

## ARTS DEPARTMENT.

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## SOLUTIONS

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145. In 1870 a Frenchman in New York proposed to invest \$5000 U. S. currency in the French 6% loan, then being sold in London at 85. Gold being at 110, London exchange 4.87, brokerage in New York  $\frac{1}{2}\%$ , commission for buying in London  $\frac{1}{2}\%$ , and London exchange on Paris being 25.43; what per cent. will the investor secure per annum, the *rentes* being payable in gold, exchange on Paris at 5.15, and gold at 115?

$$(5000 - \frac{1}{2}\% \text{ of } 5000) \times \frac{100}{110} \times \frac{100}{4.87} = £931.025$$

= amount of bill on London;

$$(931.025 - \frac{1}{2}\% \text{ of } 931.025) \times 25.43 = .23567.59$$

= amount of bill on Paris;

$$23567.59 \times \frac{100}{85} \times \frac{6}{100} = \text{int. rec'd in France,}$$

$$23567.59 \times \frac{100}{85} \times \frac{6}{100} \times \frac{115}{100} = 371.39$$

=  $7\frac{1}{2}\%$  nearly.

146. A Canadian cent is one inch in diameter,  $\frac{1}{16}$  of an inch thick, and 100 of them weigh a pound. What is the weight of a mass of the metal from which these cents are made, in the form of a sphere, four inches in diameter?

Let  $R$  be the radius of the cent and  $R'$  the radius of the sphere; then weight =

$$\frac{\frac{4}{3} \pi R'^3}{\frac{1}{16} \pi R^2} = \frac{\frac{4}{3} \pi 2^3}{\frac{1}{16} \pi (\frac{1}{2})^2} = \frac{\frac{4}{3} \times 8}{\frac{1}{16} \times \frac{1}{4}} = 426\frac{2}{3} = \text{Number}$$

of cents that can be coined, or weight =  $4.26\frac{2}{3}$  lbs.

147. If  $x = 4y$ , shew that the arithmetic mean of  $x$  and  $y$  is to the geometric mean as 5 is to 4.

$$\begin{aligned} x &= 4y \therefore x : y :: 4 : 1, \\ \text{or } (x-y)^2 &: (x+y)^2 :: 3^2 : 5^2, \\ \text{or } (x-y)^2 &: 4xy :: 9 : 16, \\ \text{or } x-y &: 2\sqrt{xy} :: 3 : 5; \\ \text{but } x-y &: x+y :: 3 : 5; \end{aligned}$$

$$\therefore \frac{2\sqrt{xy}}{x+y} = \frac{4}{5}, \therefore \frac{x+y}{2} = \sqrt{xy} :: 5 : 4.$$

148. If  $\frac{r}{2}a^2 + x^2a^2b + 2b^2$  is the perfect square of a binomial, find  $x$  in terms of  $r$ .

$$x = 4r.$$

149. Reduce to lowest terms

$$\begin{aligned} &(x^{\frac{1}{2}} + b^2)^2 - (a^2 - b^2 + c^2)^2 \\ &(x^{\frac{1}{2}} + b^2)(a^2 - b^2 + c^2) + (a^2 - b^2 + c^2)^2 + (x^{\frac{1}{2}} + b^2)^2 \\ &x^{\frac{1}{2}} + b^2 - a^2 + b^2 - c^2. \end{aligned}$$

150. Why is it that if any *three* consecutive numbers be multiplied together the product is divisible by 6?

Because one factor at least is divisible by 2 and one by 3.

151. Resolve  $m^4 - 4m^3 + 5m^2 - 2m$  into elementary factors, and shew that it is divisible by 12 for all values of  $m$  above 2.

$m(m-1)(m-1)(m-2)$ . Now, there are three consecutive numbers here as factors;  $\therefore 3$  is a divisor, and whether  $m$  be odd or even *two* of the factors are divisible each by 2;  $\therefore 4$  is also a divisor.