

Figure A2: Detection probability function $d_r(q)$, when r > 1

If $r \le 1$ then $d_r(q) = rq$ as before. If r > 1, than $d_r(q) = rq$ if 0 < q < 1/r and $d_r(q) = 1$ if 1/r < q < 1. The iteration equation (A1) becomes

$$V_{n,k} = p \left[d_{r}(q)(-K) + (1-d_{r}(q))(q) + V_{n-1,k-1} \right] + (1-p)[q+V_{n-1,k}] \quad (A4)$$

As in the Theorem, the optimal cheating level $q = q^*$ must make the partial derivative of V_{nk} with respect to p vanish. But the partial derivative of V_{nk} with respect to p is

$$V_{n-1,k-1} - V_{n-1,k} - (K+q)d_{r}(q)$$

It follows that $q^* < 1$ if

$$\frac{V_{n-1,k-1} - V_{n-1,k}}{K + 1/r} < 1,$$

which is certainly true if $V_{n-1,k-1} - V_{n-1,k} < K$. In practice, this sufficient condition was found to be adequate; as long as the value of K was large enough that for all n and k, the expected value difference $V_{n-1,k-1} - V_{n-1,k}$ did not exceed K, then any value of r could be allowed without altering the interpretation of the model, because $q^* < 1/r$. It should be noted that this sufficient condition reflects that intuition that, for E to cheat at a level that makes detection certain (if there is inspection), the gain to E in seeing R use up an inspection must be very large.

As noted in the text, the basic model embodied in (A1) can be modified to include a variable, w, representing concealment effort. Concealment effort refers to activities of the inspectee, E, which reduce the detectability of violations but also reduce the value. Suppose that w = 1 is the standard level of concealment effort, and a value w > 0 is actually chosen by E, changing detectability from r to r = r/w. Let $\alpha > 0$ be a parameter measuring the ratio of the relative rate of change (with respect to w) of the value q of undetected cheating at level q to the relative rate of change of r with respect to w. It follows that $q = q/w^{\alpha}$. Denoting E's expected payoff by V when concealment effort is included in the model, the recursion equation (A1) must be replaced by

$$\mathbf{V}_{nk} = p[\mathbf{rq}(-K) + (1 - \mathbf{rq}) \mathbf{q} + \mathbf{V}_{n-1,k-1}] + (1 - p)[\mathbf{q} + \mathbf{V}_{n-1,k}]$$
(A5)

To see how (A5) can be solved recursively, multiply each term by w^{α} to obtain

$$w^{\alpha}V_{n,k} = p[rq(-Kw^{\alpha}) + (1-rq)q + w^{\alpha}V_{n-1,k-1}] + (1-p)[q + w^{\alpha}V_{n-1,k}]$$
(A6)