |
| 12 | 156.26 | 76.04 | 37.51 | 12.40 | 12 |
| 13 | 150.42 | 73.20 | 36.11 | 11.93 | 13 |
| 14 | 145.53 | 70.82 | 34.94 | 11.54 | 14 |
| 15 | 141.40 | 68.81 | 33.95 | 11.22 | 15 |
| 16 | 137.88 | 67.10 | 33.10 | 10.94 | 16 |
| 17 | 134.87 | 65.63 | 32.38 | 10.70 | 17 |
| 18 | 132.28 | 64.37 | 31.76 | 10.49 | 18 |
| 19 | 130.03 | 63.28 | 31.22 | 10.32 | 19 |
| 20 | 128.07 | 62.32 | 30.75 | 10.16 | 20 |

Nomnal Rate of Interest : 11 per cent. per annum payable half-yearly; 10.85276 per cent. per annum payable quarterly; 10.75608 per cent. per annum payable monthly.

Actual Rate: 11.3025 per cent. per annum ; $5 \frac{1}{2}$ per cent. per half-year; 2.71319 per cent. per quarter ; 0.80634 per cent. per month.

Interest 11 per Cent. per Annum, Payable Malf-yearly.

TABLE II.
Present Value of Instalment of \$1 payable

| Years | Yearly. | Half-Yearly. | Quarterly. | Monthly. | Years. |
| ---: | ---: | :---: | :---: | :---: | :---: |
| 1 | 0.89845 | 1.8463 | 3.7427 | 11.8291 | 1 |
| 2 | 1.70567 | 3.5052 | 7.1024 | 21.5078 | 2 |
| 3 | 2.43092 | 4.9955 | 10.1266 | 30.6529 | 3 |
| 4 | 3.08252 | 6.3345 | 12.8410 | 38.8693 | 4 |
| 5 | 3.66795 | 7.5376 | 15.2798 | 46.2514 | 5 |
| 6 | 4.19393 | 8.6185 | 17.4709 | 52.8838 | 6 |
| 7 | 4.66650 | 9.5897 | 19.4395 | 58.8427 | 7 |
| 8 | 5.09108 | 10.4622 | 21.2082 | 64.1965 | 8 |
| 9 | 5.47254 | 11.2461 | 29.7973 | 69.0067 | 9 |
| 10 | 5.81527 | 11.9504 | 24.2250 | 73.3284 | 10 |
| 11 | 6.12320 | 12.5832 | 25.5077 | 77.2112 | 11 |
| 12 | 6.39986 | 13.1517 | 26.6602 | 80.6997 | 12 |
| 13 | 6.64841 | 13.6625 | 27.6957 | 83.8340 | 13 |
| 14 | 6.87174 | 14.1214 | 28.6260 | 86.6500 | 14 |
| 15 | 7.07238 | 14.5337 | 29.4618 | 89.1801 | 15 |
| 16 | 7.25265 | 14.9042 | 30.2128 | 91.4532 | 16 |
| 17 | 7.41461 | 15.2370 | 30.8875 | 93.4955 | 17 |
| 18 | 7.56013 | 15.5361 | 31.4937 | 95.3304 | 18 |
| 19 | 7.69087 | 15.8047 | 32.0883 | 96.9790 | 19 |
| 20 | 7.80833 | 16.0461 | 32.5276 | 98.4601 | 20 |

Interest 11 per Cent. per Annum, Payable Maly-yearly.

TABLE 11 .
Present value of $\$ 1$ dive after. ann, momber of months firom 1 to 12.

| Months. | Present Value. |
| :---: | :---: |
| 1 | 0.9911162 |
| 2 | 0.9823114 |
| 3 | 0.9785848 |
| 4 | 0.9649356 |
| 5 | 0.9563693 |
| 6 | 0.9478673 |
| 7 | 0.9394467 |
| 8 | 0.9311009 |
| 9 | 0.9298292 |
| 10 | 0.9146310 |
| 11 | 0.9065050 |
| 12 | 0.8984524 |

TABLE IV.
The present value of an Instalment of \$1, payable at the end of eachmonth churing the named member of months.

| Months. | Present Value. |
| :---: | :---: |
| 1 | 0.991110 |
| 2 | 1.978428 |
| 3 | 2.947012 |
| 4 | 3.911948 |
| 5 | 4.868311 |
| 6 | 5.816179 |
| 7 | 6.755625 |
| 8 | 7.686726 |
| 9 | 8.609555 |
| 10 | 9.524186 |
| 11 | 10.430692 |
| 12 | 11.329144 |

Interest 11 per Cent. per Annum, Payable Halfyearly.

TABLE VI.

TABLEV.
Amount of $\$ 1$ in any mumber of months from 1 to 12.

| Months. | Amounts. |
| :---: | :---: |
| 1 | 1.008963 |
| 2 | 1.018008 |
| 3 | 1.027132 |
| 4 | 1.036338 |
| 5 | 1.045628 |
| 6 | 1.055000 |
| 7 | 1.064456 |
| 8 | 1.073997 |
| 9 | 1.083624 |
| 10 | 1.093327 |
| 11 | 1.103137 |
| 12 | 1.113095 |

Amonnt at the end of any number. of monthes, from 1 to 12 , of a month!y Instalment of \$1, paid at the end of each month during that period.

| Months. | Amounts. |
| :---: | :---: |
| 1 | 1.000000 |
| 1 | 2.008963 |
| 9 | 3.026971 |
| 3 | 4.054103 |
| 4 | 5.090441 |
| 5 | 6.136069 |
| 6 | 7.191069 |
| 7 | 8.255525 |
| 8 | 9.329522 |
| 9 | 10.413146 |
| 10 | 11.506483 |
| 12 | 12.600620 |

Interest 11 per Cent. per Annum, Payable Half-yearly.

TABLE VIII.
Present value of \$1 due at the end of any number of years from 1 to 20 .

| Yrs. | Present Values. | Yrs. | Present Values. |
| :---: | :---: | :---: | :---: |
| 1 | 0.8984524 | 11 | 0.3079256 |
| 2 | 0.8072162 | 12 | 0.2766566 |
| 3 | 0.7252458 | 13 | 0.2485627 |
| 4 | 0.6515982 | 14 | 0.2238218 |
| 5 | $0.585431) 5$ | 15 | 0.2006440 |
| 6 | 0.5259816 | 16 | 0.1802691 |
| 7 | 0.4725693 | 17 | 0.1619632 |
| 8 | 0.4245811 | 18 | 0.1455162 |
| 9 | 0.3814659 | 19 | 0.1307394 |
| 10 | 0.3427290 | 20 | 0.1174631 |

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Interest 12 fer Cent. pre Annum, Payable Half-yearify.

TABLE I.
Instalments to repay a L.orm of $\$ 1000$, in the named number. of years, payatle

| Years. | Yearly. | Half-yearly. | Quarterly. | Monthly. | Years. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 1123.60 | 545.44 | 268.75 | 88.72 | 1 |
| 2 | 594.50 | 288.60 | 142.20 | 46.94 | 2 |
| 3 | 418.93 | 203.37 | 100.21 | 33.08 | 3 |
| 4 | 831.74 | 161.04 | 79.35 | 26.20 | 4 |
| 5 | 279.89 | 135.87 | 66.95 | 22.10 | 5 |
| 6 | 215.72 | 119.28 | 58.77 | 19.40 | 6 |
| 7 | 221.63 | 107.59 | 53.01 | 17.50 | 7 |
| 8 | 203.85 | 98.96 | 48.76 | 16.10 | 8 |
| 9 | 190.96 | 92.86 | 45.51 | 15.03 | 9 |
| 10 | 179.61 | 87.19 | 42.96 | 14.19 | 10 |
| 11 | 171.03 | 83.05 | 4092 | 13.51 | 11 |
| 12 | 161.14 | 79.68 | 39.26 | 12.96 | 12 |
| 13 | 158.43 | 76.91 | 3790 | 12.51 | 13 |
| 14 | 153.66 | 74.60 | 36.76 | :2.14 | 14 |
| 15 | 149.66 | 72.65 | 35.80 | 11.82 | 15 |
| 16 | 146.27 | 71.01 | 34.99 | 11.55 | 16 |
| 17 | 143.38 | 6960 | 34.30 | 11.32 | 17 |
| 18 | 140.90 | 68.40 | 83.70 | 11.13 | 18 |
| 19 | 138.76 | 67.30 | 33.19 | 10.96 | 19 |
| $\underline{0}$ | 136.91 | 66.47 | 32.75 | 10.81 | 20 |

Nominal Rates of Interest: 12 per cent per annm, payable half-yearly; 11.8252 per cent. per amum, payablequarterly; 11.71056 per cent. per annum, payable monthly.

Actual Rates: 12.36 per cent. per annum; 6 per cent. per half-year; 2.9563 per cent. per quarter; 0.97588 per cent. per month.

Interest 12 per Cent. per Annum, Payable Half-yearly.

TABLE II.
Present Value of Instalment of \$1 payable

| Years. | Yearly. | Half-Yearly. | Quarterly. | Monthly. | Years. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.89000 | 1.8334 | 3.7210 | 11.2722 | 1 |
|  | 1.68209 | 3.4651 | 7.0326 | 21.8045 | 2 |
| 3 | 2.38705 | 4.9173 | 9.9800 | 20.2332 | 3 |
| 4 | 3.01446 | 6.2098 | 12.6032 | 38.1797 | 4 |
| 5 | 3.57286 | 7.3601 | 14.9378 | 45.2520 | 5 |
| 6 | 4.06983 | 8.3838 | 17.0155 | 51.5464 | 6 |
| 7 | 4.51213 | 9.2950 | 18.8648 | 57.1484 | 7 |
| 8 | 4.90577 | 10.1059 | 20.5106 | 62.1341 | 8 |
| 9 | 5.25612 | 10.8276 | 21.9753 | 66.5714 | 9 |
| 10 | 5.56792 | 11.4699 | 23.2789 | 70.5205 | 10 |
| 11 | 5.81543 | 12.0416 | 24.4392 | 74.0853 | 11 |
| 12 | 6.09241 | 12.5504 | 25.4717 | 77.1634 | 12 |
| 13 | 6.31222 | 13.0032 | 26.3908 | 79.9474 | 13 |
| 14 | 6.50785 | 13 | 4062 | 27.2087 | 82.4251 |
| 15 | 6.68196 | 13.7648 | 27.9366 | 84.6303 | 15 |
| 16 | 6.83691 | 14.0840 | 28.5845 | 86.5929 | 16 |
| 17 | 6.97483 | 14.3681 | 29.1611 | 88.3897 | 17 |
| 18 | 7.09757 | 14.6210 | 29.6742 | 89.8942 | 18 |
| 19 | 7.20681 | 14.8460 | 30.1509 | 91.2778 | 19 |
| 20 | 7.30403 | 15.0463 | 30.5874 | 92.5092 | 20 |

Interbst 12 per Cent. fer Annuar, Payable Halz-yearly.

TABLE III.
Present value of \$1 due after any number of months, from 1 to 12.

| Months. | Present Values. |
| :---: | :---: |
| 1 | 0.9903356 |
| 2 | 0.9807645 |
| 3 | 0.9712858 |
| 4 | 0.9618989 |
| 5 | 0.9526026 |
| 6 | 09433960 |
| 7 | 0.9342786 |
| 8 | 0.9252495 |
| 9 | 0.9163074 |
| 10 | 0.9074517 |
| 11 | 0.8986816 |
| 12 | 0.8899965 |

TABLE IV.
The present value of an Instal. ment of $\$ 1$, payable at the end of each month during the named momber of months.

| Months. | Present Values, |
| :---: | :---: |
| 1 | 0.990336 |
| 2 | 1.971100 |
| 3 | 2.942386 |
| 4 | 3.904285 |
| 5 | 4.856887 |
| 6 | 5.800283 |
| 7 | 6.734562 |
| 8 | 7.659812 |
| 9 | 8.576119 |
| 10 | 9.483571 |
| 11 | 10.382252 |
| 4 | 11.272249 |

Interest 12 per Cent. per Annum, Pafable Half-yearly.

TABLE VI.
TABLE V.
Amount of $\$ 1$ in any number of months, from 1 to 12.

| Months. | Amounts. |
| :---: | :---: |
| 1 | 1.009759 |
| 2 | 1.019612 |
| 3 | 1.029562 |
| 4 | 1.039610 |
| 5 | 1.049756 |
| 6 | 1.060000 |
| 7 | 1.070344 |
| 8 | 1.080789 |
| 9 | 1.091338 |
| 10 | 1.101987 |
| 11 | 1.112741 |
| 12 | 1.123600 |

Amount at the end of any number of months, from 1 to 12, of a Monthly Instalment of $\$ 1$, paid at the end of each month during that period.

| Months. | Amounts. |
| :---: | :---: |
| 1 | 1.000000 |
| 2 | 2.009759 |
| 3 | 3.029371 |
| 4 | 4.058933 |
| 5 | 5.098543 |
| 6 | 6.148299 |
| 7 | 7.208299 |
| 8 | 8.278643 |
| 9 | 9.359432 |
| 10 | 10.450770 |
| 11 | 11.552757 |
| 12 | 12.665498 |

Interest 12 per Cent. per Annum, Paynble Half-yearly.

TABLE VIII.
Present Value of \$1 due at the erd of any

TABLE VII.
Amount at the end of any number of quarters, from 1 to 4, of a quarterly Instalment of $\$ 1$, paid at the end of each quarter during that period.


Interest 13 per Cent. per Annum, Payable Half-yearly.

> TABLE I.
> Instalments to repay a Loan of $\$ 1000$ in the named number of years, payable

| Years. | Yearly. | Half-yearly. | Quarterly. | Monthly. | Years. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 1134.23 | 549.27 | 270.31 | 89.16 | 1 |
| 2 | 602.78 | 291.91 | 143.66 | 47.39 | 2 |
| 3 | 426.57 | 206.57 | 101.66 | 3354 | 3 |
| 4 | 339.15 | 164.24 | 80.83 | 26.66 | 4 |
| 5 | 287.26 | 139.11 | 68.46 | 22.58 | 5 |
| 6 | 253.11 | 122.57 | 60.32 | 19.90 | 6 |
| 7 | 229.10 | 110.94 | 54.60 | 18.01 | 7 |
| 8 | 211.41 | 102.38 | 50.39 | 16.62 | 8 |
| 9 | 197.94 | 95.86 | 47.18 | 15.56 | 9 |
| 10 | 187.42 | 90.76 | 44.67 | 14.74 | 10 |
| 11 | 179.02 | 86.70 | 42.67 | 14.88 | 11 |
| 12 | 172.22 | 83.40 | 41.05 | 13.54 | 12 |
| 19 | 166.64 | 80.70 | 39.72 | 13.10 | 13 |
| 14 | 162.01 | 78.46 | 38.61 | 12.74 | 14 |
| 15 | 158.14 | 76.58 | 37.69 | 12.43 | 15 |
| 16 | 154.87 | 75.00 | 36.91 | 12.18 | 16 |
| 17 | 152.10 | 73.66 | 36.25 | 11.96 | 17 |
| 18 | 149.74 | 72.52 | 85.69 | 11.77 | 18 |
| 19 | 147.72 | 71.54 | 35.21 | 11.62 | 19 |
| 20 | 145.99 | 70.70 | 34.79 | 11.48 | 20 |

Nominal Rates of Interest : 13 per eent. por anmm payable halfeycarly; 12.7956 yer cent. per annum payable quarterly ; 12.6612 per cent. per ansum payable monthly.

Actuál Rates: 13.4225 per cent. per annum ; $6 \frac{1}{2}$ per cent. per half-year; 3.1089 per cent. per quarter ; 1.0551 per cent. per month.

Interest 13 per Cent. per Annum, Payable Half-yearly.

TABLE II.
Present value of Instalment of $\$ 1$ payable

| Years. | Yearly. | Half.yearly. | Quarterly. | Monthly. | Years. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.88166 | 1.8206 | 3.6995 | 11.2160 | $\mathbf{1}$ |
| $\mathbf{1}$ | 1.65898 | 3.4258 | 6.9612 | 21.1047 | 2 |
| 3 | 2.34432 | 4.8410 | 9.8369 | 29.8231 | 3 |
| 4 | 2.94855 | 6.0888 | 12.3723 | 37.5098 | 4 |
| 5 | 3.48127 | 7.1888 | 14.6076 | 44.2869 | 5 |
| 6 | 3.95096 | 8.1587 | 16.5784 | 50.2619 | 6 |
| 7 | 4.36506 | 9.0138 | 18.3160 | 55.5299 | 7 |
| 8 | 4.73015 | 9.7678 | 19.8480 | 60.1744 | 8 |
| 9 | 5.05204 | 10.4825 | 21.1987 | 64.2693 | 9 |
| 10 | 5.33584 | 11.0185 | 22.3895 | 67.8796 | 10 |
| 11 | 5.58605 | 11.5352 | 23.4394 | 71.0627 | 11 |
| 12 | 5.80665 | 11.9907 | 24.3650 | 73.8691 | 12. |
| 13 | 6.00115 | 12.3924 | 25.1812 | 76.3433 | 13 |
| 14 | 6.17263 | 12.7465 | 25.9007 | 78.5248 | 14 |
| 15 | 6.32381 | 18.0587 | 26.5351 | 80.4481 | 15 |
| 16 | 6.45711 | 13.3339 | 27.0944 | 82.1438 | 16 |
| 17 | 6.57463 | 13.5766 | 27.5875 | 83.6388 | 17 |
| 18 | 6.67824 | 137906 | 28 | 0223 | 84.9569 |
| 19 | 6.76959 | 13.9792 | 28 | 4056 | 86.1191 |
| 20 | 6.85013 | 14.1455 | 28.7436 | 87.1437 | 20 |

Interest 13 per Cent. per Annum, Payable Malf-yearly.

## TABLE III.

Present value af $\$ 1$ due after any number of months, from 1 to 12.

| Months. | Present Value. |
| :---: | :---: |
| 1 | 0.9895592 |
| 2 | 0.9792270 |
| 3 | 0.9690082 |
| 4 | 0.9588859 |
| 5 | 0.9488743 |
| 6 | 0.9389672. |
| 7 | 0.9291635 |
| 8 | 0.9194623 |
| 9 | 0.9098622 |
| 10 | 0.9003621 |
| 11 | 0.8909618 |
| 12 | 0.8816594 |

TABLE IV.
The present value of an Instalmont of \$1, payable at the end or each mon th during the named number of mouths.

| Months. | Present Values. |
| :---: | :---: |
| 1 | 0.989559 |
| 2 | 1.968786 |
| 3 | 2.937789 |
| 4 | 3.896675 |
| 5 | 4.845550 |
| 6 | 5.784517 |
| 7 | 6.713680 |
| 8 | 7.633143 |
| 9 | 8.543005 |
| 10 | 9.443367 |
| 11 | 10.334329 |
| 12 | 11.215988 |

Interest 13 per Cent. per Annum, Payable Inalf-yearly.

## TAbLE V.

Amount of $\$ 1$ in amy mumber of moithes from 1 to 12.

| Months. | Amounts. |
| :---: | :---: |
| 1 | 1.010551 |
| 2 | 1021213 |
| 3 | 1.031989 |
| 4 | 1.042976 |
| 5 | 1.053981 |
| 6 | 1.065000 |
| 7 | 1.076237 |
| 8 | 1.087593 |
| 9 | 3.099068 |
| 10 | 1.110665 |
| 11 | 1.122383 |
| 12 | 1.134225 |

TABLE VI.
Amonnt at the end of any mumber. of mouths, firom 1 to 12 , of a Monthly Instalment of \& 1, paid at the end of ecrech month during that period.

| Months. | Amounts. |
| :---: | :---: |
| 1 | 1.000000 |
| 2 | 2.010551 |
| 3 | 3.031764 |
| 4 | 4.063753 |
| 5 | 5.106629 |
| 6 | 6.160510 |
| 7 | 7.225510 |
| 8 | 8.301747 |
| 9 | 9.389340 |
| 10 | 10.488408 |
| 12 | 11.599073 |
| 12.721456 |  |

Interest 13 per Cent: per Annum, Payable Malf-yeably.

TABLE VIII.
Prescent value of $\$ 1$ due at the eml of any number of years from 1 to 20.
TABLE VII.
Amount at the end of any mumber of quarters, from ${ }^{1}$ to 4, of a quarterly Instalment of \$1, paid at the end of cach quarter during that period.

| Qrs. | Amounts. |
| :---: | :---: |
| - |  |
| 1 | 1.000000 |
| 2 | 2.031989 |
| 3 | 3.096989 |
| 4 | 4.196057 |


| Yrs. | Present Values. | Yrs. | Present Values. |
| :---: | :---: | :---: | :---: |
| 1 | 0.581659 | 11 | 0.250212 |
| 2 | 0.777523 | 12 | 0.220602 |
| 3 | 0.685334 | 13 | 0.194496 |
| 4 | 0.604231 | 14 | 0.171479 |
| 5 | 0.532726 | 15 | 0.151186 |
| 6 | 0.469683 | 16 | 0.133295 |
| 7 | 0.414100 | 17 | 0.117520 |
| 8 | 0.365095 | 18 | 0.103611 |
| 9 | 0.321890 | 19 | 0.091351 |
| 10 | 0.283797 | 20 | 0.080541 |

## APPENDIX.

Note I.-If $i$ is the yearly rate of interest per unit, and $R=$ $1+i$, the amount ( $M$ ) of a sum $P$ in $n$ years is given by

$$
M=P R^{n}
$$

and the present value $(P)$ of a sum ( $M$ ) due $n$ years hence is given by

$$
P=M R^{-n} .
$$

In these formulas $n$ may be integral or fractional ; thus, the amount of 1 in the $p$ th part of a year is $\Gamma^{\frac{1}{p}}$, and the rate of interest per the $p$ th part of the year is $R^{\frac{1}{p}}-1$.
Hence the rate per half-year is $R^{\frac{1}{2}}-1$.

$$
\begin{array}{ll}
\text { " } & \text { quarter is }{R^{\frac{1}{4}}}-1 \\
\text { " } & \text { " } \\
\text { month is } R^{\frac{1}{12}}-1
\end{array}
$$

But if $i$ is the nominal yearly rate of interest per unit, payable $p$ times a year, meaning thereby that $\frac{i}{p}$ is the interest payable at the end of each $p$ th part of a year, then the amount of 1 in a year is $\left(1+\begin{array}{l}i \\ p\end{array}\right)^{p}$, and the true yearly rate of interest is $\left(1+\frac{i}{p}\right)^{p}-1$.

Note II.-If $A$ is an instalment payable at the end of each year for $n$ years from the present time, and $P$ its present value, then

$$
P=A . \frac{1-R^{-n}}{R-1}
$$

in which formula $n$ is necessarily a whole number.
If $A$ is payable at the end of each of $p$ equal intervals in a year, and the payments continue for $n$ years, then

$$
P=A . \frac{1-R^{-n}}{R^{\frac{1}{p}}-1}
$$

where $n$ may be fractional, but such that the whole time contains an exact number of the intervals.

Thus if the instalment $A$ is payable

$$
\begin{aligned}
& \text { laalf-yearly, then } P=A . \quad \frac{1-R^{-n}}{R^{\frac{1}{2}}-1} \\
& \text { quarterly, } \quad \text { " } P=A . \quad \frac{1-R^{-n}}{R^{\frac{1}{4}}-1} \\
& \text { monthly, } \quad \text { " } P=A . \quad \frac{1-R^{-n}}{R^{1}{ }^{12}-1}
\end{aligned}
$$

These formulas give the relation between the loan and the instalment, and also give the present value of an instalment having any exact number of periods t r run.

If the time to rum is not an exact number of periods, the present value will be found by taking the present value for the whole number of periods less than the given period, discounting this for the broken interval, and adding the present value of the instalment payable at the end of the broken period. Thas, if a yearly instal. ment $A$ has $n$ years and $m$ months to run, its present value is given by

$$
P=A R^{-\frac{n}{12} \cdot} \frac{1-R^{-n}}{R-1}+A R^{-\frac{m}{12}}
$$

Notn III.-If $v$ is the present value of 1 due at the end of any interval, and $A$ is an instalment payable at the end of each of $u$ such intervals, then

$$
P=A\left(v+v^{2}+v^{3} \perp \ldots \text { to } n \text { terms. }\right)
$$

If the interval is a year, than $v=R^{-}$; if a half year, $v=R^{-\frac{1}{2}}$; if a quarter, $v-R^{-\frac{1}{2}}$; if a month, $v=R^{-\frac{1}{1} \Sigma}$

Tables III. and VIII. give the values of $v$ for months and years.
Tables II. and IV. have been formed by the addition of the $v$ 's.
Table I has been formed by taking the reciprocals of the numbers in Table II., and are given exact to the next cent above the true value when the difference exceeds ${ }_{3} \frac{1}{0}$ th of a cent. In all the other tables, the values are made true to the nearest decimal.

Note IV.-When the loan ( $P$ ), instalment (A), and time are given, and it is required to find the rate of interest, $R$ must be obtained from the equation

$$
i=A \cdot \frac{1-R^{-n}}{h-1}
$$

where $n$ is the number of payments at the end of each interval, and $R=1+$ interest per unit for one interval $=1+i$.

The solution of this equation, ly Iorner's method, theugh theoretically possible in all cases, becomes impracticable when $u$ is not a small number, on account of the length of the operations, and in general ityis better to proceed by Newton's approximation, which, however, converges but slowly and is often very troublesome to apply. Several approximate formulas have been devised to sare this labor, of which the following may be noticed.
(i.) Ialley's formula.

Calculating $\left(\frac{n A}{P}\right)^{\frac{2}{n+1}}-1$, and calling this value $\beta$, then

$$
i=\frac{6}{n-1}\left(1-\sqrt{1-\frac{n-1}{3} \beta}\right)
$$

(ii.) Using the same notation,

$$
i=\beta+\frac{1}{1 \frac{1}{2}} \overline{n-1} \beta^{2}+\frac{1}{7^{2}} \bar{n}-1^{2} \beta^{3} .
$$

(iii.) Baily's formula with the same notation: -

$$
i=\frac{(12-\overline{n-1} \beta) \beta}{12-2 \overline{n-13}}
$$

Of these formulas, (i.) fails altogether when $\beta$ exceeds $\frac{3}{n-1}$ and becomes less correct the nearer $\beta$ approaches to this limit; (ii.) is of more easy application than (i.), as the successive terms are readily found by aid of a table of squares and cubes; it becomes more and more erroneous vader the same circumstances as (i.), the degree of error being indicated by the less convergence of the second and third terms relatively to the first term. (iii.) is also a modification of (i.); it fails when $\beta$ gets beyond $\frac{6}{n-1}$ and becomes less correct as $\beta$ approaches this lin it. It is more troublesome to work than either (i.) or (ii.), but its great disadvantage is that it gives no indication in itself of its degree of error.

None of the three give good approximations when the period o: the rate is large. For example, $A=1, P=9.99927484, n=x 100$, $\beta=04762$. Here (i.) fails; in (ii.) the terms diverge; (iii.) gives $i=13477$, which is quite astray, the true value oeing $i=$ - 10000.

- The method of "reversion of series" may also be used for the solution, but it is liable to the same objections as above unless the series is carried to so large a number of terms as to render the operation too laborious to be practically useful.

Note V.-The foregoing Tables will be found useful in enabling. Building Socicties to keep a proper account with each borrower. These accounts should be kept on the principle that whenever an instalment is paid, the borrower is charged with interest at the Society's rate on the sum in his possession since the date of the last payment, and credited with the amount paid; or, which comes to the samo thing, instead of balancing an account whenevel an instalment is paid, the borrower may at the end of the year be debited with the amount due at the beginning of the year, with interest on the same, and credited with the instalments paid in this interval with interest from the times of payment. This method, which is the one to be adopted in practice, is illustrated in the following examples. The multiplications that oceur in the calculations are most conveniently performed by means of the Arithmometer of M. Thomas, of Colmar, France, an instrument which should be in the possession of every Building Society.* In these examples the books of the Society are closed on the first day of December in each year, payments made on that day being included in the accounts, and all loans are supposed to be contracted on the first day of a month.

[^0]Example 1.-August 1,1872 . A. B. borrows $\$ 1,000.00$, to be re-paid in 6 years by yearly instalments of $\$ 231.30$ cach.

The amounts on the Dr. side are calculated by means of Table V. by multiplying the sum at the head of a column by the factor corresponding to the number of months between the dates at the head and foot of the column.

Thus in the first column 1,000 is multiplied by the factor 1.033062 corresponding to the interval 4 months, giving 1033.06 .

The amounts on the Cr . side are calculated in like manner.
Thus in the second column the instalment, 231.30, is multiplied by the same factor, giving 238.95.

No instalment having been paid before Dec. 1, 18ヶ2, the borrower is charged with $\$ 1,033.06$ in opening the account for the next year. The difference between $\$ 1,138.95$ and $\$ 238.95$ is $\$ 900.00$, the present value of the mortgage on Dec. 1,1873 , and this is the amount with which the borrower is properly charged in opening the account for the next year. The account is closed Aug. 1, 1878, when there is a difference of nine cents between the Cr. and Dr. sides. This difference arises from the fact that the instalment, $\$ 231.30$, is somewhat greater than the true valuc. If the more accurate valuc, $\$ 231.202$, be taken, the account will be found to balance exactly. Omitting dates, \&c., the account would then stand as follows:

Dr.

| $1,000.000$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $1,033.062$ |$\left|\frac{1,033.062}{1,138.951}\right| \frac{000.012}{992.263}\left|\frac{753.324}{830.540}\right| \frac{591.601}{652.240}\left|\frac{413.301}{455.664}\right| \frac{216.725}{231.292}$

$C r$.

| 0.000 | 231.292 | 231.292 | 231.292 | 231.292 | 231.292 | 231.292 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.000 | 238.939 | $\underline{288.939}$ | 238.939 | 238.939 | 238.939 | 231.292 |
| 1,033.062 | 900.012 | 753.324 | 591.601 | 413.301 | 216.725 | 0.000 |
| 1,033.062 | 1,138.951 | 992. 263 | 880.640 | 652.240 | 455.664 | 231.292 |

Example 2.-March 1, 1872. C. D. borrows $\$ 1,000.00$ to be repaid in 5 years by half-gearly instalments of $\$ 129.51$ each.

The amounts on the Dr. side aro calculated as in Example 1.
The amounts on the Cr. side are found by multiplying each instalment by the fuctor corresponding to the proper interval, and addin ${ }_{5}$ together the products so obtained.

Thus for 1873 the first instnlment is multiplied by tho factor for 9 months, and the second instalment by the factor for 3 months.

Example 3.-October 1, 1872. E. F. borrows $\$ 1,00000$ to be repaid in 3 years by quarterly instalments of $\$ 97.31$ ench.

The amounts on the Dr. side are calculated as in previous Examples.

The amounts on the Cr. side may be obtained by multiplying each instalment $\$ 97.31$ by the factor corresponding to the proper interval, and adding together the products so obtained.

Thus for 1873 the first instalment is multiplied by the factor for 11 months, the second by the factor for 8 months, the third by the factor for 5 months, and tho fourth by the factor for 2 months, thus giving 410.52.

But this result is more casily obtained with the aid of Table VII by multiplying the instalment by the factor corresponding to the number of payinents in Table VII, and then multiplying this result by the factor in Table V corresponding to the interval between the last payment and the end of the year.
Thus in the abjve example, the instalment 97.31 is multiplied by the factor 4.150624 in Table VII corresponding to four payments, and then by the factor 1.016597 in Table V, corresponding to the remaining period ${ }^{\circ}$ months, giving 410.52.

And in the last col $\quad 1875$ the amount of the instalments at date of last $\mathrm{pa}^{-}$, given at once from Table VII by multiplying the instal. . 77.31 by the factor corresponding to 4 payments, 4.150624, giving 403.90.

Example 4.-September 1, 1872. G. II. borrows $\$ 1,000.00$ to be repaid in 3 years by monthly instalments of $\$ 32.18$ each.

The amounts on the Dr. side are obtained as before.
The amounts on the Cr, side are obtained by means oi Table VI, by multiplying the instalment 32.18 by the factor corresdonding to as many months as there have bean instalments paid.

Thus in the first column 32.18 is multiplied by the factor 3.024562 corresponding to 3 months, giving 97.33 . In the second column 32.18 is multiplied by the factor 12.553810 correspondine to 12 months, giving 403.98 ; and in the fourth column 32.18 is multiplied by the factor 9.299604 corresponding to 9 months, giving 299.26.

As in the previous examples, the small difference between the final amounts on the two sides 290.20 and 298.91 arises from the fact that the instalment was only given to the nearest cent above the true value; if the more correct value 32.17235 had been used, the balance would have come out exact, the final sums on each side of the account being 299.1 ©口. In the great majority of cases a small balance will be found to tho adrantage of the society, which may be carried to Profit and Loss.



A．B．

| Prosent value of morlgage．．．． | $\begin{gathered} \text { 18ヶొ. } \\ \text { Aug. } 1 \ldots . . .81,000.00 \end{gathered}$ | $\begin{gathered} 1872 . \\ \text { Dec. } 1 \ldots . .81,033.00 \end{gathered}$ | $\begin{aligned} & 1873 . \\ & \text { De. } 1 \ldots . . \$ 900.00 \end{aligned}$ | $\begin{aligned} & 1874 . \\ & \text { Dec. } 1 \ldots . \ldots 788.80 \end{aligned}$ | $\begin{aligned} & 1875 . \\ & \text { Dee. } 1 \ldots . . .8591 .60 \end{aligned}$ | $\begin{aligned} & 1876 . \\ & \text { Dec. } 1 \ldots . \ldots 412.24 \end{aligned}$ | $\begin{aligned} & 1877 . \\ & \text { Dec. } 1 \ldots .8210 .65 \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Amount lo date ．． | Dec．1．．．．81，033．06 | $\begin{aligned} & 1873 . \\ & \text { Dec. } 1 \ldots . .81,188.95 \end{aligned}$ | $\begin{gathered} 1874 . \\ \text { Dec. } 1 \ldots . . \\ 290.25 \end{gathered}$ | $\stackrel{1875 .}{\text { Dec. } 1 \ldots . \ldots 830.51}$ | $\begin{aligned} & 1876 . \\ & \text { Dec. } 1 \ldots . .8652 .19 \end{aligned}$ | $\begin{aligned} & 1877 . \\ & \text { Dec, 1.... 8455. } 60 \end{aligned}$ | $\begin{aligned} & 1878 . \\ & \text { Aug. } 1 \ldots . . . \$ 231.21 \end{aligned}$ |
| Cr．A．B． |  |  |  |  |  |  |  |
| Instniment ．．．．．． | 1872． | $\begin{aligned} & 1873 . \\ & \text { Aug. } 1 \ldots . . \\ & \$ 231.30 \end{aligned}$ | $\stackrel{\text { 187.1. }}{\text { Aug. } 1 . . . .8231 .80}$ | $\begin{aligned} & 1875 . \\ & \text { Aug. } 1 \ldots . \ldots 231.30 \end{aligned}$ | $\begin{aligned} & 1876 . \\ & \text { Aug. } 1 . \ldots .8231 .80 \end{aligned}$ | $\stackrel{1877 .}{\text { Aug. } 1 \ldots . .8281 .80}$ | $\begin{aligned} & 1878 . \\ & \text { Aug. } 1 . . .8231 .30 \end{aligned}$ |
| Amount to date ．． <br> Balance ．．．．．．．．．． |  | Dec． $1 . . .$. ．．．．．．． \＄238．95 940.00 | Dec． $1 . . . .{ }^{\text {a }}$ 238．95 |  |  |  |  |
|  | \＄1，035 06 | \＄1，138．95 | \＄992．25 | \＄830．51 | \＄652．18 | 8455.60 | \＄251．30 |
| Dr． |  | C． D ． |  |  |  |  |  |
| $\left.\begin{array}{r} \text { Present value of } \\ \text { mortgage.... } \end{array}\right\}$ | $\begin{aligned} & 18,2 . \\ & \text { Mar. } 1 \ldots . \leqslant 1,000.00 \end{aligned}$ | $\begin{array}{cc} 1872 . \\ \text { Dec, } 1 \ldots . . & 8913.22 \end{array}$ | 1873. <br> Dee．1．．．．$\$ 707.85$ | $\begin{aligned} & \text { 187.1. } \\ & \text { Dec. } 1 \ldots . .5574 .50 \end{aligned}$ | $18 \% \%$ <br> Dec． 1 ．．．$\$ 361.84$ | $\begin{aligned} & 1876 . \\ & \text { Dee. } 1 \ldots . . .8120 .83 \end{aligned}$ |  |
| Amount to date ．．Dec．1．．．．81，0ヶ5．93 |  | $\begin{aligned} & 18 \text { is. } \\ & \text { Dec. } 1 \ldots . \ldots 1,059.90 \end{aligned}$ | $\begin{gathered} 1874 . \\ \text { Dec, } 1 \ldots . . . \$ 846.55 \end{gathered}$ | $\begin{aligned} & \text { 1875. } \\ & \text { Dec. } 1 \ldots \ldots 33.39 \end{aligned}$ | $\begin{aligned} & 1870 . \\ & \text { Dec. } 1 \ldots . \ldots 8398.38 \end{aligned}$ | $\begin{aligned} & 1877 . \\ & \text { Mnr. } 1 . . .8129 .45 \end{aligned}$ |  |
| Cr．C．D． |  |  |  |  |  |  |  |
| Instalment．．．．．．． | 1872. <br> Mar． $1 . . .$. <br> 1 | $\begin{array}{cc} 1873 . \\ \text { Mar. } 1 \ldots . & \\ \text { Sept. 1.... } & 129.51 \\ \hline \end{array}$ | $\begin{aligned} & 1874 . \\ & \text { Mar. } 1 \ldots .{ }^{2} 129.51 \\ & \text { Sept. } 1 . . . .129 .51 \end{aligned}$ | 1875.Mar． $1 \ldots . .8129 .51$Sept． $1 \ldots . .129 .51$ | $\begin{aligned} & 1870 . \\ & \text { Mar. } 1 \ldots . . \$ 199.51 \\ & \text { Sept. } 1 \ldots .129 .51 \end{aligned}$ | 187. <br> Mar．1．．．．8129．51 |  |
|  | Sept．1．．． 129.15 |  |  |  |  |  |  |
| Ameunt to dalo．． <br> Balance．．．．．．．．．．． |  | $\begin{array}{\|ccc\|} \hline \text { Yec. } 1 & \ldots . . & 8929.05 \\ \cdots . . & \frac{867.85}{\$ 1,039.90} \end{array}$ | $\begin{gathered} \text { Dec. } \left.1 \ldots . . \begin{array}{\|c} \$ 272.05 \\ \ldots 74.50 \\ \$ 8.10 .55 \end{array} \right\rvert\, \end{gathered}$ |  |  | Mar．1．．．．$\$ 129.51$ |  |
|  | ．．．．．．．．．．948．22 |  |  |  |  | ．．．．．．．．．． 0.00 |  |
|  | \＄1，075．93 |  |  |  | 8398.88 | \＄129．51 |  |


| $\left.\begin{array}{c}\text { Present value of } \\ \text { mortgage．．．．．}\end{array}\right\}$ | $\stackrel{1872 .}{\text { Oet. } 1 \ldots \$ 1,00) .00}$ | $\begin{aligned} & 1872 . \\ & \text { Dec. } 1 \ldots . \ldots 1,010.40 \end{aligned}$ | $\begin{aligned} & 1873 . \\ & \text { Dec. } 1 \ldots . \ldots 710.06 \end{aligned}$ | 1874. <br> Dec．1．．．．8372．32 |
| :---: | :---: | :---: | :---: | :---: |
| Amount to date ．． | ec． 1 ．${ }^{\text {s }} 1,416.411$ | $\stackrel{18 ヶ 3 .}{\text { Dee. } 1 . . .81,120.58}$ | $\begin{aligned} & \text { 184. } \\ & \text { Dec. } 1 . . . . \$ 782.84 \end{aligned}$ | $\stackrel{18 \% 5 .}{\text { Oct. } 1 . . . . \$ 408.86}$ |


| Cr． |  | E．F． |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Instalment | 1872. | 187.6 | 1874. | 1875. |
|  | 80.018 | Jan．1．．．． 397.31 | Jan．1．．．． 597.81 | Jan．1．．．．§97．81 |
|  |  | Apl．1．．．． 97.31 | Apl，1．．．． 97.31 | Apl．1．．．． 97.81 |
|  |  | Jnly 1．．．． 97.31 | July 1 ．．． 97.31 | July 1．．．． 97.31 |
|  |  | Oct．1．．． 97.81 | Oct．1．．．． 97.31 | Oct．1．．．． 97.81 |
| Amount to dnte． <br> Balanee $\qquad$ | ．\％80．00 | trec．1．．．\＄410．52 | 1）ee． 1 ．．\＄110．52 | Oct， $1 . . .8163 .90$ |
|  | ．1，016．40 | － 710.00 | ．．．．．．．．．．372．82 | 0.00 |
|  | \＄1，016．10 | \＄1，120．58 | \＄782．8．1 | \＄108．40 |



## I N D Fi X .

To tind the present value of a sum due after a number
of years.
p. 10; s. (7); Table VIII

To find the present value of a sum due after a number of months less than a year. p. 10; s. (7); Table III.

To find the present value of a sum due after a broken period of years and some moaths.
p. 10; s. (7); Tables III., VIII.

To find the amount, with interest, of a sum, after any number of monthe, from 1 to $12 . \quad$ p. 8; s. (5); Table V.

To find the amount, with interest, of a sum, after a period of years and some months.
p. 12; s. (9); Tables III., VIII., or V., VIII.
(Divide the sum by the factor corresponding to the number of year: in Table VIll.; then divide this quotient by the factor corresponding to the number of months in T'able 111., or multiply this quotient by the factor corresponding to the number of montlis in Table V.)

To find the yearly, half-yearly, quarterly, or monthly instalment required to repay a loan in a given number of years. p. 5 ; s. (1); Table I.

To find the present value of an instalment payable at the end of each year, half-year, quarter or month, during a given number of years.
p. 5; s. (2) ; Table II.

To find the present value of a yearly, half-yearly, or quarterly instalment, in payment of a loan having a broken period of years and some months to run.

First method (best) p. 6; s. (3); Tables II., III. Second method, p. 8; s. (5); Tables II., V

## INDEX.

To find the present value of a monthly instalment, in payment of a loan having a period of years and some months to run.

First method, p. 7 ; s. (4); Tables II., III., IV. Second method, p 9; s. (6); Tables II., V., VI.

To find the present value of an ordinary mortgage.
p. 10: s. (8); Tables II., III., VIII.

To find the reduction in the instalment or in the period to run, produced by the payment of an additional sum at any time during the period.

To find the rate of interest when the instalment, loan, and period are given.

$$
\text { p. } 13 \text {; s. (10); and Appendix, Note IV., p. } 46 .
$$

How the account of a borrower should be kept.
Appendix, Note V., p. 48.
es II., III., IV. les II., V., VI.
II., III., VIII. period
tional
12, 13; s. (9).
loan,
Note IV., p. 46.

Note V., p. 48.



[^0]:    * London agents: C. \& J. Layton, 150 Fleet Street. A 12-figure machine will be found sufficient. In multiplying a sum by a factor, it will be better to begin from the left of the multiplier, as follows: Having set the multiplicand with the buttons, raise the plate and carry it to the right, so as to leave at least one hole to the left of the left-hand button. Multiply by the left hand figure of the multiplier; raise the plate and carry it one stage to the left ; then multiply by the next figure, and so oll. In this way the operation can be stopped without taking in unnceessary figures, when sufflefent accuracy has been attaised.

