

## PROBLEM XLIX.

**To Find a Third Proportional to Two Given Lines, A and B.—(Figs. 59 and 60.)**

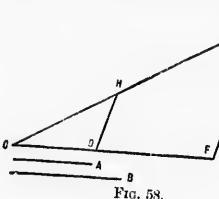


FIG. 58.

**FIRST.—** Let it be required to find a third proportional which will be greater than  $A$  or  $B$ .—(Fig. 59.)

Draw any line  $CF$  making  $CD$  equal to  $A$  and  $DF$  equal to  $B$ . From  $C$  draw a line,  $CG$ , of indefinite length forming

any angle with  $CF$ , and on it measure  $CH$  equal to  $B$ . Join  $HD$ . From  $F$  draw a line parallel to  $HD$  (problem vii.) to meet  $CG$  in  $K$ . Then  $HK$  will be the proportional required, that is  $CD : CH :: CH : HK$ . (*Euclid* vi. 11.)

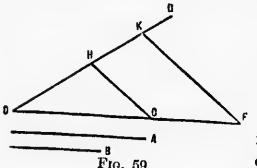


FIG. 59.

**SECOND.—** Let it be required to find a third proportional which will be less than  $A$  or  $B$ .—(Fig. 60.)

Draw any line,  $CF$ , making  $CD$  equal to  $A$  and  $DF$  equal to  $B$ . From  $C$  draw a line,  $CG$ , of indefinite length,

forming any angle with  $CF$ , and on it measure  $CH$  equal to  $B$ . Join  $HD$ . From  $F$  draw a line parallel to  $HD$  (problem vii.) to meet  $CG$  in  $K$ . Then  $HK$  will be the proportional required, that is,  $CD : CH :: CH : HK$ . (*Euclid* vi. 11.)

## EXERCISES.

94. Draw two lines  $\frac{4}{5}$ " and  $\frac{7}{8}$ " long respectively and find a third proportional which will be greater than either.
95. Draw two lines bearing the ratio of 4 and 5 and find a third proportional less than either.
96. Find a third proportional (greater) to two lines bearing the ratio of 3 and 5.
97. Find a third proportional (less) to two lines  $1\frac{1}{4}$ " and 1" long respectively.