

EXERCISES.

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8. The angles at the vertices of two triangles are both  $67^\circ$ , and the sides about these angles are 40, 60 and 44, 66 millimetres. Construct the triangles. Show by measurement that triangles are equi-angular, and that the remaining sides are as 10 : 11.

9. Construct an angle  $BAC$  of  $39^\circ$ , and from  $P$  in  $AC$  draw  $PN$  perpendicular to  $AB$ . Measure the lengths of  $AP$ ,  $AN$ ,  $PN$  in millimetres, and find the numerical values to two places of decimals of the ratios

$$\frac{PN}{AP}, \quad \frac{AN}{AP} \quad \text{and} \quad \frac{PN}{AN}.$$

10. In the preceding question, keeping to the angle of  $39^\circ$ , take the point  $P$  in different positions on  $AC$ , drop the perpendicular  $PN$ , for each position of  $P$  repeat the measurements and calculate to two decimal places the values of the preceding ratios. Compare values with those already obtained.

11. Keeping to same angle  $39^\circ$ , take the point  $P$  in  $AB$  and drop  $PN$  perpendicular on  $AC$ . Again calculate these ratios.

State your conclusion as to the values of these ratios,—perp. to hyp. ; base to hyp. ; perp. to base—so far as the angle  $39^\circ$  is concerned.

12. BC of a right-angled triangle ABC ( $C=90^\circ$ ) is found to be 748 ft., and the angle  $ABC$  is  $39^\circ$ . Use the results of the three preceding questions to find approximately the lengths of  $AC$  and  $AB$  in feet.