

Changing the unit of time to two hundred and fifty years, the equations (a) (b) and (c) give the following values of the derivatives of ϵ_1 and ψ :

Zero-epoch.	$D_r \epsilon$		$D_r \psi$	
	- 250 Y	+ 250 Y	- 250 Y	+ 250 Y
	"	"	"	"
1600	- 1.4636	+ 0.7400	12600.33	12573.65
1850	- 1.1768	+ 0.4527	12603.44	12576.65
2100	- 0.8898	+ 0.1665	12606.57	12579.71

At the respective epochs $D_r \epsilon_1$ vanishes, and $D_r \psi$ has the values of the lunisolar precession in longitude (§ 100).

Developing in powers of τ we have the following results:

$$\begin{aligned}
 \text{Zero-epoch.} \quad & \circ \quad ' \quad '' \quad '' \quad '' \\
 1600; \epsilon_1 &= 23 \ 29 \ 28.69 + 0.5509 \tau^2 - 0.1206 \tau^3 \\
 1850; \epsilon_1 &= 23 \ 27 \ 31.68 + 0.4074 \quad - 0.1207 \\
 2100; \epsilon_1 &= 23 \ 25 \ 34.56 + 0.2641 \quad - 0.1206 \\
 \\
 1600; \psi &= 12587.00 \tau - 6.67 \tau^2 \\
 1850; \psi &= 12590.05 \quad - 6.70 \\
 2100; \psi &= 12593.14 \quad - 6.72 \\
 \\
 1600; \lambda &= 45.28 \tau - 14.83 \tau^2 \\
 1850; \lambda &= 33.52 \quad - 14.86 \\
 2100; \lambda &= 21.75 \quad - 14.88
 \end{aligned}$$

These values of ϵ_1 and ψ completely fix the position of the equator at the time τ relative to the zero ecliptic and equinox. For the reduction of coordinates from one epoch to another we must express the position of the equator at the time τ . We consider the triangle $P E_0 P_0$, of which the sides and opposite angles are designated

$$\begin{array}{ccccccc}
 \text{Sides,} & & \epsilon_0 & & \epsilon_1 & & \theta \\
 \text{Opposite angles,} & 90^\circ - \zeta & & 90^\circ - \zeta_1 & & \psi
 \end{array}$$

If, in the Gaussian relations between the parts of this triangle, we put

$$\sin \frac{1}{2} (\epsilon_1 - \epsilon_0) = \frac{1}{2} (\epsilon_1 - \epsilon_0) = \frac{1}{2} \Delta \epsilon$$