

$C = \phi(A, B, c)$, je dis que la ligne c ne doit point entrer dans la fonction ϕ . Un effet, on a vu que C doit être entièrement déterminé par les seules données A, B, c , sans autre angle ou ligne quelconque ; mais la ligne c est hétérogène avec les nombres A, B, C ; et si on avait une équation quelconque entre A, B, C et c , on en pourrait tirer la valeur de c en A, B, C , d'où il résulterait que c est égale à un nombre, ce qui est absurde. Donc c ne peut entrer dans la valeur de C et on a simplement $C = \phi(A, B)$." Sir John Leslie committed the unaccountable mistake of supposing the argument here stated, to be, "that the line c is of nature heterogeneous to the angles A and B , and therefore cannot be compounded with these quantities"—whereas the argument plainly is that c , which is a line, cannot be expressed in terms solely of A, B, C , which are numbers. "The quantities A, B, C ," says Playfair, in his exposition of Legendre's reasoning, are "angles ; they are of the same nature with numbers, or mere expressions of ratio, and, according to the language of Algebra, are of no dimension. The quantity c , on the other hand, is the base of a triangle ; that is to say, a straight line, or a quantity of one dimension. Of the four quantities, therefore, A, B, C, c , the first three are of no dimensions, and the fourth or last is of one dimension. No equation, therefore, can exist involving all these four quantities and them only : for, if there did, a value of c might be found in terms of A, B , and C ; and c therefore would be equal to a quantity of no dimensions : which is impossible."

In this reasoning it is assumed, that, because C is *determined by* A, B, c , therefore C can be *expressed in terms of* A, B, c . Now Legendre does not prove that when a quantity is determined by certain others, it can be expressed in terms of them ; and I affirm that such a principle, without limitation, is not true.

For example, consider the angle C of the triangle ABC . And let it be observed that I mean the angle itself, that is, the inclination of a and b to one another, and not the numerical value of the angle, calculated upon the supposition that a right angle, or any other angle, has been assumed as a unit of measure. The angle C is *determined by* the sides, a, b, c ; yet it cannot be expressed in terms of these quantities alone ; because *the value of an angle can only be indicated by pointing out its relation to some other angle or angles* ; and therefore cannot be expressed by means simply of lines. It is true that *the numerical value* of C may be expressed in terms of a, b , and c :