

ARTS DEPARTMENT.

ARCHIBALD MACMURCHY, M.A., MATHEMATICAL EDITOR, C. E. M.

Our correspondents will please bear in mind, that the arranging of the matter for the printer is greatly facilitated when they kindly write out their contributions, intended for insertion, on one side of the paper ONLY, or so that each distinct answer or subject may admit of an easy separation from other matter without the necessity of having it re-written.

SOLUTIONS.

Solutions by Prof. Edgar Frisby, M.A.,
Naval Observatory, Washington.

$$107. \text{ If } x + y - axy = 0$$

$$y + z - byz = 0$$

$$z + x - cxy = 0,$$

and if $azy + bxz + cxy = 0$, then

$$\frac{a}{b^2 - (a-c)^2} + \frac{b}{c^2 - (b-a)^2} + \frac{c}{a^2 - (c-b)^2} = 0.$$

From first and third equations we have

$$y = \frac{x}{ax - 1}; z = \frac{x}{cx - 1}.$$

Substituting in (2) gives $(a + \dots)x^2 - 2x = bx^2$,

whence $x = 0$ or $x = \frac{2}{a + c - b}$,

similarly $y = 0$ $y = \frac{2}{a + b - c}$

and $z = 0$ $z = \frac{2}{b + c - a}$,

and substituting the last values in

$azy + bxz + cxy = 0$ gives the relation.

111. Divide without expansion

$$(x^3 - \frac{1}{2}yz)^2 + \frac{27}{8}y^2z^2 \text{ by } x^2 + yz.$$

$$\left(x^3 - \frac{yz}{2}\right)^2 + \left(\frac{3yz}{2}\right)^2 = \left(x^3 - \frac{yz}{2} + \frac{3yz}{2}\right)$$

$$\left(x^4 - x^2yz + \frac{y^2z^2}{4} + \frac{9y^2z^2}{4} - \frac{3x^2yz}{2} + \frac{3y^2z^2}{4}\right)$$

$$= (x^2 + yz) \left(x^4 - \frac{5}{2}x^2yz + \frac{13}{4}y^2z^2\right),$$

whence dividing by the first factor we have

$$x^4 - \frac{5}{2}x^2yz + \frac{13}{4}y^2z^2.$$

Solutions by F. Boulteb, Univ. Coll.

110. Factor $l(m+nx)^2 - (l+nx)(m+nx)$

$$- l n (l + n x) (m + n x) + n (l + n x)^2.$$

$$= (m + n x) \left\{ l (m + n x) - (l + n x) \right\}$$

$$- n (l + n x) \left\{ l (m + n x) - (l + n x) \right\}$$

$$= \left\{ (m + n x) - n (l + n x) \right\}$$

$$\left\{ l (m + n x) - (l + n x) \right\}.$$

108. (See January number, 1880).

$$(1-x)^{-2n} = 1 + 2nx + \dots$$

$$+ \frac{2n(2n+r-2)}{r-1} x^{r-1} + \frac{2n(2n+r+1)}{r} x^r$$

$$(1-x)^{-n} = 1 + nx + \dots$$

$$+ \frac{n(n+r-2)}{r-1} x^{r-1} + \frac{n(n+1)-(n+r-1)}{r} x^r.$$

Multiplying together we see that given expression equals coefficient of x^r in

$$(1-x)^{-2n} \times (1-x)^{-n}$$

equals coefficient x^r in $(1-x)^{-3n}$

$$\frac{3n(3n+1) \dots (3n+r-1)}{r}.$$

112. Two equal circles intersect in A and B through D any point in the line AB ; DEC is drawn at right angles to AB , meeting the circles in E and C respectively; join BE and AE and produce them to meet AC