

In the *first* series, the first term and com. diff. are 1 and $\frac{1}{2}$; in the *second*, 1 and $\frac{1}{3}$; then by the question,

$$\frac{n}{2} \left\{ 2 + (n-1)\frac{1}{2} \right\} = 4 \frac{n}{2} \left\{ 2 + (n-1)\frac{1}{3} \right\};$$

$$\therefore n = 37; \frac{3}{2}.$$

8. The attraction of a planet upon a body at its surface varies directly as the planet's mass and inversely as the square of its radius. The length of a pendulum varies directly as the attraction and inversely as the square of the number of beats which it makes in a given time. The mass of the earth being 75 and of the moon 1, the radius of the earth 4,000 miles and of the moon 1,100, and the length of a pendulum which beats 5 times in 2 seconds at the earth's surface being 6.26 in., find the length of a second's pendulum at the moon's surface.

8. For earth we have $A = p \frac{M}{r^2}$, $l = p \frac{A}{n^2}$, by

the question, where A = attractive force, M = mass, r radius, n number of beats, and l length of pendulum: from these $= ns$,

$$A = \frac{\sqrt{939}}{1600\sqrt{2}}, \text{ and } p \text{ (constant factor)} \\ = 400\sqrt{\frac{313}{6}}.$$

For moon, we have

$$l = p^2 \frac{M}{r^2 n^2} \\ = 160000 \times \frac{313}{6} \times \frac{1}{1210000} \\ = 6.89 \text{ in.}$$

9. From a company of 15 men, 6 are selected each night as a guard. How often, respectively, will A and B be together (1) with C? (2) without C? (3) with C or D? (4) with C and D?

$$9. (1) \frac{12, 11, 10}{[3]}, (2) \frac{14, 13, 12, 11}{[4]}, \\ (3) 2 \frac{12, 11, 10}{[3]}, (4) \frac{11, 10}{[2]}.$$

$$10. \text{ Given } x^2 + \frac{a-b}{ab}x + \frac{ab}{a-b} = 0.$$

(1) Express b in terms of a when the two values of x are (a) equal in magnitude and

opposite in signs; (3) equal in magnitude and of like signs.

(2) If x_1, x_2 be the roots, express the value of $\frac{1}{x_1} + \frac{1}{x_2}$ in terms of a and b .

$$10. (1) (a) \frac{b-a}{2ab} = \text{either root};$$

$$\therefore \frac{(b-a)^2}{4a^2b^2} = \frac{ab}{b-a} \text{ or } b = \frac{a}{1-a\sqrt{\frac{a}{4}}},$$

$$(\beta) b = \frac{a}{1+a\sqrt{\frac{a}{4}}}.$$

$$(2) \frac{1}{x_1} + \frac{1}{x_2} = \frac{x_1 + x_2}{x_1 x_2} = - \left(\frac{a-b}{ab} \right)^2.$$

UNIVERSITY OF LONDON.

MATRICULATION EXAMINATIONS JUNE, 1883.

ARITHMETIC AND ALGEBRA.

Examiners—Dr. John Hopkinson, M.A., F.R.S., and Benjamin Williamson, Esq., M.A., F.R.S.

1. From the sum of $\frac{1}{2}$, $\frac{1}{3}$, $\frac{1}{4}$, and $\frac{1}{5}$ of a pound subtract the sum of $\frac{1}{6}$, $\frac{1}{7}$, and $\frac{1}{8}$ of a guinea, and express the result as a fraction of five pounds reduced to its simplest form.

2. Express $\sqrt{\frac{0.678 \times 9.01}{0.0234}}$ correctly to the nearest integer.

3. Reduce $\frac{0.01747}{0.002477}$ to a vulgar fraction in its simplest form.

4. A reduction of 10 per cent. in the price of coal would enable a purchaser to obtain for the sum of £13 10s. two tons more than at the higher price. What may be the price of coal before reduction?

5. Divide £11 4s. 6d. between three men, four women, five boys, and six girls, in such wise that each woman has one-fourth less than a man, each boy two-sevenths as much as a man and woman together, and each girl one-fifth as much as a man, woman, and boy together.

6. Simplify

$$\frac{x^2 + y^2 - x}{\frac{y}{1} - \frac{1}{x}} \times \frac{x^2 - y^2}{x^3 + y^3}; \text{ and } a \times \frac{1}{1 + \frac{a+1}{3-a}}.$$