

CIHM/ICMH Microfiche Series.

N,

CIHM/ICMH Collection de microfiches.



Canadian Institute for Historical Microreproductions / Institut canadien de microreproductions historiques

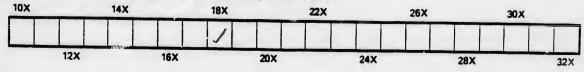


# Technical and bibliographic Notes/Notes techniques et bibliographiques

The Institute has attempted to obtain the best original cnpy available for filming. Features of this copy which may be bibliographically unique, which may alter any of the images in the reproduction, or which may significantly change the usual method of filming, are checked below. L'Institut a microfilmé le meilleur exemplaire qu'il lui a été possible de se procurer. Les détails de cet exemplaire qui sont peut-être uniques du point de vue bibliographique, qui peuvent modifier une image reproduite, ou qui peuvent exiger une modification dans la méthode normale de filmage sont indiqués ci-dessous.

	Coloured covers/		Coloured pages/
	Couverture de couleur		Pages de couleur
	Covers damaged/		Pages damaged/
	Couverture endommagée		Pages endommagées
	Covers restored and/or laminated/		Pages restored and/or laminated/
	Couverture restaurée et/ou pelliculée		Pages restaurées et/ou pelliculées
	Cover title missing/		Pages discoloured, stained or foxed/
	Le titre de couverture manque		Pages décolorées, tachetées ou piquées
	Coloured maps/		Pages detached/
	Cartes géographiques en couleur		Pages détachées
	Coloured ink (i.e. other than blue or black)/		Showthrough/
	Encre de couleur (i.e. autre que bleue ou noire)	$\checkmark$	Transparence
	Coloured plates and/or illustrations/		Quality of print varies/
	Planches et/ou illustrations en couleur		Qualité inégale de l'impression
	Bound with other material/		Includes supplementary material/
	Relié avec d'autres documents		Comprend du matériel supplémentaire
	Tight binding may cause shadows or distortion		Only edition available/
	along intericr margin/ La reliure serrée peut causer de l'ombre ou de la		Seule édition disponible
	distorsion le long de la marge intérieure		Pages wholly or partially obscured by errata
	Blank leaves added during restoration may		slips, tissues, etc., have been refilmed to
	appear within the text. Whenever possible, these have been omitted from filming/		ensure the best possible image/ Les pages totalement ou partiellement
	Il se peut que certaines pages blanches ajoutées		obscurcies par un feuillet d'errata, une pelure, etc., ont été filmées à nouveau de façon à
	lors d'une restauration apparaissent dans le texte, mais, lorsque cela était possible, ces pages n'ont		obtenir la meilleure image possible.
	pas été filmées.		
_	Additional comments:/		
	Commentaires supplémentaires:		

This item is filmed at the reduction ratio checked below/ Ce document est filmé au taux de réduction indiqué ci-dessous.



The copy filmed here has been reproduced thanks to the generosity of:

McLennan Library McGill University Montreal

uls

1u

difier

ine

age

ta

ure,

The images appearing here are the best quality possible considering the condition and legibility of the original copy and in keeping with the filming contract specifications.

Original copies in printed paper covers are filmed beginning with the front cover and ending on the last page with a printed or iliustrated impression, or the back cover when appropriate. Ail other original copies are filmed beginning on the first page with a printed or iliustrated impression, and ending on the last page with e printed or illustrated impression.

The last recorded frame "n each microfiche shall contain the symbol → (meaning "CON-TINUED"), or the symbol ♥ (meaning "END"), whichever applies.

Maps, plates, charts, etc., may be flimed et different reduction ratios. Those too large to be entirely included in one exposure are filmed beginning in the upper left hand corner, left to right end top to bottom, as many frames as required. The following diagrams illustrate the method:

1	2	3

L'axemplaire filmé fut reproduit grâce à la générosité de:

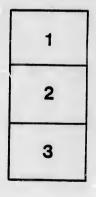
McLennan Library McGill University Montreal

Les images suivantes ont été reproduites avec le pius grand soln, compte tenu de la condition et de la netteté de l'exemplaire filmé, et en conformité avec les conditions du contrat de filmage.

Les exemplaires originaux dont la couverture en papier est imprimée sont filmés en commençant par le premier plat at en terminant soit par la dernière page qui comporte une ampreinte d'Impression ou d'iliustration, soit par le second plat, selon le cae. Tous les autres exemplaires originaux sont filmés en commençant par le première page qui comporte une emprainte d'Impression ou d'iliustration at on terminant par la dernière page qui comporte une talle empreinte.

Un des symboles suivants apparaîtra sur la dernière image de chaque microfiche, selon le cas: le symbole —> signifie "A SUIVRE", le symbole ▼ signifie "FIN".

Los cartes, planches, tableaux, etc., peuvent être flimée à des taux de réduction différents. Lorsque le document est trop grand pour être reproduit en un seul cliché, il est filmé à partir de l'angle supérieur gauche, de gauche à droite, et de haut en bas, en prenant le trombre d'images nécessaire. Les diagrammes suivants illustrent le méthode.



1	2	3
4	5	6

1 2287. Walkingame. Me .74 11 2H

# THE TUTOR'S ASSISTANT:

BEING A COMPENDIUM OF

# PRACTICAL ARITHMETIC.

## FOR THE USE OF

# SCHOOLS OR PRIVATE STUDENTS ;

### CONTAINING

- I. Arithmetic in Whole Numbers : the Rules of which are expressed in a clear, the utmost perspirately ; with involuconcise, and intelligible manner; and the operations illustrated by examples worked at length, and by numerons explanatory notes and observations; with an ample variety of examples for the exercise of Learners, calculated to initiate them in the Knowledge of Real Tables, adapted to the present Legisla-tive Regulations of Weights and Mea-
- sures and the modern practice of Trade. II. Vulgar Fractions; explained in an easy and familiar manner, in the practice of which the most elegant and abbreviated modes of operation are peculturly inculcated.
- tion, Evolution, Position, Progression, and the calculation of Interest and Annuities, on an extended scale,
- IV. Duodecimals : or the Multiplication of Feet and Inches; with numerous examples for practice, adapted to the various business of Artificers.
- V. Mensuration of Superficies; preced-ed by plain and concise Geometrical Definitions.
- VI. A Collection of Questions, promiscu-ously arranged; intended as recapitu-latory exercises in the principal Rules of Arithmetic.
- VII. A Compendious System of Bookkeeping.

# BY FRANCIS WALKINGAME, Writing-Master and Accountant.

# FROM THE FORTY-THIRD DERBY EDITION.

Revised, Corrected, and Enlarged by the addition of SUPERFICIAL MENSURATION,

AND A

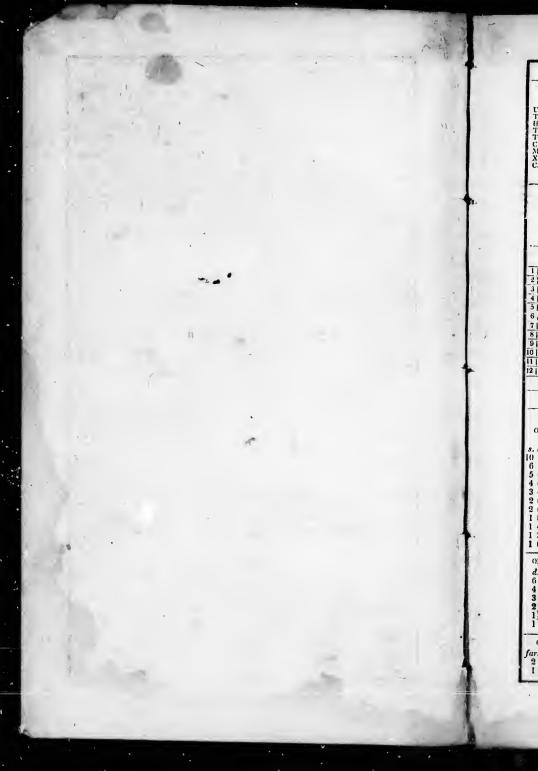
COMPENDIUM OF BOOK-KEEPING BY SINGLE ENTRY, BY WILLIAM BIRKIN,

Editor of the Improved Edition of Jones' Dictionary; Author of the Rational English Expositor, &c.

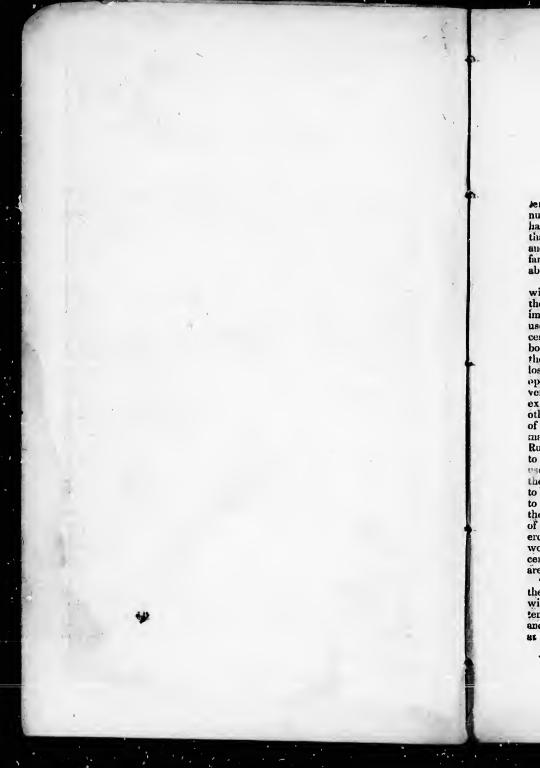
# TORONTO:

PUBLISHED BY BREWER, McPHAIL, & CO., PRINTERS, BOOKSELLERS, AND STATIONERS, 46, KING STREET EAST.

1850.



ARITH	IMETICAL	TABLES	S	LONG MEASURE.
	1		HILLINGS.	3 barley-corns 1 inch
NUMERA	TION.	. s. d. s	. L. s.	12 inches 1 foot 3 feet 1 yard
Units	1 0	0 are 1 8 2	Dare 1 0	6 feet 1 fatt
Tens	· · 13 3	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	0 - 1 10 0 - 2 0	-2 Jacob acce I post
Tens of Theoremands	. 1.234 30	6 3 0 5		40 poles 1 fur. 8 furlong 1 mile
C. of Thousands	- 12,345 4( 123,456 4)	0.34 0	) 3 ()	3 miles llean
Millions 1 X. of Millions 1 2	123,456 42	5 4 0 70 0 4 2 50		(9) miles 1 deg
X. of Multions 1 2 C. of Multions 1 2 3	1456.789 66	) 5 0 90		LAND MEASURE.
	70		) 5 6	9 feet make 1 yard
	Ni			304 yds 1 pole
CURRENT M	IONEY. SI	1 7 0 130	0 6 10	40 poles 1 rood 4 roods 1 acre
4 Farthings make	<ul> <li>L'enny 96</li> </ul>		) 7 0	
12 Pence - 20 Shillings, I Pound	Shillour			CLOTH MEASURE. 24 inch. make 1 nail
	1918	. 9 0 170	) 8 10	4 nails 1 quar
•	12(	) 10 0   180	) 9 0	3 qrs 1 Fl. e
MULTI	PLICATION.			4 qrs 1 yard 5 qrs 1 En.e
11 21 31 41 51 6	1 -1	111 12		6 qrs   Fr. e
2 4 6 8 10 12 3 6 9 12 15 19 4 8 12 16 20 21	14 16 15 201	22 24		
3     6     9     12     13     19       4     8     12     16     20     21       5     10     13     20     3     3	21 21 27 30	33   36		TIME. 50 sec 1 minut
5 10 15 20 25 3)			is lable may I to Division	60 min 1 hour
0 12 18 24 30 36	42 48 54 60	35         40         be applied           35         40         be applied           66         72         2% in 4 ar           77         84         in 6 are 3	ing it: as the	24 hours 1 day
4 4 4 2 28 35 42	49 56 63 70	77   84 in 6 are 3	, &c.	7 days 1 week 4 weeks 1 month
8   16   24   32   40   48 9   18   27   36   43   54	56 64 72 80	88 96		
V 20 30 40 50 60	1701 -01 00 1 100 1 1	101		DRY MEASURE.
66 00 1 (3) 66	177 1881 001 101 1	111 1 103		2 gall make 1 peck 4 pecks 1 bushe
2   24   36   48   60   72	8. 96 105 120 1	32   144		4 bushels - 1 sack
	Andrew of Management and			8 bushels - Iquarte. 4 quarters - 1 chald.
Talles o	f Weights an	d fiteasure	5.	10 quarters - 1 last
PRACTICE,	OF A TON.	APOTHEC.		SOLID MEASURE.
OF A POUND, OR	Cwt. T.	20 gr. make	1 scruple	1728 inches 1 solid foo
OF A POUND, OR SOVEREIGN.	10 are 1 half	3 scr	I dram	27 feet 1 yard
s. d. '£.	5 1 fourth 4 1 fifth	12 07.	I pound	COAL MEASURE.
0 0 are:1 half 6 8 1 third	$2\frac{1}{2}$ . 1 eighth	wcoi		3 bushels 1 sack
50 1 fourth	2 I tenth	7 lb, make	1 clove	36 bushels i chald.
401 fifth 341 sixth	1 is 1 twentieth	2 cloves	. I stone	CUSTOMARY
3 4 1 sixth 2 6 1 eighth	OF A HUNDRED.	2 stones	1 wer l	WEIGHT OF GOODS. lbs
	gr. 1b. Cwt.	2 weys	1 sack	A firkin of butter is 56
18 I twelfth	2 0 are 1 half	2 weys 12 sacks	1 last	A firkin of scap 64
	1 0 is 1 fourth 0 16 are 1 seventl	ALE AND.	BEER.	A barrel of pot ash. 200 A barrel of ancho. 30
	0 14 1 eighth		Iquart	A barrel of spap - 256
		9 gallons	1 firkin	A barrel of spap - 256 A barrel of butter 224
1		(1) distains	1 1.21.3	A fother of lead, 19
OF A SHILLING,	TROY.	2 firkins		CWL 2018 or _ 0104
OF A SHILLING, d. s. 6 are 1 half	24 gr. make 1 dwt.	2 kilderkins	l barre	A barrel of candles 120
OF A SHILLING, d. s. 6 are 1 half 4 1 third	24 gr. make 1 dwt. 20 dwt 1 oz.	2 kilderkins	l barre	A stone of iron or
OF A SHILLING,           d.         s.           6 are 1 half           4 1 third           3 1 fourth	24 gr. make 1 dwt.	2 kilderkins	1 barrel 1 hhd. 1 punc.	A stone of iron or shot 14
OF A SHILLING,           d.         s.           6 are I half           4 1 third           3 1 fourth           2 1 sixth	24 gr. make 1 dwt. 20 dwt 1 oz. 12 oz 1 lb.	2 kilderkins 1½ barrel 2 barrels 3 barrels WINE	l barre l hhd. l punc. l butt	A stone of iron or shot 14
OF A SHILLING,           d.         s.           6 are I half           4 I third           3 I fourth           2 I sixth           1 is I eighth           1 threading	24 gr. make 1 dwt. 20 dwt 1 oz. 12 oz 1 lb. AVOIRDUPOIS.	2 kilderkins 12 barrel 2 barrels 3 barrels WINE 2 pints make	l barret l hhd. l punc. l butt	A pairel of candles 190 A stone of iron or shot 14 A gallon of train oil 74 A lagot of steel 100 A stone of glass 0
OF A SHILLING, d. s. 6 are 1 half 4 1 third 3 1 fourth 2 1 sixth 12 is 1 eighth 1 1 tweighth	24 gr. make 1 dwt. 20 dwt 1 oz. 12 oz 1 15. AVOIRDUTOIS. 16 dr. make 1 oz. 16 oz 1 15.	2 kilderkins 12 barrel 2 barrels 3 barrels WINE 2 pints make 4 quarts 10 grallons	l barret l hhd. l punc. l butt l guart l gal.	A barrel of candles 190 A stone of iron or shot
OF A SHILLING,       s.         d.       s.         6 are 1 half       s.         1 d       1 third         3       1 fourth         2       1 fourth         1       1 fourth         1       1 sixth         1       1 twelkh         OF A PENNY.	24 gr. make 1 dwt. 20 dwt 1 oz. 12 oz 1 lb. AVOIRDUTOIS. 16 dr. make 1 oz. 16 oz 1 lb. 14 Jb 1 stone	2 kilderkins 12 barrel 2 barrels 3 barrels WINE 2 pints make 4 quarts 10 grallons	l barret l hhd. l punc. l butt l guart l gal.	A barrel of candles 190 A stone of iron or shot
OF A SHILLING, d. s. 6 are 1 half 4 1 third 3 1 fourth 2 1 sixth $1^2$ is 1 eighth $1^2$ is 1 eighth 1 1 twelchh OF A PENNY. Farth $d.$	24 gr. make 1 dwt. 20 dwt 1 oz. 12 oz 1 lb. AVOIRDUTOIS. 16 dr. make 1 oz. 16 oz 1 lb. 14 lb 1 stone 3 lb 1 gr.	2 kilderkins 14 barrel 2 barrels 3 barrels 3 barrels 2 pints make 4 quarts 10 gallons 42 gallons 53 gallons	l barrel l barrel l barrel l ponc. l butt l butt l gal. l ank. ltierce	shot 14 A gallon of train oil 74 A lagot of steel 100 A store of glass 6 A scan of glass 24 stone, or 120 A roll of parchment, 6 dozen skins
OF A SHILLING, d. s. 6 are 1 half 4 1 third 3 1 fourth 2 1 sixth 12 is 1 eighth 1 1 tweixth OF A PENNY. arth d. 2 urg 1 half	24 gr. make 1 dwt. 20 dwt 1 oz. 12 oz 1 lb. AVOIRDUTOIS. 16 dr. make 1 oz. 16 oz 1 lb. 14 Jb 1 stone	2 kilderkins 14 barrel 2 barrels 3 barrels 3 barrels 2 pints make 4 quarts 10 gallons 42 gallons 53 gallons	l barrel l barrel l barrel l barrel l burt l ppnc. l butt l gal. l gal. l gal. l tank. l tierce l hhd. l pp. 2 l hhd. l pp. 2 l barrel l ba	A barrel of candles 120 A stone of iron or shot



# THE AUTHOR'S PREFACE.

The public will, no doubt, be surprised to find there is another attempt made to publish a book of ARITHMETIC, when there are such numbers already extant on the same subject, and several of them that have so lately made their appearance in the world; but I flatter myself that the following reasons, which induced me to compile it, the method and the conciseness of the Rules, which are laid down in so plain and familiar a manner, will have some weight towards its having a favourable reception.

Having some time ago drawn up a set of Rules and proper Questions, with their Answers annexed, for the use of my own school, and divided them into several books, as well for more ease to myself as the readier improvement of my scholars, I found then, by experience, of infinite use; for when a master takes upon him that laborious (though unnecessary) method of writing out the Rules and Questions in the children's books, he must either be toiling and slaving himself, after the fatigue of the school is over, to get ready the books for the next day, or else must lose that time which would be much better spent in instructing and opening the minds of his pupils. There was, however, still an inconvenience which prevented them from giving me the satisfaction I at first expected; that is, where there are several boys in a class, some one or other must wait till the boy who first has the book finishes the writing of those rules or questions he wants, which detains the others from making that progress they otherwise might, had they a proper book of Rules and Examples for each boy; to remedy which I was prompted to compile one, in order to have it printed, which might not only be of use in my own school, but in other schools, where the instructors wish their scholars to make a quick progress. It will also be of great use to such persons as have acquired some knowledge of numbers at school, to make them the more perfect; likewise, to such as have completed themselves therein, it will prove, after an impartia perusal, on account of its great variety and brevity, a most agreeable and entertaining Exercise Book. I shall not presume to say anything more in favour of this work, but beg leave to refer the naprejudiced reader to the remark of a certain Author,\* concerning compositions of this nature. His words are as follow :-

"And now after all, it is possible that some, who like best to tread the old beaten path, and to toil at their business when they may do it with pleasure, may start an objection against the use of this well-intended Assistant because the course-of Arithmetic s. ways the same; and therefore say that some boys, lazly inclined, when they see another at work upon the same question, will be apt to make his operation pass

\* Dilworth

### PREFACE.

Sor their own. But these little forgeries are soon detected by the dillgence of the Tutor; therefore, as different questions to different boys do not in the lenst promote their improvement, so neither do the same questions impede it. Neither is it in the power of any macter, (in the course of his business,) how full of spirits soever he may be, to frame new examples at pleasure in any Rule; but the same question will frequently occur in the same Rule, notwithstanding his greatest care and skill to the contrary.

"It may also be farther objected, that to teach by a printed book is an argument of ignorance and incapacity, which is no less trifling than the former. He, indeed, (if such a one there be,) who is afraid his scholars will improve too fast, will indonbtedly decry this method, but that master's ignorance can never be bronght in question who can begin and end it readily; and, most certainly, that scholar's non-improvement can be as little questioned who makes a much greater progress by this than by the common method."

To enter into a long detail of every Rule would tire the reader, and swell the preface to an unusual length; I shall, therefore, only give a general idea of the method of proceeding, and leave the rest to speak for itself, which, I hope, the reader will find to answer the title, and the recommendation given it. As to the Rales, they follow in the same manner as the table of contents specifies, and in much the same order as they are generally taught in schools. I have gone through the four fundamental Rules in Integers first, before those of several denominations, in order that, they being well understood, the latter will be performed with much more ease and despatch, according to the rules shown, than by the customary method of dotting. In Multiplication I have shown both the beauty and use of that excellent Rule in resolving most Questions that occur in merchandising, and have prefixed to Reduction several Bills of Parcels, which are applicable to real business. In working Interest by Decimals I have added tables to the Rules, for the more ready calculating of Ammitics, &c., and have not only shown the use, but the method of making them; likewise a Table calculated for finding the Interest of Money for any number of days, at any rate per cent., by Multiplication and Addition only, which may also be applied to the calculation of Incomes, Salaries, or Wages, for any number of days; and I may venture to say, I have gone through the whole with so much plainness and perspicuity, that there is none better extant.

I have nothing farther to add but a return of my sincere thanks to all those gentlemen, schoolnasters, and others, whose kind approbation and encouragement have now established the use of this book in almost every school of eininence throughout the kingdom, but I think my gratitude more especially due to those who have favoured me with their remarks; though I must still beg of every candid and judicious reader, that if he should, by chance, find a transposition of a letter, or a false figure, to excuse it; for, notwithstanding there has been grea. we taken in correcting, yet errors of the press will inevitably creep in, and some may also have pped my observation; in either of which cases the ad monition of a good-natured reader will be very acceptable to his

Much obliged and most obedient humble servant,

#### F. WALKINGAME

Sin k Dis Con Equ Bar Pro Fell Alli Con M Peri Defi

De

Re

Co

Pro

Ru

Du

Pre

Tai

Inv

Red Add Snb Mul Divi Rule

Def

Dou

# CONTENTS.

Rora Herrimani

)]\_ ya ne

he ne ·e• nd is un is nt in nt iis nd a nk he nø er ur 1aern, vø st on ·kre se, dt., he nd ch all on ost ıtireer, se en ne ad

Page	l E.J.D
MERATION and notation9	Addition
INTEGERS.	Subtraction
imple Addition	Multiplication
Subtraction	Division
Multiplication	Circulating Decimals
—— Division	Reduction 101
Arithmetical and Commercial	Tables 103
Tables	Rule of Three 136
Definitions	Exchange
Reduction	Conjoined Proportion
Compound Addition	Involution
Subtraction	Evolution
Multiplicaton 40	Biquadrate Root
Multiplication	Roots of all Powers
	Single Position
Rule of Three Direct 40	Double Position
Inverse 63	Progression Arithmetical 123
Double Rule of Three	Geometrical
Practice	Simple Interest and Annuities 130
Tare and Tret	Discount
	Equation Try as
Simple Interest, Commission, Bro-	Compou- and Annui-
kerage, Purchasing Stock, &c. 66	Compou- ties
Disconnt	Discour
Compound Interest	DUODECI
Equation of Payments	SUPER. SATION.
Barter	G 1 t.
Profit and Loss	Mongunation of a Reputaleum
Fellowship	Mensuration of a Parattelogram, &c134
Alligation	Triangle 165
Comparison of Weights and	Trapezium,&c. 165
Measures	Trapezium, &c. 165
Permutation	Figure
	Figure
VULGAR FRACTIONS.	gon
Definitions, &c	Circle
	, Area of 169
Addition	, Inscribed square
Subtraction	Circular Arc
	Sector
	Segments
Rule of Three	Ellineo
Double Rule of Thuse	Ellipse
DECIMAL FRACTIONS.	Supplemental Questions
Defe itions &c	Rook-Kooning
	www.wixceping

.

-1

### EXPLANATION OF

# ARITHMETICAL SIGNS OR CHARACTERS.

+ is the sign of ADDITION; and is called plus, or more.

- is called minus, or less, and denotes SUBTRACTION.

× ----- into, and denotes MULTIPLICATION.

÷ \_\_\_\_ by, and denotes Division.

- is the sign of EQUALITY.

: .:: are the signs of PROPORTION.

V is the Radical Sign, or sign of Evolution.

of denotes the difference between two quantities when it is uncertain which is the greater.

#### ILLUSTRATIONS.

6+3=9 signifies 6 plus 3 equal 9: that is, 6 added to 3 equal 9. 7-4=3 signifies 7 minus 4 equal 3: that is, 4 taken from 7 leaves 3.

 $4 \times 3 = 12$  is read 4 into 3 genul 12: that is, 4 multiplied by 3 equal 15.

12-: 4=3 is read 12 by 4 equal 3. But Division is more conveniently expressed in the form of a Fraction: thue.

 $\frac{1}{4}^2 = 3$ ; twelve divided by four equal three.

As 2:4::8:16; As 2 are to 4, so are 8 to 16.

√16=4; the Square Root of 16 equal 4.

<sup>•</sup>√64=4; the Cube Root of 64 equal 4.

A vinculum connects two or more terms which are to be considered as forming one term or quantity. It is signified by a line drawn over them; or by parentheses including them.

A point is often used instead of the cross to denote Multiplication; and in Algebraical Theorems, &c., the multiplication of the quantities denoted by different letters is understood by placing the letters together without any sign between them. Thus 2.5+7, denotes that 5 and 7 are to be added, and the sum (12) to be multiplied by 2. Also, (ab+c). (n-1)denotes that a and b are to be multiplied, c added to the product, and the whole to be multiplied by one less than the number or quantity represented by n.

	The common sizes of Books are	marked
Folio,	of which 2 leaves make a sheet,	ffo.
Quarto,		4to.
Octavo,		8vo.
Duodecimo,		12mo.
Octodecimo,		18mo.

# Art cal unit figu sign and no

A deno secu crea A ures

# TUTOR'S ASSISTANT;

### EEING & COMPENDIUM OF

# PRACTICAL ARITHMETIC.

### Integers, or Whole Numbers.

12

9.

17

v 3

on-

u#.

on-

v a

lti-

ca.

er-

een ed,

-1) ro-

m7

ked

). ). 10.

0.

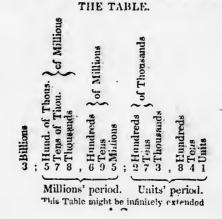
ARITHMETIC is the science of numbers; or the art of numerical computation. A whole number is a unit, or a collection of units.

Numbers are expressed by ten written characters called figures, or digits : viz. 1, 2, 3, 4, 5, 6, 7, 8, 9, which are significant figures, all declaring their own values by the names; and the eipher, or naught (0) an insignificant figure, indicating no value when it stands alone.

### NUMERATION AND NOTATION.

A figure standing alone, or the first on the right of others; denotes only its simple value, as so many units, or ones; the second is so many tens; the third, so many hundreds, &c., increasing continually towards the left in a tenfold proportion.

Numeration is the art of reading numbers expressed in figures; and Notation, the art of expressing numbers by frame.



THE

Note. To read any Number. Divide it into periods of six figures each, beginning at the right hand: and each period into semi-periods with a different mark, for the sake of distinction. The first on the right hand is the Units' period, the second the Millions' period, &c. Beginning at the left, observe that the three figures of every complete semiperiod must be reckoned as so many hundreds, tens, and units; joining the word thousands when you come to the middle of the period, and the proper name of the period at the end of it.

2. To express any given Number in Figures. Begin at the left, and write the figures which denote (as so many hundreds, cens, and units.) the number in that semi-period; and proceed thus with each successive semi-period, till the whole is completed; placing a separating comma in the middle of each period, or immediately after the thonsands, and a semicolon between the periods. But observe, that though every semiperiod but the first on the loft must have its complete number of three figures, that may be incomplete, and consist of only one or two figures: also, w here significant figures are not required in any part of a number, no se mi-period must be omitted, but the places must be filled up with eiphers.

Example. Write in figures, seventy thousand four hundred billions, two hundred and ten thousand millions, and ninety-six.

First, write 70 (seventy) with a comma, these being thousands; then 400 (four hundred) with a semicolon, denoting the end of the period; next, write 210 (two hundred and ten) and, because they are thousands, but a comma after them, and then 000 (three ciphers, there being no more millions) followed by a semicolon, to denote the completion of the period; again, put 000 (three more ciphers, denoting the absence of thousands) with a comma after them, and then 096, (ninety-si<sup>\*</sup>,) which will complete the number: thus, 70,400; 210,000; 009,096.

### EXERCISES IN NUMERATION AND NOTATION.

Read, or write in words the following numbers

*(1) 3 (2) 30 (3) 33 (4) 300 (5) 303 (6) 330 (7) 333 (8) 127 (9) 172 (10) 217 (11) 271	<ul> <li>(13) 721</li> <li>(14) 906</li> <li>(15) 4294</li> <li>(16) 94294</li> <li>(17) 294294</li> <li>(18) 3703</li> <li>(19) 703703</li> <li>(20) 311311</li> <li>(21) 113113</li> <li>(22) 131131131</li> <li>(23) 708807780</li> </ul>	<ul> <li>(25) 570050005</li> <li>(26) 1010100</li> <li>(27) 11110101</li> <li>(28) 499994949</li> <li>(29) 3584600987</li> <li>(30) 584610070840</li> <li>(31) 5846100708400</li> <li>(32) 37613590200116</li> <li>(33) 5008000400000</li> <li>(34) 60100800180070</li> <li>(35) 3700000000075048</li> </ul>
	(23) 708807780 (24) 807078087	(35) 37000000000075048

• The figures in parentheses refer to the Editor's Key to this work.

dre nin eig and ele two thr 8110 for tho six նա 8110

the

### ASSISTANT.]

#### NUMERATION.

# Express in figures the following numbers.

(1) Nine; ninety; ninety-nine; nine hundred; nine hundred and nine; nine hundred and ninety; nine hundred and ninety-nine.

(2) One hundred and eight; one hundred and eighty; eight hundred and one; eight hundred and ten; one hundred and sixteen; one hundred and sixty-one; six hundred and eleven.

(3) One hundred and twenty-three; one hundred and thirtytwo; two hundred and thirteen; two hundred and thirty-onethree hundred and twenty-one.

(4) 'I wo thousand five hundred and seventy-two.

(5) Seventy-two thousand five hundred and seventy-two.

(6) Five hundred and seventy-two thousand five hundred and seventy-two.

(7) Ten thousand nine hundred and ten.

(8) Nine hundred and ten thousand nine hundred and ter.

(9) One hundred and nine thousand nine hundred and onc.

(10) One hundred and ninety thousand and ninety-one.

(11) Nine hundred and one thousand and nineteen.

(12) One hundred and fourteen millions, one hundred and forty-one thousand four hundred and eleven.

(13) Four hundred and six millions, six hundred and four thousand four hundred and sixty.

(14) Six hundred and forty millions, forty-six thousand and sixty-four.

(15) Seven millions, seventy thousand seven hundred.

(16) Seven hundred millions, seven thousand and seventy.

(17) Ten millions, one thousand one hundred.

(18) One hundred and one millions, eleven thousand one hundred and ten.

(19) Twelve billions, seventeen thousand and nine millions and eighty-nine.

(20) Seven thousand five hundred and four trillions, sixty thousand millions, eight hundred thousand.

### Roman Numerals.

I	1	Oue.	171	6	Six.	XI	11	Eleven.	
11	2	Two.	VII	7	Sever.	XII	12	Twelve.	
Ш	3	Three	111	8	Eight	XIII	13	Thirtee:	
ΕV	4	Four.	X	9	Nine	XIV	14	Four' /	
Y	5	Five	×	10	Ten	XV	15	Fifte 1	

this

DR'S riods the Bcsemi-

join-

, and

and nits.) ssive mma and a semie figalso, r, no with

lions,

then riod; ands, ag no on of senco -si<sup>-</sup>,)

#### ADDITION OF INTEGERS.

XVI	16	Six teen.	I CC	200	Two hundred.
XVII	17	Seventeen.	ccc		Three hundred.
XVIII			CCCC	400	Four hundred.
	18	Eighteen.			
- XIX	19	Nineteen.	D	500	Five hundred.
XX	20	Twenty.	DC	600	Six hundred.
XXX	30	Thirty.	DCC .	700	Seven hundred.
XL	40	Forty.	DCCC	800	Eight hundred.
L	50	Fifty.	DCCCC	900	Nine hundred.
LX	60	Sixty.		1000	One thousand.
LXX	70	Seventy.	MDCCC	XXX	1830 One thousand
LXXX	80	Eighty.	1		eight hundred and
XC	90	Ninety.	1		thirty.
· C	100	One hundred.	1		

Norr. A less numerical letter standing before a greater, must be taken from it, as I before V or X, and X before L or C, &c., thus, IV. Four; IX. Nine; XL. Forty; XC. Ninety, &c. And a less numerical letter standing after a greater, is to be added to it, thus, VI. Six; XI. Eleven; LX. Sixty; CX. One Hundred and Ten.

All operations in Arithmetic are comprised under four elementary or fundamental Rules: viz., Addition, Subtraction, Multiplication, and Division.

## ADDITION

### **TEACHES** to find the sum of several numbers.

RULE. Place the numbers one under another, so that units may stand inder units, tens under tens, &c.; add the units, set down the units in heir sum, and carry the tens as so many ones to the next row; prosed thus to the last row, under which set down the whole amount.

**PROOF.** Begin at the top and add the figures downwards: if the sum und the same as before, it is presumed to be right.

1) 275	(2) 1234	(3) 75245	(4) 271048
110	7098	37502	325476
473	3314	91474	107584
354	6732	32145	625608
271	2546	47258	754087
352	6709	21476	279736
			•

• Say 2 and 1 are 3, and 4 are 7, and 3 are 10, and 5 are 15, set down 5 and carry 1; 1 and 5 are 6, and 7 are 13, and 5 are 18, and 7 are 25, and one are 26, and 7 are 33, set down 3 and carry 3; 3 and 3 are 6, and 2 are 8, and 3 are 11, and 4 are 15, and 1 are 16, and 2 are 18, set down 18: so the sum is 1835.

After practising a few examples, it will be better for the learner to

97 98

F

the

23

52

the

wł

or

ter

fro

gra

° (

€2 £1

por

coe

£1

add umi 1, 8 T A2SISTANT.]

ADDITION OF INTEGERS.

13

(5) 590046	(6) 370416	(7)	781943
73921	2890		56820
400080	60872		1693748
4987	998		300486
19874	47523		920437500
201486	9836		78632109
9883	26627	1 .	9408175

(8) What is the sum of 43, 401, 9747, 3464, 2263, 314, 974?

(9) Add 246034, 298765, 47321, 58653, 64218, 5376, 9821, and 640 together.

(10) If A has  $\pounds$ 56. B  $\pounds$ 104. C  $\pounds$ 274. D  $\pounds$ 1390. E  $\pounds$ 7003. F  $\pounds$ 1500. and G  $\pounds$ 998.; how much is the whole amount of their money?

(11) How many days are in the twelve calendar months?

(12) Add 87929, 135594, 7964, 3621, 27123, 8345, 35921, 2374, 64223, 42354, 3560, and 152165 together.

(13) Add 6228, 27305, 7856, 287, 7664, 100, 1423, 25258, 528, 3135, and 838.

(14) How many days are there in the first six months of the year; how many in the last six; and how many in the whole?

(15) In the year 1832, how many days from the Epiphany or Twelfth-day (Jan. 6th) to the last day of July?

(16) In the common year how many days from each Quarter-day to the next? That is, from Lady-day to Midsummer-day, from thence to Michaelmas-day, from thence to Christmasday, and from Christmas-day to the ensuing Lady-day?

(17) When will the lease of a farm expire, which was granted in the year 1799, for ninety-nine years?

(18) A person deceased left his widow in possession of £2500. His eldest son inherited property of the value of £11340. To his two other sons he bequeathed a thousand pounds each more than to his daughter; whose portion exceeded the property left to her mother by £500. A nephew and a niece had legacies of £525. each; z public charity £105.; and his four servants the same sum to be divided

add the figures without naming them. Thus, in adding the first column of the above example, say 2, 3, 7, 10, 15; set down 5 and carry 1, &c.

T' prethod will tend both to quickness and precision.

and

R'

IV. IV. rical XI.

iour ion,

tand ts in pro-

81114

25, and own

own

r to

# SUBTRACTION OF INTEGERS

[TUTOR 8

G

t١

n d

'n

1

b 1

is

b

Ν

e

h

ia

lo

A

el

32

8

24 32 do 1 f en tw tic 7;

amongst them. What was the aggregate amount of his property?

(19) 'Tell the name and signification of the sign put between the following numbers: and find what they are equal to, as the sign requires.

# 1724 + 649 + 17 + 5400 + 12 + 999.

(20) Required the sum of forty-nine thousand and sixteen; four thousand eight hundred and forty; eight millions, seven hundred and seven thousand one hundred; nine hundred and ninety-nine; and eleven thousand one hundred and ten.

(21) When will a person, born in 1819, attain the age of 45 ?

(22) Henry came of age 13 years before the birth of his cousin James. How old will Henry be when James is of age ?

(23) Homer, the celebrated Greek poet, is supposed to have flourished 907 years previous to the commencement of the Christian era. Admitting this to be fact, how many years was it from Homer's time, to the close of the 18th century; and how long to A. D. 1827?

# SUBTRACTION

TEACHES to take a less number from a greater, to find the remainder or Difference.

The number to be subtracted is the Subtrahend, and the other is called the Minuend.

RULE. Having placed the Subtrahend under the Minuend, (in the same order as in Addition,) begin at the units, and subtract each figure from that above it, setting down the remainder underneath. But when the lower figure is the greater, borrow ten; which add to the upper, and then subtract; set down the remainder, and carry one to the next figure of the Subtrahend for the ten that was borrowed.

PROOF. Add the Difference to the Subtrahend, and their sum will be U.e. Minucud.

(1) F T	rom 2714754 aķe 1542725	(4)	271508300 72841699	(7)	$\frac{1000000000}{987654321}$
(2)	42087296 34096187	(5)	375021599 278104609	(8)	2746981340 1095681539
· (3)	45270509 32761684	(6)	400087635 9184267	(9)	666740825 109348172

R 8

ro-

een as

en; ven red ten. 45 ? his ge ? ave the

1'23

and

re-

the

the and ure

00 21

10

25

2

# ABSISTANT.] SUBTRACTION OF INTEGERS.

(10) From 123456789 subtract 98765432.

(11) From 31147680975 subtract 767380799.

(12) Subtract 641870035 from 1630054154.

(13) Required the difference between 240914 and 24091

(14) How much does twenty-five thousand and four exceed sixteen thousand three hundred and ninety ?

(15) If eighty-four thousand and forty-eight be deducted from half a million, what will remain?

(16) The annual income of Mr. Lemmington, senior, is twelve thousand five hundred and sixty pounds. Mr. Lemmington, junior, has an income of seven thousand eight hundred and eighteen pounds per annum. How much is the son's income less than his father's ?

(17) George the Fourth, at his accession to the throne, in 1820, was in the 58th year of his age. In what year was he born, and how long had he reigned on the 29th of January, 1829, the anniversary of his accession?

(18) The sum of two numbers is 36570, and one of them is twenty thousand and twelve: what is the other?

(19) Thomas has 115 marbles in two bags. In the green bag there are 68: how many are there in the other?

(20) Two brothers who were sailors in Admiral Lord Nelson's fleet, were born, the elder in 1767, and the younger in 1775. What was the difference of their ages, and how old was each when they fought in the battle of Trafalgar, in 1805 !

(21) Henry Jenkins died in 1670, at the age of 169. How long prior to his death was the discovery of the continent of America by Columbus, in 1498 ?—Also, how many years have elapsed from his birth to 1827 ?

EXAMPLE. From 32906547 subtract 8210468.

32906547Minuend.Say 8 from 7 I cannot; borrow 10, and 7 are8210468Subtrahend.17, 3 from 17, 9 remain; set down 9 and carry24696079Difference.17, 1 and 6 are 7, 7 from 4 I cannot; borrow32906547Proof.10, and 4 are 14, 7 from 14, 7; set down 7 and<br/>carry 1.—1 and 4 are 5, 5 from 5, nothing; setdown (0)nanght.—0 from 6, 6; set down 6.—1 from 0 I cannot; but1 from 10, 9; set down 9 and carry 1.Proceed in like manner to the

When the pupil is initiated in the practice by working an example or two, he may simplify the work by omitting to  $c_{x}$  ress some of the particulars. Thus, in the preceding example, it will be sufficient merely to say, 3 from 17, 9; set down 9 and carry 1; 1 and 6 are 7, 7 from 14 7; set down 7 and carry 1. &c. (22) Borrowed at various times, £644., £957., £90., £1378., and £1293.; and paid again the different sums of £763., £591., £1161., £1000., and £847.—What remains unpaid?

(23) Explain the name and signification of the sign used; and work the two following examples.

10874 - 9999 51170 - 50049

(24) John is seventeen years younger than Thomas: how old will Thomas be when John is of age; and how old will John be when Thomas is 50?

# MULTIPLICATION

TEACHES to repeat a given number as many times as there are units in another given number.

The number to be multiplied is called the Multiplicand; that by which we multiply is the Multiplier; and the number produced by multiplying is the Product.

RULE. When the multiplier is not more than 12 multiply the units' figure of the multiplicand, set down the units of the product, reserving the tens; multiply the next figure, to the product of which carry the tens reserved: proceed thus till the whole is multiplied, and set down the last product in full.\*

1	2	3	4	5	6	7	8	9	10	11	12
2	- 4	6	8	10	12	14	16	18	20	22	24
3	6	9	12	15	18	21	24	27	30	33	36
4	8	12	16	20	24	28	.32	36	40	44	48
5	10	15	20	25	30	35	40	45	50	55	60
6	12	18	24	30	36	42	48	54	60	66	. 72
7	14	21	28	35	42	49	56	63	70	77	84
8	16	24	32	40	48	56	64	72	80	88	96
9	18	27	/36	45	54	63	72	81.	90	99	108
0	20	30	40	50	60	70	80	90	100	110	120
11	22	33	44.	55	66	77	88	99	110	121	132
2	24	36	48	60	72	84	96	108		132	144

713097

2852388

Say 4 times 7 are 25, set down 3 and carry 2; 4 times 9 are 36 and 2 are 38, set down 8 and carry 3; 4 times 0 (naught) and 3 are 3, set down 3; 4 times 3 are 12, set down 2 and carry 1; 4 times 1 are 4 and 1 are 5, set down 5; 4 times 7 are 28, set down 28. (5) (6)

ASS

(1)

(2)

(3)

(4)

ì

the

last

(15)(16)

(17)

V

by . of (

the

piod

Pr

oper proof

figur you them

\* duct.

+

96

1440

\$ ]

### ASSISTANT.] MULTIPLICATION OF INTEGERS.

Multiply 25104736 by 2.
 Multiply 52471021 by 3.
 Multiply 52471021 by 3.
 Multiply 7925437521 by 4.
 Multiply 27104107 by 5.
 Multiply 23104759 by 6.
 Multiply 7092516 by 7.

(12) Multiply 780149326 by 3, 4, 5, 6, 7, 8, 9, and 10.

(13) Multiply 123456789 by 4, 5, 6, 7, 8, and 9.

(14) Multiply 987654321 by 9, 10, 11, and 12.

When the multiplier is between 12 and 20, multiply by the units' figure in the multiplier, adding to each product the last figure multiplied.<sup>†</sup>

When the multiplier consists of several figures, multiply by each of them separately, observing to put the first figure of every product under that figure you multiply by. Add the several products together, and their sum will be the total product.<sup>‡</sup>

**PROOF.** Make the former multiplicand the multiplier, and the multiplier the multiplicand; and if the work is right, the products of both operations will correspond. *Otherwise.* A presumptive or probable proof (not a positive one) may be obtained thus: Add together the figures in *each factor*, casting out or rejecting the *nines* in the sums as you proceed; set down the remainders on each side of a *cross*, multiply them together, and set down the *excess* above the nines in their product.

\* To multiply by 10, annex a cipher to the multiplicand, for the product. To multiply by 100, annex two ciphers, &c.

#### EXAMPLES.

+ Multiply 96048 by 15.

96048 15 1440720

0..

of

ns

d ;

W

ih

re

1;

n-

ts'

ng

he vn

2

4680

24

6

8

0

2

4

et

Say 5 times 8 are 40, set down 0 and carry 4; 5 times 4 are 20 and 4 are 24, and 8 are 32, set down 2 and carry 3; 5 times 0 and 3 are 3, and 4 are 7, set down 7; 5 times 6 are 30, set down 0 and carry 3; 5 times 9 are 45 and 3 are 43, and 6 are 54, set down 4 and carry 5; 5 and 9 are 14, set down 14.

1 Multiply 76047 by 249.

76047

249 684423 Product by 9. 304188 do. by 40. 152094 do. by 200. 18935703 Total product

Proof. 0 6×6 0

# MULTIPLICATION OF INTEGERS.

[TUTOR'S

at the top of the cross. Then cast out the nines from the product, and place the excess below the cross. If these two correspond, the work is probably right: if not, it is certainly wrong.

When ciphers are intermixed with the significant figures in the multiplier, they may be omitted; but great care must be taken to place the first figure of the next product under the figure you multiply by.\*

Ciphers on the right of the multiplier or multiplicand (if omitted in the work) must be placed in the total product.<sup>†</sup>

(27)		(30)	1379500×3400.
	7561240325×57002.	(31)	7271000×52600.
(23)	562710934×590030.		74837000×975000

A number produced from multiplying two numbers together is called a *composite number*; and the two numbers producing it are called the *factors*, or *component parts*. When the multiplier is a *composite number*, you may multiply by one of the *factors*; and that product multiplied by the *other* will give the total product.<sup>‡</sup>

- (33)  $771039 \times 35.$ (34)  $921563 \times 32.$ (35)  $715241 \times 56.$
- (36) 679998×132.

(37) 7984956×144.

(35) 8760472×999.§ (39) 7039654×99999.

(40) A boy can point 16000 pins in an hour. How many can five boys do in six days, supposing them to work 10 clear hours in a day?

* Multiply 31864 by 7003. 31864 7008 Proof. 254912 6 223048 4×6 223302919 6 † Multiply 63850 by 5200. 63850 5200 Proof. 12770 1 31925 4×7 332020000 1	EXAMPLES. t Multiply 63175 by 45. 63175 5×9=45 315875 9 2842875 <sup>2</sup> . § For an abridged method of multiplying by a series of nincs, see the Key.
--	--

ASS (man a y ( diff

TE! othe • 'I whi divi divi ed a left. R it is den plus find and H is co be c mult vidu divid as be  $\mathbf{P}$ the 1 the d

(1

\* I Divise Quoti

and 2

TOR'S

ct, and work

9. 79.

res in st be r the

d (if ٠t

). )0. s to-

bers /hen one will

9. any

lear

of 1C... ASSISTANT.]

(41) If a person walks upon an average 7 miles a day, how many miles will he travel in 42 years, reckoning 365 days to a year?

(42) Multiply the sum of 365, 9081, and 22048, by the difference between 9081 and 22048.

(43) Required the continued product of 112, 45, 17, and 99.

Note. Multiply all the numbers one into another.

# DIVISION

TEACHES to find how often one number is contained in another: or to divide a number into any equal parts required.

\* The number to be divided is called the Dividend; that by which we divide is the Divisor; and the number obtained by dividing is the Quotient ; which shows how many times the divisor is contained in the dividend. When it is not contained an exact number of times, there is a part of the dividend left, which is called the Remainder.

RULE. When the divisor is not more than 12, find how often it is contained in the first figure (or two figures) of the dividend; set down the quotient underneath, and carry the overplus (if any) to the next in the dividend, as so many tens; find how often the divisor is contained therein, set it down, and continue in the same manner to the end.

When the divisor exceeds 12, find the number of times it is contained in a sufficient part of the dividend, which may be called a dividual; place the quotient figure on the right, multiply the divisor by it, subtract the product from the dividual, and to the remainder bring down the next figure of the dividend, which will form a new dividual: proceed with this as before, and so on, till all the figures are brought down.

PROOF. Multiply the divisor and quotient together, adding the remainder (if any) and the product will be the same as the dividend.

(1) Divide 725107 by 2.\* ! (2) Divide 7210172 by 3.

\* EXAMPLE. Divide 7323105 by 4. Divisor 4)7328105 Dividend. Quotient 1832026-1 Rem.

7328105 Proof.

Say the fours in 7, once and 3 over; the fours in 33, 3 times 4 are 32 and 1 over; the fours in 12, 3 times; the fours in 8. twice; the fours in 1, 0 and 1 over; the fours in 10, twice 4 are 8. and 2 over; the fours in 25, six fours are 24 and 1 over.

# DIVISION OF INTEGERS.

	Divide		4.	(14) 7210473	÷37.*	
(4)	Divide	7203287 by		(15) 42749467		
(5)	Divide	5231037 bi	7 6	(16) 721007142	÷347.	
(6)	Divide	2532701 by	7.	(16)734097143 (17)1610476407	-5743.	1
(7)	Divide	2517325 by	8.	(17)1610478407	÷51716.	
(8)	Divide	25047306 by	. 0.	(18) 4973401891	$\div 510834.$	
(9)	Divide	70319645 1.	9.	(19) 5170456787	1 - 4765043	
(10)	Divide	12804763 by	10.	(20) 17453798940	$3123741 \div$	
in	Divido	7004203 by	11.	31479461.		
(19)	Divide	79013260 by	12.	(21) 25473221	$\div 27100.1$	
(12)	Divide	37000421 by	3,	(22)725347216	$\div 572100.$	
(10)	0, 7, 7, 7, 7, 7, 7, 7, 7, 7, 7, 7, 7, 7,	and Q.		(23)752473729	$\div 373000.$	
(13)	Divide	111111111 b	y 6,		$\div 215000.$	
	9, 11	, and 12.				

When the divisor is a composite number, you may divide the dividend by one of the component parts, and that quotient by the other; which will give the quotient required. But the true remainder must be found by the following

RULE. Multiply the second remainder by the first divisor: to that product add the first remainder, which will give the true one.

(25)  $3210473 \div 27.$ § (26)  $7210473 \div 35.$ 

(27)  $6251043 \div 42$ . (28)  $5761034 \div 54$ .

\* When the divisor is large, the quotient figures are most cusily found by tria's of the first figure (or two) in the leading figures of the dividend.

t Ciphers at the right of the divisor may be cut off, and as meny figures from the right of the dividend; but these must be annexed us the remainder at last.

§ EXAMPLE. Divide 314659 by 21. 21=7×3)314659

$$\frac{7)104836-1}{14983-5} = 5 \times 3 + 1 = 16 \text{ rem.}$$

.

TUTOR .

cut figu 107 the 8th and N WOI ( the Ho equ row ( one mai ( rou yea in a mot ( quo duc is 1 quo ſ whe ŀ hoù at v that aré m th

### TUTOR I

7.\* 47. 743. 1716. 10834. 765043 741÷

7100.<u>†</u> 72100. 73000. 5000.

ide the ient by But the

ivisor: ve the

ousily I the

meny red u

### ASSISTANT.]

A number may be divided by 10, 100, 1000, &c., by merely cutting off one, two, three, &c., figures on the right : the other figures are the quotient, those cut off are the remainder.

Thue 76390÷10=7639; 238157÷10=23845 and 7 rem. And 4598653÷1000=4598 and 653 rem.

(29) 65941089 $\div$ 10.

(31) 18043329 $\div$  10000. (30) 7208465÷100.

(32) 7406572÷1200.

(33) What is the difference between the 12th part of 107724, and the 23d part of 346610?

(34) If a ship bound to Jamaica set sail from Liverpool on the 25th of January, 1828, and arrived at that island on the 8th of March, what was the velocity of her sailing per day and per hour; the distance being 4558 miles?

NOTE. This is the direct distance. The circuitous course of the ship would be considerably more.

(35) The period of Jupiter's revolution in his orbit round the sun, which is the year of that planet, is 4330 of our days. How many of our years, reckoning 365 days to the year, are equal to five years of Jupiter?

(36) I would plant 2072 clins in 14 rows, the trees in each row 17 feet asunder : what length will the grove be ?

(37) If a chest of oranges, 1292 in number, be distributed, one moiety among 19 boys, the other among 17 girls : how many will fall to the share of each ?

(38) The circumference of the earth's orbit, or annual path round the sun, is about 596440000 miles. Supposing the year to be exactly 3651 days, or 8766 hours, how many miles in an hour, and how many in a minute, are we carried by this motion?

(39) Required the sum, the difference, the product, and the quotient, of 3679 and 283: and also the quotient of the product divided by the sum.

(40) The sum of two numbers is 4290; the less number is 143 : what is their difference, product, and quotient ; and the quotient of the product divided by the difference ?

(41) The product of a certain number multiplied by 694, when 320 are added, is equal to 500000 : what is that number ?

(42) Allowing the earth to revolve on its axis in exactly 24 hours, and the circumference at the equator to be 24864 miles; at what rate per hour and per minute are the inhabitants of that part carried round by the revolution ? Also, at what rate are the inhabitants of London carried round, the circumference in that latitude being 15480 miles ?

TABLES OF MONEY.

4

& ACTHMETICAL AND COMMERCIAL TABLES.

# STERLING MONEY.

4 farthings (qrs.) make 1 penny, d.

22 2 8

12 pence . . . . . 1 shilling, s.

5 shillings . . . 1 crown, cr.

20 shillings 1 pound, or sovereign, £.

 $\frac{1}{2}d$ . denotes a farthing,  $\frac{1}{2}d$ . a halfpenny, and  $\frac{3}{4}d$ . three farings.

Qrs. 4 = 1 penny. 48 = 12 = 1 shilling. 240 = 60 = 5 = 1 crown. 960 = 240 = 20 = 4 = 1 pound.

OBSOLETE COINS.

A gninea (weight 5 dwts. 94 grs.) value 21s. A moidore, 27s. A pistole, 17s. A murk, 13s. 4d. An angel, 10s. A noble, 6s. 6d. A tester, 6d. A groat, 4d.

Notes. Gold is considered the standard metal; and there is no alteration in the *new coin*, either in fineness or weight, from that of former coinages; 21 sovereigns being equal in weight to 20 guineas. 1869 sovereigns weigh exactly 40 hs troy. A sovereign is therefore a little more than 5 dwts.  $3\frac{1}{4}$  grs. (5 dwts.  $3\cdot274$  grs.) and a half sovereign rather exceeds 2 dwts.  $13\frac{1}{2}$  grs. (2 dwts.  $13\cdot637$  grs.) The *new silver coin* is of the same fineness as that of former coinages; but 1 h. of filver is now coined into 66s. instead of 62s., as it was formerly, so that one shilling now weighs 3 dwts.  $15\frac{3}{11}$  grs., and other silver pieces in proportion.

The mint value of gold is £3..17..10½. per onnce, and of silver 52.6d. The standard for gold coin is 22 parts (commonly called *carats*) of fine gold, and 2 parts (or *carats*) of copper, melted together. For silver coin, 11 oz. 2 dots. of fine silver, alloyed with 18 dots. of copper.

Farthings.	Farthings.	Pence.	Pence.	Pence.	1 61.102
A ree	4100 40	1 (4. 8.	d. ed	d. 8. d.	
4 are 1	32 rate 8	36 are 3		160 are 13 4	8. £. s.
6 14	34 84	43 4		170 14 0	80 are 4 0
8 2	36 9	60 5		17014 2	90 4 10
10 24		70	40 3 4	18015 0	100 5 0
23			50 4 2	19015 10	110 5 10
	40	84 7	60 5 0	20016 8	120 6 0
4 34	Two USI	/()	20 510	1	100 0.44
· · · · · · ·	33	100 91	8068	Shillinge	140 7 0
V D	4818.	132. 11	100 9 4	90	160 0 0
		14412	110 9 2	30 1 10	120 0 10
4 6	Pence.	156. 13	12010 0		100 8 10
6 64	d. 8.	168. 14	130 10 10	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	180 9 0
	12 are 1	190 15	14011 8	30 2 10	190 9 10
· 71	94 9	109 10	150 10 0		20010. 0
	24 2	19410	15012 6	70 3 10	21010 10

MONEY TABLE.

Note lings, 1

TUTOR'S

lings, 1 £12. 10 gives 1

These ar

16 16

14

2 35

71 286 5734 By this

ed. A transfer. transfer. are a stor goods of y cmt. or 12 G

Note. When the units' figure is cut off from any number of shillings, half the remaining figures will be the pounds. Thus, 256s.= £12. 16s. because half of 25=12; and the one over prefixed to the 6, gives 16s.

# WEIGHTS AND MEASURES.

### TROY WEIGHT.

24 grains (gr.) make 1 pennyweight,	dwt.
20 pennyweights 1 ounce	02.
12 ounces 1 pound,	ib.
Grains. 24 == 1 pennyweight.	
480 = 20 = 1 ounce.	
5760 = 240 = 19 = 1 nound	
iond, silver, and gems, are weighed by this	weight

### APOTHECARIES' WEIGHT.

20	grains (	gr.)	m	ake	1	scruple,		Э	
3 :	scruples				1	dram.		3	
80	urams		•	•	1	ounce.		7	
12 0	ounces				1	pound,		ħ.	
Trains. 2	0 == 1	scru	ple			1	•		
6	0 = 3	2272	1 d	ram					
48	0 = 24	-	8 =	= 1 (	ou	nce.			

5760 = 283 = 96 = 12 = 1 pound.

This is used only in the mixing of medicines.

These are the same grain, onnce, and pound, as those in Troy Weight.

### AVOIRDUPOIS WEIGHT.

16	drams (dr.) make	3					1 ounce		0.
16	ounces					•	1 nound	•	72
14	pounds	•	•	•	•	•	1 pound, .	•	10.
28	pounds on 0 ston		•	•	•	•	1 stone, .	•	st.
20	pounds, or 2 ston	es	•	•	•	•	1 quarter,		gr.
	quarters, or o st.	OL.	112	2 10			1 hundrod		annt
20	hundreds	•	•				1 ton.		+
Drams.	16 = , 1 ounce.						,	•	••

	256	=	16	-	1 pc	ound.			
	3584	=	224	-			tone.		•
	7168			-	28 =	2 -		quarter.	
	28672	-	1792		112 -	8 -	- 1	- 1 curt	ŀ.
-	573440	-	35840	-	2240 =	160 =	= 80	= 20 = 1	ton

By this weight nearly all the common necessaries of life are weighed. A truss of hay=56 b. and one of straw=36 b. A load is 36 trusses. A peck loaf weighs 17 b. 6 oz. 1 dr. In the metropolis, 8 b. are a stone of meat. A fother of lead is 194 cwt. In some districts, goods of various descriptions (as cheese, coal, &c., are sold by the long ent. or 120 b.

e far-

TOR's

3.

d. A alterormer 1869 little rathcoin

А

ver is t one propro-

) of siloer.

3,

#### WEIGHTS AND MEASURES

### WOOL.

When wool is purchased from the grower, the legal stone of 14 th, and the tod of 28 lb, are used. But in the dealings between woolstaplers and manufacturers.

15 pounds are .	1 stone.
2 stones or 30 Hz	1 tod.
8 tods, or 240 lb.	1 pack or sack.

## COMPARISON OF WEIGHTS.

175 ounces troy=192 ounces avoirdupois. We may, therefore, reduce lbs. Troy into Avoirdupois by multiplying them by 144, and dividing by 175, &c.

### LINEAL, OR LONG MEASURE.

12 inches (in.) make	1 foot, ft
3 feet, or 36 inches	1 yard, yd.
2 yards. or 6 feet	1 fathom, fa.
$5\frac{1}{2}$ yards, or $16\frac{1}{2}$ feet	1 pole, rod, or perch, p.
4 poles, or 22 yards	1 land chain,* . ch.
40 poles, or 10 ch., or 220 yds.	1 furlong, fur.
8 furlongs, or 1760 yards	1 mile, m.
3 miles	1 league, l.
Barley-comis	

Barley-corns.

Note. It is commonly supposed that the English includes original by taken from three grains of barley, selected from the middle of the ear and well dried.

A twelfth part of an inch is called a line.

4 inches are a hand, used in measuring the height of horses. 5 feet are a pace. A cubit = 14 feet nearly.

This measure determines the length of lines. A line has the dimension of length only, without breadth or thickness.

\* The class consists of 100 links, each link being = 7.02 inches.

TUTOR'S

14

30

Roof ing 100 By the A supe

A cor 128 cub A stac 108 cub This mension [TUTOR'S

gal stone the deal-

1

ultiplying

ft yd. fa. ch, p. ch. fur. m. l.

s original dle of the

s. 5 feet he dimen

neties.

ASSISTANT.

10

### TABLES OF MEASURES.

### CLOTH MEASURE.

$2\frac{1}{4}$ inches (in.) make 1 nail, n.	
4 nails, or 9 inches 1 quarter, . gr.	
4 quarters 1 yard, yd.	
5 quarters 1 English ell. E. e	
A Flemish ell is 3 qrs. A French ell 6 qrs.	

Used for all drapery goods.

## SUPERFICIAL, OR SQUARE MEASURE.

144 square inches (sq. in.) make 1 square foot, sq. ft. 9 square feet . . . . 1 square yard, sq. yd. 30<sup>1</sup>/<sub>4</sub> sq. yards, or  $272\frac{1}{4}$  sq. feet 1 sq. rod, pole, or perch

# Also, in the measure of land,

40 perches make 1 rood,	r.	
4 roods, or 4840 yards 1 acre.	a.	
,000 square links 1 square chain.	sa e	
10 sq. chains, or 100,000 links 1 acre,	a.	
640 acres 1 square mile,	sa. m	
Inches. $144 = 1$ foot.	1	
1296 = 9 = 1 yard		
39204 = 2724 = 304 - 1 pole		
1000100 = 10000 = 1210 = 40 = 10000		
6272640 = 43560 = 4840 = 160 = 4 = 1  acre.		

Roofing, flooring, &c., are commonly charged by the Square, containing 100 square feet.

By this measure is expressed the area of any superficies, or surface. A superficies has measurable length and breadth

## CUBIC, OR SOLID MEASURE.

1728 cubic inches (in.) make	1 cubic foot.
27 cubic feet	1 cubic vard *
40 leet of round timber, or )	
50 feet of hewn timber	1 ton, or load.
	1 ton of shipping.
	in the second se

A cord of wood is 4 feet broad, 4 feet deep, and 8 feet long, being 128 cubic feet.

A stack of wood is 3 feet broad, 3 feet deep, and 12 feet long, being 108 cubic feet.

This determines the solid contents of bodies. A solid has three dimensions, length, breadth, and thickness.

# \* A solid yard of earth is called a load.

### TABLES OF MEASURES.

26

# IMPERIAL MEASURE.

This is the standard now established by Act of Parliament, as a general measure of capacity for liquid and dry articles.

2 pints (pt.) make . . . 1 quart, qt. 4 quarts . . . . . . 1 gallon, gal.

The imperial or standard gallon must contain 10 lbs Avoirdupois weight of pure water, at the temperature of 62° of Fahrenheit's thermometer. This quantity measures 277<sup>1\*</sup> cubic inches; being about one-fifth greater than the old wine measure, one-thirty-second greater than the old dry measure, and one-sixtieth less than the old ale measure.

### IN DRY MEASURE,

2 gallons	(ga	1.)	ma	ke			1	peck,	pk.
4 pecks	•	•	•				1	bushel,	Ъ.
8 bushels	•	•	•	•	•	•	1	quarter,	qr.

Corn to be stricken off the measure with a round stick, or roller. Obsolete. A coom = 4 bushels; a chaldron = 4 quarters; a wey = 5 quarters; a last = 2 weys.

Solid inches. 2774 = 1 gallon.

 $554\frac{1}{2} = 2 = 1$  peck. 2218 = 8 = 4 = 1 bushel.

17741 = 64 = 32 = 3 = 1 quarter.

#### OF COALS,

3	bushels make	•	1 sack.
12	sacks, or 36 bushels		1 chaldron.
21	chaldrons		1 score.

All the measures used for heaped goods are to be of cylindrical form; the diameter being at least double the depth. The height of the raised cone to be equal to three-fourths of the depth of the measure.

The old dry gallon contained 2684 cubic inches.

NOTE. The bushel, for measuring heaped goods, must be 17.81 inches in diameter, and 8.904 inches deep; or if made 18 inches in diameter, the depth will be 3.717 inches. The cone to be raised 6.6 inches in height.

In WINE AND SPIRIT MEASURE, the old gallon contained 231 cubic inches.

63 gallons were . . . . a hogshead, hhd.

2 hogsheads, or 126 gallons a pipe or butt.

4 hogsheads, or 252 gallons a tun.

\* More accurately, 277-274 cubic inches.

### TUTOR'S

e n

C

wit (E) less

par

CI

is, a

a pi V

neou

# TUTOR'S

rliament, rticles.

s Avoirof 62° of es 2771\* old wine measure,

· roller. ; a wey =

of cylinie depth. ourths of

t be 17.81 inches in raised 6.8

nined 231

hd.

### ASSISTANT.]

# TABLES OF MEASURES.

Some other denominations have been ng obsolete ; as, an anker (10 gallons;) a ruulet (18 gallons;) a tierce (42 gallons;) a puncheon (84 gallons.) But casks of most descriptions are generally charged according to the number of gallons contained. Solid inche

es. $34_3^2$		1 pint				
	8=	2 =	1 qu	art.		
$277\frac{1}{4}$		8 =	4 =	1 σ	allon.	
$17466_{1}^{3}$	=	504 =	252 =	63 =	1 hor	shead.
34933;	=1	008 = -	504 =	126 =	2 = 1	nine
69867	= 2	016 = 1	008 ==	252 -	4=2	=1 tun.

In ALE, BEER, OF PORTER MEASURE, the old gallon contain ed 282 cubic inches; and measures of the following denomi nations have been in use :---

A firkin, containing.	• • 9 gallons.
A kilderkin	. 18 gallong
A barrel	36 gallona
A hogshord	· · Jo ganons.
A hogshead	• • 54 gallons.
A butt	· . 108 gallons.
Cubic inches $34\frac{21}{32} = 1$ pint.	
$09_{16} = 2 = 1$ or	uart.
$277\frac{1}{1} = 8 = 4 =$	1 gallon
$2495_4 = 72 = 36 =$	9 = 1 firkin
$4990\frac{1}{2} = 144 = 72 =$	18 = 2 = 1 kilderkin
9981 = 288 = 144 =	36 = 4 = 9 - 1 harrol
$14971\frac{1}{2} = 432 = 216 =$	$54 = 6 = 3 = 1\frac{1}{2} = 1$ hogsh'd.
$29943^{\circ} = 864 = 432 =$	108 = 12 = 6 = 3 = 2 = 1 hogsin d.
001 - 105 -	100 - 12 - 0 = 3 = 2 = 1 butt.

# \*RULES FOR CHANGING OLD MEASURES TO IMPERIAL.

ALE Multiply by 60, and divide by 59; or add 1 part. (True within 10000 part of the whole.)

Or, multiply by 179, and divide by 176. (True, within 1000000 part.) DRv. Multiply by 32, and divide by 33; or deduct 13 part (Error, less than  $\frac{1}{3700}$  part.)

WINE. Multiply by 5, and divide by 6, or deduct  $\frac{1}{6}$  part. (Error, less than  $\frac{1}{4000}$  part.)

Or, multiply by 624, and divide by 749. (Error, less than corrors part.)

\*RULES FOR CHANGING IMPERIAL TO OLD MEASURES.

ALE. Multiply by 59, and divide by 60, or deduct 1 part.

Or, multiply by 176, and divide by 179.

DRY. Multiply by 33, and divide by 32, or add 1 part.-That is, add one peck in every quarter, one quart in every bushel, or half a pint in every peck.

WINE. Multiply by 6, and divide by 5, or add  $\frac{1}{3}$  part.

Otherwise, multiply by 749, and divide by 624.

\* Examples applying to these Rules will be found in the Miscelle neous Questions in the latter part of the book.

TIME.

### 'TUTOR'S

0

fe

p

U

Is

in

th er

th

202

808

#### TIME.

60	seconds	(sec.	) ma	ke						1 minute, . min
60	minutes									1 hour, hr.
										1 day,* <i>d</i> .
7	days .				•	•	•	•	•	1 week, wh.
$52 \\ 365$	weeks, days, 6	1 day hour	y,6ł s.	iour	's, (	or }	•	•		1 Julian year, yr.
365	days, 5	hour	s, 48	mi	n.,	51 <u>1</u>	se	con	ıds	The Solar year.
										1 century.
Seco	nds. 60									

3600 = 60 = 1 hour.

86400 = 1440 = 24 = 1 da 604800 = 10080 = 168 = 7 = P week.

31557600 = 525960 = 8766 = 365 d. 6h. = 52 w. 1 d. 6h. = 1 Julian year.  $31556931 = 525943 = 8765 = 365 d. 5 h. 48 m. 51\frac{1}{2}$  == 1 Solar year.

The year is divided into 12 Calendar months; January, February, March, April, May, June, July, August, September, October, November, December.

The days are thirty in September, | And in each other thirty-one: In April, June, and in November; | But every leap-year we assign Twenty-eight in February alone, To February twenty-nine.

The leap-years are those which can be exactly divided by 4; as, 1824, 1828, &c. Hence it appears that the year is accounted 365 days, for three years together ; and 366 days in the fourth: the average being 3651 days. (The Julian Year.)

Four weeks are frequently called a month; but in this sense it is better to avoid the term.

NOTE. In all questions in this book, where the proposed or required time consists of years, months, weeks, &c., allow 4 weeks to a month, and 13 months to a year.

#### GEOMETRY.

60	seconds	(")	mak	6			1 minute, '	
60	minutes	•		•	•		1 degree, <sup>o</sup>	
360	degrees				•	•	1 circle.	

Many highly important calculations in the mathematical sciences are founded on this division of the circle.

In Astronomy, the great circle of the ecliptic (or of the zodiac) is divided into 12 signs, each 30°.

+ The Solar, or true year, is that portion of time in which the earth makes one entire revolution round the sun.

A day is the time in which the earth revolves once upon its axis. by law and custom it is reckoned from midnight to midnight; but the astronomical day begins at noon.

TOR'S

min hr. d. wh.

', *yr*. ear.†

an year. r.

bruary, ember,

-one: ssign .e.

led by year is lays in Year.) s sense

equired month,

natical

the zo-

ts axis. but the

e earth

ASSISTANT.]

### REDUCTION.

In Geography, a degree of latitude, or of longitude on the equator, measures nearly  $69\frac{1}{10}$  British miles. But a minuto of a degree is called a geographical mile.

# ARTICLES SOLD BY TALE.

12 articles o	of	nny	kii	nd,	are		24 sheets	of	pa	per	1 anire.	
12 dozen .	•	•	•	•	•	OPOSS.	196 univos				1	
20 articles	:	:	:	:	•		2 reams	•	•	•	1 bundle	•
				-	•	1 000101						

### DEFINITIONS.

1. A NUMBER is called *ábstract*, when it is considered *simply* or without reference to any subject; as seven, a thousand, &c.

2. When a number is applied to denote so many of a particular subject, it is a *concréte* number; as seven pounds, a thousand yards, & c.

3. A denomination is a name of any particular distinctive part of money, weight, or measure; as penny, pound, yard, &c.

4. The association of a concrete number with its subject, forms a quantity.

5. A simple quantity has only one denomination; as seven pounds.

6. A compound quantity consists of more denominations than one; as seven pounds five shillings.

# REDUCTION

Is the method of changing quantities of one denomination into another denomination, retaining the same value.

RULE. Consider how many of the less name make one of the greater; and multiply by that number to reduce the greater name to the less, or divide by it to reduce the less name to the greater.

£. s. d. 3 8 64	EXAMPLES.
20	Reduce £8861. into farthings.
168 s. 12	The £2, being multiplied by 20, and the 8s. add-
2022 d. 4 1090 grs. Ans.	the 6 <i>d</i> . added, make 2022 <i>d</i> .; which being multiplied by 4 and the 2 farthings added make it the
000 grs. Ans.	whole 8090 farthings.

#### REDUCTION.

(1) In £12. how many shillings, pence, and farthings? Ans. 240s. 2880d. 11520 qrs.

(2) In 311520 farthings, how many pounds? Ans. £324..10.
(3) Change 21 guineas into farthings. Ans. 21168 qrs.
(4) In £17..5..3], how many farthings? Ans. 16573 qrs.
(5) In £25..14..1, how many pence? Ans. 6169d.
(6) Reduce 17940 pence to crowns. Ans. 299 crowns.
(7) In 15 crowns, how many shillings and sixpences? Ans. 75s. 150 sixpences.

(8) Change 57 half-crowns into threepences, pence, and farthings. Ans. 570 threepences, 1710d. 6840 farthings.

(9) How many half-crowns, and how many sixpences, are equivalent to £25..17..6.? Ans. 207 half-cr. 1035 sixpences.
(10) Convert £17..11..9. into threepences.

Ans. 1407 threep.

(11) Change £10..13..101. into halfpence. Ans. 5133.

(12) In 52 crowns, as many half-erowns, shillings, and pence, how many farthings? Ans. 21424 far.

(13) Convert 17380 farthings into £. Ans. £18.2.1.

(14) In 21424 farthings, how many crowns, half-crowns shillings, and pence, of each an equal number? Ans. 52.
(15) Reduce 60 guineas to shillings, crowns, and pounds.

(5) Reduce of guineas to similarly, crowns, and points. Ans. 1260s. 252 crowns,  $\pounds 63$ .

(16) Reduce 76 moidores\* into pounds. Ans. £102..12.

(17) How many shillings, half-crowns, and crowns, an equal number of each, are there in  $\pounds 556.?$ 

Ans. 1308 of each, and 2s. over.

(18) In 1308 crowns, as many half-crowns, and as many shillings, how many pounds? Ans. £555..18.

(19) Seven men brought  $\pounds 15..10$ . each into the mint, to be exchanged for gnineas; how many would they have?

Ans. 103 guineas and 7s. over.

(20) In 525 American dollars, at 4s. 6d. each, how many pounds sterling? Ans. £118..2..6.

### Cónverse to the preceding EXAMPLE.

In 8090 farthings, how many pounds?

4)8090 qrs. 12)20221 d. 2|0)16|8s. 61d. Ans. £8..8..61.

30

Dividing the farthings by 4, we obtain 2022*a* and 2 over, which are *farthings*, because the remainder is a part of the dividend. Divide 2022 by 12, and we obtain 168s, and 6*d*. over: these shillings divided by 20, give  $\pounds$ 8 8s., so that the answer is  $\pounds$ 8...65.

• 27 shillings. The moidore is current in Portugal, but not in Eng land.

Ű

ai he

ar

ma ya

### TOR'S

s? nrs. 4..10. nrs. 9d. ns. ? ccs. ccs. cs. and ogs. s, aro ccs.

cep. 33. s, and far. 2..1. 52. unds. 52. unds. 263. .12. as, an

wer. many .18. t, to be

*ver.* many 2..6.

the rede 2022 these that the

in Eng



### REDUCTION.

# WEIGHTS AND MEASURES.

TROY WEIGHT.

(21) In 27 ounces of gold, how many grains? Ans. 12960.

(22) Reduce 3 lb. 10 oz. 7 dwt. 5 gr. to grains ? Ans. 22253.

(23) In 8 ingots of silver, each ingot weighing 7 lb. 4 oz. 17 dwts. 15 gr. how many grains? Ans. 341304 gr.

(21) How many ingots weighing 7 lb. 4 oz. 17 dwts. 15 gr. each are there in 341304 grains? Ans. 8 ingots.

### APOTHECARIES' WEIGHT.

(25) In 27<sup>tb</sup>. 7 5. 2 3. 1 D. 2 gr. how many grains? Ans. 159022 grains.

(26) In a compound of 93.43.13. how many pills of 5 grains each? Ans. 916 pills.

AVOIRDUPOIS WEIGHT.

(27) In 14769 ounces, how many cwt.?

Ans. 8 cwt. 0 gr. 27 lb. 1 oz.

(28) In 34 tons, 17 cwt. 1 qr. 19 lb. how many pounds? Ans. 78111 lb.

(29) In 9 cwt. 2 qrs. 14 lb. of indigo, how many half stones, and how many pounds? Ans. 154 half stones, 1078 lb.

(30) How many stones and pounds are there in 27 hogsheads of tobacco, each weighing neat  $8\frac{3}{4}$  cwt.?

Ans. 1890 stones, 26460 lb.

(31) Bought 32 bags of hops, each bag 2 cwt. 1 qr. 14 lb., and another of 150 lb., how many cwt. are there in the whole? Ans. 77 cwt. 1 qr. 10 lb.

(32) In 27 cut. of raisins, how many parcels of 18 lb. each ? Ans. 168.

#### CLOTH MEASURE.

(33) In 27 yards, how many nails? Ans. 432.

(34) In 75 English ells, how many yards?

Ans. 93 yards, 3 grs

(35) In 24 pieces, each containing 32 Flemish ells, how many English ells? Ans. 460 English ells, 4 qrs.

(36) In 17 pieces of cloth, each 27 Flemish ells, how many yar's? Ans. 344 yards, 1 gr.

(37) In 911<sup>1</sup> yards, how many English ells? Ans. 729.
(32) In 12 bales of cloth, each containing 25 pieces, of 15 English ells, ho v many yards? Ans. 5625.

LONG MEASURE.

(39) In M<sup>1</sup>/<sub>2</sub> miles, how many furlongs and poles ? Ans 460 furlongs, 12400 poles.

#### REDUCTION

TUTOR'S

# (40) In 7 miles, how many feet and inches?

Ans. 36960 feet, 443520 inches.

(41) In 72 leagues, how many yards? Ans. 380160 yards.
(42) If the distance from London to Bawtry be accounted

150 miles, what is the number of leagues, and also the number of yards, feet, and inches?

Ans. 50 leagues, 264000 yards, 792000 feet, 9504000 inches.

(43) How often will the wheel of a coach, that is 17 feet in circumference, turn in 100 miles? Ans. 3105844 times round.

(44) How many barley-corns will reach round the globe, the circumference being 360 degrees, supposing that each degree were 69 miles and a half? Ans. 4755801600

See Table of Geometry, page 28.

#### LAND MEASURE.

(45) In 27 a. 3 r. 19 p. how many perches? Ans. 4459.

(46) A person having a piece of ground, containing 37 acres, 1 perch, intends to dispose of 15 acres; how many perches will he have left? Ans. 3521 perches.

(47) There are 4 fields to be divided into shares of 75 perches each; the first field contains 5 acres; the second 4 acres, 2 perches; the third 7 acres, 3 roods; and the fourth 2 acres, 1 rood: how many shares will there be?

Ans. 40 shares, 42 perches rem.

(48) In a field of 9 acres and a half, how many gardens may be made, each containing 500 square yards?

Ans. 91, and 480 yards rem.

#### IMPERIAL MEASURE,

(49) In 10080 pints of port wine, how many tuns? Ans. 5 tuns.

(50) In 35 pipes of Madeira, how many gallons and pints? Ans. 4410 gals. 35280 pints.

(51) A gentleman ordered his butler to bottle off  $\frac{2}{3}$  of a pipe of French wine into quarts, and the rest into pints. How many dozen of each had he? Ans. 28 dozen of each.

(52) In 46 barrels of beer, ho v many pints? Ans. 13248

(53) In 10 barrels of ale, how many gallons and quarts? Ans. 360 gals. 1440 qts.

(54) In 12480 pints of porter, how many kilderkins? Ans. 86 kil. 1 fir. 3 gals.

(55) In 108 barrels of ale, how many hogsheads? Ans. 72.

(56) In 120 quarters of corn, how many bushels, pecks, gallons, and quarts? Ans. 960 bv. 3840 pks. 7680 gal. 30720 qts. te

fe 11

d

n

S

ti

8

UTOR'S

ches. yards. ounted e num-

inches. feet in round. globe, t each 600

459. ing 37 many ches. of 75 cond 4 fourth

*rem.* ardens

rem.

uns. pints? ints. 3 of a pints. f each. 13248 urts? qts. ? als. rals. rals. 20 qts. ASSISTANT.

#### COMPOUND ADDITION.

(57) How many bushels are there in 970 pints?

(58) In 1 score, 16 chaldrons of coals, how r sacks and bushels? Ans. 444 sacks, 1332 c.5 ls.

#### TIME.

(59) In 72015 hours, how many weeks?

Ans. 428 wreks, 4 days, 15 hours.

(60) How many days were there from the birth of Christ, to Christmas, 1794, estimating  $365\frac{1}{4}$  days to the year?

Ans. 6552581 days.

(61) Stowe writes, that London was built 1108 years before our Saviour's birth. Find the number of hours to Christmas, 1794. Ans. 25438932 hours.

(62) From July 18th, 1799, to April 18th, 1826, how many days? Ans.  $9770\frac{1}{2}$  days, reckoning  $365\frac{1}{4}$  days to a year.

(63) In a lunar month, containing 29 days, 12 hours, 44 minutes, 2 seconds and eight-tenths, how many tenth parts of seconds? Ans. 25514428.

(64) How many seconds are there in 18 centuries, estimating the solar year at 365 days, 5 hours, 48 minutes,  $51\frac{1}{2}$  seconds? Ans. 56802476700 seconds.

#### COMPOUND ADDITION

'TEACHES to find the sum of Compound Quantities.

**RULE.** Add the numbers of the *least denomination*; divide the sum by as many as make one of the next greater; set down the remainder (if any) and carry the unotient to those of the next greater: proceed thus to the greatest denomination, which add as in Simple Addition. **PROOF.** As in simple Addition.

Ex	AMPI	LE.
£.	8.	d.
- 15	7.	. 41
17		
1.11		
6	10.	.114
4.	0.	. 9 <del>1</del>
45	17	43
The Property and the		

Say 1, 2, 5, 7 farthings are 1 penny 3 farthings; set down  $\frac{3}{4}$  and carry 'd.-1, 10, 11, 16, 20, 30, 40d. are 3s. 4d.; set down 4d. and carry 3s.-3, 12, 20, 27, 37, 47, 57s. are  $\pounds 2$ . 17s.; set down 17s. and carry  $\pounds 2$ . The rest as in Simple Addition.

In Addition of Money, the reduction of one denomination to the *next greater* is the addy done without the trouble of *dividing*, by the knowledge previously acquired of the Money Tables.

**B**2

#

COMPOUND ADDITION.

[TUTOR'S

.

(

90 1: 1: 2:

AN S S S S S S

	MON	EY.	
(1) <b>£</b> $\delta$ , $d$ . <b>2</b> 13 $5\frac{1}{2}$ <b>7</b> 9 $4\frac{1}{4}$ <b>5</b> 15 $4\frac{1}{2}$ <b>9</b> 17 $6\frac{1}{4}$ <b>7</b> 16 3 <b>5</b> 14 $7\frac{3}{4}$	$\begin{array}{c} (4) \\ \textbf{f}, \textbf{f},$	$\begin{array}{c} (7) \\ \pounds & s. & d. \\ 21 & 14 & 7\frac{1}{4} \\ 75 & 16 & 0 \\ 79 & 2 & 4\frac{1}{4} \\ 57 & 16 & 5\frac{1}{2} \\ 26 & 13 & 8\frac{3}{4} \\ 54 & 2 & 7 \end{array}$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
$\begin{array}{c} (2) \\ \pounds. & d. \\ 27 & 7 & 0 \\ 34 & 14 & 101 \\ 57 & 19 & 21 \\ 91 & 16 & 0 \\ 75 & 18 & 73 \\ 97 & 13 & 5 \end{array}$	$\begin{array}{c} (5)\\ \pounds & s. \ d.\\ 257 & 1 \ 5\frac{1}{4}\\ 734 & 3 \ 7\frac{3}{4}\\ 595 & 5 \ 3\\ 159 \ 14 \ 7\frac{1}{2}\\ 207 \ 5 \ 4\\ 798 \ 16 \ 7\frac{1}{4}\\ \end{array}$	$\begin{array}{c} (8) \\ \textbf{f}, \textbf{s}, \textbf{d}, \\ 73 & 2 & 1\frac{1}{2} \\ 25 & 12 & 7 \\ 96 & 13 & 5\frac{1}{2} \\ 76 & 17 & 3\frac{1}{4} \\ 97 & 14 & 1\frac{1}{2} \\ 54 & 11 & 7\frac{1}{4} \end{array}$	$\begin{array}{c} (11)\\ \pounds & s. & d.\\ 31 & 1 & 1\frac{1}{4}\\ 75 & 13 & 1\\ 39 & 19 & 7\frac{1}{4}\\ 97 & 17 & 3\\ 36 & 13 & 5\\ 24 & 16 & 3\frac{1}{4} \end{array}$
$\begin{array}{c} (3)\\ \pounds. \ s. \ d.\\ 35 \ 17 \ 0\\ 59 \ 14 \ 10\frac{1}{2}\\ 97 \ 13 \ 10\frac{1}{4}\\ 37 \ 16 \ 8\frac{1}{5}\\ 97 \ 15 \ 7\\ 59 \ 16 \ 0\frac{1}{2} \end{array}$	$\begin{array}{c} (6) \\ \pounds & s. \ d. \\ 525 & 2 \ 4\frac{1}{4} \\ 179 & 3 \ 5 \\ 250 \ 4 \ 7\frac{1}{4} \\ 975 \ 3 \ 5\frac{1}{4} \\ 254 \ 5 \ 7 \\ 379 \ 4 \ 5\frac{3}{4} \end{array}$	$\begin{array}{c} (9) \\ \pounds & s. \ d. \\ 127 & 4 & 7\frac{1}{2} \\ 525 & 3 & 10 \\ 271 & 0 & 0 \\ 524 & 9 & 1 \\ 379 & 4 & 0\frac{1}{9} \\ 215 & 5 & 11\frac{3}{4} \end{array}$	$\begin{array}{c} (12) \\ \pounds. s. d. \\ 27 13 5\frac{1}{2} \\ 16 12 10\frac{1}{4} \\ 9 13 0\frac{1}{2} \\ 15 2 10\frac{1}{2} \\ 37 19 0 \\ 56 19 1\frac{3}{4} \end{array}$

# WEIGHTS AND MEASURES.

	TR	loy w	EIG	HT.		) A	рот	HE(	CARI	ES' W			
(1	3)	1	(	14)			(15)	)		1	(16	3)	
oz. dı	ot. gr	r. 16.			gr.	В.	3.	3.	Э.	3.	3.	Э.	gr.
5 1	1	4 5	2	15	<b>Ž2</b>	17	10	7	1	2	1	0	12
7 1	9 2	1 3	11	17	14	9	5	<b>2</b>	2	1	7	1	17
3 1	5 1	4 3	7	15	19	27	11	1	2	10	2		14
7 1	9 22	2   9	1	13	21	9	5	6	1	5	7	1	15
9 1	8 1	5 3	9	7	23	37	10	5	2	9	5	2	13
8 1	3 12	2 5	2	15	17	49	0	7	0	1	4	1	18
-		-   -											
-					-							-	-

#### COMPOUND ADDITION.

ASSISTANT.

(17)

#### AVOIR DUPOIS WEIGHT.

<i>W. oz. dr.</i> 152 15 15	(13) cwt. qrs. lb. 25 1 17	(19) t. cwt. qrs. lh 7 17 2 12
272 14 10	$   \begin{array}{ccccccccccccccccccccccccccccccccccc$	5 5 3 14
$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
173 6 2	17 0 19	7 9 3 20
635 13 13	55 2 16	8 5 1 24
	LONG MEASURE.	

(20)	yds.	ft.	in.	(21) lea.	m.	fur	. po.	(22)	m.	fur	.yds.
	225	1	9	72	2	1	<b>i</b> 9		39	6	
	171	0	3	27	1	7	22		14	7	214
	52	2	6	35	2	5	31		3	4	160
	397	0	10	79	0	6	12		45	3	202
	154	2	7	51	1	6	17		17	1	19
	137	1	4	72	0	5	21		32	4	176
						-		1			•
						10.100		÷			

LAND MEASURE. CLOTH MEASURE. (23)(24)(25) (26)yds. E. e. qrs, n. qrs. n. α. r. p. а.  $\mathbf{2}$ , З 79 0 

#### IMPERIAL MEASURE.

	W	INE.	ALE AND BEER							
(27)		(28)	(29)	30						
hhds.gals.	qts.	t. hhd.gal.qts.	bar. fir ga!	khd. gai. its.						
31 57	1	14 3 27 2	25 2 7	76 51 2						
97 18	2	19 2 56 3	17 3 5	57 3 3						
76 13	1	17 0 39 2	96 2 6	97 27 3						
55 46	2	75 2 16 1	75 1 8	22 17 2						
87 38	3	54 1 19 2	96 3 7	32 :9 .3						
55 17	1	97 3 54 3	75 0 5	55 18 3						
			1							
-										

\$

T.

TOR'S

đ.

d.

-

2 13 1 18 р. 14

۰.

#### COMPOUND ADDITION.

LTUTCR'S

SFU

t:

fi

1

l

t

	D	RY.				1			TIME				
			(3	12)			(33)		1		(34)		
Ъ.	p.	b.	p.	gal.	gts.	w.	d.	h.	10.	à.	h.	15.	
2	1	16	2	1	2	71	3	11	57	2	15	42	41
0	1	21	0	1	3	51	2	9	95	3	21	27	51
7	0	7	3	0	0	76	0	21	76	0	15	37	28
3	2	15	1	1	2	95	3	21	53	2	21	42	27
6	3	3	2	0	1	79	1	15	98	2	18	47	38
	-												
	0 7 3	(31) <b>b. p.</b> <b>2</b> 1 <b>0</b> 1 <b>7</b> 0 <b>3</b> 2	b.     p.     b.       2     1     16       0     1     21       7     0     7       3     2     15	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$								

(35) A, B, C, and D, were partners in the purchase of a quantity of goods: A laid out  $\pounds$ 7. half-a-guinea, and a crown; B, 49s. C, 54s. 6d. and D, 87d. What was the purchase? Ans.  $\pounds$ 13.6.3.

(36) A man lent his friend at different times these several sums, viz.  $\pounds 63.-\pounds 25.15.-\pounds 32..7.-\pounds 15..14..10$ . and four score and nineteen pounds, half-a-guinea, and a shilling. How much was the whole loan? Ans.  $\pounds 236..8..4$ .

(37) Bought goods, for which I paid  $\pounds 54..17$ ; for packing 13s. 8d.; carriage  $\pounds 1..5..4$ ; and expenses over making the bargain 14s. 3d. What was the whole cost? Ans.  $\pounds 57..10..3$ .

(38) A nobleman, previous to quitting town, wished to discharge his tradesmen's bills. On inquiry he found that he owed 82 guineas for rent;—to his wine-merchant, £72.5; to his confectioner, £12..13..4;—to his draper, £47..13..2; to his tailor, £110..15..6;—to his coach-maker, £157..8;—to his tailow chandler, £8..17..9;—to his corn-factor, £170..6..8; —to his brewer, £52..17..0;—to his butcher, £122..11..5; to his baker, £37..9..5;—and to his servants for wages, £53..18. What money must he draw from his banker, including £100. that he wished to take with him?

Ans. £1032..17..3.

(39) A father was 24 years of age (allowing 13 months to a year, and 28 days to a month) at the birth of his first child : between the eldest and next born was 1 year, 11 months, and 14 days; between the second and third were 2 years, 1 month, and 15 days; between the third and fourth, 2 years, 10 months, and 25 days. When the fourth was 27 years, 9 months, and 12 days old, what age was the father?

Ans. 58 years, 7 months, 10 days.

(40) A clerk having been out collecting debts, presented an account that A paid him  $\pounds 7..5..2$ ;—B  $\pounds 15..18..61$ ;— C  $\pounds 150..13..21$ ;—D  $\pounds 17..6..8$ ;—E 5 guineas, 2 crown pieces.

#### COMPOUND SUBTRACTION.

ASSISTANT.

4 half-crowns and 4s. 2d.;—F paid him only twenty groats;— G £76..15..9 $\frac{1}{2}$ ;—and H £121..12..4. How much was the whole amount? Ans. £396..7..6 $\frac{1}{2}$ .

(41) A nobleman had a service of plate, which consisted of twenty dishes, weighing 203 oz. 8 dwts.; 36 plates, 408 oz. 9 dwts.; 5 dozen spoons, 112 oz. 8 dwts.; 6 salts, and 6 pepper-boxes, 71 oz. 7 dwts.; knives and forks, 73 oz. 5 dwts.; two large cups, a tankard, and a mug, 121 oz. 4 dwts.; a teaurn and lamp, 131 oz. 7 dwts.; with sundry other small articles, weighing 105 oz. 5 dwts. The weight of the whole is required. Ans. 102 lb. 2 oz. 13 dwts.

(42) A hop-merchant buys 5 bags of hops, of which the first weighed 2 cwt. 3 qrs. 13 lb.; the second, 2 cwt. 2 qrs. 11 lb.; the third, 2 cwt. 3 qrs. 5 lb.; the fourth, 2 cwt. 3 qrs. 12 lb.; the fifth, 2 cwt. 3 qrs. 15 lb. He purchased also two pockets, each pocket weighing 84 lb. I desire to know the weight of the whole. Ans. 15 cwt. 2 qrs.

#### COMPOUND SUBTRACTION

#### TEACHES to find the difference of Compound Quantities.

RULE. Subtract as in integers: but borrow (when there is occasion) as many as are equal to one of the next greater denomination: observing to carry one to the next for that which was borrowed."

**PROOF.** As in Simple Subtraction.

#### MONEY.

(1) £. From 715 Take 476	s. 22 3	$d. 7\frac{1}{4} \\ 8\frac{1}{2}$	(2)	£. 316 218		(3)	£. 87 79	-	
			I		 	I		 	

\*.EXAMPLE. Subtract £54..17..93. from £89..12..71.

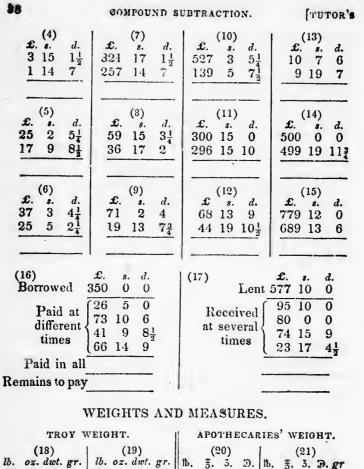
£. s. d.	Because 3 farthings cannot be taken from 2, say 3
89.,1271	from 4, 1, and 2 are 3; set down 3 and carry 11 and
54.:1793	9 are 10, 10 from 12, 2, and 7 are 9; set down 9 and
24.14.91	carry 11 and 17 are 18, 18 from 20, 2, and 12 are 14; set down 14 and carry 1 to the pounds.

TCR'S

of a own; 50 ? ..3. overal four illing. ..4. cking e bar-10..3. o disat he .5;---.2;--;-to .6..8; .5;---

ages, or, in-...3. ths to

hild ; , and ionth, onths, , and



TROY WEIGHT.	APOTHECARIES' WEIGHT.					
(18) 10. oz. dwt. gr. 52 1 7 2 7 2 2 7 (19) 10. oz. dwt. gr. 7 2 2 7		(21) 1b. 3. 3. <b>D. gr</b> 9 7 2 1 13				
<u>39 0 15 7</u> 5 7 1 5	$\left\  \frac{2  5  2  1}{\underline{\qquad}} \right\ $	5 7 3 1 18				
(22) 1b. ox. dr. (23) cw 35 10 5 33	t. qr. lb.   (24	) t. cwt. qrs. lb. 21 1 2 7 9 11 3 15				

y 10

3.

\*(

pa

it, CE in he he

ye

ASSISTANT.]

LCNG 1	MEASURE.	IMPERIAL MEASUREWINE.						
(25)	(26)	(31) (32)						
yds. ft. in.	lca. mi. fur. po.	hhd. gal. qts. pts.	tun hhd. gal.qts.					
107 2 10	147 2 6 29	47 47 2 1	42 2 37 2					
78 2 11	58 2 7 33	28 59 3 0	17 3 49 3					
CLOTH	MEASURE.	ALE ANI	D BEER.					
(27)	(28)	(33)	(34)					
yds. grs. n.	E.e. grs. n.	ar. fir. gal.	hhd.gal. qts.					
71 1 2	35 2 1	37 2 1	27 27 1					
3 2 1	14 3 2	25 1 7	12 50 2					
	IEASURE.	CORN AN						
(29)	(30)	(35)	(36)					
<i>a. r. p.</i> <b>175</b> 1 27	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	sc. ch. sa. b. 3 16 1 0					
	$   \begin{array}{ccccccccccccccccccccccccccccccccccc$							
59 0 37	279 3 5	57 2 3						
		ME.						
	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	m. sec.   † (3	39) yrs. m. d. 10 7 20					
		<u>19 53 47</u>						

(40) When an estate of £300. per annum is reduced by the payment of taxes to 12 score and £14..6. what are the taxes? Ans. £45..14.

(41) A horse with his furniture is worth £37..5; without it, 14 guineas; how much does the price of the furniture exceed that of the horse? Ans. £7..17.

(42) A merchant commencing trade, owed  $\pounds 750$ ; he had in cash, commodities, the stocks, and good debts,  $\pounds 12510..7$ ; he cleared the first year by commerce  $\pounds 452..3..6$ . What was he then worth? Ans.  $\pounds 12212..10..6$ .

(43) A gentleman left £45247. to his two daughters, of

• In this example allow 4 weeks to a month, and 13 months to the year.

\* In this, reckon 30 days to a month, and 12 months to the year.

OR's

d. 6 7

d. 0 113

> d. 0 6

)

1-2

٢.

gr 13

18

ta ar

11

pe

which the younger was to have 15 thousand, 15 hundred, and twice  $\pounds$ 15. What was the elder sister's fortune ?

Ans. £28717. (44) A tradesman being insolvent, called all his creditors together, and found he owed to A £53..7..6;—to B £105..10, —to C £34..5..2;—to D £28..16..5;—to E £14..15..8;—to F £112..9;—and to G £143..12..9. The value of his stock was £212..6; and the amount of good book-debts was £112..8..3; besides £21..10..5. money in hand. How much would his creditors lose by taking the whole of his effects? Ans. The creditors lost £146..11..10.

(45) My agent at Seville, in Spain, renders use 2.140.111.10. ing account of money received for the sale of goods sent him on commission, viz. for bees' wax £37..15..4; stockings' £37..6..7; tobacco £125..11..6; linen cloth £112..14..8; tin £115..10..5. He informs me at the same time, that he has shipped, agreeably to my order, wines, value £250..15; fruit £51..12..6; figs £19..17..6; oil £19..12..4; and Spanish wool, value £115..15..6. How stands the balance of the account between us? Ans. Due to the agent £28..14..4.

(46) The great bell at Oxford, the heaviest in England, is stated to weigh 7 tons, 11 cwt. 3 qrs. 4 lbs., that of St. Paul's, in London, 5 tons, 2 cwt. 1 qr. 22 lbs., and that of Lincoln, called the Great Tom, 4 tons, 16 cwt. 3 qrs. 16 lbs. How much is the aggregate weight of these three bells inferior to that of the great bell at Moscow, which is 198 tons?

Ans. 180 tons, 8 cwt. 3 qrs. 14 lbs.

# COMPOUND MULTIPLICATION

Is the method of multiplying Compound Quantities.

RULE. Multiply the *least denomination*; reduce the product and carry to the next, as directed in Compound Addition; and the same with the rest.

When the multiplier is a composite number above 12, multiply (as before directed) by its component parts. For other numbers, multiply by the factors of the nearest-composite; adding to the last product, so many times the top line as will supply the deficiency; or subtracting so many times, if there is an excess.

#### UTOR'S

ed, and

28717. editors 5..10, 3 ;---to stock s was inuch ects ? .10. ollows sent kings ' 8; tin e has ; fruit wool, count ..4. nd, is aul's. icoln, How ior to

duct and

bs.

mulother site : will here

ASSISTANT.

MON	EY.
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
1 5 31	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	7 $2\frac{3}{4} \times 75$ . (20) 0 6 4×43.

(21) What is the value of 127 th. of souchong tea, at 12s. 3d. per 1b.? Ans. £77..15..9.

(22) 135 stones of soap, at 7s. 5d. per stone? Ans. £50..1..3.

(23) 74 ells of diaper, at 1s.  $4\frac{1}{2}d$ . per ell? Ans. £5..1..9. (24) 6 doz. pairs of gloves, at 1s. 10d. per pair? Ans. £6..12.

Note, When the fraction  $\frac{1}{4}$ ,  $\frac{1}{2}$ , or  $\frac{3}{4}$  is connected with the multiplier, take half the given price (or the price of one) for 1, half of that for 1, and for 2, add them both together.§

\* In this example, say twice 3 are 6, 6 farthings are 1.1d. set down 1d. and carry 1; twice 7 are 14 and 1 are 15, 15d. are 1s.  $\overline{3}d$ . set down  $\overline{3}d$ . and carry 1; twice 12 are 24 and 1 are 25, 25s. are £1..5. set down 5s. and carry 1; twice 5 are 10 and 1 are 11, set down 1 and carry 1; twice 3 are 6 and 1 are 7, set down 7.

s. d.	£. s. d.
† 9 6	<b>‡</b> 1 2 6
$2 \times 9 = 18$	8×3+2=26
19 0	9 0 0
9	3
£811 0 Ans.	27. 0. 0
	Multiplicand×2=2 5 0
§ EXAMPLE. What is the value of 114 lbs. of tea, at 10s. 9d. per 3. ?	$\begin{array}{c} \underline{11} \\ \underline{11} \\ \underline{11} \\ \underline{11} \\ \underline{11} \\ \underline{15} \\ \underline{15} \\ \underline{15} \\ \underline{11} \\ \underline{15} \\ \underline{11} \\ \underline{15} \\$
•	£6 6 33 Ans.
	and on of Arts.

41

COMPOUND MULTIPIICA" JN.

(25) What is the value of 251 ells of Holland, at 3s. 41d er ell? Ans. £4..6..03. (26)  $75\frac{1}{3}$  lb. of hemp, at 1s. 3d. per lb.? Ans. £4..14..41. (27) 191 yds. of muslin, at 4s. 3d. per yd. ? Ans. £4..2..101. (28) 351 cwt. of raw sugar, at £4..15..6. per cwt.? Ans. £169..10..3. (29) 1511 cwt. of raisins, at £1..17..10. per cwt.? Ans. £755..15..3. (30) 117<sup>1</sup>/<sub>4</sub> gallons of gin, at 12s. 6d. per gallon ? Ans. £73..5..71. (31) 853 cwt. of logwood, at £1..7..8. per cwt. ? Ans. £118..12..5. (32) 17<sup>3</sup>/<sub>4</sub> yards of superfine scarlet cloth, at £1..3..6. per yard? Ans. £20..17..11. (33) 371 lb. of hyson tea, at 12s. 4d. per lb.? Ans. £23..2..6 (34) 563 cwt. of molasses, at £2..18..7. per cwt. ? Ans. £166..4..71. (35) 873 lb. of 'Turkey coffee, at 4s. 3d. per lb.? Ans. £18..12..111. (36)  $120\frac{3}{4}$  cwt. of hops, at £4..7..6. per cwt.? Ans. £528..5..71. When the multiplier is large, multiply the given quantity

(or price) by a series of *tens*, to find 10, 100, 1000 times, &c., as far as to the value of the *highest place* of the multiplier; multiply the last product by the figure in that place, and each preceding product by the figure of corresponding value; that is, the product for 100 by the *number of hundreds*, the product for 10 by the *number of tens*, and the *original quantity* by the *units' figure*. cc. The *sum* of the products thus obtained will be the *total product*.\*

\* EXAMPLE. Multiply £7..14..93. by 3645.

	$\pounds$ s. d. $\pounds$ s. d. times. 714. $9_{3}^{1} \times 5 = 331311_{2}^{1} = 5$ 10
The product for 10	$77711 \times 4 = 309118 = 40$
The product for 100	$773192 \times 6 = 4643150 = 600$
The product for 1000	$\begin{array}{c} \overline{7739118} \times 3 = 23218150 = 3000 \\ Ans. 232101571 = 3645 \end{array}$

42

[TUTOR'S

уe

m

of

of

hi

ea gi

to

£ ha

ye

w If 1(

1

ar

3 m

#### ASSISTANT.] COMPOUND MULTIPLICATION.

(37) 407 lb. of gall-nuts, at 3s.  $9\frac{1}{2}d$ . per lb.?

(38) 729 stones of beef, at 7s.  $7\frac{1}{4}d$ . per stone ?

Ans. £277..3..54.

(39) 2068 yards of lace, at 9s. 5<sup>1</sup>/<sub>2</sub>d. per yard? Ans. £977..19 10.
(40) What is the produce of a toll-gate in the course of the year, if the tolls amount, on an average, to 11s. 7<sup>1</sup>/<sub>2</sub>d. per day?

Ans. £212. 3.11.

48

(41) How much money must be equally divided among 18 men, to give each £14.6.8 $\frac{1}{2}$ ? Ans. £258.0.9.

(42) A privateer manned with 250 sailors captured a prize of which each man shared  $\pounds 125..15..6$ . What was the value of the prize? Ans.  $\pounds 31443..15$ .

(43) What sum did a gentleman receive as a dower with his wife, whose fortune was a cabinet with two divisions, in each division 87 drawers, and each drawer containing 21 guineas?  $Ans. \pm 3836..14$ .

(44) A merchant began trade with £19118; for 5 years together he cleared £1086. a year; and the next 4 years £2715..10.6. a year; but the last 3 years he was in rade he had the misfortune to lose, upon an average, £475..4..6. a year. What was his real fortune at the end of the 12 years ? Ans. £33984..8..6.

(45) In many parts of the kingdom coals are weighed in the wagon or cart upon a machine, constructed for the purpose. If 3 of these draughts amounted together to 137 cwt. 2 qrs. 10 lb.; and the tare, or weight of the wagon, was 13 cwt. 1 qr.; how many coals had the customer in 12 such draughts? Ans. 391 cwt. 1 qr. 12 lb.

(46) A certain gentleman lays up every year  $\pounds 294..12..6$ . and spends daily  $\pounds 1..12..6$ . What is his annual income? Ans.  $\pounds 887..15$ .

#### WEIGHTS AND MEASURES.

(47) Multiply 9 lb. 10 oz. 15 dwts. 19 gr. by 9, 11, and 12

(48) Multiply 23 tons, 9 cwt. 3 qrs. 18 lb. by 7, 8, and 9.

(49) Multiply 107 yards, 3 qrs. 2 nails, by 10, 17, and 29.

(50) Multiply 33 bar. 2 fir. 3 gal. by 11, and 12.

(51) Multiply 110 miles, 6 fur. 26 poles, by 12, 13, and 39.
(52) A humar month contains 29 days, 12 hours, 44 min.
3 seconds nearly. What time is contained in 13 lunar months?

TOR'S

 $.0\frac{3}{4}.$ 

.4<u>1</u>. 2..10<u>1</u>.

)..3.

5..3.

.71.

2..5. 6. per .1<u>‡</u>.

..2..6

 $.7\frac{1}{4}.$ 

11.

 $.7\frac{1}{2}.$ 

antity , &c., ; muleach ; that roduct

oy the d will

28.

Ans. £77..3..21.

# COMPOUND DIVISION

# TEACHES to find any required part of a Compound Quantity

RULE. Divide the greatest denomination; reduce the remainder to the next less, to which add the next; divide that, and proceed as be fore to the end.

When the divisor is above 12, the work must be done at length: un less it is a *compósite* number, for which observe the directions in Simple Division.

PROOF by Multiplication.

41

#### MONEY.

$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	(16) 248 17 4 by 99. (17) 928 12 8 by 110 (18) 608 13 9 by 144.

(19) Divide £1407..17..7. by 243.

(20) Divide £700791 .14..4. by 1794.

(21) Divide £490981..3..712. by 31715.

(22) Divide £19743052..5.712. by 214723.

(23) If a man spend £257..2..5. in 12 months, what is that per month? Ans. £21..8.. $6\frac{1}{4}$   $\frac{8}{2}$ .

(24) The clothing of 35 charity boys came to  $\pounds 57..3..7$ . what was the expense of each boy? Ans.  $\pounds 1..12..8_{12}^{12}$ .

(25) If I gave £37..6..4 $\frac{3}{4}$ . for nine pieces of cloth, what was that per piece? Ans. £4..2..11 $\frac{7}{4}$ .

\* EXAMPLE. Divide £27..14..111. by 5.

 $\begin{array}{c} \textbf{\pounds. s. d.} \\ \textbf{5)} 27..1 \frac{4..111}{5..10..11\frac{3}{3}} \end{array}$ 

Say the fives in 27, 5 times 5 are 25 and 2 over; £2. are 40s. and 14 are 54, the fives in 54, 10 times 5 are 50 and 4 over; 4s. are 48d. and 11 are 59, the fives in 59, 11 fives are 55 and 4 over; 4d. are 16 qrs. and 2 are 18, the fives in 18, 3 times five are 15, and 3 over, or  $\frac{3}{4}$ . £2 pri

.

mi

the

the

fer

bo

wi

he

#### FUTOR'S

#### antity

under to d as bo

sth: nn 1 Simple

*d*. 0

1. 2. 2.

9. 10 44.

s that  $\frac{3}{2}$ . 3..7.  $\frac{2}{5}$ . what  $\frac{7}{5}$ .

imes 59, are five

#### ASSISTANT.]

#### PROMISCUOUS EXAMPLES.

(26) If 20 cwt. of tobacco cost  $\pounds 27..5..4\frac{1}{2}$ ; at what rate did I buy it per cwt.? Ans.  $\pounds 1..7..3\frac{1}{2}$ .

(27) What is the value of one hogshead of beer, when 120 hogsheads are sold for £154..17. 10? Ans. £1 .5.9 $\frac{3}{4}$   $\frac{1.6}{120}$ .

(28) Bought 72 yards of cloth for  $\pounds$ 85..6. What was the price per yard? Ans.  $\pounds$ 1..3..8 $\frac{1}{4}$  $\frac{24}{7}$ .

(29) Gave £275..3..4. for 18 bales of cloth. What is the price of one bale? Ans. £15..5..8 $\frac{3}{2}$   $\frac{19}{2}$ .

(30) A prize of £7257..3..6. is to be equally divided among 500 suilors. What is each man's share ? Ans. £14..10..31  $\frac{2}{3}$ 

(31) A club of 25 persons joined to purchase a lottery ticket of  $\pounds 10$ . value, which was drawn a prize of  $\pounds 4000$ . What was each man's contribution, and his share of the prizemoney? Ans. Each contribution 8s. and share of prize  $\pounds 160$ .

(32) A tradesman cleared £2805. in  $7\frac{1}{2}$  years. What was his yearly profit? Ans. £374.

(33) What was the weekly salary of a clerk who received  $\pounds 266..18..1\frac{1}{2}$ . for 90 weeks? Ans.  $\pounds 2..19..3\frac{3}{2}$ .

(34) If 100000 quills cost me £187..17..1. what is the price per thousand? Ans. £1..17. $6\frac{3}{4} \frac{40}{100}$ .

#### WEIGHTS AND MEASURES.

(35) Divide 83 lb. 5 oz. 10 dwts. 17 gr. by 8, 10, and 12.

(36) Divide 29 tons, 17 cwt. 0 qrs. 18 lb. by 9, 15, and 19.

(37) Divide 114 yards, 3 qrs. 2 nails, by 10, and 16.

(38) Divide 1017 miles, 6 fur. 38 poles, by 11, and 49.

(39) Divide 2019 acres, 3 roods, 29 perches, by 26.

(40) Divide 117 years, 7 months, 26 days, 11 hours, 27 minutes, by 37.

#### PROMISCUOUS EXAMPLES.

(1) Of three numbers, the first is 215, the second 519, and the third is equal to the other two. What is the sum of  $\Leftrightarrow$  them all ? Ans. 1468.

(2) The less of two sums of money is  $\pounds 40$ . and their difference  $\pounds 14$ . What is the greater sum, and the amount of both? Ans.  $\pounds 54$ . the greater,  $\pounds 94$ . the sum.

(3) what number added to ten thousand and eighty-nine,
will make the sum fifteen thousand and forty? Ans. 4951.
(4) What is the difference between six dozen dozen, and half a dozen dozen; and what is their sum and product?

Ans. Diff. 792, sum 930, product 62208.

(5) What difference is there between twice night and fifty and twice fifty-eight, and what is their product ?

Ans. 50 diff. 7656 product.

(6) The greater of two numbers is 37 times 45, and their difference is 19 times 4 : required their sum and product. Ans. 3254 sum, 2645685 product.

(7) A gentleman left his elder daughter  $\pounds 1500$ . more than the younger, whose fortune was 11 thousand, 11 hundred, and  $\pounds 11$ . Find the portion of the elder, and the amount of both. Ans. Elder's portion £13611. amount £25722.

(8) The sum of two numbers is 360, the less is 144. What is their difference and their product?

Ans. 72 difference, 31104 product.

(9) There are 2545 bullocks to be divided among 509 men. Required the number and the value of each man's share, supposing every bullock worth £9..14..6.

Ans. Each man had 5 bullocks, and £48..12. 6. for his share. (10) How many cubic feet are contained in a room, the length of which is 24 feet, the breadth 14 feet, and the height 11 feet ?\* Ans. 3696.

(11) A gendeman's garden, containing 9625 square yards, is 35 yards broad : what is the length ? Ans. 275 yards.

(12) What sum added to the 43d part of £4429, will make the total amount =  $\pounds 240$ ? Ans. £137.

(13) Divide 20s. among A, B, and C, so that A may have 2s. less than B, and C 2s. more than B.

Ans. A 4s. 8d. B 6s. 8d. and C 8s. 8d. (14) In an army consisting of 187 squadrons of horse, each 157 men, and 207 battalions of foot, each 560 men, how many effective soldiers are there, supposing that in 7 hospitals there are 473 sick? Ans. 144806.

(15) A tradesman gave his daughter, as a marriage portion, a scrutoire, containing 12 drawers ; in each drawer were six divisions, and in each division there were £50. four crown pieces, and eight half-crown pieces. How much had she to her fortune? Ans. £3744.

(16) There are 1000 men in a regiment, of whom 50 are officers : how many privates are there to one officer ? Ans. 19.

(17) What number must 7847 be multiplied by, to produce 3013248? Ans. 384.

." Multiply the three dimensions continually together.

qua apa

(

ſ

ren

sun

riot

four

eac

equ

pub

-te

kce

Wh

12s

purs

the

is th

weig

(?

(% ed 1

(

( £1

(

ASS

quir (2 and 178 (2man (2ing

sterl

sabti

# UTOR'S

ASSISTANT.]

d fifty

uct. I their et. uct. e than ndred, unt of 22. 144.

met. men. , sup-

share. a, the height 96. vards, ds. make 87. have

Bd. each nany here 6. tion, six own ie to 4. are . 19. luce 4.

#### PROMISCUOUS EXAMPLES.

(18) Suppose I pay eight guineas and half-a-crown for a quarter's rent, but am allowed 15s. for repairs; what does my apartment cost me annually, and how much in seven years?

Ans. In one year,  $\pounds$ 31..2. In seven,  $\pounds$ 217..14. (19) The quotient is 1083; the divisor 28604; and the remainder 1788; what is the dividend? Ans. 30979920.

(20) An assessment was made on a certain hundred, for the sum of £386...15..6. the amount of the damage done by a riotous assemblage. Four parishes paid £37..14..2. each; four hamlets £31..4..2. each; and four townships £18..12..6. each: how much was deficient? Ans £36..12..2

(21) An army, consisting of 20,000 men, got a booty of  $\pounds 12,000$ ; what was each man's share, if the whole were equally divided among them? Ans. 12s.

(22) A gentleman left, by will, to his wife, £4560;—to a public charity, £572..10;—to four nephews, £750..10. each; —to four nieces, £375. 12..6. each;—to thirty poor house-keepers, 10 guineas each;—and to his executors, 150 guineas. What was the amount of his property? Ans. £10109..10.

(23) My purse and money, said Dick to Harry, are worth 12s. 8d. but the money is worth seven times the value of the purse : what did the purse contain ? Ans. 11s. 1d.

(24) Supposing 20 to be the remainder of a division, 423 the quotient, and the divisor the sum of both, plus 19; what is the dividend? Ans. 195446.

(25) A merchant bought two lots of tobacco, which weighed 12 cwt. 3 qrs 15 lb. for £114..15..6.; their difference in weight was 1 cwt. 2 qrs. 13 lb. and in price £7..15..6. Required their respective weights and value.\*

Ans. Greater weight 7 cwt. 1 qr. value £ ....5..6.

Less weight 5 cwt. 2 qrs. 15 lb. value £53..10. (26) Divide 1000 crowns in such a manner among A, B. and C, that A may receive 129 crowns more than B, and B. 178 less than C. Ans. A 360 crowns, B 231, C 409.

(27) If 103 guineas and 7s. be divided among 7 men, 1 many pounds sterling is the share of each? Ans. £15..10.

(28) A certain person had 25 purses, each purse containing 12 guineas, a crown, and a moidoire, how many pounds sterling had he in all? Ans. £355.

subtract the difference to the sum, and divide by 2 for the greater;

#### PROPORTION.

48

[TUTOR'S

(29) A gentleman, in his will, left £50. to the poor, and ordered that  $\frac{1}{3}$  should be given to old men, each man to have  $5s.-\frac{1}{4}$  to old women, each woman to have  $2s. 6d.-\frac{1}{4}$  to poor boys, each boy to have  $1s.-\frac{1}{6}$  to poor girls, each girl to have 9d. and the remainder to the person who distributed it: how many of each sort were there, and what remained for the person who distributed the money?

# Ans. 66 men, 100 women, 200 boys, 222 girls; £2.13.6. for the distributor.

(30) A gentleman sent a tankard to his goldsmith, that weighed 50 oz. 8 dwts. to be made into spoons, each weighing 2 oz. 16 dwts. how many would he have? Ans. 18.

(31) A gentleman has sent to a silversmith 137 oz. 6 dwts 9 gr. of silver to be made into tankards of 17 oz. 15 dwts. 10 gr each; spoons, of 21 oz. 11 dwts. 13 gr. per dozen; salts, of 3 oz. 10 dwts. each; and forks, of 21 oz. 11 dwts. 13 gr. per dozen; and for every tankard to have one salt, a dozen spoons and a dozen forks: what number of each will he have?

Ans. Two of each sort, 8 oz. 9 dwts. 9 gr. over.

(32) How many parcels of sugar of 16 lb. 2 oz. each are there in 16 cwt. 1 qr. 15 lb.?

Ans. 113 parcels, and 12 lb. 14 oz. over.

(33) In an arc of 7 signs, 14° 3' 53", how many seconds? Ans. 806633".

(34) How many *lbs.* of *lead* would counterpoise a mass of *bullion* weighing 100 *lbs.* Troy ?\* Ans. 82 *lb.* 4 oz.  $9_{175}^{25} dr$ .

(35) If an apothecary mixes together 1 *lb*. avoirdupois of white wax, 4 *lbs*. of spermaceti, and 12 *lbs*. of olive oil, how many ounces, apothecaries' weight, will the mass of ointment weigh, and how many masses of 3 drams each will it contain? Ans. The whole 247 oz.  $7_{T^{6}AZ}$  dr. and 661 of 3 dr. each.

# PROPORTI

PROPORTION is either DIRECT, OF INVERSE. It is commonly called the RULE OF THREE; there being always three num. bers or terms given, two of which are terms of supposition; and the other is the term of demand : because it requires a fourth

\* But is the term denoting gold or silver in the mass. Lead is weighed by Avoirdupois weight. See the Table of Comparison of WriteHTS.

A551

term whi of a is o whi A thir low

> RE the the

R duc nati T T to r 2 be o quo 3 cati

\*

and ans be t

D11 ed

arri

froi

or tha the

pro

reg

I

#### TUTOR'S

to have to poor to have it: how for the

#### girls;

th, that weighs. 18. 6 dwts f. 10 gr alts, of gr. per spoons e? over. ach are

over. econds ? 533''. mass of  $\frac{2}{75} dr$ . pois of bil, how intment ontain ? each.

nmonly e nun. on; and fourth

Lead is

#### ASSISTANT.]

term to be found, in the same proportion to itself, as that which is between the other two.

GENERAL RULE FOR STATING THE QUESTION. Fut the term of demand in the third place: that term of supposition which is of the same kind as the demand, the first; and the other, which is of the same kind as the required term, the second.\*

Also, the terms being thus arranged, reduce the first and third (if necessary) into one name, and the second into the lowest denomination mentioned.

#### THE RULE OF THREE DIRLOT

**REQUIRES** the *fourth* term to be greater than the second, when the third is greater than the first; or the fourth to be less than the second, when the third is less than the first.

RULE. Multiply the second and third together, and divide their product by the first: the quotient will be the answer, in the same denomination as the second.

The following methods of contracting the operations in the RULE or THREE are highly important, and should never be lost sight of:--

1. Let the first and third terms be reduced no lower than is necessary to make them of the same denomination.

2. Let the dividing term and either (but not both) of the other terms be divided by any number that will divide them exactly; and use the quotients instead of the original numbers.

3. When it is conveniently practicable, work by Compound Multiplication and Division, instead of reducing the terms.

\* Some modern authors prefer placing the term of demand the second, and that similar to the required term the third. This arrangement will answer the purpose equally well, observing that those of like kind must be reduced (if necessary) to the same name.

† The following GENERAL RULE comprehends both the cases of DIRECT and INVERSE PROPORTION under one head; which is considered by many scientific men of the present day as a more systematic arrangement.

RULE. The question being stated, and the terms prepared, consider, from the nature of the case, whether the required term is to be greater or less than the second, or term of similar kind: if greater, nultiply that similar to the answer by the greater of the other two, and divide the product by the less; if less, multiply it by the less and divide the product by the greater. In either case the quotient will be the term required, in the same denomination as the similar term.

Note. It is evident that the above Rule will answer generally, whether the term of demand is put in the second or third place.

# RULE OF THREE DIRECT.

TUTOR'S

(1) If one lb. of sugar cost  $4\frac{1}{2}d$ . what will 54 lb. cost? (2) If a gallon of beer cost 10d. what is that per barrel?

(3) If a pair of shoes cost 4s. 6d. what is the value of 12 dozen pairs ?†

m

ya

E

5

of

pı

W

tĿ

ir

al

n

e

V

1

ri

W

р

(4) If one yard of cloth cost 15s. 6d. what will 32 yards cost at the same rate ?

(5) If 32 yards of cloth cost  $\pounds 24..16$ , what is the value of one yard?

(6) If I gave £4..18. for 1 cut. of sugar, at what rate did I buy it per lb.?

(7) Bought 20 pieces of cloth, each piece 20 ells, for 12s 6d. per ell, what is the value of the whole? Ans. £250.

(8) What will 25 cwt. 3 qrs. 14 lb. of tobacco come to, at 151.d. per lb.?

(9) Bought 271 yards of muslin, at 6s.  $9\frac{1}{2}d$ . per yard, what is the amount of the whole?

(10) Bought 17 ewt. 1 qr. 14 lb. of iron, at 34d. per lb what was the price of the whole ?

(11) If coffee is sold for  $5\frac{1}{2}d$ . per ounce, what will be the price of 2 cwt.?

(12) How many yards of cloth may be bought for £21. 11..1 $\frac{1}{2}$ . when  $3\frac{1}{2}$  yards cost £2..14..3.?

Ans. 27 yards, 3 qrs. 13, nail. (13) If 1 cut. of Cheshire cheese cost £1..14..8. what must I give for 34 16.?

(14) Bought 1 cwt. 24 lb. 8 oz. of old lead, at 9s. per cwt. what did the lead cost?

Ans. 10s. 111 1224d. (15) If a gentleman's income be £500. a year, and he spend 19s. 4d. per day, what is his annual saving? Ans. £147..3..4.

(16) If 14 yards of cloth cost 10 guineas, how many Flemish ells can 1 buy for £283..17..6. ? Ans. 504 Fl. ells, 2 grs.

(17) If 504 Flemish ells, 2 quarters, cost £283..17..6. what is the cost of 14 yards? Ans. £10..10.

* As 1: $4\frac{1}{4}$ : : 54 $\frac{4}{18}$ $\frac{13}{4979}$ $\frac{13}{48}$	1	6 <sup>5</sup>	pr. s. d. prs. A. 1 : 4.6 : : 144
$\frac{18}{12)243} \frac{\overline{4})972}{20s} \frac{qrs.}{3d.}$	•£103.	Ans.	2140 12 £328.0, Ana

# TUTOR'S

b. cost ? er barrel ? . £1..10. value of 12 ll 32 yards £24..16. ie value of

15s. 6d. at rate did s.  $10\frac{1}{2}d$ . s, for 12s  $\pounds$  £250. ome to, at 0.7.3.3. rard, what  $0.0\frac{3}{2}\frac{1}{2}$ . l. per lb  $0.7.0\frac{1}{2}$ .

ill be tho 2..2..8. or £21.

nail. hat must s. 1d. per cwt. 1212d. te spend 47..3..4. y Flems, 2 qrs. 6. what

prs. : 144

# ASSISTANT.] RULE OF THREE DIRECT.

(18) At the rate of  $\pounds 1..1..8$ . for 3 lb. of gum acacia, what must be given for 29 lb. 4 oz.? Ans. 10..11..3.

(19) If 1 English ell, 2 quarters, cost 4s. 7d. what will 39 yards cost at the same rate? Ans. £5..3..54 4.

(20) If 27 yards of Holland cost £5..12..6. how many E. glist ells can I buy for £100.? Ans. 384 ells.

(21) If 7 yards of cloth cost 17s. 8d. what is the value of 5 pieces, each containing  $27\frac{1}{2}$  yards? Ans. 17..7..0 $\frac{1}{4}$ .

(22) A draper bought 420 yards of broadcloth, at the rate of 14s.  $10\frac{3}{4}d$ . per ell English: what was the amount of the purchase money? Ans. £250..5.

(23) A grocer bought 4 hogsheads of sugar, each hogshead weighing neat 6 cwt. 2 qrs. 14 lb. at  $\pounds 2...8..6$ . per cwt. what is the value ? Ans.  $\pounds 64...5..3$ .

(24) A drayer bought 8 packs of cloth, each pack containing 4 parcels, each parcel 10 pieces and each piece 26 yards; at the rate of ±4.10. for 6 yards: what was the purchase money? Ans. £6656.

(25) If 24 *lb*. of raisins cost 6s. 6d. what will 18 frails cost, each frail weighing neat 3 qrs. 18  $lb_{4}$ ? Ans. 224..17..3.

(26) When the price of silver is 5s. per ounce, what is the value of 14 ingots, each ingot weighing 7 lb. 5 oz. 10 dwts.? Ans. £313..5.

(27) What is the value of a pack of wool, weighing 2 cwt. 1 gr. 19 lb. at 17s. per tod of 28 lb.?

Ans. £8..4..61 28.

(28) Bought 171 tons of lead, at £14. per ton; paid carriage and other incidental charges, £4..10. Required the whole cost, and the cost per lb.

Ans. £2398..10. the whole cost, and the cost per lb.  $1\frac{1}{2}d_{-\frac{4}{3}\frac{3}{8}\frac{3}{3}\frac{7}{3}}$ . (29) If a pair of stockings cost 10 groats, how many dozen

pairs can I buy for £43..5.? Ans. 21 doz.  $7\frac{1}{2}$  pairs.

(30) Bought 27 doz. 5 lb. of candles, at the rate of 5s. 9d. a dozen : what did they cost ? Ans. £7..17..73.

(31) A factor bought 86 pieces of stuff, which cost im £517..17..10. at 4s. 10d. per yard. How many yards were there in the whole, and how many English ells in a piece?

Ans. 2143 yards; and 19 ells. 4 qrs. 260 nails, in ~ piece.

(32) A gentleman has an annuity of £896..17. What may he seend daily, that at the year's end he may lay up 200 guinease after giving to the poor quarterly 10 moidores?

Ans. 21..14..8 44.

# RULE OF THREE INVERSE.

52

# THE RULE OF THREE INVERSE

REQUIRES the fourth term to be less than the second, where the third is greater than the first; or the fourth to be greater than the second, when the third is less than the first.

RULE. Multiply the first and second together, and divide their product by the third: the quotient will be the answer, as before.

(1) If 8 men can do a piece of work in 12 days, in how many days can 16 men do the same ?\*

(2) If 54 men can build a house in 90 days, how many men can do the same in 50 days ?

Ans. 971 men. (3) If, when a peck of wheat is sold for 2s. the penny loaf weighs 8 oz.; how much must it weigh when the peck is worth but 1s. 6d.? Ans. 102 oz.

(4) How many sovereigns, of 20s. each, are equivalent to 240 pieces, value 12s. each ? Ans. 144.

(5) How many yards of stuff three quarters wide, are equal in measure to 30 yards of 5 quarters wide? Ans. 50 yds.

(6) If I lend a friend £200. for 12 months, how long ought he to lend me  $\pounds 150.?$ Ans. 16 months.

(7) If for 24s. I have 1200 12. carried 36 miles, what weight can I have carried 24 miles for the same money ?

Ans. 1800 lb.

(8) If I have a right to keep 45 sheep on a common 20 we ks, how long may I keep 50 upon it? Ans. 18 weeks.

(9) A besieged town has a garrison of 1000 soldiers, with provisions for only 3 months. How many must be sent away, that the provisions may last 5 months?

\* Ans. 400. (10) If £20. worth of wine be sufficient to serve an ordinary of 100 men, when the price is £30. per tun ; how many will £20. worth suffice, when the price is only £24. per tun?

Ans. 125 men.

(11) A courier makes a journey in 24 days, by travelling 12 hours a day : how many days will he be in going the same journey, travelling 16 hours a day ? Ans. 18 days.

(12) How much will line a cloak, which is made of 4 yards of plush, 7 quarters wide, the stuff for the lining being but 3 quarters wide? Ans. 91 yards.~

> m. d.m. As 8: 12:: 16:  $\frac{8\times 12}{16} = 6$  days. Ans.

TUTOR'S

DIR pur ( day cas ( requ

ASSI

per at ] coa as wil £1 W

tim yaı £1 wh cw

to

. ju

wi

H.

m

#### DOUBLE RULE OF THREE.

#### ASSISTANT.

ond, wher be greater st.

TUTOR'S

le their pro. ne.

s, in how

low many 7<u>1</u> men. enny loaf e peck is 102 02. ivalent to s. 144. are equal 50 yds. ong ought nonths. at weight

500 *lb*. 1mon 20 weeks. ers, with nt away, . 400. an ordiw many per tun? men. avelling he same days. 4 vards g but 3 ards.~

# DIRECT AND INVERSE PROPORTION PROMISCUOUSLY ARRANGED.

(1) If 14 yards of broadcloth cost £9..12. what is the Ans. £51..8.. $6\frac{3}{4}$   $\frac{6}{14}$ . purchase of 75 yards?

(2) If 14 pioneers make a trench in 18 days, in how many days would 34 men make a similar trench; working, in both cases, 12 hours a day? Ans. 7 days, 4 hours, 563 minutes.

(3) How much must I lend to a friend for 12 months, to requite his kindness in having lent me £64. for 8 months? Ans. £42..13..4.

(4) Bought 59 cwt. 2 grs. 21 lb. of tobacco, at £2..17..4 Ans. £171..2..1. per cut. what does it come to?

(5) A woollen draper purchased 147 yards of broadcloth, at 14s. 6d. per yard. Suppose that he sold it in pieces for coats, each  $1\frac{3}{4}$  yard, how much must he charge for each, so Ans. £1..9..33. as to gain  $\pounds 16..10..9$ . by the whole ?

(6) If £100. gain £4..10. interest in 12 months, what sum Ans. £66..13..4. will gain the same in 18 months?

(7) A draper having sold 147 yards of cloth, at the rate of £1..9..33. for  $1\frac{3}{4}$  yard, found that he had gained £16..10..9. What did the whole cost him, and how much per yard?

Ans. The whole £106..11..6. and 14s. 6d. per yard.

(8) If £100. in 12 months gain £4..10. interest, in what time will £66..13..4 gain the same interest? Ans. 18 months.

(9) If a draper bought 147 yards of cloth, at 14s. 6d. per yard, and sold it in pieces for coats, each 13 yard, for £1..9..3<sup>3</sup>,; how much would be gain per yard, and by the Ans. 2s. 3d. per yard, £16..10..9. by the whole. whole ?

(10) If 1 cwt. cost £12..12..6. what must be given for 14 Ans. £182..0..111 1 18 cwt. 1 gr. 19 lb.?

(11) If £100. gain £4..10. in 12 months, what interest will 2375. gain in the same time?

(12) A regiment of soldiers, consisting of 1000 men, are to have new coats, each to be made of 21 yards of cloth, 5 quarters wide, and to be lined with shalloon of 3 quarters wide. How many yards of shalloon will line them ?

Ans. 4166 yards, 2 grs. 2<sup>2</sup>/<sub>3</sub> nails.

#### THE DOUBLE RULE OF THREE

Has five terms given, three of supposition and two of demand, in find a sixth, in the same proportion with the terms of demand, as that of the terms of supposition. It comprises two operations of the SINGLE RULE.—But it may comprise three four, or more operations of the Single Rule; as there may be seven terms given to find an eighth, or nine to find a tenth, &c. In this respect it is unlimited; and is therefore more properly called COMPOUND PROPORTION.

RULE 1. Put the terms of demand one under another in the third place; the terms of supposition in the same order in the first place; except that which is of the same nature as the required term, which Even in the second place.

Examine the statings separately, using the middle term in each, to know if the proportion is *direct* or *inverse*. When direct, mark the *first* term with an asterisk: when inverse, mark the *third* term.

Find the product of the marked terms for a Divisor, and the product of all the rest for a Dividend: divide, and the quotient will be the answer.\*

RULE 2. (1) Of the conditional terms, put the principal cause of action, gain or loss, &c., in the *first* place. (2) Put that which denotes time or distance, &c., in the *second*, and the other in the *third*. (3) Put the terms of demand under the *like* terms of supposition. (4) If the blank falls in the *third* place, multiply the first and second terms for a divisor, and the other three for a dividend. (5) But if the blank is in the *first* or *second* place, divide the product of the rest by the product of the third and fourth terms, for the answer.

Note. It will save much labour to write the terms of the Dividend over, and those of the Divisor under a linc, like those of a compound fraction, and to cancel them accordingly. See Reduction of Vulgar Fractions, Case 6.

PROOF. By two operations of the Single Rule of Three. (1) If 14 horses eat 56 bushels of oats in 16 days, how many bushels will serve 20 horses 24 days?

* See	also Supplemental Qu	estions, Nos. 6 and 7.	
† By Rule 1	l. 1		``
$As * 14 \\ d. \}$ :	$b_{.}^{b_{.}}$ $(56)$	$\frac{10  12}{\times 20 \times 24}$ $\frac{12}{14 \times 10} = 120 \text{ bus}$	
*16 \$	245	$\frac{14 \times 16}{2} = 120 \text{ bus}$	hels.
By Rule 2.	1	1 I By two single st	atingo
$\begin{array}{c} n \\ 14 : 16 : 56 \\ 20 : 24 : - \end{array}$	$\frac{\$ 10 12}{\$6 \times 20 \times 24} \xrightarrow{b.}{120}$	(1) As $14:56:24$	<i>b.</i> 0:80 <sup>~</sup>
		(2) As $16:80:24$	3. 4:120

ASSI ( mar C will wiÌ wil 150 7 c man p<sup>2</sup>y sun sol day day wh san

ma

ls tra

& c

or ed of t

cer alic

### [TUTOR'S

prise three cre may be tenth, &c. re properly

in the third first place; term, which

in each, to t, mark the tern. the product will be the

al cause of ich denotes third. (3) on. (4) If cond terms f the blank by the pro-

e Dividend compound of Vulgar

f Three. ays, how

shels.

statings h. b. 20:80

d. 8. 24:120

#### ASSISTANT.

(2) If 8 men in 14 days can mow 112 acres of grass, how many men can mow 2000 acres in ten days? Ans. 200 men (3) If  $\pounds 100$ . in 12 months gain  $\pounds 6$ . interest, how much

will £75. gain in 9 months ? Ans. £3..7..6. (4) If £100. in 12 months gain £6. interest, what principal

(4) If  $\pounds 1(0, \ln 12 \text{ months gain } \pounds 0, \text{ interest, what principal will gain } \pounds 3..7..6, in 9 months ? Ans. <math>\pounds 75$ .

(5) If  $\pounds 100$ . gain  $\pounds 6$ . interest in 12 months, in what time will  $\pounds 75$ . gain  $\pounds 3..7..6$ . interest ? Ans. 9 months.

(6) If a carrier charges  $\pounds 2...2$ . for the carriage of 3 cwt. 150 miles, how much ought he to charge for the carriage of 7 cwt. 3 qrs. 14 lb. 50 miles? Ans.  $\pounds 1..16..9$ .

(7) If 40 acres of grass be mown by 8 men in 7 days, how many acres can be mown by 24 men in 28 days? Ans. 480.

(8) If £2. will pay 8 men for 5 days' work, how much will pay 32 men for 24 days' work? Ans. £38..8.

(9) If a regiment of soldiers, consisting of 1360 men, consume 351 quarters of wheat in 108 days, how much will 11232 soldiers consume in 56 days? Ans.  $1503_{35}^{*}$ . grs.

(10) If 939 horses consume 351 quarters of oats in 168 days, how many horses will consume 1404 quarters in 56 days? Ans. 11268.

(11) If I pay  $\pounds 14..10$ . for the carriage of 60 cwt. 20 miles, what weight can I have carried 30 miles for  $\pounds 5..8..9$ . at the same rate? Ans. 15 cwt.

(12) If 144 threepenny loaves serve 18 men for 6 days, how many fourpenny loaves will serve 21 men for 9 days?

Ans. 189.

#### PRACTICE

Is so called from its general use among merchants and tradesmen.

It is a concise method of computing the value of articles, &c., by taking aliquot parts.

. The GENERAL RULE is to suppose the price one pound, one shilling, or one penny each. Then will the given number of articles, considered accordingly as pounds, or shillings, or pence, be the supposed value of the whole; out of which the aliquot part or parts are to be taken for the real price

Notz. An aliquot part of a number is such a part as being taken a certain number of times will produce the number exactly: thus, 4 is an aliquot part of 12; because 3 fours are 12.

PRACTICE.

[TUTOR'S

ASS (4)  $\frac{1}{(5)}$ 

 $\frac{A}{(6)}$ 

(7)

 $\overline{(8)}$ 

(9)

(10

(1

 $\overline{(1)}$ 

(1 (1

(1

(1

(1

ť. 20 W

ALIQ	UОТ	PARTS.
------	-----	--------

Of a pound.         s.         d.         £.           10         0 are $\frac{1}{2}$ 6           6         8 $\frac{1}{3}$ 5         0 $\frac{1}{4}$ 4         0 $\frac{1}{6}$ 2         6 $\frac{1}{6}$ 2         0 $\frac{1}{6}$ 2         0 $\frac{1}{6}$ 1         8 $\frac{1}{12}$ 1         4 $\frac{1}{5}$ 1         3 $\frac{1}{16}$ 1         0 $\frac{1}{2}$ 0         8 $\frac{1}{10}$ 0         8 $\frac{1}{2}$ 0         8 $\frac{1}{3}$	Of a penny.           2 qrs. are $\frac{1}{2}d$ .           1 qr. is $\frac{1}{4}d$ .           Of a ton.           cwt. ton.           10 are $\frac{1}{2}$ 5	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	Of an oz. Troy. The same as the parts of a £. changing the names from shillings to dwts.
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	Of a cwt. ar. lb. cwt	$ \begin{array}{c} 8 & \text{are } \frac{1}{2} \\ 4 & \cdots & \frac{1}{4} \\ 2 & \cdots & \frac{1}{4} \\ 1 & \text{is } \frac{1}{16} \\ \hline Of \ a \ lb. \ Troy. \\ oz. \qquad lb. \\ 6 & \text{are } \frac{1}{4} \\ 4, \&c., \text{as in } \\ the \ parts \ of \\ a \ shilling. \end{array} $	$\begin{array}{cccccccccccccccccccccccccccccccccccc$

RULE 1. When the price is less than a penny, call the given num. ber pence, and take the aliquot parts that are in a penny; then divido by 12 and 20, to reduce the answer to pounds. (1)

$\frac{1}{4} \frac{1}{4} \frac{1}{4} \frac{1}{4} \frac{5704}{1204} \frac{1}{4} \frac{1}{4}$	(2) 7695 at $\frac{1}{2}d$ . Ans. £1607 $\frac{1}{2}$ .	(4) 6547 at $\frac{3}{4}d$ . Ans. £20921.
$\frac{2 0)11 810}{Ans. \pounds 51810}$	(3) 5470 at $\frac{1}{2}d$ . Ans. £11711.	(5) 4573 at $\frac{3}{4}d$ . Ans. £14593.

RULE 2. When the price is less than a shilling, call the given num-ber shillings, take the aliquot part or parts that are in a shilling, add the quotients together, and divide by 20, as in the preceding rule.

\*(1) 7547 at 1d.  $|\dagger(2)|$  3751 at  $1\frac{1}{4}d$ . (3) 54325 at 11d. Ans. £31..8..11. Ans. £19..10..83. Ans. £339..10..71

\* 1d. =  $\frac{1}{12}$  7547s. 20)628..11 Ans. £31..8..11.

 $\dagger 1d. = \frac{1}{12} 3751s.$  $\frac{1}{4} = \frac{1}{4}$  312..7 78..13 20)39 0.82 £19..10..83. Ans [TUTOR'S

ASSISTANT.

oz. Troy. e same as arts of a changing names shillings ts.

a dwt. dwt. re • • • ••• •• •• ••  $\frac{1}{18}$  $\frac{1}{18}$  $\frac{1}{24}$ ••

ven num hen divido

is

at  $\frac{3}{4}d$ . 0..9..21.

at  $\frac{3}{4}d$ . 1..5..93. iven numg, add the

t 11d. .10..71

A715

(4) 6254 at $1\frac{3}{4}d$ .		(32) 9872 at 83d.
Ans. £45120 $\frac{1}{2}$ .	Ans. £59793.	Ans. £359184
(5) 2351 at 2d.	(19) 3120 at $5\frac{1}{2}d$ .	(33) 5272 at 9d.
Ans. £191110.	Ans. £7110.	Ans. £19714
(6) 7210 at $2\frac{1}{4}d$ .	(20) 7521 at $5\frac{5}{4}d$ .	(34) 6325 at 91d.
Ans. £67111012.	Ans. £180393.	Ans. £243156].
$(7)$ 2710 at $2\frac{1}{2}d$ .	(21) 3271 at 6d.	$(35)$ 7924 at $9\frac{1}{2}d$ .
Ans. £2847.	Ans. £81156.	Ans. £313132.
(8) 3250 at $2\frac{3}{4}d$ .	(22) 7914 at $6\frac{1}{4}d$ .	(36) 2150 at $9\frac{3}{4}d$ .
Ans. 2374912.	Ans. $\pm 206110\frac{1}{2}$ .	Ans. £876101
(9) 2715 at 3d.	(23) 3250 at $6\frac{1}{2}d$ .	(37) 6325 at 10d.
Ans. £33189.	Ans. £8805.	Ans. £2631010
(10) 7062 at $3\frac{1}{4}d$ .	(24) 2708 at $6\frac{3}{4}d$ .	(38) 5724 at $10\frac{1}{4}d$ .
Ans. £9512712.	Ans. £7633.	Ans. £24493
(11) 2147 at $3\frac{1}{2}d$ .	(25) 3271 at 7d.	(39) 6327 at $10\frac{1}{4}d$ .
Ans. £3162 $\frac{1}{2}$		Ans. £270433.
(12) 7000 at $3\frac{3}{4}d$ .	(26) 3254 at $7\frac{1}{4}d$ .	(40) 3254 at 101d.
Ans. £10976.	Ans. $\pounds 98511\frac{1}{3}$	Ans. £14273.
(13) 3257 at 4d.	(27) 2701 at $7\frac{1}{2}d$ .	(41) 7291 at $10\frac{3}{4}d$ .
Ans. £5458		
(14) 2056 at $4\frac{1}{4}d$ .	(28) 3714 at $7\frac{3}{4}d$ .	(42) 3256 at 11d.
Ans. £3682	. Ans. £119187 $\frac{1}{2}$	Ans. £14948.
(15) 3752 at $4\frac{1}{2}d$ .	(29) 2710 at 8d.	(43) 7254 at $11\frac{1}{4}d$ .
Ans. £7070		Ans. £340071.
(16) 2107 at $4\frac{3}{4}d$ .	(30) 3514 at $8\frac{1}{4}d$ .	(44) 3754 at $11\frac{1}{2}d$ .
Ans. £411401		Ans. £179177.
(17) 3210 at 5d.	(31) 2759 at $8\frac{1}{2}d$ .	$(45)$ 7972 at $11\frac{3}{4}d$ .
Ans. £66176	Ans. £97143	Ans. £390511.

PRACTICE.

RULE 3. When the price is more than one shilling, and less than two, take the part or parts for the excess above a shilling, add the quotients to the given quantity, and reduce the whole to pounds as before. Or, when convenient, take the aliquot part of a pound.

(1) 2106 at  $12\frac{1}{4}d$ . |(2) 3715 at  $12\frac{1}{2}d$ . |(3) 2712 at  $12\frac{3}{4}d$ . Ans. £144..1..6 Ans. £107..9..101. Ans. £193..9.91.

2106s. of (175..6) $43..10\frac{1}{2}$ 20)214 9..101 Ans. £107..9..1012.

This example is worked by taking  $\frac{1}{12}$ , and then  $\frac{1}{4}$  of that; because a farthing is  $\frac{1}{16}$  of a shilling; which is  $=\frac{1}{12}$  of  $\frac{1}{4}$ , or  $\frac{1}{4}$  of  $\frac{1}{12}$ , because 4 twelves are 48.

C2

# PRACTICE.

[futor's

**AS** (1

Ru qu wi \*( (2 (3

Ī

(4) 2107 at 1s. 1d. $l(19)$ 2750 at 1s. 43 $l(0.1)$ at a
(4) 2107 at 1s. 1d. (19) 2750 at 1s. $4\frac{3}{4}d$ . (34) 7104 at 1s. $8\frac{1}{2}d$ . Ans. £11427. (5) 3215 at 1s. $1\frac{1}{4}d$ . (20) 3725 at 1s. $6\frac{1}{2}$ . Ans. £60616.
(b) 2190 at 1s. $[\pm d](21)$ 7950 at 1, $\pm 11$ (90)
$\begin{array}{c} Ans. \ \pounds 156189.\\ \hline (7) \ 7904 \ at \ 1s \ 13 \ \pounds 521110\frac{1}{2}.\\ \hline (7) \ 7904 \ at \ 1s \ 13 \ \pounds 521 \ 110\frac{1}{2}.\\ \hline Ans. \ \pounds 1842\\ \hline \end{array}$
(1) $7504$ at 1s. $1\frac{3}{4}d$ . (22) 2597 at 1s. $5\frac{1}{4}d$ . (37) 2571 at 1. 013
Ang. (31) 15 (20) 1210 at 18. $5\frac{3}{2}d$ . (38) 2104 at 18. $9\frac{1}{2}d$
Ans $f_{105} = 0.3$ (24) 7524 at 1s. 6d. (39) 7506 at 1s. 93d.
(10) 9254 at 1s $21d$ (25) 7102 rd 1 $310$ Ans. £680.471
$\begin{array}{c} \hline (10) \ 9254 \ \text{at } 1s. \ 2\frac{1}{2} \ d. \\ \hline (25) \ 7103 \ \text{at } 1s. \ 6\frac{1}{4} \ d. \\ \hline (40) \ 1071 \ \text{at } 1s. \ 10d. \\ \hline (11) \ 7250 \ \text{at } 1s. \ 554025\frac{3}{4}. \\ \hline (11) \ 7250 \ \text{at } 1s. \ 9836. \\ \end{array}$
(11) 1400 dt 18, 220 (26) 3954 of 1 - C1 21(11)
Ans. £445115 $\frac{1}{2}$ Ans. £250167. Ans. £4821 8
(12) 7591 at 1s. $3d.(27)$ 7925 at 1s. $631/(40)$ at 1s.
$\frac{Ans. \pounds 47489}{(13) 6325 \text{ at } 1s. 3\frac{1}{2d}} \frac{Ans. \pounds 61929\frac{3}{4}}{(28) 9271 \text{ at } 1s. 3\frac{1}{2d}} \frac{Ans. \pounds 19894\frac{1}{4}}{(28) 9271 \text{ at } 1}$
A 0107 04 100 0211 at 18. (d. (43) 1007 0+1 0 1021
$\frac{Ans. \ \pounds 401180\frac{1}{4}}{(14)\ 5271\ at\ 1s.\ 3\frac{1}{4}} \frac{Ans.\ \pounds 733191}{(20)\ 7210\ ct\ 1} \frac{Ans.\ \pounds 9591\frac{1}{4}}{(14)\ 5271\ at\ 1s.\ 3\frac{1}{4}}$
(14) $5271$ at 1s. $3\frac{1}{2}d$ . (29) 7210 at 1s. $7\frac{1}{2}d$ . (44) 5000 at 1s. 11
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
4
$\frac{Ans. \pm 2131010_{\frac{1}{2}}}{(16) 2915 \text{ at } 1s. 4d} \stackrel{Ans. \pm 187139}{(10) 2504 \text{ at } 1s. 51} \stackrel{Ans. \pm 2031851}{(10) 2504 \text{ at } 1s. 51}$
Ans. £194.6.8 Ang G202 $\frac{13}{4}d$ . (46) 1006 at 1s. 11 $\frac{1}{2}d$
Ans. £1946.8.       Ans. £2061.2.       Ans. £98101         (17) 3270 at 1s. $4\frac{1}{4}d$ .       (32) 7152 at 1s. 8d.       (47) 2705 at 1s. $11\frac{3}{4}d$ Ans. £22181 $\frac{1}{2}$ .       Ans. £596       Ans. £067 10
Ans. $\pounds 22181\frac{1}{2}$ . Ans. $\pounds 596$ Ans. $\pounds 667$ 10
(18) 7059 at 1s, 41d (33) 2005 $\times$ 1 2005 $\times$ 1 207.13.73
RULE 4. When the price is an even number of shillings, the given
quantity may be maltiplied by half that number of shillings, the given figure of the product for shillings, and the rest of the product.
figure of the product for shillings, and the rest of the product will be pounds. Or take the aliquot part of a pound.
(1) $2750$ at 2s (4) 1570
Ans. £275. Ans 6698 16
(2) $3254$ at $4s$ . (5) $2102$ at $10s$ (8) $2102$
Ans. £1051. Ans. £1051. Ans. £9408 8
(3) $2710$ at 6s. (6) $2101$ at $12s$ . (9) $1075$ at $16s$
Ans. 2813. Ans. £ 26012. Ans. £860
· · · · · · · · · · · · · · · · · · ·

# [futor's

at 1s. 81d. £606..16. at 1s. 83d. 286..16..1. at 1s. 9d. £184..2 at 1s. 91d. 7..12..93. at 1s. 91d. 188..9..8. t 1s. 93d. 80..4..71. t 1s. 10d. £98..**3..6**. 1s. 101d. 182..1..8. 1s. 101d 8..9..41 1s. 103d 5..9..11 1s. 11d 79..3..4 ls. 111d ..18..51 . s. 111d 8..10..1 s. 113d .13..73 s. 111d 

ne giver ne units will be

4s. 89.14. 6s. 198.8 3s. £860

#### ASSISTANT.]

#### PRACTICE.

(10) 1621 at 18s. Norr. At 2s. take the *tenth*, and at 10s. take the *half* of so many £.

**RULE.** 5. When the price is an *odd* number of shillings, work by Rule 4th for the *greatest even* number, and add  $\frac{1}{2\sigma}$  of the given quantity for the odd shilling.—Or, take such parts of a pound as will make the given price.

*(1) 3270 at 3s.	(4) $3214$ at $9s$ .	(7) 2150 at 15s
Ans. £49010.	Ans. £14466.	Ans. £161210.
(2) 3271 at 5s.	(5) 2710 at 11s.	(8) 3142 at 17s.
Ans. £81715.	Ans. £149010.	Ans. £267014.
(3) 2715 et 7s.	(6) 3179 at 13s.	(9) 2150 at 19s.
Ans. £9505.	Ans. £20667.	Ans. £204210.

RULE 6. When the price consists of shillings and pence, suppose the given number to be *pounds*, and take such *aliquot part*, or the *sum* of such *aliquot parts*, as will make the given price.—Or, work for the shillings as in the preceding Rules, and take parts for the residue.

t(1) 2710 at 6s. 8d.	‡(7) 2710 at 3s. 2d.	$(13)$ 7152 at 17s. $6\frac{3}{4}d$ .
Ans. £90368.		Ans. £62807.
(2) 3150 at 3s. 4d.	(8) 7514 at 4s. 7d.	(14) 2510 at 14s. 7 <sup>1</sup> / <sub>4</sub> d.
Ans. £525.	Ans. 1721192.	Ans. £1832165 $\frac{1}{2}$ .
(3) 2715 at 2s. 6d.	(9) 2517 at 5s. 3d.	$(15)$ 3715 at 9s. $4\frac{1}{2}d$ .
		Ans. $\pounds 174181\frac{1}{2}$ .
(4) 7150 at 1s. 8d.	(10) 2547 at 7s. $3\frac{1}{2}d$ .	$(16)$ 2572 at 13s. $7\frac{1}{2}d$ .
Ans. £595168.	Ans. £92811. 1012.	Ans. £17523 6.
(5) 3215 at 1s. 4d.	$(11)$ 3271 at 5s. $9\frac{1}{4}d$ .	$(17)7251$ at 14s. $8\frac{1}{4}d$ .
Ans. £21468.	Ans. £9431643.	Ans. $\pounds 5324190\frac{3}{4}$ .
(6) 7211 at 1s. 3d.	$(12)$ 2103 at 15s. $4\frac{1}{2}d$ .	$(18)$ 3210 at 15s. $7\frac{3}{4}d$
Ans. £45013.9.	Ans. £16161371/2.	Ans. £2511314d

RULE 7. When the price consists of pounds, shillings, and pence multiply the given quantity by the *number* of pounds, and take *aliquot parts* for the residue.—Or, work for the shillings as in the preceding **Bules**, &c.—Or, when the given number of articles is  $\tau \tau$  large, work by Compound Multiplication.

s. d. £. s. d. s.  $† 6..8 = \frac{1}{3} 2710$ 1 2..6 = 1 3270 8-24 397 Ans. £903..1 8. 163..10 Ans. £490..10

£.

2710

338. 15

9(

#### PRACTICE.

*(1) 7215 at £74. (7) 2107 at £1 12	
(1) 7215 at $\pounds 74$ . Ans. $\pounds 51049$ (7) 2107 at $\pounds 113$ .	/101
	(13) 3210 at £11863.
(2) 2104 at £5 2 Ans. £347611.	
(4) 2104 at 15.3	Ans. £618957
	14) 0115
	14) 2157 at £2744.
	Ans. £51097104.
	Ans. 50109.7.101
	15) 142 at £11521.
	10) 142 at £1.15.98
[4] 7150	Ans. £250264.
	Ans. 12302.64.
Ama Conceas I I al al LZ. A I	16) 95 at £15147.
	10) 50 41 10.14.71.
(5) 2710 at £2374. (11) 2715 at £1.17 at	Ans. £149474
(11) 2715 et f1 18 of	1100 - 1204.1.44
	17) 37 at £1 10
(6) 3215 at £117. (12) 2157 at £3 15 01	Ans. £7308.
(12) 2157 at £3 15 01 73	
Ans. £594715. (12) 2157 at £31524.	8) 2175 at £9 15 41
(6) 3215 at £117. Ans. £594715. (12) 2157 at £31524. (1 Ans. £81081954.	4. 00000.10
Para o ma	Ans. £6022074

RULE 8. When the given quantity consists of several denominations, multiply the price by the number of the highest, and take aliquot parts for the inferior denominations.

(1) At £3..17..6. per cwt. what is the value of 25 cw. 2 grs. 14 lb. of soap?

(2) At £1..4..9. per cwt. what is the value of 17 cwt. 1 gr.

(3) Sold 85 cwt. 1 qr. 10 lb. of iron, at  $\pounds 1...7..8$ . per cwt. what is the value of the whole?

(4) If hops are sold at  $\pounds 4..5..8$ . per cwt. what must be given for 72 cwt. 1 gr. 18 lb.? Ans.  $\pounds 118..1..01$ .

(5) What is the value of 27 cwt. 2 qrs. 15 lb. of logwood at  $\pounds 1..1..4$ . per cwt.? (6) Rought 78 cwt. 2 cwt. 10 lb.  $\pounds 10...3..2$ . Ans.  $\pounds 29...9..61$ .

(6) Bought 78 cwt. 3 qrs. 12 lb. of molasses, at  $\pounds 23..3..01$ . per cwt. what must I give for the whole ? Ans.  $\pounds 227..14$ . (7) Sold 56 cmt 1 cm 17 lb - 5

(7) Sold 56 cwt. 1 qr. 17 lb. of sugar, at £2..15..9. per cwt how much is the whole charge? Ans. £157..4..41. (8) What is the value of  $0^{-7}$ 

(8) What is the value of 97 cwt. 15 lb. of currants, a  $\pm 3..17..10$ . per cwt.? (9) At 54 14 5 the currants  $\pm 378..0..3$ 

(9) At £4..14..6. the cwt. what is the value of 37 cwt. 2 are 13 lb. of raw sugar? Ans. £177..14..81

Ш.

14=1

12 grs.=1 £3..17..6

19.. 7..6

96..17..6

1..18..9 9..8<del>1</del> £99..5..111

5×5=25

\* 4= 1 7215 7 50505 1443 £51948 Ans [TUTOR'S

48

fo

at

lb.

W

14

pu

th

hi

620

qu 33

### [TUTOR'S

at  $\pounds$ 1.18.61.  $\pounds$ 6189.5.71 at  $\pounds$ 2.7.44. 5109.7.104.  $\pounds$ 1.15.21.  $\pounds$ 250.2.64.  $\pounds$ 250.2.64.  $\pounds$ 15.14.71.  $\pounds$ 1494.7.44  $\pounds$ 1.19.55.  $\pounds$ 73.0.88.  $\pounds$ 2.15.44.  $\pounds$ 22.0.74

ominations. liquot parts

25 cw.

cwt. 1 gr. .10..8. por cwt. 3..1..04. must be ..3..2. logwood 9..64. 2..17..9 7..14. per cwt 4..44. ants, a .0..3 t. 2 gr.

...81

ASSISTANT.]

(10) Bought sugar at £3..14..6. the cwt. what did I give for 15 cwt. 1 gr. 10 lb.? Ans. £57..2..9.

(11) Required the value of 17 oz. 8 dwts. 18 grs. of gold, at £3..17..101. per ounce. Ans. £67..17..11.

(12) At £37..6.8. per *cwt*. the value of 1 *cwt*. 2 *qrs*. 10<del>1</del> *lb*. of cochineal is required. Ans. £59..10.

(13) Required the value of 13 hhds. 42 gals. of Champagne wine, at £25..13..6. per hhd. Ans. £350..17..10.

(14) A gentleman purchased at an auction an estate of 149 a. 3 r. 20 p. at  $\pounds 54..10$ . per acre. What was the whole purchase money, including the auction duty of 7d. in the  $\pounds$ . the attorney's bill for the deeds of conveyance,  $\pounds 33..6..8$ . and his surveyor's charge for measuring it, at 1s. per acre? Ans.  $\pounds 8447..5..04$ .

RULE 9. To find the price of 1 lb. at a given number of shillings per ewt.

Multiply the shillings by 3 and divide the product by 7; the quotient will be the price of 1 *lb*. in farthings.\*

(1) What is the price of 1 lb. at 44s. 4d. per cwt. ?†

(2) What are the respective prices per lb. at 86s. 4d.; 91s.; ana 116s. 8d. per cwt.? Ans.  $9\frac{1}{4}d.$ ,  $9\frac{3}{4}d.$ , and 1s.  $0\frac{1}{4}d.$ 

RULE 10 It is sometimes expedient to change the price and the quantity for each other. Thus 48 yards at 2s. 9d. will be equivalent to 33 yards at 4s.; because 2s. 9d. = 33d. and 4s. = 48d.

(1) What is the value of 72 yds. at 3s. 5d. and at 14s. 7d. (her yard? Ans.  $\pounds 12..6.$ , and  $\pounds 52..10$ .

(2) 80 yds. at 15s. 3d. and at 16s. 8d. per yard?

Ans. £61., and £66..13..4.

(3) 42 lbs. at  $11\frac{1}{4}d$ . and at 1s.  $3\frac{1}{4}d$ . per lb. ? Ans. £2..0..3., and £2..13..4 $\frac{1}{4}$ .

#### TARE AND TRET.

Gross weight is the weight of any goods, together with that of the package which contains them.

Multiplying by 3 reduces the shillings to fourpences, and 7 fourpraces (or 2s. 1d.) are the value of 1 cwt. at 1 farthing per U.

 $\begin{array}{c} + 44s. 4d. \\ 3 \\ 7 \\ \hline 133 \\ \hline 19 \text{ farthings} = 4 \frac{3}{4} d. \text{ per } Jb. Ans. \end{array}$ 

#### TARE AND TRET.

[ **TUTOR'S** 

CID

We

gro

we

to

88

we

and

2 9

mu

15

 $\mathbf{2}$ 

17

Neat weight is that of the articles alone, or what remains after the deduction of all allowances.

Tare is an allowance for the weight of the package. It is either so much in the whole, or at so much per bag, box, barrel, &c., or at so much in the cwt.

Tret is an allowance of 4 lb. in 104 lb. (or  $\frac{1}{26}$  part) for waste.

Cloff is an allowance of 2 lb. in 3 cwt. on some goods : but both these are nearly obsolete.

Suttle is the remainder when any particular allowance has been deducted.

RULE. When the Tare is at so much for each bag, &c., the whole Tare may be found by multiplying by the number of them. When it is at so much per cut. take the aliquot parts of the Gross for the Tare. Subtract the Tare from the Gross; the remainder is the Neat; unless

If Tret is allowed, it is  $\frac{1}{20}$  of the Tare sutlle, which being subtracted from it, the remainder is the Neat. But if Cloff also is to be allowed, the cwts. Tret suttle, multiplied by 2, and divided by 3, will be the lbs. Cloff, which subtract to find the Neat.

(1) In 7 frails of raisins, each weighing 5 cut. 2 grs. 5 lb. gross, tare at 23 16. per frail, how much neat weight ?\*

(2) What is the neat weight of 25 hogsheads of tobacco, weighing gross 163 cut. 2 qrs. 15 lb. tare 100 lb. per hogs-Ans. 141 cwt. 1 gr. 7 lb.

(3) In 16 bags of pepper, each weighing 85 lb. 4 oz. gross. tare per bag, 3 lb. 5 oz. how many pounds neat? Ans. 1311 lb

(4) What is the neat weight of 5 hogsheads of tobacco, weighing gross 75 cut. 1 gr. 14 lb. tare in the whole 752 lb.?

Ans. 68 cut. 2 grs. 18 lb. (5) In 75 barrels of figs, each 2 qrs. 27 lb. gross, tare in the whole 597 lb. how much neat weight? Ans. 50 cwt. 1 qr.

(6) What is the neat weight of 18 butts of currants, each 8 cwi. 2 qrs. 5 lb. gross, tare at 14 lb. per cwt. ?†

	cwt. ar. Th
	cwt.qr. lb. * 52 5 gross.
	23 tare.
	5110 neat of 1 frail.
1.5	
28.	37.1.14 neat of the whole.
	>

	cwt. qr. lb.	
	t 82 5 9×2=10	
	76317	
i=1	2 1533 6 wholegr	-
• "	190251 tare.	U

Ans. 134..2., 8

# [rutor's

# at remains

age. It is , g, box, bar-

r waste. s: but both

e has been

, the whole When it the Tare. at; unless

also is to livided by

qrs. 5 lb.

tobacco, er hogs-. 7 lb. z. gross. 1311 lb tobacco, 752 lb.? 18 lb. tare in wt. 1 qr. ts, each

10

legross

#### INVOICES.

(7) In 25 barrels of figs, each 2 cwt. 1 qr gross, tare per cwt. 16 lb. how much neat weight? Ans. 48 cwt. 0 qr. 24 lb.

(8) What is the neat weight of 9 hogsheads of sugar, each weighing gross 8 cut. 3 qrs. 14 lb. tare 16 lb per cut.?

Ans. 68 civt. 1 qr. 24 lb.

(9) In 1 butt of currents, weighing 12 cut. 2 qrs. 24 lb. gross, tare 14 lb. per cut. tret 4 lb. per 104 lb. what is the neat weight !\*

(10) In 7 cwt. 3 qrs. 27 lb. gross, tare 36 lb. tret according to custom, how many pounds neat? Ans. 826 lb.

(11) In 152 cwt. 1 qr. 3 lb. gross, tare 10 lb. per cwt. tret as usual, how much neat weight? Ans. 133 cwt. 1 qr. 12 lb.

(12) What is the neat weight of 3 hogsheads of tobacco, weighing 15 cwt. 3 qrs. 20 lb. gross, tare 7 lb. per. cwt. tret and cloff as usual ?†

(13) In 7 hogsheads of tobacco, each weighing gross 5 cwt. 2 qrs. 7 lb.; tare 8 lb. per cwt. tret and cloff as usual, how much neat weight? Ans. 34 cwt. 2 qrs. 8 lb.

# INVOICES, OR BILLS OF PARCELS.

(1) Mrs. Bland,

ASSISTANT.]

# . London, Sept. 1, 1830. Bought of Jane Harris.

			<i>s</i> .	d. £. s. d.	
*	15	pairs worsted stockings at	4	6 per pr 3. 7. 6	
	1	doz. thread ditto at	3	2	
	ł	doz. black silk ditto . at	8	3 4 1:56	
	11	doz. milled hose at	4	2	
	$\tilde{2}$	doz. cotton ditto at	7	6	
	17	pairs kid gloves at	1	8 1.7.4	
				F91 18 A /	1

 $\begin{array}{c} lb. & cwt. qrs. lb.\\ \bullet 14 = \frac{1}{8} & 12.. 2.. 24 \text{ gross}\\ lb. & 1.. 2.. 10 \text{ tare.}\\ 4 = \frac{1}{26} & 11.. 0.. 14 \text{ suttle.}\\ & 1.. 19 \text{ tret.}\\ \hline Ans. & 10.. 2.. 23 \text{ neat.} \end{array}$ 

### INVOICES.

TUTOR'S (2) Mr. Isaac Pearson, Derby, June 3, 1630 Bought of John Sims and Son S. d. yds. satin . £. s. d. 15 at 9 6 per yard 181 yds. flowered silk . 1. 2. 6 at 17 12 yds. rich brocade . 4 ..... at 19 8 ..... 161 yds. sarcenet . . .15.16.4 at 3 2 ..... 131 yds. Genoz velvet. at 27 6 ..... .11. 16. 1 23 yds. lustring . 2. 12 at 6 3 ..... (3) Miss Enfield, Nottingham, June 4, 1830. Bought of Joseph Thompsor. d. S. 41 yds. cambric £. s. d. at 12 6 per yard . 2. 16., 3 121 yds. muslin'. . . at 8 3 ..... yds. printed calico. at 5 4 · K. J. 1 ..... doz. napkins 2 . 4.0.0 . . at 2 3 each .. 14 ells diaper. . . 2, 141. . . at 1 7 per ell 35 ells dowlas, . .1. 2. 2 . at 1 11 ..... . / 19.42 £17..14..11 Received the above,

Joseph Thompson.

15.

and

Re

pe

Ēε

łb

20

18

A

M

Ju

S

4)

F

(4) Mrs. Mary Bright sold to the Right Honourable Lady Anna Maria Lamb 18 yards of French lace at 12s. 3d. per yd 5 pairs of fine kid gloves at 2s. 2d. per pair, 1 dozen French fans at 3s. 6d. each, two superb silk shawls at three guineas each, 4 dozen Irish lamb at 1s. 3d. per pair, and 6 sets of knots at 2s. 6d. per set .- Please to make the Invoice for her.

Total amount £23..14..4. (5) Mr. Thomas Ward sold to James Russell Vernon, Eso, 17] yards of fine serge at 3s. 9d. per yd. 18 yds. of drugget at 9s. per yd. 151 yds. of superfine scarlet at 22s. per yd. 163 yds. of Yorkshire black at 18s. per yd. 25 yds. of shalloon at 1s. 9d. per yd. and 17 yds. of drab at 17s. 6d. per yd .- Maro an Invoice of these articles. Total amount £60..10..54. (6) Mr. Samuel Green, of Wolverhampton, sent to Messys. Wright and Johnson, agreeably to order, 27 calf skins at 3s. 6d. each, 75 sheep skins at 1s. 7d. 39 coloured ditto at

G-\*

#### INVOICES.

1s. 8d. 15 buck skins at 11s.6d. 17 Russia hides at 10s.7d. and 125 lamb skins at  $1s.2\frac{1}{2}d$ .—Draw up the Invoice. Total amount £39..1..8 $\frac{1}{2}$ .

(7) Mr. Richard Groves sent the following articles to the Rev. Samuel Walsingham: viz. 2 stones of raw sugar at  $6\frac{1}{2}d$ . per lb. 2 loaves of sugar,  $15\frac{1}{2}$  lb. at  $11\frac{1}{2}d$ . per lb. a stone of East India rice at  $3\frac{1}{2}d$ . per lb. 2 stones Carolina rice at 5d. per lb. 15 oz. nutmegs at  $5\frac{1}{2}d$ . per oz. and half a stone of Dutch coffee at 1s 10d. per lb.—Make a copy of the Invoice. Total amount £3..5.5 $\frac{3}{4}$ .

#### BILLS OF BOOK-DEBTS.

Chester. (8) Mr Charles Cross, To Samuel Grant and Co., Dr d. £. s. d. S. 1830. April 14. Belfast butter, 1 cwt. at 0 61 per B. . 3.0., Cheese, 7 cwt. 3 qrs. 12 lb. at 56 0 long cwt 22. 0, 0 May 8. Butter, 1 firkin, 28 lb. at 0 51 per 1. 0,12.10 3.0. July 17. 5 Chesh. cheeses, 127 lb. at 0 66 61 Sept. 4. 2 Stilton ditto, 15 lb. at 0 101 Cream cheese, 13 lb. at 0 81 1012. 66 66 1 6/11. £30..1.. Dec. 28. Received the contents, Samuel Grant. Newark. (9) Mr. Charles Septimus Twigg, To Isaac Jones, Dr. S. s. d s. d. . 829. Dct. 22. Tares, 39 bushels at 1 10 per bush 3, 11, C Pease, 18 bushels at 30 4 per qr. 3 8 3 .830. Malt, 7 qrs. . at 63 6 per qr. 22 4 c Hops, 2 cwt. 1 qr at 1 5 per B. 17, 13 0 Feb. 18. Malt, 41 per bush. 5, 12mg Feb. 20. Oats, 6 qrs. . at 2 Beans, 17 qrs. . at 37 4 per qr. 01.14. 8 £84..9..11

1830. July 1. Received the above for Isaac Jones Thomas West.

TUTOR'S

ASSISTANT.]

June 3, 1830

£. s. d. 1. 2. 6 15. 16. 4 11. 16. 0 15. 16. 4 11. 16. 0 15. 16. 4 11. 16. 0 15. 16. 4 11. 16. 0 15. 16. 4 16. 4 16

une 4, 1830.

npson.

able Lady 3d. per yd en French e guineas 6 sets of ce for her. 3..14..4. non, Esa. drugget at r yd. 164 alloon at -Maro 10..51. Messes. skins u ditto 1

. 22."

# SIMPLE INTEREST.

# SIMPLE INTEREST

Is the premium allowed for the loan of any sum of money during a given space of time.

The Prin\_ipal is the money lent, for which Interest is to be received.

The Rate per cent. per annum is the quantity of Interes, (agreed on between the Borrower and the Lender) to be paid for the use of every £100. of the Principal, for one year.

The Amount is the Principal and Interest added together.

1. To find the Interest of any Sum of Money for a Year.

RULE. Multiply the Principal by the Rate per cent. and that Product divided by 100 will give the Interest required.

Note. When the Rate is an aliquot part of 100, the Interest may be calculated more expeditiously by taking such part of the *Principal.* Thus, for 5 per cent. take  $\frac{1}{2\sigma}$ ; for 4 per cent.  $\frac{1}{25}$ , or  $\frac{1}{5}$ of  $\frac{1}{5}$ ; for 2 per cent.  $\frac{1}{30}$ ; for  $2\frac{1}{2}$  per cent.  $\frac{1}{40}$ ; for 3 per cent.  $\frac{1}{30}$ ; plus ; of that ; & c.

This Rule is applied to the calculation of Commission. Brokeraga, Purchasing Stocks, Insurance, Discounting of Bills,

II. For several Years. Multiply the Interest of one year by the number of years, and the product will be the answer.

For parts of a year, as months and days, &c., the Interest may be found by taking the aliquot parts of a year; or by the Rule of Three: and it is customary to allow 12 months to the year, and 30 days to a 'nonth.

\* To discount a Bill of Exchange is to advance the cash for it before it becomes due; deducting the Interest for the time it has to run. Bank-

ers always charge Discount as the Interest of the sum. † At the rate of 5 per cent the interest of £1. for a year is 1s., or

one penny for a month. Therefore, the principal X the number of months, gives the interest in pence. Or. take the parts of a year for the months, out of as many shillings

as there are pounds in the principal.

Thus, to find the interest of £40..10. for 2 months, say  $40\frac{1}{2}d. \times 2 =$ **81**d. = 6s. 9d.; or, 2 months being  $\frac{1}{6}$  of a year, 40s.  $6d. \div 6 = 6s. 5d$ .

For days, take the aliquot parts of a month. The interest for days at 5 per cent. may also be found by multiplying the principal by the number of days; and the product divided by 365 will give the answer in shillings; or divided by 7300 ( $-365 \times 20$ ) will give the answer in

66

IUTOK S

16

ce

ce

ar

pe

p

al 86

tc

n

N

ir n ľ

r

2

p

I

ITTOK .

of money

est is to be

of Interes, to be paid to year. together.

a Year. Id that Pro-

the Interest part of the nt.  $\frac{1}{25}$ , or  $\frac{1}{5}$ r cent.  $\frac{1}{50}$ ,

sion. Broof Bills.

one year answer. Interest or by the conths to

it before n. Bank-

is 1s., or umber of

shillings

1. × 2= = 6s. 5a.

for days by the answer swer in ASSISTANT.]

#### SIMPLE INTEREST.

(1) What is the interest of £375. for a year, at £5. per cent. per annum?\*

(2) What is the interest of £945..10. for a year, at £4. per cent. per annum? Ans. £37..16.. $4\frac{3}{4}$ .

(3) What is the interest of £547..15. at £5. per cent. per annum, for 3 years? Ans. £82..3..3.

(4) What is the interest of £254..17..6. for 5 years, at £4. per cent. per annum? Ans. £50..19..6.

(5) What is the amount of  $\pounds 556..13..4$ . at  $\pounds 5$ . per cent. per annum, in 5 years? Ans.  $\pounds 695..16..8$ .

Nore. Commission and Brokerage (commonly called Brokage) are allowances of so much per cent. to an agent or broker, for buying or selling goods, or transacting business for another.

(6) My correspondent informs me that he has bought goods to the amount of  $\pounds 754..16$ . on my account, what is his commission at  $\pounds 2\frac{1}{2}$ . per cent.? Ans.  $\pounds 18..17..4\frac{3}{4}$ .

(7) If I allow my factor  $\pounds 3\frac{3}{4}$ . per cent. for commission, what will he require on  $\pounds 876..5..10$ ? Ans.  $\pounds 32..17..2\frac{1}{2}$ .

NOTE. Stock is a general term to designate the Capitals of our Trading Companies; or to denote *Property* in the *Public Funds*; which means the Money paid by Government for the interest of the *National*. *Debt.* The quantity of Stock is a *nominal* sum, for which the owner receives a certain rate of interest while he holds the same.

(8) At  $\pounds 110\frac{1}{4}$ . per cent. what is the purchase of  $\pounds 2054..16$ . South Sea stock? Ans.  $\pounds 2265..8..4$ .

(9) At  $\pounds 104\frac{3}{8}$ . per cent. South Sea annuities, what is the purchase of  $\pounds 1797..14$ ? Ans.  $\pounds 1376..6..11\frac{3}{4}$ .

(10) At  $\pounds 96\frac{3}{4}$ . per cent. what is the purchase of  $\pounds 577..19$ . Bank annuities? Ans.  $\pounds 559..3..3\frac{3}{4}$ .

(11) At  $\pounds 124\frac{5}{8}$ . per cent. what is the purchase of  $\pounds 758..$ 17..10. India stock? Ans.  $\pounds 945..15..4\frac{1}{4}$ .

(12) What sum will purchase £1284. of the 3 per cent. Consols, at  $\pounds 59\frac{7}{8}$ . per cent.; including the broker's charge of 1, or 2s. 6d. per cent. on the amount of stock?

Ans. £770..7..113.

* £. 375	Better thus :
0 10125	$\pounds$ . $\pounds$ .
£. 18 75 20	$5=\frac{1}{20}375$
s. 15 00	Ans.£1815.

#### Ans. £18..15.

<sup>2</sup> Cutting the two figures in the above divides the number by 100: see Division, p. 21

## SIMPLE INTEREST.

(13) If I employ a broker to buy goods for me, to the amount of £2575.17..6. what is the brokerage at 4s. per

(14) What is the broker's charge on a sale amounting to £7105..5..10. at 5s. 6d. per cent.? Ans. £19..10..91.

(15) What is the brokage on goods sold for  $\pounds 975..6.4$ . at 6s. 6d. per cent.? Ans. £3..3..41.

(16) What is the interest of £257..5..1. at £4. per cent. per annum, for a year and three quarters ? Ans. £18..0..11.

(17) What is the interest of £479..5. for  $5\frac{1}{4}$  years, at £5. per cent. per annum ? Ans. £125..16..03.

(18) What is the amount of £576..2..7. in  $7\frac{1}{4}$  years, at £4 $\frac{1}{2}$ . per cent. per annum? Ans. £764..1..81.

(19) What is the interest of £259..13..5. for 20 weeks, at £5. per cent. per annum?

Ans. £4..19..101. (20) What is the interest of £2726.1.4. at £41/2. per cen. per annum, for 3 years, 154 days ?

Ans. £419..15..61. (21) Compute the interest of £155. for 49 days, and for 146 days, at £5. per cent. per annum.

Ans.  $\pounds 1..0..9\frac{1}{2}$  and  $\pounds 3..2..0$ . (22) What will a banker charge for the discount of a bill of £76..10. and another of £54. negotiated on the 18th of May; the former becoming due June 30, and the latter July 13; discounting at £5. per cent.? Ans. 8s. 11d. and 8s. 3d.

When the Amount, Time, and Rate per cent. are given, to find the Principal.

RULE. As the amount of 2. .00. at the rate and for the time given is to £109., so is the amount given to the principal required.

(23) What principal being put to interest will amount to £402..10. in 5 years, at  $\mathcal{L}3$ . per cent. per annum ?†

(24) What principal being put to interest for 9 years will amount to £734..8. at £4. per cent. per annum?

Ans.	£340

and the second	The standards of the standard state of the s
s. £. s. d.	and a second
* $4 = \frac{1}{5} \frac{\pounds}{2575176}$	03
£. 5 15 3 6	12
20	42
s. 3 03 Ans. £5304.	4
2108. 20304.	1 68
hit.	£. f a f

+£3×5+100=£115. As 115 : 100 : : 402..10 : 350 Ans

68

ASS

TUTOR'S

 $\pounds 5$ 

W

ł ter

pe: pe

pe

W

int and

in

in in

> Is foi ga m he

me, to the at 4s. per

tounting to  $0..10..9\frac{1}{4}$ . 75..6..4. at  $3..3..4\frac{1}{2}$ . er cent. per  $8..0..1\frac{1}{2}$ . rs, at £5.  $..16..0\frac{3}{4}$ . rs, at £4 $\frac{1}{2}$ . weeks, at  $9..10\frac{1}{4}$ . per cent.  $15..6\frac{1}{4}$ .

, and for

3.2.0. of a bill 18th of utter July d 8s. 3d.

n, to find

e given is

nount to

ars will

E340.

#### ASSISTANT.]

#### DISCOUNT.

(25) What principal, being put to interest for 7 years at  $\pounds$ 5. per cent. per annum, will amount to  $\pounds$ 334.16.?

Ans. £248.

## When the Principal, Rate per cent. and Amount are given, to find the Time.

RULE. As the interest for 1 year is to 1 year, so is the whole interest to the number of years.

(26) In what time will £350. amount to £402..10. at £3. per cent. per annum ?\*

(27) In what time will  $\pounds 540$ . amount to  $\pounds 734...8$ . at  $\pounds 4$ . per cent. per annum? Ans. 9 years.

(28) In what time will  $\pounds 248$ . amount to  $\pounds 334..16$ . at  $\pounds 5$ . per cent. per annum? Ans. 7 years.

## When the Principal, Amount, and Time are given, to find the Rate per cent.

**RULE.** As the principal is to the whole interest, so is  $\pounds 100$ . to its interest for the given time. Divide that interest by the number of years, and the quotient will be the rate per cent.

(29) At what rate per cent. will  $\pounds$ 350. amount to  $\pounds$ 402..10. in 5 years ?†

(30) At what rate per cent. will £248. amount to £334..16. in 7 years? Ans. £5. per cent.

(31) At what rate per cent. will £540. amount to £734..8. in 9 years? Ans. £4. per cent.

#### DISCOUNT

Is the abatement of so much money, on any sum received before it is due, as the money received, if put to interest, would gain at the rate, and in the time given. Thus  $\pounds 100$ . promit money would discharge a debt of  $\pounds 105$ . to be paid a year hence, Discount being made at  $\pounds 5$ . per cent.

 $\frac{350\times3}{100} = \pounds 10..10$ . the interest for 1 year.

£.

£402..10. - £350. = £52..10. the whole interest.

- As £10..10 : 1 year :: £52..10 : 5 years. Ans.
- t As £350 : £52.10 :: £100 : £15 == the interest of £100. for 5 years. Then  $15 \div 5 = \pounds 3$  the rate per cent.

RULE. As £100. with its interest for the time given is to that interest, so is the sum given to the Discount required.

... Also, As that Amount of £100. is to £100., so is the given sum to the

But if either the Discount or the Present worth be found by the proportion the other may be found by subtracting that from the given.

(1) What are the discount and present worth of £386..5. for 6 months, at £6. per cent. per annum ?\*

(2) How much shall I receive in present payment for a debt of £357..10. due 9 months hence, allowing discount at £5. per cent. per annum?

Ans. £344..11..63 15. (3) What is the discount of £275..10. for 7 months, at £5. per cent. per annum ?

Ans. £7..16..13 95 (4) What is the present worth of £527 .9..1. payable in 7 months, at  $\pounds 4\frac{1}{4}$ . per cent. per annum ?

Ans. £514..13..101 6930. (5) Required the present worth of £875..5..6. due in 5 1 ionths, at  $\pounds 4\frac{1}{2}$  per cent. per annum. Ans.  $\pounds 859..3..3\frac{3}{4}$   $\frac{7}{4075}$ .

(6) What is the present worth of £500. payable in 10 months, at  $\pounds 5$ . per cent. per annum?

(7) How much ready money ought I to receive for a note Ans. £480. of £75. due in 15 months, at £5. per cent. per annum?

Ans. £70..11..93.

[TUTOR'S

pe

6

cre

m

1

pre An

See

Is.

tha

no

In

the

for anc

ye

cei

per

per

and

1

(8) What will be the present worth of £150. payable at 3instalments of four months; i. e. one-third at 4 months, onethird at 8 months, and one-third at 12 months, discounting at £5. per cent. per annum? Ans. £145..3..81.

(9) Of a debt of £575..10. one moiety is to be paid in 3 months, and the other in 6 months. What discount must be allowed for present payment, at £5. per cent. per annum?

Ans. £10..11..43.

6 m. =  $\frac{1}{2}$  £6 £. 100 + 3 = 103 =amount of £100. in 6 months £. £. £. As 103 : 3 : : 386.. 5 £. s. 3 386..5 103)1158..15( 11..5 discount. 1133375..0 present worth. 25 20 103)515 = 5s.

is to that in-

ven sum to the

nd by the pro-

of £386..5.

yment for **a** discount at  $11..6\frac{3}{4}$   $\frac{15}{83}$ . onths, at **£5**.  $5..1\frac{3}{4}$   $\frac{95}{247}$ . payable in **7** 

 $\frac{1}{2}$   $\frac{6930}{24595}$ 3. due in 5 .3..34 4075. able in 10 s. £480. e tor a note num? .11..9-17. ayable at 3 onths, onecounting at 5..3..81 e paid in 3 nt must be nnum? ..11..43.

ASSISTANT.]

(10) What is the present worth of  $\pounds 500$ . at  $\pounds 4.4$  per cent. per annum,  $\pounds 100$ . being to be paid down, and the rest it two 6 months? Ans.  $\pounds 488..7..8\frac{1}{2}$ .

(11) Bought goods amounting to £109.16. at 6 months' credit, or  $\pounds 3\frac{1}{2}$ , per cent. discount for prompt payment. How, much ready money will discharge the account?\*

Ans. £105..13..41.

Note. The Rule to find the present worth of any sum of money is precisely identical with that case in Simple Interest in which the Amount, Time, and Rate per cent. are given to find the Principal. See page 68.

#### COMPOUND INTEREST

Is that which arises from both the Principal and Interest: that is, when the interest of money, having become due, and not being paid, is added to the Principal, and the subsequent Interest is computed on the *Amount*.

RULE. Compute the first year's interest, which add to the principal: then find the interest of that amount, which add as before, and so on for the number of years. Subtract the given sum from the *last Amount*, and the remainder will be the *Compound Interest*.

(1) What is the compound interest of  $\pounds 500$ . forborne 3 years, at  $\pounds 5$ . per cent. per annum ?†

(2) What is the amount of £400. in  $3\frac{1}{2}$  years, at £5. per cent. per annum, compound interest? Ans. £474..12..6<sup>1</sup>/<sub>4</sub>.

(3) What will £650. amount to in 5 years, at £5. per cent. per annum, compound interest? Ans. £829..11..7 $\frac{1}{2}$ .

(4) What is the amount of £550..10. for  $3\frac{1}{2}$  years, at £6 per cent. per annum, compound interest? Ans. £675..6..5.

(5) What is the compound interest of  $\pounds$ 764. for 4 years and 9 months, at  $\pounds$ 6. per cent. per annum?

Ans. £243..18..8.

• The discount in cases of this sort is so much per cent. on the sum, without regard to time. It is, therefore, computed as a year's interest.

 $1_{10}$  25 27.11..3 

  $1_{10}$  525 amount in 1 yr.
 578..16..3 amount in 3 years.

 26..5 500..0..0 principal subtract.

 551..5 do. in 2 yrs.
 278..16..3 Ans.

## EQUATION OF PAYMENTS.

(6) What is the compound interest of  $\pounds 57..10..6.$  for 5 years, 7 months, and 15 days, at  $\pounds 5.$  per cent. per annum? Ans.  $\pounds 18..3..81.$ 

(7) What is the compound interest of  $\pounds 259.10$ . for **3** years, 9 months, and 10 days, at  $\pounds 4\frac{1}{2}$ . per cent. per annum? Ans.  $\pounds 46..19..10\frac{1}{2}$ .

# EQUATION OF PAYMENTS

Is when several sums are due at different times, to find a mean time for paying the whole debt; to do which, this is the common

RULE. Multiply each term by its time, and divide the sum of the products by the whole debt, the quotient is accounted the mean time

(1) A owes B  $\pounds 200$ . whereof  $\pounds 40$ . is to be paid at 3 months,  $\pounds 60$ . at 5 months, and  $\pounds 100$ . at 10 months: at what time may the whole debt be paid together without prejudice to either?

L.			
$40 \times$			
$60 \times$			
$100 \times 100 \times 100$	10 = 1	L00 <b>0</b>	
2	00)ī	4 20	
1	4 <i>ns</i> .	7 1 month	s

[TUTOR'S

Is

arti at t

n abo

por

Rul

cha

16.

has

to

20

4 :

per

per

the

for

mu

per

for

(

(

(

(2) B owes C £800. whereof £200. is to be paid at 3 months, £100. at 4 months, £300. at 5 months, and £200. at 6 months; but they agree that the whole shall be paid at once; what is the equated time? Ans. 4 months,  $18\frac{6}{2}$  days.

(3) A debt of £360. was to have been paid as follows: viz.: £120. at 2 months, £200. at 4 months, and the rest at 5 months; but the parties have agreed to have it paid at one mean time: what is that time? Ans. 3 months,  $13\frac{1}{3}$  days.

(4) A merchant bought goods to the value of £500. to pay £100. at the end of 3 months, £150. at the end of 6 months, and £250. at the end of 12 months; but it was afterwards agreed to discharge the debt at one payment: required the time. Ans. 8 months, 12 days.

(5) H is indebted to L a certain sun, which is to be paid at 6 different payments, that is  $\frac{1}{4}$  at 2 months,  $\frac{1}{8}$  at 3 months,  $\frac{1}{4}$  at 4 months.  $\frac{1}{4}$  at 5 months,  $\frac{1}{8}$  at 6 months, and the rest at 7 months; but they mutually agree that the whole shall be paid at one equated time: what is that time? Ans.  $4\frac{1}{4}$  months. (6) A is indebted to B of 120 where of the interval

(6) A is indebted to B  $\pounds 120$ . whereof  $\frac{1}{4}$  is to be paid at 3 months,  $\frac{1}{4}$  at 6 months, and the rest at 9 months: what is the equated time of the whole payment? Ans.  $5\frac{1}{4}$  months.

.10..6. for 5 per annum ? C18..3..81. 9.10. for 3 per annum ? 5..19..101.

s, to find a

e sum of the ne mean time

- 120
- 300
- 000
- 112.0
- 4|20

 $7\frac{1}{10}$  months.

paid at 3 and £200. be paid at 8ª days. s follows: he rest at 5 aid at one  $3\frac{1}{3}$  days. 00. to pay 6 months, afterwards quired the 2 days. to be paid 3 months, he rest at e shall be 1 months. paid at 3 hat is the nonths.

#### ASSISTANT.]

480d.

BARTER.

#### BARTER

#### Is the exchanging of commodities.

RULE. Compute, by the most expeditious method, the value of the article whose quantity is given: then find what quantity of the other at the rate proposed, may be had for the same money.

Note: Sometimes one tradesman, in bartering, advances his goods above the ready money price. In this case, it will be necessary to proportionate the other's bartering price to his ready money price, by the Rule of Three.

(1) What quantity of chocolate at 4s. per lb. must be exchanged for 2 cwt. of tea, at 9s. per lb.  $3^*$ 

(2) A and B. barter: A has 20 cwt. of prunes, at 4d. per lb. ready money, but in barter will have 5d. per lb, and B has hops worth 32s. per cwt. ready money: what ought B to charge his hops, and what quantity must be give for the 20 cwt. of prunes?

(?) How much tea at 9s. per lb. can 1 have in barrer for 4 swt. 2 qrs. of chocolate, at 4s. per lb.? Ans. 2 cwt.

(4) A exchanges with B  $23\frac{1}{2}$  cwt. of cheese, worth 52s 6d. per cwt., for 8 pieces of cloth containing 248 yards, at 4s. 4d. per yard; the difference to be paid in money. Who receives the balance, and how much? Ans. A receives £7.19.1.

(5) How much ginger at  $15\frac{1}{4}d$ . per *lb*. must be exchanged for  $3\frac{1}{2}$  *lb*. of pepper, at  $13\frac{1}{2}d$ . per *lb*.? Ans. 3 *lb*.  $1\frac{3}{6}\frac{4}{7}$  oz.

(6) How many dozen of candles, at 5s. 2*d*. per dozen, must be bartered for 3 cwt. 2 qrs. 16 lb. of tallow, at 37s. 4*d*. per cwt. ? Ans. 26 dozen,  $3\frac{5}{64}$  lb.

(7) A exchanges with B 608 yards of cloth, worth 14s. per

\*  $224 \times 9 = 2016s$ . the value of the tea. As  $4s. : 1 \ lb. :: 2016s. : 501 \ lb.$  of chocolate. Ans. † As 4d. : 5d. :: 32s. : 40s. the price per *cwt*. to be charged for the hops.  $20 \ cwt. = 2240 \ lb.$ 

11200d. the value of the prunes.

As 40s. : 1 cwt. :: 11200d. :  $\frac{11200}{480} = 23 \text{ cwt. 1 } qr. 9_{18}^{16}$  lb. An

## PROFIT AND LOSS.

# yard, for 85 cwt. 2 qrs. 24 lb. of bees' wax, and £125..12. in cash. What was the wax charged per cut. ? Ans. 23..10.

(8) A barters with B 320 dozen of candles at 4s. 6d. per dozen, for cotton at 8d. per lb. and £30. in cash. What was the quantity of cotton? Ans. 11 cwt. 1 qr.

(9) How much cotton, at 1s. 2d. per lb. must be given for 114 lb. of tobacco, at 6d. per lb.? Ans. 489 1b.

## PROFIT AND LOSS

Is a Rule by which we discover the gain or loss in the buying and selling of goods ; and which enables us to adjust the prices of articles, so as to gain or lose so much per cent., &c.

The questions are solved by the Rule of Three, or Practice

The prime cost means the purchase money : therefore

The prime cost  $\begin{cases} plus \text{ the gain, or} \\ minus \text{ the loss,} \end{cases}$  equal the selling price.

The selling price minus { the prime cost equal the gain. the gain equal the prime cost. The selling price plus the loss equal the prime cost.

Gain or loss per cent. means so much on £100. purchase money, or prime cost: therefore, when £20. per cent. are gained, £120. is the selling price per cent.; when £20. per cent. are lost, £80. is the sell

Case 1. Given, the prime cost and the selling price of an integer or quantity, to find the gain or loss per cent.

As the prime cost given : the gain or loss : : £100. : the gain or loss per cent.

Case 2. Given, the prime cost as before, with a proposed gain or loss per cent. to find the selling price.

As  $\pounds 100.: \{ \pounds 100. \text{ plus the } gain \} :: the prime cost : the selling$  $or <math>\pounds 100. \text{ minus the } loss \}$  price.

Case 3. Given, the selling price of an integer or quantity, and the gain or loss per cent. to find the prime cost.

As £100 plus the gain  $\left\{ : \pounds 100. :: \text{ the selling price : the prime cost.} \right\}$ Case 4. Given, the selling price of an integer, and the gain per cent.

to find the gain per cent. at some other proposed price. As the selling price : £100. plus the gain :: the proposed price : the

selling price per cent. from which deduct £100. for the gain per cent.

Secondly, To find another selling price, at a different gain per cent. As £100. plus the gain : the selling price :: £100. plus the proposed goin : the setling price required.

A much greater variety of cases may occur; but it is presumed that the student was arains a due knowledge of these will easily campus

74

TUTOR'S

w fo

18

18

ce

fo

fo

ce ce

th

ya

ga

ĥi

83

re

sa

re

ga

5125..12. in
as. \$\alpha\$3..10.
4s. 6d. per
What was
cwt. 1 qr.
be given for
s. 484 lb.

in the buyadjust the cent., &c. or Practice

ice.

e money, of 120. is the is the sell

a integer or

gain or loss

gain or loss

the selling

nd the gain

prime cost. in per cent.

price : the n per cent.

per cent. e proposed

umed that

ASSISTANT.]

(1) If 1 yard of cloth cost 11s. and is sold for 12s. 6d. what is the gain per cent. ?\*

(2) If 60 ells of Holland cost  $\mathcal{L}18$ , what must 1 ell be sold for to gain  $\mathcal{L}8$ . per cent. ?†

(3) If 1 lb. of tobacco cost 16d. and be sold for 20d. what is the gain per cent. ? Ans. £25.

(4) If a parcel of cloth be sold for £560, gaining £12, per cent. what is the prime cost? Ans. £500.

(5) If a yard of cloth be bought for 13s. 4d. and sold again for 16s. what is the gain per cent.? Ans. £20.

(6) If 112 lb. of iron cost 27s. 6d. what must 1 cwt. be sold for to gain £15. per cent.? Ans. £1..11..7 $\frac{1}{2}$ .

(7) If 375 yards of cloth be sold for £490. at £20. per cent. profit, what did it cost per yard ? Ans. £1..1.9 $\frac{1}{4}$   $\frac{125}{375}$ .

(8) Sold 1 *cwt*. of hops for £6..15. at the rate of £25. per cent. profit. What would have been the gain per cent. if they had been sold for £8. per *cwt*.? Ans. £48..2..11 $\frac{1}{2}$ ?

(9) If 90 ells of cambric cost £60, how must I sell it per vard to gain £18, per cent.? Ans. 12s.  $7_{\pm 150}^{\pm 16} d$ .

(10) A plumber sold 10 fothers of lead for £204..15. and gained after the rate of £12..10. per cent. What did it cost him per cwt.? Ans. 18s. 8d.

(11) What was the profit on 436 yards of cloth, bought at 8s. 6d. and sold at 10s. 4d. per yard? Ans. £39..19..4.

(12) Bought 14 tons of steel at £69. per ton, which was retailed at 6d. per lb. What was the loss sustained?

Ans. £182.

(13) Bought 124 yards of linen for £32. How should the same be retailed per yard to gain £15. per cent.?

Ans. 5s.  $11_{\frac{28}{124}}d$ .

(14) Bought 249 yards of cloth at 3s. 4d. per yard, and retailed the same at 4s. 2d. per yard. What was the whole gain, and how much per cent. ?

Ans. £10..7..6. profit, and £25. per cent.

	$\begin{array}{c} \begin{array}{c} gain \\ : 1s. \ 6d. \ : : \ \pounds 100 \ : \ \frac{100 \times 3}{22} = \pounds 13128\frac{1}{2} \frac{10}{11}. \ Ans. \end{array}$	
sixp. 22 cost	$\frac{3}{s. price} cost 108 \times 18$	
† As £100 price. And	s. price cost $108 \times 18$ : £108 : : £18 : $108 \times 18$ = £1989 $\frac{1}{2}$ $\frac{4}{10}$ the selling £1989 $\frac{1}{2} \div 60 = 6s$ . $5\frac{3}{4}d$ . the price per ell. solving of this question, see Cases 1 and 2.	
For the	solving of this question, see Cases 1 and 2.	

#### FELLOWSHIP.

## "UTOR's

# FELLOWSHIP, OR PARTNERSHIP

Is a rule by which any number or quantity may be divided into certain proportionate parts. It is applied to determine the respective shares of gain or loss of the several partners in a company, in proportion to their respective shares of the capital employed as a joint stock : also in the division of common lands, and other cases of a similar kind,

# FELLOWSHIP WITHOUT TIME.

Ren. As the whole stock is to the whole gain or loss; so is each individual share to the correspondent gain or loss.

PROOF. The sum of the shares will be equal to the whole gain or loss.

(1) A and B join in trade. A puts into stock £20. and B £40; they gain £50. What is the share of each ?\*

(2) A, B, and C joined in trade; A put in  $\pounds 20$ ; B  $\pounds 30$ and C  $\pounds 40$ ; and they gained  $\pounds 180$ . What is each man's part of the gain? Ans. A  $\pounds 40$ . B  $\pounds 60$ . C  $\pounds 80$ .

(3) Four persons, B, C, D, and E formed a joint stock; B put in £227; C £349; D £115; and E £439; they gained £428. Required each person's share of the gain.

Ans. B £85..19..63  $1_{113}^{9.9}$ . C £132..3..9  $1_{23}^{12}$ .

(4) D, E, and F entered into partnership. D's stock was  $\pounds$  750; E's  $\pounds$  460; and F's  $\pounds$  500; and at the end of 12 months they had gained  $\pounds$  684. What is each man's particular share of the gain? Ans. D  $\pounds$  300. E  $\pounds$  184. and F  $\pounds$  200.

(5) A tradesman is indebted to B  $\pounds 275...14$ ; to C  $\pounds 304...7$ ; to D  $\pounds 152$ ; and to E  $\pounds 104..6$ ; but upon his decease his estate is found to be worth but  $\pounds 675...15$ . How must it be divided among his creditors ?

Ans. B's share £222..15..2-6584. C's £245..18..1 $\frac{1}{2}$ -15750. D's £122..16..2 $\frac{3}{4}$ -12227. and E's £84..5..5-15620.

(6) Four persons trade together with a joint capital; of which A has  $\frac{1}{3}$ , B  $\frac{1}{4}$ , C  $\frac{1}{5}$ , and D  $\frac{1}{6}$ , and at the end of 6

\* 20+40=60As 60 : 50 : :  $\begin{cases} 20 : \pounds 16..13..4 = \Lambda$ 's s/nare.  $40 : \frac{33..6..8}{50..0.0}$  Proof. ASSI

mont

(7 ing . and purc

> spec and stoc

> > (stoc what

R is to resp

( three £7( join mor £3(

put

## "UTOR'S

ASSISTANT.]

divided termine artners of the of com-

is each

ole gain

and B

£30 man's 80. ck; B gained

 $\frac{12}{13}$ . 113. k was onths share 00. )4..7:e his it be

5750. 20. l; of of 6

#### FELLOWSHIP.

months they gain £100. What is each person's share of the Ans. A £35..1..9-12. B £26..6..33-9. gain?

C £21..1..01-30. and D £17..10..101-6. (7) Two persons joined in the purchase of an estate yielding £1700. per annum, for £27200, whereof D paid £15000. and E the rest: some time after, they sold it for 24 years purchase. What was each person's share ?\*

Ans. D £22500. E £18300.

(8) D, E, and F, form a joint capital of £647. Their respective shares are in proportion to each other as 4, 6, and 8. and the gain is equal to D's stock. Required each person's stock and gain.

Ans. D's stock £143..15..6% gain, £31..19..04.

E's . . . 215..13..4 . . . 47..18..6 %.

 $F's \ldots 287..11..1\frac{3}{9} \ldots 63..18..0\frac{8}{27}$ 

(9) D, E, and F, joined in partnership; the amount of their stock was £100; D's gain was £3; E's £5; and F's £8; what was each man's stock ?

Ans. D's stock £18..15. E's £31..5. and F's £50.

#### FELLOWSHIP WITH TIME.

RULE. As the sum of the products of each persou's money and time is to the whole gain or loss; so is each individual product to the corresponding gain or loss.

(1) D and E enter into partnership; D puts in £40. for three months, and E £75. for four months, and they gain £70. What is each man's share of the gain ?†

(2) Three tradesmen joined in company; D put into the joint stock £195..14. for three months; E £169..18..3. for 5 months; and F £59.14..10. for 11 months: they gained £364..18. What is each man's share of the gain ?

Ans. D's £102..6..4-5008. E's £148..1..1-482802. and F's £114. 10..6 $\frac{1}{4}$ -14707.

(3) Three merchants join in company for 18 months: D puts in £500. and at 5 months' end takes out £200. at 10

". The sale of a property for so many years' purchase, is understood to be, for so much present money as the annual rent or value  $\times$  that number of years.

1.40 × =120 75×4=300 420

As 42|0:7|0::  $\begin{cases} 120: \pounds 20=D$ 's share. 300: 50=E's share. 70 Proof.

#### ALLIGATION.

[TUTOR'S

months' end puts in £300. and at the end of 14 months takes out £130; E puts in £400. and at the end of 3 months £270 more, at 9 months he takes out £140. but puts in £100. at the end of 12 months, and withdraws £99. at the end of 15 months; F puts in £900. and at 6 months takes out £200. at the end of 11 months puts in £500. but takes out £200. £100. more at the end of 13 months. They gain £206. Required each man's share of the gain.

Ans. D £50..7..6-21720. E £62..12..5 $\pm$ -29859. and F £87..0..0 $\pm$ -14167.

(4) D, E, and F, hold a piece of ground in common, for which they are to pay  $\pounds 36.10.6$ : D pits in 23 oxen 27 days; E 21 oxen 35 days; and F 16 oxen 25 days. What is each man to pay of the said rent?

Ans.  $D \pounds 13..3..1\frac{1}{2}$  624.  $E \pounds 15..11..5$  1688. and  $I \pounds 7..15..11$  1136.

## ALLIGATION

Is a rule by which we ascertain the mcan price of any compound formed by mixing ingredients of various prices; or the quantities of the various articles which will form a mixture of a certain mcan or average value. It comprises four distinct cases.

CASE 1. ALLIGATION MEDIAL. The various quantities and prices being given, to find the mean price of the mixture.

RULE. Multiply each quantity by its price, and divide the sum of the products by the sum of the quantities.\*

(1) A grocer mix d 4 cwt of sugar, at 56s. per cwt. with 7 cwt. at 43s. per cwt. and 5 cwt. at 37s. per cwt. What is the value of 1 cwt. of this mixture?

(2) A vintner mixes 15 gallons of canary, at 8s. per gallon, with 20 gallons, at 7s. 4d. per gallon; 10 gallons of sherry,

#### EXAMPLE.

\* A farmer mixed 20 bushels of wheat, at 5s. per bushel, and 36 bushels of rye, at 3s. per bushel, with 40 bushels of barley, at 2s. per bushel. What is the worth of a bushel of this mixture?

 $\begin{array}{c} 20 \times 5 = 100 \\ 36 \times 3 = 108 \\ 40 \times 2 = 80 \\ \overline{96} \quad 96)\overline{288}(3s. \quad An \end{array}$ 

at 6s per g (3 quar

ASSIS

quart quart (4 with Lisb per o

(f with the

> C bein bear

Ru avera Li Pla Is lin quan

> No ncco bers

202 be 1

ths takes as  $\pounds 270$  $\pounds 100.$  at ad of 15 at  $\pounds 200.$ that and a  $\pounds 200.$ 

859. and

non, for oxen 27 What

88. and

y comces; or a mixes four

intities

sum of

hat is  $.4\frac{1}{2}$  with  $.4\frac{1}{2}$  wit

#### ALLIGATION.

ASSISTANT.]

at 6s. 8d. per gallon; and 24 gallons of white wine, at 4s per gallon. What is the worth of a gallon of this mixture ? Ans. 6s.  $2\frac{1}{2}$   $\frac{4}{5}d$ .

(3) A malster mixes 30 quarters of brown malt, at 28s. per quarter, with 46 quarters of pale, at 30s. per quarter, and 24 quarters of 1 igh dried ditto, at 25s. per quarter. What is one quarter of the mixture worth? Ans.  $\pounds 1..8..2\frac{1}{10}d$ .

(4) A vintuer mixes 20 quarts of port, at 5s. 4d. per quart, with 12 quarts of white wine, at 5s. per quart, 30 quarts of Lisbon, at 6s. per quart, and 20 quarts of mountain, at 4s. 6d. per quart. What is a quart of this mixture worth?

Ans. 5s. 33 58d.

(5) A refiner melts 12 *lb.* of silver bullion, of 6 *oz.* fine, with 8 *lb.* of 7 *oz.* fine, and 10 *lb.* of 8 *oz.* fine; required the fineness of 1 *lb.* of that mixture.

Ans. 6 oz. 18 dwt. 16 gr.

CASE 2. ALLIGATION ALTERNATE. The various prices being given, to find the quantities which may be mixed, to bear a certain average price.

RULE. Arrange the given prices in one column, with the proposed average price on the left.

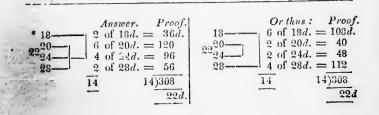
Link each less than the average will, one greater.

Place against each term the difference between that with which it is linked and the mean: and the respective differences will be the quantities required.

Note. Questions in this rule admit of a great variety of answers, according to the manner of linking them. also by taking other numbers proportional to the answers found.

(1)  $\therefore$  vintuer would mix four sorts of wine together, of 18d. 20d. 24d. and 28d. per quart, what quantity of each sort must be take to sell the mixture at 22d. per quart ?\*

(2) A grocer would mix sugar at 4d. 6d. and 10d. per lb



## ALLIGATION.

so as to sell the compound for 8d. per lb. What quantity of each kind must he take ?

Ans. 2 lb. at 1d. 2 lb. at 6d. and 6 lb. at 10d. (3) How much tea at 16s. 14s. 9s. and 8s. per lb. will compose a mixture worth 10s. per lb.?

Ans. 1 lb. at 16s. 2 lb. at 14s. 6 lb. at 9s. and 4 lb. at 8s. (4) A farmer would mix as much barley, at 3s. 6d. per

bushel, rye at 4s. per bushel, and oats at 2s. per bushel, as will make a mixture worth 2s. 6d. per bushel. How much of each sort ? Ans. 6 b. of barley, 6 of rye, and 30 of oats.

(5) A tobacconist would mix tobacco at 2s., 1s. 6d., and 1s. 3d. per lb. so that the compound may be worth 1s. 8d. per 16. What quantity of each sort must he take ?

Ans. 7 lb. at 2s. 4 lo. at 1s. 6d. and 4 lb. at 1s. 3d.

CASE 3. ALLIGATION PARTIAL. This is similar to Case 2, except that one of the quantities is limited.

RULE. Link the prices, and place the differences as before.

Then, as the difference opposite to that whose quantity is given, is to each other difference; so is the given quantity to each required

(1) A tobacconist intends to mix 20 lb. of tobacco at 15d. per lb. with others at 16d. 18d. and 22d. per lb. How many pounds of each sort must he take to make one pound of the mixture worth 17d. ?\*

(2) How much coffee, at 3s. at 2s. and at 1s. 6a. per lb. With 20 lb. at 55, mill make a mixture worth 2s. 8d. per lb.?

Ans, 35 .... at 3s. 70 lb. at 2s. and 10 lb. at 1s. 6d. (3) A distiller would mix 10 gallons of French brandy, at 48s. per gallon, with British at 28s. and spirits at 16s. per gallon. What quantity of each sort must he take to afford it for 32s. per gallon? Ans. 8 British, and 8 spirits.

(4) What quantity of teas at 12s. 10s. and 6s. must be mixed with 20 b. at 4s. per b. that the mixture may be worth 8s. per 1b.? Ans. 10 lb. at 6s. 10 lb. at 10s. 20 lb. at 12s.

Answer. Proof. 16. 16. 5 20 lb. at 15d. = 300d. As 5:1::20:4 \* 15-1 4 lb. at 16d. = 64d.17<sup>16-</sup> 18-1 4 lb. at 18d. = 72d. As 5:2::20:8 2 8 lb. at 22d. = 176d.22-As 36 18 : 612d. : : 1 1b. : 17d.

ASSIST

[TUTOR'S.

CAS 2, exc RULE

'fhen so is th

(1)4d. pe 8d. pe (2)per lb What Ans. (3)

16s. 1 per g mixtu tity o A

(4) 24, 2 of 42 each 02. 01

> C TI 11 many (2 ells a

## antity of

at 10d. will com-

at 8s. 6d. per ushel, as much of *f* oats. 6d., and 1s. 8d.

s. 3d.

Case 2,

given, is required

at 15d. v many of the

per lb.? or lb.? 6d. ody, at ford it rits. ust be worth 12s.

# ASSISTANT.] COMPARISON OF WEIGHTS AND MEASURES.

CASE 4. ALLIGATION TOTAL. This is also similar to Case 2, except that the whole quantity of the compound is limited.

RULE. Link the prices, and place the differences as before.

Then, As the sum of the differences is to each particular difference; so is the quantity given to each required quantity.

(1) A grocer has four sorts of sugar at 12*d*. 10*d*. 6*d*. and 4*d*. per *lb*. and would make a composition of 144 *lb*. worth 8*d*. per *lb*. What quantity of each sort must he take?\*

(2) A grocer having 4 sorts of tea at 5s. 6s. 8s. and 9s. per *lb*. would have a composition of 87 *lb*. worth 7s. per *lb*. What quantity must there be of each sort?

Ans. 141 lb. of 5s. 29 lb. of 6s. 29 lb. of 8s. and 141 lb. of 9s.

(3) A vintner having 4 sorts of wine, viz. white wine at 16s. per gallon, Flemish at 24s. per gallon, Malaga at 32s. per gallon, and Canary at 40s. per gallon; would make a mixture of 60 gallons worth 20s. per gallon. What quantity of each sort must he take?

Ans. 45 gallons of white wine, 5 of Flemish, 5 of Malaga, and 5 of Canary.

(4) A jeweller would melt together four sorts of gold, of 24, 22, 20, and 15 carats fine, so as to produce a compound of 42 oz. of 17 carats fine. How much must he take of each sort? Ans. 4 oz. of 24, 4 oz. of 22, 4 oz. of 20, and 30 oz. of 15 carats fine.

## COMPARISON OF WEIGHTS AND MEASURES.

This is merely an application of the Rule of Proportion. (1) If 50 Dutch pence be worth 65 French pence, how many Dutch pence are equal to 350 French pence ?†

(2) If 12 yards at London make 8 ells at Paris, how many ells at Paris will make 64 yards at London ? Ans. 423

	A	Inswer.		Proof.						16.		lb.	
* 12	4	48 at	12d.	= 576	As	12	:	£	::	144	:	48	
10	2	24 at	10d.	= 240	As	12	: :	2	::	144	:	24	
8 6				= 144									
4	4			= 192									
Sum	12	144	e 14	4)1152(	8 <i>d</i> .								
t As 65 : 50 or, as 13 : 10	::	350 :	$\frac{3500}{13}$	$=260\frac{3}{1}$	<u>.</u>	Ans							
-1				D2									

# VULGAR FRACTIONS.

[TUTOR'S

(3) If 30 *lb* at London make 28 *lb*. at Amsterdam, how many *lb*. at London will be equal to 350 *lb*. at Amsterdam ?

(4) If 95  $\mathcal{B}$ . Flemish make 100  $\mathcal{B}$ . English, how many  $\mathcal{B}$ . English are equal to 275  $\mathcal{B}$ . Flemish? Ans.  $289\frac{n}{16}$ 

# PERMUTATION

# Is the changing or varying of the order of things.

# To find the number of changes that may be reade in the position of any given number of things.

RULE Multiply the numbers 1, 2, 3, 4, &c., continually together, to the given number of terms, and the last product will be the answer.

(1) How many changes may be rung upon 12 bells, and in what time would they be rung, at the rate of 10 changes in a minute, and reckoning the year to contain 365 days, 6 hours?

 $1 \times 2 \times 3 \times 4 \times 5 \times 6 \times 7 \times 8 \times 9 \times 10 \times 11 \times 12 = 479001600$ changes, which  $\div 10 = 47900160$  minutes = 91 years, 26 days, 6 hours.

(2) A young scholar, coming to town for the convenience of a good library, made a bargain with the person with whom he lodged, to give him  $\pounds 40$ . for his board and lodging during so long a time as he could place the family (consisting of 6 persons besides himself) in different positions, every day at dinner. How long might he stay for his  $\pounds 40$ .?

Ans. 5040 days.

# VULGAR FRACTIONS.

### DEFINITIONS.

1. A Fraction is a part or parts of a unit, or of any whole number or quantity; and is expressed by two numbers, called the *terms*, with a line between them.

2. The upper term is called the Numerator, and the lower term, the Denominator. The Denominator shows into how

#### ASSIST

many numbe 3. I the N divisor

## 4. denom

5. sists  $\frac{1}{2}$  of  $\frac{1}{2}$ sever

> 6. *less* t

7. tor ei  $\frac{8}{4}, \frac{15}{12}$ 8.

a frac 9. denot  $\frac{2}{3}$ , t

and t

\* 1 the *i* parts 15. 0 those same † '. ed in twelf twel remo **‡** . four prop grea T

dam, how terdam ? s. 375. many *lb*. 289.<sup>p</sup>

## position

gether, to unswer.

ells, and changes 5 days,

001600 1 years,

enience on with lodging consists, every ? lays.

whole called

louer how

#### ASSISTANT.]

## VULGAR FRACTIONS.

many equal parts *unity* is divided; and the Numerator is the number of those equal parts signified by the Fraction.\*

3. Every Fraction may be understood to represent Division; the Numerator being the dividend, and the Denominator the divisor.

# Fractions are distinguished as follows:

4. A SIMPLE FRACTION consists of one numerator and one denominator : as  $\frac{3}{4}$ ,  $\frac{1}{12}$ , &c.

5. A COMPOUND FRACTION, or fraction of a fraction, consists of two or more fractions connected by the word of: as  $\frac{1}{2}$  of  $\frac{3}{5}$  of  $\frac{7}{12}$ , &c. This properly denotes the *product* of the several fractions.

6. A PROPER FRACTION is one which has the numerator less than the denominator: as  $\frac{1}{4}$ ,  $\frac{2}{4}$ ,  $\frac{3}{4}$ ,  $\frac{11}{12}$ , &c.‡

7. An IMPROPER FRACTION is one which has the numerator either equal to, or greater than the denominator: as  $\frac{1}{4}$ ,  $\frac{5}{4}$ ,  $\frac{1}{5}$ , &c. $\frac{1}{5}$ 

8. A MIXED NUMBER is composed of a whole number and a fraction, as  $1\frac{9}{3}$ ,  $17\frac{1}{2}$ ,  $8\frac{71}{91}$ , &c.

9. A COMPLEX FRACTION has a fractional numerator or denominator: but this denotes Division of Fractions. Thus,

 $\frac{\frac{2}{3}}{\frac{5}{6}}$ , two-thirds divided by five-sixths,  $\frac{8}{1\frac{9}{5}}$ , eight divided by one and two-thirds.

\* In the fraction five-twelfths  $(\frac{5}{12},)$  the Denominator 12 shows that the unit or whole quantity is surposed to be divided into 12 equal parts : so that if it be one shilling, each part will be one-twelfth of 1s. or one penny. The Numerator shows that 5 is the number of those twelfth parts intended to be taken : so  $\frac{5}{12}$  of a shilling are the same as 5 pence;  $\frac{5}{12}$  of a foot, the same as 5 inches.

<sup>†</sup> The fraction  $\frac{5}{12}$  signifies not only  $\frac{5}{12}$  of a unit, but 5 units divided into 12 parts, or a twelfth part of five : and it is obvious that five twelfth parts of one shilling (or five peace) is the same as one. twelfth part of five shillings. This date of considering Fractions removes many of the student's difficulties.

<sup>‡</sup> A proper fraction is always less than unity: thus <sup>3</sup> wants one. fourth, and  $\frac{1}{12}$  wants one-twelfth of being equa, to 1. But an improper fraction is equal to unity when the terms are equal, are greater than unity when the numerator is the greater.

Thus  $\frac{4}{7}$ , or  $\frac{11}{11}$ , or  $\frac{73}{73}$ , is each =1; and  $\frac{1}{7}$  is  $\frac{1}{7}$  is  $\frac{69}{20} = 3\frac{9}{20}$ .

# VULGAR FRACTIONS.

10. A COMMON MEASURE (or DIVISOR) is a number that will exactly divide both the terms. When it is the greatest number by which they are both divisible, it is called the GREATEST COMMON MEASURE.

Note. A prime number has no factor, except itself and unity.

84

A multiple signifies any product of a number; and is therefore divisible by the number of which it is a multiple: thus 14, 21, 28, &c., are multiples of seven. Also 14 is a common multiple of 2 and 7; 21, of

# REDUCTION

Is the method of changing the form of fractional numbers or quantities, without altering the value.

# Case 1. To reduce a fraction to its lowest terms.

RULE. Divide both the terms by any common measure that can be discovered by inspection; which will produce an equivalent fraction in lower terms. Treat the new fraction in a similar manner; repeating the operation till the lowest terms are obtained.\*

When the object cannot be accomplished by this process, divide the greater term by the less, and that divisor by the remainder, and so on till nothing remains. The last divisor will be the greatest common measure; by which divide both terms of the fraction, and the quotients will be the *lowest terms*.

<ul> <li>(3) R (3) R (3)</li></ul>	Ans. 25. Ans. 177. Ans. 3. Ans. 35. Ans. 3. Ans. 3. Ans. 3.
--	---

\* This first method of *abbreviating* fractions is, when practicable, always to be preferred : and in the application of it, the following observations will be found exceedingly useful.

An even number is divisible by 2.

A number is divisible by 4, when the tens and units are so; and by 3, when the hundreds, tens, and units are divisible by 3.

A number is a multiple of 3, or of 9, when the sum of its digite is a multiple of 3, or of 9.

A 5 or a 0 in the units' place, admits of division by 5; one cipher ad mits of division by 10, two, by 100, &c. ASSIST

[TUTOR'S

(7) (8)

Cas

RUL

(1)(2) (3) (4)

(5)(6)

#### Case

Run sion, a which

No by pu (1)

A n digits contai A n tiple o All place

> (1) terms  $\div -1$  $\frac{126}{162}$ (2) terms  $\div$

ber that greatest

ity.

ore divisi-&c., are 7; 21, of

bers or

can be ction in peating

d so on common notients

25. 171. 3.55 3.55 4.

cable,

nd by

e 181 8

er ad

#### ASSISTANT.]

3

#### REDUCTION.

(7)	Reduce $99713$ to the lowest terms.	Ans. 7
(8)	Reduce $\frac{90715}{113960}$ to the lowest terms. What are the lowest terms of $\frac{3108}{3552}$ ?	Ans. 7.

Case 2. To reduce an improper fraction to its equivalent number.

RULE. Divide the upper term by the lower.

This is evident from Definition 3.

(1) Reduce	129 to a mixed number. 129	=183. Ans.
(2) Reduce	<sup>6</sup> <sup>9</sup> to its equivalent number.	Ans. 133.
(3) Reduce	<sup>2</sup> 5 to its equivalent number.	Ans. 273.
(4) Reduce	1245 to its equivalent number.	Ans. 5613.
(5) Reduce	<sup>3</sup> <sup>§</sup> / <sub>21</sub> <sup>9</sup> to its equivalent number.	Ans. 1837.
(6) Reduce	$1\frac{15}{10}$ to its equivalent number.	Ans. 7115.

Case 3. To reduce a mixed number to an improper fraction.\*

RULE. Multiply the whole number by the denominator of the fracsion, and to the product add the numerator for the numerator required, which place over the denominator.

Note. Any whole number may be expressed in a fractional form by putting 1 for the denominator : thus  $11 = \frac{11}{1}$ .

(1) Reduce  $18\frac{3}{7}$  to the form of a fraction.

A number is a multiple of 11, when the sum of the 1st, 3d, 5th, &c., digits = that of the 2d, 4th, 6th, &c., digits, after retrenching the elevens contained in each.

A multiple of both 2 and 3 is, of course, a multiple of 6; and a multiple of 3 and 4 may be divided by 12.

All prime numbers, except 2 and 5, have 1, 3, 7, or 9, in the units' place; all othors are composite.

#### EXAMPLES.

terms possible. $\div 10 \div 9$			ause we cannot easily common measure, pro-
(2) Reduce $\frac{12}{21}$	$\frac{14}{18} = \frac{7}{6}$ . Ans. $\frac{1540}{045}$ to the lowest	76)133(1 76	then 19)76 19)133 = $\frac{4}{7}$ . Ans.
terms.		57)76	(1
	$\div$ 11		(+
13540 = 2508	$=\frac{836}{1463}=\frac{76}{133}$	51	
\$1842 4208	greatest con	n. meas., 19)	57(3
	greatest cor	n. moust, 10,	
			57
ett" m 2000	* This is the cór	werse of Ca	se 2.
	$+ 18\frac{3}{7} = \frac{18 \times 7 + 7}{7}$	$\frac{-3}{-}=\frac{129}{7}$ .	Ans.

86	VULGAR FRACTIONS.	[TUTOR'S
(0)	Reduce $56\frac{13}{2}$ to an improper fraction. Reduce $183\frac{5}{2}$ to an improper fraction.	4
(5)	Reduce 27? to its equivalent fraction.	Ans. $\frac{69}{5}$ . Ans. $\frac{24}{5}$ .
(0)	the duce $514_{16}^{2}$ to a fractional form.	Ans. 8229.
	To reduce a fraction to another of the ping a certain proposed numerator or den	ominator.
proposed	As the present numerator is to the denominator numerator to its denominator. Or, as the pr the numerator, so is the proposed denomination	inator, so is the
(1) R	educe $\frac{2}{3}$ to a fraction of the same values shall be 12.	ne, whose nu-
(2) R	educe $\frac{5}{2}$ to a fraction of the same set	
nerator	educe $\frac{5}{7}$ to a fraction of the same valu shall be 47.	ic, whose nu Ans. $\frac{47}{654}$ .
(4) Re	educe $\frac{2}{3}$ to a fraction of the same valu r shall be 18.	e, whose de-
(5) Re	educe 5 to a fraction of the sume mil	
ominato	educe $\frac{3}{9}$ to a fraction of the same value r shall be 19.	e, whose de-
		Ans. $\frac{16\frac{9}{9}}{19}$ .
	To reduce complex and compound fraction form.	
RULE. H	for a <i>complex</i> fraction, reduce both terms to sin <i>perting</i> the lower fraction, they may be cons <i>compound</i> fraction. And to reduce a compound	uple fractions:
rms of a c nge all th ith the si wer terms ucing their ne with t	compound function. And to reduce a compound in numerators above a line, and the denomi- gns of multiplication interserted: divide all : is that are commensurable,* cancelling them with r quotients above and below them respective the quotients: thus the methods are a second to be a second the quotients.	ndered as the ad fraction, ar. nators below, he upper and th a dash, and
ll give the	e single fraction in its lowest terms.	eued numbers
This rule	having a common divisor. e is of the highest importance as tending to exp	
	c and produce as tending to exp	pearte the bu-

 $1\frac{245}{22}$   $3\frac{848}{21}$   $S. \frac{69}{5}$   $3\frac{45}{2}$   $8\frac{229}{16}$ 

e vulae, pr.

so is the enominats nume-

be nu-  $1\frac{2}{16}$ .  $1\frac{2}{5}$ .  $\frac{2}{5}\frac{5}{5}$ .  $\frac{47}{55\frac{1}{5}}$ .  $\frac{47}{55\frac{1}{5}}$ . se de-  $\frac{12}{5\frac{5}{5}}$ . se de-  $\frac{2}{5\frac{5}{5}}$ . se de- $\frac{69}{5\frac{9}{19}}$ .

simple

etions: as the on, ar. below, er and h, and bo the mbers

e bu-

## ASSISTANT.]

## REDUCTION.

(1) Reduce $\frac{36\frac{2}{3}}{48}$ to a simple fraction.	Ans. 55.
(2) Reduce $\frac{23\frac{5}{7}}{38}$ to a simple fraction.	Ans. 183.
(3) Reduce $\frac{47}{65\frac{1}{5}}$ to a simple fraction.	Ans. §.
(4) Reduce $\frac{19}{44\frac{1}{4}}$ to a simple fraction.	Ans. 3.
(5) Reduce $\frac{2}{9}$ of $\frac{3}{5}$ of $\frac{5}{8}$ to a single fraction. (6) Reduce $\frac{5}{9}$ of $\frac{4}{7}$ of $\frac{1}{1\frac{1}{2}}$ to a simple fraction.	Ans. $\frac{1}{4}$ . Ans. $\frac{5.5}{180}$ .

siness of computation, by *abbreviating to the utmost* all fractional expressions, as we proceed.

#### EXAMPLES.

(1) Reduce the complex fraction  $\frac{7\frac{1}{3}}{8\frac{5}{3}}$  to a sumple form.

$$\frac{\frac{7_1}{3}}{\frac{8_9}{9}} = \frac{\frac{2}{3}}{\frac{7}{9}} = \frac{\frac{2}{22} \times 9}{\frac{3}{3} \times \pi \pi} = \frac{e}{7} Ans.$$

(2) Reduce  $\frac{9}{10}$  of  $\frac{2}{3}$  of  $\frac{7}{3}$  of  $\frac{5}{14}$  to a simple fraction.

$$r_{16}^{9}$$
 of  $r_{3}^{2}$  of  $r_{8}^{7}$  of  $r_{14}^{5} = \frac{3 \times 2 \times 7 \times 5}{4 \times 2 \times 7 \times 3 \times 3 \times 3 \times 3 \times 3} = \frac{3}{16}$ . Ans.

(3) Reduce the annexed fractional expression to its proper quaniny.

$\frac{16}{11}$ of $\frac{111}{108}$	$\frac{\frac{9}{13}}{\frac{13}{2}} \text{ of } \frac{\frac{73}{147}}{\frac{18}{23}} \text{ of }$	$f \frac{6\frac{8}{13}}{24\frac{8}{13}}$ of 8	$\mathcal{L}_{\frac{5}{64}} = \frac{16}{11}$	$\times \frac{\frac{1452}{13}}{\frac{108}{1}} >$	$\langle \frac{\frac{72}{147}}{\frac{13}{25}} \rangle$	$\left( \frac{\frac{93}{13}}{\frac{320}{13}} \times \frac{567}{64} \right)$
1 .X\$ >	11 X2X < XA52 ×	$1$ $\$$ $1 \times 72 \times$	1 5 A 25 × 9	\$×13×	567	£. 177 £.
- <u>11</u> ×	$\langle I \emptyset \$ \times I \\ \$ \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1$	(\$×1\$×. 1 2 1	¥477 × 329 21 2 3	0×15× 0 3 4 1	64 8	$\frac{1}{32} = 2\frac{1}{32}$

### VULGAR FRACTIONS.

(7) Reduce  $\frac{1}{12}$  of  $\frac{13\frac{3}{5}}{14\frac{4}{6\frac{3}{5}}}$  of  $\frac{28}{38\frac{3}{3}}$  to a simple fraction. (8) Reduce  $\frac{3}{4}$  of  $\frac{6}{5}$  of  $11\frac{3}{8}$  to a single fraction. Ans.  $\frac{9}{16}$ . (9) Reduce  $\frac{777}{128}$  of  $37\frac{1}{3}$  of 5 to its equivalent number. Ans. 143. (10) Reduce  $\frac{1}{14} of \frac{3}{3} of \frac{1}{2}$  to its equivalent number. Ans. 112 4. Ans. 77. Case 6. To reduce a fractional quantity of a given denomina tion to an equivalent fraction of another denomination. RULE. Consider what numbers would reduce the greater denomina tion to the less; then to reduce to a greater name, multiply the denom inator by those numbers, and to reduce to a less name, multiply the

numerator: the compound thus produced, when reduced to a simple form, will be the fraction required.

- (1) Reduce  $\frac{7}{6}$  of a penny to the fraction of a pound.\*
- (2) Reduce  $\frac{3}{4}d$  to the fraction of a crown. Ans.  $\frac{1}{80}$  cr.
- (3) Reduce  $\frac{4}{3}$  dwts. to the fraction of a lb. troy. Ans.  $\frac{1}{360}$  lb. (4) Reduce  $\frac{4}{7}$  lb. avoirdupois to the fraction of a cut.

Ans. 196 cwt.

- (5) Reduce  $\frac{7}{1520}$  of a pound to the fraction of a penny.
- (6) Reduce  $\mathcal{L}_{\frac{1}{320}}$ , to the fraction of a penny. Ans.  $\frac{3}{4}d$ .

(7) Reduce  $\frac{1}{3b}$  of a pound troy to the fraction of a penny-weight. Ans.  $\frac{4}{5}$  dwt.

(6) Reduce  $\frac{1}{165}$  cwt. to the fraction of a *lb*. Ans. 4 1b.

# Case 7. To find the proper value of a fractional quantity.

RULE. Reduce the numerator to such lower denomination as may be necessary, and divide by the denominator; abbreviating as much as possible in valuing the remainders.

Norr. It is evident, from Definition 3, that this Case is precisely that of Compound Division.

(1) Reduce  $\frac{3}{4}$  of a pound sterling to its proper value.

\* 
$$\frac{1}{8}d. = \frac{7}{8 \times 12 \times 20} = \mathcal{L}_{\overline{1920}}^{7}$$
. Ans.  
†  $\mathcal{L}_{\overline{1920}}^{7} = \frac{7 \times 20 \times 12}{1920} = \frac{7 \times 12}{96} = \frac{7}{8}d.$  Ans.  
‡  $\mathcal{L}_{4}^{3} = \frac{3 \times 20}{4} = 3 \times 5 = 15s.$  Ans.

88

ASSIST

[TUTOR'S

(2)**(**3)

(4) (5)

(3)

(7) (8)

(9)

(10

Case

RUL nomin the de

(1)

 $\binom{2}{(3)}$ 

(4) (5)

(6)

eil. (7)

(8)

(9)

(10 Case

Rul

is a fa a com

n.  $\frac{1}{2}\frac{4}{3}\frac{3}{2}$ .  $4ns. \frac{9}{6}$ . mber.  $112\frac{7}{34}$ . ber.  $1ns. 7\frac{3}{3}$ .

denomin**a** ation.

denomina the denom ultiply the o a simple

nd.\* <sup>3</sup>5 cr. s. 355 lb. wt.

 $\frac{1}{6} cwt.$ penny. penny.  $as. \frac{3}{4}d.$ on of a  $\frac{4}{5} dwt.$  $. \frac{4}{4} lb.$ 

intity.

ns may be much as

isely that

0.1

#### ASSISTANT.]

(2) Reduce *§s.* to its proper value.

## REDUCTION.

(3) Reduce 4 of a lb, avoirdupois to its proper value.

Ans. 9 oz. 23 dr. Ans. 3 qrs. 31 lb. (4) Reduce  $\frac{\pi}{4}$  cwt. to its proper value. (5) Reduce  $\frac{3}{5}$  of a *lb*. troy to its proper value. Ans. 7 oz. 4 duts. (3) Reduce  $\frac{14}{25}$  of an ell English to its proper value. Ans. 2 qrs. 31 nails. (7) What is the value of  $\pounds \frac{57}{7} \frac{1}{6} \frac{9}{7}$ ? Ans. 19s. 101 1 (8) Reduce 235 of a mile to its proper value. Ans. 6 fur. 105 yds. (9) Reduce  $\frac{73}{4}$  of an acre to its proper value. Ans. 1 a. 2 r. 31 per. (10) Find the value of  $\frac{15487}{34167}$  cut. Ans. 1 qr. 22 lb.  $\frac{237}{387}$ . To reduce any given quantity to the fraction of a Case 8. greater denomination. RULE. Reduce the given quantity (if compound) to the lowest denomination mentioned, that it may assume a simple form : then multiply the denominator, as in Case 6. (1) Reduce 15s. to the fraction of a pound sterling.  $15s. = \mathcal{L}_{\frac{1}{2}0}^{\frac{1}{2}} = \mathcal{L}_{\frac{3}{4}}^{\frac{3}{4}}$ . Ans. (2) Reduce 4d.  $3\frac{1}{5}$  qrs. to the fraction of a shilling. Ans. 2 (3) Reduce 9 oz.  $2\frac{3}{4}$  dr. to the fraction of a lb. avoirdupois Ans. 4 16. (4) Reduce 3 grs. 31 lb. to the fraction of a cut. Ans. 7 civt. (5) Reduce 7 oz. 4 dwts. to the fraction of a lb. troy. Ans. 3 16. (6) Reduce 2 qrs.  $3\frac{1}{9}$  nails to the fraction of an English eil Ans. & ell. (7) Reduce 14s.  $6\frac{1}{2}d$ .  $\frac{2}{11}$  to the fraction of a  $\mathcal{L}$ . Ans.  $\pounds_{\frac{8}{11}}$ . (8) Reduce 4d.  $1\frac{1}{13}$  qrs. to the fraction of a crown. Ans.  $\frac{29}{340}$  cr. (9) What fraction of an acre are 3 roods, 32 perches? Ans.  $\frac{19}{20}$  a. (10) What part of a shilling are  $\frac{2}{3}$  of 2d. Ans. 1s Case 9. To find the least common multiple of two or more numbers. RULE. Arrange the given numbers in a line, (omitting any one that is a factor of one of the others,) and divide any two or more of them by a common divisor, placing the quotients and undivided numbers below;

Ans. 4d. 31 yrs.

# VULGAR FRACTIONS

## TUTOR'S

proceed with these in the same manner, and repeat the process till there remain not any two numbers commensurable : the continued product of the divisors, quotients, and undivided numbers, will be the least common

(1) Required the least common multiple of 2, 3, 4, 5, 6, 7, 8, 9, part 10.\*

(2) Find the least number divisible by 3, 4, 5, 6, 7, and 8.

(3) What is the least common multiple of 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, and 12? Ans. 27720.

Case 10. To reduce fractions to a common denominator.

Multiply each numerator into all the denominators, except RULE 1. its own, for a numerator; and all the denominators for a control de-RULE 2.

Find the least common multiple of the denominators, which will be the least common denominator. Divide this by each denominator, and multiply the several quotients by the respective numerators for

(1) Reduce  $\frac{2}{4}$  and  $\frac{4}{7}$  to a common denominator. (2) Reduce  $\frac{1}{2}$ ,  $\frac{3}{4}$ , and  $\frac{5}{6}$ , to a common denominator. Ans.  $\frac{32}{64}$ ,  $\frac{49}{64}$ , and  $\frac{40}{64}$ ; or  $\frac{4}{3}$ ,  $\frac{9}{8}$ , and  $\frac{5}{8}$ . (3) Reduce  $\frac{7}{8}$ ,  $\frac{4}{5}$ ,  $\frac{6}{10}$ , and  $\frac{6}{7}$ , to a common denominator. Ans. 735, 560, 504, and 720. (4) Reduce  $\frac{3}{5}$ ,  $\frac{1}{2}$ , and  $\frac{1}{7}$ , to a common denominator. (5) Reduce  $\frac{3}{11}$ ,  $\frac{4}{7}$ , and  $\frac{3\frac{1}{2}}{15}$  of 2, to a common denominator  $Ans. \frac{4}{70}, \frac{3}{5}, and \frac{1}{70}$ . (6) Reduce  $1\frac{1}{4}$ ,  $2\frac{1}{5}$ , and  $\frac{1}{3}$  of  $1\frac{1}{4}$ , to a common denominator. Ans. 75, 132, and 25.

\* 2 and 4, being factors of 3, 3 a factor of 9, and 5 a factor of 10, may be omitted. Thus,

2)6,	7,	8,	9,	10
3)3,	7,	4,	9,	5
1,	7,	4,	З,	5
		and the owner.		and the second second

Then  $2 \times 3 \times 7 \times 4 \times 3 \times 5 = 42 \times 60 =$ 2520, the least number divisible by all the given numbers.

 $\begin{array}{c} 1 & 2 \times 7 = 14 \\ 4 \times 4 = 16 \end{array}$  numerators. Ans,  $\frac{14}{28}$  and  $\frac{16}{28}$  $4 \times 7 = 28$  the denominator.

RULE. which I

ASSIST.

(1) Ac

(2) Ad (3) Ad

(4) Ad

(5) Ad

Fra and th

(10)

(11)

(12)

(13)

(14)? of a (15)

roods,

RULE which Whe er than the cou of he

(1)(2)(3)

(4) (5)

Fra ss dire

\* W sum of Thu 413. A

ocess till there ned product of least common

3, 4, 5, 6, 7,

6, 7, and 8. 1ns. 840.

, 4, 5, 6, 7, . 27720.

minator.

ators, except contain de-

ators, which h denominamerators for

or.

, and s. inator. nd 128. or. and 10. ominator. 1 539 ominator. nd 25.

of 10, may

 $2 \times 60 =$ risible by

#### ASSISTANT.]

# SUBTRACTION.

#### ADDITION.

RULE. Reduce the given fractions to a common denominator, over which place the sum of the numerators. . . . . . . . .

<ul> <li>(3) Add <sup>1</sup>/<sub>5</sub>, 4<sup>1</sup>/<sub>3</sub>, and <sup>2</sup>/<sub>2</sub>.*</li> <li>(4) Add 7<sup>2</sup>/<sub>5</sub> and <sup>2</sup>/<sub>4</sub> together.</li> </ul>	(6) Add $5\frac{2}{3}$ , $6\frac{7}{8}$ , and $4\frac{1}{2}$ . (7) Add $1\frac{4}{9}$ , $3\frac{1}{7}$ , and $\frac{1}{2}$ of 7. (8) Add $\frac{9}{10}$ of $6\frac{7}{8}$ , and $\frac{4}{7}$ of $7\frac{1}{3}$ .
Fractional quantities may be and the sum found by Compou	$  (9)$ Add $\frac{1}{5}$ of $9\frac{3}{8}$ , and $\frac{2}{3}$ of $4\frac{5}{8}$ . = reduced to their proper values, and Addition. = of a shilling. Ans. 8s. 4d.

Ans. 14s.

- (11) Add  $\frac{1}{2}d$ .  $\frac{5}{3}s$ . and  $\pounds \frac{2}{3}$ .
- (12) Add  $\frac{3}{5}$  lb. troy,  $\frac{1}{6}$  oz. and  $\frac{5}{8}$  oz.

Ans. 7 oz. 19 dwts. 20 gr.

(13) Add 4 of a ton to  $\frac{5}{6}$  of a cwt.

Ans. 12 cwt. 1 gr. 11 lb.

(14) What is the sum of  $\frac{2}{3}$  of £17..7..6d.,  $\frac{4}{5}$  of £1 $\frac{2}{3}$ . and Ans.  $\pounds 13..0..2\frac{1}{2}$ . ? of a crown?

(15) Add  $\frac{4}{5}$  of 3 a. 1 r. 20 p.,  $\frac{3}{8}$  of an acre, and  $\frac{3}{4}$  of 3 Ans. 3 a. 2 r. 334 p. roods, 15 perches.

#### SUBTRACTION.

RULE. Reduce the given fractions to a common denominator, over which place the difference of the numerators.

When the numerator of the fractional part in the subtrahend is greater than the other numerator, borrow a fraction equal to unity, having the common denominator; then subtract, and carry one to the integer of he subtrahend.

- (1) From  $\frac{3}{4}$  take  $\frac{5}{7}$ .  $\frac{3}{4} \frac{5}{7} = \frac{2}{2} \frac{1}{8} \frac{2}{2} \frac{0}{8} = \frac{1}{28}$ . Ans.

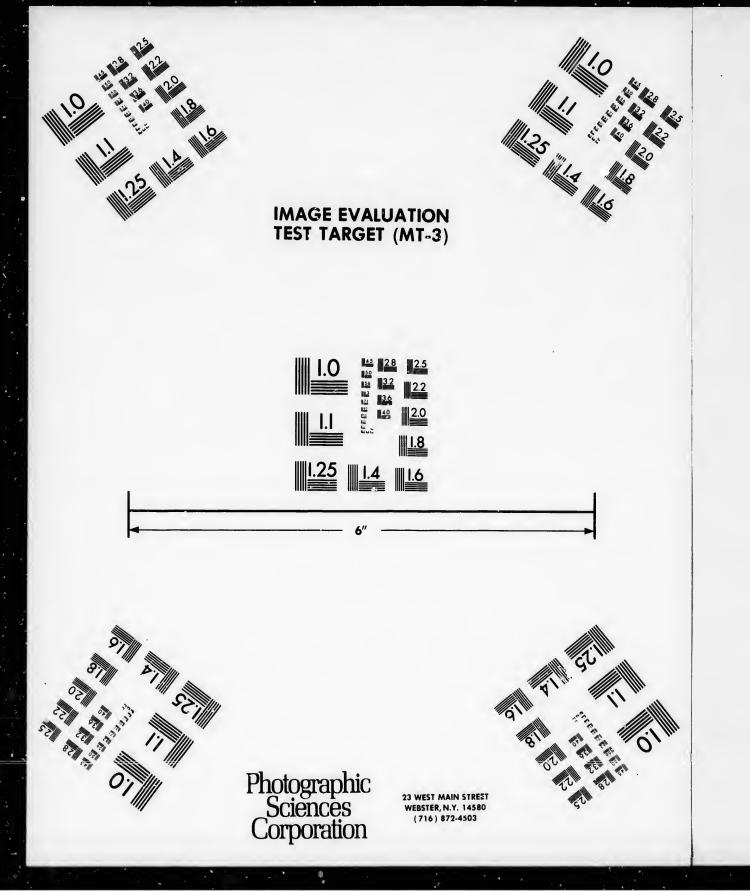
- (2) From  $\frac{5}{6}$  take  $\frac{3}{5}$ . (3) From  $5\frac{2}{3}$  take  $\frac{9}{10}$  of  $\frac{5}{8}$ . (4) From  $\frac{3}{4\frac{8}{5}}$  take  $\frac{3}{6}$  of  $\frac{1}{3}$ . (5) From  $\frac{1}{2\frac{6}{5}}$  take  $\frac{1}{7}$  of  $\frac{2}{3}$ . (6) From  $64\frac{1}{4}$  take  $\frac{2}{3}$  of  $\frac{3}{4}$ . (7) From  $15\frac{1}{6}$  take  $12\frac{7}{40}$ . (8) Subtract  $\frac{23}{35}$  from  $1\frac{3}{3}$ . (9) Subtract  $\frac{1}{2\frac{7}{4}}$  from  $\frac{1}{8}$  of 9.

Fractional quantities may be reduced to their proper values, **58** directed in Addition

\* When there are integers among the given numbers, first find the sum of the fractions, to which add the integers.

Thus in Ex. 3,  $\frac{1}{5} + \frac{2}{5} = \frac{3}{5}$ ; then  $\frac{3}{5} + \frac{1}{3} = \frac{9}{15} + \frac{5}{15} = \frac{14}{15}$ ; and  $4 + \frac{14}{15} = \frac{14}{15}$ 414. Ans.







## VULGAR FRACTIONS.

92

(10) From  $\frac{3}{8}$  of a pound take  $\frac{3}{8}$  of a shilling. Ans. 7s.  $1\frac{1}{2}d$ 

(11) From  $1\frac{2}{3}s$ . take  $\frac{2}{3}$  of  $7\frac{1}{2}d$ . Ans. 1s. 3d.

(12) What is the difference between  $\frac{3}{8}$  of  $\pounds l_{\frac{5}{24}}$ ; and 15 of £133.? Ans. 2d. 31 qrs.

- (13) Subtract 5 cwt. from 4 ton. Ans. 10 cwt. 2 qrs. 102 1b.
- (14) From  $\frac{2}{3}$  of 5 lb. troy subtract  $\frac{5}{2}$  of  $3\frac{1}{2}$  oz.

Ans. 3 1b. 2 oz. 1 dwt. 22 gr.

(15) Subtract  $7\frac{1}{2}\frac{3}{2}\frac{1}{9}$  furlongs from  $1\frac{5}{11}$  mile.

Ans. 4 fur. 9 yds.

[TUTOR'S

## MULTIPLICATION.

RULE. Prepare the given numbers (if they require it) by the rules of Reduction: then multiply all the numerators together for the numerator of the product, and all the denominators for the denominator.

- (1) Multiply  $\frac{3}{4}$  by  $\frac{3}{5}$ .  $\frac{3}{4} \times \frac{3}{5} = \frac{9}{20}$ . Ans.
- (2) Multiply  $\frac{7}{4}$  by  $\frac{2}{3}$ .
- (6) Multiply 1 of 3 by 5. (3) Multiply 483 by 135. (7) Multiply 54 by 5.
- (8) Multiply 24 by 2. (4) Multiply 4303 by 183.
- (5) Multiply  $\frac{1}{2}$  by  $\frac{3}{1}$  of  $\frac{5}{4}$ . (9) Multiply  $\frac{3}{4}$  of 9 by  $\frac{7}{8}$ .
- (10) Multiply £3..15..91 is by 1 of 5. Ans. £15..9..112 51 (11) Multiply  $3\frac{15}{44}$  miles by  $\frac{4}{7}$  of  $4\frac{37}{98}$ .

Ans. 8 m. 2 f. 1884 yds. (12) Required the product, in square feet, of 14 ft. 7 in by 8 ft. 9 in. Ans. 12729 sq. ft

### DIVISION.

RULE. Prepare the given numbers (if they require it) by the rules of Reduction ; then invert the divisor, and proceed as in Multiplication."

(1)	Divide $\frac{9}{20}$ by $\frac{3}{5}$ .	
(2)	Divide 14 by 5.	1(7) D' 11 111 111 111
(3)	Divide 672 - by 135.	(7) Divide $\frac{1}{9}\frac{4}{3}\frac{1}{5}$ by $\frac{3}{10}$ of $\frac{101}{2}$ .
(4)	Divide 793524 by 183.	
(5)	Divide 16 by 24.	(8) Divide $9\frac{1}{6}$ by $\frac{1}{2}$ of 7,
(6)	Divide $\frac{9}{16}$ by $4\frac{1}{2}$ .	(9) Divide $\frac{3}{8}$ by $\frac{9}{3}$ of $\frac{3}{4}$ of $\frac{4}{6}$ .
``	16 09 12.	(10) Divide 2 of 16 by 4 of 3.

\* A number *inverted* becomes the reciprocal of that number: which is the quotient arising from dividing unity by the given num ber: thus  $1 \div 7 = \frac{1}{2}$ , the reciprocal of 7;  $1 \div \frac{3}{3} = \frac{5}{3}$ , the reciprocal of  $\frac{3}{4}$ .

 $\dagger \frac{9}{20} \div \frac{3}{5} = \frac{9}{20} \times \frac{5}{3} = \frac{2}{4}$ . Ans.

(11)(12)(13) cwt.; :

(14)£21..1

> RULE Reduct viously the thr

> > 1)

3 cost? (5) men o (6)cost a (7)

make (8)cost a (9)

to ma

how

(1)cwt.  $(1 \cdot$ come 1. (1 mak 1

vard

 $\begin{array}{l} ns. \ 7s. \ 1\frac{1}{2}d \\ r. \ 1s. \ 3d. \\ r. \ \frac{1}{2}\frac{5}{4}, \ r. \ and \\ r. \ \frac{3}{4} \ qrs. \\ qrs. \ 10\frac{2}{3} \ lb. \end{array}$ 

t. 22 gr.

r. 9 yds.

by the rules in the numer-

 3
 by 5.

 y 5.
 y 2.

 9
 by 7.

 9.113
 7.

84 yds. ft. 7 in sq. ft

y the rules plication.\*

of  $\frac{10\frac{1}{2}}{\frac{7}{14}}$ . f 7,  $\frac{3}{4}$  of  $\frac{3}{6}$ .

number : ven núm ocal of 3.

#### ASSISTANT.]

## RULE OF THREE.

(11) Divide  $\pounds_{\frac{12}{2}10}^{\frac{12}{10}}$  by  $\frac{32}{5}$  of  $1\frac{2}{3}$ . Ans.  $\pounds_{3.17.101}^{\frac{12}{5}}$ .

(12) Divide 1s.  $4\frac{1}{2}d.\frac{5}{6}$  Ly  $\frac{2}{3}$  of  $\frac{1.8}{5}$ . Ans. 6d.  $3\frac{6}{72}qrs.$ (13) Divide  $3 qrs. 24\frac{1.5}{16}$  lb. by  $\frac{7}{15}$  of  $1\frac{1}{2}$ , in the fraction of a

(13) Divide  $5qrs. 27_{16}$  to  $5grs. 2r_{16}$  to  $2grs. 2r_{16}$  to

# THE RULE OF THREE.

RULE. Prepare the terms, previous to stating, so that no subsequent Reduction will be necessary: then, having stated the question, as previously directed, *invert* the *dividing term*, and the continued product of the three will be the answer.

(1) If  $\frac{2}{4}$  of a yard cost  $\mathcal{L}_{\frac{5}{8}}^{\frac{5}{8}}$ , what will  $\frac{9}{10}$  of a yard cost? (2) If  $\frac{5}{0}$  yd. cost  $\mathcal{L}_{\frac{3}{3}}^{\frac{9}{3}}$ , what will  $\frac{11}{12}$  yd. cost? Ans. 14s. 8d (3) If  $\frac{3}{4}$  of a yard of lawn cost 7s. 3d. what will  $10\frac{1}{3}$  yards Cost? Ans.  $\mathcal{L}4$ .19..10 $\frac{1}{2}\frac{2}{3}$ .

(4) If  $\frac{7}{8}$  lb. cost  $\frac{3}{4}s$ . how much will  $\frac{3}{9}s$ . buy? Ans.  $1\frac{1}{27}$  lb. (5) If 48 men can build a wall in 244 days, how many

men can do the same in 192 days? (6) If  $\frac{3}{4}$  of a yard of Holland cost  $\pounds_{\frac{1}{3}}^1$  what will 12 $\frac{2}{3}$  ells cost at the same rate? Ans.  $\pounds_{1.0..8\frac{3}{4}\frac{5}{9}}$ .

(7) If  $3\frac{1}{4}$  yards of cloth, that is  $1\frac{1}{5}$  yard wide, be sufficient to make a cloak, how much that is  $\frac{4}{5}$  of a yard wide will make another of the same size? Ans.  $4\frac{7}{6}$  yards.

(8) If 121 yards of cloth cost 15s. 9d. what will 481 yards cost at the same rate? Ans. £3..0.91  $\frac{481}{25}$ .

(9) If  $25\frac{2}{7}s$ , will pay for the carriage of 1 cwt.  $145\frac{1}{4}$  miles, how far may  $6\frac{1}{2}$  cwt. be carried for the same money?

Ans.  $22\frac{9}{26}$  miles.

(10) If  $\frac{9}{10}$  of a cwt. cost £14. 4s. what is the value of  $7\frac{1}{2}$ swt.?

(11) If  $\frac{3}{4}$  lb. of cochineal cost £1..5. what will  $36\frac{7}{16}$  lb come to?

(12) How much in length that is  $7\frac{3}{16}$  inches broad will make a foot square ? Ans.  $20\frac{4}{15}$  inches.

(13) What is the value of 4 pieces of broadcloth, each 27] yards, at 15 s. per yard? Ans. £85..14..3] 4.

 $:: \frac{yd}{16}: \frac{\frac{1}{5}}{\frac{9}{16}} \times \frac{\frac{3}{9}}{\frac{1}{46}} \times \frac{\frac{1}{4}}{\frac{3}{3}} = \frac{\pounds}{4} = 15s. Ans.$ 

(14) If a penny white loaf weigh 7 oz. when a bushel of wheat costs 5s. 6d. what is the bushel worth when a penny white loaf weighs but  $2\frac{1}{2}$  oz.? Ans. 15s. 4d.  $3\frac{1}{5}$  qrs.

(15) What quantity of shalloon that is  $\frac{3}{4}$  of a yard wide will line  $7\frac{1}{2}$  yards of cloth that is  $1\frac{1}{2}$  yard wide? Ans. 15 yards.

(16) Bought  $3\frac{1}{2}$  pieces of silk, each containing  $24\frac{3}{4}$  ells, at 6s.  $0\frac{3}{4}d$ . per ell. How must I sell it per yard to gain £5. by the bargain? Ans. 5s.  $9\frac{1}{4}d$ .  $\frac{3}{4}\frac{6}{2}\frac{3}{4}$ .

# THE DOUBLE RULE OF THREE.

(1) If a carrier receive  $\pounds 2\frac{1}{10}$  for the carriage of 3 *cwt*. 150 miles, how much ought he to receive for the carriage of 7 *cwt*.  $3\frac{1}{2}$  *qrs.*, 50 miles? Ans £1 16 0

(2) If £100. in 12 months gain £51. interest, what principal will gain £3 $\frac{3}{8}$ . in 9 months? Ans. £85..14..31  $\frac{5}{4}$ .

(3) If 9 students spend  $\pounds 10\frac{7}{9}$  in 18 days, how much will 20 students spend in 30 days? Ans.  $\pounds 39..18..4\frac{2}{9}\frac{9}{7}$ .

(4) Two persons earned  $4\frac{5}{8}s$ . for one day's labour: how much would 5 persons earn in  $10\frac{1}{2}$  days, at the same rate?

(5) If £50. in 5 months gain  $\pounds 2_{\frac{37}{144}}^{37}$ . what time will  $\pounds 13_{\frac{1}{2}}^{37}$ . require to gain  $\pounds 1_{\frac{1}{2}}^{12}$ ?

(6) If the carriage of 60 cwt., 20 miles, cost  $\pounds 14\frac{1}{2}$ , what weight can I have carried 30 miles for  $\pounds 5\frac{7}{16}$ ? Ans. 15 cwt.

# DECIMAL FRACTIONS.

IN Decimal Fractions the unit is supposed to be divided into tenths, hundredths, thousandth parts, &c., consequently the denominator is always 10, or 100, or 1000, &c.

In our system of Notation, the figures of a whole number follow each other in a decimal (or tenfold) proportion. Hence, the numerator of a decimal Fraction is written as a whole number, only distinguished by a separating point prefixed to it. Thus 5 for  $\frac{25}{150}$ , 25 for  $\frac{25}{100}$ , 123 for  $\frac{123}{1000}$ .

The denominator is, therefore, not expressed; being always understood to be 1, with as many ciphers affixed as there are places in the numerator.

The different values of figures will be evident in the an-

Fre fracti propo Cip value one c ciphe Α or 5, 0 tion, n'umb have they are ca On &c.; than 36, & and . Pumixed mal b Fir ciphe

Cin

figur

unequ etend

prime

th .9:

and fit four,

BHIST

bushel of n a penny  $3\frac{1}{5}$  qrs. l wide will 15 yards.

of 3 cut. irriage of ..16..9. hat prin-...31 4. uch will 8.429. ur: how rate? ...43 1. ll £134. onths. 1/2., what . 15 cwt.

divided quently

number Hence, whole d to it.

always ere are

10 an-

#### ASHISTAN'T.1

43 ells, at in £5. by d. 369.

DECIMALS

	1	Int	eg	er	8.		Deci	nai	p	art	8.
7	6	5	4	3	2	1	234	5	6	7,	S.c
Millions.	Hundreds of thous.	Tens of thous.	Thousands.	Hundreds.	er Tens.	1 Units.	De o Hundredth parts. 2 Tenth parts of <i>unity</i> .	Ten thous. parts.	Hund. thous. parts.	Willionth parts.	

From this it plainly appears that the figures of the decimal fraction decrease successively from left to right in a tenfold proportion, precisely as those of the whole number.\*

Ciphers on the right of other decimals do not alter their value: for  $2 = \frac{2}{10}$ ,  $20 = \frac{20}{100}$ ,  $200 = \frac{200}{1000}$ , are all equal. But one cipher on the left diminishes the value ten times, two ciphers, one hundred times, &c., for  $02 = \frac{2}{100}$ ,  $002 = \frac{2}{1000}$ , &c.

A vulgar fraction having a denominator compounded of 2, or 5, or of both, when converted into its equivalent decimal fraction, will be finite: that is, will terminate at some certain number of places. All others are *infinite*; and because they have one or more figures continually repeated without end, they are called Circulating Decimals. The repeating figures are called repetends.

One repeating figure is called a single repetend; as 222, &c.; generally written thus,  $\cdot 2'$ ; or thus  $\cdot 2$ . But when more than one repeat, the decimal is a compound repetend; as .36 36, &c., or 142857 142857, &c. These may be written '36', and .142857'; or .36, and .142857.

Pure repetends consist of the repeating figures alone; but mixed repetends have other figures before the circulating decimal begins : as .045', .96`354'.

Finite decimals may be considered as infinite, by making ciphers to recur, which do not alter the value.

Circulating decimals having the same number of repeating figures are called similar repetends, and those which have an unequal number are dissimilar. Similar and conterminous repetends begin and terminate at the same places.

The first, second, third, fourth, &c., places of decimals are called primes, seconds, thirds, fourths, &c., respectively; and decimals are read th 9: 57 57 fifty-seven, and five, seven, of a decimal; that is, fifty soven. and fifty-seven hundredths. 206:043 two hundred and six, and maxer. four, three; that is, 206, and forty-three thousandths

#### DECIMALS.

#### ADDITION.

RULE. Place the numbers so that the decimal points may stand in a perpendicular line: then will units be under units, &c., according to their respective values. Then add as in integers.

- (1) Add  $72 \cdot 5 + 32 \cdot 071 + 2 \cdot 1574 + 371 \cdot 4 + 2 \cdot 75$ .
- (2) Add  $30.07 \pm 2.0071 \pm 59.432 \pm 7.1$ .
- (3) Add 3.5+47.25+927.01+2.0073+1.5.

(4) Add 52.75+47.21+724+31.452+.3075.

- (5) Add  $3275+27\cdot514+1\cdot005+725+7\cdot32$ .
- (6) Add  $27 \cdot 5 + 52 + 3 \cdot 2675 + 5741 + 2720$ .

## SUBTRACTION.

RULE. Place the *subtrahead* under the *minuend* with the decimal points as in Addition; and subtract as in integers.

(1) From 2754 take 2371.	(5) From 571 take 54.72.
(2) From 2.37 take 1.73.	(6) From 625 take 76.91.
	(7) From 23.415 take .3742
(4) From 270.2 take 75.4075.	(8) From 107 take 0007.

## MULTIPLICATION.

RULE. Place the factors, and multiply them as in whole numbers and in the product point off as many decimal places as there are in both factors together. When there are not so many figures in the product, supply the defect with ciphers on the left.

(1)	Multiply 2.071 by 2.27.	(7)	$27.35 \times 7.70011$	
(2)	Multiply 27:15 by 24.3.*	(8)	$57.21 \times .0075.$	
(3)	Multiply 2365 by 2435.	(9)	$\cdot 007 \times \cdot 007.$	
(4)	Multiply 72347 by 23-15.	(10)	$20.15 \times .2705$ .	
(5)	Multiply 17105 by 3257.	(11)	$\cdot 907  imes \cdot 0025.$	
(6)	Multiply 17105 by .0327.	(12)	$\cdot 3409803 \times \cdot 0016218.$	

When the multiplier is 10, 100, 1006, &c., it is only removing the separating point in the multiplicand so many places towards the right as there are ciphers in the multiplier: thus,  $.578 \times 10 = 578$ ,  $.578 \times 1000 = 578$ ,  $.578 \times 1000 = 578$ 

#### CONTRACTED MULTIPLICATION.

RULE. Write the multiplier under the multiplicand in an *inverted* order, the units' figure under that place which is intended to be retained in the product.

\* The 2nd example may be multiplied in two products, first by 3. and that product by 8 for 24. The 3rd, 6th, 7th, and 12th may be constructed in a similar way.

#### 48518

LICICR'S

In tands and s row. Inc arise l rate o inclus Nor sired,

(1) four (1) place (1) gers (1) place

actual

(1' lace

Dr will I stand the p when

Not quotie visor a 2. V divisor extent LIUICR'S

according to

the decimal

ke 54.72. ke 76.91. take 3742 ke 0007.

e are in both the product,

70011. 075. 07. 2705. 025.

016218.

emoving the ds the right  $5.78, \cdot 578 \times$ 

an inverted to be retain-

, first by 3. may be con ASSISTANT.

## DIVISION.

In multiplying, begin with that figure of the multiplicand which stands over the multiplying figure, rejecting all on the right of that; and set down the first figures of all the products in a perpendicular row.

Increase the first figure of each product by carrying to it what would arise from multiplying the two next rejected figures on the right, at the rate of one from 5 to 14 inclusive, two from 15 to 24, three from 25 to 34 inclusive, &c.

NOTE. If perfect accuracy as far as the last decimal figure be desired, it will be eligible to find one figure more in the product than is actually wanted.

(13) Multiply 384.672158 by 3.683, and let there be only four places of decimals in the product.\*

(14) Multiply 3 141592 by 52 7438, retaining only four places of decimals in the product. Aus. 165 6995.

(15) Multiply 238.615 by 8217.5, retaining only the integers in the product. Ans. 1961064.

(16) Multiply 375 13758 by 16 7324, and reserve only one place of decimals; and again, reserving three places.

Ans. 6276.9, and 6276.951.

(17) Multiply 395.3756 by .75642, retaining only four laces of decimals. Ans. 299.0700.

#### DIVISION.

DIVIDE as in integers, and the first figure of the quotient will be of the same value as that figure of the dividend which stands over the units in the first product of the divisor, so that the point must be placed accordingly; ciphers being prefixed, when necessary.

NOTE 1. After proceeding through the dividend, to ascertain if the quotient is correctly *pointed*, observe that the decimal places in the divisor and quotient together must equal in number those of the dividend.

2. When there are *fewer* decimal places in the dividend than in the divisor, *equalize* them by *affixing ciphers*; and the quotient, to *that* extent, will be a whole number.

* Contracted method.	Common method
384.672158	384.672158
386.3	3.683
11540165	11540 16474
2308033	307737 7264
307738	2308032 943
11540	11540164 74
1416.7476	1416.7475 57914

#### DECIMALS.

[TUTOR'S

3. Ciphers may be subjoined to the decimal part of the dividend, or brought down as if they were subjoined, in order to continue the operation to may degree of exactness desired.

(1) Divide 217.75 by 65.	$(7)$ 7382.54 $\div$ 6.4252.
(2) Divide 709 by 2.574.	(8) $\cdot 0851648 \div 423.$
(3) Divide 125 by .1045.	(9) $267 \cdot 15975 \div 13 \cdot 25$ .
(4) Divide 48 by 144.	(10) $72 \cdot 1564 \div \cdot 1347.$
(5) Divide 5.714 by 8275.	(11) $85643 \cdot 825 \div 6 \cdot 321$ .
(6) Divide 715 by 3075.	$(12)$ $1 \div 3.1416.$

To divide by 10, 100, 1000, &c., remove the separating point in the dividend so many places towards the left as there are ciphers in the divisor, and the thing is accomplished.

Thus  $5784 \div 10 = 5784$ ,  $5784 \div 100 = 5784$ ,  $5784 \div 1000 = 5784$ ,  $5784 \div 1000 = 5784$ .

(13)	$3719 \div 10.$	(15)	$130.7 \div 1000$
(14)	$3.74 \div 100.$	(16)	34·012 ÷ 10000

### CONTRACTED DIVISION.

Ascertain the value of the first quotient figure, from which it will be known what number of figures in the quotient will serve the purpose required. Use that number of the figures in the divisor, (rejecting the others on the right,) and a sufficient number of the dividend, to find the first figure of the quotient; make each remainder a new dividual, and for each succeeding figure reject another from the divisor: but observe to carry to each product from the rejected figures, as in Contracted Multiplication.

Note. When there are *fewer* figures in the divisor than the number wanted in the quotient, proceed by the common rule till those in the divisor are just as many as remain to be found in the quotient, and then use the contraction.

(17) Divide 70.23 by 7.9863, to three places of decimals.
(18) Divide 721.17562 by 2.257432, to the extent of only three places of decimals in the quotient.

(19) Divide 25.1367 by 217.35, to the fourth decimal.

* Contracted Method.	Common Method.		
7.9863)70.230(8.793	7.99:3)70:2300(8:793		
63890	638.^74		
6340	633960		
5590	559041		
750 719 31	749190 718767		
24 7	30 4230 23 9589 6 4641		

k num 2. mak cons subj

vul

(

tion •0

3.

3.5

In mak on cont

Ne add In figur

tinu is d li tion

dene

ASSISTANT.]

as dividend, or

 $\begin{array}{l}
\div 6.4252, \\
\div 423, \\
\div 13.25, \\
\div .1347, \\
\div 6.321, \\
\end{array}$ 

÷ 3.1416.

g point in the ciphers in the

1000 = 5.784

10001 10000......

hich it will be the purpose (rejecting the ad, to find the dividual, and but observe in Contracted

in the number 1 those in the tient, and then

f decimals.\* tent of only

lecimal.

#### CIRCULATING DECIMALS.

(20) Divide 51.47542 by .123415, to the second decimal.
(21) Divide 27104 by .3712, the integral quotient only.

#### CIRCULATING DECIMALS.

## To reduce a circulate to a vulgar fraction.

RULE. 1. For a pure repetend, make the circulating figures the numerator, to as many nines for the denominator.

2. For a mixed repetend, subtract the finite part from the whole, and make the difference the numerator; the denominator to which will consist of as many nines as there are repetends, with as many ciphers subjoined as there are finite figures.

#### EXAMPLES.

(1) Reduce 1', 3', 9', 01', and 142857' to their equivalent vulgar fractions.

 $\begin{array}{c} 1' = \frac{1}{9}; \ 3' = \frac{3}{9} = \frac{1}{3}; \ 9' = \frac{9}{9} = 1; \ 01' = \frac{1}{99}; \ \text{and} \ 142857' \\ = \frac{1}{9} \frac{4}{9} \frac{2}{9} \frac{3}{9} \frac{7}{9} = \frac{1}{15} \frac{5}{11} \frac{7}{11} \frac{3}{10} \frac{5}{37} = \frac{4}{3} \frac{6}{307} = \frac{1}{7}. \end{array}$ 

(2) Reduce '03'45' and 3.5'126' to equivalent vulgar fractions

In ADDITION and SUBTRACTION of Circulating Decimals, make them *similar* and *conterminous*, and carry to the figures on the right whatever would arise from the *repetends being continued*.

Note In all cases, when the repetend is 9, make it a cipher, and add 1 to the next figure: for 999, &c. = 1.

In MULTIPLICATION, carry to the product of the right hand figure what would arise from the product of the repetends continued; and in finding the sum of the products, observe what is directed in ADDITION.

In DIVISION, it is only necessary to observe that the operation may be carried on with the *repeating* figures of the dividend, to any extent required.

NOTE. When the Multiplier or the Divisor is a circulate, the most convenient method is, to change it into a common fraction.

#### DECIMALS.

[TUTOR'S

I tor:

To

F the den

of 1

mil

## EXAMPLES.

(3) What is the sum of 25. 142857', 10 3'90', 12.035', and 4.02 567'?

25.`142857' 10.3`90'	Similar. 25``142857' 1C`3`909090'	-	ar and conterminous. 25.14`285714' 10.39`090909'
12·035' 4·02`567'	 12.03`555555' 4.02`567567'		12.03`555555'
. 0.0 001	 1 02 301301		4·02`567567' 51·59`499746'

(4) What is the difference between 567.367' and 55.0.9729'? Also, between 57, and 49.8.53'?

	= 567.3`6736		57.
55.0.9729	= 55.0.9729	997299729 <b>′</b>	49.8.53
differen	e 512·2`700	6763 <b>7</b> 3943′ dif	f. 7·1·46'

) Multiply 65.316' by .753.	(6) Multiply 13.45' by 3.36'.
65.316/	$3^{1}36' = 3\frac{3}{9}\frac{6}{9} = 3\frac{4}{11} = \frac{37}{11}$
.753	13.45
195950	37
3265833/	94`18'
457216661	403`6 <b>3′</b>
product 49.183450	11)497.'81'
, ,	product 45.256198, &c.

(7) Divide  $150.9^{\circ}045'$  by 33. (8) Divide 17.8054' by 3.6'. 3) $150.9^{\circ}045'$ 11) $50.3^{\circ}015'$ 4.5 $^{\circ}728637'$  quotient. (8) Divide 17.8054' by 3.6'.  $3.6' = 3\frac{6}{9} = 3\frac{2}{3} = \frac{1}{3}$ .  $17.8054' \times \frac{3}{77} = \frac{53.4163'}{11}$ 

(9) What are the equivalents to  $\cdot 004'354'$  and  $65 \cdot 00063'648'?$ Ans.  $\frac{29}{6660}$ , and  $65_{740000}$ .

(10) What is the sum of  $57 \cdot 575 + 3 \cdot 59 \cdot 163' + 210 \cdot 16' + 06' \cdot 3759'$ ? Ans.  $271 \cdot 397' \cdot 057674235892'$ .

(11) Required the difference between 36.30.4520 and 47.280.43'. Ans. 10.975.9135982268'.

(12) Multiply 4. 428571' by 347; and 17.0.54' by 6. 148'. Ans. 1536. 714285'; and 104.85. 387205'.

(13) Divide 1536. 714285' by 347; and 104.85'387205' by 6. 148'. Ans 4. 428571'; and 17.0.54'.

(5

12.035', and

nous. 55 0 97291 7. 9.8.53/ 7.1.46' 5' by 3.136'.  $3_{11}^4 = 3_{11}^7$ 13.45/ 37 94'18' 03`63' 97.'81' 56198, &c. ' by 3.6'. 3 = 4. 53.4163/

. 11

00063<sup>6</sup>48<sup>?</sup> -210<sup>16</sup>+ 235892<sup>.</sup> 4520 and 982258<sup>.</sup> by 6<sup>.</sup>148<sup>.</sup> 387205<sup>.</sup> 387205<sup>.</sup> by 17<sup>.054<sup>.</sup></sup>

### REDUCTION.

ABBISTAN T.]

### **REDUCTION.**

### To reduce a Vulgar Fraction to a Decimal.

RULE. Add ciphers to the numerator, and divide by the denomica tor; the quotient will be the decimal fraction required.

(1) Reduce  $\frac{1}{4}$ ,  $\frac{1}{4}$ ,  $\frac{3}{4}$ , and  $\frac{3}{4}$ , to decimals.

	25, 5, 75, and 375.
(2) Reduce $\frac{1}{3}$ , $\frac{1}{5}$ , $\frac{1}{7}$ , and $\frac{1}{9}$ , to decim	nals.
Ans. 3',	2, . 142857', and .1'.
(3) Reduce $\frac{5}{2\pi}$ to a decimal.	Ans. 1'923076'.
(4) Reduce $\frac{11}{14}$ of $\frac{19}{18}$ to a decimal.	Ans. '6'043956'.

### To reduce a given quantity to the Decimal of any denomination required.

RULE. Reduce those of the lowest denomination to decimal parts of the next superior, on the left of which place the given quantity of that denomination; reduce this to the next, and proceed as before, till it is of the denomination required.

(5) Reduce  $5s.^*$  9s. and 16s. to the decimals of a pound. Ans.  $\pounds \cdot 25$ ,  $\pounds \cdot 45$ , and  $\pounds \cdot 8$ .

- (6) Reduce 8s. 4d. to the decimal of a £. Ans. £.416'.
- (7) Reduce 16s.  $7\frac{3}{4}d$ . to the decimal of a  $\pounds$ .
- (8) Reduce 19s.  $5\frac{1}{2}d$ . to the decimal of a  $\pounds$ .

Ans. £

(9) Reduce 12 grains to the decimal of a lb. tr

Ans. 1b. ·C

(10) Reduce  $12\frac{1}{6}\frac{3}{4}$  drams to the decimal of a lb. avora

Ans. 1b. 047668--.

(11) Reduce 2 qrs.  $14\frac{1}{4}$  lb. to the decimal of a civt.

Ans. cwt. 62723+.

(12) Reduce 2 furlongs,  $161\frac{1}{2}$  yards to the decimal of a mile. Ans.  $341761^{\circ}36'$  mile.

(13) Reduce  $5\frac{14}{15}$  pints to the decimal of a gallon. Ans. 7416' gal.

(14) Reduce  $4\frac{1}{2}$  gallons of wine to the decimal of a hogshead. Ans. 0`714285'.

> \* 20)5.00s. £.25 Ans.

 $\begin{array}{c} \dagger & 4 \\ 12 \\ \hline 7.75 \ d. \\ 20 \\ \hline 16^{\circ} 64583' \ s. \\ \hline \pounds \cdot 8322916' \ Ans. \end{array}$ 

### DECIMALS.

### [TUTOR'S

S

Lo

Pe In

(15) Required the mixed decimal number equivalent to  $\pounds 3.9.1\frac{163}{1220}d$ . Ans.  $\pounds 3.45471$ .

(16) Express 7 weeks, 3 days, in the decimal of a year. Ans. yr. 142465+.

# To find the proper value of a Decimal Fraction of any Integer.

RUL: Multiply the given decimal by the proper number to reduce it to the next inferior denomination, pointing off the given number of decimals in the product; reduce these to the next, and so on to the lowest; and the whole numbers on the left (being collected together) will be the value required.

A decimal of a  $\mathcal{L}$  may be thus valued by inspection. Double the tenths for shillings, and call the number in the second and third, farthings, abating one above 12, and two above 37. But if the second is 5, or upwards, call the 5 one shilling, and reckon only the excess above five with the third.

By reversing these directions, any given sum in shillings, &c., may be expressed in the decimal of a  $\pounds$ .—Thus, half the shillings are tenths. and an odd shilling, 5 hundredths; the rest (in farthings) add into the second and third places, increasi  $\therefore$  one above 11 farthings, and two above 36.

(17) What is the value of  $\cdot 8322916$  of a £.\*

(18) Reduce £.740596 to its proper value.

Ans. 14s. 9d..2.97216 grs.

(19) What is the value of .082084 of a *lb*. troy ? Ans. 19 *dwts*. 16.80384 grains.

(20) What is the value of 4909375 *lb*. avoirdupois? Ans. 7 oz. 13.68 drams.

(21) What is the value of  $\pounds$  19895?

Ans. 3s. 11d..2.992 grs.

(22) What is the value of .625 of a cwt.? Ans. 2 grs. 14 lb.

(23) What is the value of .071428 of a hogshead of wine ! Ans. 4 gal. 1.999856 qts

(24) What is the value of .0625 of a barrel of beer? Ans. 2 gallons, 1 quart

(25) What is the value of .142465 of a year? Ans. 51.999725 days

* £. ·8322916 20		By	insp	ection.
s. 16.6458320		£.	-	s. d.
12		•8	=	160
d. 7.749984		.035	.=	0.7
4	s. a.	·832	=	167
qrs. 2.999936 Ans.	1674 ver	y nearly.		

equivalent to £3·45471. of a year. 142465-[-.

### any Integer.

nber to reduce en number of on to the lowtogether) will

Double the nd third, farhe second is 5, excess above

ugs, &c., may igs are tenths. ) add into the ings, and two

7216 qrs. 7? 4 grains. pois ? 68 drams.

992 qrs. 2 qrs. 14 lk. ad of wine ! 9856 qts beer ? 1 quart

25 days

n. d. 3..0

..74

### ASSISTANT.]

DECIMALS.

109

		Arecu	mai 1	luces of Co	in, Weight, a	which we want the same data is not set of the same data is a same data in the same data is a s	
	TAI	BLE I.		-	0/10=	Grains.	Decimals
STE.	RLIN	G Mo	DNEY.	3qrs.		12	.025
		e Inte		2	·041666	11	022916
21		e inte	ger.	1	·020833	10	·020833
s.	dec	. S.	dec.	TAB	LE III.	9	.01875
19	.95	9	.45		WEIGHT.	8	·016666
18	.9	8	•4			7	·014583
17	.85	17	.35		e Integer.	6 ·	·0125
16	.8	6	•3		s the same	5	·010416
15	.75	5	.25	as Pence	in Table 11.	4	·008333
14	.7	4	.2		1	3	.00625
13	.65	3	.15	diets.	Decimals.	2	.004166
12	.6	2	.1	10	.041666	1	·002083
11	05		.05	9	.0375		
10	.5			8	.033333		LE IV.
	1			7	.029166	Avoir. WEIGH	
6	d.	.025		6	.025	1 cwt. th	ie Integer
5			5	.020833			
4		·016		4	.016666	Qrs.	Decimals
3		.012		3	.0125	3	.75
2		-008		2	.008333	$\frac{2}{1}$	•5
ĩ		.004		1	.004166	1	.25
		001					
3	grs.	·003	195	12 gr.	·002033	14 <i>lbs</i> .	$\cdot 125$
2	· 1		0833	11	·001910	13	$\cdot 116071$
ĩ			0416	10	.001736	12	$\cdot 107143$
	1	100.	0410	9	.001562	11	$\cdot 098214$
	TAB	LE II.		8	.001382	10	·089286
E	NG. (	COIN	18	7	001389	9	·080357
		as. 1			001215	8	$\cdot 071428$
		ntegei		5	0001542	7	·0625
		nego		4	000694	6	053571
ence				3	·000521	5	·044643
Inch	es.	Decin	nals.	2	000321	4	·035714
6		•5		ĩ	000347	3	$\cdot 026786$
5	1.1	•416				2	.017857
4		·3333	333		e Integer.	1	·008928
. 3	5.	.25		Penny-we	eights the	1	
2	2	.1666		same a	s Shillings	8 oz.	·004464
-1.	17 1 L	·083:	333	in the f	irst Table.	7	·003906

.,

DECIMALS.

[TUTOR'S

6

	1)					
	Decimal	Tables of	Coin, Weigh	it, and M	easure.	
60.	z. 003348	8 008	- 31746	0	1	
5	.002790	) 70	.27777	7	pts	05952
4	.00223:	60	$\cdot 23809$	5 2		03968
* 3	001674	50	.19841	2   1	•0	01984
2	001116		15873	0		
1	.000558	30	.11904	7	TABLE	V11.
3	.000418	20	.07936	5 1	MEASUR	ES.
	.000279	10	.03968;	2   13		
1	.000139	9	·035714	t   1		Dry.
		8	.031746		Gal. 1	
T.	ABLE V.	7	027777	r tl	ie Integ	ger.
AVOIR	WEIGHT.	6	.023809			
		1 3	019841	Pts.	Dec.	Bush.
	he Integer.	4	015873		•5	4
Ounces	. Decimals.	- 3	.011904	3	·375	3
8	.5	2	.007936		$\cdot 25$	2
7	.4375	1	003968	1	.125	1
6	.375	Ante	1.001001		.09375	3 p.
5	.3125	4 pts 3		1 +	.0625	2
4	.25	2	.001488	I	03125	ĩ
3	1875		.000992	1		-
2	125	1	.000496	Decim	als. Qr	. Pks.
1	.0625			- 0234	375	3
	1 00.00	1 Hog	shead the	·0156		2
Cdr.	.03125	1		·0078	125	1
7	0.027343	In	iteger.	.0058	50	0
6	023437			. 0039		3 pts.
5	.019531	Gallons.	Decimals.	0019	52	2
4	015625	30	.476190	0019	55	1 1
3	.011718	20	.317460			
2	.007812	10	.158730		BLE VIII	
1	·003906	9	142857	LONG	Measu	RE.
[		8	$\cdot 126984$	1 Mile	the Inte	eger.
TAB	LE VI.	7	111111		1	
IQUID ]	MEASURE.	6	.095238	Yards.	Decin	nals.
	e Integer,	5	079365	1000	.5681	82
	-	4	.063492	900	.5113	
allons.	Decimals.	3	.047619	800	.4545	
100	306325	2	.031746	700	.3977	
90	.357142	1	015873	600	·3409	00

104

Ģ

1 Y

Mon Pe

[TUTOR'S ASSIS	FANT.]	DE	CIMALS		1
	Decimal 'I	ables of C	oin, Weight,	and Measu	ure.
500	yd.   ·284091	80 d.	219178	1	and the second sec
005952 1 400	·227272	70	.191781		BLĖ X.
003968 300	.170454	60	.164383		MEASURE
001984 200	.113636	50	$\cdot 136986$	1 Yard	the Integer.
100	.056818	40	.109589		he same as
vп. 90	•051136	30	.082192	11	able IV.
RES. 80	•045454	20	.054794	Nails.	Decimals.
Dry. 70	.039773	10	0.027397	3	.1875
0. 00	.034091	9	$\cdot 024657$	2	.125
	·028409	8	021918	1	.0625
ger. 40	.022727	7	·019178		
30	.017045	6	.016438		BLE XI.
Bush 20	.011364	5	·013698		WEIGHT.
4 10	· <b>0</b> 05682	4	·010959	A Foth.	the Integer.
3 9	.005114	3	.008219	Hund.	Decimals.
2 8	.004545	2	.005479	10	·512820
1 7	.003977	1	.002739	9	•461538
3 p. 6	.003409	1 Day t	he Integer.	8	410256
2 5	.002841	12/1rs.		7	.358974
1 4	.002273	11	. 458333	6	307692
3	.001704	10	•416666	5	256410
r. Pks. 2	.001136	9	.375	4	205128
3 1	.000568	8	•333333	3	153846
$\frac{2}{2f}$	t. 0003787	7	291666	2	102564
	.0001894	6	-251000	1	051282
B pts. 6 i		5	·208333	-	
3	.0000474	4	166666	3qrs	·038461
. 2	.0000315	3	125	. 2	.025641
	·0000158	2	.083333	L	·012820
	1 0000100	ĩ	.041666	14 lbs.	
T.	BLE IX.	30 m.	strange water to do a sume	13	$\cdot 0059523$
RE.		$\frac{30 m}{20}$	020833	12.	·0054945
ger.	TIME.	10	·013888	11	·0050366
1 Year	the Integer.	9	·006944	10	·0045787
als. March	the same as	8	·00625	9	$\cdot 0041208$
Day Down	in Table II.	7	·005555	8	.0036630
04	in rabio it.	6	·004861	7	.0032051
5 Days.	Decimals.	5	.004166	6	$\cdot 0027472$
200	·821918	-	003472	5	$\cdot 0022893$
9 200	•547945	4	·002777	4	0018315
100	273973	32	.002083	3	$\cdot 0013736$
	246575		·001388	2	$\cdot 0009157$
	1 4120010		·000694	1	.0004578

ñ

F2

#### DECIMALS.

### THE RULE OF THREE.

(1) If 261 yords cost £3..16..3. what will 321 yds. cost ?\*

(2) If  $7\frac{3}{4}$  yards of cloth cost £2..12..9. what will 1404 yards of the same cost? Ans. £47..16..31.

(3) If a chest of sugar, weighing 7 cwt. 2 grs. 14 lb. cest £36..12..9. what will 2 cwt. 1 qr. 21 lb. of the same cost? Ans. £11..14..23.

(4) What will  $326\frac{1}{4}$  lb. of coffee be worth when  $1\frac{1}{2}$  lb. is sold for 3s. 6d.? Ans. £38.1..3.

(5) What is the value of 19 oz. 3 dwts. 5 grs. of gold, at £2..19. per oz.? Ans. £56..10..5..2.3 grs.

(6) What is the charge for  $827\frac{3}{4}$  yards of painting, at  $10\frac{1}{4}d$ . per yard? Ans. £36..4..3..1.5 grs.

(7) If I lent my friend £34. for  $\frac{5}{8}$  of a year, how much ought he to lend me for  $\frac{5}{12}$  of a year? - Ans. £51.

(8) If  $\frac{3}{4}$  of a yard of cloth, that is  $2\frac{1}{4}$  yards broad, make a garment, how much of  $\frac{4}{5}$  of a yard wide will make a similar one? Ans. 2 yds. 1.75 nail.

(9) If 1 oz. of silver is worth 5s. 6d. what is the price of a tankard that weighs 1 lb. 10 oz. 10 dwts. 4 grs.?

Ans. £6..3..9..2.2 grs.

(10) What is the value of 15 cwt. 1 qr. 19 lb. of cotton, at 15d. per lb.? Ans. £107..18..9.

(11) If 1 cwt. of currants cost £2..9..6. what will 45 cwt. grs. 14 lb. cost at the same rate ? Ans. £113..10..93.

(12) Bought 6 chests of sugar, each 6 cwt. 3 qrs. at £2..16. per cwt. What do they come to? Ans. £113..8.

(13) Bought a tankard for £10..12. at the rate of 5s. 4d. per oz. What was the weight? Ans. 39 oz. 15 dwts.

(14) Gave £187..3..3. for 25 cwt. 3 grs. 14 lb. of coffee: at what rate did I buy it per lb.? Ans. 1.5. 31d

(15) Bought 29 lb. 4 oz. of snuff for £10..11..3. What is the value of 3 lb.? Ans. £1..1..8.

(16) If I give 1s. 1d. for  $3\frac{1}{2}$  lb. of rags, what will be the value of 1 cwt.? Ans. £1..14..8.

> yds.£. yds. £. As 26.5 : 3.8125 :: 32.25 : 4.63974 32.25 26.5)122.953125(4.63974 -£4 12..91. Ans.

106

Ís . of

of m of

the

mo oft

the tri

T ali ł exc

eig

wil

sol

= 4

an E

4.5

[TUTOR'S

1 yds. cost ?\*

hat will 140

rs. 14 lb. cest

when 11 lb. is

rs. of gold, at

nting, at 104d.

ar, how much

s broad, make

nake a similar 5. 1·75 *nail*.

s the price of

o. of cotton, at

at will  $45 \ cwt$ . 13..10..9 $\frac{3}{4}$ . ars. at £2..16.

..9..2.2 grs.

107..18..9.

s. £113..8.

z. 15 dwts. lb. of coffee:

1s. 1s. 31d

s. £1..1..8.

£1..14..8.

Ans.

...3. What is

at will be the

ate of 5s. 4d.

s. ?

247..16..33.

same cost?

211..14..23.

. £38.1..3.

..5..2·3 grs.

...3..1.5 grs.

Ans. £51.

ASSISTANT.]

### EXCHANGE

### EXCHANGE

is the act of bartering the money of one place for that of another, by means of a written instrument called a *Bill of Exchange*.

The operations in this Rule consist in finding the quantity of one sort of money that will be equal to a given sum of the other, according to the existing Course of Exchange.

Par of Exchange signifies the equality in the intrinsic value of two sums of money of different countries, and shows how much of the one is worth a constant sum (or piece of coin) of the other.

Course of Exchange is the comparative value between the money of two different countries at any particular time, which often fluctuates above or below the *Par*.

Agio is a difference of so much per cent. in the value of the Bank-money and the Current-money of some foreign countries, the former being of superior value.

### To change Foreign Money into British Sterling Money, or Sterling into Foreign, according to a given Course of Exchange.

RULE. As the quantity of FC eign mentioned in the given course of exchange is to the quantity of Sterling, so is any other sum of the Foreign to he corresponding value in Sterling money.

And by mutually changing the words Foreign and Sterling, the Rule will serve for changing Sterling into Foreign money.

### I. FRANCE.

Accounts are kept at Paris, Lyons, and Rouen, in livres, sols, and deniers, and exchange is made by the écu, or crown = 4s. 6d. at par.

TABLE. 12 deniers make 1 sol.

20 sols . . . 1 livre. 3 livres . . 1 écu, or crown.

(1) How many crowns must be paid at Paris to receive **r** London £180. exchange at 4s. 6d. per crown ?\*

s. d. cr. £. As 4..6:1::100 2  $\frac{2}{9}$  sixp.  $9)\overline{7200}$  sixp.  $\overline{800}$  crowns. Ans

### EXCHANGE.

(2) How mucr. sering must be paid in London, to receive in Paris 758 crowns, exchange at 4s. 8d. per crown?

Ans. £176..17..4.

TUTOR'S

(3) A merchant in London remits £176..17..4. to his correspondent at Paris : what is the value in French crowns, at 4s. 8d. per crown? Ans. 758 crowns.

(4) Change 725 crowns, 17 sols, 7 deniers, at 4s. 6<sup>1</sup>/<sub>4</sub>a. per erown, into sterling money. Ans. £164..14..01.  $\frac{3}{246}$ .

(5) Change £164..14..01. sterling into French crowns, exchange at 4s.  $6\frac{1}{2}d$ . per crown.

Ans. 725 crowns, 17 sols, 741 deniers.

### II. SPAIN.

Accounts are kept at Madrid, Cadiz, and Seville, in dollars, rials, and maravedies, and exchange is made by the piece of eight = 4s. 6d. at par.

34 maravedies make 1 rial. TABLE.

8 rials . . . 1 piastre, or piece of eight. 10 rials . . . . 1 dollar.

(6) A merchant at Cadiz remits to London 2547 pieces of eight, at 4s. 8d. per piece : how much sterling is the sum ?

Ans. £594..6. (7) How many pieces of eight, at 4s. 8d. each, will answer a bill of £594..6. sterling? Ans. 2547.

(8) If I pay here a bill of £2500., for what Spanish money may I draw my bill at Madrid, exchange at 4s.  $9\frac{1}{2}d$ . per piece of eight? Ans. 10434 pieces of eight, 6 rials,  $8\frac{2}{23}$  mar.

### III. ITALY.

Accounts are kept at Genoa and Leghorn in livres, sols, and deniers, and exchange is made by the piece of eight or dollar=4s. 6d. at par.

TABLE. 12 deniers make 1 sol.

20 sols . . . 1 livre.

5 livres . . 1 piece of eight at Genoa.

6 livres . . 1 piece of eight at Leghorn.

N. B. The exchange at Florence is by ducatoons ; at Venice by ducats.

TABLE. 6 solidi make 1 gross.

24 gross . . 1 ducat.

(9) How much sterling money may a person receive in London, if he pay in Genoa 976 dollars at 4s. 5d. per dollar? Ans. £215..10 8

108

2

po mi

lin

wł

ch

bu

85

ch

pe

18

to

to

V

ASSISTANT.]

n, to receive own ?
176..17..4.
4. to his corh crowns, at 58 crowns.
4s. 6<sup>1</sup>/<sub>2</sub>a. per ..0<sup>1</sup>/<sub>4</sub>. <sup>3</sup>/<sub>3</sub>/<sub>6</sub><sup>8</sup>. crowns, ex-

deniers.

e, in dollars, the piece of

ce of eight.

7 pieces of the sum ?  $\pounds 594..6.$ will answer as. 2547. nish money 2. per piece  $8\frac{2}{2}\frac{9}{3}$  mar.

ivres, sols, of eight or

enoa. eghorn. at Venice

eceive in er dollar? ..10 8 EXCHANGE.

(10) A factor has sold goods at Florence for 250 ducatoons, at 4s. 6d. each: what is the value in pounds sterling? Ans. £56..5.

(11) If 275 ducats, at 4s. 5d. each, be remitted from Venice to London, what is the value in pounds sterling?

Ans. £60..14..7.

(12) A traveller would exchange  $\pounds 60..14..7$ . sterling for Venice ducats, at 4s. 5d. each; how many must he receive? Ans. 275.

### IV. PORTUGAL.

Accounts are kept at Oporto and Lisbon, in reas, and exchange is made by the milrea = 6s.  $8\frac{1}{2}d$ . at par.

TABLE. 1000 reas make 1 milrea.

(13) A gentleman being desirous to remit to his correspondent in London 2750 milreas, exchange at 6s. 5d. per. milrea, for how much sterling will he be creditor in London? Ans. £882..5..10.

(14) A merchant at Oporto remits to London 4366 milreas, 183 reas, at 5s.  $5\frac{5}{8}d$ . exchange per milrea : how much sterting must be paid in London for this remittance?

Ans. £1193..17..6..3.0375 grs.

(15) If I pay a bill in London of £1193..17..6..3.0375 qrs what must I draw for on my correspondent in Lisbon, exchange at 5s.  $5\frac{5}{8}d$ . per milrea? Ans. 4366 milreas, 183 reas

### V. HOLLAND, FLANDERS, AND GERMANY.

At Antwerp, Amsterdam, Brussels, Rotterdam, and Hamburgh, some accounts are kept in pounds, shillings, and pence, as in England; others in guilders, stivers, and pennings: exchange with London, at from 33s. to 36s. or 38s. Flemish per pound sterling.

TABLE. 8 pennings make ..... 1 groat.

2 groats, or 16 pennings 1 stiver.

20 stivers ..... 1 guilder, or florin.

ALSO, 12 groats, or six stivers, make 1 schelling.

20 schellings, or 6 guilders .... 1 pound.

(16) Remitted from London to Amsterdam a bill of £754..10. sterling: how many pounds Flemish is the sum, the exchange at 33s. 6d. Flemish per pound sterling?

Ans. £1263..15..9. Flemish.

(17) A merchant in Rotterdam remits  $\pounds 1263..15..9$ . Flemish to be paid in London; how much sterling money mean

## CONJOINED PROPORTION.

TUTOR'S

t

q

a

a

1

I

h

ŋ

li

I

s

le

d

1 Ί

22 a

draw for, the exchange being at 33s. 6d. Flemish per pound

(18) If I pay in London £852..12..6. sterling, how many guilders must I draw for at Amsterdam, exchange at 34 schellings, 41 groats Flemish per pound sterling ?

Ans. 8792 guild. 13 stiv. 1 gr. 61 pennings. (19) What must I draw for in London, if I pay in Amsterdam 8792 guild. 13 stiv. 141 pennings, exchange at 34 schellings, 41 groats per pound sterling?

Ans. £852..12..6. To convert Bank Money into Currency ; and the contrary.

As 100 : 100 plus the agio : : the Bank-money : the Currency.

As 100 plus the agio : 100 : : the Currency : the Bankmoney.

(20) Change 794 guilders, 15 stivers, Current money, into Bank florins, agio 43 per cent.

Ans. 761 guilders, 8 stivers, 11735 pennings. (21) Change 761 guilders, 9 stivers Bank, into Current money, agio 43 per cent.

Ans. 794 guilders, 15 stivers, 47 pennings.

### VI. IRELAND.

The par of exchange, long established with Ireland, was £108..6..8. Irish = £100. English. That is, £1..1..8. Irish - £1. English; or 13d. Irish = 1s. English.

But the English and Irish currency are now assimilated. (22) A gentleman remitted to Ireland £575..15. sterling : what would be receive there, the exchange being at  $\pounds 10$ . per

(23) What would be paid in London for a remittance of . £633..6..6. Irish, exchange at £10. per cent.? Ans. £575..15.

# CONJOINED PROPORTION; OR COMPOUND ARBI, TRATION OF EXCHANGE

Is the method of comparing the coins, weights, or measures of one country with those of another, when the comparison is to be made through the medium of those of other countries.

Case 1. When it is required to find how many of the first sort mentioned are equal to a given quantity of the last

ASSISTANT.]

sh per pound £754..10. g, how many e at 34 schel-

y in Amsterat 34 schel-352..12..6.

contrary.

v : the Cur-

the Bank-

noney, into

to Current

connings.

land, was 1..8. Irish

nilated. stering: £10. per 3..6..6. ttance of £575..15.

ARBI,

neasuros nparison Duntries. the *first*  RULE. Place the terms alternately, antecedents and consequents, in two columns, left and right. The last term, being an antecedent, will stand on the left.

Divide the product of the antecedents by the product of the consequents for the answer.

PROOF. By as many single statements as the question requires.

(1) If 20 *lb*. at London make 23 *lb*. at Antwerp, and 155 *lb* at Antwerp make 180 *lb*. at Leghorn, how many *lb*. at London are equal to 72 *lb*. at Leghorn ?\*

(2) If 12 *lb.* at London make 10 *lb.* at Amsterdam, and 100 *lb.* at Amsterdam 120 *lb.* at Toulouse, how many *lb.* at London are equal to 40 *lb.* at Toulouse? Ans. 40 *lb.* 

(3) If 140 braces at Venice be equal to 156 braces at Leghorn, and 7 braces at Leghorn equal to 4 ells English, how many braces at Venice are equal to 16 ells English?

Ans. 2535.

(4) If 40 *lb*. at London make 36 *lb*. at Amsterdam, and 90 *lb*. at Amsterdam make 116 *lb*. at Dantzic, how many *lb*. at London are equal to 130 *lb*. at Dantzic? Ans.  $112_{23}$ .

Case 2. When it is required to find how many of the last sort mentioned are equal to a given quantity of the first.

RULE. Place the *antecedent* and *consequent* terms as before; but the last term, being a *consequent*, will stand on the right. Divide the pro duct of the consequents by that of the antecedents.

(5) If 12 *lb*. at London make 10 *lb*. at Amsterdam, and 100 *lb*. at Amsterdam 120 *lb*. at Toulouse, how many *lb*. at Toulouse are equal to 40 *lb*. at London? Ans. 40 *lb*.

(6) If 40 *lb*. at London make 36 *lb*. at Amsterdam, and 90 *lb*. at Amsterdam 116 *lb*. at Dantzic, how many *lb*. at Dantzic are equal to 122 *lb*. at London? Ans.=14113

> \* Antecedents. Consequents. 20 lb. London = 23 lb. Antwerp. 155 lb. Antwerp = 160 lb. Leghorn. 72 lb. Leghorn = how many London? 1 8  $\frac{20 \times 155 \times 52}{23 \times 159} = \frac{1240}{23} = 53\frac{21}{23}$  lb. Ans. 9 1

### EVOLUTION.

### [TJTOR'S

### INVOLUTION

Is the method of finding the powers of numbers.

Any number is the first power of itself, and the root of all its powers: and when the root is multiplied by itself the product is the second power; the second multiplied by the first produces the third, &c.

The second power is commonly called the square, and the third power the cube.

Numbers called indices, or exponents, are placed on the right, a little above the line, to denote the respective powers. Thus, 32 signifies the square, or second power of 3; the small figure <sup>2</sup> being the index, or exponent.

## To involve a number to any power.

Multiply the given number (or root) by itself continually one RULE. time less than the index of the power: that is, once for the second, twice

Observe, that any two or more powers multiplied together will produce a power whose index is the sum of their indices. Thus, the seventh power is the product of the fourth and the third, because the sum of the indices 4+5=7.

### ILLUSTRATIONS.

The first power of 3 is 3<sup>1</sup>, or 3. The second power of 5 is  $5^2 = 5 \times 5 = 25.$ The third power of 4 is  $4^{3} = 4 \times 4 \times 4 = 64.$ The fourth power of  $\cdot 05$  is  $\cdot 05^4 = \cdot 05 \times \cdot 05 \times \cdot 05 \times \cdot 05 =$ ·00000625.

The fifth power of  $\frac{2}{3}$  is  $\frac{2}{3} = \frac{2}{3} \times \frac{2}{3} \times \frac{2}{3} \times \frac{2}{3} \times \frac{2}{3} = \frac{32}{248}$ . (1) Required the squares of 43, 2174, 4.3, and 2174.

Ans. 1849, 4726276, 1849, and 04726276

(2) Cube 111, 1.11,  $\frac{3}{4}$ , and  $2\frac{5}{8}$ .

Ans. 1367631, 1.367631, 27, and 1845 (3) Involve 9 to the ninth power. Ans. 387420489

(4) Find the third, fifth, and eighth powers (without fin-1ing the fourth, sixth, and seventh) of 1.7.

Ans. 4.913, 14 19857, and 69 75757441 (5) What are the third and sixth powers of 05?

Ans. 000125, and 000000015625

### EVOLUTION

Is the method of extracting the roots of powers. It is therefore the reverse of Involution; by referring to which it will

### ASI

be itse mu of

N wh roo may

H ter 2 tain ing 3

ann com trac 4

solv hefe

N first ber

2. ciph In a oùs,

rout of all elf the proby the first

re, and the

ed on the ve powers. the small

tinually one econd, twice

er will prous, the serise the sum

.05=

= 32 174. 26276

845 20489 out fin-l-

7441

5625

s thereit will

SQUARE ROOT.

ASSISTANT.]

be obvious, that the Square Root of a number, multiplied by itself, will produce that number; and that the Cube Root, multiplied twice by itself, will produce the number (or power) of which it is the root.

Note. The roots of complete powers are called rational; and those which cannot be completely extracted, are called surds, or irrational roots: thus  $\sqrt{4} = 2$ , is rational; Lut  $\sqrt{5}$  is a surd. The surd roots may, however, he found to any extent proposed.

#### SQUARE ROOT.

RULE 1. Place points over the units, hundreds, &c., so as to form seriods of two figures each.

2. From the first period on the left, subtract the greatest square contained in it; put the root on the right as a quotient; annex the succeeding period to the remainder, and call that number the Résolvend.

3. Divide the resolvend, exclusive of the units, by double the root; annex the quotient to the root, and also to the right of the divisor to complete it: then multiply the divisor by that quotient figure, and subtract the product from the resolvend.

4. The remainder, with the next period joined, will form a new resolvend; and double the root, a new divisor; with which proceed as hefore.

Note 1. When the number of figures in the Integer is uneven, the first period will consist of but one figure. When there is an odd number of decimals, a cipher must be added to complete the periods.

2. When the figures of the whole number are exhausted, periods of ciphers may be used at pleasure, to continue the extraction in decimals. In all cases, the root will consist of as many figures as there are periods, whether integral or decimal.

ROOTS. 1.  $\mathbf{2}$ . 3. 4. 5. 6. 7. 8. 9. SQUARES. 9. 16. 25. 36. 49, 64, 81. 1. 4.

(1) What is the square root of 119025 ?\*

(2) What is the square root of 106929?

(3) What is the square root of 22071204?

-4148	•	521.	
Ans.	4	698.	

* 119025(345 the root.	345
9	345
64)290 250	1725
	1380
685)3425 3425	1035
3425	Proof 119025.

#### EVOLUTION.

114

TUTOR'S

(4) What is the square root of 2268741? Ans. 1506.23+.
(5) What is the square root of 7596796? Ans. 2756 228+.
(6) What is the square root of 4.372594? Ans. 2.091+.
(7) What is the square root of 2.2710957? Ans. 1.50701+.
(8) What is the square root of .00082754? Ans. .01809+.
(9) What is the square root of 1.270059? Ans. 1.1269+.

### To find the Roots of fractional Numbers.

RULE. When the terms of a Fraction are complete powers, extract their roots for the corresponding terms of the root.

When they are surds, find an equivalent fraction, by multiplying both terms by the denominator; or by the least number that will make the denominator a square. Then divide the root of the munerator by the root of the denominator for the answer.—Or, reduce the fraction to a decimal, and extract its root.

Mixed numbers may either be reduced to their equivalent fractions ; or into a decimel form.

(10)	What is	the square	root of	2304?		Ans. 2.
(11)	What is	the square	root of	9216 ?		Ans. 4.
(12)	What is	the square	root of	5121?		Ans. 71.
(13)	What is	the square	root of	27 8 ?		Ans. 51.
(14)	What is	the square	root of	943 ?		Ans. 34.
(15)	What is	the square	root of	275?	Ans	89802
(16)	What is	the square	root of	478?	Ans.	·93309+
(17)	What is	the square	root of	8514 ?	An	s. 9.27+
(18)	What is	the square	root of	85?	Ans.	2.9519+.

To find a mean proportional between any two given numbers.

RULE. Extract the square root of their product.

(19) What is the mean proportional between 3 and 12?

 $\sqrt{3\times 12} = \sqrt{36} = 6$  the mean proportional. Ans.

(20) What is the mean proportional between 4276 and 842? Ans. 1897.4+.

### To find the side of a square equal in area to any given surface.

RULE. Extract the square root of the given area for the side of the, square sought.

(21) If the content of a given circle be 160, what is the side of the square equal? Ans. 12.64911.

(22) If the area of a circle is 750, what is the side of the square equal? Ans. 27.38612,

### ASSISTA

RULE. of the dia and the r

(23)

other en acre of measure

### $T_{\ell}$

' RULE. of the cir and the j

(24)

(25)

Two si

Case 1

RULE.

Case 2

RULE.

Case 3

RULE.

and it i

nmst a

top of

(26)

06.23+. 66.228+. 2.091+. 50701+. 01809+. 1269+.

s, extract

lying both make the or by the ction to a

fractions ;

 $\begin{array}{c} ns. \frac{2}{3}.\\ ns. \frac{4}{7}.\\ s. 7\frac{1}{3}.\\ s. 5\frac{1}{4}.\\ s. 3\frac{1}{4}.\\ 802+\\ 809+\\ 27+\\ 519+. \end{array}$ 

umbers.

d 12 ? Ans. 276 and 7.4+.

surface. de of the

at is the 4911.

e of th<del>e</del> 8612, ASSISTANT.]

#### SQUARE ROOT.

### The area of a circle given, to find the diameter.

RULE. As 355 : 452, or, as 1 : 1.973239 :: the area : the square of the diameter; or, multiply the square root of the area by 1.12837, and the product will be the diameter.

(23) What length of cord must be tied to a cow's tail, the other end fixed in the ground, to enable her to eat just an acre of grass, and no more; supposing the cow and tail to measure  $5\frac{1}{2}$  yards? Ans. 33.75 yards.

### The area of a circle given, to find the circumference.

<sup>'</sup> RULE. As 113 : 1420, or, as 1 : 12.56637 : : the area : the square of the circumference; or, multiply the square root of the area by 3.5449, and the product will be the circumference.

(24) When the area is 12, what is the circumference? Ans. 12.279.

(25) When the area is 160, what is the circumference? Ans. 44.839.

Two sides of a right-angled triangle being given, to find the third side.

Case 1. The base and perpendicular being given, to find the hypoten re.

RULE. The square root of the sum of the squares of the base and perpendicular is the length of the hypotenuse.

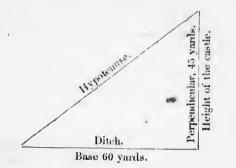
Case 2. The hypotenuse and perpendicular being given, to find the base.

RULE. The square root of the difference of the squares of the hypotenuse and perpendicular is the length of the base.

Case 3. The base and hypotenuse being given, to find the perpendicular.

RULE. The square root of the difference of the squares of the hypotenuse and base is the height of the perpendicular.

(26) The top of a castle from the ground is 45 yards high, and it is surrounded with a ditch 60 yards broad : what length must a ladder be to reach from the outside of the ditch to the top of the castle ? Ans. 75 yards



(27) The wall of a town is 25 feet high, and is surrounded by a moat of 30 feet in breadth: required the length of a ladder that will reach from the outside of the moat to the top of the wall? Ans. 39.05 feet.

N. B. These two questions may be varied for examples to the second and third cases.

(28) In an army consisting of 331776 men, how many must be in rank and file to form a solid square? Ans. 576.

(29) A certain square pavement contains 48841 equal square stones. How many are contained in one of the sides?

Ans. 221.

#### CUBE ROOT.

**RULE 1.** Point even third figure of the given number, beginning at the units' place; find the greatest cube in the first period, and subtract it therefrom; put the root in the quotient, and bring down the figures in the next period to the remainder for a *Resolvend*.

2. Multiply the square of the root found by 300 for a *Divisor*, and annex to the root the number of times which that is contained in the *Resolvend*.

3. Add 30 times the preceding figure (or figures) multiplied by the last and the square of the last, to the divisor, and multiply the sam by the last for a *Subtraneod*; subtract it from the *Resolvend*, and repeat the process as lar as necessary.<sup>4</sup>

\* The subjoined Theorems (deduced from Problem 91, page 266, Emerson's Algebra) are very convenient approximations for the Cube Root.

 $\frac{1}{3}r + \frac{1}{4}\sqrt{\left(\frac{4n-r^3}{3r}\right)} = \frac{1}{2}r + \sqrt{\left(\frac{n}{3r} - \frac{1}{12}r^2\right)} =$ 

### ABSISTAN

TUTOR'S

Note. times only always co as in the s will hold

> Roo Cui

- (1) W
- (2) W = (3) W
  - (4) W
  - (5) W
  - (6) W
  - (7) W
    - (8) W
    - (9) V

R, the re and r an The se cause it e

expressed Divide

the quoti root of th root requi

### ASSISTANT.]

### CUBE ROOT.

NOTE. As the units must always be pointed, there will be cometimes only one or two figures in the first period.—The decimals must always consist of so many figures as will constitute complete periods, us in the Square Root.—Also, what is observed in Note 2, Square Root, will hold good in this Rule.

R		1.	2.	3.	4.	5.	6.	7.	8.	9.
С	UBES.	1.	8.	27.	64.	25.	216.	343.	512.	729.
(1)	What	is the	cu	be r	oot of	999	25284	7 ?*		
(2)	What	is the	e cu	be r	oot o	38	9017?			ns. 73.
(3)	What	is the	cu	be r	oot of	57:	;5339	?	An	s. 179.
(4)	What	is the	e cu	he r	oot o	f 32-	46175	9 ?	An	s. 319.
(5)	What	is the	cu	be r	oot of	84	60451	9?	An	s. 439.
(6)	What	is the	e cu	be r	oot o	271	05403	6008	? Ans	. 3002.
(7)	What	is the	e cu	be 1	coot o.	67:	33730	97125	? Ans	s. 8765.
(8)	What	is the	e cu	be r	oot o	f 12	9778	75 ?	An	s. 2·35.
(9)	What	is the	o ci	be i	root o	f .00	01906	624?	An.	s. ·124.

the top of 05 feet.

urrounded 1 of a lad-

the second

any must s. 576. al square les ? s. 221.

eginning at ad subtract the figures

ivisor, and ned in the

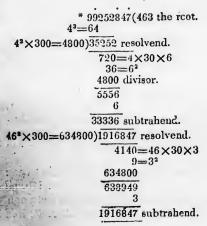
ied by the he sum by and repeat

e 266, Em-

**R**, the required root, nearly. In which n denotes the given number, and r an assumed root found by trial.

The second formula, which is more convenient than the other, because it contains no higher power than the square of r, may be thus expressed.

Divide the given number by three times the assumed root, and from the quotient subtract  $\frac{1}{12}$  of the square of the assumed root: the square root of the remainder, added to half the assumed root, will give the root required. See also the method of extracting ANY ROOT by approximation.



#### EVOLUTION.

118

[TUTOR'S

(10) What is the cube root of 36155 02756? Ans. 33 06+.
(11) What is the cube root of 33 230979937? Ans. 3 215+.
(12) What is the cube root of 15926 972504? Ans. 25 16+.

### To find the Roots of Fractional Numbers.

RULE. When the terms of a fraction are complete powers, extract their roots for the corresponding terms of the root.

When they are *surds*, if both terms be multiplied by the *square of the denominator*, an equal fraction will be produced, the denominator of which will be a *cube*. Then divide the root of the numerator by the root of the denominator for the answer.—Or, the fraction may be reduced to a decimal, and its root extracted.

Mixed numbers may be reduced as in the Square Root.

(13)	What is	the cube	root of	250?		Ans. §.
(14)	What is	the cube	root of	$\frac{324}{1500}$ ?		Ans. 3.
(15)	What is	the cube	root of	$12\frac{19}{27}$ ?	1	$1ns. 2\frac{1}{3}.$
(16)	What is	the cube	root of	$31\frac{1}{34}\frac{5}{3}$ ?	1	4ns. 34.
(17)	What is	the cube	root of	$405\frac{28}{125}$	? A	Ins. 72.
(18)	What is	the cube	root of	$\frac{4}{7}$ ?	Ans. 829	8265 <del>+</del> .
(19)	What is	the cube	root of	5 ?	Ans. 822	0707+.
(20)	What is	the cube	root of	$7\frac{1}{5}?$	Ans. 1.93	0978+.
(21)	What is	the cube	root of	91 ?	Ans. 2.092	2845 + .
(22)	What is	the cube	root of	857?	Ans. 2.057	8352 + .
1091	A motor	intown in	the for	n of a cit	he contain	a 60 aubie

(23) A water eistern in the form of a cube contains 60 cubic feet, 143 inches; what is the length of the side?

Ans. 47 inches.

(24) There is an excavation made for a cellar equal in length, breadth, and depth; which required 4913 cubic feet of earth to be dug out. What is the length of the side?

Ans. 17 feet.

(25) There is a building of cubic form, which contains. 389017 solid feet: what is the superficial content of one of its sides ? Ans. 5329 sq. feet.

### Between two numbers given, to find two mean proportionals.

RULE. Divide the greater extreme by the less, and the cube root of the quotient multiplied by the less extreme gives the *less mean*; multiply the said cube root by the less mean, and the product will be the greater mean proportional.

(26) What are the two mean proportionals between 6 and 162? Ans. 18 and 54.

(27) What are the two mean proportionals between 4 and 108? Ans. 12 and 36.

ASSISTA

To fine

Rule. of equal (28)

side of

The sic shal

RULE. root of 1 (29)

it is red tain thr

RULE. square r quired.

> (1)(2) (3)

### AGENE

i. F two fig 2. F from th 3. E mainde 4. In

one; an divisor. 5, F to the for a su 6, I period trahena

thus to

. 33·06+. . 3·215+. . 25·16+.

xtract their

e square of cominator of ator by the be reduced

Ans.  $\frac{5}{4}$ . Ans.  $\frac{2}{3}$ . Ins.  $\frac{2}{3}$ . Ins.  $\frac{2}{3}$ . Ins.  $7\frac{2}{5}$ . 3265+. 3265+. 3707+. 9978+. 845+. 3352+.

s 60 cubic

inches. equal in bic feet of ? ? feet. contains of one of q. feet.

ortionals.

the root of nean; mulwill be the

een 6 and and 51. een 4 and and 36. ASSISTANT.]

### ROOTS OF ALL POWERS.

To find the side of a cube equal in solidity to any given solid as a globe, cylinder, prism, cone, &c.

RULE. The cube root of the solid content given is the side of a cube of equal solidity.

(28) If the solid content of a globe is 10648, what is the side of a cube of equal solidity? Ans. 22.

The side of a cube being given, to find the side of a cube that shall be double, treble, S.c., in quantity to the cube given.

Rele. Cube the side given, and multiply it by 2, 3, &c., the cube root of the product will be the side sought.

(29) There is a cubical vessel whose side is 12 inches, and it is required to find the side of another vessel that will contain three times as much. Ans. 17:30699 inches.

### BIQUADRATE ROOT.

RULE. Extract the square root of the given number, and then the square root of that square root, which will be the biquadrate root required.

What is the biquadrate root of 531441?
 Ans. 27.
 What is the biquadrate root of 33362176?
 Ans. 76.

(3) What is the biquadrate root of 5719140625? Ans. 275.

### A GENERAL RULE FOR EXTRACTING THE ROOTS OF ALL POWERS.

i. PREPARE the given number by pointing it into periods of two figures each for the square root, three for the cube root, &c.

2. Find the first figure of the roct, and subtract its power from the first period.

3. Bring down the first figure in the next period to the remainder, and call that the *dividend*.

4. Involve the root to the next inferior power to the given one; and multiply it by the index of the given power for a *livisor*.

5. Find a quotient figure by common division, and annex it to the root; then involve the whole root to the given power for a subtrahend, which subtract from the first two periods.

6. To the remainder bring down the first figure of the next period for a new dividend; find a new divisor and a new subtrakend, as before; subtract from three periods, and proceed thus to the end.

#### POSITION.

### Otherwise. To find ANY ROOT by approximation.

RULE. Let g denote the given number or power, n the index of the power, a an assumed power nearly equal to g, r its root, and R the required root.

Then, as  $\frac{(n+1)a + (n-1)g}{2}$  :  $a \circ g$  :: r :  $R \circ r$ ;\* which dif-

ference or correctional number, being added or subtracted, (as required,) will give R, and by repeating the process, any degree of accuracy may be obtained.

- (1) What is the square root of 141376?
- (2) What is the cube root of 53157376?

(3) What is the fourth root of 19987173376? Ans. 376.

(4) Required the fifth root of 2508.474615614240625.

Ans. 4.785.

[TUTOR'S

Ans. 376.

(5) Required the sixth root of 3.1416. Ans. 1.210201+

#### SINGLE POSTTION

Is the method of using one supposed number, and working with it as the true one, to find the real number required.<sup>‡</sup>

RULE. As the result from the supposition is to the true result, so is the supposed number to the true one required.

**PROOF.** Add the several parts together, according to the conditions of the question.

(1) A schoolmaster being asked how many scholars he had, said, "If I had as many, half as many, and one quarter as many more, I should have 88." How many had he?

\* This for the Cube Root will be, As  $2a + g : a \circ g :: r : R \circ r$ .

+ 141376(376 the root. 9  $3 \times 2 = 6)51$  dividend.  $37^2 = 1369$  subtrahend.  $37 \times 2 = 74)447$  dividend.  $276^2 = 141376$  subtrahend.

t Questions belonging to this Rule have the results proportional to their suppositions; the conditions requiring the number sought to be increased by the addition of itself, or of some known multiple or part thereof, or to be diminished by the subtraction of such part.

§ Suppose he had 40. Then 40 + 40 + 20 + 10 = 110. And, as  $110: 83:: 40: \frac{83 \times 4|0}{11|0} = \frac{352}{11} - 32$  Ans.

### ASSISTAN

(2) A said, if added to

(3) A being do the price (4) V at  $\pounds 6$ . F

(5) A £120. r than A, man pay (6) A horse ir of the h den for

REQUIR required

RULE. in the rethe true and mult

If the given nu the prod and the answer.

> \* Que traction required sitions.

† The Multip and divid

ASSISTANT-1

### tion.

dex of the R the re-

which dif-

required,) uracy may

Ans. 376. Ans. 376. 0625. as. 4.785. 210201+

king with

esult, so is

conditions

s he had, uarter as ?§

: R () r.

ortional to aght to be pie or part

### POSITION.

(2) A person who had a certain number of antique coins, said, if the third, fourth, and sixth parts of the number were added together, they would make 54. How many had he? Ans. 72.

(3) A chaise, a horse, and harness, cost  $\pounds 60$ ; the horse being double the price of the harness, and the chaise double the price of the horse and harness. What was given for each?

Ans. Horse £13..6..8. harness £6...13..4. chaise £40.
(4) What sum of money will amount to £300 in ten years,

at £6. per cent. per annum, simple interest? Ans. £187..10.

(5) A, B, and C, dividing a quantity of goods, which cost  $\pounds$ 120. mutually agreed that B should have a third part more than A, and C a fourth part more than B. What must each man pay? Ans. A  $\pounds$ 30. B  $\pounds$ 40. C  $\pounds$ 50.

(6) A gentleman bought a house, with a garden, and a horse in the stable for  $\pounds 500$ . He paid four times the price of the horse for the garden, and 5 times the price of the garden for the house. What were their respective prices?

Ans. Horse £20. garden £80. house £400.

### DOUBLE POSITION

**REQUIRES the use of** two supposed numbers to find the true one required.\*

RULE. Work with the two supposed numbers, and mark the errors in the results with + or -, according as they exceed or fall short of the true result; theu place the errors against their respective positions, and multiply them crosswise.

If the errors be of *like* kinds, i. e. *both greater*, or *both less* than the given number, take their difference for a divisor, and the difference of the products for a dividend. But if *unlike*, take their sum for a divisor, and the sum of their products for a dividend: the quotient will be the answer.<sup>†</sup>

\* Questions belong to this Rule which require the addition or subtraction of a number, &c., which is not any known part of the number required. The results are, therefore, not proportional to their suppositions.

+ The following Rule will, in some cases, be found more eligible:

Multiply the difference of the supposed numbers by the less error; and divide the product by the difference of the errors when they are of

#### POSITION.

(1) A, B, and C, would divide £200. among them, so that B may have £6. more than A, and C £8. more than B. How much must each have ?\*

(2) A man had two silver cups of unequal weight, having one cover to both of 5 ounces. Now if the cover is put on the less cup, it will double the weight of the greater; and put on the greater cup, it will be thrice as heavy as the less. What is the weight of each ?

Ans. 3 ounces the less, and 4 the greater. (3) Three persons conversing about their ages; says K, "My age is equal to that of H, and  $\frac{1}{4}$  of L's;" and L says, "I am as old as both of you together." Required the ages of K and L; H's being 30. Ans. K 50, and L 80.

(4) D, E, and F, playing at cards, staked 324 crowns; but disputing about the tricks, each man seized as many as he could: E got 15 more than D; and F got a fifth part of both their sums added together. How many did each person get? Ans.  $D \ 127\frac{1}{2}$ ,  $E \ 142\frac{1}{2}$ , and  $F \ 54$ .

(5) A gentleman meeting with some ladies, said to them, "Good morning to you, ten fair maids." "Sir, you mistake,"

like kinds, or by their sum, when unlike; the quotient will be a correctional number; which being added to the nearest supposition when defective, or subtracted from it when excessive, will give the number required.

£.	£.
* 1st. Suppose A's share = 40	2ud. Suppose A's share = 70
then B's = $46$	then B's $=$ 76
and C's 📟 54	and C's $=$ 84
Sum 140	Sum 230
Therefore the error is	Here the error is $+$ 30, or 30 ton
- 60, or 60 too little.	much.
sup. err.	£.
• 49 60	A 60
$_{70}^{10} \times _{30}^{10}$	В 66
4200 1200	C 74
1200	200 Proof.
U1 4 1.4 01 .	
60- -30=9 0)540 0 dividend.	
$\pounds 60 = A's$ shar	
Or, by the Rule in the No	-
$\frac{70 - 40 \times 30}{60 + 30} = \frac{30 \times 30}{90} =$	10, the correctional number.
Then $70 - 10 = 60 = A$ 's share,	

### ASSISTAL

[TUTOR'S

answere times as we are 1

An Ar or decre 1, 2, 2, 5, 9, 8,

Observation of the observation of the observation of the servation of the

16, 12,

In an middle t two terms the dout In an equal to terms. 10 = 14: To gi cases, th Thus

Note. ing Theor a = z - (n)

Any t

 $d = \frac{z - a}{n - 1}$ 

n, so that B. How

ht, having is put on ater; and s the less.

greater.

; says K, d L says, e ages of d L 80. owns; but any as he rt of both erson get? d F 54. I to them. mistake,"

ill be a corstion when the number

£. e = 70s = 76s = 84Sum 230 30, or 30 ton

roof.

nber.

### ASSISTANT.]

### PROGRESSION.

answered one of them, "we are not ten; but if we were the times as many as we are, we should be as many above ten as we are now under." How many were they? . Ans. 5.

### ARITHMETICAL PROGRESSION.

An Aruhmetical Progression is a series of numbers increasing or decreasing uniformly by a *continued equal difference*. Thus.

1, 2, 3, 4, 5, &c. 2, 5, 8, 11, 14, &c. } are increasing Arithmetical Series.

9, 8, 7, 6, 5, &c. 16, 12, 8, 4, 0, &c. } are decreasing Arithmetical Series.

Observe, that the *terms* of the first series are formed by adding successively the common difference 1, and the second by the common difference 3. The terms of the third and the fourth diminish continually by the subtraction of 1 and 4 respectively.

In an odd number of terms, the double of the mean (or middle term) is equal to the sum of the extremes, or of any two terms equidistant from the mean. Thus, in 1, 2, 3, 4, 5, the double of 3=1+5=2+4=6.

In an even number of terms, the sum of the two means is equal to the sum of the extremes, or of any two equidistant 10 = 14:

To give Theorems or Rules for the solution of the various cases, the terms are represented by symbols, or letters.

Thus let a denote the less extreme, or least term,

2	the greater	extreme,	or	greatest	term,
1	4h			0	

the common difference,

the number of terms, and

the sum of all the terms.

Any three being given, the others may be found.

п

NOTE. The twenty cases in this Rule may be resolved by the follow ing Theorems :---

 $a = z - (n-1)d = \frac{2s}{n} - z = \frac{s}{n} - \frac{1}{2}d(n-1) = \frac{1}{2}d + \sqrt{(\frac{1}{2}d+z)^2 - 2ds}.$  $s = a + (n-1)d = \frac{2s}{n} - a = \frac{1}{n} + \frac{1}{2}d(n-1) = \sqrt{(\frac{1}{2}d-a)^2 + 2ds} - \frac{1}{2}ds$  $d = \frac{z - a}{n - 1} = \frac{s - an}{n - 1} \cdot \frac{2}{n} = \frac{nz - s}{n - 1} \cdot \frac{2}{n} = \frac{(z + a) \cdot (z - a)}{2s - a - z}$ 

$$n = \frac{z - a}{d} + 1 = \frac{2s}{a + z} = \frac{\frac{1}{2}d - a + \sqrt{(\frac{1}{2}d - a)^2 + 2ds}}{d} = \frac{\frac{1}{2}d + z - \sqrt{(\frac{1}{2}d + z)^2 - 2ds}}{d}.$$

 $s = \frac{1}{2}n(a+z) = \frac{a+z}{2} \cdot \frac{z-a+d}{d} = \frac{1}{2}n \cdot \frac{z-a+d}{2} = \frac{1}{2}n \cdot \frac{z-a+d}{2}$ 

Moreover, when the least term a = nothing, the Theorems become z=d(n-1,) and  $s=\frac{1}{2}nz$ .

Case 1. The two extremes and the number of terms being given, to find the sum.

RULE. Multiply the sum of the extremes by the number of terms, and half the product will be the answer.\*

(1) How many strokes does the hammer of a clock strike in 12 hours ?†

(2) A man bought 17 yards of cloth, and gave for the first yard 2s. and for the last 10s. What was the price of the 17 yards?  $Ans. \pounds 5..2$ .

(3) If 100 eggs be placed in a right line, exactly a yard from each other, and the first a yard from a basket, how far must a person travel to gather them all up singly, and return with every egg to put it into the basket?

Ans. 5 miles, 1300 yards.

### Case 2. The same three terms given, to find the common difference.

RULE. Divide the difference of the extremes by the number of terms less 1, and the quotient will be the answer.

(4) A man had eight sons, whose ages were in arithmetical progression; the youngest being 4 years old, and the eldest
32. What was the common difference of their ages ?‡

(5) A man travelling from London to a certain place, went 3 miles the first day, and increased every day by an equal excess, making the twelfth day's journey 58 miles.

 $+12+1 \times 6 = 13 \times 6 = 73$ . Ans.

± 32-4-2-1=28-7=4 years. Ans.

#### ASSISTAN

TUTOR'S

What w days ? Ans.

Case 3.

RULE. ence, and

(6) A
first day
58 miles
(7) A
the you
his fam
had he

Case 4.

RULE. 1; subtr will be t

(8) A country by 4 m

(9) *I* many d former

Case 5

RULE. subtract terms le

(10) each p bestow is. W

Case 6

RULE

<sup>\*</sup> The learner should find each of these cases among the preced ing *Theorems*. Thus, the present Rule will be found designated by  $s=\frac{1}{2}n(a+z)$ , &c.

-d(n-1.)

Theorems

cing given,

er of terms,

lock strike

for the first e of the 17 s. £5..2. ctly a yard et, how far and return

)0 yards.

ommon dif-

nber of terms

arithmetical l the eldest ges ?‡ rtain place, y day by an y 58 miles.

g the preced lesignated by ASSISTANT.]

### PROGRESSION.

What was the daily increase, and how far did he travel in 12 days?

Ans. 5 miles daily increase, the whole distance 366 miles.

Case 3. The two extremes and the common difference being given, to find the number of terms.

RULE. Divide the difference of the extremes by the common difference, and the quotient increased by *unity* is the number sought.

(6) A person travelling into the country, went 3 miles the first day, and increased every day 5 miles, till at last he went 58 miles in one day. How many days did he travel ? Ans. 12.

(7) A man being asked how many sons he had, said, that the youngest was 4 years old, and the eldest  $32 \cdot$  and that his family had increased one in every 4 years. How many had he? Ans. 8.

Case 4. The greater extreme, the number of terms, and the common difference being given, to find the less extreme.

RULE. Multiply the common difference by the number of terms less 1; subtract the product from the greater extreme, and the difference will be the less extreme.

(8) A man went from London to a certain town in the country in 10 days; every day's journey exceeding the former by 4 miles, and the last being 46 miles : what was the first? Ans. 10 miles.

(9) A man took out of his pocket, at 8 several times, so many different numbers of shillings, every one exceeding the former by 6, the last being 46: what was the first? Ans. 4.

Case 5. The common difference, the number of terms, and the sum being given, to find the less extreme.

RULE. Divide the sum by the number of terms: from the quotient subtract half the product of the common difference into the number of terms less 1; and the remainder will be the less extreme.

(10) A man is to receive £360. at 12 several payments, each payment to exceed the former by £4. and is willing to bestow the first payment on any one that can tell him what  $\cdot$ is. What will that person have for his pains? Ans. £8.

Case 6. The less extreme, the common difference, and the num ber of terms being given, to find the greater extreme

RULE. Multiply the number of terms less 1 by the common differ

#### PROGRESSION.

ence; to this product add the less extreme, and the sum will be the greater extreme.

(11) What is the last number of an arithmetical progression, beginning at 6, and continuing by the increase of 8 to 20 places ? Ans. 158.

#### GEOMETRICAL PROGRESSION.

A Geometrical Progression is a series of numbers increasing or decreasing uniformly by a common ratio; that is, by the continual multiplication or division of some particular number. Thus,

1, 2, 4, 8, 16, 32, &c., is an *increasing Geometrical Series*, in which the terms are formed by multiplying successively by the ratio 2.

81, 27, 9, 3, 1,  $\frac{1}{3}$ , &c., is a decreasing Geometrical Series, in which the terms are formed by dividing successively by the ratio 3. It is evident that either of these may be continued without end.

In an odd number of terms, the square of the mean is equal to the product of the extremes, or of any two terms equidistant from the mean. Thus, in 3, 6, 12, 24, 48;  $12 \times 12 = 3 \times 48$ =  $6 \times 24 = 144$ .

In an even number of terms, the *product* of the *two means* is equal to the *product* of the *extremes*, or of any *two equidistant terms*. Thus, in 32, 16, 8, 4, 2, 1;  $8 \times 4 = 32 \times 1 = 16 \times 2 = 32$ .

To give *Theorems*, or Rules expressed in symbols, for the solution of the various cases, as in Arithmetical Progression, let a denote the *less cxtrcme*,

z the greater extreme,

the ratio.

*n* the *number* of terms, and

s the sum of all the terms.

Any three being given, the others may be found.

Note. The twenty *Theorems* following solve all the possible cases in Geometrical Progression.

Theor. I.  $r^{n-1} = \frac{z^*}{a}$ ; or,  $\frac{\text{Log. } z - \log. a}{\log. r} + 1 = n$ .

\* In this case, if the quotient of  $\frac{z}{a}$  be divided continually by r, till nothing remains; the number of divisions + 1 will give n.

ASSIST

TUTOR'S

II. -

III.

IV.

VI.

or, Lo

VII

X. 1

XI.

Double

found i

XII

XV.

XVI

Froi Positio

XIX

In a =0, an

18

or

D

will be the

il progresse of 8 to ns. 158.

increasing is, by the ular num-

ical Series, essively by

l Series, in ely by the continued

an is equal equidistant  $12 = 3 \times 48$ 

two means vo cquidis- $=32 \times 1 =$ 

ols, for the rogression,

und. ossible cases

lly by r, tili

ABSISTANT.] PROGRESSION. 127  
II. 
$$\frac{rz-a}{r-1} = s$$
; or,  $z + \frac{z-a}{r-1} = s$ .  
III.  $\left(\frac{z}{a}\right)^{\frac{1}{n-1}} = r$ ; or,  $\overline{\text{Log. } z - \log . a \div n - 1} = \text{Log. } r$   
IV.  $z + \frac{z-a}{\left(\frac{z}{a}\right)^{\frac{1}{n-1}} - 1} = s$ .  
V.  $\frac{s-a}{s-z} = r$ .  
VI.  $\left(\frac{s-a}{s-z}\right)^{n-1} = \frac{z}{a}$ ; from which  $n$  may be found, as in  
or,  $\frac{\text{Log. } z - \log . a}{\text{Log. } (s-a) - \log . (s-z)} + 1 = n$ . VII.  $ar^{n-1} = z$ .  
VIII.  $\frac{a(r^n-1)}{r-1} = s$ . IX.  $\frac{(r-1)s+a}{r} = s - \frac{s-a}{r} = z$   
X.  $r^n = \frac{(r-1)s}{a} + 1$ ; or,  $\frac{\text{Log. } (r-1)s+a - \log . a}{\text{Log. } r} = r$ .  
XI.  $z \times \overline{s-z} = n^{n-1} = a \times \overline{s-a} = n^{n-1}$ ; whence  $z$  may be found by  
Double Position. XII.  $\frac{sr}{a} - r^n = \frac{s-a}{a}$ ; whence  $r$  may be  
found in the same manner.  
XIII.  $\frac{z}{r^{n-1}} = a$ . XIV.  $\frac{z(r^n-1)}{r^n - r^{n-1}} = s$ .

$$\frac{\text{Log. } z - \log . rz - (r-1)s}{\text{Log. } r} + 1 = n.$$
**XVII.**  $a \times \overline{s-a} |^{n-1} = z \times \overline{s-z} |^{n-1}$ . XVIII.  $\frac{r^{n-1}s}{s-z} r^n = \frac{z}{s-z}$ 
From the two preceding, *a* and *r* are to be found by Doubl

**XV.** rz - (r-1)s = a. XVI.  $r^{n-1} = \frac{z}{rz - (r-1)s}$ ; or,

Position.

XIX. 
$$\frac{(r-1)s}{r^n-1} = a$$
. XX.  $\frac{r^n-r^{n-1}}{r^n-1} \times s = z$ .

In a Geometrical series decreasing ad infinitum, a becomes =0, and n is infinite, or greater than any assignable number.

#### PROGRESSION

Hence the three following will exhibit all the various cases of such a series.

I. 
$$s = \frac{rz}{r-1} = z + \frac{z}{r-1} = \frac{z^2}{z - \frac{z}{r}}$$
. II.  $z = \frac{s(r-1)}{r}$ . III.  $r = \frac{s}{s-z}$ .

NOTE. In these cases, when the ratio is a proper fraction, r must be taken = the reciprocal of the function. Thus, when the ratio is  $\frac{1}{2}$ ,  $r = \frac{4}{3}$ .

### Case 1. The less extreme, the ratio, and the number of terms being given, to find the greater extreme (or any remote term) without producing all the intermediate terms.

RULE 1. When the least term is cqual to the *ratio*. Write down a few of the leading terms of the series, and over them the arithmetical series, 1, 2, 3, 4, &c., as *indices* or *exponents*. Find which of the *i*-*dices*, *added together*, will give the *index* of the *term sought*, and the continual product of the terms standing under those indices will be the term sought.

2. When the least term is not equal to the ratio. Write down the leading terms as before, and over them the indices, 0, 1, 2, 3, 4, &co. Examine which of these, added together, will give an index one less than the number of the term sought; multiply the terms under such indices into each other, dividing the product of every two by the first term, and the last quotient will be the term required.\*

Otherwise, By Theorem VII.

(1) A man agrees, for 12 peaches, to pay only the price of the last; reckoning a farthing for the first, and a halfpenny for the second, &c., doubling the price to the last. What must he give for them ? $\dagger$ 

(2) A farmer, who went to a fair to buy some oxen, met with a drover who had 23, for which he asked him  $\pounds 16$ . a piece. After a great deal of dodging between the parties, it was finally agreed that the farmer should pay the price of the last ox only, reckoning a farthing for the first, and doubling it to the last. How much would they cost him?

Ans. £1369..1..4.

\* If the least term is unity, there will (of course) be no division.

 $\dagger$  Here a = 1, r = 2, and n = 12, a and r being unequal.

Indices, 0, 1, 2, 3, 4. Geom. series, 1, 2, 4, 8, 16. Hence  $16 \times 16 \times 8 = 2048$  grs. = z, and 2048 grs. = £2..2.3 Ans ASSIST

TUTOR'S

(3)
first to
portion
(4)
execut
To hit
to the

Case

the el

Rut. betwee er extu rem V.

> (5)gentle give the s amou (6)a fart suppo was 1 (7) day, doubl year. (8) gentl for 2 porti

> > Gee

т <del>=</del> 559

ious cases

I.  $r = \frac{s}{s - -s}$ .

e ratio is 2,

r of terms mote term)

Vrite down a arithmetical h of the *i*ght, and the s will be the

te down the , 2, 3, 4, &co. one less than such indices rst term, and

he price of lfpenny for What must

oxen, met im  $\pounds 16$ . a e parties, it price of the d doubling

69..1..4.

division.

1 = n - 1.2..8 Ans

ASSISTANT.]

### PROGRESSION.

(3) A sum of money is to be divided among 8 persons, the first to have  $\pounds 20$ . the second 360. and so on in triple proportion. What will the last have?\* Ans.  $\pounds 43740$ .

(4) A gentleman dying left nine sons, to whom and to his executors he bequeathed his estate in the manner following: To his executors  $\pounds 50.$ , to his youngest son twice as much as to the executors, to the next double that sum, and so on to the eldest. What was his fortune ? Ans.  $\pounds 25600.$ 

# Case 2. The less extreme, the ratio, and the number of terms being given, to find the sum. If all the terms.

**RULE.** Find the greater extreme as before, and divide the difference between the extremes by the ratio less 1; to the quotient add the greater extreme for the sum required. This is Theorem II. Or, by Theorem VIII; without finding z.

(5) A young man conversant with numbers, agreed with a gentleman to serve him twelve months, provided he would give him a farthing for his first month's service, a penny for the second, and 4d. for the third, &c. What did his wages amount to ?†  $Ans. \pm 5825..8..5\frac{1}{4}$ .

(6) A man bought a horse, and by agreement was to give a farthing for the first nail, three for the second, &c. Now supposing there were 8 nails in each of his four shoes, what was the price of the horse? Ans.  $\pounds 965114681693..13..4$ .

(7) A person whose daughter was married on new-year's day, gave her husband 1s. towards her portion; promising to double the sum on the first day of every month during the year. What was her portion? Ans. £204..15.

(8) A laceman, well versed in numbers, agreed with a gentleman to sell him 22 yards of rich brocaded gold lace, for 2 pins the first yard, 6 pins the second, &c., in triple proportion. What was the price of the lace, valuing the pins

\* Indices 0, 1, 2, 3. Geom. series 20, 60, 180, 540. Hence  $\frac{540 \times 540 \times 60}{20 \times 20} = 540 \times 27 \times 3 = 43740 = z.$ Otherwise  $ar^{n-1} = 20 \times 3^7 = 43740 = z.$ 

t Here a=1, r=4, and z=12. Therefore  $s = \frac{4^{12}-1}{4-1} = \frac{16777215}{3}$ = 5592405 grs.

### SIMPLE INTEREST.

[TUTOR'S

# at 100 for a farthing? Also, what did the laceman gain supposing the lace to have cost him $\pounds 7$ . per yard?

### Ans. The lace sold for £326886..0..9. Gain £326732..0..9.

### Case 3. The first term, and the ratio, being given, to find the sum of an infinite decreasing series.

RULE. Divide the square of the first term by the difference between the first and second.\*

(9) What is the sum of the circulating decimal 9', or the series  $\frac{1}{10} + \frac{1}{1000} + \frac{1}{10000} + \frac{1}{10000000}$ , &c., continued ad infinitum? Ans. 1. (10) Required the sum of the infinite series  $\frac{1}{2} + \frac{1}{4} + \frac{1}{4}$ ,

**&c.**; also of the series  $\frac{1}{3} + \frac{1}{3} + \frac{1}{27}$ , &c. Ans. 1, and  $\frac{1}{2}$ .

(11) Suppose a body to be put in motion by a force which gives it a velocity of 10 miles the first minute, (or any given space of time,) 9 miles in the second equal space, and so on in the ratio of  $\frac{1}{10}$ ; how many miles would it pass over, if continued in motion for ever? Ans. 100 miles.

### SIMPLE INTEREST, BY DECIMALS.

To give Theorems for the solution of the different cases in Simple Interest, let p denote the principal, r the ratio, t the time, (in years,) i the interest, and a the amount.

Note. The Ratio is the interest of  $\pounds$ 1. for one year, at the rate per cent. propose 1, and may be found by Proportion: thus, at  $\pounds$ 5. per cent. per annum, s<sup>-v</sup>,

### As £100 : £5 : : 1£ : £ 05, the ratio.

### Therefore the ratio at

3 per	ce	nt.	is		•		·03	41	per	• 0	ent.	is				·045
Ω¥ –	•	•			•	• '	·035	5	•	•		•	•			·05
4	•	•	•	•	•	•	∙03 ∙035 ∙04	$5\frac{1}{2}$	•	•	•	•	•	• '	055	, &c

Case 1. When the principal, rate per cent. and time are given, to find the interest.

RULE. Multiply the principal, ratio, and time together, and the product will be the interest required.

That is, prt = i.

(1) What is the interest of  $\pounds 945..10$ . for 3 years, at  $\pounds 5$ . per cent. per annum ?†

\* See the third formula, Theorem I. for infinite series, page 128.  $t prt = \pounds 945 \cdot 5 \times \cdot 05 \times 3 = \pounds 141 \cdot 255 = \pounds 141 \cdot .16 \cdot .6$ . Ans.

#### ASSIST

(2)
annum
(3)
annum
(4)
per ce
(5)
month
(6)
month

Run the pri

At£2

2 3 (7) cent. (8) per co (9) per co (10 1826,

Run (11 per ed (12 per c

annur

\* Т

+ ·0

ain sup-

32..0..9.

find the

between

7, or the 2 Ans. 1.  $+\frac{1}{4}+\frac{1}{4}$ , and  $\frac{1}{2}$ . we which my given nd so on over, if miles.

cases in tio, t the

e rate per . per cent.

· ·045 · ·05 055, &c re given,

d the pro

, at £5.

e 128.

### ASSISTANT.]

### SIMPLE INTEREST.

(2) What is the interest of £547..14, at £4. per cent. per annum, for 6 years ? Ans. £131..8..11..2 08 qrs.

(3) What is the interest of £796..15., at  $\pounds 4\frac{1}{2}$ . per cent. per annum, for 5 years? Ans.  $\pounds 179..5..4\frac{1}{2}$ .

(4) What is the interest of  $\pounds 397..9..5$ . for  $2\frac{1}{2}$  years, at  $\pounds 3\frac{1}{2}$ . per cent. per annum? Ans.  $\pounds 34..15..6..3.55$  qrs.

(5) What is the interest of £554..17..6. for 3 years, 8 months, at £41. per cent. per annum? Ans. £91..11..1.05d.

(6) What is the interest of £236..18..8. for 3 years, 8 months, at £51. per cent. per annum?

### Ans. £47..15..7..2.293 qrs.

### When the interest is for any number of days only.

Rurz. Multiply the interest of £1. for a day, at the given rate, by the principal and the number of days, and the product will be the answer.

### The Interest of £1. for one day.

At £2 per ce	nt.=_f	C·00005479452*	at £4=-00010958904
21		·00006849315	$4\frac{1}{2} = 00012328767$
3		$\cdot 00008219178$	5 = 00013698630
. 3 <del>1</del>		$\cdot 00009589041$	$5\frac{1}{2} = 00015068493$ , &c.

(7) What is the interest of  $\pounds 240$ . for 120 days, at  $\pounds 4$ . per cent. per annum ?†

(8) What is the interest of £364..18. for 154 days, at £5. per cent. per annum? Ans. £7..13..11 $\frac{1}{4}$ .

(9) What is the interest of £725..15. for 74 days, at £4. per cent. per annum? Ans. £5..17..8 $\frac{1}{2}$ .

(10) What is the interest of £100. from the 1st of June, 1826, to the 9th of March following, at £5. per cent. per annum?  $Ans. £3..16..11\frac{2}{3}$ .

### Case 2. When p, r, and t are given, to find a.

**RULE.** prt + p = a.

(11) What will £279..12. amount to in 7 years, at £4 $\frac{1}{2}$  per cent. per annum ?‡

(12) What will  $\pounds$  320..17 amount to in 5 years, at  $\pounds$  3 per cent. per annum? Ans.  $\pounds$  376..19..11..2.8 qrs.

\* The table is formed thus :--

•As 365 days : £.02 :: 1 day : £.00005479452, &c.

\*  $\cdot 00010958904 \times 240 \times 120 = \pounds 3 \cdot 156164352 = \pounds 3 ...3 ...14$ . Ans.

 $.279.6 \times .045 \times 7 + 279.6 = \pounds 367.674 = \pounds 367..13..5..3.04$  grs.

#### SIMPLE INTEREST.

[TUTOR'S

(13) What will £926..12. amount to in  $5\frac{1}{2}$  years, at £4. per cent. per annum? Ans. £1130..9..0..1.92 qrs.

(14) What will £273..18. amount to in 4 years, 175 days. at £3. per cent. per annum? Ans. £310..14..1..33512 grs

Case 3. When a, r, and t are given, to find p.

RULE.  $\frac{a}{rt+1} = p$ 

132

(15) What principal, being put to interest, will amount to  $\pounds 367.13.5.3.04 \ qrs.$  in 7 years, at  $\pounds 4\frac{1}{2}$ . per cent. per annum?\*

(16) What principal will amount to £376..19..11..28 qrs. in 5 years, at £3<sup>1</sup>/<sub>2</sub>. per cent. per annum? Ans. £320..17.

(17) What principal will amount to £1130..9.0.1.92 qrs. in  $5\frac{1}{2}$  years, at £4. per cent. per annum? Ans. £926..12.

(18) What principal will amount to  $\pounds 310..14..1..33512$ grs. in 4 years, 175 days, at £3. per cent. per annum? Ans.  $\pounds 273..18$ .

Case 4. When a, p, and t are given, to find r.

RULE.  $\frac{a-p}{pt} = r.$ 

(19) At what rate per cent. per annum will £279..12. amount to £367..13..5..3.04 qrs. in 7 years ?†

(20) At what rate per cent. per annum will £320..17. amount to £376..19..11..2.8 qrs. in 5 years ?

Ans. £31. per cent.

(21) At what rate per cent. per annum will £926..12 amount to £1130..9..0..1.92 qrs. in  $5\frac{1}{2}$  years?

Ans. £4. per cent.

(22) At what rate per cent. per annum will £273..18 amount to £310..14..1..3·3512 qrs. in 4 years, 175 days? Ans. £3. per cent

Case 5. When a, p, and r are given, to find t.

RULE.  $\frac{a-p}{pr} = t.$ 

\*  $.045 \times 7 + 1 = 1.315$ ; then  $367.674 \div 1.315 = .2279.6 = £279..12$ Ans.

 $\frac{1}{279.6 \times 7} = \frac{88.074}{1957.2} = .045, \text{ or } \pounds 4\frac{1}{2}. \text{ per cent. Ans.}$ 

ASSIS

(23 3.04 (24 2.8 q (25 1.92 q (26 3.351

An are th ties an to con

Le

RUL

(27 cent. (28 will in (29 per an torest (30 8 year

Norn denote and t, t (31 unpaid ing in

\* 36

 $\div 12.5$   $\dagger \left(\frac{4}{-}\right)$ 

150 =

, at £4. 2 qrs. 75 days. 512 qrs

nount to nnum?\* 2·8 qrs. 0..17. ·92 qrs. 026..12. .3·3512 ? 3..18.

279..12.

320..17.

cent. 26..12

cent. 73..18 ys ? er cent

279..12

### ASSISTANT.]

(23) In what time will £279..12 amount to £367..13..5.. 3.04 ors at £4 $\frac{1}{2}$  per cent per annum ?\*

(24) In what time will £320..17. amount to £376..19..11.. 2.8 qrs. at £3 $\frac{1}{2}$ . per cent per annum? Ans. 5 years.

(25) In what time will £926..12. amount to £1130..9..0.. 1.92 qrs. at £4. per cent. per annum? Ans.  $5\frac{1}{2}$  years.

(26) In what time will £273..18. amount to £310..14..1.. 3.3512 qrs. at £3. per cent. per annum?

Ans. 4 years, 175 days.

#### ANNUITIES.

An annuity is a yearly income or rent. *Perpetual Annuities* are those which are to continue for ever; *Terminable Annuities* are to cease within a limited time; and *Life Annuities* are to continue during the term of life of one or more persons.

### The Amount of Annuities in Arrears.

Let u denote the annuity, r, t, and a, as before. Case 1. Given, u, r, and t, to find a.

RULE.  $\left(\frac{\overline{t-1.r}}{2}+1\right) \times tu = a.$ 

(27) If a salary of £150. be forborne 5 years, at £5. per cent. per annum, what will be the amount ?†

(28) If £250. yearly pension be forborne 7 years, what will it amount to at £4. per cent. per annum? Ans. £1960.

(29) There is a house let upon lease for  $5\frac{1}{2}$  years, at £60. per annum, what will be the accumulated rent, allowing interest at £4 $\frac{1}{2}$ . per cent. per annum? Ans. £363..8..3

(30) Suppose an annual pension of £28. remain unpaid for 8 years, what would it amount to at £5. per cent. per annum?

Ans. £263..4.

Note. When the annuity is payable half-yearly, or quarterly, u will denote a single payment, r, the interest of  $\pounds 1$ . for that interval of time, and t, the number of payments.

(31) If a salary of £150., payable every half-year, remain unpaid for 5 years, what will it amount to in that time, allowing interest at £5. per cent. per annum? Ans. £834..7.6.

\* 367.674 - 279.6 = 38.074, and  $279.6 \times .045 = 12.582$ ; then  $88.074 \div 12.582 = 7$  years, Ans.

 $\frac{\dagger}{2} \left( \frac{4 \times \cdot 05}{2} + 1 \right) \times 5 \times 150 = \overline{(2 \times \cdot 05} + 1) \times 5 \times 150 = 1.1 \times 5 \times 150 = \pounds 825; Ans.$ 

### SIMPLE INTEREST.

.(32) If a salary of £150., payable every quarter, were left unpaid for 5 years, what would it amount to in that time at £5. per cont, per annum? Ans. £839. 1..3.

Note. It may be observed by comparing the results of the 27th, 31st, and 32nd examples, that half-yearly payments are more advantageous than yearly, and quarterly more than half-yearly.

Case 2. When a, r, and t, are given, to find u.

RULE. 
$$\frac{2a}{(r.(t-1)+2)\times t} = u.$$

(33) If a salary amounted to £825. in 5 years, at £5. per cent. per annum, what was the salary ?\*

(34) If a house has been let upon lease for  $5\frac{1}{2}$  years, and the amount in that time is £363..8..3. at £4 $\frac{1}{2}$ . per cent. per annum, what is the yearly rent? Ans. £60.

(35) If a pension amounted to  $\pounds 1960$ . in 7 years, at  $\pounds 4$ . per cent. per annum, what was the pension? Ans.  $\pounds 250$ .

(36) Suppose the amount of a pension was £263..4. in 8 years, at £5. per cent. per annum, what was the pension? Ans. £28.

(37) If the amount of a salary, payable half-yearly, be  $\pounds 834..7..6$ . in 5 years, at  $\pounds 5$ . per cent. per annum; what is the salary per year?<sup>†</sup> Ans.  $\pounds 150$ .

(38) If the amount of an annuity, payable quarterly, was  $\pounds 839..1..3$ . in 5 years, at  $\pounds 5$ . per cent per annum; what was the annuity? Ans.  $\pounds 150$ .

Case 3. When u, a, and t are given, to find r.

RULE. 
$$\frac{(a-ut)\times 2}{(t-1)\times ut}=r.$$

(39) If a salary of  $\pounds 150$ . per annun amounts to  $\pounds 823$ . in 5 years, what is the rate per cent. ?‡

(40) If a house has been let upon lease for  $5\frac{1}{2}$  years, at £60. per annum, at what rate per cent. would it amount to £363..8..3? Ans. £4 $\frac{1}{2}$ . per cent

<ul> <li>■ 825 × 2</li> </ul>	1650	1650	£150. Ans.	
$(\cdot 05 \times 4 + 25) \times 5$	$2 \cdot 2 \times 5$	11	LIGU. Ans.	
+ See note, p. 133. + $(825 - \overline{150 \times 5})$	( )			
$\frac{4 \times 150 \times 5}{4 \times 150 \times 5}$	1382	$\frac{25 - 750}{(150 \times 5)} = \frac{1}{2}$	$\frac{75}{150 \times 10} =$	$=\frac{1}{20}=.05$

= r: therefore the rate is £5. per cent.

### [TUTOR'S

(41)in 7 y (42)£263.

ASSIST

(43 amour

(44 amour

RUL

Or, I

(45 amour (46 amour term o (47 borne long h (48 £263. (49 yearly was tl (50 amour been t

> \* Sec t 1/ 8

1.40 ×

(41) If a pension of £250. per annum amounts to £1960. in 7 years, what is the rate per cent.? Ans. £4. per cent.

(42) Suppose the amount of a yearly pension of £28. be £263..4. in 8 years, what is the rate per cent. per annum? Ans. £5. per cent.

(43) If a salary of £150. per annum, payable half-yearly, amount to £834..7..6. in 5 years, what is the rate per cent. ?\* Ans. £5. per cent.

(44) If an annuity of £150. per annum, payable quarterly, amount to £839..1..3. in 5 years, what is the rate per cent.? Ans. £5. per cent.

Case 4. When u, a, and r are given, to find t.

Rule. 
$$\frac{\sqrt{8r\frac{a}{u} + (2-r)^2 - (2-r)}}{2r} = t.$$
  
Or, put  $\frac{1}{r} - \frac{1}{2} = m$ ; then  $\sqrt{\left(\frac{2a}{ur} + m^2\right)} - m = t.$ 

(45) In what time will a salary of  $\pounds$ 150. per annum amount to  $\pounds$ 825. at  $\pounds$ 5. per cent. ?†

(46) If a house is let upon lease at £60, per annum till it amount to £363..8..3, at £4 $\frac{1}{2}$ , per cent. per annum, for what term of years was it let? Ans. 5 $\frac{1}{2}$  years.

(47) If a pension of  $\pounds 250$ , per annum, having been forborne a certain time, amount to  $\pounds 1960$ , at  $\pounds 4$ , per cent., how long has been the time of forbearance? Ans. 7 years.

(48) In what time will a yearly pension of £28. amount to £263..4. at £5. per cent. per annum? Ans. 8 years.

(49) If an annuity of £150. per annum, payable halfyearly, amounted to £834..7..6. at £5. per cent, what time was the payment forborne ?\* Ans. 5 years.

(50) If a yearly pension of  $\pounds 150$ , payable quarterly, amounts to  $\pounds 839..1..3$ . at  $\pounds 5$ . per cent. per annum, what has been the time of forbearance? Ans. 5 years.

\* See Note, p. 133  $t \sqrt{8 \times .05 \times \frac{.825}{.150} + (2 - .05)^2 - (2 - .05)}}_{2 \times .05} = ...$ 

TUTOR'S

ASSISTANT.

time at 1..3.

he 27th, advanta-

£5. per

rs, and ent. per  $\pounds 60.$ at  $\pounds 4.$ 2250. 4. in 8 ion ?  $\pounds 28.$ rly, be what is 150. y, was hat was 150.

823. in

ars, at ount to cent

- .05

SIMPLE INTEREST.

[TUTOR'S

No.	£. s. d.	qrs.	No.	s. d.	qrs.	No.	qrs.
30000	82 3 10	0.11	200	10 11	2.03	1	2.63
20000	54 15 10	2.74	100	5 5	3.01	0.9	2.37
10000	27 7 11	1.37	90	4 11	0.71	0.8	2.10
9000	24 13 1	3.23	80	4 4	2.41	0.7	1.84
8000	21 18 4	1.10	70.	3 10	0.11	0.6	1.58
7000	19 3 6	2.96	60	3 3	1.81	0.5	1.32
6000	16 8 9	0.85	50	2 8	3.51	0.4	1.05
5000	13 13 11	2.68	40	2 2	1.21	0.3	0.79
4000	10 19 2	0.55	30	1 7	2.90	0.5	0.53
3000	8 4 4	2.41	20	1 i	0.60	0.1	0.26
2000	597	0.27	10	0 6	2.30	0.09	0.24
1000	2 14 9	2.14	9	0 5	3.67	0.03	0.21
900	2 9 3	3.12	8	0 5	1.04	0.07	0.18
800	2 3 10	0.11	7	0 4	2.41	0.00	0.16
700	1 18 4	1.10	6	0 3	3.78	0.05	0.13
600	1 12 10	2.08	5	0 3	1.15	0.04	0.11
500	1 7 4	3.07	4	0 2	2.52	0.03	0.08
400	1 1 11	0.05	3	0 1	3.89	0.05	0.05
<b>30</b> 0	0 16 5	1.04	2	0 1	1.26	0.01	0.03

A Table by which the Interest of any sum from £1. to £30000. may be easily computed for any number of days, at any rate per cent.

The above Table is thus constructed: as  $365 \text{ days} : \pounds 1. :: 1 \text{ day} : 2.63 qrs., \&c.$  Hence it appears that the several tabular sums are those which answer to the respective numbers of days, at the rate of  $\pounds 1.$  per year.

In a similar Table in *Rees's Cyclopædia*, there are no fewer than 16 errors. In Dr. Hutton's Table, (Arithmetic, page 84, 12th edition,) there is one error. The above may be depended on as accurate.

**RULE.** Multiply the principal by the rate, both in pounds, and the product by the number of days: divide the last product by 100, collect from the Table the several sums answering to the several parts of the quotient, and the aggregate amount will be the Interest; required.

Example 1. What	It is the interest of $\pounds 37010$	for 220 days
at £41. per cent. p	er annum? $\pounds$ . s.	d. ars.
370.5	Against 3000 stands 8 4	4 2.41
4.2	600 1 12	
18525	60 0 3	3 1.81
14820	7 0 0	4 2.41
1667.25	$0.9.\ldots 0  0$	
220	0.05.00	0 0.13
3334500		11 3.21 Ans
333450	True to the la	ist decimal.
3667 95.00		

485157

Exa 3

280

Ex at £4

> 9 9

To j

Mu lay: befor Ex rate of

> Nот 131, о

### rutor's

. may be cent.

	5
qrs.	
2.63	
2.37	
2.10	
1.84	
1.58	
1.32	
1.02	
0.79	
0.23	
0.56	
0.24	
0.51	
0.18	
0.16	
0.13	
0.11	
0.08	
0.05	
0.03	

1 day 2 are thore f £1. per

r than 16 edition,) te.

and the 0, collect ts of the red.

20 days s. 1

8

31

1

3

Ans

imal.

ASSISTANT.]

### SIMPLE INTEREST.

Example 2. Taking Ex. 8, page 131, we have 364.9

5	£.	5.	d.	qrs.
1824.5	Against 2000 stands 5	9	7	Õ·27
154	800 2	3	10	0·11
72980	9 0	0	5	3.67
273675	0.7 0	0	0	1.84
	0.03 0	0	0	0.08
2809 73.0	2809.73 7	13	11	1.97 Ans

Example 3. What is the interest of £17..16. for 117 days at  $\pounds 4\frac{3}{2}$ . per cent. per annum?

17.5	•		/		
4.75		£.	s.	d.	qrs.
875	Against 90 stands	0	4	11	Õ•71
1225	7	0	0	4	2.41
700	0.2	0	0	0	0.53
83.125	0.05	0	0	0	0.13
117	97.25	0	5	3	3.78 Ans.
581875					
914375					
97 25.625					

To find the amount of a yearly income or salary, &c., for a number of days.

Multiply the number of pounds per year by the number of lay: collect the Tabular sums answering to the product, as before, and their aggregate will be the answer.

Example. What will a person receive for 45 days, at the rate of  $\pounds 105$ . per annum?

105			£.	s.	d.	qrs.
45	Against 4000	stands	10	19	2	0.55
525	700	•••••	1	<b>18</b>	4	1.10
420	20	•••••	0	1	1	0.60
4725	5	•••••	0	0	3	1.15
	4725		12	18	10	3.40 Ans.

NOTE. Any of the preceding examples of interest for days, in page 131, or examples 20 and 21, page 63, may be worked by this method.

#### DISCOUNT.

	A	S	8	I	8	т	
--	---	---	---	---	---	---	--

A Table showing the number of days from any day in the month to the same day in any other month through the year

													-
	То	Jan.	Feb.	Mar.	Apr.	May	June	July	Aug.	Sept.	Oct.	Nov.	Dec.
	[ Jan.	365	31	59	90	120	151	181	212	213	273	304	334
	Feb.	334	365	28				150					
ł		306			31	61	92	122					
1		275					61	91	122	153	183	214	244
-	May	245	276	304	335	365	31	61	92	123	153	184	214
10	June	214	245	273'	304	334	365	30	-01	92	122	153	183
From	July	184	215	243	274	304	335	365	31	62	92	123	153
	Aug.	153	184	212	243	273	304	334'	365'	31	61		
	Sept.	122	153	181	212	242	273	303	334	365	30	61	91
	Oct.	92	123	151	182	212	243	273	304	335	365	31	61
	Nov.	61	92	120	151	181	212	242	273	304	334	365	30
	Dec.	31		90	121	151	182	212	243	274	304	335	365

### DISCOUNT.

LET s represent the sum to be discounted, r the ratio, t the time, (in years,) and p the present worth.

Case 1. Given s, r, and t, to find p.

RULE. 
$$\frac{s}{rt+1} = p$$
.

(1) What is the present worth of £357..10. to be paid 9 months hence, at £5. per cent. per annum ?\*

(2) What is the present worth of £275..10 due 7 months hence, at £5. per cent per annum? Ans. £267..13..10 $\cdot$ 152d.

(3) What is the present worth of £875..5. 6. due 5 months hence, at  $\pounds 4\frac{1}{2}$ . per cent. per annum?

Ans. £859..3..3.01824 grs.

(4) How much ready money can I receive for a note of £75 due 15 months hence, at £5. per cent. per annum? Ans. £70.11..9.1764d.

\*  $357.5 - 05 \times .75 + 1 = 344.5783 = \pounds 344..11..6..3.168 \ qrs. Ans$ 

RULE

(5)
hence,
3.168
(6)
agrees
allowin
is the
(7)
of more
cent. p

(8) month discou

### RULE

(9) able 9 (10)payabl presen (11)payabl £859. (12)able 1 £70.1

RULE

### UTOR'S

h to the

	Dec.
)4	334
73	303
15	275
	244
34	214
53	183
3	153
12	122
1	91
1	61
5	30
5	365

o. t the

paid 9

nonths ·152d. aonths

grs. ote of 1? 54d.

Ans

DISCOUNT.

Case 2. When p, r, and t are given, to find s.

### RULE prt + p = s.

ASSISTANT.]

(5) If the present worth of a sum of money due 9 months hence, allowing £5. per cent. per annun, be £344..11..6. 3.168 qrs., what was the sum due ?\*

(6) A person owing a certain sum, payable 7 months hence agrees with the creditor to pay him down £267..13..10152d., allowing £5. per cent. per annum for present payment : what is the debt? Ans. £275..10.

(7) A person receives  $\pounds 859..3..3..3.01824$  grs. for a sum of money due 5 months hence, allowing the debtor  $\mathcal{L}4\frac{1}{2}$ , per cent. per annum for present payment: what was the sum due ? Ans. £875..5..6.

(8) A person paid £70..11..9.1764d. for a debt due 15 months hence, being allowed  $\pounds 5$ . per cent. per aunum for the discount. How much was the debt? Ans. £75.

Case 3. When s, p, and t are given, to find r.

RULE.  $\frac{s-p}{nt}=r.$ 

(9) At what rate per cent. per annum will  $\pounds 357..10$ , payable 9 months hence, produce £344..11..6..3.168 grs. for present payment ?†

(10) At what rate per cent. per annum will £275..10., payable 7 months hence, be worth £267..13..10.152d. for present payment? Ans. £5. per cent.

(11) At what rate per cent. per annum will £875..5..6., payable 5 months hence, produce the present payment of £859..3..3..3.01824 grs.? Ans. £41. per cent.

(12) At what rate per cent. per annum will £75., payable 15 months hence, produce the present payment of £70..11..9.1764d. Ans. £5. per cent.

Case 4. When s, p, and r are given, to find t.

RULE. 
$$\frac{s-p}{pr} = t$$

\*  $344.5783 \times .05 \times .75 + 344.5733 = £357..10$ . Ans.

 $\frac{1}{344\cdot5783} \frac{357\cdot5-344\cdot5783}{344\cdot5783} = 05 \text{ or } \pounds 5. \text{ per cent. Ans.}$ 

### EQUATION OF PAYMENTS.

#### [TUTOR'S

 $\frac{s}{rt+1} = p.$ 

equated time.

(13) The present worth of £357..10., due at a certain time to come, is £314..11..6..3.168 grs. at £5. per cent. per annum : in what time should the sum have been paid without any discount ?\*

(14) The present worth of £275..10., due at a certain time to come, is £267..13..10.152d. at £5. per cent. per annum: in what time should the sum have been paid without discount? Ans. 7 months.

(15) A person receives £859..3..3.01824 grs. for £875.. 5.6., due at a certain time to come, allowing  $\pounds 4\frac{1}{2}$ . per cent. per annum discount : in what time should the debt have been discharged without any discount? Ans. 5 months.

(16) I have received £70..11..9.1764d. for a debt of £75., allowing the person £5. per cent. per annum for prompt payment : when would the debt have been payable without discount? Ans. 15 months.

### EQUATION OF PAYMENTS.

### To find the equated time for the payment of a sum of money due at several times.

RULE. Find the present worth of each payment for its respective time by Case 1, Discount, page 138, thus :---

Add all the present worths together, call their  $\frac{s'-p'}{p'r} = e$ , the Add all the present worths together, call their by Case 4, Discount, p. 139.†

357.5-344.5783 -=:75=9 months. Ans.  $344.5783 \times .05$ 

† The above is Kersey's Rule. It produces a result something less than the precise truth, but sufficiently accurate for any purpose of real The only Rule that is strictly true for the equation of two payutility. ments at Simple Interest is that given by Malcolm, which is founded on the principle, that the interest of the money withheld after it becomes due, ought to be equal to the discount of that which is paid before it is due. But Malcolm's Rule, though it has been simplified in expression by Bonnycastle and others, and is capable of further simplification than I have yet seen in print, is at best very operose, and may be regarded, as Mr. Keith justly observes, as a useless curiasity .- EDITOR.

### ASSIS

(1 mont time allow (2mont they at th requ ·(3  $\pounds 20$ the e men The

> т and in S Rule Prop Α per at 3 3 4

and -

+1 Inter born eithe to co the c

### [TUTOR'S

tain time annum : hout any

tain time annum : hout disnonths. or £875.. per cent. ave been nonths. of £75., prompt

without

oney due

= p.

= e, the ated time.

thing less se of real *f two pay*bunded on *t becomes efore it is* xpression tion than regarded,

### ASSISTANT.]

### COMPOUND INTEREST.

(1) D owes E £200., whereof £40. is to be paid at three months, £60. at 6 months, and £100. at 9 months: at what time may the whole debt be paid together, discount being allowed at £5. per cent. per annum?\*

(2) D owes E £800., whereof £200. is to be paid in 3 months, £200. at 4 months, and £400. at 6 months; but they agree to have the whole paid at once, allowing discount at the rate of £5. per cent. per annum. The equated time is required. Ans. 4 months, 22 days.

(3) E owes F  $\pounds$ 1200., which is to be paid as follows:  $\pounds$ 200. down,  $\pounds$ 500. at the end of ten months, and the rest at the end of 20 months; but they agree to have only one payment of the whole, discounting at  $\pounds$ 3. per cent. per annum. The equated time is required. Ans. 1 year, 11 days.

### COMPOUND INTEREST.

THE same symbols are adopted in this as in Simple Interest, and denote the same things; except that the *ratio* (r,) which in Simple Interest denotes the *interest* of £1., signifies in this Rule the *amount* of £1. for a year. It may be thus found by Proportion.

As  $\pounds 100 : \pounds 105 : : \pounds 1 : \pounds 1.05$ , the ratio at  $\pounds 5$  per cent. per annum. The ratios are, therefore,

at	3 per	cent.	•	•	•	1.03 a	t 4 <u>1</u> pe	er cent.		1.045
	31	"		•	•	1.035	$5^{-}$	"	•	1.05
	4			•	•	1.04	$5\frac{1}{2}$	"	•	1.055, &c.

 $\frac{40}{1\cdot0125} = 39\cdot5061; \frac{60}{1\cdot025} = 58\cdot5365; \frac{100}{1\cdot0375} = 96\cdot3855;$ then  $200 - \overline{39\cdot5061 + 58\cdot5365 + 96\cdot3855} = 5\cdot5719;$ 

and  $\frac{5 \cdot 5719}{194 \cdot 4281 \times \cdot 05} = \cdot 57315 = 6$  months, 26 days. Ans.

<sup>+</sup> The law of England does not allow the lender to receive *Compound Interest* for his money when the receipt of the Interest has been forborne. But in the granting or purchasing of Annuities, Leases, &c., either immediate or in reversion, it is customary, and indeed necessary, to compute them on the principles of *Compound Interest*, for otherwise the calculation would involve meet corregious injustice and absurdity.

[TUTOR'S

### COMPOUND INTEREST.

A Table of the Amount of £1. for years.

			imount of L			
Yrs	3 per Cent.	34 per Cent.	4 per Cent.	4. per Cent.	5 per Cent.	
1	1.0300000	1.0350000	1.0.100000	1.0450000	1.0200000	1
2	1.0609000	1.0712250	1.0816000	1.0020250	1.1025000	
3	1.0927270	1.1037179	1.1248640	1.1411661	1.1576250	
4	1.1255038	1.1475230	1.1698586	1.1925186	1.2155062	
5	1.1592741	1.1876863	1.2166529	1.2461819	1.2762816	
6	1.1940523	1.2292553	1.2653190	1.3022601	1.3400956	
7	1.2298739	1.27.227.93	1.3159318	1.3603618	1.4071004	
8	1.2667701	1.3168090	1.3685690	1.4221006	1.1774554	
9	1.3047732	1.3628974	1.4233118	1.4860951	1.5513282	
10	$1 \cdot 3 \cdot 4 3 9 1 6 1$	1.4105938	1.4802443	1.5529694	1.6288946	
11	1.3842339	1.4599697	1.5394541	1.6228530	1.7103394	
12	1.4257609	1.5110687	1.6010322	1.6958814	1.7958563	
13	1.4685337	1.5639561	1.6650735	1.7721961	1.8856491	
14	1.5125897	1.6186945	1.7316764	1.8519449	1.9799316	
15	1.5579674	1.6753438	1.8009435	1.9352824	2.0789282	
16	1.6047064	1.7339360	1.8729812	2.0223702	2.1828746	
17	1.6528476	1.7946756	1.9479005	$2 \cdot 1133768$	2.2920183	
18	1.7024334	1.3574392	2.0258165	2.208 1788	2.4066192	
19	1.7535060	1.9225013	$2 \cdot 1063492$	2.3078603	2.5269502	
20	1.8061112	1.9397389	2.1911231	2.4117140	2.6532977	
21	1.8602946	2.0594315	2.2787681	2.5202412	2.7859626	
22	1.9161034	2 1315116	2.3699183	2.6336520	2.9252607	
23	1.9735865	22061145	2.4647155	2.7521663	3.0715237	
24	2.0327941	2.2833285	$2 \cdot 5633042$	2.8760133	3.2250999	
25	2.0937779	2.3632450	2.6658363	3.0054345	3.3863549	
26	2.1565913	2.4159586	2.7724698	3.1406790	3.5556727	
27	2.2212890	2.5315671	2.8833686	3.2820096	3.7334563	
28	2.2879277	2.6201720	2.9937033	3.4297000	3.9201291	
29	2.3565655	2.7118780	3.1186514	3.5840365	4.1161356	
30	2.4272625	2.8067937	3.2433975	3.7453181	4.3219424	
31	2.5000803	2.9050315	3.3731334	3.9138574	4.5380395	
32	2.5750327	3.0067076	3.5030587	4.0399810	4.7649414	
33	2.6523352	3.1119423	3.6433811	4.2740302	5.0031885	
<b>34</b>	2.7319053	3.2508603	3.7943163	4.4663615	5.2533479	
35	2.8138624	3.3335904	3.9460890	4.6673478	5.5160153	
36	2.8982783	3.4502661	4.1039325	4.8773785	5.7918161	
37	2.9852266	3.5710254	4.2680898	5.0968605	6.0814069	
38	3.0747834	3.6960113	$4 \cdot 4388134$	5.3262192	6.3854773	
<b>39</b>	3.1670269	3.8253717	4.6163660	5.5658991	6.7047511	
40	3 2620378	3.9592597	4.8010206	5.8163645	7.0399887	

These tabular numbers are the successive powers of r; thus,  $1.05^2$  =  $\therefore 1025$ , &c.\*

\* The am of  $\mathcal{L}1$  in t years is the last term of an increasing geo metrical series, of which the first term = the ratio, and the number of terms = t, because the first year's amount is identical with the ratio; and as  $1: r:: r: r^2$  = the amount in 2 years, as  $1: r:: r^2: r^3$  = the amount in 3 years, &c. The successive amounts  $r, r^2, r^3$ , &c., are evidently in geometrical progression, and the amount in t years is ASSIST

RULE Or by pal and (1) per ann (2) per ann (3) per ann (4) cent. p

(5)

£260.. (6) £243...

(7) *qrs.* in

 $= r^4$ , bed ring to Z such las The in for a longer the with the

thing, ph Christian ry, would this sum When, h coin such gold, cace quate ide adscittion understa The an

1s. 103d. \* 1.05

+ 260.

UTOR'S

Cent.

000

000 250

062

816

956

004

554

282

946 394

563

491 316

282 746

183

192

502 977

626

607

237

999 549 727

563

291

356

424

395

414 885

479

153

161

069

773

511

887

1.052=

ng geo

nber of

ratio;

s = thezc., are rears is

#### ASSISTANT.]

#### COMPOUND INTEREST.

#### Case 1. When p, r, and t are given, to find a.

RULE. pr'=a. Or, log.  $r \times t + \log$ .  $p = \log$ . a.

Or by the Table. Multiply the tabular amount of £1. by the principal and the product will be the amount required.

(1) What will £225, amount to in 3 years, at £5. per cent. per annum?\*

(2) What will £200. amount to in 4 years, at £5. per cent per annum? Ans. £243..2..0..1.2 qrs

(3) What will £450. amount to in 5 years, at £4. per cent. Ans. £547..9..10..2.0538368 grs. per annum?

(4) What will £500. amount to in 4 years, at £41. per cent. per annum ? Ans. £596..5..2.232075d.

Case 2. When a, r, and t are given, to find p.

RULE.  $\frac{a}{d} = p$ . Or,  $\log a - \log r \times t = \log p$ .

(5) What principal, being put to interest, will amount to £260..9..3 $\frac{3}{4}$ . in 3 years, at £5. per cent. per annum ?†

(6) What principal, being put to interest, will amount to £243..2..0..1.2 qrs. in 4 years, at £5. per cent. per annum? Ans. £200.

(7) What principal will amount to £547..9..10..2.0538368 grs. in 5 years, at £4. per cent. per annum? Ans. £450.

 $= r^4$ , because the *index* always corresponds with the time. By referring to Theorem VII, Geometrical Progression, it will also be seen that such last term  $= r \times r^{t-1} = r^t$ , when a = r.

The immense increase of money accumulating at Compound Interest for a long period is sufficient to astonish the human mind, and to stagger the credibility of persons who are not in some degree conversant with the properties of Geometrical Progression. The amount of a farthing, placed out at Compound Interest at the commencement of the Christian era, and continued to the conclusion of the eighteenth century, would be 144035 quintillions of pounds. But of the magnitude of this sum, spoken of in the abstract, no just conception can be formed When, however, by a further calculation, we have ascertained that to coin such a quantity of money (were it possible) in sovereigns of the present weight and fineness, would require 60,308170 solid globes of gold, each as large as the earth, we are enabled to entertain a more adequate idea of the sum whose vastness, without having recourse to this adscititious assistance, placed it almost beyond the reach of our limited understandings.

The amount at Simple Interest, for the same period, would be only 1s. 103d.--EDITOR.

- \*  $1.05^3 \times 225 = 1.57625 \times 225 = 260.465625 = \pounds 260..9..3$  Ans
- $+ \frac{260 \cdot 465625}{1 \cdot 05^3} \frac{260 \cdot 465625}{1 \cdot 157625} = \pounds 225. Ans.$

### COMPOUND INTEREST

[TUTOR'S

(8) What principal will amount to £596..5.. $2\cdot 232075d$ . in 4 years, at £4 $\frac{1}{2}$ . per cent. per annum? Ans. £500.

Case 3. When p, a, and t are given, to find r.

RULE.  $\frac{a}{p} = r^{t}$ , the root of which, being extracted, will give r. Or,  $\log a - \log p \div t = \log r$ .

(9) At what rate per cent. per annum will £225. amount to £260..9..33. in 3 years ?\*

(10) At what rate per cent. per annum will £200. amount to £243..2..0..1.2 qrs. in 4 years? Ans. £5. per cent.

(11) At what rate per cent. per annum will £450, amount to £547..9..10..2.0538368 grs. in 5 years? Ans. £4. per cent.

(12) At what rate per cent. per annum will  $\pounds 500$ . amount to  $\pounds 596 \cdot 2593003125$  in 4 years? Ans.  $\pounds 4\frac{1}{2}$ , per cent.

Case 4. When p, a, and r are given, to find t.

RULE.  $\frac{a}{p} = r^2$ , which being continually divided by r till nothing remains, the number of the divisions will be equal to t.

Or,  $\log. a - \log. p + \log. r = t.t$ 

(13) In what time will £225. amount to £260..9..3 $\frac{3}{4}$ . at £5. per cent. per annum ?‡

(14) In what time will £200. amount to £243..2.025s. a  $\pounds$ 5. per cent. per annum? Ans. 4 years.

(15) In what time will  $\pounds 450$ . amount to  $\pounds 547...9..10$ 2.0538368 grs. at  $\pounds 4$ . per cent. per annum? Ans. 5 years.

(16) In what time will  $\pounds 500$ . amount to  $\pounds 596 \cdot 2593003125$ at  $\pounds 4\frac{1}{2}$ . per cent. per annum? Ans. 4 years.

#### THE AMOUNT OF ANNUITIES IN ARREARS.

Note. u represents the annuity, persion, or yearly rent; a, r, and t as before.

\* 260.465625 = 1.157625, and <sup>8</sup> / 1.157625 = 1.05, or £5. per cent. Ans

+ In all cases of this nature t cannot be found without Logarithms, unless it be a whole number.

 $\ddagger \frac{260 \cdot 465625}{225} = 1.157625; \frac{1.157625}{1.05} = 1.1025; \frac{1.1025}{1.05} = 1.05; \frac{1.05}{1.05} = 1.05$ 

the number of divisions being three. which gives the time sought = 3 years. Ans.

**72212.1** 

Yrs.
0.0
4
5
7
9
11
12 13
14 15
16
18
19 20
21 99
23
25
26 27
28 29
30
$\begin{array}{c} 1\\ 2\\ 3\\ 4\\ 5\\ 6\\ 7\\ 8\\ 9\\ 10\\ 11\\ 12\\ 13\\ 14\\ 15\\ 16\\ 17\\ 18\\ 19\\ 20\\ 21\\ 22\\ 23\\ 24\\ 25\\ 26\\ 27\\ 28\\ 29\\ 30\\ 31\\ 35\\ 6\\ 37\\ 36\\ 37\\ 36\\ 37\\ 36\\ 37\\ 37\\ 36\\ 37\\ 36\\ 37\\ 37\\ 37\\ 36\\ 37\\ 37\\ 37\\ 37\\ 37\\ 37\\ 37\\ 37\\ 37\\ 37$
34
35
37
39

18 £1., a

1=3

### TUTOR'S

075*d*. in £500.

•

give r.

. amount

. amount r cent. . amount per cent. . amount r cent.

ill nothing l be eq:1al

.9..33. at

·025s. a years. 7..9..10 years. 3003125 years.

a, r, and t

cent. Ans

ogarithms,

 $; \frac{1 \cdot 05}{1 \cdot 05} = 1 \cdot$ ought = 3

ASSISTANT.]

COMPONND INTEREST.

A Table of the amount of £1. annuity for years.

Yrs.	management of		Column and succession of	cnt.	4 per	Cent.	11 per	Cent.	5 per Ce	nt.
1	1.00	00000	1.000	0000	1.90	00000	1.00	00000	1.00000	09
2	2.03	00000	2.035	0000	2.04	00000	2.04	50000	2.0200	00
3		09000		2250	3.15	16000		0250	3.15250	000
4		36270				64640	4.278	31911	4.31012	50
5	5.30	91358	5.362	1659	5:41	63226	5.171	07097	5.52563	12
6	6.46	84099	6.550	1522	6.63	297.55	6.710	53916	6.30191	23
7	7.66	24622	7.779	1075	7-89	82945	8.011	1517	8.14200	84
8	8.89	23361	9.051	3860	9.21	42263	9.33(	0135	9.54910	33
9	10.15	91062	10.368	1958	10.58	27953	10.80:	21141	11.02656	49
10	11.46	38794	11.78	.932	12.00	61071	12.233	3:200:2	12.57789	24
11	12.80	77950	13-1 . 10	1 20	13.48	63514	13.91	1786	14-20678	70
12	14.19	20297	14.66	1.17	15.02		15.4	0316	15.91712	
13	15.61	77306	16-145	,304	16:62	68377	17.15	09130	17.71298	27
14	17.08	63243	17:6769	0865	18.29	19112	18 93	21091	19.59863	18
15	18:59	89140	19.295	5810,	20.02	35876	20-73	10540	21.57356	34
16	20.15	68814	20.971	1298	21.32	45311	22.711	03364	23.65749	16
17		15878	22.705			75123			25.84036	
18	23.41	44354	24.4996	5914		54128	26.85.	56334	28.13233	
19	25.11	68685	26.357	1806	27.67	12293	29.06:	35622	30.53900	
20	26.87	03745	28.2790	\$819	29.77	80785	31.371	1225	33.06595	
21	28.67	64857	30.269	1703	31.96	0.016	33.78	1365	35.71925	16
22		67203					36.30		39.50521	
23	32. 5		34.460		36.61		35.937		41.430.47	
24		64702			39.03		41.685		44.50199	
25	36.45	92643	38.9498	3569	41.61	59032	41.56	2023	47.72702	
26	38.55	30422	41.313	019	14.21	17445	47.570	13 1 12	51.11345	
27		96335	43.7590		47.03		50.711		54.66912	
28		09225					53.905		58.402589	
29		88502			52.96		57.425		62.32271	
30	47.57	54157	51.6220				61.007		66.43884	
31	50.00	26789	54.429		59:32	-	64 755	-	70.76078	_
32		27585			62.70		68.666		75-29882	
:5	55.07		60.3415		56.20		72.750		80.06377	
34	57.73		63.453		69.85		77.030		85.03395	
35	60.46		66.6740		73.65		81-496		90.32030	
36	63.27		70.007		77.59		86.163		95.836329	
37	66.17		73.4578		81.70		91.041		95.83632 101.62813	
:8	69.15		77.0288		85.970		96.138		107.70954	
39	72.23		80.724				101.464		114.005029	
40			84.5505				107.030		120.79977:	
10		1~0.00	01 0.10.	110	50 030	10100	107-030	0227	120.799/73	33

Note: The preceding Table is formed thus: the first year's amount is  $\mathfrak{L}_1$ , and  $1 \times 1.05 + 1 = 2.05$ , the second year's amount;  $2.05 \times 1.05 + 1 = 3.1523$ , the third year's amount. &c.

d

### COMPOUND INTEREST

TUTOR'S

Case 1. When u, t, and r are given to find a.

RULE. 
$$\frac{r-1}{r-1} \times u = a$$
.

146

Or, by the Table. Multiply the tabular amount of £1. annuity by the given annuity, and the product will be the amount required.

(17) What will an annuity of £50: per annum amount to in 4 years, at £5. per cent. per annum ?\*.

(18) What will a pension of £45. per annum, payable yearly, amount to in 5 years, at £5. per cent. per annum? Ans. £248..13s..3.27 grs.

(19) If an annual salary of £40. be forborne 6 years, at £4. per cent. per annum, what is the amount?'

Ass. £265..6..4..2.25775616 grs.

(20) If an annuity of £75., payable yearly, be omitted to be paid for 10 years, what is the amount at £5. per cent. per annum? Ans. £943..6..10.0656d.+

Case 2. When a, r, and t are given, to find u.

RULE.  $\frac{r-1}{d-1} \times a = u$ .

(21) What annuity, being forborne 4 years, will amount to  $\pounds 215..10..1$ , at  $\pounds 5.$  per cent. per annum ?

(22) What pension, forborne 5 years, will amount to £248. 13s..3.27 grs. at £5. per cent. per annum? Ans. £45.

(23) What salary, being omitted to be paid 6 years, will amount to £265..6..4..2.25775616 grs. at £4. per cent. per annum? Ans. £40.

(24) If the payment of an annuity, being forborne 10 years, amount to £943..6..10.0656d. at £5. per cent. per annum, Ans. £75. what is the annuity?

Case 3. When u, a, and r are given, to find t.

•  $\frac{1\cdot05^4-1}{\cdot05} \times 50 = (1\cdot21550625-1) \times 1000 = 215\cdot50625 = 2215$ . 10..11. Ans.

Or, by the Table, thus: 4.310125 × 50 = £215.50625. as before.

·05 × 215·50625 .05 × 215·50625 - ·05 × 1009 - £50. Ane. 1.0.74 - 1 21550625

459187 RULI

(25)10 34 (26)135..3 ance e (27)6..4..2

(28)6..10 of pay

Noti Simple tirely u the jud real ut are, ho studen an opp the fals ple Int ing obs The calcula Note, r rate, w than th (by the The at Sim pound naity o ties, pa is ovide

0.5

being c the yea

ASSISTANT.

RULE.  $\frac{(r-1)a}{u} + 1 = r^{t}$ , which being continually divided by r till nothing remains, the number of divisions will be equal to t.

(25) In what time will £50. per annum amount to £215.. 10 11. at £5. per cent. per annum, for non-payment?"

(26) In what time will £45. per annum amount to £248. 13s..3.27 grs. allowing £5. per cent. per annum for forbearance of payment? Ans. 5 years.

(27) In what time will £40. per annum amount to £265 6.4..2.25775616 grs. at £4. per cent. per annum?

Ans. 6 years.

(28) In what time will £75. per annum amount to £943.. 6..10.0656d. allowing £5. per cent. per annum for forbearance of payment? Ans. 10 years.

NOTE. The examples relating to the Present Worth of Annuities at Simple Interest are now expunged from this work, because, being entirely useless, except as a mere arithmetical exercise, it is presumed that the judicious teacher will prefer the substitution of other matter of more real utility which is introduced to supply their place. The Theorems are, however, retained in a note, page 148, in order that the ingenious student, who may wish to calculate any example both ways. may have an opportunity of indulging his curiosity, and of comparing the true and the false results. That the principle of computing their value by Simple Interest is erroncous and absurd, will be manifested by the following observations :---

The present worth of an annuity of £150., to continue only 40 years, calculated at £5. per cent. per annum, Simple Interest, (by Theorem 1, Note, page 148,) would be £3950. But this sum, put out at the same rate, will produce £197..10. annual interest (or £47..10. a year more than the proposed annuity) for ever. If computed on the true principle, (by the Theorem, Case 1, page 149,) the present value is £2573..17..3.

The present value of any perpetual annuity (great or small) computed at Simple Interest, is an unlimited or infinite sum; but by using Compound Interest, we shall obtain a rational result. For instance, an annaity of £150., to continue for ever, will, (by Case 1, Perpetual Annuities, page 152,) at £5. per cent., be worth £3000. purchase; which, it is evident, is the sum that will yield £150. annual interest.-EDITOR.

 $\frac{0.5 \times 215 \cdot 50625}{1} + 1 = \cdot 001 \times 215 \cdot 50625 + 1 = 1 \cdot 21550625; \text{ which}$ being continually divided by 1.05, the number of divisions will be 4 the years required. Ans.

AND AND AND

nuity by

ount to

payable um? qrs. ears, at

grs. itted to ent. per 6d.+

iount to

£248. £45. rs, will ent. per £40. ) years, annum, £75.

£215 .

efore.

Ano.

### COMPOUND INTERBST.

[TUTOR'S.

### THE PRESENT WORTH OF ANNUITIES.\*

A Table of the present worth of £1. annui'y for years.

	10 00 1	1.1			
	states an or management survey with the			4 per Cont. 5 per Ce	nt.
1	0.9708738		0.9615385	0.9569378 0.95238	
2	-1.9134697			1.8726677 1.85941	
3	2.8286114			2.7439643 2.72324	81
4	3.7170984			3.5875256 3.54595	
ð	4.5797072	4.5150524	4.4518223	4.3899766 4.32947	68
6	5.4171915	5:3285530	5.2421368	5.1578723 5.07569	22
. 7	6.2303330	6.1145440	6.0020546	5.8927008 5.78637	35
1 8'	7.0196922			6-5958859 6-46321	29
9	7.7861039	7.6076866	7.4353315	7.2687903 7.10782	18
10	8-5302028	8.3166054	8.1108956	7.9127180 7.72173	51
11	9.2526241	9.0015511	8.7604765	8.5289167 3.30641	44
12	9.9540040			9.1185806 8.86325	
13	10.6349553			9.6828522 9.39357	
14	11-2960731	10.9205203			
15	11.9379350	11.5174109	11.1183872	10.7395455 10.37965	83
16	12:5611019	12.0741168	11.6522954	11-2340148 10-83776	98
17	13.1661183				
18		13.1896817		12.1599916 11.68958	
19	14.3237989		-13-1339391		
20	14.8774747				
21	15.4150240				
22	15.9369165				
23	16.4436083			1	
24	16.9355420				
25	17.4131476			14.8282088 14.09394	
26	17.8763423			15.1466113 14.37518	
20	18.3270314				
28	18.7641032				
29	19.1834546				
30	19.6004414			16.2883884 15.37245	
31		18.7362757	17.5894933	16.5443908 15.59281	
32 33	20:3887656 20:7657919			$16.7888907 15.80267 \\ 17.0228649 16.00254$	
33	21.1318368			17.2467578 16.19290	
34	21.1318.308			17.4610122 16.37419	
		1			
36	21.8322526			17.6660404 16.54685	
37	22.1672355			17.8622396 16.71128	
38	22.4924617			18.0409900 16.86789	
39		21.1024998		18.2296555 17.01704	
10	33.1147721	21.3550723	19.7927735	18.4015842 17.15908	65

\* Present Worth of Annuities at Simple Interest.

Theor. I.  $\frac{r(t-1)+2}{2tr+2} \times tu = p$ . If  $\frac{tr+1}{(r.(t-1)+2).t} \times 2p = 0$ .

ABSIS

Noti presen to the 2 years 2.7232

Case

RUL

Or, given i require

(29 contin (30 annun

(31 to cor

(32 worth

RUL

(33

IV

For Rev for Rev cording Interes

\* 30 ÷ ·05 = Or, i UTOR'S.

Cent. 

 $p = \mathbf{n}$ 

#### ABSISTANT.]

Note. The above table is thus formed:  $\pounds 1. \div 1.05 = .9523810$ , the present worth of the first year; this  $\div 1.05 = .9070295$ , which added to the first year's present worth, gives 1.8594105, the present worth of 2 years; then  $.9070295 \div 1.05$ , and the quotient added to 1.3594105 = 2.7232481, the present worth of 3 years, &c.

Case 1. When u, t, and r are given, to find p, the present worth.

RULE. 
$$(u-\frac{u}{r^4})\div (r-1)=p.$$

Or, by the Table. Multiply the tabular present worth for the time given by the giver multy, and the product will be the present worth required.

(29) What is the present worth of an annuity of £30., to continue 7 years, at £5. per cent. per annum ?\*

(30) What is the present worth of a pension of  $\pounds$ 40. per annum, to continue 8 years, at  $\pounds$ 5. per cent. per annum? Ans.  $\pounds$ 258..10.6..3.264 ors.

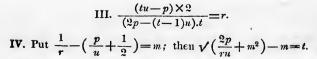
(31) What is the present worth of an annual salary of £35,
 to continue 7 years, at £4. per cent. per annum?
 Ans. £210.1.5.04d.

(32) What is the yearly rent of £50., to continue 5 years, worth in ready money, at £5. per cent. per annum? . Ans. £216..9..5..2.08 qrs.

Case 2. When p, t, and r are given, to find u.

RULE.  $\frac{pr^t(r-1)}{r^t-1}=u.$ 

(33) If an annuity be purchased for  $\pounds 173..11..10.08d.$ , to



For Annuities in Reversion, it is only necessary to observe the Rules for Reversionary Annuities at Compound Interest, and to calculate (according to the directions therein given) by the Theorems for Simple Interest.

\*  $30 - \frac{30}{1 \cdot 05^7} = 30 - \frac{30}{1 \cdot 4071} = 30 - 21 \cdot 3204 = 8 \cdot 6796$  and  $8 \cdot 6796$ 

÷ .05 = £173.592 = £173.11..10.03d. Ans.

Or, by the Table, 5.7863735 × 30 = £173.591205. Ans.

### COMPOUND INTEREST.

TUTOR'S

be continued 7 years, at £5. per cent. per annum, what is the annuity ?\*

(34) If £258..10..6..3.264 qrs. be paid down for a salary 8 years to come, at £5. per cent. per annum, what is the salary? Ans £40.

(35) If the present payment of  $\pounds 210..1..504d$ , be required for a pension for 7 years to come, at  $\pounds 4$ , per cent. per annum, what is the pension ? Ans.  $\pounds 35$ .

(36) If the present worth of an annuity, 5 years to come, be  $\pounds 216..9..5..2.08$  qrs. at  $\pounds 5.$  per cent. per annum, what is the annuity ? Ans.  $\pounds 50.$ 

Case 3. When u, p, and r are given, to find t.

RULE. p+u-pr

which being continually divided by r till nothing remains, the number of divisions will be equal to t.

(37) How long may a lease of £30. yearly rent be had for £173..11..10.08*a*., allowing £5. per cent. per annum to the purchaser ?†

(38) If £258..10..6..3.264 qrs. is paid down for a lease of £40. per annum, at £5. per cent. per annum, how long is the lease purchased for? Ans. 8 years.

(39) If a house is let upon lease for £35. per annum, and the lessor disposes of the lease for £210..1..5.04d., allowing after the rate of £4. per cent. per annum, what term of the lease remains unexpired? Ans. 7 years.

(40) For what time is a lease of £50. per annum purchased, when present payment is made of £216..9..5.. $2\cdot08$  qrs., at £5. per cent. per annum? Ans. 5 years.

#### ANNUITIES, ETC., IN REVERSION.

To find the present worth of annuities in reversion.

RULE 1. Find the present worth of the annuity, for the time of its continuance, as if it vore to commence immediately, by Case 1. page 149. Then find what principal will amount to that sum in the given

\*  $173 \cdot 592 \times 1 \cdot 4071 \times \cdot 05 \div \cdot 4071 = 12 \cdot 213 \div \cdot 4071 = \pounds 30$ . Ans. Or, by the Table,  $173 \cdot 592 \div 5 \cdot 7863735 = \pounds 30$ . Ans.

+  $173 \cdot 592 + 30 - (173 \cdot 592 \times 1.05) = 203 \cdot 592 - 182 \cdot 2716 = 21 \cdot 3204$ ; and  $30 \div 21 \cdot 3204 = 1 \cdot 4071$ ; which being continually divided by 1.05, the number of divisions will be 7: therefore t = 7 years. Ans. Or, by the Table,  $173 \cdot 592 \div 30 = 5 \cdot 7864$ ; and referring to the column of 5 per cert, we find the number  $5 \cdot 7863735$  against 7 years. ASSIS

time ( 143,)

> Ru comm the p nuity prese

No

Ru (by ( found quire

> (4)£40 till t the I (4) £60 till t the I (4) 4 ye

term to bonu to bo

To.

Ri nuity be th Ca

. (4

10·1:

TUTOR'S

ASSISTANT.]

at is the

a salary  $\pounds$  is the  $\pounds 40.$ required annum,  $\pounds 35.$ o come, what is  $\pounds 50.$ 

by r till divisions

had for a to the

ease of g is the years. and allowing h of the years. burchas-08 qrs., years.

n.

me of its 1. page he given

Ans.

21.3204; by 1.05, Or, by of 5 per COMTOUND INTERIST.

time before the annuity commences, (by Case 2, Compound Interest, page 143,) which will be the present worth.

**RULE 2.** Find the present worth of a similar annuity supposed to commence immediately, and continue during the whole period; and also the present worth of the same till the time when the reversionary annuity actually commences, and the difference of these two will be the present value required.

NOTE When calculating by the Table, this is the most eligible method.

RULE 3. Find the amount of the annuity at the time of its cessation. (by Case 1, page 146.) and the present worth of that amount (being found by Case 2, Compound Interest, page 143) will be the value required.

(41) What is the present worth of a reversion of a lease of  $\pounds 40$ . per annum, : 2 continue for 6 years, but not to commence till the end of 2 years, allowing  $\pounds 5$ . per cent. per annum to the purchaser ?\*

(42) What is the present worth of a reversion of a lease of  $\pounds 60$ . per annum, to continue 7 years, but not to commence till the end of 3 years, allowing  $\pounds 5$ . per cent. per annum to the purchaser? Ans.  $\pounds 299..18..216d$ .

(43) A house is let at £30. per annum on a lease, of which 4 years are yet up expired, and which the lessee is desirous of renewing at the same rental, to continue 7 years beyond the term of the present lease. What will the lessor expect as a *bonus* for such a renewal of the lease, considering the house to be worth double the present rent, and allowing interest for the money now advanced at £5. per cent. per annum?

Ars. £142..16..3..1.152 qrs.

To find the annuity in reversion which a given sum will purchase.

RULE. Find the amount of the given sum for the time before the annuity commences, by Case 1, Compound Interest, page 143, which will be the value of the annuity at its commencement.

Call this value p, and then find the annuity as in Case 2, page 149.

(44) What annuity, to be entered upon 2 years hence, and

\*  $40 - \frac{40}{1 \cdot 05^6} = 40 - \frac{40}{1 \cdot 3400956} = 40 - 29 \cdot 84861 = 10 \cdot 15139$ ; and 10 \cdot 15139 \dots \cdot 05 = 203 \cdot 0278; then 203 \cdot 0278 \dots 1 \cdot 05^2 = £184 \cdot 1522 == £184 \cdot 8.0 \cdot 0.2 \cdot 112 \quad qrs. Ans.

[TUTOR'S

then to continue 6 years, may be purchased for £184..3..0.. 2.112 grs. at £5. per cent. per annum?\*

(45) The present worth of a lease, taken in reversion for 7 years, but not to commence till the end of three years, is  $\pounds 299..18..2\cdot 16d.$ , allowing  $\pounds 5$ . per cent. per annum to the purchaser: what is the yearly rent? Ans.  $\pounds 60.$ 

(46) There is a lease that has yet 4 years to run, and the lessee has purchased the reversion of a renewed lease, at the same rental of  $\pounds$ 30. per annum, for the term of 7 years, commencing at the expiration of the present lease, for which he has paid down  $\pounds$ 142.16..3..1·152 grs. What increase of rent is reckoned on the property according to this contract, allowing  $\pounds$ 5. per cent. per annum for present payment? Ans.  $\pounds$ 30.

PERPETUAL ANNUITIES, OR FREEHOLD ESTATES.

Case 1. When u and r are given, to find p, the present worth, or purchase money.

RULE.  $\frac{w}{r-1} = p.t$ 

(47) What is the worth of a freehold estate of £50. yearly rent, allowing £5. per cept. per annum to the buyer ?

(48) What is a real estate of £140. per annum worth in present money, allowing £4. per cent. per annum to the purchaser? Ans. £3500.

(49) What must the purchaser give for a freehold estate of  $\pounds 437..10$ . yearly rent, so as to make  $\pm 3\frac{1}{2}$ . per cent. per annum by the investment of his capital? Ans.  $\pounds 12500$ .

Case 2. When p and r are given, to find u.

RULE.  $p \times r - 1 = u$ .

(50) If a freehold estate is bought for £1000., what must

* $164 \cdot 1522 \times 1 \cdot 1025 = 203 \cdot 0278$ ; then $203 \cdot 0278 \times 1 \cdot 3400956 \times \cdot 05$
•3400956
$203.0278 \times 1 + (203.0278 \times .3400956)$ 203.0278
$\frac{203.0278 \times 1 + (203.0278 \times 3400956)}{\cdot 3400956} \times \cdot 05 = \frac{203.0278}{\cdot 3400956} + 203.0278 \times \cdot 05 = 800.0005 \times \cdot 05 = \pounds 40. Ars.$
+ $203.0278 \times .05 = 800.0005 \times .05 = \pounds 40.$ Ans. Or, by the Table, $184.1522 \div (6.4632129 - 1.8594105) = 184.1522 \div 4.6038024 = \pounds 40.$ Ans.

t This rule is deduced from the formula in page 149; for, in Annul ties continuing for ever, t is *infinite*, and the subtractive quantity  $n \div r^i = o$ ; therefore the theorem assumes the above form.

\$ 50 ÷ 05 = £1000. Ans.

ASSISTAN

be the ye num inte (51) I rent allo

(52) ] yield the yearly re

RULE.

(53) what is (54) £3500.

(55) sold for

To fit RULE. immediat (p) to be previous principal

(56) hold of ailowing for his (57) estate of

per cent before t

• 1000 † 50 † 50 ± 50 ÷ • 432 gr.

### TUTOR'S

4.....

sion for rears, is to the  $\pounds 60$ . and the e, at the rs, comhich he of rent , allows.  $\pounds 30$ .

. t warth,

orth in he pur-500. state of per an-500.

at must

3

1522 ÷

Annui Intity # ASSISTANT.]

### COMPOUND INTEREST.

be the yearly rent, to pay the purchaser £5. per cent. per annum interest for his money ?\*

(51) If an estate be sold for £3500., what is the yearly rent allowing to the purchaser £4. per cent. per annum?

Ans. £140.

(52) If a freehold estate is bought for  $\pounds 12500.$ , and will yield the purchaser  $\pounds 3\frac{1}{2}$ . per cent. per annum, what is the yearly rent? Ans.  $\pounds 437..10.$ 

Case 3. When p and u are given, to find r.

Rule.  $\frac{u}{p} + 1 = r$ .

(53) If an estate of £50. per annum is bought for £1000., what is the rate per cent. per annum ? $\dagger$ 

(54) If a freehold estate of  $\pounds$ 140. per annum is sold for  $\pounds$ 3500., what interest will it pay to the purchaser?

Ans. £4. per cent.

(55) If an estate in perpetuity of £437..10. per annum is sold for £12500., what interest will it pay to the purchaser? Ans. £3 $\frac{1}{2}$ . per cent.

### FREEHOLD ESTATES IN REVERSION.

To find the present worth of a freehold estate in reversion.

**BULE.** Find the value of the estate, supposing it were to come into summediate possession, as in Case 1, page 152. Then suppose that value (p) to be a, and find what principal will amount to a in the time to come, previous to possession, by Case 2, Compound Interest, page 143. Such principal will be the present value.

(56) What must be paid down for the purchase of a freehold of  $\pm 50$ . per annum, to be entered upon 4 years hence, allowing the purchaser at the rate of  $\pm 5$ . per cent. per annum for his purchase money ?‡

(57) What must be paid down for the reversion of a real estate of £200, per annum, so as to pay the purchaser £4. per cent. per annum for his capital, supposing 2 years to elapse before the estate comes into possession?

Ans. £4622..15..7..1.76 qrs.

- 1000 × ·05 = £50. Ans.
- $\frac{50}{1000} + 1 = 1.05 = \text{\pounds}5. \text{ per cent. Ans.}$

\$ 50 ÷ ·05 = 1000; then 1000 ÷ 1·2155 = £822.7067 = £822..14..1.. \$•432 grs. Ans

#### COMPOUND INTEREST.

154

TUTOR 8

(58) A freehold, producing  $\pounds 280$ . annual rent, is to be disposed of, with a reserve of the next 3 years' rent to the present proprietor. What is it worth in ready money, allowing  $\pounds 31$ . Let cent. per annum to the purchaser?

Ans. £7215..10..9..3.36 qrs.

### To find the yearly rent of an estate in reversion, having its present value given.

**RULE.** Find the amount of the given present value in the *time before* possession: thus,  $pr! \equiv a$ . Then consider that amount to be the present value (p) of the perpetual annuity, and find the annuity thus:  $p \times (r-1) \equiv u$ .

(59) What must be the rent of a freehold property, to come into possession 4 years hence, for which  $\pounds 822..14..1..2.432$  qrs. is paid down, allowing the purchaser  $\pounds 5$ . per cent. per annum?\*

(60) A freehold estate is sold for  $\pounds 4622..15..7..1$ .76 qrs., the vender reserving to himself the first two years' rent. Required the annual value to pay the purchaser  $\pounds 4$ . per cent. per annum for his capital. Ans.  $\pounds 200$ .

(61) A freehold estate has been purchased for £7215..10.. 9..3.36 qrs., the possession of which is not to be given up till after the expiration of 3 years. What must be the annual rent to pay the purchaser at the rate of £31/2. per cent. per annum? Ans. £280.

#### DISCOUNT, ON THE PRINCIPLES OF COMPOUND INTEREST.

NOTE. The following Table is constructed by the continual division of 1 by the ratio (r): thus 1 - 1.05 = .9523810, the first year's present worth; then .9523810 - 1.05 = .9070295, the second year's present worth; and .9070295 - 1.05 = .8638376, the third, &c.

\*  $822.70625 \times 1.2155 \pm 1000$ ; then  $1000 \times .05 \pm \pounds 50$ . Ans.

† This is merely a repetition of the various cases in Compound Interest. For instance, to find the present worth of any debt due some time hence, is precisely the same operation as finding what principal will amount to that sum in the given time; and this observation will equally apply to the identity of the other cases. The entire omission, therefore, of *Discount*, (at *Compound Interest*,) arranged under that specific head, would be no detrinicat to the learner. It is, however, retained here, for the sake of those who may think some repetition of the subject desirable.—EDITOR. ASSIST

A Table

Yrs.

12

3

4

5

6

78

9

10

11

12 13

14

15

16

17

18

19 20

21

22

23 24

25 26

27

28

29

30 31 32

33

34

35

36

37

38

39

### TUTOR 8

to be disthe preallowing

36 grs.

aving its

ime before the present thus: pX

, to come ..1..2.432 cent. per

1.76 grs., ent. Reper cent. £200. 7215..10.. en up till ie annual cent. per £280.

EREST.

ual division ar's present r's present

ns.

npound Int due some at principal vation will e omission, er that speowever, reASSISTAN'T.]

1

2

3

4

31

32

33

34

35

36

37

38

39

40

 $\cdot 3999872$ 

·3883370

·3770263

·3660449

·3553834

·3450324

 $\cdot 3349829$ 

·3252262

·3157536

·3065568

·3442304

 $\cdot 3325897$ 

 $\cdot 3213427$ 

 $\cdot 3104761$ 

 $\cdot 2999769$ 

·2898327

·2800316

·2705619

·2614125

 $\cdot 2525725$ 

·9708738

·9425959

·9151417

·\*888·1870

### COMPOUND INTEREST.

		0.000.101.0	0/11100	0.710012	0000010	00001020
0.	5	·8626088	·8419732	·8219271	·8024510	·7835262
	6	·8374843	·8135006	.7903145	.7678957	•7462154
	7	·8130915	.7859910	.7599178	.7348285	•7106813
	8	.7894032	.7594116	·7306902	.7031851	·6768394
	9	·7664167	·7337310	·7025867	.6729044	·6446089
	10	•7440939	•7089188	·6755641	·6439277	·6139133
	11	.7224213	·6849457	·6495809	·6161937	·5846793
	12	·7013799	·6617833	·6245970	·5896639	•5568374
	13	·6809513	•6394041	:6005741	·5642716	.5303214
	14	.6611178	.6177818	.5774751	•5399729	·5050680
	15	-6418619	·5968906	•5552645	.5167204	•4810171
	16	·6231669	•5767059	.5339082	.4944693	•4581115
	17	.6.50164	•5572038	•5133732	•4731764	•4362967
	18	·5873946	·5383611	·4936281	·4528004	4155207
	19	·5702860	.5201557	4746424	•4333018	·3957340
	20	·5536758	·5025659	-4563869	•4146429	·3768895
	21	·5375493	•4855709	·4388336	·3967374	·3589424
	22	·5218925	·4691506	·4219554	·3797009	·3418499
	23	·5066918	•4532856	•4057263	•3633501	·3255713
	24	$\cdot 4919337$	·4379571	·3901215	•3477035	
	25	·4776056	·4231470	·3751168	·3327306	2953028
	26	·4636947	•4088377	·3606892	·3184025	·2812407
	27	·4501891	·3930122	·3468166	•3046914	·26784\$3
	28	·4370769	·3816543	·3334775	-2915707	2550936
	29	$\cdot 4243464$	·3687482	·3206514	·2790150	·2429463
	30	·4119868	·3562784	·3033187	·2670000	·2313774
						and the second s

·2964603

·2850579

·2740942

 $\cdot 2635521$ 

 $\cdot 2534155$ 

·2436687

·2342963 ·2252854

 $\cdot 2166206$ 

2082890

·2555024

·2444999

-2339712

·2238959

·2142544

2050282

 $\cdot 1961992$ 

·1877 504

·17964.55

11 6.17

2203595

·2098662

 $\cdot 1998725$ 

+1903548

·1812903

·1726574

1644356

 $\cdot 1566054$ 

 $\cdot 1491480$ 

·1420457

A Table of the present worth of £1. due any number of years hence from 1 to 40.

Yrs. 3 per Cent. 31 per Cent. 4 per Cent. 41 per Cent. 5 per Cent.

·9661836

 $\cdot 9335107$ 

.9019427

·8714422

·9615385

·9245562

·8339963

·8548042

·9569378

 $\cdot 9157299$ 

·8762966

·8385613

.9523810

·9070295

·8638376

.8227025

COMPOUND INTEREST.

### Case 1. To find the present worth of any sum due after a cer tain period.

RULE. The same as in Case 2, Compound Interest, considering a as the debt whose present value is required.

(1) If £344..14..9..1.92 grs. be payable in 7 years' time, what is the present worth, discount being made at £5. per cent. per annum ?\*

(2) A debt of £409..9.00992s., payable 4 years hence, is agreed to be paid in present money : what sum must the creditor receive, discounting at £4. per cent. per annum 7 Ans. £350.

### Cuse 2. To find the debt whose present worth is given.

### RULE. - See Case 1, Compound Interest.

(3) If £245, be received for a debt payable 7 years hence, allowing £5. per cent. per annum to the debtor for present payment, what is the debt ?†

(4) There is a sum of money due at the expiration of 4 years, but the creditor agrees to take £350. in ready money, allowing £4. per cent. per annum discount. What was the Ans. £409.9.00992s. debt?

### Case 3. When the rest are given, to find the time.

### RULE. Soo Cuso 4, Compound Interest.

(5) A person receives £245. now for a debt of £344. 14..9.. 1.92 grs., discounting at £5. per cent. per annum: in what time was the debt payable ?!

(6) There is a debt of £409..9 00992s. due a certain time hence, but £4. per cent. per annum being allowed to the debtor for the present payment of £350., it is required to find in what time the sum was to be paid. Ans. 4 years.

Case 4. When the rest are given, to find the rate per cent. ROLE. As in Case 3, Compound Interest.

(7) The present worth of £344..14..9..1.92 grs., payable

\* 344.7395 ÷ 1.4071 = £245. Ans. \*

Or, by the Table, 7105813 × 344.7395 = £245. Ans.

+ 245 × 1.4071 = £344.7395 = £344..14..9..1.92 grs. Ans.

\$ 344.7395 - 245 = 1.4071; the continual divisions of which by 1.05 will be 7 == the number of years. Ans.

ASSIS'I

7 year discou (8) but it the rat

RUL add the that pr equate

2. F: till the the las of the from th equate

(1)debt c end o £5. p (2)three of the annun (3) vears.

ought per co

ARE ing t amon and la

\* 34 per ce t Fo see th

TUTOR'S

UTOR'S

r a cer

ing a as

s' time, C5. per

ust the im? 350.

en.

hence, present

on, of 4money, was the 092s.

8.

n what

he debtfind in *jears*.

cent.

payable

1 by 1.05

### ASSISTANT.]

### DUODECIMALS.

7 years hence, is  $\pounds 245$ ., at what rate per cent. per annum is discount allowed ?\*

(8) There is a debt of  $\pounds 409..9 \cdot 00992s$ . payable in 4 years, but it is agreed to take  $\pounds 350$ . present payment. Required the rate of discount. Ans.  $\pounds 4$ . per cent.

### EQUATION OF PAYMENTS AT COMPOUND INTEREST.

RULE 1. Find the present worth of each payment respectively; and add them together for the whole present worth : then the time in which that present worth will amount to the sum of the debts will be the true equated time required.

2. Find the amount of each dobt from the time of its becoming due till the time of the last payment, and add the respective amounts and the last payment into one sum. Then find the time in which the sum of the debts would amount to that sum of the amounts: subtract this from the time of the last payment, and the difference will be the true equated time.

(1) Required the true equated time for the payment of a debt of £400. of which £320. is now due, and the rest at the end of 5 years; reckoning compound interest at the rate of £5. per cent per annum. Ans. 90714 years.

(2) If  $\pounds 100$ . will become due one year hence, and  $\pounds 104$ . three years hence, what is the true equated time for payment of the whole, allowing compound interest at  $\pounds 4$ . per cent. per annum? Ans. 2 years.

(3) If a person will have to receive £200, at the end of 3 years, and £80, more at the end of 5 years, in what time ought he to receive the whole at one payment, allowing £5 per cent. per annum, compound interest?

Ans. 3.5518 years.

### DUODECIMALS

ARE so named from the integer of each denomination containing twelve of the next inferior. They are in general use among artificers for computing the quantities of their materials and labour; both in Superficial and Solid Measure.<sup>†</sup>

\*  $344.7395 \div 245 = 1.4071$ ; and '1/1.4071 = 1.05; which gives £5. per cent. Ans.

† For a clear and intelligible explanation of the different Measures see the Tables, page 24, &c.

### DUODECIMALS.

### 12 inches (') make 1 foot. 12 seconds ('') ...... 1 inch, or prime.

12 thirds ("") ...... 1 second, &c.

### To multiply duodecimally.

RULE 1. Under the multiplicand write the corresponding terms of the multiplier.

2. Multiply by the feet in the multiplier, observing to carry one for every twelve, from each lower denomination to the next superior.

3. In the same manner multiply by the inches in the multiplier, setting the result from each term one place farther to the right.

4. Proceed in like manner with the remaining denominations, and the sum of the products will be the total product.

NOTE 1. Length and breadth multiplied together produce the area of a superficies; and this multiplied by the thickness, produces the solid content of a body.

2. It is generally more eligible to take *cliquot parts* ont of the multiplicand for the inches, &c., in the multiplier.

-		0	,		,	~		,,,		0				
(1)	3.6 1.	ft.		"		ſt	•			- f.,	'	"		""
(1)	Mult.	7	9		by	3	6'							
(2)	Mult.	8	5		by	4	7		Ans.		6	11		
(3)	Mult.	9	8		by		6		a.	72	6	0		
(4)	Mult.	8	1		by	3	5		<i>a</i> .	27	7	5		
(5)	Mult.	7	6		by	5	9		<i>a</i> .	43	1	.6		
(6)	Mult.	4	7		by	3	10		а.	17	.6	10	-	
(7)	Mult.	7	5	9	by	3	5	3	<i>a</i> .	25	8	6	2	3.
(8)	Mult.	10	4	5	by	7	8	6	2.	79	11	0	6	6.
(9)	Mult.	75	7		by	9	8		a.	730	7	8		
(10)	Mult.	97	8		by	8	9		a.	854	7	0		
(11)	Mult.	57	9		by	9	5		a.	543	9	9		
(12)	Mult.	75	9		by	17	7		<i>a</i> .	1331	11	3		
(13)	Mult.	87	5		by	35	8		<i>a</i> .	3117	10	4		5
(14)	Mult.	179	3		by	38	10		a.	6960	10	6		
(15)	Mult.	259	2		by	48	11		a. ]	2677	6	10		
(16)	Mult.	257	9		by	39	11			0288	6	3		
(17)	Mult.	311	4	7	by	36	7	5		1402	2	4	11	11.
(18)	Mult.		7	3	by	9	3	6		2988	2	10	4	6.
ft.	in.		in	. (	Dther	wise		P	roof by	Decin	als.			-
* 7	9				37	9		-	7.7					
3 6 3 3.5														
	3				23	3			387	5				
3 1	These and the second se					-	6"		2325	_				
27	G				27	1	6		27.12	5 sq. 1	cet		4.	2

A381

6

[TUTOR's

wor F Joint R B (1) 'ne 6 fe of e cost (2) ing per (2)

by 1

long (2

of w

at 3. (2 squa 54 fe (2 heig 2s. 8

(2 inche yard

rutor's

ns of the

one for or. lier, set-

and the

the area

e multi

111 111

3.

6.

1 11.

ASSISTANT.]

#### DUODECIMALS.

Glazing, Masons' flat work, and some parts of Joiners' work, are computed at so much per square foot.

Painters', Plasterers', Pavers', and some descriptions of Ioiners' work, are estimated by the square yard.

Roofs, Floors, Partitions, Sc., by the square of 100 feet. Bricklayers' work by the square rod, containing 2721 feet

(19) A certain house has 3 tiers of windows, 3 in a tier the height of the first tier being 7 feet 10 inches, the second 6 feet 8 inches, and the third 5 feet 4 inches, and the breadth of each window is 3 feet 11 inches. What will the glazing cost at 14d. per square foot ?\*

(20) What is the price of 8 squares of glass, each measuring 4 feet 10 inches long, and 2 feet 11 inches broad, at 41d. per square foot? Ans. £1..18..9.

(21) What is the value of 8 squares, each measuring 3 feet by 1 foot 6 inches, at  $7\frac{3}{4}d$ . per square foot? Ans. £1..3..3.

(22) What is the price of a marble slab 5 feet 7 inches long and 1 foot 10 inches broad, at 6s. per square foot?

Ans. £3..1..5.

(23) What will be the expense of ceiling a room the length of which is 74 feet 9 inches, and the width 11 feet 6 inches, at  $3s. 10\frac{1}{2}d$ . per square yard? Ans. £18.10.1.

(24) What will the paving of a court-yard cost at  $4\frac{3}{4}d$ . per square yard, the length being 58 feet 6 inches, and the breadth 54 feet 9 inches? Ans. £7..0..10.

(25) The circuit of a room is 97 feet 8 inches, and the height 9 feet 10 inches: what is the charge for painting it, at 2s.  $8\frac{3}{4}d$ . per square yard? Ans. £14..11.2.

(26) What is the expense of a piece of wainscot 8 ieet 3 inches long and 6 feet 6 inches broad, at 6s.  $7\frac{1}{2}d$ . per square yard? Ans. £1..19..5.

ft in	··· ···
ft. in. * 7 10	$an. ft. in. 6 = \frac{1}{2}$ 19 10
	$0 = \frac{1}{2} = \frac{19}{10} = \frac{10}{11}$
5 4	$in. \frac{11}{218}$
19 10 the whole height.	$3 = \frac{1}{2}  9  11$
3 11	8. 4 11 6"
3	$1 = \frac{1}{20} 233  0  6 \text{ at } 14.$
11 9 the whole breadth.	d
bearing the second seco	$2 = \frac{1}{6} \pounds 11 \ 13 \ 0$ the value at 1.
	1 18 11 the volue of 94
valu	$10 \text{ of } 6'' = 0 \ 0 \ 0 \ 1$
	£13 11 101 Ans.

[TUTOR'S

(27) What will the paving of a court-yard cost at 3s. 2d. per square yard, the length being 27 feet 10 inches, and the breadth 14 feet 9 inches? Ans.  $\pounds 7..4..5$ .

(28) A certain court-yard is 42 feet 9 inches in front, and 68 feet 6 inches long; a causeway the whole length, and 5 feet 6 inches broad, is laid with Furbeck stone, at 3s. 6d. per square yard, and the rest is paved with pebbles, 2t 3s. per square yard. What is the expense? Ans. £43..17..04.

(29) What will the plastering of a ceiling cost at 10d. per square yard, supposing the length 21 feet 8 inches, and the breadth 14 feet 10 inches? Ans.  $\pounds 1.9.9$ .

(30) What will the wainscoting of a room cost at 6s. per square yard, supposing the height of the room (including the cornice and moulding) is 12 feet 6 inches, and the compass 83 feet 8 inches; the three window shutters each 7 feet 8 inches by 3 feet 6 inches, and the door 7 feet by 3 feet 6 inches? The shutters and door being worked on both sides, are reckoned work and half-work. Ans.  $\pounds 36..12..21$ .

(3!) In a piece of partitioning 173 feet 10 inches long, and 10 feet 7 inches in height, how many squares?

Ans. 18 squares, 39 feet, 8' 10".

(32) A house of three stories, besides the ground floor, measuring 20 feet 8 inches by 16 feet 9 inches, is to be floored at  $\pounds 6..10$ . per square: there are 7 fire-places, two of which measure 6 feet by 4 feet 6 inches each, two others 6 feet by 5 feet 4 inches each, two other 2 5 feet 8 inches by 4 feet 8 inches each, and the seventh 5 feet 2 inches by 4 feet, and the well-hole for the stairs is 10 feet 6 inches by 8 feet 9 inches. What will the whole amount to ?

Ans. £53..13..34.

(33) If a house measures within the walls 52 feet 8 inches in length, and 30 feet 6 inches in breadth, the roof being of a true pitch, what will it cost roofing at 10s. 6d. per square? Ans.  $\pounds 12..12..11$ .

Notr. A roof is said to be of a true pitch when the rafters are **1** of the breadth of the building. In this case, therefore, the breadth must be accounted equal to the breadth and half-breadth of the building.

(34) What will the tiling of a barn cost at 25s. 6d. per square, the length being 43 feet 10 inches, and the breadth 27 feet 5 inches on the flat, the eave-boards projecting 16 inches on each side ? Ans.  $\pounds 24..9..53$ .

Nors. Bricklayers compute their work at the sys of a brick and

ASSISTA

a half this must be a the wall the produ

\*(35) two bric standard (36) inches h tain ?

(37) feet 8 in

(38) length; inches; courses to the his bricks th and the whole w

To multi

RULE. multiplier multiply t which add the tens i hundreds product of multiplier, multiplier through, b

First, 4 and 1 that  $+(3 \times 2)$ ly,  $(5 \times 4)$ and carry + 4 carries  $+(2 \times 2)$ 

In thi

### ASSISTANT.]

#### DUODBCIMALS.

a half thick; therefore, if the thickness of a wall is more or less, it must be reduced to the standard thickness by multiplying the area of the wall by the number of half bricks in the thickness, and dividing the product by 3.

\*(35) If the area of a wall is 4085 feet, and the thickness two bricks and a half, how many rods does it contain of the standard thickness? Ans. 25 rods, 8 feet.

(36) If a garden wall is 254 feet in compass, 12 feet 7 inches high, and 3 bricks thick, how many rods does it contain? Ans. 23 rods, 136 feet.

(37) How many rods are there in a wall  $62\frac{1}{3}$  feet long; 14 feet 8 inches high, and  $2\frac{1}{3}$  bricks thick ?

### Ans. 5 rods, 167 feet.

(38) The end wail of a house is 28 feet 10 inches in length; the height of the roof from the ground is 55 feet 8 inches; and the gable (or triangular part at the top) rises 42 courses of bricks, reckoning 4 courses to a foot. The wall ' to the height of 20 feet is  $2\frac{1}{2}$  bricks thick, 20 feet more, 2 bricks thick, and the remaining part a brick and a half thick; and the gable is 1 brick thick. What is the charge for the whole wall, at £5..16. per rod ? Ans. £48..13..5 $\frac{1}{2}$ .

To multiply several figures by several, and obtain the product in one line only.

RULE. Multiply the units of the multiplicand by the units of the multiplier, set down the units of the product, and carry the tens; next multiply the tens in the multiplicand by the units of the multiplier, to which add the product of the units of the multiplicand multiplied by the tens in the multiplier, and the tens carried; then multiply the hundreds in the multiplicand by the units of the multiplier, adding the product of the tens in the multiplicand multiplied by the tens in the multiplier, and the units of the multiplied by the tens in the multiplier, and the units of the multiplied by the tens in the multiplier; and so proceed till you have multiplied the multiplicand all through, by every figure in the multiplier.

#### EXPLANATION.

First,  $4 \times 4 = 16$ , that is 6 and carry 1. Secondly,  $(3 \times 4) + (4 \times 2)$ and 1 that is carried = 21, set down 1 and carry 2. Thirdly,  $(2 \times 4) + (3 \times 2) + (4 \times 4) + 2$  carried = 32; that is, 2 and carry 3. Fourthly,  $(5 \times 4) + (2 \times 2) + (3 \times 4) + (4 \times 2) + 3$  carried = 47; set down 7 and carry 4. Fifthly,  $(3 \times 4) + (5 \times 2) + (2 \times 4) + (3 \times 2) + (4 \times 3) + 4$  carried = 60; set down 0 and carry 6. Sixthly,  $(3 \times 2) + (5 \times 4) + (2 \times 2) + (3 \times 5) + 6$  carried = 51; set down 1 and carry 5. Sev

• In this and the three following examples the rod is considered = 272 feet.

ORS

:. 2d. l the .5. , and nd 5 . per . per ų. . per the .9. . per g the ss 83 ches hes? eckţ.

, and

floor, oored hich et by set 8

and et 9

t. ches of a ? ?

g. g.

per adth g 16 <del>3</del>.

bas :

enthly,  $(3 \times 4) + (5 \times 2) + (2 \times 5) + 5$  carried = 37; set down 7 and carry 3. Eighthly,  $(3 \times 2) + (5 \times 5) + 3$  carried = 34; set down 4 and carry 3. Lastly,  $3 \times 5 + 3$  carried = 18; set down 18, and the work is finished.

### MENSURATION OF SUPERFICIES.

### GEOMETRICAL DEFINITIONS.

GEOMETRY is the science which investigates the nature and properties of lines, angles, surfaces, and solid bodies.

A point has no parts or magnitude.

A line has length only, without breadth or thickness.

A line drawn wholly in the same direc-

tion, or the shortest distance between two points, is a *right* or *straight line*. That which continually changes its direction is a curve.

Parallel lines preserve the same distance from each other throughout; and therefore would never meet, though infinitely produced.

An angle is the degree of inclination of two lines, or the opening between them when they meet in a point; which is called the angular point.

When a line meeting another inclines not either way, but makes equal angles on each side, those are called right angles; and the lines are perpendicular to each other. Thus the angle ADC = the angle BDC.\*

An oblique angle is either acute or obtuse. An acute angle is less than a right angle, as BDE; and an obtuse angle, greater than a right angle, as ADE.

\* When more than two lines meet, forming several angles at the same point, it is necessary to designate cach angle by three letters, placing that which is at the angular point in the middle. Thus, the angle BDC is that formed by the knew BD and CD.



TUTOR'S

### ASSISTAN

A supe and has t A solid three din A tria quadrang A righ an obtuse angled tr An equ the three An iso A scal A pare equal an called a is a squa A rhor A rhor equal. All ot that has The b stand; a perpendi height. Right. polygons one of s A circ called th from the tains mo A stra the circa

ameter ;<sup>h</sup> centre to An are

Figs. 1
The lin
Fig. 7

### ASSISTANT.] MENSURATION OF SUPERFICIES.

A superficies or surface is a space contained within ines and has two dimensions, length and breadth.

A solid is a space or body bounded by surfaces, and has three dimensions, length, breadth, and thickness.

A triangle is a superficies bounded by three lines. A quadrangle, or quadrilateral, is bounded by four lines.

A right-angled triangle has one right angle, (Fig. page 116,) an obtuse-angled triangle has one obtuse angle, and an acuteangled triangle has all its angles acute.

An equilateral triangle has the three sides (and consequently the three angles) all equal to each other.

An isosceles triangle has two equal sides.

A scalene triangle has all the three sides unequal.

A parallelogram is a quadrangle having the opposite sides equal and parallel.<sup>a</sup> When the angles are right ones, it is called a *rectangle*.<sup>b</sup> And a rectangle having all its sides equal is a square.<sup>a</sup>

A rhombus has all its sides equal, but oblique an cles.<sup>d</sup>

A rhomboid has oblique angles, and only its opposite sides equal.

All other quadrilaterals are *trapeziums*; but a trapezium that has two sides parallel is called a *trapezoid*.

The base<sup>f</sup> of a figure is the side on which it is supposed to stand; and a line drawn from the vertex, or opposite angle, perpendicular to the base, is the *altitude*,<sup>f</sup> or perpendicular height.

Right-lined plane figures of more than four sides are called *polygons*. A polygon of five sides (or angles) is a *pentagon*, one of six a *hexagon*, &c. Vide Table, page 166.

A circle<sup>g</sup> is a plane figure, contained under one curve line, called the circumference, which is in every part equidistant from the centre, or middle point within it. The circle contains more space than any other plane figure of equal compass.

A straight line passing through the centre, and meeting the circumference in two opposite points, is called the *diameter*,<sup>h</sup> and half the diameter, or the distance from the. centre to the circumference, is the *radius*.<sup>1</sup>

An arc of a circle is any portion of the circumference.\*

Figs. 1, 2, and 3. <sup>b</sup> Fig. 2. <sup>c</sup> Fig. 1. <sup>d</sup> Fig. 3. <sup>c</sup> Fig. 5.
<sup>f</sup> The line AB, Figs. 3 and 4, is the *base*, and CD the *altitude*.
<sup>g</sup> Fig. 7. <sup>h</sup> The line AB Fig. 7. <sup>l</sup> AC or BC. <sup>k</sup> AD or ADB, Fig. 8.

UTOR'S

wn 7 and wn 4 and work is

une and

B

te angle

e angle,

the same

he angle

### MENSURATION OF SUPERFICIES.

TUTOR'S

A chord is a right line joining the extremes of an arc.<sup>1</sup>

The versed sine is part of the diameter cut off by the chord.<sup>m</sup>

A segment is a space contained between an arc and its chord.<sup>n</sup> A semicircle is a segment, the chord of which is the diameter.

A sector is bounded by an arc and two radii.<sup>o</sup> When the two radii are at right angles it is a *quadrant*, or fourth part of the circle.

The circumference of every circle is supposed to be divided into 360 equal parts, called degrees; and each degree into 60 equal parts, called minutes, &c.

The measure of an angle is determined by the number of degrees in the arc of a circle contained between the two lines forming the angle, described round the angular point as a centre Thus the angle ACB (Fig. 8.) is an angle of so many degrees as are contained in the arc AB. Hence, a right angle contains 90 degrees.

An ellipse (or regular oval) is a plane figure bounded by a curve called the *circumference*, returning into itself, and described from two points, called the *foci* or *focuses*, in the *transverse* (or longest) *diameter*. The shortest diameter, which intersects the *transverse* at right angles, is called the *conjugate*. The diameters are also called *axes*.<sup>P</sup>

#### MENSURATION.

Problem 1. To find the area of a Parallelogram, whether it be a Square, an oblong Rectangle, a Rhombus, or a Rhomboid.

RULE. Multiply the length by the altitude or perpendicular breadth: the product will be the area.

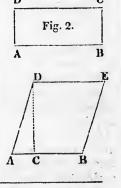


(1) The base of the largest Egyptian pyramid is a square, whose side is 693 feet. Upon how many acres of ground does it stand?

(2) Required the area of a rectangular board, whose length is  $12\frac{1}{2}$  feet, and breadth 9 inches.

": (3) What 'quantity of land does a

1 AB or AD, Fig. 8. " DF. " AEBDA. • Fig. 9. " Fig. 10.



### ABSISTANT.

rhombus co dicular brea

Problem 2.

RULE. Mo

(1) Req yards in a feet, and h (2) Wh of a house, the eaves the perpen middle of

RULE 2. of the sides three remain product will

(3) The and 415 y which it o

### Problem 3 Trapez

RULE. I two triangle the diagona perpendicul half the pro

For a traperpendicul the area

Ho
 um, whose
 33½ feet?
 (2) Fin
 links, ease
 links; and
 angle 483

### UTOR'S

rc.<sup>1</sup> by the

and its h is the

hen the part of

be diviree into

nber of volines nt as a o many nt angle

ed by a and dein the , which e conju-

her it be mboid.



ig. 10.

### ABSISTANT.] MENSURATION OF SUPERFICIES.

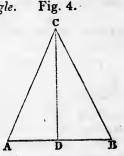
rhombus contain, the base of which is 1490, and the perpendicular breadth 1280 links?

### Problem 2. To find the area of a Triangle. Fig

RULE. Multiply the base by the altitude. and half the product will be the area.

(1) Required the number of square yards in a triangle, whose base is 49 feet, and height  $25\frac{1}{4}$  feet.

(2) What is the area of the gable of a house, the base or distance between the eaves being 22 feet 5 inches, and the perpendicular from the ridge to the middle of the base, 9 feet 4 inches?

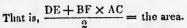


Rule 2. When the three sides only are given.—From half the sum of the sides subtract each side severally: rultiply the half sum and the three remainders continually together; and the square root of their product will be the area.

(3) The three sides of a triangular fish-pond are 140, 336, and 415 yards respectively. What is the value of the land which it occupies, at  $\pounds 225$ . per acre?

# Problem 3. To find the area of a Trapezium, or a Trapezoid.

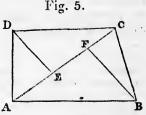
RULE. Divide the *trapezium* into two triangles by a *diagonal*: multiply the diagonal by the sum of the two perpendiculars falling upon it; and half the product will be the area.



For a *trapezoid*. Multiply the sum of the two parallel sides by the perpendicular distance between them; and half the product will be the area.

(1) How many square yards of paving are in the trapezium, whose diagonal is 65 feet, and the perpendiculars 28 and 33½ feet ?

(2) Find the area of a trapezium whose south side is 2740 links, east side 3575, west side 4105, and north side 3755 links; and the diagonal from the south-west to the north-east angle 4835 links.



TUTOR'S

(3) Required the area of a trapezoid whose parallel sides are  $20\frac{1}{2}$  feet and  $12\frac{1}{4}$  feet respectively; the perpendicular distance being  $10\frac{3}{4}$  feet?

(4) How many square feet are in a board, whose length is 121 feet, and the breadths of the two ends 15 inches and 11 inches respectively?

## Problem 4. To find the area of an Irregular Figure.

RULE. Divide it by drawing diagonals into trapeziums and triangles Find the area of each, and their sum will be the area of the whole.

1. Required the content of the irregular figure ABCDEFGA, in which are given the following diagonals and perpendiculars: namely, AC = 5.5

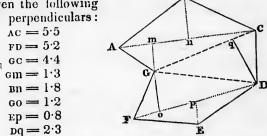


Fig. 6.

B

### Problem 5. To find the area of a Regular Polygon.

RULE 1. Multiply the perimeter (or sum of the sides) by the perpendicular drawn from the centre to one of the sides; and half the product will be the area.

RULE 2. Multiply the square of the side by the corresponding tabnlar area, or multiplier opposite to the name in the following table; and the product will be the area.

No. of sides.	Names of Polygons.	Areas, or Multipliers.
3	Trigon, or Equilateral Triangle	0.4330127
4	Tetragon, or square	1.0000000
5	Pentagon	1.7204774
6	Hexagon	2.5980762
7	Heptagon	3.6339124
8	Octagon	4.8284271
9	Nonagon	6.1818242
10	Decagon	7.6942088
in	Undecagon	9-3656399
112	Duodecagon	11.1961524

ASSISTANT.

(1) Requ 25 feet. (2) Requ

Problem 6.

RULE. As or, as or, as circumference diameter.

(1)) Req is 12.

\* To find ter, and ther the anxie: ly considere mations hav a degree of orbit of the of miles, we ing given) s it so much a in the Rule

† This is of Syracuse era. It ans is not requi

<sup>‡</sup> This we since. It is sixth figure

§ This is who was n laborious in (3.141598, . than 100 p circumstanc division, in ter is given

|| As 7 :

or, as I

or, as 1

TOR'S

sides r dis-

gth is nd 11

e. angles ole.



s. perpenhe pro-

ing tabg table;

MENSURATION OF SUPERFICIES.

(1) Required the area of a regular pentagon whose side is 25 feet.

(2) Required the area of an octagon whose side is 20 feet.

Problem 6. To find the diameter or circumference of a Circle, the one from the other.\*

Fig. 7.

RULE. As 7: 22† or, as 113: 355‡ or, as 1:3·1416§ circumference; and reversing the terms will find the diameter.

(1)) Required the circumference of a circle whose diameter is 12.

\* To find the proportion which the circumference bears to the diameter, and there to find the area of a circle, is a problem that has engaged the anxie. Attention of mathematicians of all ages. It is now general ly considered impossible to determine it exactly; but various approximations have been found, some of which have been carried to so great a degree of accuracy, that in a circle as immense in magnitude as the orbit of the planet Saturn, the diameter of which is about 158 millions of miles, we are enabled to express the circumference (the diameter being given) so nearly approximating to the truth, as not to deviate from it so much as the breadth of a single hair. The three approximations in the Rule are those in general use.

t This is the ratio assigned by Archimēdes, a celebrated philosopher of Syracuse, who flourished about two centuries before the Christian era. It answers the purpose sufficiently well when particular accuracy is not required.

<sup>‡</sup> This was discovered by Metius, a Dutchman, about two centuries since. It is a very good approximation, agreeing with the truth to the sixth figure.

§ This is an abridgment of the celebrated Van Ceulen's proportion, who was nearly contemporary with Metius. By a patient and most laborious investigation, he determined it truly to 36 places of figures, (3.141598, &c.) But it has been since extended to considerably more than 100 places. This proportion is extremely convenient, from the circumstance of the first term being unity; which saves the labour of division, in finding the circumference of any other circle whose diameter is given. It is not quite so accurate as the preceding.

As 7 : 22 :: 12 : $\frac{22 \times 12}{7} = \frac{264}{7} = 37.71428$	15
As 7 : 22 :: 12 : $\frac{22 \times 12}{7} = \frac{264}{7} = 37.71428$ or, as 113 : 355 :: 12 : $\frac{355 \times 12}{113} = 37.69913$	15 ence.4
or, as 1 : 3.1416 :: 12 : 3.1416 × 12 = 37.6592	

TUTOR'S

(2) What is the circumference when the diameter is 25? (3) What is the diameter of a column whose circumference is 9 feet 6 inches?

(4) If the circumference of a great circle of the earth (as the equator) were exactly 25000 miles, what would be the diameter?

### Problem 7. To find the area of a Circle.

RULE 1. The area is equal to a fourth part of the product of the circumference into the diameter, or the product of half the circumference into half the diameter.

Therefore, when the diameter is 1, the area  $=\frac{1 \times 3.1416}{4} = .7354$ ;

### whence we have

RULE 2. Multiply the square of the diameter by '7854, and the pro duct will be the area.

RULE 3. Multiply the square of the circumference by 07958 for the area.

(1) Required the area of the circle proposed in Example 1, Problem 6.\*

(2) Find the area of the circle proposed in Example 2. Problem 6.

(3) What is the area of the end of a roller whose diameter is 2 feet 3 inches?

(4) Required the area when the circumference is  $8\frac{1}{4}$  feet.

### Problem 8. To find the side of a square inscribed in a circle.

RULE. Multiply the radius by 1.4142, (that is, by  $\sqrt{2}$ ,) or multiply the diameter by 7071.1

(1) Find the side of the square inscribed in the circle whose diameter is 12.

(2). What is the side of the square inscribed in a circle whose diameter is 6 feet 5 inches?

•  $\frac{37 \cdot 6992 \times 12}{4} = 37 \cdot 6992 \times 3 = 113 \cdot 0976$  the area. or, 122× 7854 = 12 × 12 × 7854 = 113.0976

The following Rules exhibit the principal relations between the. circle and its equal square, or inscribed square.

#### ABSISTAN'

### Pro

RULE 1. chord of ha the chord o and 1 of th be the le nearly.

That is 3 = arc AI

Note. and the ve which bein

RULE 2. a d the pr

(1) Tl 8. what

(2) W

half are i (3) Re

baing 10

### Probl

RULE 1. the arc by p. oduct w

Ruiz 2. in the arc : he area

(1) Re and the (2) W and the r (3) R and the v

- 6. The
- 7. The 8. The

9. The

By th part of the

all the req

#### MENSURATION OF SUPERFICIES. ABSISTANT.]

### Problem 9. To find the length of a Circular Arc.

RULE 1. From 8 times the Fig. 8. chord of half the arc subtract the chord of the whole arc, and i of the difference will be the length of the arc, nearly.

That is  $AD \times 8 - AB \div$ 3 = arc ADB.

3

Notz. Half the chord of the whole arc, the chord of half the arc, and the versed sine, are sides of a right angled triangle; any two of which being given, the third may be found as directed in page 115.

RULE 2. Multiply the number of degrees in the arc by the radius, a d the product by 01745, for the length of the arc.

(1) The chord of the whole arc is 30, and the versed sine 8. what is the length of the arc?

(2) What is the length of the arc when the chord of the balf arc is 10.625, and its versed sine 5?

(3) Required the length of an arc of 12° 10', the radius being 10 feet.

Problem 10. To find the area of a Sector of a circle.

Fig. 9.

RULE 1. Multiply the length of the arc by the radius, and half the n oduct will be the area.

Rule 2. As 360° : the degrees in the arc : : the area of the circle : the area of the Sector.

(1) Required the area of the sector, when the radius is 15. and the chord of the whole arc 18 feet.

(2) What is the area of a sector whose arc is 147° 29'. and the radius 25?

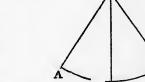
(3) Required the area of a sector, whose radius is 20 feet, and the versed sine 1 foot 9 inches.\*

6. The side of a square  $\times 1.414214 =$  the diameter of its circum-

7. The side of a square  $\times 4.442363 =$  the circumf. scribing circle. 8. The side of a square  $\times 1.128379 =$  the diameter of an equal cir-

9. The side of a square  $\times 3.544908 =$  the circumf. cle.

• By the properties of the circle, the versed sine × the remaining part of the diameter = the square of helf the chord of the arc; whence all the requisites may be found.



th (as be the

TOR'S.

131 rence

the cirference

: .78541

he pro for the

ple 1,

ple 2.

ameter

feet.

circle. ultiply

circle

circle

een the

quare

169

H

#### MENSURATION OF SUPERFICIES. .

[TUTOR'S

(4) What is the area of the sector, when the chord of half its arc is 14 feet 2 inches, and the versed sine 6 feet 8 inches?\*

### Problem 11. To find the area of a Circular Segment.

RELE 1. Find the area of the sector; and also the area of the trisingle formed by the chord and the two radii of the sector: their difference, when the segment is *less* than a semicircle, or their sum, when it is greater, will be the area of the segment.

RULE 2. Divide the height of the segment by the diameter, and find the quotient in the column of heights in the following table. Multiply the corresponding area by the square of the diameter, for the area of the segment.

Table of the Inter of Cheatar legation										
lfeight.	Area (f Segment.	Height.	Arca of Segment.	Height.	Area of Segment.	Height.	Area of Segment.			
.01	+00133	.14	-06683	.26	16226	·39	·28359			
$\cdot 02$	$\cdot 00375$	.15	.07387	.27	.17109	•40	·29337			
.03	.00687	.16	·08111	.28	.18002	•41	·30319			
•04	.01054	.17	·08854	.29	·18905	.42	·31304			
·05	.01468	.18	·09613	.30	·19817	·43	·32293			
.06	.01924	.19	·10390	•31	·20738	•44	·33284			
.07	.02417	.20	.11132	. 32	·21667	•45	$\cdot 34278$			
.08	.02944	.21	·11990	.33	·22603	•46	·35274			
.09	·03501	22	.12811	.34	·23547	•47	$\cdot 36272$			
.10	·04088	23	.13647	.35	24498	•48	·37270			
.11	·04701	-24	.14494	.36	.25455	.49	·38270			
.12	·05339	.25	·15355	·37	·26418	·50	·39270			
.13	·060 <b>0</b> 0			.38	·27386					

### Table of the Arcas of Circular Segments.

(1) What is the area of a segment, when the chord of the whole are is 60, and the chord of half the arc  $37\frac{1}{2}$ ?

\* When the half chord (see AE, Fig. 7) of the arc is found by the properties of a right angled triangle, then  $AE^2 =$  the versed sine (DE) X the remaining part of the diameter; whence the diameter (and consequently the radius) will be known.

<sup>†</sup> When there is a remainder (or fraction) after the second quotient figure, in dividing the height by the diameter; having taken out the area answering to the two figures, add to it such *fractional part* of the *difference* between *that* and the *next succeeding* area, for the sake of greater accuracy.

### ASSISTA

(2) the dian (3) is 2 and (4) is 24, t the arc (5)

the seg

### Problem

RULE. of half th two dian product nearly.\*

(1) ence of verse d jugate (2) spective

### RULE.

(1) F (2) V den, wh (3) F London conjuga

### Problem

RULE. part, and to the qu

\* If th product v purposes

#### ASSISTANT.] MENSURATION OF SUPERFICIES.

(2) What is the area of a segment whose height is 18, and the diameter of the circle 48?

(3) Required the area of a circular segment whose height is 2 and chord 20.

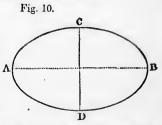
(4) What is the area of the segment of a circle whose radius is 24, the chord of the whole arc 20, and the chord of half the arc 10.2?

(5) If the radius of a circle is 10 feet, what is the area of the segment whose chord is 12 feet?

### Problem 12. To find the circumference of an Ellipse, the trans verse and conjugate diameters being given.

RULE. Multiply the square root of half the sum of the squares of the iwe diameters by 3.1416, and the preduct will be the circumference nearly.\*

(1) What is the circumference of an ellipse whose transverse diameter is 24, and conjugate 18?



(2) The two axes of an ellipse are 60 and 45 yards re spectively: what is the circumference?

### Problem 13. To find the area of an Ellipse.

RULE. Multiply the product of the axes by 7854 for the area.

(1) Required the area of an ellipse whose axes are 35 and 25.

(2) What will be the expense of trenching an elliptic garden, whose axes are 70 and 50 feet, at  $3\frac{3}{4}d$ . per square yard?

(3) Required the area of the ellipse in Grosvenor Square, London, the transverse diameter being 8.40 chains, and the conjugate 6.12 chains.

### Problem 14. To find the area of an Elliptic Segment, the base being parallel to either axis.

RULE. Divide the height of the segment by that axe of which it is a part, and find, in the *Table of Circular Segments*, a versed sine equal to the quotient.

\* If the half sum of the two diameters be multiplied by 3.1416, the product will gi.s the circumference sufficiently near for most practical purposes.

OR'S

half et 8

•

ne tridifferwhen

d find iltiply rea of

of the

270

by the e (DE) conse-

uotient out the of the sake of Multiply the corresponding tabular area and the two axes continu ally together, and the product will be the area required.

(1) What is the area of an elliptic segment cut off by a line (called a double ordinate) parallel to the conjugate diameter at the distance of 36 yards from the centre, the axes being 120 and 40 yards respectively?

(2) Required the number of square yards in the segment of an ellipse, cut off by an ordinate parallel to the transverse diameter; the height being 5 feet, and the two axes 35 and 25 feet respectively.

### A COLLECTION OF QUESTIONS.

(1) WHAT is the value of 14 barrels of soap, at  $4\frac{1}{2}d$ . per *lb.*, each barrel containing 254 *lb.*? Ans. £66..13..6.

(2) A and B joined in partnership; A put into the joint stock £320. for 5 months, and B £460. for 3 months: they gained £100. What is each man's share of the gain?

Ans. A's £53..13..9 $\frac{270}{208}$ , and B's £46..6.. $2\frac{28}{278}$ . (3) How many yards of cloth, at 17s. 6d. per yard, can I have for 13 cwt. 2 qrs. of wool, at 14d. per lb.?

Ans. 100 yards,  $3\frac{1}{5}$  qrs.

(4) If I buy 1000 ells of Flemish tinen for  $\pounds 90.$ , at what price must I sell it per English ell to gain  $\pounds 10$ . by the whole ? Ans. 3s. 4d. per ell.

(5) A has 648 yards of cloth at 14s. per yard, ready money, but in barter will have 16s. B has wine at £42. per tun, ready money: what must he charge it per tun in barter, and what quantity must be given in exchange for the cloth?

Ans. £48. per tun, and the quantity, 10 tuns, 3 hhds., 123 gals.

(6) A jeweller sold jewels to the value of £1200., for which he has received in part 876 French pistoles, at 16s. 6d. each. How much more is due to him? Ans. £477..6.

(7) An oilman bought 417 cwt. 1 qr. 15 lb. gross weight of train oil, tare 20 lb. per cwt.: how many neat gallons were there, allowing  $7\frac{1}{2}$  lb. to a gallon? Ans. 5120 gallons.

(8) If 1 buy cloth at 14s. 6d. per yard, and sell it at 16s 9d., what is the gain per cent.? Ans. £15.10.. $4\frac{4}{25}$ .

(9) Bought 27 bags of ginger, each weighing gross 844 lb., tare 14 lb. per bag, tret as usual: what is the value at 84d. per lb.? Ans. £76..13..24. ASSIST.

(10) (11) cost? (12) £1..7.. nual in (13) of lead

(14) tured a fifth, a What

(15) 10. in (16) worth in case (17) and C and B

(18) manne much

(19) feet 9

(20 provis taining men n due 5 (21 The s (22 cattle and h was th (23)

## ARSISTANT.] A COLLECTION OF QUESTIONS.

(10) If  $\frac{2}{3}$  oz. cost  $\frac{2}{3}s$ . what will  $\frac{2}{6}$  lb. cost? Ans. 17s. 6d. (11) If  $\frac{2}{6}$  of a gallon cost of a  $\pounds$ . what will  $\frac{2}{6}$  of a tun cost? Ans.  $\pounds 105$ .

(12) A gentleman who spends one day with another  $\pounds 1..7..10\frac{1}{2}$ . lays up at the year's end  $\pounds 340$ . What is his annual income? Ans.  $\pounds 848..14..4\frac{1}{2}$ .

(13) What is the difference in ounces, between 13 fothers of lead, and 39 boxes of tin, each box weighing 388 lb ? Ans. 212160 ounces.

(14) A captain, commanding a crew of 160 mariners, captured a prize worth £1360. The captain was allowed onefifth, and the rest was equally divided among the sailors. What was each man's share ?

Ans. The captain had £272. and each sailor £6..16. (15) At what rate per cent. will £956. amount to £1314..

10. in  $7\frac{1}{2}$  years, at simple interest? Ans. £5. per cent. (16) A has 24 cows worth £3.12. each, and B 7 horses worth £13. each. How much will make good the difference,

in case they interchange their droves of cattle? Ans. £4..12. (17) A man left £120. to be given to three persons, A, B,

and C; B to have twice as much  $r \ge A$ , and C as much as A and B; what was the share of each?

Ans. A £20. B £40. and C £60.

(18)  $\pounds$ 1000. is to be divided among three men, in such a manner, that if A has  $\pounds$ 3. B shall have  $\pounds$ 5. and C  $\pounds$ 8. How much will each n n have ?

Ans. A £187..10. B £312..10. and C £500.

(19) A piece of wainscot is 8 feet 6<sup>1</sup>/<sub>2</sub> inches long, and 2 feet 9<sup>2</sup>/<sub>3</sub> in hes broad : what is the superficial content?

Ans. 24 feet 0' 3" 4" 6"".

(20) A garrison of 360 men, who had originally six months' provisions, having endured a siege of 5 months, without obtaining any relief or fresh supply, wish to know how many men mus' depart, that the provisions may suffice for the residue 5 months longer? Ans. 288 men.

(21) The less of two numbers is 187; the difference 34. The square of their product is required. Ans. 1707920329

(22) A butcher sent his man with £216. to a fair to but cattle; he bought oxen at £11. cows at 40s. colts at  $t^{-\mu}$  and hogs at £1..15. each, and of each a like number. What was the number of each ? Ans. 13 of each sort, and £8. or  $t^{-\mu}$ 

(23) What number added to  $11\frac{5}{7}$  will produce  $36\frac{3}{3}\frac{7}{7}$ Ans.  $24\frac{2}{3}\frac{1}{15}$ .

nu.

П.-)е-

ent rse ind

per oint ney

n I

hat the l. ady per ter, h? als hich ach. 5.

t of vere s. 16s

1*b.*, 84d.

ţ.

#### A COLLECTION OF QUESTIONS.

- [TUTOR'S

(24) What number multiplied by  $\frac{3}{7}$  will produce  $11_{\frac{9}{7}}$ ? Ans.  $26\frac{4}{7}$ .

(25) What is the value of 179 hogsheads of tobacco, each weighing 13 cwt. at £2..7..1. per cwt. ? Ans. £5478..2..11.

(26) My factor informs me that he has bought goods on my account, of the value of £500..13..6 What will his commission come to at £31/2. per cent.? Ans. £17..10..5..217/25 qrs

-(27) If  $\frac{1}{3}$  of 6 were three, what would  $\frac{1}{4}$  of 20 be ? Ans.  $7\frac{1}{2}$ (28) Reduce 3 grs. 14 lb. to the decimal of a *cwi*.

Ans. . 875 cwt.

(29) How many lb. of sugar, at  $4\frac{1}{2}d$ . per lb. must be given in barter for 60 gross of inkle, at 8s. 8d. per gross?

Ans. 13862 lb.

(30) If I buy yarn for 9d. per *lb*. and sell it again for  $13\frac{1}{2}d$ per *lb*. what is the gain per cent. ? Ans. £50.

(31) A tobacconist mixes 20 lb. of tobacco at 9d. per lb. with 60 lb. at 12d. per lb. 40 lb. at 18d. per lb. and 12 lb. at 2s. per lb. what is a pound of the mixture worth?

Ans. 1s. 21d. P.

(32) What is the difference between twice eight and twenty, and twice twenty-eight; also between twice five and fifty and twice fifty-five? Ans. 20, and 50.

(33) Whereas a noble and a mark just 15 yards did buy; How many ells of the same cloth for  $\pounds 50$ . had I? Ans. 600 ells.

(34) A broker bought for his principal, in the year 1720  $\pounds$ 400. South Sea stock, at  $\pounds$ 650. per cent. and sold it again when it was worth but  $\pounds$ 130. per cent. What was the whole loss? Ans.  $\pounds$ 2080.

(35) C has candles at 6s. per dozen ready money, but in barter will have 6s. 6d. per dozen; D has cotton at 9d. per *lb*. ready money: what price must the cotton be charged in barter; and how much must be exchanged for 100 dozen of candles? Ans. The cotton at  $9\frac{3}{4}d$ . per *lb*. and the quantity. 7 cwt. 0 qrs. 16 *lb*.

(36) If a clerk's salary is  $\pounds 73$ . a year, what is that pe day? Ans. 4s.

(37) B has an estate of £53. per annum, and pays 5s. 10. to the subsidy: what must C pay, whose estate is worta £100. per annum? Ans. 11s.  $0\frac{4}{53}d$ .

(38) If I buy 100 yards of riband, at 3 yards for a shilling and 100 yards more at 2 yards for a shilling, and sell the ASSIST

whole gain or (39) remains (40) 3s., and the mix

(41) the wh (42) lon. I (43)  $\frac{1}{2}$  of hi the arm 880 gu missior

(44) so that the fou

(45) per cer (46) 4 mont annum (47) ed with wide w (48)

riage p two ye

(49) for a d and to descrip (50) feet 6 deep? (51) sailors ing 22.

#### ASSISTANT.] A COLLECTION OF QUESTIONS.

whole at the rate of 5 yards for 2 shillings; whether do I gain or lose, and how much? Ans. Lose 3s. 4d.

(39) From what number must  $\frac{3}{5}$  be deducted, that the remainder may be  $\frac{1}{8}$ ? Ans.  $\frac{2}{40}$ .

(40) A farmer wishes to mix rye at 4s. a bushel, barley at 3s., and oats at 2s. How much must he take of each to sell the mixture at 2s. 6d. per bushel?

Ans. 6 of rye, 6 of barley, and 24 of oats.

(41) If  $\frac{3}{8}$  of a ship is worth £3740., what is the value of the whole? Ans. £9973..6.8.

(42) Bought a cask of wine for  $\pounds 62..8$ . at 5s. 4d. per gallon. How many gallons were there? Ans. 234.

(43) A dissipated young fellow in a short time got through  $\frac{1}{5}$  of his fortune; he then gave  $\mathcal{L}2200$ . for a commission in the army: his profusion continued till he had no more than 880 guineas left, which was  $\frac{3}{20}$  of his money after the commission was bought. What was his fortune at first?

Ans. £10450.

(44) A sum of money is to be divided amongst four men, so that the first shall have  $\frac{1}{3}$ , the second  $\frac{1}{4}$ , the third  $\frac{1}{6}$ , and the fourth the remainder, which is £28. What is the sum? Ans. £112.

(45) What is the amount of  $\pounds 1000$ . in  $5\frac{1}{2}$  years at  $\pounds 4\frac{3}{4}$ . per cent. per annum, simple interest? Ans.  $\pounds 1261..5$ .

(46) Sold goods, amounting to the value of £700., at two 4 months. What is the present worth at £5. per cent. per annum, simple interest? Ans. £682..19..5 $\frac{1}{4}$ ,  $\frac{1}{150}$ .

(47) A room 30 feet long and 18 feet wide is to be covered with painted cloth. How many yards of three-quarters wide will cover it? Ans. 80 yards.

(48) Betty told her brother George that, though her marriage portion took £19312. out of her family, it was but  $\frac{3}{5}$  of two years' rent. What was his annual income?

Ans. £16093..6..8.

(49) A gentleman having 50s. to pay among his labourers for a day's work, gave to every boy 6d., to every woman 8d, and to every man 16d. There was an equal number of each description. What was that number ? Ans. 20 of each.

(50) What is the solid content of a stone that measures 4 feet 6 inches long, 2 feet 9 means broad, and 3 feet 4 inches deep? Ans.  $41\frac{1}{4}$  sourd feet.

(51) What does the pay of a ship's crew, consisting of 64C sailors, amount to for 32 months' service, each man's pay being 22s. 6d. per month? Ans. £23040.

R's

ach 1. my nis qrs $7\frac{1}{2}$ 

t. ven

b.  $3\frac{1}{2}d$ (). (). (). at

r. nty, ifty

). y; ? s. 720

gain hole D. it in per

d in n o' tity.

pe s. 10. orto d. ling the 176

[TUTOR'S

(52) A traveller would change 500 French crowns, at 4s. 6d. per crown, into sterling money, but he must pay a halfpenny per crown for change. How much sterling money will be receive ? Ans. £111..9..2.

(53) B and C traded together. and gained £100; B put in £640, C put in so much that he was entitled to £60. of the gain. What was C's stock? Ans. £960.

(54) From what principal sum did £20. interest arise in one year, at the rate of £5. per cent. per annum? Ans. £400.

(55) How many French pistoles, at 17s. 6d. each, are equal to 672 Spanish guilders, at 2s. each? Ans. 764.

(56) Out of 7 cheeses, each weighing 1 cwt. 2 qrs. 5 lb., how many allowances for seamen may be cut, each weighing 5 or. 7 drams? Ans. 356333.

(57) If 48 taken from 120 leaves 72, and 72 taken from 9' leaves 19, and 7 taken from thence leaves 12, what numler is that, out of which, when you have taken 48, 72, 19, and 7, leaves 12? Ans. 158.

(58) A farmer, unskilled in numbers, ordered £500. to be divided among his 5 sons, thus: "Give A, says he,  $\frac{1}{3}$ , B  $\frac{1}{4}$ C  $\frac{1}{5}$ , D  $\frac{1}{6}$ , and E  $\frac{1}{7}$  part." Divide this equitably among them according to the father's intention.

Ans. A £152..10..1 $\frac{1}{4}$   $\frac{1}{4}$   $\frac{8}{5}$ . B £114..7..6 $\frac{2}{4}$   $\frac{423}{459}$ . C £91..10..0 $\frac{3}{4}$   $\frac{63}{459}$ . D £76..5..0 $\frac{1}{2}$   $\frac{292}{459}$ . E £65..7..2 $\frac{1}{4}$   $\frac{45}{459}$ (59) When first the marriage knot was tied

Between my wife and me,

My age did hers as far exceed,

As three times three does three;

But when ten years, and half ten years,

We man and wife had been,

Her age came then as near to mine

As eight is to sixteen.

Quest. What was each of our ages when we married? Ans. 45 years the man, 15 the woman.

#### SUPPLEMENTAL QUESTIONS.

(1) How many gallons of the imperial standard measure are respectively equal to a hogshead of wine and a hogshead of ale, old measure; and what was the difference between the two hogsheads in cubic inches?

(2) What quantity of the old ale measure would correspond to 54 gallens of the imperial standard ?

(3) H in quanti (4) R

ASSISTAL

its equiv (5) A was bety exact tim

an hour time.

(6) If and 2 fe 240 yard (7) T

> es broad a bar of broad, a

(8) A younger remainder the your half his

same rat brother's (9) A

from Ma meet at

\* Quest ous may b following Rule.

the correst them; sup necting the ually the arising from the blank

If  $7 \cdot 32$ 

(3) How many gallons of the old wine measure are equal in quantity to 63 gallons, imperial measure?

(4) Reduce 15 quarters, 3 bushels, 1 peck, old measure, to its equivalent in the imperial standard measure.

177

(5) A lady who was asked the time of the day, said that it was between *three* and *four*: but being desired to name the *exact* time, she replied, "The minute hand is advanced half an hour precisely before the hour hand." Required the exact time.

(6) If 7 men can build a wall 40 yards long, 4 feet high, and 2 feet thick, in 32 days; how many men will build a wall 240 yards long, 6 feet high, and 3 feet thick, in 8 days?\*

(7) The weight of a certain bar of iron 2 feet long, 3 inches broad, and 1 inch thick, is 20 *lbs.* What is the weight of a bar of similar quality which is  $7\frac{1}{4}$  feet long,  $4\frac{1}{2}$  inches broad, and  $3\frac{1}{2}$  inches thick?

(8) A person who had five-ninths of a mine, made his younger brother a present of half his share, and sold half the remainder to his cousin John, who soon after purchased  $\frac{1}{3}$  of the younger brother's share; but now offers to dispose of half his interest in the mine for £150. Estimating at the same rate, what is the value of the whole mine, and of each brother's share?

(9) A, travelling from London to Manchester, and B, from Manchester to London, set out at the same time. They meet at the end of six days, A having travelled 3 miles a day

\* Questions of *Compound Proportion* in which the terms are numer ous may be solved by Rule 1, for the Double Rule of Three; but the following method is more convenient.

RULE. Arrange the terms of the *first cause* and *effect* in one line, and the corresponding terms of the *second cause* and *effect* exactly under them; supplying the place of the term sought with an *asterisk*, and connecting the *contrary* causes and effects by cross lines. Multiply continually the terms of *each cause* and the *other effect*: divide the product arising from the *full* number of terms by the product of these with which the *blank* term is connected, and the quotient will be the answer.

#### Solution of the above exemple.

 $\begin{array}{c} \begin{array}{c} \text{men.} & \text{dayo} & \text{build} & y. \ \log \ f. \ h. \ fl. \ th. \\ \hline \mathbf{f} & 7 & 33 \\ \hline \ast & : & 8 \\ & 240 & . \ 6 & : \ 3 \end{array} \right) \\ \begin{array}{c} \mathcal{A} & 6 & 3 \\ \hline & 7 \times 32 \times 240 \times 6 \times 3 \\ \hline & \varphi \times 40 \times 4 \times 2 \\ \hline & 1 & 1 & 1 \end{array} \right) \\ \end{array} \\ \begin{array}{c} \mathcal{A} & 6 & 3 \\ \hline & \mathcal{A} & 6 \\ \hline & 7 \times 32 \times 240 \times 6 \times 3 \\ \hline & \varphi \times 40 \times 4 \times 2 \\ \hline & 1 & 1 & 1 \end{array} \right) \\ \end{array} \\ \begin{array}{c} \mathcal{A} & 6 & 3 \\ \hline & \mathcal{A} & 0 \\ \hline & \mathcal{A} & \mathcal{A} \\ \hline & \mathcal{A} & \mathcal{A} & \mathcal{A} \\ \end{array} \\ \begin{array}{c} \mathcal{A} & \mathcal{A} & \mathcal{A} \\ \mathcal{A} & \mathcal{A} \\ \mathcal{A} & \mathcal{A} \\ \mathcal{A} & \mathcal{A} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \mathcal{A} & \mathcal{A} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \mathcal{A} & \mathcal{A} \\ \mathcal{A} \\ \mathcal{A} & \mathcal{A} \\ \mathcal{A} \\$ 

TOR'S

at 4s. halfy will ..2. put in of the 60. n one 00. equal 54. 5 lb., ghing ¥. from num-, and **i8**. to be B 1 hem

423. 459. 459

n.

sa**re** Jear<sup>i</sup> Vecn

Teli

#### SUPPLEMENTAL QUESTIONS.

[TUTOR'S

more than B. At what rate did each go, the distance being 186 miles?

(10) A coach, which runs the whole distance in 31 hours, starts from London at the same time that another, which does it in 21 hours, starts from Manchester. Required the number of hours elapsed, and the distance travelled by each when they meet.

(11) A load of corn was sold for  $\pounds 15$ . at a loss of 15 per cent. What should it have been sold for to gain as much per cent. as the corn cost?

(12) Two men purchased a grinding stone 42 inches in diameter for a guinea; of which the first paid twelve shillings. They agree that the first shall use it till his share is worn down. What will be the diameter when the second receives it?

(13) If A and B together do a piece of work in  $7\frac{3}{4}$  days, which A alone would accomplish in  $12\frac{1}{2}$  days; in what time would B do it himself?

(14) A person lent  $\pounds$ 400, and agreed to receive in return a yearly payment of  $\pounds$ 50, for 13 years. Whether would he gain or lose thereby, reckoning Compound Interest at  $\pounds$ 5, per cent. per annum?

(15) By selling a horse for £50. I gained one-fourth of what he cost me; but the whole cost (including the expense of his keep) was one-fourth more than the original purchase. How much did I give for him, what did I expend in keeping him and what did i in per cent.?

(16) It has been a found by experiment, that sound is conveyed throug and air at the rate of 1142 feet in a second. How far distant is the cloud, when  $7\frac{3}{4}$  seconds elapse between seeing the flash of lightning and hearing the thunder?

(17) What is the height of a tower that projects a shadow 75.75 yards long, at the same time that a perpendicular staff, 3 feet high, gives a shade of 4.55 feet in length?

(18) A bankrupt owes  $\pounds 2580$ , and the value of his effects is  $\pounds 846$ , and the amount of recoverable debts  $\pounds 358..12$ , besides which he has an unexpired lease that has 13 years to run, valued at  $\pounds 12$ , a year more than the stipulated rent. If the lease be disposed of for present money, allowing Compound Interest at  $\pounds 5$ , per cent, per annum; and if the working of the commission and other expenses amount to  $\pounds 472$ ; wha will his creditors have in the pound, provided they allow him  $\pounds 150$ , to recommence business?

(19) A youth aged 12 years, having had bequeathed to him

ASSISTA

an annu of age, exchang continue cation a reserved (20)round w travels how ma many c (21)£52..10 of May (22)purchas at six : paymen on acc sion at the end (23)1s. 6d. of 4s. Insurat or 2s. (24)2; oxe eat 24 winly (25)of whi in 50 1 in 25 1 in wha efflux (26)one pl had £ (27)

178

•

٩W

## ASSISTANT ] SUPPLEMENTAL QUESTIONS.

an annuity of £50. for 12 years, to commence when he comes of age, the executors think it will be more advantageous to exchange this for an annuity to commence immediately, and continue till he is 21, to enable them to give him some education and a trade. What will be such annuity, £100. being reserved at the conclusion to set him up in business?

(20) There is an island 73 miles in circumference, to travel round which three pedestrians all start at the same time: A travels 5 miles a day, B travels 8, and C 10 miles a day. In how many days will they all come together again, and how many circuits will each have made?

(21) What will a banker charge for discounting a bill of  $\pounds 52..10$ . on the 7th of April, the bill being due on the 19th of May?

(22) My agent in London having advised me that he has purchased goods on any account to the amount of £756.10. at six months' credit, or £7½. per cent. discount for prompt payment, if I send a remittance of £400. to be paid down on account, after deducting out of it his charge for commission at £2¼. per cent., what will remain to be discharged at the end of six months ?\*

(23) If I insure a house for £250. at the annual charge of 1s. 6d. per cent., and the furniture, &c., for £150. at the rate of 4s. 6d. per cent., what shall I have to pay yearly to the Insurance office, including the duty paid to Government of  $\frac{1}{6}$ , or 2s. 6d. per cent.?

(24) If 12 oxén will eat 3<sup>1</sup>/<sub>3</sub> acres of grass in 4 weeks, and 2; oxen will eat 10 acres in 9 weeks, how many oxen will eat 24 acres in 18 weeks, allowing the grass to grow unitormly?

(25) A bath is supplied with water by two cocks, from one of which it may be filled in 10 minutes, and from the other in 50 minutes: a discharging cock will empty it (when filled) in 25 minutes. If all the three be opened at the same time, in what time will the bath be filled, supposing the influx and efflux to be uniform ?

(26) A person who had spent two-thirds of his money at one place, and half the remainder at another, found that he had  $\pounds 32.12$ . left. How much had he at first ?

(27) The length, breadth, and height of a room are ! 6

\* See Note to Example 11, Discount, page 71.

or's

being

ours, bes it er of they

5 per h per

n diings. own.

days, time

urn a d hê 5. pe**r** 

what of his How him

concond. ween

ado**w** staf**f,** 

flects 2. bears to . If Comrking what y him

o him

[TUTOR'S

and 4 yards respectively. What is the longest right line that can be taken within that room ?

(28) What must be the length of a cord with which a horse may be tethered to a certain point in a straight fence, so as to allow him the liberty of grazing to the extent of 1 rood, supposing that he can reach 2 yards beyond the tether ?

(29) A person playing at cards, lost three nights successively. The first night he lost half his sovereigns and half a sovereign besides; the second night he lost half the remainder and half a sovereign more; and the third night half the remainder and half a sovereign more, which reduced his stock to twenty. How many sovereigns had he at first?

(30) The month of July, 1828, was remarkable, both in England and several parts of the Continent, for excessive rains. At Derby, the quantity collected in the *pluviameter* (or rain-guage).between the hours of *nine*, A. M., of the 9th of that month and *six* the following morning (an interval of 21 hours) was 3.59 inches; to the evening of the 15th it amounted to  $7\frac{1}{4}$  inches; and by the conclusion of the 29th, an interval of 21 days, of which 10 only were very rainy, he total depth of water collected was  $11\frac{1}{3}$  inches. How many hogsheads, of 54 and 63 imperial gallons respectively, fall on an acre of ground to amount to the depth of *one inch*; and how many hogsheads of each kind fell on the surface of an acre during each of the three several intervals above mentioned ?

(31) A person who occupies a piece of ground for which he pays a rent of £10. per annum, wishes to take it upon a lease for forty years, with the obligation of laying out upon it during the present year £600. in the erection of a building, which is to be left in good tenantable condition at the termination of the lease. The question is, how much will be a fair annual rent for the lessee to pay during the term of continuance of such tenure, admitting the ground rent paid at present to be a fair one, and supposing the customary interest of money to be at the rate of £5. per cent. per annum? Also, supposing interest to be at £4. per cent. per annum?

(32) What will be the expense of covering and guttering a roof with lead at 18s. per cwt., the length of the roof being 43 feet, and the breadth or girt over it 32 feet; the guttering 57 feet long and 2 feet wide: the lead for the former being 9831 *lb.*, and for the latter 7.373 *lb*, to the square foot? Inte

BOOK-

trans The scie general pr any particibe easily a Single

ally ador The C ing, is,

To mo ceives fr from hin The be Book, th

The D inventory in the re and sold The C

It is rule sums rec Balance amount of some con Cash in

In the from the one folio and thos the *Bala* sides) m ring of a called *pa* 

In many former en cerns of n other, cal In the

Receivable session, a upon and Note.

but many ¢1 for the

'OR'S

that

as to sup-

cesalf a nainthe his

h in sive *icter* 9th 1 of h it 9th, iny, Iow cly, *ich*; e of

nich n a pon ing, mifair inusent of lso,

ien-

ing ing ing ing

## (181)

### A COMPENDIUM OF

# BOOK-K E E P I N G,

#### BY SINGLE ENTRY;

#### Intended for the purpose of initiating Youth in the *LEADING PRINCIPLES* of that important Branch of Science.

**B**OOK-KEEPING is the art of recording pecuniary or commercial transactions in a regular and systematic manner.

The science of Book-keeping admits of innumcrable varieties of method: but its general principles are invariable. These being well understood, the knowledge of any particular system, adapted to the peculiar concerns of any counting-house, will be easily acquired.

Single Entry, being the most simple and concise, is the method usually adopted in retail business.

The General Rule to be observed in every system of Book-keeping, is,

To make any person Debtor (Dr.) for money or goods which he receives from me, and to make him Creditor (Cr.) for whatever I receive from him.

The books usually kept in *Single Entry*, are the Day-Book, the Cash-Book, the Ledger, and the Bill-Book.

The Day-Book, when a person commences business, begins with an inventory of the existing state of his affairs: after which are entered, in the regular order of time, the daily transactions of Goods bought and sold.

The Cash-Book contains the particulars of all Money transactions. It is ruled in a folio form: on the left hand page, Cash is debited to all sums received, and on the right, Cash is credited by all sums paid. The Balance (or quantity which the Dr. side exceeds the Cr.) shows the amount of Cash in hand. This should be ascertained weekly, and in some concerns daily, in order to prove if it corresponds with the real Cash in hand.

In the Ledger are collected the dispersed accounts of each person from the Day-Book and Cash-Book, and entered in a concise manner in one folio; the sums in which he is Dr. being arranged on the left-hand, and those in which he is Cr. on the right-hand page of the folio: so that the *Balance* of his account (the difference between the Dr. and Cr. sides) may always be easily ascertained by inspection. The transferring of accounts from the Day-Book and Cash-Book to the Ledger, is called *posting*.

In many trades it is found convenient to keep the accounts of Goods Sold at the former end, and those of Goods Bought at the latter end of the Ledger. But in concerns of magnitude, two Ledgers are more convenient; one for Goods Sold, and the other, called the "Bought Ledger," for Goods Bought. In the BILL-BOOK are copied the particulars of all Bills of Exchange, whother Receivable or Payable. The former are those which come into the Tradesman's pos

In the BILL-BOOK are copied the particulars of all Bills of Exchange, whother Receivable or Payable. The former are those which come into the Tradesman'n pos session, and are drawn upon some other person; the latter are those which are drawn upon and accepted by him.—Printed Bill-Books may be had of any Bookseller. NorE. In the following transactions, Bills Receivable are considered as Cash:

NOTE. In the following transactions, Bills Receivable are considered as Cash: but many Accountants do not enter them as such, till Cash has been actually receiv & I for them 1 182 )

## MEMORANDUM

#### OF THE TRANSACTIONS STATED IN THE FOLLOWING BOOKS.

Follo of Ledger

Lh

Bu

Te

Ra

.Ia

B

4

1

1 Ja

1

2

1

2

.1

\* T1

any ac † Th ‡ Th ed; bu

i

- **2n. 5. Received** from Allen, Wild, and Co. of Leeds, on credit, 3 pieces of super blue cloth, each 36 yds. at 25s. 6d. per yard :—and 2 pieces of narrow brown, 84 yds. at 4s. 9d.
- \*8. Sold Bernard Mason 2 st. raw sugar, at 91d. per lb.-34 lb. green tea, at 8s. 6d.-and 34 yds. blue cloth, at 28s.
- 9. Bought of Samuel Fletcher, 1 cwt. 1 qr. 5 lb. Kent hops, at £5..7. per cwt.—and 14 cwt. of Worcester, at £5..11..6;—six mouths' credit, or 5 per cent. discount for cash.—Paid him Bill, No. 1, £24..3..9. and received from him a cheque on Smith and Co. Bankers, for the difference, including discount.
- "9. Bought of Simmonds and Co. Liverpool, 2 cwt. yellow soap, at 76s.-12 doz. dip candles. at 3s. '6d.-and 4 doz. mould do. at 11s. 3d.
- 14. Sold William Tomlinson 7 yds. narrow cloth, at 5s. 3d.-and 15 yds. calico, at 24d.
- Sold Hazard and Jones 11 st. yellow soap. at 9d. per lb. 1 st. mottled, at 91d. 9 lb. candles, at 9d. and 3 lb. mould do. at 121d. Paid Cash for Bill, No. 1, W. Holmes, £45..10.
- 23. Received from J. Sanderson, goods as per invoice £7..3..6.
- **22.** Sold Hazard and Jones  $17\frac{1}{2}\frac{10}{2}$ , loaf sugar, at 1s. 1d.-12 lb. raw do. at  $10d.-1\frac{1}{4}\frac{10}{10}$ . Congou tea, at 7s.  $6d.-and \frac{1}{2}\frac{10}{10}$ . Hyson, at 12s.
- 21. Paid the balance due to J. Herdson, cash £37..5.6. abatement 4d.—Sold him on credit 10 lb. hops, at 13d.—and half a ream of cap-paper, at 7d. per quire.
- Feb. 1. Sold W. Tomlinson 2 st. yellow soap, at 9.d. per lb.-6 lb. mould candles, at 1s. 1d.-and 16 lb. lump sugar, at 124d. Received of him cash for account due, including the present goods, £4..13. abatement 34d.

Paid Bernard Mason the balance due, cash £232; abatement 5s. 22d.

- 4. Received of James Taylor  $\frac{1}{2}$  yr's, interest on £70, due this day, £1..15.
- 3. Sold W. Tomlinson 1 piece super blue cloth, 36 yds. at 27s. 6d.-for Bill at one month.
- W. Tomliuson paid me a Bill on Jones and Co. London, due May 10, £60. which should have been at one month.—Charged him discount, 10s.—Paid, agreeably to his order, the difference to J. Sims, in cash, £10.
- Dought of J. Sanderson, cheese 25 cwt. 3 qrs. 17 lb. at £3.2.6.
   per cwt.—Paid his whole account in cash, £83. abatement 1s. 8§d.
   Accepted Allen, Wild, and Co.'s Bill at two months, drawn Jan
   \$\$, £80.
- Received of Hazard and Jones's assignce, cash £2.7..21: for com position on £3..15..6. at 12s. 6d. in the £.

## (183)

## DAY-BOOK, (page 1.)

Folio of Ledger.*	Inventory, January 1st, 1830.	£.	8.	đ.
Fol	I have in Ready Money	1500	0	0
	I have in Recarg money         Bills Receivable, No. 1, on S. Johnson, due 29th         instant         cwt. qr. lb.         Tea, 3 chests gross wt. 3 1 17         tare       0 2 7	24	3	9
	Duty included on 2 3 10 at 6s. 2d. per lb.	98		0
	cwt. qr. lb. Raw Sugar, 2 hhds. weighing 27 3 18 neat, at £3148. per cwt. James Taylor owes me on bond, dated August	104	4	Ø
1	4th, 1826, with interest at £5. per cent. per annum	70	0	0
1		1796	8	9
1	I owe as follows:- John Herdson, a balance of accounts -	37	5	10
1	John Hernson, a binnee of my house by anc- Bernard Mason, for purchase of my house by anc- tion, to be paid 1st February next - £800 } Duty on do. at £5. per cent 40 } Bills payable, viz.: No. 1, W. Holmes's bill, to	840	0	0
•2	H. Williams or order, accepted by me, due 19th instant	45	10	0
1		922	15	10
	Allen, Wild, and Co., Leeds Cr. +By 3 pieces superfine blue cloth, each 36 yds. at 25s. 6d. per yd. 2 pieces narrow brown, 34 yds. at 4s. 9d. Wrappers	137 19 (	19	0 0 6
2	3	15	7 18	6
-	Bernard Mason     Dr.       * To 2 st. raw sugar. at 94d. per lb.     34 lb. green tea, at 8s. 6d.       33 yds blue cloth, at 28s.		1 2 1 7 5 5	2 74 0
•			7 14	91

This column contains the figures of reference to the folio of the Ledger in which any account is posted. They should be written in red ink.
The preposition By is always put before any article for which a person is credited.
The preposition To is generally placed before articles for which a person is debit ed; but some Bookkeepers omit it

pieces pieces

green

£5..7. redit, ..3..9. or the

ap, at lo. at

5 yels. -1 st.

w do.

ment m of

6 13. eived 1..13.

t 5s.

day,

-for

May disns, in

2..6. 8ªd.

Jan com DAY-BOOK, (page 2.)

.]

£ .

Jam T 1

Wi T

F

Jan

All 2

> Oa 1

2

3

8

3

3

1

1

\* This practice. † Vide

t In th only a ge opening

Joi

	1830, Jan. 9.			
	Samuel Fletcher Cr	£.	8.	4.
	cwt. gr. lb. £. s. d.			
	By Kenthops, 1 1 5 at 5 7 0	6	18	6
	Worcester do. 1 2 0 at 5 11 6 -	0	7	3
2	Six months' credit, or £5. per cent. discount for		-	
		15	5	9
	Simmonds and Co., Liverpool Cr.			
	By Yellow soap, 2 cwt. at 76s.	7	12	0
	12 doz. candles, at 8s. 6d	5	2	Ō
	4 doz. mould do. at 11s. 3d	2	5	0
2	14	14	19	0
	William Tomlinson D.			
	To narrow cloth, 7 yds. at 5s. 6d.	1	18	6
	calleo, $15 \ yds. at \ 0s. \ 8\frac{1}{2}d.$ -	ō	10	71
2		2	9	14
	Hazard and Jones			
	To 11 st. yellow soap, at 9d. per lb.			
	st. mottled do. at 91d.	0	15	: 9
	9 lb. candles, at 9d.	0 0	56	64
	3 1b. moulds, at 1s. 01d	0	3	9 13
3		1	11	- <u>12</u> 2
	James Sanderson			
3	James Sanderson By goods as per Invoice*			
-		7	3	6
	Hazard and Jones Dr.		. 18	
	JO 1/4 10. loat sugar, at 1s. 1d.	0	18	114
	12 lb. raw do. at 10d.	0	10	0
	14 lb. Congou tea, at 7s. 6d. 1 lb. Hyson, at 12s.	0	9	44
3	5 20. Hyson, - at 12s	0	6	0
		2	4	4
	John Herdson Dr			
	To Hops, 10 lb. at 1s. 1d.	0	10	10
	2 ream cap paper, at 7 d. per quire -	ŏ	5	10
_ 1		0	16	8
	William Tomlinson Pr			
1	To 2 st. yellow soap, at 9d. per lb.			
	6 lb. mould candles, at 1s. 1d.	1	1	0
	16 16. lump sugar, at 1s. 01d.	0	6	6
2		0	16	8
		2	4	2

\* Many tradesmen keep an *Invoice Book*, into which all invoices of goods purchased are regularly transcribed. Some paste the invoices themselves within a blank book The account of Allen, Wild, and Co. (D. B., p. 1,) is supposed to be a copy from their invoice. Some make the *Invoice Book* serve also for the "*Bought Ledger*." This last method, when the nature of the trade will admit, is well worth adopting

## DAY-BOOK, (page 3.)

	1830, Feb. 4	£.		d.
1	James Taylor Dr. To half a year's interest on £70. at £5. per cent. per annum 5	1	15	0
c?	William Tomlinson Dr. To 1 piece superfine blue c' :h, 36 yds. at 27s. 6d. For bill at one month.	49	10	0
3	James Sanderson cwt. qr. lb. £. s. d. By cheese* 25 3 17 at 3 2 6 per cwt. 10	80	18	23
2	Allen, Wild, and Co., Leeds Dr. To my acceptance of their Bill at 2 months, drawn 3rd Jan. B. P. Book. No. 2.	80	0	0
	Oats' Purveyance, in Partnership with J. Herdson.† Dr. To Cash, for Oats parchased by met Do. do by J. Herdson Do. for warehouse room, &c.	26 449 1	11 0 13	0 3 8
8	Cr.	477	4	11
	By Cash received for Oats sold Do, do. by J. H.	507 55	9 2	2 8
3		562	11	10
3	£. s. d. Dr. To Profit, ½ (42135½) being my share J. H. ½ (42135½) being his share	85	6	11
	John Herdson Dr. To Cash advanced to him on Oats' concern Oats sold and received for by him	433 55	17 2	08
1		488	19	8
	Cr. By Oats purchased by him his share of profit	449 42	0 19	3 54
1		491	1.2	81

\* This is supposed to be bought by the long cwt. (120 12.) agreeably to the general practice.

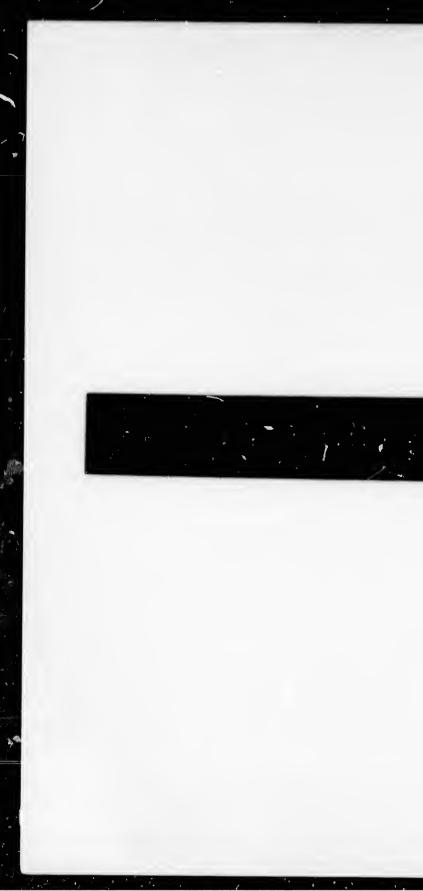
† Vide Example of a Partnership Concern, p. 187,

\* In this concern, the entries of Cash are not made in the Cash-Book ; this being only a general statement of transactions supposed to have taken place. before the opening of these books

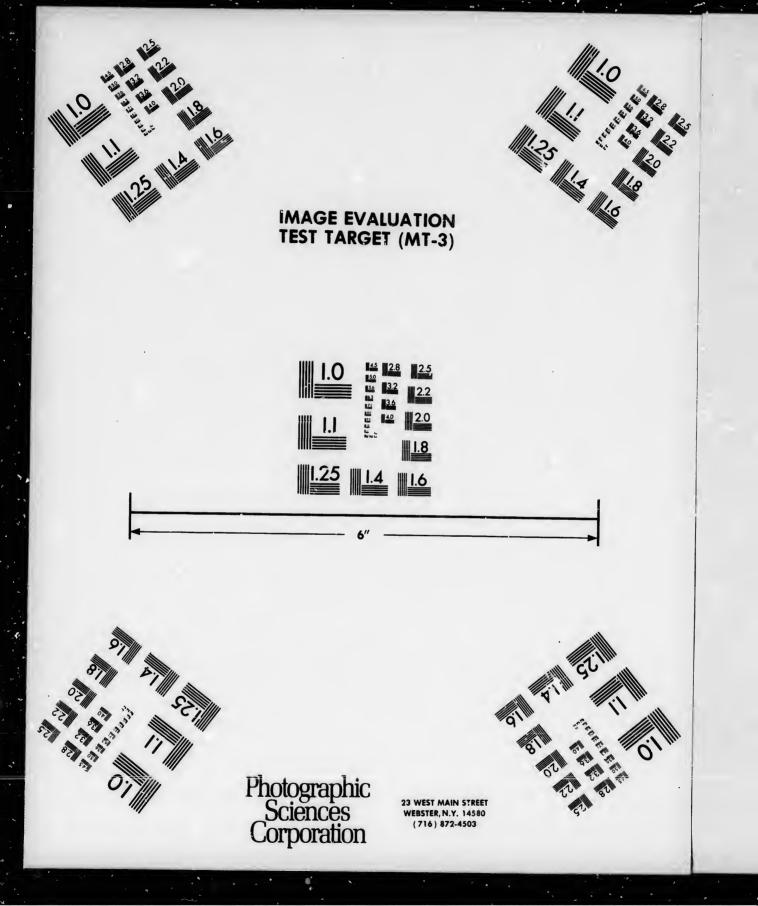
ased ook heir last

d.

6



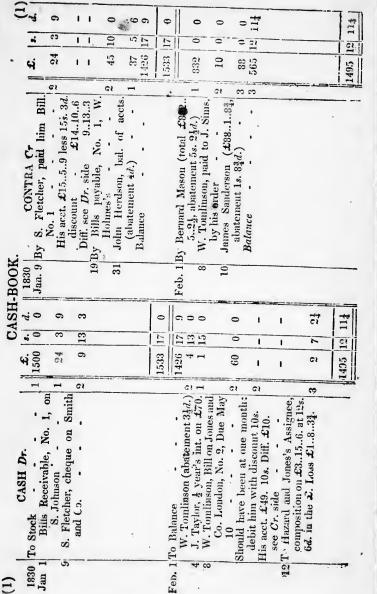






186

CASH-BOCK.



John the arm has paid face di £55..2... wareho collecte the tran It ma real occ spplied

\* The

J

]

#### LEDGER INDEX.

64

1

495 12

114

22

1405

7

2

5

## INDEX TO THE LEDGER \*

A Allen, Wild, and Co. 2	N
B Bills payable 2	O Oats' purveyance - ? .
С	P
D	Q
Έ	R
F Fletcher Samuel - 2	S Stock 1 Simmonds and Co 2
G	Sanderson James - 3
H Herdson John 1 Hazard and Jones - 3	T Taylor James - 1 Tomlinson Wm 2
I J_	UV ·
K	W
L	ХҮ.
M Mason Bernard 1	Z

\* The Ledger has an Alphabetical Index, showing, at one view, in what folio any serson's account may be found.

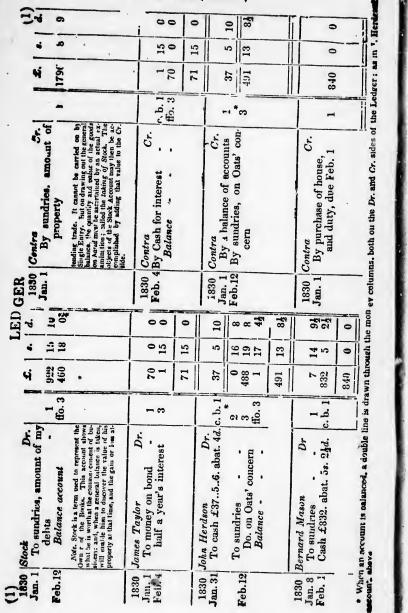
## EXAMPLE OF A PARTNERSHIP CONCERN.

John Herdson and I have been engaged in a joint concern as purveyors of od.s for the army. I have purchased oats for the joint stock to the amount of  $\mathcal{L}20$ ...11. H has paid, for oats purchased by him,  $\pounds$ 449.0.3. I have received, for oats that nave from disposed of,  $\pounds$ 507.9.2.; and my partner has received, from the same source,  $\pounds$ 53.2.8. I have advanced to him, at different times,  $\pounds$ 433..17.; and have paid, for warehouse room and other sundry expenses,  $\pounds$ 1..13..8. From these general heads, collected from the particulars recorded in the Granary Book, it is required to state the transactions.

It may, perhaps, be interesting to the learner to be informed that the above was a real occurrence; for an accurate statement of which the writer was some time since spplied to by the parties concerned.

162

LEDGER, (folio 1.)



1830 |Bills Payable To Cash Jan. 19

2

By Holmes's hill, No. 1 || 1830 |Contra Jan. 1 EDGER. 0 d. 10 • Dr. c.b. 1 45

Illen Wild and Co's hill

Cr.

NO

:01

0 5

040

-

T 'no E ch' T

• When an account is calanced, a double line is drawn through the mon ev columns, both ou the *Dr*, and *Cr*, sides of the Ledger ; as in ". Herde

# LEDGER, (folio 2.)

ê		LEDGER, (fo	lio 2.)		189
	0 C	6 6 6	0	3 30	0
-9	18	13 13	19	13 0 13	0
44	80	15 9 24	14	40 4	3
-	p.b.1	c. b. 1	51   19	c 5.1 c 5.1	c 6 1
Cr. No. 1	. Cr.	ra ra Cr. 2 Cheque on Smith & Co. c. b. 1	5. 5		
is bill and C	•	onSm	·	as'n Abatemont	•
$\begin{array}{c c} \mathbf{J} \mathbf{F} \mathbf{D} \mathbf{G} \mathbf{E} \mathbf{R} \\ \mathbf{d} \\ \mathbf{d} \\ 0 \\ \mathbf{D} \\ \mathbf{n} \\ \mathbf{D} \\ \mathbf{h} \\ 1 \\ 0 \\ \mathbf{n} \\ n$	No. 2 - ontra By Cloth	Contra By Hops Cheque	Jan. 10 By goods		By Bill
R. Con	1830 Contra Jan. 5 By C	U	1830 Contra an. 10 By g		63
LEDGER.	1830 Jan. 5	1830 Jan. 9	Jan.	Feb	
d. d.	0 0 0	0	0	2. 2 T	1000
10.	18 18 0	19	10	94 5	
÷ + +		54	1 2 1	63 63 4	10 10 60
c. b. 1 45	10. 3 ff0. 3	c. b. 1	ffo. 3	N N	с. b. J
Ч	Feb.12 Badance	1830 Saruel Fletcher Dr. Jan. 9 To Bill, and disc. on hops c. b. 1	pool, Dr.	William Tomineon Dr. To goods	To Cloth Cash £10. Discount 10s. c. b. 1
2) 1830 <i>Bil</i> Jan. 19 7	reb.12 1830 <i>All</i> Feb.10	1830 Sc Jan. 9	Feb. 12	1830 14 Jan. 14 Feb. 1	13 00

-	100	
	1.90	
	a. v v .	

# LEDGER, (10110 3.)

24 53 28 9 10 44 0900 FIL in co 15 Ó 18 11 18 18 11 0 9 4 01 -က 80 88 562 2 14 635 80 By cash for composition, c. b. 1 remainder lost [c. b. 1] C2 C2 €¥ 65 3 ffo. C. Cr. Сr. . Çr. By J. Herdson, I owe Bills Payable Stock account debited Allen, Wild and Co Simmonds and Co. BALANCE. By sundries By goods cheese 1830 |Contra 1830 Contra 1830 Contra Contra LEUGER. Feb.12 Jan. 23 114 Feb.12 Feb.10 Feb.12 1830 \$ 833 e. 9 114 10 II Π ~ 22 11 -4 ç 120 11 12 બં - 01 က 83 562477 55 635 James Taylor, owes me Ifo. 1 70 70 To cash £38. abat. 1s. 83d. c. b. 1 ର ର က က Oats' Purveyance, in Co. with Profit, <u>4</u> to self £42..13..54 } Å. Dr.Dr. Dr. . To soap and candles . 4 1830 |Hazard and Jones Sugar and tea • GENERAL To cash in hand 1830 James Sanderson To Sundries J. Herdson Balance Jan. 19 28 Feb.10 Feb.12 Feb.12 1830 1830 3



# BR

3 ER I vi of Walki L C

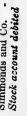
A larg

B., of the Provin on the

BC

Bindi





 HI	1
12	
 635	

FOR SALE, WHOLESALE AND RETAIL, BY BREWER, MCPHAIL, & CO., TORONTO.

**3ERIES OF NATIONAL SCHOOL BOOKS,** viz.:--First, Second, Third, Fourth, and Fifth Books of Lessons, an English Grammar, and an Arithmetic.

Walkingame's Arithmetic; English Reader; Kirkham's, Lennie's, and Murray's Grammars; Canada, Mavor's, Carpenter's, Cobb's, and Webster's Spelling Books, &c.

## -ALSO,-

A large assortment of Works on Rhetoric, Logic, Philoso. phy, Chemistry, Botany, Phisiology, Phrenology, and Mechanics.

B., McP., & Co. have always on hand a well-selected Stock of the Classics, and other School Books generally used in the Province, which are supplied to Merchants and Teachers on the best Terms.

A LIBERAL DISCOUNT FOR CASH PURCHASES.

**BOOK & JOB PRINTING** 

TASTEFULLY EXECUTED.

BOOKS, STATIONERY, &c. &c.

Binding executed in all its Branches, on liberal Terms.

English, French, and American Paper Hangings.



