

mine the *latent heat of fusion of ice*. | to show that the radiating power of a
 Illustrate by a numerical example. | heated body depends upon the nature
 8. Describe two distinct experiments | of the surface of this body.

FORM III., 1898.

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8. (a) Noticing that $3\sqrt{2} - 2\sqrt{3} = (3 - \sqrt{6})\sqrt{2}$ we have

$$\frac{3\sqrt{2}+3}{3-\sqrt{6}} - \frac{2\sqrt{3}+6}{3\sqrt{2}-2\sqrt{3}} = \frac{\sqrt{2}(3\sqrt{2}+3) - (2\sqrt{3}+6)}{3\sqrt{2}-2\sqrt{3}} = 1.$$

$$(b) \left(\frac{a^x + a^{-x}}{2} \right)^2 + \left(\frac{a^x - a^{-x}}{2\sqrt{-1}} \right)^2 = \frac{a^{2x} + a^{-2x} + 2}{4} + \frac{a^{2x} + a^{-2x} - 2}{-4} = 1.$$

9. This question admits of a neater solution by arithmetic than by algebra, For an algebraical solution :

(a) Let x = time elapsed when going in the same direction. A goes 1 more lap than B. $\therefore \frac{x}{12} - \frac{x}{14\frac{2}{5}} = 1$, from which $x = 72'$.

(b) In going in opposite directions they go together 1 lap.

$$\therefore \frac{x}{12} + \frac{x}{14\frac{2}{5}} = 1, \text{ or } x = 61\frac{6}{11}'.$$

10. Book-work.

11. $x^2 - 2(a+y)x + ay$ is a complete square if $x^2 - 2(a+y)x + ay = 0$ has equal roots; that is, if $\{-2(a+y)\}^2_{4a^2} = 4$. I. ay , and $y^2 + ay + a^2 = 0$.

$$\text{Solving for } y, y = \frac{a}{2} \left\{ \frac{-1 \pm \sqrt{-3}}{2} \right\}$$

12. Let x = one side. Let d = difference of sides. Let e = diagonal.

$$\therefore x^2 + (x+d)^2 = e^2. \quad 2x^2 + 2dx + d^2 = e^2.$$

$$\text{Solving for } x \text{ we have } x = \frac{-d \pm \sqrt{2e^2 - d^2}}{2} \therefore x + d = \frac{d \pm \sqrt{2e^2 - d^2}}{2}$$

$$13. x^4 + x^2y^2 + y^4 = 741 \quad (1) \quad x^2 + xy + y^2 = 39 \quad (2)$$

$$(1) \div (2) \text{ gives } x^2 - xy + y^2 = 19 \quad (3) \quad (2) - (3) \text{ gives } xy = 10$$

$$(4) \quad (2) + (4) \text{ gives } x + y = \pm 7 \quad (3) - (4) \text{ gives } x - y = \pm 3$$

$$\text{From which } \begin{cases} x = \pm 5 \text{ or } \pm 2 \\ y = \pm 2 \text{ or } \pm 5 \end{cases}$$