$\frac{c}{3 \sin 2\theta}$  (found by combining (1) and (2) for r, simplifying and reducing.

$$AH \text{ becomes} = \frac{c}{6} \frac{(2 + \cos 2\theta)}{\cos \theta}$$
  
and HO becomes =  $\frac{c}{6} \frac{(2 - \cos 2\theta)}{\sin \theta}$  = equation (4)

Referring to Fig. (1)

$$AB = AH + HB = AH + OK \tan \frac{I}{2} =$$
equation (5)

$$dL = \sqrt{(dc)^2 + c^2 (d^{\theta})^2}$$
  
but by (b)  $(d^{\theta})^2 = \frac{c^2 dc^2}{m^2 - c^4}$ 

$$\therefore dL = \frac{m \, dc}{\sqrt{m^2 - c^4}} = m \, (m^2 - c^4)^{-\frac{1}{2}} \, dc = \left(1 - \frac{c^4}{m^2}\right)^{-\frac{1}{2}} \, dc$$

expanding by the Binomial Theorem

$$dL = \left(1 + \frac{c^4}{2m^2} + \frac{3 c^8}{8 m^4} + \right) dc$$

integrating, 
$$L = c + \frac{c^5}{10m^2} + \frac{c^9}{24m^4} =$$
equation (6)

when m = 1031337, (the number chosen in making up the table);  $\frac{c^5}{10m^2}$  the second term in the above series  $=\frac{1}{10}$  of a foot when