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## 解. (3. ©age \& Co's eftathematical Series.

# MENTAL ARI'THMETIC, --BY.- <br> J. A. McLetllan, M. A., LL.I)., Inspector of Ili,gh Schools, Ontario. 

## PARTII.

## PERCENTAGE AND ITS APPLICATIONS, VARIOUS RULES, GENERAL ANALYSIS.

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> EIGHTH EDITION.

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## PREFACE.

> Tile Second Part of the Canadian Mental Arithmetic is now submitted to the public.

It contains a great variety of properly classified puestions in Percentage and its applications, Stocks und Shares, Interest, Discount, \&c., together with soluions of almost every type of question likely to be set with in any treatise on arithmetic. Many of ${ }^{1}, \$ 8 e$ solutions are original, $\dagger$ and are now published for : he first time. It is believed that students who receive a fair training in the methods of the following pages, will find no difficulty with any treatise or written arithmetic ; and that systematic mental drill will produce better arithmeticians, and at a less expenditure of time and energy than the rule and routine methods that have too long prevailed.

[^0]The publishers desire to express their great satisfaction with the very favorable reception accorded to the "First Parr" by the most experienced teachers in the Dominion, and venture to hope that the "Second Part" will meet with an equally kind reception, and prove a still more valuable aid to both teachers and students.

Tononta, lat Nov., 1872

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## CHAPTER 1.

## PERCENTAGE AND ITS APPLICATIONS.

## Section I.-Introductory.

> Exampies.-1.

1. A boy spends 1 cent of every 5 cents he has : how many does he spend of 20 cents?

Sol.-He spends 1 of every 5 ; there are 4 tines 5 in $20 . \cdot$ he spends 4 times 1 , or 4 ( $=20 \times 1 \div 5$, or $=20 \times \frac{1}{5}$ ).
2. A hoy spends 2 cents of every 6 he has: how many does he spend of 30 ?

Sol.-He spends 2 out of cvery 6 ; there are 5 sixes in $30 . \cdot$ he spends 5 times 2 or 10 ( $30 \times 2 \div 6=30 \times \frac{2}{6}$ ).
8. If he spends 4 out of every 10 , how many does he spend of 60 ?

Sol.-He spends 4 of every 10 ; there are 6 tens in $60 . \therefore$ he spends 6 times 4 , or 24 ( $=60 \times 4 \div 10=$ also $60 \times \frac{4}{10}=60 \times .4$ ).
4. A boy gave away 6 marbles of every 20 he had : how many did he give away of $40 ?$ of 60 ? of 100 ?
5. A man expended in groceries $\$ 6$ of every $\$ 10$ he had : how much did he spe:i: or $\$ 45$ ?

Sol. - He spent $\$ 6$ of every $\$ 10$; there are $4 \frac{1}{2}$ tens in $45 . \cdot$ he spent $4 \frac{1}{2}$ times $\$ 6=\$ 27$ $\left(=45 \times 6 \div 10\right.$, also $\left.=45 \times \frac{6}{10}\right)$.
6. A man had 300 sheep, he sold 8 out of every 100: how many did he sell?

Sol.-He sold 8 of overy hundred; there are 3 hundred. $\cdot$. he sold 3 times 8 , or $24(=300$ $\times 8 \div 100$, or $=300 \times{ }_{\mathbf{T}}^{8}{ }^{8}$ ).
7. A s.an paid away $\$ 7$ out of every hundred he had : how mueh did l:o pry out of 200? 400 ? 500 ? 800 ? 900 ?
8. A man received $\$ 8$ for every $\$ 100$ lent for a cercain time: how much did ho receive for $\$ 350$ ?

Sol.-He recoived $\$ 8$ for 1 hundred; there were $3 \frac{1}{2}$ hundred lent. $\cdot$ he received $3 \frac{1}{2} \times 8$ $=\$ 28\left(=350 \times 8 \div 100=350 \times{ }_{\text {1 }}^{8}{ }_{0}^{8}\right)$.
9. A man borrowed money for a time and paid $\$ 8$ for ovory hundred : how much did he pay on $\$ 550$; $\$ 525\} \$ 575$ ?

Instead of using the phrases 2 m . every hundred, 3 on every hundred, 4 on every hundred, 5 on every hundred, 6 on every hundred, \&c., \&c., we say 2 ; cent. 3 per cent. 4 per cent. 5 per cent. \&c., \&c., the words per cent. meaning "on every hundred."-Notc.-The symbol \% is often used for the words per cent.
10. How much is 5 per cent of $\$ 300\} \$ 400\} \$ 800$ ?
11. How much is 8 per cent. of $\$ 325$ ? $\$ 450$ ? $\$ 5751$

Sol.-In 325 there are 31 hundreds $\therefore 8$ per cent. $=31 \times 8=26 .=(325 \div 100) \times 8=$ $325 \times{ }_{\top} \frac{8}{0 \pi}$, also $=325 \times .08$.
12. 5 is what part of $100 ? 6$ is wha part of 1001 7181
18. What part of a hundred is 5 per cent. of it 9 6 per cent. 97 per cent. 88 per cent?
14. Since 5 per cent. of $100=\frac{1}{2}$ of it, how much will 5 per cent of 200 be? $300 ? 400 ? 7001900$ ? Sol.-Since 5 per cent. of $100=\frac{1}{2}$ of 100,5 per cent of $200=-\frac{2}{20}$ of $100=3_{0}^{1}$ of 200. So 5 per cent. of $300=\frac{2^{3}}{6}$ of $100=2_{2}^{1}$ of 300 , \&c.
15. What part of 545 is 5 per cent. of it?

Sol.-5 per cent. of $\$ 545=\$ 10.4 \times 5=\$ 545 \times$

Or 100 per cent. of $\$ 545=\$ 545$.
$\therefore 1$ per cent. " $=\$ \frac{5}{5} \mathbf{0}_{0}$.
And 5 per cent. $\quad "=\$ \frac{545}{100} \times 5=\$ 545 \times \frac{1}{20}$.
16. What part of any number is 5 per cent. of it? Sul.-100 per cent. of the number=the number. $l$ per cent of the number $=\frac{T}{1} \delta_{0}$ of the number. .5 per cent. of the number $={ }_{10}^{5} \sigma=$ ${ }^{1} \frac{1}{0}$ of the number.
17. What is 5 per cent. of 809 of $60 \%$ of $40 ?$ of 85 of 90 ?

Sol.-5 per cent. of $80=80 \times{ }_{\frac{1}{2} 0}=4$; or $=(80$ $\div 100) \times 5=\frac{4}{6} \times 5=4$; or $=80 \times 5=4$; or $80 \times{ }_{10} \frac{5}{0}=80 \times \cdot 05=4$.
18. What is 8 per cent. of $\$ 325$ ?

Sol. -8 per cent. of $\$ 325=325 \times \frac{1_{0}}{80}$ (or $\frac{2}{26}$ ) $=28$; or $=\frac{325}{3} 05 \times 8=3 \frac{1}{6} \times 8=28$; or $=3.25$ $\times 8=28$; or $=325 \times 08=28$.
19. What then are the various ways of finding any por cent. of a number?

Examples.-2.

1. What part of a number is 6 per cent. of it? 3 per cent. of it? 4 per cent. of it $? 8$ per cent. of it?
2. What part of a number is 5 per cent. of it? 10 per cent.? 15 per cent. $? 22$ per cent.? 40 per cent.? 55 per cent. $\} 12$ per cent. $\{80$ per cent. $?$ 35 per cent.? 65 per cent. $\% 135$ per cent. ?
3. What part of a number is $12 \frac{1}{2}$ per cent. of it? $18 \frac{3}{4}$ per cent. $36 \frac{1}{4}$ per cent.? $8_{4}$ per cent. $? 37 \frac{1}{2}$ per cent. $3 \quad 26$ per cent. $\left\{10 \frac{5}{5}\right.$ per cent. $387 \frac{1}{2}$ per cent. $\%$
4. What part of a number is $\frac{1}{2}$ per cent. of it? $?$ per cent. ? $\frac{5}{8}$ per cent. $? \quad \frac{7}{10}$ per cent. $\} \quad \frac{5}{12}$ per cent. ? $\frac{7}{8}$ per cent.?
5. What per cent. of a number is $\frac{1}{6}$ of it?

Sol.-The entire number is 100 per cent. $\therefore \frac{1}{8}$ of it $=20$ per cent.
6. What per cent. of a number is $\frac{1}{3}$ of it? $\frac{3}{6}$ of it 1 $\frac{3}{4}$ of it? $\frac{6}{25}$ of it: $\frac{2}{3}$ of $\frac{3}{4}$ of it?
7. What per cent. of 16 is 4 ?

Sol.-4 is $\frac{1}{4}$ of 16 , and $\frac{1}{4}$ of a number is 25 per. cent. of it.
8. What per cent. of 140 is 5 ? 10 ? 14 ? 21 ? 35? 105? 112 ?
9. A man bought a horse for $\$ 145$, and paid 40 per cent. of it in cash and the balance by note: find the amount of the note.

Sol. -40 per cent. of $\$ 145=\frac{2}{5}$ of $145=\$ 58 . \cdot$ note $=\$ 145-\$ 58=\$ 87$.
10. A boy lost 20 per cent. of his marblea, sold 25
per cent. of the remainder, and had $36 \mathrm{le}_{2} \mathrm{z}$ : how many had he at first?

$$
\text { Sol. }-20 \text { per cont lost }=\frac{1}{5} \text { loss. } \cdot \frac{4}{6} \text { rem. : } 25
$$

per cent. of this sold $=\frac{1}{4}$ sold. $\therefore \frac{3}{5} \mathrm{rem} .=36$, $\therefore$. \&c.
11. 80 per cent of $\$ 250$ is $62 \frac{1}{2} \mathrm{per}$ cent. of what u:y watch cost : find the cost.
12. In a school, 20 per cent. of the scholare are in the 5th class, each of the next three classes contains $18 \frac{1}{3}$ per cent. of the remainder : what percentage of the school is in the primary class?

Sol.-20 per cent. in 5 th class $\therefore 80$ per cent. $=\frac{4}{5}$ in the other classes ; $18 \frac{1}{3}$ per cent. $\times 3=$ 55 per cent. $=\frac{1}{2} \frac{1}{2}$, and $\frac{1}{2} \frac{1}{6}$ of $\frac{4}{5}=\frac{1}{2} \frac{1}{5}$ in three of remaining classes $\therefore{ }_{6}^{4}-\frac{1}{2} \frac{1}{6}=\frac{9}{2}=36$ per cent. in last class.

## Examples.-3.

1. If I add $\frac{1}{2}$ of unity to itself, what fractional part of the sum must I take off so that tho remainder may be unity?
2. What part taken from a number is equal to of the remainder?

Sol.-The remainder $+\frac{1}{4}$ of rem. ( $=\frac{5}{4}$ rem.) $=$ given number.$\cdot \frac{4}{5}$ of number $=$ rem., and $\frac{1}{5}$ has to be subtracted.
8. To a number $\frac{1}{8}$ of itsclf is added, what part must be taken from the sum to get the number?
4. What part taken from a number is equal to $\frac{g}{B}$ of the remainder 9
5. To a certain number $\frac{3}{8}$ of itself is added : what part must be subtracted from the sum to get the number?
6. How does the mumerator of the part subtracted, compare with the numerator of what is added?
7. How does the denominator of what is taken off compare with the numerator and the denominator of what is added?
8. What per cent. taken from a number is equal to 40 per cent. of the remainder?

Sol.-Rem. +40 per cent. of rem. $=140$ per cent. of rem. $=\frac{7}{5}$ of rem. = given number $\therefore$ rem. $=\frac{5}{7}$ of given number, and $\frac{3}{7}$ or $288_{7}^{4}$ per ceint. must have been taken off.
8. What per cent. subtracted from a number is equal to 25 per cent. of the remainder?
10. 30 per cent. is added to a number: what per cent. must bo taken from the sum to give the original number?
11. When $12 \frac{1}{2}$ per cent. is added, what per cent. subtracted will sive the number that was increased?
12. 40 is 8 per cent. of what?

Sol.-8 per cent. $=\frac{{ }_{1}}{80}$ of it $=40 \cdot \cdot \cdot \frac{1}{10}=5$, and number $=500$.
18. If I take off $\frac{1}{6}$ of my price when selling an uticle, what per cent. of my price is left?
14. If I ask 96 cts . for a book and take off $12 \frac{1}{2}$ pur cent., how much do I get for it?
15. What per cent. must I add to the price of an article, so that when 1 take off 10 per cent. for eustomer I may neither lose nor gain 1

## Section II.-Cormission.

## Examples.-4.

1. A man received $\$ 45$ for selling goods on a com mission of $2 \frac{1}{2} \%$ : find the price at which the goods sold.

$$
\begin{aligned}
& \text { Sol. }-2 \frac{1}{2} \%={ }_{4}^{1} \frac{1}{6} \text { of price }=\$ 45 \therefore \text { price }=40 \times \\
& \quad 45=\$ 1,800 .
\end{aligned}
$$

2. Paid $3 \frac{1}{8} \%$ for coilecting a debt of $\$ 320$ : rhat sum do I receive?
3. An auctioneer sells goods on a commission of $2 \frac{1}{4} \%$ : what will he receive on a sale of 2,500 dollare' worth ?
4. A broker sold $\$ 6,000$ Bank of Commerce stock, on a commission of $\frac{5}{8}$ per cont. : find amount of his commission.
5. At $\frac{4}{5}$ per cent. what will it cost to buy a bill of exchange for $\$ 1,250$ ?

Sol. $-\$ 1,250=12 \frac{1}{2}$ hundreds $\therefore$ com. $=\frac{4}{3} \times 12 \frac{1}{2}$ $=\$ 10$.
6. A Toronto merchant consigns 12,000 bushels of wheat to his agent in Montreal, who sells it at $\$ 1.20$ a bushel, on a commission of $1 \frac{3}{4}$ per cent: find the amount of the commission.
7. A planter paid his agent in New York $\$ 125$ for selling $40,000 \mathrm{lbs}$. of cotton, on a commission of $2 \frac{1}{2}$ per cent. : for what price per lb, was the cotton sold? Sol.- ${ }_{4}^{1}{ }^{1}$ of cotton $=1,000 \mathrm{lbs}$. went for commission $=$ in value $\$ 125 \therefore$ cotton $\$ \frac{1}{5}$, or $1 \%{ }_{j}$ ctas.

8a. An agent receives $\$ 225$ for selling goods to the value of $\$ 5,000$ : find his rate per cent. cf commission.

$$
\begin{aligned}
& \text { Sol. }-\$ 5,000 \text { gives } \$ 225 \text { com. : } \$ 1 \text { gives } \mathbf{S O N O}^{25}
\end{aligned}
$$

$$
\begin{aligned}
& \text { Or } 50 \times 100(=5,000) \text {, gives } 225 \therefore 100 \text { gives } \\
& 225 \div 50=4 \frac{1}{2} \text {. }
\end{aligned}
$$

8. An agent received $\$ 117$ for selling 800 barrels of flour, at $\$ 6.50$ : find his rate of commission.
9. A tax collector receives $1 \frac{1}{2}$ per cent. for all sums paid within 30 days, and 3 per cent. for all paid after that time : the taxes are $\$ 45,000$, of which $\$ 25,000$ is paid within 30 days: find the whole amount of the collector's fees.
10. A druggist sends his agent $\$ 630$ with which to buy goods, after deducting his commission, 5 per cent. on the price paid for the goods : find the agent's commission.

Sol.-For every $\$ 105$ sent, the agent receives \$5 $\therefore$ he receives $\frac{1}{21}$ of whole amount sunt $=$ ${ }_{2}^{1} \mathrm{~T}$ of $\$ 630=\$ 30$.
11. A manufacturer sent $\$ 2,601$ to a wool dea . . with which to purchase wool, allowing him 2 per cent. for the money paid out : how much would be invested in wool?

12a. An agent sold flour on a commission of 3 per cent., and with the proceeds, minus his commission for both transactions, purchased tea on a commission of 2 per cent. on the price paid for it; his entire commission waa $\$ 200$ : find amount received for the tom

Sol. (1.)-3 per cent. +2 per cent. $=5$ per cent. If 5 per cent. ( $=\frac{1}{2 \sigma}$ ) had been charged on the whole amount of sales, the com. would have been 2 per cent. of $\$ 200=\$ 4$ more, i.e., the entire com. would have been $\$ 200+\$ 4=\$ 204=\frac{1}{20}$ of sales, which $\therefore$ amounted to $20 \times 204=\$ 4080$. Further : if the 5 per cent. com. had been taken on amount of purchase money, the entire com. would have been 3 per cent. of $\$ 200=\$ 6$ less than it was, $=200-6$ $=\$ 194=\frac{2^{-0}}{0}$ of amount of purchase, which $=\therefore \$ 3880$. See " Exam. Papors in Arith-metic."-Preface.
Sol. (2.)-It will be found that un every $\$ 102$ from sale there is $\$ 5$ entire commission : Suppose we allow for com. on purchase, \$2 of the 102 , leaving $\$ 100$. For com. on sale, $\$ 3$ of the $\$ 100$, leaving $\$ 97=\$ 5 \mathrm{com}$.

In the former case we have charged 2 per cent. of $\$ 3=6$ cents too much. But in the latter case we have charged 3 per cent. of $\$ 2$ $=6$ cents too little. i.e., the excess equals the deficit, and we have still $\$ 5$ entire commission. Then, ${ }_{\frac{5}{0} 5}^{5}$ of sales $=\$ 200$ $_{10}^{102}=$ $\$ 40$, and the whole $=\$ 4,080$.

It is seen from the above that the com. $=$ $T^{\frac{5}{0} 2}\left(=T_{0}{ }^{5}+2\right.$ ) of the sales; and equals ${ }^{5}=$ ( $=10^{5}-8$ ) of purchase money.

Sol. (3.)-The formal analysis is : Take 8100 for reference. $\$ 3=\mathrm{com}$, on sale : $\boldsymbol{T}_{0}^{\mathrm{I} 2}$ of ( 100 $-3)=\mathrm{com}$. on purchase. $\cdot$. Entire com. $=\$ 3$

$$
-\frac{6}{10} \overline{2}+\frac{200}{0}=\frac{500}{102}=\frac{5}{10} 52 \text { of } 100 .
$$

Nete.-If com. on sale is 4 por cent. and on purchase 3 per cent., the entire com. $=\frac{4+3}{103}=\frac{7}{7} 3$ of sale moncy, and $=\frac{4+3}{98}$; (i.e., $\frac{10}{\mathbf{1} 0}-4$ of purchase money). And generally if we have $n$ per cent. on salcs, and $n$ per cent. on purchase, the entire com. $=\frac{m+n}{\mathrm{i} 10+n}$ of sale money, and $=\frac{m+n}{100-m}$ of purchase money.

12b. A merchant sold tea on a commission of 5 per cent., and purchased (as in last Ex.) cotton on a com. of 3 per cent. ; his entire com. was $\$ 400$ : find amount reccived for the goods,
12. In the last question, find also the amount invested in cotton.
12. A merchant sends his agent $\$ 390$ to expend for goods, after deducting his commission at 4 per cent. on the price paid for the goods : find the agent's commission.
13. A merchant sends his agent $\$ 5,200$ with which to purchase wheat, allowing him a commission of 4 per cent. on the p e paid; he paid 81.25 a bushel : how many bushels did he buy?
14. A commission merchant received 5 per cent. for selling goods, and purchased with the proceeds (after delucting his commission for both transactions) a quantity of oats on a commission of 5 per cent. on the amount paid for the oats: he paid 57 cents a bushel, and his entire comunission was $\$ 60$ : how many bushels did he buy 1

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## Section III. - Insurance.

> Examples.-5.

1. A man effected an insurance of $\$ 1,575$ on his If use, at 2 per cent. premium : how much did he pay?
2. What will it cost to insure $\$ 2,400$ worth of furniture at $\frac{3}{8}$ per cent. premium?
3. A produce dealer paid $\beta^{2} 5$ for an insurance on goods valued at $\$ 800$ : what rate of premium did he pay?
4. An insurance company which charged a rate of $\frac{5}{8}$ per cent. receivel $\$ 22.50$ for insuring a house to the amount of 75 per cent. of its value: find is value.

Sol. $-\$ 5$ from $100 \therefore \$ 1$ from $\$ 160$ and $\$ 22 \frac{1}{2}$ from $22 \frac{1}{2} \times 160=\$ 3,600$; or, $\frac{5}{8}$ from $\$ 100 \therefore$ $22 \frac{1}{2} \div \frac{5}{8}=36=$ no.hundreds, \&c.
5. An 1 surance agent took a risk on a slip at $2 \frac{1}{2}$ per cent., and immediately re-insured 80 per cent. of the risk in another company at 2 aer cent. : the premium received exceeded the premiurn praid by $\$ 225$ : for how much was the ship insured?
6. A farmer paid an agent $\$ 8.25$ for insuring lis baun and its contents at $\frac{1}{2}$ per cent. : for what amount did he insure?

Sol.- $\$ \frac{1}{2}$ prem. on $\$ 100$ insured, and $\$ 1$ on $\$ 200$ $\therefore \$ 8 \frac{1}{4}$ on $\$ 200 \times 8 \frac{1}{4}=\$ 1,650$.
7. For how much must I insure at 4 per cent. a property worth $\$ 3,600$, so as to suffer no loss in case the property is destroyed $?$

Sol.-I must receive both value of property and premium paid, and since the premium is $4 \%$ of amount insured, the property must be $100 \%-4 \%=96 \%=\frac{2}{2} \frac{4}{3}$ of amt. insured, $\therefore \frac{2}{2} \frac{4}{5}$ of this amt. $=\$ 3,600$ and amt. $=\$ 3,750$.
8. For how much must a house costing $\$ 1,470$ be insured at 2 per cent., so that the owner, in case of loss, may recover its value and the premium paid?
9. A ship's cargo is valued at $\$ 28,500$ : what premium must be paid at 5 per cent. so that in case of shipwreck the insurer may suffer nu loss?
10. My property is worth $\$ 4,800$ : what is the tax on it at $1 \frac{1}{4}$ per cent. $?$

10 a. The tax on a lot worth $\$ 500$ is $\$ 6$ : what is the rate on the dollar?

Sol. $-\$ 500$ gives $\$ 6$..$\$ 1$ gives $\$_{5}{ }_{0}^{6}{ }_{0}=1 \frac{1}{5}$ cents $=12$ mills.
11. At 17 milis on the dollar my income tax is $\$ 25.50$ : on what amount do I pay income tax?
12. A man who owns property to the amount of $\$ 4,250$ pays $\$ 72.25$ in taxes : find the rate in the dollar.
13. A tax collector pays $\$ 11,400$ to the treasure of a municipality, after deducting his commission al 5 per cent. : how much did he collect?

Sol. $-5 \%=\frac{1}{2} 0$ for collecting $\therefore \frac{19}{2}{ }_{0}$ left $=\$ 11,40($ $\therefore \frac{1}{20}=\$ 600$, etc.
14. For how much must a town assess itself so as to allow the collector 4 per cent. and still realize $\$ 18,000$ ?
15. What is the duty on 750 gallons of wine at $\$ 1.20$ a gallon?
16. A lot of books is invoiced at $\$ 775$ : find the duty at 5 per cent.
17. Paid a specific duty of 50 cents a gallon and an ad vaiorem duty of $17 \frac{1}{2}$ per cent. on 500 gallons of brandy : find the amount of duty paid.
18. A man owns $\frac{7}{64}$ of a ship worth $\$ 40,000$. It is insured for a certain voyage at 2 per cent : find amount of his premium.

## Section IV.-Profit and Loss.

Examples.-6.

1. A man bought tea at 45 cts . a lb., and sold it at 65 cts : find his gain per cent.

Sol.-45 gains $10 \therefore 1$ gains $\frac{1}{4} \frac{0}{5}$, and 100 gains $\frac{1}{4} \frac{0}{5} \times 100=22 \frac{2}{9}$.
2. A merchant bought flour for $\$ 6$ a bbl., and sold it at $\$ 7.50$ : find his gain per cent.
3. Bought cloth at 80 cts. a yard, and sold it at $\$ 1.10$ : find the gain per cent.
4. Bought a quantity of wheat at $\$ 1.20$ per bushel, and sold it at $\$ 1.10$ : find the loss per cent.
5. An apple-woren bought apples at $\$ 1.25$ per hundred, and sold them at 2 cents each: what was her gain per cent?
6. Invested $\$ 4,500$ in flour at $\$ 6.75$ a bll.; sold it at $\$ 7.50$ a bbl. : find entire gain.
7. A man sold a horse for $\$ 150$, which was $\frac{3}{8}$ of what he paid for it: find his loss per cent.
8. A merchant bought 300 barrels of flour at $\$ 5$ a bbl., sold two-thirds of it at $\$ 8$ a bbl., and the rest at cost: find his gain per cent.
9. A grocer sells 8 lbs. of tea for what 9 lbs. cost him : what is lis gain per cent?

Sol.-He gains 1 ll . on 8 , or $\frac{1}{8}$ on $1 . \therefore$ gain

$$
=12 \frac{1}{2} \%
$$

10. Bought a horse for twenty per cent. less than $\$ 150$, and sold him for 10 per cent. more than \$150: find gain per cent.
11. I sold goods to $\mathbf{A}$ at 10 per cent. profit; $A$ sells them to $B$ at 20 per cent. profit: what per cent. should I have made if I had sold directly to $B$ at the price A received $?$
12. A merchant marks his goods at an advance of 25 per cent. on cost; what per cent. must he reduce his marked price to sell certain danaged goods at cost?

Sol. $-\frac{5}{4}$ of cost $=$ selling price $\therefore \frac{4}{5}$ of latter $=$ cost, $\frac{1}{5}$ off selling price $=20$ per cent. ouf.

$$
\text { Examples. - } 7 .
$$

1. Bought tea at 50 cents per lb ., and sold it so as to gain 25 per cent.: find the selli:g price.

$$
\text { Sol. }-25^{\circ} \text { per cent. }=\frac{1}{4}, \text { and } \frac{1}{4} \text { of } 50=12 \frac{1}{2} \therefore
$$ $50+12 \frac{1}{2}=62 \frac{1}{2}$. Ans.

2. Land was bought at $\$ 20$ an acre, and sold so as to gain 45 per cent. : find the selling price.
3. A grain merchant bought wheat at $\$ 1.20$, and sold it at a loss of 15 per cent. : find the selling price.
4. A merchant "marks down" a lot of old goods 121 per cent.: what will be the price of cloth for which his price had been $\$ 3.68$ a yard?
5. A town had a population of 4,045 in 1870 ; in 1875 the population had decreased $11 \frac{1}{y}$ per cent. : find its population at latter date.
6. By selling cotton at 12 cents a yard, there is a gain of 20 per cent. : what was the cost price?

$$
\text { Sol. -20 per cent. }=\frac{1}{5} \therefore 1 \frac{1}{5} \text { cost }=12 \text {, and }
$$ cost $=10$.

7. A merchant sold rea at 64 cents, gaining 33$\}$ per cent. : find the cost of the tea.
8. $\Lambda$ man sold his honse for $\$ 2,400$, which was $2:$ per cent. below cost: find the cost.
9. A drover sold 120 sheep for $\$ 504$, gaining 24 per cent.: what did they cost him a piece?
10. A grocer bought coffee so that he could sell it at 36 cents and make a profit of $33_{3}^{1}$ per cent. : find the cost.
11. By selling cigars at 65 cents a dozen, 30 pe, cent. was gained: what selling price would have. gained 60 percent. ?

Sol. $-13{ }_{10}^{3}$ cost $=65 \therefore$ cost $=50$, ald 60 per cent., we have $50+30=80$.
12. B sells a lot to C , and gains 121 per celct. C seils it to D for $\$ 1,180$, gaining 18 per cent. : vhard did the lot cost B ?
13. A merchant gains 30 per cent. by selling maslin at 39 cents a yard : by what selling price would he lose 40 per cent. 7

Sol. $-\frac{13}{10}$ cost $=39 \therefore$ cost $=30-40$ per cent. of this $=18 \mathrm{c}$.

## Examples.-8.

1. A horse was sold for $\$ 180$, which was 10 per cent. less than it cost: what was the cost?
2. By selling coffee at 30 cents a pound, there is a loss of 20 per cent.: what selling price would have gained 20 per cent. $?$

Sol.-Sold for $\frac{4}{5}$ of cost ; to gain 20 per cent. it must sell for $\frac{6}{5}$ of cost, which is one-half more than $\frac{4}{6} \cdot \cdot 45$ cents.
8. A man sold a horse and carriage for $\$ 480$, losing 4 per cent. ; if he had sold them at $\$ 600$ what would he have gained per cent.?
4. A man sold two lots at $\$ 400$ each : on one he lost 20 per cent., and on the other he gained 20 per cent : how much did he gain or lose on the whole?

Sol. $-\$ 400=1 \frac{1}{5}$ cost of one $=\frac{4}{5}$ cost of the other $\therefore$ costs are $\$ 500,333 \frac{1}{3}$, etc.
5. What must be the marked price of cloth that cost $\$ 150$ a yard, so that the seller may reduce his price 10 per cent. and still make 20 per cent. profit?

Sol. $-\frac{9}{40}$ of marked price $=1 \frac{1}{6}$ cost $=\$ 1.80 . \cdot$ marked price $=\$ 2$.
6. If 10 per cent. more is gained by selling a horse for $\$ 280$, than by selling him for $\$ 260$, find his cost price.
7. A merchant invested $\$ 1,096$ in broadcloth; he marked it at an advance of 20 per cent. on cost, but finally took 20 per cento less than he asked: find his entire lome

Sol.-100 sold for 120: 20 per cent of this= $24,120-24=96 . \cdot 4$ lost on $100=4$ per cent.
8. By selling a house which cost $\$ 4,800$, I gained $7_{1 / 3}^{9}$ per cent. of the selling price: find the selling price.
9. By selling tea which cost 48 cents a lb., I lost $11 \frac{1}{9}$ per cent. of the selling price: what was the loss per cent. on the cost?

Sol. - $\frac{1}{9}$ of selling price lost $\cdot \therefore \frac{10}{5}$ of do. $=$ cost $\therefore$ If cost lust $=10{ }_{2}^{1}$ per cent.
10. I sold one farm which cost $\$ 6,000$, at a gain of $16 \frac{2}{3}$ per cent. of the selling price, and another which cost $\$ 7,200$ at a loss of 20 per cent. of the selling price: fud my whole gain or loss per cent.
11. How many yards of cloth at $\$ 4$ a yard must a merchant buy, so that by selling it at 10 per cent. profit he may gain $\$ 24$ ?

Sol.-10 per cent. of $\$ 4=_{5}^{2}=$ gain on 1 yard and $\$ 24=$ gain on $24 \div \frac{2}{5}=60$ yards.
12. At what must I mark goods that cost 60 cents per yard, so that I can take off 20 per cent. for a customer and neither gain nor lose?

Sol. - $\frac{1}{5}$ off marked price $=$ cost $\cdot \cdot \frac{1}{4}$ (or 25 per cent.) added to cost $=$ selling price.
13. At what must I mark goods that cost 50 cents per yard, so that I can take off 10 per cent. for a customer and have 13 cents profit?
14. At what must I mark a book which cost 97 cents, so that after taking off $12 \frac{1}{2}$ per cent. for a customer I may lose 6 cents,

## MENTAL ARITHMETIC.

15. Cloth which cost 96 cents a yard was sold at a profit of 25 per cent., and $\$ 16$ was gained in all : how many yards were there?
16. A boy bought peaches at the rate of 3 for 10 cents. and sold them at the rate of 5 for 20 cents.: what did he gain per cent. ?
17. At what must I mark goods worth 96 cents per yard, so that I can take of 20 per cent. for a customer and have 25 per cent. profit?

$$
\begin{aligned}
& \text { Sol. }-96+25 \text { per cent. of } 96=120 ; \frac{1}{5} \text { off marked } \\
& \text { price }=120 \cdot \cdot .120+\frac{1}{4} \text { of } 120=150 .
\end{aligned}
$$

18. At what must I have marked goods that cost $\$ 1.80$ per yard, that arter taking off 10 per cent. I lost 6 per cent. ?
19. Sold a lot for $\$ 230$, which was 8 per cent. less than it cost : had it been sold for $\$ 300$ what would have been the gain?
20. Bought a quantity of apples at 80 per cent. off the market price, and sold them for 10 per cent. more than the market price : find the gain per cent.
21. A man sells wheat at 90 cents a bushel, and gains $12 \frac{1}{2}$ per cent. : what will he gain or lose per cent. by selling it at 85 cents a bushel?
22. A grocer bought 40 llbs. of tea for 80 cents a lb., and intended to sell it so as to gain 25 per cent., but by unintentionally using a false balance, he really gains $33 \frac{1}{3}$ per cent. : how many ounces did he give for alb?

$$
\begin{aligned}
& \text { Sol.-Cost }=\$ 32 \text {, selling rrice }=\$ 32+\frac{1}{3} \\
& \text { of } \$ 32=. \$ 42 \frac{2}{3}, \text { which at } \$ 1 \text { nominal lb. }
\end{aligned}
$$

represents $42 \frac{2}{3}$ lbs. (false) $=40$ (true) $\therefore 1$ false $=40 \div 42_{3}^{2}=\frac{15}{16}$ true.$\cdot 15$ ounces to lb .
23. I bought a horse for $\$ 100$, which was $16_{3}^{2}$ per vent. less than his real value, and sold him for 10 per cent. more than his real value on a credit of $3 \frac{1}{3}$ years, money being worth 10 per cent. per annum : did ! gain or lose, and how much?
24. The workmen in a New Brunswick ship-yard who work 11 hours a day, demand that the day's work be decreased by one hour ; the employers agree to grant an equivalent to the demand by increasing the wages, the hours to remain the same: what increase per cent. in wages should be made?
25. The imports of Prince Edward Island amount to $1 \frac{1}{2}$ million dollars annually, and the exports to 2 millions, each peison on an average contributing $33 \frac{1}{3}$ per cent. more to the exports than he receives from the imports, both for one person being $\$ 35$ : what is the population of the island?
26. A man marks his goods 20 per cent. above cost; $\mathbf{5}$ per eent. of his sales are bad debts on whic! he only receives 10 per cent., the cost of collecting is 2 per cent.: find his gain or loss per cent.
27. In a mixture of wine and water, 20 per cent. of the whole is water; 20 gallons more wine are added, and now the water is only 4 per cent. of the whole: how many gallons of wine were there at Cirst 8

Sol.-At first ${ }_{5}^{1}$ water $\frac{4}{5}$ wine, i.e., wine $=1$ times water. Then $\frac{1}{2} 5$ water $\frac{24}{2} \frac{4}{5}$ wine, i.e., wine $=24$ times water.$\therefore$ wine $=20$ times water must have been added . $\cdot 1$ gallon of water and 4 wine.
28. A school-room not containing seats for six of the pupils, the number of seats was increased $33 \frac{1}{3}$ per cent., and now there are seats for 12 more than the whole number of pupils, allowing two pupils to a seat: how many pupils were there in the school?

## Section V.-Stocks and Shares.

$$
\text { Examples.- } 9 .
$$

1. How much cash will be realized by selling out $\$ 4,000$ stock in Dominion 5's at $95 \frac{1}{4}$ ?

Sol. $-\$ 100$ brings $95 \frac{1}{4}$ cash $. \cdot \$ 4,000$ bringn $40 \times 95 \frac{1}{4}=\$ 3,810$.
2. What eash will be obtained by the sale of $\$ 7,800$ 3 per cent. stock at 89 ?
3. What amount will be received by selling out $\$ 4,500$ Dominion 6's at $106 \frac{3}{8}$, allowing brokerage ${ }_{8}^{1} 7$

Sol.-Every $\$ 100$ brings $106 \frac{3}{8}-\frac{1}{8}=106 \frac{2}{8}$, \&c.
4. Find amount realized by the sale of $\$ 5,000$ Bank of Commerce stock at $120 \frac{5}{8}$, allowing $\frac{1}{8}$ for brokerage.
5. How much stock can be bought at 92 for $\$ 2,760$ ? Sol. - 92 will buy $\$ 100$ stock.$^{\cdot}$. given sum will buy ${ }^{2} \frac{7 \pi}{9} 0 \times 100=30 \times 100=\$ 3,000$.
6. Hew much stock can be bought at $92 \frac{1}{2}$ for $\$ 1,480$ ?
$10=4$
7. How much stock will $\{1,200$ buy in the 4 per cents at 75 ?
8. How much Dominion 3 nk Stock at 120 can be hought for $\$ 5,400$ ?
9. How much will $\$ 2,1^{\prime}$ : buy in the 3 per cents at $91 \frac{1}{2}$, allowing brokerage $\frac{1}{8}$ ?
10. What semi-annual income will be derived from investing $\$ 9,000$ in Dominion Bank Stock at 120, and paying 4 per cent. half yearly dividends 3

Sol.-1 20 will buy 100 stock, which brings $\$ 4$ income, and $\frac{4}{120}=\frac{1}{2} \quad \therefore$ income is $\frac{1}{16}$ of investment ; $\frac{1}{1}_{5}^{15}$ of $\$ 9,000=\$ 600$.
11. What income will be derived from an invest. ment of $\$ 2,940$ in 4 per cent. stock at 98 ?
12. What semi-annual income will be derived from investing $\$ 3,195$ in stock selling at $88 \frac{3}{4}$, and paying 3 per cent. half-yearly?
13. What income will be received from investing $\$ 3,360$ in $5 \frac{1}{2}$ per cent. stock at 96$\}$
14. What income is got from investing $\$ 7,450$ in 3 per cent. stock at $74 \frac{3}{8}$, allowing brokerage $\frac{1}{8}$ ?

Sol. - 100 stock costs $744_{8}^{3}+\frac{1}{8}=74 \frac{1}{2}$, and lyings $\$ 3$ income, and $7450 \div 74 \frac{1}{2}=100 .{ }^{\circ}$. income $=100 \times 3=300$.

## Examples-10.

1. If $I$ invest in 7 per cent. stock at 120 , what ste of interest do I obtain?

Sol. $-\$ 120$ buys 100 stcck, which entitles me to $\$ 7 . \because \$ 1$ brings $\frac{7}{1} \frac{7}{2}$ income $=\frac{7}{\frac{7}{2}}{ }^{5} \times 100$, per cent. $=55$.
2. Bought stock in the 3 per cents at 80 : what rate of interest was realized?
3. Invested $£ 8,750$ in the $3 \frac{1}{2}$ per cents at $87 \frac{1}{2}$ : find the rate per cent. obtained from the investment.
4. Invested in railway stock selling at 85 and paying 5 per cent. dividends: find rate of interest.
5. What per cent. is obtained by investing in $3 \frac{1}{2}$ per cent. stock at 75 ?
6. What amount of bank stock at 120 must be sold to prodrce $\$ 1,800$ cash?

Sol.- $\$ 120$ cash is got from $\$ 100$ ctock, and $\$ 1$ from $\frac{100}{1} \frac{0}{0}=\frac{5}{6} \cdot \cdot 1,800$ from $5 \times 1,800=$ 1500.
7. When the English funds are at 75, what stock must be sold to realize £125?
8. What amount of 8 per cent. stock at $\$ 125$ musi be sold to produce $\$ 3,750$ eash ?
9. What amount must be sold of Dominion 5's at 921 to produce \$G66?
10. What amount must be sold out if the $17 \frac{1}{2}$ per cents at 128 to produce $\$ 1,024$ ?
11. What sum must be invested in 8 per cent. stock at 120 to give ineome of $\$ 200$ ?

> Sol.-8 arises from $120 \therefore 1$ from $15 \& 200$ from $200 \times 15=3,000$.
12. What sum must be invested in 8 per cent. stock at 120 to give an income of $\$ 320$ ?
13. What sum must, be invested in the 5 per cents at 90 to give an ineome of $\$ 375$ ?
14. What sum must be invested in the $4 \frac{1}{2}$ per cents at 67 to produce $\$ 279$ income?

## Examples.--11.

1. Which is the better investment, insurance stock at 140 and paying 12 per cent. dividends, or bank stock at 120 and paying 9 per cent. dividends?

Sol.-In first case, 140 brings $12 . \cdot 1$ brings $\frac{14}{140}={ }_{3}^{3}{ }^{3}$.

In second case 120 brings $9 . \therefore 1$ brings $\frac{9}{2} 0=\frac{3}{40}$, and the first fraction is greater than the second.$\because 1$ st is better investment.
2. Which is the better investment, the 6 per cents at $98 \frac{1}{2}$, or the 5 per cents at 85 , brokerage in each case being $\frac{1}{2}$ ?
3. Which is the better investment, 5 per cent. stock at 95 , or 6 per cent. at 106 ?
4. $\Lambda$ mau having $\$ 12,500$ Dominion Bank stock paying 8 per cent., sells out at 120 , and invests in Bank of Commerce stock at 125 , and paying $8 \frac{1}{2}$ per cent. : find alteration in his income.

Sol.-Income from D. B. $-8 \times 125=\$ 1,600$. The D. B. sells at $\frac{1}{5}$ advance, giving $\$ 15,000$ 125 in B. C. gives $8 \frac{1}{2} \cdot \therefore 1,000$ gives 68 , and 15,000 gives $68 \times 15=1,020 . \therefore 1,020-$ $1000=\$ 20$ inerease.
5. Low much stock at 140 can be boaght by selling out $\$ 14,000$ of a different stock which is at 120 ?

Sol.- $\$ 1$ of latter stock will buy $\$ \frac{120}{120}=\$ \$_{7}^{6}$ of former . $\cdot$ given amt. will duy $\$ \frac{0}{7} \times$ $14,000=\$ 12,000$.
6. How much stocis at 95 anu be bought by selling put $\$ 3,80^{\prime}$ of a diflenent stock at 120 ?
7. How much stock at $99{ }_{4}^{3}$ can be bought with the proceeds of $\$ 4,200$ of a different stock at 95 ?
8. When gold is at $102 \frac{1}{2}$, what is the discount on greenbacks?
9. I invested a certain sum in railway stock at 80 and paying 5 per cent. dividends, and an equal sum in bink stock at 120 , and paying 8 per cent.; the difference in the two incomes was $\$ 12$ : find the amount invested in each kind of stock.

Sol.-The first pays $\frac{1}{16}$, the second $\frac{1}{15}$ (of amt. invested) $\therefore \frac{1}{15}-\frac{1}{16}=\frac{1}{240}$ of amt. $=\$ 12 \therefore$ ant. $=\$ 3,880$.
10. A certain sum was invested in 4 per cent. stock at 80 , and an equal sum in 5 per cent. stock at 95 ; the difference in incomes was $\$ 10$ : how much was in. vested $?$
11. A sum of money was invested in insurance stock selling at 144 , and paying 12 per cent. dividends, and twice the amount was invested in bank stock selling at 120 , and paying 8 per cent. dividends; the income from the latter investment was $\$ 125$ greater than that from the former : how much was invested in each stock?
12. A person sells $£ 1,250$ stock of the 3 per cent. consols, when the funds are at 96 , and invests the proceeds in railway stock at 75, paying an annual dividend of $2 \frac{1}{2}$ per cent. : find the alteration in his income.
13. How much 3 per cent. stock must be bought at $88 \frac{1}{2}$ in order that by selling out at $88 \frac{3}{4}$, there may be a gain of $\$ 21$ ?
14. A person sells $\$ 2,400$ stock at 95 , which pays 5 per cent. in order to invest in 6 per cent. stocr •
what price must he pay for the latter that his income may remain unaltered.

Sol.-lncome per ann. in lst catse $=\frac{5}{9} 5=\frac{1}{15}$
$=$ income per ann. in the 2nd cuse $={ }_{6 \times 19}^{6}$
$={ }_{1} \frac{6}{14} \therefore 114$ is the price.
15. A man invests $\$ 19,450$ in Bank of Montreal stock at 104, and \$19,850 in Bank of Toronto stock at 198, paying in each ease brokerage $\frac{1}{2}$ per cent. on stock purchased: the former pays $6 \frac{1}{1}$ per cent., the latter $6 \frac{1}{4}$ per cent. half-yearly dividends: find the total income for the half year.

## Section VI.-Interest.

Examples.-12.

1. At 8 per cent. for 4 years, what part of the principal is the interest?

Sol.-Interest for one year $=\frac{8}{10 \%}$, and interest for 4 years $=4 \times \frac{8}{10 \overline{0}}=\frac{8}{85}$.
2. At 8 per cent. for 5 years, what part of the prinwipal does the interest equal?
3. At 6 per cent. for 5 years 8 months, what part of the principal equals the interest?
4. At 8 per cent. for 2 years 9 months, to what part of the principal is the interest equal?
5. Find interest on $\$ 60$ for 6 yeurs, at 5 per cent.? at 6 per cent. $?$ at 7 per cent. $\%$ at 8 per cent. $?$ at $7 \frac{1}{2}$ per cent.?
6. What is the interest on $\$ 600$ for $2 \frac{1}{4}$ years at 4 per eent. $\} 5$ per cent. $\} 6$ per cent. $\} 7$ per cent. 18 percent. $38 \frac{1}{4}$ per cent, $?$
7. What is the interest on $\$ 480$ for 3 years 9 months, at 8 per cent.? at 6 per cent. 7 at 5 per cent. ? at 10 per cent.?
8. Find the interest on $\$ 480$ for 5 years 10 months, at 6 per cent? at 8 per cent. ? at 10 per cent. 9
9. What is the interest on $\$ 300$ for five years, at $3 \frac{1}{3}$ per cent. $\}$ at 6 per cent. $\}$ at $6 \frac{2}{3}$ per cent. 3 at $7 \frac{1}{5}$ per cent.?
10. What is the interest on $\$ 800$ at 8 per cent. for 3 months? for 4 months? for 5 months? for 7 months? for 9 months? for $7 \frac{1}{2}$ months? for 10 months?
11. What is the interest on $\$ 24.50$, at 8 per cent. for 12 months? for 9 months? 6 months? 15 months?
12. What is the interest at 8 per eent. on $\$ 137.50$ for 1 year? for 15 months? 18 months? 14 months? 10 months? 8 months? 7 months? 9 months?
13. What is the interest on $\$ 146$ for 45 days, at 5 per cent. 3

$$
\begin{aligned}
& \text { Sol. }-45 \text { days }=\frac{45}{36} \text { year }=\frac{9}{73}, \therefore \text { interest } \\
& =\frac{9}{73} \times 146 \times \frac{50}{\frac{5}{0} \overline{0}}=\$ \frac{9}{10}=90 \text { cents. }
\end{aligned}
$$

14. What is the interest on $\$ 73$ at 6 per cent. for 35 days? 40 days? 50 days? 65 days? 90 days? 95 days? 115 days?
15. Find the interest on $\$ 109.50$, at 8 per cent. for' 40 days? 45 days? 90 days? 120 days?
16. What is the interest on $\$ 182,50$ for 90 days, at 6 per cent. $\%$ at $7 \frac{1}{2}$ per cent. 7 at 8 per cent. 2 at 10 per cent.?
17. Find the interest on $\$ 240$ for 8 months at 6 per cent,

Sol.-At 6 per cent. interest on $\$ 1=\frac{1}{2}$ cent per month $=4$ cts. for 8 months. $\cdot$ interest on $\$ 240=240 \times 4$ cts. $=\$ 9.60$.
18. Interest on $\$ 225$ at 6 per cent. for 4 months? 6 months? 7 months? 8 months? 14 months? $i 3$ months?
19. Interest on $\$ 240$ for 11 months at 6 per cent.? at 7 per cent. $\%$ at 8 per cent. $\%$ at $7 \frac{1}{2}$ per cent. $\}$ at 5 per cent.?
20. Find the interest on $\$ 800$ for 42 days at 6 per cent.?

Sul.-Reckoning a year 360 days, the interest on $\$ 1$ is a mill (ion of $\$ 1$ ) every 6 days, $\therefore$ interest on the above $=\frac{62}{6} \times 800$ (mills) $=\$ 5.60$.
Note.-The interest as found by this rule is greater than the true interest by ${ }_{i=3}$ of itself; in the last example the interest found is too great by nearly 8 cents.
21. What is the rmount of $\$ 75$ for 5 years at 8 per cent.?

$$
\begin{aligned}
& \text { Sol.- Interest }=\frac{2}{5} \text { of } \$ 75=\$ 30 \therefore \text { amount }=\$ 75 \\
& \quad+\$ 30=\$ 105 .
\end{aligned}
$$

22. Find the amount of $\$ 120$ for 4 years at 6 per cent. 3 at 7 per cent. $\%$ at 8 per cent. $\%$ at 10 per cent.?
23. Find the interest, for 7 years 6 months, on $\$ 600$ at 6 per cent., at $7 \frac{1}{2}$ per cent., at o per cent., at 10 per cent.
24. A and B wish to divide the amount of $\$ 800$ for 8 years at 5 per cent., so that A's part shall be 6 times B's.: find each man's share.
25. A's money is $\$ 500$, which is $\frac{1}{4}$ of B's : what interest will cach receive on his money for 15 months at 8 per cent. 3
26. $A, B$, and $C$ have together, $\$ 1201$, of which $B$ has 3 times as much and $\Lambda 4$ times as much as C : find the amount of each man's money for $2 \frac{1}{2}$ years at 8 per cent.

## Exampias.- 13.

1. What principal will, in $2 \frac{1}{2}$ years at 8 per cent., give $\$ 30$ interest?

Sol.-Interest $=8$ per cent. $\times 2 \frac{1}{2}=\frac{1}{5}$ of princi pal $\cdot \cdot$ principal $=83 \times 5=\$ 150$.
2. What principal, in 2 years at 8 per cent., wilh give $\$ 16$ interest? $\$ 12\} \quad \$ 24$ ? $\$ 19.20$ ?
3. What principal, in $5 \frac{1}{2}$ jears at 3 per cent., '.ril give \$11? \$22? \$16.50? \$13.20? \$49.50?
4. I reccive $\mathrm{S}_{1} 160$ interest for 2 years 8 monthe on a sum of money lent at 6 per cent.: find the smm.
5. The interst on $\frac{2}{3}$ of $\Lambda$ 's money for $6 \frac{1}{4}$ years at 8 per cent., is $\$ 125:$ how much money has he at interest?
6. What principal will give $8 S 0$ interest, if lent for 1 year and 8 months, at 9 per cent.?
7. I pay $\$ 98$ annual interest on money borrowed at 7 per cent.: find the amomet borrowed.
8. The interest on the sum of B's money and $A$ 's, for $2 \frac{1}{4}$ years at 8 per cent. is $\$ 360.72$ : A's money is $\$ 204$ more than B's : find each man's money.

Sol.-Interest $2{ }_{4}^{1}$ years $\times 8=18$ per cent.
$=\frac{9}{50}$ of joint sum $=\$ 360.72 \cdot \therefore \frac{{ }^{1}}{0}=-\$ 40.08$
and whole $=\$ 2,004 \cdot \cdot$ shares are $\$ 900, \$ 1104$.
9. The amount due on a note which hat been on intrest for 3 yeurs and 4 months at 6 per cent. is $\$ 720$ : find the face of the note.
10. A had a sum of money at interest for 15 months at 8 per cent and B 4 times as much for 18 months, at 6 per cent.; the sum of their interests was $\$ 23$ : how much had each at interest?
11. What principal will produce 30 cents interest in 25 days at 6 per cent. 3

Sol. $-\frac{25}{365}=\frac{5}{73}$ year $\therefore$ interest $=\frac{5}{73} \times{ }_{3}^{3} \quad 11$ principal $=30$ ets. and principal $=833$.
12. The interest on a note for 100 days at 8 ןי•• cent. is $\$ 2.40$ : find the face of the note?
13. The interest on a sum of money at 10 per cent. for 1 year and 20 days, is $\$ 77$ : find the sum.
14. The anount required to pay a note which has run 150 days at 8 per cent. is 8730 : tind lace of the note.

## Examples.-14.

1. The interest on $\$ 400$ at $\delta$ per cent. for a certain time is $\$ 60$ : find the time?

Sol.-At 5 per cent. $\$ 20$ is the interest for one year $\cdot \$ 00$ is the interest for $\frac{60}{20}$ years $=3$ years.
2. In what time will $\$ 40$ make $\$ 8$ interest at 2 prent?
3. I lent $\$ 720$ at 6 per cent. and received $\$ 140$ interest: for how long was the money lent?
4. The interest on $\$ 02.50$ at 8 per cent. was $\$ 12$ : how long was it on interest?
5. In what time will $\frac{100}{} 10$ at per cent. give $\$ 120$ interest?
6. The interest on a note for $8: 20$ at $6 \frac{1}{4}$ per cent. was $\$ 40$ : for what time was the note drawa?
7. In what time will $\$ 90$ make $\$ 10.80$ interest at 6 per cent. ?
8. In what time will $\$ 125$ amount to $\$ 137.59$ at 8 per cent.?
9. In what time will $\$ 64$ amount to $\$ 76.20$ at ? per. cent.?
10. It required $\$ 1,520$ to discharge a note drawn for $2 \frac{1}{2}$ yoars, at $7 \frac{1}{2}$ per cent. : find the face ?
11. In what time will a sum of meney double itselt at 8 per cent. $?$

Sol. -It produces $\frac{2}{2}$ of itself $\left(=-\frac{8}{100}\right)$ in ! yenr $\therefore$ it produces a sum equal to itself in $1 \div \frac{2}{2} 5$ years $=12 \frac{1}{2}$ years.
Or, at 1 per cent. it coubles itself in 100 yesiss $\therefore$ at 8 per cent. it doubles itself in $\frac{1}{8}$ of 100 years $=12 \frac{1}{2}$ years.
12. In what time will a sum of money troble itself at 6 per cent. $\}$ at 8 per cent. 3 á 7 per cent. if at 10 per cent.?
13. In what time will a given principal quadruple itself at 8 per cent. ? at 10 per cent. 1 at 20 per cent. $?$
14. The amount of a certain principal for a certain time, at 8 per cent., is $\$ 280$, and at 5 per cent. the amount is $\$ 250$ : find the time and the principal?

Sol. $-\$ 280-\$ 250=\$ 30=$ interest at 3 per cent. for the required time.$\therefore$ interest at 5 per cent $=53 \times \$ 30=550$ and $\$ 250-\$ 50=$
$\$ 200$ the required principal, and $\$ ? 00$ pro duces, at 5 per cent., $\$ 50$ in 5 years, the reguired timo.
15. The amount of a principal for a certain timu at 6 per cent. was $\$ 455$, and at 8 per cent. the amount was 8490 : find the principal and the time.
16. The ano int of a cortain sum of money for a certain time at $7 \frac{1}{2}$ per cent. is $\$ 445$. and the amount at 10 per cent. is $\$ 460$ : required, the time and the prineipai.

1\%. A sum oi money on interest at 6 per cent. amonats to $\$ 300$, and at 10 per cent. for the same time it amounts to $\$ 350$ : find the time and the principal.

$$
\text { Ezamples. }-15 .
$$

1. At what rate will $\$ 120$ in $2 \frac{1}{2}$ years give $\$ 21$ interest:

Sol.-At 1 per cent. for $2 \frac{1}{2}$ years the interest
$={\underset{1}{1} 0}_{1}^{0}$ of principal $=\frac{1}{4} 0$ of $\$ 120=\$ 3$, and if $\$ 3$ come from 1 per cent., $\$ 21$ will come from $21 \div 3=7$ per cent.
2. At what per cent. will $\$ 30$ in $2 \frac{1}{2}$ years give $\$ 20$ interest?
3. If the interest on $\$ 450$ for 3 years and 4 months is $\$ 70$, find the rate per cent.
4. At what rate per cent. will $\$ 200$ make $\$ 49$ interest in $3 \frac{1}{2}$ years?
5. At what rate will $\$ 300$ make $\$ 88$ interest in 1 yaar and 10 months?
6. At what rats $\because$ iil 9800 make $\$ 75$ interest in 1 year and 3 months?
7. At what rate per cent. will $\$ 2,500$ make $\$ 260$ interest in 15 montis in
8. At what rate will $\$ \hat{0}$ amount to $\mathbb{\$}$ in 3 years and 4 months?
9. At what rete will a givon princioal doweie itsolf in 10 years?

Scl.-In 10 years it gains $\frac{1}{\text { to }}$ of itself at 1 per cent. . $\cdot$. In 10 yeare it gains $10(=1)$ of itself at 10 por cent.
10. At what per cen's will a puincipa! gain 2,3 , 4, 5, 6 times itself in twentoy gears?
11. At what rats per cenc. wiik e civen prinsipel double itself in 10 years? 12 yeare 20 years: 25 years?
12. at what rate will a principal become 212 times itself in 6 yeurs? 8 years? 10 years?
13. The amount of a principal for 4 years at $p$ ce:tain rate per cent. is $\$ 620$, and for 5 gears $\$ 700$ : find the principal and the rate.

Sol. $-\$ 700-\$ 620=\$ 80=$ interest on required pincipa: for $2(=5-3)$ years.$\therefore \$ 120$ ( $=\frac{3}{2} \times \$ 80$ ) $=$ interest for 3 ycars, and required principal $=\$ 020-\$ 120=8500$, end $\$ 500$ gives $\$ 120$ in 3 years, or $\$ 40$ in 1 year $\therefore$ rate $=8$.
14. The amount of a principal for 4 years at a certain rats per cent. was $\$ 600$, and for 6 years, at the same rate, the amount was $\$ 750$ : find the principal and the rate.
15. The amount of a certain principal for 7 years at a certain rate per cent. is $\$ 540$, and for 10 years, $\$ 600$ : find the principal and the rate per cent.
16. The amount of a principal for 4 years at a certain rate per cent, is $\$ 420$, and for 9 years the amount is $\$ 570$ : find the rate and the principal.
17. The amount of a certain principal for $3 \frac{1}{2}$ years at a certain rate per cent. is $\$ 160$, and for 4 years $\$ 165$ : find the principal and dis rate per cent.

18 A note bearing interest for 200 days amounted to $\$ 770$ : find the rate per cent. Face $\$ 730$.

19 c. I paid $\$ 28.50$ interest on a note drawn payable in 95 days : find the rate of interest. Fron $\$ 438$.
19. At $12 \frac{1}{2}$ per cent. what wouli be the bank discount on $\$ 72$ for $4 \frac{1}{2}$ months?
20. At 25 per cent. per annum, what would be the bank discount on $\$ 24.96$, for 9 months?
21. What is the bank discount on $\$ 75$ for 4 monthis, at 13 per $\sim$ nnt. $?$
22. What is the bank discount on $\$ 250$ for 219 days, at 12 per cent.?
23. Find the bank discount on a note of $\$ 27.60$, duawn at 70 days (allow the three days' grace), at $16 \frac{3}{3}$ per cent. 1
24. How much ready money can you get at the bank lor a note of $\$ 6.25$, due in 3 months, discounted nt 16 per cent?
25. What amount must I mark on the face of a note drawn at 9 months, so that when discounted at $13!$ pur cent., I maty get 327.18 ?
26. A banker charged me $\$ 7$ discount on a note of $\$ 140$, due in 8 months: find the rate per cent.?

Sol. $-\$ 7$ for 8 months $=10 \frac{1}{2}$ for 12 , if 140 brings this, 100 will bring $7 \frac{1}{2}$.
27. I pay $\$ 14$ discount on a note of $\$ 250$, at 93 per cent. : find the time for whis t ante was discounted.
28. The difference between the discount on a note and the cash received for $i$ i, was $\$ 264$--the note being discounted for 5 months, at $14 \frac{2}{\overline{3}}$ per cent.: find the face of the note.

## Section VII.-Discount (True). Examples.-16.

1. Find the true discount on $\$ 360$ for three years four months, at 6 per cent.

Sol. -6 per cent. $\times 3 \frac{1}{3}=20$ per cent - ?re-
 present worth $=\$ 300 . \cdot$ disct. $=60$. is we have to add $\frac{1}{5}$ to p . w. to grat the amouint (\$360). $\cdot$ we have to subtra, fiom amount to get p.w., $\frac{1}{6}$ of $360=60$. Note.-It is seen that the disct. =int. on present worth.
2. Find discount on $\$ 162$ for 1 year 4 months, at 6 per cent.; and on 858.58 for $1 \frac{1}{2}$ years, at 8 per cent.
3. What is the present worih of $\$ 1\}$ ? $1, r 1 \frac{1}{2}$ years, at 8 per cent? what is the present worth $5.82 ? 6$, due in 2 years 11 months, at 12 per cent. $?$
4. The simple interest on principal for a certain time and rate is $\frac{1}{5}$ of itseif: what fraction of it is the true discount for the same time and rate? 22.6, due

Sol.-Since the interest of any sum is $\frac{1}{5}$ of itself $\therefore$ the present worth of the prineipal-1 $+\frac{1}{5}$ of this p.w. $=$ the principal ; i.e., $\frac{5}{5}$ of p.w. $=$ the principal, and p.w. $=5$ of the principal $\therefore \frac{1}{6}$ of it is the discount.
5. If the simple interest is $\frac{1}{9}$ of the sum, what fraction is the true discount? if $\frac{1}{7}$ ? if $\frac{1}{12}$ ? if $\frac{1}{8}$ ? if $2_{2}^{1}$ ?
6. Find the discount on $\$ 570$, for 1 year 9 months, at 8 per cent. per annum.

Sol.-At simple interest $\$ 100$ would amount to $\$ 114$; thus $\$ 114$ gives $\$ 14$ discount, $\$ 1$ gives $=1_{114}^{14}=\frac{7}{57}$, and $\$ 570$ gives $\$ 70$.
7. The simple interest of a sum for a certain time and rate is ${ }_{8}^{3}$ of the sum : what fraction is the true discount?

Sol.-Present worth $+\frac{3}{8}$ of present worth $=\frac{11}{8}$ present worth, $=$ given sum $\quad \therefore$ present worth $=\frac{8}{11}$ given sum, and. $\therefore \frac{3}{11}$ of given . sum $=$ discount.
8. If the simple interest is ${ }_{50}^{3}$ of principal, what is the true discount? if $\frac{2}{25}$ \& if $\frac{7}{50}$ ? if ${ }_{b}^{n}$ ?
9. If the true diseount on a sum is ${ }_{4}{ }_{3}$ of it , what is the simple interest? if ${ }_{2}^{3}$ ? ${ }^{2}$ if $5_{5}^{7}$ ? if ${ }^{4}$ ?

Sol. $-1--\frac{3}{43}=\frac{40}{43}=$ present worth, and $\frac{3}{43}$ is the inturest on $\frac{40}{4} . \cdots$ interest on 1 is $\frac{4}{4}_{3}{ }_{3} \div \frac{4}{4} \frac{0}{3}=\frac{3}{40}$ (Note, $\left.={ }_{4}^{4} \frac{3}{3}-\overline{3}\right)$.
10. What fractional part of a note bearing interest at 20 per cent. would you havo to add to it in order to find its value in one year hence?
11. If by adding $\frac{1}{5}$ to its face you get the amount of a n.te one year hence, how much must you take off
the amount of a note due in one year to find its present value?
12. If by adding on 30 per cent., or $\frac{3}{10}$, you get the umount of a note, how much taken off would reduce it again to its present value?
13. How does the numerator of what is taken off compare with the numerator of what is added?
14. How does the denominator of the fractional part taken off compare with the numerator and the denominator of what is added?
15. If adding $\frac{2}{\bar{j}}$ of a note of $\$ 15$ to it make it worth $\$ 2 l$ in one year, what flactional part would you have to take ofl' a note worth $\$ 21$ in one year to find its true discount, an ! what would its tree discount be?
16. Find the true discount on a note of $\$ 54$, due in 6 monthes, at 16 per cent.
17. Find the true discount on a note of $\$ 153$, due in 2 months, at 12 per cent.

$$
\begin{aligned}
& \text { Sul.-Interest }=\frac{1}{50} \cdot \cdot \text { discount }=\frac{1}{41}=\frac{1}{63} \text { of } 153 \\
& =\$ 3 .
\end{aligned}
$$

18. Find the present value of a noie of $\$ 164$ due in 4 months, at $7 \frac{1}{2}$ per cent.
19. If the true discoment for one ycar is $\$ 5$, and the amoment of the note $\$ 15$, find the rate per cent.
20. If $\frac{1}{4}$ taken off gives the bank discount for a certain time and date, what taken off would give the true discount?
21. What is the difference between the bank dis. count and the true discount, at $33 \frac{1}{3}$ per cent., for 1 year 1 for 2 years?

Sol.-For 1 year, interest $=\frac{1}{3} \cdot \therefore$ discount $=\frac{1}{4}$ of principal ; for 2 yours, interest $=\frac{3}{3}$ of principal $\therefore$ discount $=\frac{2}{5}$; difference in former case $=$ $\frac{1}{3}-\frac{1}{4}=\frac{1}{12}$, \&c.
22. What is the difference between the bank discornt and the true discount, at 20 per cent., for 1 year? for 3 years?
23. Find the difference between the bank discount and the true discount on a note of $\$ 126$, at $16{ }_{3}^{2}$ per cent, for 1 year ; for 2 years.
24. Find the difference between the bank discount and the true discoment, on a note cf $\$ 36$, at $12 \frac{1}{2}$ per cent., for 1 year ; for 2 years.
25. Find the difference between the bank discount and the true discount, on a note of $\$ 1,640$, due in 4 months, at $7 \frac{1}{2}$ per cent.
26. If $\$ \dot{\$}$ is the differnec between the bank discount and the true discount, at 10 per cent. for 1 year, what was the amount of the note?
27. If the rate per cent. is 20 , what fraction will the true discount be of the bank discount, for 1 year? for 3 years?
28. If the true discount for a year is $\frac{7}{8}$ of the bank discoment, find the rate per cent. What will be the ratio of the discount to the interest for two years?
29. If the true discount for 6 months is $\$ 10$, and the bank discount $\$ 11$ for the same time, find the rate per cent. and the amount of the note.
30. Find the rate per cent. and the time, if the bank discount of a note of $\$ 120$ is $\$ 8.10$, the rate per cent. being equal to the number of months for which the note was drawn.

Sol. $-\$ 8.10$ is found to be $\frac{81}{\frac{81}{20} 0}$ of principal: At 1 per cont. per annum, the int. for !
 annum, the interest for 9 months would be $T^{8} \frac{1}{2} \frac{1}{\delta}$. Ans. 9 per cent. for 9 months.
31. If $\$ 13$ is the bank discount on a note of $\$ 65$ for 8 months, what would be the true discount on the sime note for 1 year?
32. The simple interest on a sum of money, for a certain time and rate is $\$ 150$, and the true discount is $\$ 120$ : find the sum of money.
33. I lent a man $\$ 100$ for the year 1877, and at the end of the year he returned it, ani lent me $\$ 100$ for the year 1878 , expecting neither of us would have any advantage over the other. How much better off would I be at the end of 1878 if I had invested my $\$ 100$ money being worth 10 per cent.?
34. I have a $\$ 50$ note due in 6 years, not bearing interest: what would I get for it at the bank, discomited at 10 per cent.?
35. I have two notes (l year to run) which are worth $\$ 38$, the one I get discounted at a bank, the other by true discount; th:e whole discount paid is © 7 , rate in both cases 20 per cent.: find the face of the note discounted at the bank.

Sol.-Interest $=\frac{1}{6}$ liscount $=\frac{1}{6}:$ bank discount on ioth notes would havo been $\frac{1}{5}$ of $\$ 38=\$ 7 \frac{3}{5} ; \$ 7 \frac{3}{5}-\$ 7=\frac{3}{5}$ loss: $\$ 1$ gives loss of $\frac{1}{5}-\frac{1}{6}=\frac{1}{3} \pi$. What will give loss of $\left.\${ }_{5}^{3}\right\} \quad \frac{3}{8} \div \frac{1}{3}=\$ 18=$ amount of note on which true discount was taken. $\cdot$. 38-18= $\$ 20=$ do. bank discount.

35a. I had two notes ( 15 months to run) amounting to $\$ 210$; both are discounted at 10 per cent., one at bank discount, the other at true discount-the entire discount being $\$ 25$ : find the face of the nute on which true discount was allowed.
36. The intercst on a certain sum for a certain time is $\frac{1}{19}$ of the principal: what fraction of the principal is the discount for the same time and rate 1
37. The interest is $\frac{3}{5}$ of the principal, and the difference between the interest and discount is $\$ 8$ : find the principal.
38. The interest is $\$ 5$, the discount for same time and rate is $\$ 4$ : what is the sum?
39. In what time, at 8 per cent. simple interest, will the amount be $1 \frac{4}{5}$ of the principal ?
40. The discount on a certain sum for swo years is $\$ 2 \frac{8}{11}$, and the interest for the same time and rate is $\$ 3$ : find sum and rate per cent.
41. The interest is $\$ 40$, and the interest on the discount for same time and rate is $\$ 3_{\frac{7}{1}}^{7}$ : find the discount.
42. The interest is $\$ 2$, and the difference between the interest and discount is $16 \frac{2}{3}$ cents: find the principal.

Sol. $-\$ 2-\$ \frac{1}{5}=\${ }_{6}^{1{ }^{1}}=$ discount and $\$ \frac{1}{\frac{1}{6}}$ is interest on $\frac{11}{6} \therefore$ interest is $\frac{1}{6} \div \frac{11}{6}=\frac{1}{11}$ of principal $\cdot \$ 2 \times 11=22$, the required principal.
43. $\$ 200$ has $\$ 40$ for its interest: find discount for same time and rate.
44. A horse that cust $\$ 90$ is offered far sals on a
credit of 12 months: what price should the sellet ask so that he may fill $9_{\frac{1}{1}}^{1}$ per cent. of his asking price and still have $11 \frac{1}{9}$ per cent. profit, money being worth 10 per cent.?
45. A man bought an article for $\$ 106$ on 12 months' credit and sold it on 9 months' credit, so as to neither gain nor lose: find his selling price, money being worth 6 per cent.
46. A note drawn at 9 months at 8 per cent. interest, is discounted at a bank 6 months before maturity: what fiaction of the face of the note must the bauk give for it to make 10 per cent. on its money? Sol.-At 8 per cent for 9 months the note will amount to ${ }_{53}^{50}$ of its face, banker is to make $\frac{1}{20}$ of his outlay in 6 months. $\therefore \frac{2}{20}$ of outlay $=\frac{53}{50}$ of face of note, and outlay $=$ $\frac{20}{2} \frac{0}{1}$ of $\frac{53}{5}=\frac{106}{10}$ of face of note.
47. A note of $\$ 200$ drawn for six months at 8 per cent. per amum is discounted by a broker 4 months before it is due: what must the broker pay for it in order to make 12 per cent. per annum on his moncy 1

CHAPTER II.

## VARIOUS RULES.

Section I.-Ratio and Proportion.
Examples.-17.

1. What part of 4 is $2 ?$

Sol. - 1 is $\frac{1}{4}$ of $4 . \therefore 2$ is $2 \times \frac{1}{4}=\frac{2}{4}=\frac{1}{2}$. In this case $\frac{1}{2}$, that is, the quotient of 2 by 4 , is called the ratio of 2 to 4 , which is sometimes written 2: 4.
sellet asking being on 12 so as to money cent. inbefore te must money? he note er is to s. $\therefore \frac{2}{2} 0$ outlay= at 8 per months for it in money '
on.

In this , is called ometimes
2. What is the ratio of 3 to $6 ? 4$ to $69 \quad 9$ to $12 ?$ $\$ 10$ to $\$ 12 ? \quad 600$ to 800 ?
3. What part of ${ }_{5}^{4}$ is $\frac{2}{3}$ ?

Sol. $\frac{4}{5}=\frac{1}{1} \frac{2}{5}$, and $\frac{2}{3}=\frac{10}{1}$, and the ratio of 10 units of any kind to 12 units of the same kind is $\frac{10}{10}=\frac{5}{6}=\frac{2}{3} \div \frac{4}{5}$, as in the former case.
4. What is the ratio of $\frac{3}{4}$ to $\frac{5}{5} ? \frac{1}{2}$ to $\frac{9}{10}$ ? $\frac{6}{7}$ to $\frac{5}{8}$ ?
5. What is the ratio of $2 \frac{1}{2}$ to 3 ? $3 \frac{1}{3}$ to $2 \frac{1}{2}$ ? $\frac{8}{9}$ to 2? 6 to $\frac{3}{6}$ ?
6. What is the ratio of $\$ 5$ to $\$ 25\} 3 s .6 d$. to $2 s$. $9 d\}$.1 bush. 1 pk . to 12 qts .?
7. What is the ratio of 1 ft . Gin. to $1 \frac{1}{2} \mathrm{yds}$ ? of $4 \frac{1}{2}$ acres to $\frac{1}{3}$ of $3 \frac{1}{4}$ acres?
8. Compare the rates at which two men travel per hour, one of whon goes $2 \frac{1}{2}$ miles in one homr, the other $3 \frac{1}{3}$ miles in one hour.
9. One stemer makes $8 \frac{1}{2}$ miles in 40 mir.utes, and a second makes 9 miles in 45 minutes : compare their rates per hour.
10. To what number has 6 the sane ratio that 3 has to 21 ?

Sol.- $3: 21={ }_{2}^{3}{ }^{3}=\frac{1}{7}$, so the question really isUf what number is 6 the $\frac{1}{7}$ ? 6 is $\frac{1}{7}$ of 42 $\therefore 3$ to 21 has the same ratio that 6 has to 43. (Note that $42=1{ }_{3}^{21} \times_{6} ; 7$ is called the " fourth proportional" to the other three. Let teacher show relation betweon extremes and means.)
12. To what has 7 the same ratio that 4 has to 32 ? 12. To what has $\frac{1}{2}$ the sime ratio that 2 has to 41 13. Five shillings has to 7 c . $6 d$. the same ratio that $\$ 8$ has to what?
14. To what has six hours the same ratio that 3 men has to five men?
15. To what has 1 acre the same ratio that 15 dwt. has to $2 \frac{1}{2}$ oz. $?$
16. Compound the ratio $3: 4$ and $8: 12$.

Sol. $-3: 4=3 ; 8: 12=\frac{8}{12} ;$ and $\frac{3}{4} \times{ }_{12}^{8}=\frac{24}{4}$
$=24: 48$ (or $=1: 2$ ), what is the ratio compounded of the two given ratios?
17. Compound the ratios $4: 5$ and $7: 8$; also $\frac{5}{9}$ and $\frac{3}{3}$.
18. The ratio of $A: B$ is $3: 4$, and of $B: C$ it is $4: 5$; find the ratio of $\mathrm{A}: \mathrm{C}$.
19. One milkman adds 3 pints of water to every $1 \frac{1}{2}$ gallon of milk, another adds 5 pints to every $2 \frac{1}{2}$ gallons: compare the quantity of water in the two samples of milk.
20. The ratio of $A: B$ is $\frac{1}{2}$ of $B: C 3: 4$, of $A: D$ $4: 5$ : find the ratio of $A: D$.
21. If 4 melons afe worth 12 oranges, and 5 oranges are worth 15 cents, how many cents are 12 melons worth?
22. What number bears to 6 the same ratio that 6 bears to 9 ?

Sol. $-6: 9=\frac{2}{3} \cdot \cdots$ the required no. $=\frac{2}{3}$ of $6=4$. We have then 9:6::6:4.
Note.-Six is called the " mean proportional ' between 9 and $4: 6^{2}=449 \cdot .6==\sqrt{4 \times 9}$.
23. Find the mean proportionals between 8 and 2, 4 and 16, 5 and 20, 9 and 16.
that 3
$\bar{s} d w t$.
$y_{2}^{2}={ }_{4}^{4}$
o cour-
also $\frac{5}{9}$
is $4: 5$;
very $1 \frac{1}{2}$
very $2 \frac{1}{2}$ he two
of $A: D$
oranges melons

Examples.-18.

1. If 5 acres cost $\$ 75$, what will 8 acres cost?

To the cost of 8 acres $\$ 75$ will have the rat tio of $5: 8$; i.e., $\frac{5}{8}$ of some number is 75 , what is the number? $\frac{5}{8}$ is $75, \frac{1}{8}$ is 15 , and $\frac{8}{8}$ is $8 \times 15=120$.
2. Ten pounds of sugar cost 95 cents: what will \& cost?
3. A man digs a ditch in 20 days, working 10 hous:; a day: how long will it take him if he works 8 hours a day?
4. It costs $\$ 60$ to carpet a room 15 feet wide, and 18 feet long: how much would it cost if the room were 16 ft .6 in. long ?
5. John earns $\$ 7$ as often as James earns $\$ 10 \frac{1}{2}$ : when Jimes has earned $\$ 52 \frac{1}{2}$ how much has John earned?
6. If $\frac{3}{8}$ of a yard of cloth cost $\$ \frac{7}{8}$, how much will $1 \frac{7}{8}$ yds. cost?
7. Two persons travel towards each other ; the first travels 6 miles while the second travels 5 : when they meet it is found that the first has travelle $j i$ miles : how far were they apart when they started?
8. If 5 men receive $\$ 75$ wages in 10 days, how much would 15 men receive in 40 days at the same rate?

Sol.-In 10 days 15 men would receive $\frac{15}{3} \times$ $75=\$ 225 . \therefore$ in 40 days 15 men would receive $4 \times 225=\$ 900$.
9. If $\$ 150$ gain $\$ 12$ in 12 months, how long will it take $\$ 600$ to gain $\$ 188$

4
10. If 6 horses eat 9 tons of hat in 8 months, how many tons would 5 horses cat in 12 months?

Sol.-In 12 months 6 horses would eat 131 tons. $\cdot 5$ would eat $\frac{8}{6}$ or $13 \frac{1}{2}=\frac{48}{4}=11 \frac{1}{4}$.
11. If the freight on 8 ewt. for 36 miles is $\$ 8$, what would it bu for 20 ewt., 18 miles, at the same rate?
12. If 12 oz . of bread can be $\mathrm{r}^{\wedge} \mathrm{g} \mathrm{ght}$ for 6 cents when flour is $\$ 6$ a barel : how mu ionld be bought for 8 cents whe:a flour is $\$ 4$ a bara.. .
13. How many men in six days of 10 hours each can earn ats mach as 6 men in 20 days of 8 hours each?
14. If 4 men can do a work in 6 days, in what time will it be completed if they receive the assistance of 10 men, when one-fourth of the work is done?
15. If 6 men ean do the work of 18 women, and 2 women cun to the work of 3 boys, how many men can do the work of 36 boys?

Sol.-It will take $\frac{36}{3} \times 2=24$ women . $\cdot$ it will take $\frac{24}{18} \times 6=8$ men.
16. How many sheep ean you buy for 3 horses, if 10 cows are worth 5 horses, and 6 sheep are worth 2 cows?
17. How many oranges can you buy for 20 cents, if 4 oranges are worth 8 apples, and 6 apples are worth 12 cents?
18. If 5 lbs . of cheese are equal in value to 2 lbs . of butter, and 6 lbs . of butter to 2 bushels of oats, how many lbs. of cheeso will pay for 8 bushels of oats?
19. If 9 men build 10 rods of wall in 8 days, in
whit time can 20 rods be built, if $\frac{3}{3}$ of their number leave when the work is half done?

## Section 11.-Proportional Parts.

Examiles.-19.

1. Divite $\$ 35$ into two parts which shall be in the ratio of 2:3.

Sol.-5 thus divided would give the numbers 2 and $3 . \therefore 35$ thas divided would give the numbers $7 \times 2$ and $7 \times 3$, or 14 and 21 .
2. Divide 21 acres between $\Lambda$ und 13 in the ratio of $3: 4$.

Sul.-Of 7 acres A gets 3 and B $4 . \therefore$ A is to get $\frac{3}{7}$ of the whole, and $B \frac{4}{7}$ of the whole, or 9 and 12 respectively.
3. Divide 48 into two parts which shall have the ratio 5:7.
4. Divide 144 into parts which shall be as $3: 5$, as $4: 5$, as $5: 7$, as $7: 11$, as $11: 13$.
5. Divide $\$ 70$ between Harry and Willio, so that. as often as Harry gets $\% 4$ Willie may receive $\$ 3$.
6. $\$ 45$ is divided between two boys, so that as often as the first gets $\$ \frac{1}{2}$ the secoud gets $\$ \frac{2}{6}$ : find their shares.
7. 60 apples are divided among three boys, so that their shares may be in proportion to $3,4,5$.

Sol.-Of 12 the first would get 3 , the second 4, and the third $5 . \cdot$ of 60 the first would get $5 \times 3$, the second $5 \times 4$, and the third $5 \times 5$.
8. Three men bought 75 horses, and as often as the first paid $\$ 4$, the second paid $\$ 5$, and the third 6 : how many horses should each receive?
9. The sum of two numbers is 105 , and the first is to the second as $\frac{1}{2}: \frac{3}{4}$ : find the numbers.
10. Three mon went into a speculation, contribut. ing $\$ 250, \$ 3 \mathrm{C} 0, \$ 350$ respectively ; they gain $\$ 1,350$ : how should this be divided?
11. Three men do a certain work for $\$ 60$, they work the same number of days, and are to receive $\$ 1$, $\$ 1.25$, and $\$ 1.50$ a day respectively : how should the money be divided?
12. Divide $\$ 900$ among $A, B, C$, so that $B$ may get twice as much as $A$, and $C$ three times as much as B.

Sol.-B's share is 2 times A's, and C's $==3$ times B's $=6$ times A's.$\cdot$ A's + B's + C's $=1+2+6=9$ times A's share $=$ $\$ 900 .{ }^{\circ}$. 1 's $=\$ 100, \mathrm{~B}$ 's $\$ 200, \mathrm{C}$ 's $\$ 600$.
13. In an orchard are 96 trecs; there are 5 apple trees for every 4 peach trees, and 4 peach trees for every 3 pear trees : how many trees of each kind are there?
14. Three men hired a pasture for $\$ 30$; A put in 3 horses, B 4 horses, and C 5 horses: how much should each pay?
15. Divide $\$ 340$ among $\Lambda, B, C$, in the proportion of $1, \frac{2}{5}, \frac{3}{10}$.
16. Divide $\$ 125$ among 2 men, 3 women, and 4 boys, so that as often as each boy gets $\$ 2$, each woman may get $\$ 3$, and each man, $\$ 4$.

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2. 

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4.
first
5.
as m how
47. $\frac{1}{5}$ of the time past noon is $\frac{1}{3}$ of the time bill midnight: what o'eluck is it?

Sol.-Time from noon till midnight $=12$ bcurs
$\therefore$ Divide 12 in ratio of $\frac{1}{3}: \frac{1}{5}$, i.e., $5: 3$.
$O_{r}, \frac{1}{5}$ of time past noon $=\frac{1}{5}$ time till midnight.
$\therefore$ time past noon $=\frac{5}{3}$ timed till midnight, \&c.
18. What o'clock is it when the time past noon is ${ }_{5}^{5}$ of the time till midnight?
19. A's fortune added to $\frac{1}{2}$ of B's equals $\$ 2,000$; and A's is to B's as 3:4: find the fortune of each.
20. I bought two lots, the prices of which were as $9: 8 ; \frac{1}{3}$ of price of tirst lot added to $\frac{1}{4}$ of that of feecnd equals 8500 : find the price of each. for $2 \frac{1}{2}$ years at $7 \frac{1}{2}$ per cent. : find the face $\frac{1}{2}$

## Examples.-20.

1. John's age being doubled, and increas? by $\frac{8}{4}$ of his age +10 years, equals 50 : how old is he?
2. John's age is to Richard's in the ratio of $\frac{3}{4}$ to $1 \frac{1}{4}$, and the sum of their ages is 32 : find the age of each.
3. What number is that which being inereased by the difference between its ficurth and fifth parts, equals 42 ?
4. The sum of two numbers is 22 , and $\frac{2}{3}$ of the first equals $\frac{4}{5}$ of the second: find the numbers.

Sol.-The first $=\frac{4}{6} \div \frac{2}{3}=\frac{6}{6}$ of second.
$\therefore$ second $+\frac{6}{8}$ of second $={ }_{5}^{1}$, of second
$=22$, and second is 10 , first 12.
5. Mary gave $\frac{3}{4}$ of her money in charity, saved $\frac{2}{8}$ as much as she had given away, and then had $\$ 60$ : how much had she at first?
6. $\mathbf{A}, \mathrm{B}$, and $\mathbf{C}$ are worth together $\$ 4,800 ; \mathbf{A}$ is worth $\frac{2}{3}$ as much as $B$, and $C \frac{1}{2}$ as much as $A$ : how much is each worth ?
7. $\$ 500$ is divided among 4 men ; the first has $\frac{1}{4}$ as
14. than eath?
15. much as the second, the second $\frac{1}{2}$ as much as the third, and the third $\frac{2}{3}$ as much as the fourth : how much does each receive?
8. Find two numbers whose sum is 121 , and which have the ratio of $\frac{5}{8}: \frac{3}{4}$.
9. A boy spent $\frac{2}{5}$ of his money, and then found $\$ 15$ was $\frac{5}{8}$ of what he had $r$ naining: how much had he at first?

Sol. $\frac{2}{8}$ spent $\therefore \frac{3}{5}$ left ; $\frac{8}{8}$ of this $=\frac{3}{8}=\$ 15$. $\therefore$ \$40 at first.
10. If $\frac{2}{5}$ of a number bo multiplied by $2 \frac{1}{8}$, and 70 be taken from the product, the result is $\frac{1}{2}$ the number: find the number.
11. A horse and harness cost $\$ 150$, and $\$$ of the cost of the horse was $3 \frac{1}{6}$ times the cost of the harness: find the cost of each.
12. A calf, a cow, and a colt were sold for $\$ 110$, the colt brought $\$ 15$ less than the cow, and the calf $\$ 25$ less than the colt: what did each bring?

Sol.-Colt brought $\$ 15$ less than the cow, and the calf $\$ 25$ less than the colt, i.e., $\$ 40$ less than the cow $\therefore 3$ times price of cow, less $\$ 55=\$ 110$; and 3 times price $=\$ 110+$ $\$ 55=\$ 165, \& c$.
13. Divide 200 into three such parts that the second shall be 4 times the first, and the third 5 timem the second.
14. Two farmers have 165 sheep; one has 5 less than $3 \frac{1}{4}$ times what the other has: how many has. each?
15. I sold ? of my farm, afterwards bought 40 acres, and had then 130 acres: how much had I at tirst?
16. Three lots cost $\% 00$, the second cost 850 more than the first, and the third $\$ 100$ more than the second : find the cost of each.
17. Find two numbers whose difference is 20 , and wheh have the ratio $5: 4$.

Sol.-The less is plainly $\frac{4}{5}$ of greater . ${ }^{-}$. difler ence $=\frac{1}{6}$ of greater $=20$ and greater $=$ 100.
18. My agu now is to my a C 10 years ngo as $9: 7$ : find iny present age.
19. $\Lambda$ cow and a loorse cost $\$ 165$; the cow cost B1C less than $\tilde{5}_{5}^{2}$ of what the horse cost : tind the cost of each.
20. Divide 324 into 3 such parts that $\frac{1}{2}$ of the first shatl be twice the second, and $\frac{1}{4}$ of the second 4 times the thind.
21. ${ }_{3}^{3}$ of A s age 4 years ago is ${ }_{7}^{3}$ of what it will br $t$ yeu's hence: tind his age.

## Section III.-Partnership.

Examples.-21.

1. Three partners put into a business, $\$ 200, \$ 300$, $\$ 400$ they gain $\$ 1,350$ : how should this be divided 1 Sol. $-\$ 900$ gains $\$ 1350,1$ gains $1350 \div 900 \Rightarrow$
$\$ 1 \frac{1}{2} \cdot \therefore$ the shares are $200 \times 1 \frac{1}{2}, 300 \times 1 \frac{1}{2}$
2. $400 \times 1 \frac{1}{2}: 16 ; \$ 300, \$ 450, \$ 600 ;$ Or:the amounts of capital are as $2,3,4 \therefore$ the first gets $\frac{2}{9}$ of the gain, the second $\frac{3}{9}$, and the third $\frac{4}{9}$.
8). A owes B $\$ 200, \mathrm{C} \$ 300$, and $\mathrm{D} \$ 400$; his property is worth only $\$ 450$ : how much do $\mathrm{B}, \mathrm{C}, \mathrm{D}$, each receive?
3. $\Lambda, B, C$, hire a pastiure for $830 ; \Lambda$ put in one cow 5 months; B 2 cows 3 months; C 3 cows 3 months: how much should each pay?

Sol.-1 cow 5 months $=5$ cows for 1 month; 2 cows 3 months $=6$ cows for 1 month; 3 cows 3 months $=9$ cows for $1 \mathrm{mcnth} . \therefore 5$, 6,9 are the proportions in which the cost must be paid $5+6+9=20 . \frac{2}{20}_{5}^{5}$ of 80 , $\frac{6}{20}$ of $80, \frac{9}{20}$ of 80 , or ${ }^{3} 20, \$ 24$, and $\$ 36$, are the amounts.
4. Four men in partnership divide their stock into 40 shares ; $\Lambda$ has 6 shares, B 8, C 12, and D 14; they gain $\$ 15,000$ : how should this be divided?
5. A and $B$ are partners, $\Lambda$ furnished $\$ 500$ for 6 months; and $B \$ 750$ for 8 months; they gain $\$ 1500$ : how should this be divided?
6. The stock oi a bank is divided into 1500 shares; when it makes : dividend of $\$ 7,500$, how much does A receive who owns 19 shares?
7. A puts in $\$ 250$ for 6 months, and $B \$ 350$ for 4 months; they gain $\$ 580$ : how should this be divided?
8. A, B, C form a partnership; A puts in $\frac{1}{4}, \mathrm{~B} \frac{8}{8}$, and C the remainder: C's gain is $\$ 240$ : what does wach of the others grim?
9. $A$ and $B$ are partners, $A$ put in $\frac{5}{T^{2}} \mathrm{o}^{f}$ the stock, and $B$ the remainder; B's gain was $\$ 1400$ : find A's.
10. A and B are partners, A puts in $\frac{2}{5}$ of the stock for 4 months, and $B$ the remainder for 3 months: how should a gain of $\$ 1700$ be divided ?

Sol.- ${ }_{5}^{2}$ for 4 months $=\frac{8}{6}$ for 1 month, and $\frac{3}{5}$ for 3 months $=\frac{9}{6}$ for 1 month $\therefore$ gain is to be divided in rates $8: 9 ; \$ 800, \$ 900$
11. A and B ship a cargo of coal faom Picton to Montreal, agreoing to share gains and expenses equally. A paid $\$ S 0$ for loading and freight. The coal was sold in Montreal for \$680. B had previously lent A \$100 to purehase coal, and he also owed $A \$ 20$ on a previous shipment; how should the proceeds of the coal be divided?
12. A rented a house for one year, agrecing to give $\$ 6$ a month, and pay the taxcs for the year; he ro. mained in the house 3 months, and during that time paid the taxes. If the rent of the house paid the owair 9 per cent. on his money, and the assessment in the locality was $1 \frac{1}{2}$ cents on the dollar: what, in jastice, slould A pay for his 3 months rent?
is. Smith and Jones hire a horse for $\$ 5$, to 80 frum Truro to Windsor, a distance of 40 miles. Itaving driven 10 miles they took up Brown, brought him to Windsor and back to where they found him: how much of the horse hire should each man pay?
14. A, B, and C are partners, whose respective shares of the stock are as 1,2 , and 3 . They gain $\$ 600$. If, on dividing the profits, $A$ relinquish his parts of the gain, how much will cach of the others reccivo ?
15. A and B start business. A put in $\$ 30$ for 4 months, and $B$ a certain sum for two months, they gain $\$ 44$, of which A takes $\$ 24$ for his share: find the sum B puts in.

Sol.-A's stock $\times$ time $=30 \times 4=120$; the gains are as $24: 20$; or $6: 5 \therefore \frac{6}{6}$ of $130=$ product of $B$ 's stock by time, which $\therefore=$ $\$ 100 \therefore \$ 100 \div 2=\$ 50, \mathrm{~B}$ 's stock.
16. An old man agrecd to thresh pease for a farmer and take the tenth thashel for his pay ; the farmer, who could thresh as much in 5 hours as the cld man in 7, worked with him: what bushel of the combined threshing should the old man get?
17. Two men, $A$ and $B$, rent a pasture for $\$ 21.50$. A put in 2 cows, and is 3 horses. Supposing a horse to eat half as much again as a cow in the same time, but the cows to he on the grass one-third as long regain as the horses, find what each man should pay.
18. $A$ and $B$ invest capital in the proportion of $1: 2$, at the end of 2 months they each withdraw $\frac{1}{2}$ the sum invested, at the end of the year the gain is found to be 8210 : how should this be divided.
19. Three men, A, B and C, entci into partnership for the purpose of renting a skating rink at $\$ 90$. A put in his money for 3 months, $B$ his for 1 month, and C his for 2 months. The earnings of the rink for the season heing divided, $\Lambda$ got $\$ 30, \mathrm{~B} \$ 15$, and $\mathrm{C} \$ 20$ : how much money did each man put in ?
20. A and B do a piece of work for $\$ 10$, they agree to divide the money in proportion to their ability in
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mo combined
r \$21.50. horse to time, but argain as
n of 1:2, the sum and to be k for the 1 C 520 :
icy agree bility on
work, which is as 1 to 2 , and also to the time each worked which is as 2 to 3 : how should the money be divided?
21. $A$ and $B$ form a partnership; A puts in $\$ 200$ for a ceitain time, $\mathrm{N} \$ 300$ for 2 months, B's share of the gain is $\$ 450$, and $\Lambda$ 's $\$ 600$ : how long was $A$ 's money in the business?

$$
\begin{aligned}
& \text { Sol.-A's share }=\frac{4}{3} \text { B's } . \therefore \text { A's product of } \\
& \text { stock by time }=\frac{4}{3} \text { of } 300 \times 3=800 \text {, and } \\
& 800 \div 200=4=\text { A's time. }
\end{aligned}
$$

22. A and I are partners ; A puts in $\$ 150$ for 6 months, and $B \$ 250$ for a certain time; the profits are divided in the ratio of $9: 10$ : find the time E's stock was in.
23. A and B are partners; $A$ contributes $\frac{2}{3}$ of the joint capital for 5 months, and $B$ receives $\frac{6}{11}$ of the gain : find b's time of investment.
24. How much copper ore was mised to produce $5\left(0\right.$ tons of metal, allowing $\frac{3}{5}$ of the ore to be lost in roasting, and $\frac{1}{3}$ of the remainder in smelting?
25. In what proprtion must water be mixed with milk, to redice the value from 20 cents a gallon to 16 cents?

Sol.-The milk in the mixture is worth 16 cts., $\therefore$ there must be $\frac{16}{20}\left(=\frac{1}{3}\right)$ of gallon, ind hence : gallon of water . $\cdot$ the ratio is $1: 4$.
26. A grocer has 60 lbs . of mixture of coffee and chicory, the former to the latter as $5: 1$ : how much chicory must be added to make the matio $4: 1$ ?

## Section IV.-Alligation.

Examples. - 22.

1. A milkman sells milk at 16 centr a gallon : in what proportion must he add water so as to reduce the price to 14 cents a gallon?

Sol.-1 gallon milk soid at 14 cts. gives loss 2 cts ; 1 gallon water sold at 14 cts gives gain 14 cts. $\therefore \frac{1}{7}$ gal. water gives gain 2 cts., Which balances the 2 cts. loss. $\cdot$ ratio is $1_{7}$ : 1 , or $1: 7$.
2 How much water per gallon must be added to brandy worth $\$ 4$ a gallon, to reduce the price to $\$ 3$ a gallon?
3. In what proportion must wines worth 108 . and 14s. agallon respectively, be mixed, so that the mixture may be worth $13 s$, a gallon?

Sol.-By selling 1 gal. $10 s$. quality at $13 s$. thete is gain of $3 s$.; by selling 1 gal. $14 s$. quality at 13 s . there is loss of 1 s ., and 3 of latter gives loss of $3 s$., which balances gain of $3 s$. $\therefore$ ratio is $1: 3$.
4. How much wine at 14 s . a gallon and 18 s . must be taken to form mixture worth ios.?
5. How much sugar at 6 cts. and 10 cts. per lb. must be taken to form a mixture worth 7 cts ?
6. How much chicory at 10 cts . a lb, and coffee at 30 cts., must be taken to make 20 lbs . worth 25 cents per lb. 1

Sol.-Find first the proportion in which they are to be mixed ; 1 lb . chicory sold at 25 cts. gives gain 15 cts., 1 lb . colfeo sold at 25 cts. gives loss 5 cts. Hence 3 lbs . of coffee must
llon : in o reduce
es loss 2 ves gain h 2 cts., tio is $\frac{1}{7}$ :
added to to $\$ 3$ a

108 . and mixture

3s. thete quality of latter in of $3 s$.
38. must per lb. offee at 5 centa be taken to 1 of chicory.$\cdot$ dividing 20 lbs . (required mixture), in ratio of $1: 3$, we get 5 lbs chicory and 15 lbs . coffec.
7. How much chicory at 8 cts. and coffee at 24 cts. must be mixed to get 40 lbs . of a mixture worth 22 cents a pouad?
8. How much sugar at 6 cents a pound must be mixed with 30 lbs at 10 cents to get a mixture worth 7 cts. $?$

Sol.- Find first the prop. in mixture. As before, this will be found to be 3 lbs. at 6 ets., and 1 lb . at 10 cts ., but we require 30 lbs . at 10 cts. $\cdot 30 \times 3=90 \mathrm{lbs}$. at 6 cents.
9. How much water must be mixed with 10 gallons of milk worth 20 cts. a gallon, to get a mixture worth 18 cts. a gallon?
10. How much sugar at 6 cts., 8cts. and 10 cts. per lb. must be taken to form amixture worth 9 cts. per lb. I

Sol. -1 lb . of 6 ct . sold at 9 , gives 3 cts. grain ; 1 lb .8 ct . sold at 9 cts . gives 1 ct . gain-total gain, 4 cts.; ilb. 10 ct. sold at 9 gives 1 ct. loss . $\cdot 4$ at 10 gives 4 cts. loss to balance 4 cts. gain, and proportions are 1, 1, 4.
11. In what proportions must flow worth 2 ats, 3 cis., 5 cts. per lb. respectively, be taken so as to get a mixture worth 4 cts. per lb. 1
12. In what proportions mast wine worth $10 / 8$. 14s., 18s. a gallon, be taken to form a mixture worth 16s. $?$
13. A grocer mixed sugar at 6 cts. and 12 cts., and by selling the mixture at 8 cts., he gained 25 per cent. on the first kind, and $33 \frac{1}{3}$ per cent. on the second kind : in what proportion did he mix them?

Sol. -Six cts. +25 per cent. of it $=7 \frac{1}{2} ; 12$ cts. + $33 \frac{1}{2}$ per cent. of $\mathrm{it}=16 \mathrm{cts}$. 1 lb . of $7 \frac{1}{2}$ sold at 8 , grains $\frac{1}{2} \mathrm{ct}$ : 1 lb . of 16 sold at 8 loses 8 , $\therefore$ ratio is $8: \frac{1}{2}=16: 1$.
14.--A grocer mixed coflce at 20 cts a lb . with another quality worth 35 cts. a lb, and by selling the mixture at 30 cts . a lb. he gained 25 per cent. on the former, and 20 per cent. on the latter: in what propor. non did he mix them?

## Section V.-Special Methods.

$$
\text { Examples.- } 23 .
$$

1. Find the square of 37 .

Sul. $-37^{2}(3 \text { ten }+7)^{2}=$ (by actual multipli. cation) 9 ten ${ }^{2}+$ twice $7 \times 3$ ten $+49=$ 90 ten +42 ten +4 ten $+9=136$ ten $+9=1369$.
2. Find the square of $206 \quad(=20$ ten +6$)$.

Sol. $-206^{2}=400 \times 10^{2}+240 \times 10+36$ $=4243 \times 10+6=42,436$.
3. Equire $196=(20$ ten -4$)$.

SSol.- $(196)^{2}=(20 \text { ten-4 })^{2}=400 \times 10^{2}-$ $160 \times 10+16=4,000$ ten -160 ten + $16=3,840$.ten $+16=38,416$.
$10 s$ worth, ., and cent. kind :
cts. + $7 \frac{1}{2}$ sold loses 8 ,
J. with ing the on the propor.
4. Find squares of $116,105,195,304,299$.
5. Write down the squares of $197,711,801,795$, 497, 509, 805.

Note. When the number is less than 100 , a convenient rule, derived from the rule for squaring as above, is: Add the anits to the number, multiply by the tens, and add the square of the units, e.g.:
6. Square 35.

$$
\text { Sol. }-(35+5) \times 30+5^{2}=1225 .
$$

7. Find the squares of $25,45,65,84,85$.
8. Find the squares of $36,39,72,85,89$.
9. Find the squares of $69,58,23,87,61$.
10. Square $8 \frac{1}{2}$.

$$
\begin{aligned}
& \text { Sol. }-\left(8 \frac{1}{2}\right)^{2}=\left(8+\frac{1}{2}\right)^{2}=8^{2}+2 \times \frac{1}{2} \times 8+\frac{1}{4} \\
& =8^{2}+\text { one } \times 8+\frac{1}{4}=8(8+1)+\frac{1}{4} \\
& =72 \frac{1}{4} .
\end{aligned}
$$

11. Find the squares of $3 \frac{1}{2}, 5 \frac{1}{2}, 7 \frac{1}{2}, 10 \frac{1}{2}, 12 \frac{1}{2}$.
12. Find the squares of $14 \frac{1}{2}, 19 \frac{1}{2}, 24 \frac{1}{2}, 29 \frac{1}{2}$.
13. Find the square of 8 .

Sul.- $\left(8_{4}^{1}\right)^{2}=\left(8+\frac{1}{4}\right)^{2}=8^{2}+\frac{1}{2} \times 8 \times{ }_{16}^{1}=$ $68 \frac{1}{16}$.
14. Find the squares of $4 \frac{1}{4}, 6 \frac{1}{4}, 10 \frac{1}{4}, 12 \frac{1}{4}$.

Find the squares of $3 \frac{1}{4}, 5 \frac{1}{4}, 20 \frac{1}{4}, 16 \frac{1}{4}, 14$.
15. Multiply 37 by 35 (i.e. 3 ten +7 by 3 ten +5 ).

Sol. $(3$ ten +7$)(3$ ten +5$)=90$ ten + $(7+5) \times 3$ ten $+35=90$ ten +36 ten +3 tens $+5=129$ ten $+5=1,295$.
16. Find the products of 34 and 37,32 and 39 , 45 :and 47, 56 and 54, 63 and 67.
17. Find the product of $6 \frac{1}{4}$ by $6 \frac{3}{4}$.

Sul.-61 $\times 6 \frac{3}{4}=\left(6+\frac{1}{4}\right)\left(6+\frac{3}{4}\right)=6+1$

$$
\times 6+\frac{1}{6} \times \frac{3}{1}=6(1+6)+\frac{3}{16}=422_{16}^{3} .
$$

18. Find the products of 5 and 54,74 and 78 , $7 \frac{1}{5}$ and $7 \frac{1}{5}, 83$ and $8 \frac{4}{7}, 10 \frac{1}{6}$ and $10 \frac{4}{6}$.
19. Find the number of square rods in a lot which is 32 rods square.
20. Find the cost of 93 lbs . of sugar at 94 cents per lb.
21. What will $5 \frac{5}{8}$ cords of wood come to at $\$ 5 \frac{3}{3}$ per cord?
22. Find the cost of $15 \frac{1}{2}$ yards of print at $15 \frac{1}{2}$ cts. per yard.
23. What will $5 \frac{4}{5}$ yards of broadcloth cost at $\$ 5.20$ \& yavd

$$
\text { Examples. - } 24 .
$$

1. Multiply 237 by 14 .
*Sol.-Multiply each firure of multiplicand by the units of multiplier, and add the figure to the right of the one multiplicd: $4 \times 7$ $=28$, write down $8 ; 4 \times 3+7(+2$ carried) $=21$, write down $1 ; 4 \times 2+3+$ 2 (curried) $=13$, write down 3 ; then $2+1$ (carried) $=3$, write down $3 . \therefore$ product is 3,318.
2. Find product of 345 by 17,39 by 19,121 by 18. Write down product of 632 by $15,32,217$ by 13 , 479,632 by $14,215,762$ by $18,31,451$ by $19,3,474,263$ by 17 .
3. Multiply 4,347 by 31 .

Sol.-Write down the units figure of multipliv. cand ; multiply by the tens of the multi

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ly
$1 s$.
plicr, adding to each result the figure to the left of the one multiplied, e.g.: Write down $7 ; 3 \times 7+4=25$, write down $5 ; 3 \times$ $4+3+2$ carried $=17$, write down $7 ; 3$ $\times 3+4+1$ carried $=14$, write down 4 ; $3 \times 4+1$ carried $=13$, write down 3 ; +1 carried $=1$, write down $1 . \cdot$ proluct is 134,757 .
4. Write down the products in the following cases: $-2357 \times 31,48765 \times 41,987643 \times 51,2131476$ by 91,28745 by 101.
5. Write down $4627143 \times 71,6219473$ ly 121, S1!л7 $\times 118,7648 \times 125,82143 \times 99,267 \times 1001$.
6. Simplify $35^{2}-25^{2}$.
\[

$$
\begin{aligned}
& \text { Sol. }-35^{2}-25^{2}=(35+25)(35-25=60 \\
& \quad \times 10=600
\end{aligned}
$$
\]

7. Simplify $85^{2}-65^{2}, 95^{2}-75^{2}, 65^{2}-35^{2}$ $312^{2}-311^{2}, 629^{2}-621^{2}$.
8. Write down the results in the following cases:$7210^{2}, 7207^{2}, 1376^{2}-1370^{2}, 1321^{2}-1221^{2}, 1619^{2}$, $-1609^{2}, 12105^{2}-13005^{2},(164369)^{2}-(164119)^{2}$.
9. Find the price of 288 yards of linen at 93 . per yard.

Sul.-288 at $9 \frac{3}{4}=72$ at $3 s .3 d .=9$ at $26 s s_{0}=$ £11168.
10. Find the cost of 512 yards of cotton at $6 \frac{1}{4}$ cents.

Sol.-512 at $G_{4}^{1}=128$ at $25=32$ at $\$ 1=\$ 32$.
11. Find cost of 280 yards at 63 cents ; 376 yards at $7 \frac{1}{2}$ cents.
12. Find the cost of 960 yards of dress goods at 1s. $3_{4}^{3} d$.
13. Find the cost of 1,216 yards at $3{ }_{4}^{3} d ; 72$ yards at 4 s. $4 \frac{1}{4}$ d.
14. $37 \frac{1}{2} \mathrm{lbs}$. of tea at 40 cents ; 96 lbs . at $3 \mathrm{~s} .4 \frac{1}{2} d$.
15. Find the cost of 236 yards of Canadian tweed at 80 cents a yard.
16. Bought 24 yards of silk at $78.6 d$. sterling a yard : find the cost in Canadian currency, the shilling sterling being worth $24 \frac{1}{3}$ cents.
17. Cost in Camadian currency of 360 yards of cotton at $6_{4}{ }^{2}$. stg. a yard.
18. Find the cost in Canadian currency of 128 yarr!s of dress goods at 1 s .9 d . stg. a yard.

## Section VI.-Mensuration.

$$
\text { Examples. - } 25 .
$$

1. A board is $15 \frac{1}{2}$ inciaes wide and 16 feet long: how many square feet dons it contain?

$$
\text { Sol. }- \text { Area }=\text { length } \times \text { oreadth }=1 \frac{7}{24} \text { feet } \times
$$ $16={ }_{2}^{3.1} \times 16={ }_{3}^{3} \times 2=20_{3}^{2}$ sq. feet.

Or: Calculate first for 12 feet long; then a board $15 \frac{1}{2}$ inches wide and 12 feet long $=$ one 12 in. wide and $15 \frac{1}{2} \mathrm{ft}$. long $=15 \frac{1}{2} \mathrm{ft}$. Then 12 ft . long gives $15 \frac{1}{2} \mathrm{ft}$. are. $\cdot 16 \mathrm{ft}$. long gives $\frac{1}{3}$ more, $=15 \frac{1}{2}+\frac{1}{3}$ of $15 \frac{1}{2}=15 \frac{1}{2}$ $+5 \frac{1}{6}=20 \frac{2}{3}$.
2. Find area of a board 15 feet long, 13 inches wide; 18 foet lagg, 14 inches wide; 14 feet leng, 162 inches wide.
8. How muc! lumber, inch measure, in 6 planks,
each $18 \frac{1}{2}$ inches wide. 16 feet long, and 3 inches thick ?

Sol.- $18 \frac{1}{2} \mathrm{in}$. wide, 16 ft . long $=24 \frac{2}{3}$ (i.e., $18 \frac{1}{2}$ $+\frac{1}{3}$ of $18 \frac{1}{2}$ ) long, and 12 in . (wide) $=24 \frac{2}{3}$ ft. This $\times$ by $3=74 \mathrm{ft} .=\mathrm{amt}$. in 1 plank $74 \times 6=644 \mathrm{ft}$.
4. How much lumber in 12 deals 18 feet long, $15 \frac{1}{2}$ inches wide, and 3 inches thick?
5. How many square yards in the floor of a room 17 feet long and 16 feet wide, and what will it cost to carpet it at $\$ 1.80$ ner square yard 1

Sol.-Dịmensions are $5 \frac{2}{3}$ yds., $5 \frac{1}{3}$ yds. ; are $=$ $5 \frac{2}{2} \times 5 \frac{1}{3}=25+5+\frac{2}{8}=30 \frac{2}{9}$ yds., which, at $\$ 1.80,=\$ 54.40$.
6. What is the area of the floor of a room 16 ft .6 in. square, and what will it cost to carpet it with carpet 1 yd. wide and $\$ 1.20$ a yard?
7. If the carpet is only 27 inches wide, what will be the cost in last question?

Sol. -No. sq. yds. in room $=30 \frac{1}{4}$, and cost $=$ $\$ 36.30$ when carpet is 1 yd . wide ; but if carpet is 1 -fourth less in width, the cost will be $1-$ third more $=\$ 36.30+\$ 12.10=\$ 48.40$
8. What will it cost to carpet a room 23 ft . long and 22 ft .6 in . wide, with carpet 27 in . wide, and cos'ing $\$ 1.35$ per yard?
d. Hall is 29 ft .6 in . by 11 ft .3 in . ; carpet $\frac{5}{8} \mathrm{yd}$. wide, and 90 cents a yard: find cost.
$S_{o l}-{ }^{59} \times{ }_{6}^{15} \times \frac{8}{5}=59$ yils., which, at 90 cents $=\$ 53.10$.
10. A hall is 10 yards long and 3 wide, what will
it cost to carpet it with carpet 27 inches wide, at $\$ 1.75$ a yard?
11. If, in last question, the carpet is 4.5 inches wide, and same price per yard, what will the cost be?

Sol. $-10 \times 3=30$ sq. yds.; if carpet was 1 yarl wide, the cost would be $30 \times 13=$ $\$ 52 \frac{1}{2}$. hat it is 1 fourth more. $\cdot$. the quantity (and cost) will be $1-\mathrm{fifth}$ less, and $\$ 52 \frac{1}{2}$ $\frac{1}{5}$ of $\$ 52!=\$ 42$.
12. It costs 840 to carpet a room which is 18 feet long and 15 feet wide: what would have been the cost if it had been 18 feet wide?
$\boldsymbol{S}_{0}$. - 18 ft . is $\frac{1}{5}$ more than $15 \mathrm{ft} . .^{\cdot}$. cost would be $\frac{1}{5}$ more $=\$ 40+\frac{1}{5}$ of $\$ 40=\$ 48$.
13. If in last example the room had been a yard longer and a yard wider, what would have been the cost?

Sol.-Square yds. $=30 ; \frac{1}{6}$ longer would make $30+5=35$, and ! wider would make $35+7=42$ yds., which will cost $\frac{2}{5}$ more than 30 yds., or $\$ 56$.
14. What would have been the cost in last ex. :mple, if the room had heen a yard longer, and a yard less in brealth? If it had been a yard shorter as well as a yard narrower?
15. The length of a room is $\frac{1}{5}$ more than its imadth; it takes 30 square yards to carpet it: find the length and breadth.

Sol.-Length $=g_{\delta}$ of breadth $\cdot \therefore$ length $X$ breadth $=\frac{5}{5}$ of squave of breutth $=30 \mathrm{yds}$, and square of breadth $=25 \mathrm{yds} . . \therefore$ breadth $=5 \mathrm{gds}$. lengioh 6 yarda. een the Il make 1 make $\frac{2}{5}$ more last ex. 1 a yad as well
hnn its it: find
16. The brealth of a hall is $\frac{3}{8}$ of its length, and it costs \$05.60 to cover it with English oil-cloth, at \$1.60 a yard : find the length and breadth.

Examples.-26.

1. Find the cost of papering the walls of a room 16 ft .6 in . lougg, 13 ft .6 in . wide, and 10 ft .6 in . high, the paper being 27 inches wide, and 20 cts. a yard.

Sol. $-2 \times 5 \frac{1}{2}+2 \times 4 \frac{1}{2}=20(\mathrm{yds})=$. cir cuit of room, thinn $3 \frac{1}{2} \times 20=70$ yds. ; if paper were a yard wide it would cost $70 \times$ $20=\$ 14.00$, but it is 1 fourlh less than a yard wide. $\cdot$ cost will be 1 -third more ; $i . c$. $\$ 4_{3}^{2}$ more.$\cdot$ cost $=\$ 14+\$ 4 \frac{2}{3},==\$ 18 \frac{2}{3}$.
2. A room is 18 ft .9 in . long, 12 ft .9 in . wide, and 10 ft . high: what will it cost to paint its walls at 22 cts. a yard, allowing 6 square yards off for the evenings?
3. It costs $\$ 28$ to paper tho walls of a room 15 ft . square, with paper 27 inches wide, and 30 cents a yard : find the height of the room.
4. A school room is 30 ft . wide, and 36 feet long, and is seated for 60 pupils ; how many square feet are allower, on the average, to each mupil ?
5. If, in the last exumple, the room is 12 feet high ; how many cubic feet of space is allowed each pupil?
6. $\Lambda$ rectangular boiler is 2 ft . 2 in . long, 1 ft .4 in. wide, and $9 \frac{1}{4}$ in. deep: how many gallons will it hold if a pint contains $34^{2}$ cubic inches?

$$
\begin{aligned}
& \text { Sol. }-26 \times 16 \times 94 \times{ }_{10}^{3}=12 \times 9 \frac{1}{4}=111 \\
& \text { pints }=137 \text { gal. }
\end{aligned}
$$

7. A plate of eopper 1 ft .4 in . long, 10 in . wide and $\frac{8}{4}$ of en in. thick, is rolled into a sheet 2 ft .6 in . long and 8 in . wide: find the thickness of the sheet.
8. A cistern is 4 ft . long, $3 \frac{1}{2} \mathrm{ft}$. wide, and 4 ft . deef): what will it cost to cover the bottom and sides with lead, at 90 cts . per square yard?
9. What was the cost, at 90 cents per cubic yarl, of digging a cistern 6 ft . long, 6 ft . wide, and 5 ft .6 in. deep 3
10. The length of a room is to its breadth as $4: 3$, its height is 10 feet, and it contains 1,080 cubic feet of air: find its lengtiond breadth.

Sol.-Culbic feet $={ }_{3}^{4}$ of scpare of breadth $\times$ $10=1080$, and $\frac{4}{3}$ of square of breadth $=108$, $\therefore$ square of breadth $=81 \therefore$, breadh $=9$.
11. The length of a room which contains 45 cubic yards, is $\frac{1}{4}$ more than the breadth, tie length being 9 feet: find the length and breadth.
12. Find the value, at $\$ 3.50$ a cord, of a pile of woul 96 ft . long and 9 ft . high.

Sol.-Pile is 12 cords long and $2 \frac{1}{4}$ cords high ; $2 \frac{3}{4} \times 12=27$ cords-cost, $27 \times 3 \frac{1}{2}=\$ 94.50$.
13. A pile of wood is 128 ft . long and 7 ft . high : fiul its worth at $\$ 4.25$ per cord.
14. The length of a bath room whose ceiling is : 1, ? ft. high, is $\frac{1}{2}$ more than the breadth, and the area of its walls is 35 yards: find the length and breadtl:.

Sol.-Length $=1 \frac{1}{2}$ breadth $\cdot$. cirenit of room $=2$ breadth +3 do $=5$ times breadth, and this $\times 3 \frac{1}{2}=35$ yards. $\therefore 5$ times breadth $m=10$ yards, and breadth $=2$ yards,
15. The length of a room is $\frac{1}{3}$ more than the breadth, the height is 9 ft .9 inches, and the area of the walls 39 square yards: find the length and brealth.
16. A wall, whose height is 4 times its thickness, and whose length is 5 times its height, contains 2,160 cubic feet: find the dimensions of the wall.
17. Find the area of a circle whose diameter is 7 feet. Note.-Area of circle $=2 \frac{2}{7} \times$ square of radius. Sol. - Radius $=\frac{7}{2} . \because$ area $=\frac{22}{7} \times \frac{49}{4}=\frac{77}{2}=38 \frac{1}{2}$.
18. What is the area of a circle whose radius is $\%$ feet? 1 ft .9 inches? $3 \frac{1}{2}$ inches?
19. Out of a circular plate of 9 inches radins, is cut a concentric circular plate of radius 6 inches: find the areat of the circular ring (annulus.)

Sol.- $-\frac{2}{7}(9+6)(9-6)=\frac{22}{7} \times 45=141 \frac{3}{7}$.
20. Find tine are: of a circular ring whose inner and outer diameters are 10 and 4 resprectively.
21. Find the num:ber of cubic inches in a cylindrical vessel whose inner diameter is 8 inches, and height 7 inches.
22. A hollow metallic column is 10 feet leng, its diameter is 10 inches, and its thickness 3 inches: find the number of cubie inehes of metal.

Sol.-Radii 5 in: and 2 in:.$\cdot$ area of circu-
lar ring of section of column $=\frac{22}{7}(5+2)$ $(5-2)=66$, and $. \therefore 66 \times 120=7920$ cubic incles.
23. An iron pipe is 14 feet long, its diameter from outside to outside is 8 inches, and the thickness is 2 inches: find the quantity of metal in the pipe.
24. Two circular plates of gold, each an inch thick,
and of diameters 6 inches and 8 inches respectively, are melted into a single plate of same thickness: find its diameter.

Sol.-Since thickness is same, the square of radius of new plate $=3^{2}+4^{2}=25 . \therefore$ radius $=5$, diameter 10 .
25. Two circles have radii 8 feet and 6 feet respectively : find the radius of a single circle equal to both in area.
26. There is a circuiar annulus of gold plate 1 inch thick, whose outer and inner diameters are 10 inches and 4 inches respectively; it is melted into a single plate of gold whose diameter is 14 inches: find its thickness.
27. If the radius of the silver dollar be to that of the halt dollar, as $3: 2$, compare their thicknesses.
$S_{10} 7 .-$ Their values are proportional to their solid contents, let $t, t$, be the thickness, $\cdot \cdot$ solid contents are proportional to $\frac{3^{2} t}{2^{2} t}=\mathbf{2}, ~ \cdot$ $\frac{\mathbf{t}}{\mathbf{t}^{\prime}}=\frac{8}{9}$ the required ratio.
28. If the diameter of a sovereign be to that of a guinea as 7:8, find the ratio of their thicknesses.

## OHAPTER III.

## GENERAL ANALYSIS.

## Examples 27.

1. A can do a piece of work in $\frac{1}{3}$ of a day and $B$ in $\pm$ of a day: how long will it take both to do it?

$$
\text { Sol.-A can do } 3 \text { timos the work in } 1 \text { day, } \mathbf{B}
$$

4 times. . . both can do 7 times the work in 1 day, and the work in $\frac{1}{7}$ of a day.
2. Two pipes can fill a cistern in 3 hours ; one of them can do it in 5 hours: how lung will it take the other?

Sol.-Both can fill $\frac{1}{3}$ of cistern in 1 hour, one can fili $\frac{1}{5} \cdot{ }^{\circ}$ the other can fill $\frac{1}{3}-\frac{1}{6}=$ $\frac{2}{15}$ in 1 homr, arai the whole in $7 \frac{1}{2}$ homs.
8. If 2 men can reap a field in 6 hours, and one of them can do it in 10 heurs, how long will it take the other?
4. A and B can mow a field in 2 hours, B and C in 4 hours, and A and C in 3 hours.

$$
\begin{aligned}
& \text { Sol. }- \text { A's work per hour }+ \text { D's }=\frac{1}{2} \text {, B's }+ \\
& \text { C's }=\frac{1}{4}, \text { C's }+ \text { A's }=\frac{1}{3} .2 \text { twice (A's }+ \\
& \text { B's }+ \text { C's) }=\frac{1}{2}+\frac{1}{4}+\frac{1}{3}=13, \text { and } \Lambda^{\prime} \text { 's }+ \\
& \text { B's }+ \text { C's }=\frac{13}{2}, \text { but A's }+ \text { B's }=\frac{1}{2} \therefore \\
& \text { C's }=\frac{1}{2} 3-\frac{1}{2}=\frac{1}{2} . \therefore \text { C in } 24 \text { days, de. }
\end{aligned}
$$

5. $A$ and $B$ can dig a cellar in 6 days, $B$ and $O$ in 12 ditys, and A and C in 8 days ; how long would it take each?
6. John can do a work in $\frac{2}{5}$ of a day and Janes in $\frac{2}{3}$ of a day: how long would it take them both together?
7. A can do a work in 2 days, $B$ in 3 days, but with the aid of C they can do it in $\frac{6}{11}$ of a day : how long would it take $C$ alone?
8. $A$ and $B$ do a work in 4 days; B can do in a day only $\frac{3}{5}$ as much as A: how long would it take each :

Sol.-B in 1 dily does $\frac{3}{5}$ as much as A. $\cdot$ in 4 days $4 \times \frac{3}{5}={ }_{\frac{1}{6}}^{2}$ A's work in 1 day.$~$ A working for 4 days $+{ }_{6}^{12}$ days does the whole work.
8. A and B do a work in $\frac{7}{8}$ of a day, A does per day $\frac{1}{2}$ more than $B$ : how long would it take each?
10. A does twice as much work as B in a given tinee, and C does ${ }_{3}^{4}$ as much work as A and $B$ together, and all together can do a picce of work in $24 \frac{4}{7}$ days: how long would it take each?

Sol.-A's work per day + B's + C's $=2$ B's + D's +4 B's $=7$ B's work per day $=\frac{7}{18}$ of work. $\cdot$ B in 18 days, \&e.
 much as A and B, and all do a job in 7 days: find the time for each.
12. Two men or 3 boys can do a work in $\frac{1}{6}$ of a day: how long will it take 3 men and 2 boys to do it?
13. To do a piece of work A requires twice as long as 13 and $C$, and $C 3$ times as long as $A$ and $B$ to. gether; they all together do a piece of work worth $\$ 120$ : how should the money be divided?

Sol.-B's work per day + C's $=2$ A's.$\therefore$ A's + B's + C's $=3$ A's $\cdot \cdot$ A does $\frac{1}{3}$ of work and is entitled to $\$ 40$. So, A's + J's $=$ 3 C's $\cdot \cdot$. A's $+B^{\prime}$ 's $+C$ 's $=4$ C's, C does $\frac{1}{4}$ \&c.
14. D can dig a ditch in 9 days, and D and E in 6 days: how long will it take E to do what remains after D has done $\frac{2}{3}$ of it?
16. $C$ can do $\frac{13}{9}$ as much work as $A$ and $B$ together: and $B$ as much as $A$ and $C$ together ; they all together do a piece of work worth $\$ 110$ : how much should tach receive?

Examples.-28.

1. At what time after 3 o'clock are the hour and minute hands of a clock together?

Sol.-Minute hand gains 11 rounds in 12 hours ; at 3 o'clock, hour hand is $\frac{1}{4}$ round in advance; 1 round in $\frac{12}{1}$ hour, $\therefore \frac{1}{4}$ round in $\frac{1}{4} \times \frac{2}{11}=\frac{3}{11}$ hour past 3 o'elock.
2. What time after 15 minutes past 7 will the bauds of a clock be together?
3. At $\frac{1}{2}$ past 4 o'clock how many minutes will elapse "Gore the minute hand will be opposite the homr hand
4. What is the first time after 8 o'clock that the fands of a watch will be five minutes' space apart?

5 At a $\ddagger$ to 4 o'clock how many minutes will elapse before the minute hand is three hours' space in advance of the hour hand?
6. What is the first time after twelve o'clock that the hands of a clock will form an angle of 120 degrees?
7. The time since 6 o'clock is $\frac{5}{7}$ of the time to noon: vhat o'clock is it?

Sol.-Time to noon $+{ }_{7}^{5}$ of do. $=\frac{1}{7}$ of do. $=0$
hours $\cdot \therefore \frac{1}{7}$ of do. $=\frac{1}{2}$ an hour, and the whole
$=7 \times \frac{1}{2}=3 \frac{1}{2}$ hours. $.8 \frac{1}{2}$ hours a.m.
6. If $\frac{1}{2}$ the time past noon is equal $\frac{f}{6}$ of the time to aldnight, find the time.
9. Half the time since midnight is $\frac{1}{2}$ of the time to 10 o'elock a.m. : what o'clock is it?
10. A clock which is right on Monday at noon, loses 2 minutes in 4 hous : what is the true time when it shows 4 o'clock p.m. on 'Tuestay?
11. What is the hour if $\frac{2}{3}$ of the time since 10 o'elock u.m., is the time to 3 o'clock p.m. ?
12. Supposing the minute hand of a clock to move from right to left, while the hour hand moves in the ordinary way, and that the hands are together at 12 , what hour will they indicate when they aro next together.
13. Find the time when $1 \frac{2}{3}$ of time since 9 o'clock A. 1 . is the time to 9 o'elock p.m.
14. It is between 9 and 10 o'clock, a line joining the points of the minate and the hour hand forms an isosceles triangle having each of the angles at the base double of the third angle : find the time.
15. What is the hour when $\frac{1}{2}$ the time since 6 p.m. is $\frac{1}{1}$ of the time since midnight?
16. Two watches hang side by side, and both show 12 o'clock at the time of observation ; one keeps correct time, the other loses 10 minutes in 12 hours: in how many hours will the minute hands be at right angles to each other?
17. There is a mechanical contrivance resembling a clock; numbers from 1 to 20 are marked at equal intervals round the dial ; the hands move in the same direction, one passing over two spaces in $\frac{3}{4}$ of a minute, while the other passes over 10 . If the hands are placed together at 8 , what number will they indicate when they are next together ?

Examples.-29.

1. The sum of 2 numbers is 40 , their difference $i$ 8 : find the numbers.

Sol.-The less + the less $+8=2$ times less $+8=$ $40 . \therefore$ less 16 , greater 24.
Note.-The less $=\frac{1}{2}$ sum- $\frac{1}{2}$ the difference; the greater $=\frac{1}{2}$ the sum $+\frac{1}{2}$ the diffierence.
2. The sum of two numbers is 25 , their difference is 8 : find the numbers.
3. The sum of two fractions is $\frac{7}{9}$, their difference is $\frac{1}{3}$ : find them.
4. The sum of two mixed numbers is $8 \frac{5}{6}$, their dit erence is $2 \frac{1}{2}$ : find them.
5. If a man can row 8 miles per hour on still water, md a stream flows at the rate of 4 miles an $b \cdots r$, find he sum of their rates per hour.
6. If a marr can row 7 miles per hour on still water, and a strenm flows at the rate of 2 miles per hour, find the difference of their rates per hour.
7. If a man can row at the rate of 7 miles per hour on still water, and starts down a stream flowing at the rate of 3 miles per hour, how far down the stream will he go in 1 hour?
8. If a man can row at the rate of 7 miles per hour on still water, and starts up a stream which flows at the rate of 3 miles per hour, how far up the stream can ho go in 1 hour?
9. If the sum of a man's and a stream's rate is 10 ailes per hour, and their difference is 4 miles per hour, Gid their rates.
10. If, with the help of a stream, a man can go lu miles down in. 1 hour, and when the stream is against him he can come up 4 miles per hour, find their rates per hour.
11. A man, with the help of a stream, can row 24 miles in 4 hours: find the sum of their rates per hour.
12. A man rowing against a stream goes from $\boldsymbol{\Lambda}$ to 13, a distance of 33 miles, in 6 hours: find the diflerence of their rates per hour.
13. A man can row 8 miles down a stream in 1 hour and 20 minutes, and he can row back again in 2 hours: find his rate per hoar and the rate of the stream. Ans. 5 and 1 miles.
14. If a man can row down a stream 16 miles at the rate of $s$ miles per hour, and back again at the rate of 2 miles per hour, compare the ratio his time coming up the stream bears to his time going down the stream, with the ratio the sum of their rates per hour bears to the difference of their rates per hour.
15. A man can row down a stream in 50 minutos, and back again in 70 minutes: compare his rate with the rate of the stream.
16. A crew can row up a stream a certain distance in 64 minutes, and back again in 60 minutes : determine the distance, the rate of the stream being half a mile per hour.

Sol. --Whole distance down in 1 hour, 15 of distance up in 1 hour $\therefore$. it $_{6}$ of distance $=$ 2 rate of stream $=1$ mile, and distance $=$ 16 milem
20. A man can row 6 miles down a stream and up agrain in 2 hours 40 mimutes, and his rate of rowing in still water is twice as grent as the rate of the stream : find his rate of rowing.
21. How far may $u$ boat whose velocity is 8 miles un hour in still water, go up a stream whose rate is 4 miles an hour, so that the round thip may take only 8 hours?

Examples.-30.

1. A merchant sold cloth for $\$ 2$ a yard, and lost $\$ 6$; had he sold it at $\$ 4$ a yard he would have gained \$18: how many yards did he sell !

Scl. - \$2 more cn a yard makes a total difference of $\$ 0+\$ 18=\$ 24 . \cdot 24 \div 2=12$ yards.
2. A boy bousht some peaches for 3 cents each; hat he prid 5 eonts each, they would have cost 40 cents wore: how many did he buy?
3. A train moves fren $\Delta$ to $B$ in 6 homrs; if it fucreases its speed 10 miles per hour it will make the distance in 4 homs: find the listance.
4. A and $B$ walk towards each other, $A$ at the rato of : mi's an hour, and B at the inte of $4 \frac{1}{2}$ miles an hour ; whe a they meet it is forme that $B$ has walked 6 miles more than $A$ : find their distance apart when they set out.

Sol.-In a dist. of $4 \frac{1}{2}+3=7 \frac{1}{2}$ milos $A$ makes
it more than B. $\cdot$ he makes 6 miles more in 30 miles.
6. A news-boy bonght a number of papers at $22^{2}$ cents each, and had! 5 cents left; had he paid 3 cents each, he would have been 7 cents short: find the number of papers.
6. A man's board was 75 cents a duy, and his watges $\$ 2.25$; at the end of 40 days he had $\$ 45$ : how many days was he idle?
7. A man agrees to dig a weli for $\$ 4$ a day, on condition that he should forfeit $\$ 5$ for every idle day; he finished the well in 12 days, and received $\$ 30$ : how many days was he idle?

Sol. - Had he worked all the 12 days he would have received $\$ 48$; but he received only
$\$ 30 . \therefore \$ 48-. . \$ 30=\$ 18$ loss ; he loses $\$ 4$ $+\$ 5=\$ 9$ every idle day $. \therefore \$ 18 \div 9=2$ idle days.
8. $\mathbf{A}$ man is to receive $\$ 1.50$ for every day he works, and pay for every itlle day 50 cents for board; at the end of 24 diays he received only 824 : how many days did he work?

9 A man reecived $\$ 2.50$ a day for every day he worked, and paid 50 cents for every ille day; at the expiration of 40 day's he had saved $\$ 50$ : how many days was he idle?
10. A man bousht a number of sheep for $\$ 100$; having killed 8 of them, he sold $\frac{3}{3}$ of the remainder at cost, receiving for them $\$ 40$ : how many did he buy? Sol. $-\frac{2}{3}$ of rem. cost $\$ 40 \therefore$ rem. cost $\$ 60$, and the $S$ killed must. $\because$ have cost $8100-$ $\$ 60=\$ 10$, or $\$ 5$ each. $100 \div 5=20$, number bought.
11. A mall bought a momber of calves for $\$ 80$; he first sold 5 of them, and then $\frac{2}{3}$ of the remainder at eost for $\$ 40$ : how many did he hoy?
12. A person bourght a quantity of Canadian tweed for $\$ 150$; ater cutling of $6 y^{*}$ rats, he sold 啚 of the remainder for \$60 : how many yards tid he purchase?
13. A famer bought a number of sheep, and having kilfed 10 of them, he soid, at cost, $\frac{7}{10}$ of the re. mainder for \$294, which was \$186 less than the entire lot cost: how many did ho buy?
14. A dog killet $\frac{1}{4}$ of A's lambs; if he sells the mamander at cost he will recoive $\$ 120$; but reserving 8 , and selling $\frac{1}{2}$ of the remainler at cost, he will re. weive $\$ 44$ : 6 how many had he at first ?
15. When John was 8 years younger his age was ${ }_{3}^{3}$ of his present uge : how ohl is he?

$$
\text { Lixamples. - } 31 \text {. }
$$

1. If 20 ttss . of sea-water contain 1 ib . of salt, how mach fresh water musi be added so that $\mathfrak{f}$ His. of the hew mixture may contain \& 1 lb , of salt?

Sul. - $\frac{1}{5} \mathrm{Ib}$. salt in every 6 lbs . of new mixture $\therefore 1 \mathrm{ll}$. salt in every 30 libs. of ne: mixture $30-20=10 \mathrm{lbs}$. fresh water added.
2. If 50 lbs of sea-water contain 2 lbs . of salt, how monel fresh water must be added so that 5 tbs . of new nixture may contain $\frac{1}{6} \mathrm{mb}$. of sillt?
3. In a 60 -ounce mixture of silver and copper, there are 4 oz of colper' : how much silver must be added to the mixture so that there may be $\frac{1}{9}$ oz. of copper in 2 oz. of the mixture?
4. If a sample of alcohol contains 80 parts of every landred pure alcohol, and the rest water, how much water must be added so that the new mixture shall 1. mtatin 60 parts in every hundred pure alcohol?

Sol-60 parts alleohol in 100 of new mixture ; but there are 80 parts in all $\therefore$ if 60 patis be fouml in 100, 80 (which $=60+\frac{1}{3}$ of 60 ) will be found in $100+\frac{1}{3}$ of $100=1333$ - $33 \frac{1}{8}$ parts are to be added.
5. How much water alded to alcohol 96 per cent, strong will reduce it to 80 per eent, strong?
6. In a drove of 100 animals consisting of horsen und cows, the latter are to the former as $2: 3$ : how many horses must be sold that there may remain 4 cows to 5 horwes?
7. In a mixture of 120 lbs . of green tea and black, the quantity of green is to that of black as $3: 5$ : how much green tea must be added so as to make the ratio of green to black as $5: 3$ \}
8. How much water added to 25 gallons on alcohol 30 per cent. strong, will make it 75 per cent. strong?
9. If 62 lbs . of sea-water contain 2 hss . of salt, how much salt must be added so that 42 lts . of sea-water will contain 2 lbs . of salt?

Sol.-In given mixture there are 60 lbs . fresh
+2 of salt; in new mixture there are 40 tibs. of fresh +2 of salt. Then, if in 40 of fresh there are 2 of salt, in 60 of fresh there aro 3 of salt.$\therefore 1 \mathrm{lb}$. of salt is to be added.
10. If 75 lbs . of se,t-water contain 3 Dbs. of salt, how much salt must be added so that 10 lbs . of new mixsure will contain 1 B . of salt?
11. How much (weight) of fresh water must be added to 50 lbs . of brine 4 per cent. strong, to make the mixture 3 per cent. strong?
12. How much alloy added to 9 oz . of gold 22 carats fine will make 18 carats fine?

Sol. - $2_{2}^{2}$ of $9 \mathrm{oz} .=81 \mathrm{oz}$ of pu:o gold and of alloy in $1^{\text {st }}$ case, in $2^{\text {ad }}$ case the ratio is $18: 6=3: 1$, i.e., the pure gold is 3 times the alloy which. $\cdot=81 \div 3=\frac{1}{4}=23$ $\cdot 2 \frac{3}{4}-\frac{3}{4}=2$ oz. alloy to be added.
13. How much alloy added to 6 oz . of gold 20 carats fine, will give a simple 15 carats fine?
14. In a mixture of gold and silver consisting of S) $1 \%$. there are three oz. of silver: how much gold must be added that there maty be $z^{\prime} 0 \mathrm{oz}$ of silver to 1 oz, of gold ?
15. A chemist dissolved 3 oz . of a salt in 27 oz . of water; but when his assistant by mistake added more water, he, to find the gumatity of wator added, evaporated 1 oz . of the new mixture and found $\frac{1}{18}$ oz. of the salt: how much water hawi been added by the assistant?
16. If 5 dwt. of gold 22 carats fine he mixed with 3 dwt. 14 carats finc, :ssertain the fineness of the mixture.

$\therefore \quad$ " $\quad$ in 8 dwt. $=\frac{110}{24}+\frac{40}{24}=\frac{152}{24}$ und in 1 dwt. $=\frac{19}{2} \therefore 19$ carats fine.
17. If 8 oz of gold 18 curats fine be molted with $40 \% .15$ carats fine, what is the fineness of the mistuc?
18. $A$ has $\$ 40$ in gohl and silver; for every $\$ 3$ in swhi! !n has se in silver: how much gold must he added so that there may be 83 of silver to $\$ 9$ of gold 1
19. $4 \frac{1}{2}$ dwt. of goll 18 carats line are melted with $3!$ dwet. 22 carats tine : how fins is the mixture?
20. If one gallon of alcohol 96 per cent. strong is mixed with one quart 81 per cent. strong, how strully is the mixture?
21. How much atcohol 90 per eent. strong must be mixed with 1 grillons 75 per eemt. strone to make the mixiuve 85 pir cenl. strong 1

Sol.--1 gallon of 90 per cent. is 5 per cent. stronger than gallon of new mixture; 1 gallon of 75 per cent. is 10 per cent. weaker than gallon of ncw mixture.$\therefore \frac{1}{2}$ gallon of 75 per cent. compensates for 1 gallon of 95 per cent, and 4 gallons of 75 per cent. compensates for 8 gallons of 95 per cent., 8 is $\therefore$ the number required.
22. How much alcohol 96 per cent. strong must he mixed with 8 gallons 60 per cent. strong to make mixture 80 per cent. strong?
23. How many dwt. of gold 15 carats fine must be melted with 15 dwot. 22 canats fine, to make a mixture 18 carats fine?

## Examples, - 32.

1. Charles is 16 years ohd and Willie is 7 : in how many yens will Charles be twice as old as Willie?

> Sol.-16-7=9= differenee of ages, which is constant. At the required time C 's age $=$ 2 times W's, ${ }^{\circ}$. dilference of ages is 2 tim* W's - W's $=W$ 's $=9$, and $9-7=2$, the required time.
2. John is 28 yems old and Mary 8: in how many yaurs will John be "' times as old as Mary?
3. A man is 40 years old and his son 20 years: how long since the father was 5 times as old as the soll?
4. Charles is 18 years of age and Harry 15 years: how long since Harry was hali' the age of Charlea
5. Mary is 25 years old and Susic 7 years : in how many years will Susie be $\frac{1}{2}$ as old as Mary? $\frac{1}{3}$ as old?
6. A man is 48 years old and his son is 16 years: what was the man's age when he was 9 times as old as his son?
7. Julia's age is to Mary's as 3 to 2 , and the sum of their ages is 25 years: in how long will Mary's age be to Julia's as 5 to 6 , and what will then be the sum of their ages?
8. Two-thirds of John's age equals $\frac{4}{5}$ of William's, and the difference between their ages is 10 years: how long since John was 3 times as old as William ; Sol.- $\frac{2}{3}$ of J's $=\frac{4}{5}$ of W's age, and J's $=\frac{6}{5}$ of W's, and $\frac{6}{5}$ of W's $-W$ 's $={ }_{5}^{1} \mathrm{~W}$ 's $=10$ $\therefore$ W's age $=50, J$ 's $=60$. Also, when W. was born J. was 10 years old, when will $\mathbf{J}$. be 3 times as old? 3 W 's age - J's age $=$ 10 years . . W's age $=\mathbf{5}$ years, which was $50-5=45$ years ago.
9. Ilulf of A's age equals $\frac{1}{3}$ of B's age, and the differ. ence of their ages is $\mathbf{1 0}$ years : in how many years will $\frac{1}{8}$ of A's age equal $\frac{1}{4}$ of ll's.
10. Two thirds of $\Lambda$ 's agn equila $\frac{3}{3}$ of I's uge, and the sum of their ages is 68 years : how long since of of A's age equalled $\frac{4}{8}$ of 13 's $?$
11. Mary is $\frac{1}{4}$ as old as her aunt, but in 20 years she will be half as old: find the age of each.
12. A man is twice as old as his wife ; $\mathbf{1 6}$ years ago he was 3 times as old: find the age of each.

Sol.-Difference of ages=2 wife's age-wife's age wife's age (present) ; also, difference of
ages $=3$ wife's age一wife's ag' $=2$ wife's age (former) $=$ wife's present age $\cdot \cdot 16$ ycars $=$ wife's former age.
13. John is 5 times ans old as James, but in 8 years he will be only 3 times as old: find the arge of each.
14. When A married he was three times as old as his wife, but in 15 years he was only twice as oll: find the age of each at marriage.
15. T'en years ago $A$ was four times as old as B, now he is only twice as old: find their ages.
16. 'l'wo trains moving in the same direction at rate of 10 miles an hour, pass a station, one 54 minutes behind the other : how many minutes will elapse before the forward train is 4 times as far from the station as the other?

Examples.-33.

1. How far may a person go in a stage which makes fi miles an hom, so that by walking back at 4 miles an how he may bo gone only 5 liours?

Sol.-Me groes 1 mile in $\frac{1}{6}$ hour ; he returns 1 mile in $\frac{1}{4}$ hour.$\therefore$ he goes and returns 1 mile in $\frac{1}{6}+\frac{1}{4}=\frac{5}{5}$; and in 5 hours he goes and returns $5 \div i_{2}=10$ miles.
2. Ilow fir may a person ride in a coach at the rate of 10 miles an hour, so that walking back at 5 miles un hour ho may be gone only 6 homs?
3. How far may I sail in one steamer groing at rate of 15 miles an hour, so that returning at rate of 12 prices an lour I may be grene but 9 hours?
4. A stemmer whose rate of sailin! is 12 miles an hour, descended a river whose emrrent is 4 miles an hour, and returned; sho was gone 6 hours: how fiur did she go ?
5. A steamer whose speed is 10 miles an hour, plies between two cities on a river whose velocity averages $3 \frac{1}{2}$ miles an hour: if the trip down and un takes 9 hours, what is the distance betwern the phaces? Sol.--Rate down $=10 \frac{1}{2}+3 \frac{1}{2}=14$; rate $u p=$ $10 \frac{1}{2}-3 \frac{1}{2}=7$; then divide 9 homs in ratio of $14: 7=2: 1 . \therefore 3$ hours for time down, and 6 hours for time $\mathrm{up}_{\mathrm{p}}=42$ miles (see on Ques. 1).
6. A boat which can make 12 miles an hour, take; 12 hours for the round trip on a river whose current is 4 miles an hour how firl does she go?
7. If $:$ boat whose speed is 15 miles an hour is 3 hours making a trip down stream, and 6 hours in returning, what is the rate of the stream ant the length of the trip?
8. I went to Niagara (fiom Toronto), in the "City of 'loronto," which makes 14 miles an hour, and returned in the "Rothesay," which makes 15 miles an hour, and the romed trip took 4 hours and 50 minntes: timd the distance between 'loronto and Niagara.
9. Six men hire a conveyance for a certain sim, but taking in two more, the expense to each was reduced by 50 cents: what was paid for the conveyance? Sol.-Lxpense to 1 is climinished 50 cents. expense to 6 is diminished $6 \times \frac{1}{2}=\$ 3$ which the two pay, then 1 pays $\frac{1}{7} \frac{1}{4}$, and $8 \times 1 \frac{1}{2}=\$ 12$ whole cost,
10. Ten men hire a coach for a certain sum, but taking in 5 persons more the expense of each is reduced 20 cents: what did the coach cust them?
11. Five men hire a conveyance, but 3 more join them, and the expense of cach was reduced $\$ 1.50$ : what wis paid for the conveyance?

Sol. - 3 men make a difference of $\$ 5 \times \$ 1.50=$ $\$ 7.50 .1$ man makes a diflerence of $\$ 2.50$ and $8 \times 2 \frac{1}{2}=\$ 20$.
12. Three persons rented a church pew, and liy taking in two more, the expense of each was diminished \$3: what was the rent of the pew?
13. Ten men chartered a boat, but 2 of them failed to pay, and the expense of each of the others was increased 81.50 : what was charged for the hoat?
14. John bought 25 oratiges and had 15 given to lim, by which the average cost was reduced $1 \frac{1}{5}$ cent : what did the 25 cost?
15. A news-boy bought 20 papers, but losing 5 of them, the cost of each was increased $\frac{1}{2}$ a cent: what did he pay for the papers?

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\text { Examples. - } 34 \text {. }
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1. There is a fish weighing 72 bis. ; his head weighs twice as much as his tail, and his boty weighs as much as his head and tail together : find the weight of each part.
Sol. - Head $=2 \times$ weight of tail, body $=$ tail + head $=3$ $\times$ weight of tail $\therefore$ head + bolly + tail $=$ whole weight $=6 \times$ weight of tail $=72 . \therefore$ de.
2. A tish weighs $64 \mathrm{ll} . \mathrm{s}$; the head weighs 3 times
as much as the tail, and the body weighs as much an the head and tail together: find the weight of enck. part.
3. A watch and seal aro worth $\$ 160$, the cost of the seal is $\$ 8$ less than 20 per cent. of the cost of the watch: find the cost of each.
4. The liead of a fish is four feet long, the tail is as long as the head and half the body, and the borly is as long as the lead and tail: find the length of the fish?

Sol. - Head $=4$ feet, tail $=4$ fect $+\frac{1}{2}$ body $\cdot$. body $=\frac{1}{2}$ body +8 feet.$\cdot$ body $=16$ feet, ..nd $32=$ whole length.
5. The head of a fish is 3 feet long, the tail is as long as the head and half the boty, and the body is as long as the head and tail: find the whole length of the fish.
6. The tail of a pike weighs 3 ounces, the hear weighs as much as the tail and $\frac{1}{4}$ of the weight of the hody, and the body weighs twice as much as the head and tail : find the weight of the fish.
7. A boy spent $\$ 15$, and then earned $\frac{1}{3}$ as moh as he had remaining, and then found he had $\frac{1}{2}$ as much as he had at first: how mucl, had he at first?

Sol.-Remainder (alter spenting \$15) $+\frac{1}{3}$ of remainder $=\frac{4}{3}$ of remainder $=\frac{1}{2}$ he had at first. $\therefore \frac{3}{3}$ of remainder $=\frac{3}{8}$ what he had at first. $\cdot \frac{5}{8}$ what he had at first $=\$ 15$, and whole amount $=\$ 24$.
8. A man spent $\$ 22$, ant then earned $\frac{1}{4}$ of what he hatl left, and then had $\frac{1}{3}$ as much as he had at first: how much had he at first?
9. A boy paid out 40 cents, and afterwards received 75 per cent. of as much as he had remaining ; se then had $\frac{1}{6}$ more than he had at first : how much had he at first?
10. If my age 4 years hence be diminished by $\frac{3}{8}$ of $\mathrm{i}^{2}$ self, the remainder will equal $\frac{5}{6}$ of my age 6 years ago: find my age.
11. A boy went to a store and spent 21 cents, and then borrowing $\frac{1}{5}$ of what he had remaining, had $\frac{1}{2}$ as much as he had at first: how much had he at first?
12. $A, \mathrm{~B}$, and C live together for a certain time ; A and lipay the entire expense in the ratio of $2: 3$; C gives $\$ 25$ : how should this be divided between $A$ and 13 ?
13. Suppose that for every 4 cows a f.rmer has, he should plow an acre of land, and allow one acre of pasturage for every 2 cows: how many cows could he keep on 18 gries?

Sol.-4 cows require 1 acre plowed land. $\cdot 1$ cow requires $\frac{1}{4}$ acre, 2 cows require 1 acre pasture. $\therefore 1$ cow requires $\frac{1}{2}$ acre $\therefore 1$ cow requires $\frac{1}{4}$ acre $+\frac{1}{2}$ acre $=\frac{3}{4}$ acre $\cdot \cdot 18$ acres $\div \frac{3}{4}$ acre $=24=$ mmber cows.
14. A farmer has to plow 1 acre for every 3 cows kipt, and keep an acre of pasturage ior every 2 cows: how many cows can be kept on 30 acres?
15. A famer keeps 36 cows on 30 neres of plowed and pasture-land ; he plows one acre tor every 3 cows: how many acres of pasture must ho allow for 4 cows?
16. A farmer keeps 48 cows on 14 acres of plowed

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## IMAGE EVALUATION TEST TARGET (MT-3)





Photographic ${ }^{\circ}$ Sciences

and pastife-lands; he reserved 1 acre of pasture for every 6 cows : how many acres will he plow for every 16 cows?

Sol.-6 cows for 1 acre pasture.$\therefore 48$ cows for 8 acres; hence 6 acres plowed for 48 , and $\therefore 2$ acres for 16 cows.

$$
\text { Examples. }-35
$$

1. I sold goods at 10 per cent. gain, hut if they had cost $\$ 100$ more, I should have lost 10 per cent. by selling as I did : find the cost of the goods.

Sol. - ${ }_{10}^{9}$ of new cost $=\frac{1}{1} \frac{1}{0}$ of actual cost.
$\because$ new cost $=\frac{1}{9}$ of actual cost.
$\therefore \$ 100=\frac{2}{9}$ of actual cost, which $. \cdot=\$ 450$.
2. Goods were sold at 10 per cent. gain, but if they
if th gric cost hiul cost $\$ 60$ more, there would, at the same selling price, have been 10 per cent. loss : find the cost of the goods.
3. A merchant sold goods at a gain of 20 per cent. ; if they had eest $\$ 100$ more, the same selling price would have entailed a loss of 20 per cent. : what did the goods cost ?
4. A merchant inarked cloth to make a profit, at he supposed, of 20 per cent.; but the cloth had cost $\$ 3$ a yard more than he had supposed, and he therefore lost 25 per cent. : what did the cloth cost per yardi

Sul. - $\frac{3}{4}$ actual cost $==\frac{6}{6}$ supposed cost.
$\therefore$ actual cost $=\frac{\pi}{5}$ supposed cost.
$\therefore \$ 3={ }_{5}^{3}$ of supposed cost, which $. \therefore=$ $\$ 5$, and $\$ 5+\$ 3=\$ 8$, actual cost.
6. A merchant sold goods at 20 per cent. gain; but
if they had cost $\$ 150$ less, his gain at the same selling grice would have been 30 per cent. mote: find the cost of the goods.
6. I sold tea at a gain oif 25 per cent. ; if it had cost 10 cents a pound less, the same selling price would have realized 50 per cent. gain : find the cost of the tea per pound.
7. Sold tea at a loss of 20 per cent. ; if it had cost 25 cents a pound less, the same selling price would have gained 20 per cent. : find the cost of the tea per pound.
8. If an article had cost me 20 per cent. less, the gain would have been 30 per cent. more: what was the gain per cent.?

Sol.-'Taking 1 -fifth off the cost price (leaving the stane selling price) would give the same increase in the percentage as adding 1 -fourth to the selling price; then $\frac{1}{4}$ of selling price $=$ (by question) 30 per cent. of cost.$\because$ selling price $=120$ per cent. of cost ; and gain was 20 per cent.
Ur, new cost is 80 per cent. of the old ; to sell at old ecst would . $\cdot$ give a profit of 25 per cent. on new cost and nothing on old ; also, 1 per cent. on old cost represents $1 \frac{1}{4}$ per cent. on new cost, i.e., every l per cent. on old cost represents increase of $\frac{1}{4}$ per cent. on new cost . $\quad$ to give 30 per cent. - 25 per cent. $=5$ per cent. we should require $\theta+\hbar=20=$ per cent on old cost.

## mental arithmetio.

9. If an article had cost me 10 per cent. less, the same selling price would have brought me 12 per cent. more : what was the gain per cent?
10. If the cost had been 25 per cent. less, the gain, on same selling price, would have been 16 jer cent. more: find the gain per cent.
11. If the cost had been 8 per cent. less, the gain would have been 10 per cent. more: find the gain per cent.

Sol. -8 per cent. $={ }_{2}^{2}{ }^{2} 3 ; 2^{2}{ }^{2}$ off cost gives same increase in the per cent. as $\frac{{ }_{2} 3^{2}-2}{}=\frac{2}{23}$ added to selling price $\therefore \frac{2^{2}}{2}$ of selling price $=$ (by question) 10 per cent. of cost price; ${ }_{2}^{1} \frac{1}{3}$ of do. $=5$ per cent. of cost.$\therefore$ selling price $=115$ per cent. of cost, or gain is 15 per cent.
Note.-lt will be seen that $\frac{z}{3}$ off cost gives same as 4 on selling price; $\frac{3}{3}$ off is same as $\frac{2}{6}$ on; $\frac{1}{n}$ of same as $\frac{1}{n-1}$ on, and generally $\frac{a}{b}$ off cost $=a^{a} \downarrow$ on selling price.
12. If cost had been 16 per cent. less, gain would have been 20 per cent. more: find the gain per cent.
13. If cost had been 4 per cent. less, the gain would have been $4 \frac{2}{3}$ per cent. more: find the gain per cent. at which the goods were sold.
14. If cost had been 20 per cent. less, gain would have been 28 per cent. more: find gain per cent.
15. If cost had been 20 per cent. less, the gain, per cent. at same selling price, would have been doubled: at what per cent. profit were the goods sold 1

Sol. -20 per cent. $=\frac{1}{6} ; \frac{1}{5}$ off cost $=\frac{1}{4}$ on melling price, thus $f$ selling price $=$ gain
cent.
wonld
17. less, great
18.
tain goods his $g$ more
19.
cent. loss:
per cont. $\cdot \cdot \frac{3}{4}$ of selling price $=$ cost hence there is gain of 1 in $3=33 \frac{1}{3}$ per cent.

Illustration.-Let $100=$ old cost, then $80=$ new cost, and $133 \frac{1}{3}$ selling price; now 80 sells for $133 \frac{1}{3}=66 \frac{2}{3}$ per cent. gain.
16. If the cost of certain goods had been 25 per cent. less, the gain per cent. (same selling price) would have been trebled : find the gain per cent.
17. If the cost of an article had been 30 per cent. less, the gain per cent. would have been $2 \frac{1}{2}$ times as great: find the gain per cent.
18. A merchant marked his goods to make a certain rate of profit; he afterwards found that the goods had actually cost him 5 per cent. less, and that his gain per cent. was in consequence 6 per cent. more : for what rate of profit dirl he mark his goods?
19. If the cost of certain goods had been 12 per cent. more, the gain per cent. would hive een 15 loss: find tine gain per cel ${ }^{\prime}$.

Sol. -12 per cent. $=\frac{3}{2^{3}} ; \frac{x^{3}}{5}$ increase in cost $=25^{3}+\frac{3}{2}={ }^{3}$ recrease in selling price $=(b y$ question) 15 per cent. of cost.
$\therefore 2^{1} 8$ of selling price $=5$ per cent. uf cost, and selling price $=140$ per cent. of cost, and. $\because$ gain was 40 per cent.
20. If cost of certain gools had been 10 per cent. more, the gain per cent. would have been 12 less: find the gain pes ceato
21. If the cost had been 20 per cent. more, the gain per cent. would have been 25 less : find the gain per cent.

Note.-If cost is $\frac{1}{2}$ more, gain will be $\frac{\}}{3}$ of selling price less; cost $\frac{1}{8}$ more, gain less; cost $\frac{1}{n}$ more, gain $\frac{1}{n+1}$ of selling price, less, \&c. If cost $\frac{2}{5}$ more, selling price $\frac{2}{a+b}$ less.
22. If the cost of goods had been 20 per cent. more, the gain per cent. would have been only onehalf what it actually was: find the gain per cent. Sol.- $\frac{1}{5}$ on cost, same as $\frac{1}{6}$ off selling price; hence $\frac{1}{6}$ selling price $=\frac{1}{2}$ gain per cent.; and selling price $=3$ gain per cent., and gain per cent. $=\frac{1}{3}$ selling'prico.$\therefore \frac{2}{3}$ of selling price $=$ cost ; there is.$\cdot$ a gain of 1 on 2 , or 50 per cent.
23. I bought goods, and mark them to make a certain rate per cent. of profit; I afterwards found that the goods had cost me $33 \frac{1}{3}$ per cent. more than I had thought, and my gain was only $\frac{1}{3}$ as much per cent. : at what per cent. profit were the goods marked?
24. Two merchants sell cloth at the same marked price, bat one, having given 25 per cent. more for the cloth than the other, makes 30 per cent. less. : what per ceat. on cost is the marked prico 8

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\text { Examples.- } 36 .
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1. A store-keeper, on a certain day, first took in as much money as he began the lay with, then paid out $\$ 10$, then took in as much as he had left, then paid out $\$ 20$, and had $\$ 40$ left: how much cash did ho begin the day with?

Sol.-He had $\$ 40$ at closing . $\cdot \$ 40+\$ 20$ $=\$ 60 ; \$ 60 \div 2=\$ 30=$ amount left after first payment $(\$ 10) . \therefore \$ 10+\$ 30=$ $\$ 40$ and $\$ 40 \div 2=\$ 20=$ amount with which he began the day.
Note.-In such questions it is generally easier to begin with last result, and work backwards.
2. A man began the day with taking in as much cash as he had, then paid out $\$ 6$, then took in as much as he had left, then paid out $\$ 3$, and had $\$ 25$ left: how much had he at first?
3. B took in twice as much as he had and then paid out $\$ 1$, then took in 3 times as much as he had ieft, then paid out $\$ 17$ and had $\$ 70$ left : how much had he at first?
4. C first took in half as much money as he had, then paid out $\$ 3$, then took in $\frac{1}{3}$ as much as he had left, then paid out $\$ 2$, and had $\$ 10$ left : how much had he at first?
5. $\Lambda$ man paid out $\$ 22$, then took in $\frac{1}{4}$ as much as he had left, and then had $\frac{1}{3}$ as much as he had at first: how much had he at first?
6. John borrowed as much money as he had, then sjent 8 cents, then borrowed as much as he had left, and spent 30 cents, and had 34 cents left : how much had he at first 1
7. $A$ min spent $\frac{1}{2}$ his money and $\$ \frac{1}{2}$ more, then $\frac{1}{2}$ of what remained and $\$ \frac{1}{2}$ more, and then had $\$ 6.75$ remaining : how much had he at first ?

$$
\underset{7}{S o l .-\$ 63}+\frac{1}{2}=\$ 7 \frac{1}{2} \text { remainder after }
$$

$$
\begin{aligned}
& \text { first payment. } \therefore \text { first payment }=2 \times 7 \frac{1}{4} \\
& =\$ 14 \frac{1}{2} \text {, and } \$ 14 \frac{1}{2}+\$ \frac{1}{2}=\$ 15=\frac{1}{2} \text { of } \\
& \text { original sum, which } . \therefore=\$ 30 .
\end{aligned}
$$

8. A man sjent $\frac{1}{2}$ his money and $\$ 5$ more, then $\frac{1}{2}$ of what remainel and 敋 more, then $\frac{1}{2}$ of what $\mathfrak{r}$ mained and $\$ \frac{1}{2}$ more, mul then had $\$ 3$ left: how much had he at first?
9. D first took in $1 \frac{1}{2}$ times as much cask as he had, then paid out $\$ 5$, then took in $2 \frac{1}{5}$ times what he had left and paid out $\$ 8$, and then had $\$ 24$ left : how much had he at first?
10. A boy spent $\frac{1}{2}$ his money and $\$ \frac{1}{2}$ more, then $\frac{1}{2}$ the remainder and $\$ \frac{1}{2}$ more, and then had $\$ 3$ left : how much had he at first?
11. A lady bought a silver wateh for $\$ 20$, also a gold watch and a chain, which together cost 4 times as much as the silver watch; the chair. and silver watch cost twice as much os the gold watch : find the value ot each.

> Sol._Gold watch $=\frac{1}{2}$ chain $+\$ 15$; chain + gold watch, $i . e .$, chain $+\frac{1}{2}$ chain $+\$ 15=$ $\$ 120 . \therefore 3$ of chain $^{3}=120-15=\$ 105 ;$ chain $=\$ 70$, ctc.
12. A man had $\$ 6$ in silver, and also some copper: and gold; the copper with the silver was twice the gold; the silver with the gold was 5 times the copper : how much of each kind had he 3
1.
tract the so the $n$
2. $\$ 10 \mathrm{n}$ 3. 10 ho in ter still
4. a disc per ce article
5. papers rach; gain?
6.
intere month (per a the no

## CILAPTER IV.

## QUESTIONS FOR EXAMINATION.

## I.

1. Increase a certain number by $33 \frac{1}{3}$ per cent., extract the cube root, then multiply by 8 , and extract the square root of the product-the result is four : find the number.
2. Divide $\$ 148$ among $\mathrm{A}, \mathrm{B}, \mathrm{C}$, so that B may have $\$ 10$ more than $C$, and $A \$ 17$ more than $B$.
3. A boat floats down stream a certain distance in 10 hours, and is rowed back by a man in 4 hours: find in terms of tho distance the man's rate of rowing in still water.
4. A person marks his goods so that he maty allow a discount of 5 per cent. and siill make a profit of 20 per cent.: what should be the marked price of an article that cost 95 eents?
5. A newsboy spent 85 cents in papers, taking 3 papers at $3 \frac{1}{3}$ cents each as often as 2 papers at $3 \frac{1}{2}$ cents rach; he sold all at 5 cents each: how much did he gilin?

Sol.-3 at $3 \frac{1}{3}=10,2$ at $3 \frac{1}{2}=7 ; 85$ divided in ratio of 10: 7 gives 50 cents and 85 cents $\therefore 15$ papers and 10 pipers, etc.
6. A note for $\$ 150$, drawn at 4 months, and bearing interest at 8 per cent., is discounted by a broker 2 months before maturity, the hover makes 12 per cent. (per annum) on his money: what does he pay for the notel
7. Find a fourth proportional to $108,972,343$.
8. A man willed $\$ 2,200$ to two children, whose ages were 11 yea's and 16 years respectively, in such a why that the shates would, at five per cent. simple interest, amount to equal sums when the children became of age: what were the shares?
9. If I retail goorls at a profit of 20 per cent., and sell at wholesale for 2.5 per cent. less than at retail, what rate per cent. do I gain at wholesale ?
10. A sum of money amounts to $\$ 370$ in six ycars, and to $\$ 330$ in four years : find the sum of money and the rate.
11. A las three times as much money as B, but if he gives $13 \$ 8$ they will have equal sums: how much has each ?

## II.

1. The circumference of the fore-wheel of a carriago is 12 feet, of the hind wheel 14 feet: how fir will the carriage go before two points, at the same time in contact with the ground, will again touch the ground together?
2. Find the smallest sum of money that can be exactly paid with guineas, sovereigns, or marks.
3. If a number be increased 25 per cent., and the sum be increased by 20 per cent., the result will be 30 : find the number.
4. A and $B$ own 40 per cent. and 60 per cent. respectively of a dish of berries; C joins them, and the three eat the berries; C gives 30 eents for his share: $b$ w much of this should $A$ get?

5 time sum
5. The interest on a sum of money for a certain time and rate is $\$ 110$; the discount is $\$ 88$ : find the sum.

Sol. - $\$ 100-\$ 88=\$ 22$, which is interest on discount ; $\$ 88$ produces $\$ 22$ interest, and $\overline{\text { 呙 }}$ $=\frac{1}{4}$; i.e., the interest $=\frac{1}{4}$ principal $. \cdot 110 \times$ $4=440$, the required sum.
6. A sold a horse to B for $\$ 200$, and took his note mayable in 70 days. A got the note discounted at the bank at 10 per cent., and found he had mude a protit of $16{ }_{3}^{2}$ per cent. : what did the horso cost A?
7. A father divided $\$ 48$ among 2 sons and 3 danghters, giving each son half as much as each daughter : how much did each receive?
8. Bought 80 barrels of flour, part at $\$ 10$ and the "est at $\$ 8$ a barrel ; the whole cost $\$ 740$ : how many barrels of each kind were there?
9. The difference between one number and $\frac{2}{3}$ of another is 7 ; the sum of the numbers is 32 : find them.
10. A fish can swim from $A$ to $B$ and back again in 4 hours, swimming against the stream 4 times as fast as tho rate of the stream: find the rate of the stream in terms of the distance.

## III.

1. In a cricket match the scores in each successiv innings are $\frac{1}{3}$ less than in the promering innings, ant the side which has had the first innongs wins by 20 what are the scores in each innings?
2. If a crew can row from $A$ to $B$ in 40 minute . and back again in 35 minutes, compare the rates on the stream and boat 1
3. John can run 10 yards whilst James runs 11 yards: what start ought James to give John in a quarter of a mile race so as to win by 1 yard?
4. James has 10 marbles, John has as many as James and $\frac{2}{3}$ of Robert's, and Robert has as many as John and uames: how many have they all $?$
5. At what time between 6 and 7 will the hour ail minute hands of a clock point directly oposite? At what time between 2 and 3 ? Between 7 and 8 ?
6. A man sold cider that cost $\$ 2.50$ a gallon for $\$ 3$. The puice of tho cider rose to $\$ 3$, he watered it so that ho could still sell it at $\$ 3$ and make the same profitas before: how much water did he put with 10 gallons of cider?
7. $\Lambda$ person insured his life for $\$ 6,000$ at the rate of $\$ 0.20$ per cent. After prying 4 premiums he died: how much more did his family receive than was paid out for preminas $?$.
8. A and B agreed to cut some wood for $\$ 40$; when the work was partly done $\Lambda$ was taken sick and received only $\$ 10$ : what part of job was finished when $A$ took sick?
9. How long will a boy take to walk around an oblong plot of gromd $\frac{1}{4}$ of a mile long by $\frac{1}{8}$ of a mile wide, if he takes 15 steps of two feet each in half a minute?
10. Divide $\$ 2$ between 3 persons, so that the first may have $\$ \frac{1}{5}$ more than the third, and $\$_{10}^{7}$ less than second.
IV.

1 Twothirds of the square of twing a number is
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equal to $\frac{4}{3}$ of the squure of $\frac{3}{2}$ of the number diminished by 3: find the number.
2. The sum of two rumbers is 40 , the difference and $\frac{1}{3}$ of one of them is 20 : find the numbers.

Sol.-The difference $+\frac{1}{3}$ of one of them $=$ difference between one and $\frac{1}{3}$ of the other, $\therefore$ first $=20+\frac{3}{3}$ of sceonal, and.$\therefore$ second $+\frac{2}{3}$ of do $+20=40$; hence $3_{3}^{3}$ of second $=20$; second 12 , first 28.
8. A quantity of tea was sold at 10 per cent. gain : if it had cost $\$ 60$ more the same selling price would have entailed 10 per cent. loss : find the cost of the tea.
4. A merchant laid out $\$ 1,000$ in buying cloth, paying 25 cents a yard for 25 per cent. of the cloth, and $33 \frac{1}{3}$ cents a yard for the remainder : how much will he cleat by selling the cloth at 50 cents a yard?
5. A kind of brass is made by fusing together old brass, refined copper, and zine, in the proportions of 3 , 4, 5: how much of each kind must be taken to produce 150 lbs . of brass, after allowing $6 \frac{1}{4}$ per cent. for waste $?$

Sol. $-6 \frac{1}{4}$ per cent. $=\frac{1}{16}$ of amount wasted . $\cdot$ $\frac{15}{15}$ of do. $=150,-\frac{1}{16}=10$ and $\frac{16}{16}=160 \mathrm{lbs}$. to be taken ; divide this in ratio of $3,4,5$.
6. The numerator of a fration is 25 per cent. less than the denominator, and the sum of both is 448 : find the fraction.
7. The dimensions of a writing-table which contains 24 square yards, are as $9: 11$ : find them.
8. A, B, C trade in company ; A's capital is to B's
as $3: 5$; C took $\$ 100$ of the $\$ 420$ gained during the half year : find the gains of A and B , also C's stock.
9. The base of a right-angled triangle is 60 per cent. of the hypotheneuse, the perimeter being 240 : find the area of the square described on the perpendicular from the right angle on the hypotheneuse.
10. If the cost had been 20 per cent. less, the loss would have been 15 per cent less : find loss per cent.

## V.

1. INow much carpeting $\frac{3}{7}$ of a yard wide will be required to cover a floor 15 feet long and 12 feet wide?
2. The quotient of a division is twice the re. mainder, and the division twice the quotient; the sum of eight times the divisor, increased by 8 , and three times the remainder, decreased by 4 , will equal 18 times the quotient: find the dividend.
3. A father divided among his three sons, A, B, and $C, \$ 4,000$ of Grand Trunk Railway stock, so that the sum of A's share and half the united shares of $B$ and $C$, will be $\$ 2,750$, and the sum of $B$ 's shave and half the united shares of $\mathbf{A}$ and C , will be $\$ 2,450$ : how much stock must $B$ obtain from $A$ and $C$ respectively, so that each son may have the same amount of stock?
4. A and $B$ agree to perform a job of work which they can do in 30 days, working 10 hours a day. If they complete the work before the 30 days have expired, they are to have $\$ 2$ extra for every day intervening between the completion of the work and the expiration of the specified time. A can do as
much hours extra divid
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much work in 5 hours as B can do in 6 ; B works 2 hours extra per day for 15 days, and A $2 \frac{1}{2}$ hours extra per day for 12 days: how should the money be divided?
5. A person lent a certain sum of money at 8 per cent. per annum, interest payable half-yearly. In receiving the interest for the first half-year, he unfortunately took a comnterfeit bill of $\$ 20$. The remainder of the half-yeu's interest was to the whole half-ycar's interest as $7: 8:$ find the principal.
6. A certain sum is put out at interest at 10 per cent. ; $3 \frac{1}{2}$ times the interest for one year $\times \$ 20$ equals ${ }_{i}^{4}$ of the amount for one year - $\$ 15$ : required the principal?
7. There are two numbers such that $\frac{1}{2}$ of the greater equals $\frac{9}{3}$ of the less. If $\frac{1}{2}$ the greater be divided by $\frac{1}{8}$ of the less, and this quotient by incrased by $\frac{1}{2}$ the the sum of the two numbers, the result will be 128 : find the numbers.
8. A can do a piece of work in 12 days; B can do in the same time $33 \frac{1}{3}$ per cer more work than $A$, but he does less than C by $33 \frac{1}{3}$ per cent. of C's work; $B$ and $\mathbf{C}$ work together 2 days, and then leave : how long will it take A to finish?
9. The difference between the simple and compound interest of a certain sum of money for 2 years at $\delta$ per cent. is $\$ 3.20$ : find the principul.
10. The length of a room is $\frac{14}{5}$ times the height, and the height is $\frac{5}{7}$ of the breadth; it requires $106 \frac{9}{8}$ yards of paper 2 feet wide to preper the walls: how much will it cost to plaster the ceiling at 15 cents per equare yard

## V1.

1. The sum of three fractions is 2 ; the numerators, when reduced to equivalent fractions laving least com. denominator, are 4, 3, 5 : find the fractions.
2. A man bought stock at 25 per cent. below par, and sold it at 20 per cent. above par ; he gained $\$ 000$ : how much stock did he buy?
3. A person discounts a note due in 15 months (without interest), so as to make 10 per cent. on his money : what rate of interest did he exact on the face of the note?

Sol. -10 per cent. for 12 months $=12 \frac{1}{2}$ per cent. $=\frac{1}{8}$ for 15 montlis.$\therefore$ what he pays for note $+\frac{1}{8}$ of ditto $=\frac{9}{8}$ of ditto $=$ face of note.$\therefore$ he pays $\frac{8}{9}$ of face of note, i.e., takes off $\frac{1}{9}$ or $11 \frac{1}{9}$ per cent. ; this for 15 months $=8 \frac{8}{9}$ per cent. per ammum.
4. A pipe $\frac{1}{2}$ an inch in dianeter will till a cistern in 20 minutes, the cistern being empty : how long a time will be required to fill it when there is a discharge pipe of $\frac{1}{4}$ inch diameter?
5. If 1 gallon of alcohol 96 per cent. strong is mixed with 1 quart 81 per cent. strong, what per cent. strong is the mixture?
6. Four circular plates of gold, two of them being of 3 inch radii, and the others of 4 inch radii, and all 1 inch thick, are melted into a single circular plate $\frac{1}{2}$ inch thick : find its radius.
7. The amount of A's money for 2 years at 5 per cent. is $\$ 60$ more than its interest for 9 years, at 10 per cento: how much has he?
8. Two partners, A and B, gain $\$ 300$; A owns within $\$ 40$ of $\frac{2}{3}$ of the entire stock, and B's gain is $\$ 120:$ required each man's stock.

Sol.-If A owned $\frac{2}{3}$ his gain would be $\$ 200$; but his gain is only $\$ 180 . \therefore \$ 200-\$ 180$ $=\$ 20=$ gain for $\$ 40$ (which is the amount less than $\frac{2}{3}$ ) $=\therefore \$ 40$ gains $\$ 20$, $\$ 1$ gains $\$ \frac{1}{2} \cdot \$ 600$ to gain $\$ 300$.
9. Paid 25 per cent. duty on a watch, and sold it at a loss of $33 \frac{1}{3}$ per cent. ; had it been sold for $\$ 44$ more, there would have been a gain of $16 \frac{2}{3}$ per cent. : find the price at which the watch was invoiced.
10. How far may one ride in a stage making 5 miles an hour, that he may walk back at 3 miles an hour, and be gone but 8 hours?

## VII.

1. A man invested $\frac{1}{3}$ of his money in bank stock at 120 , and paying 8 per cent. dividends, and the remainder in railway stock at 80 , and paying 5 per cent. :lividends: his income from both investments was 8115 : find the amount of each investment.

Sol.--In first case income is $\frac{1}{1} 5$ of investment $\therefore$ on $\frac{1}{3}$ it $=\frac{1}{8} \times \frac{1}{13}=\frac{1}{45}$.

In second case income is $\frac{1}{16}$ of investment $\therefore$ on $\frac{2}{3}$ it $=\frac{2}{3} \times \frac{1}{16}=\frac{1}{24}$.
$\therefore$ total income $=\frac{1}{45}+\frac{1}{24}=\frac{8}{36} 0+\frac{15}{360}$
$=\frac{23}{360}$ of investment $=\$ 115$.
$\therefore \frac{1}{6} \frac{1}{6}$ of income $=\$ 5$, whole $=\$ 1,800$
$=$ or $\$ 600, \$ 1,200$.
2. A and B gain $\$ 240$; A owns $\frac{3}{4}$ of the stock lacking $\$ 10$, and B's share of the gain is $\$ 65$ : find the whole stock, and the share of each?
8. The amount of a sum of money at a certain rate per cent. for 2 years is $\$ 290$, and for 4 years at $\frac{1}{2}$ the rate per cent. is $\$ 330$ : find the sum and rates.
4. A ball 3 inches in diameter weighs 4 ounces: what would a ball 2 inches in diameter weigh if composed of material 50 per cent. heavier than that of the first?
5. The difference between the interest and the dis. count on a sum of money for $1 \frac{1}{2}$ years at 8 per cent. is $\$ 18$ : find the sum of money.

Sol.-8 per cent. for $1 \frac{1}{2}$ years $=12$ per cent.
$=\frac{{ }_{2}}{5} 5 \cdot$ discount $=\frac{3}{28}$ and $\frac{3}{25}=\frac{3}{28}=$ ${ }_{7}{ }^{9}{ }_{00}=\$ 18 . \therefore \$ 1,400$.
6. $\frac{2}{3}$ of the time since $7 \frac{1}{2}$ o'clock a.m. equals $\frac{1}{2}$ the time to $9 \frac{1}{2}$ o'clock p.m.: what o'clock is it?
7. I sold goods at double their cost, but if the cost had been $\$ 15$ more, the gain would have been only 20 per cent.: find the cost.
8. The breadth of a room is to its length as $\mathbf{6}: \mathbf{\epsilon}$; it costs $\$ 30$ to carpet it with material 27 inches wide and $\$ 1.25$ a yard : find the length and breadth of the room.
9. A man had to give $\$ 51$ in bills fur $\$ 50$ in gold : at what rate of premium was gold?
10. If a town pays its tax collectors 5 per cent. and allows 5 per cent. for uncollected taxes, what should be the amount of assessment to realize $\$ 36,100$ !

## VIII.

1. A can walk 10 miles in $2 \frac{1}{4}$ hours, B can walk 15 miles in $3 \frac{1}{3}$ hours. They start to walk a match from Toronto to Whisby, a distance of 30 miles: which will arrive first, and by what amount of time will he win?
2. By selling vinegar at 1 cent per pint above cost, the gain is 50 per cent.: what per cent. is gained when it is sold at 6 cents a gallon above cost?
3. If the income tax is 5 per cent. what income nets, after paying the tax of $\$ 1,000$ ?
4. The L. C. M. of two numbers is 72 and the G. C. M. is 3 , one of the numbers is 9 : what is the other?
5. From Toronto to Guelph is 48 miles, and $\frac{5}{4}$ of this distance plus 3 miles is $\frac{1}{4} \frac{1}{4}$ of 7 times the distance from Berlin to Montreal: find the distance from Berlin to Montreal.
6. A person walks from Toronto to Brampton at the rate of 4 miles an hour, and after resting $\frac{1}{2}$ an hour rides back at the rate of 6 miles an hour and he finds he has been absent $10 \frac{1}{2}$ hours: find distance between places.
7. A lady bought some eggs at the rate of 3 for 5 cents and had 10 cents left. Had she given 25 cents a dozen she would have needed 5 cents more to pay for them: how many did she buy?
8. A person sold two houses for $\$ 3,960$ each, making 10 per cent. on one and losing 10 per cent. on the other : taking both sales into account, what was his gain or loss :
9. A publisher takes off $53 \frac{1}{3}$ per cent. of his retail prices for a wholesnle customer: what per cent. will the wholesale customer gain if he sells at the publisher's retail prices?
10. A father left some money to be divided between his three sons in the proportion of $\frac{1}{2}, \frac{1}{3}$ and $\frac{1}{4}$; the money was invested at 6 per cent., the yearly interest being $\$ 234$ : how much of the principal should each receive?

## IX.

1. How many yards of carpeting $2 \frac{1}{2}$ feet wide are inquired to cover a hall floor 7 feet wide and 15 feet long ?
2. The circumference of the hind wheels of a perambulator is $7 \frac{1}{2}$ feet and of the forewheels $3 \frac{7}{8}$ : over what distance will they pass before they are in the same relative positions as at starting? How many revolutions will each wheel have made?
3. How far can a boy ride in a carriage going at the rate of 9 miles an hour, provided he walks back at the rate of 6 miles an hour, and is gone only 10 hours?
4. A pickpocket robbed a gentleman of $\frac{4}{5}$ of his money; when he was arrested he had made away with $\frac{3}{4}$ of it, and had $\$ 50$ left: How much had the gentleman at first?
5. John and James have $\$ 60$, and 50 per cent. of John's money equals 60 per cent. of Jamea' : how ruch had each?
6. A and B can do a piece of work in 6 days; A and $O$ in 8 days, and $B$ and $C$ in 9 days: how many day: would each take working alono?
7. A gang of thieves stole 26 fowls, half of them getting 4 each, the rest 3 each, except two who obtained but 2 each: low many were there in the gang?
8. If $\$ 4$ is allowed as 12 months' discount off a bill for $\$ 76$, and at the same rate $\$ 7$ be allowed off a bill for $\$ 91$, for how long was the latter sum discounted?

Sol.—Disct. $={ }_{7}^{4}=\frac{1}{15} \therefore$ int. $=\frac{1}{1}$ : $:$ so disct. $=\frac{7}{91}=\frac{1}{13} \therefore$ int. $=\frac{1}{12}$; and since int. is proportional to the time, we have required time $=\frac{18}{1} \frac{1}{2}$ of 12 months $=18$ months.
9. What is the least sum of money with which a farmer can purchase lambs at $\$ 2 \frac{1}{2}$, sheep at $\$ 7 \frac{1}{2}$, ind pigs at $\$ 3 \frac{1}{3}$ each, and how inany ot each can he buy with this sum of money?

$$
\mathbf{X}
$$

1. Onc person expends $\$ 6$ in coal at 98 a ton, aml another $\$ 8$ in coal at $\$ 10$ a ton : what fraction of a ton has the or: ? more than the other?
2. Fifty men have provisions to last 60 days at a cortain rate of supply. Ten more min coming, and the daily supply being made $\frac{1}{3}$ less thai before, how long will the provisions last?
3. If a certain number is increased by 6 and then multiplied by 3 , the product divided by 9 and the quotient diminished by 4 , the remainder is $8:$ what is the number?
4. If I ask $20 \%$ profit on an article, but fall $10 \%$ on mj, asking price, what rate of profit do I make?
5. Divide $\frac{3}{8}$ into two parts, so that one may be ${ }_{4}^{3}{ }_{0}$ lean than the other.
6. An agent received $\$ 3,150$, from which he was to take his commission on the sum invested. The commission was at the rate of $5 \%$ on the sum invested: how many acres did the agent buy if the land cost $\$ 20$ an acre?
7. How many acres in an oblong garden, 40 rods by 15 rods? How many feet of lumber required to fence it with a tight board fence, 6 feet high?
8. A train starts at the rate of 30 miles an hour and runs at that rate for 20 minutes. It then increased its speed to $50 \%$ of its former rate: how far did it run in all during the first hour?
9. The product of three numbers is 105 , two of them are to each other as $\frac{1}{6}$ to $\frac{7}{48}$, and the third is $7 \frac{1}{2}$ : what are the numbers?
10. I sold $\$ 700$ worth of goods so as to gain $12 \frac{1}{2} \%$ of the proceeds, and another lot which cost $\$ 400$, so as to gain $20 \%$ of the proceeds: find gain $\%$ on the whole 1

## XI.

1. A room 24 feet long, 18 feet wide and 10 feet high, has a base board 6 inches wide all round: how many rolls of paper $1 \frac{1}{2}$ feet wide and 14 yards long will it take to paper it, allowing 3 rolls for the openings?
2. What will 24 packs of envlopes cost, each pack containing 25 , if a thousand cost $\$ 5$ ?
3. A dog overtook a fox after running half a milf. Four-fifths of the distance the fox ran, after the dog started, was 8 rods less than 6 times the start he had: how many rols start had the fox?

## QUESIIONS FOR EXAMINATION.

4. A does a piece of work in 5 days, B In 6 days, und C in 8 days; $\$ 60$ is paid for the work: what should each receive when they work together?
5. John has $\$ 30$ in gold and silver, and for every $\$ 6$ of gold he has $\$ 4$ of silver: how much gold must be added that there may be $\$ 3$ of gold for every $\$ 3$ of silver?
6. A man floats down a stream a certain distance in an hour and rows back in twenty minutes : compare his rate of rowing in still water with the rate of the stream.
7. A boy having 60 pigeons in one coop and a smaller number in another, found that by putting twice the number in the smaller coop from the larger, he had the same number in both coops.
8. Two horses trot in the same direction round a circular course $1 \frac{1}{2}$ miles long. One goes at the rate of 8 miles an hour, the other at the rate of 12 : how long after starting will they be together again?
9. From a pile of wood 20 feet long, 4 feet wide and 6 feet high, was sold $\$ 13.50$ worth, at $\$ 6$ a cord : how much was what remained worth, at $\$ 5 \frac{1}{2}$ a cord?
10. The head of a fish is $\boldsymbol{T}$ inches long; the tail is as long as the head and $\frac{1}{3}$ of the body, and the body is as long as the heau and tail : how long is the fish 1

## XII.

1. Eight persons engaged a pleasure boat, but before they start 4 more join them; the expense of oach is diminished by $\$_{\substack{2 \\ ~}}$ what did they pay for the boat :

2 If 4 men can remove $\frac{1}{8}$ of a heap of stones in fis of a day, how many men will be neceled to remove the whole heap in $\frac{1}{3}$ of a day?
3. A boy ugrees to carry 30 glasses to a certain stute for 8 cents a piece, on condition that for euch cre ho broke he should forfeit 12 ecnts; he received $\$ 1.40$ : How many did he break ?
4. A mixture of black and green tea weighing 7 lbs. is worth $\$ 3.90$; if the proportions of each are interchanged the mixture will le worth $\$ 3.80$; the black tea is worth 60 cents per lb. : find the price of the green tea.
5. A gardener has an oblong plot of ground $20_{6}^{5} \mathrm{ft}$. long by $12 \frac{1}{2} \mathrm{ft}$. wide, which he wishes divided into square lots of the largest size possible: how many lots will he have?
6. A gracer bought 16 bushels of potatoes; the good at 40 cents a bushel, and the bad at 25 cents. The whole ecst $\$ 5.35$ : how many bushels were good?
7. A :ope 34 feet in length was broken, so that $\frac{2}{3}$ of the length of the longer piece was equal to $\frac{3}{4}$ of the length of the shorter: what was the length of each pic:3?
8. A cat is 40 leaps ahcad of a dog, and takes 7 leaps to the dog's 4 , but 3 of the dog's leaps are equal to $(i$ of the cat's: how many leaps will the cat take be'nre bring caught?
9. Mary meeting some beggars gave each 6 cents, and had 25 cents remaining; had she given each 8 cents, she would have had 3 cents left : how many beggars were there 1
10. A garrison of 150 men have provisions for 80 days allowing each man 4 lhs . a day; after 50 days 50 more join them and their daily rations is diminished 1 lb . a day: how long will their supplies last?

## XIII.

1. If $2 \frac{5}{8}$ yards of cloth cost $\$ 4 \frac{1}{3}$, what will $5 \frac{1}{3}$ yards cost?
2. Five men agree to do a piece of work, but two of the men not coming, the work was prolonged $3 \frac{1}{2}$ lays: in what time could the 5 men do it?
3. A merchant sells 35 inches for a yard and at an advance of $\frac{1}{3}$ on cost: find his gain per cent?
4. What is the time, provided $\frac{2}{3}$ of the time past midnight, plus $1_{\frac{1}{1}}$ hours, equals $\frac{2}{6}$ of the time to midnight?
5. How far can a boy ride with his father who leaves Brampton for Toronto at 7 o'clock in the morning, and can drive the distance, 22 miles, in $3 \frac{1}{7}$ hours, so that he may be back at 9 o'clock for school, if he walk at the rate of $3 \frac{1}{2}$ miles an hour?
6. A pole is fixed in the bottom of a river. Three feet are in the air, the part in the water is 3 times as long as that in the mud, and the part in the mud is $i^{-4} 5$ of the rest of the pole : how long is the pole?
7. How many stones 3 feet long by 2 feet wide and $1 \frac{1}{2} \mathrm{ft}$. thick will it take to build the walls of a hoase 18 feet long, 12 feet wide and 3 feet thick, and 4 feet high ?
8. A boy engaged with his master for $\$ 80$ a year and a suit of clothes, but leaving at the end of 5 months, he received $\$ 24$ and the suit of clothes : find its valae
9. A room is 20 feet long und 16 feet wide: what must be the height in order that the wea of the floor and ceiling together may be equal to the area of the walls?
10. Two trains, each 88 yarls loug, when moving in the same direction pass each other in 18 seconds, and in 6 seconds when moving in opposite directions: find the rates of the trains.

## XIV.

1. The difference between the interest and the dis. count on a sum of money for one ycar and 9 months at 8 per cent. per annum, was $\$ 9.30$ : finc the sum of money.
2. A room whose length is $1 \frac{1}{6}$ times its brealth, and height 12 ft ., takes 156 yards of paper, 24 inches wide, to cover its walls : what will it cost to carpet the floor with earpet 27 inches wide and $\$ 1.25$ per yard?
3. The interest on a sum of money for 5 years is $\$ 140$, and the discount for the same time and rate in $\$ 100$ : find ther sum and rate per cent.

Sol. $-140-100=40=$ int. on $100 \therefore \frac{40}{100}=$ $\frac{2}{5} i . e .$, int. is $\frac{2}{5}$ of principal! $\therefore$ disct. $=\frac{7}{7}$; then 140 is $\frac{2}{5}$ of $\$ 3502$ principal, \&c.
4. A grocer bought green tea and black in the ratio of $2: 1$, the former costing 70 cents per pound, the latter 80 cents-the whole costing $\$ 44$ : how much will he make by selling the whole at a uniform price of 90 cents per pound?
5. What amount of accounts must an agent collect in order to pay over $\$ 1,100$ after retaining $8 \frac{1}{8}$ per cents for collecting?
6. An agent sold goods on a commission of 2$\}$ ver sent., and reserving his commission for totn transaccions, purchased bank stock on a commission of 2 jer cent. on the price paid; his entire commission being $\$ 150$, find what the goods sold for, and what was paid ont for the stock.
7. Find the cost of 3,600 yards of ribon at $28.11 d$., and the square of 711 .
8. A merchant buys cotton at 12 cents a yard : at what rate per cent. of profit must he sell it so that the money he receives for 50 yards may equal his gain on $\$ 24$ of outlay ?

Sol.-For $\$ 24$, are bought 200 yds. $\therefore$ gain on 200 yds . $=$ selling price of $50 \mathrm{yds} .=$ cost of 50 yds + gain on do. $\therefore$ gain on 150 yds. $=$ eost of 50 yds., or $33 \frac{1}{3}$ per cent.
9. Coffee at 30 cts ., and chicory at 10 cts . a pound are mixed in such proportions that the mixture sold at 30 cents, making a profit of $33 \frac{1}{3}$ per cent.: in what proportion were they mixed?
10. A debt after a deduction of 3 per cent. becomes $\$ 194$ : what would it have been after a deduction of 4 per cent?

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\mathbf{X V} .
$$

1. A grocer by selling 8 lbs . of tea at a certain rate, gained 25 per cent. afterwards he increased his price, giving only 7 lbs. for the same money: how much per cent did he make at his increased price?
2. A merchant marked cloth 25 per cent. in advance of cost, and in selling it used a yard stick 1 inch too short; his entire gain was $\$ 42$ : find the cost price of the cloth $:$

## mental arithmetio.

Sob. - 25 per cent. $=\frac{1}{4}$ honest gain ; 1 inch gained on $35=\frac{1}{3} 5$, on which there was a gain of 25 per cent. $=\frac{1}{4}$, or $\frac{1}{3} \frac{1}{3}+\frac{1}{4}$ of $3^{\frac{1}{5}}=\frac{1}{2} 5 \therefore$ entire gain $=\frac{1}{4}+\frac{1}{2}=\frac{2}{7}$ of cost $=\$ 42 ; \frac{1}{7}=\$ 21, \& c . ?$
8. A person invests a sum of moncy in railway stock at 80 , and paying 4 per cent. dividends, and $1 \frac{1}{2}$ times as much in bank stock at 120 , and paying 8 per cent. dividends; his income from both investments is $\$ 300$; find the amount invested in each kind of stock?
4. I had money at interest at 8 per cent.; afterwards the rate was reduced to 5 per ceric., and my annual interest was $\$ 168$ less: how much had I at interest?
5. A merchant bought 400 lbs . tea and 1600 lbs . sugar, the cost of the latter per lb. being $\frac{1}{6}$ that of the former ; he sold the tea at a protit of $33 \frac{1}{3}$ per cent., and the sugar at a loss of 20 per cent; his net gain was $\$ 60$ : find his buying prices?

Sol.-Take cost of tea as unit, then tea being 1 , sugar $=\frac{1}{6}$ of the same quantity ; but there is 4 times 23 much, $\therefore$ tea 1 , sugar $\frac{4}{6}=\frac{2}{5}$, gain on former, $\frac{1}{3}$ loss on latter, $\frac{1}{5}$ of $\frac{2}{5}=\frac{1}{18}$ $\therefore$ net gain $=\frac{1}{3}-\frac{2}{15}=\frac{1}{5}=\$ 60$, and whole $=\$ 300 \therefore$ sc.
6. Write down the resuit of $39211^{2}-39101^{2}$ ?
7. If the cost of goods had been 20 per cent. more, the gain would have been 25 per cent. less: what was the gain per cent?
8. How much alloy added to 6 ox. of gold 20 carats fine, will make it 15 carats fine? .
9. The interest on a principal for 6 years was $\$ 261$, and the disoount $\$ 180$ : find the princiniN and the ravo.
10. Reckoning bank discount at 5 per cent. a person would receive $\$ 21$ less than the nominal value of a note which has a year to run: what would he receive for the note if true discount were deducted?

## XVI.

1. Find the sum of the squares and the cubes of the numbers $1,2,3,4,5,6$.
2. A man is engaged to work at $\$ 1$ a day and his board, with the understanding that he is to pay $37 \frac{1}{2}$ cts. a day for his board when idle : what must be the pro. purtion of working time so that he may just kepp out of debt, supposing that he works whole days and not parts in every case?

Sol.-Wages, \$8 $;$ loss on idle days $=\$ \frac{11}{8}$, L. C. M. $=\$ 88=11$ working or 8 idle days. $\cdot\left\{\frac{1}{9}\right.$.
3. When 1 guinea is the amount of $£ 1$, for what sum is I guinea the interest?

Sol.-Amomst $=\frac{2}{3} \frac{1}{0} \cdot$ interest $=\frac{1}{2} \sigma \cdot{ }^{\circ}$ principal $=20$ interest $=£ 21$.
4. Which is the more profitabie, a cord of wood which costs $\$ 4.75$, and $\$ 1.25$ for cutting, etc., generating a temperature of $72^{\circ}$ in my room for 24 days, a ton of coal which costs $\$ 5$, which would generate a temperature of $70^{\circ}$ for 25 days, but for a loss of 80 lbs . per ton from dust and dross?

Sol. -80 lbs per ton $=4$ per cent. $=$ loss $=1$ day in 25 , leaves 24 days same as wood; $72^{\circ}$ costs $\$ 6$ with wood $\cdot 1^{\circ}$ cosis $\$ \frac{1}{\mathrm{~T}_{2}}$; with coal, $70^{\circ}$ costs $\$ 5$, or $1^{\circ}$ costs $\$ \frac{1}{14} . \therefore$ coal better.
6. Sold a horse for $\$ 246$, and lost 18 per cent. of
what he cost: what should be the selling price so that the gain might be 18 per cent. on the cost?

Sol. --18 per cent. cost $=\$ 246,1$ per cent. $=\$ 3$, cost $=\$ 300,18$ per cent. $=\$ 54$, price= $\$ 354$.
6. Bo ught benanas at 4 for a quarter, and as many at 6 for a quarter; sold them all at 5 for a quarter and lost $\$ 1$ on the business : how many bananas were bought, and what did they cost?
7. A dishonest baker set out with a basket of loaves which weighed 4 lbs . instead of 5 lbs . each; he had sold $\frac{3}{4}$ of his lot, by which his frauduleut gain was 48 cts., when the rest were confiscated, and his total loss was equal to $\frac{3}{6}$ of $b^{\text {: }}$ loaves: find the number of loaves.

Sol.-Gain $=\frac{1}{5}$ price, gain on $\frac{3}{4}=48$ cts., on whole 64 cts. . $\cdot 64 \times 5=\$ 3.20$, real value of bread; $\frac{1}{4}$ confiscated worth $\frac{4}{5}$ of $\frac{1}{4}=\frac{1}{3}$ real value of bread $=64$ cts. partial loss $\cdot \therefore$ total loss $=12$ cts. $\cdot \cdot$ price $=16 \mathrm{cts} . \cdot \cdot 20$ loaves.
8. A boy bends his hoop into the form of a triangle whose sides are 7,17 , and 20 inches: what was the diancter of the hoop, given circumference $=\frac{2}{7}$ diameter?
9. If a square rood be divided into 10 equal squares, what is the length of a diagonal of each of these smaller squares?

Sol.-Square rood - 1210 yards . $\therefore$ smaller square $=121$ square yards.$\therefore 1$ side $=11$ yds., and diagonal $=\sqrt{2} \overline{\times 11^{2}}$ or $11 \sqrt{2}$ yds.
10. The nickel cent is 1 inch in diameter : find the area of the space enclused by 3 coins, placed so as to
touch each other, knowing that the area of a circle is equal to $3-1416$ square of 1 dius, and area of equilateral triangle $=433$ square of side.

## XVII.

1 What number must be added to or subtracted from the product of the sum and difference of 11 and 14 , so that it will contain 13 evenly?
2. How many times greater is the L. C. M. of 4, 6 and 8 than the H. C. F. of $\frac{1}{2}$ and $\frac{2}{3}$ ?
3. The L. C. M. of two numbers is 63 and their G. C. M. is 3 ; one of the numbers is 9 : find the other?
4. A grocer bought 100 gcese and turkeys for $\$ 65$; for the geese he paid 30 cts each and for the turkeys 80 each : find the number of each kind.
5. A father dying leaves his estate to his two sons, ages 19 and 20 respectively, to be divided so that each shall have equal amounts at maturity. In what proportion should it be divided, interest at 5 per cent per annum? (a) Simp!e Interest. (b) Compound Intcrest.
6. A man wishing to sell a horse asks 20 per cent. more than it cost; he finally sold it for 25 per cent. less than his asking price and lost $\$ 15$ on cost: what was his asking price?
7. What should be the Policy of Insurance at 5 per cent. on a diamond necklace worth $\$ 380$, so that if lost the owner shall recover the premium and value of the necklace?
8. If the true discount off a note of $\$ 420$ for a certain
time be $\$ 20$, what will be the discount off a note of $\$ 100$ for three times as long?
9. Two quaities of vinegar, No. 1 and No. 2, are mixed in the $p$ oportion of $2: 3$. No. 1 is worth 15 cents a gallon, and No. 210 cents a gallon: what should be the marked price per gal. so that there may be a gain of 25 per cent. on cost after lowering the asking price 10 per cent?
10. Find tho perimeter of a rectangular plot of land whose length is $2 \frac{1}{2}$ times its brealth and contains $1,000 \mathrm{sq}$. perches
11. A speculator sells his goods at a profit of 50 per cent., but the purchaser fails and pays only 50 cts. on the $\$ 1$ : how much per cent. did the speculator lose or gain on his venture?

## XVIII.

1. Two partners gain $\$ 480$; A puts in $\$ 560$ more than $\frac{1}{3}$ of the stock, and his shime of the gain is $\$ 260$ : find the stock contributed by each.
2. What is the length in yards of a piece of cloth originally $1 \frac{1}{3}$ yards wide, provided the eloth after shoinking 10 per cent, in length and width, contains 9 full square yards?
3. Paid $\$ 34.50$ for corn at $\$ 0.75$, wheat at $\$ 1$, and oats at $\$ 0.50$ a bushel : sold $\frac{2}{3}$ of the corn and $\frac{1}{2}$ of the wheat at 50 per cent. advance, gaining on the corn $\frac{2}{3}$ as much as on the wheat, and on the sale, the cost of the oats : how much of each did I buy?
4. If an article had cost me 10 per cent. less, my gain would have been 11 per cent more: what was my rate of gain or loss $?$
5. At what time between 5 and 6 o'clock do the hour and minute hands make equal acute angles with the line from 12 to $6 ?$
6. At a certain time between 8 and 9 o'clock the minute hand was between 9 and 10 , within an howr afterwards the hands had changed places : what was the time first mentioned?
7. A boy sold two knives at the same price ; on the one he gained 20 per cent. on the other he lost 20 . He lost two cents by the bargain: find selling and cost price of each?
8. A sold a sheep, and lost 25 per cent; if he had paid $\$ 1$ more for it he would have lost 40 per cent: what did he pry for the shecp?
9. Bought a hind and a fore-quarter of lamb, weighing together 24 lbs ; the hind-quarter was 12 cts. and the fore-quarter 8 cts. per lb. ; the two cost me 8 cts . more than if $I$ had bought the whole at an average price of 10 cts. per $\mathbf{l b}$. : how mition did each quirter weigh ?
10. The true discount on a sum of money for a yrar and a half at 8 per cent. being $\$ 12$, fiml the true dis count on the same sum and for same time at $55_{8}^{5} \mathrm{D}^{\prime \prime \cdot} \cdot$ ©



[^0]:    $\dagger$ The elegant solution (No. 1), page 17, was suggested independently by Mr. Fessenden, of Brampton, an accomplished mathematician. It is substantially the same as that given lu the praface to the "Exanumatioy Papmar in Aritionetic."

[^1]:    - Rules derived from actual multiplication.

