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or I should have determined all the values of α required at the outset, and checked them by comparison with one another.

I have determined the ionization-constants (k and l) in all cases in which more than two observations of a property on solutions of sufficient dilution were available, by the method of least squares. The constants thus determined and used in the calculations are tabulated below. In all cases the available observations had been made on solutions of such great concentration that the values of the constants obtained cannot be regarded as exact; but the calculations may serve as a test of the general applicability of the expression referred to above. The only available observations, as far as I know, on solutions of sufficient dilution for the determination of the ionizationconstants and the limits of concentration within which the above expression is applicable, are those by Kohlrausch and Hallwachs* on the specific gravity of dilute solutions, from which two of my students have undertaken to determine the density constants for the salts and acids examined.

With regard to the observations which I used in determining the various ionization-constants, the following statements should be made :---

Bender's determinations of density (*i. e.* specific gravity referred to water at 4° C.) were made at 15° C., but were readily reduced to 18° by the aid of his observations on the thermal expansion between 15° and 20° of the same solutions. According to his statement, the fourth place of decimals in his values may be in error by ± 2 or ± 3 . The density of water was taken to be 0.99863.

Bender's determinations of thermal expansion are for the interval between 15° and 20° C, and will therefore be sufficiently nearly proportional to the coefficients of expansion at 18° for my purpose. He considers that they may be in error by ± 2 in the sixth place of decimals. On plotting his observations, however, it becomes obvious that they do not all attain this degree

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^{*} Wied. Ann. 1iil. (1894) p. 14.