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obtaining the values of these quantities which was described in §10, and we will use the present instance for that purpose. To find a we take the equation (25),

$$(\delta A + 2\gamma \tau)^2 = (y - a^2) \{ y (2kt + y)(4kt + y) - 2(k^2 + t^2 y)^2 \}^2.$$
(29)
$$A = \frac{3y}{4} - \frac{p_4}{20} = -\frac{47}{500}.$$

Also, from the values of k, y and t above given,

$$2kt + y = -\frac{517}{1000}$$
$$4kt + y = -\frac{521}{1000},$$
$$k^2 + \ell^2 y = \frac{47}{1000}.$$

Therefore

$$\begin{split} \delta &= ay \left(4kt + y \right) - 2y \left(k^2 + t^2 y \right) = -\frac{521a + 47}{62500} \,, \\ \gamma &= y \left(2kt + y \right) - a \left(k^2 + t^2 y \right) = \frac{-47 \left(125a + 11 \right)}{125000} \,, \\ \tau &= k^2 - t^2 y = -\frac{1}{500} \,. \end{split}$$

Hence (29) becomes

$$125 (323a + 29)^2 = 36^2 (1 - 125a^2). (30)$$

One root of this equation is $-\frac{11}{125}$. But this root proves on examination to be inadmissible. We must therefore take the other root, which is $-\frac{9439}{25^3 \times 13^2}$.

Then, since
$$c=\frac{7a}{4}$$
, and $a^2z=\frac{1}{125}$, we have
$$a=-\frac{9439}{25^3\times 13^3}=-\frac{9439}{25\times 4225},$$

$$c=-\frac{7\times 9439}{422500},$$

$$z=\frac{5\times 4225^2}{9439^2},$$

$$e=\frac{398}{392}.$$

The sign of e is determined in the way pointed out in §10. By means of the values of e, z, a, c that have been obtained, we get, from the two equations (26),

$$\theta = \frac{125}{199}, \, \phi = -\frac{18 \times 9439}{199 \times 845} : \theta^2 - \phi^2 z = -\frac{125}{199}.$$