

becomes

$$\frac{1}{2} \left(50y - \frac{2}{5} p_4 \right) = p_5.$$

$$\therefore y = \frac{1}{17} \therefore a\sqrt{z} = \sqrt{y} = \frac{\sqrt{17}}{17}.$$

Therefore also $c\sqrt{z} = t(a\sqrt{z}) = \frac{\sqrt{17}}{34}$. Therefore, by (20),

$$yB'\sqrt{z} = -2(c^2z)(c\sqrt{z}) \therefore B'\sqrt{z} = -\frac{\sqrt{17}}{68}.$$

And, by the second of equations (9), $B = -\frac{1}{68}$. Therefore

$$B + B'\sqrt{z} = -\frac{1}{68} (1 + \sqrt{17}).$$

And $u_1 u_4 = \frac{\sqrt{17}}{17}$. Therefore

$$\begin{aligned} x = & \left[-\frac{1}{68} (1 + \sqrt{17}) + \sqrt{\left\{ \left(\frac{1 + \sqrt{17}}{68} \right)^2 - \left(\frac{\sqrt{17}}{17} \right)^5 \right\}} \right]^{\frac{1}{4}} \\ & + \left[-\frac{1}{68} (1 + \sqrt{17}) - \sqrt{\left\{ \left(\frac{1 + \sqrt{17}}{68} \right)^2 - \left(\frac{\sqrt{17}}{17} \right)^5 \right\}} \right]^{\frac{1}{4}} \\ & + \left[-\frac{1}{68} (1 - \sqrt{17}) + \sqrt{\left\{ \left(\frac{1 - \sqrt{17}}{68} \right)^2 + \left(\frac{\sqrt{17}}{17} \right)^5 \right\}} \right]^{\frac{1}{4}} \\ & + \left[-\frac{1}{68} (1 - \sqrt{17}) - \sqrt{\left\{ \left(\frac{1 - \sqrt{17}}{68} \right)^2 + \left(\frac{\sqrt{17}}{17} \right)^5 \right\}} \right]^{\frac{1}{4}}. \end{aligned}$$

§37. *Eleventh Example.*—Let

$$x^5 - \frac{4x}{13} + \frac{29}{65} = 0.$$

The equations furnishing the criterion of solvability are

$$\begin{aligned} -\frac{4}{13} &= \frac{5n^4(3-m)}{16+m^2}, \\ \frac{29}{65} &= \frac{n^5(22+m)}{16+m^2}, \end{aligned}$$

and they are satisfied by the values $m = 7, n = 1$. By §25, $n = 2t$. Therefore $t = \frac{1}{2}$. Therefore, from (11), $y = \frac{1}{65}$. Therefore

$$a\sqrt{z} = \frac{\sqrt{65}}{65} \therefore c\sqrt{z} = t(a\sqrt{z}) = \frac{\sqrt{65}}{130}.$$

Therefore, by (20), $yB'\sqrt{z} = -2(c^2z)(c\sqrt{z})$. Therefore $B'\sqrt{z} = -\frac{\sqrt{65}}{260}$. And,

by the second of equations (9), $B = -\frac{9}{260}$. Therefore

$$B + B'\sqrt{z} = -\frac{9 + \sqrt{65}}{260}.$$