## THE APPLICATION OF TRIGONOMETRY

Then to determine the side b (with A and B), B becomes the middle part, and A and b the extremes disjunct or opposites. Hence:

$$R \cos B = \sin A \cos b$$
. And, consequently,  
 $\cos b = \frac{R \cos B}{\sin A}$ .

With the two sides a and b, thus obtained, the axes x and  $\breve{x}$  are readily calculated. As  $\overline{x} = \text{unity}$ ,  $x = \cot a$ , or  $\log x = \log \cot a$  $a) - \log R$ . An inspection of the figure will show this. Finally, axis  $\breve{x} = (\tan b) \times x$ ; or  $\log \breve{x} = (\log \tan b + \log x) - \log R$ .

This understood, let us proceed, by way of example, to calculate the axial ratios of the three octahedrons in our crystal of sulphur, fig. 12.

## 1. The Lower Form.

In this form (lettered P), A (see figure 13) =  $53^{\circ}$  19'; and B = 42° 29'. Then:

 $(\text{Log cos } 53^\circ 19') + 10 = 19.7762593$  $\text{Log sin } 42^\circ 29' = 9.8295454$ 

 $9.9467139 = \log \cos a = \log \cos 27^{\circ}48'.$  (seconds being neglected.

The log cot of this latter value  $(27^{\circ}48') = 10.2779915$ . Deducting 10 (or log R) from this, and seeking for 'the corresponding number, we obtain, for axis x, the value 1.897.

Secondly:

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 $(\text{Log cos } 42^{\circ}29') + 10 = 19.8677466$  $\text{Log sin } 53^{\circ}19 = 9.9041470$ 

 $9.9635996 = \log \cos b = \log \cos 23^{\circ}8'$ .

The log tan of this angle  $(23^\circ 8') = 9.6306556$ . Adding the logarithmic value of x to this, and deducting 10 (or log R) from the sum, we obtain  $(9.6306556 + 0.2779915) - 10 = \overline{1.9086571} = \log_{10} \overline{x} = \log_{10} 0.8103$ .

## 2. The Middle Form.

In this form, A becomes 63°30'; and B, 56°35'. Calculating from

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