

2.9 Solve for Maneuver Positions and Launch Azimuth (Continued)

$$A_S - \Omega = \tan^{-1} [\cos i_t \tan(\omega_t + \theta_t)]$$

$A_S$  = right ascension of the satellite at the point of injection into the final orbit.

$L_S$  = latitude of the point of injection

$$L_S = \sin^{-1} (\sin i_t \sin (\omega_t + \theta_t))$$

(b) Injection Into Transfer Orbit

(Assuming injection occurs at perigee of transfer orbit)

$$A_p - \Omega = \tan^{-1} [\cos i_t \tan \omega_t]$$

$$L_p = \sin^{-1} [\sin i_t \sin \omega_t]$$

( $\theta_t = 0$  at perigee)

(c) Injection Into Intermediate Orbit

$$A_{BO} - \Omega = \tan^{-1} [\cos i_t \tan(\omega_t - \phi)]$$

$$L_{BO} = \sin^{-1} [\sin i_t \sin(\omega_t - \phi)]$$

$\phi$  = central angle in waiting orbit,  $\phi = \omega + \theta$ .

(d) Position of Launch Site

$$A_L - \Omega = \tan^{-1} \left[ \cos i_t \tan \left( \omega_t + \phi - \frac{x}{R_e} \right) \right]$$

$$L_L = \sin^{-1} \left[ \sin i_t \sin \left( \omega_t - \phi - \frac{x}{R_e} \right) \right]$$

$x$  = ground range attained in ascent to the waiting orbit over a non-rotating earth and is obtained from the launch vehicle data.

(e) Launch Azimuth

From spherical trigonometry, the uncorrected launch azimuth is given by: