

PROBLEM XVI.

To construct a rectangle $c x$ on a given base c , equivalent to a given square a^2 .

$$\text{Altitude } x = \frac{a^2}{c} \quad \text{N. S.}$$

$$= \frac{a \times a}{c} \quad \text{G. S.}$$

PROBLEM XVII.

To construct a trapezoid $\frac{p(m+n)}{2}$ equivalent to a given square a^2 , having given the two bases, m and n .

$$\text{Altitude } p = \frac{a^2}{\frac{1}{2}(m+n)} \quad \text{N. S.}$$

$$= \frac{a^2}{y} \quad (\text{See Problem IX.})$$

$$= \frac{a \times a}{y} \quad \text{G. S.}$$

PROBLEM XVIII.

To construct a trapezoid $\frac{p(m+n)}{2}$ equivalent to a given square a^2 , having given one of the bases m , and the altitude p .

$$\text{the other base } n = \frac{a^2 - \frac{1}{2} p m}{\frac{1}{2} p} \quad \text{N. S.}$$

make $\frac{1}{2} p m = y^2$ by Problem VIII., then

$$n = \frac{a^2 - y^2}{\frac{1}{2} p}$$

make $a^2 - y^2 = z^2$ by the 5th formula, then

$$n = \frac{z^2}{\frac{1}{2} p} = \frac{z \times z}{\frac{1}{2} p} \quad \text{G. S.}$$

PROBLEM XIX.

To construct a regular polygon $\frac{b c r}{2}$, equivalent to a given square a^2 , having given the side c , and the number of sides b .

$$\text{Apothem } r = \frac{2 a^2}{b c} \quad \text{N. S.}$$