

To give an example, following Nordhaus let us assume

$$B(R) = \beta R^\alpha, \quad (8a)$$

where  $\alpha$  is the constant elasticity of cost reduction with respect to research. Using (8a) equation (5) becomes

$$R = \left[ \frac{\psi \alpha \beta}{\rho s} \right]^{\frac{1}{1-\alpha}}. \quad (8b)$$

From equations (8a) and (8b), the size of the invention is:

$$B = \beta \left[ \frac{\psi \alpha \beta}{\rho s} \right]^{\frac{\alpha}{1-\alpha}}. \quad (8c)$$

When (8c) is substituted in (7), the optimal patent term  $\psi^*$  may be obtained from the solution of the equation:

$$\psi + \psi^{\frac{1}{1-\alpha}} [\eta \beta \left\{ \frac{(\beta \alpha)}{\rho s} \right\}^{\frac{\alpha}{1-\alpha}} (1 + \frac{k}{2})] - \psi^{\frac{\alpha}{1-\alpha}} [\eta \beta \left\{ \frac{(\beta \alpha)}{(\rho s)} \right\}^{\frac{\alpha}{1-\alpha}}] = 1. \quad (8d)$$

It is extremely difficult to solve for  $\psi$  from equation (8d). However, it is possible to compute values of  $T$  that would satisfy (7) for different values of  $B$  and  $\eta$  and determine whether the existing patent term is greater or less than the optimal patent term. The reasoning for this may be illustrated in Figure 3. In Figure 3,  $PP'$  represents the solution of the policy maker's equilibrium (7) and represents the existing life of a patent (which is 20 years in Canada and in the United States). The curves  $OI_1$ ,  $OI_2$  and  $OI_3$  represent inventor equilibria for different industries -  $I_1$ ,  $I_2$  and  $I_3$ . At the existing patent life  $\psi_0$  the observed size of the inventions in the three industries will be  $B_1$ ,  $B_2$  and  $B_3$ . By examining the observed equilibrium points  $(\psi_0, B_1)$ ,  $(\psi_0, B_2)$  and  $(\psi_0, B_3)$ , we can determine whether the existing life is longer or shorter than the optimal. For  $I_1$ ,  $I_2$  and  $I_3$ , the inventor equilibria are respectively to the right of, on and to the left of  $PP'$ . Thus, for  $I_1$ , the existing life is longer than the optimal; for  $I_3$  the existing life is shorter than the optimal; whereas for  $I_2$ , the existing life is optimal.