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## THE CANADTAN JOURNAL.

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## A POPULAR EXPOSITION OF THE MINERALS AND GEOLOGY OF CANADA.*

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Read, in abstract, before the Canadian Institute, December 5th, 1859.

## Introductory Notice.

In attempting to convey to the general reader a practical or really useful knowledge of the Minerals and Geology of Canada, it is advisable to consider the subject under the following heads:

1. How minerals are distinguished from one another.
2. The minerals and metallic ores met with in Canada.
3. How rocks are classified and distinguished.
4. Organic Remains: their use and teachings.
5. Subdivisions and distribution of Canadian rocks.

The term "Geology" comprises, strictly, a knowledge of the physical history of the Earth, as revealed to us by the study of the rock-

[^0]masses which lie around and beneath us; and by a comparison of the results of ancient phenomena, with the forces and agencies still at work in modifying the surface of the globe. As geology is thus essentially based on the study of rocks and their contents, and as rocks are made up of a certain number of simple minerals, it is necessary, or at least advisable, to obtain a knowledge of these latter (so as to be able to recognize them when met with), before proceeding to the discussion of the rocks into which they enter. With these minerals, also, it is convenient to consider a few others of economic application and common occurrence, including the more important metallic ores. In this consideration, the characters or properties by which minerals are distinguished from one another will first be explained, introductory to a Tabular Distribution of Canadian minerals. The latter will be so arranged as to enable the reader to make out the name of any one of the included species, with great facility.

## I. How Minerals are distinguished from one another.

Minerals are distinguished from one another by certain characters or properties which they possess : such as form, degree of hardness, fusibility, \&c. Hence, it is to these characters that our attention must be first directed.

Mineral characters are of two kinds : physical or external characters, and chemical characters. The former are exhibited by the mineral under ordinary conditions; the latter, only when the mineral is exposed to the action of heat or mineral acids, by which, in general, a certain degree of chemical decomposition is effected. Hence the term "chemical" as applied to these latter characters.

The physical properties of minerals are somewhat numerous; but many, although of the highest interest in indicating the existence of natural laws, and in their relations to physical science generally, are not readily available as a means of mineral discrimination. These, consequently, will be omitted from consideration in the following pages; and the other characters will be discussed only in so far as they admit of direct application to the end in view-namely, the practical discrimination of minerals one from another.*

[^1]The following are the characters in question :

> 1. Aspect or Lustre.
> 2. Colour.
> 3. Streak.
> 4. Form.
> 5. Structure.
> 6. Hardness.
> 7. Specific Gravity.
> 8. Relative Malleability.
> 9. Magnetism.
> 10. Taste, \&c.

1. Aspect or Lustre. -We have here to consider, first: the kind; and, secondly, the degree or intensity of the lustre, as possessed by the mineral under examination. The kind of lustre may be cither metallic, as that of a piece of copper, silver, \&c.; or sub-metallic, as that of most kinds of anthracite coal; or non-metallic, as that of stones in general. Of the non-metallic lustre there are several varieties, as, more especially : the vitreous or glassy lustre-example : rockcrystal ; the resinous lustre-ex. : native sulphur; the pearly lustreex.: tale; the silfy lustre (usually accompanying a fibrous struc-ture)-ex.; fibrous gypsum ; the stony aspect; the earthy aspect, \&c. These terms sufficiently explain themselves. Occasionally, two kinds of non-metallic lustre are simultaneously present, as in obsidian, which exhibits a "resino-vitreous" aspect; and the lustre in some zeolites is pearly within, and vitreous externally. In mica, and some few other minerals, there is frequently a pseudo-metallic lustre. This may be distinguished from the metallic lustre properly so-called, by being accompanied by a degree of translucency, or by the powder of the mineral being white or light-colored: minerals of a true metallic aspect being always opaque, and their powder being always black or dark-colore. So far as regards the metallic and the nonmetallic lustres, there are very few minerals which exhibit (in their different varieties) more than one kind. Thus, galena, the common ore of lead, copper pyrites, \&c., always present a metallic lustre; whilst, on the other hand, quartz, feldspar, calc-spar, gypsum, \&c., are never found otherwise than with a non-metallic sspect. Hence, by means of this easily-recognized character, we may divide all minerals into two broad groups; and thus, if we pick up a specimen
and wish to ascertain its name, we need only look for it amongst the minerals of that group with which it agrees in lustre. The first step towards the determination of the substance will in this way be effected.

The degree of lustre may be either splendent, shining, glistening, glimmering, or dull; but the character is one of comparatively little importance.
2. Colouti.-When combined with a metallic aspect, colour becomes a valuable character in the determination of minerals, because it then remains constant as regards a given substance. Thus galena, the common ore of lead, is always lead-grey; copper pyrites, always brass-yellow; native gold, always gold-yellow; and so forth. When accompanied, however, by a vitreous or other non-metallic lustre, colour is, practically, a character of no value; as in that case, the mineral may present, in its different varieties, every variety of colour. Thus, we have colourless quartz, amethystine or violet quartz, red quartz, yellow quartz, \&c., just as in the vegetable kingdom, we have red, white, and yellow roses; and dahlias, \&c., of almost every shade. When combined with a metaliic aspect, the colour is said to be metallic; and of metallic colours we may enumerate the following:

```
White... \(\left\{\begin{array}{l}\text { Silver-white ...... ex. Native silver. } \\ \text { Tin-white }\end{array}\right.\)
    (Tin-white ......... ex. Pure tin; cobalt ore.
Grey ... \(\left\{\begin{array}{l}\text { Lead-grey......... ex. Galena. }\end{array}\right.\)
    Steel-grey......... ex. Specular iron ore.
Black ...... Iron-black (usually with sub-metallic lustre) ex. Mag.
                                netic iron ore.
Yellow.. \(\left\{\begin{array}{l}\text { Gold-yellow ...... ex. Native gold. } \\ \text { Brass-yellow..... ex. Copper-pyrites. } \\ \text { Bronze-yellow (a brownish-yellow) ex. }\end{array}\right.\)
Red ........Copper-red ....... ex. native copper.
```

These metallic colours are often more or less obscured by a black, brownish, purple, or iridescent surface-tarnish. Hence, in noting the colour of a mineral, a newly-fractured surface should be observed. The non-metallic colours comprise, white, grey, black, blue, green, red, yellow, and brown, with their various shades and intermixtures; as orange-yellow, straw-yellow, reddish-brown, greenish-black, \&c. In minerals of a non-metallic aspect, the colour is sometimes uniform; and at other times, two or more colours are present together, in
spots, bands, \&c., as in the varieties of quartz, called agate, bloodstone, jasper, and so forth. In Labradorite, or Labrador feldspar, a beautiful play or change of colour is observed in certain directions. The finer varieties of Opal also exhibit a beautiful and well-known iridescence.
3. Streak.-Under this technical term is comprised the colour of the powder produced by drawing or "streaking" the mineral under obserration, across a file or piece of unglazed porcelain. The character is a valuable one on account of its uniformity; as, no matter how varied the colcur of a mineral may be in different specimens, the streak will remain of one and the same colour throughout. Thus, blue, green, yellow, red, violet, and other specimens of fluor spar, quartz, \&c., exhibit equally a white or "uncoloured" streak. The streak is sometimes "unchanged," or of the same tint as the external colour of the mineral; but far more frequently it presents a different colour. Thus, Cinnabar, the ore of mercury, has a red colour and red streak; realgar, or sulphide of arsenic, has a red colour and orange-yellow streak; copper pyrites, a brass-yellow colour, and greenish-black streak; and so forth. In certain malleable and sectile minerals, whilst the colour remains unchanged in the streak, the lustre is increased. The streak is then said to be "shining." Finally, it should be remarked, that in trying the streak of very hard minerals, we must crush a small fragment to powder, in place of using the file; because otherwise, a greyish-black streak, arising from the abrasion of the file, might very possibly be obtained, and so conduce to error. It may be observed, however, that all minerals of a non-metallic aspect, and sufficient hardness to resist the file, have a white streak.
4. Form.-The forms presented by minerals, may be either regular or irregular. Regular forms are called crystals, whether the minerals which present them be transparent or opaque. The term "crystal" was first applied to transparent vitreons specimens of quartz or rockcrystal; but, as it was subsequently found that opaque specimens of quartz presented exactly the same forms, and that oporque as well as transparent forms of other minerals existed, the term gradually lost its original signification, and came to be applied to all regular forms of minerals, whether transparent, translucent, or opaque. Minerals of a metallic lustre are always opaque; and many of these, as iron pyrites and galena, occur frequently in very regular and symmetricai
crystals. Crystals originate in almost all cases in which matter pas se from a gaseous, or liquid, into a solid state; but if the process take place too quickly, or the matter solidify without free space for expansion, crystalline masses, in place of regular crystals, will result. If a small fragment of arsenical pyrites, or native arsenic, be heated at one end of an open glass tube (five or six inches long and one-fourth of an inch in diameter), the arsenic, in volatilizing, will combine with oxygen, and form arsenious acid, which will be deposited at the other end of the tube, in the form of minute octahedrons (Fig. 3, below). In like manner, if a few particles of common salt be dissolved in a small quantity of water, and a drop of the solution be evaporated gently (or suffered to evaporate spontancously) on a piece of glass, numerous little cubes and hupper-shaped cubical aggregations will result. Boiling water, again, saturated with common alum, will deposit octahedral crystals on cooling: the cooled water not being able to retain in solution the full amount of alum dissolved by the hot water. In like manner, sugar, sulphur, and other bodies crystallise by slow cooling from the molten state.

The study of crystal-forms constitutes the science of Crystallography. To enter into the details of this science would extend our present discussion beyond its proposed limits, and carry us altogether beyond the object in view-the simple determination of the names of commonly-occurring minerals-and hence we shall confine ourselves to the general statement, that crystals admit of being arranged in six groups, or "systems;" the forms of each individual group passing into one another by simple transitions, but having no relations to the forms of the other groups.* The names of these respective groups,

[^2]Part III.-Optical and other physical relations of Crystallography.
with figures of a few of their more common forms and combinations, are given in the annexed tabular view.

The Monometric or Regular System.-This group includes the cube (Fig. 1), the rhombic dodecahedron (Fig. 2), the regular octahedron (Fig. 3), trapezohedrons or leucitoids (Fig. 4), pentagonal dodecahedrons (Fig. 5), \&c. Fig. 6 is a combination of the cube and


Pig. 1.


Fig. 2.


Fig. 3.


Fig. 4.


Fig. 5.


Ftg. 6.


Fig. 7.
octahedron ; Fig 7, a combination of the cube and pentagonal dodecahedron. Native gold, silver, copper, iron pyrites, galena, magnetic iron ore, garnet, fluor spar, rock salt, and numerous other minerals, crystallize in this system.

The Dimetric or Square-Prismatic system.-This includes, principally, square-based prisms and pyramids (or octahedrons), and their combinations. Figures $S$ and nine are examples of Dimetric crystals.


Fig. 8.


Fig. 9.

Amongst minerals, Copper Pyrites, Tin-stoue, Zircon, and Idocrase, may be cited as belouging to the group.

The Hexagonal system.-Regular six-sided prisms (Fig. 10) and pyramids (Fig. 11), combinations of these (Fig 12), rbombohedrons
(Figs. 13 and 14), and scalenohedrons (Fig. 15), are included under this system. Graphite, Red Silver ores, Cinnabar, Specular Iron Ore, Corundum, Quartz, Beryl, Apatite or phosphate of lime, Cal-


Rig. 10.


Tig. 13.


Fig. 11.

Fig. 34.



Rig. 12.


Fig. 15.
carcous Spar, Dolomite, and Carbonate of Iron, are some of the principal minerals which belong to it.

The Trimetric or Rhombic system.-This system iucludes rightrhombic prisms, rectangular prisms, rhombic octahedrons, \&c., and their combinations. Fig. 16 is a rhombic prism; figs. 17 and 18 are


Fig. 16.


Fig. 17.


Fig. 18.
combinations beionging to this system. White iron-pyrites, mispickel or arsenical pyrites, native sulphur, topaz, staurolite, arragonite, heary spar, celostine, and Epsom salt, are some of the principal minerals which belong to this group.

The Monoclinic or Oblique Rhombic system.-Rhombic prisms and pyramids, and rectangular prisins and pyramids, with obligue or sloping base, belong to this system. Figs. 19 and 20 are monoclinic
combinations. The principal minerals comprise: Augite, Hornblende, Epidote, Orthoclase, or potash feldspar, Stilbite, and Gypsum.


Fig. 19.


Fig. 20.

The Triclinic, or Doubly Oblique system.-The forms of this system are oblique (or they incline) in two directions. The crystals in general are more or less flat and unsymmetrical in appearance. No two planes meet at right angles; and there are never more than two similar planes present in any crystal belonging to the group. Axinite, Albite or soda feldspar, Labradorite or lime feldspar, and sulphate of copper, are the principal tricinic minerals.

Such is a brief exposition of the six crystal systems. For present purposes it will only be necessary for the student to impress upon his memory the following forms, so as to be able to recognize them when met with. The cube (Fig. 1), the regular octahedron (3), the shombic dodecahearon (2), the pentagonal dodecahedron (5), the cubo-octahedron (6), the regular six-sided prism (10), a combination of a six-sided prism and pyramid (12) a rhombohedron (13 and 14), a scalenohedron (15), a rhombic prism (16).

The irregular forms presented by minerals are of very subordinate importance; so that a few of the more common need only be mentioned. Most of the terms used in reference to these, explain themselves.

Irregular mineral forms:-Globular or nodular, ex. quartz, iron pyrites; reniform or kidncy-shaped, ex. quartz, \&c. ; botryoidal mammillated: a form made up of a series of rounded elevations and depressions, or otherwise exhibiting a surface of this character, ex. red and brown iron ore, calcedony, \&c.; stalactitic, ex. calc spar, \&c.; coralliform, resembling certain branching corals, ex. arragouite; dendritic or arborescent, a branching form, often made up of small aggregated crystals, ex. native silver, native copper, \&e.; filiform or wire-like, ex. native silver: acicular, in needle-like crystallizations, ex. many varicties of augite, hornblende, epidote, \&c. When a
mineral has a perfectly indefinite shape it is said to be " massive" or "amorphous."

Structure :- In the majority of minerals, a certain kind of structure, or, in other words, the shape as well as the mode of aggregation of the smaller masses of which they are composed, is always observable. Structure in minerals may be either lamellar, laminar or foliated, prismatic, fibrous, granular, or compact. When the mineral, as in most varieties of calc-spar, heary-spar, feldspar, and gypsum, for example, is made up of broad tabular masses producing a more or less stratified appearance, the structure is said to be lamellar. When the tabular masses (whether straight, wavy, or curved,) become extremely thin or leafy, as in mica more especialiy, the structure is said to be laminar, or foliated, or sometimes micaceous. The scaly structure is a variety of this, in which the lamine are of small size. When the component masses are much longer than broad or deep, as m many specimens of tourmaline beryl, calc-spar, \&c., the structure is said to be prismatic or colunimar. When the prismatic concretions become very narrow, the fibrous structure originates. Fibrous minerals may have either: a straight or parallel-fibrous structure, as in many specimens of gypsum, calc-spar, \&c.; a confusedly-fibrous structure, as in many specimens of augite and hornblende; or a radiated-fibrous structure, as in the radiated varieties of iron pyrites, in natrolite, wavellite, \&c.,-the fibres radiating from one or more central points. Minerals made up of small grains or granular masses are said to have a granular structure; ex. granular or saccharoidal limestone, granular gypsum, \&c. Finally, when the component particles are not apparent, the mineral is said to have a compact structure, as in the native malleable metals, obsidian, and most varieties of quartz. Hard and vitreous minerals of a compact structure (ex. obsidian), generally show when broken, a conchoidal fracture, or a series of circular markings resembling the lines of growth on the external surface of a bivalve shell.

Almost all minerals, especially those of a lamellar structure, separate more readily in certain directions than in others. This peculiarity is called cleavage. The fragments resulting from "cleavage" have often a perfectly regular or definite form. Thus the purer specimens of calc-spar, no matter what their external form, break very readily into rhombohedrons, which measure $105^{\circ} 5^{\prime}$ over their obtuse edges. Galena, the common ore of lead, yields rectangular
or cubical cleavage forms; whilst the cubes of fluor-spar break off most readily at the corners or angles, and yir $d$ regular octahedrons, fig. 3.

Hardness.-The bardness of a mineral is its relative power of resisting abrasion, not that of resisting blows : many of the hardest minerals being exceedingly brittle. Practically, the character is of great importance. By its aid gypsum may be distinguished in a moment from calc-spar or limestone, calc-spar from feldspar, and copper pyrites from iron pyrites, not to mention other examples.* The degree of harduess in minerals is conventionally assumed to vary from 1 to 10 ( 1 being the lowest) as in the following scale drawn up by a German mineralogist, Möhs, and now generally adopted:

## Scale of Hardness-Möhs' Scale.

1. Foliated Tarc.
2. Roak Salit, a transpa int cleavable variety.
3. Calcareous Spar, 8 insparent variety.
4. Fluur Spar.
5. Apatite.
6. Feldspar.
7. Rock Crystal.
8. Topaz.
9. Corunduar.
10. The Diamond.

In order to ascertain the hardness of a mineral by means of this scale, we attempt to scratch the substance under examination, by the different specimens belonging to the scale; beginning with the hardest, in order not to expose the specimens to unnecessary wear. Or, we take a fine file, and compare the hardness of the mineral with that of the individual members of the scale, by drawing the file briskly across them. The comparative hardness is estimated by the resistance offered to the file; by the noise produced by the file in passing across the specimens; and by the amount of powder so

[^3]obtained. The degree of hardness of the mineral is then said to be equal to that of the member of the scale with which it agrees the nearest. Thus, if the mineral agrees in hardness with Fluor-spar we say, in its description, II (or hardness) $=4$. If, on the other hand, it be somewhat softer than fluor-spar, but harder than calcareous spar, we say, $H=3.5$. Finally, if, as frequently happens, the hardness of a mineral vary slightly in different specimens, the limits of the hardness are always stated. Thus, if in some specimens, a mineral agree in hardness with calc-spar, and in others with fluorspar, we say, $\mathrm{H}=3$ to 4 ; or, more commonly, $\mathrm{H}=3-4$. If the harduess be very rigorously tested, it will frequently be found to differ slightly on different faces of a crystallized specimen, or on the broad faces and the edges of the lamine of foliated specimens,-but this, so far as regards the simple determination of minerals, is practically of little moment.

As the minerals of which the scale of Mohs consists, may not be in all places obtainable, or always at hand when required, the author of this paper coutrived some years ago another scale, agreeing closely enough for practical purposes with that of Mohs, and exacting for its application only such objects as are always to be met with. The following is the scale in question; its use explains itself:

Chapman's Convenient Scale of Elardness, to correspond with that of Möks.

1. Yields easily to the nail.
2. Does not yield to the nail. Does not scratch a copper coin.
3. Scratches a copper coin, but is also scratched by one, being of about the same degree of hardness.
4. Not scratched by a copper coin. Does not seratch glass (ordinary window-glass).
5. Scratches glass very feebly. Yields easily to the knife.
6. Scratches glass easily. Yields with difficulty to the knife.
7. Does not yield to the knife. Yields with dificulty to the edge of a file.
8, 9, 10. Harder than flint or rock-crystal.
Convenient terms of comparison for 'degrees of hardness above No. 7 cannot be easily obtained; but that is of little consequence, as there are but few minerals of common occurrence which exbibit a higher degres; and these are readily distinguished by other char-
acters. Where, in the above senle, two terms of comparison are employed, both must of course be attended to in the determination of the hardness.

Specifc Gravity.-This is also a character of great value in the determination of minerals. The specific gravity of a body is its weight compared with the weight of an equal bulk of pure water. In order to ascertain the specific gravity of a mineral we weigh the specimen first in air and then in water. The loss of weight in the latter case exactly equals the weight of the displaced water, or, in other words, of a volume of water equal to the volume of the mineral. Now, the specific gravity of pure water, at a temperature of about 620 , being assumed to equal 1 , or unity, it follows that the specific gravity of a mineral is obtained by dividing its weight in air by its loss of weight in water. Thus, if $a=$ the weight in air, and $w=$ the weight in water, $G$, or sp. $g r .=\frac{a}{a-w}$.

Example.-A piece of calcareous spar weighs 66 grs . in air, and 42 grs. when immersed in rain or distilled water. Hence its sp. gr. $=\frac{66}{66-42}=\frac{66}{24}=2.75 . *$
The weight of the mineral may be ascertained most conveniently and with sufficient exactness for general purposes, by a pair of small sicules such as are commonly called "npothecaries" scales." These may be purchased for a couple of dollars, or even less. A small hole must be made in the centre of one of the pans for the passage of a horse-hair or silken fibre, about four inches in length, and furnished at its free end with a "slip-knot" or ruuning noose, to hold the specimen whilst it is being weighed in rater. The strings of the perforated pan may also be somerbat shortened, but the balance must in this case be brought into equilibrium by a few strokes of a file on the under side of the other pan, or by attaching thinner strings to it. If grain weights be used with this balance, the following will be required : 50 grs., $30,20,10,5,3,2,1,05,0.3,0.2$, C.1.
The specific gravity bottle often recommended in mineralogical works, is too heavy to be carried by the scales described above. Bottles of the smallest capacity, weigh, when filled with water, at least 500 grains; and these scales will not carry more than 200, or 250 grains at the most. They are not very sensitive, indeed, when

[^4]loaded with more than 50 or 60 grains in each pan, altbough often. of great delicacy when carrying lesser weights. The use of the sp. gr. bottle requires a chemical balance, costing, at the very lowest, some twenty-five or thirty dollars, besides being of difficult portability; and hence its employment for general purposes is scarcely available.

Relative Malleability.-Some few minerals, as native gold, native silver, sulphide of silver, native copper, \&c., are malleable or ductile, flattening out when struck, instead of breaking. A few other minerals, as talc, serpentine, \&c., are sectile, or admit of being cut by a knife; whilst the majority of minerals are brittle, or incapable of being cut or beaten out without breaking. In testing the relative malleability of a mineral, a sinall fragment should be placed on a little anvil, or block of steel polished on one of its faces,* and struck once or twice by a light haminer. 'To prevent the fragment from flying off when -struck, it may be covered by a strip of thin paper, held down by the forefinger and thumb of the left hand. Thus treated, malleable bodies flatten into discs or spangles, whilst brittle ones break into powder.

Magnetism.-Few minerals attract the magnet in their natural condition, although many do so after exposure to the blowpipe. (See below.) In trying if a mineral be magnetic, we chip off a small fragment, and apply to it a little horse-shoe magnet, such as may be purchased anywhere for a quarter of a dollar; or otherwise we apply the specimen to a properly suspended magnetic needle. In this manner the black granular masses which occur frequently in our gneissoid or Laurentian rocks, and in the boulders derived from them, may easily be recognised as magnetic iron ore. $\dagger$ Many specimens of magnetic iron ore (and also of magnetic pyrites) exbibit "polarity," or attract from a given point, one end of the needle, and repel the other.

Taste.-This is a very characteristic althougb limited property, being exhibited only by a few soluble minerals. In these, the taste may be saline, as in rock salt; or bitter, as in Epsom salt; or metallic, as in sulphate of iron, and so forth.

[^5]Chemical Charaoters.*-These, so far as regards the determination of mineral species, comprise the results produced by the action of acids; and the relative fusibility, \&c., of minerals, as ascertained by the employment of the blow-pipe.
dction of Acids.-The acid-test is resorted to, chiefly 'for the purpose of distinguishing the carbonates from other mineral substances. The majority of carbonates, as carbonate of lime, carbonate of oxide of copper, \&c., when touched with a drop of diluted hydrochloric acid (the "spirit of salt" of the shops), produce a more or less vigorous effervescence. This reaction is still more marked, if a small fragment of the mineral be dropped into a test-tube containing a little of the acid. The effervescence arises from the escape of carbonic acid. Some carbonates, as carbonate of iron, dissolve very slowly, and scarcely produce any effervescence, unless employed in a pulverised state, or unless the acid be gently heated. Sulphate of lime and various other minerals dissolve in hydrochloric acid, but without causing effervescence. Quartz, feldspar, \&c., on the other hand, are quite insoluble. Certain silicates, and more especially those named "zeolites" dissolve partially in hot hydrochloric acid, leaving the undissolved silica in the form of a gelatious mass. Gold and platinum are not attacked by strong nitric acid, which dissolves copper, silver, \&c., very readily. Cupreous acid-solutions have always a green or blue colour. Red copper ore dissolves with effervescence in nitric acid producing a coloured solution; by which characters it may be readily distinguished from the red silver ores.

[^6]The acids used in these experiments may be conveniently leept in. small glass bottles furnished with a long glass stopper, reaching to the botton of the bottle, and with a glass cap to prevent the escape of corrosive fumes. For geological purposes (testing calcareous rocks, \& ,) strong hydrochloric acid diluted with half its bulk of pure water, is principally used. The "specimen basket" may be provided near its upper edge with a little nest, or wicker-work pocket, for the reception of the acid bottle.

Action of the Blow-pips -The blow-pipe in its simplest form is merely a narrow tube of brass or other metal, bent round at one extremity, and terminating at that end in a point with a very fine orifice (a: fig. 21). If we place the pointed end of this instrument just within the flame (and a little above


Fig. 21. the wick) of a lamp or common candle, and theu blow gently down the tube, the flame will be deflected into a horizontal position, and its heating powers will be wonderfully inereased. Many minerals when held in the form of a thin splinter at the point of the blow-pipe flame, melt with the greatest ense; and some are either wholly or partially volatilized. Other minerals, on the contrary, remain unaltered; and thus, by the aid of the blow-pipe, we are often enabled to distinguish from one another, in a moment, various minerals which in external characters may be closely alike.*

The blow-pipe has, strictly, a three-fold application. It may be employed, as just pointed out, to dislinguish minerals from one another; some of these being fusible, whilst others are infusible; some attracting the magnet after exposure to the blow-pipe, whilst others do not exhibit that reaction; some imparting a colour to the flame, others volatilizing, and so forth. Secondly, the blow-pipe may be employed to ascertain the general composition of $a$ mineral, or the presence or absence of some particular substance in it, as copper, lead, iron, cobalt, manganese, sulphur, arsenic, aud the like. Thirdly, the blow-pipe may be used to determine in certain special

[^7]cases the actual amount of a metallic or other ingredient previously ascertained to be present in the substance under examination.*

In the employment of the blow-pipe (in conjunction with external characters) in the simple determination of our Canadian minerals, we are never compelled to resort to more than two experiments: the fusion-trial, and the water-test. The student will find it of advantage, however, to study in addition the reactions of the more common metals and metallic oxides as given in special works on the Blowpipe. To describe these reactions in the present essay would extend the subject much beyond its allotted limits.

The Trial of Fusibility.-In order to ascertain the relative fusibility of a substance, we chip off a small particle (the smaller the better) and expose the point of this to the extremity of the blor-pipe flame -holding the test-fragment in a small pair of tongs or forceps with platinum tips ; $\dagger$ or supporting it, if it be of a metallic aspect or of a certain weight and exbibit at the same time a coloured streak, on a piece of well-burnt pine charcoal. The particle thus exposed to the flame ought not to be larger than a small carraway seed. If it be fusible, its point, in the course of ten or fifteen seconds, will become rounded into a bead or globule. The proper method of blowing can be acquired by half-an-hour's practice. The cheeks are to be filled with air, and this is to be urged gently and continuously down the tube by the compression of the cheek muscles, the operator breathing at the same time (if he require to do so) through his nose. By a little practice this becomes exceedingly easy; and the blowing need never be kept up (at least in experiments of this kind) for more than a quarter of a minute at a time. A thin splinter will exhibit sigus of fusion in ten or twelve seconds, or not at all. The use of the instrument, therefore, is easily acquired, and is in no way injurious to the health.

Thus treated:
(a) 'The test-fragment may "decrepitate" or" fly to pieces. Example, most specimens of galena. In this case, a larger fragment

[^8]Vox. V.
must be heated in a test-tube over a small spirit lamp, and after decrepitation has taken place, one of the resulting fragments may be exposed to the blow-pipe flame as already explained.
(b) The test-fragment may change colour (with or without fusing) and become attractable by a magnet. Example, carbonate of iron. This becomes firstred, then black, and attracts the magnet, but does not fuse. Iron pyrites on the other hand becomes black and magnetic, but fuses also.
(c) The test-fragment may colour the flame. Thus, most copper compounds impart a rich green colour to the flame; compounds containing baryta, and many phosphates and borates, with the mineral molybdenite, colour the flame pale green; sulphur, selenium, lead, and chloride of copper colour the flame blue of different degrees of intensity; compounds containing strontia and lithia impart a crimson colour to the flame; some lime compounds impart to it a paler red colour ; soda compounds, a deep yellow colour; and potash compounds, a violet tint.
(d) The test-fragment may become caustic. Example, carbonate of lime. The carbonic acid is burned off, and caustic lime remains. This restores the blue colour of reddened litmus paper. It also imparts if moistened, a burning sensation to the back of the hand or other sensitive part.
(e) The test-fragment may take fire and burn. Example, native sulphur ; common bituminous coal, \&c.
( $f$ ) The test-fragment may "rolatilize," or dissipate in fumes, either wholly or partially, and ..ith or without an accompanying odor. Thus, grey antimony ore volatilizes with dense white fumes; arsenical pyrites volatilizes in part, with a strong odor of garlic; common iron pyrites yields an odour of brimstene, and so forth.
(g) The test-fragment may fuse, either wholly, or only at the point and edges; and the fusion may take place quietly, or with bubbling, and with or without a previous "intumescence" or expansion of the fragment. Most of the so-called zeolites, for example, (minerals abundant in Trap rocks), swell or curl up on exposure to the blowpipe, and then fuse quietly. Lepidolite fuses with great bubbling, and colours the flame red. Feldspar only melts on the edges, at least, in ordinary cases.
(h) The test-fragment may remain unchanged. Example, Quartz, and various other infusible minerals.

The Water-test.-Many solid minerals contain a considerable amount of water, or the elements of wator, in some unknown physical condition. Gypsum, for example, contains 20.98 per cent. of water. In order to ascertain if a substance yield water, we chip of a fragment (of about the size of a small pea) and heet this in a common test-tube (or better, in a small "bulb-tube" or glass tube closed and


Fra. 22. expanded at one end, as shown in the accompanying figure) over the flame of a little spirit lamp. If water be present, it will rise and condense in the form of a thin fllm, or in small drops, on the cold neck or upper part of the tube. When the moisture begins to appear, the tube must be held in \& more or iess horizontal position, otherwise a fracture may be occasioned by the water flowing down and coming in contact with the hot glass. A small spirit lamp may be made by fitting a piece of glass tubing an inch long (to serve as a wick holder) into the cork of any short, stout bottle. A proper lamp, however, with a glass cap to prevent the evaporation of the spirit when the lamp is not in use, can be purchased for a quarter of a dollar.

This concludes our review of the more common characters possessed or exuibited by mineral bodies. The application of these characters to the actual determination of Canadian minerals, by means of an original Tabuiar Distribution or Arrangement, will be shewn in the next number of the Journal.

## errata.

Figure 7 (on page 7) has been accidentally printed in a reversed position.
Page 5, line 17, for "realgar, or sulphide of arsenic", read "renlgar, a sulphide of arsenic."
Page 15, line 5 from bottom, for "whicl;" read "whilst this."

## RESOLUTION OF ALGEBRAICAL EQOATIONS.


#### Abstract

Proof of the impossibility of representing in finite algebraical functions, in the most general case, the roots of algedraical equations of degrees higher than the fourth; soith methocls for finuling the roots of equations of the 5 th, 6th, 7h, ©e., ilegrees, in those cases wohero the coofficients in the given equations involve a gential or cariable quantily, but where, in consequence of relations subsisting betwcen the coefficients, the roots of the equations happen to admit of being oxactly represented in finite algebraical functions.


BY THE REV. GEORGE PATTONK IOTNG, AF.A., PRORESSOR OP LOGIC AND MEMAPMYSICS IN KNOX'S COLLEGE, TORONTO.

Read before the Canadian Institute, 19th February, 1859.

## Definitions.

Def. 1. In the functions which are to be considered, $a$ variable is involved; and, when quantities are spoken of as rational or irrational, the meaning always is, rational or irrational with respect to the variable. Thus, $c$ being constant, and $p$ variable, the former of the expressions, $c+\sqrt{ } p, \sqrt{ } c+p$, is surd or irrational; and the latter, rational.

Def. 2. Surds may be distinguished as of different orders. The $n^{\text {th }}$ root of a rational expression, $n$ being a prime uumber, distinct from unity, is a surd of the first order. But the $n^{\text {th }}$ root of a rational expression, when $n=n_{3} n_{2} n_{3} \ldots n_{3}$, each of the numbers, $n_{1}, n_{2}$, \&c., being a prime number disinct from unity, is a surd of the $s^{\text {th }}$ order. Again, the $n^{\text {th }}$ root of an expression involving surds of the $s^{\text {th }}$ order, but of no higher order, when $n=n_{1} n_{\mathrm{o}} n_{3} \ldots n_{\mathrm{t}}$, each of the numbers, $n_{1}, n_{9}, \& c$., being a prime number distinct from unity, is a surd of the $(s+t)^{\text {th }}$ order, and so on. Thus, the first of the expressions,

$$
(c+p)^{\frac{1}{13}},\left\{(c+p)^{\frac{1}{12}}+p\right\}^{\frac{2}{3}}, c^{2}+\left[\left\{\left(c+p^{\frac{1}{6}}\right)^{\frac{2}{2}}+p^{\frac{1}{26}}\right\}^{\frac{1}{3}}+\sqrt{ } p\right]^{\frac{1}{33}}
$$

is a surd of the third order; the second, of the fourth order; and the third, of the seventh order. .

Def. 3. Every surd of a certain order is formed by the extraction of some root, (as the $n^{\text {tb }}$ ), of an expression involving ouly surds of the order immediately inferior, $n$ being a prime number, When we
speals of the index of the surd so formed, the fraction $\frac{1}{n}$ is meant. For instance, if we regard $(c+p)^{\frac{1}{15}}$ as generated by the extraction of the fifth root of $(c+p)^{\frac{2}{s}}$, it is a surd of the second order, with the index $\frac{1}{5}$. From another point of viers, it might be described as a surd of the second order, with the index $\frac{2}{3}$.
Def. 4. In the case of a surd of a certain order, we may distinguish the principal surd from its subordinates. Thus, under the principal surd, $(c+\sqrt{ } p)^{\frac{2}{3}}$, is involved the subordinate $\sqrt{ } p$. Under the principal surd,

$$
\left[\left\{c+\left(1+p^{2}\right)^{\frac{5}{7}}\right\}^{\frac{1}{3}}+(2+p)^{\frac{2}{3}}\right]^{\frac{2}{2}},
$$

$c$ being a constant quantity, are involved the subordinates,

$$
\begin{aligned}
& \left(1+p^{3}\right)^{\frac{1}{2}},(2+p)^{\frac{2}{5}},\left\{c+\left(1+p^{2}\right)^{\frac{1}{7}}\right\}^{\frac{1}{2}}, \\
& \left\{c+\left(1+p^{\frac{2}{4}}\right)^{\frac{5}{4}},\left\{c+\left(1+p^{2}\right)^{\frac{7}{7}}\right\}^{\frac{1}{3}} ;\right.
\end{aligned}
$$

the first appearing in the principal surd only in its fifth power; and the second only in its second power. A surd which is a subordinate of the surd $X$, but is not a subordinate of any surd which is itself subordinate to $Y$, may be termed a chief subordinate of $\bar{X}$; while those surds which are subordinates of surds subordinate to $Y$ may be called secondary subordinates of X.

Def. 5. Ar integral function of a rariable is one in which no surd, principal or subordinate, occurs as the denominator, or a term in the denominator, of a fraction. For instance, $c$ being constant, and $p$ variable, the first of the expressions,

$$
\frac{\sqrt{ } p}{\sqrt{ } c},\left(c^{2}+\frac{1}{c+\sqrt{ } p}\right)^{\frac{1}{3}}, c+\frac{1}{\sqrt{ } p},
$$

is an integral function of $p$; but the two last are not.
Cor. A given algebraical function $f(p)$ of a variable $p$ alrays admits of being exhibited as an integral function. For, reduce the function to the form $\frac{N}{D}$; where each of the quantities $N$ and $D$ is the sum of a rational expression, which may be zero, and of a finite series of terms, each of them the product of a rational coefficient
by some power of an integral surd, or by the continued product of several such powers. Take $Y$, one of the surds of highest order present in any of its powers in the function; and arrange the terms in $N$ and $D$ according to the powers of $Y$ not exceeding the $(m-1)^{\text {th }}$, $\frac{1}{m}$ being the index of the surd $Y$. Then

$$
f(p)=\frac{a+a_{1} X+a_{2} Y^{3}+\ldots+a_{m-1} Y^{m-1}}{b+b_{1} Y+b_{2} Y^{2}+\ldots+b_{m-1} Y^{m-1}}
$$

where the coefficients, $b, a, b_{1}, a_{1}: \& c$., may involve powers of any sura in $f(p)$, except $X$. No powers of $Y$ bigher than the $(m-1)^{\text {th }}$ are written; because, for instance, if there were a term $A Y^{m+2}$ in the numerator, A being an expression clear of the said $X$, it might be written, $\left(A Y^{m}\right) Y^{2}$. But $X^{m}$ may be written so as to involve only the subordinate surds of $\Psi$; and hence the term $A Y^{m+2}$ may be considered as contained in the term, $a_{2} Y^{2}$. Assume

$$
\frac{a+a_{1} \bar{Y}+\& c}{b+b_{1} \bar{Y}+\& c .}=c+c_{1} \bar{Y}+\ldots \ldots+c_{m .1} \bar{Y}^{m-2} ;
$$

and, when the expressions, $b+b_{1} Y+\& c ., c+c_{3} Y+\& c$., are multiplied by one another, let the product, arranged according to the powers of Y not exceeding the ( $n-1)^{\text {th }}$, be, $d+d_{3} Y+\& c$.; where $d, d_{1}$, \&c., are clear of the surd Y. Then

$$
a+a_{1} Y+\& c=d+d_{1} Y+\ldots \ldots+d_{m-2} Y^{m-2}
$$

Determine the $m$ unknown quantities, $c, c_{1}, \ldots \ldots, c_{\text {man }}$, by the $m$ simple equations,

$$
d=a, d_{1}=a_{1}, \ldots \ldots, d_{\mathrm{m}-1}=a_{\mathrm{ma}-1} .
$$

Then the function may be written,

$$
f(p)=c+c_{1} Y+c_{2} Y^{\circ}+\& c .
$$

Where the coefficients, $c, c_{1}, \& c$., are clear of the surd Y. Again, let a surd of the highest order present in any of its powers in the coefficients $c, c_{1}, \& c$. , be $V$; and its index $\frac{2}{n}$. By the process already exemplified, we may find, for each of the coefficients, $c_{2} c_{1}$, \&c., an equivalent expression such as

$$
h+h_{1} \nabla+h_{8} \nabla^{2}+\ldots \ldots+h_{n-3} \nabla^{\mathrm{n}-1} ;
$$

where $h_{1}, \Pi_{1}$, Sc., are clear of the surds $V$ and $Y$. Let it be remarked, that, in conseguence of our having commenced with $\bar{Y}$, a surd of the
highest order in $f(p)$, it is impossible, after $\bar{X}$ has once been disposed of, as above, that it can ever return upon our hands, as it might do, if it were a subordinate of any of the principal surds in $c, c_{1}$, \&c. From the same consideration we selected $V, a$ surd of the highest order in $c, c_{1}$, \&c. We may obviously go on in the manner described, till we have exhausted all the surds that need to be disposed of, in order to make the expression for $f(p)$ altogether an integral function of $p$.

Def. 6. Let $f(p)$ be an algebraical function of a variable $p$. Instead of $\mathrm{Y}_{1}$, a surd of the lowest order in $f(\mathrm{p})$, baring the index $\frac{1}{n}$, write $z_{1} \bar{Y}_{1}$ in every place where $\bar{Y}_{1}$ occurs in $f(p)$ in any of its powers, $z_{1}$ being an indefinite $m^{\text {th }}$ root of unity. Do in like manner with all the other surds of the lowest order. Again, $\mathbf{Y}_{2}$ being a surd of the order nest to the lowest in $f(p)$ thus altered, having $\frac{1}{n}$ for its index, and $z_{2}$ being an indefinite $n^{\text {th }}$ root of unity, write $z_{2} Y_{9}$ for $\mathbf{Y}_{2}$ in every place where $Y_{2}$ occurs in the function in any of its powers. Proceed in this way, till modifications of the kind described have been made upon all the surds in the function, including those of the highest order ; and let the function, after having suffered all these changes, become $\phi(p)$. Denote by $\phi_{1}, \phi_{2}, \phi_{3}, \ldots . ., \phi_{\lambda}$, the values of $\phi(p)$, not necessarily all unequal, that result from taking all the possible values of the indefinite numerical quantities, $z_{1}, z_{2}, \& c$., which have been introduced into the function. These expressions, $\phi_{1}, \phi_{2}, \& c$., may be termed the cognate functions of $f(p)$.

As it is important that a clear apprehension be formed of the manner in which we understand the terms $\phi_{1}, \phi_{2}, \mathbb{\&}$.., we subjoin illustrative examples. Let

$$
f(p)=(1+\sqrt{ } p)^{\frac{2}{3}}+(1+\sqrt{ } p)^{\frac{2}{3}} .
$$

Then, $\phi(p)=z_{2}\left(1+z_{1} \sqrt{ } p\right)^{\frac{2}{3}}+z_{2}\left(1+z_{1} \sqrt{ } p\right)^{\frac{2}{3}}$.
Here there are, including $f(p)$, six cognate functions;

$$
\begin{array}{r}
f(p)=\phi_{1}=(1+\sqrt{ } p)^{\frac{2}{3}}+(1+\sqrt{ } p)^{\frac{2}{3}} ; \\
\phi_{3}=z(1+\sqrt{ } p)^{\frac{2}{3}}+z^{2}(1+\sqrt{ } p)^{\frac{2}{3}} ; \\
\phi_{3}=z^{2}(1+\sqrt{ } p)^{\frac{3}{3}}+z(1+\sqrt{ } p)^{\frac{2}{3}} ;
\end{array}
$$

$$
\begin{aligned}
& \phi_{4}^{\prime}=(1-\sqrt{ } p)^{\frac{2}{3}}+(1-\sqrt{ } p)^{\frac{3}{3}} ; \\
& \phi_{5}=z(1-\sqrt{ } p)^{\frac{3}{3}}+z^{3}(1-\sqrt{ } p)^{\frac{2}{3}} ; \\
& \phi_{0}=z^{2}(1-\sqrt{ } p)^{\frac{2}{3}}+z(1-\sqrt{ } p)^{\frac{2}{3}} ;
\end{aligned}, .
$$

where $z$ is a definite third root of unity, distinct from unity. In the three first of these equations, in order that $\phi_{1}, \phi_{2}^{*}$, and $\phi_{3}$, may be definite, we must talke a definite value of $\sqrt{ } p$, and then also a definite value of $(1+\sqrt{ } p)^{\frac{2}{3}}$. As a new surd, $(1-\sqrt{ } p)^{\frac{2}{3}}$, occurs in the three last equations, te must fix upon some definite value of this surd, retaining the definite value already assigned to $v p$; and then $\phi_{1}, \phi_{5}$, and $\phi_{6}$, will be definitely determined. Had we assumed

$$
f(p)=\left(p+\sqrt{p^{2}-1}\right)^{\frac{1}{3}}+\left(p-\sqrt{p^{2}-1}\right)\left(p+\sqrt{p^{2}-1}\right)^{\frac{2}{3}}
$$

we should have got six cognate functions; but three of them merely a repetition of the other three; for the three which result from taking $\sqrt{p^{2}-1}$ with the negative sign are the same as those which result from taking it with the positive sign.
Def. 7. Suppose that we form the cognate functions of $f(p)$, as described in the previous definition, with this difference, that we now proceed as though certain surds, $X_{12} X_{2}$, \&c., (in such a series all the subordinates of any surd mentioned are necessarily included), were rational. In other words, attach no indefiuite numerical multipliers, (as $z_{1}, z_{2}$, , sc., ) to any of the surds, $Y_{1}, Y_{3}$, \&ec.; but consider each of these surds as having a single definite value. The cognate functions of $f(p)$, so obtained, may be termed the cognate functions of $f(p)$, taken without refcrence to the surd character of the surds $Y_{1}, X_{2}$, \&c. For instance, let

$$
f(p)=\left(2+p^{\frac{1}{5}}\right)^{\frac{1}{7}}+\left(1+v^{\prime} p\right)^{\frac{1}{3}}+(1+\sqrt{p})^{\frac{2}{3}}+v_{p} ;
$$

then the cognate functions of $f(p)$, taken without reference to the surd character of the surds, $\Delta^{\prime} p, p^{\frac{1}{5}},\left(2+p^{\frac{1}{5}}\right)^{\frac{1}{4}}$, are,

$$
\begin{aligned}
& \phi_{1}=\left(2+p^{\frac{1}{3}}\right)^{\frac{1}{2}}+(1+\checkmark p)^{\frac{2}{3}}+(1+\checkmark p)^{\frac{2}{3}}+v^{\prime} p ; \\
& \phi_{2}=\left(2+p^{\frac{1}{5}}\right)^{\frac{1}{2}}+z\left(1+\sqrt{ }{ }^{\frac{3}{3}}+z^{2}\left(1+\sqrt{ }(p)^{\frac{2}{3}}+v^{\prime} p ;\right.\right.
\end{aligned}
$$

$$
\phi_{3}=\left(2+p^{\frac{1}{5}}\right)^{\frac{1}{7}}+z^{2}\left(1+v_{p}\right)^{\frac{3}{3}}+z\left(1+v_{p}\right)^{\frac{2}{3}}+v_{p} ;
$$

$z$ being a definite third root of unity.
Def. S. Jet $f(p)$ be an integral function of a variable $p$; and suppose, that, if $Y$ be any surd whatever, principal or subordinate, occuring in the function in its $c^{\text {th }}$ power, and having (see Def. 3) the inder $-\frac{1}{s}, c$ is less than $s$. Also, the form of the function being,

$$
f(p)=A+A_{1} Y_{1}+A_{2} Y_{2}+\ldots \ldots+A_{m} Y_{m}
$$

where the coefficients $A, A_{1}, \& c$., are (see Def. 1) rational, and each of the terms $\mathrm{I}_{1}, \mathrm{X}_{2}$, \&c., is either some powor of an integral surd, or the contimued product of several such powers, suppose that no two of the terms, $Y_{1}, Y_{2}$, \&c., are identical. Tinally, if $Y$ be any surd, principal or subordinate, occurring in the fuaction in its $n^{\text {th }}$ power, and if the form of $V^{n}$ be,

$$
V^{n}=\left(B+B_{1} Y_{1}+B_{2} Y_{2}+\ldots .+B_{c} Y_{c}\right)^{\frac{n}{5}},
$$

where the coefficients, $B, B_{1}$, \&c., are rational, and each of the terms; $Y_{1}, Y_{2}$, ©c., is either some power of an integral surd, or the continued product of several such powers, the inder of the surd $V$ being $\frac{1}{r}$, suppose that no two of the quantities, $Y_{1}, Y_{2}, \& c$., are identical. When these conditions are satisfied, the function $f(p)$ may be described as satisfying the conditions of Def. 8.

Cor. Any given algebraical function $f(p)$ of a variable $p$ admits of being exhibited so as to satisfy the comditions of the Definition. For should a surd $X$, principal or subordinate, with the index $\frac{1}{s}$, uccur in the function in its $c^{\text {th }}$ power, $c$ not being less than $s$, let ws be the greatest multiple of $s$ in $c$; the excess of $c$ above ws, (which may be zero), being $l$. Then we may replace $X^{0}$ by ( $\left.Y^{w \prime \prime}\right) Y^{k}$; and, since the index of the surd $Y$ is $\frac{1}{3}, X^{\text {rs }}$ may be rritten out so as to involve only the subordinate surds of Y . Thus the violation of the first condition of the Definition, insolved in the term $Y^{e}$, is got quit of. For instance,

$$
\mathbf{Y}^{c}=\left(1+\wedge^{\wedge} p\right)^{\frac{8}{5}}=\left(1+\wedge^{\prime} p\right)^{\frac{8}{5}}+\wedge^{\prime} p(1+\wedge p)^{\frac{3}{5}} .
$$

Next, should any such quantities as $Y_{2}, Y_{2}$, \&c., (seo above), be
identical, the terms containing the identical quantities, as described, may be combined into a sing $n$ term. For instance,

$$
\begin{gathered}
f(p)=p+\left\{1+p^{\wedge} p+p^{2}{ }^{\wedge} p\right\}^{\frac{2}{3}}+p\left\{1+p{ }^{\wedge} p+p^{2} \wedge p\right\}^{\frac{2}{3}} \\
=p+(1+p)\left\{1+\left(p+p^{2}\right) \vee p\right\}^{\frac{2}{3}} .
\end{gathered}
$$

Def. 9. An irrational function, $f(p)$, of a variable $p$, is said to be ir a simple form, when no equation such as,

$$
\begin{equation*}
\mathrm{A}+\mathrm{BD}+\mathrm{CV}+\ldots \ldots+\mathrm{DY}+\ldots \ldots+\mathrm{ET}=0, \tag{1}
\end{equation*}
$$

can subsist; where the coefficients, $B, C, \ldots . ., E$, all of them distinct from zero, are (see Def. 1) rational ; A likewise being rational; and each of the terms, $U, V, \ldots \ldots, T$, is either some power of an integral surd occurring in $f(p)$, or the continued product of several such powers; the expression on the left hand side of the equation satisfying the conditions of Def. 8. Let it be observed, that, in this paper, when we speak of a surd occurring in a function, we mean that the surd appears in the function, as a principal or subordinate surd, in some one or more of its powers, but not necessarily in the first power. Thus, the surds which occur in the function,

$$
p+\sqrt{7}+\left(p-\sqrt{p^{2}-1}\right)^{\frac{2}{7}}+\left(p-\sqrt{p^{2}-1}\right)^{\frac{5}{7}},
$$

are, $\sqrt{p^{2}-1}$, and, $\left(p-\sqrt{p^{2}-1}\right)^{\frac{1}{2}}$. The first occurs in its first power; the second, in its second and fifth powers. This being kept in view, we may instance, as violating the condition above mentioned, the function,

$$
\begin{equation*}
f(p)=\left(p+{\sqrt{p^{2}-1}}^{\frac{1}{3}}+\left(p-\sqrt{p^{2}-1}\right)^{\frac{2}{3}} .\right. \tag{2}
\end{equation*}
$$

For the equation, of the form (1), subsists:

$$
\left(p-\sqrt{p^{2}-1}\right)^{\frac{1}{3}}-\left(p+\sqrt{p^{2}-1}\right)^{\frac{2}{3}}\left(p-\sqrt{p^{2}-1}\right)=0
$$

Hence $f(p)$, as exhibited in (2), is not in a simple form.
Cor. 1. The Definition implies, that, should an irrational function of a variable $p$, in a simple form, and equal to zero, present itself in the form,

$$
f(p)=\mathrm{A}+\mathrm{BD}+\mathrm{CV}+\ldots \ldots+\mathrm{ET}
$$

where $\mathrm{U}, \mathrm{V}, \& \mathrm{c}$, are terms of the same kind as in equation (1), and
$A, B, \& c$. , are rational, the coeflicients $A, B$, , \&c., must vanish separately. Also, should $f(p)$ be of the form,

$$
f(p)=A+A_{1} V_{1}+A_{g} V_{z}+\ldots \ldots+A_{c} \nabla_{c},
$$

where each of the terms, $V_{t}, \nabla_{g}$, scc., no two of them identical mith one another, is either some power of an integral surd, or the coutinued product of several such powers, while the expressions $A, A_{1}$, \&e., involve only surds distinct from those whose powers constitute the factors of the terms $\mathrm{V}_{1}, \mathrm{~V}_{2}$, \&c., then [it being understood, as before, that $f(p)$ is in a simple form and equal to zero $]$ the cofficients $A, A_{1}$, \&c., must vanish separately.

Cor. 2. If $f(p)$, a function of a variable $p$, be in a simple form, and if
$A+A_{1} Y_{1}+A_{2} Y_{9}+\ldots+A_{c} Y_{c}=B+B_{1} U_{1}+B_{2} U_{2}+\ldots+B_{m} V^{m D} ;$
where $A_{1}, B_{1}, A_{2}, B_{2}$, \&c., none of them being zero, are rational ; A and $B$ also being rational; and each of the expressions, $Y_{1}, U_{1}, Y_{2}$, $\tilde{U}_{2}, \& e$. , is either some power of an integral surd occuring in $f(p)$, or the continued product of several such powers; the expressions, $A+A_{1} X_{1}+\& c ., B+B_{1} U_{1}+\& c$. , having been arranged so as severally to satisff the conditions of Def. 8; then the surd parts,

$$
\begin{equation*}
X_{1}, Y_{g}, \ldots \ldots \ldots, Y_{c} . \tag{4}
\end{equation*}
$$

are identical, taken in same order, with the surd paris,

$$
\begin{equation*}
\mathrm{U}_{\mathrm{t}}, \mathrm{U}_{\mathrm{g}}, \ldots \ldots \ldots, \mathrm{U}_{\mathrm{n}} ; \tag{5}
\end{equation*}
$$

and, $U_{1}$ being the part identical with $Y_{1}$, the rational coefficient $B_{1}$ is equal to the rational coefficient $A_{1}$. What we mean by identical with, as distinguished from equal to, may be shown by an example. The surd $\sqrt{p^{2}-1}$ is equal to the product of the two surds, $\sqrt{p+1}$, $\sqrt{p-1}$. But the expressions, $\sqrt{p^{2}-1}, \sqrt{p+1} \sqrt{p-1}$, are not identical ; because the only surd which appears in the former is not found in the latter; and the surds which constitute the factors of the latter do not appear in the former. The truth of the Corollary may thus be shown. Should any term in (4), as $Y_{1}$, be identical with a term in (5), as $U_{b}$, let the two terms, $A_{1} Y_{1}$ and $B_{1} U_{b}$, in (3), the latter removed to the left hand side of the equation, be written as one term, $Y_{5}\left(A_{1}-B_{1}\right)$. No other term in (5) can be identical with $Y_{1}$, for then it would also be identical with $U_{2}$; but since the expression, $B+B_{1} U_{3}+, 8 C_{0}$, satisfies the conditions of Def. 8 , no two terms in
(5) are identical. If $U_{2}$ be identical with a term in (4), necessarily distinct from $Y_{1}$, let that term be $Y_{2}$; and let the two terms, $A_{2} Y_{2}$ and $B_{2} U_{y}$, in (3), the latter removed to the left hand side of the equation, be written, $Y_{2}\left(A_{2}-B_{g}\right)$ : Make all other such modifications as are possible. Then equation (3) becomes,

$$
\begin{equation*}
(A-B)+Y_{1}\left(\Lambda_{1}-E_{1}\right)+\ldots \ldots \ldots+A_{2} Y_{n}-B_{n} U_{n}+\& c .=0 ; \tag{6}
\end{equation*}
$$

where all the terms, $Y_{1}, Y_{n}, U_{n}$, Se., are distinct; so that the expression on the left-hand side of equation (6) satisfics the conditions of Def. 8. Therefore, by Cor. 1 , the coefficients, $A_{1}-B_{1}, \ldots \ldots, A_{a}, B_{n}$, Sc., vanish separately. But, since the terms $A_{1}, B_{1}$, dc., are all (by hypothesis) distinct from zero, this shows that there are, in fact, no such terms in (6) as those which we have written, $A_{a} Y_{a},-B_{n} . U_{n}$. Fence the terms in (4) are identical, taken in same order, with those in (5). Also, $Y_{1}$ being identical with $U_{1}$, we have seen that $A_{1}$ is equal to $B_{1}$.

## Prop sition I.

If $f(p)$ be an integral function of a variable $p$, not in a simple form, then an equation,

$$
\mathrm{Y}_{\mathrm{c}}=\mathrm{PY}_{1}{ }^{\lambda_{1}} \mathrm{Y}_{2}{ }^{\lambda_{o}} \ldots \ldots \ldots \mathrm{Y}_{\mathrm{a}}{ }^{\lambda_{\mathrm{a}}} \ldots \ldots \ldots \ldots \ldots \text { (1) }
$$

must subsist; where $Y_{c}, Y_{1}$, \&c., are surds, principal or subordinate, occurring in $f(p)$, of the same order, and with a common index $\frac{1}{s}$; $\lambda_{1}, \lambda_{2}$, \&c., being whole numbers, less than $s$; while $P$ is an expression involving only such surds, occurring in $f(p)$, as are of lower orders than the surds $Y_{c}, Y_{1}$, \&c.

For, since $f(p)$ is not in a simple form, an equation such as (1), Def. 9,

$$
A+B U+C V+\ldots \ldots .+D Y+\ldots \ldots+E T=0, \ldots \ldots \text { (2) }
$$

subsists; all the surds involved in the equation being surds present in $f(p)$. Let

$$
\begin{equation*}
Y_{c}=P Y_{1} \lambda_{1} Y_{I_{2}} \lambda_{\mathrm{o}} \ldots \ldots Y_{a}^{\lambda_{z}} . \tag{3}
\end{equation*}
$$

be an equation such as (1), with this difference, that the indices of the surds $X_{c}, Y_{1}$, \&re., are not assumed to be equal to one another; but $\lambda_{1}$ is less than the denominator of the index of $Y_{1}, \lambda_{2}$ less than the denominator of the index of $\mathrm{Y}_{2}$, and so on. Of the terms, $\mathrm{U}, \mathrm{V}$, ......, T, in (2), let those which involve among their factors surds of the
highest order in equation (2), be, $U, V, \ldots . ., \mathrm{Y}$; and let the sum of A and of those terms, such as ET, in (2), which do not involve surds of the highest order present in (2), be II. Then

$$
\mathrm{FI}+\mathrm{BU}+\mathrm{CV}+\ldots \ldots \ldots \ldots+\mathrm{DY}=0 .
$$

Again, let

$$
U=H_{1} X_{1}, V=H_{2} X_{2}, \ldots \ldots \ldots \ldots, Y=H_{a} X_{n} ;
$$

where $X_{1}$ is the contimed product of those factors of $U$, which are powers of surds of the highest order in (2); $X_{2}$, the continued product of those factors of V , which are powers of surds of the highest order in (2); and so on. Then, putting

$$
\begin{equation*}
\mathrm{H}+\mathrm{BH}_{1} \mathrm{X}_{1}+\mathrm{CH}_{2} \mathrm{X}_{2}+\ldots \ldots+\mathrm{DH}_{2} \mathrm{X}_{\mathrm{a}}=0, . . \tag{4}
\end{equation*}
$$

let us suppose, if possible, that no such equation as (3) can subsist ; and, in connection wich this supposition, let us make the hypothesis, that the terms, $\mathbf{X}_{1}, X_{2}$, \&c., are all distinct from one another. By differentiating (4) with regard to $p$, we get
$\mathrm{H} \frac{d\{\log (\mathrm{H})\}}{d p}+\mathrm{BH}_{1} \mathrm{X}_{1} \frac{d\left\{\log \left(\mathrm{BH}_{1} \mathrm{X}_{1}\right)\right\}}{d p}+\delta c .=0$
Multiply (4) by the coefficient of $\mathrm{BH}_{1} \mathrm{X}_{1}$ in (5), and subtract the product from (5). Then
$h \mathrm{H}+h_{2} \mathrm{CH}_{2} \mathrm{X}_{2}+\ldots \ldots \ldots+h_{2} \mathrm{DH}_{2} \mathrm{X}_{2}=0 ;$
where the values of $h, h_{2}$, \&c., a are

$$
\begin{aligned}
& h=\frac{d\left\{\log \left(\frac{\mathrm{H}}{\mathrm{BH} \mathrm{X}_{1}}\right)\right.}{d p} \\
& h_{2}=\frac{d\left\{\log \left(\frac{\mathrm{CH}_{2} \mathrm{X}_{9}}{\mathrm{BH} \mathrm{X}_{3}}\right)\right.}{d p}
\end{aligned}
$$

and so on. None of the factors of the coefficient of $\mathrm{X}_{2}$ in (6) vanish. For C (by hypothesis) is not zero. The equation, $\mathrm{H}_{3}=0$, is virtually of the form (3), which we have supposed inadmissible. And, if $h_{1}$ were zero, we should have, by integrating the value of $i_{2}$,

$$
\begin{equation*}
\mathrm{BH}_{2} \mathrm{X}_{2}=z \mathrm{CH}_{8} \mathrm{X}_{2}, \tag{7}
\end{equation*}
$$

瓜 being a constant quantity, that is, a quantity independent of $p$. But since $\mathrm{X}_{\mathbf{1}}$ and $\mathrm{X}_{2}$ are not identical, there must be one factor of
$X_{1}$, as $M^{\frac{0}{\lambda}}$, such that $X$, either has no power of the surd $M^{\frac{1}{\lambda}}$ as one of its factors, or a power of $M^{\frac{1}{\lambda}}$ distinct from the $c^{\text {th }}$. Both of these alternatives are included in the assumption that $M^{\frac{r}{\lambda}}$ is a factor of $X_{2}$, $r$ being a whole number, which is not equal to $c$, but may be zero. Hence, if equation (7) subsist, we have

$$
\begin{equation*}
\mathrm{BH}_{1} \mathrm{X}^{\prime} \mathrm{M}^{\frac{c-r}{\lambda}}=k \mathrm{CH}_{2} \mathrm{X}^{\prime \prime}, \tag{8}
\end{equation*}
$$

where $X^{\prime}$ is what $X_{1}$ becomes when the factor $M^{\frac{c}{\lambda}}$ is rejected; and $X^{\prime \prime}$ is what $X_{2}$ becomes on the rejection of the factor $M^{\frac{r}{\lambda}}$. Since $c$ and $r$ are whole numbers, different from one another, and each less than the prime number $\lambda$, we can choose whole numbers, $m$ and $n$, such that $m(c-r)=n \lambda+1$. Then

$$
\begin{array}{r}
\quad\left(\mathrm{BH}_{1} \mathrm{X}^{\prime}\right)^{\mathrm{m}} \mathrm{M}^{\mathrm{n}} \mathrm{M}^{\frac{1}{\lambda}}=\left(k \mathrm{CH}_{2} \mathrm{X}^{\prime \prime}\right)^{m} . \\
\therefore \mathrm{M}^{\frac{1}{\lambda}}=\left(\mathrm{BH}_{1} \mathrm{X}^{\prime}\right)^{-\mathrm{m}} \mathrm{M}^{-\mathrm{n}}\left(k \mathrm{CH}_{2} \mathrm{X}^{\prime \prime}\right)^{\mathrm{m}} \cdot \ldots \ldots . . \tag{9}
\end{array}
$$

But this equation will be readily seen, when the expression on its right hand side is rendered (Cor. Def. 5) integral, and made to satisfy the conditions of Def. 8 , to be of the inadmissible form (3). Consequently $h_{2}$ camnot be zero; and therefore the coefficient of $X_{2}$ in (6) is not zero. In like manner it can be shown that the coefficients of all the other terms, such as $X_{2}$, in (6), are distinct from zero. Again, the coefficients of the terms, $H, X_{3}, X_{a}, \& c$., in (6), when rendered integral functions, and made to satisfy the conditions of Def. 8, involve no surd of so high an order as those whose powers constitute the factors of $\mathrm{X}_{8}, \mathrm{X}_{2}$, \&c. This will be plain if it be considered that the differential coefficient of the logarithm of any power of a surd does not involve, when arranged so as to satisfy the conditions of Def. 8, the surd in question. For instance,

$$
\frac{d\left\{\log (1+\sqrt{ } p)^{\frac{2}{3}}\right\}}{d p}=\frac{\sqrt{ } p-p}{8 p(1-p)}
$$

Where the differential coefficient obtained is clear of the surd
$(1+\sqrt{ } p)^{\frac{1}{3}}$. Since therefore the coeflicients of the terms, $\mathbf{H}, \mathbf{X}_{\mathbf{2}}$, ........., $\mathrm{X}_{\mathrm{a}}$, in (6), when arranged so as to satisfy the conditions of Def. 8, involve only surds of lower orders than those whose powers constitute the factors of $\mathrm{X}_{2}, \mathrm{X}_{2}$, \&c., and since the coefficients of the terms, $\mathbf{X}_{2}, \ldots \ldots . . ., \mathbf{X}_{a}$, in ( $\mathbf{b}$ ), are all distinct from zero, it follows that equation (6) is of the same character as equation (4). But equation (6) contains one term less than equation (4), $X_{1}$, having been eliminated. Therefore, in the same way in which equation (6) was derived from (4), we may deduce from (6) another equation of the same character as ( 6 ;, but with a term fewer. And so on, till ultimately we get

$$
l \mathrm{H}+l \mathrm{X}_{\mathrm{s}}=0 ;
$$

where $l$ and $b$, the former not zero, involve no surds of so high an order as those whose powers constitute the factors of $\mathbf{X}_{2}$. But [compare the reasoning by which equation (9) was deduced from (8)] this is virtually an equation of the inadmissible form (3). Hence, in consistency with the hypothesis that equation (3) cannot subsist, it cannot be supposed that the terms, $\mathrm{X}_{1}, \mathrm{X}_{2}, \ldots \ldots \ldots, \mathrm{X}_{\mathrm{n}}$, in (4), are all distinct from one another. Should $\mathbf{X}_{\mathbf{a}}$ then be identical with $\mathrm{X}_{2}$, let the two terms, $\mathrm{BH}_{1} \mathrm{X}_{1}, \mathrm{DH}_{\mathrm{a}} \mathrm{X}_{\mathrm{a}}$, be combined into the single term, $\mathrm{X}_{2}\left(\mathrm{BH}_{2}+\mathrm{DH}_{2}\right)$. Make all other such modifications on equation (4) as are possible. Ultimately we get
$\mathrm{H}+\mathrm{X}_{1}\left(\mathrm{BH}_{1}+\mathrm{DH}_{2}+\& \mathrm{c}.\right)+\mathrm{X}_{2}\left(\mathrm{CH}_{2}+\& \mathrm{c}.\right)+8 \mathrm{c} .=0 \ldots(10)$ where no two of the terms, $\mathrm{X}_{1}, \mathrm{X}_{2}$, \&c., are identical. But, by what has been proved, this is impossible, except upon condition that the coefficiests of $\mathrm{X}_{1}, \mathrm{X}_{2}$, \&c., vanish separately. Put therefore

$$
\begin{equation*}
\mathrm{BH}_{1}+\mathrm{DH}_{\mathrm{a}}+\& \mathrm{c} .=0 \tag{11}
\end{equation*}
$$

If we compare this equation with (2), we perceive that it is of the same character as (2), with this difference, that there is no surd in equation (11) of so high an order as some of the surds in equation (2). But, in the same manner in which we derived (11) from (2), we may deduce from (11) another equation bearing the same relation to (11) as (11) bears to (2). And so on, till ultimately one of the equations, such as (10), at which we arrive, contains only one term such as $\mathrm{X}_{1}$, with no more than a single term, such as $\mathrm{BH}_{2}$, for its coefficient: from which it follows that B must be zero; whereas all the coefficients, B, C,........., E, in (2), were supposed (see Def. 9) to
be distinct from zero. Hence some equation such as (3) must of necessity admit of being formed. Now suppose that the indices of the surds, $Y_{c}, Y_{1}, \& c$, in (3), are, $\frac{1}{s}, \frac{1}{s_{1}}, \& c$; and that $s_{1}$ is not equal to 3 . By raising both sides of equation (3) to the $s_{1}^{\text {th }}$ power, we may easily [compare the manner in which equation (9) was deduced from (S) $\rfloor$ transform (3) into an equation, not involviag the surd $\Psi_{1}$,

$$
Y_{4}=P_{1} Y_{3}^{\beta_{2}} Y_{3}^{\beta_{3}} \ldots \ldots \ldots Y_{a}^{\beta_{2}},
$$

where $\mathrm{P}_{1}$ is an expression such as $\mathrm{P} ; \beta_{3}$ being a whole number less than the denominator of the inder of $Y_{3} ; \beta_{3}, a$ whole number less than the denominator of the index of $\mathrm{X}_{3}$; and so on. By continuing this process of reduction as far as necessary, we ultimately arrive at an equation such as (1).

Cor. Let each of the terms, $\mathrm{X}_{1}, \mathrm{Y}_{2}, \& c$., be either some power of an integral surd, or the continned product of several such powers; while $A_{1}, A_{2}$, \&c., are algebraical expressions, distinct from zero; and $A$ is an algebraical expression not assumed to be distinct from zero. Then, if

$$
\begin{equation*}
A+A_{1} Y_{1}+A_{z} Y_{2}+\ldots \ldots+A_{c} Y_{c}=0 \tag{12}
\end{equation*}
$$

an equation of the form;

$$
\begin{equation*}
\mathrm{Y}_{1}=\mathrm{P} \dot{Y}_{\mathrm{n}}^{\boldsymbol{m}} \tag{13}
\end{equation*}
$$

must subsist; where P is an expression involving only such surds as are present in the coefficients $A, A_{1}$, \&c., or are subordinates of some of the surds whose powers constitute the factors of $Y_{1}, Y_{2}$, \&c.; and $Y_{n}$ is a term in the series, $Y_{2}, \ldots \ldots \ldots, Y_{c} ; m$ being either unity or zero. For, in the same way in which we eliminated $X_{1}$ from equation (4), we may procced to eliminate successively the terms $X_{2}, \ldots \ldots, Y_{c}$, from (12). The result of the elimination of $X_{2}$ is,

$$
\ldots \ldots+A_{1} Y_{1} \frac{d\left\{\log \left(\frac{A_{1} Y_{1}}{A_{2} Y_{2}}\right)\right\}}{d p}+8 c .=0 \ldots \ldots(14)
$$

Here (see remarks in the Proposition) the coefficient of $X_{1}$, when made to satisfy the conditions of Def. 8, involves no surds except such as are found in $A_{1}$ or $A_{2}$, or are subordinates of the surds whose powers constitute the factors of $Y_{1}$ and $Y_{2}$. Hence the coefficient of $X_{1}$ in (14) is ann expression such as $P$ in (13). Should this coefficient vanish, we have $A_{2} Y_{1}=K_{2} A_{2} Y_{2}, l i b e i n g ~ a ~ c o n-~$
stant ; which equation is of the form (13). Suppose that the coeffcient of $Y_{1}$ in (14) does not vanish; and let equations (14), for the sake of simplicity, be written,

$$
B+B_{1} Y_{1}+B_{3} Y_{3}+\ldots \ldots+B_{c} Y_{c}=0 \ldots \ldots \ldots \ldots(15)
$$

In the same manner in which we proved $B_{1}$ to be an expression such as $P$, it can be shown that all the other terms, $B, B_{3}$, \&c., are expressions such as $P$. Eliminate $Y_{3}$ from equation (15), as $X_{2}$ was eliminated from (12). The result of the elimination is

$$
\ldots \ldots+\mathrm{B}_{1} \mathrm{X}_{1} \frac{d\left\{\log \left(\frac{\mathrm{~B}_{1} \bar{Y}_{1}}{\mathrm{~B}_{3}} \bar{Y}_{3}\right)\right\}}{d p}+\& c .=0 \ldots \ldots(16)
$$

As above, the coefficient of $\Psi_{1}$ here is an expression such as $P$. Also, if that coefficient vauish, we have $\mathrm{B}_{1} \mathrm{Y}_{1}=k \mathrm{~B}_{3} \mathrm{Y}_{3}$, $k$ being a constant quantity. And this equation is of the form (13). Should the coefficient of $Y_{1}$ in (16) not vanish, we may proceed to eliminate another of the terms, $Y_{2}, \mathbf{Y}_{3}, \ldots, \mathbf{Y}_{c}$; and it will be found that the coeflicient of $\bar{Y}$ in the equations that result from such eliminations can never at any stage become zero, unless such an equation as (13) subsist. Suppose then that all the terms, $\mathbf{Y}_{2}, \mathbf{Y}_{3}, \ldots \ldots, \mathbf{Y}_{c}$, can be eliminated in the manner described, without the coefficient of $Y_{1}$ at any stage becoming zero. Then ultimately we get

$$
H A+K A_{1} Y_{1}=0,
$$

where H and K , the latter (and consequently also the former) not zero, are expressions such as $P$. And this is an equation of the form (13), $n$ being taken equal to zero. Hence an equation such as (13) muit necessarily subsist.

## Pborosition II.

In $f(p)$, an integral function of a variable $p$, in a simple form, satisfying the conditions of Def. 8, let $\bar{Y}$ be a surd which is not subordinate to any other in the function, its index being $\frac{1}{s}$. Arrange $f(p)$ as follows:

$$
f(p)=A+A_{c} Y^{c}+A_{n} Y^{n}+A_{m} Y^{m}+\& c
$$

where $A_{0}, A_{n}, \& c$., are expressions distinct from zero, and clear of the surd $\bar{Y} ; A$ being also clear of the $\operatorname{surd} \bar{Y} ;$ and $\bar{Y}^{c}, \mathbf{Y}^{\mathbf{n}}$, \&c., being Vox. $V$.
distinct powers of $Y$, not exceeding the $(s-1)^{\text {th }}$. Let the surd $T$ be a chief (see Def. 4) suburdinate of $\Psi$, but not a subordinate of any other surd in $f(p)$; its index being $\frac{1}{r}$; and, by changing. T, wherever it occurs in $f(p)$ in any of its powers, into $z \mathrm{~T}, z$ being an $r^{\text {th }}$ root of unity, distinct from unity, iet $f(p), A, Y, A_{c}, \& c$. , be transformed into $\mathrm{F}(p), \mathrm{B}, \mathrm{U}, \mathrm{B}_{\mathrm{c}}$, \&c.; so that

$$
F(p)=B+B_{c} U^{c}+B_{n} U^{n}+\& c
$$

Then, if $\mathrm{F}(p)=f(p)$, the terms,

$$
A, A_{0} Y^{c}, A_{n} Y^{n}, d c, \ldots \ldots \ldots \ldots(1)
$$

taken in same order, are equal to the terms,

$$
B, B_{c} U^{c}, B_{n} U^{n}, \& c ., \ldots \ldots \ldots \ldots . . \text { (2) }
$$

each to each; A being equal to $B$.
For, since $\mathrm{F}(p)=f(p)$, we have
$(A-B)+A_{c} X^{c}+A_{n} Y^{n}+\& c .-B_{c} U^{c}-\& c .=0$.
Hence (Cor. Prop. I) one or other of the following equations must subsist:

$$
\left.\begin{array}{l}
A_{c} X^{c}=D(A-B),  \tag{4}\\
A_{0} X^{c}=D A_{m} Y^{m}, \\
A_{c} X^{c}=D B_{m} U^{m} ;
\end{array}\right\} .
$$

where $D$ is an expression involving only such surds as occur in the expressions $A, B, A_{c}, B_{c}, \& c$. or are subordinates of $Y$ or of $U ; X^{m}$ being a term in the series, $\bar{Y}^{c}, Y^{n}$, sc., distinct from $Y^{0}$; and $U^{m}$ representing some term in the series, $\tilde{U}^{c}, U^{n}$, \&c. But, since $T$ is not a subordinate of any surd in $f(p)$ except $Y$, the coefficients $B$, $B_{c}$, \&c., involve no surds different from those which enter into the coefficients $A, A_{.}, \& c$. ; and therefore involve only surds which are found in $f(p)$. Also, since $T$ is not subordinate to any of the subordinates of $\bar{Y}$, it follows that the subordinates of $U$ are the same with those of $\bar{Y}$. Hence $D$ involyes only such surds as occur in $f(p)$. Therefore (Cor. 1, Def. 9,) the first and second of equations (4) are inadmissible; and the third must subsist. Adopting then the equation, $A, Y^{c}=D B_{m} U^{m}$, we say that no other term in (1) than $A_{c} Y$ cas be equal to the product of $B_{m} U^{m}$ by an expression such as
$D$; for, should $A_{n} X^{n}=D_{1} B_{m} \sigma^{m}$, where $D_{1}$ involves only such surds, exclusive of $Y$, as occur in $f(p)$, this would give us,

$$
\begin{equation*}
D_{1} A_{c} Y^{c}=D A_{n} Y^{n} \tag{5}
\end{equation*}
$$

Now $D$ cannot be zero, else $A_{c} Y^{c}$ would vanish; but $A_{c}$ is (by hypothesis) not zero; and the equation, $\bar{Y}=0$, is impossible by Def. 9. Hence, since $D$ is not zero, equation (5) is (Cor. $1, D e f$. 9) inadmissible. Therefore we cannot have $A_{n} X^{n}=D_{1} B_{m} U^{20}$. Consequently, as we established the third of equations (4), we can establish similar equations for all the terms in (1), after the first:

$$
\begin{aligned}
& A_{n} Y^{n}=D_{1} B_{r} U^{r} \\
& A_{m} Y^{m}=D_{2} B_{a} U^{n}
\end{aligned}
$$

and so on; the terms, $A_{c} \Psi^{c}, A_{n} Y^{n}, A_{m} Y^{m}$, \&c., being all different from one another, on the one hand; and the terms, $B_{m} \mathbb{D}^{m}, B_{r} \mathbb{D}^{r}$, $B_{a} U^{2}$, \&.c., being all different from one another, on the other hand. Hence equation (3) becomes,

$$
(A-B) Y^{c}\left(1-D^{-1}\right) A_{c}+Y^{n}\left(1-D_{1}^{-1}\right) A_{n}+\& c .=0
$$

where (Cor. 1, Def. 9) the coefficients, $A-B, A_{c}\left(1-D^{-1}\right)$, \&e., vanish separately. That is, the terms in the series (1), taken in some order, are equal to those in the series (2), each to each; A being equal to $B$.

## Proposition III.

Let $f(p)$ be an algebraical function of a rariable $p$, in a simple form; and let $Y_{c}, Y_{1}$, \&ec., certain surds, with the common index $\frac{1}{s}$, no one of them a subordinate of any of the others, be such that all their subordinates occur in $f(p)$. Suppose that

$$
\mathrm{Y}_{\mathrm{c}}=\mathrm{PY}_{1}^{\lambda_{1}} \mathrm{Y}_{2}^{\lambda_{2}} \ldots \ldots \mathrm{Y}_{\mathrm{a}}^{\lambda_{2}},
$$

or, as the equation may be written,

$$
\begin{equation*}
Y=P, \tag{1}
\end{equation*}
$$

Where $Y$ is merely a symbol used (for the sake of simplicity) to denote the continued product of the expressions $\overline{Y_{c}}, \overline{Y_{1}}, \overline{\lambda_{1}}, \overline{Y_{2}}$
$\mathrm{Y}_{\mathrm{a}}^{-\lambda_{\mathrm{a}}}$; and P is an expression involving only such surds as occur in $f(p)$; the whole numbers $\lambda_{1}, \lambda_{2}, \& c$. , being less than $s$. Take $\phi$, the gencral expression which includes (see def. vi.) all the cognate functions of $f(p)$ : one of its particular forms, distinct from $f(p)$, being $\phi_{1}$. In pas $\Delta \mathrm{l}_{\mathrm{y}}$ from $f(p)$ to $\phi$, let P and Y become respectively $Q$ and $y$; and, in passing from $\phi$ to $\phi_{2}$, let $Q$ and $y$ become respectively $P_{1}$ and $y_{1}$. Then the equation,

$$
\begin{equation*}
y_{1}=I_{c} \mathrm{P}_{1}, \tag{2}
\end{equation*}
$$

subsists; $k$ being an $s^{\text {h }}$ root of unity.
Explanatory remark.-When we speak of Y becoming $y$ in passing from $f(p)$ to $\phi$, we do not assume that the expression $\mathbf{Y}$ is present in $f(p)$; but we mean that all the surds which occur in $f(p)$, and are also found in Y , must, in order that Y may be transformed into $y$, undergo the same changes which they require to suffer in order that $f(p)$ may become $\phi$.

We proceed with the proof of the Proposition. In the first place, should $P$ be zero, $Y_{c}=0$. Let $Y_{c}$ be of the form,

$$
\mathrm{Y}_{\mathrm{c}}=\left(a+a_{1} \mathrm{~S}_{1}+a_{2} \mathrm{~S}_{2}+\ldots \ldots+a_{\mathrm{n}} \mathrm{~S}_{\mathrm{n}}\right)^{\frac{1}{3}} ;
$$

where the coefficients, $a, a_{1}, \& c$., are rational; and each of the terms $S_{1}, S_{2}$, \&c., is either some power of an integral surd, or the continued product of sereral such powers; the expression, $a+a_{1} \mathrm{~S}_{1}+$ \&c.., satisfying the conditions of Def. 8. Then, since $Y_{c}=0$, we have

$$
a+a_{1} \mathrm{~S}_{\mathrm{I}}+a_{2} \mathrm{~S}_{2}+8 \mathrm{c} .=0 .
$$

Now all the surds present in this equation, being subordinates of $\mathrm{Y}_{c}$, are (by hypothesis) surds occurring in $f(p)$, a function in a simple form. Therefore (Cor. 1, Def. 9) the coefficients, $a, a_{1}$, \&c., vanish separately. But, if $Y_{c}^{\prime}$ be what $\mathrm{Y}_{\mathrm{c}}$ becomes in passing from $f(p)$ to $\phi$, and $Y_{c}^{4}$ be what $Y_{c}^{\prime}$ becomes in passing from $\phi$ to $\phi_{1}$, we have

$$
Y_{c}^{\prime \prime}=\left(a+a_{1} S_{1}^{\prime}+\ldots \ldots \mp a_{\mathrm{n}} \mathrm{~S}_{\mathrm{n}}^{\prime}\right)^{\frac{1}{2}},
$$

where $\mathrm{S}_{1}^{\prime}$, \&c., are what $\mathrm{S}_{1}$, \&c., become in passing from $f(p)$ to $\phi_{1}$. Therefore $\mathrm{Y}_{\mathrm{c}}^{*}=0$. But, in the same way in which, from the fact that $Y_{c}$ is zero, we have deduced the conclusion that $Y_{c}^{\text {u }}$ is zero, we may, from the fact that $P$ is zero, deduce the conclusion that $P_{1}$ is
zero. Also, since $X_{c}^{\prime \prime}$ is a factor of $y_{1}, y_{1}$ must be zero. Therefore $y_{1}=k P_{1}$.

In the next place, should $\mathbf{P}$ not be zero, the expressions $y^{3}, \mathrm{Y}^{\mathbf{3}}, y_{i^{z}}$, developed by the ordinary process of involution, rendered integral, and made to satisfy the conditions of Def. 8, are of the forms,

$$
\left.\begin{array}{rl}
y^{2} & =A+A_{1} v+A_{2} t+\& c .,  \tag{3}\\
\mathrm{Y}^{s} & =A+A_{1} \mathrm{~V}+\mathrm{A}_{2} \mathrm{~T}+\& \mathrm{C} ., \\
y_{1}^{s} & =\mathrm{A}+\mathrm{A}_{1} \mathrm{~V}_{1}+A_{2} \mathrm{~T}_{1}+\& \mathrm{Sc} . ;
\end{array}\right\}
$$

where $\mathrm{A}, \mathrm{A}_{1}$, \&c., are rational ; and each of the expressions, $v, t, \& c$. , is either some power of an integral surd, or the continued product of several such powers ; the expressions $\backslash, T, \& c$. , being what $v, t$, \&c., become in passing from $\phi$ to $f(p)$; and $\mathrm{V}_{1}, \mathrm{~T}_{1}$, \&c., what $v, t$, \&e., become in passing from $\phi$ to $\phi_{1}$. In like mamer, the expressions, $Q^{3}, P^{5}, P_{1}^{3}$, satisfying the conditions of Def. 8 , are of the forms,

$$
\left.\begin{array}{l}
Q^{s}=B+B_{1} n+B_{2} l+\mathbb{C} .,  \tag{4}\\
P^{s}=B+B_{1} M+B_{2} L+\& c ., \\
P_{1}^{s}=B+B_{1} M_{1}+B_{2} X_{1}+\& c . ;
\end{array}\right\}
$$

where $B, B_{1}$, \&c., are rational; and each of the expressions, $m, l$, \&c., is either some power of an integral surd, or the continued product of several such powers; M, L, \&c., being what $n, l, \& \& c$. , become in passing from $\phi$ to $f(p)$; and $\mathrm{M}_{1}, \mathrm{~L}_{1}$, \&c., what $m, l, \& c$. , become in passing from $\phi$ to $\phi_{1}$. From (1), (3), and (4), we hare,

$$
\begin{equation*}
\mathrm{A} \div \mathrm{A}_{\mathrm{I}} \mathrm{~V}+\mathrm{A}_{2} \mathrm{~T}+\& \mathrm{cc}=\mathrm{B}+\mathrm{B}_{1} \mathrm{M}+\mathrm{B}_{2} \mathrm{~L}+\mathbb{}+\ldots \ldots \tag{5}
\end{equation*}
$$

But the surds occurring in the expression on the left hand side of this equation, being necessarily subordinates of some of the surds, $\mathrm{Y}_{\mathrm{c}}, \mathrm{Y}_{1}, \ldots \ldots, \mathrm{X}_{\mathrm{n}}$, are all present in $f(p)$. Those occurring in the expression on the right hand side of the equation are likewise all present in $f(p)$. Therefore, since equation (5) subsists, the surd parts, V, T, \&c., are (Cor. 2, Def. 9) severally identical, taken in some order, with the surd parts, L, M, \&c. ; which also (Cor. 1, Def. 9) implies, that, if $V$ be the surd part identical with $M, A_{1}$ is equal to $B_{1}$; and so on. But since $V$ is identical with $M$, and $A_{1}$ equal to $B_{1}$, and $T$ is identical with (we may suppose) $L$, and $\mathrm{A}_{2}$ equal to $\mathrm{B}_{2}$, and so on, the equation,

$$
\begin{equation*}
A+A_{1} V_{1}+A_{2} T_{1}+\& c=B \div B_{1} M_{1}+B_{2} L_{1}+\& c, \tag{6}
\end{equation*}
$$

must subsist; because, in passing from $f(p)$ to $\phi_{1}, \mathrm{~V}$ becomes $\nabla_{1}$, and $M$ becomes $M_{1}$, so that $V_{1}$ and $M_{1}$ are identical, and hence $A_{1} V_{1}$ is equal to $B_{1} M_{1}$ : and so of the other terms. Therefore from (6), (3), and (4),

$$
\stackrel{s}{y_{1}}=\mathrm{P}_{1}^{s} \therefore y_{1}=k \mathrm{P}_{1} .
$$

## Proposifion YV.

If $f(p)$, an integral function of a variable $p$, be in a simple form, each of its cognate functions is in a simple form.
It is self-evident that the Proposition is true for all functions which involve only surds of the first order. Suppose the law to have been found to hold for all functions which do not involve surds above the ( $n-1)^{\text {ih }}$ order: it may then be proved true for a function, $f(p)$, involving surds of the $n^{\text {th }}$, but of no higher, order.
For take $\phi$, the general expression which includes all the cognate functions of $f(p)$; one of its particular forms, distinct from $\vec{f}(p)$, being $\phi_{1}$; and suppose, if possible, that $\phi_{1}$ is not in a simple form. Then an equation such as (1). Prop. I,

$$
\mathrm{Y}_{\mathrm{c}}=\mathrm{PY}_{1}^{\lambda_{1}} \mathrm{Y}_{2 . \ldots}^{\lambda_{2} \ldots \ldots . \mathrm{X}_{\mathrm{a}}^{\lambda_{2}},}
$$

must (Prop. I.) subsist; all the surds involved in the equation being. surds which occur in $\phi_{1}$. We may write this equation in the form,

$$
\begin{equation*}
y_{1}=P, \tag{1}
\end{equation*}
$$

where $y_{1}$ denotes the continued product of the expressions $\mathbf{Y}$, $\mathrm{Y}_{1}^{-\lambda_{1}}$, \&c. Let $y_{1}$ in $\phi_{1}$ correspond to $y$ in $\phi$, and to Y in $f(p)$ : that is to say, $y$ is what Y becomes in passing from $f(p)$ to $\phi$, and $y_{1}$ is what $y$ becomes in passing from $\phi$ to $\phi_{1}$. In like manner, let P in $\phi_{1}$ correspond to Q in $\phi$, and to R in $f(p)$. Let the the surds $Y_{c}, Y_{1}, \& c$. , in $\phi_{1}$, correspond to $Y_{c}^{\prime}, Y_{1}^{\prime}, \& c$. , in $f(p)$; and since the surds $Y_{c}^{\prime}, Y_{1}^{\prime}$, scc., have the common index $\frac{1}{s}$, let their forms be,

$$
Y_{c}^{\prime}=V_{1}^{\frac{1}{3}}, Y_{1}^{\prime}=V_{I}^{\frac{1}{3}}, \ldots \ldots, Y_{a}^{\prime}=V_{a}^{\frac{1}{3}}
$$

Take $\mathrm{F}(p)$, a function involving all the surds which occur in the expressions $R, V_{c}, V_{1}, \ldots \ldots, V_{a}$; and let the particular cognate function of $\mathrm{F}(p)$, obtained by making the same changes in the surds involved in $\mathrm{F}(p)$ as require to be made in order to pass from $f(p)$ to
$\phi_{1}$, be $\mathrm{F}_{1}(p)$. Then the surds occurring in $\mathrm{F}(p)$ are all of lower orders than $X_{c}^{\prime}, Y_{1}^{\prime}$, \&c.; hence they are all of lower orders than the $n^{\text {lh }}$. But we are at present reasoning on the hypothesis that the law sought to be established in the Proposition holds for all functions which do not involve surds above the $(n-1)^{\text {ih }}$ order. Therefore, since $\mathrm{F}(p)$, containing only surds which occur in $f(p)$, is in a simple form, it follows that the function $\mathrm{F}_{1}(p)$ also is in a simple form. Now, if we refer to equation (1), we find that the surds involved in $P$, and all the subordinates of those surds whose powers constitute the factors of $y_{1}$, occur in the function $\mathrm{F}_{1}(p)$. Therefore, by Prop. III, we can deduce from (1) the equation,

$$
\mathrm{Y}=k \mathbf{R},
$$

$k$ being a constant quantity. But this is an equation such as (1), Prop.I.; all the surds appearing in the equation being surds which occur in $f(p)$. Such an equation, however, is directly at variance with the hypothesis that $f(p)$ is in a simple form. And hence $\phi_{1}$ cannot but be in a simple form. Consequently the law sought to be established in the Proposition holds good for all functions which do not involve surds above the $n^{\text {th }}$ order.

Since, therefore, the law holds good for functions involving only surds of the first order, and since, on the hypothesis of its holding good for functions involving only surds of orders not higher than the $(n-1)^{\text {in, }}$, we have shown that it must hold good for functions involving only surds of orders not higher than the $n^{\text {til }}$, it holds good universally.

## Proposition $V$.

If $f(p)$, an integral function of a variable $p$, in a simple form, be a root of the algebraical equation, $\mathrm{F}(x)=0$, in which the coefficients of the powers of $x$ are rational functions of $p$, then $\phi_{1}$, any one of the cognate functions of $f(p)$, is a root of the same equation.

For take $\phi$, the indefinite expression which includes all the cognate functions of $f(p)$; and let $\mathrm{F}(\phi), \mathrm{F}\{f(p)\}, F\left(\phi_{1}\right)$, developed by the ordinary process of involution, and arranged so as to satisfy the conditions of Def. 8, be,

$$
\begin{aligned}
\mathrm{F}(\phi) & =\mathrm{A}+\mathrm{A}_{1} \mathrm{Y}_{\mathrm{r}}+\mathrm{A}_{2} \mathrm{Y}_{2}+\ldots \ldots+\mathrm{A}_{\mathrm{c}} \mathrm{Y}_{\mathrm{c}}, \\
\mathrm{~F}\{f(p)\} & =\mathrm{A}+\mathrm{A}_{1} \mathrm{~V}_{1}+\mathrm{A}_{2} \mathrm{~V}_{2}+\ldots \ldots+.+\mathrm{A}_{\mathrm{c}} \mathrm{~V}_{\mathrm{c}}, \\
\mathrm{~F}\left(\phi_{1}\right) & =\mathrm{A}+\mathrm{A}_{1} \mathrm{U}_{1}+\mathrm{A}_{2} \mathrm{U}_{2}+\ldots \ldots+\mathrm{A}_{\mathrm{c}} \mathrm{U}^{\mathrm{c}} ;
\end{aligned}
$$

where $A, A_{1}$, \&c., are rational ; and each of the terms, $\mathrm{Y}_{1}, \mathrm{Y}_{2}, \& c$. , is either some power of an integral surd, or the continued product of several such powers; $V_{1}, V_{2}$, \&c., being what $Y_{1}, Y_{2}$, \&c., become in passing from $\phi$ to $f(p)$; and $\mathrm{U}_{1}, \mathrm{U}_{2}, \& \in$., what $\mathrm{Y}_{1}$, $\mathbf{Y}_{2}$, \&c., become in passing from $\phi$ to $\phi_{1}$. The expression for F $\{f(p)\}$ can only involve such surds as are present in some of their powers in $f(p)$. And $f(p)$, by hypothesis, is in a simple form. Therefore $\mathrm{F}\{f(p)\}$, as exhibited above, is in a simple form. It also satisfies the conditions of Def. S. But, since $f(p)$ is a root of the equation, $\mathrm{F}(x)=0, \mathrm{~F}\{f(p)\}$ is equal to zero. Therefore, in the expression for $\mathrm{F}\{f(p)\}$, the coefficients $\mathrm{A}, \mathrm{A}_{1}, \& c$., must (Cor. 1, Def. 9) vanish separately. Hence, $\mathrm{F}\left(\phi_{1}\right)=0$; and consequently $\phi_{1}$ is a root of the equation, $F(x)=0$.

Cor.-Let $f(p)$ be an integral function of $p$, in a simple form; and let certain surds in $f(p)$, viz. : $y_{1}, y_{2}$, \&ec., (in which series of terms, as was noticed in Def. 7, all the subordinates of any surd mentioned are necessarily included), have definite values attached to them ; and let the cognate functions of $f(p)$, taken according to the manner described in Def. 7, without reference to the surd character of $y_{1}, y_{2}, \& c$., be

$$
\phi_{1}, \phi_{2}, \phi_{3}, \ldots \ldots, \phi_{1} .
$$

Also let $\mathrm{F}(x)=0$, be an ecquation in which the coefficients of the powers of $x$ are rational as far as all surds except $y_{1}, y_{2}$, \&c., are concerned; that is, the coefficients contain no surds besides $y_{1}, y_{2}$, $\& c$. Then, if $f(p)$ be a root of the equation, $\mathrm{F}(x)=0$, any one of the terms, $\phi_{1}, \phi_{2}, \ldots \ldots, \phi_{n}$, (the definite values of $y_{1}, y_{2}$, \&c., being adhered to), is a root of the same equation. For, in this case, in the same manner in which the expressions for $\mathrm{F}\{f(p)\}$ and F ( $\phi_{1}$ ) in the Proposition were formed, we get.

$$
\begin{gathered}
\mathrm{F}\{f(p)\}=\mathrm{A}+\mathrm{A}_{1} \mathrm{~V}_{1}+\mathrm{A}_{2} \mathrm{~V}_{2}+\& \mathrm{c} . \\
\mathrm{F}\left(\phi_{2}\right)=\mathrm{A}+\mathrm{A}_{1} \mathrm{U}_{1}+\mathrm{A}_{2} \mathrm{U}_{2}+\& c .
\end{gathered}
$$

where $\mathrm{A}, \mathrm{A}_{1}$, \&c., are rational as far as all surds except $y_{1}, y_{2}, \mathcal{\&}$., are concerned; and each of the expressions, $\nabla_{1}, \nabla_{2}$, \&c., is cither some power of a surd in $f(p)$, not contained in the series, $y_{1}, y_{2}$, \&c., or the continued product of several such powers; $\mathrm{U}_{1}, \mathrm{U}_{2}$, \&c., being what $V_{1}, V_{2}$, \&c., become in passing from $f(p)$ to $\phi$ : the expressions for $\mathrm{F}\{f(p)\}$ and $\mathrm{F}\left(\phi_{1}\right)$ satisfying the conditions of

Def. 8. In passing from $f(p)$ to $\phi$, no change is made on $\mathbf{A}, \mathrm{A}_{1}$, \&c., because the surds entering into these expressions are the same in $f(p)$ as in $\phi_{1}$. But since $\mathrm{F}\left\{f^{\prime}(p)\right\}$ is equal to zero, the coefficients $\mathrm{A}, \mathrm{A}_{1}$, \&c., must (Cor. 1, Def. 9) vanish separately. Therefore $\mathrm{F}\left(\phi_{1}\right)=0$; and $\phi_{1}$ is a root of the equation, $\mathrm{F}(x)=0$.
(To be continued.)

## ON THE GEOLOGY OF BELLEVILLE AND THE SURROUNDING DISTRICT.

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For the informatio. of distant readers, it may be observed that the town of Belleville, in Canada West, is situated at the mouth of the River Moira near the western or closed extremity of the Bay of Quinté. The Trent, a broad and important river, enters this bay at the upper end, about ten miles west of the Moira, or rather constitutes by its exextension, the bay itself. The Salmon River or Shannon on the other hand flows into the same waters some eight or nine miles to the east of Belleville. The observations contained in the present paper apply almost exclusively to the tract of country thus bounded respectively on the east and west by the Salmon River and the Trent; and extending from a short distance along the shore of Prince Edward's County (south of the Bay of Quinté,) to some ten or twelve miles inland or to the north of the Bay. A few remarks, however, furnished by a hasty visit to the back township of Elzevir, are also incorporated in this paper-leaving the geological details of the iron district of Belmont, Madoc, \&e., for a future communication.

Throughout this tract of country (as indeed almost everywhere within the Province, ) the eye is at once struck by evidences of ancient denuding forces of an action both prior and subsequent to the deposition of the Drift; and, as a corollary to this action, of the much lower level of the land, relative to the water, at a comparatively recent period
of geological history. The shores of the Bay of Quinté in very many places, and the high banks or terraces which run, with more or less of interruption, a short distance inland along the course of the abovenamed rivers, and which were evidently washed at one time by waters either salt or fresh, afford abundant proofs of this earlier physical condition of the district. The foundation rock, so to say, of this locality, is the well-known Trenton Limestone. This, although exposed in numerous places, is generally capped by a considerable thickness of Drift clay, sand, and gravel, with boulders of limestone and various gneissoid rocks, such as lie more or less immediately along the northern confines of the tract in question. Around Belleville itself, more particularly, the upper portion of the Drift con'ists of very finely stratified sand and light-coloured plastic clay, overlying gravel and other coarser materials with boulders of various kinds. The accompanying sketchsection across the River Moira will serve to convey an idea of the extensive denudation to which the Drift has been here subjected. In

this section, $a$ is the upper thin-bedded portion of the Trenton limestone, and $b$ and $c$ are the Drift beds. In consequence of this denudation the beds $c$ are only of partial occurence, but I remarked them in several places at considerable distances apart. They are especially well shewn on the side of a hill or steep bank through which a street is cut, in the vicinity of the Court-house, Belleville.

A deposit of calcareous tufa derived in great part from minute freshwater shells belonging to cyclas, planorbis, and other genera, cunstitutes a comparatively recent formation extending over a considerable area on: the top of the drift bank or high ground on the west side of the river. It marks the site of an old swamp, now drained off. The same modern calcareous formation occurs still more extensively along the foot of the so-called " mountain" at Trenton, (where it was kindly pointed out to me by the Rev. Mr. Bleasdell of that village, ) and undoubtedly in many other places; although the above were the only spots in which it came under my personal observation. It may be stated, as a general
rule, that a deposit of calcareous tufa or shell-marl will be fornd under the vegetable mould aroand the margins of almost all our smaller lakes, these having occupied at one period a larger extent of surface than that included within their present areas. As a mineral manure, this calcarcous deposit ought to possess considerable value, but I did not find any particular importance attached to it either at Belleville or Trenton, and it seemed to be very little used.

The limestone surface immediately under the Drift appears throughout the entire district to have been polished and grooved by glacial action; but it is only here and there, and more especially where a recent removal of the Drift deposit has taken-place, that the results of this action are now visible. At the period of my visit to Belleville (June 1859) a beautiful example of polished and striated rock had just been laid bare in some adrain excavations on the south side of Bridge Street, west of the Moira; and I observed the same effects on the exposed faces of limestone at "The Plains," between the Moira and the Shannon; and, still more distinctly, opposite the Shannonville Station, on the north side of the Grand Trunk Railway. At the latter locality, large slabs of rock exhibited a polished surface equal to that of plate-glass, with fine striæ running across it in a gencral N.W. and S.E. direction. By the effect of weaihering, however, these results of ancient glacial action become more or less rapidly obliterated.

The Trenton limestone of the district in question is lithologically divisable into two distinct sets of beds. Of these, the upper are thinbedded (passing indeed into shales,) and are exceedingiy fossiliferous; whilst the lower are thick-bedded and almost destitute of fossils. These lower beds are well displayed at the quarries on Ox Point, and at other places eastward along the Bay of Quiné. They form a most excellent building stone. The upper or thin bedded limestones crop out extensively along the banks of the Trent, Moira, and Salmonrivers, and are exposed in most of the road cuttings of the district, and along the line of the Grand Trunk Railway. They literally teem with the more common fossils. of the Trenton group. A list of those actually collected, is given below. These beds lie apparently in horizontal layers, but at Ox Point and other places some low anticlinals or undulations are visible, and a careful examination of the district shows a slight but general dip towards the south-west. A road cutting near the west bank of the Moira exposes a bed of calcareous clay about a foot in thickness interstratified with the shaly limestones of the upper
part of the Trenton series. This bed, pointed out to me, by Campbell Wallbridge, Esq., of Belleville, contains numerous impressions of strophomena alternata and other Trenton forms, and is thus (as shown moreover by its position amongst the shaly limestones) a true member of the group. It is the first example of this kind of association that I have met with in the Trenton series, but a similar interstratification of clay and limestone beds has been seen, I believe, in other places.

About Belleville, the most prolific fossil localities are the river banks, and an old cutting for a mill-race on the east bank of the river, a little north of the Railway Station. The banks of the river (the Salmon) at Shannonville, and a cutting on the Railway at that place, about half a mile west of the Station, are also good localities; whilst around Trenton village many excavations and smail quarries will be found exceedingly rich in fossils. On the steep side also of the high land at Rednersville in Prince Edward's County, some good specimens may be procured. This is the highest position occupied by the Trenton Limestone immediately around Belleville. I was led to understand by persons residing in Belleville, that the rock was not limestone; but it consists simply of the same shaly limestone as that seen on the banks of the Moira, as shewn in the following section (lettered as in figure 1), from which moreover, an idea may be gleaned of the vast amount of denudation which must have taken place in that neighbourhood, both before and after the deposition of the Drift.


At some of the above mentioned localities, and especially in the old mill-race near the Railway Station at Bellevile, I found Columnaria alveolata, until recently considered typical of the Black River Limestone, associated with ordinary Trenton fossils; and near the Episcopalian Church at Shannonville, I found the same coral with Stromatocerizm rugosum, also accompanying Trenton species. These types therefore, (as already shewn by Sir William Logan and others,
from the examination of other localitics) although highly characteristic of the Black River Limestone, are not absolutely peculiar to that formation (or sub-formation) as was formerly thought to be the case. The subjoined Table gives an enumeration of the fossils collected, during my visit, at Belleville and in the surrounding district.

## Plants:

Indistinct fucoids, and at Rednersville an undescribed form presenting a thick primary stem-mass, with numerous dichotomous branchings.

## Corals and Crinoids:

Stromatocerium rugosum (Shannonville). Stenopora fibrosa (the Chetetes lycoperdon of Hall, \&c.): Variety 1, ramosa, the branched form, most abundant on the surfaces of the flat layers along the banks of the Moira; Variety 2, concava, the flattened or salver-shaped form concave above, abundant everywhere, more especially at the Railway cutting near Shannonville; Variety 3, globosa, the true "puff-ball" form, rather uncommon. Columnaria alveolata (Belleville, Shannonrille). Petraia (Streptelasma) cornicula. Glyptocrinus ramulosus? (stem fragments only.

Bryozoons:
Ptilodictya (Stictopora) acuta, common at most of the fossiliferous localities, with a few other (indeterminable) forms.

## Brachiopods:

Lingula quadrata. Rhynconella increbescens (not common). Strophomena alternata and S. filitexta (both exceedingly abundant). Leptcena sericea. Orthis testudinaria (also very abundant); O. tricenaria (beautifully preserved) ; O. pectinella; 0 . lynx (only observed by me at Trenton).

## Conchifers:

Of this Class I did not meet with any determinable forms.
Gasteropods:
Pleurotomaria lenticularis, Murchisonia gracilis; M. bellicincta; M. sub-fusiformis (?) Subulites elongata.

> Pteropods (?):

Conularia Trentonensis (not very common).

## Cephalopods:

Orthoceras (Endoceras.) proteiforme ; O. bilineatum; O. (undetermined species) ; O. tenuiflum, or a related species with beaded siphuncle.

## Trilobites:

Asaphus platycephalus ( $=$ Isotelus gigas, exceedingly common in a fragmentary state); A. megistos (rare). Ceraurus pleurexanthemus (very abundant). Calymene Blumenbachii (tolerably common, and well preserved). Trinucleus concentricus (two fragments only, found at Shannonville).

In the above list it will be seen that I have placed the coral commonly known as Chietetes lycoperdon, under the genus Stenopora, of Lonsdale. D'Orbigny's Monticulipora, to which genus the branched form has been referred, appears to agree in all essential respects with Stenopora, and to be thus an unnecessary addition to the list of Favositian genera. Calamopora of Goldfuss (including amongst others, Favosites, Stenopora and Cheetetes) can scarcely be employed without risk of misconception, and is therefore now almost universally abandoned. Favosites differs essentially from Stenopora and Chatetec in possessing perforated cell-walls. The imperforate favositoidean corals fall into two series: the one exhibiting fissiparous and the other gemmiparous reproduction. The former show in the fracture the interior of the tubes, and constitute the genus Chatetes. The latter show the outside of the cell-walls (reproduction taking place by the lateral interpolation of new tubes) and they form the genus Stenojora. To this genus, if the above definition as given by McCoy and others, hold good, our so called Cheetetes undoubtedly belong. This admitted, our common forms, the Calamopora fibrosa of Goldfuss, may be legitimately placed under McCoy's Stenopora fibrosa, and conveniently sub-divided into three varicties : the branching form (variety ramosa) ; the flat, cup-shaped or salver-shaped hemispherical form (variety concava) ; and the globular or true "puff-ball" form (variety globosa or lycoperdon). It often happens that whilst one varicty is exceedingly abundant at a special locality, the other two are altogether absent. McCoy ("British Palæozoic Fossils," p. 24,) makes but two varieties: lycopodites and regularis, the latter including the branched and polymorphous forms; but those given above, so far as regards Canadian examples, will be found I think of more convenient adoption.

The "petites saillics coniques," the distinguishing character of d'Orbigny's Monticulipora, appear to be a necessary consequence of the mode of reproduction exhibited by Stenopora.*

On proceeding north of Belleville, the thin-bedded limestone gives place to the lower or thick beds, and these in turn merge into a silicious limestone, the probable equivalent of the Black River subdivision ; although the country is so thickly covered by Drift, that sections are only observable here and there. At the village of Hungeiford, in the township of that name, the grey silicious limestone is seen to overlie a series of thin flat layers of a reddish calcareous sandstone with pale green spots distributed irregularly through its mass, This rock is apparently an abnormal form of the Poisdam sandstone, or, perhaps a bed of passage between the Potsdam sandstone and the Calcareous sand rock, as it contains from 40 to 50 per cent. of dolomitic carbonate of lime. I found no traces of organic remains in it. I should be inclined to look upon it as the calcareous sand rock, were it not for its agreement, in certain of its physical characters, with the Potsdam sandstone as recognised elsewhere. From this part of the country however, westward to Georgian Bay, the beds between the base of the Trenton and the outcrop of the Laurentian series, are more or less ob-scure-thinning out altogether, or merging, as it were, one into the other. About three miles north of Hungerford village (or perhaps less, the intermediate space being greatly obscured by Drift) the Laurentian or Gneissoid rocks begin to crop out, dipping at a high angle to the north-east, or in a contrary direction to the slight dip of the Silurian strata. Close to the southern limit of the Laurentian outcrop a fine band of crystalline limestone occurs, interstratified with dark grey and reddish beds of gneiss. This may be conveniently examined at the village of Bridgewater in Elzevir Township on the property of Billa Flint, Esq., to whose enterprising spirit, that part of the country owes so much. The specimens of crystalline limestone obtained at this spot, form a marble of excellent quality. I have to regret that from want of time I was unable to examine the run of the band, and its quality at other points. A few fragments of galena and some impure steatite were shown to me, as having been met with near at haud.

[^9]The accompanying sketch-section across the little River Scoot, was taken near Mr. Flint's village. It may serve to convey an idea of the relative positions of the various beds which occur there. In this section, $A$ represents the Gneissoid strata, with the band of crystalline limestone $b ; C$ denotes the Lower Silurian beds (limestone above, and, by inference, the retaish sand-rock below, as seen farther south); and $D$, denotes the Drift deposit.


Iu concluding this brief notice of the more salient geological features of Belleville and its vicinity, I am anxious to express my obligations to the family of Lewiş Wallbridge, Esq., M.P. P., for mnch information respecting points of interest to be risited, and for the presentation of many fossils obtained in the neighbourhood.

## REVIEWS.

Galbraith and Haughton's Scientific Manuals. Experimental and Natural Science Series: Manual of the Animal Kingdom; Protozoa. By Professor J. Reay Greene.
This small volume has a double title; we have chosen that which presents it as. the commencement of an extended series of manuals, because we thus give most information to our readers. Those who obtain it alone from curiosity respecting its particular subject, would make use of the other.

It is a beautifully printed, carefully illustrated, and neatly got up volume, containing owly 88 pages, with a Bibliography of the subject, questions for examination, and an index; to this are prefixed 30 pages of general introduction. Of course there is, within such limits, no attempt to characterise or enumerate genera and species. The object aimed at, is a general view of structure, arrangement and distriba-
tion. In the case of the Protozoa, this may be all that most people need or could profit $\omega \mathrm{y}$, but as we rise in the animal kingdom, such a manual would appear very meagre. We see aunounced as forthcoming, another Zoological volume from the pen of the author of that which lies before us, and a Botanical one from that of Professor Harvey of Dublin. We are curious to see whether the present manual is to be a model as to size, and if so, how the learned authors will aequit themselves in such trammels; but our present business is with Professor Greene's manual of the sub-kingdom, Protozoa. It must in the first place be conceded that in this department of zoology, accessible and trust-worthy information is greatly needed, and would be gladly received by a large class of readers. Professor Greene appears to be well acquainted with what has been written on the subject, and has laudably exerted himself, to give a clear, though much compressed account of what is known, in relation to these elementary forms of animal life. We are not satisfied with bis mode of treating their classification. He regards them as being as yet too little understood for the limits of classes and orders to be well determined, and therefore only gives under the titles of the several groups which have been proposed, the subdivisions recommerded by the authors who have chiefly studied them, accompanied by such structural and physiological particulars respecting at least some typical species as seem to be established by sufficient authority. For practical usefulness we should have preferred some attempt, even if confessedly only provisional, to harmonise that we seem to have learned from various investigators into a consistent system whose parts are brought into proper relation to each other and to the whole; and we confess we have no such ideas as to the necessary foundations and limits of what are entitled to be called classes and orders, as would deter us from applying these terms to the greater and secondary divisions, which, though liable to modification by increasing knowledge, seem now to express the relations of the creatures, which we agree with the author in regarding as a distinct, well established subkingdom of the animal kingdom. He indeed complains of the characters of Prorozos being almost wholly negative, but this may perhaps appear to be almost unavoidable in a lowest division of any large collection of objects. In the vegetable kingdom, the method we prefer, separates as a sub-kingdom, those plants which are without Vascular tissue-the mode of diposing that tissue when present,
giving characters to the remaining sub-kingdoms,-and so in the animal kingdom, the development and disposition of the nervous system characterise the four higher divisions, whilst Protozoa are animals consisting of an animated jelly, (Sarcodium) with little differentiation of parts and no perceptible nervous system. We are aware indeed that there may possibly not be one of the sub-kingdoms, certainly none excepting the highest, in which there are not instances, where no nervous system can be demonstrated; but in all such instances there is a manifest conformity to a type of structure, which directs our judgment as to the position of the object, whilst in Protozoa, wherever we have a tolerable acquaintance with the life history of the creature we recognise not only the absence of the characteristics of another sub-kingdom, but the presence of certain features properly belonging to that we are considering. If we have materials in our hands which really justify us in establishing a sub-kingdom of Protozoa, they can hardly fail to suggest some opinion as to the mode of sub-dividing it. If groups of creatures have been examined and intelligibly described, the question of their relation to other known groups, and the comparative importance of their distinctive marks will arise, and should be solved to the best of our ability.

It seems to us, that the possession of a mouth, and consequently of an alimentary sac, with a somewhat definite figure, and an outer covering, differing in some degree from the mass of the body, characterise Infusoria (in the now received limited sense,) as the highest class of Protozoa. From them, Rhizopoda are distinguished, by having no difference, so far as is known, or only a slight difference in certain parts, in their external covering from the mass of their bodies, and by their power $c^{f}$ protruding portions of their substance, in the form denominated Pseudopodia. Possibly the uaked Rhizopoda, the Arcellina, the Foraminifera, and the Polycystina may be so many good orders in this class. Thalassicollida may be nearer akin to Sponges : of Gregarinida, nothing can as yet be satisfactorily decided, until a full history of at least some species, removes the doubts which at present are unavoidable respecting their nature.

Sponges for which we may adopt the name of Amorphosoa, form a thirà distinct class. Since no protrusion of pseudopodia is attributed to Thalassicollida and in some of them at least, cellæform bodies, seeming to contain germs are surrounded by spicules, not unlike the peculiar ovarian spicules of some sponges; we may perhaps regard
these organisms as one order of Amorphozoa. Without waiting for the expression of Dr. Bowerbank's views, we would not decide on the subdivision of the class, but would temporarily employ one of the existing arrangements to afford us that aid of system without which we can hardly proceed a step usefully in the study of nature. Whatever may be its defects, that founded on the nature of the skeleton, may serve the purpose, and at least exhibits remarkable annlogies with the arangement of Rhizopoda; 'Thalassicollida representing naked Rhizopoda, the horny sponges having a certain correspondence with Arcellina-those with Silicious spicula being the analogues of Polycystina, and those with Calcareous spicula of Foraminifera. Did our space permit, we should endeavour to ascertain the proper arrangement of Infusoria also, being well convinced, that all other information is in a great degree thrown away, if not connected with an intelligible system, and that methods which are necessarily only provisioual and in which we may be sensibie of great defects, are yet far preferable to any attempts at communicating auatomical, physiological, or descriptive matter independently of systems, which never carry the student beyond insulated facts, and barren, because unconnected observations.

Although Professor Greene may not exactly see these things in the same light that we do, we are by no means insensible to the merits of his book. The Introduction is excellent and useful, and its extent can hardly deter the idlest reader. His accounts of the low, and generally minute organisms of which he treats are highly interesting, and cannot fail to diffuse information, and lead to the increase of knowledge, by eulisting a host of new inquirers. The proprietors of the series have done their part well, and their first number holds out a favourable promise for those which are to follow; if What is more important is not sacrificed to over-anxiety after compression.
W. H.

The Old Glaciers of Switzerland and North Wales. By A. C. Ramsay, F.R.S. and G.S. London: Printed by Spottiswood and Co. 1859.

Amongst the various records of a by-gone condition of things presented by Nature's archives to the interpretation of the geologist, few can compete in interest, and perhaps in difficulty of solution,
with those belonging to the great Drift or Glacial epoch : that period in the history of the earth's mutations, which immediately preceded, and gradually passaged into, the present or historic age. Broadly spread across the entire nortbern hemisphere, southward to a mean latitude (on this continent) of about $40^{\circ} \mathrm{N}$., and again extending many degrees northwards from the southern pole, lie vast beds of clay, and sand, and gravel, mixed up with and overlaid by heaps of travelled stones or boulders; stones that have been brought by natural agencies, often across intervening seas and valleys, and over mountain ridges, miles and miles away from their original localities. Where hard and compact rocks lie underneath this boulder formation, or rise up amengst it, their surfaces are almost always found to be rounded, or smoothed and polished, and marked likewise in long and straight lines with narrow grooves and scratches. If these peculiarities be not always observable on exposed rock surfaces, their absence is chiefly due to the disintegrating action of the atmosphere, as they necessarily become obliterated, sooner or later, by the effects of weathering.

In Canada the drift formation is largely developed; and in many places the underlying limestone and other rocks exhibit the polished surfaces and the long lines of grooving $t$ alluded to. But it is in mountainous countries that the phenomena of the drift opoch are portrayed to us in their grandest outlines. There, in many localities within the limits of latitude already pointed out, the hill-sides present their rounded contours, smoothed, polished, and striated; the hill-tops bear their loads of boulder stones, balanced one upon another, or perched, perhaps, on isolated points of rock; and the valleys show their excavated hollows and lake-basins, their barriers of heaped up boulders, their high and furrowed walls, with other memorials of abrading agencies belonging, it may be there, to an older time, but which are still in action amongst the frozen solitudes of the remote north, and in the higher valleys of the Alps and other mountain chains. In these vaileys the broad ice-rivers still slowly push their way amidst the surrounding rocks, wearing and abrading them, and piling up at lower levels their stony burdens in the form of huge moraines.* This bowever leaves the tale balf told. To complete our view of the phenomena under which the drift accumulations took place, we must

[^10]picture in addition the likeness of a northern sea, girt with protruding glaciers from which drift off the floating icebergs with their freight of rock and stone. This rocky freight, as the icebergs melt in lower latitudes, is necessarily scattered orer the hill-tops, the plains, and valleys of the deep sea-bottom. We must picture also, over broad areas, vast sinkings and upheavals of the land, going grandly on through the slow lapse of centuries; the stranding and piling up of icebergs on shoals and - .sts; the southern migration and subsequent retrogression of northern organisms; and the gradual dawn of softening climatic influences, coupled with the shrinking back of glacial forces to within their present limits.

It was thus by observations conducted in northern lands and seas, and in Alpine ralleys, that the true nature of our drift phenomena became gradually elucidated. Professor Ramsay, in the attractive essay nor before us, has placed in striking parallel-not from the descriptions of others, but from personal observation and researchsome of the glacier valleys of Switzerland, with the romantic Pass of Llanberis and other valleys of North Wales. Commencing with the Swiss valleys, he lays before us a rapid but graphic sketch of the glaciers of the Aar: shewing how incontestible is the fact, that, vast as are these glaciers now, they shrink into insignificance when compared with their extension in former times. The same fact is observable, indeed, with regard to almost all the glaciers of these Alpine valleys. On this subject, after mentioning some modern instances of the advance and retreat of glaciers, Professor Ramsay remarks :"But all such historical variations in the magnitude of glaciers are trifling compared with their wonderful extension in pre-historic periods. There is perhaps scarcely a allley in the High Alps in which the traveller, whose eye is educated in glacial phenomena, will not discern symptoms of the former presence of glaciers where none now exist; aud in numerons instances, far from requiring to be searched for, these indications force themselves on the attention by signs as strong as if the glacier had disappeared but a short time before the growth of the living vegetation. So startling, indeed, are these revelations that for a time the observer scarcely dares to admit to himself the justness of his conclusions, when he finds in striations, moraines, roches moutonnées, and blocs perchés, unequivocal marks of the former extension of an existing glacier, a long day's march
beyond its present termination; and further, that its actual surface of to-day is a thonsand feet and more beneath its ancient level."

With regard to the Aar valley, the glaciers of which are taken as type-forms in relation to this inquiry, our author observes in addition: "Below the lower glacier of the Aar, the stream winds through one of those gravelly flats, so frequent in old glacier valleys, and at its lower end, where this plain narrows towards the Grimsel, a boss of granitic gneiss, well moutonnée, nearly bars the valleys across which the path leads. It is partly covered by striations, well marked on the slope that looks up the valley, telling the observer not only of the previous extension of the glacier thus far, but also that the ice which filled the plain pressed strongly on the higher side of the boss, and was forced upwards till it fairly slid over the rock, the lower part of the ice being quite unchecked by the opposing bar. I mention this especially, because similar phenomena were often pointed out by Buckland in describing the old glaciers of North Wales. On either hand, all the way from the glacier to this point, the wrountain sides show the same mammillated contours that mark the rock above the ice, and a little further down the valley, the sigus of glacial action become even unusually obtrusive. A large bill rises from the valley on the right, up which the road winds to the Hospice of the Grimsel. On the left is the narrow gorge of the Aar, and on the other side of the hill the sullen lake of the Grimsel half encircles it far above the level of the river. At its outflow the lake is partly dammed up by a little moraine-like dêbris; but it requires no soundings to tell that the rounded rocks close by, passing under the rubbish, form the chief retaining barrier of the water. On both banks, except when weather-worn, the rocks are ice-worn, and the lake is nearly looped into two by roches moutonnées that project from either bank toward the centre, like Llyn Idwal above Nant Francon, and the lakes of Llanberis, if these were undivided by the alluvial strip below Dolbadarn Tower. At its farther end a long, narrow, high, rounded barrier of solid rock (over which the glacier formerly poured) crosses the valley, damming up the lake in that direction; and here so great has been the pressure, that I found proof of the ice having been forced into a narrow transverse fissure, which it polished and striated quite out of the direction of its general flow. The lake is a complete rock basin similar to some of the tarns of North

Wales, and such as I only know in regions where glaciers once have been.
"On the hill that rises behind the Hospice, the glacial striations on the rocks gradually circle round to the further end of the lake, following the sweep of the valley; and it soon becomes apparent that this hill itself, is but a gigantic roche moutonnée, mammilated and striated all over, on which erratic blocks were left by the decrease of the glacier of the Aar after a period in which it rose so high, that it not only filled tue hollow of the lake, and pressed upward over the ridgy barrier at its further end, but actually overflowed the entire hill. If from its polished side you survey the opposite ridge of the Aar valley, the vast size of the old glacier becomes still more strongly impressed upon the mind. A great wall of rock rises sharply above the river course, and on its side the striations which cover it, have been deflected upwards, at a low angle, the effect of the intense jamming to which the thick ice was subjected in its downward course, when obstructed by the great roche moutonnée that rises in the middle of the valley between the lake and the mountains on the opposite side of the Aar. Above this wall, the mountain is moutonnée almost to the very summit, where at length the serrated peaks of the highest ridge rise sharply above the ice-worn surfaces. The valley has been filled with ice almost to the very brim."

After thas discussing in their past and present bearings, the glacial phenomena of these Swiss valleys, our author turns to the valleys of Cænarvonshire that lie around the majestic Snowden, and traces out, in these, step by step, the former existence of immense glaciers, whose dimensions rivalled in grandeur the great ice-rivers of the ancient Alps. He then considers the question of identity of time with respect to the extinct glacial phenomena of Wales and the ancient extension of the Alpine glaciers. "But these things being true, [the former existence, \&c., of glaciers in the valleys around Snowden], what relation in time is there between the old glaciers of Switzerland and those of Wales? The elements from which to attempt a solution of this question are few. First, it may be said that the signs of glaciation in the former extension of still existing Swiss glaciers, are not only identical in all respects with those of the extinct glaciers of Wales, but also that in many an Alpine valley all the ice marks remain, even when no diminished glacier still holds its place amid its uppermost recesses. These in all respects may be compared to the ancient glaciers of the neighbouring Jura, the Vosges, or of Wales. Again, when we consider that
the great old glaciers of the Oberland apparently opened out on the broad drift-covered territory that extends northward to the Jura, there is another point of resemblance. So similar in general structure and in all its adjuncts is this Drift with that of the north of Europe, that I see no reason whatever to doubt their identity. To add weight to this opinion, I may quote the high authority of Mr. Smith of Jordan Hill, who informed me, that he recollects seeing in the museum at Berne, a neglected collection of Swiss shells, aretic in their grouping, and subfossil, like those of our Newer Pliocene beds; and in the museum at Geneva a similar collection, among which was $\mathrm{h}_{\mathrm{l}} / \mathrm{ya}$ Udivalensis. Further, it is well known that in the superficial deposits associated with these, the bones of the great hairy elephant ( $\mathbf{E}$. primigenius), and other mammalian remains, occur by the Lake of Geneva, at Winterthur, and in other places; and though no one that I know of, has yet attempted to prove the ploughing of drift out of the mouths of Swiss valleys by the older and larger glaciers, yet in every other respect the conditions àre so identical, that I am prepared to expect that this also will be proved, and I cannot resist the conclusion that, when glaciers filled the valleys of Wales, it was at that very time (the Newer Pliocene epoch) that the glaciers of Switzerland attained their great original extension.

Further, in spite of the modern fact that far south of the equator, the cold is greater than in equivalent northern latitudes, it is difficult not to speculate on the probable existence of a climate perhaps colder for the whole world, during what is often called the glacial period; a period when not only the Alps, but all Scandinavia, were full of great rivers of ice descending to the sea; when the White Mountains of North America also had their glaciers, (as I was informed in 1857 , in conversation with Agassiz,) and when the great glaciers of the Himalayah, as described by Dr. Joseph Hooker, descended 5000 feet below their present levels, the older moraines being in one instance only 9000 feet above the sea, whereas the present end of the glacier lies tit a height of 14,000 feet.

Another point often occurs to my mind, -what relation have these extinct glaciers to the human period? This is a subject on which we still are in the dark, but considering that in Newer Pliocene bonecaves, flint knives have been found, -there is reason to believe, coeval with elephants, rhinoceroses, and other Mammalia, partly extinct; and that in France, at Abbeville and Amiens, well formed flint
batchets of an old type occur in fresh-water and marine strata of socalled Opper Tertiary date; and also, that a human skull was dug out of the so-called Pliocene volcanic ashes of Auvergne, it is possible, and perhaps even probable, that, long after the Drift was raised above the sea, the eyes of men may have looked upon the glaciers of Wales, when in their latter days, the ice had shrunk far up into the highest recesses of the mountains."

In calling the attention of our readers to this ably-written essay, we must not forget to mention, that its author has added much to the interest of his descriptions by a number of charming little vignette illustrations, and by a valuable map of the country around Snowden. In the latter, the directions of the rock-striæ, with the moraines and other vestiges of the ancient glaciers of North Wales, are indicated from Professor Ramsay's personal explorations.
E. J. C.

## The Family Herald. John Lovell, Montreal.

A periodical of a somewhat novel and attractive character has been added to our Canadian Literature under this name. Issued in the form of a Newspaper sheet, and embracing scientific, literary and general news ; it partakes in some respects of the united characteristics of Chamber's Journal, and the London Athenceum. A tale or novel runs through a series of chapters, in successive numbers; well selected stories, poems, and literary gleanings occupy other of its columns; and a good space is devoted in each number to Reviews. Its news columns are severally set apart to "Canada and the Lower Provinces," "EEagland," "Scotland," "Ireland," and The " United States." The only thing omitted is party politics;-and, without any disparagement to the uses and value of our free press, as one of the elements of our social hife and freedom, we believe that to many fair and young readers, The Framily Frerald will be none the less welcome for the omission.

The Editor of this new Canadian periodical is Mr. G. P. Ure, a gentleman long connected with the press; and the character of the earlier numbers of his new serial, show that he is making the best use of his opportunities and experience. When the great influence of the daily press is considered, not on politics only, but in forming the tastes, and training the minds of so large a portion of the community,
to whom, such constitutes their most frequent reading, it cannot but be acknowledged that a periodical thus combining somewhat of the attractiveness and accessible brevity of the newspaper, with the careful literary characteristics of the scientific periodical, or monthly magazine, supplies one of the great wants of our industrious and advancing community. If the Family Ferald, is conducted with the same good taste and judiciousness in the selection of its materials, which have been manifested in its carlier numbers, it cannot fail to meet with the success it merits.
D. W.

On the Classification and Geographical Distributior: of the Mammalia -being the lecture on Sir Robert Reade's foundation, delivered before the University of Cambridge, in the Senate-house, May 10, 1859,-to which is added an appendix, on the Gorilla, and on the extinction and transmutation of species. By Richard Owen, F.R.S. \&c. \&c. London : John W. Parker and Son, West Strand. 1859.

Everything which proceeds from the pen of Professor Owen will be received with lively interest and with respectful attention. The present lecture is a pretty full exposition of his views respecting the Classification of Mammalia according to the cerebral system, which he has derived from a long series of dissections, and a diligent use of such opportunities as have perhaps never before been possessed by a comparative anatomist. That his system is an important improvement on that of Cuvier, can hardly be denied.

Every unprejudiced observer of nature will feel favourably disposed towards a method which brings Edentata, [Bruta] Cheiroptera, In. sectivora and Rodertia into close relationship. We cannot help looking a little suspiciously at the multiplication of orders, and are disposed to anticipate still further improvements. In the meantime, all honour is due to Professor Owen's labours; and his present explanation of the characters of the various tribes is to be highly valued. In connection with this lecture, the author has published two papers which form an appropriate and valuable supplement to it. Appendix $A$ is a note on the extinction of species, " being the conclusion of the Fullerian course of lectures on Physiology for 1859." Appendix B is on the Orang, Chimpansee, and Gorilla, in reference to the transmutation of species, and runs to a considerable extent. Our present limits forbid extracts, or analysis, but in naming the subjects we excite the curiosity of our
readers to know the opinions of the chief of comparative anatomists, and they can readily satisfy it, by having recourse to the work itself, which deserves the careful study of all who are interested in these pursuits.
W. H.

Archaia; Or. Studies of the Cosmogony and Natural History of the Hebrew Scriptures. By J. W. Dawson, LL.D., F.G.S., Principal of McGill College, \&c. Montreal : B. Dawson and Son. 1860.

Dr. Dawson's recent contribution to the literature of the Bible-for in such light must his Archaia be chiefly regarded,-has reached us just as we are going to press; and, hence, we are unable to devote to it the space to which it is so justly entitled, both by the distinguished name of its author and by its own intrinsic merits. As the issue, moreover, of a Canadian publisher, it has further claims upon us : ill met, we are afraid, by this too scanty and too hurried notice. Archaia is essentially composed of a series of critical essays or discourses founded on the opening chapter of Genesis; but the author enlarges his field of inquiry by various references to other passages of the sacred writings; more especially in the bearings of these on the Mosaic record of creation, and in their connexion with the study of nature generally. For the successful composition of a work of this kind, the author possesses many peculiar qualifications : a ready command of language, a clear and logical method of discussion, an intimate acquaintance with the discoveries and researches of modern science, and, above all, an evidently sincere and strong faitin in the divine truths of Revelation. With these qualifications, although preceded on the same path by many active investigators, he has prosduced, as might be expeccted, an interesting and popularly written book; and one, moreover, containing various subordinate points of a novel character. The very nature of the subject renders, however, a work of this description more or less unsatisfactory to many readers. Perhaps to the scientific investigator, and to those whose thoughts have long dwelt on these questions, more especially; but if the work before us, leave the mind in some respects unsatisfied, we cannot but admit that in its expansive treatment of the subject it has gone far beyond its predecessors. The author, in his preface, hopes that his work may aid in some degree in redeeming the subject from the narrow views which are unhappily too prevalent: and of this, if those
who entertain surh views can be led to read the book, we have but little douht. In this respect alone, therefore, apart from its general value, we may fairly welcome it, and urge its perusal upon those who still blindly look upon geology, and upon natural science generally, as antagonistic in some undefined manner to the spirit of Revelation.

It is difficult to extract a passage, sufficiently independent of the context for quotation, without occupying a larger space than our limits permit; but the following from one of the introductory chapters, in which the author claims for the Holy Scriptures a deeper insight into ontural phenomena than many have hitherto foreseen, may serve as an ample of the style and general expression of the work:
"The law of type or pattern in nature is distiuctly indicated in the Bible. This is a principle only recently understood by naturalists, but it has more or less dimly dawned on the misds of many great thinkers in all ages. Nor is this wonderful, for the idea of type is scarcely ever absent from our own conceptions of any work that we may undertake. In any such work ve anticipate recurring daily toil, like the returning cycles of nature. Wo look for progress, like that of the growth of the universe. We study adaptation both of the several parts to subordinate uses and of the whole to some general design. But we also keep in view some pattern, style, or:order, according to which the whole is arranged, and the mutual relations of the parts are \{adjusted. The architect must adhere to some order of arohitecture, and to some style within that order. The potter, the calico-printer, and the silversmith, must equally study uniformity of patterr in their several manufactures. 'The Almighty Worker has exhibited the same idea in his works. In the animal kingdom, for instance, we have four leading types of structure. Taking any one of these-the vertebrate, for example-we have: a uniform general plan, embracing the vertebral column constructed of the same elements; the members, whether the arm of man, the limb of the guadruped, or the wing of the bat or the bird, or the swimming paddle of the whate, built of the same bones. In iike manner all the parts of the vertebral column itself in the same animal, whether in the skull, the neck or the trunk, are composed of the same elementary structures. These types are farther found to be sketched out,-first in their more general, and then in their special features-in proceeding from the lower species of the same type to the higher, in proceeding from the earlier to the later stages of embryonic development, and in proceeding from the more ancient to the more recent creatures that have succeeded each other in geological time. Man, the highest of the vertebrates, is thus the archetype, representing and including all the lower and earlier members of the vertebrate type. The above are but trite and familiar examples of a doctrine which may furnish and has furnished the material of volumes. There can be no question that the Hebrew Bible is the oldest book in which shis principle is stated. In the first chapter of Genesis we have specific type in the creation of plauts and animals after their kinds or species, aud in the formation of man in the image atd likeness of the

Oreator ; and, as we shall find in the sequel, there are some curious ideas of higher and more gencral types in the grouping of the creatures referred to. The samo idea is indicated in the closing chapters of Job, where the three higher classes of the vertebrates are represented ly a number of examples, and tho typical likeness of one of these-the hippopotamus-to man seems to be recugnised. A late able writer has quoted, as an illustration of the doctrine of types, a very remarkable passage from Psalm exrxix.:-
> "' I will praise Thee, for I am fearfully and wonderfully made.
> Marvellous are thy works, And that my soul knoweth right well.
> My substance was yot hid from Thee
> When I was made in sceret,
> And curiously wrourpht in the lowest parts of the earth:
> Thine eyes did see my substance yet boing imperfect,
> And in Thy book all my members were written,
> Which in continuance were fashioned when as yet there was none of them.'

"It would too much tax the faith of exegists to ask them to believe that the writer of the above passage, or the spirit that inspived him, actually meant to teach-what we now know so well from geology, that the prototypes of all the parts of the archetypal human structure may be found in those fossil remains of extinct animals which may, in nearly every country, be dug up from the rocks of the earth. No objection need, however, be taken to our reading in it the doctriae of embrgonic development according to a systematic type.
"In that spiritual department which is the special field of scripture, the doctrine of type has been so extensively recognised by expositors, that I need only refer to its typical numbers, its typical personages, its typical rites and ceremonies, and lastly, to its recognition of the Divine Redeemer as the great archetype of the spiritunl world, as man himself is of the matural. In this last respect the New Testament cleurly teaches that, in the resurrection, the human body formed after Adam as its type, is to be sublimated and reformed after the heavenly body of the Son of God, rising to some point of perfection higher than that of the present earthly archetype.
"It is more than curious that this idea of type, so long existing in an isolated and often despised form, as a theological thought in the imagery of scripture, should now be a leading idea of natural science; and that while comparative anatomy teaches us that the structures of all past and present lower animals point to man, who, as Prof. Owen expresses it, has had all his parts and organs 'sketched out in auticipation in the inferior animals,' the Bible points still farther forward to an exaltation of the buman type itself into what even the comparative anatomist might perhaps regard as among the 'possible modifications of it beyond those realized in this little orb of ours,' could he but lenrn its real nature."

The passage given above, even if we cannot go with the author to the full extent of his argument, will shew the suggestive, thoughtcreating character of Dr. Dawson's work. As such, it will shew also, the value of the work itself to the biblical or theological student,
who, shaking off the trammels of a too narrow school, is willing to allow a place in his philosophy to the teachings of the great cosmic harmony which circles around him, and which proclaims through all its changes, $I$, too, am of God.
E. J. C.

## SCIENTIFIC AND LITERARY NOTES.

## PROFESSOR GEORGE WILSON, M.D., F.R.S.E.

Death has of late thinned the ranks of Edinburgh's men of science and letters. Some of the last veterams of the oid Edinburgh Reviev, the foremost of Scottish Metaphysicians, and one eminent in her raaks of native Geologists, have rapidly followed one another to the tomb; but a sense of sorrow not less inteuse than that which was felt on the painful aud sudden loss of Hugh Miller, bus been oceasioned by the death of Dr. George Wilson, the first Regius Professor of Technology in the Uuiversity of Ediaburgh. Dr. Wilson is widely known as the biographer of Cavendish and Reid; the author of "Researches on Colour Blindness," and other scieutific worls; besides numerous valuable papers contributed to scientific periodicals, and to the Transactions of the Royal Society and other learned bodies of which he was a member. His researches embraced a great variety of subjects, and included many discoverics of interest and value; among which may be noted his iurestigations into the history of medical electricity, and his discovery of fluorine in sea-water and in blood.
Dying, however, in his forty-first year, when, to those who knew him best, he seemed only to be ripening for the works of his matured genius: the best of his productions very partially indicate the wide range of thought and the original capacity of his mind. He has left incomplete the biography of his old friend and colleague, Professor Edward Forbes; and many of his papers furnish mere glimpses of the original views in his favourite science of Chemistry which he had purposed to worts out in the leisure of later years he was never destined to see.
In addition to his professorship, Dr. Wilson was Director of the Scottish Industrial Museum. Of this national Institution awriter in the Athencerm, has justly remarked: "Dr. George Wilson was in no small degree the originator of that museum; be gave to it his heart, his genius, and his hopes of success and fame." It would not, indeed, be uujust to say that his life was in some degree the encrifice made by his devotion to that favourite object. Of a warm and generous nature, and with the well-tempered enthusiasm of true genius, he threw his whole heart into whatever he did; and his loss is mourned in his native city with demonstrations of public grief rarely manifested with like intensity. His remaine were followed to the grave by the City Magistrates, the professors of the University, and the representatives of scientific societies and public bodies: and the day of his
funeral was observed as one of public mourning. Such an expression of general grief, was due perbaps even more to the worth of a siugularly upright and genial Curistian man, than to the admiration excited by his rare eluquence as a lecturer, and the fascination of a peculiarly winning and attractive manzer, alike in publie and private. To those who knew him in the iutimate relations of private life, his loss crentes a blank that nothing can replace. To a wider circle it may suffice to say, the world has lost in him,-at the carly age of forty-one,-a most faithful and conscientious serfant of science, and a singularly honest and painstakiug searcher after its truthe. What he has done will give his vame a place among the honoured rauks of our scientific discoverers, -but what be was capable of doing, Ead life been granted to him, would have rendered all he bas done of little account.

## BRITISH ASSOCIATION FOR TGE ADVANCEMENT OF SCIENCE.

The twenty-ninth Annual Meeting of the British Association for the advancement of Science, which opened its proceediags under the presidency of His Royal Highness Prince Albert at Aberdeen, on Wednesday, September 14th, 1859, appears to have fully equalled in general interest the most successful of its predecessors. The attendance was much beyoud the average; and so numerous were the papers communicated to the various Sections, that a mere enumeration of their titles, alone, would occupy many pages of our Journal. In the first Section, for example, comprising Mathematical and Physical Science, ucarly eighty papers were read; and the total number of communications and Reports brought forward at the Meeting, is not far short of four hundred. Some of these papers are of the highest value: but a considerable number are of merely local interest, and many, indeed, appear to be entirely destitute of any special novelty or importance. Considering the uadesirable manner it which really valuable ${ }^{*}$ communications, on account of the limited duration of the Mectings, are obliged to be hurried through, and their discussion greatly shortened, it would seem advisable to restrict the readiug of the papers to such only as contain new facts or practical demonstrations, or which refer to questions of a debatable nature bearing or the philosoply of Science. Mere details of local geology (however useful in their way), with descriptions of ordinary fossils, analyses of river-waters, ordinary metcorological observations, and other papers of a similar character, that neither clear up doubtful points nor open out new paths of inguiry, might surely be forwarded with equal profit to some of the numerous scientific journals, in which, if worthy of regard, they would readily receive insertion. Some plan, at least, will have to be adopted sooner or later, to keep down the formidable array of papers, brought forward, in increasing numbers, at each successive meetiag of the Association.

We give below (from copies of the Aberdeen Ficrald, kindly placed at our disposal by K iofessor Wilson, a Repori of the President's Address, and a fetr of the more important or generally-interesting papers communicated at this Meeting.

THE PRESIDENT'S ADDRESS.

## Gratlemen of tuxe Britism Association,-

Your kind ipvitation to me to undertake the office of your President for the ensuing year could not but startle me on its first announcement. The high position which science occupies, the vast number of distinguished men who labour in her sacred cause, and whose achievements, while spreading innumerable benefits, justly attract the admiration of mankind, contrasted strongly in my mind with the consciousness of my own insignificance in this respect. I, a simple admirer, and wouldbe student of scicuce, to take the place of chief and spokesman of the scientific men of the day, assembled in furtherance of their important objects-the thing appeared to me impossible. Yet, on reflection, I came to the conclusion, that, if not as a contributor to or director of your labours, I might still be useful to you, useful to scieuce, by accepting your offer. Remembering that this Association is a popular Association, not a secret confraternity of men jealously guarding the mysteries of their profession, but invitiag the uninitiated, the public at large, to join them, having as one of its objects to break down those imaginary and hurtful barriers which exist between men of sciense and so-culled men of practice-I felt that I could, from the peculiar position in which Providence had placed me in this country, appear as the representative of that large public, which profits by and admires your exertions, but is wable actively to join in them; that my election was an act of humility on your part which to reject would have looked like false humility, that is like pride, on mine. But I reflected further, and saw in my acceptance the means, of which necessarily so few are offered to her Majesty, of testifying to you, through the instrumentality of her busband, that your labours are not unappreciated by your Sovereign, and that she wishes her people to know this as well as yourselves. Guided by these reflections, my choice was speedily made, for the path of duty lay straight before me.

If these, however, are the motives which have induced me to accept your flattering offer of the Presidency, a request on my part is hardly neccessary that you will receive my efforts to fulfil its duties with kind indulgence.
If it were possible for anytaing to make me still more aware how much $I$ stand in peed of this indulgeace, it is the recollection of the person whou I have to succeed as your President-a man of whom this country is justly proud, and whose name stands among the foremost of the naturalists in Europe for his patience in investigation, conscientiousuess in observation, bolduess of imagination, and acuteness in reasoning. Yon have no doubt listened with pleasure to his parting address, and I beg to thank him for the flattering manoer in which he has alluded to me in it.

The Association meets for the first time to-day in these regions, and in this ancient and interesting city. The poet, in his works of fiction, bas to choose, and anxiously to weigh, where to lay his scene, knowing thai, like the painter, he is thus laying in the background of bis picture, which will give tone and colour to the whole. The stern and dry reality of life is governed by the same laws, and we are here living, feeling, and thinking under the influeuce of the local innpressions of this northern seaport. The choice appears to me a good one. The travelling philosophers bave
had to come far, but in approaching the Highlands of Scotland they meet nature in its wild and primitive form, and nature is the object of their studies. The geologist will not find many novelties in youder mountains, because he will stand there on the bare backbone of the globe, but the primary rocks which stand out in ther nakedness, exhibit the grandeur and beauty of their peculiar form, aud in the splendid quarries of this neighbourhood are seen to peculiar advantage the closeness and hardness of their mass, and their inexhaustible supply for the use of man, made available by the application of new mechanical powers. On this primitive soil the botanist and 20ologist will be attracted only by a limited range of plants and animals, but they are the very species which the extension of agriculture and increase of population are gradually driving out of many parts of the country. On those blue hills the red deer, in vast berds, holds undisturbed dominion over the wide heathery forest, until the sportsman, fatigued and unstrung by the busy life of the bustling town, invades the moor, to regain health and vigone by measuring his strength with that of the antlered monarch of the hill. But, notwithstauding all his efforts to overcome an antatgonist possessed of such superiority of power, swiftuess, caution, and keenness of all the senses, the sportsman would find himself baffed, had not science supplied him with the telescope, and those terrible weapons which seem daily to progress in the precision with which they carry the deadly bullet, mocking distauce, to the mark.

In return for the help which science has afforded him, the sportsman cau supply the naturalist with many facts which he alone has opportunity of observing, and which may assist the solution of some interesting problems suggested by the life of the deer. Man also, the highest object of our study, is found in vigorous healthy developement, presenting a happy mixture of the Celt, Goth, Saxou, and Dane, acquiring his streagth on the hills on the sea. The Aberdeen whaler braves the icy regions of the Polar Sea, to seek and do battle with the great monster of the deep: he has materially assisted in opening these icebound regions to the researches of Science; he fearlessly aided in the search after Sir John Franklin and his gallant companions, whom their country sent forth on this mission, but to whom Providence, alas! has denied the reward of their labours, the return to their homes, to the affectionate embrace of their families and friends, and the acknowledgments of a grateful nation." The City of Aberdeen itself is rich in interest for the philosopher. Its two laicly united Universities make it a seat of Learning aud Science. The Collection of Antiquitics, formed for the present occasion, enables him to dive into olden times, aud, by contact with the remains of the handiwork of the ancient iuhabitants of Scotland, to enter into the spirit of that peculiar and interesting people, which bas attracted the attention and touched the hearts of men accessible to the influence of heroic poetry. The Spalding Club, founded in this city for the preservation of the historical and literary remains of the northeastern counties of Scotland, is honourably linown by its important publications.

Gentlemen!-This is the 29th Aniversary of the foundation of this Association; and weil may we look back with satisfaction to its operation and achievements, throughout the time of its existence. When, on the 27th September, 1831, the Meeting of the Yorbshire Philosophical Society took place at York, in the theatre of the Yorkshire Mluseum, under the presidency of the late Earl Fitzwilliam, then

Viscount Milton, and the Rev. W. Vernou Harcourt eloquently set forth the plan for the formation of a British Association for the promotion of Science, which he showed to have become a want for his country, the most ardent supporter of this resolution could not have anticipated that it would start into life full-grownas it were, enter at once upon its career of usefuluess, and pursue it without deviation from the original design, triumphing over the oppositions which he had to encounter in common with everything that is new and claims to be useful. Gentlemen, this proved that the want was a real, and not au imaginary one, and that the mode is which it was intended to supply that want was based upon a just appreciation of unalterable truths. Mr. Vernon Harcourt summed up the desiderata in graphic words, which have almost identically been retained as the exposition of the objects of the Society, printed at the head of the annually-appearing volume of its Transactions:-" to give a strouger impulse and more systematic direction to scientific inquiry-to promote the iutercourse of those who cultivate Science in different parts of the Empire, with one another and with foreign Philosophers-and to obtain a more general attention to the objects of Scieuce, and a removal of any disadvantages of a public tind which impede its progres."

To define the nature of Science, to give an exact and complete definition of what that Science, to whose service the Association is devoted, is and means, has as it naturally must, at all times oceupied the Metaphysiciau. He has answered the question in various ways, more or less satisfactorily to himself or others. To me, Science, in its most general and comprehensive acceptation, means the knowledge of what I know, the consciousness of human knowledge. Hence, to know, is the object of all Science; and all special knowledge, if brought to our consciousness in its separate distiuctiveness from, and yet in its recoguised relation to the totality of our knowledge, is scientific knowledge. We require, then, for Science-that is to say, for the acquisition of scientific knowledge-those two activities of our miud which are necessary for the acquisition of any knowledge-analysis and synthesis; the first, to dissect and reduce into its component parts the objects to be investigated, and to render an necurate account to ourselves of the nature and qualities of these parts by obserration; the second to recompose the observed and understood parts into a unity in our consciousness, exactly answering to the object of our investigation. The labours of the man of Science are therefore at once the most humble aud the loftiest which man can undertake. He only does what every little child does from its first awakening into life, and must do every moment of its existence; and yet he aims at the gradual approximation to divine truth itself If then, there exists no difference between the work of the man of Science and that of the merest child, what constitutes the distinction? Meraly the conscious selfdetermination. The child observes what accident brings before it, and unconsciously forms its notion of it; the socalled practical man observes what his special work forces upon him, and he forms his notions upon it with reference to this peculiar work. The man of Science observes what he intends to observe, and knows why he intends it. The value which the peculiar object has in his eyes is not determined by accident, nor by an exterual cause, such as the mere connexion with work to be performed, but by the place which he knows this objeet to hold in the general universe of knowledge, by the relation which it bears to oither paris of that general knowledge.

To arrange and classify that universe of knowledge becomes therefore the first and perhaps the most important, object and duty of Science. It is only when brought into a aystem, by separating the incongruous and combining those elements in which we have been enable to discover the internal connexion which the Almighty has implanted in them, that we can hope to grapple with the boundless. ness of His creation, and with the laws which govern both miud and matter. The operation of Science then has been, systematically to divide human knowledge, and raise, as it were, the separate groups of subjects for ecieutific consideration, into different and distinct sciences. The tendency to create new sciences is peculiarly apparent in our present age, and is perbaps inseparable from so rapid a progress as we have seen in our days; for the acquaintance with aud mastering of distiuct branches of knowledge enables the eye, from the newly-gained poiuts of sight, to see the new ramifications into which they divide themselves in strict consecutivi ness and with logical necessity. But in thus gaining nesp centres of light, from Which to direct our researches, and new and powerful means of adding to its everincreasing treasures, science approaches no uenrer to the limits of its range. although travelling further and further from its original point of departure. For God's world is infinite; and the boundlessness of the universe, whose confines appear ever to retreat before our fuite minds: strikes us no less with awe when, prying into the starry crowd of heaven, we find new worlds revealed to us by every increase in the power of the telescope, than when the microscope discloses to us in a drop of water, or an atom of clust, nerv worlds of life and animination, or the remains of such as have passed away.

Whilst the tendency to push systematic investigation in every di"ection enables. the individual mind of man to bring all the power of which he is capable to bear on the specialities of his study, and enables a greater number of labourers to take partin the universal work, it may be feared that that consciousness of its unity which must pervade the whole of science, if it is not to lose its last and highest point of sight, may suffer. It has occasionally been given to rare intellects and the highest genius, to follow the various sciences in their divergent roads, and yet to preserve that point. of sight from which alone their totality can be contemplated and directed. Yet hav rare is the appearance of such gifted intellects! And if they be found at intervals, they remain still single.individuals, with all the imperfections of human nature.

The:anly mode of supplying with any certainty this want, is to be sought in the combination of men of science representing all the specialities, and working together for the common object of preserving that unity and presiding over that general direction. This has bees, to some extent, done in many countries by the establishment of academies embracing the whole range of the sciences, whether physical or metaplysical, historical or political. In the abseace of such an institution in this.country, all lovers of science must rejoice at the existence and activity of this Association, which embraces in its sphere of action, if pot the whole range of the sciences, yet a very large and important section of them, those known as the inductive saicnces, excluding all that are not approached by the inductive methoc of investigation. It has, for instance (and, considering its peculiar organisation and mode of setion, perhaps not uowisely), eliminated from its consideration and discussions those which come under the description of moral and
political sciences. This has not been done from undervaluing their importance and denying their sacred right to the special attention of mankind, but from a desire to deal with those subjects only which can be reduced to positive proof, and do not rest on opinion or faith. The subjects of the moral and political seiences involve not only opinions but feclings; and their discussion frequently rouses passions. For feelings are "subjective," as the German metaphysician has it-they are iuseparable from the individual being-an attac $k$ upou them is felt as one upon the persou itself; whilst facts are "objective," and belong to every-body-they remain the same facts at all times and under ell circumstances: they can bo proved; they bave to be proved; and when proved, are finally settled. It is with facts only that the Association deals. There may, for a time, exist differences of opiniou on these also, but the process of removing them and resolving them into agreement is a different oue from that in the moral and political sciences. These are generally appronched by the deductive process; but if the reasoning be ever so acute und logically correct, and the point of departure, which may be arbitrarily selected, is disputed, no agreement is possible; whilst we proceel here by the inductive process, taking nothing on trust, nuthing for granted, but reasoning uprards from the meane-t fact established, and making every step sure before going one beyond it, like the eugineer in his appronehes to a fortress. We thus gain ultimately a roadway, -a ladder by which even a child may, almost without knowiog it, ascend to the summit of truth, and obtain that immensely wide and extemsive view which is spread below the feet of the astonished beholder. This road has been shown us by the great Bacon; and who can coutem plate the prospects which it opens, without almost falling into a trance similar to that in which he allowed his imagination to wander over future ages of discovery!

From amongst the political sciences it has been attempted in modern times to detach one which admits of being severed from individual political opinions, and of being reduced to abstract laws derived from well-authenticated facts. I mean political economy, based on geueral statistics. A new Association has recently been formed, imitating our perambulating habits, and striving to comprehend in its investigations and discussions even a still more extended rauge of subjects, in what is called "sucial scieuce." These efforts deserve our warmest approbation and good-will. May they succeed in obtaining a purely and strictly scientific character! Our own Association has, siuce its meeting in Dublin, recogoized the growing claims of political economy to scientific brotherhood, and admitted it into its statistical section. It could not have doue so under abler guidance aud happier auspices than the Presidency of the Archbishop of Dublin, Dr. Whately, Whose efforts in this direction are so universally appreciated. But even in this section, and whilst statistics alone were treated in it, the Association, as far back as 1833 , made $i_{i}$ a rale that, in order to ensure positive results, only those classes - of facts should be admitted which were capable of being expressed by numbers, and which promised, when sufficiently multiplied, to indicate general laws.

If, then, the main object of science-and I beg to be understo od, henceforth, as speaking only of that section which the Association has under its special care viz., inductive science-if I say, the object of science is the discovery of the laws which govern natural phenomema, the primary condition for its success is:-Accurate obserpation and collection of facts in such comprelensiveness and com-
pleteness as to furnieh the philosopher with the necessary material from which to draw safe conciusions.

Science is not of yesterday. We stand on the shoulders of past ages, and the amount of observations made, and facts ascertainel, has been transmitted to us, and carefully preserved in the various storehouses of science; other crops have been reaped, but still lie seattered on the field; many a rich harvest is ripe for cutting, but waits for the renper. Economy of labour is the essence of good husbandry, and no less so in the field of science. Our Association has felt the importance of this truth, and may well claim, as one of its priucipal merits, tho constant endeavour to secure that economy. One of the latest undertakings of the Association has been, in conjunction with the Royal Society, to attempt the compilation of a classified catalogue of scientific memoirs, which, by combining under one head the titles of all memoirs written on a certain subject, will, when completed, enable the student who wishes to gain information on that subject to do so with the greatest ease. It gives him, as it were, the plan of the house, and the key to the different apartments in which the treasures relating to his subject are stored, saving him at once a painful and laborious search, and affording him at the same time all assurance that what is here offered contains the whole of the treasures yet acquired.

While this has been one of the latest attempts, the Associntion has from its very beginning hept in view that its main sphere of usefulness lay in that concentrated attention to all scientific operations which a general gives to the movements of his army, watching and regulating the progress of his impetuous soldiers in the different directions to which their ardour may have led them, carefully noting the gaps which may arise from their independent and eccentric action, and attentively observing what impediments may have stopped, or may threaten to stop, the progress of certain columns. Thus it attempts to fix and record the position and progress of the different labours, by its reports on the state of sciences published ammally in its transactions;-thus it directs the attention of the labourers to those gaps which require to be filled up, if the progress is to be a safe and steady one -thus it comes forward with a helping hand, in striving to remove those impediments which the unaided efforts of the individual labourer have been or may be unable to overcome.

Let us follow the activity of the Association in these three different birections. The Reports on the state of Science originate in the conviction of the necessity for fixing, at given inter-als, with accuracy and completeness, the position at Which it has arrived. For this object, the General Com mittee of the Association entrusts to distinguished individuals in the different branches of science the charge of becoming, as it were, the biographets of the period. There are special points in different sciences in which it sometimes appears desirable to the different sections to have specinl reports elaborated; in such cases the General Committee, in its capacity of the representative assembly of all the sciences, reserves to itself the right of judging what may be of sufficient importance to be chus recorded

The special subject: which the Association points out for investigation, in order to supply the gaps which it may have observed, are-either such as the philosopher alone can successfully investigate, because they require the close attention of a practised observer, and a thorough knowledge of the particular subject; or
they are such as require the greatest possiblo number of facts to be obtained. Here science ofteu-stands in need of the assistance of the genoral public, nod gratefully necepts any contribution offered, provided the facts be accurately observed. In either ease the Association points out what is to observed. and how it is to be observed. The first is the result of the same careful sifting process which the Association employs in directing the issue of specinl reports. The investigations are entrusted to specially-appoiated committees or selected individuals. They are in most cases not unattended with considerable expense, and the Association, not content with merely suggesting and directing, furnishes by special grants the pecuniary means for defraying the outhy caused by the nature and the extent of the inquiry. If we consider that the income of the Association is solely derived from the contributions of its members, the fact that no less a sum than $£ 17,000$ bis, since its commencement, been thus granted for scientific purposes, is certainly most gratifying. The question how to observe, resolves itself into troo,-that of thie scientific method which is to be employed in appronching a problem or making an observation, and that of the philosophical instruments used in the observatiou or experiment. The Association brings to bear the combined knowledge and experience of the scientific men not only of this but other countries, on the discovery of that niethod which, while it economises time and labour; promises the most accurate'results. The method to which, after careful examination, the palm has been awarded, is then placed at the free disposal and use of all scientific investigators. The Assaciation also issues, where practicable, printed forms, merely requiring the different heads to be filled up, which, by their uniformity, become an important means for assisting the subsequent reduction of the observations for the abstraction of the laws which they may indicate. At the same time most searching teste and inquiries are constaritly carried on in the Observatory at Kew, given to the Association by Her Majesty, the object of which is practically to test the relative value of different methods and iastruments, and to guide the constantly progressive improvements in the construction of the latter. The establishment at Kew has undertaken the further important service of verifying and correcting to a fixed standard the instruments of any maker, to enable observafions made with them to be reduced to the same numerical expression. I need hardly remind the inhabitints of Aberdeen that the Association, in one of the first years of its existence, undertook the comparative measurement of the Aberdeen standard scale with that of Greenwichi-ia research ably carried out by the late Mr. Baily.

The impedinients to the general progress of science, the removal of which I have indicated as one of the tasks which the Association has set for itself, are of trarious kinds. If they were only such as direction, advice, and encouragement would enable the idedividual, or even combined efforts of philosophers, to overcome, the exertions of the Association which I have just alluded to might be sufficient for the purpose. But they are often such as can only be successfully dealt with by the powerfularm of the State; or tlie long purse of the nation. These impediments may be caused either by the social condition of the country itself, by restrictions arising out of pecculiar laws, by the politieal separation of different countries, or by the magnitude of the undertakings being out of all proportion to the means and power of single individuals of the Asseciation, or even the volun-
tary efforts of the public. In these cases the Association, together with its sister Society, "the Royal Society," becomes the spokesman of Science with the Crown, the Government, or Parlinment-sometimes, even, through the Home Goverament, with Foreign Governments. Thus it obilined the establishment, by the British Government, of magnetic and meteorological observatories in six different parts of the globe, the beginning of a network of stations which we must hope will be so far extended as to compass, by their geographical distribution, the whole of the phenomena which throw light on this important point in our tellurian and even cosmical existence. Tho Institute of France, at the recommendation of M5. Arato, whose loss the scientific world must long deplore, cheerfully co-operated with our Council on this occasion. It was our Association which, in conjunction with the Royal Society, suggested the Antarctic Expedition, with a view to further the discovery of the laws of terrestrial magnetism, and thus led to the discovery of the southern polar continent. It urged on the Admiralty the prosecution of the tidal observations, which that Department has since fully carried out. It recommonded the establishment, it the British Museum, of the conchological collection, exhibiting present and extinct species, which has now become an object of the greatest interest.

I will not weary you by further examples, with which most of you are better acquainted than I am myself, but inerely express my satisfaction that there should exist bodies of men who will bring the well-considered and understood waots of science before the public and the Goverament, who will even hand round the begging-box, and expose themsalves to refusals and rebuffs to which all beggars are liable, with the certainty besides, of being considered great bores. Please to recollect that this species of bore is a most useful animal, well adapted for the ends for which nature inteuded him. He alone, by constantly returning to the charge, and repeating the same truths and the same requests, succeeds in awakening attention to the cause which he adrocates, and obtains that hearing which is granted him at last for self-protection, as the minor evil compared to his importunity, but which is requisite to make his cause understood. This is more particularly the case in a rree, active, enterprising, and self-determining people like ours, where every interest works for itself, considers itself the all-important one, and makes its way in the world by its own efforts. Is it, then, to be wondered at, that the interests of science, abstract as science appears, and not immediately showing a return in pounds, shillings, and pence, should be postponed, at least, to others which promise immediate tangible results? Is it to be wondered at, that even our public men require an effort to wean themselves from other subjects, in order to give their attention to science and men of science, when it is remembered that science, with the exception of mathematics, was, until of late, almost systematically excluded from our school and university educntion;-bthat the traditions of early life are those which make and leave the strongest impression on the human mind, and that the subjects with which we become acquainted, and to which orre energies are devoted in youth, are those for which we retain the liveliest intcrest in after years, and that for these reasons the effort required must be both a mental and a moral one? A deep debt of gratitude is therefore due to bodies like this Association, which not only urges the wants of science on the

Government, but furnishes it at once with well-matured plans how to supply them with the greatest certainty and to the greatest public advantage.

We may be justified in hoping, however, that by the gradual diffusion of science, and its increasing recognition as a principal part of our uational education; the public in general, no less than the Legislature and the State, will more and more recoguise the claims of science to their attention; so that it may no longer require the begging-box, but speak to the State, like a favoured child toits parent, sure of his parental solicitude for its welfare; that the State will recognise in science oue of its elemeuts of strength and prosperity, to foster which the clearest dictates of self.interest demand.
If the activity of this Association, such as I have endeavoured to describe it, ever found or could fiud its personification in one individual-its incarnation, as it were-this had been found in that distinguished and revered philosopher who has been removed from amongst us, in his ninetieth yenr, within these last few months. Alexander von Humboldt ineessautly strove after dominion over that universality of buman knowledge which stands in need of thoughtful government and direction to preserve its integrity; he strove to tie up the fasces of scientific knowledge, to give them strength in unity. He treated all scientific men as members of one family, enthusiastically directing, fostering, and encouraging inquiry, where he saw either the want of, or the willingoess for, it. His protection of the young and ardeat student led many to success in their pursuit. His personal influence with the Courts and Governments of most couutrics in Europe, evabled him to plead the canse of science in a manner which made it more difficult for them to refuse than to grant what he requested. All lovers of science deeply mourn for the loss of such a man. Gentlemen, it is a singular coincidence, that this very day on which we are here assembled, and are thus giving expression to our admiration of him, should be the anniversary of his birth.
To return to ourselves, however. One part of the functions of the Association can receive no persoual representation-no incarnation. I mean, the very fact of meetings like that which we are at present inaugurating. This is not the thoughtful direction of one mind over acquired kuowledge, but the production of nerr thought by the contact of many minds, as the spark is produced by the friction of flint and steel; it is not the action of the monarchy or a paternal government, but the republican activity of the Roman Eorum. These meetings draw forth the philosopher from the hidden recesses of his study, call in the wanderer over the field of science to mect his brethren, to lay before them the results of his labours, to set forth the deductions at which he bas arrived, to ask for their examination, to maiatain in the combat of debate the truth of his position and the accuracy of his observations. These reeetings, unlike those of any other society, throw open the arena to the cultivators of all sciences, to their mutual advantage: the Geelogist learns from the Chemist that there are problems for which he bad no clue. but which that science cau solve for him; the Geographer receives light fro he Naturalist, the Astronomer from the Physicist and Engineer, and so on. And all find a ficld upon which to meet the public at large, invite them to listen to their reports, and even to take part in their discussions; show to them that philosophers are not vain theorists, but essentially men of practice-not conceited pedants, wrapped up in their own mysterious importance, but humble in-
quirers after truth, proud only of what they may have achieved or won for the general use of man. Neither are they daring and presumptuous unbelievers-a character which ignorance has sometimes aftred to them-who would, like the Titans. storm heaven, by placing mountain upon mountain, till huled down from the height attained by the terrible thuaders of outraged Jove; but rather the pious pilgrims to the Holy Laud, who toil on in search of the sacred shrine, in search of truth-God's truth-God's laws as manifested in His works, in His creation.
[A very interesting communication, laid before the Geological Section, by Sir Charles Lyell, "On the Results of some Observations in France, in reference to the Antiquity of the Human Race," appeared in the last number of the Canalian Journal, Vol.IV. p 497. In the present Number we give two additional papers: one of great value, "On Fossil and Recent Reptilia," by Professor Orven; and a communication of much general interest, "On Japan;" by Lawrence Oliphant, E:q.]

ON TER ORDERS OF FOBSIE AND DECENT REPTILIA, AND THEIR DISTBIBUTYON IN TIME,* BY PROR, UWEN, F.R.S., ETC.
Professor Owen began by remarking that, with the eaception of Geology, no collateral science had profited so largely from the study of organic remains as Zoology. The catalogues of animal species had received immense accessions from the determination of the nature and affinities of those which had become extinct, and much deeper and clearer insight had been gained into the natural arrangement and subdivision of the classes of animals since Palæontology had expanded our survey of them., Of this the class Reptilia, or cold-blooded airbreathing Vertebrates, afforded a striking example. In the latest edition of the 'Regne Animal,' of Cuvier, 1829, as in the 'Elemens do Zoologie' of M. Edwards, 1834-37, and the still more recent monograph on American Testudinata, by Agassiz, 4to, 1857, the quadruple division of the class, proposed by Brongniart in 1802, was adhered to, viz., Chelonia (tortoises, turtles), Sauria (crocodiles, lizards), Ophidia (serpents); Batrachia (frogs, newts); only the last group is made a distinct class by the distinguished Professor of the United States:-"After this separation of the Batrachians from the true Reptiles we have only three orders left in the class of Reptiles proper,-the Ophidians, the Saurians, and the Chelonians," l. c. p. 239. In Prof. Owen's Reports on British Fossil Reptiles, to the British Association, in 1839 and 1841, it was proposed to divide the class into eight orders, viz, Enaliosauria, Crocodilia, Dinosauria, Lacertilia, Pterosuuria, Chelonia, Ophidia, and Batrachia, which were severally characterized. Subsequent researches had brought to light additional forms and struotural modifications of cold-blooded air-breathing animals now extinct, which bad suggested corresponding modifications of their distribution into ordinal groups. Another result of such deeper insight into the forms that have passed away, bas been the clearer recognition of the artificiality of the boundary between the classes Pisces and lieptilia of modern zoological systems. The conformity of pattern in the arrangement of the bones of the outwardly well-ossified skull in certain

[^11]fighes with well developed lung-like air-bladders (Polypterus, Lepidosteus, Sturio), and in the extinct reptiles, Archegosaurus and Labyrinthodon: the persistence of the notochord (chorda dorsalis) in Archegosaurus as in Sturio: the persistence of the notochord and branchial arches in Archegosaurus and Lepidosiren: the absence of occipital condyle or condyles in Archegosaurus as in Lepidosiren: the presence of teeth with the labyrinthic saterblendiug of dental tissues in Dendrodus, Lepidosteus, and Archegosnurus, as in Lalyrinthodon: the large median and lateral throat-plates in Archegosaurus as in Megalichthys, and in the modern fishes Arapaima and Lepidosteus:-all these characters, as the author had urged in his Lectures at the Government Schuol of Mines (March, 1858), pointed to one great natural group, remarkable for the extensive gradations of development, linking and blending together fishes and reptiles within the limits of such group. The salamandroid (or so-called "sauroid") Ganoids-Lepidosteus and Polypterusare the most ichthyoid, the Labyrinthodonts the most sauroid, of the great group: the Lepidosiren and Archegosaurus are intermediate gradations, one haviag more of the piscine, the other more of the reptilian, character. Archegosaurus conducts the march of development from the fish proper to the Labyrinthodont type; Lepidosiren conducts it to the pereanibranchiate, or modern batrachian, type. Both forms expose the artificiality of the ordinary class-distinction between Pisces and Reptilia, and illustrate the naturality of the cold-blooded Vertebrates, or "Hæmatocrya" ( $a \mu \mu$, blood, крvos, frost: the correlative group is the "hæmatotherma.") Reptiles are defined as "cold-blooded, air-breathing Vertebrates;" but the Siren and Proteus chiefly breathe by gills, as did most probably the Archegosaurus. The modern naked Batrachin annually mature, at once, a large number of small ova. The embryo is developed with but a small allantoic appendage, and is hatched with external gills. These are retained throughout life by a few species; the rest undergo a more or less degree of metamorphosis. Other existing reptiles have comparatively few and large eggs; and the embryo is inclosed in a free amnios, and is more or less enveloped by a large allantois. It undergoes no marked transformation after being hatched. On this difference the Batrachia have been by some naturalists separated as a distinct class from the Reptilia. But the number of ova simultaneously developed in the viviparous land salamanders is much less than in the siren, and not more than in the turtle; and, save in respect of the external gills, wbich disappear before or soon after birth, the salamauder does not undergo a more marked transformation, after being hatched, than does the turtle or crocodile.* It depends, therefore, upon the value assigned to the different propurtions of the allantois in the embryo of the salamander and lizard, whether they be prononnced to belong or not to distinct classes of animals. This embryonic, or developmental, character, is unascertainable in the extinct Archegosaurus and Labyrinthodon. The affinity of Labyrinthodon to Ichthyosaurus, and those structures which have led the ablest Germans palæontologists to pronounce the Labyrinthodonts to be true Saurians, under the names of Mastodonsaurus, Trematosaurus. Capitosaurus, \&ce., may well support the conjecture that modifications more "reptilian" than those in Salamandra may have attended the development of their young. Characters derived

[^12]from the nature of the cutaneous covorings equally fail to determine the classcharacters of Batrachia as contra-distinguished from Reptilia. It is true that all existing Batrachia have a scaleless skin, or very miaute senles (Crecilin), but not all existing reptiles have horny seales. The crocodiles and certain lizards show a development of dermal boues similar to that in certain placoid and gauoid fishes. This develnpment is greater, and the resemblanco is closer, in those ancient forms of Reptilin which exhibit in their endo-skeletou unmistakeable signs of their affinity to ganoid fishes and Batrachia. In a survey, therefore, of the present bnoma forms of cold-blooded, air-breathing Vertebrates, recent and fossil, Prof. Owen could not define any real and adequate boundary,for dividing them primarily into two distinct classes of Batrachians and Reptiles. As little was he able to point out a character dividing the air-breathing from the water-breathing Hama-tocryn-the reptiles from the fishes. In the present communication the author drew an arbitrary line between Lepidnsiren and Archegosaurus, nud proposed to begin his review of the ordinal groups of Reptilia, or air-breathiag Hzmatocrya, with that of which the Archegosaurus was the trin.

Order I. Ganocephala.-For this group or 0 ier he proposed the name of Gainocephala ( $\gamma$ avos, listre, $\kappa \in \phi \alpha \lambda \eta$, head), in reference to the sculptured und ex-ternally-polished or ganoid bony plates with which the entire head was defended. These plates include the "postorbital" and "supertemporal" ones, which snof over the temporal fossm. No occipital condyles. The teeth have converitins inflected folds of cement at their basal half. The notochord is persistent; the vertebral arches and peripheral elements are ossified ; the pleurapophyses are short and straight; pectoral and pelvic limbs, which are natatory and very small; large median and lateral "throat-plates;" scales small, carinate, sub-ganoid; traces of branchial arches. The above combination of characters gives the value of an ordinal group in the cold-blooded Vertebrata. The extinct animals which manifest it were first indicated by certain fossils discovered in the sphærosideritic clay-slate forming the upper member of the Bavarian conl-measures, and also in splitting spheroidal enncretions from the coal-field of Sanybbruck, near Treves; these fossils were originally referred to the class of fishes (Pygopterus Lnscius, Agassiz.) But a specimen from the "Brandschiefer" of Münster-Appel presented characters which were recognised by Dr. Gergens to be those of a Salamandroid reptile.* Dr. Gergens placed his supposed "Salamander" in the hands of M. Hermann von Meyer for description ; who communicated the result of his examination in a later number of the under-cited journal.t In this notice the author states that the Salamander-affiaities of the fossil in question, for which he proposes the name of Apateon pedestris, "are by no means demonstrated." $\ddagger$ "Its bead might be that of a fish, as well as of a lizard, or of a batrachimo." "There is no unace of bones of limbs." M. von Meyer concludes by stating that, "in order

[^13]to test the hypothesis of the Apateon being a fossil fish, he has sent to Agassiz adrawing, with a description of it." Theree years later, better preserved and more instructive specimens of the problematical fissil were obtained by Prof. von Dechen from the Bavarian coal-fielde, and were submitled to the examination of Prof. Goldfuss, of Bonu; he published a quarto memoir on them, with good figures, referring them to a Saurian genus, which he calls Archegosaurus, or "primeval lizard"-deeming it to be a transitional type between the fish-like Batrachia and the lizards and crocodiles.* The estimable author, on the occasion of publisbing the above memoir, transmitted to Prof. Owen excellent casts of the originals therein described and figured These casts were presented by the Professor to the Museum of the Royal College of Surgeons, London, aud were described by him in his 'Catalogue of the Fossil Reptiles,' in that Museum, (4to. 1854). The conclusions which Prof. Owen formed thereupon, as to the position and affinities of the Archegosaurus in the reptilian class, are published in that Catalogue, and were communicated to and discussed at the Geological Society of London (ste the 'Quarterly Journal of the Geological Society,' Vol. iv., 1848). One of the specimens appeared to present evidence of persistent branchial arches. The osseous structure of the skull, especially of the orbits, through the completed zygonatic arches, indicited an affinity to the Labyrinthodonts; but the vertebre and numerous very short ribs, with the indications of stunted swimming limbs, impressed the writer with the conviction of the near alliance of the Archegosaurus with the Proteus and other perenuibrauchiate reptiles. This conclusion of the affinity of Archegosaurus to existing types of the reptilian class is confirmed by the subsequently discovered specimens described and figured by $\mathbf{M}$. von Meyer, in his ' Palæon'ographica' (Bd. vi., 2te Hef. 1857).-more especinlly by his discovery of the embryonal condition of the vertebral column $\dagger$-i. e., of the persistence of the notochord, and the restriction of ossification to the arches and peripheral vertebral ilements. In this structure the old carbnaiferous Repiiie resembled the existing Lepidosiren, and afforded further ground for regarding that remarkable existing animal as , me which obliterates the line of demarcation between the fishes and the reptiles. Coincident with this nor-ossifed stiste of the basis of the vertebrate bodies of the trunk is the absence of the ossified occipital condyles, which condyles characterize the skull in better duveloped Batrachia. The fore part of the notochord has extended into the basi-splevoid region. and its capsule has connected it, by ligament, to the broad, flat ossifications of expansions of the same capsule, forming the basi-occipital or basi-sphenoid plate. The vertebræ of the trunk in the fully developed full-sized animal present the following stages of ossification. The neurapophyses coalesce at the top, to form the arch, from the summit of which was developed a compressed, subquadrate, moderately high spine, with the truneate, or slightly convex, summit, expanded in the fore and aft direction. so as to touch the contiguous spines in the back: the spines are distinct in the tail. The sides of the base of the neurai arch are thickeped and extended outwards into diapophyses, having a convex articular surface for the attachment

[^14]of the rib: the fore part is slightly produced at each augle into a zygapophysis looking upward and a little forward; the hinder part was much produced backwards, supporting two-thirds of the neural spine, and each augle developed into a zygapophysis, with a surface of opposite aspects to the auterior one. In the capsule of the notochord three bony plates were developed, one on the ventral surface, and one on each side, at or near the back part of the diapophysis. These bony plates may be termed "cortical parts" of the centrum, in the same seuse in which that term is applied to the element which is called "body of the atias" in man and Mammalia, and "sub-vertebral wedge-bone" at the fore part of the neek in Eunliosauria. As such ventral or inferior cortical elements co-exist with seemingly complete centrums in the Ichthyosaurus, thus affording ground for deeming them essentially distinct from a true centrum, the term "hypapophyses" had been proposed by Prof. 0 , ou for such independent inferior ossifications in and from the notochordal capsule, aud by this term may be signified the sub-motochordal plates in Archegosaurus, which co-exist with proper "immapophyses," in the tail. In the trunk they are flat, stibquadrate, oblong bodies, with the angles rouaded off; in the tail they bend upwards by the extension of the ossification from the :nder to the side parts of the notochordal capsule; sometimes touchiog the lateral cortical pates. These serve to strengthen the notochord and support the intervertebral nerve in its outward passage. The ribs are short, almost straight, expanded and flattened at the er ds, round and slender at the middle. They are developed throughout the trumk and along part of the tail, ec-existivg there with the hemal arches, as in the meuopone.* The hamal arches, which are at first open at their base, become closed by extension of ossification inwards from each produced augle, converting the notch into a foramen. This forri. a wide oval, the apex being produced into a long spine; but towards the end of the tail the spine becomes shortened, and the hen al arch is reduced to a mere fatiened ring. The eize of the canal for the protection of the caudal blood-vessels indicates the powerful muscular actions of that part; as the produced spines from both neural and hemal arches bespeak the provision made for muscular attachments, and the vertical development of the caudal swmming organ. all these modifications of the vertebral column denonstrate the aquatic habits of the Archegosaurus; the limbs being in like mauner modified as fius, but so smaill and feeble, as to leave the wain part of the function of swimining to be performed, as in fishes and perenuibranchiate batrachia, by the tail. The skull of the Arcl. gozaurus appears to have retained much of its primary cartilage internally, and ossification to have been chiefly active at the surface; where, as in the combined dermo-neural ossifieations of the skull in the sturgeons and salamandrcid fishes, c.g., Polypterus, Amin, Lepidosteus, these ossifications have started from centres more numerous, than those of the true vertebral sy,tew in the skall of Saurian reptiles. The teetb are usually shed alternately. They consist of osteo-dentine, deutine, and cement. The first substance occupies the centre, the last covers the superficies of the tooth, but is intruduced into its substauce by many concentric folds extending along the basal half. These folds are indicated by fine longitudinal straight strix along that half of the crown. The section of the tooth at that part gives the

[^15]same structure which is shown by a like section of a tooth of the Lepidosteus. oxyurus.* The same principle of dental composition is exemplified in the teeth of most of the ganoid fishes of the Carboniferous and Devonian systems, and is carried out to a great and beautifr' degree of complication in the old red Dendrodonts. The repetition of the same principle of dental structure in one of the earliest $\ddagger$ euera of Reptilia, associated with the defect of ossification of the endoskeleton and the excess of ossification in the exa-skeleton of the head, decisively illustrate the true affinities and low position in the Reptilian class of the so-called Archegosari. For other details of the peculiar and interesting structure of the animals representing the earliest or oldest known order of Reptiles, Prof. Owen referred to the article "Palæontology" in the "Eucyclopædia Britannica.' This order is "carbonifernus."

Order II.-Labyrinthodontia.-Head defended, as in the Ganocephala, by a continuous casque of extemally eculptured and unusually hard and polished osseous plates, includiug the supplementary "postorbital" and "supertemporal" bones, but leaving a "foramen parietale." $\dagger$ Two occipital condyles. Vomer divided and dentigerous. Two nostrils. Vertebral centra, as well as arches, ossified, biconcave. Pleurapophyses of the trunk, long and bent. Teeth rendered complex by undulation and side branches of the converging folds of eement, wheace the name of the order. Osseous scutes in some. The reptiles presenting the above characters have been divided, according to minor modifications exemplified by the form and proportions of the skull, by the relative position and size of orbital, nasal and temporal cavities, \&c., into the several genera; as e.g. Mastodonsaurus. Trematosaurus, Metopias, Capitosaurus, Zygosaurus, Xestorrhytias. The relation of these remarkible repiiles to the Saurian order has been advocated as being one of close and true affinity, chicfly on the character of the extent of ossification of the skull and of the outward sculpturing of the cranial bones. But the true nature of some of these bones appears to have been overlooked, and the gaze of research for analogous structures has been too exclusively upward. If directed downward from the Labyrinthodontia to the Ganocephali, and to certain gavoid fishes, it suggests other conclusions, which had been worked out by Prof. Owen, in his article on "Palæcntology," above referred to. There is nothing in the known structure of the so-named Archegosaurus or Mastodensaurus that truly indicates a belonging to the Saurian or Crocodilian-order of reptiles. The exterior ossifications of the skull and the cavine-shaped labyriuthic teeth are both examples of the Salamandroid modification of the gavoid type of fishes. The small proportion of the forelimb of the Mystriosaurus in nowise illustrates this alleged saurian affinity; for though it be as shortas in Archegosauras, it is as perfectly constructed as in the Crocodile, whereas the short fore-limb of Archegosaurus is constructed after the simple type of that of the Proteus and Siren. Bue the futility oi this argument of the sauroid affinities is made manifest by the proportions of the hind-limb of Archegosaurus; it is as stunted as the fore-limb. In the Jabyrinthodonts it presented larger proportions, which, however, may be illustrated as naturally by these proportions of the limbs in certain Batrachia, as in the Teleosaurus.

[^16]Order III.-Ichthyopterygia.-The bones of the head still include the supplementary "post-orbitals" and "supra-temporals," but there are simall tempral and other vacuities between the cravial bones: a "foramen parictale," a single convex occipital coudyle,* and one vomer which is edentulous. Two antorbital nostrils. Vertebral centra, ossified, biconcave. Pleurapophyses of the trunk long and bent the anterior ones with bifurcate heads. Teeth with converging folds of cement at their base; implanted in a common alvenle.: groove, and confived to the maxillary, premaxillary, and premandibular bones. Premaxillaries much exceeding the maxillaries in size. Orbit very large : a circle of sclerotic plates. Limbs natatory; with more than five multiarticulate digits; no sacrum. With the retention of characters which indicate, as in the precediug orders, an affinity to the higher Ganoidea, the present exelusively marine Reptilia more directly exemplify the Ichthyic type in the proportions of the premaxillary and maxillary bones; in the shortness and great number of the biconcave vertebre; in the length of the pleurapophyses of the vertebræ near the head; in the iarge proportional size of the eyeball, and its well-ossified sclerotic coat, and especially in the structure of the pectoral and ventral fins. The stia is naked. The order ranges from the lias to the chalk.

Order IV.-Sauropterygia.-No post-orbital and supra-temporal bone: $\dagger$ large temporal and other vacuities between certain crauial boues; a foramen parietale; two antorbital nostrils; teeth simple, in distiact sockets of premaxillary, maxillary, and premandibular bones. rarely on the palatine or pterygoid bones; maxillaries larger than premaxillaries. Limbs natatory; not more than five digits. A sacrum of one or two vertebrof for the atachment of the pelvic arch in sume, numerous cervical vertebre in most. Pleurapophyses vith simple heads; those of the trunk long and bent. Tn the Pliosaurus the neck vertebre are enmparatively few in number, short and flat. The sauropterggian type seems to hav's attained its maximum dimensions in this genus: the species of which are peculiar to the Oxfordian and Kimmeridgian divisions of the Upper Oolitic system. M. von Meyer regards the number of cervical vertebro and the length of neck as characters of prime importance in the classification of Reptilia, and founds thereon his Order called Macrotracheleu, in which he includes Simosaurus, Pistosaurus and Nothosaurus, with Plesiosaurus. No doubt the number of vertebrse in the same skeleton bears a certain relation to ordinal groups; the Ophidia find a common character therein; jet it is not their easential character; for the snake-like form, dependent on multiplied vertebra, characterizes equally eertain Batrachians (Cæcilia) and fishes (Murœaa). Certain regions of the vertebral columa are the seats of great varieties in the same natural group of Reptilia. We have longtailed and short-tailed lizards: but do not, therefore, separate those with numerous caudai vertebr as "Macrouran," from those with few or none. The extinct Dolichosaurus $L_{\text {. }}$ the Kentish chalk, wibh its procolian vertebre, cannot be ordinally separated, by reason of its more numerous cervical vertebrx, from other shorter-necked procelian lizards. As little can we separate the short-necked and, the big-headed amphicclian Pliosaur from the Macrotrachelians of Von Meyer-

[^17]with which it has its most intimate and true affinities. There is much reason, indeed, to suspect shat some of the Muschelkalk Saurians, which are as closely allied to Nothosaurus as Pliosaurus is to Plesiosaurus, may have presented adalogous mudifications in the number and proportions of the cervical vertebre. It is hardly possible to contemplate the brond and short-suouted skull of the Simosaurus, wihh its proportiouably large teeth, without inferring that such a head must have been supported by a shorter and more powerful neck than that which bore the long and slender head of the Nothosaurus or Pistosaurus. The like inference is more strongly impressed upon the mind by the skull of the Placodus, still shorter and broader than that of Simosaurus, and with vastly larger teeeh, of a shape indicative of their adaptation to crushing molluseous or crustaceous shells. Neither the proportions and armature of the skull of Placodus, nor the mode of obtaining the food indicated by its cranial aud dental characters, permit the supposition that the head was supported by other than a comparatively short and strong neck. Yet the composition of the skull, its proportions, cavities and other light-giving auatomical characters, all bespeak the close essential relationship of Placodus to Simosaurus and nther so-called Macrotrachelian reptiles of the Muschelkalk beds. Prof. Owen continued, therefore, as in his Report of 1841, to regard he fin-like modification of the limbs as a better ordinal character than the number, of vertebre in nay particular reyoin of the spine. Yet this limb-character is subordinate to the characters derivod from the structure of the skull and of the teeth. If, therefore, the geueral term Enaliosauria may bo sometimes fouad convenient in its application to the natatory group of Snurian Reptilen, the essential distinctness of the orders Sauropterygii and Iehthyopterygii, typified by the Ichthyosaurus and Plesiosaurus respectively, should be borne in mind. The Plesiosaurus, with its very numerous cervical vertebre, sometimes thirty in number may be regarded as the type of the Sauropterygii, or pentedeotyle sea.lizaids. Oif all existing ruptiles, the lizards, and, amongst these, the Old World monitors, (Varanus, Fitz.), by reason of the cranial vacuitics in front of the orbits, most resemble the Plesiosaur in the structure of the skull; as in the division of the nostrils, the vacuitiesin the occipital region between the exoccipitals and tympa dics, the parietal foramen, the zygomatic extension of the post-frontal, the palatomaxillary, and pterygo-sphenoid vacuities in the bony palate; and all these are lacertian characters as contradistinguished from crocodilian ones. But the antorbital racuities, between the nasai, prefroutal, and maxillary bones, are the sole external nostrils in the Plesiosaurs. The zygomatic arch abuts against the fore pari oi the tympanic aud fixes it: a much greater extent of the roof of the mouth is ossified than in lizards, and the palato-maxillary and pterggo-sphenoid fissures are reduced to small size. The teeth, finally, are implanted in distinct sockets. That the Plesiosnur hed the "head of a lizard" is an emphatic mode of expressing the amount of resemblance in their cranial conformation. The crocodilian affinities, however, are not confined to the teetb, but are exemplified in some particulars of the strueture of the skull itself. In the simple mode of articulation of the ribs the lacertian affinity is again strongly manifested; but to this vertebral character such affiuity is limited. All the others exemplify the ordinal distinction of the Plesiosaurs from known existing reptiles. The shape of the joints of the centra; the number of vertebra between the head and tail, especially of those of the neck;
the slight iudication of the sacral vertebre; the non-confluence of the caudal hæmapophyses with onch other, are all "plesiosauroid." In the size and number of abdominal ribs and steruum may perhaps be discerned a frite step in that series of devel.pment of the hemapophyses of the trunk, which reaches its maximum in the plastron of the Chelonin. The counexion of the clavicle with the scapula is common to the Chelonia with the Plesiosauri; the expausion of the coracoidsoxtreme in Plesiosnuri-is greater in Chelomia than in Crocodilia; but is still greater in some Lacertia. The form and proportions of the pubis and ischium, as compared with the ilium, in the pelvic arch of the Plesiosauri, find their nearest approach in the pelvis of marive Chelonia; and no other existing reptile now offers so near, although it be so remote, a resemblance to the structure of the paddles of the Plesiosaur. Both Nothosaurus and Pistosaurus had many neck-vertebre, and the transition from these to the dorsal series was effected, as in Plesiosaurus, by the ascent of the rib-surface from the centrum to the ueurapophysis; but the surface, when divided betwee the two elements, projected further ou fards than in most Plesiosauri. In both Nothosaurus aud Pistosaurus the pelvic vertebra developes a combined process (par- and di-upophysis). but of relatively larger, vertically longer size, stauding well out, and from near the fore part of the side of the vertebra. This process with the coalesced riblet indicates a stronger ilium, and a firmer base of attachment of the hind limb to the trunk than in Plesiosaurus. Both this structure and the greater length of the bones of the fore-arm and leg show that the Muschelkalk predecessors of the liassic Plesiosauri were better organized for-oceasional progression on dry land. The Sauropterygii extend from the Trias to the chalk inclusive.

Order V.-Anomoilontia (aropos, lawless, oôous, tooth).-This order is representeà by three families, all the species of which are extinct, and appear to lenee been restricted to the triassic period. Teeth wanting, or confluent with tusk-shaped premaxillaries, or confined to a single pair in the upper jaw, which bave the form and proportions of eanine tusks. A foramen parietale and twe nostrils; tympanic pedicle fixed. Vertebra biconcave; pleurapophysis of the trunk long and curved the anterior oues with bifurcate heads; a sacrum of four or five vertebre forming with broad iliac and pubic bones, a large pelvis. Limbs ambulatory.- Family Dicynodoutia. A long ever growing tusk in each maxilhary bone; premaxillaries conuate, and forming with the lower jaw : beak-shaped mouth, probably shenthed with horn. This includes two genera-Dicynodon and Ptychognathus--all the known species of which are founded on fossils from rocks of probably triassic age in South Atrica:- Family Cryptodontia. Upper as well as lower jaw edeutulous. The genas Oudenodon closely conforms to the dicynodont type, and the species are from the same rocks and localities.-Family (inathodontia. Two curved tuskshaped bodies holding the place of the premixillaries, and consisting of confluent, dentinal and osseous substance, descending in front of the symphysis mandibula. These bodies are homologous with the pair of confluent premaxillary teeth and bones in the existing New Zealand amphiccelian lizard Rhynchocephalus; they are analogous to the tusks in the Dicynodonts, and must bave senved a similar purpose in the extinet reptiles of the New Red (Triss) Sandstone of Shropshire-(Rhynohosaurus), in which alone thie structure, with an otherwise edentulous.beak-shaped
mouth, has hitherto been met with. To this order belonge the Rynchosauroid, reptile, from the Elgin sandstone, with palatal teeth, called Hyperodapedou, by Prof. Huxley.

Order VI. Pterosauria.--Although some members of the preceding ()rder resombled birds in the shape or the edentulous state of the mouth, the reptiles of the present order make a closer approneh to the feahhered class in the texture and and pueumatic character of most of the bones, and in the modifcation of the pectoral limbs for the function of flight. This is due to the elongation of the antebrachial bones, and more eapecinlly to the still greater length of the metacarpal and phalaugial bones of the fifth or outermost digit, the last phalanx of which termiuates in a point. The other fingers were of more ordinary length and size, and were terminated by claws, the number of their phalanges progressively increasing to the fourth, which had four joints. The whole osseous system is modified in accordance with the possession of wings: the bones are light, hollow, most of them permeated by sir-cells, with thin, compact outer walls. The scapula and corowoid are long and narrow, but strong. The vertebre of the neck are few but large and strong,-for the support of a large head with long jaws, armed with sharp-pointed teeth. The skull was lightened by large vacuities, of which one was iuterposed between the nostril and the orbit. The vertebre of the back are small as are those of the sacrum, which were from two to five in number, but combined with a small pelvis and weak hind-limbs, bespeaking a creature unable to stand and walk like a bird; the body must have been dragged along the ground like that of a bat. The vertebral budies were united by ball-and-sucket joints, the cup being auterior, and in them we have the earliest manifestation of the "procolian" type of vertebra. The Pterosauria are distributed into genera accordug to modifica. tions of the jaws and teeth. In the oldest known species, from the lias, the teeth are of two kinds : a ferv, at the fore part of the jaws, are long, large, elarp-pointed, with a full elliptical base, in distinct and separated sockets; behind them is a close-set row of short, compressed, very small, laveet-shaped teeth. 'I hese form the genus Dimorphodon, Ow. In the genss Ramphorynchus, V. M., the fore parof each jaw is without teeth, and may have been incased by a horny beak; but behind the edentulous production there are four or five large and loug teeth followed by several smaller oues. The tail is long, stiff, and slender. In the genus Pterodactylus, Cuv., the jaws are provided with teeth to their extremities; all the teeth are long, slender, sharp-pointed, set well apart. The toil is very short. $P$. longirostris, Ok., about ten inches in length. From lithographic slute at Pappenheim, P. crassirostris. Goldf., about one font long, P. Sedgwickii, Ow., from the greensand, with an expanse of wing of twenty feet, exemplify the Prerodactyles proper. The oldest well-known Pterodactyle is the Dimorphodon macronyx of the lower lias; but bones of Pterodactyie have been discovered in coeval lias of Wirtemberg. The next in point of age is the Dimorphodon Banthensis, from the "Posidonomyed.Schiefer" of Banz in Bavaria, auswering to the alum shate of the Whitby lias. Then follows the P. Bucklardi, from the Stonesfield oolite. Above this come the first-defined and numerous species of Pterodactyle from the lithographic slates of the middle oolitic system in Germany, and from Curin on the Rhone. The Pterudactyles of the Wealden are, as yet, known to us by only a few

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bones and bone fragments. The largest known species are the $P$. Sedgwickii and $P$. Fittoni, from the upper greensand of Cambridgeshire. Finally, the Pterodactyles of the middle chalk of Kent, almost as remarkable for their great size constitute the last forms of flying reptile known in the history of the crust of this earth.

Order VII. Thecodontia.-Vertebral bodies biconcave: ribs of the trunk long and bent, the anterior ones with a bifurcate head : sacrum of three vertebre: limbs ambulatory, femur with a third trochanter. Teeth with the crown more or less compressed, pointed, with trenchant aud finely serrate margins: implanted in disn tirct sockets. This order is represented by the extinct genera Thecodontosaurus and Palæosaurus of Riley and Stutchbury, from probably triassic strata, near Bristol: by the Cladyodon of the New Red Saudstone of Warwickshire, with which, probably, the Belodon of the Keuper Sandstone of Wirtemberg is generically synonymous. The Bathyguathus, Leidy, from New Red Sandstone of Prince Edward's Island, North America, is probably, a member of the present order: which seems to have been the forerunner of the next.

Order VIII. Dinosauria.-Cervical and anterior dorsal vertebre, with par- and di-apophyses, articulating with bifurcate ribs: dorsal vertebre with a neural platform; sacral vertebre from four to six in number. Articular ends of the free vertebre, more or less flat; but in the cervical becoming convex in front and concave behind, in some species. Limbs ambulatory, strong, long and unguiculate. Femur with a third trochanter in some. The species of this order were of large bulk, and were eminently adapted for terrestrial life; some, e. g., Iguanodon and, proioably, Hylæosaurus, were more or less vegetable feeders; others, o. g., Megalosar, were carnivorous. The Dinosauria ranged, in time, from the lias (Scelidosaurus Ow., from Charmouth) to the upper greensand (Iguanodon). The Megaiosaurus occurs in the lower oolite to the Wealden inclusive. The latter formation is that in which the Dinosauria appear to have flourished in greatest numbers and of hugest dimensions.

Order IX. Crocodilia.-Teeth in a single row, implanted in distinct sockets, external nostril single and terminal or subterminal. Anterior trunk; vertebræ with par- and di-apophyses, and bifurcate ribs; sacral vertebræ two, each supporting its own netral arch. Skin protected by bony, usually pitted, plates.

Sub-Order Amphiccelia ( $\alpha \mu ф \iota$, both; коtлоs, hollow; the vertebræ being bollow ed at both ends).-Crocodiles, closely resembling in general form the long nnd slender-jawed kind of the Ganges, called Gavial, existed from the time of the deposition of the lower lias. The teeth of the liassic forms were similarly long slender, and sharp, adapted for the prehension of fishes, and their skeleton was modified for more efficient progress in water, by both the terminal vertebral sur faces being slightly concave, by the hind liml; being relatively larger and stronger, and by the orbits forming no prominent obstruction to progress ihrough water. From the nature of the deposits containing the remains of the so-modified crocodiles they were marine. The fossil crocodiie from the Whitby lias, described and figured in the Philosophical Transactions, $1768, \mathrm{p} .638$, is the type of the: 0 Amphicclian species. They have been grouped under tho following genecic heads:-Teleosaurus, Mystriosaurus, Macrospondylus, Massospondylus, Pelagosau-
rus, Acolodon, Suchosaurus, Goniopholis, Pœcilopleuron, Stagonolepis, (?) \&c.* Species of the above genera range from the lias to the chalk inclusive.
Sub-Order Opisthocolia (ottrAos, behind, kotлos, hollow: vertebra concave behind, convex in front). -The small group of Crocodilia, so-called, is an artificial one based upon more or less of the anterior trunk vertebre being united by ball and-socket joints, but having the ball in front, instead of, as in modern crocodiles, behind. Cuvier first pointed out this peculiarity $\dagger$ in a crocodilian from the Oxfordian beds at Harfleur and the Kimmeridgian at Havre. Prof. Owen had deseribed similar Opisthoccelian vertebra fron: the Great Dolite at Chipping Norton, from the Upper Lias of Whitby, and, but of much larger size, from the Wealden formations of Sussex and the Isle of Wight. These specimens probably belonged, as suggested by him in $1841, \ddagger$ to the fore part of the same vertebral column as the vertebre, flat at the fure part, and slightly hollow behind, on which he founded the genus Celivsaurus. The smaller Opisthococlina vertebre described by Cuvier have been referred by Von Meyer to a genus called Streptospondylus. In une species from the Wealden, dorsal vertebre, measuring eight inches across, are ouly fuur inches in length, and caudal vertebre nearly seven inches across are less than four inches in leagth. These characterize the species called Cetiosaurus brevis. Caudal vertebra, me:suriug seven inches deep and five and a half inches in length, from the Lawer Oulite at Chippiug Norton, and the Great Oolite at Enstone, represent the species called Cetiosaurus medius. Caudal vertebræ from the Portland Stone at Garsington, Oxfordshire, measuring seven inches nine lines across and seven inches in length, were referred by the author to the Cetiosaurus longus. The latter, he remalked, must have been the most gigantic of crocodiliaus.

Sub-Order Proclia ( (ppos, frout, kotдos, hollow: vertebre with the cup at the fore part and the ball behind). Crocodilians with cup-and-ball vertebre, like those of living species, first make their appearance in the greensand of N. America (Croc. basifissus aud C. basitruncatus, Ow.)\| In Europe their remains are first found in the tertiary strata. Such remains from the plastic clay of Meudon have been referred to Crocodilus isorhynchus, C. ceelorhyncus, C. Becquercli. In the ' Calcaire Grossier' of Argenton and Casteloaudry have been found the C. Rallinati, and C. Dodanii. In the coeval eocene London clay, at Sheppy Island, the entire skull and charaeteristic parts of the skeleton of C. toliapicus and C. champsoides occur. In the sonewhat later eocene beds at Bracklesham occur the remains of the Gavial-like (!. Dixoni. In the Hordle beds have been found the $C$.

[^18]Hastingsia, with short and broad jaws ; and also a true alligatur (C Hantoniensis). It is remarkable that furms of procolian Crocodilia, now geographically restricted, the gavial to Asia and the alligator to America, should have been associated with true crocodiles, and represented by species which lived, during vearly the same geological pariod, in rivers flowing over what now forms the south cuast of Eng land. Many species of proceelinn Crocodilia have been founded on fossils from miocene and pliocene tertiaries. One of these, of the gavial sub-genus ( $C$. crassidens), from the Sewalik tertiary, was of gigantic dimensions.

Order X. Lacertilia.-Vertebræ, in most, procelian, with a siugle transverse process on each side, and with single-headed ribs; sacral vertebre, not exceeding two. Small vertebre of this type have been found in the Wealden of Sussex. They are more abundant, and are associated with other and more characteristic parts of the species in the cretaceous strata. On such evidence have been based the Rhapiosaurus subulidens, the Coniasaurus crassidens, aud the Dolichosaurus longicollis. But the most remarkable and extreme modifications of the lacertian type, in che cretaceous period, is that manifested by the huge species of which a cranium, five feet long, was discovered in the upper chalk of St. Peter's Mount. near Maestricht, in 1780 . This species, under the name Mosasaurus, is well known by the descriptions of Cuvier. Allie. species have been found in the cretaceous strata of England and North America. The Letudou anceps of the Norfolk chalk was a nearly-allied marine Lacertian. The structure of the limbs is not yet wellunderstood; it may lead to a sub-ordinal separation of the Mosasauroids from the land lizards, most of which are represented by existing species, in which a close transition is manifested to the next order.

Order XI. Ophidia.-Vertebræ very numerous, proccelian, with a single transverse process on each side, no sacrum; no visible limbs. The earliest evidence, at present, of this order is given by the fossil vertebre of the large serpent (Palæophis, Ow.) from the London clay of Sheppy and Bracklesham. Remains of a poisonous serper ${ }^{2}$, apparently a Vipera, have been found in miocene deposits at Sansans, south of L'rance. Ophidiolites, from Gningen, have been referred to the genus Colubei.

Order XII. Chelonia.-The characters of this order, including the extremely and:peculiarly modified forms of torloises, terrapenes and tarries, are sufficiently well known. The chief modifications in oolitic Chelonia known to Prof. Owen were the additional pair of boaes, interposed between the hyosternals and hyposternals of the plastron, in the genus Pleurosternon from the Upper Oolite at Purbeck. It would be very hazardous to infer the existence of reptiles, with the characteristic structure of the restricted genus Testudo, from the foot-prints in the triassic sandstone of Dumfries-shire. But Prof. Owen concurred in the general conclusions based upon the admirable figures and descriptions in the splendid monograph by Sir Wm. Jardine, Bart., F.R.S., that some of those foot-prints most probably belonged to species of the Cheloniau order. As enormous species of true turtle (chelone grgas), the skull of which measurnd oue foot across the back part, had left its remains in the eocene clay at sheppy. The terrestrial type of the order had been exempliGed on a still more gigantic scale by the Colossochelys of the Sewalik tertiaries.

Order XIII. Batrachia.-Vertebræ biconcave (Siren), procelian (Rana), or opisthocœelian (Pipa) : pleurapophyses short, straight. Two occipital condyles and two vomerine bones, in most dentigerous: no seales or scutes. Larva with gills, in most deciduous. Representatives of existing fmmilies or genera of true Batrachia have been found fossil, chiefly in tertiary and post-tertiary strata. Indications of a perennibranchiate batrachian had recently been detected by Prof. Owen, in a collection of minute Purbeck fossils. Avourous genera (Palcoophrynus), allied to the toad, occurred in the Guiugen tertiaries, and here also the remains of the gigantic Salamander (Andrias Schewzeri) were discovered.

Summary of the above definel Orders.<br>Province-Vertebrata. Class-Hematocrya.<br>Sub-Class-Reptilia.<br>Orders.<br>I. Ganocephala. II. Labyrinthodontia.<br>III. Ichthyopterygia.<br>IV. Sauropterygia.<br>V. Anomodontia.<br>VI. Pterosauria<br>VII. Thecodontia.<br>VIII. Dinosauria. IX. Crocodilia.<br>X. Lacertilia.<br>XI. Ophidia.<br>XII. Chelonia.<br>XIII. Batrachia.

NOTES ON JAPAN. BY LAWRENOR OLIPTANT, F.R.G.S.
The following Notes are the results of personal observation during the recent mission of Lord Elgin to the Empire of Japan.

The three ports of the Empire visited by the mission, and which fell more immediately under our observation, were Nagasaki, situated in the Island of Kinsin; Simioda, a port opened by Commodore Perry on the Promontory of Idsa; aud Yeddo, the capital city of the Empire. Of these Nagasaki is the one with which we have been for the longest period familiar. In former times it was a fishing village situated in the Priucipality of Omura. It is now an imperial demesue, and the most flururishin port in the Empire. It owes its origin to the establishment, at this advantageous point, of a Portuguesa settlement in the year 1569 ; and its prosperity, to the enlighteved policy pursued by the Christian Prince of Omura, in whose territory it was situated. Its transference to the Orown property was the result of political intrigues on the part of the Portuguese settlers, in consequence of which the celcbrated Tageo Sama included it among the lands apper-
taining to the Crown. Situated almost at the westernmost extremity of the Empire, at the head of a deep land-locked harbour, and in convenient proximity to some of the wealthiest and most productive Principalities, Nagasaki possesses great local advantages, anc will doubtless continue an important commercial emporium, even when the trade of the Empire at large is more fully developed, and has found an outlet through other ports. The town is pleasantly situated on a belt of level ground which intervene between the water and the swelling hills. These, with their slopes terraced with rice fields; their wooded valleys and gushing streams; and their projecting points crowned with temples no frowning with batteries. form an ampaitheatre of great scenic beauty ; and the whele aspect of the place produces a most favourable impression on the mind of the stranger visiting Japan for the first time.

The Empire of Japan is stated, according to native authority, to consist of upwards of three thnusand islands. The majority of these, however, are uninhabited rocks. The principal island is known to the natives as Dai Nipon. The word Nipon is, doubtless, the origin of the term Japan, now applied to the whole gro ?. The Chinese have called Nipon, "Jipun, the Empire proceeding from the sun." Marco Polo calls it Jypanger, but all these words have clearly a common origin. Yesso, Kinsin, and Sikok complete the group of larger islands, which contain a territorial superficies, roughly estimated at 160,000 square miles. To these must be added the Japancse settlements in the neighbouring island of Tarakai, where the boundary which divides them from Russia, and marks the limit of that spreading Empire in this direction, remains yet undecided.

The city itself contains a population of about fifty thousand, and consists of between eighty and ninety streets, ruuning at right avgles to each other-broad enough to admit of the passage of wheeled vehicles, were any to be seen in them -and kept scrupulousiy clean. A canal intersects the city, spanned by thirty-five bridges, of which fifteen are handsomely constructed of stone. The Dutch factory is placed upon a small fan-shaped island about two hundred yards in length, and connected with the mainland by a bridge. Until recently, the members of the factory were confined exclusively to this limited area, and kept under a strict and rigid surveillance. The old regime is now however, rapidly passing away; and the his tory of their imprisonment, of the indignities to which they were exposed, and the insults they suffered, has already become a matter of tradition.

Kinsin, or "the Island of Nine," in which Nagasaki is situated, is so called because it is divided into nine provinces. It contains an area of about sixteen thousand miles, being in extent nearly equal to Sardinia. The provinces of whichit is composed are-Fizen, Tsikuzen, Tsikugo, Buzen, Bungo, Figo, Oosom, Fingo, and Satsuma. I have enumerated these by name, not so much for the purpose of information as to convey some idea of the words and names in the Japanese language. All these provinces are divided among many princes, who are vassals of the empire. The supremacy, however, in cach is generally vested in a single family. whose hereditary position among the aristocracy of the country confers upon it a recognized ascendancy.

Ir Kinsin, the most important of these Principalities, are Fizen and Satsuma. The largest city in the island, Saga, is the capital of Fizen and residence of its

Prince. Attached to this province there are no fewer than 1016 islands. One of these, Firando, is interesting to us, from the fact that, in the year 1613, an English factory was established there, which however, after a brief existence, failed, in consequence of a combiuation of adverse circumstances to which it is not necesary here to allude, more especially as we have no reason to anticipate that they will again ariso to nip in the bud the commerce that is rapidly growing in those regionsSimabarra is another port of this province possessing historical interest. Its siege forms a celebrated but melancholy episode in the history of Christianity in Japan. Thirty-five thousand Roman Catholic Christians, who had taken refuge within its waters were bombarded by the Dutch at the behest of the Japanese Goverument, and utterly exterminated.
In former days Nagasaki was comprised within the limits of Fisen, and even now the defence of the city, in time of war, devolves upon the prince. The revenue of this high dignitary is stated to amount to about $£ 360,000$ a-year. His territory is one of the most productive in the empire, which will account for this enormous revenue. Besidos rice, and various descriptions oi grain, it produces tea, tobacco, and cotton, with fruit of divers sorts. Among the most important of its producte, however, should be mentioned the vegetable tallow, ove cargo of which has already reached this country, and been disposed of at a large profit. Among its mineral productions are iron, sulphur, cinnabar, and marble. There is a coal mine at Wukumote which some of the Dutch Mission have descended. They describe the mine as being well and judiciously worked, and the coal as being bituminousinits nature, and made into coke for use. Old Kainipfer tells a story (by way of illustrating the volcanic nature of the country) of a coal mine in this province which, through the carelessness of the miners, teok fire, and has been burning ever since. The nearest coal mine is not more than seven miles from Nagasaki. Another very extensive one is situated in Tsekugen, about one hundred miles distant. A very excellent description of porcelain clay is also found here, and the Europenn demand for eggahell Chinu, which is sold in great quantities at Nagasaki, is chiefly supplied by the sabjects of the princes of Ligon and Satsuma. The ruler of Ligon is, so far as we could learn from our Dutch informants at Nagasaki, a man of tolerably advanced views, and favourably disposed towards foreigners. He has already adopted many of our wisest inventions, but has not succeeded in thoroughly divesting himself of old prejudices. This was illustrated a short time prior to our visit, by his refusal to allow the Dutch to enter his territory to put up a steam engine which he himself had ordered out from Europe, to pump water out of one of hig coalmines. But the Prince who has distinguished himself most notably by his progressive views is his Highuess of Satsuma. Unfortumately, since our return to this country, we have received intelligence of the death of this most enlightened nobleman. A man of the highest rank, of enormous wealth, of great malitical influence, the Prince of Satsuma was ever ready to advance the intereste of foreiguers, and to introduce into his own State their arts and inventions. I was informed by a Dutch gentlemen who had visited him that he bad established an electric telegraph between his castle and Hagosima, the chief city of his province, a distauce of about three miles. He has also extensive glass factories, and cannon foundries, in which 800 workmen are employed.

Some ider, may be formed of the scale upon which his establishment was conducted, from the fact that he possessed nine town houses in Yedo, and slways travelled to that city with an escort of several thousand men. He was nearly connected with the Royal Fanily, his daughter being married to the late Tycoon, or Temporal Emperor, whose demise took place about the period of our arrival at Yedo.

A former Prince of Satsuma, was the conqueror of the Leweher Islands. The Province of Satsuma contains great quantities of sulphur, which may form an mportant item in our trade with Japan. At its southern extremity is situated the Island of Loogasina, or Sulphur Island, which is said to burn incessantly. We did not pass within sight of it however. The mines of the island yield the Prince of Satsuma an annual revenue of 200 chests of silver.

The whole of the Istand of Kiusin is eminently volcanic, notwithstanding its general fertility and varied products. Parts of it are wild and barren; the aspect of its shores and general character of its mountains would betray its origin, even did not incessant volcanic action exist to put the matter beyond a doubt. There are uo less than five volcswoes active in this island-they are, Mitake, in the Province of Satsuma ; Kirisima Yamma, in Fingo; Asogammo, in Figo; Wunzler, in Fizen; and Tsurminyauma, in Bungo.

The most celebrated of these are the Iirisma Yamma and Wunzler, or the "High Mountain of Warm Spriags." Ifiva, on referring to the Chinese Repository, that in 1793 the summit of the mountain sunk entirely down; torrents of boiling water issued from all parts of the deep cavity which was thus formed, and the vapour arose like thi is smoke. In one of its eruptions, it is recorded to have destroyed the ill-fated city of Simabara, when 35,000 persons are said to have perished There are also many hot and sulphurous springs, which are used as baths, and accounted to have great medical qualities. To some of these, curious superstitions are attached. They are considered departments for punishment in the inferaal regions. To one which is covered at the top with a white crean like froth, are consigned pastry-cooks and confectioners who practised adulteration while in life; while deceitful brewers pass a miserable existence in a spring as thick and muddy as the beer and sakee they sold their customers. The Island of Kinsin is well watered; a hardy and industrious population inhabits its fertile valleys; its lofty mountain ranges contain scenes of great grandeur and sublinity, while its shores, indented with deep aud secure harbours and feathered with wood, owe much of their picturesque beauty to the numerous islands which stud those inland waters.

It is separated from the Island of Nipon by the narrow Straits of Vander Capellen or Simonerki, which connect the Straits of the Corea with the Purvonadei Sea. It was origiually the intention of Lord Elgin to have explored on his retnra voyage this most remarkable sheet of waler, never get traversed by foreign keel, and which must afford a most interestivg field for surveys of scieutific character, as also for general observation. Unfortunately, however, our time did not admit of his putting this design into execution. The South sea is thickly covered with islands, and was reported to us by the Japanese as navigable for ships of large drauglt. The lirge and important island of Sikok intervenes between it and the North Pacific Oceau with which this sea is counected, by the Straits of Bangon on
the west, and the narrow Channel of Kind on the east. Sikok is, as its name im. plies, divided•into four provinces ; as, however, we did not even sight its shores we had no opportunity of obtaining any information about it. It is about 150 miles long, with an average breadth of $70^{\circ}$ miles, and is computed to contain about 10,000 square miles.

With the Suwonda Sea, however we are more closely interested, for upon its margin is the Port of Hiogo, opened by the late treaty to the commerce of the west.

This port is situated in the Bay of Othosaka, opposite to the celebrated city of that name, from which it is ten or twelve miles distant. The Japanese Govern* ment have expended vast sums in their engineering efforts to improve its once dangerous anchorage. A break water, which was erected at a prodigious expense, and which cost the lives of numbers of workmen, has proved sufficient for the object for which it was designed. There is a tradition that a superstition existed in connection with this dyke, to the effect that it would never be finished, unless an individual could be found sufficieutly patriotic to suffe: himself to be buried in it. A Japannese Curtius was not long in fortheoming, to whom a debt of gratitude will be due in all time to come, from every British ship that rides securely at her anchor behind the breakwater.

Hiogo has now become the port of Ghosaken and Miaci, and will in all probability, be the principal port of European trade in the empire. Tle city is described as equal in size to Nagasaki. When Kainipfer visited it, he found 300 junks at anchor in its bay.

The Dutch describe Ohosaka as a more attractive resort even than Yedo. While this latter city may be regarded as the Loudou of Japan, Ohosaka seems to be its Paris. Here are the most oelebrated theatres, the most sumptuous teahouses, the most extensive pleasure-gardens. It is the abode of luxury and wealth, the farourite resort of fashionable Japanese, who come here to spend their time in gaiety and pleasure. Ohosaka is one of the five Imperial cities, and contains a vast population. It is situated on the left bank of the Jedogawa, a stream which rises in the Lake of Oity, situated a day and a-half's journey in the intesior. It is navigable for boats of large tonnage as far as Miaco, and is spanned by numerous handsome bridges.

The port of Eiago and the city of Osaca will not be opened to Europeans until the lst of January, 1863. The foreign residents will then be allowed to explore the country in any direction, for a distauce of twenty-five miles, except towards Miaco, or, as it is more properly called, Kioto. They will not be allowed to approach nearer than twenty-five miles to this far famed city.

As the Dutch have constantly been in the babit of passing through Kioto, it is probable thal before very long this restriction will be removed, and Europeans will be permitted to visit, what is, without question, the most interesting spot in the Empire. If Yedo is the London, and Othosaka the Paris, Kioto is certainly the Rome of Japan. It is here that the spiritua! Emperor resides, and that enormous ecclesiastical Court by which he is surrounded, and which is called the Dairic, is permanently fixed. It is here that the celebrated tomb of the Great Sayco Sena, the most fanous of Japanese temporal Emperors is situnted; and here are
to be seen the most magnificient and imposing temples of which the Empire can boast. The population of Kioto is said to be half a million, and it has had the reputation of being the principal manufacturing town in the Empire. It is situated as nearly as possible in the centre of Dai Nipon, the largest and most important island in the Japanese group, and which now demands a brief descriptive notice. Accordiug to Kainipfer, its length measured along the middle of the island exceeds 900 miles, and its average widh may be estimated at more than 100 miles-its surface may, therefore cover an area of about 100,000 square miles. It is traversed in its whole length by a chain almost of uniform elevation, and in many places. crowned with peaks covered with perpetual snow. This chain divides the streams which flow to the south and east, and which fall into the Pacific Ocean, from those which pursue a northerly course to the sea of Japan. Very many of its peaks are volcanic-among the most important of these is the Fusyanuner, the highest mountain in Japan. Its elevation is estimated at about 11,000 feet above the sealevel. It has been quiescent for upwards of a century ; its summit was sheathed with snow when we saw it at midsummer. The volcauoe of Pries, situated on an island under which we passed, was in action. Nipon is divided into upwards of 50 separate provinces, and contains the capital city of the Empire: Yedo. The first point in it at which we touched was the port of Simoda, situated on the promontory of Idsu, and opened to foreign trade by Commodore Perry in 1852.

As this port is under the new treaty to be closed to foreigners, it is scarcely necessary to allude to it. At no time favourably situated for trade, and under all circumstances a dangerous harbour, the anchorage was totally destroyed by an earthquake, which took place in December, 1854. Placed at the extreme end of a mountainous promontory, to pass from which into the interior of the island it is necessary to cross a mountain range 6000 feet high, and inhabited by a poor population of fishermen, Simoda cam never offer attractions to the merchant, or give us cause to regret that it is no longer available for commercial purposes. The promontory of Idsu forms the eastern shore of the Bay of Yedo. The distance from Simoda to that city is about eighty miles. At Uraga the opposite shores. approach to within ten miles of each other, and the straits which are thus formed afford scenery of much picturesque beauty. Eighteen miles from Yedo, and situated in a curvature of the western shore, lies the new port of Kanagawa, affording secure anchorage within half.a-mile of the land. Connected with Yedo by an excellent road, practicable for wheeled vehicles, and containing a considerable population already, Kanagawa possesses many adrautages as a focus of trade. As, horvever, we did not land here, I do not venture to describe it further, the more especially as it has now beeu open to Europeans for upwards of two months, and we shall doubtless ere long have a full account of it from some of the pioneers of commercial enterprise who have already gone to establish themselves there. Foreigners are permitted by treaty to go into the interior for a distance of tweaty-five miles, except toward Yedo. The Logos river, distant about ten miles from this city, is their limit in that direction.
Fortunately, no such restriction applied to us, and we were enabled, during a residence of ten drys in that most interesting capital, to acquire some informa-
tion with reference to the manners and customs of the singular race who inhabit it, of their mode of government, and of the resources of the country generally.

Situated at the head of a bay, or rather gulf, so extensive that the opposite shores are not visible to each other,' Yedo spreads itself in a continuous line of houses along its partially undulating, partially level margin, foi a distance of about ten miles. Including suburbs, at its greatest width it is probably about seven miles across, but for a portion of the distance it narrows to a mere strip of houses. Any rough calculation of the population of $s 0$ vast a city must necessarilly be very vague and uncertrin ; but, after some experience of Chinese cities, two millions does not seem too high an estimate at which to place Yedo.

In consequence of the great extent of the aren occupied by the residences of the Princes, there are quarters of the town in which the inhabitants are very scarce. The citadel, or residence of the temporal Emperor, connot be less than five or six miles in circumference, and yet it only contains about 40,000 souls. On the cther hand, there are parts of the city in which the inhabitants seem almost as closely packed as they are in Chinese towns.

The streets are broad and admirably drained, some of them are lined with peach and plum trees, and when these are in blossom must present a gay and lively appearance. These which iraverse the Prince's quarter are for the most part as quiet and deserted as aristocratic thoroughfares generally are. Those which pass through the commercial and manufacturing quarters are densely crowded with passengers on font, in chairs, and on horseback, while occasionally but not often, an ox waggon rumbles and creaks along. The houses are only of two stories, sometimes built of freestone, sometimes of sunburnt brick, and sometimes of wood; the roofs are either tiles or shingles. The shops are completely open to the street; some of them are very extensive, the show rooms for the more expensive fabrics being up stairs as with us. The eastern part of the city is built upon a level plain, watered by the Toda Gawa, which flows.through this section of the town, and supplies with water the large moats which surround the citadel. It is spanned by the Nipon; has a wooden bridge of enormious length, celebrated as the Hyde Park Corner of Japan, as from it all distances throughout the empire are measured. Towards the western quarter of the city the country becomes. more broken, swelling hills rise above the housetops, richly clothed with foliage, from out the waving masses of which appear the upturned gables of a temple, or the many roofs of a Pagoda.

It will be some satisfaction to foreigners to know that they are not to:be excluded for ever from this most interesting city, By the treaty concluded in it by Lord Elgin, on the first of Japuary, 1862, British subjects will be allowed to. reside there, and it is not improbable that a great portion of the trade may be transferred to it from Kanagawa. There is plenty of water and a good anchorage at a distance of about a mile and a half from the western suburb of Linagawa.

The only other port which has been opened by the late Treaty in the Island of Nipon is the Port of Nee-e-gata, situated upon its western const. As this port bas never get been visited by Europeans, it is stipulated that if it be found
inconvenient as a harbour, another shall be substituted for it, to be opene? on tho first of January, 1860.
It will thus be seen that we have one port in Kinsin, Nagasaki; three in Nipon, Hiogo, Kavagawa, and Nee.e.gata. In the remaining large Island of the Jupanese group-viz., Yessa, we bave secured Hakodadi. It was opened to foreign trade on the 1st of last July. Our ships of war have recently visited Hakodadi frequently. It is described as a beautiful spot, situated in a country resembling Englaud in its clinate, productions, and natural features.
The limits of this paper will not, unfortunately, admit of my adverting, at any length, to the singular political aud social institutions of this most remarkable people-otherwise, it might have becu iateresting to have described the spiritual Emperor passlng a sub-celestial existence at Miaco, reminded only of his humanity by twelve wives, who are not spiritual; and the temporal Emperor, confined within the massive walls of his handsome palace, little better than a State prisoner. We cannot now speculate upon the power aud influence wielded by the Council of State, composed of flve feudal nobles; or discuss the share which an ancient and powerful aristociacy possess in the administration of public affairs. Tinat most striking feature in the social government of Japan, which consists of an elaborate systen of espionage, exorcised alike upon prince and beggar, and retaining all within the thraldrom of its iron grasp, would be a fertile theme for a paper in iiself; while the celebrated Hara Kiri, or happy despatch, already so familiar to all, that it is scarcely necessary to allude to it as the resource alike of the unsuccessful politician, the detected criminal, aud the injured member of society. It may not, however, be so well known that the old practice of ripping open the abdomen has been extinguished in farour of a less disgusting method of immolation, by which the duty of terminating the existence of the victio falls not upon. himself but upon his friend, who decapitates him in the presence of his family and relations.

Still less can we now venture upon a discussion of the various creeds which obtain in Japan, of the old uational roligions of the Empire, known as the Sinsyn religion or faith of the gods, or of the e:ient to. which it has become modified by those more recently introduced dogmas of Bhuddism (now a faith widely diffused throughout the Empire, ) or of the influence exercised upon both by the more Confucian tenets practised by those who follow Suitoo, or the way of the philosophers.

Having, thus enumerated and briefly discussed, so far as our limited information will admit, the five ports of Japan recently opened by treaty to the commerce and enterprise of the West, it may not be uninteresting to glance at the probable nature and extent of that commerce. which is likely to spring up at them.

From the little we know of the internal resources of Japan, jutis: probable that we shall find a more profitable source of trade in its mineral than its vegetable productions. Unless we have been totally misinformed, these former are of vast extent and great value.

We know that the principal profits of the early Portuguese settlers were derived from the export of gold and silver. So lucrative"twas it that Kainipfer remarks--"It is believed that, had the. Portuguese enjoyed the trado of Sapan: but twenty years longer, upon the same footing as thes did for some time, much riches
would have been transported out of this Ophir to Macao, and there would have beeu such a plenty and flow of gold and silver in that town, as sacred writ mentions there was at Jerusalem in ine time of Solomon, At a later period, the Dutch carried on this same traffic to so great an extent that a native political economist, writiug in 1708 on the subject, computes the annual exportation of gold at about 150,000 cobaugs, so that in ten years the empire was drained of 1,500,000 cobaugs, or about two millions and a half sterling.

The gold is found in various localities. That procured from Sado has the reputation of being the fiuest, and it is stated that the ore will yield from one to two oz. of fine metal per li l lb. The copper mines in Garonga are stated to be very rich, the copper ore raised also being impregnated with gold. The ore from Satsuma yields from 4 to 6 oz . per $\mathrm{l} \frac{\mathrm{l}}{\mathrm{l}} \mathrm{lb}$. These are the principal mines. Gold dust is found in some of the streams. Copper is superabundant, as is evident from the lavish use made of it for ornamental purposes.

For a long period the Dutch received at Nagasaki (in exchange for their merchandize) Japan copper. This however, as well as the sale of gold, has been stopped for many years. The Government allows no more copper to be produced now than is absolutely necessary for home cionsumption, which is comparatively very small. It will be for us to develope more fully one of the most important elements in the wealth of this vast empire.

By the treaty recenily concluded, gold and silver coins may be exported from Japan, but not as cargo; the exportation of copper coin, as well as copper in bars, is prohibited, but she government engages to sell from time to tinie at public auction, any surplus quantity of copper that may be produced.

Iron abounds in various parts of Japan. The mines of iron are extensively worked, much more so at present than those of copper. Judging from articles of casting of their own construction, the ores must be of excellent quanlity. Specimens of wrought iron, cast and blister steel, have been examined with very satisfactory results. The wrought iron is usually hammered, and in smalletiat bars varying from 12 to 80 lbs . each. This is probably to be attributed to a want of proper rachinery for heavier bars, and its being suited to their purposes. The steel of which the swords were composed which we procured at Yedo, was of admirable temper and quality.

I have already alluded to the coal mines which exist in the Island of Kinsiuone of them is distant only seven miles from Nagasaki. They are a Government monopoly. Hitherto the coal brought for sale since the opening of trade at Nagasaki has been surface eoal, and consequently inferior in quality; it is described as small. It burns slaty, leaving considerable ash, and is very light. There can be little doubt that good coalis to be found in the island, when the minea begin to be properly worked. By the treaty of Yedo, coals, zinc, lead, and tin, are to be exported, at a duty of five per cent.

The vegetable productions of Japan, which are most probably destined to become articles of commerce, are camphor, vegetable tallow, rice, what, drugs, seaweed, \&c. Among manufactured articles we may mention lacquer ware and porselain, but it is almost impossible at this early stage of our commercial relations to predict either their character or extent. Immediately on our return
from Japan, some merchant ships went out to Nagasaki-not altogether strictly in accordance with international law-to open trade at that port. Since November last we have an actual experience to refer to ; but we must beware of drawing conclusions rashly from it. That the result has not equalled the anticipations formed at the commencement is due to the fact that trade has not been carried on under -ie provisions of the treaty concluded at Yeddo, but undor that now obsolete system formerly pursued by the Ducch, in which the foreigu merchant was compelled to deal with and through Government alone. The consequence was, that after the first few Government contracts were completed, the trade could only be carried on under those restrictions and disadvantages which have readered it so little profitable to the Dutch throughout this long course of yeare. Now, however that those restrictions are re.aved, and a currency established, which will once more enable merchants to enter upon extensive commercial transactions under favorable conditions, instead of confining them to a paltry-barter trade, carried out under Government' regulations, I have no doubt that we shall receive very different accounts of our mercantile prospects in this quarter. When we hear that between November, 185̄S, and March, 1859, no less than 15,000 tons of British and American shipping have lett Shanghae for Nagasaki, a port the annual trude of which had been carried on by two Dutch ships, and that upwards of 11,000 tons bave returned thence, many of the vessels being announced to go back again, we are driven to suppose either that the British merchant is more than usually blind to his own interest, or that there really is a trade worth engaging in. About fourteein hundred bales of silk in all have been procured and exported at Nagasaki, since the trade began last November. It is expected that the supply of this article will increase materially, the climate being suitable for the growth of the mulberry, and the hahits of the people well adapted to the manipulation of silk.
Among the imports into Japan, produce from the Straits and China naturally forms a large proportion. This is for the most part conposed of drugs and what is technically termed Chow-chow eargo-viz., spices and condiments of various sorts; also Sandal aud Sapan wood. We have contributed damasks, cottons, muslins, velvets, woollens, \&c; while American piece goods have found a ready market. As yet, however, our merchants are only feeling their way, and some time must elapse before it will be possible for us to predict with any certainty either the nature or extent of that trade which is capable of being created in this most interesting quarter of the globe. Meantime, a heavy responsibility will rest alike upon the merchants engaged in developing commerial relations in this country, and on our own official agents employed in supporting them nad at the same time in protecting the Government to which they are accredited in due exercise of their treaty rights.

We are ignorant of the political considerations which induced the Japinese Gorernment to relinquish that syslem of exclusiveness which had for many years distinguished it among the natious of the East. We do know, however, that this result was not arrived at without much angry discussion and violent opposition on the part of some of the most influential members of the aristocracy; and we can have little douht that a strong feeling adverse to intercourse with foreigners
or the estallishment of commercial relations with them, exists throughout a large important class in Japan.

At present, this party is in the minority, but whether it will remain so or not, must depend upon the skill and tact with which our political relations are conducted, and upon the impression which the foreign mereantiic community will create upon the people generally. Of a haughty and independent spirit, the Japanese are also suspicious and vindictive, and it is possible that, unacustomed to contact with Europenus, they may grow restive under the amnoyances and evils which follow in the wake of civilization, and manifest a temper calculated to irritate the nation with which they have so recently entered into a friendly compact. It will be at this juncture that we shall be called upon to exercise that forbearance and moderation which it is ever becoming in the strong to display towards the weak
It would be well to remember that while we have achieved a great result in thus opening to the world this prosperous and happy community, we have aleo incurred serious obligations towards them, and are bound not to take advantage of their ignorance and inexperience in their dealings with western nations. We can only hope to commend our civilization to them by maintaining a high moral standard, both in our commercial and political intercourse. They are sufficiently enlightened to appreciate a policy inflienced by higher considerations than those involved in the accumulation of wealth. Unless we follow such a policy, it is not too much to predict that we shall lose alike their confidence and respect, and involve ourselves in complications disastrous to our commerce, and discreditable to our national character. Of all the nations of the enst, the Japanese are the most susceptible to civilizing influences, and I quote the words of an eminent Chinese and Japanese scholar in saying that, in one respect, they are far in advance of their ancient neighbours the Chinese, in that their attention is directed to obtain a knowledge of other pations. Their owa efforts in this way will form their greatest security. Their soldiers once formed the bolyguard of the King of Siam, their Cousuls once examined Spanish ships in Acapulco, their sailors once took a Dutch Governor out of his house in Formosa, and carried him prisoner to their rulers, their princes once sent an embassy to the Pupe, their Emperor once defied the vengeance of Portugal, by executing her Ambassadors. The knowledge of these historical events remains among them. We may reasomably hope for a great preponderance of good results from an extension of an intercourse which has recommenced peacefully. Let us indulge in the expectation that the land of the rising sun may not only soon be fitted to take her place among nations, but also among Christian nations, with all the institutions, and liberty, and purity, of the best of these.

## ERRATUM.

Vol. IV., page 442, line 10, for ${ }^{6}$ procis," read "proboscis."

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## REMARIKS ON TORONTO METEOROLOGICAL REGISTER FOR SEPTEJBER．

 30th．Ground Fog at 6 a．m．Ifeavy dew recorded on 9 mornings during the month． from 1848 to 1850 inclusive，were respectively iv $59^{\circ} \mathrm{W}$ ，and 0.99 miles． Mrean Temperature was $2^{\circ} .80$ below the average of 20 years，being the coldest sep－ tember save tTo（ 1810 and 181S）during that period．Tho depth of rain recorded was 0.57 .4 inches on the surface less than the average of 19 years，ard the nean
velocity of the wind 0.05 miles per hour above the average of 12 years．

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Resultant direction $\mathrm{N} .41^{\circ} \mathrm{W}$ ．Resultant Velosity 1.60 miles per hour．
 nost windy day．．．．．．．．．．．．．．．．．．．．．．．．．．．13th．．．．Ican velocity 18.00 miles per hour．
DIost windy hour．．．．．．noon to i p．in．．．．．．．．．．．．．Jrean velocity 9.36 dilto．$\}$ Diference ．．．．．．．Brean velocity 4.15 ditto．$\} 5.21$ miles．
$\infty$

comparative rable for october.

$$
=\text { osun: }
$$

Suowing on \& davs; depth inappreciable: duration of fall 4.0 hours.

cloudy hour observed, niidnight, mean $=0.48$.
Sums of the components of the Atmospheric Current, c.ipressed in Niles.
Wauth.
Nast.
South
1072.30

laximum velocity - 35.2 miles per hour, from 11 a.m. to noon on 18 th.


7th. Solar Halo durmg tho forenoon-
15th. Sigh Ran and rain w. to $830 \mathrm{p} . \mathrm{m}$.

$$
\left.\begin{array}{l}
6040 \\
27087
\end{array}\right\} \text { Difference }=32963 .
$$

18th. Slicet Lightning in Ni W. 8.50 the s.at of temperature from 6 a. m.
19th. First Snow of the sasson, from 10 p . m . Depth inappreciable
 Range in 14 hours $=32^{\circ} 0$.
Fo on th, 13 th, at $G$ a.m. Heary Dew on 2 nd and 11 th at $G a . m$.
Hoar Frost recorded on 6 mornings. Thin Ice registered on 10 mornings.

## 101



HONTILY METEOROLOGIOAL REGISTER, ST, HARTIN, ISLE JESUS, OANADA EASTMAUGUST; 1859. (NINE MILES west of HoNTREAL.)

Latitude-45 deg. 32 min . North. Lonyitule-73 deg. 30 min . West. Height above the Level of the Sea- 118 fcet.

| Barom. corrected and reduced to $32^{\circ}$ |  |  |  | Temp. of tho Air. |  |  | Tension of Vapor. |  |  | Humidity of Air. |  |  | Dircetion of Wind. |  |  | Velocity in miles per hour. |  |  |  |  | WEATHER, \&ic. <br> A clondy sky is represented by 10 ; A cloudless sky by $B$. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | P.35. |  | 2 P. 3. | 10p.as. | $\underset{8}{6}$ | p.35. |  | d 3 | M. |  |  |  | 10 P.M. | ${ }_{4.3}^{\text {a }}$ | ${ }^{2} \mathrm{ar}$. | P. 10. |  |  | 6 4.35, | 2 F .35. | 10 P. 3 I. |
|  | 20.660 | 29.69 | 20.48 | 40.8 | 65 |  | 260 | . 319 | . 376 | . 75 | . 47 | . 57 | 8 | I |  |  |  |  |  |  |  | Cu. Str. 4. |  |
|  | 347 | 43.1 | 68 | 50.1 | 50.6 | 52.3 | 335 | 312 | 323 | 93 | 78 | 83 | V S W | W N | W 5 | 4.0 | 15.13 | 14.95 | 0.1 |  |  |  |  |
|  | S | 667 | 22 | 50.0 | 87.0 | 52.9 | 309 | 350 | 361 | 85 | 75 | 93 | SW | $s$ b | SE | E. 41 | 1.96 | 3.64 | 0.301 |  | C. Cum, f |  | Rain. |
|  | 058 | 7 | 870 | 50.4 | 60.9 | 51.2 | 300 | 328 | 296 | 85 | 61 | 79 | w S W | w bs | vs w | 8.01 | 12.21 | 10.05 | 0.800 |  | Cl | C. | Cl |
|  | 837 | 009 | 937 | 50.6 | 61.0 | 53.0 | 328 | 310 | 348 | 89 | 60 | 86 | S y | W | WS | 363 | 2.08 | 4.17 | Inap |  | Str | cu: | Clear |
|  | 30.050 | 30.086 | 30.113 | 60.8 | 63.2 | 49.1 | 2 G 5 | 255 | 297 | 75 | 53 | 83 | $\stackrel{\mathrm{N}}{\mathrm{S}} \mathrm{W}$ | N NT | 8 w b i | 0.61 | 6.26 | 4.53 |  | $\ldots$ |  | O. O. Str. 0. | Do. |
|  | 051 | 000 | 077 | 45.7 | 65.0 | 54.6 | 211 | 296 | 335 | 72 | 45 | 80 | S S W if W | WS W SSw | SW bw | 0.21 0.00 | 4.00 | 1.75 2.15 | $\ldots$ |  | $\mathbf{S t}$ | Cu. Str. 4. <br> Clear. | Cir. Cum. 4. Clear. |
|  | 072 | 067 | 00 | 47. | 60.4 | 54.0 | 201 | 529 | 33 | 89 | 75 | S0 | WSW | SSW | S S W | 0.00 6.07 | 1.31 | 2.5 |  |  | St | clear. | Clear |
| 10 | 29.922 | 20.821 | 20.754 | 52.8 | 61.5 | 61.2 | 351 | 498 | 580 | 90 | 91 | 97 | B | S 5 | S | 0. | 0.5 |  | 0.330 |  | C. Stri 8. | Ra | Ra |
|  | 546 | 28 | 358 | 6.4 | 64.6 | 61.3 | 590 | 529 | 478 | 97 | 89 | 85 | ${ }^{\mathrm{H}}$ | $\boldsymbol{\sim} \mathrm{E}$ | S | 1.2 | 8.57 | 3. | 3.89 |  | Rain and |  | Cl |
|  | 31.4 | 128 | 167 | 60.3 | 7.4.1 | , | 499 | 563 | 453 | 00 | 07 | S0 | 8 | S W | 5 w | 3.30 | 2.80 | 7. |  |  | Cu. Str. 0. | C. | Cu |
| 13 | 14 | 262 | 310 | 60.8 | 69.0 | 0.1 | 303 | 239 | 262 | 76 | 57 |  | W | W | IF | 110 | 0.1 | 19.2 |  |  | Do. | Cu |  |
| 4 | 267 | 50 t | 850 | . 5 | 47.8 | 38.1 | 180 | 150 | 186 | 7 | 4 | 8 | W | w v w | \% | 11. | 19.13 | 17.01 | . 773 |  | . | Do. | ar |
| 15 | 30.083 | 30.107 | 30,151 | 37.2 | 50.0 | 33.4 | 178 | 130 | $10{ }^{\circ}$ | 81 | 39 | 72 | F Niv | wbs | 8 w | 21.86 | 14.15 | 3.70 |  |  | car Frost |  |  |
| 16 | 1201 | 061 | 20.993 | 34.2 | 61.3 | 4f 6 | 142 | 249 | 241 | 75 | 47 | 81 | S E | ESE | ESE | 0.01 | 0.78 | 0. |  |  |  |  |  |
| 17 | 29.856 | 20.730 | 834 | 42.0 | 53.2 | $\underline{62.2}$ | 223 | 387 | 361 | 87 | 80 | 93 | ${ }_{\text {E }}$ | EbN | NSbs | 0.40 | 1.30 | 4.33 |  |  | Cu. Str | Cu | Cu. Str. 10. |
| 18 | 810 | 862 | 815 | 4 S .0 | 75.7 | 50.4 | 303 | 574 | 290 | 80 | 70 | 82 | V |  | - | 1.92 | 0.07 | 0 |  |  | Do. |  | Cl. Ft.Au.Bo. |
| 19 | 010 | 02 | 6 | 40. | 77.0 | 61.7 | 2 | 539 | 412 | 72 | 50 | 83 | E | Sbe | SEbs |  | 0.17 | 0.15 |  |  | Clar. |  | Cu. Str. 9. <br> Clear Aur Bo. |
|  | 032 | 81.4 | 873 | 55. | 62.4 | 46.3 | 405 | d2 | 23 S | 91 | 77 | 73 | ${ }_{\sim}^{N}$ | vib |  | 2. 87 | . |  | 0.930 0.771 |  | $\begin{aligned} & \text { Rait } \\ & \text { Do. } \end{aligned}$ | Cu. Str. 10. Rain. | Clear. Aur.Bo. Siight raili. |
|  | 30.008 | 013 8511 811 | 936 837 | 43.0 | . 0 | 43.0 53.6 | 294 | 201 | 31 | 0 | 06 | 90 | ¢ NE HEb |  | NEbE NEbE | 17.87 15.76 | 2.26 | 17.18 9.18 | 0.771 1.409 |  | C. Str. | $\frac{\mathrm{Ra}}{\mathrm{D}}$ | Sight raill. <br> C. Str. 10. |
|  | $20.0 \pm 0$ | 851 | 837 | 30.2 50.0 | 51.3 55.2 |  | $22 \pm$ | 3 | 3307 | 09 | 90 | 95 | NEDE | NE | NEbE | 15.76 | 7.65 | 4.18 | 1.409 1.970 |  | C. Str | Do | $\begin{aligned} & \text { C. Str. } \\ & \text { Do. } \\ & 10 . \\ & \hline \end{aligned}$ |
| 2 | 531 | S 60 | 791 | 50.9 | 63.2 | 05.2 | $3!5$ | 420 | 383 | 92 | 77 | , | $\mathrm{Ni}^{\text {a }}$ | NE | त Ebe | 0.2 | 0.4 | . 20 | - |  | Cu. Str. 9 | Cu. Str. 6 | Cll. Str. 10. |
| 2 | 370 | 86.4 | 86 | 53.0 | 62.3 | 59.6 | 3j1 | 436 | 462 | 90 | 80 | 90 | ESE | ESE | Ss w | 0.36 | 3.16 | 0.01 |  |  | Do. 10. | Do. | Do. 10. |
| 26 | 7311 | 810 | 702 | 56.0 | 71.1 | 1.5 | 41 | 54 | 498 | 90 | 73 | 91 | gs w | 8 H | S 5 | 0. | 0.50 | 0.09 |  |  |  | Do. 4. | Do. 8. |
| 27 | 711 | 740 | $76{ }^{\circ}$ | 57.8 | 63.2 | - | 436 | 0.13 | 535 | 90 | 73 | 92 | SSY | Siv | \% | 0.30 | 2.4 | 1.83 | Inap |  |  | Do. 8. | Do. 10. |
| 2 | 87. | 972 | 30.021 | 0.7 | 56.2 | 50.8 | 336 | 357 | 233 | 75 | 78 | 78 | NEbE | \% ME | N b | 8.80 | 0.12 | 4.04 | Inap |  |  | Do. 9. | 0. |
| 20 | 30.170 | 30.160 | 201 | 42.7 | 63.0 | 43.2 | 2301 | 311 | 218 | 8 | 5 | 83 | be |  | EsE | 1.95 | 4.67 | 0.09 |  |  |  | Cirr. 2. | CL. Ft. Au. Bo. |
| 0 | 170 | 003 | 320.015 | 40.3 | 70.0 | 53. | 23 | 42 | 319 | 91 | 50 |  | EbN | SE | 88 E | 0.67 | 1. | 2. |  |  | Cu, Str. 4. | Clear. | Clear. |

## REMIARKS ON THE ST. MARTLN, ISLE JESUS, METEOROLOGICAL REGISTER FOR AUGUST, 1859.


REMARKS ON THE ST. MARTIN, ISLE JESUS, METEOROLOGICAL REGISTER FOR SFPTEMEBER, 1859.
Highest, the 29th day ..... 30.201
Lomest, the $12 t 11$ day ..... 29.138 Monthly Mrean ..... 29.771
Monthly Range. ..... 1.063
Highest, the 9 th day ..... 7804
Lowest. the 16th day ..... $29^{\circ} 2$  Monthiy Range ..... $49^{\circ} 9$
Greatest intensity op the Sun's Rays ..... $101^{\circ} 6$
Lowest point of Teriestrial Radiation. ..... $15^{02}$
Mrean of Humidity ..... 739
Amount of evaporation ..... 1.42 inches
Rain fell on 14 days, amounting to 11.810 inches; it was raining 112 hours 17 minutes, and was accompanied by thunder on 1 day.
Most prevalent wind, N. E.b E.
Least prevalent wind, N.
Most windy day, the 1.1th day; mean miles per hour, 16.04.
Icast windy day, the 19th day; mean mi!es per hour, 0.10.
Aurora Borealis visible on 5 nights.
The electrical state of the atmosphere has indicated rather feeble intensity. Uzone was present in rather large quantity.

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## REMARKS ON THE ST. MARTIN, ISLE JESUS, METEOROLOGICAL REGISTER FOR OCTOBER, 1859.

Highest, the 12th day 30.160<br>Barometer ...... \(\left\{\begin{array}{l}Lowest, the 27th day ............................................................................ 29.251<br>Sionth\end{array}\right.\) M Monthly Mean ............................................................................... 20.779<br>(Monthly Range........................................................................................................................ 0.4 0. 90.4<br>(Highest, the 5th day.<br>..... $83^{\circ} 1$<br>Thermomoter<br>Lowest, the 25th day<br>..... $19^{\circ} 4$<br><br>Greatest Intensity of the Sun's Rays<br>..... $105^{\circ} 8$<br>Lowest point of Terrestrial Radiation<br>..... $14^{\circ} 2$<br>Meau of Humidity<br>..... 754<br>Amount of evaporation<br>..... 1.27<br>Rain fell on 6 days, amounting to 1.629 inches; it was raining 20 hours and 15 minutes, andwas accompanied by thunder on 1 day.<br>Snow fell on 3 days, amountiug to 230 inches; it was snowing 24 hours.<br>First snow of the season fell on the 20 th day.<br>Most provalent wind, the W. N. W.<br>Least prevalent wind, E.<br>Most windy day, the 19th day; mean miles per hour, 21.81 .<br>Least winds day, the 17th day; mean miles per hour, 0.29 .<br>Aurora Borealis visible on 4 nights.<br>Lunar Haloes visible on 2 nights.<br>The electrical state of the atmosphere has indicated high andjconstant tension.<br>Ozone was present in moderate quantity.
REMARKS ON THE ST. MARTIN, ISLE JESUS, METEOROLOGICAL REGISTER FOR NOVEMBER, 1859.
Barometer ...... $\left\{\begin{array}{l}\text { Lnurest, the 13th day } \\ \text { Monthy Mean ........ }\end{array}\right.$ ..... 30.439
Monthly Range ..... 28.040
(Highest, the 18th day ..... $57^{\circ} 6$
Thermometer $\left\{\begin{array}{l}\text { Monthly Mean }\end{array}\right.$ ..... $29^{\circ} 38$ ..... $43^{\circ} 0$
Greatest intensity of the Sun's rays ..... 9607
Lowest point of terrestrial radiation ..... 501
Mean of Humidity ..... 819
Rain fell m 10 days, amounting to 7.936 inches; it was raining 76 hours 55 minutes.
Snow fell 12 days, amounting to $17 . S 3$ inches; it was snowing 76 hours 20 miuutes.
Most pre :ent wind, N. E. by E.
Least pre lient wind, E.
Most wind day, the 3rd day; mean miles per hour, 23.08 .
Aurora Borealis visible on - nights.
Snow Birds ("Phlectorphanes nivalis,") first seen on 3rd day.
Lunar Halo visible ou j night.
Ozone was present in large quantities.


[^0]:    * The object of the series of papers to be published under this ticle, is twofold : First, to enable our surveyors. farmers, and others, to determine the Canadian minerals that mas come, under their observation; and, secondly, to serve as an introduction to the valuable reports and other publications issued by our Geological Survey.
    Tou. V.

[^1]:    * In the explanation of these various charantery, it is occasionally necessary to refer, as examples, to a few substances of foreign occurrence. The reader will therefore understand, that the present Part of this Essay makes no special mention of the minerals of Canada, but is simply an Introduction to Part II, in which these minerals will be found arranged together.

[^2]:    -The reader desirous to take up the study of Crystallography in a morecxtended manner, may attend the author's special courses of lectures which inchade that subject. In these, the use of crystallographic instruments is shewn, and the lectures are illustrated by numerous wood and porcelain models, drawings, and natural crystals. The following is extracted from the syllabus of the advanced course on Mineralozy :
    Crxstallograpmx, Part I.-Ceystals, how defiued. Formation of Crystals. Elements of Cystals: planes, edges, anfles; diagomals, axes. Forms and combinations. Replacing planes. General nomenclature of Forms and simple Crystals. Law of constant Angles. Measurement of Angles. Laws of Symmetry: Holohedral, Hemihedral, and Tetartohedral Forms. Classification of Crystals, Dimorphism. [somorphism. Compound Crystals. Distortions. Psendomorphs.
    Part II.-The six systems of Crystalization. The Monometric system. The Dimetric system. The Hexayonal system. The Trimetric system. The Monoclinic system. The Triclinic system. Mrethod of ascertaining the system of a given Crystal.

[^3]:    * Gynsum may be scratched by tho finger nail. Calc-spar and copper pyrites may bo scratched easily by a knife; whilst feldspar and iron pgrites are hard enough to scratch window-glass. Not long ago, as mentioned by Sir William Logan, a farmer in the Ottawa district was put to much expense and annoyance by mistaking feldspar for crystalline limestone, and attempting to burn it irto lime.

[^4]:    - This is the maximum sperific gravity of calcareous spar.

[^5]:    * The little anvils called "Watch-makers' anviis," are very suitable for this purpose. They may be purchased (where Watch-makers' tools are sold) for half-a-dollar, or even less.
    t The other dark-coloured cleavable masses in these rocks consist of mica or more rarely of hornblende.

[^6]:    * The Chemical Characters of minerals are discussed in the present paper in the briefest terms. To have entered fully into thescicharacters, would have carried us altogether beyond the object in view: the simple determination of the names of Canadian minerals. The advanced lectures given daily during the Michaelmas Term in University College, Toronto, by the anthor, are open to all students desirous of obtaining more ample information on the subject. The annexed extract is taken from the author's syllabus to this course of lectures:
    "the chemical relations of mineralogy.
    "The Chemical Oorstitution of AFinerals.-1, Chemical Nomenclature as applied tc Mineralogy; 2, The Laws of Combination; 3, The Atomic Theery : 4, Chemical Notation: $\quad$, Construction of Chemical Formula; 6, Isomorphism, or Law of Substitution; 7, Atomic Volumes.
    "The Chemical Examination of Minerals-1, Action of Acids, Ac. 2, Employment of the Blow-pipe, comprising : $a$, Instruments and Appliances; $b$. Reagents; $c$, Operations; $d$, Reactions; and $e$, Plan of Analysis in the examination of an unknown substance."

    Students attending these lectures, are strongly advised to go through, also, a course of Practical Chemistry, in the Laboratory of University College, under the direction of Professor Croft.

[^7]:    - More convenient forms of blow-pipe will be found described in special works on the use of that instrument, but the common form described above is quite sufficent for the simple experiments required in the determination of our ordinary minerals.

[^8]:    * See, for example, a paper by the author " on the Assaying of Coals by the Blow-pipe,", frst published in this Journal: Vol. III., page 208. Also Plattner's "Probirkunst mit-dem Lothrohre."
    t These forceps may bo obtained from any dealer in chemical apparatus. For simple expe. riments they may be replaced by $a$ strip of thin sheet ircu bent into the form of a pair of nippers or tongs. Some twine or silk must be twisted round the middle part to prevent the fingers from being burned.

[^9]:    * These remarks were written several months ago. In the last number of the Canadian Naturalist, we were gratified to find the identity of the so-called Cheetetes lycoperdon with Stenopora fibrosa also adopted by Mr. Billings.

[^10]:    - In many glaciers the formation of a terminal moraine is prevented it should be observed by the action of the stream which results from the melting of the ice.

[^11]:    * From The Athencum of October 1, 1859.

[^12]:    * The Cxcilia may probably depart still further from the type-batrachian mode of development, and approach more to the type-reptilian mode.

[^13]:    *"Mainz, Oktober, 1843.-In dem Brandschicfer von Mūnster-Appel, in Rhoin-Baiern, habe ich in vorigen Jahre cinen Salamander aufrefunden. Gehört dieser Schiefer der Kohlen-formation? in diosene falle wite der Fund auch in anderen Hinsicht interressant." Jeonhart und Bronn, Neues Jahrbuch für Mineralogie, Sc., 18qe. p. 49.

    + Ibid. 184, p. 336.
    $\not{ }^{\prime \prime} \mathrm{Ob}$ das-Apatcon pedestris-cin Salamander-artiges Geschöpf war, ist keineswegs Busgemacht."

[^14]:    * "Archegosaurus: Fossile Saurier ans dem Steinkohlengebirce die den Uebergang des Teh'bygden zu den Iacerter: und İrokodilen bilden," p. 3. "Beitrage zur vorveltlichen Fauna des Steinkohlengchirges,' 4 to. 185\%,
    †'Reptilien ausder Steinkohlen Formation in Deutschland,' Sechster Band, p. 61.

[^15]:    *" Principal Forms of tho Skeleton," Orr's 'Circie of tine Sciences,' p. 187, fis. 11.

[^16]:    - Wyman, ' dmerican Journal of the Natural Sciences,' October, 1843.
    $\dagger$ The corresponding vacuity is larger in some ganoid fishes.

[^17]:    * This character is retained throughout the resi of the class, save in Batracbia, and will not afterwards be expressed in their characters.
    + These bones do rot reappear in the subsequent orders.

[^18]:    *This was referred to the present order by the author, after inspection of the specimens brought to the Br'tish Association Meeting, at Leeds, by Sir R. Murchison, 'יut with a nc te oin the greater rela:ive breadth of the coracoid, as shown by the pari of the bone then exposed.-(Encyclo. Brit. Art. ' Palæontology'). Prof. Hiusley, to whom the specimens were subsequently consigned for description, together with others directly transmitted to him, confirms the general crocodilian charactor of Stagonolepis. I regard the modifications of the limb-bones as indications of allanity with the Thecodontia; but the structure of the cranium must be ascertained to determine this point. The associated fossils, especially those allied to Rynchosaurus, in the Elgin saudstones, have a triassic character.
    $\dagger$ 'Anur es du Muscum,' tom. xii, p. 83, pl. x. xi.
    $\ddagger$ 'Report on British Fossil Reptiles,' Trans. British Associatios, for.18s1; p.98.
    Quarterly Journal of the Geological Society.

