

- (10.) Transpose, and $x^2 - 2xy + y^2 + y^2 - 2yz + z^2 + z^2 - 2uz + u^2 = (x-y)^2 + (y-z)^2 + (z-u)^2$. Since the square of any quantity is positive, $\therefore$ each expression is positive, and cannot be zero unless each quantity is zero, $\therefore x-y=0$, $y-z=0$, $z-u=0$, $\therefore x=y=z=u$.

EXERCISE XXIV.

- (1.) $a^3 - 8a^2 + 23a - 26$. (2.) . (3.) . (4.) .
 Page 53. (5.) 29 miles. (6.) $\frac{1}{x}$. (7.) . (8.) .
 (9.) $x^2 - (a+b)x + ab = x^2 + x + 1$. Since co-efficients of like powers are equal, $\therefore a+b = -1$ and $ab=1$, $\therefore a^3 + b^3 = 2$.
 (10.) $a+b = -c$, multiply by $a-b$, etc.

EXERCISE XXV.

- (1.) . (2.) $x=6$. (3.) $\frac{1}{abe}$. (4.) $x = \frac{13a}{2}$.
 (5.) $a=8$. (6.) $\frac{x}{3-x}$. (7.) $5x^2 - 2x - 1$. (8.) $x=10$.
 (9.) Let $x-3$, $x-1$, $x+1$, $x+3$, be the numbers, etc.
 (10.) .

EXERCISE XXVI.

- Page 54. (1.) $x=10a$. (2.) Let $x=\text{one}$, $x+d$ the other, etc.
 (3.) $\frac{b^2+c^2-a^2}{2bc} + 1 = m+1$, etc. (4.) 216.
 (5.) $a^3 + 2a^2b - ab^2 - 2b^3$. (6.) $m^2 - 12m + 35$.
 (7.) $(x^2 - 3x + 17)(x^2 + 3x + 17)$.
 (8.) $x^2 - 3x + 2$ is a factor and $=0$, $\therefore$ expression $=0$.
 (9.) Write $(1 - \frac{1}{a} + 1 - \frac{1}{b} + 1 - \frac{1}{c} - 1) \div 2 -$
 $(\frac{1}{a} + \frac{1}{b} + \frac{1}{c})$, etc., $=1$. (10.) .

EXERCISE XXVII.

- (1.) Factor the expression. (2.) $\frac{4x^2+2x-1}{3x+1}$.
 (3.) . (4.) . (5.) $\frac{1}{2}a + \frac{3}{2}b - \frac{1}{2}c$.
 (6.) . (7.) $\frac{1}{18}$.
 Page 55. (8.) 6. (9.) 405 yards. (10.) $x=a+b+c$.