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NEW BRUNSWICK SCHOOL SERIES.

THE

ELEMENTARY ARITHMETIC.

Compiled and arranged by

W. R. MULHOLLAND.

REVISED EDITION.

With Metric System of Weights and Measures.

PRESCRIBED BY THE BOARD OF EDUCATION FOR THE PROVINCE OF NEW BRUNSWICK.

HALIFAX, N. S.: A. & W. MACKINLAY. SAINT JOHN, N. B.: T. H. HALL. 1882. EDUCATION OFFICE, Province of New Brunswick. The Board of Education has prescribed "Mulholland's Elementary Arithmetic" as a text book for use in the Schools of this Province.

THEODORE H. RAND, Chief Superintendent of Education.

Entered, according to Act of Parliament of Canada, in the year 1881 By A. & W. MACKINLAY, In the office of the Minister of Agriculture, at Ottawa.

PREFACE.

The "Elementary Arithmetic" is intended to occupy an intermediate position, coming between the concrete and the advanced stages, and is adapted for the junior classes in our common schools, for securing the mental development, as well as the accuracy and expedition in calculation of the pupils between seven and eleven years of age.

The plan consists of such a delineation of the principles that the pupils are enabled, by induction, to form the appropriate rules.

After the accuracy of their knowledge is tested by a few mental exercises, the examples are reduced to practice on the blackboard or slate.

A number of self-testing exercises to many of the rules are introduced, which will save the teacher much labour, and be of benefit to the pupils.

The definitions and tables have been interspersed through the work, thereby rendering them more available to the student.

After Practice, the Unitary Method is explained, and some exercises given thereon. Proportion is introduced in a way not usually found in works of the kind; and several operations generally included under Interest and other rules, are grouped together, by which means the pupils are enabled to solve all questions where ratio is involved.

Under each rule will be found a large number of well graded exercises, many of which have been selected trom real occurrences in business.

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PREFACE.

The compiler has availed himself of the best works in the New and the Old World, viz., Dr. Robinson's, edited by Fish, Dr. Thomson's, Greenleaf's, Barnard Smith's, Currie's, Hay's and others, but especially that of Dr Robinson.

23 In the Appendix will be found a short and complete account of the Metric System of Weights and Measures, with practical exercises. This system was legalized by the Parliament of Canada in 1879.

Note.—In this Work, \pounds s. d. mean Sterling Money; \$ and cts mean Canada Currency

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THE

ELEMENTARY ARITHMETIC.

DEFINITIONS.

1. Anything which can be *multiplied*, *divided* or *measured* is called QUANTITY. Thus, lines, weight, time, number, &c., are quantities.

2. Arithmetic is the science of number, and teaches how to represent numbers by symbols or signs, and the various methods of using these in calculation.

3. Numbers are expressions for one or more units. Thus, the words *one*, *two*, *three*, *four*, &c., or the characters 1, 2, 3, 4, &c., are expressions by which we indicate how many single things, or units, are to be taken.

4. Numbers are divided into two classes, **Abstract** and **Concrete** or DENOMINATE. If the units represented have no reference to any particular object, as when we say seven and two are nine, they are called abstract numbers. If the units have reference to particular objects, as two days, seven men, &c., they are called concrete or denominate numbers.

NOTATION AND NUMERATION.

Art. 1. Notation is the writing or expressing of numbers by characters; and

Numeration is the reading of numbers expressed by haracters.

2. Two systems of notation are in general use—the Roman and the Arabic.

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NOTATION AND NUMERATION.

The Roman Notation

3. Employs seven capital letters to express numbers. Thus,

Letters— I	V	X	L	C	D	M
Values -one,	fire,	ten,	fifly,	one	five	one
				hundred,	hundred,	thousand.

By combining these letters, the ancient Romans formed the following Table of Natation.

						-			
I	••	1 VHI		8]	XV	15	XL	• •	49
н		2 IX		9 3	XVI	16	L	• •	50
341		3 X	· ·	30 1	KVH	17	LXX	••	79
JV	• •	4 XI		11 X	VIII.	18	C.	••	100
v		5 XII		12	XIX	19	Ð	••	500
VI		6 XIII	• •	13	XX	20	M	••	1000
VII	• •	7 XIV		F4 2	(XX	30	MD		1500

This system of notation is principally confined to the numbering of chapters of books, public documents, &c.

Express the following numbers by letters:

- 1. Eleven.
- 2. Fifteen.
- 3. Seventeen.
- 4. Twenty-five.
- 5. Thirty-nine.
- 7. Ninety-nine thousand, four hundred. 8. One thousand, nine hun
 - dred and ten.
- 9. Express the present year
- 6. One thousand and one.

The Arabic Notation

4. Employs ten characters, or figures, to express numbers Thus.

Figures. 3 1 Names) one, two, three, four, five, six, seven, eight, nine, nought and or cipher.

values,

The first nine characters are called significant figures, because each has a value of its own. They are also called digits, a word derived from the Latin word digitus, a finger, it being supposed the ancients first counted by their fingers.

The nought or cipher is also called nothing or zero. The cipher has, of itself, no value, but is used to indicate the order of the significant figures which precede it.

The ten Arabic characters are the Alphabet of Arithmetic; and by combining them according to certain principles, all numbers can be expressed.

NOTATION AND NUMERATION.

5. 'To facilitate the reading of large numbers they are divided into periods of three figures each, beginning at the right-hand side, according to the following

		Numeration	Table.
Period	I.	Units {	Units, Tens, Hundreds.
66	II.	Thousands	Units of Thousands, Tens of Thousands, Hundreds of Thousands,
46	III.	Millions	Units of Millions, Tens of Millions, Hundreds of Millions.
46	IV.	Billions { **	Units of Billions, Tens of Billions, Hundreds of Billions.
46	v.	Trillions $\begin{cases} \infty \\ \infty \\ \neg \end{cases}$	Units of Trillions, Tens of Trillions, Hundreds of Trillions.
46	VI.	Quadrillions {	Units of Quadrillions, Tens of Quadrillions, Hundreds of Quadrillions.

6. Figures occupying different places in a number, as units, tens, hundreds, &c., are said to express different orders of units.

Simple units	are called	units of the	first or	der
Tens	66	"	second	"
Hundreds	"	44	thir:1	"
Thousands	46	"	forrth	"

and so on. Thus, 327 contains 3 units of the third order, 2 units of the second order, and 7 units of the first order.

Exercises for the Slate.

Write and read the following numbers:

1. One unit of the third order, four of the second.

2. Eight units of the fifth order, three of the second.

3. Two units of the seventh order, five of the sixth, three of the fourth, nine of the third, eight of the first.

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4. Four units of the tenth order, six of the eighth, four of the seventh, three of the fifth, seven of the fourth, nine of the second, one of the first order.

7. Principles of Notation and Numeration.

1st. Figures have two values, Simple and Local.

The Simple Value of a figure is its value when taken alone. Thus, 3, 4, 5.

The Local Value of a figure is its value when used with another figure or figures in the same number. Thus, in 472 the simple values of the several figures are 4, 7, and 2; but the local value of the 4 is 400; of the 7 is 7 tens, or 70; and of the 2 is 2 units.

NOTE.—When a figure occupies the first place, its simple and local values are the same.

2nd. A digit or figure, if used in the second place, expresses tens; in the third place, hundreds; in the fourth place, thousands; and so on.

3rd. As 10 units make 1 ten, 10 tens 1 hundred, 10 hundreds 1 thousand, and 10 units of any order, or in any place, make 1 unit of the next higher order, we readily see that the Arabic form of notation is based on the following

GENERAL LAWS.

I. The different orders of units increase from right to left, in a ten-fold ratio.

II. Every removal of a figure one place to the left, increases its local value ten-fold; and every removal of a figure one place to the right, diminishes its local value to one-tenth of its previous value. Thus,

6 is 6 units.

60 is 10 times 6 units.

600 is 10 times 6 tens.

6000 is 10 times 6 hundreds.

4th. Every period contains three figures, (units, tens, and hundreds,) except the lett hand period, which sometimes contains only one or two figures, (units, or units and tens.)

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RULE FOR NOTATION.

I. Beginning at the left hand, write the figures belonging to the highest period.

II. Write the hundreds, tens, and units of each successive period in their order, placing a cipher wherever an order of figures is wanting.

RULE FOR NUMERATION.

I. Separate the number into periods of three tigu as each, commencing at the right hand.

II. Beginning at the left hand, read off the number of units of each order in each period separately, and add the name of the period.

NOTE .- In reading numbers the name of the last, or right-hand period, is usually omitted.

8. Until the pupil can write numbers readily, it may be well for him to write several periods of ciphers, point them off, and over each period write its name. Thus,

Trillions, Billions, Millions, Thousands, Units. 000,000,000,000,000,000

And then write the given numbers in their appropriate places.

Exercises for the Slate.

Express the following numbers by figures .

1. Thirty-six.

2. Three hundred and thirty-six.

3. Five thousand, three hundred and thirty-six.

4. Fourteen thousand, two hundred and forty-seven.

5. Four hundred and fifty thousand, and fifty-nine.

6. Ninety-six thousand and four.

7. Nine hundred thousand, and linety.

8. Sixty-one billions, four millions, and ninety-seven.

Point off, and read the following numbers:

9.	489	14.	3786	19.	2987654300
10.	586	15.	20900	20.	4783006001
11.	4070	16.	57631	21	3456780019
12.	307	17.	37000	99	69904999012
13.	10010	18	94000554	44.	0000420001
	10010	TO *	04000004	23.	1932643162

24. Write seven millions and thirty-six.

25. What orders of units are contained in the number 10370509?

ADDITION.

Explanatory Exercises.

9. 1. John gave 5 dollars for a vest, and 9 dollars for a coat; how many dollars did he pay for both?

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ngucver ANALYSIS.—He gave as many dollars as 5 dollars and 9 dollars, which are 14 dollars.

2. A farmer sold a lamb for 3 dollars, and a calf for 4 dollars; how many dollars did he receive for both?

3. Job n got 3 apples from his mother, 2 apples from his sister, and 1 apple from his brother; how many apples did he get altogether?

4. How many are 4 and 5? 4 and 7? 3 and 6?

5. How many are 5 cents, 6 cents, and 7 cents?

10. From the preceding operations we perceive that Addition is the process of uniting several numbers into one equivalent number.

11. The Sum or Amount is the result obtained by the process of addition.

Note.—Concrete numbers, that is numbers of objects, cannot be added together unless the objects are of the same kind. Thus, 4 grammars and 5 geographies cannot be added together. If, however, we drop the distinctive names of the objects, and use in their stead a more general term, which will include the several kinds in one class, the addition can be performed. Thus, if we consider geographies and grammars merely as books, we may say 4 grammars (books) and 6 geographies (books) are 10 books. This principle applies to all operations with concrete numbers.

12. The sign +, is called *plus*, which signifies more. When placed between two numbers, it denotes that they are to be added together. Thus, 6 + 3, shows that 3 is to be added to 6.

CASE 1.

13. When the amount of each column is less than 10.

EXAMPLE 1.—A farmer sold a horse for 103 dollars, seven cows for 271 dollars, and some hay and on 3 for 124 dollars; how much did he receive for all?

OPERATION.

ANALYSIS.—We arrange the numbers so that units of like order shall stand in the same column. We then add the columns separately, for convenience commencing at the right hand, and write each result under the column added. Thus, we have 4 and 1 and 3 are 8, the sum of the units; 2 and 7 are 9, the sum of the tens; 1 and 2 and 1 are 4, the sum of the hundreds. Hence, the entire amount is 4 hundreds 9 tens and 8 units, or 498, the Answer. Ar 5 6 7 firs ma

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ADDITION.

Exercises for the Slate.

	SECT		
1.	2.	3.	4.
Dollars.	Miles	Cents.	Days.
172	437	361	245
116	140	227	321
101	321	410	132

Ans. 389

5. What is the sum of 126, 321 and 232? Ans. 679

6. What is the amount of 521, 142 and 231? Ans. 894. 7. A stock farmer bought three droves of sheep. The first contained 225, the second 301, and the third 463; how many sheep did he buy in all? Ans. 989.

CASE II.

14. When the amount of any column equals or exceeds 10.

EXAMPLE 2.—A gentleman pays 596 dollars a year for house rent, 366 dollars for servants' wages, and 989 dollars for other expenses; what is the amount of his expenses?

OPERATION.

Sum of the units 21Sum of the hundreds 17Total amount 1951

ANALYSIS.—Arranging the numbers as in Case I. we first add the column of units, and find the sum to be 21 units. We write the 1 unit in the place of units, and the two tens in the place of tens. The sum of the figures in the column of tens is 23 tens, which is 2 hundreds, and 3 tens. We write the 3 tens in the place of tens, and the two hundreds in the place of hundreds.-We next add the column

of hundreds, and find the sum to be 17 hundreds, which is 1 thousand and 7 hundreds. We write the 7 hundreds in the place of hundreds, and 1 thousand in the place of thousands. Lastly, by uniting the sum of the units with the sum of the tens and hundreds, we find the total amount to be 1 thousand 9 hundreds 5 tens and 1 unit, or 1951.

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ADDITION.

This example may be performed by another method, which is the one in common use. Thus,

PERATION.	ANALYSIS Arranging the number of 1
596	fore, we add the first column 16 1.
366	to he 21 units, and the sum
989	column for writing the 1 unit under the
000	column of units, we add the two tens to the
	column of tens, and find the sum to be 25 tons:
1951	writing the 5 tens under the column of tens we

add the two hundreds to the column of hundreds, and find the sum to be 19 hundreds; as this is the last column, we write down its amount, 19, and we have the *whole amount*, 1951, as before.

NOTE.—Units of the same order are written in the same column; and when the sum in any column is 10, or more than 10, it produces one or more units of a higher order, which must be added to the next column. This process is sometimes called "carrying the tens."

15. From the preceding examples and illustrations we deduce the following

RULE. I. Write the numbers to be added so that all the units of the same order shall stand in the same column; that is, units under units, tens under tens, &c.

II. Commencing at uni[±]s, add each column separately, and write the sum underneath, if it be less than ten.

III. If the sum of any column be ten, or more than ten, write the unit figure only, and add the ten or tens to the next column.

IV. Write the entire sum of the last column.

Mental Exercise.

1. How many are 6 and 7? 6 and 9? 6 and 13?

2. How many are 6 units, 9 tens, and 15 units?

3. How many are 8 dollars, and 13 dollars, and 15 dollars?

4. How many are 6 + 7 + 8 + 9 + 12 + 13 + 8?

5. A man gave 12 dollars for some oats, 8 dollars for a ton of hay, and 7 dollars for a barrel of flour; how many dollars did he pay for all?

6. A man bought a sleigh for 26 dollars, paid 10 dollars for lining it and 11 dollars for painting it; what did it cost him?

7. A tailor bought three pieces of cloth, the first containing 29 yards, the second 27 yards, and the third 42; how many yards did the three pieces contain?

8. A man bought a barrel of flour for 7 dollars and sold it so as to gain 3 dollars; how much did he sell it for? N hay be f

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ADDITION.

Exercises for the Slate.

NOTE.—All the Exercises for the slate, given in this work, which have not the answers at ached are self-testing, the Key to which may be found in the appendix.

	SECT	ION II.	
(1)	(2)	(3)	(4)
3456	4563	5787	35109
3456	4563	5787	35109
6912	9126	11574	70218
10368	13689	17361	105327
17280	22815	28935	175545
(5)	(6)	(7)	(8)
67896	24687	84906	54639
67896	24687	84906	54639
135792	49374	169812	109278
203688	74061	254718	163917
339480	123435	424530	273195

16. The sign =, is called the sign of *equality*. When placed between two numbers, or sets of numbers, it signifies that they are equal to each other. Thus, the expression 6 + 4 = 10, is read 6 *plus* 4 is *equal to* 10, and denotes that the numbers 6 and 4 taken together, equal the number 10.

SECTION III.

[Apart from all other methods, the pupil should be required to test the accuracy of his work in addition, by adding from the top of the columns downwards.]

In the following exercises take the given number for the first and second lines or rows, their sum for the third, the sum of the third and second for the fourth, and so on, adding the last two for the next row. Finally, add the whole.

NOTE.-5r. means 5 rows, 6 r. means 6 rows, &c.

EXAMPLE.—What is the sum of 3456 extended to 5 rows.

	0	P	E	R	A	T	I	0	r	٧.	
1.9.0								~			

First row 3456

Second " 3456 Same as first row.

Third " 6912 = Sum of second and first.

Fourth " $10368 \equiv$ Sum of third and second.

Fifth " 17280 = Sum of fourth and third

Ans. $41472 \equiv$ Sum of all the rows.

	6 r.		6 r.		6 r.			6 r	
(1)	63	. (8)	171	(15)	1233	(2)	2)	109872	1
(2)	72 :	(9)	621	(16)	4581	(2:	3)	234531	
(3)	45	(10)	531	(17)	6543	(24	б.	901827	
(4)	54	(11)	432	(18)	7632	(28	5)	728109	
(5)	27	(12)	135	(19)	8901	(20	() ·	879102	
$\begin{pmatrix} 6 \\ 7 \end{pmatrix}$	36	(13)	252	(20)	9342	(27	Ú)	512361	
(0)	18	(14)	801	(21)	1899	(28)	987642	
(29)	6327	81	(34)	12345	84	(39)	240	357897	1
(30)	0971	82	(35)	27810	99	(40)	304	578927	
$(\partial 1)$	9870	06	(36)	37657	89	(41) •	457	028973	
(32)	0108	11	(37)	45721	71	(42)	758	203434	
(00)	1010	00	(38)	57060	18	(43)	987	645312	

SHOW THAT

(1)	45	extended	8	r.	-	18	extended	8	r.	+	27	extended	8 1	
(2)	54	""	8	r.		36	"	8	r.	+	18	"	8 -	
(3)	153	"	6	r.		90	"	6	r.	+	63	"	6 -	•
(4)	162	"	6	r.	===	72	"	6	r.	+	90	"	6 -	•
(5)	549	"	5	r.	_	261	"	5	r.	+	288	**	5 1	•
(6)	1089	"	4	r.	==	531	"	4	r.	+	558	"	4 r	

SECTION IV.

1. Find the sum of 1247 + 91679 + 27 + 1987 + 1800+ 1796. Ans. 98536.

2. What is the sum of 250120 + 30402 + 7850 + 465000 + 10046 + 65045. Ans. 828463.

3. Add together 786, 840, 910, 403, 783, 650, 809, 670 408, 310, and 652. Ans. 7221.

4. Add together 16075, 250763, 7561, 830654, 293106, 2537104, and 316725. Ans. 4251988.

5. Find the sum of 629405, 7629, 31000401, 263012, 1300512, 390217, and 13268. Ans. 33604444.

6. A man gave 5460 dollars to his eldest son, to the next 4065, to the next 6750, to the next 8000, and to the youngest 7276; how much did he give to all. Ans. 31551 dollars.

7. A merchant on settling up his business, found he owed one creditor 176 dollars, another 841 dollars, another 1356 dollars, another 2370 dollars, another 840 dollars; what was the amount of his debts? Ans. 5583 dollars.

8. Find the sum of the following numbers : seven hundred and fifty-six, four hundred and twenty-five, six hundred and

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thirty-three, five hundred and forty-one, nine hundred and sixty-nine. Ans. 3324.

9. Add together six, sixty-five, six hundred and fifty-five, three thousand six hundred and fifty-five, twenty-six thousand three hundred and fifty-nine. Ans. 30740.

10. A man willed his estate to his wife, two sons, and four daughters. To his daughters he gave 2630 dollars apiece, to his sons, each 4647 dollars, and to his wife 3595 dollars or what value was his estate? Ans 23409 dollars.

11. A man bought three houses and lots for 15780 dollars, and sold them so as to gain 695 dollars on each lot; for how much did he sell them? Ans. 17865 dollars.

SUBTRACTION.

Explanatory Exercises.

17. A farmer having 8 cows, sold 3 of them, how many cows had he left?

ANALYSIS.—He had as many left as 8 cows less 3 cows, which are 5 cows. Therefore he had 5 cows left.

2. David has 9 peaches, and George has seven peaches how many more peaches has David than George?

ANALYSIS.—Here, as in the former case, he has as many more as 9 peaches less 7, which are 2 peaches. Therefore he has 2 peaches more than George.

3. A merchant having 14 barrels of flour, sells nine of them; how many has he left?

4. Paid 19 dollars for a coat, and 4 dollars for a vest; how much more did the coat cost than the vest?

18. We see from the foregoing that Subtraction is the process of finding the difference between two numbers.

19. The Minuend is the number to be subtracted from.

20. The Subtrahend is the number to be subtracted.

21. The **Difference** or **Remainder** is the result obtained by the process of subtraction.

22. The sign —, is called *minus*, which signifies *less*. When blaced between two numbers, it denotes that the one

ed 8 r. 8 r. 6 r. 6 r. 5 r.

4 r.

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50 +8463. , 670 7221. 3106, 1988. 3012, 4444. next ngest llars. owed 1356 was llars. idred

l and

SUBTRACTION.

after it is to be taken from the one before it. Thus, 7-3, is read 7 minus 3, and means that 3 is to be taken from 7.

CASE I.

23. When no figure in the subtrahend is greater than the corresponding figure in the minuend.

EXAMPLE 1.—From 697 take 432.

18

OPERATION.ANALYSIS.—We write the less num-
ber under the greater, with units under
units, tens under tens, &c., and draw a
line underneath. Then, beginning at
the right hand, we subtract separately

each figure of the subtrahend from the figure above it in the minuend. Thus, 2 from 7 leaves 5, which is the difference of the units; 3 from 9 leaves 6, the difference of the tens; 4 from 6 leaves 2, the difference of the hundreds. Hence, we have for the whole difference 2 hundreds, 6 tens, and 5 units, or 265.

Exercises for the Slate.

SECTION I.

Minuend Subtrahend	(1) 543 212	(2) 876 334	(3) 367 152	(4) 978 725
-				
Remainder	331	542	215	253

 5. From 98765 take 74251
 Remainders.

 6. From 291352 take 170341
 24514

 7. Subtract 291352 from 895752
 604400

8. A man bought a property for 3724 dollars, and sold it for 4856 dollars; how much did he gain? Ans. 1132 dollars.

9. A drover bought 1598 sheep, and sold 473 of them; how many had he left? Ans. 1125 sheep.

10. A merchant sold flour to the amount of 6578 dollars, and by so doing gained 2426 dollars; how much did he pay for the flour? Ans. 4152 dollars.

CASE II.

24. When any figure in the subtrahend is greater than the corresponding figure in the minuend.

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2

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doll. 3. yard 4. and rem 5.

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8 53

ainders. 24514121011 604400 l sold it dollars. them: sheep. dollars, he pay dollars.

er than

EXAMPLE 1.-From 846 take 359.

OPERATION.

ANALYSIS .- Since we cannot take 9 units Hundreds. Tens. Units. from 6 units, we take 1 ten from the 4 tens, and add it to the 6 units, which makes 16 units; 9 units from 16 units leave 7 units. Having taken 1 ten from the 4 tens we have only 3 tens left, and as we cannot take 5 tens from 3 tens 846 we take 1 hundred from the 8 hundreds, and 3 5 9 add it to the 3 tens, which makes 13 tens; 5 tens from 13 tens leave 8 tens. Having taken 4 8 7 1 hundred from the 8 hundreds we have only

7 hundreds left, and 3 hundreds from 7 hundreds leave 4 hundreds; we therefore have for the total remainder 487.

25. From the preceding examples and illustration we have the following general

RULE. I. Write the less number under the greater, placing units of the same order in the same column.

II. Begin at the right hand, and take each figure of the subtrahend from the figure above it, and write the result underneath.

III. If any figure in the subtrahend be greater than the corresponding figure above it, add 10 to that upper figure before subtracting, and in subtracting the next left hand figure remember that the figure above is 1 less.

Mental Exercises.

1. A man, having 25 dollars due him, received a ton of hay worth 11 dollars, and the remainder in money; how much money did he receive ?

A farmer sold a cow for 23 dollars, that cost him 31 2. dollars; how much did he lose by the bargain ?

3. From a piece of broadcloth containing 72 yards, 26 yards were cut; how many yards remained ?

4. A boy found 8 apples under one tree, 10 under another, and 6 under another; he ate 4, gave away 6, and carried the remainder home; how many did he take home?

A farmer had 43 sheep in one lot, 39 in another, and 5. 40 in another; from the first he sold 20, from the second 15, and from the third 17; how many had he at first, and how many had he left?

Exercises for the Slate.

NOTE.—To test the accuracy of the work, require the pupil to subtract the answer from the minuend; the result, if correct, will give the subtrahend.

	,	SECT	ION II.			
	(1) 203688 135792	(2) 10368 6912	(13 9	3) 689 126	(4) 17361 11574	
	(5) 74061 49374	(6) 254718 169812	(7 163 109	7) 917. 278	(8) 2367468 1578312	۱
			1 (1 0)			r.
(9)	18717-	- 12478	(16)	23959	6137 - 159730758	
(10)	703701-	- 469134	$\left(\begin{array}{c}17\\1\end{array}\right)$	24340	1058 - 162267372	*
	103/010-	- 691344	(18)	27272	9889-181819926	•
(12)	1281938-	- 804022	(19)	11100	00292 - 14031320	
(13)	9017035	- 400/044	$\begin{pmatrix} 20\\ 01 \end{pmatrix}$	20920	112024/14	
15	2017030-	-1608048		1090	3505 - 19875670	
(10)	41140+4-	- 1000040	(22)	1001		
		SECTI	ON III.			
1.	From 723	8469153 take	42983	76593		1)
~.	110m (20		12000		Ans. 2940092560	
2.	From 975	8354961 take	49382	97562.		
					Ans. 4820057399.	
3.	From 973	8426549 take	94236	89284.		
					Ans. 314737265.	
4.	Take 642	8395823 from	903548	32762.		
	(T) 1 700				Ans. 2607086939.	
5.	Take 729	384 from 9203	376842.	•		
0	E 079	4 1 9009 4-1			Ans. 919647458.	
0.	r rom 978	4 + 3968, tai	ce 5268	s + 5	4 mg 5910	
7	From 876	1 1 998 1 4	1 taka	30 1	Alls. 0210.	
••	FIOM 010	* + 000 + *	1, take	00 T	Ang 2359	
8.	A man o	wning a bloc	k of }	mildin	rs worth 155965	
dollar	rs, keeps it	insured for 10	9240 d	ollars	how much would	
he los	se in case t	he buildings sl	hould h	e dest	roved by fire?	
				A	ns. 46025 dollars.	•
9.	A mercha	int paid 1789	4 dolla	ars for	a steamboat, and	

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afterwar by nis b 10. thousan 11. barrels another how ma

26. Ana:

15 cent instead cents, 3 2. I cost? 3. V 4. V tons cos 27.

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86939.

47458.

. 5210. 24. . 2359. 155265 . would re? dollars. at, and afterwards sold it for 16985 dollars; how much did he lose by nis bargain? Ans. 909 dollars.

10. What sum added to 13678 will make twenty-six thousand and twenty-three? Ans. 12345

11. A forwarding merchant had in his warehouse 7560 barrels of flour; he shipped at one time 1970 barrels, at another time 1150 barrels, and at another time 1685 barrels; how many barrels remained? Ans 2755 barrels.

MULTIPLICATION.

Explanatory Exercises.

26. 1. What will 3 melons cost at 15 cents apiece?

ANALYSIS.—Three melons will cost as much as the price, 15 cents, taken 3 times. Thus, 15 + 15 + 15 = 45. But, instead of adding, we may say,—since one melon costs 15 cents, 3 melons will cost 3 times 15 cents, or 45 cents.

2. If a ream of paper cost 3 dollars, what will 12 reams cost?

3. What will 5 hats cost at 2 shillings each ?

4. When hay is selling for 16 dollars a ton, what will 8 tons cost? 9 tons? 12 tons? 15 tons?

27. Multiplication is the process of taking one of two given numbers as many times as there are units in the other.

28. The Multiplicand is the number to be taken.

29. The Multiplier is the number which shows how many times the multiplicand is to be taken.

30. The **Product** is the result obtained by the process of multiplication.

31. The Factors are the multiplicand and multiplier.

NOTE.--1. Factors are producers, and the multiplicand and multiplier are called factors because they produce the product.

2. Multiplication is a short method of performing addition when the numbers are equal.

32. The sign, \times , placed between two numbers, denotes that they are to be multiplied together. Thus, 9×5 , is read 9 multiplied by 5, or 5 times 9.

Multiplication Table.

1	Twi	ce	3	tir	nes	4	time	es	1 5	tin	les	1 6	tim	09	7	tim	1
1	ar	e 2	1	ar	e 3	1	are	4	1	are	5	1	aro	GO G	1	UIII	ies
2	2 66	4	2	66	6	2	66	8	2	66	10	2	41 G	19	1	are	1.4
3	3 66	6	3	66	9	3	66	12	3	"	15	3	66	18	2	"	14
4	66	8	4	66	12	4	66	16	4	66	20	1	66	94	0	"	21
5	5 66	10	5	66	15	5	"	20	5	66	25	5	66	20	4 5	"	20
6	66	12	6	66	18	6	66	24	6	66	30	6	66	96	C		30
7	66	14	7	66	21	7	66	28	7	66	35	7	"	19	07	44	42
8	66	16	8	66	24	8	"	32	8	66	40	8	66 .	44	0		49
9	66	18	9	46	27	9	"	36	9	66	15	0	"	40	0		20
10	66	20	10	46	30	10	"	40	10	66	50	10	44	04	9		63
11	66	22	11	"	33	11	"	44	11	66	55	11	"	00	10		70
12	66	24	12	66	36	19	66	18	19	"	60	10		00	11	••	77
					00			401	14		00	12		12	12	••	84
8	tim	es	1	9	time	s	10	ti	mes	5	11	tin	nes	,	12	tim	es
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	are	8		1	are	9	1	ar	6 I.	V	1	are	11		1	are	12
2	are "	16		12	are "	9 18	$\begin{vmatrix} 1\\2 \end{vmatrix}$	ar	2	0	$\frac{1}{2}$	are "	11 22		1 2	are "	12 24
2 3	are "	8 16 24		1 2 3	are "	9 18 27	$\begin{vmatrix} 1\\2\\3 \end{vmatrix}$	ar "	20	0	1 2 3	are "	11 22 33		1 2 3	are "	12 24 36
2 3 4	are "	16 24 32		1 2 3 4	are "	9 18 27 36	$\begin{vmatrix} 1\\2\\3\\4 \end{vmatrix}$	ar "	20 20 30 40	0	1 2 3 4	are " "	11 22 33 44		1 2 3 4	are "	12 24 36 48
2 3 4 5	are " "	8 16 24 32 40		1 2 3 4 5	« « «	9 18 27 36 45	$ 1 \\ 2 \\ 3 \\ 4 \\ 5 $	ar ""	20 30 40 50		$ \begin{array}{c} 1 \\ 2 \\ 3 \\ 4 \\ 5 \end{array} $	are " " "	11 22 33 44 55		1 2 3 4 5	are " "	12 24 36 48 60
2 3 4 5 6	are "	8 16 24 32 40 48		1 2 3 4 5 6		5 18 27 36 45 54	$\begin{vmatrix} 1\\ 2\\ 3\\ 4\\ 5\\ 6\end{vmatrix}$	ar "' "'	20 30 40 50 60		1 2 3 4 5 6	are " " "	11 22 33 44 55 66		1 2 3 4 5 6	are " " " "	12 24 36 48 60 79
2 3 4 5 6 7	are " " " "	$ \begin{array}{r} 8 \\ 16 \\ 24 \\ 32 \\ 40 \\ 48 \\ 56 \\ \end{array} $		1 2 3 4 5 6 7		9 18 27 36 45 54 53	$ \begin{bmatrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \\ 7 $	ar "' "' "'	8 1 2 3 4 5 6 7		1 2 3 4 5 6 7	are ((((((((11 22 33 44 55 66 77		1 2 3 4 5 6 7	are " " " " " "	12 24 36 48 60 72 84
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2 3 4 5 6 7 8 9	are " " " " " " "	16 24 32 40 48 56 64 72		1 2 3 4 5 6 7 8 9		9 18 27 36 45 54 53 72 81	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	ar "" " " "	20 20 30 40 50 60 70 80 90		1 2 3 4 5 6 7 8 9	are " " " " " " "	11 22 33 44 55 66 77 88 99		1 2 3 4 5 6 7 8 9	are " " " " " " " " " " "	12 24 36 48 60 72 84 96
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2 3 4 5 6 7 8 9 10 11	are 	16 24 32 40 48 56 64 72 80 88 96	1	1 2 3 4 5 6 7 8 9 0 1 9		9 18 27 36 45 54 53 72 31 90 9	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	ar "" "" "" "" "" "" "" "" "" "	20 30 40 50 60 70 80 90 100 110		$ \begin{array}{c} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \\ 7 \\ 8 \\ 9 \\ 10 \\ 11 \\ 12 \\ 12 \\ 10 \\ 11 \\ 12 \\ 11 \\ 12 \\ 11 \\ 12 \\ 11 \\ 12$	are " " " " " " " " " " " " "	11 22 33 44 55 66 77 88 99 .10 .21		1 2 3 4 5 6 7 8 9 10	are "	12 24 36 48 60 72 84 96 08 20 32

CASE I.

When the multiplier does not exceed 12. 33. EXAMPLE 1.-Multiply 484 by 4.

		Hundreds.	Tens.	Units.	
Multiplicand		4	8	4	
Multiplier				4	
Units			1	6	
Fens		3	2		
Hundreds	1	6			
roduct	1	9	3	6	

ANALYSIS.-In this example it 18 OPERATION. required to take 484 four times. If we take the units of each order 4 times, we shall take the entire number 4 times. Therefore, writing the multiplier under the unit figures of the multiplicand, we proceed as follows: 4 times 4 units are 16 units; 4 times 8 tens are 32 tens; 4 times 4 hundred are 16 hundreds; and adding these partial products, we obtain the entire product, 1936

The other v OPER. 4

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as man 4. day, a earn in 5. 6 dolla dollars the ves

> I I 1.

2.

The operation in this example may be performed in another way, which is the one in common use

OPERATION. ANALYSIS.—Writing the numbers as before, 484 we begin at the right hand or unit figure, and 4

1936

say: 4 times 4 units are 16 units, which is 1 ten and 6 units; write the 6 units in the product in units' place, and reserve the 1 ten to add to the next product. 4 times 8 tens are 32

tens, and the 1 ten reserved in the last product added, are 33 tens, which is 3 hundreds and 3 tens; write the 3 tens in the product in tens' place, and reserve the 3 hundreds to add to the next product. 4 times 4 hundreds are 16 hundreds, and 3 hundreds added are 19 hundreds, which being written in the product in the places of hundreds and thousands, gives, for the entire product, 1936.

34. From the preceding example and illustration we have the following

RULE. I. Write the multiplier under the multiplicand, placing units of the same order under each other.

II. Beginning with the unit figure multiply each figure of the multiplicand by the multiplier, writing down and carrying as in addition.

Mental Exercises.

1. If a man can dig 28 bushels of potatoes in one day how many can he dig in 7 days? in 9 days? in 12 days?

2. At 81 dollars apiece, what will be the cost of 4 horses ? of 11 horses? of 9 horses?

In an orchard there are 16 cherry trees, and 9 times 3. as many apple trees; how many apple trees are there?

4. If one boy earns 15 cents a day, another 22 cents a day, and another 30 cents a day; how much can the 3 boys earn in 5 days?

A man bought 9 yards of cloth for a suit of clothes, at 5.6 dollars a yard : he paid 5 doilars for making the coat, 2 dollars for making the pantaloons, and 1 dollar for making the vest; what did the suit cost him?

Exercises for the Slate.

SECTION I.

1. Multiply 543216573 by 2, 3, 4, 5, 6, 7

2. Multiply 345678921 by 9, 8, 7, 6, 11.

imple it is times. If h order 4 tire numriting the figures of roceed as 16 units; ; 4 times eds; and ducts, we 1936

7 times

66 3

66 4

7

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1 are

2 66 14

5 " 35

6 66

7 66 49

8 " 56

9 "

10 "

11 " 77

12 66

> 2 66 24

3 66 36

5 " 60

6 66 72

7 " 84

8 " 96

9

10

11

12

12 times

1 are 12

" 4

" 108

" 120

"132

" 144

Verify the following-

3)	47	×	2		19	×	2	+	28	×	2	L	(7)	369	×	2	-	246	×	2+	123	X	1
(4)	59	×	2	-	27	×	2		32	×	2	L	(8)	663	×	2	-	431	×	2+	232	×	4
(5)	75	X	2		49	×	2	+	26	×	2	ł.	(9)	984	×	2 :	=	615	×	2+	369	X	00
(6)	124	X	2	-	56	Х	2	+	68	×	2	1	(10)	196	X	2:		94	X	2+	102	X	-

NOTE.—Instead of 2 as multiplier take successively 3, 4, 5, 6, 7, 8 9, 10, 11, and 12 as multipliers, using the exercises in the section.— Thus,

(10) $196 \times 9 = 94 \times 9 + 102 \times 9$, &c.

11. What will be the cost of 344 cords of wood at 4 dolars a cord? Ans. 1376 dollars.

12. In one day are 86400 seconds; how many seconds in 7 days? Ans. 604800 seconds.

13. In one bushel there are 256 gills; how many gills are there in 12 bushels? Ans. 3072 gills.

CASE II.

35. When the multiplier is a composite number, none of whose factors is greater than 12.

36. A Composite Number is one that may be produced by multiplying together two or more numbers. Thus, 18 is a composite number, since $(\times 3 = 18; \text{ or } 9 \times 2 = 18; \text{ or } 3 \times 3 \times 2 = 18.$

37. The **Component Factors** of a number are the several numbers which, multiplied together, produce the given number. Thus, the component factors of 16 are 4 and 4, $(4 \times 4 = 16)$; or, 8 and 2, $(8 \times 2 = 16)$; or, 2 and 2 and 2 and 2, $(2 \times 2 \times 2 \times 2 = 16)$.

NOTE.—The pupil must not confound the factors with the parts of a number. Thus, the factors of which 14 is composed are 7 and 2. $(7 \times 2 = 14)$; while the parts of which 14 is composed are 8 and 6 (8 + 6 = 14), or, 10 and 4, (10 + 4 = 14). The factors are multiplied, while the parts are added.

EXAMPLE 2.—What will 36 cows cost, at 196 dollars each? Multiplicand 196 cost of 1 cow. ANALYSIS.—The

1st factor	4
	784 cost of 4 cowe
2nd factor	9
Product	7056 . ost of 36 cows.

A NALYSIS.—The factors of 36 are 4 and 9. If we multiply the cost of 1 cow by 4, we obtain the cost of 4 cows; and by multiplying the cost of 4 cows by 9, we obtain the cost Hence

RULI more fa

II. M and tha have be product

> Find (1) (2)

(3)(4)(5)

(6) (7)

15.

16. how mu

17. and, sev 18. piece co did the

38.

Exan Multipli Mujtipli

Product

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the cost of 9 times 4 cows, or 36 cows, the number bought. Hence we have the following

RULE. I. Separate the composite number into two or more factors.

II. Multiply the multiplicand by one of these factors, and that product by another, and so on until all the factors have been used successively, the last product will be the product required.

SECTION IL.

Find the product of-

(1)	1236456	X	15	(8)	87645231×32	
(2)	2345679	X	16	(9)	18765432×35	
(3)	4571325	X	18	(10)	33236775×36	
(4)	7235469	X	21	(11)	21876543×42	
(5)	9876519	X	24	(12)	54670104 × 44	
6)	8297568	X	27	(13)	32336775×54	
7)	9726354	X	35	(14)	68206986×55	

15. What will 573 oxen cost, at 63 dollars each? . Ans. 36099 dollars.

16. If an army consume 1645 pounds of bread in a day, how much will they consume in 96 days?

Ans. 157920 pounds. 17. How many are 84 times six hundred and four thousand, seven hundred and fifty-six? Ans. 50799504. 18. A merchant bought 145 pieces of broadcloth, each

piece containing 48 yards, at 4 dollars a yard; how much did the whole cost? Ans. 27840 dollars

CASE III.

38. When the multiplier consists of two or more figures.

EXAMPLE 3.—Multiply 646 by 29.

Multiplicand 646 Multiplier 29

> 5814 9 times the multiplicand. 1292 20 times the multiplicand.

Product 18734 29 times the multiplicand.

the multiplier, exactly as in Case I. We then multiply by the 2 tens. 2 tens times 6 units, or 6 times 2 tens, are 12 tens, equal to 1 hundred, and 2 tens we place the two tens

ANALYSIS.— Writing the multiplicand and mul tiplier as in Case I, we first multiply each figure of the multiplicand by the unit figure of

 $+123 \times 2$ +232 $\times 2$ +369 $\times 2$ +102 $\times 2$

, 5, 6, 7, 8 e section.—

l at 4 dol-6 dollars. seconds in 0 seconds. y gills are 3072 gills.

, none of

y be pros. Thus, 2 = 18;

r are the oduce the are 4 and 2 and 2

n the parts re 7 and 2, are 8 and 6 are multi-

ars each? 15.— The ure 4 and htiply the by 4, we cost of 4 by multiost of 4 we obtain

under the tens' place in the product already obtained. 12 tens times 4 tens are 8 hundreds, and 1 hundred of the last product added are 9 hundreds; we write the 9 under the hundreds' place in the product. 2 tens times 6 hundreds are 12 thousands, equal to 1 ten thousand and 2 thousands, which we write in their appropriate places in the product. Then adding the two products we have the entire product, 18734.

Note.—1. When the multiplier contains two or more figures, the several products obtained by multiplying by each figure are called *partial* products.

2. When there are ciphers between the significant figures of the multiplier, pass over them and multiply by the significant figures only. remembering to put the results in their proper places.

39. From the preceding examples and illustrations we deduce the following general

RULE. I. Write the multiplier under the multiplicand, placing units of the same order under each other.

II. Multiply the multiplicand by each figure of the multiplier successively, beginning with the unit figure, and write the first figure of each partial product under the figure of the multiplier used, writing down and carrying as in Addition.

III. If there are partial products, add them, and their sum will be the product required.

NOTE.—To multiply any number by 10, annex 0 to the number, thus: $64 \times 10 = 640$; to multiply by 100 annex 00, thus: 64×100 = 6400; to multiply by 1000 annex 000, and so on.

40. When there are ciphers at the right hand of one cr both the factors.

RULE. Multiply the significant figures of the multiplicand by those of the multiplier, and to the product annex as many ciphers as there are on the right of both factors.

SECTION III.

Multiply and add together the products of-

(1)	1678583214 by 701 and 299	(6) 912837654 by 827 and 173	
(2)	7843221567 by 679 and 321	(7) 764583912 by 531 and 469	
(3)	8976510234 by 348 and 652	(8) 837654219 by 204 and 796	
(4)	2190678093 by 959 and 41	(9) 376542198 by 304 and 696	
(5)	3672815490 by 869 and 131	(10) 6354819027 by 801 and 199	

SECTION IV.

EXAMPLE. $-546372 \times 47 = 546372 \times 19 + 546372 \times 28$. Thus,

38 218

5

256

Work

1) 8765

(2) 1325 (3) 5431

(4) 6578

(5) 7321

(6) 8314

(7) 9076

(8) 7569 (9) 7986

(10) 5776

Divide three figu as in the 134865

Sum or pro The multip

Sum of pro

(2) (2) (2) (3) (2) (4) (3) (4) (3) (5) (5) (5) (6) (4)

(7) (7) (7)

(8) 4

(9) 3 (10) 7

546372 47	$\begin{array}{c} 546372 \\ 19 \end{array}$	546372 28
3824604 2185488	$\overline{\begin{array}{c}4917348\\546372\end{array}}$	4370976 1092744
25679484	$\frac{10381068}{15288416}$	15298416

25699484

Work the following as the preceding example-

(1)	87654321	X	14 =	87654321	X	6 +	87654321	X	8
(2)	13254876	×	19 =	13254876	X	8 +	13254876	$\hat{\mathbf{x}}$	11
(3)	54312786	\times	25 =	54312786	X	12 +	54312786	$\hat{\mathbf{x}}$	13
(4)	65784123	\times	37 =	65784123	X	18 +	65784123	X	19
(5)	73214658	\times	49 =	73214658	X	24 +	73214658	X	25
(6)	83146752	\times	65 =	83146752	X	39 +	83146752	x	26
(7)	90765639	\times	104 =	90765639	Х	39 🕂	90765639	X	65
(8)	75697281	\times	143 =	75697281	X	88 -	75697281	x	55
(9)	79865379	\times	592 =	79865379	X	286 +	79865379	X	306
(10)	57763323	X	111 =	57763323	X	99 -	57763393	$\mathbf{\nabla}$	10

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SECTION V.

Divide each of the following exercises into two periods of three figures each, use these as multipliers, and test the results as in the following example : 134865 thus divided gives the multiplie

of

of one cr	1348 1348	$65 \times 134 = 18071910$ $65 \times 865 = 116658225$	ers 154, 865, then
actors.	Sum or products The multiplicand	$\frac{134730135}{134865}$	
	Sum of products and	multiplicand 134865000 =	[plicand. = 1000 times the multi-
27 and 173 31 and 469 04 and 796 04 and 696 01 and 199		$ \begin{array}{r} (11) & 309690 \\ (12) & 327672 \\ (13) & 427572 \\ (14) & 456543 \\ (15) & 502497 \\ (16) & 617382 \\ (17) & 604205 \end{array} $	$\begin{array}{cccccc} (21) & 892107 \\ (22) & 807192 \\ (23) & 735264 \\ (24) & 702297 \\ (25) & 586413 \\ (26) & 475524 \end{array}$
546372 X	$ \begin{array}{c} (1) & 357643 \\ (8) & 463536 \\ (9) & 375624 \\ (10) & 705294 \end{array} $	(17) 694305 (18) 264735 (19) 763236 (20) 789210	$\begin{array}{ccccc} (27) & 486515 \\ (28) & 390609 \\ (29) & 420579 \\ (30) & 614385 \end{array}$

Let the following questions be worked and their accuracy tested by casting out the 9's as follows :

Add together the figures in each factor, casting out the 9's as they arise in summing, and multiply the remainders together; then if the excess of the 9's in the product is equal to the excess of the 9's in the total product, the work, unless errors are made which counterbalance each other, is correct.

EXAMP	LE.	
Jultiplicand	5468	PROOF.
Iultiplier	74	
		\1/
	21872	5 2
	38276	1
Product	101022	
TOUTUCE	404002	

The excess of the 9's in the multiplicand is 5, and in the multiplier is 2, their product is 10, and the excess of the 9's is 1, which is equal to the excess of the 9's in the total product.

(1)	Multiply	7482695	by	598.	Ans.	4,474,651,610
(2)	Multiply	6574189	by	679.		4.463.874.331
(3)	Multiply	5394628	bv	786.		4.240.177.608
(4)	Multiply	5984783	by	203.		1.214.910.949

For further exercises take the examples in Section III, page 26, using the first multiplier only in each question, and doubling the first figure of the multiplicand.

SECTION VI.

1 What is the product of 71476×9187 ?

Ans. 656650012

2. Multiply 8010700 by 9000909. Ans. 72103581726300.

3. In 1 mile there are 63360 inches; how many inches in 45 miles? Ans. 2851200.

4. If in one year there are 8766 hours; how many hours in 72 years? Ans. 631152 hours.

5. What cost 97 oxen at 29 dollars each?

Ans. 2813 dollars.

6. If a person deposit annually in the Savings' Bank 407 dollars; what will be the sum deposited in 27 years?

 Ans. 10989 dollars.

 7. Multiply 875946 by 807004
 Ans. 706891925784.

 8. Multiply 948657 by 908070.
 Ans. 861446961990.

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51,610 74,331 77,608 10,949 Section III. estion, and

656650012 581726300. y inches in s. 2851200. nany hours 152 hours.

13 dollars. ' Bank 407 rs?89 dollars. 391925784. 46961990.

Multiply 496783 by 4263. 9.

Ans. 2117785929. 10. If a hogshead of sugar contains 1096 pounds; how many pounds in 27 hogsheads ? Ans. 29592 pounds.

11. Find the continued product of 186, 396 and 56.

Ans. 4124736.

12. Multiply eight thousand and nine by nine thousand and sixteen. Ans. 72209144.

13. Multiply one million one thousand one hundred by nine thousand nine hundred and ninety. Ans. 10000989000

14. If a railroad car moves 38 miles an hour; how far would it go in 30 days, of 24 hours each, allowing 2 hours each day for stopping? Ans. 25080 miles.

15. If 9 men can do a piece of work in 13 days; how long would it take one man to do the same work? How many men would do it in one day? Ans. 117 days. 117 men.

16. A merchant bought 563 barrels of shoe pegs, each barrel containing 4 bushels, at 5 shillings a bushel; how many shillings did he give for the whole ? Ans. 11260 shillings.

DIVISION.

Explanatory Exercises.

41. 1. A boy has 32 cents which he wishes to give to 4 of his companions, to each an equal number how many cents must each receive?

ANALYSIS .- Since there are four companions each must receive as many cents as 4 is contained times in 32, which is 8 times. Therefore, each boy will receive 8 cents.

How many barrels of flour, at 8 dollars per barrel, can 2. you buy for 56 dollars?

ANALYSIS .--- Since 8 dollars will buy one barrel, 56 dollars will buy as many barrels as 8 is contained times in 56, which 18 7 times. Therefore 7 barrels of flour, at 8 dollars each, can be bought for 56 dollars.

3. If a man can dig 6 rods of ditch in a day, how many days will it take him to dig 96 rods?

4. A farmer bought 49 sheep for 196 dollars; what did they cost a piece?

42. Division is the process of finding how many times one number is contained in another.

48. The Dividend is the number to be divided.

44. The Divisor is the number divided by.

45. The **Quotient** is the result obtained by the process of division, and shows how many times the divisor is contained in the dividend.

Note.--1. When the dividend does not contain the divisor an exact number of times the part of the dividend left is called the *remainder*, and it must be less than the divisor.

2. As the remainder is always part of the dividend, it is always of the same name or kind.

3. When there is no remainder the division is said to be complete.

46. The sign, \div , placed between two numbers, denotes division, and shows that the number on the *left* is to be divided by the number on the *right*. Thus, $39 \div 3$, is read 39 divided by 3.

Division is often indicated by writing the dividend above and the divisor below a short horizontal line. Thus, $\frac{3}{2}$

CASE I.

47. When the divisor does not exceed 12.

EXAMPLE 1.—How many times is 3 contained in 936?

OPERATION. Dividend. D visor 3)936

312

Qu tient

ANALYSIS.—After writing the divisor on the left of the dividend, with a line between them, we begin at the left hand and say: 3 is contained in 9 hundreds, 3 hundreds times, and write

3 in hundreds' place in the quotient: then 3 is contained in 3 tens 1 ten times, and write 1 in tens' place in the quotient; then 3 is contained in 6 units 2 units times; and writing the 2 in units' place in the quotient, we nave the entire quotient, 312.

2. How many times is 4 contained in 1684?

OPERATION. ANALYSIS .- As we cannot divide 1 thousand

4)1684 by 4, we take the 1 thousand and the 6 hundreds together, and say, 4 is contained in 16 hundreds 4 hundreds times, which we write in

hundreds' place in the quotient; then 4 is contained in 8 tens 2 tens times, which we write in he tens' place in the quotient; and 4 is contained in 4 units 1 unit time, which we write in the units' place in the quotient, and we have the entire quotient, 421. the un we en

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IV. than prefix in the

V. place

How many times is 7 contained in 2835? 3.

OPERATION.

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d above

36? e diviwith a the left l 1n 9 l write otient: n tens' 2 units it, we

usand hunin 16 ite in s contens' unit , and

ANALYSIS .- Beginning as in the last example, we say, 7 is contained in 28 hundreds 7)28354 hundreds times, which we write in the hun-405 dreds' place in the quotient; then, 7 is contained

in 3 tens no times, and we write a cipher in the tens' place in the quotient; and taking the 3 tens and 5 units together, 7 is contained in 35 units 5 units times, which we write in the units' place in the quotient, and we have the entire quotient, 405.

4. How many times is 8 contained in 987?

OPERATION. 8)987 123 3 Rem. or 123를

ANALYSIS.—Here 8 is contained in 9 hundreds 1 hundred times, and 1 hundred, or 10 tens, over, which, united to the 8 tens, make 18 tens; 8 in 18 tens, 2 tens times and 2 tens, or 20 units, over, which, united to the 7 units, make

27 units; 8 in 27 units 3 units times and 3 units over. The 3 which is left after performing the division, should be divided by 8; but the method of doing so cannot be explained until we reach fractions; so we merely indicate the division by placing the divisor under the dividend, thus, 3. (46). The entire quotient is written $123\frac{3}{8}$, which may be read, one hundred and twenty-three and three-eighths, or one hundred and twenty-three and a remainder of three.

From the foregoing examples and illustrations, we deduce the following

RULE. I. Write the divisor at the left of the dividend, with a line between them.

II. Beginning at the left hand, find how many times the divisor is contained in the fewest number of figures of the dividend that will contain it, and write the result under the dividend.

III. If there be a remainder after dividing any figure, regard it as prefixed to the figure of the next lower order in the dividend, and divide as before.

IV. Should any figure or part of the dividend be less than the divisor, write a cipher in the quotient, and prefix the number to the figure of the next lower order in the dividend, and divide as before.

V. If there be a remainder after dividing the last figure, place it over the divisor at the right hand of the quotient.

Mental Exercises.

1. If 4 casks of lime cost 12 dollars, what is the cost of 1 cask?

2. If a man perform a certain piece of work in 30 days, how long will it take 5 men to do the same? How long will it take 6 men? How long will it take 7 men?

3. If 24 pounds of tea can be purchased for 12 dollars, how much can be bought for 1 dollar? How much for 9 dollars? How much for 5 dollars?

4. Gave 96 cents for 6 pounds of raisins, what cost 1 pound? What cost 7 pounds?

5. A man gave 15 dollars for 3 barrels of apples; what was the cost of each barrel? What would 5 barrels cost at the same rate?

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Exercises for the Slate.

SECTION I.

(1)	$42240 \div 2, 4, 6, 8, 10, 11$	(5) 30888 \div 9, 3, 8
(2)	14784 - 3, 7, 11, 2, 4, 8	(6) 13608 \div 7 3 9
(3)		(7) 24648 \cdot 0 0
X	20060 5 7 6 4 9	(1) 54008 - 0, 9, 3
(4)	20500 - 5, 1, 0, 4, 8	(8) 363285 \div 5, 9, 3

SHOW THAT

(9)	369 -	- 3 ==	246 -	- 3 +	123 -	- 3
(10)	1035 -	-5 =	690 -	- 5	345 -	- 5
(11)	1368 -	-4 =	912 -	-4-	456 -	- 4
(12)	1701 -	-7 =	1134 -	-7-	567 -	- 7
(13)	7866 -	- 9 =	3231 -	-9-	4635 -	- 9

SECTION II.

$\begin{array}{c} (1) & 42 \\ (2) & 14 \\ (3) & 24 \\ (4) & 67 \\ (5) & 78 \end{array}$	$2544830 \div 6 = \\4284263 \div 7 = \\4486456 \div 8 = \\7879284 \div 6 = \\3485617 \div 7 = 1$	Quotients. 7090805 2040609 3060807 11313214 11212231	(ů) (7) (8) (9) (10)	$\begin{array}{c} 49368768 \div \\ 28949076 \div \\ 59987688 \div \\ 23935734 \div \\ 98765711 \div \end{array}$	$\begin{array}{c} \text{Quotients,} \\ 6 = 8228128 \\ 12 = 2412423 \\ 12 = 4998974 \\ 6 = 3989289 \\ 11 = 8978701 \end{array}$
	(11) 73415	$68 \div 7$		Quotients.	Rem.
	31796	$32 \div 5$ $16 \div 8$			
	842017	$63 \div 9$			•
	29476	$91 \div 12$			
	420847	$96 \div 6$			
. 5	um of Quotients	and Remai	inders	20680083	28

CASE II.

When the divisor is a composite number. 48.

EXAMPLE 1.-If 5376 dellars be divided equally among 42 men, how many dollars will each receive ? OPERATION.

ANALYSIS .- If 5376 dollars be divided 6)5376 equaliy among 42 men, each man will receive as many dollars as 42 is contained in 5376 7)896 dollars. 42 may be resolved into the factors 6 and 7; and we may suppose the 42 men Ans. 128 divided into six groups of 7 men each; divid-

ing the 5376 by 6, the number of groups, we have 896, the number of dollars to be given to each group; and dividing 896 by 7, the number of men in each group, we have 128, the number of dollars that each man will receive.

RULE. Divide the dividend by one of the factors, and the quotient thus obtained by another, and so on if there be more than two factors, until every factor has been made a divisor. The last quotient will be the quotient

SECTION III.

1.	Divide	985768545	hu	15	Quotients.
2	Divida	00700010	by	$10 = 3 \times 5$	65717909
~	Divide	08/698464	bv	$16 - 4 \vee 4$	1000.
3.	Divide	931684770	- h		42981154.
4	Dinia.	001004140	JOY	$40 = 5 \times 9$	20704100
Ξ.	Divide	945328608	bv	56 - 8 2 7	20104100.
ŏ.	Divide	3949767990	ĩ	Joo - o X /	16880868.
2	D' '1	0040101388	ъŊ	$108 = 12 \times 9$	96500011
	Divide	3176823672	hy	199 - 10	00002041.
			Uy	$102 = 12 \times 11$	24066866

49. To find the true remainder.

EXAMPLE 2.-Divide 1143 by 56, using the factors 7 and 8, and find the true remainder.

(7)1143	
56	8)163	2 rem.
(•
	20	³ rem.

 $7 \times 3 = 21$, to which is added the first remainder 2, which makes the true remainder 23.

EXPLANATION.-Suppose the dividend in the example to be pencils and to be divided into parcels each to contain 7 pencils, there will be 163 parcels and 2 pencils over. If we

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Rem.

33
DIVISION.

divide these parcels into larger ones each containing 8 of the smaller, we shall have 20 large parcels, and 3 small parcels over; but each small parcel contains 7 pencils, the second remainder is therefore equal to 21 pencils, or 7×3 , to which is added the 2 pencils which remained after the first division. Hence the

RULE. Multiply the first divisor by the second remainder, to which add the first remainder, if any.

Note .- Dividing by three factors is seldom practised.

SECTION IV.

1.	234567 - 18	6 751119 · c	•
2	345679 07	0. 101110 - 0.)
	040012 - 21	7. $804024 - 7$	>
3.	427311 - 36	8 887695 0	
1	459670 45	0. 001020 - 8.	L
	400072 - 40	$9.999999 \div 999999$	
5.	672345 - 54	10 709170 1 100	5
		10. 123430 - 108	٢.

SECTION V.

1.	958768461 -	- 27	Ans.	35509943
24	726894784 -	32	"	22715462
3.	729368465 -	35	66	20839099.
4.	675487368 -	- 36 -	"	18763538.
5.	945328608 -	56	"	16880868.
6.	1796842688 -	- 64	"	28075667.
7.	897684192 -	- 72	46	12467836.
8.	910364312 -	- 88	66	10345049.
9.	3948767388 -	-108	"	36562661.
10.	3176823672 -	-132	"	24066846

CASE III.

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50. To divide by a number consisting of several figures.

Note.—To illustrate the method of operation more clearly we will take an example usually performed by Short Division.

1. How many times is 6 contained in 564.

OPERATION.	ANALYSISAs 6 is not contained in 5 hun-
5)564(94	dreds, we take 5 and 6 as one number and
54	consider how many times 6 is contained in this
	partial dividend, 56 tens, and find that it is
24	contained 9 tens times, and a remainder To
24	find this remainder, we multiply the divisor 6
distant -an	by the quotient figure, 9 tens, and subtract the
	product, 54 tens, from the partial dividend, 56

ng 8 of the all parcels the second 7×3 , to er the first

d remain-

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DIVISION

tens, and there remain 2 tens. To this remainder we bring down the 4 mits, and consider the 24 muts the second partial dividend. Then, 6 is contained in 24 units 4 units times. Multiplying and subtracting as before, we find that nothing remains, and we have for the entire quotient, 94.

How many times is 23 contained in 4807? 2

OPERATION.
ivisor. Dividend. Quotient.
23) 4807 (209
46
207
207

D

ANALYSIS .- We first find how many times 23 is contained in 48. the least number of figures that will contain 23, and place the result in the quotient on the right of the dividend. We then multiply the divisor, 23, by the quotient figure, 2, and subtract the product, 46,

from the part of the dividend used, and to the remainder bring down the next figure of the dividend, which is 0, making 20, for the second partial dividend. Then, since 23 is contained in 20 no times, we place a cipher in the quotient, and bring down the next figure of the dividend, making a third partial dividend, 207; 23 is contained in 207, 9 times: multiplying and subtracting as before, nothing remains, and we have for the entire quotient, 209.

Notes .-- 1. When the process of dividing is performed mentally, and the results only are written, as in Case 1 the operation is termed

2. When the whole process of division is written, the operation is termed Long Division.

From the preceding illustrations we derive the following general

RULE. I. Write the divisor at the left of the dividend, as in Short Division.

II. Divide the least number of the left hand figures in the dividend that will contain the divisor one or more times, and place the quotient at the right of the dividend, with a line between them.

III. Multiply the divisor by this quotient figure, sub-tract the product from the partial dividend used, and to the remainder bring down the next figure of the dividend

Divide as before, until all the figures of the dividend have been brought down and divided.

V. If any partial dividend will not contain the divisor, place a cipher in the quotient, and bring down the next figure of the dividend, and divide as before.

 $\sqrt{1}$. If there be a remainder after dividing all the figures of the dividend, it must be written in the quotient, with the divisor underneath.

Nore .- 1. If any remainder be equal to, or greater than the divisor, the quotient figure is too small, and must be increased.

2. If the product of the divisor by the quotient figure be greater than the partial dividend, the quotient figure is too large, and must be diminished.

3. Work fire questions in Section II, page 32, by long division, before working the following questions.

SECTION VI.

$\begin{array}{c} (1) & 79865379 \div 702 \\ (2) & 81136863 \div 801 \\ (3) & 90909963 \div 117 \\ (4) & 23659245 \div 126 \\ (5) & 37018764 \div 135 \end{array}$	(6) $53146827 \rightarrow 459$ (7) $61327548 \rightarrow 558$ (8) $128713536 + 567$ (9) $123456789 + 576$ (10) $9765499 + 576$	$\begin{array}{c} (11) \ 769005474 \rightarrow 882 \\ (12) \ 407049570 \rightarrow 918 \\ (13) \ 981234567 \rightarrow 891 \\ (14) \ 900664200 \rightarrow 9099 \end{array}$
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SECTION VII.

1.	Divide 5560804464 ky 7346	Ama 750004
2.	Divide 1747071955 by 6499	1148. 150984.
2	Divide 920704 (200 by 0480.	Ans. 269485.
0.	Invide 828/864532 by 8594.	Ans. 964378.
4.	Divide 35365114332 by 93846.	Aug 970040
5.	Divide 520090979776 by 654991	A 570042.
6	Divida 749007415000 1 04021.	Ans. 794856.
7	Divide 1420921419293 by 8496427.	Ans. 874359.
f .	Divide 936864889704 by 987654.	Ans. 948576

The number of post offices in the United States in 1853 was 22320, and the revenue of this department was 5937120 dollars; what was the average revenue of each office ? Ans. 266 dollars.

A bag containing three hundred and twenty-four nuts 9. was divided among nine boys; how many did each boy get?

Ans. 36.

10. Find the 17th part of 5508.

Ans. 324.

How many miles an he ur does a train go which travels 11. 1692 miles in 47 hours ? Ans. 36.

A gentleman left £5000. By his will he directed 12. that after paying his debts, amounting to £275, the rest should be divided equally among his seven children; what was the share of each? Ans. £675.

The product of two numbers is 31383450, and one of 13. the numbers is 4050; what is the other number? Ans. 7749.

CASE IV.

51. To divide by 10, 100, 1000, &c.

EXAMPLE 1.-Divide 486 acres of land equally among 10 men; how many acres will each have?

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DIVISION.

OPERATION.

10)48 6

48 6 rem.

ANALYSIS .- According to the decimal system of notation if we remove a fignre one place toward the left by annexing a cipher, its value is increased ten fold, or is multiplied

by 10, so on the contrary, by entting off, or taking away the right hand figure of a number, each of the figures is removed one place toward the right, and consequently reduced to one-tenth its former value, or divided

For similar reasons, if we cut off two figures we divide by 100, if three, we divide by 1000, and so on. Hence the

RULE. From the right hand of the dividend cut off as many figures as there are ciphers in the divisor. Under the figures so cut off, place the divisor, and the whole will form the quotient

52. To divide by a number having ciphers on the right hand. EXAMPLE 1.—Divide 587618 by 400.

OPERATION.

4|00)5876|18

1469 18 rem.

ANALYSIS.-In this example we resolve 400 into the factors, 4 and 100, and divide first by 100, by cutting off the two right hand figures of the dividend,

(51) and we have a quotient of 5876, and a remainder of 18. We next divide by 4, and obtain 1469 for a quotient; and the entire quotient is $1469\frac{18}{400}$.

53. When there is a remainder atter dividing by the significant figures, it must be prefixed to the figures cut off from the dividend to give the true remainder.

SECTION VIII.

- 1. Divide 48600 by 100.
- 2. Divide 59673 by 1000.

3. Divide 34716 by 900.

4. Divide 178930 by 10.

6.

Divide 47321046 by 45000. 5.

Divide 1047634 by 2400.

Ans. 486.

Ans. 59 rem. 673 or 59 673 Ans. 38 rem. 516 or 38516.

Ans. 17893.

Ans. 1051, rem. 26046 Or 105126046.

Ans. 436, rem. 1234 Or 4361234.

The sum of 40000 dollars is paid to 1600 men; what 7. does each man receive ?

8. The circumference of the earth at the equator is 24898 miles. How many hours would a train of cars require to travel that distance, going at the rate of 60 miles an hour ?

Ans. 41458.

, and must g division,

the divisor,

e be greater

5474-+882 $9570 \div 918$ $4567 \div 891$ 4200+9093 $7111 \div 9009$

. 756984. . 269485. . 964378. . 376842. . 794856. . 874359. . 948576.

States in nent was of each 3 dollars. four nuts boy get? Ans. 36. Ins. 324. h travels Ans. 36. directed the rest n; what s. £675. l one of ns. 7749.

nong 10

DIVISION.

MULTIPLICATION AND DIVISION BY FRACTIONAL NUMBERS.

NOTE.—The pupil should have a clear idea of the value of simple fractions before commencing these exercises. A few oral illustrations will suffice.

EXAMPLE 1.-Multiply 1482 by 1235.

OPERATION.ANALYSIS.—Here we multiply 1483 hy1483123 in the usual way; but before adding the1235partial products we find the 5 eighths of 1483,4449namely 9267, and write it under the partial2966products, as in addition, then adding the1483four lines we obtain the required product.

10000-7

9267

1833357

We multiply by $\frac{5}{8}$ (or any other fraction) by multiplying the given number by the upper number of the given fraction and dividing the product by the lower. Thus, 1483 \times 5 (the upper figure) = 7415 which divided by eight (the lower figure) = 926 $\frac{7}{8}$.

EXAMPLE 2.-Divide 1234 by 4³/₁.

$\begin{array}{c} \text{OPERATION.} \\ 4_{4}^{3} \\ 1234 \\ 4 \\ 4 \\ 4 \\ \end{array}$	ANALYSIS.—We first bring both divisor and dividend to the same name as the given fraction—that is (in this instance) to fourths, then proceed as in division
$ \begin{array}{c} 19 \\ 38 \\ -113 \end{array} $	
$\begin{array}{r} 95\\ \hline 186\\ 171 \end{array}$	
(1) 18947635	ercises for the Slate. 2×51
$\begin{array}{c} (2) & 46738479 \\ (3) & 94327865 \\ (4) & 29768349 \end{array}$	$2 \times 6\frac{5}{2}$ Ans. 104211976 $0 \times 6\frac{1}{2}$ $303800113\frac{1}{2}$ $0 \times 30\frac{1}{4}$ $2853417916\frac{1}{4}$ $2 \times 10\frac{2}{3}$ $317528981\frac{1}{4}$
$\begin{array}{cccc} (5) & 29648732 \\ (6) & 43796284 \\ (7) & 49625483 \\ (8) & 876587938 \end{array}$	$\begin{array}{ccccccc} & \times & 2006\frac{19}{14} & & 595023097\overset{8}{8}4 \overset{8}{11} \\ \hline & & 6\frac{1}{1} & & 6737889\frac{11}{14} \\ \hline & & 30\frac{1}{14} & & 1640511\frac{19}{12}1 \\ \hline & & 143\frac{9}{14} & & 5911479\frac{3}{14}3\frac{1}{14} \end{array}$

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PRIME NUMBERS.

PROMISCUOUS EXERCISES IN THE PRECEDING RULES.

One school contains 60 pupils, a second 83, a third 1. 125, a fourth 234, a fifth 672, and a sixth 1003; how many pupils are there in the six schools

Ans. 2177. The Clyde is 100 miles long, the Forth 115, the Thames 2. 215, the Shannon 224, and the Severn 240; what would be the length of a river equal to them all?

Ans. 894 miles. Two factors are 57682 and 8493; what is their product? 3.

Ans. 489893226. How much less is 7289 than 8723? 4. Ans. 1434. There are 4 chests of drawers; in each chest there are 5. 12 drawers, and in each drawer there are placed 12 dollars ;. how many dollars are there altogether in the chests?

Ans. 576 dollars,

Multiply 94836 by 768, and divide the product by 6. 9216. Ans. 7903.

7. From the snm of 189649, 283726, 542893, 248567, 693284 and 256893 subtract 48972, multiply the remainder

by 84762, and divide the product by 9418. Ans. 19494360. 8. A man commenced business when 22 years old, and retired at the age of seventy with a fortune of 48768 dollars. Required how much he cleared on an average each year?

Ans. 1016 dollars. A wood of 6723 trees is to be thinned by cutting 9. down one tree in nine; how many will be left after this Ans. 5976.

PRIME NUMBERS.

A Prime Number is one that cannot be resolved 54. into two or more integral factors; thus 7, 3, 11, &c., are prime because they are not divisible by any number greater than 1, without a remainder.

55. To find the prime factors of any composite number. EXAMPLE 1.-What are the prime factors of 30?

OPERATION.

ANALYSIS .- We divide the given number by 2, the least prime factor; this gives an odd

• number for the quotient, divisible by the prime ____ 3 15 factor, 3, and giving the quotient 5; this being a prime number, the division cannot be carried 5 5

any further. The divisors and the last quotient, 2, 3 and 5, are all the prime factors of the given number, 30. Hence the

proof $2 \times 3 \times 5 \times 1 \equiv 30$.

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RULE. Divide the given number by the least prime factor; divide the quotient in the same manner, and so continue the division until the quotient is a prime number. The several divisors and the last quotient will be the prime factors required.

Mental Exercises.

- 1. What are the prime factors of 9, 12, 15, 16 and 18? 2. What are the prime factors of 9, 12, 15, 16 and 18?
- What are the prime factors of 39, 26, 34, 38 and 42?
 What are the prime factors of 39, 26, 34, 38 and 42?

3. What are the prime factors of 65, 85, 95, 105 and 115?

Exercises for the Slate.

Find the prime factors of the following numbers and prove he results.

$\begin{array}{c} (1) & 15 \\ (2) & 18 \\ (3) & 24 \\ (4) & 36 \end{array}$	$\begin{array}{c} (5) & 39 \\ (6) & 42 \\ (7) & 45 \\ (8) & 49 \end{array}$	(9) 57 (10) 69 (11) 78 (12) 88	$egin{pmatrix} (13) & 85 \ (14) & 91 \ (15) & 99 \ (16) & 108 \ \end{pmatrix}$	(17) 120 (18) 144 (19) 714 (20) 836	$\begin{array}{c} (21) \ 1492 \\ (22) \ 8032 \\ (23) \ 4604 \\ (24) \ 1728 \end{array}$
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GI EATEST COMMON MEASURE.

56. A Common Divisor of two or more numbers is a number that will exactly divide each of them.

57. The Greatest Common Divisor of two or more numbers is the greatest number that will exactly divide each of them.

Numbers prime to each other are such as have no common divisor.

Note.—A common divisor is called a common measure; and the greatest common divisor, the greatest common measure. The latter is usually indicated by the initial letters G. C. M.

58. To find the greatest common measure of two numbers. Ex.—Find the greatest

Ex.—Find the greatest common measure of 105 and 165. OPERATION. ANALYSIS Here we divide the

105)165(1)105

 $\overline{\begin{array}{c}
 60)105(1 \\
 60 \\
 \overline{\begin{array}{c}
 45)60(1 \\
 45 \\
 \overline{\begin{array}{c}
 15)45(3 \\
 45
 \end{array}}}$

ANALYSIS.—Here we divide the greater number, 165, by the less, 105, and thus obtain a remainder, 60, which we now make a divisor, and 105, the former divisor, the dividend, and so on. When the remainder, 15, is used as a divisor it leaves no remainder, and is therefore the greatest common measure required. Hence, $\mathbf{2}$

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(2) (3) (4)

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GREATEST COMMON MEASURE.

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165. e the less, nder. visor, divie resor it efore e re-

RULE. I. Divide the greater number by the less.

II. Divide the preceding divisor by the last remainder, and so on till nothing remains. The last divisor will be the greatest common measure.

To find the greatest common measure of three or more given numbers.

Find the C C

RULE. I. Find the greatest common measure of any two of the given numbers, by the last rule.

II. Then, that of the common divisor thus obtained and of another of the given numbers, and so on through all the given numbers.

III. The last common divisor found win oe the greatest common measure of all the given numbers.

Exercises for the Slate.

SECTION I.

$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	4623
and 384?	

12. What is the greatest common measure of 300, 525, 225, and 375?

EXAMPLE 2.-Find the greatest common measure of 42, 63, and 105.

OPERATION. $\begin{array}{c} 42 = 2 \times 3 \times 7 \\ 63 = 3 \times 3 \times 7 \end{array}$ prime factors. $105 = 3 \times 5 \times 7$ 66 "

The factors common to the three given numbers are 3 and 7. Therefore $3 \times 7 = 21$, the greatest common measure. Hence,

RULE. I. Resolve each number into its prime factors. II. Select those which are common to all the numbers, and their product will be their greatest common measure.

SECTION II.

Find the G. C. M. of (1) 10 00

(2) (3) (4)	12, 50, 60 and 72. 18, 24, 30, 36 and 42. 36, 126, 72, 216. 32, 80 and 256.	Ans. 12 .6 18 16	(5) 200, 625, and 150. Ån (6) 252, 630, 1134 and 1386. (7) 28, 140 and 280 (8) 468 and 1184.	s. 25 126 28
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LEAST COMMON MULTIPLE.

LEAST COMMON MULTIPLE.

A Multiple is a number exactly divisible by a 60. given number; thus 16 is a multiple of 4.

61. A Common Multiple is a number exactly divisible by two or more given numbers; thus, 16 is a common multiple of 2, 4, and 8.

The Least Common Multiple is the least num-62. ber exactly divisible by two or more given numbers; thus 24 is the least common multiple of 2, 4, 6, and 8. It is usually indicated by the initial letters L. C. M.

63. To find the Least Common Multiple of two or more given numbers.

EXAMPLE.-Find the L. C. M. of 4, 6, 7 and 9.

2)	4,	01 6,	РЕ 7,	RA 9	TI	ON.
3)	2,	3,	7 ₂	9	•	
	2,	1,	7,	3		

EXAMPLE. — If these numbers were prime to each other, their product would be their least common multiple. If two of the numbers or three, &c., $2 \times 7 \times 3 \times 2 \times 3 = 252$ L.C.M. which compose this pro-

duet have a common measure it must be thrown out or neglected in order to find the least common multiple. These common measures may be thrown out gradually by means of the successive divisions as 2 is a measure of 4 and 6, and 3 is a measure of 6 above. These measures should therefore be thrown out of and 9. these numbers in order to make them prime numbers. When we divide by 2 which is the smallest measure that divides as many of them as any other divisor would, we obtain for quotients, 2, 3, 7, 9, the 7 and 9 are written down because they are not divisible by 2 without a remainder. These numbers are not yet prime to each other, and we divide by 3 the smallest number that divides as many of them as any other divisor would, and we obtain 2, 1, 7, 3, the 2 and the 7 are taken down for a like reason as before-that they cannot be divided equally by 3. The numbers are now prime to each other, and their product with the divisors used = 252 the least common multiple. From this example we deduce the

RULE. Write the given numbers in a line; divide by the smallest number that will measure as many of them as any other divisor would, or that would measure more of them; write the quotients and the numbers not divided

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DECIMALS.

in another line under the former; divide the numbers in this line in the same manner, and so on till all the quo-tients are prime to each other. Then multiply these quotients with the divisors used and the product will be

NOTE .- The work is often shortened by rejecting in any line any number that is a measure of any other number in the same line, e, g,in 3, 6, 7, 12. 3 and 6 may both be rejected since they are each a measure of 12; the remaining numbers 7 and 12 being prime to each other, their product would be the least common multiple of these four

Find the L. C. M. of the following numbers.

1.	7, 35 and 98.	518.
2.	4, 9, 6 and 8.	Ans. 490.
3.	8, 15, 77 and 385.	72.
4.	12, 15, 42 and 60.	9240.
5.	21, 35 and 42.	420.
<u> </u>	4, 16, 20, 48, 60 and 72.	210.
7.	5, 10, 15, 20, 25, 30, 35 and 40	720.
8.	3, 6, 9, 12, 48, 21, 24 and 16	4200.
9.	15, 12, 128, 30, 16, 4, 320 and 96	1008.
10.	2, 4, 6, 8, 10, 12, 14, 16, 18, 20, 20, 21	1920.
32.	, = 1, 10, 10, 20, 22, 24	, 26, 28, 30 and
11.	What is the m	Ans. 1441440

What is the smallest sum of money for which I could purchase an exact number of books, at 5 dollars, or 3 dollars, or 4 dollars, or 6 dollars each? Ans. 60 dollars.

DECIMALS.

64. Decimal Fractions are the decimal divisions of a unit; thus a unit is divided into ten equal parts called tenths; each of these tenths is divided into ten other equal parts called hundredths; and so on. Since the denominators of decimal fractions increase and decrease by the scale of 10, the same as simple numbers, in writing decimals the denominators are generally omitted.

65. In simple numbers the unit's place is the starting point of notation and numeration; and so also is it in decimals.

The Decimal Point is a period, (.) which must always be placed before the left hand figure of the decimal.

 $\frac{6}{10}$ is expressed .6

$\frac{567}{1000}$ 66 .567

67. The names of the different orders of decimals, or places below units, may be easily learned from the following

e by a

divisiomnion

st numthus 24 usually

or more

f these ime to product st comtwo of ee, &c., is pron meand the nay be sions as re of 6 out of When divides ain for Decause These ide by as any nd the it they re now rs used ple we

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44 NOTATION AND NUMERATION OF DECIMALS.



By examining this table we se that

Tenths are expressed by one figure. Hundredths " two figures. Thousandths " three figures.

68. Every cipher on the left hand of a decimal reduces it to one-tenth its previous value. Thus, .5 is 5 tenths, .05 is 5 hundredths, and .005 is 5 thousandths.

Ciphers on the right do not alter the value, for .5, .50, .500 are the same as $\frac{5}{10}$, $\frac{50}{100}$, $\frac{500}{1000}$, and these are all equal.

NOTATION AND NUMERATION OF DECIMALS.

69. Rule for decimal notation.

I. Write the decimals as a whole number, placing ciphers where necessary to give each significant figure its true local value.

II. Place the decimal point before the first figure.

70. Rule for decimal numeration.

RULE. I. Numerate from the decimal point, to determine the denominator.

II. Numerate towards the decimal point, to determine the numerator.

III. Read the decimal as a whole number, giving it the mean or denomination of the right hand figure.

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3. 4.

 $(1) \\ (2)$

(3) (4) (5)

ADDITION OF DECIMALS.

4.5

Exercises for the Slate.

٤., Write 265 ten thousandths. 2.

Write six hundred and thirteen thousandths. 3.

Write 365 thousands, and 4 billionths. 4.

Write seven hundred thousandths. 5.

Write one hundred, and 2 tenths. 6.

Read the following numbers :

1.265	4.0005	C 0007
3.898	17 2000	0.0007
.5967	110.0000	1267.9876543
\$6 790=	£19.3200	3.0000678
TU.1020	.5000	123.45607890

ADDITION OF DECIMALS.

71. EXAMPLE 1.-Add 3 tenths, 45 huadredths, 16 tenths, and 365 thousandths.

OPERATION. ANALYSIS .- As in simple numbers, we write the numbers so that units shall stand under units, tenths under tenths, hundredths under hun-.45 1.6

dredths, &c. This brings the decimal points .365

directly under each other. Commencing at the

right hand we add each column, and carry as in 2.715 whole numbers, and in the result we place a

point between the units and tenths, or directly under the decimal point in the numbers added. Hence the

RULE. I. Write the numbers so that the decimal points shall stand directly under each other.

II. Add as in whole numbers, and place the decimal point, in the result, directly under the points in the num-bers added.

Mental Exercises.

1. Add .6 and .06; 10 and .01; 3.6 and 3.607; .8 and .9 2.

Add 6 hundredths and 56 thousandths; .06 and .056.

Add 20 cents and 156 cents; .20 and 1.56. 3.

Add 256 dollars and 3 dollars and 25 cents; 256 + 3 4. +.25.

Exercises for the Slate.

SECTION I.

- (1) 27.655 + 71.784 + 98.687 + 84.769.
- (2) 219.373 + 376.458 + 843.847 + 591.738 + 456.153. (3) 26.3756 + 74.5673 + 56.8948 + 74.7355 + 53.1052.
- (4) 254.172 + 888.627 + 568.296 + 756 939 + 531.704.
- (5) 214.735 + 607.434 + 669.758 + 496.376 + 730.242.

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SUBTRACTION OF DECIMALS.

SECTION II.

1. Add 25.7, 8.389, 23.056. 2.

Ans. 57.145.

Add 36.258, 2.0675, 382.45. Ans. 420.7755 Add 32.764, 5.78, 16.0037 and 49.3046. Ans. 103.8523. 3.

Add 1152.01, 14.11018, 152348.21, 9.000083. 4.

Ans. 153523.330263.

Add 37.03, 0.521, .9, 1000, 4000.0004. 5. Ans. 5038.4514.

6. What is the sum of twenty-six, and twenty-six hundredths; seven tenths; six, and eighty-three thousandths; four, and four thousandths? Ans. 37.047.

How many yards in three pieces of cloth, the first piece 7. containing 18.375 yards, the second piece 41.625 yards, and the third piece 35.5 yards? Ans. 95.5 yards.

SUBTRACTION OF DECIMALS.

72. EXAMPLE 1.—From 31.63 take 27.85.

OPERATION.	ANALYSIS.—In each of these three
31.63	examples, we write the subtrahend un-
27.85	der the minuend, placing units under
	units, tenths under tenths, &c. Com-
3.78	mencing at the right hand we subtract
71 - 70	as in whole numbers, and in the remain-
Ex. 2From	ders we place the decimal points directly
3.8674 take 1.36.	under those in the numbers above. In
OPERATION.	the second example the number of dogi-
3.8674	mal places in the minney is master
1 36	then the number of the streater
1.00	than the number in the subtrahend,
	and in the third example less. In both
2.5074	cases, we reduce both minuend and sub-
	trahend to the same name, or number
Ex. 3.—From	of decimal places by approxing einhors.
15.36 take 8 1934	or we suppose them to 1
ODUDATION	or we suppose mean to be annexed
OFERATION.	before performing the subtraction
19.36	Hence.

7.2366

8.1234

RULE. Place the numbers as in addition, subtract as in simple numbers, and insert the decimal point directly under the points in the given numbers.

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2.

3. 4.

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MULTIPLICATION OF DECIMALS.

Mental Exercises.

From five tenths take forty-nine hundredths. 1.

- From .63 take .496; 2.19 take .63; .5 take .005. 2.
- 8.
- From 16 take .006; 12.34 take 2.345; 100 take .001. From one take two hundredths. 4.
- From 3.10 dollars take 75 cents; 3.10 take .75. 5.

Exercises for the Slate.

SECTION I.

1.	From 20.34	take	13.56	15.	From	52 0704	tako	94 5100
2.	From 40.68	"	27.12	6	From	490 00104	take	34.7136
3.	From 16.272	"	10.848	17	Tuom	400.2816		286.8544
4.	From 6.5088	"	4 9900	1.	r rom	2603.52	**	1735.68
	+10000		4.0092	8.	From	983.9607	**	655 9739

SECTION II.

Find the value of-

(1) 111.1116 -22.22222 . At (2) 279.00906 -117.916 . (3) 8.135 -2.6875 . (4) 627.4 -91.7469	ns. 88.88938 161.09306 5.4475 535.6531	$\begin{array}{c} (5) \ 21.00475 \\ (6) \ 714.0916 \\ (7) \ 2298 \\ (8) \ 1000001 \end{array}$	Ans. 20.254 713.084 1 702 999 999
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MULTIPLICATION OF DECIMALS.

73. EXAMPLE.—What is the product of .25 multiplied by .5

OPERATION. ANALYSIS.—We perform the multiplication .25 in the same way as in whole numbers. Since .5 the multiplicand is 25 hundredths, and the multiplier 5 tenths, and hundredths multiplied by .125 tenths give thousandths, and thousandths being

expressed by three figures, we must have three places of decimals in the product. Hence we see the product contains as many decimal places as are contained in both multiplicand and multiplier. Hence,

NOTE 1.-If there are not as many figures in the product as there are decimals in both factors, supply the deficiency by prefixing ciphers.

2.-To multiply by 10, 100, 1000, &c., remove the decimal point as many places to the right as there are ciphers on the right of the mul-

57.145. 20.7755 03.8523.

.330263.38.4514. six hunsandths; . 37.047. rst piece rds, and 5 yards.

se three end uns under Comsubtract remaindirectly ve. In of decigreater rahend, In both nd subnumber ciphers; nnexed ction.---

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DIVISION OF DECIMALS.

Mental Exercises.

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1. If a man can reap .96 of an acre in a day, how much can he reap in .5 of a day?

2. If 1 pound of coffee cost .3 of a dollar, what will 4 pounds cost?

3. Add 3.6 + .26 + .006 + 3.006, and multiply the pro-

4. From 3.606 take 1.4, and multiply the result by .09

5. If 1 ton of hay cost 8.75 dollars, what will .25 of a ton cost?

Exercises for the Slate.

SECTION I.

Multiply and add together the products of-

(1)	1234.56789	by	78.91	and	21.09) (6)	by	550.8	and	149.3
(2)	345.789612	by	35.79	and	64.21	(7)	by	900.9	and s	99.ľ
(3)	406.783089	by	60.09	and	39.91	(8)	by	428.6	and a	571 4
(4)	2492.67339	by	42.82	and	57.18	(9)	by	624.8	and a	375.2
(5)	5063.48001	by	.99	and	99.01	(10)	by	99.73	and	.27

SECTION II.

Find the product of-

(1) 32×241 Ans. 031812 (6) 0	006 × .00012 Aus000000872
$\begin{array}{c} (2) & 2.5 \\ (3) & 21.716 \times 2.06 \end{array} \qquad \begin{array}{c} .00207 \\ 44.73496 \\ (8) & 16 \end{array}$	$0004 \times .004$.0320016 54.023×12.88 .2112.61694
$\begin{array}{c} (4) & 11.111 \times 9.7116 \\ (5) & .2 \times .7 \times .06 \times .004 \times 1 \\ \end{array} \begin{array}{c} 1007.9055876 \\ 100900226 \\ \end{array} \begin{array}{c} (9) \\ (10) \\ 10 \\ \end{array}$	8.006 × 100.001 17800.778006

11. Multiply four hundred, and four thousandths by thirty and three hundredths. Ans. 12012.12012.

12. If a cord of wood be worth 2.37 bushels of wheat, how many bushels of wheat must be given for 9.58 cords of wood? Ans. 22.7046 bushels.

DIVISION OF DECIMALS.

74. EXAMPLE.—What is the quotient of .156 divided by .6

OPERATION.	ANALYSIS.—We perform the division as in
.6).156	whole numbers. Since the dividend, which is
· · · · · · · · · · · · · · · · · · ·	the product of the divisor and quotient, con-
Ans26	tains three places, and the divisor contains one
	place, the quotient must contain two places of
decunals for,	2 + 1 = 3, or $3 - 1 = 2$, (73.) Hence.

DIVISION OF DECIMALS.

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.000000072 .0320016 2112.61624 800.778806 25.86

by thirty 2.12012. wheat, cords of bushels.

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on as in which is nt, conains one laces of Hence,

RULE. Divide as in whole numbers, and from the right hand of the quotient point off as many places for decimals, as the decimal places in the dividend exceed those of the

Nore 1.- The dividend must always contain at least as many places of decimals as the divisor, before commencing the division.

2.-If the number of figures in the quotient be less than the excess deficiency must be supplied by *prefixing* ciphers. 3.—To divide by 10, 100, 1000, &c., remove the decimal point as many places to the left as there are ciphers on the right hand of the divisor.

Mental Exercises.

How many bushels of oats at .2 of a dollar a bushel, 1. ean be bought for .84 of a dollar ?

If 15 pounds of coffee cost 4.50 dollars, what cost 1 2. pound? 3.

If a team can plough .75 of an acre in .5 of a day, how much will it plough in one day? 4.

How many boxes will be required to pack 49.5 pounds of butter, if you put 5.5 pounds in each? 5. If a man can walk 16.5 miles in a day, how long will

it take him to walk 36.30 miles?

Exercises for the Slate.

SECTION I.

$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	
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SECTION II.

What is the quotient of-

Find the value of-

$\begin{array}{c} (1) \ 40.84 \div 7.9 \\ (2) \ 67234 \div .85 \\ (3) \ 60 \ 0001 \div 1.01 \\ (4) \ 0.00006 \div .003 \\ (5) \ 6541.234567 \div 9 \end{array}$	$\begin{array}{c} \text{Ans.} 5.9291 + \\ 79098.8235 + \\ 59.4060 + \\ 0.02 \\ 21\ 311.487360 + \end{array}$	$ \begin{array}{c} (6) \ 4. \div .00001 \ \mathrm{Ar} \\ (7) \ 2.39015 \div .007 \\ (8) \ 785.4 \div 1000 \\ (9) \ 3.6 \div .00006 \\ (10) \ .8 \div 476.3 \end{array} $	1s. 400000 341.45 .7854 60000 .001679 +
4.4 70			

11. If 25 men build 154.125 rods of fence in a day, how many does each man build? Ans. 6.165 rods.

12. How many coats can be made from 16.2 yards of eloth, allowing 2.7 yards for each coat? Ans. 6 coats.

REDUCTION.

REDUCTION.

75. A Concrete Number is a number of but one name, or denomination; thus, 5 pounds, 27 bushels, 72 dollars, are concrete numbers.

76. A Compound Number is a concrete number of two or more denominations; thus, 5 dollars 23 cents, 14 bushels 3 pecks, 9 days 7 hours, are compound numbers.

77. Reduction is the process of changing a number from one denomination to another without altering its value. Reduction is of two kinds, Descending and Ascending.

78. Reduction Descending is changing a number of one denomination to another denomination of less unit value; thus 1 dollar = 10 dimes = 100 cents = 1000 mills.

79. Reduction Ascending is changing a number of one denomination to another denomination of greater unit value; thus 1000 mills = 100 cents = 10 dimes = 1 dollar.

CURRENCY.

80. Currency is coin, bank bills, &c., in circulation as a medium of trade:

ENGLISH OR STERLING MONEY.

2	Farthings :	make	1	Half-penny,	marked	금네.
2	Half-pence	46	1	Penny,	66	d.
12	Pence	46	1	Shilling,	"	s.
20	Shillings	"	1	Pound.	44	£

NOTE.—A Crown is a silver coin equal to 5 shillings. A Sovereign is a gold coin equal to 20 shillings, and a Guinea is a gold coin equal to 21 shillings.

CASE I.

81. To perform Reduction descending.

EXAMPLE .- Reduce £23 16s. 74d. to farthings.

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4)22

12)5

2|0)

£ Ans.

lings, with succe Henc

RU: the ta inatic

REDUCTION.

ANALYSIS .- Since in £1 there are 20s., in £23 there are 20s. \times 23 = 460s., and 71 16s. in the given number added, make 476s. in £23 16s. Since in 1s. there are 12d., in 476s. there are 12d. × 476 = 5712d, and 7d. in the given number added make 5719d. in £23 16s. 7d. Since there are 4 farthings in 1d., in 5719d. there are 4 far. \times 5719 = 22876 far., and 1 far in the given number added makes 22877 far. in £23 16s. 74d.

NOTE.-When two numbers are to be multiplied together, it is a matter of indifference, so far as the product is concerned, which of them is taken as the multiplicand or multiplier. For convenience we multiply £23 by 20 and call the product shillings, and so with the

Hence the following general

RULE. I. Multiply the highest denomination of the given number by that number in the table which will re-duce it to he next lower denomination, and add to the product the given number, if any, of that lower denomi-

II. Proceed in the same manner with the results obtained in each lower denomination, until the reduction is brought to the denomination required.

CASE II.

To perform Reduction ascending. 82.

EXAMPLE.-Reduce 22877 farthings to pounds.

0PERATION. 4)22877	ANALYSIS.—We first divide the 22877 far. by 4, because there are one
12)5719d. + 1 far.	fourth as many pence as farthings, and we find that 22877 far 57104
2 0)47 6s. + 7d.	far. We next divide 5719d. by 12, because there are one twild by 12,
£23 13s.	shillings as pence, and we find that $5719d - 476c$
Ans. $\pounds 23$ 16s. $7\frac{1}{4}$ d.	vide the 476s. by 20, because there are

one-twentieth as many pounds as shillings, and we find that $476s. = \pounds 23 + 16s$. The last quotient with the several remainders annexed in the order of the succeeding denominations gives the answer £23 16s. $7\frac{1}{4}d$. Hence the following general

RULE. I. Divide the given number by that number in the table which will reduce it to the next higher denom-

lation as

but one

, 72 dol-

umber of

ents, 14

number

ts value.

less unit

00 mills. umber of ater unit

: dollar.

ers.

ng. number

Sovereign oin equal

REDUCTION.

II. Divide the quotient by the next higher number in the table; and so proceed to the highest denomination required. The last quotient, with the several remainders annexed in a reversed order, will be the answer.

Mental Exercises.

1. How many farthings are there in 4d.? in 9d.? in 111d.? in 15d?

2. How many pence are there in 4s.? in 12s.? in 15s.? in 12s. 6d.?

3. How many pounds, &c., are there in 27s.? in 28s.? in 156s.?

4. How many shillings are there in £6? in £5 7s.? in £6 17s.? in £12 5s.?

5. Five yards of cloth cost £1 2s. 6d.; what was the cost of one yard, in pence?

.6. Reduce 960 farthings to pounds. In 690s. how many pounds?

7. What cost 85 pairs of gloves at 7 pence per pair ?

Exercises for the Slate.

SECTION I.

Reduce to Farthings.

£	s.	р.		£	8.	D.	U	£	8.	p.
(1) 0	1	81	[7(7)]	129	3	0	(13)	\$974	0	81
(2) 1	1	111	(8)	103	12	$9\frac{3}{4}$	(14)	1009	15	51
(3) 2	7	75	(9)	354	10	101	(15)	4983	16	11
(4) 2	17	41	(10)	520	17	$2\frac{1}{4}$	(16)	5993	11	68
(5) 2	0	6	(11)	531	2	3	(17)	5221	4	21
(6)28	1	111	(12)	531	7	331	(18)	5575	15	08

In £71 13s. 6¹/₂d. how many farthings? Ans. 68810.
 In £295 18s. 3³/₄d. how many farthings. Ans. 284079.
 In 95 guineas, 17s. 9³/₄d., how many farthings?

Ans. 96615.

Reduce £15 15s. 6d. to sixpences. Ans. 631.
 Reduce £15 14s. 9d. to three pences. Ans 1259.

SECTION II.

Reduce to Pounds.

(1) 17448 far.	(6)	34904 far.	(11)	21816	half pence.
(2) 43632 "	(7)	78536 "	(12)	21600	46 T
(3) 138657 "	(8)	198786 "	(13)	99393	66
(4) 156113 "	(9)	302547 "	(14)	224726	pence
(5) 182289 "	(10)	103753 "	(15)	170666	4

83 inatiis on Tl State ward

1 (16 17

(18

(19

fart

at 3

2

2

21

84

Nor (\$) of and ce would cents. 2. ten, th dimes.

85. make

89. annex To To To mills to

REDUCTION OF DECIMAL CURRENCY.

umber in mination mainders

9d.? in

in 15s. ?

in 28s.?

5 7s.? in

s the cost

ow many

pair ?

S. D. $0 81_{4}$ $5 51_{4}$ $6 1_{22}$ $1 6_{4}$ $4 2_{1}$ $5 0_{4}^{8}$ **s.** 68810.

. 284079. s? s. 96615. Ans. 631. ns 1259.

If pence.

Reduce

(16)	197424 far. to shillings.	(20)	6480 far. to c	
(17)	171504 half pence "	(21)	11340 penee	
(18)	756 shillings to guineas.	(22)	2700 "	
(19)	4536 three pences "	(23)	2160 half peneo	
(19)	4536 three pences "	(23)	2160 half pence	, «

24. How many pounds, shillings, &e., are there in 367841 farrisings ?- Ans. £383 3s. 44d.

25. In 1059120 pence how many sovereigns? Ans. 4413.
26. A farmer, during the year, sold 1367 quarts of milk

at 3 pence per quart, what did it all amount to?

Ans. £17 1s. 9d.

LEDUCTION OF DECIMAL CURRENCY.

83. A Decimal Currency is a currency whose denominations increase in a ten-fold ratio, and each denomination is one-tenth the value of the next higher.

The currency of the Dominion of Canada, the United States, France, Barbadoes and some others of the Windward Islands, and Demerara, is decimal.

84.

CANADA CURRENCY.

TABLE.

10 Mills (m)	make	1	Cent,	marked	Ct. or C.
10 Cents	66	1	Dime.	66	1
10 Dimes	44	1	Dollar		\$.

NOTE 1.—It is usual in writing dollars and cents, to place the sign (\$) of dollars in front of the sum, and a point (.) between the dollars and cents. Thus, fifty six dollars, four dimes, six cents, and five mills would be written \$56.465, or $\$56.46\frac{1}{2}$, and read 56 dollars and $46\frac{1}{2}$

2. If the sum consists of dollars, and a number of cents less than ten, there must be a cipher between the dollars and cents in place or dimes. Thus, 5 dollars and 4 cents must be written \$5.04.

85. By examining the above table we see that 10 mills make 1 eent, and 100 cents, or 1000 mills one dollar; hence

89. To change dollars to cents, multiply by 100; that is, annex two ciphers.

To change dollars to mills, annex three ciphers.

To change cents to mills, annex one cipher.

To change dollars and cents to cents, or dollars, cents and mills to mills, remove the decimal point and the sign **\$**.

REDUCTION OF DECIMAL CURRENCY.

Exercises for the Slate.

1.	Change \$196	to cents.	Ans. 19600.	
----	--------------	-----------	-------------	--

2.	66	\$1325 to mills.	66	1325000
0	11	M 4 10 1		4

3. \$1.46 to cents. " 146. " 4. "

54

- 56 cents to mills. 560. " 5. \$19.425 to mills. "
- 19425.

87. To change cents to dollars, divide by 100; that is, point off two figures from the right.

To change mills to dollars, point off three figures.

To change mills to cents, point off one figure.

Exercises for the Slate.

1.	Change 1967 cents to dollars.	Ans \$19.67
2.	" 1432 mills to "	Ang \$1 499
3.	In 34567 mills how many dollars?	Ang 94 567
4.	Reduce 3195 mills to dollars and cents.	Ans \$3 191

88. As the above currency is on the same principle as decimal notation, any operation, as addition, subtraction, multiplication, &c., may be performed upon it in the same manner as upon decimals.

NOTE .- The exercises in Section I of Addition and of Subtraction of Decimals, should be reviewed as exercises in Canadian currency.

89. Accounts are kept in sterling pounds, shillings and pence in Great Britain, Newfoundland, Australia and New Zealand.

90. To reduce sterling pounds, shillings, pence, and farthings to Canada currency,

TABLE.

	1 Farthing, 1	marked $1 = 78$ C.
4 Farthings m	ake 1 Penny.	(1 - 21)
12 Pence	" 1 Shilling	44 = -236
20 Shillings	" 1 Pound.	$f = \frac{24}{9}$

EXAMPLE.—Reduce £5 10s. $1\frac{1}{4}d$. to Canada currency

$\begin{array}{c} 01\\ \pounds 5\\ =\end{array}$	PER. 10s = 52	AT $1\frac{1}{4}$ 85 73	ion d far.	•
	158 3699	55 5		

144)385805(\$26.79

ANALYSIS .- Since pounds shillings and pence are composed of farthings, multiplying by 20, 12 and 4, reduces the whole amount to farthings = 5285 farthings. And since one farthing is equal to $\frac{73}{144}$ of a Canadian cent, 5285 farthings are equal to 5285 $\times \frac{73}{144}$, (p. 38 ex. 1), or \$26.79. Hence,

R(fartl tien Ne reject No 486 2 Appe

1. pieco 2.28, 01 in 3. 3. 10s, c ereig ereig

Re (1) a (2) £ (3) £ (4) £ (5)£1; $(6) \pounds 1$ $(7) \pm 3$

91.

RUI multi ings t $\mathbf{E}\mathbf{x}$

\$110.1 farthir Noti the form 1

92.

12 I

3 F

51 I

40 R

8 F 3 N 691 N

REDUCTION OF DECIMAL CURRENCY.

RULE. Reduce pounds, shillings and pence sterling to farthings, and multiply by 73 and divide by 144. The quo-tient will be the equivalent in Canada currency.

Note 1.—In a final remainder reckou over $\frac{1}{2}$ as a cent, less than $\frac{1}{2}$ reject.

NOTE 2.—When there are only pounds in the exercise multiply by 486 2-3, the number of Canadian cents in a pound sterling. See

Mental Exercises.

1. How many Canadian cents are there in a three-penny piece ? in a four-penny piece ? in a sixpence ? in a shilling ?

2. How many Canadian dollars and cents are there in 2s, or a florin ? in 5 florins ? in 5s, or a crown ? in 10 crowns ? in 3 florins + 2 crowns?

3. How many Canadian dollars and cents are there in 10s, or a half-sovereign? in £1, or a sovereign? in 10 sovereigns? in £1 1s, or a guinea? in 2 guineas + 3 half-sovereigns?

Exercises for the Slate.

Reduce the following to Canadian currency :-(1) $\pounds 1 3$ 61 Ans. \$5.73 (8) ± 27 6 $7\frac{1}{4}$ Ans \$133.01 (2) £11 11 64 \$56.35 £26 16 84 (9)(3) £44 15 \$130.60 $7\frac{3}{3}$ \$217.94 (10)£10 11 $4\frac{3}{4}$ (4) £26 18 91 \$51.44 \$131.11(11) $\pounds 25$ (5)£115 16 11 0 0 \$121.67 \$563.80 (12) $\pounds 82$ 0 0 (6) £110 11 111 \$399.07 \$538.26(13)£64 0 0 $(7) \pounds 365 4 5\frac{1}{4}$ \$311.47 \$1777.41 (14)£5 0 0 \$24.33 91.

To reduce Canadian currency to pounds, &c., Stg.

RULE. Reduce the dollars and cents to farthings by multiplying by 144 and dividing by 73. Reduce the farth-ings to pounds, shillings and pence. See Appendix II.

EXAMPLE.—Reduce $$110.12\frac{1}{2}$ to pounds, &c., sig

OPERATION.

 $110.12\frac{1}{2} \times 144 = 1585800$, and $1585800 \div 73 = 21723$ farthings = £22 12s. $6\frac{3}{4}$ d.

NOTE.-For exercises under this rule the pupil may prove those of the former one.

REDUCTION OF LINEAR OR LONG MEASURE. 92.

LONG MEASURE-TABLE.

12 Inches	make	1	Foot n	narke	d ft
3 Feet	66	1	Yard	46	u /1.
51 Yards	66	1	Rod Pole on Pon	ah u	ya.
40 Rods or Perehe	S 66	1	Furlong	cn ···	ra. or p.
8 Furlongs	66	1	Milo		fur.
3 Miles	66	1	T on ou's	••	m.
691 Miles (noarly)	"	1	Deague	66	lea.
g - files (ileally)		1	Degree	66	deg. or °

; that is,

ns. \$19.67. ns. \$1.432. ns. 34.567. ıs. \$3.191. inciple as

ibtraction, the same

Subtraction currency. llings and and New

nce, and

⁸/₁₁ C. $4.86\frac{2}{3}$

rency

inds shiluposed of v 20, 12 monnt to gs. And to $\frac{73}{144}$ of hings are 38 ex. 1),

56 REDUCTION OF LINEAR OR LONG MEASURE.

EXAMPLES.

1. In 18 po. 1 ft. 6 in. how	2. Reduce 5373 inches to
many inches?	poles, &c.
OPERATION.	OPERATION
18 po. 0 yd. 1 ft. 6 in.	12)5373
$5\frac{1}{2}$	
_	3)447 ft. 9 inches.
90	
9	51)149 vds.
· ·	2^{2} 2
99 == yds. in 18 po.	
3	11)298
298 = ft. in 18 po. 1 ft.	$27 \text{ po.} \frac{1}{2} \text{ vd.}; \text{ and } \frac{1}{2} \text{ vd.}$
12	= 1 ft. 6 in.
	+ 9 in.
3582 = in. in 18 po. 1 ft.6 in.	
1	27 po. 0 yd. 2 ft. 3 in
Mental Ex	orgisos

1. How many inches are there in 3 ft.? in 5 ft.? in 10 ft.? in 12 ft. 4 in.?

2. How many feet are there in 4 yds.? in 6 yds.? in 9 yds.? in 15 yds.?

3. How many furlongs are there in 5 miles? in 6 m. 3 fur.? in 12 m. 7 fur?

4. In 100 inches how many yards, feet and inches?

5. At 9 dimes a foot, how many dollars will 4 yds. 2 ft. of iron railing cost?

Exercises for the Slate.

(1) Red	ace 71280 in. to fur. (6) Reduce 36 po. 3 ft. to inches.
(2) "	3564 in. to po. (7) " 45 m. 8 po. 1 vd. to vds.
(3)	63360 yds. to miles. (8) " 27 m. 1 po. 3 yd. to feet.
(5 11	570240 m. to miles. (9) " 72 m. 13 po. $\frac{1}{2}$ yd. to yds.
0	190080 ft. to miles. (10) "74 m. 5 fur. 1 po. 1 yd. to yds
11.	In 9768042 inches how many miles?
	Ans. 154 m. 1 fur. 13 po. 3 vds.
12.	In 897682 yards how many miles?
	Ans. 510 m 0 fur 14 no 5 wds
13.	Reduce 103 m. 5 fur. 32 po. 5 vds. to feet
03.	Ang 547683
	CLOTH MEASURE—TABLE.
	$2\frac{1}{4}$ Inches make 1 Nail.
	4 Nails " 1 Quarter, or.
	4 Quarters " 1 Yard vd
	a material year

no pr. 1. to ind 27 4 1114

 $44 : 2\frac{1}{4}$

888 111

999 **=**

No

1.] in 2 yd 2.] qrs. ? i

3. H 123 nls.

1. F

94.

144 Sc 9 Sc 301 Sc 40 Sc 40 Sc 40 Sc 640 Ac

SURE.

73 inches to ON.

hes.

and & yd. in. in.

l. 2 ft. 3 in

in 10 ft.?

yds.? in

in 6 m. 3

les? ls. 2 ft. of

ches.

. to yds. d. to feet. d. to yds. yd. to yds

po. 3 yds.

oo. 5 vds.

. 547683.

REDUCTION OF LINEAR OR LONG MEASURE. 57

Note.-English, French and Flemish Ells are omitted, as being of no practical value. EXAMPLES.

1. Reduce 27 yards 3 qr. 2. Reduce 153 nails to to inches yds, &c. OPERATION. 27 yds. 3 qr. OPERATION. 4)1534 4)38 qrs. 1 nl. 111 = qrs. in 27 yds. 3 qr. 9 yds. 2 qrs. 1 nl. 44 = nls. in 27 yds. 3 qr. $2\frac{1}{4}$. 888 111

999 = in. in 27 yds. 3 qr.

Mental Exercises.

1. How many inches are there in 3 nls.? in 2 qr. 1 nl.? in 2 yds. 1 nl.? in 5 qrs.?

2. How many quarters are there in 5 yds.? in 3 yds. 3 qrs. ? in 6 yds. 2 qrs. ?

3. How many yards are there in 5 qrs. ? in 17 nls. ? in 123 nls. ? in 196 qrs. ?

Exercises for the Slate.

Reduce 648 inches to yards. 1. 2.

Reduce 2268 inches to quarters. 3.

Reduce 127 yds. 3 qrs. 2 nls. to inches. Ans. 46031. 4.

In 39678 inches how many yards?

Ans. 1102 yds. 2 nls. 11/2 in.

94.

REDUCTION OF SQUARE MEASURE. TABLE.

 144 Square incl. 9 Square feet 301 Square yard 40 Square pole 4 Roods 640 A cress 	les make ls " s "	1 Square foot, 1 1 Square yard, 1 Square pole, 1 Square rood, 1 Acre,	marked sq. ft. " sq. yd. " sq. po. " ro.
640 Acres	"	Acre, I Square mile.	" - ас.

REDUCTION OF SQUARE MEASURE.

EXAMPLES

1	- · · ·
1. Reduce 135 ac. 3 ro. 15 po. to poles.	2. Reduce 261414 yards to acres.
OPERATION.	OPERATION.
135 ac. 3 ro. 15 po. •	$30\frac{1}{4})261414$
4	4 4 .
543 ro in 135 ag 3 ro	191
40	(11)1045656
21735 po. in 135 ac. 3 ro. 15 po	(11) 95059, 7 95 $-$ 938
	$4 0) \overline{864} 1,8 \int \frac{1}{4} \frac{-25}{4}$
	4)216 ro. 1 po.
	$54 \text{ ac. 0 ro. 1 po. } 23\frac{3}{4}$
Mental I	Exercises.
1. How many square feet a	re there in 6 square vards?
in 19 vds. 3 feet? in 15 vds. 2	ft.?
2. How many acres are the	ere in 880 poles ? in 160 poles ?
in 320 poles? in 1240 poles?	
3. At \$4 per acre what wi	ll 920 poles of land cost?
4. Find the cost of 12 yard	ls 3 feet at 7 dimes per foot.
Exercises fo	or the Slate.
 (1) Reduce 126 ac. 4 po. 5 yds. to yd (2) "162 ac. 5 po.10 ½ yds. to yd (3) "9 po. 9 in. to inches. (4) "90 ac. 18 yds. to yards. 	 (5) Reduce 1411380 in. to poles. (6) " 304983 yds.to acres. (7) 94ac.2ro. 1po.5⁴/₂ yds. to yds. (8) " 697104 yds.to acres.
9 In 36 ac. 3 ro. 28 po. 5 y	ds., how many feet ?
10. Reduce 29 ac. 3 ro. 38	Ans. 1608498. po. $15\frac{1}{2}$ yds. 8 feet to inches.
11 In 6463761 feet how m	Ans. 188122032.
Ans	14 ac 3 ro 14 no 6 vds 1 foot
1115.	14 ac. 510. 14 po. 6 yus. 1 1000
REDUCTION OF CUBIC	OR SOLID MEASURE.
95. SOLID MEAS	URE-TABLE.
1798 Cubic inches	ake 1 Cubic foot marked ou ft.
27 Cubic feet	" 1 Cubie vard, " en ud.
198 Cubic foot	" 1 Coul of fine wood

N valı fire cont John

1.

 $2. \\ 3.$

4.

96

Nor disuse.

1. 1 gal. 27 b 4

 ${}^{219}_{4}$ ga

877 qt

1755 pi Note. Liquids a

1. H in 6 qts.

REDUCTION OF CUBIC OR SOLID MEASURE.

59

Note.--The ton is omitted from the table as being of little practical value in an elementary treatise. In buying and selling, the Cord of fire wood is allowed to be 8 ft. long, 4 ft. wide and 4 ft. 4 in. high, as containing a solid mass equal to 128 cubic feet. In the city of Saint John, usage allows 5 ft. in height instead of 4 ft. 4 in.

Exercises for the Slate.

In 125 cu. ft. 840 cu. in. how many cu. in. ? 1. 2. Reduce 5224 cubic feet to cords. Ans. 216840. In 216840 cubic inches how many cubic feet ? Ans. 40 13. 3. Ans. 125 cu. ft., 840 cu. in. In 94 cords 6 cubic feet how many cubic feet ? 4. Ans. 12038 cu. ft. 96. MEASURE OF CAPACITY-TABLE. 4 Gills (g) make 1 Pint, marked pt. 2 Pints 1 Quart, qt. 4 Quarts 66 1 Gallon, " gal. 2 Gallons 66 1 Peck, " pk. 4 Pecks " 1 Bushel, 66 bush, 8 Bushels " 1 Quarter " NOTE. --- 36 bushels are considered a chaldron, but is falling into disuse. EXAMPLES. 1. Reduce 27 bus. 1 pk. 2. Reduce 594 gills to gal. 1 gal. 1 qt. 1 pint to pints. lons. OPERATION. 27 bus. 1 pk. 1 gal. 1 qt. 1 pt. 4)594 OPERATION. 2)148 pts. 2 gills. 109 pks. 2 4)74 qts. 0 pts. 219 gals 18 gals. 2 qts. 0 pts. 2 gills. 877 qts. 9 1755 pints. NOTE .- The above Measure of Capacity is now used both for Liquids and for Dry Goods. Mental Exercises. 1. How many gills are there in 4 pts.? in 3 qts. 3 pts.? in 6 qts. 3 pts. 1 gill ?

5.

ON.

 $\left\{ \frac{95}{4} = 23\frac{8}{4} \right\}$

1414 yards

po. [yds. ro. 1 po. 23[§]

*

e yards?

n 160 poles ?

cost? s per foot.

80 in . to poles. 8 yds.to acres. 54 yds. to yds. 4 yds.to acres.

t? ns. 1608498. to inches. 188122032.

3 yds. 1 foot.

URE.

arked *cu. ft. " cu. yd.* wood.

REDUCTION OF CUBIC OR SOLID MEASURE.

How many quarts are there in 6 gals. ? in 3 gals. 2 qts. ? 2. in 2 pks. 1 qt. ?

How many gallons are there in 8 qts. ? in 8 pts. ? in 3. 24 pts. ? in 38 qts. ?
4. What will be the cost of 7 gals. 3 qts of burning fluid

at 15 cents a quart?

EXCruises 10	or the state.
(1) Reduce 19 gals. 1 pt. to gills.	(5) Reduce 1942 bus. 1 gt to gts.
(2) " 11 pKs. 1 gal. 1 qt. 5 gli, to g	(10, 10) (10) $(10, 10)$ $(10,$
(4) " $2 \text{ bus. 1 gal. 1 gin to gins.}$	ills. (8) " 594 ats to bush.
9 In 1083965 cills how m	any quarts?
5. In 4985205 gms now m	Ang 622908 ats 1 mill
10 D 1 1001 - 0	Ans, 022500 ques. 1 gint
10. Reduce 126 bus. 3 pks	Ans. or prints. Ans. or or a
11. Reduce 1467896 quart	ts to chaldrons?
	Ans. 1274 ch. 7 bus. 3 pks.
12. An innkeeper bought	50 bushels of oats at 65 cents a
bushel, and retailed them at 2	5 cents a peck ; how much did
be make by the lot?	Ans. \$17.50.
REDUCTION	OF WEIGHTS,
97. TROY WEIG	HT-TABLE.
• 24 Grains make	1 Pennyweight, 1 dwt.
24 Granis marci	1 Ounce 1 oz
20 Tennyweights	1 Dound 1 lb
12 Ounces	1 Found, 1 10.
This weight is used in weight	ghing the precious metals and
stones.	
EXAN	APLES.
1. Reduce 31 lbs, 10 oz. 8	2. Reduce 28197 dwt. to
dwts. 12 grs. to grains.	los.
OPERATION.	OPERATION.
31 lbs 1007 8dwt 19grs	210)281917
10 105. 1002. Ouwi. 12gis	
12	10)1400 or 17 dw
	12)1409 02. 17 dw
382 oz.	
20	117 lbs. 5 oz. 17 dwt.
7648 dwt.	
24	
30604	
15000	
10200	

1. grain 2. in 24

3.

3 cer 4, dwts. 5.

many

(1) Re((2) (3) (4)

9.

10.

11.

12. much w

8.

NOTE .hool ter

99.

20

NOTE 1. ight, the is calle The r

JRE.

als. 2 qts. ?

8 pts.? in

ming fluid

. 1 gt to qts. s to pks. lls to bus. s to bush.

qts. 1 gill Ans. 8113,

bus. 3 pks. 65 cents a much did ns. \$17.50.

wt. z. b. netals and

7 dwt. to

٧.

w

z. 17 dwt.

REDUCTION OF WEIGHTS.

Mental Exercises.

1. How many grains are there in 5 dwts.? in 6 dwts. 7 grains? in 15 dwts. 3 grs. ? 2.

How many ounces are there in 120 dwt.? in 200 dwt.? in 240 dwts. ?

3. What will a gold chain weighing 9 dwt. 15 grs. cost at 3 cents a grain?

4, What is the value of a silver cup, weighing 5 oz. 4 dwts. at 15 cents per pennyweight?

5. In 5 ingots of gold, each weighing 9 oz. 5 dwt. how many dwts. ?

Exercises for the Slate.

1) 1 2) 3) 4)	'' 1 lb. 1 oz. 19 dwts. to grs. (5) Reduce '' 1 lb. 1 oz. 19 dwts. to grs. (6) '' '' 1 lb. 3 oz. 9 dwt. to grs. (7) '' '' 20 lbs, 10oz. 18 dwts. to dwts. (8) ''	207396 grs. to Ibs. 4338 dwts. to Ibs. 155520 grs. to Ibs. 17280 dwts. to Ibs.
9.	Reduce 37 lbs. 11 oz. 19 dwtg to 1	

is. to dwts.

Ans. 9119 dwts.

Reduce 87 lbs. 19 grs. to grains. Ans. 501139. Rednce 578096 grains to pounds. 11.

Ans. 100 lbs. 4 oz. 7 dwts. 8 grs. A miner had 14 lbs. 10 oz. 18 dwt. of gold dust : how 12. much was it worth at 75 cents a dwt.? Ans. \$2683.50.

98.

10.

APOTHECARIES' WEIGHT-TABLE.

Note.-This table is omitted as being of no practical value in a school text. 99.

AVOIRDUPOIS WEIGHT-TABLE. 16 D ...

10 Drams	make	1 Ounce marked 1
16 Ounces	66	1 Pound Harked 1 oz.
25 Pounds	66	1 Dunit, " 1 lb.
4 Quarters	44	1 Quarter, " 1 gr.
20 Hundrodweint		1 Hundredweight 1 cmt.
	••	1 Ton, " 1 ton
		· · · · · · · · · · · · · · · · · · ·

NOTE 1.-In Great Britain 28 lbs. make one quarter; a hundred weight, therefore, is, in Great Britain, 112 lbs. Throughout this book this is called "long weight."

2. The pound avoirdupois is equal to 7000 grains Troy.

٩,

REDUCTION OF WEIGHTS.

EXAMPLES.

1. Reduce 81 cwt. 2qrs. 25	2. Reduce 72 cwt. 2 qrs.
lbs., long weight, to pounds.	22 lbs., to pounds.
OPERATION.	OPERATION.
81 cwt. 2 qrs. 25 lbs.	72 cwt. 2 qr. 22 lbs.
4	4
326 grs.	290 qrs.
28	25
2633	1472
652	580
9153 lbs.	7272 lbs.
Or,	Or,
81 cwt. 2 qrs. 25 lbs.	72 cwt. 2 qrs. 22 lbs
$8100 = 81 \times 100$	$7200 \equiv \text{pounds in } 72 \text{ cwt.}$
$972 \pm 81 \times 12$	50 = " " 2 qrs.
56 = pounds in 2 grs.	22 = "given.
25 = " given."	7272 = " required.
$\overline{9153} = $ " required.	1

Mestal Exercises.

1. How many ounces are there in 3 lbs.? in 5 lbs. 10 oz.? 6 lbs. 13 oz.?

2. In 3 cwt. 5 lbs. how many pounds? How many ounces?

5 3

No

days,

days,

1.

in 5]

2.

3 days

3.

in 63

4. 10th ir

3. What will 1 ton 5 cwt. of hay cost, if 5 cwt. cost \$3?

4. What will 2 cwt. 12 lbs. of beef cost at 6 cents a pound?

5. If 8 ounces of tea cost 40 cents, what is the cost of 2 lbs.?

Exercises for the Slate.

Note. - In the following exercises where the answers are not given let the work be tested by reversing the process.

- 1. Reduce 8 cwt. 2 qrs. 19 lbs. 4 oz. 12 drs., to drs.
- 2. " 1 ton 2 cwt. 3 qrs. 7 lbs. 9 oz. 13 drs., to drs.
- 3. " 22 tons 13 cwt. 1 qr. 5 lbs. 9 oz., to drs.
- 4. " 25 tons 2 cwt. 1 gr. 13 oz., to oz.
- 5. " 42 tons 14 cwt. 2 qrs. 3 lbs. 5 oz., to ounces.

REDUCTION OF TIME.

6. " 7 cwt. 1 qr. 4 lbs. 7 oz. 5 drs., to drs. 7. " 6939 drams to pounds. 8. 1032228 drams to cwt., long weight. 66 9. 66 3 qrs. 15 lbs. 15 oz. 15 drs., long weight, to drs. Ans. 25599 drs. 10. " 94 tons 19 cwt. 2 qrs. 24 lbs. 10 oz. 15 drs., long weight, to drams. Ans. 54468783. 11. " 493865 lbs. to tons, long weight. Ans. 220 tons 9 c. 2 qr. 1 lb. 12. 66 204250 oz. to cwt. Ans. 127 cwt. 2 qr. 15 lb. 10 oz.

100.

REDUCTION OF TIME.

TABLE.

60 Second is	writ	ten thus: 1/	/	
60 Minutes	make	e 1 Minute.	marka	1 1/
24 Hours	"	1 Hour,	66	1 1 2 2
7 Days	"	1 Day,	46	1 day
28 Davs		1 Week,	"	1 wk
28, 29, 30, or 31 Dava	••	1 Lunar m	onth.	
12 Calendar months	"	1 Calendar	month	
B65 Days	"	1 Year.		*
366 Days	"	1 Common	year.	
		Leap yea	r.	

Note.—Seven of the months contain 31 days. Four contain 30 days, viz., September, April, June and November. Eebruary has 28 days, but in leap-year it has 29 days.

Mental Exercises.

1. How many seconds are there in 3 hrs.? in 4 hrs. 20 ?

2. How many hours are there in 4 days 5 hrs.? in 2 wks, 3 days 12 hrs.?

3. How many weeks are there in 72 days? in 85 days?

4. How many days are there from April 15th to August 10th inclusive?

cwt. 2 qrs.

lbs.

hbs in 72 cwt. " 2 qrs. given. required.

lbs. 10 oz.?

any ounces? wt. cost \$3? t 6 cents a

the cost of

are not given

to drs. lrs., to drs. o drs.

o ounces.

REDUCTION OF TIME.

Exercises for the Slate.

REDUCE

(1) 18 days 27 min. 18 sec. to sec.	(6) 365 dys. 5 hrs. 48 min. 45 sec. to sec.
9) 97 days 36 min 27 sec to sec.	(7) 8 yrs. 5 days 45 min. to seconds.
2) 21 days 50 mm. 21 800. 00 800.	(a) 000004000 upp to voorta

- (3) 720 d. 11 h. 37 min. 30 sec. to sec.
 (4) 36 yrs. 9 hrs. 36 min. to min.
 (5) 9460800 min. to years. (5) 9 yrs. 2 hrs. 45 min. 9 sec. to sec. (10) 103680 min. to days.

 - Reduce 48 days 17 sec. to seconds. Ans. 4147217 sec. 11.
 - Reduce 53 days 23 hrs. 26 min. to minutes. 12.

Ans. 77726 min.

How many times does a clock pendulum, beating 13. seconds, vibrate in one day? Ans. 86400. 14. How much time will a person gain in 30 years, by

rising, each day, 42 minutes earlier than his usual time? Ans. 319 days 9 hours.

MISCELLANEOUS TABLE.

12 individual things make 1 dozen.

12	dozen	"	1 gross.
12	oross	"	1 great gross.
20	individual things	44	1 score.
24	sheets of paper	66	1 quire.
20	quires	66	1 ream.
112	pounds	66	1 quintal.
200	66	66	1 barrel of pork or beef
196	66	66	1 barrel of flour.
14	"	66	1 stone.

Exercises for the Slate.

1. In 365 gross 11 doz. 9 units, how many individual Ans. 52701. things?

A person bought 219 cwt. 2 qrs. 2 lbs., short weight, or 2. codfish at \$5 a quintal, what did the whole amount to?

Ans. \$980.00.

What will 6 tons 6 cwt., long weight, of flour cost at 3. Ans. \$558.00. \$7.75 a barrel?

4. What will 15 reams of paper cost at one cent per sheet? Ans. \$72.00

It is said Mr. Jos. Gillott, of Birmingham, manufactures 5. annually 150 millions of different kinds of pens; how many boxes will it require to hold them, each box holding one Ans. 1041666 and 8 doz. pens over. gross?

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1. 2. 3. 1st, 2 c and the whole '

COMPOUND ADDITION.

COMPOUND ADDITION.

101.

Compound Addition is the method of collecting several numbers of the same kind, but containing different denominations of that kind into one number.

102. To Add Compound Numbers

FXAMPLE.—A merchant paid £16 3s. 91d. for tea; £46 11s. $1\frac{1}{4}d$. for sugar ; £101 3s. 5d. for flour ; £13 14s. $2\frac{1}{4}d$. for molasses, and £108 11s. 4_4^3 d. for dry goods; what was the

OPE	KA'	FION.
£	8.	d.
16	3	91
46	11	11
101	3	5^{+}
13	14	21
108	11	43
-		
$\pounds 286$	3	103
		4

ANALYSIS .- Arranging the numbers in columns, placing units of the same denom ination under each other, we first begin at the right hand column, or lowest denomination, and find the amount to be 7 far., which is equal to 1 penny 3 farthings. We write the farthings under the column of farthings, and add the 1 penny to the column of pence We find the amount of

the second column, (with the 1 penny added), to be 22 pence, which is equal to 1 shilling and 10 pence. Writing the 10 pence under the column of pence, we add the 1 shilling to the next column. Adding this column as the preceding ones, we find the amount to be 43 shillings, which is equal to £2 and 3 shillings. Placing the 3s. under the column of shillings, we add £2 to the column of pounds. Adding this last column, we find the amount to be £286, and the whole result, or answer to be $\pounds 286$ 3s. $10\frac{3}{4}$. Hence,

RULE. I. Write the numbers so that those of the same unit value will stand in the same column.

II. Beginning at the right hand, add each denomination as in simple numbers, carrying to each succeeding denomi-nation one for as many units as it takes of the demonina-tion added to make one of the next higher denomination added, to make one of the next higher denomination.

Mental Exercises.

Add together $5\frac{1}{4}d.$, $6\frac{1}{4}d.$, $3\frac{1}{2}d.$, and 2s. $6d\frac{1}{4}d.$ 1.

2. Find the sum of 1s. 2d., 1s. 33d., 4s. 61d.

3. A farmer sold 4 bundles of hay, weighing as follows, . 1st, 2 ewt. 3 qrs., 2nd, 1 ewt. 2 qrs. 14 lbs., 3rd, 1 ewt. 3 qr., and the 4th, 2 cwt. 0 qr. 14 lbs.; what was the weight of the 3

5 sec. to sec. seconds.

7217 sec.

726 min. , beating ns. 86400. years, by me? s 9 hours.

or beef.

individual ns. 52701. weight, ot t to? . \$980.00. ur cost at \$558.00. persheet?ns. \$72.00 nufactures how many olding one pens over.

COMPOUND ADDITION.

			Exci	rci	ses	før	the	51	late				
	(1)	6	6	2)			6	3)				(4)	1
2	S	d.	£	8.	đ.		8 8		d.		£	s.	d.
2	16	3	2	7	8		21	0	73		29	9	107
8	17	6	2 1	4	5		7 1	6 1	10		25	18	41
8	18	5	9 1	0	7		9 1.	4	91		76	16	118
9	5 1		9	2 1	0		8 1	5	8		94	14	3
	(5)			(6)	ý			(7)		•		(8)	
2	8.	ð.	Ths.	oz	dr.		ewt.	ar.	Ib.		tons	. ewt	. ar
3	10	54	22	10	7		31	2	23		3	17	2
7	13	4.3	37	8	13		27	1	16		1	13	0
6	12	81	78	12	8		49	0	8		5	8	3
4	9	61	65	14	5		57	3	12		6	12	1
5	13	54	26	6	10		79	2	6		7	13	2
5	18	43	81	13	8		50	3	20		4	11	9
4	16	6 1	14	7	11		32	0	16		2	17	2
-												(4.0)	
	(9)		(10)	¥		(11)	•			(12)	
OZ.	dwt.	grs.	yds.	ft.	in,		yd. (prs.	nl.		m	. fur	. po.
35	12	21	35	2	10		38	2	3		36	6	33
64	17	19	34	0	6		45	1	2		67	4	16
48	15	11	69	2	8		37	0	3		62	5 5	9
65	18	4	42	1	11		12	3	1		20	5 6	25
91	13	23	30	2	9		42	20	2		04		01
30	19	14	56	1	5		42	0	3		51	. 7	15
		(18)			-	(3)					(15)		
	0	(13)	'			(14)				(10)		
	IUI	. po.	yas.		ae	ro.	. po.			ac.	ro.	po.	
	0i) 20	01		01 05	1	19			70	0	20	
	64 8.1	t 00 7 17	52		20	2	36			15	9	23	
	1	3 9	A1		34	2	15			53	3	19	
	65	5 14	3		46	1	13			40	0	34	
	19	2 22	01		50	1	0			17	1	1	
	8	3 31	12		63	3	22			49	1	37	
		~*	•			0					-		

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COMPOUND SUBTRACTION.

16. Find the sum of 34 lb. 6 oz. 14 dwt., 53 lbs. 10 oz. 5 dwt., 76 lb. 4 oz. 12 dwt., 38 lb. 8 oz. 10 dwt., 83 lb 11 oz 18 dwt., 67 lb. 5 oz. 7 dwt

(4)

14 3

(8)

17 2

8 3

12 1

17 2

(12)

6 33

4 16

5

6 25

2

4 31

7 15

ро. 7

38

23

19 34

1

37

fur. po.

9

8

cwt. qr.

13 0

13 2

11 9

s. d.

9 107

17. Find the sum of 31 da. 17 h. 53 m., 25 da. 21 h. 39 m., 72 da. 8 h. 16 m., 66 da. 23 h. 45 m., 74 da. 7 h. 23 m., 55 da. 15 h. 44 m.

18. A farmer has 23 ac. 1 ro. 26 po. in wheat, 45 ac. 2 ro. 31 po. in oats, 24 ac. 1 ro. 17 po. in barley, 87 ac. 3 ro. 15 po. in grass, and 65 ac. 2 ro. 23 po. in wood land, how much has he altogether?

19. Find the sum of 79 m. 7 fur. 24 po. 4 yd. 2 ft. 7 in., 58 m. 3 fur. 34 po. 3 yd. 1 ft. 10 in., 61 m. 6 fur. 23 po. 2 yd. 2 ft. 8 in., 97 m. 5 fur. 39 po. 5 yd. 1 ft. 9 in., 25 m. 3 fur. 24 po. 1 yd. 0 ft. 11 in. Ans. 323 m. 3 fur. 27 po. 1 yd. 2 ft. 3 in.

20. Add together 324 tons 19 cwt. 2 qrs., 264 tons 14 cwt 15 lbs., 98 tons 3 qrs. 16 lbs. 14 oz., 981 tons 13 oz. 15 drs., long weight. Ans. 1668 tons 14 cwt. 2 qrs. 4 lbs. 11 oz. 15 drs.

21. A farmer received 60 cents a bushel for 4 loads of oats weighing as follows: 2385, 2761, 3962, and 1500 pounds; how many bushels were there, and what was the whole amount, if 1 bush. = 34 lbs.? Ans. 312 bus. \$187.20,

22. Find the sum of 23 bus. 3 pks. 7 qts. 1 pt., 34 bus. 2 pk. 1 pt., 42 bus. 3 pk. 5 qt., 51 bus. 1 pk. 4 qt. 1 pt., 23 bus. 3 qt., 11 bus. 3 pk. 4 qt.

Ans. 187 bus. 3 pks. 1 pt. 23. A man in digging a cellar removed 163 cu. yds. 26 cu. ft. of earth; in digging a trench 19 cu. yds. 14 cu. ft.; and in digging a cistern 17 cu yds. 14 cu. ft.; what was the amountof earth removed, and what did it cost at 22 cents per cubic Ans. 201 cu. yd. \$44.22.

WEIGHT

COMPOUND SUBTRACTION.

103. Compound Subtraction is the method of finding the difference between two numbers of the same kind containing different denominations of that kind.

104. To subtract compound numbers.

EXAMPLE.—A merchant bought 15 cwt. 3 qrs. 14 lb. (long weight) of sugar and sold 9 cwt. 2 qrs. 18 lbs.; how much had he left.

OPE:	RAT	ION.
cwt.	qrs.	lbs.
15	3 '	14
9	2	18
-	_	

0 24

ANALYSIS.—Writing the subtrahend under the minuend, placing units of the same denomination under each other, we begin at the right hand, or lowest denomination; since we cannot take 18 lbs. from 14 lbs., we add 1 qr. or 28 lbs., to 14 making 42 lbs.; and taking 18 lbs. from

42 lbs., we write the remainder, 24 lbs., underneath the column of pounds. Since we took the 1 qr. from the 3 qrs., 2 qrs. remain; and 3 qrs. from 3 qrs. leaves 0 qrs., which we write in the remainder, under the column of quarters. Lastly, we take 9 ewt. from 15 cwt. and write the remainder, 6 cwt., under the column of hundreds weight. Hence,

RULE. I. Write the subtrahend under the minuend, so that units of the same denomination shall stand under each other.

II. Beginning at the right hand, subtract each denomination separately, as in simple numbers.

111. If the number of any denomination in the subtrahend exceed that of the same denomination in the minuend, take 1 from the next higher denomination in the minuend and add as many units to this lower denomination as make one of the higher, and then subtract; in this case it is to be remembered that the number above is one less than before subtracting. Proceed in the same manner with each denomination.

Mental Exercises.

From $3\frac{1}{2}$ d. take $1\frac{3}{4}$ d.; 1s. 9d. take 11d.; 2s. $9\frac{1}{2}$ d. take 1s. $6\frac{1}{2}$ d. 2. A man having 4 ac. 2 ro. of land sold 1 ac. 3 ro., how

much land had he left?

3. A person having £3 6s. 3d., bought 14s. 8d. worth of tea, how much money was left after paying for it?

4. A miner having 5 dwt. 12 grs. of gold, sold 2 dwt. 20 grs., how much had he left?

Exercises for the Slate.

SECTION I.

15

tor

14

2 y

	£	<i>s</i> .	d.	£	8.	d.	1	£	<i>s</i> .	d.	£	s.	d.
(1)	40	15	3-	-13	9	11	(9)	147	0	03	29	16	81
(2)	77	12	5-	-13	19	11	(10)	365	1	11 -	139	16	$10\frac{2}{10}$
(3)	95	10	0	-13	13	10	(11)	558	13	11-	216	4	81
(4)	120	9	5 -	-47	15	1	(12)	721	2	6	387	15	11
(5)	94	10	6-	-39	19	10	(13)	185	2	1 —	67	18	83
(6)	92	0	7	-46	11	7	(14)	526	1	11	318	19	83
(7)	82	14	1-	- 0	17	11	(15)	381	5	73-	11	11	11
(8)	100	0	0-	- 0	0	4	(16)	980	7	$2\frac{1}{4}$ -	583	7	$11\frac{1}{2}$

68

Ans. 6

COMPOUND SUBTRACTION.

SECTION II.

The following exercises are to be worked as the given example.

Note.--1. The teacher may require the pupil after finishing the sub-traction in each exercise, to add all the lines together.

Ex. 1.
EXAMPLE. 10 18 $2\frac{3}{4}$ —Minuend.
6 10 $11\frac{1}{4}$ —Subtrahend
4 7 $3\frac{1}{2}$ 2nd line subtracted C
2 3 $7\frac{3}{2}$ and " subtracted from first.
$2 \ 3 \ 7\frac{3}{2} - 4$ th " second
third
$\pounds 26 3 9 \text{sum} = 12 \text{ times 5th line}$
s. d. s. d.
$ \begin{array}{c} (1) & 1 & 10\frac{1}{2} \\ (2) & 1 & 10\frac{1}{2} \\ (3) & 2 & 15 \\ (5) & 2 & 15 \\ (5) & 2 & 15 \\ (6) & 2 & 15 \\$
$\begin{pmatrix} 2 \\ 2 \end{pmatrix} 2 2 2 \frac{1}{4} - 1 3 \frac{3}{4} \qquad \begin{pmatrix} 0 \\ 6 \end{pmatrix} 4 10 10 \frac{1}{4} - 2 5 3 \frac{3}{4}$
$\binom{3}{3}$ $\binom{3}{3}$ $\binom{23}{4}$ -1 $11\frac{1}{4}$ $\binom{0}{7}$ $\binom{4}{5}$ $\binom{103}{7}$ -2 19 $11\frac{1}{4}$
$(4) 11 10\frac{1}{2} - 7 1\frac{1}{1} \qquad (4) 3 17 7\frac{1}{4} - 3 10 6\frac{1}{4}$
(0) yds ft. in. yds. ft. in. (0) o 18 $5\frac{1}{4}$ -4 3 $0\frac{3}{4}$
(10) 29 1 9-11 2 3 (11) 44 9 01 yds. ft. in
(10) 23 0 7-13 2 9 (12) 70 9 $0^{\frac{1}{2}}$ 26 2 $10\frac{1}{2}$
(12) yds. qrs. nls. yds. qrs. nls. (12) 0^{-4} 0^{-4} 0^{-4} 5^{-5}
(13) 79 2 $3 - 47$ 3 1 (17) 57 2 28 21 m. fur. po. yds
(14) 112 3 1 - 67 2 3 (18) 61 6 18 1 97 0 00 1
(13) 634 1 $3\frac{1}{4}$ -380 2 $2\frac{3}{2}$ (19) 44 6 22 48 370 26 5
(10) 69 3 $2\frac{3}{4}$ 41 3 $3\frac{1}{4}$ (20) 16 4 4 01 0.7 12 $1\frac{3}{4}$
(a) ac. ro. po. ac. ro. po $\frac{4}{100}$ $\frac{104}{2}$ $\frac{4}{2}$ $\frac{01}{2}$ $\frac{102}{2}$ $\frac{102}{2}$
(21) 74 1 20 - 44 2 20 (25) $\frac{100}{74}$ bus. pks. gals. bus. pks. gals
(22) 44 3 35 - 26 3 37 (26) 82 0 1 - 44 2 1
(23) 284 1 15 -170 2 17 (27) 602 2 11 - 49 5 1
(24) 131 3 121 - 79 0 151 (22) 002 3 01 - 361 2 11
2 - 102 + (20)301 3 1 - 181 0 1
29. From 546 lbs. 10 oz. 2 dwt 8 cm tal. 20-11
15 dwt. 14 grs. Ans 148 lbs 10
30. From 486 years take 395 years ?
Ang 00 3 wks. 5 days.
31. From 310 tons 13 cwt 2 cm 1 ms. 30 yrs. 3 mo. 2 days.
tons 13 cwt. 1 qr. 14 lbs, four times, long weight, take 77
32. From 481 acres 1 ro 18 no 111 Ans. 0.
14 po. 18 yds. four times.
33. What is the difference between Ans. 0.
2 yd. 1 ft. 10 in. and 300 miles ?
A por

Ans. 101 m. 14 po. 2 yd. 2ft. 8 in.

rahend of the er, we deno-18 lbs. , to 14 from olumn 2 qrs. rite in e take under

nd, so reach

nomi-

ahend , take d and ce one be reh de-

s. 63d. , how

rth o.

vt. 20
34. A person having 63 gallons of wine, drank, on an average, for five years, including two leap years, one gill of wine a day; how much remained?

Ans. 5 gals. 3 qts. 1 pt. 1 gill. 35. A man having dug from a trench 126 cub. yds. 16 cub. ft., from a cistern 18 cu. yd. 18 cu. ft. 196 cu. in., and from other places 126 cu. yd. 26 cu. ft., was paid for 196 cu. yd. 26 cu. ft. 1714 cu. in.; how much remained unpaid?

Ans. 75 cub. yd. 6 cub. ft. 210 cub. in.

COMPOUND MULTIPLICATION.

105. Compound Multiplication is the method of multiplying a quantity consisting of several denominations by a given number.

106. To Multiply a Compound Number.

CASE I.

107. When the multiplier is under 12.

EXAMPLE 1.—A man sold 6 lots of land, each lot containing 4 ac. 2 ro. 14 po.: how much land is there in all?

ANALYSIS.—In 6 lots there are 6 times as much land as in 1 lot. We write the multiplier under the lowest denomination of the multiplicand, and proceed thus; 6 times 14 po. are 84 poles, equal to 2 ro. 4 po.; and we write the 4 po. under the number multiplied, and carry the 2 ro. to the next

product. Then, 6 times 2 ro. are 12 ro., and 2 ro. added make 14 ro, equal to 3 ac. 2 ro.; and we write the 2 ro. under the number multiplied. Again, 6 times 4 ac. are 24 ac., and 3 ac. added make 27 ac., which we write under the number multiplied.

From the above example and illustration we deduce the following general rule

RULE. I. Write the multiplier under the lowest denomination of the multiplicand.

II. Multiply as in simple numbers, and carry as in addition of compound numbers.

Mental Exercises.

Find the cost of 5 lbs. of tea at 3s. 9d. per pound. 1. 2.

What will 9 lbs. of coffee cost at 1s. 6d. per pound ? 3.

What will 36 pairs of stockings cost at 3s. 11d. per pair? 4.

How many acres are there in four fields each containing 2 ac. 3 ro. 10 po.?

5. If a tailor requires 3 yds. 1 qr. 1 nl. of cloth to make a coat, how many yards must he have to make five coats of the

Exercises for the Slate.

SECTION I.

EXAMPLE.—Multiply £1 2s. $9\frac{1}{4}d$. by 4, and £8 7s. $2\frac{3}{4}d$. by 4.

$\begin{array}{c} \text{OPERATION.} \\ \pounds & s. & d. \\ 1 & 2 & 9\frac{1}{4} \\ \hline & 4 \\ \hline \\$	$\begin{array}{c} \text{OPERATION.} \\ & \pounds & \text{s. } d. \\ & 8 & 17 & 2\frac{3}{4} \\ & & 4 \\ & & & & \\ & & & \\ & & & & \\ & & & \\ & & & \\ & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ &$	$\begin{array}{c} & \mathbf{\hat{x}} & s. & d. \\ & 4 & 11 & 1 \\ & 35 & 8 & 11 \end{array}$	TEST. 1. £ s. 1 2 8 17			
z4 11 1	£35 8 11	40 0 0	10	0	0 4	
			40	0	0	

Multiply each of the following couplets by 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12. Multiply them all first by 2, then all by 3, then all by 4, &c., and test the products as above.

S. a. e. d	
(1) 2 3 and 17 0	\pounds s. d. f s. d
(2) 3 4 and 16 o	(6) 4 3 9 $\frac{1}{2}$ and 5 16 91
(3) 4 52 and 15 at	(7) 3 12 83 and 6 7 21
(4) 7 91 and 15 64	(8) 8 19 113 and 1 0 01
(5) 6 91 and 12 24	(9) 5 17 6 + and 4 2 51
(°) 0 03 and 13 31	(10) 6 13 9 3 and 3 6 91
ac. ro. po. yds. ac. ro. po vds.	
11) 2 3 21 16 and 7 0 18 141	(15) 2 grs. nls. yds. qrs. nls.
12) 5 3 24 19 and 4 0 15 111	(15) 5 3 3 and 6 0 1
13) 3 2 17 3 and 6 1 22 271	(10) 7 2 1 and 2 1 3
(4) 6 0 27 15 and 3 3 12 154	(19) 0 1 1 and 1 2 3
104	(10) 2 12 and 0 1 21

CASE II.

108. When the Multiplier is a Composite nu aber. EXAMPLE.-What is the weight of 42 bundles of hay each weighing 3 cwt. 2 qrs. 12 lbs?

on an gill of

. 1 gill. 16 cub. d from . yd. 26

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ot con-11? mes as multiof the nes 14 ; and umber e next added e 2 ro. 24 ac., er the

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OPER cwt. 3	АТІ qr. 2	co n. lbs., 12 6	ANALYSIS.—Multiply- ing the weight of 1-bundle by 6, we obtain the weight of 6 bundles, and the
21	2	22 weight of 6 bundles. 7	weight of 6 bundles mul- tiplied by 7, gives the weight of 42 bundles.

152 4 weight of 42 bundles. 0

SECTION II.

EXAMPLE .- Multiply £46 13s. 101d., and £53 6s. 11d. by 48.

орегаті £ s. 46 13	ON, <i>d</i> . 10 <u>1</u> 6	OPERATION £ s. d. 53 6 1 12	v. 12	£	<i>s</i> .	d.
280 3	3 8	639 13 6 4	– Test,	$\left\{ {{2241}\atop{2558}} ight.$	$6 \\ 14$	0 0
£2241 6	0	$\pounds 2558 14 0$		£4800	0	0

Multiply each of the following couplets by 14, 16, 18, 20, 21, 22, 24, 27, 28, 30, 32, 36, 40, 42, 45, 48, 50, 54, 56, 60, 64, 72, 81, 96, testing the products as above.

	£	8.	d		£	8.	6	1. 1		lbs.	07.	dr.		lbs.	oz.	dr.
(1)	89	13	(54 an	d 10	6	5	51	(4)	19	14	14	and	80	1	2
(2)	72	14		31 an	d 27	5	8		(4)	89	15	11	and	10	Ô	5
(3) :	36	10	1	14 an	d 63	9	0	$\tilde{1}_{4}^{\tilde{3}}$	(6)	72	13	$-3\frac{1}{4}$	and	27	2	123
to	ns (ewt.	\mathbf{qrs}	3. lbs.	tons	cw	t. qr	s.lbs		ewt.	ars.	lbs		ewt.	ars	lh
(7) 8	33	15	3	27 a	nd1(54	Ũ	1	(11)) 72	3	22	and	27	0	3
(8)	72	16	2	$22\frac{1}{2}$	" 27	3	1	51	(12)	91	1	24	66	8	2	1
(9) 9	91	18	3	114	" 8	1	0	163	(13) 12	3	19		87	õ	51
(10)5	54	15	2	$27\frac{3}{4}$	" 45	4	1	04	(14)	87	1	22	"	12	2	21

Multiply each of the above by 100, 110, 120, 121, 132, 144, using two factors, and by 112, 144, 420, 441, 504, using three factors, e.g. $\begin{array}{r} 420 = 10 \times 6 \times 7 \\ 504 = 8 \times 9 \times 7 \end{array}$

CASE III.

109. When the multiplier cannot be reduced to factors. EXAMPLE.-How many bushels of oats in 47 barrels, each containing 3 bus. 1 pk.?

$\begin{array}{c} \text{OPERATION.} \\ 47 = (5 \times 9) + 2 \\ \text{hus she} \end{array}$
$3 1 \times 2 \\ 5 5$
$\begin{array}{ccc} 16 & 1 & \text{in 5 barrels.} \\ 9 & \end{array}$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$
152 3 in 47 barrels.
31.1.1.1

ANALYSIS .- Multiplying the contents of 1 barrel by 5, and the resulting product by 9, we have the contents of 45 barrels, which is the composite number next less than the given prime number 47. Next multiplying the contents of 1 barrel by 2, we have the contents of 2 barrels, which added to the contents of 45 barrels, gives us the contents of 45 + 2 = 47 barrels.

73

SECTION JII.

Multiply each of the following couplets by 19, 29, 31, 43. 67, 76, 83, 91, 97, 111, 113. 127, 131, 143, 139, and test the results as in the preceding section.

(1) (2) (3)	135 635 299	pks. 3 1 0	gal. 1 0 1	qts. 3 2 1	pts. bus. 1 and 864 1 and 364 1 and 700	pks. 0 2 3	gal. 0 1 0	qts. U 1 9	pts. 1 1
						J	0	2	1

SECTION IV.

110. When the multiplier exceeds 156.

. EXAMPLE. What is the price of 428 articles at £3 17s. $9\frac{1}{2}$ d. each.

014	GRATI	ON.			
1st line	£ 3	8. 17	$d. \\ 9\frac{1}{2} \\ 10$		
3rd line	38	17	11 10	Product by 10	
5th line	388	19	$\frac{2}{4}$	Product by 100	
Multiply 3rd line by $2 =$ Multiply 1st line by $8 =$	1555 77 31	$\begin{array}{c}16\\15\\2\end{array}$	8 10 4	Product by 400 Product by 20 Product by 8	
Add last three results	1664	14	10	•	

each

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s. d.

6 0

14 0

0 0 8, 20, 6, 60,

oz. dr.

1 2

BS.

EXPLANATION.—We see from the above example that there are three figures in the multiplier, and that we have multiplied successively by 10 twice, and then multiplied the last product by the figure of the highest order of the multiplier, the preceeding product by the next lower order of figure, and the first line by the lowest order; we then added the three last products to find the answer. Hence the

RULE. -Multiply successively by 10 as many times less one as there are figures in the multiplier, then multiply the last product by the figure of the highest order of the multiplier, the preceding product by the next lower order of figure, and so on with the other figures. Then the sum of the new products will be the answer.

NOTE.—It is sometimes more convenient to reduce the multiplicand to the lowest denomination and then multiply; and afterwards reduce the product to the highest denomination.

1. Multiply 16 bush. 3 pks. 1 gal. by 678.

Ans. 11441 bush. 1 pk. 2. Multiply 23 m. 6 fur. 33 rods 4 yds. by 247.

Ans. 5892 m. 2 fur. 10 rods 3½ yds. Multiply £3 16s. 5¼d. by 3178. Ans. £10556 18s. 4½d.

SECTION V.

Find the value of—

3.

2.

74

1. 37 tons 13 cwt. 3 qrs. 12 lbs., long weight, $\times 6$

. Ans. 226 tons 3 cwt. 16 lbs. 39 m. 7 fur. 28 po. 4 yds. \times 6.

Ans. 239 m. 6 fur. 12 po. 2 yd. 3. 92 yd. 3 qr. 1 nl. 2 in. \times 765. Ans. 71044 yd. 0 qr. 1 nl. 4. 27 y. 54 days 15 h. 29 m. \times 921.

Ans. 25004 y. 323 d. 4 h. 9 m.

b

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5. If 1 acre of land produce 45 bus. 3 pks. 6 qts. 1 pt. of corn, how much will 64 acres produce ? Ans. 2941 bus.

6. If \$80 purchase 4 ac. 3 ro. 26 po. 20 sq. yd. 3 sq. ft. of land, how much will \$4800 buy? Ans. 295 ac. 10 sq. yd.

7. What will 16 tons of hay cost at £3 19s. $6\frac{1}{2}$ d. per ton ? Ans. £63 12s. 8d.

8. What is the cost of 8 bus. 3 pks. of beans at $5\frac{1}{2}d$. per quart? Ans. £6 8s. 4d.

9. If 1 pt. 3 gills of wine fill 1 bottle, how much will be required to fill a great gross of bottles of the same capacity? Ans. 378 gals.

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. 1 pk.

31 yds. 8s. 41d.

16 lbs.

o. 2 yd. r. 1 nl.

h. 9 m. 1 pt. of 41 bus. 1. ft. of sq. yd. er ton?12s. 8d. Id. per 8s. 4d. will be pacity? 78 gals.

10. Saint John, March 17th, 1866. MR. C. CLARKE, Bo't of J. C. SMITH & Co. 25 lbs. Sugar, at \$0.11 \$ 5 lbs. Tea, 66 .621 4 gals. Molasses, " .49 30-yds. White Cotton, " .27

Received payment,

\$15.933

J. C. Sмітн & Co. per John Newcomb.

11. Halifax, March 19th, 1866. WILLIAM JONES, ESQ., T. W D D

Jan. 1. Dec. 6.	To 15 lbs. Tea, at 50c. \$	
Feb. 5. Mar 14	" 1 bbl. Flour, at \$9.50,	
Tracel . 1.7.	20 yds. Grey Homespun, at 62 ¹ / ₃ c.	

\$35.75

12. MR. JAMES CROWE,

Fredericton, Feb. 22nd, 1866.

 17 lbs. Sugar, 3¹/₂ lbs. Tea, 13 lbs. Coffee, 3 gals. Burning Fluid, 15 lbs. Brown Soap, 	Bought of S JOHNSON. at 6 ¹ / ₂ d. £ " 2s. 7 ¹ / ₂ d. " 1s. 9d. " 7s. 6d. " 4 ¹ / ₄ d.	
1,	£3 9	31

Saint Stephen, Feb. 17th, 1866--Mr. Andrew Bryden, 13. bought of John Fraser, 17¹/₂ yds. superfine cloth at 22s. 6d. per yd., 271 yds. drab cloth at 12s. 8d., 341 drugget at 7s. 10d., $18\frac{1}{8}$ yds. broad cloth at 17s. 4d., $29\frac{3}{8}$ yds. serge at 2s. 10d.

Ans. £70 4s. 71d.

Chatham, Feb. 22nd, 1866 .- Mr. James Scott, bought 14. of John Young, 24 yds. white cotton, at 27 cents per yard, $17\frac{3}{4}$ yds. flannel at \$0.45, $26\frac{1}{2}$ yds. shalloon at \$0.37, $5\frac{1}{4}$ yds. broad cloth at \$4.75, 15 yds. broad cloth at \$1.82, 27 yds. lining cotton at 71 cents. Ans. \$78.531.

15. Moncton, Sep. 1st, 1880.—Mr. Robert Jones bought of Thomas Fraser, 65 bbls. of flour, at \$6.50 per bbl., $38\frac{1}{2}$ cwt. of sugar at the rate of 9 cents per lb., 3 boxes of tea, each containing 65 lbs. at 45 cents per lb., $16\frac{1}{2}$ yds. of cloth at \$3.50 per yd., 14 gals. of oil at the rate of 10 cents per quart. Ans. \$920.10.

NOTE.—Questions 13, 14 and 15 should be written out in the same form as the three previous examples.

COMPOUND DIVISION.

111. Compound Division is the method of dividing a quantity consisting of several denominations.

112. Compound division is divided into two cases— 1st, When the divisor is an Abstract number. 2nd. When the divisor is a Compound number.

CASE I.

EXAMPLE.—If 6 acres of land produce 153 bushels 3 pks. 3 qts of oats, how much will 1 acre produce ?

OPERATION. bus. pks. qts. pts.

6)153 3 3 0

 $25 \ 2 \ 4 \ 1$

ANALYSIS.—One acre will produce $\frac{1}{6}$ as much as 6 acres. Writing the divisor on the left of the dividend, we divide 153 bus. by 6, and obtain a quotient of 25 bus., and a remainder of 3 bus. We write the 25 bus. under the denom-

ination of bushels, and reduce the 3 bus. to pecks, making 12 pecks, and the 3 pecks of the dividend added make 15 pecks. Dividing 15 pks. by 6, we obtain a quotient of 2 pks. and a remainder of 3 pks.; writing the 2 pecks under the order of pecks, we next reduce 3 pks to quarts, adding the 3 qts. of the dividend, making 27 qts., which being divided by 6 gives a quotient of 4 qts. and a remainder of 3 qts. Writing the 4 qts. under the order of quarts, and reducing the remainder, 3 qts., to pints, we have 6 pints, which divided by 6 give a quotient of 1 pt., which we write under the order of pints, and the work is finished.

EXAMPLE 2.—When 98 acres produce 2739 bush. 1 pk. 5 qts. of grain, what will 1 acre produce ?

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1 pk.

OPERATION. bus. pks. gal. qts. 3) 2739 1 0 5 '27 bus. 196 779 686 93 4	When the divisor is large and not a composite number, we di- vide by long division, as shown in the operation. From these examples we form the following rule:
373(3 pks. 294 79 2 158(1 gal. 98 60	
4 245(2 qts. 196 49 2 98(1 pt.	

Ans. 27 bu. 3 pks. 1 gal. 2 qt. 1 pt.

RULE. I. Divide the highest denomination, as in simple numbers, and each succeeding denomination in the same manner, if there be no remainder.

II. If there be a remainder after dividing any denomi-nation, reduce it to the next lower denomination, adding in the given number of that denomination in the dividend, if any, and divide as before.

III. The several partial quotients will be the quotient required.

Notes .-- 1. When the divisor is large and is a composite number, we may shorten the work by dividing by the factors.

When the divisor contains a fraction, as 54, &c., proceed as di-2. rected in Simple Division. See page 38.

Mental Exercises.

1. How much sugar at 9d. per lb. may be bought for 117 pence?

How much white sugar at 8d. per lb. may be bought $\mathbf{2.}$ for 1s. 8d. ?

3. How much cloth at 7s. per yard, may be bought for £3 17s.?

4. If 9 boxes of figs weighed 28 lbs. 2 oz., what was the weight of 1 box?

5. If 7 bags of rice weighed 12 cwt. 3 qrs. (long weight), what was the weight of 1 bag?

⁶. How much molasses, at $7\frac{1}{2}d$. per quart, may be purchased for £1 17s. 6d.

Exercises for the Slate.

SECTION I.

Answers to be tested by multiplying the quotient.

(1)	£ 19	16	$0 \stackrel{\cdot}{-} 2$	(11)	£ 7947	6	8 - 14
(2)	109	1	4 - 2	(12)	1640	G	$11\frac{1}{2} - 14$
(3)	324	4	$6\frac{3}{4} - 3$	(13)	2927	2	$4\frac{1}{2} - 18$
(4)	858	10	$11\frac{1}{4} \div 5$	(14)	6121	4	7 - 20
(5)	904	0	11 - 5	(15)	4636	3	$0\frac{3}{4} - 27$
(6)	1515	2	3 - 6	(16)	21624	4	$0^{-1} \xrightarrow{\cdot} 96$
(7)	1513	2	$5\frac{1}{2} - 7$	(17)	25055	6	41 - 121
(8)	2521	4	6 - 8	(18)	48483	12	0^{-128}
(9)	1488	17	$2\frac{3}{1} - 11$	(19)	80886	13	4 - 178
10)	1624	4	3 - 12	(20)	46690	13	0 - 216

SECTION II.

In the following exercises the remainders (if any) are divisible by 9.

	tons.	cwt.	qrs.	lbs.	0Z.	drs. (long weight.)
(1)	0	82	0	27	3	8 - 45, 81 and 171
(2)		101	0	2	3	11 - 54, 63 and 162
(3)	181	2	1	13	15	0 - 243, 423 and 432
(4)	1631	18	2	8	10	15 - 621, 162 and 261
(5)	72036	1	1	27	10	9 - 765, 675 and 999
(6)	80163	0	3	2	0	7 - 4392, 5904 and 9045
	lbs.	oz.	dwt.	gra	3.	
(7)	46	5	11	() -	18, 27 and 36
(8)	326	4	10	5) -	126, 261 and 396
(9)	7908	7	2	21		576, 729 and 891

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-14 -14 -18 -20 -27 -96 -121 -128-176

divi-

- 216

	miles.	fur.	po.	yds	. ft.	in.			
(14)	887	3	30	2	10	9 -	· 621.	. 54 and	702
(11)	2662	\$	11	+	2	3 -	- 207.	594 and	945
(12)	4644	3	31	í	0	9 -	- 846.	468 and	711
(13)	59816	1	18	5	0	6 -	- 333	549 and	27
	dys.	hrs.	min.	sec	3.				
(14)	1314	•	2	42	- 4	5. 72. 8	1 and	99	
(15)	32626	10	8	24	÷ 6	12.711	. 549 :	and 279	
(16)	32627	22	4	21	- 3	24, 981	, 117 :	wad 819	
	yrs.	neo.	wks.	dys.	hrs.	min.	sec.		
(17)	353	0	0	182	6	46	48 -	- 62 and	117
(18)	1278	0	9	199	10	37	12 -	- 972 and	714
(19)	7877	G	ø	4	17	84	48-	- 567 and	756
(20)	\$274	1	1	4	10	10	48 -	- 576 and	657

CASE II.

113. When the divisor is a compound number.

EXAMPLE.—How many times are £5 10c. 10d. contained in £537 10s. 10d. ?

	GPER	ATI	ON.	ANALYSIS Here we		
£ s. 5 10 20 12 \$30	d. £ 10)557 20 10750 12 125010 11970	<i>s</i> . 10	d. 10(97 times.	reduce both divisor and dividend to pence, that being the lowest denomi- nation contained in either. We then find the divisor, 1330, is contained in the dividend 97 times.		
	9310 9310			Hence the following		

RULE.-Reduce both divisor and dividend to the lowest denomination in either, then proceed as in simple num-

SECTION III.

1. How often is £2 10s. contained in £17 10s.

2. If a gold ring cost £3 12s. ¢d., how many of the same kind may I have for £130 10s.? Ans. 3¢.

3. How many yards of cloth worth 4s. 6³/₄d. a yard, myst be given in exchange for 36 yards at £1 2s. 93d.? Ans. 180. 4. How many barrels are there in 151 bus. 3 pks. 1 ral.

of oats, if 1 barrel contain 3 bu. 1 pk. 1 gal.?

Ans. 4. Trarels.

SECTION IV.

General Exercises.

Divide

4.

69 miles 4 fur. 4 po. 2 yds. by 8. 1.

Ans. 8 m. 5 fur. 20 po. 3 yd.

31 lbs. 11 oz. 15 dwt., by 5. 2. Ans. 6 lb. 4 oz. 15 dwt. 35 days 22 h. 52 m. 48 see., by 6. 3.

Ans. 5 d. 23 h. 48 m. 48 sec. 6429 miles 6 fur. 2 po. 1 yd. 1 ft. 8 in., by 76.

Ans. 84 m. 4 fur. 32 po. 3 yds. 1 ft. 11 in. 5. 646 yds. 3 qrs., by 26. Ans. 24 yds. 3 qrs. 2 nls. 6.

£468 3s. 71d., by 41.

Ans. £104 0s. 91d. 5. 7. $\pounds 429$ 18s. $3\frac{1}{4}$ d. by $43\frac{5}{6}$.

Ans. £9 16s. 18d. 157. 8921 tons 15 cwt. 2 qrs. 18 lbs. 15 oz. 15 drs., fong 8. weight, by 599. Ans. 14 tons. 17 cwt 3 qrs. 15 lbs. 9 oz. 9 dr. 9.

7154 days 16 h. 52 m. 48 sec., by 57.

Ans. 125 d. 12 h. 30 m. 24 sec,

How often is £5 10s. contained in £38 10s. 10.

Ans. 7 times. 11. How many yards of cloth worth 7s. 81d. a yard, can be bought for £32 7s. 6d.? Ans. 84 yards.

12. If a single article cost 4s. $6\frac{1}{2}$ d., how many dozen may be bought for £196 4s.? Ans. 72.

13. How many yards of cloth worth 4s. 63 d. a yard, must be given in exchange for 36 yards at £1 2s. $9\frac{3}{4}$ d. per yard?

Ans. 180. 14. A man travelled by railroad 1000 miles in one day; what was the average rate per hour ?

Ans. 41 m. 5 fur. 13 po. 5 ft. 6 in. 15. If a family use 10 bbls. of flour in a year, what is the average amount each day? Ans. 5 lb. 5 oz. 1450 dr.

16. A tailor put 276 yds. 3 qrs. of cloth into 20 cloaks; how much cloth did each cloak contain ?

Ans. 13 yds. 3 qrs. 12 nls. 17. A clothier bought 4 pieces of cloth, each containing 60 yds. 2.25 qrs.; after selling $\frac{1}{3}$ of the whole, he had the remainder made into suits containing 9 yd. 2 qr. each; how many suits did it make ? Ans. 17.

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PROMISCUOUS EXERCISES.

PROMISCUOUS EXERCISES IN THE PRECEDING RULES.

When going over these and subsequent exercises, the pupil should be required to state in general terms-1st. What is given and what is required in each problem. 2nd. How it is proposed to us it, giving each step clearly and briefly in its

If a pupil be thoroughly subjected to this training, day after day at the black-board, clearing up every difficulty in each problem before the teacher and class, his success in arithmetic is in a great measure certain

1. A merchant bought a quantity of sugar for 290 guineas, but paid for it with half-crowns, required how many he gave?

2. How many feet will a boy walk to school, which is distant 1 m. 7 fur. 38 po. 4 yds. 2 ft.? 3.

If $36\frac{1}{2}$ bushels of corn grow on one acre, how many Ans. 10541 feet. acres will produce 657 bushels?

4. A man wishes to ship 1560 bushels of shoe pegs in Ans. 18 acres. barrels containing 3 bus. 1 pk. each; how many barrels will

5. A farm consisting of 4 fields, has in one 28 ac. 37 po., in another 27 ac. 2 ro. 26 yds., in another 41 ac. 2 ro. 39 po. 5 ft., and in another 17 ac. 3 ro. 14 yd. 142 inches; required how many inches are in the whole?

Ans. 722817646. From the sum of £2 17s. $6\frac{1}{4}d$. + £5 11s. $4\frac{1}{2}d$. + £5 6. 16s. $10\frac{1}{2}d. + \pounds 4$ 10s. $1\frac{3}{4}d. + \pounds 7$ 16s. $6\frac{1}{2}d.$ take £18 15s. 11d.; multiply the remainder by 11, and divide the product by 13.

7. A merchant bought goods for £456 17s. $3\frac{1}{4}$ d. and sold them for £530 0s. 6d.; what did he clear on his purchase?

Ans. £73 3s. 23d.

Suppose the pulse to beat once in a second, how often 8. will it beat during a year of 365 days?

Ans. 31536000 times. 9. A jeweller bought 35 gold watches at £24 10s. each, 49 silver watches at £6 15s. each, 85 gold rings at £1 16s. each, 97 brooches at 17s. 6d. each ; how much money did he 10. Supposing a pair of trousers require 2 yds. 2 qrs. 3 nls.; Ans. £1426 2s. 6d. how much cloth will it require to make 3 doz. pairs?

Ans. 96 yds. 3 qrs.

rd, must ns. 180. s. 1 gal.

i . rels.

). 3 vd. 15 dwt.

48 sec.

. 11 in. . 2 nls. 91d. 5. d. 157. , long z. 9 dr.

24 sec,

times. d, can yards. n may ns. 72. must yard? . 180. day;

6 in. is the adr. oaks;

2 nls. ining ie rehow 3. 17.

PROMISCUOUS EXERCISES.

11. What distance will a train travel in 24 hours at the rate of 19 miles 7 fur. 39 po. 5 yds. per hour?

Ans. 479 miles 7 fur. 37 po. 41 yas.

12. If seven horses cost £69 6s., what will one cost? Ans. £9 18s.

13. If 3 yds. cost £1 2s. what will 27 yds. cost? Ans. £9 18s.

Note. -27 yds. will cost 9 times more than 3 yds.; therefore $\pounds 1 2s. 9d. \times 9 = Ans.$

14. The wages of 8 men amount to \$28.48, what will the wages of 128 men amount to ? Ans. \$455.68

Nor....The wages of one man will be $$28.48 \div 8 = 3.56 , which multiplied by 128 = Ans.

15. If 56 sheep cost \$316.80, what will 7 cost?

Ans. \$39.60.

16. How long would 36 labourers take to dig a field which 12 men can dig in 27 days? Ans. 9 days.

17. A farmer bought 3 score of lambs at 17s. 6d. each, 2 score of sheep at £1 19s. 11d. each, 24 cows at £9 15s. 8d. each, 6 horses at 39 guineas each, the expenses of getting them all home amounted to 15 guineas; how much money must he draw from his banker to meet the outlay?

Ans. £628 11s. 8d.

18. If 35 sheep cost \$508.90, what is the cost of 5 ? Ans. \$72.70.

19. When eggs are selling 5 for 2 pence, what should 11 doz. and 3 eggs cost? Ans. 4s. 6d.

NOTE -- The price of one egg = $\frac{2}{5}$ d.

20. I went to a shop and bought 7 yds. of cloth at 7s. 6d. per yd., 20 yds. white cotton at 35 cents per yard; what change did I get out of £5? Ans. 18s. 8³/₄d.

21. An estate consisting of 1977 acres 3 roods is divided into farms containing on an average 98 acres 3 ro. 20 poles each; required the number of farms in the estate?

Ans. 20 farms.

22. If a bushel of barley cost \$0.80, what will 21 bus. 2 pks. cost at the same rate? Ans. \$17.20.

23. Mr. Flint has two shares in a shoe factory, the capital of which is made up of one hundred and six equal shares, there is a clear gain of \$2098.80 at the end of the year. How much should Mr. F. receive? Ans. \$39.60.

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VULGAR OR COMMON FRACTIONS.

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. \$39.60. g a field . 9 days. d. each, 15s. 8d. f getting h moncy

11s. 8d. 5? . \$72.70. hould 11 s. 4s. 6d.

at 7s. 6d. d; what 18s. 8³d. s divided 20 poles

20 farms. us. 2 pks. a. \$17.20. ne capital dl shares, the year. s. \$39.60.

VULGAR OR COMMON FRACTIONS.

Definitions, Notation and Numeration.

114. If a unit be divided into 2 equal parts, one of these parts is called one half.

If a unit be divided into 3 equal parts, one of the parts is called one third, two of the parts two thirds.

If a unit be divided into 4 equal parts, one of the parts is called one fourth, two of the parts two fourths, three of the parts three fourths, &e.

The parts are expressed by figures ; thus,

One half is	written	12	One fourth is	written	1
One third	66 I		Two fourths	"	4 04
Two thirds	66 -		Three fourths	66	4

Hence we see that the parts into which a unit is divided take their name and their value from the number of equal parts into which the unit is divided. Thus, if we divide an apple into three equal parts, the parts are called *thirds*; if into 4 equal parts, *fourths*, &e.; and each *fourth* is less in value than each *third*, and the greater the *number* of parts the less the value of each.

When a unit is divided into any number of equal parts, one or more such parts is a fractional part of the whole number, and is called a *fraction*. Hence,

115. A Fraction is one or more of the equal parts of a unit.

116. To write a fraction we require two integers, one to express the number of parts into which the whole number is divided, and the other to express the number of parts taken. Thus, if one orange be divided into 5 equal parts, the parts are called *fifths*, and three of these parts are called *three fifths* of an orange.

These may be written

3 the number of parts saken.

5 the number of parts into which the orange is divided.

117. The **Denominator** is the number below the line. It denominates or names the parts; and It shows how many parts are equal to a unit.

VULGAR OR COMMON FRACTIONS.

118. The **Numerator** is the number above the line. It numerates or numbers the parts : and

It shows how many parts are taken or expressed by the fraction.

119. The **Terms** of a fraction are the numerator and denominator taken together.

120. Fractions indicate division, the numerator answering the dividend, and the denominator to the divisor. Hence,

121. The Value of a fraction is the quotient of the numerator divided by the denominator.

Exercises in Notation and Numeration.

Express the following fractions by figures :---

- 1. Seven eighths.
- 2. Three twenty-fifths.
- 3. Twenty-seven ninetf-sixths.
- 4. Seven one hundred and twenty-sevenths.
- 5. Two hundred and four four hundred and fifty-thirds.

6. Nine hundred one thousand and fifty-fourths.

122. To analyze a fraction is to designate and describe its numerator and denominator. Thus, $\frac{3}{4}$ is analyzed as follows :—

4 is the *denominator* and shows that the unit is divided into 4 equal parts; it is the divisor.

3 is the numerator, and shows that 3 parts are taken; it is the dividend, or integer divided.

3 and 4 are the terms, considered as dividend and divisor. The value of the fraction is the quotient of $3 \div 4$, or $\frac{3}{4}$.

Read and analyze the following fractions :-

- 7. $\frac{8}{7}$; $\frac{11}{12}$; $\frac{5}{6}$; $\frac{13}{27}$; $\frac{16}{156}$; $\frac{19}{37}$; $\frac{11}{151}$; $\frac{125}{168}$.
- 8. $\frac{17}{104}$; $\frac{19}{101}$; $\frac{355}{4867}$; $\frac{51}{1000}$; $\frac{3867}{100017}$.

123. Fractions are distinguished as Proper and Improper, and as Simple, Compound, Complex.

A **Proper Fraction** is one whose numerator is less than its denominator. As $\frac{3}{4}$, $\frac{5}{6}$, $\frac{11}{12}$.

An Improper Fraction is one whose numerator equals or exceeds its denominator. As $\frac{8}{8}$, $\frac{17}{16}$, $\frac{35}{32}$, $\frac{39}{16}$.

A Simple Fraction has but one numerator and one denominator, as $\frac{3}{4}$.

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A Compound Fraction is a fraction of a fraction, as 3 of ₽

A Complex Fraction is that which has a fraction either in its enumerator or denominator, or in each of them, as,

$2\frac{1}{3}$	$3\frac{1}{5}$	23
2'	$\overline{4\frac{1}{3}}'$	47

124. A Mixed Number is a number expressed by a whole number and a fraction. As $14\frac{1}{2}$, $11\frac{9}{15}$.

125. Since the value of a fraction is the quotient obtained by dividing the numerator by the denominator, by the laws of Division we have the following

General principles of Fractions.

126. PEIN. I. Multiplying the numerator multiplies the fraction, and dividing the numerator divides the frac-

PRIN. II. Multiplying the denominator divides the fraction, and dividing the denominator multiplies the frac-

PRIN. III. Multiplying or dividing both terms of the fraction by the same number does not alter the value of the

REDUCTION OF FRACTIONS.

CASE T.

127. To reduce fractions to their lowest terms.

A fraction is in its lowest terms when its numerator and denominator are prime to each other; that is, when both terms have no common divisor.

EXAMPLE.—Reduce the fraction $\frac{3.0}{4.8}$ to its lowest terms. FIRST OPERATION.

 $\frac{8_{\frac{30}{48}}}{\frac{10}{16}} = \frac{2}{\frac{10}{16}} = \frac{5}{8}$ Ans.

ANALYSIS .- Dividing both

terms of a fraction by the same

number does not alter the value of the fraction or quotient (126, Prin. III.,) hence, we divide both terms of $\frac{30}{18}$ by 3, both terms of the result, $\frac{10}{16}$, by 2. the terms of $\frac{5}{8}$ are prime to each other, the lowest terms of $\frac{30}{48}$ are $\frac{5}{8}$. We have, in effect cancelled all the factors common to the numerator and domainator.

SECOND OPERATION. In this operation we have divided $6)_{\frac{30}{48}=\frac{5}{8}}^{30}$, Ans. the terms of the fraction by the great-

est common divisor, (57,) and thus

performed the reduction at a single division. Hence the

RULE. I. Cancel or reject all factors common to both numerator and denominator. Or,

II. Divide both terms by their greatest common measure, or divisor.

Mental Exercises.

Reduce the following fractions to their lowest terms :- $\frac{1}{6}$: $\frac{3}{26}$; $\frac{13}{26}$; $\frac{21}{27}$; $\frac{18}{36}$; $\frac{5}{55}$; $\frac{9}{54}$; $\frac{8}{72}$; $\frac{16}{72}$; $\frac{26}{78}$; $\frac{28}{112}$; $\frac{16}{112}$; $\frac{19}{95}$; $\frac{105}{140}$ and $\frac{112}{26}$.

Exercises for the Slate.

1.	$\frac{155}{180}$	Ans. $\frac{31}{36}$	6.	$\frac{3080}{5940}$	Ans. $\frac{17}{33}$
2.	288	45	7.	$\tfrac{172}{1118}$	$\frac{2}{13}$
3.	$\frac{441}{462}$	$\frac{21}{22}$	8.	$\frac{5643}{5940}$	1920
4.	$\frac{675}{810}$	56	9.	$\frac{315}{345}$	$\frac{21}{23}$
5.	$\frac{1155}{1260}$	$\frac{11}{12}$	10.	$\begin{array}{r} 684\\ 1558 \end{array}$	$\frac{18}{41}$

CASE II.

128. To reduce an improper fraction to a whole or mixea number.

EXAMPLE.—Reduce $\frac{3}{7}$ to a whole or mixed number.

OPERATION.	ANALYSISSince 7 sevenths
$\frac{3}{7} = 32 - 7 = 44$, Ans.	equal 1, 32 sevenths are equal
	to as many times 1 as 7 is con-

tained in 32, which is 44 times. Hence the following-

RULE.-Divide the numerator by the denominator.

Notes.—1. When the dependator exactly divides the numerator, the result is a whole number.

2. In all answers ϵ ntain ng fractions, the fractions should be reduced to their lowest comp

Mental Exercises.

1. How many whole things are in 12 halves? 16 halves? 24 halves?

2. How many whole things are in 15 thirds? in 18 thirds? 3. Reduce $\frac{7}{3}$, $\frac{5}{4}$, $\frac{16}{5}$, $\frac{21}{5}$, $\frac{54}{7}$, $\frac{125}{7}$, $\frac{121}{4}$, $\frac{144}{12}$, $\frac{118}{11}$, $\frac{199}{19}$, $\frac{1678}{10}$, to whole or mixed numbers.

Exercises for the Slate.

1.	In $\frac{113}{7}$ of a month, how many months?	Ans. 161
2.	In $\frac{117}{5}$ of a bushel, how many bushels?	233
3.	In 563 of a dollar, how many dollars?	1873
4.	In $\frac{176}{8}$ of a ton, how many tons?	22
5.	Reduce $\frac{1437}{701}$ to a mixed number.	$2\frac{35}{501}$
6.	Reduce $\frac{6570}{292}$ to a mixed number.	$22\frac{1}{2}$
7.	Change $\frac{2531520}{360}$ to a whole number.	7032

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CASE III.

129. To reduce a whole number to a fraction having a given denominator.

EXAMPLE.—Reduce 15 bushels to sevenths of a bushel. OPERATION.

15

7

ANALYSIS .- Since in 1 bushel there are 7 sevenths, in 15 bus. there are 15 times 7 sevenths, which are 105 sevenths = 105. In practice we multiply 15, the number of 105 Ans. bushels, by 7, the given denominator, and taking the product 105, for the numerator of

a fraction, and the given denominator, 7, for the denominator, we have $\frac{105}{7}$. Hence we have the

RULE. Multiply the whole number by the given denom-inator, take the product for a numerator, under which write the given denominator.

NOTE .- A whole number is reduced to a fractional form by writing 1 under it for a denominator. Thus $12 = \frac{1}{2}$.

Mental Exercises.

Reduce 25 bushels to 4ths of a bushel. 1.

2. Reduce 7 yards to 4ths of a yard.

In 56 dollars how many 10ths of a dollar? 3.

A man distributed 3 dollars among some poor persons, 4. giving $\frac{1}{5}$ of a dollar to each; how many persons received the money ?

Exercises for the Slate.

Change 126 to a fraction whose denominator shall be 1. 19. Ans. 2394 2. Reduce 145 pounds to 16ths of a pound. Ans. 2320

Change 365 to the form of a fraction. 3.

4. In 196 gallons how many 8ths? Ans. 1568

5. Change 187 to a fraction whose denominator shall be 23.Ans. 4301

CASE IV.

130. To reduce a mixed number to an improper fraction.

EXAMPLE	-In $6\frac{1}{8}$ dollars, how many eighths of a dollar?
OPERATION.	ANALYSIS.—Since in 1 dollar there are 8
$6\frac{1}{8}$	eighths, in 6 dollars there are 6 times 8
8	eighths, or 48 eighths, and 48 eighths + 1
49	eighth = 49 eighths, or $\frac{4.9}{2}$. From this we
8	derive the following

RULE. Multiply the whole number by the denominator of the fraction; to the product add the numerator, and under the sum write the denominator.

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8 thirds? $\frac{99}{9}, \frac{1678}{10},$

Ans. 161 232 $187\frac{2}{3}$ 22 $2\frac{35}{701}$ $22\frac{1}{2}$ 7032

Mental Exercises.

1. How many times $\frac{1}{7}$, or how many sevenths, are in $6\frac{3}{7}$? in $18\frac{3}{7}$? in $16\frac{6}{7}$?

2. How many times $\frac{1}{10}$ are in $5\frac{1}{10}$? in $8\frac{3}{10}$? in $15\frac{4}{10}$? in $22\frac{8}{10}$?

3. In $16\frac{1}{3}$ how many thirds?

88

4. In $9\frac{7}{12}$ how many twelfths?

5. Reduce $20\frac{2}{3}$ to an improper fraction.

6. How do you change a whole number to a fraction having a required denominator?

7. How do you change a mixed number to an improper fraction?

Exercises for the Slate.

Reduce the following mixed numbers to improper fractions

1.	718	Ans. 358	7.	22514	Ans. 5639
2.	$161\frac{2}{4}\frac{1}{0}^{4}$	<u>6461</u>	8.	$21\frac{7}{7}$	<u>126</u>
3.	$27\frac{19}{31}$	856	9.	13121	60 <u>8820</u>
4.	$39\frac{1}{3}\frac{8}{8}$	1495	10.	$156\frac{29}{13}$	29 2353
5.	126_{181}	22809	11.	$1111_{-1}^{1.5}$	$\begin{array}{r}15\\128882\end{array}$
6.	$567\frac{4}{121}$		12.	$1234\frac{123}{124}$	111

CASE V.

181. To reduce a fraction to a given denominator.

As fractions may be reduced to *lower terms* by division, they may also be reduced to *higher terms* by multiplication; and all the higher terms must be multiples of the lowest terms.

EXAMPLE.-Reduce $\frac{5}{6}$ to a fraction whose denominator is 24.OPERATION.ANALYSIS.-We first divide 24, the $24 \div 6 \equiv 4$ required denominator, by 6, the de-
nominator of the given fraction, to
ascertain if it be a multiple of this term 6.

The division shows that it is a multiple of this term 6. factor which must be used to produce this multiple of 6. We therefore multiply both terms of $\frac{5}{6}$ by 4, (**126**, P. III.,) and obtain $\frac{20}{24}$, the desired result. Hence the

RULE.—Divide the required denominater by the denominator of the given fraction, and multiply both terms of the fraction by the quotient. 132 inator. A C

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 $\begin{array}{c} \text{OPERA} \\ \frac{3}{4} \times \begin{array}{c} 6 \\ 6 \\ \frac{5}{6} \times \begin{array}{c} 4 \\ 4 \end{array} \end{array}$

must re new de nators. RUL: nomina

NOTE

Redunator. 1. $\frac{1}{2}$ 2. $\frac{4}{5}$ 3. $\frac{9}{1}$ 4. $\frac{5}{6}$

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Mental Exercises.

In 1 of 1 how many tenths? 1. 2.

In # of 1 how many twentieths? 3.

In $\frac{1}{9}$ of 1 how many thirty-sixths? 4.

- In 5 of 1 how many fourteenths? 5.
 - In $\frac{25}{90}$ of 1 how many one hundred and eightieths?

Exercises for the Slate.

Reduce $\frac{3}{8}$ to a fraction whose denominator is 264. 1.

Reduce $\frac{12}{17}$ to a fraction whose denominator is 51. Ans. $\frac{991}{264}$ 2. 3. Ans. 36

Reduce $\frac{125}{436}$ to a fraction whose denominator is 3488. Ans. $\frac{1000}{3488}$ 4.

Reduce $\frac{5}{9}$ to a fraction whose denominator is 6300. Ans. 3500

CASE VI.

To reduce two or more fractions to a common denom-132 inalor.

A Common Denominator is a denominator common to two or more fractions. Thus 4 is the common denominator of 1, 3 and 2.

EXAMPLE.—Reduce $\frac{3}{4}$ and $\frac{5}{6}$ to a common denominator. OPERATION.

ANALYSIS .- We multiply the terms of $\frac{3}{4} \times \frac{6}{6} = \frac{18}{24}$ the first fraction by the denominator of the $\frac{5}{8} \times \frac{4}{4} = \frac{20}{24}$ second, and the terms of the second fraction by the denominator of the first, (126.) This must reduce each fraction to the same denominator, for each new denominator will be the product of the given denominators. Hence the

RULE. Multiply the terms of each fraction by the de-nominators of all the other fractions.

NOTE .- Mixed numbers must first be reduced to improper fractions

Exercises for the Slate.

Reduce to equivalent fractions having a common denominator.

1. 2.	$\frac{1}{2}, \frac{3}{4}, \frac{3}{6}$ and $\frac{1}{9}$.	Ans. 31 3, 324, 360, 48
3.	9 16. 1 and 2.	$\frac{288}{360}, \frac{210}{360}, \frac{300}{360}$
4.	$\frac{5}{6}, 2\frac{1}{2}, \frac{3}{4}$ and $\frac{1}{3}$.	$\begin{array}{c} 4327 \\ 437 \\ 437 \\ 437 \\ 437 \\ 437 \\ 437 \\ 4$
	$\frac{1}{8}, \frac{1}{10}$ and 4.	

CASE VII.

183. To reduce fractions to the least common denominator. The **Least Common Denominator** of two or more fractions, is the least common denominator to which they can all be reduced, and it must be the least common multiple of the lowest denominators.

NOTE .-. . . stands for therefore.

EXAMPLE.—Reduce $\frac{1}{6}$, $\frac{3}{4}$ and $\frac{5}{8}$ to the least common denominator.

0	PE	RATIC	N.	
2	6	(4)	8	
	3	•	4	

 $3 \times 4 \times 2 \equiv 24$

Therefore $2 \times 2 \times 2 \times 3 \equiv 24$

Since	$24 \div 6 = 4 \therefore \frac{1}{6} \times \frac{4}{4} = \frac{4}{24}$
66	$24 \div 4 = 6 \therefore \frac{3}{4} \times \frac{6}{6} = \frac{18}{24}$
66	$24 \div 8 \equiv 3 \therefore \frac{5}{8} \times \frac{3}{3} \div \frac{15}{24}$

ANALYSIS.—We find the least common multiple of the given denominators, which is 24.— This must be the least common denominator to which the fractions can be reduced. We then divide this least common multiple, 24, by the denominator of the given fraction, and multiplying each term of that fraction by the

quotient, (126,) we have the answer. Hence the

RULE. I. Find the least common multiple of the given denominators, for the least common denominator

II. Divide this common denominator by each of the given denominators, and multiply each numerator by the corresponding quotient. The products will be the new numerators.

Note. 1. Mixed numbers must first be reduced to improper fractions.

2. If the several fractions are not in their lowest terms, they should be reduced to their lowest terms before applying the rule.

Exercises for the Slate.

Reduce the following to their least common denominator.

1.	$\frac{2}{25}, \frac{3}{10}, \frac{47}{50}$ and $\frac{4}{75}$.	Ans. 12, 45, 141, 8
2.	$\frac{1}{2}, \frac{3}{4}, \frac{5}{6}, \frac{7}{8}, \frac{9}{20}, \text{ and } \frac{11}{12}$	60 00 100 105 54 110
	Ans.	120, 120, 120, 120, 120, 120
3.	$\frac{1}{2}, \frac{4}{7}, \frac{3}{16}, \text{ and } \frac{2}{21}$.	$\frac{168}{336}, \frac{192}{336}, \frac{63}{336}, \frac{82}{336}$
4.	$\frac{3}{7}, \frac{9}{14}, \frac{11}{28}$ and $5\frac{3}{7}$.	$\frac{12}{28}, \frac{18}{28}, \frac{11}{28}, \frac{15}{28}$
5.	4, 2, 1, 1, 1, and 1.	16 24 12 9 6 8

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 6. $7\frac{3}{4}, 5\frac{6}{11}, 7, and 8.$ $\frac{341}{44}, \frac{244}{44}, \frac{308}{44}, \frac{852}{44}$

 7. $\frac{25}{40}, \frac{25}{120}, and \frac{14}{64}.$ $\frac{60}{60}, \frac{20}{66}, \frac{21}{66}$

 8. $\frac{4}{15}, \frac{5}{75}, \frac{82}{56}, and \frac{4}{3}.$ $\frac{28}{105}, \frac{7}{105}, \frac{60}{105}, \frac{216}{105}$

 9. $1\frac{1}{2}, 2\frac{1}{3}, 3\frac{1}{4}, 5\frac{1}{6}, and \frac{7}{9}.$ $\frac{54}{86}, \frac{84}{86}, \frac{117}{36}, \frac{186}{366}, \frac{28}{66}$

 10. $\frac{4}{17}, 7\frac{1}{2}, \frac{29}{33}$ and 5.
 $\frac{24}{244}, \frac{40}{44}, \frac{414}{44}, \frac{4$

EXAMPLE.—Reduce $\frac{5}{6}$ of $\frac{3}{7}$ to a simple fraction.

EXPLANATION.—To take $\frac{1}{6}$ of $\frac{3}{7}$ we divide by 6, that is we multiply the denominator 7 by 6, and obtain $\frac{3}{42}$; and if $\frac{3}{42}$ is $\frac{1}{4}$, $\frac{5}{6}$ will be 5 times $\frac{3}{42}$; that is $\frac{3}{42} \times 5 = \frac{15}{42}$. We see from this operation that we have multiplied the 7 by 6 and the 3 by 5, thus $\frac{5 \times 3}{6 \times 7} = \frac{15}{42} = \frac{5}{14}$. Hence we have the following—

RULE. — Multiply the numerators together for the numerator, and the denominators for the denominator.

Note.-The work is shortened by cancelling all factors common to both numerator and denominator before multiplying, thus

$$\frac{2}{6}$$
 of $\frac{2}{7} = \frac{2}{2}$ of $\frac{1}{7} = \frac{5}{14}$.

Exercises.

1.	Reduce $\frac{3}{11}$ of $\frac{13}{16}$ to a simple fraction.	Ans 117
2.	Reduce 1 of 3 of 5 to 2 simple function	176
9	Poduce 7 . C. 5 C. c. a simple traction.	Ans. $\frac{5}{48}$
0.	Reduce $\frac{1}{16}$ of $\frac{3}{14}$ of $\frac{8}{10}$ to a simple fraction.	Ans. 1
4.	Reduce 5 of 3 of 9 to a simple fraction	Ang. 013
5.	Reduce 4 of 21 of 5 to a state 1 of at	Ans. 218
0	Reduce $\frac{1}{6}$ of $\frac{3}{2}$ of $\frac{3}{6}$ to a simple fraction.	Ans. $1\frac{2}{3}$
6.	Keduce $\frac{1}{3}$ of $4\frac{1}{5}$ of 5 to a simple fraction.	Ang 7
7.	What part of a vd is 1 of 1 of 1 and 2	4110. 1
0	What C is $\frac{1}{5}$ or $\frac{1}{8}$ or $\frac{1}{9}$ yr $\frac{1}{7}$	Ans. $\frac{1}{40}$ yd.
0.	what fraction of 1 cwt. is $\frac{2}{5}$ of $\frac{1}{5}$ of $\frac{4}{5}$ cwt. ?	
	An	S8_ owt
To	reduce a complex function to a i 1 c	135 CWL.
Ū	raction to a simple fraction	

EXAMPLE.—Reduce $\frac{3\frac{1}{4}}{5\frac{2}{3}}$ to a simple fraction.

EXPLANATION.—To reduce the fraction to a simple one we have to get rid of the fractional part in the numerator and denominator. This can be done by multiplying the terms of the fraction by the least common multiple of the denominators of the fraction parts, thus $\frac{3\frac{1}{4} \times 12}{5\frac{2}{3} \times 12} = \frac{39}{68}$ Ans.

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ADDITION OF FRACTIONS.

2nd	EXAMPLE	educe $\frac{\frac{1}{3}}{\frac{3}{3}}$	to a	a simple	fraction.	
-----	---------	---	------	----------	-----------	--

EXPLANATION.—The least common multiple of the denomnators 5 and 4 is 20. Multiply the terms by 20, thus $\frac{4}{5} = \frac{4}{5} \times 20$ = 16 = 1.1 Unuse the

	_	-	-		 41	1 ==	1 7	2.	llence	the
84		814	\times	20	1	5	- 1	9		

RULE.-Multiply the terms of the fraction by the least common multiple of the denominators of the fractional parts.

Exercises.

1. Reduce $\frac{4\frac{1}{2}}{2\frac{1}{4}}$ to a simple fraction.	Ans. 2
---	--------

2. Reduce $\frac{11\frac{3}{7}}{\frac{4}{7}}$ to a simple fraction. Ans. 20

3.	Reduce $\frac{\frac{1}{2} \text{ of } \frac{3}{4}}{\frac{1}{4} \text{ of } \frac{5}{4}}$	to a simple fraction.	Aus. $3\frac{3}{20}$
3.	Reduce $\frac{1}{\frac{1}{6}}$ of $\frac{5}{7}$	to a simple fraction.	Aus. 3

NOTE.—Reduce the compound fraction to a simple one before applying the rule.

4.—Reduce
$$\frac{\frac{2}{5} \text{ of } \frac{6}{6}}{\frac{2}{9} \text{ of } 4\frac{1}{2}}$$
 to a simple fraction. Ans. $\frac{1}{2}$

5. Reduce
$$\frac{1524}{15\frac{3}{4}}$$
 to a simple fraction. Ans. $\frac{1}{27}$

6. Reduce $\frac{17}{18\frac{1}{2}}$ to a simple fraction. Ans. $\frac{34}{37}$

NOTE.—Complex fractions are sometimes reduced to simple fractions by means of division of fractions. The above method will generally be found more convenient.

ADDITION OF FRACTIONS.

CASE I.

134. To add fractions having a common denominator. EXAMPLE.—What is the sum of $\frac{1}{9}$, $\frac{2}{9}$, $\frac{3}{9}$ and $\frac{7}{9}$?

OPERATION. ANALYSIS.—Since $\frac{1}{9} + \frac{2}{9} + \frac{3}{9} + \frac{7}{9} = \frac{13}{9} = 1\frac{4}{9}$, Ans. the given fractions have a common denominator, 9, their sum may be found by adding their numerators, 1, 2, 3, and 7, and placing the sum, 13, over the common denominator. We thus obtain $\frac{13}{9} = 1\frac{4}{9}$, the required sum. Hence the RU com

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 $\frac{4}{5} = 36$ $\frac{1}{6} = 35$

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Ac

ADDITION OF FRACTIONS.

RULE. Add the numerators, and place the sum over the common denominator.

Exercises for the Slate.

2. Add 5 8 4 7 and 10.	Ans. 34
3. Add $\frac{12}{12}$, $\frac{3}{12}$, $\frac{7}{12}$, $\frac{9}{12}$, and $\frac{1}{12}$.	21
4. Find the sum of $\frac{5}{27}$, $\frac{7}{77}$, $\frac{11}{23}$ and $\frac{21}{21}$	225
5. Find the sum of $\frac{13}{225}$, $\frac{76}{225}$, $\frac{101}{225}$ and $\frac{125}{225}$.	18

CASE II.

18. To add fractions having different denominators.

EXAMPLE.—What is the sum of $\frac{4}{5}$ and $\frac{7}{9}$?

FIRST OPERATION. $\frac{4}{5} + \frac{7}{9} = \frac{86}{45} + \frac{35}{45} = \frac{71}{45} = 1\frac{26}{45}$ Ans. bers only, or those of the same unit value; so in fractions we can add like numerators when they have a common denominator, but not otherwise. As $\frac{4}{5}$ and $\frac{7}{9}$ have not a common denominator, we first reduce them to a common denominator, (132 or 133) and then add the numerators, 36 + 35 = 71, the same as whole numbers, and place the sum over the common denominator.

4 - 20)
$\frac{5}{5} = \frac{36}{35} $ 45 L. C. M.
71 - 126 4
45 = 148 Ans.

A 7 1

ANALYSIS.—Since it is easier to perform addition when the numbers are in columns, we therefore place the new numerators as in addition of simple numbers and write the common denominator at

the side. From the above examples we have the following

RULE. I. Reduce the fractions to a common or to their least common denominator. II. Add the numerator

II. Add the numerators, and place the sum over the common denominator.

Exercises for the Slate.

1.	Aug $\frac{1}{2}, \frac{1}{4}, \frac{1}{6}, \frac{1}{8}$ and $\frac{9}{10}$.	Ang 3108
2.	Add $\frac{3}{4}, \frac{1}{8}, \frac{2}{8}$ and $\frac{5}{10}$.	1115. 0120
3.	Add 42, 9, 7 and 1	1107
4.	Add 7, 11, 17, 23 and 26	$\frac{3}{4}$
5	Add $\frac{8}{29}$ 10 11 12 12	$4\frac{71}{108}$
	9, 10, 11, 12, 18, 14 and 18.	$6\frac{1}{3}\frac{4}{6}\frac{4}{0}\frac{0}{3}$

e denomthus

the least ractional

Ans. 2

Ans. 20

Aus. $3\frac{3}{20}$

one before

Ans. $\frac{1}{3}$

Ans. $\frac{1}{27}$

Ans. 34

mple fracethod will

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s.—Since fractions amon deeir nnmethe comrequired







SUBTRACTION OF FRACTIONS.

CASE III.

136. To add mixed numbers

EXAMPLE.-Add 31, 53, and 77.

OPERATION.	ANALYSIS.—The sum of the
$3\frac{1}{2} = 3\frac{8}{12}$	fractions, $\frac{1}{2}$, $\frac{8}{4}$, and $\frac{1}{16}$, is $1\frac{5}{16}$;
$5\frac{3}{2} = 5\frac{12}{2}$	the sum of the integers 3, 5,
$7\frac{4}{1} = 7\frac{16}{1}$	and 7, is 15: and the sum of
10 16	both fractions and integers is
	TT 11 C 11

15	18	 16 16	Ans.	$16\frac{5}{16}$.	Hence	the	followit	1g-
							-	-

RULE.—Add the fractions and integers separately, and then add their sums.

Exercises for the Slate.

1.	Add 51 31, 45 and 61.	Ans. $19\frac{1}{2}$
	Ind of og, ig and of.	2

2. Find the sum of $\frac{7}{8}$, $1\frac{7}{12}$, $10\frac{5}{6}$, and 5.

3. Find the sum of 126¹/₄, 183⁶/₈, and 196⁸/₁₆. 505¹/₁₆

4. What is the sum of $3\frac{1}{7}$, $126\frac{1}{8}$, and $144\frac{5}{28}$. $273\frac{2}{66}$

5. Bought 5 lots of land containing $12\frac{7}{8}$ acres, $105\frac{9}{10}$ acres, $18\frac{1}{4}$ acres, $15\frac{11}{12}$ acres, and $5\frac{1}{6}$ acres; how many acres are in the 5 lots? Ans. $158\frac{13}{120}$

6. A grain merchant bought $126\frac{3}{4}$ bushels of wheat for $136\frac{9}{10}$ dollars, $367\frac{1}{4}$ bushels of barley for $219\frac{3}{4}$ dollars, $506\frac{1}{4}$ bushels of oats for $236\frac{3}{16}$ dollars; how many bushels of grain lid he buy, and how much did he pay for the whole?

Ans. $\begin{cases} 1000\frac{1}{12} \text{ bushels.} \\ 592\frac{67}{80} \text{ dollars.} \end{cases}$

1824

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SUBTRACTION OF FRACTIONS.

CASE 1.

137. To subtract fractions having a common denominator. EXAMPLE.—From $\frac{7}{10}$ take $\frac{8}{10}$.

OPERATION. $r_{\overline{0}} - rac{3}{10} = rac{7-3}{10} = rac{4}{10} = rac{2}{10}$ ANALVSIS.— Since the given fractions have a common denominator, 10, we find

the difference by subtracting 3, the less numerator, from 7, the greater, and write the remainder, 4, over the common denominator, 10. We thus obtain $\frac{4}{10} = \frac{2}{5}$, the required difference. Hence the following—

RULE Subtract the numerator of the subtrahend from the numerator of the minuend, and place the difference over the common denominator.

Exercises for the Slate.

F.	From z take z	Ang 2
2.	From 18 take 35.	ALIS. 3
3.	From 15 take 181.	13
4.	From 16.81 take 154	17
5.	From 75 take 47	168
6.	From 182 take 110.	7 262
	010	20

CASE II.

139. To subtract fractions having different denominators.

EXAMPLE .- From & take 3.

OPERATION. $-\frac{3}{7} = \frac{35}{56} - \frac{24}{56} = \frac{35-24}{56} = \frac{11}{56}$, Ans.	
$\begin{cases} \frac{3}{2} = \frac{35}{24} \\ \frac{3}{2} = \frac{24}{24} \end{cases}$ 56 C. D.	
11/56, Ans.	8
067	

ANALYSIS.— As in whole numbers we subtract *like* numbers only, or those having the same unit value, so, we can subtract fractions only when they

have a common denominator. As $\frac{5}{8}$ and $\frac{3}{7}$ have not a common denominator, we first reduce them to a common denominator, and then subtract the less numerator, 24, from the greater numerator, 35, and write the difference, 11, over the common denominator, 56. We thus obtain $\frac{11}{56}$, the required difference. Hence the following—

RULE. Reduce the fractions to a common denominator and subtract as in the former rule.

Exercises for the Slate

1.	From ⁷ / ₈ take ⁵ / ₈ .	Ang 1
2.	From 19 take 5.	27
3.	From 184 take 4.	62 41
4.	From $\frac{35}{80}$ take $\frac{14}{14}$.	70
5.	From 18 take 31	475
	106	303

The sum of the ad $\frac{1}{16}$, is $1\frac{5}{16}$; integers 3, 5, 1 the sum of ad integers is e following—

parately, and

Ans. $19\frac{1}{24}$ $18\frac{1}{24}$ $505\frac{1}{16}$ $273\frac{2}{56}$

, $105\frac{9}{16}$ acres, any acres are Ans. $158\frac{18}{126}$ cf wheat for lollars, $506\frac{1}{12}$ shels of grain whole ? $900\frac{1}{2}$ bushels. $592\frac{67}{80}$ dollars.

denominator.

.-- Since the have a comor, 10, we find

erator, from 7, the common e required dif-

CASE III.

139, To subtract mixed numbers.

EXAMPLE.-What is the difference between 184 and 71.

OPE	RATION.
$18\frac{1}{4} =$	= 18 3
73=	$= 7\frac{4}{12}$
	1011

ANALYSIS.—We first reduce the fractional parts, $\frac{1}{4}$ and $\frac{1}{3}$, to a common denominator, 12. Since we cannot take $\frac{1}{12}$ from $\frac{3}{12}$, we add $1 = \frac{1}{12}$ to $\frac{3}{12}$, which makes $\frac{1}{12}$, and $\frac{1}{12}$ from $\frac{15}{12}$ leaves $\frac{1}{12}$. Having taken 1 from the

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to

6

12

43

18 there remain 17, from which the 7 in the subtrahend is taken away, leaving 10. We thus obtain $10\frac{11}{12}$ the difference required.—Hence the following—

RULE.—Reduce the fractional parts to a common denominator, and then subtract the fractional and integral parts separately. Or,

We may reduce the mixed numbers to improper fractions, and subtract the less from the greater by the usual method.

Exercises for the Slate.

i .	From $8\frac{1}{4}$ take $5\frac{1}{8}$.	Ans. 31
2.	From $27\frac{5}{6}$ take $19\frac{7}{10}$.	8.2
3.	From $5\frac{1}{2}$ take $4\frac{3}{4}$.	1 8 <u>3</u>
4.	From 27 take 181.	· 88
5.	From 317 take 1,487.	$2\frac{167}{167}$
6.	From a barrel of Kerosene oil	containing 561 gallons
$\frac{1}{4}g$	allons were drawn; how many g	callons remained?

7. If flour, which cost $6\frac{7}{8}$ per barrel, be sold for $7\frac{3}{4}$ per barrel, what will be the gain per barrel? Ans. $5\frac{7}{4}$

8. From the sum of $5\frac{1}{4}$, $3\frac{1}{8}$ and $8\frac{1}{16}$ take the sum of $2\frac{1}{8}$, $7\frac{7}{9}$ and $\frac{13}{27}$. Ans. $6\frac{23}{482}$

9. What fraction added to $\frac{13}{14}$ will make $\frac{19}{26}$? Ans. $\frac{3}{140}$ 10. A man having $368\frac{1}{5}$ dollars, paid $$100\frac{7}{10}$ for a horse, $$25\frac{1}{4}$ for a set of harness, $$\frac{3}{16}$ for a whip, and $$175\frac{7}{12}$ for a waggon; how much had he left? Ans. $$66\frac{97}{240}$

 $\mathbf{2}^{\prime}$

MULTIPLICATION OF FRACTIONS.

MULTIPLICATION OF FRACTIONS.

CASE I.

140. To multiply a fraction by an integer.

EXAMPLE 1.—If 1 yard of cloth cost \pounds_4^3 , how much will 7 yds. cost?

OPERATION ANALYSIS .- Since 1 yd. cost 3 $\frac{3}{4} \times 7 = \frac{21}{4} = 5\frac{1}{4}$ Ans. fourths of one pound, 7 yds. will cost 7 times 3 fourths of one pound,

or 21 fourths, equal to £51.

A fraction is multiplied by multiplying its numerator (123.)

EXAMPLE 2.—If 1 pound of Tea cost $\frac{9}{20}$ of a dollar, how much will 4 lbs. cost?

9 7Ø 5	×	4 =	$\frac{9}{5}$	$=1\frac{4}{5}$	Ans.
0					

ANALYSIS.—Since 4, the multiplier, is a factor of 20, the denominator, of the multiplicand, we perform the multiplication by dividing

the denotainator, 20, by the multiplier, 4, and we have $\frac{9}{5} = 1\frac{4}{5}$ dollars.

A fraction is multiplied by dividing its denominator, (126). Hence the following-

RULE. Multiply the numerator of the fraction by the whole number, and write the product over the denomina-tor. Or,

Divide the denominator by the whole number, when this can be done without a remainder.

Exercises for the Slate.

1.	Multiply 5 by 6	
2.	Multiply 11 by 0	Ans. 37
3.	Multiply 8 has 5	81
4	Multiply 15 by 5.	22
5	$\frac{Multiply}{21} \xrightarrow{21} y 84.$	16
0.	multiply 2'5 by 55.	154
6.	Multiply 64 by 7.	493
	OPERATION.	ANALVER, In multi
64	Or,	nlying a mined
7	61 = 25	prying a mixed number,
	$25 \times 7 - 175 - 493$	we first multiply the frac-
13	$4 \land - \frac{4}{4} - \frac{434}{4}$	tional part, and then the
-4 9		integer, and add the two
4		products, or we reduce
		the mixed number to an
54		improner fraction - 1
		then multiple in and
	4	then multiply it.
	-	

1 and 71. educe the a common ve cannot $= \frac{12}{12} to$ 4 from 15 1 from the trahend is difference

n denomgral parts

fractions, 1 method.

Ans. 31 $8\frac{2}{15}$ 34 88 $2\frac{167}{750}$ 61/8 gallons red ? Ans. 287 r \$73 per Ans. \$7 sum of $2\frac{1}{8}$, Ans. $6\frac{23}{432}$ Ans. 140 r a horse, $5\frac{7}{12}$ for a s. \$66-97

4

MULTIPLICATION OF FRACTIONS.

7.	Multiply 171 by 5.	- Ans. 85
8.	Multiply $\frac{31}{10}$ by 7.	1,90
9.	Multiply 165 by 16.	266
10.	Multiply 181 by 544.	404
11.	If 1 ton of hay cost \$838, what will	12 tons cost?
	. 10,	Ans. \$1058

12. What will 14 yds. of silk cost at 17/8 dollars per yard? Ans. \$264

CASE II.

141. To multiply a whole number by a fraction.

EXAMPLE.—At 83 dollars an acre, how much will $\frac{3}{5}$ of an acre cost?

OPERATION. 83 price of 1 acro. 3

 $5)249 \equiv cost of 3 acres.$

494 == " ³/₄ of an acre.

ANALYSIS. — Multiplying the price of 1 acre by 3, we have the price of 3 acres; and as $\frac{1}{5}$ of 3 acres is the same as $\frac{3}{5}$ of 1 acre, we divide the cost of 3 acres by 5, and we have the cost of $\frac{3}{5}$ of an acre.—

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t

CC

Hence the following-

RULE. Multiply the given number by the numerator and divide the product by the denominator.

NOTE.—When the denominator is exactly contained in the given number, it will be found easier to first divide by it, and then multiply the quotient by the numerator.

Exercises for the Slate.

1.	Multiply 4 by 5.	Ans. 22
2.	Multiply 165 by 4.	2 Ů
3.	Multiply 457 by $\frac{7}{12}$.	266_{72}
4.	What is $\frac{11}{128}$ of 4261.	366-25
5.	What is $\frac{7}{12}$ of 1644.	95 9
6.	Multiply 26 by 53.	
	OPERATION.	ANALYSIS We
26	Or $5\frac{3}{8} = \frac{43}{8}$	multiply by the inte-
58	$26 \times \frac{43}{5} = \frac{1118}{5}$	ger and fraction se-

Ans.

5 <u>8</u>	26	43 =
		139
03 8 of 96		

 $\frac{54}{120} = \frac{120}{20}$

1393, Ans.

ANALYSIS. — We multiply by the integer and fraction separately, and add the products; or reduce the mixed number to an improper fraction, and then multiply

by it.

MULTIPLICATION OF FRACTIONS.

Ans. 857 1-20 266404 cost? ns. \$105% per yard? Ans. \$26

vill $\frac{3}{2}$ of an

- Multiply-1 acre by price of 3 of 3 acres of 1 acre, cost of 3 we have an acre.-

umerator

n the given then multi-

sis.-We y the inteaction send add the or reduce number to er fraction, multiply

7. Multiply 83 by 74. Multiply 45 by 81. 8.

9. Multiply 156 by 35.

10. If a man walk 16 miles in one day, how many will he travel in 1123 days? Ans. 1798 11.

At 18 dollars per ton, what is the cost of 187 tons of hay? Ans. \$338

CASE III.

142. To multiply a fraction by a fraction.

EXAMPLE 1.—At $\frac{3}{8}$ of a dollar per yard, how much will $\frac{3}{4}$ of a yard cost?

				-
8		1	V	8
0 0	-	T.	A	R
82				0

and $\frac{3}{32} \times 3 = \frac{9}{32}$ Ans.

ANALYSIS .- Since 1 yard cost $\frac{3}{8}$ of a dollar, $\frac{1}{4}$ of a yard will cost $\frac{3}{4}$ of $\frac{3}{8}$, which is $\frac{3}{32}$ of a dollar; and as $\frac{1}{4}$ of a yard costs $\frac{3}{32}$ of a

times as much, or $\frac{3}{32} \times 3 = \frac{3}{32}$. It will readily be seen that we have multiplied together the two numerators, 3 and 3, for a new numerator, and the two denominators, 8 and 4, for a new denominator, as shown in the whole work of the operation. Hence for multiplication of fractions we have this general

RULE. I. Reduce all integers and mixed numbers to improper fractions.

II. Multiply together the numerators for a new numera-tor, and the denominators for a new denominator.

Note.-Cancel all factors common to numerators and denominators.

Exercises for the Slate.

τ.	Multiply 3 by 3.	Ang 6 - 1
2.	Multiply 5 by 17	Ans. 12 = 2
3.	Multiply \$8 by 100	16
4	Multiply + of 75 by 2 of 98	186 475
5	Multiply 4 of 103 by 2 of 91	700
6.	Multiply 7 of 9 of 90 h. of	$47\frac{3}{10}$
7.	At 8 of a dellar a	401§
ost?	it is of a donar per pound, what	will § of a pound
8.	What cost 1951 111 as	Ans. $\frac{1}{3}$ of a doll.
.	that cost 1203 DDIs. of flour at \$73	per bbl. ?

Ans. \$9725

99

375

108

Ans. 5974

9. If a man travels 40³/₆ miles per day, how far will he travel in 135¹/₂ days? Ans. 5501³/₅ miles.

10. Bought 1264 barrels of flour at \$78 per barrel; and sold 584 barrels at \$78 per barrel, and the balance at $\$8_{16}^{1}$ per barrel; how much was the gain? Ans. \$6148

DIVISION OF FRACTIONS.

CASE I.

143. To divide a fraction by a whole number.

EXAMPLE.—If 4 yards of cotton cost § of a dollar, what will 1 yard cost?

OPERATION.ANALYSIS.— If 4 yards cost \$, 1
yard will cost 1 fourth of \$, or \$ divided $\$ \div 4 = \frac{2}{9}$. Ans.yard will cost 1 fourth of \$, or \$ divideded by 4.Since a fraction is divided

by dividing its numerator (126), we divide the numerator of the fraction, $\frac{8}{9}$, by 4, and we have $\frac{2}{9}$, the answer

EXAMPLE 2.—If 5 bushels of apples cost $\frac{11}{12}$ of a pound, what will 1 bushel cost?

OPERATION. $\frac{11}{12} \div 5 = \frac{11}{12 \times 5} = \frac{11}{60}$, Ans. ANALYSIS. — Here we cannot divide the numerator by 5 without leaving a

> in SI

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remainder; but since a fraction is divided by multiplying the denominator, (126), we multiply the denominator of the fraction, $\frac{11}{12}$, by 5, and we have $\frac{11}{60}$, the required result. Hence the following—

RULE. Divide the numerator by the whole number, when it can be done without leaving a remainder; but when this cannot be done, multiply the denominator by the whole number.

	Excreises for the Slate.	
1.	Divide $\frac{18}{28}$ by 9.	Ans. 2
2.	Divide ²⁴ / ₃₁ by 8.	8
3.	Divide $\frac{75}{125}$ by 25.	125
4.	Divide $\frac{64}{121}$ by 16.	T ⁴ 7
5.	Divide $\frac{13}{17}$ by 14.	13
6.	Divide $\frac{51}{72}$ by 6.	51
7.	At 18 dollars per ton, what part of a ton	of hay can be
boug	nt for \${ ?	Åns. $\frac{7}{144}$

DIVISION OF FRACTIONS.

far will he 01-8 miles. parrel; and nce at \$8,1,6 Ans. \$6118

lollar, what

cost \$\$, 1 , or § dividn is divided numerator er

of a pound,

-Here we he numerat leaving a tiplying the ator of the ired result.

le number, inder; but minator by

Ans. $\frac{2}{23}$ 31 125 121 $\frac{13}{238}$ 432 f hay can be Ans. 144

8. If 9 bushels of oats cost $7\frac{1}{8}$ dollars, how much will 1 bushel eost?

OPERATION. $7\frac{1}{8} = \frac{57}{8}$ $\frac{57}{8} \div 9 = \frac{57}{72} = \frac{19}{24}$, Ans.

NOTE .- We reduce the mixed number to an improper fraction and divide as before.

9. If 8 barrels of flour cost $126\frac{5}{8}$ dollars, how much will 1 barrel eost? OPERATION.

8)1265

ANALYSIS .- Here we first divide as in simple numbers, and we have a remainder of 65.

We reduce this to an improper fraction, $\frac{58}{8}$,

1558 which we divide (as in Ex. 1) and annex

the result, $\frac{53}{64}$, to the partial quotient, 15, and we have, $15\frac{53}{64}$, the required result.

10. If 126s dollars were paid for 4 cows, what was the price of each? Ans. 3119

11. If 22 horses eat $\frac{1}{8}$ of $1126\frac{1}{8}$ pounds of hay in a day how much does each horse consume? Ans. 6 561 pounds.

CASE II.

144. To divide a whole number by a fraction.

EXAMPLE.—How many pounds of tea at $\frac{3}{4}$ of a dollar can be purchased for 15 dollars? FIDET OF

TRST OPERATION.	ANALYSIS - As money new 1
15	of a d ll in the many pounds as 3
	of a dollar, the price of 1 pound in
4	contained times in 15 1 11 pould 18
	Contained times in 15 dollars. Whole
	numbers eannot be divided by C
3)60	because il
	because they are not of the same de
	nomination Dada
20 lbs Ame	formination. Reducing 15 dollars to
20 IDS. Ans.	fourths by multiplying by 4 1
	so family manufighing by 4, we have
60 6 7 00	ou jourins; and 3 fourths is contained
Jourths 20 times	the required must a contained
	, ac required mimber of nounda

in ther of pounds. SECION

DECOND OPERATIO	ON.
3)15	

5 4

ANALYSIS.—Here we divide the integer by the numerator of the fraction, and multiply the quotient by the denominator, which produces the same result. Hence the following-

20 pounds.

RULE. Multiply by the denominator and divide the product by the numerator.

DIVISION OF FRACTIONS.

		Exercises	for	the	Slate.	
1.	Divide	21 by 3.				Ans. 49
2.	Divide	63 by 7.				77
8,	Divide	316 by 9/25.				8777
4.	Divide	75 by §.				135
5.	Divide	120 by 103.				1173
6.	Divide	145 by 121.				1193
7.	Divide	5 of 320 by 5	of 9	1.		255
8.	Divide	1 of \$32 by 1	of 7	ł.		\$31

CASE III.

145. To divide a fraction by a fraction.

EXAMPLE.—At $\frac{2}{3}$ of a dollar per pound, how much tea can be bought for $\frac{4}{3}$ of a dollar?

OPERATION.	
$4 \times 3 = \frac{12}{3}$	
12 - 2 = 12 = 11 Ans.	

ANALYSIS.—As many pounds as $\frac{2}{3}$ of a dollar is contained times in $\frac{4}{5}$ of a dollar. 1 is contained in $\frac{4}{5}$, $\frac{4}{5}$ times, and $\frac{1}{3}$ is contained 3

times as many times as 1, or 3 times 4, which is $\frac{1}{2}$ times, which is the number of pounds that can be bought at $\frac{1}{3}$ of a dollar per pound; but $\frac{2}{3}$ is contained $\frac{1}{2}$ as many times as $\frac{1}{3}$, and $\frac{1}{2}$ divided by 2 gives $\frac{1}{16}$, equal to $1\frac{1}{5}$ times, or the number of pounds that can be bought at $\frac{2}{3}$ of a dollar per pound.

We see in the operation that we have multiplied the dividend by the denominator of the divisor, and divided the result by the numerator of the divisor. Hence for division of fractions we have this general

RULE. I. Reduce whole and mixed numbers to improper fractions.

II. Invert the terms of the Divisor, and proceed as in multiplication.

Notes.—1. The dividend and divisor may be reduced to a common denominator, and the numerator of the dividend be divided by the numerator of the divisor; this will give the same result as the rule.

2. Use cancellation where practicable.

Exercises for the Slate.

- 1. Divide 5 by 8.
- 2. Divide $\frac{5}{9}$ by $\frac{1}{6}$.
- 3. Divide $\frac{1}{3}$ by $\frac{7}{12}$.

Ans. $\frac{15}{16}$ $3\frac{1}{8}$ y(

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720
ABBUCTION OF DENOMINATE FRACTIONS. 1	0
4. Divide 47 by 84.	
5. Divide $\frac{1}{2}$ of $\frac{3}{2}$ of 6 by $\frac{2}{3}$ of 5	1
6. Divide $\frac{4}{9}$ of $\frac{4}{9}$ of $\frac{1}{9}$ by $\frac{1}{9}$ of $\frac{2}{9}$ of $\frac{2}{9}$ of $\frac{2}{9}$	1
7. How many times is 4 contained in 5.2	ň
8. How many times is $\frac{1}{2}$ of $\frac{3}{4}$ contained in $\frac{3}{7}$ of $2\frac{1}{2}$?	24
9. What is the quotient of $\frac{1}{5}$ of $\frac{5}{8}$ of 36 divided by 1 times $\frac{3}{8}$?	87 80
10. Divide $\frac{1}{3}$ by $\frac{21}{24}$ Ans. 23	4
11. At 18 ³ / ₄ cents a dozen, how many dozen of eggs car	4 n

12. A grocer sold $15\frac{1}{2}$ pounds of soda for $93\frac{3}{4}$ cents; how

13. If g of a yard cost g of a dollar, what will 1 yard cost?

14. How many times will $11\frac{1}{3}$ gallons of oil fill a can

nuch tea

y pounds ned times contained ntained 3 12 times, ought at as many 11 times, f a dollar

the divivided the r division

improper

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to a comdivided by sult as the

> Ans. $\frac{15}{16}$ 31

> > 4

REDUCTION OF DENOMINATE FRACTIONS.

A Denominate Fraction is a fraction whose 146. integral unit is one of a denomination of some compound number. Thus, § of an hour is a denominate fraction, the integral unit being one hour; so are $\frac{3}{5}$ of a mile, $\frac{2}{5}$ of a bushel, &c., denominate fractions.

CASE I.

147. To reduce a fraction of a higher denomination to an quivalent fraction of a lower denomination.

EXAMPLE.—Reduce \pounds_{720}^{2} to the fraction of a penny. £

OPERATION. $7\frac{2}{20} \times \frac{20}{1} \times \frac{1}{1^2} = \frac{480}{720} = \frac{2}{3}$ d. Ans. OR, 3 *60* 720 $3 | 2 = \frac{2}{3}$, Ans.

you buy for 874 cents?

much was that per pound?

which holds $\frac{1}{8}$ of $\frac{5}{6}$ of 2 gallons?

ANALYSIS .- To reduce pounds to pence, we must multiply by 20, and 12, the numbers in the table of money. And since the given number is a fraction of a pound, we indicate the process as in ,niul

Ans. 42 doz.

Ans. 63 cts.

Ans. \$11

Aus. 542

tiplication of fractions, and after cancelling, obtain ²/₃ the answer. Hence the following—

RULE. Multiply the fraction of the higher denomination by the numbers in the table, successively, between the given and required denominations.

Exercises for the Slate.

1. Reduce $\frac{1}{217}$ of 1 lb. avoirdupois to the fraction of an Ans. $\frac{1}{217}$ oz.

2. Reduce $\frac{25}{67}$ of a day to the fraction of an hour. Ans. $6\frac{75}{67}$ hours.

3. Reduce $\frac{6}{2784}$ of 1 mile to the fraction of a pole. Ans. $\frac{29}{28}$ pole.

4. Reduce $\frac{1}{80}$ of 1 bushel to the fraction of a pint. Ans. $\frac{4}{5}$ pt.

5. Reduce $\frac{1}{3}$ of $\frac{2}{5}$ of 1 pound, avoirdupois, to the fraction of an ounce. Ans. $\frac{3}{27}$ or $1\frac{5}{27}$ oz.

6. Reduce $\frac{2}{9}$ of $\frac{1}{8}$ of 2 pounds to the fraction of an ounce Troy. Ans. $\frac{2}{3}$ oz.

CASE II.

148. To reduce a fraction of a lower denomination to an equivalent of a higher denomination.

EXAMPLE.—Reduce $\frac{2}{3}$ of a penny to the fraction of £1.

	OPE	RATION	Γ.	
X	$\frac{1}{2} \times \frac{1}{20} =$	$=\frac{2}{720}=$	= 3 to £,	Ans.
3 ^ 12	2 ~ 20	720	360~,	

01	R, Ž	
6 12 20	/	
360	$1 = \frac{1}{380} \pounds$	Ans

ANALYSIS. — To reduce pence to pounds, we must divide by 12 and 20, the numbers in the table. And since the given number of pence is a fraction, we indicate the process, as in division of fractions, and cancelling, obtain $\frac{1}{860}$

the answer. Hence the following-

RULE. Divide the fraction of the lower denomination by the numbers in the table, successively, between the given and required denominations.

Exercises for the Slate.

1. Reduce $\frac{1}{6}$ of a foot to the fraction of a yard. Ans. $\frac{1}{18}$ yd.

REDUCTION OF DENOMINATE FRACTIONS. 105

N5.

tain 3 the

omination tween the

tion of an ns. $\frac{\beta_4}{217}$ oz. our. $6\frac{7}{4}$ hours. pole. pole. pole. pint. Ans. $\frac{4}{5}$ pt. the iration or $1\frac{5}{27}$ oz. of an ounce

Ans. 2 oz.

nation to an

on of £1.

s. — To reto pounds, deby 12 and abers in the l since the er of pence we indicate as in divictions, and obtain $\frac{1}{860}$,

nominaticn etween the

 $\frac{1}{18}$ yd.

2.	Reduce	Carrie	of	a	yard	to	the	fraction	of	a	mile.	

3. Reduce $\frac{3}{4}$ of a pound to the fraction of 1 cwt.

4. What part of a pound is $\frac{3}{2}$ of a dram?

Ans. 1280 lb.

- 5. What part of a bushel is \$ of a pint? Ans. 12 bus.
- 6. What fraction of a day is 678 hours? Ans. 24 days.

CASE III.

149. To find the value of a fraction in whole numbers of a lower denomination.

EXAMPLE. -- Find the value of $\frac{1}{27}$ of a cwt.

$\begin{array}{c} \text{OPERATION.} \\ \text{ewt. cwt. qrs. lbs.} \\ \text{9) } 17 (0 \ 2 \ 8\frac{18}{29} \\ \hline 4 \\ \hline 68 \\ 58 \\ \hline 10 \\ 25 \\ \hline 950 \end{array}$	ANALYSIS.—since $\frac{17}{29}$ cwt. is the same $3\frac{1}{29}$ of 17 cwt., we divide 17 cwt. by 29 as in division of com- pound numbers, (112,) and obtain for the answer 2 qrs. $8\frac{18}{29}$ lbs. Hence the following—
250	
232	
18	

RULE. Consider the numerator of the given fraction as so many units of the given denomination, and divide by the denominator.

Exercises for the Slate.

Find the value of the following fractions.

1. 2.	a of a week.	Ans. 2 da. 15 h. 3 wk. 2 da. 8 h.
3. A	$\frac{1}{2}$ of $\frac{3}{4}$ of 4 cwt.	2 cwt. 2 qrs. 71/2 lbs.
4. 5.	\$ of an acre	2 cwt. 1 qr.
6.	$\frac{1}{2}$ of $\frac{3}{2}$ of \pounds 2.	$3 \text{ ro. } 13\frac{1}{3} \text{ po.}$
7.	3 of 33 acres.	1 ac. 1 ro. 20 po.
ð. 9	TT of 1+ of a pound, Apoth.	2 oz. 3 drs. 2 ser. 1668 grs.
0.	$\frac{1}{26}$ or a day.	16 h. 36 min. 55 5 sec.

CASE IV.

150. To reduce a compound number to a fraction of a higher denomination.

EXAMPLE.-What part of £2 is 6 shillings and 3 pence? OPERATION. ANALYS: 3.- To find what part

6s. 3d. = 75 pence. $\pounds 2 = 480$ pence. $\frac{75}{480} = \frac{5}{32}$ Åns.

one compound number is of another, they must be reduced to the same denomination. In 6s. 3d there are 75 pence, and in £2 there 480

pence. Since 1 penny is $\frac{1}{480}$ of £2, 75 pence is $\frac{75}{480} = \frac{5}{32}$ Hence the following rule : of £2.

RULE. I. Reduce both quantities to the lowest denomination contained in either.

II. Then place that quantity which is to be the fraction of the other as numerator, and the remaining quantity as denominator.

Exercises for the Slate.

Reduce $4\frac{2}{3}$ shillings to the fraction of a pound. 1.

Ans. ±3

7 yd.

igal.

W

an

- 2. Reduce 4s. 7d. to the fraction of £1.
- Reduce 9s. 74d. to the fraction of £7 12s. 6d. 3.
- $\pounds_{\overline{1220}}$ 4. What part of 1 lb. Troy is 16 dwt. 3 grs. ?

43 lb. Troy.

- 5. What part of 1 yd. is 2 ft. 4 in.?
- 6. What part of 2 po. 4 yd. is 11 feet?
- Reduce $\frac{4}{5}$ of 1 qt. to the fraction of 1 gal. 7.
- 8. Reduce $\frac{7}{8}$ of 1 hour to the fraction of a day. 192 day

What part of 10 bu. is 10 qts.? 9.

10. From a piece of land contain ng 4 ac. 2 ro. a farmer

took 1 ro. 15 po. for a garden; what part of the whole did he take? Ans. 11

11. What fraction of 1 lb. avoirdupois is 1 lb. troy ?

NOTE .-- See note on table of avoirdupois weight.

REDUCTION OF DECIMALS.

CASE I.

To reduce a decimal to a common fraction. 151.

OPERATION. $.125 = \frac{125}{1000} = \frac{1}{8}$

EXAMPLE.-Reduce .125 to its equivalent common fraction. ANALYSIS.—We omit the decimal point, supply the proper denominator. to the decimal, and then reduce the

REDUCTION OF DECIMALS.

raction of a

d 3 pence? I what part s of another, to the same Bd there are there 480 is $\frac{75}{480} = \frac{5}{32}$

est denomi-

he fraction quantity as

ind.

Ans. $\pounds \frac{7}{44}$ 6d. $\pounds \frac{1}{1220}$ 6d. $\pounds \frac{1}{1220}$ $\frac{3}{0}$ lb. Troy. $\frac{7}{9}$ yd. $\frac{1}{5}$ gal. $\frac{7}{192}$ day 5. a farmer

whole did Ans. 11 troy ?

n.

on fraction. the decimal enominator reduce the common fraction thus formed to its lowest terms. Hence the following-

RULE. Omit the decimal point, and supply the proper denominator.

Exercises for the Slate.

Reduce the following to common fractions-

1.	.1674	Ans8 87 7625	Ane 5
2.	.125	1 800375	ADS. 8
3.	.468		800
4.	.008	-1 - 10 - 0005	8
5.	.725	$\frac{125}{29}$ 11 1876	2000
6.	.9375	$\frac{40}{15}$ 12, 1005	2500
		16	2000

CASE VI.

152. To reduce a common fraction to a decimal.

EXAMPLE 1.-Reduce 5 to its equivalent decimal.

FIRST OPERATION. $\frac{5}{8} = \frac{5000}{8000} = \frac{625}{1000} = .625$, Ars. SECOND OPERATION. 8)5.000

.625

ANALYSIS.—We first annex the same number of ciphers to both terms of the fraction, this does not alter its value. We then divide both resulting terms by 8, the sig-

nificant figure of the denominator, to obtain the decimal denominator, 1000. Then the fraction is changed to the decimal form by omitting the denominator. If the intermediate steps be omitted, the true result may be obtained as in the second operation.

EXAMPLE 2.—Reduce $\frac{3}{32}$ to its equivalent decimal.

OPERATION. 32)3.00000

.09375, Ans.

ANALYSIS.—Dividing as in the former example, we obtain a quotient of 4 figures, 9375. But since we annexed 5 ciphers, there must be 5 places in the required decimal f hence we prefix one

cipher. From these illustrations we derive the following

RULE. I. Annex ciphers to the numerator and divide by the denominator.

II. Point off as many decimal places in the result as are equal to the number of ciphers annexed.

Note.--A common fraction can be reduced to an *exact* decimal when its lowest denominator contains only the prime factors 2 and 5, and not otherwise.

REDUCTION OF DECIMALS.

Exercises for the Slate.

Reduce the following fractional quantities to decimals-

1.	$\frac{1}{2}$	Ans5	6.	$\frac{17}{256}$	Ans06640625
2.	34	.75	7.	19	.1484375
3.	78	.875	8.	13	.203125
4.	816	.1875	9.	512	.009765625
5.	$\frac{15}{40}$.375	10.	128	.0234375
	11.	Reduce $\frac{1}{6}$ to a decimal		120	Ans. 0.1666 +
	12.	Reduce $\frac{41}{333}$ to a decim	ıal.		0.123123 +

NOTE. 1. The answers to the last two examples are called *repeating* decimals. The figure 6 in the 11th example, and the figures 123 in the 12th, are called *repetends*, because they are repeated, or occur in regular order. The sign + indicates that there is still a remainder.

2. A repetend has a point placed over the first and last figures to mark where it begins and ends.

CASE III.

158. To reduce a denominate decimal to whole numbers of lower denominations.

EXAMPLE.-Reduce £.675 to shillings and pence.

PERATION.	ANALYSIS.— We first multiply by
.675	20 to reduce the given number from
20	pounds to shillings, and the result is 13
	shillings and the decimal .500 of a
13,500	shilling. We then multiply this deci-
12	mal by 12 to reduce it to pence, and
	get 6 pence. Hence the answer is
6,000	13s. 6d.
\$0 12a 6d	

Ans. £0 13s. 6d.

BULE. I. Multiply the given decimal by that number in the table which will reduce it to the next lower denomination, and point off as in multiplication of decimals.

II. Proceed with the decimal part of the product in the same manner, until reduced to the required denominations. The integers on the left of the decimal point will be the answer required.

Exercises for the Slate.

Find the value of the following decimals.

 1. $\pounds.725.$ Ans. $\pounds 0$ 14s. 6d.

 2. .125 ewt.
 12 lb. 8 oz.

 3. .435 lbs. (avoir.)
 6 oz. $15\frac{9}{25}$ drs.

REDUCTION OF DECIMALS.

4.	.4826 gal.	1 qt. 1 pt. 3.4432 gi.
Э.	.845 hours.	50 min. 42 sec.
0. 7	.67 of a league.	2 m. 3 po. 1 yd. 3% in.
6.	.18875 of a long ton.	15 cwt. 3 qrs. 2 lb. 12.8 oz.
o. 0	.969625 of a mile.	7 fur. 29 po.
10	07 of 69 10	9 oz. 15 dwt. 18 grs.
11	$0.0701 \pm 2 10s.$	3s. 6d.
19	875 of £2 5- 01	1. $10s. 1\frac{1}{2}d.$
	.010 01 20 08. 6d.	£2 17s. 3 ³ d.

CASE IV.

154. To reduce a compound number to a decimal of a higher denomination.

EXAMPLE.- Reduce 3 qts. 1 pt. 3 gills to the decimal of a gallon.

ANALYSIS.—Since 4 gills make 1 pint, 2 pints make 1 quart, and 4 quarts 1 gal-

lon, there will be $\frac{1}{4}$ as many pints as gills, $\frac{1}{2}$ as many

quarts as pints, and 4 as

many gallons as quarts .--

Or we may reduce 3 qts.

1 pt. 3 gills to the fraction

of a gallon (as in 150),

and we have 31 of a gal-

lon, which reduced to a de-

cimal equals .96875. Hence

	OPERATION.
4	3.00
2	1.750
4	3.87500
	.96875 gal. Ans.
	OR,
ats.	nt. 3 mile - 21 m

3 qts.	1 pt.	3 gills	= 31	gills.
1 gal.			= 32	gills.
$\frac{8}{32} =$.9687	75 gal.	Ans.	0

the following-

RULE. I. Divide the lowest denominaton given by that number in the table which will reduce it to the next higher, and annex the quotient as a decimal to that higher.

II. Proceed in the same manner until the whole is reduced to the denominaton required. Or,

Reduce the given number to a fraction of the required denominaton (150), and reduce this fraction to a decimal.

Exercises for the Slate.

Reduce

1.	$\pounds 0$ 7s. 4 ⁴ / ₅ d. to the decimal of $\pounds 1$.	Ans. £.37
2.	10s. 03d. to the decimal of £1.	£ 508195
3.	3 pks. 1.12 qt. to the decimal of a bushel.	.785 bu

d *repeating* igures 123 d, or occur remainder. figures to

umbers of

е.

ltiply by aber from esult is 13 500 of a this decience, and answer is

umber in enomina-

ict in the ninations.

0 14s. 6d. 2 lb. 8 oz. $15\frac{9}{25}$ drs.

PROMISCUOUS EXERCISES.

	4.	10 oz. 13 dwt. 9 grs. to the decimal of 1	l lb. Troy.
		Ans	8890625 lb.
•	5.	2 oz. 13 dwt. to the decimal of 1 lb.	.22083 lb.
	6.	4 da. 18 hrs. to the decimal of 1 week.	.67857142 wk.
	7.	$2\frac{1}{8}$ inches to the decimal of $2\frac{1}{5}$ miles.	.000015 +
	8.	$3\frac{1}{2}$ acres to the decimal of $3\frac{1}{4}$ sq. yards.	5212.307692
*	9.	$\frac{5}{8}$ of a crown to the decimal of 21s.	.148809523

NOTE.—After working the preceding exercises, require the pupil to reduce the sterling money on page 55 to Canada currency, at the rate of \$4 863.

PROMISCUOUS EXERCISES IN THE PRECEDING RULES.

1. Reduce $\frac{1}{3}$, $\frac{1}{4}$, $\frac{1}{5}$ and 6 to fractions having a common denominator. Ans. $\frac{20}{60}$, $\frac{15}{60}$, $\frac{10}{60}$, $\frac{369}{60}$

- 2. What is the value of .75 of a yd? Ans. 3 qr.
- 3. Add 41, 31, 51, 8 of 31, and 11. Ans. 1581.
- 4. What number multiplied by § will produce 114111? Ans. 30431

5. If the dividend be $\frac{3}{4}$ and the quotient $\frac{1}{8}$, what is the divisor? Ans. 6

6. If $\frac{3}{10}$ of a barrel of flour cost \$2.34, what will be the cost of a whole barrel. Ans. \$7.80

7. If the smaller of two fractions be $\frac{24}{91}$, and their difference $\frac{7}{93}$, what is the greater? Ans. $\frac{79}{93}$

8. Find the difference between $\frac{3}{2}$ of $6\frac{7}{10}$ and $\frac{5}{2}$ of $4\frac{8}{15}$. Ans. $1\frac{1}{13\frac{25}{5}}$

9. Reduce $\frac{4}{\frac{1}{6}}$ and $\frac{2\frac{1}{3}}{1\frac{1}{4}}$ to their simplest form.

Ans. 24 and 118

10. Find the difference between $\frac{3}{4}$ of $5\frac{1}{5}$ and $\frac{1}{8}$ of $2\frac{3}{4}$. Ans. $3\frac{89}{166}$

11. Reduce $\frac{2}{3}$ of 13s. 6d. to the decimal of £1.

12. Reduce 7 guineas to the decimal of £5 10s. 11d. Ans. 1.3251 +

13. From the sum of $\frac{1}{4}$, $\frac{1}{6}$, $\frac{8}{8}$, and $3\frac{1}{4}$ take the sum of $\frac{1}{6}$, $\frac{1}{7}$, $\frac{1}{6}$, and $\frac{1}{6}$ of $\frac{5}{8}$ and multiply the difference by $\frac{1}{5}$ of $3\frac{1}{2}$.

14. Change 5 to an equivalent fraction having 91 for its denominator. Ans. $\frac{2\frac{3}{2}\frac{3}{2}}{5}$

Ans. £.45

PROMISCUOUS BXERCISES

Troy. 3890625 lb. .22083 lb. 857142 wk. .000015 + 212.307692 .148809523

re the pupil ency, at the

G RULES.

a common 5, 12, 360 Ans. 3 qr. Ans. 1521 114114 Ans. 30431 hat is the Ans. 6 vill be the Ans. \$7.80 heir differ-Ans. $\frac{79}{93}$ of 4_{15}^{8} . Ans. $1\frac{23}{25}$

4 and 118 of 23. Ans. 389

Ans. £.45 11d. 1.3251 +im of $\frac{1}{5}, \frac{1}{7}, \frac{1}{$

Ans. 65

15. At $\frac{1}{3}$ of $3\frac{1}{2}$ dollars per bushel, how many bushels of apples can be bought for $\$6\frac{1}{2}$? Ans. 14 $\frac{6}{4}$ bu. 16. A man owning $\frac{2}{3}$ of a factory sold $\frac{1}{3}$ of his share for $\$901\frac{1}{4}$; what was the whole value of the factory? 17. What number diminished by the difference between $\frac{3}{4}$ and $\frac{3}{5}$ of itself, leaves a remainder of 34? Ans. 4018. Find the sum of $\frac{2\frac{1}{5}}{5}$ of $7\frac{3}{4}$ and $1\frac{3}{4} \div 2\frac{1}{8}$. Ans. $4\frac{95}{134}$

19. Simplify $\left\{\frac{3}{4} + \frac{7}{4} \text{ of } 5\frac{1}{2}\right\} \times \left\{\frac{5}{4} + \frac{2}{3} + 3\frac{3}{4}\right\}$ Ans. $37\frac{5}{4}$

NOTE.-Each of the quantities within the brackets { { is first to be worked as indicated therein, before being multiplied together.

20. Simplify $\frac{4}{5}$ of $\frac{1}{2}$ — $\frac{2}{5}$ of $\frac{1}{17}$ + $\frac{2}{5}$ of $1\frac{12}{17}$. Ans. 1 21. If $57\frac{1}{4}$ will buy $3\frac{1}{4}$ cords of wood, how many cords can be bought for $510\frac{1}{5}$? Ans. $4\frac{1}{5}\frac{1}{5}$ 22. What is the sum of $\frac{1}{5}$ of a vard $\frac{1}{5}$ of a foot and 1 of

22. What is the sum of $\frac{1}{7}$ of a yard, $\frac{1}{7}$ of a foot, and $\frac{1}{7}$ of a not, and $\frac{1}{7}$

23. If 3 tons of hay cost \$49, what will $7\frac{4}{11}$ tons cost? Ans. \$120.27

24. A man sold .15 of an estate to one person and then $\frac{15}{17}$ of the remainder to another person; what part of the estate did he still retain? Ans. §

25. Express $\frac{1}{2}(6\frac{1}{2}+2\frac{2}{3}-3)$ as a decimal. Ans. 3.083

26. Add together $\frac{3}{5}$ of a day, $\frac{2}{3}$ of an hour, and $\frac{4}{5}$ of 6 hours; and express the result as the decimal of a week.

Ans. .11825396

27. A man sold 1 ton of hay for \$12, and received $\frac{1}{2}$ the amount in sugar, at $\$\frac{1}{8}$ a pound, $\frac{1}{3}$ in money, and the remainder in molasses at $\$\frac{2}{5}$ a gallon; how many pounds of sugar, and how many gallons of molasses did he receive?

Ans. 48 lb. sugar.

5 gal. molasses.

28. A man gave $\frac{2}{3}$ of $1\frac{1}{5}$ times his ready money for a buggy, $\frac{3}{4}$ of what was left for a set of harness, and had \$12 remaining; what did he pay for the buggy? Ans. \$192

29. Express $\frac{3}{8}$ of a crown + $\frac{4}{5}$ of a shilling as a decimal of 7 shillings. Ans. .382142857

30. Reduce $\frac{21}{15000}$ of a year to the decimal of a day.

Ans. .511

PRACTICE.

EXAMPLE.—Find the price of 286 yards of cloth at £1 5s. $7\frac{1}{2}d$. per yard.

If we first find the price at £1, then at 5s., and at $7\frac{1}{2}d$., and add these three results, we shall have the price at £1 5s. $7\frac{1}{2}d$.

Now the price of 286 yards at £1 being £286, the price at 5s. will be $\frac{1}{4}$ of that, or £71 10s, ; and the price at 7 $\frac{1}{4}$ d. will be $\frac{1}{4}$ of the price at 5s., that is £8 18s. 9d. Adding these three results, we find the price at £1 5s. 7 $\frac{1}{4}$ d. to be £366 8s. 9d. The operation may be written thus :—

Price of	286	yards	at	£1	0	0	£2	286	0	0	
Price	66	66	66	0	5	0 1	11	71	10	0	
Price	66	"	66	0	Ō	$7\frac{1}{2}$	418	8	18	ŏ	

Price of 286 yards at £1 5 71 £366 8 9

The answer to this question might be found by compound multiplication: but the process is longer. The method of finding prices by aliquot parts is therefore commonly practised; hence it is called "Practice."

155. From the preceding operation we perceive that **Practice** is a short, or compendious, method of finding the value of any quantity, or number of articles, when the price of a unit of any denomination is given.

156. An Aliquot part of a quantity is such a part as, when taken a certain number of times will exactly make that quantity.

Preliminary Exercises.

1. Make a table of aliquot parts of a penny, a shilling, and a pound.

2. In the following list of aliquot parts name what part each is of another denomination. Thus--What is 3s. 4d.? One sixth of a \pounds .

3s. 4d., 2s. 6d., 10s., 2s., 3d., 4d., 6d., 1¹/₂d., 4d., 2s. 6d., 5s., 7¹/₂d., 2 cwt., 15 cwt.; 5 lbs., 2 qrs., 2 gals., 4 pks.

3. What part of

2s. is 8d. 10s. is 1s. 3d. 11s. is 11d.	1 £2 is 59
2s. 4d. " 4d. 5s. " 5d. 1s. " 140	1. +9 4 80
68. 8d. " 1s. 8d. 5s. 6d " 51d. 9s. 6d. " 91d	f9 4 10g
10s. "2s. 6d. 8s. 6d" 8id. 3d."	-fA (4 16a
7s. ". 7d. 1s. 3d" 5d. 9d." 41d	£1 46 60 90
8s. " 8d. 4s. "2s. 4d. 12s. 6d. "2s 6d	
10s. "3s. 4d. 13s. 6d" 31d. £1 "2s. 6d	£9 (119- C)
4s. " 8d. 3s. 4d" 8d. 10g "10 2d.	22 12S. 00.

loth at £1

t 71d., and E1 5s. 71d. ie price at t 7id. will ling these o be £366

0 0 0

9

compound nethod of only prac-

eive that f finding when the

h a part tly make

a shilling,

that part 3s. 4d. ?

. 6d., 5s.,

is 5s. " 8s. " 10s. " 16s. " 6s. 8a " 7s. 6d. " 12s. 6d. 66 83d

1

4. What	is the		
$\frac{1}{4} \text{ of } 8s.$ $\frac{1}{5} \text{ `` 10s.}$ $\frac{1}{4} \text{ `` 3s. 4d}$ $\frac{1}{4} \text{ `` 10s.}$ 5. Give the formula of the formula	$ \begin{array}{c c} \frac{1}{8} \text{ of } 16s. \\ \frac{1}{12} & 4s. \\ \frac{1}{2} & 7s. \\ \frac{3}{4} & \\ \begin{array}{c} \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \end{array} \\ \end{array} \\$	$\begin{array}{c c} \begin{array}{c} \frac{8}{4} \text{ of } \pounds 1 \\ \frac{8}{4} & 5 \\ 5 \\ \frac{1}{4} & 7 \\ \frac{1}{3} & 7 \\ \frac{2}{3} & \pounds 1 \end{array}$ ts for	$ \begin{array}{c} \frac{1}{3} \text{ of } \pounds 4 \\ \frac{1}{3} & \pounds 5 \\ \frac{1}{4} & \pounds 5 \\ \frac{1}{6} & \pounds 6 \end{array} $
12s. 14s. 13s. 9d. 15s. 6s. 3s. 9d. 3s.	6s. 3d. 12s. 6d. 17s. 6d. 18s. 2d. 8s. 4d. 7s. 4d. 12s. 8d.	$\begin{array}{c} 3s. \ 7\frac{1}{2}d.\\ 15s. \ 7\frac{1}{2}d.\\ 17s. \ 9d.\\ 16s. \ 3d.\\ 10s. \ 10d,\\ 0s. \ 5\frac{1}{2}d.\\ 0s. \ 5\frac{1}{2}d.\\ \end{array}$	1 ro. 4 po. 2 ro. 15 po. 3 ro. 39 po. 3 ro, 37½ po, 5 dwt. 9 grs. 3 drs. 5 grs.
14s. 12s. 2d.	14s. 8d. 5s. 2 ¹ / ₂ d.	$16s. \ 3\frac{1}{2}d.$ 1s. $1\frac{1}{2}d.$	2 qrs. 5 lbs. 6 fur. 15 po.

CASE I.

To find the value, when the given quantity is a simple 157. number, and the price less than 1 shilling.

EXAMPLE 1.—Calculate the price of 44 articles at 7d.

OPERATION.

44 at 1d. = 3s. 8d. 44 at 7d, = 7 times 3s. 8d. = £1 5s. 8d.

OR, 6d. is $\frac{1}{2}$ of 1s. 44 at 7d. 1d. is 1/8 of 6d. $\mathbf{22}$ $0 \equiv$ price at 6d, 3 $8 \equiv$ price at 1d.

£1 5 8 \equiv price at 7d

From the above illustration we have the following-RULE. — Find the price at 1 penny, and multiply by the pence in the price. Or, Find the price by means of aliquot parts.

Exercises for the Slate.

Calculate the value of the following articles.

	9 A	of 0.1	1			0		
T •	44	at su.	and	at 9d.	7.	196 of	10d and sta	1
9	90	11 17 1				140 au	i rou. and at 2	α.
<i></i>	90	··· 7a,	and	" 5d.	8	199 (6	111 and 11 +	
2	40	11 01			1 0.	100	11a and $1a$	d.
υ.	40	··· 8a.	and	" 4d.	9	997 66	0.1 - 1 11 0	1
4	00	11 101			0.	201	og. and " 3	d
±.	03	·• 10d.	and	" 20	1 10	197 44	0.1 . 1 // .	
E.	20	11 4 4 3			1 10.	101	ou. and • 40	
J.	12	"IId.	and	6 14	1 1 1	109 11	71 1 11 -	
•	0.0		conte	T.C.	11.	400	7d. and " 5c	1.
э.	65	" 5d.	anti	66 7/1	10	000 11		
		· · u.	CUARCE	ru.	14.	209 .	- 5d. and 4 7c	1

	126 at 1d. = 10s. 6d. 126 at $7\frac{1}{2} = 7\frac{1}{4}$ times 10s. 6d - fo 10 6	-
	0 5 3 3 13 6	
	£3 18 9	
	OR, 126 at 7½d.	
	6d. is $\frac{1}{2}$ of 1s. $1\frac{1}{2}$ d, is $\frac{1}{4}$ of 6d. $15 9 \equiv \text{price at } 6d.$ $1\frac{1}{2}$ d.	
	$\pounds 3 \ 18 \ 9 = \text{price at } 7\frac{1}{2}\text{d.}$	
13.	48 at $7\frac{1}{2}d$, and at $4\frac{1}{2}d$. 19. 246 at $1\frac{3}{4}d$. and at 10.	d
15.	72 " $73d$ and " $41d$ 21 101 " $51d$ and " $84d$	d.
6.	$126 \text{ ``} 1\frac{1}{4}$ d. and $4\frac{1}{4}$ and $5\frac{1}{4}$ d.	d.
	$173 " 5\frac{3}{2}$ d. and " $6\frac{1}{2}$ d. 23 365 " 91d and " 44	a. J
7.		

158. To find the value when the given quantity is a simple number, and the price given in shillings.

EXAMPLE 1.-Find the price of 322 yds. at 6s. per yard.

OPERATION.

 $322 \text{ at } 1s. = \pounds 16 2s.$ 322 at 6s. = 6 times £16 2 = £96 12s.

OR, Multiplying by half the price and doubling the unit figure for shillings thus,

322 at 6s. 3

¥

£96 12 Ans. as before

EXAMPLE 2.-Find the price of 137 yards at 17 shillings per yard.

> OPERATION. 137 81 = 17 68 rem. = 1. 1096 twice 4 = 8.

£116 9 0 Answer. From the above we derive the following

RULE.—Multiply by half the number of shillings; double the units figure of the product for shillings and take the others as pounds.

Exercises for the Slate.

Find the value of

1.	126	\mathbf{at}	16s.	and	at	4s.	6.	384	at	4s.	and	ati	160
2.	132	"	15s.	and	""	5s.	7.	596	66	98.	and	66 1	110
3.	689	"	14s.	and	"	6s.	8.	1832	"	11s.	and	"	0.0
4.	128	"	18s.	and	66	2s.	9.	1596	"	12s.	and	"	80
5.	136	"	17s.	and	٤.	3s.	10.	1118	"	13s.	and	"	7s.
11. 12. 13. 13.	1896 at 1346" 1284"	16s 17s 3s	3. A 1. 1.	lns. £	E15 E11 £1	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	14. 15. 16.	48 at 186 " 327 "''	9s. 7s. 11s.		Ans.	£2] £6{ £179	1 12.

CASE III.

159. To find the value when the price consists of pounds and shillings.

EXAMPLE.—What is the cost of 187 tons at £6 11s. per ton OPERATION.

per yard.

is a simple

d at 101d. id "

d ..

d 14

d "

d "

83d.

63d.

44d.

27d.

58d. equent rules verify the

init figure

$65\frac{1}{2}$ = half the number of shillings in the price.

9,3 93,5 1122	remai: twice	nder 8		1 16
			-	
f1991 11	7 0			

187

17

Hence the

RULE. To the number of pounds annex half the number of shillings for a multiplier. Double the units figure of the product for shillings.

ach.

6

73

3

6

Exercises for the Slate.

Find the value of

$\begin{array}{c}(1) & 426\\(2) & 446\\(3) & 642\\(4) & 741\\(5) & 684\end{array}$	at £7 8s. and at "£4 3s. and " "£5 7s. and " "£6 9s. and " "£9 13s. and "	$\begin{array}{c} \pounds 2 \ 12s. \ (6) \ 563 \ a\\ \pounds 5 \ 17s. \ (7) \ 851 \ a\\ \pounds 4 \ 13s. \ (8) \ 754 \ a\\ \pounds 3 \ 11s. \ (9) \ 694 \ a\\ \pounds 0 \ 7s. \ (10) \ 339 \end{array}$	at £6 7s. and at £3 13s. "£8 13s. and "£1 7s. "£6 17s. and "£3 3s. "£4 15s. and "£5 5s. "£5 15s. and "£5 5s.
11.	183 at £2 13s.		Ans. £484 19s.
13.	486 " £8 18s.		£999 15s.
14.	596 " £9 19s.		\$23720.80

CASE IV.

To find the value of any number of articles, when the 160. price is given in shillings and pence, or in pounds, shillings and pence.

EXAMPLE 1.--If 1 yard cost 16s. 3d., what will 127 yards cost at the same rate?

OPERATION.

127 at 16s. 3d. per yard.

	103	3	9 - price at		16	3
5s. is $\frac{1}{2}$ of 10s. 1s. 3d. is $\frac{1}{2}$ of 5s	31	15	0 =	0	5	0
10s. is $\frac{1}{2}$ of £1	63	10	0 - price at	£A	10	^

EXAMPLE 2.—Find the price of 187 yards at £2 13s. 4d. per yard.

OPERATION.

187 at £2 13s. 4d. 2

374 $0 \equiv \text{price at } \pounds 2 = 0$ 0 0 per yard 10s. is 1 of £1 93 10 0 =" 0 10 0 3s. 4d. is 1 of 10s. 31 3 " 4 = -0 3 " 4 £498 13 4 = price at £2 13 4

From the foregoing we have the following

RULE.—Multiply the quantity by the pounds, if any, and take allquot parts for the shillings and pence.

Exercises for the Slate.

	at 3s. 9d. and at 16s 3d. " 3s. 4d. $\neg nd$ " 16s. 8d. " 18s. 4d. and " 1s. 8d. " 12s. 6d. and " 7s 6d. " 17s. 5d. and " 2s. 7d. " 11s. 7d. and " 8s. 5d. 2436 at 15s. 2739 at 10s. 10d. 4938 at 15s. $7\frac{1}{2}d.$ 9852 at 15s. 11 $\frac{1}{4}d.$ 3482 at 19s. 11 $\frac{1}{4}d.$ 9584 at 11s. $6\frac{2}{3}d.$ 7947 at 18s. $0\frac{1}{4}d.$ 543 at £1 8s. 8d. 296 at £2 13s. 4d.	$ \begin{array}{c} (7) 127 \text{ at } 58. 7\frac{1}{2} \text{ d. and at } 148. 4\frac{1}{2} \text{ d.} \\ (8) 295 `` 128. 2\frac{1}{2} \text{ d. and } `` 78. 9\frac{1}{2} \text{ d.} \\ (9) 987 `` 128. 1\frac{1}{2} \text{ d. and } `` 78. 10\frac{1}{2} \text{ d.} \\ (10) 1118 \text{ at } 148. 8\frac{1}{4} \text{ d. and } `` 78. 10\frac{1}{2} \text{ d.} \\ (11) 5639 `` 188. 4\frac{1}{2} \text{ d. and } `` 18. 7\frac{1}{2} \text{ d.} \\ (12) 3017 `` 168. 2\frac{3}{4} \text{ d. and } `` 18. 7\frac{1}{2} \text{ d.} \\ \hline \text{Ans. } \pounds 1827 \text{ 0s. 0d.} \\ \pounds 1483 128. 6\text{ d.} \\ \pounds 3857 168. 3\text{ d.} \\ \pounds 7850 168. 3\text{ d.} \\ \pounds 3471 28. 4\frac{1}{2} \text{ d.} \\ \pounds 5540 158. 0\text{ d.} \\ \pounds 778 68. 0\text{ d.} \\ \pounds 7789 68. 8\text{ d.} \\ \pounds 789 68. 8\text{ d.} \\ \end{array} $
7.07	CASI	E V.
1411		

161. To find the value of a compound quantity when the price of a unit of the quantity is given in dollars and cents. EXAMPLE 1.-Find the value of 126 cwt. 3 qrs. 14 lbs.

(long weight) at \$14.621 per cwt.

OPI	ERATION.
126 cwt. 3 qrs. 14 lbs. at \$1	4.625
	126
$\begin{array}{c} & & & \\ 2 \text{ qrs.} = \frac{1}{2} \text{ of } 1 \text{ cwt.} \\ 1 \text{ qr.} = \frac{1}{2} \text{ of } 2 \text{ qrs.} \\ 14 \text{ lbs.} = \frac{1}{2} \text{ of } 1 \text{ qr.} \end{array}$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$
\$.18 EXAMPLE 2.—What wi weight) of oatmeal cost, at 3	355.546875 = price of 126 cwt.,&c. ill 13 cwt. 2 qrs. 15 lbs. (short \$3.75 per cwt.?
OPE 13 cwt. 2 qrs. 15 lbs. at \$	RATION. 3.75 per 100 lbs. 13
$2 \text{ grs.} = \frac{1}{2} \text{ of } 1 \text{ cwt.}$	$\frac{1}{1.875} = \text{price of 13 cwt.}$

1.875 ==

.375 =

.1875 <u></u>

10 lbs. $= \frac{1}{5}$ of 2 qrs.

5 lbs. $= \frac{1}{2}$ of 10 lbs.

66

66

\$51.1875 = price of 13 ewt., &c.

2 qrs.

10 lbs.

5 lbt.

nd at £3 138. nd " £1 78. nd " £3 38. nd " £5 5s. ad " £4 5s. £484 19s. £999 15s. \$17301.60. \$23720.80

es, when the ds, shillings

l 127 yards

16 3

E2 13s. 4d.

per yard "

f any, and

OR, 13 cwt. 2 grs. 15 lbs. == 13.65 cwt. at \$3.75

3.75

68	25
955	5
095	

\$51.1875 = price as before.

FFEXAMPLE 3.—Find the price of 14 ac. 3 ro. 35 po. at \$22.16¹/₅ per acre.

OPERATION.

11

14 ac. 3 ro. 35 po. at \$22.162 per acre.

	310.268		price of 14 ac.
$2 \text{ ro.} = \frac{1}{2} \text{ of } 1 \text{ ac.}$	11.081	-	2 ro.
$1 \text{ ro.} = \frac{1}{2} \text{ of } 2 \text{ ro.}$	5.5405		1 ro.
20 pb. $= \frac{1}{2}$ of 1 ro.	2.77025		20 po.
10 po. = $\frac{1}{2}$ of 20 po.	1.385125		10 po.
5 po. $= \frac{1}{2}$ of 10 po.	.6925625	_	5 po.

\$331.7374375 == price of 14 ac., &c.

OR,

14 ac. 3 ro. 35 po. = $14_{3\frac{1}{2}}^{81}$ ac. = 14.96875 ac. at $\$22.16\frac{1}{5}$ 22.161

\$331.7374375 Ans. as before.

From these illustrations we deduce the following general

RULE. Multiply the price by the integral part of the quantity, then separate the remainder into aliquot parts of 1 of the quantity whose rate is given, or successively of each other, as the case may require. Or, which will often be found more convenient,

Reduce the quantity to a decimal of the same denomination as the quantity whose rate is given, and multiply as in decimals.

Exercises for the Slate.

as before. 0. 35 po. at

8.75

of 14 ac. 2 ro. 1 ro. 20 po. 10 po. 5 po.

f 14 ac., &c.

t \$22.161

as before.

ng general

part of the uot parts of essively of will often be

denominaltiply as in

	cwt.	grs.	Ibs. (long meight)	
1.	163	3	14 at \$15.20	Answers.
2.	115	2	17 at \$19 101	\$2490.90
3.	18	3	01 of \$14 101	\$1515.6166+
4	190	9	21 at @14.184.	\$268.581093
5	100	2	27 Rt 22 198. 6d.	£406 16s. 11d.
0.	10	3	24 1 at £5 15s. 5 1d.	£109 98. 8.46 +
0.	181	3	15 at £2 3s. 9d.	£397 188, 11d
7.	165	2	22 at \$4.374.	\$ 795 095
8.	172	3	18 at \$19.19	@ 9910 5007
9.	111	1	1 at \$4.334.	#JJJ10.J207
				482.03395
10	101	- ro - 9	. po.	
11	121	0	14 at #15.61.	1901.883375
11.	130	2	19 at £2 14s. 5 ¹ / ₄ d.	£371 178. 2127.
12.	183	1	381 at \$15.551.	\$2854 1961
	vds.	ors.	pls	\$2001.100T
13.	15	3	1 at \$9 10	#00.000 h
14.	16	2	3 of \$1 501	\$33.2061
15.	28	ã	91 04 01 4 101	\$75.5109-
	20	0	og at \$14.104.	\$408.5317-

RULES.

162. In calculating the price of

1. Hundreds, quarters and pounds, long weight, at £1 per cwt., multiply the pounds by 24 for pence, and the quarters by 5 for shillings.

2. Tons, hundreds and quarters, at £1 per ton, take the tons and hundreds as pounds and shillings, and multiply the quarters by 3 for pence.

3. Acres, roods and poles, at £1 per acre, multiply the poles by $1\frac{1}{2}$ for pence, and the roods by 5 for shillings.

4. Yards, quarters and nails, at £1 per yard, take each quarter at 5s. and each nail at 1s. 3d.

5. Oz., dwts. and grains, Troy weight, at £1 per ounce, take the ounces as pounds, the pennyweights as shillings, and half the grains as pence.

163. In calculating by means of aliquot parts, it will often be more convenient to use the decimal form of remainder instead of the common fractional. It will be sufficient to earry the decimals to two places, as in the following example.

EXAMPLE 3.—What will 126 ac. 3 ro. 15 po. cost at £2 11s. 3d. per acre?

126	3 5	15 at £2 11s. 3d. $1\frac{1}{2}$
£126	16	$10.50 = \text{price at } \pounds 1 \text{ per acre.}$
s. $= \frac{1}{2}$ of £1 3d. $= \frac{1}{8}$ of 10s. 7	$ \begin{array}{r} 13 \\ 8 \\ 18 \end{array} $	9.00 = price at £2 0 0 per acre 5.25 = " 0 10 0 " 6.66 = " 0 1 3 "
£325	0	8.91 = price at £2 11 3 per acre

Note.—In working by this method the^{*}penny is supposed to be divided into 100 equal parts. Hence .25d. = $\frac{1}{4}$, .50d. = $\frac{1}{2}$, .75d. = $\frac{3}{4}$

In valuing the decimal in the answer we consider to which of these it is nearest and value it accordingly.

App'v the above rules to such of the preceding exercises as can e solved by them.

164. The Unitary Method. --1. In the foregoing exercises on the Rules of Practice as well as in several of the promiscuous exercises following the Compound Rules, there are three things or terms given. Of the three terms given two are always of the same kind, and the remaining term is always of the same kind as the term required for the answer. For example: If 1 yd. cost \$4.25 what is the price of 46 yds. The two terms of the same kind here are 1 yd. and 46 yds., and the remaining term \$4.25 is of the same kind as the term required for the answer.

It is clear that since we have the price of 1 yd. we have only to multiply that price by the number of yards given to find the answer.

2. If 6 lbs. cost \$54 what will 16 lbs. cost? Here 6 lbs. and 16 lbs. are the two terms of the same kind and the remaining term \$54 is of the same kind as the term required for the answer. Though we have not in this example got the price of 1 lb. we can very readily find it by dividing \$54, the price of 6 yds., by 6, and if we multiply the price of 1 yd. by 16 we obtain the price of 16 yards.

We thus see that if in any question we have three terms

120

10 1s. po. cost at

per acre.

0 0 peracre 0 0 " 1 3 "

3 per acre

pposed to be $\frac{1}{2}$, .75d. = $\frac{3}{4}$

ch of these it

g exercises

foregoing eral of the ules, there erms given ng term is he answer. of 46 yds., s the term

. we have given to

6 lbs. and remaining he answer. f 1 lb. we of 6 yds., we obtain

ee terms

PRACTICE.

given with two of them of the same kind, and the remaining term of the same kind as the one required for the answer, we can reason from the given numbers to unity and from unity to the required result. Hence

The process of solving arithmetical questions by reasoning from the given numbers to unity and from unity to the required result is called *The Unitary Method*. (It is sometimes called *Analysis.*)

EXAMPLE 1.—If 8 yds cost \$48, what should be the price of 11 yds.? If 8 yds. cost \$48, 1 yd. will cost $\frac{1}{8}$ of \$48 which is \$6, and if 1 yd. cost \$6, 11 yds. will cost 11 times \$6=\$66 Ans.: or shortly $\frac{48}{5} \times 11$

Ans.; or shortly
$$\frac{48 \times 11}{8} =$$
\$66.

EXAMPLE 2.—If 16 cwt. cost \$54 what will 64 cwt. cost? If 16 cwt. cost \$54 1 cwt. will cost $\frac{1}{16}$ of $54 = \frac{54}{16} = 3\frac{3}{8}$; and if 1 cwt. cost $3\frac{3}{8}$, 64 cwt. will cost 64 times $3\frac{3}{8} = 216 ;

or shortly $\frac{54 \times \beta_{\star}^4}{\chi_{\beta}} = \$216.$

We see from the short method of this second example that it is sometimes more convenient to find how many times more one quantity will cost than another quantity. In this example 64 cwt. will cost 4 times more than 16 cwt.

EXAMPLE 3.—If $\frac{3}{4}$ lb. cost 36 cents what will 5 lbs. cost ? If $\frac{3}{4}$ lb. cost 36 cents $\frac{1}{4}$ will cost $\frac{1}{3}$ of 36 cents=12 cents, and $\frac{4}{4}$ lb. or 1 lb. will cost 4 times 12 cents = 48 cents, and if 1 lb. cost 48 cents 5 lbs. will cost $48 \times 5 = 2.40 ; or shortly $\frac{3}{4}$ lb. = 36 cents.

 $\frac{1}{4}$ lb. = 12 " $\frac{4}{4}$ or 1 lb. = 48 cents.

 $\therefore 5$ ib. = 48 $\times 5$ = \$2.40 Ans.

EXAMPLE 4.—If $\frac{17}{25}$ of a ton cost \$4.25 what will $1\frac{7}{25}$ tons cost? $\frac{17}{25}$ cost $$4\frac{1}{4}$... 1 ton will cost as many dollars as $\frac{17}{25}$ is contained times in $4\frac{1}{4}$ that is $4\frac{1}{4}$... $\frac{17}{25} = \frac{25}{4}$; and if 1 ton cost $$\frac{25}{4}$, $1\frac{7}{25}$ tons will cost $\frac{25}{4} \times 1\frac{7}{25} = \frac{25}{4} \times \frac{32}{5} = 8 .

EXERCISES.

1. If 19 lbs. of sugar cost \$1.52 what cost 25 lbs. Ans. \$2. 2. When 4 men can do a piece of work in 23 days in what time will 15 men do it ? Ans. $6\frac{1}{15}$ days.

PROPORTION.

3. If $\frac{1}{2}$ lb. of tea cost $22\frac{1}{2}$ cents what will 8 lbs. cost?

Ans. \$3.60. 4. If 25 lbs. of tea cost \$16, how many lbs. can be bought for \$56? Ans. 874 lbs.

5. How many lbs. of coffee can be bought for \$15, if 40 lbs. cost \$8? Ans. 75 lbs.

6. If $\frac{5}{8}$ of a yard cost \$4 what will 7 yards cost?

Ans. \$44.80.

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- 7. If ²/₈ cost 14 cents what will ⁵/₆ cost ? Ans. 17¹/₄ cents.
- 8. If \$16 buy 20 lbs. what quantity will \$40 buy?

Ans. 50 lbs.

Note.—The Unitary Method is the more natural and philosophical method of solving arithmetical questions, and is now generally practised when it is applicable. There are, however, certain classes of examples where the principles of Proportion are best applied.

PROPORTION.

ą

165. Ratio. When we compare two numbers of the same kind, the quotient which is obtained by dividing the first by the second is called the *ratio* of the first to the second; thus the ratio of 20 to 5 is 4, and the ratio of 9 to 36 is $\frac{9}{36}$ or $\frac{1}{4}$.

166. The Terms of a ratio are the two numbers compared, and when spoken of together are called a COUPLET.

167. Two dots are generally used to separate the terms of a ratio; thus the ratio of 20 to 5 is expressed by 20:5, and that of 9 to 36 by 9:36. This sign is an abbreviated form of \div and has a like meaning

168. The Antecedent is the first term of a ratio.

169. The Consequent is the second term.

When the antecedent is equal to the consequent, the ratio is called a ratio of equality, as 12 to 12; when the antecedent is greater than the consequent, it is called a ratio of greater inequality, as 12 to 7, when the antecedent is less than the consequent, it is called a ratio of less inequality as 7 to 12.

170. A Simple Ratio consists of a single couplet as 4:12.

171. A Compound Ratio is the product of two or more simple ratios. Thus,

PROPORTION.

The simple ratio of 8 to 4 is 2 The simple ratio of 9 to 3 is 3

The compound ratio of these is 72 to 12 = 6

Ratios are compounded by multiplying all the antecedents together for a new antecedent, and all the consequents together for a new consequent.

172. In comparing numbers with each other, they must be of the same kind, and of the same denomination. Thus, shillings have a ratio to shillings. A foot has a ratio to a yard; for one is *three times* as long as the other; but a foot has not properly a ratio to an hour, for one cannot be said to be *longer* or *shorter* than the other.

Exercises for the Slate.

1. What is the ratio of 3 to 27?

2. What is the ratio of 32 to 8?

Ans.

3. What is the ratio of 4 oz. to 3 lbs.?

Ans. 4 oz. : 3 lbs. = 4 oz. : 48 oz. = $\frac{1}{12}$

Required the ratios of the following numbers-

1.	7 to 14	5.	6 lbs. to 18 lbs.	1 9.	20 ft. to 40 vds
2.	9 to 36	6.	28 lbs. to 4 lbs.	10.	60 m, to 4 fur
3.	108 to 18	7.	9 oz. to 63 lbs.	11.	45 bus, to 3 ats
4.	136 to 17	8.	17 yds. to 68 yds.	12.	3s. to 15 shillings

13. Which is the greater, the ratio of 9 to 63, or that or 8 to 72?

14. Which is the greater, the ratio of 120 to 85, or that of 240 to 170?

15. What is the ratio compounded of 8:10 and 20:16?
Ans. 1
16. What is the ratio compounded of 85:40 and 20:16?

16. What is the ratio compounded of 35:40, and 60:75and 21:19? Ans. $\frac{147}{47}$

17. What is the r. io of 19 lbs. 5 oz. 8 dwts. to 58 lbs. sz. 4 dwts. Ans. 1

18. If the antecedent be $\frac{3}{5}$ and the ratio 6, what is the consequent?

19. If the antecedent be 14.5 and the ratio $\frac{1}{3}$, what is the consequent? Ans. 43.5

20. What sum of money will contain £6 10s. as often as 32 yards contain 8 yards? Ans. £26

st? 5. \$3.60. 6 bought 871 lbs. 6, if 40 . 75 lbs.

\$44.80. \$ cents. ? 50 lbs.

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of the ng the econd; $6 \text{ is } \frac{9}{86}$

rs com-UPLET. terms 20:5, viated

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PROPORTION.

124

21. To how many acres of land will 7 ac. have the same ratio that £16 has to £112? Ans. 49 ac.

22. To how many yards of cloth will 3 yds. 2 qrs. 2 nls. have the same ratio that $\pounds 2$ 16s. 3d. has to $\pounds 9$ 16s. $10\frac{1}{2}$ d. ? Ans: 12 yds. 2 qrs. 3 nls.

23. What number compared with 8 will form a ratio equal to that of 4 to 6? Ans. 53

173. When the ratio of two numbers is equal to that of two other numbers, they are said to be proportional. Thus, the ratio of 4 to 6 is equal to the ratio of 8 to 12; and the four numbers are on that account said to be proportional, or to form a simple proportion.

174. Proportion is usually indicated by placing a double colon (::) between the two ratios. Thus, 4:6::8:12, and are read, As 4 is to 6 so is 8 to 12.

175. Since each ratio consists of two terms, every proportion must consist of at least *four terms*.

176. The Extremes are the first and fourth terms. The Means are the second and third terms.

177. In every proportion the product of the extremes is equal to the product of the means. Thus, in the proportion 4:8::5:10 we have $4 \times 10 = 5 \times 8$.

178. From the preceding principles and illustrations, it follows that, any three terms of a proportion being given, the fourth may readily be found by the following

RULE. I. Divide the product of the extremes by one of the means, and the quotient will be the other mean. Or,

II. Divide the product of the means by one of the extremes, and the quotient will be the other extreme.

NOTE.—When the first and second terms are not both of the same name they must be reduced. The fourth term is always the same as the third term.

Exercises for the Slate.

Find the term not given in each of the following proportions:

1.	48 :20::():50.	Ans. 120
2.	42:70::3:().	5
3.	16:129::112:().	903
4.	48 yd.: ()::\$67.25:\$201.75.	144 vd.
5.	$17 \text{ yd.}: 221 \text{ yd.}:: (): \pounds 1 \text{ 1s.} 11 \frac{1}{4} \text{d.}$	1s. 8 ⁴ d.
6.	(): 160 yd. :: 8s. $5\frac{1}{4}$ d. : 13s. 6d.	100 vd.
7.	$3s. 4\frac{1}{2}d. : ():: 17 \text{ yd.}:: 187 \text{ yd.}$	£1 17s. 14d.
8.	$\frac{5}{16}$: ():: $\frac{1}{3}$: $\frac{2}{5}$.	3

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SIMPLE PROPORTION.

Simple Proportion is an equality of two simple 179. ratios, and consists of four terms, any three of which being given, the fourth may readily be found.

EXAMPLE 1.-If 8 yds. of cloth cost \$96, how much will 20 yds. cost at the same rate?

OPERATION. yd. yd. As, 8:20:: \$96 $\mathbf{20}$ 8)1920 \$240 Ans.

ANALYSIS .- Since 8 yards have the same ratio to 20 yds.as \$96, the cost of the former has to the cost of the latter, we have the first three terms of a proportion given, namely one of the extremes and the two means. Now to arrange the given num-

bers in the order of a proportion, or state the question, we make \$96 the third term, because it is of the same kind, and has the same ratio to the required answer, or fourth term, as the first has to the second. From the nature of the question, since the answer will be more than \$96, or the third term, the second term must be larger than the first; we therefore put 20, the larger number, for the second term, and 8, the smaller, for the first term, and then the product of the means divided by the given extreme, gives the required extreme.

EXAMPLE 2.-If 35 men consume a certain quantity or flour in 20 days, how long would it take 50 men to consume a like quantity?

OPERATION. men men days As 50 : 35 :: 20 20	ANALYSIS.—Having stated the question as in the last example, we perceive that the first and second terms have a common factor. 5 we
50)700	therefore cancel it, which leaves 19 and 7 as the new ratio. Again the
14 Ans.	factor 10 is common to the first and last terms, and we cancel it also.
As $59:35:20$ 10:7	then multiplying 7 by 2 we have the answer as before.

14 as before.

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OPERATION.

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the same ns. 49 ac. rs. 2 nls. . 10¹/_d. ? rs. 3 nls. tio equal Ans. 5 at of two Thus, the the four

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portions: Ans. 120 5 903 144 yd. 1s. 8¹/₄d. 100 yd. 17s. 1 d.

Exercises for the Slate.

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1.	13 yds. : 143 yds. :: 3s. 44d. :	Ans. £1 17s. 14d
2.	39 yds. : 432 yds. : : £1 1s. 11 d. :	£12 3s. 0d.
3.	8s. 5 ¹ / ₄ d. : 13s. 6d. : : 50 yds. :	80 yds-
4.	13s. 6d. : £2 17s. 4 ¹ / ₃ d. : : 68 yds. :	289 yds.
5.	48 men : 12 men : : 20 days :	5 days.
6.	5 bu. : 470 bu. : : £3 38. :	£296 2s. 0d.
7.	136 ewt. : 51 ewt. : : \$9.86.	$15s. 2\frac{1}{4}d.$
8.	£13 18. 54d. : £95 8s. 64d. : : 165 to	ons: 1131 tons.
9.	144 days : 89 days : : £60 15s. :	£37 10s. 11 ¹ / ₄ d.
10.	\$41.87 : £58 19s. 6 ³ / ₄ d. : : 34 years.	: 233 years.
11.	9 ac. 2 ro. 38 po. : 14 ac. 2 ro. 17 pc	b. : : \$8.45.
	-	Ans. $$12.67\frac{1}{2}$
12.	27 ac. 1 ro. 8 po. : 16 ac. 3 ro. 24 po.	$:: \pounds 22 \; 3s. \; 7\frac{1}{2}d. : \; 3$
		Ans. \$66.8
13.	£14 6s. $11\frac{3}{4}$: \$27.92 $\frac{1}{2}$:: 19 yds. 2	qrs. 3 nls.
	Ans	. 7 yds. 3 qrs. 2 nls.
14.	2 days : 3 years :: \$1.10 :	Ans. $\pounds 124$ 6s. $6\frac{3}{4}$ d.
15.	6 weeks : 68 years :: $\pounds 4$ 15s. $4\frac{1}{2}$:	
		Ans. £2810 7s. 8d.
16.	2 oz. 3 dwt. 21 grs : 4 oz. 17 dwt. 1	$8 \text{ grs}, :: \pounds 1 2 \text{s}. 9 \frac{1}{2} \text{d}.$
		Ans. \$11.09
180	D. From the preceding illustrations	and principles, we
deduc	e the following general	

RULE. I. Write for the third term that number which

KULE. 1. Write for the third term that number which is of the same name as the required fourth term. II. Of the other two numbers, write the larger for the second term, and the smaller for the first, when the answer should exceed the third term; but write the less for the second term, and the greater for the first, when the answer should be less than the third term. III. Multiply the second and third terms together, and divide their product by the first.

NOTE .- To shorten the work factors common to the first and second terms, or to the first and third terms, may be cancelled.

Exercises for the Slate.

1. If I get 60 yards of cloth for \$486.662, how many yards Ans. 24 yards. will I get for £40?

If 36 men earn \$192 in a week, what will 72 men earn 2. in the same time? Ans. \$384

3. If a railway train can run 525 miles in 15 hours, how Ans. 245 miles. far would it run in 7 hours?

4. If a grass field maintain 34 cows for 6 months, how long will it maintain 51 cows? Ans. 4 months.

5. If 17 cwt. long weight be bought for £14, how many may be bought for \$116.80? Ans. 29 ewt. 16 lbs.

A silversmith pays £144 for 19 lbs. of silver, how much 6. ought he to get for £234? Ans. 30 lbs. 10 oz. 10 dwt.

7. A lump of gold weighing 154 oz. costs \$2258.14, what will be the weight of a nugget which costs £290?

Ans. 96 oz. 5 dwt. 8. I bought 24 cwt. of sugar at £52 16s., required the price of 16 ewt.? Ans. £35 4s.

9. The wages of 6 men amount to \$18, required the wages of 9 men? Ans. \$27

Three score of sheep cost £66 16s. 8d., what will 36 10. sheep eost? Ans. \$195.16

A truekman charges \$15.47 $\frac{1}{2}$ for 84 miles, how much 11. is that for 56 miles? Ans. £2 11s. 7d.

If 43 yds. cost £2 16s. 3d., what will 9 yds. cost at the 12. same rate? Ans. \$27.38

A snail travels at the rate of 16 po. 2 yds. 2 ft. 9 in. in 13. 3 hours, how far will he have gone in 2 days, travelling night and day? Ans. 6 fur. 24 po. 2 yds. 2 ft.

A school-room containing 120 pupils is 92 yds. 2 ft. in 14. area, how much is that for each pupil? Ans. 6 ft. 132 in.

If $24\frac{3}{4}$ barrels of fish cost $39.27\frac{1}{2}$, what will $8\frac{1}{4}$ barrels 15. cost? Ans. \$13.091

If $2\frac{3}{4}$ tons of eoal cost \$13.33, required the price of 16. $19\frac{1}{4}$ tons ? Ans. £19 3s. 54d.

17. A person saves each week as much money as buys a square pole of ground, in what time will he be able to purchase a farm containing 21 ae. 7 po.? Ans. 64 yrs. 39 wks.

18. If 2 yds. 2 qrs. cost 16s. 71d., what will 12 yds. 2 qrs. cost? Ans. 20.23

19. A boy who lives 455 yds. from the school goes to it in 6 min. 30 sec., how lorg would he take to go, if he were 2 miles 6 fur. 26 po. 1 yd. from it?

Ans. 1 h. 11 min. 12 see. 20. If a man mow 6 ac. 2 ro. 36 po. of barley in 5 days 8 hours, working 10 hours a day, in what time would he mow 16 ac. 3 ro. 10 po. ? Ans. 14 da. 5 ho.

21. If 13 ewt. 0 qr. 9 lbs., long weight, cost £22 14s. 5³/₄d., what will 20 cwt. 3 qrs. 20 lb. cost? Ans. £36 7s. 2d.

22. A farmer draws a net profit of £23 17s. $2\frac{1}{4}$ d. from 2 ae. 17 po.; how much should he receive at the same rate from 38 acres 3 ro. 32 po. ? Ans. \$2147.28

7s. 1 d 2 3s. 0d. 80 yds. 289 yds. 5 days. 5 2s. 0d. 5s. 2¹/₄d. 31 tons.)s. 11¹/₄d. 3 years.

 $$12.67\frac{1}{3}$ 73d.: 3 s. \$66.8

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23. If $8\frac{3}{4}$ bushels of corn cost \$4.20, what will be the cost of 134 bushels at the same rate?
24. If $1\frac{3}{4}$ yds. of cotton cloth cost $$0.10\frac{6}{12}$, how many yds. can be bought for $$100$? Ans. $16\frac{2}{5}$ yds.
25. If $15\frac{5}{8}$ bu. of clover seed cost $$156\frac{1}{4}$, what will 9 bu.
2 pk. 2 ² / ₅ qt. cost ? Ans. \$95.75
26. If $\frac{7}{4}$ of a barrel of apples cost $\$_{11}^{5}$, how many can be bought for $\$_{77}^{60}$? Ans. $\frac{5}{6}$ of a barrel.
27. A butcher selling meat sells $14\frac{1}{16}$ oz. for a pound ; how much does he cheat a customer who buys of him to the amount of \$30? Ans. $$2.46\frac{3}{32}$
28. If I pay \$6 for the loan of \$100 for 1 year, what should I pay for \$493? Ans. \$29.58
29. If I borrow \$2000, and keep it 1 year 4 mo., how long should I lend \$240 as an equivalent for the favour?
Ans. II yr. $1\frac{1}{5}$ mo. 20 If 3 of 5 of 4 no cost 1 of 5 of \$140 what is the cost of
11 acres? Ans. $$36\frac{2}{3}$
31. If I pay $$4\frac{1}{8}$ to a person for buying \$100 worth of goods for me, what should I pay for buying \$189.75 worth? Ans. \$7.82 $\frac{3}{4}$ nearly.
32. If a merchant makes a reduction of 1 penny in each shillings' worth of goods sold, how much is that in £100? Ans. £8 6s. 8d.
33. An insolvent debtor fails for \$2000, of which he is able to pay only \$860, how much is that in each dollar, and how much will a person receive whose claim is \$900?
Ans. \$0.43 and \$387
34. If £100 gain £3 in one year, what will £256 10s. 6d. gain in the same time? Ans. £7 13s. 11d. nearly.
35. Find the interest of £126 for one year at £5 per cent. Ans. £6 6s.
NOTE.—In this exercise there are apparently only two terms. $\pounds 5$ per cent, however, just means $\pounds 5$ for $\pounds 100$. The above may therefore be written thus:—
If £100 gain £5 in one year, how much will £126 gain in the same time?
36. Find the interest of £126 14s. 6d. for 1 year at $8\frac{1}{3}$ per cent.

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be the cost ans. \$6.48 many yds. s. 16²/₃ yds. will 9 bu. ns. \$95.75 any can be of a barrel. ound; how he amount is. \$2.46 $\frac{3}{32}$ that should ons. \$29.58 ., how long yr. 1 $\frac{1}{3}$ mo.

the cost of Ans. \$363 0 worth of worth ? 323 nearly. ay in each in £100? £8 6s. 8d. h he is able r, and how

3 and \$387 56 10s. 6d. 1d. nearly. 5 per cent. Ans. £6 6s. terms. £5 may there-

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year at $8\frac{1}{3}$

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OPERATION.

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\$14.88 Ans.

ANALYSIS.—Here, and in all similar cases, the first term being 100, we make no formal statement but merely multiply the second term by the third and divide by 100 as in **50**.

Here the third term is con tained exactly 12 times in 100, we therefore cancel it. Dividing the second term by 12 we obtain the answer.

37. Find the interest of \$186 for 1 year at 8 per cent.

ANALYSIS. — Here, dividing the first and third terms by 100 we have the quotients 1 and .08. We therefore multiply the second term by .08, and obtain the required interest. In a similar manner we may find the interest for one year at any given per cent.

Write out and solve the following exercises-

38. Find the interest of £186 10s. for 1 year at 6¼ per cent.
39. At 54 per cent what is the interest of £186 10s. for 1 year at 6¼ per cent.

39. At 5¹/₁ per cent., what is the interest of £196 16s.8d.
for 1 year?

Ans. £10 1s. 9¹/₂d.

40. Find the interest of \$196.78 for 8¹/₂ per cent. for 1 year.

41. What is the interest for 12 months of \$1836 at 6 per cent? Ans. \$110.16

COMPOUND PROPORTION.

42. What is the interest of \$1234.871 for 1 year at 75 per cent? Ans. \$87.983

43. Borrowed \$500.10 for 3 months, at 7 per cent; whas will be the interest? Ans. \$8.753

44. Gave a note for \$88.96 due in 2½ years, at 64 per cent; what will be the interest? Ans. \$13.90

45. Borrowed \$988.65 for 2 years and 9 months, at 6 per cent; what will be the interest? Ans. \$163.12725

NOTE.- Let the pupil apply the Unitary Method to such of the preceding questions as can be readily solved thereby.

COMPOUND PROPORTION.

181. Compound Properties is an equality between a compound ratio and a simple one.

Thus 6:3 Into 4:2 : 12:3

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That is $6 \times 4: 3 \times 2:: 12 \times 3$; for $6 \times 4 \times 3 = 12 \times 3 \times 2$

NOTE.—Compound proportion is chiefly applied to the solution of questions which would require two or more statements in simple proportion.

EXAMPLE 1.—If 8 men can reap 32 acres in 6 days, how many acres can 12 men reap in 15 days?

		STA	1	TEN	IENT.					
As	8 6	men days	: ::	12 15	men days	2	::	32	ac.	

ANALYSIS.—In this example it is supposed that 8 men can reap 32 acres in 6 days; this being the case,

it is asked or demanded how many acres 12 men can reap in 15 days. The question may therefore be divided into two parts, supposition and demand.

In order to state the question in the form of a proportion, we take from the supposition that quantity, 32 acres, which is of the same kind as the answer required, and place it for the third term. Then, taking the next number, 8 men, in the supposition, and 12 men, the corresponding number in the demand, and considering these with reference to the third term only, as in simple proportion, we find the answer is to exceed E bow E

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COMPOUND PROPORTION.

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6 days, how

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proportion, es, which is e it for the in the supin the dethird term s to exceed the third torm, and therefore place 12 men for the second term and 8 for the first. Again, comparing the remaining quantity, 6 days, in the supposition with the corresponding quantity, 15 days, in the demand with reference to the third term, 32 acres, we observe that if the time be increased the number of acres will also be increased; we therefore place 15 days in the second term and the 6 days in the first, and the question is stated.

OPERATION. ANALYSIS .- Since the product of As 8 : 12] the antecedents has the same ratio to :: 32 6 : 15 the product of the consequents, as 32 has to the answer, we multiply 8 oy 48 :180 6 and 12 by 15 to form a simple 32 ratio. The remainder of the work is the same as simple proportion. 360 540 - acres. 48)5760(120 A.ns. 48 .. 96 96

EXAMPLE 2.—If 12 horses can plough 11 acres in 5 days, how many horses can plough 33 acres in 18 days?

Dividing the question into supposition and demand we have

12 horses	As 11 acres : 33 acres 18 days : 5 days } :: 12 horses
5 days ? 33 acres 18 days	$ \begin{array}{r} 198 : 165 \\ 165 \times 12 \\ \hline 198 \\ \hline 198 \\ 10 \text{ horses.} \end{array} $

Stating and working as in the former example we obtain 10 horses for the answer.

BY CANCELLATION. $\begin{array}{c} 3 \\ 3 \\ 1 \\ 1 \\ 3 \\ 3 \\ 3 \\ 3 \\ 3 \\ 2 \end{array}$

 $5 \times 2 = 10$ as before.

Here 11 is a common factor of the first and second terms, we therefore cancel it. Again, 3 being a common factor of 3 and 18, we divide each (3 and 18) by it, and set down the quotients 1 and 6. For similar reasons we omit 6 and write 2 instead of 12. We then multiply 5 and 2 together and find the answer as before.

From these examples and illustrations we have the following

RULE. I. Take from the supposition that number which is of the same kind as the answer required, and place it for the third term.

II. Take the remaining numbers in pairs, one from the supposition and a corresponding one from the demand, and arrange them as in Simple Proportion.

III. Finally, multiply together all the second and third terms, divide the result by the product of the first terms, and the quotient will be the fourth term or answer.

NOTE. -When the first term has factors which are common to the second or third terms, cancel the factors which are common, then divide he product of those remaining in the second and third terms by the prouct of those remaining in the first, and the quotient will be the answer.

Exercises for the Slate.

1 If 18 masons can build a wall 120 feet long in 3 days, in what time will 24 men build a wall 480 feet long?

Ans. 9 days.

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2. If the wages for 8 men for 12 days be \$64, what will be the wages of 10 men for 6 days? Ans: \$40

3. If \$100 gain \$4 of interest in 12 months, how much will \$60 gain in 15 months? Ans. \$3

4. If £100 gain £5 of interest in 10 months, how much would £250 gain in 8 months? Ans. £10

5. The wages of 8 men for 4 days are \$19.50, what will be the wages of 12 men for 2 days? Ans. \$14.62

6. If 12 reapers cut 71 ac. 2 ro. 8 po. in 6 days, how many acres will 8 reapers cut in 10 days? Ans. 79 ac. 2 ro.

7. If 16 horses in 9 days plough 110 acres, how many acres will 27 horses plough in 6 days. Ans. 123 ac. 3 ro.

8. If 208 families consume 6 cwt. of tea in 42 weeks, how much will 63 families consume in a year. Ans. 2 ¹/₄cwt.

9. If 18 men plant 29 ac. 2 ro. 263 po. of potatoes with the spade in 15 days, how many men would plant 17 ac. 3 ro. 8 po. in 6 days. Ans. 27 men.

10. If 69 yards of cloth 3 qrs. wide, make 24 pairs of trousers, how many pairs will 301 yds. 3 qrs. 2 nls., which is 1 yard wide, make? Ans. 140 pairs.

11. If a man walk 170 miles in 6 days, walking 15 hours a day, how many miles will he walk in 5 days, walking 12 hours a-day? Ans. 113 miles 2 fur. 26 po. 3²/₃ yds.

12. If 18 reapers cut 30 acres of barley in 6 days, working 10 hours a-day, how many reapers will it take to eut 40 acres in 4 days, working 12 hours a-day? Ans. 30 reapers.

13. If 16 men earn \$62.40 in 18 days, how many men will it take to earn \$140.40 in 24 days? Ans. 27 men.

If a family of 8 persons spend \$200 in 9 months, how 14. much will 18 persons spend in 12 months? Ans. \$600

15. If 15 men working 12 hours a-day, can hoe 60 acres in 20 days, how long will it take 30 boys working 10 hours a-day, to hoe 96 acres, 6 men being equal to 10 boys? Ans. 32 days.

16. If 125 men can make an embankment 100 yards long, 20 feet wide, and 4 feet high in 4 days, working 12 hours a-day, how many men must be employed to make an embankment 1000 yards long, 16 feet wide, and 6 feet high, in 3 days, working 10 hours a-day? Ans. 2400 men.

17. A log of wood 60 feet long, 4 broad, 2 thick cost \$128, what would be the price of one 45 feet long, $3\frac{1}{2}$ broad, and $2\frac{3}{4}$ thick? Ans. \$115.50.

18. If 421 yards of eloth, which is 18 in. wide, cost \$238.831, what will 1181 yards of yard-wide eloth of the same quality eost? Ans. \$1329.04.

19. If 400 men can make a canal which is to be a mile long, 40 feet broad, and 12 feet deep, in 20 days, working 8 hours a day, what length of eanal, 30 feet wide and 16 deep, could 300 men make in 45 days, working 10 hours a day ?

Ans. 2 miles 35 po.

Forty men engaged to finish a road, which was to be a mile long, in 60 days, but after three-fourths of it was done they left off. How many men would it take to finish the remainder in 6 days? Ans. 100 men.

21. If 5 horses require as much oats as 8 ponies, and 120 bushels last 12 ponies for 64 days, how long may 25 horses be kept for \$165 when oats are selling at \$0.55 per bushel?

Ans. 48 days.

If \$250 gain \$30 in 2 years, what will be the interest 22.of \$750 for 5 years? Ans. \$225

If \$100 gain \$5 in 1 year, what will be the interest of 23.\$575 for 31 years? Ans. \$100.623

What will be the interest of £125 for 4 years, if £150 24. will gain £10 10s. in 1 year? Ans. £35

25. If £100 gain £3 10s. in 1 year, what will £375 gain in 3 years and 8 months? Ans. £48 2s. 6d

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ns. 9 days. hat will be Ans: \$40 much will Ans. \$3 how much Ans. £10 hat will be s. \$14.623 how many 79 ac. 2 ro. nany aeres 23 ae. 3 ro. veeks, how ns. $2\frac{1}{4}$ cwt. atoes with t 17 ac. 3 1s. 27 men. irs of trouh is 1 yard . 140 pairs. 15 hours a ng 12 hours po. 32 yds.

COMPOUND PROPORTION,

26. If \$100 gain \$4.50 in 1 year, what \$426.66²/₅ gain from June 15th, 1865, to Sept. 18th, 1865? Ans. \$4.99

27. If $\pounds 100$ gain $\pounds 4$ in 365 days, what will be the gain on $\pounds 690$ 10s. 6d. for 85 days? Ans. $\pounds 6$ 8s. $7\frac{1}{2}d$.

28. Find the interest of 2737.50 for 56 days at $3\frac{1}{2}$ per cent. Ans. 14.70

NOTE.—The pupil may suppose that the full number of terms are not given in this exercise: but it will be readily seen that $3\frac{1}{2}$ per cent is in reality $3\frac{3}{2}$ for the loan or interest of \$100 for one year or 365 days. The above question may be written thus:--

If \$100 gain \$3½ in 365 days. how much will \$2737.50 gain in 56 days?

Note.—The terms *per cent, interest,* $\mathcal{G}c.$, have not been explained in the preceding pages: but as the illustrations of percentage in general depend on proportion, the pupil should, at this stage, be made acquainted with the principles involved. This will enable him to solve almost every question relating to per centage without considering them under any special rule.

29. Find the interest of £812 6s. 8d. for 7 years 3 months at 5 per cent. Ans. £294 9s. 5d.

30. Lent \$2400 for 4 months, and received \$24.60 for interest; what was the rate per cent? Ans. 3.07}

31. Find the interest of \$3311.50 for 292 days at $2\frac{1}{2}$ per cent. Ans. \$66.23

32. What is the interest of $\pounds 660$ for 8 months at $4\frac{1}{2}$ per cent? Ans. $\pounds 19$ 16s.

33. The value of a share in a railway is \$300, and the half yearly dividend is \$16.80; required the rate per cent?

Ans. 11 p. c.

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34. Bought \$6000 worth of goods, and at the end of 70 days sold them for \$6200, what was the gain per cent?

Ans. 17⁸/₂₁ p. c.

35. A person having borrowed a certain sum of money at 5 per cent., at the end of 3 months paid \$15, the amount of interest then due; how much did he borrow? Ans. \$1200

36. A person having mortgaged his property, pays \$40 of interest every three months; for what amount was the mortgage drawn, interest being charged at 6 per cent?

Ans. \$2666.663

37. Dec. 18th, 1865—I borrowed \$6866.46. with which I purchased flour at \$6.66 a barrel. March 17th, 1866—I sold the flour for $7.37\frac{1}{2}$ a barrel, cash. How much did I gain by the transaction, interest being reckoned at 6 per cent?

Ans. \$636.711

PERCENTAGE.

182. Per Cent. is a term derived from the Latin words per centum, and signifies by the hundred, or hundredths, that is, a certain number of parts of each one hundred parts, of whatever denomination. Thus, by 4 per cent., is meant \$4 of every \$100, 4 bushels for every 100 bushels, &c. Therefore, 4 per cent equals 4 hundredths = $.04 = \frac{4}{100} = \frac{2}{50} = \frac{1}{25}$.

183. Percentage is such a part of a number as indicated by the per cent.

184. The **Base** of percentage is the number on which the percentage is computed.

185. Since per cent. is any number of hundredths, it is usually expressed in the form of a *decimal*; but it may be expressed either as a *decimal* or a *common fraction* as in the following table.

NOTE .- In business, per cent is usually indicated by the sign %.

TABLE.

	Decimals.	Co	mmon fractio	on.	Lowest terms
1 per cent.	.01		100		1
2 per cent.	= .02		120		100
4 per cent.	= 04	-	140	-	1
5 per cent.	= .05	-	100		2.5
6 per cent.	= .06		100		20
7 per cent.	.07		77	-	50
10 per cent.	= .1		10	-	100
$12\frac{1}{2}$ per cent. =	= .125		$\frac{125}{1000}$		10
			* * * * *		0

Exercises for the Slate.

1. Express decimally 3 per cent.; 4 per cent.; 6 per cent. 9 per cent.; 11 per cent.; 15 per cent.; 20 per cent.; 25 per cent.; 130 per cent.; 375 per cent.

2. Express decimally $5\frac{1}{2}$ per cent.; $6\frac{1}{4}$ per cent.; $7\frac{1}{6}$ per cent.; $9\frac{1}{2}$ per cent.; $13\frac{1}{2}$ per cent.; $16\frac{1}{8}$ per cent.; $11\frac{5}{8}$ per cent.; $11\frac{5}{8}$ per cent.; $33\frac{1}{5}$ per cent.; $62\frac{1}{2}$ per cent.

3. Express decimally and as a vulgar fraction $1\frac{1}{4}$ per cent. 21 per cent. 25 per cent.

gain from Ans. \$4.99 he gain on 6 8s. 7½d. at 3½ per ns. \$14.70 of terms are 3½ per cent year or 365

37.50 gain

n explained tage in genge, be made able him to ut consider-

s 3 months 94 9s. 5d. \$24.60 for Ans. $3.07\frac{1}{2}$ s at $2\frac{1}{2}$ per as. \$66.23at $4\frac{1}{2}$ per s. £19 16s. at the half ent? s. $11\frac{1}{2}$ p. c. end of 70

nt? . $17\frac{8}{21}$ p. c. f money at

amount of Ans. \$1200 pays \$40 of s the mort-

\$2666.66 th which I 866—I sold d I gain by cent ? s. \$636.71

Express decimally $\frac{1}{4}$ per cent.; $\frac{3}{4}$ per cent.; $\frac{5}{8}$ per cent. 4. 5. Express in the form of common fractions, in their lowest terms, 6 per cent.; 5 per cent.; 33¹/₄ per cent.; 31¹/₄ per cent.; 113 per cent.; 185 per cent.

CASE I.

186. To find the percentage of any number.

EXAMPLE.- A man having 125 bushels of wheat, sold 25 per cent. of the quantity, how much did he sell?

OPERATION.	ANALYSIS.—Since 25 per cent. is $\frac{25}{100}$
125	$=.25$, he sold $.25 \times 125$ bus., or 125 bush.
.25	$\times .25 = 31\frac{1}{4}$ bhshels. Or, 25 per cent. is
	$\frac{25}{100} = \frac{1}{4}$, and $\frac{1}{4}$ of $125 = 31\frac{1}{4}$. Hence the
625	following—
250	0
	·
$31.25 = 31\frac{1}{4}$	

RULE. Multiply the given number or quantity by the rate per cent., expressed decimally, and point off as in decimals. Or,

Take such a part of the given number as the number expressing the rate is part of 100.

Exercises.

1.	What is 5 per cent. of \$18940?	Ans. \$947
2.	What is $8\frac{1}{2}$ per cent. of \$1248?	\$106.08
3.	What is $7\frac{1}{4}$ per cent. of \$56.75?	$\$4.11\frac{7}{16}$
4.	What is $6\frac{3}{4}$ per cent. of 1967 bus. ?	132.7725 bus.
5.	What is 94 per cent. of 275 miles?	26.95 miles.
6.	What is 25 per cent. of $\frac{5}{2}$?	
	$25 \text{ per cent.} = \frac{25}{100} = \frac{1}{4}, \text{ and}$	$\frac{5}{8} \times \frac{1}{4} = \frac{5}{32}$ Ans.
7.	What is $\frac{1}{4}$ per cent. of \$2526.40?	Ans. \$6.316.
8.	What is 1 per cent. of \$75,900?	\$250.00
9.	A farmer having 1500 sheep, sold 25	per cent. of them;
how n	nany did he sell?	Ans. 375 sheep.
10.	A merchant imported 1500 boxes of	oranges, and $12\frac{1}{2}$
per e	ent. of them decayed; how many be	oxes did he lose,
and 1	now many had he left?	ns. 187.5 lost.

CASE II.

To find what per cent. one number is of another. 187.

EXAMPLE.—A man having purchased a horse for \$170, sold him for \$17 less; what per cent. of his money did he lose?

136

and how many had he left?

17

17

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31.

 $31\frac{1}{4}$ 25

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1312.5 saved.

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OPERATION.

 $17 \div 170 = .10 = 10$ per cent. OR, $\frac{17}{170} = \frac{1}{10} = .10 = 10$ per cent. ANALYSIS.—We multiply the base by the rate per cent. to obtain the percentage (188); conversely, we divide the per

centage by the base to obtain the rate. Or, since \$170 is 100 per cent. of his money, \$17 is $\frac{17}{170}$, equal to $\frac{1}{10}$ of 100 per cent., which is 10 per cent. Hence the following—

RULE. Divide the per centage by the base, and the quotient will be the rate per cent., expressed decimally. Or, Take such a part of 100 as the per centage is part of the base.

Exercises for the Slate.

1. What per cent. of \$9876 is \$2469? 2. What per cent. of \$7656 is \$957?

What per cent. of \$7656 is \$957 ? Ans. 121

3. What per cent. of 4 tons 16 cwt. is 3 tons. 12 cwt?

Ans. 75 per cent.

Ans. 25

4. What per cent. of 6 bushels 1 peck is 4 bushels 2 pecks 6 quarts ? Ans. 75 per cent.

5. A man having 900 acres of land, sold $\frac{1}{3}$ of it at one time, and $\frac{1}{2}$ of the remainder at another time; what per cent. remained unsold? Ans. $33\frac{1}{3}$ per cent.

CASE III.

188. To find a number when a certain per cent. of it is given.

EXAMPLE.—A man sold $31\frac{1}{4}$ bushels of wheat, being 25 per cent. of all he had; how much had he at first?

31.25 b	ushels $\div .25 = 125$
$\frac{31\frac{1}{4}}{25}$ ×	$0R, \\ 100 = \frac{125}{100} \times 100 = 125$

ANALYSIS.—We are here required to find the base, of which 31¼ bushels is the percentage.— Now, percentage equals base multiplied by the

rate per cent.; conversely, base equals percentage divided by the rate per cent. Or, $31\frac{1}{4}$ bushels is 25 per cent. of all he had; $\frac{1}{25}$ of $31\frac{1}{4}$ bushels, or $\frac{125}{100}$ equals 1 per cent. of all he had, and 100 times $\frac{125}{100}$ equals 100 per cent. of all he had. Hence the following—

RULE. Divide the percentage by the rate per cent., expressed decimally, and the quotient will be the base, or number required. Or,

Take as many times 100 as the percentage is times the rate per cent.

tity by the as in deci-

💈 per cent.

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per cent.;

eat, sold 25

ent. is $\frac{25}{100}$ 125 bush.

per cent. is Hence the

umber ex-

Ans. \$947 \$106.08 \$4.117 2.7725 bus. 26.95 miles.

 $\frac{1}{4} = \frac{5}{32}$ Ans. ns. \$6.316. \$250.00 at. of them; . 375 sheep. ges, and $12\frac{1}{2}$ lid he lose, 87.5 lost. 312.5 saved.

nother.

se for \$170, did he lose?

Excreises for the Slate.

24 is 8 per cent. of what number ?Ans. 3002. 42 is 7 per cent. of what number ?600

3. 39½ is 5 per cent. of what number ? 790

4. A man, owning 30 per cent. of a shoe factory, sells 33 per cent. of his share for \$1111.275, what is the value of the whole factory? Ans. 11112.75

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Ans. 300 600 790 , sells 33 lue of the 11112.75

APPENDIX I.

KEY TO THE SELF-TESTING EXERCISES.

ADDITION.

All the exercises given in this Rule as self-testing are formed as shown in section 3.

To test the sum of any number of rows or lines we may use any of the three following methods.

1st. As the first line of each exercise is a multiple of 9, the sum of any number of lines must also be a multiple of 9; therefore easting the 9's out of the sum, if the work is correct, there will be no excess.

If there be an error in any of the lines it may also be deteeted by casting out the 9's in the same manner.

2nd. If the exercise is composed of 5 rows, the sum of all the rows will be 12 times the first line. If composed of 6 rows it will be 20 times the first line, and so on as may be seen in the following examples.

(1) 1467 First line = 1 times 1467 Second " = 1 " 2934 Third " = 2 " 1st line. 4401 Fourth " = 3 " " 7335 Fifth " = 5 " "	(2) 1467 First line = 1 1467 Second " = 1 2934 Third " = 2 4401 Fourth " = 3 7335 Fifth " = 5
17604 Sum =12 times 1st line.	$\frac{11736 \text{ Sixth } "=8}{20046 \text{ G}}$
	29340 Sum $= 20$ times 1st line.

3rd. The sum of a required number of lines added to the first line will be equal to the line that is *two* more than the required number of lines. Thus let 6 be the required number of lines. The sum of six lines added to the first line will be equal to the eighth line. Let 11 be the required number of lines. The sum of eleven lines added to the first line will give the 13th line.

EXAMPLE.--Find the sum of 162 extended to 8 rows, and test the result by the tenth line.

OFFICATIO	UN.
Ist line 162	
2nd " 162	
Brd " 324	
4th " 486	
5th ' 810	
6th "1296	
7th " 2106	
8th " 3402	
	8748 == sum of eight lines.
9th " 5508	162 = first line.

Tenth line 8910 = 8910 = 1 line that is two more than the required number of lines, *i. e.*, (8 + 2) 10th line.

NOTE.—As soon as the pupil fully understands the principles of addition he should be required to test his work as above, and thus facilitate his progress.

SUBTRACTION.

The exercises under this rule are to be worked by the pupil as shown in the following example.

18717	minuend.	ANALYSISWe
12478	subtrahend.	first take the sub-
		trahend from the
6239	difference.	minuend, then this
6239	difference betwen 2d and 3d line.	difference from the
		subtrahend. If the
two la	st lines are alike the work is corre	et.

MULTIPLICATION.

SECTION 1.—The test of the exercises in this section may be seen from the construction of each.

SECTION 2.—In the exercises in this section the teacher will observe that every line in the working, and every product, is a multiple of nine, and by adding the digits in any line or product he can ascertain if it is correct. S in th

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ction may

e teacher very proits in any SECTIONS 3, 4 and 5.--The manner of testing the exercises in these sections may be readily seen from their construction.

DIVISION.

SECTION 1.—Each dividend is a multiple of its divisor, consequently, if worked correctly there will be no remainders. SECTIONS 4 and 6.—In the exercises under these sections each dividend is a multiple of nine, also each divisor, and the remainders, if any, are divisible by 9, and each dividend is divisible by all the divisors given with remainders as above.

ADDITION OF DECIMALS.

Increase each figure of the second line by unity, and prefix the first figure of the exercise. The effect of 9 occurring in the second line should be particularly noted.

NOTE .- The second line may be varied at pleasure.

SUBTRACTION OF DECIMALS.

Same as Simple Subtraction.

MULTIPLICATION OF DECIMALS. Same as Section 3 of Simple Multiplication.

DIVISION OF DECIMALS.

The quotients are without remainders, and each is a multiple of 9.

COMPOUND ADDITION.

Test exactly the same as in addition of decimals, with the exception that unity must be added, not to each figure, but to each denomination excepting farthings.

COMPOUND SUBTRACTION.

SECTION 2.—May be seen in example worked. The exercises under Division, and Practice are sufficiently explicit.

APPENDIX II.

(54

(7)

TABLE I.

EQUIVALENT OF CANADA CURRENCY IN FENCE STERLING.

 1
 d.493150684

 22
 .986301369

 3
 1.47945205

 4
 1.97260273

 5
 2.46575342

 6
 2.95890410

 8.45205479
 3.945205479

 108
 3.94520547

 9
 4.4\$8\$35616

NOTE-

For any number of CENTS from 1 to 9, point as in the Table. "10 to 90 move the point 1 place to the right.

For	DOLLARS S	61 to \$9	move the poi	int2r's	ces to th	se right
66	16 \$	10 to \$90	"	U	66	64
66	4 \$1	00 to \$900	66	4	66	66
4	·· \$10	00 to \$9000	44	5	66	66
66	" \$10.0	00 to \$90.00	0	6	"	66
46	" \$100.0	00 to \$900.0	09 4	7	66	44
66	"\$1,000,0	00 to \$9,000	,000 "'	8	"	66

Im working exercises, if the figures to the right of the point range from-

.13	to	.38	reckon them	1d
.39	to	.63	66	106
.54	to	.88	**	2.d
.89	to	.99	4	Ĩđ

EXAMPLES.—Convert the following amounts, Canada eurrency, to pounds, shillings and pence, stg:—(1) 0.08; (2) 0.10; (3) 10; (4) 100; (5) 1000; (6) 1000; (7) 1000000000; (7)

(1) $8 \text{ cts}=4d$	(2) 10 $ets=5d$
(3) \$10=12)493.15	(4) \$100=12)4931.50
$2,0)1,1.1\frac{1}{4}$	$\overline{2,0}$)41,0. 11 $\frac{1}{2}$
£2. 1s 11d	£29. 10s 132d

(3 \$1,0 0=12)49315. 2,0(410,9. 7 £205. 9s 7d

Y IN

(6) \$10,000=12)493150.68

2,0)4109,5. 104

£2054 15s 1034

(7)	\$1,060,600.90 .10		49315	068. 4.	.4 4 .93			
	\$1,009,000.10	12)	49315	073.	37			
		2,0)41095	8,9.	54			
			£2054	79.	9s 540	1		
			(8)	\$2	00.		9863.	01
				1	20.		986.	20
				•	5.		246.	57
					.50	-	24.	65
					.65		2.	46
				63	25.55	12)	11123.	98
						2,0),92,6. 1	11
						£	46 fs.	12.4

place to

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" the point

66

ada eur-.08;(2) 00;(7)

111 0s 131d 145

. . . ?

TABLE II.

EQUIVALENT OF POUNDS, SHILLINGS & PENCE STG., IN CANADA CURRENCY.

£		15.	1	d.	1
1	\$4.86666666	1	\$.243	1	\$.02
2	9.73333333	2	.486	2	.04
3	14.59999999	3	.729	3	.06
4	19.46666666	4	.973	4	.08
5	24.333333333	5	1.216	5	.10
6	29.19999999	6	1.459	6	.12
7	34.06666666	7	1.703	7	.14
8	38.93333333	8	1.946	8	.16
U	43.79999999	9	2.189	9	.18
1		10	2.433	10	.20
		11	2.676	11	.22
		12	2.919		
		13	3.163	f.	
		14	3.406	1	.005
		15	3.649	2	010
		16	3.893	2	.015
	Ļ	17	4.136	-	.010
	1	18	4.379		
		19	4.623		
	1	1			

Note-For shillings, pence and farthings, point as in the table "POUNDS from £1 to £9" """ £10 to £90 move the point 1 place to right £100 to £900 "" 2 places ""

2100 10 2900	••	z places	••	
£1000 to £9000	66	3 "	66	
£10,000 to £90,000	"	4 "	66	
£100,000 to £900,000	66	5 "	"	
£1,000,000 to £9,000,000	* *	6 "	**	

If the mills reach 6 or over reckon them as 1 cent.

EXAMPLES.—Convert the following amounts, sterling money, to Canadian currency :—

(1) $\pounds 1 = \$4.87$	(7) £4 10s 94d
(2) $\pounds 100 = \$486.67$	$\pounds 4 = \$19.466$
(3) $\pounds 1000 = \$4866.67$	10s = 2.433
(4) $\pm 10,000 = \$48666.67$	9d = .18
$(5) \pm 100,000 = \$486666.67$	2f = .01
(6) $\pounds 1,000,000 = \$4,866,666.67$	
	\$22.09

& PENCE

APPENDIX.

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APPENDIX III.

THE METRIC SYSTEM.

The metric system of weights and measures has been used in France to the exclusion of all others since 1840. It is now also in use in many other countries of Europe as well as in several countries of South America. It has been legalized in Great Britain, the Dominion of Canada, and in the United States, though not enforced or as yet generally adopted. Being a decimal system all calculations are by it rendered extremely simple, which has brought it into general use amongst the scientific men of all countries. The present generation of schoolbovs will probably witness its adoption for commercial purposes in most of the civilized countries of the world.

A length equal to the one ten millionth part of a quadrant, or the distance from the North Pole to the Equator, was taken as the measure of the unit of length and as the base of the system. This length is called a metre (meé-ter) and is equal to 39.37 English inches nearly.

Upon the metre are based the following primary units.

1. The Gramme (gram) The unit of weight. 2. The Litre (lefter) The unit of conscient

- 2. The Litre (leé-ter) The unit of capacity.
- 3. The Are (ār)
- The unit of surface.
- 4. The Stere (steer)
 - The unit of solidity.

From these primary units the higher and lower order of units are derived decimally. The names of the higher order of units are formed by prefixing to the name of the primary unit, Greek numerals :- deca (dec'-a) 10, hecto (hec'-to) 100, kilo (kī-lo) 1000, myria (myr'-ia) 10,000. For example,-

A decametre (dec'a-mēter) = 10 metres.

A hectolitre (hec/to-leeter = 100 litres.

A kilogramme (kilo-gram) = 1000 grammes.

A myriametre (myria-mēter) \equiv 10000 metres.

The names of the lower orders of units are formed by prefixing to the name of the primary unit Latin numerals :----

table

ace to right ces 66 66 " " 44 11 44 44

•

, sterling

deci (des'e) 10th part, centi (sen-te) 100th part, milli (mil'-le) 1000th part. For example,

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A decimetre (desi-meter) = 1 metre.

A centilitre (sent'e letter) = 01 litre.

A milligramme (mil'-le-gram) = 001 gramme.

MEASURE OF WEIGHT.

The Gramme which is the unit of weight is equal to 15.432 English grains It is the weight of a cubic centimetre (sentimē-ter) of distilled water, that is, a quantity of water which fills the cube of the hundredth part of a metre.

TABLE.

10 milligrammes = 1 centigramme.

10 centigrammes \equiv 1 decigramme.

10, decigrammes $\equiv 1$ Gramme.

10 decagrammes \equiv 1 hectogramme.

10 hectogrammes \equiv 1 kilogramme.

10 kilogrammes = 1 myriagramme.

The kilogramme is considered the unit in weighing heavy articles. It is of course equal to 15432 grains or 2 2045lbs. avoirdupois, there being 7000 grains in a lb. avoirdupois.

EXERCISES.

Express each of the following quantities in grammes;
 (1) 7.4 decagrammes, (2) 984 centigrammes, (3) 386 decigrammes?
 Ans. (1) 74, (2) 9.84, (3) 38.6 grammes.
 How many kilogrammes are contained in each of the following quantities; (1) 7.4 hectogrammes, (2) 9342 grammes, (3) 14 myriagrammes?

Ans. (1) 74, (2) 9.342, (3) 140 kilogrammes. 3. How many centigrammes are contained in 4387 kilo grammes? Ans. 438700000 centigrams.

4. How many kilogrammes are contained in 4.76432 milligrams? Ans. .00000476432 kilog.

5. Reduce 25 grammes to (1) centigrammes, (2) decagrammes, (3) hectogrammes?

Ans. (1) .25, (2) 250, (3) 2500.

6. What is the value in English weight of (1) 1 decigramme, (2) 1 centigramme, (3) 1 milligramme ? (mil'-le)

8.

o 15.432 e (sentir which

g heavy 20454 irdupois.

numes; 36 decirammes. 1 of the 2) 9342

rammes. 87 kilo tigrams. 4.76432 82 kilog. 2) deca-

3) 2500. 1 deci-

APPENDIX.

Ans. (1) 1.5432, (2) .15432, (3) .015432 grains. 7. Find the value in English weight of (1) 3 decagrammes, (2) 5 hectogrammes, (3) 4 kilogrammes?

Ans. (1) 46296, (2) '716, (3) 61728 grains. How many lbs. avoirdupois in 20 kilogrammes?

Ans. 44.08 lbs. avoir.

MEASURE OF CAPACITY.

The Litre is the primary unit in measuring liquids as milk, and dry articles as grain, salt, &c. It is the volume of a cubic decimetre, that is the cube of the tenth part of a metre, and contains .22009 imperial gallon or pearly 13 pints.

TABLE.

10 millilitres = 1 centilitre. 10 centilitres = 1 decilitre. 10 decilitres = 1 *Litre*. 10 decalitres = 1 hectolitre. 10 heetolitres = 1 kilolitre.

The hectolitre is the common measure for grain, and is equal to .3439 imperial quarter or nearly $2\frac{3}{4}$ imperial bushels.

EXERCISES.

1. Reduce (1) 347 centilitres, (2) 98 decalitres, (3) 574 millilitres to litres? Ans. (1) 3.47, (2) 980, (3) .574 litres. 2. In 15 htres find (1) how many centilitres, (2) how

many hectolitres? Ans. (1) 1500, (2) .15.

3. How many centilitres are contained in 45 decalitres? Ans. 45000 centilitres.

4. In 3 hectolitres, 6 decalitres, and 2 litres, how many millilitres? Ans. 362000 millilitres.

5. In 4 millilitres how many (1) decalitres, (2) hectolitres? Ans. (1) .0004, (2) .00004.

6. From a cask containing 4 hectolitres of oil there were drawn off 38 litres, 5 centilitres, how much remained?

Ans. 361.95 litres. 7. How many imperial gallons are contained in 19 hectolitres? Ans. 2.64108.

8. How many hectolitres are contained in 2.64108 imperial gallons?

MEASURE OF LENGTH.

The Metre is not only the primary unit of length, but is, as has been stated above, the basis of the metric system. Its length is 39.37 inches nearly.

TABLE.

10 millimetres = 1 centimetre.

10 centimetres = 1 decimetre.

10 decimetres $\equiv 1$ Metre.

10 metres = 1 decametre.

10 decametres = 1 hectometre.

10 hectometres = 1 kilometre.

10 kilometres \equiv 1 myriametre.

In measuring long distances, the kilometre, which is about 5-8 of a mile (39370 inches) is regarded as the unit.

EXERCISES.

 How many centimetres in 17.36 metres ? Ans. 1736 centimetres.
 Reduce 25.86 metres to kilometres ?

Ans. ·02586 kilometres.

3. Find how many kilometres are in 376 decimetres? Ans. .0376.

4. How many inches in 10 kilometres? Ans. 393700 inches.

In 393700 inches how many kilometres?

6. How many millimetres in one inch?

Ans. 25.4 millimetres.

7. In two kilometres how many miles? Ans. 1.24 miles.

8. How many metres in a furlong? Ans. 201.168 metres.

MEASURE OF SURFACE.

The Square Metre is the primary unit in the measurement of small surfaces. In the measurement of large surfaces, such as a field, the Are is regarded as the primary unit. A square metre is 10 decimetres in length and 10 in breadth, hence a square metre is equal to 100 decimetres. For a similar reason a square decimetre is equal to 100 centimetres. The Are is a square, whose side is 10 metres, and hence it is equal to 100 square metres=1076 sq. feet, or 119.55 sq. yds., or about 1-40 of an acre. me ar of in for

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TABLE.

100 sq. millimetres = 1 sq. centimetre.100 sq. centimetres = 1 sq. decimetre.100 sq. decimetres = 1 sq. metre.100 sq. metres = 1 Are.

100 āres=1 hectare.

A square metre is called a centiare (sen'-ti-āre) in land measure, hence 100 centiares=1 are. The names centiares, ares, and hectares only are used in land measure.

NOTE.—While measures of length increase and decrease by a scale of tens, it will be seen from the table above that measures of surface increase and decrease by a scale of hundreds. Hence it is necessary in writing numbers denoting surfaces to allow two decimal places for square decimetres, &c., e. g. 9 sq. metres, 4 sq. decimeters are written 9.04 sq. metres.

EXERCISES.

Express the following in sq. metres (1) 8 decimetres, 1. Ans. .08, (2) .0026. (2) 26 centimetres.

2. Express the following in square metres and add them : 25 sq. decimetres, 49 sq. metres, 58 sq. centimetres, 6.7 sq. Ans. 55.9558. metres?

3. How many sq. metres are there in a surface 7 metres long and 25 metres wide? Ans. 175.

4. Find the cost of polishing a surface 3 metres, 6 decimetres long and 2 metres, 4 decimetres wide at \$2.50 per sq. Ans. \$21.60. metre?

5. Express the following in ares and add them :- 2.4 hectares, 243.4 ares, 58 hectares, 15 centiares?

Ans. 6283.55 ares.

6. How many hectares in (1) 425.3 ares, (2) 48 cen-Ans. (1) 4.253, (2) .0048 hectares. tiares?

7. Sold 9 hectares, 4 ares, and 6 centiares of land at \$6.25 an are, how much was received for the land?

Ans. \$5650.374.

How many ares in 1 English acre? Ans. 40.48 ares. 8.

MEASURE OF SOLIDS.

The cubic metre is the primary unit in the measurement of solids; but in the measurement of firewood, stone, &c., the stere is the primary unit. A cubic metre is a cube which is

but is, em. Its

is about

timetres.

lometres. tres? s. .0376. 00 inches.

llimetres. 24 miles. 8 metres.

surement surfaces. unit. A breadth. For a 00 centietres, and feet, or

10 decimetres in length, 10 decimetres in breadth, and 10 decimetres in height or depth, and hence it contains $10 \times 10 \times 10 = 1000$ cubic decimetres = 35.3165 cubic feet or 1.308 cubic yards. The stere is of the same value.

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TABLE.

1000 cubic millimetres = 1 cubic centimetre.

1000 cubic centimetres = 1 cubic decimetre.

1000 cubic decimetres = 1 cubic metre or stere.

- 10 decisteres = 1 stere.
- 10 steres=1 decastere.

Where the measures increase and decrease by a scale of thousands, three decimal places must be allowed in writing decimetres, &c, e. g. 9 cubic metres, 4 cubic decimetres are written 9.004 cubic metres.

EXERCISES.

1. How many cubic metres in 76.4 cubic metres, 3.6 cubic decimetres? Ans. 76.4036.

2. How many cubic metres in 57 cubic centimetres? Ans. .000057 cubic metres.

3. How many cubic metres in a cube whose scale is 3.5 metres? Ans. 42.875.

4. How many cubic metres of air will a room contain whose height is 4.3 metres, breadth 3.5 metres and height 43 decimetres? Ans 64.715.

5. In 14 steres how many (1) decasteres, (2) decisteres ?

Ans. (1) 1.4 decasteres, (2) 140 decisteres.

6. In 7 decasteres, 5 steres, 7 decisteres, how many decisteres? Ans. 757 decisteres.

7. How many steres in a pile of wood 2 metres wide, 6.34 metres lorg, and 5 decimetres high? Ans. 6.34 steres.

8. How many steres in 726 cubic yards? Ans. 555.04.

MISCELLANEOUS EXERCISES.

1. How many square centimetres are there in 248 millimetres? Ans. 2.48.

2. How many litres are contained in 3789 millilitres? Ans. 3.789.

3. How many centigrammes are contained in 5.346 kilogrammes? Ans. 534600.

4. How many milligrammes are contained in 6 cubic centimetres of water? Ans. 6000.

5. In 96.5 grammes of gold how many cubic centimetres, gold being 19.3 times as heavy as water?

Ans. 5 cubic centimetres. 6. If mercury is 13.5 times as heavy as water, how many grammes will a vessel contain whose capacity is 20 centimetres? Ans. 270 grammes.

7. How many litres of wheat can be put into a bin that is 2 metres long, 1.4 metres wide and 1.6 metres high?

Ans. 4480 litres.

8. In 6 metres how many inches? Ans. 236.22.

9. How many feet in 8 metres? Ans. 26.246.

10. How many square yards are then in 20 ares?

Ans. 2391 sq. yds.

11. In 4782 sq. yds. how many ares? Ans. 40 ares.

12. How many acres in a field of 7 hectares, 2 arcs? Ans. 17.546 acres.

13. How many imperial gallons in 24 kilolitres? Ans. 5282.16 imp. gals.

14. In 15846.48 imperial gallons, how many kilolitres? Ans. 2 kilolitres.

15. In 23 kilogrammes how many lbs. avoirdupois? Ans. 50.705 lbs. avoir.

NOTE.—The superiority of the metric system above that in use with us will readily be seen from the foregoing exercises, but one or two additional questions will present the matter to the pupil in a clearer light.

How many square feet are there in 346 square inches?

By our present method we have to divide 346 by 144; $\frac{44}{244} = 2.402$ sq feet.

"How many square centimetres are there in 346 square millimetres?

By the metric system we have only to divide by 100, *i. e.*, point off two figures to the right; $\frac{346}{160} = 3.46$ sq. centimetres.

How many cubic yards are there in 537 cubic feet ?

By our present method we have to divide 537 by 27; $\frac{537}{2} = 19.88$.

How many litres are there in 43584 millilitres?

By the metric system we have only to divide by 1000, *i. e.*, cut off three figures to the right; $\frac{43584}{1000} = 43.584$ litres.

Further illustrations need not be given since a like sim plicity characterizes every operation in the system.

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