Expanding and collecting terms we get the two formulæ.

(a) 
$$(a+b+c)^3+(a+b-c)^3$$
  
  $= \{(a+b)+c\}^3+\{(a+b)-c\}^3$   
  $= 2\{(a+b)^3+3c^2(a+b)\}.$   
  $(b) (a+b+c)^3-(a-b-c)^3$   
  $= \{a+(b+c)^3-\{a-(b+c)^3\}^3$   
  $= 2\{3a^2(b+c)+(b+c)^3\}.$   
  $(c) (x+y+1)^3-(x+y-1)^3-2\{3(x+y)^2+1\}$   
  $= 2\{3(x+y)^2+1\}-2\{3(x+y)^2+1\}=0.$   
 179. Simplify  
  $(a) (x+a+b)^3+(x+a-b)^3$   
  $+6(x+a)(x+a)^2-6b^2(x+a);$   
  $(b) 8(x+a+b)^3-(2x+2a)^3$   
  $-8b^2-24b(x+a)(x+a+b).$   
  $(a) (x+a+b)^3+(x+a-b)^3+6(x+a)(x+a)^2$   
  $-6b^2(x+a)=(x+a+b)^3+(x+a-b)^3$   
  $+3\times2(x+a)\{(x+a)^2-b^2\}$   
  $= \{(x+a+b)+(x+a-b)\}^3$   
  $= (2x+2a)^3.$   
  $(b) 8(x+a+b)^3-(2x+2a)^3$   
  $-8b^3-24b(x+a)(x+a+b)$   
  $= (2x+2a)^3.$   
  $(b) 8(x+a+b)^3-(2x+2a)^3$   
  $-8b^3-24b(x+a)(x+a+b)$   
  $= (2x+2a)^3+(2b)^3+3\times2b(2x+2a)$   
  $= (2x+2a)^3+(2b)^3+3\times2b(2x+2a)$   
  $= (2x+2a)^3+8b^3+24b(x+a)(x+a+b)$   
  $-\{(2x+2a)^3+8b^3+24b(x+a)(x+a+b)$   
  $-\{(2x+2a)^3-8b^3-24b(x+a)(x+a+b)$   
  $-\{(2x+2a)^3-8b^3-24b(x+a)(x+a+b)$   
  $-\{(2x+2a)^3-8b^3-24b(x+a)(x+a+b)$   
  $-\{(2x+2a)^3-8b^3-24b(x+a)(x+a+b)$   
  $-\{(2x+2a)^3-8b^3-24b(x+a)(x+a+b)$   
  $-\{(2x+2a)^3-8b^3-24b(x+a)(x+a+b)$   
  $-\{(2x+2a)^3-8b^3-24b(x+a)(x+a+b)$   
  $-\{(2x+2a)^3-8b^3-24b(x+a)(x+a+b)$ 

180. If a cubic foot of water weighs 1,000 ounces, and the specific gravity of silver be 10.5, find how many ounces of silver would be required to make an inkstand, in the form of the frustrum of a regular hexagon, 4 inches high, each of whose sides at the base is two inches long and at the top 1 inch long, the hollow being in the form of a right cylinder, extending to within one inch of the bottom, and arranged about the central axis, so as to leave a wall  $\frac{1}{4}$  of an inch thick at the middle of each side at the top.

Dividing the upper and under surfaces into equilateral triangles to find their areas, we get for the number of square inches in these respective surfaces  $6\sqrt{3}$  &  $\sqrt[4]{3}$  inches,

.. vol. of frustrum if solid would be  $(6\sqrt{3} + \frac{6}{2}\sqrt{3} + \frac{6}{4}\sqrt{3})\frac{4}{3} = 14\sqrt{3}$  cub. in. The diameter of hollow cylinder is .616 inches; ... its vol. is  $(.616)^2 \times \pi \times 3 = 3.5762 + \text{inches}$ , ... number cubic inches of silver is  $14\sqrt{3} - 3.5762 = 20.672$ , and  $\frac{20.672}{1728} \times 1000 \times 10.5 = 125.61$  ozs. of silver.

181. A owes \$4,000, due in three years, bearing interest at 6 per cent. per annum. He wishes to make equal half-yearly deposits in the bank, so that at the end of the three years, these deposits, with accrued interest, may be just sufficient to cancel the debt, the bank allowing interest at 5 per cent. per annum, payable half yearly, and the first deposit to be made at the end of the first half year. Just after making his payment at the end of the second year he is compelled to draw out of the bank \$1,000; find how much each of his last two payments must be increased on this account; also find the total amount of the last deposit.

Amount of debt in 3 years at 6 per cent. per annum is \$4764.064+; if paid as at first intended each deposit would be

$$4764.064 \div \{(1.025)^{5} + (1.025)^{4} + (1.025)^{3} + (1.025)^{2} + 1.025 + 1\} = $145;814.$$

These deposits with interest, at end of 2nd year amount to

3097.0049 + 3097.0049 - 1000 = 2097.0049. which at end of 3rd year amounts to

\$2203.1678+4764.064 - 2203.1678: =2667.058=amount to be met by last two deposits,  $2667.058 \div (1.025 + 1) = 1265.615$ =amount of each payment

\$1265.615-745.814=518.801+
=amount by which last payment was increased on account of \$1000 being drawn;
1265.615=amount of last payment.

182. A brass scale of a barometer has been correctly graduated at 62° Fahr.; find the true reading of the barometer when it shews 30 inches at 87° Fahr., corrections being made for the expansions of the scale and the mercury, the co-efficient of expansion of brass being .00001 for every degree Fahr.,