

ARTS DEPARTMENT.

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UNIVERSITY OF TORONTO,

* Junior Matriculation.

MATHEMATICS.—PASS.

Solutions by WILBUR GRANT, Toronto Collegiate Institute. (See C. E. MONTHLY for July-August, 1881.)

8. Solve the equations

$$(4) \begin{cases} xy - yz = 18. & (1) \\ x^2 + z^2 = 4y^2 + 2xz. & (2) \\ x^2 - 8 = 2xy + 2xz. & (3) \end{cases}$$

(1) gives $(x-z)y = 18$.

(2) " $(x-z)^2 = 4y^2$,
which give $y = 3$,

(2) - (3) $z^2 + 8 = 4y^2 - 2xy$.

Substituting from (1) for $2xy$

$$z^2 + 2yz + 44 = 4y^2.$$

Substituting value of y and solving as quadratic in z we get $z = -2$ or -4 ,

$$\therefore x = 4 \text{ or } 2$$

$$y = 3.$$

9. There are two vessels, A and B , each containing a mixture of water and wine, A in the ratio of 2 : 3, B in the ratio of 3 : 7. What quantity must be taken from each in order to form a third mixture which shall contain 5 gallons of water and 11 of wine?

* Let x = quantity of water taken from A .

a = " wine " A .

y = " water " B .

b = " wine " B .

$$\frac{x}{a} = \frac{2}{3} \quad \frac{y}{b} = \frac{3}{7} \quad x + y = 5$$

$$\frac{a}{b} = \frac{3}{7} \quad a + b = 11,$$

from which four equations we get

$$x + a = 2 \text{ galls.} = \text{quantity from } A,$$

$$x + b = 14 \text{ " " " " } B.$$

10. A straight line AD is divided into three equal parts by the points B and C ; on AB , BC , CD are described equilateral triangles AEB , BFC , CGD respectively; shew that the three straight lines AE , AF , AG , can form a triangle equal in area to the equilateral triangle AEB .

$$AB = BC = CD \triangle ABE = \triangle BCF \\ = \triangle CDG \text{ in all respects,}$$

$\therefore FG$ is parallel to AD ;

but $\angle DCG = \angle CBF$,

$\therefore CG$ is parallel to BF ;

$\therefore BG$ is a parallelogram and $\triangle BFC$

$$= \triangle CFG; \text{ but } \triangle FAG = \triangle FCG,$$

$$\therefore \triangle FAG = \triangle ABE.$$

PROBLEMS.—HONORS.

1. If a straight line terminated by the sides of a triangle be bisected, no other line terminated by the same two sides can be bisected in the same point.

BE is bisected at F . Suppose GH bisected at F also, join AH .

Because $BF = FE$,

$$\therefore \triangle ABF = \triangle AFE.$$

Because $AE > AH$,

$$\therefore \triangle AEF > \triangle AHF,$$

$$\therefore \triangle ABF > \triangle AHF.$$

But since $GF = FH$,

$$\therefore \triangle AFG = \triangle AFH.$$

But $\triangle ABF > \triangle AFH$,

$$\therefore \triangle ABF > \triangle AGF,$$

$$\therefore AB > AG, \text{ which is impossible,}$$

$$\therefore \text{no line but } BE \text{ can be bisected}$$

at F and terminated by sides.

2. If two equal circles be described cutting