

$$(79.) \quad x^2y = z(x-z)^2 + 2yz(x-z) + zy^2, \therefore z(x-z)^2 = x^2y - 2yz(x-z) - zy^2 \text{ or } (x-z)^2 = yz.$$

$$(80.) \quad \text{Multiply by } x \text{ and add unity to each side; } \therefore (1-x)^2, \text{ etc.}$$

$$(81.) \quad b^2x^2 - a^2y^2 = ab^2x - a^2by, \text{ etc.}$$

$$(82.) \quad (a+b)x + ab =, \text{ etc.}$$

$$(83.) \quad x = -(y+z), \therefore -(y+z)(a^2 - bc) + (b^2 - ca)y + (c^2 - ab)z = 0, \therefore (b^2 - ca - a^2 + bc)y = (a^2 - bc - c^2 + ab)z, \text{ etc.}$$

$$(84.) \quad \text{Subtract 2nd from 1st, divide by } y-z, \text{ etc.}$$

$$(85.) \quad 1+a = 1 + \frac{x-y}{x+y} \text{ and } 1-a = 1 - \frac{x-y}{x+y} \therefore \frac{1+a}{1-a} = \frac{x}{y}, \text{ etc.}$$

$$(86.) \quad \text{Write } \left(\frac{1-x^2}{1-x}\right) \left(\frac{1-x^4}{1-x^2}\right), \text{ etc.}$$

$$(87.) \quad x^2 - xy + y^2 = 0, \therefore (x-y)^2 = -xy, \therefore \text{expression} = x^2y^2(x-y) - xy(x-y)xy = 0, \therefore x^2 - xy + y^2 \text{ is a factor.} \quad (88.)$$

$$(89.) \quad \text{Add the equalities, etc., but left hand will be } (x-y)(y-z)(z-x) \text{ which } = 3abc, \text{ etc.}$$

$$(90.) \quad -z = \frac{1-x}{1-2x}, \text{ which divided out gives } 1+x+2x^2, \text{ etc.}$$

$$(91.) \quad a^2 - 5a - 14. \quad (92.) \quad \frac{1}{x^m + 1}y. \quad (93.)$$

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$$(95.) \quad \text{Let } m \text{ be quantity subtracted, and instead of } a, b, c, \text{ write } a-m, b-m, c-m; \therefore \text{expression} = (a-m)^2 - (b-m)(c-m) + (b-m)^2 - (a-m)(c-m) + (c-m)^2 - (a-m)(b-m). \text{ Simplify, etc.}$$

$$(96.) \quad (97.) \quad x = 1.$$

$$(98.) \quad \text{Expression} = a(b^2 + bc + c^2) +, \text{ etc., } = (a+b+c)(bc + ca + ab), \therefore = 0. \quad (99.) \quad p = 25, q = -24.$$

$$(100.) \quad -\frac{4}{3}. \quad (101.) \quad x = 5.$$

$$(102.) \quad A = 2, B = 3, C = 1, D = 1.$$

$$(103.) \quad \text{Divide each by } x+a, \text{ and remainders } = 0. \text{ Subtract, } \therefore a(l-p) = m-q, \text{ etc.} \quad (104.) \quad 1 - m^3 - m^4.$$

$$(105.) \quad \text{If reduced, } x+1 \text{ or } x+2 \text{ must be a factor, } \therefore x = -1 \text{ or } -2, \text{ and hence } p = 3 \text{ or } \frac{1}{2}.$$

$$(106.) \quad (xy + xz + yz - x^2 - y^2 - z^2) \text{ is the other factor.}$$