

these lines will be equal in length to  $b, d$  and  $d, a$  respectively. Therefore, since  $b, d$  was proved to be equal to  $d, a$  the weight will equal the resistance.

3. Bisect  $AC$  in  $G$ ;  $G$  is the centre of gravity of the square. Produce  $EB$  to intersect  $AC$  in  $F$ . Let  $w$  equal the weight of the squares. The force acting along  $FB$  will equal  $q + w + 3q + w = 4q + 2w$ .

Take moments around  $G$ ;

$$(3q + w)AG - (4q + 2w)FG - qGC = 0$$

$$\text{But } AG = GC$$

$$\therefore FG = \frac{1}{2}AG.$$

4. Since their velocities at the moment of collision were equal, had no collision occurred the first particle on arriving at  $B$  would have had the initial velocity (here zero) of the second particle

$$\therefore \text{height of } B = 384^2 \div 2g = 2304.$$

5. Let  $g'$  be the value of  $g$  resolved along  $CB$

$$\begin{array}{ccccccc} \text{" } g' \text{"} & \text{" } & \text{" } & \text{" } & \text{" } & \text{" } & \text{CA} \\ g' & z & & & & & \\ \therefore \frac{g'}{g'} & \frac{z}{x} & - & - & - & - & (i) \end{array}$$

$$\sqrt{\frac{2x}{g'}} = \sqrt{\frac{2z}{g'}} - \sqrt{\frac{2y}{g'}} \quad (ii)$$

$$\therefore \frac{\sqrt{z}}{\sqrt{x}} = \frac{\sqrt{x}}{\sqrt{z} - \sqrt{y}}$$

$$\therefore z - \sqrt{(yz)} = x$$

$$\therefore (z - x)^2 = yz.$$

6. Resolving the initial velocity horizontally and vertically gives for the latter component 160 ft. per second, hence the time of flight from  $A$  to  $B$  would be  $2(160 \div g) = 10$ , therefore the time of the second particle's flight was  $\frac{1}{2}(10 - 4) = 3$  seconds and therefore the height of the point of collision was  $3 \times 160 - 16 \times 9 = 336$  ft.

7. Let  $c$  equal the contents of the body in cubic feet, the weight of the body when immersed in water will be decreased by  $1000c$  oz. Hence when immersed in the first liquid its weight will be decreased by  $(1000c + 1)$  oz., and when immersed in the second liquid by  $(1000c - 1)$  oz. these

therefore will be the respective weights of  $c$  cubic feet of each of the liquids

$$\therefore \frac{1000c + 1}{1000c - 1} = \frac{1000t + 1}{1000t - 1}$$

$$\therefore c = t.$$

8. 15 lbs. per square inch is 34560 oz. per square foot, therefore pressure at the surface is 34560 oz. per square foot and at a depth of 7 feet in the liquid it is  $(7000s + 34560)$  oz. per square foot,  $s$  being the specific gravity of the liquid.

Writing *a.u.c.* for "air in unimmersed cone"

and *a.i.c.* for "air in immersed cone" height *a.u.c.* : height of *a.i.c.* :: 7 feet 7 in. : 7 ft. :: 13 : 12

Similar solids are in the triplicate ratio of their like linear dimensions

$$\therefore \text{volume of } a.u.c. : \text{volume of } a.i.c. :: 13^3 : 12^3 :: 2197 : 1728$$

$$\therefore \text{by Boyle's Law}$$

$$7000s + 34560 : 34560 :: 2197 : 1728$$

$$\therefore S = 1.34.$$

NOTES.

1. Using the system of notation explained in solutions Nos. 2 and 3, page 239 of the August No., this solution becomes  $(nj^2 + 2oj^3); B + mj; C + 2oj^3; G + (5\sqrt{3} + 5j^3); A = 0$

$$\therefore n = 5\sqrt{3}$$

$$m = 45,$$

$$\text{and } AC = 2CB.$$

Some of our readers seem troubled about taking moments; it is simply the principle of the lever the point about which the moments are taken corresponding to the fulcrum. Treat  $AB$  as a lever with fulcrum at  $G$ , (iii) shows where an upward force of 45 lbs. ( $m = 45$ ) must be applied to balance a downward force of 20 lbs. at  $B$  and one of 5 lbs. at  $A$ . (iv) is the statement of the relative distances of this point from  $A$  and  $B$ . Again in 3 treat  $AC$  as a lever with fulcrum at  $G$ , find where an upward force of  $4q + 2w$  (the force exerted by the string) must be applied to balance two downward forces one  $q + w$  at  $A$  the other  $q$  at  $C$ .