

7.—de Prony's with Wiesbach's Coefficients.

Mean velocity—

$$\begin{aligned}
 v &= (.00024 + 9675 \text{ mi})^{\frac{1}{2}} - .013 \\
 &= (.00024 + 8676 \times 19.9 \times .000025) - .015 \\
 &= (.00024 + 4.29413)^{\frac{1}{2}} - .015 \\
 &= \sqrt{4.29437} - .015 \\
 &= 2.072 - .015 \\
 &= 2.057 \text{ feet per second.}
 \end{aligned}$$

8.—Rankine's Formula.

Mean velocity—

$$\begin{aligned}
 v &= 8.025 \sqrt{\frac{m i}{.007565}} = \sqrt{8512 \text{ mi}} = 92.26 \sqrt{m i} \\
 &= 92.26 \sqrt{18.8 \times .000025} \\
 &= 92.26 \times .02225 \\
 &= 2.053 \text{ feet per second.}
 \end{aligned}$$

Mean velocities.

|   |           |                  |
|---|-----------|------------------|
| 1. By Kutter's formula.....                       | v = 2.5   | feet per second. |
| 2. " de Prony's ".....                            | v = 2.073 | "                |
| 3. " Dupuit's ".....                              | v = 2.055 | "                |
| 4. " Chezy's ".....                               | v = 2.225 | "                |
| 5. " Humphrey's and Abbot's formula.....          | v = 3.197 | "                |
| 6. " Hagen's formula.....                         | v = 3.341 | "                |
| 7. " de Prony's with Wiesbach's Coefficients..... | v = 2.057 | "                |
| 8. " Rankine's formula.....                       | v = 2.053 | "                |

$$\begin{array}{r}
 8)19.501 \\
 \hline
 v = 2.438
 \end{array}$$

Grand mean velocity..... v = 2.438

To find the probable errors by the method of least squares, assuming each of the formulæ to have equal weights :

| No. of Formula. | Velocity. | Difference from Mean. | Square of Residuals. |
|-----------------|-----------|-----------------------|----------------------|
| 1.....          | 2.5       | - 0.062               | 0.0038               |
| 2.....          | 2.073     | + 0.365               | 0.1322               |
| 3.....          | 2.055     | + 0.383               | 0.1467               |
| 4.....          | 2.225     | + 0.213               | 0.0454               |
| 5.....          | 3.197     | - 0.759               | 0.5761               |
| 6.....          | 3.341     | - 0.901               | 0.8118               |
| 7.....          | 2.057     | + 0.381               | 0.1452               |
| 8.....          | 2.053     | + 0.385               | 0.1482               |

Mean = 2.438

[n n<sub>1</sub>] = 2.0104

Probable error—

$$\begin{aligned}
 r &= .6745 \sqrt{\frac{[n n_1]}{m-1}} = .6745 \sqrt{\frac{2.0104}{8-1}} \\
 &= .6745 \sqrt{0.2872} = 6.745 \times \pm 0.53 \\
 &= \pm 0.36 \text{ feet.}
 \end{aligned}$$

Probable error of Arithmetical Mean—

$$\begin{aligned}
 r(x) &= \frac{.6745}{\sqrt{m}} \sqrt{\frac{[n n_1]}{m-1}} = \frac{.6745}{\sqrt{8}} \sqrt{\frac{2.0104}{8-1}} \\
 &= \frac{.6745}{2.8284} \sqrt{0.2872} = .2385 \times \pm 0.53 \\
 &= \pm 0.126 \text{ feet}
 \end{aligned}$$

Mean discharge..... D = 6179.52 × 2.438 = 15,066 cubic feet per second.