

## EXERCISES CXXVIII. Pages 322-328.

**A 1.**  $97x^2 - 53x - 17 = 0$ .   **2.**  $2(-1 \pm \sqrt{-3})$ .   **4.**  $x^3 + 2x^2 - 8x + 1$ .

**5.**  $(1, 2, 3)$ ,  $(3, 2, 1)$ ,  $\{(6 \pm \sqrt{-3}) + 3\}$ ,  $(6 \mp 2\sqrt{-3}) \div 3$ ,  
 $\{(6 \pm \sqrt{-3}) \div 3\}$ ,  $(-1, -2, -3)$ ,  $(-3, -2, -1)$ ,  $\{(-6 \pm \sqrt{-3}) + 3\}$ ,  
 $(-6 \mp 2\sqrt{-3}) \div 3$ ,  $(-6 \pm \sqrt{-3}) \div 3\}$ .

**B 1.** For  $x = \frac{2}{3}$  and  $3\frac{4}{13}$ ; for  $\frac{2}{3} < x < 3\frac{4}{13}$ ; for  $x < \frac{2}{3}$  and for  $x > 3\frac{4}{13}$ .

**3.** Each = sum of  $x$  and  $y$  multiples of numerators divided by the  $x$  and  $y$  multiples of denominators, etc.   **5.** 72.

**C 1.**  $(x-y)(x+y)(x+y-a)(x+y+a)$ .   **2. 1.**   **3.** 3,  $(3 \pm \sqrt{3}) \div 2$ .

**5.**  $33\frac{1}{3}$  mi. an hour;  $48\frac{1}{3}$  mi.

**D 1.** (i)  $(x+3+\sqrt{2})(x+3-\sqrt{2})$ ; (ii)  $(x-\frac{5}{4}+\sqrt{\frac{13}{4}})(x-\frac{5}{2}-\sqrt{\frac{13}{4}})$ .

**2.** A circle of radius 5.   **4.**  $b$  is zero, and then the common factor is  $x$ , or  $b$  is 9 and then the common factor is  $x+3$ .   **5.** 5.

**E 2.** (i)  $\left(\frac{1}{l} + \frac{1}{m} + \frac{1}{n}\right)$  of work; (ii)  $\frac{lmn}{mn+nl+lm}$  da.   **3.** (2, 1),  
 $(-2, -1)$ ,  $(\pm 6 \div \sqrt{569}, \mp 25 \div \sqrt{569})$ .   **4.** (i)  $(2x-3y-5z)(x+5y-3z)$ ;  
(ii)  $(x+1)(x^2+p-1x+1)$ .

**F 1.** 8 mi. and 10 mi. an hr.   **3.** 1,  $c(a-b) \div a(b-c)$ .   **4.** (i)  
 $x^3 + 9x^2 + 23x + 15$ ; (ii)  $x^3 - 2bx + b^2 - y^2 + 2ay - a^2$ .

**G 1.** (4, -3), (-3, 4).   **3.** 5, 7.   **4.** (i)  $(5x-2y)(2x+3y)$ ;  
(ii)  $(3x-2y+z)(x+2y-3z)$ .   **5.**  $5(x-3)^4 + 37(x-3)^3 + 148(x-3) + 91$ .

**H 1.**  $6\frac{1}{4}$ .   **2.** Not true of  $\frac{1}{2}$ .   **3.** Equals 4.   **4.**  $\left(\frac{a}{2}, \frac{b}{3}\right)$ .

**I 3.** \$1.00 and  $6\frac{2}{3}$ c. a lb.   **4.**  $m=3$  and the two roots are 3 and 3, or  $m=5$  and the two roots are 5 and 5.

**J 1.** (i)  $(a+b+c) \div 3$ ; (ii)  $\sqrt[3]{\frac{2401}{8}}$ .   **2.** 27.   **4.** (i)  $(ax-b)$   
 $(cx^2-dx+c)$ ; (ii)  $(x-1)(x+2)(x-4)(2x+3)$ .   **5.**  $-\frac{9}{64}$ ; minimum for  $x = \frac{9}{8}$ .

**K 2.** (+5, +7), (+7, +5), (-5, -7), (-7, -5).   **3.** The latter excludes the solution  $(x=0, y=0)$  of the former.   **5.**  $(x-1)^4 + 10(x-1)^3 + 10(x-1)^2 + 5(x-1)$ .