

Draw two other bases B_1C_1 , B_2C_2 of lengths 30 and 45 millimetres. At B_1 and B_2 make angles $C_1B_1A_1$, $C_2B_2A_2$, each equal to CBA ; and at C_1 and C_2 make angles $B_1C_1A_1$, $B_2C_2A_2$, each equal to BCA . It follows (Ch. III., 4) that the angles at A , A_1 , A_2 are equal to one another. Hence the three triangles are equiangular and *similar*.

Now measure the lengths of the sides of the triangles $A_1B_1C_1$ and $A_2B_2C_2$. If the constructions have been accurately made, we shall have the following numerical values:

$BC = 15$	$B_1C_1 = 30$	$B_2C_2 = 45$
$AB = 20$	$A_1B_1 = 40$	$A_2B_2 = 60$
$AC = 25$	$A_1C_1 = 50$	$A_2C_2 = 75$

Then calling those sides *corresponding sides* which are opposite to equal angles, we observe that corresponding sides about equal angles are proportional, *i.e.*,

$$\frac{15}{20} = \frac{30}{40} = \frac{45}{60}$$

$$\frac{20}{25} = \frac{40}{50} = \frac{60}{75}$$

$$\frac{15}{25} = \frac{30}{50} = \frac{45}{75}$$

3. Again, construct a triangle ABC , whose base BC is 24, and sides AB and AC , 30 and 40 millimetres. Draw two other bases B_1C_1 and B_2C_2 of lengths 36 and 60 millimetres. At B_1 and B_2 make angles $C_1B_1A_1$, $C_2B_2A_2$, each equal to CBA ; and at C_1 and C_2 make angles $B_1C_1A_1$, $B_2C_2A_2$, each equal to BCA . It follows (Ch. III., 4) that the angles at A , A_1 , A_2 are equal to one another. Hence the three triangles are equiangular and *similar*.